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AIRCRAFT ARMAMENT FOR AIR-TO-GROUND OPERATIONS (S)

PROJECT VISTA

CALIFORNIA INSTITUTE OF TECHNOLOGY

Pasadena, California

November 30, 1951

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FOREWORD

This report was prepared by R. M. Stevens of the Cornell Aeronautical Laboratories during his association with Project Vista during the summer and fall of 1951. It represents the opinions of the author and may not in detail reflect the viewpoints of Project Vista.

B. H. Sage

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AIRCRAFT ARMAMENT FOR AIR-TO-GROUND OPERATIONS

INTRODUCTION

Of late, extensive and valuable studies have been made of the aircraft weapons systems in their undisputed, but not necessarily most productive role, air-to-air combat. Comparatively little attention has been given to their other domains of usefulness, in particular, that of tactical air-to-ground operations.

A comprehensive and detailed study of this operation is beyond the scope of this project. However, it is believed necessary to identify sufficiently well the governing physical phenomena that substantial bases are provided for recommendations either for further studies or specific actions.

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In particular, this report will be concerned with aircraft armament, the ammunition and propellant system carried aboard the airplane. However, the other parts of the system, the target, the tactical situation, the airplane, the fire control system, the navigation system, and the general logistics of the operation will be considered wherever the characteristics of the armament cannot be considered independently. Specifically, this report will

- 1. Submit a measure of aircraft armament effectiveness, Ik
- 2. Examine systems and tactical parameters of which I_k is a function, and indicate methods of maximizing I_k
- 3. Compare Ik's of various aircreft armament systems
- 4. Recommend specific actions toward obtaining the maximum aircraft armament effectiveness

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A Measure of Aircraft Armament Effectiveness

It is submitted without argument that an adequate measure of aircraft armament effectiveness will be the ratio of the number of kills obtained against specified targets to the weight of the armament installation which must be carried by the aircraft to obtain those kills. Symbolically

$$I_{h} = \frac{|N_{h}|T}{W_{0}} = \frac{N_{R}(|P_{h}|T)}{W_{0}} = \frac{N_{R}(|P_{h}/h)T}{W_{h}} = \frac{|P_{h}|_{T}}{|P_{h}/h|_{T}} = \frac{|P_{h}|_{T}}{|P_{h}/h|_{T}} = \frac{|P_{h}|_{T}}{|V_{0}|_{T}} = \frac{|P$$

Wo = Weight of armament systems installation

wh " Weight of warhead per round

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Wh - Total weight of warbead in Wo

 $W_{\rm H}$ = Mumber of rounds of amunition in W₀

[Nk]T = Number of kills obtained against target, T, in Wo

P₁ = Probability of kill per round against target, T

P(k/h)T = Probability of kill per hit against target, 1

Ph Single-shot probability of hit per round against target, T

The affectiveness index equals the product of the probability of hit par round, the probability of kill per hit per pound of warhead, and the ratio of the total weight of warhead to the total weight of armament system installation.

In other EngOrd reports, the inverse of the product of hit probability and the ratio of total warhead weight to ordnance system weight has been called the ordnance logistic factor, L. We shall adopt the same terminology, but since in this case we are

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considering in W_o only part of the ordnance system weight (ignoring the airplane weight) we shall say that:

$$\mathbf{I}_{\mathbf{k}} = \frac{1}{\mathbf{L}_{w}} \frac{\left| \mathbf{P}_{(\mathbf{k}/\mathbf{h})} \right|_{T}}{w_{\mathbf{h}}}$$

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 L_W = The aircraft armament logistic factor For the relationship between L and L_W see (9).

Examination of Parameters

$$\frac{(k/h)T}{W_h} - \frac{\text{Probability of kill per hit per unit warhead weight.}}{W_h}$$

The parameter $\frac{P_{(k/h)T}}{W_h}$ is principally a function of the type of

target, the type of warhead, the striking velocity, the striking attitude, and the type of fuzing. For simplicity, it will be assumed that comparatively this parameter is invariant among all aircraft armament propellant systems capable of delivering equal warhead weight, w_{h} .

L. - Aircraft armament logistic factor.

L is a function of two parameters, which in turn are functions of many variables peculiar to the operation, as follows:

 $|P_h|_T$ = Probability of hit per round against target, T, is a function of:

R = Slant range from point of release to target

 $T = T (A_{m}, x_{m}, y_{m}) = Target (area, shape, normal to trajectory)$

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- √i = Dispersions of round due to all causes other than release error along the sight line
- $\nabla_g =$ Dispersion of round due to release errors along the sight line, in turn a function of:
 - R = Slant range from point of release to target

 V_a [#] Airplane velocity at release

 $V_r = Velocity$ of round

- * Airplane dive angle at release
- دهد * Balease errors along sight line, in range, diverangle, and airplane speed

Wh/Wo

The ratio of total warhead weight to the ordnance system weight is a function of the ratios of round, gun, installation and control weights to the weight of the warhead per round (W_R, W_g, W_i, W_a) $\overline{W_h}$ $\overline{W_h}$ $\overline{W_h}$ $\overline{W_h}$ $\overline{W_h}$

which in turn are functions of variables peculiar to the operation as follows:

E Batio of gun (or propelling system) weight to warbaad weight, n e function of:

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 $V_r \equiv Valocity of round$ $D_{\rm b}$ = Caliber of round N_g & Mimber of guns M_R = Number of rounds r_{σ} = Rate of fire Gi a Type of guns W₁ E Ratio of installation weight to warherd weight a function of: W. Wy = Weight of gua Dh = Caliber of round $\mathbf{M}_{g} \ge \mathbf{Humber}$ of guns M_P = Number of rounds r_g = Eate of fire G₁ = Type of guns Ii = Type of Installation

> Batio of control weight to warhead weight, a function of rates of change of the fundamental variables as well as of the variables.

There are other fundamental variables and relationships than these listed above. However, it is believed that enough have been recognized for fairly accurate general comparison of aircraft armament systems, yet the number has been kept sufficiently low that fairly simple analytic expressions may be derived.

Thus we say:

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 $P_{h} = f(R, T, T_{i}, T_{g}(R, V_{a}, V_{r}, \Theta_{s} \Delta \mathcal{E}_{si}))$

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Wa

$$\begin{split} \mathbf{w}_{h}/\mathbf{w}_{o} &= g(\frac{W_{R}}{W_{h}}(V_{r}, D_{h}, R_{i}), \frac{W_{a}}{W_{R}}(V_{r}, D_{h}, N_{r}, \tau_{g}, G_{i}), \frac{W_{i}}{W_{h}}(W_{g}, W_{h}, I_{i}) \\ \mathbf{L}_{w} &= 1/g_{f} \\ \mathbf{I}_{k} &= K/g_{f} \\ \end{split}$$

It will be observed that f and g are functions of common variables. Therefore, P_h and W_h/W_o cannot be treated independently in maximizing L_W .

An Expression for Ph

Assume a rectangular target of width, w, and length, l, (normal to the target). Assume that the dispersion of the weapons system may be represented by a linear standard deviation of σ_{yR} in y (width) and ∇_{xR} in x (length), where ∇_x and ∇_y are measured in mile.

Then:

$$P_{h} = P_{hx} P_{hy} = \frac{1}{\sqrt{2\pi} \sigma_{\chi} R} \left(e^{-\frac{1}{2} \left(\frac{x}{\sigma_{\chi} R} \right)^{2}} d_{\chi} - \frac{1}{\sqrt{2\pi} \sigma_{\chi} R} d_{\chi} \right)^{2}}{\frac{-\frac{1}{2} \left(\frac{y}{\sigma_{\chi} R} \right)^{2}}{\frac{-\frac{1}{2} \left(\frac{x}{\sigma_{\chi} R} \right)^{2}}{\frac{1}{2} \left(\frac{y}{\sigma_{\chi} R} \right)^{2}} d_{\chi} d$$

decreasing values of $h/2\sigma_{\overline{z}}R$. Thus for $\frac{h}{2\sigma_{\overline{z}}R} \ll 1.0$: $P_{h} \cong \frac{2}{TT} \frac{l}{2\sigma_{\overline{z}}R} \frac{w}{2\sigma_{\overline{y}}R}$

with errors not greater than 35%.

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If it is assumed that the number of rounds required per hit is equal to the reciprocal of the single-shot hit probability, to the nearest higher integer.

 $N_{R} = \frac{1}{P_{R}}$ for values of $\frac{h}{2\sigma_{z}R} < 1.0$, the maximum error will not be greater than 50%, and this error will be greatest for the least number of rounds required (1.5 required by approximation as against 3 required by exact expression for $\frac{L}{2\sigma_{z}R} = \frac{W}{2\sigma_{y}R} = 0.99$). Inasmuch as for the targets and ranges with which we are most con-

corned, $\frac{h}{2\sqrt{2}R} \ll 1.0$, it is considered that the following expression for hit probability is a satisfactory approximation.

$$P_{h} \doteq \frac{2}{\pi} \frac{l}{2\sigma_{\chi}R} \frac{W}{2\sigma_{\chi}R} = \frac{A_{T}}{2\pi R^{2}} \frac{l}{\sigma_{\chi}\sigma_{y}} \begin{bmatrix} \frac{1}{2\sigma_{\chi}R} - 1\\ \frac{1}{2\sigma_{\chi}R} \end{bmatrix}$$

In the above expression, the variables which are not fundamental are ∇_x and ∇_y . ∇_x is a function of both ∇_i and ∇_g , while ∇_y is primarily a function only of ∇_i as defined above. It will be assumed that for each type of aircraft armament ∇_i is a constant, the value averaged from firing tests. However, as defined above.

$$\nabla_{g} = \nabla_{g} (R, V_{a}, V_{R}, \Theta, \Delta E_{xi})$$

so that $\nabla y = \nabla y (\nabla_{i}) = const = \nabla_{i}$

With the above assumption:

$$P_{h} \stackrel{\cdot}{=} \frac{A_{T}}{2\pi R^{2}} \cdot \frac{1}{\sigma_{\chi} \sqrt{\sigma_{\chi}^{2} + \sigma_{g}^{2}}}$$

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It may be shown that for a vacuum trajectory (see Figure 1) the trajectory drop may be expressed as:

$$\mathcal{E} = \frac{m}{R} = \frac{9}{2} \frac{R}{(Var)^2} core$$

where:

- E = Trajectory drop (ft./ft.)
- m = Trajectory drop (ft.)
- \mathbf{R} = Slant range (ft.)

 V_{av} = Average velocity of projectile (ft./sec.) over slant range, R. Θ = Angle of airplane flight path to horizontal at time of firing. V_a = Airplane velocity at time of firing.

And
$$\frac{\partial \mathcal{E}}{\partial R} = \frac{g}{2} \frac{R}{V_{2}} \cos \theta \left[\frac{1}{R} - \frac{2}{V_{2}} \frac{\partial V_{2}}{\partial R} \right]$$

 $\frac{\partial \mathcal{E}}{\partial V_{2}} = -g \cdot \frac{R}{V_{2}} \cos \theta \frac{\partial V_{2}}{\partial V_{2}}$
 $\frac{\partial \mathcal{E}}{\partial V_{2}} = -\frac{g}{2} \frac{R}{V_{2}} \cos \theta \left[\frac{\partial V_{2}}{\nabla A_{2}} - \frac{\partial V_{2}}{\partial V_{2}} - \frac{\partial V_{2}}{\partial \theta} - \frac{\partial V_{2}}{\partial V_{2}} - \frac{\partial V_{2}}{\partial \theta} - \frac{\partial V_{2}}{\partial \theta} \right]$
If it is assumed that $\frac{\partial \mathcal{E}}{\partial \theta} = \frac{\partial \mathcal{E}}{\partial \theta} = \frac{\partial \mathcal{E}}{\partial \theta}$

$$\begin{aligned}
\mathcal{T}_{R} &= \Delta \mathcal{E}_{R} = \frac{\Delta \mathcal{R}}{R} - \frac{9}{2} \frac{R_{cond}}{V_{av}^{2}} \left[1 - \frac{2R}{V_{av}} - \frac{9V_{av}}{9R} \right] \\
\mathcal{T}_{V_{av}} &= \Delta \mathcal{E}_{r} \doteq \frac{-2\Delta V_{a}}{V_{av}} - \frac{9}{2} \frac{R_{cond}}{V_{av}^{2}} \frac{9V_{av}}{2} - 2 \frac{\Delta V_{a}}{V_{av}} \frac{9}{2} \frac{R_{cond}}{V_{av}} \frac{9V_{av}}{9V_{av}} \frac{9V_{av}}{2} \frac{9V_{av}}{2} \frac{9V_{av}}{V_{av}} \frac{9V_{av}}{2} \frac{9V_{av}}{V_{av}} \frac{9V_{av}}{2} \frac{9V_{av}}{2} \frac{9V_{av}}{V_{av}} \frac{9V_{av}}{2} \frac{9V_{av}}{2} \frac{9V_{av}}{V_{av}} \frac{9V_{av}}{2} \frac{9V_{av}}{V_{av}} \frac{9V_{av}}{2} \frac{9V_{av}}{V_{av}} \frac{9V_{av}}{2} \frac{9V_{av}}{V_{av}} \frac{9V_{av}}{2} \frac{9V_{av}}{2} \frac{9V_{av}}{2} \frac{9V_{av}}{2} \frac{9V_{av}}{V_{av}} \frac{9V_{av}}{2} \frac{9V_{av}}{2} \frac{9V_{av}}{2} \frac{9V_{av}}{V_{av}} \frac{9V_{av}}{2} \frac{9V_{av}}{2} \frac{9V_{av}}{V_{av}} \frac{9V_{av}}{2} \frac{9V_{av}}{2}$$

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and that these release errors are the principal ones not included in $\sigma_{\overline{i}}$,

then:
$$T_{y} \doteq \sqrt{T_{R}^{2} + T_{v}^{2} + T_{o}^{2}}$$

 $\doteq \frac{9}{2} \frac{R \cos \theta}{V_{av}} \sqrt{\left[\frac{\Delta R}{R} \left(\frac{1-2R}{V_{av}} \frac{\partial V_{av}}{\partial R}\right)\right]^{2} + \left[\frac{2\Delta V_{a}}{V_{a}} \frac{V_{a}}{V_{av}} \frac{\partial V_{av}}{\partial V_{a}}\right]^{2}}$
 $+ \left[\frac{\Delta \theta}{\theta} \left(\theta \tan \theta + \frac{2\theta}{V_{av}} \frac{\partial V_{av}}{\partial \theta}\right)\right]^{2}$

Assume for a moment that ∇_{av} may be chosen arbitrarily, independent of R, ∇_{a} , and Θ , then:

$$\nabla g = \frac{9}{2} \frac{R \cos \theta}{V_{aur}} \sqrt{\left(\frac{\Delta R}{R}\right)^2 + (\Delta \theta \tan \theta)^2}$$

and $P_{h} = \frac{A_{T} V_{aw}^{2}}{\pi g R^{3} coa \Theta} \cdot \frac{1}{\sigma_{L} \sqrt{\left(\frac{2 V_{aw}^{2} \sigma_{L}}{\rho R}\right)^{2} + \left(\frac{\Delta R}{\rho}\right)^{2} + \left(\Delta \Theta \tan \Theta\right)^{2}}}$

Here we observe that if ∇_1 is small relative to ∇_g , $(\operatorname{say} \nabla_i \stackrel{>}{>} 3 \overline{g})$, and $\frac{h}{2\nabla_z h} < 1$, P_h increases linearly with A_t increases as the square of V_{av}

increases as the reciprocal of the cube of the range

increases as the reciprocals of
$$\nabla_i$$
 and $\nabla \Delta \in \mathbb{R}^3$
increases as the reciprocal of $\cos \Theta$

If, on the other hand $abla_i$ is large relative to $abla_g$ (say $abla_L \ge 3\sigma_g$), and $\frac{4}{2\sigma_2} < l$, P_h increases linearly with A_t increases as the reciprocal of the square of the range

increases as the reciprocals of ∇_i and $\sqrt{\Delta} \in \mathcal{L}_{\mathcal{U}}^2$ Now, $\frac{W_{ii}}{W_0}$ is also a function of V_{av} so without further exploration of their relationship, the variation of I_k with V_a cannot be stated. However, $\frac{W_h}{W_0}$ is not a function of the other variables except as V_{av} is a function of them, so that for our assumption of an arbitrary V_{av} , the

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variations of I_k with A_T , R, Θ , $\overline{\tau_i}$ and $\sqrt{\Delta \mathcal{E}_{si}}$ are generally the same as those of P_h .

It should be observed that range has a very significant effect on P_h and I_k .

 $\frac{\mathcal{I}_{\kappa_1}}{\mathcal{I}_{\kappa_2}} - \left(\frac{R_2}{R_1}\right)^{(2-3)}$

Therefore, training and equipment plans should consider the very considerable gains to be obtained by firing at short range. (For example, although aircraft armor to protect against small-arms antiaircraft fire and fragment damage would increase W_0 , the reduction in safe firing range resulting from its installation might well increase P_h sufficiently to result in higher I_k 's for the armored airplanes.)

For a particular weapon, where V_{aV} may not be independent of R, V_a , and Θ , the same general trends follow, modified as indicated in the above expression for σ_p .

The above analysis has been based upon an approximation for the projectile trajectory. The errors introduced by this ap_{f} oximation should be explored. First it is necessary to obtain expressions for the average velocities and their derivatives for the various weapons. These follow: For bomba:

$$V_{av} = V_a$$
 (within 1.10 $V_a > V_{av} > V_a$ { $R \le 6000$ FC.
 $V_a \ge 500$ F.p.s.

For rockets:

$$V_{av} = \frac{R(V_{a}+V_{b})}{R+V_{b}t_{b}/2}; ((V_{a}+V_{b}/2)t_{b} < R) (within \frac{R}{t_{f}} < V_{av} < 1.10 \frac{R}{t_{f}}; \\ = \frac{V_{a}}{2} [1+\sqrt{1+\frac{2V_{b}R}{V_{a}^{2}t_{b}}}]; ((V_{a}+V_{b}/2)t_{b} > R) R \le 600 \text{ Ft.})$$

For guns:

$$V_{av} = V_a + V_m$$
 (within $\frac{R}{T_F} < V_{av} < 1.10 \frac{R}{T_F}$; $R \le 6000$ ft)



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For bombs:

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$$\begin{aligned}
\nabla_{R} &\doteq \frac{\Delta R}{R} \left[1 - \left(\frac{V_{b} t_{b}}{2R} \right)^{2} \right] \frac{g}{2} \frac{R \cos \theta}{(V_{a} + V_{b})^{2}} \left(\frac{V_{b} t_{b}}{2R} < 1 - \frac{V_{a}}{R} \right) \\
\nabla_{R} &= -2 \frac{\Delta V_{a}}{V_{a}} \frac{V_{a}}{(V_{a} + V_{b})} \left(1 + \frac{V_{b} t_{b}}{2R} \right)^{2} \frac{g}{2} \frac{R \cos \theta}{(V_{a} + V_{b})^{2}} \left(\frac{V_{b} t_{b}}{2R} < 1 - \frac{V_{a}}{R} \right) \\
\nabla_{\theta} &\doteq -\frac{\Delta \theta}{\theta} \left(\theta \tan \theta \right) \left(1 + \frac{V_{b} t_{b}}{2R} \right)^{2} \frac{g}{2} \frac{R \cos \theta}{(V_{a} + V_{b})^{2}} \left(\frac{V_{b} t_{b}}{2R} < 1 - \frac{V_{a}}{R} \right) \\
\end{array}$$

For guns:

$$\begin{aligned}
\nabla_{R} &= \frac{\Delta R}{R} \frac{9}{2} \frac{R \cos \Theta}{(V_{a} + V_{m})^{2}} \\
\nabla_{V_{a}} &= \frac{2 \Delta V_{a}}{V_{a}} \frac{V_{a}}{(V_{a} + V_{m})^{2}} \frac{3}{(V_{a} + V_{m})^{2}} \\
\nabla_{\Theta} &= \frac{\Delta \Theta}{\Theta} (\Theta \tan \Theta) \frac{9}{2} \frac{R \cos \Theta}{(V_{a} + V_{b})^{2}}
\end{aligned}$$

Then, assuming that the errors are independent:

For boabs:

$$\nabla_{j} = \frac{9}{2} \frac{R \cos \Theta}{V_{a}^{2}} \frac{\Delta R}{R} \left(1 + 4 \left(\frac{\Delta V_{a}}{V_{a}} \frac{R}{\Delta R} \right)^{2} + \Theta^{2} \tan^{2} \Theta \left(\frac{\Delta \Theta}{\Theta} \frac{R}{\Delta R} \right)^{2} \right)$$

For rockets:

For gu

$$T_{g} = \frac{1}{2} \frac{R_{could}}{(V_{a} + V_{m})^{2}} \frac{\Delta R}{R} \sqrt{1 + 4\left(\frac{V_{a}}{V_{a} + V_{m}}\right)^{2} \left(\frac{\Delta V_{a}}{V_{a}} \frac{R}{\Delta R}\right)^{2} + \theta^{2} t_{a+1}^{2} \theta \left(\frac{\Delta \theta}{\theta} \frac{R}{\Delta R}\right)^{2}}$$

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If it is assumed that
$$\frac{\Delta R}{R} = \frac{\Delta V}{V} = \frac{\Delta \Theta}{\Theta}$$

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For bombs:

$$T_g = \frac{9}{2} \frac{R_{cos}\theta}{V_a^2} \frac{\Delta R}{R} \sqrt{5 + \theta^2 tan^2 \theta}$$

For rockets:

$$\nabla_{g} = \frac{g}{2} \frac{R_{000}}{(V_{0}+V_{0})^{2}} \frac{\Delta R}{K} \frac{1}{[1-(\frac{V_{0}t_{0}}{2R})^{2}]^{2}} + (\frac{1+V_{0}t_{0}}{2R}) \frac{1}{[4(\frac{V_{0}}{V_{0}+V_{0}})^{2}} + \theta^{2} \tan \theta}{2R}$$

For guns:

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$$T_{g} = \frac{g}{2} \frac{R \cos \theta}{\left(V_{a} + V_{m}\right)^{2}} \frac{\Delta R}{R} \frac{1}{1 + 4} \left(\frac{V_{a}}{V_{a} + V_{m}}\right)^{2} + \theta^{2} \tan^{2} \theta$$

Figure 4 plots $\nabla_{\overline{g}}$ versus \mathbb{B}_1 ($\frac{\Delta R}{R} = \frac{\Delta V_a}{V_{a_T}} = \frac{\Delta \Theta}{\Theta} = 0.005$) for various values of Θ , V_b , and V_m corresponding to existing bombs, rockets, and guns. For rockets and bombs, V_a was set equal 500 ft./sec.; for guns, V_a was set equal to zero. Actual values of $\mathcal{T}_{\overline{g}}$ as taken from trajectory Table I are shown for comparison. It will be observed that the calculated rocket deviations correspond quite well to the actual, the errors ranging from 2 to 7 percent high for the bomb, 2 to 12 percent low for the 5^m AR, 14 to 26 percent low for the 5^m HVAR, and 8 to 13 percent low for the gun. These errors are, in most cases, no greater than those which must result from assumptions for \mathcal{T}_1 . It appears then that trends shown by the approximate analytic expressions derived above will be generally correct and that the absolute values will not be greatly in error.

 σ_1

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It will be assumed that these errors are circular. The values given below are for the linear components $(\nabla_{\chi} = \nabla_{\chi} = 0.707 \sigma_{L}(cmc))$. The free flight ballistic dispersions have been given in other EngOrd reports (2,3,4,5) and are approximately:

3-4 mils - Bombs (Existing bombs with modified fin assemblies and proposed new family of bombs)

3-7 mils - ockets (Air-fired, fin-stabilized)

1-3 mils - Ouns (Air-fired)

There have been no satisfactory isolations of the other dispersions contained in ∇_{i} . Therefore, for the remainder of this analysis two assumptions as to its value will be made. The first (lower limit) will be that ∇_{i} is equal to the ballistic dispersion alone, value to be:

4 mils - Bombs

- 4 mils Rockets
- 2 mils Guns

The second (upper limit) will be that ∇_{j} is equal to dispersions generally found in firing tests corrected for ∇_{y} . These values are approximately (6).

9 mils - Bomba

9 mils - Rockets

5 mils - Guns

Release Error Control Requirements

With the aid of the above equations and numbers it is possible to approximate the values within which $\triangle R$, $\triangle V$, and $\triangle \Theta$ must be maintained in order that dispersion along the sight line, ∇_X^{-} , will approach its minimum practical limit. Since

$$\sigma_{\chi} = \sqrt{\sigma_i^2 + \sigma_g^2}$$

the minimum limit will be ∇_1 , with $\triangle R$, $\triangle V$, $\triangle \Theta$ all equal to zero.

However, it will be assumed that a minimum limit below which further expenditure of effort to reduce release errors would be impractical will be:

Then for bombs and rockets:

For guns:

Then using the approximate equation for \mathcal{T}_{σ} :

$$.663 \ge \nabla_g \doteq \frac{9}{2} \frac{R \cos \theta}{V_{aur}^2} \sqrt{\left(\frac{\Delta R}{R}\right)^2 + \left(2 \frac{\Delta V_a}{V_{aur}}\right)^2 + \left(\Delta \theta \tan \theta\right)^2}$$

$$1.326 \frac{\nabla_z V_{aur}^2}{9 R \cos \theta} \doteq \sqrt{\left(\frac{\Delta R}{R}\right)^2 + \left(2 \frac{\Delta V_a}{V_{aur}}\right)^2 + \left(\Delta \theta \tan \theta\right)^2} = \Delta^2$$

Using the above equation, the maximum allowable value of \triangle may be approximated. Then it is necessary to assign maximum allowable value to $\frac{\triangle R}{R}$, $\frac{\triangle V_{\Delta}}{V_{\Delta}}$, and $\triangle \Theta$.

First, it will be assumed that there are maximum limits within which these errors can be controlled by even a very simple fire control system (fixed sight, standard release range, trained pilot). \triangle R is probably the most difficult error to estimate or control; $\triangle V_{\rm R}$ somewhat less difficult; and $\triangle \Theta$ is the least difficult. Experiences of trained gunnery pilots, firing with fixed sights indicate that these errors can be held within the following maximum limits:

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$$\Delta R = 0.5 R$$
 $\Delta V_{a} = 50 \text{ ft./sec.}$ $\Delta \theta = 5^{\circ}$

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It will be assumed that no errors greater than these will be permitted. Then the necessary reductions below these limits to satisfy the above equation will be determined. The distribution of errors will be such that when all the allowable maximum errors are below the simply controllable maximum limits,

$$\frac{\partial \sigma_{i}}{\partial \left(\frac{\Delta R}{R}\right)} = \frac{\partial \sigma_{i}}{\partial \left(2 \frac{\Delta V_{a}}{V_{av}}\right)} = \frac{\partial \sigma_{i}}{\partial \left(\Delta \theta \tan \theta\right)}$$

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With these assumptions, the maximum allowable values have been computed for a range of V_{av} 's from 500 to 3000 ft./sec., R = 3000 and 6000 feet, $\Theta = 20^{\circ}$ and 60° , $\nabla_{o} = 2$, 5, and 9 mils and $V_{a} = 500$ ft./sec. The results are presented in Table I. A generalized summary of the results is given below, for $\nabla_{i} = 1$ mils.

Weapon	Range	Allowable Errors		
		△ H/H	$\Delta V_{a}/V_{a}$	Ð
Guns (V _m 1500 ft./sec.)	6000	0.15	0.1	5°
	3000	0.3	0.1	5°
Rockets (V _M 1000 ft./sec.)	6000	0.05	0.1	50
	3000	0.15	0.1	50
Rockats (500 V _B 1000 ft./sec.)	6000	0.02	0.02	20
	3000	0.05	0.05	50
Bozaba	6000	0.005	0.003	1°
	3000	0.01	0.006	1°

Therefore, if the effect of gravity drop is to be reduced to a minimum practical limit, range error must be controlled within limits from $\frac{\Delta R}{R} < 0.005$ for bombs to $\frac{\Delta R}{R} < 0.15$ for guns. Velocity and range error effects, for errors below those controllable by fairly simple systems, are negligible, except in the case of bombing.

Figures ha through he show the effects of release error on σ_1 for



various weapons at various ranges and release angles.

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Finally then, the following expressions are derived for Ph.

For bombs:

$$P_{h} \stackrel{=}{=} \frac{A_{\tau} V_{a}^{2}}{\pi g R^{3} cou \Theta} \frac{1}{\tau_{B} \frac{\Delta R}{R}} \frac{1}{\sqrt{1 + \left(\frac{2 V_{a}^{2} \sigma_{LB}}{g R cou \Theta}\right)^{2} \left(\frac{R}{\Delta R}\right)^{2} + 4 \left(\frac{\Delta V_{a}}{V_{a}} \frac{R}{\Delta R}\right)^{2} + \Theta^{2} t_{a}^{2} \Theta^{2} \Theta^{2} \Theta^{2} \Theta^{2} \Theta^{2}}{\left(\frac{\Delta R}{\sigma R}\right)^{2} + \Theta^{2} t_{a}^{2} \Theta^{2} \Theta^{2} \Theta^{2} \Theta^{2}} \left(\frac{A \Theta R}{\sigma R}\right)^{2} + \Theta^{2} t_{a}^{2} \Theta^{2} \Theta^{2} \Theta^{2} \Theta^{2} \Theta^{2}}{\left(\frac{\Delta R}{\sigma R}\right)^{2} + \Theta^{2} t_{a}^{2} \Theta^{2} \Theta^{2} \Theta^{2}} \left(\frac{A \Theta R}{\sigma R}\right)^{2} + \Theta^{2} t_{a}^{2} \Theta^{2} \Theta^{2} \Theta^{2} \Theta^{2} \Theta^{2}}{\left(\frac{\Delta R}{\sigma R}\right)^{2} + \Theta^{2} t_{a}^{2} \Theta^{2} \Theta^{2}} \left(\frac{A \Theta R}{\sigma R}\right)^{2} + \Theta^{2} t_{a}^{2} \Theta^{2} \Theta^{2} \Theta^{2}}{\left(\frac{\Delta R}{\sigma R}\right)^{2} + \Theta^{2} t_{a}^{2} \Theta^{2} \Theta^{2}} \left(\frac{A \Theta R}{\sigma R}\right)^{2} + \Theta^{2} t_{a}^{2} \Theta^{2} \Theta^{2} \Theta^{2} \Theta^{2}}{\left(\frac{\Delta R}{\sigma R}\right)^{2} + \Theta^{2} t_{a}^{2} \Theta^{2} \Theta^{2}} \left(\frac{A \Theta R}{\sigma R}\right)^{2} + \Theta^{2} t_{a}^{2} \Theta^{2} \Theta^{2} \Theta^{2} \Theta^{2}}{\left(\frac{\Delta R}{\sigma R}\right)^{2} + \Theta^{2} t_{a}^{2} \Theta^{2} \Theta^{2}} \left(\frac{A \Theta R}{\sigma R}\right)^{2} + \Theta^{2} t_{a}^{2} \Theta^{2} \Theta^{2} \Theta^{2}} \left(\frac{A \Theta R}{\sigma R}\right)^{2} + \Theta^{2} t_{a}^{2} \Theta^{2} \Theta^{$$

Ror rockets:

$$P_{h} \doteq \frac{A_{T}(V_{A}+V_{b})^{2}}{T_{q}R^{3}cou\theta} = \frac{1}{V_{L_{R}}\left[1-\left(\frac{V_{b}t_{b}}{2R}\right)^{2}\right]\frac{\Delta R}{R}} \sqrt{1+\left[\frac{2(V_{a}+V_{b})^{3}T_{c}R}{gRcou\theta}\right]^{2}} \left(\frac{R_{t}}{\Delta R}\right)^{2} + \frac{1}{\left(\frac{V_{a}+V_{b}}{2R}\right)^{2}} \left(\frac{R_{t}}{\Delta R}\right)^{2} + \frac{1}{\left(\frac{V_{a}+V_{b}}{2R}\right)^{2}} \left(\frac{R_{t}}{\Delta R}\right)^{2} + \frac{1}{\left(\frac{V_{b}t_{b}}{2R}\right)^{2}} \left(\frac{R_{t}}{\Delta R}\right)^{2} + \frac{1}{\left(\frac{V_{b}t_{b}}{2R}\right)^{2}} + \frac{1}{\left(\frac{V_{b$$

Figures 5a through 5d show the values of $\frac{h}{A_T}$ for various weapons, dive angles, and the limiting values of σ_i , plotted as a function of range. Figures 6a and 6b show P_h/A_T plotted as a function of V_b for rockets, and V_m for guns. The marked increase of hit probability with decreasing range will be noted in Figure 5. It will be noted that no significant improvements in rocket hit probabilities will be made until reductions in inherent dispersions are accomplished. However, improvements in bombing fire control above those assumed will result in significant improvements in bombing hit probabilities. Figure 6 indicates that as

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long as fire control errors remain large, burnt or muzzle velocities should be kept high to improve hit probabilities. As fire control errors are reduced, velocities may be correspondingly reduced. It is obvious, that with perfect fire control, velocity will have no effect on hit probability. Similarly as long as inherent dispersions are high, burnt or muzzle velocities may remain relatively low. As inherent dispersions are reduced, velocities should be increased to improve hit probabilities.

In Figure 5, the hit probabilities obtained in Air Proving Ground tests with 5" HVAR rockets, using the A-ICH sight with varying degrees of sensitivity has been shown (7). Ranges were uncertain, between 2500 and 3500 Next. Results were in remarkable agreement with those hypethesized with the use of the foregoing approximations.

Based on the data of Figure 5, Figure 7 shows the number of rounds required per hit (subject to the errors inherent in use of the approximate formula) as a function of range and target area for guns, rockets, and bombs and for the combinations of maximum range errors and inherent dispersion and minimum range errors and inherent dispersions. The maximums may be considered as approximating present systems, the minimums as the limit of inherent improvement. Three target areas have been chosen, 200 sq. ft. (approximately that of a tank, side on), 2000 sq. ft. (a pillbox or artillery emplacement) and 20,000 sq. ft. (troop vehicles or supply concentration).

In analyzing these data, let us consider that a maximum of 8 rounds per hit are desired. Then the following table indicates the maximum ranges in feet at which the various weapons may be used.

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Target Area	Guns		Rocket	5	Bomba	
	Present Errors	Improved	P. E.	Imp.	P.B.	Imp.
200 sq. ft.	R<3000 ft.	R< 6000	R<1500	R < 3000	R~1000	R<1500
2000 sq. ft.	R < 6000	R < 6000	R< 4000	R< 6000	R<2000	R = 3500
20,000 sq. ft.	R < 6000	R < 6000	R = 6000	R < 6000	R=4500	R-6000

On the basis of hit probabilities above, with specifications as established, guns should be used for the 200 sq. ft. target, bombs should not be used, and extremely close ranges are necessary with rockets. Either guns or rockets might be used against the intermediate area target, but close ranges are necessary with bombs. Guns, rockets, or bombs might be used against the 20,000 sq. ft. target.

Wh - Ratio of Total Murhead Weight to Armament System Weight The total warhead weight carried by the airplane:

 $w_{h} = N_{R} w_{h}$

The total armament system weight:

$$w_{o} = W_{R} + W_{g} + W_{k} + W_{e}$$
$$w_{R} = N_{R} W_{R}$$
$$w_{g} = N_{g} W_{g}$$

where:

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 $W_0 = Armament$ system weight

Wh = Total warhead weight

 $W_R =$ Total round weight

 $W_j = Total installation weight$

W_e = Total fire control weight

 W_{g} = Total gun weight

 $\mathbb{N}_{\mathbb{R}}$ = Number of rounds

 $N_p = Number of guns$

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wh = Warhead weight per round

W_R = Round weight

wg = Gun weight

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$$\frac{W_{h}}{W_{0}} = \frac{1}{\frac{N_{R}W_{R} + N_{g}w_{g} + W_{i} + W_{e}}{N_{R}w_{h}}}$$

$$= \frac{1}{\frac{W_{R}}{W_{h}} + \frac{N_{g}}{N_{R}}\frac{W_{g}}{W_{h}} + \frac{W_{i}}{N_{R}w_{h}} + \frac{W_{e}}{N_{g}w_{h}}}$$

In other EngOrd reports (2, 3, 4, 5, 9) expressions have been derived for $\frac{W_R}{w_h} = \frac{W_g}{w_h}$ and W'_L as functions of round diameter, rate of fire, velocity of round, and subsidiary parameters characteristic of the type of weapon. However, there are no such expressions derived for $\frac{W_e}{N_R}$. Therefore, in this report, it will be considered that comparable fire control systems are provided for all weapons (weapons will be compared for the same release errors), W_R will be included in the basic airplane weight, and the term eliminated from the above expression.

Bombs

For bombs, gun weight is zero, and the installation weight per round varies roughly linearly with the weight of the round. Thus

$$\frac{w_{q}}{w_{h}} = 0$$

and from (2),

$$\frac{W_{L}}{N_{R}} \stackrel{i}{=} 0.04$$

$$\frac{W_{R}}{W_{R}} \stackrel{i}{=} 1.05$$

(considering warhead weight to be the total bomb weight minus the stabilizing system weight)

So that:

$$\frac{w_h}{W_h} = \frac{1}{1.05 \pm 0.04} = 0.92$$

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Rockets

As for bombs, gun weight is zero, and the installation weight per round varies roughly linearly with the weight of the round. Thus

 $\frac{w_{a}}{w_{h}}=0$

and from (3),

$$\frac{W_{i}}{N_{R}w_{h}} = \begin{cases} .10 (pylon launcher) \\ .50 (packaged launcher) \\ \frac{W_{R}}{w_{h}} \doteq \frac{e^{V_{b}/6800}}{1 + w_{N}w_{p}(1 - e^{V_{b}/6800})} \\ \frac{W_{m}}{w_{p}} = \begin{cases} .15 + 2.7/O_{m}(new-rockete(5"HPAG 2" 75 AAFFR, 8 cm '0 EF)) \\ .5.0 + 2.7/O_{m}(std. WW.II rockete(5"HVAR, 3."5 AR, 11."75 AR)) \end{cases}$$

 $D_m =$ Motor diameter, inches

V_b = Burnt velocity, relative to launcher, ft./sec.

 $\frac{W_{m}}{W_{p}}$ = Ratio of rocket motor weight (burnt) to propellant weight. Then:

$$\frac{W_{h}}{W_{0}} \doteq \frac{1}{\frac{e^{V_{b}/6800} + K}{W_{p}(1 - e^{V_{b}/6800})}} + K. (500 < V_{b} < 2500)$$

$$= \frac{1}{1 + V_{b} / 6800} + K. (500 < V_{b} < 2500)$$

$$= \frac{1}{1 - \frac{W_{m}}{W_{p}} \frac{V_{b}}{6800}} + \frac{1}{(6800 - W_{m}/W_{p})} + \frac{1}{(6800 + V_{b})}$$

For simplicity, say

$$\frac{W_{i}}{N_{\rm R}W_{\rm h}} = K \doteq 0.3$$

And that

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Then:
$$\frac{W_{h}}{W_{0}} = \frac{6800 - V_{b}}{8840 + 0.7V_{b}} (new rocket)$$

= $\frac{6800 - 3V_{b}}{8840 + 0.1V_{b}} (older std. rocket)$

These values are plotted in Figure 8. Actual values are shown for comparison. Good agreement is shown between the estimated and actual values for the older rockets but probably will be approached as development continues. It will be noted that $\frac{w_h}{W_0}$ decreases markedly with increasing V_b .

Standard Guns

From (4,5):

$$\frac{W_g}{W_h} \doteq \frac{V_m}{D_h} + 1 \left[19.1 + .0455 r \right] \times 10^{-6}$$

where

R

 $V_{n} = \text{Muzzle velocity, ft./sec.}$ $D_{h} = \text{Projectile diameter, inches}$ r = Rate of fire, rounds per minute $\frac{W_{R}}{W_{h}} \doteq \frac{\cdot 136 V_{m}^{-1} + 10^{-6}}{D_{h}^{-41}} + 1.2$ $\frac{W_{i}}{N_{R}} \doteq \frac{\cdot 9 w_{g}}{N_{R}} \frac{1}{N_{R}} \frac{\cdot 9 w_{g}}{N_{R}} \frac{1}{N_{R}} \frac{1}{N_{$

For example, let us consider two classes of guns, a small caliber, high cyclic rate gun (say 20 mm., 650 rpm) and a large caliber, low cyclic rate gun (say 75 mm., 10 rpm). Then

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$$\frac{W_{h}}{W_{o}} (20 \text{ mm}) = \frac{.406 \times 10^{6}}{V_{m}^{2} [.136 + 925 \frac{N_{g}}{N_{R}}] + 1.09 \times 10^{6}}$$

$$\frac{W_{h}}{W_{o}} (75 \text{ mm}) = \frac{1.553 \times 10^{6}}{V_{m}^{2} [.136 + 37.2 \frac{N_{g}}{N_{R}}] + 1.863 \times 10^{6}}$$

Values are plotted in Figure 9, and compared against actual values. Good agreement is found. Again, it is found that $\frac{Wn}{W_0}$ decreases markedly with increasing muscle velocity. It will be noted that a number of rounds pur gun has a significant effect on $\frac{Wn}{W_0}$, the larger number of rounds per gun giving higher $\frac{Wn}{W_0}$ ratios. This would be expected until the total weight of the rounds are equal to or greater than the total weight of the gun. Also, inspection of the above equations reveals that for the same muscle velocities and rounds per gun, increases in rates of fire decreases $\frac{Wn}{W_0}$. Recoilless Guns

From (5 and 8):

$$\frac{W_{0}}{W_{h}} = \frac{9.5 \times 10^{-6} \text{ Vm}^{2}}{4.8 \times 10^{-6} \text{ Vm}^{2}} \qquad (\text{existing designs}) \qquad (\text{not including automatic feed})$$

$$\frac{W_{R}}{W_{h}} = \frac{W_{h} + W_{c} + W_{p}}{W_{h}} = 1 + \frac{W_{c} + W_{p}}{W_{c} + W_{p}} = 1 + \frac{W_{c} + W_{p}}{(57-105 \text{ mm. puns})}$$

$$\frac{W_{p}}{W_{h}} = 6.78 \times 10^{-6} \frac{V_{m}}{D_{h}} \cdot 615$$

$$W_{c} = 0.7 \text{ Wp}$$

For an automatic feed mechanism, we shall assume (based on the

standard gun) $\frac{w_{F}}{w_{h}} \doteq .0455 \pi \frac{V_{m}^{2}}{D_{h} \cdot 41} \times 10^{-6} + .1 \frac{w_{g}}{w_{h}}$ = $V_{m}^{2} \times 10^{-6} \left[.95 + \frac{.0455 \pi}{D_{h} \cdot 6} \right]$

(existing design)

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$$= V_{m}^{2} \times 10^{6} \left[.48 + \frac{.0455r}{D_{h}^{.6}} \right]$$

(proposed new design)

Then:

$$\frac{W_{g}}{W_{h}} \doteq V_{m}^{2} \times 10^{-6} \left[10, 45 + \frac{.6455\pi}{D_{h}^{-6}} \right] \quad (\text{existing design})$$

$$\doteq V_{m}^{2} \times 10^{-6} \left[5.28 + \frac{.0455\pi}{D_{h}^{-6}} \right] \quad (\text{proposed new design})$$

$$\frac{W_{R}}{W_{h}} \doteq 1 + 11.5 \times 10^{-6} \frac{V_{m}}{D_{h}^{-6}}$$

where:

w. = Weight of automatic feed mechanism

Wc = Weight of care of round

The installation weight should be between those for rockets and standard guns, say

$$\frac{W_{i}}{N_{R}w_{n}} \doteq .5 \frac{W_{q}}{N_{R}w_{n}}$$

Then:

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$$\frac{W_{h}}{W_{0}} = \frac{1}{1 + V_{m}^{2} \times 10^{-6} \left[\frac{11.5}{D_{h}^{-6} V_{m}^{-4}} + 1.5 \frac{N_{g}}{N_{R}} \left(10.45 + \frac{.0455\tau}{D_{h}^{-6} J}\right)\right]}{\frac{1}{1 + V_{m}^{2} \times 10^{-6} \left[\frac{11.5}{D_{h}^{-6} V_{m}^{-4}} + 1.5 \frac{N_{g}}{N_{R}} \left(5.28 + \frac{.0455\tau}{D_{h}^{-6} J}\right)\right]}$$
Let us now consider a large caliber, low cyclic rate gun (say

the second s

$$\frac{W_{h}}{W_{0}} = \frac{1}{1 + V_{m}^{2} \times 10^{-6} \left[\frac{6.25}{V_{m}} + 16\frac{N_{g}}{N_{R}}\right]}$$

$$= \frac{1}{1 + V_{m}^{2} \times 10^{-6} \left[\frac{6.25}{V_{m}} + 8.28\frac{N_{g}}{N_{R}}\right]}$$
(proposed guns)

Values are plotted in Figure 10. The same trend of marked decrease of $\frac{Wh}{W_0}$ with increase in ${\tt V}_m$ is found as with guns. The

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significance of the number of rounds per gun will again be noted. Gun-Launched Rockets

Inasmuch as gun-launched rockets (or closed-breech rocket launchers) are still in early development stages, there are little statistical data against which empirical relationships describing the family can be checked. In general, it would appear that the weight of the launcher must be increased over that for the pure rocket as a function of the rate of fire and velocity upon leaving the launcher, as in the case of guns. The ratio of rocket warhead weight to round weight would be expected to be less than for the pure rocket because of the necessity for strengthening the case to withstand the higher initial accelerations. Therefore, the over-all $\frac{W_{\rm h}}{W_{\odot}}$ for the gun-launched rocket would be less than for the pure rocket. Counterbalancing this, however, is the increase in accuracy, the dispersions approaching those of guns.

For the T131 rocket, used with the T110E2 launcher

 $w_h = 5.2 \text{ lb.}$ $w_g = 300 \text{ lb.}$ (launcher, magazine, and feed weight) $w_R = 10.7 \text{ lb.}$ $v_b = 2500 \text{ ft./sec.}$ $N_H = 25$ $W_{gr} = 650 \text{ rpm}$

Assuming an installation weight equal to 0.5 W_{g}

 $\frac{W_{h}}{W_{o}}$ = 0.182 @ V_b = 2500 ft./sec.

This compares with the values of 0.14 found for the pure rockets, (light case), 0.038 for a standard gun with the same performance, or 0.095 for a recoilless gun with the same performance.

Comparison of $\frac{W_A}{W_0}$ for Various Weapons

Of the weapons described, the bomb has the highest value of $\frac{W_k}{W_k}$

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because no propellant, or structure to resist the supporting forces is necessary. The rocket (except for the closed breech launched rocket) requires a comparatively large amount of propellant, but relatively little structure. The recoilless gun requires less propellant than the rocket, but more structure. The gun requires even less propellant, but even more structure. This will be noted in the comparison of warhead weight to round weights where the rocket has the lowest ratio of the three, the recoilless gun an intermediate ratio, and the pun the lowest ratio. Therefore, at space number of rounds per gun, the $\frac{W_h}{W_p}$ ratios of the three weapons should be the same, that weapon requiring the greatest structural weight requiring the most rounds per gun. These numbers are tabulated below, the numbers corresponding to the number of rounds per gun which must be carried to give an $\frac{Wh}{Wh}$ equal to that of a rocket, the gun muzzle velocities being equal to the rocket's burnt velocity. An intermediate velocity of 1500 feet per second was chosen for this comparison.

Projectile Diameter	Nur	nber of Rounds per	Gun Required at
	10 rpm	600 xyxa	
1 inch	235	550	
2 inch	145	345	Standard guns
5 inch	90	215	
1 inch			
2 inch	2095	875	Recoilless Guns
5 inch	50	145	

A similar table based on the number of rounds per pun required to equal the $\frac{W_n}{W_0}$ of the T131 rocket and launcher, 2075 projectile, 650 rpm, 25 rounds per launcher and 2500 feet per second burnt velocity is

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given below.

Projectile Diameter	Number of rounds	per gun required at
	650 rpm	
2175	105	Standard Gun
2175	70	Recoilless Gun

Values of L, The Aircraft Armanent Logistic Factor for Various Weapons.

As previously defined, the aircraft armament logistic factor is the product of the reciprocal of the probability of hit and the ratio of total weight of armament system carried to total weight of warbead carried. Thus:

 $L_{w} = \frac{1}{P_{h}} \frac{W_{o}}{W_{h}}$ $\frac{1}{L_{w}} = P_{h} \frac{W_{h}}{W_{o}}$

 P_h and $\frac{W_h}{W_0}$ are mutually related by their dependence on muscle (gun) or burnt (rocket) velocities. Their variations as functions of velocity have been individually discussed in previous sections. The over-all variation will be discussed below.

Bombs

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For bunds $\frac{W_h}{W_c}$ is essentially fixed. Therefore $1/L_w$ varies linearly with the probability of hit. Relative values of the product of L_w and the target area are given in the following table:

and the state of the					
	3000	3000		<u>00 feet</u>	
	4	9	4	9 mils	
12R/2					
0.1	9500	21,500	74,000	180,000	
0.5	22,000	49,000	175,000	390,000	

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Rockets

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The variation of $1/L_{w}A_{T}$ for rockets as a function of range, \bigtriangledown_{1} , burnt velocity and range release error is plotted in Figure 11. It will be noted that $1/L_{w}$ reaches a maximum (L_{w} reaches a minimum) within the velocity range of the rocket. As might be expected, the optimum velocity is somewhat lower for small release errors than for high; somewhat lower for large inherent dispersions than for small; and somewhat lower for short ranges than for long. The best compromise velocities (weighted toward firing at long ranges), appear to be approximately 1000 feet per second for the older (higher case weight) rockets, and 1600 feet per second for the newer (low case weight) rockets. Both values are sumewhat lower than those found in existing designs. Relative values of the product of $L_{w}A_{T}$ are shown below:

R →		30	00	L _W An	6000	feet	
AR	\$\$	4	9	4	9	mils	
ĸ							
0.1		2600	11,000	13,500	52,500	Older rockets	
0.5		5350	15,500	43,500	95,000		
0.1		1650	9100	8150	35,500	fewer pockets	
0.5		2650	9800	18,500	50,000		

Standard Guns

The variation of $1/L_w A_T$ for standard guns, as a function of range, T_1 , muscle velocity, and range release error are plotted for two guns (a small caliber high cyclic rate, and a large caliber, low cyclic rate gun, for various numbers of rounds per gun) in Figure 12. There, optimum velocities are also shown to be lower than standard design, approximately

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1700 feet per second for both types. The trends of variation of optimum velocity with release error, inherent dispersions, and range are the same as with rockets. Relative values of the product of $L_w A_T$ are shown below.

R→ 3		3000	600	6000		
∇ _ℓ →	2	5	2	5	mils	
AR						ann an an Anna an Anna an Anna an Anna an Anna
0.1	785	4550	4000	20,000	200 rounds	
0.5	1.700	6650	12,000	33,500	per gun	Small
0.1	600	3500	3250	15,000	400 rounds	high cyclic
0.5	1200	4750	9500	23,500	ber Km	T.S. C.S.
0.1	1550	14,000	11,500	30,000	10 rounds	
0.5	4650	15,500	35,500	85,000	ber Kau	Large
0.1	1250	7050	6150	29,500	20 rounds	low syclic
0.5	2550	9250	20,000	51,500	her forr	2-1 4

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It will be noted that for corresponding inherent dispersions, in the ranges of rounds per gun shown, the logistic factor for guns is higher than for the newer rockets (effectiveness per pound of installation weight is lower). This was indicated in the comparison given in the section discussing $\frac{Wh}{W_0}$. The lower limiting values for guns than for rockets are due to the lower range of dispersions.

Recoilless Guns

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The variation of $1/L_W A_T$ for recoilless guns, as a function of range, T_1 , muscle velocity and range release error are plotted in Figure 13 for two gun designs, one corresponding to existing practice, and a

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lighter one corresponding to proposed new designs, both taken as a large caliber, low cyclic rate weapon. The optimum velocity is shown to be approximately 1200 feet per second (weighted toward the longer range firing), for present design and approximately 1400 feet per second for the new design. The trends of variation of optimum velocity with release error, inherent dispersions, and range are the same as with rockets and standard guns. Relative values of the product of L_W and the target area, for the above velocities are shown below:

R >	3	000	6000		feet		
√,→	2	5	2	5	mils	and the second second second second	
0.5	1150 3300	3330 9100	7350 41.,500	28,000	10 rounds per gun	Present Designs	
0.1	800 2300	2300 6600	5100 18,000	18,000 49,000	20 rounds per gun		
0.1 0.5	900 2300	4750 6650	5250 18,000	22,000 45,500	10 rounds per gun	New	
0.1 0.5	685 1750	3600 5400	3900 13,500	16,000 26,500	20 rounda per gun		

L_W AT

It will be noted that for recoilless guns, as with standard guns, in the ranges of rounds per gun shown, for corresponding inherent dispersions, the logistic factor is higher than for the newer rockets, as was indicated in the $\frac{W_H}{W_O}$ comparison. The lower limiting values for recoilless guns than for rockets are due to the lower range of dispersions. However, the logistic factors for large caliber low cyclic rate recoilless guns are smaller than those for corresponding standard guns under

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comparable conditions.

Gun-Launched Rockets

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ia. ŭ The logistic factor for gun-launched rockets can be confidently determined only at the design velocity of the existing weapon, the T131 at 2500 feet per second. Assuming its dispersions to be in the same range as guns, the relative values of the product of $L_w A_T$ are given below.

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R >	3000		600	00
5.7	2	5	2	5
AR/R			,	
0.1	1300	7800	5650	32,000
0.5	1950	8550	12,500	42,500

These values are higher than for the recoilless gun (20 rounds per gun) at its best velocity. However, a reduction in the velocity of the T131 would reduce the logistic factors, until, at the same velocity the comparison would be approximately the same as given in the section on

 $\frac{W_{h}}{W_{O}}$, since the same inherent dispersions were assumed both for the Wo recoilless gun and the gun-launched rocket.

Comparison of Weapons on the Basis of L_{W^*}

Figure 14 shows the values of L_{W} versus range for the following weapons, against three target areas, 200, 2000, and 20,000 square feet.

- 1. Bomb
- 2. Rocket Light case, 1600 ft./sec.
- 3. Recoilless Guns, Large caliber, 1400 ft./sec.
 - a. 10 rpm, 10 rounds per gun
 - b. 650 rpm, 20 rounds per gun

-29-SECRET 4. Standard Guns, 1700 ft./sec.

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a. Large caliber, 10 rpm, 10 rounds per gun

b. Small caliber, 650 rpm, 600 rounds per gun

5. Gun-Launched Rocket T131, 2500 ft./sec., 650 rpm, 25 rounds per gun

No small caliber recoilless guns are included, since previous examination of logistic factors has indicated their relative inferiority to other weapons. No high cyclic rate large caliber standard guns are included because of the practical difficulties associated with their design and installation, and their relative inferiority in L_w . The projectile velocities are the optimum indicated in the previous sections, except for the T131, whose design velocity was taken.

The target areas, as stated previously, were selected to roughly correspond to the following tactical targets.

200 sq. ft. - Tank, or transport on rail or road

2000 sq. ft. - Pill box, artillery emplacement, or bridge abutment 20,000 sq. ft. - Troop vehicles or supply concentration

In general, the trends follow those shown in the hit probability section, emphasizing the greater weight of the hit probability term in the logistic factor. For the 200 sq. ft. targets at the longer ranges, the better guns have lower logistic factors than rockets, and rockets have lower logistic factors than bombs. For the 2000 sq. ft. targets, the rockets are generally comparable with guns, but better than bombs. For the 20,000 sq. ft. targets, rockets are better than most guns, but at short ranges or low errors and dispersions, bombs are better than all. Above 20,000 feet bombs will be best.

The effect of range is again emphasized, particularly against small

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targets. Against tanks, effectiveness is gained only by firing at short ranges, no matter what the weapon.

There are some rather important supplements to the conclusions reached in the section on hit probabilities when the weight characteristics of the weapon are considered. The gain in effectiveness from the use of guns over rockets against small targets is not nearly as marked because of the greater weight ratios of the guns. However, the effectiveness of all weapons is so low against small targets that even the small gains in effectiveness made possible by the use of guns should be utilized, since it may make the difference between failure and success of a sortie.

Among the various guns or gun-launched rockets, the small caliber, high cyclic rate, large number of rounds per gun standard gun is superior against all areas. It also has a good logistic factor compared with rockets or bombs. The large caliber standard gun, however, is the least effective of the guns. Between these two lie the gun-launched rocket and the recoilless guns. The gun-launched rocket, for comparable rates of fire and rounds per gun, appears somewhat superior to the recoilless rifle at the longer ranges, higher dispersions, and smaller areas. The two are nearly equal at the shorter ranges, lower dispersions and larger targets.

Examination of Effectiveness Index of Various Weapons

The previous section compared weapons on the basis of logistic factor. However, the results must be modified by the influence of $\left(\begin{array}{c} \sqrt{h} \\ \sqrt{h} \end{array}\right)T$, the remaining term in the effectiveness index. There are not sufficient effectiveness data to quantitize the effectiveness index in detail. However, the relative index of the different weapons may be examined qualitatively.

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Against small targets, the small caliber high cyclic rate gun has the most generally favorable logistic factor. However, $\left(\frac{P(n/n)}{v_n}\right)r$ for this weapon is essentially zero, when used against armored targets. The low cyclic rate recoilless rifle, or gun-launched rocket, which can deliver larger caliber and weight projectiles would have the best effectiveness index against tanks. The small caliber, high cyclic rate guns would have the best effectiveness index against convoys or trains of vehicles and troops.

Against the intermediate sized targets, unarmored or of light structure, the small caliber gun still shows the best effectiveness index. Against heavy structures, guns or rockets would show approximately equal effectiveness indices, but the lower accelerations of the rocket would enable the more efficient use of a greater number of warheads.

Against targets of 20,000 square foot area and greater, bombs have generally the highest effectiveness index, except where penetration must be accomplished by the kinetic energy of the round rather than by explosive effects.

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TABLE I

RELEASE ERROR CONTROL REQUIREMENTS

	$\nabla_{i} = 2$ mils			Ti= 5 mils			$G_i = 9$ mils		
Vav	▲ R/R	∆v/v _a	۵0(°)	∆ r/r	∆v/v _a	4 0 (*)	$\Delta R/R$	av/v _e	79(_{\$})
500 1000 1500 2000 2500 3000	0.0021 0.0084 0.019 0.035 0.076 0.12	0.0011 0.0084 0.029 0.070 0.1 0.1	0.33 1.3 3.0 5.0 5.0 5.0	0.0053 0.021 0.054 0.13 0.22 0.32	0.0027 0.021 0.081 0.1 0.1 0.1	0.84 3.2 5.0 5.0 5.0 5.0	0.0095 0.041 0.13 0.26 0.41 0.5	0.0048 0.041 0.1 0.1 0.1 0.1 0.1	1.5 5.0 5.0 5.0 5.0 5.0
				e = 60°					
500 1000 1500 2000 2500 3000	0.0040 0.016 0.036 0.069 0.12 0.17	0.0020 0.016 0.048 0.1 0.1 0.1	0.13 0.053 1.2 2.3 4.0 5.0	0.0099 0.040 0.098 0.22 0.40 0.5	0.0050 0.040 0.1 0.1 0.1 0.1	0.32 1.3 3.2 5.0 5.0 5.0	0.018 0.071 0.22 0.47 0.5 0.5	0.009 0.071 0.1 0.1 0.1 0.1	0.60 2.3 5.0 5.0 5.0 5.0
				R = 300 $V_{a} = 500$ $\Theta = 20^{\circ}$	0' ft./sec.				
500 1000 1500 2000 2500 3000	0.0042 0.017 0.041 0.10 0.18 0.26	0.0021 0.017 0.062 0.1 0.1 0.1	0.65 2.7 5.0 5.0 5.0 5.0	0.011 0.046 0.15 0.29 0.45 0.5	0.006 0.046 0.1 0.1 0.1 0.1].•7 5•0 5•0 5•0 5•0 5•0 5•0	0.019 0.090 0.28 0.5 0.5 0.5	0.010 0.090 0.1 0.1 0.1 0.1	3.0 5.0 5.0 5.0 5.0 5.0
$\Theta = 60^{\circ}$									
500 1000 1500 2000 2500 3000	0.0079 0.031 0.073 0.15 0.30 0.47	0.0040 0.031 0.1 0.1 0.1 0.1	0.26 1.0 2.4 5.0 5.0 5.0	0.020 0.079 0.30 0.5 0.5 0.5	0.010 0.079 0.1 0.1 0.1 0.1	0.66 2.6 5.0 5.0 5.0 5.0	0.036 0.16 0.5 0.5 0.5 0.5	0.018 0.1 0.1 0.1 0.1 0.1	1.2 5.0 5.0 5.0 5.0 5.0

* Below $\frac{\Delta R}{R} = 0.5$, $\frac{\Delta V_{a}}{V_{a}} = 0.1$, $\Delta \Theta = 5.0$



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FIGURE I. EFFECT OF GRAVITY UPON TRAJECTORY OF A PROJECTILE IN A VACUUM



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ASSUME SIGHT SETS DEFLECTION ANGLE E0 AT R0 BUT RANGE INFORMATION IS UNCERTAIN WITHIN $R_1 = R_0 + \Delta R > R_0 - \Delta R = R_2$ TOTAL DISPERSION AT TARGET (MIL) = $\Delta E_0 = \Delta E_{02} - \Delta E_{01} = \left(\frac{E_0 R_2 - \gamma_2}{R_0}\right) - \left(\frac{E_0 R_1 - \gamma_1}{R_0}\right)$ $\frac{E_0 R_2 - E_2 R_2 - E_0 R_1 + E_1 R_1}{R_0} = \frac{R_2 (E_0 - E_2) + R_1 (E_1 - E_0)}{R_0}$ $\frac{1}{2} \left(\frac{R_0 - \Delta R}{E_0 - E_2} + (R_0 + \Delta R) (E_1 - E_0) \right)}{R_0}$ $\stackrel{\cdot}{=} E_1 - E_2 + \frac{\Delta R}{R_0} \left[\left(E_1 - E_0 \right) - \left(E_0 - E_2 \right) \right]$ BUT $(E_1 - E_0) \doteq CONST. \times \Delta R \doteq (E_0 - E_2)$

SO, $\Delta E_0 = E_1 - E_2$ THE LOCATION OF THE MEAN CENTER OF IMPACT (MIL) = - COUST $\left(\frac{\Delta R^2}{R_0}\right)$ INSERTED IN E₀, KNOWING RANGE OF $\frac{\Delta R}{R_0}$ THEN INCREMENT OF LINEAR ERROR FROM MEAN (MIL) = $\pm \frac{E_1 - E_2}{2}$ ASSUME $f_{R} = \frac{E_1 - E_2}{2} = CONST. (\Delta R)$

FIGURE 2. ASSUMPTIONS FOR RANGE ERROR

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FIGURE 3. COMPARISON OF APPROXIMATE AND EXACT $\Delta \Sigma g^{1}s$

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FIGURE 4.A. EFFECT OF UNCERTAINTIES AS TO POINT OF RELEASE ON DISPERSION OF BOMBS

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FIGURE 4 B. EFFECT OF UNCERTAINTIES AS TO POINT OF RELEASE ON DISPERSION OF BOMBS

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FIGURE 4C. EFFECT OF RELEASE ERROR ON OF

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FIGURE 5 A. EFFECT OF RANGE UPON HIT PROBABILITY PER SQUARE FOOT OF TARGET AREA

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FIGURE 5.B. PROBABILITY OF HIT PER SQUARE FOOT OF TARGET AREA AS A FUNCTION OF RANGE



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> FIGURE 5d - EFFECT OF RANGE UPON HIT PROBABILITY PER SQUARE FOOT OF TARGET AREA.



FIGURE 6a-EFFECT OF VELOCITY OF PROJECTILE RELATIVE TO AIRCRAFT UPON HIT PROBABILITY PER SQUARE FOOT OF TARGET.



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FIGURE 6 B. EFFECT OF VELOCITY OF PROJECTILE RELATIVE TO AIRCRAFT UPON HIT PROBABILITY PER SQUARE FOOT OF TARGET

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FIGURE 7. EFFECT OF RELEASE ERROR ON OX

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110 Va.= 500 F.P.S. Va $\Theta = 30^{\circ}$ 100 Ā0**-**5° 200 SQ.FT. TARGET 90 PER HIT. R 80 4MILS BOMBS Oi 2MILS GUNS NUMBER OF ROUNDS REQUIRED 70 60 BOMB 50 0 700 F.P.S. ROCKET R 0 R BOMBS 1360 F.P.S.ROCKET 2500 F.P.S. GUN JANILS GUNS Δ 40 30 20 10 4000 6000 6000 2000 4000 2000 SLANT RANGE (FEET)

> FIGURE 7A. EFFECT OF SLANT RANGE UPON ROUNDS REQUIRED PER HIT FOR A SPECIFIED TARGET AREA

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FIGURE 7 B. EFFECT OF SLANT RANGE UPON ROUNDS REQUIRED PER HIT FOR A SPECIFIED TARGET AREA





FIGURE 7C. NUMBER OF ROUNDS REQUIRED PER HIT AS A FUNCTION OF RANGE - TARGET AREA = 20,000 SQUARE FEET

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FIGURE 9-EFFECT OF MUZZLE VELOCITY OF GUN PROJECTILE UPON RATIO OF WEIGHT OF WARHEAD TO THAT OF TOTAL ARMAMENT SYSTEM.



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FIGURE II a - RECIPROCAL OF AIRCRAFT ARMAMENT LOGISTIC FACTOR AS A FUNCTION OF ROCKET BURNT VELOCITY.



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FIGURE II 6 - RECIPROCAL OF AIRCRAFT ORDNANCE LOGISTIC FACTOR AS A FUNCTION OF ROCKET BURNT VELOCITY.



FIGURE 12A. RECIPROCAL OF AIRCRAFT ARMAMENT LOGISTIC FACTOR AS A FUNCTION OF GUN MUZZLE VELOCITY

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FIGURE 12B. RECIPROCAL OF AIRCRAFT ARMAMENT LOGISTIC FACTOR AS A FUNCTION OF GUN MUZZLE VELOCITY

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FIGURE ISA. RECIPROCAL OF AIRCRAFT ARMAMENT LOGISTIC FACTOR AS A FUNCTION OF GUN MUZZLE VELOCITY

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LOW CYCLIC RATE -- LARGE CALIBER RECOILLESS GUNS --- NEW DESIGNS.

FIGURE 13 B. RECIPROCAL OF AIRCRAFT ARMAMENT LOGISTIC FACTOR AS A FUNCTION OF MUZZLE VELOCITY OF PROJECTILE FROM RECOILLESS GUN

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FIGURE I4AEFFECT OF SLANT RANGE UPON AIRPLANE ARMAMENT LOGISTIC FACTOR.



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FIGURE 14 B. AIRPLANE ARMAMENT LOGISTIC FACTOR AS A FUNCTION OF RANGE TARGET AREA = 2000 SQUARE FEET

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FIGURE 14C. AIRPLANE ARMAMENT LOGISTIC FACTOR AS A FUNCTION OF RANGE

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