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in partial fulfillment of the requirements for the
degree of
Master of Science

By
William P. Martin
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HYPERSONIC WAVERIDER CONFIGURATIONS
 FOR TRANS-ATMOSPHERIC VEHICLES
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I would like to dedicate this work to my family--especially my wife Kathleen. Her emotional support and continual confidence in me was the force which kept me going. Her love has made it all worthwhile.

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ABSTRACT

This thesis describes the development of a catalogue of waverider shapes generated from axisymmetric conical flow. A simple but reliable method of calculating the viscous drag is presented and over one-hundred configurations are shown with various aerodynamic and pertinent geometric design factors. All of the configurations presented are based on Mach number of 10 and Reynolds number (based on the length of the waverider) of 10^6 . However, the analysis presented here adapts itself to any Mach or Reynolds number. The lift-to-drag ratios presented range from 4.32 to 5.06 while the average skin friction coefficient ranged from 0.00176 to 0.00205. The volume to area ratio $V^{2/3}/S_p$ ranged from 0.224 to 0.153. *Kug...*

$$V^{2/3}/S(P)$$

→ Hypersonic waverider configurations,
Hypersonic missiles, Aircraft characteristics.
(Sonic)

Nomenclature

A_b/A_{bi}	ratio of base areas of an arbitrary waverider with the idealized cone derived waverider
b/l_w	aspect ratio, base of waverider divided by the length of waverider
C_D	drag coefficient
$\overline{C_{fc}}$	average skin friction coefficient for the compression surface
C_{fe}	skin friction coefficient based on conditions just outside the boundary layer
$\overline{C_{ff}}$	average skin friction coefficient for the freestream surface
C_{fe}	average skin friction coefficient for the compression surface
$\overline{C_{ft}}$	average total skin friction coefficient
C_{ftav}	same as $\overline{C_{ft}}$
k_w	thermal conductivity at the wall
l	length of basic cone
l_w	length of waverider
$(L/D)_{vis}$	viscous lift to drag ratio
M_e	Mach number just outside the boundary layer
M_∞	Mach number at infinity or freestream

	conditions
Pr	Prandtl number
q	dynamic pressure
q_w	heat flux at the wall
r	distance from the origin of axis to a point on the waverider surface
R_{cb}	distance from origin to an arbitrary point on the the compression surface projected to the base plane
R_{exe}	Reynolds number based on conditions just out-side the boundary layer
R_{exo}	Reynolds number based on freestream conditions
R_{ob}	distance from origin to an arbitrary point on the freestream surface projected to the base plane
S_p/S_{pi}	ratio of planform areas of waverider to the idealized waverider
S_w/S_p	ratio of wetted area to planform area
SSD	shock standoff distance in the base plane
S_I	Stanton number
S_{wc}	wetted area of compression surface
S_{wf}	wetted area of freestream surface
T_{aw}	adiabatic wall temperature
T_w	temperature at the wall

V/V_1	volume ratio of waverider to idealized wave- rider
$V^{2/3}/S_p$	nondimensionalized volume to planform area ratio
β	half angle of shock cone
δ	half angle of basic cone
$\delta(x)$	boundary layer thickness boundary layer thickness in the transformed coordinates
Φ	angle between $-\Phi_1$ and Φ_1
Φ_1	dihedral angle of waverider in the base plane
Φ_z	dihedral angle of waverider at an arbitrary crosssection
	ratio of specific heats
μ_e	viscosity coefficient just outside the boundary layer
μ_w	viscosity coefficient at the wall
σ	β/δ , radius of shock cone in the base plane of nondimensional coordinate system
σ_z	radius of shock cone at an arbitrary cross section of nondimensional coordinate system
τ_w	surface stresses at the wall

CHAPTER 1

Introduction

1.1 Introductory Remarks

Lifting-body configurations are currently of interest as a means for achieving long-range and high-performance hypersonic missile and aircraft characteristics. Semi-empirical methods used heretofore for calculating the flow fields and aerodynamics of blended wing-body shapes are not appropriate for modern hypersonic flight. Design requirements for hypersonic aircraft are discussed by Townend¹ and Stollery². Elaborate computer codes have become necessary for predicting the characteristics of arbitrary configurations. Since these codes are still in evolutionary stages and are quite expensive as well as complex, a need for a simplified calculation scheme exists.

Waverider analysis provides one means for studying blended body configurations on a relatively simplified scale. The work presented here is well adapted to the personal computer. Shapes derived by this analysis yield flow fields and aerodynamic properties that are known for their particular on-design conditions, and allow for systematic variation of parameters pertinent to the design process.

An historical background on waveriders is provided by Kuchemann³ and Hemsch and Nielsen⁴ offer additional perspectives. Also, in recent times there have been several papers dealing with geometry variations, optimization, viscous effects, experimental verification, and applications.⁵⁻¹⁵

1.2 Primary Goals

This study has two primary goals. The first is essentially an extension of the work by Rasmussen and Stevens¹⁴. In this sense, this work is a catalog of many shapes and variations of waveriders (over 100 are presented) that can be generated by axisymmetric flow past a cone. Lift, drag, and friction coefficients as well as lift-to-drag ratios are calculated together with pertinent design factors such as projected planform area, base area, wetted surface area, volume ratio, and aspect ratio.

The other goal of this study is the calculation of the viscous drag in a simple but reliable fashion. The viscous drag has been calculated previously by an average skin friction coefficient, such as outlined by reference 8, or by means of an elaborate integral boundary-layer method¹³. Here however, a new method is presented for laminar boundary layers that allows for variations in Mach number, Reynolds

numbers based on body length, and wall temperature conditions. The method involves simple quadratures associated with the wetted surface area of the waveriders.

It is hoped that we can present some configurations that heretofore were not envisaged using cone derived waveriders. None-the-less these perhaps unusual shapes still render flow fields that are known based on supersonic flow past a cone.

CHAPTER 2

Development of Waverider Shape

2.1 Introductory Remarks

We will start by defining a coordinate system and basic parameters. Then we will determine in a systematic way the waverider shape starting with the base plane view. Finally, we will present views at arbitrary cross sections and a view from overhead.

2.2 Coordinate System and Basic Definitions

To begin we will use the spherical coordinate system shown below in figure 2-1.

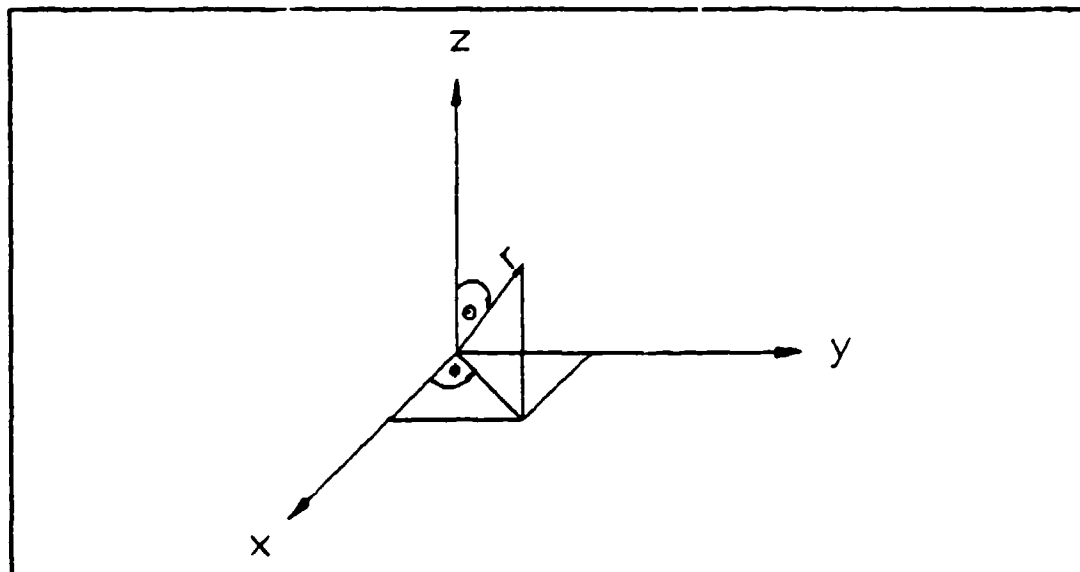


Figure 2-1 Spherical Coordinate System

This figure lends itself to the following set of basic equations.

$$x = r \sin \theta \cos \phi, \quad y = r \sin \theta \sin \phi, \quad z = r \cos \theta \quad (2-1)$$

We now wish to impose that θ be restricted to small angles and we reduce this set of equations to,

$$x = r \theta \cos \phi, \quad y = r \theta \sin \phi, \quad z = r \quad (2-2)$$

Next, we rotate the conventional spherical coordinate system and impose a cone symmetric about the z -axis with the vertex at the origin, and establish a free stream Mach number aligned with and pointing in the $+z$ direction. This creates a shock cone that is also symmetric about the z -axis. Figure 2-2 below shows this.

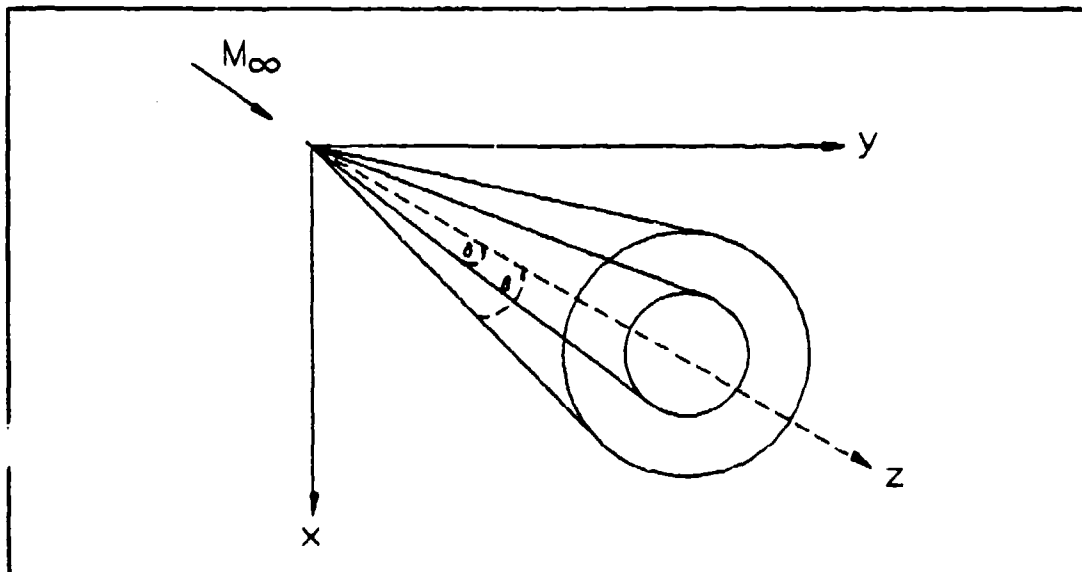


Figure 2-2 Basic Cone and Shock Cone

We now want to construct a non-conical body that will have a flow field that remains conical between the body compression surface and the shock surface. This is done using the procedure in reference 14.

To begin, we define the trailing edge of the free stream surface. In this thesis we will use a sixth-order polynomial to describe this line. Now, we trace undisturbed free streamlines (i.e., streamlines parallel to M_∞) upstream until we intersect the shock cone, thus describing the freestream surface. Next, we trace corresponding streamlines through the shock layer until we intersect the base plane of the cone, thus describing the compression surface of the waverider.

When we determine the streamlines in the compression surface that correspond to those in the freestream surface we require the aid of figure 2-3. Imagine that we pass a plane through the axis of the basic cone. This plane then identifies corresponding streamlines for the freestream and compression surfaces. For example, we may choose any point on the trailing edge of the freestream surface and pass a plane through the axis of the basic cone which also intersects this point. Now staying in the plane we trace upstream until we intersect the shock. Then we trace back a streamline that intersects the shock and stays in the plane until we get back to the base of the cone. Now if we sweep the plane from point

to point along the freestream surface we define the compression surface. Therefore, simply by describing the trailing edge of the freestream surface we have means to determine the entire shape of the waverider body.

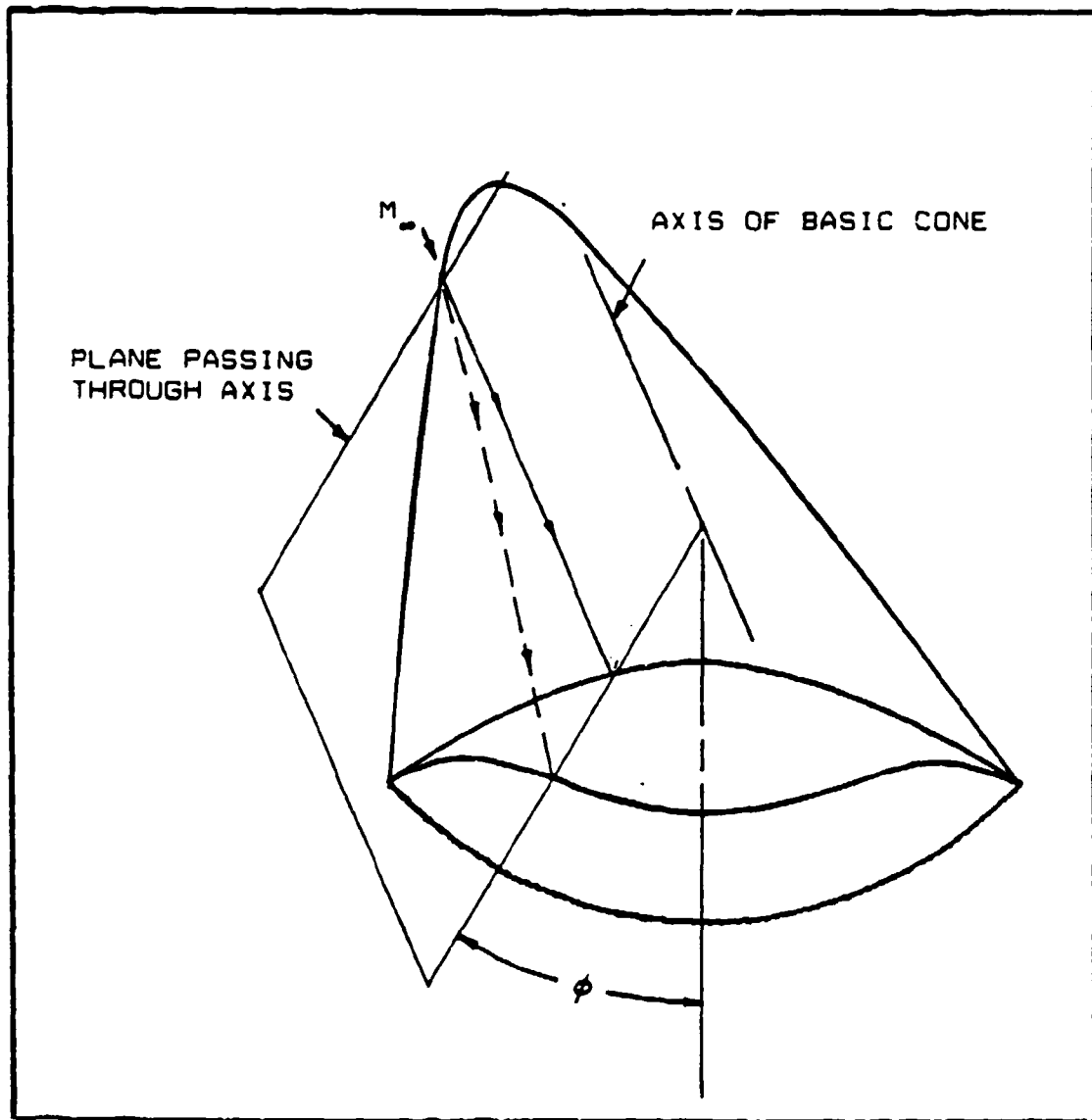


Figure 2-3

According to reference 14, the freestream and compression surfaces are described by

$$r\theta = r_s(\phi)\beta \quad (2-3)$$

$$r(\theta_c^2 - \delta^2)^{1/2} = r_s(\phi)(\beta^2 - \delta^2)^{1/2} \quad (2-4)$$

where r is a line from the origin of our coordinate system to any arbitrary point on the freestream or compression surface, θ is the angle between r and the axis of the cone (z-axis), and r_s is the line from the origin to the intersection of the compression and freestream surfaces. Also, β and δ are the half angles for the shock cone and the basic cone respectively. Figure 2-4 below shows a 2-D side view of these definitions.

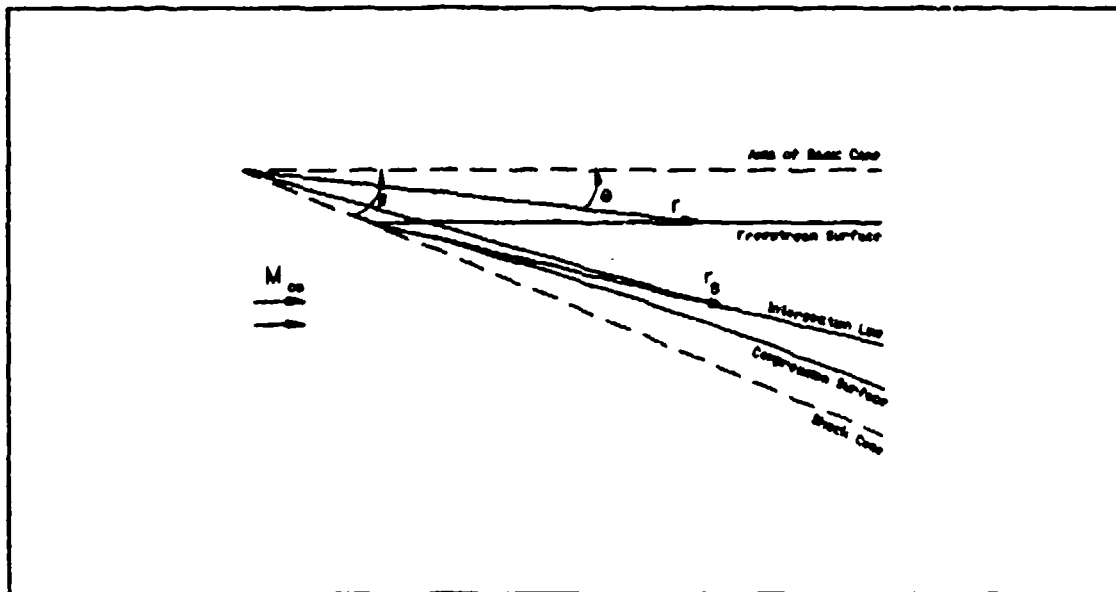


Figure 2-4 Two Dimensional Side View

2.3 The base plane view

We would like to represent the trailing edge of the free-stream surface by a 4-term, sixth-order polynomial like the following

$$x = A + By^2 + Cy^4 + Dy^6 \quad (2-5)$$

A representation of this form will allow us to be symmetric about a plane passing through the z-axis in the x-direction. Consider a base plane representation as is shown below in figure 2-5 along with the above equation (2-5).

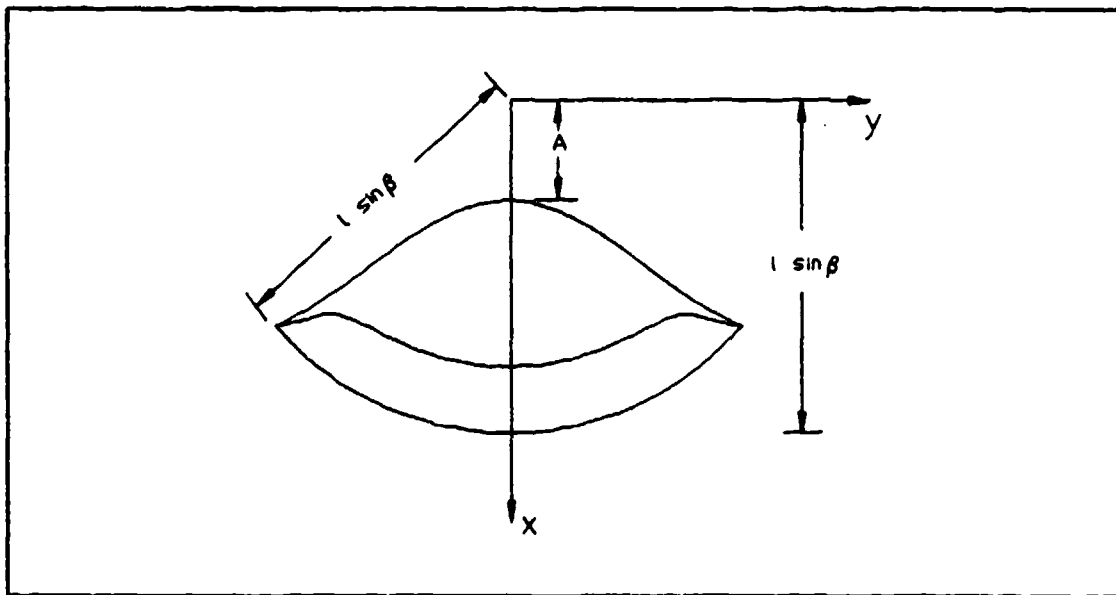


Figure 2-5 Baseplane Representation (dimensional)

We can see from equation (2-5) that,

$$x = A \text{ when } y = 0 \quad (2-6)$$

Also, considering figure 2-4 we have the distance from the origin to the shock as $l \sin \beta$. Note that this is also the distance from the origin to the intersection of the two

surfaces since the shock remains conical. This perhaps suggest that we normalize with $l \sin \beta$. However, considering the relationship between β and δ given in reference 14 as,

$$\sigma \approx \frac{\beta}{\delta} = \left[\frac{(\gamma+1)}{2} + \frac{1}{(M_\infty \delta)^2} \right]^{1/2} \quad (2-7)$$

we choose to normalize with $l \sin \delta$ or $l \delta$ since we have restricted ourselves to small angles. Dividing equation (2-5) by $l \delta$ yields

$$x/(l \delta) = A/(l \delta) + 1/(l \delta) [B y^2 + C y^4 + D y^6] \quad (2-8)$$

Now as a matter of convenience since B , C , and D are as yet arbitrary we will define them in the following way

$$B = b_2/(l \delta), \quad C = b_4/(l \delta)^3, \quad D = b_6/(l \delta)^5 \quad (2-9)$$

where b_2 , b_4 , and b_6 are yet to be described. Also, we will define $A/(l \delta)$ as a new parameter with the symbol R_0 . Doing this we rewrite equation (2-8) as,

$$X = R_0 + b_2 Y^2 + b_4 Y^4 + b_6 Y^6 \quad (2-10)$$

where,

$$X = x/(l \delta), \quad Y = y/(l \delta) \quad (2-11)$$

This normalized system renders the following new baseplane representation shown in figure 2-6. It is this new normalized system that we will use to develop a method of determining an infinite variety of waverider baseplane shapes.

This system allows the following conditions:

$$i) \quad X = R_0 \quad \text{when} \quad Y = 0$$

$$ii) \quad X = \sigma \cos \phi_1 \quad \text{when} \quad Y = \sigma \sin \phi_1$$

Additionally, we will require that the slope at the tip of the waverider be between zero and ϕ_1 . This helps to prevent double intersections with the compression surface. We will call this condition three.

$$iii) \quad 0 \leq dX/dY \leq \phi_1$$

The four terms of equation (2-11) are determined using these conditions. Substitute condition ii) into (2-11) to yield,

$$\sigma \cos \phi_1 = R_0 + b_2 \sigma^2 \sin^2 \phi_1 + b_4 \sigma^4 \sin^4 \phi_1 + b_6 \sigma^6 \sin^6 \phi_1 \quad (2-12)$$

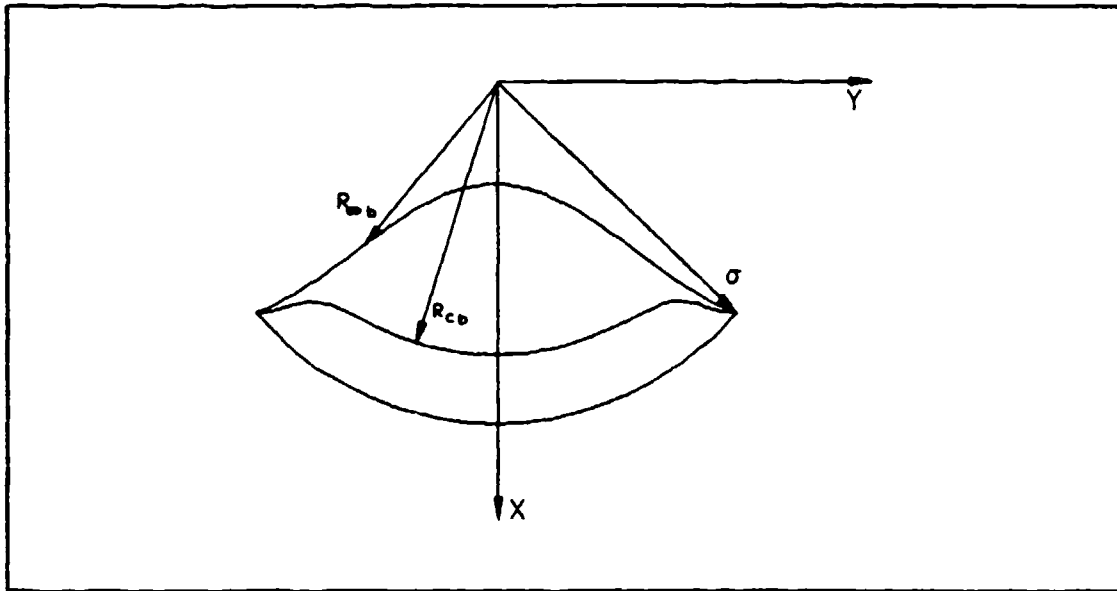


Figure 2-6 Baseplane Representation (non-dimensional)

We see that in order for (2-12) to hold we must choose R_0 , ϕ_1 , b_2 , b_4 , and b_6 accordingly. To do this we may choose any one variable to be dependent and let the others remain independent.

For example, choose b_2 to be the dependent variable. Solving equation (2-12) for b_2 yields,

$$b_2 = \frac{\sigma \cos \phi_1 - R_0 - b_4 \sigma^4 \sin^4 \phi_1 - b_6 \sigma^6 \sin^6 \phi_1}{\sigma^2 \sin^2 \phi_1} \quad (2-13)$$

We may therefore use (2-10) to describe a general waverider freestream edge providing we use (2-13) to determine b_2 once we have arbitrarily chosen R_0 , ϕ_1 , b_4 , and b_6 .

Additionally, we will restrict attention to the cases when condition (iii) holds as well. To see if (iii) holds we merely calculate $dX/dY = 2b_2Y + 4b_4Y^3 + 6b_6Y^5$ and see if the criterion is met.

We now have a means to make various freestream trailing edge shapes. Referring to the above coordinate system we see that the negative most value of Y is,

$$Y_{neg} = -\sigma \sin \phi_1 \quad (2-14)$$

and clearly the positive most value of Y is,

$$Y_{pos} = +\sigma \sin \phi_1 \quad (2-15)$$

All other values of Y must lie in between (2-14) and (2-15).

We therefore start at $Y = -\sigma \sin \phi_1$ and march away in

small increments until we reach $Y = +\sigma \sin \phi_1$. At each step along the way we stop and use (2-10) to determine X . We now have many X, Y data points available to plot the freestream edge. If the increments are significantly small we may use a straight line approximation in between data points.

The above is a procedure to determine the freestream edge in the base plane. We now develop the procedure to determine the compression surface. Recall figure 2-6. At each set of points X, Y we may calculate R_{ob} by using the Pythagorean theorem

$$R_{ob} = (X^2 + Y^2)^{1/2} \quad (2-16)$$

where R_{ob} is the distance from the origin of the base plane coordinate system too a point on the surface of the freestream edge in the base plane.

Now we must determine the compression surface that goes with a chosen freestream surface. This is accomplished in reference 14 and is given as

$$R_{cb} = [1 + (\sigma^2 - 1)R_{ob}^2/\sigma^2]^{1/2} \quad (2-17)$$

We will now define the X, Y data points for the compression surface as X_c and Y_c to prevent confusion. To determine the X_c, Y_c data points for the compression surface we use simple trigonometric relations,

$$X_c = R_{cb} \cos \phi, \quad Y_c = R_{cb} \sin \phi \quad (2-18)$$

But, $\cos \phi = X/R_{ob}$ and $\sin \phi = Y/R_{ob}$ and we rewrite (2-18) as

$$X_c = X(R_{cb}/R_{ob}), \quad Y_c = Y(R_{cb}/R_{ob}) \quad (2-19)$$

The above gives a systematic way to explore virtually an infinite number of waverider base plane shapes. All we need do is choose different variables subject to the given conditions and plot our picture.

We will now look at arbitrary crosssections of the waverider viewed from a base plane perspective.

2.4 Arbitrary Crosssectional Views

The freestream surface at any arbitrary cross section is still given by the general equation,

$$X = R_0 + b_2 Y^2 + b_4 Y^4 + b_6 Y^6 \quad (2-20)$$

however the range of Y is clearly not the same. Recall figure 2-3. From the figure we can see that ϕ_z is dependent on location along the Z axis. Note ϕ_z is the angle between the Z -axis and the outermost value of Y .

Now recall condition ii) given earlier. We can use the same condition at any arbitrary cross section simply by replacing ϕ_1 with ϕ_z and σ with σ_z . This gives,

$$X = \sigma_z \cos \phi_z \text{ when } Y = \sigma_z \sin \phi_z \quad (2-21)$$

substituting (2-21) into (2-20) gives,

$$\sigma_z \cos \phi_z = R_0 + b_2 \sigma_z^2 \sin^2 \phi_z + b_4 \sigma_z^4 \sin^4 \phi_z + b_6 \sigma_z^6 \sin^6 \phi_z \quad (2-22)$$

There are two unknowns in (2-22). They are σ_z and ϕ_z . Considering figure (2-7) below we can produce a relationship that will give us σ_z .

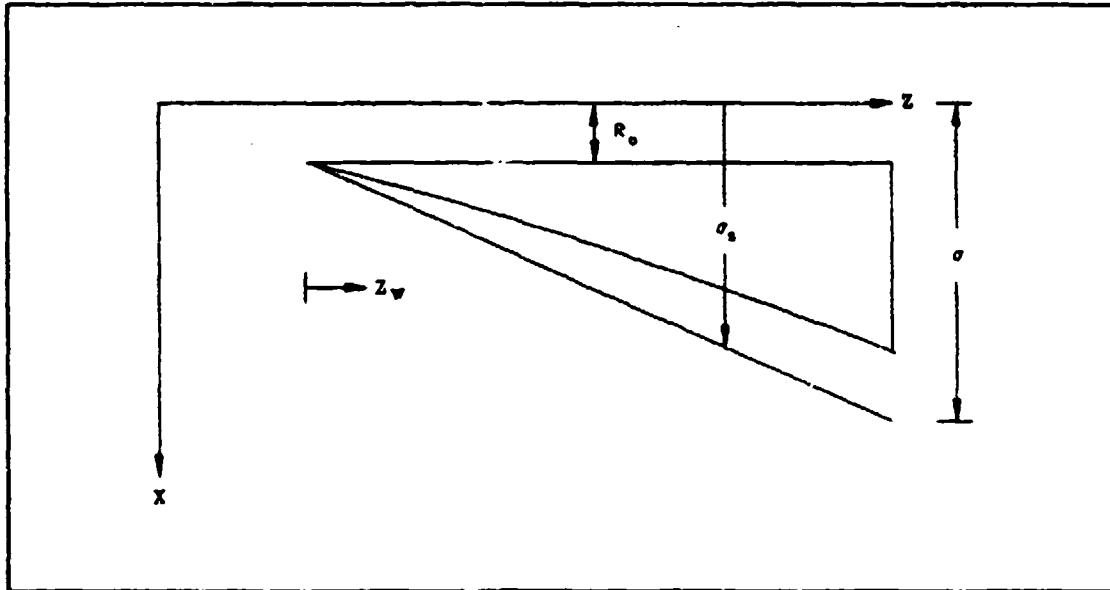


Figure 2-7 Side View (non-dimensional)

Recall that σ_1 is the distance from the Z axis to the line of intersection of the shock and waverider body (in the non-dimensional system). But, this is also the distance from the Z axis to the shock in the X-direction. Therefore simple triangle relations give us,

$$\sigma_1 = R_0 + Z_w/l_w(\sigma - R_0) \quad (2-23)$$

where Z_w/l_w is the percentage back from the leading edge. i.e., 0.1, 0.35 etc...

Now equation (2-23) gives us σ_1 , and then (2-22) will give us ϕ_1 . Due to the difficulty of solving (2-22) for ϕ_1 , we may use a numerical, instead of analytical approach to solving it. Once ϕ_1 and σ_1 are known the free stream edge is simply plotted as before by replacing σ and ϕ_1 by σ_1 and ϕ_1 in

equations (2-14) and (2-15). We may call these equations (2-14) and (2-15) modified.

We now proceed to determine the compression surface at an arbitrary cross section. Recall equation (2-4) describing the compression surface,

$$r^2(\theta_c^2 - \delta^2) = r_s^2(\Phi)(\beta^2 - \delta^2) \quad (2-24)$$

Dividing through by l^2 we obtain,

$$(r^2/l^2)(\theta_c^2 - \delta^2) = r_s^2(\Phi)/l^2(\beta^2 - \delta^2) \quad (2-25)$$

Now we define θ_{ob} as the angle between r and the Z -axis where r is a line from the origin to any point on the free-stream trailing edge in the base plane. With this definition then we can say that,

$$l\theta_{ob} = r_s\beta \quad (2-26)$$

where r_s is a line from the origin to the point of intersection of the two surfaces. Dividing through by δ we obtain,

$$l\theta_{ob}/\delta = r_s\beta/\delta = r_s\sigma \quad (2-27)$$

and solving for θ_{ob}/δ yields,

$$\theta_{ob}/\delta = r_s\sigma/l \quad (2-28)$$

Now θ_{ob}/δ is also equal to R_{ob} and we can write,

$$R_{ob} = r_s\sigma/l \quad (2-29)$$

or

$$r_s^2/l^2 = R_{ob}^2/\sigma^2 \quad (2-30)$$

Substituting (2-30) into (2-25) gives,

$$(r^2/l^2)(\theta_c^2 - \delta^2) = (R_{ob}^2/\sigma^2)(\beta^2 - \delta^2) \quad (2-31)$$

and dividing through by δ^2 yields,

$$r^2/l^2(\theta_c^2/\delta^2 - 1) = R_{ob}^2/\sigma^2(\beta^2/\delta^2 - 1) \quad (2-32)$$

Solving (2-32) for θ_c^2/δ^2 and replacing r with z yields,

$$\theta_c^2/\delta^2 = 1 + (l^2/z^2)[(\sigma^2 - 1)R_{ob}^2(\phi)/\sigma^2] \quad (2-33)$$

We note that $\theta_c^2/\delta^2 = R_{ob}^2$ and therefore (2-33) is remarkably close to equation (2-17) except for the factor l^2/z^2 .

Since we want to view the arbitrary cross section from a base plane perspective we want to project θ_c onto the base plane. Figure 2-8 below represents this.

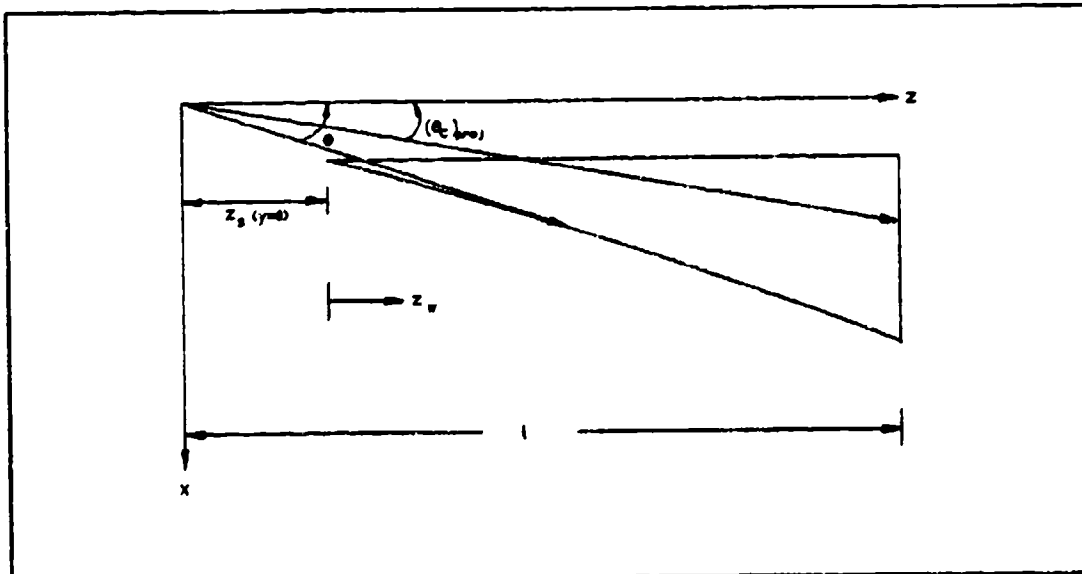


Figure 2-8 Side View Dimensional

We see that,

$$z\theta_c = l(\theta_c)_{proj} \quad (2-34)$$

or

$$(\theta_c)_{proj} = z\theta_c/l \quad (2-35)$$

Substituting (2-35) into (2-33) yields,

$$(R_{cb}^2)_{proj} = z^2/l^2 + (\sigma^2 - 1)R_{ob}^2(\Phi)/\sigma^2 \quad (2-36)$$

From the above figure we see that,

$$z_w = z - R_0 l/\sigma \quad (2-37)$$

and

$$l_w = l - R_0 l/\sigma = l(1 - R_0/\sigma) \quad (2-38)$$

Equation (2-38) lets us normalize (2-36) with l_w . Solving (2-38) for l and substituting into (2-37) we get after rearranging,

$$z_w/l_w = (z/l - R_0/\sigma)/(1 - R_0/\sigma) \quad (2-39)$$

We now solve (2-39) for z/l to yield,

$$z/l = (z_w/l_w)(1 - R_0/\sigma) + R_0/\sigma \quad (2-40)$$

Now substitute (2-40) into (2-36) to give the desired result,

$$(R_{cb}^2)_{proj} = (z_w/l_w(1 - R_0/\sigma) + R_0/\sigma)^2 + (\sigma^2 - 1)R_{ob}^2(\Phi)/\sigma^2 \quad (2-41)$$

We now determine X_c , Y_c data points to plot the arbitrary cross section compression surface. We recall equations (2-14) and (2-15) modified.

$$Y_{neg} = -\sigma_z \sin \Phi_z, \quad Y_{pos} = +\sigma_z \sin \Phi_z \quad (2-42)$$

Now start at Y_{neg} and march away in small increments until you reach Y_{pos} . At each step along the way stop and calculate X

according to equation (2-20) and R_{eb} according to equation (2-16). We can now determine $(R_{cb})_{proj}$ using (2-41). With $(R_{cb})_{proj}$ known we determine X_c , Y_c with the following simple trigonometric relations,

$$X_c = X(R_{cb})_{proj}/R_{eb} \quad (2-43)$$

$$Y_c = Y(R_{cb})_{proj}/R_{eb} \quad (2-44)$$

Note that equations (2-43) and (2-44) are similar to equations (2-19). Also in equation (2-41), z_w/l_w is an arbitrary input value depending on what cross section is being viewed. For example, if it is desired to view the cross-section at say 30% from the leading edge then $z_w/l_w = 0.30$.

We now have a systematic way to view the waverider shape at any arbitrary cross section from the leading edge to the base plane. Figure 2-9 below gives an example of the results using this procedure. The figure shows a base plane perspective of the waverider at 0.1 intervals from the leading edge.

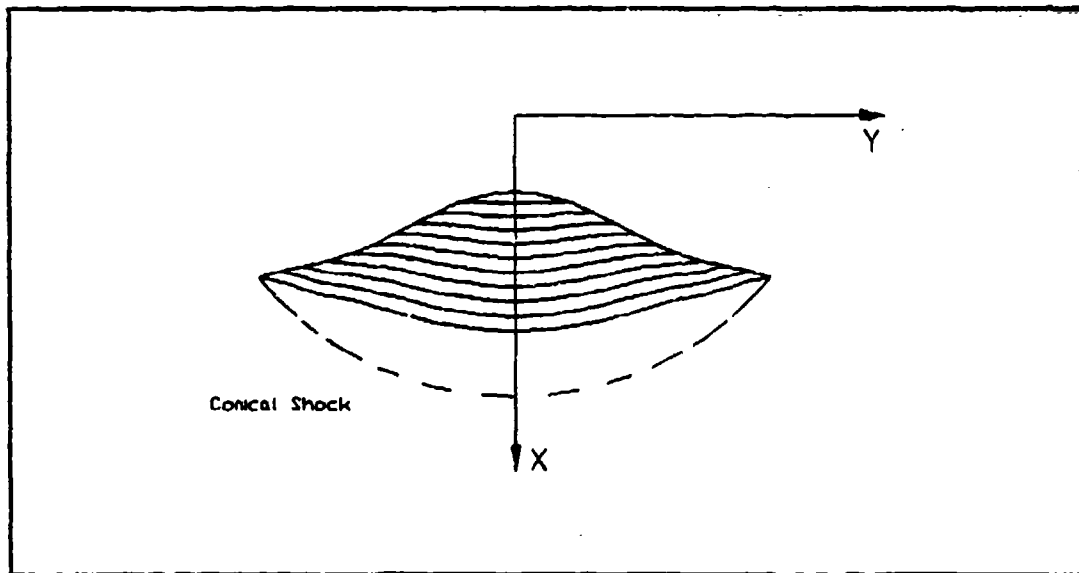


Figure 2-9 Baseplane Perspective of Arbitrary Crosssections

2.5 The Top (planform) View

To determine the planform view of the waverider we consider the following coordinate system. We note that along the freestream surface $r\theta$ is a constant, and if we project to the base plane we see that $r\theta = r_s\beta$. Therefore we have

$$r\theta = r_s\beta = \text{constant} \quad (2-45)$$

We now establish a relationship between l and l_w . We can see that from figure 2-10a,

$$l - l_w = z_s(y=0) \quad (2-46)$$

and from figure 2-10b, $\theta = \beta$ when r is drawn to the leading edge of the waverider where the shock intersects the body. Redrawing figure 2-10b we have

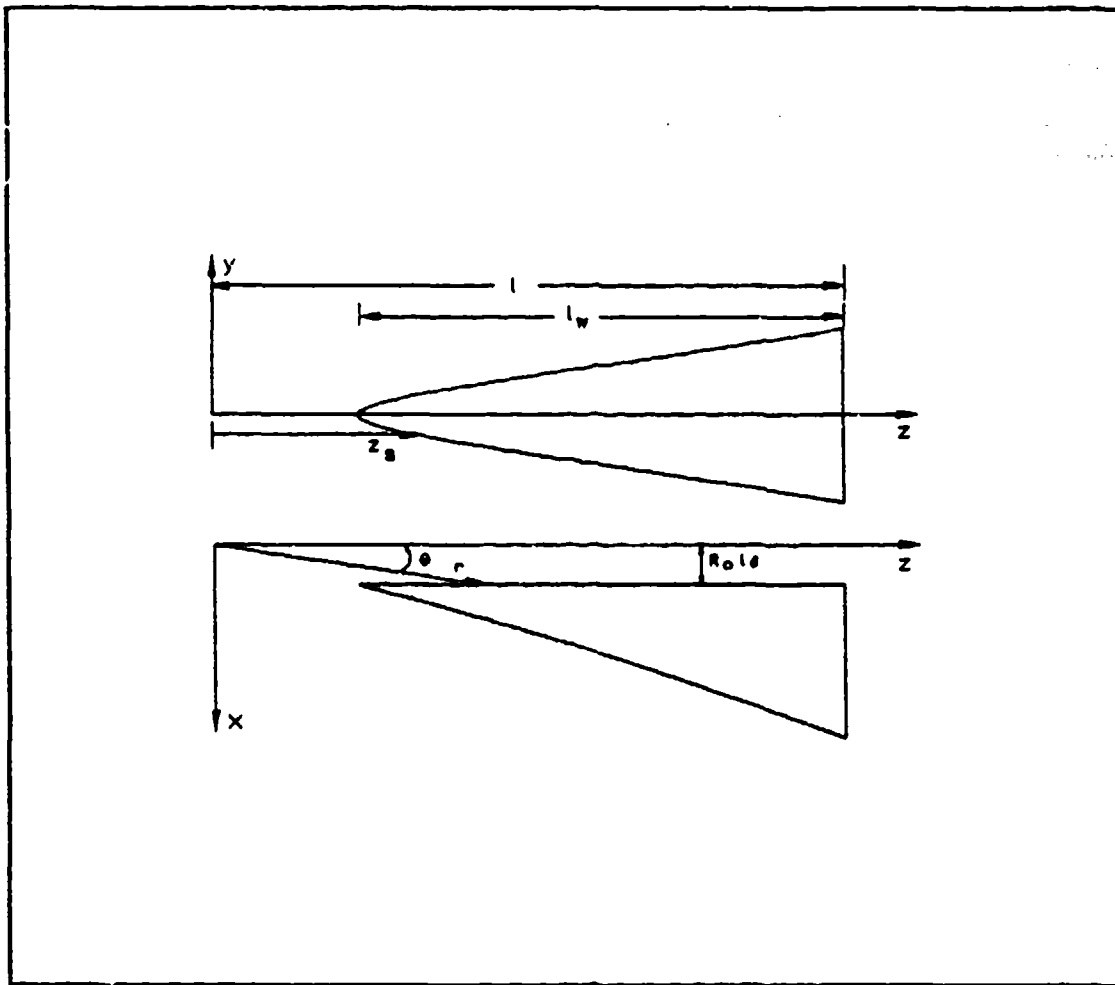


Figure 2-10 Planform and Side View Coordinate System (dimensional)

Now using basic trigonometry we see that,

$$z_s(y=0) = R_0 l \delta / \tan \beta \quad (2-47)$$

but using small angle approximations $\tan \beta = \beta$, therefore

$$z_s(y=0) = R_0 l \delta / \beta = R_0 l / \sigma \quad (2-48)$$

Substituting (2-48) into (2-46) we have

$$1 - l_w = R_0 l / \sigma$$

or

$$l_w = l(1 - R_0 l / \sigma) \quad (2-49)$$

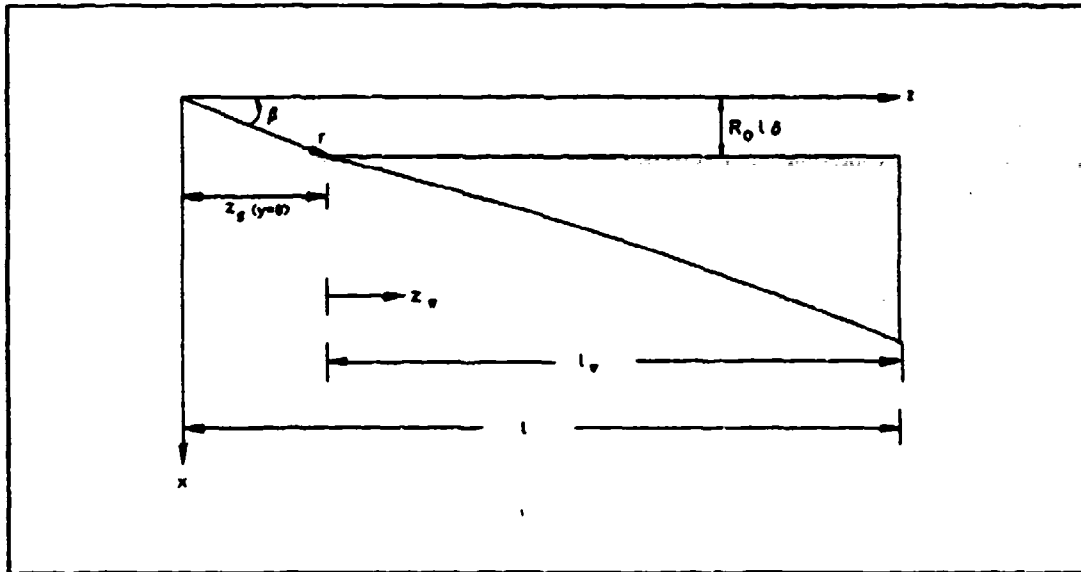


Figure 2-11 Side View (dimensional)

Equation (2-49) gives us a relationship between l and l_v .

Now at the base plane $r = 1$, therefore

$$l\theta_{ob} = r_s\beta = \text{constant}$$

Dividing through by δ and rearranging we obtain

$$\theta_{ob}/\delta = r_s\beta/(l\delta) = r_s\sigma/l \quad (2-50)$$

Recall that θ and r_s vary for a given shape and δ , β , and σ do not. Now $\theta_{ob}/\delta = R_{ob}(\phi)$ and this gives us

$$R_{ob}(\phi) = r_s\sigma/l \quad (2-51)$$

For small angles $r_s = z_s$ and we rewrite (2-51) as,

$$z_s/l = R_{ob}(\phi)/\sigma \quad (2-52)$$

Now recall from our spherical coordinate system that,

$$y = r\theta\sin\phi, \quad z = r \quad (2-53)$$

or

$$y = z\theta\sin\phi \quad (2-54)$$

Along the boundary (where the shock and body intersect) $\theta =$

β . Replacing z with r_s and dividing through by 1 we have,

$$y/l = r_s \beta \sin \phi / l \quad (2-55)$$

but $r_s/l = R_{\theta 0}(\phi)/\sigma$ from (2-52). Therefore substituting yields,

$$y/l = R_{\theta 0}(\phi) \delta \sin \phi \quad (2-56)$$

Equations (2-52) and (2-56) give us a way of drawing the planform view normalized with 1. However, it may be more convenient to normalize with l_w . Using (2-49) to accomplish this we have,

$$z_s/l_w = R_{\theta 0}(\phi)/(\sigma - R_0) \quad (2-57)$$

$$y_s/l_w = R_{\theta 0}(\phi) \delta \sin \phi / (1 - R_0/\sigma) \quad (2-58)$$

Equations (2-57) and (2-58) give us a method of plotting our waverider as viewed from the top normalized with l_w . The appendix of this thesis devotes much of its bulk to showing various planform and baseplane views of different waveriders determined by a choice of different parameters in equation (2-10).

2.6 Three Dimensional Views

Development of a three-dimensional view of an arbitrary waverider shape can be an extension of the arbitrary cross section and planform views presented earlier. Adams¹⁶ has developed a code using this analysis to present a 3-D view. Several views are presented in appendix H using this code.

CHAPTER 3

Surface Skin-Friction Coefficients

3.1 Introductory Remarks

In this chapter we wish to derive expressions for the average skin-friction coefficients for both the freestream and compression surfaces. Although these expressions will be approximate, they will reflect the proper trends for variations in Reynolds number, Mach number, and surface wall temperature. Since the pressure is constant on the freestream surface of the waverider and varies slowly along an inviscid streamline on the compression surface, we will assume that the friction coefficient can be modeled after a flat plate for the freestream surface and a wedge for the compression surface. In both cases, the pressure gradient along an inviscid surface streamline is zero. We shall use the momentum-integral formulation for compressible boundary layers.

3.2 Momentum-Integral Equation for Flat Plates and Wedges

The momentum-integral equation for zero pressure gradient is given by reference 18 as,

$$\frac{d\theta}{dx} = \frac{\tau_w}{\rho_e U_e^2} \quad (3-1)$$

Where θ is the compressible momentum thickness given by,

$$\theta = \int_0^{\delta} \frac{\rho}{\rho_e} \frac{U}{U_e} \left(1 - \frac{U}{U_e} \right) dy \quad (3-2)$$

and τ_w is the surface stress determined by,

$$\tau_w = \mu_w \left(\frac{\partial U}{\partial y} \right)_w \quad (3-3)$$

Here x and y are measured along and normal to the surface in the usual way, as shown in figure 3-1. The thickness of the boundary layer is denoted by $\delta = \delta(x)$. The subscripts e and w denote conditions at the outer edge of the boundary layer and at the wall surface.

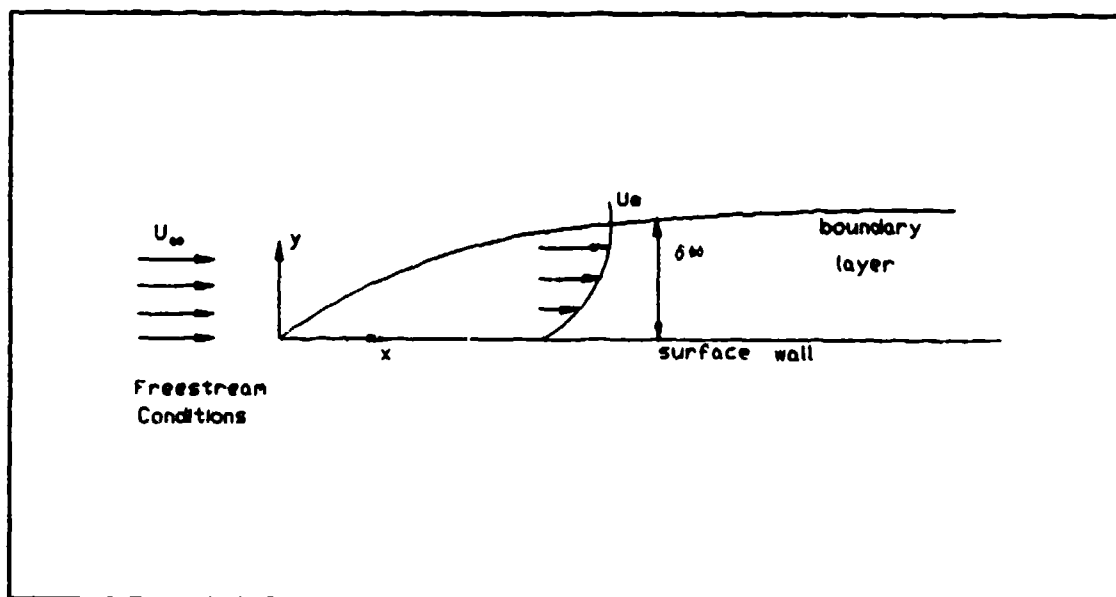


Figure 3-1 Boundary Layer Definitions

To account for compressibility effects, we introduce a transformed normal coordinate Y defined by,

$$dY = \frac{\rho}{\rho_e} dy \quad (3-4)$$

The momentum thickness can now be written as,

$$\theta = \int_0^{\Delta} \frac{U}{U_e} \left(1 - \frac{U}{U_e} \right) dY \quad (3-5)$$

where $Y = \Delta$ is the location of the outer edge of the boundary layer for the transformed coordinate. The wall friction is given by,

$$\tau_w = \frac{\rho_w \mu}{\rho_e} \left(\frac{\partial U}{\partial Y} \right)_w \quad (3-6)$$

3.3 Approximate Solution Based on Assumed Velocity Profile

An approximate solution for the momentum integral equation can be obtained by using an assumed velocity profile having the form,

$$\frac{U}{U_e} = f\left(\frac{Y}{\Delta}\right) \quad (3-7)$$

The momentum integral and wall friction can now be expressed as

$$\theta = \Delta \alpha_2 \quad (3-8a)$$

(3-8b)

$$\tau_w = \frac{\rho_w \mu_w}{\rho_e} \frac{U_e}{\Delta} \alpha_1$$

where

$$\alpha_2 = \int_0^1 \frac{U}{U_e} \left(1 - \frac{U}{U_e} \right) d\left(\frac{Y}{\Delta}\right) \quad (3-9a)$$

$$\alpha_1 = \left[\frac{\partial(U/U_e)}{\partial(Y/\Delta)} \right]_w \quad (3-9b)$$

For this problem, we assume that the pressure gradient is zero and that the wall temperature is a constant, and thus that α_1 and α_2 are constants that depend only on the assumed velocity profile. The momentum-integral equation (3-1) can now be expressed as,

$$\Delta \frac{d\Delta}{dx} = C_w \frac{\mu_e}{\rho_e U_e} \frac{\alpha_1}{\alpha_2} \quad (3-10)$$

where

$$C_w = \frac{\rho_w \mu_w}{\rho_e \mu_e} \quad (3-11)$$

For this problem, the right side of equation (3-10) is a constant. Thus we can integrate it without difficulty, subject to the boundary condition $\Delta(0) = 0$, and obtain

$$\Delta = \sqrt{C_w \frac{2\alpha_1}{\alpha_2} \frac{\mu_e x}{\rho_e U_e}} \quad (3-12)$$

We thus obtain the well-known result for flat plates that the transformed boundary-layer thickness grows like the square root of x .

The local skin friction can now be obtained from equation (3-8b). The local skin-friction coefficient, based on the external-flow conditions is,

$$C_{f_e} \equiv \frac{\sqrt{2 \alpha_1 \alpha_2 C_w}}{\sqrt{R_{ex_e}}} \quad (3-13)$$

where

$$R_{ex_e} \equiv \frac{\rho_e U_e x}{\mu_e} \quad (3-14)$$

is the Reynolds number based on the external flow conditions. Equation (3-13) has the same form as that obtained from the classical Blasius equation for constant-density flow past a flat plate. For compressible flow, the factor C_w depends on the assumed viscosity-temperature relation. The factor $\alpha_1 \alpha_2$ depends on the assumed velocity profile.

3.4 Viscosity-Temperature Power-Law Relation

In this analysis, we shall assume the viscosity-temperature power-law relation

$$\frac{\mu}{\mu_e} = \left(\frac{T}{T_e} \right)^\omega \quad (3-15)$$

where ω is a constant usually taken to lie in the range $.5 \leq \omega \leq 1$, depending on the temperatures involved in the problem. Generally, ω is taken to be about 3/4.

For the special case $\omega = 1$, equation (3-15) takes the form

$$\frac{T_e}{T} \frac{\mu}{\mu_e} = 1 \quad (3-16)$$

Since the pressure is a constant across the boundary layer, we have for a thermally perfect gas ($P = \rho RT$) that $\frac{T_e}{T} = \frac{\rho}{\rho_e}$, and thus that

$$\frac{\rho \mu}{\rho_e \mu_e} = 1 \quad (3-17)$$

For this case, therefore, we have that $C_w = 1$. Thus for $\omega = 1$, C_{fe} from equation (3-13) has the same form as for incompressible flow, provided that ρ and μ are evaluated at the external flow conditions.

If $\omega \neq 1$, equation (3-15) can be written in the form

$$\frac{\mu}{\mu_e} = C \frac{T}{T_e} \quad (3-18)$$

where

$$C \equiv \frac{\rho \mu}{\rho_e \mu_e} = \left(\frac{T}{T_e} \right)^{\omega - 1} \quad (3-19)$$

Equation (3-18) is sometimes referred to as the Chapman-Rubesin form of the viscosity-temperature law, when C is taken as some constant or some function of x , but not as a function of y . For our purposes here, since T is a function of y , we will consider that C is also a function of y , given by equation (3-19). It correspondingly follows that,

$$C_w = \left(\frac{T_w}{T_e} \right)^{\omega - 1} \quad (3-20)$$

3.5 Assumed Velocity Profile

We shall assume that $U/U_e = f(Y/\Delta)$ has the specific form following the Karman-Pohlhausen technique. Namely, a fourth-order polynomial having the form,

$$\frac{U}{U_e} = A \left(\frac{Y}{\Delta} \right) + B \left(\frac{Y}{\Delta} \right)^2 + C \left(\frac{Y}{\Delta} \right)^3 + (1 - A - B - C) \left(\frac{Y}{\Delta} \right)^4 \quad (3-21)$$

This expression satisfies the condition at the outer edge of the boundary layer that $U/U_e(1) = 1$. The constants A , B , and C are as follows to meet boundary conditions.

$$A = \left[\frac{\partial(U/U_e)}{\partial(Y/\Delta)} \right]_w = \alpha_1 \quad (3-22a)$$

$$B = \frac{1}{2} \left[\frac{\partial^2(U/U_e)}{\partial(Y/\Delta)^2} \right]_w \quad (3-22b)$$

$$C = (-2 - B) \quad (3-22c)$$

To specify A and B and thus C, we start by noting from the boundary-layer momentum differential equation that at the wall

$$\left[\frac{\partial}{\partial y} \left(\mu \frac{\partial U}{\partial y} \right) \right]_w = 0 \quad (3-23a)$$

provided the pressure gradient along the wall is zero. In terms of the transformed variable Y, this is

$$\left[\frac{\partial}{\partial Y} \left(C \mu_0 \frac{\partial U}{\partial Y} \right) \right]_w = 0 \quad (3-23b)$$

Since μ_0 does not depend on Y, we can expand equation (3-23b) and get

$$\begin{aligned} \left(\frac{\partial^2 U}{\partial Y^2} \right)_w &= - \left(\frac{\partial \ln C}{\partial Y} \right)_w \left(\frac{\partial U}{\partial Y} \right)_w \\ &= - \left(\frac{\partial \ln C}{\partial T} \right)_w \left(\frac{\partial T}{\partial Y} \right)_w \left(\frac{\partial U}{\partial Y} \right)_w \\ &= - \frac{(\omega - 1)}{T_w} \left(\frac{\partial T}{\partial Y} \right)_w \left(\frac{\partial U}{\partial Y} \right)_w \end{aligned} \quad (3-24)$$

Equation (3-22) provides a relation between the first and second derivative of the velocity at the wall, that is, between A and B. It is useful to place it in an alternative form. We note along with the expressions (3-3) and (3-6) at the wall that we have similar expressions for the heat flux

at the wall:

$$q_w = -k_w \left(\frac{\partial T}{\partial y} \right)_w = - \frac{\rho_w k_w}{\rho_\infty} \left(\frac{\partial T}{\partial Y} \right)_w \quad (3-25)$$

Consequently, equation (3-24) can be written alternatively as

$$\left(\frac{\partial^2 U}{\partial Y^2} \right)_w = \frac{(\omega - 1)}{T_w} \frac{P_r}{C_p} \frac{q_w}{\tau_w} \left(\frac{\partial U}{\partial Y} \right)_w^2 \quad (3-26)$$

where

$$P_r = C_p \mu_w / k_w \quad (3-27)$$

is the Prandtl number evaluated at the wall, and C_p is the specific heat at constant pressure. We assume that both P_r and C_p are constants.

It is further useful to introduce the Stanton number as the dimensionless heat-transfer coefficient:

$$S_T = \frac{q_w}{\rho_\infty U_\infty C_p (T_w - T_{aw})} \quad (3-28)$$

Here the Stanton number is based on the external flow conditions, and T_{aw} is the adiabatic wall temperature, to be specified later. Note that if heat is transferred from the fluid to the wall, then $T_w < T_{aw}$ and $q_w < 0$. In terms of S_T and C_p , defined by equation (3-13), we can rewrite equation (3-24) as

$$\left[\frac{\partial^2 (U/U_0)}{\partial (Y/\Delta)^2} \right] = (\omega - 1) \frac{(T_w - T_{0w})}{T_w} \frac{2 P_r S_T}{C_f} \left[\frac{\partial (U/U_0)}{\partial (Y/\Delta)} \right]_w^2 \quad (3-29a)$$

or

$$B = \frac{(\omega - 1)(T_w - T_{0w})}{2 T_w} \frac{2 P_r S_T}{C_f} A^2 \quad (3-29b)$$

The factor $2S_T/C_f$ is known as the Reynolds-analogy factor. It will be specified later. Note when $\omega = 1$ that $B = 0$, and also when C is a constant or a function of x only that B again is zero.

Since B is a function of A , we need a condition on the assumed profile (3-19) to determine A . To do this, we assume the following condition at the outer edge of the boundary layer:

$$\left[\frac{\partial (U/U_0)}{\partial (Y/\Delta)} \right]_{Y=\Delta} = 0 \quad (3-30)$$

This gives,

$$A + 2B + 3C + 4(1-A-B-C) = 0$$

substituting the relations for B and C yield,

$$DA^2 + 3A - 6 = 0 \quad (3-31)$$

where

$$D = \frac{(\omega - 1)(T_w - T_{0w})}{2 T_w} \frac{2 P_r S_T}{C_f} \quad (3-32)$$

Solving the quadratic equation for A gives

$$A = 12/(3 + \sqrt{9+24D}) \quad (3-33)$$

When $D = 0$, then $A = 2$, and the velocity profile reduces to

$$\frac{U}{U_e} = 2\left(\frac{Y}{\Delta}\right) - 2\left(\frac{Y}{\Delta}\right)^3 + \left(\frac{Y}{\Delta}\right)^4 \quad (3-34)$$

3.6 Effects of Mach Number and Heat Transfer on the Friction Coefficient

The momentum-thickness parameter α_2 can now be evaluated from the basic definition equation (3-9a):

$$\alpha_2 = 1/35 + 4A/15 - A^2/9 + DA^2(1/14 - 9A/140 - DA^2/105) \quad (3-35a)$$

Since A depends on the factor D from equation (3-33), then α_2 depends on D only. Using the relationships from reference 17,

$$A = 2 + \frac{\Lambda}{6}, \quad \Lambda = -2B \quad (3-35b)$$

and that $D = BA^2$ allows us to write (3-35a) in the same manner as is done in the same reference namely,

$$\alpha_2 = \frac{1}{63} \left(\frac{37}{5} - \frac{\Lambda}{15} - \frac{\Lambda^2}{144} \right) \quad (3-35c)$$

When $D = 0$, that is, when $\omega = 1$ or when $T_w = T_{aw}$ (no heat transfer), then $A = 2$. We then have $\alpha_2 \approx 0.1175$. Likewise for this case we have $C_w = 1$, and the factor $f(2\alpha_1\alpha_2)$ appearing in the friction coefficient C_{fe} , equation (3-13), takes the value,

$$f(2\alpha_1\alpha_2) \approx 0.685.$$

The correct value for this factor evaluated by the Blasius profile from laminar boundary-layer theory is 0.664. Thus, for this case, the profile from equation (3-34) leads to an error of 3 percent.

Although this error is quite acceptable for our present purposes, the important utility of the present analysis lies in the result for α_2 , equation (3-35), that produces combined results for $\omega \neq 1$ and for wall heat transfer, and for which there are no corresponding analytical results from the differential-equation analysis of compressible laminar boundary-layer theory. To proceed further, we need to evaluate the factor D , and to do this we need expressions for the adiabatic wall temperature and the Reynolds analogy factor. We shall thus assume the relations

$$T_{ow} = T_e \left(1 + \sqrt{Pr} \frac{\gamma - 1}{2} M_e^2 \right) \quad (3-36)$$

$$2S_T/C_f = Pr^{-2/3} \quad (3-37)$$

which are well known approximations for flat plates and wedges. The factor D thus becomes

$$D = \frac{\omega - 1}{2} P_r^{1/3} \left[1 - \frac{T_e}{T_w} \left(1 + \sqrt{P_r} \frac{\gamma - 1}{2} M_e^2 \right) \right] \quad (3-38)$$

With these results, we now have the general functional dependence

$$C_{fe} = f \left(R_{exe}, M_e, \frac{T_e}{T_w}, P_r, \omega, \gamma \right) \quad (3-39)$$

By means of equation (3-20) we can write equation (3-13) as

$$C_{fe} = \frac{\sqrt{2 \alpha_1 \alpha_2}}{\sqrt{R_{exe}}} \left(\frac{T_e}{T_w} \right)^{\frac{1-\omega}{2}} \quad (3-40)$$

with the factor $f(2\alpha_1\alpha_2)$ being a function of D as given by equation (3-38). For adiabatic walls, the results simplify since $D = 0$, and we have

$$C_{fe} = \frac{0.685}{\sqrt{R_{exe}}} \frac{1}{\left(1 + \sqrt{P_r} \frac{\gamma - 1}{2} M_e^2 \right)^{\frac{1-\omega}{2}}}$$

The factor $C_{fe} f(R_{exe})$ is plotted versus M_e in figure 3-2 for $\gamma = 1.4$, $\omega = 0.7$, $P_r = 0.72$. It can be seen that increasing the external-flow Mach number can reduce the local

skin-friction coefficient considerably.

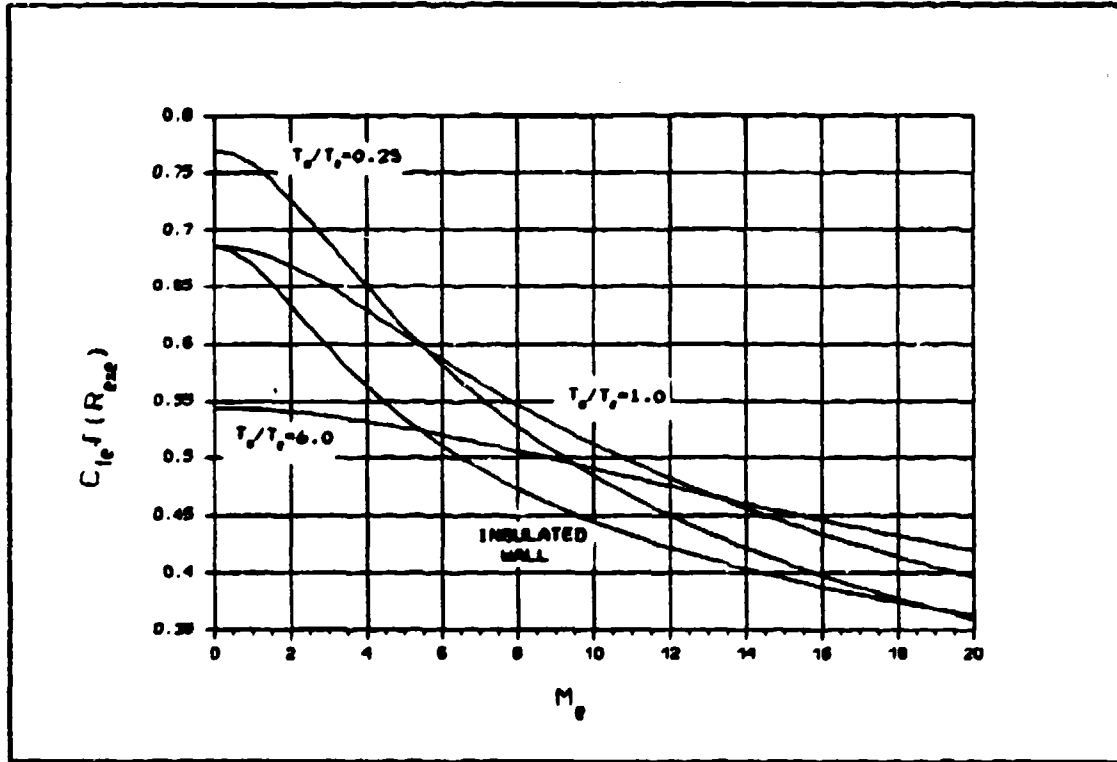


Figure 3-2

Figure 3-2 also shows two curves for when the wall temperature is held fixed, that is, for $T_w/T_e = 1$ and 6. Again these curves are calculated by means of equations (3-39), (3-36), (3-33) and (3-31). Again, the local skin friction coefficient decreases as M_{∞} increases. These curves are in agreement with corresponding results obtained by numerical integration of the similarity boundary-layer equations of reference 19 and 20.

3.7 Application to Waverider Freestream Surface

For flat plates the external conditions are the same as the freestream conditions. Since the inviscid surface streamlines are straight lines with zero pressure gradient on the upper freestream surface of the waverider, we can apply the previous formulas for C_{f_e} by replacing the subscript e with the subscript ∞ . In doing this we ignore the fact that there is actually a cross flow in the boundary layer. This occurs because the boundary layer originates at different locations along the leading edge. In a subsequent section, we will obtain an average skin friction coefficient for the freestream wetted surface by integrating the local skin-friction coefficient along each straight streamline on the freestream surface and then integrating again across the span of the surface. This approximate result can be obtained straight forwardly and provides a simple means for making parametric studies of friction drag.

3.8 Compression Surface of the Waverider

For the compression surface of the waverider, the external conditions for the boundary layer are not the same as the freestream conditions because the inviscid surface streamlines pass through the conical bow shock. To express the local skin-friction coefficient and the local Reynolds number in terms of the freestream conditions, we therefore rewrite equation (3-13) as follows:

$$\begin{aligned}
C_{f_{\infty}} &= \frac{2\tau_w}{\rho_{\infty} U_{\infty}^2} = \frac{\rho_e U_e^2}{\rho_{\infty} U_{\infty}^2} C_{f_e} \\
&= \frac{\rho_e U_e^2}{\rho_{\infty} U_{\infty}^2} \left(\frac{T_e}{T_w} \right)^{\frac{1-\omega}{2}} \frac{\sqrt{2\alpha_1\alpha_2}}{\sqrt{\frac{\rho_e U_e \mu_{\infty}}{\rho_{\infty} U_{\infty} \mu_e} Re_{x_{\infty}}}} \\
&= \sqrt{\frac{\rho_e}{\rho_{\infty}}} \left(\frac{U_e}{U_{\infty}} \right)^{3/2} \left(\frac{T_e}{T_{\infty}} \right)^{\omega/2} \left(\frac{T_e}{T_w} \right)^{\frac{1-\omega}{2}} \frac{\sqrt{2\alpha_1\alpha_2}}{\sqrt{Re_{x_{\infty}}}}
\end{aligned} \tag{3-42}$$

where

$$Re_{x_{\infty}} = \frac{\rho_{\infty} U_{\infty} x}{\mu_{\infty}} \tag{3-43}$$

For a thermally perfect gas we have

$$\frac{\rho_e}{\rho_{\infty}} = \frac{P_e}{P_{\infty}} \frac{T_{\infty}}{T_e} \tag{3-44}$$

Thus, when the density is eliminated in favor of the pressure, equation (3-42) becomes

$$C_{f_{\infty}} = \sqrt{\frac{P_e}{P_{\infty}}} \left(\frac{U_e}{U_{\infty}} \right)^{3/2} \left(\frac{T_{\infty}}{T_w} \right)^{\frac{1-\omega}{2}} \frac{\sqrt{2\alpha_1\alpha_2}}{\sqrt{Re_{x_{\infty}}}} \tag{3-45}$$

The inviscid surface streamlines on the compression side of the waverider lie in a plane, and the pressure increases slowly along the streamline. Although the boundary layer has

a cross flow and is thus actually three dimensional, we assume these effects are small enough to ignore, and thus the boundary layer along an inviscid surface streamline behaves nearly as that of a flat plate. Further, we assume that the external flow conditions are given by the conditions immediately behind the conical bow shock. If we evaluate these conditions by hypersonic small-disturbance theory then we have

$$\frac{U_e}{U_\infty} \approx 1 \quad (3-46a)$$

$$\frac{P_e}{P_\infty} \approx 1 + \gamma K_\delta^2 \quad (3-46b)$$

$$\frac{(\gamma-1)M_\infty^2 + 2}{(\gamma-1)M_e^2 + 2} = \frac{T_e}{T_\infty} = 1 + \frac{(\gamma-1)}{2} K_\delta^2 \left(2 - \frac{1}{\sigma^2} \right) \quad (3-46c)$$

where

$$\sigma^2 = \frac{(\gamma+1)}{2} + \frac{1}{K_\delta^2} \quad (3-46d)$$

and $K_\delta \equiv M_\delta$. Equation (3-45) now takes the form

$$C_{f_\infty} = \sqrt{\frac{P_e}{P_\infty}} \left(\frac{T_\infty}{T_w} \right)^{\frac{1-\gamma}{2}} \frac{\sqrt{2 \alpha_1 \alpha_2}}{\sqrt{Re_{x_\infty}}} \quad (3-47)$$

The factor $(\alpha_1 \alpha_2)_e$ must be evaluated such that T_e and M_e in the factor D are calculated in terms of the infinity conditions

by means of equation (3-46c).

We may simplify equation (3-47) by writing it in terms of the freestream skin friction coefficient given by equation (3-40). Doing so gives,

$$C_{f\infty} = K(C_{f\infty})_{fs} \quad (3-48)$$

where

$$K = \sqrt{\frac{P_e}{P_\infty}} \sqrt{\frac{(\alpha_1 \alpha_2)_e}{\alpha_1 \alpha_2}} \quad (3-49)$$

In the factor K the dominant term is $\sqrt{(P_e/P_\infty)}$ since $\sqrt{((\alpha_1 \alpha_2)_e/(\alpha_1 \alpha_2))}$ is close to unity. In fact it is unity when $Pr = 1$.

3.9 Average Skin Friction Coefficients

The average skin friction coefficient is determined by summing up all of the local coefficients along each streamline and then dividing through by the wetted area of the surface.

Considering figure 3-3 below, we have for the average skin friction coefficient for the freestream surface

$$\overline{C_{ff}} = \frac{2 \int_s \int_{zs}^l C_{f\infty} dz ds}{2 \int_s \int_{zs}^l dz ds} \quad (3-50)$$

In this section we will skip the details of the analysis of the above equation and save it for appendix A. However, after this analysis we have,

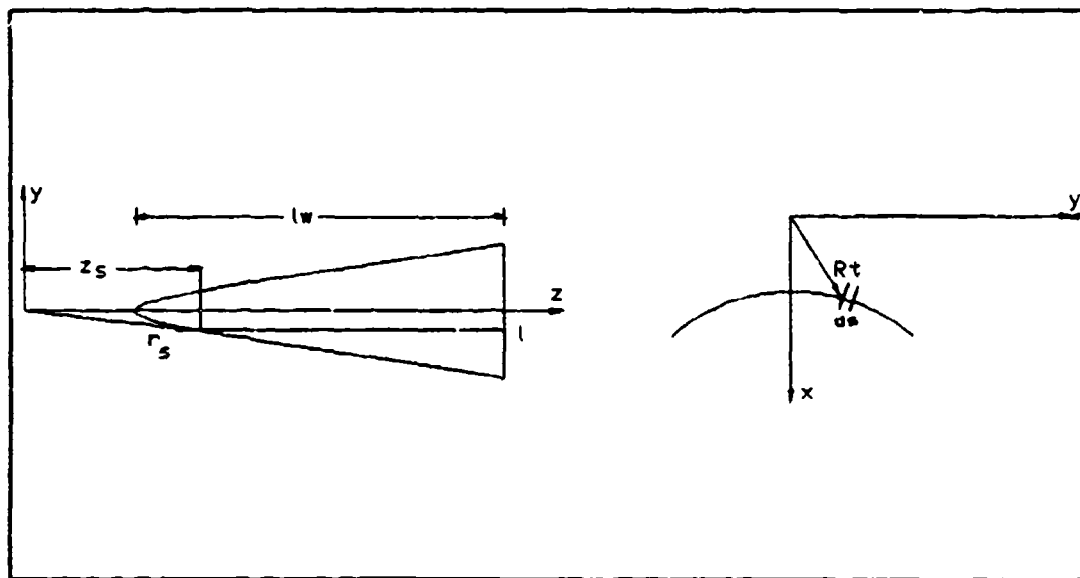


Figure 3-3 The Freestream Surface

$$\overline{C_{f1}} = \frac{\sqrt{1-R_0/\sigma} C_{f1} 2 \int_0^{Y_b} \sqrt{1-R_t/\sigma} \sqrt{1+(dX/dY)^2} dY}{\int_0^{Y_b} (1-R_t/\sigma) \sqrt{1+(dX/dY)^2} dY} \quad (3-51)$$

The reader may choose any numerical integration scheme desired to evaluate the integrals.

Now, to determine the average skin friction coefficient for the compression surface we will make the assumption that the wetted area for the compression surface is approximately

the same as that of the freestream surface. Using this approximation gives for the compression surface,

$$\overline{C_{fc}} = \frac{\sqrt{1-R_0/\sigma} C_{fc} 2 \int_0^{Y_t} \sqrt{1-R_t/\sigma} \sqrt{1+(dX/dY)^2} dY}{\int_0^{Y_t} (1-R_t/\sigma) \sqrt{1+(dX/dY)^2} dY} \quad (3-52)$$

In equations (3-51) and (3-52) above C_{ff} and C_{fc} are the local skin friction coefficients determined using the analysis of the previous sections.

3.10 Estimation of Total Drag

A good discussion on various types of Drag is presented in reference 21. Here, we will begin with the following definition

$$D = D_w + D_f + D_b \quad (3-53)$$

where D_w is the wave drag, D_f is the skin friction drag and D_b is the base drag.

The wave drag exists at supersonic/hypersonic speeds and is caused by static pressure gradients across the shock wave. We will define the wave drag as

$$D_w = q A_b C_w \quad (3-54)$$

where $q = 1/2 \rho_\infty U_\infty^2$, A_b is the base area of the waverider and C_w is the wave drag coefficient.

The skin friction drag is caused by shearing stresses over the wetted surface of the body. We will define the friction drag as

$$D_f = q \overline{C_{ff}} (S_{wf} + S_{wc}) \quad (3-55)$$

where S_{wf} and S_{wc} represent the wetted surface area of the freestream and compression surfaces respectively. Also, $\overline{C_{ff}}$ is the average total skin friction coefficient. However, using the analysis of the previous sections we can rewrite (3-55) as

$$D_f = q (S_{wf} \overline{C_{ff}} + S_{wc} C_{fc}) \quad (3-56)$$

or using the results of equation (3-48) we have,

$$D_f = q \overline{C_{ff}} (S_{wf} + K S_{wc}) \quad (3-57)$$

The base drag is caused by the blunt end of a body. This is because the pressure at the base is usually not the same as the surrounding infinity conditions. We will ignore this effect however, as is usually done when comparing different configurations¹⁴. Thereby setting $P_b = P_\infty$.

Ignoring the base drag and combining equations (3-51) and (3-50) into (3-49) gives

$$D = q (C_w A_b + \overline{C_{ff}} S_{wf} + C_{fc} S_{wc}) \quad (3-58)$$

or using the results of (3-57) we have

$$D = q [C_w A_b + \overline{C_{ff}} (S_{wf} + K S_{wc})] \quad (3-59)$$

It may be more convenient to have the total drag in terms of the average total skin friction coefficient. Equating (3-

55) and (3-57) and solving for $\overline{C_{ff}}$ yields,

$$\overline{C_{ff}} = \overline{C_{ft}}[(S_{nf} + S_{nc})/(S_{nf} + KS_{nc})] \quad (3-60)$$

Substituting (3-60) into (3-59) gives,

$$D = q[C_{nb} + \overline{C_{ft}}(S_{nf} + S_{nc})] \quad (3-61)$$

where

$$\overline{C_{ft}} = \overline{C_{ff}}[(S_{nf} + KS_{nc})/(S_{nf} + S_{nc})] \quad (3-62)$$

In the appendix to this thesis we present the lift-to-drag ratio as well as the average total skin friction coefficient for each particular configuration shown.

CHAPTER 4

Comparing Configurations

4.1 Introductory Remarks

Here we will describe what happens as we change different parameters of the waverider configuration. In order to do this we must establish a basic shape from which we will base our comparisons. Once the basic configuration is chosen then we will discuss what happens when we change the coefficients of Y of equation (2-10) namely, b_2 , b_4 , and b_6 . After this we will compare shapes with different values for R_0 , ϕ_1 , and δ and include a discussion on the Mach number and Reynolds number.

4.2 The Basic Waverider Configuration

The basic shape is chosen to have the parameters shown below in table 4.1

Table 4-1
Basic Configuration Parameters

ϕ	δ	Mach Number	Reynolds Number	γ
50°	8	10	1×10^6	1.4
R_0	b_2	b_4	b_6	slope
0.5	0.903	-1.0	0.437	25°

The basic parameters were chosen arbitrarily except for b_2 and b_6 . The value of b_6 was chosen such that the slope at the edge of the waverider freestream surface was 25° . This value is in between the limits imposed by condition iii) of chapter 2. The value of b_2 was fixed according to equation (2-13). These basic configuration parameters resulted in the waverider configuration shown below in figure 4-1.

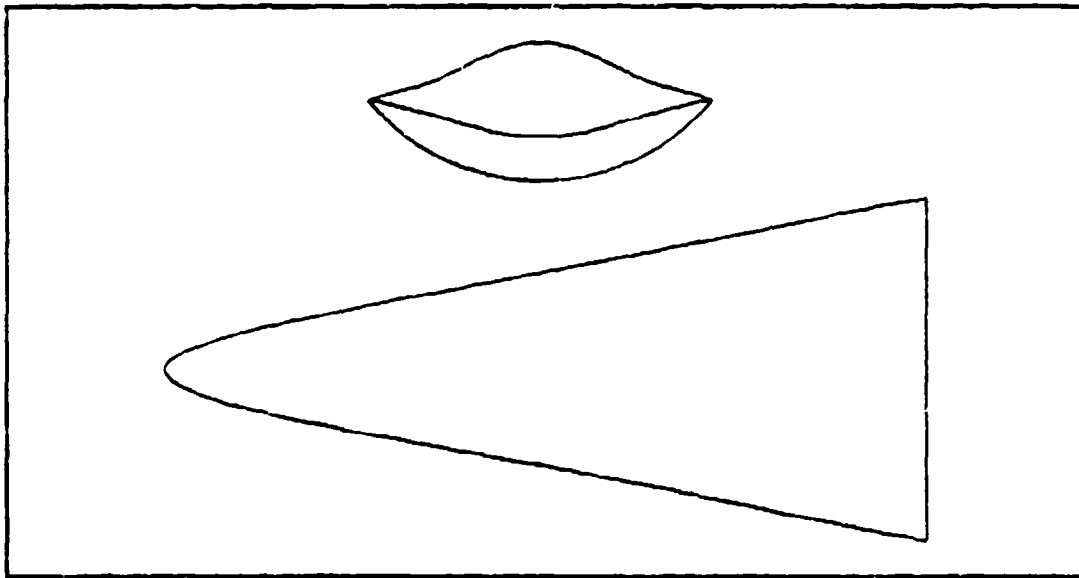


Figure 4-1 Basic Configuration Base Plane and Planform Views

We will now vary these parameters and see how the basic configuration changes.

2.3 Changing the Coefficients of Y of the Equation Describing the Freestream Edge in the Base Plane With Consideration of the Edge Slope

Here, we will hold the parameters, ϕ_1 , δ , M , Re_y , and constant and vary in a systematic way the coefficients of Y equation (2-10).

Suppose we want to change b_4 from a -1.0 as shown in table 4.1, to a -2.0. This is easily done. However, due to equation (2-13) changing b_4 will result in a different value of b_2 as well. We must also keep in mind the imposed condition of the slope at the edge of the waverider. Changing b_4 will also change the slope at the edge of the waverider. We can however, keep the slope at a constant value by letting b_6 change by a suitable amount. Table 4-2 below shows what happens when we change b_4 from -1.0 to -2.0, holding R_0 and the edge slope constant. Also, figure 4-2 shows the corresponding waverider configuration.

Table 4-2

ϕ	δ	Mach Number	Reynolds Number	γ
50°	8	10	1×10^6	1.4
R_0	b_2	b_4	b_6	slope
0.5	1.405	-2.0	0.935	25°

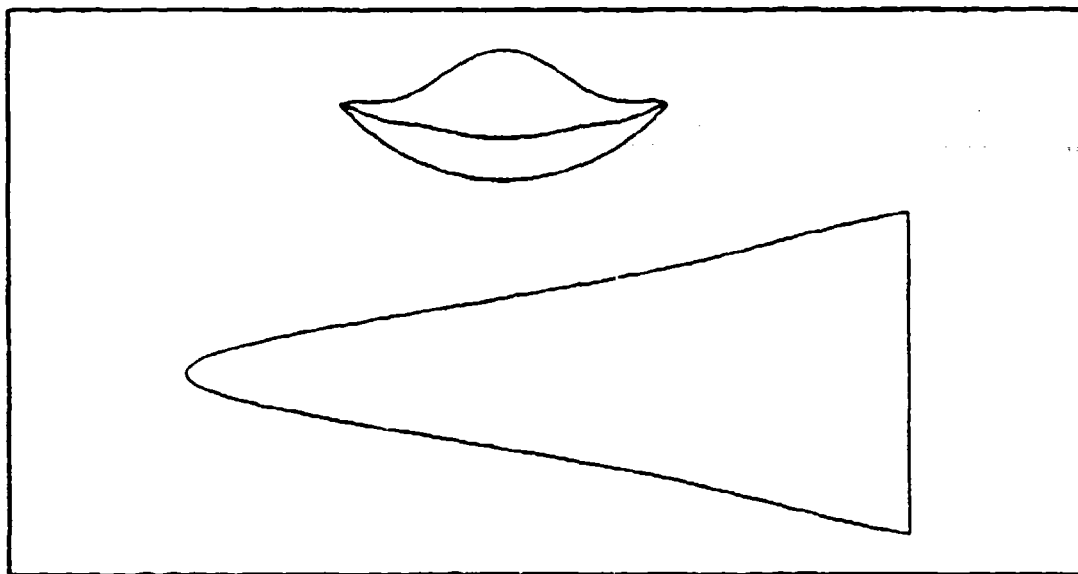


Figure 4-2 Effect of Changing b_4

This discussion shows the inherent complexities of changing what may seem to be a rather simple variable. By changing b_4 we discovered that b_2 and b_6 must also change.

Suppose now instead of changing b_4 we want to change the freestream edge slope from 25° to its maximum limit of 50° . This is accomplished by changing the value of b_6 or b_4 . However, for the sake of simplicity we will hold b_4 at its previous value of -1.0 . Setting $dx/dy = 50$ and solving gives a new value of b_6 and b_2 . Table 4-3 below shows this, and figure 4-3 shows the corresponding waverider configuration.

A similar approach to the above analysis can be done if we want the slope of the freestream edge at its minimum value.

We must also ask ourselves what are the aerodynamic and geometric consequences of changing the values of b_4 . Analysis

Table 4-3

ϕ	δ	Mach Number	Reynolds Number	γ
50°	8	10	1×10^6	1.4
R_0	b_2	b_4	b_6	slope
0.5	0.795	1.9	0.544	50°

has shown that the viscous lift to drag ratio may increase or decrease with a change in b_4 . The deciding factor is the initial value of b_4 . However, the change in magnitude of the viscous L/D appears to change only rather slightly.

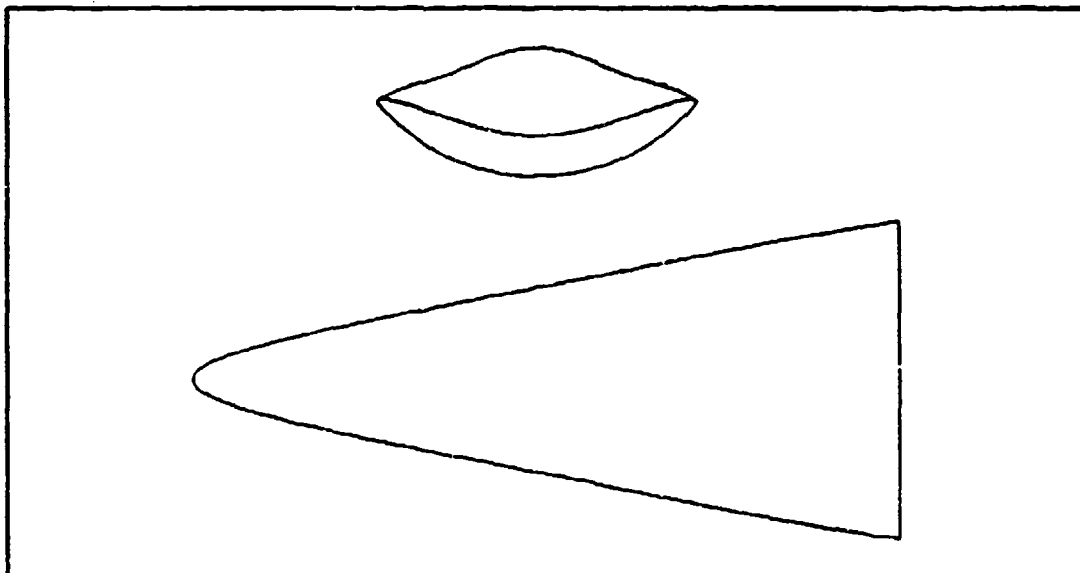


Figure 4-3 Effect of Changing Freestream Edge Slope

Similarly, the effects of changing the edge slope in general has a minor effect on the aerodynamic values. However, a slope of 50° usually gave higher L/D ratios; although in some cases this was not true.

4.4 Changing R_0 in the Equation Describing the Freestream Edge

When changing R_0 , we might say that there is no effect on the edge slope. However, a further investigation tells us that, even though dx/dy has no R_0 terms in it, the value of b_2 does depend on R_0 . Since the slope is dependent on b_2 we see that changing R_0 will result in a changing tip slope. We can however keep the tip slope constant by changing b_0 as done before.

A more dramatic affect caused by changing R_0 is the non-dimensional length of the waverider. This is easily seen by equation (2-38). Also, figure (4-4) below shows this result. We can see that small values of R_0 will result in more slender configurations. We define the aspect ratio for these configurations as b/l_w . Where b is the maximum distance across the base of the waverider. Therefore the smaller the aspect ratio the more slender the waverider. Aspect ratios are given for each configuration shown in the Appendix.

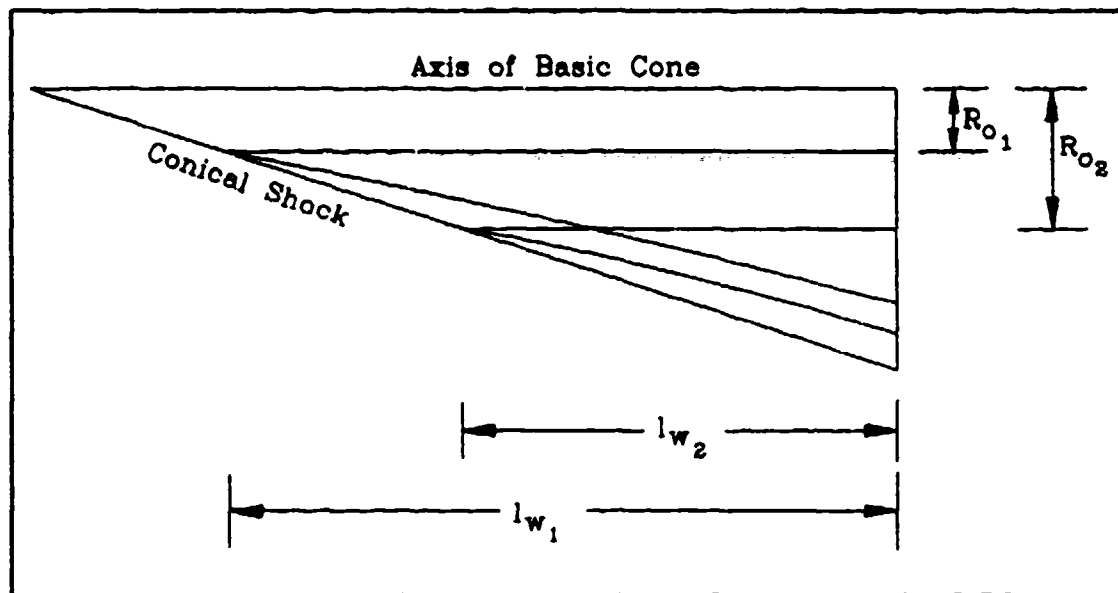


Figure 4-4 Effects of Changing R_0

Analysis shows in general that small values of R_0 usually result in better viscous lift to drag ratios.

Another effect on the waverider that occurs with a change in R_0 is the shock stand off distance. Smaller values of R_0 result in the shock being a greater distance away from the compression surface. This can be seen in the above figure. There are other factors that determine the shock stand off distance and these will be discussed as they occur.

Changing R_0 also significantly changes the shape of the base plane configuration as is shown below in figures 4-5a,b.

In figures 4-5a,b the value of the edge slope and the value of b_1 is kept constant. In general, larger values of R_0 cause the freestream surface to be flatter.

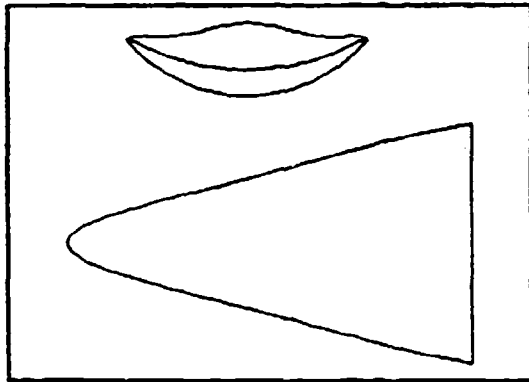


Figure 4-5a $R_0=0.7$, $b_4=-1.0$,
slope= 25°

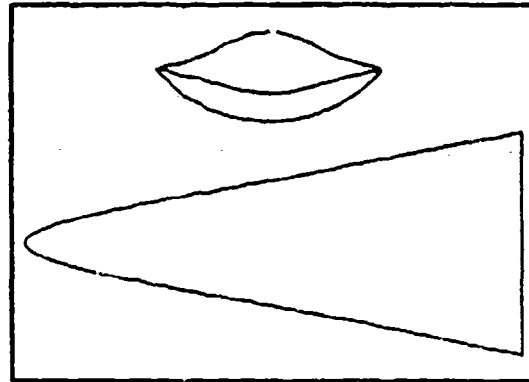


Figure 4-5b Basic Config.
 $R_0=0.5$, $b_4=-1.0$, slope= 25°

4.5 Changing the Parameter ϕ_1

When we change ϕ_1 the most significant change in the waverider shape that is first noticed is the change in maximum span or width; all other parameters remaining the same. Equations (2-14) and (2-15) give us the positive and negative most values of Y , which allow us to determine the span of the waverider. Clearly a decrease in ϕ_1 decreases the span. A decrease in the span decreases the aspect ratio and increases the slenderness of the waverider.

If we change ϕ_1 holding R_0 and b_4 constant, we get a new value for b_2 according to equation (2-13). Also, b_6 will have to change to keep the slope at the edge constant or within limits according to condition iii). Figures 4-6a,b show two configurations with identical δ , b_4 , and tip slope but with different ϕ_1 's

We see from this that a change in ϕ_1 causes a significant change in the waverider shape; not only in span but also in the curvature of the freestream and compression surface. However, there is no change in the length of the waverider.

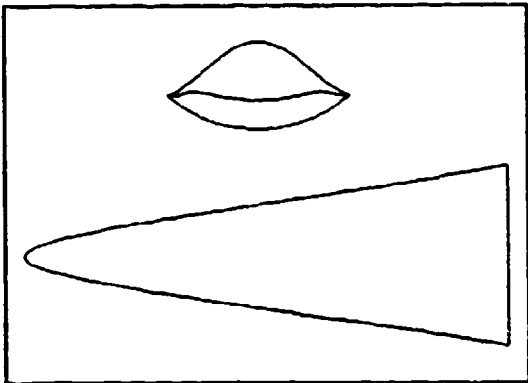


Figure 4-6a $R_0=0.5$, $b_1=-1.0$, slope= 25° , $\phi_1=40^\circ$

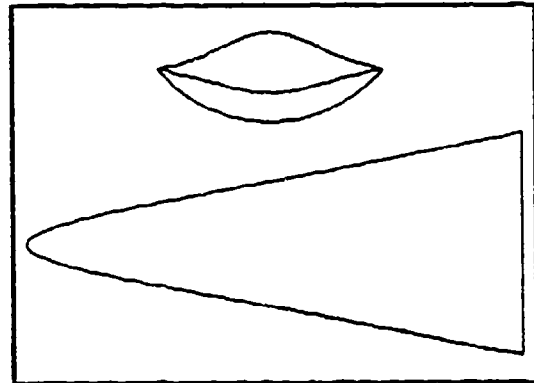


Figure 4-6b Basic Config $R_0=0.5$, $b_1=-1.0$, slope= 25° , $\phi_1=50^\circ$

4.6 Changing the Parameter δ

When we change δ the value of σ changes. This has an effect on the standoff distance between the shock and the compression surface of the waverider body. To see this we look at the definition of σ from chapter 3.

$$\sigma^2 = \frac{(\gamma+1)}{2} + \frac{1}{K_\delta^2} \quad (4-1)$$

where $K_\delta = M_\infty \delta$.

We can see from equation (4-1) that a decrease in δ will result in an increase in σ . This causes the separation

between β and δ to increase; which affects the shock standoff distance. The standoff distance becomes important when considering design of engine and engine inlet conditions. Below in figures 4-7a,b we show different waveriders with the same R_0 , ϕ_1 , b_4 , and tip slope but with different δ 's.

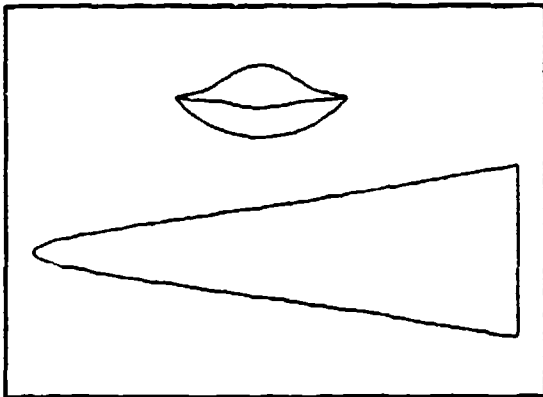


Figure 4-7a $R_0=0.5$, $b_4=-1.0$, $\delta=6$, $\phi_1=50$, slope= 25°

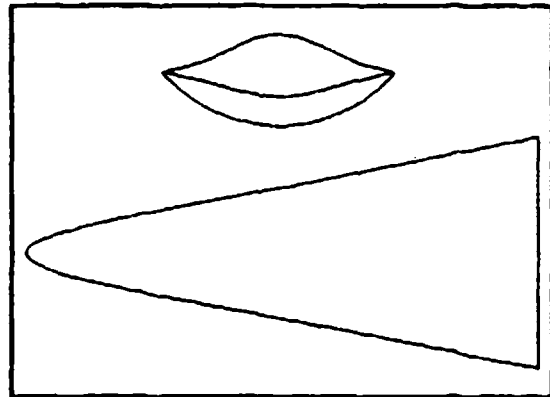


Figure 4-7b Basic Config. $R_0=0.5$, $b_4=-1.0$, $\delta=8$, $\phi_1=50$, slope= 25°

Again, changing δ and therefore σ , results in a change of b_2 according to equation (2-13) and a change in b_4 or b_6 to meet the slope condition on the edge of the waverider freestream surface. These changes cause the curvature of the freestream and compression surfaces to vary.

4.7 Changing the Mach Number

Varying the mach number has a similar effect as changing δ as we see from equation (4-1). An increase in M will cause

the standoff distance to be smaller just as an increase in δ will do. The only difference will be the magnitude of the change. Again we must take into account how changes affect σ and therefore b_2 , b_4 , and b_6 .

4.8 Changing the Reynolds Number

We realize that M has a role in the determination of the Reynolds number. However, let's assume the Mach number will remain constant. This leaves altitude and the length of the waverider as the deciding factors of the value of the Reynolds number.

Figure 4-8 below shows L/D vs. Reynolds number for the basic configuration shown in figure 4-1.

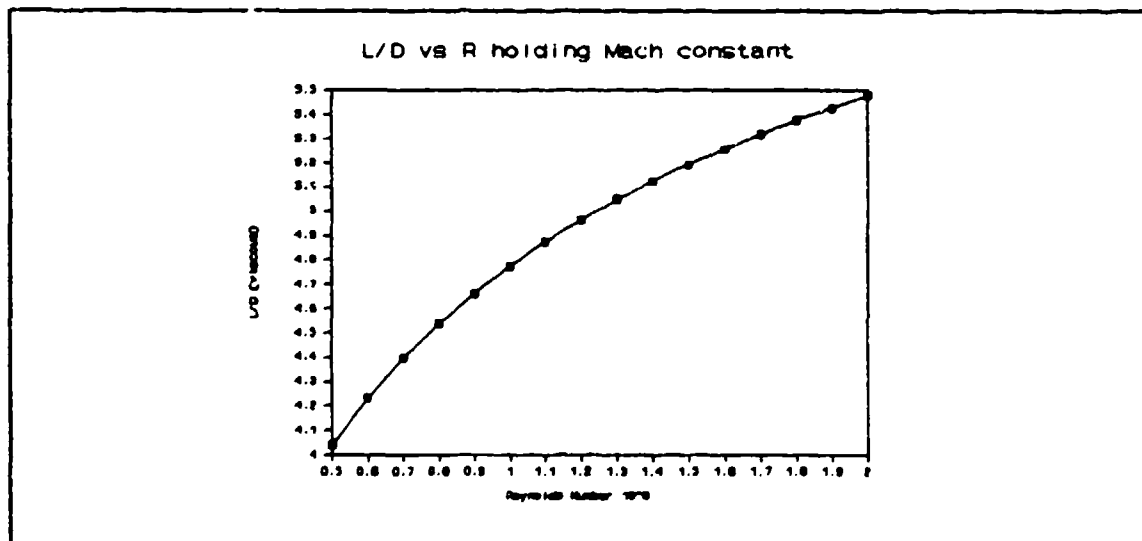


Figure 4-8 L/D vs. R holding Mach constant

CHAPTER 5

Conclusion

5.1 Summary

The two primary goals established in chapter 1 have been accomplished. In the appendices, a catalogue of over 100 shapes is presented. This catalogue shows variations of waveriders that can be generated by axisymmetric flow past a cone and is the result of the first goal.

As discussed earlier there can be an infinite number of waverider shapes so as yet the catalogue is incomplete. However, one may get an idea and a feel for waverider shapes by studying the appendices.

Chapter 3 is the result of the second primary goal. Here we developed an analytical method of estimating the skin friction coefficient -- where as before only numerical methods existed. An average total skin friction coefficient is presented in the appendices for each arbitrary waverider shape.

5.2 Results and Discussions

The best waverider shape depends on the designers main goals. As in all design processes one is usually faced with compromise. For example the waverider with the best lift-to-

drag ratio will probably not have the best volume-to-area ratio.

The following table is a tool to help in the design process. In the table we can see the effects of certain geometric and aerodynamic values when we vary parameters that affect the shape of the waverider. When using the table the results are given such that all other parameters are held constant. For example, lowering ϕ_1 will in general result in a lower value of L/D if the other parameters are held constant; namely, R_0 and b_4 . The table doesn't give magnitudes of change only direction of change. In some cases the effect of a change cannot be determined ahead of time. An example would be the effect in the volume-to-area ratio with a change in b_4 . Lowering b_4 may result in either an increase or decrease in the volume-to-area ratio depending on the original value of b_4 .

TABLE 5-1
EFFECT OF LOWERING (ϕ_1 , R_0 , and b_4)

	ϕ_1	R_0	b_4
L/D	↓	↓	↓
V/V_1	↓↑	↑	↓
$V^{2/3}/S_D$	↑	↑	↓↑
SSD	—	↑	—
b/l_w	↓	↓	—

Following this chapter in appendices B through H a catalogue of over 100 shapes is presented. All of the configurations presented are based on Mach number of 10 and Reynolds number of 10^6 . The lift-to-drag ratios were calculated and found to lie in a range from 4.32 to 5.06 while the average skin friction coefficient ranged from 0.00176 to 0.00205. The volume to area ratio $V^{2/3}/S_p$ ranged from 0.224 to 0.153. In the table under each view are various geometric and aerodynamic values. Some of them are compared with what we call the idealized waverider. Reference 14 describes this ideal waverider. The freestream surface of the ideal waverider is given by,

$$x = |y \cot \phi_1| \quad (5-1)$$

where the lines about the term on the right represent the absolute value. Note than in the above equation there is no term representing the value of R_0 . This is because R_0 is zero in this case.

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Appendix A

Development of Equation 3-51

We begin by establishing a few definitions that will be used later in this analysis. Consider the second part of figure 3-3 and we may say without much effort,

$$\begin{aligned} ds &= \sqrt{(dx)^2 + (dy)^2} \\ &= \sqrt{1 + (dx/dy)^2} dy \end{aligned} \quad A.1$$

Next, consider equations (2-5) and (2-20). From these we can show that,

$$dx/dy = dX/dY \quad A.2$$

and also that,

$$dx = l dX, \quad dy = l dY \quad A.3$$

Now considering the first part of figure 3-3 we may write that the wetted surface area of the freestream surface is,

$$\begin{aligned} S_{w\infty} &= 2 \int_0^l \int_{z_s}^l dz ds \\ &= 2 \int_0^l (l - z_s) ds \end{aligned} \quad A.4$$

Now since we are using small angles we have,

$$z_s \approx r_s \quad A.5$$

Therefore,

$$\begin{aligned} S_{w\infty} &= 2 \int_0^l (l - r_s) ds \\ &= 2l \int_0^l \left(1 - \frac{r_s}{l}\right) ds \end{aligned} \quad A.6$$

Now use equation (2-29) and that $R_t = R_{\theta}$ to give,

$$S_{w\infty} = 2\ell \int_0^{y_t} (1 - R_t/\sigma) ds \quad A.7$$

and substituting A.1 yields,

$$S_{w\infty} = 2\ell \int_0^{y_t} (1 - R_t/\sigma) \sqrt{1 + (dx/dy)^2} dy \quad A.8$$

Now if we substitute relationships A.2 and A.3 we have,

$$S_{w\infty} = 2\ell^2 \delta \int_0^{y_t} (1 - R_t/\sigma) \sqrt{1 + (dX/dY)^2} dY \quad A.9$$

Recall equation (3-50)

$$\overline{C_{ff}} = \frac{2 \int_0^{\ell} \int_{z_0}^{\ell} C_{fe} dz ds}{2 \int_0^{\ell} \int_{z_0}^{\ell} dz ds} \quad A.10$$

where C_{fe} is the local skin friction coefficient for the freestream surface. Substituting A.4 into A.10 yields,

$$\overline{C_{ff}} = \frac{2}{S_{w\infty}} \int_0^{\ell} \int_{z_0}^{\ell} C_{f\infty} dz ds \quad A.11$$

Using equation (3-40) and replacing the subscript e with ∞ according to section 3.7 yields,

$$\begin{aligned}
\overline{C_{ff}} &= \frac{2}{S_{w\infty}} \int_s \int_{zs}^l \frac{\sqrt{2\alpha_1\alpha_2}}{\sqrt{R_{ex\infty}}} \left(\frac{T_\infty}{T_w}\right)^{\frac{1-\omega}{2}} dz ds \\
&= \frac{2}{S_{w\infty}} \frac{\sqrt{2\alpha_1\alpha_2}}{\sqrt{\rho_\infty U_\infty/\mu_\infty}} \left(\frac{T_\infty}{T_w}\right)^{\frac{1-\omega}{2}} \int_s \int_{zs}^l \frac{dz ds}{\sqrt{z-z_0}} \\
&= \frac{4}{S_{w\infty}} \frac{\sqrt{2\alpha_1\alpha_2}}{\sqrt{\rho_\infty U_\infty/\mu_\infty}} \left(\frac{T_\infty}{T_w}\right)^{\frac{1-\omega}{2}} \int_s \sqrt{l-z_s} ds \\
&= \frac{4}{S_{w\infty}} \frac{\sqrt{2\alpha_1\alpha_2}}{\sqrt{\rho_\infty U_\infty/\mu_\infty}} \left(\frac{T_\infty}{T_w}\right)^{\frac{1-\omega}{2}} l^{1/2} \int_s \sqrt{1-z_s/l} ds \\
&= \frac{4}{S_{w\infty}} \frac{\sqrt{2\alpha_1\alpha_2}}{\sqrt{\rho_\infty U_\infty l_w/\mu_\infty}} \left(\frac{T_\infty}{T_w}\right)^{\frac{1-\omega}{2}} l \sqrt{l_w/l} \int_s \sqrt{1-z_s/l} ds
\end{aligned} \tag{A.12}$$

Now recall from equation (3-28) that,

$$l_w = l(1 - R_0/\sigma) \tag{A.13}$$

substituting yields,

$$\overline{C_{ff}} = \frac{4}{S_{w\infty}} \sqrt{2\alpha_1\alpha_2} \left(\frac{T_\infty}{T_w}\right)^{\frac{1-\omega}{2}} \frac{l\sqrt{1-R_0/\sigma}}{\sqrt{R_{ex\infty}}} \int_s \sqrt{1-z_s/l} ds \tag{A.14}$$

We may now make the substitutions of equation (3-40) and equations A.1, A.2, and A.3 to yield

$$\overline{C_{ff}} = \frac{C_{f\infty}}{S_{w\infty}} 4 \sqrt{1-R_0/\sigma} l^2 \delta \int_0^{y_l} \frac{\sqrt{1-R_l/\sigma}}{\sqrt{1+(dX/dY)^2}} dY \tag{A.15}$$

Now substitute equation A.9 to give us the desired result
equation (3-51)

$$\overline{C_{ff}} = \frac{C_{fm} 2 \sqrt{1-R_0/\sigma} \int_0^{Y_b} \sqrt{1-R_t/\sigma} \sqrt{1+(dX/dY)^2} dY}{\int_0^{Y_b} (1-R_t/\sigma) \sqrt{1+(dX/dY)^2} dY}$$

A.16

APPENDIX B

Presented here are configurations that have the following parameters held fixed:

$$\phi_1 = 60, \quad \delta = 8, \quad M = 10, \quad \text{Re}_y = 1 \times 10^6$$

The following parameters are varied:

$$R_0 \text{ from } 0.2 \text{ to } 0.4$$

$$b_4 \text{ from } 0.0 \text{ to } -3.0$$

The values of b_2 and b_6 are such that equation 2-13 and condition (iii) holds.

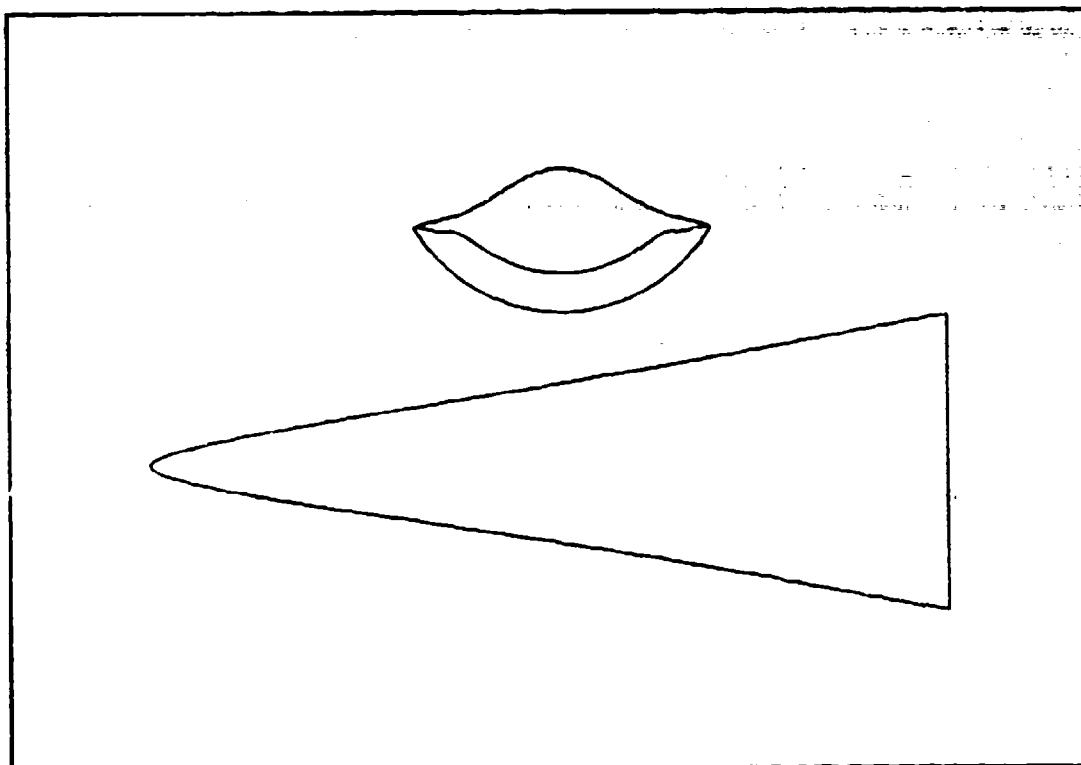


Figure B.1

Table B.1

Phi =60.0	Delta = 8.0	Mach =10.0	Rey = 0.10E+07	Gamma = 1.40
$X = 0.200 + 1.057 Y^2 + -1.000 Y^4 + 0.352 Y^6$				
Cftav = 0.001947	CL = 0.043795	CD = 0.009691		
Sw/Sp = 2.152777	V^(2/3)/Sp = 0.212286	(L/D)vis = 4.519036		
Ab/Abi = 0.870890	V/Vi = 0.774453	Sp/Spi = 0.901519		
b/lw = 0.372398	SSD = 0.300503			

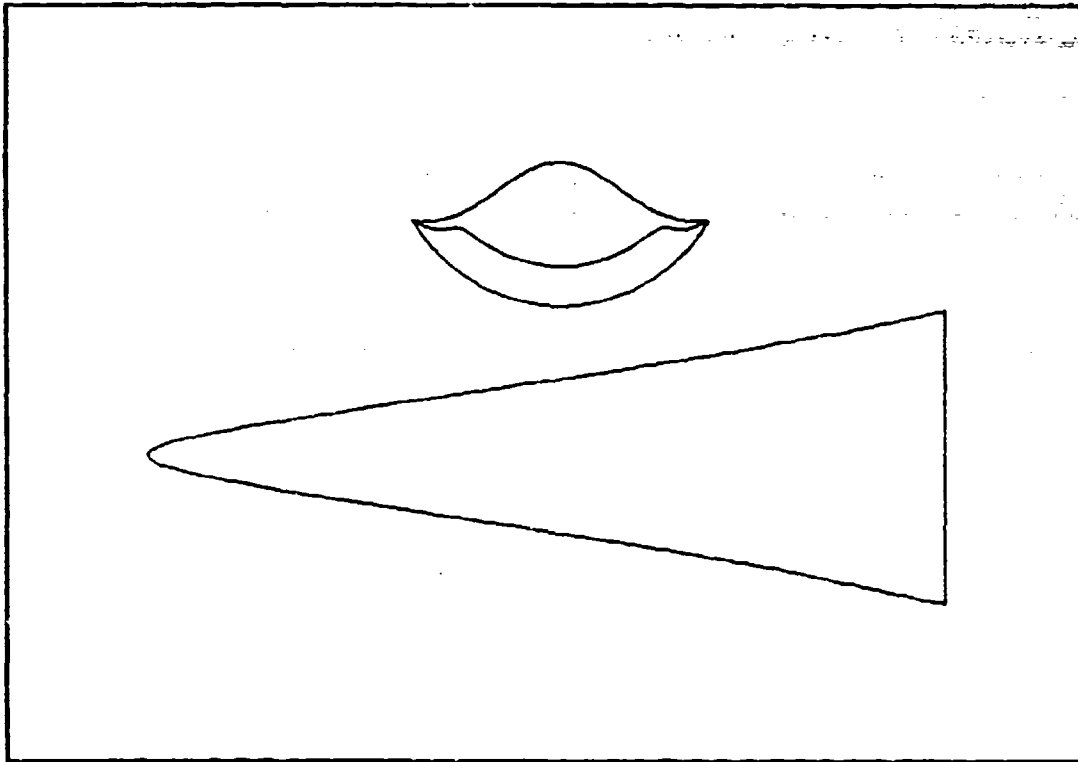


Figure B.2

Table B.2

Phi =60.0	Delta = 8.0	Mach =10.0	Rey = 0.10E+07	Gamma = 1.40
X = 0.200 + 1.171 Y^2 + -1.000 Y^4 + 0.283 Y^6				
Cftav = 0.001951	CL = 0.043789	CD = 0.009884		
Sw/Sp = 2.180042	T*(2/3)/Sp = 0.212500	(L/D)vis = 4.521998		
Ab/Abi = 0.835673	V/Vi = 0.743075	Sp/Sp1 = 0.876035		
b/lw = 0.372398	SSD = 0.300503			

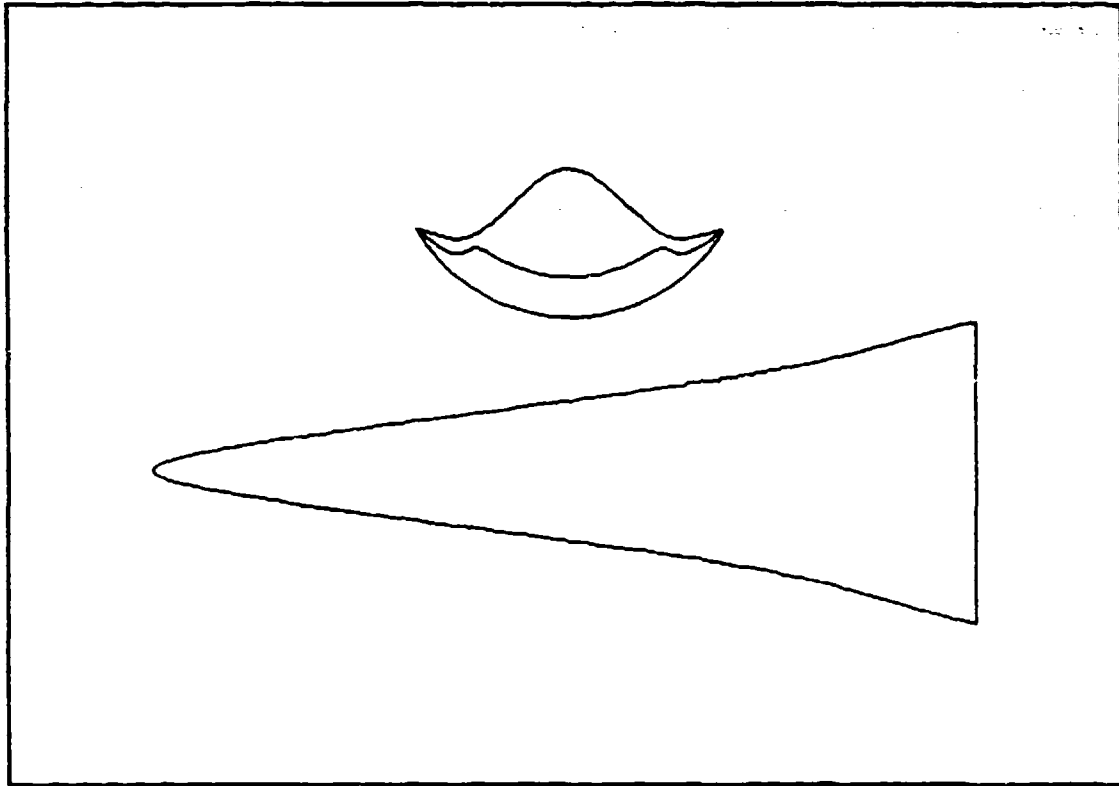


Figure B.3

Table B.3

Phi =60.0	Delta = 8.0	Mach =10.0	Rey = 0.10E+07	Gamma = 1.40
$X = 0.200 + 1.812 Y^2 + -2.000 Y^4 + 0.673 Y^6$				
Cftav = 0.001973	CL = 0.043690	CD = 0.009756		
Sw/Sp = 2.263438	V^(2/3)/Sp = 0.211051	(L/D)vis = 4.478099		
Ab/Ab1 = 0.756626	V/V1 = 0.655907	Sp/Spi = 0.811647		
b/lw = 0.372398	SSD = 0.300503			

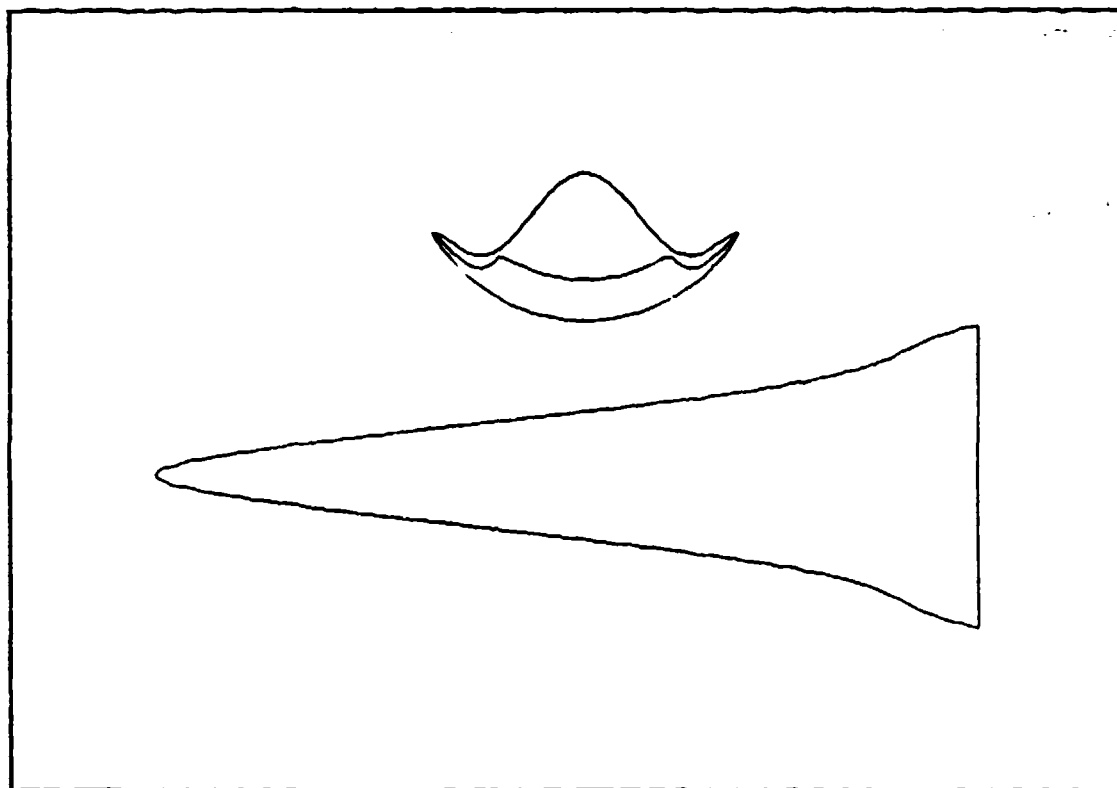


Figure B.4

Table B.4

Phi =60.0	Delta = 8.0	Mach =10.0	Rey = 0.10E+07	Gamma = 1.40
X = 0.200 + 2.457 Y^2 + -3.000 Y^4 + 1.061 Y^6				
Cftav = 0.002009	CL = 0.043637	CD = 0.009994		
Sw/Sp = 2.399271	V^(2/3)/S = 0.212883	(L/D)vis = 4.366130		
Ab/Ab1 = 0.576559	V/V1 = 0.579832	Sp/Spi = 0.741174		
b/lw = 0.372398	SSD = 0.300503			

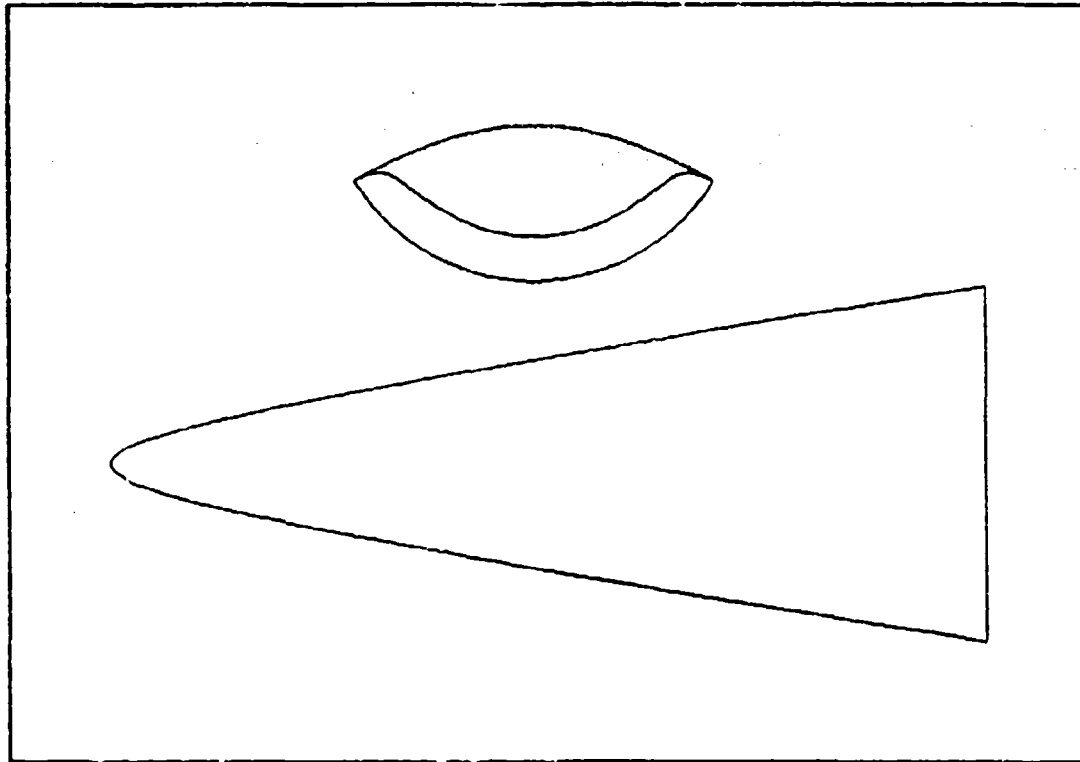


Figure B.5

Table B.5

Phi =60.0	Delta = 8.0	Mach =10.0	Rey = 0.10E+07	Gamma = 1.40
$X = 0.300 + 0.297 Y^2 + 0.000 Y^4 + -0.013 Y^6$				
Cftav = 0.001916	CL = 0.043599	CD = 0.009593		
Sw/Sp = 2.107515	V'(2/C)/S _γ = 0.207946	(L/D) _{vis} = 4.545040		
Δb/Δb ₁ = 0.878447	V/V ₁ = 0.743837	S _γ = 0.395832		
b/lw = 0.409313	SSD = 0.290236			

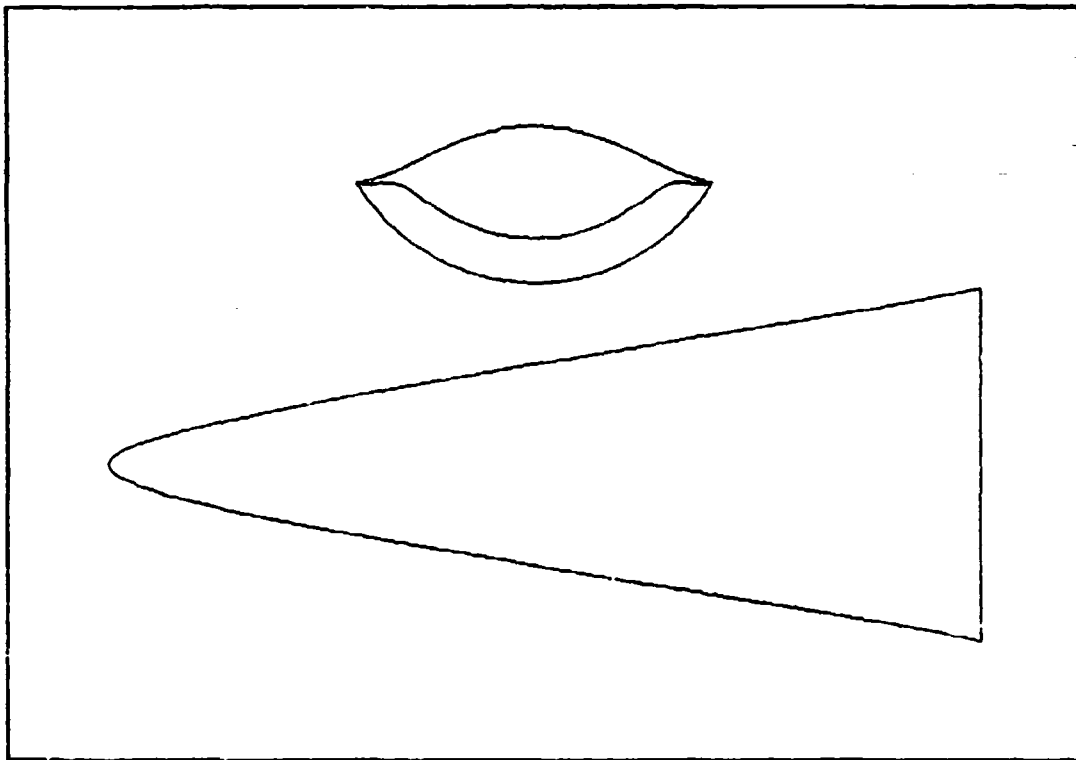


Figure B.6

Table B.6

$\Phi = 60.0$	$\Delta = 8.0$	$Mach = 10.0$	$Re = 0.10 \times 10^7$	$\Gamma = 1.40$
$X = 0.300 + 0.411 Y^2 + 0.000 Y^4 + -0.082 Y^6$				
$C_{ftav} = 0.001918$	$CL = 0.043578$	$CD = 0.009516$		
$S_w/S_p = 2.106905$	$V^{(2/3)}/S_p = 0.207258$	$(L/D)_{vis} = 4.579339$		
$\Delta b/\Delta b_1 = 0.843229$	$V/V_1 = 0.710444$	$S_p/S_{p1} = 0.871710$		
$b/l_w = 0.402313$	$SSD = 0.290236$			

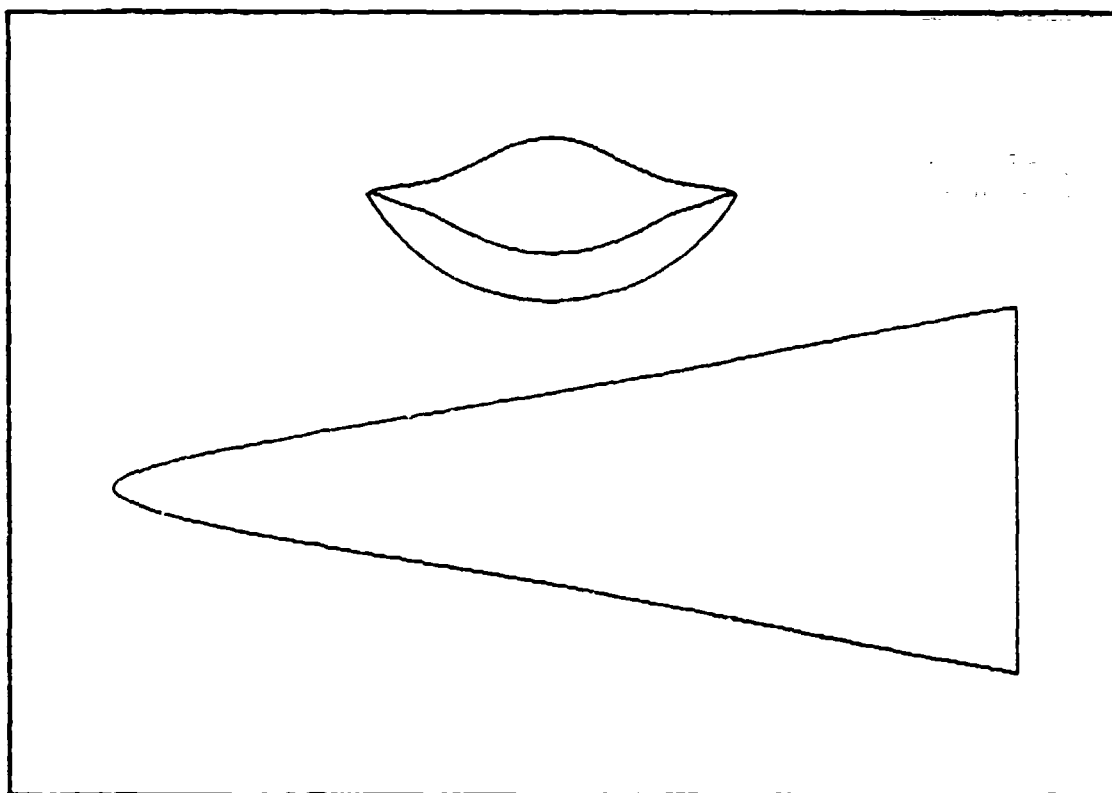


Figure B.7

Table B.7

Phi =60.0	Delta = 8.0	Kach =10.0	Rey = 0.10E+07	Gamma = 1.40
$X = 0.300 + 0.940 Y^2 + -1.000 Y^4 + 0.376 Y^6$				
Cftav = 0.001932	CL = 0.043448	CD = 0.009450		
Sw/Sp = 2.102324	V^(2/3)/Sp = 0.203256	(L/D)vis = 4.597888		
Ab/Ab1 = 0.798890	V/V1 = 0.847930	Sp/Sp1 = 0.835926		
b/lw = 0.409313	SSD = 0.256236			

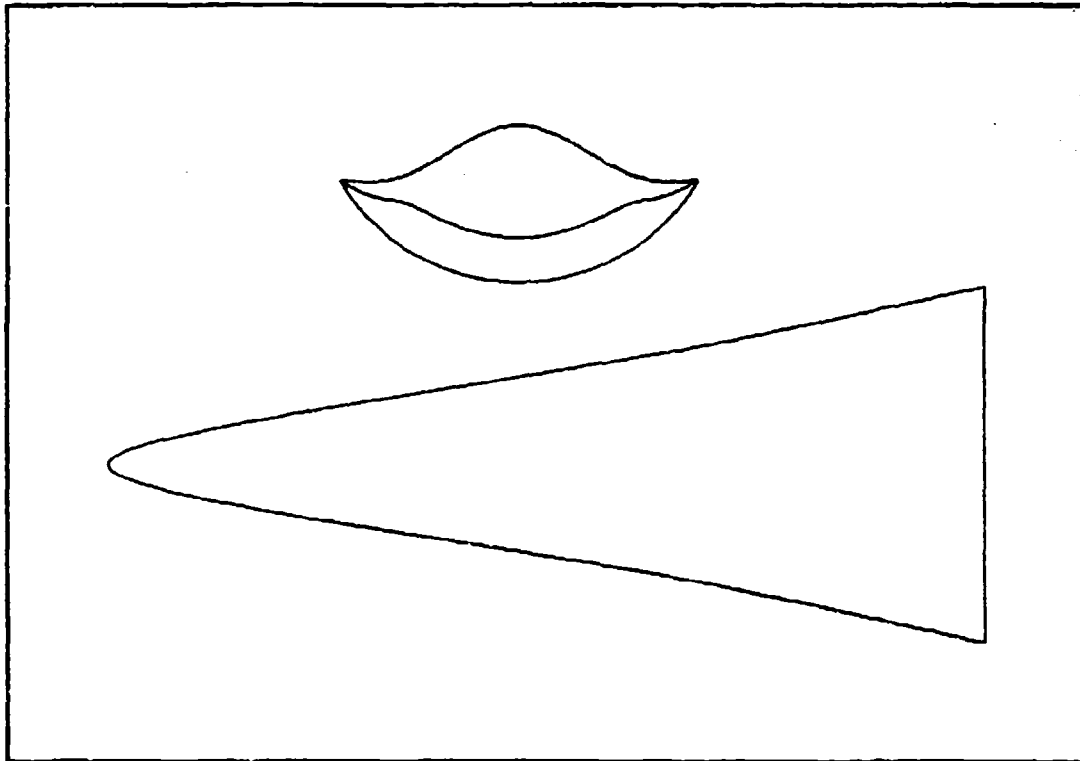


Figure B.8

Table B.8

Phi =60.0	Delta = 8.0	Mach =10.0	Rey = 0.10E+07	Gamma = 1.40
X = 0.300 + 1.056 Y^2 + -1.000 Y^4 + 0.306 Y^6				
Cftav = 0.001939	CL = 0.043437	CD = 0.009431		
Sw/Sp = 2.121517	V^(2/3)/Sf = 0.203593	(L/D)vis = 4.605786		
Ab/Abl = 0.763162	V/Vi = 0.618193	Sp/SpI = 0.808807		
b/iw = 0.409313	SSD = 0.290238			

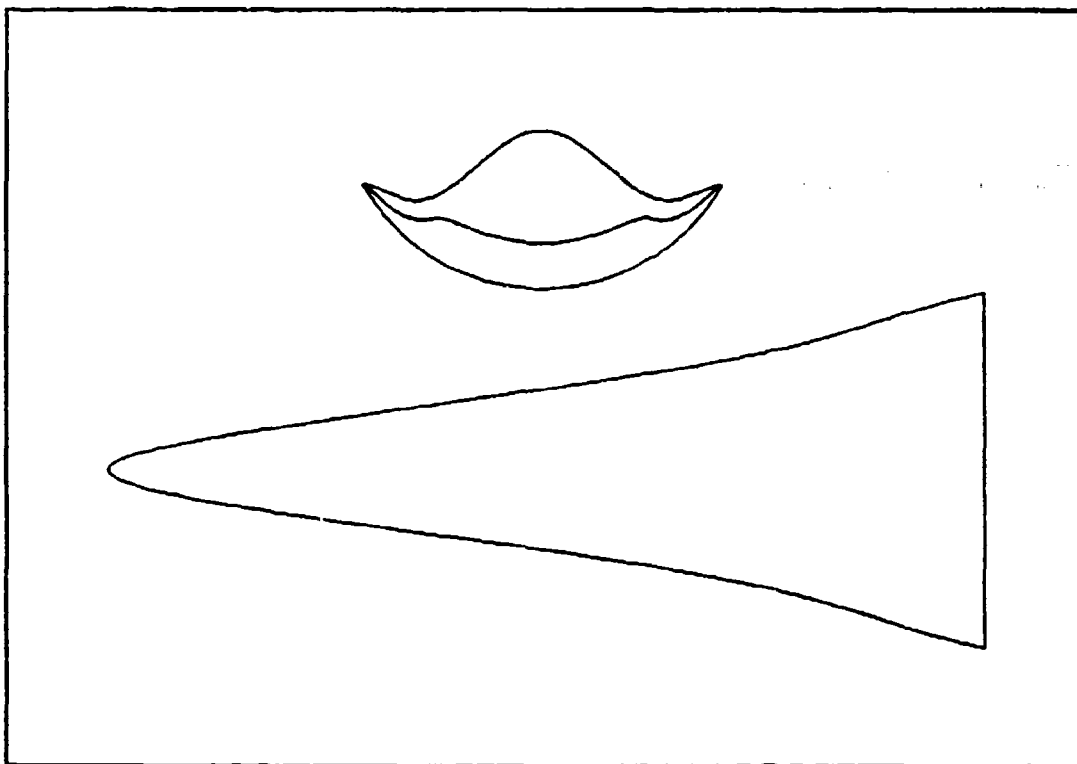


Figure B.9

Table B.9

Phi =60.0	Delta = 8.0	Mach =10.0	Rey = 0.10E+07	Gamma = 1.40
$X = 0.300 + 1.697 Y^2 + -2.000 Y^4 + 0.696 Y^6$				
Cftav = 0.001974	CL = 0.043324	CD = 0.009531		
Sw/Sp = 2.200773	V^(2/3)/Sp = 0.202816	(L/D)vis = 4.545457		
Ab/Abi = 0.684115	V/Vi = 0.538133	Sp/Sp1 = 0.740933		
b/lw = 0.409313	SBD = 0.290236			

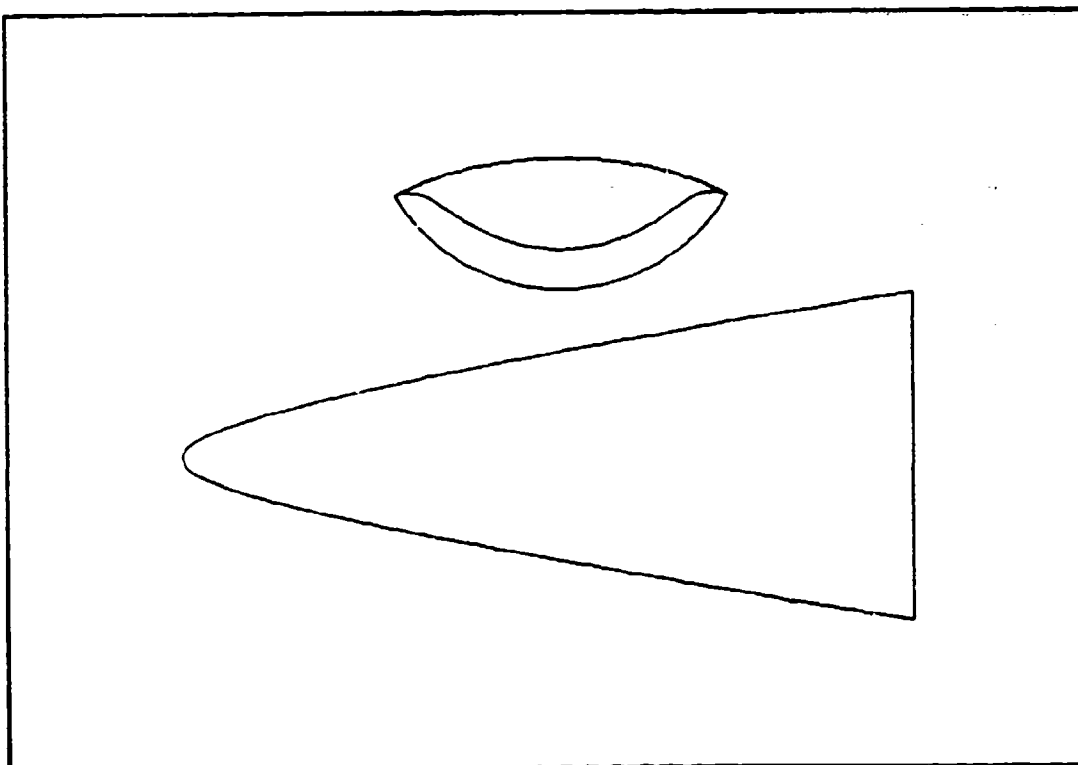


Figure B.10

Table B.10

Phi = 60.0	Delta = 8.0	Mach = 10.0	Rey = 0.10E+07	Gamma = 1.40
$I = 0.400 + 0.180 Y^2 + 0.000 Y^4 + 0.011 Y^6$				
Cftav = 0.001891	CL = 0.043239	CD = 0.009377		
Sw/Sp = 2.077541	V^(2/3)/Sp = 0.198999	(L/D)vis = 4.611255		
Ab/Abi = 0.806447	V/Vi = 0.621062	Sp/Sp1 = 0.830038		
b/lw = 0.454352	S8D = 0.276033			

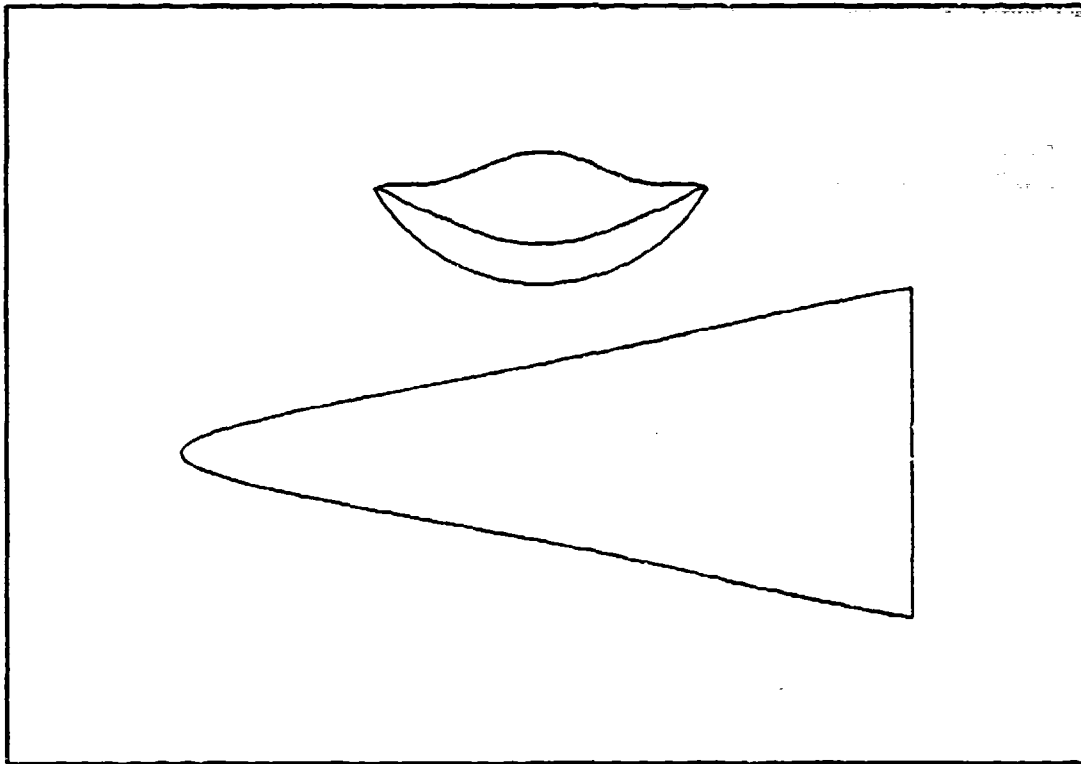


Figure B.11

Table B.11

Phi =60.0	Delta = 8.0	Mach =10.0	Rey = 0.10E+07	Gamma = 1.40
$I = 0.400 + 0.829 Y^2 + -1.000 Y^4 + 0.396 Y^6$				
Cftav = 0.001927	CL = 0.043063	CD = 0.009269		
Sw/Sp = 2.077201	$V^{(2/3)}/Sp = 0.194364$	(L/D)vis = 4.635796		
Ab/Abi = 0.724848	V/Vi = 0.530231	Sp/Sp1 = 0.764733		
b/lw = 0.454352	SSD = 0.276033			

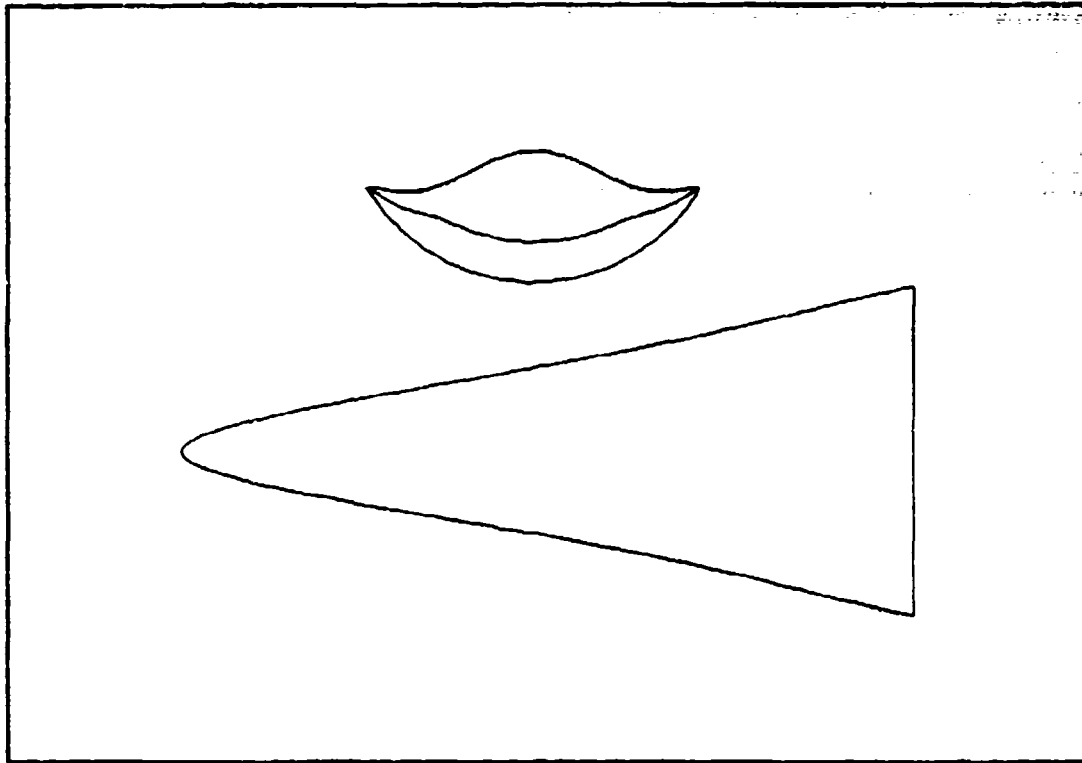


Figure B.12

Table B.12

Phi =60.0	Delta = 8.0	Mach =10.0	Rey = 0.10E+07	Gamma = 1.40
$X = 0.400 + 0.938 Y^2 + -1.000 Y^4 + 0.330 Y^6$				
Cftav = 0.001937	CL = 0.043048	CD = 0.009288		
Sw/Sp = 2.089441	V*(2/3)/Sp = 0.194770	(L/D)vis = 4.844742		
Ab/Abi = 0.891162	V/Vi = 0.504332	Sp/Sp1 = 0.738157		
b/lw = 0.454352	SSD = 0.276033			

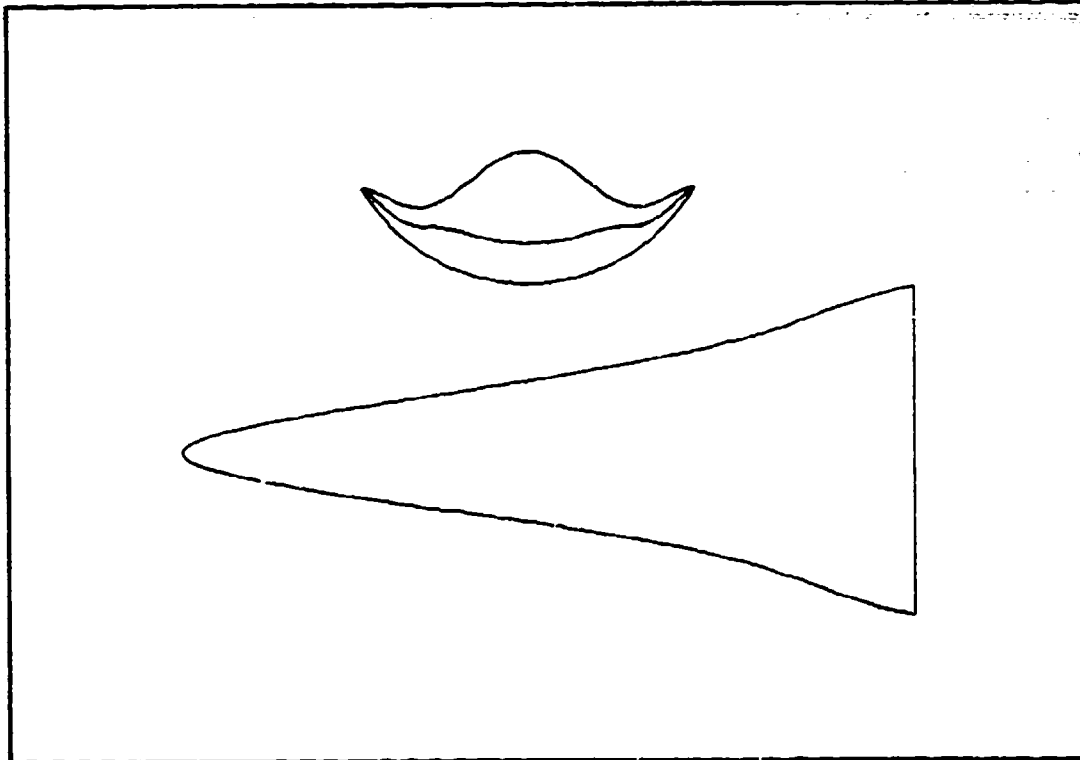


Figure B.13

Table B.13

Phi =60.0	Delta = 8.0	Mach =10.0	Rey = 0.10E+07	Gamma = 1.40
I = 0.400 + 1.577 Y^2 + -2.000 Y^4 + 0.721 Y^6				
Cftav = 0.001987	CL = 0.042925	CD = 0.009398		
Sw/Sp = 2.164243	V^(2/3)/Sp = 0.194121	(L/D)vis = 4.567488		
Ab/Abi = 0.612625	V/Vi = 0.432013	Sp/Sp1 = 0.668012		
b/lw = 0.454352	SSD = 0.276033			

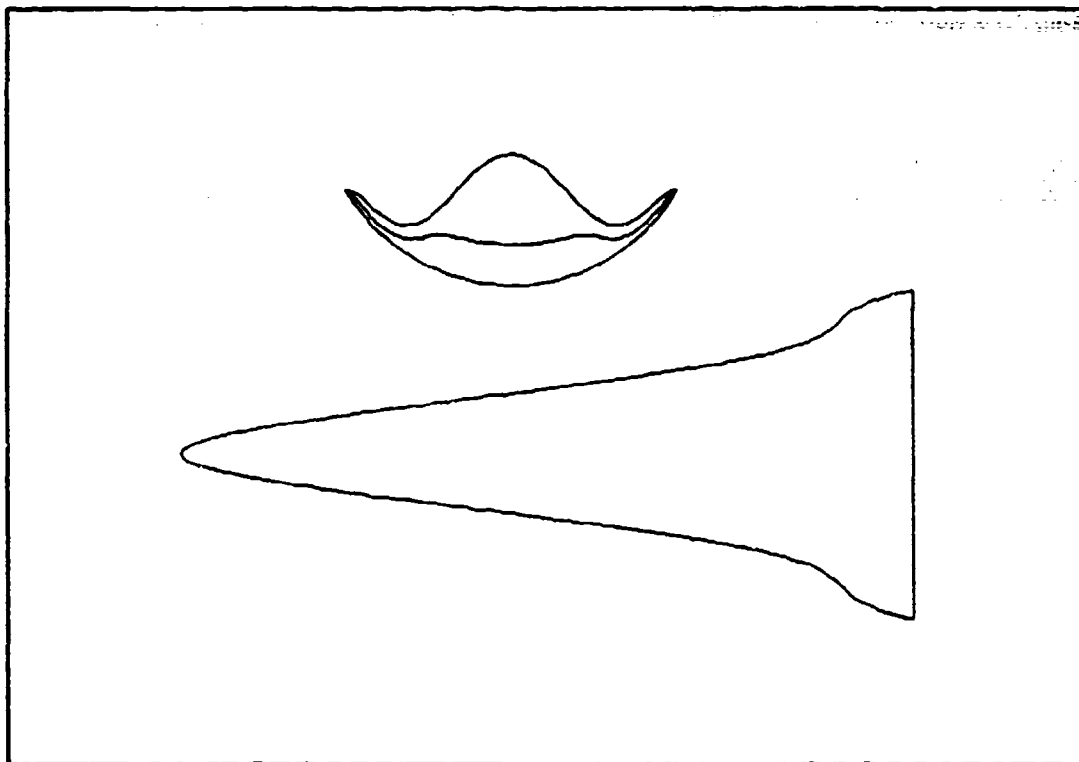


Figure B.14

Table B.14

Phi =60.0	Delta = 8.0	Mach =10.0	Rey = 0.10E+07	Gamma = 1.40
X = 0.400 + 2.220 Y^2 + -3.000 Y^4 + 1.110 Y^6				
Cftav = 0.002045	CL = 0.042875	CD = 0.009654		
Sw/Sp = 2.281403	V^(2/3)/Sp = 0.197759	(L/D)vis = 4.441051		
Ab/Abi = 0.533069	V/Vi = 0.371700	Sp/Sp1 = 0.593176		
b/lw = 0.454352	SSD = 0.276033			

APPENDIX C

Presented here are configurations that have the following parameters held fixed:

$$\phi_1 = 50, \quad \delta = 8, \quad M = 10, \quad \text{Re}_y = 1 \times 10^6$$

The following parameters are varied:

$$R_0 \text{ from } 0.3 \text{ to } 0.7$$

$$b_4 \text{ from } 0.0 \text{ to } -3.0$$

The values of b_2 and b_6 are such that equation 2-13 and condition (iii) holds.

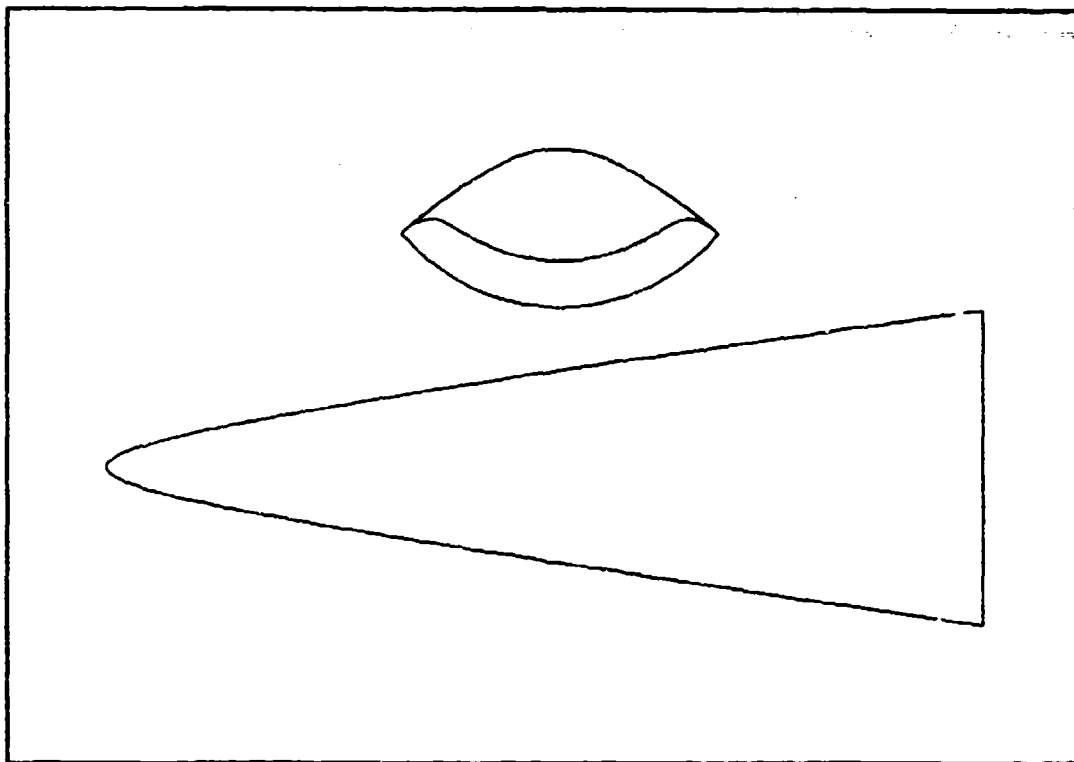


Figure C.1

Table C.1

Phi =50.0	Delta = 8.0	Mach =10.0	Rey = 0.10E+07	Gamma = 1.40
$X = 0.300 + 0.792 Y^2 + -0.400 Y^4 + 0.147 Y^6$				
Cftav = 0.001905	CL = 0.043600	CD = 0.009381		
Sw/Sp = 2.154487	V^(2/3)/Sp = 0.210144	(L/D)vis = 4.647765		
Ab/Ab1 = 0.885660	V/V1 = 0.754987	Sp/Sp1 = 0.896308		
b/lw = 0.362059	SSD = 0.290236			

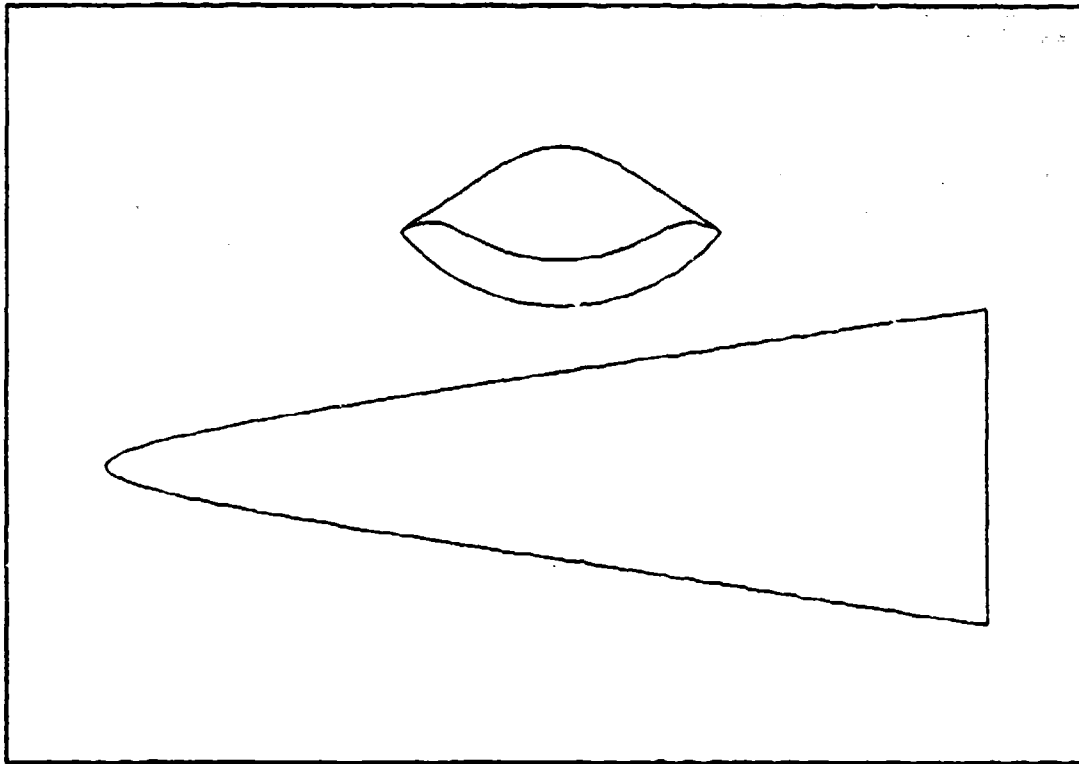


Figure C.2

Table C.2

Phi =50.0	Delta = 8.0	Mach =10.0	Rey = 0.10E+07	Gamma = 1.40
$X = 0.300 + 0.993 Y^2 + -0.800 Y^4 + 0.346 Y^6$				
Cftav = 0.001906	CL = 0.043558	CD = 0.009344		
Sw/Sp = 2.151257	V^(2/3)/Sp = 0.209198	(L/D)vis = 4.661775		
Ab/Abi = 0.865016	V/Vi = 0.729159	Sp/Spi = 0.879708		
b/lw = 0.362059	SSD = 0.290236			

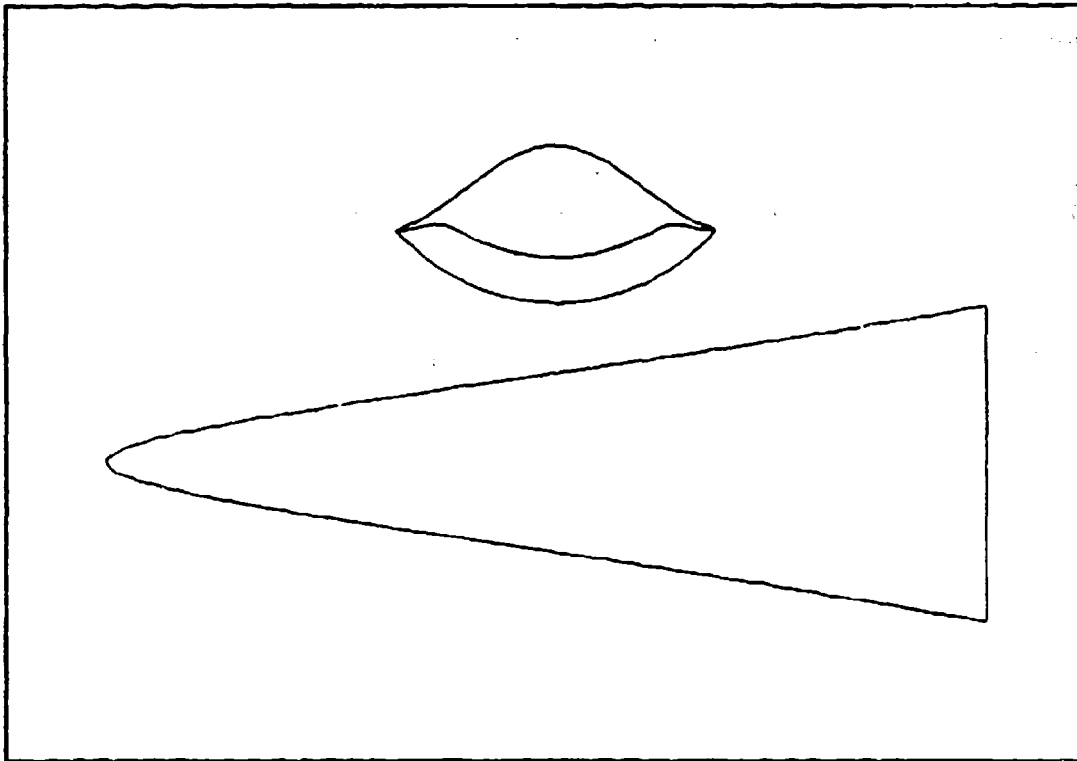


Figure C.3

Table C.3

Phi =50.0	Delta = 8.0	Mach =10.0	Rey = 0.10E+07	Gama = 1.40
$X = 0.300 + 1.100 Y^2 + -0.800 Y^4 + 0.240 Y^6$				
Cftav = 0.001908	CL = 0.043545	CD = 0.009335		
Sw/Sp = 2.167182	V*(2/3)/Sp = 0.209543	(L/D)vis = 4.664793		
Ab/Ab1 = 0.837507	V/V1 = 0.703896	Sp/Sp1 = 0.857857		
b/lw = 0.362059	SSD = 0.290236			

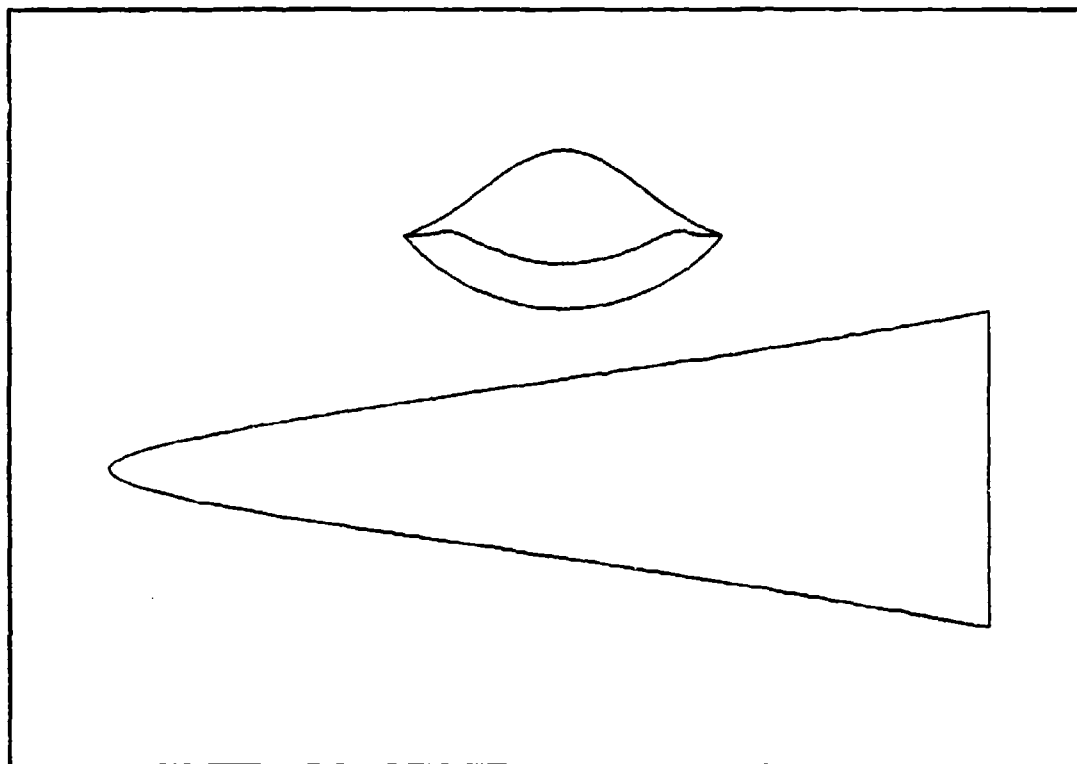


Figure C.4

Table C.4

Phi =50.0	Delta = 8.0	Mach =10.0	Rey = 0.10E+07	Gamma = 1.40
X = 0.300 + 1.201 Y^2 + -1.000 Y^4 + 0.339 Y^6				
Cftav = 0.001907	CL = 0.043525	CD = 0.009328		
Sw/Sp = 2.170346	V^(2/3)/Sp = 0.209224	(L/D)vis = 4.666131		
Ab/Abi = 0.827055	V/Vi = 0.691601	Sp/Sp1 = 0.849130		
b/lw = 0.362059	SSD = 0.290236			

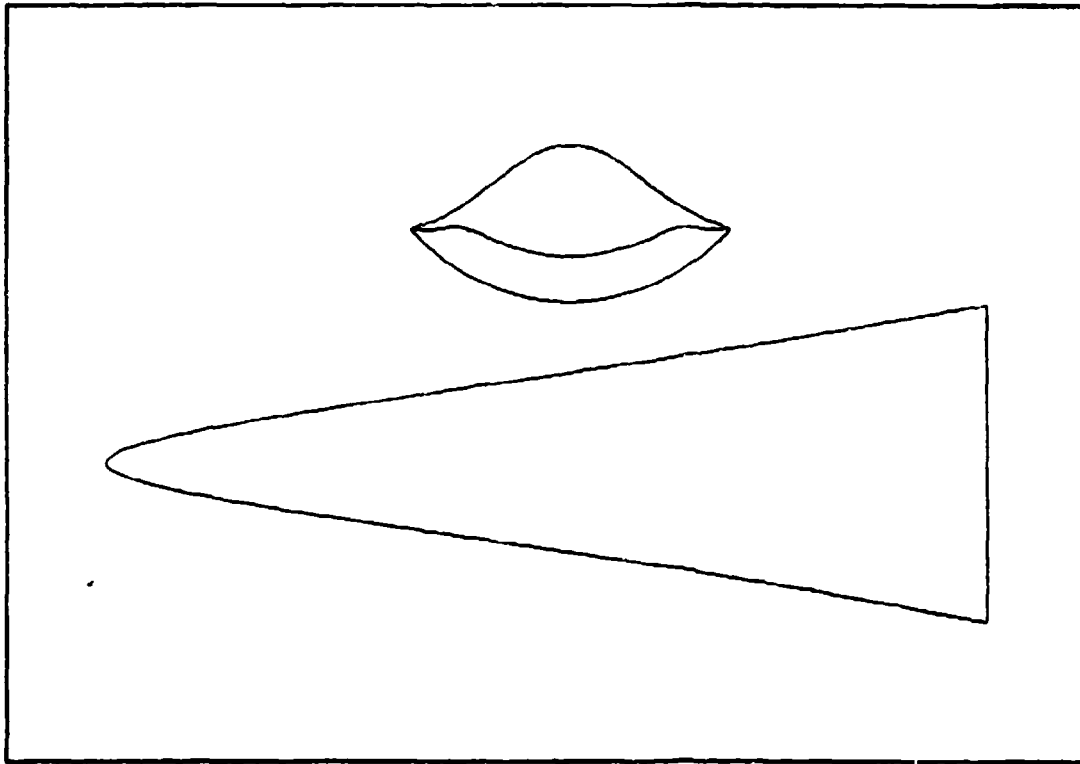


Figure C.5

Table C.5

Phi =50.0	Delta = 8.0	Mach =10.0	Rey = 0.10E+07	Gamma = 1.40
X = 0.300 + 1.302 Y^2 + -1.200 Y^4 + 0.438 Y^6				
Cftav = 0.001908	CL = 0.043507	CD = 0.009325		
Sw/Sp = 2.174980	V^(2/3)/Sp = 0.208944	(L/D)vis = 4.865699		
Ab/Abi = 0.816603	V/Vi = 0.879505	Sp/Spi = 0.840323		
b/lw = 0.382059	SSD = 0.290236			

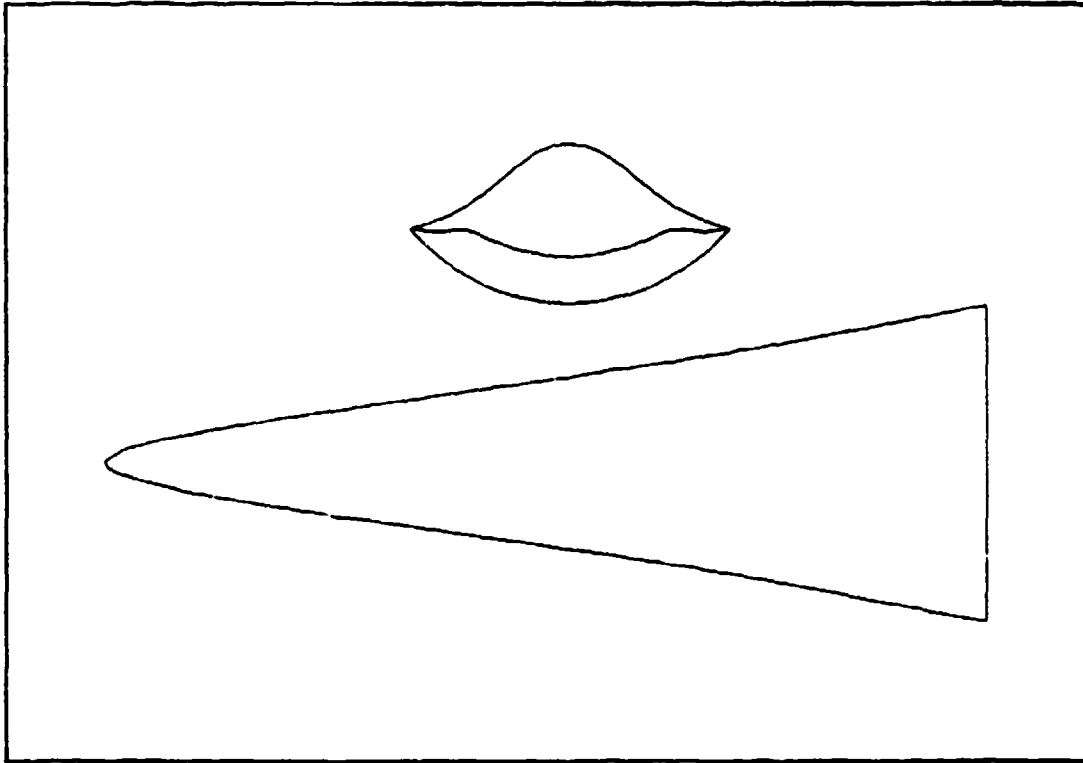


Figure C.6

Table C.6

Phi =50.0	Delta = 8.0	Mach =10.0	Rey = 0.10E+07	Gamma = 1.40
$I = 0.300 + 1.503 Y^2 + -1.600 Y^4 + 0.637 Y^6$				
Cftav = 0.001911	CL = 0.043470	CD = 0.009329		
Sw/Sp = 2.187994	V^(2/3)/Sp = 0.208499	(L/D)vis = 4.659933		
Ab/Abi = 0.795958	V/Vi = 0.656134	Sp/Spi = 0.822696		
b/lw = 0.362059	SSD = 0.290236			

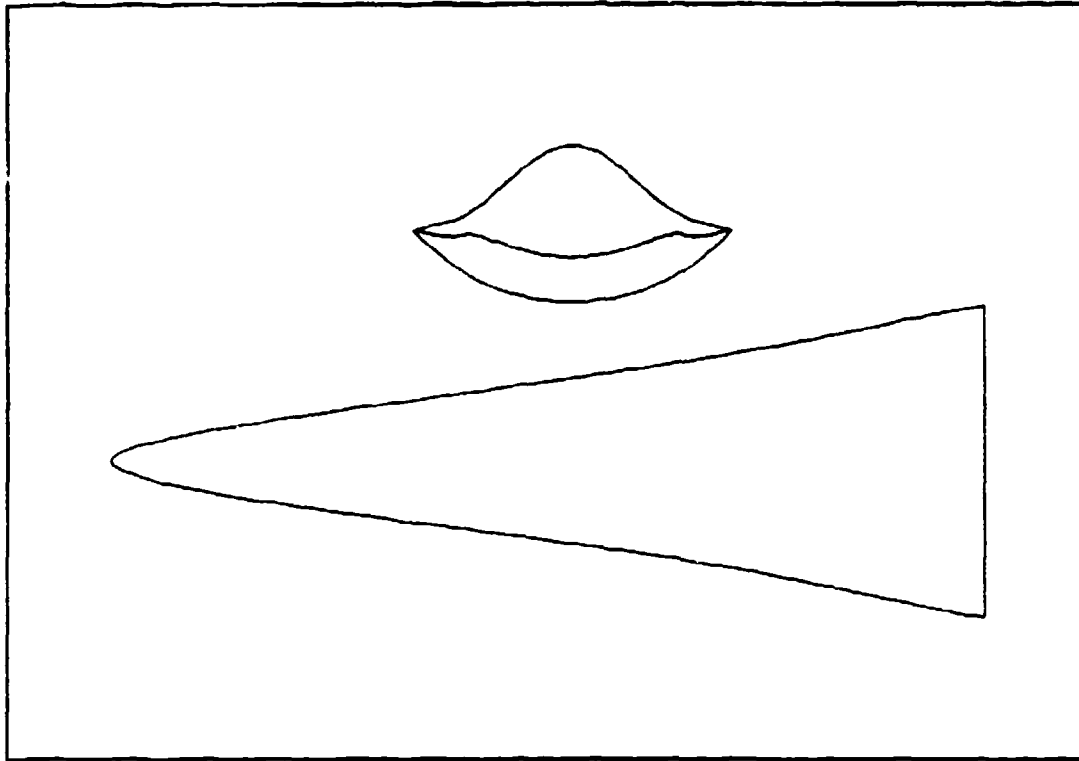


Figure C.7

Table C.7

Phi =50.0	Delta = 8.0	Mach =10.0	Rey = 0.10E+07	Gamma = 1.40
X = 0.300 + 1.704 Y^2 + -2.000 Y^4 + 0.836 Y^6				
Cftav = 0.001915	CL = 0.043437	CD = 0.009345		
Sw/Sp = 2.205945	V^(2/3)/Sp = 0.208223	(L/D)vis = 4.648007		
Ab/Abi = 0.775313	V/Vi = 0.633565	Sp/Spi = 0.804787		
b/lw = 0.362059	SSD = 0.290236			

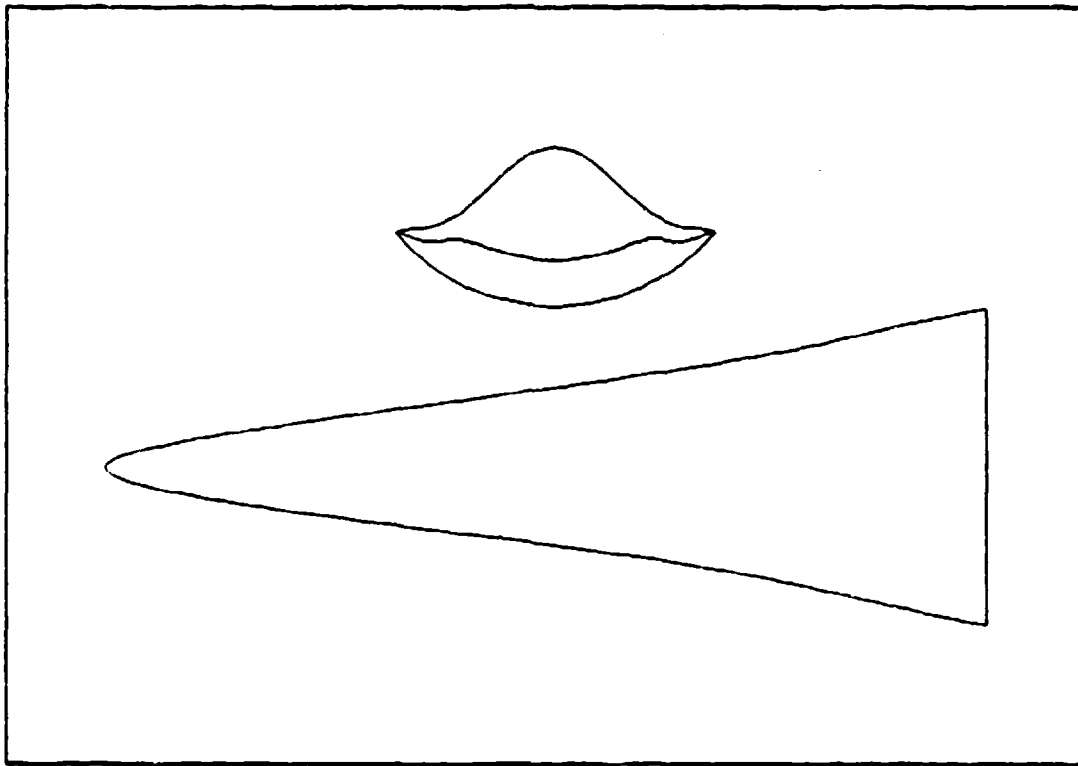


Figure C.8

Table C.8

Phi =50.0	Delta = 8.0	Mach =10.0	Rey = 0.10E+07	Gamma = 1.40
$X = 0.300 + 1.905 Y^2 + -2.400 Y^4 + 1.035 Y^6$				
Cftav = 0.001921	CL = 0.043405	CD = 0.009374		
Sw/Sp = 2.228375	$V^{(2/3)}/Sp = 0.208129$	(L/D)vis = 4.630399		
Ab/Abi = 0.754669	V/V1 = 0.611813	Sp/Spi = 0.788616		
b/lw = 0.362059	SSD = 0.290236			

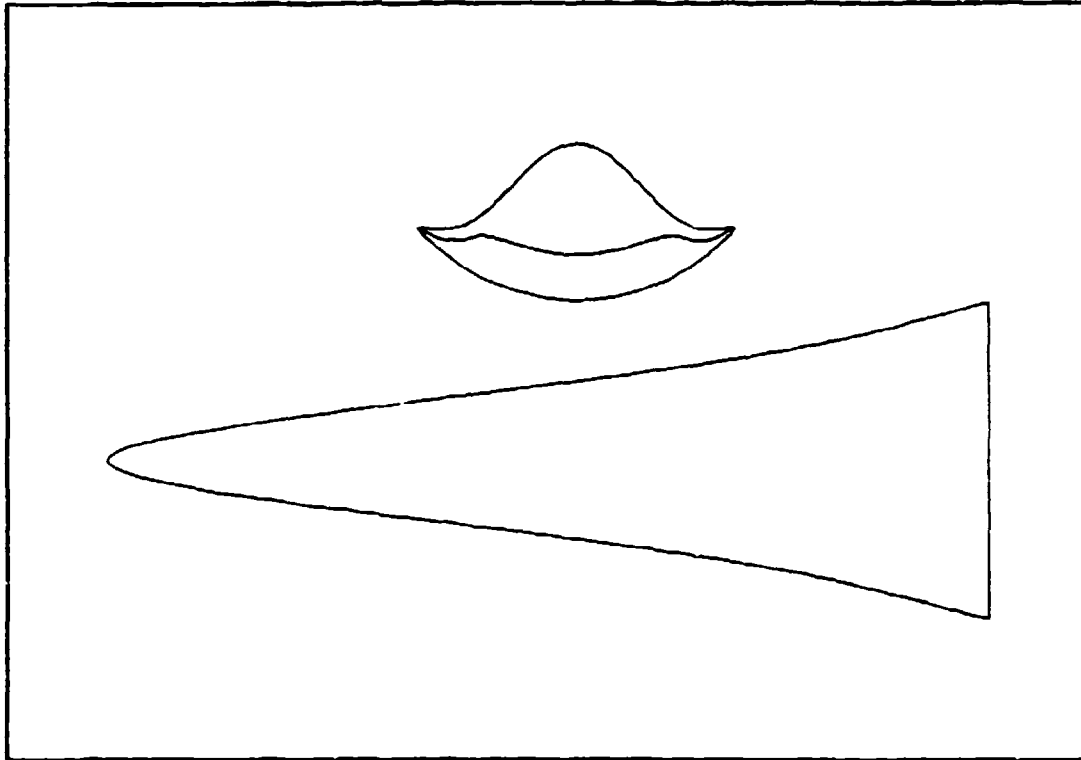


Figure C.9

Table C.9

Phi =50.0	Delta = 8.0	Mach =10.0	Rey = 0.10E+07	Gamma = 1.40
$X = 0.300 + 2.013 Y^2 + -2.400 Y^4 + 0.928 Y^6$				
Cftav = 0.001926	CL = 0.043415	CD = 0.009424		
Sw/Sp = 2.264482	$V^{(2/3)}/Sp = 0.209875$	(L/D)vis = 4.606875		
Ab/Abi = 0.728901	V/Vi = 0.591549	Sp/Spi = 0.762748		
b/lw = 0.362059	SSD = 0.290236			

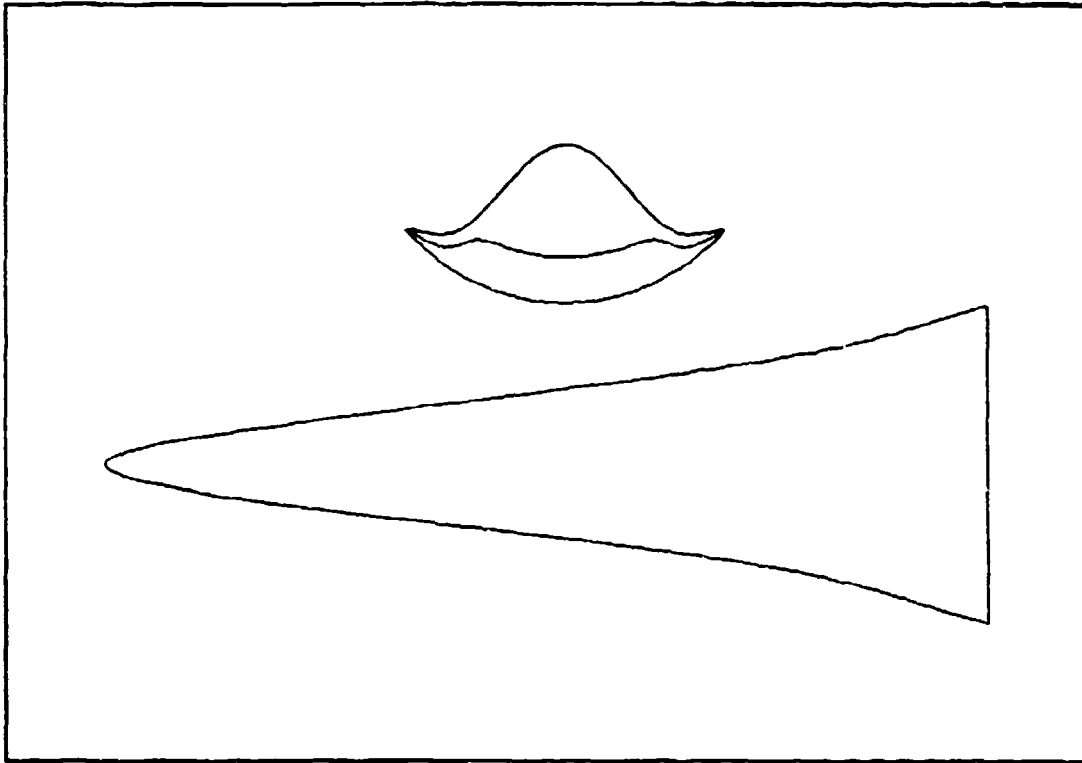


Figure C.10

Table C.10

Phi =50.0	Delta = 8.0	Mach =10.0	Rey = 0.10E+07	Gamma = 1.40
$X = 0.300 + 2.312 Y^2 + -3.000 Y^4 + 1.229 Y^6$				
Cftar = 0.001936	CL = 0.043382	CD = 0.009498		
Sw/Sp = 2.308484	V^(2/3)/Sp = 0.210525	(L/D)vis = 4.567349		
Ab/Abi = 0.696582	V/Vi = 0.562402	Sp/Spi = 0.735208		
b/lw = 0.362059	SSD = 0.290238			

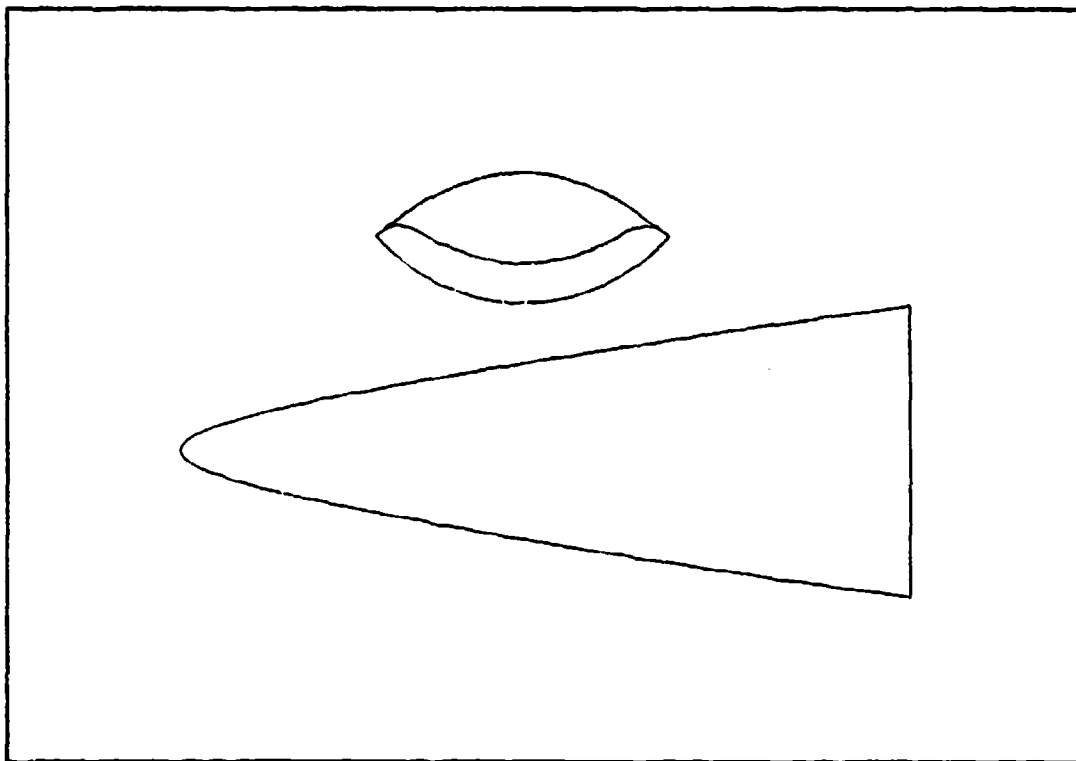


Figure C.11

Table C.11

Phi =50.0	Delta = 8.0	Mach =10.0	Rey = 0.10E+07	Gamma = 1.40
Y = 0.400 + 0.441 Y^2 + 0.000 Y^4 + -0.002 Y^6				
Cftav = 0.001882	CL = 0.043288	CD = 0.009180		
Sw/Sp = 2.106585	V^(2/3)/Sp = 0.202395	(L/D)vis = 4.713079		
Ab/Abi = 0.829852	V/Vi = 0.649641	Sp/Spi = 0.841907		
b/lw = 0.401898	SSD = 0.276033			

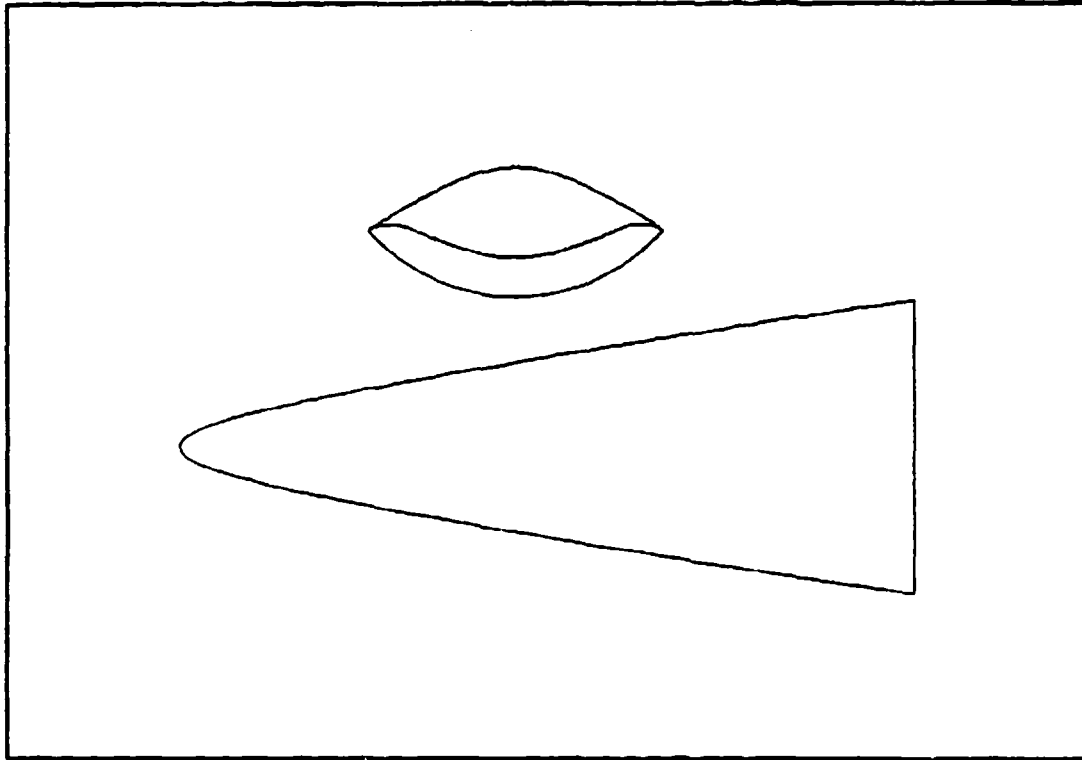


Figure C.12

Table C.12

Phi =50.0	Delta = 8.0	Mach =10.0	Rey = 0.10E+07	Gamma = 1.40
X = 0.400 + 0.642 Y^2 + -0.400 Y^4 + 0.197 Y^6				
Cftav = 0.001887	CL = 0.043220	CD = 0.009145		
Sw/Sp = 2.093222	V^(2/3)/Sp = 0.201318	(L/D)vis = 4.726161		
Ab/Abi = 0.809208	V/Vi = 0.624954	Sp/Spi = 0.824831		
b/lw = 0.401898	SSD = 0.276033			

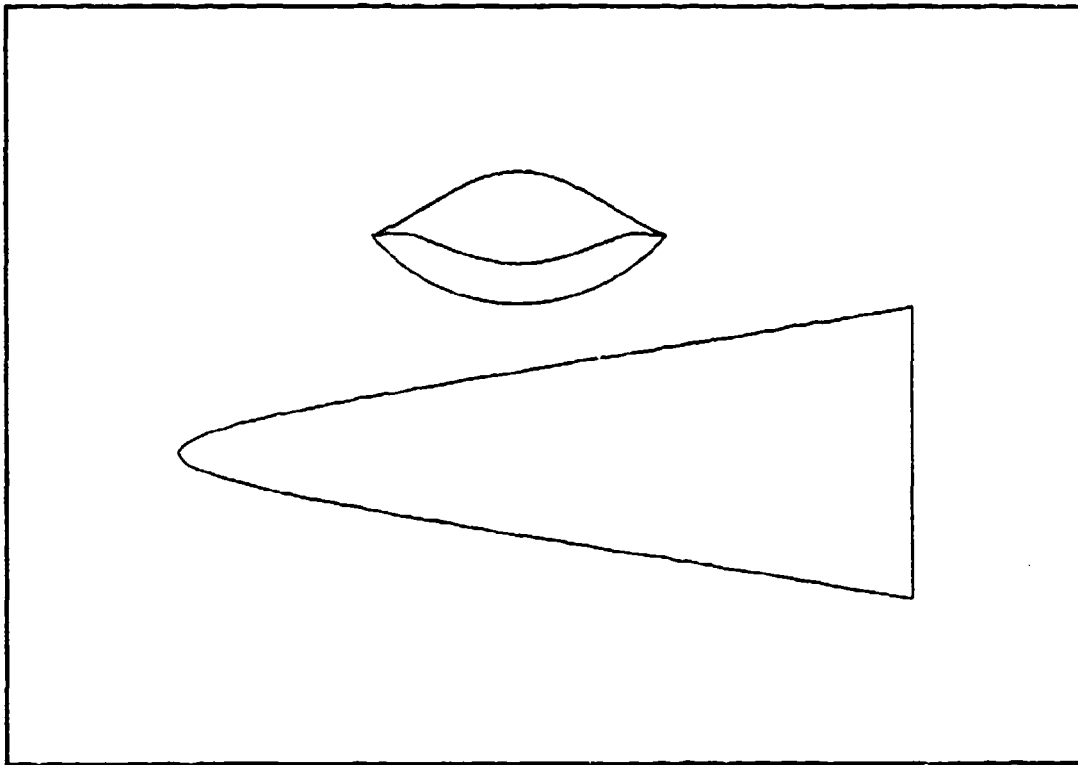


Figure C.13

Table C.13

Phi =50.0	Delta = 8.0	Mach =10.0	Rey = 0.10E+07	Gamma = 1.40
I = 0.400 + 0.750 Y^2 + -0.400 Y^4 + 0.090 Y^6				
Cftav = 0.501889	CL = 0.043199	CD = 0.009122		
Sw/Sp = 2.106453	V^(2/3)/Sp = 0.201476	(L/D)vis = 4.735799		
Ab/Abi = 0.781440	V/Vi = 0.603359	Sp/Spi = 0.802415		
b/lw = 0.401898	SSD = 0.276033			

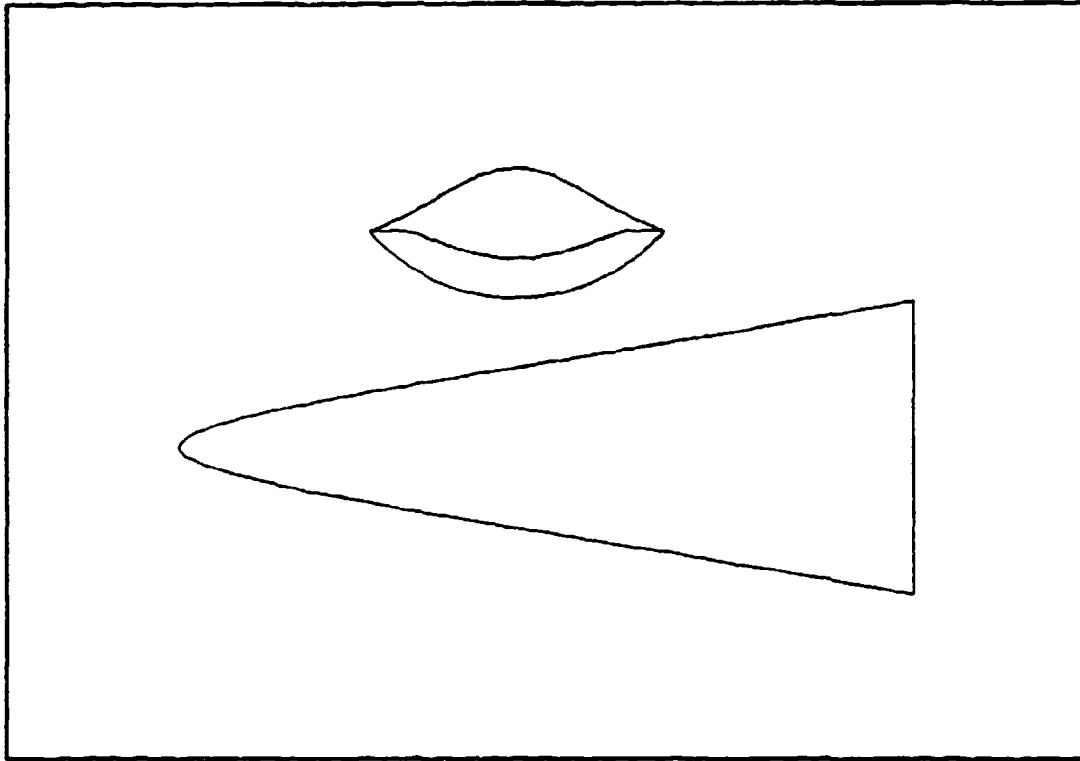


Figure C.14

Table C.14

Phi =50.0	Delta = 8.0	Mach =10.0	Rey = 0.108+07	Gamma = 1.40
I = 0.400 + 0.851 Y^2 + -0.600 Y^4 + 0.189 Y^6				
Cftav = 0.001892	CL = 0.043177	CD = 0.009115		
Sw/Sp = 2.107503	V^(2/3)/Sp = 0.201090	(L/D)vis = 4.736885		
Ab/Abi = 0.770988	V/Vi = 0.588658	Sp/Spi = 0.793473		
b/lw = 0.401898	SSD = 0.276033			

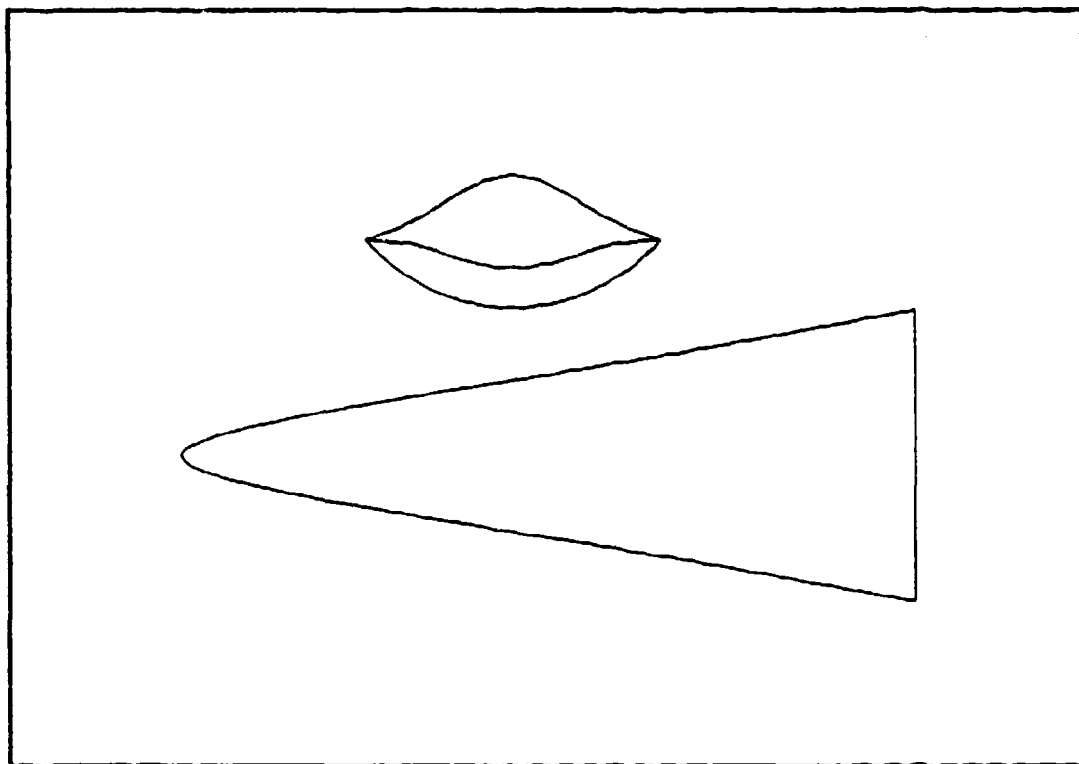


Figure C.15

Table C.15

Phi =50.0	Delta = 8.0	Mach =10.0	Rey = 0.10E+07	Gamma = 1.40
$X = 0.400 + 1.052 Y^2 + -1.000 Y^4 + 0.388 Y^6$				
Cftav = 0.001898	CL = 0.043133	CD = 0.009111		
Sw/Sp = 2.113615	V^(2/3)/Sp = 0.200432	(L/D)vis = 4.734126		
Ab/Abi = 0.750343	V/Vi = 0.566081	Sp/Spi = 0.775592		
b/lw = 0.401898	SSD = 0.276033			

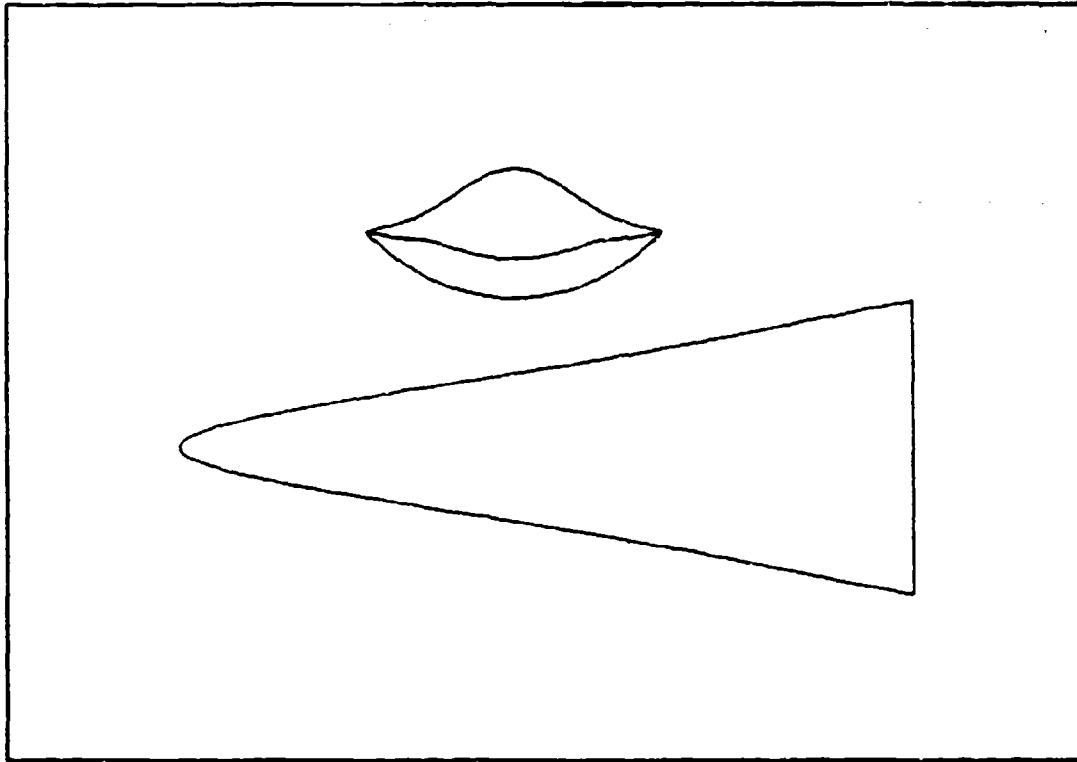


Figure C.16

Table C.16

Phi = 50.0	Delta = 8.0	Mach = 10.0	Rey = 0.10E+07	Gamma = 1.40
$Y = 0.400 + 1.253 Y^2 + -1.400 Y^4 + 0.587 Y^6$				
Cftav = 0.001905	CL = 0.043092	CD = 0.009120		
Sw/Sp = 2.124808	V^(2/3)/Sp = 0.199939	(L/D)vis = 4.725195		
Ab/Abi = 0.729698	V/Vi = 0.544315	Sp/Sp1 = 0.757447		
b/lw = 0.401898	SSD = 0.276033			

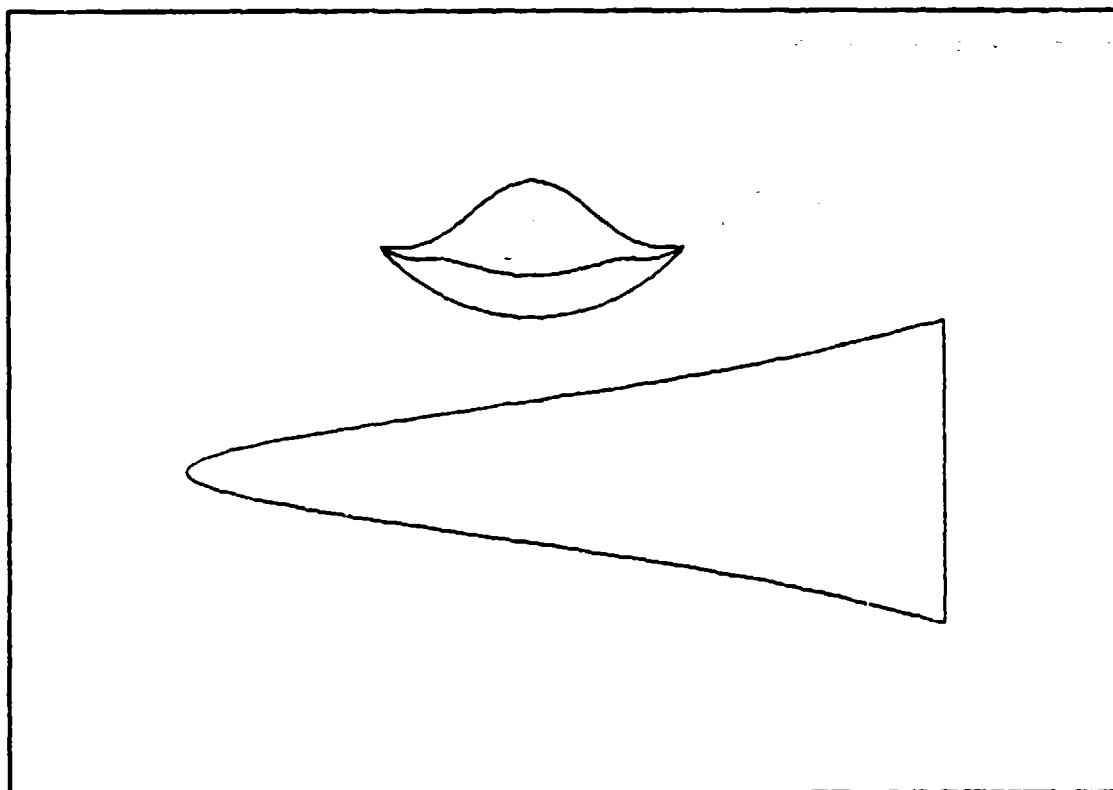


Figure C.17

Table C.17

Phi =50.0	Delta = 8.0	Mach =10.0	Rey = 0.10E+07	Gamma = 1.40
$X = 0.400 + 1.562 Y^2 + -1.800 Y^4 + 0.679 Y^6$				
Cftav = 0.001919	CL = 0.043054	CD = 0.009171		
Sw/Sp = 2.167452	V*(2/3)/Sp = 0.201086	(L/D)vis = 4.694574		
Ab/Abi = 0.681286	V/Vi = 0.503584	Sp/Sp1 = 0.715070		
b/lw = 0.401898	SSD = 0.276033			

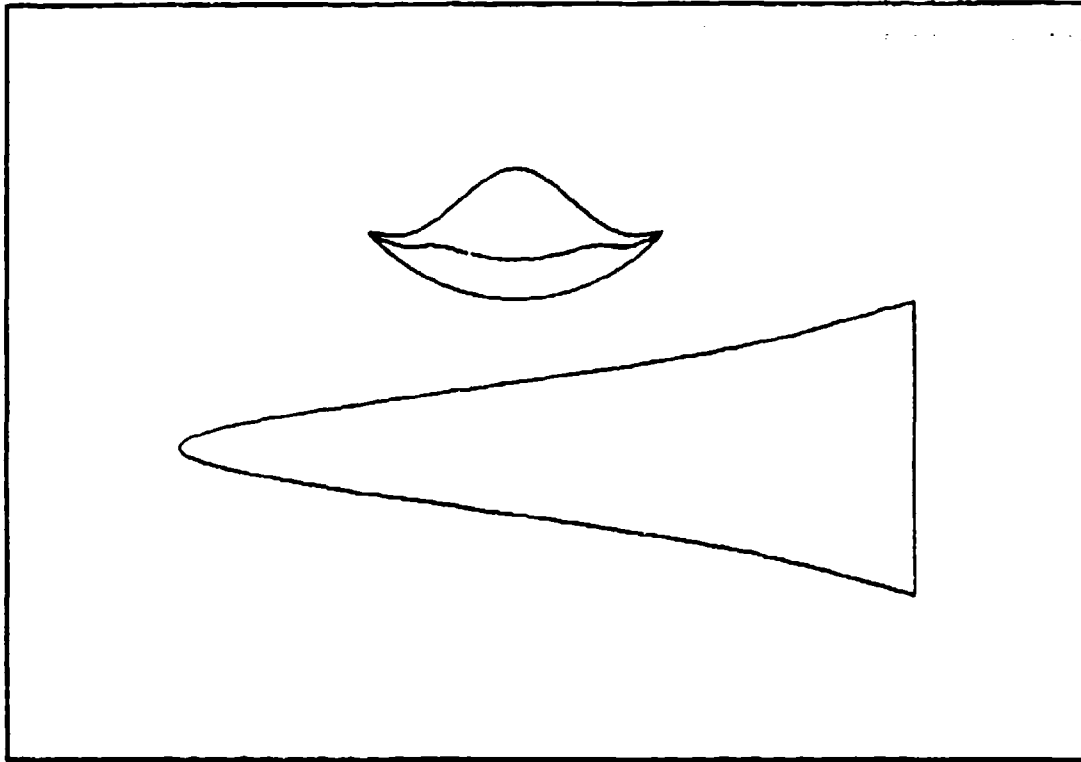


Figure C.18

Table C.18

Phi =50.0	Delta = 8.0	Mach =10.0	Rey = 0.10E+07	Gamma = 1.40
$X = 0.400 + 1.763 Y^2 + -2.200 Y^4 + 0.878 Y^6$				
Cftav = 0.001928	CL = 0.043024	CD = 0.009211		
Sw/Sp = 2.190453	V*(2/3)/Sp = 0.201283	(L/D)vis = 4.671057		
Ab/Abi = 0.660641	V/Vi = 0.484482	Sp/Sp1 = 0.696187		
b/lw = 0.401896	SSD = 0.276033			

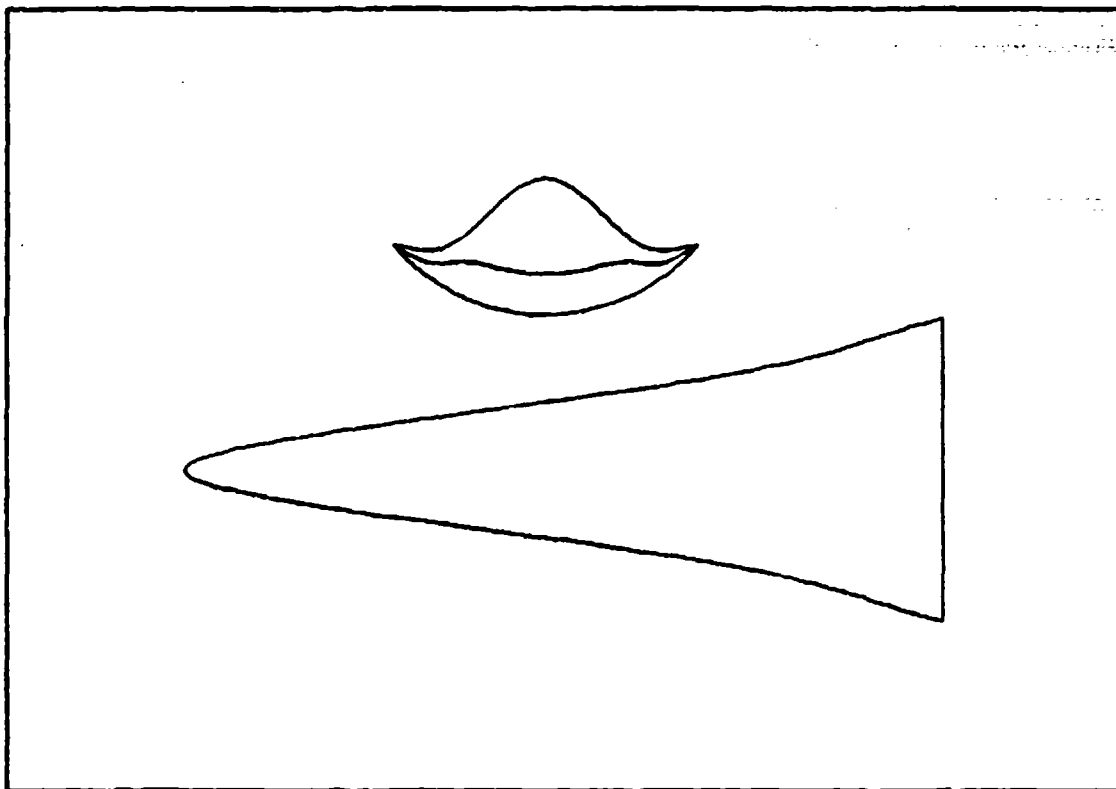


Figure C.19

Table C.19

Phi =50.0	Delta = 8.0	Mach =10.0	Rey = 0.10E+07	Gamma = 1.40
$X = 0.400 + 1.984 Y^2 + -2.800 Y^4 + 1.077 Y^6$				
Cftar = 0.001938	CL = 0.042999	CD = 0.009261		
Sw/Sp = 2.217187	V*(2/3)/Sp = 0.201728	(L/D)vis = 4.843071		
Ab/Ab1 = 0.639998	V/V1 = 0.466241	Sp/Sp1 = 0.677104		
b/lw = 0.401898	SSD = 0.276033			

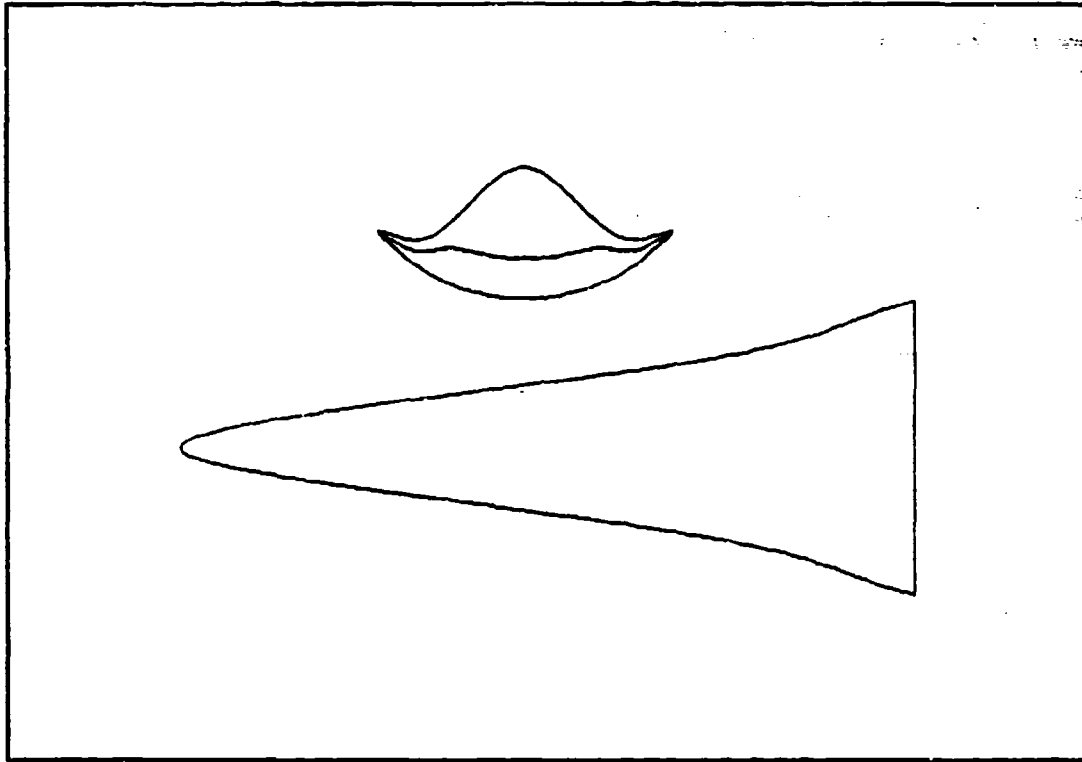


Figure C.20

Table C.20

$\Phi = 50.0$	$\Delta = 8.0$	$Mach = 10.0$	$Re_\gamma = 0.10E+07$	$\Gamma = 1.40$
$X = 0.400 + 2.165 Y^2 + -3.000 Y^4 + 1.276 Y^6$				
$C_{ftav} = 0.001948$	$CL = 0.042978$	$CD = 0.009321$		
$S_w/S_p = 2.247389$	$V^{(2/3)}/S_p = 0.202447$	$(L/D)_{vis} = 4.611121$		
$\Delta b/\Delta b_1 = 0.619351$	$V/V_1 = 0.448869$	$S_p/S_{p1} = 0.657835$		
$b/l_w = 0.401898$	$S_{SD} = 0.278033$			

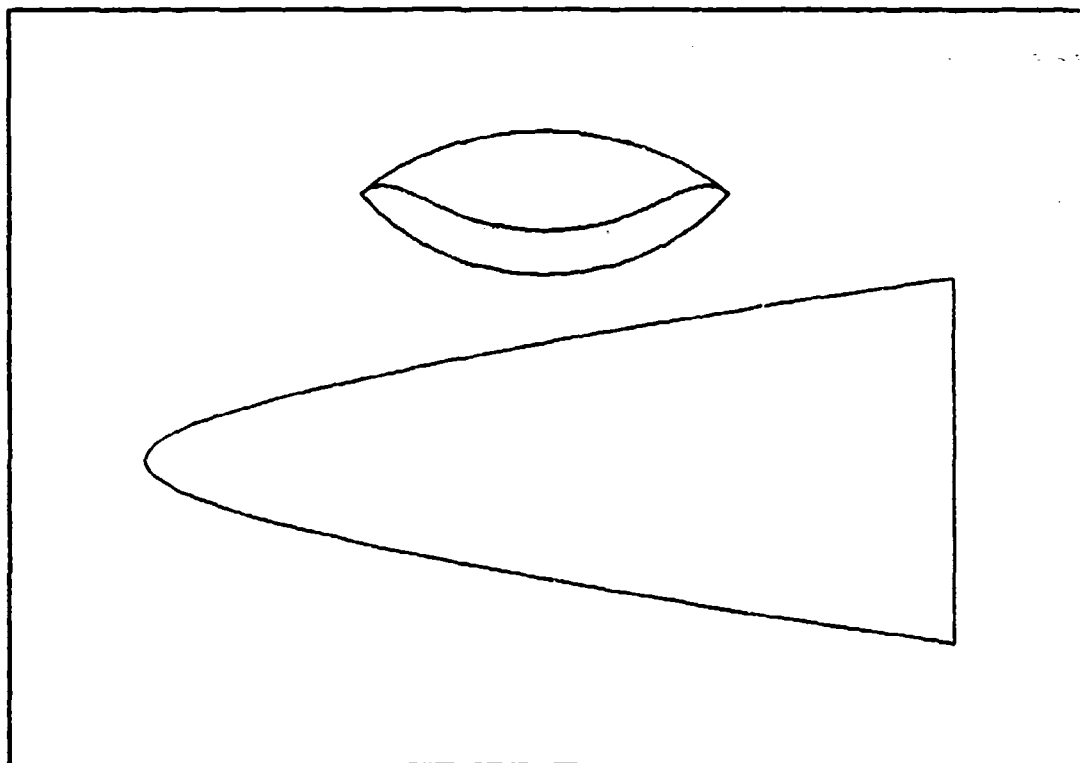


Figure C.21

Table C.21

Phi =50.0	Delta = 0.0	Mach =10.0	Rey = 0.10E+07	Gamma = 1.40
$X = 0.500 + 0.292 Y^2 + 0.000 Y^4 + 0.047 Y^6$				
Citav = 0.001862	CL = 0.042867	CD = 0.008987		
Sw/Sp = 2.070644	V^(2/3)/Sp = 0.193480	(L/D)vis = 4.769799		
Ab/Abi = 0.753140	V/Vi = 0.529250	Sp/Sp1 = 0.768223		
b/lw = 0.451589	SSD = 0.258054			

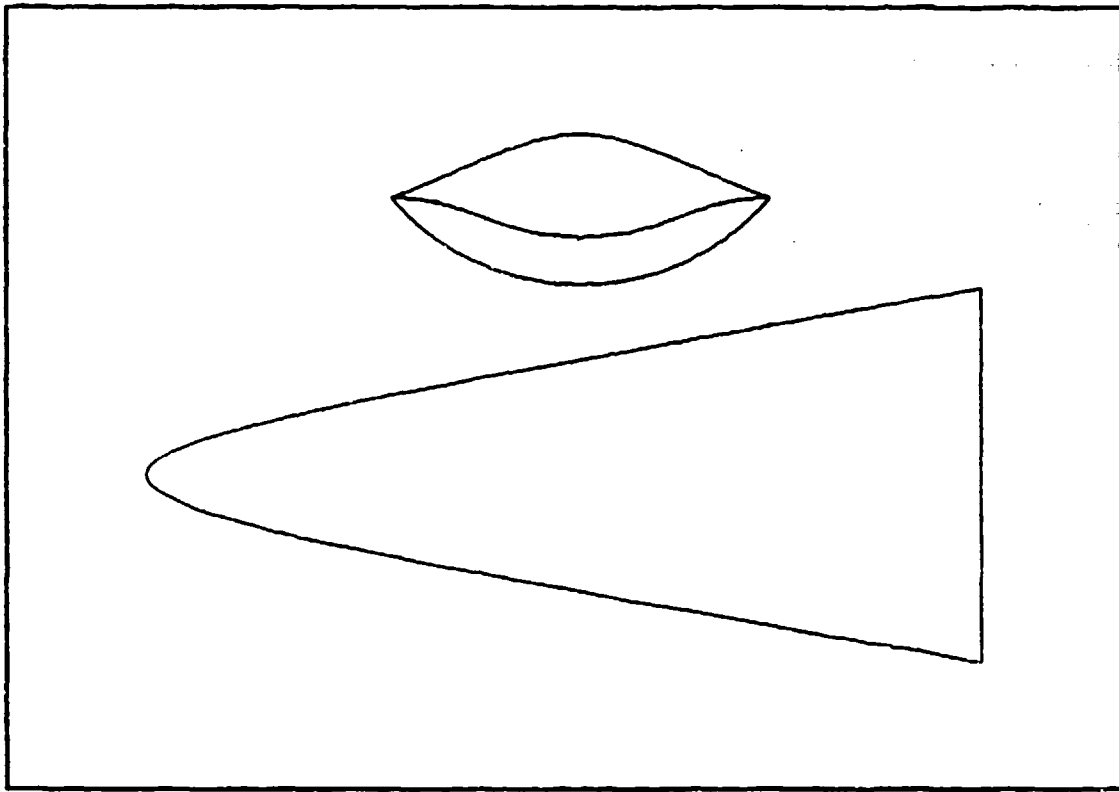


Figure C.22

Table C.22

Phi =50.0	Delta = 8.0	Mach =10.0	Rey = 0.10E+07	Gamma = 1.40
$X = 0.500 + 0.601 Y^2 + -0.400 Y^4 + 0.139 Y^6$				
Cftav = 0.001877	CL = 0.042788	CD = 0.008942		
Sw/Sp = 2.067719	V^(2/3)/Sp = 0.192469	(L/D)vis = 4.784768		
Ab/Abi = 0.704728	V/Vi = 0.483838	Sp/Spi = 0.727426		
b/lw = 0.451589	SSD = 0.258054			

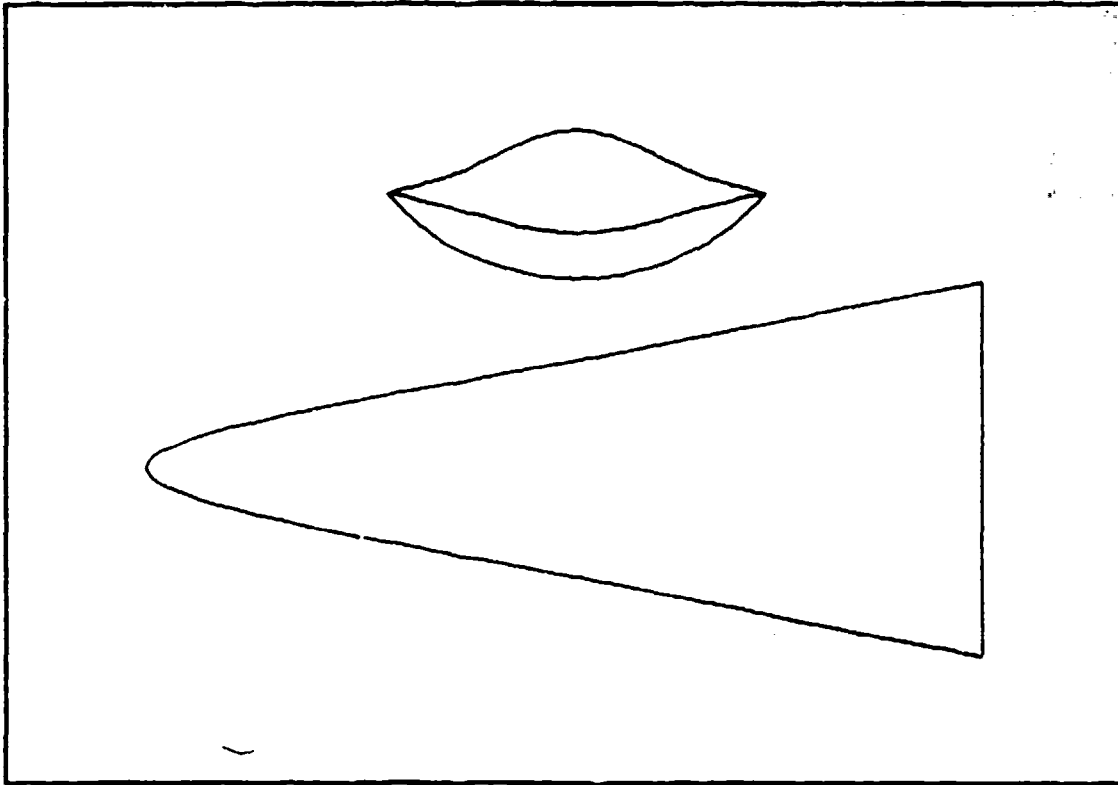


Figure C.23

Table C.23

Phi =50.0	Delta = 8.0	Mach =10.0	Rey = 0.10E+07	Gamma = 1.40
X = 0.500 + 0.903 Y^2 + -1.000 Y^4 + 0.437 Y^6				
Cftav = 0.001894	CL = 0.042716	CD = 0.008949		
Sw/Sp = 2.075381	V^(2/3)/Sp = 0.191391	(L/D)vis = 4.773218		
Ab/Abi = 0.873631	V/Vi = 0.452848	Sp/SpI = 0.699733		
b/lw = 0.451589	SSD = 0.258054			

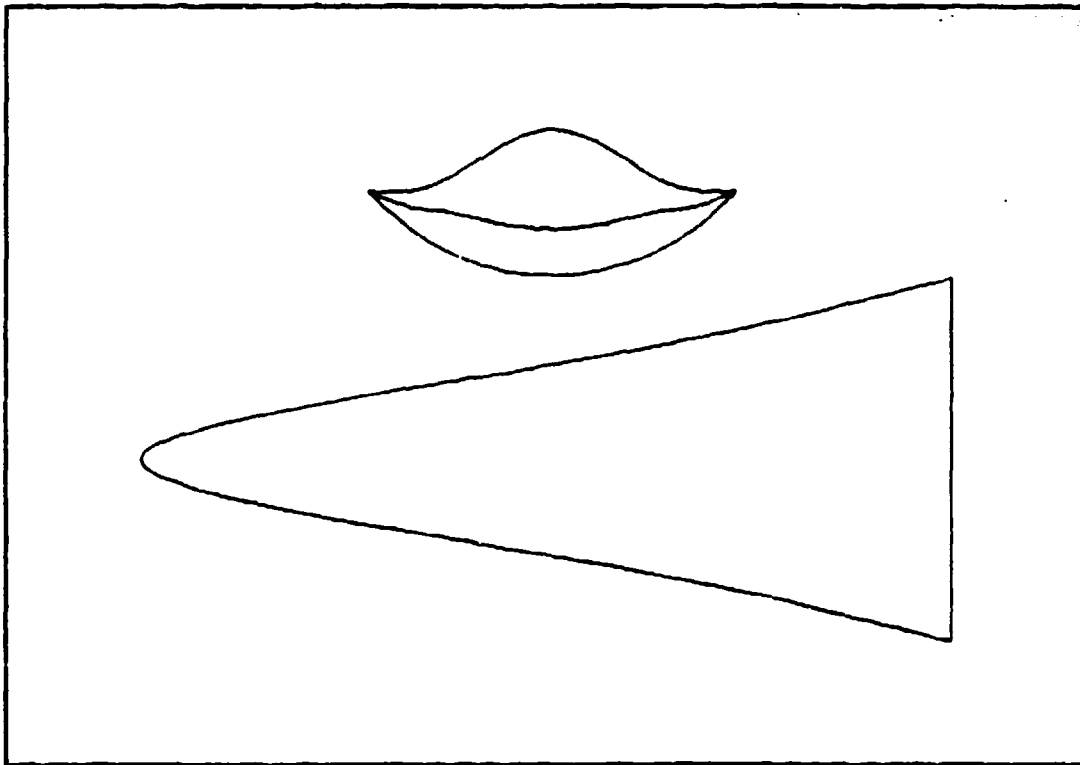


Figure C.24

Table C.24

Phi =50.0	Delta = 8.0	Mach =10.0	Rey = 0.10E+07	Gamma = 1.40
$X = 0.500 + 1.212 Y^2 + -1.400 Y^4 + 0.529 Y^6$				
Cftar = 0.001915	CL = 0.042664	CD = 0.008987		
Sw/Sp = 2.105614	V^(2/3)/Sp = 0.192161	(L/D)vis = 4.747234		
Ab/Abi = 0.625218	V/Vi = 0.414169	Sp/Sp1 = 0.656853		
b/lw = 0.451589	SSD = 0.258054			

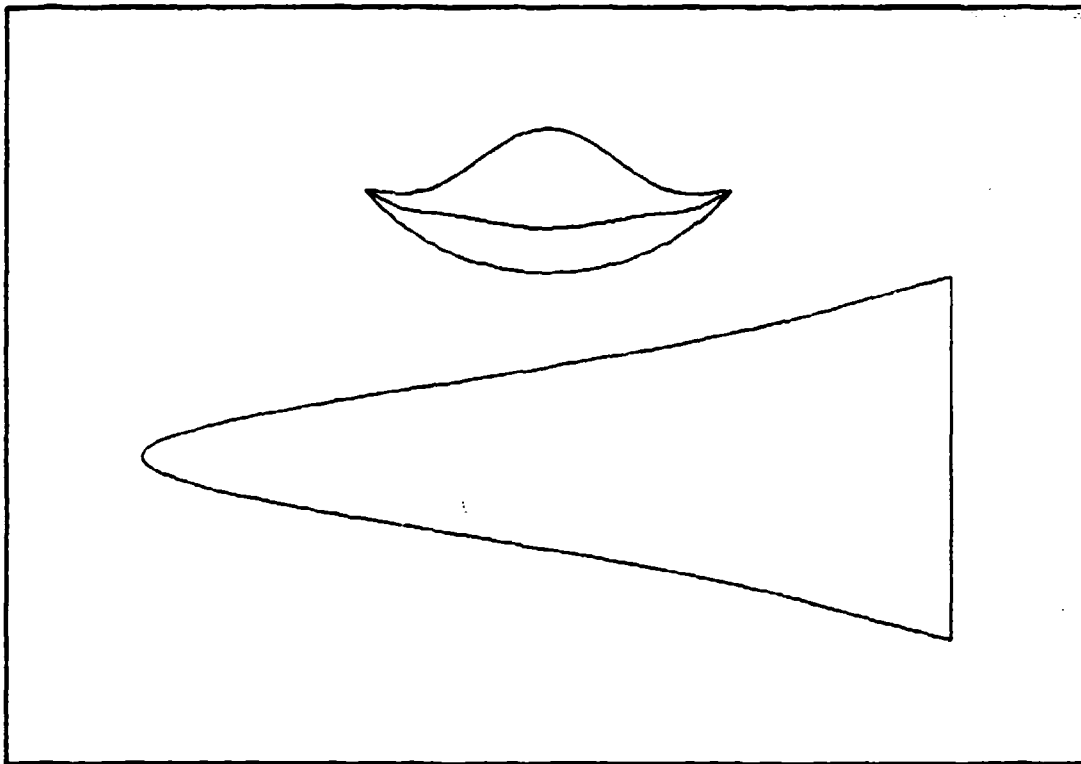


Figure C.25

Table C.25

Phi = 50.0	Delta = 8.0	Mach = 10.0	Rey = 0.10E+07	Gamma = 1.40
$I = 0.500 + 1.413 Y^2 + -1.800 Y^4 + 0.728 Y^6$				
Cftav = 0.001927	CL = 0.042628	CD = 0.009025		
Sw/Sp = 2.124140	V^(2/3)/Sp = 0.192207	(L/D)vis = 4.723290		
Ab/Abi = 0.604573	V/Vi = 0.396348	Sp/Sp1 = 0.637721		
b/lw = 0.451589	SSD = 0.258054			

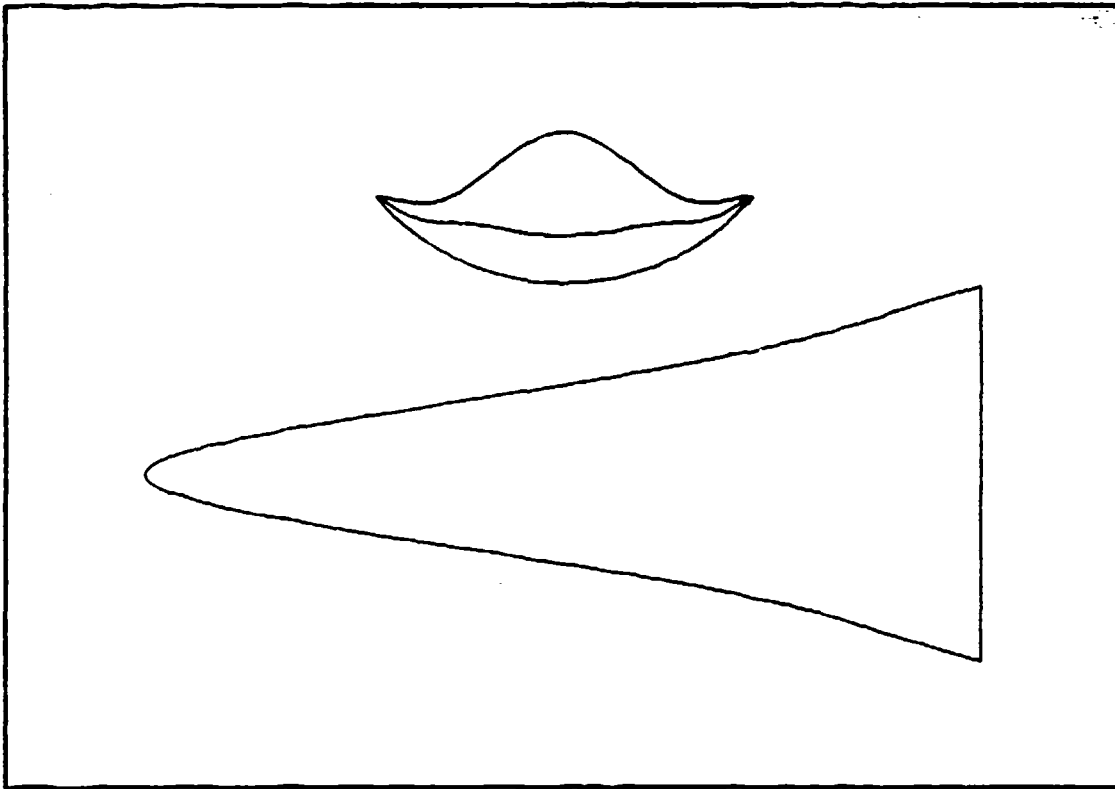


Figure C.26

Table C.26

Phi =50.0	Delta = 8.0	Mach =10.0	Rey = 0.10E+07	Gamma = 1.40
$I = 0.500 + 1.614 Y^2 + -2.200 Y^4 + 0.927 Y^6$				
Cftav = 0.001941	CL = 0.042597	CD = 0.009073		
Sw/Sp = 2.146518	V^(2/3)/Sp = 0.192518	(L/D)vis = 4.694764		
Ab/Abi = 0.583929	V/Vi = 0.379397	Sp/Spi = 0.618405		
b/lw = 0.451589	SSD = 0.258054			

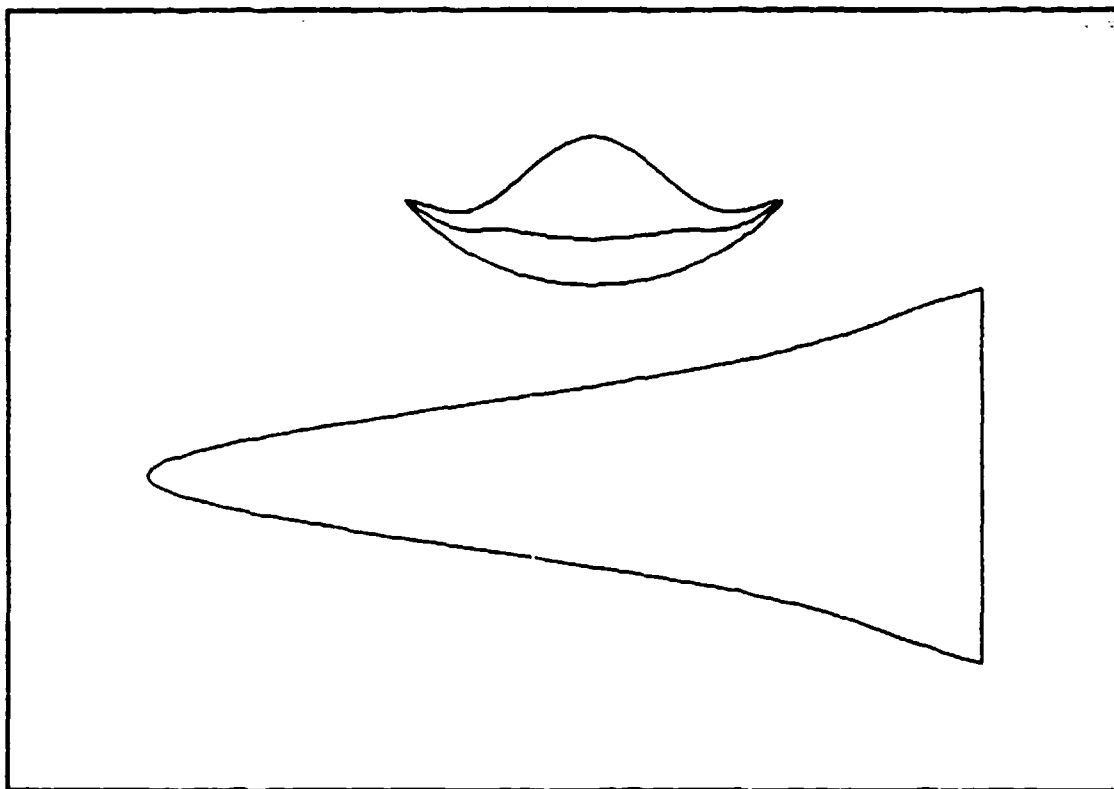


Figure C.27

Table C.27

Phi =50.0	Delta = 8.0	Mach =10.0	Rey = 0.10E+07	Gamma = 1.40
$X = 0.500 + 1.815 Y^2 + -2.600 Y^4 + 1.126 Y^6$				
Cftav = 0.001955	CL = 0.042571	CD = 0.009131		
Sw/Sp = 2.172462	V^(2/3)/Sp = 0.193128	(L/D)vis = 4.662208		
Ab/Abi = 0.563284	V/Vi = 0.363326	Sp/Sp1 = 0.598916		
b/lw = 0.451589	SSD = 0.258054			

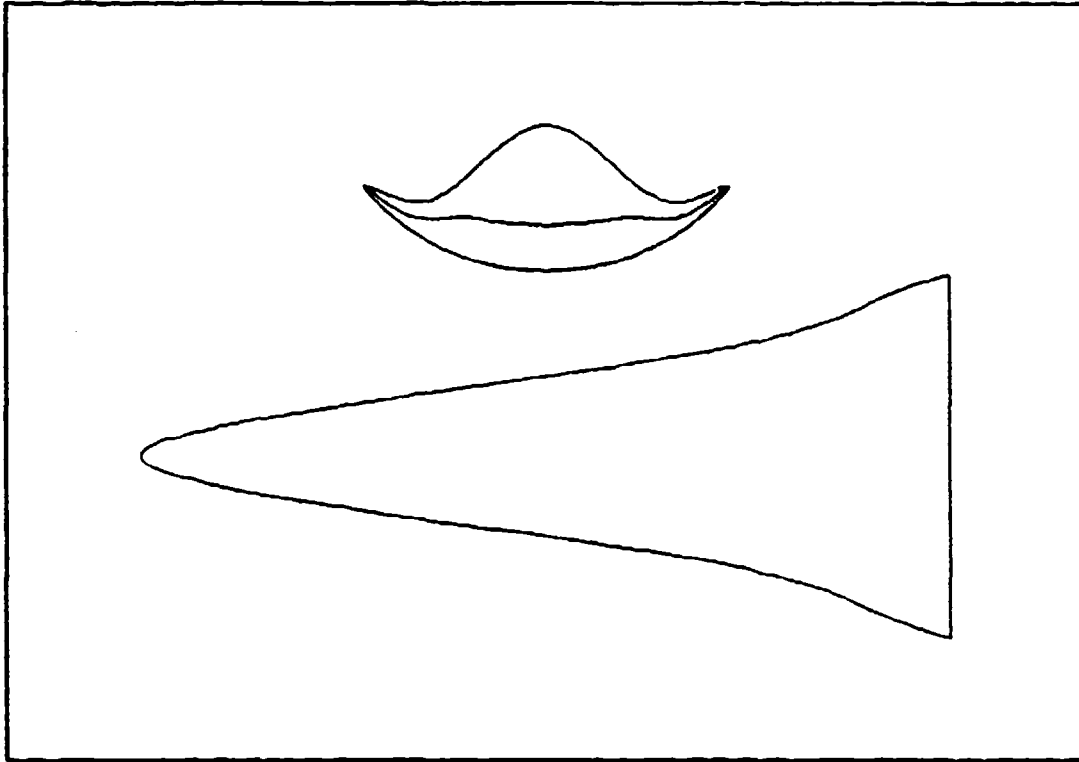


Figure C.28

Table C.28

Phi =50.0	Delta = 8.0	Mach =10.0	Rey = 0.10E+07	Gamma = 1.40
$X = 0.500 + 2.016 Y^2 + -3.000 Y^4 + 1.325 Y^6$				
Cftav = 0.001969	CL = 0.042552	CD = 0.009198		
Sw/Sp = 2.201684	V^(2/3)/Sp = 0.194077	(L/D)vis = 4.626232		
Ab/Abi = 0.542639	V/Vi = 0.348142	Sp/Spi = 0.579266		
b/lw = 0.451589	SSD = 0.258054			

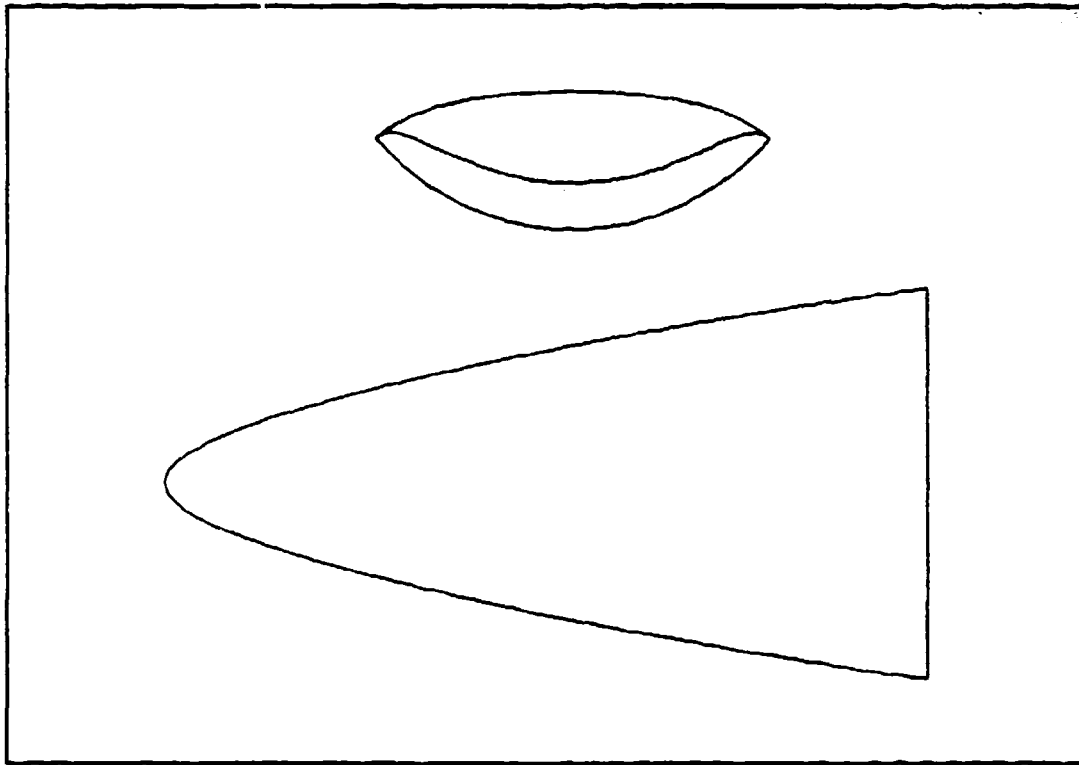


Figure C.29

Table C.29

Phi =50.0	Delta = 8.0	Mach =10.0	Rey = 0.10E+07	Gamma = 1.40
$X = 0.600 + 0.143 Y^2 + 0.000 Y^4 + 0.096 Y^6$				
Cftav = 0.001841	CL = 0.042447	CD = 0.008833		
Sw/Sp = 2.051067	V^(2/3)/Sp = 0.184276	(L/D)vis = 4.805467		
Ab/Abi = 0.676428	V/Vi = 0.421012	Sp/Spi = 0.692483		
b/lw = 0.515302	SSD = 0.236489			

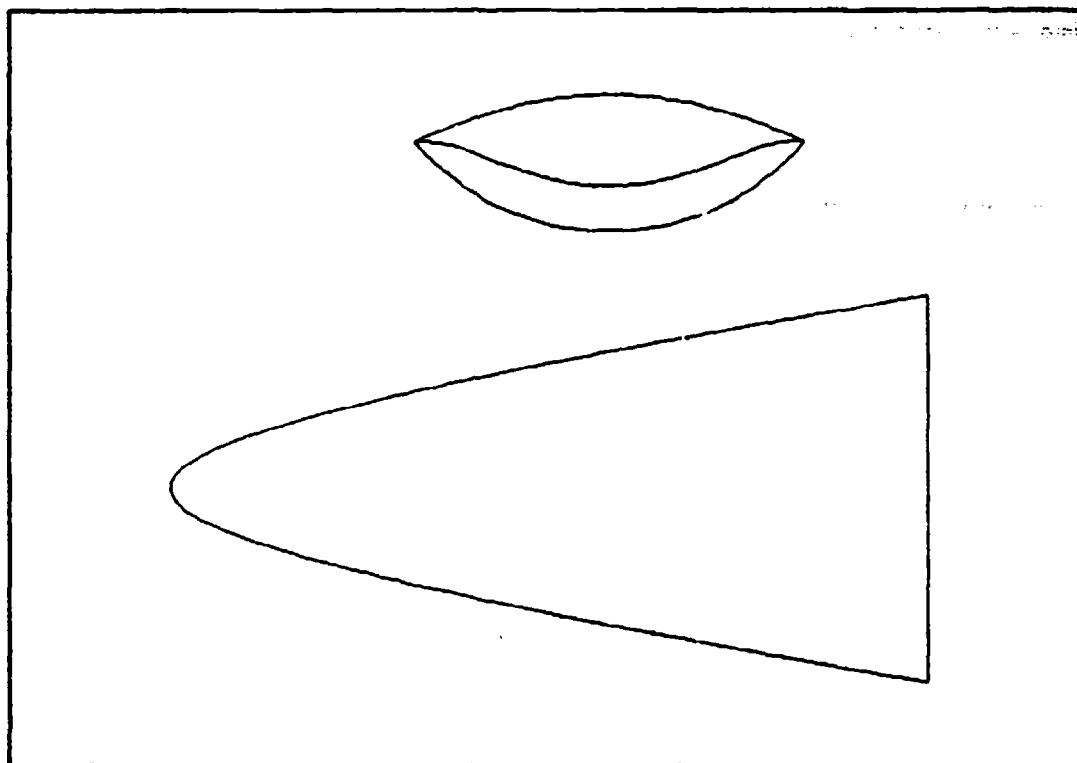


Figure C.30

Table C.30

Phi =50.0	Delta = 8.0	Mach =10.0	Rey = 0.10E+07	Gamma = 1.40
$I = 0.600 + 0.251 Y^2 + 0.000 Y^4 + -0.011 Y^6$				
Cftav = 0.001851	CL = 0.042412	CD = 0.008800		
Sw/Sp = 2.045426	V^(2/3)/Sp = 0.184069	(L/D)vis = 4.819488		
Ab/Abi = 0.648661	V/Vi = 0.399285	Sp/Sp1 = 0.669200		
b/lw = 0.515302	SSD = 0.236489			

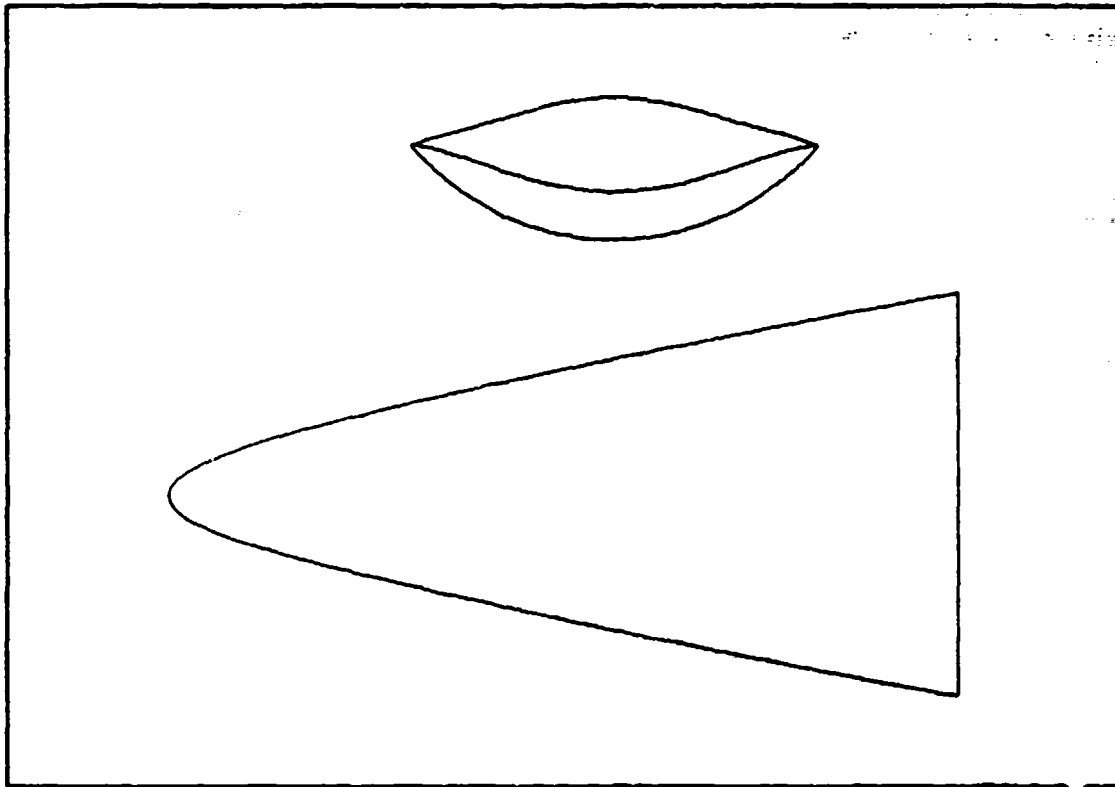


Figure C.31

Table C.31

Phi = 50.0	Delta = 8.0	Mach = 10.0	Re _y = 0.108+07	Gamma = 1.40
$I = 0.600 + 0.452 Y^2 + -0.400 Y^4 + 0.188 Y^6$				
C _{ftav} = 0.001867	CL = 0.042357	CD = 0.008801		
S _w /S _p = 2.043804	V ^{*(2/3)} /S _p = 0.183058	(L/D) _{vis} = 4.812801		
Ab/Abi = 0.628016	V/V _i = 0.379812	S _p /S _{p1} = 0.650807		
b/l _w = 0.515302	SSD = 0.236489			

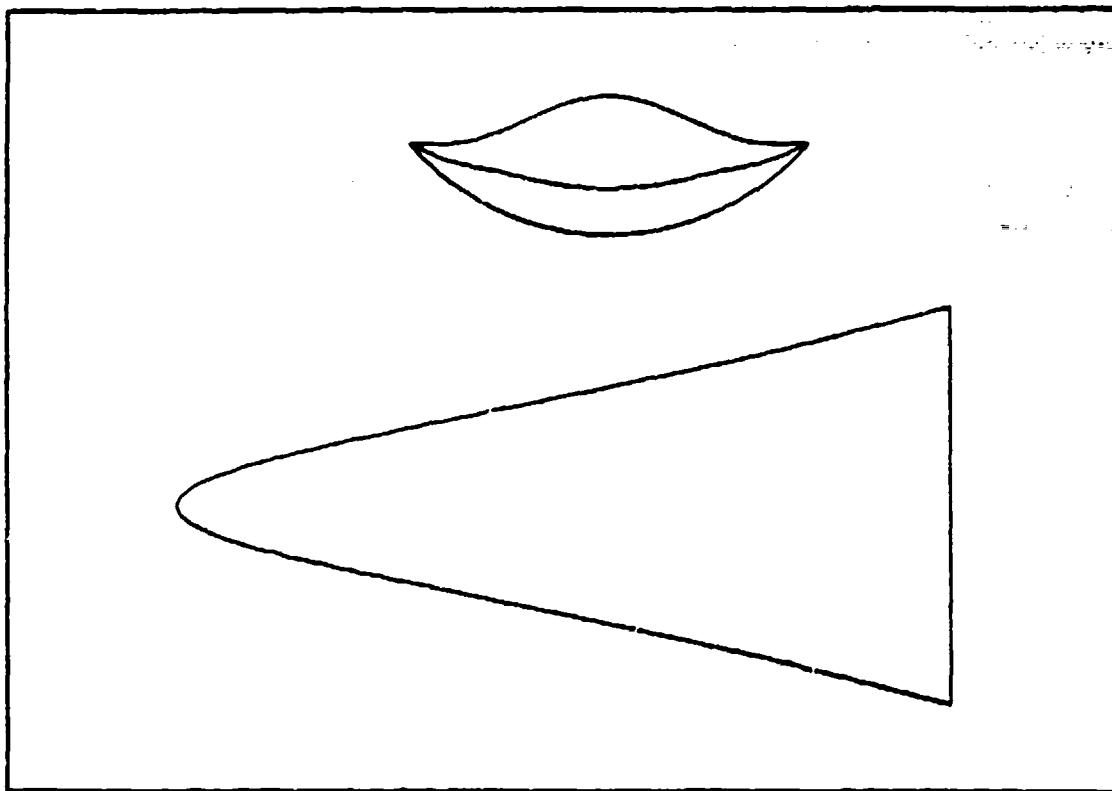


Figure C.32

Table C.32

Phi =50.0	Delta = 8.0	Mach =10.0	Rey = 0.10E+07	Gamma = 1.40
$X = 0.600 + 0.862 Y^2 + -1.000 Y^4 + 0.379 Y^6$				
Cftav = 0.001906	CL = 0.042262	CD = 0.008834		
Sw/Sp = 2.061863	V*(2/3)/Sp = 0.182863	(L/D)vis = 4.784272		
Ab/Abi = 0.589151	V/Vi = 0.333822	Sp/Sp1 = 0.597814		
b/lw = 0.515302	SSD = 0.236489			

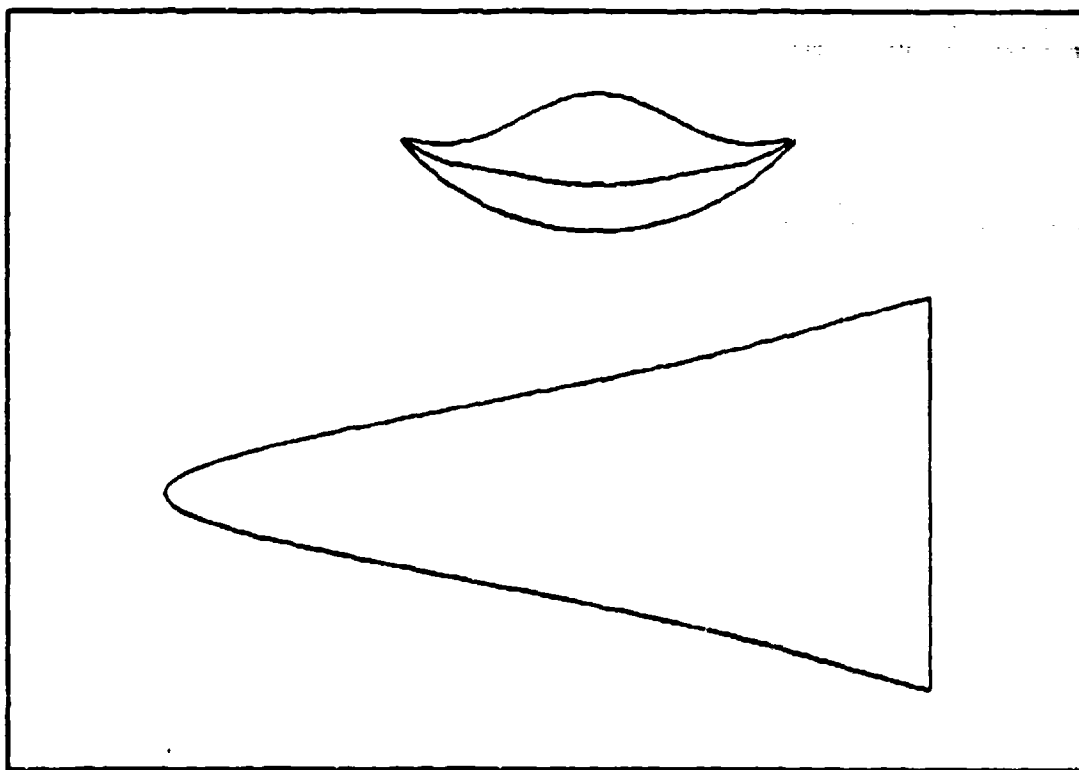


Figure C.33

Table C.33

Phi =50.0	Delta = 8.0	Mach =10.0	Rey = 0.10E+07	Gamma = 1.40
$I = 0.600 + 1.063 Y^2 + -1.400 Y^4 + 0.578 Y^6$				
Cftev = 0.001923	CL = 0.042220	CD = 0.008871		
Sw/Sp = 2.075419	V^(2/3)/Sp = 0.182690	(L/D)vis = 4.759373		
Ab/Abi = 0.548506	V/Vi = 0.317303	Sp/Sp1 = 0.578473		
b/lw = 0.515302	SSD = 0.236489			

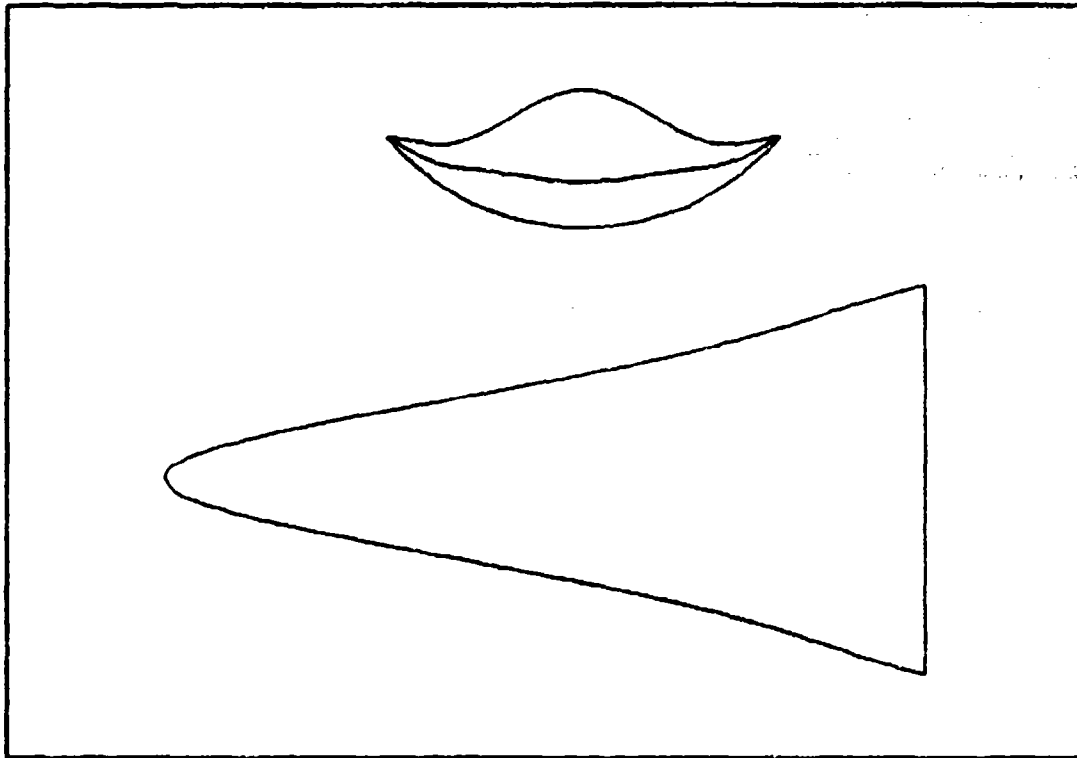


Figure C.34

Table C.34

Phi = 50.0	Delta = 8.0	Mach = 10.0	Rey = 0.10E+07	Gamma = 1.40
$Y = 0.600 + 1.264 Y^2 + -1.800 Y^4 + 0.777 Y^6$				
Cftav = 0.001942	CL = 0.042183	CD = 0.008919		
Sw/Sp = 2.092990	V*(2/3)/Sp = 0.182802	(L/D)vis = 4.729744		
Ab/Abi = 0.527861	V/Vi = 0.301864	Sp/SpI = 0.558982		
b/lv = 0.515302	SSD = 0.238489			

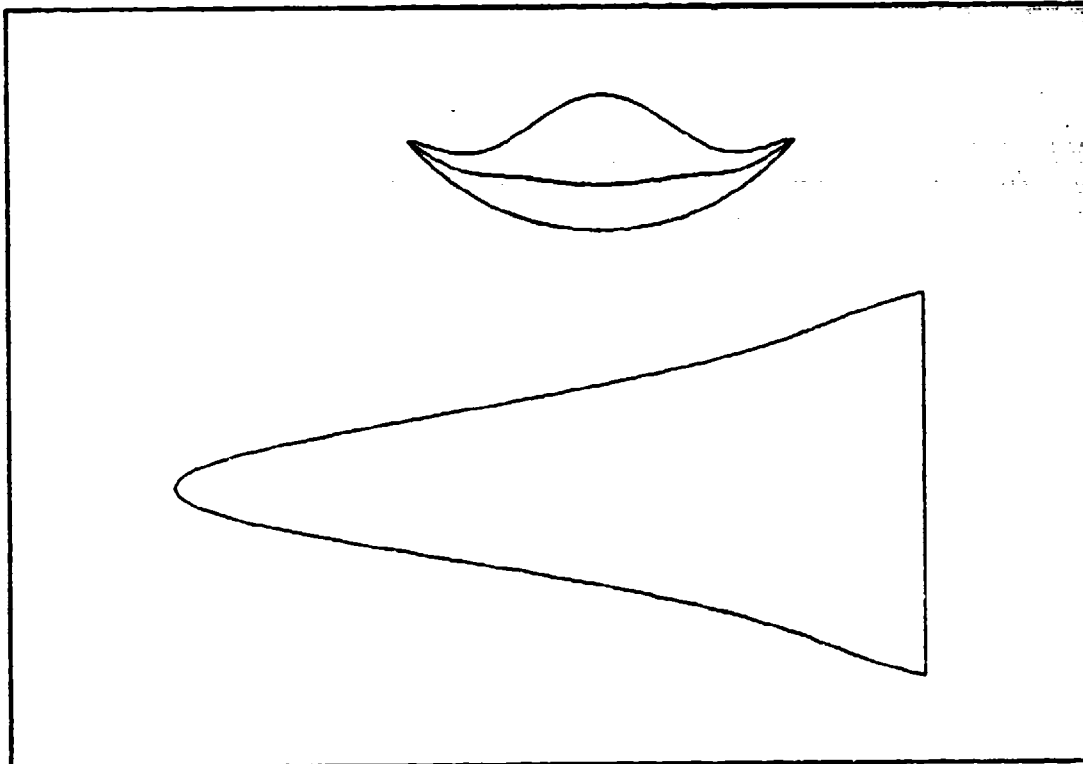


Figure C.35

Table C.35

Phi =50.0	Delta = 8.0	Mach =10.0	Rey = 0.10E+07	Gamma = 1.40
$I = 0.600 + 1.465 Y^2 + -2.200 Y^4 + 0.976 Y^6$				
Cftav = 0.001961	CL = 0.042152	CD = 0.008976		
Sw/Sp = 2.114278	V^(2/3)/Sp = 0.183242	(L/D)vis = 4.695912		
Ab/Abi = 0.507217	V/Vi = 0.286913	Sp/Spi = 0.539290		
b/lw = 0.515302	SSD = 0.236489			

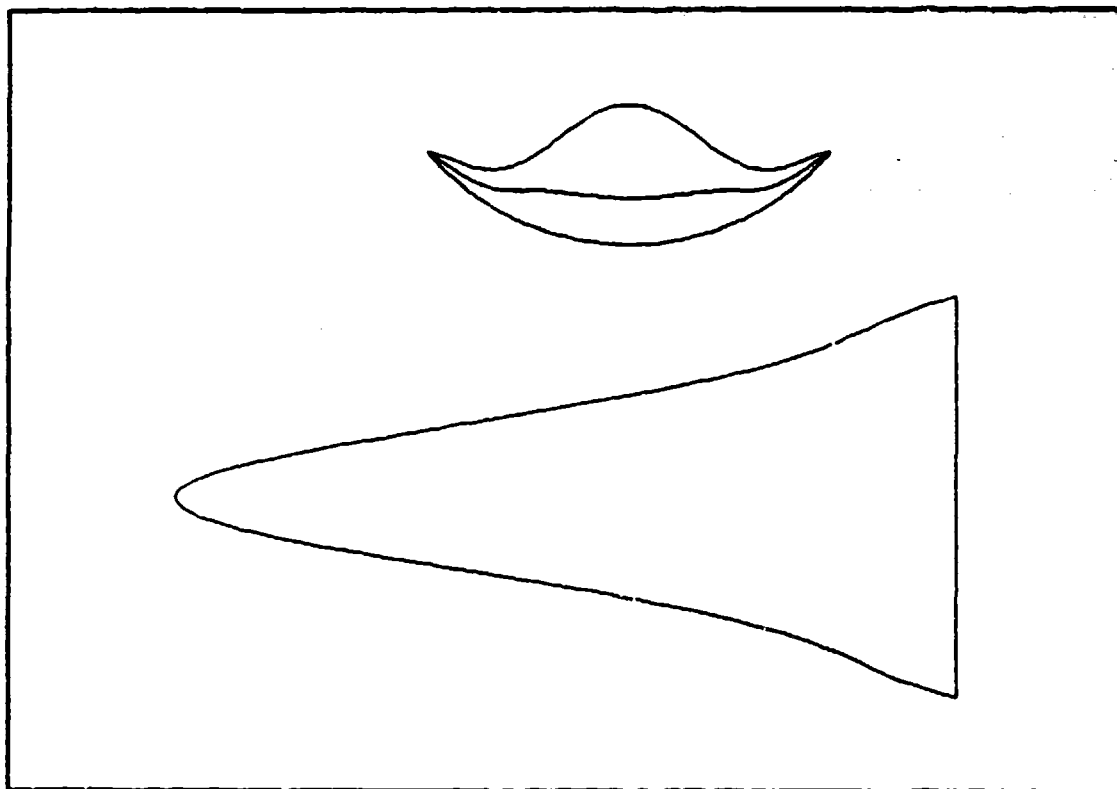


Figure C.36

Table C.36

Phi =50.0	Delta = 8.0	Mach =10.0	Rey = 0.10E+07	Gamma = 1.40
$X = 0.600 + 1.668 Y^2 + -2.600 Y^4 + 1.175 Y^6$				
Cftav = 0.001980	CL = 0.042127	CD = 0.009043		
Sw/Sp = 2.138979	V^(2/3)/Sp = 0.184060	(L/D)vis = 4.658574		
Ab/Abi = 0.486572	V/Vi = 0.273058	Sp/Sp1 = 0.519468		
b/lw = 0.515302	SSD = 0.236489			

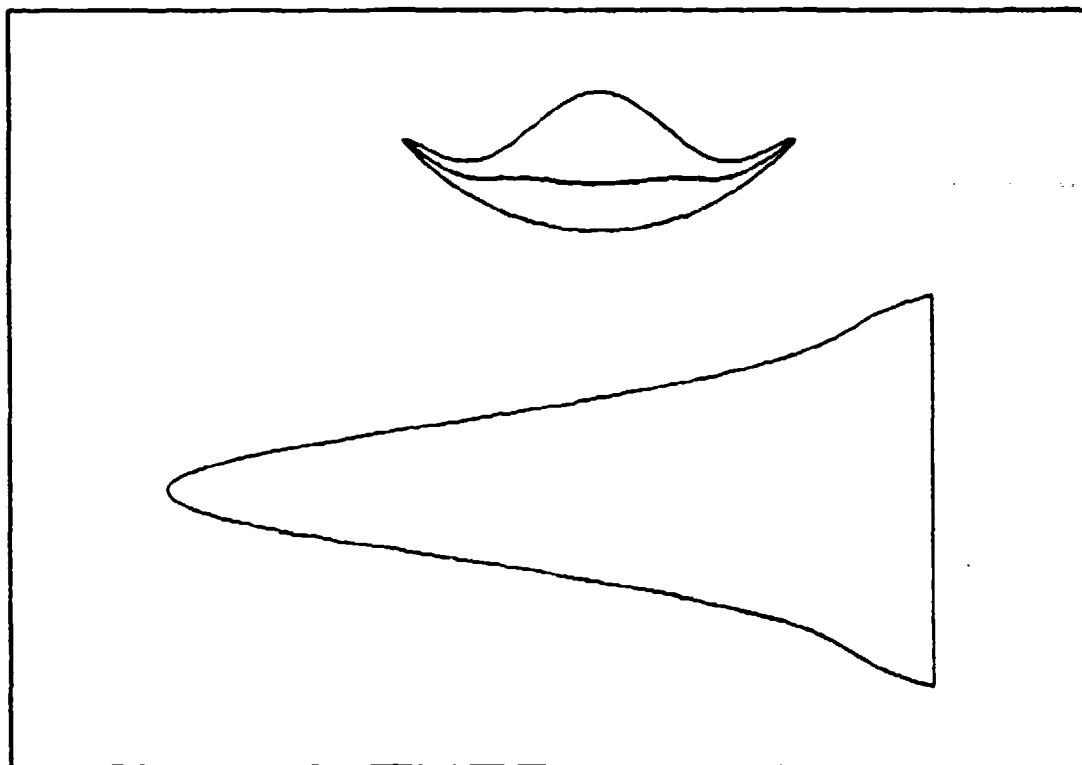


Figure C.37

Table C.37

Phi =50.0	Delta = 8.0	Mach =10.0	Rey = 0.10E+07	Gamma = 1.40
$I = 0.600 + 1.867 Y^2 + -3.000 Y^4 + 1.374 Y^6$				
Cftav = 0.001999	CL = 0.042110	CD = 0.009118		
Sw/Sp = 2.166782	V^(2/3)/Sp = 0.185314	(L/D)vis = 4.618535		
Ab/Abi = 0.465927	V/Vi = 0.280108	Sp/Sp1 = 0.499505		
b/lw = 0.515302	SSD = 0.236489			

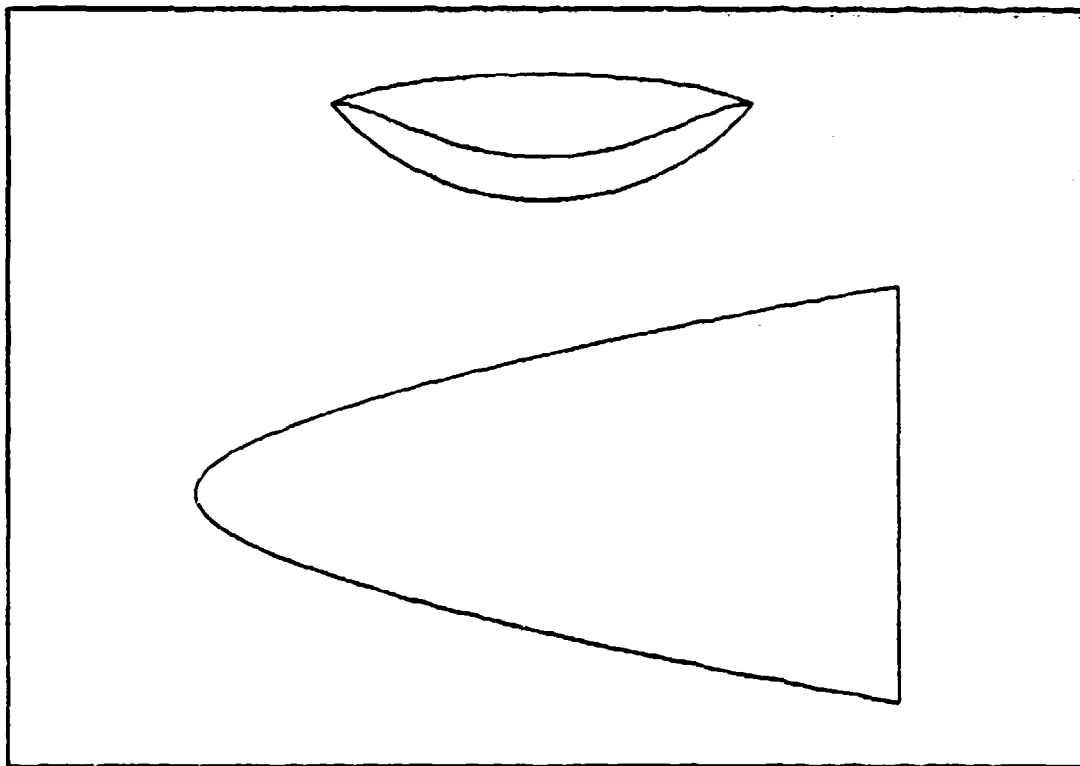


Figure C.38

Table C.38

Phi =50.0	Delta = 8.0	Mach =16.0	Rey = 0.10E+07	Gamma = 1.40
X = 0.700 + 0.102 Y^2 + 0.000 Y^4 + 0.038 Y^6				
Cftav = 0.001833	CL = 0.041972	CD = 0.008676		
Sw/Sp = 2.035391	V^(2/3)/Sp = 0.174208	(L/D)vis = 4.837829		
Ab/Abi = 0.571949	V/Vi = 0.305445	Sp/Sp1 = 0.591427		
b/lw = 0.599945	SSD = 0.211550			

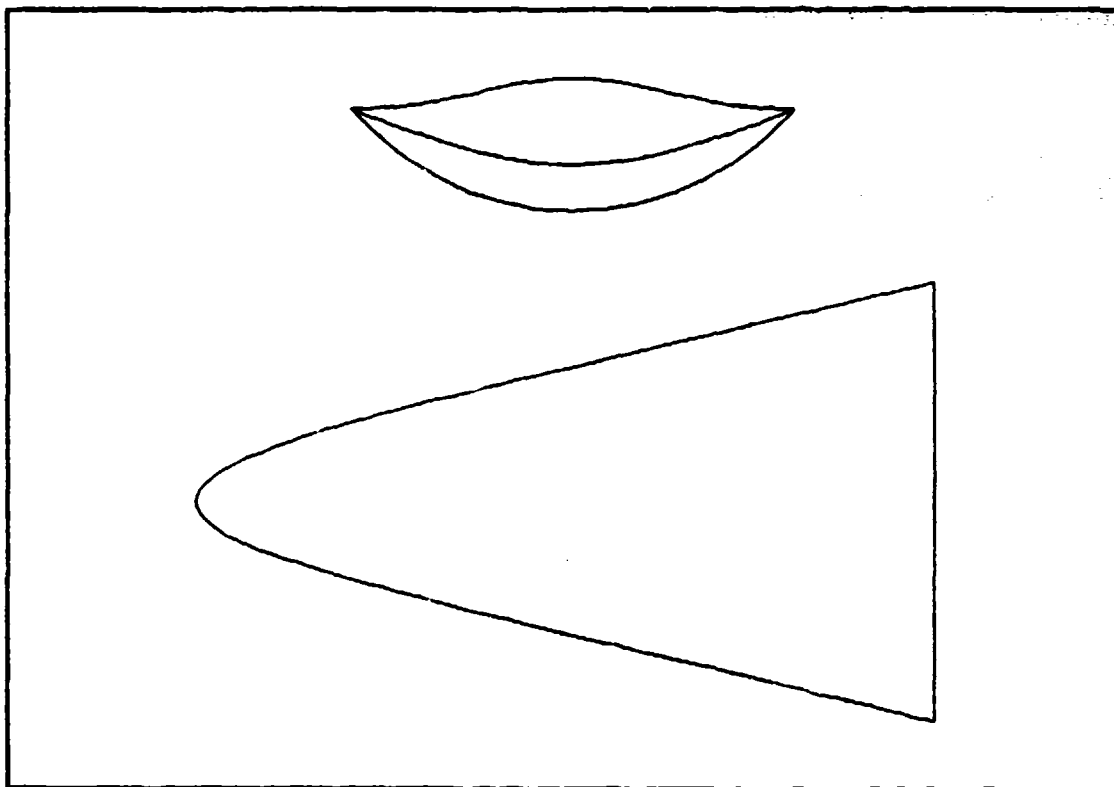


Figure C.39

Table C.39

Phi =50.0	Delta = 8.0	Mach =10.0	Rey = 0.10E+07	Gamma = 1.40
$X = 0.700 + 0.411 Y^2 + -0.400 Y^4 + 0.130 Y^6$				
Cltav = 0.001875	CL = 0.041883	CD = 0.008686		
Sw/Sp = 2.033808	V*(2/3)/Sp = 0.173457	(L/D)vis = 4.821683		
Ab/Abi = 0.523536	V/Vi = 0.270647	Sp/Sp1 = 0.547973		
b/lw = 0.599945	SSD = 0.211550			

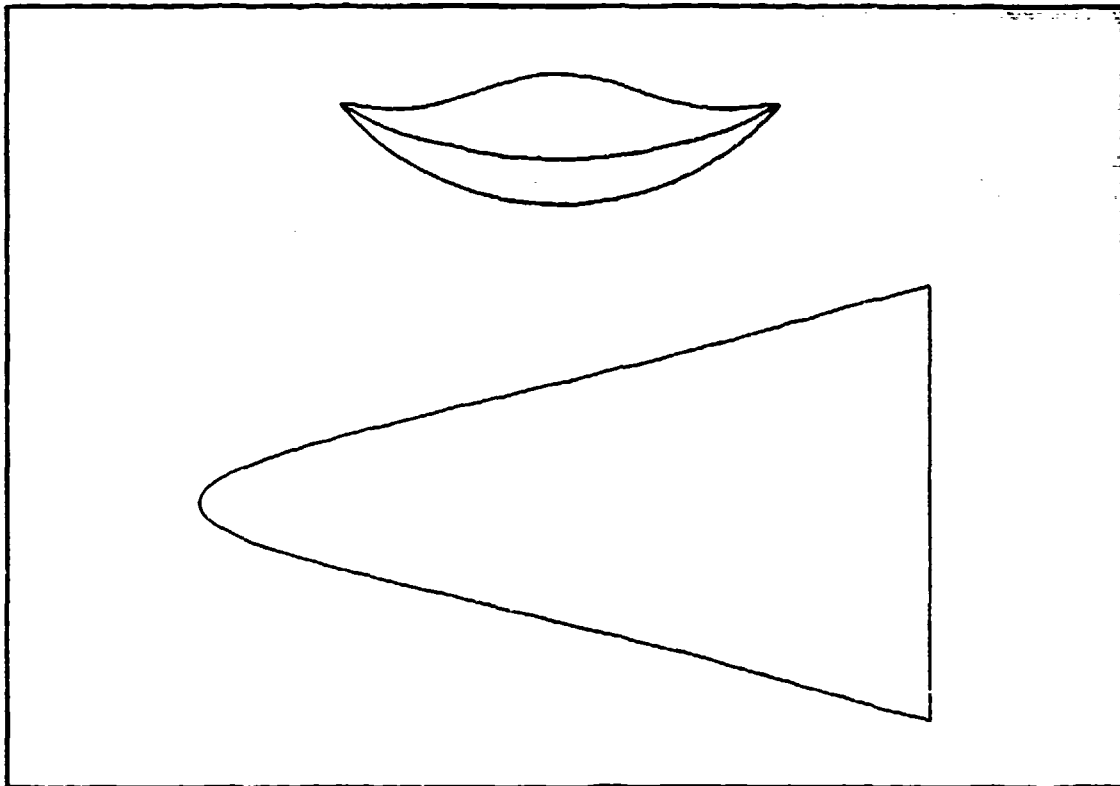


Figure C.40

Table C.40

Phi =50.0	Delta = 8.0	Mach =10.0	Rey = 0.10E+07	Gamma = 1.40
$X = 0.700 + 0.712 Y^2 + -1.000 Y^4 + 0.429 Y^6$				
Cftav = 0.001911	CL = 0.041807	CD = 0.008740		
Sw/Sp = 2.044167	V^(2/3)/Sp = 0.172623	(L/D)vis = 4.783686		
Ab/Abi = 0.492698	V/Vi = 0.247583	Sp/Spi = 0.518875		
b/lw = 0.599945	SSD = 0.211550			

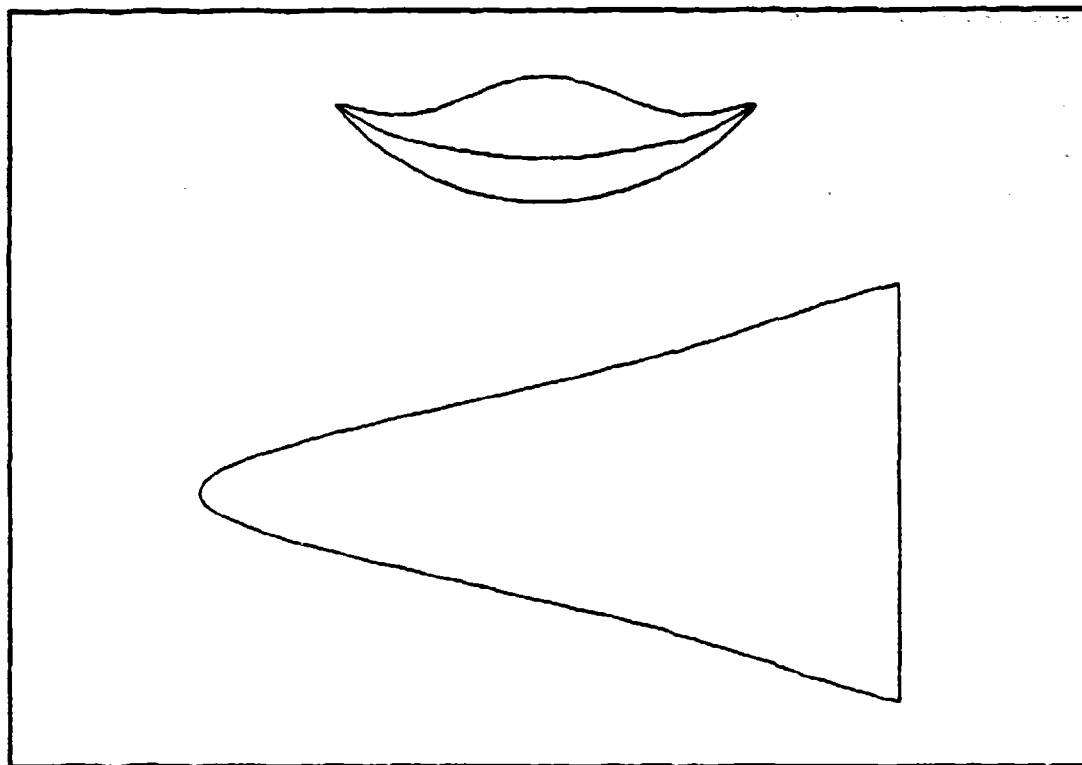


Figure C.41

Table C.41

Phi =50.0	Delta = 8.0	Mach =10.0	Rey = 0.10E+07	Gamma = 1.40
X = 0.700 + 0.913 Y^2 + -1.400 Y^4 + 0.628 Y^6				
Cftav = 0.001936	CL = 0.041763	CD = 0.008788		
Sw/Sp = 2.056345	V^(2/3)/Sp = 0.172440	(L/D)vis = 4.752065		
Ab/Abi = 0.472053	V/Vi = 0.233263	Sp/Spi = 0.499199		
b/lw = 0.599945	SSD = 0.211550			

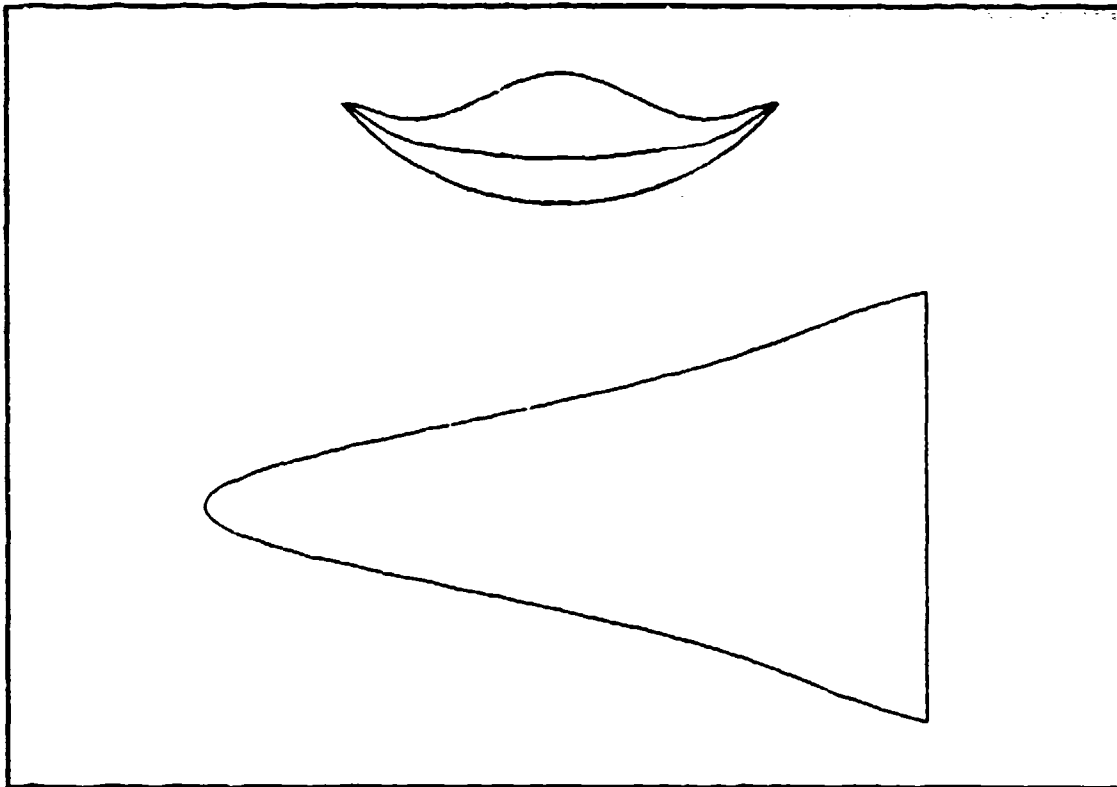


Figure C.42

Table C.42

Phi =50.0	Delta = 8.0	Mach =10.0	Rey = 0.10E+07	Gamma = 1.40
X = 0.700 + 1.114 Y^2 + -1.800 Y^4 + 0.827 Y^6				
Cftav = 0.001961	CL = 0.041724	CD = 0.008847		
Sw/Sp = 2.072390	V^(2/3)/Sp = 0.172614	(L/D)vis = 4.716013		
Ab/Abi = 0.451409	V/Vi = 0.219838	Sp/Spi = 0.479373		
b/lw = 0.599945	SSD = 0.211550			

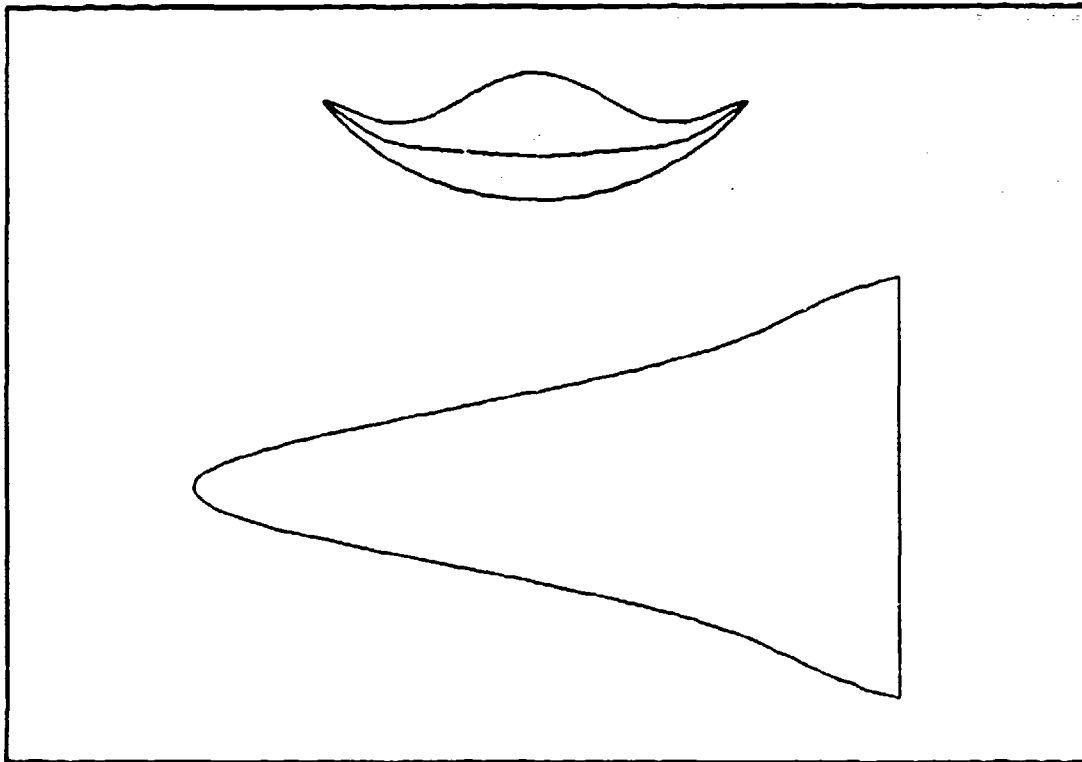


Figure C.43

Table C.43

Phi =50.0	Delta = 8.0	Mach =10.0	Rey = 0.10E+07	Gamma = 1.40
$X = 0.700 + 1.315 Y^2 + -2.200 Y^4 + 1.026 Y^6$				
Cftav = 0.001987	CL = 0.041693	CD = 0.008916		
Sw/Sp = 2.091982	V^(2/3)/Sp = 0.173211	(L/D)vis = 4.676222		
Ab/Abi = 0.430764	V/Vi = 0.207317	Sp/Spi = 0.459405		
b/lw = 0.599945	SSD = 0.211550			

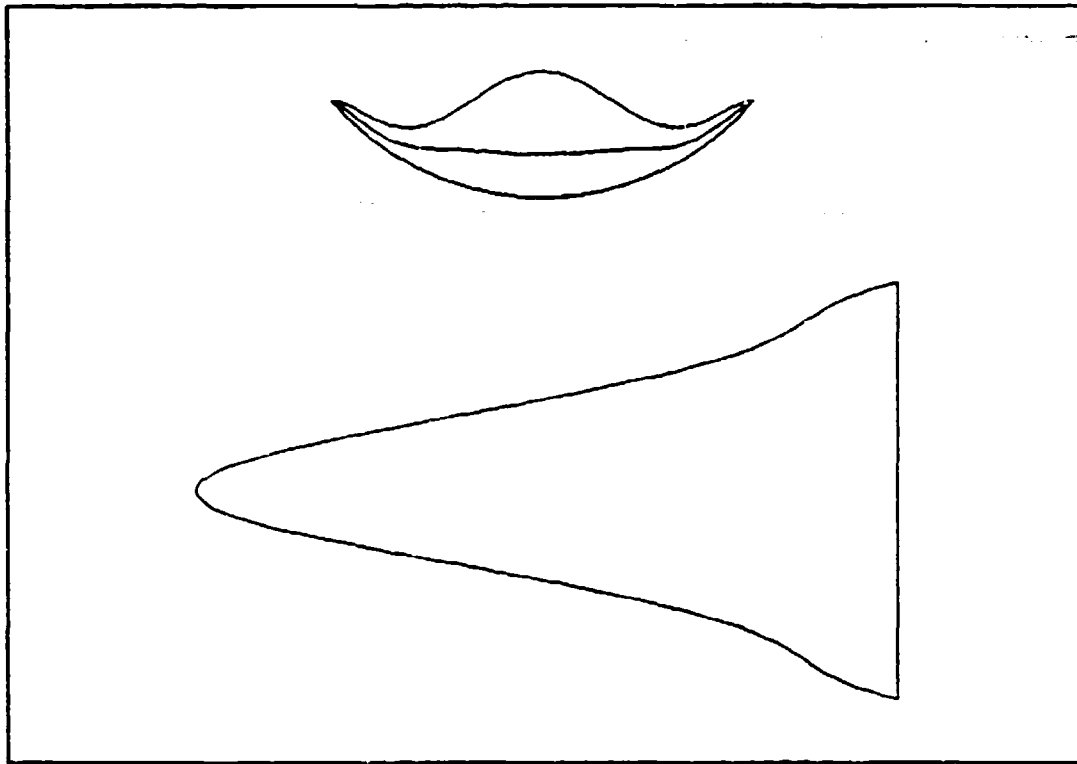


Figure C.44

Table C.44

Phi =50.0	Delta = 8.0	Mach =10.0	Rey = 0.10E+07	Gamma = 1.40
$X = 0.700 + 1.516 Y^2 + -2.600 Y^4 + 1.225 Y^6$				
Cftav = 0.002013	CL = 0.041670	CD = 0.008993		
Sw/Sp = 2.114785	V^(2/3)/Sp = 0.174308	(L/D)vis = 4.633859		
Ab/Abi = 0.410119	V/Vi = 0.195705	Sp/Spi = 0.439305		
b/lw = 0.599945	SSD = 0.211550			

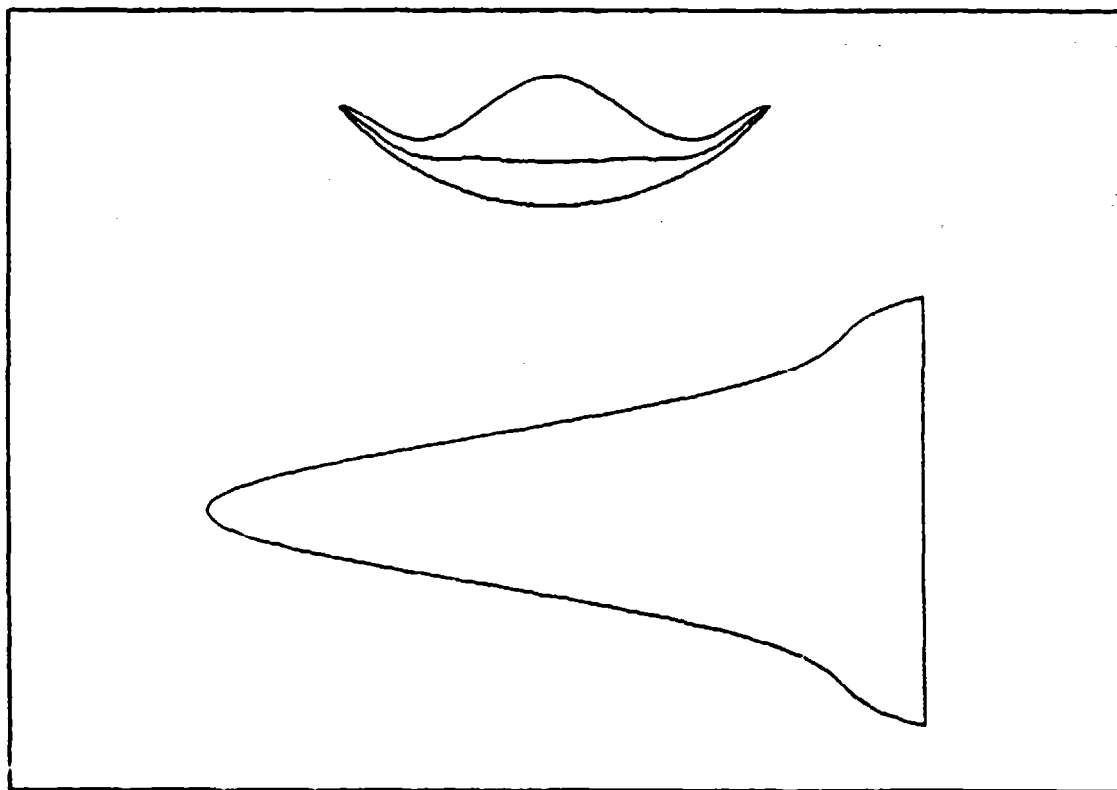


Figure C.45

Table C.45

Phi =50.0	Delta = 8.0	Mach =10.0	Rey = 0.10E+07	Gamma = 1.40
$X = 0.700 + 1.717 Y^2 + -3.000 Y^4 + 1.424 Y^6$				
Cftav = 0.002039	CL = 0.041657	CD = 0.009076		
Sw/Sp = 2.140448	V^(2/3)/Sp = 0.176001	(L/D)vis = 4.589540		
Ab/Abi = 0.389474	V/V1 = 0.185009	Sp/Sp1 = 0.419079		
b/lw = 0.599945	SSD = 0.211550			

APPENDIX D

Presented here are configurations that have the following parameters held fixed:

$$\phi_1 = 40, \quad \delta = 8, \quad M = 10, \quad \text{Rey} = 1 \times 10^6$$

The following parameters are varied:

$$R_0 \text{ from } 0.4 \text{ to } 0.8$$

$$b_4 \text{ from } 0.0 \text{ to } -2.0$$

The values of b_2 and b_6 are such that equation 2-13 and condition (iii) holds.

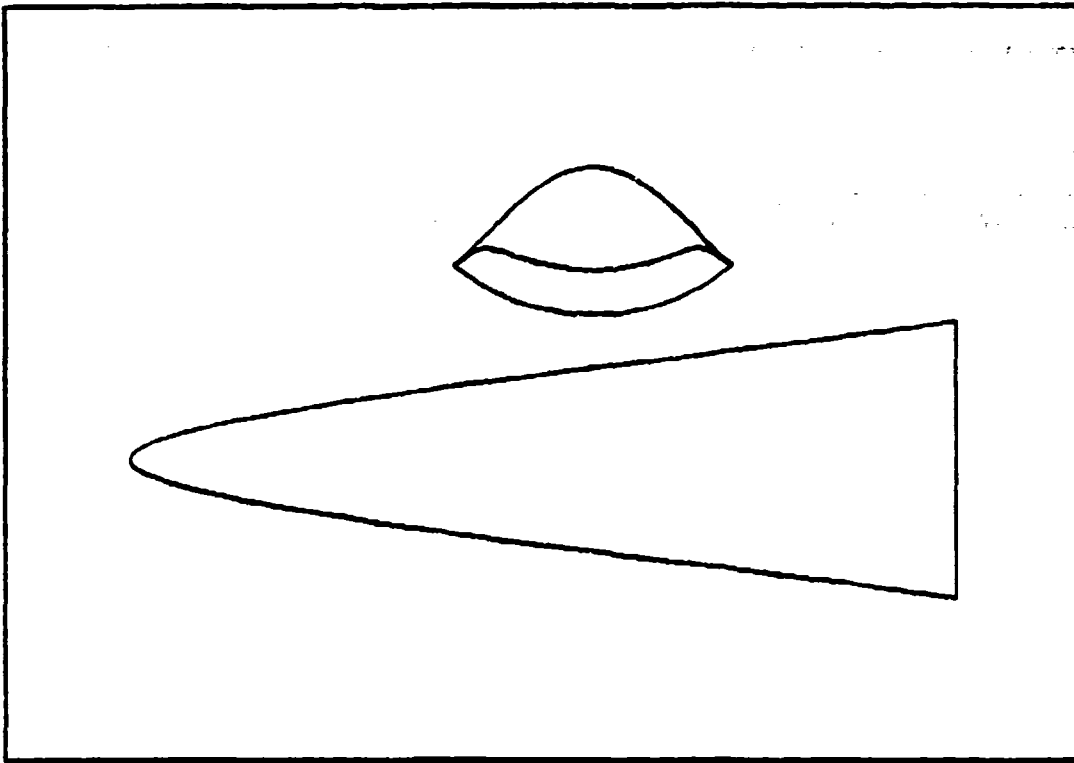


Figure D.1

Table D.1

$\Phi = 40.0$	$\Delta = 8.0$	$Mach = 10.0$	$Re_\gamma = 0.10 \times 10^7$	$\Gamma = 1.40$
$I = 0.400 + 1.070 Y^2 + 0.000 Y^4 + -0.436 Y^6$				
$C_{f_{\text{tar}}} = 0.001072$	$CL = 0.043200$	$CD = 0.009150$		
$S_w/S_p = 2.220440$	$Y'(2/3)/S_p = 0.210620$	$(L/D)_{\text{vis}} = 4.725020$		
$\Delta b/\Delta b_1 = 0.010400$	$Y/Y_1 = 0.640400$	$S_p/S_{p1} = 0.020151$		
$b/l_w = 0.337233$	$S_{SD} = 0.270033$			

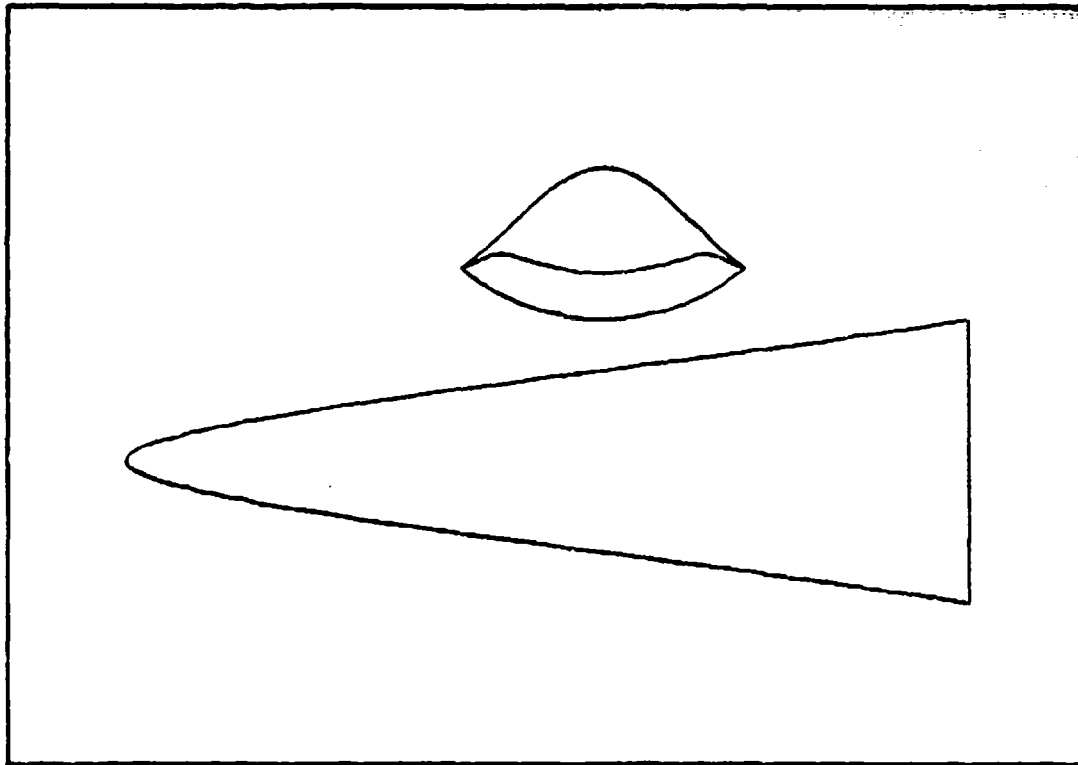


Figure D.2

Table D.2

Phi =40.0	Delta = 8.0	Nach =10.0	Rey = 0.10E+07	Gamma = 1.40
$X = 0.400 + 1.424 Y^2 + -1.600 Y^4 + 0.270 Y^6$				
Cftav = 0.001875	CL = 0.043219	CD = 0.009140		
Sw/Sp = 2.227980	V*(2/3)/Sp = 0.209891	(L/D)vis = 4.728425		
Ab/Abi = 0.791594	V/Vi = 0.615215	Sp/Sp1 = 0.604055		
b/lw = 0.337233	88D = 0.276033			

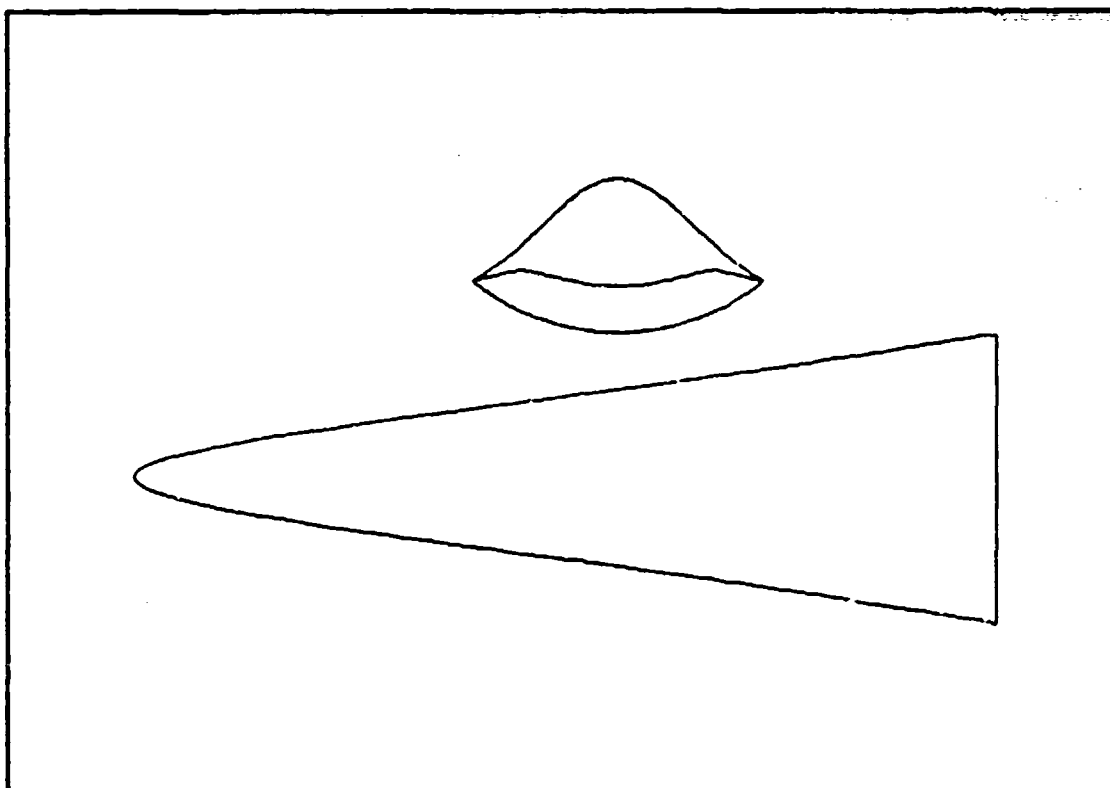


Figure D.3

Table D.3

Phi =40.0	Delta = 8.0	Mach =10.0	Rey = 0.10E+07	Gamma = 1.40
$X = 0.400 + 1.778 Y^2 + -2.000 Y^4 + 0.977 Y^6$				
Cftav = 0.001879	CL = 0.043182	CD = 0.009145		
Sw/Sp = 2.240033	V^(2/3)/Sp = 0.209406	(L/D)vis = 4.719671		
Ab/Ab1 = 0.764796	V/V1 = 0.585466	Sp/Spi = 0.779723		
b/lw = 0.337233	SSD = 0.276033			

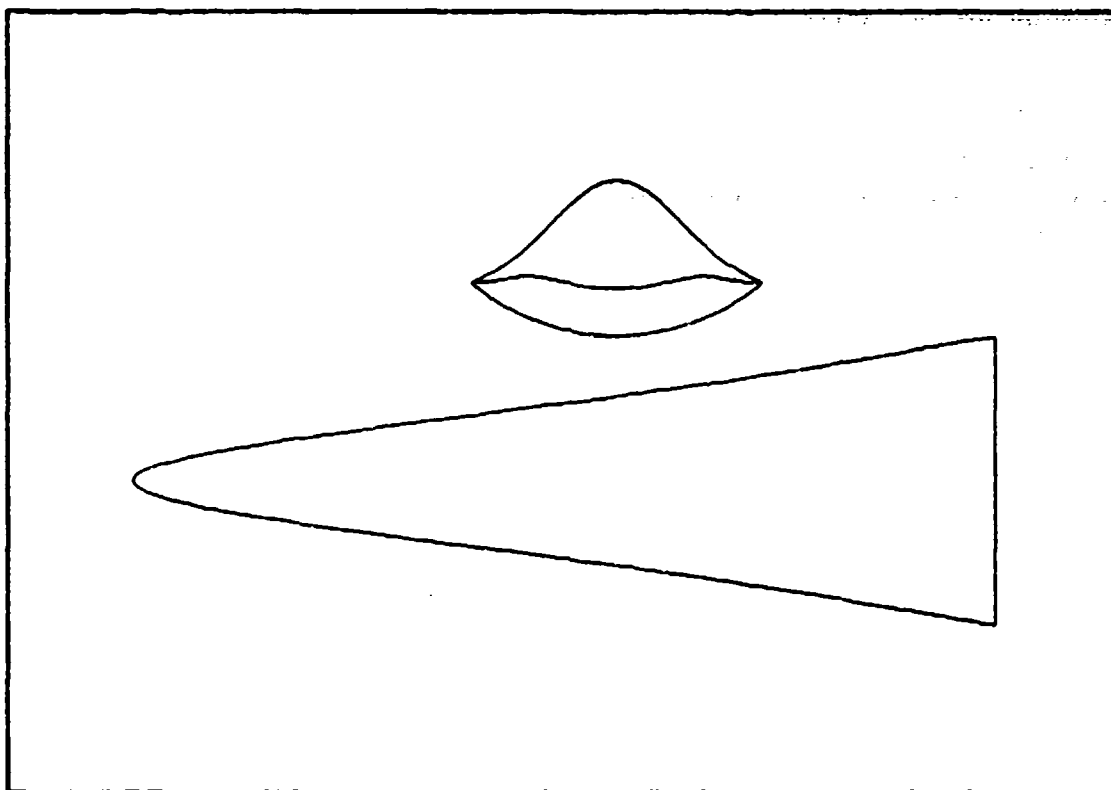


Figure D.4

Table D.4

Phi =40.0	Delta = 8.0	Mach =10.0	Rey = 0.10E+07	Gamma = 1.40
$X = 0.400 + 2.132 Y^2 + -3.000 Y^4 + 1.682 Y^6$				
Cftav = 0.001883	CL = 0.043109	CD = 0.009172		
Sw/Sp = 2.262038	V^(2/3)/Sp = 0.209216	(L/D)vis = 4.700094		
Ab/Abi = 0.737809	V/Vi = 0.557007	Sp/Sp1 = 0.754930		
b/lw = 0.337233	SSD = 0.276033			

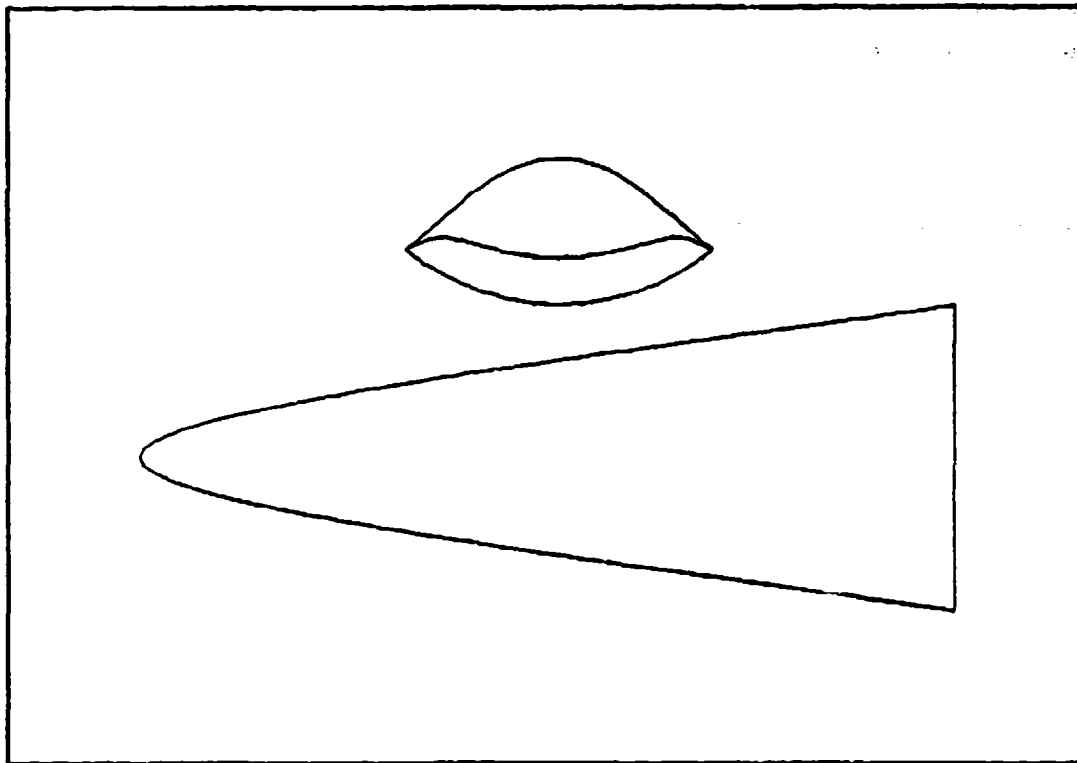


Figure D.5

Table D.5

Phi =40.0	Delta = 8.0	Mach =10.0	Rey = 0.10E+07	Gamma = 1.40
$X = 0.500 + 0.858 Y^2 + 0.000 Y^4 + -0.295 Y^6$				
Cftav = 0.001859	CL = 0.042861	CD = 0.008915		
Sw/Sy = 2.151700	V^(2/3)/Sy = 0.201529	(L/D)vis = 4.807703		
Ab/Ab1 = 0.738083	V/V1 = 0.521240	Sy/Sy1 = 0.749808		
b/lw = 0.378929	SSD = 0.258054			

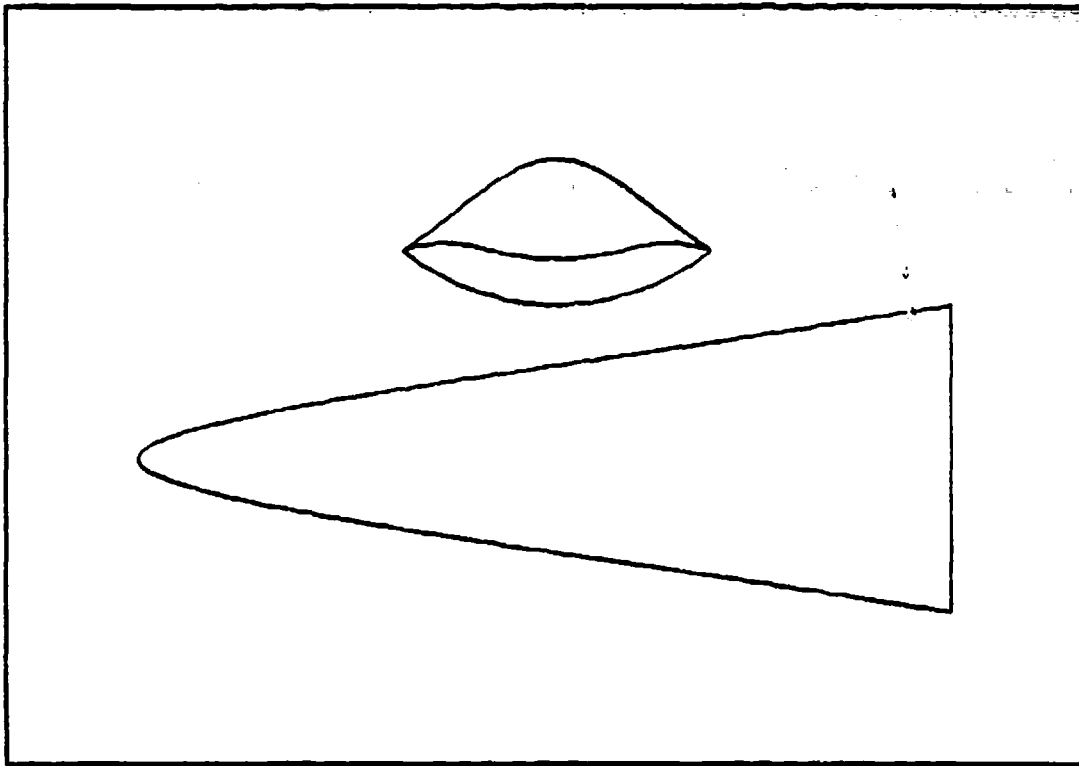


Figure D.6

Table D.6

Phi =40.0	Delta = 8.0	Mach =10.0	Rey = 0.10E+07	Gamma = 1.40
I = 0.500 + 1.212 Y^2 + -1.000 Y^4 + 0.411 Y^6				
Cftav = 0.001866	CL = 0.042796	CD = 0.008912		
Sw/Sp = 2.154438	V^(2/3)/Sp = 0.200740	(L/D)vis = 4.801750		
Ab/Ab1 = 0.711191	V/V1 = 0.492833	Sp/Sp1 = 0.725149		
b/lw = 0.378929	SSD = 0.258054			

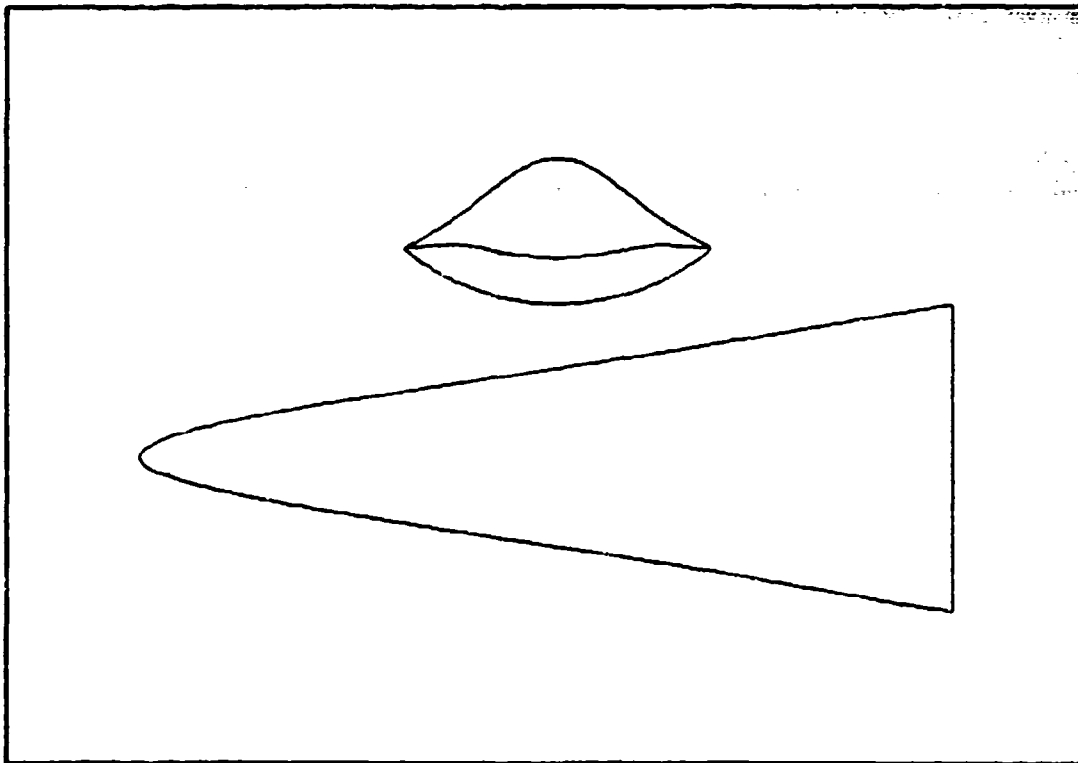


Figure D.7

Table D.7

Phi =40.0	Delta = 8.0	Mach =10.0	Rey = 0.10E+07	Gamma = 1.40
X = 0.500 + 1.586 Y^2 + -2.000 Y^4 + 1.118 Y^6				
Cftav = 0.001877	CL = 0.042733	CD = 0.008931		
Sw/Sp = 2.167306	V^(2/3)/Sp = 0.200233	(L/D)vis = 4.785007		
Ab/Abi = 0.684393	V/Vi = 0.465955	Sp/Spi = 0.700308		
b/lw = 0.378929	SSD = 0.258054			

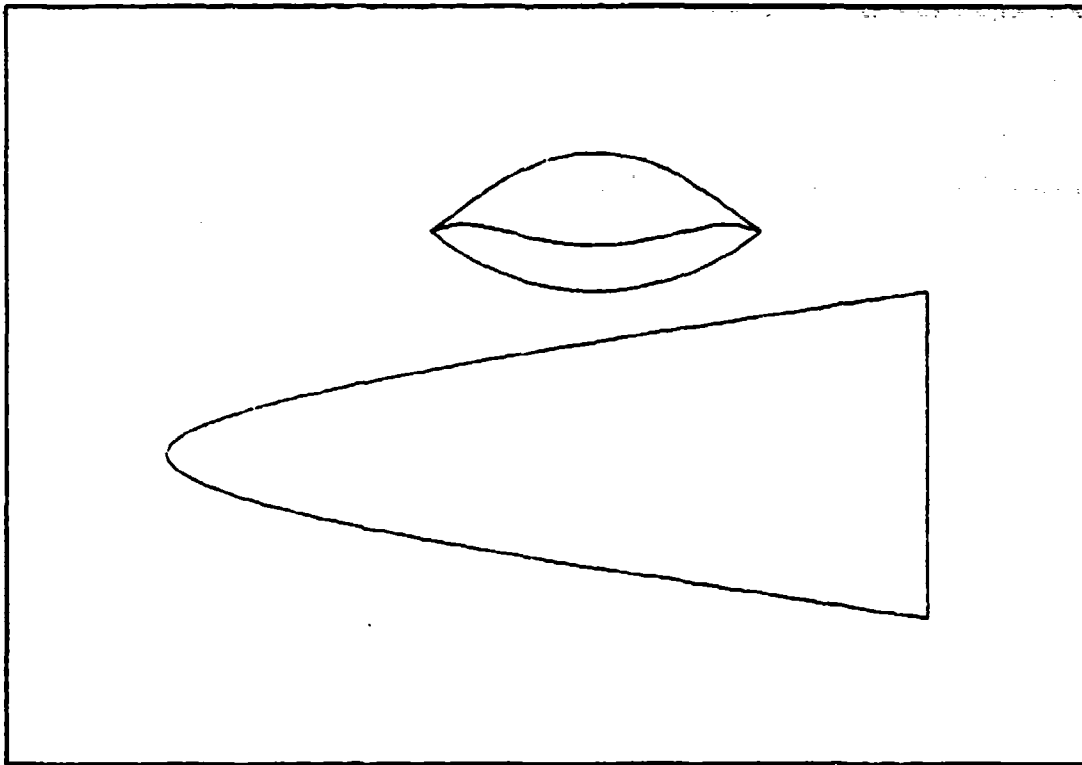


Figure D.8

Table D.8

Phi =40.0	Delta = 8.0	Mach =10.0	Rey = 0.10E+07	Gamma = 1.40
$X = 0.600 + 0.648 Y^2 + 0.000 Y^4 + -0.154 Y^6$				
Cftav = 0.001847	CL = 0.042424	CD = 0.008715		
Sw/Sp = 2.095432	V^(2/3)/Sp = 0.191944	(L/D)vis = 4.868124		
Ab/Abi = 0.657681	V/Vi = 0.409299	Sp/Spi = 0.670060		
b/lw = 0.432390	SSD = 0.236489			

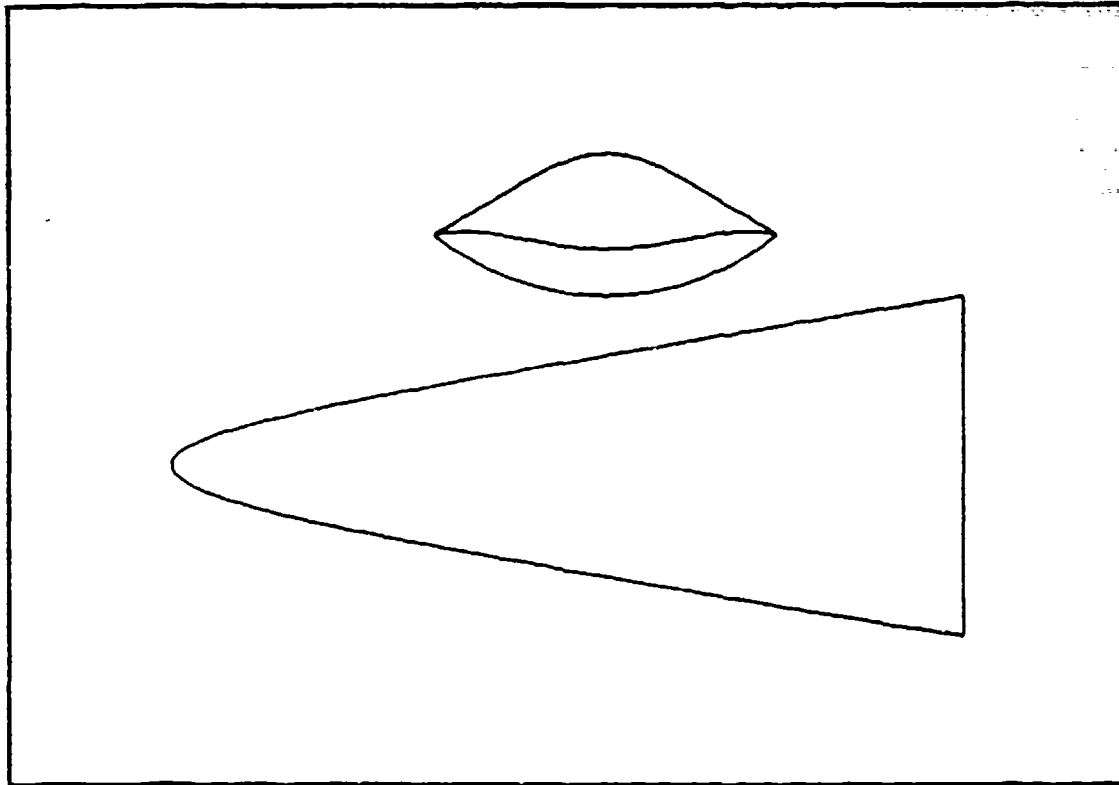


Figure D.9

Table D.9

Phi = 40.0	Delta = 8.0	Mach = 10.0	Re _y = 0.10E+07	Gamma = 1.40
$X = 0.600 + 1.000 Y^2 + -1.000 Y^4 + 0.552 Y^6$				
C _f av = 0.001862	CL = 0.042353	CD = 0.008725		
Sw/Sp = 2.097928	V ^{2/3} /Sp = 0.191047	(L/D) _{vis} = 4.853993		
Ab/Abi = 0.630788	V/Vi = 0.383805	Sp/Spi = 0.644953		
b/lw = 0.432390	SSD = 0.236489			

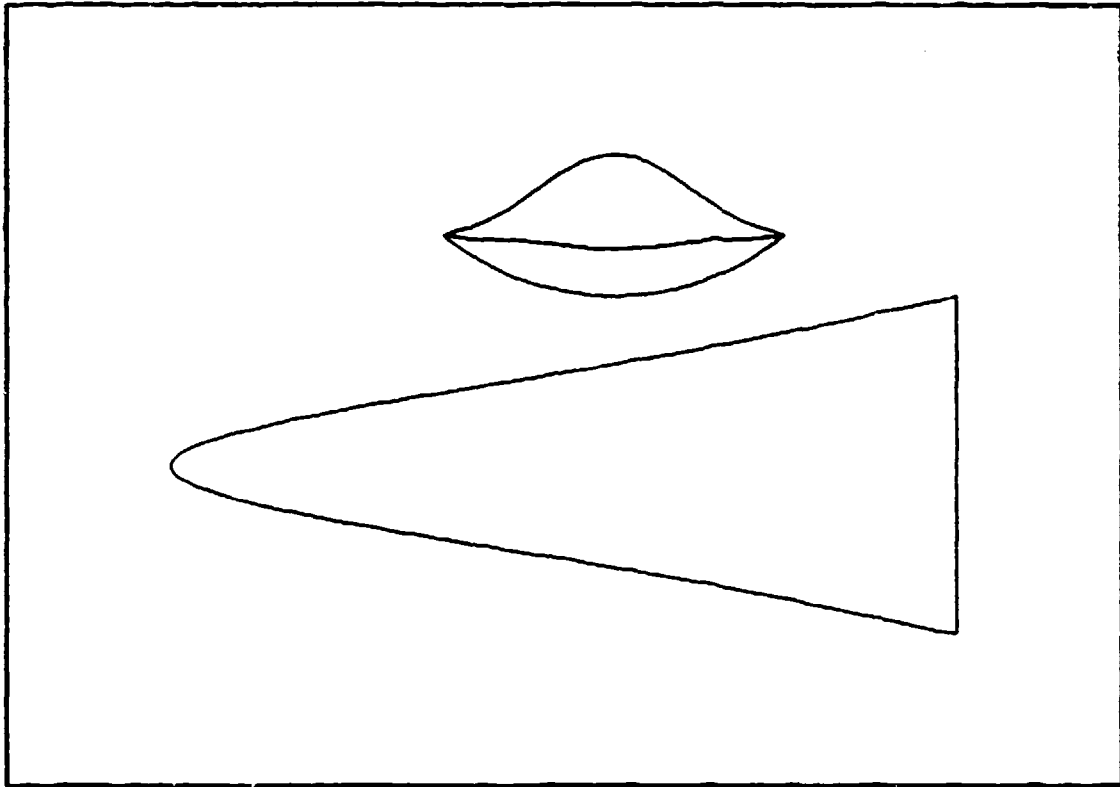


Figure D.10

Table D.10

Phi =40.0	Delta = 8.0	Mach =10.0	Rey = 0.10E+07	Gamma = 1.40
$X = 0.600 + 1.457 Y^2 + -2.000 Y^4 + 1.053 Y^6$				
Cftav = 0.001884	CL = 0.042278	CD = 0.008783		
Sw/Sp = 2.127193	V^(2/3)/Sp = 0.191596	(L/D)vis = 4.813523		
Ab/Abi = 0.584419	V/Vi = 0.347349	Sp/Spi = 0.601709		
b/lw = 0.432390	SSD = 0.236489			

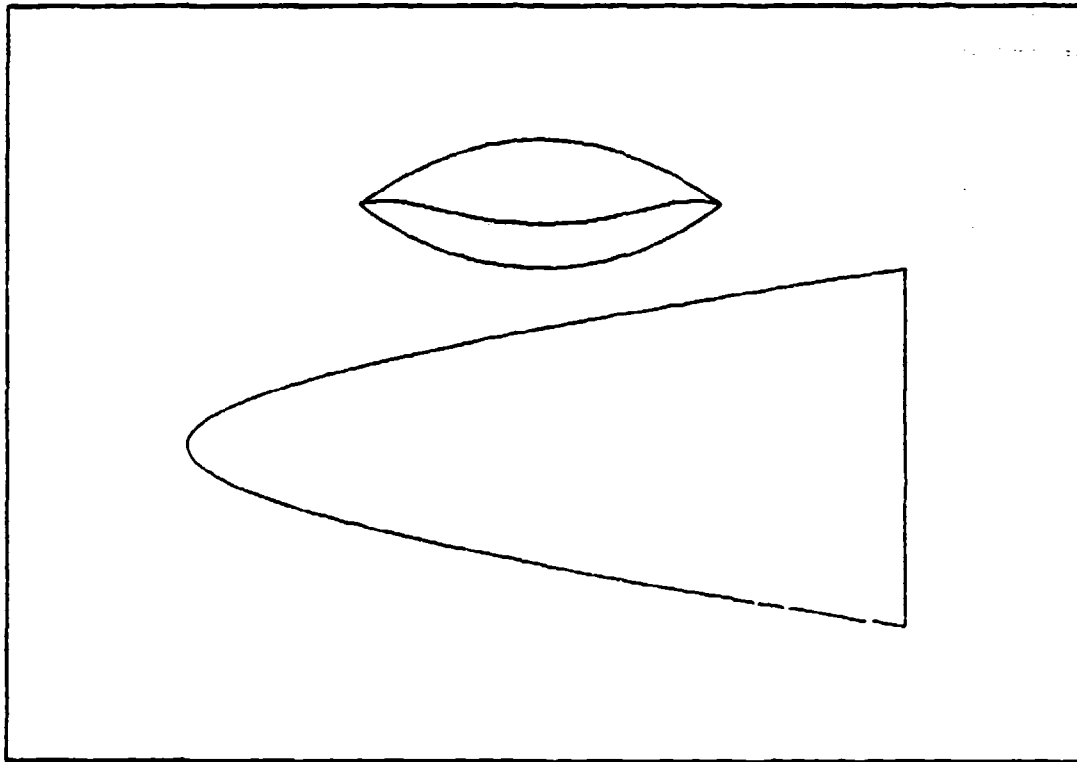


Figure D.11

Table D.11

Phi =40.0	Delta = 8.0	Mach =10.0	Rey = 0.10E+07	Gamma = 1.40
$X = 0.700 + 0.434 Y^2 + 0.000 Y^4 + -0.013 Y^6$				
Cftav = 0.001833	CL = 0.041974	CD = 0.008546		
Sw/Sp = 2.055271	$V^{(2/3)}/Sp = 0.181677$	(L/D)vis = 4.911695		
Ab/Abi = 0.577278	V/Vi = 0.310836	Sp/Spi = 0.589272		
b/lw = 0.503414	SSD = 0.211550			

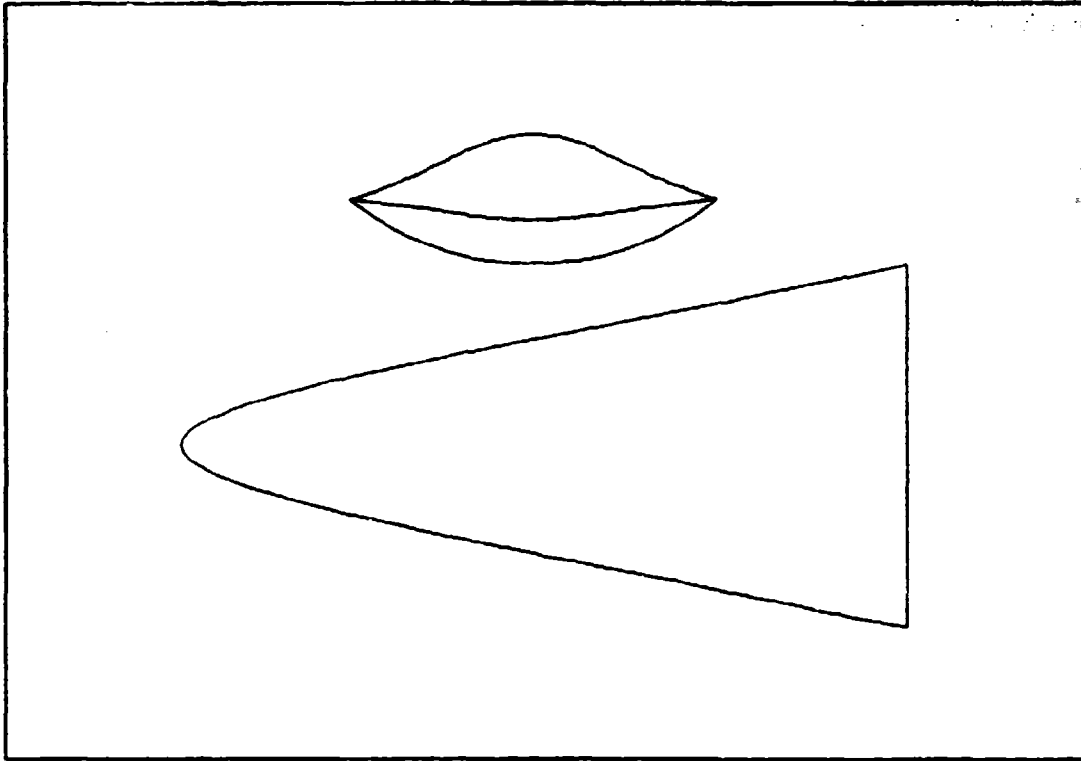


Figure D.12

Table D.12

Phi =40.0	Delta = 8.0	Mach =10.0	Rey = 0.10E+07	Gamma = 1.40
$X = 0.700 + 0.891 Y^2 + -1.000 Y^4 + 0.487 Y^6$				
Cftav = 0.001866	CL = 0.041880	CD = 0.008588		
Sw/Sp = 2.065478	V^(2/3)/Sp = 0.181381	(L/D)vis = 4.876789		
Ab/Ab1 = 0.530814	V/V1 = 0.276368	Sp/Sp1 = 0.545752		
b/lw = 0.503414	SSD = 0.211550			

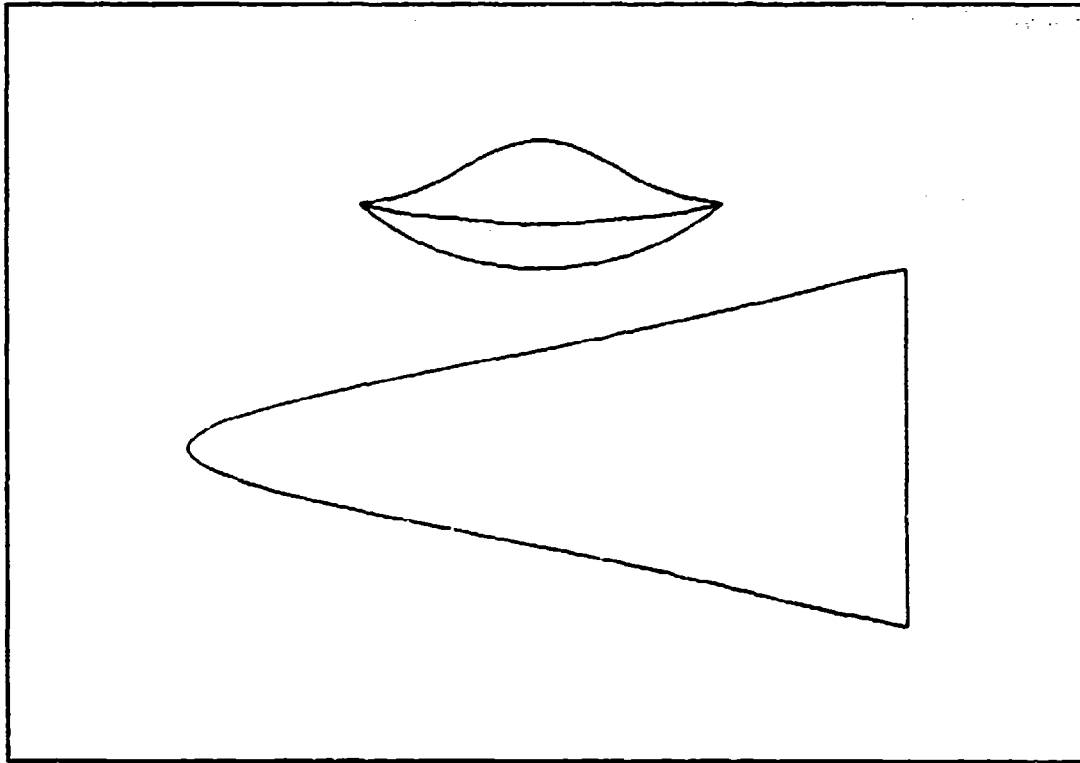


Figure D.13

Table D.13

Phi =40.0	Delta = 8.0	Mach =10.0	Rey = 0.10E+07	Gamma = 1.40
$X = 0.700 + 1.245 Y^2 + -2.000 Y^4 + 1.194 Y^6$				
Cftav = 0.001891	CL = 0.041818	CD = 0.008842		
Sw/Sp = 2.080921	Y^(2/3)/Sp = 0.181055	(L/D)vis = 4.838809		
Ab/Abi = 0.504018	Y/Yi = 0.256373	Sp/Sp1 = 0.520036		
b/lw = 0.503414	SSD = 0.211550			

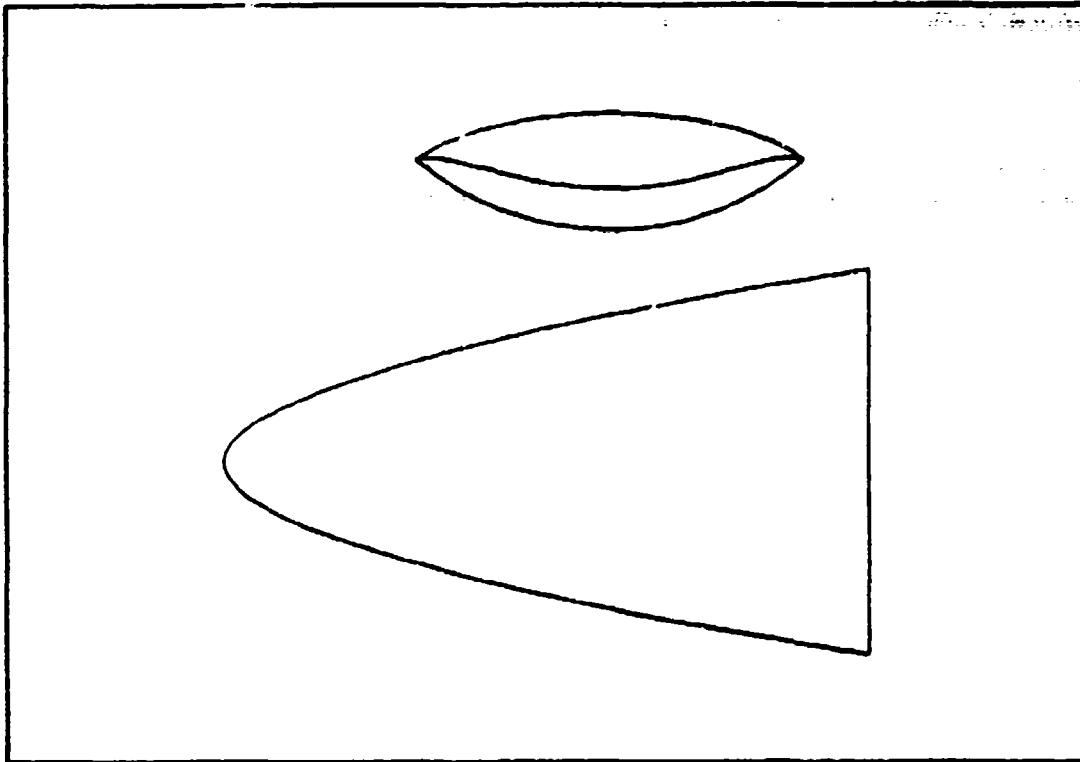


Figure D.14

Table D.14

Phi =40.0	Delta = 8.0	Mach =10.0	Rey = 0.10E+07	Gamma = 1.40
I = 0.800 + 0.222 Y^2 + 0.000 Y^4 + 0.128 Y^6				
Cftav = 0.001814	CL = 0.041516	CD = 0.008402		
Sw/Sp = 2.031092	V^(2/3)/Sp = 0.170501	(L/D)vis = 4.941123		
Ab/Abi = 0.496875	V/Vi = 0.225988	Sp/Sp1 = 0.507682		
b/lw = 0.602357	SSD = 0.183460			

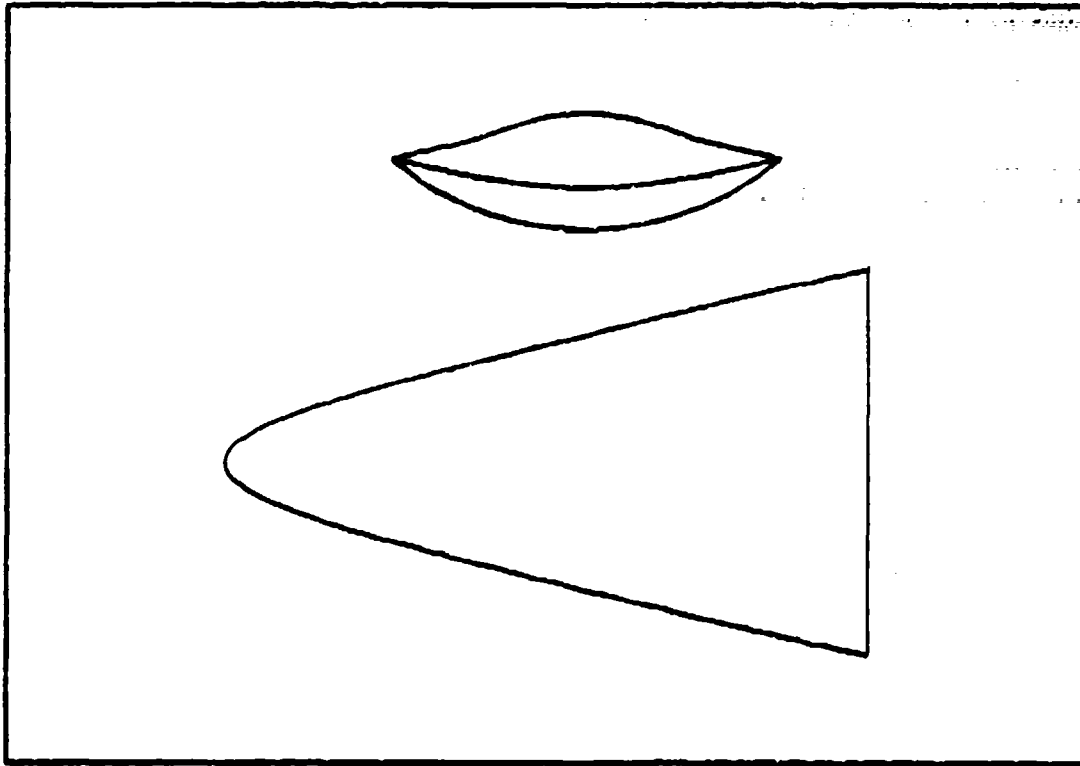


Figure D.15

Table D.15

Phi =40.0	Delta = 0.0	Mach =10.0	Rey = 0.10E+07	Gamma = 1.40
$X = 0.000 + 0.679 Y'^2 + -1.000 Y'^4 + 0.628 Y'^6$				
Cftav = 0.001064	CL = 0.041412	CD = 0.008462		
Sw/Sp = 2.035007	Y'(2/3)/Sp = 0.169021	(L/D)vis = 4.893669		
Ab/Ab1 = 0.460411	Y/Y1 = 0.196078	Sp/Sp1 = 0.463604		
b/lw = 0.602367	SSD = 0.183460			

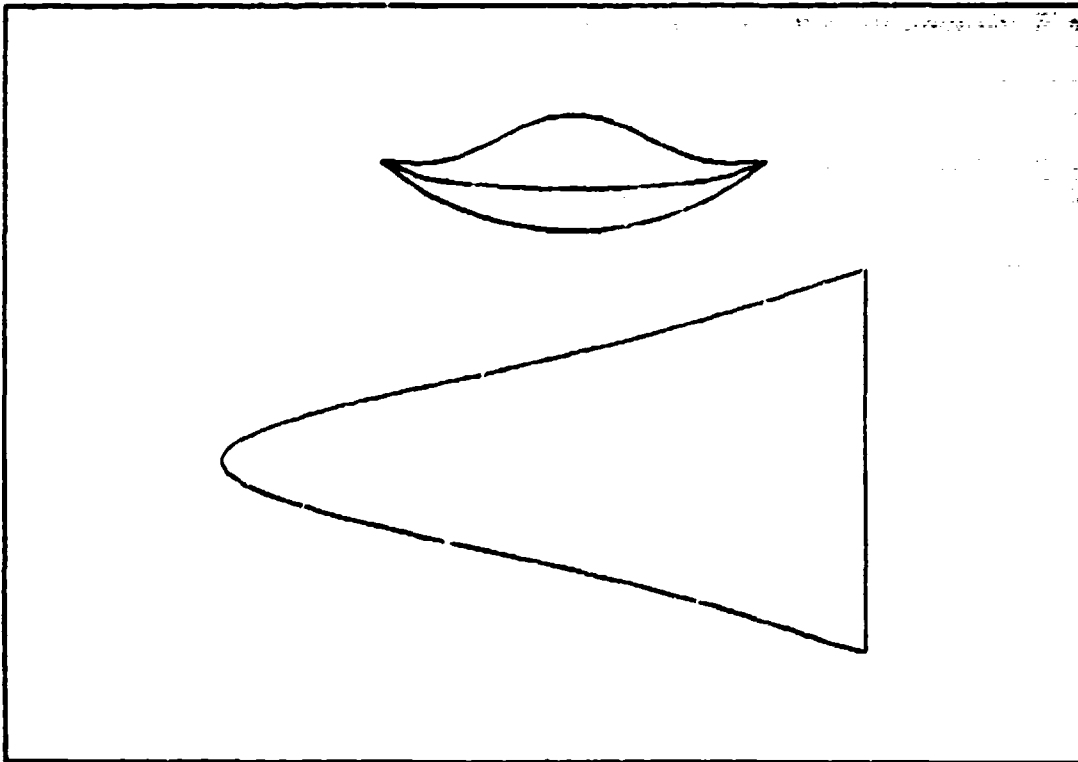


Figure D.16

Table D.16

Phi =40.0	Delta = 8.0	Mach =10.0	Rey = 0.10E+07	Gamma = 1.40
$X = 0.800 + 1.137 Y^2 + -2.000 Y^4 + 1.128 Y^6$				
Cftav = 0.001915	CL = 0.041839	CD = 0.008571		
Sw/Sy = 2.081023	V*(2/3)/Sp = 0.171124	(L/D)vis = 4.823078		
Ab/Ab1 = 0.403946	V/V1 = 0.170474	Sp/Sp1 = 0.419171		
b/lw = 0.602357	SSD = 0.183460			

APPENDIX E

Presented here are configurations that have the following parameters held fixed:

$$\phi_1 = 30, \quad \delta = 8, \quad M = 10, \quad \text{Re}_y = 1 \times 10^6$$

The following parameters are varied:

$$R_0 \text{ from } 0.5 \text{ to } 0.9$$

$$b_1 \text{ from } 0.0 \text{ to } -15.0$$

The values of b_2 and b_6 are such that equation 2-13 and condition (iii) holds.

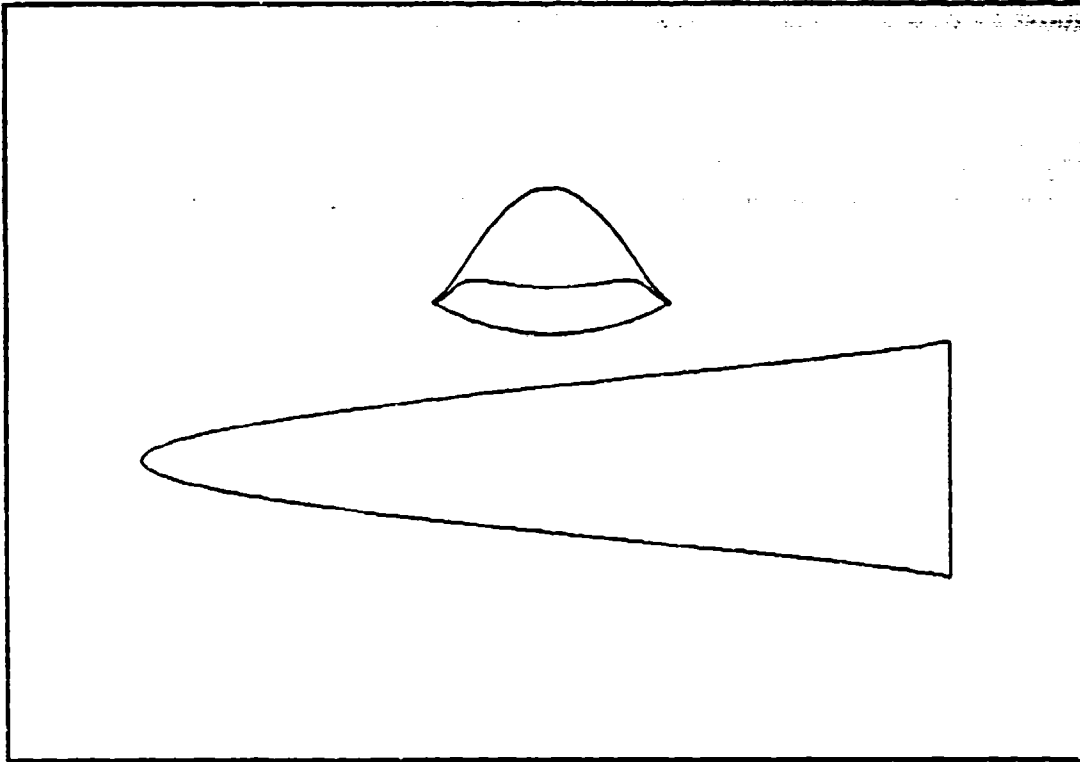


Figure E.1

Table E.1

Phi =30.0	Delta = 8.0	Mach =10.0	Rey = 0.10E+07	Gamma = 1.40
$I = 0.500 + 2.019 Y^2 + 0.000 Y^4 + -2.943 Y^6$				
Cftav = 0.001849	CL = 0.042870	CD = 0.009184		
Sw/Sp = 2.387981	V^(2/3)/Sp = 0.217357	(L/D)vis = 4.667721		
Ab/Ab1 = 0.725007	V/V1 = 0.515734	Sp/Sp1 = 0.732560		
b/lw = 0.294754	SSD = 0.258054			

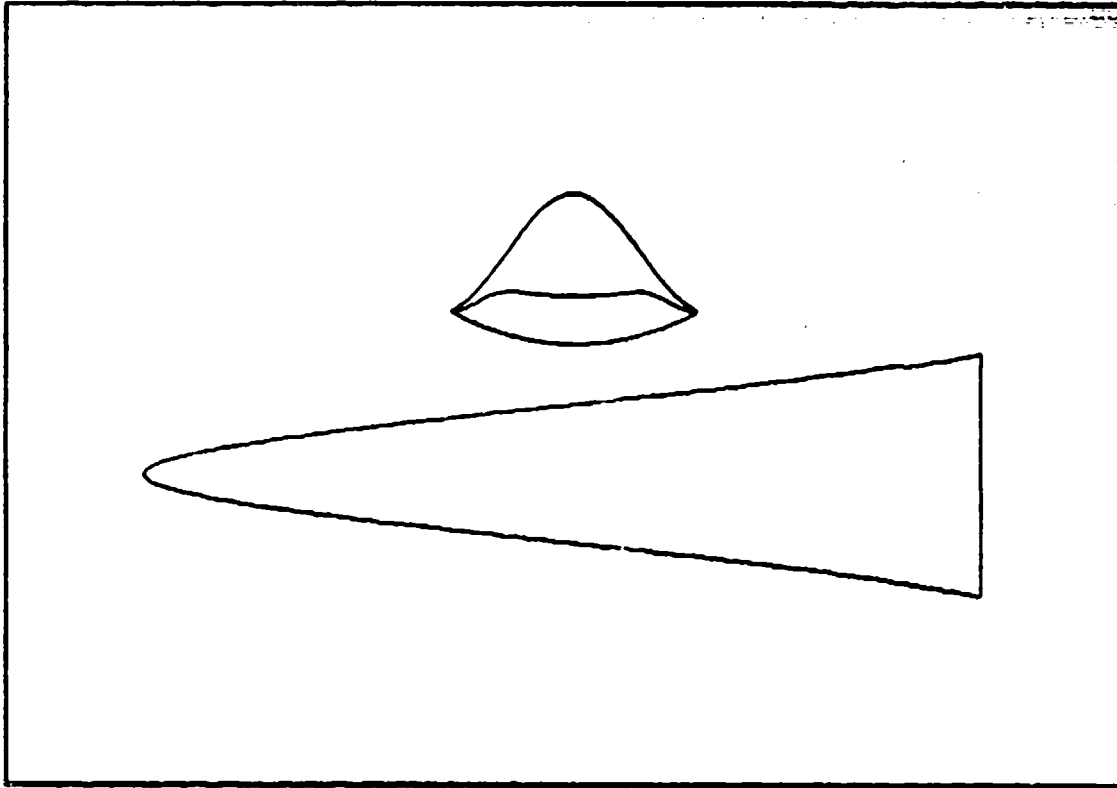


Figure E.2

Table E.2

Phi =30.0	Delta = 8.0	Mach =10.0	Rey = 0.10E+07	Gamma = 1.40
X = 0.500 + 3.089 Y^2 + -5.000 Y^4 + 2.895 Y^6				
Cftav = 0.001857	CL = 0.042758	CD = 0.009247		
Sw/Sp = 2.429212	V^(2/3)/Sp = 0.217310	(L/D)vis = 4.623816		
Ab/Ab1 = 0.674038	V/V1 = 0.464878	Sp/Sp1 = 0.683721		
b/lw = 0.294754	SSD = 0.258054			

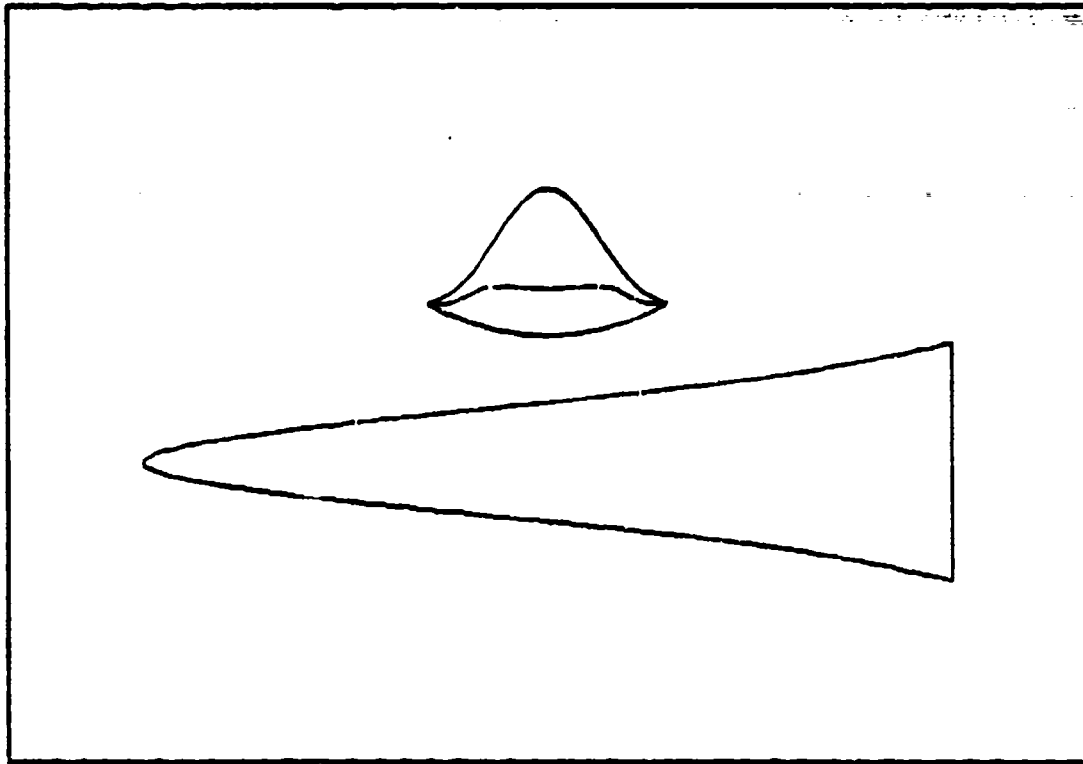


Figure E.3

Table E.3

Phi =30.0	Delta = 8.0	Mach =10.0	Rey = 0.10E+07	Gamma = 1.40
$X = 0.500 + 4.160 Y^2 + -10.000 Y^4 + 8.733 Y^6$				
Cftav = 0.001000	CL = 0.042071	CD = 0.009392		
8w/8p = 2.509903	V'(2/3)/8p = 0.218708	(L/D)vis = 4.543412		
Ab/Abi = 0.623006	V/Vi = 0.419518	8p/8pi = 0.624407		
b/lw = 0.294754	88D = 0.258054			

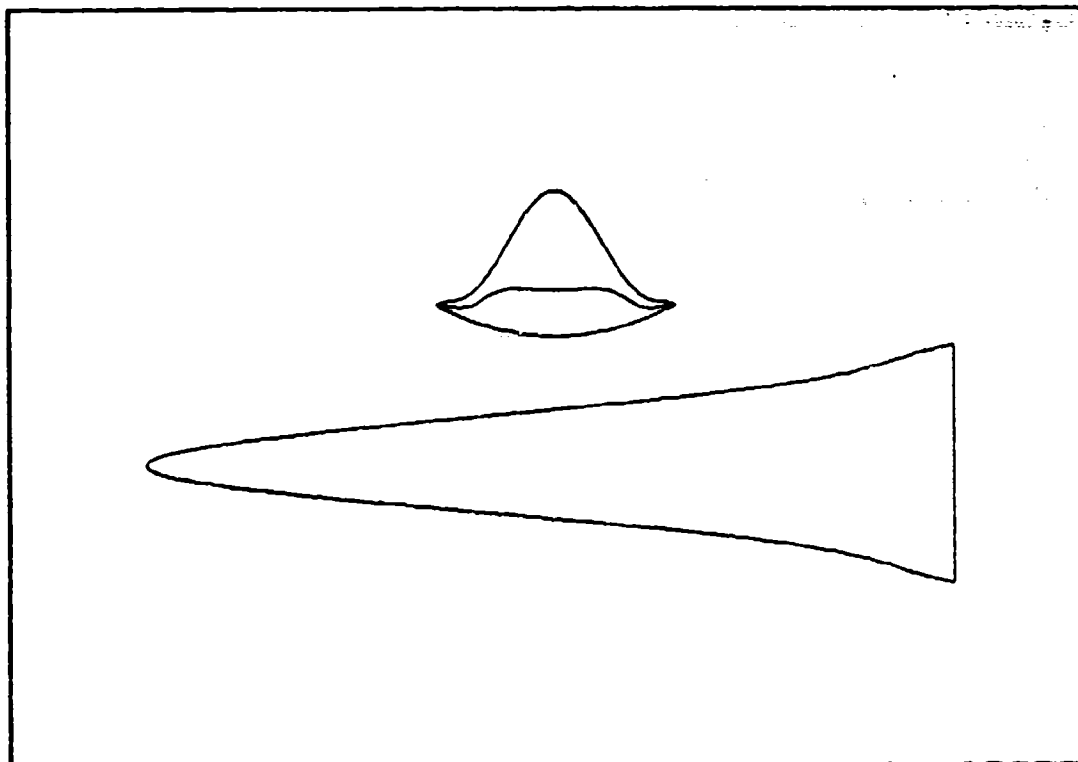


Figure E.4

Table E.4

Phi =30.0	Delta = 8.0	Mach =10.0	Rey = 0.10E+07	Gamma = 1.40
I = 0.500 + 5.212 Y^2 + -15.000 Y^4 + 14.670 Y^6				
Cftav = 0.001879	CL = 0.042618	CD = 0.009808		
Sw/Sp = 2.620803	V^(2/3)/Sp = 0.221677	(L/D)vis = 4.435354		
Ab/Ab1 = 0.574256	V/V1 = 0.380793	Sp/Sp1 = 0.586776		
b/lw = 0.294754	SSD = 0.258054			

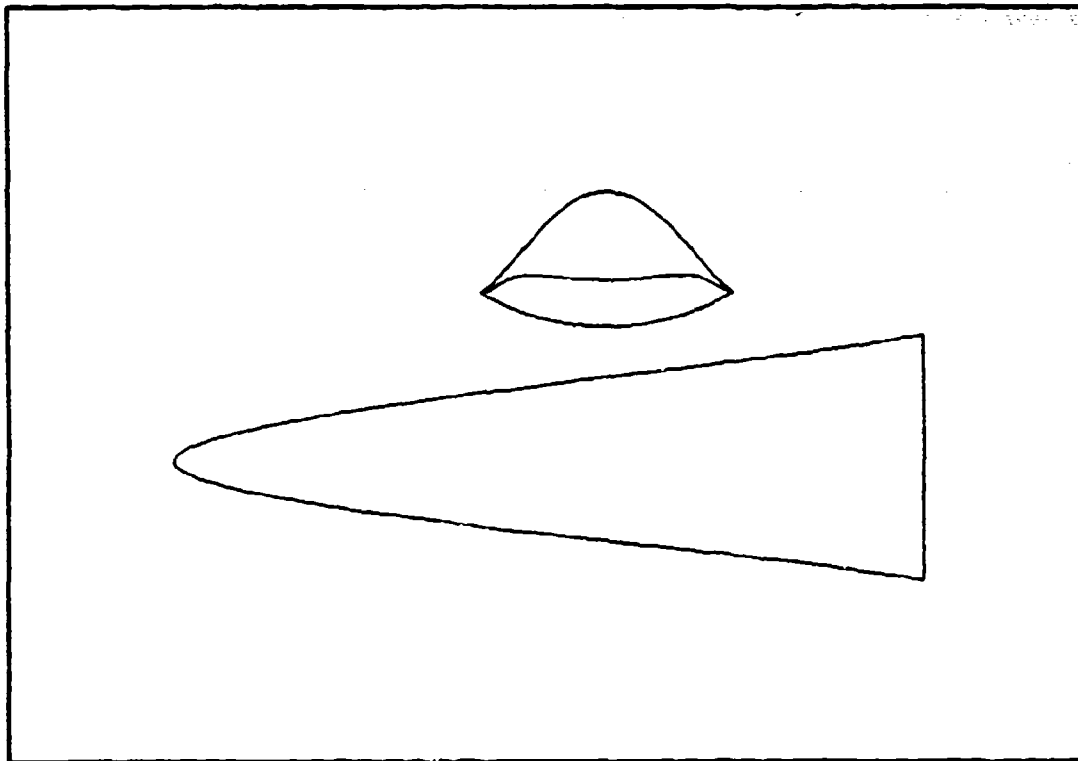


Figure E.5

Table E.5

Phi = 30.0	Delta = 8.0	Mach = 10.0	Re _y = 0.10E+07	Gamma = 1.40
$X = 0.800 + 1.669 Y^2 + 0.000 Y^4 + -2.306 Y^6$				
C _{ftav} = 0.001845	C _L = 0.042420		C _D = 0.008904	
S _w /S _p = 2.277009	V ^(2/3) /S _p = 0.207252		(L/D) _{vis} = 4.764273	
Ab/Abi = 0.641628	V/Vi = 0.400941		Sp/Spi = 0.649562	
b/lw = 0.336339	SSD = 0.236489			

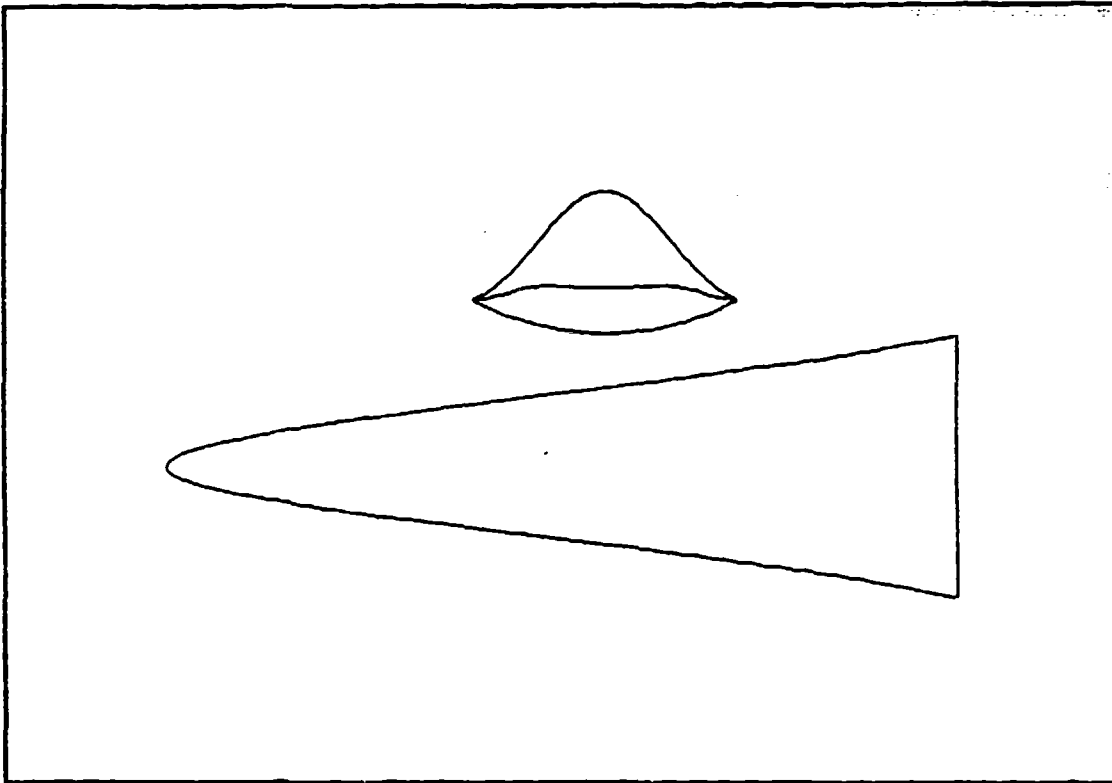


Figure E.6

Table E.6

Phi = 30.0	Delta = 8.0	Mach = 10.0	Rey = 0.10E+07	Gamma = 1.40
$X = 0.600 + 2.739 Y^2 + -5.000 Y^4 + 3.531 Y^6$				
Cftav = 0.001863	CL = 0.042302	CD = 0.008987		
Sw/Sp = 2.317458	V^(2/3)/Sp = 0.207171	(L/D)vis = 4.707104		
Ab/Ab1 = 0.590635	V/V1 = 0.355951	Sp/Spi = 0.600247		
b/lw = 0.336339	SSD = 0.236489			

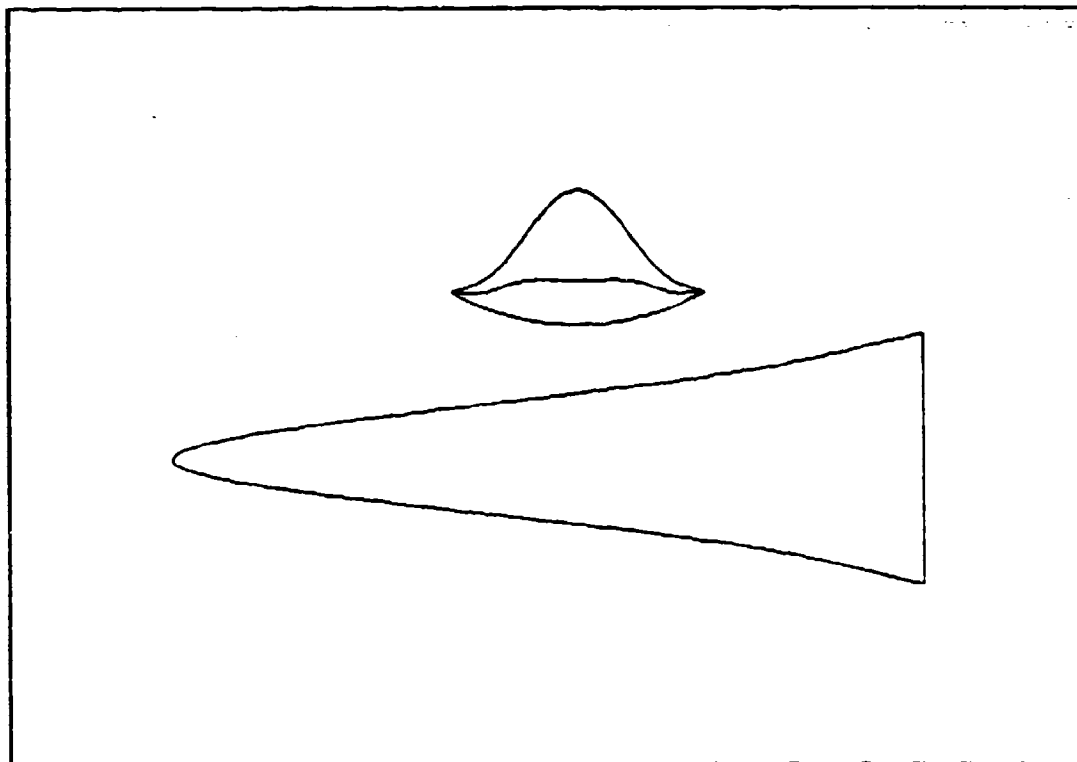


Figure E.7

Table E.7

Phi =30.0	Delta = 8.0	Mach =10.0	Rey = 0.10E+07	Gamma = 1.40
X = 0.600 + 3.810 Y^2 + -10.000 Y^4 + 9.369 Y^6				
Cftav = 0.001881	CL = 0.042215	CD = 0.009155		
Sw/Sp = 2.399240	V^(2/3)/Sp = 0.208868	(L/D)vis = 4.611248		
Ab/Abi = 0.539665	V/Vi = 0.316522	Sp/Spi = 0.550550		
b/lw = 0.336339	SSD = 0.236489			

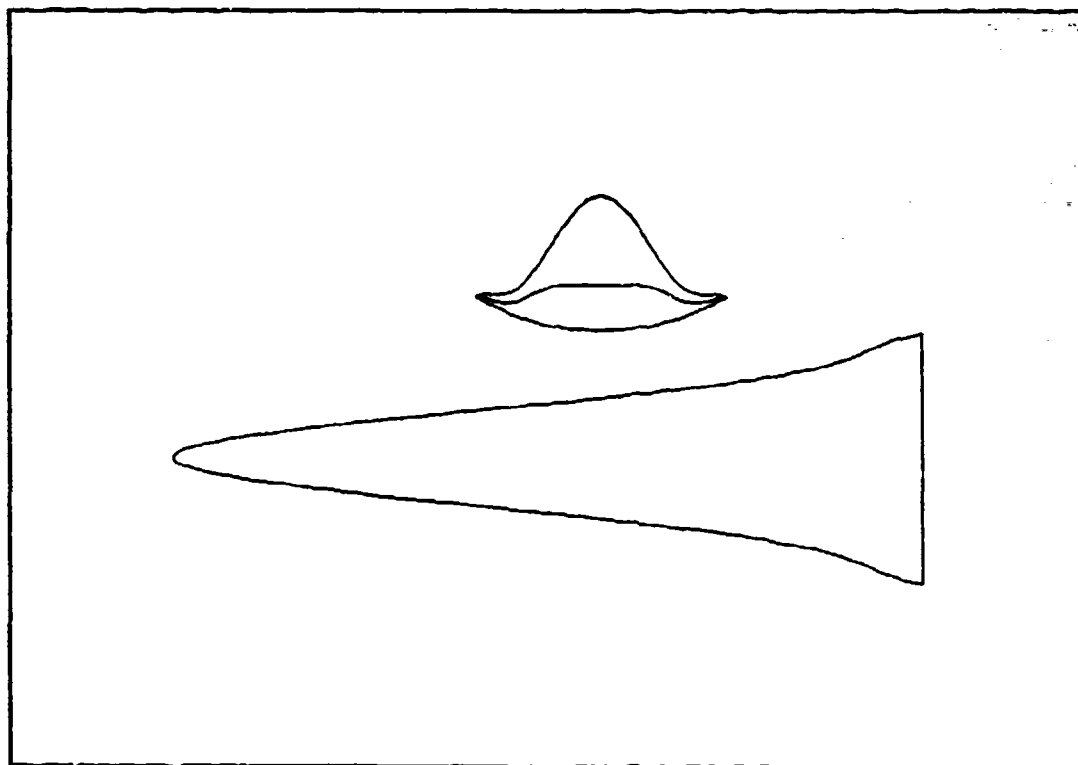


Figure E.8

Table E.8

Phi =30.0	Delta = 8.0	Mach =10.0	Rey = 0.10E+07	Gamma = 1.40
$X = 0.600 + 4.981 Y^2 + -15.000 Y^4 + 15.205 Y^6$				
Cftav = 0.001902	CL = 0.042170	CD = 0.009410		
Sw/Sp = 2.518831	V^(2/3)/Sp = 0.213079	(L/D)vis = 4.481304		
Ab/Abi = 0.488651	V/Vi = 0.282666	Sp/Spi = 0.500467		
b/lw = 0.536339	SSD = 0.238489			

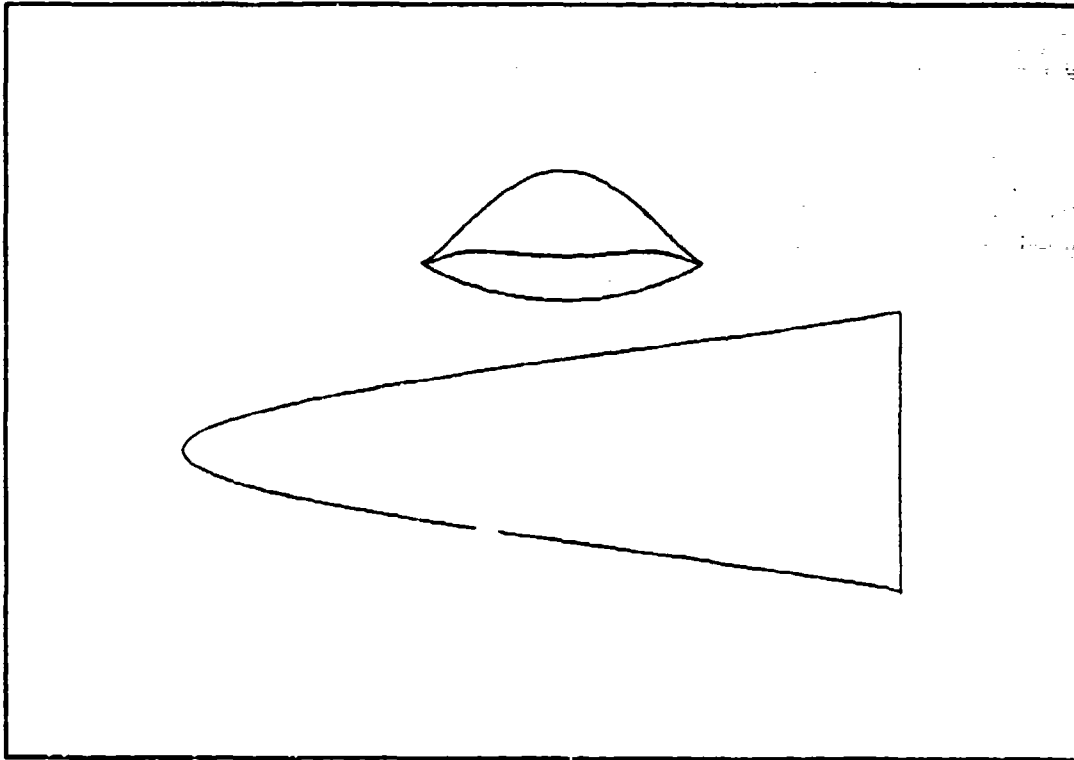


Figure E.9

Table E.9

Phi =30.0	Delta = 8.0	Mach =10.0	Rey = 0.10E+07	Gamma = 1.40
$X = 0.700 + 1.318 Y^2 + 0.000 Y^4 + -1.667 Y^6$				
Cftav = 0.001840	CL = 0.041957	CD = 0.008657		
Sw/Sp = 2.183216	V^(2/3)/Sp = 0.198271	(L/D)vis = 4.846844		
Ab/Abi = 0.558292	V/Vi = 0.300542	Sp/Spi = 0.565997		
b/lw = 0.391586	SSD = 0.211550			

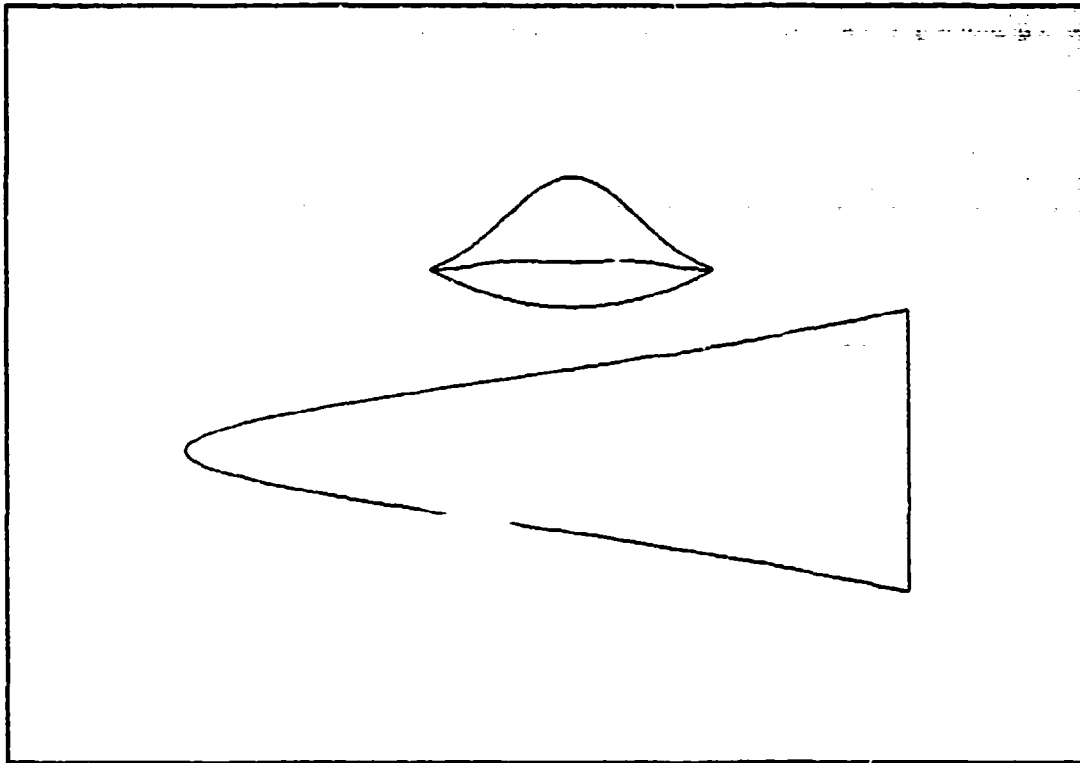


Figure E.10

Table E.10

Phi =30.0	Delta = 8.0	Mach =10.0	Rey = 0.10E+07	Gamma = 1.40
$X = 0.700 + 2.389 Y^2 + -5.000 Y^4 + 4.167 Y^6$				
Cftav = 0.001871	CL = 0.041834	CD = 0.008763		
Sw/Sp = 2.221092	V^(2/3)/Sp = 0.198094	(L/D)vis = 4.774157		
Ab/Abi = 0.507235	V/Vi = 0.261449	Sp/Sp1 = 0.516250		
b/lw = 0.391596	SSD = 0.211550			

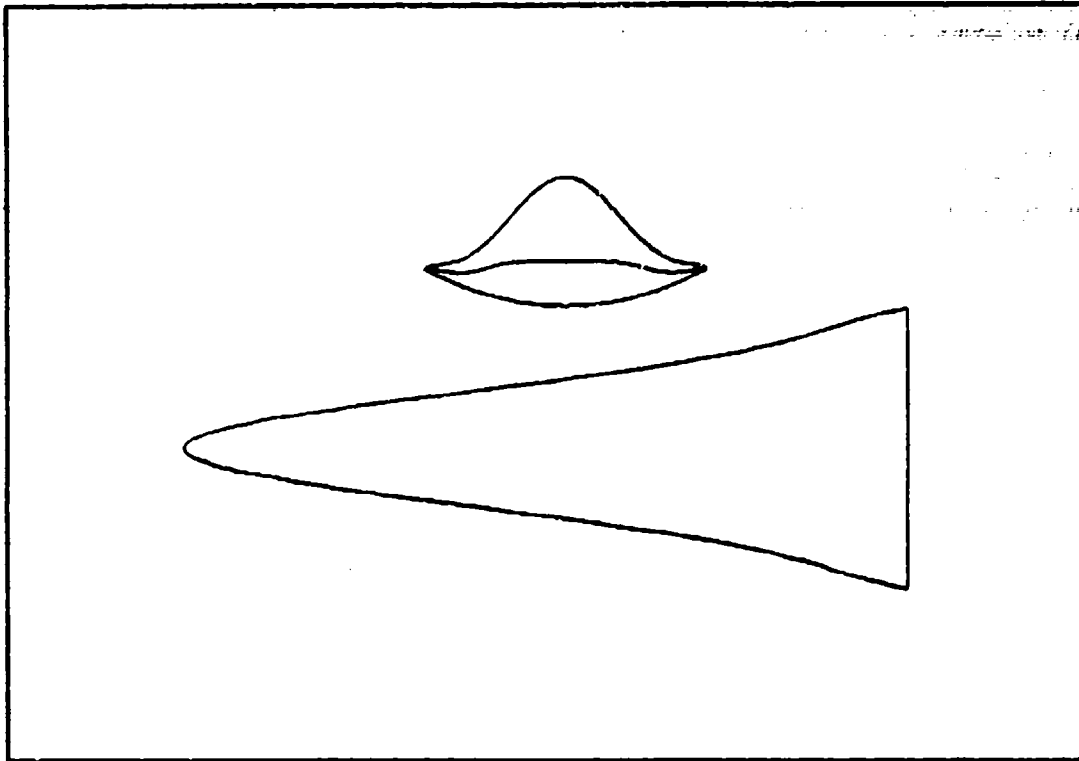


Figure E.11

Table E.11

Phi =30.0	Delta = 8.0	Mach =10.0	Rey = 0.10E+07	Gamma = 1.40
$X = 0.700 + 3.480 Y^2 + -10.000 Y^4 + 10.000 Y^6$				
Cftav = 0.001903	CL = 0.041748	CD = 0.008959		
Sw/Sp = 2.302922	V^(2/3)/Sp = 0.198184	(L/D)vis = 4.659729		
Ab/Abi = 0.456286	V/Vi = 0.228006	Sp/Sp1 = 0.486280		
b/lw = 0.391586	SSD = 0.211550			

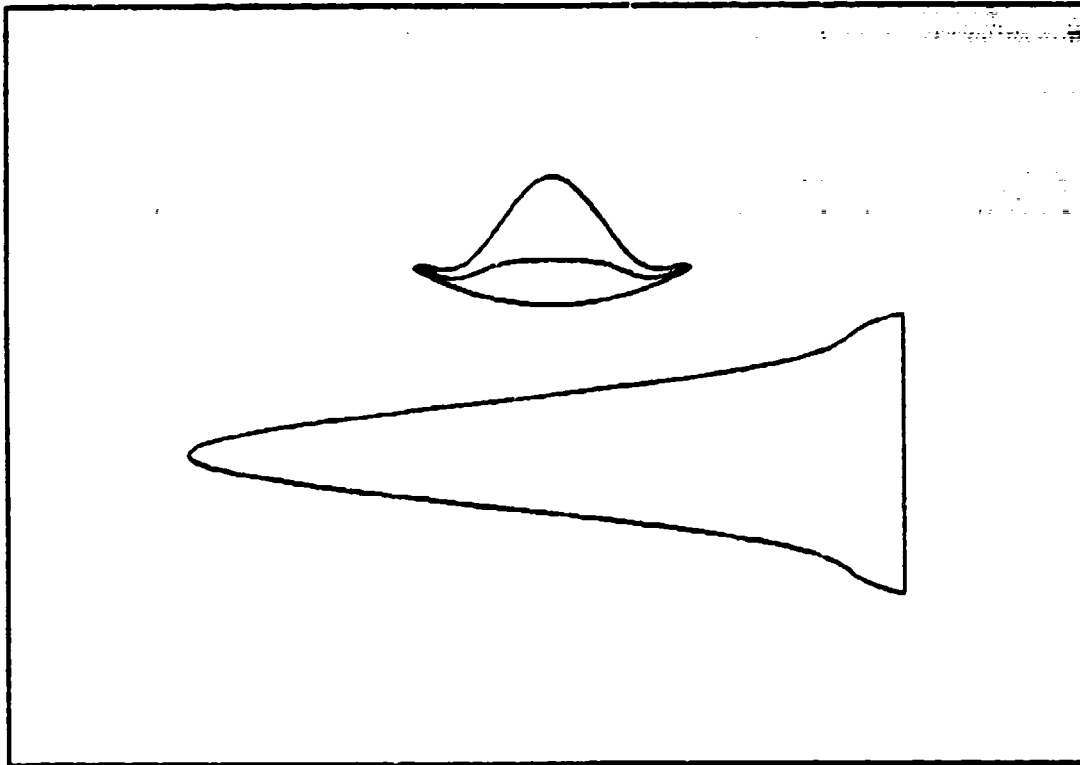


Figure E.12

Table E.12

Phi =30.0	Delta = 0.0	Mach =10.0	Rey = 0.10E+07	Gamma = 1.40
X = 0.700 + 4.532 Y^2 + -15.000 Y^4 + 15.835 Y^6				
Cftav = 0.001936	CL = 0.041715	CD = 0.009249		
Sw/Sp = 2.424993	V^(2/3)/Sp = 0.203740	(L/D)vis = 4.510335		
Ab/Abi = 0.405119	V/Vi = 0.200114	Sp/Sp1 = 0.415759		
b/lw = 0.391586	SSD = 0.211550			

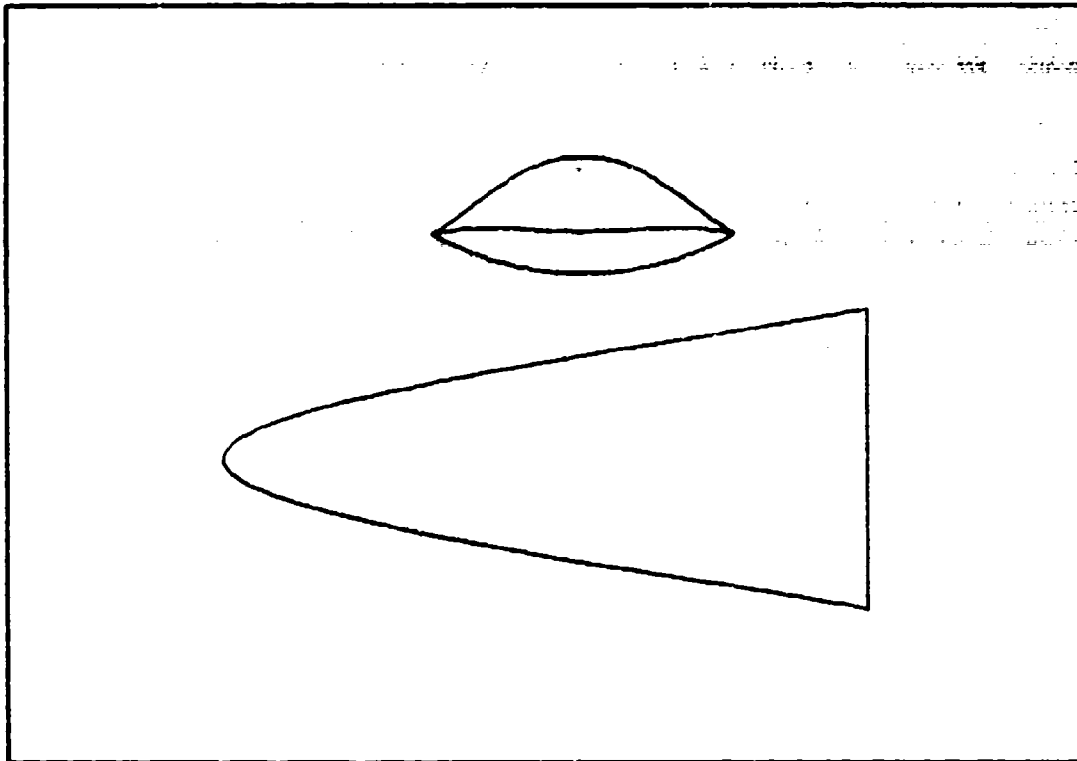


Figure E.13

Table E.13

Phi =30.0	Delta = 8.0	Mach =10.0	Rey = 0.10E+07	Gamma = 1.40
I = 0.800 + 0.968 Y^2 + 0.000 Y^4 + -1.033 Y^6				
Cftav = 0.001833	CL = 0.041485	CD = 0.008441		
Sw/Sp = 2.107252	V^(2/3)/Sp = 0.184133	(L/D)vis = 4.914905		
Ab/Abi = 0.474848	V/Vi = 0.214528	Sp/Sp1 = 0.481883		
b/lw = 0.488550	SSD = 0.183460			

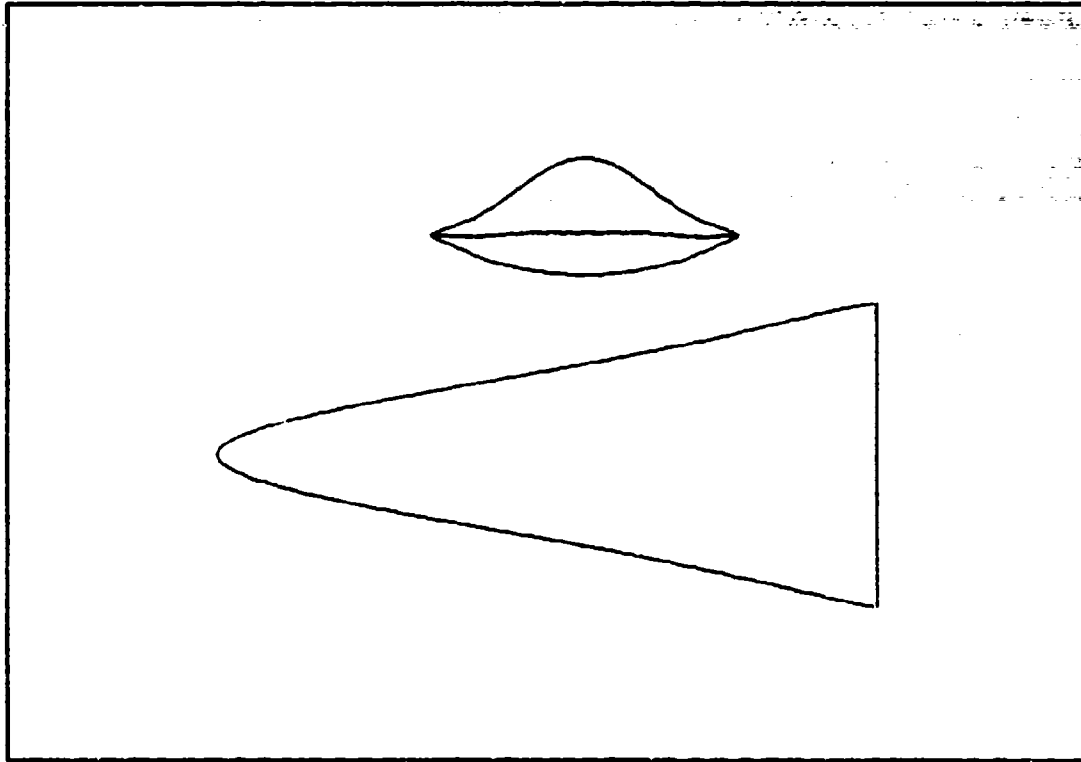


Figure E.14

Table E.14

Phi =30.0	Delta = 8.0	Mach =10.0	Rey = 0.10E+07	Gamma = 1.40
$X = 0.800 + 2.039 Y^2 + -5.000 Y^4 + 4.804 Y^6$				
Cftav = 0.001883	CL = 0.041357	CD = 0.008576		
Sw/Sp = 2.140818	V^(2/3)/Sp = 0.183749	(L/D)vis = 4.822828		
Ab/Abi = 0.423856	V/Vi = 0.181456	Sp/Spi = 0.431872		
b/lw = 0.468550	SSD = 0.183460			

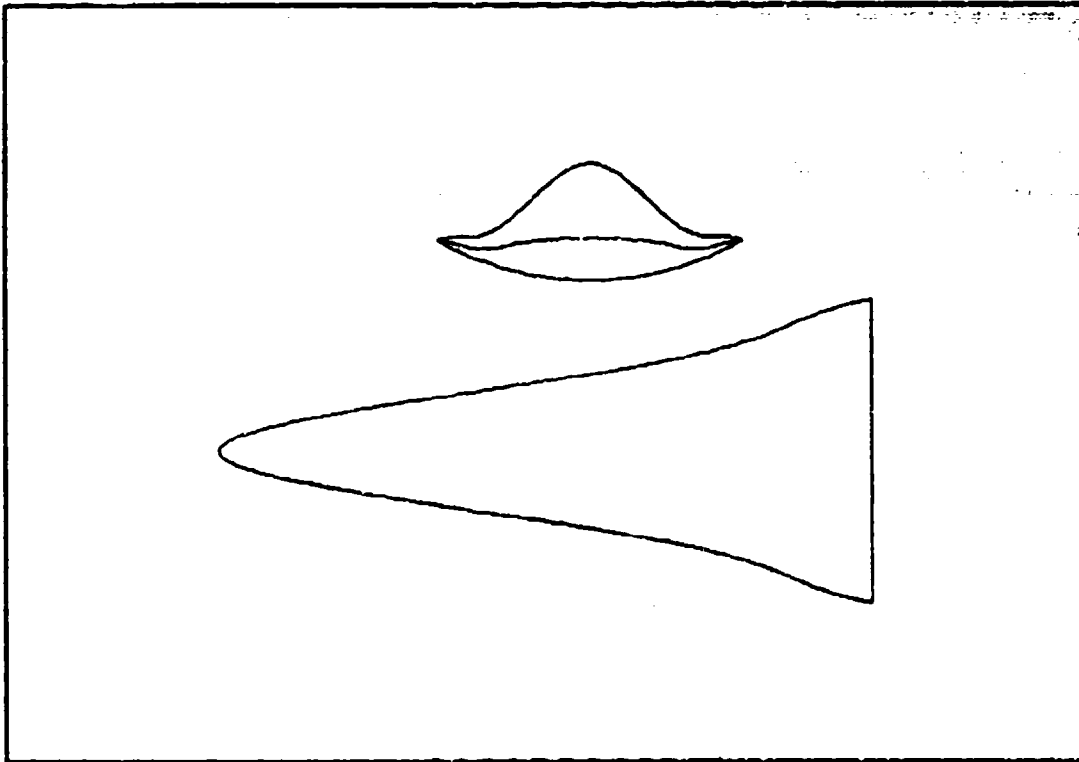


Figure E.15

Table E.15

Phi =30.0	Delta = 8.6	Mach =10.0	Rey = 0.10E+07	Gamma = 1.40
$X = 0.800 + 3.109 Y^2 + -10.000 Y^4 + 10.842 Y^6$				
Cftev = 0.001934	CL = 0.041275	CD = 0.008812		
Sw/Sp = 2.221630	V^(2/3)/Sp = 0.100425	(L/D)vis = 4.684116		
Ab/Abi = 0.372885	V/Vi = 0.154016	Sp/Sp1 = 0.381598		
b/lw = 0.468550	SSD = 0.183460			

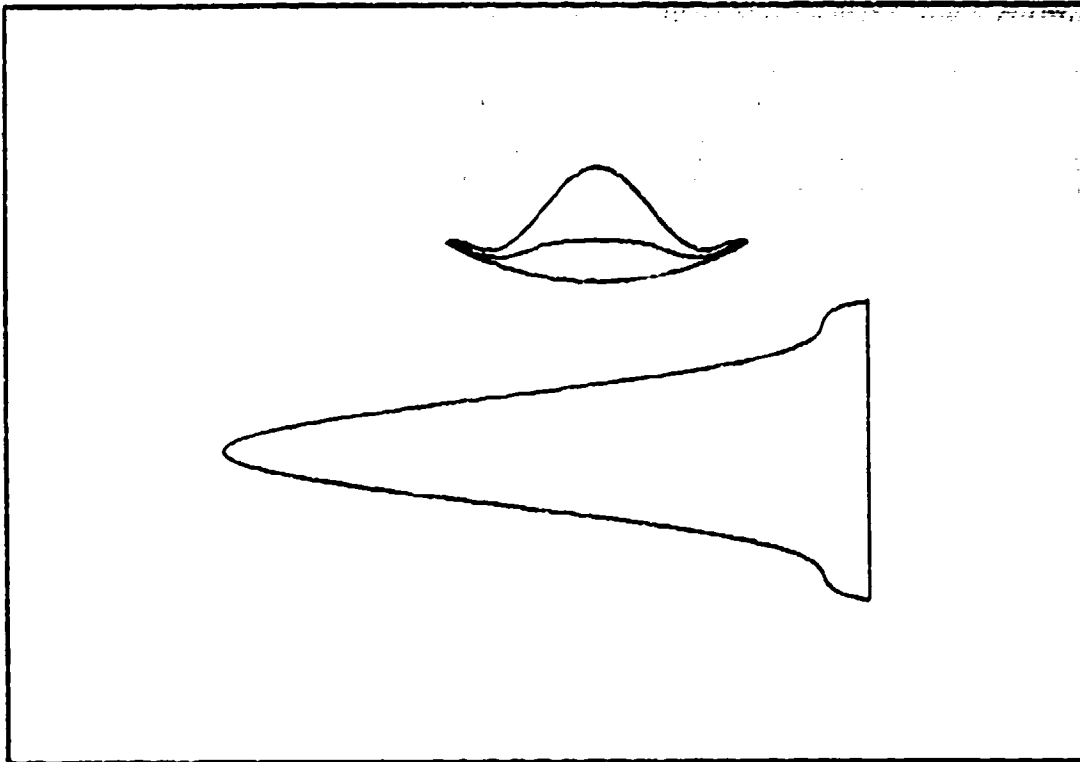


Figure E.16

Table E.16

$\Phi = 36.0$	$\Delta = 8.0$	$Mach = 10.0$	$Re = 0.10E+07$	$\Gamma = 1.40$
$X = 0.800 + 4.100 Y^2 + -15.000 Y^4 + 16.481 Y^6$				
$C_{ftav} = 0.001982$	$CL = 0.041260$	$CD = 0.009137$		
$S_w/S_p = 2.343866$	$V^{(2/3)}/S_p = 0.194103$	$(L/D)_{vis} = 4.515485$		
$A_b/A_{bl} = 0.321937$	$V/V_1 = 0.132237$	$S_p/S_{pi} = 0.331083$		
$b/lw = 0.468550$	$SSD = 0.183460$			

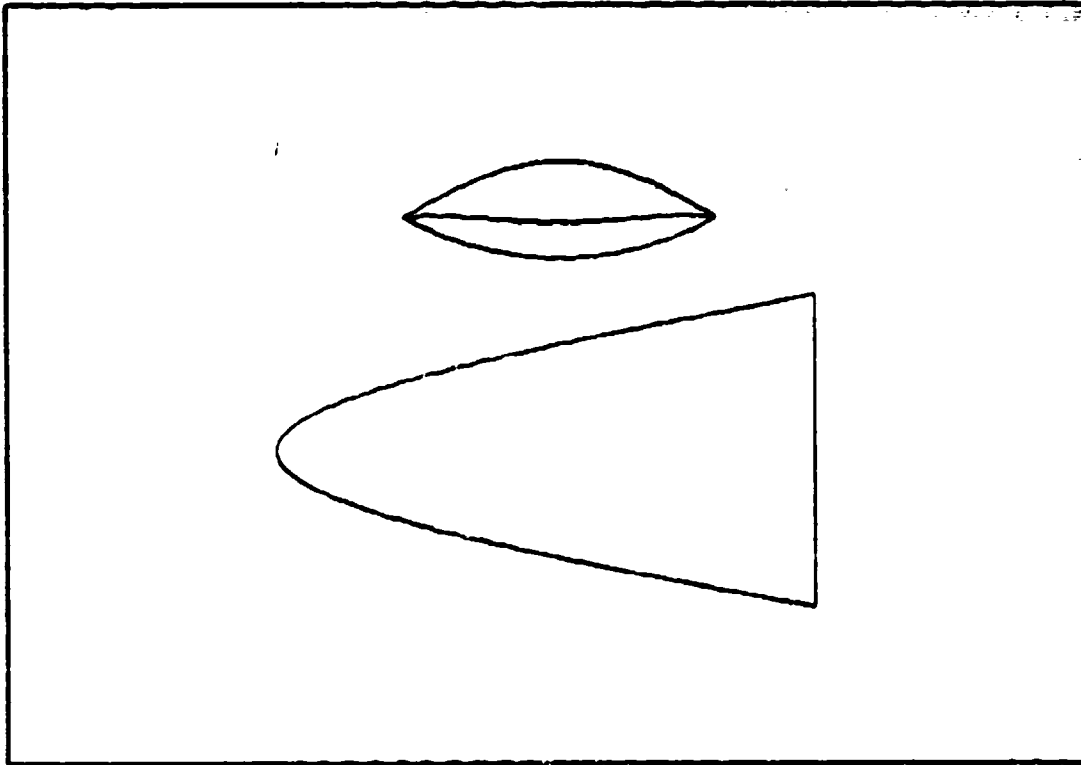


Figure E.17

Table E.17

Phi =30.0	Delta = 8.0	Mach =10.0	Rey = 0.10E+07	Gamma = 1.40
$I = 0.900 + 0.618 Y^2 + 0.000 Y^4 + -0.397 Y^6$				
Cftav = 0.001021	CL = 0.041009	CD = 0.000254		
Sw/Sp = 2.051210	V^(2/3)/Sp = 0.170417	(L/D)vis = 4.988442		
Ab/Abi = 0.391447	V/Vi = 0.143081	Sp/Spi = 0.397405		
b/lw = 0.583198	SBD = 0.152450			

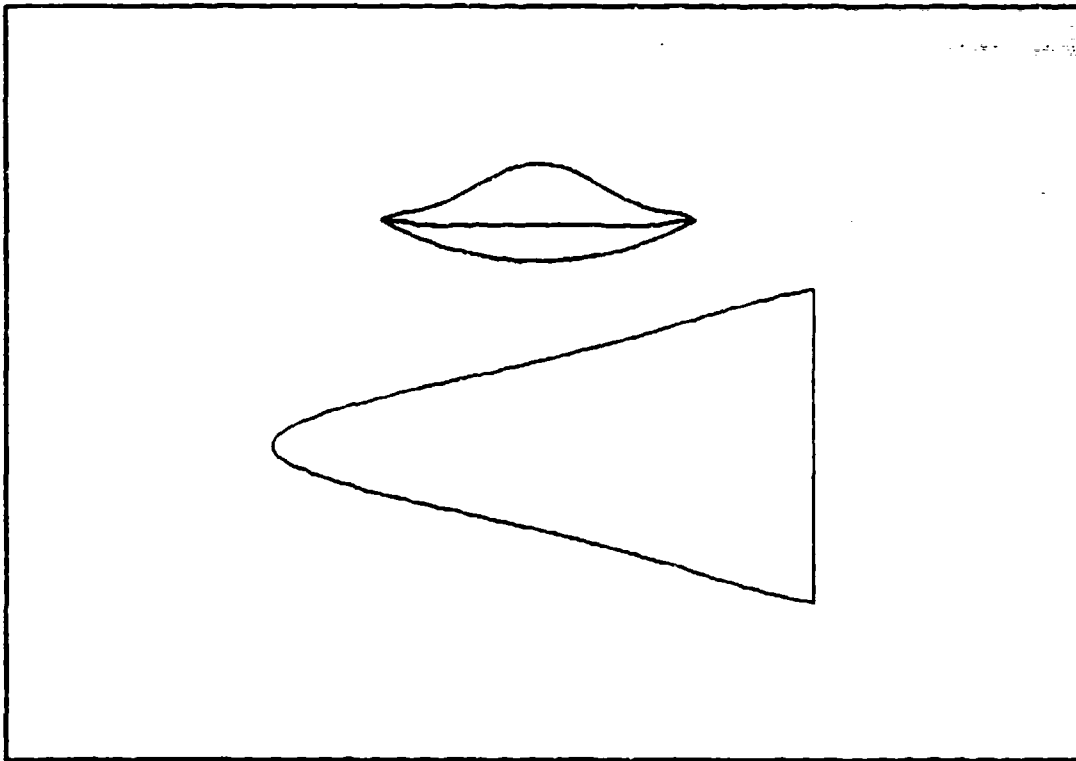


Figure E.18

Table E.18

Phi = 30.0	Delta = 8.0	Mach = 10.0	Rey = 0.10E+07	Gamma = 1.40
$X = 0.900 + 1.088 Y^2 + -5.000 Y^4 + 5.442 Y^6$				
Cftav = 0.001899	CL = 0.040875	CD = 0.008433		
Sw/Sp = 2.079087	V*(2/3)/Sp = 0.169635	(L/D)vis = 4.847222		
Ab/Abi = 0.340499	V/Vi = 0.116021	Sp/Sp1 = 0.347197		
b/lw = 0.563168	SSD = 0.152450			

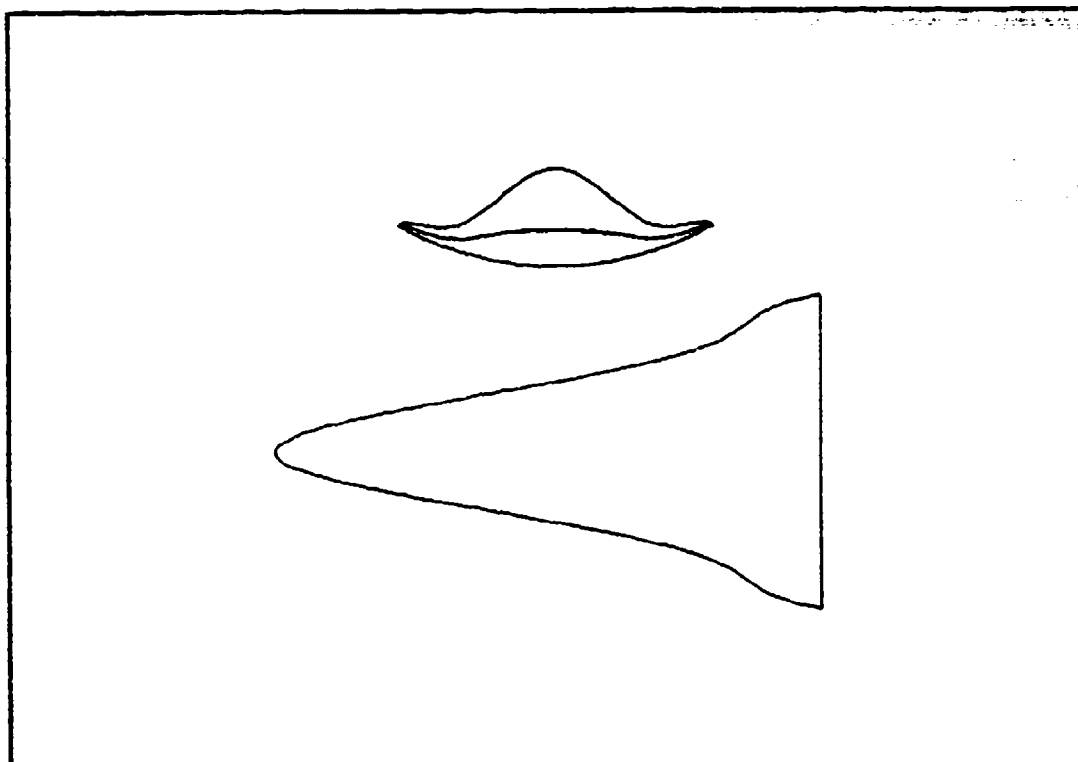


Figure E.19

Table E.19

Phi =30.0	Delta = 8.0	Mach =10.0	Rey = 0.10E+07	Gamma = 1.40
X = 0.900 + 2.759 Y^2 + -10.000 Y^4 + 11.280 Y^6				
Cftav = 0.001981	CL = 0.040799	CD = 0.008725		
Sw/Sp = 2.158927	V^(2/3)/Sp = 0.173278	(L/D)vis = 4.676111		
Ab/Abi = 0.289528	V/Vi = 0.094622	Sp/Spi = 0.296699		
b/lw = 0.583168	SSD = 0.152450			

APPENDIX F

Presented here are configurations that have the following parameters held fixed:

$$\phi_1 = 20, \quad \delta = 8, \quad M = 10, \quad \text{Rey} = 1 \times 10^6$$

The following parameters are varied:

$$R_0 \text{ from } 1.0 \text{ to } 1.1$$

$$b_4 \text{ from } 8.0 \text{ to } -8.0$$

The values of b_2 and b_6 are such that equation 2-13 and condition (iii) holds.

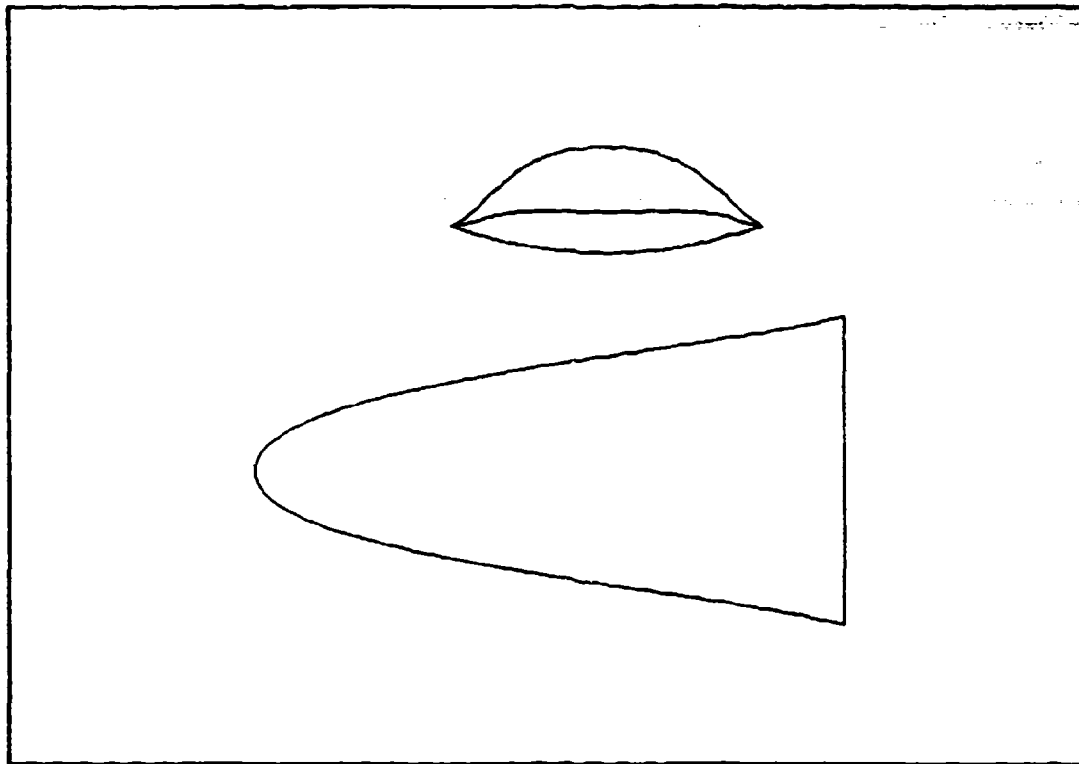


Figure F.1

Table F.1

Phi =20.0	Delta = 8.0	Mach =10.0	Rey = 0.10E+07	Gamma = 1.40
X = 1.000 + 0.725 Y^2 + 8.000 Y^4 + -29.400 Y^6				
Cftav = 0.001798	CL = 0.040560	CD = 0.008193		
Sw/Sp = 2.116358	V^(2/3)/Sp = 0.176644	(L/D)vic = 4.950312		
Ab/Abi = 0.305388	V/Vi = 0.087251	Sp/Spi = 0.307613		
b/lw = 0.528095	SSD = 0.118747			

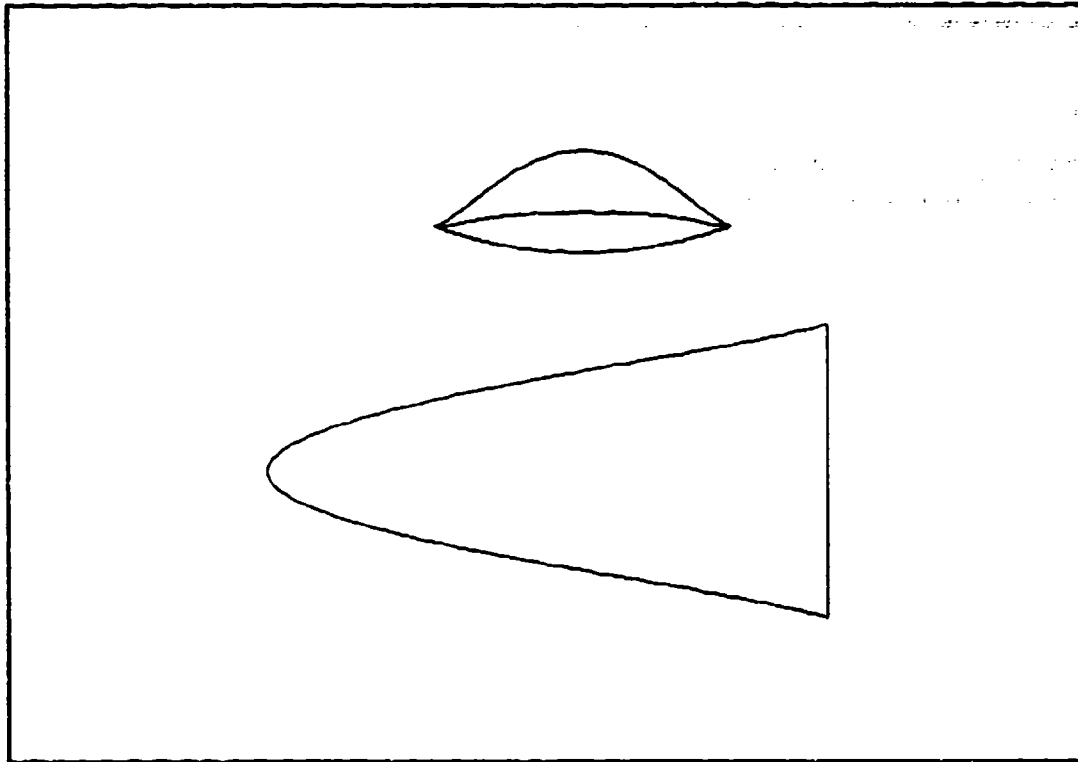


Figure F.2

Table F.2

Phi =20.0	Delta = 8.0	Mach =10.0	Rey = 0.10E+07	Gamma = 1.40
$I = 1.000 + 1.526 Y^2 + 0.000 Y^4 + -9.440 Y^6$				
Cftav = 0.001832	CL = 0.040506	CD = 0.008260		
Sw/Sp = 2.118220	V^(2/3)/sp = 0.175973	(L/D)vis = 4.903740		
Ab/Abi = 0.287061	V/Vi = 0.079159	Sp/Spi = 0.289387		
b/lw = 0.528095	SSD = 0.118747			

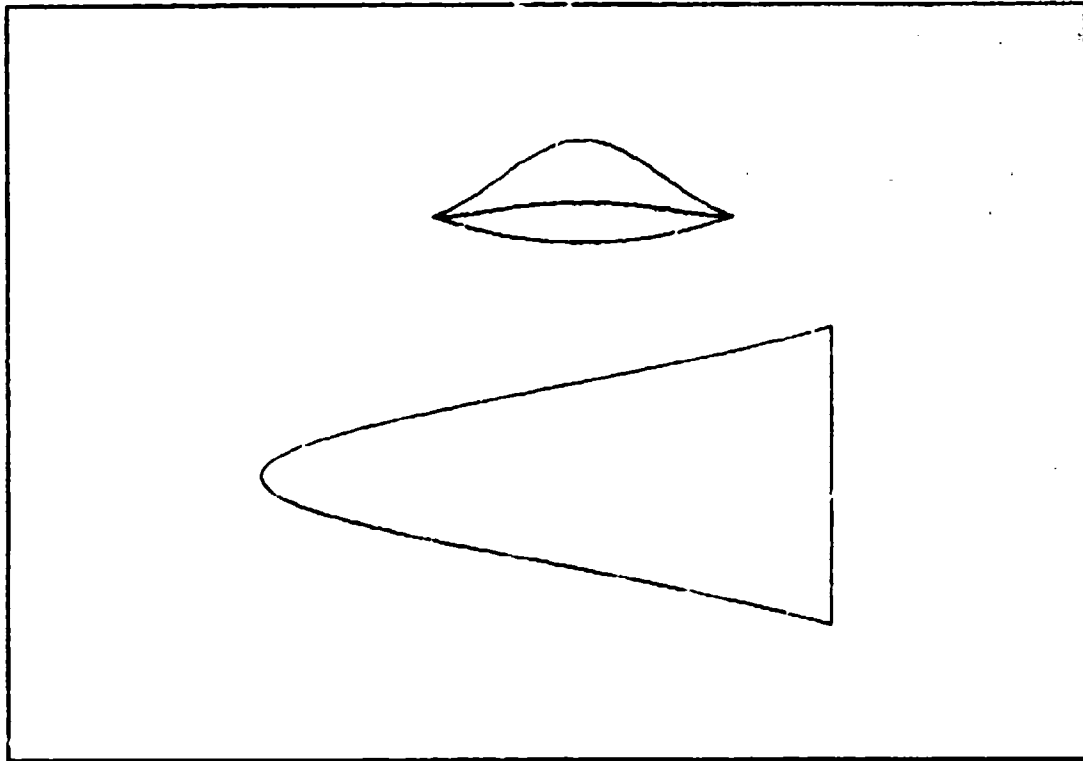


Figure F.3

Table F.3

Phi =20.0	Delta = 8.0	Mach =10.0	Rey = 0.10E+07	Gamma = 1.40
$1 = 1.000 + 2.327 Y^2 + -8.000 Y^4 + 10.530 Y^6$				
Cftar = 0.001488	CL = 0.040459	CD = 0.008350		
Sw/Sp = 2.133018	V*(2/3)/Sp = 0.175985	(L/D)vis = 4.845502		
Ab/Ab1 = 0.288757	V/V1 = 0.0718*0	Sp/ v1 = 0.271188		
b/lw = 0.528095	SSD = 0.118747			

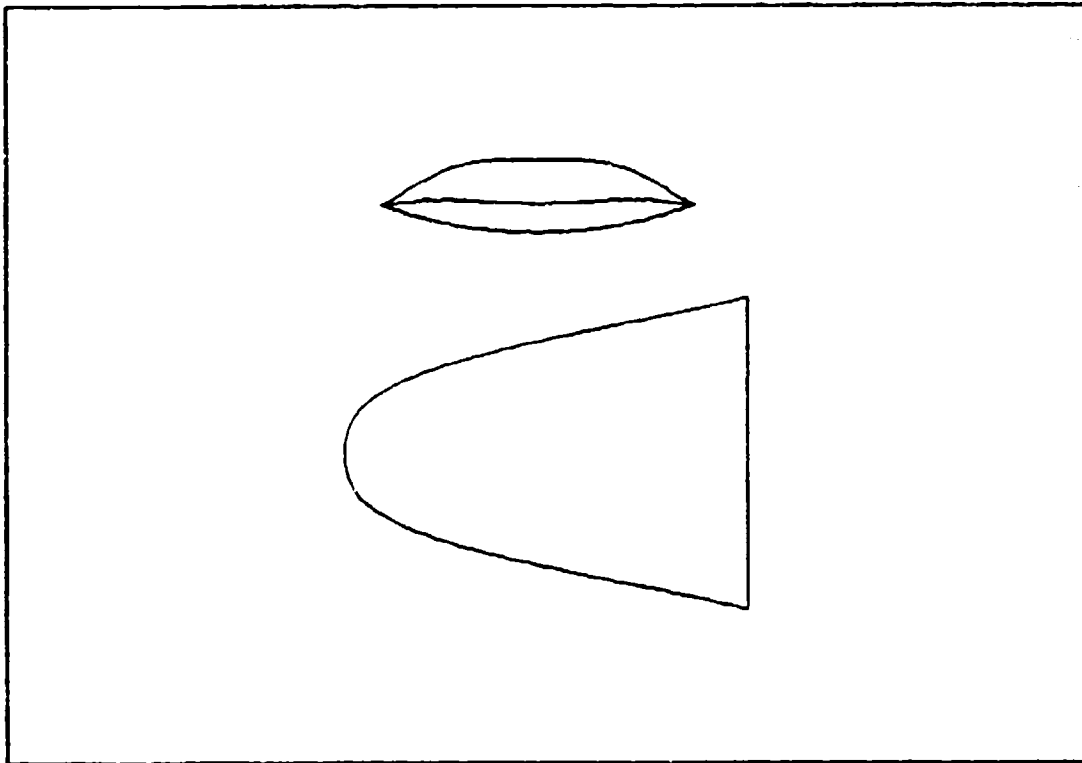


Figure F.4

Table F.4

Phi =20.0	Delta = 8.0	Mach =10.0	Rey = 0.108*07	Gamma = 1.40
X = 1.100 + -0.024 Y^2 + 8.000 Y^4 + -23.180 Y^6				
Cftav = 0.001755	CL = 0.040081	CD = 0.007917		
Sw/Sp = 2.040828	V^(2/3)/Sp = 0.154899	(L/D)vis = 5.082539		
Ab/Ab1 = 0.219841	V/V1 = 0.043740	Sp/Sp1 = 0.221973		
b/lw = 0.781022	SSD = 0.082674			

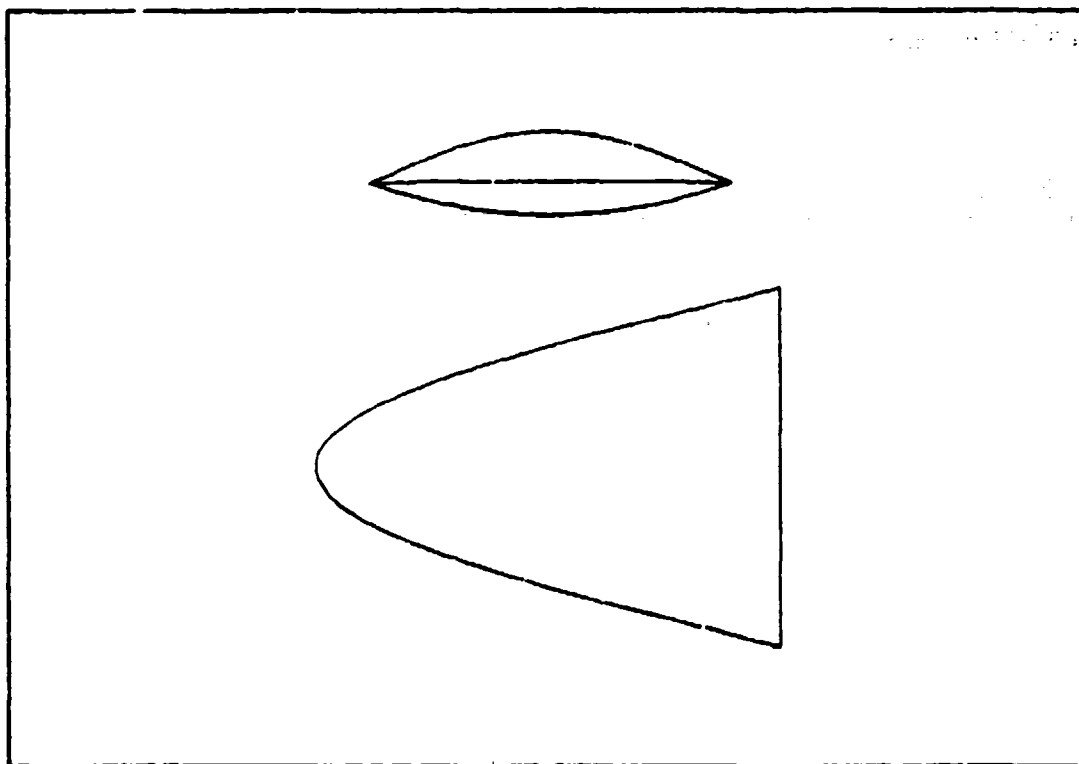


Figure F.5

Table F.5

Phi =20.0	Delta = 8.0	Mach =10.0	Rey = 0.10E+07	Gamma = 1.40
X = 1.100 + 0.777 Y^2 + 0.000 Y^4 + -3.210 Y^6				
Cftav = 0.001816	CL = 0.040021	CD = 0.066021		
Sw/Sp = 2.035581	V*(2/3)/Sp = 0.153377	(L/D)vis = 4.989471		
Ab/Ab1 = 0.201537	V/V1 = 0.037883	Sp/Sp1 = 0.203138		
b/lw = 0.781022	3SD = 0.082574			

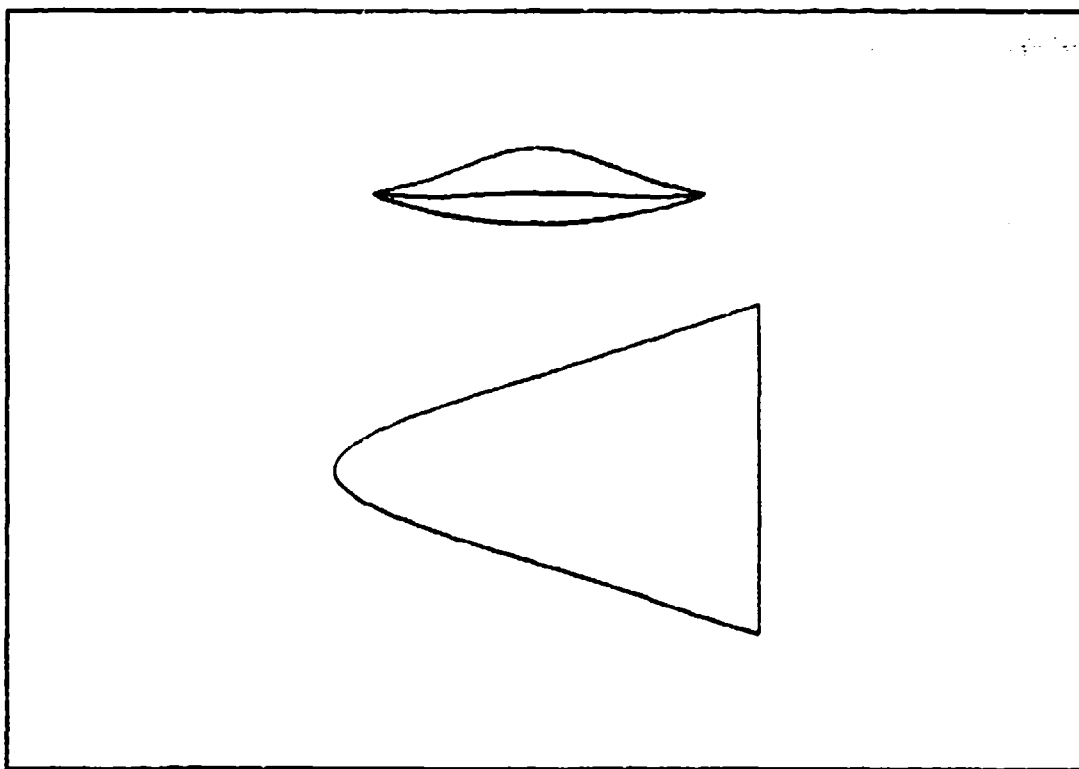


Figure F.6

Table F.6

Phi =20.0	Delta = 8.0	Mach =10.0	Rey = 0.10E+07	Gamma = 1.40
$I = 1.100 + 1.579 Y^2 + -0.000 Y^4 + 16.740 Y^6$				
Cftav = 0.001079	CL = 0.039971	CD = 0.008167		
Sm/Sp = 2.045004	V*(2/3)/Sp = 0.162971	(L/D)vis = 4.900140		
Ab/Abi = 0.103107	V/V1 = 0.032752	Sp/Sp1 = 0.104043		
b/lw = 0.701022	SSD = 0.082574			

APPENDIX G

Presented here are configurations that have the following parameters held fixed:

$$\phi_1 = 10, \quad \delta = 8, \quad M = 10, \quad \text{Rey} = 1 \times 10^6$$

The following parameters are varied:

$$R_0 \text{ from } 1.0 \text{ to } 1.1$$

$$b_4 \text{ from } 120.0 \text{ to } -120.0$$

The values of b_2 and b_6 are such that equation 2-13 and condition (iii) holds.

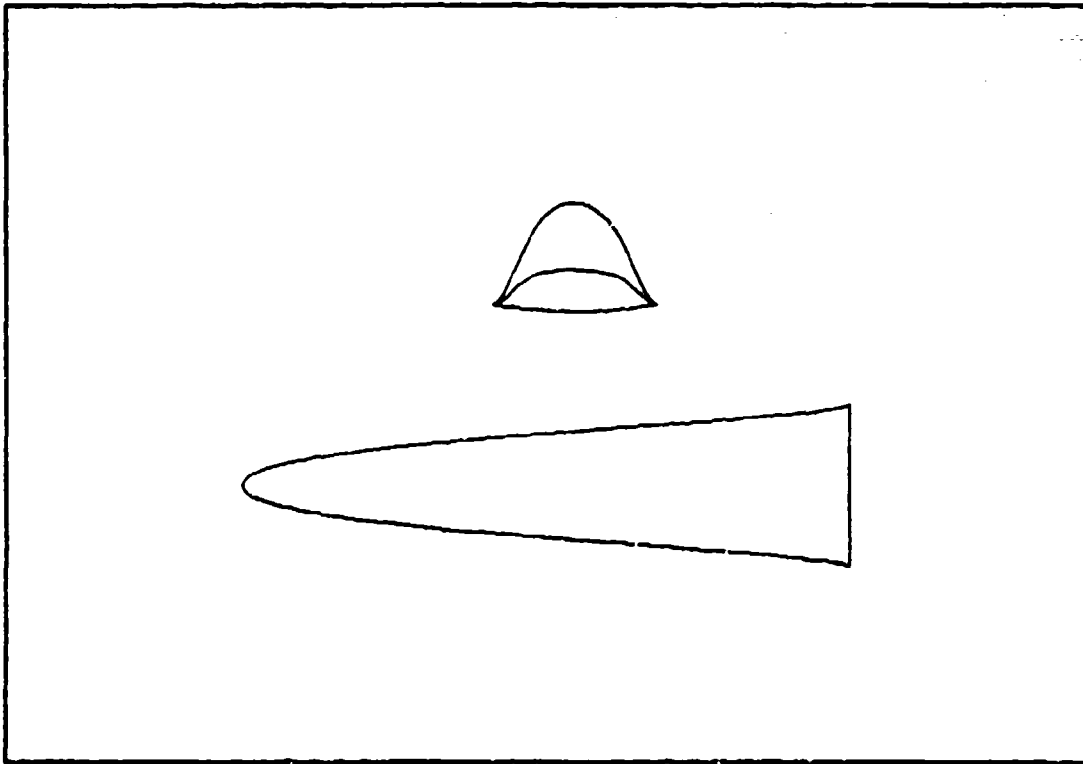


Figure G.1

Table G.1

Phi =10.0	Delta = 8.0	Mach =10.0	Rey = 0.10E+07	Gamma = 1.40
$I = 1.000 + 5.099 Y^2 + 120.000 Y^4 + -2138.0 Y^6$				
Cftav = 0.001814	CL = 0.040548	CD = 0.009108		
Sw/Sp = 2.825714	V^(2/3)/Sp = 0.222710	(L/D)vis = 4.452075		
Ab/Ab1 = 0.292599	V/V1 = 0.083182	Sp/Sp1 = 0.293198		
b/lw = 0.288121	SSD = 0.118747			

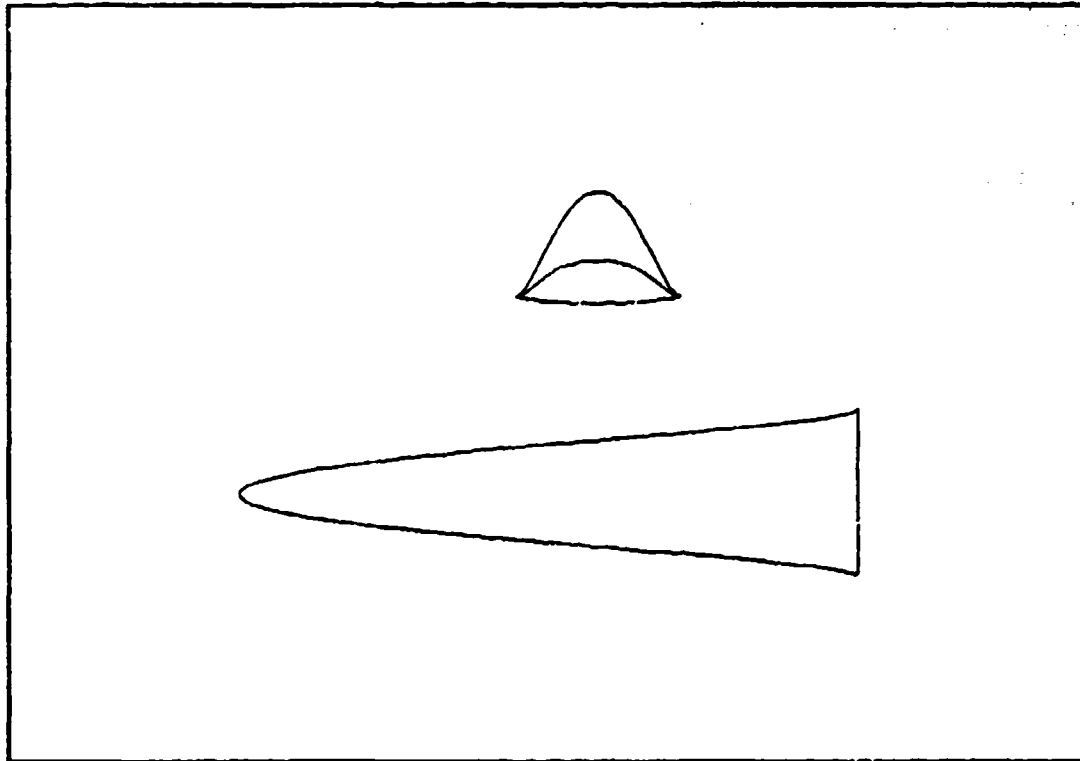


Figure G.2

Table G.2

Phi =10.0	Delta = 8.0	Mach =10.0	Rey = 0.10E+07	Gamma = 1.40
X = 1.000 + 8.200 Y^2 + 0.000 Y^4 + -977.0 Y^6				
Cftar = 0.001331	CL = 0.040500	CD = 0.009214		
Sw/Sp : 2.683484	V^(2/3)/Sp = 0.222903	(L/D)vis = 4.395571		
Ab/Ab1 : 0.274031	V/V1 = 0.075496	Sp/Sp1 = 0.274654		
b/lw = 0.268121	SSD = 0.118747			

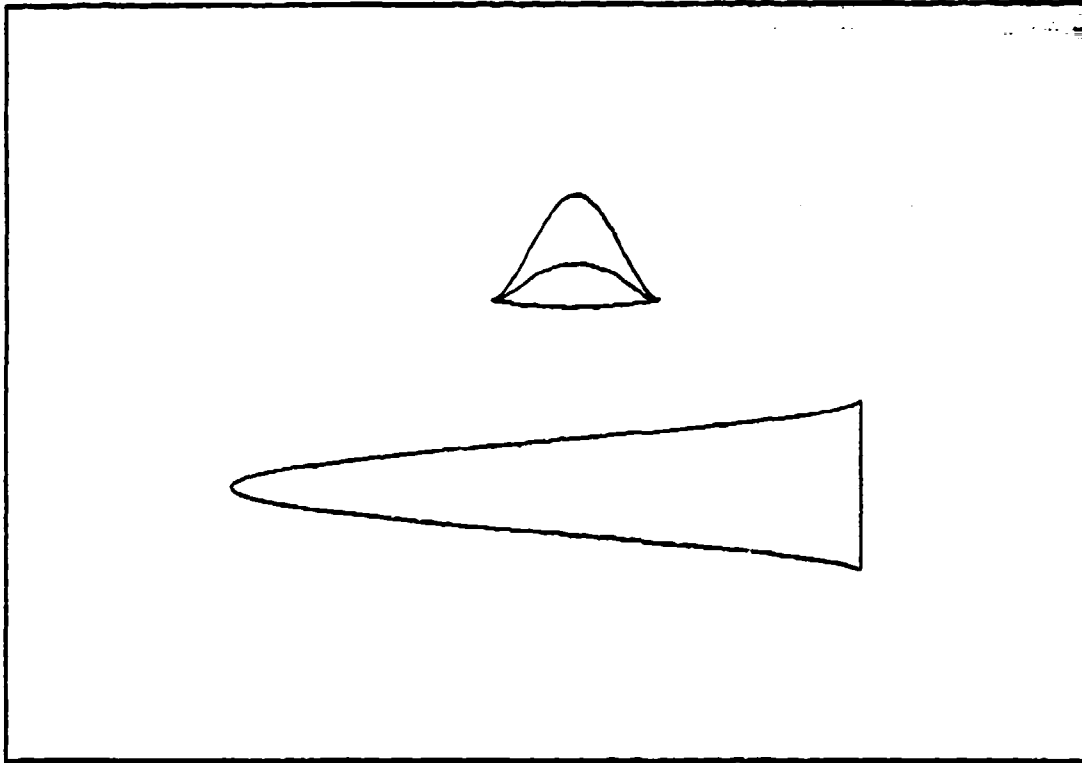


Figure G.3

Table G.3

$\Phi = 10.0$	$\Delta = 8.0$	$Mach = 10.0$	$Re = 0.10E+07$	$\Gamma = 1.40$
$X = 1.000 + 11.309 Y^2 + 120.000 Y^4 + 181.0 Y^6$				
$C_{f_{avg}} = 0.001844$	$CL = 0.040462$	$CD = 0.009387$		
$S_w/S_p = 2.731035$	$V^{(2/3)}/S_p = 0.224272$	$(L/D)_{vis} = 4.319472$		
$\Delta b/\Delta b_1 = 0.255343$	$V/V_1 = 0.088559$	$S_p/S_{p1} = 0.255987$		
$b/l_v = 0.288121$	$SSD = 0.118747$			

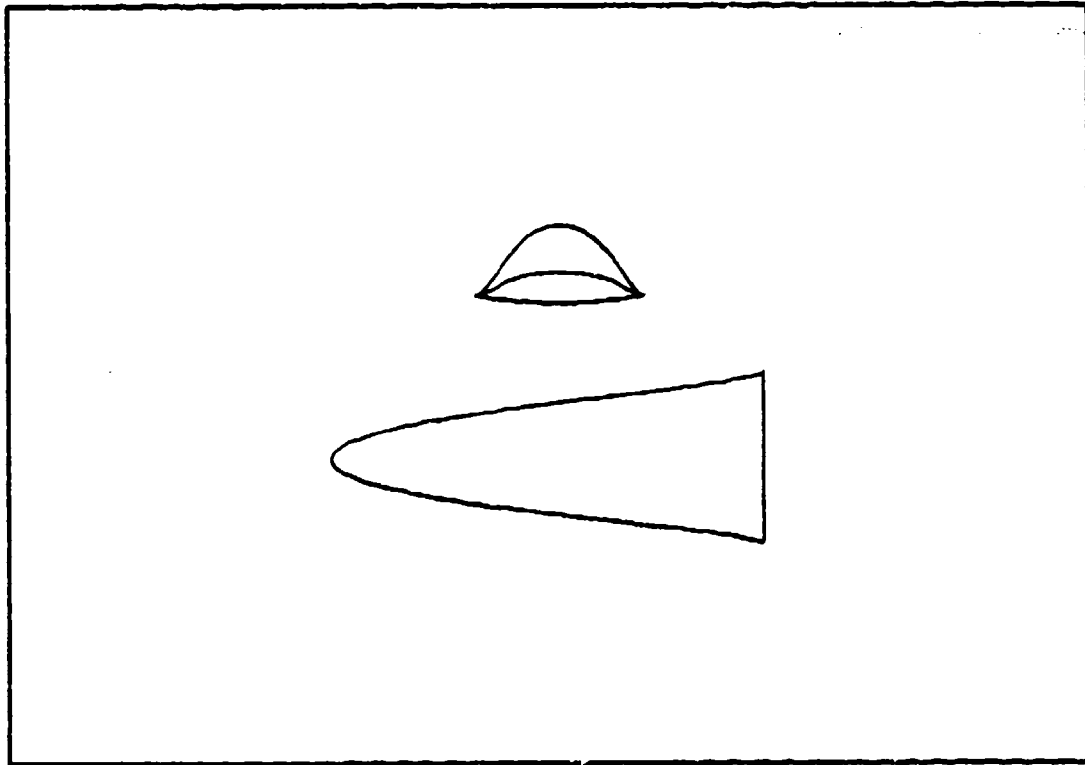


Figure G.4

Table G.4

$Pb1 = 10.0$	$\Delta = 8.0$	$Mach = 10.0$	$Rey = 0.10E+07$	$\Gamma = 1.40$
$X = 1.100 + 3.746 Y^2 + 60.000 Y^4 + -1195.0 Y^6$				
$Cf_{tar} = 0.001821$	$CL = 0.040033$	$CD = 0.008489$		
$Su/S_p = 2.308139$	$V^{(2/3)}/S_p = 0.194968$	$(L/D)_{vis} = 4.715981$		
$\Delta b/\Delta b1 = 0.196422$	$V/V1 = 0.037475$	$S_p/S_{p1} = 0.196855$		
$b/lv = 0.396535$	$S_{SD} = 0.082574$			

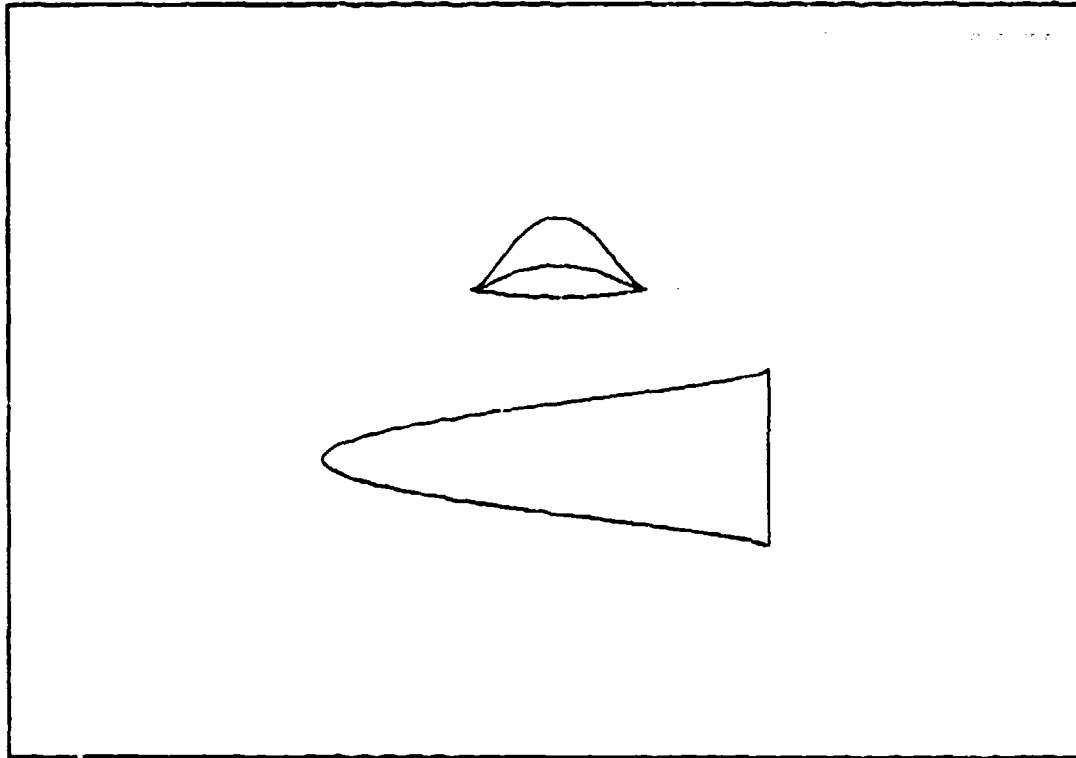


Figure G.5

Table G.5

Phi = 10.0	Delta = 8.0	Mach = 10.0	Re _y = 0.10E+07	Gamma = 1.40
$X = 1.100 + 5.295 Y^2 + 0.000 Y^4 + -614.0 Y^6$				
C _{ftav} = 0.001841	C _L = 0.040009	C _D = 0.008556		
S _w /S _p = 2.321589	V ^{*(2/3)} /S _p = 0.195055	(L/D) _{vls} = 4.676066		
A _b /A _{b1} = 0.187158	V/V ₁ = 0.034888	S _p /S _{p1} = 0.187598		
b/lw = 0.396535	S _{SD} = 0.002574			

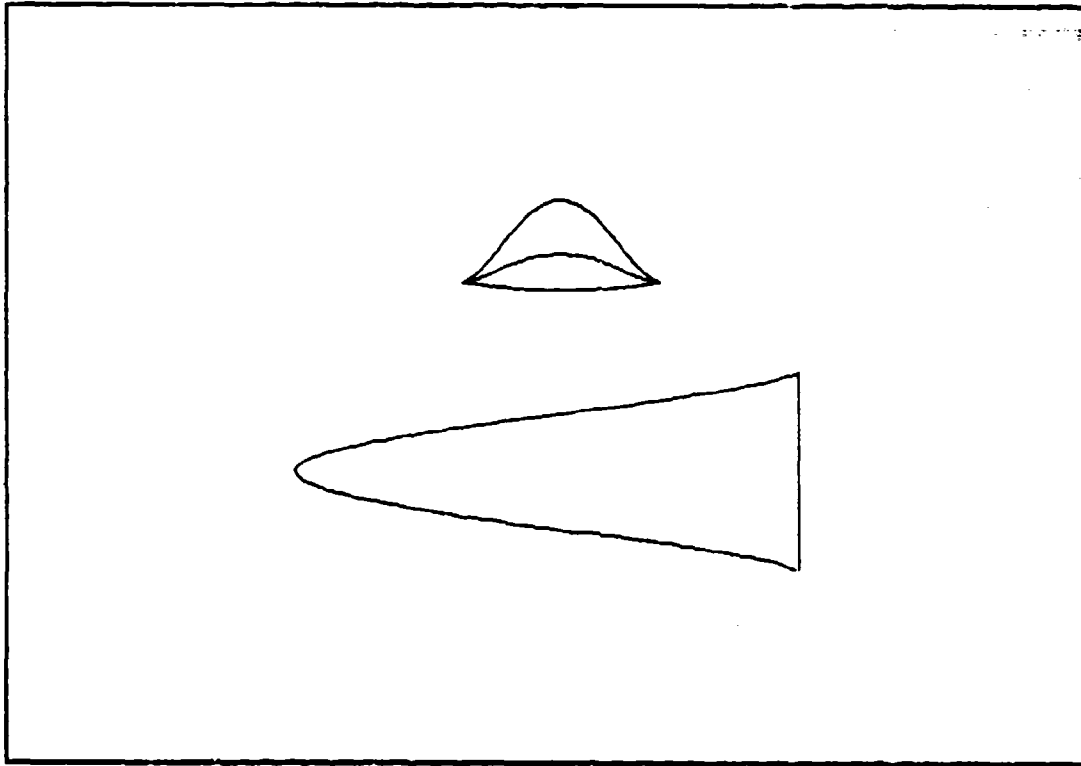


Figure G.6

Table G.6

Phi =10.0	Delta = 8.0	Hach =10.0	Rey = 0.10E+07	Gamma = 1.40
$X = 1.100 + 6.845 Y^2 + -60.000 Y^4 + -33.0 Y^6$				
Cftav = 0.001859	CL = 0.039989	CD = 0.008639		
Sw/Sp = 2.344983	V^(2/3)/Sp = 0.195659	(L/D)vis = 4.828691		
Ab/Ab1 = 0.177894	V/V1 = 0.032486	Sp/Sp1 = 0.178241		
b/lw = 0.398535	SSD = 0.002574			

APPENDIX H

Here in appendix H we show several different configurations in a three-dimensional setting. The configurations shown are repeats of earlier configurations in the above appendices.

These 3-D views are presented so that the reader gets a better perception of the configurations shown and even ones that are shown only in the 2-D views of earlier appendices.

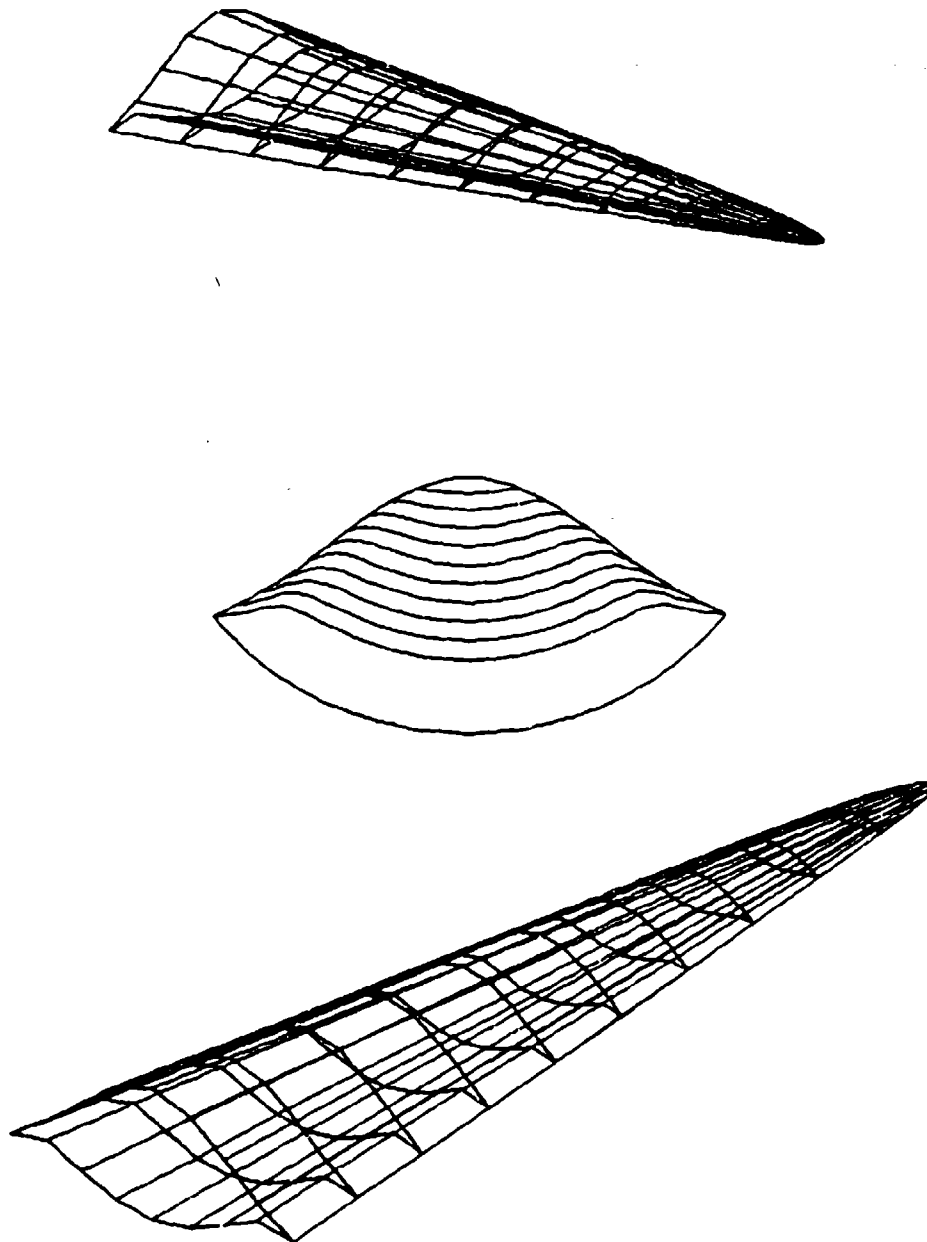


Figure H.1 (C.3)

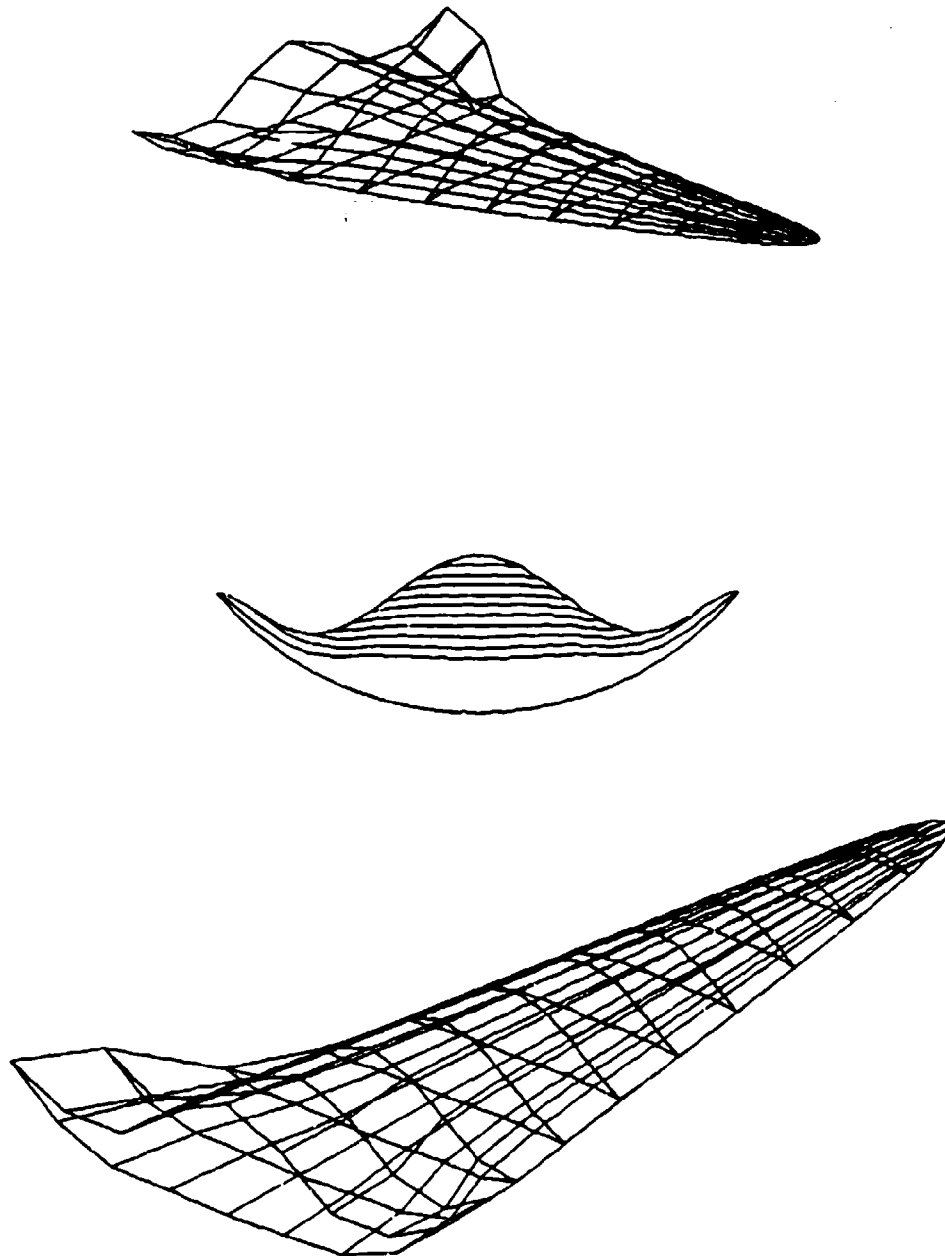


Figure H.2 (C.45)

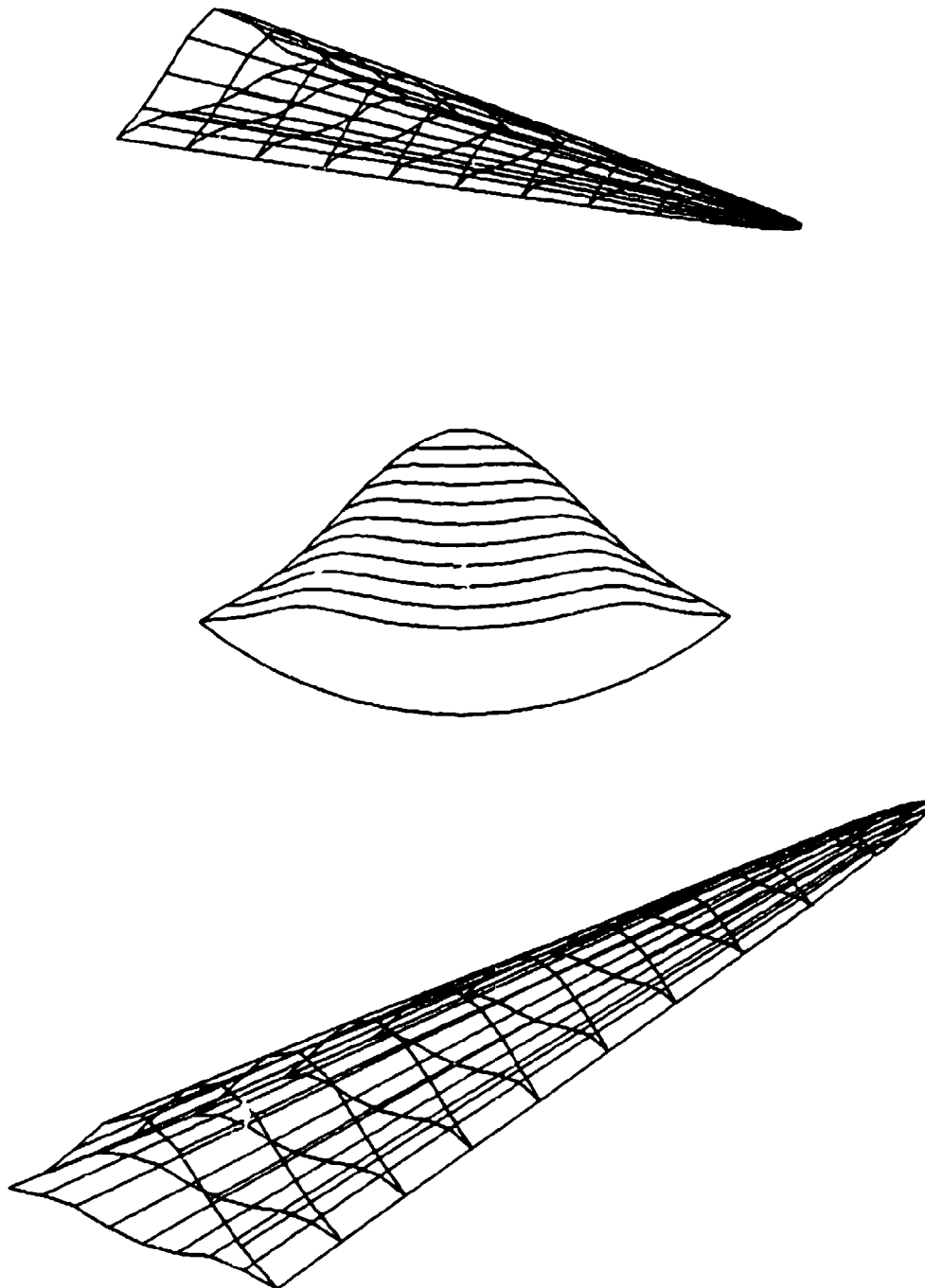


Figure H.3 (D.4)

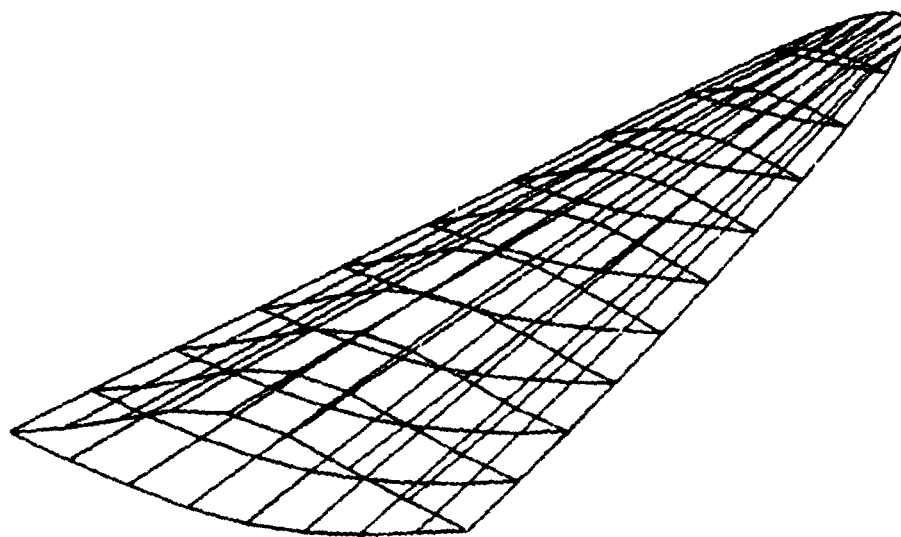
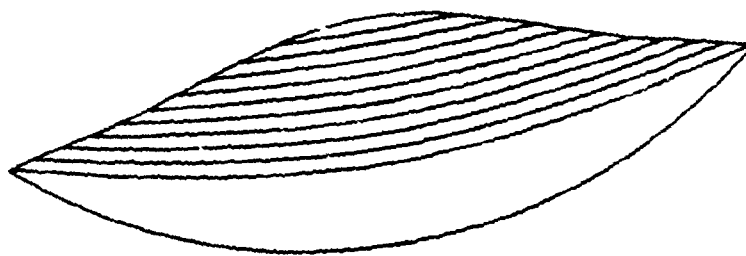
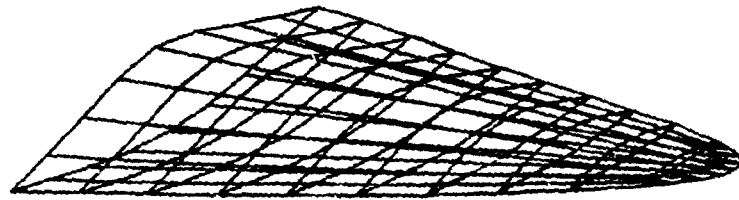


Figure H.4 (D.16)

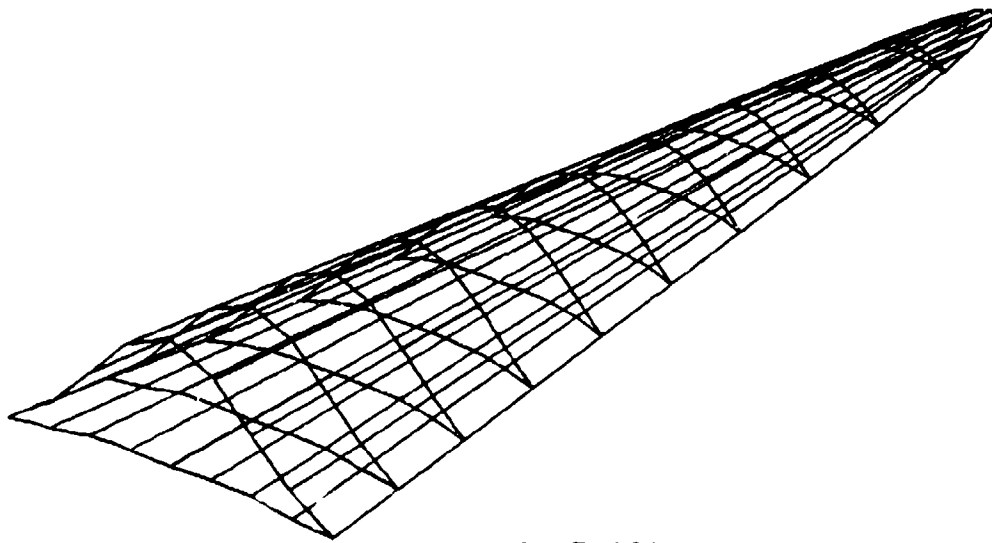
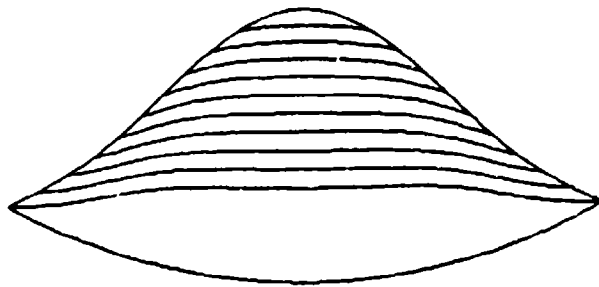
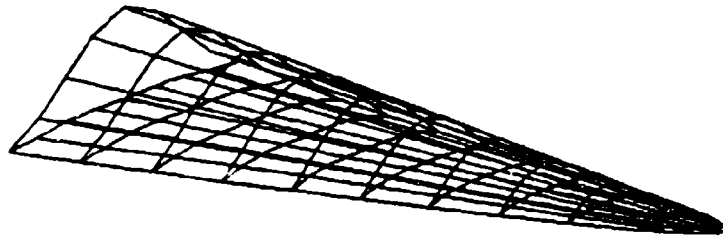


Figure H.5 (E.10)

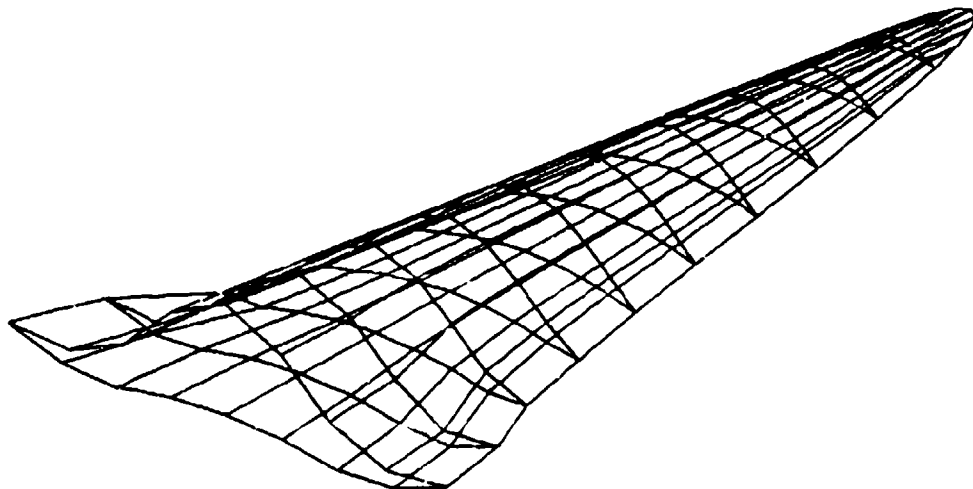
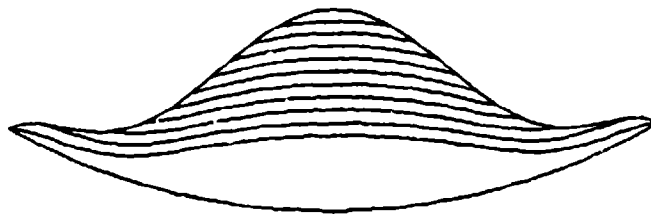
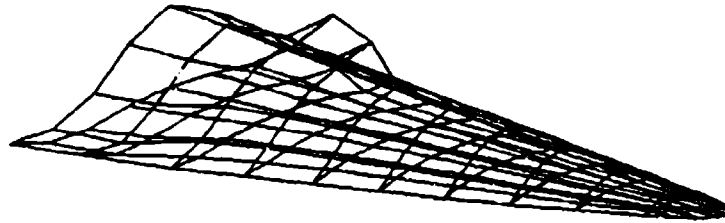


Figure H.6 (E.19)

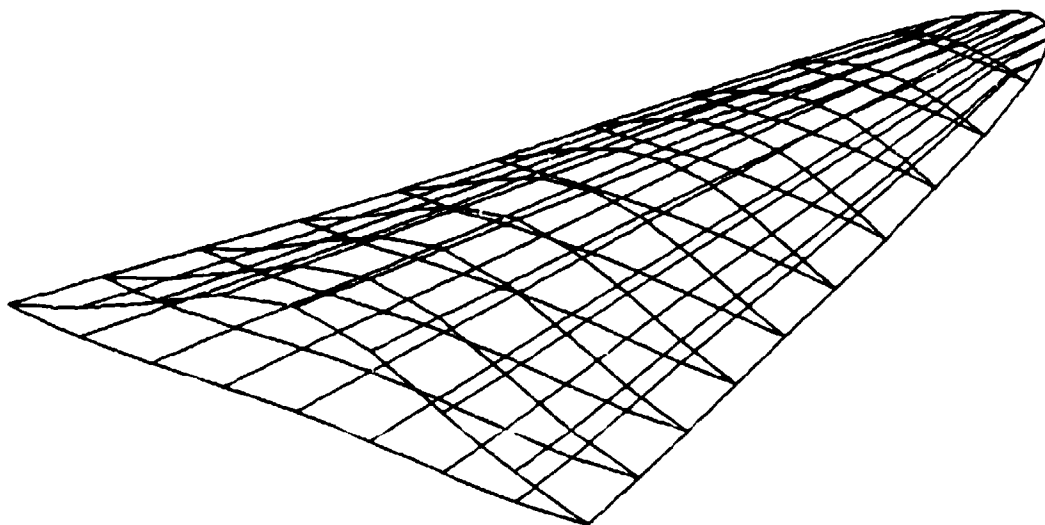
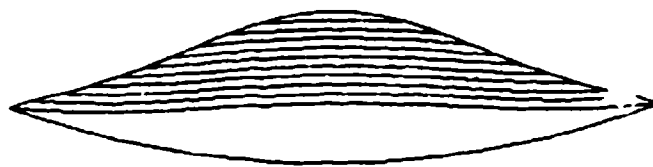
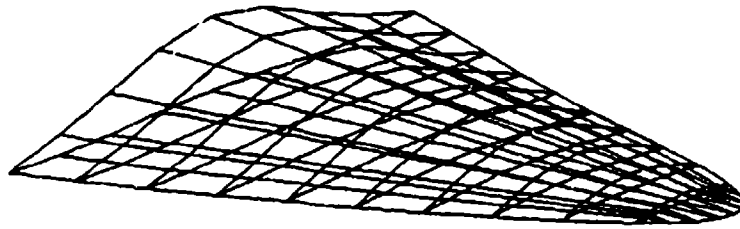


Figure H.7 (F.6)

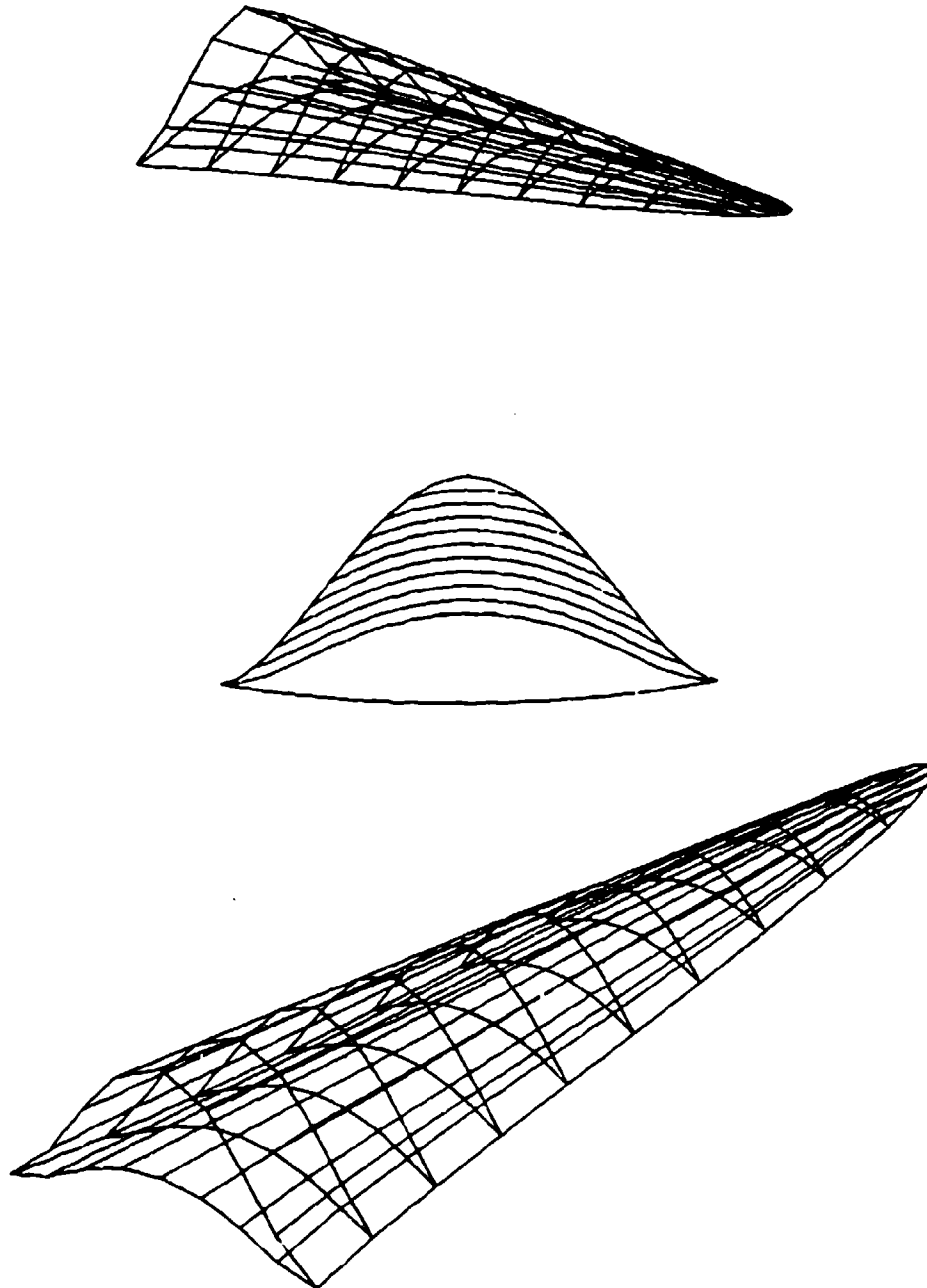


Figure H.8 (G.6)