

AD-A211 936

NSWC TR 88-146

GRAPHITE HEATING ELEMENT THERMAL AND STRUCTURAL PERFORMANCE IN THE NSWC HYPERVELOCITY WIND TUNNEL 9 - A FINITE ELEMENT ANALYSIS

BY MICHAEL A. METZGER

STRATEGIC SYSTEMS DEPARTMENT

JUNE 1988

DTIC
ELECTE
SEP 05 1989
S D CG D

Approved for public release; distribution is unlimited.

*Original contains color
plates: All DTIC reproductions
will be in black and
white.



NAVAL SURFACE WARFARE CENTER

Dahlgren, Virginia 22448-5000 • Silver Spring, Maryland 20903-5000

89 9 01139

UNCLASSIFIED

SECURITY CLASSIFICATION OF THIS PAGE

REPORT DOCUMENTATION PAGE

1a. REPORT SECURITY CLASSIFICATION UNCLASSIFIED			1b. RESTRICTIVE MARKINGS		
2a. SECURITY CLASSIFICATION AUTHORITY			3. DISTRIBUTION / AVAILABILITY OF REPORT Approved for public release; distribution is unlimited.		
2b. DECLASSIFICATION / DOWNGRADING SCHEDULE					
4. PERFORMING ORGANIZATION REPORT NUMBER(S) NSWC TR 88-146			5. MONITORING ORGANIZATION REPORT NUMBER(S)		
6a. NAME OF PERFORMING ORGANIZATION Naval Surface Warfare Center		6b. OFFICE SYMBOL (If applicable) K23		7a. NAME OF MONITORING ORGANIZATION	
6c. ADDRESS (City, State, and ZIP Code) 10901 New Hampshire Avenue Silver Spring, MD 20903-5000			7b. ADDRESS (City, State, and ZIP Code)		
8a. NAME OF FUNDING / SPONSORING ORGANIZATION		8b. OFFICE SYMBOL (If applicable)		9. PROCUREMENT INSTRUMENT IDENTIFICATION NUMBER	
8c. ADDRESS (City, State, and ZIP Code)			10. SOURCE OF FUNDING NUMBERS		
			PROGRAM ELEMENT NO.	PROJECT NO.	TASK NO.
11. TITLE (Include Security Classification) Graphite Heating Element Thermal and Structural Performance in the NSWC Hypervelocity Wind Tunnel 9--A Finite Element Analysis					
12. PERSONAL AUTHOR(S) Metzger, Michael A.					
13a. TYPE OF REPORT Final		13b. TIME COVERED FROM TO		14. DATE OF REPORT (Year, Month, Day) 1988 June	
15. PAGE COUNT 78					
16. SUPPLEMENTARY NOTATION					
17. COSATI CODES			18. SUBJECT TERMS (Continue on reverse if necessary and identify by block number)		
FIELD	GROUP	SUB-GROUP	SEE REVERSE		
13	01				
20	11				
19. ABSTRACT (Continue on reverse if necessary and identify by block number) A general finite element based method for investigating the electrical, thermal, and thermostructural performance of electrically powered heating devices is presented. The method is used to investigate the performance of a graphite heater configuration utilized in the NSWC Hypervelocity Wind Tunnel Facility (No. 9) for heating nitrogen gas to temperatures up to 3100°F prior to a tunnel run to prevent condensation of the gas during tunnel operation. The graphite heaters presently have a limited and erratic service life--a newly installed heater may fail after only 1 or as many as 100 or more tunnel run cycles. Electrical, thermal, and thermostructural performance data are presented for two graphite heater configurations. The thermostructural model is shown to correctly predict brittle fracture at fillet locations in the heater body where, in fact, most fractures are known to occur. Two methods for reducing fillet stresses are proposed which, if implemented, could substantially increase the useful service life of the graphite heaters.					
20. DISTRIBUTION / AVAILABILITY OF ABSTRACT ☐ UNCLASSIFIED/UNLIMITED ☒ SAME AS RPT ☐ DTIC USERS			21. ABSTRACT SECURITY CLASSIFICATION UNCLASSIFIED		
22a. NAME OF RESPONSIBLE INDIVIDUAL Michael A. Metzger			22b. TELEPHONE (Include Area Code) 202/394-2063		22c. OFFICE SYMBOL K23

DD FORM 1473, 84 MAR

83 APR edition may be used until exhausted
All other editions are obsolete

SECURITY CLASSIFICATION OF THIS PAGE

★ U.S. Government Printing Office: 1986-607-044

UNCLASSIFIED

18. Cont.

Graphite
Brittle Failure
Maximum Normal Stress
Thermal-electric analogy
Hypervelocity
Refractory
Fatigue
Strain
Thermal Stress/strain
Joule Heating
PATRAN
Current Density
Resistivity
Thermal Expansion
Strain-to-failure

Heating elements
Failure Theory
Hypersonic
Electrical
Crack
Probability
Heat transfer
Voltage
Heat flux
Convection
Principal stress
Radiation
Free Convection
Service life

Brittle fracture
Fracture
Wind Tunnel
Finite element
Nitrogen
Thermostructural
Stress
Temperature
Resistance Heating
ABAQUS
Current
Conductivity
Tensile strength

FOREWORD

This report documents an investigation of the electrical, thermal, and thermostructural performance of graphite heating elements used in the Naval Surface Warfare Center (NSWC) Hypervelocity Wind Tunnel No. 9. This study is part of a larger and ongoing effort by the Aerodynamic Facilities Branch (Code K23) to reduce or eliminate the problem of frequent and costly failures of the graphite heaters. The analysis herein focuses on the nitrogen preheating period of the tunnel run cycle during which most heater failures are known to occur.

A general finite element-based method for investigating the performance of electrically powered heating elements is presented. The technique is applied to the Tunnel No. 9 graphite heater, and it is shown to correctly predict brittle fracture at fillet locations in the heater body where, in fact, most heater fractures occur. Two methods for reducing fillet stresses are proposed which, if implemented, could substantially increase the useful service life of the graphite heaters.

The author wishes to thank Dr. Robert Edwards and the K22 Structural Mechanics Group members for their guidance concerning this study. Also, thanks are extended to Margie Fung, Aero-Thermodynamics Group (Code K22), for providing the procedure for calculating free-convection film coefficients, to Mr. Ray Trohanowsky for developing the POWER Fortran subroutine. And, finally, thanks to the author's branch head Dr. J. Michael Etheridge for the many useful suggestions for improving this technical report.

Accession For	
NTIS CRA&I	☒
DTIC TAB	☐
Unannounced	☐
Justification	
By	
Distribution /	
Availability Codes	
Dist	Avail and/or Special
A-1	

Approved by:

R. L. Schmidt
R. L. SCHMIDT, Head
Strategic Systems Department

iii/iv



CONTENTS

<u>Chapter</u>		<u>Page</u>
1	INTRODUCTION	1
	BACKGROUND	1
	TUNNEL-9 OPERATION	1
	HEATER ELEMENT BREAKAGE PROBLEM.	2
2	GENERAL HEATER ELEMENT PERFORMANCE ANALYSIS	
	PROCEDURE	5
	ANALYSIS PROCEDURE	5
	ELECTRIC RESISTANCE HEATING--STEP 1.	6
	GRAPHITE ELEMENT HEATING--STEP 2	7
	GRAPHITE ELEMENT THERMAL STRESSES--STEP 3.	8
	PRACTICUM.	8
3	PERFORMANCE ANALYSIS RESULTS FOR TUNNEL-9	
	GRAPHITE HEATING ELEMENTS	11
	ANALYSIS RESULTS	11
	ELECTRICAL ANALYSIS RESULTS--STEP 1.	11
	THERMAL ANALYSIS RESULTS--STEP 2	12
	THERMOSTRUCTURAL ANALYSIS RESULTS--STEP 3.	12
	GRAPHITE HEATER ELEMENT FILLET STRESSES	15
	FILLET STRESS BREAKDOWN.	15
	STRESS REDUCTION METHODS	16
	ASSUMPTIONS	17
4	CONCLUSIONS	18
	REFERENCES	63
	DISTRIBUTION	(1)

<u>Appendix</u>		<u>Page</u>
A	ANALYSIS SUPPORT PROGRAMS.	A-1
B	ABAQUS INPUT FILES	B-1
C	FREE CONVECTION HEAT TRANSFER FILM COEFFICIENT CALCULATION FOR MACH-14 END HEAT CONDITIONS.	C-1
D	TENSILE STRENGTH AND STRAIN-TO-FAILURE EXPERIMENTAL DATA FOR HEATER GRAPHITE.	D-1

ILLUSTRATIONS

<u>Figure</u>		<u>Page</u>
1	SCHEMATIC OF TUNNEL NO. 9 FACILITY.	19
2	VERTICAL HEATER AND DIAPHRAGM SECTION	19
3	HEATER GAS CONDITIONS FOR A TYPICAL MACH-14 WIND TUNNEL RUN	20
4	COMPLETELY FAILED HEATER--TOP FILLET LOCATION	21
5	COMPLETELY FAILED HEATER--BOTTOM FILLET LOCATION.	21
6	TOP AND BOTTOM FILLET CRACK LOCATIONS IN THE GRAPHITE HEATER	22
7	PARTIAL TOP FILLET CRACK.	23
8	PARTIAL BOTTOM FILLET CRACKS.	23
9	HEATER GRAPHITE ELECTRICAL RESISTIVITY VERSUS TEMPERATURE	24
10	J HEATER DRAWING.	25
11	K HEATER DRAWING.	26
12	MACH-10 HEATER BASE DRAWING	27
13	J HEATER FINITE ELEMENT MODEL	28
14	K HEATER FINITE ELEMENT MODEL	28
15	FINITE ELEMENT MODEL USES HEATER SYMMETRY TO REDUCE MODEL SIZE	29
16	MACH-10 HEATER BASE FINITE ELEMENT MODEL.	29
17	VOLTAGE POTENTIALS IN THE J HEATER.	30
18	CURRENT DENSITY CONTOURS IN THE J HEATER.	31
19	START HEAT TEMPERATURES IN J HEATER	33
20	END HEAT TEMPERATURES IN THE J HEATER	33
21	END HEAT TEMPERATURES IN THE J HEATER	35
22	START HEAT TEMPERATURES IN THE K HEATER	35
23	START HEAT TEMPERATURES IN THE MACH-10 BASE	37
24	AXIAL STRESS IN MACH-10 BASE.	37
25	HEATER ELEMENT/BASE CLAMPING ARRANGEMENT.	39
26	DEFORMED SHAPE PLOTS--FLOATING BASE	40
27	DEFORMED SHAPE PLOTS--CLAMPED BASE.	41
28	AXIAL STRESS IN J HEATER.	43
29	AXIAL STRESS IN K HEATER.	43
30	MAXIMUM PRINCIPAL STRESS--J HEATER, START HEAT.	45
31	MAXIMUM PRINCIPAL STRESS--J HEATER, END HEAT.	45
32	MAXIMUM PRINCIPAL STRESS--J HEATER, FREE BASE	47
33	MAXIMUM PRINCIPAL STRESS--K HEATER, START HEAT.	47
34	MAXIMUM PRINCIPAL STRESS--MACH 10 BASE.	49
35	TEMPERATURES IN SQUARE AND ROUNDED CORNER HEATER LEG.	49

ILLUSTRATIONS (Cont.)

<u>Figure</u>		<u>Page</u>
36	TOTAL PRINCIPAL STRESS AND TEMPERATURE PROFILES EXTRAPOLATED TO HEATER SURFACE. TOP FILLET LOCATION	51
37	TOTAL PRINCIPAL STRESS AND TEMPERATURE PROFILES EXTRAPOLATED TO HEATER SURFACE. BOTTOM FILLET LOCATION	52
38	TOTAL PRINCIPAL ELASTIC STRAIN PROFILE EXTRAPOLATED TO HEATER SURFACE. TOP FILLET LOCATION	53
39	TOTAL PRINCIPAL ELASTIC STRAIN PROFILE EXTRAPOLATED TO HEATER SURFACE. BOTTOM FILLET LOCATION	53
40	GRAPHITE HEATER SERVICE LIFE IN TUNNEL RUNS VS. CUMULATIVE FREQUENCY.	54
41	BREAKDOWN OF THERMAL STRESS AT BOTTOM FILLET.	55
42	FINITE ELEMENT MODEL WITH SLOT EDGES ROUNDED TO REDUCE FILLET STRESSES.	56
43	COOLING SLOTS FORMED IN HEATER LEGS BY SECTIONING AT AA AND SEPARATING HALVES	56
44	CONCEPT FOR HEATER ELEMENT WITH COOLING SLOTS	57

TABLES

<u>Table</u>		<u>Page</u>
1	HEATER ELEMENT SERVICE LIFE HISTORY FOR 1985 AND 1986.	58
2	SUMMARY OF HEATER ANALYSIS STEPS.	59
3	HEAT TRANSFER INPUT DATA.	60
4	PEAK THERMAL STRESS-STRAIN STATES IN GRAPHITE HEATER.	61
5	PROBABILITY OF FAILURE FOR GRAPHITE HEATERS	61

CHAPTER 1

INTRODUCTION

The Naval Surface Warfare Center (NSWC) Hypervelocity Wind Tunnel No. 9 uses an electrically powered graphite heating element to preheat nitrogen working gas to temperatures up to 3100°F. This prevents condensation of the gas which cools as it expands through a nozzle to hypersonic speeds of Mach 10 or Mach 14. The graphite heater elements have a limited and erratic service life--a newly installed heater element may fail after only 1 or as many as 100 or more tunnel run cycles. Element replacement is costly (approximately \$10,000 including installation), and a half day or more may be required to replace a broken heater element which adversely impacts the tunnel test schedule. This report documents a general method for investigating the electrical, thermal, and thermostructural performance of electrically powered heating elements. It also presents the results of an investigation of the heating characteristics of the Tunnel-9 graphite heater elements. This study was initiated to determine if thermal stresses induced in the heater elements during the nitrogen preheating period could be the cause of the heater element failures.

BACKGROUND

Tunnel-9 Operation

The NSWC Tunnel-9 wind tunnel is a "blow-down" type tunnel which runs at Mach 10 or 14. High pressure vertical heater and driver vessels (shown in Figure 1) are precharged with nitrogen gas prior to a wind tunnel run while a vacuum sphere downstream of the test section is evacuated. The fixed volume of gas in the heater vessel is preheated to the extreme temperature required. A tunnel run is initiated by bursting a set of metal diaphragms located just upstream of a 40-foot long nozzle which allows the high-pressure, high-temperature nitrogen (typically 20,000 psi at 3100°F for Mach 14) to accelerate through the nozzle section and reach speeds of Mach 10 or 14 in the 5-foot diameter test section. Relatively cool driver vessel gas pushes the hot gas out of the heater vessel under constant pressure to maintain constant flow conditions in the test section during the tunnel run. The tunnel run continues until all of the hot gas has been expended, a typical run lasting approximately from .25 second to as long 10 seconds.

The heater vessel (shown in Figure 2) is lined with a refractory insulation liner which safely contains the nitrogen gas during the preheating process. The liner encloses the graphite heater element which heats the nitrogen precharge to the specified final temperature of 1500°F (for Mach 10) or 3100°F (for Mach 14). This heating process is depicted in Figure 3. During the heating period, which lasts about 15 minutes, a 60 Hz, single phase ac current of 5500-6500 rms amps is passed through the hairpin-shaped graphite heater element which reaches a temperature of 4000-5000°F as a result of resistance heating. The nitrogen gas, which is essentially transparent to radiation, is heated primarily by convection and conduction off the hot graphite element and hot liner walls. Since the volume of nitrogen in the heater vessel is fixed, both its temperature and pressure rise during the constant volume heating process until the final desired pressure and temperature are reached. At this point the tunnel flow is started by rupturing the metal sealing diaphragms.

Heater Element Breakage Problem

Service life histories for heater elements used during FY 1985 and 1986 are shown in Table 1. A heater element is typically operated until it fails "catastrophically," usually by fracturing completely through one of the heating legs as shown in Figures 4 and 5. The timing and mode of failure are fairly consistent. The element usually fails completely at some point during the nitrogen heating period. The fracture is always a brittle-type fracture typically located at either a top fillet or bottom fillet (as shown in Figure 6) with the crack surfaces oriented approximately perpendicular to the longitudinal axis of the heater element.

Interestingly, it is now fairly well documented that a heater may develop partial cracks at the top or bottom fillets (as shown in Figures 7 and 8) which, at least for a time, will not adversely affect the heater operation. However, eventually the element fails completely and must be replaced. Although complete element failure occurs during the heating period, it is not clear if a partial crack is initiated at this or some other time.

Other work has been done to try to improve heater element life. Results of an investigation of thermal stresses, induced by quenching of the heater as the cool driver gas fills the heater vessel during a tunnel run, did not correlate well with Tunnel-9 experience. In another study, graphite material samples taken from both long-lived and short-lived failed heater elements were tested in an attempt to correlate service life with certain, easily obtained, non-destructive test measurements which could then be used as a quality control criterion for screening out unacceptable graphite material billets; however, no definite correlations were found.¹

The present study is concerned with determining if thermal stresses induced in the heater elements during the nitrogen preheating period could be the cause of heater element failures.

CHAPTER 2

GENERAL HEATER ELEMENT PERFORMANCE ANALYSIS PROCEDURE

ANALYSIS PROCEDURE

The heater analysis procedure can be broken down into three basic steps:

- Step 1: Solve the Electrical Problem--Get volumetric resistance heating in the graphite heater generated by a (5500 amp) current flow through the heater.
- Step 2: Solve the Thermal Problem--Use internal heating from Step 1 to "heat up" the graphite element and obtain graphite temperatures.
- Step 3: Solve the Structural Problem
 - o Use temperatures from Step 2 to obtain thermal stress and strain in heater due to thermal expansion. Determine maximum principal stress and strain in the heater.
 - o Subtract the hydrostatic stress or strain (generated by the high-pressure nitrogen gas surrounding the heater) from the peak principal stress or strain to obtain the net maximum principal stress or strain.
 - o Compare net maximum principal stress or strain with graphite strength to determine the probability of failure.

The entire three-step procedure above was implemented using the ABAQUS² Finite Element Analysis software (version 4-5) in conjunction with the PATRAN³ pre- and post-processing code. The implementation of each of the three steps is described in more detail below.

Electric Resistance Heating--Step 1

Implementation of Step 1, that is, obtaining the volumetric resistance heating (also known as joule heating) due to the electric current passing through the graphite heater element, required a novel application of the well documented thermal/electric (T/E) analogy principal.⁴ The T/E analogy has been widely used to solve analogous engineering problems in the fields of heat conduction, fluid dynamics, and solid mechanics. Phenomena which are governed by the Laplace equation, such as both electrical and heat conduction, yield mathematically identical solutions; the solution of a particular electrical conduction problem is also applicable to the corresponding or analogous heat conduction problem and vice versa. Analogous mathematical terms for the T/E analogy are given below:

THERMAL	ELECTRICAL
-----	-----
Heat, Q	Charge, Q
Temperature, T	Voltage, V
Heat Flux Vector, q	Current Density Vector, j
Thermal Conductivity, k	Electrical Conductivity, s

The typical approach to applying the T/E analogy has been to obtain a solution to a particular heat conduction problem using an analogous electrical conduction model (e.g., electrolytic tanks or conductive sheet models). In the present analysis, however, the opposite approach has been taken; that is, the electrical conduction in the heater is obtained by solving the analogous heat conduction problem using a geometrically similar finite element heat conduction model.

The ABAQUS thermal conduction capability can be utilized to easily solve for current flow in an arbitrarily shaped conductor subjected to some prescribed voltage. Since ABAQUS does not "know" that it is solving an analogous electrical conduction problem, it will state the results as "temperatures" and "heat-flux," etc. However if consistent analogous electrical terms are input, the "temperature" and "heat-flux" results from ABAQUS will actually be voltage and current-density, respectively. For this analysis, the units used for the input quantities were inches, volts and, for electrical conductivity, 1/ohm-in which produce units of volts and amps/sq in for the voltage and current-density output quantities, respectively. ABAQUS will calculate the components and also the magnitude of the current-density vector, j, at each gauss point in the finite element model. The volumetric resistance heating at each gauss point can then be obtained by Equation (1):

$$q = |j|^2 p \quad (1)$$

where: q = volumetric heat flux (watts/cu in)
 |j| = current density magnitude (amps/sq in)
 p = electrical resistivity (ohm-in)

This last step of calculating the heat flux at each gauss point is done by running a short Fortran program I2RFIL (listed in Appendix A). This program simply reads the current density values from the ABAQUS results (FIL) file and generates a file of volumetric heat flux at each gauss point using Equation (1). This file of heat flux values is then used to heat-up the graphite element (Step 2 in the analysis procedure) to obtain the temperature in the heater.

Limitations of T/E Method. There are two principal limitations in the T/E method described above. First, the electrical conductivity must remain constant with temperature. Although ABAQUS will handle temperature dependent thermal conductivity, this capability cannot presently be utilized for temperature dependent electrical conductivity since the actual temperatures are not known in Step 1. They are computed later on during Step 2 in the analysis procedure. As Figure 9 shows, the electrical resistivity (the resistivity is simply the inverse of conductivity) of the graphite material is strongly temperature dependent up to about 1400°F, then remains fairly constant at temperatures above this. It was found that the heater element legs run at temperatures above this, except for the initial heat-up period, which lasts about a minute, so that for most of the 15-20 minute nitrogen heating period the electrical conductivity can be taken to be uniform and constant.

This method is also in a strict sense limited to dc electrical power. Recall that the Tunnel-9 heater elements are powered by a 60 Hz, ac power source. An ac current produces a so-called "skin effect" which causes a concentration of the current density at the outer surface of a conductor rather than being uniformly distributed through the cross section as in dc current flow. This effect is proportional to the ac frequency and size of the conductor and is inversely proportional to resistivity. It was determined that, in regard to the volumetric heating, this effect would be secondary for the graphite heater elements so that the dc current flow analogy should adequately model the heating characteristics.

Graphite Element Heating--Step 2

Since both Steps 1 and 2 in this analysis procedure use a heat conduction finite element model, the basic model used in Step 1 can be used in Step 2 with changes in the boundary conditions to reflect the new nature of the problem. ABAQUS is capable of solving very general transient and steady-state heat transfer problems involving internal heat generation, radiation, and convection with temperature dependent properties.

Recall from Figure 3 that once power to the heater is turned on at the start of the heating period, the graphite element heats up in about 1 minute. During this time the temperature of the

nitrogen gas in the heater vessel does not increase appreciably. For analysis purposes this initial heating transient must be viewed as a nonsteady-state phenomenon. After about 1 minute, the heater element temperature reaches a nearly steady-state level and, thereafter, both the heater and nitrogen gas temperatures rise slowly for the remaining 15-20 minutes of heating time. For analysis purposes this relatively slow heating process can be treated as a quasi-steady state process so that the heater temperature can be assumed to be a function solely of the surrounding gas/liner-wall temperature. The problem of obtaining the temperature distribution in the heater at any point during the quasi-steady heating reduces to simply fixing the gas/wall temperature and solving for the steady-state heater temperature distribution. Since performing a transient analysis is in general much more costly, it was decided to limit the present study to investigating the heater temperatures and stresses at selected points in time within this quasi-steady heating period. The two points selected for study were at the start and end of the quasi-steady heating period and which are designated as "START HEAT" and "END HEAT" in Figure 3. Additionally, the gas and liner-wall temperatures were assumed to be identical permitting the use of one sink temperature for both radiation and convection boundary conditions.

Obtaining the temperature distribution in the graphite heater at the START or END HEAT is a matter of specifying the proper sink temperature in ABAQUS, as well as specifying radiation and convection heat transfer coefficients, and then allowing ABAQUS to solve for the steady-state temperatures in the heater due to the resistance heating provided by Step 1. Since the resistance heating in the heater is non-uniform, the ABAQUS subroutine option DFLUX is used with the subroutine given in Appendix A to read the heating flux values from the file generated in Step 1. ABAQUS calculates the temperatures in the heater which are then used to evaluate thermal performance of the heater and to obtain thermal stresses in the heater.

Graphite Element Thermal Stresses--Step 3

Once again the same basic finite element model from Steps 1 and 2 can be used in Step 3 if the element type designator is changed to the corresponding solid structural element. ABAQUS will then use the temperatures obtained from Step 2 to compute the thermal stresses and strains in the graphite heater element. A suitable failure criteria can then be applied to the stress or strain results to determine probability of failure or assess margins of safety of the heater design.

PRACTICUM

In practice, implementation of this three-step analysis procedure involves additional work, primarily in Step 1, to

ensure that correct results are obtained. Table 2 summarizes the semi-automated steps for the entire procedure as implemented on a VAX computer system. In Step 1 the user specifies a heater voltage and ABAQUS solves for current flow. The current checking program CURRENT (Appendix A) will verify that the net current flow through the heater is correct. If it is not, then the applied voltage may be adjusted. Once the correct net current is obtained, the program I2RFIL (Appendix A) is run which creates the resistance heating file (FOR032.DAT file) from the ABAQUS results file. Once the heating file is generated, it should be checked by running the POWER program (Appendix A) which calculates the total heater power that will be generated by the heating file. The total power calculated by POWER should be within a few percent of the specified heater voltage multiplied by the total heater current computed by CURRENT (i.e., the total resistance-heating power should equal applied heater volts times total amps). Some discrepancy can be expected since the algorithm used in POWER to compute finite element volumes is not exact for quadratic elements with curved edges.

CHAPTER 3

PERFORMANCE ANALYSIS RESULTS FOR TUNNEL-9 GRAPHITE
HEATING ELEMENTS

ANALYSIS RESULTS

The two most current graphite heater element configurations, hereafter referred to as the J-type and K-type heaters, are shown in Figure 10 and 11. The drawing for the Mach 10 heater base is shown in Figure 12. The K heater has superceded the J heater, the differences being in the flared top and the side slots. In the K design, the slight flare-out of the outer diameter at the top end was lengthened, and the slot was also lengthened in order to "beef-up" the top fillet region where the earlier J-type heaters tended to break. This change appears to have reduced top fillet breaks but, unfortunately, the K heaters continued to fracture at the bottom fillet. Both the J and K heaters were analyzed with the basic finite element models shown in Figure 13 and 14. Both are 1/4-symmetry models utilizing the two planes of symmetry in the heater to reduce model size as shown in Figure 15. The J model is a full-length model, whereas only the top portion of the K design was analyzed. Extensive studies showed that such top models would give the same stress results as the full model when out-of-plane motion of the cross section at the cutoff is prevented. Quadratic finite elements were used in both the thermal models and the stress models (20-node hexes and 15-node wedges, ABAQUS DC3D20- and C3D20-type elements, respectively). The Mach 10 graphite heater base, which holds the heater element, was also analyzed separately using the 1/4-symmetry model shown in Figure 16. Only the bottom portion of the heater element, up to the bottom fillet region, is included in the base model. The results of the base analysis will not be discussed extensively in this report--these results are presented for reference.

Electrical Analysis Results--Step 1

Results for voltage and current density distributions in the J-type heater are shown in Figure 17 and 18, respectively. The current density plot can be viewed as a topographical map with peaks showing regions of high current densities, such as at both the top and bottom fillets, and valleys indicating areas of relatively low current densities. The ABAQUS material and boundary conditions are given in Appendix B for the J heater electrical model.

Thermal Analysis Results--Step 2

Thermal Model Setup. In all cases convection heat transfer was allowed on the inner diameter (I.D.) and outer diameter (O.D.) "wetted" surfaces of the heater element as well as on the rounded end of the crown and edges of the side slots. The O.D. and I.D. of the threaded-base portion of the J heater was fixed at 300°F. Radiation heat transfer was allowed on the wetted O.D., slot edges, and the rounded end of the crown. No radiation was allowed on the wetted I.D. since the inside surfaces of the heater element legs face each other so that the net radiation to each surface is taken to be zero as a first approximation. Table 3 lists the film coefficients and radiation boundary conditions used. ABAQUS input data for the J thermal model are given in Appendix B, and Appendix C shows the method used to compute the free convection film coefficient.

Thermal Results. Figures 19-23 show temperature results for the three models analyzed. Figures 19 and 20 show temperatures in the J heater for a standard 613 kW power case (5481.8 A @ 112 V) for both START HEAT and END HEAT periods. The peak temperatures in the graphite are 3620°F at START HEAT and 4858°F at END HEAT, and they occur at the "hotspot" apparent on the I.D. surface near the top fillet. Cross-sectional temperature profiles at the top and bottom fillets for the END HEAT case (Figure 21) reveal internal hotspots at both fillet locations corresponding approximately to the locations where the high current densities occur. Also readily observed in these plots is the hot core along the inside center of the heater element leg which is undoubtedly due to the lack of radiation cooling on the I.D. of the heater leg. An END-HEAT case was run at 913 kW (6680 A) which resulted in an increase of peak temperature to 5622°F. No experimental data were available at this time to correlate with these temperature results.

Figure 22 shows the temperature results for the K heater which was run only at the START HEAT condition. The graphite base model results are shown in Figure 23. The base results shown in Figures 23 and 24 are for a slightly higher heater power of 653 kW.

Thermostructural Analysis Results--Step 3

Although the heater element is clamped to the graphite base with set screws (as shown in Figure 25) both clamped and free heater element leg end-fixity conditions were analyzed to study the effects of end-fixity on stresses. ABAQUS input data for the clamped-base J model are given in Appendix B. Figure 26 and 27 give highly exaggerated deformation plots showing both the clamped- and free-end results. The fact that the heater element leg deflects inward at the free end is probably due to the

relatively cool edges of the heater element leg, which do not grow by thermal expansion as much as the hotter center portion, and tend to pull or warp the center toward the edges.

Since it is known in advance that the heater elements fail by brittle fracture at the top and bottom fillets and that the fracture plane is approximately perpendicular to the heater element longitudinal axis, one might expect to find high axial tensile stresses at these fillet locations if, indeed, the thermal heating stresses are the cause of heater failures. The plots of axial stress in Figure 28 in fact show peak tensile stresses of 6896 and 7046 psi occurring in the J heater at the top and bottom fillets, respectively, for START HEAT. The axial stress distributions in the K heater and the heater base are shown in Figures 29 and 24. An assessment of heater element failures, based on these stress results, is given in the following two sections.

Failure Analysis--Stress Based. For brittle-type fractures in an isotropic material the so-called "maximum normal stress" failure theory can be used as the failure criterion.⁵ This theory states that tensile fracture will occur when the maximum tensile principal stress exceeds the tensile ultimate strength of the material. The (algebraically) maximum principal stress plots for the J and K heater and the heater base are shown in Figures 30-34 (Figure 35 is discussed on page 16). Peak tensile principal stresses at START HEAT of 7000 psi* occur at the fillets in the J heater in Figure 30, but the K heater in Figure 33 shows a relatively low stress at the fillet and a relatively low peak stress at the center of the leg of 4124 psi. Table 4 lists the state of thermal stress and strain at each gauss point in the top and bottom fillets where the highest principal stress occurs. As shown in Table 4 by the "axial tilt" angles of 6-19 degrees, these principal stresses act approximately in the axial direction as expected.

High axial principal stresses also occur at the threaded base of the heater element where it necks down to the thinner wall, and they are especially noticeable for the END HEAT cases (both clamped and free) in Figures 31 and 32. Failures in this base region are fairly rare, however, indicating that perhaps there is some give at the base/heater interface which limits these stresses.

The principal stress profile in the graphite near the surface of the fillets can be seen in Figures 36 and 37. These figures show profiles of temperature and the total principal

*The axial fillet stresses in Figure 28 are "nodal averaged" results whereas the principal stresses in Figure 30 were manual extrapolations to the fillet surfaces of more accurate gauss point data. The use of two different extrapolation methods accounts for the predicted bottom fillet axial stress being higher than the principal stress.

stress (the total principal stress is equal to the thermal stress minus the 750 psi compressive stress due to the hydrostatic pressure of the nitrogen gas which surrounds the heater). The stress reaches the maximum level at the fillet surface where both the temperature and the strength of the graphite are lowest. The strength of graphite, unlike most common engineering materials, actually increases substantially with increasing temperature up to about 5000°F. In both Figure 36 and 37, the stress at or near the fillet surface exceeds the indicated 4100 ksi tensile strength of the graphite indicating that a fracture is likely to occur in the fillets. This result correlates very well with the failures observed in the Tunnel-9 heater elements.

Failure Analysis--Strain Based. Table 4 lists the strains at the critical locations in the top and bottom fillets. Both the total strains and elastic strains are shown. The elastic strain (or "strain due to stress") is equal to the total strain minus the thermal strain component, $\alpha \Delta T$, at the point in question. This elastic strain value can be compared to conventional strain-to-failure data to assess probability of failure. Test data for strain-to-failure, taken from actual heater element graphite material, is shown in Appendix D. The data are for axial and circumferential directions at an elevated temperature of 2000°F, and they are plotted as strain versus probability-of-failure (POF). A POF of 60 percent, for example, means that 60 percent of the test samples failed at the indicated strain level. Profiles of total principal elastic strain in the top and bottom fillets are shown in Figures 38 and 39. As in the stress case, the maximum strain occurs at the fillet surface. The estimated maximum principal strains indicated in Figures 38 and 39 were obtained by increasing the axial strain by the principal to axial stress ratio at the point in question and then subtracting the hydrostatic strain* as shown here:

$$\begin{aligned} \text{principal strain} &= \text{axial strain} \left(\frac{\text{principal stress}}{\text{axial stress}} \right) - \text{hydro. strain} \\ &= .00319 (5815/5471) - .000326 \\ &= .00306 \text{ in/in } (\text{@ Top Fillet, GAUSS POINT 7}) \end{aligned}$$

The maximum principal elastic strains at START HEAT are .00375 and .00388 in/in in the top and bottom fillets, respectively, as shown in Figures 38 and 39. These strain levels correspond to a POF of 65 percent and 75 percent, respectively, which says 65 to 75 percent of the heater elements should fail relatively quickly, and that the remainder should have relatively long service lives. The actual heater element service lives shown earlier in Table 1 can be plotted statistically as service

* The hydrostatic strain, E_h , due to the 750 psi gas pressure is computed using: $E_h = (1-2\nu)P/E$ where E_h =hydrostatic strain, ν =poisson ratio, P =pressure, E = Young's modulus.

versus percentage of heater elements which will fail by this life (cumulative frequency) as Figure 40 shows. Interestingly, the data show that up to about 70 percent of the heater elements had average (20 cycles) or shorter service lives, and about 20 percent had relatively long service lives of 50 or more cycles. This result agrees well with the strain based failure rate prediction, and this is somewhat fortuitous considering the small statistical population used and other factors. This result shows that, for a linear stress analysis such as this one, the strain based failure criterion yields more realistic results than the stress based one which, in all cases, predicts a 100 percent failure rate based on the data in Appendix D. This is due to the fact that graphite material exhibits a strain-softening stress-strain relation which, if ignored, will cause the thermal stresses to be over-predicted.

Table 5 summarizes the stress and strain failure analysis results. Note that even the strain failure rate is 100 percent for the high power (913 kW) case in Table 5 owing to the substantial increase in fillet stress with increased heater power. It has been found that, in fact, heater element failures occur more frequently when the heater elements are run at higher power levels.

GRAPHITE HEATER ELEMENT FILLET STRESSES

During the course of this investigation various studies were performed to:

1. Explain why high axial tensile stresses occur at the top and bottom fillets.
2. Investigate methods to reduce high stresses in the graphite heater elements, thereby providing a means to extend the useful service life of a heater element.

Fillet Stress Breakdown

Parametric studies were performed to breakdown the bottom fillet stress into component parts. Figure 41 presents the results of these studies. Five main effects are identified here in order of importance:

1. Differential Radiation Effect (42 percent)
2. Edge Cooling Effect (31 percent)
3. Thickness Cooling Effect (17 percent)
4. Beam Bending Effect (6 percent)
5. Fillet Hotspot Effect (4 percent)

Each effect is described below briefly.

Differential Radiation Effect. The O.D. of the heater tube radiates freely to the heater vessel liner whereas the I.D. is more or less enclosed; hence, there is a decreasing temperature gradient from the I.D. to the O.D., tending to induce axial tension at the O.D. and axial compression at the I.D.

Edge Cooling Effect. The edges of the heater element legs are more efficiently cooled than the center portion because of exposure to the cool nitrogen gas on three surfaces instead of just two. Hence the edges tend to stay at a lower temperature than the center and, due to less thermal expansion, are "stretched" axially by the hotter center and develop axial tensile stress.

Thickness Cooling Effect. Internal volumetric heating in a thin slab with cooling on the slab surfaces produces a parabolic temperature gradient. The core of the slab tends to expand more than the outer material creating a compressive core and tensile skin.

Beam Bending Effect. The gross thermal expansion of the heater element sets up "beam bending"-type stresses in the heater element legs when the base is clamped. The 6 percent figure indicated for this effect may be conservative since it is based on a case where the heater was uniformly heated to 4000°F which does not induce the more severe gross warping evident in Figure 26.

Hotspot Effect. Additional thermal expansion of material at the internal hot-spots located near the fillets tends to put additional tensile stress in the fillets.

The first three effects perhaps explain why the axial thermal stresses in the heater element leg are tensile at the O.D., even more tensile at the edges, and compressive at the center core. The last two effects may explain in part why the tensile edge stresses tend to peak out at the top and bottom fillets.

Stress Reduction Methods

Regarding the edge cooling effect, it was noticed in the course of these studies that the temperature in a heater element leg is lowest at the sharp corners on the edges of the leg (as shown in Figure 35). This cooler material cannot expand as much as the core and, hence, the corners are stretched in tension as the hot core expands. It was found that rounding off the sharp corners, as shown in Figure 35 and 42, substantially reduced fillet stresses on the order of 20 to 30 percent.

Another technique which may be useful for reducing fillet and edge tensile stresses is to provide a "cooling slot" at the center of each heater element leg to help cool the hot core. Figure 43 shows how this could be done by "slicing" the legs through at section AA and rotating the halves outward. A prototype design for such a heater element is shown in Figure 44 where the cooling slot extends the full length of the hot portion of the heater element leg. It was found in one analysis of a cooling slot design that the top and bottom fillet stresses decreased by 25 percent and 35 percent, respectively, as compared to the nonslotted heater element.

ASSUMPTIONS

Various assumptions were made in this analysis. For example, the use of one identical sink temperature for both convection and radiation heat transfer assumes the insulation liners run at the same temperature as the nitrogen gas. However, since nitrogen gas is essentially transparent to heater radiation, the liner receives radiation directly from the heater element and probably runs hotter than the gas. (Preliminary calculations indicate that the liner may run 800°F hotter.) This effect would lead to a hotter element and, as some preliminary analyses have recently shown, somewhat lower thermal fillet stresses in the heater element (perhaps 20 percent lower). On the other hand, although the fillet stresses may be lower, the true ultimate tensile strength of a given volume of graphite may be significantly lower than the average strength used here. This is due to the actual strength of a brittle material (such as graphite) being determined by the distribution of flaws in the material.⁶ For this reason the tensile strength of graphite is highly variable to such a point that the true strength of any one sample can vary significantly from the average strength data. The statistical tensile strength plots in Appendix D were obtained from tensile tests on actual graphite samples which were machined from failed heater element material, and they show the scatter typical for this graphite. The statistical strength variation shown in Appendix D holds only for the specific volume of material associated with the tensile specimen gauge section (Vol = 0.066 cu in). In order to accurately assess failure in a graphite part such as a heater element, a sophisticated failure assessment must be carried out that accounts for the volume of material in the element which is subjected to high tensile stresses. A failure criterion with these features requires a large body of statistical material data which is currently not available for the heater element.⁷

CHAPTER 4

CONCLUSIONS

This report documents a general finite element method for investigating the electrical, thermal, and thermostructural performance of electrically powered heating devices. The method was applied to a graphite heater element utilized in the NSWC Hypervelocity Tunnel No. 9 to pre-heat nitrogen working gas to temperatures of 3100°F. Electric current density and temperature distributions at the start and end of the nitrogen preheating period are presented. Thermal stresses in the graphite heater element are presented which predict that crack initiation of the type actually exhibited in the heater elements is likely to occur at the top or bottom fillet of the J-type heater due to high tensile thermal stresses which occur in these regions. The likelihood of a crack starting is greater near the beginning of the heating period. Also, it is greater with lower Reynold's Number tunnel conditions since the relatively low hydrostatic pressure of nitrogen gas at these conditions does not relieve the tensile fillet stresses enough to prevent fracture. The results correctly predict that crack initiation is more likely at higher heater powers due to an increase in fillet thermal stresses with increased power. The stress models also correctly predict that the K-type heater will tend to fail at the bottom fillet because the geometry of the K heater at the top fillet effectively limits the axial tensile stress in the top fillet to relatively low levels.

Two methods for reducing fillet stress levels are presented. First, the technique of rounding the edges of the heater element legs is shown to reduce fillet stresses by perhaps 20 to 30 percent. Second, by providing a central cooling slot in each heater element leg, the fillet stresses were reduced by 25 to 35 percent.

The results presented here suggest that the fillet stresses generated during the nitrogen heating period are a primary cause of heater element fracture. The exact mechanism for initial fracture may be tensile fracture or fatigue. If high tensile fillet stresses during heating are in fact causing the heater element failures, then the two methods presented for reducing fillet and edge stresses, if implemented, may significantly increase the survivability of the Tunnel-9 graphite heater element.

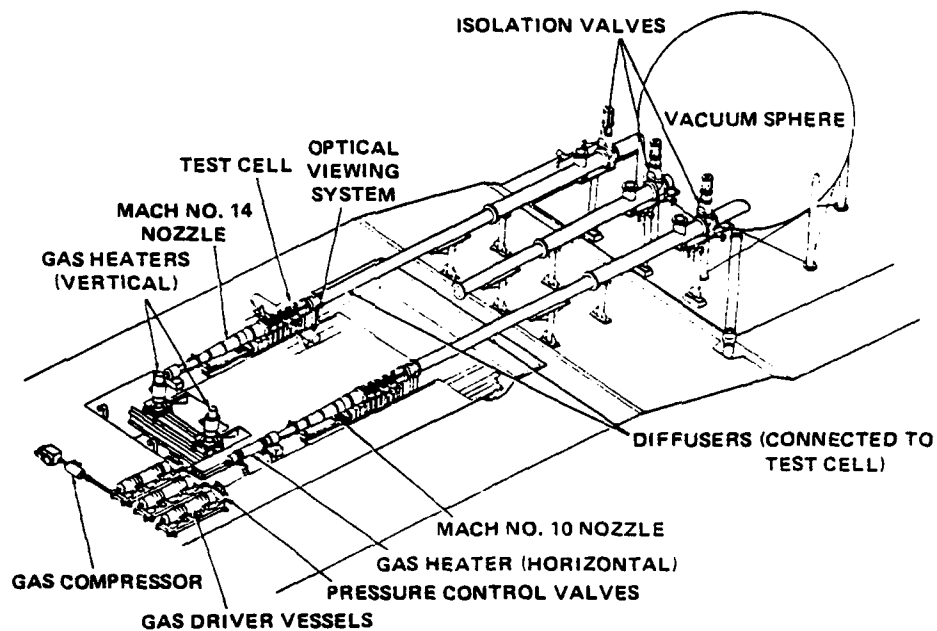


FIGURE 1. SCHEMATIC OF TUNNEL NO. 9 FACILITY

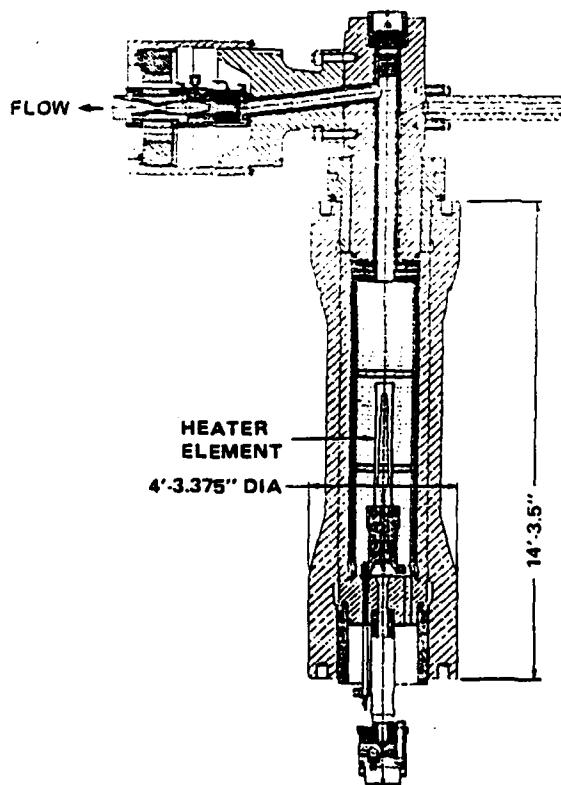


FIGURE 2. VERTICAL HEATER AND DIAPHRAGM SECTION

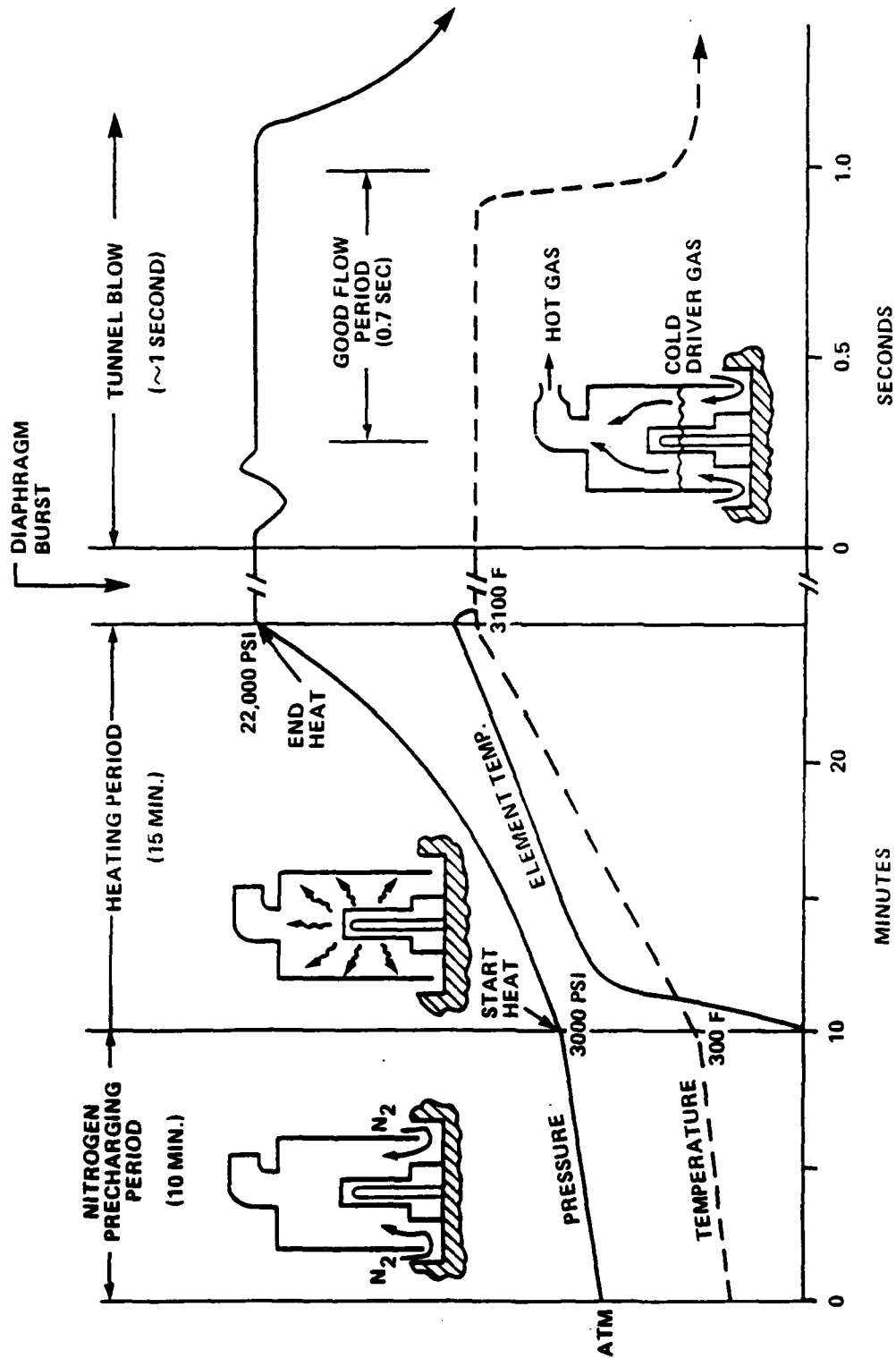


FIGURE 3. HEATER GAS CONDITIONS FOR A TYPICAL MACH-14 WIND TUNNEL RUN

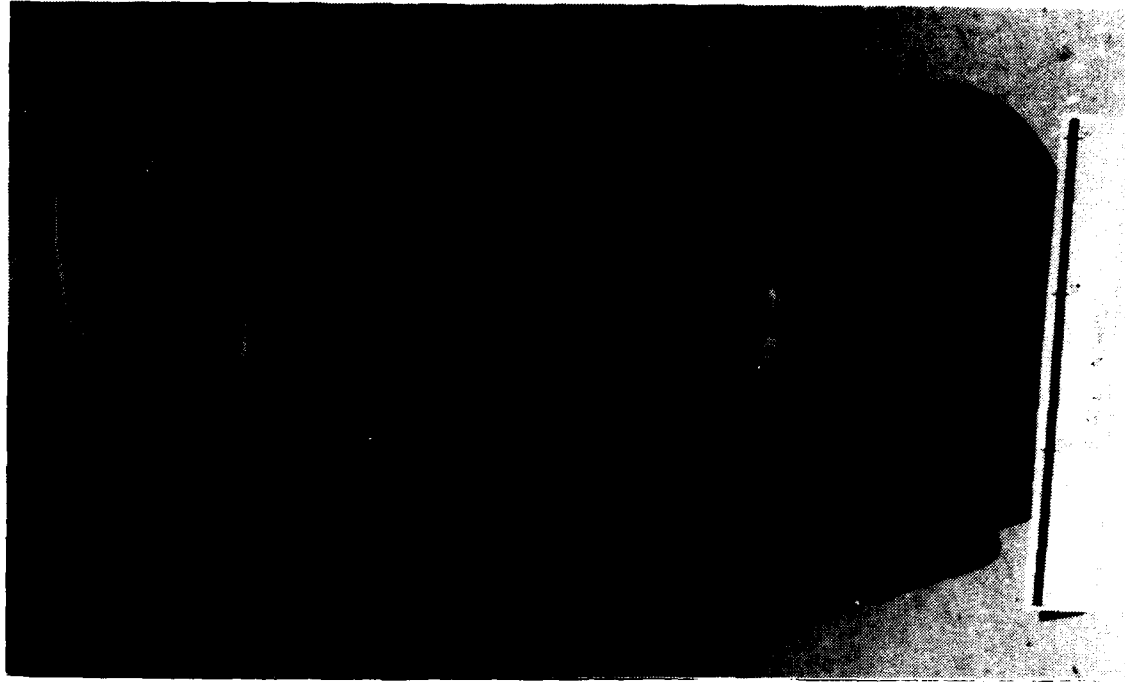


FIGURE 5. COMPLETELY FAILED HEATER - BOTTOM
FILLET LOCATION

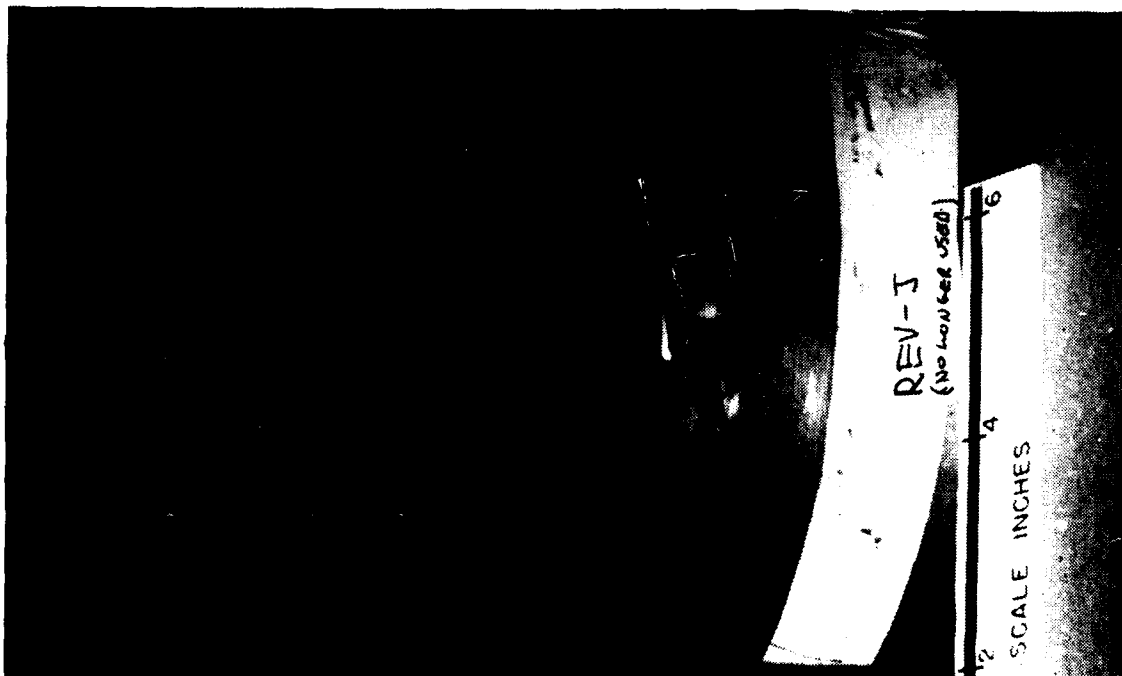


FIGURE 4. COMPLETELY FAILED HEATER - TOP FILLET
LOCATION

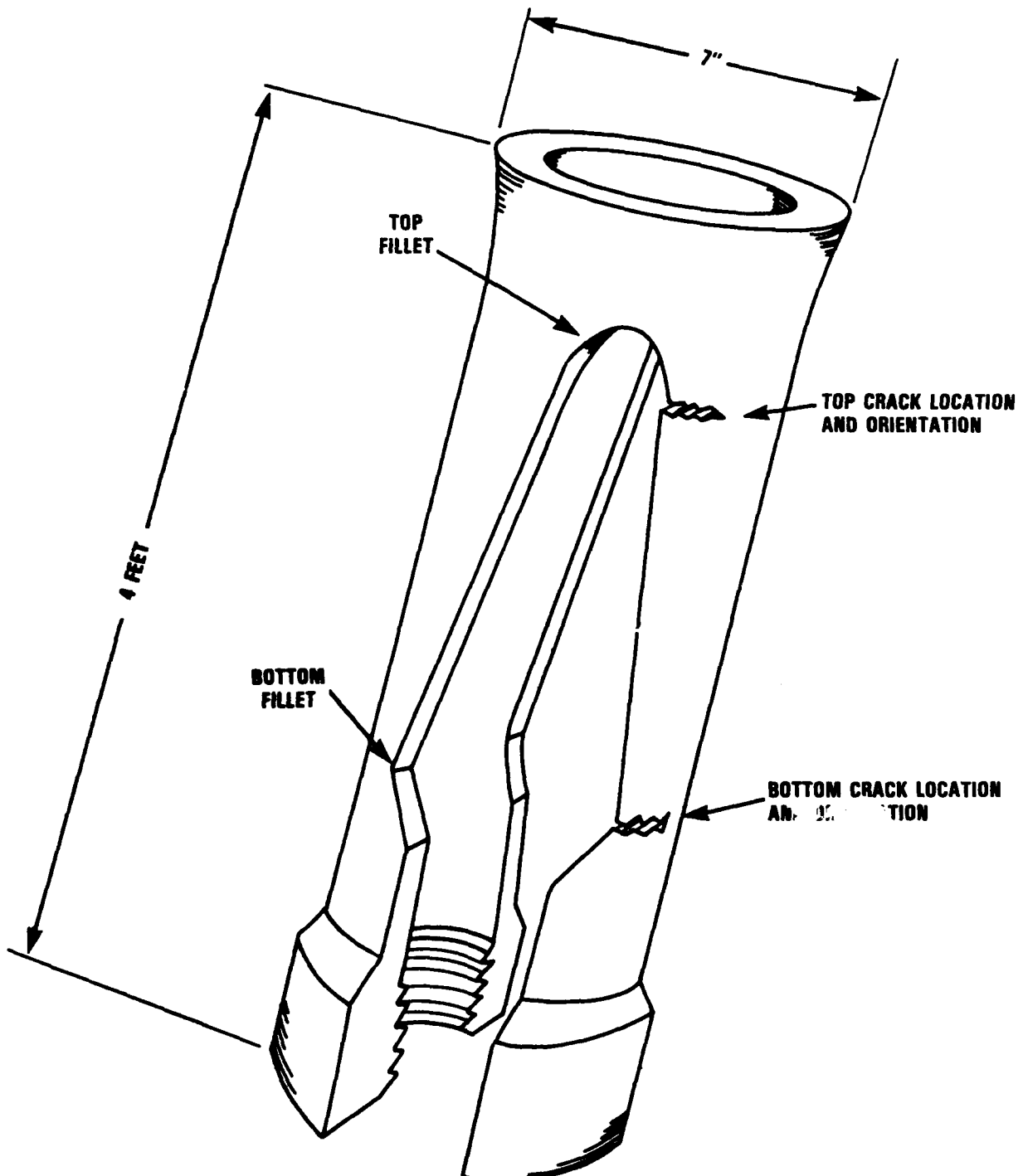


FIGURE 6. TOP AND BOTTOM FILLET CRACK LOCATIONS IN THE GRAPHITE HEATER

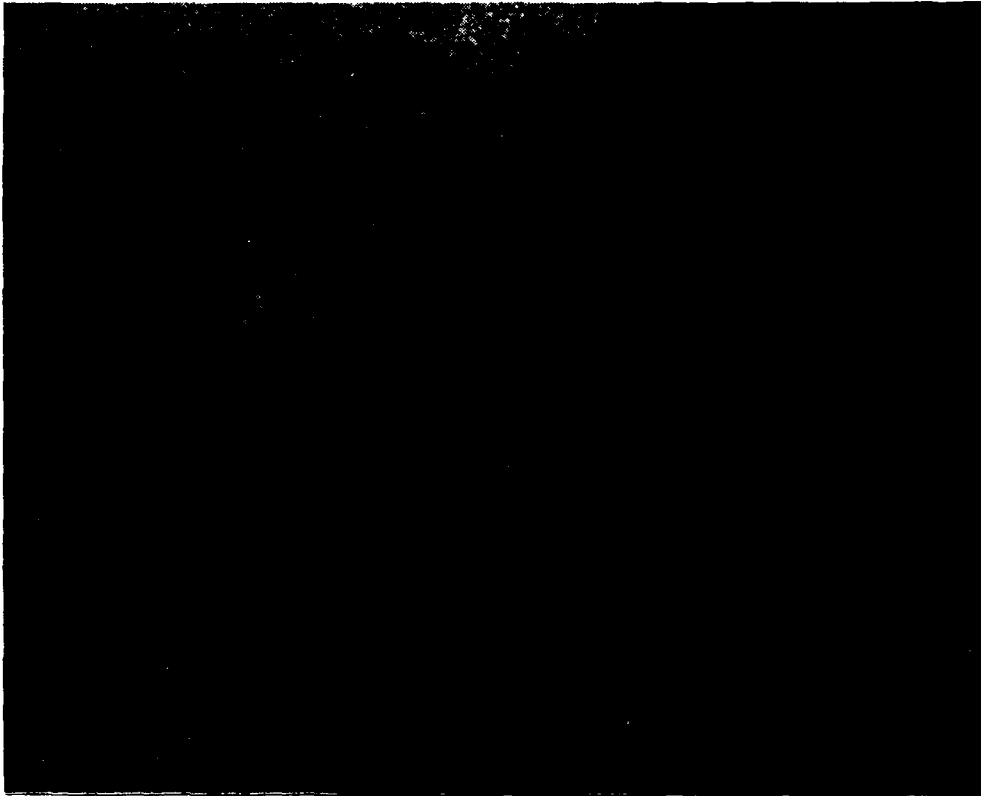


FIGURE 7. PARTIAL TOP FILLET CRACK

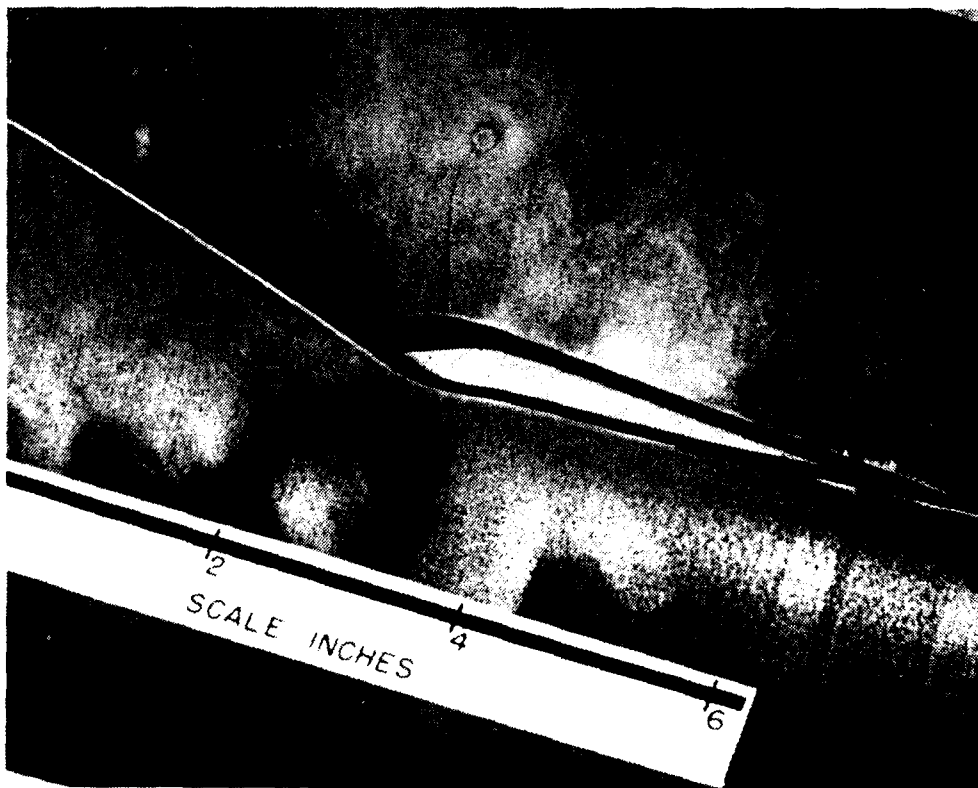


FIGURE 8. PARTIAL BOTTOM FILLET CRACKS

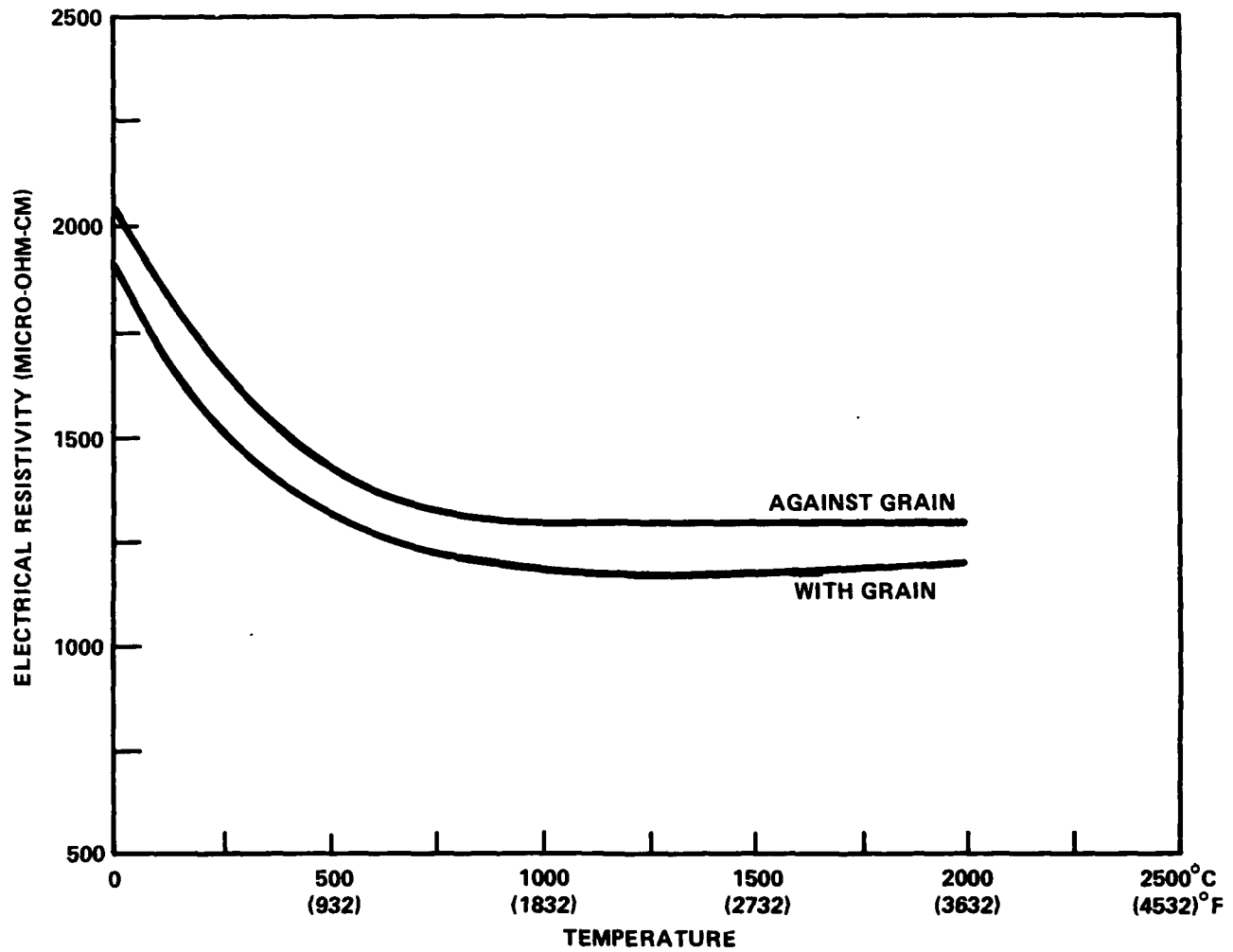


FIGURE 9. HEATER GRAPHITE ELECTRICAL RESISTIVITY VERSUS TEMPERATURE

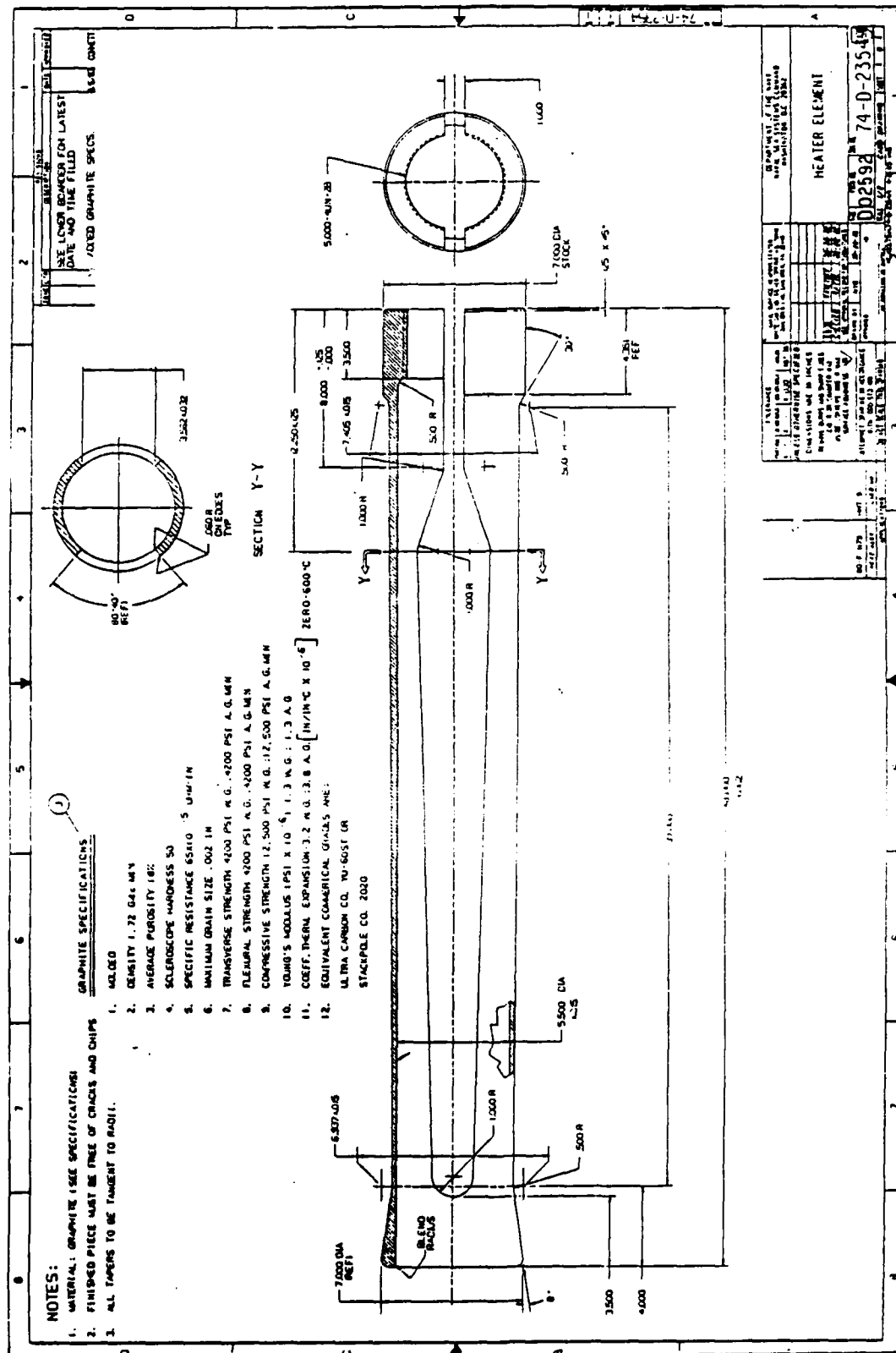
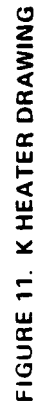


FIGURE 10. J HEATER DRAWING





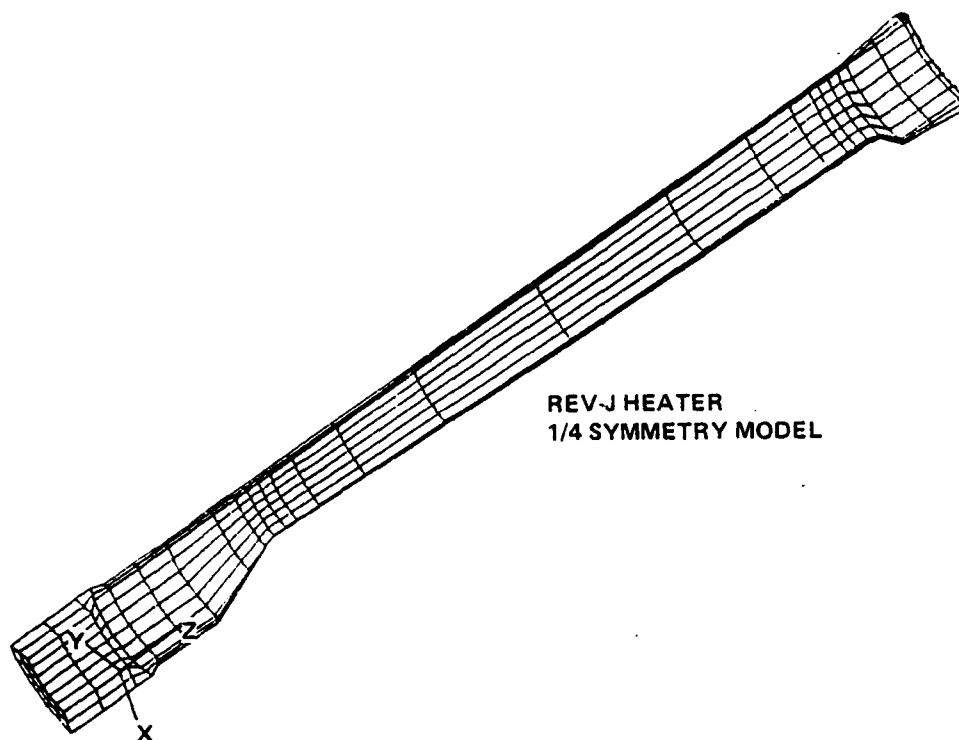


FIGURE 13. J HEATER FINITE ELEMENT MODEL

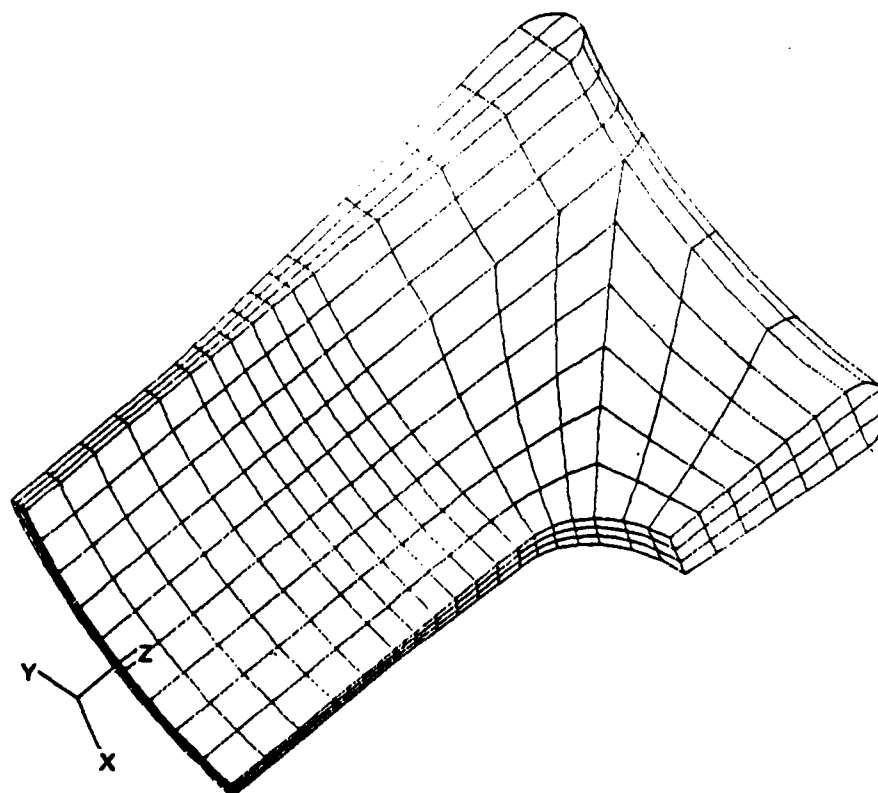


FIGURE 14. K HEATER FINITE ELEMENT MODEL

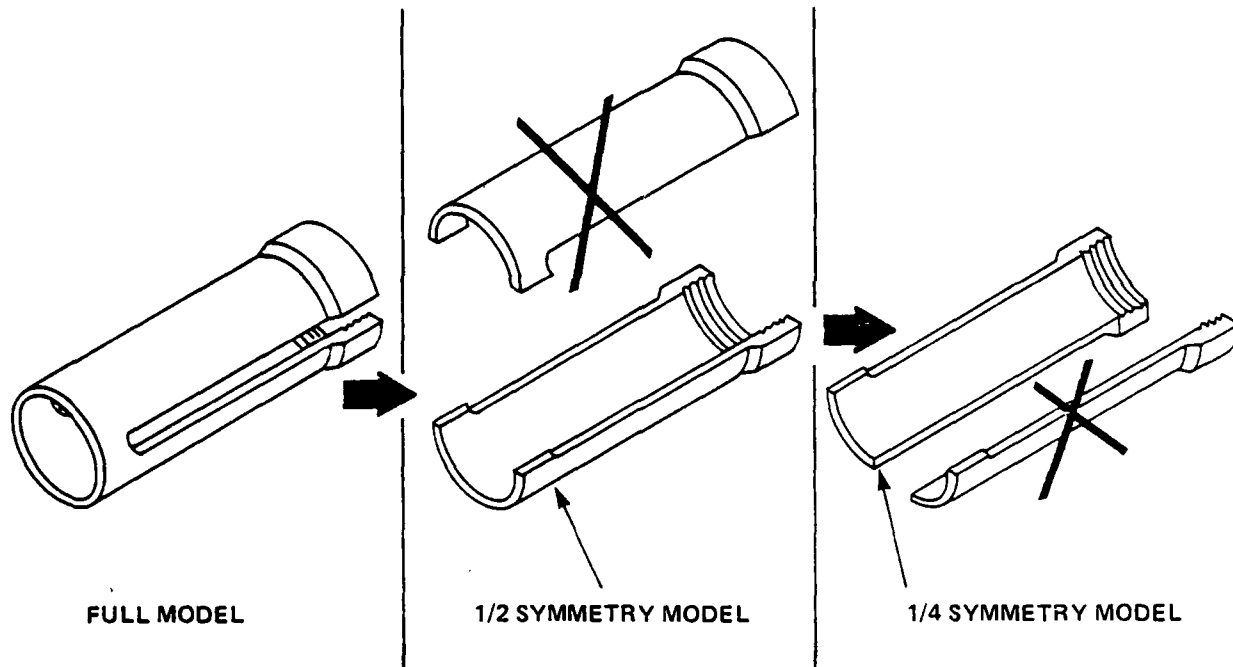


FIGURE 15. FINITE ELEMENT MODEL USES HEATER SYMMETRY TO REDUCE MODEL SIZE

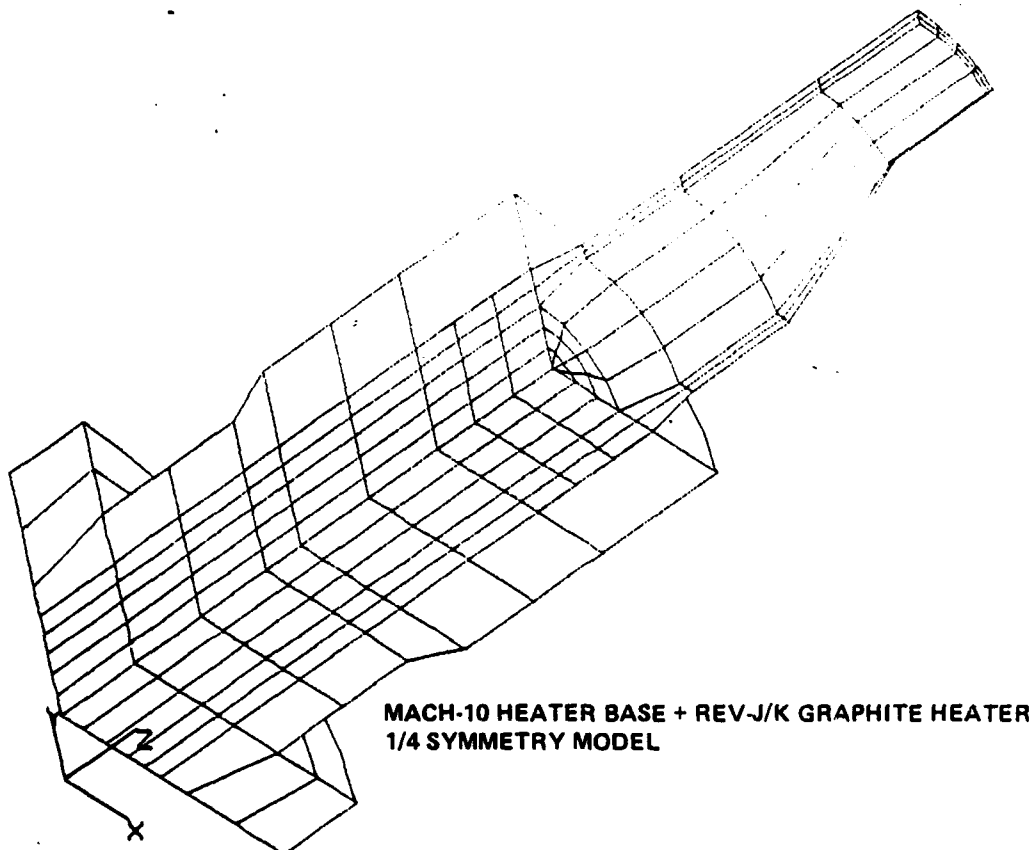


FIGURE 16. MACH-10 HEATER BASE FINITE ELEMENT MODEL

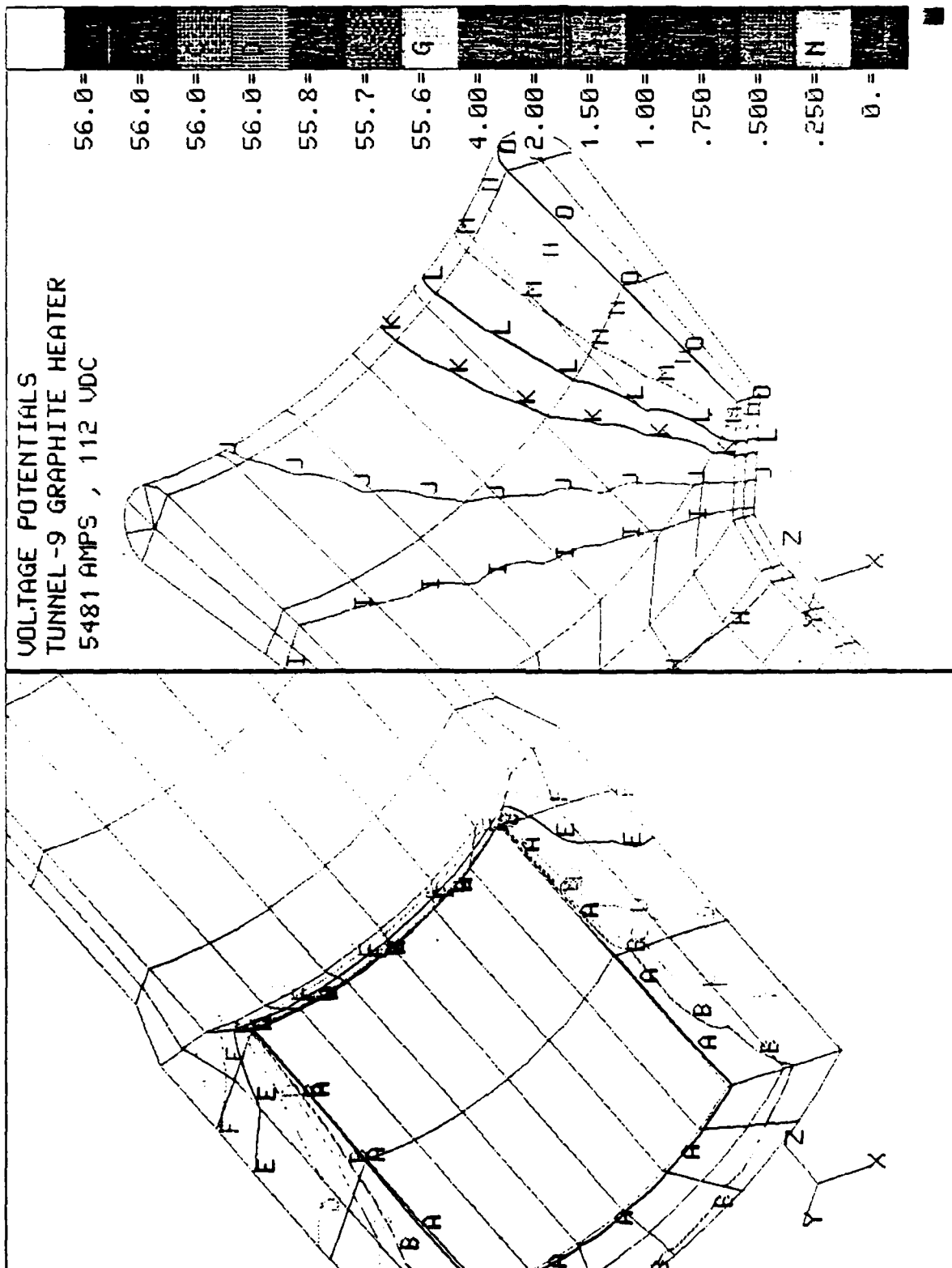


FIGURE 17. VOLTAGE POTENTIALS IN THE J HEATER

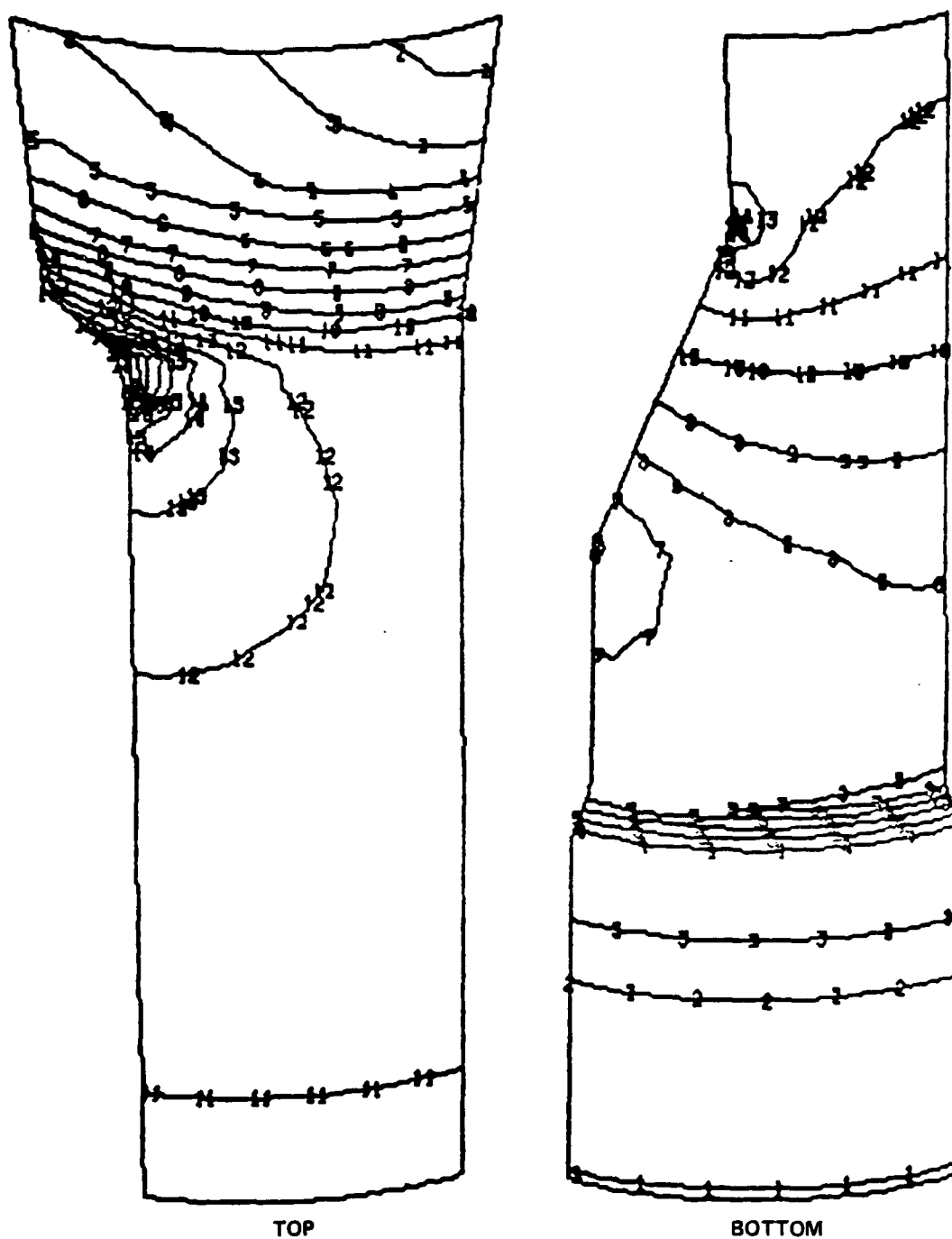


FIGURE 18. CURRENT DENSITY CONTOURS IN THE J HEATER

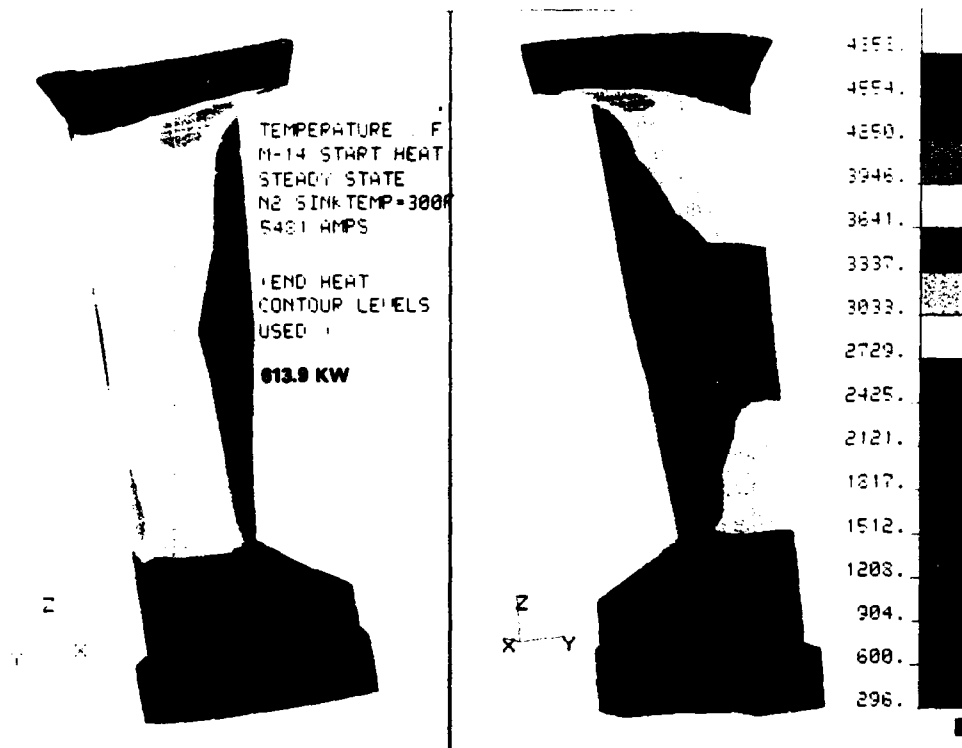


FIGURE 19. START HEAT TEMPERATURES IN THE J HEATER

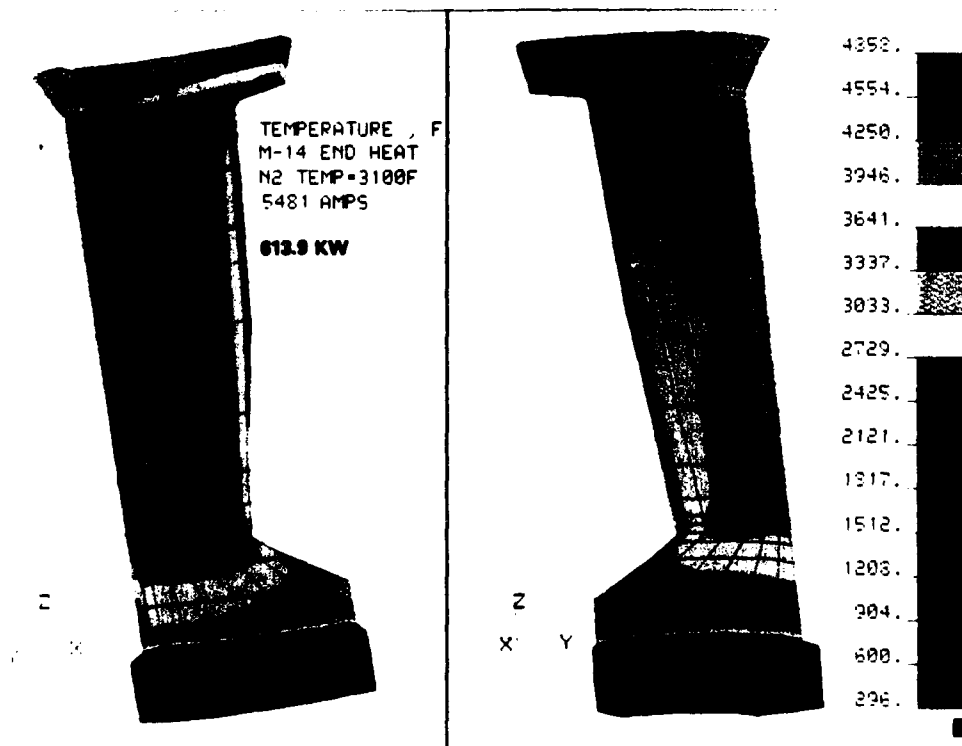


FIGURE 20. END HEAT TEMPERATURES IN THE J HEATER

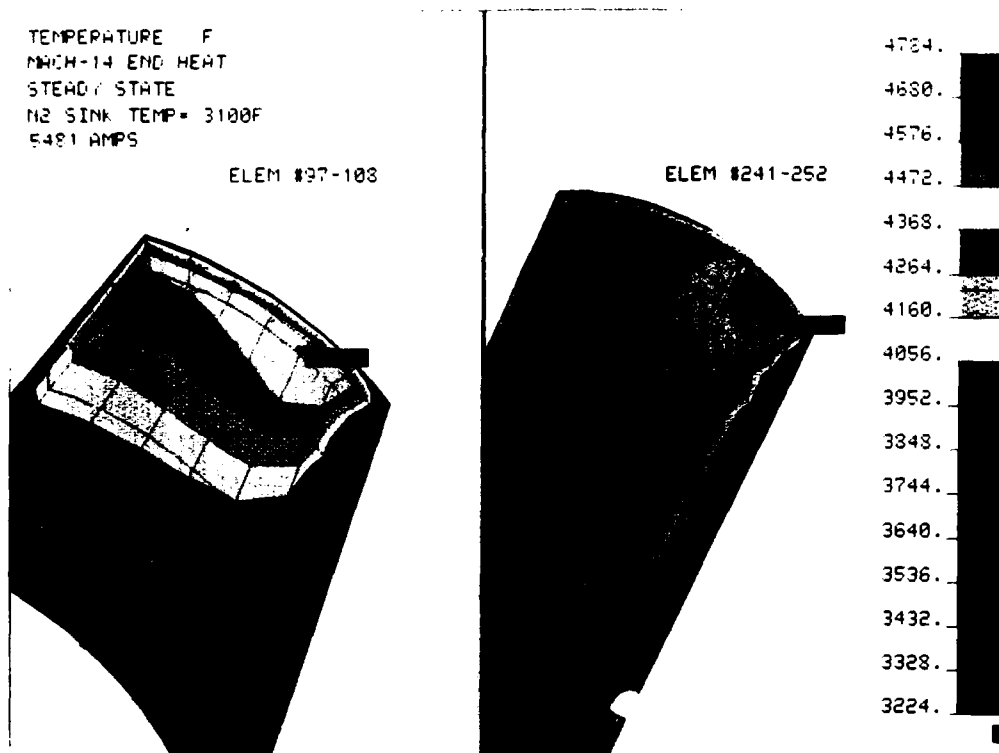


FIGURE 21. END HEAT TEMPERATURES IN THE J HEATER

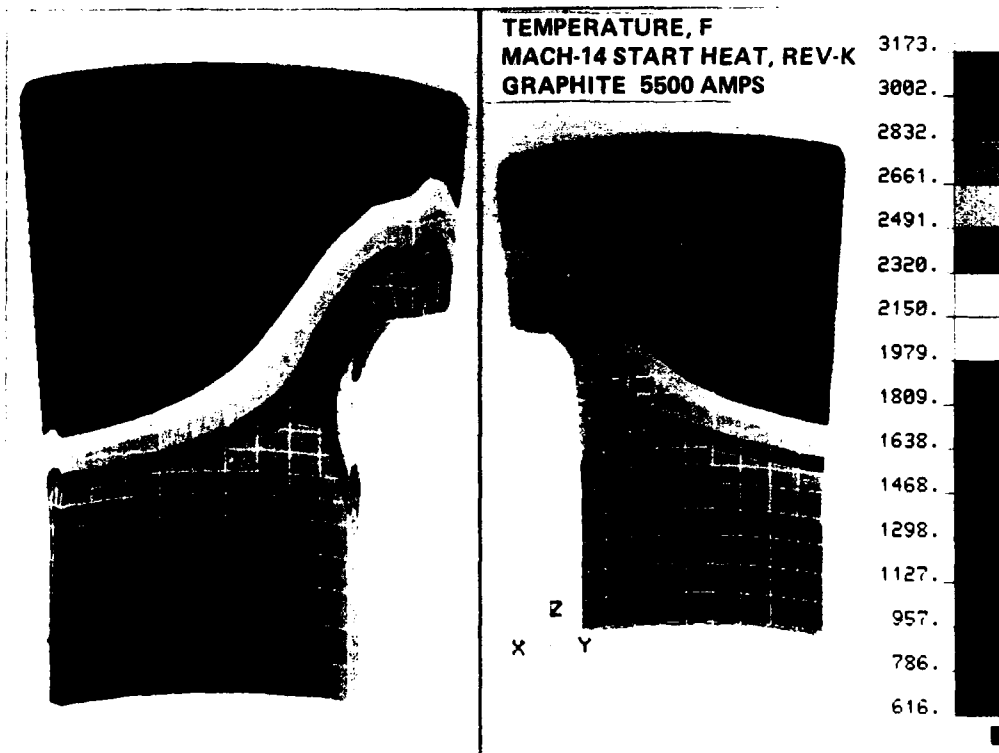


FIGURE 22. START HEAT TEMPERATURES IN THE K HEATER

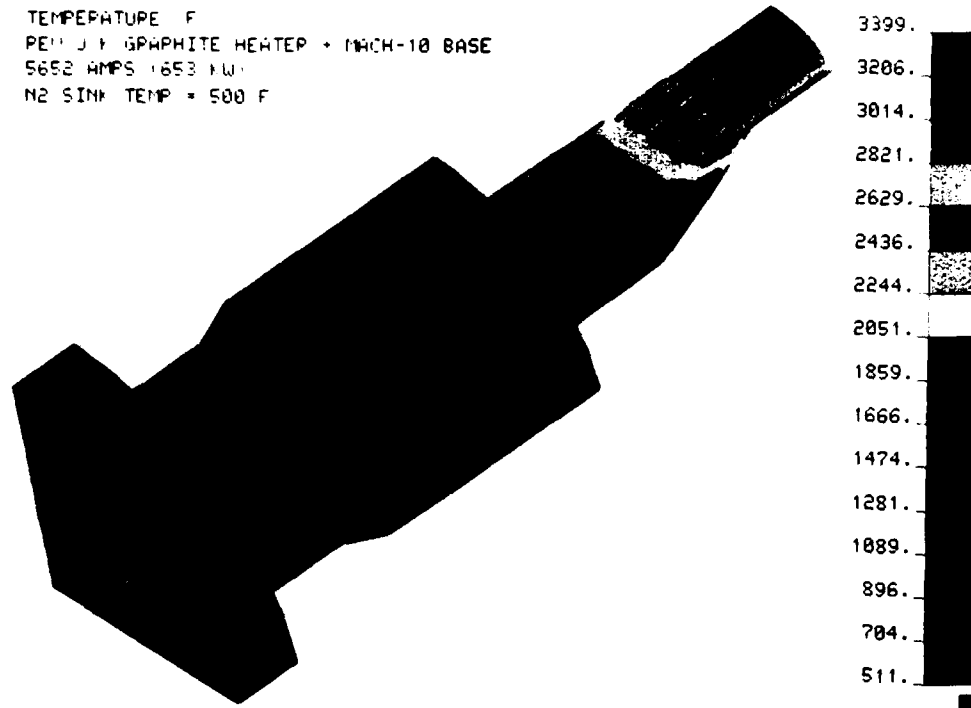


FIGURE 23. START HEAT TEMPERATURE IN THE MACH-10 BASE

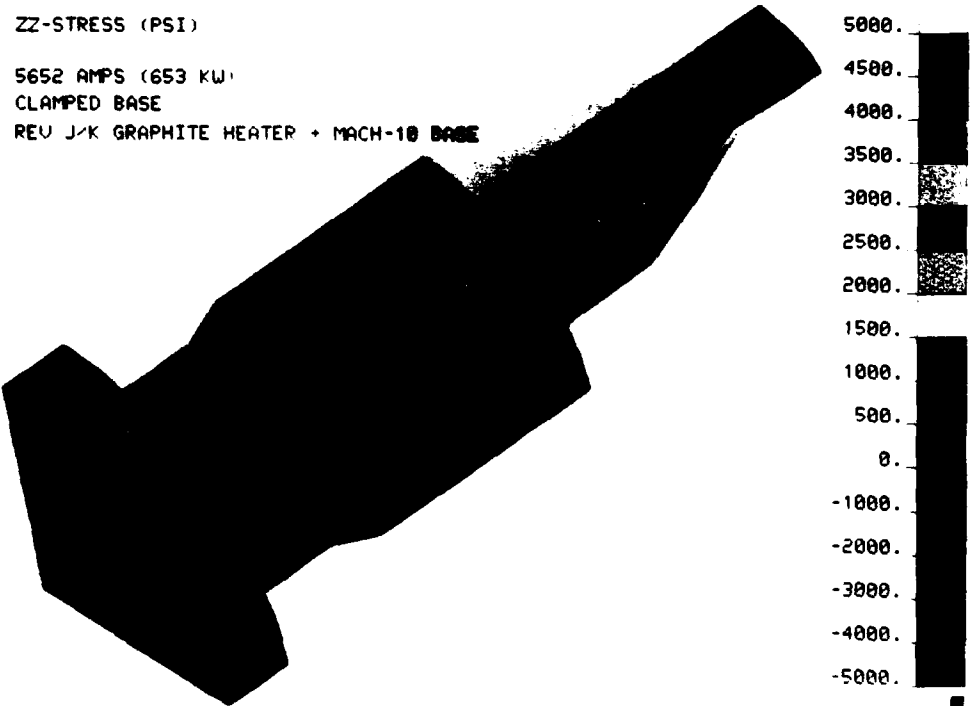


FIGURE 24. AXIAL STRESS IN MACH-10 BASE

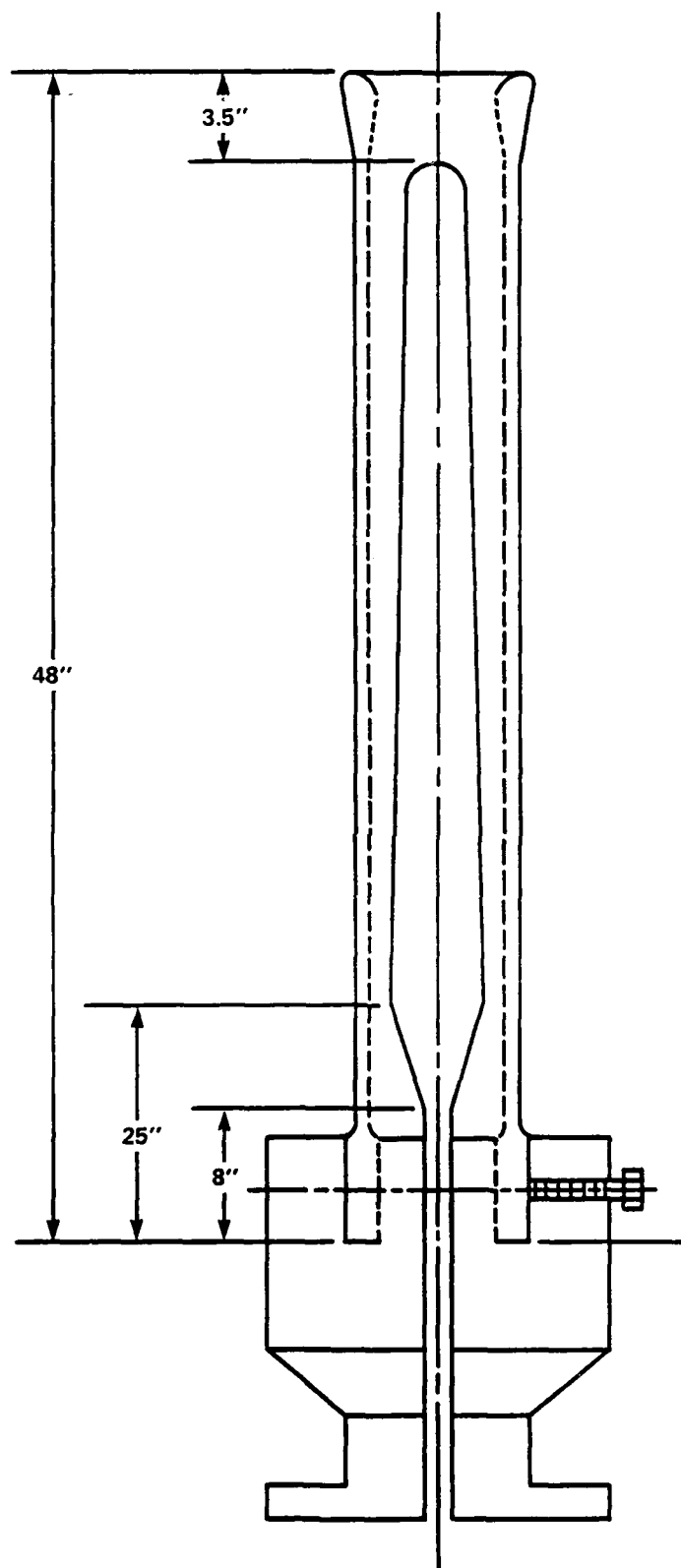


FIGURE 25. HEATER ELEMENT/BASE CLAMPING ARRANGEMENT

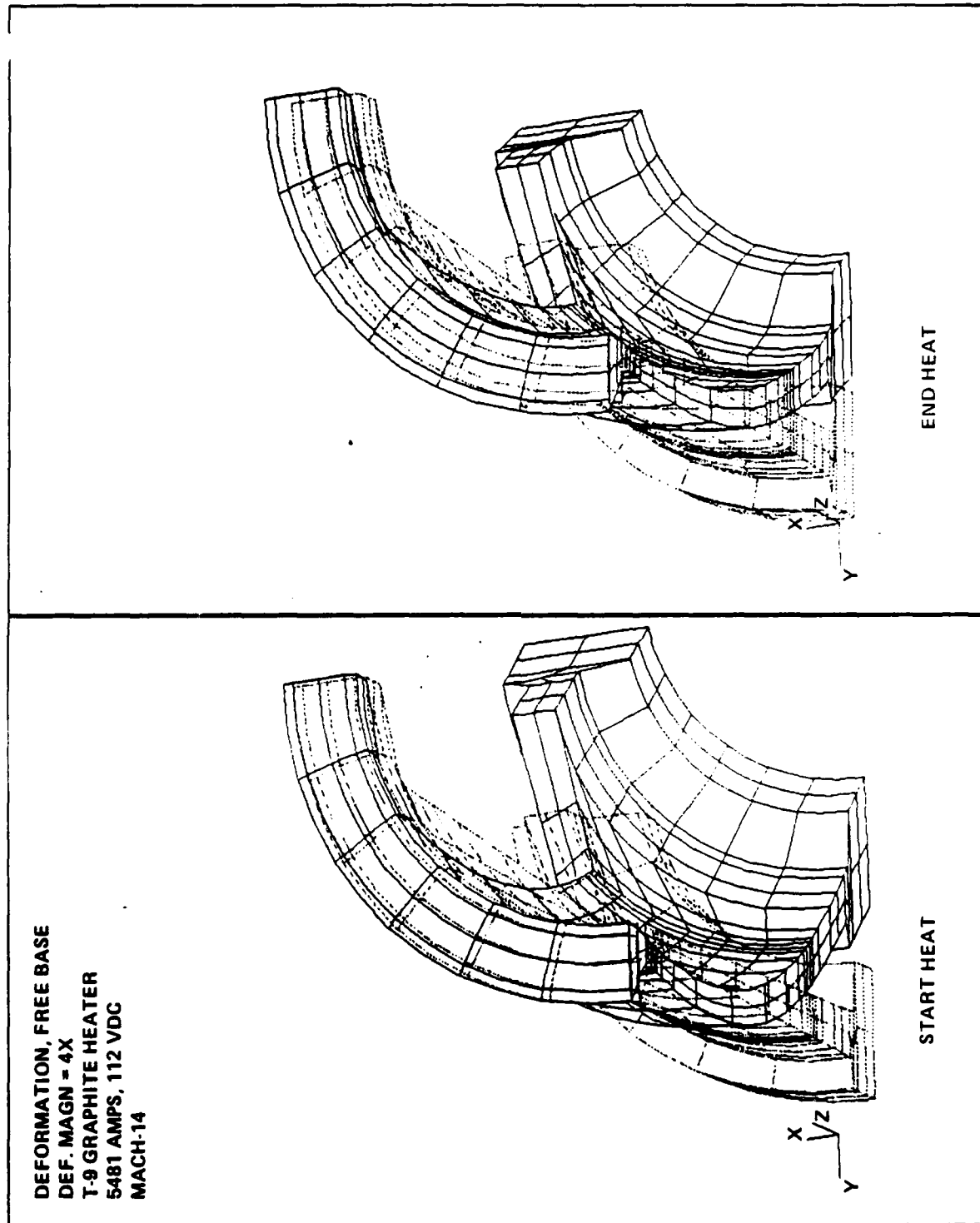


FIGURE 26. DEFORMED SHAPE PLOTS -- FLOATING BASE

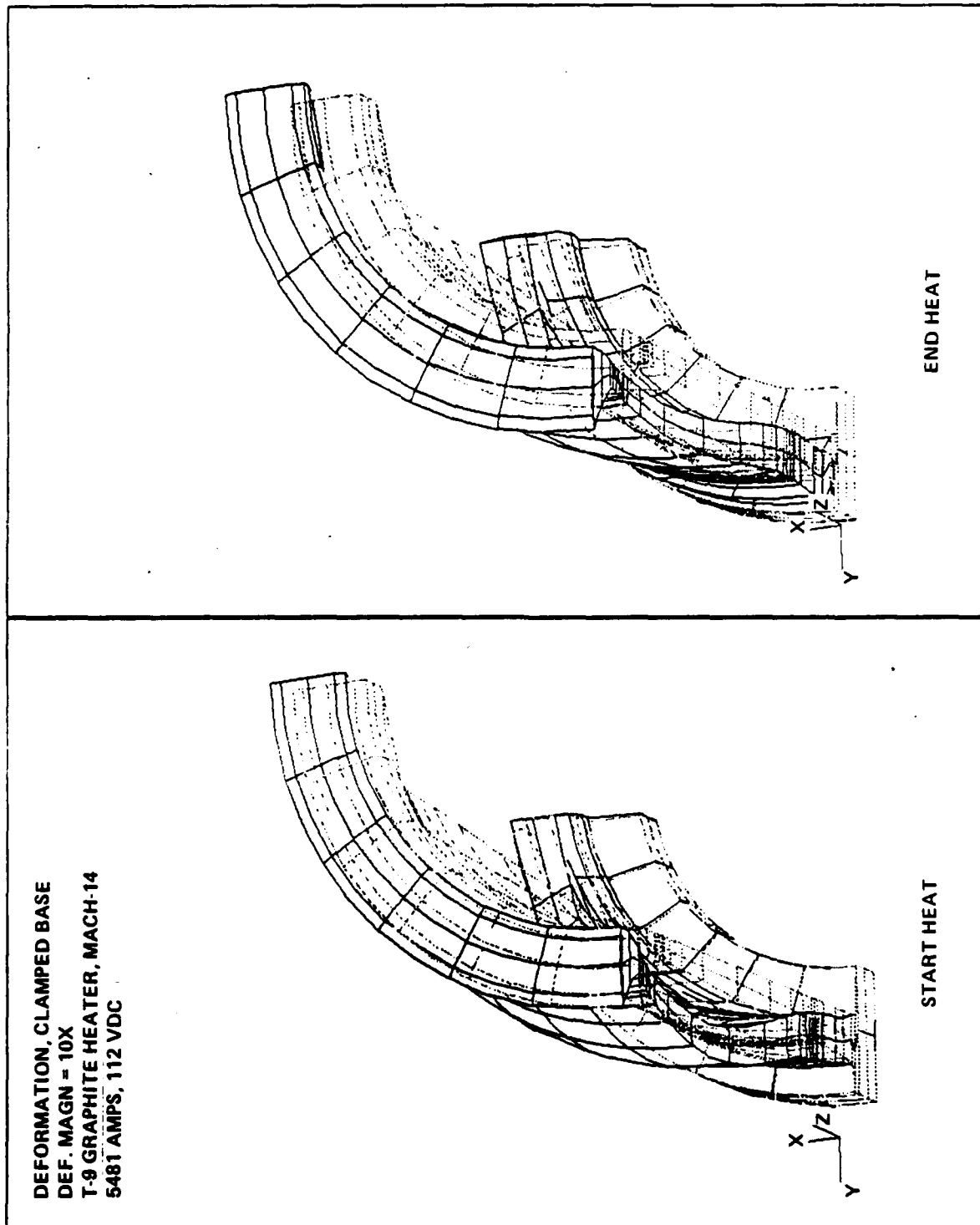


FIGURE 27. DEFORMED SHAPE PLOTS - CLAMPED BASE

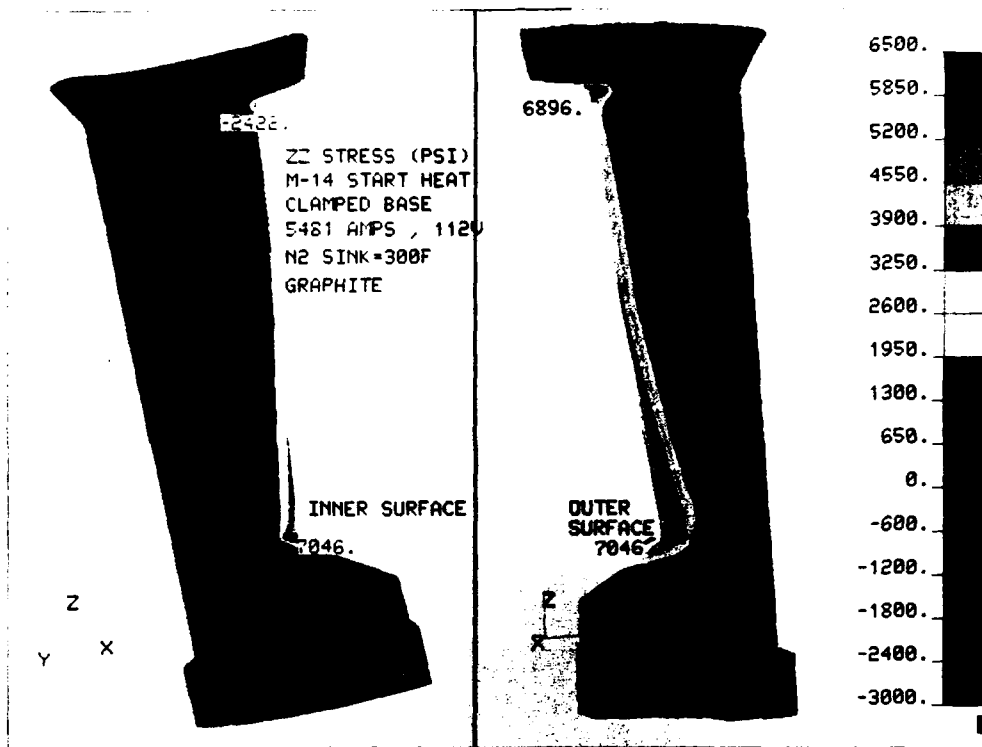


FIGURE 28. AXIAL STRESS IN J HEATER

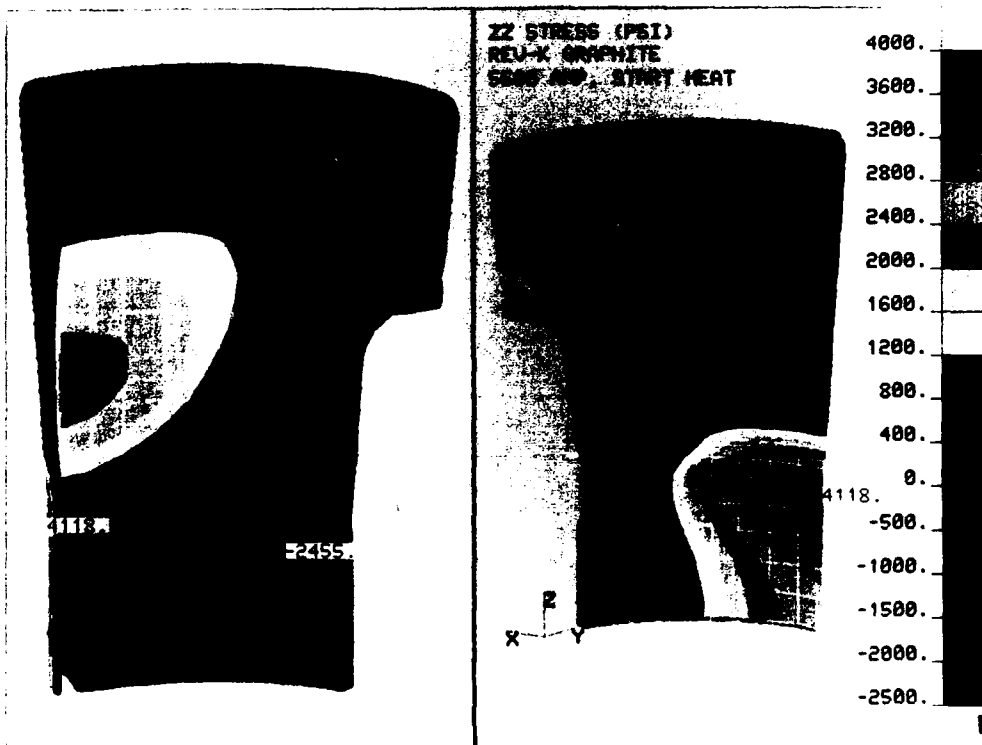


FIGURE 29. AXIAL STRESS IN K HEATER

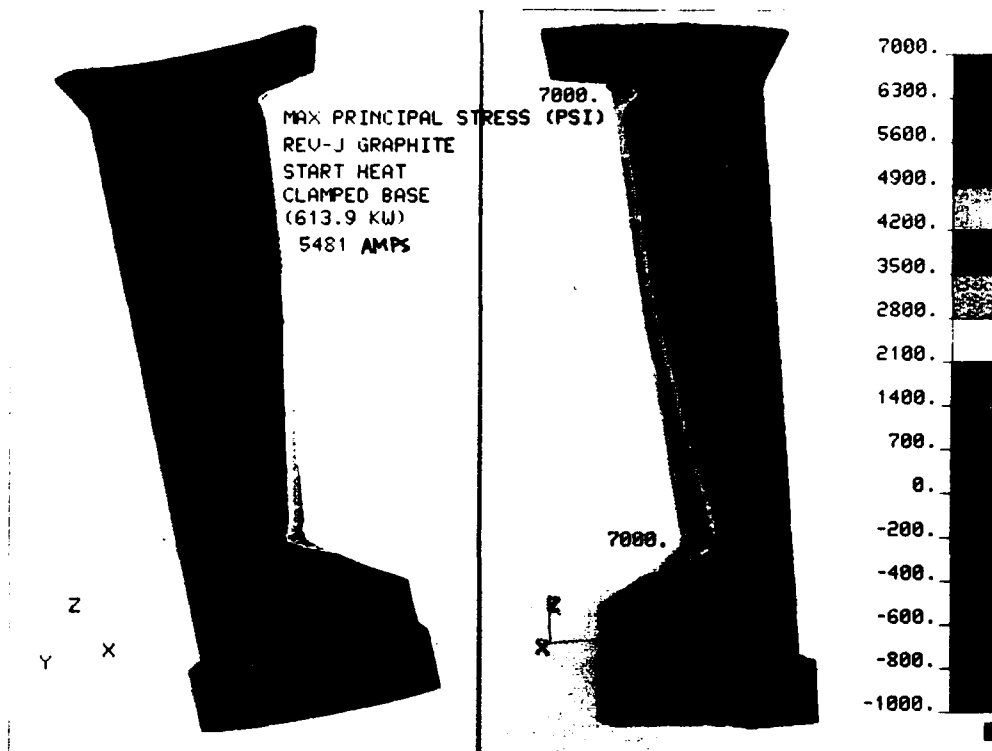


FIGURE 30. MAXIMUM PRINCIPAL STRESS - J HEATER, START HEAT

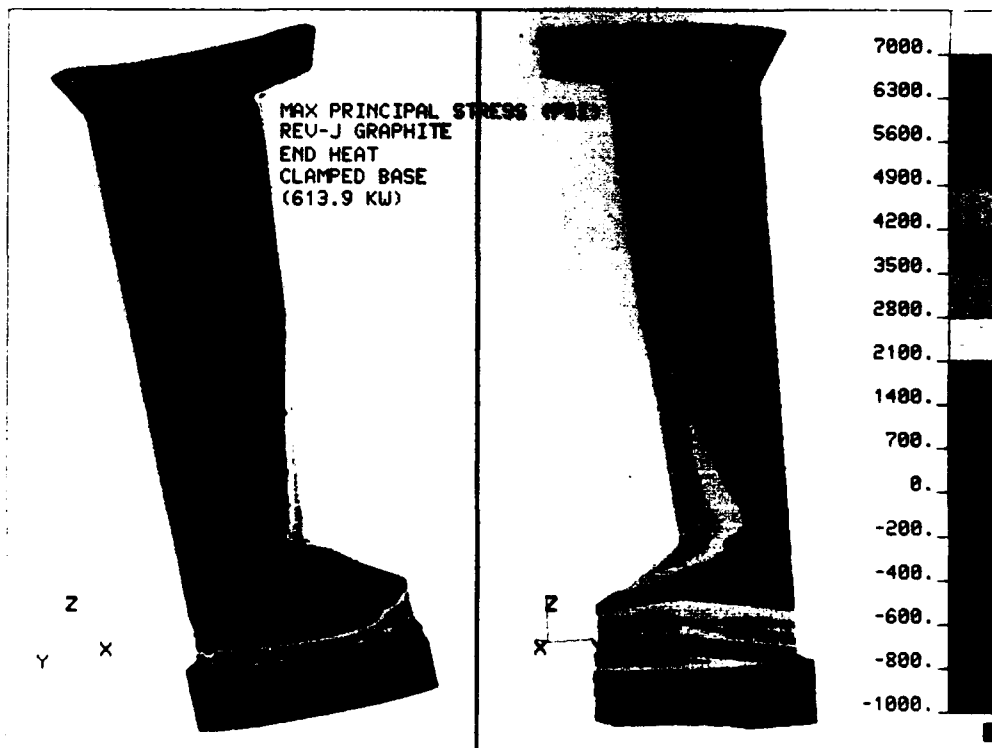


FIGURE 31. MAXIMUM PRINCIPAL STRESS - J HEATER, END HEAT

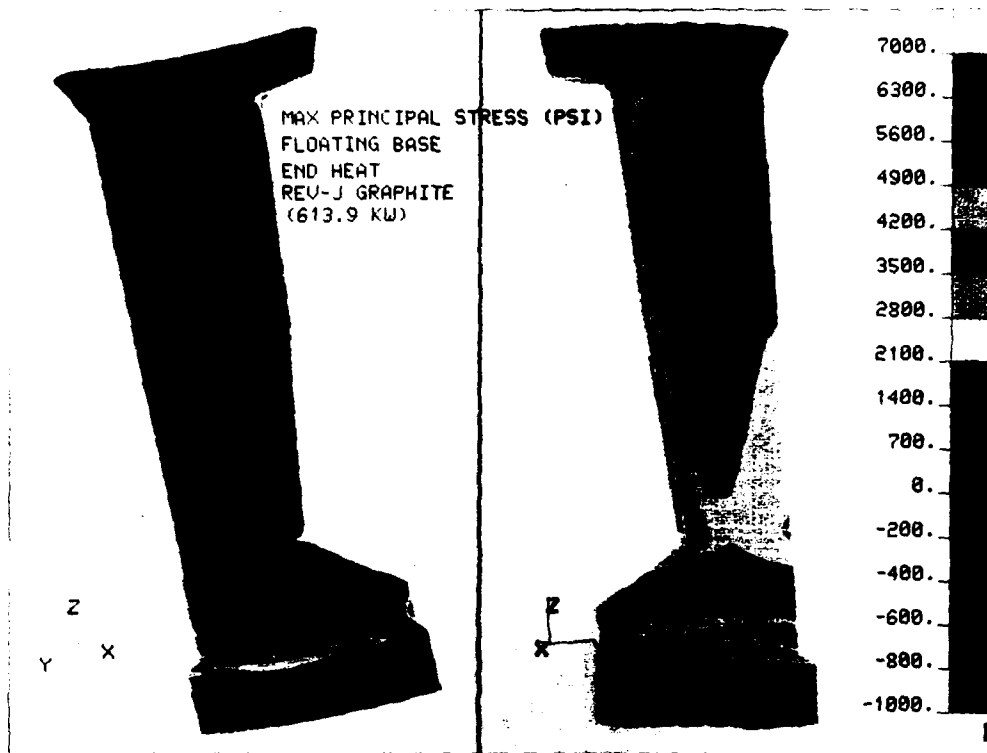


FIGURE 32. MAXIMUM PRINCIPAL STRESS - J HEATER, FREE BASE

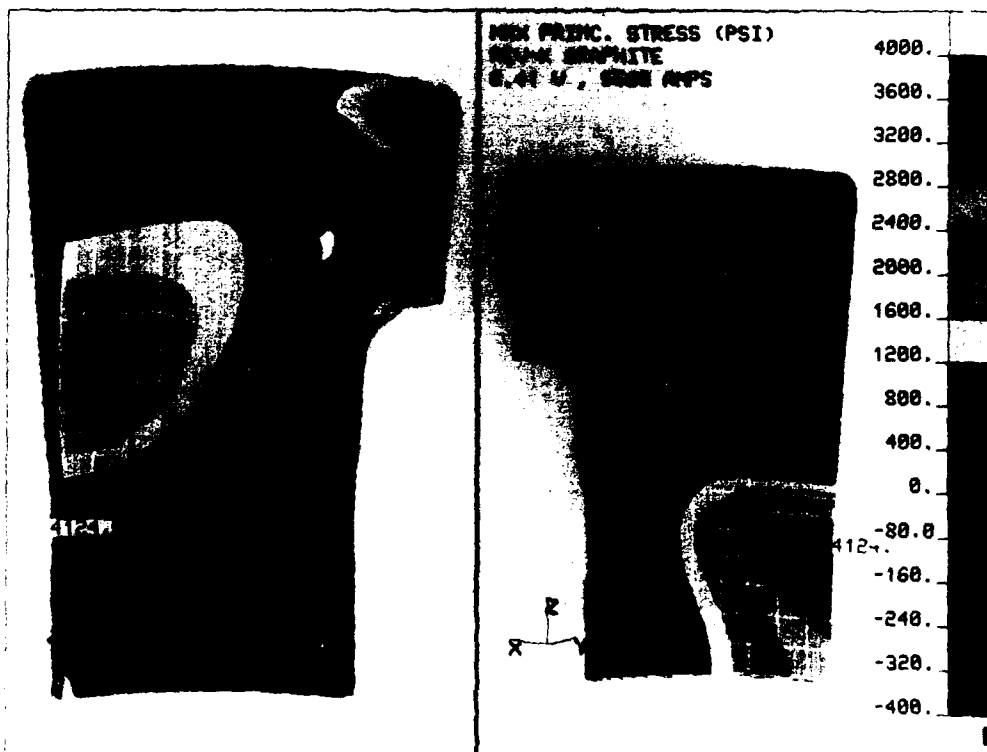


FIGURE 33. MAXIMUM PRINCIPAL STRESS - K HEATER, START HEAT

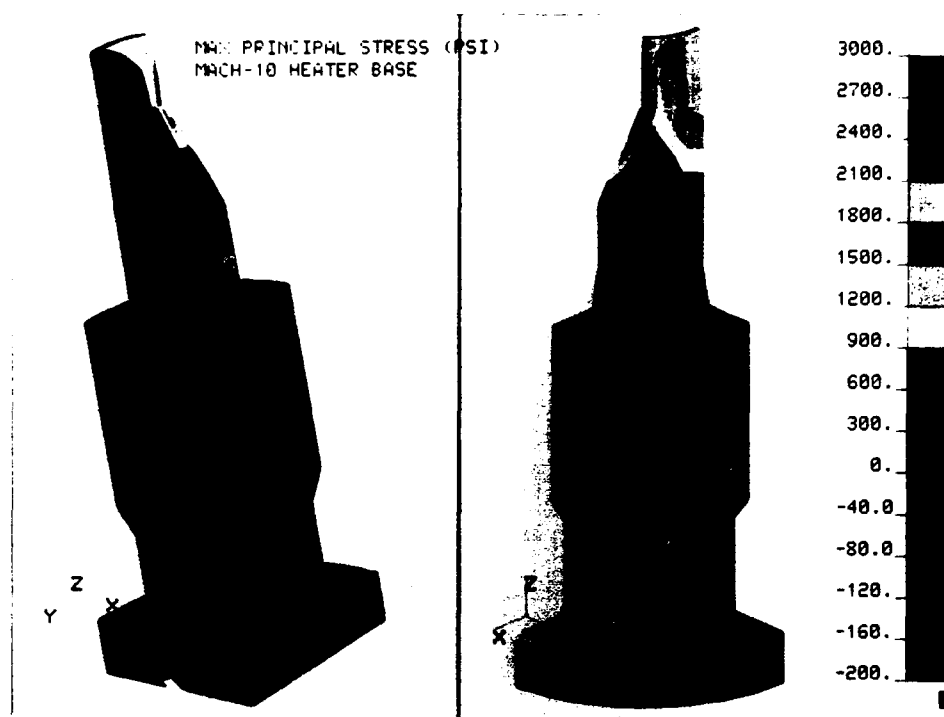


FIGURE 34. MAXIMUM PRINCIPAL STRESS - MACH-10 BASE

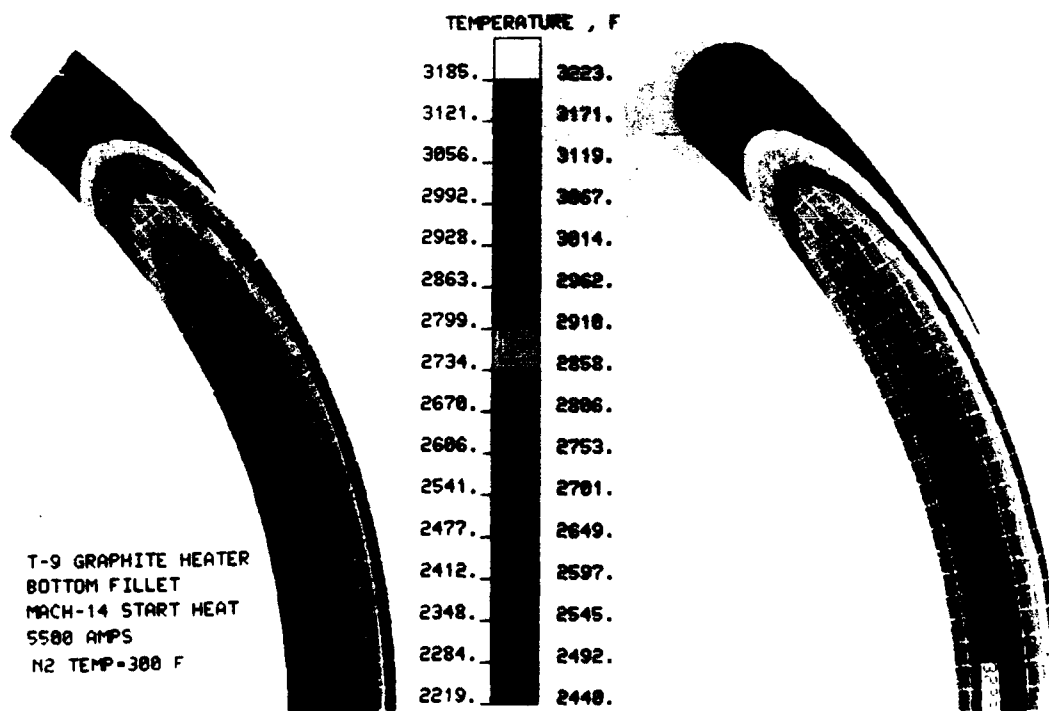


FIGURE 35. TEMPERATURE IN SQUARE AND ROUNDED CORNER HEATER LEG

J HEATER, TOP FILLET
HYDROSTATIC PRESSURE = 750 PSI
613 KWATTS @ START HEAT
FINITE ELEMENT #263

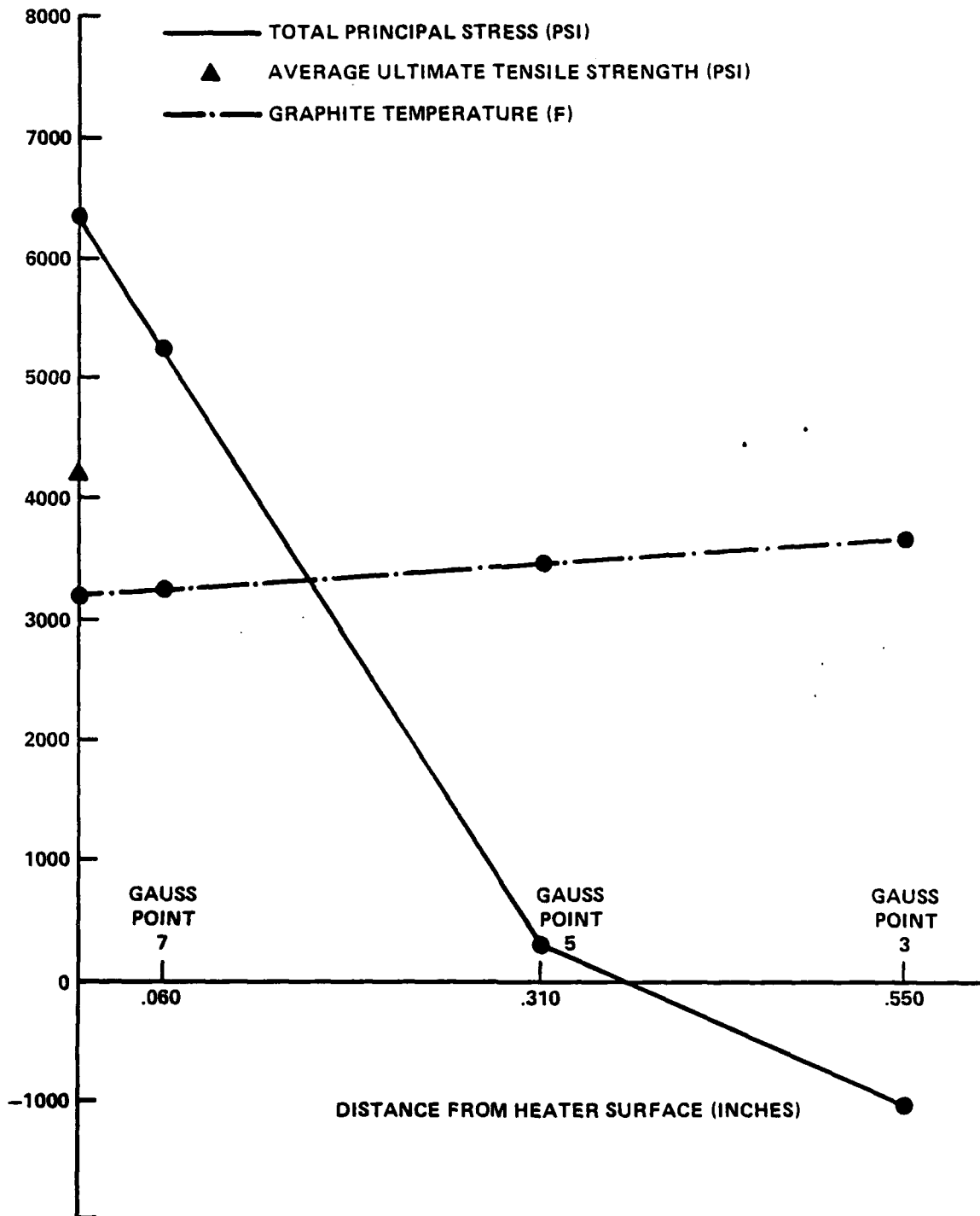


FIGURE 36. TOTAL PRINCIPAL STRESS AND TEMPERATURE PROFILES EXTRAPOLATED TO HEATER SURFACE. TOP FILLET LOCATION

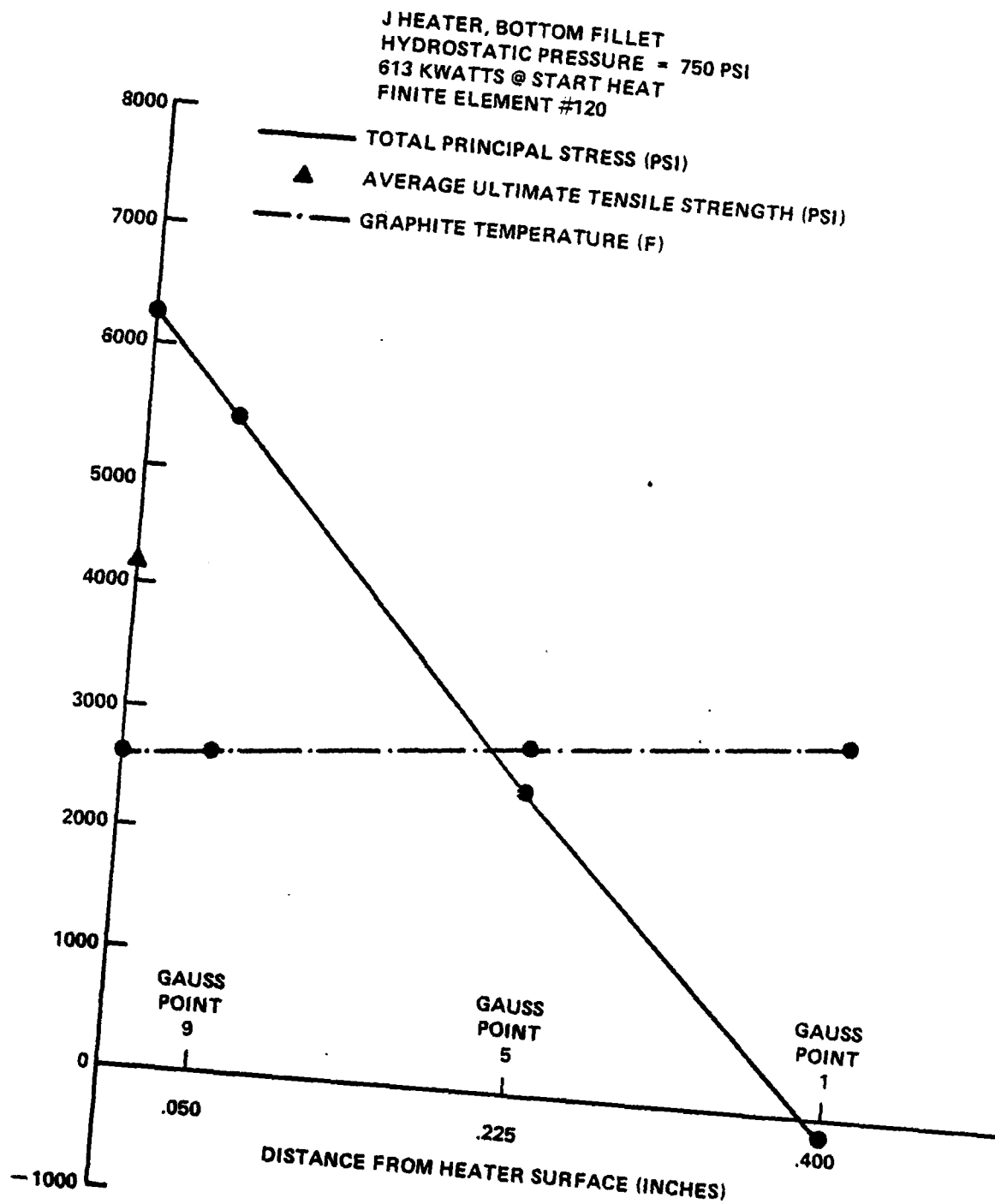


FIGURE 37. TOTAL PRINCIPAL STRESS AND TEMPERATURE PROFILES EXTRAPOLATED TO HEATER SURFACE. BOTTOM FILLET LOCATION

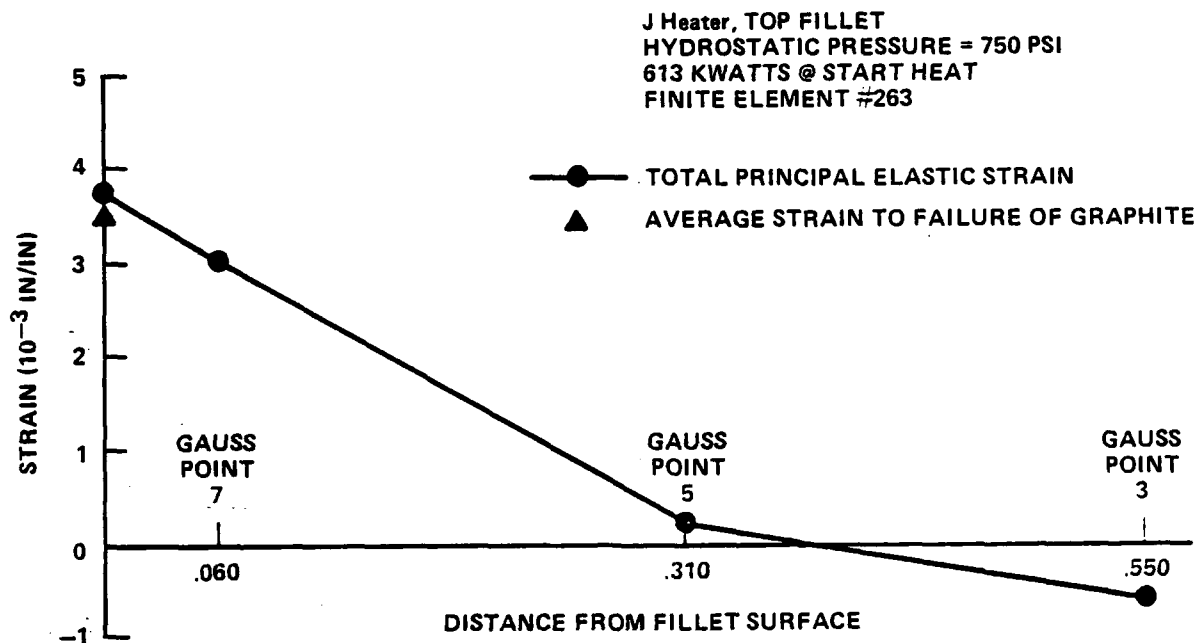


FIGURE 38. TOTAL PRINCIPAL ELASTIC STRAIN PROFILE EXTRAPOLATED TO HEATER SURFACE, TOP FILLET LOCATION

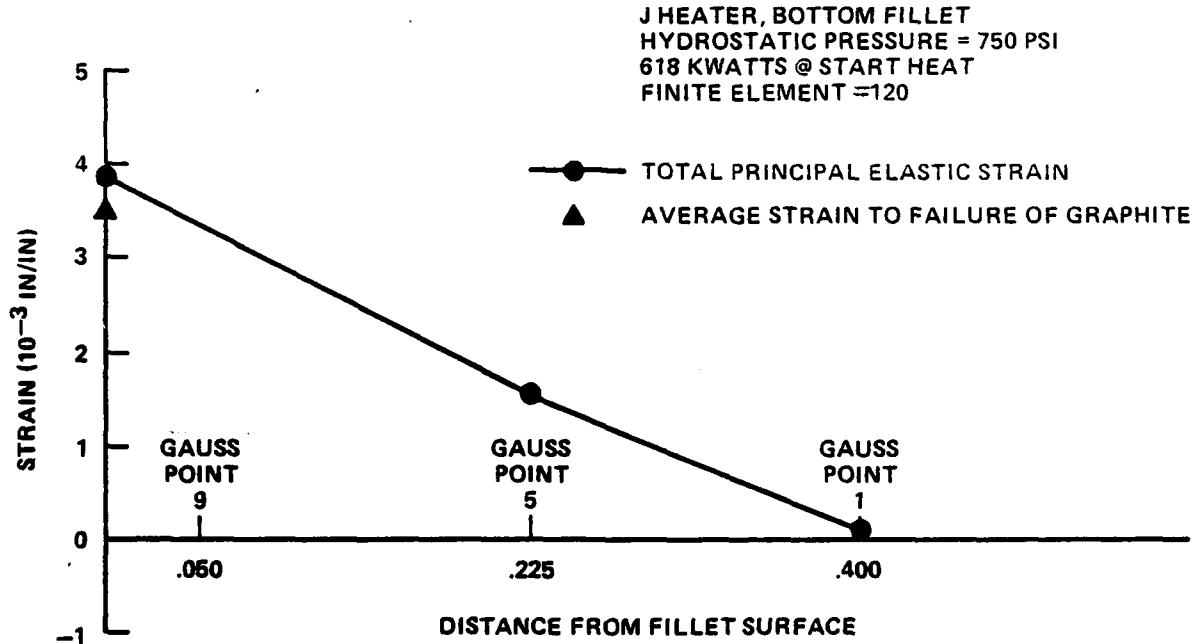


FIGURE 39. TOTAL PRINCIPAL ELASTIC STRAIN PROFILE EXTRAPOLATED TO HEATER SURFACE, BOTTOM FILLET LOCATION

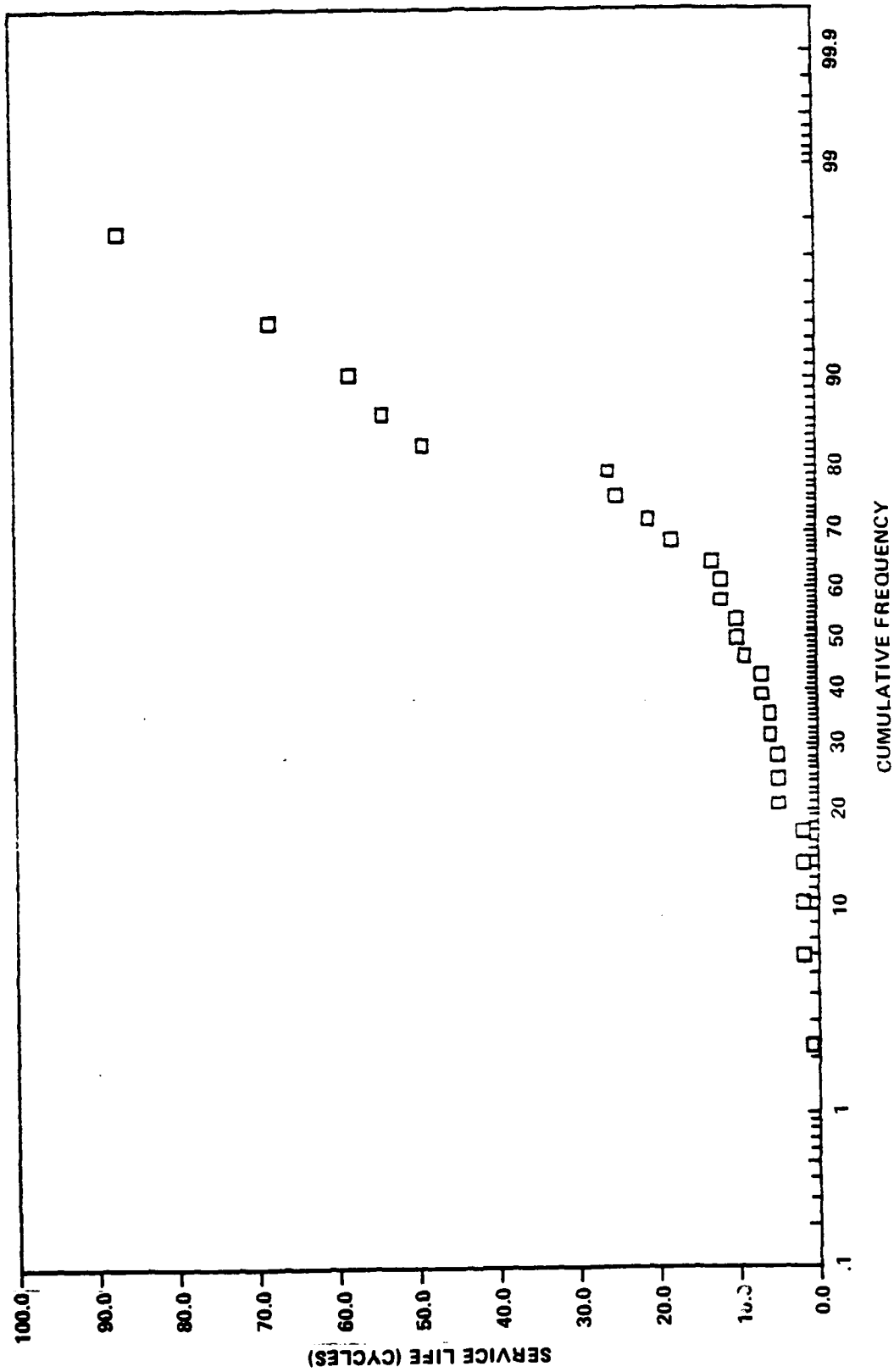


FIGURE 40. GRAPHITE HEATER SERVICE LIFE IN TUNNEL RUNS VS. CUMULATIVE FREQUENCY

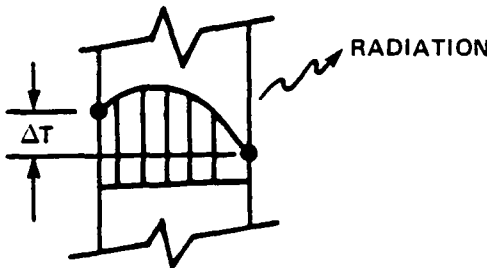
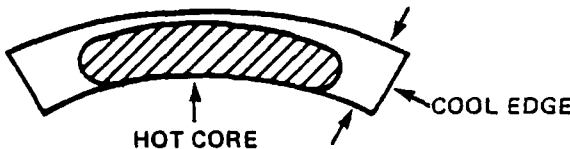
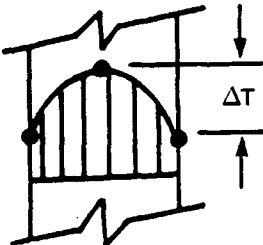
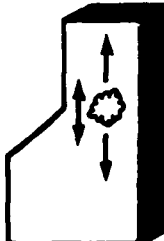
<u>EFFECT</u>		<u>AMOUNT</u> PSI / %
● DIFFERENTIAL RADIATION		2917 / 42
● EDGE COOLING		2186 / 31
● THICKNESS COOLING		1169 / 17
● BEAM BENDING (CLAMPED BASE)		437 / 6
● HOT SPOT @ FILLET		291 / 4 7000 / 100%

FIGURE 41. BREAKDOWN OF THERMAL STRESS AT BOTTOM FILLET

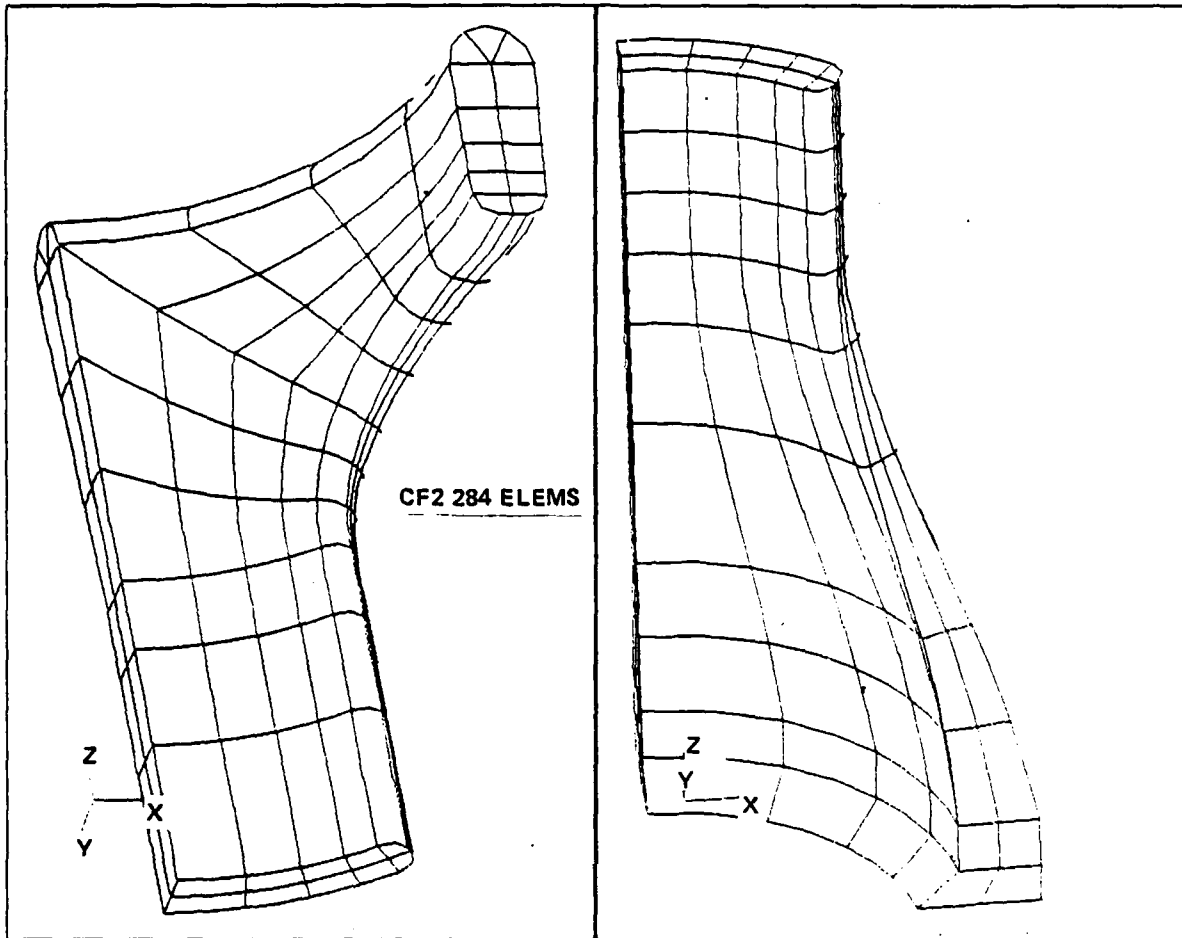


FIGURE 42. FINITE ELEMENT MODEL WITH SLOT EDGES ROUNDED TO REDUCE FILLET STRESSES

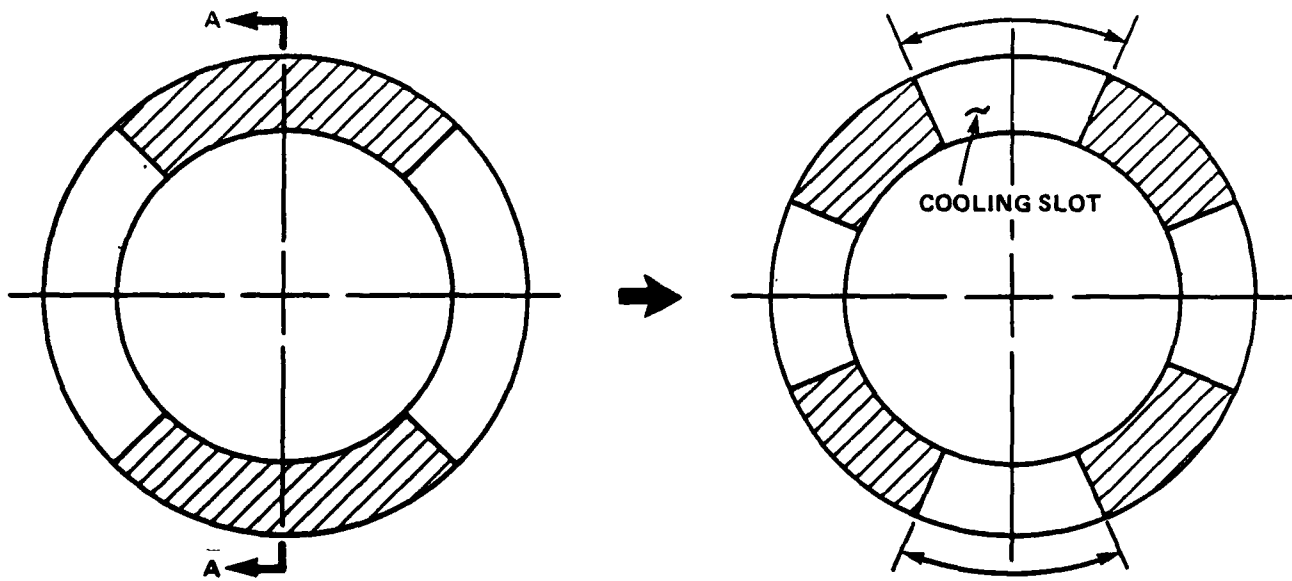


FIGURE 43. COOLING SLOTS FORMED IN HEATER LEGS BY SECTIONING AT AA AND SEPARATING HALVES

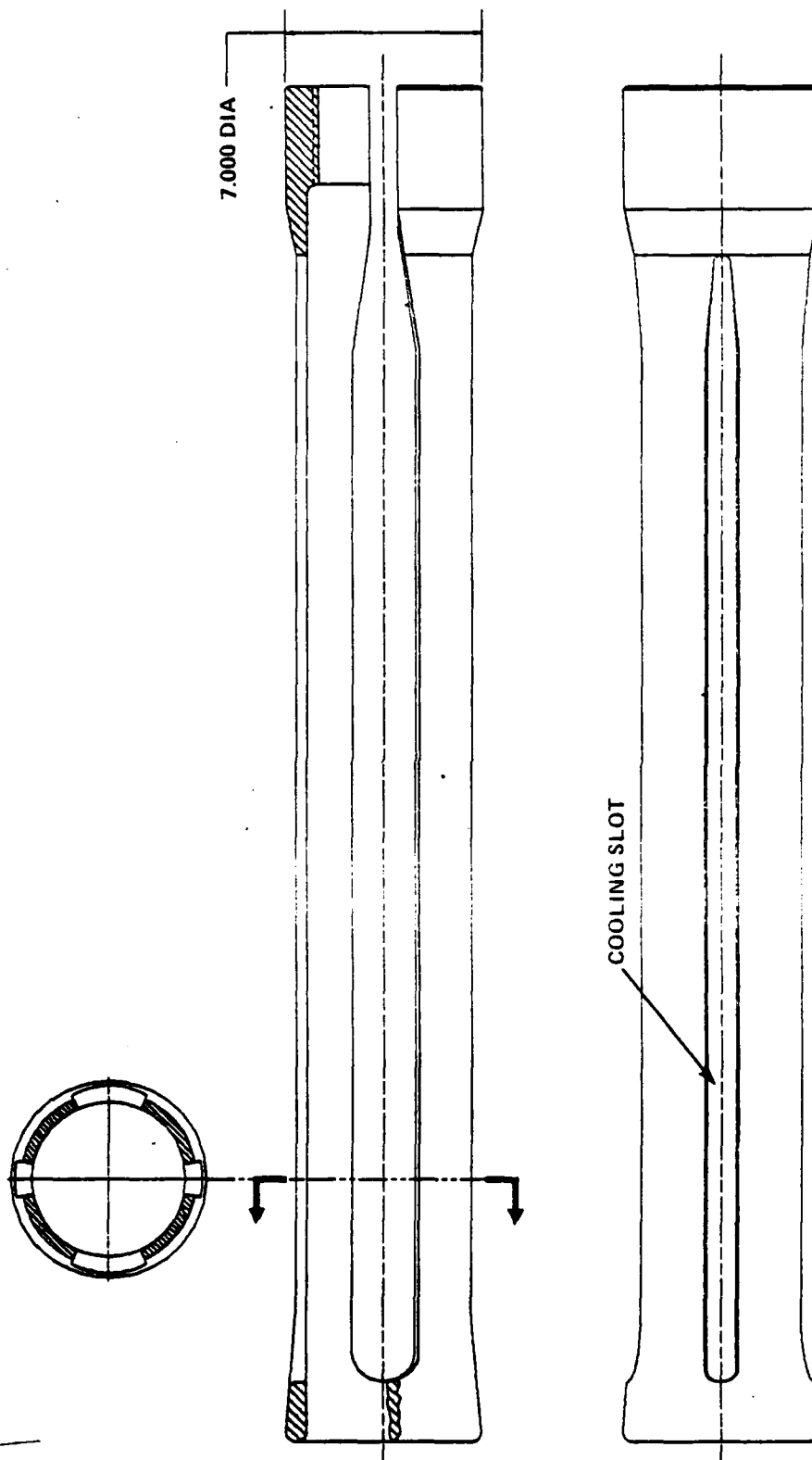


FIGURE 44. CONCEPT FOR HEATER ELEMENT WITH COOLING SLOTS

TABLE 1. HEATER ELEMENT SERVICE LIFE HISTORY FOR 1985 AND 1986

<u>ELEMENT LIFE</u> (TUNNEL RUNS)					
<u>1985 FAILURES</u>			<u>1986 FAILURES</u>		
2	10	5	54	5	9
6	25	12	2	2	18
12	7	7	2	49	87
58	6	13			
1/2	10	5			
68	26	21			
	↓			↓	
18 ELEMENTS, 294 RUNS			9 ELEMENTS, 228 RUNS		
AVERAGE RUNS PER ELEMENT = 19.3					
AVERAGE ELEMENTS PER YEAR ≈ 13.5					

TABLE 2. SUMMARY OF HEATER ANALYSIS STEPS

ANALYSIS STEP	ACTION	PROGRAM/INPUT	OUTPUT
1	● CREATE FINITE ELEMENT MODEL ● SOLVE ELECTRICAL PROBLEM ● VERIFY CORRECT CURRENT ● VERIFY TOTAL HEATER POWER ● CREATE RESISTANCE HEATING FILE	PATRAN ABAQUS CURRENT/.FIL POWER/.FIL I2RFIL/.FIL	2D OR 3D F.E. MODEL ABAQUS X. FIL RESULTS FILE - FOR054.DAT DATA FILE FOR032.DAT VOLUMETRIC HEATING DATA FILE
2	● SOLVE FOR TEMPERATURES IN HEATER	ABAQUS/FOR032.DAT/ DFLUX. FOR	ABAQUS.FIL FILE CONTAINING TEMPERATURES
3	● SOLVE FOR THERMAL STRESSES IN HEATER	ABAQUS/.FIL FILE FROM STEP 2	ABAQUS.FIL FILE CONTAINING THERMAL STRESS/STRAIN

TABLE 3. HEAT TRANSFER INPUT DATA

MACH 14

CONFIG.	REGION	RADIATION/CONVECTION SINK TEMPS		PRESCRIBED TEMP °F	START HEAT		END HEAT		START HEAT		END HEAT	
		START HEAT	R/C		R/C	R/C	R/C	°F	BTU/FT ² ·HR·R $\frac{1}{h}$	EMISSIVITY	BTU/FT ² ·HR·R $\frac{1}{h}$	EMISSIVITY
J/K	WETTED O.D.	300/300	R/C	3100/3100	300/300	3100/3100	3100/3100	—	88.5	.85	117	.85
J/K	WETTED I.D.	—/300	—/300	—/3100	—/300	—/3100	—/3100	—	88.5	—	117	—
J/K	WETTED SLOT EDGES	300/300	300/300	3100/3100	300/300	3100/3100	3100/3100	—	88.5	.85	117	.85
J/K	RADIUS CROWN	300/300	300/300	3100/3100	300/300	3100/3100	3100/3100	—	88.5	.85	117	.85
J	THREADED BASE OD & ID	—/—	—/—	300*	—/—	—/—	—/—	300*	—	—	—	—
BASE	WETTED O.D.	500/500	500/500	—	500/500	—	—	—	100.0	.85	—	—
	WETTED TOP SURFACE	500/500	500/500	—	500/500	—	—	—	100.0	.85	—	—
	WETTED BOTTOM SURFACE	500/500	500/500	—	500/500	—	—	—	80.0	.85	—	—
	WETTED FLAT	—/500	—/500	—	—/500	—	—	—	100.0	.85	—	—
	THREADED HEATER BASE:	—/500	—/500	—	—/500	—	—	—	25.0	—	—	—
	— OD SURFACE	—/500	—/500	—	—/500	—	—	—	25.0	—	—	—
	— MATCHING BASE SURFACE	—/500	—/500	—	—/500	—	—	—	—	—	—	—
	THREADED HEATER BASE:	—/500	—/500	—	—/500	—	—	—	25.0	—	—	—
	— BOTTOM SURFACE	—/500	—/500	—	—/500	—	—	—	25.0	—	—	—
	— MATCHING BASE SURFACE	—/500	—/500	—	—/500	—	—	—	25.0	—	—	—
J/K	J/K HEATER OD	500/500	500/500	—	500/500	—	—	—	100.0	.85	—	—
	J/K HEATER ID	500/500	500/500	—	500/500	—	—	—	100.0	—	—	—
	J/K HEATER SLOT EDGE	500/500	500/500	—	500/500	—	—	—	100.0	.85	—	—

*FOR 913 KWATT CASE THESE SURFACES TREATED SAME AS WETTED O.D. & I.D. OF HEATER LEGS.

TABLE 4. PEAK THERMAL STRESS-STRAIN STATES IN GRAPHITE HEATER

FILLET	ELEM/GS. RT.	HEAT PERIOD	STRESS/TOTAL STRAIN/ELASTIC STRAIN COMPONENTS (PSI) (IN/IN)						MAX PRINCIPAL		TEMP (F)
			XX	YY	ZZ	XY	XZ	YZ	STRESS (PSI)	TILT ANGLE (FROM ZZ) (DEGREES)	
TOP	263/7	START	-152 1.024E-02 -5.591E-04	642 1.077E-02 -2.932E-05	5471 1.399E-02 3.193E-03	-192 -2.559E-04 -2.559E-04	385 5.138E-04 5.138E-04	-1273 -1.699E-03 -1.699E-03	5815	14.5	3221
			319 8.455E-03 -2.964E-04	168 8.351E-03 -4.001E-04	6021 1.239E-02 3.634E-03	-194 -2.672E-04 -2.672E-04	-244 -3.36E-04 -3.36E-04	592 8.165E-04 8.165E-04	6092	6.3	2669
TOP	263/7	END	-118 1.403E-02 -5.375E-04	827 1.465E-02 8.886E-05	5317 1.763E-02 3.064E-03	-250 -3.320E-04 -3.320E-04	397 5.26E-04 5.26E-04	-1684 -2.232E-03 -2.232E-03	5913	9.0	4192
BOTTOM	119/7	END	44.8 1.265E-02 -4.760E-04	478 1.293E-02 -1.918E-04	6169 1.667E-02 3.545E-03	-215 -2.828E-04 -2.828E-04	-384 -5.037E-04 -5.037E-04	793 1.041E-03 1.041E-03	6304	8.8	3829

TABLE 5. PROBABILITY OF FAILURE FOR GRAPHITE HEATERS

HEATER CONFIG.	HEATER POWER (KWATTS)	HEATING PERIOD	FILLET LOCATION	PRINCIPAL STRESS STRAIN	HYDRO-STATIC STRESS STRAIN	TOTAL PRINCIPAL STRESS STRAIN	P.O.F. %
J	613	START	TOP TOP	7000 PSI .00407 IN/IN	750 .000326	6250 .00375	100 65
J/K	613	START	BOTTOM BOTTOM	7000 PSI .00419 IN/IN	750 .000326	6250 .00387	100 75
J*	913	START	TOP TOP	8615 PSI .00500 IN/IN	750 .000326	7865 .00468	100 100

*ESTIMATED DATA BASED ON A SIMILAR END HEAT ANALYSIS

REFERENCES

1. Southern Research Institute, Evaluation and Comparison of Graphite Heater Tube Materials Used in the Hypervelocity Wind Tunnel, SoRI-EAS-86-508-5787-I-F, Southern Research Institute, Birmingham, AL, Jul 1986.
2. ABAQUS (Version 4-5), Hibbitt, Karlsson, and Sorensen, Inc., Providence, RI, Jul 1985.
3. PATRAN, PDA Engineering, Santa Ana, CA, Dec 1985.
4. Schneider, P. J., Conduction Heat Transfer, Addison-Wesley Publishing Company, Inc., Reading Massachusetts, pp 338, 1955.
5. Juvinall, R. C., Stress, Strain, and Strength, McGraw-Hill Book Co., Inc., New York, NY, 1967.
6. Dieter, G. E., Mechanical Metallurgy, Second Edition, McGraw-Hill Book Co., Inc., NewYork, NY, 1976.
7. Buch, J. D., Crose, J. G., and Robinson, E. Y., Failure Criteria in Graphite Program, AFML-TR-77-16, Air Force Materials Laboratory, Wright Patterson Airforce Base, OH, Mar 1977.

APPENDIX A
ANALYSES SUPPORT PROGRAMS

PROGRAM CURRENT

```

C   PROGRAM TO COMPUTE TOTAL CURRENT IN ABAQUS
C   HEATER MODEL BY SUMMING REACTION FLUXES FROM
C   ABAQUS THERMAL ANALYSIS RESULTS. USER MUST SUPPLY
C   NODES IN THE DATA STATEMENT WHICH DEFINE CROSS-
C   SECTION FOR WHICH TOTAL CURRENT IS DESIRED.
C   USER MUST UPDATE NODEN AND IMPLIED DO LIMIT BELOW.
C   BEFORE RUNNING ASSIGN THE XXX.FIL FILE
C   TO FORTRAN UNIT FOR008. ONLY NODES FOR WHICH TEMPERATURES
C   HAVE BEEN PRESCRIBED CAN BE SPECIFIED.

```

```

IMPLICIT REAL*8(A-H,O-Z)
DOUBLE PRECISION ARRAY
DIMENSION ARRAY(513), JRRAY(2,513), NSET(500)
EQUIVALENCE (ARRAY(1), JRRAY(1,1))
CALL INITF

```

```

NODEN=29
RFLUX=0.0

```

```

C   DATA (NSET(L),L=1,29) /
1 109, 110, 111, 112, 113, 114,
2 115, 116, 117, 118, 119, 120,
3 382, 383, 384, 385,
4 386, 387, 388, 389, 390, 391,
5 392, 393, 394, 395, 396, 397, 398/

```

```

C   K=1
DO WHILE (K.LE.999999)
  CALL DBFILE (0,ARRAY,JRCD)
  IF (JRCD.NE.0) GO TO 100
  KEY= JRRAY(1,2)
  IF (KEY.EQ.214) THEN
    M=1
    DO WHILE (M.LE.NODEN)
      IF (NSET(M).EQ.JRRAY(1,3)) THEN
        RFLUX=RFLUX+ARRAY(4)
      END IF
      M=M+1
    END DO
  END IF
  K=K+1
END DO
100 CURENT= RFLUX*2.0
WRITE (6,2000) CURENT
2000 FORMAT(10X,24H TOTAL HEATER CURRENT = F10.3,1X,7HAMPERES)
STOP
END

```

PROGRAM I2RFIL

```

C      PROGRAM TO READ FLUXES AT MAT'L CALCULATION
C      POINTS (=GAUSS PTS FOR DC3D20) FROM ABAQUS
C      GENERATED XXX.FIL FILE AND CONVERT FLUXES TO
C      ELECTRICAL RESISTANCE (I2R) HEATING VALUES. PROGRAM
C      WRITES HEATING VALUES TO FILE UNIT 032. BEFORE
C      RUNNING ASSIGN THE XXX.FIL FILE TO FORTRAN UNIT
C      FOR008. PROGRAM ASSUMES FLUXES ARE CURRENT
C      DENSITIES.

```

```

      IMPLICIT REAL*8(A-H,O-Z)
      DOUBLE PRECISION ARRAY
      DIMENSION ARRAY(513), JRRAY(2,513)
      EQUIVALENCE (ARRAY(1) , JRRAY(1,1))
      CALL INITF

```

```

C***** SPECIFY MATERIAL ELECTRICAL CONDUCTIVITY, SIGMA
C***** FOR BODY FLUX UNITS OF BTU/SEC-CU.IN.
C***** USE SIGMA UNITS OF (OHM-IN)**-1

```

```

C      SIGMA=2032.0

      DO 100 K = 1 , 99999
        CALL DBFILE(0,ARRAY,JRCD)
        IF(JRCD.NE.0) GO TO 110
        KEY=JRRAY(1,2)
        IF(KEY.EQ.1) GO TO 10
        IF(KEY.EQ.28) GO TO 20
        GO TO 100
      10 CONTINUE
        JEL=JRRAY(1,3)
        JPNT=JRRAY(1,4)
        GO TO 100
      20 CONTINUE
        RBFLUX=ARRAY(3)*ARRAY(3)/SIGMA

```

```

C      C***** CONVERSION FOR BODY FLUX UNITS OF B.T.U./SEC-CU.IN.
      RBFLUX=RBFLUX*0.000948451

```

```

      WRITE(32,120) JEL,JPNT,RBFLUX
      120 FORMAT(2I5,E10.3)
      100 CONTINUE
      110 CONTINUE
      ENDFILE 32
      STOP
      END

```

```
SUBROUTINE DFLUX (FLUX,TEMP,KSTEP,KINC,TIME,NOEL,NPT,COORDS,JLTYP)
IMPLICIT DOUBLE PRECISION (A-H,O-Z)
DIMENSION COORDS(3), RBFLUX(1000,27)
DATA KSET/0/
C*****
C***** FLUXES ARE READ FROM FILE 32 AND LOADED
C***** INTO LOOK-UP TABLE RBFLUX ON FIRST CALL
C***** OF THIS SUBROUTINE
C*****
      IF (KSET.EQ.0) THEN
        DO 20 I=1,30000
          READ(32,1000,END=30) NNOEL,NNPT,BFLUX
1000      FORMAT(2I5,E10.3)
          RBFLUX(NNOEL,NNPT)=BFLUX
20      CONTINUE
30      KSET=1
      END IF
C*****
C***** DEFINE FLUX
C*****
      FLUX=RBFLUX(NOEL,NPT)
      RETURN
      END
```

PROGRAM POWER

```

* TO RUN THIS PROGRAM YOU MUST:
*   (1) ASSIGN A XXX.FIL FILE TO A FORTRAN FOR008 FILE
*   (2) LINK/NOMAP/EXE:POWER POWER,VAXA$DUA1:[ABAGUS]ABQ5LIB/LIB
*
* THIS PROGRAM WILL COMPUTE:
*
* THE TOTAL POWER GENERATED IN THE MODEL, TOTAL VOLUME OF THE MODEL
* AND IT WILL SHOW THE AVERAGE POWER GENERATED FROM EACH ELEMENT
*
* THE ELEMENTS MAKE UP ONE QUARTER OF THE MODEL, SO
* THE TOTAL VOLUME AND TOTAL POWER IS MULTIPLIED BY 4 IN PROGRAM
*

```

```

IMPLICIT REAL*8(A-H,O-Z)
DOUBLE PRECISION ARRAY
DIMENSION ARRAY(513),JRRAY(2,513)

```

```

*
* YOU MAY WANT TO CHANGE THE VALUES DIMENSIONED IF YOU HAVE A
* LARGER OR SMALLER MODEL

```

```

DIMENSION NODE(5000), X(5000), Y(5000), Z(5000)
DIMENSION NELE(1000),NOD1(1000),NOD2(1000),NOD3(1000),NOD4(1000)
DIMENSION NOD5(1000), NOD6(1000), NOD7(1000), NOD8(1000)
DIMENSION AVE(1000), NELA(1000), VOL(1000)

```

```

EQUIVALENCE (ARRAY(1) , JRRAY(1,1))
CALL INITF

```

```

L=0
N=0
DO 500 K = 1,99999
  CALL DBFILE(0,ARRAY,JRCD)
  IF (JRCD.NE.0) GO TO 300
  KEY = JRRAY(1,2)

```

```

*
* KEY 1901 IS USED TO OBTAIN THE COORDINATES OF EACH NODE
*

```

```

IF(KEY.EQ.1901) THEN
  N=N+1
  NODE(N) = JRRAY(1,3)
  X(N) = ARRAY(4)
  Y(N) = ARRAY(5)
  Z(N) = ARRAY(6)

```

```

*
* KEY 1900 IS USED TO OBTAIN THE NODE POINTS OF EACH ELEMENT
*

```

```
ELSE IF (KEY.EQ.1900) THEN
```

```
  L=L+1
```

```
  NELE(L) = JRRAY(1,3)
```

```
  NOD1(L) = JRRAY(1,5)
```

```
  NOD2(L) = JRRAY(1,6)
```

```
  NOD3(L) = JRRAY(1,7)
```

```
  NOD4(L) = JRRAY(1,8)
```

```
  NOD5(L) = JRRAY(1,9)
```

```
  NOD6(L) = JRRAY(1,10)
```

```
  NOD7(L) = JRRAY(1,11)
```

```
  NOD8(L) = JRRAY(1,12)
```

```
ELSE
```

```
  T=2
```

```
END IF
```

```
500 CONTINUE
```

```
600 TOTVOL = 0
```

```
  DO 900 I = 1,L
```

```
    LEVEL = 0
```

```
    DO 800 J = 1,N
```

```
      IF(LEVEL.EQ.9) GO TO 850
```

```
* IF-THEN LOOP CHECKS AND GETS THE COORDINATES FOR THE 8 NODE POINTS
* FOR EACH ELEMENT, THESE COORDINATES ARE LATER USED TO FIND VOLUME
```

```
      IF (NODE(J).EQ.NOD1(I)) THEN
```

```
        LEVEL=LEVEL+1
```

```
        PA =J
```

```
      END IF
```

```
      IF (NODE(J).EQ.NOD2(I)) THEN
```

```
        LEVEL = LEVEL + 1
```

```
        PB =J
```

```
      END IF
```

```
      IF (NODE(J).EQ.NOD3(I)) THEN
```

```
        LEVEL = LEVEL + 1
```

```
        PC =J
```

```
      END IF
```

```
      IF (NODE(J).EQ.NOD4(I)) THEN
```

```
        LEVEL = LEVEL + 1
```

```
        PD =J
```

```
      END IF
```

```
      IF (NODE(J).EQ.NOD5(I)) THEN
```

```
        LEVEL = LEVEL + 1
```

```
        PE =J
```

```
      END IF
```

```
      IF (NODE(J).EQ.NOD6(I)) THEN
```

```
        LEVEL = LEVEL + 1
```

```
        PF =J
```

```
      END IF
```

```
      IF (NODE(J).EQ.NOD7(I)) THEN
```

```
        LEVEL = LEVEL + 1
```

```
        PG =J
```

```
      END IF
```

```
      IF (NODE(J).EQ.NOD8(I)) THEN
```

```
        LEVEL = LEVEL + 1
```

```
        PH =J
```

```
      END IF
```

```
800
```

```
CONTINUE
```

* THE FOLLOWING CALCULATION WILL DETERMINE THE VOL OF EACH ELEMENT

```

850    AJ1=-X(PA)-X(PB)+X(PC)+X(PD)-X(PE)-X(PF)+X(PG)+X(PH)
      AJ4=-X(PA)-X(PB)-X(PC)-X(PD)+X(PE)+X(PF)+X(PG)+X(PH)
      AJ7=-X(PA)+X(PB)+X(PC)-X(PD)-X(PE)+X(PF)+X(PG)-X(PH)
      AJ2=-Y(PA)-Y(PB)+Y(PC)+Y(PD)-Y(PE)-Y(PF)+Y(PG)+Y(PH)
      AJ5=-Y(PA)-Y(PB)-Y(PC)-Y(PD)+Y(PE)+Y(PF)+Y(PG)+Y(PH)
      AJ8=-Y(PA)+Y(PB)+Y(PC)-Y(PD)-Y(PE)+Y(PF)+Y(PG)-Y(PH)
      AJ3=-Z(PA)-Z(PB)+Z(PC)+Z(PD)-Z(PE)-Z(PF)+Z(PG)+Z(PH)
      AJ6=-Z(PA)-Z(PB)-Z(PC)-Z(PD)+Z(PE)+Z(PF)+Z(PG)+Z(PH)
      AJ9=-Z(PA)+Z(PB)+Z(PC)-Z(PD)-Z(PE)+Z(PF)+Z(PG)-Z(PH)

      VOLA=AJ1*AJ5*AJ9+AJ2*AJ6*AJ7+AJ3*AJ4*AJ8-AJ3*AJ5*AJ7
      VOLB=-AJ2*AJ4*AJ9-AJ1*AJ6*AJ8
      VOL(I) = 0.0156250*(VOLA+VOLB)
      TOTVOL = TOTVOL + VOL(I)
900 CONTINUE
      TOTVOL = 4*TOTVOL

```

* THIS PART OF THE PROGRAM IS USED TO OBTAIN THE AVERAGE FLUX
 * FOR EACH ELEMENT
 *

```

      SUM = 0
      NUMB = 1
      KB = 0
      DO 2000 KA = 1,99999
        IF(NUMB.LE.27) THEN
          READ(32,1500,END=2100) NEL,NPNT,FLUX
1500      FORMAT(215,E10.3)
          SUM = SUM + FLUX
          NUMB = NUMB + 1
        ELSE
          KB = KB + 1

```

* THE AVERAGE FLUX IS MULTIPLIED BY 1054.5 TO CONVERT FROM
 * BTU/SEC TO WATTS

```

      AVE(KB) =(SUM/27)*1054.5
      NELA(KB) = NEL
      SUM = 0
      NUMB = 1
      END IF
2000 CONTINUE

```

```

2100 TOTPOW = 0

```

* THIS PORTION OF THE PROGRAM IS USED TO WRITE OUT ALL THE PERTINENT
 * INFORMATION TO FILE FOR054.DAT
 * ALSO THE TOTAL POWER IS SUMMED UP BELOW
 *

```

      WRITE(54,2150)
2150  FORMAT(1H1,8X,33HTUNNEL-9 GRAPHITE HEATER ELEMENT /)
      WRITE(54,2200)
2200  FORMAT(1X,6X,37HELECTRICAL RESISTANCE HEAT GENERATION////)
      WRITE(54,2250)
2250  FORMAT(1X,7HELEMENT,5X,6HVOLUME,7X,8HAVE FLUX,7X,10HAVE POWER /)
      WRITE(54,2300)
2300  FORMAT(1X,10X,11H(CUBIC IN.),4X,11H(WATT/IN^3),6X,7H(WATTS)/)

      DO 2750 IEL = 1 , L
          POW = VOL(IEL) * AVE(IEL)
          WRITE(54,2500)NELE(IEL),VOL(IEL),AVE(IEL),POW
2500    FORMAT(17,4X,3(E10.3,5X))
          TOTPOW = TOTPOW + POW
2750  CONTINUE

      TOTPOW = 4*TOTPOW

      WRITE(54,2800)
2800  FORMAT(1X///1X,2X,11HTOTAL POWER,12X,13HTOTAL VOLUME /)
      WRITE(54,2900) TOTPOW,TOTVOL
2900  FORMAT(E10.3,1X,5HWATTS,7X,E10.3,1X,9HCUBIC IN.)
3000  END FILE 54
      STOP
      END

```

APPENDIX B
ABAQUS INPUT FILES

ABAQUS THERMAL/ELECTRIC ANALOGUE INPUT FILE
REV-J HEATER
653 KWATTS

*BOUNDARY
INBASE,11,,57.748
LIGA,11,,0.0
*MATERIAL
*CONDUCTIVITY, TYPE=ISO
** UNITS ARE (OHM-IN)**-1
2032.0
*RESTART,WRITE
*STEP, LINEAR
*HEAT TRANSFER, STEADY STATE
*NODE PRINT
2,,,2,2,,2
*EL FILE, TEMPS, HEAT FLUX, COORDS,LOADS
*NODE FILE
2,,,2,2,,2
*END STEP

ABAQUS THERMAL ANALYSIS INPUT FILE
 REV-J GRAPHITE HEATER
 END HEAT

*MATERIAL
 *CONDUCTIVITY, TYPE=ISO
 ** UNITS=BTU/IN-SEC-F
 9.745E-4, 70.0
 7.731E-4, 500.0
 5.763E-4, 1000.0
 4.537E-4, 1500.0
 3.773E-4, 2000.0
 3.356E-4, 2500.0
 3.055E-4, 3000.0
 2.870E-4, 3500.0
 2.685E-4, 4000.0
 2.523E-4, 4500.0
 2.291E-4, 5000.0
 *RESTART,WRITE
 *STEP, CYCLE=100
 *HEAT TRANSFER, STEADY STATE, TEMTOL=10
 *RADIATE, ZERO=-460.0
 ** EMISSIVITY=.85, STEFAN-BOLTZMAN =
 ** 3.303E-15 BTU/SQ.IN.-SEC-F**4
 CUTOUT,R5,3100.0,2.807E-15
 CROWN,R4,3100.0,2.807E-15
 ODDOUT,R6,3100.0,2.807E-15
 *FILM
 ** UNITS = BTU/SEC-SQ.IN.-F
 CUTOUT,F5, 3100.0, 2.272E-04
 CROWN,F4, 3100.0, 2.272E-04
 ODDOUT,F6, 3100.0, 2.272E-04
 EVENIN,F4, 3100.0, 2.272E-04
 *DFLUX
 ALL,BFNU
 *EL PRINT, TEMPS, HEAT FLUX, COORDS,LOADS
 *NODE PRINT
 2,,,2,2,,2
 *EL FILE, TEMPS, HEAT FLUX, COORDS,LOADS
 *NODE FILE
 2,,,2,2,,2
 *END STEP

ABAQUS STRESS ANALYSIS INPUT FILE
CLAMPED BASE
REV-J GRAPHITE HEATER

*MATERIAL

*ELASTIC, TYPE=ISOTROPIC

1.31E+06, 0.13, 70.0

1.34E+06, 0.13, 932.0

1.50E+06, 0.13, 1832.0

1.65E+06, 0.13, 2732.0

1.73E+06, 0.13, 3632.0

1.69E+06, 0.13, 4532.0

1.62E+06, 0.13, 5432.0

*EXPANSION, ZERO=70.0, TYPE=ISO

** MEAN COEFF'S OF EXPANSION. REF STRESS-FREE TEMP=70.0 F

1.75E-06, 70.0

3.30E-06, 2500.0

3.60E-06, 5000.0

*BOUNDARY

XZERO,2,,0.0

LIGA,2,,0.0

INBASE,1,,0.0

INBASE,3,,0.0

OUTBAS,1,,0.0

OUTBAS,3,,0.0

*RESTART,WRITE

*STEP, LINEAR

*STATIC

*TEMPERATURE, FILE=15, BSTEP=1(INC=1), ESTEP=1(INC=1)

*NODE PRINT

2,,,1,1

*EL FILE, TEMPS, COORDS

2,2

2

2,2,1,2

*NODE FILE

2,,,,,2,2

*END STEP

APPENDIX C

FREE CONVECTION HEAT TRANSFER FILM COEFFICIENT
CALCULATION FOR MACH-14 END HEAT CONDITIONS

Heater Gas Conditions: Gas = Nitrogen
 Pressure = 22,000 psi = 1496 atm
 Temp. = 3100°F (=3560°R = 1977°K)

First compute Grashof Number to determine whether laminar or turbulent conditions apply:

$$Gr = g(T_s - T_g) \beta L^3 (\rho/u)^2$$

where:

T_s = Heater Surface Temperature = 5000°F (=5460°R = 3033°K)
 T_g = Nitrogen Gas Temperature
 β = Coefficient of Expansion = $1/T_g = 1/3560^\circ R$
 g = gravity constant = 32 ft/sec/sec
 L = vertical distance from Heater Element Base
 ρ = Nitrogen Density @ T_{ave}
 u = Viscosity of Nitrogen @ T_{ave}
 T_{ave} = Average Film Temperature = $(T_g + T_s)/2 = 2505^\circ K = 4510^\circ R$

Compute density and viscosity of nitrogen gas:

$$\rho \Big|_{T_{ave}} = 11 \text{ lb/cu ft (at 22,000 psi from nitrogen table)}$$

$$u \Big|_{T_{ave}} = 6.111 \times 10^{-5} \text{ lbm/sec-ft}$$

Compute Grashof Number:

$$Gr = (32 \text{ ft/sec}^2) \frac{(5460 - 3560)}{3560^\circ R} (4 \text{ ft})^3 \left(\frac{11 \text{ lb/cu ft}}{(6.111 \times 10^{-5} \text{ lbm/sec-ft})} \right)^2$$

$$Gr = 3.686 \text{ E13}$$

The following criteria apply:

Laminar Convection: $Gr < 1.0 \text{ E+09}$
 Turbulent Convection: $Gr \geq 1.0 \text{ E+09}$

It turns out that the flow is laminar for only an inch or so from the heater element base, so turbulent flow is assumed to exist over the full length of the heater. The average film coefficient, h , can be gotten then from Figure 7-4, Reference C-1, for vertical cylinders.

$$\bar{h} = .021 (k/L) (Gr \cdot Pr)^{0.4}$$

Where:

$\bar{h}$ = Average Film Coefficient
 k = Thermal Conductivity of gas at T_{ave}
 L = Vertical height of Heater = 4 ft
 Gr = Grashof Number
 Pr = Prandtl Number = $c_p \cdot u / k$
 c_p = Specific Heat of gas at T_{ave}

Compute conductivity and specific heat at average film temperature:

$$k \text{ (@4510 R)} = 0.0975 \text{ BTU/hr-ft-R}$$

$$c_p \quad " \quad = 0.305 \text{ BTU/lbm R}$$

Then

$$Pr = (.305)(.22)/(0.0975) = 0.689$$

Evaluate Film Coefficient:

$$\bar{h} = (.021) (0.0975) (.689 \cdot 3.686 \text{ E13})^{0.4} / 4$$

$$\bar{h} = \underline{117.8 \text{ BTU/hr-sq ft-R}}$$

REFERENCES

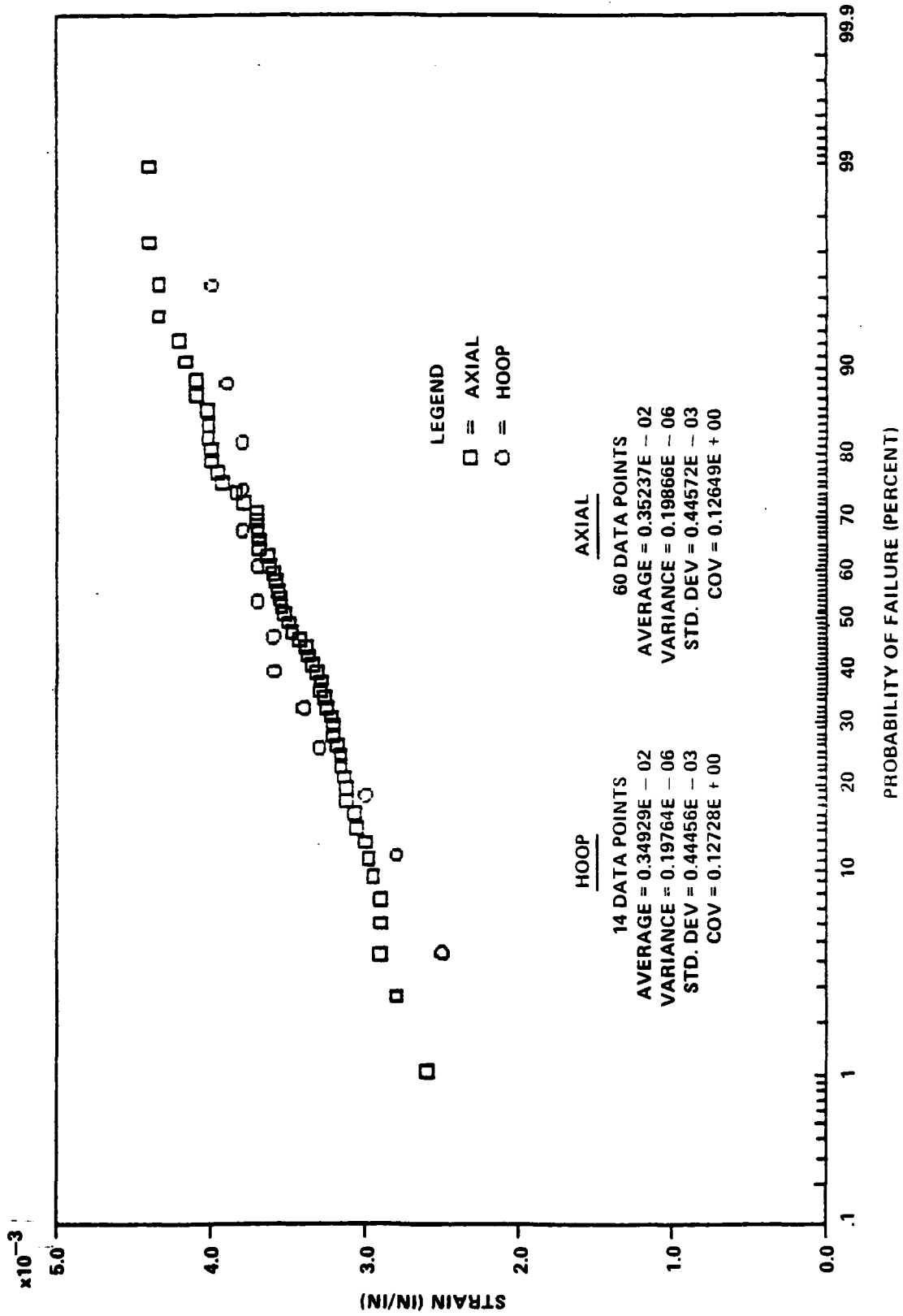
- C-1. Kreith, F., Principles of Heat Transfer, International Textbook Co., New York, NY, 1973.

APPENDIX D

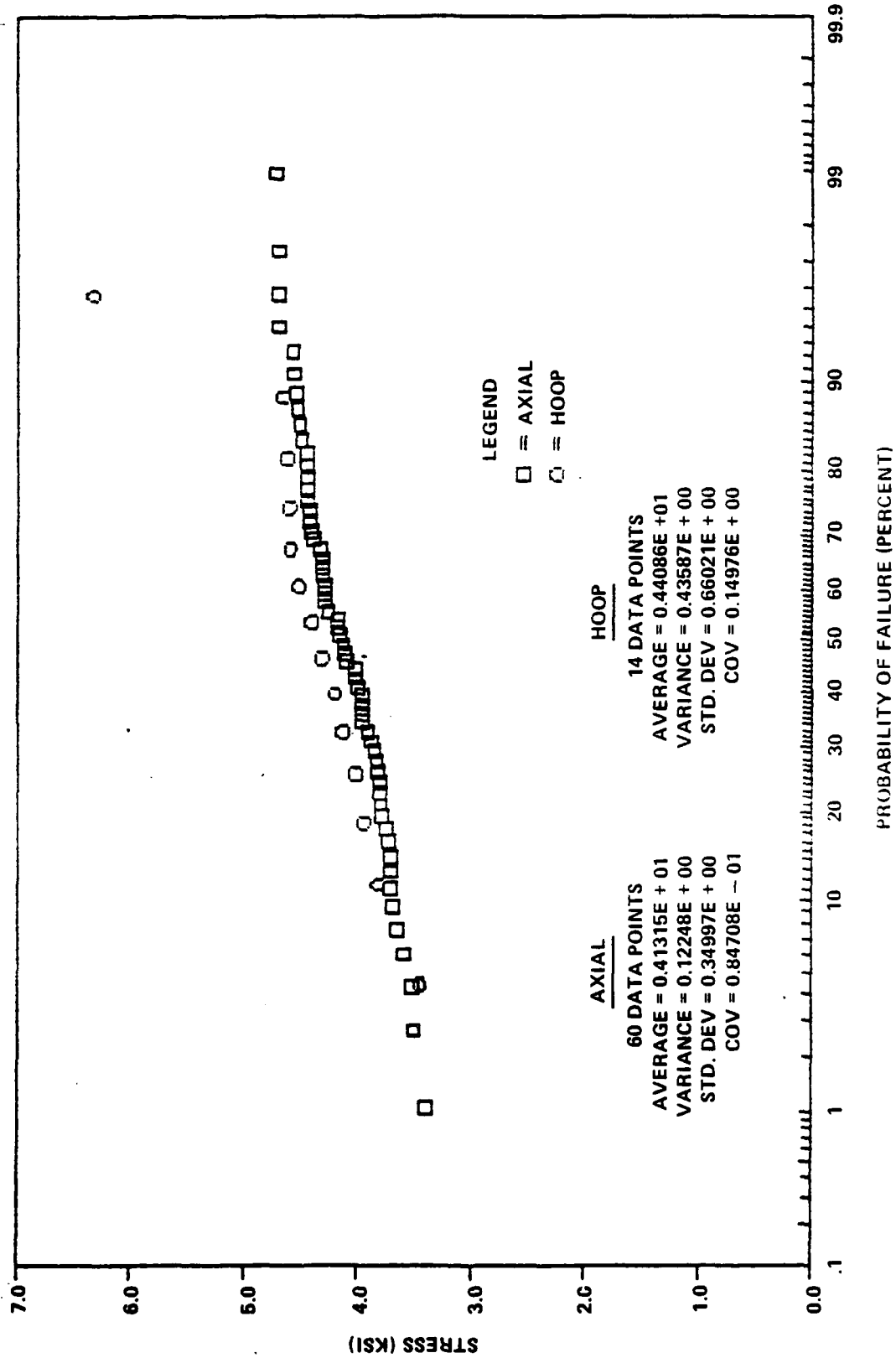
TENSILE STENGTH AND STRAIN-TO-FAILURE
EXPERIMENTAL DATA FOR HEATER GRAPHITE

The Strength Data presented here was obtained from Reference D-1 and D-2. The data are for 2020-type graphite manufactured by the Stackpole Corporation and YU60ST graphite made by Ultracarbon Corporation.

APPENDIX D. STRAIN TO FAILURE AT 2000°F



APPENDIX D. TENSILE STRENGTH AT 2000°F



REFERENCES

- D-1. Southern Research Institute, Evaluation and Comparison of Graphite Heater Tube Materials Used in the Hypervelocity Wind Tunnel, SoRI-EAS-86-508-5787-I-F, Southern Research Institute, Birmingham, AL, Jul 1986.
- D-2. Southern Research Institute, Test and Evaluation of Carbon-Carbon Noستip Materials: Evaluation of Failed Heater Elements, SoRI-Eas-82-770-4179-8-I-F, Southern Research Institute, Birmingham, AL, Nov 1982.

DISTRIBUTION

	<u>Copies</u>		<u>Copies</u>
Center for Naval Analyses		Internal Distribution:	
4401 Fort Avenue		K	1
P.O. Box 16268		K20	1
Alexandria, VA 22302-0268	1	K22	1
		K22 (E. Becker)	1
Calspan Corporation		K22 (W. Dorsey)	1
AEDC Division		K22 (R. Edwards)	1
Attn: R.K. Matthews	1	K22 (M. Fung)	1
Aerophysics Branch		K22 (D. Vavrick)	1
Von Karman Facility		K22 (L. Zentz)	1
Arnold Air Force Station,		K23	1
TN 37389		K23 (J. Etheridge)	1
		K23 (C. Higgins)	1
Materials Sciences Corporation		K23 (E. Larach)	1
Attn: Kent Buesking	1	K23 (M. Metzger)	10
Gwynedd Plaza II		K23 (D. Newell)	1
Bethlehem Pike		K23 (C. Rozanski)	1
Spring House, PA 19477		K23 (J. Waldo)	1
		K23 (R. Waser)	1
Southern Research Institute		K24	1
Attn: Sam Causey	1	K24 (R. Driftmyer)	1
2000 Ninth Ave South		R14 (R. Kavetsky)	1
P.O. Box 55305		E231	2
Birmingham, AL 35255-5305		E232	15
Library of Congress			
Attn: Gift and Exchange			
Division	4		
Washington, DC 20540			
Defense Technical Information			
Center			
Cameron Station			
Alexandria, VA 22304-6145	12		