

NAVAL POSTGRADUATE SCHOOL

Monterey, California



# **THESIS**

ADAPTIVE NOTCH FILTER
SUPPRESSION OF BENDING MCDES

· by

William L. Marks

December 1980

Thesis Advisor:

R. D. Strum

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# ADAPTIVE NOTCH FILTER SUPPRESSION OF BENDING MODES

by

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Submitted in partial fulfillment of the requirements for the degree of

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#### **ABSTRACT**

A simple, microprocessor oriented algorithm is developed to identify, track and suppress bending mode signals from a control system's rate and position feedback signals using adaptive digital notch filters. The algorithm can be used to suppress bending modes having center frequencies as close as one octave above the control system gain cross-over frequency without introduction of the excessive phase loss associated with conventional lowpass filtering techniques. A third order model of the trident missile autopilot pitch attitude control loop is contaminated with two dynamic, destabilizing bending modes and used as a concept demonstration model. The algorithm is demonstrated by stabilizing the pitch attitude loop in the presence of two bending modes with unknown gains, damping, center frequencies and rates of change of center frequencies.

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# TABLE OF SYMBOLS

θ <sub>c</sub>	Missile pitch attitude angle command in radians
θ	Missile pitch attitude angle in radians = $x_1$
ė	Missile pitch rate in radians/seconds = $x_2$
α	Angle of attack in pitch plane in radians = $x_3$
x <sub>4</sub> ,x <sub>5</sub> ,x <sub>6</sub>	5,x <sub>7</sub> Bending mode dynamic state variables
$M_{\alpha}$	Aerodynamic stability derivative (pitch plane in second <sup>-2</sup>
	$= \frac{\overline{q} S_{o}C_{n\alpha 1\alpha}}{I_{yy}}$
M <sub>5</sub>	Aerodynamic stability derivative (pitch plane) in second-2
	$=\frac{T1}{I_{yy}}$
$z_{\alpha}$	Aerodynamic force stability derivative (pitch) coefficient in ft/sec <sup>2</sup> /RAD
	$= \frac{\overline{q} S_0 C_{n\alpha}}{M}$
Zδ	Pitch force rigid body coefficient forcing from thrust in $ft/sec^2/RAD$
	$=\frac{T}{M}$
$\overline{q}$	Aerodynamic Pressure in 1b/ft <sup>2</sup>
s <sub>o</sub>	Missile aerodynamic reference area in ft <sup>2</sup>
$c_{n\alpha}$	Aerodynamic normal coefficient (pitch plane) in radian-1
1 <sub>a</sub>	Distance from vehicle C.G. to guidance accelerometer in ft,
Iyy	Vehicle pitch moment of inertia in slug-ft <sup>2</sup>
r	Vehicle axial thrust in 1b.

1 <sub>D</sub>	Distance from nozzle pivot point to vehicle C.G, in ft.
M	Vehicle mass in slug
κ <sub>θ</sub>	Pitch autopilot attitude gain
K <sub>rθ</sub>	Pitch autopilot rate gain
V	Vehicle velocity in ft/second
2	Damping ratio
ω, W	Undamped natural frequency in radians
rg	Rate gyro gain volts/rad/sec
<sup>⊕</sup> GA	Attitude gyro gain volts/rad
$G_{L}$	Low frequency bending mode gain
G <sub>h</sub>	High frequency bending mode gain
BL	Low frequency bending mode bandwidth in radians/sec
B <sub>h</sub>	High frequency bending mode bandwidth in radians/sec
<i>3</i> ?	Digital frequency, radians

## I. INTRODUCTION

The purpose of this thesis is to develop a simple, micro-processor-oriented scheme that eliminates body bending mode signals in a missile control system by adaptive digital notch filtering of the bending mode resonant frequencies from the rate and attitude gyro feedback signals. Although this thesis uses the Trident Fleet Ballistic Missile as a conceptual demonstration model, the process is applicable to many control systems having unknown and/or time varying mechanical resonances.

#### A. THE BODY BENDING PROBLEM

Body bending is a composite term which encompasses the coupling of all structure-borne vibrations from various sources into the missile control system through the mechanical sensors such as rate gyros and accelerometers. The effect of the body bending mode signals in the rate and attitude gyro feedback signals is destabilizing since if left unattenuated, the missile control system tries to compensate for the sensed body bending rate through the thrust vector control (TVC) system thus further exciting the bending mode and the inertial or rigid body rates soon become insignificant and go uncorrected.

Some of the sources of body bending are:

The missile acting as a cantilevered beam.

- Hydraulic servo resonance.
- 3. Structural bending at the attachment points for hydraulic actuators.
- 4. Beam-like resonance of sub-assemblies such as upper stage motors and payload.

The body bending problem in missiles is traditionally approached in one of three ways:

- at nulls in the lower frequency bending modes and the natural bandwidth of the control system and lowpass filters are used to attenuate the higher frequency bending modes. Reference [1] contains a detailed description of the analysis and testing required to implement this approach in the control system of the XSM-65 missile. The popular name, if any, of the XSM-65 missile is unknown.
- 2. The mechanical sensors are physically located at a position in the missile where the deflections due to the lower frequency body bending modes are in phase with each other. Phase shifting networks are used to ensure that the bending mode signals are fed back in such a manner that the bending modes are attenuated. Lowpass filters are still used to attenuate the higher frequency bending modes.

  Reference [2] contains a general description of how this method is implemented in the control system for the Saturn Missile.

3. Lowpass or bandstop filters are used in the feedback control loops to attenuate the body bending mode frequencies from the rate and attitude gyro feedback signals.

A general description of how this method is used in the Trident Missile Control System is contained in Ref. [3].

In the Trident Missile the above three approaches have many undesirable features. Location of the sensors at nulls or where the body bending modes are in phase requires a very precise knowledge of the bending mode characteristics and the freedom in the initial design to locate the sensors at the anticipated optimum locations. In a solid fuel missile such as the Trident, the location of the sensors is predetermined to be located with the other flight control electronics with very little latitude to select a null or position where the bending modes are in phase. The second major limitation is the lack of precise knowledge of the bending mode characteristics. The bending mode resonant frequencies, gains, damping and phase are a function of many factors including time into the flight, attitude, payload configuration, skin temperature, and thrust level. For example, the Trident Missile is designed to compensate for as much as a twenty-five percent variation in thrust level due to slight variations in the solid propellant mixture and casting while only a three percent thrust variation is acceptable on the liquid fueled Saturn Missile [2]. a precise knowledge of the parameters controlling the bending mode resonant frequencies, gains, damping and phase, the lowpass and bandstop filters must be designed on a worst case basis and as a result reduce the control system bandwidth and phase margins much more than if a narrow notch filter had been used at each specific bending mode frequency to remove the bending mode component from the rate and position gyro output signals.

As the Trident Missile evolves into the next generation, the anticipated bending mode frequencies will become much lower and approach the natural frequencies of the flight control system. The use of conventional lowpass filters under these conditions would produce so much phase loss that the missile would become unstable.

### B. THE PROPOSED SOLUTION

The proposed solution to the bending mode problem is an extension of preliminary work done by Lockheed Missiles and Space Company [3].

If the bending mode resonant frequencies can be determined in near real time during the flight and tracked as their controlling parameters change, then adaptive notch digital filters in the rate and position gyro signal feedback paths can be implemented to attenuate a selected number of bending mode signals that are contaminating the desired rigid body rate and attitude signals.

The difficulty in the implementation of such a solution lies in the in-flight determination of the bending mode frequencies rapidly and with sufficient accuracy. The rapid determination of the bending mode frequencies is essential in order to place the notch filter at the proper bending mode frequency before the bending mode signals can degrade the missile attitude and rates to a point from which it cannot recover within the allowable flight trajectory envelope. The allowable time for the initial determination of the bending mode frequencies is a function of the initial frequency and bandwidth of the individual notch filters. In general the time available to eliminate the effects of the bending modes before the Trident Missile deviates from an acceptable flight trajectory is one-half second. requirement for accuracy is essential to allow the minimum bandwidth notch filters to be used. As successive notch filters are added to the control system to attenuate the bending mode signals, an increasing amount of phase loss will be experienced at the frequencies used by the control system resulting in a decrease in the already minimal phase margin for overall missile stability. If very narrow notch filters are used to minimize the phase loss at the control system frequencies, then the center frequency of the notch must be placed much more accurately to be effective.

Four methods were investigated as to their potential to be used for inflight bending mode frequency identification and tracking:

- 1. Reference [3] summarizes the use of Fourier integral filters to measure the power spectral density at integer frequencies. Second order curve fitting techniques were then used to estimate the bending mode frequencies from the output of the filters. The major drawback of this technique is that it required at least one-half second of integration time for each repeated frequency determination. Reference [3] did not address the ability of this technique to accurately track a dynamic bending mode, although the data indicated that a bending mode that was changing as little as 0.2 hertz per second would cause sufficient distortion of the frequency determination as to render the technique ineffective.
- 2. The author conducted a feasibility study of using a Fast Fourier Transform (FFT) algorithm to determine the spectrum of the rate gyro output signal in order to determine the bending mode frequencies. The method was disregarded for two reasons. The rate gyro signal would have to be sampled for ten seconds to obtain a minimum frequency resolution of 0.1 hertz and, the computational capability required to execute the FFT algorithm was felt to be excessive.

- 3. The feasibility of using a phaselock loop to lock-on and track a bending mode frequency was investigated by the author. Simulation of a phaselock loop with an eighthertz center frequency and a three-hertz acquisition range revealed that while the tracking characteristics of the phaselock loop were very good, the ability to achieve lock with a random phase signal at the extremes of its acquisition range was unreliable if the signal was contaminated with frequency components from the plant and a second bending mode at anticiapted signal levels. The technique was not pursued further but with the addition of prefilters on the phaselock loop input this technique has the potential to be more effective than the technique used in this thesis. Considerable refinement in the simulation of the phaselock loop nonlinearities would be required.
- 4. The technique used in this thesis to identify and track the bending mode frequencies uses a microprocessor to compute the frequency of each bending mode by use of digital bandpass filters and linear estimation of the zero crossing times. The use of discrete signal processing by the microprocessor will not require additional sampling circuitry since the missile attitude and rate gyro signals are currently sampled and put in digital form in the Trident Missile for use in the digital autopilot. As shown in Figure 1-1, the microprocessor uses the sampled rate gyro data by passing it through a set of parallel digital

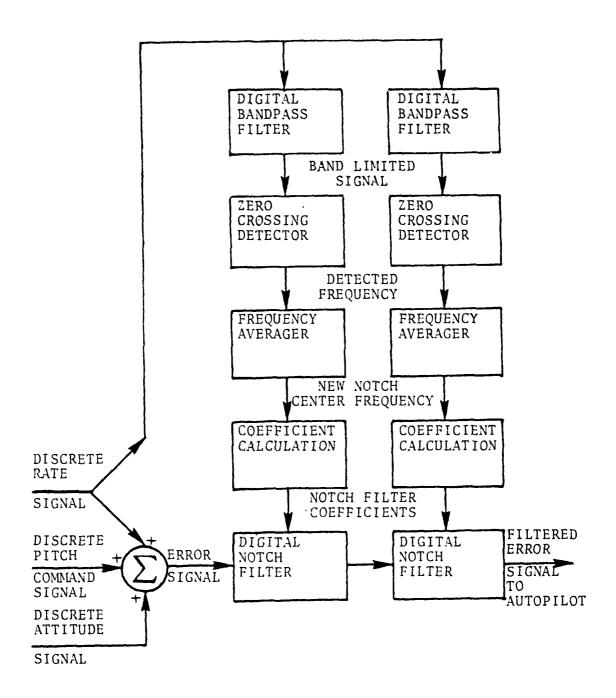


Figure 1-1 Microprocessor Algorithm Modules

bandpass filters in order to decompose the signal into frequency bands that are only wide enough to contain one bending mode frequency. The output of each of the bandpass digital filters is examined after each sample to see if the amplitude of the signal in that band has changed signs. If the amplitude has changed signs then the time of the zero crossing is linearly estimated based on the amplitude of the signal before and after the zero crossing and the sampling period. The half period detected is converted to a frequency and averaged with the frequency that the digital notch filter devoted to that band is currently tracking. The average of the current and computed frequency is then used to compute new coefficients such that the digital notch filter will be centered at the new average frequency. details of the algorithm and design are discussed in Chapter Three and the concept is demonstrated by simulation in Chapter Four.

### II. MODEL DEVELOPMENT

In order to verify the ability of the tracking notch filter concept to stabilize the missile in the presence of bending mode feedback, a model of the system was developed to be used as the basis for simulation.

#### A. THE MODEL OF THE PLANT

Figure 2-1 is a block diagram representation of the reduced order pitch plane attitude control loop of the Trident I Missile autopilot. The model was provided by Lockheed Missile and Space Company by reference [3], and was modified only to the extent that the signs at the summers for  $x_1$  and  $x_3$  were changed to allow all the model coefficients to be considered positive quantities. Table 2-1 shows the time varying values for the parameters used in this model. The model shown in Figure 2-1 represents the rigid body dynamics of the missile and is referred to as the plant. When bending modes are added to the rigid body model the resulting composite model is referred to as the system.

The state space representation of the plant for any time is:

$$x_1 = x_2$$

$$\dot{x}_2 = -K_\theta M_\delta X_1 - K_{r\theta} K_\theta M_\delta X_2 - M_\alpha X_3 - K_\theta M_\delta \Theta_c$$

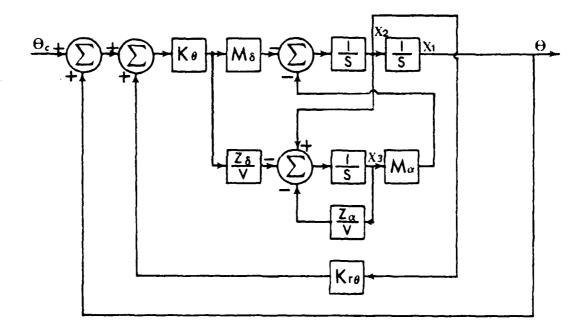


Figure 2-1 Pitch Plane Attitude Control Loop (Plant)

PARAMETER	T=25 SEC.	T=40 SEC.	T=50 SEC.
Ma	18.625	28.625	17.5
M <sub>S</sub>	22.51	24.17	32.0
Za	88.87	180.0	140.0
$z_{s}$	119.19	113.75	137.5
V	1750	2500	3400
Ψrg	0.06	0.06	0.06
$^{\psi}$ GA	0.06	0.06	0.06
К	1.5	1.48	0.946
K <sub>r9</sub>	0.2	0.2	0.2

NOTE: The units of each parameter are listed on the list of symbols. The signs of the parameters are all positive to be consistent with the structure of the model used.

$$\dot{x}_{3} = -K_{\theta} \frac{z}{v} x_{1} + (1 - K_{r\theta} K_{\theta} \frac{z}{v}) x_{2} - \frac{z}{v} \alpha^{x}_{3} - K_{\theta} \frac{z}{v} \delta^{\Theta} c$$

where:

 $\mathbf{x}_1$  is the missile pitch angle.

 $\mathbf{x}_{2}$  is the missile pitch angle rate.

 $x_3$  is the angle of attack.

Using matrix notation the plant is then described by:

$$\dot{x} = AX + B\Theta_{C}$$

$$\Theta = CX$$

where

$$\underbrace{A} = \begin{bmatrix}
0 & 1 & 0 \\
-K_{\theta}M_{\delta} & -K_{r\theta}K_{\theta}M_{\delta} & -M_{\alpha} \\
-K_{\theta}Z_{\delta} & (1-K_{r\theta}K_{\theta}Z_{\delta}) & -Z_{\alpha} \\
V & V
\end{bmatrix}$$

$$\underline{B} = \begin{bmatrix} 0 & -K_{\theta}M_{\delta} & K_{\theta}\underline{Z}_{\delta} \end{bmatrix}^{T}$$

$$C = [1 \ 0 \ 0]$$

The transfer function relating the missile pitch angle  $\theta$  to the commanded pitch angle  $\theta_{\rm C}$  is:

$$\frac{\theta(s)}{\theta(s)} = H(s)$$

$$H(s) = \frac{-K_{\theta} [M_{\delta} s + (M_{\delta} \frac{Z}{\alpha} - M_{\alpha} \frac{Z}{\delta})]}{s^{3} + (\frac{Z_{\alpha} + K_{\theta} K_{r\theta} M_{\delta}) s^{2} + [M_{\alpha} + K_{r\theta} K_{\theta} (M_{\delta} \frac{Z}{\alpha} - M_{\alpha} \frac{Z}{\delta}) + K_{\theta} M_{\delta}] s + K_{\theta} (M_{\delta} \frac{Z}{\alpha} - M_{\alpha} \frac{Z}{\delta})}{V}}$$
(1)

The transfer function can be factored with a root finder and used to plot the poles and zeros of the transfer function in order to provide an intuitive feeling as to the response of the system not otherwise apparent with the state-space representation. The state-space representation of the system is used primarily in the simulation programs to obtain the time-domain solution to the differential equations of motion.

#### B. THE CHARACTERISTICS OF THE PLANT

The model of the plant given in Figure 2-1 is a model of the rigid body dynamics including two Newtonian integrators and the positive feedback of the angle of attack,  $\mathbf{x}_3$ . The

output pitch angle  $\theta$  is opposite in sign to the commanded pitch  $\theta_{\rm C}$ . This reversal is compensated for in the outer guidance loop not included in this model. The sign of the forward gains  $M_{\delta}$  and  $Z_{\delta}$  are normally specified as negative quantities which results in a net negative feedback. For computational convenience the gains are treated as positive quantities and the signs at the summers have been changed. The sign of the rate and position feedback summers remains positive to clearly indicate the nature of the positive feedback of the bending modes from the pitch rate and pitch angle gyros.

The model of the plant was designed to simulate the transient behavior of the system and not the steady state behavior. As a result the simulation studies are only valid for about two seconds of transient behavior.

To establish a baseline or nominal performance the plant was simulated for a ramp and a step input with system parameter values fixed at the time = 40 second values. The reasoning behind the selection of inputs and parameter values is discussed in Chapter Four.

Selecting the appropriate values for the system parameters from Table 2-1 for time = 40 seconds, the transfer function, given by equation (1) becomes:

$$H(s) = \frac{-35.77(\pm +0.01779)}{(\pm +0.0098)(\pm +3.608 +/-J 7.17)}$$
(2)

The poles and zeros of the transfer function are plotted in Figure 2-2.

An examination of the poles and zeros of the transfer function indicates the system is stable with a pair of complex poles having a natural frequency  $\omega_n$  = 8.02 RAD/SEC and a coefficient of damping  $\xi$  = 0.449. There is also a very slow pole at s = -0.0098 and a zero at s = -0.01779.

To establish the baseline or nominal performance of the plant without bending modes, the plant was simulated using the IBM DSL/360 language. The values of the plant parameters from Table 2-1 for time = 40 seconds are used throughout this thesis. A detailed discussion of the simulation programs and the selection of the plant parameter values is contained in Chapter Four. Figure 2-3 illustrates the plant response to a step input pitch command of 0.1 radians.

Figure 2-4 illustrates the response of the plant to a ramp input of 0.05 radians/sec.

Note: It will be the convention in this thesis when presenting computer generated output in the form of a figure to include the computer program that was used to generate that figure in the computer program appendix properly labelled to indicate the figure number. If reference is made to the program it will be referred to as program (figure number).

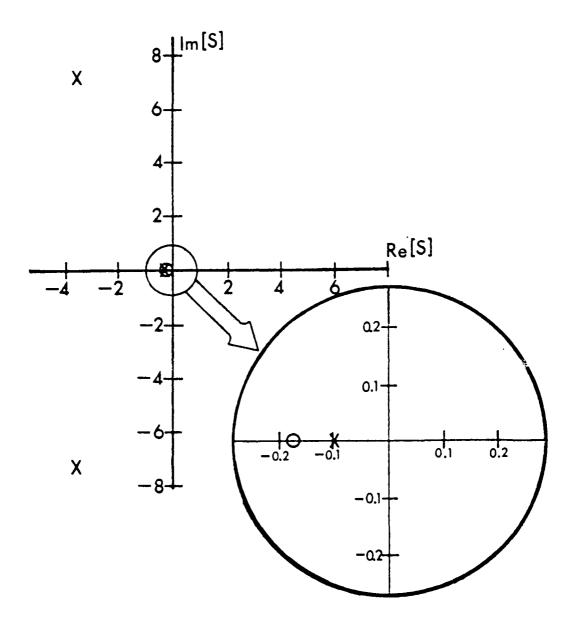
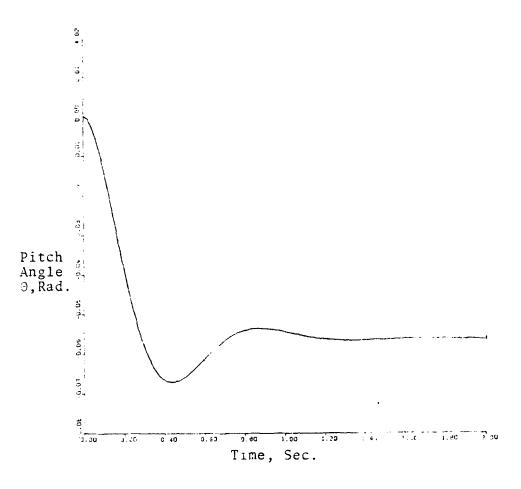


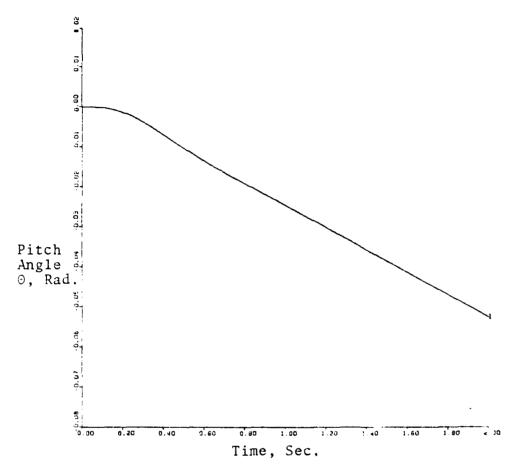
Figure 2-2 Locations of the Poles and Zeros of the Plant



Third order missile model without bending modes System:

Input: 0.1 Radian step pitch command

Figure 2-3 Missile response for a step command



System: Third order missile model without bending modes

Input: 0.05t radian/sec ramp pitch command

Figure 2-4 Missile response for a ramp command

Although all simulations in this thesis are performed using the third-order model of the plant, it is possible to reduce the model to a second-order model without introducing significant error. The second-order model provides a convenient preliminary design model since the characteristics of second-order systems are well established. The second-order model is derived by analysis of the time domain response of the third-order system and eliminating the effects of the slow pole and zero. The validity of the second-order model is established by comparison with the third-order model simulation results.

To obtain the time domain response to a 0.1 radian step input the transfer function of equation (2) will be multiplied by 0.1/s and the resulting function expanded in a partial fraction expansion.

$$\theta(s) = \frac{0.1}{s} H(s) = \frac{-3.577(s+0.01779)}{s(s+0.0098)(s+3.608+/-J 7.17)}$$

which yields:

$$\begin{array}{rcl} & -0.0098t & -3.608t \\ \theta(t) = -0.1 + 0.0453 & e & + 0.06218e & COS(7.17t - 0.453) \\ & \text{at t} = 2.0 & \text{sec.} \\ \\ \theta(2) = -0.1 & + 0.0453(0.98) & + 0.06218(0.00072)COS(14.34 - 0.453) \\ & = -0.552 \end{array}$$

Examining the time domain response one finds that the influence of the slow pole is so slow that one may consider the response of the system due to that pole to be essentially a constant for the two second duration of the simulation with less than two percent error. Treating the term due to the slow pose as a constant reduces the time-domain solution to:

$$-3.608t$$

$$\theta(t) = -0.0547 + 0.06218e \qquad COS(7.17t - 0.453) \qquad (3)$$

The system now can be considered as second-order and the response can be very closely approximated from tabulations of the characteristics of second order systems [4].

The transform of equation (3) is

$$L[\theta(t)] = \theta(s) = \frac{-0.0547}{s} + \frac{(0.05589)(s+7.098)}{s^2 + 7.226s + 64.4265}$$

Placing all terms over a common denominator:

$$\theta(s) = \frac{-0.0547 \text{ s}^2 - 0.3952 \text{ s} - 3.524 + 0.05589 \text{ s}^2 + 0.3967 \text{ s}}{\text{s} (\text{s}^2 + 7.226 \text{ s} + 64.4265)}$$

Cancelling the essentially equal  $s^2$  and s terms in the numerator and factoring out the transform of the 0.1 radian step input (0.1/s) yields the following reduced order transfer function relating the missile pitch angle 9 to the commanded pitch angle  $\theta_c$ .

$$\frac{\theta(s)}{\theta_c(s)} = H_r(s) = \frac{-35.24}{s^2 + 7.226 s + 64.4265}$$
 (3a)

The steady state gain of the system is:

$$LIM = \frac{s H_r(s)}{s \rightarrow 0} = -0.547$$

The peak overshoot will be:

$$M_{\text{Pt}} = 1 + e^{-\frac{\pi \zeta}{\sqrt{1 - \zeta^2}}} = 1.21$$

The time of peak overshoot will be

$$t_p = \frac{\pi}{W_n \sqrt{1 - \zeta^2}} = 0.438 \text{ sec}$$

Using the approximation for the settling time

$$t_s = \frac{4.0}{\zeta W_p} = 1.11 \text{ sec}$$

The second secon

The validity of the second-order model for a ramp input is established by comparison of the value of the missile pitch angle determined analytically from the second-order transfer function at time = 2 seconds with the value resulting from the simulation of the third-order plant.

Given a transfer function in the form:

$$G(s) = \frac{B_0 + B_1 s + B_2 s^2 + \dots + B_m s^m}{A_0 + A_1 s + A_2 s^2 + \dots + A_n s^n}$$

The steady state time domain response of the output to a ramp input, u(t) = at, can be determined from the following formula [5]:

$$y_s(t) = \frac{B_0}{A_0} at + \frac{(A_0B_1 - B_0A_1)}{A_0^2}$$

Using the second-order transfer function determined in equation (3a) one finds that the output at time=2 for a ramp input, u(t) = 0.05t is:

$$\theta_{S}(t) = \frac{-35.24(0.05)t}{64.4265} + \frac{0.05(35.24)(7.226)}{(64.4265)^{2}} = -0.05242$$

Table 2-2 summarizes the results obtained from the secondorder model with those resulting from simulation of the thirdorder model. Again, it must be noted that the simulation
studies contained in this thesis were performed using the
third-order model of the plant. The second-order model was
derived only as a convenient preliminary design tool for any
subsequent studies.

TABLE 2-2
COMPARISON OF THIRD-ORDER AND SECOND-ORDER MODEL RESPONSES

CHARACTERISTIC	SECOND- ORDER MODEL	THIRD- ORDER SIMULATION
MAXIMUM OVERSHOOT	1.21	1.21
TIME AT MAX. OVERSHOOT	0.44 SEC	0.44 SEC
STEADY STATE GAIN	-0.5625	-0.547
SETTLING TIME (2%)	1.11 SEC	1.11 SEC
RAMP OUTPUT AT T=2 SEC	-0.0524	-0.0526

#### C. THE MODEL OF THE BENDING MODES

Reference [3] provided the model of the plant with one bending mode shown in Figure 2-5. The bending mode attitude signal  $\mathbf{x}_4$  and bending mode rate signal  $\mathbf{x}_5$  are added to the rigid body attitude signal  $\mathbf{x}_1$  and rigid body rate signal  $\mathbf{x}_2$  respectively. The composite attitude and rate signals are each fed back to the system input in a positive sense and the overall system becomes highly unstable.

Reference [2] states that the bending mode contamination of the rigid body rate signal has a much greater destabilizing effect than does the bending mode contamination of the rigid body attitude signal. The bending mode model is therefore based on modeling the bending mode rate and the bending mode attitude signal is formed by integrating the rate signal.

Reference [6] contains the bending mode frequency response for a Poseidon Missile when the bending modes were excited by slewing the first stage TVC nozzles. Although the data was measured on the Poseidon Missile with various flight configurations, the results are consistent with the general distribution of bending modes shown in Figure 3.3-1 of Ref. [2]. The distribution of the bending modes indicates that the bandwidth of the bending modes increases as the center frequency of the bending mode increases. The distribution of the bending mode increases. The distribution of the bending modes used in this thesis is shown in Figure 2-6. The low frequency bending mode may be centered anywhere in a band from 5 to 8 hertz and the high frequency

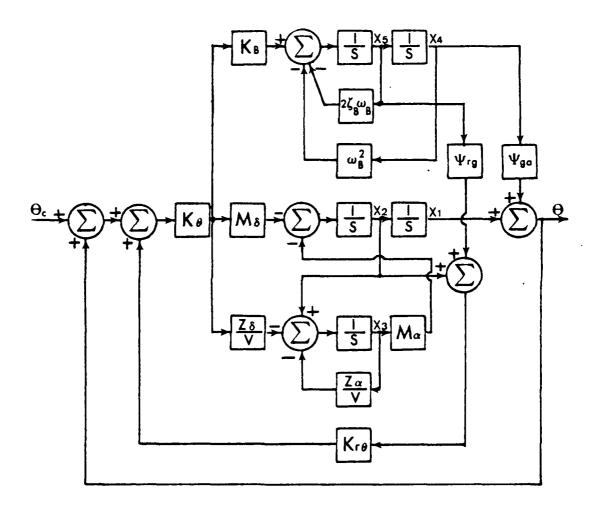


Figure 2-5 Model of the Plant with One Bending Mode

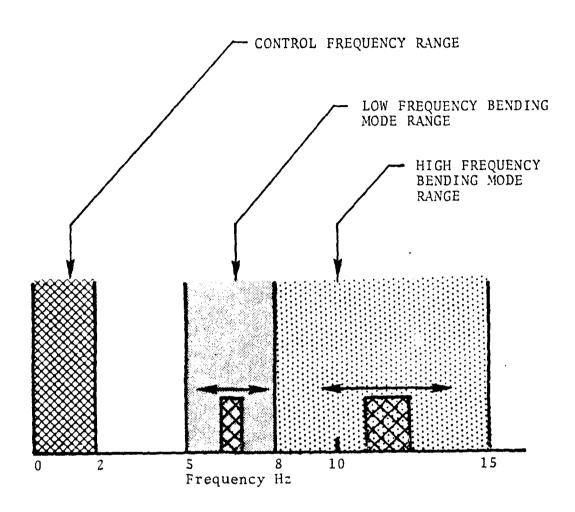


Figure 2-6 Dynamic Bending Mode Distribution

bending mode may be centered anywhere in the band from 8 to 15 hertz. The high frequency bending mode has approximately twice the bandwidth of the low frequency bending mode. The simulation studies contained in Chapter Four demonstrate the ability of the adaptive notch filtering scheme to identify, track and filter bending modes that have time varying gains, bandwidths and center frequencies.

The bending mode rates were modeled as the outputs of bandpass filters with a very high Q. The transfer function relating the output Y(s) to the input U(s) for a general second-order bandpass filter is:

$$G(s) = \frac{Bs}{s^2 + Bs + W_c^2}$$

where:

 $W_c$  = the center frequency of the filter

B = the 3 dB bandwidth of the filter

The block diagram of G(s) is shown in Figure 2-7. Y(s) represents the bending mode rate output and since the bending mode attitude output is the integral of the bending mode rate, an output of the bending mode attitude is also available from the rate model as indicated in Figure 2-8 where  $Y_1(s)$  is the bending mode rate output and  $Y_2(s)$  is the bending mode attitude output.

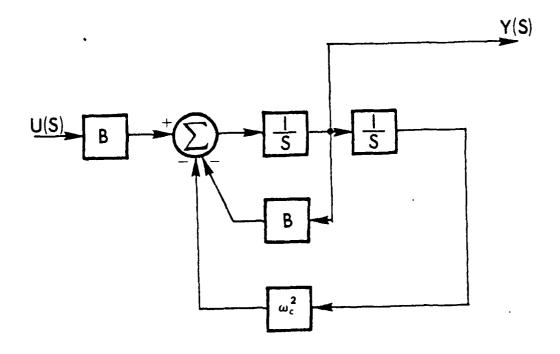


Figure 2-7 Bending Mode Rate Model

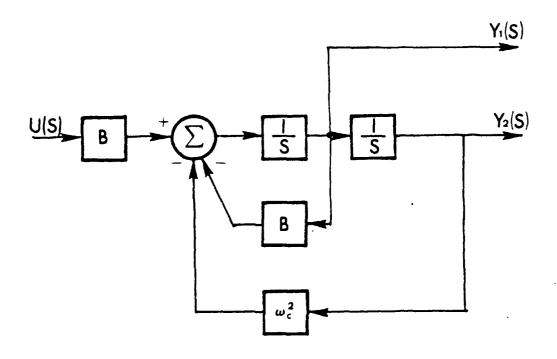


Figure 2-8 Bending Mode Rate and Attitude Model

Inspection of Figure 2-8 reveals that modeling the bending mode rate as a bandpass filter is equivalent to the bending mode model shown in Figure 2-5.

Figure 2-9 shows the system model consisting of the plant and two bending modes that are used for the simulation studies in this thesis.

## D. CHARACTERISTICS OF THE PLANT WITH TWO BENDING MODES

Preliminary values for the bending mode parameters of gain, center frequency and bandwidth were selected for the purposes of analysis and to develop some insight as to the elements controlling the behavior of the system. The bending mode parameters are varied during the simulation studies presented in Chapter Four but the detailed analysis is not repeated for each parameter study.

The bending mode parameters selected for analysis of the system are:

 $G_{h} = 20.0$ 

 $B_h = 1.10 \text{ RAD/SEC}$ 

 $W_h = 62.83 \text{ RAD/SEC} (10 \text{ Hz center frequency})$ 

 $G_1 = 240.0$ 

 $B_1 = 0.1 \text{ RAD/SEC}$ 

W, = 37.7 RAD/SEC (6 Hz center frequency)

The frequency response of the transfer function relating the missile pitch angle  $\theta(s)$  to the input pitch command  $\theta_c(s)$  with the rate and attitude feedback loops open was determined

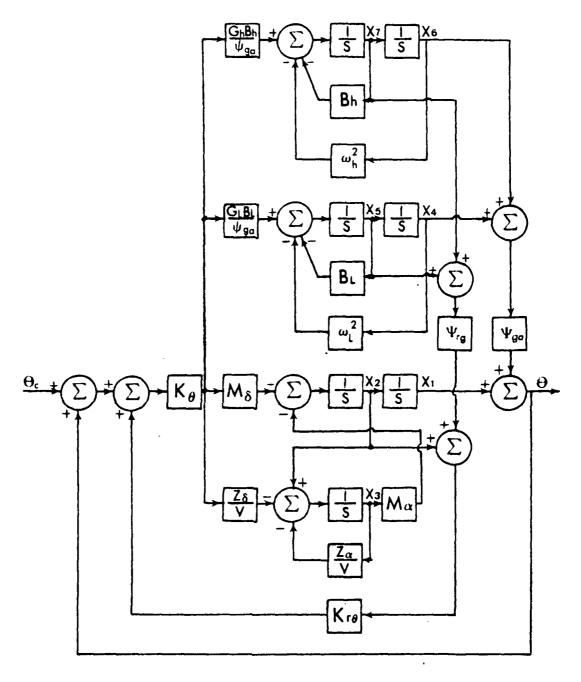


Figure 2-9 Model of Plant with Two Bending Modes

for various configurations of the plant and bending modes shown in Figure 2-9. The plant parameters from Table 2-1 for time = 40 seconds were used.

Figure 2-10 shows the open loop frequency response of the plant with no bending modes.

Figure 2-11 shows the open loop frequency response of the 6.0 Hz bending mode alone.

Figure 2-12 shows the open loop frequency response of the plant and the 6.0 Hz bending mode.

Figure 2-13 shows the open loop frequency response of the 10.0 Hz bending mode alone.

Figure 2-14 shows the open loop frequency response of the plant and the 10.0 Hz bending mode.

Figure 2-15 shows the open loop frequency response of the plant with both the 6.0 Hz and the 10.0 Hz bending modes.

The matrix representation of the state equations derived from the closed loop system shown in Figure 2-9 is:

$$x = Ax + B\theta_{C}$$

$$\theta = Cx$$

where:

 $\mathbf{x}_1$  is the rigid body pitch angle of the missile

 $x_2$  is the rigid body pitch rate of the missile

 $x_z$  is the missile angle of attack

 $\mathbf{x}_4$  is the pitch angle resulting from the lower frequency bending mode

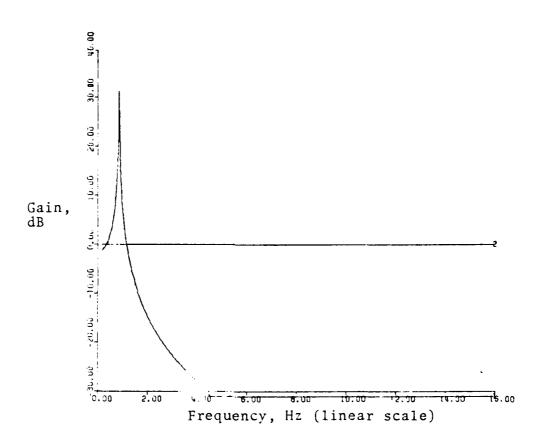


Figure 2-10 Open Loop Frequency Response of the Plant

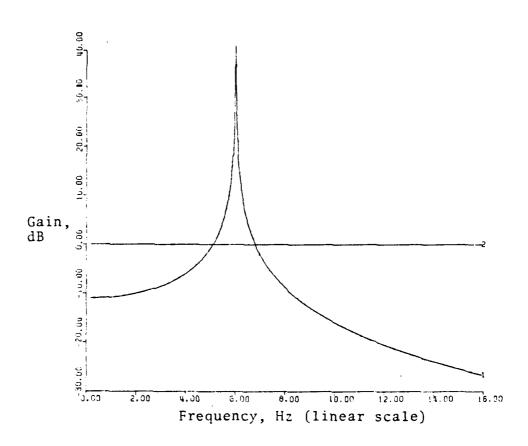


Figure 2-11 Open Loop Frequency Response Of Low Frequency Bending Mode

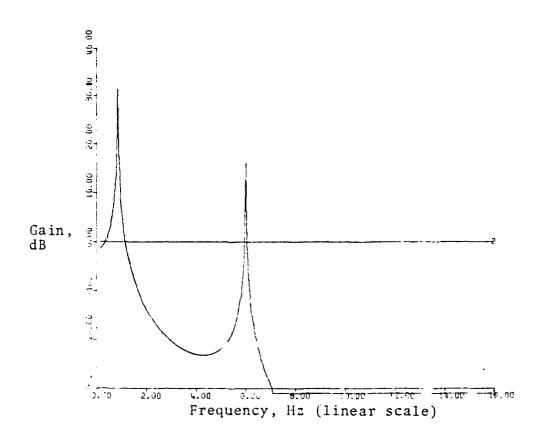


Figure 2-12 Open Loop Frequency Response of the Plant and Low Frequency Bending Mode

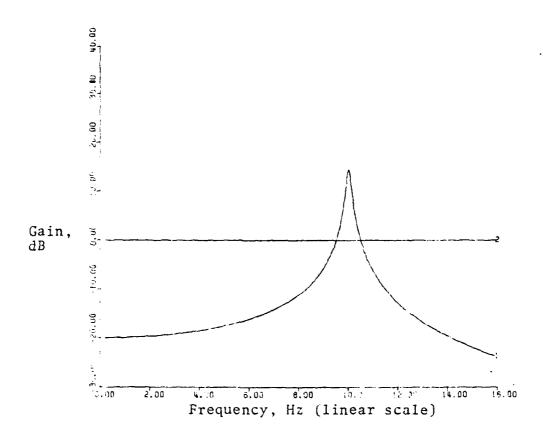


Figure 2-13 Open Loop Frequency Response of the High Frequency Bending Mode

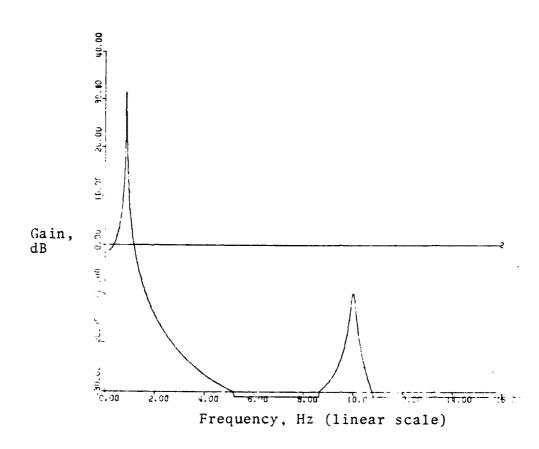


Figure 2-14 Open Loop Frequency Response of the Plant and High Frequency Bending Mode

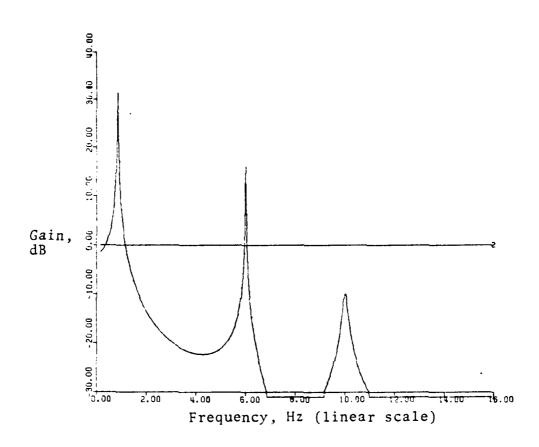


Figure 2-15 Open Loop Frequency Response of Plant with two Bending Modes

- $\boldsymbol{x}_{5}$  is the pitch rate resulting from the lower frequency bending mode
- $\mathbf{x}_{6}$  is the pitch angle resulting from the higher frequency bending mode
- $\mathbf{x}_7$  is the pitch rate resulting from the higher frequency bending mode
- $\boldsymbol{\theta}_{_{\boldsymbol{C}}}$  is the commanded pitch angle
- 6 is the missile pitch angle

## The A matrix is:

The B matrix is:

[B1 B2 B3 B4 B5 B6 B7]<sup>T</sup>

The C matrix is:

[C1 C2 C3 C4 C5 C6 C7]

where:

A73 = 0.0

C3 = 0.0

$$A74 = G_{H}B_{H}K_{\theta}$$

$$A75 = G_{H}B_{H}K_{r\theta}K_{\theta}\frac{\psi_{rg}}{\psi_{GA}}$$

$$B5 = G_{L}B_{L}\frac{K_{\theta}}{\psi_{GA}}$$

$$C5 = 0.0$$

$$A76 = G_{H}B_{H}K_{\theta}-W_{H}^{2}$$

$$B6 = 0.0$$

$$C6 = \psi_{GA}$$

$$A77 = G_{H}B_{H}K_{r\theta}K_{\theta}\frac{\psi_{rG}}{\psi_{GA}}-B_{H}$$

$$B7 = G_{H}B_{H}\frac{K_{\theta}}{\psi_{GA}}$$

$$C7 = 0.0$$

The closed loop transfer function  $H(\tilde{s})$  relating the missile pitch angle  $\theta$  to the commanded pitch angle  $\theta_c$  is:

$$H(S) = \frac{N_5 \dot{s}^5 + N_4 s^4 + N_3 s^3 + N_2 \dot{s}^2 + N_1 s + N_0}{s^7 + D_6 s^6 + D_5 s^5 + D_4 s^4 + D_3 s^3 + D_2 s^2 + D_1 s + D_0}$$

where:

$$\begin{split} N_{5} &= -M_{\delta} + G_{H}B_{H} + G_{H}B_{H} \\ N_{4} &= -B_{H}M_{\delta} - M_{\delta}B_{L} + (M_{\alpha}\frac{z_{\delta}}{v} - M_{\delta}\frac{z_{\alpha}}{v}) + G_{L}B_{L}B_{H} + \frac{z_{\alpha}}{v}B_{L}B_{H} + \frac{z_{\alpha}}{v}B_{L}B_{H} + G_{H}B_{H}\frac{z_{\alpha}}{v} + G_{H}B_{L}B_{H} \\ N_{3} &= -M_{\delta}W_{H}^{2} - M_{\delta}B_{L}B_{H} + B_{H}(M_{\alpha}\frac{z_{\delta}}{v} - M_{\delta}\frac{z_{\alpha}}{v}) + B_{L}(M_{\alpha}\frac{z_{\delta}}{v} - M_{\delta}\frac{z_{\alpha}}{v}) - M_{\delta}W_{L}^{2} + G_{L}W_{H}^{2}B_{L} \\ &+ G_{L}B_{L}B_{H}\frac{z_{\alpha}}{v} + M_{\alpha}G_{L}B_{L} + M_{\alpha}G_{H}B_{H} + G_{H}B_{L}B_{H}\frac{z_{\alpha}}{v} + G_{H}W_{L}^{2}B_{H} \\ N_{2} &= -M_{\delta}W_{H}^{2}B_{L} + W_{H}^{2}(M_{\alpha}\frac{z_{\delta}}{v} - M_{\delta}\frac{z_{\alpha}}{v}) - M_{\delta}W_{L}^{2}B_{H} + B_{L}B_{H}(M_{\delta}\frac{z_{\delta}}{v} - M\frac{z_{\alpha}}{v}) \\ &+ W_{L}^{2}(M_{\alpha}\frac{z_{\delta}}{v} - M_{\delta}\frac{z_{\alpha}}{v}) + W_{H}^{2}G_{L}B_{L}\frac{z_{\alpha}}{v} + B_{H}G_{L}B_{L}M_{\alpha} + B_{L}G_{H}B_{H}M_{\alpha} + W_{L}^{2}G_{H}B_{H}\frac{z_{\alpha}}{v} \\ \end{split}$$

$$\begin{split} N_{1} &= -M_{3}W_{H}^{2}W_{L}^{2} + W_{H}^{2}B_{L}(M_{\alpha}\frac{2S}{V} - M_{\delta}\frac{2\alpha}{V}) + B_{H}W_{L}^{2}(M_{\alpha}\frac{2S}{V} - M_{\delta}\frac{2\alpha}{V}) + W_{H}^{2}G_{L}B_{L}M_{\alpha} \\ &+ W_{L}^{2}G_{H}B_{H}M_{\alpha} \\ N_{0} &= W_{H}^{2}W_{L}^{2}(M_{\alpha}\frac{2S}{V} - M_{S}\frac{2\alpha}{V}) \\ D_{6} &= B_{L} + B_{H} + \frac{2\alpha}{V} - K_{9}K_{r}_{9}N_{S} \\ D_{5} &= W_{L}^{2} + B_{L}\frac{2\alpha}{V} + M_{\alpha} + B_{L}B_{H} + B_{H}\frac{2\alpha}{V} + W_{H}^{2} - K_{9}K_{r}_{9}N_{4} - K_{9}N_{5} \\ D_{4} &= B_{L}M_{\alpha} + W_{L}^{2}\frac{2\alpha}{V} + B_{H}W_{L}^{2} + B_{H}B_{L}\frac{2\alpha}{V} + B_{H}M_{\alpha} + W_{H}^{2}B_{L} + W_{H}^{2}\frac{2\alpha}{V} - K_{9}K_{r}_{9}N_{5} - K_{9}N_{4} \\ D_{5} &= W_{L}^{2}M_{\alpha} + B_{H}B_{L}M_{\alpha} + B_{H}W_{L}^{2}\frac{2\alpha}{V} + W_{H}^{2}W_{H}^{2} + W_{H}^{2}B_{L}\frac{2\alpha}{V} + W_{H}^{2}M_{\alpha} - K_{9}K_{r}_{9}N_{2} - K_{9}N_{5} \\ D_{2} &= B_{H}W_{L}^{2}M_{\alpha} + B_{L}W_{H}^{2}M_{\alpha} + W_{L}^{2}W_{H}^{2}\frac{2\alpha}{V} - K_{9}K_{r}_{9}N_{1} - K_{9}N_{2} \\ D_{1} &= W_{L}^{2}W_{H}^{2}M_{\alpha} - K_{9}K_{r}_{9}N_{0} - K_{9}N_{1} \\ D_{0} &= -K_{9}N_{0} \end{split}$$

For the bending mode parameters selected and the plant parameters for time = 40 seconds the transfer function H(s) is:

$$H(s) = \frac{\theta(s)}{\theta_c(s)} = \frac{34.97(s+48.4)(s-48.7)(s+0.018)(s+0.215+/-j48.65)}{(s+0.01)(s+3.63+/-j6.997)(s-3.54+/-j38.15)}$$

$$(s-2.91+/-j62.25)$$

The transfer function H(s) was factored using the "roots" program contained in Ref. [7]. The location of the poles was confirmed by finding the eigenvalues of the A matrix using the "BASMAT" program also contained in Ref. [7]. The poles and zeros of H(s) are plotted in Figure 2-16.

The system composed of the plant plus bending modes is clearly unstable with four poles of the closed loop transfer function in the right half of the S-plane.

Figure 2-17 shows the simulation the system shown in Figure 2-9 for a step input of 0.1 radians. Line 1 of Figure 2-17 is the response of the plant without bending modes and line 2 is the response of the system composed of the plant with bending modes. The vertical scaling in Figure 2-17 was restricted to keep the response of the plant in proper perspective. The restriction of the vertical scale causes saturation of the plot of the system response (line 2). Figure 2-18 shows the response of the system with the vertical scale extended to remove the effects of saturation of the plot. For clarity, the response of the plant without bending modes was not included in Figure 2-18.

To validate the simulation, the time response of the state equations with a 0.1 radian step input was determined by using the "RTRESP" program contained in Ref. [7]. The pitch angle of the missile,  $\theta$  was found to be described by the equation:

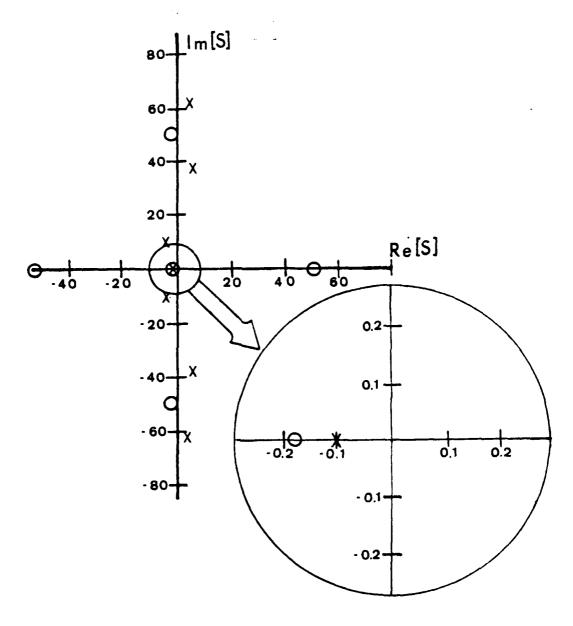
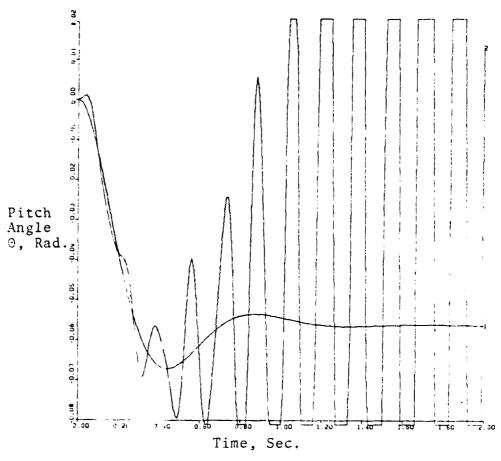


Figure 2-16 Location of Polse and Zeros of the Plant with Two Bending Modes



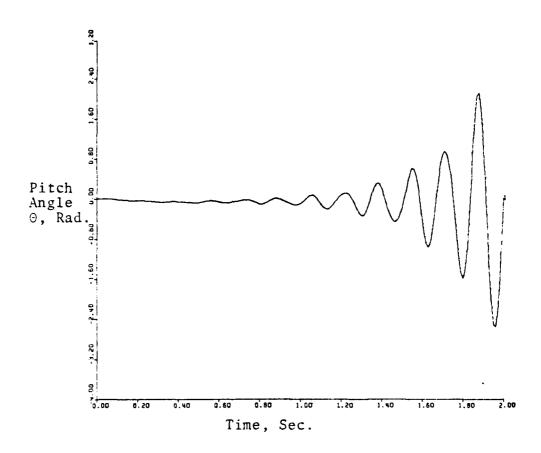
System: Third order missile model with two bending modes and no adaptive notch filters

Input: 0.1 radian step command

Line 1 is the nominal missile response without bending modes

Line 2 is the missile response with two bending modes

Figure 2-17 Missile Response with Two Bending Modes



System: Third order missile model with two bending modes and no adaptive notch filters

Input: 0.1 radian step command

Figure 2-18 Missile Response with Two Bending Modes (Expanded Scale)

$$\theta(t) = -0.09952 + 0.0457 e^{-0.01t}$$

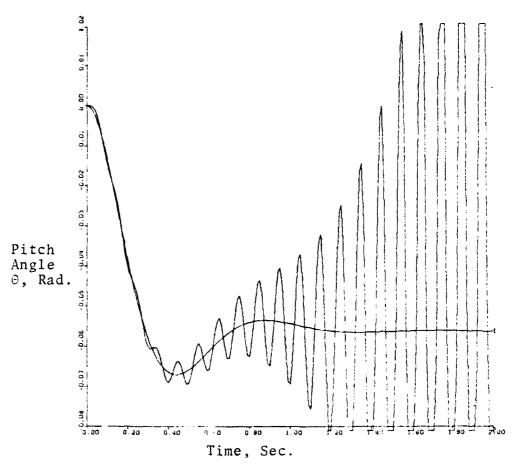
$$+ 0.0582 e^{-3.63t} \cos(6.997t - 0.41)$$

$$+ 0.00246 e^{3.54t} \cos(38.15t - 2.45)$$

$$+ 0.00093 e^{2.91t} \cos(62.25t + 3.06)$$

At time = 1.0 seconds, the above equation indicates the pitch angle will be  $\theta(1)$  = -0.10162 radians. The numerical results of the simulation used to generate Figure 2-17 indicate the pitch angle to be  $\theta(1)$  = -0.1017 radians. The preceeding results indicate the simulation program is valid.

The system was simulated with only the high frequency bending mode and with only the low frequency bending mode. The purpose of these simulations was to show that each bending mode would by itself destabilize the system and that the frequency of the oscillation of the resulting unstable system would reflect very nearly the center frequency of the bending mode that destabilized the system. Figure 2-19 illustrates the response of the system for a 0.1 radian step input when only the high frequency bending mode was present. Figure 2-20 shows the same simulation with an expanded vertical scale. Figure 2-21 shows the response of the system for a 0.1 radian step input with only the low frequency bending mode present. Figure 2-22 shows the same simulation with an expanded vertical scale. Figure 2-23 shows the system response with both bending modes for a ramp input  $\theta_c(t) = 0.05t.$ 



System: Third order missile model with 10 Hz bending mode and no adaptive notch filter

Input: 0.1 radian step command

Line 1 is the nominal missile response without bending modes

Line 2 is the missile response with 10 Hz bending modes

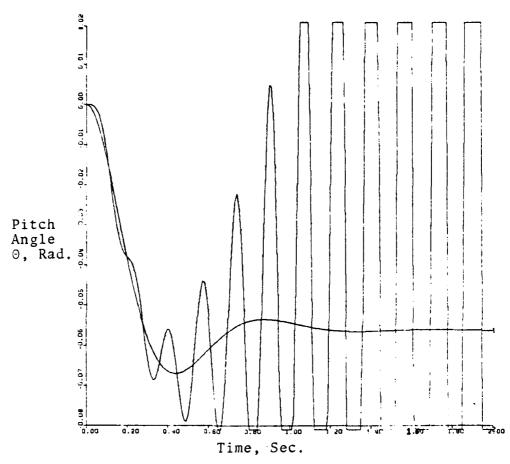
Figure 2-19 Missile Response with 10 Hz Bending Modes

Pitch Angle Θ, Rad. 0.80 0.20 0.40 Time, Sec.

> Third order missile model with 10 Hz bending mode and no adaptive notch filter System:

Input: 0.1 radian step command

Missile Response with 10 Hz Bending Mode (expanded scale) Figure 2-20



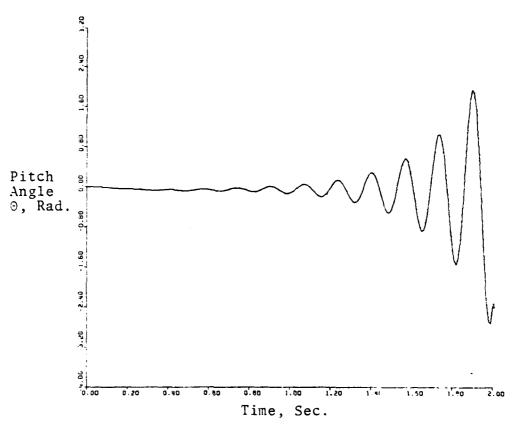
System: Third order missile model with 6 Hz bending mode and no adaptive notch filters

Input: 0.1 radian step command

Line 1 is the nominal missile response without bending modes

Line 2 is the missile response with 6 Hz bending modes

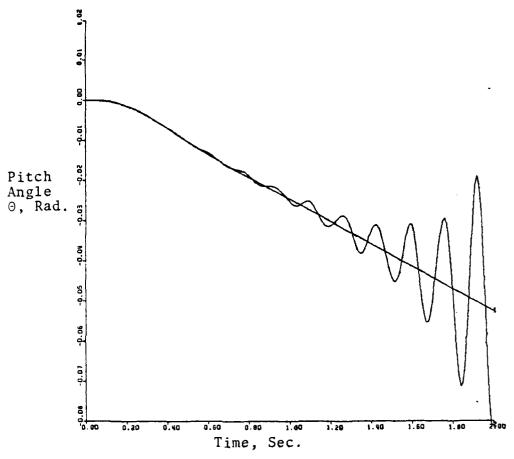
Figure 2-21 Missile Response with 6 Hz Bending Mode



System: Third order missile model with 6 Hz bending mode and no adaptive notch filters

Input: 0.1 radian step command

Figure 2-22 Missile Response with 6 Hz Bending Mode (expanded scale)



System: Third order missile model with 6 and 10 Hz bending modes and no adaptive notch filters

Input: 0.05 radian/sec ramp command

Line 1 is the nominal missile response without bending modes

Line 2 is the missile response with bending modes

Figure 2-23 Missile Response for a Ramp Input with Bending Modes

Figures 2-19 through 2-22 clearly indicate that each bending mode is in itself destabilizing. Analysis of the numerical data associated with Figures 2-19 through 2-22 confirms that the frequency of the oscillations is essentially at the frequency of the bending mode center frequency.

# III. ADAPTIVE DIGITAL FILTER DESIGN

#### A. FACTORS AFFECTING THE DESIGN

The emphasis of the design was simplicity. Significant improvement in the results could have been achieved by use of higher order filters and by using more sophisticated filters, but the improved performance would have been accomplished at the expense of obscuring the very simplicity which makes the proposed technique so appealing.

The sampling frequency used throughout this thesis is 100 hertz. This selection is dictated by the sampling frequency used by the autopilot in the Trident Missile. Higher sampling frequencies were found not to significantly improve the performance of the algorithm, however, sampling frequencies lower than 60 Hz degraded the algorithm to where it would not perform reliably.

The bending mode frequencies were selected such that one and only one bending mode would be in each of the bands of 5-8 hertz and 8-12 hertz as shown in Figure 2-6. A priori knowledge of the band or range of frequencies over which a given bending mode may vary during the flight of the missile is essential in this design. If specific events during the flight such as staging change the bands of the bending modes then the algorithm may also be modified to adapt to the new distribution with the only requirement being that the times

or events which change the band limitations be preprogrammed in the microprocessor algorithm.

#### B. DESIGN OF THE ALGORITHM MODULES

Figure 3-1 shows the modular nature of the algorithm for the determination, tracking and notch filtering of the bending mode signals. The sequence of modules associated with the determination, tracking and notch filtering for each of the bending modes are collectively termed a channel. The channels are identical except for the numerical values of the coefficients; therefore, only the design of the 8-12 hertz (high) channel is presented in detail. The results of the design of each of the modules comprising the low channel are presented when different from the corresponding module in the high channel.

## 1. The Bandpass Filter Module

The overall bandpass filter was designed as two cascaded second-order bandpass sections. The first section is a first-order Butterworth lowpass Filter transformed into a bandpass filter and then transformed into the z-domain using the bilinear transformation. The second section is also a bandpass filter designed to adjust the overall shape of the gain curve to the desired form.

A first-order Butterworth lowpass Filter normalized to a cutoff frequency of 1 radian/second has a transfer function:

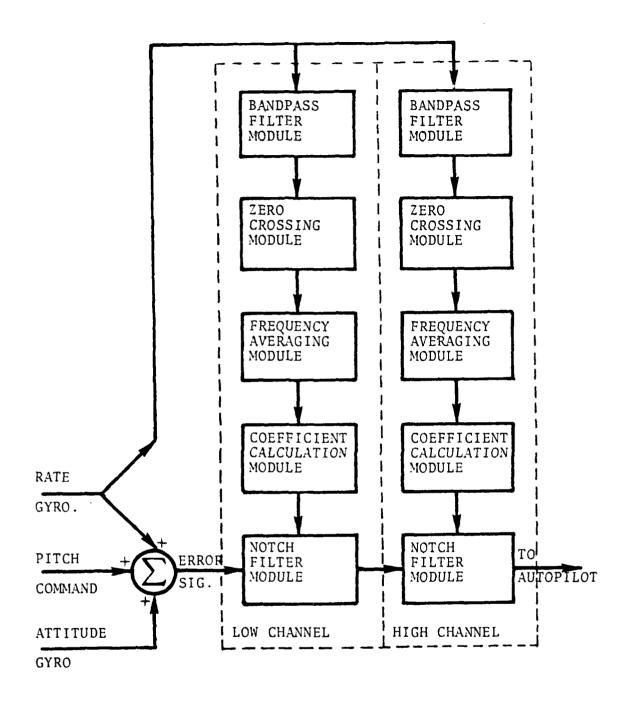


Figure 3-1 Adaptive Notch Filter Algorithm Modules

$$H_{LP}(s) = \frac{1}{s+1}$$

The transformation from lowpass to bandpass is:

$$s + \frac{s^2 + W_c^2}{Bs}$$

where:

B is the 3 dB bandwidth defined as  $\rm W_{C}$  -  $\rm W_{L}$ 

 $\text{W}_{\text{c}}$  is the center frequency defined as  $\sqrt{\text{W}_{\text{c}}\text{W}_{\text{L}}}$ 

 $\rm W_{C}$  is the upper 3 dB frequency in rad/sec and  $\rm W_{L}$  is the lower 3 dB frequency in rad/sec.

The resulting analog domain transfer function for the bandpass filter is:

$$H_{BP}(s) = \frac{Bs}{s^2 + Bs + W_c^2}$$
 (4)

Before applying the bilinear transformation to transform the analog bandpass filter to the discrete domain it is necessary to prewarp the center frequency  $W_{C}$  [8]. The prewarping is done by using the following transformation:

$$W_{A} = \frac{2 \text{ TAN } \left(\frac{\Omega_{D}}{2}\right)}{T} \tag{5}$$

where:

 $\boldsymbol{\Omega}_{D}$  is the desired discrete or digital frequency defined as:

$$\Omega_D = W_C T$$

T is the sampling frequency.

 $W_c$  is the analog center frequency defined as  $W_c = (W_u W_L)^{1/2}$ 

Selecting 8.0 hertz as the lower cutoff frequency and 12.0 hertz as the upper cutoff frequency. The values to be used in equations (4) and (5) become:

$$W_L = 2\pi \cdot 8.0 = 50.265 \text{ rad/sec}$$
 $W_u = 2\pi \cdot 12.0 = 75.398 \text{ rad/sec}$ 
 $W_c = (W_u W_L)^{1/2} = 61.652 \text{ rad/sec}$ 

$$B = W_{11} - W_{L} = 25.133 \text{ rad/sec}$$

Applying equation (5) with the selected value of  $\mathbf{W}_{\mathbf{C}}$  yield the prewarped center frequency:

$$W_A = 63.582 \text{ rad/sec}$$

Substituting the above value, equation (4) becomes:

$$H(s) = \frac{25.133 \text{ s}}{s^2 + 25.133 \text{ s} + 4042.77}$$
 (6)

The bilinear transformation for the s-domain to the z-domain is:

$$s = \frac{2(Z - 1)}{T(Z + 1)}$$

Applying the transformation to equation (6), the discrete transfer function for the bandpass filter becomes:

$$H_1(Z) = \frac{0.103(Z^2 - 1)}{Z^2 - 1.4677 Z + 0.79405}$$

After slight adjustments to obtain the desired gain and crossover frequency with the low frequency channel bandpass filter (see Figure 3-9), the transfer function  $H_1(Z)$  is:

$$H_1(Z) = \frac{0.1 (Z^2 - 1)}{Z^2 - 1.45625 Z + 0.81}$$

The pole and zero configuration of  $H_1(Z)$  is shown in Figure 3-2 and the frequency response of  $H_1(Z)$  is shown in Figure 3-3.

As expected, the frequency response of H<sub>1</sub>(Z) is too flat to provide the needed stopband attenuation for the adjacent channels. The frequency response of the overall bandpass filter is greatly improved by adding a second section of filter with a sharp resonant peak at the center frequency. A bandpass filter with the desired resonant peak was designed directly in the z-domain using a digital filter frequency response program (program 3-5) to adjust the poles and zeros to obtain the desired characteristics. The transfer function of the second filter section is:

$$H_2(Z) = \frac{0.456(Z^2 - 0.809 Z + 0.25)}{Z^2 - 1.3753 Z + 0.7225}$$

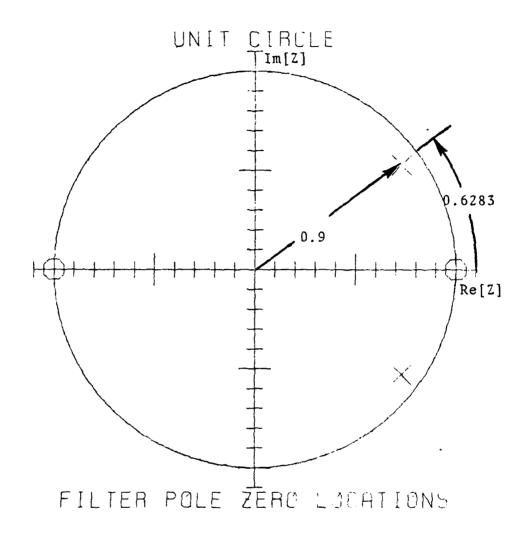


Figure 3-2 Discrete Bandpass Filter Pole/Zero Locations

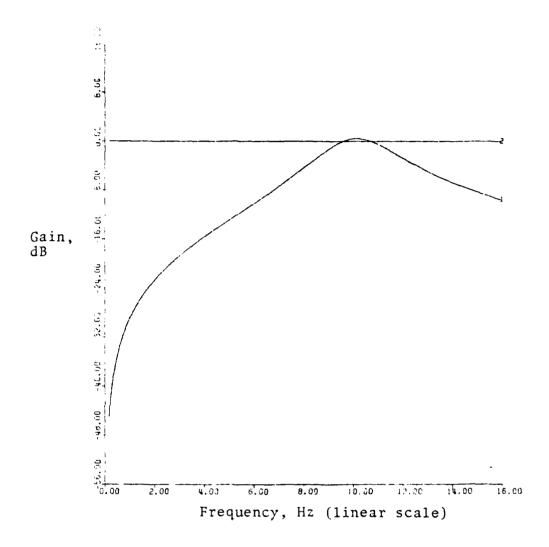


Figure 3-3 Frequency Response of the Tirst Section of the High Frequency Digital Bandpass Filter

The pole and zero configuration of  $H_2(\mathbb{Z})$  is shown in Figure 3-4. The frequency response of  $H_2(\mathbb{Z})$  is shown in Figure 3-5.

Figure 3-6 shows the flow graph of the algorithm for the implementation of the two cascaded sections and Figure 3-7 shows the resulting frequency response of the cascaded sections.

Figure 3-8 shows the frequency response of the low channel bandpass filter designed in the same manner. Figure 3-9 illustrates the resulting band coverage of each channel.

The possibility of a bending mode occurring at the eight-hertz cross-over frequency between channels causing both channels to lock on that frequency and leaving one bending mode unattenuated is compensated for by initializing both notch filters at the cross-over frequency, thereby attenuating a bending mode at eight-hertz immediately and freeing either channel to track and remove the unattenuated bending mode.

## 2. The Zero Crossing Detector Module

The zero crossing detector is based on a linear estimate of the crossing time if the amplitude of the output of the bandpass filter changes signs between samples. Linear estimation of the crossing time is a feature incorporated into the digital simulation language program (DSL) as the cross function but could also be programmed using the algorithm shown in Figure 3-10. The potential for using

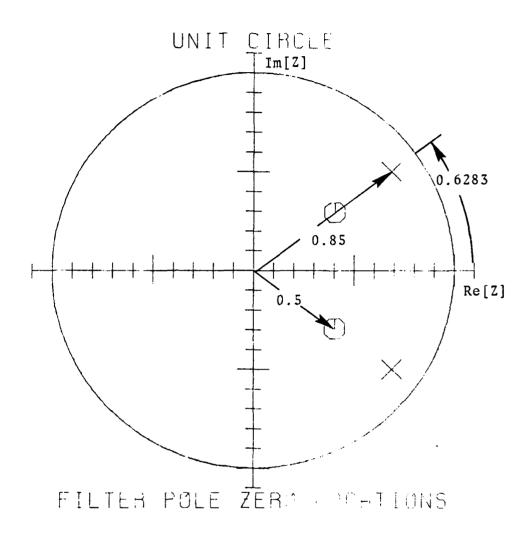


Figure 3-4 Discrete Bandpass Filter Pole/Zero Locations

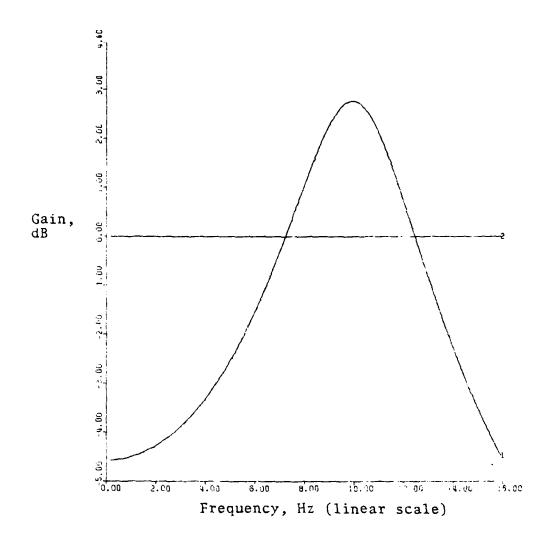


Figure 3-5 Frequency Response of the Second Section of the High Frequency Digital Bandpass Filter

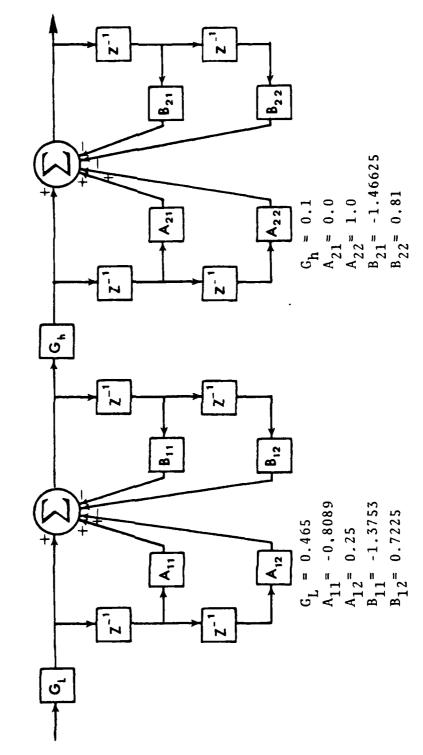


Figure 3.6 Digital Filter Implementation

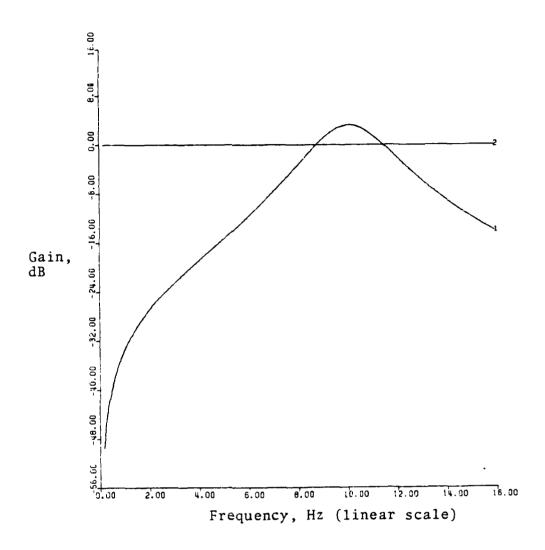


Figure 3-7 Frequency Response of Cascaded Filter Sections of the High Frequency Bandpass Filter

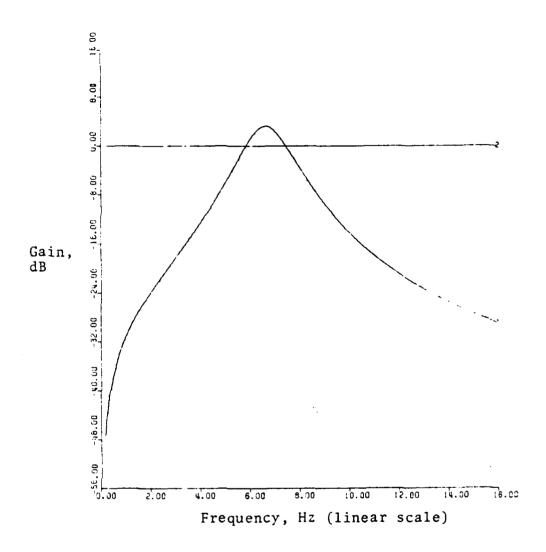


Figure 3-8 Frequency Response of Low Frequency Digital Bandpass Filter

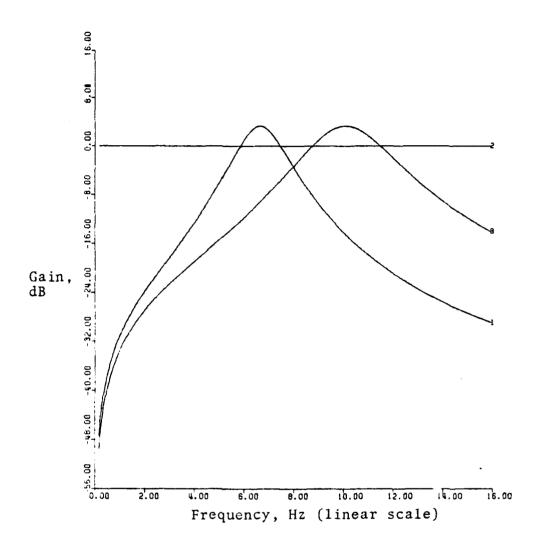


Figure 3-9 Frequency Coverage of High and Low Frequency Digital Bandpass Filter

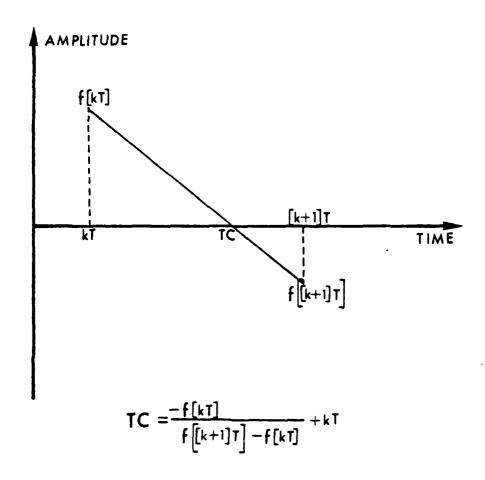


Figure 3-10  $\,$  Zero Crossing Time Algorithm

a sinusoidal curve estimation rather than a linear estimation was considered and dismissed because any increase in the accuracy of the estimate of the zero crossing time was offset by the jitter in the actual crossing time caused by leakage into the channel of the adjacent bending mode and plant frequencies.

The major deficiency in the use of a zero crossing detector as a frequency measuring device is the nonlinear error in the frequency estimate as a function of the actual frequency. For example, if the frequency being measured is 5.0 hertz the half-period measured should be 0.1 seconds. If noise caused a 0.01 second measurement error and the measured half-period was 0.09 seconds then the frequency detector would estimate the input frequency to be 5.55 hertz. If the input frequency was 10.0 hertz the same 0.01 second error would result in an estimate of the input frequency of 12.5 hertz, a five times greater error for the same measurement error.

The effect of the nonlinear quality of the estimated frequency in the presence of noise causes a much greater variation in the estimate of the higher frequency bending modes and contributes to the limit cycle problem described below.

### 3. The Frequency Averaging Module

The primary source of limit cycle behavior in the tracking algorithm appears to be due to leakage of an

adjacent bending mode frequency into the zero crossing detector causing a periodic error in the frequency determination. The frequency averaging module simply determines the mean of the last detected frequency from the frequency detector and the current notch filter center frequency. The mean of the two frequencies becomes the new notch filter center frequency. The process of averaging the last detected frequency with the current notch filter center frequency reduces the amplitude of the limit cycle but does not eliminate it. To further reduce the amplitude of the limit cycle, several approaches may be taken:

- (a) Greatly improve the stopband attenuation and rolloff characteristics of the bandpass filters. This approach is discussed in the conclusions contained in Chapter Five.
- (b) Average the detected frequency over 3 sufficient number of zero crossings before moving the notch. This approach was found to significantly reduce the amplitude of the limit cycle but was so slow in moving the notch to the correct frequency that the bending modes would increase to such an amplitude that the missile would be destroyed

# 4. Design of the Notch Filter Module

The design of a discrete notch filter and the calculation of the coefficients is simple and efficient. Figure 3-11 illustrates the pole and zero location of a second-order notch filter on the Z-plane. Since the zero is located on the unit circle, the center frequency  $W_{\rm C}$  of the notch is completely specified by the angle  $\Omega_{\rm C}$ .

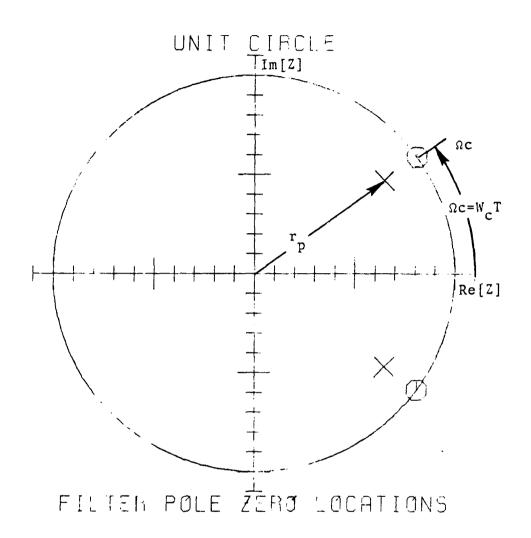


Figure 3-11 General Pole/Zero Locations for a Second-Order Discrete Notch Filter

The angle  $\Omega_{\rm C}$  is referred to as the discrete frequency and is defined as the angle from the positive real axis to the zero such that:

$$\Omega_{C} = W_{C}T$$

where:

 $\mathbf{W}_{\mathbf{C}}$  is the desired notch center frequency in rad/sec T is the sampling period in seconds

The location of the zero on the unit circle at a selected discrete frequency,  $\Omega_{\rm C}$ , ensures that the center of the notch will be at the desired frequency completely independent of the selected location of the poles. The location of the poles on the same radial (discrete frequency) as the zero maintains the approximate symmetry of the notch. The radius of the poles determines the bandwidth of the notch. The closer the poles are to the unit circle, the narrower the notch will be and the longer the settling time.

The transfer function  $H_{N}\left( Z\right)$  for the notch filter is of the form:

$$H_N(Z) = \frac{G(Z^2 - A1 Z + 1)}{Z^2 - B1 Z + B2}$$

where the coefficients are defined by the following formulas:

$$A1 = 2 \cos (W_C T)$$

$$B1 = 2 r_{p} cos (W_{c}T)$$

$$B2 = r_{p}^{2}$$

 $\mathbf{r}_{p}$  is the radius of the poles  $\mathbf{W}_{c}$  is the desired center frequency of the notch in rad/sec G is the gain

For unity DC gain  $H(Z) \mid Z=+1=1$  yields the formula

$$G = \frac{1 - B1 + B2}{2 - A1}$$

The relationship between the pole radius and the 3 dB bandwidth of the notch filter is a function of center frequency but can be approximated by making certain simplifying assumptions. Figure 3-12 shows the geometry on the unit circle when the discrete frequency,  $W_{\rm D}T$  is at the 3 dB cutoff frequency. The gain at the cutoff frequency is:

$$G = \frac{|{}^{2}\mathbf{1}|}{|{}^{2}\mathbf{1}|} \frac{|{}^{2}\mathbf{2}|}{|{}^{2}\mathbf{1}|} = 0.707 \tag{7}$$

In this application it is reasonable to assume that  $|Z_2|\tilde{z}|P_2|$ , the poles are close to the unit circle, and the bandwidth of the filter is small  $(W_C T\tilde{z}W_D T)$ . With the above assumptions, equation (7) then reduces to:

$$G = \frac{|Z_1|}{|P_1|} = 0.707 \tag{8}$$

Using the pythagorean theorem and substituting  $Z_1^2 = 0.5 P_1^2$  from equation (8) the following relationship can be found:

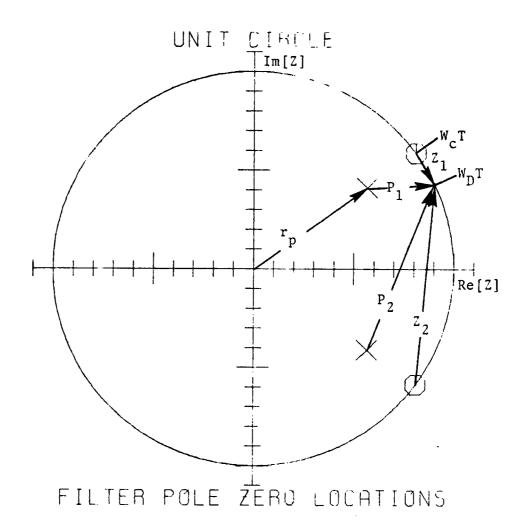


Figure 3-12 Vectors Used to Calculate Notch Filter Bandwidth

$$(1 - r_p) = Z1 \tag{9}$$

For small angles the cord can be assumed to be equal to the ARC length, therefore:

$$Z1 = W_C T - W_D T = 0.5 B_D = 0.5 B_W T$$
 (10)

where:

 $\boldsymbol{B}_{\boldsymbol{D}}$  is the discrete bandwidth in rad

 $\mathbf{B}_{\mathbf{W}}$  is the analog bandwidth in rad/sec

Substituting equation (10) into equation (9) and solving for  $B_W$  yields the approximate relationship between the notch filter analog frequency bandwidth and the pole radius in the discrete domain.

$$B_{W} = \frac{2(1-r_{p})}{T} \tag{11}$$

The numerical data associated with the frequency response curves for the notch filters indicates that equation (11) yields bandwidths that are larger than the desired bandwidths but the error is less than 10 percent in the frequency range of 5 to 15 hertz.

Figure 3-13 shows the gain vs frequency response of the low channel notch filter with a center frequency of 6.0 hertz and a pole radius of 0.9. This configuration has a

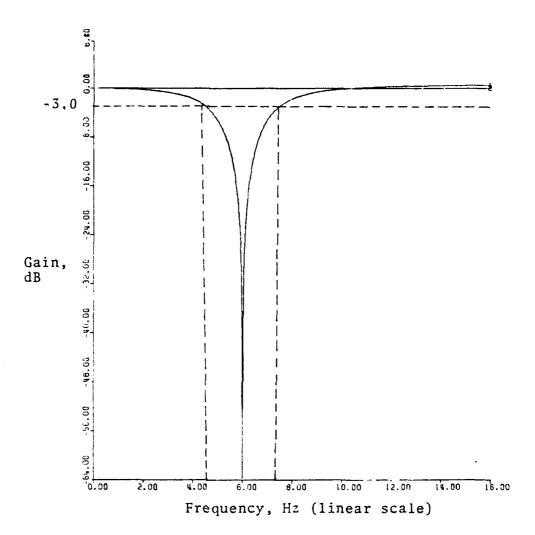


Figure 3-13 Frequency Response of Digital Notch Filter with 0.9 Pole Radius Centered at 6 Hz

3 dB bandwidth of 2.95 hertz. Figure 3-14 shows the phase vs frequency response of the same notch filter.

Figure 3-15 shows the gain vs frequency response of the high channel notch filter with a center frequency of 10.0 hertz and a pole radius of 0.8. This configuration has a 3 dB bandwidth of 5.9 hertz. Figure 3-16 shows the phase vs frequency response of the same notch.

The argument used to create Figure 2-6 established that the higher of the two bending modes would have a wider bandwidth than the lower frequency bending mode, therefore the bandwidth of the notch filter for the high channel was designed to be wider than the low channel. There is a limit to which the notch bandwidth can be increased without inducing excessive phase loss at the plant operating frequency of two-hertz. For the notch bandwidths used in this algorithm the high channel, with the notch centered at 10.0 hertz, introduces a phase loss of 7.75 degrees at two-hertz and the low channel, with the notch centered at 6.0 hertz, introduces a phase loss of 11.0 degrees at two-hertz. The combined phase loss introduced by the notch filters used in this algorithm does not have a pronounced effect on the stability of the plant.

# 5. Flow Chart of the Algorithm

Figure 3-17 provides a flow chart of the entire algorithm. The "prime time" computations are the processing of the error signal and outputting the filtered value to the

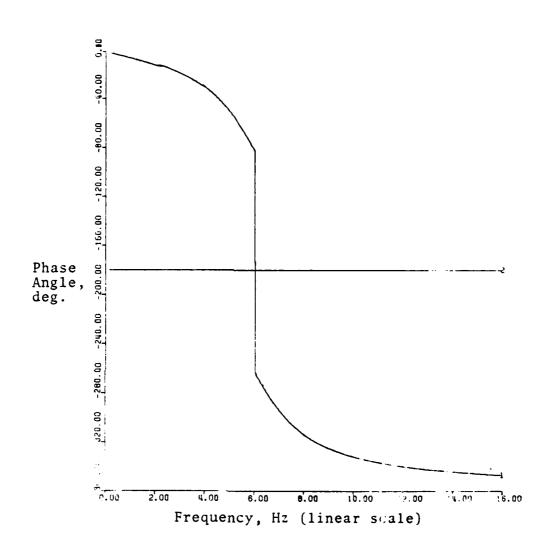


Figure 3-14 Frequency Response of Digital Notch Filter with 0.9 Pole Radius Centered at 6 Hz

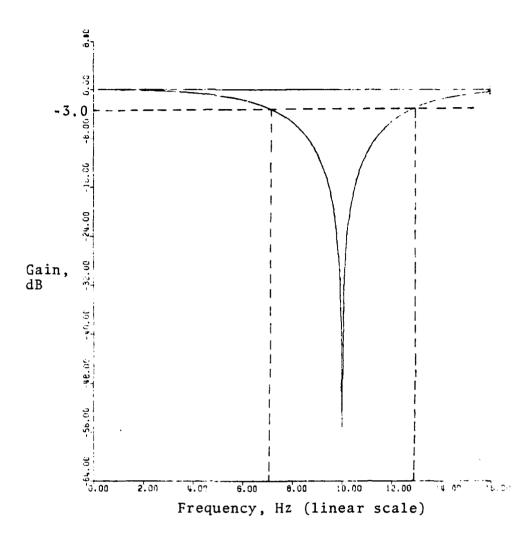


Figure 3-15 Frequency Response of Digital Notch Filter with 0.8 Pole Radius Centered at 10 Hz

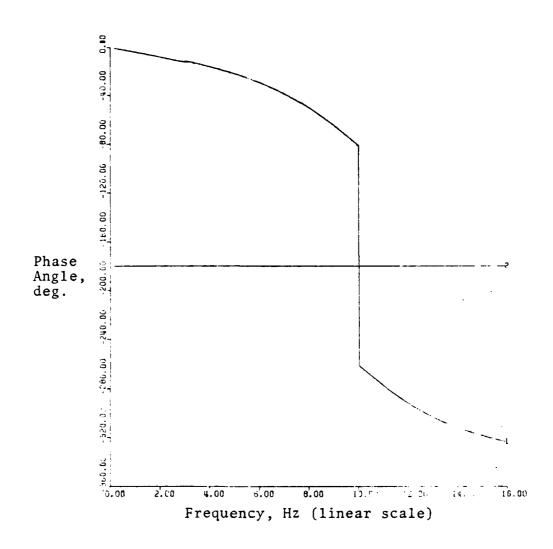


Figure 3-16 Frequency Response of Digital Notch Filter with 0.8 Pole Radius Centered at 10 Hz

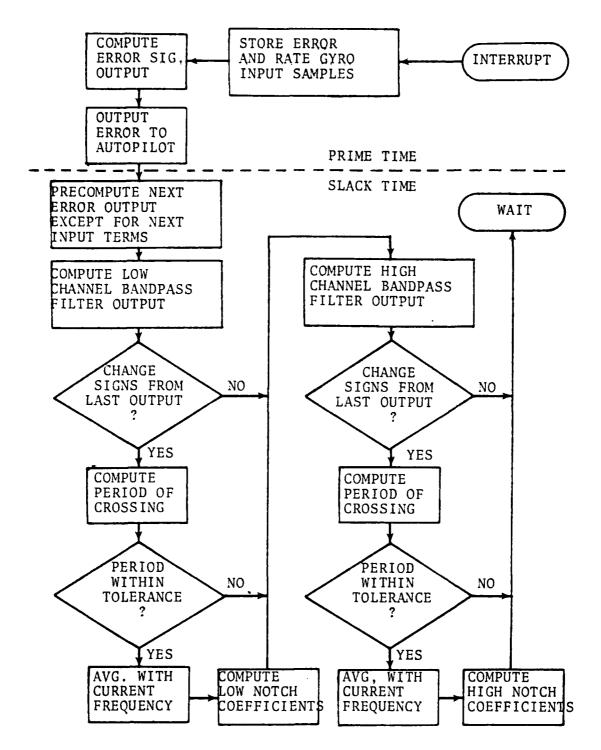


Figure 3-17 Algorithm Flowchart

autopilot with minimum processing delay. The "slack time" computations are the computations performed after the error signal has been processed and which do not introduce processing delay in the control system. With a 100 hertz sampling frequency, sufficient time should be available to complete all slack time calculations every cycle, with currently available microprocessors.

#### C. TEST OF THE ALGORITHM

The algorithm was first tested as shown in Figure 3-18. An input signal consisting of the sum of equal amplitude 2.0, 6.0 and 10.0 hertz sine waves initially in phase was used to simulate the rate gyro output signal with bending mode contamination. The signal was first passed through the tracking notch filter modules and the result was then used as an input to the two channels of the bending mode frequency determination, tracking and filtering algorithm. The unusual process of passing the input signal through the notch filters first was done to allow the effects of feedback to be observed as the notch filters remove the very signals that the remainder of the algorithm is trying to track.

Figure 3-19 shows the two-hertz input signal (line 3) to the notch filters and the resulting output signal (line 2, accentuated). The notch filters were reasonably able to filter out the 6 and 10 hertz components and pass the

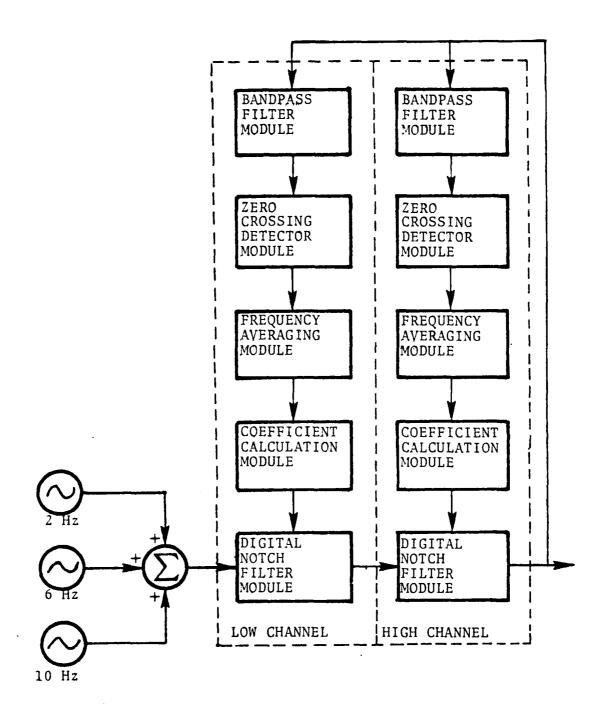
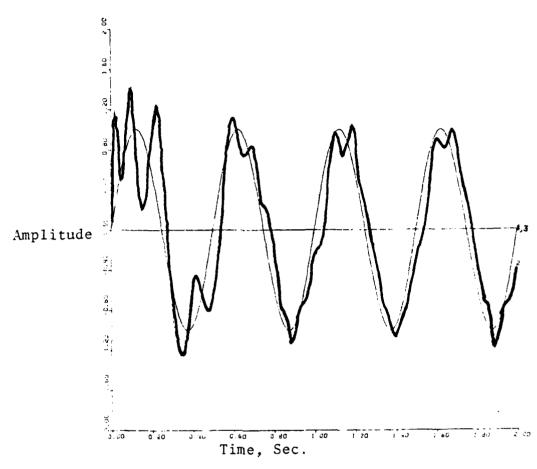


Figure 3-18 Adaptive Notch Filter Algorithm Test Arrangement



Line 1 is zero amplitude reference

Line 2 is the output of the adaptive digital notch filters

Line 3 is 2 Hz input signal

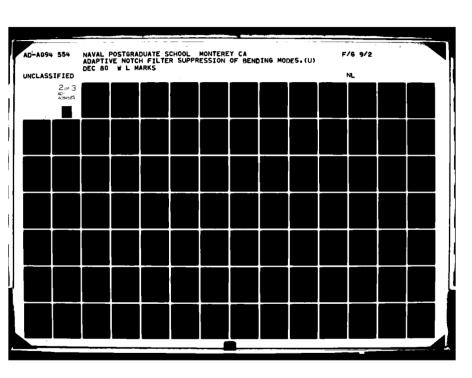
Figure 3-19 Output of the Adaptive Digital Notch Filters

two-hertz. The numerical data associated with Figure 3-19 indicates an average phase loss of 18 degrees was experienced over the 2 seconds of simulation.

Figure 3-20 shows the tracking history of each of the channels. The low channel locked on the six-hertz frequency (actual lock on frequency was 6.0546 Hz) after 0.56 seconds and remained locked on for the remainder of the simulation. The high channel went into a four cycle per second limit cycle with an average frequency of 9.85 hertz. The cause of the limit cycle is leadage of the two-hertz signal when the amplitude of the two-hertz reaches near maximum amplitudes. The limit cycle has a minimum effect on the output of the notch filters since the high channel notch bandwidth is nearly six-hertz and the magnitude of the limit cycle is only 1.65 hertz.

Figure 3-21 shows the input (line 1) and output (line 2, accentuated) of the low frequency channel bandpass filter.

Figure 3-22 shows the input (line 1) and the output (line 2, accentuated) of the high channel bandpass filter. The effects of the leadage of the two-hertz signal can be seen in the output of both filters.



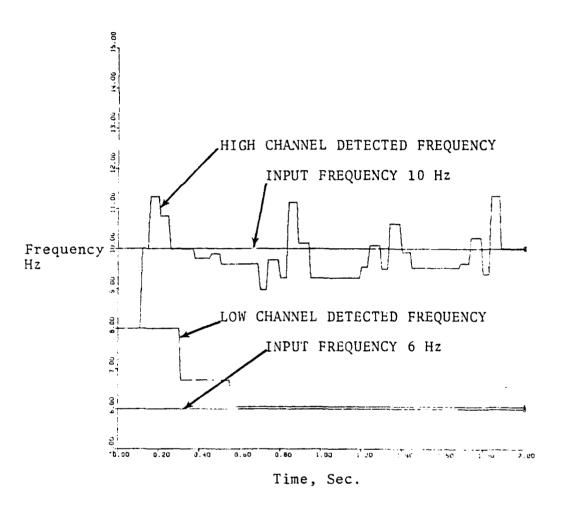
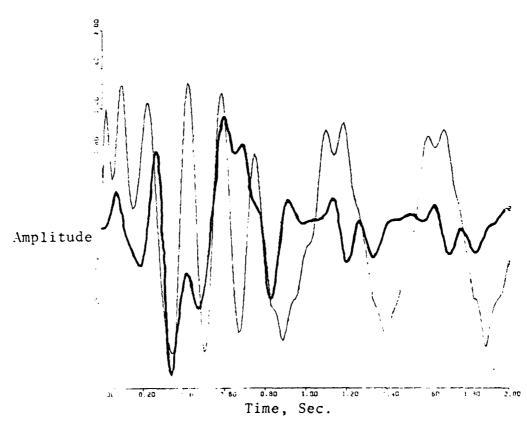


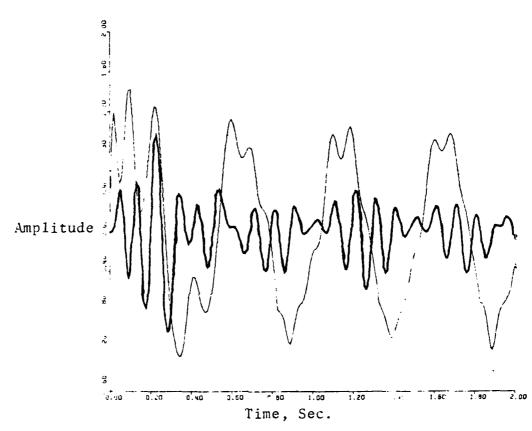
Figure 3-20 Frequency Detector Output for 6 and 10 Hz Input



Line 1 is the output from the adaptive notch filter

Line 2 is the output from the low channel bandpass filter

Figure 3-21 Low Channel Bandpass Filter Output



Line 1 is the output from the adaptive notch filters

Line 2 is the output from the high channel bandpass filter

Figure 3-22 Output from the High Channel Bandpass Filter

## IV. SIMULATION STUDIES

### A. DIGITAL SIMULATION LANGUAGE (DSL/360)

The programming languages used throughout this thesis are the IBM Digital Simulation Language (DSL/360) [9] and FORTRAN IV. DSL/360 has not been released for general use by the IBM Corporation but was used in this thesis for the simulation studies due to its enhanced capabilities. The exclusive features of DSL/360 were used only in modeling of the continuous systems. The modules of the adaptive digital filter are programmed exclusively in FORTRAN IV and may be used with any continuous systems simulation language that will accept FORTRAN subroutines.

#### B. BLOCK DIAGRAM OF THE SIMULATION MODEL

Figure 4-1 illustrates the block diagram of the system used to develop Program 4-2. The block diagram forms the core program for all the simulation studies in this chapter with the only changes being the addition of a ramp function for the input command in Program 4-3 and ramp functions to create dynamic bending mode frequencies in Programs 4-10 and 4-12.

#### C. SIMULATION CONDITIONS

The parameters of the plant selected for all the following simulation studies are from Table 2-1 at time = 40 seconds.

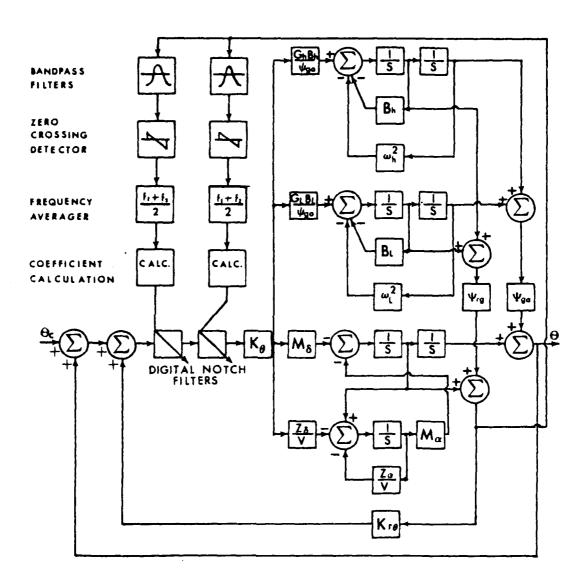


Figure 4-1 Simulation Study Model

The selected plant parameters represent the values when the missile passes through the point of maximum dynamic pressure (max Q) and is the least stable even without the presence of bending modes. When simulation studies were conducted with plant parameters yielding a more stable plant the results indicated the proposed adaptive digital filtering technique functioned essentially the same and therefore only the worst case conditions are presented.

Two pitch commands from the guidance system were selected for simulation: a 0.1 radian step input and a 0.05 radian per second ramp. The step command simulates a command from the autopilot which would normally occur at water exit, staging, or inflight restart of the guidance system after a failure. The simulation studies with a step input are intended to simulate the condition of a guidance system restart at the point in the flight when the missile has the least stability, a highly unlikely but undoubtably severe condition. The ramp input simulates a more normal condition where the autopilot responds to wind shear at the point of least stability. The ramp input response serves to demonstrate that although the bending modes are not excited as violently as they are with a step input, the adaptive digital filters successfully detect their presence and provide the proper filtering. The ramp input again includes the simulation of an inflight restart of the guidance system since

the simulation is started with no history available to the adaptive digital filters or frequency detector algorithms.

The bending mode frequencies were the primary variable in the simulation studies. The first two studies have fixed bending mode frequencies centered at 6.0 and 10.0 hertz. The third study has the bending mode frequencies again fixed but at 7.0 and 9.0 hertz to ensure that the algorithm can separate two close bending mode frequencies. The fourth study has the bending modes fixed at 5.5 and 14.0 hertz to test the ability of the algorithm to properly filter two widely separated bending mode frequencies. The final two studies have dynamic bending modes with the upper bending mode changing at the rate of 1.5 hertz per second and the lower bending mode changing at 1.0 hertz per second. rates of change far exceed the rates of change anticipated but were included as a demonstration of the capability of the algorithm to track very high rates of change in the bending mode frequencies. The final two studies illustrate the response of the system with the bending mode frequencies converging and diverging.

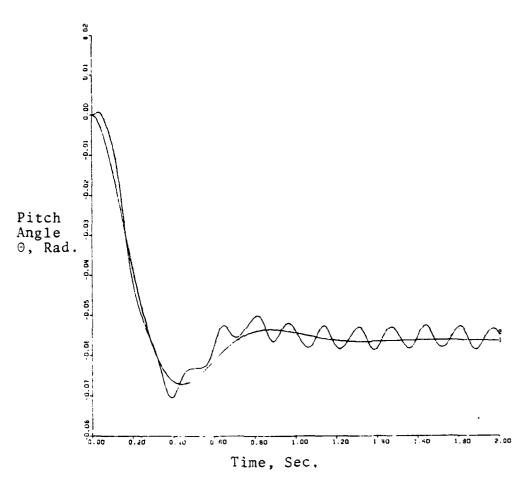
Table 4-1 provides a summary of the conditions used in the six simulation studies.

### D. SIMULATION RESULTS

Figures 4-2 and 4-3 illustrate the system response for a 0.1 radian step pitch command with the bending mode frequencies fixed at 6.0 and 10.0 Hz. Line 1 in Figure 4-2 is

TABLE 4-1

FIGURES	INPUT	BENDING MODES
4 - 2 4 - 3	0.1 rad STEP	6.0 Hz and 10.0 Hz
4 - 4 4 - 5	0.05*T rad/sec	6.0 Hz and 10.0 Hz
4 - 6 4 - 7	0.1 rad STEP	7.0 Hz and 9.0 Hz FIXED
4 - 8 4 - 9	0.1 rad STEP	5.5 Hz and 14.0 Hz FIXED
4-10 4-11	0.1 rad STEP	6.0 Hz + 1.0 Hz/sec DYNAMIC
4-12 4-13	0.1 rad STEP	8.0 Hz - 1.0 Hz/sec 9.0 Hz + 1.5 Hz/sec DYNAMIC



System: Third order missile model with fixed bending modes at 6 and 10 Hz

Input; 0.1 radian step command

Line 1 is the nominal missile response without bending modes

Line 2 is the missile response with bending modes

Figure 4-2 Missile Step Response with Fixed 6 and 10 Hz Bending Modes

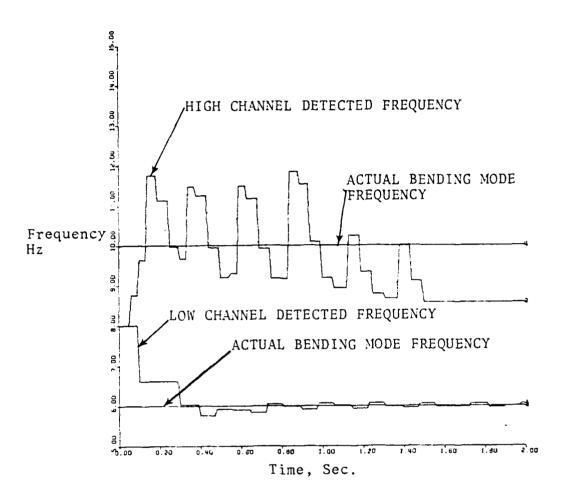


Figure 4-3 Frequency Detector Output for Fixed 6 and 10 Hz Bending Modes

the nominal response of the plant without bending modes to the same input. It is provided as a standard by which the effectiveness of the adaptive digital notch filtering may be evaluated. Line 2 in Figure 4-2 is the response of the system with the bending modes and the adaptive digital notch filters.

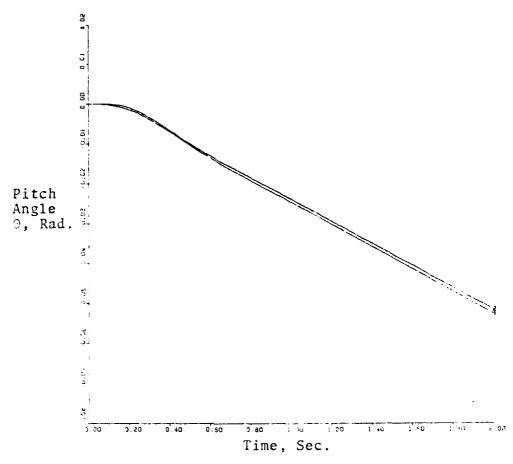
Figure 4-3 provides a history of the center frequency of the high and low channel notch filters. Line 1 is the history of the low channel (5.0-8.0 Hz) notch center frequency and Line 2 is the history of the high channel (8.0-12.0 Hz) notch center frequency. Lines 3 and 4 indicate the actual bending mode center frequencies.

Figure 4-2 must be compared with Figure 2-17 to gain the proper perspective on the degree to which the system has been stabilized by the adaptive notch filters. Figure 2-17 is precisely the same system and the same input except the adaptive digital notch filters were not in the system simulated in Figure 2-17. The amount of leakage of the 6.0 hertz bending mode frequency through the notch filer is due to the relatively low precision coefficients used in the notch filters. Simulation with double precision coefficients reduced the leakage considerably but the implementation of the notch filter with this precision was not considered practical for implementation with a microprocessor and therefore not pursued.

Figure 4-3 illustrates that the algorithm can rapidly and accurately track the 6.0 hertz bending mode frequency but exhibits limit cycle behavior when tracking the 10.0 hertz bending mode. The limit cycle behavior can be attributed to the low frequencies associated with the plant dynamics causing errors in the frequency detector as discussed in Chapter Three. The limit cycle does not appear to diminish the high channel's effectiveness in eliminating the 10.0 Hz bending mode in that there is no evidence of the 10.0 hertz bending mode in the output and it is attenuated to the point that the frequency detector can no longer track it after 1.5 seconds.

Figures 4-4 and 4-5 show the response of the system for a 0.05\*T ramp pitch command with bending modes centered at 6.0 and 10.0 hertz. Comparing Figure 4-4 with Figure 2-23 it is evident that when the adaptive digital notch filters are included in the system the response is essentially the same as if no bending modes were present. Figure 4-5 shows the ability of the high channel to much more accurately lock onto the 10.0 hertz bending mode when the high plant rates are not present. The very satisfactory performance for a ramp input indicated that this input did not stress the ability of the adaptive digital notch filter algorithm and it was therefore not used in the remainder of the simulation studies.

Figures 4-6 and 4-7 show the response of the system for a 0.1 radian step input when the bending mode frequencies



Third order missile model with fixed bending modes at 6 and 10  $\rm Hz$ System:

Input: 0.05 radian/sec ramp command

Line 1 is the nominal missile response without bending modes

Line 2 is the missile response with bending modes

Figure 4-4 Missile Ramp Response with Fixed 6 and 10 Hz Bending Modes

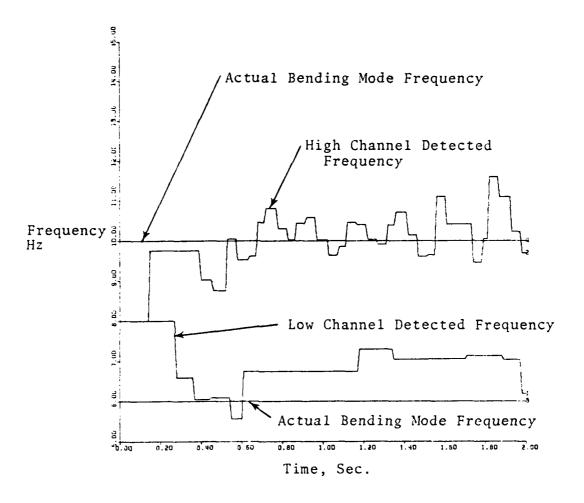
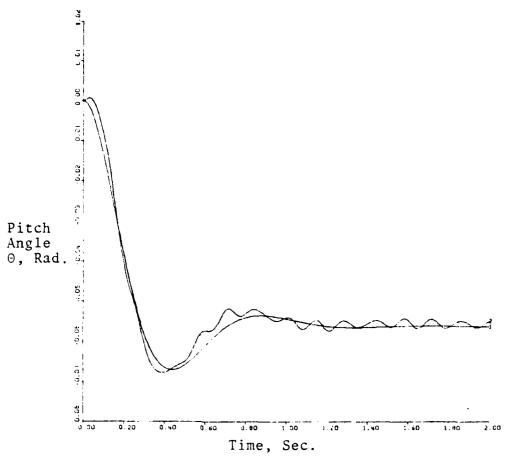


Figure 4-5 Frequency Detector Output for Fixed 6 and 10 Hz Bending Modes



System: Third order missile model with fixed bending modes at 7 and 9 Hz

Input: 0.1 radian step command

Line 1 is the nominal missile response without bending modes

Line 2 is the missile response with bending modes

Figure 4-6 Missile Step Response for Fixed 7 and 9 Hz Bending Modes

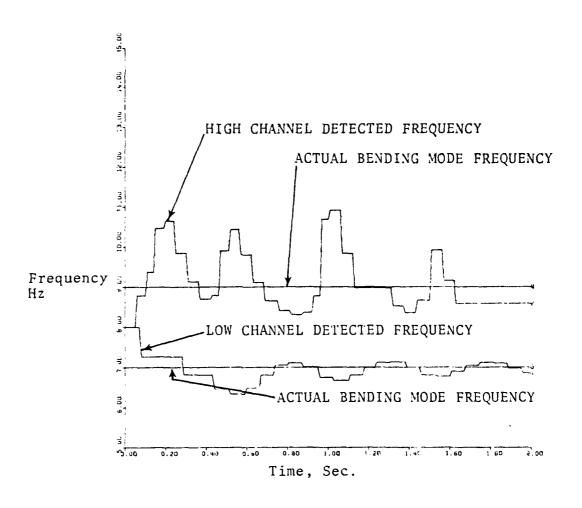
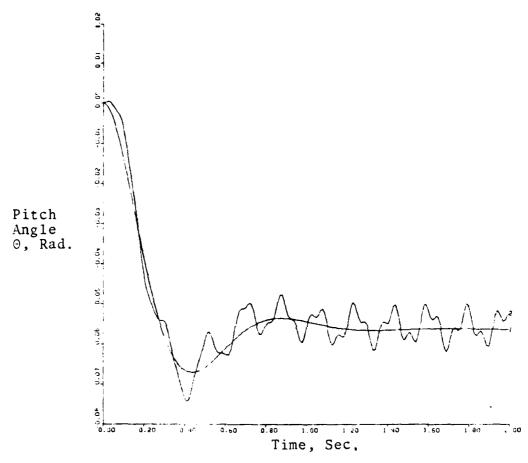


Figure 4-7 Frequency Detector Output for Fixed 7 and 9 Hz Bending Modes

were fixed and only separated by 2.0 hertz. The system response is very close to the nominal plant with some evidence of both bending modes present in the output. The cross channel leakage can be seen to cause oscillations in both of the frequency detectors.

Figures 4-8 and 4-9 show the response of the system to a 0.1 radian step input with the bending modes separated by 7.5 hertz. The lower frequency bending mode is at 5.5 hertz or 0.5 hertz above the lower limit to which the algorithm is allowed to track and the upper frequency bending mode is 14.0 hertz. The upper bending mode frequency is outside of the passband for the high channel frequency detector but within the 15.0 hertz that the high channel is allowed to track a bending mode. The performance of the system is marginal at best. This simulation clearly illustrates the inability of the algorithm to reliably acquire or track a bending mode higher than 12.0 hertz. The problem is not accentuated by the bandpass filter in the high channel attenuating frequencies above 12.0 hertz. Increasing the bandwidth of the high channel to 15.0 hertz did not enhance the ability of the algorithm to reliably identify a frequency above 12.0 hertz.

Figures 4-10 and 4-11 show the system response for a 0.1 radian step input with dynamic, converging bending mode frequencies. The high frequency bending mode starts at 12.0 hertz and decreases at 1.5 hertz per second to 9.0 hertz.



System: Third order missile model with fixed bending modes at 5.5 and 14.0 Hz

Input: 0.1 radian step command

Line 1 is the nominal missile response without bending modes

Line 2 is the missile response with bending modes  $% \left( 1\right) =\left( 1\right) \left( 1\right) \left($ 

Figure 4-8 Missile Response with Fixed 5.5 and 14.0 Hz Bending Modes

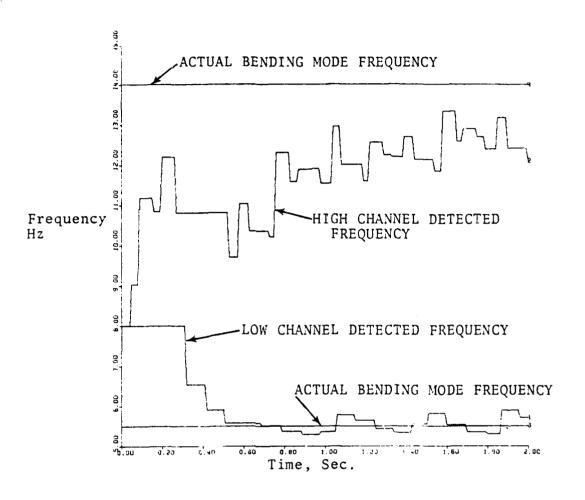
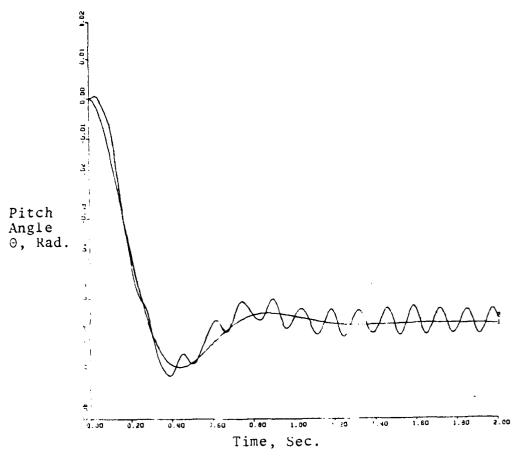


Figure 4-9 Frequency Detector Output for Fixed 5.5 and 14.0 Hz Bending Modes



System: Third order missile mode with converging dynamic bending modes

Input: 0.1 radian step command

Line 1 is the nominal missile response without bending modes

Line 2 is the missile response with bending modes

Figure 4-10 Missile Step Response with Converging Dynamic Bending Modes

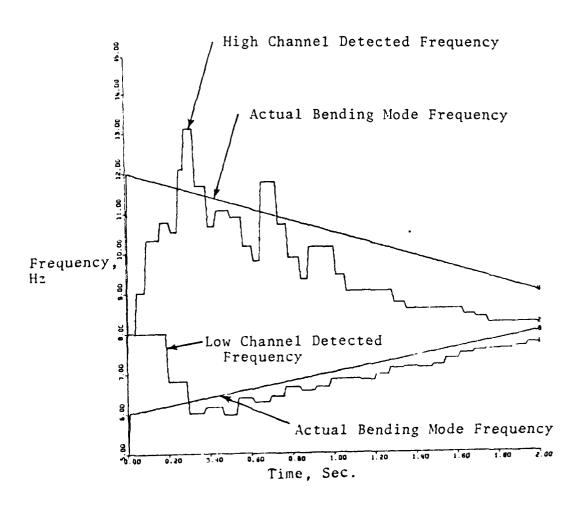
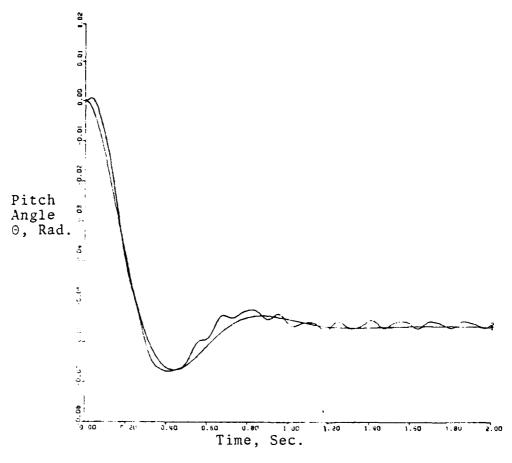


Figure 4-11 Frequency Detector Output for Converging Dynamic Bending Modes

The low frequency bending mode starts at 6.0 hertz and increases at 1.0 hertz per second to 8.0 hertz. The ability of the adaptive digital notch filters to stabilize the system with such high rates of change was not expected. When higher rates of change were simulated for the converging case, the error in the high frequency estimate became so poor that the system became unstable at the frequency of the high bending mode. A rate of 1.5 hertz per second is felt to be the limit on the rate of change of either bending mode frequency.

Figures 4-12 and 4-13 show the system response to a 0.1 radian step input with dynamic diverging bending mode frequencies. The upper bending mode frequency starts at 9.0 hertz and increases at the rate of 1.5 hertz per second to 12.0 hertz. The lower frequency bending mode starts at 8.0 hertz and decreases at the rate of 1.0 hertz per second to 6.0 hertz. The very good performance of the system is probably due to the notch filters being initialized at 8.0 hertz. The inability of the high channel to track a bending mode frequency greater than 12.0 hertz is evident as the high bending mode frequency increases.



System: Third order missile model with diverging dynamic bending modes

Input: 0.1 radian step command

Line 1 is the nominal missile response without bending modes

Line 2 is the missile response with bending modes

Figure 4-12 Missile Step Response with Diverging Dynamic Bending Modes

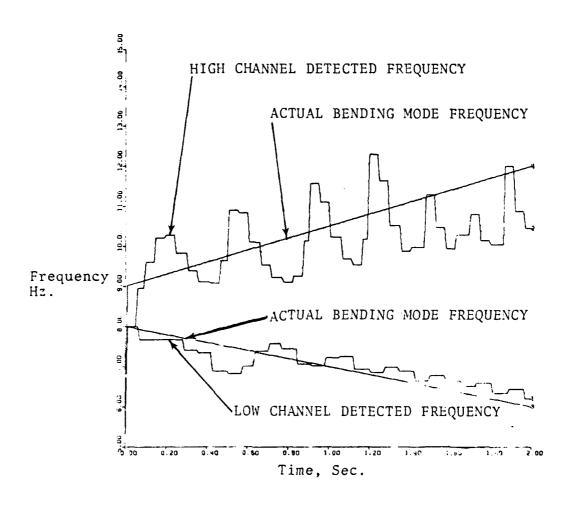


Figure 4-13 Frequency Detector Output for Diverging Dynamic Bending Modes

## V. CONCLUSIONS AND RECOMMENDATIONS

## A. CONCLUSIONS

The feasibility of implementing an adaptive digital notch filter to stabilize the Trident Missile Control System when two dynamic bending modes are present has been demonstrated. The conditions simulated in Chapter Four represent the worst case conditions and the performance of the algorithm under these conditions was satisfactory considering the very desirable response to less violent and more likely commands as shown in Figure 4-4.

The algorithms used in the simulation studies contained in Chapter Four were developed with the ability to implement them in a microprocessor program as a primary concern. Simplicity of the algorithm was maintained, perhaps at the expense of performance, to ensure that the algorithm could be implemented on a microprocessor for subsequent real-time studies. The time varying, nonlinear characteristics of the system when the adaptive digital notch filters are tracking dynamic bending modes with varying input commands deny an analytical approach and therefore require extensive simulation to optimize the algorithm.

## B. RECOMMENDATIONS FOR FURTHER STUDIES

The simplicity of the digital bandpass filters allows an excessive amount of out of band interference. The performance of the bandpass filters could be significantly improved without an appreciable increase in the order of the filters by using more sophisticated types of filters such as a Chebyshev or an elliptical filter. The temptation to enhance the performance of the bandpass filter in nonreal-time simulations without considering the implementation problem on a microprocessor must be resisted.

The direct realization of the bandpass and notch digital filters did not minimize memory, noise due to finite precision coefficients or the number of multiplications required for each output. The structure of the filters needs to be examined with a specific microprocessor's capabilities considered. The ZILOG Z-8000 microprocessor capabilities were considered during the development of the algorithm as a current state-of-the-art microprocessor.

The algorithm must be evaluated on the six degree of freedom model of the Trident Missile available at Lockheed Missile and Space Company, Sunnyvale, California. The results of the simulation studies contained in Chapter Four are only as valid as the assumptions made in modeling the bending modes and in simplifying the plant. It must be emphasized that the algorithm contained in this thesis will not perform satisfactorily with the bending mode frequencies

present in the current Trident Missile. The algorithm in this thesis was designed to identify, track and attenuate bending modes that are a full octave below those of the current Trident Missile.

A phaselock loop scheme should be reconsidered as a frequency detector. The phaselock loop has precisely the desired characteristic of seeking out and locking onto a frequency within its predetermined acquisition range and seems ideally suited for the task of i intifying and tracking the bending mode frequencies. It is recommended that future studies of the application of phaselock loops in this application use actual phaselock loops rather than computer simulation due to the inability to properly simulate the non linear behavior of the phaselock loop with algorithms known to the author. The feasibility of prefiltering the input to the phaselock loop with a bandpass filter to attenuate out of track range signals and thereby reduce the lockon time should be considered.

PROGRAM 2-3

ASSOCIATED FIGURE 2-3

// EXEC DSL

TITLE PLANT RESPONSE WITHOUT BENDING MODES TITLE TO A STEP INPUT.

PROGRAM CONTROL PARAMETERS

INTGER NPLOT

PLANT PARAMETERS

### PARAM MALFA=28.625
PARAM MDELTA=24.17
PARAM ZALFA=180.0
PARAM ZDELTA=113.75
PARAM VEL=2500.0
PARAM KTHETA=1.48
PARAM RRTHET=0.2

DER I VATIVE

MODEL OF THE THIRD ORDER SYSTEM

PE=PC+PO GAMA=PE+P8 PI=GAMA\*KTHETA

```
S
```

```
TERMINAL
CONTRL FINTIM=2.0 , DELT=0.01, DELS=0.01
PRINT 0.01.P3.PC
END
STUP
//C.SYSPRINT DD DSN=, SYSOUT=A
//PLOIT.STEPLIB DD DSN=C0044.Q,UNIT=3330,VOL=SER=DISKO2,DISP=SHR
CPLOIT.STEPLIB DD &
CPLOIT.SYSIN DD &
CPLOIT.SYSIN DD &
CPLOIT.SYSIN DD &
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      10.0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      10.0
                                                                                                                                                                                                                                         PROGRAM CONTROL AND PLOTTER CONTROL
                                                                                                                                                                                                                                                                                            SAMPLE CALL DRWG(1,1,TIME,PD)
TERMINAL
P2=MDELTA*P1
P3=-P2-MA
MA=MALFA*ALFA
P5=PR-P4-P6
P6=ZALFA*ALFA/VEL
P7=PR
P8=KRTHET*P7
P9=INTGRL(0.0,PR)
P0=P9
PR=INTGRL(0.0,P3)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      -0.08
```

PROGRAM 2-4

ASSOCIATED FIGURE 2-4

// EXEC DSL // DSL INPUT DD \*

TITLE PLANT RESPONSE WITHOUT BENDING MODES ITTLE TO A RAMP INPJF.

PROGRAM CONTROL PARAMETERS

INTGER NPLOT

PLANT PARAMETERS

DYNAMIC \* PC=RAMP(.0) PC=0.05\*PC

DERIVATIVE \* \*

```
SAMPLE
CALL DRWG(1,1,TIME,PO)
TERMINAL
CONTRL FINTIM=2.0, DELT=0.01, DELS=0.01
CONTRL FINTIM=2.0, DELT=0.01, DELS=0.01
RI O.01,PO,PC
END
STOP
//C. SYSPRINT OD DSN=,SYSOUT=A
//PLOT-STEPLIB DD DSN=C0044.Q,UNIT=3330,VOL=SER=DISK02,DISP=SHR
//PLOT-STEPLIB DD &*
CPLOT-SYSIN DD **
CPLOT-SYSIN DD **
                                                                                                                                                                                                                                                                                                                PROGRAM CONTROL AND PLOTTER CONTROL
OF THE THIRD DRDER SYSTEM
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   10.0
                                           PE=PC+PO
GAMA=PE+P8
P1=GAMA*KTHETA
P2=MDELTA*PI
P3=-P2-MA
MA=ZDELTA*PI/VEL
P5=PR-P4-P6
P6=ZALFA*ALFA
P6=ZALFA*ALFA
P6=ZALFA*ALFA/VEL
P7=PR
P9=INTGRL(0.0,PR)
P0=P9
PR=INTGRL(0.0,PR)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   -0.08
 MODEL
```

PROGRAM 2-10 ASSOCIATED FIGURE 2-10

// EXEC DSL //DSL.INPUT OD \* PROGRAM CONTROL PARAMETERS

INTGER NPLOT

COMMON/CAREA/S, D, N, G, H, BL, BH, P, T COMMON/CAREA/S, D, N, G, H, BL, BH, P, T IITLE OPEN LOOP FREQUENCY RESPONSE OF THE PLANT

SYSTEM PARAMETERS

127

```
BL=(GAINL*BWL/PSI)/(S**2+BWL*S+WL**2)
BH=(GAINH*BWH/PSI)/(S**2+BWH*S+WH**2)
P=(-MD*S+(ZD*MA/V-ZA*MD/V))/(S*(S**2+ZA/V*S+MA))
G=P
MAG=CABS(G)
MDB=20.*ALOGIO(MAG)
                                                                                                                                                                                                                                                                                                                                     8.0
                                                                                                                                                                                        PROGRAM AND PLOTTER CONTROL
                                                                                                       SYSTEM DYNAMICS
                                                                   M=RAMP(0.0)+1
H2=W/6.28
S=CMPLX(0.0.W)
                      DBZER0=0.0
                                        #
DYNAMIC
#
INITIAL
```

PROGRAM 2-11 ASSOCIATED FIGURE 2-11

// EXEC DSL

PROGRAM CONTROL PARAMETERS

INTGER NPLOT

COMPLEX S,D,N,G,H,BL,BH,P,T COMMON/CAREA/S,D,N,G,H,BL,8H,P,T TITLE OPEN L3OP FREQUENCY RESPONSE OF LOW FREQUENCY IITLE BENDING MODE.

SYSTEM PARAMETERS

PARAM GAINL=240 PARAM GAINL=240 PARAM PSI=26.0 PARAM MA=28.625 PARAM ZA=28.625 PARAM ZD=113.75 PARAM KT=1.48 PARAM KT=6.2 PARAM MH=62.83

129

```
SAMPLE
CALL DRWG(1,1,W/6.28,MDB)
TERMINAL
CONTRL FINTIM=99.0,DELT=0.1,DELS=0.1
PRI NT 0.1,W,HZ,MDB
STOP
STOP
CALL B DD DSN=,SYSDUT=A
//C.SYSPRINT DD DSN=,SYSDUT=A
//C.SYSPRINT DD SN=,SYSDUT=A
//C.SYSPRINT DD SN=,SYSDUT=A
//C.SYSPRINT DD SN=,SYSDUT=A
//C.SYSPRINT DD DSN=,SYSDUT=A
//C.SYSPRINT DD DSN=,SYSDUT=A
//C.SYSPRINT DD SN=,SYSDUT=A
//C.SYSPRINT DD SN=,SYSDUT=A
//C.SYSPRINT DD SN=,SYSDUT=A
//C.SYSPRINT DD SN=,SYSDUT=A
//PLOT SYSIN DD #
C.P.DI SCALE=0.55 & END
                                                                                                                                                                                                                                                                                                                                  BL=(GAINL#BWL/PSI)/(S**2+BWL*S+WL**2)
BH=(GAINH*BWH/PSI)/(S**2+BWH*S+WH**2)
P=(-MD*S+(ZD*MA/V-ZA*MD/V))/(S*(S**2+ZA/V*S+MA))
T=(P+PSI*(BL+BH))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          8.0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               PROGRAM CONTROL AND PLOTTER CONTROL
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            10.0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            -30.0
                                                                                                                                                                                                                                                                                                                                                                                                                                 G=BL
MAG=CABS(G)
MDB=20.*ALGG13(MAG)
                                                                                                                                                                                                                                                                          SYSTEM DYNAMICS
                                                                                                                                                                          W=RAMP(0.0)+1
H2=W/6.28
S=CMPLX(0.0,W)
                                                        DBZER0=0.0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          2.0
                                                                                                    DYNAMIC
**
INITIAL
```

PROGRAM 2-12 ASSOCIATED FIGURE 2-12

// EXEC DSL //DSL.INPUT DD \* PROGRAM CONTROL PARAMETERS

INTGER NPLOT CONST NPLOT=1 COMMON/CAREA/S,D,N,G,H,BL,BH,P,T COMMON/CAREA/S,D,N,G,H,BL,BH,P,T TLE OPEN LOOP FREQUENCY RESPONSE OF THE PLANT TLE WITH LOW BENDING MODE ADDED

SYSTEM PARAMETERS

#
PARAM GAINI=240.0
PARAM GAINI=240.0
PARAM PSI=0.06
PARAM MD=28.07
PARAM ZA=180.0
PARAM ZA=180.0
PARAM X = 180.0
PARAM X = 180.0
PARAM X = 180.0
PARAM KT=0.2
PARAM KT=0.2
PARAM WH=62.83
PARAM WH=62.83

NITIAL

```
CALL DRWG(1,1,W/6.28,MDB)
CALL DRWG(1,2,W/6.28,DBZERO)
TERMINAL
CALL ENDRW(NPLOT)
CALL ENDRW(NPLOT)
CALL ENDRW(NPLOT)
CONTRL FINTIM=99.0, DELT=0.1, DELS=0.1
PRINT 0.1,W,HZ,MDB
STOP
//C.SYSPRINT DD DSN=,SYSOUT=A
//PLOT. STEPLIB DD DSN=C0044.Q,UNIT=3330,VOL=SER=DISKO2,DISP=SHR
//PLOT. PLOTPARM DD *
CPLOT SCALE=0.55 CEND
//PLOT. SYSIN DD *
                                                                                                                                                                                                                                         BL=(GAINL*BWL/PSI)/(S**2+BWL*S+WL*#2)
BH=(GAINH*BWH/PSI)/(S**2+BWH*S+WH**2)
P=(-MD*S+(20*MA/V-ZA*MD/V))/(S*(S**2+ZA/V*S+MA))
T=(P+PSI*(BL+BH))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      7.0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      8.0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        10.0
                                                                                                                                                                                                                                                                                                                                                                                                                     PROGRAM AND PLOTTER CONTROL
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        -30.0
                                                                                                                                                                                                                                                                                                                                G=P+PSI #BL
MAG=CABS(G)
MDB=20.*ALOGIO(MAG)
                                                                                                                                                                                         SYSTEM DYNAMICS
                                                                                                     W=RAMP(0.0)+1
HZ=W/6.28
S=CMPLX(0.0,W)
DBZER0=0.0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      2.0
                                                  DYNAMIC
*
                                                                                                                                                                                                                                                                                                                                                                                                                                                                       SAMPLE
```

2-13 PROGRAM

2-13 ASSOCIATED FIGURE // EXEC DSL // DSL.INPUT DD #

PROGRAM CONTROL PARAMETERS

INTGER NPLUT

COMPLEX 5,0,N,G,H,BL,BH,P,T COMMON/CAREA/S,D,N,G,H,BL,BH,P,T

ITLE OPEN LOOP FREQUENCY RESPONSE OF HIGH FREQUENCY ITLE BENDING MODE.

SYSTEM PARAMETERS

GAINL=240.0 GAINH=20.0 PSI=0.06 MD=24.17 MA=28.625 ZA=113.75 ZD=113.75 V=2500.0 KRT=0.2 ML=37.7 BWL=0.1

133

```
Ŋ
```

```
SAMPLE

CALL DRWG(1,1,W/6.28,MDB)

TERMINAL

CALL ENDRW(NPLDT)

CONTRL FINTIM =99.0.0ELT=0.1.DELS=0.1

PRINT 0.1.W.HZ.MDB

FROD

STOP

STO
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     BL=(GAINL*BWL/PSI)/(S**2+BWL*S+WL**2)
BH=(GAINH*BWH/PSI)/(S**2+BWH*S+WH**2)
P=(-MD*S+(ZD*MA/V-ZA*MD/V))/(S*(S**2+ZA/V*S+MA))
T=(P+PSI*(BL+BH))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                7.0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                8.0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           PROGRAM CONTROL AND PLOTTER CONTROL
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      10.0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                -30.0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                G=BH
MAG=CABS(G)
MDB=20.*ALGG13(MAG)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               SYSTEM DYNAMICS
                                                                                                                                                                                                                                                                                                                                               W=RAMP(0.0)+1
HZ=W/6.28
S=CMPLX(0.0,W)
DBZER0=0.0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                2.0
                                                                                                                           DYNAMIC
**
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      0.0
```

PROGRAM 2-14 ASSOCIATED FIGURE

// EXEC DSL // DSL. INPUT DD \*

PROGRAM CONTROL PARAMETERS

INTGER NPLOT

TITLE OPEN LOOP FREQUENCY RESPONSE OF THE PLANT COMPLEX S,D,N,G,H,BL,BH,P,T COMMON/CAREA/S,D,N,G,H,5L,BH,P,T

SYSTEM PARAMETERS

GAINL=240.0 GAINH=20.0 GAINH=20.0 MA=28.05 I MA=28.625 I MA=28.625 I MA=28.625 I MA=28.625 I MA=28.625 I MA=28.625 I MA=25.00.0 I KT=1.48 WL=37.7 WL=37.7 WH=62.83 BWL=0.1

```
S
```

```
//C. SYSPRINT DD DSN=,SYSOUT=A
//PLOT.STEPLIB DD DSN=C0044.Q,UNIT=3330,VOL=SER=DISKO2,DISP=SHR
//PLOT.PLOTPARM DD #
EPLOT SCALE=0.55 &END
//PLOT.SYSIN DD *
                                                                                                                                                                                                           BL=(GAINL*BWL/PSI)/(S#2+BWL*S+WL*#2)
BH=(GAINH*BWH/PSI)/(S#2+BWH*S+WH*#2)
P=(-MD#S+(ZU#MA/V-ZA*MD/VI)/(S#(S#*2+ZA/V*S+MA))
T=(P+PSI*(BL+BH))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     7.0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      8.0
                                                                                                                                                                                                                                                                                                                                                                                CALL DRWG(1,1,W/6.28,MDB)
CALL DRWG(1,2,W/6.28,DBZERD)
TERMINAL
CALL ENDRW(NPLOT)
CONTRL FINTIM=99.0,DELT=0.1,DELS=0.1
END
SŢOP
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      10.0
                                                                                                                                                                                                                                                                                                                                                               PROGRAM AND PLOTTER CONTROL
                                                                                                                                                                                                                                                                                     G=P+PSI *BH
MAG=CABS(G)
MDB=20. *ALOG13(MAG)
                                                                                                                                                                 SYSTEM DYNAMICS
                                                                                       W=RAMP(0.0)+1
HZ=W/6.28
S=CMPLX(0.0,W)
DBZER0=0.0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     2.0
                                           DYNAMIC
*
```

PROGRAM 2-15 ASSOCIATED FIGURE 2-15

// EXEC DSL //DSL.INPUT DD \* PROGRAM CONTROL PARAMETERS

INTGER NPLOT

COMPLEX S,D,N,G,H,BL,BH,P,T COMMON/CAREA/S,D,N,G,H,BL,BH,P,T TITLE OPEN LOOP FREQUENCY RESPONSE OF THE PLANT ITTLE WITH BOTH HIGH AND LOW FREQUENCY BENDING MODES.

SYSTEM PARAMETERS

\* Param Gainl=240.0 Param Gainh=20.0 Param Psi=0.06 Param md=24.17

PARAMI PA

14 T T T

```
TERMINAL
CALL ENDRW(NPLOT)
CONTRL FINTIM=99.0,00ELT=0.1,0ELS=0.1
PRINT 0.1,W,HZ,MDB
END
STOP
//C.SYSPRINT DD DSN=,SYSDUT=A
//PLOT.STEPLIB DD DSN=C0044.0,UNIT=3330,VOL=SER=DISKO2,DISP=SHR
//PLOT.PLOTPARM DD *
EPLOT SCALE=0.55 & END
//PLOT.SYSIN DD **
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         (S##2+BWL#S+WL##2)
(S##2+BMH#S+WH##2)
A*MD/V))/(S#(S##2+ZA/V#S+MA))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            7.0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            8.0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            10.0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       CALL DRWG(1,1,W/6.28,MDB)
CALL DRWG(1,2,W/6.28,DBZERO)
TERMINAL
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    PROGRAM AND PLOTTER CONTROL
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    BL=(GAINL*BML/PSI)/(SBH=(GAINH*BWH/PSI)/(SP=(-MD*S+(2D*MA/V-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*(BL+BH))-ZA*T=(P+PS[*
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            -30.0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              MAG=CABS(G)
MDB=20.*ALGG10(MAG)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            SYSTEM DYNAMICS
                                                                                                                                                                                       W=RAMP(0.0)+1
HZ=W/6.28
S=CMPLX(0.0,W)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 2.0
DYNAMIC
*
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            SAMPLE
```

D82ER0=0.0

PROGRAM 2-17 ASSOCIATED FIGURES 2-17 2-18

// EXEC DSL //DSL.INPUT DD \* TITLE PLANT CONTAMINATED WITH TWO TITLE BENDING MODES CENTERED AT 10 HZ. TITLE AND 6.0 HZ. STEP INPUT=0.1 RAD. TITLE NO DIGITAL FILTER

PROGRAM CONTROL PARAMETERS

\* INTGER NPLOT CONST NPLOT=1 SYSTEM PARAMETERS

PARAM PSIGA=0.06 PARAM PSIRG=0.06 PARAM MALFA=28.625 PARAM ZALFA=180.0 PARAM ZALFA=1130.0 PARAM VEL=2500.0 PARAM VEL=2500.0 PARAM ZETABH=1.19 PARAM WBL=37.7 PARAM ZETABE=0.1 PARAM KTHETA=1.48

INPUT COMMAND

PARAM PC=0.1

DER I VAT I VE \*

MODEL OF THE THIRD ORDER PLANT WITH BENDING MODE

PE=PC+PO GAMA=PE+PB P1=GAMA=KTHETA P2=MDELTA\*PI P3=-P2-MA MA=HALFA\*PI P5=PR-P4-P6 P6=ZALFA\*ALFA/VEL P7=PR+PII P8=KRIHET\*P7 P9=INTGRL(0.0.PR) P10=P5+IG\*BO P10=P5+IG\*BO P10=P5+IG\*BO P10=P5+IG\*BO P10=P5+IG\*BO P1=P5IG\*BO P1=P5IG\*BO NARROW BAND MODEL OF LOW BAND BENDING MODE

BL1=GAI NL/PSIGA\*P1 BL2=ZETABL\*BL1 BL3=BL2-ZETABL\*BL4-BL5\*WBL\*\*2.0 BL4=INTGRL(0.0,BL3) BL5=INTGRL(0.0,BL4) NARROW BAND MODEL OF HIGH BAND PASS BENDING MODE

BH1=GAINH/PSI3A\*P1 BH2=ZETABH\*BH1 BH3=BH2-ZETABH\*BH4-BH5\*WBH\*\*2.0

```
10.0
                                                        MODEL OF THE PLANT WITHOUT BENDING MODES TO ESTABLISH NOMINAL PERFORMANCE.
                                                                                                                                                                                                                                                                                                                                                                                                                              10.0
                                                                                                                                                                                                                                                                                                                                                                                                                                                           10.0
                                                                                                                                                                                                                         AND PLOTTER CONTROL
                                                                                                                                                                                                                                                                                                                                                                                                                              0.01
                                                                                             P21=PC+P27
P22=P21+P31
P23=KTHETA*P22
P24=MDELTA*P23
P25=-P24-MALFA*P30
P26=INTGRL(0.0, P25)
P27=INTGRL(0.0, P26)
P29=-P28-ZALFA/VEL*P330
P30=INTGRL(0.0, P29)
P31=KRTHET*P26
                                                                                                                                                                                                                                                              CALL DRWG(1,1,TIME,P27)
CALL DRWG(1,2,TIME,P0)
CALL DRWG(2,1,TIME,P0)
BH4=INTGRL(0.0,8H3)
BH5=INTGRL(0.0,BH4)
BR=BH4+BL4
BO=BH5+BL5
                                                                                                                                                                                                                                                                                                                                                                                                                             -0.08
                                                                                                                                                                                                                        PROGRAM CONTROL
                                                                                                                                                                                                                                                                                                                                                                                                                              0.2
                                                                                                                                                                                                                                                                                                                                                                                                                                                          0.2
                                                                                                                                                                                                                                                     SAMPLE
                                                                                                                                                                                                                                                                                                                                                                                                                              0.0
                                                                                                                                                                                                                                                                                                                                                                                                                                                          0.0
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PROGRAM 2-19

ASSOCIATED FIGURES 2-19

// EXEC DSL //DSL.INPUT DD \*

PLANT CONTAMINATED WITH ONE BENDING MODE CENTERED AT 10 HZ. STEP INPUT=0.1 RAD. NO DIGITAL FILTER 1111E 1111E 1111E

PROGRAM CONTROL PARAMETERS

INTGER NPLOT

SYSTEM PARAMETERS

PSIGA=0.06
PSIRG=0.06
MALFA=28.625
ADELTA=180.0
ZDELTA=180.0
ZDELTA=180.0
WBH=62.83
ZETABH=1.9
ZETABH=1.9
ZETABH=0.0
WBL=37.7
ZETABL=0.0
WBL=37.7
ZETABL=0.0

INPUT COMMAND

PARAM PC=0.1

ĎER I VAT I VE \* MODEL OF THE THIRD ORDER PLANT

NARROW BAND MODEL OF LOW BAND BENDING MODE

BL1=GAINL/PSIGA\*P1 BL2=ZETABL\*BL1 BL3=BL2-ZETABL\*BL4-BL5\*WBL\*\*2.0 BL4=INTGRL{0.0,BL3} BL5=INTGRL{0.0,BL4} NARROW BAND MODEL OF HIGH BAND BENDING MODE

BH1=GAINH/PSIGA\*P1 BH2=ZETABH\*BH1 BH3=BH2-ZETABH\*BH4-BH5\*WBH\*\*2.0

	G MODES				-1	570P //C.SYSPRINT DD DSN=,SYSQUT=A //PLOT.STEPLIB DD DSN=C0044.Q,UNIT=3330,VOL=SER=DISKO2,DISP=SHR //PLOT.PLOTPARM DD * &PLOT SCALE=0.45 &END //PLOT.SYSIN DD *	10.0 10.0	10.0
	PLANT WITHOUT BENDING NOMINAL PERFORMANCE .	P30+P26	CONTROL	P27) P0) P0)	0.01, DELS≈0.0	UT=A 44.Q.UNIT=3330	0.01	
8H4=INTGRL(0.0,8H3) 8H5=INTGRL(0.0,8H4) 8R=8H4+8L4 8O=8H5+8L5	MODEL OF THE PLANT TO ESTABLISH NOMINA	P21=PC+P27 P22=P21+P31 P23=KTHETA*P22 P24=MDELTA*P23 P25=-P24-MALFA*P30 P26=INTGRL(0.0, P25) P27=INTGRL(0.0, P25) P29=-P28-ZALFA/VEL*P30+P26 P30=INTGRL(0.0, P29) P30=INTGRL(0.0, P29)	PROGRAM AND PLOTTER CONTROL	)RWG(1,1,TIME,P27) )RWG(1,2,TIME,P0) )RWG(2,1,TIME,P0)	CALL ENDRW(NPLOT) CONTRL FINTIM=2.0, DELT=0.01, D INTEG RKSFX PRINT 0.01,PD,BR	DO DSN=+SYSO   18 DD DSN=C00   28 M DD #   50 45 EEND	.2 -0.08	2
6H4=IN 6H5=IN 8R=6H4 80=8H5	* MODEL * TO EST		*** PROGRA	SAMPLE CALL OCALL DCALL	CONTRE FINITE INTEGRASSIVE	STOP //C.SYSPRINT //PLOT.STEPL //PLOT.PLOTP &PLOT.SYSIN	0.0 0.2	0.0

PROGRAM 2-21 ASSOCIATED FIGURES 2-21

// EXEC DSL //DSL.INPUT DD \*

PLANT CONTAMINATED WITH ONE BENDING MODE CENTERED AT 6 HZ. STEP INPUT=0.1 RAD. NO DIGITAL FILTER 7117 7176 7176 7176

PROGRAM CONTROL PARAMETERS

INTGER NPLOT CONST NPLOT=1

SYSTEM PARAMETERS

PSIGA=0.06 PSIRG=0.06 MALFA=28.625 ADELTA=180.0 ZDELTA=113.75 VEL=2500.0 WBH=62.83 ZETABH=1.19 GAINH=0.0 GAINH=0.0 KTHETA=1.48 KTHETA=1.48

145

INPUT COMMAND

PARAM PC=0.1

DERIVATIVE \*

OF THE THIRD ORDER PLANT MODEL

PE=PC+PO GAMA=PE+PB P1=GAMA\*KTHETA P2=MDELTA\*PI P3=-P2-MA MA=MALFA\*ALFA P5=PR-P4-P6 P5=PR-P1 P6=ZALFA\*ALFA P6=ZALFA\*ALFA P6=ZALFA\*ALFA P6=ZALFA\*ALFA P6=ZALFA\*ALFA P7=PR+P11 P8=KRTHET\*P7 P9=INTGRL(0.0,PR) P10=PSIGA\*BR P11=PSIGA\*BR

NARROW BAND MODEL OF LOW BAND BENDING MODE

BL1=GAI NL/PSIGA\*P1 BL2=ZETABL\*BL1 BL3=BL2-ZETABL\*BL4-BL5\*WBL\*\*2.0 BL4=INTGRL(0.0, BL3) BL5=INTGRL(0.0, BL4)

NARROW BAND MODEL OF HIGH BAND BENDING MODE

BH1=GAI NH/P SIGA\*P1 BH2=ZET ABH\*BH1

```
TERMINAL
CALL ENDRWINPLOT)
CONTRL FINTIM=2.0 , DELT=0.01, DELS=0.01
INTEG RKSFX
PRI NT 0.01,PD.BR
END
STOP
//C SYSPRINT DD DSN=,SYSOUT=A
//PLOT-STEPLIB DD DSN=C0044.Q,UNIT=3330,VOL=SER=DISK02,DISP=SHR
//PLOT-STEPLIB DD **
EPLOT SCALE=0.45 EEND
//PLOT-SYSIN DD **
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        10.0
                                                                                                                    PLANT WITHOUT BENDING MODES
NOMINAL PERFORMANCE .
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         10.0
BH3=BH2-ZETABH*BH4-BH5*WBH**2.0
BH4=INTGRL(0.0, BH3)
BH5=INTGRL(0.0, BH4)
BR=BH4+BL4
BO=BH5+BL5
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        0.01
                                                                                                                                                                                      P21=PC+P27
P22=P21+P31
P23=KTHETA*P22
P24=MDELTA*P23
P25=-P24-MALFA*P30
P26=INTGRL(0.0,P25)
P27=INTGRL(0.0,P25)
P28=-D28-ZALFA/VEL*P30+P26
P30=INTGRL(0.0,P29)
P31=KRTHET*P26
                                                                                                                                                                                                                                                                                                                                                                                                              PROGRAM AND PLOTTER CONTROL
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                CALL DRWG(1,1,TIME,P27)
CALL DRWG(1,2,TIME,P0)
CALL DRWG(2,1,TIME,P0)
                                                                                                                      MODEL OF THE
TO ESTABLISH
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   TERMINA
                                                                                                                                                                                                                                                                                                                                                                                                                                                                SAMPLE
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0.01

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2-23 PROGRAM 2-23 ASSOCIATED FIGURE

// EXEC DSL // DSL. INPUT DD \*

TITLE PLANT CONTAMINATED WITH TWO TITLE BENDING MODES CENTERED AT 10 HZ. TITLE AND 6.0 HZ. RAMP INPUT = 0.05\*TIME.

PROGRAM CONTROL PARAMETERS

INTGER NPLOT

SYSTEM PARAMETERS

PSIGA=0.06 PSIRG=0.06 MALFA=28.625 ADELTA=180.0 2DELTA=113.75 VEL=2500.0 WBH=62.83 ZETABH=1.19 CAINH=27.0 WBL=37.7 ZETABL=0.1 GAINL=240.0 KTHETA=1.48

DYNAMIC \* INPUT COMMAND

PC=0.05\*TIME

DERIVATIVE \*

MODEL OF THE THIRD ORDER PLANT WITH BENDING MODE

PE=PC+PO GAMA=PE+PB P1=GAMA\*KTHETA P2=MDELTA\*PI P3=-P2-MA M4=MALFA\*ALFA P4=ZDELTA\*PI/VEL P5=PK-P4-P6 P6=ZALFA\*ALFA/PL P6=ZALFA\*ALFA/PL P7=PK+PII P9=INTGRL(0.0,PR) P10=P9+P10 P10=P9+P10 P10=P5IRG\*BD P11=PSIGA\*BR PR=INTGRL(0.0,P3) NARROW BAND MODEL OF LOW BAND BENDING MUDE

BL1=GAINL/PSIGA\*P1 BL2=ZETABL\*BL1 BL3=BL2-ZETABL\*BL4-BL5\*WBL\*\*2.0 BL4=INTGRL(0.0,BL3) BL5=INTGRL(0.0,BL4) NARROW BAND MOJEL OF HIGH BAND PASS BENDING MODE

BHI=GAINH/PSIGA\*PI

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S
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```
//C.SYSPRINT DD DSN=,SYSQUT=A
//PLQT.STEPLIB DD DSN=C0044.Q,UNIT=3330,VOL=SER=DISKO2,DISP=SHR
//PLQT.PLQTPARM DD *
&PLQT SCALE=0.45 &END
//PLQT.SYSIN DD *
                                                                                                                                MODEL OF THE PLANT WITHOUT BENDING MODES TO ESTABLISH NOMINAL PERFORMANCE.
                                                                                                                                                                                                                                                                                                                                                                                                                         PROGRAM CONTROL AND PLOTTER CONTROL
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    CONTRL ENDRWINPLOT)
CONTRL FINITM=2.0 , DELT=0.01, DELS=0.01
INTEG RKSFX
PRINT 0.01.P0.8R
STOP
BH2=ZETABH*BH1
BH3=BH2-ZETABH*BH4-BH5*WBH**2.0
BH4=INTGRL(0.0,BH3)
BH5=INTGRL(0.0,BH4)
BR=BH4+BL4
BO=BH5+BL5
                                                                                                                                                                                                  P21=PC+P27
P22=P21+P31
P23=KTHETA*P22
P24=MDELTA*P22
P25=-P24-MALFA*P30
P26=INIGRL(0.0,P25)
P27=INIGRL(0.0,P25)
P28=ZDELTA/VEL*P30+P26
P30=INIGRL(0.0,P29)
P30=INIGRL(0.0,P29)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     CALL DRWG(1,1), TIME, P27
CALL DRWG(1,2,TIME, P0)
TERMINAL
                                                                                                                                                                                                                                                                                                                                                                                                                                                                            SAMPLE
```

10

10.0

0.5

0.0

PROGRAM 3-3

ASSOCIATED FIGURE 3-3

// EXEC DSL //DSL.INPUT DD \* PROGRAM CONTROL PARAMETERS

INTGER NPLOT CONST NPLOT=1 TITLE FIRST STAGE OF THE HIGH FREQUENCY BANDPASS
TITLE FREQUENCY DETECTOR FILTER DESIGNED BY USE OF
TITLE THE BILINEAR TRANSFORMATION OF AN ANALOG
TITLE BANDPASS FILTER AND CORRECTING THE FREQUENCY.

ENTER THE SAMPLING INTERVAL T.

PARAM T=0.01

COMPLEX S, Z, N, D, NI, N2, W3, D1, D2, D3, G COMMON/CAREA/S, Z, N, D, NI, N2, N3, D1, D2, D3, G

INITIAL \*

PHI180=-180.0 DBZER0=0.0

\* DYNAMIC \* #=RAMP(0.0)+1.0
HZ=W/6.28
S=CMP(5.28
S=CMP(5.28
S=CMP(5.28)
S=CMP(5.28)
S=CMP(5.28)
S=CMP(5.28)
S=CMP(5.28)
S=CMP(5.28)
N1=CMP(5.28)
N1=N2 N3 CAN BE USED AS SUB-FUNCTIONS OF N2=0.142\*\*2-0.12135\*2+0.0375)\*6.0
N2=0.142\*\*2-0.12135\*2+0.0375)\*6.0
N2=0.142\*\*2-1.3753\*2+.7225
D1=2\*\*2-1.3753\*2+.7225
D2=2\*\*2-1.45625\*2+0.81
D1=2\*\*2-1.45625\*2+0.81

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CONTRL FINITM=99.0, DELT=0.1, DELS=0.1 PRINT 0.1,HZ,MD8,PHI

DRWG(1,1,W/6.28,MDB)
DRWG(1,2,W/6.28,DBZERD)
DRWG(2,1,W/6.28,PHI)
DRWG(2,2,W/6.28,PHI180)

TERMINALL D

\* SAMPLE

PROGRAM AND PLOTTER CONTROL

END \$10P //C.SYSPRINT DD DSN=,SYSOUT=A //PLOT.STEPLIB DD DSN=C0044.Q,UNIT=3330,VOL=SER=DISKO2,DISP=SHR //PLOT.PLOTPARM DD \* &PLOT SCALE=0.55 &END //PLOT.SYSIN DD \* 8.0 8.0 0.0 0.0

PROGRAM 3-5

ASSOCIATED FIGURE 3+5

PROGRAM CONTROL PARAMETERS

INTGER NPLOT

TITLE SECUND STAGE OF THE HIGH FREQUENCY BANDPASS TITLE FREQUENCY DETECTOR FILTER DESIGNED DIRECTLY INTLE ON THE Z-PLANE.

ENTER THE SAMPLING INTERVAL T.

PARAM T=0.01

COMPLEX S, Z, N, D, N1, N2, N3, D1, J2, D3, G COMMON/CAREA/S, Z, N, D, N1, N2, N3, D1, D2, D3, G

INITIAL

PHI180=-180.0 DBZERO=0.0

ĎYNAMIC \*

W=RAMP(0.0)+1.0 HZ=W/6.28 S=CMPLX(0.0.W) Z=CEXP(S#T)

ENTER THE NUMERATOR POLYNOMIAL IN 2. NJ N2. NJ CAN BE USED AS SUB-FUNCTIONS OF THE NUMERATOR.

NI=(0.15\*2\*\*2-0.12135\*2+0.0375)\*3.1 N2=0.1\*2\*\*2-0.1 N=N1

ENTER THE DENOMINATOR PULYNOMIAL IN Z. D1, D2, D3 CAN BE USED AS SUB-FUNCTIONS OF THE DENOMINATOR.

D1=2\*\*2-1.3753\*2+.7225 D2=2\*\*2-1.45625\*2+0.81 D=D1

G=N/D MAG=CABS(G) MDB=20.0\*ALGG10(MAG) RE=REAL(G) IM=AIMAG(G) PHI=57.3\*ATAN2(IM,RE) IF(PHI.6T.0.0) PHI=PHI-360.0

PROGRAM AND PLOTTER CONTROL

CALL DRWG(1,1,W/6.28,MD8)
CALL DRWG(1,2,W/6.28,DBZERO)
CALL DRWG(2,1,W/6.28,PHI)
CALL DRWG(2,2,W/6.28,PHI)
TERMINAL
CALL ENDRW(NPLOT)
CALL ENDRW(NPLOT)
CALL FINIM=99.0, DELT=0.1, DELS=0.1
PRINT 0.1,HZ,MD8,PHI

10

STOP //C.SYSPRINT DD DSN=,SYSQUT=A //PLOT.STEPLIB DD DSN=C0044.Q,UNIT=3330,VOL=SER=DISKO2,DISP=SHR //PLOT.PLOTPARM DD # &PLOT SCALE=0.55 &END //PLOT.SYSIN DD # 8.0 8.0 2.0 0.0 0.0 PROGRAM 3-7

ASSOCIATED FIGURE 3-7

// EXEC DSL

PROGRAM CONTROL PARAMETERS

INTGER NPLOT

TITLE FREQUENCY RESPONSE OF THE HIGH FREQUENCY BANDPASS IITLE FREQUENCY DETECTOR FILTER.

ENTER THE SAMPLING INTERVAL T.

PARAM T=0.01

COMPLEX S, Z, N, D, NI, N2, N3, D1, D2, D3, G COMMON/CAREA/S, Z, N, D, NI, N2, N3, D1, D2, D3, G

INITIAL

HI180=-180.0 BZERO=0.0

\* DYNAMIC \*

W=RAMP (0.0)+1.0

ENTER THE DENDMINATOR POLYNOMIAL IN Z. DI. 02, D3 CAN BE USED AS SUB-FUNCTIONS OF THE DENOMINATOR. ENTER THE NUMERATOR POLYNOMIAL IN Z. NI, N2, N3 CAN BE USED AS SUB-FUNCTIONS THE NUMERATOR. N1=(0.15\*2\*\*2-0.12135\*2+0.0375)\*3.1 N2=0.1\*2\*\*2-0.1 N=N1\*N2 D1=Z\*\*2-1.3753\*Z+.7225 D2=Z\*\*2-1.45625\*Z+0.81 D=D1\*D2 HZ=W/6.28 S=CMPLX(0.0.W) Z=CEXP(S\*T)

PROGRAM AND PLOTTER CONTROL

G=N/D MAG=CABS(G) MDB=20.0\*ALGG10(MAG) RE=REAL(G) IM=AIMAG(G) PHI=57.3\*ATAN2(IM!RE) IF(PHI.GT.0.0)

CALL DRWG(1,1,W/6.28,MDB)
CALL DRWG(1,2,W/6.28,DBZERJ)
CALL DRWG(2,1,W/6.28,PHI)
TERMINAL
CONTRL FINTIM=99.0, DELT=0.1, DELS=0.1
END

//C.SYSPRINT DD DSN=,SYSOUT=A //PLOT.STEPLIB DD DSN=C0044.Q,UNIT=3330,VOL=SER=DISKO2,DISP=SHR //PLOT.PLOTPARM DD \* EPLOT.SCALE=0.55 & END //PLOT.SYSIN DD \* 8.0 8.0 0.0 0.0 PROGRAM 3-8

ASSOCIATED FIGURE 3-8

// EXEC DSL DD \*

PROGRAM CONTROL PARAMETERS

INT GER NPLOT

TITLE FREQUENCY RESPONSE OF THE LOW FREQUENCY BANDPASS ILTLE FREQUENCY DETECTOR FILTER.

ENTER THE SAMPLING INTERVAL T.

PARAM T=0.01

COMPLEX S, Z, N, D, NI, N2, N3, D1, D2, D3, G COMMON/CAREA/S, Z, N, D, NI, N2, N3, D1, D2, D3, G

INITIAL

PHI180=-180.0 DBZERD=0.0

DYNAMIC \*

W=RAMP (0.0)+1.0

ENTER THE DENOMINATOR POLYNOMIAL IN Z. DI. D2. D3 CAN BE USED AS SUB-FUNCTIONS THE DENOMINATOR. ENTER THE NUMERATOR POLYNOMIAL IN Z. NI. N2, N3 CAN BE USED AS SUB-FUNCTIONS THE NUMERATOR. N1=0.15\*Z\*\*2-0.12354\*Z+0.030375 N2=0.1\*Z\*\*2-0.1 N=N1\*N2 G=N/D MAG=CABS(G) MDB=20.0\*ALGG10(MAG) RE=REAL(G) PHI=STAAG(G) PHI=ST3\*ATAN2(IM,RE) IF(PHI.GT.0.0) PHI=PHI-360.0 D1=Z\*\*2-1.7228\*Z+.88604 D2=Z\*\*2-1.64725\*Z+0.81 D=D1\*D2 HZ=W/6.28 S=CMPLX(0.0,W) Z=CEXP(S\*T)

9

9

PROGRAM AND PLOTTER CONTROL

CALL DRWG(1,1,W/6.28,MDB)
CALL DRWG(1,2,W/6.28,DBZERO)
CALL DRWG(2,1,W/6.28,PHI)
CALL DRWG(2,1,W/6.28,PHI)
TERMINAL
CONTRL FINTIM=99.0, DELT=0.1, DELS=0.1
END
STOP

//C.SYSPRINT DD DSN=,SYSGUT=A //PLOT.STEPLIB DD DSN=C0044.Q.UNIT=3330,VUL=SER=DISKO2,DISP=SHR //PLOT.PLOTPARM DD \* EPLOT SCALE=0.55 EEND //PLOT.SYSIN DD \* 8.0 8.0 2.0 0.0

PROGRAM 3-9

ASSOCIATED FIGURE 3-9

// EXEC DSL

PROGRAM CONTROL PARAMETERS

INTGER NPLOT

ITLE FREQUENCY RESPONSE OF THE BOTH BANDPASS

ENTER THE SAMPLING INTERVAL T.

PARAM T=0.01

COMPLEX S, Z,N,NN,D,DD,N1,N2,N3,N4,D1,D2,D3,D4,G,GG COMMON/CAREA/S, Z,N,NN,D,DD,N1,N2,N3,N4,D1,D2,D3,D4,G,GG

INITIAL

DBZER0=0.0

ĎYNAMIC #

W=RAMP(0.0)+1.0 HZ=W/6.28

S=CMPLX(0.0,W) Z=CEXP(S\*T) ENTER THE LOW FREQUENCY BANDPASS FILTER NUMERATOR.

N1=0.15\*2\*\*2-0.12354\*Z+0.030375 N2=0.1\*Z\*\*2-0.1 N=N1\*N2 ENTER THE HIGH FREQUENCY BANDPASS FILTER NUMERATOR.

N3=(0.15\*2\*\*2-0.12135\*Z+0.0375)\*3.1 N4=0.1\*Z\*\*2-0.1 NN=N3\*N4 ENTER THE LOW FREQUENCY BANDPASS FILTER DENOMINATOR.

D1=2\*\*2-1.7228\*2+.88604 D2=Z\*\*2-1.64725\*2+0.81 D=D1\*D2 ENTER THE HIGH FREQUENCY FILTER DENOMINATOR.

03=2\*\*/-1.3753\*2+0.7225 04=2\*\*2-1.45625\*2+0.81 00=03\*04

G=N/D MAG=CABS(G) MDB=20.0\*ALOG10(MAG) GG=NN/DD IMAG=CABS(GG) IMDB=20.0\*ALGGIO(IMAG) PROGRAM AND PLOTTER CONTROL

```
CONTRL FINTIM=99.0, DELT=0.1, DELS=0.1
PRINT 0.1, HZ, MDB, IMDB
END
STOP
//C. SYSPRINT DD DSN=, SYSDUT=A
//PLOT. STEPLIB DD DSN=C0044.0, UNIT=3330, VOL=SER=DISK02, DISP=SHR
EPLOT SCALE=0.55 & END
//PLOT. SYSIN DD *
                                                                                                                                                                                                                                     8.0
           CALL DRWG(1,1,W/6.29,MDB)
CALL DRWG(1,2,W/6.28,DBZERO)
CALL DRWG(1,3,W/6.28,IMDB)
TERMINAL
*
SAMPLE
                                                                                                                                                                                                                                      0.0
```

PROGRAM 3-13 ASSOCIATED FIGURES 3-13 3-14

// EXEC DSL //DSL.INPUT DD \*

PROGRAM CONTROL PARAMETERS

INTGER NPLOT

FITLE FREQUENCY RESPONSE OF A NOTCH FILTER CENTERED FITLE AT 6.0 HZ. WITH A POLE RADIUS OF 0.9.

ENTER THE SAMPLING INTERVAL T.

PARAM T=0.01

COMPLEX S, Z, N, D, N1, N2, N3, D1, D2, D3, G COMMON/CAREA/S, Z, N, D, N1, N2, N3, D1, D2, D3, G

INI TIAL

PHI180=-180.0 DBZER0=0.0

DYNAMIC \*\*

W=RAMP (0.0)+1.0

HZ=W/6.28 S=CMPLX(0.0,W) Z=CEXP(S\*T)

ENTER THE NUMERATOR POLYNOMIAL IN 2. NI, N2, N3 CAN BE USED AS SUB-FUNCTIONS OF THE NUMERATOR.

N=0.9708\*(2\*\*2-1.8595\*2+1.0)

OF. ENTER THE DENDMINATOR POLYNOMIAL IN Z. DI. DZ. D3 CAN BE USED AS SUB-FUNCTIONS THE DENOMINATOR.

D=Z\*\*2-1.6736\*Z+0.81

G=N/D MAG=CABS(G) MUB=20.0\*ALGG10(MAG) RE=REAL(G) RE=REAL(G) PHI=ST.3\*AIAN2(IM, RE) IF(PHI.GI.0.0) PHI=PHI-360.0

PROGRAM AND PLOTTER CONTROL

CALL DRWG(1,1,W/6.28,MDB)
CALL DRWG(1,2,W/6.28,DBZERG)
CALL DRWG(2,1,W/6.28,PHI)
CALL DRWG(2,1,W/6.28,PHI)
CALL DRWG(2,2,W/6.28,PHI)
TERMINAL
CALL ENDRW(NPLDT)
CONTRL FINTIM=99.0, DELT=0.1, DELS=0.1
PRINT 0.1,HZ,MDB,PHI
END
STOP
//C.SYSPRINT DD DSN=,SYSOUT=A
//PLOT.STEPLIB DD DSN=C0044.0,UNIT=3330,VOL=SER=DISKO2,DISP=SHR
//PLOT.PLOTPARM DD \*
CPLOT.SCALE=0.55 & END \* SAMPLE

السر بدرور

10

0 0

//PLOT.SYSIN DD \*
0.0 2.0
0.0 2.0

PROGRAM 3-15 ASSOCIATED FIGURES 3-15 3-16

// EXEC DSL

PROGRAM CONTROL PARAMETERS

INTGER NPLOT CONST NPLOT=1 TITLE FREQUENCY RESPONSE OF A NOTCH FILTER CENTERED ITLE AT 10.0 HZ. WITH A POLE RADIUS OF 0.8.

ENTER THE SAMPLING INTERVAL T.

ARAM T=0.01

COMPLEX S, Z, N, D, N1, N2, N3, D1, D2, D3, G COMMON/CAREA/S, Z, N, D, N1, N2, N3, D1, D2, D3, G

INITIAL

PHI180=-180.0 DBZERO=0.0

DYNAMIC \*

W=RAMP(0.0)+1.0

ENTER THE DENOMINATUR PULYNOMIAL IN Z. DI. 02, D3 CAN BE USED AS SUB-FUNCTIONS OF THE DENOMINATOR. ENTER THE NUMERATOR POLYNOMIAL IN Z. NI. NZ. N3 CAN BE USED AS SUB-FUNCTIONS OF THE NUMERATOR. G=N/D MAG=CABS(G) MDB=20.04LGG10(MAG) RE=REAL(G) IN=AIMAG(G) PHI=57.3\*ATAN2(IM,RE) IF(PHI.6T.0.0) CALL DRWG(1,1,W/6.28,MDB) CALL DRWG(1,2,W/6.28,DBZERO) CALL DRWG(2,1,W/6.28,PHI) CALL DRWG(2,2,W/6.28,PHI) PROGRAM AND PLOTTER CONTROL N=0.9044\*(Z\*\*2-1.618\*Z+1.0) 0=2\*\*2-1.2944\*2+0.64 HZ=W/6.28 S=CMPLX(0.0,W) Z=CEXP(S\*T) SAMPLE

10

8.0

//PLOT.SYSIN DD \*
0.0 2.0
0.0 2.0

PROGRAM

ASSOCIATED FIGURES

3-19 3-20 3-21 3-21

QQ // EXEC DSL TEST OF THE BENDING MODE TRACKING AND FILTERING ALGORITHM. INPUT IS THE SUM OF THREE EQUAL AMPLITUDE SINE WAVES. ONE AT 2 HZ., ONE AT 6 HZ. AND ONE AT 10 HZ.

PROGRAM CONTROL PARAMETERS

CONST NPLOT=1

INITIAL DIGITAL BENDING MODE FILTER PARAMETERS

F1SET=8.0 F2SET=8.0 RADUS1=0.9 RADUS2=0.8 P1=3.14159 ZERO=0.0 

INITIAL

CALCULATE THE BENDING MODE FREQUENCIES IN HERTZ.

LHZ=6.0 HHZ=10.0

DYNAMIC \*

SET THE INITIAL DIGITAL FILTER PARAMETERS

IF(TIME.NE.0.0)60 TO

CALCULATE THE FILTER COEFFICIENTS

RADIUS=RADUSI All, Bll, Bl2, GAIN1=COEFF (FISET, DELT, RADIUS) RADIUS=RADUS2 A21, B21, B22, GAIN2=COEFF (F2SET, DELT, RADIUS) GO TO 100 CONTINUE

GENERATE INPUT SIGNAL COMPOSED SINE WAVES OF EQUAL AMPLITUDE.

**7**H 10

AND

9 2,

OF

F1=SINE(0.0,2.0\*2.0\*PI,0.0) F2=SINE(0.0,6.0\*2.0\*PI,0.0) F3=SINE(0.0,10.0\*2.0\*PI,0.0) FILTIN=F1+F2+F3

DIGITAL BANDPASS FILTER AND FREQUENCY DETECTOR 2H 8 5 10 BLIOUT=0.15\*FILOUT-0.12354\*BL11+0.030375\*BL12+1.7228\*BL21...
-0.88604\*BL22
BL20UT=0.1\*BL10UT-0.1\*BL32+1.64725\*BL41-0.81\*BL42
BL12=BL11
BL2=BL11
BL2=BL21
BL2=BL21
BL2=BL21
BL2=BL21
BL3=BL20UT
BL3=BL30UT
BL3=BL3UOT
BL4=BL41
BL4=BL20UT

COMPUTE THE CENTER FREQUENCY FOR THE LOW FREQUENCY NOTCH.

=CROSS(TIME, BL10UT, 0.0) TC1, EQ.0.0) GO TO 50 H1=FC1-LTINT

COMPUTE THE CENTER FREQUENCY FOR THE HIGH FREQUENCY NOTCH

TC2=CRDSS(TIME, BH2DUT, 0.0)
IF(TC2, Eq. 0.0) GO TO 100
IINT2=TC2-L TINT2
LTINT2=TC2
LTINT2=TC2
IF(TINT2=TC2
IF(TINT2-LT.0.0525) GO TO 100
IF(TINT2-LT.0.033333) GO TO 100
FREQ=1.0/(2.0\*TINT2)

F10UT=F1LTIN+A11\*F111+F112-B11\*F011-B12\*F012 F20UT=F10UT+A21\*F121+F122-B21\*F021-B22\*F022 = 1.0PROGRAM AND PLOTTER CONTROL FILOUT=F20UT\*GAINI\*GAINZ FILZ=F111 FILZ=F111 F012=F011 F011=F10UT F121=F10UT F121=F10UT F022=F021 F022=F021 INME, FILTIN INME, FILCOUT ADJUST OUTPUT FOR DC GAIN SECOND NOTCH FILTER FIRST NOTCH FILTER DRANGG(L)
DRANGG(L)
DRANGG(L)
DRANGG(R)
DRANGG(R) CONTINUE SAMPLE 001

177

	FILTER COEFFICIENTS	(N)					//C.SYSPRINT DD DSN=,SYSOUT=A //PLOT.STEPLIB DD DSN=C0044.Q,UNIT=3330,VOL=SER=DISKO2,DISP=SHR //PLOT.PLOTPARM DD * &PLOT SCALE=0.45 EEND //PLOT.SYSIN DD *				10.0	0.01
<b>.</b>	ш	* FORTRAN SUBROUTINE COEFF(FREQ.DELT,RADIUS,A1,B1,B2,GAIN)	10	ELT)	入上コフ		0 •VOL=SER=D 19	10.0	10.0	10.0	10.0	10.0
TERMINAL CALL ENDRW(NPLOT) CONTRL FINTIM=2.0 , DELT=0.01, DELS=0.01 INTEG RKSFX INTEG RKSFX END STOP	CALCULATE 1	•DELT•RADIUS	FILTER COEFFICIENTS	PI=3.14159 AI=-2.0 *COS (FREQ *2.0 *PI *DELT) BI=-2.0 *RADIUS*COS (FREQ *2.0 *PI *DELT) B2=RADIUS**2.0	C GAIN TO UP	+A1)	=A •Q•UNIT=333				n•1	<b>9.</b> 0
(NPLOT) 0 , DELT=0.( N,FILOUT,FI	FORTRAN SUBROUTINE TO CALCULATE	COEFF ( FREQ	THE FILTER	S (FREQ#2.0# DIUS#COS(FR #2.0	HE FILTER D	81+821/(2.0	D SN= , S Y SOUT D D SN= C 0044 DD * S END				5.0	-2.0
CALL ENDRW CALL ENDRW FINTIM=2. RKSFX 0.01.FILTI	FORTRAN SU	N SUBROUT INE	CALCULATE THE	PI=3.14159 AI=-2.0*CO BI=-2.0*RA B2=RADIUS*	ADJUST T	GAIN= (1.0+ RETURN	FND YSPRINT DD T.STEPLIB D T.SCATERA T.SCALE 0.4	0.2	0.2	0.2	0.2	0.5
TERMIN CONTRI PRINTEG STOP *	***	* FOR TR!	يان	، د	ان	J	1/2 1/2 1/2 1/2 1/2 1/2 1/2 1/2 1/2 1/2	0.0	0.0	0.0	0.0	0.0

4-2 4-2 PROGRAM ASSOCIATED FIGURES

// EXEC DSL //DSL.INPUT DD \*

TITLE \*\*\* 3RD ORDER SYSTEM WITH BENDING MODE
TITLE \*\*\* TWO BENDING MODES CENTERED AT 10.0 HZ AND
TITLE \*\*\* 6.0 HZ.
TITLE \*\*\* DIGITAL FREQUENCY DETECTOR BANDPASS FILTERS.
TITLE \*\*\* DUAL TRACKING DIGITAL FILTERS
TITLE \*\*\* INPUT IS A 0.1 RADIAN SIEP

PROGRAM CONTROL PARAMETERS

INTGER NPLOT

SYSTEM PARAMETERS

PARAM PSIGA=0.06
PARAM MALFA=28.625
PARAM MALFA=28.625
PARAM ZALFA=180.0
PARAM ZALFA=113.75
PARAM VEL=2500.0
PARAM WBH=62.83
PARAM GAINH=20.0
PARAM GAINH=20.0
PARAM ZETABH=1.19
PARAM ZETABH=1.19
PARAM ZETABH=1.19
PARAM ZETABH=1.19
PARAM ZETABH=0.1

PAKAM KRTHET=0.2

INPUT COMMAND

PARAM PC=0.1

INITIAL DIGITAL BENDING MODE FILTER PARAMETERS

PARAM FISET=8.0 PARAM F2SET=8.0 PARAM RADUSI=0.9 PARAM RADUS2=0.8

INITIAL

CALCULATE THE BENDING MODE FREQUENCIES IN HZ.

LHZ=WBL/6.28 HHZ=WBH/6.28

PYNAMIC\*

SET THE INITIAL DIGITAL FILTER PARAMETERS

IF(TIME.NE.0.0)GO TO 10

CALCULATE THE FILTER COEFFICIENTS

R ADIUS=RADUS1 A11, B11, B12, GAIN1=COEFF (FISET, DELT, RADIUS) R ADIUS=RADUS2 A21, B21, B22, GAIN2=COEFF (F2SET, DELT, RADIUS) GO TO 100 CONTINUE DIGITAL BANDPASS FILTER AND FREQUENCY DETECTOR 2H 8 10

BLIOUT=0.15\*BR-0.12354\*BLI1+0.030375\*BL12+1.7228\*BL21-0.88604\*BL22 BLI20UT=0.1\*BLIDUT-0.1\*BL32+1.64725\*BL41-0.81\*BL42 BLI2=BL11 BL22=BL21 BL21=BL21 BL21=BL1DUT BL31=BL30UT BL31=BL3UT BL31=BL3UT BL31=BL3UT

DIGITAL BANDPASS FILTER AND FREQUENCY DETECTOR 74 15 10 BHIOUT = 0.465\*8R-0.3761\*8HI1+0.1162\*8HI2+1.3753\*8H21-0.7225\*8H22 BH20UT=0.1\*8HI0UT-0.1\*8H32+1.45625\*8H41-0.81\*8H42 BH12=8H11 BH22=8H21 BH22=8H21 BH32=8H31 BH31=8H10UT BH31=8H10UT BH42=8H41

COMPUTE THE CENTER FREQUENCY FOR THE LOW FREQUENCY NOTCH.

TC1=CROSS(TIME, BL10UT, 0.0)
IF(TC1, EQ.0.0)
IINT1=TC1-LTINT1
LTINT1=TC1-LTINT1
LTINT1=TC1-LTINT1
IF(TINT1-C1.0.0)
IF(TINT1-LT.0.0625) GO TO 50
IF(TINT1-LT.0.0625) GO TO 50
FREQ=1,0/(2.0\*TINT1)
FREQ=(F1S ET+FREQ)/2.0
RADIUS=RADUS1
A 11,8 11,8 12,6 AIN1=COEFF(FREQ, DELT, RADIUS)
FISET=FREQ

COMPUTE THE CENTER FREQUENCY FOR THE HIGH FREQUENCY NOTCH

PE=PC+PD GAMA=PE+PB FILTIN=GAMA\*KTHETA PI=FILQUI P2=MDELTA\*PI P3=—PE-NA P4=ZDELTA\*PI/VEL P5=PR-P4-P6 P6=ZALFA\*ALFA/VEL P5=PR-P1 P7=PRTHET\*P7 P0=PSFIG\*BD P1=PSFIG\*BD P1=PSFIG\*BD

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MODEL OF LOW BAND BENDING MODE

BL1=GAINL/PSIGA\*P1 BL2=ZETABL\*BL1 BL3=BL2-ZETABL\*BL4-BL5\*WBL\*\*2.0 BL4=INTGRL(0.0, BL3) BL5=INTGRL(0.0, BL4) MODEL OF HIGH BAND BENDING MODE

BH1=GAINH/PSIGA\*P1 BH2=ZETABH\*BH1 BH3=BH2-ZETABH\*BH4-BH5\*WBH\*\*2.0 BH4=INTGRL(0.0,BH3) BH5=INTGRL(0.0,BH4) BR=BH4+BL4 BC=BH5+BL4 MODEL OF THE PLANT WITHOUT BENDING MODES TO ESTABLISH NOMINAL PERFORMANCE.

P21=PC+P27

FORTRAN SUBROUTINE TO CALCULATE THE NOTCH FILTER COEFFICIENTS FORTRAN SUBROUTINE COEFF(FREQ,DELT,RADIUS,A1,B1,B2,GAIN) PI=3.14159 AI=-2.0\*COS(FREQ\*2.0\*PI\*DELT) BI=-2.0\*RADIUS\*COS(FREQ\*2.0\*PI\*DELT) B2=RADIUS\*\*2.0 TO UNITY CONTRL FINITY=2.0 , DELT=0.01, DELS=0.01
INTEG RKSFX
PRINT 0.01,P0,BR,F1SET,F2SET
END
\$TOP CALCULATE THE FILTER COEFFICIENTS P22=P21+P31 P23=KTHETA\*P22 P24=MDELTA\*P23 P25=-P24-MALFA\*P30 P26=INTGRL(0.0, P25) P27=INTGRL(0.0, P25) P28=-DELTA/VEL\*P30+P26 P30=INTGRL(0.0, P29) P30=INTGRL(0.0, P29) ADJUST THE FILTER DC GAIN PROGRAM AND PLGITER CONTROL DRWG(1,1,TIME,P27)
DRWG(2,1,TIME,P0)
DRWG(2,2,TIME,F1SET)
DRWG(2,3,TIME,F2SET)
DRWG(2,3,TIME,HZ) GAIN=(1.0+81+82)/(2.0+A1) RETURN ER INCOCOL SAMPLE ပပပ

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ano = ao	X		
0	=015N02401=	10.0	10.0
	30,VUL=SER	10.0	10.0
<b>4</b>	. 0. UNI T=33.	0.01	1.0
SN≈,SYSOUT:	DSN=C0044	-0.08	5.0
END SPRINT DD D	//PLOT.STEPLIB_DD_DSN=C0044.Q.UNIT=3330,VUL=SEK=UISKUZ;UISF-SFK //PLOT.PLOTPARM DD * EPLOT SCALE=0.45 &END //PLOT.SYSIN DD *	0.2	0.2
E! ##	1014/ 1014/ 1014/	0.0	0.0

ASSOCIATED FIGURES 4-4-5 PROGRAM 4-4

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// EXEC DSL //DSL.INPUT DD \*

3RD ORDER SYSTEM WITH BENDING MODE TWO BENDING MODES CENTERED AT 10.0 HZ AND 6.0 HZ. DIGITAL FREQUENCY DETECTOR BANDPASS FILTERS. DUAL TRACKING DIGITAL FILTERS INPUT IS A 0.05\*T RAMP.

PROGRAM CONTROL PARAMETERS

INTGER NPLOT

SYSTEM PARAMETERS

P SIGA=0.06 P SIRG=0.06 MALFA=28.625 MDELTA=24.17 ZALFA=180.0 ZDELTA=113.75 VEL=2500.0 WBH=862.83 ZETABH=1.19 GAINH=20.0 WBL=37.7 ZETABL=0.1 GAINL=240.0

PARAM KRTHET=0.2

INITIAL DIGITAL BENDING MODE FILTER PARAMETERS

F1SET=8.0 F2SET=8.0 RADUS1=0.9 RADUS2=0.8 

INI TIAL

BENDING MODE FREQUENCIES IN HERTZ. CALCULATE THE LHZ=WBL/6.28

DYNAMIC \*

SET THE INITIAL DIGITAL FILTER PARAMETERS

IF(TIME.NE.0.0)60 TO 10

CALCULATE THE FILTER COEFFICIENTS

RADIUS=RADUSI All, Bll, Bl2, GAINI=COEFF (FISET, DELT, RADIUS) RADIUS=RADUS2 A21, B21, B22, GAIN2=COEFF (F2SET, DELT, RADIUS) GO TO 100 CONTINUE

GENERATE A RAMP INPUT COMMAND

PC=RAMP (0.0) PC=0.05\*PC

5 TO 8 HZ DIGITAL BANDPASS FILTER AND FREQUENCY DETECTOR

BL10UT=0.15\*BR-0.12354\*BL11+0.030375\*BL12+1.7228\*BL21-0.88604\*BL22 BL12=BL11 BL12=BL11 BL22=BL21 BL22=BL21 BL22=BL21 BL32=BL31 BL32=BL31 BL32=BL31 BL3=BL30UT BL42=BL41 BL42=BL41 BL42=BL41 BL42=BL41

15 HZ DIGITAL BANDPASS FILTER AND FREQUENCY DETECTOR 10

\*\*\*

BHIOUT=0.465\*BR-0.3761\*BH11+0.1162\*BH12+1.3753\*BH21-0.7225\*BH22 BH20UT=0.1\*BH10UT-0.1\*BH32+1.45625\*BH41-0.81\*BH42 BH12=BH11 BH2=BH21 BH2=BH20UT BH31=BH10UT BH31=BH10UT BH31=BH10UT BH41=BH20UT

CENTER FREQUENCY FOR THE LOW FREQUENCY NOTCH. COMPUTE THE

TC1=CRDSS(TIME, BLIQUT, 0.0)
IF(TC1, EQ.0.0) GO TO 50
TINT1=TC1-LTINT1
LTINT1=TC1
LTINT1=TC1
IF(TINT1-GT.0.1) GO TO 50
IF(TINT1-LT.0.0625) GO TO 50
FREQ=(FISET+FREQ)/2.0
FREQ=(FISET+FREQ)/2.0
RADIUS=RADUS1
All, Bli, Bl2, GAINI=COEFF(FREQ, DELT, RADIUS)
FISET=FREQ

COMPUTE THE CENTER FREQUENCY FOR THE HIGH FREQUENCY NOTCH

F10UT=FILTIN+A11\*FI11+F112-B11\*F011-B12\*F012 TC2=CROSS(TIME, BH20UT, 0.0)
IF(TC2, EQ.0.0) GO TO 100
TINT2=TC2-LTINT2
IF(TINT2-TC2
IF(TINT2-LT.0.0625) GO TO 100
IF(TINT2-LT.0.03333) GO TO 100
FREQ=1.0/(2.0\*TINT2)
FREQ=1.0/(2.0\*TINT2) F20UT=F10UT+A21\*F121+F122-621\*F021-822\*F022 ADJUST OUTPUT FOR DC GAIN = 1.0 FILOUT=F20UT\*GAINI\*GAINZ FII2=FII1 FII1=FILTIN F012=F011 F011=F10UT F122=F121 F121=F10UT F022=F021 SECOND NOTCH FILTER FIRST NOTCH FILTER 100 20

CONTINUE

**200** 

DER IVATIVE

MODEL OF THE THIRD ORDER PLANT

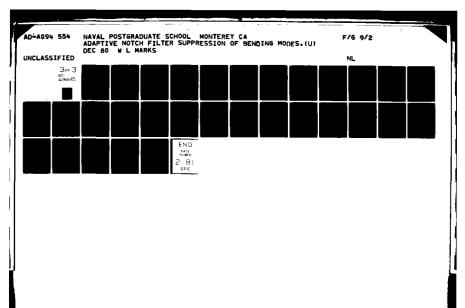
PE=PC+PO GAMA=PE+PB FILTIN=GAMA\*KTHETA PI=FILOUT P2=MDELTA\*PI P3=-P2-MA MA=MALFA\*ALFA P5=PR-P4-P6 P6=ZALFA\*ALFA P6=ZALFA\*ALFA P6=ZALFA\*ALFA P7=PR+PII P7=PR+PII P7=PR+PII P8=KRTHET\*P7 P9=INTGRL(0.0,PR) P10=PSIGA\*BR PR=INTGRL(0.0,P3) ALFA=INTGRL(0.0,P3) MODEL OF LOW BAND BENDING MODE

BL1=GAINL/PSIGA\*P1 BL2=ZETABL\*BL1 BL3=BL2-ZETABL\*BL4-BL5\*WBL\*\*2.0 BL4=INTGRL(0.0,BL3) BL5=INTGRL(0.0,BL4) MODEL OF HIGH BAND BENDING MODE

BH1=GAINH/PSIGA\*P1 BH2=ZETABH\*BH1 BH3=BH2-ZETABH\*BH4-BH5\*WBH\*\*2.0 BH4=INTGRL(0.0,BH3) BH5=INTGRL(0.0,BH4) BR=BH4+BL4 BO=BH5+BL5 MODEL OF THE PLANT WITHOUT BENDING MODES TO ESTABLISH NOMINAL PERFORMANCE.

P21=PC+P27 P22=P21+P31

FORTRAN SUBROUTINE TO CALCULATE NOTCH FILTER COEFFICIENTS FOKTRAN SUBROUTINE COEFF(FREQ,DELT,RADIUS,A1,B1,B2,GAIN) CALL DRWG(1,1,TIME,P27)
CALL DRWG(1,2,TIME,P0)
CALL DRWG(2,2,TIME,P0)
CALL DRWG(2,2,TIME,F12)
CALL DRWG(2,3,TIME,H12)
CALL DRWG(2,3,TIME,HH2)
TERMINAL
CALL ENDRW(NPLDT)
CONTRL FINTIM=2.0 , DELT=0.01, DELS=0.01
INTEG RKSFX
PRINT 0.01,P0,BR,F1SET,F2SET
END
STOP PI=3。14159 AI=-2。0\*COS(FREQ\*2。0\*PI\*DELT) BI=-2。0\*RADIUS\*COS(FREQ\*2。0\*PI\*DELT) B2=RADIUS\*\*2。0 ADJUST THE FILTER DC GAIN TO UNITY FILTER COEFFICIENTS P23=KTHETA\*P22 P24=MDELTA\*P23 P25=-P24-MALFA\*P30 P27=INTGRL(0.0,P25) P27=INTGRL(0.0,P25) P28=-DELTA/VEL\*P23 P29=-P28-ZALFA/VEL\*P30+P26 P30=INTGRL(0.0,P29) PROGRAM AND PLOTTER CONTROL GAIN=(1.0+81+82)/(2.0+A1) RETURN END CALCULATE THE 000ပပပ



SHR		
*//C.SYSPRINT DD DSN=,SYSOUT=A //PLGT.STEPLIB DD DSN=C0044.Q,UNIT=3330,VOL=SER=DISKO2,DISP=SHR //PLGT.PLCTPARM DD * EPLGT SCALE=0.45 EEND //PLGT.SYSIN DD *	10.0	10.0
30,VOL=SER=	10.0	10.0
=A •Q•UNI T=33	0.01	1.0
SN=, SYSOUT DSN=C0044 D * CEND	-0.08	5.0
SPRINT OD D STEPLIB DD PLOTPARM D SCALE=0.45 SYSIN DD *	0.2	0.2
**************************************	0.0	0.0

ASSOCIATED FIGURES 4-6 PROGRAM 4-6

计分类操作系统 经存货的 经存货 经存货 经存货 计连续存储 计操作 经存货 经存货 经存货的 经存货的 经存货的 经存货 医动物 医多种性 计连续设计 计记录器

// EXEC DSL

TITLE \*\*\* 3RD ORDER SYSTEM WITH BENDING MODE

IITLE \*\*\* TWD BENDING MODES CENTERED AT 9.0 HZ AND

IITLE \*\*\* 7.0 HZ.

IITLE \*\*\* DIGITAL FREQUENCY DETECTOR BANDPASS FILTERS.

IITLE \*\*\* DUAL TRACKING DIGITAL FILTERS

IITLE \*\*\* INPUT IS A 0.1 RADIAN STEP

PROGRAM CONTROL PARAMETERS

INTGER NPLOT

SYSTEM PARAMETERS

PARAM PSIGA=0.06 PARAM MALFA=20.06 PARAM MALFA=28.625 PARAM ZALFA=180.0 PARAM ZDELTA=13.75 PARAM VEL=2500.0 PARAM VEL=2500.0 PARAM GAINH=1.19 PARAM GAINH=20.0 PARAM ZETABH=1.19 PARAM ZETABH=1.19 PARAM ZETABH=1.19 PARAM ZETABH=1.19

PARAM KRTHET=0.2

INPUT COMMAND

PARAM PC=0.1

INITIAL DIGITAL BENDING MODE FILTER PARAMETERS

F1SET=8.0 F2SET=8.0 RADUS1=0.9 RADUS2=0.8 

INI TIAL

CALCULATE THE BENDING MODE FREQUENCIES IN HERTZ.

LHZ=WBL/6.28 HHZ=WBH/6.28

DYNAMIC \*

SET THE INITIAL DIGITAL FILTER PARAMETERS

IF(TIME.NE.0.0)G0 T0 10

CALCULATE THE FILTER COEFFICIENTS

RADIUS=RADUSI All, Bll, Bl2, GAINI=COEFF (FISET, DELT, RADIUS) RADIUS=RADUS2 A21, B21, B22, GAIN2=COEFF (F2SET, DELT, RADIUS) GO TO 100 CONTINUE

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5 TO 8 HZ DIGITAL BANDPASS FILTER AND FREQUENCY DETECTOR

BL10UT=0.15\*BR-0.12354\*BL11+0.030375\*BL12+1.7228\*BL21-0.88604\*BL22 BL12=BL11 BL12=BL11 BL12=BL21 BL2=BL21 BL2=BL21 BL3=BL3 BL3=BL3

8 TO 15 HZ DIGITAL BANDPASS FILTER AND FREQUENCY DETECTOR

BH10UT=0.465\*BR-0.3761\*BH11+0.1162\*BH12+1.3753\*BH21-0.7225\*BH22 BH20UT=0.1\*BH10UT-0.1\*BH32+1.45625\*BH41-0.81\*BH42 BH12=BH11 BH12=BH21 BH21=BH10UT BH31=BH10UT BH31=BH10UT BH31=BH10UT BH41=BH20UT

COMPUTE THE CENTER FREQUENCY FOR THE LOW FREQUENCY NOTCH.

TC1=CROSS(TIME, BL10UT, 0.0)
IF(TC1, EQ.0.0) GO TO 50
TINT1=TC1-LTIVT1
LTINT1=TC1
IF(TINT1-GT.0.1) GO TO 50
IF(TINT1-LT.0.0625) GO TO 50
FREQ=1.0/(2.04TINT1)
FREQ=(FISET+FREQ)/2.0
RADIUS=RADUS1
All, Bl1, Bl2, GAIN1=COEFF(FREQ, DELT, RADIUS)
FISET=FREQ

COMPUTE THE CENTER FREQUENCY FOR THE HIGH FREQUENCY NOTCH

F10UT=F1LTIN+A11\*F111+F112-B11\*F011-B12\*F012 TC2=CRDSS(TIME, BH2OUT, 0.0)
IF(TC2, EQ.0.0) GO TO 100
TINT2=TC2-LTINT2
LTINT2=TC2
IF(TINT2-TC.0.033333) GO TO 100
IF(TINT2-TT.0.033333) GO TO 100
FREQ=1.0/(2.0\*TINT2)
FREQ=(FREQ+F2SET)/2.0
RADIUS=RADUS2
A21, B21, B22, GAIN2=COEFF(FREQ, DELT, RADIUS) F20UT=F10UT+A21\*F121+F122-B21\*F021-B22\*F022 SECOND NOTCH FILTER FIRST NOTCH FILTER 100

ADJUST GUTPUT FOR DC GAIN

FILOUT=F20UT\*GAINI\*GAINZ FILZ=F111 FILZ=F111 F012=F011 F012=F10UT F122=F121 F122=F121 F022=F021

CONTINUE **500** 

\* Derivative \*

MODEL OF THE THIRD ORDER PLANT

PE=PC+PO GAMA=PE+PB FILTIN=GAMA\*KTHETA PI=FILOUT P2=MDELTA\*PI P3=-P2-MA M4=MALFA\*ALFA M4=ZDELTA\*PI/VEL P5=PR-P4-P6 P6=ZALFA\*ALFA P6=ZALFA\*ALFA P6=ZALFA\*ALFA P6=ZALFA\*ALFA P6=ZALFA\*ALFA P7=PR+PI P9=INTGRL(0.0.PR) P10=PSIRG\*BU P11=PSIGA\*BR P11=PSIGA\*BR P11=PSIGA\*BR MODEL OF LOW BAND BENDING MODE

BL1=GAINL/PSIGA\*P1 BL2=ZETABL\*BL1 BL3=BL2-ZETABL\*BL4-BL5\*WBL\*\*2.0 BL4=INTGRL(0.0,8L3) BL5=INTGRL(0.0,8L4) MODEL OF HIGH BAND BENDING MODE

BH1=GAI NH/PSIGA\*P1
BH2=ZETABH\*BH1
BH3=BH2-ZETABH\*BH4-BH5\*WBH\*\*2.0
BH4=INTGRL(0.0,BH3)
BH5=INTGRL(0.0,BH4)
BR=BH4+BL4
BO=BH5+BL5

MCDEL OF THE PLANT WITHOUT BENDING MODES TO ESTABLISH NOMINAL PERFORMANCE .

P21=PC+P27

FGRIRAN SUBROJIINE TO CALCULATE THE NOTCH FILTER CDEFFICIENTS # FORTRAN SUBROUTINE COEFF(FREQ,DELT,RADIUS,A1,B1,B2,GAIN) CALL DRWG(1,1,TIME,P27)
CALL DRWG(1,2,TIME,P0)
CALL DRWG(2,2,TIME,F2SET)
CALL DRWG(2,2,TIME,F1SET)
CALL DRWG(2,3,TIME,HAZ)
CALL DRWG(2,4,TIME,HHZ)
CALL ENDRW(NPLOT)
CALL ENDRW(NPLOT)
CALL ENDRW(NPLOT)
CALL ENDRW(NPLOT)
CALL ENDRW(NPLOT)
STOP PI=3.14159 AI=-2.0\*COS(FREQ\*2.0\*PI\*DELT) BI=-2.0\*RADIUS\*COS(FREQ\*2.0\*PI\*DELT) B2=RADIUS\*\*2.0 ADJUST THE FILTER DC GAIN TO UNITY CALCULATE THE FILTER COEFFICIENTS P22=P21+P31 P23=KTHETA\*P22 P24=MDELTA\*P23 P25=-P24-MALFA\*P30 P26=INTGRL(0.0, P25) P27=INTGRL(0.0, P25) P28=ZDELTA/VEL\*P30+P26 P30=INTGRL(0.0, P29) P30=INTGRL(0.0, P29) PROGRAM AND PLOTTER CONTROL GAIN=(1.0+81+82)/(2.0+A1) RETURN ပပပ

*  * //C.SYSPRINT DD DSN=,SYSOUT=A //PLOT.STEPLIB DD DSN=C0044.Q,UNIT=3330,VOL=SER=DISKO2,DISP=SHR //PLOT.PLOTPARM DO * EPLOT SCALE=0.45 & END //PLOT.SYSIN DD *	0 10.0	10.0
:3330 • VOL	10.0	10,
T=A 4.Q.UNI T=	0.01	0,1
00 D SN=, SY SOU'S S DD DSN=C 004. RM DD * 0, 45 & END	-0.08	ה ה
SYSPRINT CONT. SYSPRINT CONT. PLOTPARED OT SYSIN CONT.	0.2	6.0
**///2/	0.0	0.0

PROGRAM 4-8 ASSOCIATED FIGURES 4-8

// EXEC DSL //DSL.INPUT DD \* ITLE \*\*\* 3RD ORDER SYSTEM WITH BENDING MODE

ITLE \*\*\* TWO BENDING MODES CENTERED AT 14.0 HZ AND

ITLE \*\*\* 5.5 HZ.

ITLE \*\*\* DIGITAL FREQUENCY DETECTOR BANDPASS FILTERS.

ITLE \*\*\* DUAL TRACKING DIGITAL FILTERS

ITLE \*\*\* INPUT IS A 0.1 RADIAN STEP

PROGRAM CONTROL PARAMETERS

INTGER NPLOT

SYSTEM PARAMETERS

# PARAM PSIGA=0.06 PARAM PSIRG=0.06 PARAM MALFA=28.625 PARAM MALFA=28.625 PARAM ZALFA=180.0 PARAM ZALFA=113.75 PARAM ZELABH=1.19 PARAM ZETABH=1.19 PARAM ZETABH=1.19 PARAM ZETABH=240.0 PARAM ZETABH=240.0

200

PARAM KRTHET=0.2

INPUT COMMAND

PARAM PC=0.1

INITIAL DIGITAL BENDING MODE FILTER PARAMETERS

PARAM F1SET=8.0 PARAM F2SET=8.0 PARAM RADUS1=0.9 PARAM RADUS2=0.8

INI TIAL

CALCULATE THE BENDING MODE FREQUENCIES IN HERTZ.

LHZ=WBL/6.28 HHZ=WBH/6.28

DYNAMIC

SET THE INITIAL DIGITAL FILTER PARAMETERS

IF(TIME.NE.0.0)60 TO 10

CALCULATE THE FILTER COEFFICIENTS

RADIUS=RADUSI All'Bli;Bl2;GAIN1=COEFF(F1SET;DELT;RADIUS) RADIUS=RADUS2 A21;B21;B22;GAIN2=COEFF(F2SET;DELT;RADIUS) GO TO 100 CONTINUE BANDPASS FILTER AND FREQUENCY DETECTOR DIGITAL **ZH** œ 10

BLIOUT=0.15\*BR-0.12354\*BL11+0.030375\*BL12+1.7228\*BL21-0.88604\*BL22 BLI2=BL11 BLI2=BL11 BLI2=BL11 BL2=BL21 BL2=BL21 BL3=BL31 BL3=BL10UT BL3=BL10UT BL3=BL10UT BL3=BL10UT BL4=BL10UT BL4=BL20UT

HZ DIGITAL BANDPASS FILTER AND FREQUENCY DETECTOR 15 10

\*\*\*

BH10UT=0.465\*BR-0.3761\*BH11+0.1162\*BH12+1.3753\*BH21-0.7225\*BH22 BH20UT=0.1\*BH10UT-0.1\*BH32+1.45625\*BH41-0.81\*BH42 BH12=BH11 BH11=BR BH2=BH21 BH31=BH10UT BH31=BH10UT BH31=BH10UT BH41=BH20UT

\*\*\*

COMPUTE THE CENTER FREQUENCY FOR THE LOW FREQUENCY NOTCH.

TC1=CR3SS(TIME, BL10UT, 0.0)
IF(IC1, EQ.0.0) GO TO 50
TINT1=TC1-LTIVT1
LTINT1=TC1
LTINT1=TC1
IF(TINT1-GT.0.1) GO TO 50
IF(TINT1-LT.0.0625) GO TO 50
FREQ=(F1SET+FREQ)/2.0
RADIUS=RADUS1
All, Bl1, Bl2, GAIN1=COEFF(FREQ, DELT, RADIUS)
F1SET=FREQ

COMPUTE THE CENTER FREQUENCY FOR THE HIGH FREQUENCY NOTCH

200 CONTINUE

DER IVATIVE

MODEL OF THE THIRD ORDER PLANT

PE=PC+P0 GAMA=PE+P8 FILTIN=GAMA\*KTHETA PI=FILQUT P2=MDELTA\*P1 P3=-P2-MA MA=MALFA\*ALFA P4=ZDELTA\*P1/VEL P5=PR-P4-P6 P6=ZALFA\*ALFA/VEL P6=ZALFA\*ALFA/VEL P6=ZALFA\*ALFA/VEL P7=PR+P10 P0=P9+P10 P10=P51GA\*BR P10=P51GA\*BR PR=INTGRL(0.0,P3) ALFA=INTGRL(0.0,P3) MODEL OF LOW BAND BENDING MODE

BL1=GAINL/PSIGA\*P1 BL2=ZETABL\*BL1 BL3=BL2-ZETABL\*BL4-BL5\*WBL\*\*2.0 BL4=INIGRL(0.0,BL3) BL5=INIGRL(0.0,BL4) MODEL OF HIGH BAND BENDING MODE

BH1=GAINH/PSIGA\*PI BH2=ZETABH\*BH1 BH3=BH2-ZETABH\*BH4-BH5\*WBH\*\*2.0 BH4=INTGRL(0.0, BH3) BH5=INTGRL(0.0, BH4) BR=BH4+BL4 BO=BH5+BL5 MODEL OF THE PLANT WITHOUT BENDING MODES TO ESTABLISH NOMINAL PERFORMANCE.

P21=PC+P27

FORTRAN SUBROUTINE TO CALCULATE THE NOTCH FILTER COEFFICIENTS FORTRAN Subroutine coeff(FREQ.DELT,RADIUS,A1,81,82,GAIN) CALL DRWG(1,1,TIME,P27)

CALL DRWG(1,2,TIME,P27)

CALL DRWG(2,2,TIME,F1SET)

CALL DRWG(2,3,TIME,LHZ)

CALL DRWG(2,3,TIME,HHZ)

TERMINAL

CONTRL FINTIM=2.0, DELT=0.01, DELS=0.01

INTEG RKSFX

FNO STOP PI=3.14159 AI=-2.0\*COS(FREQ\*2.0\*PI\*DELT) BI=-2.0\*RADIUS\*COS(FREQ\*2.0\*PI\*DELT) B2=RADIUS\*\*2.0 ADJUST THE FILTER DC GAIN TO UNITY CALCULATE THE FILTER COEFFICIENTS P22=P21+P31 P23=KTHETA\*P22 P24=MDELTA\*P23 P25=-P24-MALFA\*P30 P26=INTGRL(0.0, P25) P27=INTGRL(0.0, P25) P28=2DELTA/VEL\*P30+P26 P30=INTGRL(0.0, P29) P30=INTGRL(0.0, P29) PROGRAM AND PLOTTER CONTROL GAIN=(1.0+B1+B2)/(2.0+A1) RETURN ںںں

######################################	10.0	0.01
30,VOL=SER:	10.0	
=A •Q•UNI T=333	0.01	-
SN=, SY SOUT: DSN=C0044 D # &END	-0.08	c u
SPRINT DD D. STEPLIB DD SCALE OF SYSIN DD * 55 STEPLIB DD * 55 SYSIN DD	0.2	
** //C.SYS //PLOT. //PLOT. //PLOT.	0.0	•

PRUGRAM 4-10 ASSOCIATED FIGURES 4-10

// EXEC DSL //DSL.INPUT DD \* ILE \*\*\* 3RD GRDER SYSTEM WITH DYNAMIC BENDING MODES
ILE \*\*\* LOW MODE STARTS AT 6.0 HZ. AND INCREASES AT
ILE \*\*\* I.O HZ PER SECOND. THE HIGH MODE STARTS AT 12.0 HZ.
ILE \*\*\* AND DECREASES AT 1.5 HZ PER SECOND.
ILE \*\*\* DIGITAL FREQUENCY DETECTOR BANDPASS FILTERS.
ILE \*\*\* DUAL TRACKING DIGITAL FILTERS
ILE \*\*\* INPUT IS A 0.1 RADIAN STEP

PROGRAM CONTROL PARAMETERS

INTGER NPLOT CONST NPLOT=1 SYSTEM PARAMETERS

\*\*
PARAM PSIGA=0.06
PARAM PSIGG=0.06
PARAM MALFA=28.625
PARAM ZALFA=180.0
PARAM ZELTA=113.75
PARAM ZELTA=113.75
PARAM ZETABH=1.19
PARAM ZETABH=1.19
PARAM ZETABH=2.0.0
PARAM ZETABH=2.0.0
PARAM ZETABH=2.0.0
PARAM KTHETA=1.48

PARAM PI=3.14159

INPUT COMMAND

PARAM PC=0.1

INITIAL DIGITAL BENDING MODE FILTER PARAMETERS

PARAM FISET=8.0 PARAM F2SET=8.0 PARAM RADUS1=0.9 PARAM RADUS2=0.8

\* DYNAMIC \* SET THE INITIAL DIGITAL FILTER PARAMETERS

IF(TIME.NE.0.0)G0 T0 10

CALCULATE THE FILTER COEFFICIENTS

RADIUS=RADUSI All, Bli, Bl2, GAIN1=COEFF (FISET, DELT, RADIUS) RADIUS=RADUS2 A21, B21, B22, GAIN2=COEFF (F2SET, DELT, RADIUS) GO TO 100 CONTINUE

COMPUTE THE BENDING MODE FREQUENCIES

HDEL=RAMP(0.0) LDDEL=RAMP(0.0) WBH=(12.0-1.5\*HDEL)\*2.0\*PI WBL=(6.0+LODEL)\*2.0\*PI LHZ=WBL/6.28 HHZ=WBH/6.28 5 TO 8 HZ DIGITAL BANDPASS FILTER AND FREQUENCY DETECTOR

BLIOUT=0.15\*BR-0.12354\*BL11+0.030375\*BL12+1.7228\*BL21-0.88604\*BL22 BL20UT=0.1\*BL10UT-0.1\*BL32+1.64725\*BL41-0.81\*BL42 BL12=BL11 BL21=BL21=BL21 BL32=BL31 BL31=BL10UT BL31=BL10UT BL42=BL41 BL42=BL41 BL42=BL41

8 TO 15 HZ DIGITAL BANDPASS FILTER AND FREQUENCY DETECTOR

BH10UT=0.465\*BR-0.3761\*BH11+0.1162\*BH12+1.3753\*BH21-0.7225\*BH22 BH20UT=0.1\*BH10UT-0.1\*BH32+1.45625\*BH41-0.81\*BH42 BH12=BH11 BH2=BH21 BH32=BH31 BH31=BH10UT BH31=BH10UT BH42=BH41 BH42=BH41

COMPUTE THE CENTER FREQUENCY FOR THE LOW FREQUENCY NOTCH.

ICI=CROSS(TIME, BLIQUT, 0.0)
IF(TCI, EQ.0.0) GO TO 50
TINTI=TCI-LTINTI
LINTI=TCI-LTINTI
LINTI=TCI-LTINTI
IF(TINTI-GT.0.1) GO TO 50
IF(TINTI-LT.0.0625) GO TO 50
FREQ=(FISET+FREQ)/2.0
FREQ=(FISET+FREQ)/2.0
RADIUS=RADUSI
All, Bl2, GAINI=COEFF(FREQ, DELT, RADIUS)
FISET=FREQ

COMPUTE THE CENTER FREQUENCY FOR THE HIGH FREQUENCY NOTCH

50 TC2=CROSS(TIME, BH20UT<sub>10</sub>0,0)
IF(TC2=CROSS(TIME, BH20UT<sub>10</sub>0,0)
IINT2=TC2-LTINT2
LTINT2=TC2-LTINT2
LTINT2=TC2-LTINT2
IF(TINT2=CT-LTINT2)
IF(TINT2-CT-0.0625) GD TD 100
IF(TINT2-CT-0.063333) GD TD 100
FREQ=100/C 0.013333 GD TD 100
FREQ=100/C 0.01333 GD TD 100
FREQ=100/C FILTER

FIRST NOTCH FILTER

FOUT=FILTIN+A11\*FI11+FI12-B11\*F011-B12\*F012

SECOND NOTCH FILTER

FOUT=FILDUT=FGUT\*GAIN1\*GAIN2
FILCUT=FGUT\*GAIN1\*GAIN2
FILCUT=FILTIN
FOUT=FILTIN
FOUT

MODEL OF THE THIRD ORDER PLANT

CONTINUE

200

DER I VAT I VE \*

PE=PC+P0 GAMA=PE+P8 FILTIN=GAMA\*KTHETA PI=FILOUT P2=MDELTA\*P1 P3=-P2-MA MA=MALFA\*ALFA P5=PR-P4-P6 P5=PR+P11 P6=ZDELTA\*ALFA/VEL P5=RRTHET\*P7 P0=P9+RTHET\*P7 P0=P9+RTHET\*P7 P0=P9+RTHET\*P7 P10=P9+P1 P1=PSIGA\*BR PR=INTGRL(0.0,P3) ALFA=INTGRL(0.0,P3) MODEL OF LOW BAND BENDING MODE

BL1=GAINL/PSIGA\*P1 BL2=ZETABL\*BL1 BL3=BL2-ZETABL\*BL4-BL5\*WBL\*\*2.0 BL4=INTGRL(0.0, BL3) BL5=INTGRL(0.0, BL4) MUDEL OF HIGH BAND BENDING MODE

BHI=GAINH/PSIGA\*PI BH2=ZETABH\*BHI BH3=BH2-ZETABH\*BH4-BH5\*WBH\*\*2.0 BH4=INTGRL(0.0, BH3) BH5=INTGRL(0.0, BH4) BR=BH4+BL4 MODEL OF THE PLANT WITHOUT BENDING MODES TO ESTABLISH NOMINAL PERFORMANCE.

\*\*\*\*

FORTRAN SUBROUTINE TO CALCULATE THE NOTCH FILTER CDEFFICIENTS FORTRAN Subroutine coeff(freq,Delt,Radius,A1,B1,B2,GAIN) CALL DRWG(1,1,TIME,P27)
CALL DRWG(2,1,TIME,P0)
CALL DRWG(2,1,TIME,F1SET)
CALL DRWG(2,2,TIME,F2SET)
CALL DRWG(2,4,TIME,HHZ)
TERMINAL
CALL ENDRW(NPLOT)
TONTRL FINTIM=2.0 , DELT=0.01, DELS=0.01
INTEG RKSFX
PRINT 0.01,P0,BR,LHZ,F1SET,HHZ,F2SET
END
STOP PI=3.14159 AI=-2.0\*COS(FREQ\*2.0\*PI\*DELT) BI=-2.0\*RADIUS\*COS(FREQ\*2.0\*PI\*DELT) B2=RADIUS\*\*2.0 UNI TY CALCULATE THE FILTER COEFFICIENTS 10 P21=PC+P27 P22=P21+P31 P23=KTHETA\*P22 P24=MDELTA\*P23 P25=-P24-MALFA\*P30 P26=INTGRL(0.0, P25) P27=INTGRL(0.0, P25) P28=-P28-ZALFA/VEL\*P30+P26 P30=INTGRL(0.0, P29) ADJUST THE FILTER DC GAIN PROGRAM AND PLOTTER CONTROL GAIN=(1.0+81+82)/(2.0+A1) SOO

	*// SYSPRINT DD DSN=,SYSQUI=A //PLOT.STEPLIB DD DSN=C0044.Q,UNIT=3330,VOL=SER=DISK02,DISP=SHR //PLOT.PLOTPARM DD * EPLOT SCALE=0.45 &END //PLOT.SYSIN DD *	10.0	10.0
	30,VOL=SER	10.0	10.0
	A, UNI T=333	0.01	1.0
	SN=, SYSOUT= DSN=C0044. D * EEND	-0-08	5.0
RETURN END	PRINT DD DSTEPLIB DD PLOIPARM DE SCALE=0.45	0.2	0.2
æūi *-	**************************************	0.0	0.0

PROGRAM 4-12 ASSOCIATED FIGURES

// EXEC DSL //DSL.INPUT DD \*

ILE \*\*\* 3RD ORDER SYSTEM WITH DYNAMIC BENDING MODES
ILE \*\*\* LOW MODE STARTS AT 8.0 HZ. AND DECREASES AT
ILE \*\*\* 1.0 HZ PER SECOND. THE HIGH MODE STARTS AT 9.0 HZ.
ILE \*\*\* AND INCREASES AT 1.5 HZ PER SECOND.
ILE \*\*\* DIGITAL FREQUENCY DETECTOR BANDPASS FILTERS.
ILE \*\*\* DUAL TRACKING DIGITAL FILTERS
ILE \*\*\* INPUT IS A 0.1 RADIAN STEP

PROGRAM CONTROL PARAMETERS

INTGER NPLOT CONST NPLOT=1 SYSTEM PARAMETERS

PARAM PSIGA=0.06 PARAM PSIRG=0.06 PARAM MDELTA=28.625 PARAM ZALFA=117 PARAM ZALFA=113.75 PARAM VEL=2500.0 PARAM ZETABH=1.19 PARAM GAINH=20.0 PARAM GAINH=20.0 PARAM KIHETA=1.48

214

INITIAL DIGITAL BENDING MODE FILTER PARAMETERS RADIUS=RADUSI All, Bll, Bl2, GAIN1=COEFF (FISET, DELT, RADIUS) RADIUS=RADUS2 A21, B21, B22, GAIN2=COEFF (F2SET, DELT, RADIUS) GO TO 100 CONTINUE SET THE INITIAL DIGITAL FILTER PARAMETERS CALCULATE THE FILTER COEFFICIENTS IF(TIME.NE.0.0)GD TO 10 INPUT COMMAND F1SET=8.0 F2SET=8.0 RADUS1=0.9 RADUS2=0.8 PARAM PI=3.14159 PARAM PC=0.1 DYNAMIC 

COMPUTE THE BENDING MODE FREQUENCIES

HDEL=RAMP(0.0) LODEL=RAMP(0.0) WBH=(9.0+1.5\*HDEL)\*2.0\*PI WBL=(8.0-LODEL)\*2.0\*PI LHZ=WBL/6.28 HHZ=WBH/6.28

HZ DIGITAL BANDPASS FILTER AND FREQUENCY DETECTOR œ 10 Ś

BL10UT=0.15\*BR-0.12354\*BL11+0.030375\*BL12+1.7228\*BL21-0.88604\*BL22 BL12=BL11 BL12=BL11 BL12=BL11 BL22=BL21 BL21=BL31 BL31=BL31 BL31=BL10UT BL31=BL10UT BL42=BL41 BL42=BL41 BL42=BL41

BH10UT=0.465\*BR-0.3761\*BH11+0.1162\*BH12+1.3753\*BH21-0.7225\*BH22 BH20UT=0.1\*BH10UT-0.1\*BH32+1.45625\*BH41-0.81\*BH42 BH12=BH11 BH11=BR BH2=BH21 BH31=BH10UT BH31=BH10UT BH31=BH10UT BH31=BH10UT BH41=BH20UT

DIGITAL BANDPASS FILTER AND FREQUENCY DETECTOR

**7**H

15

10

8

COMPUTE THE CENTER FREQUENCY FOR THE LOW FREQUENCY NOTCH.

TCI=CROSS(TIME, BLIQUT, 0.0)
IF(TCI, EQ.0.0)
GG TO 50
TINTI=TCI-LTINTI
LTINTI=TCI
LTINTI=TCI
IF(TINTI-GT.0.1) GO TO 50
IF(TINTI-LT.0.0625) GO TO 50
FREQ=1 FREQ=1 SET+FREQ1/2.0
RADIUS=RADUSI
A11, B11, B12, GAINI=COEFF(FREQ, DELT, RADIUS)
FISET=FREQ

COMPUTE THE CENTER FREQUENCY FOR THE HIGH FREQUENCY NOTCH

MODEL OF LOW BAND BENDING MODE
BL1=GAI NL/PSIGA\*P1
BL2=ZETABL\*BL1
BL3=BL2-ZETABL\*BL4-BL5\*WBL\*\*2.0
BL4=INTGRL(0.0, BL3)
BL5=INTGRL(0.0, BL3)

MODEL OF HIGH BAND BENDING MODE BH1=GAINH/PSIGA\*P1 BH2=ZETABH\*BH1 BH3=BH2-ZETABH\*BH4-BH5\*WBH\*\*2.0 BH4=INIGRL(0.0, BH3) BH5=INIGRL(0.0, BH4) BR=BH4+BL4 BO=BH5+BL5 MGDEL DF THE PLANT WITHOUT BENDING MODES TO ESTABLISH NOMINAL PERFORMANCE .

FORTRAN SUBROJIINE TO CALCULATE THE NOTCH FILTER COEFFICIENTS FORTRAN SUBROUTINE COEFF(FREQ, DELT, RADIUS, A1, B1, B2, GAIN) CALL DRWG(1,1,TIME,P27)
CALL DRWG(2,1,TIME,P0)
CALL DRWG(2,1,TIME,F1SET)
CALL DRWG(2,2,TIME,F2SET)
CALL DRWG(2,2,TIME,LH2)
CALL DRWG(2,4,TIME,LH2)
CALL ENDRW(NPLOT)
CONTRL FINTIM=2.0, DELT=0.01, DELS=0.01
INTEG RKSFX
PRINT 0.01,P0,BR,LHZ,F1SET,HHZ,F2SET
END
\$70P PI=3.14159 AI=-2.0\*COS(FREQ\*2.0\*PI\*DELT) BI=-2.0\*RADIUS\*COS(FREQ\*2.0\*PI\*DELT) B2=RADIUS\*\*2.0 ADJUST THE FILTER DC GAIN TO UNITY CALCULATE THE FILTER COEFFICIENTS P21=PC+P27 P22=P21+P31 P23=KTHETA\*P22 P24=MDELTA\*P23 P25=-P24-MALFA\*P30 P26=INTGRL(0.0,P25) P27=INTGRL(0.0,P25) P28=-DELTA/VEL\*P30+P26 P30=INTGRL(0.0,P29) P31=KRTHET\*P26 PROGRAM AND PLOTTER CONTROL GAIN=(1.0+81+82)/(2.0+A1) COO

######################################	10.0	10.0
30,VOL=SER	10.0	10.0
-A -0,UNIT=33.	0.01	1.0
SN=, SYSOUT= DSN=C0044, D # EEND	-0.08	5.0
PRINT DD D STEPLIB DD PLOTPARM D SCALE=0.45 SYSIN DD *	0.2	0.2
**************************************	0.0	0.0

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