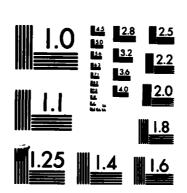
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THESIS

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ROBUST FLIGHT CONTROLLERS

THESIS

Presented to the Faculty of the School of Engineering
of the Air Force Institute of Technology
Air University
in Partial Fulfillment of the
Requirements for the Degree of
Master of Science

by

Jean M. Howey, B.S.

2Lt

USAF

Graduate Aeronautical Engineering

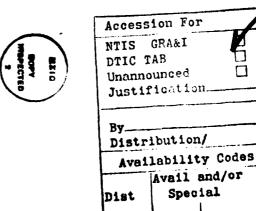
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Preface

In the past two decades, one of the major stumbling blocks in applying optimal control theory to flight control problems has been that measurements of all the states of the system are not available. Thus, it is necessary to use some type of observer or filter to reconstruct the states of the aircraft. However, when this is done, all guarantees of desirable stability robustness properties are lost. This thesis addresses this problem and evaluates the success of some techniques to recover the good stability robustness properties associated with full-state feedback.

I wish to thank my advisor, Professor Peter S. Maybeck for his invaluable guidance during the course of this research and for his thorough editing of this document. In addition, I would like to thank my committee members, Professors John J. D'Azzo and Robert Calico for their suggestions and comments. Finally, I wish to thank Captain Richard Floyd for his assistance in modifying and correcting the computer programs used to accomplish this project.



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Abstract

This study examines the concept of robustifying a controlled system against differences which may exist between the real world system and the low-order design model upon which the controller design is based. The types of controllers considered are based upon the Linear system model, Quadratic cost, and Gaussian (LQG) noise process methodology of optimal control theory. It is assumed that full-state feedback is not available and a Kalman filter is employed to provide state estimates to the controller. Both continuous-time and sampled-data controllers are considered.

Two robustification techniques are considered. The first is the method of injecting zero-mean white Gaussian noise into the design model at the point of entry of the control inputs during the process of tuning the Kalman filter. The second method is an extension of the first, where the white noise is replaced by a time-correlated noise. This allows the primary strength of the noise to be concentrated only in the frequency range where robustification is desired. Comparing the results of applying the two methods allows a designer to make a trade-off between the amount of desired robustification and the performance degradation at the design conditions which occurs when the techniques are applied.

Both methods are found to improve substantially the robustness properties of the controllers considered. For the specific flight control problem considered in this thesis, the technique of injecting white input noise into the design model produced the desired degree of robustification without prohibitively degrading performance at the design conditions.

The second method, though effective, did not yield substantial enough performance benefits over the first to warrant use in actual implementation.

ROBUST FLIGHT CONTROLLERS

I. Introduction

1.1 Background

A vital element of a flight control system is that it be "robust". Robustness implies that the controller provides adequate (i.e., stable closed-loop) performance over a wide range of operating conditions and system parameters. For example, finite-dimension models of the dynamics of an aircraft are typically generated by linearizing the aircraft equations of motion about a limited number of specific equilibrium flight conditions. Controllers are then designed for these "trim" conditions. However, at flight conditions other than the specific trim condition used for controller design, the closed-loop performance of the controller system may be inadequate or unstable. That is, at the off-design flight condition, the aircraft parameters (upon which the design is based) have changed sufficiently to make performance of the controller inadequate. One method used in the past has been to schedule feedback gains for the controller so as to compensate for the change in system parameters. However, it is desirable to have enlarged regions about nominal design conditions within which a specific controller design will yield adequate performance. This would allow linear perturbation techniques to be used with more confidence and may also reduce the number of required design conditions about which such perturbations are defined. It may even be desirable to have a fixed controller which is sufficiently robust to produce acceptable performance for all conditions in the aircraft's flight envelope.

Robustness is also a concern when controllers are designed using purposefully reduced order models. A robust controller will provide stable closed-loop performance even when states of the real-world system have been ignored in the design model. A third robustness issue is survivability. Robustness can also imply the ability to maintain closed-loop stability if, for instance, part of the flight control system is lost due to ground fire: i.e., the "true" system is vastly different than the system model upon which the controller was designed. Such a robust controller will provide a stable, though degraded, aircraft performance while adaptation algorithms attempt to discern what system elements have been lost and to determine an appropriate modification of controller characteristics for future use.

In the 1960's, modern control theory methods, such as optimal control theory, showed promise in application to flight control problems. One drawback of applying optimal control theory techniques to flight control problems, however, is that the resulting controllers require full-state feedback, but measurements of all states are generally not available. Thus, it becomes necessary to include a filter or observer in the controlled system to estimate the states. However, once an observer has been inserted into the loop, stability robustness becomes a major concern (Ref 5).

Recently, efforts to improve the robustness properties of observer-based controllers have included a technique, developed by J.C. Doyle and G. Stein (Ref 6), which injects white noise into a controller system model at the point of entry of the control inputs during the process of tuning the Kalman filter. It is claimed that, as the strength of the input noise

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is increased, the filter-based controller will asymptotically recover the good robustness properties of a full-state feedback system in the continuous-time case. A disadvantage of this technique is that the additional noise can degrade the performance of the system at the design conditions.

A natural extension to the idea of injecting white input noise into a system model is to consider time-correlated noise. This allows the robustification technique to be applied only over a desired frequency range rather than over all frequencies as in the original Doyle and Stein method. Thus, the degradation in performance due to the additional noise can be reduced (Ref 15;16;28).

The techniques described above are applied in this thesis to a specific aircraft flight control problem. Two types of controllers are considered. The first is an optimal Linear Quadratic Gaussian (LQG) regulator. Available software allows the design of a continuous-time and a digital controller. The second type of controller is an optimal LQG-based Proportional-plus-Integral digital controller. For both types of controller, a Kalman filter is implemented to provide estimates of the states of the system. The success of applying the robustification techniques is determined by designing a Kalman filter and controller for one trim condition, then evaluating the performance of the controller at an off-design flight condition, as well as designing the filter and controller on the basis of purposely reduced-order models for computational loading reasons. Time histories of the mean and standard deviations of the aircraft states and controls are examined. Additionally, it is desired to compare the performance of the controller at the design conditions with

no input noise, white noise and time-correlated noise used for filter retuning (robustification) to determine how much the performance is degraded by the input of the noise, and also to determine if performance benefits can be gained by using time-correlated noise as opposed to white noise.

1.2 Problem

The primary objectives of this thesis are:

- To apply the robustification techniques of injecting white or time-correlated noise into a system model at the control entry points during filter tuning to a flight control problem for a high performance aircraft.
- To extend the techniques for LQG regulators to LQG-based PI controllers.
- 3. To evaluate the robustness properties of the controller designs by performing covariance analyses for the controlled systems at both the design flight condition and other off-design conditions within the aircraft's operational flight envelope, using a purposefully reduced-order design model. Robustified designs are to be compared to unrobustified designs and also to full-state feedback designs when possible.

1.3 Sequence of Presentation

The body of this thesis is contained in Chapter II-V. Chapter II presents the equations used for designing and evaluating optimal deterministic LQG regulators for both the continous- and discrete-time case.

Also included is the application of the Doyle and Stein technique to continuous-time systems and several extensions of the technique to discrete-time systems.

Chapter III presents the equations necessary to design and evaluate optimal LQG-based PI controllers for the discrete-time case. Then the Doyle and Stein technique is applied to systems employing PI controllers. As pointed out in the text, robustification by this technique is a procedure which affects only the Kalman filter design; thus, the same method is used for PI controllers as for regulators in this thesis.

Chapter IV examines the idea of injecting time-correlated noise rather than white noise into a controlled system model during tuning of the filter, to improve the tradeoff of the controller's robustness properties versus performance degradation at design conditions. First, a stochastic process model (shaping filter) is developed for the noise process which is then augmented with the system state differential equations. Then, the types of time-correlated noise of interest to this thesis are considered, including a discussion of the specific shaping filters to generate the desired noise process.

Chapter V presents the model of a high-performance aircraft to be used in this thesis. A design flight condition is chosen and linearized perturbation equations of motion are developed for the aircraft about that operating point. The design model for the Kalman filter and controller is purposefully reduced in order from the full set of linearized equations so that this aspect of robustness can be examined. Finally, models at other flight conditions are listed with which the robustness of the system to parameter changes will be evaluated.

The findings of this thesis, results and conclusions are presented in Chapter VI. Recommendations for further research are made in Chapter VII.

Four appendices are included. The first presents a generic format for a controller into which the types of controllers in Chapters II and III can be rearranged. The usefulness of the format becomes apparent in a performance analysis, when the same set of equations can be used to evaluate the performance of any controller in the standard format.

Appendix B lists the source code for a Fortran program used in designing LQG regulators. Included are a discussion of how the program is executed and modifications from a previous version to allow the input of time-correlated noise (Ref 21).

Appendix C lists the modification to the software of Reference 13 and 30 to allow the input of white and time-correlated noise into the system model. The software is an interactive program used for designing PI regulators with a Command Generator Tracker in the feed-forward loop. This thesis will exploit only the PI regulator design capabilities.

Appendix D includes further performance analysis results in addition to the findings in Chapter VI. It was stated in Reference 6 that the Doyle and Stein technique is not guaranteed to improve robustness if the design model is non-minimum phase (i.e., there are transmission zeroes in the right-half s-plane). Appendix D shows a case where the design model was non-minimum phase and where the addition of input noise to the system model has actually drive an initially stable closed-loop system to be unstable.

II. LQG REGULATORS

2.1 Introduction

This chapter presents the equations used in designing optimal Linear Quadratic Gaussian (LQG) controllers for a system modelled as linear, time-invariant, and driven by zero-mean, white Gaussian noise and deterministic inputs, subject to quadratic costs for defining optimality criteria. The model used for this thesis is described in Chapter V. The methods used are taken primarily from Reference 24 unless otherwise stated.

In the first section, the controller equations for a continuoustime system having continuous-time measurements are given. The structures
of controllers assuming perfect access to all the states of a system
versus controllers with a Kalman filter to estimate states are examined.

Next, the equations needed to evaluate the performance of controller
designs are given. Finally, a technique developed by Doyle and Stein
(Ref 6) to robustify the Kalman filter for continuous-time systems is
presented.

The fourth section contains the controller equations for a continuoustime system having sampled-data measurements. Next the performance analysis equations for the sampled-data system are developed.

The final sections contain alternative methods for applying the Doyle and Stein technique to sampled-data systems. Three possible basic approaches are simply to discretize the controller designed for the continuous system or to modify the technique in one of two ways so that it applies directly to a discrete system.

All methods described in this chapter are incorporated in a Fortran program originally written by Captain Eric Lloyd and modified to some extent by this author. For source codes and information about the program, see Reference 21. Modifications and additions to the program are listed in Appendix B.

2.2 Continuous-Time Controllers

The state description for an important class of continuous-time systems is given by the linear stochastic differential equation

$$\dot{\underline{x}}(t) = F(t) \underline{x}(t) + B(t) \underline{u}(t) + G(t) \underline{w}(t)$$
 (2-1)

where $\underline{w}(t)$ is a white Gaussian noise with statistics

$$\mathbf{E}\{\underline{\mathbf{w}}(\mathsf{t})\} = \underline{\mathbf{0}} \tag{2-2a}$$

$$E\{\underline{w}(t) \ \underline{w}^{T}(t+\tau)\} = Q(t)\delta(\tau)$$
 (2-2b)

An optimal LQG controller for the system minimizes the cost functional

$$J_{c} = E \left\{ \frac{1}{2} \underline{x}^{T}(t_{f}) X_{f} \underline{x}(t_{f}) \right\}$$

$$+ \frac{1}{2} \int_{t_{o}}^{t_{f}} \left\{ \begin{bmatrix} \underline{x}(t) \\ \underline{u}(t) \end{bmatrix}^{T} \begin{bmatrix} W_{xx}(t) & W_{xu}(t) \\ W_{xu}(t) & W_{uu}(t) \end{bmatrix} \begin{bmatrix} \underline{x}(t) \\ \underline{u}(t) \end{bmatrix} \right\} dt \tag{2-3}$$

where $W_{xx}(t)$ is a positive semi-definite weighting matrix associated with the system states, $\underline{x}(t)$; $W_{uu}(t)$ is a positive definite weighting matrix associated with the controls, $\underline{u}(t)$, applied, to the system; $W_{xu}(t)$ is a cost-weighting matrix associated with cross terms of $\underline{x}(t)$ and $\underline{u}(t)$ and is

chosen so that the composite matrix of Equation (2-3) is positive semi-definite; and X_f is a positive semi-definite weighting matrix associated with the states at the final time, $\underline{x}(t_f)$.

The optimal control to be applied at time t which minimizes the above cost function is described as

$$\underline{u}^{*}(t) = -G_{c}^{*}(t) \underline{x}(t)$$
 (2-4)

with the gain matrix, $G_c^*(t)$, given by

$$G_c^*(t) = W_{uu}^{-1}(t) B^T(t) K_c(t)$$
 (2-5)

and $K_{c}(t)$ is calculated using the backward Riccati differential equation

$$-\dot{K}_{c}(t) = F^{T}(t) K_{c}(t) + K_{c}(t) F(t) + W_{xx}(t)$$

$$- K_{c}(t) B(t) W_{yy}^{-1}(t) B^{T}(t) K_{c}(t)$$
(2-6)

subject to the final condition

$$K_{c}(t_{f}) = X_{f}$$
 (2-7)

Notice that Equation (2-6) assumes that the cross weighting matrix $W_{xu}(t)$ is zero. If this is not the case, an appropriate variable transformation can be made which will account for the non-zero cross terms and allow equation (2-6) to be used (Ref 24:202-203; 19:79-86).

Up to this point, the controller equations have been derived allowing for time-varying systems, cost-weighting matrices and feedback gains.

However, as described in Chapter V, the model used for this thesis is time-invariant with stationary noises (i.e., the covariance kernel

 $E\{w(t)w^T(t+\tau)\}$ is a function of only the time difference τ (Ref 23:139-140)) and constant weighting matrices. Thus a steady-state constant gain controller can be used, ignoring terminal transients in the feedback gain

$$\underline{\mathbf{u}}^{*}(t) = -\mathbf{G}_{\mathbf{c}}^{*}\underline{\mathbf{x}}(t) = -\left[\mathbf{W}_{\mathbf{u}\mathbf{u}}^{-1}\mathbf{B}^{\mathsf{T}}\,\bar{\mathbf{K}}_{\mathbf{c}}\right]\underline{\mathbf{x}}(t) \tag{2-8}$$

where \overline{K}_{c} is now the solution to the steady-state Riccati equation

$$-\frac{\dot{\bar{K}}}{c} = 0 = F^{T}\bar{K}_{c} + \bar{K}_{c}F + W_{xx} - \bar{K}_{c}BW_{uu}^{-1}B^{T}\bar{K}_{c}$$
 (2-9)

Henceforth, the assumption of a time-invariant system with stationary noises and constant weighting matrices is made, and the time argument is omitted unless needed to avoid confusion.

The optimal control law of Equation (2-4) is given as a gain matrix times the state values at a particular time. If, however, perfect knowledge of the states is not available, then an estimate of the state, $\hat{x}(t)$, must be used in place of x(t). In this case, a Kalman filter is employed to evaluate the conditional mean, $\hat{x}(t)$, and conditional covariance, P(t), of the states of the system.

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Instead of the actual values of the states, assume that what are accessible from the system are noise-corrupted measurements of the time-invariant form

$$z(t) = H \underline{x}(t) + \underline{v}(t)$$
 (2-10)

where $\underline{v}(t)$ is a stationary white Gaussian noise assumed independent of the dynamics driving noise $\underline{w}(t)$ and with statistics

$$E\{v(t)\} = 0$$
 (2-11a)

$$E\{\underline{v}(t) \ \underline{v}^{T}(t+\tau)\} = R\delta(\tau)$$
 (2-11b)

Then the Kalman filter equations yield an estimate of the states and the covariance via (Ref 23:257,259)

$$\frac{\hat{\mathbf{x}}(t) = \mathbf{F}\hat{\mathbf{x}}(t) + \mathbf{B}\mathbf{u}(t) + \mathbf{PH}^{\mathsf{T}}\mathbf{R}^{-1} \left[\underline{\mathbf{z}}(t) - \mathbf{H}\hat{\mathbf{x}}(t)\right]$$
 (2-12a)

$$P(t) = FP(t) + P(t)F^{T} + GQG^{T} - P(t)H^{T}R^{-1}HP(t)$$
 (2-12b)

These differential equations are solved forward in time subject to the initial conditions

$$E\{\underline{x}(t_0)\} = \overline{x}_0 \qquad (2-13a)$$

$$E\{[\underline{x}(t_o) - \overline{\underline{x}}_o] [\underline{x}(t_o) - \overline{\underline{x}}_o]^T\} = P_o \qquad (2-13b)$$

which are obtained from an a priori Gaussian density function for the states at the initial time.

The precomputable Kalman filter gain for the continuous-time system is expressed in Equation (2-12a) as

$$K(t) = P(t) H^{T} R^{-1}$$
 (2-14)

If it is assumed that the initial transients of Equation (2-12b) are short compared to the total time of interest, the steady-state covariance, \bar{P} , can be computed as the solution to

$$\dot{\bar{P}}(t) = 0 = F\bar{P} + \bar{P}F^{T} + GQG^{T} - \bar{P}H^{T}R^{-1}H\bar{P}$$
 (2-15)

and the constant Kalman filter gain is given by

$$K = \overline{P}H^{T}R^{-1} \tag{2-16}$$

Do not confuse the Kalman Filter gain, K, with $K_{\mbox{\scriptsize c}}$ of Equation (2-6) and (2-9).

Figure (2-1) shows the form of the continuous-time controller.

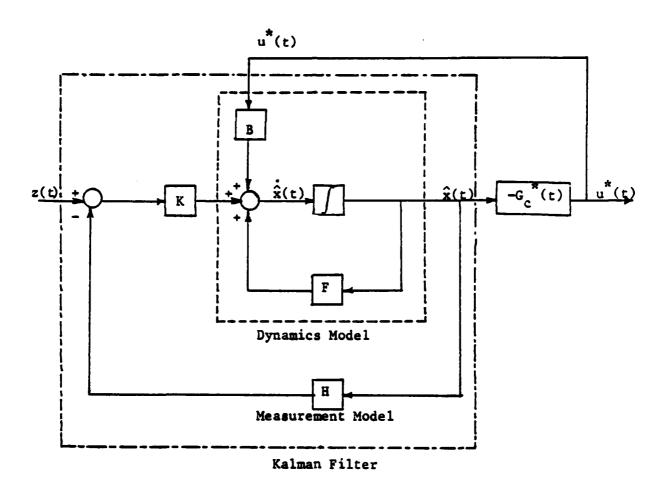


Figure 2-1: Continuous Measurement LQG Optimal Stochastic Controller

2.3 Continuous-Time Performance Analysis

The performance analysis for a continuous-time LQG controller is based on the development for a sampled-data controller given in Reference 23 and derived in Reference 21.

First, a "truth model" is developed for a given system which is judged to represent adequately the response of a system to inputs and disturbances encountered in the real world. Then, controllers for the system can be designed, generally based on lower order, simplified models. The performance is determined by examining the statistical characteristics of the truth model states, $\underline{x}_t(t)$, and the controls, $\underline{u}(t)$, for each proposed controller inserted into the real world simulation provided by the truth model. This is depicted in Figure (2-2).

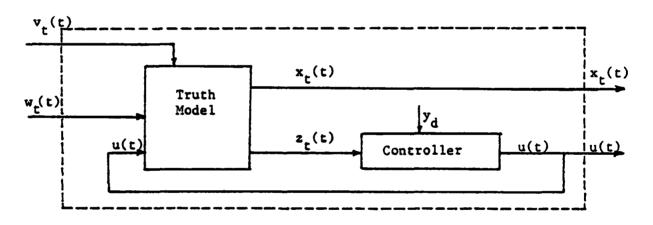


Figure 2-2: Performance Evaluation for Linear Sampled-Data Controller

The performance evaluation determines the statistical characteristics of $\underline{x}_t(t)$, the truth model states, rather than the states of the simplified controller model. It is important to determine the effect of applying controls from a reduced order controller on the actual system response.

Additionally, the statistical characteristics of the controls are examined to ensure that they do not exceed physical limits or design specifications.

The assumed linear differential equation describing the continuoustime truth model system and available measurements are

$$\underline{\dot{x}}_{t}(t) = F_{t}\underline{x}(t) + B_{t}\underline{u}(t) + G_{t}\underline{w}_{t}(t)$$
 (2-17)

$$\underline{z}_{t}(t) = H_{t}\underline{x}(t) + \underline{v}_{t}(t)$$
 (2-18)

where initial conditions and statistics of the noise are given by

$$E\{\underline{x}_{t}(t_{o})\} = \underline{\bar{x}}_{to}$$
 (2-19)

$$E\{\left[\underline{x}_{t}(t_{o}) - \underline{\overline{X}}_{to}\right]\left[\underline{\overline{x}}_{t}(t_{o}) - \underline{\overline{x}}_{to}\right]\} = P_{to}$$
 (2-20)

$$\mathbb{E}\{\underline{\mathbf{w}}_{+}(\mathbf{t})\} = 0 \tag{2-21}$$

$$E\{\underline{w}_{t}(t) \ \underline{w}_{t}^{T} (t+\tau)\} = Q_{t}\delta(\tau)$$
 (2-22)

$$\mathbb{E}\{\underline{\mathbf{v}}_{+}(\mathbf{t})\} = \underline{\mathbf{0}} \tag{2-23}$$

$$E\{\underline{v}_{t}(t) \ \underline{v}_{t}^{T}(t+\tau)\} = R_{t}\delta(\tau)$$
 (2-24)

Note that $\underline{\mathbf{v}}_{\mathsf{t}}(\mathsf{t})$ and $\underline{\mathbf{w}}_{\mathsf{t}}(\mathsf{t})$ are assumed to be independent of each other and that the subscript t refers to the truth model.

A useful form of expressing the control law of Equation (2-4) and other more general linear control algorithms, and an equation to propagate the internal states of the controller, are given by

$$\underline{\mathbf{u}}(t) = G_{cx} \mathbf{x}_{c}(t) + G_{cz} \mathbf{z}_{t}(t) + G_{cy} \mathbf{y}_{d}(t)$$
 (2-25)

$$\frac{\dot{x}}{c}(t) = F_c \frac{x}{c}(t) + B_{cz} \frac{z}{c}(t) = B_{cy} \frac{y}{d}(t)$$
 (2-26)

where $\underline{y}_d(t)$ refers to a command input for the system controlled variable, $\underline{y}(t)$, to track, where

$$\underline{y}(t) = C\underline{x}(t) + D_{\underline{y}} \underline{u}(t)$$
 (2-27)

The gain matrices in Equations (2-25) and (2-26) are evaluated explicitly in Appendix A. Putting the control law into the generic form allows direct comparison of different types of linear control laws.

Determination of time histories are desired of the mean and covariance of an augmented vector

$$\underline{y}_{a}(t) = \begin{bmatrix} \underline{x}_{t}(t) \\ \\ \underline{u}(t) \end{bmatrix}$$
 (2-28)

All quantities of interest in a performance analysis are assumed to be components or linear combinations of components of this vector. If \mathbf{q}_k is a scalar quantity of interest, i.e.,

$$q_k = \underline{q}_k^T \underline{y}_a(t) \tag{2-29}$$

then the statistics of $\mathbf{q}_{\mathbf{k}}$ are given by

$$mean\{q_k(t)\} = \underline{q}_k^T \underline{m}_{y_a}(t)$$
 (2-30a)

$$cov \{q_k(t)\} = \underline{q_k}^T P_{y_a y_a}(t) \underline{q_k}$$
 (2-30b)

where $\underline{\underline{m}}_{y_a}(t)$ is the mean and $P_{y_ay_a}(t)$ is the covariance of the augmented vector $\underline{y}_a(t)$.

To evaluated the first two moments of $\underline{y}_a(t)$, it is first necessary to form another augmented vector composed of the internal states of the truth model and the controller model

$$\underline{\mathbf{x}}_{\mathbf{a}}(t) = \begin{bmatrix} \underline{\mathbf{x}}_{\mathbf{t}}(t) \\ \\ \underline{\mathbf{x}}_{\mathbf{c}}(t) \end{bmatrix}$$
 (2-31)

Using Equation (2-18) and (2-25), $\underline{u}(t)$ and $\underline{z}(t)$ are eliminated from Equation (2-17)

$$\dot{x}_{t}(t) = \{ F_{t} + B_{t} G_{cz} H_{t} \} \underline{x}_{t}(t) + B_{t} G_{cx} \underline{x}_{c}(t)$$

$$+ B_{t} G_{cy} \underline{y}_{d}(t) + B_{t} G_{cz} \underline{y}_{t}(t) + G_{t} \underline{w}_{t}(t)$$
(2-32)

Similar substitution into Equation (2-26) yields

$$\underline{\dot{x}}_{c}(t) = F_{c}\underline{x}_{c}(t) + B_{cy}\underline{y}_{d}(t) + B_{cz}[H_{t}\underline{x}_{t}(t) + \underline{y}_{t}(t)] \qquad (2-33)$$

Form the augmented noise vector

$$\underline{\underline{w}}_{a}(t) = \begin{bmatrix} \underline{\underline{w}}_{t}(t) \\ \\ \underline{\underline{v}}_{t}(t) \end{bmatrix}$$
 (2-34)

as a zero-mean white Gaussian noise with covariance kernel $E\{w_a(t)w_a^{\ T}(t + \tau)\} = Q_a \delta(\tau) \,, \text{ where }$

$$Q_{a} = \begin{bmatrix} Q_{t} & 0 \\ 0 & R_{t} \end{bmatrix}$$
 (2-35)

Non-zero cross terms can easily handle the case of $\underline{\underline{w}}_t(t)$ and $\underline{\underline{v}}_t(t)$ being correlated. Now an augmented system equation can be written as

$$\frac{\dot{x}}{a}(t) = F_{a}x_{a}(t) + B_{a}y_{d}(t) + G_{a}y_{a}(t)$$
(2-36)

where

$$\mathbf{F_a} = \begin{bmatrix} \mathbf{F_t} + \mathbf{B_t} & \mathbf{G_{cz}} \mathbf{H_t} & \mathbf{B_t} \mathbf{G_{cx}} \\ & & & \\ & & & \\ & & & \\ \mathbf{B_{cz}} & \mathbf{F_c} \end{bmatrix}$$
(2-37)

$$B_{a} = \begin{bmatrix} B_{t}G_{cy} \\ B_{cy} \end{bmatrix}$$
 (2-38)

$$G_{\mathbf{a}} = \begin{bmatrix} G_{\mathbf{t}} & B_{\mathbf{t}}G_{\mathbf{c}\mathbf{z}} \\ & & \\ 0 & B_{\mathbf{c}\mathbf{z}} \end{bmatrix}$$
 (2-39)

The initial conditions for the augmented vector are

$$\mathbb{E}\left\{\underline{\mathbf{x}}_{\mathbf{a}}(\mathbf{t}_{0})\right\} = \begin{bmatrix} \underline{\mathbf{x}}_{\mathbf{t}0} \\ \underline{\mathbf{x}}_{\mathbf{c}0} \end{bmatrix} = \underline{\mathbf{x}}_{\mathbf{a}0}$$
 (2-40)

$$P_a(t_0) = \begin{bmatrix} P_0 & 0 \\ 0 & 0 \\ 0 & 0 \end{bmatrix}$$
 (2-41)

Initial conditions on the controller states are often assumed to be zero: $\frac{1}{x_{co}} = 0$.

The mean and covariance of the states in Equation (2-36) propagate as

$$\underline{\underline{m}}_{x_a}(t) = F_{a}\underline{\underline{m}}_{x_a}(t) + B_{a}\underline{\underline{y}}_{d}(t)$$
(2-42)

$$P_{x_a x_a}(t) = F_a P_{x_a x_a}(t) + P_{x_a x_a}(t) F_a^T + G_a Q_a G_a^T \qquad (2-43)$$

or solving the differential equation yields

$$\underline{\underline{\mathbf{m}}}_{\mathbf{a}}(t) = \phi_{\mathbf{a}}(t,t_{0}) \underline{\underline{\mathbf{x}}}_{\mathbf{a}0} + \int_{t_{0}}^{t} \phi_{\mathbf{a}}(t,\tau) B_{\mathbf{a}} \underline{\mathbf{y}}_{\mathbf{d}}(\tau) d\tau \qquad (2-44)$$

$$P_{x_a x_a}(t) = \phi_a(t, t_0) P_{ao} \phi_a^{T}(t, t_0)$$

$$+ \int_{t_0}^{t} \phi_a(t,\tau) G_a Q_a G_a^{T} \phi_a^{T}(t,\tau) d\tau \qquad (2-45)$$

where $\phi_a(t,t_o)$ is the state transition matrix associated with F_a , i.e., $\phi_a(t,t_o) = \phi_a(t-t_o) = \exp\{F_a(t-t_o)\}.$

However, the requirement is to solve for the statistics of the vector $\underline{\mathbf{y}}_{\mathbf{a}}(t)$ defined in Equation (2-32). This vector is related to $\underline{\mathbf{x}}_{\mathbf{a}}(t)$ by

$$\underline{y}_{a}(t) = \begin{bmatrix} I & 0 \\ \\ G_{cz}^{H}_{t} & G_{cx} \end{bmatrix} \begin{bmatrix} \underline{x}_{t}(t) \\ \\ \underline{x}_{c}(t) \end{bmatrix} + \begin{bmatrix} 0 \\ \\ G_{cy} \end{bmatrix} \underline{y}_{d}(t) + \begin{bmatrix} 0 \\ \\ G_{cz} \end{bmatrix} \underline{v}_{t}(t) \quad (2-46)$$

The vector is seen to be a linear combination of jointly Gaussian variables with known statistics. Thus, the desired statistics can be generated from Equation (2-39) using the method shown in Reference 23:112.

$$\underline{\underline{\mathbf{m}}}_{\mathbf{y}_{\mathbf{a}}}(t) = \begin{bmatrix} \mathbf{I} & \mathbf{0} \\ & & \\ G_{\mathbf{c}\mathbf{z}}^{\mathbf{H}} \mathbf{t} & G_{\mathbf{c}\mathbf{x}} \end{bmatrix} \underline{\underline{\mathbf{m}}}_{\mathbf{x}_{\mathbf{a}}}(t) + \begin{bmatrix} \mathbf{0} \\ & \\ G_{\mathbf{c}\mathbf{y}} \end{bmatrix} \underline{\underline{\mathbf{y}}}_{\mathbf{d}}(t)$$
 (2-47)

$$P_{y_a y_a}(t) = \begin{bmatrix} I & 0 \\ \\ G_{cz} H_t & G_{cx} \end{bmatrix} P_{x_a x_a}(t) \begin{bmatrix} I & 0 \\ \\ G_{cz} H_t & G_{cx} \end{bmatrix}^T$$

$$+\begin{bmatrix} I & O \\ & & \\ G_{cz}H_t & G_{cx} \end{bmatrix} P_{x_av_t(t)} \begin{bmatrix} O & G_{cz}^T \end{bmatrix}$$

$$+ \begin{bmatrix} 0 \\ \\ G_{cz} \end{bmatrix} P_{x_a v_t}^{T}(t) \begin{bmatrix} I & 0 \\ \\ \\ G_{cz} H_t & G_{cx} \end{bmatrix}^{T}$$

$$+ \begin{bmatrix} 0 \\ G_{cz} \end{bmatrix} P_{v_t v_t(t)} \begin{bmatrix} 0 & G_{cz}^T \end{bmatrix}$$
 (2-48)

In the last term, note that $P_{v_t^{v_t}}(t) = R_t^{\delta}(0)$ and that $\delta(0) = \infty$. This

terms gives an infinite value to the lower right-hand partition of the covariance matrix. However, it is still of interest to look at the contribution of the other three terms separately. To evaluate Equation (2-48) fully, it is necessary to find an expression for $P_{x_a}v_t$ (t). This

can be written as

$$P_{x_a v_t} = E\{ [\underline{x}_a(t) - \underline{m}_{x_a}(t)] [\underline{v}_t(t) - \underline{m}_{v_t}(t)]^T \}$$
 (2-49)

Expand this, noting that $\underline{\underline{m}}_{V_+}(t) = 0$

$$P_{x_a v_t}(t) = E\{\underline{x}_a(t)\underline{v}_t^T(t) - \underline{m}_{x_a}(t)\underline{v}_t^T(t)\}$$
 (2-50)

$$p_{\underline{x}_{\underline{a}}v_{\underline{t}}} = \mathbb{E}\left\{\underline{x}_{\underline{a}}(t)\underline{v}_{\underline{t}}^{T}(t)\right\} - \underline{m}_{\underline{a}}(t)\mathbb{E}\left\{\underline{v}_{\underline{t}}^{T}(t)\right\} \quad (2-51)$$

but $E\{\underline{v}_t^T(t)\} = \underline{m}_{v_t}^T(t) = \underline{o}^T$, therefore

$$P_{\underline{x}_{\underline{a}}v_{\underline{t}}}(t) = E \{\underline{x}_{\underline{a}}(t)\underline{v}_{\underline{t}}^{T}(t)\}$$
 (2-52)

Replace $\underline{x}_a(t)$ with the solution form for Equation (2-36)

$$P_{\mathbf{x}_{a}\mathbf{v}_{t}}(t) = E\{\phi_{a}(t,t_{o})\underline{\mathbf{x}}_{a}(t_{o})\underline{\mathbf{v}}_{t}^{T}(t)$$

$$+ \int_{t_{o}}^{t} \phi_{a}(t,\tau)B_{a}\underline{\mathbf{v}}_{d}(\tau) \underline{\mathbf{v}}_{t}^{T}(t) d\tau$$

$$+ \int_{t_{o}}^{t} \phi_{a}(t,\tau)G_{a}\underline{\mathbf{w}}_{a}(\tau) \underline{\mathbf{v}}_{t}^{T}(t) d\tau\} \qquad (2-53)$$

Making the assumption that $\underline{x}_a(t_0)$ and $\underline{v}_t(t)$ are independent (and thus uncorrelated), the first term in Equation (2-53) is zero since $E\{v_t^T(t)\} = \underline{0}^T$. Substituting in the augmented matrices, the remaining terms are

$$P_{\mathbf{x}_{\mathbf{a}}\mathbf{v}_{\mathbf{t}}}(t) = \mathbb{E}\left\{ \int_{t_{0}}^{t} \phi_{\mathbf{a}}(t,\tau) \begin{bmatrix} B_{\mathbf{t}} & G_{\mathbf{cy}} \\ & & \\ & & \end{bmatrix} \frac{\mathbf{y}_{\mathbf{d}}(\tau) & \mathbf{v}_{\mathbf{t}}^{T}(t) d\tau}{B_{\mathbf{cy}}} \right\}$$

$$+ \int_{t_{0}}^{t} \phi_{\mathbf{a}}(t,\tau) \begin{bmatrix} G_{t} & B_{t}G_{cz} \\ & & \\ 0 & B_{cz} \end{bmatrix} \begin{bmatrix} \underline{\mathbf{w}}_{t}(\tau) \\ \\ \underline{\mathbf{v}}_{t}(\tau) \end{bmatrix} \underline{\mathbf{v}}_{t}^{T}(t) d\tau$$
(2-54)

which can be rewritten as

$$P_{\mathbf{x}_{\mathbf{a}}\mathbf{v}_{\mathbf{t}}}(\mathbf{t}) = E \begin{cases} \int_{\mathbf{t}_{o}}^{\mathbf{t}} \phi_{\mathbf{a}}(\mathbf{t}, \tau) & \begin{bmatrix} B_{\mathbf{t}}G_{\mathbf{c}y} \\ \\ B_{\mathbf{c}y} \end{bmatrix} \underline{y}_{\mathbf{d}}(\tau) \ \underline{v}_{\mathbf{t}}^{\mathbf{T}}(\mathbf{t}) d\tau \end{cases}$$

$$+ \int_{0}^{t} \phi_{a}(t,\tau) \begin{bmatrix} G_{t} \underline{w}_{t}(\tau) + B_{t} G_{cz} \underline{v}_{t}(\tau) \\ B_{cz} \underline{v}_{t}(\tau) \end{bmatrix} \underline{v}_{t}^{T}(t) d\tau$$
(2-55)

Again, the first term is zero since $\underline{v}_t(t)$ is zero-mean, and $\underline{v}_d(\tau)$ is deterministic. This leaves

$$P_{\mathbf{x}_{\mathbf{a}}\mathbf{v}_{\mathbf{t}}}(t) = E \left\{ \int_{t_{0}}^{t} \phi_{\mathbf{a}}(t,\tau) \begin{bmatrix} G_{\mathbf{t}}\mathbf{w}_{\mathbf{t}}(\tau) + B_{\mathbf{t}}G_{\mathbf{c}\mathbf{z}}\mathbf{v}_{\mathbf{t}}(\tau) \\ & & \\ B_{\mathbf{c}\mathbf{z}}\mathbf{v}_{\mathbf{t}}(\tau) \end{bmatrix} \mathbf{v}_{\mathbf{t}}^{T}(t)d\tau \right\}$$
(2-56)

Noting that $\underline{\underline{w}}_t(\tau)$ and $\underline{\underline{v}}_t(t)$ are assumed independent and

$$E\{\underline{v}_{t}(\tau)\underline{v}_{t}^{T}(t)\} = R_{t}\delta(t-\tau)$$
 (2-57)

the expected value operation can be moved inside the integral, and Equation (2-56) further reduces to

$$P_{\mathbf{x}_{a}\mathbf{v}_{t}}(t) = \int_{t_{o}}^{t} \phi_{a}(t,\tau) \begin{bmatrix} B_{t}G_{cz} \\ B_{cz} \end{bmatrix} R_{t}\delta(t-\tau)d\tau \qquad (2-58)$$

Applying the Dirac delta sifting property to the above equation, noting that t is the upper limit of the integration and that it also appears in the delta function argument, yields

$$P_{x_a v_t}(t) = \phi_a(t,t) \begin{bmatrix} B_t G_{cz} \\ B_{cz} \end{bmatrix} \frac{1}{2} R_t$$
 (2-59)

The state transition matrix $\phi_a(t,t)$ is the identity matrix I. The value of $\frac{1}{2}$ appears when integrating the Dirac delta function between the time limits t_0 and t since its argument goes to zero at τ = t, i.e., at its upper limit. The resulting form is

$$P_{x_a v_t} = \frac{1}{2} \begin{bmatrix} B_t G_{cz} \\ B_{cz} \end{bmatrix} R_t$$
 (2-60)

At this point, all quantities needed to obtain the performance analysis for a linear, time-invariant, continuous-time system and controller have been defined in this section. The primary result is that, for a truth model given by Equations (2-17) and (2-24) and a controller of the form (2-25) and (2-26), the statistics of desired outputs are given by (2-47) and (2-48), using (2-42) through (2-45) and (2-60).

2.4 Improving Robustness in Continuous-Time Controllers

The stability robustness of LQG controllers is guaranteed assuming that full-state feedback is available. However, once a Kalman filter is inserted into the loop, all guarantees of robustness, such as minimum gain and phase margins, are lost (Ref 6). J.C. Doyle demonstrated this for a simple case of an observer-based controller in Reference 5.

In Reference 6, Doyle and Stein introduced a method for improving the robustness of a control system that employs an observer or state estimator to generate estimates of states when full-state feedback is unavailable. In many practical systems, this is the case. Their method assumes that the linear, time-invariant system to be controlled is observable, controllable and has no transmission zeros in the right-half s-plane, (i.e., it is minimum phase).

Figure (2-3) shows the structures for a full-state feedback controller and an observer-based controller. Doyle and Stein claim that if

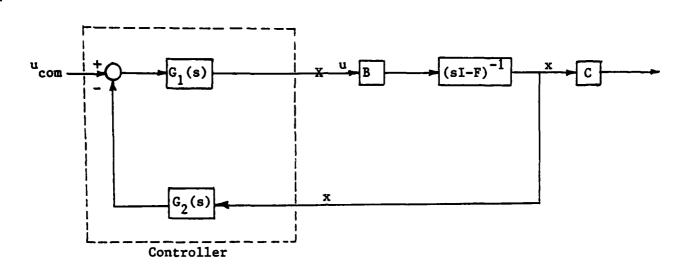


Figure 2-3a: Full-State Feedback System

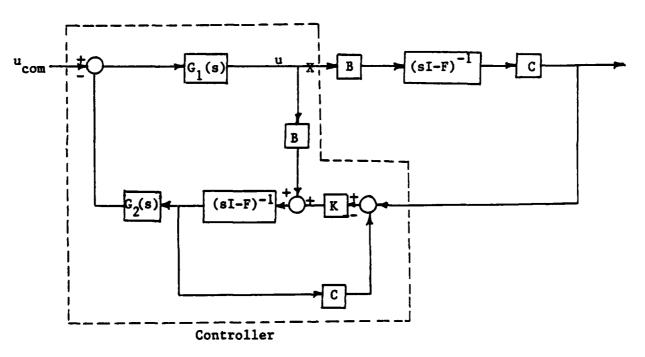


Figure 2-3b: Observer Based Feedback System

the corresponding return-difference mappings are asymptotically equal when the control loops are broken at point x (the point of entry of the control inputs), then the robustness properties of the observer-based controller will asymptotically approach those of the full-state feedback controller.

The return-difference mappings of Figure (2-3) are equal if the observer satisfies the following equation

$$K[I + H(sI-F)^{-1}K]^{-1} = B[H(sI-F)^{-1}B]^{-1}$$
 (2-61)

where H,F, and B are system matrices and K is the observer gain. Let K be parameterized as a function of the scalar variable, q. Equation (2-61) is satisfied asymptotically as q approaches infinity if

$$\frac{K(q)}{q} \longrightarrow BW \qquad (2-62)$$

where W is any nonsingular matrix. If the observer used is Kalman filter, then K(q) becomes the Kalman filter gain

$$K(q) = \overline{P}(q)H^{T}R^{-1}$$
 (2-63)

and $\vec{P}(q)$ replaces in Equation (2-16).

To implement the Doyle and Stein technique, the value of GQG^T in Equation (2-16) must be altered. Let Q_O be the matrix GQG^T of the original system (i.e., let G=I) and O(q) be the modified matrix after the robustification technique is applied. The modified matrix is

$$Q(q) = Q_0 + q^2 B V B^T$$
 (2-64)

where q is the design parameter chosen to reflect the amount of desired robustification and V is a positive definite symmetric matrix. Note that the second term of Equation (2-64) implies adding additional pseudonoise to the system at the point of entry of the control inputs, $\underline{u}(t)$, rather than the point of entry of the dynamic driving noise, $\underline{w}(t)$. As q approaches infinity, the observer-based controller recovers the robustness properties of a full-state feedback controller. Note that if q is zero, Q(q) is the QQG^T matrix of the original system.

2.5 Sampled-Data Controller

For a continuous-time system, represented by Equation (2-1), having sampled-data measurements, an equivalent discrete-time stochastic difference equation (Ref 23:170) can be written as

$$\underline{\mathbf{x}}(t_{i+1}) = \phi(t_{i+1}, t_i) \underline{\mathbf{x}}(t_i) + \mathbf{B}_{\mathbf{d}}(t_i) \underline{\mathbf{u}}(t_i) + \mathbf{G}_{\mathbf{d}}(t_i) \underline{\mathbf{w}}_{\mathbf{d}}(t_i)$$
(2-65)

where $\underline{\mathbf{w}}_{\mathbf{d}}(\mathbf{t}_{\mathbf{i}})$ is a discrete-time white Gaussian noise with statistics

$$E\{\underline{w}_{d}(t_{1})\} = \underline{0}$$
 (2-66a)

$$\mathbb{E}\{\underline{\mathbf{w}}_{\mathbf{d}}(\mathbf{t}_{\mathbf{i}}) \ \underline{\mathbf{w}}_{\mathbf{d}}^{\mathbf{T}}(\mathbf{t}_{\mathbf{i}})\} = \mathbf{Q}_{\mathbf{d}}(\mathbf{t}_{\mathbf{i}})\delta_{\mathbf{i}\mathbf{i}}$$
(2-66b)

and δ_{ij} is the Kronecker delta, equal to one if i=j and zero if i \neq j.

The matrix $\phi(t_{i+1}, t_i)$ is the state transition matrix for the system over a single sample period and $B_d(t_i)$ and $Q_d(t_i)$ are defined in terms of the continuous-time system matrices to be

$$B_{d}(t_{i}) = \int_{t_{i}}^{t_{i+1}} \phi(t_{i+1}, \tau) B(\tau) d\tau$$
 (2-67)

$$Q_{d}(t_{i}) = \int_{t_{i}}^{t_{i+1}} \phi(t_{i+1}, \tau) G(\tau) Q(\tau) G^{T}(\tau) \phi^{T}(t_{i+1}, \tau) d\tau \qquad (2-68)$$

Note that Equation (2-67) inherently assumes $\underline{u}(t)$ is held constant over a sample period, i.e., $\underline{u}(t) = \underline{u}(t_i)$ for all t_i in the interval $[t_i, t_{i+1})$. $G_d(t_i)$ is defined to be an identity matrix I. If, as in the continuous-time controller case, a time invariant system model and stationary noises are assumed, and if in addition a fixed sample period is assumed, the integrations of Equation (2-67) and (2-68) need only be performed once and B_d and Q_d are constant matrices.

A discrete-time cost function similar to that of Equation (2-3) can be generated as

$$J_{c} = E \left\{ \frac{1}{2} \underline{x}^{T}(t_{n+1}) X_{f} \underline{x}(t_{n+1}) + \sum_{i=0}^{n} \frac{1}{2} \begin{bmatrix} \underline{x}(t_{i}) \\ \underline{u}(t_{i}) \end{bmatrix}^{T} \begin{bmatrix} X(t_{i}) & S(t_{i}) \\ S^{T}(t_{i}) & U(t_{i}) \end{bmatrix} \underbrace{\underline{x}(t_{i})}_{\underline{u}(t_{i})} \right\} (2-69)$$

In the above equation, t_n is the last time at which a control is applied. It is assumed that a zero-order-hold is used to interface with the continuous-time system. X_f and $X(t_i)$ are positive semi-definite weighting matrices and $U(t_i)$ is a positive definite weighting matrix. $S(t_i)$ is chosen so that the composite matrix of Equation (2-69) is positive semi-definite. The weighting matrices are again assumed constant henceforth, in order to obtain constant gain control laws eventually.

The LQ optimal full-state feedback control law is given by

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$$u^*(t_i) = -G_c^*(t_i) \underline{x}(t_i)$$
 (2-70)

where $G_c^*(t_i)$ is the solution to the equation

$$G_c^*(t_i) = [U + B_d^T K_c(t_{i+1}) B_d]^{-1} [B_d^T K_c(t_{i+1}) \phi + S^T]$$
 (2-71)

and $K_c(t_i)$ satisfies the backward recursive Riccati difference quation

$$K_c(t_i) = X + \phi^T K_c(t_{i+1}) \phi - [B_d^T K_c(t_{i+1}) \phi + S^T]^T G_c^*(t_i)$$
 (2-72)

subject to the final condition

$$K_c(t_{n+1}) = X_f$$
 (2-73)

As in the case of a continuous-time system having continuous-time measurements, perfect access to all the states usually is not available. Instead, sampled-data measurements may be available in the form of

$$\underline{z}(t_i) = \underline{H} \underline{x}(t_i) + \underline{v}_d(t_i)$$
 (2-74)

where $\underline{\mathbf{v}}_{\mathbf{d}}(\mathbf{t}_{\mathbf{i}})$ is a discrete-time white Gaussian noise assumed independent of dynamics driving noise $\underline{\mathbf{w}}_{\mathbf{d}}(\mathbf{t}_{\mathbf{i}})$ in Equation (2-65), with statistics

$$E\left\{\underline{\mathbf{v}}_{\mathbf{d}}(\mathbf{t}_{\mathbf{i}})\right\} = \underline{\mathbf{0}} \tag{2-75a}$$

$$\mathbb{E}\{\underline{\mathbf{v}}_{\mathbf{d}}(\mathbf{t}_{\mathbf{i}}) \ \underline{\mathbf{v}}_{\mathbf{d}}^{\mathbf{T}}(\mathbf{t}_{\mathbf{j}})\} = \mathbb{R}_{\mathbf{d}} \quad \delta_{\mathbf{i}\mathbf{j}}$$
 (2-75b)

Again, a Kalman filter is employed to generate an estimate of the

conditional mean, $\hat{\underline{x}}(t_i^+)$, and conditional covariance, $P(t_i^+)$, of the states of the system.

The mean and covariance are propagated between sampled times by these equations (Ref 23:217)

$$\hat{x}(t_{i+1}) = \phi \underline{x}(t_i^{\dagger}) + B_d \underline{u}(t_i)$$
 (2-76a)

$$P(t_{i+1}^{-}) = \phi P(t_{i}^{+}) \phi^{T} + G_{d} Q_{d} G_{d}^{T}$$
 (2-76b)

Then, at the sample times when measurements are taken, the mean and covariance are updated by (Ref 23:217)

$$\hat{x}(t_i^+) = \hat{x}(t_i^-) + K(t_i^-) [\underline{z}(t_i^-) - H \underline{\hat{x}}(t_i^-)]$$
 (2-77)

$$P(t_{i}^{+}) = P(t_{i}^{-}) - K(t_{i})H P(t_{i}^{-})$$
 (2-78)

where $K(t_i)$ is the Kalman filter gain, given by

$$K(t_i) = P(t_i^-) H^T [H P(t_i^-) H^T + R_d]^{-1}$$
 (2-79)

The superscripts, - and +, refer to quantities just before and just after the measurements at the samples times are taken, respectively.

The mean and covariance are propagated and updated forward in time by the above discrete-time Kalman filter equations subject to the initial conditions

$$E\{\underline{x}(t_0)\} = \overline{x}_0 \tag{2-80a}$$

$$E\{\left[\underline{x}(t_{o}) - \overline{\underline{x}}_{o}\right]\left[\underline{x}(t_{o}) - \overline{\underline{x}}_{o}\right]^{T}\} = P_{o}$$
 (2-80b)

which are obtained from an a priori Gaussian density function of the states at the initial time, as discussed below Equation (2-13).

As in the continuous-measurement case, it is desired to generate a constant-gain, steady-state LQG controller. Thus, steady-state solutions from Equations (2-72), (2-76b) and (2-78) are desired to generate a constant Kalman filter gain matrix, K, and a constant feedback gain matrix, G_c^* .

The form of the sampled-data controller is shown in Figure (2-4).

2.6 Sampled-Data Performance Analysis

The performance analysis for a sampled-data LQG controller is based on the development in Reference 24:Ch 14.

Similar to Section 2.3, a truth model for a given system is developed which has the following form

$$\underline{\dot{x}}_{t}(t) = F_{t} \underline{x}_{t}(t) + B_{t} \underline{u}(t) + G_{t} \underline{w}_{t}(t)$$
 (2-81a)

$$\underline{z}_{t}(t_{i}) = H_{t} \underline{x}_{t}(t_{i}) + \underline{v}_{dt}(t_{i})$$
 (2-81b)

The measurements are now in sampled-data form, and $\underline{v}_{dt}(t_i)$ is a discrete time white Gaussian noise of covariance R_{dt} .

As shown in Figure (2-5), proposed sampled-data controllers can be inserted into the truth model simulation of the real world and their performance evaluated.

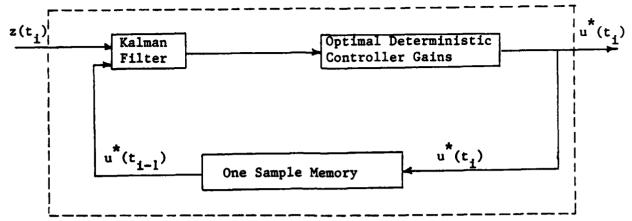


Figure 2-4a: Overall Structure of Sampled-Data LQG Regulator

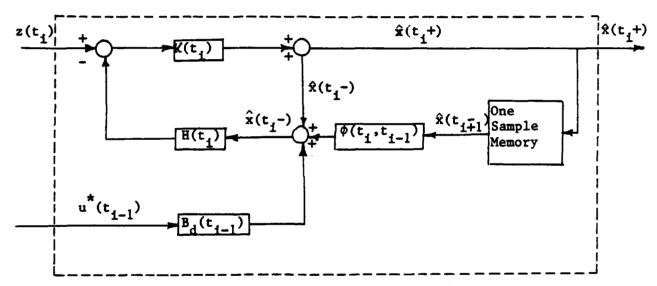
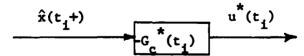


Figure 2-4b: Kalman Filter Block in (A)



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Figure 2-4c: Optimal Deterministic Controller Block in (A)

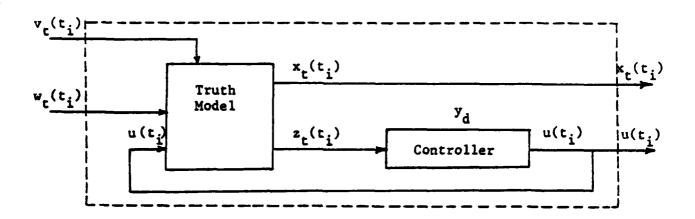


Figure 2-5: Performance Evaluation for Linear Sampled-Data Controller

For each controller, it is desired to evaluate a control law of the generic form

$$\underline{u}(t_{i}) = G_{cx} \underline{x}_{c}(t_{i}) + G_{cz} \underline{z}(t_{i}) + G_{cy} \underline{y}_{d}(t_{i})$$
 (2-82)

where $\underline{u}(t_1)$ uses measurements up to and including the ith measurement and is held constant over the ith sample period. The states of the controller can be propagated by the linear difference equation

$$\underline{x}_{c}(t_{i+1}) = \phi_{c}\underline{x}_{c}(t_{i}) + B_{c}\underline{z}_{c}(t_{i}) + B_{c}\underline{y}_{d}(t_{i})$$
 (2-83)

Note the analogous form of the above two equation to that of Equation (2-25) and (2-26). Expressions for the gains multiplying $\underline{x}_c(t_i)$, $\underline{z}_t(t_i)$ and $\underline{y}_d(t_i)$ are given in Appendix A. Initial conditions for the controller states are usually assumed zero.

The performance of a controller is evaluated by generating time histories of the mean and covariance of the augmented Gaussian vector

$$\underline{y}_{\mathbf{a}}(\mathbf{t}_{\mathbf{i}}) = \begin{bmatrix} \underline{\mathbf{x}}_{\mathbf{t}}(\mathbf{t}_{\mathbf{i}}) \\ \\ \underline{\mathbf{u}}(\mathbf{t}_{\mathbf{i}}) \end{bmatrix}$$
 (2-84)

and the corresponding vector between sample times. This is developed subsequent to a description pertaining to sample times only.

First, as in Section 2.4, it is necessary to evaluate the statistics of a second augmented vector

$$\underline{\mathbf{x}}_{\mathbf{a}}(\mathbf{t}_{\mathbf{i}}) = \begin{bmatrix} \underline{\mathbf{x}}_{\mathbf{t}}(\mathbf{t}_{\mathbf{i}}) \\ \\ \underline{\mathbf{x}}_{\mathbf{c}}(\mathbf{t}_{\mathbf{i}}) \end{bmatrix}$$
 (2-85)

By performing the integrations indicated in Equations (2-67) and (2-68), an equivalent discrete-time equation can be generated for Equation (2-81a). Then by substituting Equations (2-81b) and (2-82) into the equations for the truth model and controller states, Equations (2-81a) and (2-83) can be rewritten as

$$x_{t}(t_{i+1}) = [\phi_{t} + B_{dt}G_{cz}H_{t}] \underline{x}_{t}(t_{i})$$

$$+ B_{dt}G_{cx}\underline{x}_{c}(t_{i}) + B_{dt}G_{cy}\underline{y}_{d}(t_{i})$$

$$+ I \underline{w}_{dt}(t_{i}) + B_{dt}G_{cz}\underline{v}_{dt}(t_{i}) \qquad (2-86)$$

$$\underline{\mathbf{x}}_{c}(t_{i+1}) + \phi_{c}\underline{\mathbf{x}}_{c}(t_{i}) + B_{cz}H_{t}\underline{\mathbf{x}}_{t}(t_{i}) + B_{cy}\underline{\mathbf{y}}_{d}(t_{i}) + B_{cz}\underline{\mathbf{v}}_{dt}(t_{i})$$
(2-87)

The subscript d referes to a discrete quantity,

Form the augmented, stationary, zero-mean white Gaussian noise vector

$$\underline{\mathbf{w}}_{da}(t_i) = \begin{bmatrix} \underline{\mathbf{w}}_{dt}(t_i) \\ \\ \underline{\mathbf{v}}_{dt}(t_i) \end{bmatrix}$$
 (2-88)

with covariance

$$Q_{da} = \begin{bmatrix} Q_{dt} & 0 \\ 0 & R_{dt} \end{bmatrix}$$
 (2-89)

If $\underline{\mathbf{w}}_{dt}(t_i)$ and $\underline{\mathbf{v}}_{dt}(t_i)$ are correlated when off-diagonal terms can be added to Equation (2-89).

Now an augmented system equation can be written by combining Equations (2-86) and (2-87)

$$\underline{\mathbf{x}}_{\mathbf{a}}(\mathbf{t}_{\mathbf{i}+\mathbf{l}}) = \phi_{\mathbf{a}}\underline{\mathbf{x}}(\mathbf{t}_{\mathbf{i}}) + \mathbf{B}_{\mathbf{d}\mathbf{a}}\underline{\mathbf{y}}_{\mathbf{d}}(\mathbf{t}_{\mathbf{i}}) + \mathbf{G}_{\mathbf{d}\mathbf{a}}\underline{\mathbf{w}}_{\mathbf{d}\mathbf{a}}(\mathbf{t}_{\mathbf{i}})$$
 (2-90)

where

$$\phi_{\mathbf{a}} = \begin{bmatrix} \phi_{\mathbf{t}} + B_{\mathbf{dt}} G_{\mathbf{cz}} H_{\mathbf{t}} & B_{\mathbf{dt}} G_{\mathbf{cx}} \\ B_{\mathbf{cz}} H_{\mathbf{t}} & \phi_{\mathbf{c}} \end{bmatrix}$$
(2-91)

$$B_{da} = \begin{bmatrix} B_{dt}^{G} & \\ &$$

$$G_{da} = \begin{bmatrix} I & B_{dt}G_{cz} \\ 0 & B_{cz} \end{bmatrix}$$
 (2-93)

The initial conditions for the augmented system are given by

$$E\{\underline{x}_{a}(t_{o})\} = \begin{bmatrix} \overline{x}_{o} \\ \underline{0} \end{bmatrix} = \overline{x}_{ao}$$
 (2-94)

$$\mathbb{E}\left\{\left[\underline{\mathbf{x}}_{\mathbf{a}}(\mathbf{t}_{0}) - \underline{\mathbf{x}}_{\mathbf{a}0}\right]\left[\underline{\mathbf{x}}_{\mathbf{a}}(\mathbf{t}_{0}) - \underline{\mathbf{x}}_{\mathbf{a}0}^{T}\right]\right\} = \begin{bmatrix} \mathbf{P} & \mathbf{0} \\ & \mathbf{0} \\ \mathbf{0} & \mathbf{0} \end{bmatrix}$$
(2-95)

If desired, a cost function for the augmented system can be formed, as shown in References 24:Ch 14:12.

The mean and covariance of the augmented vector, $\underline{\mathbf{x}}_{\mathbf{a}}(\mathbf{t}_{\mathbf{i}})$ can be propagated by

$$\underline{\underline{m}}_{x_a}(t_i) = \phi_a \underline{\underline{m}}_{x_a}(t_i) + B_{da} \underline{y}_d(t_i)$$
 (2-96)

$$P_{x_a x_a}(t_i) = \phi_a P_{x_a x_a} \phi^T + G_{da} Q_{da} G_{da}$$
 (2-97)

The vector of interest, $\underline{y}_a(t_i)$, is related to $\underline{x}_a(t_i)$ by the following equation

$$\underline{y}_{\mathbf{a}}(t_{\mathbf{i}}) = \begin{bmatrix} \underline{x}_{\mathbf{t}}(t_{\mathbf{i}}) \\ \\ \underline{u}(t_{\mathbf{i}}) \end{bmatrix} = \begin{bmatrix} \mathbf{I} & \mathbf{0} \\ \\ \\ \mathbf{G}_{\mathbf{c}z}\mathbf{H}_{\mathbf{t}} & \mathbf{G}_{\mathbf{c}z} \end{bmatrix} \begin{bmatrix} \underline{x}_{\mathbf{t}}(t_{\mathbf{i}}) \\ \\ \underline{x}_{\mathbf{c}}(t_{\mathbf{i}}) \end{bmatrix}$$

$$+ \begin{bmatrix} 0 \\ \\ G_{cy} \end{bmatrix} \underline{y}_{d}(t_{i}) + \begin{bmatrix} 0 \\ \\ G_{cz} \end{bmatrix} \underline{v}_{dt}(t_{i}) \qquad (2-98)$$

and the desired statistics are therefore generated by

$$\underline{\underline{\mathbf{m}}}_{ya}(t_i) = \begin{bmatrix} \mathbf{I} & \mathbf{0} \\ \\ \\ \mathbf{G}_{cz}^{H}_{t} & \mathbf{G}_{cx} \end{bmatrix} \underline{\underline{\mathbf{m}}}_{x_a}(t_i) + \begin{bmatrix} \mathbf{0} \\ \\ \\ \mathbf{G}_{cy} \end{bmatrix} \underline{\underline{\mathbf{y}}}_{d}(t_i)$$
 (2-99)

$$P_{y_a y_a}(t_i) = \begin{bmatrix} I & 0 \\ & & \\ G_{cz}H_t & G_{cx} \end{bmatrix} P_{x_a x_a}(t_i) \begin{bmatrix} I & 0 \\ & & \\ G_{cz}H_t & G_{cx} \end{bmatrix}^T$$

$$+ \begin{bmatrix} 0 \\ G_{cz} \end{bmatrix} R_{dt} \begin{bmatrix} 0 & G_{cz}^{T} \end{bmatrix}$$
 (2-100)

Equations (2-99) and (2-100) provide an efficient means for evaluating statistics at the sample times via the equivalent discrete-time system model. However, it may be desired to obtain more complete results between sample times, to ensure that adequate sample period choice and

system control have been achieved. Between sample instants, a differential equation for $\underline{y}_a(t)$ can be written as

$$\dot{\underline{y}}_{\mathbf{a}}(t) = \begin{bmatrix} \mathbf{f}_{t} & \mathbf{B}_{t} \\ & & \\ 0 & 0 \end{bmatrix} \underline{y}_{\mathbf{a}}(t) + \begin{bmatrix} \mathbf{G}_{t} \\ & \\ 0 \end{bmatrix} \underline{\mathbf{w}}_{\mathbf{t}}(t) \tag{2-101}$$

and the mean and covariance can be propagated from t_i to t_{i+1} , where $\underline{u}(t_i)$ undergoes a step change, using the initial conditions given by Equations (2-90) and (2-91). The propagation equations are

$$\frac{\mathbf{m}_{\mathbf{y}_{\mathbf{a}}}(\mathbf{t}) = \begin{bmatrix} \mathbf{F}_{\mathbf{t}} & \mathbf{B}_{\mathbf{t}} \\ & & \\ \mathbf{0} & \mathbf{0} \end{bmatrix} \underline{\mathbf{m}}_{\mathbf{y}_{\mathbf{a}}}(\mathbf{t}) \tag{2-102}$$

$$\dot{P}_{y_a y_a}(t) = \begin{bmatrix} F_t & B_t \\ & & \\ 0 & 0 \end{bmatrix} P_{y_a y_a}(t) + P_{y_a y_a}(t) \begin{bmatrix} F_t & B_t \\ & & \\ 0 & 0 \end{bmatrix}^T$$

$$+ \begin{bmatrix} GQG^T & 0 \\ & & \\ & & \\ & & \\ & & & \\$$

(I

At this point, all quantities of interest have been defined to evaluate the performance of a sampled-data controller. The primary results are that for a truth model given by (2-81) and a controller of the form (2-82) and (2-83), the statistics of desired outputs at the sample times are given by (2-99) and (2-100). Between sample times the statistics are given by (2-102) and (2-103).

2.7 Improving Robustness in Discrete-Time Systems

Three approaches are taken to apply the robustification technique described in Section 2.3 to sampled-data controllers. The first is simply to discretize the LQG controller designed for the continuous-time, continuous-measurement system. The second approach is to extend the technique of adding pseudonoise to the points of entry of <u>u</u> to a sampled-data system by making a first order (or better) approximation to the modified Q matrix. The third is to apply the fundamental conditions under which full-state feedback characteristics are obtained asymptotically from a controller with a filter or observer in the loop.

It has been observed in Reference 21 that, unlike the continuousmeasurement case, the scalar parameter q of Equation (2-64) cannot be adjusted arbitrarily upwards for the discrete-time case. Rather, there is a finite range of values for q that will robustify the Kalman filter, and beyond that range the closed-loop system is unstable.

2.7.1 Discretizing the Continuous-Time LQG Controller

The required format for the discretized controller is given by Equation (2-82) which requires values for $G_{\rm cx}(t_{\rm i})$, $G_{\rm cz}(t_{\rm i})$ and $G_{\rm cy}(t_{\rm i})$, and by Equation (2-83) which requires values for $\phi_{\rm c}(t_{\rm i+1},t_{\rm i})$, $B_{\rm cz}(t_{\rm i})$ and $B_{\rm cy}(t_{\rm i})$. Recall that the continuous-time controller equations are expressed as

$$\underline{\mathbf{u}}(t) = \mathbf{G}_{cx}(t) \, \underline{\mathbf{x}}_{c}(t) + \mathbf{G}_{cx}(t) \, \underline{\mathbf{z}}(t) + \mathbf{G}_{cy}(t) \, \underline{\mathbf{y}}_{d}(t) \qquad (2-104)$$

$$\underline{x}_{c}(t) = F_{c}(t) \underline{x}_{c}(t) + B_{cz}(t) \underline{z}(t) + B_{cy}(t) \underline{y}_{d}(t)$$
(2-105)

In Appendix A, it is shown that for a steady-state constant-gain LQG regulator

$$G_{cx}(t) = G_{c}^{*}$$
 (2-106a)

$$G_{cz}(t) = 0$$
 (2-106b)

$$G_{cy}(t) = 0$$
 (2-106c)

$$F_c(t) = F - BG_c^* - KH$$
 (2-106d)

$$G_{cz}(t) = K$$
 (2-106e)

$$B_{cy}(t) = 0$$
 (2-106f)

For this problem, $G_c^*(t)$ is a constant value G_c^* , and thus the discretized control law is given by

$$\underline{\mathbf{u}}(\mathbf{t_i}) = -\mathbf{G_c}^* \underline{\mathbf{x}_c}(\mathbf{t_i}) \tag{2-107}$$

To obtain a discrete propagation equation for the controller states, first-order approximations for $\phi_c(t_{i+1},t_i)$, $B_{cz}(t_i)$ and $B_{cy}(t_i)$ are obtained by

$$\phi_c(t_{i+1}, t_i) = [I + F_c(t_i)\Delta t]$$
 (2-108a)

$$B_{czd}(t_i) = B_{cz}(t_i)\Delta t \qquad (2-108b)$$

$$B_{cyd}(t_i) = B_{cy}(t_i)\Delta t \qquad (2-108c)$$

Again, for this thesis, the system is assumed time invariant and F_c , B_{cz} , and B_{cy} are constant matrices. They are evaluated explicitly in Appendix A. The quantity Δt is the sample period for the sampled-data system. Higher order approximations are also possible, but if Δt is not sufficiently small compared to the transient times of the system, this basic idea breaks down anyway, so its use is confined to problems with short sample periods

In addition, a discrete approximation for $R_{\rm dt}(t_{\rm i})$ is needed for use in the performance analysis described in Section 2.6. If the sample time is sufficiently small to allow the approximations in Equation (2-108), then it is reasonable to make a first-order approximation for the discrete measurement noise covariance $R_{\rm dt}(t_{\rm i})$. This is given by

$$R_{dt}(t_i) = R_t(t_i)/\Delta t \qquad (2-109)$$

Notice that as Δt --> 0, the discrete-time white noise $\underline{\mathbf{v}}_{dt}(t_i)$ of Equation (2-81b) converges to the continuous-time white noise described by (2-18) and (24) if (2-109) is satisfied throughout the limiting process.

2.7.2 Doyle and Stein Technique for Sampled-Data Systems

The second approach to enhancing robustness is to extend the Doyle and Stein technique and apply it directly to a sampled-data controller. Several ways of accomplishing this are considered.

If the sampled period of the system is sufficiently small, a first-order approximation for the discrete-time noise strength matrix $Q_{\underline{d}}(q)$,

can be made which is the discrete counterpart for Equation (2-64). This yields

$$Q_d(q) + Q_{do} + q^2 BVB^T \Delta t$$
 (2-110)

where Q_{do} is

$$Q_{do} = Q_{d}(t_{i}) \tag{2-111}$$

which is defined in Equation (2-68). Again, this implies that $G_d = I$.

For larger sample times, a first-order approximation may not be sufficient. If this is the case, subintervalling may be considered a higher order approximation for $Q_d(q)$, such as

$$Q_{d}(q) = \frac{1}{2} [\phi Q(q) + Q(q)\phi^{T}] \Delta t$$
 (2-112)

as given in Reference 24:172.

Another alternative is to make the return-difference mapping for the observer-based controller asymptoically equal to that of the full-state feedback controller in the discrete-time case. The two configurations are shown in Figure (2-6). The observer-based system is based upon the sub-optimal control law

$$\underline{\mathbf{u}}(\mathbf{t_i}) = -\mathbf{G_c}^* \, \hat{\underline{\mathbf{x}}}(\mathbf{t_i}^-) \tag{2-113}$$

rather than the law given by Section 2.5 using $\hat{\underline{x}}(t_i^+)$.

To recover the robustness properties of the full-state feedback system, $[\phi K]$ must be found such that

$$\phi K[I + H(zI - \phi)^{-1}\phi K]^{-1} = B_d[H(zI - \phi)^{-1}B_d]^{-1} \qquad (2-114)$$

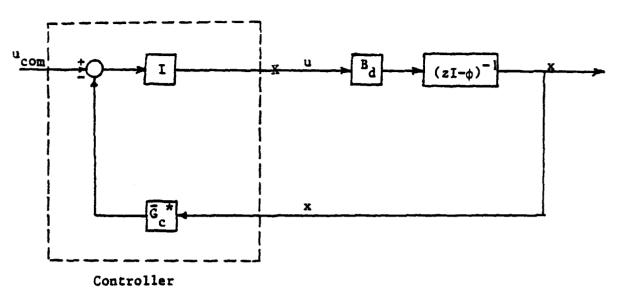


Figure 2-6a: Full-State Feedback System

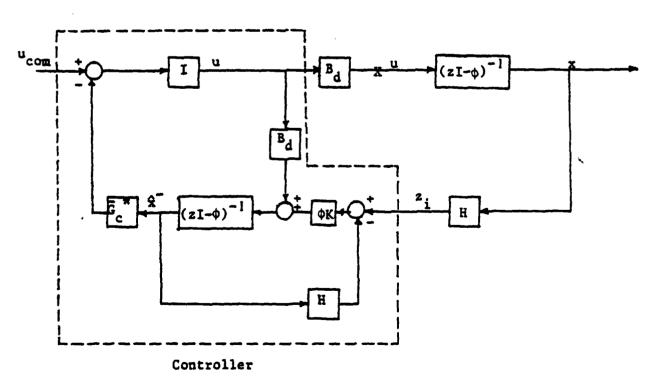


Figure 2-6b: Observer-Based Feedback System

where the analysis is carried out in the z-domain. Equation (2-114) is satisfied asymptotically when the Kalman filter gain, K, is parameterized as K(q), and

$$\lim_{q \to \infty} \frac{\phi K}{q} = B_d W \qquad (2-115)$$

where W is a nonsingular m x m matrix. Therefore, for finite values of q, K is given by

$$K = q\phi^{-1} B_d W$$
 (2-116)

Unfortunately, this does not lend itself to an interpretation of retuning via pseudonoise addition, as in the continuous-time case.

Reference 24:113-114 suggests looking at the dual state equations to select W. This yields

$$W = [H \phi^{-1} B_d]^{-1}$$
 (2-117)

which assigns m eigenvalues of the closed loop dual system to the origin and the remaining (n-m) eigenvalues to the invariant zeros of the system where n is the number of states and m is the number of controls.

To use the performance analysis equations, the sub-optimal control must be put into the generic format of Equations (2-82) and (2-83).

This is shown explicitly in Appendix A.

2.8 Summary

The preceding sections have presented the equations for designing and evaluating optimal LQG regulators. Three applications are considered:

a continuous-time controller, a discretized continuous-time controller and a sampled-data controller. The structure of these controllers was examined with and without a Kalman filter in the loop to estimate states.

For the case where a Kalman filter is necessary to estimate states, a technique was presented to robustify a controlled system against differences that exist between the controller design model and the real world system. The technique was developed for a continuous-time system and several extensions to discrete-time systems were presented.

A disadvantage of the type of controller considered in this chapter is that it will not regulate the states to zero in the face of unmodeled disturbances. Also, it only regulates the deviations in the states from an equilibrium position and does not allow the system to track a desired piecewise constant non-zero input. Chapter III presents the development for a type of controller that does exhibit these characteristics, based on an LQG methodology.

III. PI CONTROLLERS

3.1 Introduction

This chapter presents the equations used for designing Proportional-plus-Integral (PI) controllers for a system modeled as linear, time-invariant, and driven by stationary white Gaussian noise and deterministic inputs. The model used for this thesis is described in Chapter V.

The advantage of a PI controller over the regulator described in Chpater II is that, in the absence of stochastic inputs, it will maintain the system output at some nonzero commanded value with zero steadystate error, even in the presence of unmodeled constant disturbances. This is known as a "Type-1" property (Ref 4). This property is achieved by integration of the error in the controlled variables, i.e., integration of the difference between achieved and desired values of the controlled variables. In discrete-time feedback control, the PI effect is achieved by performing summation (or pseudo-integration, often interpreted as Euler integration) on either the difference between the actual and desired system outputs (regulation error). In this thesis, this structure is obtained via LQG synthesis applied to an augmented system composed of the original system states and the controls (Ref 24:141-150). Two possible implementations are "position form" and "incremental form". In position form, the control $\underline{u}(t_4)$ is specified in terms of the current position of the system state, $\underline{x}(t_i)$, as in the LQ regulator solution of the previous chapter. In incremental form, only changes in states and commands from the previous values are used to generate increments in control relative to the value at the previous sample time. For implemention, an incremental form PI controller is generally preferable because it is not necessary to provide initial

values for the controller states as in the position form. Also it lends iteself more readily to relinearizations about new nominal values and to anti-windup compensation (Ref 24).

The optimal deterministic (LQ) PI controller is developed in the first section of this chapter for a sampled-data system. Next, the Doyle and Stein technique is applied to a PI controller. Then the controller is put into the generic format presented in Chapter II, with a Kalman filter in the loop to provide estimates of the states to the controller. Once the generic form is available, the performance of the controller may be evaluated using the method of the previous chapter.

The software developed to design optimal PI controllers is described in Reference 13. Modifications to the software are described in References 26, 27 and 29. The performance analysis software is described in Reference 29. The above references deal primarily with the design of controllers that employ a PI regulator in the inner feedback loop and a Command Generator Tracker (CGT) to provide inputs to the system (Ref 12). This chapter contains the development of only the inner loop PI regulator.

3.2 Sampled-Data PI controller

The following development for a PI controller, based on augmentation to the original system state relations of equations for pseudo-integration of the control input rates, is found in Reference 24:Ch 14.

3.2.1 Control-Rate Pseudo Integration

Recall from Chapter II that an equivalent discrete-time difference equation can be generated for the continuous-time system model in the form of

$$\underline{\mathbf{x}}(\mathbf{t}_{i+1}) = \phi \underline{\mathbf{x}}(\mathbf{t}_i) + \mathbf{B}_d \underline{\mathbf{u}}(\mathbf{t}_i)$$
 (3-1)

where, by the certainty equivalence principle (Ref 24:Ch 13), the noise vector was deleted.

Define the perturbation state and control variables to be

$$\delta \underline{\mathbf{x}}(\mathbf{t}_1) = \underline{\mathbf{x}}(\mathbf{t}_1) - \underline{\mathbf{x}}_0 \tag{3-2a}$$

$$\delta \underline{u}(t_1) = \underline{u}(t_1) - \underline{u}_0 \tag{3-2b}$$

where $\underline{\mathbf{x}}_0$ and $\underline{\mathbf{u}}_0$ are the nominal values of the states and the controls to maintain the system at its equilibrium "trim" operating condition such that controlled variables assume the desired values. If an equation for the output of the system is given by

$$\underline{y}(t_i) = \underline{C}\underline{x}(t_i) + \underline{D}_{\underline{v}}\underline{u}(t_i)$$
 (3-3)

then the nominal control, \underline{u}_0 , to hold the system at that equilibrium operating point is found as the solution to

$$\underline{\mathbf{x}}_{\mathbf{o}} = \phi \underline{\mathbf{x}}_{\mathbf{o}} + \mathbf{B}_{\mathbf{d}} \ \underline{\mathbf{u}}_{\mathbf{o}} \tag{3-4a}$$

$$\underline{y}_{d} = \underline{C}\underline{x}_{o} + \underline{D}_{y} \underline{u}_{o} \tag{3-4b}$$

or

$$\begin{bmatrix} \underline{O} \\ \underline{Y}_{d} \end{bmatrix} = \begin{bmatrix} (\phi-1) & B_{d} \\ C & D_{y} \end{bmatrix} \begin{bmatrix} \underline{x}_{o} \\ \underline{u}_{o} \end{bmatrix}$$
(3-5)

where \underline{y}_{1} is the desired system output. Then, (3-5) can be solved as

$$\begin{bmatrix} \underline{\mathbf{x}}_{\mathbf{0}} \\ \underline{\mathbf{u}}_{\mathbf{0}} \end{bmatrix} = \begin{bmatrix} (\phi - \mathbf{I}) & \mathbf{B}_{\mathbf{d}} \\ & & \\ \mathbf{C} & \mathbf{D}_{\mathbf{y}} \end{bmatrix}^{-1} \begin{bmatrix} \underline{\mathbf{0}} \\ & \\ \underline{\mathbf{y}}_{\mathbf{d}} \end{bmatrix} = \begin{bmatrix} \pi_{11} & \pi_{12} \\ & \\ \pi_{21} & \pi_{22} \end{bmatrix} \begin{bmatrix} \underline{\mathbf{0}} \\ & \\ \underline{\mathbf{y}}_{\mathbf{d}} \end{bmatrix}$$
(3-6)

or

$$\frac{x}{0} = \pi_{12} \frac{y}{d}$$
 $\frac{u}{0} = \pi_{22} \frac{y}{d}$ (3-7)

The difference in perturbation control variable is

$$\delta \underline{\underline{u}}(t_{i+1}) - \delta \underline{\underline{u}}(t_i) = [\underline{\underline{u}}(t_{i+1}) - \underline{\underline{u}}_0] - [\underline{\underline{u}}(t_i) - \underline{\underline{u}}_0]$$
 (3-8)

or, equivalently

$$\delta \underline{\underline{u}}(t_{i+1}) = \delta \underline{\underline{u}}(t_i) + [\underline{\underline{u}}(t_{i+1}) - \underline{\underline{u}}(t_i)]$$
 (3-9)

The above equation has the form of an update relation for $\delta \underline{u}(t_{i+1})$. If the second term is thought of as an Euler integration of the time rate-of-change of the control input \underline{u} at time t_i , then the change in \underline{u} , i.e., the bracketed term in Equation (3-9), can be written as

$$\Delta \underline{\underline{u}}(t_i) = \left[\underline{\underline{u}}(t_{i+1}) - \underline{\underline{u}}(t_i)\right] = \underline{\underline{u}}(t_i)\Delta t$$
 (3-10)

where Δt is the sample time of the controller. Thus, $\Delta \underline{u}(t_i)$ is termed the control pseudo-rate and Equation (3-9) becomes

$$\delta \underline{u}(t_{i+1}) = \delta \underline{u}(t_i) + \Delta \underline{u}(t_i)$$
 (3-11)

At this point, an augmented state description can be written using Equations (3-1) and (3-11) for the perturbation variables $\delta \underline{x}(t_1)$ and $\delta \underline{u}(t_1)$:

$$\begin{bmatrix} \delta_{\underline{x}}(\mathbf{t_{i+1}}) \\ \delta_{\underline{u}}(\mathbf{t_{i+1}}) \end{bmatrix} = \begin{bmatrix} \phi & B_d \\ & & \\ & & \\ & & \\ \end{bmatrix} \begin{bmatrix} \delta_{\underline{x}}(\mathbf{t_i}) \\ & & \\ & & \\ \end{bmatrix} + \begin{bmatrix} 0 \\ & \\ \Delta_{\underline{u}}(\mathbf{t_i}) \end{bmatrix} \Delta_{\underline{u}}(\mathbf{t_i})$$
(3-12)

The control pseudo-rate is now considered to be the input to this augmented perturbation state equation.

3.2.2 Optimal Regulator Solution

The optimal regulator solution described in Section 2.5 can now be applied to the augmented system above, subject to a quadratic cost criterion

$$J_{c} = \frac{1}{2} \begin{bmatrix} \delta \underline{x}(t_{N+1}) \\ \delta \underline{u}(t_{N+1}) \end{bmatrix} \quad \begin{bmatrix} X_{f} & 0 \\ 0 & 0 \end{bmatrix} \quad \begin{bmatrix} \delta \underline{x}(t_{N+1}) \\ \delta \underline{u}(t_{N+1}) \end{bmatrix}$$

$$+\frac{1}{2} \begin{bmatrix} \delta \underline{\mathbf{x}}(\mathbf{t_i}) \\ \delta \underline{\mathbf{u}}(\mathbf{t_i}) \\ \delta \underline{\mathbf{u}}(\mathbf{t_i}) \end{bmatrix}^{T} \begin{bmatrix} \mathbf{x_{11}} & \mathbf{x_{12}} & \mathbf{s_1} \\ \mathbf{x_{12}}^{T} & \mathbf{x_{22}} & \mathbf{s_2} \\ \mathbf{s_1}^{T} & \mathbf{s_2}^{T} & \mathbf{U} \end{bmatrix} \begin{bmatrix} \delta \underline{\mathbf{x}}(\mathbf{t_i}) \\ \delta \underline{\mathbf{u}}(\mathbf{t_i}) \\ \delta \underline{\mathbf{u}}(\mathbf{t_i}) \end{bmatrix} (3-13)$$

where X_{11} places a weighting on state deviations away from the nominal \underline{x}_0 , X_{22} places a weighting on control deviations away from \underline{u}_0 , and U places a weighting on the control pseudo-rates, $\Delta\underline{u}(t_1)$. Notice that this term allows the designer to place a weighting on the rate of change of control inputs, i.e., to guard against commanding actuator rates that are beyond the physical limits of the actuators.

The term X_f applies a weighting on deviations of the states at the final time. The cross-terms X_{12} , S_1 and S_2 arise as the continuous-time cost is converted to a discrete-time cost, as demonstrated in Reference 24 and 12. In Equation (3-13), notice that the index for the summation begins at -1. This places a weighting on the potentially large control differences which may occur at the initial time due to a change in the setpoint (Ref 24:142).

To apply the optimal regulator solution to Equations (3-12) and (3-13), redefine the matrices as follows

$$\phi_{\delta} = \begin{bmatrix} \phi & B_{d} \\ 0 & I \end{bmatrix}$$
 (3-14)

$$\mathbf{B}_{\mathbf{d}} = \begin{bmatrix} \mathbf{0} \\ \\ \mathbf{I} \end{bmatrix} \tag{3-15}$$

$$\delta \underline{\mathbf{x}}_{\delta} = \begin{bmatrix} \delta \underline{\mathbf{x}} \\ \\ \delta \underline{\mathbf{u}} \end{bmatrix}$$
 (3-16)

$$\mathbf{x}_{\mathbf{f}\delta} = \begin{bmatrix} \mathbf{x}_{\mathbf{f}} & \mathbf{0} \\ \mathbf{0} & \mathbf{0} \end{bmatrix} \tag{3-17}$$

$$X_{\delta} = \begin{bmatrix} X_{11} & X_{12} \\ & & \\ X_{12}^{T} & X_{22} \end{bmatrix}$$
 (3-18)

$$s_{\delta} = \begin{bmatrix} s_1 \\ s_2 \end{bmatrix}$$

Thus, the state equation and cost function become

$$\delta \underline{\mathbf{x}}_{\delta} (\mathbf{t}_{i+1}) = \phi_{\delta} \delta \underline{\mathbf{x}}_{\delta} (\mathbf{t}_{i}) + \mathbf{B}_{\delta} \Delta \underline{\mathbf{u}} (\mathbf{t}_{i})$$
 (3-20)

$$J_{c} = \frac{1}{2} \delta \underline{x}_{\delta}^{T}(t_{N+1}) X_{f\delta} \delta \underline{x}_{\delta}(t_{N+1})$$

$$+\frac{1}{2} \sum_{\mathbf{i}=-1}^{N} \begin{bmatrix} \delta_{\underline{x}} \delta(\mathbf{t_i}) \\ \Delta_{\underline{u}}(\mathbf{t_i}) \end{bmatrix}^{\underline{T}} \begin{bmatrix} \mathbf{x}_{\delta} & \mathbf{s}_{\delta} \\ \mathbf{s}_{\delta}^{\underline{T}} & \mathbf{v} \end{bmatrix} \begin{bmatrix} \delta_{\underline{x}} \delta(\mathbf{t_i}) \\ \delta_{\underline{u}}(\mathbf{t_i}) \end{bmatrix}$$
(3-21)

Then, the optimal, constant-gain LQ regulator solution is given by

$$\Delta \underline{u}(t_i) = -G_c^* \delta \underline{x}_\delta(t_i)$$
 (3-22)

where

$$G_c^* = [G_{c_1}^* \ G_{c_2}^*] = [U + B_{\delta}^T \bar{K}_c B_{\delta}]^{-1} [B_{\delta}^T \bar{K}_c \phi_{\delta} + S_{\delta}^T]$$
 (3-23)

and \overline{K}_{C} is the steady-state solution to the backward Riccati difference equation

$$K_c(t_i) = X_\delta + \phi_\delta^T K_c(t_{i+1}) [\phi_\delta - B_\delta G_c^*] - S_\delta^G G_c^*$$
 (3-24)

solved backwards from the terminal condition

$$K_{c}(t_{N+1}) = X_{f\delta}$$
 (3-25)

The optimal control input is given by Equation (3-22) in partitioned form as

$$\Delta \underline{\underline{u}}^*(t_i) = -G_{c_1}^* \delta \underline{\underline{x}}(t_i) - G_{c_2}^* \delta \underline{\underline{u}}(t_i)$$
 (3-26)

Combining this with Equation (3-11) yields

$$\delta \underline{\underline{u}}^*(t_{i+1}) = \delta \underline{\underline{u}}^*(t_i) - [G_{c_1}^* \quad G_{c_2}^*] \begin{bmatrix} \delta \underline{\underline{x}}(t_i) \\ \delta \underline{\underline{u}}^*(t_i) \end{bmatrix}$$
(3-27)

Unfortunately, the above control law does not achieve the desired Type 1 property.

3.3 Achieving Type-1 Control

The desired integral characteristics for the controller can be achieved by manipulation into the form of a continuous-time PI controller (Ref 1)

$$\underline{u}^{*}(t) = -K_{\underline{x}}\underline{x}(t) + K_{\underline{z}} \int_{t_{o}}^{t} [\underline{y}_{d} - \underline{y}(\tau)] d\tau$$
 (3-28)

where y_d is the desired output and y(t) is the actual system output defined by

$$\underline{y}(t) = C\underline{x}(t) + D_{\underline{y}}\underline{u}(t)$$
 (3-29)

A discrete-time equivalent is given by

$$\underline{\mathbf{u}}^{*}(t_{\mathbf{i}}) = -K_{\mathbf{x}}\underline{\mathbf{x}}(t_{\mathbf{i}}) + K_{\mathbf{z}} \quad \begin{array}{c} \mathbf{i} - 1 \\ \Sigma \\ \mathbf{j} = -1 \end{array} \left[\underline{\mathbf{y}}_{\mathbf{d}} - \underline{\mathbf{y}}(t_{\mathbf{j}}) \right] \quad (3-30)$$

In incremental form, the above equation is expressed as

$$\underline{u}^{*}(t_{i+1}) = \underline{u}^{*}(t_{i}) - K_{x}[\underline{x}(t_{i+1}) - \underline{x}(t_{i})] + K_{z}[\underline{y}_{d} - \underline{y}(t_{i})]$$
(3-31)

Define a perturbation output equation as

$$\delta \underline{y}(t_i) = \underline{y}(t_i) - \underline{y}_d = C\delta \underline{x}(t_i) + D_y \delta \underline{u}(t_i)$$
 (3-32)

and the control law as

$$\delta \underline{\underline{u}}^*(t_{i+1}) = \delta \underline{\underline{u}}^*(t_i) - K_{\underline{x}}[\delta \underline{\underline{x}}(t_{i+1}) - \delta \underline{\underline{x}}(t_i)]$$

$$- K_{\underline{z}}[C\delta \underline{\underline{x}}(t_i) + D_{\underline{v}}\delta \underline{\underline{u}}(t_i)]$$
(3-33)

The above equation can be rewritten using Equation (3-9) as

$$\delta \underline{\underline{u}}^{*}(t_{i+1}) = \delta \underline{\underline{u}}^{*}(t_{i}) - [K_{x} \quad K_{z}] \begin{bmatrix} (\phi-I) & B_{d} \\ & & \\ C & D_{y} \end{bmatrix} \begin{bmatrix} \delta \underline{\underline{x}}(t_{i}) \\ \delta \underline{\underline{u}}(t_{i}) \end{bmatrix}$$
(3-34)

Equating Equations (3-34) and (3-27), it is seen that

$$[K_{x} \quad K_{z}] = [G_{c_{1}}^{*} \quad G_{c_{2}}^{*}] \begin{bmatrix} (\phi-I) & B_{d} \\ & & \\ & & \\ & & \end{bmatrix}$$
 (3-35)

$$\begin{bmatrix} K_{x} & K_{z} \end{bmatrix} = \begin{bmatrix} G_{c_{1}}^{*} & G_{c_{2}}^{*} \end{bmatrix} \begin{bmatrix} \pi_{11} & \pi_{12} \\ & & \\ & & \\ & & \\ & & & \\$$

The values for the feedback gains K_{x} and K_{z} are thus defined by

$$K_{x} = G_{c_{1}}^{*} \pi_{11} + G_{c_{2}}^{*} \pi_{21}$$
 (3-37a)

$$K_z = G_{c_1}^* \pi_{12} + G_{c_2}^* \pi_{22}$$
 (3-37b)

once $G_{c_1}^{}$ and $G_{c_2}^{}$ are available from the augmented state regulator solution and π_{11} , π_{12} , π_{21} , and π_{22} are obtained from Equation (3-35) and (3-36). The final form for the PI cotroller which achieves Type-1 control, implemented in incremental form is

$$\delta \underline{\underline{u}}^{*}(t_{i+1}) = \delta \underline{\underline{u}}^{*}(t_{i}) - K_{x}[\delta \underline{x}(t_{i+1}) - \delta \underline{x}(t_{i})]$$

$$+ K_{z}[\underline{y}_{d}(t_{i+1}) - \underline{y}(t_{i})]$$
(3-38)

Notice that the different time arguments on the \underline{y} terms are correct (Ref 24:147).

3.4 Doyle and Stein Technique for PI Controllers

The technique of injecting white input noise into a controlled system is accomplished for a sampled-data PI controller in a manner similar to that described in Section 2.7.2 for a sampled-data LQ regulator.

The equivalent discrete-time, stochastic difference equation to describe the system to be controlled is given by

$$\underline{\mathbf{x}}(t_{i+1}) = \phi \underline{\mathbf{x}}(t_i) + B_d \underline{\mathbf{u}}(t_i) + G_d \underline{\mathbf{w}}_d(t_i)$$
 (3-39)

where the noise vector has now been included. The discrete-time input vector, $\mathbf{B}_{\mathbf{d}}$, and the noise covariance, $\mathbf{Q}_{\mathbf{d}}$, are formed by solving the following equations

$$B_{d} = \int_{t_{i}}^{t_{i+1}} \phi(t_{i+1} - \tau) B d\tau$$
 (3-40)

$$Q_{d} = \int_{t_{i}}^{t_{i+1}} \phi(t_{i+1} - \tau) \ GQG^{T} \ \phi^{T}(t_{i+1} - \tau) \ d\tau$$
 (3-41)

where $Q_d = E(\underline{w}_d(t_i)\underline{w}_d^T(t_i))$. G_d is now defined to be the identify matrix, I.

Recall from Chapter II that input noise was added to the system by modifying the $\mathbf{Q}_{\mathbf{d}}$ matrix via

$$Q_d(q) = Q_{dQ} + q^2 B V B^T \Delta t \qquad (3-42)$$

where Q_{do} is now the original noise covariance given in Equation (3-40), B is the input vector from the continuous-time state differential equation, q^2 is a scalar design parameter which adjusts the strength of the input noise, and Δt is the sample time of the discrete controller. This, in effect, makes a first-order approximation to the discrete-time input noise.

However, the discrete-time input vector is available from Equation (3-40) and is approximated to first order by $B_d = B\Delta t$, and so it will be

used to modify the $\mathbf{Q}_{\mathbf{d}}$ matrix for PI controllers. The resulting modified noise covariance matrix is

$$Q_d(q) = Q_{do} + q^2 B_d V B_d^T / \Delta t$$
 (3-43)

where V is a nonsingular matrix, chosen to be the identity matrix for this thesis. Notice that the Kalman filter design is the same regardless of the type of controller implemented so that robustification would be accomplished in the same manner as described in Chapter II. The structure of the sampled-data PI controller is shown in Figure (3-1). The Kalman filter of Figure (3-1) is the same as for the LQG regulator shown in Figure (2-4).

3.5 Performance Analysis for PI Controllers

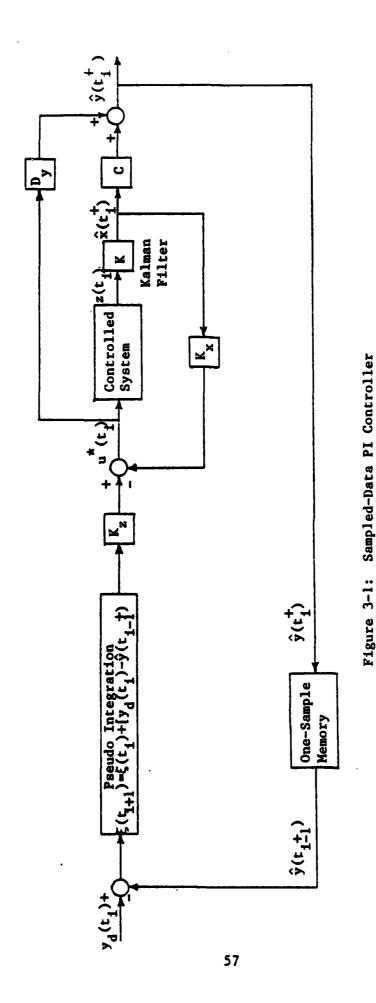
The performance analysis for a PI controller is accomplished by following the same procedure given in Section 2.6 for LQ regulators. As given in Equation (3-38), the incremental form for the optimal, deterministic PI control law is given by

$$\delta \underline{\underline{u}}^{*}(t_{i+1}) = \delta \underline{\underline{u}}^{*}(t_{i}) - K_{x} [\delta \underline{x}(t_{i+1}) - \delta \underline{x}(t_{i})]$$

$$+ K_{z} [\underline{y}_{d}(t_{i+1}) - \underline{y}(t_{i})]$$
(3-44)

Again, the differing time arguments on the y terms are correct.

When a Kalman filter is employed to estimate states for the controller, the conditional mean and covariance of the states are propagated between sample times by Equations (2-76a) and (2-76b). At the sample times, when measurements become available, the conditional mean and



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covariance are updated by Equations (2-77) and (2-78), where the Kalman filter gain is given in Equation (2-79). Using the control law of Equation (3-44) and the Kalman filter equations, the PI controller can be put into the generic format introduced in Equation (2-82) and (2-83):

$$\underline{u}^{*}(t_{i+1}) + G_{cx} \underline{x}_{c}(t_{i}) + G_{cz} \underline{z}(t_{i}) + G_{cy} \underline{y}_{d}(t_{i})$$
 (3-45a)

$$\underline{\mathbf{x}}_{\mathbf{c}}(\mathbf{t}_{i+1}) = \phi_{\mathbf{c}} \, \underline{\mathbf{x}}_{\mathbf{c}}(\mathbf{t}_{i}) + \mathbf{B}_{\mathbf{c}\mathbf{z}} \, \underline{\mathbf{z}}(\mathbf{t}_{i}) + \mathbf{B}_{\mathbf{c}\mathbf{v}} \, \underline{\mathbf{y}}_{\mathbf{d}}(\mathbf{t}_{i})$$
 (3-45b)

where the subscript c refers to states of the controller. The gain matrices of Equations (3-45a) and (3-45b) are evaluated explicitly in Appendix A.

At this point, the performance of the PI controller may be evaluated using the method of Section 2.6, evaluating the statistical characteristics of an augmented vector

$$\underline{y}_{\mathbf{a}}(\mathbf{t}_{\mathbf{i}}) = \begin{bmatrix} \underline{\mathbf{x}}_{\mathbf{t}}(\mathbf{t}_{\mathbf{i}}) \\ \underline{\mathbf{u}}(\mathbf{t}_{\mathbf{i}}) \end{bmatrix}$$
(3-46)

which is composed of the states of the truth model and the controls generated by the PI controller.

3.6 Summary

The chapter has presented the equations for designing and evaluating PI controllers based on an LQG methodology. The advantage of a PI controller over the LQG regulator discussed in Chapter II is that it will track a desired output with zero steady-state error (in a deterministic

setting, or in zero steady-state mean error in a stochastic environment) even in the face of unmodeled constant disturbance. The type chosen for implementation was an incremental form of PI controller that is based on augmentation of system state equations with relations involving pseudointegration of the control rates.

The Doyle and Stein stability robustness enhancement technique of inputting white noise into the system model at the control entry points during filter tuning was applied to PI controllers. The following chapter will extend this method to allow time-correlated input noise for the case where robustification is desired over only a limited frequency range.

Chapter IV. Time-Correlated Input Noise

4.1 Introduction

Section 2.4 introduced the idea of robustifying a Kalman filter by adding pseudonoise to a system at the point of entry of the control inputs, <u>u</u>. By increasing the intensity of this pseudonoise, the stability robustness properties of a full-state feedback system could by asymptotically recovered by the observer-based sytem.

One disadvantage of this techniques is that the noise addition degrades the performance of the system at the design conditions. The white noise adds uncertainty to the model with the same intensity throughout the frequency spectrum. It may be desired to robustify the Kalman filter only over a certain frequency range where confidence in the adequacy of the controller design model may be low. Thus, a natural extension to the Doyle and Stein technique (Ref 6) is to add time-correlated (colored) input noise where the strength of the noise is highest for the frequency range of interest. This chapter develops this idea and describes how to apply it to the types of controllers discussed in Chapter II and III (Ref 15;16;18).

In the first section, a stochastic model is developed for the fictitious colored noise process. Then, this is augmented with the model used to describe the system. Finally, the colored noise processes to be used in this thesis are described, including the shaping filters to generate them.

4.2 Stochastic Model

Stationary, time-correlated input noise is represented as the

steady-state output of a linear time-invariant system driven by white Gaussian noise as

$$\underline{\dot{x}}_{u}(t) = F_{u} \underline{x}_{u}(t) + G_{u} \underline{w}_{u}(t)$$
 (4-1a)

$$\underline{\mathbf{n}}_{\mathbf{u}}(\mathsf{t}) = \mathbf{H}_{\mathbf{u}} \, \underline{\mathbf{x}}_{\mathbf{u}}(\mathsf{t}) + \mathbf{D}_{\mathbf{u}} \, \underline{\mathbf{w}}_{\mathbf{u}}(\mathsf{t}) \tag{4-1b}$$

The subscript u refers to uncertainty parameters. The statistics of the stationary white noise, $\underline{\mathbf{w}}_{\mathbf{u}}(t)$, are given by

$$E\{\underline{w}_{11}(t)\} = \underline{0} \tag{4-2a}$$

$$E\{\underline{\mathbf{w}}_{\mathbf{u}}(\mathsf{t}) \ \underline{\mathbf{w}}_{\mathbf{u}}^{\mathsf{T}}(\mathsf{t}+\tau)\} = Q_{\mathbf{u}}\delta(\tau) \tag{4-2b}$$

The colored noise process, $\underline{n}_{u}(t)$, is added to the system model, given by

$$\underline{\dot{x}}(t) = F \underline{x}(t) + B \underline{u}(t) + G \underline{w}(t)$$
 (4-3a)

$$\underline{z}(t) = \exists \underline{x}(t) + \underline{v}(t)$$
 (4-3b)

at the point of entry of \underline{u} . This results in

$$\underline{\dot{x}}(t) = F \underline{x}(t) + B \left[\underline{u}(t) + \underline{n}_{\dot{u}}(t)\right] + G \underline{w}_{\dot{u}}(t)$$
 (4-4)

Define an augmented vector to be the system states and the uncertainty model states

$$\underline{\mathbf{x}}_{\mathbf{g}}(t) = \begin{bmatrix} \underline{\mathbf{x}}(t) \\ \underline{\mathbf{x}}_{\mathbf{u}}(t) \end{bmatrix}$$
 (4-5)

Next, augment the uncertainty state differential equations with those of the original system. This yields an augmented system equation, given by

$$\underline{\dot{x}}_{s}(t) = F_{s} \underline{x}_{s}(t) + B_{s} \underline{u}(t) + G_{s} \underline{w}_{s}(t)$$
 (4-6a)

$$\underline{z}_{s}(t) = H_{s} \underline{x}_{s}(t) + \underline{v}(t)$$
 (4-6b)

The above matrices are described by

$$F_{s} = \begin{bmatrix} F & BH_{u} \\ O & F_{u} \end{bmatrix}$$
 (4-7)

$$B_{s} = \begin{bmatrix} B \\ 0 \end{bmatrix} \tag{4-8}$$

$$G_{s} = \begin{bmatrix} G & BD_{u} \\ & & \\ 0 & G_{u} \end{bmatrix}$$
 (4-9)

$$H_{\mathbf{s}} = \begin{bmatrix} H & O \end{bmatrix} \tag{4-10}$$

The noise vector, $\underline{\mathbf{w}}_{\mathbf{s}}(t)$, is given by

$$\underline{\underline{w}}_{g}(t) = \begin{bmatrix} \underline{\underline{w}}(t) \\ \underline{\underline{w}}_{U}(t) \end{bmatrix}$$
 (4-11)

with covariance kernal $E\{\underline{w}_s(t)\underline{w}_s^T(t+\tau)\} = Q_s\delta(\tau)$, where

$$Q_{s} = \begin{bmatrix} Q & O \\ & & \\ O & Q_{u} \end{bmatrix}$$
 (4-12)

The augmented system model described in Equations (4-5) through (4-12) is used to design either the continuous-time Kalman filter in Equations (2-12a) and (2-12b) or the sampled-data Kalman filter in Equations (2-76) through (2-79). However, it is not necessary to feed back the uncertainty model states in the controller algorithm; they are used only to modify the filter within the overall controller. Therefore, the original system model is used to design the LQ regulator of Chapter II or the PI controller of Chapter III. However, the dimensions of the Kalman filter and the controller are now incompatible. This is solved by augmenting the controller gain matrix with zeros

$$G_{c_s}^{*} = \left[G_c^{*} \middle| 0 \right]$$
 (4-13)

Thus, the order of the original system has been increased to reflect the adding of uncertainty model states, but these are fed back through the controller with zero gains.

At this point, the control law is put into the continuous-time generic form of Equations (2-25) and (2-26) or the sampled-data form of Equations (2-82) and (2-83). then, the performance of the robustified system is evaluated using the performance analysis described in Chapter II.

4.3 Shaping Filter Design

The time-correlated noise processes to be examined in this thesis are generated by inputting white noise to first- or second-order shaping filters as described in Reference 23:180-186. The following sections describe the form of the shaping filters.

4.3.1 First-Order Colored Noise Processes

A noise process which has low intensity at low frequencies and high intensity at high frequencies (or high intensity at low frequencies and low intensity at high frequencies) can be generated as the output of a system with a transfer function of the form

$$\frac{x_{u}(s)}{w_{u}(s)} = \frac{s+a}{s+b}$$
 (4-14)

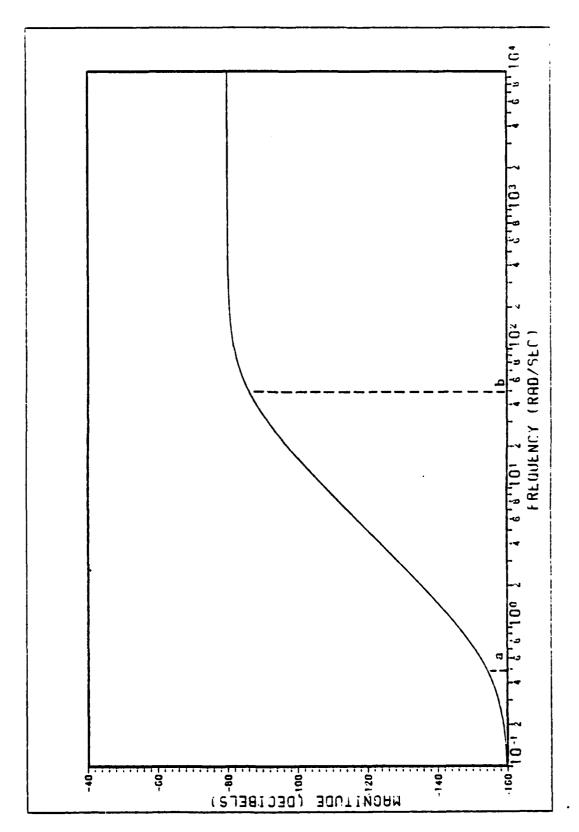
In Chapter V, it is shown that the model used for this thesis is adequate for low frequencies but may not be for higher frequencies. Thus, for this case, the strength of the noise should be kept low at low frequencies and then increased where the adequacy of the model is in doubt. Figure (4-1) shows the power spectral density function for this process.

Using the standard controllable form given in Reference 23:Ch 2, the state-space representation for Equation (4-14) is

$$\dot{x}_{ij}(t) = -b x_{ij}(t) + w_{ij}(t)$$
 (4-15a)

$$n_u(t) = (a - b) x_u(t) + w_u(t)$$
 (4-15b)

For this first-order shaping filter, the uncertainty model matrices are thus scalar and given by



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Pigure 4-1: Power Spectral Density Function for a First-Order Shaping Filter

$$F_{11} = -b \tag{4-16a}$$

$$B_{u} = 1$$
 (4-16b)

$$H_{11} = (a - b)$$
 (4-16c)

$$D_{11} = 1$$
 (4-16d)

Note that a noise process is generated for each control applied to the system. Thus, the dimension of the augmented system is that of the basic system plus the number of controls.

4.3.2 Second-Order Colored Noise Processes

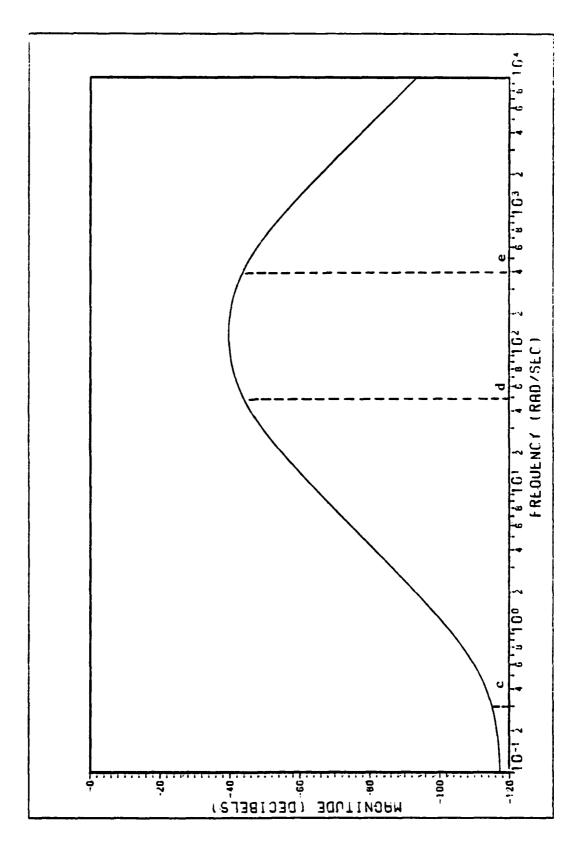
A noise process which has high intensity over only a limited frequency range can be generated by passing white noise through a linear system model that has a transfer function of the form

$$\frac{x_{u}(s)}{w_{u}(s)} = \frac{s+c}{(s+d)(s+e)}$$
 (4-17)

If it is the case where the adequacy of the design model is in doubt over a limited frequency range, then a second-order shaping filter as in Equation (4-17) would be appropriate. The power spectral density function for this process is shown in Figure (4-2).

A state-space representation for this process, using standard controllable form is given by

$$\begin{bmatrix} \dot{\mathbf{x}}_{\mathbf{u}_{1}}(t) \\ \dot{\mathbf{x}}_{\mathbf{u}_{2}}(t) \end{bmatrix} = \begin{bmatrix} 0 & 1 \\ -de & -(d+e) \end{bmatrix} \begin{bmatrix} \mathbf{x}_{\mathbf{u}_{1}}(t) \\ \mathbf{x}_{\mathbf{u}_{2}}(t) \end{bmatrix} + \begin{bmatrix} 0 \\ 1 \end{bmatrix} \mathbf{w}_{\mathbf{u}}(t) \quad (4-18a)$$



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Figure 4-2: Power Spectral Density Function for a Second-Order Colored Noise Process

$$n_{\mathbf{u}}(t) = \begin{bmatrix} c & 1 \end{bmatrix} \begin{bmatrix} x_{\mathbf{u}_{1}}(t) \\ x_{\mathbf{u}_{2}}(t) \end{bmatrix}$$
 (4-18b)

For this second-order shaping filter, the uncertainty model matrices are thus given by

$$F_{u} = \begin{bmatrix} .0 & 1 \\ & & \\ -de & -(d+e) \end{bmatrix}$$
 (4-19a)

$$B_{u} = \begin{bmatrix} 0 \\ 1 \end{bmatrix}$$
 (4-19b)

$$H_{u} = \begin{bmatrix} c & 1 \end{bmatrix} \tag{4-19c}$$

$$D_{u} = \begin{bmatrix} 0 \end{bmatrix} \tag{4-19d}$$

For this case, the dimensionality of the original system is increased by two times the number of controls when these shaping filter states are augmented to the system states.

The above technique for robustifying the Kalman filter in a control system is incorporated into two subroutines added to the LQG regulator design program described in Reference 21. Source code and instructions for running the program with the additional routines are listed in Appendix B.

Similarly, for PI controllers, the user must input the original design model, before augmenting the shaping filter states, to the program described in Reference 13. The original model is used to design the PI controller. Then, the shaping filter states are augmented with the model for the Kalman filter design. Finally, the PI controller feedback gain matrix is augmented with zeros to make the dimensions of the two solutions compatible. Modifications to the software in Reference 13 are listed in Appendix C.

4.4 Summary

This chapter has presented an extension to the Doyle and Stein robustness method of injecting white input noise into a controlled system during the process of tuning the Kalman filter. The extension allows time-correlated noise to be injected into the system model, which is accomplished by augmenting shaping filter states to the state differential equations of the system to be controlled. Thus, the strength of the colored noise can be concentrated at frequencies where robustification is desired and attenuated elsewhere.

Two types of shaping filters to generate the colored noise were examined. The first concentrated the strength of the noise at higher frequencies. The second concentrated the strength of the noise over a limited frequency range. Then, the method was applied to the types of controllers discussed in this thesis.

At this point, the types of controllers which are designed for this thesis have been discussed. In addition, techniques to enhance the robustness characteristics of the controllers have been presented. The following chapter presents the linear, time-invariant model to which the above mentioned methods are applied in this thesis.

Chapter V. AFTI/F-16 Flight Control Design

5.1 Introduction

This chapter presents the longitudinal dynamic equations for the Advanced Fighter Technology Integration aircraft, an F-16 aircraft (AFTI/ F-16) modified for advanced controls research. For longitudinal control, the aircraft is equipped with a decoupled horizontal tail and trailing edge flap which make it possible for the AFTI/F-16 to perform such maneuvers as pitch pointing. A pitch-pointing maneuver allows the aircraft's attitude angle to be changed while holding the flight path angle constant. The controllers to be designed lend themselves readily to multiple-input multiple-output (MIMO) system methods such as those described in this thesis. The aircraft equations are adequately portrayed as linear and time invariant by linearization about specified trim conditions in the aircraft's flight envelope. The controllers described in earlier chapters will be designed for the AFTI/F-16, applying the techniques of tuning the Kalman filter for robustness purposes by injecting fictitious white or time-correlated noise into the system model at the point of entry of the control inputs.

Data used to form the AFTI/F-16 longitudinal equations was taken from References 11 and 12. Reference 11 lists dimensional stability derivatives in a body-axis coordinate system for the aircraft, but does not include data for the trailing-edge flap. This information is given in Reference 12 in a stability-axis coordinate system. The necessary transformations were performed to convert all values to the body-axis frame.

The development of a linear perturbation model for an aircraft's longitudinal dynamics is found in References 7;8;9;10;25. The model for clear air turbulence is developed in Reference 17 and used in Reference 12. Both these models are incorporated to form the AFTI/F-16 equations described later in this chapter.

The first section of this chapter describes a thirteen-state linear perturbation truth model for the AFTI/F-16. This thirteen-state model is unobservable because a measurement is not available for all four aircraft states. Therefore, the unobservable state is deleted from the full model to leave a twelve-state truth model. This model, described in a second section, will be used to evaluate the performance of lower order controller models. The lower order (eight-state) controller model is described in a third section. The final section gives the data and longitudinal equations for one twelve-state truth model at an off-design flight condition. This will be used to evaluate the robustness of the controllers designed.

5.2 AFTI/F-16 Truth Model

The longitudinal aircraft truth model consists of four aircraft states, three turbulence (gust) states, and six additional states to describe the third order dynamics for each of the horizontal tail and trailing-edge-flap actuators. The aircraft states are: Θ , attitude angle; α , angle of attack, q, pitch rate, and; u, forward perturbation velocity. There are two angle of attack gust states and one pitch-rate gust state. Noise-corrupted measurements are available for Θ , α , and q, and the measurement for α includes an angle-of-attack gust state. The actuator and gust models will be described first.

5.2.1 Actuator Dynamics

The actuators for the horizontal tail and trailing-edge-flap are modeled as third-order systems, yielding delivered angle δ in response to commanded angle δ_{com} , of the form

$$\frac{\delta(s)}{\delta_{com}(s)} = \frac{(1/T_s) (\omega_n^2)}{(s + 1/T_s) (s^2 + 2\xi \omega_n s + \omega_n^2)}$$
(5-1)

Multiplying the numerator and denominator terms yields

$$\frac{\delta(s)}{\delta_{com}(s)} = \frac{a_o}{s^3 + a_2 s^2 + a_1 s + a_o}$$
 (5-2)

Using the standard observable state space representation given in Reference 23:Ch 2, the corresponding model is

$$\begin{bmatrix} \dot{\delta}(t) \\ \dot{\delta}_{1}(t) \\ \dot{\delta}_{2}(t) \end{bmatrix} = \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ -a_{0} & -a_{1} & -a_{2} \end{bmatrix} \begin{bmatrix} \delta(t) \\ \delta_{1}(t) \\ \delta_{2}(t) \end{bmatrix} + \begin{bmatrix} b_{1} \\ b_{2} \\ b_{3} \end{bmatrix} \delta_{com}(t) (5-3a)$$

$$\delta(t) = \begin{bmatrix} 1 & 0 & 0 \end{bmatrix} \begin{bmatrix} \delta(t) \\ \delta_1(t) \\ \delta_2(t) \end{bmatrix}$$
 (5-3b)

where the b_i's arise when taking the Laurent series for G(s). Notice that δ_{com} is the command surface deflection and δ is the surface deflection output from the actuators. Two intermediate states, δ_1 and δ_2 , are needed to describe fully the actuator dynamics.

The values chosen for the parameters in Equation (5-1) are specified in Reference 27 as

$$\frac{\delta(s)}{\delta_{com}(s)} = \frac{(20.2) (71.4)^2}{(s + 20.2) (s^2 + 2(.736) (71.4) + 71.4^2)}$$
(5-4)

The same actuator equations are used for both the horizontal tail and trailing-edge-flap. Expanding Equation (5-4) yields

$$\frac{\delta(s)}{\delta_{com}(s)} = \frac{102980}{(s^3 + 125.3s^2 + 7221s + 102980)}$$
(5-5)

Thus the resulting state equation is

$$\begin{bmatrix} \dot{\delta}(t) \\ \dot{\delta}_{1}(t) \\ \dot{\delta}_{2}(t) \end{bmatrix} = \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ -102980. & -7221. & -125.3 \end{bmatrix} \begin{bmatrix} \delta(t) \\ \delta_{1}(t) \\ \delta_{2}(t) \end{bmatrix} + \begin{bmatrix} 0 \\ 0 \\ \delta_{com}(t) & (5-6) \\ 102980 \end{bmatrix}$$

5.2.2 Turbalence State Equations

The model used for clear air turbulence is found in References 12 and 17. The state equations for the three gust states are given by

$$\dot{\alpha}_{g} = a_{g_{1}}^{\dagger} \alpha_{g} + n_{\alpha} \qquad (5-7a)$$

$$\alpha_g = \alpha_g \quad \alpha_g + \alpha_g = \alpha_n \quad (5-7b)$$

$$\dot{q}_g = a_{g_d} \dot{q}_g + q_{g_1} q_g$$
 (5-7c)

The noise source, n_{α} , is modeled as a white Gaussian noise with statistics

$$E\{n_{\alpha}(t)\} = 0 \qquad (5-8a)$$

$$E\{n_{\alpha}(t) n_{\alpha}^{T} (t + \tau)\} = \delta(\tau)$$
 (5-8b)

The coefficients in Equations (5-7) are computed using the following equations

$$a_{g_1} = \frac{-V_t}{L_w}$$
 (5-9a)

$$a_{g_2} = \frac{\sigma_w}{L_w} (1. - \sqrt{3.}) \sqrt{\frac{v_t}{L_w}}$$
 (5-9b)

$$a_{g} = \frac{-V_{t}}{L_{w}}$$
 (5-9c)

$$a_n = \frac{\sigma_w}{v_t} \sqrt{\frac{3v_t}{L_w}}$$
 (5-9d)

$$a_{g_d} = \frac{\pi^{V_t}}{4b}$$
 (5-9e)

$$q_{g_1} = \frac{-\pi v_t}{4b} \tag{5-9f}$$

 V_t is aircraft velocity and b is the wing span. The quantities σ_w and L_w are given in Reference 3 as functions of altitude, where σ_w is the root mean square intensity of the clear air turbulence in feet per

second and L is a reference scale length in feet.

5.2.3 System Equations

The thirteen states for the unobservable truth model are listed in Equation (5-10) on the following page.

As demonstrated in Reference 12, it is convenient to define the truth model equations in two stages. First, define the ssytem matrix, F_t^i of Equation (2-25), neglecting all α stability derivative terms and also the α_g term in Equation (5-7c). Then modify the matrix to incorporate the neglected terms. This is done for mathematical convenience as the α terms are neglected in a later truth model. Defining the system matrix in two stages does not change the definition of the states; the second stage is merely a more adequate model. The initial matrix is given in Equation (5-11) on the following page.

To incorporate the neglected terms, rows 2,3,4 and 13 are modified with the following equations (using standard double-index array notation $F_{t}(I,J)$ for the I-th row and J-th column of F_{t}).

$$F_t(2,J) = F_t'(2,J) / (1. - Z_{\dot{\alpha}})$$
 (5-12a)

$$F_{t}(3,J) = F_{t}(3,J) + M_{o} \times F_{t}(2,J)$$
 (5-12b)

$$F_t(4,J) = F_t^*(4,J) + X_{\alpha} \times F_t(2,J)$$
 (5-12c)

$$F_t(13,J) = F_t'(13,J) + a_{g_d} \times F_t'(12,J)$$
 (5-12d)

The column index J ranges from 1 to 13.

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 $\theta(t)$ $\alpha(t)$ q(t) u(t) $\delta_{HT}(t)$ $\delta_{HT_{1}}(t)$ $\delta_{HT_{2}}(t)$ $\delta_{TEF_{1}}(t)$ $\delta_{TEF_{2}}(t)$ $\alpha_{g}'(t)$ $\alpha_{g}'(t)$

(5-11)

0. 0. 0. 1. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0.														
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In Equations (5-11) and (5-12), the dimensional stability derivatives "X", "Z", and "M" refer to body forces acting along the X- and Z-axes (forward and down axes) and the pitching moment about the Y-axis, (axis emanating from aircraft center of mass toward the right wing) respectively. The subscript identifies the state with respect to which the derivative is taken. The term "g" is the acceleration due to gravity. The subscripts HT and TEF refer to deflections of the horizontal tail and trailing-edge-flap, respectively. The terms α_0 , u_0 and w_0 refer to trim values of angle of attack, and velocity components along the X- and Z-axes, respectively. A trim condition is a steady-state level flight condition about which the longitudinal dynamic equations are linearized. For this case, the trim condition is chosen to be steady level flight at a Mach number of 0.6 and an altitude of 10,000 feet.

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Table (5-1) gives the values needed to define the thirteen-state truth model. Note that the value of $\alpha_{_{\rm W}}$ given in the gust model coefficients is for "Level 1" or light to moderate air turbulence. This level of air turbulence has a high probability of being encountered in flight.

From Chapter II, the truth model is of the form

$$\underline{\dot{\mathbf{x}}}_{\mathsf{t}}(\mathsf{t}) = \mathbf{F}_{\mathsf{t}} \ \underline{\mathbf{x}}_{\mathsf{t}}(\mathsf{t}) + \mathbf{B}_{\mathsf{t}} \ \underline{\mathbf{u}}(\mathsf{t}) + \mathbf{G}_{\mathsf{t}} \ \underline{\mathbf{w}}_{\mathsf{t}}(\mathsf{t}) \tag{5-13}$$

The control vector, u, is given by

$$\underline{\mathbf{u}} = \begin{bmatrix} \delta_{\mathrm{HT}_{\mathrm{com}}} & (t) \\ \delta_{\mathrm{TEF}_{\mathrm{com}}} & (5-14) \end{bmatrix}$$



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	Table 5-1	
AFTI	AFTI/F-16 Data for $M = 0.6$, $H = 10,000$ Feet	0 Feet
TRIM CONDITIONS	ACTUATOR PARAMETERS	ADDITIONAL PARAMETERS
V _T = 646.4 Ft/Sec	a = 102980.0	g = 32.174 Ft/Sec ²
$\alpha = 2.174 \text{ Deg}$	$T_S = 20.2$ /Sec	b = 30 Ft
u = 645.9 Ft/Sec	ξ = 0.736	σ = 5.0 Ft/Sec
w = 24.52 Ft/Sec	$\omega = 71.4$ /Sec	L = 1750.0 Ft

		LONGITUDINAL STABILITY DERIVATIVES	
	Z - BODY FORCES	X - BODY FORCES	PITCHING MOMENTS
2 ¤	= -1.355 /Sec	$x_{\alpha} = 7.56 \text{ Ft/Sec}^2$	$M_{\alpha} = 4.95 \times 10^{-2} / \text{Sec}^2$
ζ.	$= 2.241 \times 10^{-3}$	$X_{\alpha} = -5.5 \times 10^{-2} \text{ Ft/Sec}$	$M_{\alpha} = -0.1556 / \text{Sec}$
2 d	$= -5.435 \times 10^{-3}$	X = 0.1334 Ft/Sec	M = -0.5376 /sec
n Z	$= -1.215X10^{-4} / Ft$	$x_{\rm u} = -6.47 \text{X} 10^{-3} / \text{Sec}$	M = -6.55X10 ⁻⁴ /Sec/Ft
Z ^δ HT	= -0.1335 /Sec/Rad	$x\delta_{HT} = 0.8404 \text{ Ft/Sec}^2/\text{Rad}$	$M\delta_{\rm HT} = -0.1332 / \rm Sec^2/Rad$
Zô _{TE}	Z& _{TEF} = -0.2365 /Sec/Rad	$x\delta_{TEF} = -2.38 \text{ Ft/Sec}^2/\text{Rad}$	Mõ _{TEF} = -1.32 /Sec ² /Rad

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The B_t and G_t matrices are given by Equations (5-15) and (5-16) on the following page. The last element of the G_t matrix is defined to be

$$q_n = a_{g_d} \times a_n \tag{5-17}$$

where a_n and a_{d} were defined previously in Equations (5-9d) and (5-9e).

Employing the data of Table (5-1) and Equations (5-11) and (5-12), the F_t matrix is given by Equation (5-18). Equations (5-19) through (5-22) give the other system matrices with their numerical values inserted.

Recall the continuous-time measurement equation is of the form

$$\underline{z}_{t}(t) = H_{t} \underline{x}_{t} + \underline{v}_{t}(t)$$
 (5-23)

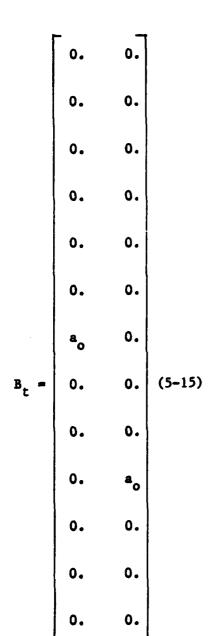
The covariance kernel description, R_t , for the measurement noise, $\underline{v}_t(t)$, (Equation (2-28)) was established using the values given in Reference 12. The results are listed in Equation (5-24).

$$R_{t} = \begin{bmatrix} 9.52 \times 10^{-8} & 0 & 0 \\ 0 & 2.44 \times 10^{-7} & 0 \\ 0 & 0 & 6.44 \times 10^{-7} \end{bmatrix}$$
 (5-24)

Recall from Equation (2-120) that a first order approximation for a discrete-time $R_{
m dt}$, to be used to design a sampled-data controller is given by

$$R_{dt} = R_t/\Delta t \tag{5-25}$$

The truth model described above will hereafter be referred to as (T13,10,0.6). "T" indicates truth model, 13 refers to the number of



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							·					
0.0	-1.358 -5.447x10 ⁻³	5367	.1337		0.0	0.0	0.0	0.0	0.0	0.0	0.0	-16.92
0.0	-1.358	.2622	7.635	0.0	0.0	0.0	0.0	0.0	0.0	0.0	-33694	-2 -6.250 -16.92
0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	3694	4.271X10 ⁻³	2.151X10 ⁻²
0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	1.0	-125.3	0.0	0.0	0.0
0.0	0.0	0.0	0.0	0.0	0.0	0.0	0:1	0.0	-7221	0.0	0.0	0.0
0.0	-0.237	-1.283	-2.367	0.0	0.0		0.0	o. o.	1 -102980	0.0	0.0	0.0
0.0	0.0	0.0	0.0	0.0	1.0	-125.3	0.0	0.0	0.0	0.0	0.0	0.0
0.0	o. 0	0.0	0.0	1.0	0.0	-7221	0.0	0.0	0.0	0.0	0.0	0.0
0.0	1338	-13.30	.8478	0.0	0.0	-102980	0.0	0.0	0.0	0.0	0.0	0.0
0.0	-1.218X10-4	-6.359X10-4	-6.463X10 ⁻³	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.1	8966.	6937	-24.45	0.0	0.0	0.0	o.c	0.0	0.0	0.0	0.0	0.0
0.0	-1.357	.2622	7.635	0.0	0.0	0.0	0:0	0.0	0.0	0.0	0.0	0.0
0.0	-1.894x10 ⁻³ -1.357 .9968	2.996X10 ⁻⁴	-32.18	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0

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 $Q_{t} = [1]$ (5-21)

states, 10 refers to the altitude in thousands of feet, and 0.6 to the Mach number for which the equations were computed.

5.3 Reduced Order Truth Model

The truth model of the previous section represents an unobservable system because a measurement of the fourth state, u, is unavailable. In practice, it is rarely desirable to feed back this state through a controller. Therefore, the fourth state is deleted from the truth model before any further simplification to yield models upon which to base a controller/estimator design. In addition, all terms involving $\dot{\alpha}$ stability derivations are ignored because their effects on the terms of Equation (5-19) are negligible. Incorporating these derivatives causes the values for the $F_{\rm t}$ matrix to change only slightly, except for the terms involving, u, which were deleted. Thus, the modifications listed in Equations (5-12a), (5-12b) and (5-12c) are not necessary. Equation (5-12d) now becomes

$$F_t(12,J) = F_t'(12,J) + a_{g_d} \times F_t'(11,J)$$
 (5-26)

The matrices needed to define the twelve-state truth model are given in Equations (5-27) through (5-33). Note that R_{t} was defined previously in Equation (5-24).

The twelve-state truth model based on linearization about a trim condition at 10000 feet and Mach 0.6 will be referred to as (T12,10,0.6).

5.4 Controller Design Model

The reduced order controller is formed by modelling the AFTI/F-16 actuator dynamics as first-order lags instead of third-order systems as



$$\theta(t)$$

$$\alpha(t)$$

$$q(t)$$

$$\phi_{HT}(t)$$

$$\delta_{HT_1}(t)$$

$$\delta_{HT_2}(t)$$

$$\delta_{TEF_1}(t)$$

$$\delta_{TEF_2}(t)$$

$$\alpha'_g(t)$$

$$\alpha'_g(t)$$

$$\alpha'_g(t)$$

$$\alpha'_g(t)$$

$$\underline{u}(t) = \begin{bmatrix} \delta_{HT_{com}}(t) \\ \delta_{(t)} \\ TEF_{com} \end{bmatrix}$$
 (5-28)

(5-29)

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 $Q_{t} = [1]$ (5-32)

given in Equation (5-1). The transfer function for a first-order lag with a coefficient of $1/T_{\rm g}$, i.e., a lag time of $T_{\rm g}$, is given by

$$\frac{\delta(s)}{\delta_{com}^{(s)}} = \frac{1/T_s}{s + 1/T_s}$$
 (5-34)

In state space representation, the above equation becomes

$$\dot{\delta}(t) = (-1/T_s) \delta(t) + (1/T_s) \delta_{com}(t)$$
 (5-35)

where T_s is the time constant for the actuator. Again, δ_{com} is the command surface deflection and δ is the surface deflection output from the actuator. A good fit to the frequency response of the actuators yields $1/T_s = 20.2$ (Ref 27). Equation (5-35) then becomes

$$\dot{\delta}(t) = -20.2 \, \delta(t) + 20.2 \, \delta_{com}(t)$$
 (5-36)

Making this modification to the twelve-state truth model of Section 5.3 yields an eight-state controller design model. The matrices needed to define the controller model are given in Equations (5-37) through (5-43).

This eight-state controller model will be referred to as (C8,10,0.6).

5.5 Truth Models at Off-Design Conditions

To evaluate the effectiveness of the techniques previous described for robustifying the Kalman filter, the performance of the controllers are to be evaluated at flight conditions other than that for which the controllers were designed, as well as by using truth models of higher order than the design model. This is accomplished by using a truth model defined at an off-design condition in the performance analysis described in Chapter III. The following sections contain one such truth model.

$$\begin{array}{c}
\alpha(t) \\
\alpha(t) \\
q(t) \\
\delta_{HT}(t) \\
\delta_{TEF}(t) \\
\alpha_{g}'(t) \\
\alpha_{g}(t) \\
q_{g}(t)
\end{array}$$

$$\begin{array}{c}
\underline{u}(t) = \begin{bmatrix} \delta_{HT}(t) \\ \delta_{HT}(t) \\ \delta_{TEF}(t) \\ \delta_{TEF}(t) \\
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		(5-39)								
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•	-1.355	4.95X10 ⁻²	•0	 0 	0	-0.3694	-6.25			
•	0.	.0	0.	0.	1	-1.271X10 ⁻³	-2.151X10 ⁻²			
·	-0.2365	-1.32	.0	-20.2	.0		·			
•	-0.1335	-13.32	-20.2	0.	0.	•	.0			
	0.9946	-0.5376	· · · · · · · · · · · · · · · · · · ·	0	•0	ö	•			
•	-1.355	4.95X10 ⁻²	0.	0.	0.	.0	•			
·	-1.889X10 ⁻³	·	0.	0	o	°	·			

$$\begin{bmatrix}
0. & 0. \\
0. & 0. \\
0. & 0. \\
0. & 0. \\
20.2 & 0. \\
0. & 20.2 \\
0. & 0. \\
0. & 0. \\
0. & 0.
\end{bmatrix}$$

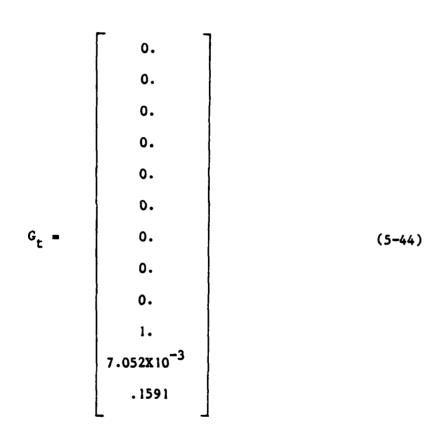
$$G = \begin{bmatrix} 0. \\ 0. \\ 0. \\ 0. \\ 0. \\ 1. \\ 8.142 \times 10^{-3} \\ 0.1378 \end{bmatrix}$$
 (5-41)

$$Q = [1]$$
 (5-42)

$$H = \begin{bmatrix} 1. & 0. & 0. & 0. & 0. & 0. & 0. \\ 0. & 1. & 0. & 0. & 0. & 1. & 0. \\ 0. & 0. & 1. & 0. & 0. & 0. & 0. \end{bmatrix}$$
 (5-43)

5.5.1 Truth Model (T12,20,0.6)

This truth model is defined for an altitude of 20,000 feet and a Mach number of 0.6. The values of parameters and stability derivatives needed to form the system matrices are given in Table (5-2). The truth model G_t and F_t matrices are given in Equation (5-44) and (5-45).



5.6 Summary

THE PARTY CONTROL OF THE PARTY OF THE PARTY

This chapter has presented the model which will be used to design LQG regulators as in Chapter II and PI controllers as in Chapter III for the AFTI/F-16. The robustification methods detailed in Chapters II and IV will

be applied to the model, and the effect of this will be examined by performing covariance analysis as described in Chapter II. The results of this study are presented in the following chapter.

	Table 5-2	
AF	AFTI/F-16 Data for M = 0.6, H = 20,000 Feet	Feet
TRIM CONDITIONS	ACTUATOR PARAMETERS	ADDITIONAL PARAMETERS
V _T = 622.15 Ft/Sec	a = 102980.	g = 32.174 Ft/Sec
α ₀ = 3.152 Deg	T _S = 20.2 /Sec	b = 30 Ft
u = 621.2 Ft/Sec	ξ = 0.736	σ _w = 2.5 Ft/Sec
w _o = 34.2 Ft/Sec	$\omega_n = 71.4$ /Sec	L, = 1750. Ft

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	LONGITUDINAL STABILITY DERIVATIVES	
Z - BODY FORCES	X - BODY FORCES	PITCHING MOMENTS
= -1.006 /Sec	$x_{\alpha} = 23.79 \text{ Ft/Sec}^2$	$M_{\alpha} = -1.218 / Sec^2$
$= 1.66 \times 10^{-3}$	$x_{\alpha} = -5.69 \times 10^{-2} \text{ Ft/Sec}$	M _α = -0.1068 /sec
$= -3.97 \text{X} 10^{-3}$	X = 0.136 Ft/Sec	M = -0.384 /Sec
= -1.48X10 ⁻⁴ /Ft	$x_{\rm u} = -4.827 \times 10^{-3} / \text{Sec}$	$M_{\rm u} = -7.09 \times 10^{-4} / \text{Sec/Ft}$
Z6 _{HT} = -9.18X10 ⁻² /Sec/Rad	$x\delta_{\rm HT} = 0.711 \text{Ft/Sec}^3/\text{Rad}$	$M_{HT} = -8.95 / Sec^2 / RAD$
Z\$reF = -0.1689 /Sec/Rad	$x\delta_{TEF} = -2.165 \text{ Ft/Sec}^2/\text{RAD}$	$^{\rm M}_{ m TEF} = -0.7736 / { m Sec}^2/{ m Rad}$

	-4.83X10 ⁻³	-0.470	·	•	ė	•	ö	ė ,	ė	ö	-21.72
•	-1.397	-0.8540 -0.470	ė	o ·	ö	ė	ó	ö	ó	-0.4740	-10.29
·		ö	.0			ö	ö		-0.4740	-7.200x10 ⁻⁴	4.564X10 ⁻²
•	•	0.	•		0.	•	:	-125.3	ó	ė	•
ö	0	•	•	ó	0.	-	0	-7221.	•	ó	ė
•	-0.220	-4.18	ó	<i>.</i>	ö		.	-102980, -7221.	· o	ė	•
•	ó	.	•	:	-125.3	ó	ö	0.	0.	0.	
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•	-1.377	-0.8540	•	ö	ö	•	ö	0.	0.	•	ö
•	-1.510X10 ⁻⁴	Ö	•	ó	ė	ò	•	0	•	ö	.

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VI. Results

6.1 Introduction

The results of the study of methods to improve the robustness properties of controlled systems are presented in this chapter. The two methods examined are the techniques of tuning the Kalman filter by inputting both stationary white and time-correlated Gaussian noise into the system model at the control entry points.

The results of applying these techniques are presented first for LQG regulators. In the first sections, results are given for a continuous-time system. Then, two approaches for a discrete-time system are examined: discretizing the continuous-time controller using first-order approximations, and designing a sampled-data controller.

Finally, in the last sections, the robustification techniques are applied to a sampled-data PI controller.

6.2 Robust LQG Regulators

Two separate issues of robustness are addressed in the following sections. The first is the idea of robustifying a system against differences between the real world and the finite-dimension, low-order model that is chosen for controller and Kalman filter design. As discussed in Chapter V, the model to represent the real world (the truth model) and the lower-order controller model were purposefully established so that the differences between them occur in a specific high frequency range. As proposed by Doyle and Stein (Ref 6), the stability characteristics of a full-state feedback system can be recovered by adding white noise at the control entry points during the process of filter tuning. The validity

of this claim is examined by looking first at a purposefully reduced-order controller evaluated against a truth model of the same dimension with first-order actuator dynamics. That is, the low-order controller model is evaluated as if it were a perfect representation of the real-world system. The performance of this controller is the best that can be expected with a Kalman filter to estimate the states. Then, the higher-order actuator dynamics are introduced into the truth model to demonstrate the effects of ignored states on the performance of the system. Next, the robustification techniques are introduced to attempt to recover the stability characteristics of a reduced order but full-state feedback system. It would be desirable also to examine the performance of a full-state feedback system to evaluate the claim that the stability robustness properties of the filter-based controller will asymptotically approach those of the full-state feedback controller using the Doyle and Stein technique. Unfortunately, the software used to design and evalute LQG regulators does not include the option of designing an LQ full-state controller. An attempt was made to approximate full-state feedback by setting the measurement noise intensities to small values and assuming a measurement was available for each state, but the results were inconclusive. Therefore, performance comparisons are only presented between designs using the robustified or unmodified Kalman filter.

As discussed in Chapter V, the difference between the controller design model and the truth model against which the performance is evaluated lies in the dynamics model for the actuators. Open loop frequency responses for the third-order model and the first-order model are shown in Figure (6-1). It is seen that the frequency responses differ

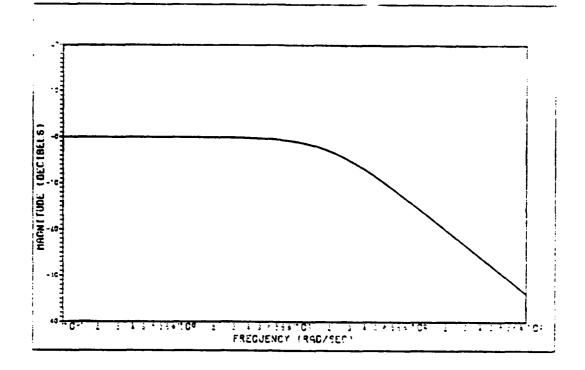


Figure 6-la: Open Loop Frequency Response for First-Order Actuator Model

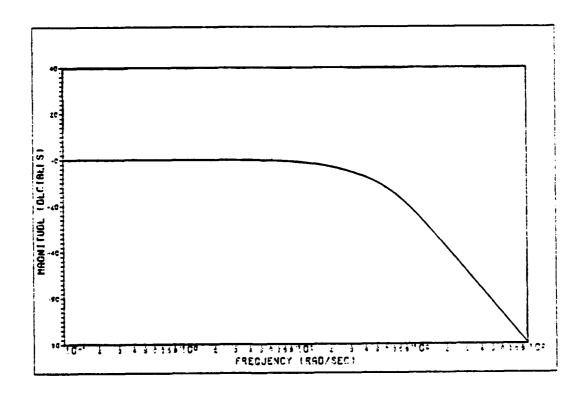


Figure 6-1b: Open-Loop Frequency Response for Third-Order Actuator Model

in the region around 70 rad/sec and beyond, where the complex poles are located in the third-order model. Robustification of the LQG controller based on the reduced-order model can be accomplished by adding white noise to the filter's system model at the point of entry of \underline{u} , or, by adding time-correlated noise with the primary power concentrated around the region of the model inadequacy, i.e., around 70 rad/sec and higher.

One first-order and one second-order shaping filter transfer function are considered, each of which concentrates the highest strength of the time-correlated noise in the region where the design model and truth-model actuator dynamics differ. The first-order shaping filter is described by the transfer function

$$\frac{x_u}{w_u} = \frac{s + 0.5}{s + 50} \tag{6-1}$$

A power spectral density plot of the time-correlated noise generated by this shaping filter is shown in Figure (6-2a).

The second-order shaping filter is described by the transfer function

$$\frac{x_u}{w_u} = \frac{s + 0.5}{(s + 50) (s + 400)}$$
 (6-2)

Figure (6-2b) shows the power spectral density function for the time-correlated noise generated by the above shaping filter. The values in Equations (6-1) and (6-2) were chosen by examining power spectral density plots of the time-correlated noise with the poles and zeroes of the shaping filters in different locations. The chosen values generate the

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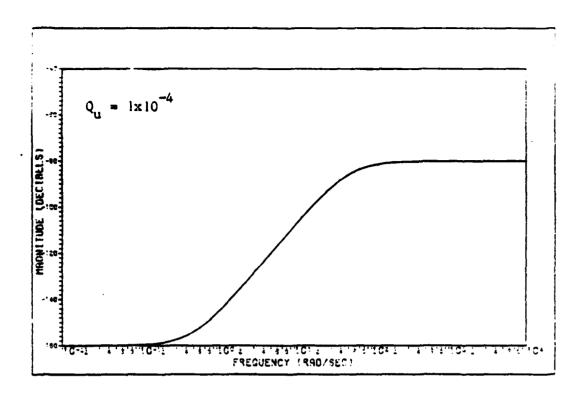


Figure 6-2a: First-Order Colored Noise Process
Power Spectral Density

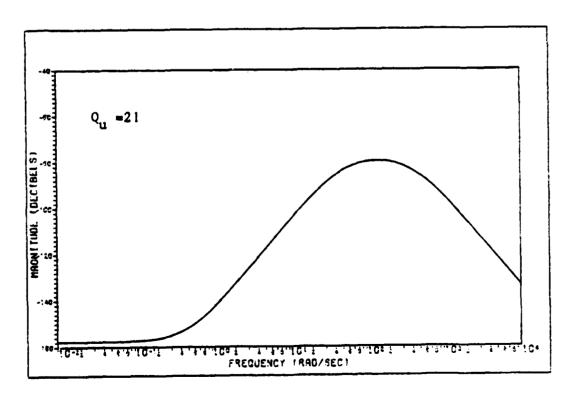


Figure 6-2b: Second-Order Colored Noise Process
Power Spectral Density

desired noise, the strength of which is highest in the frequencies where the truth and design model frequency responses differ.

The second robustness issue is concerned with operation of the controlled system at flight conditions other than the design condition. The differences between the real world and the reduced-order design model now occur in other frequency ranges besides those given by the actuator dynamics models. Since these frequency ranges are now unknown, the use of white input noise would be motivated since it injects equal uncertainty into the system model over the entire frequency spectrum. The additional performance degradation or instabilities that arise in going from the design condition to an off-design condition with a Kalman filter in the loop are examined to determine the success of the Kalman filter robustification techniques. That is, if the full-state feedback system (based on a reduced-order design model) is stable, then the LQG system (which may well yield an unstable closed-loop system with the unrobustified filter in the loop) can be stabilized with the addition of white input noise (as claimed by Ref 6) and possibly by colored noise if the robustification is applied over the appropriate frequency ranges.

The cost-weighting matrices used in Equation (2-3) are the same for the continuous-time, discretized, and sampled-data regulators (discretizing (2-3) to yield (2-69) is accomplished as in Ref 24). The values used are based on those given in References 12 and 22, with some iteration on the control weightings to achieve designs with commanded control surface deflections that do not exceed physical limits of the horizontal tail and tailing-edge flap. The state, control and cross-weighting matrices are given by

$$W_{XX} = \begin{bmatrix} 50 & -0- \\ & 50 \\ & & 150 \\ & & -0- \end{bmatrix}$$
 (6-3)

$$W_{XU} = [0] \tag{6-4}$$

$$W_{uu} = \begin{bmatrix} 10 & 0 \\ & & \\ 0 & 10 \end{bmatrix}$$
 (6-5)

It is desired to make a direct comparison between the performance of the controlled system with white and time-correlated input noise added to the model upon which the Kalman filter is based, where the maximum intensity of the time-correlated noise is equal to the intensity of the white noise. By equating the maximum magnitudes of the white and time-correlated noise, it can be determined if there are performance benefits in choosing one type of noise over another by comparing the degree of robustification achieved by each. This is accomplished using the frequency domain shaping filter design techniques in Reference 23, which state that

$$PSD_{o}(s) = G(s) G(-s) PSD_{i}(s)$$
 (6-6)

where PSD_1 and PSD_0 are the power spectral densities of the input and output of a shaping filter, respectively. G(s) is the transfer function of the shaping filter. It is desired to have the maximum magnitude of

the right-hand side of Equation (6-6) be equal the magnitude of the white input noise, (the scalar white noise parameter, q^2 of Equation (2-64)). Thus, by setting PSD_0 equal to q^2 and solving for the value of PSD_1 which makes this true, the value of Q_1 in Equation (4-12) can be found for the time-correlated noise. Thus, it is the intensity, Q_1 , of the white driving noise, W_1 (t) to the shaping filter which will generate a time-correlated noise with a maximum intensity of q^2 . Table (6-1) lists the values of Q_1 which make the maximum intensity of the

Table 6-1
Strength of Dynamic Driving Noise to Shaping Filters

G(s) = 1	$G(s) = \frac{s + 0.5}{s + 50}$	$G(s) = \frac{s + 0.5}{(s + 50)(s + 400)}$
q ²	Qu	Q _u
1 x 10 ⁻⁶	1 x 10 ⁻⁶	0.21
1 x 10 ⁻⁴	1 x 10 ⁻⁴	21.
1 x 10 ⁻²	1 x 10 ⁻²	2100.

time-correlated noise equal to that of the white noise. The values were arrived at using the software described in Reference 20.

6.2.1 Continuous-Time LQG Regulators at Design Condition

Figure (6-3) shows time histories of the mean and standard deviation of the aircraft state, Θ , for an eight-state controller evaluated against a truth model of the same dimension (the truth model and controller model are identical as given in Section 5.4). A perfectly known initial condition of one degree (or 0.0175 radians) was placed on Θ , and the

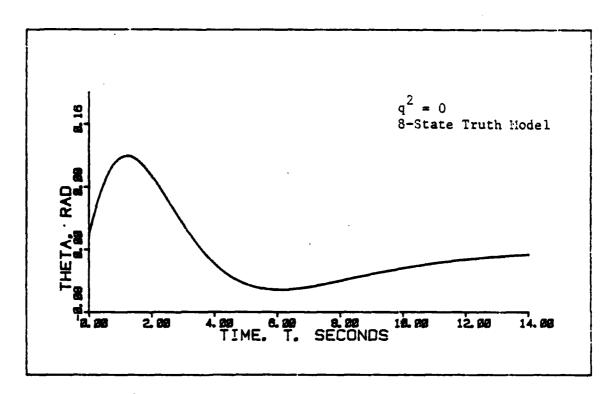


Figure 6-3a: Mean of Θ at the Design Condition

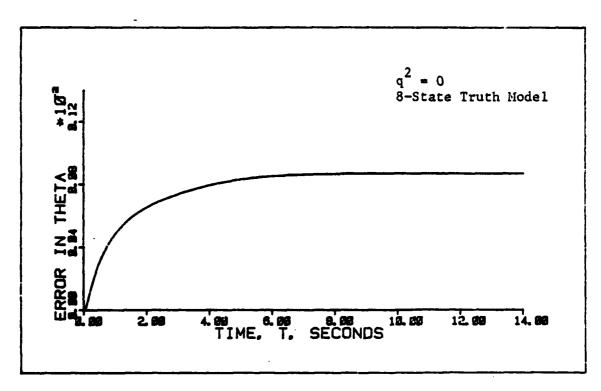


Figure 6-3b: Standard Deviation of Θ at the Design Condition

plot shows the response of Θ to the initial perturbation and to the dynamic driving noise built into the model. The trends are similar for all three aircraft states, therefore only one will be examined in detail in this chapter.

The time response is stable, although slow. The slow response is typical of systems with a Kalman filter to estimate states. The added dynamics of the filter tend to slow down the response. However, the controller does respond to the perturbation and regulate the state back to zero. Figure (6-4) shows the response of the same controller when specific ignored states are now accounted for in the truth model. This figure is the result of a performance analysis when third-order actuator dynamics are included in the twelve-state truth model, while only first-order dynamics are used in the eight-state design model. As can be seen, the system is still stable, bu the mean of Θ response has degraded substantially, especially in steady-state.

Figures (6-5a) and (6-5b) show the response of the same state with a white Gaussian noise of strength $q^2 = 1 \times 10^{-4}$ injected into the system model. The transient time, the overshoot, and the error in the final mean value of Θ have all been substantially improved with the noise addition. The standard deviation of Θ has not changed noticeably from the previous case. The trend for lower and higher e^2 values is shown in Figures (6-5c,e,d,f). It is seen that noise of a very small intensity (1×10^{-6}) enhances the robustness properties dramatically, and increasing the intensity of the noise only serves to change the transient characteristics of the mean time response and the magnitude of the standard deviation.

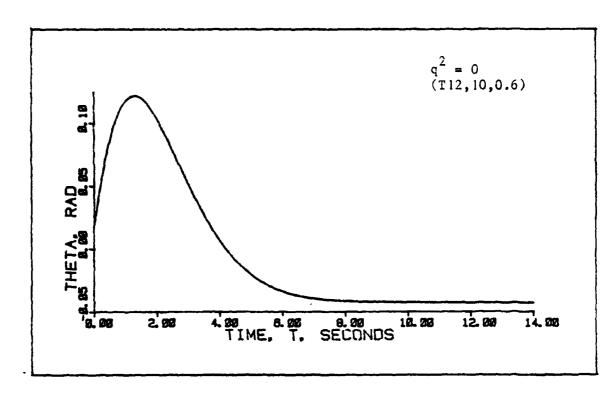


Figure 6-4a: Mean of 3 With no Noise Addition

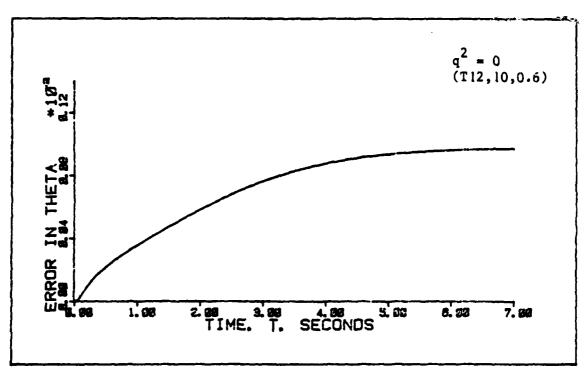


Figure 6-4b: Standard Deviation of @ With No Noise Addition

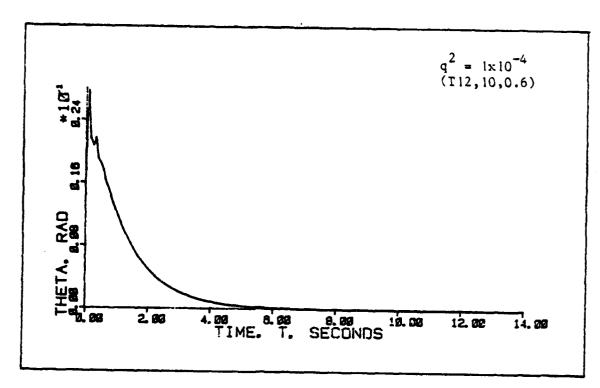
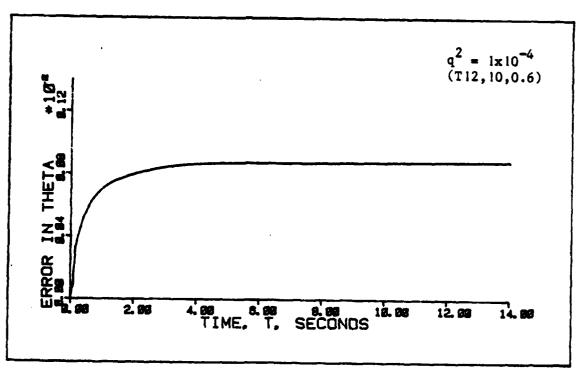


Figure 6-5a: Mean of θ With White Noise Addition



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Figure 6-5b: Standard Deviation of 8 With White Noise Addition

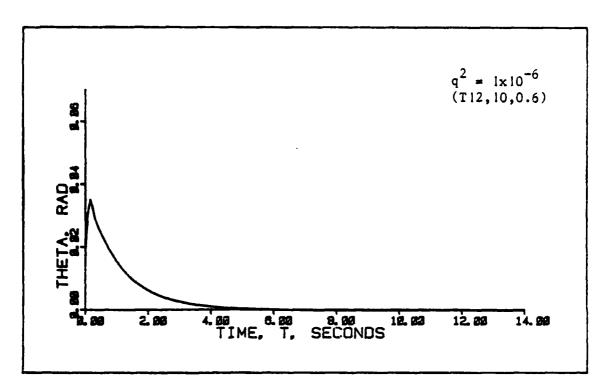
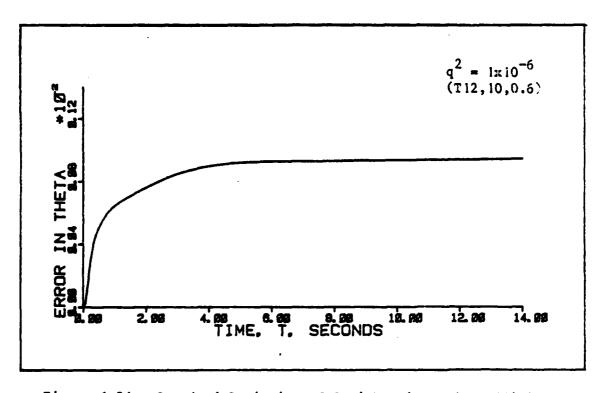


Figure 6-5c: Mean of θ With White Noise Addition



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Figure 6-5d: Standard Deviation of 0 With White Noise Addition

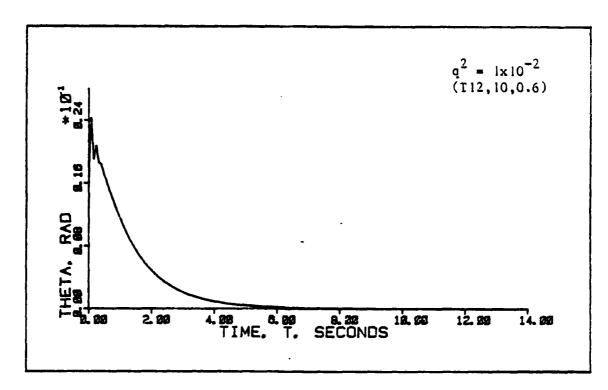


Figure 6-5e: Mean of 9 With White Noise Addition

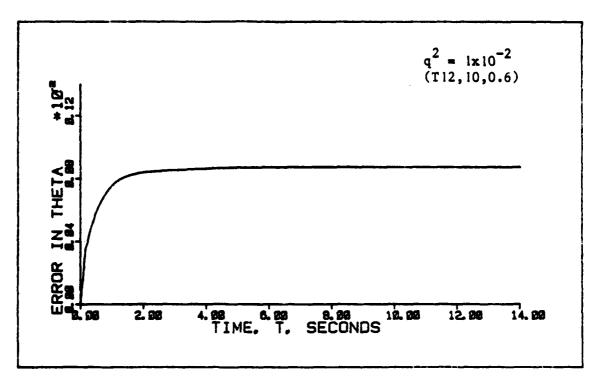


Figure 6-5f: Standard Deviation of θ With White Noise Addition 109

Then, as shown in Figure (6-6), time-correlated noise generated by a first-order shaping filter is injected into the system model. The maximum power spectral density of the noise is 1×10^{-4} . The figure demonstrates that the improvement in the transient time, overshoot, and final value of Θ is as dramatic as for the white noise case. Again, the standard deviation has not changed enough to be discernible in the figure.

Finally, time-correlated noise generated by a second-order shaping filter is injected into the design model. As can be seen in Figure (6-7), the transient time is approximately the same as for the original system, but much slower than the cases above. However, the state is converging to zero, and the overshoot has been reduced to about half of the original value. Any change in the steady-state value of the standard deviation is not noticeable in the figure.

Thus, Figures (6-3) through (6-7) demonstrate that the robustification techniques can recover the stability robustness characteristics that would be expected from a full-state feedback system. The methods of injecting white and first-order colored noise produce very similar improvements, while the second-order colored noise produced less but still noticeable benefits in the time response.

However, it was stated in previous chapters that the addition of noise into the design model will degrade the performance (as measured by the standard deviation of the states or how well known the states are) of the system at the design conditions. Additionally, it was claimed that the performance degradation will be less for colored noise than for white noise. To evaluate this claim, Table (6-2) lists the steady-state values of the standard deviations of all three aircraft states with no input

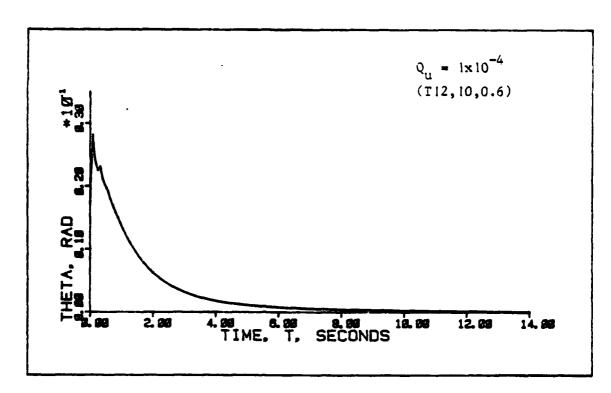


Figure 6-6a: Mean of 0 With First-Order Colored Noise Addition

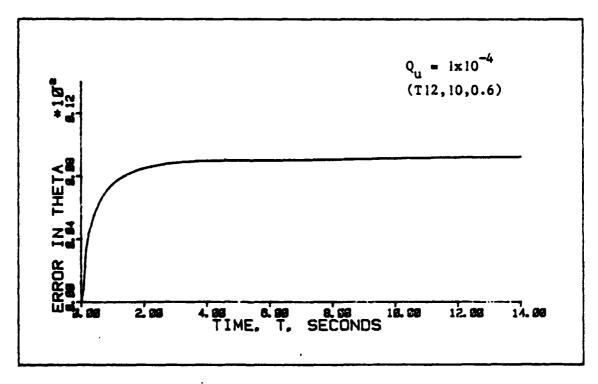


Figure 6-6b: Standard Deviation of 9 With First-Order Colored Noise Addition

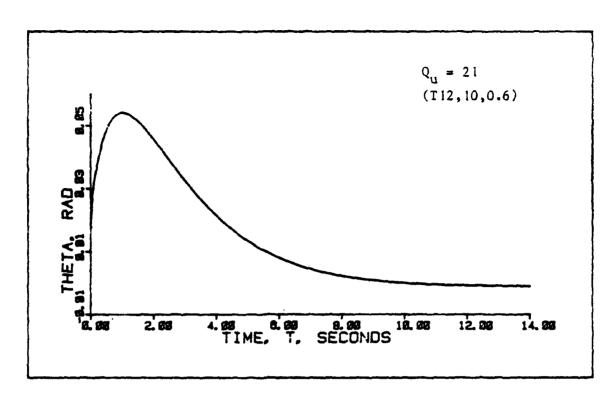


Figure 6-7a: Mean of 0 With Second-Order Colored Noise Addition

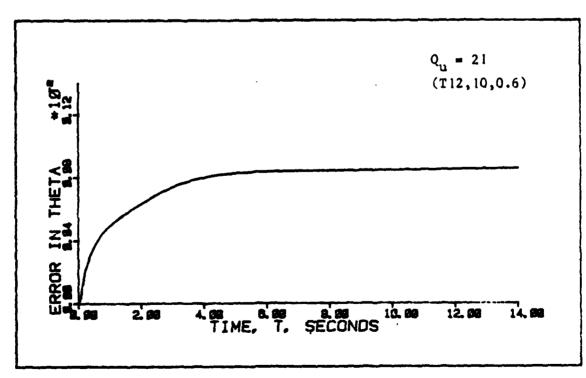


Figure 6-7b: Standard Deviation of 9 With Second-Order Colored Noise Addition

noise, white noise, and first-order and second-order time-correlated noise for one value of noise intensity. The values listed are the results of a performance evaluation where the unmodified controller design model and truth model are identical (both are of dimension eight at the design condition). The results shown in the table only partially substantiate the claim that time-correlated noise can minimize the performance degradation. The addition of white noise to the system model increased the standard deviation of all three aircraft states as expected.

It was expected that the addition of first-order colored noise would reduce the standard deviation of the aircraft states to values less than those for white noise, but still larger than the case with no noise addition. Table (6-2) shows that this is not the case. Rather, the standard deviations have increased, if only slightly for θ and α . Only the pitch rate, q, has decreased as expected. Recall from Figures (6-5a) and (6-6a) that white and first-order colored noise produce similar mean of theta responses. That is, the robustness enhancement is very similar for the two cases. However, even though the added uncertainty is applied over a

Table 6-2

Comparison of Steady-State Deviations of Aircraft States at the Design Condition for a Continuous Time System

	q ²	Qu	σθ	σα	σ _q
No noise	0	-	8.705×10 ⁻⁴	5.035×10 ⁻³	1.200x10 ⁻³
White Noise	1x10 ⁻⁴	-	9.590x10 ⁻⁴	5.306x10 ⁻³	1.978x10 ⁻³
lst-order Shaping Filter	-	1x10 ⁻⁴	1.006x10 ⁻³	5.823x10 ⁻³	1.761x10 ⁻³
2nd-order Shaping Filter	_	21	8.704x10 ⁻⁴	5.039x10 ⁻³	1.201x10 ⁻³

more limited frequency range when first-order colored noise is injected into the model, the standard deviations have increased slightly. This is not well understood, except to say that time-correlated noise actually changes the structure of the Kalman filter design model. The added complexity of the design model may overcome any benefits that are realized because the noise was not applied over all frequencies as in the white noise case.

As expected, the performance at design conditions is degraded less by using a second-order filter as opposed to a first-order filter or white noise. However, the greater complexity of the Kalman filter design model (four additional states in this case) is not justified by the performance benefits seen in Table (6-2). In this instance, white noise injected into the system design model provides the desired robustification while not degrading the performance at the design condition substantially.

Table (6-3) presents similar steady-state standard deviation information about the three aircraft states as shown in Table (6-2). However, the values listed here are the results of a performance evaluation of the eight-state controller evaluated against the twelve-state truth model, accounting for higher-order actuator dynamics. An important difference between Tables (6-2) and (6-3) is the effect of adding white input noise on the standard derivation of Θ . At the design condition, adding white noise detunes the filter and results in a performance degradation. However, when third-order actuator dynamics are included in the truth model, adding white noise improves the tuning for the Θ channel, and the standard deviation decreases for this state. Thus, when the performance

of the system is evaluated in an environment different from the design condition, the noise addition can result in a performance enhancement. It is seen that for this case, second-order time correlated noise again accomplishes improved filter tuning over first-order and white noise. The improvement, though, is still not substantial enough to justify the added complexity of the Kalman filter design model. White input noise, as stated above, accomplishes the desired robustness enhancement without adding states to the design model.

Table 6-3

Comparison of Steady-State Standard Deviations of Aircraft States with Higher-Order Actuator Dynamics for a Continuous-Time System.

	q 2	Q _u	σθ	σα	σ _q
No noise	0	-	8.984x10 ⁻⁴	4.894×10 ⁻³	1.189×10 ⁻³
White Noise	1x10 ⁻⁴	-	8.850x10 ⁻⁴	5.689x10 ⁻³	4.979x10 ⁻³
lst Order Shaping Filter	-	1x10 ⁻⁴	9.232x10 ⁻⁴	5.813x10 ⁻³	5.092x10 ⁻³
2nd Order Shaping Filter	_	21	8.571x10 ⁻⁴	5.168x10 ⁻³	1.969×10 ⁻³

6.2.2 Continuous-Time LQG Regulators at Off-Design Condition

Figure (6-8) shows the results of a performance analysis for the unrobustified system with a Kalman filter at an off-design flight condition (T12,20,0.6) for the eight-state controller design model. As shown in the figure, the system is unstable. The mean of θ is diverging, and the standard deviation is growing with time. In addition, the inputs generated by the controller are growing with time beyond the actual limits of the control surfaces (± 23) degrees for the horizontal tail and ± 20 degrees for the trailing-edge flap: Ref 27). This is demonstrated in the mean plots of Figure (6-9).

Figures (6-10a) and (6-10b) show the system responses at the same off-design flight condition, except now white noise of strength $q^2 = 1 \times 10^{-4}$ has been injected into the filter's sytem model at the control entry points. The addition of this noise is sufficient to stabilize the system, driving the aircraft state towards zero and the standard deviation of the state to a finite value. Figures (6-10c,d,e,f) demonstrate the trend for a lower and higher value of q. As noted before, stability is recovered with a very low noise strength. Higher values change only transient characteristics and the magnitude of the standard deviation. Figure (6-11) demonstrates that the mean of the commanded controls are no longer exceeding the physical limits of the control surfaces. However, the large initial changes in the command inputs do exceed the actuator rate limits of the control surfaces because there is no weighting on input rates in the cost function for an LQG regulator.

For a time-correlated noise generated by a first-order shaping filter with a maximum intensity of 1×10^{-4} , the results are similar to those of

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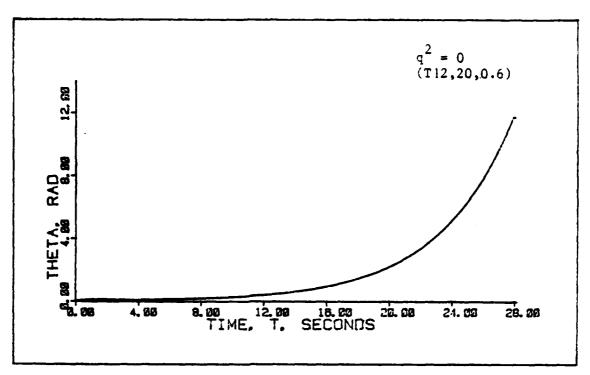
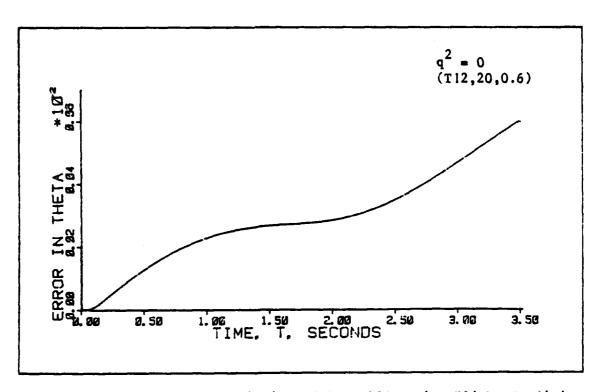


Figure 6-8a: Mean of Theta at Off Design Flight Condition



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Figure 6-8b: Standard Deviation of θ at Off-Design Flight Condition

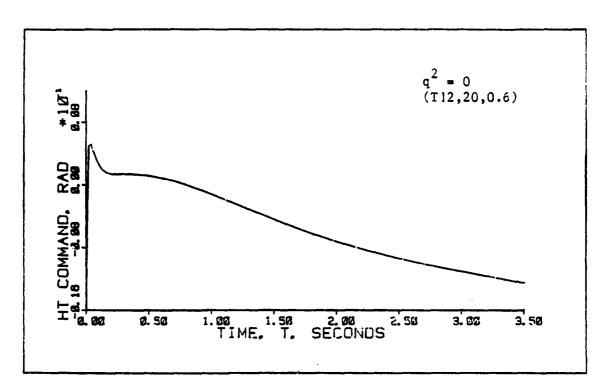


Figure 6-9a: Mean of Horizontal Tail Commanded Deflection

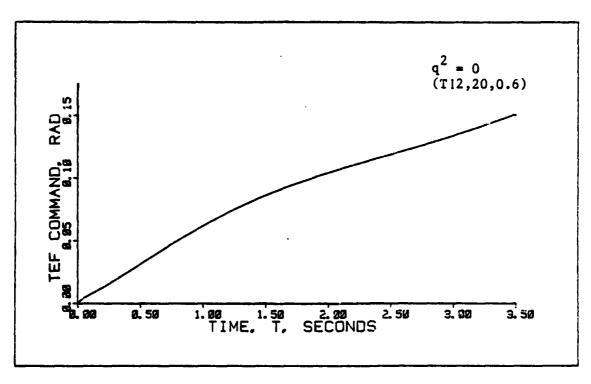


Figure 6-9b: Mean of Trailing Edge Flap Commanded Deflection

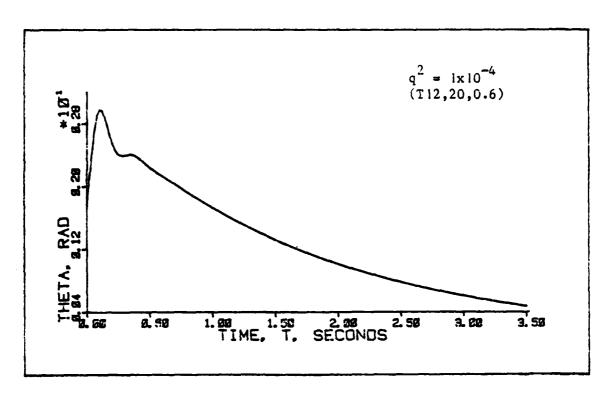
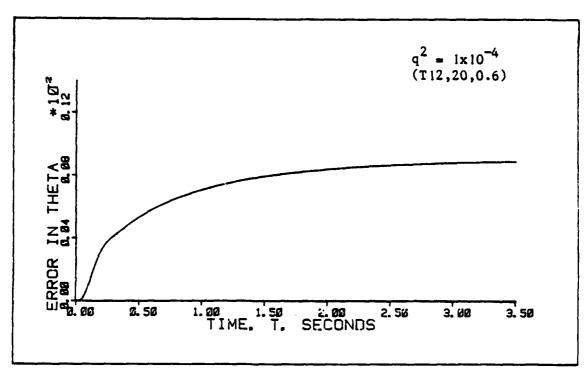


Figure 6-10a: Mean of θ With White Moise Addition at Off-Design Flight Condition



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Figure 6-10b: Standard Deviation of θ With White Noise Addition at Off-Design Flight Condition

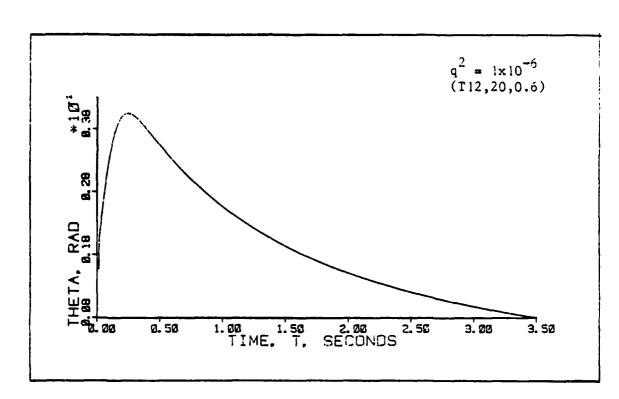


Figure 6-10c: Mean of Θ With White Noise Addition with an Off-Design Flight Condition

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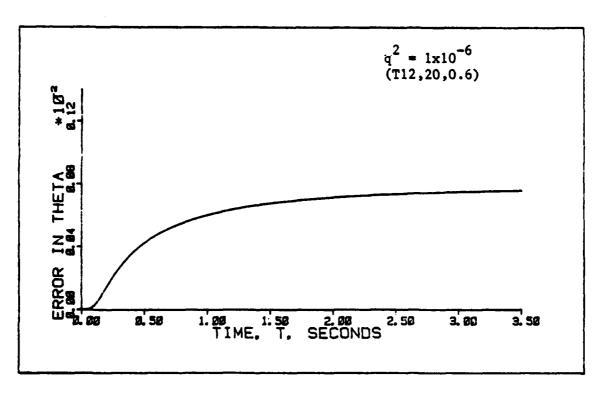


Figure 6-10d: Standard Deviation of Θ With Whise Noise Addition at An Off-Design Flight Condition

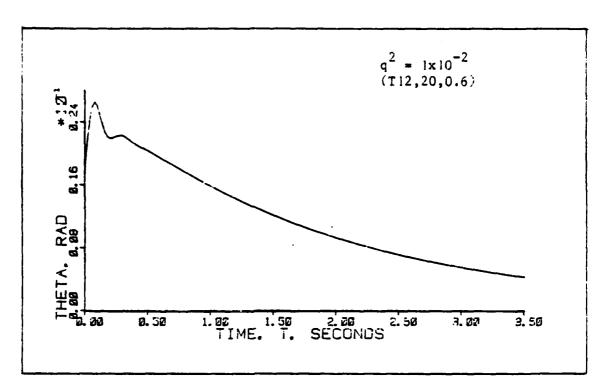


Figure 6-10e: Mean of ⊖ With White Noise Addition at Off-Design Flight Condition

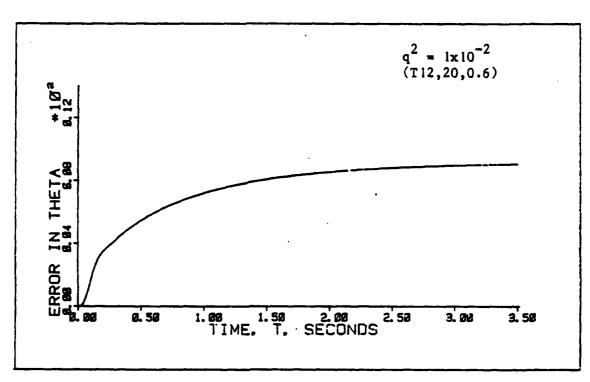


Figure 6-10f: Standard Deviation of Θ With White Noise Addition at Off-Design Flight Condition

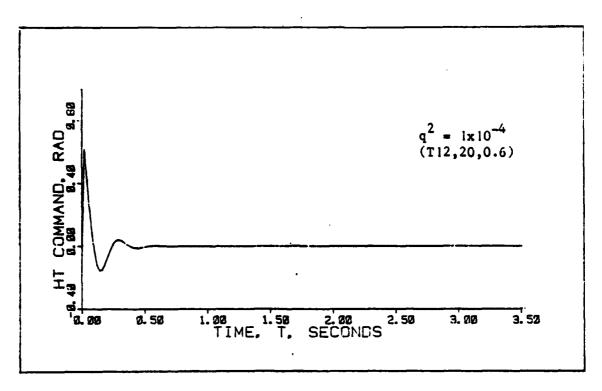


Figure 6-11a: Mean Horizontal Tail Commanded Deflection With White Noise Addition

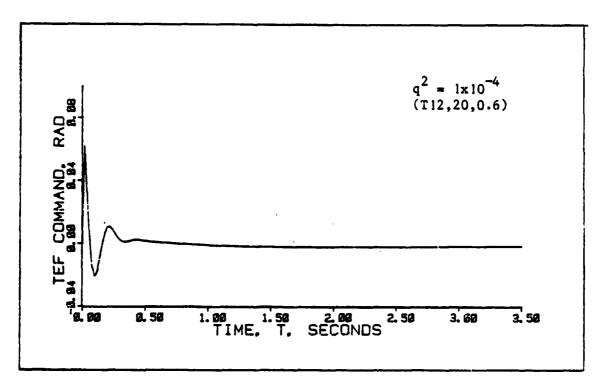


Figure 6-11b: Mean Trailing Edge Flap Commanded
Deflection With White Noise Addition

the white noise. This is shown in Figure (6-12). At the off-design flight condition which was initially unstable with no noise addition, the response is stable with the mean of θ approaching zero, and the standard deviation approaching a finite value.

As shown in Figure (6-13), the addition of colored noise generated by a second-order shaping filter with a maximum intensity of $1x10^{-4}$ is not sufficient to stabilize the system. The standard deviation of θ is growing with time, although the mean is approaching zero. However, increasing the intensity to $1x10^{-2}$, the standard deviation does approach a finite value as shown in Figure (6-14).

Thus, Figures (6-10) through (6-14) demonstrate that the stability robustness of the controlled system is enhanced by the addition of all three types of input noise, such that the response of the system is stable even in the face of parameter changes in the real world. White and firstorder colored noise of the same maximum intensity produce very similar results. Robustness can also be improved using second-order colored noise, but a greater maximum noise intensity is necessary to achieve a comparable response to the previous two cases. Figure (6-15) shows a power spectral density plot of the second-order time-correlated noise for the case of Q_{ij} = 2100. The magnitude of the time-correlated noise at low frequencies (at 0.1 Hz and below) was found to be 1.3x10⁻⁶, after converting from decibels to a linear magnitude scale. Inputting a white noise of this approximate intensity is sufficient to recover the stability of the system as is demonstrated in Figure (6-16). This implies that the robustness improvement is not primarily due to the time-correlated noise concentrated around 70 rad/sec; rather the magnitude of the noise

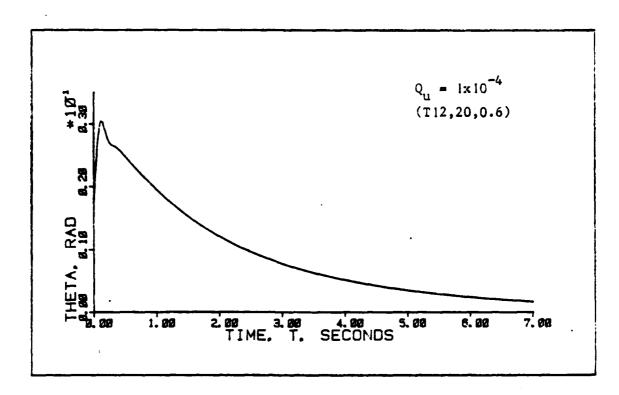


Figure 6-12a: Mean of Θ With First-Order Colored Noise Addition at Off-Design Flight Condition

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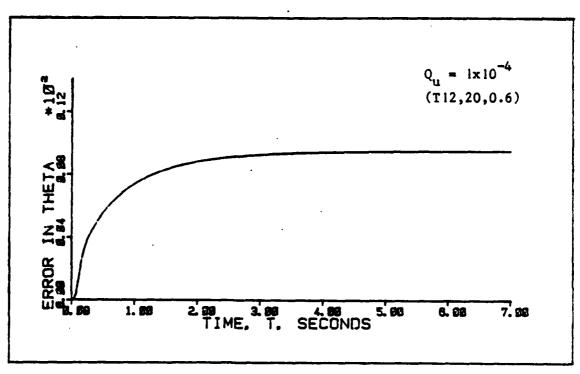


Figure 6-12b: Standard Deviation of Θ With First-Order Colored Noise Addition at Off-Design Flight Condition

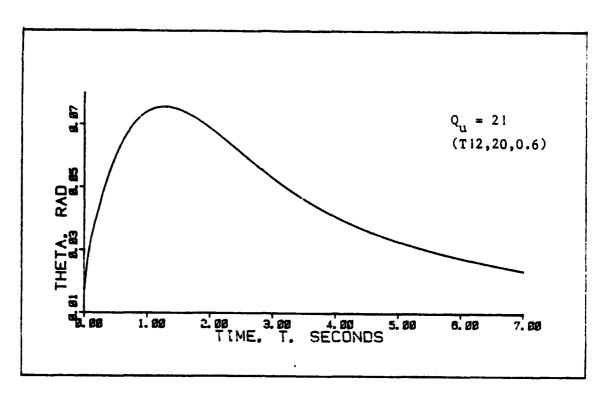


Figure 6-13a: Mean of Θ With the Second-Order Colored Noise Addition at Off-Design Flight Condition

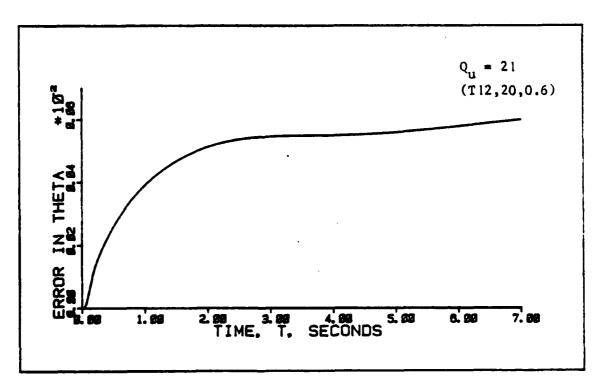


Figure 6-13b: Standard Deviation of © With Second-Order Colored Noise Addition at Off-Design Flight Condition

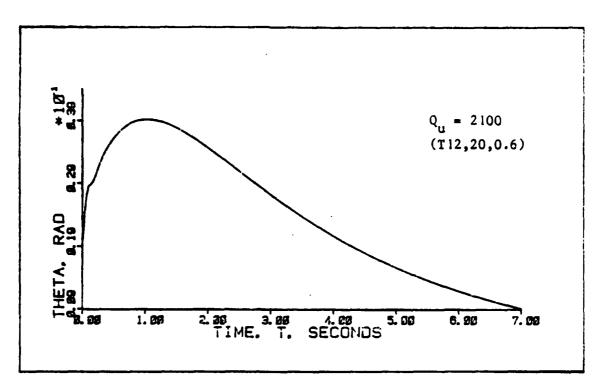
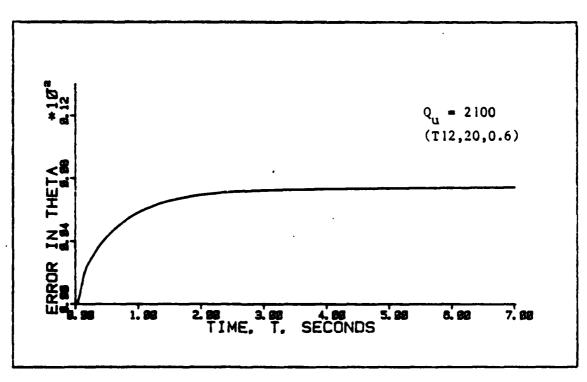
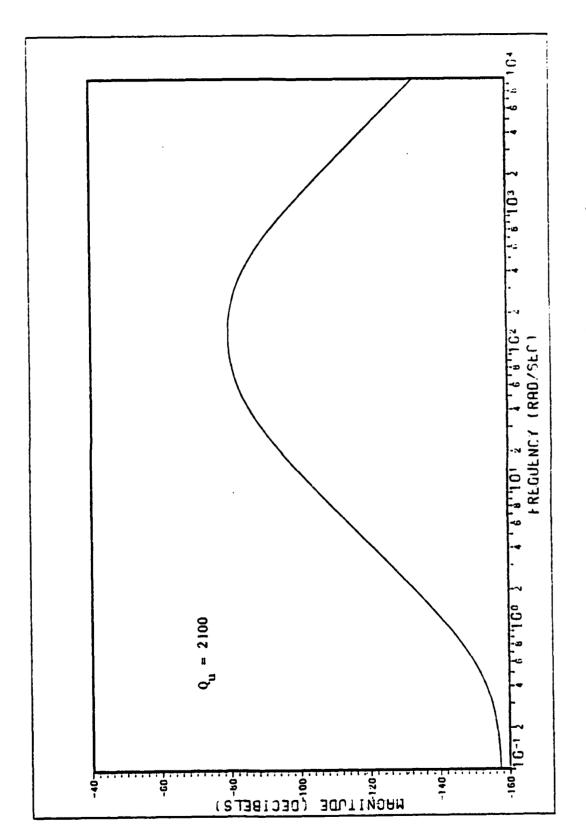


Figure 6-14a: Mean of ⊖ With Second-Order Colored Noise Addition at Off-Design Flight Condition



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Figure 6-14b: Standard Deviation of @ With Second-Order Colored Noise Addition at Off-Design Flight Condition



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Figure 6-15: Power Spectral Density Function for a Second-Order Colored Noise Process

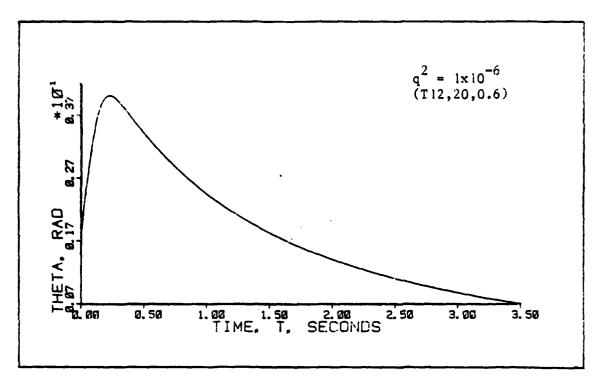
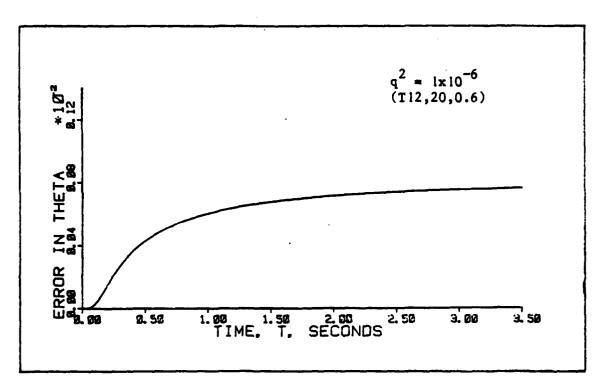


Figure 6-16a: Mean of Θ With White Noise Addition at Off-Design Flight Condition



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Figure 6-16b: Standard Deviation of Θ With White Noise Addition at Off-Design Flight Condition

elsewhere is sufficiently high to achieve the desired robustification.

6.2.3 Discretized Continuous-Time LQG Regulators at Design Condition

This method of extending the robustification techniques to discretetime systems was introduced in Section 2.7.1. A continuous-time
controller identical to that of Sections 6.2.1 and 6.2.2 is designed, then
discrete controller equations are formed by making first-order approximations to the discrete controller gain matrices. The sample rate of the
discretized controller is 50 Hertz. The design model matrices are given
in Section 6.4.

The time histories of the mean and standard deviation of θ for the eight-state controller evaluted against a truth model of the same dimension are shown in Figure (6-17). Again, the state was given a perfectly known initial condition of one degree. The performance of the discretized controller is very similar to that for the continuous-time case; the state converges to zero fairly slowly. This similarity is as expected since the sample period is short compared to natural system transients. Figure (6-18) shows the response of the same controller evaluated against a twelve-state truth model with higher-order actuator models. As can be seen, changing the environment in which the controller is evaluated introduces a slightly larger initial overshoot and steady-state error in the mean of θ response. Again, the unmodified system does not display good robustness properties.

Figure (6-19) shows the response of the same controller with the filter robustified by adding a white noise of strength $q = 1x10^{-6}$ to the design model. The improvement in transient time, initial overshoot, and

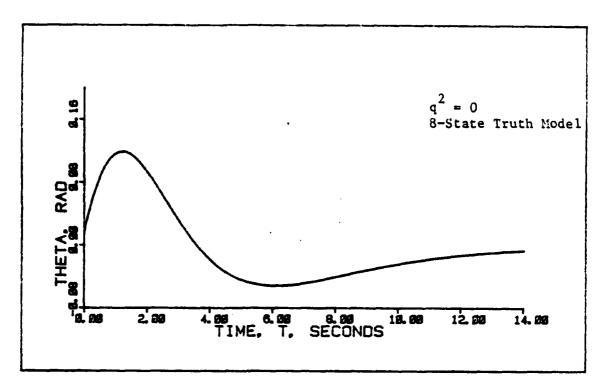


Figure 6-17a: Mean of Θ at the Design Condition

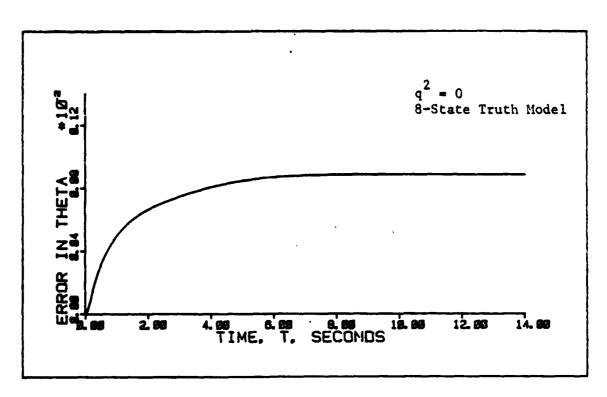


Figure 6-17b: Standard Deviation of Θ at the Design Condition

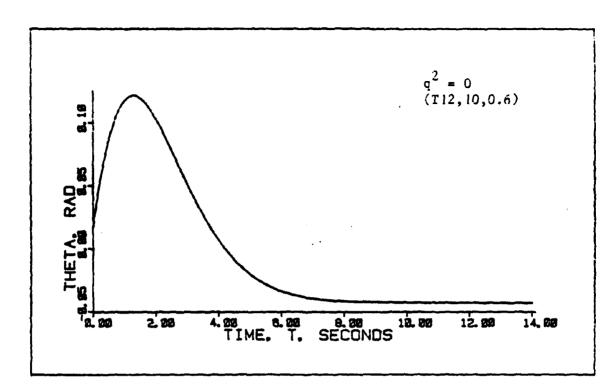


Figure 6-18a: Mean of ⊖ With No Noise Addition

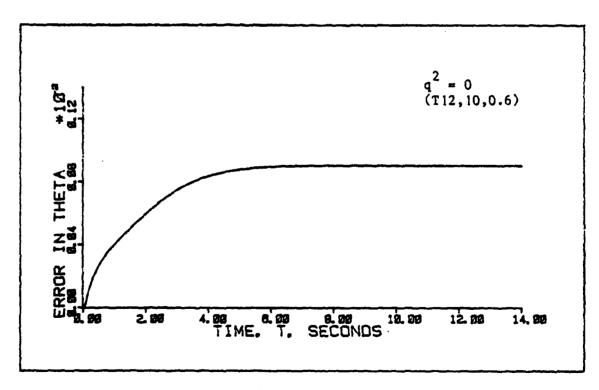


Figure 6-18b: Standard Deviation of Θ With No Noise Addition

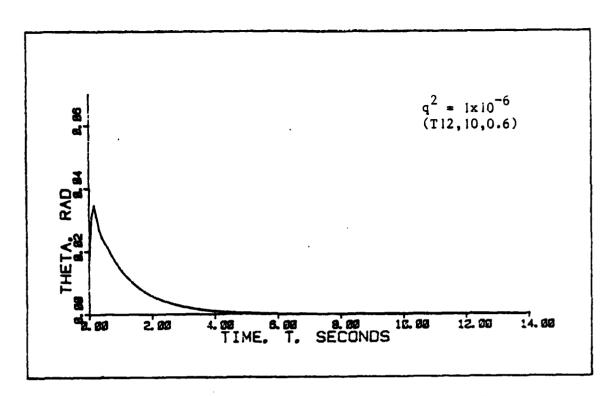


Figure 6-19a: Mean of Θ With White Noise Addition

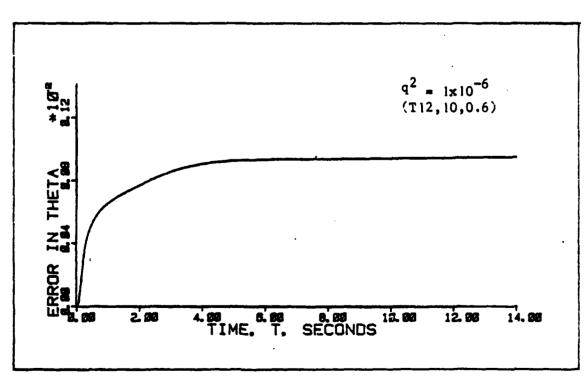


Figure 6-19b: Standard Deviation of Θ With White Noise Addition

steady-state value is comparable to the continuous-time case with no noticeable change in the standard deviation.

The results of applying colored noise generated by a first-order shaping filter are shown in Figure (6-20). The overshoot is larger than for the white noise addition, and there is still a slight steady-state mean error, but the improvement over the unrobustified case is still substantial.

It was found that augmenting second-order shaping filter states with the design model, designing a continuous-time controller, than discretizing the concroller produced an unstable closed-loop system for any value of Q_{μ} . This characteristic was not observed in the continuous-time case.

In addition, as described previously in Reference 21, it was observed that the strength of the white and colored noise could not be adjusted arbitrarily upwards. It was found that, with the twelve-state truth model (T12,10,0.6), q^2 and Q_u could be adjusted between zero and 1×10^{-6} , and the robustification improvement was similar to the continous-time case. However, noise intensities beyond this value $(Q_u = 2 \times 10^{-6})$ would actually drive closed-loop system eigenvalues outside of the z-domain unit circle.

A comparison of the steady-state values of the standard deviations of the aircraft states are given in Table (6-4). The table includes values for a system with no noise addition, white and first-order colored noise of the same maximum intensity. The results are similar to the continuous-time case. It is seen that the addition of white noise increases the values of the standard deviations of the states. As in the previous case, colored noise addition generated by a first-order shaping filter did not yield lower standard deviations than white noise

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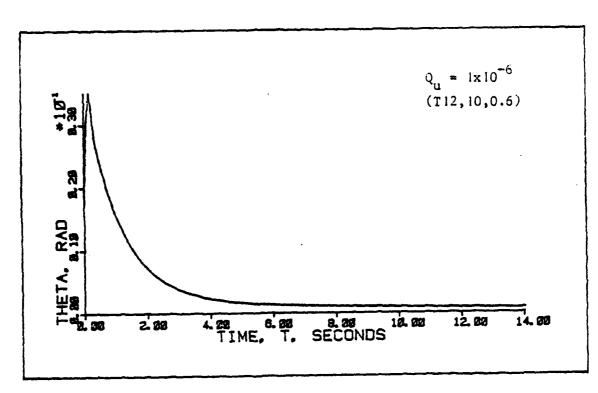
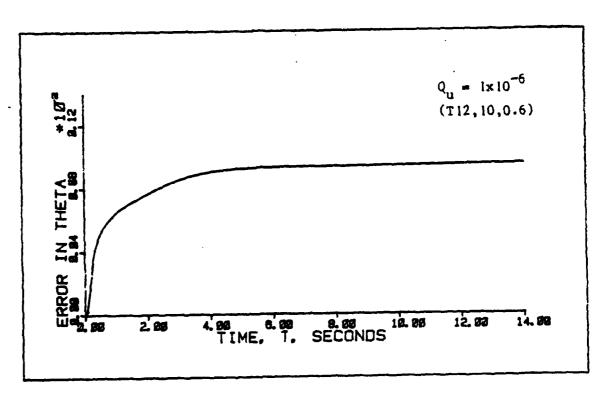


Figure 6-20a: Mean of Θ With First-Order Colored Noise Addition



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Figure 6-20b: Standard Deviation of @ With First-Order Colored Noise Addition

Table 6-4

Comparison of Steady-State Standard Deviations of Aircraft States at the Design Condition for a Discretized Continuous-Time System

	q ²	Q _u	σ _Θ	σα	σ _q
No Noise	0	-	8.877x10 ⁻⁴	5.035x10 ⁻³	1.258x10 ⁻³
White Noise	1x10 ⁻⁴	-	9.645x10 ⁻⁴	5.310x10 ⁻³	2.113x10 ⁻³
lst Order Shaping Filter	-	1x10 ⁻⁴	1.005x10 ⁻³	5.821x10 ⁻³	1.817x10 ⁻⁴
2nd Order Shaping Filter	-	-	Unstable	Unstable	Unstable

Table 6-5

Comparison of Steady-State Standard Deviations of Aircraft States With Higher-Order Actuators For a Discretized Continuous-Time System

	q ²	Q _u	σ _Θ	^σ α.	σq
No Noise	0	1	9.053x10 ⁻⁴	4.899x10 ⁻³	1.257×10 ⁻³
White Noise	1x10 ⁻⁶	-	9.511x10 ⁻⁴	5.198x10 ⁻⁴	2.825x10 ⁻⁴
lst Order Shaping Filter	-	1×10 ⁻⁶	9.524x10 ⁻⁴	5.212x10 ⁻³	2.758x10 ⁻⁴
2nd Order Shaping Filter	-	-	Unstable	Unstable	Unstable



addition except for the pitch rate, q. Table (6-5) indicates identical trends for the case where higher-order dynamics are included in the truth model. The lower maximum noise intensity than that used for Table (6-4) reflects the fact that, with a higher-dimension truth model, the closed-loop system is driven unstable for a lower value of q^2 .

Thus, it is seen that the desired robustness enhancement can be gained by adding white input noise to the system model. Time-correlated noise is not appropriate for this problem because it does not yield performance benefits and only serves to increase the complexity of the design model.

6.2.4 Discretized Continuous-Time LQG Regulators at Off-Design Condition

Figure (6-21) demonstrates that the system exhibits an unstable response when the flight condition is changed to an altitude of 20000 feet and a Mach number of 0.6 (T12,20,0.6).

Again, it was found that the robustness characteristics could be improved with the injection of white and colored noise for a finite range of q^2 and Q_u . At the off-design condition, for values of q^2 and Q_u beyond 2.5x10⁻⁵, the closed-loop system was unstable.

The response of the system with the maximum value of q^2 is shown in Figures (6-22a) and (6-22b). As can be seen, the stability has been recovered, indicating that the full-state feedback system was stable. Thus, by the addition of white input noise, the characteristics approach that of a full-state feedback controller. Figures (6-22c) and (6-22d) show that stability is recovered with a lower value of q^2 . Increasing it beyond this value changes only the transients of the mean and the magnitude of the standard deviation.

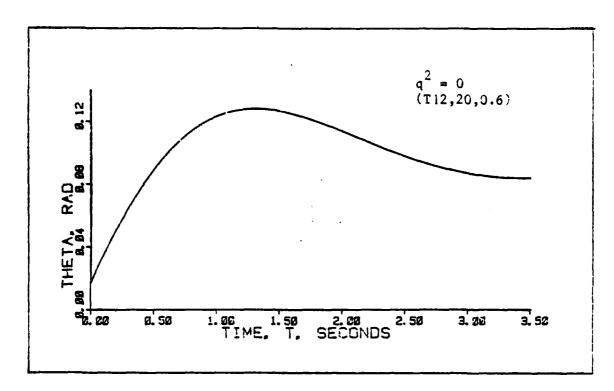


Figure 6-21a: Mean of Θ With No Noise Addition at Off-Design Flight Condition

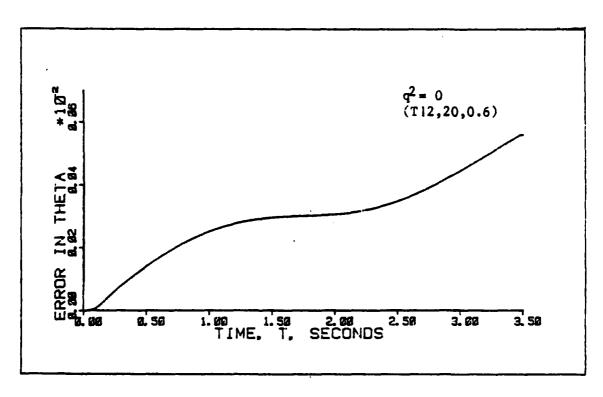


Figure 6-21b: Standard Deviation of Θ With No Noise Addition at the Off-Design Flight Condition

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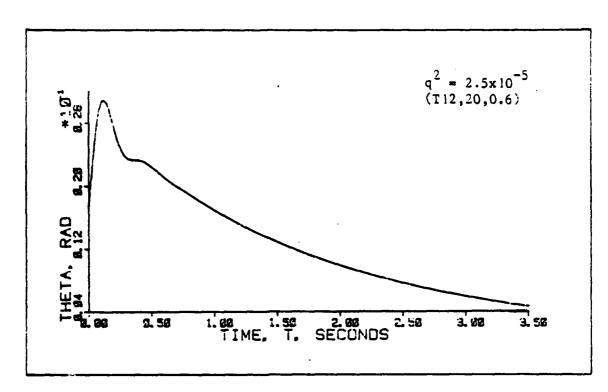


Figure 6-22a: Mean of Θ With White Noise Addition at Off-Design Flight Condition

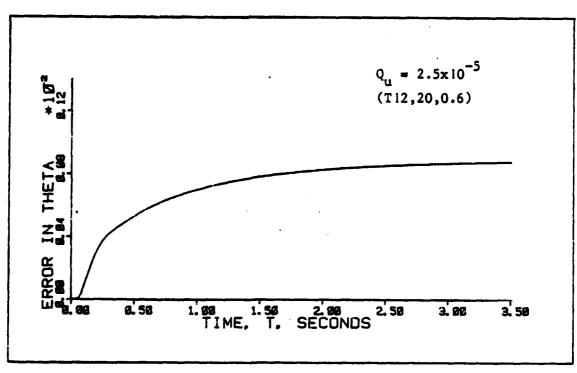


Figure 6-22b: Standard Deviation of ⊖ With White Noise Addition at the Off-Design Flight Condition

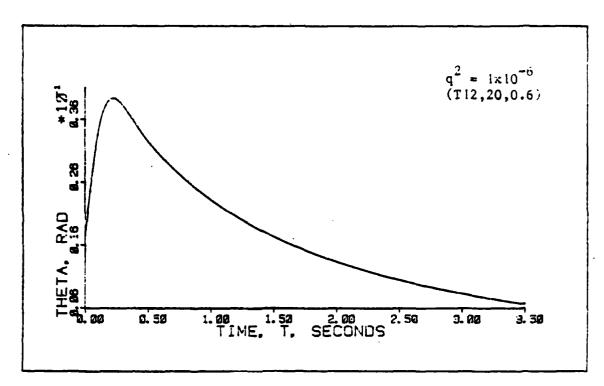


Figure 6-22c: Mean of Θ With White Noise Addition at an Off-Design Flight Condition

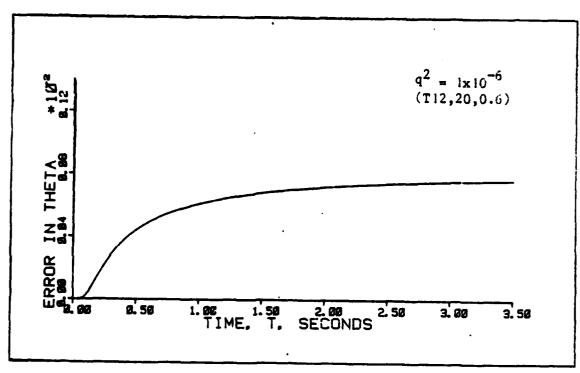


Figure 6-22d: Standard Deviation of Θ With White Noise Addition at an Off-Design Flight Condition

Figure (6-23) demonstrates that adding colored noise generated by a first-order shaping filter achieves the same degree of robustness enhancement with only an increase in the initial overshoot of θ compared to that of Figure (6-22a). The steady-state standard deviations of Figures (6-22b) and (6-23b) are not significantly different.

Augmenting second-order shaping filter states with the system model again resulted in an unstable closed-loop system. For any non-zero value of $\mathbf{Q}_{\mathbf{u}}$, some of the closed-loop system eigenvalues were driven outside the unit circle in the z-domain.

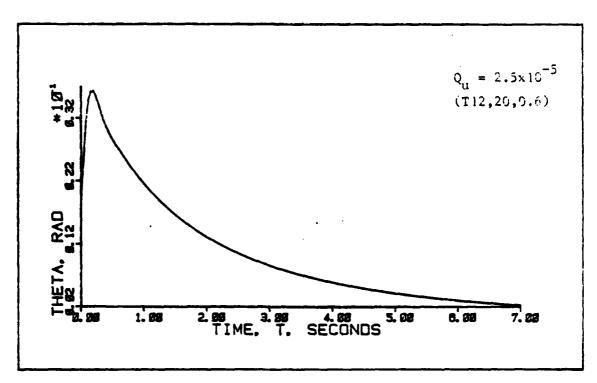
Because of the sensitivity of the system to slight changes in the strength of the added noise, it is felt that this method is inappropriate for this problem. The range of admissible values for q^2 and Q_u is very slight, and the loss of closed-loop system stability is very abrupt when the range is exceeded. In addition, there is no range of Q_u which improves the robustness characteristics of the controlled system when colored-noise generated by a second-order filter is added to the model.

6.2.5 Sampled-Data LQG Regulators at Design Condition

This method of extending the robustification techniques to sampled-data systems was introduced in Section 2.7.2. For this case, the continuous-time system equations are discretized, then a sampled-data Kalman filter and controller are designed from the onset.

The results of performance analyses for the sampled-data controller with a sample rate of 50 Hertz are found to be extremely similar to those for the continuous-time controller.

Figure (6-24) shows the response of θ to an initial condition of one degree. This is the result of a performance analysis where the dimensions



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Figure 6-23a: Mean of Θ With First-Order Colored Noise Addition at Off-Design Flight Condition

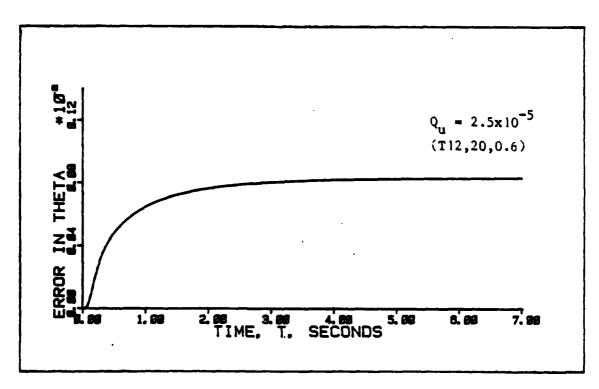


Figure 6-23b: Standard Deviation of Θ With First-Order Colored Noise Addition at an Off-Design Flight Condition

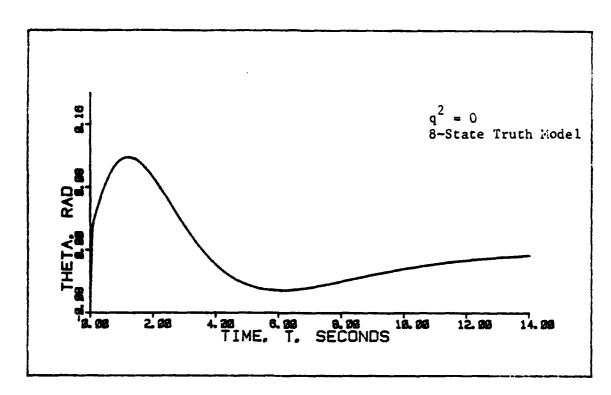


Figure 6-24a: Mean of Θ at the Design Condition

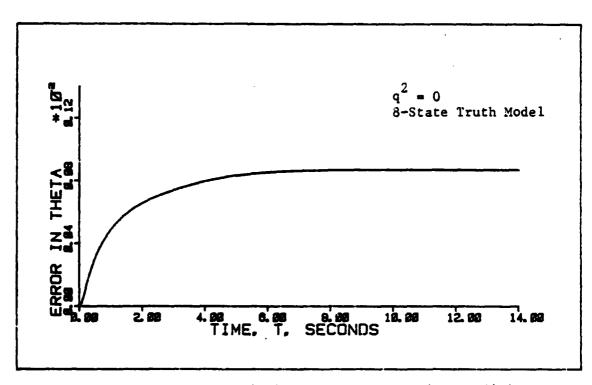


Figure 6-24b: Standard Deviation of Θ at the Design Condition

of the truth model and the design model are the same (Section 5.4). As observed previously, the mean of Θ converges slowly to zero. Figure (6-25) shows the response of the same controller when higher-order actuator dynamics are introduced in the truth model. Again, large initial overshoots and steady-state mean errors are introduced. The unmodified sampled-data controller does not exhibit good robustness properties when certain states are ignored in the design model.

With the addition of white input noise, (as described in Section 2.7.2), the undesirable characteristics of the unrobustified system do not appear in the time response. This is shown in Figures (6-26a) and (6-26b). Figures (6-26c,d,e,f) show the trend for a higher and lower value of q^2 . Increasing the magnitude of the white noise changes the transient mean response and the magnitude of the standard deviation. For this problem (where the evaluation was performed using the truth model (T12,10,0.6), in the range of values of q^2 that were examined $(0 \le q^2 \le 1)$, the dramatic instabilities observed in Sections 6.2.3 and 6.2.4 do not occur.

Figure (6-27) demonstrates that nearly identical robustness benefits can be gained with the addition of colored noise generated by a first-order shaping filter as with a white noise. However, the addition of colored noise generated by a second-order shaping filter does not have the fast time response of the previous two cases, as shown in Figure (6-28). Nonetheless, the steady-state error and initial overshoot have been substantially improved.

Table (6-6) makes a comparison of the steady-state values of all three aircraft states at the design condition (truth and model dimension equal) for cases with no noise addition, white noise, and first- and

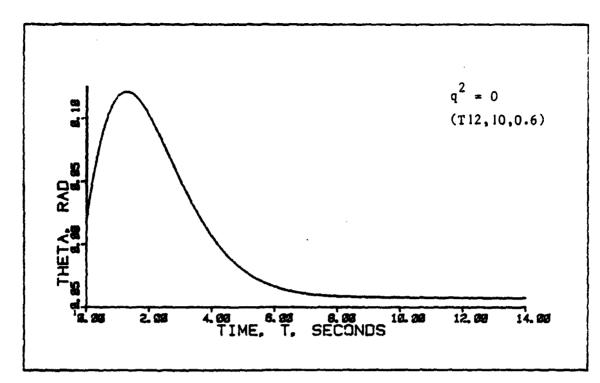


Figure 6-25a: Mean of Θ With No Noise Addition

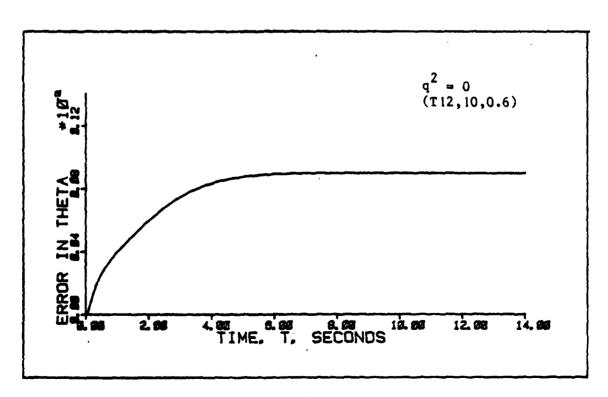


Figure 6-25b: Standard Deviation of 0 With No Noise Addition

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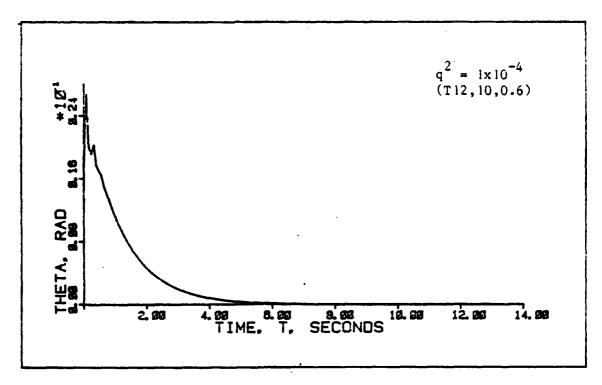


Figure 6-26a: Mean of Θ With White Noise Addition

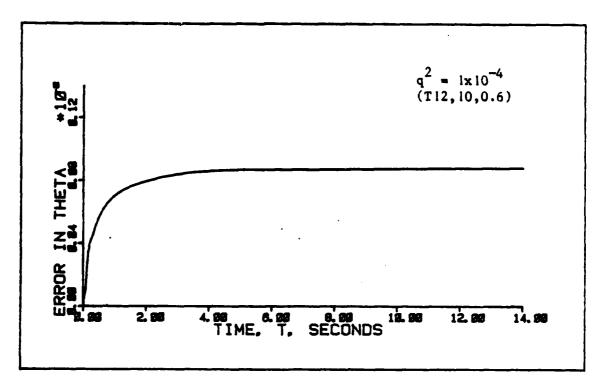


Figure 6-26b: Standard Deviation of Θ With White Noise Addition

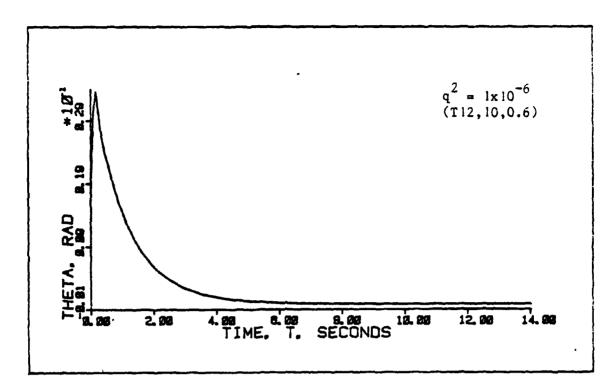


Figure 6-26c: Mean of Θ With White Noise Addition

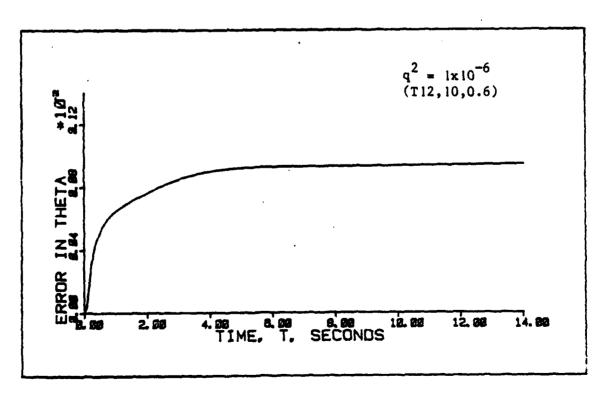


Figure 6-26d: Standard Deviation of @ With White Noise Addition

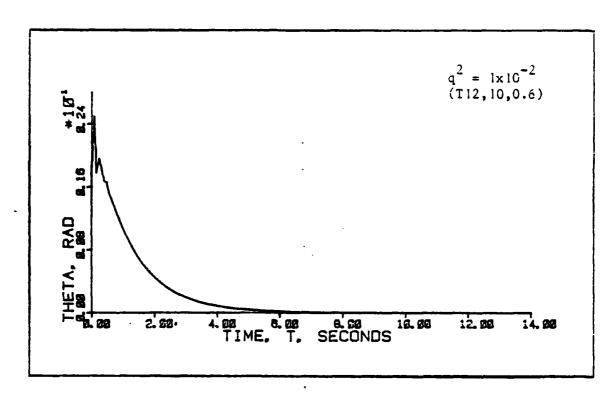


Figure 6-26e: Mean of Θ With White Noise Addition

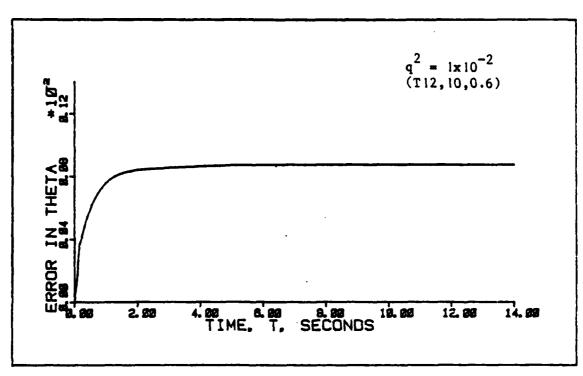


Figure 6-26f: Standard Deviation of 9 With White Noise Addition

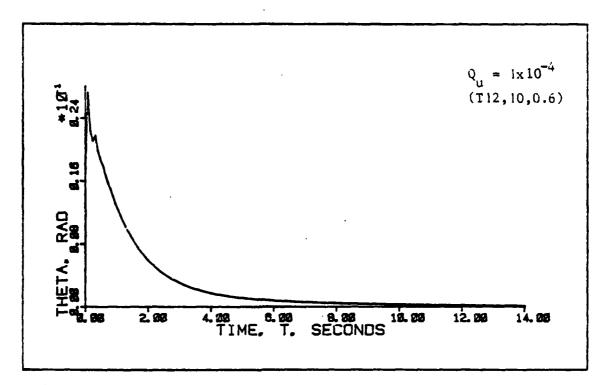


Figure 6-27a: Mean of Θ With First-Order Colored Noise Addition

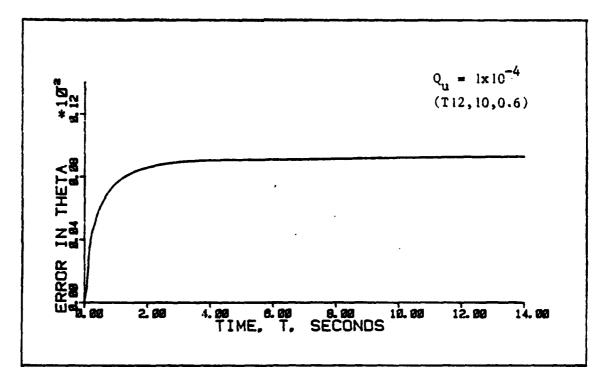


Figure 6-27b: Standard Deviation of © With First-Order Colored Noise Addition

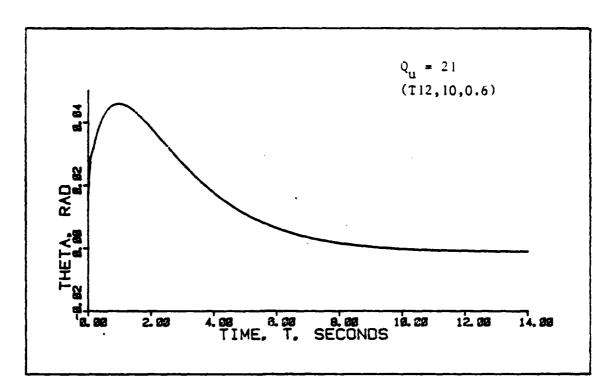


Figure 6-28a: Mean of 9 With Second-Order Colored Noise Addition

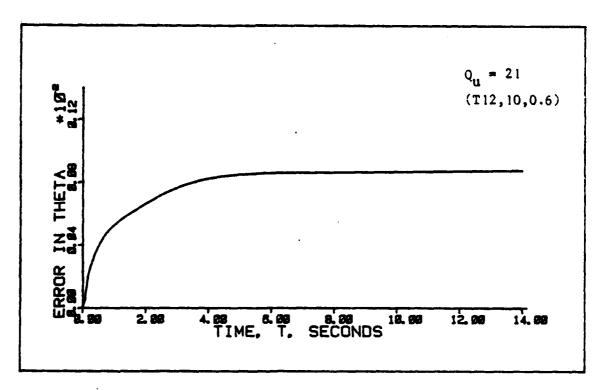


Figure 6-28b: Standard Deviation of Θ With Second-Order Colored Noise Addition

Table 6-6

Comparison of Steady-State Standard Deviations of Aircraft States at the Design Condition For A Sampled-Data System

	q ²	Qu	σ _Q	σ _α	σ _q
No Noise	0	-	8.712×10 ⁻⁴	5.036×10 ⁻³	1.206x10 ⁻³
White Noise	1x10 ⁻⁴	-	9.583x10 ⁻⁴	5.307x10 ⁻³	1.980x10 ⁻³
lst Order Shaping Filter	-	1x10 ⁻⁴	1.002x10 ⁻³	1.842×10 ⁻³	1.765×10 ⁻³
2nd Order Shaping Filter	-	21	8.700x10 ⁻⁴	5.040×10 ⁻³	1.208×10 ⁻³

second-order colored noise. The results are essentially the same as for the continuous-time controller. The same trend is observed in Table (6-7) where higher-order actuator dynamics are included in the truth model. As in the continuous-time case, adding white noise to the model does degrade the performance for all states at the design condition. However, when third-order dynamics are included in the truth model, white input noise decreases the standard deviation Θ . When the filter is evaluated in an environment other than the design condition, adding noise can improve the filter tuning. Decreases in the standard deviations appear in all states for second-order colored noise, and they are not substantial enough to justify the added complexity of the design model. Thus, the Doyle and Stein technique extended to a sampled-data system provides the desired robustification against ignored states for the problem considered in this thesis. Significant performance benefits are not gained by adding time-correlated noise to the system model as opposed to white noise.

Table 6-7

Comparison of Steady-State Standard Deviations
Of Aircraft States with Higher-Order Actuator
Dynamics For A Sampled-Data System

	q ²	Qu	σ _Θ	σα	σ _q
No noise	0	-	8.984x10 ⁻⁴	4.894×10 ⁻³	1.197×10 ⁻³
White Noise	1x10 ⁻⁴	-	8.831x10 ⁻⁴	5.689×10 ⁻³	4.859x10 ⁻³
1st Order Shaping Filter	-	1x10 ⁻⁴	9.311×10 ⁻⁴	5.815×10 ⁻³	5.143×10 ⁻³
2nd Order Shaping Filter	_	21	8.789x10 ⁻⁴	5.170x10 ⁻³	2.342x10 ⁻³

6.2.6 Sampled-Data LQG Regulators at Off-Design Condition

As shown in Figure (6-29), the response of the system is unstable at the off-design flight condition with no noise addition.

White noise addition of strength $q^2 = 1 \times 10^{-4}$, as shown in Figure (6-30) is sufficient to recover the stability of the system. First-order colored noise of the same maximum intensity produces a very similar response, as shown in Figure (6-31). However, second-order colored noise of the same maximum intensity is not sufficient to recover stability completely as demonstrated by the divergence of the standard deviation in Figure (6-32). Increasing the maximum noise intensity to 1×10^{-2} achieves the desired stability characteristics as shown in Figure (6-33), but the time response is still much slower than for the previous two cases.

It is observed in Figures (6-29) through (6-33) that all three types of input noise substantially improve the robustness properties of the

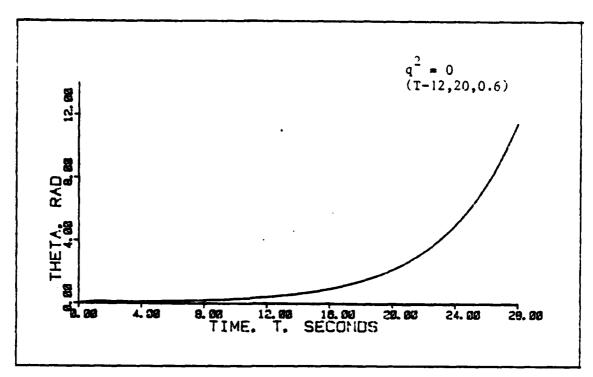


Figure 6-29a: Mean of Θ With No Noise Addition at the Off-Design Flight Condition

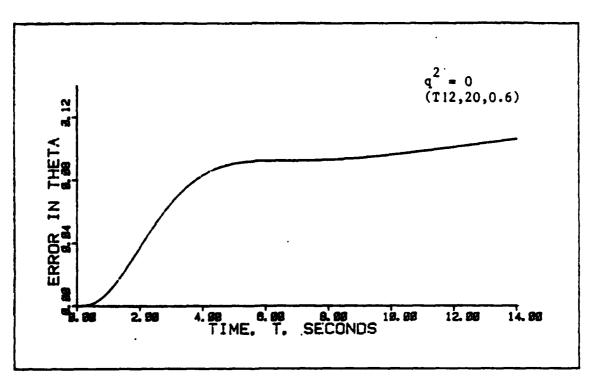


Figure 6-29b: Standard Deviation of Θ With No Noise Addition at the Off-Design COndition

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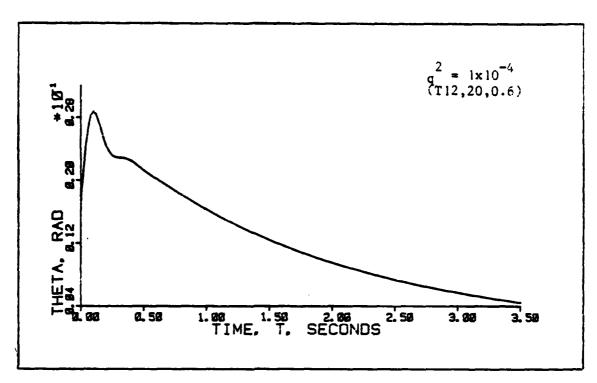


Figure 6-30a: Mean of Θ With White Noise Addition Off-Design Flight Condition

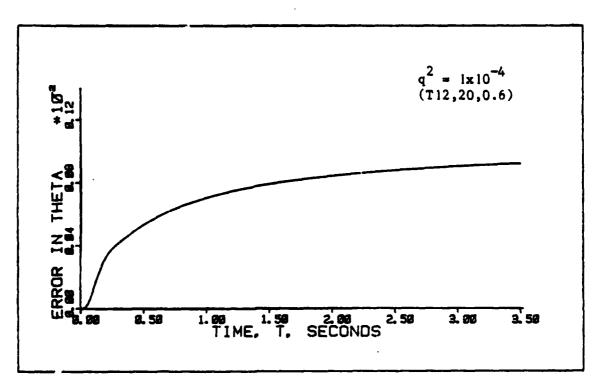


Figure 6-30b: Standard Deviation of ⊖ With White Noise Addition at the Off-Design Flight Condition

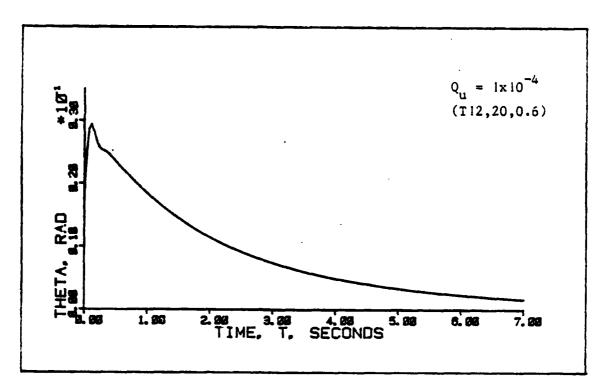


Figure 6-31a: Mean of Θ With First-Order Colored Noise Addition at the Off-Design Flight Condition

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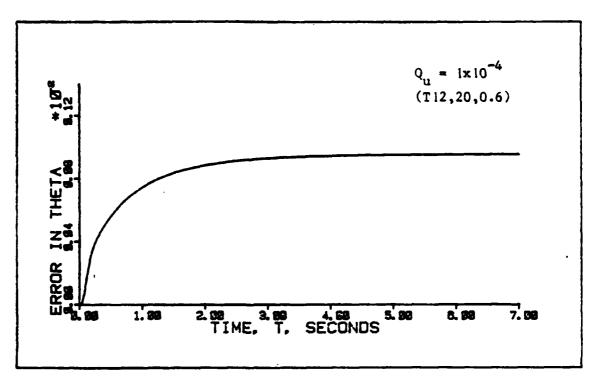


Figure 6-31b: Standard Deviation of Θ With First-Order Colored Noise Addition at the Off-Design Flight Condition

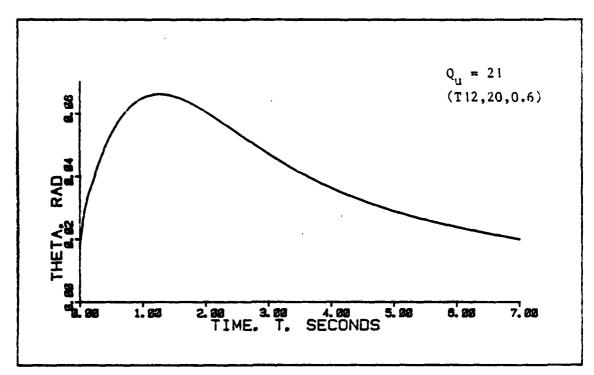


Figure 6-32a: Mean of Θ With Second-Order Colored Noise Addition at the Off-Design Flight Condition

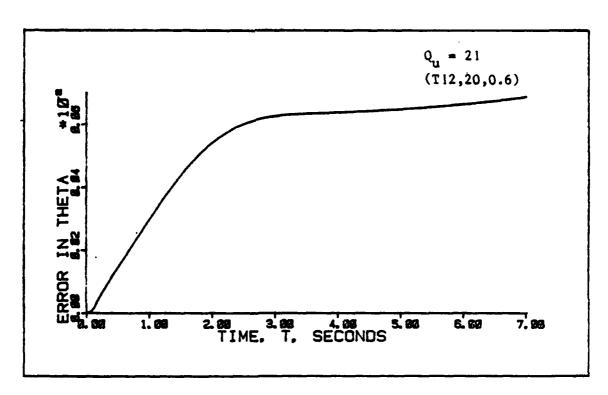


Figure 6-32b: Standard Deviation of Θ With Second-Order Colored Noise Addition at the Off-Design Flight Condition

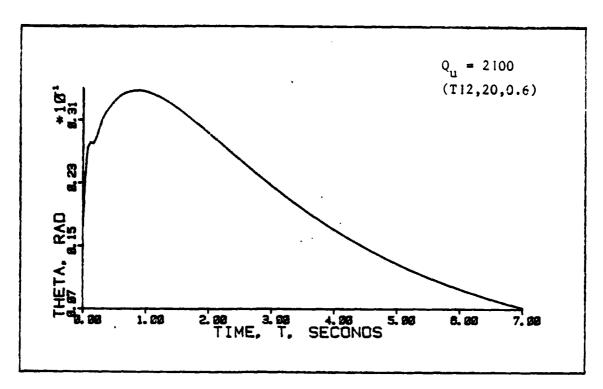


Figure 6-33a: Mean of Θ With Second-Order Colored Noise Addition at the Off-Design Flight Condition

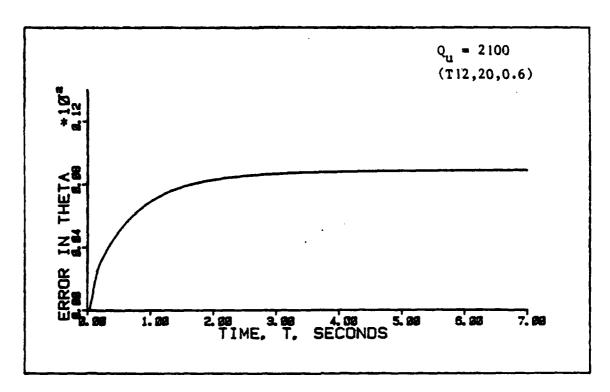


Figure 6-33b: Standard Deviation of © With Second-Order Colored Noise Addition at the Off-Design Flight Condition

meters. The improvement due to the addition of white and first-order colored noise is very similar. This indicates that even at the off-design flight condition, the design model is still fairly adequate at low frequencies where the power spectral density of the first-order colored noise is low. Robustness can also be enhanced with second-order colored noise to a lesser degree if the maximum intensity of the noise is sufficiently high. As in the continuous-time case, it is felt that this effect is partially due to the magnitude of the noise at other frequencies, not just the peak near 70 radians/second.

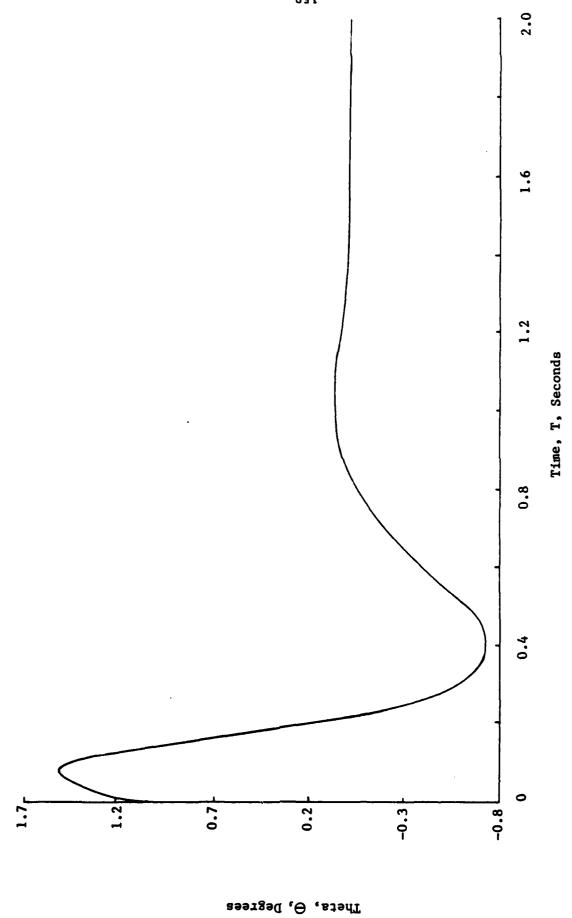
6.3 Sampled-Data PI Controllers

The results of applying the Doyle and Stein technique to a sampled-data PI controller were inconclusive for this problem. However, some results are presented to show how employing a Kalman filter to estimate the states of a system can adversely affect stability.

The software used to design the PI controller allows the design of a full-state feedback controller or one with a Kalman filter in the loop. The performance analysis program then generates time histories of the standard deviation of the states both with and without a filter.

The weighting on the states, controls and control rates are defined in Section 3.2.2 and are given below:





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Figure 6-34: Full-State Feedback PI Controller Response of ⊖

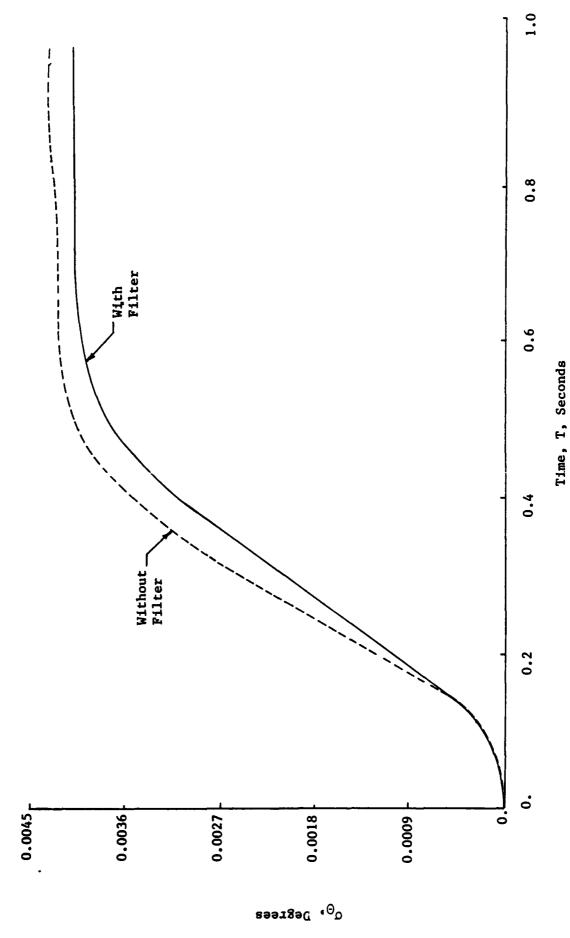


Figure 6-35: Standard Deviation of $\boldsymbol{\theta}$ at Design Condition

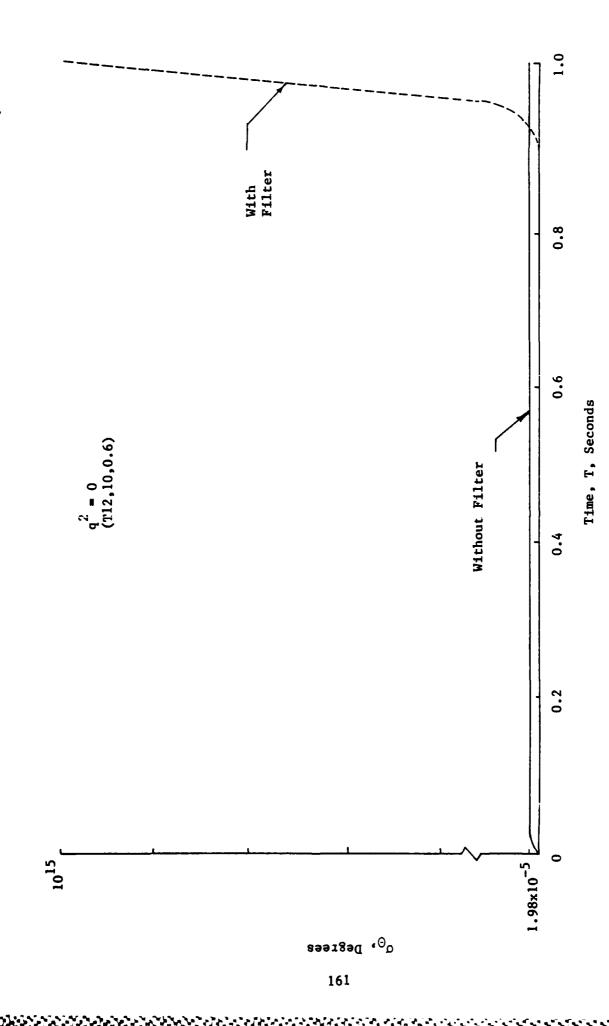
$$\mathbf{x}_{22} = \begin{bmatrix} 1 & 0 \\ & & \\ 0 & 1 \end{bmatrix} \tag{6-4}$$

The weighting matrices specified above are given in Reference 27.

They are arrived at using a methodology called 'implicit model following".

As mentioned before, the software used to design PI regulators also includes a method for designing a Command Generator Tracker to specify feedforward gains that cause the output of the controlled system to track the output of a command model in which the desired characteristics of the response have been built in (damping ratio, overshoot, settling time, etc.). Implicit model following can be used to affect the feedback gains of the PI controller in a way that makes the controlled system more robust. A more detailed explanation of implicit model following is given in References 27 and 29.

Figure (6-34) shows the time-response of the full-state feedback system with an initial condition of one degree on Θ evaluated against a deterministic truth model of the same dimension. It is seen that the response has very nice, well-damped second-order characteristics. Figure (6-35) demonstrates the standard deviations for this controller in a stochastic environment are very similar with and without a filter in the loop. The design model is defined in Section 5.4. In Figure (6-36),



Standard Deviation of Θ Evaluated Against Third-Order Actuator Dynamics

Figure 6-36:

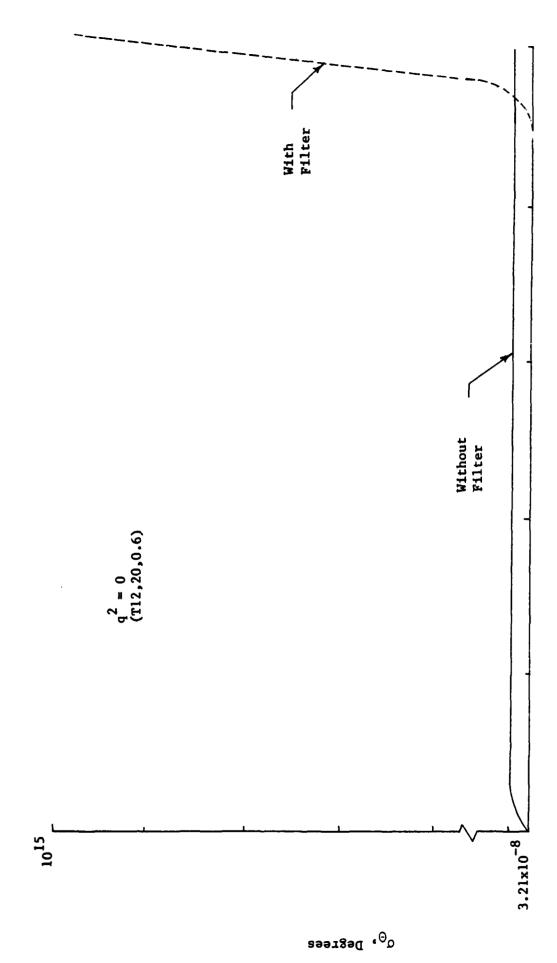


Figure 6-37: Standard Deviation of Θ At an Off-Design Flight Condition

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the results of the performance analysis are shown, where the eight-state controller was evaluated against a truth model with higher order actuator dynamics in the truth model. It is seen that without full-state feedback, stability was lost. The results are the same at an off-design condition (T12,20,0.6) as shown in Figure (6-37). Thus, the figures demonstrate that when actuator states are ignored in the design model, a full-state feedback controller exhibits good stability robustness properties. However, once a filter is inserted into the loop, these properties are lost.

Attempts were made to recover the stability of the controlled system by applying the Doyle and Stein technique. It was found that any non-zero value of q^2 only made the standard deviations diverge more rapidly. This was true for both flight conditions.

Recall that the Doyle and Stein technique was applied to sampled-data LQG regulators by modifying the \mathbf{Q}_{ij} matrix as follows:

$$Q_{d}(q) = Q_{do} + q^{2}BVB^{T}\Delta t$$
 (6-6)

using the B matrix of the continuous-time system equation.

The technique was applied to sampled-data PI controllers with the equation

$$Q_{d}(q) = Q_{do} + q^{2}B_{d}VB_{d}^{T}/\Delta t \qquad (6-7)$$

using the Bd matrix of the equivalent discrete-time system equation.

The Doyle and Stein technique was derived by equating the returndifference mappings for a full-state feedback system and a filter-based system. The derivation was based on the controllers being a full-state feedback regulator and an LQG regulator. It was expected, since the Kalman filter is the same for LQG regulators and PI controllers, that at least some robustness enhancement could be obtained by directly applying the technique to a PI controller. However, this was not found to be true.

6.4 Summary

This chapter has presented the results of applying two techniques to improve the robustness properties of a controlled system. The two methods examined are the techniques of inputting stationary white or time-correlated Gaussian noise into a system model during the process of tuning the Kalman filter.

Two separate issues of robustness were examined. The first was the idea of robustifying a controller so that instabilities do not occur when states are ignored in the controller and Kalman filter design model. For this thesis, the problem considered was an aircraft flight control problem, and the effect of ignoring states that described the actuator dynamics was examined. In this particular instance, the design model misrepresentation was confined to a particular portion of the frequency spectrum; this specifically motivated investigation of adding time-correlated rather than white noise for robustification.

The second robustness issue was the idea of robustifying a controller against changes in the real-world parameters upon which the controller design was based. Here the designed model misrepresentation was not confined to only a particular band of frequencies.

The primary result of this chapter is that the stability robustness of the controlled system can be substantially enhanced by applying both

robustification techniques. However, for the problem considered, the Doyle and Stein technique of inputting white noise into the system model is the most appropriate way to achieve the robustness enhancement.

Conclusions about the results presented in this chapter are made in the following chapter. In addition, some recommendations for further research are made.

VII. Conclusions and Recommendations

The robustification of LQG regulators by inputting white noise or time-correlated noise generated by a first-order shaping filter into the system model did work well for all three applications of the controllers examined (continuous, discretized, sampled-data). In addition, time-correlated noise generated by a second-order shaping filter improved the controller's robust-ness properties to a lesser degree for the continuous-time and sampled-data case. For the discretized case, this method produced instabilities in the response of the system and could not be used.

It was noted that in Chapter VI that few performance benefits were gained by using time-correlated noise as opposed to white noise for the problem considered in this thesis. It is felt that the range of frequencies where the design model differed from the chosen representation of the real-world was not sufficiently narrow in this case to result in performance benefits. Greater performance benefits may be realized by examining the application of colored noise addition to problems such as gust-load alleviation, flutter suppression, or aeroelastic effects such as including first-and higher-order bending modes in the truth model representation of the real world.

It is felt that the robustification techniques for LQG regulators were examined in great detail in this thesis. However, the extension to PI controllers was only touched upon, and the Doyle and Stein technique was applied unsuccessfully. To examine this more thoroughly, it is suggested that the Doyle and Stein technique be applied more directly to PI controllers. That is, the conditions analogous to those of Doyle and Stein that would make the return-difference mapping asymptotically equal

for a full-state feedback controller and a filter-based PI controller should be derived.

The technique of injecting time-correlated noise into the system model for a PI controller was not examined in this thesis. The existing software was not originally designed to allow augmenting of states with the design model. Therefore, it would be difficult to augment shaping filter states to allow for colored input noise. The modifications shown in Appendix C were made so that a few cases of colored input noise could be examined quickly. If an extensive study were made, the awkwardness of these modifications would become apparent. To examine all of the robust-ification techniques discussed in this thesis would thus require additional software.

It has been mentioned that a drawback of adding colored-noise to a system model is that it adds states to the Kalman filter model. An alternative method, called residualization (Ref 28), reduces the order of the model back to that of the original system before the shaping filter states were added. It would be useful to examine this implementation and compare it to the performance of the implementation used in this thesis for a problem where colored input noise is appropriate.

Finally, as noted in Sections 6.2.3 and 6.2.4, the technique of adding white or colored noise to a continuous-time controller, then discretizing the controller only improved robustness characteristics for a finite range of q^2 or Q_u . Beyond that range, the closed-loop system was unstable. This phenomenon is not well understood, and further research would be warranted to determine why this occurs. While it is not expected that an extension of the Doyle and Stein method would have all

the same characteristics of the original technique, it would be useful to determine what occurs during the discretization process to drive closed-loop system poles outside the z-domain unit circle so abruptly.

The results of the previous chapter have thus demonstrated that the techniques considered can substantially improve the robustness properties of a controlled system. For the particular problem considered white noise added to the system model at the control entry points is the appropriate method for accomplishing the robustification

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APPENDIX A: Generic Controller Format

Al. Introduction

In Chapter II, the idea of a standard format for a linear controller was introduced. The format is particularly useful in that any LQG controller synthesized by LQG methods can be rearranged into the standard form. Subsequently, the performance analysis equations presented in Chapter II apply to any controller put in the "generic" form, not just LQG regulators.

This appendix defines explicitly the generic form controller equations for the types of controllers considered in this thesis. In the first section, the continuous-time LQ regulator is examined, that is, a full-state feedback regulator with a control law expressed as:

$$\underline{\underline{u}}^{*}(t) = G_{c}^{*} \underline{x}(t) \tag{A-1}$$

The full-state feedback generic structure is presented because it is desired to recover the robustness characteristics of the LQ controller with the addition of input noise as covered in Chapters II and IV.

Then, the continuous-time LQG regulator is presented, based on a control law that employs state estimates from a Kalman filter:

$$\underline{\mathbf{u}}^{*}(t) = -G_{c}^{*} \hat{\mathbf{x}}(t) \tag{A-2}$$

Next, the structure of a sampled-data, full-state feedback regulator is examined with a control law expressed as

$$\underline{\underline{u}}^{*}(t_{i}) = -G_{c}^{*} \underline{x}(t_{i}) \tag{A-3}$$

Two forms of a sampled-data LQG regulator are examined. The first is based on the optimal control law given by

$$\underline{u}^{*}(t_{i}) = -G_{c}^{*} \hat{\underline{x}}(t_{i}^{+})$$
 (A-4)

The second is based on the suboptimal control law

$$\underline{\mathbf{u}}^{*}(\mathbf{t}_{i}) = -\mathbf{G}_{c}^{*} \hat{\mathbf{x}}(\mathbf{t}_{i}^{-}) \tag{A-5}$$

In the last two sections, the format is presented for a sampled-data PI controller designed on the basis of LQG methodology. First, the full-state feedback case is considered, then a Kalman filter is used to provide state estimates.

A.2 Continuous-time Controller Generic Structure

The generic format desired for the controllers considered in this thesis is given by

$$\underline{\underline{u}}^{*}(t) = G_{cx} \underline{x}_{c}(t) + G_{cz} \underline{z}(t) + G_{cy} \underline{y}_{d}(t)$$
 (A-6)

$$\underline{\mathbf{x}}_{\mathbf{c}}(t) = \mathbf{F}_{\mathbf{c}} \underline{\mathbf{x}}_{\mathbf{c}}(t) + \mathbf{B}_{\mathbf{c}\mathbf{z}} \underline{\mathbf{z}}(t) + \mathbf{B}_{\mathbf{c}\mathbf{v}} \underline{\mathbf{y}}_{\mathbf{d}}(t)$$
 (A-7)

which takes the form of an algebraic relation for the optimal control, $\underline{u}(t)$ and a propagation equation for the controller states. The controller states, $\underline{x}_{c}(t)$, are defined for the particular type of controller considered, and $\underline{z}(t)$ and $\underline{y}_{d}(t)$ are measurements and desired values of controlled variables, respectively.

For the full-state feedback case, perfect measurements of the states are available, i.e.,

$$\underline{z}(t) = \underline{x}(t) \tag{A-8}$$

and $\underline{y}_d(t) = \underline{0}$. Thus, it is seen by comparing Equations (A-1) and (A-6) that

$$G_{CX} = 0 (A-9)$$

$$G_{cz} = -G_{c}^{*} \tag{A-10}$$

$$G_{CY} = 0 (A-11)$$

In this instance, there are no internal controller states, so Equation (A-7) is not maintained.

For an LQG regulator, $\underline{y}_d(t)$ is again zero, therefore G_{cy} and B_{cy} can be set to zero. The controller states are defined to be the conditional mean estimates from a Kalman filter, $\underline{\hat{x}}(t)$. By the certainty equivalence principle, $\underline{x}(t)$ in Equation (A-2) can be replaced by $\underline{\hat{x}}(t)$ which are now the controller states, $\underline{x}_c(t)$:

$$\underline{u}^{*}(t) = -G_{c}^{*} \underline{x}_{c}(t)$$
 (A-12)

Comparing Equations (A-6) and (A-12), it is seen that

$$G_{cz} = 0 (A-13)$$

$$G_{CZ} = -G_{C}^{*} \tag{A-14}$$

Recall that the continuous-time Kalman filter equation yields an estimate of the states, $\underline{x}(t)$, where $\underline{x}(t)$ is now defined as the controller states, $\underline{x}_c(t)$. This is given by

$$\underline{\dot{\mathbf{x}}}_{\mathbf{c}}(t) = \mathbf{F} \, \underline{\mathbf{x}}_{\mathbf{c}}(t) + \mathbf{B}\underline{\mathbf{u}}^{*}(t) + \mathbf{K} \left[\underline{\mathbf{z}}(t) - \mathbf{H} \, \underline{\mathbf{x}}_{\mathbf{c}}(t)\right] \tag{A-15}$$

Substituting Equation (A-12) into the above and rearranging yields

$$\frac{\mathbf{x}}{\mathbf{c}}(t) = \left[\mathbf{F} - \mathbf{BG}_{\mathbf{c}}^* - \mathbf{KH} \right] \underline{\mathbf{x}}_{\mathbf{c}}(t) + \mathbf{K} \underline{\mathbf{z}}(t)$$
 (A-16)

Comparing Equations (A-7) and (A-16), it is seen that

$$F_{c} = \left[F - BG_{c}^{*} - KH\right] \tag{A-17}$$

$$B_{CZ} = K (A-18)$$

A.3 Optimal Sampled-Data Generic Controller Structure

The generic structure of Equations (A-4) and (A-5) is given in sampled-data form by

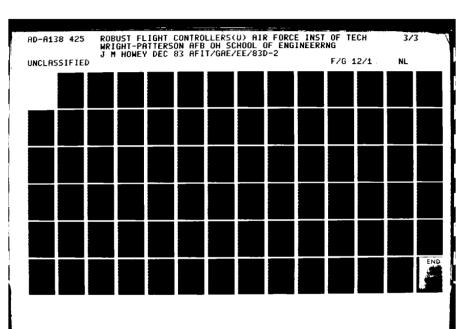
$$\underline{u}^{*}(t_{i}) = G_{cx} \underline{x}_{c}(t_{i}) + G_{cz} \underline{z}(t_{i}) + G_{cy} \underline{y}_{d}(t_{i})$$
 (A-19)

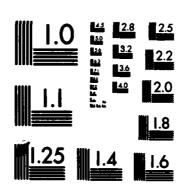
$$\underline{\mathbf{x}}_{\mathbf{c}}(t_{i+1}) = \phi_{\mathbf{c}} \underline{\mathbf{x}}_{\mathbf{c}}(t_{i}) + G_{\mathbf{c}z} \underline{\mathbf{z}}(t_{i}) + G_{\mathbf{c}y} \underline{\mathbf{y}}_{\mathbf{d}}(t_{i})$$
(A-20)

It is easily seen that for a sampled-data full-state feedback regulator, the generic form is identical to Equations (A-9) through (A-11).

For the optimal LQG regulator, the actual state values are replaced by estimates just after measurements are taken at the sample times. Again, $\underline{y}_d(t)$ will be zero for a regulator, therefore G_{cy} and B_{cy} can be set to zero. Define the controller states to be $\underline{\hat{x}}(t_i)$, the state estimates just prior to a measurement update. The Kalman filter propagation and update relations for the estimates of the states are given by

$$\underline{x}(t_{i+1}) = \phi \underline{x}(t_i^+) + B_d \underline{u}^*(t_i)$$
 (A-21)





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$$\underline{\hat{\mathbf{x}}}(\mathbf{t_i}^+) = \left[\mathbf{T} - \mathbf{KH}\right] \underline{\hat{\mathbf{x}}}(\mathbf{t_i}^-) + \mathbf{K}\underline{\mathbf{z}}(\mathbf{t_i}) \tag{A-22}$$

Replace $\hat{\mathbf{x}}(t_i)$ by $\mathbf{x}_c(t_i)$ and substitute (A-22) into (A-4) to yield

$$\underline{\underline{U}}^{*}(t_{i}) = -G_{c}^{*} \left[I - KH \right] \underline{\underline{x}}_{c}(t_{i}) - G_{c}^{*} \underline{Kz}(t_{i})$$
 (A-23)

Comparing (A-19) and (A-23), it is seen that

$$G_{cx} = -G_{c}^{*} \left[I - KH \right] \tag{A-24}$$

$$G_{cz} = -G_c^* K \qquad (A-25)$$

Now substitute Equations (A-4) and (A-22) into (A-21), replacing $\hat{\underline{x}}(t_i^-)$ with $\underline{x}_c(t_i^-)$:

$$\underline{\mathbf{x}}_{\mathbf{c}}(\mathbf{t}_{\mathbf{i}}+1) = \begin{bmatrix} \phi - \mathbf{B}_{\mathbf{d}}\mathbf{G}_{\mathbf{c}}^{*} \end{bmatrix} \begin{bmatrix} \mathbf{I} - \mathbf{K}\mathbf{H} \end{bmatrix} \underline{\mathbf{X}}_{\mathbf{c}}(\mathbf{t}_{\mathbf{i}})$$

$$+ \begin{bmatrix} \phi - \mathbf{B}_{\mathbf{d}}\mathbf{G}_{\mathbf{c}}^{*} \end{bmatrix} \mathbf{K} \underline{\mathbf{z}}(\mathbf{t}_{\mathbf{i}}) \qquad (A-26)$$

Comparing (A-20) and (A-26), it is seen that

$$\phi_{c} = \left[\phi - B_{d}G_{c}^{*}\right] \left[I - KH\right] \tag{A-27}$$

$$B_{cz} = \left[\phi - B_d G_c^{\dagger} \right] K \tag{A-28}$$

A.4 Sub-optimal Sampled-Data Generic Controller Structure

For the suboptimal control law, where the state values are replaced by estimates just prior to the sample times, the controller states are defined to be $\underline{\mathfrak{L}}(t_i)$. The output, $\underline{\mathfrak{L}}_d(t_i)$, is zero, thus G_{cy} and G_{cy} can be set to zero. By direct comparison of Equations (A-5) and (A-29), it is seen that

$$G_{CX} = -G_{C}^{*} \tag{A-29}$$

$$G_{CZ} = 0 (A-30)$$

Now substitute Equation (A-5) and (A-22) into (A-21), replacing $\hat{\underline{x}}(t_i)$ by $\underline{x}_c(t_i)$, to yield

$$\underline{\mathbf{x}}_{\mathbf{c}}(\mathbf{t}_{i+1}) = \{ \phi \left[\mathbf{I} - \mathbf{K} \mathbf{H} \right] - \mathbf{B}_{\mathbf{d}} \mathbf{G}_{\mathbf{c}}^{*} \} \ \underline{\mathbf{x}}_{\mathbf{c}}(\mathbf{t}_{i})$$

$$+ \left[\phi \mathbf{K} \right] \ \underline{\mathbf{z}}(\mathbf{t}_{i})$$
(A-31)

Thus, by comparing Equations (A-20) and (A-31), it is seen that

$$\phi_{c} = \{\phi \left[I - KH \right] - B_{d}G_{c}^{*} \} \tag{A-32}$$

$$B_{cz} = \left[\phi K \right] \tag{A-33}$$

A.5 Sampled-Data PI Confioller Generic Structure

An equivalent form for the PI control law derived in Chapter III which achieves Type-1 control is given by (Ref 1;23).

$$u^*(t_i) = -K_x \underline{x}(t_i) + K_z \underline{\xi}(t_i) + K_z \underline{y}_d(t_i)$$
 (A-34)

where $\xi(t_i)$ are termed the pseudo-integral states and are expressed as

$$\underline{\xi}(t_{i+1}) = \underline{\xi}(t_i) + \left[\underline{y}_d(t_i) - \underline{y}(t_i)\right]$$
 (A-35)

For the PI controller, a non-zero output, $\underline{y}_{d}(t_{i})$, will be allowed, where $\underline{y}(t_{i})$, the actual output of the system, is given by

$$\underline{y}(t_i) = \underline{C}\underline{x}(t_i) + \underline{D}_y \underline{u}^*(t_i)$$
 (A-36)

For the full-state feedback case, the controller states are defined to be $\underline{\xi}(t_i)$. Substituting (A-35) and (A-36) into (A-34) and recalling ahat $\underline{x}(t_i) = \underline{z}(t_i)$ yields

$$\underline{\underline{u}}^{*}(t_{i}) = K_{z}\underline{x}_{c}(t_{i}) - K_{z}\underline{z}(t_{i}) + K_{z}\underline{y}_{d}(t_{i})$$
 (A-37)

Comparing this equation (A-19), it is seen that

$$G_{Cx} = K_{Z} \tag{A-38}$$

$$G_{CZ} = -K_{x} \tag{A-39}$$

$$G_{CY} = K_{Z} \tag{A-40}$$

Then, by substituting Equations (A-34) and (A-36) into (A-35) with $\underline{\mathbf{x}}_{\mathbf{c}}(\mathbf{t}_{\mathbf{i}}) = \underline{\xi}(\mathbf{t}_{\mathbf{i}})$:

$$\underline{\mathbf{x}}_{\mathbf{c}}(\mathbf{t}_{i+1}) = \left[\mathbf{I} - \mathbf{D}_{\mathbf{y}} \mathbf{K}_{\mathbf{z}}\right] \underline{\mathbf{x}}_{\mathbf{c}}(\mathbf{t}_{i}) - \left[\mathbf{C} - \mathbf{D}_{\mathbf{y}} \mathbf{K}_{\mathbf{x}}\right] \underline{\mathbf{z}}(\mathbf{t}_{i})$$

$$+ \left[\mathbf{I} - \mathbf{D}_{\mathbf{y}} \mathbf{K}_{\mathbf{z}}\right] \underline{\mathbf{y}}_{\mathbf{d}}(\mathbf{t}_{i}) \tag{A-41}$$

and comparing this to Equation (A-20) yields

$$\phi_{c} = \left[I - D_{y} K_{z} \right] \tag{A-42}$$

$$B_{cz} = \left[C - D_{y} K_{x} \right] \tag{A-43}$$

$$B_{cy} = \left[I - D_{y} K_{z} \right] \tag{A-44}$$

With a Kalman filter in the loop, $\underline{x}(t_i)$ is replaced by $\underline{\hat{x}}(t_i^+)$ in Equations (A-34) and (A-36).

The controller states, $\underline{\mathbf{x}}_{\mathbf{c}}(\mathbf{t}_{\mathbf{i}})$, for PI controller are defined to be an augmented vector containing the state estimates just prior to a measurement update and the pseudo-integral states:

$$\underline{\mathbf{x}}_{\mathbf{c}}(\mathbf{t}_{\mathbf{i}}) = \begin{bmatrix} \hat{\mathbf{x}}(\mathbf{t}_{\mathbf{i}}^{-}) \\ \\ \underline{\boldsymbol{\xi}}(\mathbf{t}_{\mathbf{i}}) \end{bmatrix}$$
 (A-45)

To generate the generic controller structure, first substitute the Kalman filter update relation (A-22) into Equations (A-21) and (A-34). This yields

$$\underline{\hat{\mathbf{x}}}(\mathbf{t_{i+1}}^-) = \phi\{\left[\mathbf{I} - \mathbf{KH}\right] \underline{\mathbf{x}}(\mathbf{t_i}^-) + \mathbf{K} \underline{\mathbf{z}}(\mathbf{t_i})\} + \mathbf{B_d}\mathbf{u}^*(\mathbf{t_i}) \tag{A-46}$$

$$\underline{\underline{u}}^{*}(t_{\underline{i}}) = -K_{\underline{x}} \{ [I-KH] \underline{\hat{x}}(t_{\underline{i}}) + K_{\underline{z}}(t_{\underline{i}}) \} + K_{\underline{z}} \underline{\xi}(t_{\underline{i}})$$
 (A-47)

Substitute (A-47) into (A-46) to yield

$$\hat{\mathbf{x}}(\mathbf{t_{i+1}}) = \begin{bmatrix} \phi - \mathbf{B_d} \mathbf{K_x} \end{bmatrix} \begin{bmatrix} \mathbf{I} - \mathbf{KH} \end{bmatrix} \hat{\mathbf{x}}(\mathbf{t_i})$$

$$+ \mathbf{B_d} \mathbf{K_z} \underline{\xi}(\mathbf{t_i}) + \begin{bmatrix} \phi - \mathbf{B_d} \mathbf{K_x} \end{bmatrix} \mathbf{K} \underline{\mathbf{z}}(\mathbf{t_i})$$

$$+ \mathbf{B_d} \mathbf{K_z} \underline{y_d}(\mathbf{t_i})$$

$$(A-48)$$

Next, substitute Equations (A-22) and (A-36) into (A-35) to yield

$$\underline{\xi}(t_{i+1}) = -\left[C - D_{y}K_{x}\right]\left[I - KH\right] \quad \underline{\hat{x}}(t_{i}^{-})$$

$$+ \left[I - D_{y}K_{z}\right] \underline{\xi}(t_{i}) - \left[C - D_{y}K_{x}\right] K \underline{z}(t_{i})$$

$$+ \left[I - D_{y}K_{z}\right] \underline{y}_{d}(t_{i})$$
(A-49)

Equations (A-47) and (A-48) in terms of the controller states, $\underline{x}_{c}(t_{i})$, are given by

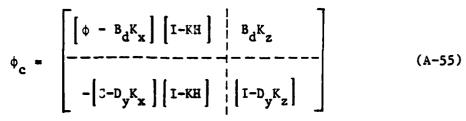
$$\underline{\mathbf{u}}^{*}(\mathbf{t}_{i}) = \begin{bmatrix} -K_{\mathbf{x}} \{\mathbf{I} - \mathbf{K}\mathbf{H}\} & K_{\mathbf{z}} \end{bmatrix} \underline{\mathbf{x}}_{\mathbf{c}}(\mathbf{t}_{i}) \\
- \begin{bmatrix} K_{\mathbf{x}} \mathbf{K} \end{bmatrix} \underline{\mathbf{z}}(\mathbf{t}_{i}) + K_{\mathbf{z}} \underline{\mathbf{y}}_{\mathbf{d}}(\mathbf{t}_{i}) \\
\underline{\mathbf{v}}_{\mathbf{x}}(\mathbf{t}_{i+1}) = \begin{bmatrix} \frac{1}{2} - B_{\mathbf{d}} K_{\mathbf{x}} & \mathbf{I} \mathbf{I} - \mathbf{K}\mathbf{H} \end{bmatrix} \underline{\mathbf{b}}_{\mathbf{d}} K_{\mathbf{z}} \\
- \begin{bmatrix} \mathbf{0} - B_{\mathbf{d}} K_{\mathbf{x}} & \mathbf{I} \mathbf{I} - \mathbf{K}\mathbf{H} \end{bmatrix} \underline{\mathbf{b}}_{\mathbf{d}} K_{\mathbf{z}} \\
- \begin{bmatrix} \mathbf{0} - D_{\mathbf{y}} K_{\mathbf{x}} & \mathbf{I} \mathbf{I} - \mathbf{K}\mathbf{H} \end{bmatrix} \underline{\mathbf{b}}_{\mathbf{d}} K_{\mathbf{z}} \end{bmatrix} \underline{\mathbf{x}}_{\mathbf{c}}(\mathbf{t}_{i}) \\
+ \begin{bmatrix} \mathbf{0} - B_{\mathbf{d}} K_{\mathbf{x}} & \mathbf{K} \\
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Comparing Equations (A-19) and (A-50), and (A-20) and (A-51), it is seen that

$$G_{CX} = \begin{bmatrix} -K_{X} \{I - KH\} & K_{Z} \end{bmatrix}$$
 (A-52)

$$G_{CZ} = \begin{bmatrix} -K_{X}K \end{bmatrix}$$
 (A-53)

$$G_{cy} = \left[K_z \right] \tag{A-54}$$



$$B_{CZ} = \begin{bmatrix} \phi - B_{d}K_{x} & K \\ - C - D_{y}K_{x} & K \end{bmatrix} K$$
(A-56)

$$B_{cy} = \begin{bmatrix} B_{d}K_{z} \\ I-D_{y}K_{z} \end{bmatrix}$$
 (A-57)

APPENDIX B: Modifications and Additions to LQGRP

A.1 Introduction

This appendix is intended to be used as a supplement to Reference 21, Appendix D, which is the user's guide to a program entitled Linear Quadratic Gaussian Regulator Performance (LQGRP). The program provides the capability of designing and evaluating the performance of continuous-time and sampled-data LQG regulators. In addition, it contains options of enhancing the robustness of both types of regulators via the Doyle and Stein technique.

Three types of changes are made to the original program which are documented herein. The first type involves corrections to errors in the original source code. The second type entails modifications that result in more convenient input and output and a more efficient program. The third type of change generates additions so that the technique of injecting time-correlated noise into the design model while tuning the Kalman filter for robustness purposes can be applied to LQG regulators.

Corrections to the original source code (contained on subsequent pages) are bracketed and marked with a "C". Modifications are bracketed and marked with an "M", and additions are bracketed and marked with an "A".

A.2 Corrections to LQGRP

The first correction appears on line 6770. The variable name IRF2 replaces IRFM in the original code. IRFM is the dimension of the design model F matrix, but what should be passed to the subroutine is the

dimension of F minus the number of deterministic states, which is IRF2.

Next, on line 15330, ICBM (the column dimension of the model B matrix) replaces IRFM in the second argument of the subroutine MAT3.

A third correction is made in lines 17120 and 17130. The original source code contains extra arguments in the call to subroutine DDTCON. They do not interfere with execution of the program, but they are not needed and have been deleted in this version.

In line 19430, BM (IDS, IDS) (starting address of the design model B matrix after deterministic states are deleted) replaces BM in the original program. It is intended to pass to the subroutine only the lower portion of the design model B matrix, BM, after the deterministic states (listed first) are deleted. The original program passes the entire B matrix. Making this correction changes the starting address of the array in subroutine DAS2 so that only the desired portion of BM is used.

Lines 19500 and 19510 are inserted into the program to correct an error in line 19520. Originally, RMD appears in place of WM4. RMD is the discrete-time measurement noise covariance matrix. However, the subroutine KFLTR requires a vector containing the diagonal elements of RMD. Thus, the diagonal elements of RMD are stored in the first column of WM4 in lines 15900 and 19510, and WM4 is passed to the subroutine instead of RMD. WM4 is a work-space array not originally being used at that point in the program.

The last correction is made to line 20840. Originally, the line read call MAT3, which calculates the transpose of the desired result. This is corrected by replacing it with CALL MAT3A.

B.3 Modifications to LQGRP

The matrices and vectors defined in lines 370 through 510 were originally of dimension 5 or 10. All matrices and vectors of dimension 5 are changed to 13, and those of dimension 10 are changed to 26. This change is reflected also in lines 680 through 700. This allows the number of states in the truth or design model to be a maximum number of 13.

The original version of LQGRP had 6 input/output options for entering and printing out truth and design model matrices. The version listed herein has 7. The first 2 options are unchanged. Option 3 now allows the user to change as many elements of a specified matrix as desired by listing the row, column and value of the element being changed. When the user enters a 0, the program exits this option. Options 4 and 5 are also unchanged. Option 6 initially zeros the entire array and then allows the user to enter as many elements as desired by entering the row, column and value of each element. Entering a 0 will exit this option. Option 7 takes the place of option 6 in the previous version. Thus, on a first run through the program, option 6 initializes the array to zero and then only non-zero elements need to be entered. On subsequent runs, changes can be made to any vector or matrix by using option 3.

The changes discussed above require that modifications be made to subroutines MVEC10 and MMAT10, which control the programs input and output. These are listed in lines 12370 to 12380, 12460 to 12530, 12590, 13060, 13130 to 13230 and 13280.

The program stores results of the performance evaluation routines to four data files for plotting. These data files contain the time histories of the following vectors and matrices, defined in Section 2.3:

 $\underline{x}_a(t)$, $P_{x_ax_a}(t)$, $\underline{u}(t)$ and $P_{uu}(t)$. The modifications listed in lines 10650 and 10690 calculate and store the square roots of the diagonal elements (standard deviations) of $P_{x_ax_a}(t)$ and $P_{uu}(t)$ rather than storing the diagonal elements (variances). This change also occurs in lines 11570 and 11600. Notice in lines 11560 through 11660 that only the first 7 states of $\underline{x}_a(t)$ and the upper left (7x7) partition of $P_{x_ax_a}(t)$ is stored for plotting. This is an option of the user. Any portion of the vector and matrix may be stored by changing the 7 in lines 10630, 10770, 11550, 11610 and 11650 to the desired value or to IREM (the dimension of the design model F matrix) if the entire vector and matrix are desired.

The four vectors and matrices listed above are printed to the terminal during execution of the program. Currently, only the first 3 states of $\underline{\mathbf{x}}_{\mathbf{a}}(t)$ and the upper-left (3x3) partition of $P_{\mathbf{x}_{\mathbf{a}}\mathbf{x}_{\mathbf{a}}}(t)$ are printed. Any portion may be printed by changing the 3 in lines 10530 and 10570 to a desired value or to IRFM if the entire vector and matrix are desired. Note that all of $\underline{\mathbf{u}}(t)$ and $P_{\mathbf{u}\mathbf{u}}(t)$ are stored and listed at the terminal.

The preceding modifications were made to LQGRP to make the program more convenient to use in conjunction with the problem considered in this thesis. None are necessary for execution of the program, as contrasted to the corrections of Section B.2.

B.4 Additions to LQGRP

This section describes the additions necessary to the program so that the technique of injecting colored noise into the design model

during filter tuning may be applied. The changes are primarily lines of code inserted into the program. However, a few lines of the original source code are altered slightly, and these will be mentioned.

For a continuous-time system, the input prompt for colored noise is given in line 13870. If colored noise is not desired, the program skips to line 13920 and continues execution. Note that line 13920 is from the original program with the label 2900 inserted in front. If colored noise is desired, the dimension of the model F matrix, IRFM, is stored in a dummy variable, IHOLD, for later use. Then, in line 13910, subroutine CNOISE is called, which controls the augmentation of shaping filter states with the original design model.

Lines 13950 through 14020 augment zeros to the deterministic controller gain matrix, G_c^* , if the colored-noise options are executed. Lines 13950 and 13960 are from the original source code, altered by replacing IRFM with IHOLD. Recall, as discussed in Section 4.3, that G_c^* is calculated using the design model of the unaugmented system, and the dimensionality difference is taken care of by augmenting G_c^* with the appropriate number of columns of zeros.

For a sampled-data system, the colored noise input prompt should appear between lines 16710 and 16720. It is missing from this listing, but should read

WRITE (KOUT,*) 'COLORED INPUT NOISE (Y OR N)>'

Lines 16720 through 16760 then control whether the colored-noise routines are executed. Line 16760 is from the original program with a label 25 inserted.

On line 17090, IRFM is again replaced by IHOLD. Lines 17120 and 17130 are also from the original program with an additional argument, IHOLD, in the parameter list. Then, lines 17140 through 17190 check to see if the colored-noise routines were executed. If so, $G_{\rm c}^{\star}$ is augmented with the appropriate number of columns of zeros.

In both the continuous-time and sampled-data case, it is desired to use the original design model for controller gain calculations, as mentioned above, in subroutines CDTCON and DDTCON, which calculate deterministic controller gains for the continuous-time and sampled-data case, respectively. These subroutines are essentially unchanged except that IHOLD is substituted for IRFM where indicated in CDTCON (lines 5110 through 5890). In DDTCON, IHOLD is an additional parameter in the argument list and replaces IRFM where indicated (lines 20480 through 21030).

Lines 24770 through 24930 contain subroutine CNOISE which controls what type of shaping filters are augmented to the design model. An input prompt asks if a first- or second-order shaping filter is desired. Subroutine FORDER is called (lines 24940 through 25510) if a first-order shaping filter is desired. If a second-order filter is desired, then subroutine SORDER is called (lines 25520 through 26160). Both subroutines prompt for the shaping filter design parameters described in Chapter IV. Then, the design model is augmented with the shaping filter states and appropriate partitions of the augmented matrices are zeroed. Finally, the dimensions of the design model F and G matrices are altered to reflect the higher dimension after augmenting.

The matrices described above thus modify LQGRP so that shaping filter states can be augmented with the original system design model. It should

be noted that the program will still ask if modification via the Doyle and Stein technique is desired if the colored-noise options are chosen. Either the colored-noise options or the Doyle and Stein options may be chosen, but not both.

Additionally, it is desirable to have the original design and truth models stored on Tape 8 (Ref 21) so that they can be read into the program via input option 18. When the colored-noise options are chosen, the design model is altered. Thus, to make subsequent runs through LQGRP, the original design and truth models must be read back in.

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c	1 1 1 1 1 1 1	R MANE COCCOCC	((((((((((GCD SUU SUU SCTP SCE HCCD MCD MCD MCD MCD MCD MCD MCD MCD MCD	(1) (2) (2) (3) (4) (4) (4) (4) (4) (4) (4) (4) (4) (4	13 (1 · · · · · · · · · · · · · · · · · ·	13) 26) 3) 4) 4) 1) 1) 1) 1) 1) 1) 1) 1) 1) 1) 1) 1) 1)) +) + C Y G M 2 1 U 4 5 6	GCTXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXX	ZUMMA Y TEMPINAGE	134 T () 1 () 1 () 1 () 1 () 1 () 1 () 1 () 1	13) (13) (13) (13) (14) (15) (17) (17) (17) (17)) + P + P Z 9 L + K3 +	GA XTI MX UH (1) (1) TI CO	125 100 AP () 125 125 AP () 126 127 AP () 127 AP ()	(12) (13) (13) (13)	6) 3) 131 1 - G(, PY , PU , P , P , P , P	A(2 OUT UMI AX(13. (13	6.1 (1: R(: 13: 13:	25) 3), 13), 6), 6), 7	PP	XV # (16 UM # 13 13 3 (2	1(2 100 1x (16. 13 16)	6 · 2) · 13) 26)) · • HV	(6) •	26)	· · ·			145676900000000000000000000000000000000000	0.0000000000000000000000000000000000000	- 8	
C	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	R MANE COCCOCC	((((((((((GCD SUU SUU SCTP SCE HCCD MCD MCD MCD MCD MCD MCD MCD MCD MCD	(1) (2) (2) (3) (4) (4) (4) (4) (4) (4) (4) (4) (4) (4	13 (1 · · · · · · · · · · · · · · · · · ·	13) 26) 3) 4) 4) 1) 1) 1) 1) 1) 1) 1) 1) 1) 1) 1) 1) 1)) +) + C Y G M 2 1 U 4 5 6	GCTXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXX	ZUMMA Y TEMPINAGE	134 T () 1 () 1 () 1 () 1 () 1 () 1 () 1 () 1	13) 113) 113) 100 100 100 100 100 100 100 100 100 10) + P + P Z 9 L + K3 +	GA XTI MX UH (1) (1) TI CO	125 100 AP () 125 125 AP () 126 127 AP () 127 AP ()	(12) (13) (13) (13)	6) 3) 131 1 - G(, PY , PU , P , P , P , P	A(2 OUT UMI AX(13. (13	6.1 (1: R(: 13: 13:	25) 3), 13), 6), 6), 7	PP	XV # (16 UM # 13 13 3 (2	1(2 100 1x (16. 13 16)	6 · 2) · 13) 26)) · • HV	(6) •	26)	· · ·			145674901234567890 14474901234567890		- 8	
C	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	R MANE COCCOCC	((((((((((GCD SUU SUU SCTP SCE HCCD MCD MCD MCD MCD MCD MCD MCD MCD MCD	(1) (2) (2) (3) (4) (4) (4) (4) (4) (4) (4) (4) (4) (4	13 (1 · · · · · · · · · · · · · · · · · ·	13) 26) 3) 4) 4) 1) 1) 1) 1) 1) 1) 1) 1) 1) 1) 1) 1) 1)) +) + C Y G M 2 1 U 4 5 6	GCTXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXX	ZUMMA Y TEMPINAGE	134 T () 1 () 1 () 1 () 1 () 1 () 1 () 1 () 1	13) 113) 113) 100 100 100 100 100 100 100 100 100 10) + P + P Z 9 L + K3 +	GA XTI MX UH (1) (1) TI CO	125 100 A N 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	(12) (13) (13) (13)	6) 3) 131 1 - G(, PY , PU , P , P , P , P	A(2 OUT UMI AX(13. (13	6.1 (1: R(: 13: 13:	25) 3), 13), 6), 6), 7	PP	XV # (16 UM # 13 13 3 (2	1(2 100 1x (16. 13 16)	6 · 2) · 13) 26)) · • HV	(6) •	26)	· · ·			-4567-490-1233-5567-890-1 -44-7-490-1523-5567-890-1 		- 8	
CCC	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	R MANE COCCOCC	((((((((((GCD SUU SUU SCTP SCE HCCD MCD MCD MCD MCD MCD MCD MCD MCD MCD	(1) (2) (2) (3) (4) (4) (4) (4) (4) (4) (4) (4) (4) (4	13 (1 · · · · · · · · · · · · · · · · · ·	13) 26) 3) 4) 4) 1) 1) 1) 1) 1) 1) 1) 1) 1) 1) 1) 1) 1)) +) + C Y G M 2 1 U 4 5 6	GCTXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXX	ZUMMA Y TEMPINAGE	134 T () 1 () 1 () 1 () 1 () 1 () 1 () 1 () 1	13) 113) 113) 100 100 100 100 100 100 100 100 100 10) + P + P Z 9 L + K3 +	GA XTI MX UH (1) (1) TI CO	125 100 A N 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	(12) (13) (13) (13)	6) 3) 131 1 - G(, PY , PU , P , P , P , P	A(2 OUT UMI AX(13. (13	6.1 (1: R(: 13: 13:	25) 3), 13), 6), 6), 7	PP	XV # (16 UM # 13 13 3 (2	1(2 100 1x (16. 13 16)	6 · 2) · 13) 26)) · • HV	(6) •	26)	· · ·			-45676901234567890162 -4567690125557890162	537.0 367.0 56.0 57.7 57.7	- 8	
C C C	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	R MANE COCCOCC	((((((((((GCD SUU SUU SCTP SCE HCCD MCD MCD MCD MCD MCD MCD MCD MCD MCD	(1) (2) (2) (3) (4) (4) (4) (4) (4) (4) (4) (4) (4) (4	13 (1 · · · · · · · · · · · · · · · · · ·	13) 26) 3) 4) 4) 1) 1) 1) 1) 1) 1) 1) 1) 1) 1) 1) 1) 1)) +) + C Y G M 2 1 U 4 5 6	GCTXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXX	ZUMMA Y TEMPINAGE	134 T () 1 () 1 () 1 () 1 () 1 () 1 () 1 () 1	13) 113) 113) 100 100 100 100 100 100 100 100 100 10) + P + P Z 9 L + K3 +	GA XTI MX UH (1) (1) TI CO	125 100 A N 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	(12) (13) (13) (13)	6) 3) 131 1 - G(, PY , PU , P , P , P , P	A(2 OUT UMI AX(13. (13	6.1 (1: R(: 13: 13:	25) 3), 13), 6), 6), 7	PP	XV # (16 UM # 13 13 3 (2	1(2 100 1x (16. 13 16)	6 · 2) · 13) 26)) · • HV	(6) •	26)	· · ·			45676901234567890123 64476901234567890123 64476901234567890123		- 8	
CCCCC	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	RINE COCCCC	PATTAMINE MINE	GCDCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCC	(1) (2) (2) (2) (2) (2) (2) (2) (2) (2) (2	13 (1 · · · · · · · · · · · · · · · · · ·	13) 26) 3) 4) 4) 1) 1) 1) 1) 1) 1) 1) 1) 1) 1) 1) 1) 1)) +) + C Y G M 2 1 U 4 5 6	GCTXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXX	ZUMMA Y TEMPINAGE	134 T () 1 () 1 () 1 () 1 () 1 () 1 () 1 () 1	13) 113) 113) 100 100 100 100 100 100 100 100 100 10) + P + P Z 9 L + K3 +	GA XTI MX UH (1) (1) TI CO	125 100 A N 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	(12) (13) (13) (13)	6) 3) 131 1 - G(, PY , PU , P , P , P , P	A(2 OUT UMI AX(13. (13	6.1 (1: R(: 13: 13:	25) 3), 13), 6), 6), 7	PP	XV # (16 UM # 13 13 3 (2	1(2 100 1x (16. 13 16)	6 · 2) · 13) 26)) · • HV	(6) •	26)	· · ·			4567490123456789012366664 476975255557890123666666666666666666666666666666666666		- 8	
C C C C	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	RINE COCCCC	PATTAMINE MINE	GCD SUU SUU SCTP SCE HCCD MCD MCD MCD MCD MCD MCD MCD MCD MCD	(1) (2) (2) (2) (2) (2) (2) (2) (2) (2) (2	13 (1 · · · · · · · · · · · · · · · · · ·	13) 26) 3) 4) 4) 1) 1) 1) 1) 1) 1) 1) 1) 1) 1) 1) 1) 1)) +) + C Y G M 2 1 U 4 5 6	GCTXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXX	ZUMMA Y TEMPINAGE	134 T () 1 () 1 () 1 () 1 () 1 () 1 () 1 () 1	13) 113) 113) 100 100 100 100 100 100 100 100 100 10) + P + P Z 9 L + K3 +	GA XTI MX UH (1) (1) TI CO	125 100 A N 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	(12) (13) (13) (13)	6) 3) 131 1 - G(, PY , PU , P , P , P , P	A(2 OUT UMI AX(13. (13	6.1 (1: R(: 13: 13:	25) 3), 13), 6), 6), 7	PP	XV # (16 UM # 13 13 3 (2	1(2 100 1x (16. 13 16)	6 · 2) · 13) 26)) · • HV	(6) •	26)	· · ·			45676901234567890123 64476901234567890123 64476901234567890123		_ 8	
c c c c c	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	WINE COCCCCC	PATTIANI PAT	GCDCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCC	(1) (2) (2) (2) (3) (3) (4) (4) (4) (4) (4) (4) (4) (4) (4) (4	13 (1 · · · · · · · · · · · · · · · · · ·	13) 26) 3) 4) 4) 1) 1) 1) 1) 1) 1) 1) 1) 1) 1) 1) 1) 1)) +) + C Y G M 2 1 U 4 5 6	GCTXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXX	ZUMMA Y TEMPINAGE	134 T () 1 () 1 () 1 () 1 () 1 () 1 () 1 () 1	13) 113) 113) 100 100 100 100 100 100 100 100 100 10) + P + P Z 9 L + K3 +	GA XTI MX UH: (1: TI) CO:	125 100 A N 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	(12) (13) (13) (13)	6) 3) 131 1 - G(, PY , PU , P , P , P , P	A(2 OUT UMI AX(13. (13	6.1 (1: R(: 13: 13:	25) 3), 13), 6), 6), 7	PP	XV # (16 UM # 13 13 3 (2	1(2 100 1x (16. 13 16)	6 · 2) · 13) 26)) · • HV	(6) •	26)	· · ·			4567490123456789012366664 476975255557890123666666666666666666666666666666666666		_ 8	
C C C C C	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	WINE COCCCC	PATTION NO.	GCUUUTE FOR COMMON TO THE	(U) (1) (U) (U) (U) (U) (U) (U) (U) (U) (U) (U	LTCO(5) F3 NAATAAAR	13) 26) 3) 4) 4) 1) 1) 1) 1) 1) 1) 1) 1) 1) 1) 1) 1) 1)) +) + C Y G M 2 1 U 4 5 6	GCTXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXX	ZUMMA Y TEMPINAGE	13 (1) (1) (1) (1) (1) (1) (1) (1) (1) (1)	13) 113) 113) 100 100 100 100 100 100 100 100 100 10) + P + P Z 9 L + K3 +	GA XTI MX UH: (1: TI) CO:	125 100 A N 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	(12) (13) (13) (13)	6) 3) 131 1 - G(, PY , PU , P , P , P , P	A(2 OUT UMI AX(13. (13	6.1 (1: R(: 13: 13:	25) 3), 13), 6), 6), 7	PP	XV # (16 UM # 13 13 3 (2	1(2 100 1x (16. 13 16)	6 · 2) · 13) 26)) · • HV	(6) •	26)	· · ·					_ 8	
C C C C	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	WINE COCCOCC KKK	P)	GCUUUTE FEBRUARE TEGE	COLITICATION OF THE COLITI	LTCO(5) F3 NAATAAAR	13) 26) 3) 4) 4) 1) 1) 1) 1) 1) 1) 1) 1) 1) 1) 1) 1) 1)) +) + C Y G M 2 1 U 4 5 6	GCTXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXX	ZUMMA Y TEMPINAGE	13 (1) (1) (1) (1) (1) (1) (1) (1) (1) (1)	13) 113) 113) 100 100 100 100 100 100 100 100 100 10) + P + P Z 9 L + K3 +	GA XTI MX UH: (1: TI) CO:	125 100 A N 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	(12) (13) (13) (13)	6) 3) 131 1 - G(, PY , PU , P , P , P , P	A(2 OUT UMI AX(13. (13	6.1 (1: R(: 13: 13:	25) 3), 13), 6), 6), 7	PP	XV # (16 UM # 13 13 3 (2	1(2 100 1x (16. 13 16)	6 · 2) · 13) 26)) · • HV	(6) •	26)	· · ·					•	
C C C C	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	WINE COCCOCC KKKNE	PO TOUR STANDS OF THE STANDS O	GCUUUTE SELECTER MACE SELECTER	COLITICAL TO THE STATE OF THE S	LICOLO SESNAME MANAGEMENT TO THE PROPERTY OF T	13) 6) BHG INNONINA) +) +CMC M21U456 +	GCTXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXX	ZUMMA Y TEMPINAGE	13 (1) (1) (1) (1) (1) (1) (1) (1) (1) (1)	13) 113) 113) 100 100 100 100 100 100 100 100 100 10) + P + P Z 9 L + K3 +	GA XTI MX UH (1) (1) TI CO	125 100 A N 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	(12) (13) (13) (13)	6) 3) 131 1 - G(, PY , PU , P , P , P , P	A(2 OUT UMI AX(13. (13	6.1 (1: R(: 13: 13:	25) 3), 13), 6), 6), 7	PP	XV # (16 UM # 13 13 3 (2	1(2 100 1x (16. 13 16)	6 · 2) · 13) 26)) · • HV	(6) •	26)	· · ·			.4567890 <u>1</u> 23456789012345678		•	1
c c c c	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	WINE GOOGGOOGGOOGGOOGGOOGGOOGGOOGGOOGGOOGGO	PATTIAN NOUNT NOUN	GOUUTE LICENSONS IN THE STATE OF THE STATE O	(U(1) 4 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	LICAL LICAL AND	13) 6) BHG INNONINA) +) +CMC M21U456 +	GCTXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXX	ZUMMA Y TEMPINAGE	13 (1) (1) (1) (1) (1) (1) (1) (1) (1) (1)	13) 113) 113) 100 100 100 100 100 100 100 100 100 10) + P + P Z 9 L + K3 +	GA XTI MX UH (1) (1) TI CO	125 100 A N 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	(12) (13) (13) (13)	6) 3) 131 1 - G(, PY , PU , P , P , P , P	A(2 OUT UMI AX(13. (13	6.1 (1: R(: 13: 13:	25) 3), 13), 6), 6), 7	PP	XV # (16 UM # 13 13 3 (2	1(2 100 1x (16. 13 16)	6 · 2) · 13) 26)) · • HV	(6) •	26)	· · ·			45678901234567890123456789010	33700 36700 36700 3700 3700 3700 3700 37	•	
cccc	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	WINESCOOLS KKNNNN	PATTAMENT NUMBER	GOUUTE	(U(2) 4 1 4 1 4 1 4 1 4 1 4 1 4 1 4 1 4 1 4	3 (1 0 (1))	13) 3) 3) 4) 4) 11 11 11 11 11 11) +) +CMC M21U456 +	GCTXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXX	ZUMMA Y TEMPINAGE	13 (1) (1) (1) (1) (1) (1) (1) (1) (1) (1)	13) 113) 113) 100 100 100 100 100 100 100 100 100 10) + P + P Z 9 L + K3 +	GA XTI MX UH (1) (1) TI CO	125 100 AP () 125 125 AP () 126 127 AP () 127 AP ()	(12) (13) (13) (13)	6) 3) 131 1 - G(, PY , PU , P , P , P , P	A(2 OUT UMI AX(13. (13	6.1 (1: R(: 13: 13:	25) 3), 13), 6), 6), 7	PP	XV # (16 UM # 13 13 3 (2	1(2 100 1x (16. 13 16)	6 · 2) · 13) 26)) · • HV	(6) •	26)	· · ·					•	
c c c c c	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	WINESCOOLS KKNNNN	PATTAMENT NUMBER	GOUUTE	(U(2) 4 1 4 1 4 1 4 1 4 1 4 1 4 1 4 1 4 1 4	LICAL LICAL AND	13) 3) 3) 4) 4) 11 11 11 11 11 11) +) +CMC M21U456 +	GCTXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXX	ZUMMA Y TEMPINAGE	134 T () 1 () 1 () 1 () 1 () 1 () 1 () 1 () 1	13) 113) 113) 100 100 100 100 100 100 100 100 100 10) + P + P Z 9 L + K3 +	GA XTI MX UH (1) (1) TI CO	125 100 AP () 125 125 AP () 126 127 AP () 127 AP ()	(12) (13) (13) (13)	6) 3) 131 1 - G(, PY , PU , P , P , P , P	A(2 OUT UMI AX(13. (13	6.1 (1: R(: 13: 13:	25) 3), 13), 6), 6), 7	PP	XV # (16 UM # 13 13 3 (2	1(2 100 1x (16. 13 16)	6 · 2) · 13) 26)) · • HV	(6) •	26)	· · ·			45678901234567890123456789010		•	



```
303743
                                                                                333753
     ************* PROGRAM FOLLOWS ******
 C--- . RAX. ICXY IND.CATE ONS.COLUMNS OF MATRIX XX
C----THIS PROGRAM GAY MANDLE UP TO 1913 DIFFERENT CONSINATION CF
                                                                                335793
           RUNTIME. DELTIM, AND UNSPECIFIED PARAMETERS
                                                                                aca336
       DO 2932 L2G=1,1900
                                                                               000813
       WRITE(KOUT. 11) " "
                                                                               855823
       FORMAT (A1./)
11
                                                                                000333
        FORMATIA11
                                                                                000940
       WRITE(KOUT, *) 'THIS IS RUN NUMBER ', LOG
                                                                                901350
       MRITE(KOUT.*) * *
                                                                               000360
       WRITE(KOUT, *) 'ENTER A DESCRIPTION OF THIS RUN>'
       WRITE(KOUT,*) * *
                                                                                003390
       READ (KIN, 12) OSCRPT
                                                                                366363
       TARITE(KOUT,*)* *
       WRITE(KOUT.*) * *
       CALL INPUTMEFT, ST, GT, HT, FM, EM, GM, HM, PO, QT, QF, RT, RM, XO,
      1 HUU, HXX, HXU)
       IF (10.69.9) THEN
                                                                               300 353
       50 TC 2933
       END IF
                                                                                000970
       CALL RGS(GCSTR.RKFSS.GCX.SCY,GCZ.aCY.aCZ.FC.YD.
                                                                                203 383
      1441. mm2, Hm3. dm4, wF5. hm5. w M7. hm4. 4m9. nm10, hv 1. WV2.
                                                                               300 390
      1WM4, bM3, a4C, WM0, WPE, WMF, FT, BT, GT, HT, QT, RT.
                                                                               351133
      1 FH.EM.GH.HM.QM.RP.XO.PC.XXY.HUU.HXU.FA.9A.GA.QA.GUA.
                                                                               901313
      1 MX4 PXA, RA, PXVA, GCZA, IRY, IFLGCZ, IFLGSO,
                                                                                301323
                                                                             001333
      LUU. PUMAX, PUMIN, PXIMAX, PXIMIN, MIMAX, MUMIN, MX AMAX, MXAMIN,
      1 PUGUT, PATOUT, MATOUT, MUGUT, Wy3, WV4)
       WRITE(KOUT,*) ' '
      WRITE(KOUT,*)'00 YOU WISH TO CALCULATE THE EIGENVALUES OF THE CLOSOCIDED 150-LOOP STATE TRANSITION MATRIX USED IN THE PERFORMANCE ANALYSIS 001070 1 (APPLICABLE TO BOTH THE CONTINUOUS-TIME AND SAMPLED-DATA CASE) 001180
                                                                               301390
       RE40 (XIV, 12) 45G
                                                                               301133
       IF (HSG.EG.'Y') THEN
                                                                                331113
       WRITE(KOUT, *) THE CLOSED-LCCP STATE TRANSITION MATRIX EIGENVALUES 001121
      1 ARE ....
                                                                               361130
       HIDM=VARM
       ZMION=MION
                                                                               001150
       1+SKIOV=1HION
                                                                               331163
       CALL MEIGN (MMA, MV 3, MV-, IRFA, MME)
                                                                               001173
       VARMENION.
       NOIH1=NSAV+1
                                                                                031190
       ENO IF
                                                                                001203
       WRITE(KOUT, *) .
                                                                                001210
       WRITE(KOUT. 1) TYPE Y TO PERFORM THE COVARIANCE ANALYSIS, TYPE 001220
      1 N TO SKIP IT>"
                                                                                331233
       PEAD (KIN, 12) 456
                                                                                001240
       IF (MSG.EG.'Y') THEN
                                                                                301253
       GO TO 2332
                                                                                021269
                                                                                211273
       CALL PERFALI IRY, IFLGCZ, MXA.GCY, GUA.PXA, PXVA, IFLGSD,
                                                                                261282
     1 PA. GCZA. YD. H MA. M MS. M ME. M MF. M MO. MULT MX TOUT, FUCUT, PX TOUT,
                                                                                331293
      1 PRAHIN-XAMAY.RIMUY.XAMUN,MINUM.XAMIXAY.MIMIXAXAMIXAMIXHU.WH.XAMIXA
                                                                                061303
      1 4/3,444)
                                                                                371313
 2932 CONTINUE
2933 WEITE(KOUT, *) PROGRAM TERMINATED, NO MORE INPUT DATA!
                                                                               001322
                                                                                001337
       END
                                                                               201343
 * DESK STORED
                                                                               031353
       SUBROUTINE STORED (INCHRY, ENTINE, DELTIM, IFSTOL, IS: 25%,
                                                                               001360
                                                                                801370
           ISL35Z.131-SZ.IS15SZ.STOF12.STOF13.STOF14.STOF15.NOIM51
        STO E DATA TO PERMANENT FILE
                                                                                001350
```

```
CTHIS SUBROUTINE STORES PLOT DATA TO LOCAL FILES. TAPELZ.TAPELS.
          TAPEL- TAPELS FOR PERMANENT STORAGE. ISXXSZ IS THE SIZE IF THESCL-03
          11:10 - PO POIENEID MERCORR DALLIAD BHT IS MICH - XXXCTEAYSA ATAC
          THE ARRAYS. MOTE THAT RUNTIMEROELTIMER GIVES THE TOTAL DITARD HUMBER OF DATA POINTS IN THE RUN. THE LAST ENTRY IN EACH DITARD DATA FILE IS THE SCALE FACTOR FOR THE DATA ON THE FILE. THE DOINGS THE DATA IN THE FILECLASS
C
      DIMENSION STORIZ(NOIME), STORIZ(NOIME), STORIZ(NOIME), STORIZ(NOIME) 0011460
       COMMON /INOU/ KIN.KOUT.KPUNCH
       IF (IFSTCL.ED.)) THEN
                                                                                 021480
C
      PUT A RUN HEADER ON THE TIPE
                                                                                 011491
       OPEN (UNIT=12. ERR=15.FILE='TAPE12', RECL=80)
                                                                                 661503
       OPEN(UNIT=13, 222=13,FILE="TAPE13",RECL=81)"
                                                                                 301513
      OPEN CUNIT=1+, ERR=13, FILE= 'TAPE1-'.RECL=63)
                                                                                 001520
      OPEN (UNIT=15, ERR=1).FILE= 'TAPE15'.RECL=60)
                                                                                221533
       WRITE(12,101) INCHRN, ANTIME, DELTIM, IS12SZ
                                                                                001543
      WRITE(13,101) IWCHRN. ENTINE, DELTIM, IS13SZ
                                                                                 031550
       MRITE(14.131) INCHRN, PNTIME, CELTIM, IS14SZ
                                                                                 001560
      WRITE(15,131) INCHRN, ANTIME, DELTIM, IS15SZ
                                                                                 301577
                ',I1J,1X,2E13.6,I13)
       FORMATIC
                                                                                 GC1580
       END IF
                                                                                 36159G
      IF (IFSTCL.LT.G) THEN
                                                                                 901533
     CLOSE FILES AND PUT END OF FILE MARKER OH THEM.
                                                                                 091510
      CL052(12,293=13)
                                                                                 001620
       CLOSE(13, ERR=10)
                                                                                 001633
       CLOSE(1+, faq=10)
                                                                                 331643
       CLJSE(15, ERR=19)
                                                                                 001653
      RETURN
                                                                                 031563
       END IF
                                                                                 221672
      HRITE(12.132) (STOR12(I).I=1.IS12SZ)
HRITE(11.132) (STOR13(I).I=1.IS13SZ)
HRITE(14.102) (STOR14(I).I=1.IS14SZ)
                                                                                 301693
                                                                                 051701
       WRITE(13,102)(STOF15(I),I=1,IS15SZ)
                                                                                 301713
                                                                                031723
                                                                                 001733
10
       "PITE(KOUT, *) 'AN ERROR HAS CCCURRED IN THE STORED POUTINE"
      F3RMAT(3(-(' ',E19.6,:),/))
                                                                                051746
                                                                                 031751
      END
. DECK INPUTH
                                                                                 301753
      SUBRCUTINE INFUTH (FT. BT. GT. FT. FF. BH. GM. HM. PO. CT. QM. RT. RH. XD.
                                                                                 031770
     INUU. WXX. AXU)
                                                                                 051783
      CHARACTER MSG+6J.MSG1+50
                                                                                 001794
       REAL FT (NOIM, NOIM), ST (NOIM, NOIM), GT (NOIM, NOIM), HT (NOIM, NOIM).
                                                                                101930
     10H(NOIM, NCIM) .RH(NOIM, NOIM) .XC(NOIM) .
                                                                                 021323
          . (HICH .MION) HB. (MION. MION) MA. (HICA. MION) XXX. (HICH. MION) UU
                                                                                 231333
     1 GM(NOIM, NOIM), WXU(NOIM, NOIM).
                                                                                 301347
     1 PO(NOIP, NOIM), QT(NOIM, NOIM), AT(NOIM, NOIM), COM1(1), COM2(1)
                                                                                 001350
     COMMEN THE INPINE MOINS
                                                                                 301363
       COMMON /MAINZ/COMZ
                                                                                 001370
                                                                              091981
       CCMMCN /MAIN1/NOIM, NOIM1, CCP1
      CONPCN / INOU/ KIN-KOUT, KPUNCH
                                                                                 001393
    CCHHCN /MAUNS/ MSG 5:1935
GOMMCN /MAIMS/ ICST.ICSH.ICFA.ICGA.LCGM.ICGT.ICGA.IRFA.IRFM.IRFT. 301912
         IRMT.IRGA,IO.LGG,IRMM.NUMGTS
                                                                                 331923
      061 330
          ICFT=1:FT, ICFM=IRFM, IRBT=IFFT, IRBM=IFFM, IRGT=IFFT, IRGM=IRFM
                                                                                 021340
          IRX=IRF, IRG=IGG=IGGH, IRR=ICR=IRHT, IRWXX=ICWXX=IRFH.
                                                                                 301353
          IRWUU=ICHUU=ICAM.ICHT=IPFT.ICHM=IRF4.IPGCZ=ICAT.ICGCZ=IRHT.
                                                                                 001361
     IO IS A INPUT COUTINE PAGA "ETER--1=READ, 2=READ&PRINT.
                                                                                 001373
      3= PRINT ONLY. 4=PUNCH
                                                                                 3:1993
                                                                                 001390
       MSAV=4DIM1
                                                                                 632333
                                                                                 552313
       MOINIENDIM
                                                                                 0:2320
       IF (LAG. EA.1) THEN
       HRITE(KOUT,*) *SG1
                                                                                 332333
       WFITE(KOUT, *) THE IND CATIONS ARE 0,1,2,3,4,5,6,.....
```

```
WRITE(<001.4)'1-READ ENTIRE ARRAY/VEGTOR, 2-READ AND PRINT'
HRITE(<001.4)'ENTIRE ARRAY/VEGTOR, 3-READ, AND A-READ AND PRINT'
HRITE(<001.4)'SELECTED HRRAY/VEGTOR ELEMENTS, 5 REINT ENTIRE'
HRITE(<001.4)'ARRAY/VEGTOR, 6 TO PRE-ZERO ARRAY ELEMENTS THEN'
HRITE(<001.4)'ENTER SELECTED ELEMENTS. 7 OR GREATER IF NO'
HRITE(<001.4)' ARRE I RUT.'
                                                                                   332.73
                                                                                    2:2333
                                                                                   352131
      WAITE(KOUT . *) 1 404E I PUT . 1
                                                                                   002103
       Walte(Kout.*) 45G1
                                                                                   ::2113
       WRITE(KOUT, +) 'SELECT WHICH PATRIX YOU WISH TO ENTER."
                                                                                   092129
      WRITE(KOUT, *) '3 T ENTERING THE APPROPRIATE NUMBER: 1-FT, 2-8T' 002133 HRITE(KOUT, *) '3-GT, --HT, 5-FT, E-3M, 7-GM, 3-MM, 9-F0, 13-GT, 11-RT, >' 002140
       WRITE(KOUT.*) '12-CH.13-RH.1--X0.15-WUW.16-WXX.17-WAW.18-EGUATE ALLGO2150
       HRITE(KOUT,*) 'GONTROLLER MGCEL MATIGES TO THEIR * 002171 WRITE(KOUT,*) 'TRUTH MODEL COUNTERPARTS,19---- NO MORE OATA* CO2183 WRITE(KOUT.*) 'EATRIER TO BE MADE OF CONTROL OF MADE OATA*
       WRITE(KOUT, -) 'ENTRIES TO BE MADE, 20--STORE ALL MATRICES ON TAPET'002190
       WRITE(KOUT, *) 'Z1- 4EAO ALL PATRICES FROM TAPES'
       WAITE(KOUT.*) 4551
                                                                                   052213
     WELTE(KOUT,+) MSG1
                                                   WEITE(KOUT,*) * *
      HRITE(KOUT,+) FOR SAMPLED DATA MEASUREMENTS, ENTER EITHER A CONTINUO32243
      LOUS AM TO USE TO APPROXIMATE THE DISCRETE TIME APDIRMO-RM/SAMPLE 002250
      TITIES OR ENTER THE DISCRETE TIME PMO" GUZZES
       WRITE(KOUT,*) 45G1
      HPITE(KOUT, *) MSG1
       END IF
                                                                                   322293
       00 952 INPUT=1,1,1);
                                                                                    002303
      WRITE(KOUT, 33333)
                                                                                   002310
33333 FCRMAT (A13./)
                                                                                   442323
       FCRMAT(A13+7)
WRITE(KOUT+*)'ENTER GOOE FOR WHICH ARKAY/VECTOR TO BE INPUT>* B0233G
        READ (KIN.4) INCHPA
        GU 13(1.2.3.4.2.6.7.3.9.1..11.12.13.14.15.16.17.18.19.24.21) INCHMAGE235;
GC---TRUTH PODEL INPUT GC2373
      WRITE(KOUT.+)'ENTER-I/O OPTION, FT MATRIX SIZE>'
                                                                                002350
       READ(KIN, *, END=27) IC. IRFT
       MSG= TRUTH MODEL F MATRIX ENTRIES!
        CALL MMATTO (FT, IRFT, IRFT, IC, KIN, KOUT, NOIM, NOIM1)
                                                                           002423
       IF (IO.EG.2) THEN
       RETURN
                                                              932440
332453
       ENO IF
      GO TC 912
     WRITE(KOUT, *) 'ENTER-I/O OPTIONS, COLUMN SIZE OF ET>'
READ(KIN, *, END=27) IO, ICST
                                                                            302470
    MSG= TRUTH MODEL 3 MATRIX ENTRIES!
                                                                              002480
202490
       CALL HMAT 10 (3T, 15FT, 1C T, 1G, KIN, KOUT, NOIH, NOIH1)
IF (IO.EG.G) THEN
RETURN
                                                                    002500
                                                                                   002512
      END IF
                                                                              032533
        GO TO 332
3 WRITE(KOUT, *) 'ENTER-I/O OPTICN, COLUMN SIZE OF GT>'
READ(KIN, **. END=27) IC. ICGT
                                                                               902541
302550
     READ(KIN. F. END=27) IC. ICGT

MSG='TRUTH MODEL G MATFIX ENTHIES'

CALL MMATIO (GT. IRFT. ICGT. IC. KIN. KOUT. NOIM. NOIM1)
                                                                                   002560
                                                                                  0:2571
       IF (IO.EG.G) THEN
       RETURN
                                                                                   202593
     END IF
                                                                                   202633
                                                                                   302510
 WRITE(KOUT, +) 'ENTER- I/O GPTICH, ROW SIZE OF HT>"
                                                                                   112523
       READ (KIN, *, END=27) IC, IRHT
                                                                                 332643
332653
       MSG='M MATRIX ENTRIES'
      GALL MMATIO (HT. IRMT. IRFT. IC. KIN, KOUT. NOIM. NOIM.)
        IF (10.29.3) THEN
                                                                                   032560
        RETURN
                                                                                   012573
        END IF
                                                                                   002580
        GC TC 342
                                                                                   002590
 C. TINEUT CONTROLLER MODEL
                                                                                    222733
```

```
MPITE(KOUT,+)/EITEPHIZO CATION, FM HATRIX SIZE>/
                                                                                212713
      #E4D(KIN, *.EVD=27) IC. IFFM
MSG='CONTROLLER MCDEL # MATRIX ENTRIES'
                                                                                1:2721
       WFITE(KOUT .+) 'ENTER THE NUMBER OF DETERMINISTIC CTATES IN THIS MODDIZTAL
      15. > "
    ____RE40 (KIJ) * .EYO=27) Y LMOTS
     CALL MMATIO (FM. IRFM. IFFM. IC. KIN. KOUT, NOIM. NOIML)
       IF (13.69.3) THEN
                                                                                3.2791
      RE TURN
                                                                                002333
       END IF
 GO TC 932
                                                                                052913
        WRITE (KOUT - - ) "ENTER-LING OPTION - COLTHN SIZE OF BM> "
                                                                                25550
      READ (KIN. . . END=27) IQ. IC 3H
                                                                               162335
       MSG= 'CONTORLLER MODEL B MATRIX ENTRIES'
       CALL MMATIO (AM, IREM, ICAM, IC, KIN, KOUT, NOIM, NOIM1)
                                                                               2:2451
    IF (10.20.3) THEN
                                                                                302363
       RETURN
                                                                                002373
     END IF
                                                                               802333
     WPITE(KOUT.=)'ENTER-I/O OPTICH. GGLUHN SIZE OF GH>'
                                                                                22233
       9E4D(KIN. * . END=27)13.ICGH
                                                                               002910
  002920
                                                                            202940
 IF (IO.EQ.3) THEN
RETURN
                                                                                302363
       END IF
       GO TC 342
    WRITE(KOUT, *) 'ENTER I/O OPTICH, ROW SIZE OF HM>'
PERO (KIN, *, END=27) IC, IRHM
                                                                               302343
      MSG='THE CONTROLLER MODEL MEASUREMENT MATRIX, MM, IS'
CALL MHATIO (HM, IRFM, IRFM, IO, KIN, KOUT, NDIM, NCIMI)
IF (IO, EQ, G) THEN
RETURN
ENDIF
                                                                               3.3929
                                                                               003030
       ENDIF
                                                                               G v 3 3 4 3
       GO TO 382
      WRITE(KOUT, *) 'FT HUST BE ENTERED THRU OPTION 1 PRICE TO USING THIS 03365 1 OPTION DO YOU HISH TO ABOUT THIS OPTION, Y OR N>' 303373
     READ(KIN, 97, END=27) MSG
IF (MSG.EQ. 'Y') THEN
                                                                         003190
      GO TO 992
END IF
                                                                               353113
      END IF

WRITE(KOUT, *) 'ENTER I/O CPTICN, IRFT IS ASSUMED SIZE OF FO>' 063120

063120

063133
  READ(KIN. *.END=27)IC

MSG= "THE INITIAL COVARIANCE MATRIX.PO. IS"

CALL MMATIO (PO.IPFT.IRFT.IC.KIN.KOUT.VOIH.NOIH1)
                                                                               353143
                                                                               003150
    IF (10.60.3) THEN
                                                                               003160
       RETURN
     END IF

GO TO 382

4RITE(KJUT.*)*ENTER I/O CFTION, ICGT IS ASSUMED SIZE OF OT>* 303200

READ(KIN.*,END=27)IC

003214
READ (KIN, *, ENG=27) IC ... LOGI LS 455 UNEU S
MEG= 'THE INPUT HOISE STRENGTH MATRIX OF IS'
                                                                               963553
       CALL MMATID (OT, ICGT, ICGKIN, KOUT, NOIMAN)
                                                                               143233
        IF (19.EQ.C) THEN
                                                                                223251
       RETURN
        END IF
        G0 TC 382
          ARITE(KOUT,+) 'ENTER I/O CPTION-IRHT IS ASSUMED SIZE OF RT>"
                                                                               013283
       READ (KIN, *, END=27) IC
MSG="THE MEASUREMENT HOISE STRENGTH MATRIX RT IS"
                                                                               063393
                                                                                203300
        GALL MHATIO (RT, IRHT, IRHT, II, KIN, KOUT, NOIP, NOIP1)
                                                                                223310
        IF (IO.EQ.J) THEN
                                                                                993322
                                                                                3:3333
        RETURN
       ENG IF
                                                                                003343
                                                                                0:3:5:
        GC T3 332
        WEITERKOUT. *) 'ENTER ING GETICN. LOGM IS ASSUMED SIZE OF GME'
```

```
9E4)(KIN.*,ENG=27)IC
      MSS= 103MTROLLER 100EL INPUT NOISE STRENSTH HATRIX, OH!
                                                                              :::*5:
                                                                             111191
      IF (13.80.3) THEN
                                                                             3.343:
      RETURN
                                                                             333-13
      END IF
      GC TO 332
                                                                             003-30
      WRITE(KOUT, ** PATER I/O OPTION, IRHM IS ASSUMED SIZE OF RMS *
13
      READ (KIN. +. ENG=27) IC
                                                                             0:3-50
      MSG="CONTROLLER MCDEL MEASUREMENT NOISE STRENGHT MATRIX, RM"
                                                                             623-69
      CALL MMATIO (RM, IRMM, IRMM, IG, KIN, KGUT, NOIM, NOIM1)
                                                                             003472
      IF (10.69.3) THEN ___
      RETURN
                                                                             163 - 96
      ENG IF
      G0 TC 932
                                                                             303514
      WRITE(KOUT. >> FT PUST BE ENTERED THRU OPTION 1 PRIOR TO USING THIS 01352)
     1 OPTION. DO YOU WISH TO ABORT THIS OPTION, 1 OR No!
                                                                             JC3531
      #E40 (KIN+97+END=2714SG
         CASS.EQ. 'Y') THEN
                                                                             123551
      GO TC 342
                                                                             333563
     END IF
                                                                             223572
        HRITE(KOUT, +) 'ENTER I/O CPTION, IRFT IS ASSUMED SIZEOF XO>'
                                                                             113589
     DI(TS=DN3, +,41X) BASF
                                                                             203592
     MSG="THE INITIAL STATE VECTOR, XO, IS"
CALL MVEGIO (XO, IRFT, IO, KIN, KCUT, NOIM)
                                                                            _ 363903_
                                                                             203613
      IF (IO.EQ.3) THEN
                                                                             303529
      RETURN
      END IF
                                                                             303643
      GO TO 342
      MPITE(KOUT. *) '3M MUST BE ENTERED THRU OPTION 6 OR 17 PRIOR TO USING 3563
     IG THIS OPTION. DO YOU WISH TO ABORT THIS OPTION, Y OR 454 DE3673
      RE40 (KIN. 97.EN0=27) MSG
                                                                             J33683
      IF (MSG.EQ. Y') THEN
                                                                             3:3593
      GO TO 342
END IF
                                                                             003700
                                                                             093710
       HR. TE (KOUT, *) "ENTER 1/0 OPTION. ICAH IS ASSUMED SIZE OF HUU>"
                                                                             863727
      READ (KIN. + . ENO=27) IC
                                                                             913734
     MSG= 'THE CONTROL FUNCTION COST WEIGHTING MATRIX. WUU' CALL MMATIO(WUU.ICBM.ICBM.IC,KIN,KOUT,NOIM,NOIM1)
                                                                            363740
   IF (10.50.6) THEN
RETURN
                                                                             003763
                                                                             993773
      ENO IF
                                                                             053783
     GO TC982
     WRITE(KOUT, +) FM MUST SE ENTERED THAU OPTION 5 OR 17 PRIOR TO USING 3483
   IG THIS OPTION. DO YOU WISH TO ABOUT THIS OPTION, Y OR ME!
     # E 40 (KIN, 97, EM0 = 27) MSG
                                                                             053826
      IF (MSG.EQ.'Y') THEN
    GO TC 332
                                                                             003844
                                                                             003350
     WATTE(KOUT,+) 'ENTER I/O OPTICH, IRFM IS ASSUMED SIZE OF WXX>"
                                                                             033360
      READ (KIN. + , ENG=27) IC
      MSG= "THE STATE COST WEIGHTING MATFIX, MXX"
                                                                             223336
      CALL MMATID(wxx, IAFP, IRFM, IC, KIN, KOUT, NOIP, NOIM1)
                                                                             003890
      IF (IO.EG.G) THEN
                                                                             003903
      RETURN
      END IF
                                                                             333923
      GO TO 392
                                                                             023930
      wpite(kgut,+) *all controller podel matrices have been set egual togc3940
     1 THEIR TRUTH MODEL COUNTERPARTS"
      DEEE2DING THE BRIDE TO USING THE TEATHER TO USING THE TEATHER TO USING THE TEATHER.
     IS OPTION. THE HUMBER OF DETERMINISTIC STATES HUST BE ENTERED IN 003970
     1 THIS OPTION(FOR CONTROLLER PODEL)."
                                                                             0:398:
      M-ITECKOUT.-1: DO YOU HISH TO ABORT THIS OPTION.Y DR NH:
                                                                             563395
      PEAG(KIN.97.5:0=27)455
      IF (MSG.E2.") THEN
                                                                             224313
      90 TC 3:2
                                                                             164121
```

```
END IF
      HPITE(KOUT, *) FENTER THE NUMBER OF DETERMINISTIC STATES IN THE CONTINUE,
     12011ER MODEL»
      7540 (KIN, 1,240=27) NU 40TS
                                                                         11-161
      IRFHEIRFT
                                                                         204373
      FCRMAT(41)
                                                                          ::4:8:
      IC3M=IC3T
                                                                          11-191
      ICGM=ICGT
                                                                          304100
      IRMM=IRMT
                                                                         394113
      CALL EQUATE(FY,FT, IRFT, IRFT)
                                                                         35+120
      CALL EQUATE(SH, ST, IRFT, ICST)
                                                                         344133
      CALL EQUATE (GA,GT, IRFT, ICGT)
                                                                         CC+ 140
      CALL EQUATE(HH, HT, IRHT, IRFT)
                                                                         034153
      CALL EQUATERNATATICGT, ICGT)
                                                                         064160
      CALL EQUATE(RM, RT, IRHT, IRHT)
                                                                         384173
      GC TG 332
      WFITE(KOUT,+) 'NOTE THAT FILAND BY MUST BE ENTERED THROUGH APPROPRISCA190
17
     TATE OPTIONS PRIOR TO EXECUTING THIS OPTION. DO YOU WISH TO ABOUT TOC4203 THIS OPTION, Y OR NOT DU4212
      READ (KIN. 97.ENO=27) MSG
                                                                         00-229
      IF (MSG.EQ. 'Y')THEN
                                                                         004230
                                                                         034243
      GO TC 932
      END IF
                                                                         014253
      WRITE(KOUT,+) 'ENTER I/O OPT.CN, IRFM X ICEM ASSSUMED SIZE MXU>'
                                                                         354263
      ₹£40 (KIN. + , END = 27 ) IC
      MSG='THE CROSS (STATE-CONTROL) COST MEIGHTING MATRIX, MXU'
                                                                         204233
      CALL MMATIO(WXU, IRFP, ICBM, IC, KIN, KOUT, NOIM, NOIM1)
                                                                         344293
      IF (10.50.3)THEN
                                                                         004303
      RETURN
                                                                         004310
      END IF
                                                                         6:432:
                                GO TC 382
                                                                         054333
      WRITE(KOUT.-) * THIS OPTION STORES ALL MATRICES ON TO TAPET, DO YOU344343
     1 WISH TO ABORT THIS OPTIONAY OR NO!
                                                                         344 354
      READ (KIN, 97) 4SG
         IF (MSG. EQ. THEN
                                                                         124 37 2
         SC TO BAR
                                                                         354333
          END IF
                                                                         634395
      write(7,+) irft, icat.icgt, irht.ikft, icam.icgm. irhm.numots
      WRITE(7,+) ((FT(1,J),J=1, 1RFT), (=1, 1RFT), ((1,J),J=1, 1C8T) =1,1R514-13
     I((FP(I,J).J=1.IRFP).;=1.JTFP).((3M(I,J).J=1.IC84).I=1.I4FP)
                                                                         534433
      1HM), ((PJ(I,J),J=1,IRFT), I=1,IRFT), (XO(I), I=1, IRFT), ((MUU(I,J),
                                                                         324+53
     1 J=1,ICam), I=1,ICam), ((WXX(I,J),J=1,IRFM),I=1,IRFM)
                                                                         224460
      TOWNER T. 1=1. (THAISTEL, (L. I) TR)), (TOO1, 1=1, (TOO1, 1=1, (L. I) TO)) (+, 7) 3 TI RH
     1HT), ((QM(I.J),J=1,ICGM),I=1,ICGM),((RY(I,J),J=1,IRHM),I=1.IRHM)
      WRITE(7,+)((WXU(I,J),J=1,ICEM),I=1,IRFM)
                                                                         224500
      GC TC 352
    ARITE(KOUT, *) * THIS OPTION -EADS ALL MATRICES FROM TAPES, DO YOUJCA513
1 WISH TO ABORT THIS OPTION, Y OR N> *
      READ (KIN. 97) 4SG
         (MSG.EG.'Y') THEM
                                                                         304540
           GO TO 352
                                                                         334553
      ENO IF
                                                                         004563
      WRITERROUT, *) 'DO YOU WISH TO REWIND TAPES BEFORE THE READ. Y 32 43 700 4575
      READ (KIN, 37) MSG
      IF (MSG.EQ. 'Y') THEN
                                                                         104591
                                                                         004503
         REWIND(S)
                                                                         304613
      ENO IF
      READ(8,+.END=10033)[RFT.IC3T,ICGT.IRHT.IRFM.IC3M.ICGM.IRMM.NUMDTS 004620
      READ (3,4, END=13033) ((FT(I,J),J=1,IRFT), I=1, IRFT),((BT(I,J),J=1,ICBG(4639
     1T),[=1,[RFT),({GT([,J),J=1,[CGT),[=1,[RFT),((MT([,J),J=1,[RFT),[=1]0+640
     1.IRHT), ((FM(I.J), J=1.IRFH),[=1.IRFH),((BM(I.J),J=1,IGBM),I=1.IRFM)004650
     READ(3,+,END=13333)((GM(I.J),J=1,ICGM),I=1,IRFM),((HM(I.J),J=1,IRF334663
     14),I=1,IZHM),((PO(I,J),J=1,ITFT),I=1,IZFT),(XC(I),I=1,IZFT),((WUU(GC457)
     1 [ .u) .j=1,ICBM) .[=1,ICB4) .((mxx(I.J).J=1.IRFM).[=1.IRFM)
```

```
17),1=1,13+7),((34(1.J),J=1,139M),1=1,139M),((34(1.J),J=1,134M),
     1 [=1,[744]
      READ (3, *) ((AXU(I,J).J=1,ID3*).I=1.I=F4)
                                                                    1-72
      Sef 57 DZ
                                                                   334733
      WRITE(MOUT, *) 'ENG OF. FILE ENGCUNTERED DURING FEBO OF TARES'
16333
         BUNITADO
982
19
          CONTINUE
                                                                   334763
      WARMELKION
                                                                   214771
      RETURN
                                                                   354785
 27
      IG=1
                                                                   364793
                                                                   004300
      ENO
                                                                   0024813
* DECK HELGH
                                                                   304 423
      SUBROUTINE MEIGN (A.AREV.AIE/.CUPSZA.WM1)
                                                                   334334
      CHARACTER MSG*62
      CHICH, MICH, MICH, (MICH) VEIL, (MICH) VERA, (MICH, MICH) ANDIANIO
      DIMENSION COMICILICOMECIL
COMMON MAINIMPRODUCTION
                                                                   204361
                                                                   304370
   COMMON /44UNS/ MSG
                                                                   33-988
    THE CALLING POUTINE MUST SUPPLY A MORKING PATRY NOIM & NOIM -- HM1
C+++FIND THE EIGENVALUES OF A , NR=0 TELLS THE ROUTINE TO CALGULATE
                                                                   364320
       EIGENVALUES ONLY
   NOIM MUST BE THE DIMENSION OF A IN THE CALLING PROGRAM
      MREJ
                                                                   354353
      112= :
                                                                 __304963
__864973
      C1=1.0
      CALL IDNT (GURSZA, WM1, C1)
                                                                 004980
C WHI =I
          CURSZA X CURSZA
                                                                   124 491
      CALL EIGEN (CURS ZA ,A ,A REV , A IEV ,WM1, NR)
                                                                   005349
      10=5
                                                                   035013
      NSAV=NDIM1
                                                                   005320
      PICH=INION
                                                                   305133
      MSG= 'REAL PARTS OF THE EIGENVALUES '
      CALL MVECTO (AREV.CURSZA. TO.KIN, KOUT, NOIM)
      MSG='IMAG PARTS OF THE EIGENVALUES '
      CALL MVECIO (AIEV, GURSZA, IO, KIN, KOUT, MOIM)
                                                                  005373
                                                                   305 330
      NOIM1= NSAV
                                                                   035393
      END
* DECK COTCON
      SUBROUTINE COTCON(FM.SM.WXX.HUU.GCSTR.IHOLD.ICSM.HM1.HM2.
                                                                  035120
     INHS, ANG, AMS, AND, FPRIM, AXXFRM)
                                                                   995133
      CHARACTER MSS+60
      1.GCSTR(NOIM.NOIM)
                                                                  005163
      , (WIDA, WIDA) UKW. (WIDA, WIDA) 5MW. (WIDA, WIDA) 5MW. (WIL
                                                                   235183
     1 WXXPRH(NOIM, NOIM) . FPGIN(NOIM, NOIM)
                                                                   115193
      DIMENSION COM1(1).COM2(1)
                                                                   215 29 1
      COMMON /MAINZ/COMZ
                                                                   CGF 213
      COMMON /MAINI/NOIP.NOIM1.COP1
                                                                  315220
      COMMON / INOU/ KIN, KOUT, KPUNCH
                                                                   035233
      COMMON /MAUNE/ MSG
                                                                   0:5241
                                                                   005 25 0
COTTOETERMINISTIC CONTROLLER GAIN CALCULATION---MODULE # 1
                                                                   005261
C
                                                                   935279
       THIS MODULE COMPUTES THE STEADY STATE DETERMINISTIC CONTROLLER
                                                                 335 293
Ċ
       "GAÎN "AFFEE, GOSTAP=(HUUI)(9MT)(KOSSPM). HUUI IS THE INVERSE OF TOUB 29G
C
       CONTROL COST WEIGHTING MATRIX, KOSSPM IS THE STEADY STATE
C
       SQLUTION TO Q(KC)/QT=(FMT)(KC)+(KQ)(FM)+WXX+(KG)(3M)(WUI)(FMT)=QC5313
       IKC). WXX IS THE COST WEIGHTING MATPIX ON THE STATES
                                                                  205 323
                                                                   225330
       KUSENHAH ROUTINES ARE EXTENSIVELY USED IN THIS MODULE
```

```
30535.
                                                                                                                                      1.5361
    TRANSFORM SYSTEM SO THAT WYU NOTED GAN STOLL BE MANDLED BY
                                                                                                                                      005370
C KLEINMAN ROUTIMES. SEE KMAKERNAAK AND SIVAN'S BOOK. PAGE 322
                                                                                                                                      115383
           CALL PRIMIT(AM1.AUU.ICEM.GOSTF.AKU.IMCLO.EM.WM2.FFFIM.AXX.AYXPRM. 01539]
          FYI
C NOW HAVE FARIMA MX4FRM CAN USE RICCATI SOLVER FOR KOSSPM
                                                                                                                                      035413
           MT=1
                                                                                                                                      545423
            CALL TRANSPOLITION TO 3M . HM2)
                                                                                                                                      005430
C HMZ=BMT ICBM X IHCLE
                                                                                                                                      015447
           CALL EQUATE(WM1, WUU, ICBM, ICEM)
                                                                                                                                      225-54
     GMINY DESTROYS THE CALLING ARRAY
                                                                                                                                      005463
           CALL GM.NV (IC3M.ICBF.AMI.HM3.MR.MT)
CALL GM.NV (IC3M.IC8F.MM1.HM3.MR.MT)
C MM3=HUUI IC8M X IC8M-----AR IS AN ERROR INDICATOR
                                                                                                                                      005479
                                                                                                                                      235483
            IF (PR.NE.ICSM) THEN
           PRINTE, 'AM ERPOR COCURRED IN INVERTING WUU, MR=', MR. 'ICAM='.ICAM | 005500
           END IF
                                                                                                                                      005310
                                                                                                                             0 15 53 <u>.</u>
0 05 54 <u>0</u>
0 05 55 <u>0</u>
0 05 55 <u>0</u>
           CALL EQUATE (AM1. WM3. ICAM, ICAM)
C WHERMULE SAVE FOR LATER COMPUTATIONS
            CALL MATI(MM3,MM2,ICBM,IGBM,IMOLD,MM4)
C WH4 = (WUUI) (SMT) ICEM X IHOLD
           NOW CALL RICCATI EQUATION SCLVER
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372
           #KCSSPM IMOLO K IMOLO
#FM-BM(4UUI)(8:4T)(KCSSPM)---I DONT USE THIS RESULT 0.5561)
#SG='KOSSPM_FOR THE DETERMINISTIC CONTROLLER IS! 0.5630
C wr5=FM-8M(4UUI) (84T) (KCSSPM) --- I DONT USE THIS RESULT
            IC=5
                                                                                                                                      335630
           NSAV = VOIY1
                                                                                                                                      005643
           MION=1MION
                                                                                                                                      005553
            CALL MMATIG(WM2+1HOLO+IHOLO+IC+KIN+KOUT+NOIM+NOIM1)
                                                                                                                                      3355607-
             NOW CALCULATE OPTIMAL SAIN MATRIX GOSTAR. NOTE I NEED THE NEGATIVE OF GOSTAR FOR THE CONTROL LAW GENERATION FROM AN LOG
                                                                                                                                      0:5570
C
                                                                                                                                      865 538
             CONTROLLER, AND THIS WILL BE THE GCX REQUIRED IN THE PERFORMANCE 005590
             ANALYSIS ROUTINE
                                                                                                                                      335743
           NO IM1= YSAV
NULHIRNSAV
C NGW HAVE KOSSPM , CALCULATE GOSTR#WUUI(BMT(KOSSPM)+WAUT)
                                                                                                                                      305720
G RECALL MUUI IN WHI
                                                                                                                                      005733
                                                                                                                                    00574<u>0</u>
           C1=1.3
            CALL HATGA (3M, MM2. ICSM. IHCLO, IHCLO, HM4)
                                                                                                                                 00575
            CALL TRANSS (IHOLD . ICBM . HXU . HM3)
           CALL MADD1 (TG3M, IHOLD , HM4 . HM3 , HM2 . G1)
                                                                                                     GC5773
            CALL MATI(WM1.4M2.ICBM.ICBM.IFOLD.GCSTR)
           NS4V=NOIN1
                                                                                                                                      835793
            NOIM1=NOIM
                                                                                                                                      905399
                                                                                                                                      305313
            IC=5
C GCSTR ICAM X IHOLD
                                                                                                                                      005320
                                                                                                                                      005333
            MSG# THE OPTIMAL STEADY STATE FEEDBACK GAIN MATRIX, GGSTR*
                                                                                                                                      305343
                                                                                                                                      0053531-
            CALL MHATIG(GCSTR.ICBH,IHJLO,IO,KIN,KOUT,NDIM.NDIM1)
            NOIM1=NSAV
                                                                                                                                      005360
                                                                                                                                      345375
C
                                                                                                                                       045 881
            END
+ DECK CKFTR
                                                                                                                                      305393
            SUBROUTINE CKFTR(FM.GM.P.HM.NUMDTS.RKFSS.G.AM1.WHZ.
                                                                                                                                      33536:
          1HH3, HH4, HH5, HM6, IRFM, IRHM, ICGM, F2, H2, BH, ICBM)
                                                                                                                                      005913
     CALLING PROGRAM MUST SUPPLY FIGHT HORK SPACE ARRAYS
                                                                                                                                     U 35 723
                                                                                                                                      005 930
 CTHIS ROUTINE CALCULATES THE KALPAN FILTER GAINS WHEN
                                                                                                                                      305943
C GIVEN THE FYORM, ON AND A MATRICES AND THE MUMAER OF
                                                                                                                                     365353
    DETERMINISTIC STATES. THE CONTROLLER MODEL MUST BE
                                                                                                                                      0:5364
    SPECIFIED SUCH THAT ALL THE DETERMINISTIC STATES APPEAR
 C FIRST AND TOSETHER. THAT IS
                                                                                                                                     GC598:
CO/OT(X1,X2....(K.XL,XM,....))T=F1
                                                                                                                                      005 990
                                                                                           (U) + (W)
                                                                           (x) +
                                                                                                                                      316338
```

```
G Z
                                                                                                    32
                                                                                                                                                           3:5110
         WHERE AS THROUGH KK ARE THE DETERMINISTED STATES AND THE
                                                                                                                                                           005020
        REMAINING STATES ARE STOCHASTIC. FL IS K X K, AND FO IS N-K &
                                                                                                                                                           016:30
        M-K. AND 31.82.1MD G2 14E PARTITIONED ACCORDINGLY.
                                                                                                                                                           306343
       THIS ROUTINE FIRST STRIPS OFF THE DETERMINISTIC STATES THEN DOMPUTES
                                                                                                                                                           336353
   CAND RETURNS KALMAN FILTER GAINSFOR THE REMAINING STATES.

G. THE KALMAN FILTER GAINS FOR THE DETERMINSTIC STAES ARE SET TO ZERO
                                                                                                                                                          506161
C AND THE KALMAN FILTER GAIN THAT IS RETURNED IS CRESS
                                                                                                                                                           336384
C WHERE THE DIMENSION OF THE ZERO VECTOR IS K AND THE RKFSS IS THE 3C6 170 C STEADY STATE KALMAN FILTER GAIN PATRIX FOR THE N-K STOCHASTIC STATES. 3C6 113 C THIS AUGMENTED MATRIX IS RETUTNED IN RKFSS 306 120
       ALSO NOTE THAT IN ORDER TTO GENERATE THE KALMAN FILTER. ONLY
                                                                                                                                                          10613:
  C MEASUREMENTS OF STACHASTIC STATES ARE NEEDED SO THE H MATRIX IS
                                                                                                                                                           0 66 140
   C REDUCED ACCORCOINGLY.
                                                                                                                                                           006150
                CHARACTER MSG+60, MSG1+1
                CITECO. (PICH.PICH.) NO. (FICH.PICH.) FM (NO. M. ON.) SH. (PICH.PICH.) FM (NO. M. ON.) FM (NO.
                    . (RION. MION) D. (RION. MION) : MW. (MION. MICH) MM. (RION. MION) F
                    (Midn, Mior) 2H W, (Mion, Mion) 4MW, (Midn, Mior) Emw, (Mior, Mior) Shw
                    (PICH, NICA) BAW
                REAL RKFSS(MDIH, NOIM), 8M(NOIM, NOIM)
                                                                                                                                                           016210
                DIMENSION COM1(1),CCM2(1)
                                                                                                                                                           136 220
                SHUDYZNIAKY NUKKOD
                                                                                                                                                          006230
                COMMON /MAIN1/NOIM, NOIM1, COM1
                                                                                                                                                           006240
                COMMON / INOU/ KIN, YOUT, KPUNCH
                COMMON /MAUNS/ 45G
                                                                                                                                                          036263
   C+++KALMAN FILTER STEADY STATE GAIN----MODULE # 2
                                                                                                                                                          036280
                PKFSS= (PMSS) (MMT) (RI), WHERE PM IS THE STEADY STATE SOLUTION TO THOSE 300
                RIGCATI EAUATION O(PH)/OT=FM(FH)+PM(FMT)+G?(Q)(GMT)-
                                                                                                                                                       006320
                 PH(PHT)(RI)(HH)(PH)
                                                                                                                                                          306333
                                                                                                                                                           1136 344
        READ (KIN, 11) HSG:
                                                                                                                                                           006413
                NUMS AV = NUMB TS
                                                                                                                                                          106420
                IF (HSG1.EQ. Y") THEN
                                                                                                                                                          066430
                " ITE (KOUT, ") 'ENTER THE NEW VALUE OF NUMBER FOR THIS RUN"
               READ (KIN. *) NUMDTS
                ENO IF
                                                                                                                                                           016463
                I+2TONUA=20I
                                                                                                                                                           666476
                00 2112 I=IOS, IRF#
                                                                                                                                                          906481
                II = I -NUMOTS
                                                                                                                                                           036493
                00 2112 J= I75. IRF#
                                                                                                                                                           216540
                STONUM-L=LL
                                                                                                                                                           006510
                                                                                                                                                          096520
! 2112 F2(JJ, II) = FM(I, J)
                IRFZ=IRFM-NUMOTS
                00 2113 I=1.194H
                                                                                                                                                          CS6541
                DO 2113 J= IDS. IRFM
                                                                                                                                                           0 26 55 0
                STONUM-L=LL
                                                                                                                                                           306563
   (L, 3) MH=(LL, 1) SH E115
          NOH FORM 32,G2
                                                                                                                                                           J2658J
                00 2114 I=IDS.IRFE
                                                                                                                                                           006593
                STONUM-I=II
                                                                                                                                                          306500
                00 2114 J=1.1CSN
    2114 WM1(II,J)=G4(I,J)
                                                                                                                                                           026523
   C WM1 =G2 IRF2 X TCGH
                                                                                                                                                           0 165 30
                00 2115 I=135.13FM
                                                                                                                                                           036540
                II=I-NUMOTS
                                                                                                                                                           266 357
                90 2115 J=1,IC34
```

2115 W-(II.J)=BM(I.J)	005670
C wh+ =32	016680
IF 42=1+4	0:5590
CALL MATS (IRF2, ICGM, MM1, Q, MMZ)	936733
: WH2#GM(3)(GHT)	AS "Q"IN KLIENMAN RICCATI ROUTINE GC6710
walte(Kout,+) 'OJ you wish to mo	SOIFY O BY THE DOYLE AND STEIN TECHIBCE725
IQUE. Y OR W>"	36733
READ (KIN-11) MSG1	066743
LI FORMAT(A1)	0.6751
IF (MSG 1.EQ. 'Y') THEN	206763
CALL DASIGNAS, WP4, AM1, ICOM, WM	
END IF	306783
NT=1	016790
CALL EQUATE(WM1.R.IRM2, IRM2)	7.7.1.1.1.1.1.1.1.1.1.1.1.1.1.1.1.1.1.1
GHINY DESTROYS THE CALLING ARRAY	066910
GALL EQUATE (WM1, R. 13M2, 1RM2) GMINV DESTROYS THE CALLING ARRAY CALL GHINV (13M2, 13M2, MM1, 4M3, MM2	(TK.)
16 (42.472.472.4) 42.4	024426
WRITE(KOUT.+) 'MP='.MR. 'IRH2='.I	TRH2 9:6941
WALTERKOUT . +) 'A-INVERSE IS FOUL	EO UF* 396357
	176461
WH3= RI IRH2 X IRH2	
CALL TRANSZ(IRHZ, IRFZ, HZ, HH4)	0:6383
WHA HET IRFE X IRHE	006599
	12, mH5) C36 30G
HM5= H2T(RI) 13F2 X 19H2	336 913
CALL NATI (NH5, HZ, IRFZ, IRMZ, IRFZ	um3) 036,929
C WM3= M2T (RI) (M2)	026933 026933
CALL MRIC(TRF2.F2.4M3.4M2.4MF.4	106943
C NOW CALL RICCATI EQUATION SOLVERTO	GET PMSS 056950
C WM6=PMSS	026 364
CALL MATICHMS . MMS . IRF2 . IRF2 . IRF	12.WM1) 006970
C WM1=RKFSS IRF2 X IFH2	046940
10=5	016 990
C FORM RKFSS WITH ZEROS ADDED FOR DE	
PRINTS. 'AUMOTSE' ANUMOTS	937318
IF (NUMOTS.NE.3) THEN	207:20
00 2119 JE1.IMP	027130
00 2118 I=1,NUMOTS	037343
2118 RKFSS(I.J)=J	067353
00 2119 I=IDS,IRFN II=I-NUMDTS	937360
II=I-NUNS	967670
RILD RKFSS(I.J)=HH1(II.J)	337383 007198
ELSE	
CALL EQUATE(RKFSS, MH1, IRFP, IRHN	367103
sun ie	207 • • 0
HSG= 'STEADY STATE KALMAN FILTER	GAIN MATRIX. QKFSS* 067120 KIN. KUN. HOLM.
CALL MMATIO(RKFSS.IRFM.IRHM.IC.	KIN.KOUT.NOIM.NOIM) 907139
NUMOTS=NUMSAV	G07140
	007150
ENO	007163
DECK FRIAUG	007173
	C.HT.GCX.aCZ.FC.GCY.BCY.GT.XO.PC. 307183
1FA, 8A, GA, QA, GUA, MM1, AM2, AM, WM8	
1MX4.FX4.RA.PXV4.GCZA.IRY.IFLGCZ	
THIS ROUTINE FORMS A SET OF AUGHEN	
PERFORMANCE ANALYSIS ROUTINES	057 225
OIMERSION O (NOIP, NOIM), R (NOIP, N	
1,dt(noim,noim),jcz(noim,noim),h	
	SCY (NOIN, NOIN), GT (NOIM, NOIM). 327253
1 AO (NOIN), PO (NOIN, NOIN), AN1 (NO	
DIMENSICY FACYDIMS, NOIMS) BACHD	
HIOA.SHION)AHH. (SMION.SPION) AD 1	
	ins).whe(noips.noips).amp oct 290
1 (NOIM. NOIM). SCY (NOIM. NOIM) . FXA	

INTEGER IFLECT	207333
CHARACTER MSG-60	377347
DIMENSION COM1(1),CCM2(1)	037350
CC.4PC.4 ZMAI 4+ZNOI42,NOIH3	0:736:
COMMCN /MAIN2/COM2	037373
GOMPON ZMAINIZON, PROCESTATOR AND CONTRACTOR AND CO	327783
COMMEN / INDU/ KIN, KUUCH	007390
CONNEN ZHAUNSZ NEG	307-88
COMMON /MAINS/ ICST, ICSM, ICFA, ICGA, ICGM, ICGT, ICTA, IRFA, IRFM, IRFT,	007413
1191.31.ADS.IC.LQG.IAHA.IC.LQG.IAHAI.	507421
WRITE(KOUT,+) . ENTER A 3 IF YOU WANT ALL THE AUGMENTED MATRICES PE	2007633
TINTEC OUT. A 7 FOR NO MATRICES TO BE PRINTED>	007-43
READ (KIN. *)10	007450
NSAV1=NOIH	337+63
NGA 1-1041	007473
NSAVZ=NOIM1	007480
NSAV3=NOIN2	007490
NSAV4=NOIY3	307383
C	937510
C+++FORM AUGHENTED MATRICES THAT ARE REQUIRED WHEN FORMING XA	037520
C WA=(HT VT)T IMPLIES THAT GA= Q ;	0 0 7 5 3 0
GJ R	007540
C	107550
C FORM GA 1994 X 1994. IR94=19HT+1CGM	007963
C FOR EQUIVALENT DISCRETE TIME SYSTEMS TROAT TREFT-TRAFT	``````````````````````````````````````
IF (IFLGSD.EQ.3) THEN	007530
IR9=ICGT	307593
ELSE	007500
IRQ=IRFT	007613
Pup + P	007622
2N9 IP 00 2703 I=1,IRQ	307535
00 2733 J=1,12HT	007543
2703 WH1(I,J)=J	007650
00 2704 I=1.IRHT	
00 2704 J=1,IRQ	GJ7660
2704 WM2(I,J)=0	067573
	017590
• • • • •	307590
NOIN3=NSAV3	007700
NOIM2=NSAV1	007713
CALL AUGHAT (WH2, R. HPO, IFGRH, IRHT, IRQ, IRHT, IRHT)	007723
CALL AUGMAT(Q, MM1, MMC. IFORM, IRQ, IRQ, IRQ, IRHT)	0 6 7 7 3 0
ICQA=IRQ+IRHT	337743
IRQA=IGQA	007753
IFORM#2	067760
NOINZ=NSAV3	007773
CALL AUGHAT (WHC.WHO.QA.IF CRH.IRQ.ICQA.IEHT.IRQ1)	307780
MSG= THE AUGHENTED DEATH TO DETRIBUTE AND MSG=	997790
CALL MAATIO(QA.IRQA,IRQA,IQ.KIN.KCUT.NSAV3,NSAV3)	367300
TMARKSVILTER	207510
C INITIALIZE PXA MXA AND STORAGE VARIABLES	327923
00 5145 IMXA=1.NSAV3	357530
5105 MXA(IMXA)=0	327343
no 6143 Thylat fast	007350
5100 MXA(IMX4)=XC(IM)A) MSG=' THE INITIAL XA VECTOR IS' GALL MVECIG(MXA.IRFA.IO.KIN.KCUT.NSAV3)	107360
MSGs THE INITIAL YA VECTOR TER	007373
CALL MYECIO(MXA, IRFA, IO, KIN, KCUT, NSAV3)	207240
DO 211 IPX 4=1, IRFT	0:7390
00 5102 JPXA=1, IRFT	
5132 PX4(IPX4.JPXA)=PO(IPX4.JPXA)	107901
PAJS FAMIAFA49JFAMJ9FUNJFAMJ DO 8404 10494.TM8	007710
DO 5101 JPX=1,IMA	007923
JP & # 4 JP & 7 L 7 L 1	007930
5101 PX4(IPXA,JPXA)=1	007343
UU 5103 1PX=1,1MA	067353
IPYA=IPX+IRFT	007963
00 5153 JPX4=1,12f4	007970
5103 PXA(IPKA, JPKA)=0	J27981

```
MSG# ! THE INTITIAL COVARIANCE MATRIX, PX4 IS!
       CALL MAATIO(PXA, 1984, 1984, 10. KIN, KOUT, NSAV3, NSAV3)
                                                                                 308363
C++*P (VA C4LOULATION--- REQUIRED CALY FIRST TIME THEOUGH LOOP
                                                                                  338313
           PXV4= ST(GCZ)
      TO USE THE KLIENMAN MULTIPLY ROUTINES, THE DECLARED DIMENSION OF OGBISS
ARRAY ARGUMENTS MUST BE THE SAME. TMEREFORE IT IS NECESSARY TO DIBUGO
        FORM GCZ4 SUCH THAT GCZ4(I,J)=GCZ(I,J) FOR I=1,IRHT, AND J=1,
        ICBM. AND ZERO ELSENHERE
       THE SAME REASON REQUIRES CALCULATION OF RA
                                                                                 008090
                                                                                058143
       IT=NSAV3-IRHT
       JT=NSAV3-ICBM
       DO 6313 IG=1, IRHT
                                                                                 008120
       00 6014 JG=1.ICBM
                                                                                 008133
6014_ GCZA(IG.JG)=GCZ(IG.JG) _ 038140
       00 6:13 JG=1,JT
       JGA=IC3P+JG
                                      6013 GCZA(IG,JGA)=ú
00 6015 IG=1,IT
                                                                                 GG8188
       IGI=IG+IRHT
       OC 6315 JG=1, YSAV3 ______ OC8200
6015 GCZA(IGI.JG)=J
                                                                                 098213
       IR=NSAV3-IRHT
                                                                                 035223
       00 6J17 IRI=1, IRHT
                                                                                 003230
       00 6:17 JRI=1, IRHT
      DO 6017 JRI=1,IRMT
RA(IRI,JRI)=R(IRI,JRI)
DO 6016 JRI=1,IR
                                                                                 018250
                                                                                 038263
       JRJ=JRI+IRHT
                                                                                 308 27 3
      RA(IRI, JRJ)=0
       00 6:18 IRI=1.IR
                                                                                 308 296
                                                                           ____ 205 700
       IRII=IRI+IQ4T
       00 5118 JRI=1,NSAV3
                                                                                 005310
                                                                              019322
     RA(IRII,JRI)=0
RA = R IN UPPER LEFT PARTITION,ZERO ELSEWHERE
TE((TELGOZ.FO.4).ANG.(TELGOD.FO.3)) THEN
      RA(IRII, JRI)=0
                                                                                 998330
IF ((IFLGCZ. EQ. 0). ANG. (IFLGSO. EQ. 1)) THEN

C CALCULATE PXV4 CNLY FCR GCZ NOT EQUAL TO ZERO MATRIX AND NOT FCR S-0 008350

C RECALL THAT (3T(GCZ) BCZ)T IS THE RIGHR PARTITION CF GA 008350
                                                                                 338340
       00 6303 IPX #=1 , IRHT
                                                                                __003380
       IP4=IPXA+ICGT
       00 6333 JPX4=1. IRF4
                                                                                 008390
                                                                             0C<u>3+02</u>
60CJ
      PXVA(JPXA, IPXA) = GA(JPXA, IPA)
       NOIM=NSAV3
       NDIM1=NSAV3+1
       CALL MSCALE(WHF.PXVA, IRFA, IRHT.C1)
CALL MATI(WMF.RA, 1RFA, IRHT.FXVA)
                                                                                 008+40
C PVXA=PXAVT IRFA X IRHT
       HSG=' CROSS COVARIANCE, PXVA IS'
     CALL MMATIO(PAJA, IRFA, IRHT, IC, KIN, KOUT, NS 3V 3, NS AV 3)
END IF
                                                                                 338513
       FA= FA11 FA12 =FT+BT(GCZ)(HT) ST(GCX)
                                                                                 008529
           =F421 F422 =8CZ(HT)
                                                                                 008530
   WHERE GCZ IS THE GAIN MATRIX THAT ACTS DIRECTLY ON THE MEASUREMENT 003560 VECTOR. AND GCX IS THE GAIN MATRIX THATS ACTS ON THE CONTROLLER 0C4576 STATE ESTIMATES. *****THESE MUST BE SUPPLIED BY THE GAIN MATRIX GJ3560
                                                                                  035603
C***FORH FA
                                                                                 008510
      NOIN1= NSAV1+1
                                                                                 008629
       NOIMENSAV1
                                                                                 208533
C
                                                                                 309663
```

سراء والمستحدد من المنافق الم	
	0136
	3085
	0235
	0136
	3387
	3187
	9687
	0657
HRITE(KOUT, ") 'ST AND 3M ARE NOT THE SAME SIZE- WILL CAUSE ERRORS'	
ENO IF	3637
	3387
HMZ=FA12 IRFT XIRFP	9087
	0087
NOT N2#/ISAV 1	8887
	0088
: WMA= (FA11 FA12)	0165
CALL MATI(8CZ.HT, IRFM, IRHT, IFFT, WM1)	G 25 5
	0083
CALL AUGHAT (WH1, FC, WH8, IFCRM, IRFM, IRFM, IRFM, IRFM)	0388
	0084
	33830
1FUR7=6	0683
IPF4=IRFT+IRFM	0085
ICFA=1RFA	06839
CALL AUGMAT(MMA, MME, FA, IFORF, IRFT, IRFT, IRFM, ICFA)	0389
nous inc augmenteu p maikly pa 12.	3489
CALL MMATIO(FA. IRFA. IRFA. IG. KIN. KOUT, NSAV3. NSAV3)	22492
ra inca a inca	8689
	0359
FORM BA FOR REGULATOR CASE , NOT REQUIRED Y=G CALL MAT1(ST,GCY,1RFT,ICST,IRY,WM1)	5083
CALL MATI(ST,GCY,IRFT,ICST,IRY,WM1)	6:39
HMI= ST (GCY) IRFT X IRY	9359
	006 30
	96839
	6230
MORE, LUE WORLSHIED & LELVIN 40°17.	0 19 1
	0093
	3393
	33934
	31939
	0090
	00957
	0090
· · · · · · · · · · · · · · · · · · ·	33939
	0091
while different total total terminals and the second secon	0091
to the control of the	3031
	3091
	36919
nomes and aggregation continuous statement for STS STS	4021
THE TOTAL TOUGHT ATTION A SKRITTER	3891
00 3301 TC=1.730	3091
	03919
CALL AUGMATIMMI ACTAUMD TERABATOEM AGITAEM TAMTI	0392
MMD=(0 RC7) TRFM X TRO-TOHT	2292
	0092
T\$02 Ms 2	0092
100 M 3 - 100 A 11 3	0492
CALL AUGHATING. HMG.GA. TEGAL TOEL TOEL TOEL TOEAL	0492
	0392
	03927
	0092
	33529
	1192
CHMC= (GT 3T(GCZ)) 19FT X 1RMT+1FQ 00 3331 1R=1,1RFM 00 3301 IC=1,1RQ 3001 WH1(IR,IC)=0 CALL AUGMAT(WM1,8CZ,WM0,1FORP,1RFM,1RR,1RFM,1RMT) CHMO=(Q 3GZ) 1RFM X 1RQ+1RHT ICSA=1RG+1RHT IFORM=2 NOIM2=NSAV3 CALL AUGMAT(WMC,WM0,GA,1FORP,1RFT,1CGA,1RFM,1CGA) MSG=* THE AUGMENTED G MATRIX GA , IS* CALL MYATIO(GA,1RFA,1CGA,10,KIM,KGUT,NSAV3,NSAV3) CGA 1RFA X 1CGA	

```
NOIMENSAVI
                                                                                  009310
      NDIY1= 45441+1
                                                                                  339320
       CALL MATI(GCZ, HT, ICST, IRMT, IAFT, WM2)
                                                                                  019330
                    ICST X IRFT
C HMZ= GCZ(HT)
                                                                                  329340
      IFORP=1
                                                                                  009350
      IVAZEESKION
      NOI MEENSAVE
                                                                                  019370
      CALL AUGHAT (MM2.GCX.GUA.IFORP.IC3T.IRFT,IC3M,IRFH)
                                                                                  C69 380
      MSG= "THE AUGMENTED MATRIX GUA IS"
                                                                                  609390
      CALL MMATID (GUA-ICBT-IRFA-IC-KIN-KGUT-MSAV3-MSAV3)
  GUA ICST X ISFA
                                                                                  239-10
C+++++AUGMENTED SYSTEM MATRICES NOW AVAILBLE FOR COMPUTATION
                                                                                  009420
                                                                                  009+30
      ILESNEMION
                                                                                  069440
      SVAZN=1MION
                                                                                  009450
      EVA? N=SMION
                                                                                  209163
      NOIM3=NSAV4
                                                                                  009-70
      ENO
                                                                                  009480
* DECK PERFAL
      SUBRCUTINE PERFAL (IRY. IFLGCZ, MX A, GCY. GUA. PX A, PXVA. IFLGSD.
                                                                                  009530
     1RA,GCZA,YO,EAT.INTGA.mmE.mmF.FUU,HM1,MUOUT.MXTOUT,PUOUT.PXTOUT,
                                                                                  039510
     AETNI, UH, XAMUA, NIHUA, XAMUH, NIHUA, XAMTXA, NIHTXA, XAMAXKI, NIMAXKI
     1 HV 3 - HV 41
                                                                                  004530
      CHARACTER 456-60
      REAL HM1 (NOIM, NOIM), EAT
                                                                                  209553
                                                                               ... 009560
     1 (NOIP2, NOIM2), INTGA (NOIM2, NDIM2), WHE(HOIM2, NOIM2),
     1WMF(NOIM2.NOIM2), WV3(NOIM2).WV4(NOIM2).
                                                                                  009573
          ,SHIGN) AVX4, (STIGN, SHIGN) AX4, (SMIGN) AXH
     INDIH2), MUCUT (NOIM), MX TOUT (NOIM), PX TOUT (NOIM), PUOUT (NOIM),
                                                                                  269590
          . (MIGN) XAHUM. (MIGN) A IHUM. (MIGN) XAMAXM. (MIGN) MIMAXM. (EMIGN).
                                                                                  009603
          PXTHIN(NOIM), PXTHAX(NOIM), PUHIN(NOIM), PUHAX(NOIM), GCZA
                                                                                  009613
          (NDIM2.HDIM2), RA(HDIM2, NDIM2), GUA(NDIM2, NDIM2), GCY(NDIM.
                                                                                _ 009620
          (SMION.SMION) ABTRI, (HIDN
                                                                                  009633
      INTEGER IFLGCZ
                                                                                  339643
      DIMENSION CON1(1), COM2(1)
                                                                                  009650
      REAL MU (NCIM) . PUU (NOIM2. NOIM2)
                                                                                 _109661
      COMMON /RATIM/ RATIME, DELTIM
     COMMON AND THE NA GIMS - NOTHS
                                                                                  069689
      COMMON /MAINZ/COMZ
                                                                                  09700
      COMMON /MAIN1/NOIM.NOIM1.COM1
      COMMON / INOU/ KIN, KOUT, KPUNCH
      DZK \ ZKULAN\ NOMNOO
      COMMON/PAINS/IGST, ICSM, ICFA, ICGA, ICGN, ICGT, ICGA, IRFA, IRFM, IRFT.
                                                                                  449734
     11241,1204.10.LQG.12+M.NUMOTS
                                                                                  009740
       MION SI VAZE
      NSAV Z=NOIM1
      NSAV 3= NOIHS
                                                                                  009770
                                                                                  009750
      45 10 4= NOI #3
                                                                                  169791
C++++PERFORMANCE ANALYSIS ROUTINE
                                                                                  009900
     THIS IS A CONTINUOUS TIME MEASUREMENT PERFCRHANCE ANALYSIS
                                                                                  003311
     ROUTINE FOR EVALUATING CONTINUOUS TIME CONTROL SYSTEMS DRIVEN BY COMBEC WHITE GAUSSIAN NOISE. IT COMPUTES THE MEAN AND COVARIANCE OF THEOLOGIST
      OF THE TRUTH MODEL STATES . THE CONTROLLER STATES, AND THE CONTROLS 0:9840
                     A SET OF AUGMENTED WATRICES IS USED TO DO THE
      GEYERATED.
                                                                                  0(995)
       CALCULATIONS --- Y= (XT USTA+) T. XA= (XT XM) T .. THE PERFCRMANCE 019860 ANALYSIS ROUTINE IS DEVELOPED IN A MASTERS THESES FOR AIR FORCE 009870
       INSTITUTE OF TECHNOLOGY BY ERIC LLCYD, TITLE 'RCBUST CONTROL
       SYSTEM DESIGH.
                                                                                  003390
                                                                                  009900
                                                                                  039313
C+++MXA.PXA CALCULATION--- THE MEAN AND COVARIANCE OF THE XA VECTOR
          FOUND USING SOLUTION FORES OF THE PROPAGATION EQUATORS
                                                                                  309933
        KLIENMAN ROUTINES ARE USED TO PROVIDE THE SOLUTIONS
                                                                                  119340
   IN THE FOLLOWING TWO EGS. THE FIRST OCCURRANCE OF FAA OR MAA IS THE JALUE AT TIME THOELTIM, THE SECOND ----AT TIME T
                                                                                  219953
                                                                                  369363
```

C	⊅x A= ≦4 Γ (PX 4) Ξ4 Γ Γ + EN T G 4	339973	
C	1KA=EAT (FXA) +INTBA	309983	
C	SEE DEFINITIONS BELCA FOR EAT , INTGA, INTEA	019995	
C		016389	
C	NCTE SINCE THIS PROGRAM CONSIDERS ONLY THE REGULATOR CASE.	015313	
C	Y- THE DESIRED INPUT- IS ASSUMED = ZERG	013320	
C		810330	
CCCC		313348	
C	MX40=(E(XO) C)T =(XO J)T E=THE EXPECTED VALUE OPERATOR	010150	
C	PXAG= PO 3	010763	
<u>c</u>) 3	01007C	
C		010380	
	EAT= EXP(FA TIME)	010393	
C		013103	
C	# BAD FOR DISCRETE SYSTEMS	013113	
C	INTGA: INT (EAT (GA) QA (GA T) EATT) FOR CONT TIME SYSTEMS	010123	
<u>C</u>	INTGA: INT(EAT(GA)QA(GAT)EATT) FOR CONT TIPE SYSTEMS # GDA(GD4)GDAT FOR DISCRETE TIPE SYSTEMS	010123	
Č	30, 30, 30, 30, 30, 30, 30, 30, 30, 30,	013143	
C.	LCOUNTED	010150	
•	IRN=NINT(PNTIME/OSLTIM)	013160	
	HRITE(KOUT, *) 'ENTER A : "IF YOU HANT NO PRINTS OF PAA, PUU, MAA,	313173	
	1 AND HU MATRICES DURING THE PERFORMANCE ANALYSIS. ELSE ENTER THE	010180	
	1 TIME INCREMENTS IN THIS RUN)>"	319200	
	1 NUMBER OF TIME INCREMENTS BETWEEN PRINTS (THERE ARE ", IRN," TOTAL 1 TIME INCREMENTS IN THIS RUN)>" READ (KIN, *) IPCNTL IF (IPCNTL.EQ.J) THEN IC=J ELSE IO=5 END IF DO 5013 IN=1,NSAV1 PHU (TN_TML=1	818213	
	IF (IPCNTL.EQ.J) THEN	313220	
	IC=4	010230	
	ELSE	110240	
	I0*5	013250	
	ENG IF	311250	
	00 5013 [N=1,NSAV1	110270	
	PUU(IN,IN) #3	111511	
	HU (IN) =0	010280 010290	
	MX AN IN (IN) = 3	313393	
	MARINIANA CONTRACTOR OF THE CO		
	MX 4 PAX (IN) = 0	310 310	
	D= (IN,IN) = 0 MU (IN) = 0 D= (IN) = 0 MIN (IN) = 0 D= (IN) XATA XATA XATA XATA XATA XATA XATA XAT	010320 010330	
	MUYIN(IY)=0	019343	
	C=(NI)XARUM	010350	
	PU AX(IN) = 0 PU NIN(IN) = 0	913300	
#40 T	PUHIN(IN)=0		
2003	CONTINUE	013383	
	WAITEROUT, *) 'ENTER THE NUMBER OF SAMPLE FERIOUS CESTRED BETWEEN	010 393	
	1 PLOT POINTS (MAX 1303 PLOT PCINTS) THERE ARE ', IRM, ' SAMPLE PERICO	313+86	
	IS REQUESTED FOR THIS FUND	319410	
	READ (KIN, +) IPLTPS	010-20	
	OELPLT=OELTIM*IPLTPS	010433	
	00 SGJJ ITLMP=1.IRM	310440	
C		010-50	
	IF (IC. EQ. 5) THEN JJ=ITLNP-1	313463	
	JJ=ITLNP-1	010470	
	IPHT=400(JJ.IPCNTL) IF((IPHT.EQ.J).OR.(ITLHP.EQ.IRN)) THEN	513480	
	IF(([PNT.EQ.]).OR.([TLMP.EQ.]EN)) THEN		
	TI 16= JJ*OELTIM WRITE(KOUT,*) *TIME= " *,TIME	212500	
	YS <u>G= '</u>	31352 <u>J</u>	
	CALL HATISIPA . 3.3.10. KIN. KCUT. NSA 43.4383)	010533	M
	MSG= * PUU *	010540	
	CALL MMATIO(PUU.IC3M.IC3M.IC,KIN,KOUT,NSAV3,NSAV3)	010550	
		010560	
	MSG="NXA" CALL M/ECIO(MXA,3,10,KIN,KGUT,NSAV3)	010573	M
	MSG= *4U *	313583	
	CALL MVECIO(MU.ICAM.IO. KIN.KOUT.NSAV1)	213598	
	190 IF	013633	
	ENO IF	012513	
C	TO STORE FOR PLOTTING, MXT.PXY.MU.PUU	315623	

		OC 123 lW-=1.7	5:063∏ — №
		M> TÜÜT (Iwa) =4) 4 (Iwa)	1164
		FXTUUT(INA)=SQRT(PX4(INA, INA))	
	123	CGNTINUE	210563
		DO 124 IWR=1.ICBM	010670
	1	MUOUT(IAR)=MU(IAR)	013583
-		personal and the contract of t	· · · · · · · · · · · · · · · · · · ·
		POOTEIR; SQRIFOOTING INCI	61869] — M
		CONTINUE	81676
	Conser	•••	C10710
	C++++	NO CROSS CORPELATION TERMS ARE PLOTTED	01072:
	č		
			016733
			<u>0,10743</u>
		IPTCTL=HOO(JJ,IPLTPS)	010750
			013765
		I.a. Taalalattii ilalai alka oo oo oo oo oo aka ahaa ahaa ka oo oo oo aa	
			010773 - M
			016783
		LCOUNT=LCOUNT+1	816793
	i	END IF	013830
			613816
		ar in regionary and the region of the second se	019523
			610830
	C RESE	T LCCUNT	210943
		Carried Control of the control of th	010850
_		END IF	010863
		DATE PX 4, MX A	G10873
	C		610583
	C		010893
	-		
			010900
	- 1	NOIH1=NSAV3+1	010913
	(CALL MATS (IRFA, IRFA, EAT, PKA, NME)	619923
_		C1=1.0	01693)
	ì	CALL MARRATTER. TEEL LMS THTEA.BVA.C4)	0.000
		CALL MADD1(IRFA,IRFA, ME, INTGA,PXA,C1) A AT NEW TIME NOW AVAILABLE	040746
	CPX	A AT NEW TIME NOW AVAILABLE	010950
	C MX A:	= EAT(M)AG)+1NTEG(EAT(BA))(YD)	010963
	1	DO 1614 IK=1.IRFA	010970
		NV 3 (TK) = 3	816982
_			
		00 1815 IX=1,IRFA	010993
		DG 1815 IJ=1,IRFA	811365_
	1815	DG 1815 IJ=1,IRFA HV3(IK)=HV3(IK)+EAT(IK,IJ)*HXA(IJ) DG 1812 IMR=1.IFFA	011316
		DC 1812 IMR=1.IFFA	611620
		File File File File File File File File	
			011335
_			611343_
			611250
	C+++HX		
	C444411	PINI CALCILLATION FOR TERM MEAN MEASUREMENT NOTES	
			811375
		TO THE STATE OF THE SERVICES AND THE SERVICES OF THE SERVICES	011370
	—— · · · ·	A AT NEW TIME NOW AVAILABLE PUU CALCULATION FOF ZERO MEAN MEASUREMENT NOISE EGUA(MXA)+GCZ(MVT)+GCY(YD)PVT ,TME MEAN OF NOISE V ASSUMED +0	
		X1=YO(LCOUNT)	011370 011983 011393
		X1=YO(LCOUNT)	
		X1=Y0(LCOUNT) NDIM=NSAV1	011292 C11100
		X1=Y0(LCOUNT) NDIM=NSAV1	011293 C11100 011113
		X1=YO(LCOUNT) NDIM=NSAV1 NDIM=NSAV1+1 CALL MSCALE(HM1,GCY,IC9M,IRY,X1)	011292 C11100 011112 011123
-	C WH1=	X1=YO(LCOUNT) NDIM=NSAV1 NDIM=NSAV1+1 CALL MSCALE(WM1.GCY.IC9M.IRY.X1) GCY(YD IC8M X 1	011393 611100 011112 011123 511133
	C WM1=	X1=YO(LCOUNT) NDIM=NSAV1 NDIM=NSAV1+1 CALL MSCALE(MM1.GCY.IC3M.IRY.X1) GCY(YD ICBM X 1	011292 C11100 011112 011123
	C WM1=	X1=YO(LCOUNT) NDIM=NSAV1 NDIM=NSAV1+1 CALL MSCALE(MM1.GCY.IC3M.IRY.X1) GCY(YD ICBM X 1	011090 C11100 011110 011120 C11130 C11140
-	C WM1=	X1=YO(LCOUNT) NDIM=NSAV1 NDIM=NSAV1+1 CALL MSCALE(MM1.GCY.IC3M.IRY.X1) GCY(YD ICBM X 1	011292 C11100 011112 011122 C11133 C11140 C11153
-	C WH1=	X1=Y0(LCOUNT) NDIM=NSAV1 NDIM=NSAV1+1 CALL MSCALE(WM1.GCY.IC9M.IRY.X1) GCY(YD ICBM X 1 NDIM=NSAV3 NDIM1=NSAV3+1 DO 1817 IJ=1.ICBM	011292 C11100 011112 011122 C11132 C11140 011152
	C WH1=	X1=Y0(LCOUNT) NDIM=NSAV1 NDIM=NSAV1+1 CALL MSCALE(WM1.GCY.IC9M.IRY.X1) GCY(YD ICBM X 1 NDIM=NSAV3 NDIM=NSAV3+1 DO 1817 IJ=1.ICBM	011292 C11100 011112 011122 C11132 C11140 C11152 011162
-	C WH1=	X1=Y0(LCOUNT) NDIM=NSAV1 NDIM=NSAV1+1 CALL MSCALE(WM1.GCY.IC9M.IRY.X1) GCY(YD ICBM X 1 NDIM=NSAV3 NDIM=NSAV3+1 DO 1817 IJ=1.ICBM WV3(IJ)=Q DO 1816 IJ=1.ICBM	011292 C11100 011112 011122 C11132 C11140 011152
	C WH1=	X1=Y0(LCOUNT) NDIM=NSAV1 NDIM=NSAV1+1 CALL MSCALE(WM1.GCY.IC9M.IRY.X1) GCY(YD ICBM X 1 NDIM=NSAV3 NDIM=NSAV3+1 DO 1817 IJ=1.ICBM WV3(IJ)=Q DO 1816 IJ=1.ICBM	011292 C11100 011112 011122 C11132 C11140 C11152 011162 C11172 G11186
	C WM1=	X1=YO(LCOUNT) NDIM=NSAV1 NDIM=NSAV1+1 CALL MSCALE(MM1.GCY.IC9M.IRY.X1) GGY(YD ICBM X 1 NDIM=NSAV3 NDIM=NSAV3+1 DO 1817 IJ=1,ICBM NV3(IJ)=G DO 1816 IJ=1,ICBM	011292 C11100 011112 011122 C11133 C11140 C11153 011162 C11173 C11186 C11193
	C WH1=	X1=YO(LCOUNT) NDIM=NSAV1 NDIM=NSAV1+1 CALL MSGALE(MM1.GCY.IC9M.IRY.X1) GGY(YD ICBM X 1 NDIM=NSAV3 NDIM=NSAV3+1 DO 1817 IJ=1.ICBM NV3(IJ)=G DO 1816 IJ=1.ICBM DO 1816 IK=1.ICBM NV3(IJ)=HV3(IJ)+GUA(IJ.IK)*PX4(IK)	011292 C11100 011112 C11122 C11132 C11140 C11155 C11160 C11172 C11160 C11191 C11191
	C WH1=	X1=YO(LCOUNT) NDIM=NSAV1 NDIM=NSAV1+1 CALL MSGALE(MM1.GCY.IC9M.IRY.X1) GGY(YD ICBM X 1 NDIM=NSAV3 NDIM=NSAV3+1 DO 1817 IJ=1.ICBM NV3(IJ)=G DO 1816 IJ=1.ICBM DO 1816 IK=1.ICBM NV3(IJ)=HV3(IJ)+GUA(IJ.IK)*PX4(IK)	011292 C11100 011112 C11122 C11132 C11140 C11155 C11160 C11172 C11160 C11191 C11191
	C WH1=	X1=YO(LCOUNT) NDIM=NSAV1 NDIM=NSAV1+1 CALL MSGALE(MM1.GCY.IC9M.IRY.X1) GGY(YD ICBM X 1 NDIM=NSAV3 NDIM=NSAV3+1 DO 1817 IJ=1.ICBM NV3(IJ)=G DO 1816 IJ=1.ICBM DO 1816 IK=1.ICBM NV3(IJ)=HV3(IJ)+GUA(IJ.IK)*PX4(IK)	011292 C11100 011112 C11122 C11132 C11140 C11155 C11160 C11172 C11160 C11191 C11191
	C WH1=	X1=YO(LCOUNT) NDIM=NSAV1 NDIM=NSAV1+1 CALL MSGALE(MM1.GCY.IC9M.IRY.X1) GGY(YD ICBM X 1 NDIM=NSAV3 NDIM=NSAV3+1 DO 1817 IJ=1.ICBM NV3(IJ)=G DO 1816 IJ=1.ICBM DO 1816 IK=1.ICBM NV3(IJ)=HV3(IJ)+GUA(IJ.IK)*PX4(IK)	011292 C11100 011112 C11122 C11132 C11140 C11155 C11160 C11172 C11160 C11191 C11191
	C HM1= 1817 1816 C NV3= C AD	X1=YO(LCOUNT) NDIM=NSAV1 NDIM=NSAV1+1 CALL MSCALE(MM1.GCY.IC3M.IRY.X1) GCY(YD ICBM X 1 NDIM=NSAV3+1 DO 1817 IJ=1.ICBM MV3(IJ)=G DO 1816 IJ=1.ICBM DO 1816 IJ=1.ICBM MV3(IJ)=WV3(IJ)+GUA(IJ.IK)=PXA(IK) GUA(MXA) IC3M X 1 DED TO WM1 ABOVE TO GET MU DO 329 I=1.IC9M	011292 C11100 011112 011123 C11140 C11150 011160 C11170 C11180 C1119: 011202 G11213 C11229 C11233
	C HM1= 1817 1816 C HV3= C AD 329	X1=YO(LCOUNT) NDIM=NSAV1 NDIM=NSAV1+1 CALL MSCALE(MM1,GCY,IC3M,IRY,X1) GCY(YD ICBM X 1 NDIM=NSAV3+1 NDIM=NSAV3+1 DC 1817 IJ=1,ICBM NV3(IJ)=G DC 1816 IJ=1,ICBM DC 1816 IK=1,IRFA NV3(IJ)=HV3(IJ)+GUA(IJ,IK)=PXA(IK) GUA(MXA) IC3M X 1 DED TO WM1 ABOVE TO GET MU DO 329 I=1,IC3M MU(I)=HV3(I)+HM1(I,1)	011292 C11100 011112 011122 C11140 C11152 011160 C11170 C11180 C1119: 011202 C11213 C11229 C11233 C11243
	1817 1816 C PV3= C AD	X1=YO(LCOUNT) NDIM=NSAV1 NDIM=NSAV1+1 CALL MSCALE(MM1.GCY.IC9M.IRY.X1) GCY(YD ICBM X 1 NDIM=NSAV3 NDIM=NSAV3+1 DO 1817 IJ=1.ICBM NV3(IJ)=G DO 1816 IJ=1.ICBM DO 1816 IK=1.ICBM DO 1816 IK=1.ICFA NV3(IJ)=NV3(IJ)+GUA(IJ.IK)*PXA(IK) GUA(MXA) IC9M X 1 DED TO MM1 ABOVE TO GET MU DO 329 I=1.IC9M HU(I)=MV3(I)+MM1(I.1) IRFA X 1NOM AVAILABLE	011292 C11100 011112 011122 C11132 C11140 C11152 011160 C11172 G1118C C1119: 01120: 011213 C11229 C11233 011243
_	1817 1816 C MV3= C AD 329 C MU C+++PU	X1=YO(LCOUNT) NDIM=NSAV1 NDIM=NSAV1+1 CALL MSCALE(MM1.GCY.IC9M.IRY.X1) GCY(YD ICBM X 1 NDIM=NSAV3 NDIM=NSAV3+1 DO 1817 IJ=1.ICBM NV3(IJ)=G DO 1816 IJ=1.ICBM DO 1816 IK=1.ICBM DO 1816 IK=1.ICFA NV3(IJ)=NV3(IJ)+GUA(IJ.IK)*PXA(IK) GUA(MXA) IC9M X 1 DED TO MM1 ABOVE TO GET MU DO 329 I=1.IC9M HU(I)=MV3(I)+MM1(I.1) IRFA X 1NOM AVAILABLE	011292 C11100 011112 011122 C11140 C11152 011160 C11170 C11180 C1119: 011202 C11213 C11229 C11233 C11243
	1817 1816 C MV3= C AD 329 C MU C+++PU	X1=YO(LCOUNT) NDIM=NSAV1 NDIM=NSAV1+1 CALL MSCALE(MM1,GCY,IC3M,IRY,X1) GCY(YD ICBM X 1 NDIM=NSAV3+1 NDIM=NSAV3+1 DC 1817 IJ=1,ICBM NV3(IJ)=G DC 1816 IJ=1,ICBM DC 1816 IK=1,IRFA NV3(IJ)=HV3(IJ)+GUA(IJ,IK)=PXA(IK) GUA(MXA) IC3M X 1 DED TO WM1 ABOVE TO GET MU DO 329 I=1,IC3M MU(I)=HV3(I)+HM1(I,1)	011292 C11100 011112 011122 C11132 C11140 C11152 011162 C11172 G1118C C11192 O11202 C11213 C11220 C11223 C112243 O11243 O11268
	1817 1816 C MV3= C AD 329 C MU C+++PUIC	X1=YO(LCOUNT) NDIM=NSAV1 NDIM=NSAV1+1 CALL MSCALE(HM1,GCY,IC3M,IRY,X1) GCY(YD ICBM X 1 NDIM=NSAV3+1 NDIM=NSAV3+1 DO 1817 IJ=1,ICBM NV3(IJ)=G DO 1816 IJ=1,ICBM NV3(IJ)=HV3(IJ)+GUA(IJ,IK)*PXA(IK) GUA(MXA) IC3M X 1 DED TO MM1 ABOVE TO GET MU DO 329 I=1,IC3M MU(I)=HV3(I)+HM1(I,1) IRFA X 1NOM AVAILABLE U CALCULATICN,PUU=GUA(PXA)GUAT+GUA(PXVA)GCZT+GCZ(PXVA)GUAT+	011292 C11100 011112 011123 C11140 C11152 011160 C11170 G11180 C1119: 011203 C11213 C11229 C11229 C11233

STATE AND STATE OF ST

C PUU=GU4(PA4)GU4T ISEM X ICEM	J11290
C****** IFLSC Z*****	011360
IF (IFLGCZ.EQ.3) THEK	C 11 311
C SINCE GCZ NOT EQUAL TO ZERO CALCULATE OTHER TERMS OF PUU	011329
Coooco I FL GC Zoooco	511335
IF (IFLGSD.EQ.J) THEN	611345
C DUNT DO THIS FOR S-D CASE	311350
GALL MATI (GUA .PAVA.ICEM .IRFA.; RHT. H MF)	611363
CALL MATE (MMF.GCZA, ICEM, IRMT.ICEM, MME)	011376
C1=1.7	011380
CALL MADDITICAM. ICAM. FUU. ME. WHE. C1)	011393
P MMEGENA PRABENTACINA PROVINCENT	044.35
C HIF-GUA (PX A) GU AT+GUA (PX VA) GCZ T	011-03
	611416
GALL MAT- (PW .GUA .ICOM. IRFA .ICOP. WHE)	011420
CALL MADD1 (IC EM . IC EM . MRE . MMF . FUU . C1)	011430
	811-40
END IF	011450
CALL MATS(ICOM, IRMT.GCZA, RA.WME)	011160
A I WAR A A PARTY TOLONY THE BUT THE B	C11460
CALL MADDICE BY LICEN AND AND AND AND AND AND AND AND AND AN	011-70
CALL EQUATE(PUU.wnf,IC3m,IC3p)	G1148C
END IF	011490
	011500
C	011516
C	011520
	011530
SGOC CONTINUE	C 11 543
00 126 IHP=1.7	311550
MATOUT (IMR) =MXA(IMR)	
	011 70.
12G PX TOUT (IMR) = SQRT (PXA (IMR, IMR))	611570
00 121 IHR=1.ICBM	011583
MICHITY ASSEMIATES	C11595
494 BURNITING TO BROWN AT UR TO MELL	
121 FUOUT(IHR)=SORT(FUU(IHR,IHR))	011606
CALL STORED(LOG,RNTIME,DELTIM,LCOUNT,7,7,ICBM,ICBM,	611613
1 MYTCHT.PXTCHT.MUCHT.PHOUT.ANTHA)	
121 PUDUT(IMR) = SORT (PUU(IMR, IMR)) CALL STORED (LOG, ENTIME, DEL TIP, LCOUNT, 7, 7, ICBM, ICBM, 1 MYTOUT, PYTOUT, MUOUT, PUDUT, NOIME)	011620
C CALL TO STORED WITH LCOUNT & TINDICATE THIS DATA RUN COMPLETE	011620 011530
C CALL TO SYCRED WITH LCOUNT & 3 INDICATE THIS DATA RUN COMPLETE LCOUNT=-12	011620 011530 011640
C CALL TO SYCRED WITH LCOUNT & 9 INDICATE THIS DATA RUN COMPLETE LCOUNT=-12 CALL STORED (LOG. R NTIME DELTIP LCOUNT - 7 - 7 - 1 CRM -	011620 011530 011640
C CALL TO SYCRED WITH LCOUNT & 9 INDICATE THIS DATA RUN COMPLETE LCOUNT=-12 CALL STORED (LOG. R NTIME DELTIP LCOUNT - 7 - 7 - 1 CRM -	011620 011530 011640 011650
C CALL TO SYCRED WITH LCOUNT 4 3 INDICATE THIS DATA RUN COMPLETE LCOUNT=-12 CALL STORED (LOG, RNTIME, DELTIP, LCOUNT, 7, 7, 108M, 1	011620 011530 011640 011650 011660
C CALL TO SYCRED WITH LCOUNT 4 3 INDICATE THIS DATA RUN COPPLETE LCOUNT=-12 CALL STORED (LOG, RNTIME, DELTIP, LCOUNT, 7, 7, 108M, 108M, 1 MXTOUT, PXTOUT, MUOUT, PUOUT, NDIME) NOIM=MSAV1	011620 011530 011640 011650 011670
C CALL TO SYCRED WITH LCOUNT 4 3 INDICATE THIS DATA RUN COMPLETE LCOUNT=-12 CALL STORED (LOG, RNTIME, DELTIP, LCOUNT, 7, 7, 108M, 1	011620 011530 011640 011650 011660
C CALL TO SYCRED WITH LCOUNT < 3 INDICATE THIS DATA RUN COPPLETE LCOUNT=-12 CALL STORED (LOG, RNTIME, DELTIP, LCOUNT, 7, 7, 108M, 108M, 108M, 1 MXTOUT, PXTOUT, MUOUT, PUOUT, NDIME) NOIM=MSAV1 NOIM1=MSAV2	011620 011530 011643 011650 011663 011670
C CALL TO SYCRED WITH LCOUNT < 3 INDICATE THIS DATA RUN COPPLETE LCOUNT=-12 CALL STORED(LOG, RNTIME, DELTIP, LCOUNT, 7, 7, 108M, 108M, 108M, 1 MXTOUT, PXTOUT, MUOUT, PUOUT, NDIM6) NDIM=MSAV1 NDIM1=MSAV2 NDIM2=MSAV3	011620 011530 011643 011650 011663 011670 011640 011590
C CALL TO SYCRED WITH LCOUNT < 3 INDICATE THIS DATA RUN COPPLETE LCOUNT=-12 CALL STORED(LOG, RNTIME, DELTIP, LCOUNT, 7, 7, 108M, 108M, 108M, 1 MXTOUT, PXTOUT, MUOUT, PUOUT, NDIM6) NDIM=MSAV1 NDIM=MSAV2 NDIM=MSAV3 NDIM=MSAV4	011620 011530 011640 011660 011670 011640 011590
C CALL TO SYCRED WITH LCOUNT < 3 INDICATE THIS DATA RUN COMPLETE LCOUNT=-12 CALL STORED(LOG, RNTIME, DELYIP, LCOUNT, 7, 7, 108M, 10	011620 011530 011643 011650 011663 011670 011680 011590 011705
C CALL TO SYCRED WITH LCOUNT 4 3 INDICATE THIS DATA RUN COPPLETE LCOUNT=-12 CALL STORED(LOG,RNTIME,DELTIP,LCOUNT,7,7.1CBM,ICBM, 1	011620 011530 011640 011660 011670 011640 011590
C CALL TO SYCRED WITH LCOUNT < 3 INDICATE THIS DATA RUN COMPLETE LCOUNT=-12 CALL STORED(LOG, RNTIME, DELYIP, LCOUNT, 7, 7, 108M, 10	011620 011630 011643 011650 011663 011670 011680 011690 011705 011713
C CALL TO SYCRED WITH LCOUNT & SINDICATE THIS DATA RUN COMPLETE LCOUNT=-12 CALL STORED(LOG, RNTIME, DELTIP, LCOUNT, 7, 7, 108M, 108M, 1	011620 011530 011640 011660 011670 011680 011590 011700 011710
C CALL TO SYCRED WITH LCOUNT 4 3 INDICATE THIS DATA RUN COPPLETE LCOUNT=-12 CALL STORED(LOG,RNTIME,DELTIP,LCOUNT,7,7.1CBM,ICBM, 1	011620 011530 011640 011660 011670 011680 011590 011790 011710 011720 011740
C CALL TO SYCRED WITH LCOUNT & SINDICATE THIS DATA RUN COMPLETE LCOUNT=-12 CALL STORED(LOG, RNTIME, DELTIP, LCOUNT, 7, 7, 108M, 108M, 1	011630 011645 011665 011670 01160 01160 01170 011715 011720 011730 011740 011750
C CALL TO SYCRED WITH LCOUNT 4 3 INDICATE THIS DATA RUN COPPLETE LCOUNT=-12 CALL STORED(LOG,RNTIME,DELTIP,LCOUNT,7,7.1CBM,ICBM, 1	011620 011530 011640 011660 011670 011680 011590 011790 011710 011720 011740
C CALL TO SYCRED WITH LCOUNT & 3 INDICATE THIS DATA RUN COPPLETE LCOUNT=-12 CALL STORED (LOG, RNTIME, DELTIP, LCOUNT, 7, 7, 1CBM, 1CBM, 1 MXTOUT, PXTOUT, MUOUT, PUOUT, NDIME) NDIM=MSAV1 NDIM=MSAV2 NDIM3=MSAV4 C RESET IO TO SOME NONZED VALUE TO AVOID TERMINATING THE PROGRAM C MMEN RETURNING TO MAIN ROUTINE, LOGRP 10=25 END DECK MYPLOT SUB.CUTINE MYPLOT	011630 011645 011663 011670 01160 01170 011720 011730 011730 011740 011753
C CALL TO SYCRED WITH LCOUNT & 3 INDICATE THIS DATA RUN COPPLETE LCOUNT=-12 CALL STORED(LOG,RNTIME,DELTIP,LCOUNT,7,7.1CBM.ICBM. 1 MXTOUT.PXTOUT,MUOUT.PUOUT,NDIME) NDIM=MSAV1 NDIM=MSAV2 NDIM2=MSAV3 NDIM3=MSAV4 C RESET IO TO SOME NONZED VALUE TO AVOID TERMINATING THE PROGRAM C MHEN RETURNING TO MAIN ROUTINE. LOGRP IO=25 END * DECK MYPLOT SUB.CUTINE MYPLOT	011620 011530 011640 011660 01160 01170 011710 011720 011720 011740 011750 011775
C CALL TO SYCRED WITH LCOUNT & 3 INDIGATE THIS DATA RUN COPPLETE LCOUNT=-12 CALL STORED (LOG, RNTIME, DELTIP, LCOUNT, 7, 7, ICBM, ICBM, 1	011630 011643 011663 011663 011660 01160 01170 01173 01173 01173 01175 01175 01175
C CALL TO SYCRED WITH LCOUNT & 3 INDICATE THIS DATA RUN COPPLETE LCOUNT=-12 CALL STORED(LOG,RNTIME,DELTIP,LCOUNT,7,7.1CBM.ICBM. 1 MXTOUT.PXTOUT,MUOUT.PUOUT,NDIME) NDIM=MSAV1 NDIM=MSAV2 NDIM2=MSAV3 NDIM3=MSAV4 C RESET IO TO SOME NONZED VALUE TO AVOID TERMINATING THE PROGRAM C MHEN RETURNING TO MAIN ROUTINE. LOGRP IO=25 END * DECK MYPLOT SUB.CUTINE MYPLOT	011630 011645 011665 011660 01160 01170 011730 011725 011740 011750 011775 011775 011775
C CALL TO SYCRED WITH LCOUNT & 3 INDIGATE THIS DATA RUN COPPLETE LCOUNT=-12 CALL STORED (LOG, RNTIME, DELTIP, LCOUNT, 7, 7, ICBM, ICBM, 1	011630 011645 011665 011660 01160 01170 011730 011725 011740 011750 011775 011775 011775
C CALL TO SYCRED WITH LCOUNT & 3 INDICATE THIS DATA RUN COMPLETE LCOUNT=-12 CALL STORED (LOG, RNTIME, DELTIP, LCOUNT, 7, 7, ICBM, ICBM, 1 MXTOUT, PXTOUT, MUOUT, PUOUT, NDIME) NDIM=MSAV1 NDIM=MSAV2 NDIM2=MSAV3 NDIM3=MSAV4 C RESET TO TO SOME NONZEDO VALUE TO AVOID TERMINATING THE PROGRAM C MHEN RETURNING TO MAIN ROUTINE, LOGRAM IO=25 END DECK MYPLOT SUB. GUTINE MYPLOT END DECK AUGMAT SUBRGUTINE AUGMAT (A1, A2, A3, IFORM, IRA1, IGA1, IRA2, ICA2) C	011630 011645 011665 011660 01160 01170 011720 011720 011750 011750 011775 011775 011775 011775
C CALL TO SYCRED WITH LCOUNT & 9 INDICATE THIS DATA RUN COPPLETE LCOUNT=-12 CALL STORED (LOG, RNTIME, DELTIP, LCOUNT, 7, 7, ICBM, ICBM, 1 MXTOUT, PXTOUT, MUOUT, PUOUT, NDIME) NDIM=MSAV1 NDIM=MSAV2 NDIM2=MSAV3 NDIM3=MSAV4 C RESET TO TO SOME NONZERO VALUE TO AVOID TERMINATING THE PROGRAM C MMEN RETURNING TO MAIN ROUTINE, LOGRAM IO=25 END DECK MYPLOT SUB. GUTINE MYPLOT END DECK AUGMAT SUBRGUTINE AUGMAT (A1, A2, A3, IFORM, IRA1, IGA1, IRA2, ICA2) C CNDIM2, NDIM3 MUST BE SET IN THEM CALLING PROGRAM BEFORE USING	011630 011645 011665 011660 011640 011640 011700 011730 011730 011750 011775 011775 011775 011775 011775
C CALL TO STORED WITH LCOUNT < 3 INDIGATE THIS DATA RUN COMPLETE LCOUNT=-12 CALL STORED(LOG, RNTIME, DELTIP, LCOUNT, 7, 7, 1CBM, 1CBM, 1 MATOUT, PXTOUT, MUOUT, PUOUT, NDIME) NDIM=MSAV1 NDIM=MSAV2 NDIM=MSAV4 C RESET TO TO SOME NONZEFO VALUE TO AVOID TERMINATING THE PROGRAM C MEN RETURNING TO MAIN ROUTINE, LOGRAM FORCK MYPLOT SUB-CUTINE MYPLOT END DECK AUGMAT SUB-CUTINE MYPLOT END C DECK AUGMAT SUB-CUTINE AUGMAT(A1, A2, A3, IFORM, IRA1, ICA1, IRA2, ICA2) C CNDIM2, NDIM3 MUST BE SET IN THEM CALLING PROGRAM BEFORE USING CNDIM2, NDIM3 MUST BE SET IN THE CALLING PROGRAM BEFORE USING	011620 011630 011662 011662 011660 011640 011790 011720 011730 011750 011763 011763 011763 011763 011763 011780 011780
C CALL TO SYCRED WITH LCOUNT & 9 INDICATE THIS DATA RUN COPPLETE LCOUNT=-12 CALL STORED (LOG, RNTIME, DELTIP, LCOUNT, 7, 7, ICBM, ICBM, 1 MXTOUT, PXTOUT, MUOUT, PUOUT, NDIME) NDIM=MSAV1 NDIM=MSAV2 NDIM2=MSAV3 NDIM3=MSAV4 C RESET TO TO SOME NONZERO VALUE TO AVOID TERMINATING THE PROGRAM C MMEN RETURNING TO MAIN ROUTINE, LOGRAM IO=25 END DECK MYPLOT SUB. GUTINE MYPLOT END DECK AUGMAT SUBRGUTINE AUGMAT (A1, A2, A3, IFORM, IRA1, IGA1, IRA2, ICA2) C CNDIM2, NDIM3 MUST BE SET IN THEM CALLING PROGRAM BEFORE USING	011630 011645 011665 011660 011640 011640 011700 011730 011730 011750 011775 011775 011775 011775 011775
C CALL TO SYCRED WITH LCOUNT & FINDICATE THIS DATA RUN COMPLETE LCOUNT=-12 CALL STORED(LOG,RNTIME, DELTIP, LCOUNT, 7, 7, 108M, 108M, 1 MATOUT, PATOUT, MUOUT, PUOUT, ADIMS) NOIM=MSAV1 NOIM=MSAV2 NOIM=MSAV3 NOIM=MSAV4 C RESET TO TO SOME NONZERO VALUE TO AVOID TERMINATING THE PROGRAM C MMEN RETURNING TO MAIN ROUTINE, LOGAP 10=25 END * DECK MYPLOT SUB-CUTINE MYPLOT ENO * DECK AUGMAT SUB-CUTINE AUGMAT(A1, A2, A3, 1FCRM, 1RA1, 1CA1, 1RA2, 1CA2) C C****NOIM2, NOIM3 MUST BE SET IN THEM CALLING PROGRAM BEFORE USING C****NOIM2, NOIM3 MUST BE SET IN THE CALLING PROGRAM BEFORE USING C****NOIM2, NOIM3 MUST BE SET IN THE CALLING PROGRAM BEFORE USING C****THIS SUBROUTINE. THEY PUST BE DECLARED IN A COMMON BLOCK	011630 011650 011660 011660 01160 01170 011720 011730 011750 0117750 0117750 0117750 0117750 0117750 0117750 0117750 0117750
C CALL TO STORED WITH LCOUNT - 7 INDICATE THIS DATA RUN COMPLETE LCOUNT=-12 CALL STORED(LOG,RNTIME,DELTIP, COUNT, 7,7.1CBM. ICBM. 1	011630 011650 011660 011660 01160 01170 011720 011730 011750 011775 011775 011775 011780 011780 011780 011780 011780
C CALL TO SYCRED WITH LCOUNT & TINDIGATE THIS DATA RUN COMPLETE LCOUNT=-12 CALL STORED(LOG, RNTIME, DELTIP, LCOUNT, 7, 7, ICBM, ICBM, 1 MATOUT, PATOUT, MUOUT, PUOUT, ADIMS) NDIM=MSAV1 NDIM=MSAV3 NDIM=MSAV4 C RESET TO TO SOME NONZEDO VALUE TO AVOID TERMINATING THE PROGRAM C MEN RETURNING TO MAIN ROUTINE, LOGAP IC=25 END DECK MYPLOT SUB. CUTINE MYPLOT END DECK AUGMAT SUBRCUTINE AUGMAT(A1, A2, A3, IFCRM, IRA1, ICA1, IRA2, ICA2) C SOME COUTINE MYPLOT COMMON MUST BE SET IN THEM CALLING PROGRAM BEFORE USING COMMON MUST BE SET IN THE CALLING PROGRAM BEFORE USING COMMON MUST BE SET IN THE CALLING PROGRAM BEFORE USING COMMON BLOCK C LABELEDMAIN4 DECK MYECIO	011630 011650 011660 011660 01160 011710 011720 011730 0117750 0117750 0117750 0117750 011780 011780 011780 011780 011780 011780
C CALL TO STORED WITH LCOUNT - INDIGATE THIS DATA RUN COMPLETE LCOUNT=-12 CALL STORED(LOG,RNTIME,DELYIP,LCOUNT,7,7,ICBM,ICBM, 1 MATOUT,PXTOUT,MUOUT,PUOUT,NDIME) NDIM=MSAV1 NDIM=MSAV2 NDIM2=MSAV3 NDIM3=MSAV4 C RESET IO TO SOME NONZERO VALUE TO AVOID TERMINATING THE PROGRAM C HHEN RETURNING TO MAIN ROUTINE, LOGRP 10=25 END DECK MYPLOT SUB-GUTINE MYPLOT END DECK AUGMAT SUB-GUTINE AUGMAT(A1,A2,A3,IFORM,IRA1,ICA1,IRA2,ICA2) C SOME NOIME, NOIME MUST BE SET IN THEM CALLING PROGRAM BEFORE USING COMMON NOIME MUST BE SET IN THE CALLING PROGRAM BEF	011630 011650 011660 011660 01160 01170 011720 011730 011750 011775 011775 011775 011780 011780 011780 011780 011780
C CALL TO SYCRED WITH LCOUNT & TINDIGATE THIS DATA RUN COMPLETE LCOUNT=-12 CALL STORED(LOG, RNTIME, DELTIP, LCOUNT, 7, 7, ICBM, ICBM, 1 MATOUT, PATOUT, MUOUT, PUOUT, ADIMS) NDIM=MSAV1 NDIM=MSAV3 NDIM=MSAV4 C RESET TO TO SOME NONZEDO VALUE TO AVOID TERMINATING THE PROGRAM C MEN RETURNING TO MAIN ROUTINE, LOGAP IC=25 END DECK MYPLOT SUB. CUTINE MYPLOT END DECK AUGMAT SUBRCUTINE AUGMAT(A1, A2, A3, IFCRM, IRA1, ICA1, IRA2, ICA2) C SOME COUTINE MYPLOT COMMON MUST BE SET IN THEM CALLING PROGRAM BEFORE USING COMMON MUST BE SET IN THE CALLING PROGRAM BEFORE USING COMMON MUST BE SET IN THE CALLING PROGRAM BEFORE USING COMMON BLOCK C LABELEDMAIN4 DECK MYECIO	011630 011650 011660 011660 01160 011710 011720 011730 0117750 0117750 0117750 0117750 011780 011780 011780 011780 011780 011780
C CALL TO STORED WITH LCOUNT < 7 INDIGATE THIS DATA RUN COMPLETE LCOUNT=-12 CALL STORED(LOG,RNTIME,DELTIP,LCOUNT,7,7,ICBH,ICBH, 1 MATOUT,PXTOUT,MUOUT,PUOUT,NDIME) NDIM=MSAV1 NDIM1=MSAV2 NDIM2=MSAV3 NOIM3=MSAV4 C RESET IO TO SOME NONZEDO VALUE TO AVOID TERMINATING THE PROGRAM C MHEN RETURNING TO MAIN ROUTINE, LOGRP 10=25 END DECK MYPLOT SUB-CUTINE MYPLOT END DECK AUGMAT SUB-GUTINE AUGMAT(A1,A2,A3,IFORM,IRA1,ICA1,IRA2,ICA2) C ***********************************	011630 011650 011660 011660 011770 011730 0117730 0117750 0117750 0117750 011760 011760 011863 011863 011863 011873
C CALL TO SYCRED WITH LCOUNT < 7 INDICATE THIS DATA RUN COMPLETE LCOUNT==12 CALL STORED(LOG,RNTIME,DELTIP,LCOUNT,7,7.ICBM,ICBM, 1 MATOUT,PATOUT, MUOUT, PUOUT, NDIME) NOIM=MSAV1 NOIM=MSAV2 NOIM2=MSAV3 NOIM3=MSAV4 C RESET TO TO SOME NONZERO VALUE TO AVOID TERMINATING THE PROGRAM C MHEN RETURNING TO MAIN ROUTINE, LOGAP 10=25 END DECK MYPLOT SUB. CUTINE MYPLOT END DECK AUGMAT SUBRCUTINE AUGMAT (A1,A2,A3,IFORM,IRA1,ICA1,IRA2,ICA2) C CNOIMZ, NDIMS MUST BE SET IN THEM CALLING PROGRAM BEFORE USING CNOIMZ, NDIMS MUST BE SET IN THE CALLING PROGRAM BEFORE USING CNOIMZ, NDIMS MUST BE SET IN THE CALLING PROGRAM BEFORE USING CNOIMZ, NDIMS MUST BE SET IN THE CALLING PROGRAM BEFORE USING C LABELEDMAIN4 DECK MVECID C THIS SUBROUTINE. THEY PUST BE DECLARED IN A COMMON BLOCK C LABELEDMAIN4 DECK MVECID C THIS SUBROUTINE FORMS AUGMENTED MATRICES CF THE FORM C IFORM=1 A3=(A1 A2) C IFORM=2 A3=(A1 A2)	011630 011660 011660 011660 0117730 0117730 0117730 0117730 0117750 01175
C CALL TO STORED WITH LCOUNT < ? INDICATE THIS DATA RUN COMPLETE LCOUNTS-12 CALL STORED(LOG,RNTIME,DELYIP,LCOUNT,7,7,108M,108M, 1 MATOUT,PXTOUT,MUOUT,PUOUT,NDIME) NOIMSMAY NOIMSMAY NOIMSMAY NOIMSMAY NOIMSMAY NOIMSMAY C RESET IO TO SOME NONZEDO VALUE TO AVOID TERMINATING THE PROGRAM C MHEN RETURNING TO MAIN ROUTINE, LOGAP 10=25 END DECK MYPLOT SUB-CUTINE MYPLOT END COMMAN TO THE AUGMAT (A1,A2,A3,IFORM,IRA1.ICA1,IRA2,ICA2) C SUB-CUTINE AUGMAT (A1,A2,A3,IFORM,IRA1.ICA1,IRA2,ICA2) C COMMAN MUST BE SET IN THEM CALLING PROGRAM BEFORE USING COMMAN MUST BE SET IN THE CALLING PROGRAM BEFORE USING COMMAN MUST BE SET IN THE CALLING PROGRAM BEFORE USING COMMAN MUST BE SET IN THE CALLING PROGRAM BEFORE USING C LABELED -MAINA DECK MYECID C THIS SUBROUTINE FORMS AUGMENTED HATRICES OF THE FORM C IFORM=1 A3=(A1 A2) C IFORM=2 A3=(A1 A2)T	011630 011650 011660 011660 011770 011730 0117730 0117750 0117750 0117750 011760 011760 011863 011863 011863 011873
C CALL TO STORED WITH LCOUNT < ? INDICATE THIS DATA RUN COMPLETE LCOUNTS-12 CALL STORED(LOG,RNTIME,DELYIP,LCOUNT,7,7,108M,108M, 1 MATOUT,PXTOUT,MUOUT,PUOUT,NDIME) NOIMSMAY NOIMSMAY NOIMSMAY NOIMSMAY NOIMSMAY NOIMSMAY C RESET IO TO SOME NONZEDO VALUE TO AVOID TERMINATING THE PROGRAM C MHEN RETURNING TO MAIN ROUTINE, LOGAP 10=25 END DECK MYPLOT SUB-CUTINE MYPLOT END COMMAN TO THE AUGMAT (A1,A2,A3,IFORM,IRA1.ICA1,IRA2,ICA2) C SUB-CUTINE AUGMAT (A1,A2,A3,IFORM,IRA1.ICA1,IRA2,ICA2) C COMMAN MUST BE SET IN THEM CALLING PROGRAM BEFORE USING COMMAN MUST BE SET IN THE CALLING PROGRAM BEFORE USING COMMAN MUST BE SET IN THE CALLING PROGRAM BEFORE USING COMMAN MUST BE SET IN THE CALLING PROGRAM BEFORE USING C LABELED -MAINA DECK MYECID C THIS SUBROUTINE FORMS AUGMENTED HATRICES OF THE FORM C IFORM=1 A3=(A1 A2) C IFORM=2 A3=(A1 A2)T	011630 011660 011660 011660 0117730 0117730 0117730 0117730 0117750 01175
C CALL TO STORED WITH LCOUNT 3 INDICATE THIS DATA RUN COMPLETE LCOUNTS-12 CALL STORED(LOG,RNTIME,DELYIP,LCOUNT,7,7,ICBM,ICBM, 1 MATOUT,PXTOUT,MUOUT,PUOUT,NDIME) NOIMSMAY NOIMSMAY NOIMSMAY NOIMSMAY NOIMSMAY NOIMSMAY C RESET TO TO SOME NONZEDO VALUE TO AVOID TERMINAYING THE PROGRAM C MMEN RETURNING TO MAIN ROUTINE, LOGAP 10=25 ENO DECK MYPLOT SUB-CUTINE MYPLOT ENO DECK AUGMAT SUB-CUTINE AUGMAT(A1,A2,A3,IFORM,IRA1,IGA1,IRA2,ICA2) C CNOIMS,NOIMS MUST BE SET IN THEM CALLING PROGRAM BEFORE USING CNOIMS,NOIMS MUST BE SET IN THE CALLING PROGRAM BEFORE USING CNOIMS,NOIMS MUST BE SET IN THE CALLING PROGRAM BEFORE USING CNOIMS,NOIMS MUST BE SET IN THE CALLING PROGRAM BEFORE USING CNOIMS,NOIMS MUST BE SET IN THE CALLING PROGRAM BEFORE USING CNOIMS SUBROUTINE. THEY MUST BE DECLARED IN A COMMON BLOCK C LABELEDMAIN+ DECK MYECIO C THIS SUBROUTINE FORMS AUGMENTED MATRICES CF THE FORM C IFORM=1 A3=(A1 A2) C IFORM=2 A3=(A1 A2) C IFORM=2 A3=(A1 A2) C IFORM=2 A3=(A1 A2) C	011630 011660 011660 011660 011770 0117730 0117730 0117730 0117750 011750
C CALL TO SYCRED WITH LCOUNT 3 INDICATE THIS DATA RUN COMPLETE LCOUNT=-12 CALL STORED(LOG,RNTIME,DELTIP,LCOUNT,7,7.ICBM.ICBM. 1 MATOUT,PATOUT, MUOUT, PUOUT, NDIME) NOIM=MSAV1 NDIM=MSAV2 NDIM3=NSAV3 NDIM3=NSAV4 C RESET TO TO SOME NONZEDO VALUE TO AVOID TERMINATING THE PROGRAM C MMEN RETURNING TO MAIN ROUTINE, LOGAP 10=25 END DECK MYPLOT SUB.GUTINE MYPLOT CONDIM2,NDIM3 MUST BE SET IN THEM CALLING PROGRAM BEFORE USING CONDIM2,NDIM3 MUST BE SET IN THEM CALLING PROGRAM BEFORE USING CONDIM2,NDIM3 MUST BE SET IN THE CALLING PROGRAM BEFORE USING CONDIM2,NDIM3 MUST BE SET IN THE CALLING PROGRAM BEFORE USING CONDIM2,NDIM3 MUST BE SET IN THE CALLING PROGRAM BEFORE USING CONDIM2,NDIM3 MUST BE SET IN THE CALLING PROGRAM BEFORE USING CONDIM2,NDIM3 MUST BE SET IN THE CALLING PROGRAM BEFORE USING CONDIM2,NDIM3 MUST BE SET IN THE CALLING PROGRAM BEFORE USING CONDIM2,NDIM3 MUST BE SET IN THE CALLING PROGRAM BEFORE USING CONDIM2,NDIM3 MUST BE SET IN THE CALLING PROGRAM BEFORE USING CONDIM2,NDIM3 MUST BE SET IN THE CALLING PROGRAM BEFORE USING CONDIM2,NDIM3 MUST BE SET IN THE CALLING PROGRAM BEFORE USING CONDIM2,NDIM3 MUST BE SET IN THE CALLING PROGRAM BEFORE USING CONDIM2,NDIM3 MUST BE SET IN THE CALLING PROGRAM BEFORE USING CONDIM2,NDIM3 MUST BE SET IN THE CALLING PROGRAM BEFORE USING CONDIM2,NDIM3 MUST BE SET IN THE CALLING PROGRAM BEFORE USING CONDIM2,NDIM3 MUST BE SET IN THE CALLING PROGRAM BEFORE USING CONDIM2,NDIM3 MUST BE SET IN THE CALLING PROGRAM BEFORE USING CONDIM2,NDIM3 MUST BE SET IN THE CALLING PROGRAM BEFORE USING CONDIM3,NDIM3 MUST BE SET IN THE CALLING PROGRAM BEFORE USING CONDIM3,NDIM3 MUST BE SET IN THE CALLING PROGRAM BEFORE USING CONDIM3,NDIM3,NDIM3 MUST BE SET IN THE CALLING PROGRAM BEFORE USING CONDIM3,ND	011630 011663 011663 011660 0117730 0117730 0117730 0117730 0117753 011753
CALL TO SYCRED WITH LCOUNT 3 INDICATE THIS DATA RUN COMPLETE LCOUNT==12 CALL STORED(LOG,RNYIME, DELYIP, LCOUNT, 7,7, ICBM, ICBM, 1 MATOUT, PATOUT, MUDUT, PUOUT, NOIP6) NOIM=MSAV1 NDIM=MSAV2 NDIM3=NSAV3 NOIM3=NSAV4 C RESET TO TO SOME NONZEDO VALUE TO AVOID TERMINATING THE PROGRAM ID=25 END DECK MYPLOT SUB-CUTINE MYPLOT END DECK AUGMAT SUB-CUTINE AUGMAT (A1, A2, A3, IFCRM, IRA1, ICA1, IRA2, ICA2) C CONDIM2, NOIM3 MUST BE SET IN THEM CALLING PROGRAM BEFORE USING CONDIM2, NOIM3 MUST BE SET IN THE CALLING PROGRAM BEFORE USING CONDIM2, NOIM3 MUST BE SET IN THE CALLING PROGRAM BEFORE USING CONDIM2, NOIM3 MUST BE SET IN THE CALLING PROGRAM BEFORE USING CONDIM2, NOIM3 MUST BE SET IN THE CALLING PROGRAM BEFORE USING CONDIM2, NOIM3 MUST BE SET IN THEY PUST BE DECLARED IN A COMMON BLOCK C LABELEDMAIN4 DECK MYECID C THIS SUBROUTINE FCRMS AUGMENTED MATRICES CF THE FORM C IFORM=1 A3=(A1 A2) C IFORM=2 A3=(A1 A2) C IFAL:IRA2,ARE ROM DIMENSIONS,ICA1.ICA2,ARE COLUMN DIMENSIONS DIMENSION A1(NOIM2,NOIM2),A2(NOIM2,NOIM2),A3(NOIF3,NOIM3)	011650 011650 011660 011660 011710 0117730 0117730 0117730 0117780 011780
C CALL TO SYCRED WITH LCOUNT 3 INDICATE THIS DATA RUN COMPLETE LCOUNT=-12 CALL STORED(LOG,RNTIME,DELTIP,LCOUNT,7,7.ICBM.ICBM. 1 MATOUT,PATOUT, MUOUT, PUOUT, NDIME) NOIM=MSAV1 NDIM=MSAV2 NDIM3=NSAV3 NDIM3=NSAV4 C RESET TO TO SOME NONZEDO VALUE TO AVOID TERMINATING THE PROGRAM C MMEN RETURNING TO MAIN ROUTINE, LOGAP 10=25 END DECK MYPLOT SUB.GUTINE MYPLOT CONDIM2,NDIM3 MUST BE SET IN THEM CALLING PROGRAM BEFORE USING CONDIM2,NDIM3 MUST BE SET IN THEM CALLING PROGRAM BEFORE USING CONDIM2,NDIM3 MUST BE SET IN THE CALLING PROGRAM BEFORE USING CONDIM2,NDIM3 MUST BE SET IN THE CALLING PROGRAM BEFORE USING CONDIM2,NDIM3 MUST BE SET IN THE CALLING PROGRAM BEFORE USING CONDIM2,NDIM3 MUST BE SET IN THE CALLING PROGRAM BEFORE USING CONDIM2,NDIM3 MUST BE SET IN THE CALLING PROGRAM BEFORE USING CONDIM2,NDIM3 MUST BE SET IN THE CALLING PROGRAM BEFORE USING CONDIM2,NDIM3 MUST BE SET IN THE CALLING PROGRAM BEFORE USING CONDIM2,NDIM3 MUST BE SET IN THE CALLING PROGRAM BEFORE USING CONDIM2,NDIM3 MUST BE SET IN THE CALLING PROGRAM BEFORE USING CONDIM2,NDIM3 MUST BE SET IN THE CALLING PROGRAM BEFORE USING CONDIM2,NDIM3 MUST BE SET IN THE CALLING PROGRAM BEFORE USING CONDIM2,NDIM3 MUST BE SET IN THE CALLING PROGRAM BEFORE USING CONDIM2,NDIM3 MUST BE SET IN THE CALLING PROGRAM BEFORE USING CONDIM2,NDIM3 MUST BE SET IN THE CALLING PROGRAM BEFORE USING CONDIM2,NDIM3 MUST BE SET IN THE CALLING PROGRAM BEFORE USING CONDIM2,NDIM3 MUST BE SET IN THE CALLING PROGRAM BEFORE USING CONDIM2,NDIM3 MUST BE SET IN THE CALLING PROGRAM BEFORE USING CONDIM3,NDIM3 MUST BE SET IN THE CALLING PROGRAM BEFORE USING CONDIM3,NDIM3 MUST BE SET IN THE CALLING PROGRAM BEFORE USING CONDIM3,NDIM3,NDIM3 MUST BE SET IN THE CALLING PROGRAM BEFORE USING CONDIM3,ND	011630 011663 011663 011660 0117730 0117730 0117730 0117730 0117753 011753
CALL TO SYCRED WITH LCOUNT TO INDICATE THIS DATA RUN COMPLETE LCOUNTS-12 CALL STORED(LOG,RNYIME, DELYIP, LCOUNT, 7,7, ICBM, ICBM, 1 MATOUT, PATOUT, MUDUT, PUOUT, NOIP6) NOIMSANSAVI NDIMISANSAVI NDIMISANSAVI NDIMISANSAVI C RESET TO TO SOME NONZEDO VALUE TO AVOID TERMINATING THE PROGRAM ID-25 END DECK MYPLOT SUB. GUTINE MYPLOT END DECK AUGMAT SUBRCUTINE AUGMAT (A1, A2, A3, IFORM, IRA1, ICA1, IRA2, ICA2) C CONDIMIZ, NDIMIS MUST BE SET IN THEM CALLING PROGRAM BEFORE USING CONDIMIZ, NDIMIS MUST BE SET IN THE CALLING PROGRAM BEFORE USING CONDIMIZ, NDIMIS MUST BE SET IN THE CALLING PROGRAM BEFORE USING CONDIMIZ, NDIMIS MUST BE SET IN THE CALLING PROGRAM BEFORE USING CONDIMIZ, NDIMIS MUST BE SET IN THE CALLING PROGRAM BEFORE USING CONDIMIZ, NDIMIS MUST BE SET IN THE CALLING PROGRAM BEFORE USING CONDIMIZ, NDIMIS MUST BE SET IN THE CALLING PROGRAM BEFORE USING CONDIMIZ, NDIMIS MUST BE SET IN THE CALLING PROGRAM BEFORE USING C LABELEDMAINS DECK MYECID C THIS SUBROUTINE FCRMS AUGMENTED MATRICES CF THE FORM C IFORM=1 A3=(A1 A2) C IFORM=2 A3=(A1 A2) C IFORM=2, ARE ROM DIMENSIONS, ICA1, ICA2, ARE COLUMN DIMENSIONS DIMENSION A1(NDIM2, NDIM2), A2(NDIM2), A3(NDIF3, NDIM3)	011650 011650 011660 011660 011710 0117730 0117730 0117730 0117780 011780

M

```
C FORM THE AUSHENTED MATRIX 43=(41 42)
                                                                                 111950
       DC 12 II=1,1741
D0 11 III=1,1641
A3(II, III)=A1(II, III)
                                                                                $11961
                                                                                 211971
 11
                                                                                011350
       DG 12 IV=1.IC42
                                                                                011390
       IVI=IV+IC41
                                                                                 612303
       (VI,II) S4 = (IVI,II) EA
                                                                                 312310
       RETURN
                                                                                 612323
       END IF
                                                                                512336
 C FORM AUGHENTED MATRIX A3=(A1 A2)T
                                                                                £12340
       IFAJ=IRA1+IRA2
                                                                                012350
       ICA3=IGA1
                                                                                C12365
DC 13 III=1,IGA3
13 A3/7TT TTT
                                                                                C12573
       A3 (III.II) = A1 (III.II)
                                                                                012586
                                                                                812095
 00 14 IV=1, IRA2
                                                                                312106
       Iv I= IV+IR41
                                                                                 012110
       (II, VI) SA=(II, IVI) EA
                                                                                012120
       RETURN
                                                                          - 312140
312153
012160
       END
       SUBROUTINE MYECIO (A. NUMEL, IC. KIN. KOUT, NDIP)
   THIS SUBROUTINE READS PRINTS ENTIRE (PORTIONS OF) THE VECTOR A. DEPENDING ON THE VALUE OF ---IO---. IO=1---READ ONLY IO=2---READ AND PRINT, IO=3 READ SELECTED VALUE, IC=4
READ AND PRINT SELECTED VALUES
                                                                               012170
                                                                              __012180
                                                                                012190
  TO USE 10=3 OR 4 THE CASLLING PROGRAM MUST INITIALZE THE VEC. 012210
 C
C ******THIS ROUTINE SETS 10=3---- WHEN NO BATA IN INPUT FILE

G 12230

CREAD IS FROM UNIT SPECIFIED BY CALLING FROGRAM IN KIN, HPITE IS TO 012243

012250
CREAD IS FROM UNIT SPECIFIED BY CALLING FROM DISCOULTER OF A IN THE CALLING 012250 012263
C PROG AM
       CHARACTER MSG*53
                                                                               012273
                                           DIMENSION A (NCIM)
       COMMON /MAUNS/ MSG
                                                                                012290
       IF (10.60.1).0k.(10.50.2)) THEN 012303
C READ ENTIRE VECTOR
     WRITE(KOUT, 0) 'ENTER ', NUMEL, 'ELEMENTS>'
                                                                                012320
       READ (KIN. +, END=29) (A(I), I=1, NUMEL)
                                                                               612330
612340
       END IF
       "IF (19.60.1) THEN
                                                                                J12350
                                                                              __012365
       RETURN
       IF ((IO.EQ.3).OR.(IC.EQ.4).GR.(IO.EQ.6)) THEN EAD ONLY SELECTED ELEMENTS. THE FT.C.
                                                                                C12373
                                                                            01230
 C READ ONLY SELECTED ELEMENTS. THE FIRST NUMBER ON EACH CARD
C IS THE SUBSCRIPT, THE SECOND IS THE DATA ENTRY
CONTRACTOR ONLY ONE DATA ENTRY BER
                                                                                012490
 C***** FIRST CARD MUST CONTAIN THE TOTAL NUMBERS OF ENTRIES TO BE 012-13
                                                                                012435
     IF(IC.NE.6) GO TO 4
       DO 3 I=1.NOI4
                                                                                ŭ 1245<u>ŭ</u>
       A(I)=G.
                                                                                 212460
                                                                                012470
       CONT INUE
       WRITE(KOUT, +) 'ENTER THE ELEPENT NUBBER , THEN ITS VALUE> *
                                                                                012486
       READ (KIN. 4, END=29) I. ENTRY
                                                                                312-91
       IF(I.LE.3) GO TO 21
                                                                                012500
       IF (I.GT. HOIM) GO TO 5
                                                                                012510
       A(I)=ENTRY
                                                                                612520
       IF (10.EQ.4)THEN
                                                                                012530
       WEITE(KOUT,33) .
                                                                           C12540
012550
       WRITE(KOUT,*).455
       WRITE( COUT . +) 'ELEPENT NUMBER . ENTRY>'
                                                                                312560
       WRITE(KOUT,11)I,A(I)
                                                                                012570
    END IF
                                                                                012583
                                                                                01259
    23 CONTINUE
                                                                                 012603
```

1201. 2.10.1.	manufacture and the control of the c	
IF ((I)=2,2),3-(I)=(I) THE C TO GST HERE IN 20 AS SO PEINT CUT ENTIRE VECTOF HRITE(KOUT,-1)** NSG HRITE(KOUT,-1)** NSG HRITE(KOUT,-2)* (AI[], THE VECTOR PASS ', NUMBEL, ' ELEMENTS' (1285) HRITE(KOUT,-2)* (AI[], THE VECTOR PASS ', NUMBEL, ' ELEMENTS' (1286) RETURN HRITE(KOUT,-2)* (AI[], THE VECTOR PASS ', NUMBEL, ' ELEMENTS' (1286) RETURN END IF (1286) RETURN END IF (1276) RETURN C PARTICLES ROUTINE SETS IOHO HHEN KG DATA IN IMPUT FILE (1276) 12 PORMATIS ROUTINE SETS IOHO HHEN KG DATA IN IMPUT FILE (1276) 12 FORMATIS ROUTINE SETS IOHO HHEN KG DATA IN IMPUT FILE (1276) 12 FORMATIS ROUTINE SETS IOHO HHEN KG DATA IN IMPUT FILE (1276) 12 FORMATIS ROUTINE SETS IOHO HHEN KG DATA IN IMPUT FILE (1276) 12 FORMATIS ROUTINE SETS IOHO HHEN KG DATA IN IMPUT FILE (1276) 12 FORMATIS ROUTINE SETS IOHO HHEN KG DATA IN IMPUT FILE (1276) 22 FORMATIS ROUTINE SETS IOHO HHEN KG DATA IN IMPUT FILE (1276) 23 FORMATIS ROUTINE SETS IOHO HHEN KG DATA IN IMPUT FILE (1276) D SUSACUTINE MHATIO (A.IR., IC., IC., KIN, KOUT, HOIN, HOIN) C CHARACTER MSG-60 O INESION AKONIN, HOIN) C CHARACTER MSG-60 O INESION AKONIN, HOIN) C C MOIN AND MAUNS / MSG C YMIS SUBGOUTINE READS AND/OR PRINTS THE MATFIX A CEPENOING ON THE (1283) C YAULUS JF IJ. IT READS FROM UNIT SECTIFICD BY KIN AND MEJITS TO UNIT (1286) C YAULUS JF IJ. IT READS FROM UNIT SECTIFICD BY KIN AND MEJITS TO UNIT (1286) C YAULUS JF IJ. IT READS FROM UNIT SECTIFICD BY KIN AND MEJITS TO UNIT (1286) C YAULUS JF IJ. IT READS FROM UNIT SECTIFICD BY KIN AND MEJITS TO UNIT (1286) C YAULUS JF IJ. IT READS FROM UNIT SECTIFICD BY KIN AND MEJITS TO UNIT (1286) C YAULUS JF IJ. IT READS FROM UNIT SECTIFICD BY KIN AND MEJITS TO UNIT (1286) C YAULUS JF IJ. IT READS FROM UNIT SECTIFICD BY KIN AND MEJITS TO UNIT (1286) C YAULUS JF IJ. IT READS FROM UNIT SECTIFIC BY KIN AND MEJITS TO UNIT (1286) C YAULUS JF IJ. IT READS FROM UNIT SECTIFIC BY KIN AND MEJITS TO UNIT (1286) C YAULUS JF IJ. IT READS FROM UNIT SECTIFIC BY KIN AND MEJITS TO UN	A E TURN	312611
IF ((10.26.2).J(10.20.5)) THEN C TO GET HERE INP. OR 5 SO PEINT CUT ENTIRE VECTOF HRITE(KOUT, 1): NSG WESTE(KOUT, 1): NSG WESTE(KOUT, 1): NSG WESTE(KOUT, 2): (A(S), IN-IN-IN-IN-IN-IN-IN-IN-IN-IN-IN-IN-IN-I	END IF	11262.
C TO GET MERE 132 OR \$ 50 POINT CUT ENTIFE VECTOR WRITEKOUT. 237 'S WRITEKOUT. 237 'S WRITEKOUT. 27 THE VECTOR PES ', NUMBEL, 'ELEMENTS' (1285) WRITEKOUT. 27 THE VECTOR PES ', NUMBEL, 'ELEMENTS' (1287) WRITEKOUT. 27 THE VECTOR PES ', NUMBEL, 'ELEMENTS' (1287) WRITEKOUT. 27 THE VECTOR PES ', NUMBEL, 'ELEMENTS' (1287) WRITEKOUT. 28 THE VECTOR PES ', NUMBEL, 'ELEMENTS' (1287) RETURN (1287) END (1277) 29 FRANTE, 'END OF DAY REACHED QURING INPUT IN HVECIC' (1275) 21 FORMAT (14.15%, 612.6) (1275) 22 FORMAT (14.15%, 612.6) (1275) 23 FORMAT (14.15%, 612.6) (1275) 24 FORMAT (14.15%, 612.6) (1275) END (1277) END (127	IF ((IJ.E2.2).JR.(IJ.EQ.E)) THEN	
## # # # # # # # # # # # # # # # # # #	C TO SET MERE THE? OF 5 SO PRINT OUT ENTIRE VECTOR	
#FITE(KOUT,*) THE VECTOR MES 'NUMBEL, ' ELEMENTS' (1267) #RITE(KOUT,*2) (A(I),*=1,NUMEL) #RO IF #RO		·
### ### ### ### ### ### ### ### ### ##		
### ### ### ### ### ### ### ### ### ##	#E11E(KOU1,*1)426	_ 0,12560
### ### ### ### ### ### ### ### ### ##	WRITE(KOUT.*)' THE VECTOR MAS 'NUMEL.' ELEMENTS'	
### RETURN 0129- ### RETURN 015	WRITE(KOUT,22)(A(I),I=1,NUMEL)	012583
END IF RETURN 29 PRINTS, CND OF DAT REACHED DURING INPUT IN MYECIC' 10: C ***********************************	RETURN	
RETURN 2 PRINT*, END OF DAT REACHED DURING INPUT IN HVECIC* 2 PRINT*, END OF DAT REACHED DURING INPUT IN HVECIC* 31 FORMATICALD*, 33 FORMATICALD*, 31 FORMATICA	ENO TE	
29 PRINT, "NO OF DAT -EACHED DURING INPUT IN MYECTO" 10=: 10=: 10=: 11	BETIEN	
C	RETURN	
C	29 PRINT - "END OF DAT REACHED DURING INPUT IN MYECIC"	C1272:
13 FORMATICALITY	168	012735
11 FORMAT(1-15%,E12.6) 22 FORMAT(10:13/1X,E12.6);,/)) 22 FORMAT(10:13/1X,E12.6);,/)) 22 FORMAT(10:13/1X,E12.6);,/)) 23 FORMAT(10:13/1X,E12.6);,/)) 24 FORMAT(10:13/1X,E12.6);,/)) 25 END 26 CAMASIO 27 SUBACUTINE MMATIO(1A,IR,IC,IC,KIM,KOUT,HDIM,HDIM1) 27 SUBACUTINE MMATIO(1A,IR,IC,IC,KIM,KOUT,HDIM,HDIM1) 28 SUBACUTINE MMATIO(1A,IR,IC,IC,KIM,KOUT,HDIM,HDIM1) 29 COMEN /MAUNJ/ MSC 20 DI MESSION A(MOIN, NO.M1) 20 COMEN /MAUNJ/ MSC 21 SUBGOUTINE READS AND/OR PRINTS THE MATFIX A DEPENDING ON THE C12850 20 COMEN /MAUNJ/ MSC 21 KALUE JF 1J. 17 READS FROM UNIT SPECIFIED BY KIN AND METETS TO UNIT C12860 21 KOUT, IONIREAD ENIZE AFRAY 10=2READ AND PRINT ENTIRE 10 SUBGOUTINE ENTANCE OF A 10-2READ AND 112850 21 C ARRAY. 10=3READ SELECTED ELEMENTS OF A 10=4READ AND 112850 21 NOIM, NOIMH ARE THE DIMENSJONS OF A 1N THE CALLIME PROGRAM 112910 22 C NOIM, NOIMH ARE THE DIMENSJONS OF A 1N THE CALLIME PROGRAM 112911 22 C THE ENTIRE ARRAY BEFORE CALL 23 C THE ENTIRE ARRAY BEFORE CALL 24 C THE MITTER ON A 10 CONTAIN THE INPUT FILE IS EMPTY 112930 25 C READ ENTIRE ARRAY IN FREE FORMAT, ROD MAJOROREN 112991 26 C READ ENTIRE ARRAY IN FREE FORMAT, ROD MAJOROREN 112991 27 FI (10.E0.1) THEN 113012 28 C THE FIRST CARD IN THE INPUT STREAM HUST CONTAIN THE TOTAL 113012 28 C THE FIRST CARD IN THE INPUT STREAM HUST CONTAIN THE TOTAL 113013 28 C THE FIRST CARD IN THE INPUT STREAM HUST CONTAIN THE TOTAL 113013 28 C THE FIRST CARD IN THE CALGARD IS THE ROD, THESECOND IS THE COL THE 113112 29 C THE FIRST CARD IN THE ROD THAT LOCATION 113112 20 C THE FIRST CARD IN THE ROD THAT LOCATION 113113 20 C THE FIRST CARD IN THE ROD THAT LOCATION 113113 21 C THE FIRST CARD IN THE ROD THAT LOCATION 113113 21 C THE FIRST CARD IN THE ROD THAT LOCATION 113113 21 C THE FIRST CARD IN THE THE ROM, AND COLUMN FOLLOWED BY ITS VALUE> 113113 21 C THE FIRST CARD THE THE ROM, AND COLUMN FOLLOWED BY ITS VALUE> 113113 21 C THE FIRST	C +++++ THIS ROUTINE SETS IC=C WHEN NO DATA IN INFUT FILE	012743
11 FORMAT(101)(1x, 12.6), 1, 1) 22 FORMAT(101)(1x, 12.6), 1, 1) 22 FORMAT(101)(1x, 12.6), 1, 1) 22 FORMAT(101)(1x, 12.6), 1, 1) 23 COMMATIO 30 SUB-CUTIME MANTIO (1x, 10, 10, 10, 10, 10, 10, 10, 10, 10, 10	TT FORMAT (A1G. /)	6+2750
22 FORMATIO (13(1X,E12,5),1,1)) RETURN END DECK MMATIO SUBSCUTTINE MMATIO (A.IR., IC.IC.KIN.KOUT, NOIM, NOIM)) CARACTER MSG-60 DIMENSION A(MOIM, NOIM) COMMCN MAUNS, MSG C THIS SUBROUTINE READS AND/OR PRINTS THE MATFIX A DEPENDING ON THE CIZESD COMMCN MAUNS, MSG C THIS SUBROUTINE READS AND/OR PRINTS THE MATFIX A DEPENDING ON THE CIZESD C VALUE 3F 13. IT READS FROM UNIT SPECIFIC BOX KIN AND METES TO UNIT CIZESD C VALUE 3F 13. IT READS FROM UNIT SPECIFIC BOX KIN AND METES TO UNIT CIZESD C VALUE 3F 13. IT READS FROM UNIT SPECIFIC BOX KIN AND METES TO UNIT CIZESD C ROUTH, IDEA SPECIFIC ELEMENTS OF A IDEA——READ AND PAINT ENTIRE METAY CIZEDO C PAINT SELECTED ELEMENTS OF A IDEA——READ AND PAINT ENTIRE ARRAY CIZESD C PAINT SELECTED ELEMENTS OF A IDEA——READ AND PAINT ENTIRE ARRAY CIZESD C PAINT SELECTED ELEMENTS OF A IN THE CALLING PROGRAM CIZESD C MOIM-NOIMH ARE THE DIMENSIONS OF A IN THE CALLING PROGRAM CIZESD C MOIM-NOIMH ARE THE DIMENSIONS OF A IN THE CALLING PROGRAM CIZESD C THE ENTIRE ARRAY BEFORE CALL C THE ENTIRE ARRAY BEFORE CALL C THE ENTIRE ARRAY BEFORE CALL C THE SITE ARRAY IN FREE FORFAT, FROM MAJOR ORDER CIZESD C MAILE ARRAY IN FOR FROM THE INPUT FILE IS EMPTY CIZESD C MAILE (COUT., ''' ENTER ''. (IR.'')C.'', ARRAY ELEMENTS IN FOW MAJORDER'' CIZESD C MAILE (COUT., ''') ENTER ''. (IR.'')C.'', ARRAY ELEMENTS IN FOW MAJORDER'' CIZESD FOR COUTH COUT., COUTH COUTH COUTH COUT., COUTH COUTH COUTH COUT., COUTH COUTH COUT., COUTH COUT., COUTH C		
DECK MMATIO DECK	11 FURNAT (14417A, E12.6)	
DECK MMATIO DECK	22 FORMAY (10(13(1X,E12.5),1,7))	012773
DECK MMATIO SUBSCUTINE MMATIO (A.IR., IC., IC., KIN, KOUT, NDIM, NDIMI) CAPACITE MSG-63 DIMENSION A(NOIM, NDIMI) COMMENSION A(NDIMI) COMENSION A(NDIMI) COMMENSION A(NDIMI) COMENSION A(NDIMI) COMENSION A(NDIMI) COMENSION A(NDIMI) COMENSION A(NDIMI) COMENSION A	RETURN	ü1278 8
* DECK MMATIO SURGUITIE MMATIO (A.TR., IC., IC., KIN, KOUT, NOIM, NOIM) COMPAND AS AND MAD AND MAD AND MAD SURVEY OF THE MATER MSG-69 OIMENSION AND MAD AND MAD AND MAD SURVEY OF THE MATER OF THE MATER OF THE MATER OF THE MAD AND MAD SURVEY OF THE MAD AND MAD AND MAD SURVEY OF THE MAD MAD MAD MAD SURVEY OF THE MAD MAD MAD MAD MAD SURVEY OF THE MAD MAD MAD MAD MAD MAD SURVEY OF THE MAD MAD MAD MAD MAD MAD SURVEY OF THE MAD	PO ON THE POPULATION OF THE PO	01279:
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DIMERSION ACKNOWN DIMENS DIMERS DIMERSION ACKNOWN DE	CHESTER MORECE	0101U
COMMEN / MAUMS / MSG C THIS SUBROUTINE READS AND/OR PRINTS THE MATFIX A DEPENDING ON THE C VALUE JF 13. IT READS FROM UNIT SPECIFIED BY KIN AND MPITES TO UNIT (1296) C KOUT. IG=1-READ ENICE APRAY IG=2-KEAD AND PRINT ENTIRE 10.2377 C COUT. IG=3READ SELECTED ELEMENTS OF A TO=1-READ AND 12.2990 C ARRAY. IG=3READ SELECTED ELEMENTS OF A TO=1-READ AND 12.2990 C PRINT SELECTED ELEMENTS OF A IG=3PRINT ENTIRE ARRAY C.2990. C NOIMHNOINI ARE THE DIMENSIONS OF A IN THE CALLING PROGRAM 12.2913 C	CHARACIER HOG-OJ	U12820
C KOUT. ID=1READ ENIXE APRAY I D=2READ AND PRINT ENTIRE D12373 C ARRAY. ID=3READ SELECTED ELEMENTS OF A ID=4READ AND 212990 C PRINT SELECTED ELEMENTS OF A ID=5PRINT ENTIRE ARRAY C12901 C NOIN, NOINI ARE THE DIMENSIONS OF A IN THE CALLING PROGRAM 012913 C D=4	07.10.407.41.41.407.41.1	0 T F 3 3 3
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C ARRAY. IG=3READ SELECTED ELEMENTS OF A 10=4READ AND 21290C C PRINT SELECTED ELEMENTS OF A 10=5PRINT ENTIRE ARRAY 12901 C NOIM, NOIM ARE THE DIMENSIONS OF A IN THE CALLING PROGRAM 012912 CNOITE IF 10=3 OK THE CALLING PROGRAM HUST INITIALIZE 112921 CNOITE IF 10=3 OK THE CALLING PROGRAM HUST INITIALIZE 112932 C THE ENTIRE ARRAY BEFORE CALL 112942 CNHEN THE INPUT FILE IS EMPTY 112952 C THE ENTIRE ARRAY BEFORE CALL 112943 C THE COLOR OF THE SETS 10 =0 WHEN THE INPUT FILE IS EMPTY 112952 C THE (10,EQ,1),OR,(10,EQ,2)) THEN 112962 C READ ENTIRE ARRAY IN FREE FORPAT,ROW MAJOR ORDER 113002 READ (KIA,***,END=29)((A(I,*)),J=1,IC),'=1,IR) 11304 END IF (10,EQ,1) THEN 11304 END IF (10,EQ,1) THEN 113053 THE (10,EQ,1) THEN 113053 C THE FIRST CARD IN THE IMPUT STEEAM HUST CONTAIN THE TOTAL 113062 C THE FIRST CARD IN THE IMPUT STEEAM HUST CONTAIN THE TOTAL 113062 C THE FIRST CARD IN THE IMPUT STEEAM HUST CONTAIN THE TOTAL 113062 C LAST ON EACH CARD IS THE DATA FOR THAT LOCATION 13112 C LAST ON EACH CARD IS THE DATA FOR THAT LOCATION 13112 C LAST ON EACH CARD IS THE DATA FOR THAT LOCATION 13112 C PREE FORMAT IS USED 113163 FF(IC,NE,6) GO TO 4 113157 C OUT INUE 113163 C PREE FORMAT IS USED 1131617 FF(IT,LE,5),OR,JU,E,0)) GC TO 2: 113202 IF(IT,GT,IR,OR,JU,E,0)) GC TO 5 LAST CHAPTER THE NOW,AND COLUMN FOLLOWED BY ITS VALUE> 113192 IF(IT,GT,IR,OR,JU,E,0)) GC TO 5 LAST CHAPT IF (10,EQ,4) THEN 113222 IF(IT,GT,IR,OR,JU,E,0)) GC TO 5: 113202 IF(IT,GT,IR,O	A ANGLE OF ANY AND THE STATE OF ANY AND ASSESSED TO ONLY	
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C PRINT SELECTED ELEMENTS OF A 10-5PRINT ENTIRE ARRAY C12901 C NOIM-NOIM ARE THE DIMENSIONS OF A IN THE CALLING PROGRAM 012917 C	C ARRAY. IG==3READ SELECTED ELEMENTS OF A IG=4READ AND	212990
C NDIM-NOUTH ARE THE DIMENSIONS OF A IN THE CALLING PROGRAM C 12923 C ***********************************	C PRINT SELECTED ELEMENTS OF A TORSPPINT FITTER APRAY	C1290:
C	C NOTH-NOTHS ARE THE OTHENS ONS OF A IN THE CALLING PROGRAM	012013
C ************************************	e de la	
C THE ENTIRE ARRAY BEFORE CALL C 012950 C 0000000000000000000000000000000000	ARABEAUTT TE TAIT OF THE PUR ON LYNE BORRAY MICH.	
C	C NCIE IF 10=3 OR & THE CALLING PROGRAM HUST INTITALIZE	
C ************************************	C THE ENTIRE ARRAY BEFORE CALL	C129+i
C		U1295:
C	CTHIS COUTINE SETS IO =0 WHEN THE INPUT FILE IS EMPTY	012960
IF ((10.EG.1).OR.(10.EG.2)) THEN C READ ENTIRE ARRAY IN FREE FORFAT, FOR HAJOR ORDER MITTE(KOUT.*)' ENTER ', (IR*IC).' ARRAY ELEMENTS IN ROW MAJ ORDER>' 013:01: READ(KIN,*, END=29) ((A(I,J),J=1,IC),I=1,IR) END IF (10.EG.1) THEN RETURN END IF ((10.EG.3).OR.(IC.EG.4).CR.((IO.EG.5)) THEN C READ IN SELECTED ELEMENTS OF A C THE FIRST CARD IN THE INPUT STREAM MUST CONTAIN THE TOTAL C NUMBER OF ELEMENTS TO BE READ IN. ONLY ONE ENTRY PER CAAD. C THE FIRST UTEN ON EACH CARD IS THE ROW. THESECOND IS THE COL THE 013:00: C LAST ON EACH CARD IS THE DATA FOR THAT LOCATION OLAST ON EACH CARD IS THE DATA FOR THAT LOCATION OLAST ON EACH CARD IS THE DATA FOR THAT LOCATION OLAST ON EACH CARD IS THE DATA FOR THAT LOCATION OLAST N=1.IC OC 45 N=1.IC OC 31161 OC 45 N=1.IC OC 45 N=1.IC OC 45 N=1.IC OC 31161 OC 45 N=1.IC OC 31161 OC 3116		012975
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## ## ## ## ## ## ## ## ## ## ## ## ##	AF (100Edd) OR (100Edd) Inch	615460
READ (KIA,*, END=29) ((A(I,J),J=1,IC), I=1,IR) END IF (IO.EQ.1) THEN RETURN END IF (IO.EQ.3).OR.(IC.EQ.4).CR.(IO.EG.6)) THEN C READ IN SELECTED ELEMENTS OF A C THE FIRST CARD IN THE INPUT STREAM HUST CONTAIN THE TOTAL C NUMBER OF ELEMENTS TO BE READ IN. ONLY ONE ENTRY PER CARD. C THE FIRST ITEM ON EACH CARD IS THE RGM. THESECOND IS THE COL THE 013100 C LAST ON EACH CARD IS THE DATA FOR THAT LOCATION C FREE FORMAT IS USED IF (IC.NE.6) GO TO 4 OC 45 N=1.IC OC 45 N=1.IC CONTINUE A (M,N)=20.3 FREAD(KIN,*, END=29)II.J.ENTRY IF (III.E.E.D).OR.(J.E.D)) GC TO 2: IF ((II.E.E.D).OR.(J.E.D)) GC TO 2: IF ((II.E.E.D).OR.(J.E.D)) GC TO 5 A (II.J)=ENTRY IF (IO.EQ.4) THEN WRITE(KOUT,*)MSG	G KEAU ENTIRE ARRAT IN PREE PURPAIARUM MAJUR URUER	812993
READ (KIA,*, END=29) ((A(I,J),J=1,IC), I=1,IR) END IF (IO.EQ.1) THEN RETURN END IF (IO.EQ.3).OR.(IC.EQ.4).CR.(IO.EG.6)) THEN C READ IN SELECTED ELEMENTS OF A C THE FIRST CARD IN THE INPUT STREAM HUST CONTAIN THE TOTAL C NUMBER OF ELEMENTS TO BE READ IN. ONLY ONE ENTRY PER CARD. C THE FIRST ITEM ON EACH CARD IS THE RGM. THESECOND IS THE COL THE 013100 C LAST ON EACH CARD IS THE DATA FOR THAT LOCATION C FREE FORMAT IS USED IF (IC.NE.6) GO TO 4 OC 45 N=1.IC OC 45 N=1.IC CONTINUE A (M,N)=20.3 FREAD(KIN,*, END=29)II.J.ENTRY IF (III.E.E.D).OR.(J.E.D)) GC TO 2: IF ((II.E.E.D).OR.(J.E.D)) GC TO 2: IF ((II.E.E.D).OR.(J.E.D)) GC TO 5 A (II.J)=ENTRY IF (IO.EQ.4) THEN WRITE(KOUT,*)MSG	WRITE(KOUT . *) 'ENTER '. (IR IC) . ARRAY ELEMENTS IN ROW MAJ ORDER > *	_013000
END IF IF (IO.EQ.1) THEN RETURN END IF IF ((IO.EQ.3).OR.(IC.EQ.4).CR.(IO.EG.6)) THEN C READ IN SELECTED ELEMENTS OF A C THE FIRST CARD IN THE INPUT STREAM MUST CONTAIN THE TOTAL C NUMBER OF ELEMENTS TO BE READ IN. ONLY ONE ENTRY PER CARD. C THE FIRST ITEM ON EACH CARD IS THE RGW, THESECOND IS THE COL THE B13100 C LAST ON EACH CARD IS THE DATA FOR THAT LOCATION C LAST ON EACH CARD IS THE DATA FOR THAT LOCATION OC +5 R=1.IR OC +5 N=1.IC A(M,N)=0.J C CONTINUE WRITE(KOUT,*)*ENTER THE ROW,AND COLUMN FOLLOWED BY ITS VALUE>** 013180 FREAD(KIN,*END=29)II.J.ENTRY IF (II.LE.D).OR.(J.LE.D)) GC TO 2: OC 13200 IF ((II.GT.IR).OR.(J.LE.D)) GC TO 2: OC 13220 IF ((II.GT.IR).OR.(J.GT.IC)) GC TO 5 WRITE(KOUT,*)*MSG	READ(KIN, -, END=29) ((4(I,J),J=1,IC),I=1,IR)	013010
IF (10.EQ.1) THEN RETURN END IF (13.EQ.3).QR.(IC.EQ.4).CR.(IO.EG.6)) THEN C13063 IF (10.EQ.3).QR.(IC.EQ.4).CR.(IO.EG.6)) THEN C13063 C READ IN SELECTED ELEMENTS OF A C THE FIRST CARD IN THE INPUT STREAM HUST CONTAIN THE TOTAL C NUMBER OF ELEMENTS TO BE READ IN. ONLY ONE ENTRY PER CARD. C THE FIRST ITEM ON EACH CARD IS THE RGM. THESECOND IS THE COL THE DISION C LAST ON EACH CARD IS THE DATA FOR THAT LOCATION C FREE FORMAT IS USED IF (IC.NE.6) GO TO 4 OC 45 N=1.IC OC 45 N=1.IC A (M,N)=û.J C CONTINUE WRITE(KOUT,*)*ENTER THE ROW,ARD COLUMN FOLLOWED BY ITS VALUE>* OC 313161 FREAD(KIN,*END=29)II.J.ENTRY IF (II.LE.E).OR.(J.LE.E)) GC TO 2: OC 3220 IF ((II.GT.IR).OR.(J.E.E.D)) GC TO 2: A (II.J)=ENTRY IF (IO.EQ.4) THEN WRITE(KOUT,*)MSG OC 33255		013323
### RETURN END IF IF ((I).EQ.3).QR.(IC.EQ.4).CR.(IO.EG.5)) THEN C READ IN SELECTED ELEMENTS OF A C THE FIRST CARD IN THE INPUT STREAM MUST CONTAIN THE TOTAL C NUMBER OF ELEMENTS TO BE READ IN. ONLY ONE ENTRY PER CARD. C THE FIRST ITEM ON EACH CARD IS THE RGW. THESECOND IS THE COL THE 013100 C LAST ON EACH CARD IS THE DATA FOR THAT LOCATION C FREE FORMAT IS USED OLISIST IF (IC.NE.6) GO TO 4 DO 45 N=1.IC OC 45 N=1.IC WRITE(KOUT.*) ENTER THE ROW.AND COLUMN FOLLOWED BY ITS VALUE>* OTHER FIRST ITEM ON AND COLUMN FOLLOWED BY ITS VALUE>* OTHER FIRST ITEM ON EACH CARD IS THE DATA FOR THAT LOCATION OTHER FIRST ITEM ON EACH CARD IS THE DATA FOR THAT LOCATION OTHER FIRST ITEM ON EACH CARD IS THE DATA FOR THAT LOCATION OTHER FIRST ITEM ON EACH CARD IS THE DATA FOR THAT LOCATION OTHER FIRST ITEM ON EACH CARD IS THE DATA FOR THAT LOCATION OTHER FIRST ITEM ON EACH CARD IS THE DATA FOR THAT LOCATION OTHER FIRST ITEM ON EACH CARD IS THE DATA FOR THAT LOCATION OTHER FIRST ITEM ON EACH CARD IS THE DATA FOR THAT LOCATION OTHER FIRST ITEM ON EACH CARD IS THE OTHER FOR THAT LOCATION OTHER FIRST ITEM ON EACH CARD IS THE OTHER FOR THAT LOCATION OTHER FIRST ITEM ON EACH CARD IS THE OTHER FOR THAT LOCATION OTHER FIRST ITEM ON EACH CARD IS THE OTHER THE OTHER FOR THAT LOCATION OTHER FIRST ITEM ON EACH CARD IS THE OTHER THE OTHER FOR THAT LOCATION OTHER FIRST ITEM ON EACH CARD IS THE OTHER THE OTHER FOR THE OTHER	15 (20.50.1) THEN	
END IF IF ((IJ.EQ.3).DR.(IC.EQ.4).CR.(IO.EQ.6)) THEN C READ IN SELECTED ELEMENTS OF A C THE FIRST CARD IN THE IMPUT STREAM MUST CONTAIN THE TOTAL C NUMBER OF ELEMENTS TO BE READ IN. OWLY ONE ENTRY PER CARD. C THE FIRST ITEM ON EACH CARD IS THE RGW. THESECOND IS THE COL THE DISION C LAST ON EACH CARD IS THE DATA FOR THAT LOCATION C FREE FORMAT IS USED IF (IC.NE.6) GO TO 4 DO 45 M=1.IR OC 45 N=1.IC CONTINUE WRITE(KOUT.*) ENTER THE ROW.AND COLUMN FOLLOWED BY ITS VALUE>** O1310: FREAD(KIN.*.END=29)II.J.ENTRY IF ((II.EL.U).OR.(J.EL.D)) GC TO 2: IF ((II.GT.IR).OR.(J.GT.IC)) GC TO 5 A (II.J)=ENTRY UN3223: HRITE(KOUT.*) THEN WRITE(KOUT.*) THEN HRITE(KOUT.*) MSG		
IF ((IJ.EG.3).OR.(IC.EG.4).CR.(IO.EG.5)) THEN C READ IN SELECTED ELEMENTS OF A C THE FIRST CARD IN THE INPUT STREAM HUST CONTAIN THE TOTAL C NUMBER OF ELEMENTS TO BE READ IN. ONLY ONE ENTRY PER CARD. C THE FIRST ITEM ON EACH CARD IS THE ROW, THESECOND IS THE COL THE 813100 C LAST ON EACH CARD IS THE DATA FOR THAT LOCATION C FREE FORMAT IS USED IF (IC.NE.6) GO TO 4 DO 45 M=1.IR OC 45 N=1.IC 45 A(M,N)=0.J CONTINUE HRITE(KOUT,*)*ENTER THE ROW, AND COLUMN FOLLOWED BY ITS VALUE>* 013127 IF (II.LE.U).OR.(J.LE.O)) GC TO 2: IF (III.LE.U).OR.(J.LE.O)) GC TO 2: IF (III.LE.U).OR.(J.GT.IC)) GC TO 5 A(II.J)=ENTRY HRITE(KOUT,*)*MSG 013245 D13245 D13245 D13245 D13245	PUR OF	
C THE FIRST CARD IN THE INPUT STREAM MUST CONTAIN THE TOTAL C NUMBER OF ELEMENTS TO BE READ IN. ONLY ONE ENTRY PER CARD. C THE FIRST ITEM ON EACH CARD IS THE RGW. THESECOND IS THE COL TME 013100 C LAST ON EACH CARD IS THE DATA FOR THAT LOCATION 013112 G FREE FORMAT IS USED 013152 IF (IG. NE.6) GO TO 4 013152 DO 45 M=1.IR 013145 CONTINUE 013160 FREAD (KIN.**) **ENTER THE ROW.AND COLUMN FOLLOWED BY ITS VALUE>** 013180 FREAD (KIN.**, END=29) II.J. ENTRY 013200 IF ((II.GT.IR).OR.(J.LE.0)) GC TO 2: 013200 IF ((II.J)=ENTRY 013232 IF (10.EQ.4) THEN 013252 WRITE(KOUT.*33)** 013252 WRITE(KOUT.*33)** 013252	ENU AF	U13U53
C THE FIRST CARD IN THE INPUT STREAM MUST CONTAIN THE TOTAL C NUMBER OF ELEMENTS TO BE READ IN. ONLY ONE ENTRY PER CARD. C THE FIRST ITEM ON EACH CARD IS THE RGW. THESECOND IS THE COL TME 013100 C LAST ON EACH CARD IS THE DATA FOR THAT LOCATION 013112 G FREE FORMAT IS USED 013152 IF (IG. NE.6) GO TO 4 013152 DO 45 M=1.IR 013145 CONTINUE 013160 FREAD (KIN.**) **ENTER THE ROW.AND COLUMN FOLLOWED BY ITS VALUE>** 013180 FREAD (KIN.**, END=29) II.J. ENTRY 013200 IF ((II.GT.IR).OR.(J.LE.0)) GC TO 2: 013200 IF ((II.J)=ENTRY 013232 IF (10.EQ.4) THEN 013252 WRITE(KOUT.*33)** 013252 WRITE(KOUT.*33)** 013252	IF ((13.EG.3).OR.((C.EG.4).CR.((10.EG.5)) THEN	01306 <u>T</u> - M
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C NUMBER OF ELEMENTS TO BE READ IN. ONLY ONE ENTRY PER CARD. C THE FIRST ITEM ON EACH CARD IS THE RGW. THESECOND IS THE COL THE 013100 C LAST ON EACH CARD IS THE DATA FOR THAT LOCATION 013111 G FREE FORMAT IS USED 01312 O1313 O1	G THE FIRST CARD IN THE INPUT STREAM MUST CONTAIN THE TOTAL	
### COLUMN COLUMN FOLLOWED BY ITS VALUES* THE FIRST ITEM ON EACH CARD IS THE DATA FOR THAT LOCATION	C MIMBER OF SLEMENTS TO BE BEAD THE DAY ONE ENTEY BES CALD	043302
C	THE PROPERTY OF THE AN EARL AND A PURE THE COURT FOR CASE OF THE PROPERTY OF THE PROPERTY OF THE PARTY OF THE	0.24.00
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DO 45 M=1,IR OC 45 N=1,IC 45 A(M,N)=0.0 CONTINUE WRITE(KOUT,*)*ENTER THE ROW,AND COLUMN FOLLOWED BY ITS VALUE>* O13180 FEAD(KIN,*,END=29)II.J,ENTRY IF((II.LE,0).OR.(J.LE.0)) GC TO 2: O1320C O1320C O1321: A(II.J)=ENTRY U13220 O13220 A(II.J)=ENTRY U13220 O13220 A(II.J)=ENTRY O13220 O13220 A(II.J)=ENTRY O13220 O13220 O13220 O13220 O13220 O13220 O13220 O13220 O13220	IF (IC. NE.6) GO TO 4	
DC 45 N=1.IC		
45 A(M,N)=0.0 GONTINUE HRITE(KOUT,*) 'ENTER THE ROW,AND COLUMN FOLLOWED BY ITS VALUE>' READ(KIN,*,END=29)II.J,ENTRY IF((II.LE.0).OR.(J.LE.0)) GC TO 2: O1320C IF((II.J)=ENTRY IF (IO.EQ.4) THEN HRITE(KOUT,*3))* HRITE(KOUT,*3))* HRITE(KOUT,*)MSG O1325:		
### CONTINUE		
#RITE(KOUT,*) 'ENTER THE ROW, AND COLUMN FOLLOWED BY ITS VALUE>' 013180 #READ(KIN,*, END=29)II.J. ENTRY IF((II.LE.U).OR.(J.LE.U)) GC TO 2: 01320C IF((II.GT.IR).OR.(J.GT.IC)) GC TO 5 A(II.J)=ENTRY IF (IO.EQ.4) THEN #RITE(KOUT, 33) ' 013245 #RITE(KOUT,*) MSG		
##ITE(KOUT.*) MSG READ(KIN.*, END=29) II.J. ENTRY		
##ITE(KOUT.*) MSG READ(KIN.*, END=29) II.J. ENTRY	WRITE(KOUT, +) 'ENTER THE ROW, AND COLUMN FOLLCHED BY ITS VALUE>'	013180
IF ((II.LE.U).OR.(J.LE.U)) GC TO 2: 01320C IF ((II.GT.IR).OR.(J.GT.IC)) GC TO 5 A(II.J)=ENTRY C1322C IF (IO.EQ.4) THEN C1323C HRITE(KOUT.33)'' 01324C HRITE(KOUT.*)MSG 01325C		
IF ((II.GT.IR).OR.(J.GT.IC)) GC TO 5 A(II.J)=ENTRY IF (IO.EQ.4) THEN HRITE(KOUT.33)'' HRITE(KOUT.*)MSG 01321: 013220 013232		
A(II,J)=ENTRY		
IF (10.EQ.4) THEN G13232 013243 013243 013252	- · - · · · · · · · · · · · · · · · · ·	
WRITE(KOUT, 33)		£13220
WRITE(KOUT, 33)	IF (10.EQ.4) THEN	013232
WRITE(KOUT.*)MSG 013252		
WFITE(KOUT,*)'('.II.'.'.J.')='.4(II.J)		
PRAIMINGUITE F & TALE & GAS IN THILLIANS	WETTERMITANIES TTO COLUMN TO A STATE AND A STATE AND ASSESSMENT OF THE STATE ASSESSMENT OF	
The state of the s	THE PROPERTY OF THE PROPERTY O	

```
END IF
                                                                               313273
                                                                               91738<u>-</u>
      SO TC 5
                                                                                         M
   ZC CONTINUE
                                                                               513293
      RETURY
                                                                               013300
      END IF
                                                                              013310
    IF ((ID.EG.2).OR.(IC.EG.5)) THEN
IO = 2 OR 5 IF MERE SC PRINT ENTIRE ARRAY
                                                                              813320
                                                                              213330
      * * (EE, TUOX)3TIRW
                                                                              413343
      WRITE(KOUT,+) 45G
      WRITE(KOUT, *) ' MATRIX SIZE IS ', IR, ' X ', IC
                                                                              0133E3
      DO 49 I=1.IR
                                                                              013376
   -9 HRITE(KOUT.48) (A(I,J).J=1.IC)
                                                                              013380
      FORMAT (ALC./)
   48 FORMAT (5(18(1x.E12.6), 1,/))
      END IF
                                                                              013410
      RETURN
                                                                              013420
   29 PRINT +, END OF DATA REACHED DURING INPUT
   ****** THIS ROUTINE SETS IO =0 ---- WHEN THE INPUT FILE IS EMPTY
      10=:
                                                                              C13450
      RETURN
                                                                              013-65
      END
                                                                              613475
• DECK CLOGRS
      SUBROUTINE CLOGES (GCSTR.FM.Br.RKFSS.HM.GCX.GCY.GCZ.
                                                                              013492
     1BCY, ECZ, FC, YD, RM, OH, FT, BT, GT, OT, RT, HT, IRY, IFLGCZ, HH1
                                                                              013500
     1 . HHZ. HH3. PO. GH. HH-. HH5 . HH6.
                                                                              C13510
        WV1.WV2.WUU.WXX.XO.WXU.WM7.WM8)
C THIS ROUTINE PERFORMS SET UP FOR USING THE CONTINUOUS TIME
                                                                              213532
 PERFORMANCE ANALYSIS FOR ANLOG REGULATOR
                                                                              013543
      DIMENSICHGESTR(NOIP, NOIM) . FF (NOIM, NOIP) . 8M (NOIM . NOIM) . PG (NOIM .
                                                                              013550
     INDIM). HM (NOIM, NOIM), GCX (NOIM, NOIM), GCY (NOIM, NOIM), GCZ (NOIM, NOIM), 013560
     18CY (NOIH, NOIH), 9CZ (NOIH, NCIP), FC (NOIH, NOIH), YO (NOIH3), WH1 (NOIH,
     1ND In) . was (NDIM, NDIM) . WM3(HDIY, NDIM) . FT(NDIM . NDIM) .
                                                                              013580
     1 8T(NDIM, NDIM), GT(NDIM, NDIM), HT(NDIM, NDIM), RM(NDIM, NDIM),
                                                                              013593
     19T(NOIH, NOIH), RT(NOIH, NOIH), CM(NOIH, NOIH), HV1(NOIH), HV2(NOIH
                                                                              013600
     1),XO(NDIH),GM(NOIP,NDIH),WUU(NOIM,NDIH),
     1 WXX (NOIM, NOIM) , WM4 (NOIM, NOIM) , WM5 (NOIM, NOIM) ,
                                                                              013623
     I wm6 (ndim, noim), wxu(ndim, ndim), wm7 (ndim, ndim), wm8 (ndim, hdim)
                                                                              013633
      DIMENSION COM1(1),COM2(1)
                                                                              213640
      CHARACTER HSG-63
                                                                              013653
     INTEGER IFLGCZ
                                                                              213660
      REAL RKFSS ( NOIM, NOIM)
                                                                              G1367C
       COMPON /MAIN4/NDIM2.NDIM3
                                                                              C13680
      COMMON /MAUNS/ HSG
                                                                              613696
      GOMMCN /MAIN1/ NDIM.NDIM1.CGM1
                                                                              01370C
                                                                              013713
      COMMON /RNTIM/RNTIME.DELTIM
                                                                              813728
      COMPCH /INOU/ KIN-KOUT-KPUNCH
                                                                              013733
      COMMON /MAINS/ICBT, ICBM, ICFA, ICGA, ICGM, ICGT, ICG4, IRFA, IRFT, IRFT,
     1 IRHT, IR GA, IO, L GG, IRHM, NUMOTS
                                                                              613750
     WRITE(KOUT, *) 'DO YOU WANT TO CALCULATE EIGENVALUES OF THE TRUTH MOD13760 1DEL AND CONTROLLED MODEL F MATRICES, Y OR N>' 613770
      PEAD (KIN, 23, END= 2933) HSG ___
                                                                              213783
      FORHAT (A1)
                                                                               013790
      IF (MSG.EQ. 'Y') THEN
                                                                               213533
      WRITE(KOUT.*) '
                                                                               613316
      WRITE(KOUT,+) "THE EIGENVALUES OF THE TRUTH MODEL F MATRIX"
                                                                               613826
       CALL MEIGN(FT, WV1, WV2, IRFT, WM1)
      WRITE(KOUT, *) 'THE EIGENVALUES OF THE CONT. MODEL F MATRIX'
                                                                              01384ü
      CALL MEIGN (FM. WV1, WV2, IRFM, WF1)
END IF
                                                                               013850
                                                                               013860
      WRITE(KOUT, +) 'COLORED INPUT NOISE (Y OR N) >'
                                                                               01387¢
      READ (KIN, 23) MSG
      INGLO= IRFP
                                                                               113390
      IF (MSG.EQ. "N") 60 10 2963
                                                                               013900
      CALL CHOISE (FM.GM.HM.BH.GM.IRFH.IRHH.ICGH.ICBH.HH1.HM2.HM3)
                                                                               513913
```

CALL CKFT- (FM.GM.ZM.HM. NUMDTS. RKFSS. OM. WM1. HM2. HM3. HM4. HM5. NM6.

1 IFFM.IFMM.ICGM.CCY.GCZ.BM.ICBM)	213931
C GOZ,GOY, IN CALL TO CKFTE 4FE USED AS DUMMY ARRAYS FOR HZ .FZ	313943
CALL COTCON(FM.5M.HXX.nUU.GCSTR.IMCLD.IC3M.nM1.dM2.dM3.nmnM5.	
1446,424,47,445)	013960
IF(IHOLD.EQ.IRFM) GC TO 35	613973
ICH=IHOLD+1	613980
DC 25 I=1,1C3M	013995
DG 25 J=ICH+IRFM	014303
25 GCSTR(I,J)=0.	614013
35 CONTINUE	014623
WRITE(KOUT,+) 'ENTER THE TOTAL RUN TIME AND THE TIPE INCREPENT>	
READ (KIN, *, END=2933) RNTIME, DELTIM	314343
C1=-1	014050
CALL IONT (IRF M.WM1.C1)	014363
C MM1=-I IRFH X IRFH	014370
CALL MAT1 (GCSTR. WM1. ICBM. IRFM. IRFM. GCX)	
10=5	014393
MSG= GCX FOLLOWS, GCY.GCZ SET=0.	
CALL MMATIDIGCX, ICBM, IRFM, IC, KIN, KOUT, NDIM, NDIM)	014106
C NOTE OTHER GAIN MATRICES, GCZ, AND GCY SHOULD BE CALCULATED IN	4 G14123
THIS MODULE FOR USE IN THE PERFCR MANCE ANALYSIS ROUTINE.	614130
DO 2902 III=1,IC8*	014146
00 2512 IIII=1.IRHM	G14153
2902 GCZ(III,IIII)=9	C14160
IFLGCZ*1	014173
C IFLGCZ=1 INDICATES GCZ IS SET TO ZEROPREF ANALYSIS ROUTINE USES	014190
00 2933 I=1,1303	814236
2903 YD(I)=0	014210
IRY*1	
DO 1723 1=1,ICBM	014220
TO WITE TO WITE TO	014230
00 1723 J=1,IRY	814243
1723 GCY (I, J) = 9	01+250
C FORM BCY	01-260
DO 1792 I=1.IRFM	014270
00 17J2 J=1,IRY	014280
1702 BCY(I, J)=1	01-290
C TO IS ALLOHED TO ONLY BE A SCALAF AT THIS TIME	014300
C FORMAGZ	014310
C1=1.J	014320
CALL EQUATE (BCZ, RKFSS, IRFF, IRHH)	014330
MSG= '8CZ FOLLOMS, 8CY=0'	<u> </u>
CALL MMATID(BCZ, IRFM. IRMM, IC, KIN, KOUT, NDIH, NDIP) C FORM FC	014350
C FORM FC	014360
CAPP UMITERIOR STEEL STEEL SHAFT	314376
CALL HADD1 (IRFH, IRFH, FH, HH1, WH2, C1)	614380
WRITE(KOUT,*)''	014390
WRITE(KOUT, *) 'DO YOU WANT TO CALCULATE THE EIGENVALUES OF THE O	
11 NUOUS-TIME LO CONTROLLER? Y OR N>	G14410
READ (KI N. 23) HSG	014-20
IF (MSG.EQ.'Y') THEN	314439
WRITE (KOUT.*) THE EIGENVALUES THAT CORRESPOND TO THE POLES	OF 21446
1 THE CONTINUOUS-TIME LQ CONTROLLER ARE	014450
CALL MEIGN(HM2.HV1.HV2.IRFM.HM1)	014-63
END IF	014473
C1=-1	614-86
CALL MATI (RKFSS, HM, IRFM, IRHF, IRFM, HM1)	014-96
WRITE(KOUT, *) *	014505
WRITE(KOUT,+) 'DO YOU HANT TO CALCULATE THE POLES OF THE CONT	INU314510
10US-TIME KALMAN FILTERT Y OR N>	61-520
READ (KIN, 23) MSG	014530
IF (MSG.EQ. YY) THEN	014540
CALL MADD1(IRFM.IPFM.FF.NF1.WH7.C1)	014553
WRITE (KOUT, *) "THE EIGENVALUES THAT ARE THE POLES OF THE CHO!	
10US-TIME KALMAN FILTER ARE	\$14575
CALL MEIGN (WM7, WV1, WV2, IRFM, WM8)	014550

```
E40 1F
                                                                                014595
     CALL MADDI (IFFM. IFFM. WM 2. WM 1. FC. C1)
                                                                                 314688
     MSG= " FC FOR THE LOG CONTORLLER IS"
                                                                                014610
      CALL MMATIO(FC. IRFM. IRFM. IC. KIN, KOUT. NOIM. NOIM)
                                                                                614 623
      PRITE(KOUT,*) * *
                                                                                 $14630
     WPITE(KOUT. *1 'OO YOU WISH TO CALCULATE THE EIGENVALUES OF THE LOG 014643 1CONTROLLER F MATRIX? Y OR N>'
      READ (KIN. 23) MSG
IF (MSG.EG. "Y") THEN
                                                                                014663
      WRITE(KOUT.*) . .
                                                                                314685
      WRITE(KOUT,+) THE EIGENVALUES OF THE LOG CONTROLLER F MATRIX APE' 014690
      CALL MEIGH (FC. HV1. HV2. IRFP. HF1)
      END IF
      RETURN
2933 - 10=6
      END
- DECK DAS1
      SUBROUTINE DAS1 (GOGT. BM. V. ICBM. HH3, IRFM)
      DIMERSION GOGT (NDIM, NDIM) . BK (NDIM, NDIM) , V (NDIM, NDIM) ,
        WH3(NDIH.NDIM).COM1(1).COM2(1)
    THIS SUBROUTINE MODIFIES GOGT AND RETURNS THE MODIFIED
     VALUE IN GOGT, WHERE GOGT IS USED IN THE KALMAN FILTER
                                                                                014800
     GAIN CALCULATIONS. THE HODS ARE IN ACCORDANCE WITH THE
                                                                                614316
     THE TECHNIQUE DEVELOPED BY DCYLE AND STEIN IN "ROBUSTNESS HITH OBSERVERS", IEEE TRANS. ON AUTO. CONTROL, VOIL AC24.
                                                                                 014430
     NO. 4.AUG. 79.PGS 627-611.
C
       THE VALUE RETURNED IN GOGT IS QQ . WHERE CQ IS 014960
                                                                               014880
014890
    QQ=GQGT+SQ(SQ)BM(V(BMT)
    SO IS A SCALAR DESIGN PARAMETER, THAT AS IT APPROACHES
    INFINITY, CAUSES THE LOG CONTROLLER TO RECOVER THE ROBUSTNESS
                                                                                014910
C PROPERTIES OF A FULL STATE FEEDBACK CONTROLLER. 014920 OTHE MATROX--V-- IS ALSO A DESIGN, PARAPETER WITH THE REQUIREMENT 014930
   THAT IT BE POSITIVE CEFINITE. BM---- IS THE CONTROLLER MODEL INPUT014940 MATRIX. GOGT --- IS THE CONTROLLER MODEL INPUT NOISE STRENGTH 014950 MATRIX ON, PREMULTIPIED BY GM AND POST MUTIPLIED BY GMT WHERE GM IS 014960
    THE INPUT NOIESE MATRIX.
                                                                                 014970
                                                                               014980
      CHARACTER MSG-63
      COMMON /MAIN1/NDIM,NOIM1.COP1
     COMMON /MAINS/ COMS
                                                                                 015000
      COMMON /INOU/ KIN, KOUT, KPUNCH
                                                                                 015320
      CONKON /MAUNS/ MSG
      WEITE(KOUT,11)
                                                                             015040
      WRITE(KOUT, *) 'THIS ROUTINE PCCIFIES THE VALUE OF GM(OH) GMT
     1 USED IN CALCULATING THE KALPAN FILTER GAIN, PKFSS."
                                                                                 015050
                                                                               015 360
      WRITE(KOUT.*) "THE MODIFIED G IS = GM(QM)GMT+SQ*SQ(BM)V(BMT)WHERE
     I SO IS A SCALAR DESIGN PARAMETER AND V IS A POSITIVE DEFINITE
                                                                                 815376
     IMATRIX DESIGN PARAMETER. THE LARGER SQ, THE MORE POBUST THE CONTOC 15 280
                                                                                 815390
     1L SYSTEM WILL BE.
                                                                                015180
      DO 5 INP=1,10G0
                                                                                 015110
      WFITE(KOUT,11) *
                                                                                 615120
      FORMAT (A10./)
       WRITE(KOUT, *) ENTER 1-TO INPUT SQ, 2-TO INPUT V 3- TOCALCULATE MODELS 130
     11FIED QO. 4- TO EXIT THIS RCUTINE>
       READ (KIN, *) ISEL
                                                                                 915156
      GC TG (1,2,3,4) ISEL
       WRITE(KOUT, 11) . .
       WRITE(KOUT, *) 'ENTER SO>G-->'
                                                                                 015180
      READ (KIN, +) SO
                                                                                 015193
       GO TC 5
       WRITE(KOUT,11)
        HRITE (KOUT. *) 'V IS INIALIZED TO .ZERO UPON ENTRY INTO THIS OPTIO015220
       DO 7 I= 1. NOIM
                                                                               015240
```

	the control of the co		
	00 7 J=1,43IM	C 15 25 G	
	7 V(I,J)=0	815261	
	WRITE(KOUT,*) 'ENTER I/O OPTION FO- POSITIVE DEF V(SEE INPUT ROUTIM		
	MATISTROOT TO SHIER IN OPILER POP POSTITUE DEP VISES INFOTROOTIES	_	
	1E)>1	C 15 28 C	
		C15293	
	the second control of	015300	
_	NOT DESCRIPTION AND DESCRIPTION OF THE PROPERTY OF THE PROPERT		
		015316	
		C 15 3 2 G	
	3 CALL MATS(IRFM.ICEM.DM.V.WHS)	C15335]-	C
	C WM3=BH(V)BYT IRFN X IRFN	045743	·
	C HM3=BH(V)BMT IRFM X IRFM	015340 015350 015360	
	\$Q1=\$Q*\$Q	D15356	
	CALL MADD1(IRFM.IRFM.GOGT.WP3.V.SQ1)	0 15 36 0	
-	CALL MADD1 (IRFM, IRFM, GOST, MF3, V, SQ1) C V IRFM X IRFM NOW CONTAINS THE MOD. VALUE QG MSG="THE DOYLE AND STEIN MCCIFED QD MATRIX IS" IO=5	045 776	
	WAS THE BOUND AND COURT MATERIA BALLEY TO	012310	
	Mag INS DOLFS WAS 21514 AGELLED OR HALKIX 12.	81290	
	IO=5 GALL MMATIO(V.IRFM.IRFM.IC.KIN.KOUT.NOIM.NDIM) 5 GGNTINUE	£ 15 39 D	
	CALL MMATIC(V.IRFM.IRFM.IC.KIN.KOUT.NOIM.NOIM)	015400	
	E PONTTHIE	045.40	
		015410	
	4 GONTINUE C QQ IS ACCEPTABLE SO PUT INTO GOGT DG 26 I=1.IRFM	015420	
_	C QQ IS ACCEPTABLE SO PUT INTO GCGT	015430	
	OG 24 I=1, IRFM	015-40	
	DO EA GETATALE	315450	
	(L, I) v= (L, I) T9090S	C15465	
		615473	
		315488	
		815493	
		û 15 50 û	
	C THIS SUBROUTINE SETS UP THE NECESSARY INTEGRALS FOR USE BY	015510	
	C INE PERFERENCE WHEN WOUTHER THE STRIE IRRUSTITION HEIRTY	015523	
	C EXP(FA-TIME)=EAT, INTEG(EAT(GA) DA (GAT) EATT), AND	015530	
	C INTEG(EAT (9A)). WHE IS A DUMMY WORK SPACE	015540	
	REAL PHI(NDIM2, NDIM2), INTGA(NDIM2, NDIM2), INTBA(NDIM2, NDIM2),	RIESEC	
	. (SMION, SMION) AB, (SMION) AD, (SMICH, SMICH) AD, (SMICH, SMICH) AND 1	01555G 015560	
	1GA (hDI M2, NDIM2) ,FA (NDIM2, HDIM2)	015570	
	DIMENSION COM1(1) COM2(1)	015580	
	COMMCN/MAIN1/NOIM.NOIM1.COM1	615596	
	COMMON /MATNEY COME	045570	
	COMPCN / TADU/ KIN-KOUT-KPUNCH	012003	
	COMPCN /INDU/ KIN, KOUT, KPUNCH COMMCN /RNTIM/RNTIME, DELTIM COMMCN /MAINL/NOIMZ, NOIMZ	915 6 13	
	COMMON /RNTIM/RATIME.DELTIM	015620	
	COMMON ZMAT M. ZMOT MZ. MOT MZ	018630	
	ARREACH CARACACA - MACRO POR MI PRAMAL ROLTING		
	COMMON FRAINCE TO THE FOR KLIENMAN ROLTINE	015043	
	C	015650	
	NSAV 1= NIOH	0156£C	
		C15676	
	WELL TO MENT WE		
		815688	
	NOIH1=NOIH2+1	J15 69 C	
		G15780	
		015710	
		015720	
	CIMIDAD LATIBATION TORK TIDY RESIDENT IN MYS INVIDED	015730	
		015746	
	AND THIS IN A LINE OF THE CONTRACT OF THE CONT		
		015750	
	CALL INTEG(IRFA,FA,PHI,INTGA,DELTIH)	315 760	
	C PHI=EXP(FA) IRFA X IRFA	015770	
		015783	
	C	615790	
	NOIM=NSAV1	615500	
		C15610	
	the state of the s	315823	
	· END	015830	
	DECK DSCRTZ	615540	
		015857	
	GUSTONIAN GUNTATTIATTIATUN MENTATATATATATATATATATATATATATATATATATATA		
		015 96 3	
	19TD,9T,GCX,ICBM)	015873	
		C15380	
		615990	
	C AND PROVIDES AN EQUIVALENT DISCRETE TIME REPRESENTATION OF THE TOUTH	015 902	

```
C MUDEL FOR USE IN THE PERFAL ROUTINE
      REALAMI (NDIM.NDIM).PHIM (NCIM.NDIM).BOYD (NDIM.NDIM).
                                                                          615 92:
     1 BCZC(NDIM, NDIM), FC(NDIM, NDIP), BCY(NDIM, NDIM),
1 BCZ(NDIM, NDIM), PHIT(NDIM, NCIM), QTO(NDIM, NDIM),
1 BCZ(NDIM, NDIM), GT(NDIM, NDIM), GT(NDIM, NDIM),
                                                                          215 933
                                                                         015340
                                                                   315 96 0
     1 FT(NOIM.NOIM). BT(NOIM.NOIM).RTO (NOIM.NOIM).
     I GCX (NDIM, NDIM), RT (NDIM, NDIM)
      REAL COM1 (1), COM2 (1)
                                                                         SAFRAC
      CHARACTER MSG+1
    COMMON/MAIN1/NOIM, NOIM1.COM1
                                                                         016383
      COMMON/MAINS/ COM2
                                                                          016315
      COMMON/PAIN-/NOIM2.NDIM3
                                                                          016:24
      CORMON /INOU/KIN, KOUT, KPUNCH
      C1=1.0
      CALL IONT (IRFH. WM1.C1)
                                                                          8:6546
                                                                          016050
      CALL MADDI (IRFM, IRFM, WHI, FC, PHIM, DELTIM)
                                                                         016:62
C PHIM=I+FC(DELTIM) IST ORDER APPRCX TO STATE TRANS MATRIX OF CONT
                                                                         016370
                                                                       ___(16380
C CALCULATE GCX =-GCSTR
                                         C1=-1.3
                                                                          £1539C
    RECALL THAT GCSTR WAS PASSED INTO THIS ROUTINE IN BTD
                                                                      016100
016110
       CALL MSCALE (GCX.8TD.ICBP.IRFP.C1)
       C1=1.0
      CALL MSCALE (BCYD. ECY. IRFM. IRY. DELTIM)
                                                                         016133
    BCYD DISCRETE TIME APPROX OF BCY
       CALL MSCALE (BCZD.BCZ, IRFM. IRFP, DELTIP)
                                                                         016153
    BCZD DISCRETE TIME APPROX OF BCZ
                                                                      016163
       SHIGH = EVA 2H
                                                                         01617C
       MION =SHION
                                                                         016180
      CALL MYINTG (PHIT, QTD, BTD, MM1, GT, QT, FT, BT, IRFT, ICGT, ICGT, ICGT)
                                                                          316190
       EVARM=SMIGM
                                                                          016203
C PHIT-QTD BTD ARE EQUIV. DISCRETE TIME REPRESTATIONS OF TRUTH MODE
C MATRICE:
                                                                          616221
      WRITE(KOUT,+) .
                                                                          016230
     HRITE(KOUT, *) * WAS THE VALUE ENTERED IN RT DURING INPUT A CONTINUC216240 1US TIME OR A DISCRETE TIME VALUE? ENTER A C FOR CONTINUOUS , A 016250
          FOR DISCRETE VALUES!
                                                                         016260
       READ (KIN, 12) HSG
                                                                          616270
      FORMAT (A1)
12
                                                                         816283
      IF (MSG.EQ. 'C') THEN
                                                                         516293
      G163CC
GALL MSGALE(RTD-RT-)RHT-)RHT-C1)
ELSE
      C1=1/DELTIM
                                                                        _016326
       ELSE
       CALL EQUATE(RTO, RT, IRHT, IRHT)
                                                                          016 330
       END IF
C RTD IS THE DISCRETE TIME APPROX OF PT
                                                                         016358
      C1=1.0
                                                                         016363
      CALL IDAT (IRFT, WH1,C1)
                                                                          016379
C WM1=GTD = I
                                                                         516385
       ENO
                                                                          316393
      . DECK DLQGRS
      1 BTD.FM.BM.QM.GM.RM.HM.GT.QT.FT.BT.RT.HT.HXX.HUU.GCSTR.RKFSS.YD. 016-23
      1 IRY .IFLGCZ.HXU.HM1.HM2.HM3.HM4.HM5.HV1.HV21
                                                                          C16+3C
        SUBROUTINE FORMATS THE SAMPLED DATA CONTROLLER INTO THE FORMAT
                                                                          016443
C REQUIRED BY THE PERFORMANCE ANALYSIS ROUTINE
                                                                          016450
C THE FORMAT IS SPECIFIED IN THE COMMENT STATEMENTS IN THE CODE, AND
                                                                          016-60
C IN PORE DETAIL IN E. LLOYD S MASTERS THESIS. Del. AFIT.
      REAL COM1 (1), COM2 (1)
                                                                          016482
       REAL GCX (NDIM, NDIM), GCY (NDIM, NDIM), GCZ (NDIM, NDIM),
                                                                          416-93
      1BCY (NOIM, WOIM) . BCZ (NDIH, NDIM) . PHIT (NDIM, NDIM) .
                                                                          0165C3
      1 PHIC(NOIM.NOIM) . RTO(NOIM. RCIP) .GTD(NOIM. NOIM) .
                                                                          516513
      1QTO(NOIM, NOIM).9TO(NOIM, NOIF).FH(NOIM, NOIM).
                                                                          16523
     1 BM(NOIM, NDIM), QM(NOIM, NCIM), GM(NOIM, NOIM),
                                                                         316533
     1 MV1(NOIM), MV2(NOIM),
                                                                         016540
     1 RH(NDIM, NDIM), HM(NDIM, NDIM), GT(NDIM, NDIM),
                                                                         016553
      1 RACKOIA, NDIA) - HACKOIA, NDIA) - GCONDIA, NDIA) - D1656G
```

```
1 HT (NOIM, NOIM), HT (NOIM, NOIM), WAK (NOIM, NOIM).
                                                                                                                                                                                                       415574
           1 WUU (NJIM, NDIM), GCSTR (NDIM, NCIM), PKESS (NDIM, NOIM),
1 MKU (NDIM, NIOM), MMI (NDIM, NDIM), MMI (NDIM, NDIM),
1 MM3 (NDIM, NDIM), MM+ (NDIM, NDIM), MM5 (NDIM, NDIM)
                                                                                                                                                                                                        016 590
                 SEAL AD (MOIMS)
                                                                                                                                                                                                         116517
                INTEGER IFLGCZ
                                                                                                                                                                                                        316625
                 CH 4 74CT ERHSG*60 . MSG 1*1. MSG 2*1
                                                                                                                                                                                                        016634
                 COMMON /MAIMI/NDIM.NDIM1.COM1
                                                                                                                                                                                                        016540
                COMMON /MAINZ/COMZ
                COMMEN/INCU/KIN, KEUT, KPUNGH
                CC MACH /MAIN-/NOIH2.NDIH3
                COMMON/MAUNS/MSG
                CONPEN ZRNTIHZRNTINE.DELTIH
                                                                                                                                                                                                        116591
                 COMMEN/PAINS/ICET.ICEM.ICFA.ICGA.ICGM.ICGT.ICGA.IRFA.IRFM.IRFT. 016700
              1 IRHT, IRGA, IO, LOG, IRHM, NUMOTS
                 WRITE(KOUT,*) 'COLORED INPUT NOISE (Y OR N) >'
                 READ (KIN, 11) MSG
                                                                                                                                                                                                        016730
                  IHOLD= IRF#
                                                                                                                                                                                                       016743
                  IF (HSG.EQ. 'N') GO TO 25
                  CALL CHOISE (FM. GM. HM. 3M. OM. IRFN. IRHM. ICGN. IC3M. WHI. WMZ, WHI)
                 WRITE(KOUT, .) 'ENTER THE TOTAL RUN TIME AND SAMPLE TIME>'
25
                                                                                                                                                                                                        J16773
                READ(KIH.*)RHTHE.OELTIM
                     FORMAT (A1)
 C CALGULATE EQUIVALENT DISCRETE TIME VERSIONS OF, 3M--BMD, GH--GMD=1, 016300 C GM--QMO, AND PHIM THE STATE TRANSITION MATRIX FOR FM 016310
 C SINGE AGRKSPACE IS AT A PREMIUP. THE TRUTH MAGOEL MATRICES 316830
CPHIT. STORE OF THE CONTROLLER MODEL 316830
 C COUNTER PARTS DURING THIS ROUTINE SEFORE THE EQUIVALENT DISCRETE U16850 CTIME TRUTH MOCEL IS COMPUTED. AT THAT TIME THERE IS NO LONGEG ANY 016860 CTIME THOSE CONTROLLER MODEL MATRICE SINCE THE CONTROLLER IS PUT 016870 THE DESERTMENTS INVESTIGATION OF THE DESERTMENT OF
 Consequence and annual and annual and annual and annual and annual and annual a
                 NS443=NOINS
                 MIDN=SHION
                                                                                                                                                                                                        316910
                 CALL MYINTG(PHIT, GTD. BTD. RTC. GH. GF. FM. BH. IRFM. ICGF. ICBM. ICGM)
 C ATO IS USED AS DUMMY HORK SPACE IN CALL TO MYINTG
                 EVARN=SMION
                                                                                                                                                                                                        316 748
                  CALL CONTIERFH.GTO.1.003)
                                                                                                                                                                                                        016350
              WPITE(KOUT,*) 'ENTER A C IF THE VALUED ENTERED INTO RM IS A CONTING16960 10005 TIME VALUE TO FORM THE BASIS OF AN APPROXIMATE DISCRETE TIME 316970
              1 RM.ENTER A D OTHERWISE>" G16 380
                 READ (KIN, 11) MSG1
                 IF (MSG1.EQ. 'C') THEN
                                                                                                                                                                                                        017000
            APPROXINATE RHO=RH/SAPPLE TIME
                                                                                                                                                                                                    _ 017323
                 C1=1/05LT24
                  CALL MSCALE (RTO . RF , IRHM , IRHF , C1)
                  ELSE
        THE VALUE IN RM IS DISCRETE TIME ALREADY
                                                                                                                                                                                                        317353
                  CAL_ EQUATE(ATD.AM, IRHM. IRHM)
                                                                                                                                                                                                        017060
                  END IF
                                                                                                                                                                                                        617370
C SET UP A . S . AND U FOR DOTCON
                                                                                                                                                                                                        017383
                 CALL ASU (GCZ.GCY.PHIC.GCX.BCY.BCZ.RKFSS.HM1.HM2.HM3.HM4.HM5.
                                                                                                                                                                                                        017393
                                                                                                                                                                                                 017103
               1 FH. am. IHOLD. I Cam. WXX. WUU. WXU. PHIT)
 C GCZ NOW CONTAINS X, PHIC CONTAINS U.GCY CONTAINS C GCX.9CZ.ECY.RKFSS HERE CUMMY WORK AREAS IN XSU
                                                                                                                                                                                                        017120
                 CALL DOTCON (PHIT, HXX, GCX, GCZ, BTD, FHIC, RKFSS, BCY, BCZ, GCY, AUU, 01713)
          1GCSTR.IHOLD)
                 IF(IHOLG.EQ.IRFM) GO TO 35
                                                                                                                                                                                                        317153
                  ICH= IHOLD+1
                                                                                                                                                                                                        317160
                                                                                                                                                                                                                               A.C
                 00 33 1=1.1094
                                                                                                                                                                                                        017173
                 DO 30 Jaich, IRFM
                                                                                                                                                                                                         017181
                GCSTR(I,J)=0.
 30
                                                                                                                                                                                                        317193
 35
                                                                                                                                                                                                        017200
                CONTINUE
 CBCY.BCZ.GCY.PHIC.GCZ.GCX.RKFSS ARE USED AS DUMMY HOPK SPACE IN ODTCON 017213
```

MPITE(KOUT.+) 100 YOU HISH TO COMPUTE THE KALMAN FILTER GAIN OF PICD1722:

1K IT DIRECTLY (AS IN MAYBECK SECTION, 14.5) ENTER A C TO COMPUTE	201/23
inter A P to Pick it disectly>'	\$17.2~\$
READ (KIN.11) MSG2	317250
IF (PSG.:EG.'C') THEN	017263
CALL DKFTR (PHIT, BTD, GTD, GTD, GCX, RTD, HM, GCY, GCZ, PHIC, PKFSS, BCY, BC	
1FM.GF.QM.3M.WF1.WF2)	517269
CGCX,GCY,GCZ,BCZ,BCY ARE USED AS DUMMY WORK SPACE IN CALL TO CKFTR	017290
ELSE	217300
CALL PROTECTORY GCZ. HH. STD. RKFSS. ICAM. IRFM. IRHM)	217313
	_ 017321
END IF	017330
C+++++++++INTHE FOLLOHING CALCULATIONS, BCY.GCY.BCZ ARE DUMPY HOPK	
G ARES UNTIL THEIR LAST USE WHEN THEY ARE SET EQUAL TO THEIR	
C++++++TINAL VALUES FOR PERFAL SUEFOUTINE	017360
C1=1.0	611313
CALL IDNT(IRFM.BCY.C1)	017360
CALL MAT1 (RKFSS, HM, IRFM, IRFM, IRFM, GGY)	117393
	017400
CALL MADD: (IRFM, IRFM, 9CY, 8CZ, C1)	C17+15
C BCZ = I-RKFSS(HM)	617 420
HRITE (KOUT, *) * *	617433
HRITE(KOUT, *) *DO YOU WISH TO CALCULATE THE SAMPLED-DATA FILTEP	
10LES? Y OR N>'	017-50
REAC(KIN, 12) MSG	317463
IF (MSG.EQ.'Y') THEN	017470
CALL MAT1(PHIT.BCZ.IRFH.IRFM.PHIC)	617486
WRITE (KOUT, +) THE EIGENVALUES THAT CORRESPOND TO THE SAMPLED-DA	TAG17493
1 FILTER POLES ARE	817580
CALL MEIGN (PHIC. HV1, HV2, IRFM, HM1)	617513
END IF	317523
GALL MSCALE (BCY.GCSTR.ICBM.IRFM.C1) C BCY=-GCSTR ICBM X IRFM TE (MSCA.EO ACA) X X X X X X X X X X X X X X X X X X X	017530
C BCY=-GCSTR ICBM X IRFM	617543
1r 1m302.600."L") imin	G17550
C FORMULATE THE OPTIMAL CONTROL LAW FOR PERFAL	617565
All Matalogu ach tagu teru teru teru	817578
C GCX= -GCSTR(I-RKFSS(FM)) ICBF X IFRM	[1755]
GALL MAT1(BCY-RKESS-ICAM-TREM-TRIM-GC7)	217593
C GCZ= -GCSTR(RKFSS) ICBM X IRHN	617665
IFLGCZ=3	CT/OTS
44.4	
CALL MAT1(BTD.BCY.IRFH.ICBM.IRFH.GCSTR)	\$17623
CALL MAT1(BTD, BCY, IRFH, ICBM, IRFH, GCSTR) C1=1.0	617630
CALL MAT1(BTD,BCY,IRFH,ICBM,IRFH,GCSTR) C1=1.0 CALL MADD1(IRFH,IRFH,PHIT,GCSTR,BCY,C1)	017630 017640
CALL MAT1(BTD, BCY, IRFH, ICBM, IRFH, GCSTR) C1=1.0 CALL MADD1(IRFH, IRFH, PHIT, GCSTR, BCY, C1) C BCY= PHIT-BTD(GCTR) IRFH X IRFH	017633 017645 017650
CALL MAT1(BTD,BCY,IRFH,ICBM,IRFH,GCSTR) C1=1.0 CALL MADD1(IRFH,IRFH,PHIT,GCSTR,BCY,C1) C BCY= PHIT-BTD(GCTR) IRFH X IRFH WRITE(KOUT,*)**	017630 017640 017650 017660
CALL MAT1(BTD,BCY,IRFH,ICBM,IRFH,GCSTR) C1=1.0 CALL MADD1(IRFH,IRFH,PHIT,GCSTR,BCY,C1) C BCY= PHIT-BTD(GCTR) IRFH X IRFH HRITE(KOUT,+)* H	017630 017640 017650 017660 AL017670
CALL MAT1(BTD,BCY,IRFM,ICBM,IRFM,GCSTR) C1=1.0 CALL MADD1(IRFM,IRFM,PHIT,GCSTR,BCY,C1) C BCY= PHIT-BTD(GCTR) IRFM X IRFM HRITE(KOUT,+)* HRITE(KOUT,+)* 1 LQ SAMPLEO-DATA CCNTRCLLER? Y OR N>*	017630 017640 017650 017660 AL017670 017680
CALL MAT1(8T0,8CY,IRFH,IC8M,IRFH,GCSTR) C1=1.0 CALL MADD1(IRFH,IRFH,PHIT,GCSTR,9CY,G1) C BCY PHIT-BTD(GCTR) IRFH X IRFH HRITE(KOUT,*)** PRITE(KOUT,*)**OO YOU HISH TO CALCULATE THE POLES OF THE CPTIM 1 LO SAMPLEO-DATA CONTROLLER? Y OR N>* FEAD(KIN,12) MSG	017633 017645 017659 017663 AL017676 017683 017693
CALL MAT1(BTD, BCY, IRFM, ICBM, IRFM, GCSTR) C1=1.0 CALL MADD1(IRFM, IRFM, PHIT, GCSTR, BCY, C1) C BCY= PHIT-BTD(GCTR) IRFM X IRFM HRITE(KOUT, **) * * * * * * * * * * * * * * * * *	617630 617640 017650 617660 AL017670 017680 617690 617790
CALL MAT1(8TO, BCY, IRFH, IC8M, IRFH, GCSTR) C1=1.0 CALL MADD1(IRFH, IRFH, PHIT, GCSTR, 9CY, G1) C BCY PHIT-BTD(GCTR) IRFH X IRFH MRITE(KOUT, *) * 0 PRITE(KOUT, *) * 00 YOU HISH TO CALCULATE THE POLES OF THE OPTIM 1 LO SAMPLED-DATA CONTROLLER? Y OR N>* FEAD(KIN, 12) MSG IF (MSG, EQ. *Y*) THEN WRITE(KOUT, *) * THE EIGENVALUES THAT CORFESPOND TO THE FOLES OF	617633 017640 017650 017650 017663 AL017670 017683 017693 017730 TM01771C
CALL MAT1(8TD, BCY, IRFH, IC8M, IRFH, GCSTR) C1=1.0 CALL MADD1(IRFH, IRFH, PHIT, GCSTR, 9CY, G1) C BGY= PHIT-BTD(GGTR) IRFH X IRFH HRITE(KOUT, *) * 0 MRITE(KOUT, *) * 00 YOU HISH TO CALCULATE THE POLES OF THE CPTIM 1 LQ SAMPLED-DATA CONTROLLER? Y OR N>* FEAD(KIN, 12) MSG IF (MSG. EQ. *Y*) THEN HRITE(KOUT, *) * THE EIGENVALUES THAT CORFESPOND TO THE FOLES OF 1E OPTIMAL LQ CONTROLLER ARE	617630 017640 017650 017650 AL017670 017690 017690 017710 TM017710 017720
CALL MAT1(8T0,8CY,IRFH,IC8M,IRFH,GCSTR) C1=1.0 CALL MADD1(IRFH,IRFH,PHIT,GCSTR,9CY,G1) C BCY	617630 017640 017650 017660 AL017570 017580 017690 017700 TMC1771C 017720 G17730
CALL MAT1(8TD, BCY, IRFM, IC8M, IRFM, GCSTR) C1=1.0 CALL MADD1(IRFM, IRFM, PHIT, GCSTR, 9CY, G1) C BCY= PHIT-BTD(GCTR) IRFM X IRFM WRITE(KOUT, *) * OO YOU WISH TO CALCULATE THE POLES OF THE OPTIM 1 LO SAMPLED-DATA CONTROLLER? Y OR N>* FEAD(KIN, 12) MSG IF (MSG. EQ. *Y*) THEN WRITE(KOUT, *) *THE EIGENVALUES THAT CORFESPOND TO THE FOLES OF 1E OPTIMAL LO CONTROLLER ARE CALL MEIGN(BCY, WY1, MY2, IRFP, FHIC) END IF	617633 017643 017654 017663 AL017676 017683 017693 TMC1771C 017723 G17733
CALL MAT1(8TO, BCY, IRFM, IC8M, IRFM, GCSTR) C1=1.0 CALL MADD1(IRFM, IRFM, PHIT, GCSTR, 9CY, G1) C BCY= PHIT-BTD(GCTR) IRFM X IRFM WRITE(KOUT,*)** HRITE(KOUT,*)** 1 LQ SAMPLED-DATA CONTROLLER? Y OR N>* FEAD(KIN, 12) MSG IF (MSG. EQ.*Y*) THEN HRITE(KOUT,*)*THE EIGENVALUES THAT CORFESPOND TO THE FOLES OF 1E OPTIMAL LO CONTROLLER ARE* CALL MEIGN(BCY, WY1, MY2, IRFP, FHIC) END IF CALL MAT1(BCY, BCZ, I=FM, IRFM, IPFM, PHIC)	617630 017640 017654 017660 AL017676 017680 017690 017710 017720 017720 017730 017730
CALL MAT1(8TO,8CY,IRFM,IC8M,IRFM,GCSTR) C1=1.0 CALL MADD1(IRFM,IRFM,PHIT.GCSTR,9CY,G1) C BCY= PHIT-BTD(GCTR) IRFM X IRFM WRITZ(KOUT,*)* " PRITE(KOUT,*)* " 1 LQ SAMPLED-DATA CCNTRCLLER? Y OR N>" FEAD(KIN,12) MSG IF (MSG.EQ.*Y*) THEN RRITZ(KOUT,*)* THE EIGENVALUES THAT CORFESPOND TO THE FOLES OF 1E OPTIMAL LO CONTROLLER ARE" CALL MEIGN(BCY, WY1, MV2, IRFP, FHIC) END IF CALL MAT1(BCY, BCZ, IFFM, IRFM, IRFM, PHIC) C PHIC *(PMIT-STD(GCSTR))(I-RKFSS(HM)) IRFM X IPFM	617630 017640 017650 017660 AL017670 017690 017690 017710 017720 017730 017750 017760
CALL MAT1(8TO, BCY, IRFM, IC8M, IRFM, GCSTR) C1=1.0 CALL MADD1(IRFM, IRFM, PHIT, GCSTR, 9CY, G1) C BCY= PHIT-BTD(GCTR) IRFM X IRFM WRITE(KOUT, *) * * * * * * * * * * * * * * * * * *	617630 017640 017650 017660 AL017676 017680 017690 017710 017720 017720 017730 017750 017760
CALL MAT1(8TO, BCY, IRFM, IC8M, IRFM, GCSTR) C1=1.0 CALL MADD1(IRFM, IRFM, PHIT, GCSTR, 9CY, G1) C BCY= PHIT-BTO(GCTR) IRFM X IRFM WRITE(KOUT, *) * * * * * * * * * * * * * * * * * *	617630 017640 017650 017660 AL017670 017680 017780 017730 017730 017740 017760 017770 017770 017770
CALL MAT1(8TO, BCY, IRFM, IC8M, IRFM, GCSTR) C1=1.0 CALL MADD1(IRFM, IRFM, PHIT, GCSTR, 9CY, C1) C BCY= PHIT-BTD(GCTR) IRFM X IRFM WRITE(KOUT, *) * * * * * * * * * * * * * * * * * *	617630 017640 017654 017660 AL017670 017680 017780 017730 017730 017743 017760 017770 017770 017770 017770
CALL MAT1(8TO, BCY, IRFM, IC8M, IRFM, GCSTR) C1=1.0 CALL MADD1(IRFM, IRFM, PHIT, GCSTR, 9CY, C1) C BCY= PHIT-BTD(GCTR) IRFM X IRFM WRITE(KOUT, *) * * * * * * * * * * * * * * * * * *	617630 017640 017650 017660 AL017670 017680 017790 017730 017730 017730 017740 017760 017770 017770 017780 017780
CALL MAT1(8TO, BCY, IRFM, IC8M, IRFM, GCSTR) C1=1.0 CALL MADD1(IRFM, IRFM, PHIT, GCSTR, 9CY, C1) C BCY= PHIT-BTD(GCTR) IRFM X IRFM WRITE(KOUT, *) * * * * * * * * * * * * * * * * * *	617630 017640 017654 017660 AL017670 017680 017780 017730 017730 017743 017760 017770 017770 017770 017770
CALL MAT1(BTD, BCY, IPFM, ICBM, IRFM, GCSTR) C1=1.0 CALL MADD1(IRFM, IRFM, PHIT, GCSTR, 9CY, C1) C BCY= PHIT-BTD(GCTR) IRFM X IRFM MRITE(KOUT, *) ' ' MRITE(KOUT, *) ' OO YOU WISH TO CALCULATE THE POLES OF THE CPTIM 1 LQ SAMPLED-DATA CONTROLLER? Y OR N>' FEAD(KIN, 12) MSG IF (MSG, EQ. 'Y') THEN NRITE(KOUT, *) 'THE EIGENVALUES THAT CORFESPOND TO THE FOLES OF 1E OPTIMAL LQ CONTROLLER ARE' CALL MEIGN(BCY, WY1, WY2, IRFP, FHIC) END IF GALL MAT1(BCY, BCZ, IFFM, IRFM, IPFM, PHIC) C PHIC = (PMIT-BTD(GCSTR))(I-RKFSS(MM)) IRFM X IPFM CALL MAT1(BCY, RKFSS, IRFM, IRFP, IRMM, BCZ) C BCZ=(PHIT-ETD(GCSTR))RKFSS IRFP X IRMM ELSE C FORMULATE THE SUBOPTIMAL CONTROL LAW USTR=-GCSTR(X AT TSUB I HINUS GALL EQUATE(GCX, BCY, ICBP, IRFM) C GCX=-GCSTR ICBM X IRFM	617630 017640 017650 017650 AL017676 017690 017730 017730 017740 017776 017776 017776 017776 017776 0177780 017780 017610
CALL MAT1(BTD, BCY, IPFM, ICBM, IRFH, GCSTR) C1=1.0 CALL MADD1(IRFM, IRFH, PHIT, GCSTR, GCY, G1) C BCY= PHIT-BTD(GCTR) IRFH X IRFH MRITE(KOUT,*)*O YOU WISH TO CALCULATE THE POLES OF THE OPTIM 1 LQ SAMPLED-DATA CONTROLLER? Y OR N>* FEAD(KIN,12) MSG IF (MSG, EQ.*Y*) THEN HRITE(KOUT,*)*THE EIGENVALUES THAT CORFESPOND TO THE POLES OF 1E OPTIMAL LQ CONTROLLER ARE* CALL MEIGN(BCY, WY1, WY2, IRFP, FHIC) END IF CALL MAT1(BCY, BCZ, IFFM, IRFM, IPFM, PHIC) C PHIC =(PMIT-BTD(GCSTR))(I-RKFSS(HM)) IRFH X IPFM CALL MAT1(BCY, RKFSS, IRFH, IRFP, IRHM, BCZ) C BCZ=(PHIT-ETD(GCSTR))RKFSS IRFP X IRHK ELSE C FORMULATE THE SUBOPTIMAL CONTROL LAW USTR=-GCSTR(X AT TSUB I MINUS CALL MAT1(PHIT, BCZ, IRFM, IRFM, GCSTR) CALL MAT1(PHIT, BCZ, IRFM, IRFM, GCSTR)	617630 017650 017650 017650 AL017670 017690 017790 77710 017730 017750 017750 017770 017770 017770 017770 017780
CALL MAT1(BTD, BCY, IPFM, ICBM, IRFM, GCSTR) C1=1.0 CALL MADD1(IRFM, IRFM, PHIT, GCSTR, 9CY, C1) C BCY= PHIT-BTD(GCTR) IRFM X IRFM MRITE(KOUT, *) ' ' MRITE(KOUT, *) ' OO YOU WISH TO CALCULATE THE POLES OF THE CPTIM 1 LQ SAMPLED-DATA CONTROLLER? Y OR N>' FEAD(KIN, 12) MSG IF (MSG, EQ. 'Y') THEN NRITE(KOUT, *) 'THE EIGENVALUES THAT CORFESPOND TO THE FOLES OF 1E OPTIMAL LQ CONTROLLER ARE' CALL MEIGN(BCY, WY1, WY2, IRFP, FHIC) END IF GALL MAT1(BCY, BCZ, IFFM, IRFM, IPFM, PHIC) C PHIC = (PMIT-BTD(GCSTR))(I-RKFSS(MM)) IRFM X IPFM CALL MAT1(BCY, RKFSS, IRFM, IRFP, IRMM, BCZ) C BCZ=(PHIT-ETD(GCSTR))RKFSS IRFP X IRMM ELSE C FORMULATE THE SUBOPTIMAL CONTROL LAW USTR=-GCSTR(X AT TSUB I HINUS GALL EQUATE(GCX, BCY, ICBP, IRFM) C GCX=-GCSTR ICBM X IRFM	617630 017650 017650 017650 AL017676 017690 017790 77710 017730 017743 017760 017760 017760 017760 017760 017760 017780 017610 017620 017620
CALL MAT1(BTD, BCY, IRFN, ICBM, IRFN, GCSTR) C1=1.0 CALL MADD1(IRFN, IRFM, PMIT, GCSTR, BCY, C1) C BCY= PHIT-BTD(GCTR) IRFN X IRFN MRITE(KOUT, *) ** 00 YOU HISH TO CALCULATE THE POLES OF THE CPTIM 1 LG SAMPLED-DATA CONTROLLER? Y OR N>* FEAD(KIN, 12) MSG IF (MSG, GQ, *Y*) THEN NRITE(KOUT, *) ** THE EIGENVALUES THAT CORFESPOND TO THE FOLES OF 1E OPTIMAL LO CONTROLLER ARE* CALL MEIGN(BCY, WY1, MY2, IRFP, FHIC) END IF CALL MAT1(BCY, BCZ, IFFM, IRFM, IPFM, PMIC) C PHIC = (PMIT-ETD(GCSTR))(I-RKFSS(MM)) IRFM X IPFM CALL MAT1(BCY, RKFSS, IRFN, IRFP, IRMH, BCZ) C BCZ=(PMIT-ETD(GCSTR))RKFSS IRFP X IRMK ELSE C FORMULATE THE SUBOPTIMAL CONTROL LAW USTR=-GCSTR(X AT TSUB I MINUS CALL EQUATE(GCX, BCY, ICBP, IRFP) C GCX=-GCSTR ICBM X IRFM CALL MAT1(PMIT, BCZ, IRFM, IRFM, BCSTR) C1=1.0 CALL MAT1(BTO, GCX, IRFM, ICBM, IRFM, BCY) WRITE(KOUT, *) **	617630 017650 017650 017660 AL017670 017690 017690 017710 017730 017730 017740 017760 017760 017760 017760 017760 017760 017610 017630 017630 017650
CALL MAT1(8TD, BCY, IRFM, IC8M, IRFM, GCSTR) C1=1.0 CALL MADD1(IRFM, IRFM, PMIT, GCSTR, 9CY, C1) C BCY= PHIT-BTD(GCTR) IRFM X IRFM WRITE(KOUT,*)**ON YOU WISH TO CALCULATE THE POLES OF THE CPTIM 1 LO SAMPLED-DATA CONTROLLER? Y OR N>* FEAD(KIN, 12) MSG IF (MSG, EQ. 'Y') THEN WRITE(KOUT,*)*THE EIGENVALUES THAT CORFESPOND TO THE FOLES OF 1E OPTIMAL LO CONTROLLER ARE* CALL MEIGN(BCY, WV1, MV2, IRFP, FHIC) END IF CALL MAT1(BCY, BCZ, IFFM, IRFM, IPFM, PHIC) C PHIC = (PMIT-PTD(GCSTR))*(I-RKFSS, (MM)) IRFM X IPFM CALL MAT1(BCY, RKFSS, IRFM, IRFP, IRMM, BCZ) C BCZ=(PMIT-ETD(GCSTR))*RKFSS IRFP X IRMM ELSE C FORMULATE THE SUBOPTIMAL CONTROL LAM USTP=-GCSTR(X AT TSUB I MINUS CALL EQUATE(GCX, BCY, IC8P, IRFP) C GCX=-GCSTR IC3M X IRFM CALL MAT1(PMIT, BCZ, IRFM, IRFM, BCSTR) CALL MAT1(PMIT, BCZ, IRFM, IRFM, BCSTR) CALL MAT1(PMIT, BCZ, IRFM, IRFM, BCSTR) CALL MAT1(BTO, GCX, IRFM, IRFM, BCSTR)	617630 017650 017650 017660 AL017670 017690 017690 017710 017730 017730 017740 017760 017760 017760 017760 017760 017760 017610 017630 017630 017650

	READ(KIN.12)MSG
	IF (MSG.ED. TY) THEN
	CALL MADD1(IRFM, IRFM, PHIT, ECY, PHIC, C1)
	WRITE(KOUT,*) "THE EIGENVALUES THAT CORRESPOND TO THE POLES OF THE
	10PTIMAL LQ CONTROLLER ARE
	CALL MEIGN (PHIC, MV1. WV 2, IRFF, HM1)
	END IF
-	CALL MADD1 (IRFM, IRFM, GCST, DECY, PHIC, C1)
-	HIC="P+IT(I-RKFS?(H+))=BTD,GCSTF
	CZ=PHLT(ZKFSS) IZFP X IEHP
0	DO 114 T-4 TOEM
	00 1613=1,124H
11	GCZ(I, J)=0
=.	IFLGCZ=1
	END IF
	IRY=1
	DG 1G2 I=1,NDIM
	DO 162 J=1.1RY
	F(T_J)=0
32	BCY (I.J)=0
	DC 167 I=1,1000
7	YD(I)=J
	10=5
	MSG= PHIC FOR THE SAMPLED DATA CONTROLLER IS CALL MMATIO(PHIC, IRFM, IRFF, IO, KIN, KOUT, NDIM, NDIM)
	WRITE(KOUT,*)* *
	WRITE(KOUT, *) 'DO YOU WANT TO CALCULATE THE EIGENVALUES OF THE LOG
	1 CONTROLLER STATE TRANSITION MATRIX, PHIC? Y OR N>"
	READ(KIN, 12) MSG
	IF (PSG.EQ. 'Y') THEN
	WRITE(KOUT,*) THE EIGENVALUES OF THE LQG CONTROLLER STATE TRANSITY
	CALL MEIGN (PHIC, NV1, NV2, IRFF, NN1)
	END IF
	MSG="BCZ FOLLOWS, BCY=0"
	CALL MMATIO(BCZ, IRFM, IRMM, IC, KIN, KGUT, NDIM, NDIM)
	MSG="GCX FOR THE SAPPLED DATA CONTROLLER IS" CALL MMATIO(GCX, IC9M, IRFM, IC, KIN, KOUT, NDIM, NDIM)
	IF (PSG2.EQ. "C") THEN
	HSG= GCZ FOR A COMPUTED KFSS'
	ELSE
	MSG= "GCZ FOR KFSS PICKED DIRECTLY"
	END IF
	CALL MMATIO(GCZ, ICBM, IRMM, IC, KIN, KOUT, NOIM, NOIM)
	WRITE(KOUT,-)' GCY IS SET = 0'
T	HIS IS A REGULATOR SO VO IS ALWAYS ZERC
	NS AV 3= NOI = 2
	NDIMZ=NOIM
_	CALL MYINTG(PHIT, QTD, STD, RTC, GT, QT, FT, ST, IRFT, ICGT, ICBT, ICGT)
R	TO IS USED AS DUMMY WORK SPACE IN CAL TO MYINTG
_	NDIM & NSAV3
PH	IT, OTO . STO ARE EQUIV. DISCRETE TIME REPRESTATIONS OF TRUTH MODL
MA	TRICE
- •	WRITE(KOUT,+)''
	WRITE(KOUT,+) " WAS THE VALUE ENTERED IN RT DURING INPUT A CONTINU
	TUS TIME OR A DISCRETE TIME VALUE? ENTER A C FOR CONTINUOUS . A
	1 D FOR DISCRETE VALUE>
	READ (KIN, 12) MSG
2	
	IF (MSG.EQ.'C') THEN
	C1=1/DELTIM
	CALL MSCALE (KTD of To IRMT of K FT C1)
	ELSE
-	CALL EQUATE (PTO.RT.IRHT.IPHT)
	ENO IF

C RTO IS THE DISCRETE TIME APPROX OF FT	しょうちょ
C1*1.1	148561
CALL IDNT(IRFT,GTD,C1)	019573
C GTD=GTU = I	016563
PETUAN	018591
	24444
END	
* DECK DKFTR	618613
SUBROUTINE OKFTR (FHIP, BMO, GPO, QMO, WM1, RMO, HM, WM3	LAMSANNE-FKESS. 018620
1 FZ.HZ.FN.GH.QN.BP.HHZ.WH-)	018633
T. Chich, usanidaida. Anusania.	
	G18643
C THIS ROUTINE CALCULATE THE STEADY STATE HALMAN	
C FOR A SAMPLED ATA CONTROLLER	C1866;
REAL PHIM(NOIM. NOIM). SHO(NOIP. NOIK) . GHO (NOIK, NOI	k). C1867.
A CANALA MATALLANDIA MATALLANDIA MATALLANDIA	R/4 0100/L
1 GMO (NDIM, NDIM) . HF1 (NDIM, NDIM) .RHO (NDIM, NCIM) .	018683
1 HM (NDIR, NDIM), HM3 (NDIM, NDIP), HM5 (NDIM, NDIM)	, (1869:
1 MM6 (NDIK, NDIK) . RKFSS (NCIP, NDIM) . FZ(NDIP, NDIM)	018700 016710
4 MOINTH MOTHS EMISOTH MOTES	046740
	010710
1 GH (NDIH, NDIH), GH (N CIM, NDIH), 2H (NDIH, NDIH),	010/27
1 WM2 (MIGM, MIGM, (MIGM, HIGM)	018733
	015740
And the Control of th	C1875C
8511 604111 6042111	
REAL COM1(1).COM2(1)	018760
COMMON /MAIN1/MDIM, NDIM1, CCM1	018776
COMMON /INOU/ KIN.KOUT.KPUNCH	018760
COMMON /RATIM/ RATIME.DELTIM	618794
	94000
COMMCN/PAIN-/NDIM2, NDIM3	018900
COMMCN/MAUN5/MSG	01661 0
COMMON /MAINZ/ GOM2	016929
COPMON /MAIN6/ICET.ICBM.ICFA.ICGA.ICGM.ICGT.ICG	ATREA TOEM TOET . PIRETT
1 IRHT, IRQA, IO, LQG, IRMM, NUMOTS	G16540
CHARAGTER MSG1+1.MSG+60	C18650
C DELETE DETERMINISTIC STATES AS IN THE CONTINUOUS TI	ME CASE C18863
MRITE(KOUT,+) "IF YOU PLAN TO USE THE DOYLE AND S	TETN TECHNIQUE FORGIAATA
**************************************	155 1 150 111 10 10 10 10 10
4 TUTE BIN YOU MAY UTCH TO MERTEY THE HALLIE OF HE	INCTO THE MIMBER ACCORD
1 THIS RUN YOU MAY HISH TO HEDIFY THE VALUE OF NU	
1F DETERMINISTIC STATES. DO YOU WANT TO CHANGE N	
1F DETERMINISTIC STATES. DO YOU WANT TO CHANGE N READ (KIN-11) MSG1	UMOTS? Y CR N>'018493 C1890G
1F DETERMINISTIC STATES. DO YOU WANT TO CHANGE N READ (KIA, 11) MSG1 NUMSAV=NUMDTS	016910 V CR N> 016993 016900 016910
1F OETERMINISTIC STATES. DO YOU WANT TO CHANGE N READ(KIA,11)MSG1 NUMSAV=NUMDTS IF (MSG1.EO."Y") THEN	016910
1F OETERMINISTIC STATES. DO YOU WANT TO CHANGE N READ (KIA, 11) MSG1 NU YSAV=NUMDTS IF (MSG1.EQ. "Y") THEN WRITE(KOUT. ") 'ENTER THE NEW VALUE OF NUMDTS FOR	C16999 (010099) (016999) (016999) (016999) (016999) (01692) (016929) (016939) (016939)
1F OETERMINISTIC STATES. DO YOU WANT TO CHANGE N READ (KIA, 11) MSG1 NU YSAV=NUMDTS IF (MSG1.EQ. "Y") THEN WRITE(KOUT. ") 'ENTER THE NEW VALUE OF NUMDTS FOR	C16999 (010099) (016999) (016999) (016999) (016999) (01692) (016929) (016939) (016939)
1F DETERMINISTIC STATES. DO YOU WANT TO CHANGE N READ (KIA, 11) MSG1 NUMSAV=NUMDTS IF (MSG1.EO."Y") THEN WRITE(KOUT, ") 'ENTER THE NEW VALUE OF NUMDTS FOR READ (KIN.") NUMDTS	THIS RUN> CR N> 016690 016900 016910 016920 018920 018930 018940
1F DETERMINISTIC STATES. DO YOU WANT TO CHANGE N READ (KIA, 11) MSG1 NUMSAV=NUMDTS IF (MSG1.EO."Y") THEN WRITE(KOUT, ") 'ENTER THE NEW VALUE OF NUMDTS FOR READ (KIN, ") MUMDTS END IF	THIS RUN> 0 N> 016693 016916 016916 016923 THIS RUN> 016938 016956
1F DETERMINISTIC STATES. DO YOU WANT TO CHANGE NEAD (KIA.11) MSG1 NUMSAV=NUMDTS IF (MSG1.EO."Y") THEN HRITE(KOUT.*) 'ENTER THE NEW VALUE OF NUMDTS FOR READ (KIN.*) NUMDTS END IF HRITE(KOUT.*) 'NUMDTS= ", NUMDTS	THIS RUN> '01890 018900 016910 018921 018930 018950 018960
1F DETERMINISTIC STATES. DO YOU WANT TO CHANGE NEAD (KIA.11) MSG1 NUMSAV=NUMDTS IF (MSG1.EO."Y") THEN HRITE(KOUT.*) 'ENTER THE NEW VALUE OF NUMDTS FOR READ (KIN.*) NUMDTS END IF HRITE(KOUT.*) 'NUMDTS= ", NUMDTS	THIS RUN> '01890 018900 016910 018921 018930 018950 018960
1F DETERMINISTIC STATES. DO YOU WANT TO CHANGE NEAD (KIA.11) HSG1 NU 4SAV= NUHDTS IF (HSG1.EQ."Y") THEN WEITE(KOUT,") 'ENTER THE NEW VALUE OF NUHDTS FOR READ (KIN.") NUHDTS END IF WRITE(KOUT,") 'NUHDTS= ', NUHDTS IDS= NUHDTS+1 IRF2=IRFH-NUHDTS	IUMDTS? Y CR N>'018890 C18900 018910 018921 TMIS RUN>' 018930 C18940 018960 018960 018980
1F DETERMINISTIC STATES. DO YOU WANT TO CHANGE NEAD (KIA, 11) MSG1 NUMSAVENUMDTS IF (MSG1.EO."Y") THEN WRITE(KOUT, ") 'ENTER THE NEW VALUE OF NUMDTS FOR READ (KIN, ") MUMDTS END IF WRITE(KOUT, ") 'NUMDTS= ", NUMDTS IDS=NUMDTS+1 IRF2=IRFH-NUMDTS	THIS RUN> CR N> 018893 018906 018923 018923 018936 018946 018950 018967 018962 018962 018962 018962
1F DETERMINISTIC STATES. DO YOU WANT TO CHANGE NEAD (KIA, 11) MSG1 NUMSAVENUMDTS IF (MSG1.EO."Y") THEN WRITE(KOUT, ") 'ENTER THE NEW VALUE OF NUMDTS FOR READ (KIN, ") MUMDTS END IF WRITE(KOUT, ") 'NUMDTS= ", NUMDTS IDS=NUMDTS+1 IRF2=IRFH-NUMDTS	THIS RUN> CR N> 018893 018906 018923 018923 018936 018946 018950 018967 018962 018962 018962 018962
1F DETERMINISTIC STATES. DO YOU WANT TO CHANGE NEAD (KIA.11) MSG1 NUMSAV=NUMDTS IF (MSG1.EQ."Y") THEN WRITE(KOUT.") 'ENTER THE NEW VALUE OF NUMDTS FOR READ (KIN.") NUMDTS END IF WRITE(KOUT.") 'NUMDTS= ', NUMDTS IOS=NUMDTS+1 IRF2=IRFM-NUMDTS IF (NUMDTS.EQ.C) THEN C STORE SYSTEM MODEL IN INTERMEDIATE MATRICES COMPATI	IUMDTS? Y CR N>'01899 018900 018923 018930 018930 018940 018960 018960 018960 018980 018980 018980 018980 018980 018980 018980 018980
1F DETERMINISTIC STATES. DO YOU WANT TO CHANGE NEAD (KIA.11) MSG1 NUMSAV=NUMDTS IF (MSG1.EQ."Y") THEN WRITE(KOUT.") 'ENTER THE NEW VALUE OF NUMDTS FOR READ (KIN.") NUMDTS END IF WRITE(KOUT.") 'NUMDTS= '.NUMDTS IDS=NUMDTS+1 IRF2=IRFM-NUMDTS IF (NUMDTS.EQ.C) THEN C STORE SYSTEM MODEL IN INTERMEDIATE MATRICES COMPATIC	IUMDTS? Y CR N>'016990 016916 016916 018923 THIS RUN>' 018930 018946 018950 018967 018985 018985 018985 018985 018985 018985 018985 018985 018985
1F DETERMINISTIC STATES. DO YOU WANT TO CHANGE NEAD (KIA.11) MSG1 NUMSAV=NUMDTS IF (MSG1.EQ."Y") THEN WRITE(KOUT.") 'ENTER THE NEW VALUE OF NUMDTS FOR READ (KIN.") NUMDTS END IF WRITE(KOUT.") 'NUMDTS= ', NUMDTS IDS=NUMDTS+1 IRF2=IRFM-NUMDTS IF (NUMDTS.EQ.C) THEN C STORE SYSTEM MODEL IN INTERMEDIATE MATRICES COMPATION OF THE CALL EQUATE(F2.PHIM.IRF2.IRF2)	IUMDTS? Y CR N>'01899 018900 018923 018930 018930 018940 018960 018960 018960 018980 018980 018980 018980 018980 018980 018980 018980
1F DETERMINISTIC STATES. DO YOU WANT TO CHANGE NEAD (KIA.11) MSG1 NUMSAV=NUMDTS IF (MSG1.EQ."Y") THEN WRITE(KOUT.") 'ENTER THE NEW VALUE OF NUMDTS FOR READ (KIN.") NUMDTS END IF WRITE(KOUT.") 'NUMDTS= ', NUMDTS IDS=NUMDTS+1 IRF2=IRFM-NUMDTS IF (NUMDTS.EQ.C) THEN C STORE SYSTEM MODEL IN INTERMEDIATE MATRICES COMPATION OF THE CALL EQUATE(F2.PHIM.IRF2.IRF2)	IUMDTS? Y CR N>'016990 016916 016916 018923 THIS RUN>' 018930 018946 018950 018967 018985 018985 018985 018985 018985 018985 018985 018985 018985
1F DETERMINISTIC STATES. DO YOU WANT TO CHANGE NEAD (KIA.11) MSG1 NUMSAV=NUMDTS IF (MSG1.EQ."Y") THEN WRITE(KOUT.") 'ENTER THE NEW VALUE OF NUMDTS FOR READ (KIN.") NUMDTS END IF WRITE(KOUT.") 'NUMDTS= ', NUMDTS IDS=NUMDTS+1 IRF2=IRFM-NUMDTS IF (NUMDTS.EQ. 3) THEN C STORE SYSTEM MODEL IN INTERMEDIATE MATRICES COMPATICE C WITH THOSE BELOW. WHEN THER ARE DETERMINISTIC STATES CALL EQUATE(MY1.GMD.IPF2.IRF2) CALL EQUATE(WY1.GMD.IPF2.IRF2)	IUMDTS? Y CR N>'01899 018906 018923 018930 018930 018950 018950 018967 018967 018967 01896 01896 01896 018970 018980 01900 01900 01900 01900 01900 01900
1F DETERMINISTIC STATES. DO YOU WANT TO CHANGE NEAD (KIA.11) MSG1 NUMSAV=NUMDTS IF (MSG1.EQ."Y") THEN WRITE(KOUT.") 'ENTER THE NEW VALUE OF NUMDTS FOR READ (KIN.") NUMDTS END IF WRITE(KOUT.") 'NUMDTS= ', NUMDTS IDS=NUMDTS+1 IRF2=IRFM-NUMDTS IF (NUMDTS.EQ. 3) THEN C STORE SYSTEM MODEL IN INTERMEDIATE MATRICES COMPATICE C WITH THOSE BELOW. WHEN THER ARE DETERMINISTIC STATES CALL EQUATE(MY1.GMD.IPF2.IRF2) CALL EQUATE(WY1.GMD.IPF2.IRF2)	IUMDTS? Y CR N>'01899 018906 018923 018930 018930 018950 018950 018967 018967 018967 01896 01896 01896 018970 018980 01900 01900 01900 01900 01900 01900
1F OETERMINISTIC STATES. DO YOU WANT TO CHANGE NEAD (KIA.11) MSG1 NUMSAV=NUMDTS IF (MSG1.EO."Y") THEN WRITE(KOUT.") 'ENTER THE NEW VALUE OF NUMDTS FOR READ (KIN.") NUMDTS END IF WRITE(KOUT.") 'NUMDTS= ", NUMDTS IOS=NUMDTS+1 IRF2=IRFM-NUMDTS IF (NUMDTS.EQ.C) THEN C STORE SYSTEM MODEL IN INTERMEDIATE MATRICES COMPATI C WITH THOSE BELON. WHEN THER ARE DETERMINISTIC STATES CALL EQUATE(F2.PMIM.IRF2.IRF2) CALL EQUATE(M1.GMO.IPF2.IRF2) CALL EQUATE(M1.GMO.IPF2.IRF2) CALL EQUATE(M1.GMO.IPF2.IRF2) CALL EQUATE(M1.GMO.IPF2.IRF2)	IUMDTS? Y CR N>'01890 018906 018921 018920 018930 018950 018950 018960 018970 018980 018980 018980 018980 018900 019010 019020 019030 019050
1F OETERMINISTIC STATES. DO YOU WANT TO CHANGE NEAD (KIA.11) MSG1 NUMSAV=NUMDTS IF (MSG1.EO."Y") THEN WRITE(KOUT.") 'ENTER THE NEW VALUE OF NUMDTS FOR READ (KIN.") NUMDTS END IF WRITE(KOUT.") 'NUMDTS= ", NUMDTS IOS=NUMDTS+1 IRF2=IRFM-NUMDTS IF (NUMDTS.EQ.C) THEN C STORE SYSTEM MODEL IN INTERMEDIATE MATRICES COMPATI C WITH THOSE BELON. WHEN THER ARE DETERMINISTIC STATES CALL EQUATE(F2.PMIM.IRF2.IRF2) CALL EQUATE(M1.GMO.IPF2.IRF2) CALL EQUATE(M1.GMO.IPF2.IRF2) CALL EQUATE(M1.GMO.IPF2.IRF2) CALL EQUATE(M1.GMO.IPF2.IRF2)	IUMDTS? Y CR N>'01890 018906 018921 018920 018930 018950 018950 018960 018970 018980 018980 018980 018980 018900 019010 019020 019030 019050
1F OETERMINISTIC STATES. DO YOU WANT TO CHANGE NEAD (KIA.11) MSG1 NUMSAV=NUMDTS IF (MSG1.EQ."Y") THEN WRITE(KOUT.") 'ENTER THE NEW VALUE OF NUMDTS FOR READ (KIN.") NUMDTS END IF WRITE(KOUT.") 'NUMDTS= ', NUMDTS IOS=NUMDTS+1 IRF2=IRFN-NUMDTS IF (NUMDTS.EQ. C) THEN C STORE SYSTEM MODEL IN INTERMEDIATE MATRICES COMPATIC WITH THOSE BELOW, WHEN THER ARE DETERMINISTIC STATES CALL EQUATE(F2.PHIM.IRF2.IRF2) CALL EQUATE(WM1.GMD.IPF2.IRF2) CALL EQUATE(WM1.GMD.IPF2.IRF2) CALL EQUATE(WM5.GMD.IRF2.IRF2) CALL EQUATE(WM5.GMD.IRF2.IRF2) EALL EQUATE(WM2.GPD.IRF2.IRF2)	IUMDTS? Y CR N>'018990 018900 018910 018920 018930 018940 018960 018960 018970 018980 018980 018980 018980 018980 018980 019010 019020 019020 019020 019020 019020 019020 019020 019020 019020 019020
1F OETERMINISTIC STATES. DO YOU WANT TO CHANGE NEAD (KIA.11) MSG1 NUMSAV=NUMDTS IF (MSG1.EQ."Y") THEN WRITE(KOUT.") 'ENTER THE NEW VALUE OF NUMDTS FOR READ (KIN.") NUMDTS END IF WRITE(KOUT.") 'NUMDTS= ', NUMDTS IOS=NUMDTS+1 IRF2=IRFN-NUMDTS IF (NUMDTS.EQ. C) THEN C STORE SYSTEM MODEL IN INTERMEDIATE MATRICES COMPATIC WITH THOSE BELOW, WHEN THER ARE DETERMINISTIC STATES CALL EQUATE(F2.PHIM.IRF2.IRF2) CALL EQUATE(WM1.GMD.IPF2.IRF2) CALL EQUATE(WM1.GMD.IPF2.IRF2) CALL EQUATE(WM5.GMD.IRF2.IRF2) CALL EQUATE(WM5.GMD.IRF2.IRF2) EALL EQUATE(WM2.GPD.IRF2.IRF2)	IUMDTS? Y CR N>'018990 018900 018910 018920 018930 018940 018960 018960 018970 018980 018980 018980 018980 018980 018980 019010 019020 019020 019020 019020 019020 019020 019020 019020 019020 019020
IF DETERMINISTIC STATES. DO YOU WANT TO CHANGE NEAD (KIA.11) MSG1 NU MSAV=NUMDTS IF (MSG1.EQ."Y") THEN WRITE(KOUT.") 'ENTER THE NEW VALUE OF NUMDTS FOR READ (KIN.") NUMDTS END IF WRITE(KOUT.") 'NUMDTS= ', NUMDTS IF(KOUT.") 'NUMDTS= ', NUMDTS IF(NUMDTS.EQ.C) THEN C STORE SYSTEM MODEL IN INTERMEDIATE MATRICES COMPATIC WITH THOSE BELOW, WHEN THER ARE DETERMINISTIC STATES CALL EQUATE(F2.PHIM.IRF2.IRF2) CALL EQUATE(WM1.GMD.IPF2.IRF2) CALL EQUATE(WM5.BMD.IRF2.ICPM) CALL EQUATE(WM5.BMD.IRF2.ICPM) CALL EQUATE(WM2.GPD.IRF2.IRF2) ELSE C DELETE THE DETERMINISTIC STATES FORM THE MODEL USED	IUMDTS? Y CR N>'018990 018900 018920 018920 018930 018950 018950 018960 018970 018980 018980 018980 018980 018930 019010 019020 019030 019050 019050 019050 019070
IF OETERMINISTIC STATES. DO YOU WANT TO CHANGE NEAD (KIA.11) MSG1 NU MSAV=NUMDTS IF (MSG1.EQ."Y") THEN WRITE(KOUT.") 'ENTER THE NEW VALUE OF NUMDTS FOR READ (KIN.") NUMDTS END IF WRITE(KOUT.") 'NUMDTS= ", NUMDTS IF (NUMDTS.EQ. C) THEN C STORE SYSTEM MODEL IN INTERMEDIATE MATRICES COMPATION OF SYSTEM MODEL USED CALL EQUATE(MM1.GMD.IPF2.IRF2) CALL EQUATE(MM1.GMD.IPF2.IRF2) CALL EQUATE(MM2.GPD.IRF2.IRF2) ELSE C DELETE THE DETERMINISTIC STATES FORM THE MODEL USED C THE STEADY STATE KALMAN FILTER GAIN MATRIX	IUMDTS? Y CR N>'01890 018900 016910 018921 018930 018950 018960 018960 018960 018960 018960 018970 018980 018980 018980 018980 019000 019000 019000 019000 019000 019000 019000 019000 019000 019000 019000 019000 019000 019000
IF DETERMINISTIC STATES. DO YOU WANT TO CHANGE NEAD (KIA.11) MSG1 NU MSAV=NUMDTS IF (MSG1.EQ."Y") THEN WEITE(KOUT.") 'ENTER THE NEW VALUE OF NUMDTS FOR READ (KIN.") NUMDTS END IF MRITE(KOUT.") 'NUMDTS= ", NUMDTS IF (NUMDTS.EQ. 3) THEN C STORE SYSTEM MODEL IN INTERMEDIATE MATRICES COMPATIC HITH THOSE BELOW. WHEN THER ARE DETERMINISTIC STATES CALL EQUATE(MY1.GMD.IPF2.IRF2) CALL EQUATE(MY1.GMD.IPF2.IRF2) CALL EQUATE(MY1.GMD.IPF2.IRF2) CALL EQUATE(MY3.GMD.IRF2.IRF2) COLL EQUATE(MY3.GMD.IRF2.IRF2)	IUMDTS? Y CR N>'018990
IF OETERMINISTIC STATES. DO YOU WANT TO CHANGE NEAD (KIA.11) MSG1 NU MSAV=NUMDTS IF (MSG1.EQ."Y") THEN WRITE(KOUT.") 'ENTER THE NEW VALUE OF NUMDTS FOR READ (KIN.") NUMDTS END IF WRITE(KOUT.") 'NUMDTS= ", NUMDTS IF (NUMDTS.EQ. C) THEN C STORE SYSTEM MODEL IN INTERMEDIATE MATRICES COMPATION OF SYSTEM MODEL USED CALL EQUATE(MM1.GMD.IPF2.IRF2) CALL EQUATE(MM1.GMD.IPF2.IRF2) CALL EQUATE(MM2.GPD.IRF2.IRF2) ELSE C DELETE THE DETERMINISTIC STATES FORM THE MODEL USED C THE STEADY STATE KALMAN FILTER GAIN MATRIX	IUMDTS? Y CR N>'01890 018900 016910 018921 018930 018950 018960 018960 018960 018960 018960 018970 018980 018980 018980 018980 019000 019000 019000 019000 019000 019000 019000 019000 019000 019000 019000 019000 019000 019000
IF OETERMINISTIC STATES. DO YOU WANT TO CHANGE NEAD (KIA.11) MSG1 NU MSAV=NUMDTS IF (MSG1.EQ."Y") THEN WEITE(KOUT.") 'ENTER THE NEW VALUE OF NUMDTS FOR READ (KIN.") NUMDTS END IF WRITE(KOUT.") 'NUMDTS= ", NUMDTS IF(NUMDTS+1) IRF2=IRFN-NUMDTS IF(NUMDTS.EQ.C) THEN C STORE SYSTEM MODEL IN INTERMEDIATE MATRICES COMPATIC MITH THOSE BELON. WHEN THER ARE DETERMINISTIC STATES CALL EQUATE(F2.PHIM.IRF2.IRF2) CALL EQUATE(WM1.GMD.IPF2.IRF2) CALL EQUATE(MM2.GMD.IPF2.IRF2) CALL EQUATE(MM5.BMD.IRF2.ICQM) CALL EQUATE(MM5.BMD.IRF2.IRF2) ELSE C DELETE THE DETERMINISTIC STATES FORM THE MODEL USED OF STEADY STATE KALMAN FILTER GAIN MATRIX DC 2112 I=105.IRFP	IUMDTS? Y CR N>'018990
IF OETERMINISTIC STATES. DO YOU WANT TO CHANGE NEAD (KIA.11) MSG1 NUMSAV=NUMDTS IF (MSG1.EQ."Y") THEN WRITE(KOUT.") 'ENTER THE NEW VALUE OF NUMDTS FOR READ (KIN.") NUMDTS END IF MRITE(KOUT.") 'NUMDTS= ".NUMDTS IF (NUMDTS.EQ. 2) THEN C STORE SYSTEM MODEL IN INTERMEDIATE MATRICES COMPATIC HITH THOSE BELOW. WHEN THER ARE DETERMINISTIC STATES CALL EQUATE(MT.GMO.IPF2.IRF2) CALL EQUATE(WM1.GMO.IPF2.IRF2) CALL EQUATE(WM2.GMO.IRF2.IRF2) CALL EQUATE(MM2.GMO.IRF2.IRF2) CALL EQUATE(MM2.GMO.IRF2.IRF2) CALL EQUATE(MM2.GMO.IRF2.IRF2) CALL EQUATE(MM2.GMO.IRF2.IRF2) CALL EQUATE(MM2.GMO.IRF2.IRF2) COLL EQUATE(MM2.GMO.IRF2.IRF2)	IUMDTS? Y CR N>'018990
IF OETERMINISTIC STATES. DO YOU WANT TO CHANGE NEAD (KIA.11) MSG1 NUMSAV=NUMDTS IF (MSG1.EQ."Y") THEN WRITE(KOUT.") 'ENTER THE NEW VALUE OF NUMDTS FOR READ (KIN.") NUMDTS END IF HRITE(KOUT.") 'NUMDTS= ", NUMDTS IF (NUMDTS.EQ. C) THEN C STORE SYSTEM MODEL IN INTERMEDIATE MATRICES COMPATIC WITH THOSE BELOW. WHEN THER ARE DETERMINISTIC STATES CALL EQUATE(F2.PHIM.IRF2.IRF2) CALL EQUATE(WM1.GMO.IPF2.IRF2) CALL EQUATE(WM1.GMO.IPF2.IRF2) CALL EQUATE(MM5.GMD.IRF2.IRF2) CALL EQUATE(MM5.GMD.IRF2.IRF2) CALL EQUATE(MM2.GPD.IRF2.IRF2) COLL EQUATE(MM2.GPD.IRF2.IRF2) COLL ETE THE DETERMINISTIC STATES FORM THE MODEL USED OF STEADY STATE KALMAN FILTER GAIN MATRIX DC 2112 I=10S.IRFP JJ=J-NUMDTS	IUMDTS? Y CR N>'018990
IF OETERMINISTIC STATES. DO YOU WANT TO CHANGE NEAD (KIA, 11) MSG1 NU MSAV=MUNDTS IF (MSG1.EQ. "Y") THEN WRITE(KOUT, ") 'ENTER THE NEW VALUE OF NUMDTS FOR READ (KIN, ") NUMDTS END IF WRITE(KOUT, ") 'NUMDTS= ", NUMDTS IDS=NUMDTS+1 IRF2=IRFM-NUMDTS IF (NUMDTS.EQ. 0) THEN C STORE SYSTEM MODEL IN INTERMEDIATE MATRICES COMPATIC HITH THOSE BELOW, WHEN THER ARE DETERMINISTIC STATES CALL EQUATE(M2, PHIM, IRF2, IRF2) CALL EQUATE(WM1, GMO, IPF2, IRF2) CALL EQUATE(WM5, 8MD, IPF2, IRF2) CALL EQUATE(WM5, 8MD, IRF2, IRF2) CALL EQUATE(WM5, 8MD, IRF2, IRF2) CALL EQUATE(WM2, OPD, IRF2, IRF2) COLL EQUATE(WM2, OPD, IRF2, IRF2) COLL EQUATE(WM2, OPD, IRF2, IRF2) INSTEADY STATE KALMAN FILTER GAIN MATRIX DC 2112 I=105, IRFP II=-MUNDTS DO 2112 J=IDS, IRFP JJ=J-NUMDTS 2112 MM+(II, JJ)=FM(I, J)	IUMDTS? Y CR N>'018990
IF DETERMINISTIC STATES. DO YOU WANT TO CHANGE NEAD (KIN, 11) MSG1 NU MSAV=NUMDTS IF (MSG1.EQ. "Y") THEN WRITE(KOUT, ") "ENTER THE NEW VALUE OF NUMDTS FOR READ (KIN, ") NUMDTS END IF WRITE(KOUT, ") "NUMDTS ", NUMDTS IF (NUMDTS.EQ. 3) THEN C STORE SYSTEM MODEL IN INTERMEDIATE MATRICES COMPATE OF HIT HISSES BELOW, WHEN THER ARE DETERMINISTIC STATES CALL EQUATE(F2, PHIM, IRF2, IRF2) CALL EQUATE(H41, GMD, IPF2, IRF2) CALL EQUATE(H42, HM, IRHM, IRF2) CALL EQUATE(H45, BMD, IRF2, ICSM) CALL EQUATE(H45, BMD, IRF2, IRF2) CALL EQUATE(M42, QPD, IRF2, IRF2) ELSE C DELETE THE DETERMINISTIC STATES FORM THE MODEL USED OF THE STEADY STATE KALMAN FILTER GAIN MATRIX OC 2112 I=IDS, IRFP II=:-NUMDTS DO 2112 J=IDS, IRFP JJ=J-NUMDTS 2112 MM+(II, JJ) =FM(I, J) DO 2113 I=1, IRMM	IUMDTS? Y CR N>'018990
IF DETERMINISTIC STATES. DO YOU WANT TO CHANGE NEAD (KIA, 11) MSG1 NU MSAV=NUMOTS IF (MSG1.EQ. "Y") THEN WRITE(KOUT, *) "ENTER THE NEW VALUE OF NUMDTS FOR READ (KIN, *) NUMDTS END IF WRITE(KOUT, *) "NUMDTS= ".NUMDTS IDS=NUMDTS+1 IRF2=IRFN-NUMDTS IF (NUMDTS.EQ. 2) THEN C STORE SYSTEM MODEL IN INTERMEDIATE MATRICES COMPATI C WITH THOSE BELOW, WHEN THER ARE DETERMINISTIC STATES CALL EQUATE (***I, GMO, IPF2, IRF2) CALL EQUATE (***I, GMO, IPF2, IRF2) CALL EQUATE (***M**I, GMO, IRF2, IRF2) CALL EQUATE (***M**I, GM	IUMDTS? Y CR N>'018990
IF DETERMINISTIC STATES. DO YOU WANT TO CHANGE NEAD (KIN,11) MSG1 NUMSAVENUMDTS IF (MSG1.EO."Y") THEN WRITE(KOUT,") "ENTER THE NEW VALUE OF NUMDTS FOR READ (KIN,") NUMDTS END IF WRITE(KOUT,") "NUMDTS= ",NUMDTS IOS=NUMDTS+1 IRF2=IRFM-NUMDTS IF (NUMDTS.EQ.3) THEN C STORE SYSTEM MODEL IN INTERMEDIATE MATRICES COMPATIC HITH THOSE BELOW, WHEN THER ARE DETERMINISTIC STATES CALL EQUATE(F2.PHIM.IRF2.IRF2) CALL EQUATE(HM1.GMO.IPF2.IRF2) CALL EQUATE(HM1.GMO.IPF2.IRF2) CALL EQUATE(HM2.GMD.IRF2.IRF2) CALL EQUATE(HM2.GMD.IRF2.IRF2) ELSE C DELETE THE DETERMINISTIC STATES FORM THE MODEL USED C THE STEADY STATE KALMAN FILTER GAIN MATRIX DC 2112 I=IOS.IRFP II=:-MUMDTS DO 2113 J=IOS.IRFP JJ=J-NUMDTS 2112 MM+(II.JJ) =FM(I.J) DO 2113 J=IOS.IRFP	IUMDTS? Y CR N>'018990
IF DETERMINISTIC STATES. DO YOU WANT TO CHANGE NEAD (KIN, 11) MSG1 NUMSAV=NUMDTS IF (MSG1.EO.*Y*) THEN WRITE(KOUT,*) *ENTER THE NEW VALUE OF NUMDTS FOR READ (KIN,*) NUMDTS END IF WRITE(KOUT,*) *NUMDTS= *,NUMDTS IOS=NUMDTS+1 IRF2=IRFM-NUMDTS IF (NUMDTS.EO.3) THEN C STORE SYSTEM MODEL IN INTERMEDIATE MATRICES COMPATIC MITH THOSE BELOW, WHEN THER ARE DETERMINISTIC STATES CALL EQUATE(H2, PMIM, IRF2, IRF2) CALL EQUATE(H41, GMO, IPF2, IRF2) CALL EQUATE(H2, PM, IRHM, IRF2) CALL EQUATE(H2, PM, IRHM, IRF2) CALL EQUATE(MM2, QPD, IRF2, IRF2) CALL EQUATE(MM2, QPD, IRF2, IRF2) C DELETE THE DETERMINISTIC STATES FORM THE MODEL USED C THE STEADY STATE KALMAN FILTER GAIN MATRIX DC 2112 I=IOS, IRFP IJ=J-NUMDTS DO 2113 J=IOS, IRFP JJ=J-NUMDTS 2112 WH+(II, JJ) =FM (I, J) DO 2113 J=IOS, IRFP JJ=J-NUMDTS	IUMDTS? Y CR N>'018990
IF DETERMINISTIC STATES. DO YOU WANT TO CHANGE NEAD (KIN,1) MSG1 NUMSAVENUMDTS IF (MSG1.EQ."Y") THEN WRITE(KOUT.") "ENTER THE NEW VALUE OF NUMBES FOR READ (KIN,") NUMBES END IF WRITE(KOUT.") "NUMBES ", NUMBES IF (MUMDTS-1 IRF2=IRFM-NUMBTS IF (MUMDTS.EQ.3) THEN G STORE SYSTEM MODEL IN INTERMEDIATE MATRICES COMPATE C WITH THOSE BELOW, WHEN THER ARE DETERMINISTIC STATES GALL EQUATE(#41,6MD.IPF2.IRF2) CALL EQUATE(M41,6MD.IPF2.IRF2) CALL EQUATE(M42,6MD.IRF2.IC6M) CALL EQUATE(M42,6MD.IRF2.IC6M) CALL EQUATE(M42,0MD.IRF2.IC6M) CALL EQUATE(M42,0MD.IRF2.IRF2) C DELETE THE DETERMINISTIC STATES FORM THE MODEL USED C THE STEADY STATE KALMAN FILTER GAIN MATRIX DC 2112 I=IDS.IRFP JJ=J-NUMDTS 2112 MM+(II.J)=FM(I.J) DO 2113 J=IDS.IRFP JJ=J-NUMDTS J=J-NUMDTS J=J-NUMDTS Z113 M2(I,JJ)=MM(I,J)	IUMDTS? Y CR N>'018990
IF DETERMINISTIC STATES. DO YOU WANT TO CHANGE NEAD (KIN, 11) MSG1 NUMSAV=NUMDTS IF (MSG1.EO.*Y*) THEN WRITE(KOUT,*) *ENTER THE NEW VALUE OF NUMDTS FOR READ (KIN,*) NUMDTS END IF WRITE(KOUT,*) *NUMDTS= *,NUMDTS IOS=NUMDTS+1 IRF2=IRFM-NUMDTS IF (NUMDTS.EO.3) THEN C STORE SYSTEM MODEL IN INTERMEDIATE MATRICES COMPATIC MITH THOSE BELOW, WHEN THER ARE DETERMINISTIC STATES CALL EQUATE(H2, PMIM, IRF2, IRF2) CALL EQUATE(H41, GMO, IPF2, IRF2) CALL EQUATE(H2, PM, IRHM, IRF2) CALL EQUATE(H2, PM, IRHM, IRF2) CALL EQUATE(MM2, QPD, IRF2, IRF2) CALL EQUATE(MM2, QPD, IRF2, IRF2) C DELETE THE DETERMINISTIC STATES FORM THE MODEL USED C THE STEADY STATE KALMAN FILTER GAIN MATRIX DC 2112 I=IOS, IRFP IJ=J-NUMDTS DO 2113 J=IOS, IRFP JJ=J-NUMDTS 2112 WH+(II, JJ) =FM (I, J) DO 2113 J=IOS, IRFP JJ=J-NUMDTS	IUMDTS? Y CR N>'018990

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0. 211; J.1		II=I-NU-DTS	119216
2115 MM3[II], J188H(I], J1 0 0 211 + 1175.7FF			
DO 211-1275.IFFP III=NUMDTS CC 2265 211- WHI(II.) = CC 115.25 212- WHI(II.) = CC 115.25 213- WHI(II.) = CC 115.25 214- WHI(II.) = CC 115.25 215- WHI(II.) = CC 115.25 215- WHI(II.) = CC 115.25 216- WHI(II.) = CC 115.25 217- WHI(II.) = CC 115.25 218- WHI(II.) = CC 115.25 219- WHI(II.) = CC 115.25 211- WHI	2115		
II = - NUMOTS			
NS.Webuiler			
NS.Webuiler		11-1-40-013	619290
NS.Webuiler		UL EILO J-11UGA	119201
NS.Webuiler	2114	11.11.12.11.11.11.11.11.11.11.11.11.11.1	113270
EALL IDNT[FF2,MH.CI] END IF C CALCULATE G40 (040) GHOT CALL MATS(1272,17F2,MH1,MH2,RKFSS) CREFSS IS CUMMY MORK SPACE AT THIS FOINT IN THE PROGRAM WRITE(AUUT.") TO YOU MISH TO HOLOFY THE CHO MATRIX BY THE DOYLE C1939: 1 AND STEIN TECHNIQUE FOR CONTINUOUS TIME CONTROLLERS EXTENDED TO (19-06) 1 THE DISGRETE TIME SYSTEMS, Y OF N>' READ(KIN,11)*SG1 FRAD(KIN,11)*SG1 IF (RSG.CO.Y**) THEN CALL DASZ(BMIJOS,IDS),RKFSS,MMI,ICBM,MH3,IRF2,MH6) CALL DASZ(BMIJOS,IDS),RKFSS,MMI,ICBM,MH3,IRF2,MH6) CALCULATE THE KALMAN FILTER GAINS, RKFSS, FCR EITHER THE HOUIFIED (19-60) CALCULATE THE KALMAN FILTER GAINS, RKFSS, FCR EITHER THE HOUIFIED (19-60) COMD IS STORED IN RKFSS CALL TRANSZ(TRHM,IRF2,MH3) COLULATE THE KALMAN FILTER GAINS, RKFSS, FCR EITHER THE HOUIFIED (19-60) CALCULATE THE WAMODIFIED QND CALL TRANSZ(TRHM,IRF2,MH3) COLULATE THE WAMODIFIED OND CALL TRANSZ(TRHM,IRF2,MH3,FKPSS,MH4,MH6,MM1,MH5) COLULATE THE WAMODIFIED OND CALL TRANSZ(TRHM,IRF2,MH3,FKPSS,MH4,MH6,MM1,MH5) COLULATE THE WAMODIFIED OND CALL KFLTATIFF2,IRHN,FZ,MH3,FKPSS,MH4,MH6,MM1,MH5) COLULATE THE WAMODIFIED OND COLULATE THE WAMODI	11	PURMATEAL	119280
EALL IDNT[FF2,MH.CI] END IF C CALCULATE G40 (040) GHOT CALL MATS(1272,17F2,MH1,MH2,RKFSS) CREFSS IS CUMMY MORK SPACE AT THIS FOINT IN THE PROGRAM WRITE(AUUT.") TO YOU MISH TO HOLOFY THE CHO MATRIX BY THE DOYLE C1939: 1 AND STEIN TECHNIQUE FOR CONTINUOUS TIME CONTROLLERS EXTENDED TO (19-06) 1 THE DISGRETE TIME SYSTEMS, Y OF N>' READ(KIN,11)*SG1 FRAD(KIN,11)*SG1 IF (RSG.CO.Y**) THEN CALL DASZ(BMIJOS,IDS),RKFSS,MMI,ICBM,MH3,IRF2,MH6) CALL DASZ(BMIJOS,IDS),RKFSS,MMI,ICBM,MH3,IRF2,MH6) CALCULATE THE KALMAN FILTER GAINS, RKFSS, FCR EITHER THE HOUIFIED (19-60) CALCULATE THE KALMAN FILTER GAINS, RKFSS, FCR EITHER THE HOUIFIED (19-60) COMD IS STORED IN RKFSS CALL TRANSZ(TRHM,IRF2,MH3) COLULATE THE KALMAN FILTER GAINS, RKFSS, FCR EITHER THE HOUIFIED (19-60) CALCULATE THE WAMODIFIED QND CALL TRANSZ(TRHM,IRF2,MH3) COLULATE THE WAMODIFIED OND CALL TRANSZ(TRHM,IRF2,MH3,FKPSS,MH4,MH6,MM1,MH5) COLULATE THE WAMODIFIED OND CALL TRANSZ(TRHM,IRF2,MH3,FKPSS,MH4,MH6,MM1,MH5) COLULATE THE WAMODIFIED OND CALL KFLTATIFF2,IRHN,FZ,MH3,FKPSS,MH4,MH6,MM1,MH5) COLULATE THE WAMODIFIED OND COLULATE THE WAMODI		NSAV=NOIMZ	C1929C
EALL IDNT[FF2,MH.CI] END IF C CALCULATE G40 (040) GHOT CALL MATS(1272,17F2,MH1,MH2,RKFSS) CREFSS IS CUMMY MORK SPACE AT THIS FOINT IN THE PROGRAM WRITE(AUUT.") TO YOU MISH TO HOLOFY THE CHO MATRIX BY THE DOYLE C1939: 1 AND STEIN TECHNIQUE FOR CONTINUOUS TIME CONTROLLERS EXTENDED TO (19-06) 1 THE DISGRETE TIME SYSTEMS, Y OF N>' READ(KIN,11)*SG1 FRAD(KIN,11)*SG1 IF (RSG.CO.Y**) THEN CALL DASZ(BMIJOS,IDS),RKFSS,MMI,ICBM,MH3,IRF2,MH6) CALL DASZ(BMIJOS,IDS),RKFSS,MMI,ICBM,MH3,IRF2,MH6) CALCULATE THE KALMAN FILTER GAINS, RKFSS, FCR EITHER THE HOUIFIED (19-60) CALCULATE THE KALMAN FILTER GAINS, RKFSS, FCR EITHER THE HOUIFIED (19-60) COMD IS STORED IN RKFSS CALL TRANSZ(TRHM,IRF2,MH3) COLULATE THE KALMAN FILTER GAINS, RKFSS, FCR EITHER THE HOUIFIED (19-60) CALCULATE THE WAMODIFIED QND CALL TRANSZ(TRHM,IRF2,MH3) COLULATE THE WAMODIFIED OND CALL TRANSZ(TRHM,IRF2,MH3,FKPSS,MH4,MH6,MM1,MH5) COLULATE THE WAMODIFIED OND CALL TRANSZ(TRHM,IRF2,MH3,FKPSS,MH4,MH6,MM1,MH5) COLULATE THE WAMODIFIED OND CALL KFLTATIFF2,IRHN,FZ,MH3,FKPSS,MH4,MH6,MM1,MH5) COLULATE THE WAMODIFIED OND COLULATE THE WAMODI		NDINZ=NDIH	C19366
EALL IDNT[FF2,MH.CI] END IF C CALCULATE G40 (040) GHOT CALL MATS(1272,17F2,MH1,MH2,RKFSS) CREFSS IS CUMMY MORK SPACE AT THIS FOINT IN THE PROGRAM WRITE(AUUT.") TO YOU MISH TO HOLOFY THE CHO MATRIX BY THE DOYLE C1939: 1 AND STEIN TECHNIQUE FOR CONTINUOUS TIME CONTROLLERS EXTENDED TO (19-06) 1 THE DISGRETE TIME SYSTEMS, Y OF N>' READ(KIN,11)*SG1 FRAD(KIN,11)*SG1 IF (RSG.CO.Y**) THEN CALL DASZ(BMIJOS,IDS),RKFSS,MMI,ICBM,MH3,IRF2,MH6) CALL DASZ(BMIJOS,IDS),RKFSS,MMI,ICBM,MH3,IRF2,MH6) CALCULATE THE KALMAN FILTER GAINS, RKFSS, FCR EITHER THE HOUIFIED (19-60) CALCULATE THE KALMAN FILTER GAINS, RKFSS, FCR EITHER THE HOUIFIED (19-60) COMD IS STORED IN RKFSS CALL TRANSZ(TRHM,IRF2,MH3) COLULATE THE KALMAN FILTER GAINS, RKFSS, FCR EITHER THE HOUIFIED (19-60) CALCULATE THE WAMODIFIED QND CALL TRANSZ(TRHM,IRF2,MH3) COLULATE THE WAMODIFIED OND CALL TRANSZ(TRHM,IRF2,MH3,FKPSS,MH4,MH6,MM1,MH5) COLULATE THE WAMODIFIED OND CALL TRANSZ(TRHM,IRF2,MH3,FKPSS,MH4,MH6,MM1,MH5) COLULATE THE WAMODIFIED OND CALL KFLTATIFF2,IRHN,FZ,MH3,FKPSS,MH4,MH6,MM1,MH5) COLULATE THE WAMODIFIED OND COLULATE THE WAMODI		CALL MYINTG(F2.4M2.4M5.4M6.4M1.GM.4M4.4M3.1RF2.IGGM.IGBM.IGGM)	619316
EALL IDNT[FF2,MH.CI] END IF C CALCULATE G40 (040) GHOT CALL MATS(1272,17F2,MH1,MH2,RKFSS) CREFSS IS CUMMY MORK SPACE AT THIS FOINT IN THE PROGRAM WRITE(AUUT.") TO YOU MISH TO HOLOFY THE CHO MATRIX BY THE DOYLE C1939: 1 AND STEIN TECHNIQUE FOR CONTINUOUS TIME CONTROLLERS EXTENDED TO (19-06) 1 THE DISGRETE TIME SYSTEMS, Y OF N>' READ(KIN,11)*SG1 FRAD(KIN,11)*SG1 IF (RSG.CO.Y**) THEN CALL DASZ(BMIJOS,IDS),RKFSS,MMI,ICBM,MH3,IRF2,MH6) CALL DASZ(BMIJOS,IDS),RKFSS,MMI,ICBM,MH3,IRF2,MH6) CALCULATE THE KALMAN FILTER GAINS, RKFSS, FCR EITHER THE HOUIFIED (19-60) CALCULATE THE KALMAN FILTER GAINS, RKFSS, FCR EITHER THE HOUIFIED (19-60) COMD IS STORED IN RKFSS CALL TRANSZ(TRHM,IRF2,MH3) COLULATE THE KALMAN FILTER GAINS, RKFSS, FCR EITHER THE HOUIFIED (19-60) CALCULATE THE WAMODIFIED QND CALL TRANSZ(TRHM,IRF2,MH3) COLULATE THE WAMODIFIED OND CALL TRANSZ(TRHM,IRF2,MH3,FKPSS,MH4,MH6,MM1,MH5) COLULATE THE WAMODIFIED OND CALL TRANSZ(TRHM,IRF2,MH3,FKPSS,MH4,MH6,MM1,MH5) COLULATE THE WAMODIFIED OND CALL KFLTATIFF2,IRHN,FZ,MH3,FKPSS,MH4,MH6,MM1,MH5) COLULATE THE WAMODIFIED OND COLULATE THE WAMODI		NDINZ= NSAV	C1932i
EALL IDNT[FF2,MH.CI] END IF C CALCULATE G40 (040) GHOT CALL MATS(1272,17F2,MH1,MH2,RKFSS) CREFSS IS CUMMY MORK SPACE AT THIS FOINT IN THE PROGRAM WRITE(AUUT.") TO YOU MISH TO HOLOFY THE CHO MATRIX BY THE DOYLE C1939: 1 AND STEIN TECHNIQUE FOR CONTINUOUS TIME CONTROLLERS EXTENDED TO (19-06) 1 THE DISGRETE TIME SYSTEMS, Y OF N>' READ(KIN,11)*SG1 FRAD(KIN,11)*SG1 IF (RSG.CO.Y**) THEN CALL DASZ(BMIJOS,IDS),RKFSS,MMI,ICBM,MH3,IRF2,MH6) CALL DASZ(BMIJOS,IDS),RKFSS,MMI,ICBM,MH3,IRF2,MH6) CALCULATE THE KALMAN FILTER GAINS, RKFSS, FCR EITHER THE HOUIFIED (19-60) CALCULATE THE KALMAN FILTER GAINS, RKFSS, FCR EITHER THE HOUIFIED (19-60) COMD IS STORED IN RKFSS CALL TRANSZ(TRHM,IRF2,MH3) COLULATE THE KALMAN FILTER GAINS, RKFSS, FCR EITHER THE HOUIFIED (19-60) CALCULATE THE WAMODIFIED QND CALL TRANSZ(TRHM,IRF2,MH3) COLULATE THE WAMODIFIED OND CALL TRANSZ(TRHM,IRF2,MH3,FKPSS,MH4,MH6,MM1,MH5) COLULATE THE WAMODIFIED OND CALL TRANSZ(TRHM,IRF2,MH3,FKPSS,MH4,MH6,MM1,MH5) COLULATE THE WAMODIFIED OND CALL KFLTATIFF2,IRHN,FZ,MH3,FKPSS,MH4,MH6,MM1,MH5) COLULATE THE WAMODIFIED OND COLULATE THE WAMODI		C1=1.0	C19338
C CALCULATE GO (0-0) GMOT CALL HAT3 (13F2,18F2, WHI, WH2, RKFSS) CRMFSS IS CUMMY WORK SPACE AT THIS POINT IN THE PROGRAM WRITE (ACULT)* OO YOU WISH TO HOLDER THE CMD WATRIX BY THE DOYLE (1398) 1 AND STEIN TECHNIQUE FOR CONTINUOUS TIME CONTROLLERS EXTENDED TO (1398) 1 THE DISCRETE TIME SYSTEMS, Y OF M>' READ (KI), 111NSG1 IF (MSG.; CO.*Y') THEN CALL DASC RHIUDS, IDS), RKFSS, MMI, ICBM, MM3, IRF2, WM6) CRETURNS A MODIFIED GMO VALUE TO BE USED IN FINDING AKFSS CALL DASC RHIUDS, IDS), RKFSS, MMI, ICBM, MM3, IRF2, WM6) COUNTY OF THE UNMODIFIED GMO VALUE TO BE USED IN FINDING AKFSS CALCULATE THE KALMAN FI.TER GALKS, RKFSS, FCR EITHER THE HOURFIED CALCULATE THE KALMAN FI.TER GALKS, RKFSS, FCR EITHER THE HOURFIED COUNTY OF THE UNMODIFIED GMO COUNTY OF THE WORK OF THE THE THE HOURFIED COUNTY OF THE UNMODIFIED GMO COUNTY OF THE WORK OF THE THE THE HOURFIED COUNTY OF THE WORK OF THE THE THE HOURFIED COUNTY OF THE WORK OF THE THE THE HOURFIED COUNTY OF THE WORK OF THE THE THE HOURFIED COUNTY OF THE THE THE THE THE THE HOURFIED COUNTY OF THE THE THE THE THE THE HOURFIED COUNTY OF THE THE THE THE THE THE HOURFIED COUNTY OF THE THE THE THE THE THE HOURFIED COUNTY OF THE THE THE THE THE THE THE HOURFIED COUNTY OF THE THE THE THE THE THE THE HOURFIED COUNTY OF THE THE THE THE THE THE THE HOURFIED COUNTY OF THE THE THE THE THE THE THE THE HOURFIED COUNTY OF THE THE THE THE THE THE THE THE THE HOURFIED COUNTY OF THE		CALL IDNI(IRF2.WM1.C1)	619345
1 AND STEIN TECHNIQUE FOR CONTINUOUS TIME CONTROLLERS EXTENDED TO 19-00 1 THE DISCRETE TIME SYSTEMS, Y OF No? READ (KIN:11)MSG1 19192 IF (MSG:20.77) THEN 19192 CALL DASZ (BANTIDS:)DS:,RKFSS.MM1.ICBM.MM3.IRFZ.MM6) 019-32 019		END IF	G19350
1 AND STEIN TECHNIQUE FOR CONTINUOUS TIME CONTROLLERS EXTENDED TO 19-00 1 THE DISCRETE TIME SYSTEMS, Y OF No? READ (KIN:11)MSG1 19192 IF (MSG:20.77) THEN 19192 CALL DASZ (BANTIDS:)DS:,RKFSS.MM1.ICBM.MM3.IRFZ.MM6) 019-32 019	C CAL	CULATE G10 (C1D) GNDT	01936)
1 AND STEIN TECHNIQUE FOR CONTINUOUS TIME CONTROLLERS EXTENDED TO 19-00 1 THE DISCRETE TIME SYSTEMS, Y OF No? READ (KIN:11)MSG1 19192 IF (MSG:20.77) THEN 19192 CALL DASZ (BANTIDS:)DS:,RKFSS.MM1.ICBM.MM3.IRFZ.MM6) 019-32 019		CALL MATS (IRF2.IRF2.WM1.WM2.RKFSS)	C19375
1 AND STEIN TECHNIQUE FOR CONTINUOUS TIME CONTROLLERS EXTENDED TO 19-00 1 THE DISCRETE TIME SYSTEMS, Y OF No? READ (KIN:11)MSG1 19192 IF (MSG:20.77) THEN 19192 CALL DASZ (BANTIDS:)DS:,RKFSS.MM1.ICBM.MM3.IRFZ.MM6) 019-32 019	CRKFS	S IS CUMMY WORK SPACE AT THIS FOINT IN THE PROGRAM	219383
1 AND STEIN TECHNIQUE FOR CONTINUOUS TIME CONTROLLERS EXTENDED TO 1 THE DISCRETE TIME SYSTEMS, Y OF N>' READ(KIN-11)MSG1 (IF (MSG1-260-47*) THEN CALL DASZ(BMIIDS,IDS),RKFSS,HM1,ICBM,HM3,IRFZ,HM6) CALL DASZ(BMIIDS,IDS),RKFSS,HM1,ICBM,HM3,IRFZ,HM6) CORTURNS A MODIFIED ORD VALUE TO BE USED IN FINDING RKFSS END IF COALGULATE THE KALMAN FILTER GAINS, RKFSS, FCR EITHER THE MODIFIED COMD IS STORED IN RKFSS COALGULATE THE KALMAN FILTER GAINS, RKFSS, FCR EITHER THE MODIFIED COMD IS STORED IN RKFSS COALGULATE THE KALMAN FILTER GAINS, RKFSS, FCR EITHER THE MODIFIED COMD IS STORED IN RKFSS COALGULATE THE KALMAN FILTER GAINS, RKFSS, FCR EITHER THE MODIFIED COMP IS STORED IN RKFSS COALGULATE THE KALMAN FILTER GAINS, RKFSS, FCR EITHER THE MODIFIED COALGULATE THE MANDIFIED COALGULATE THE MANDIFIED COALGULATE THE MANDIFIED COALGULATER TO THE COALGULATER THE MANDIFIED COALGULATER THE MANDIFIED COALGULATER TO THE COALGULATER THE COALG		WRITE(KOUT. 4) ' DO YOU WISH TO MODIF! THE CHO MATRIX BY THE DOYLE	019390
1 THE DISCRETE TIME SYSTEMS, Y OF NP' READ(XIN-11)MSG1 IF (MSG.120.40'*) THEN CALL DASCIBMICOS, IOS), RKFSS, MM1.1CBM, MM3. IPF2. MM6) CALL DASCIBMICOS, IOS), RKFSS, MM1.1CBM, MM3. IPF2. MM6) CRETURNS A MODIFIED GMD VALUE TO BE USED IN FINDING RKFSS CRETURNS A HODIFIED GMD VALUE TO BE USED IN FINDING RKFSS CRETURNS A HODIFIED GMD C1946C C GAL GULATE THE KALMAN FILTER GAINS, RKFSS, FCR EITHER THE MODIFIED C1946C C GAL OR THE UNMODIFIED GMD C GMD OR THE UNMODIFIED GMD CALL TRANSCIRMM, IRF2, MM3. CALL TRANSCIRMM, IRF2, MM3. CALL TRANSCIRMM, IRF2, MM3. CALL TRANSCIRMM, IRF2, MM3. CALL TRANSCIRMM, IRF2, MM3. KKFSS, MM4. MM6. MM1. MM5) C GALL MCTATIFEZ, IRMM, IRF2, MM3. KKFSS, MM4. MM6. MM1. MM5) C MM6-PASS, MM5 CLOSED LOOP HEAS MATRIX C MM1 = RKFSS MITHOUT THE ZEROS FCA TM2 DETERMINISTIC STATES C MOM ADO THE ZEROS FCA TMCSE STATES C MOM CO ZIS JI-1. RFM C MATRIC COLL TRANSCIPM, INC. C MM1 = RKFSSI, JI = MM1. C MM1 = RKFSSI, JI = MM1. C MM1 = RKFSSI, JI = MM1. C MM3. RETURN C MM3. RETURN C MM3. STATE SAMP. DO DATA KALMAÑ FILTER GAIN MATRIX C M990 C MOM C MATTE CUT THE RKFSS HATRIX C M990 C MC CALL MMATIO (RKFSS. IRFM, IRMM, IC.KIN, KOUT, NOIM, NOIM) C MOM C MATTE CUT THE RKFSS HATRIX C M990 C MC C MC MATTE CUT THE RKFSS HATRIX C M990 C MC C MC C MC TMC C MM1. C M970 C MC C MC C MC TMC C MM1. C MM1. MM1. MM1. MM1. NOIM, OMD (MOIM, NOIM) C M970 C MISTER CUT THE COMMING TO THE PROOFFIED IN A MANNER SIMILAR TO THE COCI990 C THE ANO STEIN TECHNIQUE FOR CCKTINUGUS TIME SYSTEMS. C MMCTATURE COMMING COMMING C MOIMS COMMING THE CUT SHOULD THE COLO990 C THE ANO STEIN TECHNIQUE FOR CCKTINUGUS TIME SYSTEMS. C SYMMETRIC MATRIX DESIGN PARAMETER. AS SQTO INFINITY IN THE COCI9940 C MTIMOUS TIME CASE, POUSTNESS PROFFITIES OF A FULL STATE FEEDBACK 1995:		1 AND STEIN TECHNIQUE FOR CONTINUOUS TIME CONTROLLERS EXTENDED TO	619486
READ (NIN.11)MSG1 IF (MSG:20.4°*) THEN CALL DAS2(BM:10S,10S),RKFSS,MM1,ICBM,MM3,IPF2,MM6) CALL DAS2(BM:10S,10S),RKFSS,MM1,ICBM,MM3,IPF2,MM6) CRETURRS A HODIFIED GHD VALUE TO BE USED IN FINDING RKFSS END IF C GALGULATE THE KALHAN FILTER GAINS, RKFSS, FCR EITHEF THE MODIFIED C1946C C GMO BY THE UNMODIFIED GND CALL TRANS2(IRMK,IRF2,M2,M3) C1940C C GMO IS STORED IN RKFSS C1940 C1940C C GMO IS STORED IN RKFSS C1940 C1950C CALL TRANS2(IRMK,IRF2,M2,M3) C1950C CALL TRANS2(IRMK,IRF2,M3,KKFSS,MM4,MM6,MM1,MM5) C1950C C MM1=PRSS,MM5 CLOSED LOOP MEAS MATRIX C MM1=PRSS,MS CLOSED LOOP MEAS MATRIX C MM1=RKFSS MITHOUT THE ZFFOS FCA TWE DETERMINISTIC STATES C MOM ADD THE ZEROS FCA TMOSE STATES C MOM ADD THE ZEROS FCA TMOSE STATES C MOM ADD THE ZEROS FCA TMOSE STATES C MOSE STATES		THE DISCRETE TIME SYSTEMS. Y OF NY	
TF (MSG:20.9*) THEN			
CALL DASCIBMIDOS, IDS), RKFSS, MMILICAM, MMILTER, LAWE) CRETURNS A HODIFIED GNO VALUE TO RE USED IN FINDING RKFSS CRED IF COLGULATE THE KALMAN FILTER GAINS, RKFSS, FCR EITHER THE MODIFIED CI94-61 COMD IS STORED IN RKFSS C194-91 CALL TRANSCIRMM, IRF2, MMI) DO 161 1=1, IRMM COMD IS STORED IN RKFSS CALL REPORT (RM, IRF2, MMI) CALL RFLITTER (II) CALL RFLITTER, IRMM, IRF2, MMI, IRFS, MMI, MM6, MMI, MMS) CALL RFLITTER, IRMM, IRF2, MMI, RKFSS, MMI, MM6, MMI, MMS) CALL RFLITTER, IRMM, IRF2, MMI, RKFSS, MMI, MM6, MMI, MMS) CALL RFLITTER, IRMM, IRF2, MMI, RKFSS, MMI, MM6, MMI, MMS) CALL RFLITTER, IRMM, IRF2, MMI, RKFSS, MMI, MM6, MMI, MMS) CALL RFLITTER, IRMM, IRF2, MMI, RKFSS, MMI, MM6, MMI, MMS) CALL RFLITTER, IRMM, IRF2, MMI, RKFSS, MMI, MM6, MMI, MMS) CALL RFLITTER, IRMM, IRF2, MMI, RKFSS, MMI, MM6, MMI, MMI, IRF3, IRF3, IRF4 CALL RKFSS, IRFM, IRMM, IRF3, IRFM, IRMM, IRFA, IRFM, IRFA,		TE CHEC. OVE THEN	
C CALCULATE THE KALMAN FILTER GILNS, RKFSS, FCR EITHER THE MODIFIED C1947C QMD OR THE UMMODIFIED OND C1948C C QMD IS STORED IN RKFSS C19-93 CALL TRANSZIRMH, IRFZ, M2, WM3) C19503 DD 101 1=1, TRMM C19503 GALL KFLTRIMFE, TRMN, F2, WM3, M3, M4, WM6, WM1, WM5) C19513 CALC KFLTRITTE, IRMN, F2, WM3, FKFSS, WM4, WM6, WM1, WM5) C19513 C WM6=PMSS, WM5 CLOSED LGOP MEAS MATRIX C19563 C MM6=PMSS, WM5 CLOSED LGOP MEAS MATRIX C19563 C MM0 MDD THE ZERGS FGR THGSE STATES C19563 IF (NUMOTS, E0.0) THEN C19563 OO 2029 1=1, IRFM C19563 DO 2029 1=1, IRFM C19563 DO 2029 1=1, IRFM C19563 DO 2113 1=1, NUMOTS C19663 C19663 C118 RKFSS(1, J) = M1(1, J) C19663 C118 RKFSS(1, J) = M1(1, J) C19663 C119		AT THUS DESCRIPT THEN CALL OF THE TRANSPORT THE TABLE TO THE TRANSPORT T	017434
C CALCULATE THE KALMAN FILTER GILNS, RKFSS, FCR EITHER THE MODIFIED C1947C QMD OR THE UMMODIFIED OND C1948C C QMD IS STORED IN RKFSS C19-93 CALL TRANSZIRMH, IRFZ, M2, WM3) C19503 DD 101 1=1, TRMM C19503 GALL KFLTRIMFE, TRMN, F2, WM3, M3, M4, WM6, WM1, WM5) C19513 CALC KFLTRITTE, IRMN, F2, WM3, FKFSS, WM4, WM6, WM1, WM5) C19513 C WM6=PMSS, WM5 CLOSED LGOP MEAS MATRIX C19563 C MM6=PMSS, WM5 CLOSED LGOP MEAS MATRIX C19563 C MM0 MDD THE ZERGS FGR THGSE STATES C19563 IF (NUMOTS, E0.0) THEN C19563 OO 2029 1=1, IRFM C19563 DO 2029 1=1, IRFM C19563 DO 2029 1=1, IRFM C19563 DO 2113 1=1, NUMOTS C19663 C19663 C118 RKFSS(1, J) = M1(1, J) C19663 C118 RKFSS(1, J) = M1(1, J) C19663 C119	a	CALL DASE (DATEDS) INSTITUTE STATEMENT STATEME	81944 <u>-</u> U
C CALCULATE THE KALMAN FILTER GILNS, RKFSS, FCR EITHER THE MODIFIED C1947C QMD OR THE UMMODIFIED OND C1948C C QMD IS STORED IN RKFSS C19-91 CALL TRANSZIRMM, IRFZ, M2, WM3) C19-50 DO 101 1=1, TRMM C11-12 TRM C19-51 GI	L KE	INVA W HONTELED AND ANTOF IC ES OPEN IN LIBRING MALES	
C QMD OR THE UNMODIFIED QMD C QMD IS STORED IN RKFSS CALL TRANSZ(IRMK-IRFZ, HZ, WM3) CALL TRANSZ(IRMK-IRFZ, HZ, WM3) COLT TRANSZ(IRMK-IRFZ, HZ, WM3, WM4, WM6, WM1, WM5) COLT TRANSZ(IRMK-IRFZ, HZ, WM3, MM4, WM6, WM1, WM5) COLT TRANSZ(IRMK-IRFZ, HZ, WM3, MM4, WM6, WM1, WM5) COLT TRANSZ(IRMK-IRFZ, HZ, WM3, MM4, WM4, WM6, WM1, WM5) COLT TRANSZ(IRMK-IRFZ, HZ, WM3, MM4, WM4, WM4, WM4, WM5) COLT TRANSZ(IRMK-IRFZ, HZ, WM3, MM4, WM4, WM4, WM4, WM4, WM4, WM3, MM4, WM3, MM4, WM3, MM4, WM3, WM3, WM3, WM3, WM3, WM3, WM3, WM3		END IF	61946.
CALL TRANS2(IRMM, IRF2, M2, WM3) 100 101 1=1,1R*M 101 M*4(I1)=+MD(I1) CALL KFLTRITR2, IRMM, F2, WM3, KKPSS, WM4, WM6, WP1, WM5) CALL KFLTRITR2, IRMM, F2, WM3, KKPSS, WM4, WM6, WP1, WM5) C MM6=PMSS, WM5 CLOSED LOOP MEAS MATRIX C MM6=PMSS, WM5 CLOSED LOOP MEAS MATRIX C MM6 ADD THE ZEROS FGR TMCSE STATES C NOM ADD THE ZEROS FGR TMCSE STATES C NOM ADD THE ZEROS FGR TMCSE STATES D 2029 I1, IRFM C 19560 D 2029 I1, IRFM C 19580 D 2029 I1, IRFM C 19580 D 2029 I1, IRFM C 19660 D 2118 I=1, NUMDTS C 196610 D 2118 RKFSS(I,J)=3 C 196610 C 2119 J=1, IRFM C 196610 C 2119 I=1DS, IRFM C 196610 C 119 KFSS(I,J)=WM1(II,J) C 196610 C NOM WRITE OUT TME RKFSS MATRIX C 196610 C NOM WRITE OUT TME RKFSS MATRIX C 19690 C NOM WRITE OUT TME RKFSS MATRIX C 19690 C NOM WRITE DUT TME RKFSS MATRIX C 19710 CALL MMATIO(RKFSS, IRFM, IRMM, IC, KIN, KOUT, NOIM, NOIM) C 19770 END D ECK DAS2 SUBRCUTINE DAS2(BM, QMD, √, ICEF, WM3, IRFP, WM1) C 19760 C WDM NOIM, NOIM), WM1(MDIM, NOIM), C 19760 C WMS STEIN TECHNIQUE FOR CENTINUOUS TIME SYSTEMS. C 19920 C WMERE SC IS A SCALAR DESIGN PASPMETER AMD V IS A POSITIVE DEFINITE C 19932 C SYMMETRIC DAS2; PODUSTNESS PPOFERIES OF A FULL STATE FEEDBACK 19951 C NTINUOUS TIME CASE, PODUSTNESS PPOFERIES OF A FULL STATE FEEDBACK 19951	C	ALCULATE THE KALMAN FILTER GAINS, RKFSS, FCR EITHER THE MODIFIED	
CALL TRANS2(IRMM, IRF2, M2, WM3) 100 101 1=1, 1RMM 101 1=1, 1RMM 101 1=10(1.1) CALL KPLTRITR2, IRMM, F2, WM3, FKPSS, WM4, WM6, WM1, WM5) CALL KPLTRITR2, IRMM, F2, WM3, FKPSS, WM4, WM6, WM1, WM5) C MM6=PMSS, WM5 CLOSED LOOP MEAS MATRIX C MM6=PMSS, WM5 CLOSED LOOP MEAS MATRIX C MM1 ADD THE ZEROS FGR TMCSE STATES C NOM ADD THE ZEROS FGR TMCSE STATES D 19550 IF (MJ9075, 60, 3) THEM C 19580 DO 2029 11, IRFM C 19580 DO 2029 11, IRFM C 19580 DO 2029 11, IRFM C 19660 DO 2118 11, NUMDIS C 19660 DO 2118 11, NUMDIS C 19660 2118 RKFSS(1, J) = WM1(11, J) C 19670 END C NOM WRITE OUT TME RKFSS MATRIX C 19660 C NOM WRITE OUT TME RKFSS MATRIX C 19670 C NOM WRITE OUT TME RKFSS MATRIX C 19670 C NOM WRITE DUT TME RKFSS MATRIX C 19710 CALL MMATIO(RKFSS, IRFM, IRMM, IC, KIN, KOUT, NOIM, NDIM) C 19720 C NOBERCUTINE DAS2(8M, QMD, \$\$, ICEP, WM3, IRFP, WM1) C 19760 SUBRCUTINE DAS2(8M, QMD, \$\$, ICEP, WM3, IRFP, WM1) C 19760 C WDM000=QMD (\$QS\$0) (EM V) BM1, NDIM) C 19760 C THIS ROUTINE ALLOWS CMD TO BE MODIFIED IN A MANNER SIMILAR TO TME DOC19900 C TIE AND STEIN TECHNIQUE FOR CCTVINUOUS TIME SYSTEMS. 219910 C WMCMC SC IS A SCALAR DESIGN PASPMETER AMD V IS A POSITIVE DEFINITE (1993) C SYMMETER C NATER C DESIGN PASPMETER AMD V IS A POSITIVE DEFINITE (1993) C SYMMETER C NATER C DESIGN PASPMETER AMD V IS A POSITIVE DEFINITE (1993) C SYMMETER C NATER C DESIGN PASPMETER AMD V IS A POSITIVE DEFINITE (1993) C SYMMETER C NATER C DESIGN PASPMETER AMD V IS A POSITIVE DEFINITE (1993) C SYMMETER C NATER C DESIGN PASPMETER AMD V IS A POSITIVE DEFINITE (1993) C SYMMETER C NATER C DESIGN PASPMETER AMD V IS A POSITIVE DEFINITE (1993) C SYMMETER C NATER C DESIGN PASPMETER AMD V IS A POSITIVE DEFINITE (1993) C SYMMETER C NATER C POPUSYNESS PPOFERIES OF A FULL STATE FEEDBACK (1995)	Ça	MD OR THE UNMODIFIED QMD	
IF (NUMDTS.ED.0) THEN C19570	C	QMD IS STORED IN RKFSS	019-93
IF (NUMDTS.ED.0) THEN C19570		CALL TRANS2(IRMM, IRF2, H2, WH3)	6195 <u>0</u>
IF (NUMDTS.ED.0) THEN C19570		DO 161 I=1.IRMM	19510
IF (NUMDTS.ED.0) THEN C19570	1G1	HM4(I,1)=RHD(I,I)	019525 ^U
IF (NUMDTS.ED.0) THEN C19570		CALL KFLTR (IRF2. IRHM.F2.WH3.FKFSS.WH4.WH6.WM1.WM5)	01953 <u>c</u>
IF (NUMDTS.ED.0) THEN C19570	C WM	6=PMSS,WM5 CLOSED LCOP MEAS MATRIX	319543
IF (NUMDTS.ED.0) THEN C19570	C MH1	* RKFSS HITHOUT THE ZEFOS FCR THE DETERMINISTIC STATES	219552
IF (NUMOTS-E0.0)THEN OO 2029 1=1,1RPM C19580 DO 2029 1=1,1RPM C19590 2029 RKFSS(I,J)=MM1(I,J) ELSE OG 2119 J=1,1RMM G19620 DO 2119 J=1,1RMM G19630 2018 RKFSS(I,J)=0 C19630 DO 2119 I=IDS,IRPM C19660 DO 2119 I=IDS,IRPM C19660 2119 RKFSS(I,J)=WM1(II,J) C19660 2119 RKFSS(I,J)=WM1(II,J) C19660 2119 RKFSS(I,J)=WM1(II,J) C19670 END IF CNOW WRITE OUT THE RKFSS HATRIX C19690 CNOW WRITE OUT THE RKFSS HATRIX C19730 MSS=*STEADY STATE SAMP_ED DATA KALMAN FILTER GAIN MATRIX* C19730 MSS=*STEADY STATE SAMP_ED DATA KALMAN FILTER GAIN MATRIX* C19730 RETURN CALL MMATIO(RKFSS,IRFM,IRMM,IC,KIN,KOUT,NOIM,NDIM) C19730 RETURN C19750 END * DECK DAS2 SUBRCUTINE DAS2(BM,QMD, J, ICEP, NM3,IRFP, NM1) C19750 SUBRCUTINE DAS2(BM,QMD, J, ICEP, NM3,IRFP, NM1) C19750 * DECK DAS2 SUBRCUTINE DAS2(BM,QMD, J, ICEP, NM3,IRFP, NM1) C19750 THIS ROUTINE ALLOMS CMD TO BE MODIFIED IN A MANNER SIMILAR TO THE DOC19000 C YLE AND STEIN TECHNIQUE FOR CCEPTINUGUS TIME SYSTEMS. C GMOMOD=CMD +(SQ*SQ)(EM(V)BNT)=SAMPLE TIME C GMOMOD=CMD +(SQ*SQ)(EM(V)BNT)=SAMPLE TIME C SYMMETRIC MATFIX DESIGN PARPMETER AND V IS A POSITIVE DEFINITE C19332 C SYMMETRIC MATFIX DESIGN PARPMETER AND V IS A POSITIVE DEFINITE C19332 C SYMMETRIC MATFIX DESIGN PARPMETER AND V IS A POSITIVE DEFINITE C19332 C SYMMETRIC MATFIX DESIGN PARPMETER AND V IS A POSITIVE DEFINITE C19332 C SYMMETRIC MATFIX DESIGN PARPMETER AND V IS A POSITIVE DEFINITE C19332 C SYMMETRIC MATFIX DESIGN PARPMETER AND V IS A POSITIVE DEFINITE C19352 C SYMMETRIC MATFIX DESIGN PARPMETERS OF A FULL STATE FETOBACK C19955			
DO 2829 1=1.18FM		IF (NUMOTS.EG.G) THEN	219570
2029 RKFSS(I,J)=MM1(I,J) ELSE OC 2119 J=1,IRMM G1962C 2118 RKFSS(I,J)=3 C1963C 2118 RKFSS(I,J)=3 C1964C 2119 RKFSS(I,J)=3 C1964C 11=I-NUMDTS C1964C 2119 RKFSS(I,J)=MM1(II,J) END IF C NOW WRITE OUT THE RKFSS HATRIX C1969C 27 IO=5 MS3="STEADY STATE SAMP_EO DATA KALMAN FILTER GAIN MATRIX" C1973D RETURN CALL MMATIO(RKFSS,IRFH,IRMM,IC,KIN,KOUT,NOIM,NDIM) END COUNTY RETURN END DECK DAS2 SUBRCUTINE DAS2(BM,QMD,V,ICEF,MM3,IRFM,MH1) PEAL BM(NDIM,NDIM),QMD(NDIM,NDIM), V(NDIM,NDIM) 1 MM3(NDIM,NDIM),QMD(NDIM,NDIM), V(NDIM,NDIM), C1976C TIMS ROUTINE ALLOWS CMD TO BE MODIFIED IN A MANNER SIMILAR TO THE DOC1990D C TIES ROUTINE ALLOWS CMD TO BE MODIFIED IN A MANNER SIMILAR TO THE DOC1990D C TIES ROUTINE ALLOWS CMD TO BE MODIFIED IN A MANNER SIMILAR TO THE DOC1990D C TIES ROUTINE ALLOWS CMD TO BE MODIFIED IN A MANNER SIMILAR TO THE DOC1990D C TIES ROUTINE ALLOWS CMD TO BE MODIFIED IN A MANNER SIMILAR TO THE DOC1990D C TIES ROUTINE ALLOWS CMD TO BE MODIFIED IN A MANNER SIMILAR TO THE DOC1990D C TIES ROUTINE ALLOWS CMD TO BE MODIFIED IN A MANNER SIMILAR TO THE DOC1990D C TIES ROUTINE ALLOWS CMD TO BE MODIFIED IN A MANNER SIMILAR TO THE DOC1990D C TIES ROUTINE ALLOWS CMD TO BE MODIFIED IN A MANNER SIMILAR TO THE DOC1990D C TIES ROUTINE ALLOWS CMD TO BE MODIFIED IN A MANNER SIMILAR TO THE DOC1990D C TIES ROUTINE ALLOWS CMD TO BE MODIFIED IN A MANNER SIMILAR TO THE DOC1990D C TIES ROUTINE ALLOWS CMD TO BE MODIFIED IN A MANNER SIMILAR TO THE DOC1990D C TIES ROUTINE ALLOWS CMD TO BE MODIFIED IN A MANNER SIMILAR TO THE DOC1990D C TIES ROUTINE ALLOWS CMD TO BE MODIFIED IN A MANNER SIMILAR TO THE DOC1990D C TIES ROUTINE ALLOWS CMD TO BE MODIFIED IN A MANNER SIMILAR TO THE DOC1990D C TIES ROUTINE ALLOWS CMD TO BE MODIFIED IN A MANNER SIMILAR TO THE DOC1990D C TIES ROUTINE ALLOWS CMD TO BE PODIFIED IN A MANNER SIMILAR TO THE DOC1990D C TIES ROUTINE ALLOWS CMD TO BE PODIFIED IN A MANNER SIMILAR TO THE DOC1990D C TIES ROUTINE ALLOWS CMD TO BE PODIFIED IN A MANNER SIMILAR TO THE DOC1990D C TIES		DO 2029 I=1.IRFM	C 1958 C
2029 RKFSS(I,J)=MM1(I,J) ELSE OC 2119 J=1,IRMM G1962C 2118 RKFSS(I,J)=3 C1963C 2118 RKFSS(I,J)=3 C1964C 2118 RKFSS(I,J)=3 C1964C DO 2119 I=IOS,IRFM G1965C 2119 RKFSS(I,J)=MM1(II,J) END IF C NOW WRITE OUT THE RKFSS HATRIX C1966C 27 IO=5 MS3="STEADY STATE SAMP_EO DATA KALMAN FILTER GAIN MATRIX" C1973D RETURN CALL MMATIO(RKFSS,IRFM,IRMM,IC,KIN,KOUT,NOIM,NDIM) END CALL MMATIO(RKFSS,IRFM,IRMM,IC,KIN,KOUT,NOIM,NDIM) END CALL MMATIO(RKFSS,IRFM,IRMM,IC,KIN,KOUT,NOIM,NDIM) END **OECK DAS2 SUBRCUTINE DAS2(BM,QMD,V,ICEF,MM3,IRFM,MH1) PEAL BM(NDIM,NDIM),QMD(NDIM,NDIM), V(NDIM,NDIM), 1 MM3(NDIM,NDIM), MM1(NDIM,NDIM), V(NDIM,NDIM), C1976C THIS ROUTINE ALLOWS CMD TO BE MODIFIED IN A MANNER SIMILAR TO TME DOC1990D C TLE AND STEIN TECHNIQUE FOR CENTINUGUS TIME SYSTEMS. 21992C C GMDMOD=QMD +(SQ=SQ)(EM(V)BMT)=SAMPLE TIME C SYMMETRIC MATFIX DESIGN PARAMETER AND V IS A PCSITIVE DEFINITE (1953C C SYMMETRIC MATFIX DESIGN PARAMETER. AS SQ>TC INFINITY IN THE COG1994D C NTINUOUS TIME CASE, POSUSTNESS PPOFERTIES OF A FULL STATE FEEDBACK (1965)		00 2;29J=1,Ik +M	C 19 59 0
DG 2119 J=1,IRMH G19620	2029	RKFSS(I.J)=HH1(I.J)	ü1968ü
DG 2119 J=1,IRMH G19620		ELSE	01961G
IG=5 IG=730 IGALL MMATIO(RKFSS.IRFM.IRMM.IG.KIN.KOUT.NDIM.NDIM) IGALL MMATIO(RKFSS.IRFM.IRMM.IG.KIN.KOUT.NDIM.NDIM) IGALL MMATIO(RKFSS.IRFM.IRMM.IG.KIN.KOUT.NDIM.NDIM) RETURN IGAL BND IGAL I		DG 2119 J=1.TRHH	619620
IG=5 IG=730 IGALL MMATIO(RKFSS.IRFM.IRMM.IG.KIN.KOUT.NDIM.NDIM) IGALL MMATIO(RKFSS.IRFM.IRMM.IG.KIN.KOUT.NDIM.NDIM) IGALL MMATIO(RKFSS.IRFM.IRMM.IG.KIN.KOUT.NDIM.NDIM) RETURN IGAL BND IGAL I		DO 21147=1.NUMOTS	019630
IG=5 IG=730 IGALL MMATIO(RKFSS.IRFM.IRMM.IG.KIN.KOUT.NDIM.NDIM) IGALL MMATIO(RKFSS.IRFM.IRMM.IG.KIN.KOUT.NDIM.NDIM) IGALL MMATIO(RKFSS.IRFM.IRMM.IG.KIN.KOUT.NDIM.NDIM) RETURN IGAL BND IGAL I	2118	RKFSS(I.J)=0	619649
IG=5 IG=730 IGALL MMATIO(RKFSS.IRFM.IRMM.IG.KIN.KOUT.NDIM.NDIM) IGALL MMATIO(RKFSS.IRFM.IRMM.IG.KIN.KOUT.NDIM.NDIM) IGALL MMATIO(RKFSS.IRFM.IRMM.IG.KIN.KOUT.NDIM.NDIM) RETURN IGAL BND IGAL I		DO 2119 I=IDS.IRFM	019650
IG=5 IG=730 IGALL MMATIO(RKFSS.IRFM.IRMM.IG.KIN.KOUT.NDIM.NDIM) IGALL MMATIO(RKFSS.IRFM.IRMM.IG.KIN.KOUT.NDIM.NDIM) IGALL MMATIO(RKFSS.IRFM.IRMM.IG.KIN.KOUT.NDIM.NDIM) RETURN IGAL BND IGAL I		TIT - MIMO TS	019660
IG=5 IG=730 IGALL MMATIO(RKFSS.IRFM.IRMM.IG.KIN.KOUT.NDIM.NDIM) IGALL MMATIO(RKFSS.IRFM.IRMM.IG.KIN.KOUT.NDIM.NDIM) IGALL MMATIO(RKFSS.IRFM.IRMM.IG.KIN.KOUT.NDIM.NDIM) RETURN IGAL BND IGAL I	2119	RKFSS(T.J)*WM1(T:.J)	019675
IG=5 IG=730 IGALL MMATIO(RKFSS.IRFM.IRMM.IG.KIN.KOUT.NDIM.NDIM) IGALL MMATIO(RKFSS.IRFM.IRMM.IG.KIN.KOUT.NDIM.NDIM) IGALL MMATIO(RKFSS.IRFM.IRMM.IG.KIN.KOUT.NDIM.NDIM) RETURN IGAL BND IGAL I	,	FND TF	319685
IG=5 NSG=*STEADY STATE SAMP_ED DATA KALMAÑ FILTER GAIN MATRIX* CALL MMATIO(RKFSS.IRFM.IRMM.IC.KIN.KOUT.NDIM.NDIM) OLGATO NUMDIS=NUMSAV RETURN END DECK DAS2 SUBRCUTINE DAS2(BM.QMD.V.ICEP.HM3.IRFM.HM1) CLGATO SUBRCUTINE DAS2(BM.QMD.V.ICEP.HM3.IRFM.HM1) CLGATO THAS (NDIM.NDIM).GMD(NDIM.NDIM) CLGATO	C NO	W MOTTE OUT THE DRESS MATERY	019498
GALL MMATIO (RKFSS.IRFM.IRMM.IC.KIN.KOUT.NDIM.NDIM) QALL MMATIO (RKFSS.IRFM.IRMM.IC.KIN.KOUT.NDIM.NDIM) QALL MMATIO (RKFSS.IRFM.IRMM.IC.KIN.KOUT.NDIM.NDIM) QALL MMATIO (RKFSS.IRFM.IRMM.IC.KIN.KOUT.NDIM.NDIM) QALL MMATIO (RKFSS.IRFM.IRMM.IC.KIN.KOUT.NDIM) QALL MMATIO (QALL COLOR COLO			
RETURN G19743 END G19743 * DECK DAS2 SUBRCUTINE DAS2(BM,QMD, \$\scrt{v}\$, ICEP, HM3, IRFM, HM1) C19760 REAL BM (NDIM, NDIM), QMD(NDIM, NDIM), C19760 1 HM3(NDIM, NDIM), HM1(NDIM, NDIM) C19763 G TMIS ROUTINE ALLONS CM3 TO BE MODIFIED IN A MANNER SIMILAR TO THE TOC19800 C YLE AND STEIN TECHNIQUE FOR CCATINUGUS TIME SYSTEMS. D19813 C QMDMOD=CMD +(SQ*SQ)(EM(V)BMT)*SAMPLE TIME G19820 C MHERE SC IS A SCALAR DESIGN PARPMETER AMD V IS A PCSITIVE DEFINITE C19832 C SYMMETRIC MATRIX DESIGN PARAMETER. AS SQ>TC INFINITY IN THE CCG19940 C NTINUOUS TIME CASE, POSUSTNESS PROPERTIES CF A FULL STATE FEEDBACK 219851	· <u>·</u>	MORTIPOTOTATO CAMO IN MATA VALMANTET, TENTRAL MATETAL	64713U
RETURN G19743 END G19743 * DECK DAS2 SUBRCUTINE DAS2(BM,QMD, \$\scrt{v}\$, ICEP, HM3, IRFM, HM1) C19760 REAL BM (NDIM, NDIM), QMD(NDIM, NDIM), C19760 1 HM3(NDIM, NDIM), HM1(NDIM, NDIM) C19763 G TMIS ROUTINE ALLONS CM3 TO BE MODIFIED IN A MANNER SIMILAR TO THE TOC19800 C YLE AND STEIN TECHNIQUE FOR CCATINUGUS TIME SYSTEMS. D19813 C QMDMOD=CMD +(SQ*SQ)(EM(V)BMT)*SAMPLE TIME G19820 C MHERE SC IS A SCALAR DESIGN PARPMETER AMD V IS A PCSITIVE DEFINITE C19832 C SYMMETRIC MATRIX DESIGN PARAMETER. AS SQ>TC INFINITY IN THE CCG19940 C NTINUOUS TIME CASE, POSUSTNESS PROPERTIES CF A FULL STATE FEEDBACK 219851		nds- diemul dimie gampet tem to vit vous notwindist.	940725
RETURN END DECK DAS2 SUBRCUTINE DAS2(BM,QHD, V, ICEP, HM3, IRFM, HM1) REAL BM (NDIM, NDIM), QMD (NDIM, NDIM), V (NDIM, NDIM), 1 HM3 (NDIM, NDIM), HM1 (NDIM, NDIM) C TMIS ROUTINE ALLOWS GMD TO BE MODIFIED IN A MANNER SIMILAR TO THE DOC19500 C YLE AND STEIN TECHNIQUE FOR CCNTINUGUS TIME SYSTEMS. C QMDMOD=QMD +(SQ*SQ)(CM(V)BMT)*SAMPLE TIME C QMDMOD=QMD +(SQ*SQ)(CM(V)BMT)*SAMPLE TIME C GMMERE SC IS A SCALAR DESIGN PARAMETER AMD V IS A POSITIVE DEFINITE C19530 C SYMMETRIC MATRIX DESIGN PARAMETER. AS SQ>TC INFINITY IN THE COG19940 C NTINUOUS TIME CASE, POSUSTNESS PROFERTIES OF A FULL STATE FEEDBACK 219651		WALL HIME AV THE TRANSPORTED TRANSPORTED TO THE POLICY OF	017/20
END DECK DAS2 SUBRCUTINE DAS2(BM,QHD, V, ICEP, HM3, IRFM, HM1) REAL BM (NDIM, NDIM), QMD (NDIM, NDIM), V (NDIM, NDIM), 1 HM3 (NDIM, NDIM), HM1 (NDIM, NDIM) THIS ROUTINE ALLOWS GMD TO BE MODIFIED IN A MANNER SIMILAR TO THE DOC19800 THE AND STEIN TECHNIQUE FOR CCTINUGUS TIME SYSTEMS. 1981) C QMDMDD=QMD +(SQ+SQ)(EM(V)BMT) +SAMPLE TIME 019520 C MHERE SC IS A SCALAR DESIGN PARAMETER AND V IS A POSITIVE DEFINITE C19532 C SYMMETRIC MATRIX DESIGN PARAMETER. AS SQ>TC INFINITY IN THE COG19940 C NTINUOUS TIME CASE, POSUSTNESS PROFERTIES OF A FULL STATE FEEDBACK 219651			
* DECK DASZ SUBRCUTINE DASZ(BM,QHD, V, ICEP, HM3, IRFM, HM1) PEAL BM (NDIM, NDIM), QMD (NDIM, NDIM), V (NDIM, NDIM), 1 HM3 (NDIM, NDIM), HM1 (NDIM, NDIM) C TMIS ROUTINE ALLOWS CMD TO BE MODIFIED IN A MANNER SIMILAR TO THE DOC19800 C YLE AND STEIN TECHNIQUE FOR CCNTINUGUS TIME SYSTEMS. C QMDMOD=QMO +(SQ*SQ)(CM(V)BMT) *SAMPLE TIME C GMDMOD=QMO +(SQ*SQ)(CM(V)BMT) *SAMPLE TIME C MHERE SC IS A SCALAR DESIGN PARAMETER AND V IS A POSITIVE DEFINITE (1953) C SYMMETRIC MATRIX DESIGN PARAMETER. AS SQ>TC INFINITY IN THE COG19940 C NTINUOUS TIME CASE, POSUSTNESS PROFERTIES OF A FULL STATE FEEDBACK (1965)			
SUBRCUTINE DAS2(BH,QHD, V, ICEP, HM3, IRFM, HM1) REAL BH(NDIM, NDIM), QMD(NDIM, NDIM), V(NDIM, NDIM), C19783 1 HH3(NDIM, NDIM), HH1(NDIM, NDIM) C THIS ROUTINE ALLOWS CHO TO BE MODIFIED IN A MANNER SIMILAR TO THE DOC19800 C YLE AND STEIN TECHNIQUE FOR CCATINUGUS TIME SYSTEMS. J19813 C QMDMOD=QMD +(SQ+SQ)(EM(V)BMT)+SAMPLE TIME 019820 C HMERE SC IS A SCALAR DESIGN PARPMETER AMD V IS A PCSITIVE DEFINITE (19832) C SYMMETRIC MATFIX DESIGN PARAMETER. AS SQ>TC INFINITY IN THE COG19940 C NTINUOUS TIME CASE, POSUSTNESS PROPERTIES OF A FULL STATE FEEDBACK (1985)			
REAL BH(NDIM, NDIM), QMD(NDIM, NDIM), V(NDIM, NDIM), C19783 1 MH3(NDIM, NDIM), MH1(NDIM, NDIM) 019793 C THIS ROUTINE ALLOWS CHO TO BE MODIFIED IN A MANNER SIMILAR TO THE DOC19800 C YLE AND STEIN TECHNIQUE FOR CCATINUGUS TIME SYSTEMS. 319813 C QMDMOD=QMD +(SQ+SQ)(EM(V)BMT)+SAMPLE TIME 019820 C MMERE SC IS A SCALAR DESIGN PARAMETER AMD V IS A PCSITIVE DEFINITE (19832) C SYMMETRIC MATRIX DESIGN PARAMETER. AS SQ>TC INFINITY IN THE COG19940 C NTINUOUS TIME CASE, POSUSTNESS PROPERTIES OF A FULL STATE FEEDBACK (1985)	- OEC	R MASC	-
1 WH3 (NDIM, NDIM). WH1 (NDIM, NDIM) C THIS ROUTINE ALLOWS CHO TO BE MODIFIED IN A MANNER SIMILAR TO THE DOC19800 C YLE AND STEIN TECHNIQUE FOR CCATINUGUS TIME SYSTEMS. C QMOMOD=CHO + (SQ+SQ) (EM (V) BMT) +SAMPLE TIME C WHERE SC IS A SCALAR DESIGN PARPMETER AND V IS A PCSITIVE DEFINITE (1953) C SYMMETRIC MATRIX DESIGN PARAMETER. AS SQ>TC INFINITY IN THE COG19940 C NTINUOUS TIME CASE, POSUSTNESS PROPERTIES OF A FULL STATE FEEDBACK (1965)			
C THIS ROUTINE ALLOWS CHO TO BE MODIFIED IN A MANNER SIMILAR TO THE DOG 19800 C YLE AND STEIN TECHNIQUE FOR CCATINUGUS TIME SYSTEMS. 319813 C QMOHOD=CHO + (SQ+SQ) (EM (V) BMT) + SAMPLE TIME 019820 C WHERE SC IS A SCALAR DESIGN PARAMETER AND V IS A POSITIVE DEFINITE (19832 C SYMMETRIC MATRIX DESIGN PARAMETER. AS SQ>TO INFINITY IN THE COG 19940 C NTINUOUS TIME CASE, POSUSTNESS PROPERTIES OF A FULL STATE FEEDBACK 219851			
C YLE AND STEIN TECHNIQUE FOR CCATINUCUS TIME SYSTEMS. C QMOMOD=CHO + (SQ+SQ) (EM (V) BMT) + SAMPLE TIME C MMERE SC IS A SCALAR DESIGN PARAMETER AND V IS A POSITIVE DEFINITE (1953) C SYMMETRIC MATRIX DESIGN PARAMETER. AS SQ>TO INFINITY IN THE COG19940 C NTINUOUS TIME CASE, POSUSTNESS PROPERTIES OF A FULL STATE FEEDBACK (1985)			
C QMOMOD=CMD + (SQ+SQ)(EM(V)BMT)+SAMPLE TIME 019620 C MMERE SC IS A SCALAR DESIGN PARAMETER AND V IS A PCSITIVE DEFINITE 119630 C SYMMETRIC MATRIX DESIGN PARAMETER. AS SQ>TC INFINITY IN THE COG19940 C NTINUOUS TIME CASE, POSUSTNESS PROPERTIES OF A FULL STATE FEEDBACK 119651	C_TH		
C WHERE SC IS A SCALAR DESIGN PARPMETER AND V IS A POSITIVE DEFINITE 119532 C SYMMETRIC MATRIX DESIGN PARAMETER. AS SQ>TO INFINITY IN THE COG19940 C NTINUOUS TIME CASE, POSUSTNESS PROPERTIES OF A FULL STATE FEEDBACK 219651			319513
G SYMMETRIC MATRIX DESIGN PARAMETER. AS SQ>TC INFINITY IN THE COG19940 G NTINUOUS TIME CASE, POPUSTNESS PROPERTIES OF A FULL STATE FEEDBACK 21985:			
G SYMMETRIC MATRIX DESIGN PARAMETER. AS SQ>TC INFINITY IN THE COG19940 G NTINUOUS TIME CASE, POPUSTNESS PROPERTIES OF A FULL STATE FEEDBACK 21985:			
C NTINUOUS TIME CASE, POSUSTNESS PROFERTIES OF A FULL STATE FEEDBACK 21985:	C SYM	METRIC MATRIX DESIGN PARAMETER. AS SQ>TO INFINITY IN THE CO	619940

ast known thereto populate manner

```
THESIS, DBL, AFIT CHARACTER MSG*60
                                                                                                                                                                   319883
             REAL COMI (1), COM2 (1)
                                                                                                                                                                   019890
            COMMON ZMAINIZNOIM.NOIM1.CCM1
                                                                                                                                                                    319900
            COMMON /RNTIM/RNTIME, OELTIM
                                                                                                                                                                   619913
        CONNEN /MAUNE/MSG
                                                                                                                                                                    319920
            CONTON MAINZO
                                                                                                                                                                   119931
            COMMON /INGU/KIN, KOUT, KPUNCH
            WRITE(KOUT,11) *
                                                                                                                                                                   119951
      WRITE(KOUT.*) THIS ROUTINE MCDIFIES THE VALUE OF OHD USED TO CALCUM19970 LLATE THE STEADY STATE KALMAN FILTER GAIN. THE MCDIFICATION PERFORMINED IS SINILAR TO THE DOYLE AND STEIN TECHNIQUE FOR CONTINUOUS-TIM019990
          1E SYSTEMS. FOR A COMPLETE DESCRIPTION SEE E. LLOYDS MASTERS THESIDEDJOD 15. AFIT, DOL. BRIEFLY THE MCDIFICATION ATTEMPTS TO ENHANCE ROBUSTDEDJID
          INESS OF THE LOG CONTROLLER AND IS OMOD=GHO(GHO)GHOT+SQ+SQ+DELTIHO20020
           1 *(3P(V)3MT))... THE LARGER THE VALUE CHOSEN FOR THE SCALAR SO THOSSISS
          1E MORE GOBUSTNESS RECOVERY (COMPARED TO FULLSTATE FEED-SACK). V MOZOJAD
           TUST EE A POSITIVE DEF. MATRIX. CHOCSING /= 1 4005 PSEUDJNOISE EQUAD 20 151
           TLLY TO ALL CONTROL INPUTS.
            WAITE(KOUT.11) . .
          WRITE(KOUT,*)'ENTER 1-- TO INPUT SQ, 2-- TO INPUT V, 3-- TC 020383

1 COMPUTE MODIFIED 7, 4-- TO EXIT ROUTINE.....NOTE 1,2 MUST 3E 020393

1 AGGCMPLISHED BEFGRE 3, AND 3 BEFORE +, BUT THAT 1,2,3, CAN BE 020130

1 OGNE ANY NUMBER OF TIMES BEFORE USING 4' 020120

WRITE(KOUT,11)'' 020120
      WRITE(KOUT,+) 'ENTER OFTION>'
                                                                                                                                                                   020130
         GO TG ( 1,2,3,4) ICPT
            WRITE(KOUT,11) .
                                                                                                                                                                   828163
            HALLE (KOUL'S) ENTER 20>
                                                                                                                                                                   3 23 170
            READ (KIN, *) SQ_
                                                                                                                                                                020180
            GO TC 5
            WPITE(KOUT, 11) * *
          MOITEROUT.1170 US INITIALIZED TO THE IDENTITY HATPIX UPON ENTRY TORORS 10 THE 10 ENTRY TORORS 11 THE 10 ENTRY TORORS 11 THE 10 ENTRY TORORS 12 ENTRY TORORS 12
         1 PRINTED AT THE BEGINNING OF THE PRIGRAM! ELSE ENTER A : >*
                                                                                                                                                                   020240
             C1=1.3
                                                                                                                                                                   020250
             CALL IONT (ICBM-V-C1)
                                                                                                                                                                   323260
             READ (KIN. +) IO
             IF (10.EQ. 0) THEN
             GO TO 5
                                                                                                                                                                   023290
            ELSE
MSG='THE CHOSEN V NATRIX IS'
                                                                                                                                                                   020300
                                                                                                                                                                   323313
             GALL HHAT 10 (V . ICBH. ICBH. ID. KIN. KOUT, NOIN, NOIN)
             ENO IF
                                                                                                                                                                   0 20 330
             GO TG 5
            WRITE(KOUT, 11) .
                                                                                                                                                                   121350
             CALL MATA (V.AM.ICOM.ICOM.IRFF.WH3)
                                                                                                                                                                   0 20 36 0
             CALL MATI(8M, WM3, IRFM, ICSM, IRFM, WM1)
             C1=SG=SQ=DELTIM
             CALL MADD1 (IRFM, IRFM, OMD, AM1, WM3,C1)
                                                                                                                                                                   020393
             10=5
             MSG= 'MODIFIED 3 MATRIX, 3MOC+'
             CALL MMATIO(WM3. IRFM. IRFM. IC. KIN. KOUT, MDIF. NOIM)
                                                                                                                                                                   8 28 42 3
             GO TC 5
                                                                                                                                                                   C 20 - 30
             CALL EQUATE (QMO, HM3, IRFM, IRFM)
      REPLACE THE VALUE IN QMO WITH GMOD
             RETURN
             END
. DECK DOTCON
             SUBRCUTINE DOTCOMIPHIM. WXX. WP1. X. BMO.U. WMZ. PHIPRP.
           1 XPRIM.S.WUU.GCSTR.IHOLD)
                                                                                                                                                                020503
            REAL COME (1), COPE (1), PHIP (NCIM, NOIM).
                                                                                                                                                                  020513
          . (MIDE, MICH) Y, (MICH, MICH) 1MH, (MICH, MICH) YAME
```

```
1 BHD (NOIM, NOIM) . U(NOIM, NOIM) . WHZ (NOIM, NOIM) .
     1 PHIP-M(NOIM.NO.M).xP-IM(NOIM.NOIM).S(NOIM.NOIM).
                                                                         526541
     1 WUU (NOIM, NOIM), GCSTR(NOIM, NOIM)
                                                                         62:35:
      CHARACTER MSG+63
                                                                         C20=6.
      COMMON /MAIN1/NDIM.NDIH1.COM1
                                                                         620570
                                                                      ___020550
      COMMON /MAINZ/ COM2
      COMMON JMAIN4/NOIMS, NOIMS
                                                                         121595
     COMMEN /INOU/KIN. KOUT, KPUNCH
                                                                         020600
      COMPON /RATIM/ RATIME.DELTIM
                                                                         626616
      COMMON /MAING/ICBT.ICBM.ICFA.LCGA.ICGM.ICGT.ICGA.IRFA.IRFM.IPFT. 020620
     1 IRHT, IRQA, IO, LQG, IRHM, NUPDTS
                                                                         628630
      COMMON /MAUNS/MSG
                                                                         020640
C THIS SUBROUTINE COMPUTES THE STESDY STATE CPTIFAL FEEDBACK GAIN MATRICECESO
CX GCSTR, BASED ON A LINEAR QUADRATIC COST GRITERICH, FOR A SAMPLED C20660
   DATA CONTROLLER
                                                                         £ 20 670
   SEE MAYBECK CHAP 14 FOR A DETAILED DISCUSSION OF ALGCRITHM AND
                                                                         020580
C EQUATIONS
                                                                         020690
0 20 7 20
   TRANSFORM SYSTEM SO KLEINMAN RICCATI SOLVER WILL HANDLE'S NOTED
                                                                         62C735
     CALL PRINITING .U . ICBH. GCSTR. S. IHOLD. BMD. HM1. PHIPRM. X. X FRIM.
                                                                         626743
     1 PHIP)
                                                                         029753
C
                                                                         020763
C WM2=UI+ST
                                                                         020773
CNOW COMPUTE KPRIM FROM RICCATI ECUATION
CALL MATS(IMOLD,ICOM,BMD,GCST=,WM1)
                                                                         02078
                                                                         626793
      CALL DRIC (IHOLD.PFIPRH; HM1.) FFIM. X, GCSTR)
                                                                         3269 90
C GCSTR CONTAINS INFO THAT IS NOT USED
                                                                         020910
C X CONTAINS **KPRIM** TREM X TREM
                                                                         820820
   NOW COMPUTE GOSTAPRIM
                                                                         62064<u>3</u>
62065<u>3</u>
      C1=1.0
      CALL MATSA (ICBM, IFOLO, BMO, X, GCSTR)
      CALL MADD1(ICOM.ICOM.U.GCSTR.WH1.C1)
                                                                         030 560
      CALL GPINV(ICSM. ICSM. NM1. GCSTR. NR. NT)
                                                                         024870
      IF (MR.NE.ICAM) THEN
                                                                         020883
      PRINT . INVERSE OF U IN ODTOON NOT OF FULL RANK, RANK IS .
                                                                         420495
     1 MR, " RANK SHOULD BE = ICAH=", ICBM
                                                                         320 960
      END IF
                                                                         326910
      GALL MAT4 (GCSTR, BPD, ICBM, ICBM, IHCLD, WM1)
                                                                         020923
      CALL HAT1 (HM1, X, ICBH, IHOLD, IHCLD, GCSTR)
                                                                         626330
      CALL MATI(GCSTR.PMIPRH.ICEF.IHOLD,IHOLD,WM1)
                                                                         020940
C WM1=GCSTRPRIM=((U+3HDT(KPRIM) BHC)) (3HD(KPRIM)PHIPRM)
                                                                         C 2: 95 C
          X IRFM
    ICBH
                                                                         030960
      CALL MADDITICEM, IMOLO, MMI, NH2, GCSTR, C1)
                                                                         G 20 973 - A
C GCSTR ICSH X ICSP
                                                                         020983
      IO =5
                                                                         0 20 993
      MSG= THE OPTIMAL STEADY STATE FEEDBACK GAIN MATRIX.GCSTR
                                                                         021300
      CALL MMATIO(GCSTR,ICSM,IHOLD,IO,KIN,KOUT,NDIF,NDIF)
                                                                         C21:13
      RETURN
                                                                         621020
      END
                                                                         021330
. DECK PKD IRC
                                                                         021343
      SUBROUTINE PROIRC (W.PHIM. WM2, WM2, HM. EMD. RKFSS, ICOM, IRFM, IRHM)
                                                                         021350
      REAL COMICID, COMECID, HENDIM, NOIM),
     1 PHIP (NOIH, NOIH) . HP1(NOIH, NCIP), HM2(NOIM, NOIM) .
                                                                         021373
     1 MM(NDIP, NDIM), BMD(NDIM, NDIP), RKFSS(NDIM, NDIM)
                                                                         321181
      CHARACTER MSG+6J, PSG1+1
                                                                         C21393
      GGMMCN /MAIN1/NDIR, NDIM1, COM1
      COMMON /MAINZ/COMZ
                                                                         021110
      COMPCH /MAUNS/ MSG
                                                                         021120
      CORMON JINOUJ KIN, KOUT, KPUNCH
                                                                         021133
   AS IN MAYBECK, SECTION 14.5, RKFSS=PHIMI(BMD)H *SG. SQ IS A
                                                                         021163
C SCALA- DESIGN PARAMETER AND W IS ANY NONSINGULAR M X M MATKIX.
   MAYBECK SUGGESTS THAT H= (H4(PHIPI)BMD) I IS A POSSIBLE CHOICE.
                                                                         021160
   THE RKFSS PICKED AS A RESULT OF THIS ALGORITHM FORMS THE BASIS
                                                                         C 21 17 6
C OF A SUBSPTIMAL CONTEL LAP, USTAR = GCSTR(A(TI-MINUS)
                                                                         621180
```

```
REITE(KOUT,12) * *
      WFITE(KOUT,*) THIS ROUTINE CALCULATES THE STEADY STATE KALMAN FILTC21201
     IER GAIN DIRECTLY! THAT IS WITH OUT USE FMSS FROM THE MATRIX RICCATE21210
     11 EQUATION AS THE BASIS OF KESS)I EQUATION AS IN SECTION 14.5 .MAY621223
     18ECK. KFSS=SO+(PHIMI)8HD(W) WHERE THE SCALAR SQ AND THE MATRIX $21230
          ARE DESIGN PARAMETERS...THE LARGER THE SO THE MORE ROBUSTNESS 021240
     1 THE SUBSEQUENT CONTROLLER WILL MAKE. NOTE THERE ARE NO STABILITERIZES:
17 CLAIMS FOR THE RESULTING CONTROLLER. SO BE SURE TO CHECK THE EIGHER 16ENVALUES OF THE SUBSEQUENT CONTROLLER. 9
      WRITE(KOUT, 12) " '
                                                                             62126 £
      FORMAT(A1/)
                                                                             621293
      HRITE(KOUT,+)*THE CPTIONS FCF THIS ROUTINE ARE 1->CHOOSE SO. Z-> CJ213GJ
     IMCOSE H, 3-. COMPUTE AND FRINT RKFSS, --> EXIT ROUTINE......
                                                                            621310
5 WRITE (KOUT, 12) * *
                                                                             621320
       WRITE (KOUT. +) "ENTER OPTION>"
                                                                             021330
      READ (KIN. *) IOPT
                                                                             821343
      GG TC (1,2,3,4) IGPT
                                                                             021355
      GO TC +
      HRITE(KOUT, 12) . .
      HRITE(KOUT.+) 'ENTER A VALUE FOR SQ. LARGER SQ GIVE BETTER RCBUSTNEC21386
     155>1
                                                                             621396
      READ (KIN, +) SQ
                                                                             C21430
      GO TC 5
                                                                             C21410
      WRITE (KOUT, 12) "
                                                                             621425
      WRITE(KOUT. *) 'DO YOU WANT TO FICK W ARSTRARILY OR DO YOU WANT W TO021436
     1_BE HM(PHIMI) BMD --INVERSE AS IN MAYBECK SECTION 14.5. NOTE THAT 021440
     TTIRMP MUST BE EGUAL TO ICOM SINCE W MUST BE ICOM X ICOM. ENTE- 021450
    1AN A FOR ARBITRARY, N OTHERNISES! 021460
      READ (KIN, 11) MSG1
                                                                             021-70
      FCRMAT (A1)
                                                                             £21485
      IF (MSG1.EQ. "A") THEN
      WRITE(KOUT,+) 'ENTER I/O OPTICA FOR WISES INPUT ROUTINE FOR EXPLANSO 2158:
     1710N OF INPUT OPTIONS 1,2,3,4,5,6)>'
                                                                             021510
      MSG= 'ARBITRARY W MATRIX'
       READ(KIN,+)10
                                                                            C21520
021533
      CALL MMATIO (M.ICBM.ICSM.IC, KIN, KOUT, NOIM, NOIM)
                                                                            021540
      ELSE
                                                                             921553
C COMPUTE H AS DESCRIBED ABOVE
      IF (ICOM. NE. IRHM) THEN
     HRITE(KOUT, *) 'NOTE THAT IRHE MUST EQUAL ICEM TO USE THIS HETHOD OF G2158 G
1 CALCULATING N. ICEM= ", ICEM, " IRHE ", IRHE " D2159C
      GO TC 5
       END IF
                                                                             221613
      CALL EQUATE (HM1.PHIH, IRFH. IRFF)
  GHINY DESTROYS THE CALLING ARRAY
                                                                             621533
      MT=1
                                                                             021640
      CALL GHINV (IRFH, IRFH, WM1, WM2, MR, MT)
                                                                             C 21 65 û
      CALL MATI (HM. WMZ. IRHM. IRFM. IRFM. WP1)
      CALL MATI(MM1,3M0,1RMM,1RFM,1C3M,MM2)
                                                                             321670
      CALL GHINY (IRMM. ICAM. WHZ. W. PR. HT)
                                                                             088153
      END IF
                                                                             821696
      GO TC 5
                                                                             021703
       WRITE(KOUT.12) . .
                                                                           021725
   CALCULATE RKFSS
       CALL EQUATE (WM1, PHIM, IRFP, IFFM)
                                                                             $21730
                                                                             C21746
   GMING DESTROYS CALLING ARRAY
      MT=1
                                                                             021752
      CALL GHINY (IFFM, IFFM, WM1, WM2, MR, MT)
                                                                             821763
      GALL MATI(MM2.8MD.IRFM.IRFM.ICBM.WM1)
                                                                             62177
                                                                           021760
      CALL MATI(HM1, H, IRFF, ICBH, ICEP, HM2)
CALL MSGALE(RKFSS, HM2, IRFP, IRFF, SG)
                                                                             62179:
      10=5
                                                                             521332
      MSG= 'RKFSS, PICKED DIRECTLY IS'
                                                                             021813
      CALL MMATIO(RKESS, IREM, IRMM, IC, KIN, KOUT, MDIK, NDIM)
                                                                             32132.
      GO TC 5
                                                                             G2183C
      RETUAN
                                                                         ___C21840
```

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E . . .
                                                                                                                                         021351
   DECK PRIMIT
                                                                                                                                          :2:56:
           SUBROUTINE PRIMIT(WM2.U.ICBM.GOSTR.S.IRFM.BMD.WM1.PHIPRM.X.XPRIM. 02187)
         1 PHIFE
       THIS SUBROUTINE COMPUTES THE PRIMED QUANTITIES MEEDED WHEN USING
                                                                                                                                         021390
       KIEINMAN RICCATI SOLVER WITH NON ZERO CROSS COST WEIGHTING
                                                                                                                                        021960
       ULW KIRTAM
                                                                                                                                         221912
           REAL HM2(NOIM, NOIM), GCSTR(NCIM, NOIM), S(NOIM, NOIM),
                                                                                                                                         521923
         18FO(NOIM.HOIM), WHICHOIM, NOIF), PHIPRH(NOIM, NOIM),
                                                                                                                                         321936
         1 x (NCIM.NOIM), x frim(NDIM, NOIF), PHIM(NDIM, NDIM)
           REAL COM1 (1), COM2 (1)
                                                                                                                                        021950
           COMMON /HAIN1/ ABIM, NOIM1.GCF1
           COMMON JHAINZ/COMZ
                                                                                                                                        021970
           CCMMCN /INOU/KIK, KOUT, KPUNCH
                                                                                                                                        621 98£
   NON COMPUTE XPRIP. PHIP: N
                                                                                                                                        821991
           CALL EQUATE (WMZ.U.ICBM.ICBM)
                                                                                                                                        822389
C GHINY DESTRIYS THE CALLING ARRAY
                                                                                                                                        022310
                                                                                                                                        $22320
           CALL GHINV (ICBM, ICBM, HMZ, GCSTF, MR, MT)
                                                                                                                                        622338
     GCSTR UI ICH X ICH
CALL HAT+(GCSTR,S,ICH,ICH,ICH,IRFM,WH2)
                                                                                                                                        0 22544
                                                                                                                                        022350
CHH2= UI(ST) ICBH X IRFM
                                                                                                                                        022960
           CALL HATI (BMD . HM2 . IRFH . ICBM . IRFH . WM1)
                                                                                                                                        222373
           C1=-1.3
                                                                                                                                        322383
           CALL MADDI (IRFM. IRFM. FHIM. WM1. PHIFRM.C1)
                                                                                                                                        6 22 2 9 6
C PHIPPH= PHIM-BHD(UI)ST IRFM
                                                               X IRFM
           CALL MATI (S.HM2. IRFN. ICOM . IRFM. HM1)
                                                                                                                                        C22110
           CALL MADD1 (IRFM, IRFM, X, HM1, XFFIF, C1)
                                                                                                                                        C22123
                                                                                                                                        022133
                                                                                                                                   022149
          RETURN
                                                                                                                                        G 22156
           END
                                                                                                                                         J 22169
* DEGK PGS
                                                                                                                                        022170
          SUBROUTINE RGS(GCSTR, RKESS, GCA, GCY, GCZ, BCY, BCZ, FC, YD,
                                                                                                                                        G 2218 j
         1 641,442,443.444,645,645,647,648,649,6416.641,412.
                                                                                                                                        5 22190
         1 WMA.WMB.WMC.WMD.WME.WMF.FT.ET.GT.HT.QT.RT.
                                                                                                                                        922293
         1 FM, EM, GM, HM, GM, RM, XO, PO, MXX, MUU, RXU, FA, BA, GA, GA, GUA,
                                                                                                                                        622210
         1MA4.FX4.RA.PXVA.GCZA.IRY.IFLGCZ.IFLGSD.
                                                                                                                                        322223
         1MU.PUMAX, PUMIN.PXTMAX,PXTHIN, MUMAX.HUHIN, MXAMAX.HXAMIN,
                                                                                                                                        022233
         1_PUOUT.PXTOUT.MXTOUT.MUOUT.AV3.WV-) _
                                                                                                                                        222243
           REAL COM1 (1) . CCM2 (1)
                                                                                                                                        02225C
                                                                                                                                        $22265
     THIS SURROUTINE SETS UP A CONTINUOUS, DISCRETIZED CONTINUOUS OF A
                                                                                                                                        022270
       SAMPLEC DATA LOG CONTROLLER BASED ON USERS REQUEST. EACH
CONTROLLER IS PUT INTO THE PROPER FORMAT FOR THE PERFORMANCE
                                                                                                                                        282283
                                                                                                                                        022290
       ANALYSIS SUBROUTINE, PERFAL.
                                                                                                                                        0 22 30 8
                                                                                                                                        022310
           CHARACTER MSG+60
                                                                                                                                        C 22 32 S
           REAL FT (NOIM, NOIP), 3T (NOIM, NCIM), GT (NOIM, NOIM),
                                                                                                                                         ú 22 335
         1 HT (NOIM, NOIM), RK (NOIM, NOIM), FM (NOIM, NOIM).
                                                                                                                                        022343
         18M(NCIM.NOIM).GM (NOIM.NCIP).XC(NOIM).
                                                                                                                                        C22355
         1HM(NCIM, NOIM).QM (NDIM.NDIP).PC(NDIM.NOIM),
1QT(NOIM, NDIM).RT (NOIM, NOIP),
                                                                                                                                        0 22 360
                                                                                                                                        6 22 373
        1GCSTR(NOIP, NOIH), SKFSS(NOIH, NCIH),
                                                                                                                                        022383
         THV1 (NOIM) . HV2 (NOIM) . HXU (NOIM, INCH);
                                                                                                                                        622390
      1WM1 (NOIH.NOIM). HM2 (NOIH.NCIM). WM3(NOIH.NOIM).
                                                                                                                                         322403
         THE CHICK THE CHICA THE CH
                                                                                                                                         122411
                                                                                                                                         022420
                                                                                                                                        0.22433
         1WMG(NDIM2, NDIM2), HMO(NDIM2, NDIM2), WME(NDIM2, NDIM2),
         1 HMF (NOIM2, NDIM2), WUU(NOIM, NCIP), WXX (NOIM, NDIP),
         1FA (HOIH2, NOIH2), BA (NOIM2, NOIH2), GA (NOIM2, NOIM2),
                                                                                                                                         C 2246:
         1MA4(ADIM2),GCK(ADIM, NDIM),GCZ(ADIM, NDIM),
                                                                                                                                         C22473
         1QA (NDIM2, NDIM2), PXA (NDIM2, NDIP2), PXVA (NDIM2, NDIM2),
                                                                                                                                        022480
                                                                                                                                         222493
         1MUOUTENDIMB, MXTOUTENDIMB, FXTCUTENDIMB
                 PEAL FUCUT (NOIM) .YD(NOIM3) .GUA(NOIM2.KDIM2) .
                                                                                                                                         0 22503
```

```
. (MICH) MINING (MICH) XAMAX (MICH) MUMIN (MI
                                                                           122510
      IMUMIX(NOIM).PATHIN(NOIM).FATHAX(NOIK).
                                                                           C2252.
      1PUMIN(NDIM).PUMAX (NDIM).GCZ2(NDIM2.NDIM2).
                                                                           922531
      IRA (NCIME, NOIME), SCY (NOIM, NCIM), SCZ (NOIM, NOIM),
                                                                           222542
      1H v3 (ADIM2) .HV ~ (ADIM2) .
                                                                           022550
      1GCY (NDIM.NDIM).FC (NCIM.ACIM)
                                                                           122560
       INTEGER IFLGCZ.IRY
       REAL MU (NDIM)
       COMMON /RNTIM/ RNTIME.DELTIF
                                                                           C22593
      COMMON /MAINZ/COM2
                                                                           009253
      COMPON /MAIN1/NOIM, NOIM1, CCF1
                                                                           622613
      COMMEN / INOU/ KIN, KOUT, KPUNCH
                                                                           022520
       COMMON WAIN- MOIRS, NOIRS
                                                                           022630
       COMMON /MAUNS/ MSG
                                                                           022640
       COMMON /MAINS/ ICBT.ICBH.ICFA.ICGA.ICGM.ICGT.ICGA.IRFA.IRFM.IRFT. 022650
          IRHT, IR GA. IO. LOG, IRHM, NUPOTS
C
      MEITE(KOUT.*) 'ENTER A C FOR CONTINUOUS TIME LOG CONTROLLES AND A 1 D FOR A SAMPLED DATA LOG CONTROLLES.'
                                                                          C 22 68 3
                                                                           322595
       READ (KIN, 12, END= 2933) MSG ___
                                                                           022713
       IF (KSG.EQ. "C") THEN
      __IFLGSD=0
       CALL CLAGRETGCSTR.FM.BM.PKFSS.HF.GCX.GCY.GCZ.ECY.ECZ.FC.YO.
                                                                           022733
         RM.QH.FT.BT.GT.GT.RT.HT.
    11RY . IFLGC Z . HM1 . HM2 . HM3
    1 .PO.GM.HM4.WM5.HM6.HV1.HV2.FUU.HXX.XO.HXU.HM7.HM8)
                                                                           222760
                                                                           022775
       IF (IO.EQ.S)THEN
      GO TG 2933
                                                                           022790
       END IF
       CALL FRHAUGIGT, RT. FT. BT. GCZ, HT. GCX, BCZ. FC. GCY, BCY. GT. XO. PO. FA. BA. 022802
      1 GA, QA, EUA, WH1, WH2, WHA, WHB, WFC, MMD, MME, WMF,
                                                                            0 2291:
   1 MAA .PXA, FA.PXVA.GCZA.IFY.IFLGCZ.IFLGSD)
                                                                           022923
       WRITE(KOUT, +) . .
                                                                           622835
       WRITE(KOUT .+) 'DO YOU WISH TO CALCULATE THE EIGENVALUES OF THE CLOSSESSES
      1ED-LCOP F MATRIX? Y OR No
       READ (KIN, 12) MSG
                                                                           322563
       IF (MSG.ED. Y') THEN
      MICHEL VASH
                                                                            0.22580
                                                                           022890
      NOIH1=NOIH2+1
                                                                           522903
       WPITE(KOUT, +) THE EIGENVALUES OF THE CLOSED-LOOP F MATRIX ARE... '822918
       CALL MEIGN (FA.HV3.HV4.IRFA.HPA)
                                                                           C22920
                                                                            122930
       NOIM=NSAV1
      NDIM1=NDIM+1
                                                                            0 22 340
                                                                            0 22 95 0
        END IF
      CALL MYINTG (HMA, HMB, HMC, HME, GA, QA, FA, BA, IRFA, ICGA, IRY, IRQA)
                                                                            522973
       ELSE
  C SOME SAMPLED DATA CONTROLLER IS MANTED
                                                                            022983
                                                                            022391
        IFLGSO=1
       WEITE(KOUT,+)'00 YOU WISH TO PERELY DISCRETIZE THE CONTINUOUS TIME 023300
      1 CONTROLLER, Y OR N>"
        READ (KIN, 12, END= 2933) MSG__
                                                                            523323
       IF (MSG.EQ. "Y") THEN
                                                                            023336
       WRITE(KOUT. *) ********NCTE THAT WHEN ENTERING THE TIME INCREMENT
                                                                            323345
      I IN THE CONTINUOUS TIME CONTROLLER SET UP. REMEMBER IT WILL BECCE 23050
    THE THE SAMPLE TIME FOR THE DISCRETIZED CONTROLLER********
                                                                            223363
        CALL CLOGRS (GCSTR, FM, BM, RKFSS, HM, GCX, GCY, GCZ, BCY, BCZ, FC, YD,
                                                                            023070
         RH.QH.FT.BT.GT.GT.RT.HT.IRY.IFLGCZ.HH1.HH2.HH3.PO.GH.
                                                                            623080
      1 RM40 MM5 , MM6 + MY1 + MY2 + MUU + MXX + XO + MXU + MM7 + MM8)
                                                                            023090
        IF (IO.EQ.G)THEN
                                                                            623109
                                                                            023110
        GO TC 2933
                                                                            D23126
        END IF
        GALL DSCRTZ(WM1, HM2, HM3, WM4, IRFM. DELTIM. FC. BCY, IRY. BCZ. IRMM.
       1 WMS WM6 GCSTR GT GT FT BT FIRFT ICGT ICBT IRHT RKESS RT GCX
                                                                            323140
                                                                            023150
       1 ICBM)
```

223165

-- WEITE(KOUT.-) * *

```
METTERKNUTGET TOO HOU AND TO CALCULATE THE ETGENGALUES OF THE STATURETY
     1E TRAISITID: MATRIX FUR THE DISCRETIZED CONTROLLER? Y OF MAT
                                                                                  023151
      # E 43 (KIN, 12) 45G
                                                                                  377107
      IF (MSG.EQ. TY!) THEN
                                                                                  023200
      WFITE(KOUT.+) *THE EIGENVALUES OF THE STATE TRANSITION MATRIX FOR TOZZZZZ
     THE DISCRETIZED CONTROLLER ASE...
                                                                                  223229
      CALL MEIGH(MM2, WV1, NV2, IRFM, ECY)
                                                                                  023233
END IF
C RKFSS, IN PRECEDING CALL STATEMENT ARE MERELY DUMMY WORK SPACES
                                                                                  023243
                                                                                  823250
   GCSTR CONTAINS BCZD UPON RETURN FROM DSCRTZ
                                                                                  023263
      CALL FRMAUG (HM6.RKFSS.HM5.GCSTR.GCZ.HT.GCX.HM4.HM2.GCY.HM3.HM1.X0.023276
     1 PJ.FA. BA. GA. CA. GUA. BCY. FC. APA. HHO, MHC. HHO, HHE, HFF. HXA. PXA. RA.
     1 PXVA,GCZA,IRY,IFLGCZ,IFLGSC)
      ELSE
                                                                                  023301
      IFLGCZ=0
                                                                                  023310
      CALL DLQGRS(GCX,GCY,GCZ,BCY,BCZ,WM3,FC,WM2,WM5,WM1,WM4,FM,BM,
                                                                                  023322
      1 QM.GM.RM.HM.GT.QT.FT.BT.RT.HT.HXX.HUU.GCSTR.RKFSS.YD.
                                                                                  023330
       IRY .IFLGCZ . WXU . HM6 . HM7 . HM8 . HM9 . HM1 . . HV1 . HV2)
                                                                                  623341
      CALL FRMAUG (HM1.HP2, MM3, NM4, GCZ, HT, GCX, BCZ, FC, GCY, BCY, HP5, XO.
                                                                                  623350
     1 PJ.FA.BA.GA.GA.GUA.RKFSS.GCSTR.HMA.HHB.HMC.HMD.HME.HMF.HXA.PXA.
                                                                                0 23 3 6 9
     1 RA, PXVA, GCZA, LRY, IFLGSZ, IFLGSD)
                                                                                  223370
  RKFSS.GCSTR ARE DUMMY WORK SPACE IN CALL TO FRMAUG
                                                                                  923389
      END IF
                                                                                  023390
      MSAV1=NDIM
      NSAVZ=NDIM1
                                                                                  223410
      NDIM1=NDI#2+1
                                                                                  023420
      NOIM=NOIM2
                                                                                  023435
      CALL EQUATE (WMA.FA, IRFA, IRFA)
      CALL EQUATE (WMC.BA. IRFA. IRY)
                                                                                  623450
                                                                                023460
        CALL MATI(GA, QA, IRFA, IRQA, IRQA, WME)
      CALL MAT4 (WME, GA, IRFA, IROA, IRFA, WMB)
                                                                                  C23470
      L VAZNEM I GN
                    NOIH1=NSAV2
                                                                                  023490
   NOTE FC AND BOY IN CALL TO FRHAUG ARE DUMMY HORKSPACES
                                                                                  C2350C
      END IF
                                                                                  023510
                                                                                  023523
      RETURN
2933
      IC= i
          F CR MAT (A1)
                                                                                  £23546
      END
                                                                                  023551
* DECK XSU
                                                                                  023563
      SUGRCUTINE XSU(X,S,U,PHIJG, BJO, PMII, INTPII, PHIJ, BJ.
       TEMP, TEMP1, TEMP2, FM, BM, IRFF, ICBM, WXX, MUU, WXU, PM, T)
IS ROUTINE COMPUTES X S AND U AT TIME T-SUB-I FOR USE IN THE
                                                                                  023580
    THIS ROUTINE COMPUTES X S AND U AT TIME T-SUB-I FOR USE
Samplec data controllerdeterministic gain calculation.
                                                                                  G23590
                                                                                  623600
    THIS ROUTINE APPROXIMATES THE INTEGRALSREQUIRED (SEE MAYBECK, EQUATIONS 14.25) BY TREATING TIME VAYING ENTITIES IN THE INTEGENOS AS CONSTANTS OVER SCHE SUBINTERVAL OF THE SAMPLE TIME
                                                                                  023623
                                                                                  623633
    THAT IS CHOSEN BY THE USER
                                                                                  023643
      REAL X (NOIM, NOIM). S(NOIM, NOIM), U(NOIM, NOIM),
                                                                                  023551
     1PHIJC(NOIM, NOIM), BJC(NOIP, NOIM), PHII(NOIM, NOIM),
     INTPIL (NOIM, NOIM), PHIJ(NOIM, NOIM), BJ(NOIM, NOIM),
                                                                                  023670
  ___ 1TEMP (NOIM, NOIM), TEMP1 (NOIM, NOIM), TEMP2 (NOIM, NOIM),
                                                                                  023683
     1FH(NOIH, NOIM), 3H (NOIH, NOIM), WXX(NOIM, NOIM),
                                                                                  023593
     1HUU (NOIP. NOIH), WXU(NOIM. NOIM), PHIT(NOIM. NOIM)
                                                                                  0237G3
      REAL COM1 (1) . COM2 (1)
                                                                                  323713
      CHARACTER MSG+61
                                                                                  623726
       CCMPON /PAIN1/NOIM.NDIM1.CCP1
                                                                                  023730
      COMMON/MAINZ/COMZ
                                                                                  0.23744
      COMMON JINOUZ KIN-KOUT-KPUNCH
                                                                                  023750
       COMMON /RNTIM/ RNTIME.DELTIM
                                                                                  023763
      COMMEN /MAUNE / MSG
                                                                                  623778
      IZIT=0
                                                                                  023780
      DO 782 IJK=1.1000
C _ GIVE USER UP TO 1316 CHANCES TO CHOOSE DIFFERENT SUBINTERVAL LENGTH 023800
      IF (IZIT.EG. 1) THEN
                                                                                  023810
      WPITE(KOUT.12)
                                                                                  02392:
```

	WHITE(KOUT-*1700 YOU WISH TO RECOMPUTE X.S.U. BASED ON A DIFFEREN	T 0 23
	I SUPINTERVAL LENGTH, YOUR 151	€23
	READ(KIN, 11) 45G	C 2 3
11	FORMAT (41)	¢23
12	FCRMAT(:1,/)	C 23
	IF (MSG.EG. 'N') THEN	023
	RETUEN	623
	ENO IF	023
	END IF	
	IZIT=1	623
-		623
	WRITE(KOUT, *) 'ENTER THE NUMBER OF SUBINTERVALS TO USE IN THE APPR	0 0 23
	1XIMATIONS OF INTEGRALS REECEC TO CALCULATE X. S. AND U (SUGGEST	<u> </u>
	1 OR FORE)>'	023
	READ (KIN, +) INTV AL	023
CN	IOW INITIALIZE VARIABLES FEQUIRED IN CALCULATIONS	623
	CON INTITALIZE VARIABLES "EQUIREC IN CALCULATIONS CONTROL CON	023
	GALL IONT (IRFM.PHIJO.C1)	023
	CALL IONT (IRFM, X, C1)	024
	CALL IONT (ICBM.U.C1)	624
	00 13 I=1.IRFH	C 2÷
	D3 13 J=1,ICBM	0 Z+
	BJ0(I:-1)=u	024
13	0=(L, I) 2	3 24
C 1	NITIALIZATION COMPLETS. NOW COMPUTE PHIJ. INTPHJ FOR SUBINTERVAL	324
Ē	HI.INTPHI ARE APPROXIMATED BY TAKING AVERAGE OF VALUES AT THE	G 24
CRE	GINNING .END AND 8 POINTS IN THE MIDDLE OF EACH SUBINTERVAL	C 24
ָ כ	THIS HEARS 9 SUB SUB INTERVAL PCINTS TO BE CALCULATED. HOWEVER. O	221
C	Y 1 CALL TO INTEGRATE ROUTINIS REQUIRED SINCE FM IS A CONSTANT	
		0 24
	IT RIX	024
	DEL=3.0	524
	SUBINT=DELTIN/(+*INTVAL)	C 24
	DO 23 JK=1, INTVAL	0 24
CC	CLB.JLING STADGU NEHT DNA LE LING STUGNC	024
	FCR EACH SUBINTERVAL	324
	C1=1.1	E 24
_	DC 371 INTVL=1,4	024
	OEL= CEL+SUBINT	024
	CALL DSGRT(IRFM,FM,DEL,PHII,INTPII,5)	
		024
_	GALL MADDI (IRFM, IRFM, PHIJC, PHII, TEMP, C1)	
	CALL EQUATE(PHIJO, TEMP, IRFK, IRFF)	824
C_PH	IJC=PHIJO+PHII	624
	CALL MATICINTPILOM, ISPH, IRSP, ICON, TEMPI)	024
	GALL HADDI (IRFH.ICAM.BJD.TEFFI.TEMP.C1)	024
	CALL EQUATE(BJO.TEMP.IRFM.ICEM)	02-
C 8	H8*II TTPI-CL8=OL	024
371		024
, 110	H CALCULATE BJ PHIJ	42.
	Clay.2	324
	CALL MSCALE(PHIJ.PHIJD, IRFM, IFFM, C1) CALL MSCALE(BJ.8J0.IRFM.ICBP.C1)	624
	CALL MOUNTE COUNTY THE MOUNT OF THE COUNTY O	0 Z4
. 8	J. PHIJ NOW AVAILABLE FOR THIS SUBINTERVAL	324
CA	16 SET PAT 10.49.10	£ 24
		G 24
	CALL EQUATE (3JO, TEMPL, 19FF, ICSM)	CZL
N	On UPDATE X.S.U FOR THIS SUBINTERVAL	324
	SUM OF (PHIJT-HXX-PHIJ-(DELTIP/INTVAL)) FOR ALL JK	C 24
	ESUM CF ((PHIJT+WXX+BJ+PHIJT+WXU)+(DELTIM/INTVAL))	
, , , 3		024
	CALL MATHA (PHIJ, WXX, IRF M, IRFM, TEMP)	024
G TE	MP= PHIJT - MXX	_524
	CALL MATI(TEMP, PHIJ, IRFP, IRFP, IRFM, TEMP1) CALL MATI(TEMP, PHIJ, IRFM, IRFM, TEMP2)	324
	CALL MATI(TEMP.BJ.IRFM.IRFM.ICBM.TEMP2)	024
•	C1A=DELTIM/INTVAL	324
		024
	CALL EQUATE (X. TEMP, IRFM, IPFF)	: 24
	. aaiaa. aaa aa ah aa iilaa iila iila aa .	
, ^	<u>IS NOW UPDATED FOR THIS SUB-SUB INTERVAL</u>	₩ € •

```
CALL HATHA (PHIJ. NXU, IPFF, IPFF, ICEM, IEMP1)
                                                                            [24-9]
      C1=1.0
                                                                             524500
      CALL MADD: (IRFM.ICBM.TEMP2.TEMP1.TEMP.C1)
                                                                            32451:
      CALL MADDI (IRFM. ICBM. S. TEMP. TEMP1. C14)
                                                                            02-523
      CALL EQUATE(S.TEMP1.IFFM.ICEM)
                                                                            026530
  S UPDATE FOR THIS SUE-SUB INTERNAL NOW COMPLETE
                                                                          324540
                                                                            024551
   U=SUM OF((3JT+XX*6J+HUU+3JT*XXV+WXUT+8J)*(DELTIM/INTVAL)) FCQ ALL JKS24560
      C1=1.0
                                                                            $24573
      CALL MATSA (ICBM, IRFM, BJ. WXX, TEMP)
                                                                            024583
      CALL MADDI (ICAM. ICAM. TEMP. WUU, TEMP1, C1)
                                                                            324592
      CALL MATLA (9J. HXU, ICEM, IRFM, ICEM, TEMP)
                                                                            024500
    CALL HADDITICSM, ICSM, TEMP1, TEMP, TEMP2, C1)
                                                                            024613
      CALL MAT44(HXU, BJ, ICBM, IRFM, ICBM, TEMP)
CALL MADD1(ICBM, ICBM, TEMP2, TEMP, TEMP1, C1)
                                                                            C24620
                                                                            024632
      CALL HADDI (ICH, ICH, TEMP1, TEMP, CIA) 024640
      CALL EQUATE (U, TEMP, ICBM, ICBM)
      UPDATE FOR THIS SUB-SUB INTERVAL NOW COMPLETE
        CONTINUE
                                                                            024670
                                                                         024683
      I0=5
      MSG='X(TI) IS'
                                                                            E24695
      CALL MMATIO(X.IRFP.IRFM.IO.KIN.KOUT.NOIM.NOIM)
                                                                            B24783
      MSG='U(TI) IS '
                                                                            G2471G
      CALL MMATIC(U, ICBM, ICBM, IG, KIN, KOUT, NOIM, NOIM)
                                                                            E24725
      MSG='S(TI) IS'
                                                                            024730
      CALL MMATIO(S, IRFM, ICBM, IC, KIN, KOUT, NOIM, NDIM)
                                                                            024740
      CONTINUE
                                                                            024750
      RETURN
                                                                            026760
      END
                                                                            024773
      SUB-CUTINE CNOISE (FM.GM.HM.BP.QM.IRFP.IQHP.ICGM.ICBM.WM1.WM2.WM3) 024780
      DIMENSION FH(NDIM, NDIM), HP(NDIM, NDIM), 8M(NDIM, NDIP), QM(NDIM, NDIM), C2479;
     1GH (NDIH, NOIH), COM1(1), W M1 (NDIM, NDIH), WH2(NDIH, NOIH), W M3 (NDIH, NDIH) G ZL 9 G G
      COMMEN/MAIN1/NDIM, NDIM1, COM1
                                                                            024810
      COMMON/INCU/KIN. KOUT. KPUNCH
                                                                            02452 J
25
      FORMAT (II)
                                                                            C24830
      WRITE(KOUT,+)'1ST OR 2NC DROER SHAPING FILTER (1 CR 2)>'
                                                                            024640
      FEAD (KIN, 25) ISIZE
                                                                            024850
    CALCULATE THE DIMENSION OF THE AUGHENTED SYSTEM
                                                                            024863
      IRFS=IRFH+(ISIZE+ICBM)
    IF (ISIZE.NE.1)GO TO 10
                                                                            024889
      CALL FORDER (FM.BH.GH.QH.HM.IRFH.IRHH.ICBH.ICGH.IRFS.HH1)
                                                                            324390
      60 TO 24
                                                                            324900
      CALL SORDER (FM, BM, GM, CM, FF, JAFM, IRHM, ICBM, ICGM, IRFS, WM1, WM2, WM3)
                                                                            024910
20
      CONTINUE
                                                                            024925
      RETURN
                                                                            C24933
      END
                                                                            624940
      SUBROUTINE FORDER (FM.BM.GM.GM.HP.IRFM.IRHP.ICBM.ICGM.IRFS.HU)
                                                                            024953
      DIMERSICH FMCHOIM, NOIM) . 8 M (NOIM, NOIM) . GM (NOIM, NOIM) . QM (NOIM, NOIM) . C24960
     1HH (HDIM-NOIM) .COM1(1) .COM2(1) .HU (NDIM-NDIM)
                                                                            024973
 COMMCN/MAIN1/NOIM.NDIM1.COM1
                                                                            024986
      COMPCH/MAINZ/COM2
                                                                            624390
      CC MMCN/INCU/KIN, KGUT, KFUNCM
      COMMEN/MAUNS/MSG
      REAL ENTRY SENTRY1
                                                                            $25020
      CHARACTER MSG-63
                                                                            2 25 1 3 3
C ZERO OUT BOTTON PARTITIONS OF GH, 9M, GH
                                                                            025040
      IFS=IRFH+1
                                                                            425053
      IGS=ICGM+1
                                                                            025463
      ICGS=ICGH+ICSH
                                                                            825370
      CALL ZPART (FM (IFS.1). ICBM, IRFS)
                                                                            0 25 38 3
      CALL ZPART (9M (IFS ,1) , IC9M, ICEP)
                                                                            025395
      CALL ZPART (GM (IFS .1) . I CBM . I CGS)
                                                                            0251GS
      CALL ZPART (MM (1, IFS), IRHM, ICEP)
                                                                            C25113
      CALL ZPART (QM (IGS.1). ICBM. ICGS)
                                                                            025 120
      CALL ZPART (OM (1.165). ICGM. ICBM)
                                                                            025133
      CALL ZPART (HU, ICBM, ICBM)
```

· · · · · · · · · · · · · · · · · · ·	
C DESIGN ONE SHAPING FILTER FOR EACH CONTROL CHANNEL	2515.
DC a_ IF=: .TCRM	225167
WFITE(KOUT,*) 'FILTER DESIGN ',IF	325175
METTE(KOUT.+) 'INPUT OFTIONS: (1) ENTER A AND R.	525183
WEITE(KOUT,*)'INPUT OFTICAS: (1) ENTER A AND B. 1(2) ENTER Q. (3) GO TO NEXT FILTER OR EXIT IF DONE!	0 25 19 1
00 93 17=1.52	625265
27 FORMAT (II)	25 21 3
WRITE(KGUT,*) 'OFTION>'	C 25 2 2 2 2
READ (KIN.27) I OPT	025232
	: : : 1
GO TO (1,2,3)!OPT 1	625245
	025253
READ (KIN, *) ENTRY, ENTRY 1	C 25 26 J
HU(IF.IF) = ENTAY-ENTRY1	02527C
FM((IRFF+IF), (IRFM+IF))=-1*ENTRY1	025 28 0
GO TC 93	C 25 29 C
2 HRITE(KOUT,*)'ENTER Q>'	625300
READ (KIN.+) ENTRY	025310
QM((IGGH+IF),(ICGH+IF))=ENTRY	025320
GC TC 9.	025330
9G CONTINUE	625346
3 CONTINUE	C 25 35 C
8G CONTINUE	0 25 36 0
C CALCULATE BH*HU AND PUT IN UPPER RIGHT PARTITION OF FM	625376
	025399
CALL MAT1(BM, HU, IFFM, ICBM, ICBM, FM(1, IFS)) C INSERT 9M INTO UPPER RIGHT PARTITION OF GM, DU=I CALL EQUATE(GM(1, IGS), BM, IRFM, ICBM)	025390
CINSERIO DE EN RIGHI PARILITUM DE GA, DOST	
	G 25 4 G C
C PUT AN IDENTITY MATRIX IN LCHER RIGHT PARTITION OF GM	025419
CALL IDNT(ICSM.GM(IGS,IGS),1.)	025420
C CHANGE COLUMN DIMENSION OF GM AND GROER OF SYSTEM	025420 125430
1001-1003	
IPFH=IRFS	C25456 - A
IHOLD=IO	525460
10=5	025476
msg= "omaug"	625480
CALL MMATIO (CM, ICGM, ICGM, IC, KIN, KOUT, NDIM, NDIM)	025490
IO=IHGLD	025500
RETURN	£2551C
ENO	C 25 5 2 3
SUBFCUTINE SORDER (FH.BH.GH.QF.HH.IRFH.IFH.ICAH.ICGM.IRFS.	025533
1HU oF Co GU)	\$25540
DIMENSION FM(NOIM, NOIM), 8M(NOIM, NOIM), GM(NOIM, NOIM),	0 25 5 5 5
10m (NDIM, ND IM), HM (NDIM, NDIP), HU (NDIM, NDIM), COM1(1).	225563
ACTION AS ENTANCEMENT OF THE ACTION OF THE A	025570
1COM2 (1) .FU (NDIM, NOIK) .GU (NDIY .NDIY)	
COMMON/MAIN1/NOIM, NOIM1, COM1	325583
	0 25 590
COHHCN/MAINZ/SOMZ	
COMMCN/INGU/KIN, KGUT, KPUNCH	C 25 60 C
COMMON/INGU/KIN, KGUT, KPUNCH COMMON/MAUN5/MSG	0 25 615
COMMON/INGU/KIN, KGUT, KPUNCH COMMON/MAUN5/MSG REAL ENTRY, ENTRY1, BAC.BTC	025613 025620
COMMON/INGU/KIN, KGUT, KPUNCH COMMON/MAUN5/MSG REAL ENTRY, ENTRY1, BAC, BTC IFS=IRFM+1	025613 025626 025630
COMMCN/INGU/KIN,KGUT,KPUNCH COMMCN/MAUN5/MSG PEAL ENTRY,ENTRY1,BAC,BTC IFS=IRFM+1 IGS=ICGM+1	0 25 613 0 25 62 0 0 25 63 0 0 25 64 0
COMMCN/INGU/KIN, KGUT, KPUNCH COMMCN/MAUN5/MSG PEAL ENTRY, ENTRY1, BAC, BTC IFS=IRFM+1 IGS=ICGM+1 ICGS=ICGM+1C9M	C 25 613 0 25 620 0 25 630 0 25 640
COMMCN/INGU/KIN, KGUT, KPUNCH COMMCN/MAUN5/MSG PEAL ENTRY, ENTRY1, BAC, BTC IFS=IRFM+1 IGS=ICGM+1 ICGS=ICGM+1C9M	C 25 613 0 25 620 0 25 630 0 25 640
COMMON/INGU/KIN, KGUT, KPUNCH COMMON/MAUN5/MSG PEAL ENTRY, ENTRY1, BAC, BTC IFS=IRFM+1 IGS=ICGM+1 ICGS=ICGM+1CBM ICBM2=2*ICBM CALL ZPART(FM(IFS, 1), ICBM2, IRFS)	C 25 61 3 0 25 62 6 0 25 63 6 0 25 64 9 6 25 65 0 0 25 67 0
COMMON/INGU/KIN, KGUT, KPUNCH COMMON/MAUN5/MSG PEAL ENTRY, ENTRY1, BAC, BTC IFS=IRFM+1 IGS=ICGM+1 ICGS=ICGM+1CBM ICBM2=2*ICBM CALL ZPART(FM(IFS, 1), ICBM2, IRFS)	C 25 61 3 0 25 62 6 0 25 63 6 0 25 64 9 6 25 65 0 0 25 66 0
COMMON/INGU/KIN, KGUT, KPUNCH COMMON/MAUN5/MSG REAL ENTRY, ENTRY1, BAC, BTC IFS=IRFM+1 IGS=ICGM+1 ICGS=ICGM+1CBM ICBM2=2+ICBM CALL ZPART(FM(IFS,1), ICBM2, IRFS) CALL ZPART(BM(IFS,1), ICBM2, ICBM)	C 25 613 0 25 62 0 0 25 63 0 0 25 64 0 0 25 65 0 0 25 66 0 0 25 68 0
COMMON/INGU/KIN, KGUT, KPUNCH COMMON/MAUN5/MSG REAL ENTRY, ENTRY1, BAC, BTC IFS=IRFM+1 IGS=ICGM+1 ICGS=ICGM+1CBM ICBM2=2+ICBM CALL ZPART(FM(IFS,1), ICBM2, IRFS) CALL ZPART(BM(IFS,1), ICBM2, ICBM) CALL ZPART(BM(IFS,1), ICBM2, ICBM) CALL ZPART(BM(IFS,1), ICBM2, ICBM)	C 25 613 0 25 62 0 0 25 63 0 0 25 64 0 0 25 65 0 0 25 66 0 0 25 68 0 0 25 68 0
COMMON/INGU/KIN, KGUT, KPUNCH COMMON/MAUN5/MSG REAL ENTRY, ENTRY1, BAC, BTC IFS=IRFM+1 IGS=ICGM+1 ICGS=ICGM+ICBM ICBM2=2+ICBM CALL ZPART(FM(IFS,1), ICBM2, IRFS) CALL ZPART(BM(IFS,1), ICBM2, ICBM) CALL ZPART(OM(IGS,1), ICBM, ICGS) CALL ZPART(OM(IGS,1), ICBM, ICGS) CALL ZPART(OM(IGS,1), ICBM, ICGS)	C 25 613 0 25 62 0 0 25 63 0 0 25 64 0 0 25 65 0 0 25 66 0 0 25 68 0 0 25 68 0 0 25 68 0
COMMON/INGU/KIN, KGUT, KPUNCH COMMON/MAUN5/MSG REAL ENTRY, ENTRY1, BAC, BTC IFS=IRFM+1 IGS=ICGM+1 ICGS=ICGM+ICBM ICBM2=2+ICBM CALL ZPART(FM(IFS,1), ICBM2, IRFS) CALL ZPART(SM(IFS,1), ICBM2, ICBM) CALL ZPART(SM(IFS,1), ICBM, ICGS) CALL ZPART(GM(IFS,1), ICBM, ICGS) CALL ZPART(GM(IFS,1), ICBM, ICGS) CALL ZPART(GM(IFS,1), ICBM, ICGS)	C 25 613 0 25 62 0 0 25 63 0 0 25 64 0 0 25 66 0 0 25 67 0 0 25 68 0 0 25 7 0 0 0 25 7 1 0
COMMON/INGU/KIN, KGUT, KPUNCH COMMON/MAUN5/MSG REAL ENTRY, ENTRY1. BAC.BTC IFS=IRFM+1 IGS=IGGM+1 ICGS=IGGM+ICBM ICBM2=2+ICBM CALL ZPART(FM(IFS,1), ICBM2.IRFS) CALL ZPART(BM(IFS,1), ICBM2.ICBM) CALL ZPART(GM(IGS,1), ICBM, ICGS) CALL ZPART(GM(IGS,1), ICBM, ICGS) CALL ZPART(GM(IFS,1), ICBM, ICGS)	C 25 613 0 25 62 0 0 25 63 0 0 25 64 0 0 25 66 0 0 25 67 0 0 25 68 0 0 25 7 0 0 0 25 7 2 0
COMMON/INGU/KIN, KGUT, KPUNCH COMMON/MAUN5/MSG PEAL ENTRY, ENTRY1, BAC, BTC IFS=IRFM+1 IGS=ICGM+1 ICGS=ICGM+ICBM ICBM2=2*ICBM CALL ZPART(FM(IFS,1), ICBM2, IRFS) CALL ZPART(GM(IFS,1), ICBM2, ICBM) CALL ZPART(GM(IFS,1), ICBM2, ICBM) CALL ZPART(GM(IFS,1), ICBM2, ICBM) CALL ZPART(GM(IFS,1), ICBM2, ICGS) CALL ZPART(GM(IFS,1), ICBM2, ICGS) CALL ZPART(GM(IFS,1), ICBM2, ICGS) CALL ZPART(GM(IFS,1), IRFM, ICBM) CALL ZPART(GM(1, IGS), IRFM, ICBM2)	C 25 613 0 25 623 C 25 643 C 25 653 C 25 663 C 25 663 C 25 683 C 25 730 C 25 730 C 25 730
COMMON/INGU/KIN, KGUT, KPUNCH COMMON/MAUN5/MSG PEAL ENTRY, ENTRY1, BAC, BTC IFS=IRFM+1 IGS=ICGM+1 ICGS=ICGM+ICBM ICBM2=2+ICBM CALL ZPART(FM(IFS,1), ICBM2, IRFS) CALL ZPART(BM(IFS,1), ICBM2, ICBM) CALL ZPART(BM(IGS,1), ICBM2, ICBM) CALL ZPART(GM(IGS,1), ICBM2, ICBM) CALL ZPART(GM(IFS,1), ICBM2, ICGS) CALL ZPART(GM(IFS,1), ICBM2, ICGS) CALL ZPART(GM(IFS,1), ICBM2, ICGS) CALL ZPART(GM(1, IGS), IRFM, ICBM2) CALL ZPART(HM(1, IFS), IRMM, ICBM2) CALL ZPART(FU, ICBM2, ICBM2)	C 25 613 0 25 623 0 25 633 0 25 653 0 25 663 0 25 683 0 25 70 0 25 710 0 25 720 0 25 730 0 25 74 6
COMMON/INGU/KIN, KGUT, KPUNCH COMMON/MAUN5/MSG REAL ENTRY, ENTRY1, BAC, BTC IFS=IRFM+1 IGS=ICGM+1 ICGS=ICGM+ICBM ICBM2=2+ICBM CALL ZPART(FM(IFS,1), ICBM2, IRFS) CALL ZPART(GM(IFS,1), ICBM2, ICBM) CALL ZPART(GM(IGS,1), ICBM2, ICBM) CALL ZPART(GM(IFS,1), ICBM2, ICGM) CALL ZPART(GM(IFS,1), ICGM, ICEM) CALL ZPART(GM(IFS,1), ICGM2, ICGS) CALL ZPART(GM(IFS,1), ICGM2, ICGM2) CALL ZPART(HM(1, IGS), IRFM, ICBM2) CALL ZPART(HM(1, IFS), IRMM, ICGM2) CALL ZPART(HM(1, ICBM2, ICBM2)	C 25 613 0 25 623 0 25 633 0 25 653 0 25 663 0 25 683 0 25 683 0 25 70 0 25 710 0 25 720 0 25 730 0 25 730 0 25 730
COMMON/INGU/KIN, KGUT, KPUNCH COMMON/MAUN5/MSG REAL ENTRY, ENTRY1, BAC, BTC IFS=IRFM+1 IGS=ICGM+1 ICGS=ICGM+ICBM ICBM2=2*ICBM CALL ZPART(FM(IFS,1), ICBM2, IRFS) CALL ZPART(GM(IFS,1), ICBM2, ICBM) CALL ZPART(GM(IFS,1), ICBM, ICGS) CALL ZPART(GM(IFS,1), ICBM, ICGS) CALL ZPART(GM(IFS,1), ICBM, ICGM) CALL ZPART(GM(IFS,1), ICBM, ICGM) CALL ZPART(GM(I, IGS), IRFM, ICBM2) CALL ZPART(HU, ICBM2, ICBM2) CALL ZPART(HU, ICBM2, ICBM2) CALL ZPART(GM, ICBM2, ICBM2)	C 25 613 0 25 623 0 25 633 0 25 643 0 25 663 0 25 670 0 25 683 0 25 70 0 25 710 0 25 710 0 25 730 0 25 730 0 25 740 0 25 760
COMMON/INGU/KIN, KGUT, KPUNCH COMMON/MAUN5/MSG REAL ENTRY, ENTRY1, BAC, BTC IFS=IRFM+1 IGS=ICGM+1 ICGS=ICGM+ICBM ICBM2=2*ICBM CALL ZPART(FM(IFS,1), ICBM2, IRFS) CALL ZPART(GM(IFS,1), ICBM2, ICGM) CALL ZPART(GM(IFS,1), ICGM, ICGS) CALL ZPART(GM(IFS,1), ICGM, ICGS) CALL ZPART(GM(IFS,1), ICGM, ICGS) CALL ZPART(GM(IFS,1), ICGM2, ICGS) CALL ZPART(GM(IFS,1), ICGM2, ICGM) CALL ZPART(GM(I, IGS), IRFM, ICGM2) CALL ZPART(HM(1, IFS), IRMM, ICGM2) CALL ZPART(HM(1, ICGM2, ICGM2) CALL ZPART(GU, ICGM2, ICGM2)	C 25 613 0 25 623 0 25 643 C 25 643 C 25 663 0 25 663 0 25 670 1 25 683 0 25 710 0 25 710 0 25 730 0 25 740 C 25 750 C 25 760 C 25 760 C 25 770
COMMON/INGU/KIN, KGUT, KPUNCH COMMON/MAUN5/MSG PEAL ENTRY, ENTRY1, BAC, BTC IFS=IRFM+1 IGS=ICGM+1 ICGS=ICGM+1CBM ICBM2=2*ICBM CALL ZPART(FM(IFS,1), ICBM2, IRFS) CALL ZPART(GM(IFS,1), ICBM2, ICGM) CALL ZPART(GM(IFS,1), ICGM, ICGS) CALL ZPART(GM(I, IGS), ICGM, ICGM) CALL ZPART(GM(1, IGS), IRFM, ICGM) CALL ZPART(GM(1, IGS), IRFM, ICBM) CALL ZPART(FU, ICBM2, ICBM2) CALL ZPART(FU, ICBM2, ICBM2) CALL ZPART(GU, ICBM2, ICBM2)	C 25 613 0 25 623 0 25 643 C 25 643 C 25 663 0 25 663 0 25 683 0 25 683 0 25 70 0 25 710 0 25 73 C 25 73 C 25 74 C 25 76 C 2
COMMON/INGU/KIN, KGUT, KPUNCH COMMON/MAUN5/MSG PEAL ENTRY, ENTRY1, BAC, BTC IFS=IRFM+1 IGS=IGGM+1 ICGS=IGGM+ICBM ICBM2=2+ICBM CALL ZPART(FM(IFS,1), ICBM2, IRFS) CALL ZPART(BM(IFS,1), ICBM2, ICBM) CALL ZPART(GM(IGS,1), ICBM, ICGS) CALL ZPART(GM(IFS,1), ICBM, ICGS) CALL ZPART(GM(IFS,1), ICBM2, ICGS) CALL ZPART(GM(I, IGS), IRFM, ICBM) CALL ZPART(GM(I, IGS), IRFM, ICBM) CALL ZPART(FU, ICBM2, ICBM2) CALL ZPART(GM, ICBM2, ICBM2) CALL ZPART(GU, ICBM2, ICBM) CALL ZPART(GU, ICBM2, ICBM) C DESIGN ONE SHAPING FILTER PER CONTROL CHANNEL DO 80 IF=1, ICBM WRITE(KOUT,*)*FILTER DESIGN*, IF	C 25 613 0 25 623 0 25 643 C 25 643 C 25 663 O 25 663 O 25 683 O 25 683 O 25 700 O 25 710 O 25 720 O 25 730 C 25 746 C 25 760 O 25 770 O 25 770 O 25 770 O 25 770 O 25 770
COMMON/INGU/KIN, KGUT, KPUNCH COMMON/MAUN5/MSG PEAL ENTRY, ENTRY1, BAC, BTC IFS=IRFM+1 IGS=ICGM+1 ICGS=ICGM+1CBM ICBM2=2*ICBM CALL ZPART(FM(IFS,1), ICBM2, IRFS) CALL ZPART(GM(IFS,1), ICBM2, ICGM) CALL ZPART(GM(IFS,1), ICGM, ICGS) CALL ZPART(GM(I, IGS), ICGM, ICGM) CALL ZPART(GM(1, IGS), IRFM, ICGM) CALL ZPART(GM(1, IGS), IRFM, ICBM) CALL ZPART(FU, ICBM2, ICBM2) CALL ZPART(FU, ICBM2, ICBM2) CALL ZPART(GU, ICBM2, ICBM2)	C 25 613 0 25 623 0 25 643 C 25 643 C 25 663 O 25 663 O 25 683 O 25 683 O 25 700 O 25 710 O 25 720 O 25 730 C 25 746 C 25 760 O 25 770 O 25 770 O 25 770 O 25 770 O 25 770

SCHOOLS IN CONTROL OF THE CONTROL OF

	1(3) ENTER Q. (4) GO TO NEXT FILTER OR EXIT IF DONE!	1253
	DC 9, IT=1,50	125 5 20
	WRITE(KOUT.*)'OPTION>'	[25:31]
26	FORMAT (II)	62534
20	READ (KIN, 28) IOPT	025 950
	GC TG (1,2,3,4) ICFT	25 3 6 1
1	WRITE(KOUT.*) 'ENTER A>'	6 25 67 6
•	READ(KIN,+)ENTRY	C 25 983
	HU(1F, (2+1F-1)) = ENTRY	625 890
	HU(IF.(2*IF))=1.	625980
	GO TO 90	025910
2	HRITE(KOUT,+)'ENTER 9 AND C>'	\$25920
<u> </u>	READ (KIN, *) ENTRY, ENTRY1	C 25936
	BAC==1* (ENTRY+ENTRY1)	825940
	BTC=-1* (ENTRY*ENTRY1)	625 95 0
	FU((2*IF-1).(2*IF))=1.	02596C
• •	FU((2*IF),(2*IF-1)) =BTC	£25.27¢
	FU((2*IF),(2*IF))*BAC	025950 A
	GO TC 90	£ 25 990
3	WRITE(KOUT,*) 'ENTER Q>'	026303
	READ (KIN,+) ENTRY	026313
	QM((ICGM+IF), (ICGP+IF))=ENTRY	026329
90 -	CONTINUE	026:30
4	CONTÎNUE	0.260.40
	GU ((IF + 2) , IF) = 1 .	626250
90	CONTINUE	0 26 56 3
C	CALCULATE 9HU AND PUT IN UPPER RIGHT PAPTITION OF FM	0 26 0 7 0
	CALL MNUL(BM.MU.IRFM.ICBM.ICBM2.FM(1.IFS))	0 26 2 8 0
C	INSERT FU INTO LOWER RIGHT PARTITION OF FM	0.26090
	CALL EQUATE (FM (IFS. IFS) .FU.ICEM2.ICEM2)	026133
C	INSERT GU INTO LONER RIGHT FARTITION OF GM	C25113
	CALL EQUATE(GM(IFS,IGS),GU,ICBM2,ICBM)	C26125
C	CHANGE COLUMN DIMENSION OF GM AND ORDER OF SYSTEM	£2613ú
	ICGM=ICGS	C 26 14C
	IRF#=IRFS	6 25 15 0
	RETURN	026160
	END	026170

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APPENDIX C: Modifications and Additions to CGTPI

C.I Introduction

This appendix is intended to be used as a supplement to References 13 and 30. These sequences are user's guides to a computer-aided design program for designing controllers employing a Command Generator Tracker in the feedforward loop and a Proportional-plus-Integral regulator in the feedback loop (CGTPI). Reference 13 describes the original version of the program. Reference 30 contains a modified version that admits implicit model following for design of controller gains and that can be run in conjunction with a performance evaluation program (PFEVAL), described in the same reference. Modifications outlined in this chapter are made to the version in Reference 30.

As stated in Chapter III, only the PI regulator design portion of the program is used for this thesis. However, to execute PFEVAL, the user must first execute all three design paths of CGTPI. These include the PI regulator design, CGT design, and Kalman filter design. By proper choice of the CGT model matrices, the controlled degenerates into a simple PI regulator. These matrices are defined below:

$$A_{m} = [I] \tag{C-1}$$

$$B_{m} = [0] \tag{C-2}$$

$$C_{m} = [0] \tag{C-3}$$

$$D_{m} = [I] \tag{C-4}$$

Modifications to the program include an additional subroutine to apply the Doyle and Stein technique. This is bracketed and marked with

an "A" in the source code at the end of this appendix. Modifications to allow inputting colored-noise into the design model are bracketed and marked with an "M". Since the modifications made to CGTPI are not extensive, only the specific subroutines that contain changes are listed.

C.2 Additions to CGTPI

One additional subroutine is added to CGTPI to allow modification of the dynamic driving noise covariance matrix, Q_d , via the Doyle and Stein technique as described in Section 3.4 Subroutine DAS is listed in lines 29730 through 29940. When executing the Kalman filter design option of CGTPI, this subroutine is called in line 18730. An input prompt will ask if the Doyle and Stein modification is desired. If so, then a prompt will ask for the scalar design parameter, q. The Q_d matrix is then modified as expressed in Equation (3-43) with the assumption that V = I. The modified Q_d matrix is also written to the LIST file.

C.3 Modifications to CGTPI

The original version of CGTPI was not written with the intention of augmenting additional states with the design model. The modifications listed in the source code in this appendix will allow the technique of injecting time-correlated noise into the design model, but the method is awkward as will become apparent.

To apply the technique requires two executions of CGTPI. In the first execution, the unaugmented design model and truth model are entered to the program. Then, the PI regulator design, CGT design, and Kalman filter design paths are executed normally. All prompts to enter either filter gains or CGT gains should be answered with an "N". In the CGT

design path, the model matrices listed in Equations (D-1) through (D-4) can be entered if only a PI regulator is desired. It is useful to write the truth model to the SAVE file. An input prompt asks if it is desired to write the model to the SAVE file. If a "Y" is entered, the model matrices are stored by the program. This file is structured so that the design model, truth model, regulator gains, CGT gains, and command model can all be written to the file for later use. Copying the SAVE file to a DATA file allows the model and gain matrices to be read directly into the program, rather than be inputted from a terminal (Ref 13). The regulator and CGT gains are also written to the SAVE file. After following all three design paths, execution of the program is halted.

Prior to the second execution, the SAVE file is copied to a DATA file. Also, it is necessary to have the augmented matrices specified in Chapter IV available to be read into the program from the terminal. In the second execution, the augmented system is entered into the design model. The truth model can be read from the DATA file containing information from the previous execution. After entering the model, the CGT path is followed again. A prompt will ask if it is desired to read in the CGT gains. A "Y" is entered, the gains are read from the DATA file, and this path is exited. This modification is listed in lines 6600 to 6630 and 6910.

Next, the Kalman filter design path is followed with the augmented design model. After execution of this option, a prompt will inquire if it is desired to store performance analysis data to the SAVE file.

A "Y" is entered, and another prompt will inquire if it is desired to

read controller gains from the DATA file. Again, a "Y" is entered. The modifications in lines 27230 through 27430 allow the program to read in PI controller gains from the previous execution and augment with columns by zeros so that the shaping filter states are not fed back through the controller. Performance evaluation data is stored and PFEVAL can thus be run normally as described in Reference 30.

The modified version also allows the option of reading in Kalman filter gains from a previous execution stored on the DATA file. These modifications are listed in lines 4230 to 4320.

Final modifications are given in lines 4470 through 4610 to reformat the PI controller gains and allow storage room for the augmented zeros.

```
SUBROUTINE COTXO
2960=
2970=
           COMMON/MAIN1/NOIH, NDIH1, COML(1)
           COHMON/MAIN2/COM2(1)
2980=
2990=
           COMMON/INOU/KIN.KOUT.KPUNCH
           COMMON/DESIGN/NVCOM, TSAMP, LFLRPI, LFLCGT, LFLKF, LTEVAL, LABORT
3000=
           COMMON/FILES/KSAVE, KDATA, KPLOT, KLIST, KTERM
3010=
3020=
           COMMON/SYSMTX/NUSM, SM(1)
           COMMON/ZMTX1/NVZM,ZM1(1)
3030=
3040=
           COHMON/ZMTX2/ZM2(1)
           COMMON/NDIMD/NND, NRD, NPD, NMD, NDD, NWD, NWDD, NPLD, NWPNWD, NNPR
3050=
3060=
           COMMON/LOCD/LAP,LGP,LPHI,LBD,LEX,LPHD,LQ,LQN,LQD,LC,LDY,LEY
3065=
          1, LHP, LR
3070=
           COMMON/DSNMTX/NVDM.NODY.NGEY.DM(1)
=050E
           COMMON/NDIMC/NNC,NRC,NPC
3090=
           COMMON/LOCC/LPHC,LBDC,LCC,LDC
           COMMON/CHOMIX/NVCH, NEWCH, NODC, CH(1)
3100=
3110=
           COMMON/NDIMT/NNT, NRT, NMT, NWT
3120=
           COMMON/LOCT/LPHT, LBOT, LQDT, LHT, LRT, LTDT, LTNT
           COMMON/TRUMTX/NVTM, TM(1)
3130=
3140=
           COMMON/LENTRL/LPI11, LPI12, LPI21, LPI22, LFHDL, LBDL
           COMMON/CONTROL/NVCTL,CTL(1)
3150=
           COMMON/LREGPI/LXDW.LUDW.LPHCL.LKX.LKZ
3140=
           COMMON/CREGPI/NVRPI,RPI(1)
3170=
3190=
           COMMON/LCGT/LA11,LA13,LA21,LA23,LA12,LA22,LKXA11,LKXA12,
3135=
           1LKXA13
           COMMON/CCGT/NUCGT,CGT(1)
3190=
3200=
           COMMON/LKF/LEADSN,LFLTRK,LFCOV
           COMMON/CKF/NUFLT, FLT(1)
3210=
3220=
           COMMON/AMC/AM(1)
           COMMON/BDG/BD(1)
3230=
3240=
           DIMENSION LD(15),ND(15)
3250=
           DATA NPLTZM/606/
3240=
           DATA IEOI,NO/-1,1HN/
           REWIND KLIST
3270=
3280=
           WRITE(KLIST, 115) DATE(DUM), TIME(DUM)
3290=
           WRITE(KTERM,115) DATE(DUM),TIME(DUM)
3300= 115
           FORMAT("1",27X,"* * * CGTPJF * * *"/14X,
          1 "PROGRAM TO DESIGN A COMMAND GENERATOR TRACKER"/8X,
3310=
          2 'USING A REGULATOR WITH PROPORTIONAL PLUS INTEGRAL CONTROL
3320=
          1º/15X,
3325=
3330=
          3 'AND A KALMAN FILTER FOR STATE ESTIMATION. 1/28X,
3340=
           4 "* * * CGTPIF * * **//L1X, DATE : ", A10//, 11X,
          5 'TIME : ",A10////)
3350=
           REWIND KSAVE
3360=
3370=
           REWIND KNATA
3380=
           WRITE(KSAVE, 112) IFOI, NPLTZM
3390=
           DO 10 I=1,15
3400= 10
           ND(I)=0
3410=
           DO 12 I=1,15
3420= 12
           LD(I)=1
3430=
           LFLRPI =0
           LFLCGT=0
3440=
3450=
           LFLKF=0
           LTEVAL=0
3460=
3470=
           LABORT=0
```

3480=

TPT=0

```
ICGT=0
3490=
3500=
           ITRU=0
           IFLTR=0
3510=
           ICODE=4
3520=
3530=
           LFAVAL=0
           LGCGT=0
3540=
           NUCOM=MINO(NDIM,NUZM)
3550=
           KOUT=KLIST
3560=
3570=
           KPUNCH=KPI_OT
           (F(NVSM.GE.NPLTZM) GO TO 50
3580=
3590=
           WRITE 101, NPLTZM
           GO TO 1000
3600=
           WRITE 102
3610= 50
           READ*, TSAMP
3620=
            IF(TSAMP.LE.O.) GO TO 50
3630=
3640=
           WRITE(KLIST.103) TSAMP
           FORMAT( 'OSAMPLE PERIOD IS ',F3.3, ' SECONDS')
3650= 103
           CALL SETUP(ND, LD, ICGT, ITRU, 1)
3660=
            IF(LABORT) 1000,100,1000
3670=
3680= 100
           LAPORT=0
            WRITE 104
3690=
           FORMAT( *OCONTROLLER DESIGN (Y OR N) >*)
3700= 104
            READ 111, TANS
3710=
            IF(TANS.EQ.NO) GO TO 500
3720=
3730=
            LFLKF=0
3740=
            CALL PINTX(IPI)
3750=
            IF(LABORT) 1000,125,1000
3760= 125
            WRITE LOS
            FORMAT("OBESTON REG/PI (Y CR N) >")
3770= 105
3730=
            READ 111, IANS
            IF(IANS.EQ.NO) GO TO 150
3790=
3800=
            CALL SREGPI
            IF(LARORT) 1000,200,1000
3810=
            WRITE 104
3820= 150
            FORMAT("ODESIGN CGT (Y OR N) >")
3830= 106
            READ 111, IANS
3840=
            JF(IANS.EG.NO) GO TO 100
3850=
            CALL SETUP(ND, LD, ICGT, ITRU, 2)
3860=
3870=
            WRITE 117
            FORMAT( OTERNINATE COT DESIGN PATH (Y OR N)? >")
3880 = 117
3890=
            READ 111, JANS
            IF(IANS.NE.NO) GO TO 500
3900=
3910=
            IF(ICGT) 155,100,155
            IF(LABORT) 100,160,1000
3920= 155
3930= 160
            CALL SCGT
            TF(LABORT) 100,170,1000
3940=
3950= 170
            IF(LFLCGT.LE.O) GO TO 125
3960= 200
            LABORT=0
            WRITE 107
FORMAT(*OCCUNTROLLER EVALUATION WRT TRUTH HODEL (Y OR N) >*)
3970=
3980= 107
3790=
            READ 111, IANS
4000=
            IF(IANS.EQ.NO) GO TO 250
            CALL SETUP(ND, LD, ICGT, ITRU, 3)
 4010=
            IF(LABORT) 200,250,1000
 4020=
4030= 250
            LTEVAL=0
            CALL CEVAL
 4040= 260
            IF(LFLCGT.EG.1) LGCGT=1
 4050=
            IF(LFAVAL.ED.O.OR.LGCGT.ER.O) 50 TO 100
 4040=
            WRITE 600
 4070= 270
```

```
4030= 400
               FORMAT("OWRITE PERFORMANCE EVALUATION DATA TO "SAVE" FILE
    4085=
               TIT OR NO
    4090=
               +>*)
    4100=
                READ 111, IANS
    4110=
                IF(IANS.EG.NO) GO TO 100
                ICODE=ICODE+1
    4120=
    4130=
                CALL PEDATA (ICODE, ND)
    4140=
                INUM=ICODE-4
    4150=
                WRITE 605. INUM
              FORMAT( *OPERFORMANCE EVALUATION DATA, NO. *12, *, WRITTEN TO
    4160= 605
  'SAVE
    4170=
               +' FILE")
                GO TO 100
    4180=
               LABORT=0
    4190= 500
    4200=
                WRITE 108
    4210= 108
                FORMAT("OFFLITER DESIGN (Y OR N) >")
                READ 111, TANS
    4220=
    4230=
                IF(IANS.EG.NO) GO TO 900
    4240=
                WRITE 777
    4250=777
                FORMAT("OREAD IN COT GAINS (Y OR N) >")
    4260=
                READ 111, TANS
    4270=
                IF(IANS.EG.NO) GO TO 505
M -
    4280=
                IF (LGCGT.NE.O) GO TO 505
                IF (IFLTR.NE.O) GO TO 505
    4290=
    4300=
                CALL READFS(SM, ND, 4, IERR)
                LGCGT=ND(2)
    4310=
    4320=505
                CALL FLTRK(IFLTR)
    4330=
                IF(IFLTR.E0.0) GO TO 900
                IF(LABORT) 1000,510,1000
    4340=
                CALL SETUP(ND,LD,ICGT,ITRU,3)
    4350= 510
    4360=
                IF(LABORT) 500,525,1000
                CALL FEVAL
    4370= 525
    4380= 530
                 IF(LABORT) 1000,540,1000
    4390= 540
                 LFAVAL=1
     4400=
                IF(LGCGT.EG.1) GO TO 270
    4410=
                60 TO 500
    4420= 700
                HRITE 109
                FORMAT("GEND DESIGN RUNS (Y OR N) >")
     4430= 109
    4440=
                READ 111, IANS
     4450=
                IF(IANS.EG.NO) GO TO 100
                IF(LFLRPI.EG.0) GO TO 1000
     4460=
    4470=
                NPNTS=NRD*NNPR
                ND(1)=NPNTS
     4480=
     4490=
                NIK(2)=LGCGT
    4500=
                ND(3)=LKX
    4510=
                NO(4)=LKZ
                CALL FTMTX(RPI(LKX),SM,NPNTS,1)
    4520=
     4530=
                ND(5)=NPNTS+1
                IF(LGCGT.EQ.O) GO TO 910
     4540=
     4550=
                ND(6)=LKXA11
     4560=
                ND(7)=LKXA12
                ND(8)=LKXA13
     4570=
                NPNTS=NRD*(NNC+NRC+NDD)
    4580=
                ND(1)=ND(1)+NPNTS
     4590=
                CALL FTHTX(CGT(LKXALL),SH(ND(5)),NPNTS,1)
     4600=
    4610=710
                CALL WETLED(4,ND(1),ND,SM)
     4620=
                WRITE 113
     4630= 1000 CONTINUE
                WRITE(KLIST, L10)
     4540=
```

のでは、**一般である。このは、一般のである。**

Parameter recognition (

```
REMIND KRAVE
4650=
           REWIND KDATA
4660=
4670=
           REWIND KLIST
4680=
           WRITE 110
           FORMAT( *OINSUFFICIENT MEMORY /SYSMTX/, NFED: *,14)
4690= 101
           FORMAT( *OENTER SAMPLE PERIOD FOR DIGITAL CONTROLLER >*)
4700= 102
           FORMAT( *OPROGRAM EXECUTION STOP*)
4710= 110
4720= 111
           FORMAT(A3)
4730= 112
           FORMAT(214)
4740= 113
47:0=
           FORMAT(6x, "REG/PI GAINS WRITTEN TO 'SAVE' FILE")
           RETURN
4740=C END SUBROUTINE CGTXQ
```

```
SUBMOUTINE SCHO(ND, LD, ICGT)
6390=
           COMMON/DESIGN/NUCOM, TSAMP, LFLRPI, LFLCGT, LFLKF, LTEVAL, LABORT
6400=
6410=
           COMMON/FILES/KSAVE, KDATA, KPLOT, KLIST, KTERM
6420=
           COMMON/SYSMIX/NUSM.SM(1)
6430=
           COMMON/ZMTX1/NVZM,ZM1(1)
5440=
           COMMON/ZMTX2/ZM2(1)
           COMMON/NDIMD/NND, NRD, NPD, NMD, NDD, NWD, NWDD. NPLD. NWFNWD, NNFR
6450=
           COMMON/NOTHC/NNC, NRC, NPC
6460=
           COMMON/CMBMTX/NVCM.NEWCH.NGDC.CM(1)
6470=
           COMMON/LREGPI/LXDN.LUDW.LPHCL.LKX.LKZ
4480=
5490=
           COMMON/CREGPT/NVRPI,RPI(1)
           DIMENSION ND(1),LD(1)
4500=
6510=
           DATA NO/1HN/
6520=
           WRITE(KLIST, 110)
          FORMAT(////11X,5(** *),*CGT DESIGN*,5(* **)////)
6530= 110
4540=
           NEWCH=0
6550=
           IF(LFLRPI) 10,5,10
4540= S
           WRITE 102
6570=
           READ 111, IANS
6530=
            IF(IANS,EQ.NO) GO TO 8
=90ق
           CALL READFS(SM,ND,4, IERR)
3400<del>=</del>
           NSIZE=ND(5)-1
           LKX=ND(3)
5610=
4420=
           LKZ=ND(4)
6630=
           CALL FTMTX(SM, RPI(LKX).NSIZE, 1)
IF(IERR.NE.O) RETURN
           CALL MATLST(RPI(LKX), NRD, NND, *KX*, KLIST)
6650≈
5660=
           CALL MATLST(RPI(LKZ).NRD,NRD.*KZ*,KLIST)
6670=
            LFLRPI=-1
=086
           GO TO 10
6690= 8
            IF(LFLCGT.GE.O) GO TO 9
6700=
            WRITE 103
6710= 103
           FORMAT( *OSYSTEM UNSTABLE - - OPEN-LOOP CGT NOT FEASIBLE *)
6720=
           RETURN
6730= 9
           LKX=1
6740=
           LKZ=1
6750=
            NSIZE=NRD*NND
5750=
            CALL ZPART(RPI(LKX),1,NSIZE,1)
            IF(ICGT.EQ.0) GO TO 12
5770= 10
5780=
            WRITE 108
           FORMAT( * MODIFY COMMAND MODEL (Y OR N) >*)
5790= 108
4800=
            READ 111, IANS
6810=
            IF(IANS.EQ.NO) RETURN
6820= 12
           CALL RSYS(SM.LD.ND.2.1CGT)
            IF (LABORT.NE.O) RETURN
6830≈
6940=
            NE WCM=1
6350=
            CALL POLES(SM, NNC, 2.2M1, ZM2)
            IF(NPC.EQ.NPD) GO TO 15
4840=
68/0=
            WRITE 104
4880=
           LABORT=-1
6890=
            RETURN
           CALL OSCRIC(LO.ZM1)
6900= 15
```

M - 6910= 102 FORMAT(* READ REG/PI GAINS FROM 'DATA' FILE (Y OR N) >*)

5920= 104 FORMAT(*OCCUMAND AND DESIGN MODEL JUTPUTS NOT EQUAL IN

6930= INUMBER*)

6940= RETURN

6950=C END SUBROUTINE SCMD

```
18250=
               SUBROUTINE FLIRK (IFLIR)
  18260=
               COMMON/MAIN1/NDIM.NDIM1,COM1(1)
               COMMON/MAIN2/COM2(1)
  18270=
  18280=
               COMMON/DESIGN/NUCOM, TSAMP, LFLRPI, LFLCGT, LFLKF, LTEVAL, LARORT
  18290=
               COMMON/FILES/KSAVE, KDATA. KPLOT, KLIST, KTERM
  19300=
               COMMON/SYSMTX/NUSH.SM(1)
  18310=
               COMMON/ZMTX1/NVZM,ZM1(1)
  18320=
               COMMON/ZHTX2/ZH2(1)
  18330=
               COMMON/NOIMD/NND, NRO, NPO, NMO, NOD, NWO, NEOD, NPLO, NEERWO, NNPR
  18340=
               COMMON/LOCD/LAP, LOP, LPHI, LBD, LEX, LPHD, LQ, LQN, LQD, LC, LDY, LEY
  18345=
              1.LHP.LR
  18350=
               COMMON/DSWMTY/NUDM, NOTIY, NOTY, DM(1)
  13360=
               COMMON/LKF/LEADSN, LFLTRK, LFCOV
  19370=
               COMMON/CKF/NUFLT.FLT(1)
  19390=
               IF(NUPNWD.GT.O) GO TO 1
  13390=
               WRITE(KTERM, 108)
  19400= 108
               FORMAT('ONO DRIVING NOISES - - FILTER DESIGN ABORT')
  18410=
               RETURN
  13420= 1
               IF(NMD.GT.0) GG TG 2
  18430=
               WRITE(KTERM.109)
               FORMAT("ONO MEASUREMENTS - - FILTER DESIGN ABORT")
  18440= 109
  18450=
               RETURN
  18460= 2
               WRITE(KLIST, 110)
  18470= 110
               FORMAT(////11x,5("# "), "FILTER DESIGN",5(" #")////)
  13480=
               NSIZE=NPLD*(1+NPLD+NMD)
  13490=
               IF(NSIZE.LE.NUFLT) GO TO 3
  18500=
               WRITE 101, NSIZE
  18510= 101
               FORMAT("OINSUFFICIENT MEMORY /CKF/, NEED: ",14)
  18520=
               LABORT=NSIZE
  18530=
               RETURN
  18540= 3
               NDIM=NPLD
  18550=
               NDIM1=NDIM+1
  18540= 5
               IF(NWB.EQ.0) GO TO 12
               IF(IFLTR.LE.O) GO TO 6
  18570=
               WRITE 105, NWD
  18580=
  18590= 105
               FORMAT( * ENTER STATE NOISE STRENGTHS: *,12)
               CALL ROUGTS (DM(LQ), NWD, 0)
  18600=
  18610= 6
               CALL DUCTOR (NUB, DM(LG), ZM1)
  18620=
               CALL MATLST(ZM1, NWD, 1, "Q", KTERM)
               CALL MATEST(DM(LQ), NWD, NWD, "Q", KLIST)
  18630= 10
  19640= 12
               TF(NWDD.EG.O) GO TO 18
  13650=
               IF(IFLTR.LE.O) GO TO 13
               WRITE 106, NWDD
  13660=
               FORMAT( * ENTER DISTURBANCE NOISE STRENGTHS: *, [2)
  19670= 106
  18680=
               CALL ROUGTS (DM(LGN), NUDD, 0)
                CALL DUCTOR(NUDD.DM(LQN).ZM1)
  18690= 13
               CALL MATLST(ZM1, NWDD, 1, "QN", KTERM)
  13700=
  18710= 15
               CALL MATEST(DM(LQN), NUDD, NUDD, 'QN', KLIST)
  18720= 18
               CALL QDSCRT(DM(LQ),DM(LQN),ZM1,ZM2)
18730=
               CALL DAS(DM(L3D), DM(LQD), TM1, ZM2)
  18740=
                IF(IFLTR.LE.O) GO TO 19
  13750=
               WRITE 107, NAB
               FORMAT( * ENTER MEASUREMENT NOISE STRENGTHS: *,12)
  13750= 107
```

```
19770=
             CALL ROWGTS (DM(LR), NMD, 0)
18780= 19
             CALL BUCTOR(NMB, BM(LR), ZM1)
             CALL MATLST(ZM1,NMD,1, "R", KTERM)
19790=
18800= 20
             CALL MATLST(DM(LR), NMD, NMD, "R", KLIST)
13810= 25.
            CALL TERMIX(DM(LHP).SM,NMU.NDIM,2)
18820=
             CALL TRANS2(NMD, NDIM, SH, ZM1)
19330=
            LFCQV=LFLTRK+NDIM*NMD
13840=
             CALL DUCTOR(NMD, DM(LR), FLT(LFCOU))
18850=
             CALL KFLTR(NDIM, NMD, FLT, ZH1, DM(LOD), FLT(LFCGV), ZM2,
18340=
            1 FLT(LFLTRK),SM)
13870=
            CALL TERMIX(SM,COM2,NDIM,NDIM.2)
15880=
             IA=1
18870=
            00 30 I=1,NPLD
            FLT(LFCOV-1+I)=SGRT(ZM2(IA))
18900=
18910= 30
             IA=TA+NDIM1
18920=
            CALL HATEST(FET(LFETRK), NDIM, NMD, 'KF', KLIST)
18730=
             CALL MATUST(FLT(LFLTRK), NOTH, NMO, *KF*, KTERM)
19940=
            IFLTR=1
18750=
            LFLKF=1
18960= 111
            FORMAT (A3)
13770±
            RETURN
18980=C END SUBROUTINE FLTRK
```

and the transfer to the territories for

```
26970=
             SUBROUTINE PROATA(ICODE,ND)
24980=
             COMMON/MAIN1/NDIM, NDIM1, COM1(1)
26990=
             COMMON/MAIN2/COM2(1)
27000=
             COMMON/INOU/KIN, KOUT, KPUNCH
27010=
             COMMON/DESIGN/NVCOM, TSAMP, LFLRPI, LFLCGT, LFLKF, LTEVAL, LABORT
27020=
             COMMON/FILES/KSAVE, KDATA, KPLOT, KLIST, KTERM
27030=
             COMMON/SYSMTX/NUSM, SN(1)
27040=
            COMMON/ZHTX1/NUZM,ZM1(1)
27050=
             COMMON/ZMTX2/ZM2(1)
27060=
             COMMON/NDIMO/NND, NRD, NPD. NMD. NWD. NWDD, NPLD, NWPNWD, NNPR
27070=
             COMMON/LOCD/LAP, LGP.LPHI, LBD, LEX, LPHD, LQ, LQN, LQD, LC, LDY, LEY
27075=
            1, LHP, LR
27080=
             COMMON/DSWMTX/NVDM.NODY.NOEY.OM(1)
27090=
             COMMON/NDIMC/NNC.NRC.NPC
             COMMON/!.OCC/LPHC+LBDC,LCC+LDC
27100=
27110=
             COMMON/CHEMTX/NUCM, NEWCM, NODO, CM(1)
27120=
             COMMON/NDIMT/NNT, NRT, NMT, NWT
27130=
             COMMON/LOCT/LPHT, LBDT, LQDT, LHT, LRT, LTDT, LTNT
             COMMON/TRUMTX/NVTM,TH(1)
27140=
27150=
             COMMON/LONTRL/LPI11,LPI12,LPI21,LPI22,LPHDL,LBDL
27150=
             COMMON/CONTROL/NUCTL,CTL(1)
27170=
             COMMON/LREGPI/LXDW, LUDW, LPHCL, LKX, LKZ
27180=
             COMMON/CREGPT/NVRPI, RPI(1)
27190=
             COMMON/LCGT/LA11,LA13,LA21,LA23,LA12,LA22,LKXA11.LKXA12,
27195=
            ILKXA13
27200=
             COMMON/CCGT/NUCGT,CGT(1)
27210=
             COMMON/LKF/LEADSN.LFL TRK.LFCOV
             COMMON/CKF/NUFLT, FLT(1)
27220=
27230=
             DIMENSION ND(1)
27240=
             DATA NO/1HN/
27250=
             WRITE 101
27250=101
             FORMAT("OREAD IN CONTROLLER GAINS? (Y OR N) >")
             READ 103, IANS
27270=
27280=103
             FORMAT(A3)
             IF (IANS.EQ.NO) GO TO 102
27290=
27300=
             CALL READFS(SM,ND,4,IERR)
            LKX=ND(3)
27310=
27320=
            LKZ=ND(4)
27330=
            LKXA1L=ND(6)
27340=
             LKXA12=ND(7)
27350=
             LKXA13=ND(8)
27360=
             NNDP=(LKZ-LKX+1)/NRD
27370=
             CALL FINTX(SM,RFT(LKX),NRD,NNDP)
27380=
             LL=LXX+NRD#NNDP
27390=
27400=
             LE=NND-NNDP
             CALL ZPART(RPI(LL), NRD, LE, NRD)
27410=
             LKZ=LL+NRD*LE
27420=
            LL=LL-UKX+1
27430=
             CALL FTHTX(SM(LL), RPI(LKZ), NRD, NPD)
             LL=ND(1)-ND(5)+1
CALL FTHTX(SM(ND(S)),CGT(LKXA11),LL,1)
ND(1)*NND
27450=
27460=102
27470=
             ND(2)=NRD
```

```
27490=
            ND(3)=NPD
27490=
            ND(4)=NMD
2/500=
            ND(5)=NDD
27510=
            ND(6)=NPLD
27520=
            ND(7)=NNC
27530=
            ND(8)=NRC
            ND(9)=NPC
27540=
27550=
            ND(10)=NNT
27530=
            ND(11)=NRT
27570=
            ND(12)=NMT
27580=
            ND(13)=NODY
27590=
            ND(14)=NOEY
27600=
            NUZHS=NUZH
27610=C
27620=
            CALL FTMTX(DM(LPHI),SM,NND,NND)
            LL=NND*NND+1
27630=
27640=
            CALL FTMTX(DH(LBD), SM(LL), NND, NRD)
            LL=NND#NRD+LL
27650=
27660=C
27670=
            IF(NDD.EQ.0) GO TO 100
27680=
                  CALL FTHTX(DM(LEX), SM(LL), NND, NDD)
27690=
                  LL=NND*NDD+LL
27/00=
                  CALL FTM(X(DM(LPHD),SM(LL),NDD,NDD)
                  ILL=NDD*NDD+ILL
27710=
27720=
                  IF(NODY.EQ.1) GO TO 90
27730=
                       CALL FIMIX (UM(LDY), SM(LL), NPD, NRD)
                       LL=NPOxNRD+LL
27740=
27750= 90
                  IF(NOEY.EQ.1) GO TO 95
                       CALL FTMTX(DM(LEY),SM(LL),NPD,NDD)
27760=
27770=
                       LL=NPII*NIIO+LL
                  CALL FTMTX(DM(LHP),SM(LL),NMD,NPLD)
27780= 95
27790=
                  ILL=NMO*NPLD+iLL
                  SD TO 200
27800=
            CONTINUE
27810= 100
27920=C
27830=
            IF(NODY.EQ.1) GQ TO 105
                 CALL FTMTX(DM(LDY), SM(LL), NPD, NRD)
27840=
27850=
                 LL=NPD*NRD+LL
27860= 105
            CALL FTMTX(DM(LHP), SM(LL), NMD, NND)
27870=
            LL=NMD*NND+LL
27880= 200
            CALL FIMIX(DM(LC).SM(LL).NPD,NND)
27890=
            LL=NPD#NND+LL
27900=
            CALL FTMTX(CM(LPHC), SM(LL), NNC, NNC)
            LL=NNC*NNC+LL
27910=
27920=
            CALL FTHTX(CM(LBDC),SM(LL),NNC,NRC)
27930=
            LL=NNC*NRC+LL
27940=
            CALL FTMTX(CM(LCC),SM(LL),NPC,NNC)
27950=
            LL=NPC*NNC+LL
27940=
            CALL FIMIX(TM(LPHT), SM(LL), NNT, NNT)
27970=
            LL=NNT*NNT+LL
27980=
            CALL FIMIX(TH(LBDT), SH(LL), NNT, NRT)
27990=
            LL=NNT*NRT+LL
            CALL FIMIX(IM(LQDT),SM(LL),NNT,NNT)
28000=
28010=
            L! =NNT*NNT+I.L
            CALL FINTX(TM(UHT).SM(LL),NMT,NNT)
23020=
28030=
            LL=NM1 #NNT+LL
```

```
CALL FINTX(TH(LRT).SH(LL),NMT.NMT)
28040=
            LL=NMT*NMT+LL
28050=
            CALL FINTX(RPI(LKX),SH(LL),NRD,NND)
28060=
            LL=NRD*NND+LL
28070=
            CALL FINTX(RPI(LKZ), SM(LL), NRD, NPD)
28080=
            LL=NRTIXNPO+LL
28090=
            CALL FTHTX(CGT(LKXA11),SH(LL),NRC,NNC)
28100=
23110=
            LL=NRC*NNC+LL
29120=C
             (F(NDD.EQ.O) GO TO 300
29130=
                  CALL FTHTX(CGT(LKXA13).SM(LL),NRD.NDB)
281.40=
                  LL=NRD*NOD+LL
28150=
                  CALL FINTX(FLT(LFLTRK),SM(LL),NPLD,NND)
28160=
                  LL=NPLD*NMU+LL
28170=
                  CALL FIMIX(TH(LIDT).SH(LL).NND.NNT)
29190=
                  LL=NND*NNT+LL
28190=
                  CALL FIMIX([M(LINT),SM(LL),NDB,NNT)
29200=
                  LL=NOU*NNT+LL
28210=
28220=
                  GO TO 310
28230= 300 CONTINUE
28240≈C
             CALL FINTX(FLT(LFLTRK), SM(LL), NND, NMD)
28250=
             LL=NNO*NMD+LL
28260=
             CALL FIMIX (TM(LTUT) . SM(LL) , NND . NNT)
28270=
             LL=NNT)*NNT+LL
28280=
28290= 310 SM(LL)=TSAMF
28300=
             ND(15)=LL
             CALL WFILED (ICODE, LL, ND, SM)
28310=
             NUZM=NUZMS
28320=
             RETURN
28330=
28340=C END SUBROUTINE PEDATA
```

```
SUBROUTINE DAS(BD.40.8DP.4P)
                                                                            027680
      COMMON/MAIN1/NDIM
                                                                            029670
      COMMON/NOIMO/NNO.ARO.NPO.NMO.NUO.NUO.NVOO.NPLO.NWFNWO.NMPR
                                                                            029700
      COMMON/FILES/KSAVE, KDATA, KPLOT, KLIST, KTERM
                                                                            029710
      DATA MO/1HM/
                                                                            129720
      WRITE 101
                                                                            029730
      FOR HAT ("9 HODIFY @ BY DOYLE AND STEINT (Y OR N)> ")
                                                                            929740
121
      READ 102. IANS
                                                                            02976C
102 FORMATCASA....
      IFCIANS.EQ.NO) RETURN
                                                                            029770
      WRITE 133
                                                                            029780
      FORMATCHSENTER GOTT
                                                                            229799
103
      READ .. QUAS
                                                                            02980
                                                                            029810
      QCAS=GBAS+GDAS
      CALL TERMIX(80,80P,NNO,NRD,2)
                                                                            029820
      IFCHMD.EG.NPLD) 60 TO 13
                                                                            027830
      L1=LAGGR(NPLD.NA 0+1,1)
                                                                            029840
                                                                            027850
10
      CALL MATZ(NPLD, NRD, 80P, 80P, 9P)
      CALL MADDI(NPLD.NPLD.QO.QP.QD.QOAS)
                                                                            027860
      CALL MATLET (QD, MPLD, MPLD, "QP", KLIST)
                                                                            029873
      RETURN
                                                                            02988C
      END
                                                                            82989Ç
```

APPENDIX D: Additional AFTI/F-16 Performance Data

D.1 Introduction

In Reference 6, it is stated that the Doyle and Stein technique for Kalman filter robustification is guaranteed to work only for a minimum-phase design model. That is, the model of the system to be controlled may not have transmission zeroes in the right-half s-plane.

The perturbation equations of motion described in Chapter V are linearized about a trim flight condition at an altitude of 10000 feet and a Mach number of 0.6. This yields a design model that is minimum phase. Initially, the trim condition was at the same altitude but with a Mach number of 0.8, to be consistent with other research done with the same model (Ref 12;27;29). At this design point, the eight-state controller model is non-minimum phase. The Doyle and Stein robustification was applied to this system with some unexpected results.

The results of a performance analysis of the eight-state continuoustime controller evaluated against a twelve-state truth model are presented in this chapter. First the performance was evaluated against a twelvestate truth model (10000 ft, M=0.6). Then, the response of the system at off-design condition is presented, with and without robustification.

D.2 Performance Evaluation of a Non-Minimum Phase Design Model

The performance of the non-minimum phase system at the design flight condition with a reduced-order design model is shown in Figure (D-1). The response of the system is stable with Θ converging to zero, and the standard deviation converging to a small finite value. The performance

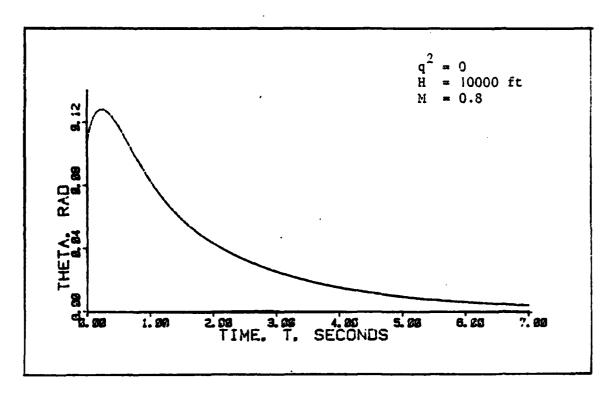


Figure D-la: Unrobustified Non-Minimum Phase Mean Response of $\boldsymbol{\Theta}$

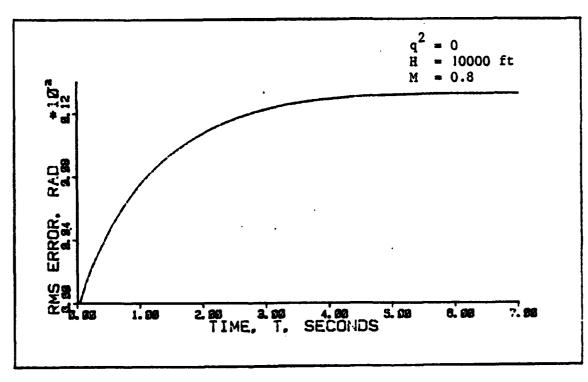


Figure D-1b: Standard Deviation of Theta for the Unrobustified Non-Minimum Phase System

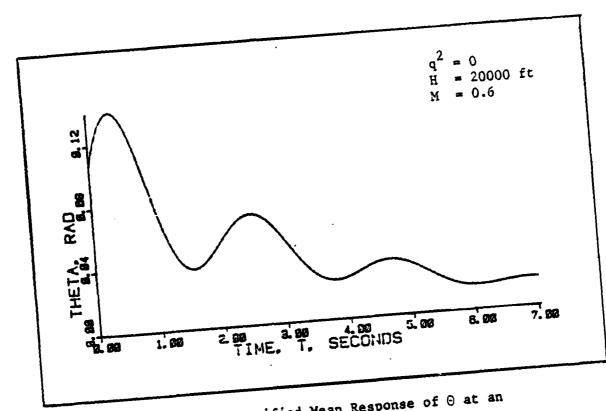


Figure D-2: Unrobustified Mean Response of ⊖ at an Off-Design Condition

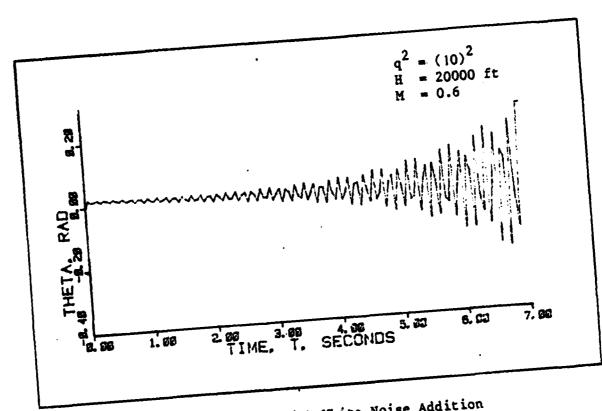


Figure D-3: Mean of Theta With White Noise Addition

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of this controller is actually better than the one described in Chapters V and VI. The transient time and steady-state error are substantially better.

Figure (D-2) shows the mean of Θ response when the flight condition is changed to an altitude of 20000 feet and a Mach number of 0.6. This response is still stable although slower and more oscillatory than the previous case. Figures (D-3) through (D-5) show the response of the same controller with progressively higher strengths of white noise added to the model at the control entry points. It is seen that the stability of the controlled system is lost with the application of the robustification technique. Examination of the eigenvalues of the closed-loop system matrix disclosed that, for any non-zero value of q, some of the eigenvalues are driven into the right-half s-plane.

If the response of the system at another off-design point (10000 feet, M=0.6) is examined (Figure D-6). It seen that the mean of Θ is diverging rapidly. However, as shown in Figure (D-7), if white noise of strength $q^2=1000$ is added to the system model, the divergence is considerably slower. Figures (D-8) and (D-9) demonstrate that adding white noise with higher strength will stabilize the pitch attitude response. The mean of Θ is actually converging to a steady-state value. Figures (D-10) through (D-12) show the same trend for the pitch rate, q.

The figures in this appendix show that the trends observed in Chapter VI do not apply if the model used for controller and Kalman filter design is non-minimum phase. A case was shown where the stability of the system at an off-design flight condition was recovered by applying

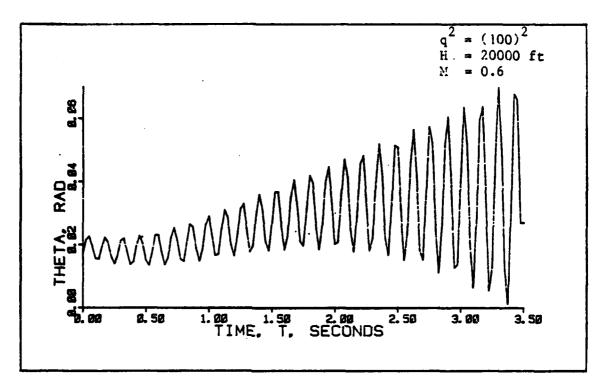


Figure D-4: Mean of Theta With White Noise Addition

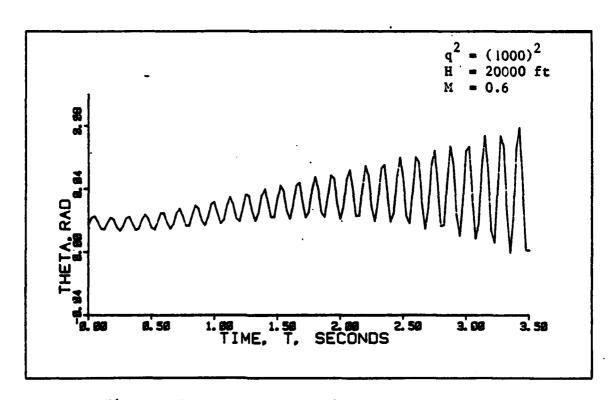


Figure D-5: Mean of Theta With White Noise Addition

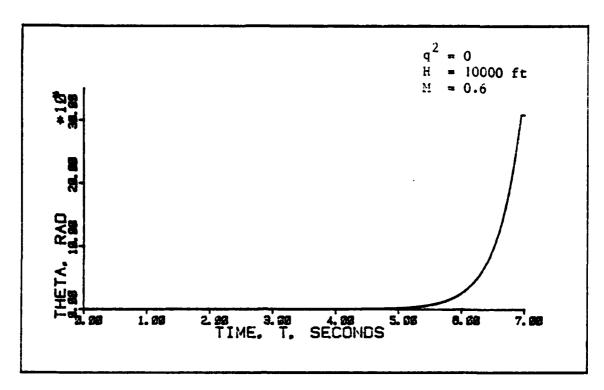


Figure D-6: Unrobustified Mean Response of Θ at an Off-Design Condition

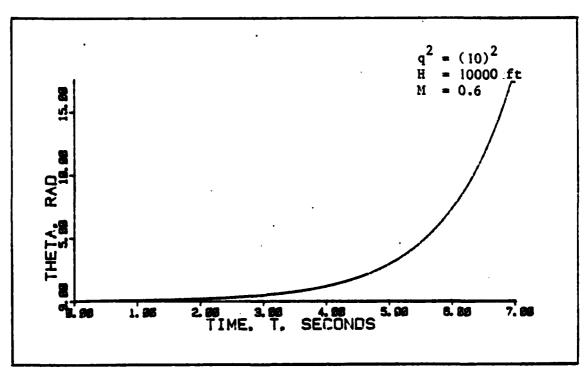


Figure D-7: Mean of Theta With White Noise Addition

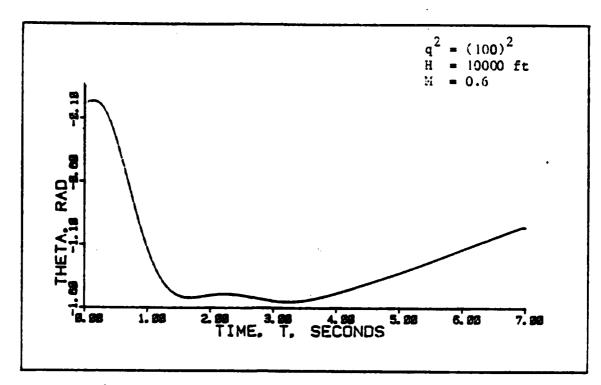


Figure D-8: Mean of Theta With White Noise Addition

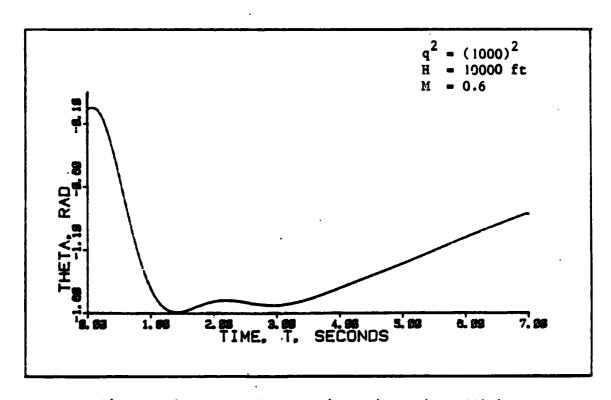


Figure D-9: Mean of Theta With White Noise Addition

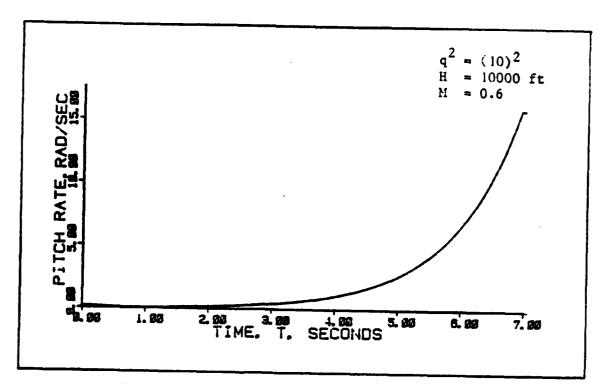
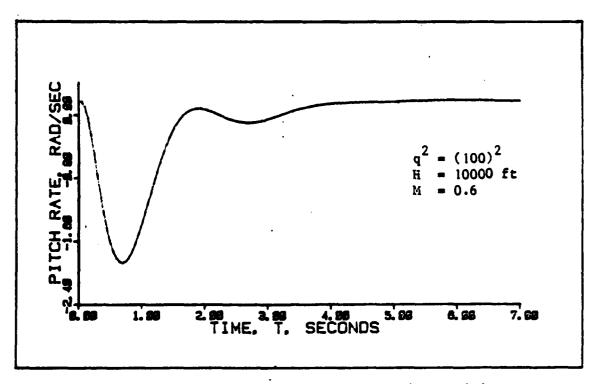


Figure D-10: Mean of q With White Noise Addition



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Figure D-11: Mean of q With White Noise Addition

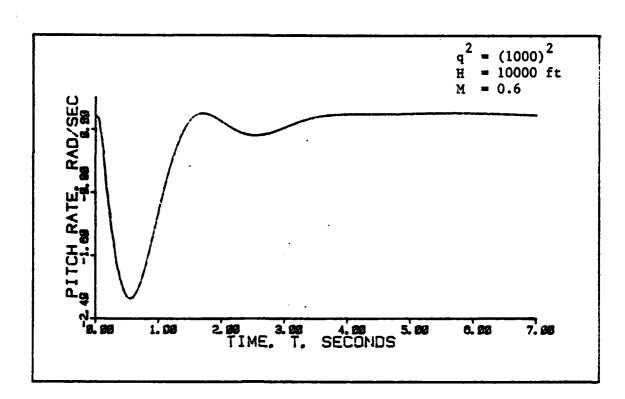


Figure D-12: Mean of q With White Noise Addition

the robustification technique. However, the noise addition destabilized the response of the system at another flight condition that was initially stable.

Reference 28 deals with the robustification technique of adding time-correlated noise to a system model at the control entry points. It states that this method is not constrained to minimum phase models as in the Doyle and Stein technique. This claim was not examined in this thesis, however, the models used would form a good basis for future research in this area.

Vita

Jean Marie Howey was born on 16 June 1960 in Kansas City, Kansas.

She graduated from high school in Meriden, Kansas in 1978. She attended the University of Kansas in Lawrence, Kansas and graduated with a Bachelor of Science in Aerospace Engineering in 1982. Upon graduation, she received a commission in the U.S. Air Force through the Reserve Officers Training Corps. She entered the School of Engineering of the Air Force Institute of Technology in June 1982 and has pursued the Stability and Control curriculum of the Aeronautical Engineering Department.

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to make a trade-off between the amount of desired robustification and the performance degradation at the design conditions which occurs when the techniques are applied.

Both methods are found to improve substantially the robustness properties of the controllers considered. For the specific flight control problem considered in this thesis, the technique of injecting white input noise into the design model produced the desired degree of robustification without prohibitively degrading performance at the design conditions.

The second method, though effective, did not yield substantial enough performance benefits over the first to warrant use in actual implementation.

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