

ARMY RESEARCH LABORATORY



Performance of the Miniature Airborne GPS Receiver

by Tom Van Flandern and Thomas B. Bahder

ARL-TR-1739

July 1998

DTIC QUALITY INSPECTED 1

19980901 009

Approved for public release; distribution unlimited.

The findings in this report are not to be construed as an official Department of the Army position unless so designated by other authorized documents.

Citation of manufacturer's or trade names does not constitute an official endorsement or approval of the use thereof.

Destroy this report when it is no longer needed. Do not return it to the originator.

Army Research Laboratory

Adelphi, MD 20783-1197

ARL-TR-1739

July 1998

Performance of the Miniature Airborne GPS Receiver

Tom Van Flandern and Thomas B. Bahder
Sensors and Electron Devices Directorate

sponsored in part by

U.S. Army Aviation and Missile Command
Redstone Arsenal, AL 35898-5240

Approved for public release; distribution unlimited.

Abstract

At a fixed, well-surveyed location, position determinations from a MAGR (Miniaturized Airborne Global Positioning System Receiver) averaged over a six-week period were correct to within 0.5 m. However, the standard deviation of an individual position determination was 56 m. Almost 20 percent of the individual position determinations had errors exceeding 20 m. One in every 300 position determinations had an error exceeding 0.5 km. This anomalously large error distribution tail raises questions about the MAGR's suitability for some Army-critical functions, such as precision guidance.

Contents

Introduction	1
Mean Position	2
Individual Position Errors	3
Anomalies	7
Conclusions	8
Discussion	9
Acknowledgments	10
Distribution	11
Report Documentation Page	17

Figures

1. MAGR (X, Y) position errors	3
2. MAGR (Y, Z) position errors	3
3. MAGR (X, T) position errors	4
4. MAGR (X, Y) position errors at successively closer views	5
5. Histogram of position errors	6
6. MAGR (X, T) position errors at high time resolution	7
7. Percentage of position errors within a sphere of radius R	8

Tables

1. WGS 84 surveyed coordinates of MAGR at GGAO	1
2. Position errors of MAGR at GGAO	2
3. Error distribution statistics	6

Introduction

From mid-October 1996 to mid-January 1997, a Rockwell Miniature Airborne GPS (Global Positioning System) Receiver (MAGR) was placed at a fixed, well-surveyed site: the NASA Goddard Space Flight Center (GSFC) Geophysical and Astronomical Observatory (GGAO) in Greenbelt, MD. Useful data were recorded during the six-week period from early December 1996 to mid-January 1997. Continual position determinations were recorded at 1-s intervals at every opportunity during that period. We report here the results of a study of the accuracy of those position determinations. In general, results in field use would be expected to be poorer than those given here, because of receiver motion and a continually changing environment.

The site in question was surveyed on 24 May 1995, and placed on the WGS 84 geodetic system. The surveyed site coordinates (X_0, Y_0, Z_0) are shown in table 1.

Over the six-week test span, the MAGR made continuous estimates (X_i, Y_i, Z_i), $i = 1, \dots, N$, of the site position in the same reference system at 1-s intervals during the periods when it was active. Because the volume of data at that fine time spacing was quite large, and because the individual position determinations were changing so little on that time scale, this study employed 30-s sampling of the total data set, except where otherwise noted. This left $N = 8573$ individual sampled position determinations on which to base our analysis. From those, we compiled a number of plots and statistics to illustrate the accuracy of these measures.

Table 1. WGS 84 surveyed coordinates of MAGR at GGAO.

Site coordinate	Surveyed value (m)
X_0	+1,130,774.372
Y_0	-4,831,255.014
Z_0	+3,994,200.505

Mean Position

First, we formed differences between the individual MAGR position determinations and the surveyed position, which we call "position errors":

$$\Delta X_i = X_i - X_0, \Delta Y_i = Y_i - Y_0, \Delta Z_i = Z_i - Z_0.$$

Then we computed simple arithmetic means of the position errors:

$$\langle \Delta X_i \rangle = \frac{1}{N} \sum_{i=1}^N \Delta X_i, \langle \Delta Y_i \rangle = \frac{1}{N} \sum_{i=1}^N \Delta Y_i, \langle \Delta Z_i \rangle = \frac{1}{N} \sum_{i=1}^N \Delta Z_i.$$

The mean position errors and their standard deviations are shown in table 2. We note that the mean position errors are zero to within one standard deviation, indicating that the MAGR apparently had no serious long-term bias problems as great as 0.5 m. However, the standard deviations are surprisingly large for such a large value of N . We show the reason for this shortly when we examine the detailed behavior.

Table 2. Position errors of MAGR at GGAO.

Coordinate	MAGR - WGS 84 (m)	
	(mean)	(st dev)
$\langle \Delta X_i \rangle$	+0.282	± 0.491
$\langle \Delta Y_i \rangle$	+0.264	± 0.342
$\langle \Delta Z_i \rangle$	-0.087	± 0.234

Individual Position Errors

For our first inspection of the individual position errors, we simply plotted ΔY_i against ΔX_i , as shown in figure 1. It was immediately evident that something serious was wrong, because errors exceeding 30 m ought to be rare for any authorized receiver capable of 10-m or better accuracy. Yet not only were 30-m position errors common, some errors even reached the 1-km level. Figure 2, which plots ΔZ_i against ΔY_i , shows that the third dimension has similar behavior, although with a somewhat less extreme range of ± 400 m in ΔZ_i .

The computed standard deviation of a single ΔX_i value is 45 m; for a single ΔY_i value it is 32 m; and for a single ΔZ_i value it is 22 m. The mathematical reason for these unexpectedly large deviations is simply that a single error of 1000 m contributes more to the standard deviation than do 8000 "normal" observations with errors of order 10 m each. So we see that the error distribution is so far from a normal distribution that it cannot be accurately represented by a standard deviation. For the same reason, we do not attempt to compute other such customary error measures, such as "circular error probable" (CEP)¹ and its three-dimensional counterpart "spherical error probable" (SEP), inasmuch as they too would be misleading.

Figure 3 plots ΔX_i against time, showing the distribution of problem points over the six-week data span. Time is measured in hours from December 1, 1996, which is the beginning of a GPS week. It is blocked into 1-week groups over the 6-week span of data collection, beginning 40 hours into the first GPS week.

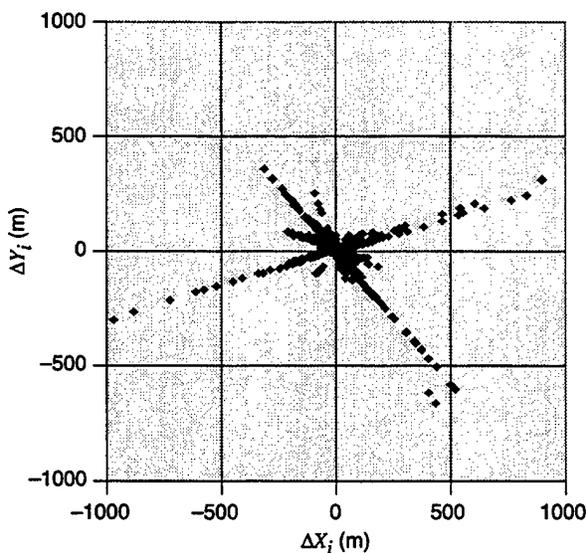


Figure 1. MAGR (X, Y) position errors.

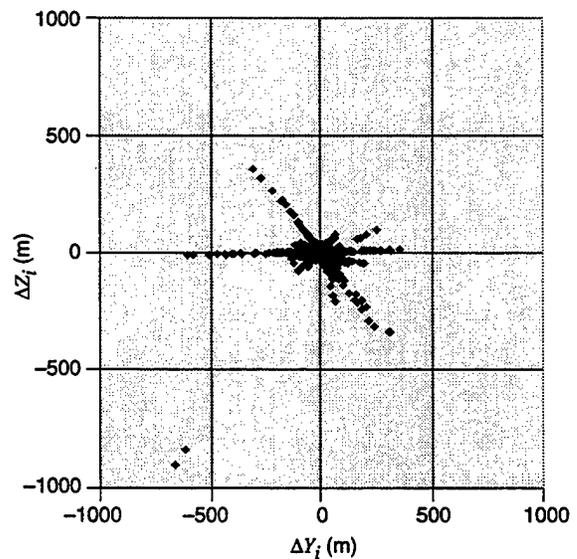


Figure 2. MAGR (Y, Z) position errors.

¹J. L. Leva, M. U. de Haag, and E. D. Van Dyke, 1996. In *Understanding GPS: Principles and Applications*, E. D. Kaplan, ed., Artech House, Boston, p 281.

Figure 3. MAGR (X, T) position errors.

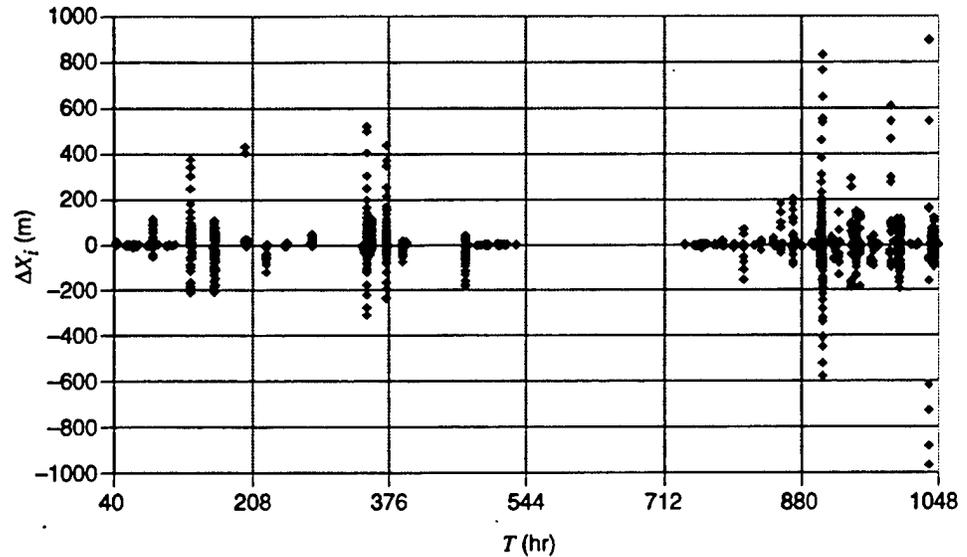


Figure 4 shows successively closer views of the center of the $(\Delta X_i, \Delta Y_i)$ -position error distribution, similar to figure 1, revealing more details for the smaller errors.

For further study, it is useful to compute the magnitude of the position error vector $(\Delta X_i, \Delta Y_i, \Delta Z_i)$ at each observation:

$$\Delta R_i = \sqrt{\Delta X_i^2 + \Delta Y_i^2 + \Delta Z_i^2} .$$

Figure 5 is a histogram showing the distribution of ΔR_i in our 8573 sampled data points. Table 3 gives the statistics that actually describe the error distribution, and which were used to plot the histogram. For example, 1583 (18.46 percent) of the 8573 ΔR_i values lie in the range from 10 to 15 m.

Note that 56 percent of the measures lie within a nominal 10-m error sphere. This result is consistent with MAGR error descriptions in other reports, which have led to such conclusions as "The probability that the error lies within a 9.5-m sphere is 50 percent, and the MAGR therefore meets specifications." However, as the table shows, that statistic is highly misleading, since many more large errors exist than it would normally imply. Because the error distribution is not even approximately a normal distribution, no valid conclusions could be drawn about MAGR position errors in general from any single summary statistic. A histogram such as figure 5 would be needed for a proper assessment of reliability. However, if the customary error parameters had been supplemented with the standard deviation of an individual position error (56 m for our MAGR data), appropriate alarms would have been raised from the start.

**Figure 4. MAGR
(X, Y) position errors
at successively closer
views.**

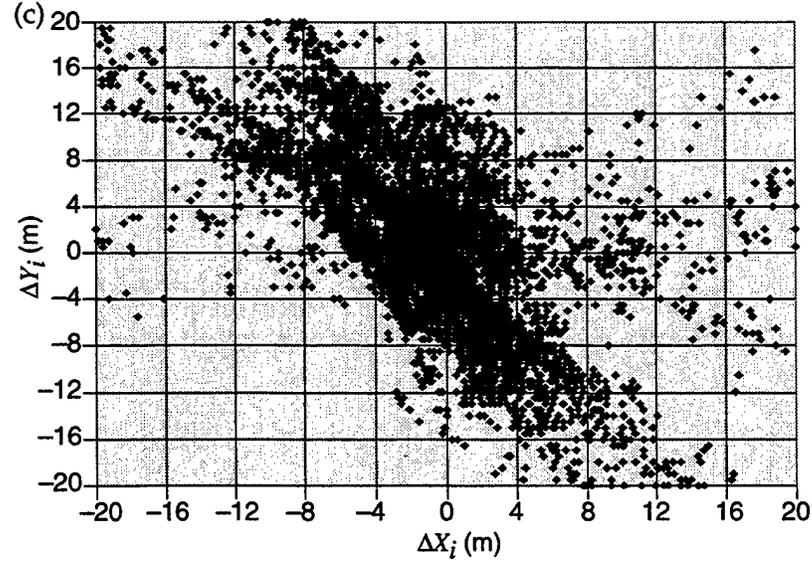
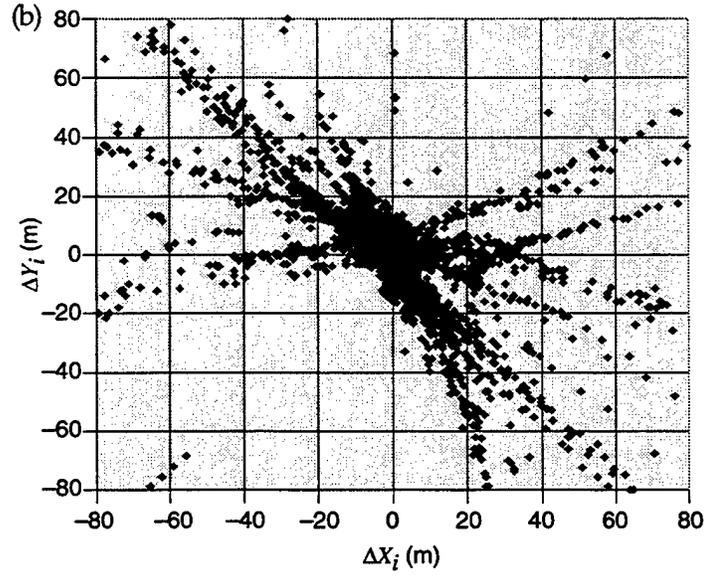
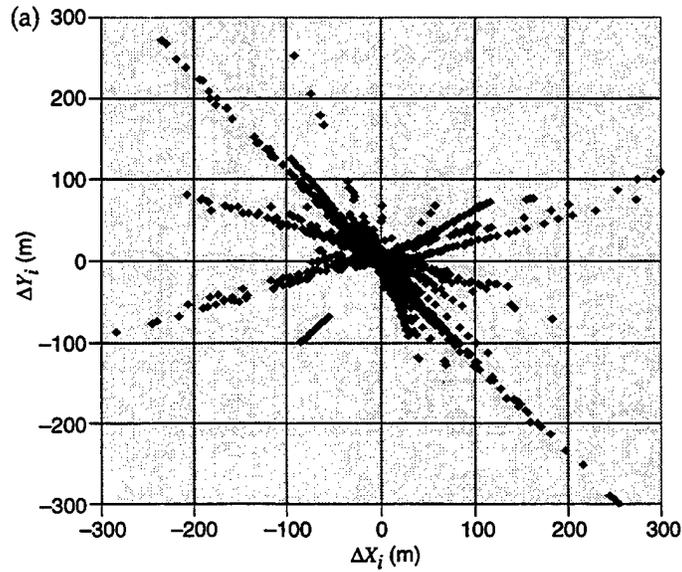


Figure 5. Histogram of position errors.

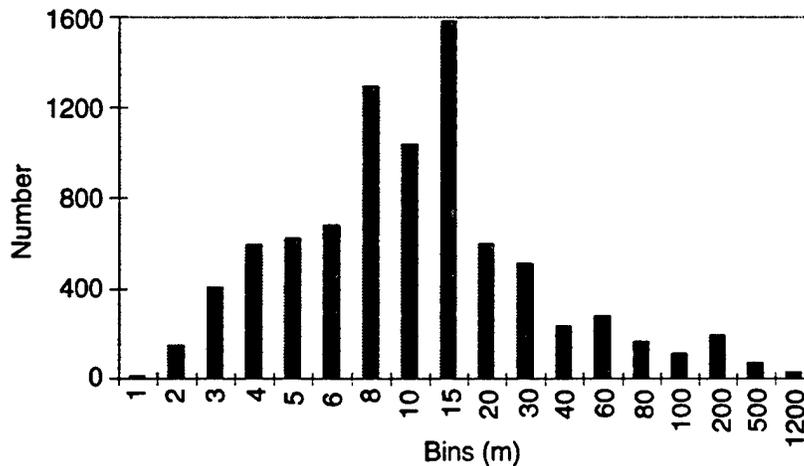


Table 3. Error distribution statistics.

Range bins (m)	Number of position errors in bin	Percentage of total errors
0-1	11	0.13
1-2	49	1.74
2-3	406	4.73
3-4	594	6.93
4-5	625	7.29
5-6	679	7.92
6-8	1293	15.08
8-10	1040	12.13
10-15	1583	18.46
15-20	599	6.98
20-30	512	5.97
30-40	235	2.74
40-60	278	3.24
60-80	166	1.94
80-100	111	1.29
100-200	193	2.25
200-500	70	0.82
500-1200	29	0.34

Anomalies

Figure 6 shows high time-resolution detail for one of the largest position error excursions. ΔX_i is plotted against time in hours over a 39-minute span. Points are at 1-s intervals (rather than the usual 30-s sampling), and individual blocks are six minutes wide. (The structure of other anomalies is usually similar.) Although the anomaly is slow to build and slow to terminate, the sudden jump in the middle takes place in just two minutes. During that interval, our stationary site at GSFC would register a velocity approaching 80 km/hr if MAGR position determinations were taken literally.

We define the fraction of individual position errors within a sphere of radius R as $n(R)$, where $0 \leq n(R) \leq 1$, $R^2 = X^2 + Y^2 + Z^2$, and $\delta(X)$ is the Dirac delta function:

$$n(R) = \frac{1}{N} \int_0^R 4\pi R^2 dR \sum_{i=1}^N \delta(X - \Delta X_i) \delta(Y - \Delta Y_i) \delta(Z - \Delta Z_i) .$$

The value of R that yields $n(R) = 0.5$ is the traditional SEP performance parameter. Figure 7 shows a plot of $100 n(R)$, the percentage of individual position errors ΔR_i within a sphere of radius R , versus $\text{Log}_{10} R$. The logarithm of radius in meters was used so that errors over such a large range can be seen in one plot. The ordinate is just the percentage of individual position errors for which $\Delta R_i < R$. As an example, the plot shows that 90 percent of the individual position errors have $\text{Log}_{10} \Delta R_i < 1.6$, which corresponds to errors less than 40 m; 10 percent of the errors are above 40 m.

Figure 6. MAGR (X, T) position errors at high time resolution.

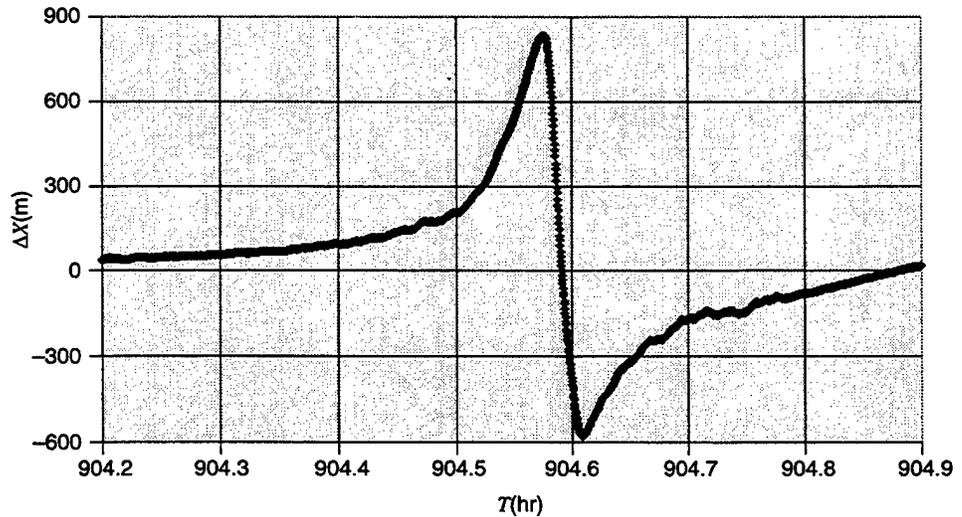
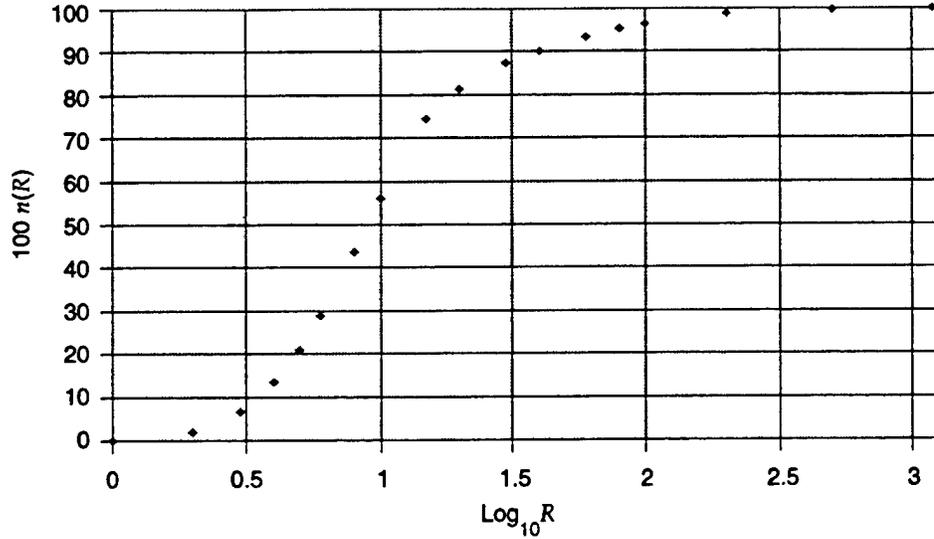


Figure 7. Percentage of position errors within a sphere of radius R .



Conclusions

The size of the anomalies, when they occur, seems fairly random. We note that most short MAGR runs would show a much smaller standard deviation. The longer the data span considered, the larger the standard deviation seems to become. It is not at all clear that we have sampled its worst behavior, and runs longer than six weeks might catch still poorer performance. But it seems clear that this anomalously large error distribution tail raises questions about the MAGR's suitability for some Army-critical functions, such as precision guidance.

Discussion

A draft copy of this report was circulated to interested parties. We have had the following feedback.

Rockwell Corporation has written a white paper (MAGR Technical Direction Note, June 15, 1998) discussing a MAGR anomaly that can occur during satellite acquisition. This feature remains in the MAGR software through Link 10. The GDOP (geometric dilution of precision) gives no hint of a problem in connection with this type of anomaly. However, the anomalies we see are not confined to acquisition or the other circumstances documented by Rockwell.

Joe Clifford of Aerospace Corp. notes the similarity of the detailed anomaly in figure 6 to a "constellation singularity," where the fourth satellite being tracked goes through the plane of the other three. He wondered if our MAGR might have been inadvertently set in "hover mode" or some other setting that freezes the constellation (private communication). Brian Baeder of MICOM, who set up the MAGR at GSFC, is quite certain no such settings were made, inadvertently or otherwise. We do agree, however, that the signature of the anomalies is like that of a constellation singularity.

Paul Olson of CECOM writes with some data from another MAGR at the Starfire Optical Range (SOR). In eight runs of roughly four hours length each, over a four-day span in October to November 1996, he also reports one large anomaly with a similar character to that in our figure 6, but cautions that other sampled data had 50-percent CEP values ranging between 3.9 and 8.1 m, with 95-percent CEP values between 7.0 and 20.7 m. He questions whether the anomalies can be as frequent as we report. He further notes that the GDOP did deteriorate during the anomaly, beginning with a MAGR constellation change, going off-scale with a second change, and then gradually recovering as the GDOP fell again to values that are more reasonable. He notes that good constellations were available to the MAGR during the anomaly, but were not used. He suggests this might be related to the characteristics of the Ashtech antenna used with the MAGR for their and our runs, perhaps inhibiting the MAGR from locking onto low-elevation satellites (private communication).

Olson's report led us to check the time distribution of our anomalies again. We noted that we also had only one large anomaly and a few much smaller ones in our first half-week of operation. During that period, our 50-percent CEP was 4.2 m, and our 95-percent CEP was 18 m, figures in the range of those seen at SOR. Then things got much worse. This lasted until an 8-day break over the Christmas–New Year's holidays, following which the MAGR was again well-behaved for several days, performed worse for the next several days, and then performed poorly for almost every run. This suggests a problem that worsens with the length of time that the MAGR has been in continuous operation—a matter of definite interest and concern to the Army.

Acknowledgments

We are indebted to Paul Olson and his group at U.S. Army CECOM for coordinating data acquisition with a CECOM MAGR at SOR, and for supplying plots that showed similar anomalies. This assured us that the problem was not unique to the particular MAGR or site we used. Charmaine Gilbreath provided laboratory facilities at SOR for data acquisition with CECOM's MAGR. We also acknowledge Cedric Lewis, the Navy's Senior GPS Systems Engineer for Aircraft Integrations at Pax River, who informs us that anomaly problems have existed at least since Link 7 of the MAGR firmware, and still exist in the latest (Link 10) release (private communication).

Carroll Alley at University of Maryland Physics provided the initial impetus for this project and some equipment needed for security at GSFC. Tom Clark provided facilities at NASA Goddard to house the receiver and associated equipment. Chuck Kodak at GSFC monitored the data acquisition. Brian Baeder at Aviation and Missile Command (MICOM) configured the MAGR in Huntsville, brought it to Maryland for data acquisition, and translated the outputs. William C. McCorkle of MICOM provided support and encouragement for the project.

Distribution

Admnstr
Defns Techl Info Ctr
Attn DTIC-OCF
8725 John J Kingman Rd Ste 0944
FT Belvoir VA 22060-6218

Defns Mapping Agency
Attn R Klotz
4211 Briars Rd
Olney MD 20832-1814

Defns Mapping Agency
Attn L-A1 B Tallman
Attn L-41 B Hagan
Attn L-41 D Morgan
Attn L-41 F Mueller
3200 2nd Stret
ST Louis MO 63116

Defns Mapping Agency Sys Ctr
Attn Code SC/Eid S Malys MS D-84
4600 Sangamore Rd
Bethesda MD 20816-5003

Ofc of the Dir Rsrch and Engrg
Attn R Menz
Pentagon Rm 3E1089
Washington DC 20301-3080

Ofc of the Secy of Defns
Attn ODDRE (R&AT)
Attn ODDRE (R&AT) S Gontarek
The Pentagon
Washington DC 20301-3080

OSD
Attn OUSD(A&T)/ODDDR&E(R) R J Trew
Washington DC 20301-7100

AMC OMP/746 TS
Attn A Chasko
PO Box 310
High Rolls NM 88325

AMCOM MRDEC
Attn AMSMI-RD W C McCorkle
Redstone Arsenal AL 35898-5240

Army Rsrch Lab
Attn AMSRL-PS-ED J Vig

Army Rsrch Lab (cont'd)
Attn AMSRL-PS W Gelnovatch
Attn AMSRL-PS-P M Dutta
FT Monmouth NJ 07703

Army Rsrch Ofc
Attn B Gunther
Attn H Everitt
Attn M Stroschio
4300 S Miami Blvd
Research Triangle Park NC 27709

Army Rsrch Physics Div
Attn AMXRO-PH D Skatrud
PO Box 12211
Research Triangle Park NC 27709-2211

CECOM
Attn PM-GPS
Attn AMSEL-RD-C2-ES P Olson Bldg 2525
FT Monmouth NJ 07703

CECOM
Sp & Terrestrial Commctn Div
Attn AMSEL-RD-ST-MC-M H Soicher
FT Monmouth NJ 07703-5203

Dir for MANPRINT
Ofc of the Deputy Chief of Staff for Prsnrl
Attn J Hiller
The Pentagon Rm 2C733
Washington DC 20301-0300

Hdqtrs Dept of the Army
Attn DAMO-FDT D Schmidt
400 Army Pentagon Rm 3C514
Washington DC 20301-0460

MICOM RDEC
Attn A Gamble
Attn AMSMI-RD A Killen
Redstone Arsenal AL 35898-5240

MICOM RDEC
Attn AMSMI-RD P Jacobs
Redstone Arsenal AL 35898-5420

MICOM RDEC Weapons Sci Dirctrt
Attn J Dowling
Redstone Arsenal AL 35898-5240

Distribution (cont'd)

PM GPS
Attn LTC J Lofgren
Bldg 914 Murphy Dr
FT Monmouth NJ 07703

US Army Edgewood RDEC
Attn SCBRD-TD J Vervier
Aberdeen Proving Ground MD 21010-5423

US Army Info Sys Engrg Cmnd
Attn ASQB-OTD F Jenia
FT Huachuca AZ 85613-5300

US Army MICOM
Attn AMSMI-RD-MG-NC G Graham
Attn B Baeder
Redstone Arsenal AL 35898-5254

US Army Natick RDEC Acting Techl Dir
Attn SSCNC-T P Brandler
Natick MA 01760-5002

US Army Rsrch Ofc
Attn G Iafrate
4300 S Miami Blvd
Research Triangle Park NC 27709

US Army Simulation, Train, & Instrmntn
Cmnd
Attn J Stahl
12350 Research Parkway
Orlando FL 32826-3726

US Army Tank-Automtv & Armaments Cmnd
Attn AMSTA-AR-TD C Spinelli
Bldg 1
Picatinny Arsenal NJ 07806-5000

US Army Tank-Automtv Cmnd Rsrch, Dev, &
Engrg Ctr
Attn AMSTA-TA J Chapin
Warren MI 48397-5000

US Army Test & Eval Cmnd
Attn R G Pollard III
Aberdeen Proving Ground MD 21005-5055

US Army Train & Doctrine Cmnd
Battle Lab Integration & Techl Dirctr
Attn ATCD-B J A Klevecz
FT Monroe VA 23651-5850

US Military Academy
Dept of Mathematical Sci
Attn MAJ D Engen
West Point NY 10996

Nav Rsrch Lab
Attn Code 8150 R Beard
Attn Code 8150/SFA J Buisson
4555 Overlook Ave
Washington DC 20375

Nav Surface Warfare Ctr
Attn Code B07 J Pennella
Attn Code K12 E Swift
Attn Code K12 J O'Toole
17320 Dahlgren Rd Bldg 1470 Rm 1101
Dahlgren VA 22448-5100

NAVSTAR GPS JPO
Attn SMC/CZJ D Crane
2435 Vela Way, Ste 1613
Los Angeles AFB CA 90245-5500

Ofc of Nav Rsrch
Attn ONR 331 H Pilloff
800 N Quincy Stret
Arlington VA 22217

US Nav Observatory
Attn K Johnston
3450 Massachusetts Ave NW
Washington DC 20392-5240

US Nav Observatory
Attn B Bollwerk
5580 Piedra Vista
Colorado Springs CO 80908

AFSPC/DRFN
Attn CAPT R Koon
150 Vandenberg Stret Ste 1105
Peterson AFB CO 80914-45900

Air Force Phillips Lab
Attn GPIM J A Klobuchar
29 Candolf Rd
Hanscom AFB MA 01731-3010

Distribution (cont'd)

ASC OL/YUH
Attn JDAM-PIP LT V Jolley
102 W D Ave
Eglin AFB FL 32542

DOT AFSPC/DRFN
Attn H Skalski
150 Vandenberg Stret
Peterson AFB CO 80914

GPS Joint Prog Ofc Dir
Attn COL J Clay
2435 Vela Way Ste 1613
Los Angeles AFB CA 90245-5500

Holloman AFB
Attn K Wernie
1644 Vandergrift Rd
Holloman AFB NM 88330-7850

US Army PM GPS GFO
Attn WR-ALC/LKNA Walker
460 2nd St Ste 221
Robins AFB GA 31098-1640

DARPA
Attn B Kaspar
Attn L Stotts
3701 N Fairfax Dr
Arlington VA 22203-1714

NIST
Attn MS 847.5 M Weiss
Attn S Jefferts
Attn R/E/SE J Kunches
325 Broadway
Boulder CO 80303

Applied Rsrch Lab Univ of Texas
Attn B Renfro
Attn J Saunders
Attn R Mach
PO Box 8029
Austin TX 78713-8029

Stanford University
Attn HEPL/GP-B D Lawrence
Attn HEPL/GP-B T Walter
Stanford CA 94305-4085

Univ of Colorado Dept of Physics
Attn N Ashby
Campus Box 390
Boulder CO 80309-0390

Univ of Maryland Dept of Physics
Attn C Alley
Attn C W Misner
College Park MD 20742

University of Texas ARL Electromag Group
Attn Campus Mail Code F0250 A Tucker
Austin TX 78713-8029

Aerospace
Attn J Langer
Attn M4/954 C Yinger
Attn M Dickerson
PO Box 92957 M4/954
Los Angeles CA 90009

Aerospace Corp
Attn A Satin
Attn J M Clifford
Attn A Wu MS M5/686
Attn B Feess MS M4/956
Attn B Winn MS M5/685
Attn H F Fliegel MS M5/685
Attn R DiEsposti
2350 E El Segundo Blvd
El Segundo CA 90245

Allen's Time
Attn D Allan
PO Box 66
Fountain Green UT 84632

ARINC
Attn L Conover
1925 Aerotech Dr Ste 212
Colorado Springs CO 80916

ARINC
Attn P Mendoza
4055 Hancock Stret
San Diego CA 92110

Distribution (cont'd)

Ashtech Inc
Attn S Gourevitch
1177 Kifer Rd
Sunnyvale CA 94086

BD Systems
Attn J Butts
385 Van Ness Ave #200
Torrance CA 90501

Charles Stark Draper Lab
Attn R Greenspan
555 Technology Sq
Cambridge MA 02139-3563

Hewlett-Packard Co
Attn J Kusters
5301 Stevens Creed Blvd
Santa Clara CA 95052

Hicks & Associates, Inc
Attn G Singley III
1710 Goodrich Dr Ste 1300
McLean VA 22102

Hughes
Attn S Peck
Attn R Malla
800 Apollo Ave PO Box 902
El Segundo CA 90245

Hughes Space & Comm
Attn MS/SC/SIO/S364 C Shecklells
PO Box 92919 Airport Station
Los Angeles CA 90009

Intermetrics Inc
Attn J McGowan
615 Hope Rd Bldg 4 2nd floor
Eatontown NJ 07724

ITT Aerospace
Attn MS 2511 R Peller
Attn MS 8528 H Rawicz
Attn MS 8538 L Doyle
Attn P Brodie
100 Kingsland Rd
Clifton NJ 07014

KERNCO
Attn R Kern
28 Harbor Stret
Danvers MA 01923

Lockheed Martin
Attn J Taylor
Attn B Marquis
1250 Academy Park Loop Ste 101
Colorado Springs CO 80910

LORAL
Attn B Mathon
700 N Frederick Pike
Gaithersburg MD 20879

LORAL
Attn B Pisor
2915 Baseline Rd #530
Boulder CO 80303

LORAL Fed Sys
Attn 182/3N73 D H Winfield
Attn S Francisco Bldg 182/3A60
700 N Frederick Ave
Gaithersburg MD 20879

LORAL Fed Sys
Attn J Kane
Attn M Baker
Attn R Astalos
9970 Federal Dr
Colorado Springs CO 80921

Magnavox Electric Sys Company
Attn D Thornburg
2829 Maricopa Stret
Torrance CA 90503

Overlook Systems
Attn D Brown
Attn T Ocvirk
1150 Academy Park Loop Ste 114
Colorado Springs CO 80910

Palisades Inst for Rsrch Svc Inc
Attn E Carr
1745 Jefferson Davis Hwy Ste 500
Arlington VA 22202-3402

Distribution (cont'd)

PAQ Commctn
Attn Q Hua
607 Shetland Ct
Milpitas CA 95035

Rockwell CACD
Attn L Burns
Attn M A Milten
400 Collins Rd NE
Cedar Rapids IA 52398

Rockwell Collins
Attn C Masko
Cedar Rapids IA 52498

Rockwell DA85
Attn W Emmer
12214 Lakewood Blvd
Downey CA 92104

Rockwell Space Ops Co
Attn AFMC SSSG DET2/NOSO/Rockwell
R Smetek
Attn B Carlson
442 Discoverer Ave Ste 38
Falcon AFB CO 80912-4438

Rockwell Space Systems Div
Attn Mailcode 841-DA49 D McMurray
12214 Lakewood Blvd
Downey CA 90241

SRI
Attn M/S BS378 M Moeglein
333 Ravenswood Ave
Menlo Park CA 94025

Stanford Telecom
Attn B F Smith
1221 Crossman Ave
Sunnyvale CA 94088

Surveying Div
Attn CETEC-TD-GS D C Oimoen
7701 Telegraph Rd
Alexandria VA 22315-3864

Trimble Nav
Attn P Turney
585 N Mary
Sunnyvale CA 94086

US Army Rsrch Lab
Attn AMSRL-CI-LL Techl Lib (3 copies)
Attn AMSRL-CS-AL-TA Mail & Records
Mgmt
Attn AMSRL-CS-EA-TP Techl Pub (3 copies)
Attn AMSRL-DD J Rocchio
Attn AMSRL-SE-EM D Wortman
Attn AMSRL-SE-EM G Simonis
Attn AMSRL-SE-EM J Bruno
Attn AMSRL-SE-EM T B Bahder (12 copies)
Attn AMSRL-SE-EM T Van Flandern
(150 copies)
Attn AMSRL-SE-SA J Eicke
2800 Powder Mill Road
Adelphi MD 20783-1197

REPORT DOCUMENTATION PAGE			<i>Form Approved</i> <i>OMB No. 0704-0188</i>	
Public reporting burden for this collection of information is estimated to average 1 hour per response, including the time for reviewing instructions, searching existing data sources, gathering and maintaining the data needed, and completing and reviewing the collection of information. Send comments regarding this burden estimate or any other aspect of this collection of information, including suggestions for reducing this burden, to Washington Headquarters Services, Directorate for Information Operations and Reports, 1215 Jefferson Davis Highway, Suite 1204, Arlington, VA 22202-4302, and to the Office of Management and Budget, Paperwork Reduction Project (0704-0188), Washington, DC 20503.				
1. AGENCY USE ONLY (Leave blank)		2. REPORT DATE July 1998	3. REPORT TYPE AND DATES COVERED Summary, October 1997 to June 1998	
4. TITLE AND SUBTITLE Performance of the Miniature Airborne GPS Receiver			5. FUNDING NUMBERS DA PR: AH47 PE: 61102A	
6. AUTHOR(S) Tom Van Flandern and Thomas B. Bahder				
7. PERFORMING ORGANIZATION NAME(S) AND ADDRESS(ES) U.S. Army Research Laboratory AMSRL-SE-EM (e-mail tvf@arl.mil) 2800 Powder Mill Road Adelphi, MD 20783-1197			8. PERFORMING ORGANIZATION REPORT NUMBER ARL-TR-1739	
9. SPONSORING/MONITORING AGENCY NAME(S) AND ADDRESS(ES) U.S. Army Research Laboratory 2800 Powder Mill Road Adelphi, MD 20783-1197			10. SPONSORING/MONITORING AGENCY REPORT NUMBER US Army Aviation & Missile Command Attn AMSAM-RD Redstone Arsenal, AL 35898-5240	
11. SUPPLEMENTARY NOTES AMS code: 611102.AH47 ARL PR: 8NENFF				
12a. DISTRIBUTION/AVAILABILITY STATEMENT Approved for public release; distribution unlimited.			12b. DISTRIBUTION CODE	
13. ABSTRACT (Maximum 200 words) <p>At a fixed, well-surveyed location, position determinations from a MAGR (Miniaturized Airborne Global Positioning System Receiver) averaged over a six-week period were correct to within 0.5 m. However, the standard deviation of an individual position determination was 56 m. Almost 20 percent of the individual position determinations had errors exceeding 20 m. One in every 300 position determinations had an error exceeding 0.5 km. This anomalously large error distribution tail raises questions about the MAGR's suitability for some Army-critical functions, such as precision guidance.</p>				
14. SUBJECT TERMS GPS, MAGR, precision guidance, time transfer			15. NUMBER OF PAGES 22	
			16. PRICE CODE	
17. SECURITY CLASSIFICATION OF REPORT Unclassified	18. SECURITY CLASSIFICATION OF THIS PAGE Unclassified	19. SECURITY CLASSIFICATION OF ABSTRACT Unclassified	20. LIMITATION OF ABSTRACT UL	