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FREDERICK ROBERTSON HABERLANDT

Submitted to the Department of Ocean Engineering in May 1978, in partial fulfillment of the requirements for the Degree of Ocean Engineer and the Degree of Master of Science in Naval Architecture and Marine Engineering.

ABSTRACT

Two distinct aspects of computer aided ship design are addressed in this thesis. First, a geometrical hull form modification technique employing the longitudinal repositioning of sections is developed. The second aspect deals with the mathematical representation of lines and line fairing. Before this is done however, justification is presented for utilizing third degree polynomials as an approximation to the spline curves of the naval architect. The results obtained indicate that a fairing procedure based on a least squares curve fitting criteria and a lines representation procedure based on parametric cubic equations could be adapted to generate faired hull forms from the roughest preliminary hull design. Additionally, the hull form modification technique could be programmed so as to produce designs with desired values of $C_{\rm D}$, LCB, $C_{\rm W}$ and LCF from a basis design of similar type.

Thesis Supervisor: Professor Chryssostomos Chryssostomidis Title: Associate Professor of Naval Architecture

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FREDERICK ROBERTSON HABERLANDT

B.S., Mechanical Engineering, University of Florida (1971)

> Submitted in Partial Fulfillment of the Requirements for the Degree of

> > OCEAN ENGINEER

and the Degree of

MASTER OF SCIENCE IN NAVAL ARCHITECTURE AND MARINE ENGINEERING

at the

MASSACHUSETTS INSTITUTE OF TECHNOLOGY

May, 1978

(c) Frederick Robertson Haberlandt 1978

Department of Ocean Engineering May 12, 1978

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TABLE OF CONTENTS

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i.

فتنابعا القاف فالمحافظ فالمحدين فستنتخص والمتعملات منيين الأناس المعترك فالكر

																									Page
TITI	e Pi	AGE.	•	•	•	•	•	•	ļ	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	1
ABSI	RAC!	c	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	2
ACKN	IOWL	EDGE	MEN	ITS			•					•	•		•			•		•	•	•	•	•	3
TARI	e oi	22.5	NT	-	S	-	_	_			_			_	_				_	_	_		_		4
	OF																					•	•	•	- 7
						-	-	-														•	•	•	, 9
1.	Inti																				•	•	•	•	
	1.1 1.2	Bac The	kgi sis	i C	nd on	te	nt	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	9 10
2.	Meti	bod	of	Hu	11	F	or	m	Mc	ibc	ļfj	ica	ti	on	l •	•	•	•	•	•	•	•	•	•	13
	2.1	Bac	:kg1	ou	nd	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•		•	13
	2.2	Dev	reic	pm	en	t	•	•	•	•	•		•	•	•	•	•	•	•	•	•		•	•	21
		2.2	2.1	Th Va	e ry	"O in	ne g	t t	(ir. 1e	nus Fr	8 F 111	Pri .ne	.sn .89	at	ic f	ar	Va E	iri Int	.at :ra	ic inc	חל	•	•	•	21
		2.2	2.3	Mi	đđ	le	ba	d	7.	•	•	•			•						to		٠	•	24
				Ac Se																			•	•	31
		2.2	2.4	A	Me	th	od	ł	y	Wł	lic	h	Cc		itz	a i	int	:8	ma	y	be)		•	33
		2.2	2.5		Me	th	od	1	y	wł	lic	h	Čc	ns	itz	:ai	Int	:8	ma	y	be	•		•	38
3.	Matl		م 4 ه									-										•	•	•	50
3.	Ship																					•	•	•	40
	3.1																								40
	3.2	Jev 3.2	.1	De	ri	va	ti	or) ()f	tł)e	Sp) 11	ne	• 0	.ut	sic	;						42
		3.2	2.2											:ia Sen										٠	42
		3.2	2.3											•							- im	al	•	٠	49
				Ap																			•		54
		3.2	2.4	Th		Ro	ta	ti	Ing	7 S	Sp]	lir	18	•	•	•	•	•	•	•	•	•	•	٠	59

4.	Mathematical Fairing of Lines
	4.1 Background
	4.2 Development
	4.2.1 The Least-Squares Criteria for Defining the Cubic Curve
	the Cubic Curve
	4.2.2 The Moving Strip Method
	4.2.2.1 STRIP1
	4.2.2.2 STRIP2
	4.2.2.3 STRIP3
	4.2.2.4 TRANS1
	4.2.3 Fairing of Curves with Infinite Slope
	4.2.3 Fairing of Curves with infinite Slope /0
	4.2.3.1 Other Transformations
5.	Computer Algorithms
	5.1 Overview
	5.1.1 Specification of Point Type
	5.1.2 Specification of End Conditions
	5.1.3 Storage of Pertinent Line Data
	5.2 Description of Subroutines
	5.2.1 Lines Fairing
	5.2.1.1 Subroutine PREFAR
	5.2.1.1 Subroutine PREFAR
	5.2.1.2 Subroutine FARCRV
	5.2.1.3 Subroutine FARLIN
	5.2.1.4 Subroutine FSTPTS
	5.2.1.5 Subroutine TRANS1
	5.2.1.5 Subroutine TRANS1
	5.2.2 Lines Representation
	5.2.2.1 Subroutine PRESPL
	5.2.2.2 Subroutine SPLINE
	5.2.2.3 Subroutine INTERP
	5.2.2.4 Subroutine CALCY
	5.2.2.5 Subroutine CALCT
6.	Comclusions and Recommendations
	6.1 Hull Form Modification
	6.2 Mathematical Representation of Lines and
	Fairing
	6.2 Mathematical Representation of Lines and Fairing
	6.2.2 Fairing
	6.2.2 Fairing
REF	ERENCES

APPENDIX	A.	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	.106
APPENDIX	B.	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	.108
APPENDIX	c.	•	•	•	•	•	٠	•	•	٠	•	•	•	•	•	•	•	•	•	•	•	•	.112
APPENDIX	D.	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	.116
APPENDIX	E.	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	.120
APPENDIX	F.	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	٠	•	•	.123
APPENDIX	G.	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	٠	•	•	.156

LIST OF FIGURES

2.1	Ship's Lines
2.2	Sectional Area Curve
2.3	Sectional Area Curve (with parallel middlebody) . 21
2.4	Sectional Area Curve
2.5	Sectional Area Curve
2.6	Sectional Area Curve
2.7	Sectional Area and Waterline Curves
2.8	Coefficient Ratio Curve
3.1	Strained Beam Element
3.2	Discretely Loaded Beam
3.3	Spline Curve Fitting Routine
3.4	Rotating Spline Routine
4.1	Least Squares Fit
4.2	Pinned End
4.3	Clamped End
4.4	Axis Rotation
5.1	Point Type Examples
6.1	Control Lines for a Typical Bulbous Bow Destroyer

B.1	Sectional Area Curve
c.1	Section Modification
D.1	Rotating Spline Routine
F.1	Flowchart of Fairing Subroutines
F.2	Flowchart of Splinning and Interpolation Subroutines
G.1	Bow Section

1. Introduction

1.1 Background

Because of the environment in which they operate, the seakeeping characteristics of a ship are of paramount importance when assessing its overall performance. In the past this aspect of a ship's performance had to be judged by the results of model tests conducted at a point in time well into the preliminary design phase. While these tests provide results of good quality, they were not obtained until the pending design was quite firmly established. In fact, the results obtained by model tests had the characteristic of being just that, results, rather than an important input into the design cycle. The obvious desire then would be to have a tool capable of providing accurate predictions of seakeeping performance based on the data available in the conceptual design phase. These predictions could then be used to influence the selection of hull form coefficients, etc. prior to the time when the hull form is actually being generated.

In 1975 Professors T. Loukakis and C. Chryssostomidis published the "Seakeeping Standard Series for Cruiser-Stern Ships".^[1] This paper corrolates the seakeeping behavior, as predicted by computer model, of the Extended Series 60

hull forms and sets forth a method by which the performance of this type of ship may be predicted based on five parameters: Froude number, F; ratio of significant wave height to ship length, S; beam/draft ratio, B/T; length/beam ratio, L/B; and block coefficient, CB. With this procedure a designer can predict the relative merits of various candidate designs at a very early stage. This represents a significant capability.

As a result of the work represented in reference [1] there is considerable interest in generating a similar seakeeping series for contemporary cruiser/destroyer type hull forms. In order to do this in the fashion of reference [1], a representative sample of the ship type must be analyzed by computer model and then the results corrolated. It was this need for sample hull forms that provided the motivation for this thesis.

1.2 Thesis Content

There are two aspects of hull form generation addressed in this thesis: first, hull form modification and second, mathematical lines representation and fairing. The technique of hull form modification developed in chapter two is based on the work of H. Lackenby reported in reference [2]. The essence of this method is that the sectional area curve

of an existing ship is redrawn in a systematic fashion to produce a curve with the desired values of prismatic coefficient, C_p , and longitudinal center of buoyancy, LCB. The sections are then shifted longitudinally to produce a modified form with these characteristics. In applying this technique to destroyer type ships there were several anomalies encountered which required that the method of Lackenby be further modified. These modifications, with the pertinent background are contained in chapter two.

The other aspect of lines generation which is addressed in chapters three and four is mathematical lines representation and fairing. Although the fairness of a hull form is not critical to the seakeeping analysis it is an unavoidable subject when considering computer aided ship design. In these chapters the use of parametric cubic splines and least squares curve fitting are addressed. While the parametric splines are shown to provide the capability of representing virtually any type of line, the least squares fairing technique is limited to use with curves representable by single valued functions. The algorithms are, however, capable of fairing lines with infinite slopes at the end points.

It is anticipated that the tools developed in this thesis could be readily fused into a single computer program with the capability of modifying an existing ship form to

obtain a faired design with the desired coefficients of form. When this is developed it will be possible to generate rapidly any number of designs for subsequent performance analysis. The implications of this are discussed in chapter six.

2. Method of Hull Form Modification

2.1 Background

During the design of all but the most trivial engineering systems, it is incumbent upon the engineer that he or she formulate a model of that system. Additionally, the designer must continually refine the model with each successive iterative cycle so that the results are of sufficient detail to be meaningful [3]. One such model used during ship design is a geometric description of the ship's hull form. The most traditional manner of providing this information is by way of the lines drawing.

The ship's lines drawing, more frequently referred to as the ship's lines, is a set of three orthogonal views of the ship's hull depicting the lines of intersection of various planes with the hull form. When viewed in conjunction with one another, they provide the capability to spatially locate any point on the moulded surface of the ship. Figure 2.1, taken from reference [4], is an example of a lines drawing for a "Mariner"-class, steel hull cargo vessel.

While the lines drawing, prepared manually by the naval architect and draftsman, has been the older and more traditional means of depicting the geometric properties of a ship,



the advent of the high speed computer has provided great impetus for defining the ship's form in a mathematical format [5]. It is interesting however, that a very successful attempt was made at representing ship's lines mathematically by Admiral David Taylor in the early 1900's [6]. This will be expanded upon a bit later.

When first confronted with the job of creating the lines of a new ship, the naval architect seeks a means of quantifying the expected form of the vessel so that he may strive to create an "optimum" design. These optimizing criteria generally take the form of requirements and restrictions placed on the various coefficients of form, i.e., C_p , C_w , LCB, LCF, etc. However, there might also be requirements placed on certain specific regions of the ship. An example of this could be the shape of the midships section for a cargo vessel or the stern configuration dictated by propeller and rudder selections. Nonetheless, when the naval architect completes his candidate design, the important product will be a faired set of ship's lines meeting all the optimizing criteria previously established.

The above procedure is clearly long and involved. For this reason much effort has been expended to develop hull form modification techniques. The objective of these procedures is to utilize an existing, successful hull design, or parent form, as a basis and then to alter this form in a

systematic fashion. This modified form should have the desired characteristics, and, hopefully, require little additional refairing. It is this fairing procedure, described in chapter 4, which requires a large proportion of the designer's effort. The remainder of this chapter addresses the modification techniques themselves.

One of the oldest and most widely used methods of hull form modification is illustrated in Figure 2.2. In essence, the sectional area curve of an existing ship is altered by some arbitrary or systematic method to produce a curve which satisfies some criteria of the designer, usually prismatic or block coefficient and longitudinal center of buoyancy. The offsets for the new design are then obtained by taking the section in the parent whose ordinate in the sectional area curve matches the ordinate of the derived curve. This is represented by the movement of section A at position X_ in the parent to section A' at position X_a , in the derived hull form. Hence, it is merely a longitudinal repositioning of the existing sections. This method works reasonably well as long as the shifts are of "moderate" amount and the designer is prepared to accept the resulting profile and waterlines without alteration.



The above method lends itself quite well to design without the aid of computers or other automatic computational devices. However, in recent years there has been much work done in the area of hull form modification with the use of high speed digital computers. In virtually all cases where computers are used, an effort is made to represent the ship's contours or surface regions [5] in a mathematical format. It is for this reason that the "Taylor Standard Series" is of interest. It was Admiral David Taylor who, in the early 1900's, generated one of the first successful hull series based on representing the sectional area curve and design waterlines by fifth degree polynomials [6].

Another procedure of hull form modification utilizes specific transformation functions to alter various regions or characteristics of the hull [7]. This form of

modification provides the user with much greater control over the specific ship form than the method of shifting sections longitudinally as previously described. An interesting description of this type of procedure may be found in reference [7].

It is, however, the method of longitudinally shifting sections which was selected for development in this thesis. The reasons for its selection are twofold. First, preliminary work with destroyer-type ships conducted at M.I.T. during the summer of 1977, indicated that the results of the modification were quite realistic and not plagued by gross unfairness. Secondly, the method was tractable and readily adopted to the peculiarities of destroyers. Those peculiarities being principly the fact that this type of ship has no parallel middle body and also that the section of maximum area, in most cases lies at a location other than midship.

The specific method of modification used is that of Lackenby [2] as subsequently modified by Moor [8], and then again by this author. Briefly, the developments presented in reference [2] are highly general, permitting the designer to vary the value of prismatic coefficient, C_p , and the longitudinal center of buoyancy, LCB, of a very wide variety of ships. Included was the capability of altering, or retaining unchanged, the parallel middle bodies of ships so configured. However, one serious drawback was that the method left no

control over the design waterline, and while this line might turn out fair, the longitudinal center of floatation, LCF, merely ended up where it did. It was to this problem that Moor [8] was concerned. By addressing himself to both the sectional area curve and the design waterline in the manner of Lackenby, and then coupling the two procedures, he was able to obtain a derived form having the desired values of C_p , C_w , LCB and LCF.

At this point only one minor problem existed with the method as it stood. For ships with keelrise fore or aft it was possible to obtain unwanted oscillations in the ship's centerline profile. To eliminate these oscillations, this author extended the logic of Moor to include the ship's profile. In so doing, the designer may be assured of a derived form having not only the four desired characteristics and coefficients previously mentioned, but also the desired profile. The only restricting requirement, other than the fact that the changes in C_p and C_w be "moderate", is that for the method to be mathematically rigorous the section of maximum beam, sectional area and local draft must be coincident. If this isn't the case a small (=1%) unpredictable error, based on the parent hull design and the desired changes is introduced.

All of these relationships are developed in full in the following section. The only other alteration to the methods of Lackenby and Moor was that the procedure had to be capable of accommodating destroyer-type ships whose maximum sections fill other than at midship. This change is also included in the derivations that follow.

2.2 Development

2.2.1 The "One Minus Prismatic" Variation

As a means of introducing the method of longitudinal repositioning of sections, the traditional "one minus prismatic" is first developed. This procedure enables the designer to modify the fineness of a parent form by expanding (creating in ships without), or reducing the region of parallel middle body. It is convenient for this, and the following derivations to refer to Figure 2.3 and the following definitions. It should also be noted that the sectional area curve is normalized with respect to both the value of maximum area and length of the half body.



For the parent design:

- ϕ = the prismatic coefficient of the half body.
- $\overline{\mathbf{x}}$ = the fractional distance from midships of the centroids of the half body.
- p = the fractional parallel middle of the half body.
- x = the fractional distance of any transverse section from midships.

For the derived form:

- $\delta \phi$ = the required change in prismatic coefficient of the half body.
- δp = the resulting change in parallel middle body.
- δx = the necessary longitudinal shift of the section at x required to generate the required change in prismatic coefficient.
- h = the fractional distance from midships of the centroid of the added "sliver" of area represented by $\delta\phi$.

In Figure 2.3 it should be recognized that AB'C is the curve of the derived form and curve ABC is that of the parent. In accordance with the method of the "one minus prismatic" the new location of the transverse sections is defined by the following equations.

$$\frac{1-(x+\delta x)}{1-x} = \frac{1-(\phi+\delta\phi)}{1-\phi}$$

 $\delta p = \frac{\delta \phi}{1-\phi} (1-p)$

$$\frac{\delta \mathbf{x}}{1-\mathbf{x}} = \frac{\delta \phi}{1-\phi}$$

 $\delta x = \frac{\delta \phi}{1 - \phi} (1 - x)$ (2.1)

The area BCD is seen to be $1 - \phi$ and the above modification simply reduces it by the factor $\frac{1 - (\phi + \delta \phi)}{1 - \phi}$.

The new area B'CD is therefore $1 - (\phi + \delta \phi)$, demonstrating that the method generates the desired prismatic coefficient of $\phi + \delta \phi$.

There is however a concomitant change in a parallel middle body found by solving for x at x = p, i.e.,

$$\frac{\delta p}{1-p} = \frac{\delta \phi}{1-\phi}$$
(2.2)

Therefore the resulting change in prismatic coefficient is obtained by altering the length of parallel middle body and then proportionally expanding or contracting the entrance and run. Because of this procedure the method has the following disadvantages:

- There is no control over the length of the parallel middle body, i.e., \$\$\$\$\$\$\$\$\$\$\$\$\$ and \$\$\$\$\$\$\$\$\$\$\$, cannot be varied independently.
- The procedure cannot be applied to reduce the fullness of a ship having no parallel middle body.
- Conversely, a ship cannot be increased in fullness without introducing parallel middle body.
- 4. The prismatic coefficient of the entrance or run cannot be altered.
- 5. The region where fullness is added cannot be controlled. That is, the maximum changes in fullness take place at the shoulders of the curve, i.e., point B.

It is because of these numerous, severe restrictions that Lackenby sought to develop a more general technique of modification.

2.2.2 Varying the Fullness of an Entrance or Run not Associated with Parallel Middle Body.

In reference [2], Lackenby concerned himself with providing a means by which to modify both C_p , LCB and the length of parallel middle body in a controllable manner.

While many of these relationships are of importance, only those which apply more specifically to destroyer-type hull forms will be pursued in any detail. However, for the readers'convenience, the most generalized case of Lackenby's formulas is included as equations (2.10) through (2.13) in the last part of this section. For the in depth derivations the reader is referred to the original paper. Nevertheless, the following derivation is the foundation upon which all the subsequent relationships are based.

In referring to figure 2.4 the various quantities have a meaning identical to those of the previous section. The only additional term requiring definition is k, defined mathematically as follows:

$$k^2 = \frac{1}{3\phi} \int_0^1 x^3 dy$$

The only other difference between figures 2.3 and 2.4 is that figure 2.4 represents a hull form not having parallel middle body, i.e., p = 0, and as a consequence the length of the entrance and run equals that of the half length of the ship.

In referring to figure 2.4, it is recognized that in order to preserve the form of the parent at both the end of ` the ship, (x = 1) and the middle of the ship, (x = 0) an equation for δx of the following form would suffice:

$$\delta \mathbf{x} = \mathbf{c} \mathbf{x} (\mathbf{1} - \mathbf{x})$$

where c is an as yet to be determined constant. It may be seen in Appendix A that the relationship for δx is:

$$\delta x = \frac{\delta \phi}{\phi (1 - 2\overline{x})} x (1 - x)$$
(2.3)



Clearly, the equation for δx is of the form of a second degree polynomial (parabola) whose values are 0 at x = 0 and x = 1, as desired. This relationship also shows that the amount by which any section in the parent is shifted is a function solely of the unchanged longitudinal position x and some as yet unknown value $\delta \phi$. At this point we must turn our attention and consider both the entrance and run concurrently if we are to lend some significance to the quantity $\delta\phi$. If we desire to specify both C_p and LCB, we are in essence placing a requirement on the area under the sectional area curve and its moment about some axis (say x = 0). Since equation (2.3) applies independently to the entrance and run, it should be possible to select the $\delta\phi$'s of these respective regions such that when taken together, the ship has the values of C_p and LCB desired.

At this point we introduce the following quantities:

- z = the distance of the parent ship's LCB
 from midships, normalized by the half
 length, (positive forward).
- $\delta \overline{z}$ = the required shift in LCB to obtain that required for the daughter hull form (positive forward).

Prime (') - denotes derived forms.

Subscripts - e = entrance or forward half-body.

r = run or after half-body.

t = a property describing the entire ship.



Referring to figure 2.5 above, we may interpret the requirements on C_p and LCB mathematically as follows:

$$p^{c} = \phi_{t} = \phi_{t} + \delta\phi_{t} = (\phi_{e} + \phi_{r}) + (\delta\phi_{e} + \delta\phi_{r}) \quad (2.4)$$

LCB = z

$$z' = \overline{z} + \delta \overline{z}$$

Summing moments of areas

$$z'(\phi_{t} + \delta\phi_{t}) = \overline{x}_{e}\phi_{e} + h_{e}\delta\phi_{e} - [\overline{x}_{r}\phi_{r} + h_{r}\delta\phi_{r}]$$

$$z' = \frac{1}{\phi_{t}'} \{\overline{x}_{e}\phi_{e} + h_{e}\delta\phi_{e} - [\overline{x}_{r}\phi_{r} + h_{r}\delta\phi_{r}]\} \qquad (2.5)$$

If equations (2.4) and (2.5) are rearranged, the expressions for $\delta \phi_{e}$ and $\delta \phi_{r}$ may be obtained.

$$\delta\phi_{e} = \frac{2}{(h_{e}+h_{r})} \left\{ \delta\phi_{t} (h_{r}+\overline{z}) + \delta\overline{z}(\phi_{t}+\delta\phi_{t}) \right\}$$
(2.6)

$$\delta\phi_{\mathbf{r}} = \frac{2}{(\mathbf{h}_{e} + \mathbf{h}_{r})} \{\delta\phi_{t}(\mathbf{h}_{e} - \overline{z}) - \delta\overline{z}(\phi_{t} + \delta\phi_{t})\}$$
(2.7)

At this point the only variables which were not previously defined are h_e and h_r . The exact expression for these variables is, with the appropriate subscript:

$$h = \frac{2\overline{x} - 3k^2}{1 - 2\overline{x}} + \frac{\delta\phi}{\phi} \left\{ \frac{(\overline{x} - 3k^2 + 2r^3)}{(1 - 2\overline{x})^2} \right\}$$
(2.8)

While equation (2.8) contains $\delta\phi$, the very thing for which it is being used to calculate, it has been stated [2] that the leading term along provides a very good approximation to h for "moderate" values of $\delta\phi$, i.e.,

$$h = \frac{2\bar{x} - 3k^2}{1 - 2\bar{x}}$$
(2.9)

Should it be desired to calculate $\delta \phi$ using equation (2.8), the solution will prove to be a quadratic which, while unwieldy, is certainly not unsolvable. The derivation of h may be found in Appendix A with the value of r defined as follows:

$$r^3 = \frac{1}{4\phi} \int_0^1 x^4 dy$$

While the above equations with the derivations in the Appendix illustrate the underlying theory, the following expressions represent the most general form of Lackenby's work.

$$\delta \phi_{\mathbf{e}} = \frac{1}{B_{\mathbf{e}} + B_{\mathbf{r}}} \{ 2 [\delta \phi_{\mathbf{t}} (B_{\mathbf{r}} + \overline{z}) + \delta \overline{z} (\phi_{\mathbf{t}} + \delta \phi_{\mathbf{t}})] + C_{\mathbf{e}} \delta p_{\mathbf{e}} - C_{\mathbf{r}} \delta p_{\mathbf{r}} \}$$

$$(2.10)$$

$$\delta \phi_{\mathbf{r}} = \frac{1}{B_{\mathbf{e}} + B_{\mathbf{r}}} \{ 2 [\delta \phi_{\mathbf{t}} (B_{\mathbf{e}} - \overline{z}) - \delta \overline{z} (\phi_{\mathbf{t}} - \delta \phi_{\mathbf{t}})] - C_{\mathbf{e}} \delta p_{\mathbf{e}} - C_{\mathbf{r}} \delta p_{\mathbf{r}} \}$$

$$(2.11)$$

In the following expressions the items refer to the entrance or run as appropriate:

$$\delta x = (1 - x) \left\{ \frac{\delta p}{1-p} + \frac{(x-p)}{A} \left[\delta \phi - \delta p \frac{(1-\phi)}{(1-p)} \right] \right\}$$
(2.12)

The practical limits on $\delta \phi_e$ and $\delta \phi_r$ are:

$$\delta\phi = \frac{\delta p (1-\phi) \pm \frac{1}{2} A [1 - \frac{\delta p}{1-p}]}{1-p}$$
(2.13)

A, B and C are calculated as follows:

$$A = \phi (1-2\overline{x}) - p(1-\phi)$$
 (2.14)

$$B = \frac{\phi}{A} \{ 2\overline{x} - 3k^2 - p(1-2\overline{x}) \}$$
 (2.15)

$$C = \frac{1}{1-p} \{ B(1-\phi) - \phi(1-2\bar{x}) \}$$
(2.16)
30

It should be recognized that in the above equations the necessary section shift, δx , is a function of the new values of C_p and LCB, and the properties of the original parent hull form.

2.2.3 Modification of Lackenby's Method to Accommodate Hull Forms with Maximum Sections not at Midships.

It should be realized that in all of the preceding developments it was assumed that the section of maximum area fell at midships. While this is certainly the case for a large class of vessels, it is virtually never true for contemporary cruisers and destroyers. It is for this reason that a new set of equations was sought while still adhering to the basic philosophy of longitudinally shifting sections.



Referring to figure 2.6, the definition of terms is, once again, consistant with the preceding section. There are, however, two very important changes. First, where \overline{z} and $\delta \overline{z}$ were originally normalized by the ships half length, they are now normalized by twice that length or the length between perpendiculars, L. Second, x, the local longitudinal position of any section is normalized by the appropriate length of entrance or run L_e or L_r respectively. Also all values of x and \overline{z} take as their origin the station of maximum sectional area.

The basic relationship for δx is still of the form $\delta x = cx(1-x)$ or $\delta x = \frac{\delta \phi}{\phi(1-2x)} x(1-x)$, the same as equation (2.3) previously. However, equations (2.4) and (2.5) now become:

$$\phi_{t} = \frac{1}{L} \{ L_{e}(\phi_{e} + \delta \phi_{e}) + L_{r}(\phi_{r} + \delta \phi_{r}) \}$$
(2.17)

$$\overline{z}' = \overline{z} + \delta \overline{z} = \frac{1}{L^{2}\phi_{t}} \{ L_{e}^{2} (\phi_{e} \overline{x}_{e} + \delta \phi_{e} h_{e}) - L_{r}^{2} (\phi_{r} \overline{x}_{r} + \delta \phi_{r} h_{r}) \}$$
(2.18)

These two equations are solved simultaneously for $\delta \phi_e$ and $\delta \phi_r$ in Appendix B, the results of which are listed below:

$$\delta \phi_{e} = \frac{1}{L_{e}^{2}h_{e}+L_{e}L_{r}h_{r}} \{ L_{r}^{2}\phi_{r}\overline{x}_{r}-L_{e}^{2}\phi_{e}\overline{x}_{e}+\overline{z}'L^{2}\phi_{t}'-L_{r}h_{r}(L_{e}\phi_{e}+L_{r}\phi_{r}-L\phi_{r}') \}$$
(2.19)
$$\delta \phi_{r} = \frac{1}{L_{r}^{2}h_{r}+L_{r}L_{e}h_{e}} \{ L_{e}^{2}\phi_{e}\overline{x}_{e}-L_{r}^{2}\phi_{r}\overline{x}_{r}-\overline{z}'L^{2}\phi_{t}'-L_{e}h_{e}(L_{e}\phi_{e}+L_{r}\phi_{r}-L\phi_{t}') \}$$

(2.20)
It was these two equations along with equation (2.3) which proved to give very satisfactory results for several sample calculations.

2.2.4 A Method by which Constraints may be Placed on the Design Waterline

In the preceding development the designer had no control over the shape of the design waterline. Because the longitudinal center of flotation LCF, was felt to be an important parameter in determining a ship's performance in a seaway, Moor [8] further developed the method of Lackenby to include control over the design waterline. It was with his revised method that Moor and his colleagues developed four distinctly different models with only their midships section identical. They were thus able to cut these four models in half to generate sixteen uniquely different hull forms.

An interesting side light of this experiment was that the parent form used was that of a fast twin-screw currently in service whose maximum section was abaft midships. They, therefore, had to first swing the original area curve to place the maximum section at midships and then proceed with the new method of modification. Although having the maximum section at amidship may have proven to be more tractable for

the creation of the models, it was not necessary for the application of Lackenby's method. This fact was demonstrated in the previous section.

The essence of Moor's method is that the sectional area curve and the design waterline are both altered in the sense of Lackenby to produce the desired values of C_p , LCB, C_w and LCF. At this point a new factor is introduced; the ratio between the sectional area ordinate and the design waterline ordinate is calculated for both the parent and derived hull forms. These ratios are then plotted as a function of ship length and it is from this curve that the longitudinal shift of sections is determined. Figures 2.7 and 2.8 illustrate the sectional area and design waterline curves and the area/waterline ratio curve respectively.

Referring to figure 2.8, to obtain the offsets for a particular section R_d in the derived form, section R_p in the parent is used as a basis. The reason for selecting station R_p in the parent is that it is the closest section to R_d with the same value of area/waterline ratio. The offsets of section R_p are then multiplied by the ratio of the beam coefficient in the derived form at section R_d to that of the parent at section R_p , i.e., B_d/B_p . These values may be seen in figure 2.7. Additionally, if the maximum beam of the derived form is different from that of the parent, the offsets of section R_p also have to be multiplied by the ratio





of the maximum beam in the derived form to the maximum beam in the parent, i.e., b_{dmax}/b_{pmax} . Therefore, the equation for any offset b_d in the derived form is:

$$b_{d} = b_{p} \frac{B_{d}}{B_{p}} \frac{b_{dmax}}{b_{pmax}}$$
(2.21)

It can be seen in figure 2.8 that there are regions of ambiguity. Such is the case where the derived curve lies below a minimum in the parent curve. It has been this author's experience confirming that in reference [8], that the regions which cannot be explicitly be defined may be faired in after defining the sections on either side.

The one remaining undesirable characteristic occurs in regions where there is some form of keel rise, i.e., the fore foot or skeg region. In these areas, if the draft of the parent is proportionally altered to equal that of the derived form, there is a concomitant and undesirable change in the area of the section. It is to this matter which the next section is addressed.

2.2.5 A Method by which Constraints may be Placed on the Ship's Profile

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Since Moor's method proved capable of constraining both the sectional area curve and the design waterline, it was decided to extend the method to include the centerline profile of the ship. The actual mechanics require only the introduction of a local draft coefficient, (local draft/ maximum draft) into the denominator of the area/beam ratio. This new ratio, (Area/Beam/Draft), is graphed and the sectional shifts determined from this graph. In determining the new offsets not only are the offsets of the parent modified transversely as described in the previous section, they are also altered in the vertical sense. This alteration is accomplished by using the water plane as a reference and moving the waterlines below a distance proportional to the ratio of the derived form draft coefficient/parent draft coefficient. Also if there is a difference in the maximum draft of the derived form and parent, the waterlines are altered by this ratio as appropriate.

As was mentioned in the background section of this chapter, section 2.1, for this modification technique to be mathematically rigorous the sections of maximum area, maximum design waterline breadth and maximum draft must be coincident. If this is not the case, the actual areas of

the sections generated will be consistantly different by a very small amount from what is desired. From the few examples this author has worked, it is estimated the difference in the value of C_p obtained and that desired is on the order of 1%. The explanation of this is seen in Appendix C.

3. Mathematical Representation of the Lines of a Ship

3.1 Background

It was established in section 2.1 that before the naval architect attempts to actually draw the lines of a new ship, he must have a "firm" description of the new design as represented by the various coefficients and curves of form. Examples of these, as cited previously, are: the sectional area curve, and hence C_p and LCB, the design waterline curve, $(C_w$ and LCF), the principle dimensions and perhaps specific information about the geometry of the midship section or stern region. These characteristics should represent what the designer feels is the "optimum" solution to his set of requirements. The naval architect now has to create one or more, of a possible infinity of, design candidates which fulfill his descriptive coefficients.

The traditional method for drawing the various lines of the ship is with the use of long, continuous strips of wood, metal, or more recently plastic, held in the desired position by weights. These tools are called splines and ducks respectively. The curves produced by this method were continuous but often times contained unwanted waviness. Removing these unwanted undulations, while preserving the

desired character of the line, is a process referred to as fairing. This topic, and the implications of placing a mathematical interpretation on it, are discussed in the next chapter. Not only did the naval architect have to generate smooth curves which pleased him visually, there also had to be a consistancy in location of the surface points when observed from the different views. This is sometimes referred to as cross-fairing and is also addressed in the final chapter. It is the fairing, and cross-fairing, which represents a very large part of the manual design effort.

It was recognized long ago, that if the ship design process was to be automated to any degree, a technique to represent the lines of the ship mathematically would have to be developed. This is especially true today where much of the work is to be done by high speed digital computers. Not only must the designer/programmer provide the mathematical algorithms for representing the ship's lines, he must also provide the logic necessary for the computer to duplicate the heretofore trial and error methods of the draftsman. The alternative to programming the logic however, would be to give the system an interactive man-machine interface at the decision points. It is, however, the mathematical representation of these ships' lines to which this chapter is devoted.

3.2 Development

3.2.1 Derivation of the Spline Cubic Equation using a Variational Approach

There are essentially two different methods by which one may arrive at a mathematical representation for ships lines.

- Select some mathematical function with several unspecified parameters whose values may be determined by some accuracy criteria and boundary conditions. Typical of this approach is the use of a polynomial and a least squares fit criterion.
- Choose some smoothness and closeness of fit criteria such that, when taken together with the boundary condition, the function and parameters are determined.

It is this second method, based on a variational smoothness criterion, that will be developed in this chapter.

In general these variational methods involve the minimization of the integral of some linear combination of the squares of the various derivatives of the function sought. In the case where the equation of the flexible spline is sought, the "smoothness" criterion is taken to be the minimization of the strain energy in the spline.

Mathematically this may be represented by [9]:

b
$$\int L(y,y',y'',...y^{(n)},x) dx = min$$
 (3.1)
a

where, for the spline equation (3.1) becomes:

s = the total path length c = flexural rigidity of the beam k = curvature defined mathematically as: $= \frac{y''}{(1-y'^2)^{3/2}}$

ds = elemental arc length
=
$$\sqrt{1 + {y'}^2} dx$$

If these values are substituted into equation (3.2) the smoothness criteria becomes:

$$I = \int_{x_{1}}^{x_{m}} \frac{y^{n^{2}}}{(1+y^{n^{2}})^{5/2}} dx = \min \qquad (3.3)$$

To complete the variational problem one must also consider a "closeness of fit" criterion which takes the following form:

$$N = \int_{a}^{b} F(y,y',y'',\dots,y^{(n)},f,x) dx \qquad (3.4)$$

It may be seen in most any text on the calculus of variations, e.g., [10] that the criteria for smoothness and closeness of fit may be combined by the introduction of the unknown Lagrange multiplier λ [10]. The results of combining equations (3.1) and (3.4) into a single variational problem is:

$$\delta \int \{L(y,y',y'',...y^{(n)},x) + a \}$$

$$\lambda F(y,y',y'',...y^{(n)},f,x) \} dx = 0 \qquad (3.5)$$

A necessary condition for the integral in (3.5) to be stationary is:

$$\frac{\partial (\mathbf{L}+\lambda \mathbf{F})}{\partial \mathbf{y}} - \frac{\mathrm{d}}{\mathrm{dx}} \left[\frac{\partial (\mathbf{L}+\lambda \mathbf{F})}{\partial \mathbf{y}^{\dagger}} \right] + \frac{\mathrm{d}^{2}}{\mathrm{dx}^{2}} \left[\frac{\partial (\mathbf{L}+\lambda \mathbf{F})}{\partial \mathbf{y}^{\dagger}} \right] - \dots (-1)^{n} \frac{\mathrm{d}^{n}}{\mathrm{dx}^{n}} \left[\frac{\partial (\mathbf{L}+\lambda \mathbf{F})}{\partial \mathbf{y}^{(n)}} \right] = 0$$
(3.6)

with boundary conditions:

$$\left\{ \left(\frac{\partial L}{\partial y^{\dagger}} - \frac{d}{dx} \frac{\partial L}{\partial y^{\dagger \dagger}} + \frac{d^{2}}{dx^{2}} \frac{\partial L}{\partial y^{\dagger \dagger \dagger \dagger}} - \dots \right) \delta y^{\dagger} \left(\frac{\partial L}{\partial y^{\dagger \dagger}} - \frac{d}{dx} \frac{\partial L}{\partial y^{\dagger \dagger \dagger \dagger}} + \frac{d^{2}}{dx^{2}} \frac{\partial L}{\partial y^{\dagger \dagger \dagger \dagger}} - \dots \right) \delta y^{\dagger} \left(\frac{\partial L}{\partial y^{\dagger \dagger \dagger}} - \frac{d}{dx} \frac{\partial L}{\partial y^{\dagger \dagger \dagger \dagger}} - \frac{d}{dx} \frac{\partial L}{\partial y^{\dagger \dagger \dagger \dagger \dagger}} + \dots \right) \delta y^{\dagger \dagger} \left(\frac{\partial L}{\partial y^{\dagger \dagger \dagger \dagger}} - \frac{d}{dx} \frac{\partial L}{\partial y^{\dagger \dagger \dagger \dagger \dagger}} - \frac{d}{dx} \frac{\partial L}{\partial y^{\dagger \dagger \dagger \dagger \dagger}} + \dots \right) \delta y^{\dagger \dagger \dagger \dagger} + \dots + \frac{\partial L}{\partial y^{(n)}} \delta y^{(n-1)} \right\}_{a}^{b} = 0$$

$$(3.7)$$

Equation (3.6) is known as the Euler differential equation for the variational problem presented in equation (3.5). The usual procedure for solving this system of equations is to first solve the Euler equation (3.6) in conjunction with the boundary conditions, expressed in equation (3.7). This solution results in an equation of the form $y = f(\lambda, x)$. This equation is then substituted into the "closeness of fit", or accuracy criterion of equation (3.4), to determine the value, or values of λ .

Another aspect of the mechanics of this procedure is revealed when the accuracy criterion requires that the resulting relationship for y = f(x) pass through a discrete set of data points. Such is the case for a "colocative spline", or a spline made to pass exactly through discrete data points. In this instance the integral in equation (3.4) would become a summation. However, in order to preserve the consistancy and similarity of working with integrals in both portions of equation (3.5), the Dirac delta function may be introduced into F.

Redirecting attention to equation (3.3), it will be noted that due to the complexity of the integrand, the differential element of strain energy, the result of equation (3.5) will not be closed form. In order to simplify the above integrand it is assumed that the demonimator, $(1+y^{+2})^{5/2}$, is

approximately 1. Or y'^2 is very small. While this may not be the actual case, if the value of y' is linearized as being the value of the slope of the chord between two successive data points, the integral in (3.3) might be thought of as follows:

$$I^{*} = \int_{-\infty}^{\infty} W(x) y'^{2} dx = \min \qquad (3.8)$$

If we were to take some mean value for W(x) for the entire domain of x, the minimization would be similar to the minimization of:

$$\int_{1}^{\infty} y''^{2} dx$$
(3.9)
$$x_{1}$$

It is also this simplification which will allow us to calculate a closed form solution to y = f(x).

One other simplification which will be made, without harm to generality, is to assume that $x \in [0,1]$. That is $0 < x_1 < x_2 < \ldots < x_{m-1} < x_m < 1$. At this point we must actually define the accuracy criterion. Assuming that the curve passes exactly through the data points, we may say:

$$y(x_i) = f_i \quad i = 1...m$$
 (3.10)

Translating the conditions of (3.9) and (3.10) into the single variational problem of the form of (3.5) we have:

$$\delta \int_{0}^{1} \{y^{*2} + 2 \sum_{j=1}^{m} \lambda_{j} \delta(x - x_{j}) (f - y)\} = 0$$
(3.11)

It should be recognized that the first delta (to the left of the integral sign) is the symbol for the variation, while the second is the Dirac delta function. f is any "candidate" function passing through the data points $(x_j, y(x_j))$ and the λ_j 's are to be determined from the accuracy criteria of equation (3.10).

The resulting Euler equation (3.6) is:

$$y^{iv} - \sum_{j=1}^{m} \lambda_j \delta(x-x_j) = 0$$
 (3.12)

The solution of this equation generates a function of the following form:

$$y(\lambda, x) = \frac{1}{12} \sum_{j=1}^{m} \lambda_{j} |x - x_{j}|^{3} + Ax^{3} + Bx^{2}$$

+ Cx + D (3.13)

Therefore the value of y and the integration constants A, B, C, and D are all linear functions of the λ_i 's. The boundary equation (3.7) for this specific problem turns out to be of the following form:

$$\begin{bmatrix} -y'' & \delta y + y'' & \delta y' \end{bmatrix}_{0}^{1} = 0 \qquad (3.14)$$

It must also be noted that (3.13) is valid for $0 \stackrel{<}{-} x \stackrel{<}{-} 1$.

While it is not intended to determine equation (3.13) for every possible situation, suffice it to say that the values of the λ_j 's and the constants A, B, C, and D are uniquely determined by the coordinate points and the end conditions of the curve [9]. The essential points to be made are:

- For the criteria used, the equation for the spline as obtained by the variational approach is of the form of a multi-coefficient third degree polynomial.
- 2. Where the curve is defined over the region (0, 1) by m data points, there is also a need for four additional pieces of information to satisfy, and fully solve equation (3.13).

It will now be demonstrated that the form of equation (3.13) is also supported by the theory developed for the small deflection of elastic beams. As it turns out, the simplifying assumptions made in the preceding derivation are exactly that which will be made in the small deflection theory. Nevertheless, the consistancy of results lends much reassurance.

3.2.2. Deflections due to Bending of a Simple Elastic Beam

In virtually any undergraduate strength of materials course the subject of beam deflections may be presented in several different ways [11]. However, it will be the method of multiple integration which will be developed here.



Referring to figure 3.1 above, it may be said that the element of the beam deforms about the neutral axis and that as a result, transverse plane sections remain plane after deformation. This results in an elongation of those fibers outside of the neutral axis and a compression of those fibers inside. Also, the amount of distortion is proportional to the distance from the neutral axis. This being the case, the following equations hold:

$$\theta = \frac{\mathbf{L}}{\rho} = \frac{\mathbf{L} + \delta}{\rho + c}$$

or, by rearranging,

$$\frac{c}{\rho} = \frac{\rho}{L} = \varepsilon = \frac{\delta}{E} = \frac{M_c}{L}$$

therefore:

$$\frac{1}{\rho} = \frac{M}{EI}$$
(3.15)

In the above equations the following definitions apply:

- M = bending moment
- E = the stiffness or Young's modulus
- I = the moment of inertia of the cross section
- ρ = the radius of curvature of the beam, measured to the neutral axis

EI = the "flexural stiffness" or "rigidity"

The mathematical expression for the radius of cruvature, or more traditionally the curvature, K, is defined as follows [12]:

$$\frac{1}{\rho} = \kappa = \frac{d^2 y/dx^2}{\left[1 + \left(\frac{dy}{dx}\right)^2\right]^{3/2}}$$
(3.16)

It is to this equation which the simplification is applied. For actual beams it is assumed that the value of $\frac{dy}{dx}$ is very small, hence, $(\frac{dy}{dx})^2 << 1$. If this is the case, the expression for curvature becomes:

$$\frac{1}{\rho} = K = \frac{d^2 y}{dx^2}$$
(3.17)

Therefore, when equations (3.15) and (3.17) are combined, the results are as follows:

$$EI\frac{d^2y}{dx^2} = M(x)$$
 (3.18)

Here, M(x) is meant to indicate that the bending moment is a function of x.

At this point we must address ourselves to the equation for the bending moment in a beam. Specifically, we will look at the results of loading a uniform elastic beam with concentrated point loads; remembering that this case most closely approximates the naval architect's ducks and splines.



It is advantagious, at this time, to introduce the concept of the singularity function defined as follows:

$$\langle x-x_{i} \rangle^{n} = \begin{cases} 0, x \leq x_{i} \\ (x-x_{i})^{n} x > x_{i} \end{cases}$$
 (3.19)

With the aid of the singularity function, and in reference to figure 3.2, the bending moment equation obtained from the application of concentrated point loads is:

$$M(x) = P_0 x + P_1 < x - x_1 > + P_2 < x - x_2 > + \dots$$

$$P_n < x - x_n >$$
(3.20)

It should be obvious that when equation (3.20) is substituted into equation (3.18) the result may be twice integrated to obtain an equation for y = f(x) which is of the following form:

EIY(x) = A + Bx +
$$\frac{1}{6}$$
 {P₀x³ + P₁1>³ + P₂2>³
... P_nn>³} (3.21)

The above equation is of a form very much the same as equation (3.13). The essential difference is that in equation (3.13), the values of the end forces P_o and P_n were still unknowns requiring the statement of two conditions at each end of the beam. It should also be apparent that the resulting values of the λ_i 's are nothing more than 2EI times the forces required to keep the beam in equilibrium. Therefore, based on the results of this and the previous section, it will be accepted without further discussion that the third degree polynomial, or cubic, is an adequate model of the ducks and splines of the naval architect. Hence the term "spline cubic".

3.2.3 Piece-wise Continuous Cubic Polynomial Approximation



Referring to figure 3.3 above, it is desired to approximate the curve y(x) by some series of cubic functions of the form:

$$g_{j}(x) = a_{j}(x-x_{j})^{3}+b_{j}(x-x_{j})^{2}+c_{j}(x-x_{j})+d_{j}$$
 (3.22)

where j represents the jth interval bounded by x_j and x_{j+1} , and $1 \le j \le n - 1$, n being the number of data points. In order for these segments to be continuous we impose the following conditions:

(1)
$$\begin{cases} g_{j}(x_{j}) = y_{j} \\ g_{n-1}(x_{n}) = y_{n} \\ \end{cases} j = 1, 2, \dots n-1$$

(2)
$$g_{j}(x_{j+1}) = g_{j+1}(x_{j+1}) \\ j = 1, 2, \dots n-2 \\ \end{cases}$$

(3)
$$g_{j}(x_{j+1}) = g_{j+1}(x_{j+1}) \\ j = 1, 2, \dots n-2 \end{cases}$$

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(4)
$$g_{j}^{*}(x_{j+1}) = g_{j+1}^{*}(x_{j+1})$$
 j=1,2,...n-2

From equation (3.22) it should be recognized that to fully describe the curve requires 4(n-1) unknown coefficients. However, the above equations provide 4n-2 conditions. We therefore require two more conditions. The obvious choice for these two additional constraints would be to specify the end conditions for the beam. Specifically, you would specify either g' or g" at the ends.

For the sake of brevity the remainder of this derivation will be abridged to include only the essential equations. For a complete and detailed description of this procedure the reader is referred to references [13] and [14].

Continuing with the derivation, the following definitions will prove useful.

 $h_j = x_{j+1} - x_j$ (3.23)

$$D_{j} = (Y_{j+1} - Y_{j})/h_{j}$$
(3.24)

We may now relate the unknown coefficients in the following manner:

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$$a_{j} = \frac{1}{6h_{j}} (s_{j+1} - s_{j})$$
 (3.25)

$$b_j = \frac{s_j}{2}$$
 (3.26)

$$c_j = D_j - \frac{h_j}{6} (2s_j + s_{j+1})$$
 (3.27)

$$\mathbf{d}_{\mathbf{j}} = \mathbf{y}_{\mathbf{j}} \tag{3.28}$$

Substituting these equations into condition (3) will generate a relationship between successive values of s_j of the following form:

$$s_{j}h_{j} + 2(h_{j} + h_{j+1}) s_{j+1} + s_{j+2}h_{j+1} = 6(D_{j+1} - D_{j})$$

 $j = 1, 2, \dots -2$ (3.29)

Equation (3.29) will thus generate the following system of equations:

(3.30)

It can be seen that, for any point x_j , s_j is the curvature at that point. For the above system of equations if the curvature is known at the end points, i.e., s_1 and s_n , the curve will be completely defined.

If instead of curvature the slope is specified at the end point, the above matrix will be modified slightly. In this case, the value of the curvature at the end point will be unknown. For the situation where the beginning slope is specified the following changes will occur. From equation (3.27):

$$D_{1} - \frac{1}{6} (2s_{1} + s_{2}) = c_{1} = t_{1}$$

or $2s_{1}h_{1} + s_{2}h_{1} = 6(D_{1} - t_{1})$ (3.31)

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The effect on the matrix system will be to change the currently existing top row and then add another top row and left column as follows:

$$\begin{bmatrix} 2h_{1} & h_{1} & \cdots \\ h_{1} & 2(h_{1}+h_{2}) & h_{3} & \cdots \end{bmatrix} \begin{bmatrix} s_{1} \\ s_{2} \end{bmatrix} = \begin{bmatrix} 6(D_{1}-t_{1}) \\ 6(D_{2}-D_{1}) \end{bmatrix}$$

If the end slope is specified a change of similar form takes place only adding a row to the bottom and a column to the right side as follows:

$$\begin{bmatrix} \cdot & \cdot & h_{n-2} & 2(h_{n-2}+h_{n-1} & h_{n-1} \\ & & \cdot & \cdot & h_{n-1} & 2h_{n-1} \end{bmatrix} \begin{bmatrix} s_{n-1} \\ s_n \end{bmatrix} = \begin{bmatrix} 6(D_{n-1}-D_{n-2}) \\ & 6(-D_{n-1}+t_n) \end{bmatrix}$$

The form of the above matrix is tridiagonal and lends itself to rapid solution by a recursive relationship [14]. This fact will save a significant amount of computational time when reduced to a computer algorithm.

3.2.4 The Rotating Spline [15]

One particular disadvantage of the "piece-wise cubic" method developed in section 3.2.3 is that it will not provide a solution for curves having infinite slopes. It is for this reason that method of the "rotating spline" was developed. Referring to figure 3.4 it may be related that this procedure is merely a modification of the "piece-wise cubic" technique.



For this method of curve approximation a cubic polynomial is generated for each interval as before. However, in this case the coordinate system is redefined for each interval, and the cubic equation is generated with respect to this local coordinate system.

Appendix E contains the steps necessary to generate the computer algorithm. There is, however, one definate disadvantage to using a rotated coordinate system. In order to obtain an interpolated ordinate on the curve the following two parametric equations must be used.

$$x = x_{i} + (x_{i+1} - x_{i}) t - (y_{i+1} - y_{i}) t (1-t) [a_{i}(1-t) - b_{i}t]$$
(3.32)

and

$$y = y_{i} + (y_{i+1} - y_{i}) t + (x_{i+1} - x_{i}) t (1-t) [a_{i}(1-t) - b_{i}t]$$
(3.33)

Both of these equations are third degree polynomials in the parameter t. To solve for some value y of the point (x,y) in the unrotated coordinate system, x is used in equation (3.32) to solve for t such that $0 \le t \le 1$ and t is also real. This value of t is then used in equation (3.33) to calculate y. It should be pointed out that the quantities a_i and b_i were determined previously as described in Appendix E.

In summary, we have shown by two methods, variational calculus and simple beam theory, that the third degree or cubic polynomial provides a good representation of the thin elastic spline used in drawing ships lines. There was, however, the disadvantage that the equations were not capable of representing curves having infinite slopes. For this reason the method of the rotating spline was introduced. This parametric method permits the representation of virtually any <u>continuous</u> curve, including those which are non singular.

4. Mathematical Fairing of Lines

4.1 Background

It has been stated previously that the lines fairing process can be the most time consuming aspect of the ship design cycle. For this very reason fairing becomes a prime candidate for automation. The difficulty, however, lies in the fact that obtaining a universally accepted mathematical definition of a faired line, or the fairing process itself, is a virtual impossibility. Perhaps the most general definition, and one which would prove the least restrictive, is the following:

> A faired line is one which retains the desired "character" but eliminates any undesired waviness or fluctuations.

It will be shown in the following sections that this result may be achieved by fitting, in a least squares sense, a third degree polynomial to a set of four or five data points. The number being dependent upon the desired boundary conditions. In addition to the similarity of the third degree polynomial to the form of an elastic spline, the polynomial also provides the capability of introducing a desired inflection point into a series of data points. It

also prohibits the introduction of multiple inflection points and undesired waviness, also an asset. Because of these characteristics and the excellent results demonstrated in reference [16], this "least squares" criteria was employed as the foundation of the fairing process.

4.2 Development

4.2.1 The Least-Squares Criteria for Defining the Cubic Curve

It was established in chapter three that the cubic polynomial would provide a "good" approximation of the shape of a spline used to construct the lines of a ship. What remains to be shown is how these polynomials are applied in order to generate the faired position of a set of data points.



$$P(x) = a_0 + a_1 x + a_2 x^2 + a_3 x^3$$
(4.1)

Referring to equation (4.1) above it should be recognized that, in order to uniquely specify the cubic polynomial in its general form, four independent pieces of information are required. The result of applying this information is to determine the values of a_0 , a_1 , a_2 and a_3 . This will produce a curve which exactly conforms to the given requirements. This is illustrated as curve I in figure 4.1 where the curve is required to pass exactly through the first four data points. The disadvantage of using this type of curve is that, since it is required to pass exactly through the given data points, it is unable to modify their position. It is this alteration however that is necessary if the curve is to be "faired".

As stated above, four pieces of information are required to uniquely specify the cubic polynomial. If, however, we were to over specify the requirements of the curve and then demand that the solution satisfy these requirements in some "best possible" but not exact manner, we begin to get a feel for how fairing can be produced. Mathematically this can be stated as follows.

Referring to curve II in figure 4.1 we will require that our resulting curve pass as close as possible to the <u>five</u> given data points. Usually this translates into a

mathematical form by requiring that the sum of the squares of the distances between the curve and the given data points should be minimized.

$$s = \sum_{i=1}^{5} [y_i - (a_0 + a_1x_i + a_2x_i^2 + a_3x_i^3)]^2 \qquad (4.2)$$

or

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$$\frac{\partial \mathbf{s}}{\partial \mathbf{a}_0} = \frac{\partial \mathbf{s}}{\partial \mathbf{a}_1} \dots = \frac{\partial \mathbf{s}}{\partial \mathbf{a}_3} = 0$$

These derivatives generate the following system of normal equations which can be solved for $a_0 \dots a_3$.

$$\begin{bmatrix} s_{0} & s_{1} & s_{2} & s_{3} \\ s_{1} & s_{2} & s_{3} & s_{4} \\ s_{2} & s_{3} & s_{4} & s_{5} \\ s_{3} & s_{4} & s_{5} & s_{6} \end{bmatrix} \begin{bmatrix} a_{0} \\ a_{1} \\ a_{2} \\ a_{3} \end{bmatrix} = \begin{bmatrix} t_{0} \\ t_{1} \\ t_{2} \\ t_{3} \end{bmatrix}$$
(4.3)

Where s_k and t_k are defined as follows:

$$\mathbf{s_k} = \sum_{i=1}^{5} \mathbf{x_i^k}$$
(4.4)

$$t_{k} = \sum_{i=1}^{5} y_{i} x_{i}^{k}$$
(4.5)

It can be seen that curve II in figure 4.1, while not passing exactly through the data points, passes "fairly close" and also displays a smooth and continuous character. It is this closeness of proximity, or minimization of the least squares difference, procedure that is the essence of the fairing criteria used in this thesis.

The following sections will develop the equations for line segments whose end position and slope or just end position are fixed. First, however, a brief explaination of how these segments are applied to fair a complete line or set of data points.

4.2.2 The Moving Strip Method

In the procedure described above it was seen that a least squares spline was passed through five data points and the points on that line were then considered to be fair. In order to fair a complete set of initially unfair points consider only five points at a time, i.e., P_k to P_{k+4} . After passing a least squares spline through these five points obtain the faired position of point P_{k+2} . Then move

the strip one unit (k = k+1) and consider the next five points, P_k to P_{k+4} , fairing P_{k+2} . For each step we could use previously faired values for P_k and P_{k+1} expecting our final solution to be obtained more rapidly. By walking this strip of five points through the entire set of data the faired position of each point may be obtained. This procedure may also be found in references [16, 17].

The following three sections develop the equations needed when considering data points whose boundary conditions are of the following type:

- Free end--the position and slope of the end is unspecified.
- Pinned end--the end position is fixed but free to rotate.
- 3. Clamped end--end position and slope are fixed.

4.2.2.1 STRIP1: Fairing an interval with free ends.

This procedure is the same as that developed in section 4.2.1. It is this routine which is used to fair the center data point (P_{k+2}) of five interior data points, i.e., $P_k \neq P_1$ and $P_{k+4} \neq P_n$, where P and P_n are the first and last points respectively in the set of given data. This routine is also used to fair P_1 , P_2 , P_{n-1} and P_n for the case where the ends are free to both rotate and translate.
Repeating equations (4.3) to (4.5) for convenience.

$$\begin{bmatrix} s_{0} & s_{1} & s_{2} & s_{3} \\ s_{1} & s_{2} & s_{3} & s_{4} \\ s_{2} & s_{3} & s_{4} & s_{5} \\ s_{3} & s_{4} & s_{5} & s_{6} \end{bmatrix} \begin{bmatrix} a_{0} \\ a_{1} \\ a_{2} \\ a_{3} \end{bmatrix} = \begin{bmatrix} t_{1} \\ t_{1} \\ t_{2} \\ t_{3} \end{bmatrix}$$
(4.3)

and

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$$s_{k} = \sum_{i=1}^{5} x_{i}^{k}$$

$$t_{k} = \sum_{i=1}^{5} y_{i}x_{i}^{k}$$

$$(4.4)$$

$$(4.5)$$

also

$$P(x) = a_0 + a_1 x + a_2 x^2 + a_3 x^3$$
(4.1)

Therefore the faired position of the second and third points in the five point strip are:

$$\overline{y}_2 = P(x_2)$$
 and $\overline{y}_3 = P(x_3)$

For the case of a free end point the first point becomes:

$$\bar{y}_1 = P(x_1)$$

It would be fair to expect that the equation P(x)would be most representative of the actual curve at its interior regions where uncertainty about end conditions would have less effect. For this reason only the center point of a strip is recalculated as being faired, i.e., P_{k+2} as opposed to recalculating both P_k and P_{k+1} .

4.2.2.2 STRIP2: Fairing an interval with pinned end.



In fitting the curve of equation (4.1) to the five data points in figure 4.2 above, we require that $P(x_1) = y_1$ exactly. If in our calculations we adjust the abscissas such that $x_1 = 0$ we may simplify this equation to:

$$P(x) = y_1 + a_1 x + a_2 x^2 + a_3 x^3$$
 (4.6)

Applying our least squares criteria to this we obtain the following normal equations:

$$\begin{bmatrix} \mathbf{s}_2 & \mathbf{s}_3 & \mathbf{s}_4 \\ \mathbf{s}_3 & \mathbf{s}_4 & \mathbf{s}_5 \\ \mathbf{s}_4 & \mathbf{s}_5 & \mathbf{s}_6 \end{bmatrix} \begin{bmatrix} \mathbf{a}_1 \\ \mathbf{a}_2 \\ \mathbf{a}_3 \end{bmatrix} = \begin{bmatrix} \mathbf{t}_1 \\ \mathbf{t}_2 \\ \mathbf{t}_3 \end{bmatrix}$$
(4.7)

where

$$s_{k} = \sum_{i=2}^{5} x_{i}^{*k}$$
(4.8)
$$t_{k} = \sum_{i=2}^{5} (y_{i} - y_{1}) x_{i}^{*k}$$
(4.9)

and

 $\mathbf{x}_{i} = \mathbf{x}_{i} - \mathbf{x}_{1}$

With the values of a_1 , a_2 and a_3 computed from equation (4.7) we can calculate the faired position of points P_2 and P_3 :

$$\bar{y}_2 = P(x_2^*), \ \bar{y}_3 = P(x_3^*)$$

where

$$x'_2 = x_2 - x_1, x'_3 = x_3 - x_1$$

After these two points are determined STRIP1 can be applied to continue the fairing process

4.2.2.3 STRIP3: Fairing an interval with clamped ends.



In order to fair an interval with both position and slope of the first point fixed we will consider only the first four points as shown in figure 4.3 above. In order to simplify the derivation we once again adjust the abscissas such that $x_1 = 0$. For this case equation (4.1) becomes:

$$P(x) = y_1 + qx + a_2 x^2 + a_3 x^3 \qquad (4.10)$$

After applying the least squares fit criteria to the four data points the normal equations obtained are:

$$\begin{bmatrix} s_4 & s_5 \\ s_5 & s_6 \end{bmatrix} \begin{bmatrix} a_2 \\ a_3 \end{bmatrix} = \begin{bmatrix} t_2 \\ t_3 \end{bmatrix}$$
(4.11)

where

$$\mathbf{s}_{\mathbf{k}} = \sum_{i=2}^{4} \mathbf{x}_{i}^{i\mathbf{k}}$$
(4.12)

$$t_k = \sum_{i=2}^{4} (y_i - qx_i^i - y_2) x_i^k$$
 (4.13)

and

 $\mathbf{x}_{\mathbf{i}}^{\prime} = \mathbf{x}_{\mathbf{i}} - \mathbf{x}_{\mathbf{i}}$

For the simple 2 X 2 system above a_2 and a_3 may be written as follows:

$$a_2 = \frac{t_2 s_6 - t_3 s_5}{s_4 s_6 - s_5^2}$$
(4.14)

$$a_{3} = \frac{t_{3}s_{4} - t_{2}s_{5}}{s_{4}s_{6} - s_{5}^{2}}$$
(4.15)

where

 $\Delta = \begin{vmatrix} s_4 & s_5 \\ s_5 & s_6 \end{vmatrix} \neq 0$

Using the values of a_2 and a_3 calculated the faired position of the second point may be readily determined as:

$$\bar{\mathbf{y}}_2 = \mathbf{P}(\mathbf{x}_2^*)$$

where

$$x_2' = x_2 - x_1$$

After fairing the second point STRIP1 can be applied to continue the fairing process, fairing point three and four the first time it is applied.

4.2.2.4 TRANS1: Fairing the last points in a given sequence of data.

As can be seen in the previous sections, the fairing procedures operate on a series of points with monotonically increasing abscissa and end conditions specified at x_1 ; where $x_1 < x_2 < x_3 \ldots$. At the time when the five point fairing interval reaches the other end of the curve, i.e., $P_k = P_{n-4}$, the following transformation must take place:

$$x_{1}^{t} = x_{n} - x_{n}^{t} = 0 \qquad y_{1}^{t} = y_{n}^{t}$$

$$x_{2}^{t} = x_{n} - x_{n-1}^{t} \qquad y_{2}^{t} = y_{n-1}^{t}$$

$$x_{3}^{t} = x_{n}^{t} - x_{n-2}^{t} \qquad y_{3}^{t} = y_{n-2}^{t}$$

$$x_{4}^{t} = x_{n}^{t} - x_{n-3}^{t} \qquad y_{4}^{t} = y_{n-3}^{t}$$

$$x_{5}^{t} = x_{n}^{t} - x_{n-4}^{t} \qquad y_{5}^{t} = y_{n-4}^{t}$$

$$(4.16)$$

This allows the fairing of the last three points as if they were the first three points. Once these three points are faired the reverse transformation is employed to place y_1^* into y_n , etc.

4.2.3 Fairing of Curves with Infinite Slopes

In ship design it is not infrequent that lines are encountered which possess infinite slopes at one or both end points. Such is the case of a section through the bow of a ship equiped with a bulbous bow. Here if the offsets y are expressed as a function of z, an infinite slope will occur at the bottom of the bulb. While the parametric rotating spline of section 3.2.4 will accommodate such a form, the simple cubic polynomial of equation (4.1) will prove indeterminate for an interval containing an end point with infinite slope.



Referring to figure 4.4 above, it can be seen that if the axis are rotated by some small anle θ , and the data points are redefined in this new coordinate system the fairing process may be carried out as normal. The following equations relate the coordinates in the two coordinate systems.

$$x' = x \cos\theta + y \sin\theta$$

$$y' = -x \sin\theta + y \cos\theta$$
(4.17)

$$x = x' \cos\theta - y' \sin\theta$$

$$y = x' \sin\theta + y' \cos\theta$$
(4.18)

It is also assumed that for small values of θ , e.g., 10°:

 $\Delta y \cong \Delta y', \quad \Delta x \cong \Delta x' = 0 \tag{4.19}$

In order to continue the fairing process the faired position of the first three points and the slope at the third point could be calculated in the rotated coordinate system and then transformed back into the unrotated coordinate system. The faired position and slope of the third point could be used to continue the fairing in the unrotated plane. The following slope transformation is also helpful.

$$\frac{dy}{dx} = \tan \left\{ \arctan \left(\frac{dy'}{dx'} \right) + \theta \right\}$$
(4.20)

4.2.3.1 Other transformations.

or

There are any number of transformations one could use to accommodate the problem of the infinite slope. One tried by this author was that of letting [18]:

$$x = \frac{1}{2}(1 - \cos \theta)$$

$$0 \stackrel{<}{-} x \stackrel{<}{-} 1$$

$$\theta = \arccos (1 - 2x)$$

$$(4.21)$$

The curve is then plotted as a cubic in θ . This has the advantage of eliminating an infinite slope at x = 0; in fact $dy/d\theta \approx \sqrt{r/2}$, where r is the radius of curvature of y = f(x)at x = 0. The disadvantage, as seen by this author, is that fairing will take place in the distorted y, θ plane. Additionally, even though the resulting curves appear to be aesthetically pleasing, some apprehension exists regarding the use

of lines faired in the two coordinate planes. For this reason the author opted for fairing in a rotated coordinate system as opposed to one which was distorted.

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5. Computer Algorithms

5.1 Overview

The system of subroutines developed in this thesis were designed to provide two distinct capabilities: (1) to provide a means of fairing a series of data points not previously considered fair, and (2) to provide the capability of representing a series of data points by an analytical mathematical expression. This second feature would also provide a means by which slopes, curvatures, etc. could be determined by interpolation. The theory of these two procedures was developed in chapters four and three respectively.

The ultimate objective of these subroutines would be their utilization in: a program to fair and draw an entire ship form. Because of this and the virtually infinite nature of the lines existing in a hull form, the program has to be capable of handling many line types. As an example of this, see figure 5.1, the programs require the following information as input.

- 1. Independent variable coordinates.
- 2. Dependent variable coordinates.
- 3. Data point type.
- 4. Number of data points.

- 5. Type of end conditions.
- 6. End slopes if required.
- An indication as to whether the input data is fair as submitted.

The only other pieces of information required for fairing are:

- 1. TOL: Is a tolerance representing a limiting distance which any data point may be moved in the fairing process.
- 2. ACC: This number represents an accuracy which, if during the fairing process a point is not moved by more than this amount, it is considered to be in a faired position.
- 3. LIMIT: This number sets a limit on the number of iterative cycles permitted in the fairing process.
- 5.1.1 Specification of Point type

The designation of point type is designed to be as consistant as possible with reference [19].

POINT	TYPE	:	DEFINITION

- 0 : Normal point at the beginning or in the interior of a continuous curved line segment.
- 1 : Break point at the end of a continuous curved segment. At present this point is treated as if it were pinned. The slope, while unspecified, is discontinuous.





- 3 : This point can be at the beginning, middle or end of a straight line segment. The slope <u>is</u> continuous at this point. This point must be specified where a curved segment joins a straight line segment since the point is considered to be a clamped end condition for the curved segment.
- 5 : Break point at the end of a straight line. The slope is discontinuous at this point.

5.1.2 Specification of End Conditions

The end condition designation is made with a two digit real number of the following format, "B.E". Here B corresponds to the end conditions at the beginning of the line and E the end condition at the end of the line.

END TYPE	:	DEFINITION
1	:	Free end. The end point is free to both rotate and translate.
2	1	Pinned end. The end point is free to rotate only, the position is fixed.
3	:	Clamped end. The end is totally con- strained. It is free to <u>neither</u> rotate or translate. The slope must also be defined.
4	:	Clamped end with infinite slope. The slope, whether $\pm \infty$ is determined by the second data point, i.e., $\pm \infty$ if $y_2 > y_1$ or $-\infty$ if $y_2 < y_1$.

5.1.3 Storage of Pertinent Line Data

The information necessary to fully describe any line is stored in a 32 x 7 two-dimensional array. This array is labeled CRV in the subroutines and its elements have the following significance. At present the first thirty rows are for data point or interval information and the last two rows are for overall curve characteristics. This could be easily expanded to allow more input data.

- Colume 1, CRV(1,1) to CRV(30,1): Abscissa of the input data points.
- Colume 2, CRV(1,2) to CRV(30,2):
 Ordinates of the original data points.
- 3. Column 3, CRV(1,3) to CRV(30,3): The faired ordinates of the data points.
- 4. Column 4, CRV(1,4) to CRV(30,4): The point type, see section 5.1.1.
- 5. Column 5, CRV(1,5) to CRV(29,5): The values of a_i as defined in Appendix D.
- 6. Column 6, CRV(1,6) to CRV(29,6): The values of b, as defined in Appendix D.
- Column 7, CRV(1,7) to CRV(30,7): The slope of the curve at the data points as defined in Appendix D.

It should be noted that the elements of columns 5, 6 and 7 are obtained as a result of the splinning option. The data in column 3 are obtained as a result of exercising the fairing option.

ELEMENT	:	DEFINITION
CRV(31,2)	:	The number of data points. At present, 6≤CRV(31,2)≤30.
CRV (31,3)	:	The slope at the beginning of the curve. Left blank if not specified.
CRV(32,1)	:	An indication of the fairness of the curve. 1.=the data submitted is fair. 2.=the data submitted is not fair.
CRV (32,2)	:	End condition specification, see section 5.1.2.
CRV(32,3)	:	The slope at the end of the curve.

The other elements of the CRV matrix are reserved for future use, e.g., in a full ship fairing program.

There are three other aspects of the program which are of the utmost importance. As was seen in the development of chapter three, the mathematical curve representation, or splinning procedure is fully capable of accommodating multivalued curves. The fairing option, however, requires that a curve be single valued over the domain of the independent variable. Therefore, while it is possible to fit a cubic curve to virtually any series of data points, care must be observed when exercising the fairing option. The second inviolable characteristic of the program is that the data points must be submitted in a monotonically sequential fashion, i.e., the points must not be submitted in a random fashion,

but rather as they are encountered while following the path of the curve. The last consideration is that in order to fair any curved line segment there must be at least six data points in the continuous curved region. This is true regardless of the end conditions of the line as a whole or the end conditions for a line segment.

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5.2 Description of Subroutines

A flow chart and subroutine listing may be found in Appendix F.

5.2.1 Lines Fairing

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The subroutines included in this section are utilized to calculate the faired position of the given data points, i.e., column 3 of the CRV matrix.

5.2.1.1 Subroutine PREFAR

This subroutine takes the data in the CRV matrix and loads all the points on a continuous curve segment into three linear arrays; X(), Y() and YORIG () representing the abscissa, faired ordinate (the original ordinate for the first iteration) and the original ordinate respectively. This process is governed by the value of point type, CRV(I,4). With these arrays established PREFAR calls either FARCRV or FARLIN, depending on whether the curve segment begins with an infinite slope.

Upon final return to this subroutine the values of the faired position of the data points will have been calculated and placed in column three of the CRV matrix.

5.2.1.2 Subroutine FARCRV

This subroutine takes the data in the X, Y, YORIG array, for those line segments which have infinite slopes, rotates the coordinate axis $10^{\circ}(\pi/18 \text{ radians})$ and then places the transformed points, equation (4.17), in an XPRIM, YPRIM and YOPRIM array. The subroutine then calls subroutine FARLIN to fair the first six data points in the rotated system. At this time subroutine SPLINE is called to determine the slope at the third point, also in the rotated system. The subroutine then completes fairing the remaining data points by matching the position and slope at the third point, in the unrotated system. That is, assuming point three to be clamped and beginning with STRIP3.

5.2.1.3 Subroutine FARLIN

This subroutine takes the points of a continuous curve segment and calls the various STRIP_ subroutines which actually compute the faired position of the points. FARLIN also calls subroutines FSTPTS and TRANS1 to fair the first and last points in the sequence.

5.2.1.4 Subroutine FSTPTS

This subroutine fairs the first three data points in a sequence of data points based on the end condition. STRIP1, 2 or 3 are called as appropriate.

5.2.1.5 Subroutine TRANS1

This subroutine fairs the last three data points based on the end condition specified. Specifically it transforms the abscissa in accordance with equation (4.16).

5.2.1.6 Subroutine STRIP1, 2 or 3

These subroutines are described in detail in sections 4.2.2.1 to 4.2.2.3. They use, as arguments, the variables in the X1, Y1 and Y0 arrays. Additionally they require values of TOL and ACC which place limits on the amount which a point may be moved and the amount of movement which is considered to be negligable. For the case where the point would move by more than TOL from its original (unfaired) position, its movement is limited by the value of TOL.

5.2.2 Lines Representation

The methodology of representing a line by a parametric cubic equation was developed in chapter three. The actual

sequence in which the process is executed is described in the following sections.

5.2.2.1 Subroutine PRESPL

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This subroutine examines the input data in the CRV matrix and places elements of continuous curved line segments into the X, Y and YORIG arrays. This assignment is based on data point type found in column four of the CRV matrix. Referring to figure 5.1A, the program would load the first eight points into X, Y and YORIG. Point nine, point type 5, would be used in conjunction with point eight to determine the slope of the curved segment ending at point eight. The program then calls SPLINE to carry out the actual curve fitting algorithm.

5.2.2.2 Subroutine SPLINE

This subroutine uses the data in X, Y and YORIG obtained from PRESPL and carries out the curve fitting algorithm presented in Appendix D. Although many intermediate terms are calculated, the only terms which are retained are a_i , b_i and d_i , these quantities are subsequently used to calculate interpolated values of the independent variable and slope at a point specified by the user.

5.2.2.3 Subroutine INTERP

This subroutine determines the interval in which a desired value of a dependent variable is located. It then passes the coordinates of the surrounding points and the values of a_i and b_i for the interval to subroutine CALCY which calculates the value of the dependent variable and slope at the desired point.

5.2.2.4 Subroutine CALCY

This subroutine calls CALCT to obtain the value of the parametric variable T. With the value of T the interpolated value of the independent variable is determined. Since the dependent and independent variables are represented parametrically, the slope of the curve is calculated by the chain rule as follows:

$$\frac{dy}{dx} = \frac{dy}{dt} / \frac{dx}{dt}$$
(5.1)

Since the value of T is determined as being the root of a third degree polynomial, CALCY is designed to calculate the interpolated value of the independent variable and slope for up to three unique and real values of T. However, the subroutine is designed to print a warning that additional points are needed to specify the curve if T has more than one real value.

5.2.2.5 Subroutine CALCT

This subroutine calculates the roots of the third degree parametric polynomial in T using the algorithm in reference [20]. This procedure is also presented in Appendix E for the readers' convenience. It should be realized, however, that only the real roots are calculated in the subroutine, the imaginary roots lack physical significance for the purpose of lines plotting.

Appendix G contains an example of a data set that was first faired then splinned and then interpolated at points equal to ene-twentieth of the domain of the independent variable. Once again it should be emphasized that, in order to fair a curved segment, at least six data points must be defined in that segment, including the end points of the segment.

6. Conclusions and Recommendations

6.1 Hull Form Modification

When work on this thesis began, the initial goal was to develop a series of destroyer-like hull forms for future use in seakeeping analysis. Preliminary efforts, using the method of longitudinally shifting sections [2,8], while showing promise, indicated that additional work would be required if the procedure was to apply accurately to destroyer type ships. Specifically, the method had to be adapted to ships whose maximum beam and section of maximum area did not lie at midships. These necessary changes were made successfully and the method was also extended to provide control over the ship's centerline profile. The primary motivation for this extension was to gain control over the hull form in the region of a sonar dome. While there was some apprehension about the criticality of changes to the geometry of the sonar dome, a telephone call to the Naval Sea Systems Command in Washington, D.C. [21], indicated that because of acoustic and hydrodynamic considerations the dome design should be maintained unchanged.

The resulting procedure for modifying hull forms does provide good results for that portion of the ship below the design waterline. However, as outlined in chapter two and

Appendix C, there are situations where the method does not provide exact results, e.g., when the station of maximum beam and section of maximum area do not coincide. Another unresolved weakness of the modification scheme is that it still does not provide the degree of control over specific hull regions often desired, e.g., an attempt to preserve the configuration of a sonar dome will result in preservation of the centerline profile only, the three dimensional geometry of the dome will be uncontrollably altered.

In summary it has been concluded that the modification technique holds a great deal of promise for use with automated methods. In particular, the procedure as it currently exists, will provide excellent results when dealing with ships for which there is no rigid requirement to keep a specific region fixed. Not only are the desired coefficients and characteristics obtained, the resulting hull forms appear to be acceptably fair.

As with virtually all work of this type there is still need for additional development. Specifically, it is felt that those aspects worthy of attention are:

> Investigate a means of controlling the resulting hull form above the design waterline. At present, excessive flair or tumblehome frequently occurs.





 Investigate a means of rigidly controlling the geometry of a specific region of the hull. This would provide a solution to the problem of keeping the sonar dome unaltered.

 Develop a computer program to carry out the extensive mathematical and graphical calculations required by the method.

6.2 Mathematical Representation of Lines and Fairing

6.2.1 Lines Representation

In chapter three it was demonstrated, by variational calculus and by simple beam theory, that a third degree or cubic polynomial could be used to approximate the shape taken by the draftsman's spline. However, it was also pointed out that the simple cubic polynomial became indeterminate if the curves contained infinite slopes. For this reason, and also because they are capable of representing multivalued functions, the parametric cubic equations of reference [15] were incorporated into this thesis. The results obtained using this method have proven to be excellent. Not only does the technique lend itself readily to being programmed, the parametric form of the curve allows the user to define either variable as being the independent variable for the purposes of interpolation. The benefit of this capability will become apparent in the discussion of cross fairing.

The only disadvantage, as seen by this author, to using the parametric equations is that they require the user to calculate the, up to three real roots, of the polynomials each time an interpolated value is sought. However, this is not seen as being restrictive since a closed form solution exists for calculating these roots and is in fact utilized in

subroutine CALCT. Therefore, because of its great flexibility, the parametric, or rotating spline technique of chapter three, is highly recommended for use with a lines fairing scheme involving the manipulation of specific waterlines and sections.

6.2.2 Fairing

The least-squares fairing criteria, as presented in chapter four, has shown to provide an effective means of altering the position of data points in order to obtain the desired "fairing" effect. That is, if provided with an adequate tolerance interval, the cubic spline passed through the resulting points will be void of extraneous oscillations and generally pleasing to the eye. When addressing the lines of a ship in the preliminary design phase, the fact that the lines satisfy a visual inspection is likely to be sufficient. For this reason, and also the excellent results obtained by this method in reference [16], this author has concluded that this scheme would be a candidate for a complete lines fairing program for destroyer-type ships.

6.2.3 Recommendations

It is obvious that, given the capability of representing lines mathematically and also a means to fair the points on a line, the next step would be to generate a method

which would fair, in the three-dimensional sense, and display an entire ship. This author has spent a great deal of time attempting to extend the methods of reference [16] in a more general form to accommodate the peculiarities which arrise in addressing displacement-type ships. The difficulty arrose from two sources. First, an attempt was made to treat the entire ship, i.e., the bow and stern were not truncated as was the case with other methods examined. Second, in trying to treat a large variety of ships, conveniently called displacement-type, the author was confronted with the problem of attempting to describe the myriad of lines of discontinuity which one may encounter. These lines are most frequently termed control lines and may consist of the ship's profile, in an obvious sense, to the locust of points, longitudinally, where rise of floor and bilge radius meet, in a more subtle sense. Figure 6.1, for a typical bulbous bow destroyer illustrates a few of the possibilities.

If we were to ignore the fairing algorithm itself for a moment, it can be seen that if a waterline A-A is taken in figure 6.1A there must be some means of communicating the effect of control line #6 on the waterline; where the explaination of the control lines is contained in table 6.1. For this case, the effect is to create a straight line region in A-A as projected in figure 6.1B. A tentative solution to this



TABLE 6.1

Explaination of Control Lines

1. Bow profile

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- 2. Locus of stern radius centers
- 3. Sonar dome profile
- 4. Main deck centerline profile
- 5. Deck edge profile
- 6. Extent of deadrise
- 7. Forward extent of parallel middlebody
- 8. After extent of parallel middlebody
- 9. Keelrise aft
- 10. Outboard transom profile
- 11. Transom centerline profile
- 12. Deck edge waterline
- 13. Forward extent of parallel middlebody
- 14. After extent of parallel middlebody
- 15. Extent of deadrise
- 16. Outboard transom profile
- 17. Deckedge transom profile
- 18. Section view of transom

problem would be to ascribe to each control line, over a region where applicable, a code designating the effect of the control line on waterlines or sections at the point of intersection. This could be easily done by assigning another column to the CRV matrix description of the line, see section 5.1.3.

Another complication which must be resolved is: when attempting to establish the offsets for, say an arbitrary waterline, how do you seek out where this waterline intersects which control lines. In the most general case, where control lines could occur at random through a hull form this problem could prove to be formidable at least. As seen by this author, the only solution to this problem is to have only certain control lines admissible for a particular class of ship. This would necessairly limit the possible intersection combinations. The control lines shown in figure 6.1 represent, what this author feels, are typical of a contemporary destroyer.

The final aspect to be addressed is that of the cross fairing algorithm itself. Reference [16] showed that by utilizing a preassigned grid in the X-Z plane the offsets (y-coordinates) at these points could be repeatedly by faired and splined by both lines of section and waterlines. The new, or faired value of each point was taken to be the mean of that obtained by fairing the two lines. These mean values were then used as unfair data points on the lines once again

and the fairing process was repeated. This iterative procedure was continued until the movement of the points on successive iterations was less than some predefined limit. The results of this cross fairing algorithm [16] proved to be quite good. Because of this, it is felt that this procedure would also prove satisfactory for the more general method of lines fairing and representation presented in this thesis.

As a final note, this author can envision where the two independent aspects of this thesis could be combined into one program of significant value. If both the fairing procedure and lines modification techniques were automated, it would provide the designer with the capability to sketch out a rough design on the back of an envelope, specifying its fundamental coefficients and dimensions, and then by passing this information through the fairing and modification routines a faired form could be obtained. The implications of this, as a savings of time and resources, are quite astounding. If the method were further extended to permit an interactive modification of the design, an individual could literally sit down and design a faired vessel in a matter of hours instead of days.
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APPENDIX A

Calculation of coefficient c and centroid of the sliver of added area. Referring to figure 2.4.

Recall: $\delta x = cx(1-x)$

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$$\delta \phi = \int_{0}^{1} \delta x \, dy = c \int_{0}^{1} x (1-x) \, dy$$

$$= c \left\{ \int_{0}^{1} x \, dy - \int_{0}^{1} x^{2} dy \right\} = c \left[\phi - 2\phi \overline{x} \right]$$

$$c = \frac{\delta \phi}{\phi - 2\phi \overline{x}} = \frac{\delta \phi}{\phi (1-2\overline{x})}$$

$$\delta x = \frac{\delta \phi}{\phi (1-2\overline{x})} x (1-x) \qquad (A.1)$$

solving for centroid, h

$$\delta \phi \cdot h = \int_{0}^{1} \delta x \left(x + \frac{\delta x}{2} \right) dy$$
$$= \int_{0}^{1} x \delta x dy + \frac{1}{2} \int_{0}^{1} \delta x^{2} dy$$

substituting for δx

$$\delta\phi \cdot h = \frac{\delta\phi}{\phi(1-2\bar{x})} \int_{0}^{1} (x^{2}-x^{3}) dy + \frac{\delta x^{2}}{2(1-2\bar{x})^{2}} \int_{0}^{1} (x^{2}-2x^{3}+x^{4}) dy$$
$$h = \frac{2\bar{x}-3k^{2}}{1-2\bar{x}} + \frac{\delta\phi}{\phi} \{\frac{\bar{x}-3k^{2}+2r^{3}}{(1-2\bar{x})^{2}}\}$$
(A.2)

For
$$\delta \phi \ll \phi$$

h $\sim \frac{2\overline{x} - 3k^2}{1-2\overline{x}}$

where:

$$k^{2} = \frac{1}{3\phi} \int_{0}^{1} x^{3} dy$$
 $r^{3} = \frac{1}{4\phi} \int_{0}^{1} x^{4} dy$

(A.3)





Referring to figure B.l above, all longitudinal dimensions are measured with respect to the point of maximum sectional area. Assume:

 $\delta \mathbf{x} = \mathbf{c} \mathbf{x} (\mathbf{1} - \mathbf{x})$

$$= \frac{\delta \phi}{\phi (1-2\overline{x})} x(1-x)$$

For the new hull form

$$\phi_{t}^{*} = \frac{1}{L} \left\{ L_{e}(\phi_{e} + \delta \phi_{e}) + L_{r}(\phi_{r} + \delta \phi_{r}) \right\}$$
(B.1)

$$\overline{z}' = \frac{1}{L^2 \phi'_{+}} \left\{ L_e^2 (\phi_e \overline{x}_e + \delta \phi_e h_e) - L_r^2 (\phi_r \overline{x}_r + \delta \phi_r h_r) \right\}$$
(B.2)

Also for the original hull form

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$$\phi_t = \frac{1}{L} \{ L_e \phi_e + L_r \phi_r \}$$
(B.3)

We now have to apply equations (B.1) and (B.2) to obtain values of $\delta \phi_e$ and $\delta \phi_r$ in terms of the known quantities \overline{z} and ϕ'_t . These quantities representing the desired values LCB and C_p for the derived form.

Solving equation (B.1) for $\delta \phi_e$.

$$\phi_{t}^{*}L = L_{e}\phi_{e} + L_{e}\delta\phi_{e} + L_{r}(\phi_{r} + \delta\phi_{r})$$

$$\delta\phi_{e} = \frac{1}{L_{e}} \{L\phi_{t}^{*} - L_{e}\phi_{e} - L_{r}(\phi_{r} + \delta\phi_{r})\}$$
(B.4)

Substituting equation (B.4) into equation (B.2) and solving for $\delta \phi_r$.

$$\overline{z}^{*}L^{2}\phi_{t}^{*} = L_{e}^{2}(\phi_{e}\overline{x}_{e} + \delta\phi_{e}h_{e}) - L_{r}^{2}(\phi_{r}\overline{x}_{r} + \delta\phi_{r}h_{r})$$

expanding the right hand side, R.H.S.

L.H.S. =
$$L_e^2 \phi_e \overline{x}_e + L_e^2 \delta \phi_e h_e - L_r^2 \phi_r \overline{x}_r - L_r^2 \delta \phi_r h_r$$

rearranging terms

$$L_r^2 \delta \phi_r h_r - L_e^2 \delta \phi_e h_e = L_e^2 \phi_e \overline{x}_e - L_r^2 \phi_r \overline{x}_r - \overline{z} L^2 \phi_t'$$

substituting in L.H.S.

$$L_{r}^{2} \delta \phi_{r} h_{r} - L_{e}^{2} h_{e} \frac{1}{L_{e}} \{L \phi_{t}^{i} - L_{e} \phi_{e}^{-} L_{r} (\phi_{r}^{i} + \delta \phi_{r}^{i})\} = R.H.S.$$

$$L_{r}^{2} \delta \phi_{r} h_{r} - L_{e} h_{e} L \phi_{t}^{i} + L_{e}^{2} h_{e} \phi_{e}^{-} + L_{r} L_{e} h_{e} \phi_{r}^{-} + L_{r} L_{e} h_{e} \delta \phi_{r}^{-} =$$

$$\delta \phi_{r} (L_{r}^{2} h_{r}^{i} + L_{r} L_{e} h_{e}^{i}) + L_{e} (L_{e} h_{e} \phi_{e}^{-} + L_{r} h_{e} \phi_{r}^{-} - h_{e} L \phi_{t}^{i}) =$$

$$\delta \phi_{r} = \frac{1}{L_{r}^{2} h_{r}^{i} + L_{r} L_{e} h_{e}^{i}} \{L_{e}^{2} \phi_{e} \overline{x}_{e}^{-} L_{r}^{2} \phi_{r}^{-} \overline{x}_{r}^{-} \overline{z}^{i} L_{e}^{2} \phi_{t}^{i} - L_{e} h_{e} (L_{e} \phi_{e}^{+} + L_{r} \phi_{r}^{-} L \phi_{t}^{i})\} \qquad (B.5)$$

Equation (B.5) may be substituted back into equation (B.4) to obtain a value for $\delta \phi_e$.

However, if the simplified form for h is not used

$$h = f(\delta \phi_r, \delta \phi_a)$$

Derivation of $\delta \phi_e$ from equation (1)

$$\delta\phi_{\mathbf{r}} = \frac{1}{L_{\mathbf{r}}} \{ L\phi_{\mathbf{t}}^{\dagger} - L_{\mathbf{e}}\phi_{\mathbf{e}} - L_{\mathbf{e}}\delta\phi_{\mathbf{e}} - L_{\mathbf{r}}\phi_{\mathbf{r}} \}$$
(B.6)

substituting into equation (B.2) and rearranging

$$\overline{z}'L^{2}\phi_{t}' - L_{e}^{2}\phi_{e}\overline{x}_{e} + L_{r}^{2}\phi_{r}\overline{x}_{r} = R.H.S.$$

$$= L_{e}^{2}h_{e}\delta\phi_{e} - L_{r}h_{r}\{L\phi_{t}'-L_{e}\phi_{e}-L_{e}\delta\phi_{e}-L_{r}\phi_{r}\}$$

$$= \delta\phi_{e}\{L_{e}^{2}h_{e}+L_{r}L_{e}h_{r}\}-L_{r}h_{r}\{L\phi_{t}'-L_{e}\phi_{e}-L_{r}\phi_{r}\}$$

$$\delta\phi_{e} = \frac{1}{L_{e}^{2}h_{e}+L_{r}L_{e}h_{r}}\{L_{r}^{2}\phi_{r}\overline{x}_{r}-L_{e}\phi_{e}\overline{x}_{e}+\overline{z}'L^{2}\phi_{t}'-L_{r}h_{r}(L_{e}\phi_{e}+L_{r}L_{e}h_{r})\}$$

$$L_{r}\phi_{r}-L\phi_{t}'\} \qquad (B.7)$$

The form of this equation is merely the transposition of subscripts by $r \rightarrow e \rightarrow r$ of equation (B.5) for $\delta \phi_r$.





Definitions:

a = area of section

b = beam of section

d = draft of section

Subscripts:

p = parent hull form

d = derived hull form

x = a maximum value, e.g., b_{dx} is the maximum value of the beam in the derived hull form

Superscript:

Further define the following ratios:

$$A = \frac{a}{a_{x}}, \qquad B = \frac{b}{b_{x}}, \qquad D = \frac{d}{d_{x}}$$
$$\alpha = \frac{A_{d}}{A_{p}}, \qquad \beta = \frac{B_{d}}{B_{p}}, \qquad \Delta = \frac{D_{d}}{D_{p}}$$

also

$$\frac{A}{B \cdot D} = R$$

It is by selecting a section in the parent, whose value of R is equal to that of the derived section being sought, that the new sections are created. It should also be evident by referring to figure C.1, that the area of the derived section will be as follows:

$$a_{\rm D} = a_{\rm p} \beta \frac{b_{\rm dx}}{b_{\rm px}} \Delta \frac{d_{\rm dx}}{d_{\rm px}}$$

It remains to be shown that in some cases the resulting area ratio is not always what is desired.

The following expression will also be useful.

$$a_{dx} = \overline{a}_{p} \overline{b} \frac{b_{dx}}{b_{px}} \overline{\Delta} \frac{d_{dx}}{d_{px}}$$

For any derived section, the area ratio obtained is:

$$\frac{a_{d}}{a_{dx}} = a_{p}\beta \quad \frac{b_{dx}}{b_{px}} \wedge \frac{d_{dx}}{d_{px}} \left\{ \frac{1}{\overline{a_{p}\beta}} \frac{b_{dx}}{\overline{b_{px}}} \wedge \frac{d_{dx}}{\overline{d_{px}}} \right\}$$
(C.1)
$$= \frac{a_{p}}{\overline{a_{p}}} \quad \frac{\beta}{\overline{\beta}} \quad \frac{\Delta}{\overline{\Delta}}$$

However, the area ratio desired is:

$$R_{p}B_{d}D_{d} = \frac{\frac{a_{p}}{a_{px}}}{\frac{b_{p}}{b_{px}} \cdot \frac{d_{p}}{d_{px}}} \left\{ \frac{b_{d}}{b_{dx}} \frac{d_{d}}{d_{dx}} \right\} = \frac{a_{p}}{a_{px}} \beta \Delta \qquad (C.2)$$

Therefore, the ratio of A_d desired to A_d obtained is:

$$\frac{\frac{a_{p}}{a_{px}}}{\frac{a_{p}}{a_{p}}} = \frac{\overline{a}_{p}}{\overline{a}_{px}} \overline{B} \overline{\Delta} = \frac{\overline{a}_{p}}{a_{px}} \frac{\overline{B}_{d}}{\overline{B}_{p}} \frac{\overline{D}_{d}}{\overline{D}_{p}}$$
$$= \overline{R}_{p} \overline{B}_{d} \overline{D}_{d}$$
(C.3)

Define:

 $S = \frac{1}{\overline{R}_{p}\overline{B}_{p}\overline{D}_{d}}$

It can be readily seen that, if the sectional area curve and the design waterline have their maximum values at the same longitudinal position, the value of S will be 1, i.e., S = 1. Hence, the area curve obtained will be equal to that desired.

If this is not the case, the designer has one option which will permit him to create a ship with the desired values of $C_{_D}$, LCB, $C_{_W}$ and LCF.

> •The designer must select a common longitudinal position about which to alter both curves. This will permit him to freeze either the point of maximum section of the point of maximum beam. Not both.

•The only other alternative is to carry out the original procedure and accept slightly different values of C_p and C_w . LCB and LCF will be as desired. The factor by which C_w will differ is:

$$W = \frac{\substack{R*D*\\pd}}{A*}$$
(C.5)

APPENDIX D, [15]



For n intervals bounded by n+l points the curve between points P_i and P_{i+1} may be computed as follows:

a.
$$g_1 = \begin{cases} \arctan [(y_2 - y_1)/(x_2 - x_1)], & \text{if } x_1 \neq x_2 \\ \pi/2, & \text{if } x_1 = x_2 \end{cases}$$

b. $p_1 = g_1$

2. Compute n times for
$$i = l(1)n$$

a.
$$\ell_i = \{(x_{i+1} - x_i)^2 + (y_{i+1} - y_i)^2\}^{1/2}$$

ь.

$$g_{i} = g_{i-1}^{+arc} \tan\{\frac{(y_{i+1}^{-y_{i}})(x_{i}^{-x_{i-1}}) - (y_{i}^{-y_{i-1}})(x_{i+1}^{-x_{i}})}{(x_{i+1}^{-x_{i}})(x_{i}^{-x_{i-1}}) + (y_{i+1}^{-y_{i}})(y_{i}^{-y_{i-1}})}\}$$

only if i > 1
c.
$$k_i = \begin{cases} -1/2, \text{ if } i = 1\\ \frac{-1}{2 + (k_{i-1} + 2) \ell_i / \ell_{i-1}}, & \text{ if } i > 1 \end{cases}$$

d.
$$r_{i} = \frac{3k_{i} (p_{i} - g_{i})}{k_{i} + 2}$$

e. $p_{i+1} = \begin{cases} p_{i} - r_{i} (1 + 1/k_{i}), \text{ if } k_{i} \neq 0\\ \frac{3g_{i} - p_{i}}{2}, \text{ if } k = 0 \end{cases}$

3. Compute once:

a.
$$q_{n+1} = 0$$

b. $d_{n+1} = p_{n+1} + q_{n+1}$

a.
$$q_i = r_i + q_{i+1} k_i$$

b. $d_i = p_i + q_i$
c. $a_i = \tan(d_i - g_i)$
d. $b_i = \tan(d_{i+1} - g_i)$

Compute n times for i = 1(-1)n

4.

The above procedure applies to the case where the ends are pinned, i.e., $d^2y/dx^2 = 0$ at $x = x_1$ and $x = x_{n+1}$. If, however, it is desired to have the beginning slope equal to t_1 , the following changes must be made:

eqn. 1.b. $p_1 = t_1$

2.c. $k_1 = 0$

If it is desired to specify the end slope as t_{n+1} :

eqn. 3.a. $q_{n+1} = t_{n+1} - p_{n+1}$

To interpolate any point on the curve the following parametric equations are used:

$$x = x_{i} + (x_{i+1} - x_{i}) t - (y_{i+1} - y_{i}) t (1-t) [a_{i}(1-t) - b_{i}t]$$

$$y = y_{i} + (y_{i+1} - y_{i}) t - (x_{i+1} - x_{i}) t (1-t) [a_{i}(1-t) - b_{i}t]$$
for $0 \le t \le t$

Section 3.2.4 describes the actual interpolation procedure.

APPENDIX E

The following procedure was taken from reference [20] and is that used to obtain the roots of the parametric equations for x and y shown in Appendix D.

Given the general form of the cubic polynomial:

$$x^{3} + ax^{2} + bx + c = 0$$
 (E.1)

this may be reduced to the following by dividing by $x = x_1 - a/3$:

$$x_1^3 = Ax_1 + B$$
 (E.2)

where

$$A = 3(a/3)^{2} - b$$

$$B = -2(a/3)^{3} + b(a/3) - c$$
(E.3)

Defining

$$p = A/3 \text{ and } q = B/2$$
 (E.4)

The roots of equation (E.2) are as follows:

Case I: $q^2 - p^3 > 0$, there is one real root

$$x_1 = \{q + \sqrt{q^2 - p^3}\}^{1/3} + \{q - \sqrt{q^2 - p^3}\}^{1/3}$$
 (E.5)

There are also two complex conjugate roots.

Case II: $q^2 - p^3 = 0$, there are three real roots of which two are repeated, i.e., only two roots are unique.

$$x_1 = 2(q)^{1/3}; x_2 = -(q)^{1/3}; x_3 = x_2$$
 (E.6)

Case III: $q^2 - p^3 < 0$, there are three real and distinct roots.

$$x_1 = 2\sqrt{p} \cos (U/3)$$

 $x_2 = 2\sqrt{p} \cos (U/3 + 2\pi/3)$ (E.7)

$$x_2 = 2\sqrt{p} \cos (U/3 + 4\pi/3)$$

where

And the second second second second

$$\cos U = q/p\sqrt{p}$$

$$0 \leq U \leq \pi$$

$$121$$
(E.8)

NOTE: These are roots of equation (E.2). To obtain the roots of equation (E.1) -p/3 must be added to the above solutions.

APPENDIX F

Figures F.1 and F.2 are conceptual flowcharts of the fairing and the splinning and interpolation procedures respectively. In the program listing that follows there is a short MAIN segment that requests the input data for a specific line and generates twenty-one (including end points) interpolated data points. While this program segment might prove of some value, it was designed primarily to test the various subroutines.

and the second of the second of the

NOTE: The program as listed requires the use of the LEQTIF Subroutine from the IMSL library. This subroutine is used in STRIP1 and STRIP2 to solve a 4x4 and a 3x3 system of simultaneous linear equations. For these SMAT is the coefficient matrix and T is the resultant column vector. If this library is not available any equivalent procedure could be substituted.

NOTE: Due to time constraints at the time of publication, the program, as listed, will not accommodate curves with point types three or five. It will, however, handle curves without straight line segments and infinite slopes at end points.





MAIN0 002 NALNO009 BAIN0015 **AAIN0016** HAIN0017 MALNO018 ALNO019 BALN0020 HAIN0034 **BAIN0035** AAI NO 00 3 **BATNO005 BAIN0006 NAIN008 HAINO012** HAIN0013 **MAIN0014** HAIN0022 HAIN0025 A I NO OO 4 **NAIN0007** BALNOO10 ALLIO011 HALNOO21 IAINO023 HALNO 024 **1 AT N0 0 26 BAIN0027** MALNO028 **BAIN0029 NAIN0030** IALK0031 HAIN0032 EEGONIAN **MAINO036** BALNOOD 1 00000130 00000150 00000010 0000020 000000000 0000050 00000000 00000080 06000000 00000100 00 000 1 10 00000120 00000140 00000160 00000170 00 000 180 00100000 00000200 00 0002 20 00000230 00000240 00000250 00000270 00000280 00000290 00000300 00000310 00000330 00000350 0000360 00 0000 70 00 000 2 10 00000260 00 000 3 20 00 000 3 40 FORMAT (°0', BEGIN ENTERING DATA FOR THE ', I2, DATA POINTS.') READ (5,*) CRV(I,1), CRV(I,2), CRV(I,4) 32 OP CRY ARRAY. ') /COM10/G (30) , S (30) , C (30) , QS (30) , B (30) , P (30) /CON4/IFAIR,ACC,LINIT /CON5/XPRIN(30),YPRIN(30),YOPRIN(30) ట /CON6/XCRV (30) , YCRV (30) , YOCRV (30) FORMAT(" ","ENTER ACC, TOL AND LIMIT.") ", PREPARE TO ENTER LINES 31 /COM1/SMAT(4,4),T(4),WKABA(4) /COM2/X(30),Y(30),YORIG(30) /CON11/YINT (10) , DYDX (10) /COM3/X1(5),Y1(5),Y0(5) /CON7/A(30) . B(30) . D(30) I=1,4) [=1,3] (I. EQ. 1) WRITE(6, 99) NPTS /CON14/RT (3) , KPLG2 READ (5,*) ACC, TOL, LIMIT (CRV (32, I), (CRV (31, I), /CON9/CRV (32,7) NPTS=INT (CRV (31, 2) +. 1) /CON12/IPT(30) /COM13/KCRV CRV (I,3) =CRV (I,2) PREFAR (TOL) DO 102 I=1, NPTS /COR8/0 00 10 I=1, NPTS WRITE (6,1000) HRITE (6,101) SHAT (N. M.) =0. 1) = 1 . 4 H=1,4 BBAD (5, *) (5, *) PORNAT (* CONT INUE COMMON COARON CONNON CORNON COMBON CONNOD CONNON CORNON CONNON COMBON COMBON CONNON CONNON COMMON CALL READ D0 2 500 41 1000 101 0 66 126

(.XQIQ .,10X, -FORMAT ('0', 'PRESPL AND SPLINE CHECK') Do 302 I=1,NPTS **PALRED** THIT PORMAT (* ', P10.4, 10X, P10.4, 10X, F10.4) HRITE (6, 107) XINT, YINT (J), DYDI (J) FORMAT (" ', INTERPOLATION CHECK') RRITE (6,103) CRV(I,2), CRV(I,3) .,10X, . ORIGINAL . 10X. PORMAT (" . . F 10. 4 . 10X . F 10. 4) CALL INTERP (NP1, XINT, KPLG1) IF (KPLG1.EQ.0) GO TO 105 WRITE (6, 104) XINT=X (1) +PLOAT (I-1) +DX IPT (I) =INT (CRV (I,4) +.1) DX= (X (NPTS)-X (1))/20. TN IX (ORIG (I) =CRV (I, 2) DO 106 J=1,KPLG1 PORMAT (.0., . D0 105 I=1,21 BRITE (6,303) WRITE (6,301) HRITE (6,201) K (I) =CRV (I, 1) Y(I) = CRY(I, 3)CALL PRESPL (I.20.1) IP1=NPTS+1 PORMAT (' ' CONTINUE CONTINUE CONTINUE STOP END 303 10 103 102 302 101 105 301 201

127

AAIN0038 BAI BOO45 BALNO055 **BAIN0059 BAIN0063** AAIN0065 **MAL NO 039** EPOONIA3 HAIN0044 RAIN0047 MAIN0048 **MAI NO 049 MAIN0050** HALN0052 NALN0053 **MAIN0056** NAIN0057 NALN0058 **MAIN062 MAL NO 037** 040040 RAINO041 BAINO042 BALN0046 NAIN0051 HAI NO 054 **MAINO 06**0 NAT NO 06 4 **BAIN0066 ALIN0061** 00000580 00000590 00000370 00000380 00000390 001000000 00000410 000000000000 00000450 00000460 00000470 00000480 06 1000000 00000500 00000510 00000520 00000530 00000540 00000550 00000560 00000570 000000000 00000610 00000620 00000030 0000000000 00000650 00000660 00000420 00000430

PRSP0015 PBS P0019 PESP0002 PRSP0005 PRSP0006 PRSP0007 PES P0010 PRSP0016 PRSP0018 PRSP0035 PRSP0001 PBSP0003 P 2 2 P 0 0 0 4 PBS P0 008 PRSP0009 PRSP0011 PESP0012 PESP0013 **PB**S**P**0020 PRSP0021 PRSP0022 PRSP0023 **PB***S***P0025 PBSP0026** PRSP0028 **PBSP0029** P**B**SP0030 PRSP0032 PRSP0033 PRSP0034 PBS P0036 PBSP0027 PESP0031 PRSP0017 PESPOOL PRSP002 00000670 01 600000 00000710 00000720 00000130 00 0000 40 00 00 00 50 F00000760 00000770 00 00 07 80 00000190 00000800 00 00008 10 00000820 00000830 00000840 00000870 00000880 00 00 08 90 00600000 00000920 00000030 01 600000 02 6000 00 00001010 00000680 00000100 00 0008 50 00000860 09 60 00 00 08 6 0 0 0 0 0 00001020 066000000 000010000 8 DATA IN A 2-D ARRAY AND SPLINES IT 10 (I.EQ.1.OR.INT (CBY (I,4)+.1).EQ.0.OR.INT (CBY (I,4)+.1).EQ.1) IF (INT (CRV(I,4)+.1).EQ.3.0R.INT (CRV(I,4)+.1).EQ.5) GO TO 401 IE. CRY (XX,5 6 0R7). DETERMINE COEFFICIENTS A, B AND ANGLES D. COMMON /COM2/X (30) , Y (30) , YORIG (30) COMMON /COM7/A (30) , B (30) , D (30) CALL SPLINE(K, EC, ES1P, ES2P) THIS SUBBOUTINE TAKES CURVE GO TO 702 COMMON /COM9/CRV (32,7) NPTS=INT (CRV (31, 2) +. 1) SUBROUTINE PRESPL IP (K.8Q.I) KP1=I DO 101 I=1,NPTS X (KP 1)=CRY (I,1) T (KP1) =CRV (I, 3) CRY (LC, 5) = A (LK) CBY (LC,6)=B(LK) CRV (LC, 5) = A (LK) C&V (LC,6)=B(LK) CRV (LC, 7) = D (LK) CBV (LC,7) =D (LK) (I.EQ.NPTS) DO 703 L=1,K D0 701 L=1.K EC=EC1+EC2 30 TO 101 GO TO 401 CONTINUE C = I + 1 - LLK = K + 1 - LLK=K-L+1 XP 1 = X + 1RETURN MARK=0 1-1=01 10 201 K = KP 11 102 2 128 666 601 701 702 703 υU

PRSP0039 PRSP0045 PBS P0048 PESP0050 PRSP0054 PRSP0055 PRS P0058 PRSP0059 **PRSP0038** PRSP0046 PRSP0049 PRSP0051 PRSP0052 PRSP0053 PBSP0057 PBS P0 060 PESP0063 PRS P0 065 **PBSP0067** PRSP0068 PRSP0069 PRS P0070 **PRSP0072** PRSP0037 PRSP0040 PESP0041 PRSP0042 PRSP0043 PRSPOO44 PESP0047 PBSP0056 PR SP0061 **PRSP0062** P**r**SP0064 PBSP0066 PRSP0071 00001030 00001060 00001070 00001080 06010000 00001120 00001150 00001160 06110000 00001210 00001230 00 00 12 40 00001250 00001260 00001270 00001290 00001310 00001320 00001370 00001040 00001050 00001100 00001110 00001130 00001140 00001170 00001180 00 00 12 00 00001220 00001280 00001300 00001330 00001340 00001350 00001360 00001380 GO TO 302 GO TO 305 GO TO 306 IF (INT (CRV (INK, 4) +. 1) . BQ. 0. 0R.INT (CRV (INK, 4) +. 1) . EQ. 1) (INT (CRV (I,4)+.1).EQ.3.0R.INT (CRV (I,4)+.1).EQ.5) (INT (CRV (I,4)+.1).EQ.0.0R.INT (CRV (I,4)+.1).EQ.1) 501 IF (I-K.EQ.1.08.I-K.EQ.0) GO TO 301 (INT (CRV(INK,4)+.1).BQ.0) EC1=3. 01 CALCULATE BEGINNING END CONDITION. 30 IP (K. EQ. 2. AND. MARK. HE.O) EC1= PLOAT (INT (CRV (32,2))) 102 (I.EQ.MPTS) GO TO 304 CALCULATE END CONDITION. 10 8 X (1) = CRV (IH1, 1)Y (1) = CRY (IN1,3) ES1P=CRY (INK,7) IP (I.EQ.NPTS) ES1P=CBV (31, 3) X (K) = CRY (I, 1) Y (K) =CBY (I , 3) INKN1=INK-1 GO TO 101 GO TO 303 GO TO 402 GO TO 402 GO TO 202 TO 999 GO TO 101 BARK=I-1 K=I-MARK 1-1=[NI X-I=XUI EC 1=2. 41 09 ЧI 11 1 F 201 401 501 303 202 301 302 402 υ υ υ υ υ

00001390 ES2P=ATAN ((CRV (I,3)-CRV (IN1,3)) / (CRV (I,1)-CRV (IN1,1)) ES1P=ATAN ((Y (IAK) -Y (IAKN 1)) / (X (IAK) - X (IAKN 1))) ES2P=CRV (32,3) EC2=CRV (32,2) -FLOAT (INT (CRV (32,2))) EC2=2. GO TO 601 END GO TO 402 GO TO 601 GO TO 601 [-]=[]] EC 1=3. EC2=3. с 306 с 304 с 305

PRSP0073 PRSP0074 PRSP0075 **PRSP0076** PRSP0078 PRSP0079 PRSP0080 **PBSP0082** PRSP0083 PRSP0085 **PBSP0086** PRSP0088 PBSP0077 **PBSP0081** PBSP0084 PBSP0087 00001510 00001400 00001420 00001430 00 00 14 40 00001460 00001480 00001490 00001500 00001530 00001450 00001470 00001540

SPLN0035 SPLN0U02 SPLN0005 SPLN0006 SPLN0008 **SPL N0009** SPLN0012 SPLN0015 SPLN0020 SPLN0025 SPL NO 030 SPL NO 033 SPLN0034 SPLN0003 SPLN0007 SPLN0010 SPL NO011 SPLN0014 SPLN0016 SPLN0018 **SPLN0019 SPL N0024** SPLN0026 SPLN0028 **SPLN0029** SPLN0032 SPLN0004 SPL NO 013 SPLN0017 SPLN0022 SPLN0023 S PL NO 03 1 SPLN0036 SPLN0001 SPLN0021 SPLK0027 00001610 00001620 00 00 17 30 00 00 17 40 00 00 17 50 00001760 00 00 17 70 00001790 00001800 00 00 18 10 00001850 00001860 00001550 THE ALGORITHN USED WASOO001560 00001570 00001590 00 00 16 30 00001640 00001660 00001670 00001680 000001690 0001700 00001720 00001780 00 00 18 20 00001830 00001840 00001870 0000 18 90 00001580 00 00 16 00 00001650 00001710 00001880 0001900 TO GENERATE A CUBIC DEVELOPED BY PROPESSOR H. SODING AND INVOLVES THE INCREMENTAL IP (I.GT.1) G(I)=G(IH1)+ATAN((A1+A2-A3+A4)/(A4+A2+A1+A3)) IP (X(2).WE.X(1)) = G(1) = ATAN((Y(2)-Y(1))/(X(2)-X(1)))COMMON / COM10/G (30) .S (30) .C (30) .QS (30) .R (30) .P (30) ROTATION OF THE ALES TO ACCONODATE INFINITE SLOPES. (I_GT_1) C(I) =- 1_/(2_+(C(IN1)+2_) *S(I)/S(IN1)) QS (NP1) = ES2-P (NP1) IF (C(I).NE.0.) P(IP1) = P(I) - R(I) + (1. + 1. / C(I)) S (I) = SQRT ((I (IP1) - I (I)) ##2+ (Y (IP1) - Y (I)) ##2) THIS SUBROUTINE CALCULATES THE DATA NECESSARY PCLYNOMIAL THROUGH A SERIES OF GIVEN POINTS. P(1)=-PI/2. P(1)=P1/2. СОННОН /СОН2/X (30) ,Y (30) ,YORIG (30) СОННОН /СОН7/A (30) , B (30) , D (30) $R(I) = 3 \cdot *C(I) * (P(I) - G(I)) / (C(I) + 2 \cdot)$ (IND. EQ. 3.0R. IND. EQ. 4) C (1) =0. SUBROUTINE SPLINE (NP1, EC, ES1, ES2) DEC=INT ((EC-PLOAT (IND) +. 01) *10.) (IND.EQ.4.AND.Y(1).GT.Y(2)) (IND. EQ.4.AND.Y (1).LE.Y (2)) (DEC. EQ. 3.0R. DEC. EQ.4) P(IP1) = (3.*G(I) - P(I)) / 2.P(1) = ES1A2=X (I)-X (IH 1) A4=X (IP1)-X (I) 13=Y (I) - Y (IN1) (I) $\gamma = \gamma$ (IP1) $\gamma = \gamma$ (I) IF (IND.EQ.3) 101 I=1,N PI=ACOS (-1.) INTEGER DEC IND=INT (EC) QS(NP1) = 0.G(1)=PI/2. P(1) = G(1)C (I) =-.5 IP1=I+1 [-]=[]] N=NP1-1 1 P 11 DO 1 L 41 101

131

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14 14	00	PLN004	PLN004	PLN004.	PLN004	PL NO 04	PL NO 04
00001910 00001920	000193	000195	000 19 6	000197	000198	000199	000200

D (NP1) = P (NP1) + QS (NP1) D0 102 I = 1, N K=N+1-I KP 1= K+1 QS (K) = R (K) + QS (KP 1) * C (K) D (K) = P (K) + QS (K) A (K) = TAN (D (K) - G (K)) RETURN END END

ENTPO015 INTPO016 INTPO002 INTPO003 **INTPO006** INTPO007 INT P0008 INTPO012 INTPO013 INTPO014 ENTPOO17 **INTPO018 ENT PO019 UTP0020** INTPO025 **ENTPO028** LNTP0029 **NTP0030** INTPOO31 NTPO033 **ENT P0034** LNTP0035 **INT P0036** L NT P0 004 INTPO005 EQUODER I INTPO010 LNTPO011 **ENTPO021** INTPO022 ENTPO023 ENTPO024 **ENTPO026** LNTP0027 **ENTPO032** INTPO001 00002030 00002050 00002070 00002080 00002090 00002120 00002200 00002220 00002290 00002330 00002010 00002020 00002040 00 00 20 60 00002100 00 00 21 10 00 00 21 30 00002140 00002150 00002160 00002170 00002180 CALL CALCY00002190 CALL CALCY00002213 00002230 00002240 00002250 00002260 00002270 00002280 00002300 00002310 00002320 00002350 00002340 00002360 POSITION AND SLOPE WILL GIVE NULTIPLE 1 (KPLG1, X (I) , X (I P1), Y (I) , X (I P1), A (I) , B (I) , XINT, IPT (IP1)) IP (X (IP1) - LT.X (I) - AND.XINT.LT.X (I) - AND.XINT.GT.X (IP1)) (X (IP 1) . GT. X (I) . AND. XINT. GT. X (I) . AND. XINT. LT. X (IP 1)) (KPLG1, X (I), X (IP1), Y (I), Y (IP1), A (I), B (I), XINT, IPT (IP1) DY DX (KPLG1) =TAN (D (IP1)) 90 H DYDX (KPLG1) = TAN (D(I))DYDX (KPLG1) = 1. E50 THIS SUBROUTINE CALCULATES INTERPOLATED VALUES DYDX (KPLG1) =1. E50 OP A CURVE THAT HAS BEEN SPLINED PREVIOUSLY. VALUES IP THE CURVE IS NOT SINGLE VALUED. (XINT.EQ.X(I).AND.I.EQ.1) GO TO 201 СОММОМ /СОИ2/X (30) Y (30) Y YORIG (30) Соммом /Сои7/A (30) B (30) D (30) Соммом /Сом9/Сву (32,7) SUBROUTINE INTERP (NP1, XINT, KPLG1) COMMON / COMIT/TINT (10) , DYDX (10) (XINT.EQ.X(IP1)) GO TO 202 (D (IP1) .NE. ACOS (-1.)/2.) (D (IP1) .EQ.ACOS (-1.)/2.) (D (I) . EQ. ACOS (-1.)/2.) (D(I) .NE.ACOS (-1.) /2.) IPT(I)=INT(CRV(I,4)+.1) COMMON /COM12/IPT(30) THT (KPLG1) = Y (IP1) IINT (KPLG1) = Y (I)DO 101 I=1, NH1 KPLG 1=KPLG 1+1 DO 99 I=1,N GO TO 101 GO TO 101 CONT INUE I + I = I 4 I KPLG 1=0N=NP1-**RETURN** END j¶a ∀ 41 41 <u>.</u> L L 4 I 201 202 101 66 U 000

SUBROUTINE CALCY (KPLG1, XI, XIP1, YIP1, AI, BI, XINT, IPTIP1) T WITHIN THE LINITS.') IF (IPTIP1.EQ.3..OR.IPTIP1.EQ.5.) GO TO 101 CALL CALCT (XI, XIP1, YI, YIP1, AL, BI, XINT) IP (DXDT.NE.O.) DYDX (KPLG1) = DYDT/DXDT YINT (KPLG1) =YI+DTDX (KPLG1) * (XINT-XI) PORMAT (" ", "THERE IS NO VALUE OF YINT (KPLG1) =YI+A 1*RT (K) +A2*A3*A6 DYDX (KPLG1) = (YIP1-YI) / (XIP1-XI)COMMON /COMIT/TINT(10) , DYDX (10) IP (KPLG2.EQ.0) GO TO 301 COMMON /COM14/BT (3) , KPLG2 A10= A9*A7-RT (K) *A8+AI A 3= BT (K) * (1. - RT (K)) DYDX (KFLG1) = 1.250A6=AI *A5-BI*RT(K) DO 102 K=1, KPLG2 DXDT=A2-A1*A10 A9=3.*RT(K) **2 DYDT=A 1+A2*A 10 A8=4.*AI+2.*BI A4=1.-2. *RT (K) KPLG1=KPLG1+1 KFLG1=KPLG1+1 WRITE (6,302) • A5=1.-RT (K) A2 = XIP1 - XIIY-IQIY=IA GO TO 999 GO TO 999 A7=AI+BI [+]=[]I RETURN 666 302 102 101 301

CLCY0014 CLCY0019 CLCY0002 CLCY0005 **CLCT0006** CLCY0008 CLCY0010 CLCY0015 **CLCY0016** C LC Y 0018 CLCY0028 CLCY0033 **CLCY0034** CLCY0001 **CLCY0003 CLCY0004** CLCY0007 CLCY0009 CLCY0011 CLCY0012 **CLCY0013** CLC Y0017 **CLCY0020** CLCY0021 CLCY0023 CLCY0024 **CLCY0025 CLCY0026 CLCI0027** CLCY0029 CLCY0030 CLCY0031 CLCY0032 CLCY0022 00002370 00002380 00002390 00002400 00 00 24 10 00002430 00002450 00002460 00002470 00002480 00002490 00002500 00002510 00002520 00002530 00002540 00002550 00002560 00002570 00002580 00002590 00002600 00 00 26 10 00 0026 20 00002630 00002640 00002650 00002660 00002670 00002680 00002700 00002420 00002440 00002690

134

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END

CLCT0005 **CLCT0006** CLCT0007 CLCT0008 CLCT0009 CLCT0010 **CLCT0012** CLCT0014 CLCT0015 CLCT0016 CLCT0017 CLCT0018 CLCT0019 CLCT0020 CLCT0023 CLCT0025 CLCT0028 CLCT0030 **CLCT0032 CLCT0033** CLCT0034 CLCT0035 **CLCT0002** CLCT0003 CLCT0004 CLCT0011 CLCT0013 CLCT0024 **CLCT0027** CLCT0031 CLCT0022 CLCT0 026 CLCT0029 **CLCT0036** CLCT0021 CLCT0001 00002710 THE VALUE OF T SELECTED00002720 00002730 00002810 00002860 00002900 00002970 00002990 00002740 00002750 YOU NEED HOREOOOO2760 00002770 00002780 00 00 28 00 00002840 00002850 00002870 00002890 00002920 00002940 00003010 00003020 00003060 00002790 00 00 28 20 00002830 00002880 00002910 00002950 00003000 00 00 29 30 00002960 00002980 00003030 00003040 00003050 THIS FUNCTION CALCULATES THE VALUE OF T USING THE CLOSED FORM CUBE IS THE ROOT THAT IS BOTH REAL AND LYING BETWEEN O AND 1. ÷ FORMAT(" ","THERE ARE HORE THAN 2 REAL ROOTS OF DEFINITING POINTS IN THIS REGION.") SUBROUTINE CALCT (XI, XIP1, YI, YIP1, AI, BI, XINT) BOOT BOUATION FOUND IN THE CRC MATH TABLES. X A=- (ABS (Q+SQD)) **E3 XB=- (ABS (Q-SQD)) **83 (X1.GT.O..AMD.X1.LT.1.) GO TO 201 XB= (Q-SQD) **E3 XA= (Q+SQD) **B3 B=-2.* (AA/3.) **3+bB* (AA/3.)-CC CONNON /CON14/RT (3) ,KPLG2 SQD=SQRT (D) 102 101 103 2 2 20 A=3. * (AA/3.) **2-BB C2=A2+(2.+AI+BI) (Q+SQD.GE.0.) Q-SQD. LT. 0.) (0+20D-II-0.) Q-SQD. GE. 0.) 8 00 8 K 1=XA+XB-AA/3. C3=-A2*(AI+BI) IF (D.GT.0.) (D.GT.O.) D.LT.0.) PI=ACOS (-1.) D- EQ-0-) 0=0++2-P++3 C1=A1-A2+AI THIL-IX=E 2=YIP1-YI N1=XIP1-XI TO 999 BB=C1/C3 AA=C2/C3 CC=C0/C3 . . . K PLG 2=0 0=B/2. P=1/3. C 0=7 3 E3=1 E 601 101 000

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135

207 202 IP (X1.GT.0..AND.X1.LT.1.) GO TO 205 209 GO TO 204 X3=2.*SQP*COS(U/3.+PI*4./3.)-AA/3. X 2=2.*S0P*COS (U/3.+PI*2./3.) -AA/3 10 GO TO 2 00 00 (X1.GT.0. AND.X1.LT.1.) (X2.GT.0. AND.X2.LT.1.) (X2-GT. 0. - AND. X2-LT. 1.) (X3.GT.0..AND.X3.LT.1.) X 1=-2.* (ABS (0)) **E3-AA/3. X 1=2.*SQP*COS (U/3.) -AA/3. (Q.GE.O.) GO TO 502 0=ACOS (Q/(P**(1.5))) K1=2.*Q**E3-AA/3. (2=-X1/2.-AA/3. X 2=-X 1/2.-AA/3. K PLG 2=K PLG 2+ 1 K PLG 2=K PLG 2+1 K FLG 2= K PLG 2+ 1 RT (KPLG2) = X2 8T (KFLG2) = X2 RT (KPLG2) = X3 SQP=SQRT (P) GO TO 208 TO 999 TO 999 GO TO 203 TO 999 GO TO 501 GO TO 999 GO TO 999 GO TO 206 RT(1) = X1RT(1) = X1RT(1) = X1KPLG 2= 1 KPLG 2= 1 K PLG 2= 1 00 A I 00 41 Ч 00 102 502 501 203 103 206 208 201 202 204 205 207 209

CLCT0039 CLCT0046 CLCT0048 CLCT0053 CLCT0055 CLCT0056 CLCT0058 CLCT0059 **CLCT0068** CLCT0038 CLCT0043 CLCT0047 CLCT0049 CLCT0050 CLCT0052 CLCT0054 CLCT0057 **CLCT0060** CLCT0064 **CLCT0067 CLCT0069** CLCT0070 CLCT0040 CLCT0041 **CLCT0042** CLCT0045 CLCT0051 **CLCT0062** CLCT0063 CLCT0065 CLCT0066 CLCT0071 CLCT0072 CLCT0044 CLCT0061 CLCT0037 00003210 00003260 00003280 00003070 06060000 00003100 00003120 00 003 1 30 011 00000 00003150 00003170 00003180 00003190 00003200 00003220 00003230 00003240 00003250 00003270 00003290 00003300 01003310 00003360 08660000 00003390 00003410 00003080 00003110 00003160 00 00 33 20 00003330 00003340 00003350 00003370 00003400 00003420

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999 IP (KPLG2.BQ.2.OR.KPLG2.EQ.3) WRITE (6,601) Return End

00003430 CLCT0073 00003440 CLCT0074 00003440 CLCT0074 ÷.

PRPR0002 PRPR0009 PRPR0015 PRPR0016 PRPR0018 PRPR0003 PR PR0004 PRPR0005 PRPR0007 P& P& 0008 PR PR0010 PRP 80013 PBP80019 PRPR0020 PEFE0006 PRFR0012 PR PR0017 PRPR0030 PRPB0035 PRPR0011 PRFR0014 PR PR0023 PRPR0028 PRP 20029 PRPR0031 PRF20032 PRPR0033 PR PR0034 PRP20036 PR PR0001 PRPR0022 PB PR0024 PB P20025 P.R.P.RO 026 PRP20027 PR FR0021 00003630 00003470 00003480 00003490 00003500 00003510 00003540 00003550 00003560 00003570 00003580 00003590 00003600 00003640 00003650 00003670 00003680 00003770 00003460 00003520 00 00 35 30 T00003610 00003620 00003660 00003690 00003700 00003710 00003720 00003730 00003740 00003760 00003750 00003780 00003790 00 80 00 00 00003810 3 OF FOINTS WITH BND CONDITIONS AND GO TO 401 (I.EQ.1.0R.INT (CRV (I,4) +.1) .EQ.0.0R.INT (CRV (I,4) +.1) .EQ.1) CALL PARCRY (K, EC, TOL, ES1P, ES2P) IP (INT (CRV(I,4)+.1).EQ. 3.0R.INT (CBV (I,4)+.1).EQ.5) COMMON /CON6/XCRY (30), YCRY (30), YOCRY (30) CALLS THE APPROPRIATE FAIRING SUBROUTINE. BND=INT ((CRV (32, 2) - PLOAT (BGN) +.01) +10.) KCRV=1 CONNON /CON2/X (30) , Y (30) , YORIG (30) THIS SUBROUTINE TAKES A SERIES (IEC1.EQ.4.08.IEC2.EQ.4) KP 1≓I (IEC1-EQ-4-0R-IEC2-EQ-4) (KCRV.NB.1) GO TO 12 [BC2=INT ([BC2+. 01) *10.) SUBROUTINE PREFAR (TOL) COMMON /COM9/CRV (32,7) NPTS= INT (CRV (31, 2) +. 1) IP (K.EQ. 1.08.K.EQ. I) YORIG (KP1) =CRV (I,2) YORIG (JJ) = YOCRY (JJ) COMMON /COM12/KCBV BGN= INT (CRV (32,2)) [BC 1=INT (EC1+.1) INTEGER BGM, END DO 101 I=1,NPTS X (KP 1) =CRY (I,1) T (KP1) = CRV (I, 3)X (JJ) =XCRV (JJ) 11 JJ=1,K C=EC1+EC2 GO TO 401 CONTINUE SONTINUS KP1=K+1 KCRV=0 A RK = 0 RETURN 10 201 K=KP1 4 I 00 -1001 102 666 601 101 υ U
PRPR0038 PRP20039 PRPR0048 PRF20053 PRPR0068 PRP20069 PR PR0070 PR PR0040 PRPR0049 PRPR0050 PRPR0054 PRPR0057 PRPR0058 PRPR0059 **PRP20060** P**r Pro**063 PRPR0066 Pa Pa0071 PRPR0072 PRPR0037 PRFR0042 PRPR0043 PRFR0045 PR PR0046 PRPR0055 PR PR0062 PRPR0065 P2720044 PRPROOUT PR PR0051 PRPR0052 PBPB0056 Pa**fa**0064 PRPR0067 PRPR0061 00003830 00003850 00003860 00003890 00 00 39 10 06 96 00 00 01 620000 00003950 09 60 00 00 08620000 06660000 00004020 00 00 40 30 01010000 00004060 00004070 00004080 06040000 00004110 00 00 4 1 20 00004130 00004160 00004170 00003820 00003870 00003880 00003900 00003920 00 00 39 70 000000000 00004010 00004050 0004100 00004150 00003840 00 00 4 1 40 FAIRING BY-PASSED.") (IEC1.ME.4.AMD.IEC2.ME.4) CALL PARLIN (K, EC, TOL, ES1P, ES2P) PORHAT (" , "NOT ENOUGH DATA POINTS TO PAIR. CALCULATE THE BEGINBING END CONDITIONS. 501 20 8 IP (K. EQ-2-AND. MARK.NE-0) GO TO 702 (I.EQ.MPTS) GO TO 102 GO TO 801 CRV (LC, 2) =YOBIG (LK) CRV (LC, 2) =YORIG (LK) YORIG (1) =CRV (IM1, 2) (ORIG (K) = CRV (I, 2) CRV (LC, 1) = X (LK) CRV (LC, 1) = X (LK) CRV(LC, 3) = Y(LK)r (1) = CRV (IN1,3) CBV (LC, 3) =Y (LK) K [1] =CRY (IM1,1) (I. EQ. NPTS) ((JJ) =YCRY (JJ) K (K) =CRY (I,1) HRITE (6,802) ((K) =CRV (I, 3) DO 701 L=1,K DO 703 L=1,K IP (K.LT.6) GO TO 101 GO TO 101 TO 101 GO TO 101 GO TO 202 C = I + 1 - L(=I-BARK LK=K-L+1 LK=K+1-L M.A.B.K = I - 1 [4 1 = I = 1 K I 1= K-1 LC=I-L 5 00 702 703 202 701 501 401 801 802 201 12 = U

PRPR0075 PR PR0078 PR PR0085 PRPR0074 PRPR0076 PBPR0077 PRPR0079 PRF20083 PRP 80084 PRP20086 PRP20087 PRPR0088 PR 720089 PRPR0090 PRPR0093 P.R. P.R.O 09 4 PRPR0095 PR PR0098 PRPR0099 PRPR0 10 1 PRP 20073 P.B. P.R.0080 PRFR0082 PRFR0092 PRPR0096 PR 720 100 **PRPR0102** PR 220081 P.R.R.R.097 PRPR0103 PRP20091 00004190 00004200 00004210 00004220 00004230 00004240 00004250 00004260 00004280 00004290 01 240000 00004350 00004360 08 6 4 00 00 00004430 00004180 00004270 00004300 00004310 00004330 000004370 00004390 00004410 00004420 000004450 00004460 00004470 00004320 000004480 GO TO 302 GO TO 305 GO TO 306 (INT (CRV (INK,4)+.1).EQ.0.0R.INT (CRV (INK,4)+.1).EQ.1) 852P=ATAN ((CRV (I,3) -CRV (IB1,3)) / (CRV (I,1) -CRV (IR1,1))) (INT (CRV (I,4) +. 1) . EQ. 3.0R. INT (CRV (I,4) +. 1) . EQ. 5) (INT (CRV (I,4) +.1) . EQ. 0.0R.INT (CRV (I,4) +.1) . EQ. 1) BS1P=ATAN((Y (IMK)-Y (IMKH 1))/(X (IMK)-X (IMKH1))) (INT (CRV (INK, 4) +.1) .EQ.0) EC1=3. (I-K.EQ.1.08.I-K.EQ.0) GO TO 301 (I.EQ.NPTS) GO TO 304 CALCULATE END CONDITIONS EC2= PLOAT (END) / 10. ES1P=CRV (IMK.7) ES2P=CBV (32, 3) ES1P=CRV (31, 3) EC 1= FLOAT (BGN) I HKH 1= INK-1 GO TO 999 TO 402 GO TO 303 TO 402 GO TO 402 GO TO 601 30 TO 601 GO TO 601 INK=I-K IN 1= I-1 EC2=.3 EC2=.2 EC 1=2. EC1=3. END 41 00 11 00 402 30¢ 306 303 301 302 305 • υ υ

140

FAIRS CURVE FOR ONE IMPINITE SLOPE AT THE BEGINNING. COMMON /COM5/XPRIM (30) ,YPRIM (30) ,YOPRIM (30) YOPRIM(I) = -XCRV(I) + SIM(R) + YOCRV(I) + COS(R)COMMON /COM6/XCRY (30), YCRY (30), YOCRY (30) YPRIM(I) = -XCBV(I) + SIM(R) + YCRV(I) + COS(R)XPRIM(I) = ICRV(I) + COS(R) + YCRV(I) + SIN(R)CALL FARLIN (6, ECPR0, TOLPB0, ESIPRN, ES2) 301 201 SUBROUTINE PARCAY (N. EC. TOL1, ES1, ES2) S THE ROTATION ANGLE OF 10 DEGRERS. COMMON /COM2/X (30) , Y (30) , YORIG (30) 5 5 10 END=INT ({EC-PLOAT (BGN) +. 01) *10..) 000 09 COMMON /COM7/A (30) "B (30) "D (30) (BGN. EQ. 4. AMD. END. NE. 4) (END. 20.4 . AND. BGN. NE. 4) YOCRV (JJ)=YORIG (JJ) COMMON /COM13/KCRV TOLPRN=TOL1/COS(R) ES 1PBM= (4./9.) + PI INTEGER BGN, END X CRV (JJ) =X (JJ) YCRY (JJ) =¥ (JJ) DO 202 I=1,6 D0 11 JJ=1,6 DO 10 JJ=1.N PI=ACOS (-1.) BGN=INT (EC) GO TO 401 ECPRM=3.1 CONTINUE R=PI /18. IPAIR=0 ITRNS=0 KCRV=1 41 1001 22 201 202 10 U υ ບບ

PRCV0013 PRC V0015 PRCV0016 PRCV0018 **PRCV0019** PRC V0003 PRCV0005 PRCV0006 PRCV0007 PBC V0 008 FRCY0009 PRCV0010 PBC V0012 PRCV0014 PRC V0017 FRCV0020 FRC V0 026 PRCV0028 FRCV0029 PRCV0031 PBCV0032 FRCV0033 PRCV0034 PRC V0035 PRCV0002 PRCV0004 PRCV0021 PRCV0022 PRCV0023 PRCV0025 PRC V0030 PRC V0036 PRC VO 011 PRC V0 024 PRCV0027 PRCV000 00004740 00004750 000004790 00004800 00004510 00004520 00004530 00004550 00004560 00 00 45 70 00004580 00004590 00004600 00004610 00004620 00 00 40 40 00004650 00004660 00004670 00004680 06910000 00004700 00004710 00 00 47 20 00004760 00004770 00004780 00004810 00004820 00004830 01840000 00004500 00004540 00004630 00004490

141

YPRIA (JJ) = Y (JJ)

PAIRS CURVE WHERE INPLUITE SLOPE IS AT THE END. CALL PARLIN (NH2, BCPRN, TOL1, ES 1PRN, ES2PRN) I.E., P(NN5) YCRY (I) = XPRIM (I) + SIN (R) + YPRIM (I) + COS (R)PARLIN (NA1, BCPRN, TOL1, ES1, ES2) CALL SPLINE (NO1, ECPRN, ES1, ES2) CALL SPLINE(6,4.1, ES1PRN, ES2) CALCULATE THE SLOPE AT POINT 3. LCULATE SLOPE AT POINT NN5. ECPRH=3. +PLOAT (BND) /10. YOPRIM (IDX) = YOCRV(I)ECPBR=PLOAT (BGN) +. 1 ES 2P RM=- (D (NAS) +R) TOLPRM=TOL 1/COS (R) (PRIM(IDX) = XCRV(I)(PBIA(IDX) = TCBV(I)ES1PRM= (4. /9.) *PI YCRY (JJP2) =Y (JJ) TPRIM (JJ) =Y (JJ) Y PRIA (JJ) = Y (JJ) DO 12 JJ=1,NH2 DO 13 JJ=1, NH1 YCRV (JJ) =Y (JJ) BS1P88=D(3)+B DO 203 I=1,6 00 302 I=1,6 DO 204 I=3,M **BS2PRH=BS2** GO TO 500 ECPRM=3.3 JJP2=JJ+2 M2=N-2 8-N=5HR IDX = I - 2KCRV=1 KCRV=0CALL 203 204 301 1 J υ U 2 14

PRC V 00 39 PRCV0050 PRCV0070 PRCV0046 PRCV0047 PRCV0048 PRCV0049 PBCV0054 PRCV0056 PRCV0059 FRCV0069 FECV0072 PRC V0 038 PRCV0040 PRC VO 042 PRCVOO43 PRC V0044 PRC VO 045 PRCV0053 FRC V0055 PRCV0057 PRCV0058 PRC V0060 PRC V0 06 6 PBC V0068 FECV0037 PRCV0041 PRCV0051 PRCV0052 PRC V0062 PRCV0063 PRC V0 067 PRC VOO71 PBCV0061 PRCV006! PRC V0 06 00005100 00005130 00005140 00005150 00004890 00004950 00004970 00004980 06640000 00005020 00 00 50 50 00005060 00005080 00002090 00005110 00005120 00005160 00005190 00005200 00004870 00004880 00600000 00004920 00004930 01610000 09640000 00005000 00005010 00005030 00005070 00005170 00005180 00004860 00004910 00000000000 00004850

PBC V0 089 PBCV0094 **FRCV0100** PRC V0 104 **FEC V0 07 3** PRCV0074 PRCV0075 PRC V0076 PBC V 0 077 PRCV0078 PRCV0079 **FRCV0081** FRCV0082 **FRCV0083** PBC V0 08 4 FRCV0085 PRCV0086 PBC V0 087 PRCV0088 PRCV0090 PRC V0 09 1 PRCV0092 FRCV0093 PRC V0 09 5 7 RC V0 096 PRCV0097 FRCV0098 PBC V0099 PBCV0101 PRCV0102 PRC V0 103 PRC V0105 PRC 70 106 Pacv0107 FRCV0108 PRC V0 080 00002390 00005210 00005220 00005230 00005240 00005250 00005260 00005270 00005280 00005290 00005300 00005310 00005320 00005330 00005340 00005350 00005360 00005370 00005380 0002400 00005410 00005420 00005430 00002440 00 00 54 50 00005460 00005470 00005480 00002490 00 0055 00 00005510 00005520 00005530 00005540 00005550 00005560 C THIS SEGNENT FAIRS THE CURVE FOR THE CASE OF INFINITE SLOPES AT BOTH YOPRIM(I) = -XCRY(I) + SIN(R) + YOCRY(I) + COS(R)CALL FARLIN (6, ECPRN, TOLPRN, ESIPRN, ES2PRN) Y CRY (IDX) = XPRIM (I) * SIN (R) + YPRIM (I) * COS (R) YOPEIN (I)=-XBAR*SIN (R) +Y OCRY (I DX) *COS (R) TPRIN (I) =- XCRV(I) +SIN(R) + YCRV(I) +COS(R)NOW FAIR THE REMAINING POINTS ON THE LINE. YCRV (I) = XPRIB (I) = SIB (R) + YPRIB (I) = COS (B)YPRIN(I) =-XBAR*SIN(R)+YCRV(IDX) *COS(R) CALL PARLIN(6, ECPRN, TOLPRN, BS 1 PRN, ES 2) $\mathbf{IPRIM}(\mathbf{I}) = \mathbf{ICRV}(\mathbf{I}) + \mathbf{COS}(\mathbf{R}) + \mathbf{ICRV}(\mathbf{I}) + \mathbf{SIN}(\mathbf{R})$ XPRIN (I) =XBA R*COS (R) +YCRY (IDX) *SIN (R) PLACE PAIRED POINTS IN THE CRY VECTORS. ROTATE AND FAIR THE FIRST FIVE POINTS. CALL SPLINE(6, BCPRM, ES 1PRN, ES2) OBTAIN THE SLOPE AT POINT 2. XBAR=XCR V (N) - XCR V (IDX) ES2PRM=- (D(2)+2.*R) TOLPRH=TOL 1/COS (R) ES1PR8= (4./9.) *PI YPRIN (JJ)=Y (JJ) (CC) = (CC) = I (JJ)DO 404 I=1 ,NM1 DO 14 JJ=1,6 DO 303 I=1.6 DO 402 I=1,6 DO 15 JJ=1,6 D0 403 I=1,6 GO TO 500 I-L+N=XCI IDX=N+1-I ECPBM=3.1 ECPRM=3.3 KC RV=1 KCRV = 1403 302 303 401 402 5 14 ں υ υ J

CALL PARLIN (NH1, BCPRN, TOLPRN, ES1PRM, ES2PRB) TCRV (IDX) = XPRIM (I) + SIM (R) + YPRIM (I) + COS (R)IOPRIM(I) = -XBAR + SIM(R) + FOCRV(IDX) + COS(R)YPRIM (I) =- IBAR*SIN (R) +YCRY (IDX) *COS (R) XPRIM(I) =XBAR*COS(R) +YCRY(IDX) *SIN(R) XBAB=XCR V (N) - XCR V (IDX) YPRIA(JJ) = Y(JJ)DO 16 JJ=1, NN1 DO 405 I=1,NM1 I DX=N+1-I I-L+N=XdI KCRV=1 RETURN KCRV = 1**10** 405 500 16

PRCV0110 **PRCV0116 FRCV0118 FRC VO 109** FRCV0111 PECV0112 PRC V0 113 PRCV0114 PRCV0115 PRCV0117 PRC V0 119 **FRCV0120** PRCV0122 FRCV0123 PRCV0121 00005570 00005580 00005590 00 00 56 00 00005610 00005620 00005630 00005640 00005650 00005660 00005670 00005680 00005690 00 C 057 10 00 00 57 00

144

END

FRLN0012 PRLN0014 PRLN0016 PRL NO017 FRLN0025 FRL NO 020 PRL NO 024 P.R.L.M0 028 **FRL N0029 FRLN0036** P.R.L.N0032 00005730 00005750 00005780 00005830 00005850 00005860 00005870 00005890 000000000 00005910 00 00 00 00 00 00002940 00005960 00005980 00005990 00000000 00005720 00 00 57 40 00005760 00005770 00005790 00005800 00 00 58 10 00005820 00005840 00005880 00005920 00005950 00005970 00000000 00006010 00006020 00006050 00006060 0000000000 00006070 THIS SUBROUTINE CALLS THE STRIP SUBBOUTINES TO PAIR LINES WITHOUT COMMON /COM5/XPRIM (30), YPRIM (30), YOPRIM (30) CALL PSTPTS (ES1, ES2, EC, TOL1) SUBROUTINE FARIIN (N. EC. TOL1, ES 1, ES 2) Common /Com2/X (30), Y (30), Yorig (30) COMMON /COM3/X1 (5) , Y1 (5) , Y0 (5) CALL TRANSI(N, EC, TOL 1, ES1, ES2) COMMON /COM4/IPAIR, ACC, LIMIT IP (KCRV.NE.1) GO TO 11 GO TO 101 **70RIG (JJ) = 70PRIM (JJ)** YO (I2) = YORIG (INDEX) COMMON /COM13/KCBV DO 10.3 I 3=I1, I1P2 CALL STRIP1 (TOL 1) Y (I3) = Y1 (I COUNT) , NH5 ICOUNT=ICOUNT+1 X (JJ) = XPRIM (JJ) Y (JJ) =YPBIN (JJ) CONNON / CON8/Q X 1 (I 2) =X (I NDEX) Y1 (I2)=Y (INDEX) INPINITE SLOPES. 102 I2=1,5 INDEX=I1-1+I2 10 JJ=1,N (11.EQ.1) (I1.EQ.1) DO 101 I 1=1 I1P2=I1+2 CONT INUE CONTINUE [COUNT=0]CONTINUE CONT INUE ITRN S=0 I PAIR=0 NA5= N-5 oq 4 I 8 1002 1001 100 102 103 101 0 1 υ u 145

PRLN0002

PR LN0 00 1

PRLN0003

PR LN0 005 **FRL N0 006** PRLN0007 PRL N0 008 PRLN0009 PRLN0010 PRLN0011

P.R.L.NO 004

FRLN0013

PRL NO 015

PRLN0018 PRLN0019 **PRL N0 022**

PRLN0023

PR.LN0026 PRLM0027

PRLN0021

PRLN0035

FRL 80033

PRLN0034

FRLN0030 FRL N0031

ITRNS=ITRNS+1 IF (ITRNS.GE.LIMIT) GO TO 500 IF (IFAIR.ME.O) GO TO 100 500 RETURN EVD

00006080 FRLM0037 00006090 FRLM0038 00006100 FRLM0038 00006110 FRLM0040 00006110 FRLM0040

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PSPT0003 FSPT0008 PSPT0009 SPT0015 SPT0019 FSPT0034 **PSPT0036** PSPT0002 PSPT0006 SPT0010 SPT0018 SPT0024 **SPT0025** 'SPT0028 SPT0029 'SPT0032 PSPT0035 FSPT0005 SPT0011 SPT0012 PSPT0016 'SPT0020 **SPT0026** PSPT0004 75 PT0 007 SPT0013 PSPT0021 SPT0023 SPT0027 SPT0030 SPT0031 SPT0033 SPTOOL PSPT0017 SPT0023 **PSPT000** THIS SUBROUTINE CALCULATES THE FAIRED POINTS FOR THE BEGINNING OF THEO0006130 00006140 00 006 150 00006160 00006170 00006180 00100000 00006200 00006210 00006230 00006240 00006250 00006270 00006280 00006290 00006310 00006320 00006330 00006340 00006350 00006360 00006370 00006390 00006410 00 0064 20 00 00 00 00 00 00006450 00 0064 70 00006220 00006260 00006300 00006380 0000000000 00006430 00006460 00006480 SLOPE GIVEN. THIS LOOP ESTABLISHES THE SECOND AND THIRD POINTS FOR FIXED ENDS. THIS LOOP ESTABLISHES THE FIRST THREE POINTS FOR FEE ENDS. THIS LOOP ESTABLISHES THE SECOND AND THIRD POINTS WITH SUBROUTINE PSTPTS(ES1,ES2,EC,TOL1) COMMON /COM2/X (30) .Y (30) .YORIG (30) CONNON /CON3/X1 (5) . Y1 (5) . Y0 (5) 302 301 GO TO 303 G0 T0 G0 T0 CALL STRIP1 (TOL1) CALL STRIP2 (TOL) YO (I6) =Y OR IG (I6) YO (I 2) = YORIG (I 2) YO (I 4) = YORIG (I 4) I2=1,5 COMMON /COM8/0 D0 403 I4=1,5 DO 405 I6=1.4 D0 402 I 3=1,3 (IBC.EQ.1) (IBC.EQ.3) (IEC. EQ.2) (1 (I 2) =Y (I 2) X1(I2)=X(I2) X1(I1)=X(I2) X 1 (I 4) = X (I 4)(hI) I=(hI) I I Y (I3) = Y1 (I3)X1 (I6) =X (I6) Y 1 (I 6) =Y (I 6) IBC=INT (BC) (3) = Y1(3)Y (2) = Y 1 (2) GO TO 101 GO TO 101 CONTINUE D0 401 0 = ES 1LINES. 41 B 1001 303 302 E0# 405 301 401 402 ပ υ υ υ U 147

CALL STRIP3(TOL1) Y(2)=Y1(2) D0 406 I7=2,6 I7H1=I7-1 X1(I7H1)=Y(I7) Y1(I7H1)=Y(I7) Y1(I7) Y1(I7

PSPT0038 PSPT0039 PSPT0045 PSPT0046 00006490 FSPT0037 00006500 PSPT0038 PSPT0040 FSPT0041 PSPT0042 E #00 Ld Sa PSPT0044 00006590 PSPT0047 00006510 00006520 00006540 00006550 00006530 00006560 00006570 00006580

TRNS0015 **TRNS0016 TRNS0018** TRNS0025 **TRN S0035 TRNS0006 TRN S0007** TRNS0008 **TRM S0009 TRNS0010** TRNS0011 **TBNS0012** TRNS0013 **TRN S0014 TRN 50017 TRNS0019 TRNS0020 TRNS0022 TRNS0023 TRN 50024 TRNS0026 TRN S0028 TRNS0029 TRN S0030 TRNS0032** TRN SO033 TR NSO 034 **TEN SO 00 3** TRN 50005 TRNS0027 TR N S003 1 TRN SO036 **TRNS0001 TRNS0002** TRNS0004 **TRNS0021** 00006790 00006810 00006820 00006860 00006870 00006890 00006950 THIS SUBRODTINE DHANGES THE ABCISSAS OF THE END POINTS TO ORIENT THE 00006600 00006650 00006660 000006690 00006700 00006730 00006740 00006760 00006780 00690000 00006920 00006930 01 690000 00006610 00006620 00006630 00 0 0 0 0 6 6 4 0 000006670 00006680 00006710 00006720 00006750 00006770 00006800 00006830 00006840 00006850 00006880 00 00 69 10 COMBON /COB1/SMAT (4,4) .T (4) .HKAREA (4) SUBROUTINE TRANSI (N. EC. TOL 1, ES 1, ES 2) DEC= INT ((EC-PLOAT (INT (EC)) +. 01) *10.) POINTS AS IF THEY ARE AT THE ORIGIN. COMMON /COM2/X (30) , Y (30) , YOR IG (30) CONNON / CON3/X1 (5) , Y1 (5) , Y0 (5) COMMON /CON4/IFAIR, ACC, LIMIT 302 GO TO 301 303 X 1 (I 1) =X (N) -X (NHI 1P1) YO(I 1) = YORIG (NHI 1P1)60 T0 G0 T0 CALL STRIP1 (TOL1) CALL STRIP2(TOL1) CALL STRIP3 (TOL1) $(I \ I \ I \ I \ I \ I) = Y (N \ I \ I \ I) = Y$ (DBC. EQ. 1) DO 101 I1=1,5 L+LI-N=LdLINN (DEC. EQ. 2) (DEC. EQ.3) Y (NH 1) = Y 1 (2) Y (BA2)=Y1(3) Y (BA 1) = Y 1 (2) Y (NA2) =Y 1(3) INTEGER DEC Y (1) =9999. (l) | Y = (H) T**TO 500** GO TO 500 GO TO 500 CONT INUE NN 2= N-2 Q=-ES2 1 I F 00 1001 101 301 302 30 J υ υ υ **U** U 149

TRNS0038 TRNS0039 TRNS0040 TRNS0044 TRNS0045 **TRNS0037** TRNS0042 TRNS0043 TRNS0046 TRNS0041 00007040 00000000000 00006970 08690000 000006900 0000000 00007010 00007020 00007030

T (NH 1) = Y 1(2) DO 304 I2=1,5 NMI2=N-I2 X1(I2) = X (NMI2) Y1(I2) = Y (NMI2) Y1(I2) = Y (NMI2) CALL STRIP1(TOL1) Y (NM2) = Y1(2) SOO RETURN END

STP 10 002 STP 10001 00000000 STRIP1 WOULD BE SUBSEQUENTLO0007070 00007080 THIS SUBBOUTINE CALCULATES THE PIRST THREE FAIRED POINTS (OR CENTER OP A SERIES OF FIVE DATA POINTS. APPLIED TO CONTINUE THE PAIRING PROCESS PCINT)

STP 10017 STP 10018 STP 10003 STP 10 004 STP 10005 **STP 10 006** STP 10007 STP 10008 STP 10009 STP10010 STP 10011 STP 10012 STP10013 STP 10014 STP 10015 STP 10016 STP10019 STP 10 020 STP 10021 STP 10023 STP 10024 STP 10025 STP10026 STP 10027 STP10028 STP10029 STP 10030 STP 10032 STP 10033 STP 10034 STP 10022 STP10031 00007150 06020000 00007100 00007110 00007120 00007130 00007140 00007160 00007170 00 007 180 00007190 00007200 00 00 72 10 00007220 00007230 00007240 00007250 00007260 00007270 00007280 00007290 00007300 00007310 00007320 00000330 000003340 00007350 00007360 00007370 00007380 000003390 COMMOM /COM1/SMAT(4,4),T(4),WKAREA(4) COMMON / COM3/X1 (5) , Y1 (5) , Y0 (5) COMMON /COM4/IFAIR, ACC, LIMIT SUBROUTINE STRIP1 (TOL1) 103 104 01 20 SHAT (4,1)=SMAT(1,4) SHAT (3,2)=SHAT (1,4) SMAT (2,2)=SMAT (1,3) SHAT (2,3) =SHAT (1,4) SHAT (2,1)=SHAT (1,2) SHAT (2,4)=SHAT (4,2) SMAT (3,4)=SMAT(4,3) SAAT (3,3)=SAAT (4,2) SHAT (3, 1) = SHAT (1, 3) SI1=SI1+X1(I2) ++I1 SHAT (1, I 1P1) =SI 1 SMAT (4, I 1H2) =SI 1 00 8 D0 102 I2=1,5 DO 101 I1=1,6 (I1.GE.4) SHAT (1, 1) = 5. (I1.LE.3) I 182=I 1-2 GO TO 105 I +1 I=1 41 I GO TO 101 GO TO 101 CONTINUE CONTINUE CONTINUE SI 1=0. 11 1 P 1001 102 103 104 105 101 000 U 151

1002 υ

CONT INUE

STP 10035 STP 10036

STP10045 STP 10055 STP 10058 STP 10065 STP10038 STP10039 STP10040 STP 10042 STP 10048 STP10049 STP 10050 STP 10052 STP10053 STP 10054 STP10059 STP10063 STP10064 STP 10 04 1 STP 10043 STP 10044 STP 10046 STP 10 047 STP 10051 STP 10056 STP 10057 STP 10060 STP10062 STP 10066 STP10037 STP 10061 00007460 00007480 00001490 00007500 00007510 00007520 00007530 00007540 00007550 00007560 00007580 00007590 000007600 00 00 76 10 00007630 00007650 00007660 00007680 00007690 00007700 00007710 00007430 00007440 00007450 00007470 00007570 00007640 00007670 00007420 00007620 IP (X1 (I4) . NE.0..08. I3. NE.1) TI3=TI3+Y1 (I4) *X1 (I4) ** (I3-1) NOW CALL LEQTIP PROM THE INSL LIBRARY TO CALCULATE THE CUBIC T1 (3) =Y0 (3) +SIGN (TOL1, DELTA1) Y 1 (2) = YO (2) + SIGN (TOL1, DELTA 1) Y1(1) = Y0(1) + SIGN(TOL1, DELTA1)[P2=T(1)+T(2)+T1(2)+T(3)+T1(2)++2+T(4)+T1(2)++3 YP 3=T (1) +T (2) +I1 (3) +T (3) +I1 (3) ++2+T (4) +X1 (3) ++3 YP1=T (1) +T (2) *X 1 (1) +T (3) *X1 (1) *+2+T (4) *X1 (1) *+3 (hI) |X+EII=E II (ABS (Y1 (1) -YP1) .GT. ACC) IPAIR=IPAIR+1 (ABS (Y1 (2) -YP2) .GT.ACC) IPAIB=IPAIB+1 (ABS(Y1(3)-YP3).GT.ACC) IPAIB=IPAIR+1 CALL LEQTIP (SMAT, 1, 4, 4, T, 0, 4KAREA, IER) (X1 (I4) . EQ. 0. . AND. I3. EQ. 1) Y1(2) = YP2Y1(3) = YP3Y + (1) = Y P + Y(DELTA.LT.TOL 1) (DELTA.GE.TOL 1) (DELTA. GE.TOL 1) IF (DELTA.LT.TOL 1) (DELTA.GE.TOL1) (DELTA. LT. TOL 1) DELTA=ABS (DELTA1) DELT A=ABS (DELTA 1) DELTA=ABS(DELTA1) DBLTA 1 = YP1 - YO(1)DELTA 1=YP2-YO(2)DELT A 1=Y P3-Y0(3) 107 I 4= 1,5 DO 106 I3=1,4 COEPPICIENTS. T (I3) =TI3 BETURN TI3=0_ **UNZ** 8 41 IP 41 41 11 ي ا 106 107

152

STP20002 STP20014 STP20015 STP20018 STP20019 **STP20028** STP20035 STP20003 STP 20005 STP 20006 STP 20 008 STP20009 STP20010 STP20012 STP20013 **STP20016** STP20017 STP20020 STP20024 STP 20025 STP20026 STP20029 STP20033 STP 20034 STP20004 STP20007 STP20011 STP 20022 STP20027 STP 20030 STP 20032 STP20036 STP20001 STP 20 03 1 STP2002 STP 2002 00007720 00 0077 30 00007740 00007760 00007780 00001790 00007810 00007820 00007830 00 00 78 40 00007850 00007860 00007870 00007880 00007890 01 00 0000 00007920 00007930 00007950 00007960 00007970 000003980 00001990 0008000 00008020 00008030 00008040 00008050 00008070 00007750 00007770 00007800 0001900 0100000 00008010 00008060 STRIP1 WOULD BE THIS SUBROUTINE CALCULATES THE SECOND AND THIRD PAIRED POINTS PRON SUBSEQUENTLY APPLIED TO CONTINUE THE PAIRING PROCESS. SERIES OF FIVE DATA POINTS WITH END POINT FIXED. CONBON /COM1/SHAT (4.4) "T (4) "WKAREA (4) TI3=TI3+ (Y1 (I4) -Y1 (1)) *X1 (I4) **L3 CORNON /CON3/ 1 (5) , Y1 (5) , Y0 (5) COMMON /COM4/1PAIR, ACC, LIMIT 104 GO TO 103 SUBROUTINE STRIP2 (TOL1) G0 T0 SHAT (3, 1) = SHAT (1, 3) SHAT (2,2) =SHAT (1,3) SMAT (2,1)=SMAT (1,2) SMAT (2,3)=SMAT (3,2) X1(L1)=X1(L1)-X8EP SI1=SI1+X1 (I2) **I1 SHAT (1. I 1M1) =SI 1 SMAT (3, I1M2) =SI1 IP (I 111.GE.4) IP (I 111.LE. 3) DO 107 I4=2,5 DO 101 I 1=2,6 DO 102 I2=2,5 DO 106 I3=1,3 00 91 L1=1,4 XREP=X1(1) GO TO 101 I-11=1811 I 182=I 1-2 GO TO 105 T (I3) =TI 3 GO TO 101 CONTINUE CONTINUE SI1=0. TI 3=0. 105 106 102 104 103 101 107 5 000 U U

153

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STP20038 STP20046 STP20049 STP 20052 STP20037 STP 20039 STP20040 STP 20041 STP20042 STP20043 STP20044 STP20045 STP20047 STP 20048 STP 20050 STP20051 00008080 06080000 0008100 00008110 00008120 00008130 00008140 00 008 1 50 00008160 00008170 00008180 00008190 00008200 00008210 00008220 NOW CALL LEQTIP PRON THE INSL LIBRARY TO CALCULATE THE COEPPICIENTS. YP2=Y1(1)+T(1) *X1(2) +T(2) *X1(2) **2+T(3) *X1(2) **3
YP3=Y1(1) +T(1) *X1(3) +T(2) *X1(3) **2+T(3) *X1(3) **3 Y1(2)=Y0(2)+SIGN(TOL1,DELTA1) Y 1 (3) = YO (3) + SIGN (TOL1, DELTA 1) (ABS (Y1 (2) -YP2) .GT. ACC) IPAIR=IPAIR+1 (ABS (Y1 (3) -YP3) .GT.ACC) IPAIR=IPAIR+1 CALL LEQTIP(SHAT, 1, 3, 4, T, 0, WKAREA, IER) Y1(3) = YP3Y1(2) =YP2 IF (DELTA.GE.TOL 1) (DELTA.GE.TOL1) (DELTA. LT.TOL 1) (DELTA. LT. TOL 1) DELTA=ABS (DELTA 1) DELTA=ABS (DELTA1) DBLTA1=YP2-Y0(2) DELTA 1=YP3-Y0 (3) 92 L2=1,4 11 41 00 11 υ

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154

X 1 (L 2) = X 1 (L 2) + X R B P

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BETURN END

STP20053 STP20054

STP 30 00 2 STP30010 STP30012 STP30013 STP30014 STP30015 STP30016 STP30017 STP30018 STP30019 STP30020 STP30025 STP30026 STP30029 STP30030 STP30031 STP30032 STP30034 STP30035 STP30003 STP30004 STP30005 STP 30 006 STP30007 STP 30008 STP 30 009 STP30021 STP30022 STP30023 STP 30024 STP30027 STP 30028 STP 30033 STP30011 STP30001 00008470 00008510 00008520 00008550 00008560 00008260 00008330 00008350 00008380 00008390 00 10 00 00 00008420 00008440 00008450 00008460 00008490 00008530 00008540 00008570 00008580 00008590 00008600 00008270 00008280 00008290 00008300 00 00 83 10 00008340 00008370 00 084 10 00008430 00008480 00008500 00008320 0908360 THIS SUBBOUTINE CALCULATES THE PAIRED SECOND DATA POINT FOR A SERIES STRIP1 NOULD BE SUBSEQUENTLY APPLIED TO (DELTA.GE.TOL1) Y1(2)=Y0(2)+SIGN(TOL1,DELTA1) [[]=T[]+ ([] ([4) -Q+X] ([4) -Y] (]) +X] ([4) ++[] 'P2=Y1(1)+Q*X1(2)+A2*X1(2)**2+A3*X1(2)**3 (ABS(Y1(2)-YP2).GT.ACC) IPAIR=IPAIR+1 COMBON /COM3/X1 (5) , Y1 (5) , Y0 (5) A2=(T2*S6-T3*S5) / (S4*S6-S5**2) A 3= (T 3 *S 4-T2 *S5) / (S4 * S6-S5 * *2) Y1(2) = YP2COMMON /COM4/IPAIR,ACC,LIMIT FALRING PROCESS. SUBROUTINE STRIP3 (TOLI) T2=TI3 T3=TI3 IS=tS S5=SI1 S6=SI1 OF FOUR DATA POINTS. SI 1= SI 1+ I (I 2) ++ I 1 (DELTA.LT.TOL 1) X 1 (L 1) = X 1 (L 1) - X REPX 1 (L 2) = X 1 (L 2) + X 8 B F DELTA=ABS(DELTA1) DELTA 1=Y P2-Y0 (2) CORNON /COR8/Q DO 102 I2=2,4 DO 101 I1=4.6 DO 104 I4=2.4 103 I 3=2,3 D0 92 L2=1,4 DO 91 L1=1,4 (I1.BQ.4) (I1.EQ.5) (I1. EQ. 6) (I3.EQ.2) (I3.EQ. 3) CONTINUE THE XREP=X1 (1) **FI 3=0.** RETURN SI1=0. END 5 8 4 41 **P**. 2 **A** L H 102 103 101 104 5 92 ບບ U

APPENDIX G

The following is an example of a typical bow section for a ship with a bulbous bow mounted sonar dome. Although the section is for a hypothetical ship it illustrates the capability of the computer program to fair, spline and interpolate a curve having an infinite slope at an end point.

In the CRV matrix shown, the items written in block numbers are input values while those in italics are values calculated by the program. The elements left blank were not used in this example. The values of tolerence, accuracy and limit are:

> TOL = 1.00 ACC = 0.05 LIMIT = 10



	1	2	3	4	5	6	7
1	0.0	0.0	0.000	0.0	0.333	-0.480	1.570
2	2.0	7.0	6.000	0.0	0.530	-0.675	0.802
3	6.0	8.0	7.301	0.0	0.394	-0.122	-0.279
4	9.0	4.0	4.999	0.0	-0.156	0.160	-0.776
5	12.0	2.0	2.805	0.0	-0.242	0.241	-0.473
6	17.0	2.0	1.609	0.0	-0.218	0.149	0.002
7	23.0	3.0	2.934	0.0	-0.041	0.009	0.366
8	28.0	5.0	5.086	0.0	0.006	-0.003	0.416
9	30.0	6.0	5.954	0.0			0.407
• •							
31	1.0	9.0	0.0	1.1			
32	2.0	4.1	0.0				

CRV MATRIX

The resulting interpolated values for increments of $\Delta X = (30-0)/20$ are as follows:

X	<u> </u>	DY/DX
0.0	0.0000	*****
1.5	5.4206	1.3048
3.0	6.8443	0.6555
4.5	7.4269	0.1361
6.0	7.3018	-0.2867
7.5	6.4713	-0.8319
9.0	4.9988	-0.9816
10.5	3.7259	-0.7238
12.0	2.8047	-0.5114
13.5	2.1714	-0.3371
15.0	1.7846	-0.1815
16.5	1.6191	-0.0415
18.0	1.6542	0.0867
19.5	1.8721	0.2010
21.0	2.2473	0.2956
22.5	2.7465	0.3656
24.0	3.3316	0.4116
25.5	3.9724	0.4396
27.0	4.6403	0.4476
28.5	5.3051	0.4368
30.0	5.9543	0.4308

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Figure G.l shows the curve generated as a result of fairing the given data points.