FLOW CONTROL FINAL TECHNICAL REPORT

Period Covered by This Report: 10/1/92-12/21/94



AVNER FRIEDMAN

December 21, 1994

OFFICE OF NAVAL RESEARCH

Grant N00014-93-1-0027

This document has been appeared for public talease and rais; its distribution is unlimited

INSTITUTE FOR MATHEMATICS AND ITS APPLICATIONS

514 Vincent Hall University of Minnesota Minneapolis, Minnesota 55455



19941227 008

TABLE OF CONTENTS

1.	Description of workshop	3
2.	Comments by the organizer	3
3.	Table of Contents for the IMA Volumes in Mathematics and its Applications # 68: Flow Control. Editor: Max D. Gunzburger	4
4.	Manuscript Published in the IMA Preprint Series	6
5.	IMA Newsletter # 198	8

Acces	ion For					
Direc Unan	CRASE TAS rotneed cation	Ŋ				
By Distribution (Availanting Course						
A-1						

1. Description of Workshop (Flow Control)

The grant from the Office of Naval Research N00014-93-1-0027 supported the research in Flow Control, part of the IMA 1992-93 program CONTROL THEORY AND ITS APPLICATIONS. Specifically, the grant partially supported the postdocs Ruben Spies and Jean-Francois Collet, who worked in areas related to flow control, and 3 one-month visitors and 7 workshop participants who were in residence at the IMA during fall 1992 and participated in the Period of Concentration on Flow Control (November 16-20, 1992), organized by Max D. Gunzburger.

Majority of the flow control participants were mathematicians involved in the analysis, approximation, and computation of flow control and optimization problems. A small number of engineers were invited and they addressed application issues. The objective of the workshop on Flow Control was to bring together the ever growing community of mathematicians who are addressing these problems by sophisticated numerical and analytical techniques. They used a variety of mathematical tools and the workshop provided them an opportunity for an exchange and comparison of the different approaches. The second objective met by the workshop was to identify some of the important problems, from the point of view of applications, that need to be addressed by mathematicians, including specific flow control and optimization problems of interest to engineers.

2. Comments by the Organizer - Max D. Gunzburger

The following comments appear in the introduction of the IMA volume 68 which contains the proceedings of the Period of Concentration in Flow Control held at the IMA in November, 1992.

The gathering of engineers and mathematicians was especially timely as it coincided with the emergence of the role of mathematics and systematic engineering analysis in flow control and optimization. Since this meeting, this role has significantly expanded to the point where now sophisticated mathematical and computational tools are being increasingly applied to the control and optimization of fluid flows. Thus, these proceedings serve as a valuable record of some important work that has gone on to influence the practical, everyday design of flows. Moreover, they also represent very nearly the state of the art in the formulation, analysis, and computation of flow control problems.

My own article in the proceedings "A prehistory of flow control and optimization" attempts to set the stage for the remaining articles by describing the history of attempts at flow control and optimization and explaining why the time is ripe for the introduction of sophisticated tools from the theory of partial differential equations, from optimization theory, and from computational fluid dynamics into the study of flow control. The remaining articles in the volume show how these tools may be introduced to attack flow control problems. Mathematical issues in optimal control, feedback control, and controllability of fluid

flows are treated in the articles by E. Casas, A. Fursikov and O. Imanuvilov, K. Ito, H. Tran and J. Scroggs, S. Sritharan, S. Stojanovic, T. Svobodny, and R. Temam. Computational studies of algorithms and of particular applications are found in the articles by H. Banks and R. Smith, J. Borggaard, J. Borggaard and J. Burns, J. Brock and W. Ng, J. Burkardt and J. Peterson, Y.-R. Ou, G. Strumulo, and A. Taylor, P. Newman, G. Hou, and H. Jones. Among the applications considered in this volume are acoustics, compressible flows and incompressible flows, chemical vapor deposition, turbulent flows, and flows with shock waves.

I would like to express my sincere thanks to all of the participants in the Period of Concentration, and especially to the speakers and those who contributed to these proceedings. Thanks are also due to the staff of the IMA for their help in the production of these proceedings. Of special note in this regard are Patricia V. Brick, Stephan J. Skogerboe and Kaye Smith. Finally, I would like to acknowledge the hospitality and help extended to me and the other participants by Avner Friedman and Willard Miller, Jr.. Without them, neither the Period of Concentration in Flow Control nor this volume would have been possible.

3. Table of Contents of the IMA Volumes in Mathematics and its Applications #68 Flow Control edited by Max D. Gunzburger. This Proceeding is scheduled to be released by the publisher, Springer-Verlag in early spring 1995.

Foreword	xi
Preface	xiii
Active control of acoustic pressure fields using smart material technologies	. 1
On the presence of shocks in domain optimization of Euler Flows	35
A sensitivity equation approach to shape optimization in fluid flows	49
Quasi-analytical shape modification for neighboring steady-state Euler solutions	79

Control of steady incompressible 2D channel flow	111
Optimality conditions for some control problems of turbulent flows Eduardo Casas	127
On controllability of certain systems simulating a fluid flow	149
A prehistory of flow control and optimization	185
Mathematical issues in optimal design of a vapor transport reactor	197
Mathematical modeling and numerical simulation in external flow control Yuh-Roung Ou	219
Optimal feedback control of hydrodynamics: a progress report	257
Nonsmooth analysis and free boundary problems for potential and Stokes Flow	275
Computational fluid dynamics analysis of the flow in an APCVD applicator system	297
Shape optimization and control of separating flow in hydrodynamics Thomas Svobodny	325
Recent advances in steady compressible aerodynamic sensitivity analysis	341
Remarks on the control of turbulent flows	357

4. Manuscript Published in the IMA Preprint Series

- 1106 John A. Burns and Ruben D. Spies, A numerical study of parameter sensitivities in Landau-Ginzburg models of phase transitions in shape memory alloys
- 1095 H.O. Fattorini and S.S. Sritharan, Optimal chattering controls for viscous flow
- 1086 Irena Lasiecka and Mary Ann Horn, Global stabilization of a dynamic von Kármán plate with nonlinear boundary feedback
- 1151 Irena Lasiecka, Angelo Favini and, Mary Ann Horn, Global existence and uniqueness of regular solutions to the dynamic von Kármán system with nonlinear boundary dissipation
- 1168 Irena Lasiecka, Angelo Favini, Mary Ann Horn & Daniel Tataru, Global existence, uniqueness and regularity of solutions to a Von Kármán system with nonlinear boundary dissipation
- 1067 Jean-Pierre Puel, Caroline Fabre, and Enrike Zuazua, Approximate controllability of the semilinear heat equation
- 1093 Jean-Pierre Puel, Caroline Fabre & Enrique Zuazua, On the density of the range of the semigroup for semilinear heat equations
- 1054 Ruben D. Spies, A state-space approach to a one-dimensional mathematical model for the dynamics of phase transitions in pseudoelastic materials
- 1106 Ruben D. Spies and John A. Burns, A numerical study of parameter sensitivities in Landau-Ginzburg models of phase transitions in shape memory alloys
- 1166 Ruben D. Spies, Local existence and regularity of solutions for a mathematical model of thermomechanical phase transitions in shape memory materials with Landau-Ginzburg free energy
- 1095 S.S. Sritharan and H.O. Fattorini, Optimal chattering controls for viscous flow
- 1113 Thomas Svobodny and Srdjan Stojanovic, A free boundary problem for the Stokes equation via nonsmooth analysis
- 1130 Janos Turi, I. Györi, and F. Hartung, Approximation of functional differential equations with time- and state-dependent delays by equations with piecewise constant arguments

- 1131 Janos Turi, I. Györi and, F. Hartung, Stability in delay equations with perturbed time lags
- 1132 Janos Turi and F. Hartung, On the asymptotic behavior of the solutions of a state-dependent delay equation, IMA Preprint Series # 1132

INSTITUTE FOR MATHEMATICS AND ITS APPLICATIO

University of Minnesota

514 Vincent Hall 206 Church Street S.E. Minneapolis, Minnesota 55455

FAX (612) 626-7370

telephone (612) 624-6066

IMA schedules on Usenet: umn.math.dept

e-mail: ima_staff@ima.umn.edu

IMA schedules via finger: finger seminar@ima.umn.edu

TEX files of Newsletters, Updates and preprints via anonymous ftp: ima.umn.edu

IMA NEWSLETTER #198

November 1 - November 30, 1992

1992-93 Program
CONTROL THEORY AND ITS APPLICATIONS

NEWS AND NOTES

IMA Period of Concentration: FLOW CONTROL

November 16 - 20, 1992 Organizer: M. Gunzburger

Historically, flow control problems have been addressed through experimental investigations. Analytic and computational research had been based on drastically simplified flow models. However, recently, a number of mathematicians and other scientists have been addressing flow control problems without invoking such simplifications. There is little doubt that research in flow control will have significant impact on applications.

The ability to control fluid flows is crucial to the design and performance of processes in a wide variety of technological applications. For example, controls can be utilized in order to minimize drag, maximize lift, avoid high temperatures, enhance or deter mixing, delay or accelerate separation, increase mass flow rates, reduce structural vibrations in problems arising in airplane design and performance, in efficient chemical vapor deposition processes, in novel ship and submarine propulsion systems, in various components of chemical and petroleum plants, and in the design of efficient automobile engines and shapes.

Historically, flow control problems have been addressed through experimental investigations. Analytic and computational research had been based on drastically simplified flow models. However, recently, a number of mathematicians and other scientists have been addressing flow control problems without invoking such simplifications. There is little doubt that research in flow control will have significant impact on applications.

PARTICIPATING INSTITUTIONS: Consiglio Nazionale delle Ricerche, Georgia Institute of Technology, Indiana University, Iowa State University, Kent State University, Michigan State University, Northern Illinois University, Northwestern University, Ohio State University, Pennsylvania State University, Purdue University, University of Chicago, University of Cincinnati, University of Houston, University of Illinois (Chicago), University of Illinois (Urbana), University of Iowa, University of Kentucky, University of Manitoba, University of Maryland, University of Michigan, University of Michigan, University of Participating Corporations: Bellcore, Cray Research, Eastman Kodak, Ford, General Motors, Hitachi, Honeywell, IBM, Kao, Motorola, Paramax, Siemens, 3M

The mathematics of flow control involves a wide variety of skills and expertise. Traditional and novel techniques of optimization and the calculus of variations, set in the environment of modern theories for partial differential equations, are used to determine and analyze mathematical models that serve to determine the optimal states and controls. In particular, the great body of work on the Navier-Stokes equations provide a starting point for the analysis of flow control problems. The study of discretization algorithms, such as those based on finite element methods, and of techniques for the solution of the formidable nonlinear system of the discrete equations that result from discretization, also requires novel approaches.

Monday, November 16

Unless otherwise stated, the talks today are in Conference Hall EE/CS 3-180

9:00 am Registration and coffee

Reception Room EE/CS 3-176

9:30 am Welco

Welcome and Orientation

Conference Hall EE/CS 3-180

9:40 am

Max Gunzburger Virginia Tech

Flow control and optimization: An introduction

Abstract: We give a very unscientific survey of flow control and optimization problems and some of their history. We discuss various approaches for the modeling, analysis, and numerical approximation of such problems and we touch on the role that mathematics can play in future developments in the field.

.0:40 am

Coffee Break

Reception Room EE/CS 3-176

11:00 am

A. V. Fursikov Moscow University

On approximate controllability of the Stokes system

Abstract: The problem of approximate controllability of the nonstationary Stokes system in a bounded domain G is investigated in case the density of external forces concentrated in an arbitrary subdomain of the domain G is a control. The approximate controllability takes place in the class of square integrable functions and it does not exist in the class of sufficiently smooth functions. The Burgers equation and semilinear parabolic equations are not approximately controlled with respect to the right-hand-sides concentrated in the subdomain.

2:00 pm

Ralph Jones, III

To be announced

Sverdrup Technology, Inc.

3:00 pm

Contributed Talks/Discussion

This session will be organized after the workshop gets underway

4:00 pm

Vincent Hall 502

IMA Tea (and more!)

(The IMA Lounge)

A variety of appetizers and beverages will be served.

Tuesday, November 17

Unless otherwise stated, the talks today are in Conference Hall EE/CS 3-180

9:30 am

John A. Burns Virginia Tech Optimal control and design of fluid/structure

interactions

Abstract: In this paper we discuss several computational issues that arise in optimal control problems for hybrid systems of partial differential equations. These problems are motivated by applications to shape optimization and to optimal control of dynamical systems that arise when fluids and structures interact. We first describe an optimal design problem related to the design of optimal forebodies for the free-jet test facility currently under development at the Arnold Engineering Development Center. This problem is used to illustrate some of the basic ideas. We also discuss a simple feedback control problem with unbounded input and output operators. This model problem is discussed in detail and used to motivate possible practical approaches to more complex fluid flow control problems. Numerical results will be presented to illustrate these ideas.

10:30 am

Coffee Break

Reception Room EE/CS 3-176

11:00 am

Srdjan Stojanovic University of Cincinnati/IMA Nonsmooth analysis and shape optimization in flow problems

Abstract: Shape optimization (i.e., free boundary problem) for potential and for Stokes flow is considered. The problem is to determine the shape of the boundary for which fluid produces the specified force field on that portion of the boundary. New approach is introduced. The variable domain problem is relaxed so that it becomes a nonsmooth optimization problem on the fixed domain for the somewhat singular state equation. State equation is considered, and the multivalued generalized gradient of the variational functional is studied. The method is constructive.

1:30 pm

Arthur C. Taylor III Old Dominion University

Recent advances in aerodynamic sensitivity analysis

Abstract: Recent advances in the development of a systematic methodology for calculating consistent discrete aerodynamic sensitivity derivatives are discussed, where these derivatives are obtained from large-scale

software which numerically solves the multidimensional Euler and Navier-Stokes equations. Special emphasis is placed on solving the large coupled systems of ill-conditioned linear equations which must be solved in accomplishing this task. Subsequent use of these aerodynamic sensitivity derivatives for approximate analysis and for design optimization is discussed and demonstrated. Finally a proposed new strategy for Simultaneous Aerodynamic Analysis and Design Optimization (SAADO) is presented.

Joint work with Gene W. Hou.

2:30 pm

Coffee Break

Reception Room EE/CS 3-176

3:00 pm

L. Steven Hou

Simon Fraser University

Optimal control for some nonlinear P.D.E.s

Abstract: We present a mathematical framework for the mathematical and numerical analysis of optimal control problems associated with nonlinear equations. In particular we study optimal control problems for the stationary Navier-Stokes equations. We establish optimality systems of equations, and analyze finite dimensional approximations of their solutions. Some numerical results will be demonstrated. Most of the results presented here are joint work with M. Gunzburger and T. Svobodny.

Wednesday, November 18

Unless otherwise stated, the talks today are in Conference Hall EE/CS 3-180

9:30 am

Gary S. Strumulo Ford Motor Company CFD analysis of and APCVD applicator for thin

film deposition on glass surfaces

Abstract: Ford Glass R&D is developing several new coatings on glass products such as car windshields and sidelights and architectural glass. These coatings will be deposited by Atmospheric Pressure Chemical Vapor Deposition (APCVD). The vapor will be applied to the glass as it is formed at around 600° C in the molten tin bath by a series of applicators each consisting of a gas feed system and two exhaust manifolds. The glass moves under the applicators at 400 inches per minute and each coated layer is a few hundred angstroms thick.

We've observed a number of problems in applying this technology successfully to produce high quality products. These have stemmed from issues related to exhaust efficiency, temperature gradients, stagnation regions where particulates can form, and a "memory" of how the gas was injected. This latter issue can cause a nonuniformity in the coating across the glass that is dramatically evident by discoloration.

We solved the Navier-Stokes equations numerically both to determine if these problems could be predicted, and to redesign the applicators to help alleviate them. We modified the gas feed system and thermal gradients and observed their effect on the flow near the glass surface.

10:30 am

Coffee Break

Reception Room EE/CS 3-176

On the control of turbulence

Roger Temam 11:00 am Indiana University

Abstract: Our aim in this lecture is to study some problems of control of turbulence. Two cases are considered. In one case the system is governed by the Navier-Stokes equations and we want to minimize turbulence measured by the L2-norm of the curl vector. Existence of optimal control, necessary optimality conditions and numerical algorithms are presented. In the second case we consider the analogous problem related to the Burgers equations. In this case a different algorithm is presented and has been effectively implemented. Important reduction of drag is observed.

2:00 pm Yuh-Roung Ou Virginia Tech

Computational study of flow control problems for a rotating cylinder

Abstract: Flow control is a critical issue in the advanced design of aero/hydro-maneuvering vehicles which may provide the real-time effect for important applications, such as highly instantaneous maneuvers for the super-maneuverable aircraft, and optimum design of aerodynamic configurations. This talk presents research on active control of viscous flow around a rotating cylinder. By treating the rotation rate as a control variable in this model, various problems associated with the development of the alternate shedding of vortices and the induced body forces on the cylinder are studied numerically. The numerical results of lift, drag and lift/drag ratio respond to a variety of time-dependent rotation rates will be discussed. Several optimal control problems of maximizing the lift-to-drag ratio are then described. Very precise periodicity of the force evolutions at certain cases are established, and it may provide direct implication of controlling the vortex formation in the cylinder wake. Other issues addressed include the possibility of suppressing vortex shedding by using active control of the rotation rate, and the mathematical formulation of an optimal control problem associated with the rotating cylinder.

Thursday, November 19

Unless otherwise stated, the talks today are in Conference Hall EE/CS 3-180

9:30 am Kazufumi Ito

Optimal design of chemical vapor deposition reactors

North Carolina State University

Abstract: Chemical Vapor Deposition (CVD) is a process that uses chemically reacting vapors to deposit a thin solid film. The transport processes in CVD are described by the gas dynamics, i.e. conservation of mass, momentum, energy and mass transfer equations. The objective of our study is to determine an optimal design of the reactor chamber in order to increase purity and uniformity of the deposition layers.

10:30 am Coffee Break

Reception Room EE/CS 3-176

11:00 am

Eduardo Casas Universidad de Cantabria/IMA

Some optimal control problems of multistate equations appearing in fluid mechanics

Abstract: This talk deals with optimal control problems associated to the Navier-Stokes equations. The state of the system is the velocity of the fluid and the controls are the body forces or the heat flux on the boundary, in this last case the Navier-Stokes equations are coupled with the heat equation. We will consider three-dimensional flows, therefore the state equations are ill-posed in the sense that the relation between the control and the state is multivalued and consequently the derivation of the optimality conditions is not obvious. To overcome this difficulty we introduce an approximate family of optimal control problems governed by well posed differential equations, we obtain the optimality conditions for these problems and

1:30 pm Thomas P. Svobodny Wright State University

Hybrid control techniques in hydrodynamics

Abstract: We investigate the mathematical control theory of some practical engineering problems involving incompressible flow. Specifically, we deal with specifying boundary conditions and controlling separating flow in exterior flows about lifting bodies and interior and exterior flows of electrically conducting liquids. We use as control the boundary velocity and/or the geometric shape of the boundary. Hybrid control means choosing these controls simultaneously in an optimal way.

2:30 pm Coffee Break

Reception Room EE/CS 3-176

Friday, November 20

Unless otherwise stated, the talks today are in Conference Hall EE/CS 3-180

9:30 am S. S. Sritharan UCLA/NCC OSC

Optimal feedback control of hydrodynamics: A progress report

Abstract: The progress made on the optimal feedback control theory of viscous incompressible flows covering practically important cases such as wind tunnel flow and exterior hydrodynamics will be discussed. Main results are

(1) Existence theory: Ordinary controls as well as Young measure-valued chattering controls.

(2) Pontryagin maximum principle: Using viscosity solution method as well as using Ekeland's variational principle for problems with target constraint.

(3) Dynamic programming: Analysis of the infinite dimensional Hamilton-Jacobi-Bellman equation and the feedback synthesis.

Current ventures include

(1) Optimal Control theory of Combustion.

(2) Optimal control of ergodic properties of turbulent flow using statistical theory of Navier-Stokes equations.

10:30 am Coffee Break

Reception Room EE/CS 3-176

11:00 am

J. S. Brock Virginia Tech The formulation of a quasi-analytical aerodynamic inverse design method

Abstract: Formulation of the quasi-analytical aerodynamic inverse design method will be presented. This is a new, direct-iterative inverse design method which couples an analysis problem with a design problem in an iterative fashion. The direct-iterative design method begins with an initial geometry and solution, and a target surface profile. The estimate of the new geometry is driven by the difference between the target surface profile and the current, calculated profile. The geometry modifications are obtained with the design portion of the algorithm and an analysis of the new geometry is repeated. The geometry is iteratively modified in this manner until the calculated and target surface profiles are closely matched. The design portion of the new method uses a truncated Taylor series expansion of the discrete residual which describes the governing equations. This provides a linear design problem (linear in the change in solution and geometry) for the nonlinear governing equations. This new linearized method causes the iterative nature of the algorithm. That is, all portions of the quasi-analytical design algorithm may utilize the Euler or Navier-Stokes equations in two or three dimensions. Therefore, the design portion or the algorithm is equally valid for subsonic, transonic, and supersonic flow regimes within viscous or inviscid flows. The quasi-analytical differentiation of the governing equations also ensures numerical consistency between analysis and design portions of the algorithm. This new method is applicable for finite difference or finite volume discretizations with either central-difference or upwind flux methods. Along with the formulation of the quasi-analytical inverse design method, results using this new method in a design-like environment will be presented.

2:00 pm Antony Jameson Princeton University

To be announced

CONFIRMED VISITORS: November 16 - 20 Period of Concentration: FLOW CONTROL

70	The some contraction. The W CONTROL	
Banks, H. Thomas Borggaard, Jeff Brock, Jerry Browning, William Burkardt, John Burns, John A. Fattorini, Hector O. Fursikov, A.V. Gunzburger, Max D. He. Feiyue Hou, Lisheng Ito, Kazufumi Jameson, Antony Kneile, Karl Kojima, Fumio Kunisch, Karl Lasiecka, Irena M. Ming, Wei Ou. Yuh-Roung Pucl. Jean-Pierre Schmidt, Georg Sritharan, S. Strumolo, Gary S. Svobodny, Thomas P. Taylor. Arthur Temam, Roger Turi. Janos	North Carolina State University VPI&SU Virginia Tech Applied Mathematics VPI&SU VPI and SU UCLA Moscow University VPI & SU University of Cincinnati Simon Fraser University North Carolina State University Princeton University Sverdrup Technology Osaka Institute of Technology TU Graz University of Virginia McGill University VPI&SU University d'Orleans McGill University UCLA/NCC OSC Ford Motor Company Wright State University Old Dominion University Indiana University University of Texas, Dallas	NOV 8 - NOV 19 NOV 15 - NOV 20 NOV 18 - NOV 22 NOV 15 - NOV 17 NOV 15 - NOV 20 NOV 15 - NOV 20 NOV 12 - NOV 21 NOV 8 - NOV 20 NOV 14 - NOV 20 NOV 14 - NOV 21 NOV 14 - NOV 21 NOV 15 - NOV 21 NOV 15 - NOV 20 NOV 15 - NOV 20 NOV 7 - NOV 21 NOV 7 - NOV 17 NOV 8 - NOV 20 NOV 14 - NOV 20 NOV 14 - NOV 20 NOV 15 - NOV 20 NOV 7 - NOV 17 NOV 8 - NOV 20 NOV 14 - NOV 20 NOV 14 - NOV 20 NOV 14 - NOV 20 NOV 15 - NOV 17 NOV 17 - NOV 17 NOV 17 - NOV 19 NOV 15 - NOV 20
Turner, James C. Jr.	University of Texas, Dallas	
Wei. Ming	Hampton University	NOV 15 - NOV 20
rren ming	McGill University	NOV 8 - NOV 20