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A MONTE CARLO MODEL
FOR DETERMINING
COPPERHEAD PROBABILITY OF ACQUISITION
AND MANEUVER

MICHAEL STARKS

AUGUST 1980

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U. S. ARMY MATERIEL SYSTEMS ANALYSIS ACTIVITY
ABERDEEN PROVING GROUND, MARYLAND

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SECURITY CLASSIFICATION OF THIS PAGE (When Date Entered)

REPORT DOCUMENTATION PAGE		READ INSTRUCTIONS BEFORE COMPLETING FORM
1. REPORT NUMBER TECHNICAL REPORT NO. 308	2. GOVT ACCESSION NO.	3. RECIPIENT'S CATALOG NUMBER
4. TITLE (and Subtitle) A MONTE CARLO MODEL FOR DETERMINING COPPERHEAD PROBABILITY OF ACQUISITION AND MANEUVER		5. TYPE OF REPORT & PERIOD COVERED
		6. PERFORMING ORG. REPORT NUMBER
7. AUTHOR(s) Michael Starks		8. CONTRACT OR GRANT NUMBER(s)
9. PERFORMING ORGANIZATION NAME AND ADDRESS US Army Materiel Systems Analysis Activity Aberdeen Proving Ground, MD 21005		10. PROGRAM ELEMENT, PROJECT, TASK AREA & WORK UNIT NUMBERS DA Project No. 1R765706M541
11. CONTROLLING OFFICE NAME AND ADDRESS DARCOM 5001 Eisenhower Avenue Alexandria, VA 22333		12. REPORT DATE AUGUST 1980
		13. NUMBER OF PAGES 45
14. MONITORING AGENCY NAME & ADDRESS (if different from Controlling Office)		15. SECURITY CLASS. (of this report) UNCLASSIFIED
		15a. DECLASSIFICATION/DOWNGRADING SCHEDULE
16. DISTRIBUTION STATEMENT (of this Report) Approved for public release; distribution unlimited.		
17. DISTRIBUTION STATEMENT (of the abstract entered in Block 20, if different from Report)		
18. SUPPLEMENTARY NOTES		
19. KEY WORDS (Continue on reverse side if necessary and identify by block number) COPPERHEAD PAM Precision Guided Munitions Probability of Acquisition Laser Guided Weapons Artillery Effectiveness COPE		
20. ABSTRACT (Continue on reverse side if necessary and identify by block number) This report documents AMSAA's Probability of Acquisition and Maneuver (PAM) model. The model is used to develop performance estimates for COPPERHEAD and related weapon systems. A mathematical method for modeling the acquisition and maneuver portions of a COPPERHEAD trajectory is presented. In addition, the report contains a FORTRAN implementation of the model, a description of the required inputs, and a sample case with input and output.		

ACKNOWLEDGEMENTS

The general method of modeling COPPERHEAD presented in this report was developed by Richard Scungio, who also wrote the first version of the program. The version of the program documented in Reference 1 was written by Julian Chernick and Michael Starks. Richard Sandmeyer wrote the subprogram which controls the interface of PAM with the COPE model.

Thanks are extended to Jo Ann C. Marderness for typing support and Robin C. DeFranks for editing and final publication.

TABLE OF CONTENTS

	Page
ACKNOWLEDGEMENTS	3
1. INTRODUCTION	5
2. ASSUMPTIONS AND LIMITATIONS.	7
3. GENERAL OVERVIEW	9
4. ACQUISITION METHODOLOGY.	13
5. MANEUVER METHODOLOGY	15
6. SUMMARY.	18
7. REFERENCES	19
APPENDIX A - PAM INPUTS.	21
APPENDIX B - FORTRAN SOURCE LIST	25
APPENDIX C - SAMPLE CASE	37
DISTRIBUTION LIST	43

A MONTE CARLO MODEL FOR DETERMINING COPPERHEAD PROBABILITY OF ACQUISITION AND MANEUVER

1. INTRODUCTION

AMSAA's Probability of Acquisition and Maneuver (PAM) model has proven to be a useful tool for evaluating the COPPERHEAD weapon system. Different versions of the model have been used in two different ways.

A "stand alone" version of the model was used in the COPPERHEAD analysis documented in Reference 1. This analysis evaluated the sensitivity of COPPERHEAD system performance to a large number of factors, including:

- cloud ceiling
- designator power
- designator range
- target reflectivity
- target location error
- atmospheric transmission
- seeker sensitivity
- gun-target range
- unguided delivery error

An improved version of the stand alone PAM model was later used to evaluate the sensitivity of COPPERHEAD system performance to:

- designator-target-howitzer azimuth angle (ANGLE-T)
- target velocity
- response time
- additional delay time
- target heading angle
- point of target's closest approach to Predicted Intercept Point (PIP)

¹Chernick, Julian A., Richard C. Scungio, Michael Starks, Utility of COPPERHEAD With Ground Laser Designation in a European Battlefield Environment (U), Technical Report No. 257, US Army Materiel Systems Analysis Activity, Aberdeen Proving Ground, MD, December 1978, (CONFIDENTIAL report).

The results of this analysis were published as part of the COPPERHEAD COEA (Reference 2). Other "stand alone" uses to which modified versions of PAM have been applied include data generation for the Advanced Anti-Armor Vehicle Evaluation (ARMVAL) tests, and for a forthcoming Joint Technical Coordinating Group for Munitions Effectiveness (JTCEG/ME) publication on COPPERHEAD.

In addition to its use as a stand-alone model, PAM serves as one of the preprocessors for AMSAA's COPPERHEAD Operational Performance Evaluation (COPE) model. For a description of the COPE model, including details of that model's interface with PAM, see Reference 3.

Thus far, the model applications mentioned have concerned the COPPERHEAD system. First-order performance estimates for other weapon systems have also been developed through use of modified versions of the PAM/COPE models. These systems include HELLFIRE and extended range COPPERHEAD (Reference 4).

The purpose of this report is to document the structure of the PAM model so that other activities may more easily use it in related analyses. The report is organized as follows:

- The assumptions made in the course of constructing the model are discussed.
- A general overview of the model structure is presented.
- The way in which the acquisition portion of the COPPERHEAD trajectory is modeled is described in detail.
- The way in which the maneuver portion of the COPPERHEAD trajectory is modeled is described in detail.
- Appendix A lists the inputs required to drive the model, along with the appropriate units.
- Appendix B contains a copy of the FORTRAN SOURCE LIST.
- Appendix C gives a sample case with input and output.

²Cost and Operational Effectiveness Analysis (COPPERHEAD, COEA)(U), ACN 18812, US Army Field Artillery School, FT Sill, OK, October 1979, (SECRET report).

³Sandmeyer, Richard S., COPE Computer Program: User and Analyst Manuals, US Army Materiel Systems Analysis Activity, Aberdeen Proving Ground, MD, Technical Report to be published.

⁴Chernick, Julian A., Preliminary Analysis of Extended Range COPPERHEAD Operational Performance (U), GWD Interim Note No. G-85, US Army Materiel Systems Analysis Activity, Aberdeen Proving Ground, MD, January 1980, (CONFIDENTIAL report).

2. ASSUMPTIONS AND LIMITATIONS

As the name of the model suggests, the PAM model computes the Probability of a COPPERHEAD projectile being able to both Acquire a target by sensing reflected laser energy, and Maneuver to that target once it has been acquired. The fundamental difference between the probability of acquisition and maneuver (PAM) and probability of hit (P_H), is that estimates of P_H for COPPERHEAD-type systems must include the effect of laser energy overspill and underspill.

Such effects are a complex function of the entire time-history of laser pulses, and simulating those effects requires detailed modeling of the system's seeker logic. The Laser Designator Weapon System Simulation (LDWSS) model (Reference 5) does simulate the seeker logic, so the resulting estimates of P_H include the effects of laser energy overspill and underspill.

The PAM model does not simulate these effects; however, there is reason to believe that this limitation is not too severe. Section 2.3.2 of Reference 6 presents LDWSS estimates of P_H for the COPPERHEAD system under various conditions. Under conditions of high visibility, high cloud ceiling, low errors, and GLLD designator, it is plausible to assume that any degradation in P_H is due to spillover/spillunder. As the data shows, there is little degradation in P_H against a fully exposed moving target out to 3 km. Therefore there is little problem with spillover/spillunder against such a target out to 3 km. However, for a partially exposed target or a target at longer range, the spillover/spillunder problem is more severe. Under these conditions the probability of acquisition and maneuver is a poor estimator of probability of hit.

A second limitation of the PAM model is the use of a lambertian reflectance distribution (cosine law) of energy from the target rather than specific reflectivity maps generated from a three-dimensional target description. While significant differences could exist in terms of the actual shape of the acquisition volume for each reflected laser pulse, the spot jitter and the time-variability of target heading is probably sufficient to smooth out the shape of the acquisition volume in such a way that the cosine law is approximately correct.

Additional limitations arise because the model uses Monte Carlo sampling. The results are somewhat noisy (<10 percent) when a sample size of 100 is used; trends which intuitively should be monotonic are not always so. Moreover, when larger sample sizes are used, the model becomes fairly time consuming to run. Still, results of good quality can be obtained with greater ease and at lesser expense than by use of LDWSS; the LDWSS model also uses Monte Carlo sampling.

⁵Lewis, C.L., A.G. Nichols, and A.W. Lee, User's Guide for the Phase I Laser Designator/Weapon System Simulation (LDWSS) of the COPPERHEAD Guided Projectile System, Vol I, Technical Report RG-77-25, US Army Missile Command, Redstone Arsenal, AL, July 1977, (UNCLASSIFIED report).

⁶Independent Evaluation Report for the 155mm XM712 COPPERHEAD (U), IER No. 6-80, US Army Materiel Systems Analysis Activity, Aberdeen Proving Ground, MD, July 1979, (CONFIDENTIAL report).

3. GENERAL OVERVIEW

The overall flow of the main PAM model is shown in Figure 1. The most important part of the model is devoted to answering the two questions which appear near the center of Figure 1: "Does the projectile acquire?" and if so, "Can the projectile maneuver to the target?"

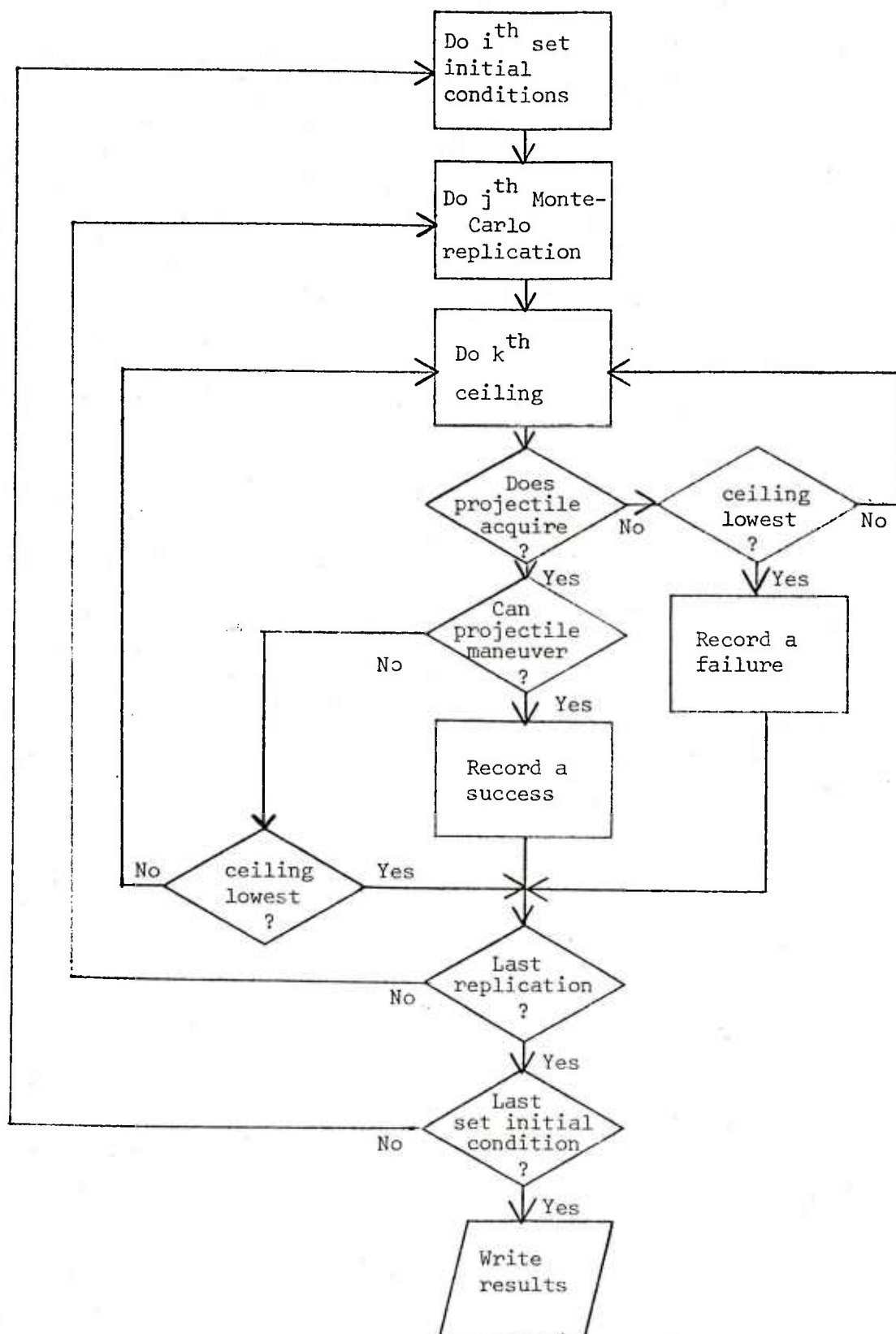
Figure 2 shows the general situation of a ground-based laser designating a target. The acquisition volume is the volume within which there is sufficient reflected laser energy for the COPPERHEAD projectile to acquire the target. The optical properties of the atmosphere determine the extent of laser energy attenuation along both the laser-target path and the target projectile path. The cloud ceiling acts as an energy cutoff level, prohibiting acquisition until the projectile descends below the cloud layer. Cloud cover is treated as opaque; beneath a cloud layer the visibility is assumed uniform.

Once the COPPERHEAD projectile breaks through a cloud ceiling, it acquires a target only if reflected laser energy reaches the seeker in sufficient quantity. This process is illustrated in Figure 3.

Since there is a ceiling at altitude A, acquisition is impossible above this ceiling. At altitude B, acquisition is possible but does not take place because insufficient energy reaches the seeker. At altitude C, sufficient energy reaches the seeker for acquisition to take place.

The (x,y) coordinates of intersection with the acquisition volume at a given altitude plane is a function of unguided delivery error. Given (x,y,z) coordinates of acquisition, the limits of projectile maneuver in the ground plane are fixed. For the case illustrated in Figure 3, the target is within the limits of projectile maneuver, so the engagement is a success.

FIGURE 1 CONCEPTUAL FLOWCHART OF PAM MODEL



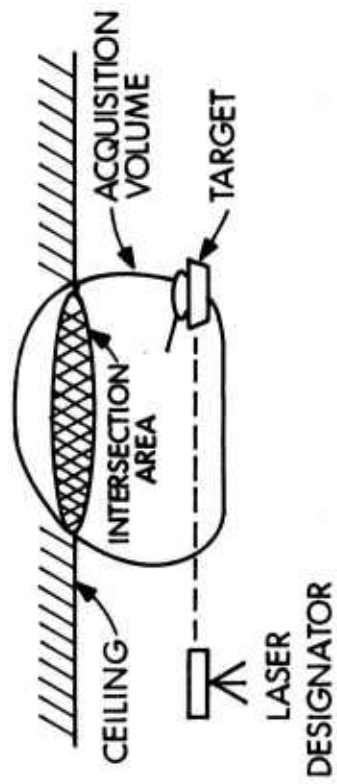
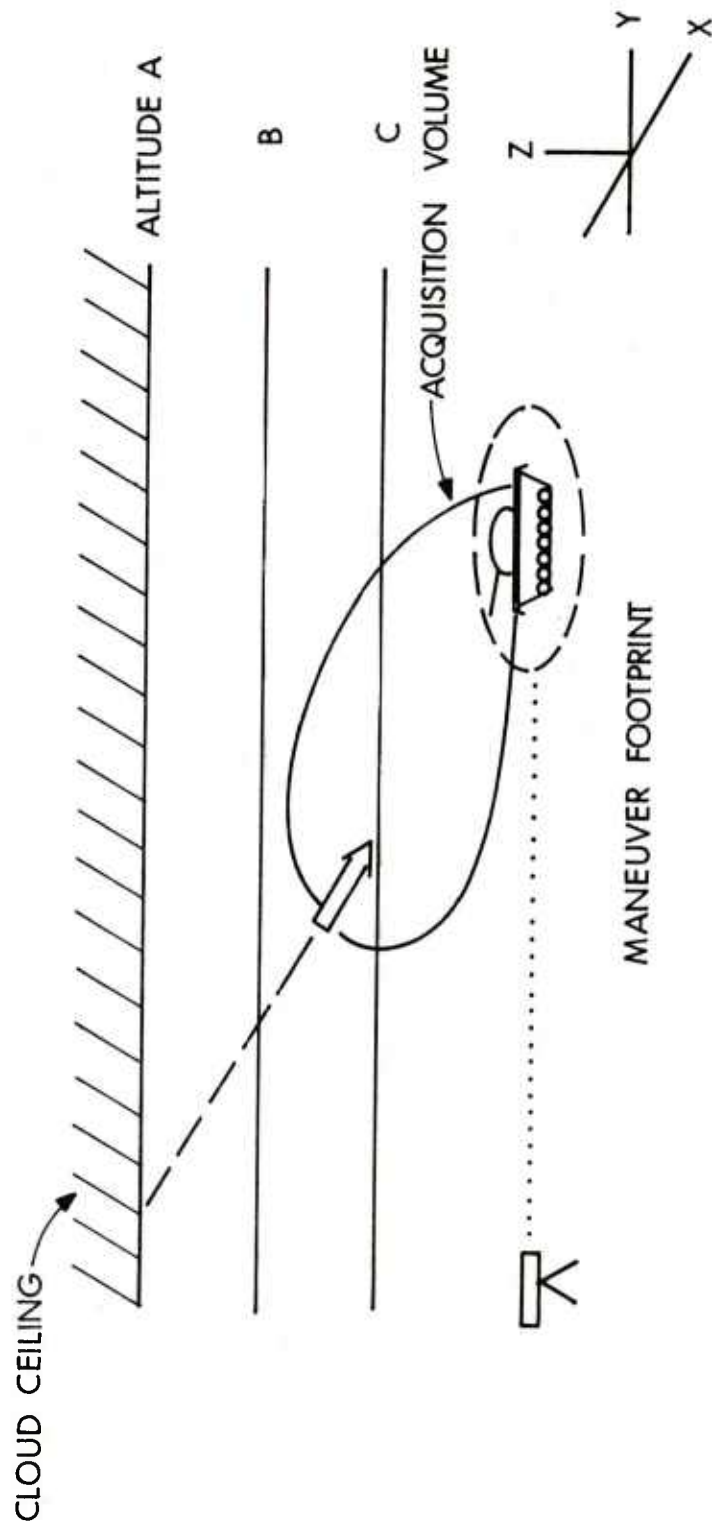


Figure 2 Laser Designating a Target.



CLOUD CEILING AT ALTITUDE A

NO ACQUISITION AT ALTITUDE B

ACQUISITION AT ALTITUDE C

Figure 3 Copperhead Acquisition and Maneuver.

4. ACQUISITION METHODOLOGY

The equations used in PAM to describe the laser energy transmission are the same as those used in the LDWSS model (Reference 5). The laser beam energy signal-to-threshold (S/T) ratio is:

$$S/T = \frac{E_d T_d T_s \rho \cos \theta}{\pi R_s^2 E_t}$$

where

E_t = threshold energy density at the seeker aperture (J/km^2)

E_d = laser designator energy (J)

T_d = designator-to-target transmission coefficient

T_s = target-to-seeker transmission coefficient

ρ = target reflectivity

θ = lambertian angle (angle from seeker LOS to designator beam)

R_s = slant range from target to seeker (km)

The transmission coefficients of the laser equation are complex functions of altitude, general atmospheric condition, and wavelength. These coefficients are calculated as functions of visibility, altitude (H_s), projectile range to the target (R_s) and designator range to the target (R_d) in km:*

$$T_d = e^{-R_d}$$

$$T_s = \begin{cases} e^{-\gamma \frac{1 - e^{-.00025H_s}}{.00025H_s}} R_s, & \text{for } H_s > 0 \text{ (Ft)} \\ e^{-\gamma R_s}, & \text{for } H_s \leq 0 \text{ (Ft)} \end{cases}$$

*It can be seen from examination of these two expressions that PAM and LDWSS both assume that electro-optical transmissivity improves as a function of increasing altitude. Recent work done at the Atmospheric Sciences Laboratory indicates that this assumption is not always true (Reference 7). During certain conditions of fog and haze, transmissivity may be as much as two orders of magnitude worse at 150m above the ground than at ground level.

⁷Pinnick, R.G., et.al., Vertical Structure in Atmospheric Fog and Haze and Its Effects on IR Extinction, Atmospheric Sciences Laboratory, White Sands Missile Range, NM, ECOM-TR-0010, July 1978.

The atmospheric attenuation coefficient (γ) is a function of visibility (VIS):

$$\gamma = \frac{.0019(.519)^Q}{VIS}$$

with Q determined as a function of visibility in kilometers:

$$\frac{VIS}{5}^{1/3}, 0 < VIS < 6$$

$$0.86 + \frac{VIS}{30}, 6 \leq VIS < 9$$

$$0.98 + \frac{VIS}{50}, \leq VIS < 12$$

$$1.15 + \frac{VIS}{200}, VIS \geq 12$$

The resultant visibility volume around the target has its maximum length along the direction of the designator and is of negligible extent for angles greater than 90 degrees from the designator-target line.

The model uses a nominal input value for angle T (FO-Target-Howitzer azimuth angle). However, the cosine law of reflectance is not applied directly to that angle, but to the input angle adjusted for the actual target location present in a particular Monte Carlo replication after unguided errors and target location errors are sampled.

5. MANEUVER METHODOLOGY

If, for a given Monte Carlo replication, the model determines that a COPPERHEAD projectile acquires a target, then computations are made to determine whether the projectile can maneuver to that target. This is accomplished by means of maneuverability footprints.*

For a given gun-target range, mode of fire, angle of fall, and altitude at which initial acquisition takes place, the footprints circumscribe an area in the ground plane within which a reliable projectile can successfully maneuver. This area is the intersection of the seeker field-of-view projected into the ground plane and the extreme limits of projectile maneuver capability. Because the footprints lack radial symmetry, they are input as a series of distances as a function of angle from the predicted target intercept point (PIP).

The model considers three kinds of error source: unguided delivery errors, random target location errors, and bias target location errors. Given values for these three error terms, the model determines whether the target is in the footprint at the time of round arrival.

Unguided delivery errors are associated with the part of the COPPERHEAD trajectory between launch and acquisition. Such errors have the effect of shifting the location of the footprint in the ground plane; they are monte carlo sampled for each simulated trajectory.

Standard deviations for these errors in range and deflection are shown in Figure 4. The information shown was supplied by Martin Marietta Corporation, and was generated by use of six-degree-of-freedom simulation techniques. Range errors are larger than deflection errors primarily because of COPPERHEAD's relatively shallow angle of fall. Although the range and deflection errors are not too different in the plane normal to the velocity vector, when they are projected into the ground plane, the range error becomes elongated.

*Both ARRADCOM and Martin Marietta Corporation have supplied AMSAA with these footprints. For details on the ARRADCOM model which generates footprints see Reference 8.

⁸Amoruso, Michael, J., Tice F. DeYoung, Dennis D. Ladd, and Roger D. Schulz, A Comprehensive Digital Flight Simulation of the Cannon Launched Guided Projectile, Rodman Laboratory, Rock Island, IL, January 1977, R-TR-77-007 (UNCLASSIFIED report).

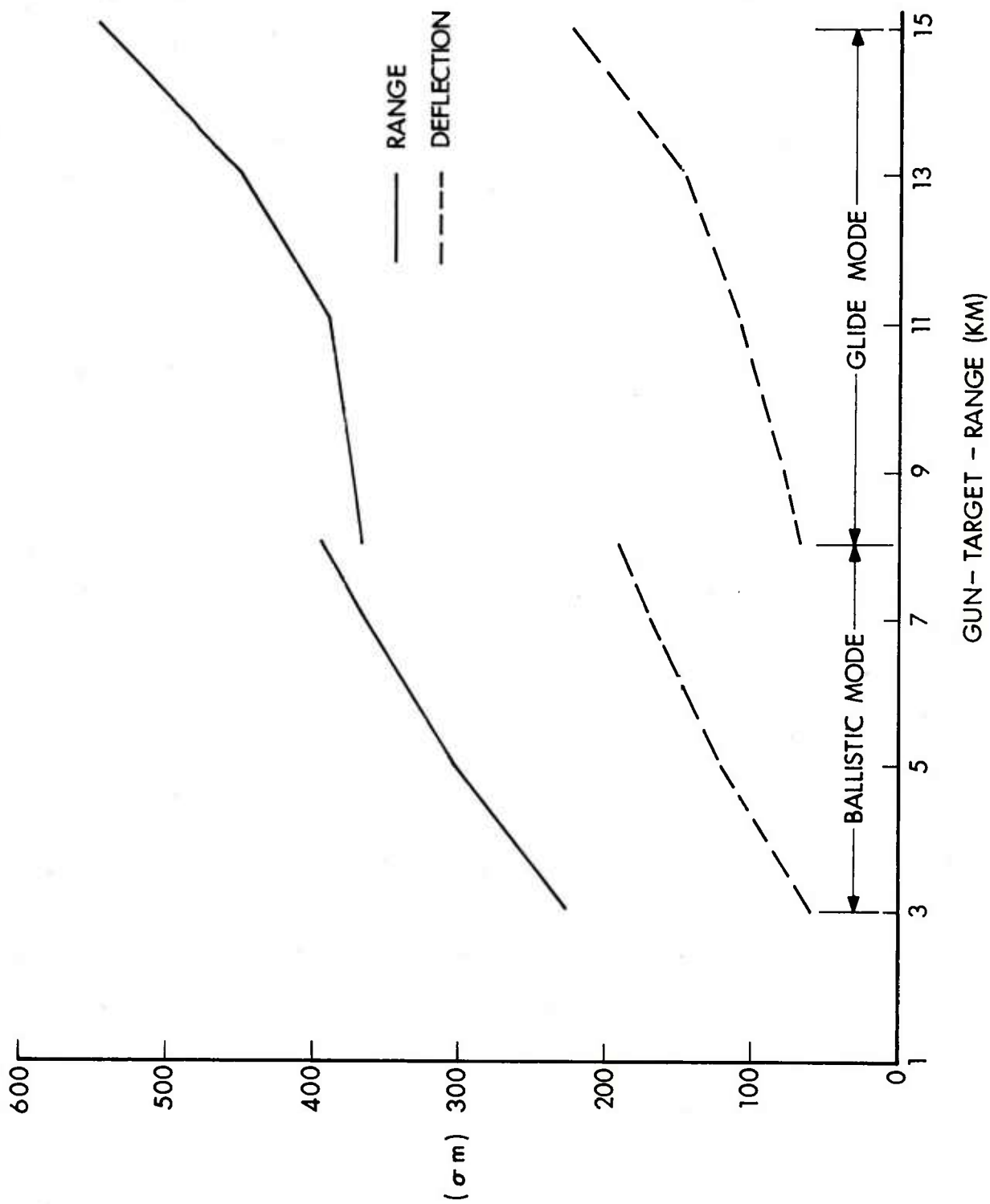


Figure 4. Unguided Delivery Errors

The random component of target location error (σ) can be input to PAM directly or computed internally according to the following algorithm derived from unpublished work of Julian Chernick.* The algorithm contains two error terms and a parameter:

$$\sigma^2_{TLE} = \sigma^2_{FO} + (\sigma^2_S \times T^2)$$

where

σ^2_{TLE} = variance of target location error

σ^2_{FO} = variance of FO/FDC error in locating FO position

σ^2_S = variance of FO error in estimating target speed

T = total system response time

The time term in the algorithm is the sum of the expected response time and the unanticipated delay time. Expected response time is the average time between the beginning of the FO's call for fire and the time of round arrival on target; it is an input to the model. Unanticipated delays are played parametrically in the model with values of 0, 30, 90, 150 and 300 seconds.

The random TLE algorithm above allows σ_{TLE} to be computed about a single target vehicle, for either a preplanned target or a target of opportunity. Since the PAM model was designed to evaluate COPPERHEAD against groups of target vehicles as well as against a single target vehicle, a method was derived to generate σ_{TLE} to the nearest target vehicle when more than one vehicle is present in a target.

Based on work reported in Reference 9, the following relationship is used for computing σ_{TLE} when the PIP is bracketed by target vehicles:

$$\sigma_{TLE} (\text{multiple}) = .68 \sigma_{TLE} (\text{single})$$

*A more general account of this type of error has recently been developed by Chernick (Reference 10). The numerical results, however, are similar to those resulting from the present algorithm.

⁹Weaver, Jonathan M., and Lawrence Bowman, Multiple Target Simulation (MUTSI) - A Discrete Monte Carlo Technique That Evaluates the Availability of Multiple Enemy Ground Targets in a GLLD/COPPERHEAD Target of Opportunity Situation, GWD Interim Note No. G-61, US Army Materiel Systems Analysis Activity, Aberdeen Proving Ground, MD, July 1979 (UNCLASSIFIED report).

¹⁰Chernick, Julian A., Moving Target Location Errors for Ground Targets, US Army Materiel Systems Analysis Activity, Aberdeen Proving Ground, MD, September 1980, to be published.

The final error source considered in the PAM model is a bias TLE. The random TLE discussed above is computed on the assumption that the mean target position at round impact is the PIP. This assumption will seldom be satisfied in combat, hence the resulting offsets from the PIP are treated as bias TLEs.

One important source of bias error is unanticipated delays in the time required to get a COPPERHEAD round on target. If the FO estimates it will take 100 seconds to get a round on target, but it actually takes 200 seconds, then the target may overrun the footprint before the round arrives.

In addition to the contribution of time delays to bias TLE, there are factors which could cause the target's point of closest approach (PCA) to the PIP to differ, on the average, from zero. If the footprint (aimpoint) is preplanned, it would be unreasonable to expect that potential targets would be headed directly towards the PIP. And for a target-of-opportunity, there is a possibility of large changes of direction after the command to fire is given.

Bias error is played in PAM as follows: If a COPPERHEAD projectile approaches the target from the direction of negative y, the x and y components of bias TLE are given by

$$XBIAS = PCA_x + \sin(H)V\tau$$

$$YBIAS = PCA_y - \cos(H)V\tau$$

where

PCA - point of closest approach

H - target heading angle

V - target velocity

τ - unanticipated delay

After these computations are made, the random and bias TLEs are summed to yield the target's location on the ground. The distance from that location to the PIP is computed, and is compared to the distance from the PIP to the edge of the maneuverability footprint for an equivalent angle. If the target is within the footprint, then the replication counts as a success; otherwise it does not.

6. SUMMARY

This report presents the general structure of the PAM model, and describes the modeling of the acquisition and maneuver positions of the COPPERHEAD trajectory in detail. In addition, a description of the input variables, a FORTRAN source listing, and a sample case are presented.

REFERENCES

1. Chernick, Julian A., Richard C. Scungio, Michael Starks, Utility of COPPERHEAD With Ground Laser Designation in a European Battlefield Environment (U), Technical Report No. 257, US Army Materiel Systems Analysis Activity, Aberdeen Proving Ground, MD, December 1978, (CONFIDENTIAL report).
2. Cost and Operational Effectiveness Analysis (COPPERHEAD, COEA) (U), US Army Field Artillery School, ACN 18812, Ft. Sill, OK, October 1979, (SECRET report).
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6. Independent Evaluation Report for the 155mm XM712 COPPERHEAD (U), IER 6-80, US Army Materiel Systems Analysis Activity, Aberdeen Proving Ground, MD, July 1979, (CONFIDENTIAL report).
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8. Amoruso, Michael, J., Tice F. DeYoung, Dennis D. Ladd, and Roger D. Schulz, A Comprehensive Digital Flight Simulation of the Cannon Launched Guided Projectile, Rodman Laboratory, Rock Island, IL January 1977, R-TR-77-007, (UNCLASSIFIED report).
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10. Weaver, Jonathan M., and Lawrence Bowman, Multiple Target Simulation (MUTSI) - A Discrete Monte Carlo Technique that Evaluates the Availability of Multiple Enemy Ground Targets in a GLLD/COPPERHEAD Target of Opportunity Situation, GWD Interim Note No. G-61, US Army Materiel Systems Analysis Activity, Aberdeen Proving Ground, MD, July 1979, (UNCLASSIFIED report).

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APPENDIX A
PAM INPUTS

APPENDIX A

PAM INPUTS

Table A-1 provides a list of the inputs required for the PAM model. These are read in with list-directed read statements as indicated in the FORTRAN listing in Appendix B.

In addition to the input variables which are read in, three arrays are filled in the program and the values could be changed at the discretion of the program user. These arrays are:

GAMARY (11)

H (6)

DTS (5)

The GAMARY array contains the laser energy attenuation coefficients, as a function of atmospheric visibility in km, from 1 to 11 km.

The H array defines the heights at which the check for acquisition is made, from highest to lowest, in meters.

The DTS array holds the values of unanticipated delay times played in seconds, as discussed in the Maneuver Methodology section of this report.

TABLE A-1 PAM INPUT VARIABLES

VARIABLE NAME	MEANING	UNITS
IMF	Mode of fire	1 = preplanned 2 = target of opportunity
ETH	Seeker Energy Threshold	Joules/SQKM
AOF	Fly under Fly out (FUFO) Angle of Fall	Degrees
TH	Target Heading Angle	Degrees
PCA	Point of Closest Approach	Meters
AZDT	Nominal Angle T	Degrees
V	Target Velocity	M/S
RHO	Target Reflectivity	N/A
ED	Designator Energy	Joules
TR	Nominal Response Time Including TOF	Seconds
NK	Number of Monte Carlo Cases	N/A
RNG	Gun Target Range	Meters
ACCX	Ballistic Error x (σ)	Meters
ACCY	Ballistic Error y (σ)	Meters
IDRMN	Minimum Designation Rng	Km
IDRMX	Maximum Designation Rng	Km
IVMX	Maximum Visibility Rng	Km
NI(J)	# of Pts in which Jth Footprint is input	N/A
THEMN(I,J)	Ith Angle from PIP in Jth footprint	Degrees
DISMH(I,J)	Ith Distance from PIP to edge of Jth Footprint	Meters

APPENDIX B
FORTRAN SOURCE LIST

APPENDIX B

FORTRAN SOURCE LIST

This Appendix contains a FORTRAN listing of the PAM model as configured for a CDC 7600 computer. The version of the program given here is for interface with the COPE model; comment cards at the beginning of the listing indicate necessary deletions for use as a stand-alone model.

Two subprograms, generally available as system routines (for example, on the Ballistic Research Laboratory computer at APG) are included to facilitate program portability. These are subroutines NRAN31 which generates pairs of normally distributed random numbers, and sub-routine DVDINT, which does divided difference interpolation.

```

1  PROGRAM PAM (INPUT,OUTPUT,TAPE5=INPUT,TAPE6=OUTPUT,TAPE7,TAPE11)
C
C  ** THIS VERSION OF PAM IS CONFIGURED FOR USE AS A PREPROCESSOR
C  ** FOR COPE. MAKE THESE CHANGES FOR STAND-ALONE RUNS:
C  ** 1. DELETE CALL TO OPENHS (FIRST EXECUTABLE STATEMENT)
C  ** 2. DELETE CALL TO PENAM2
C  ** 3. DELETE CALLS TO WRITMS AND CLOSMS
C  ** 4. DELETE SUBROUTINE PENAM2
C
10 DIMENSION ACQ(6,6), H(6), TOT(6), INDEX(6,5,2), PE(60,10,7),
1 AMTX(4260), INDX11(2001), THEMHI(11), TOT2(6,10), DISMH(11,6),
2 DISMH(11), THEMHI(11,6), NI(6), LKUP(7,5,2), PENG(70,10,6),
3 GAMAFY(11), DTS(5)
C
C EQUIVALENCE (AMTX(1),INDEX(1)), (AMTX(61),PE(1))
C
C REAL HDIS
C
C GAMARY HOLDS THE ATTENUATION COEFFICIENTS AS A FUNCTION OF RANGE
20 DATA GAMARY /2.6644, 1.2058, .7496, .5317, .4059, .3252, .2727,
1334, .2030, .1803, .1618/
PI=3.1416
C
C H ARRAY HOLDS ALTITUDES FOR WHICH ACQUISITION IS CHECKED
25 DATA H /-372.0, 9.4, 0, 762.0, 610.0, 457.0, 304.0/
C
C DTS ARRAY 'IDLS DELAY TIMES PLAYED
30 DATA DTS /0.0, 30., 90., 150., 300./
DATA IRN1 /1234567/
DATA IRN2 /7654321/
CALL OPENHS (11,INDX11,2001,1)
READ (5,*) IMF
IF (IMF.EQ.1) WRITE (6,300)
IF (IMF.EQ.2) WRITE (6,310)
READ (5,320) ETH
WRITE (6,330) ETH
35 SKSEN=ETH*1000000.
ADF=ADF*.0745329252
READ (5,*) ADF
READ (5,*) TH,PCA
READ (5,*) AZDT,V,RHO,DP,TR
WRITE (6,350) AZDT,V,RHO,DP,TR,ADF
WRITE (6,340) TH,PCA
IF (DP.EQ.-1) IDSG=-
IF (DP.EQ.07) IDSG=2
READ (5,*) HK,RNG,ACCX,ACCY
GTR=RNG/1000.
WRITE (6,360) HK,RNG,ACCX,ACCY
READ (5,*) IDRMN,IDRMX,IVMX
WRITE (6,370) IDRMN,IDRMX,IVMX
DO 110 J=1,6
110 READ (5,*) NI(J)
NIJ=NI(J)
WRITE (6,390) J,NI(J)
50 READ (5,*) (THEMH(I,J),I=1,NIJ)
READ (5,*) (DISMH(I,J),I=1,NIJ)
WRITE (6,380) (THEMH(I,J),I=1,NIJ)
000160
000170
000180
000190
000200
000210
000220
000230
000240
000250
000260
000270
000280
000290
000300
000310
000320
000330
000340
000350
000360
000370
000380
000390
000400
000410
000420
000430
000440
000450
000460
000470
000480
000490
000500
000510
000520
000530
000540
000550
000560
000570
000580
000590
000600
000610
000620
000630
000640
000650
000660
000670
000680
000690
000700
000710
000720

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FTN 4.8+508

PROGRAM PAH

76/76

UD POUND=+~*/

```

60      WRITE (6,400) (DISM(I,J), I=1,NIJ)
        DO 100 I=1,NIJ
          THENH(I,J)=THENH(I,J)*0.01745329252
        CONTINUE
110      CALL PENAN2 (TR, IDSG, V, GTR, RHO, AZDT, PCA, TH, SKSEN, IDCDE)
        WRITE (6,420) IDCDE, IDCDE
        WRITE (6,420) V, TR, DP, PHO
          C
          C
70      TH=TH*.01745329252
        DO 240 IDR=IDRIN, IDR!X
          RD=FLOAT(IDR)
          DO 230 IV=1, IVHX
            DO 220 IDELT=1, 5
              DT=DTS (IDELT)
            DO 210 INTS=1, 2
              C JUDGE SIGMA OF RANDOM TLE
              TLOC=SQRT(2500.+(TR+DT)**2)
              IF (INTS.EQ.1) TLOC=SQRT((2500.+1.5*((TR+DT)**2.)))
              IF (INTS.EQ.2.AND.IDELT.EQ.1) TLOC=.68*TLOC
            C
            C COMPUTE COORDINATES OF POINT OF CLOSEST APPROACH
            PCAX=PCA*COS(TH)
            PCAY=PCA*SIN(TH)
            C COMPUTE TARGET COORDINATES FOR GIVEN DELAY/VELOCITY
            BIASX=PCAX+(SIN(TH)*V*DT)
            BIASY=PCAY-(COS(TH)*V*DT)
          C
          C
90      BEGIN MONTE CARLO LOOP BY SAMPLING TLE
        DO 350 K=1, HK
          CALL IRAN31 (SX1, SX2, IRN1)
          TLOCY=SC*TLOC
          TLOCX=SC2*TLOC
          C
          C SUM RANDOM ERROR TO BIAS ERROR
          TLEY=TLOCX+BIASX
          TLEY=TLOCY+BIASY
          C
          C SAMPLE BALLISTIC ACCURACY
          CALL IRAN31 (SX1, SX2, IRN2)
          BIPY=SC*ACCY
          BIPX=SC2*ACCX
        C
        C
100     C
          C
          C ACQUISITION VOLUME ENERGY COMPANISON
        DO 340 IC=1, 6
          DO 130 IA=IC, 6
            YINT=-H(IA)*COT(ADF)+BIPY
            XINT=BIPX
            X=(TLEX-XINT)
            Y=(TLEY-YINT)
            ALPHA=ATAN2(X,Y)
            ANGSIN=(AZDT*.01745329252)+ALPHA
            GAM=GAMAPY(IV)
            TD=EXP(-GAM*RD)
            IIS=(H(IA)*3.28)
            PS=SQRT((XINT-TLEX)**2.+(YINT-TLEY)**2.+H(IA)**2.)

```

```

115 RS=RS/UGGQ.0
    TS=EXP((-GAM*RS)*(1.-EXP(-(00025*HS)))/(00025*HS))
    TFACT=COS(ANGSUM)
    ES=(DP*TD*TS+RHD*TFACT)/(PI*RS*PS)
    IF (ETH.GT.ES) GO TO 130
C
120 MANUEVERABILITY FOOTPRINT DISTANCE COMPARISON
C
C
    TANG=ABS((TLEY-BIPY)/(TLEX-BIPX))
    BETA=ATAN(TANG)
    BETA=1.5708-BETA
    IF (TLEY.LT.BIPY) BETA=3.1416-BETA
    DIST=SQRT((TLEX-BIPX)**2.+(TLEY-BIPY)**2.)
    HIJ=HI(IJA)
    DO 120 J=1,NIJ
    THEMHI(J)=THEMH(J,IA)
    DISMHI(J)=DISNH(J,IA)
120 CONTINUE
    CALL OVDRINT (BETA,HDIS,THEMHI,DISMHI,NIJ,2)
    IF (OIST.GT.HDIS) GO TO 130
    ACQ(IC,IA)=ACQ(IC,IA)+1.0
    GO TO 140
C
130 CONTINUE
140 CONTINUE
150 CONTINUE
C
C
    ACCUMULATE RESULTS OVER CEILING AND ALTITUDE
    DO 160 IC=1,6
    DO 160 IA=1,6
    ACQ(IC,IA)=ACQ(IC,IA)/FLOAT(NK)
    TOT(IC)=TOT(IC)+ACQ(IC,IA)
160 WRITE(6,102)(H(IC),IC=1,6),(H(IA),(ACQ(IC,IA),IC=1,6),IA=1,6)
C
C
    WRITE(6,100) (TOT(IC),IC=1,6)
C
C
    INDEX RESULTS FOR COPE INTERFACE AND FOR TAPE6 OUTPUT
    DO 170 II=1,6
    JPE=10*(II-1)+2*(IDELT-1)+IMTS
    INDEX(II,IDELT,IMTS)=JPE
170 PE(JPE,IV,IDR)=TOT(II)
    DO 180 II=1,6
    IPE=10*(IDR-1)+2*(IDELT-1)+IMTS
    LKUP(IDR,IDELT,IMTS)=IPE
180 PENG(IPE,IV,II)=TOT(II)
    DO 190 IC=1,6
    TOT2(IC,IV)=TOT(IC)
190 CONTINUE
    DO 200 IC=1,6
    DO 200 IA=1,6
    ACQ(IC,IA)=0.
    TOT(IC)=0.
200 CONTINUE
210 CONTINUE
220 CONTINUE
230 CONTINUE
240 CONTINUE
    DO 250 I=1,7

```



```

1  SUBROUTINE DVDINT (X,FX,XT,FT,NP,ND)
   DIMENSION XT(NP), FT(NP), T(16)
   N=ND
   N1=(N-1)/2
   N2=N/2
   N3=NP-N2+1
   IF (NP-N) 250,100,100
   -00 N4=N+2
   IF (XT(1)-XT(2)) 110,330,260
10  CONTINUE
   IF (X-2.*XT(1)+XT(2)) 240,240,120
120 IF (X-2.*XT(NP)+XT(NP-1)) 130,130,240
   -30 IF (NP,LT,0) GO TO -50
15  N5=NP-1
140 N5=N5/2
   N6=N4+N5
   IF (XT(N6).LT,X) N4=N6
   IF (N5.GT,1) GO TO 140
150 IF (X-XT(N4)) 180,160,160
160 IF (N4-N3) 170,180,170
170 N4=N4+1
   GO TO 150
180 N4=N4-1
   N5=N4-N1
   DO 190 I=1,N
   T(I)=FT(N5)
190 N5=N5+1
   L=(N+1)/2
   TR=T(L)
   N6=N4
   N7=N4+1
   JU=1
   N2=N-1
   UN=-1
   DO 230 J=1,N2
   N5=N4-N1
   N3=N-J
   DO 200 I=1,N3
   N8=N5+J
   T(I)=(T(I+1)-T(I))/(XT(N8)-XT(N5))
200 N5=N5+1
   GO TO (210,220), JU
210 UN=UN*(X-XT(N6))
   JU=2
   N6=N6-1
   GO TO 230
220 UN=UN*(X-XT(N7))
   JU=1
   N7=N7+1
   L=L-1
230 TP=TR+UN*T(L)
   FX=TP
   RETURN
240 WRITE (6,340) X,XT(1),XT(NP)
55 250 WRITE (6,350) NP,ND
   STOP
   C TOP
002350
002360
002370
002380
002390
002400
002410
002420
002430
002440
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002840
002850
002860
002870
002880
002890
002900
002910

```



```

1      C
      SUPERROUTINE NRAM31 (X1,X2,I)
      X3=SQRT((-2.0*ALOG((NRAM31(I))))
      X4=6.2831853072*NRAM31(I)
      X2=X3*SIN(X4)
      X1=X3*COS(X4)
      RETURN
      END
5
003140
003150
003160
003170
003180
003190
003200
003210

```

SYMBOLIC REFERENCE MAP (R=)

ENTRY POINTS
3 NRAM31

VARIABLES	SN	TYPE	RELOCATION		
0 I		INTEGER	F.P.		
U X2		REAL	F.P.		
32 X4		REAL		0 X1 31 X3	F.P.
EXTERNALS		TYPE	ARGS		
ALOG		REAL	1 LIBRARY	COS	1 LIBRARY
SIN		REAL	- LIBRARY	SQRT	1 LIBRARY
NRAM31		REAL	-		
STATISTICS					
PROGRAM LENGTH	550008	SCN USED	338	27	

07/10/80 10.11.52

FTN 4.8+508

UD ROUND=+-*/

76/76

SUBROUTINE PENAN2

```

1      SUBROUTINE PENAN2 (TR,IOT,VEL,GTR,REFL,ANGLET,DEFB,TGTHD,SKSEN,
      1  IOCODE)
      COMMON /XVALUE/ XVALUE(8,9,2)
      DIMENSION AVALUE(9), IP(9)

      * * * * * FILL IN XVALUE COMMON BLOCK * * * * *

      DATA (((XVALUE(I,J,K),I=1,8),K=1,2),J=1,9) /
      DUHHY SLOTS FOR NOMINAL RESPONSE TIMES
      1  0*0.,
      2  8*8.,
      1  1., 2., 3., 5*0.,
      2  0., 1., 1., 5*8.,
      1  2., 3., 5., 8., 3*0.,
      2  0., 0., 1., 2., 3*8.,
      1  8., 12., 20., 30., 40., 10., 16., 0.,
      2  0., 1., 2., 3., 4., 5., 6., 8.,
      1  .05, .10, .20, .30, 4*0.,
      2  0., 1., 2., 3., 4*8.,
      1  0., 25., 30., 60., 90., 120., 2*0.,
      2  0., 1., 2., 3., 4., 5., 2*8.,
      1  -200., -100., 0., 100., 200., 3*0.,
      2  0., 1., 2., 3., 4., 3*8.,
      1  -60., -30., 0., 30., 60., 3*0.,
      2  0., 1., 2., 3., 4., 3*8.,
      1  12., 18., 24., 30., 36., 3*0.,
      2  0., 1., 2., 3., 4., 3*8./

      AVALUE(1)=TR
      AVALUE(2)=IOT
      AVALUE(3)=VEL
      AVALUE(4)=GTR
      AVALUE(5)=REFL
      AVALUE(6)=ANGLET
      AVALUE(7)=DEFB
      AVALUE(8)=TGTHD
      AVALUE(9)=SKSEN

      DO 110 J=2,9
      DO 100 I=1,8
      IF (ABS(AVALUE(J)-XVALUE(I,J,1)).GT..001) GO TO 100
      IP(J)=XVALUE(I,J,2)+.5
      GO TO 110
100  CONTINUE
      STOP , IN PENAN2: ERROR NUMBER 1'
110  CONTINUE

```

```

C
60      DO 120 J=2,9
          IF (NP(J).GE.8) STOP * IN PENAH2: ERROR NUMBER 2 *
          120 CONTINUE
C
65      IF (TR.LE.0.O.OR.TR.GE.999.5) STOP * IN PENAH2: ERROR NUMBER 3 *
          NCODE=TR+.50
          DO 130 J=2,9
            130 NCODE=8*NCODE+NP(J)
C
70      ENCODE=(10,170,IDCODE) NCODE
C
          RETURN
C
75      * * * * *
          ENTRY PEIDHT
C
          DECODE=(10,180,IDCODE) NCODE
C
          DO 140 J=2,9
            NP(11-J)=MOD(NCODE,8)
            NCODE=NCODE/8
          140 CONTINUE
C
85      NP(1)=NCODE
          DO 160 J=2,9
            DO 150 I=1,8
              IF (ABS(FLOAT(NP(J))-XVALUE(I,J,2)).GT..0001) GO TO 150
              AVALUE(J)=XVALUE(I,J,1)
            GO TO 160
          150 CONTINUE
          160 CONTINUE
C
95      AVALUE(1)=NCODE
C
          TR=AVALE(1)
          IDI=AVALE(2)
          VEL=AVALE(3)
          GTP=AVALE(4)
          REFL=AVALE(5)
          ANGLET=AVALE(6)
          DEFID=AVALE(7)
          TGTID=AVALE(8)
          SKSEN=AVALE(9)
C
          RETURN
C
105
C
110      * * * F O R M A T   S T A T E M E N T S * * *
          170 FORMAT (4HPE00,R6)
          180 FORMAT (4X,R6)
          END

```

APPENDIX C
SAMPLE CASE

APPENDIX C

SAMPLE CASE

A list of input values as used in a sample PAM run is shown in Table C-1. These values are for the purpose of illustration only. The values are read into the input variables in the order that those variables are listed in Table A-1. For example, the first card indicates that the program run is for a preplanned footprint situation; the second card indicates that the seeker sensitivity being played is .00003 Joules/Km².

Part of the output which resulted from running the program with the sample input stream is shown in Figure C-2. For each combination of designation range and unanticipated delay time there is a 6 x 10 output matrix. In addition, for the case where there is no unanticipated delay, probabilities are printed for both single and multiple target TLEs.

Output values are configured in each matrix as follows:

Highest ceiling Lowest Ceiling

Visibility = 1 Km

·
·
·

Visibility = 10 Km

Variable
(See Table A1)

Sample Values(s)

IMF	1
ETH	.000030
AOF	20.0
TH,PCA	0.0.0.0
A2DT,V,RHO,ED,TR	25.0.5.,.10.,.1,106.
NK,RNG,ACCX,ACCY	100,8000.,73.,366.
IDRMN,1DRMX,IVMX	1,7,10
NI(1)	8
THEMN(1,8)	0.0.20.,30.,45.,60.,90.,135.,180.
DISMH(1,8)	1200.,1100.,1200.,1000.,600.,500.,400.,700.
NI(2)	8
THEMN(2,8)	0.,20.,30.,45.,60.,90.,135.,180.
DISMH(2,8)	1200.,1100.,1200.,1000.,600.,500.,400.,700.
NI(3)	8
THEMN(3,8)	0.,20.,30.,45.,60.,90.,135.,180.
DISMH(2,8)	1100.,1000.,1100.,900.,500.,400.,300.,700.
NI(4)	8
THEMN(4,8)	0.,20.,30.,45.,60.,90.,135.,180.
DISMH(4,8)	1000.,900.,1000.,800.,500.,300.,300.,500.
NI(5)	8
THEMN(5,8)	0.,20.,30.,45.,60.,90.,135.,180.
DISMH(5,8)	600.,500.,600.,400.,500.,400.,400.,600.
NI(6)	8
THEMN(6,8)	0.,20.,30.,45.,60.,90.,135.,180.
DISMN(6,8)	400.,300.,400.,300.,400.,300.,300.,400.

FIGURE C2 SAMPLE PAM INPUTS

PROBABILITIES OF ACQUISITION AND MANEUVER

<u>Visibility Range (km)</u>	<u>Designation Range 1 km Time Delay 30s Cloud Ceiling (Ft)</u>					
	4500	3000	2500	2000	1500	1000
1	.20	.20	.20	.20	.20	.16
2	.48	.48	.46	.44	.44	.24
3	.46	.46	.40	.34	.31	.22
4	.54	.54	.51	.49	.47	.30
5	.54	.54	.49	.47	.45	.28
6	.54	.54	.49	.44	.39	.25
7	.51	.51	.47	.44	.42	.29
8	.54	.54	.50	.48	.48	.28
9	.45	.45	.40	.36	.33	.21
10	.55	.55	.48	.45	.42	.25

FIGURE C2 SAMPLE PAM OUTPUT

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