





The Naval Ship Research and Development Center is a U.S. Navy center for laboratory effort directed at achieving improved sea and air vehicles. It was formed in March 1967 by merging the David Taylor Model Basin at Carderock, Maryland and the Marine Engineering Laboratory at Annapolis, Maryland.

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## **INTRODUCTION**

 $\sqrt{2}$ The Naval Ship Research and Development Center (NSRDC) established a broad research project under the Variable Depth Sonar Program directed • toward the deve Lopment of improved experimental and ana lytical techniques for predicting the steady-state characte ristics of cable-towed systems. The project consists of basin teats to ascertain the hydrodynamic loading functions of various types of faired sections and cables under steady conditions. This report deals with basin tests to determine the loading functions of a cable faired with sectional type fairing.<br>The differential equations for describing mathematically the two-

dimensional equilibrium configuration and forces of a cable-body system<sup>1</sup> were derived a number of years ago. Solutions for these equations can be obtained numerically using a digital computer<sup>2</sup> provided the body characteristics and cable loading functions are known. The characteristics of the towed body can either be calculated or experimentally determined using various  $mechanisms<sup>3</sup>$ <sup>4</sup>. The cable loading functions are not generally known and past practice at NSRDC has been to use the loading functions proposed by different investigators<sup>1,5,8</sup>. Some of these functions are based on limited experimental data; but in the case of faired towcables the re is conside rable doubt as to whether any of the existing functions can accurately represent the loading on an arbitrary fai red towcable . This doubt is borne out in the diffe rence obtained in tangential Loading of seve ral faired shapes recently investigated<sup>7,8,9,10</sup>

In view of the aforementioned uncertainties, the limited experimental data on which to base loading functions, an d the lack of experiments to ascertain the validity of proposed loading functions and especially on sectional fairing, the NSRDC project was established to obtain the two-dimensional steady-state hydrodynamic loading functions of a faired towcable for application to existing and future VDS systems with sectional fairing. The experimental approach consisted of towing a rigid faired-cable model in the David Taylor Model Basin at various speeds, cable angles, and model submergences and measuring the hydrodynamic force using the DTMB Cable-Fairing Dynamometer. The se

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References are listed on page 15

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data were then used with a curve-fitting computer program to obtain mathematical expressions for the loading functions.

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Thi<sup>3</sup> report is concerned with experiments on a sectional fairing similar to those conducted for the continuous trailing -fairing models . The report describes the subject fairing model, the towing dynamometer, the test instrumentation and test procedures; presents tabulated values and graphs of normal and ta ngential loading functions and drag coefficients; and provide <sup>s</sup> mathematical expressions obtained for the loading functions.  $\mathbb N$ 

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### DESCRIPTION OF FAIRED-CABLE MODEL

The faired-cable model consists of a simulated stranded-cable element on which 10 pieces of sectional fairing are attached. Table 1 gives the physical characteristics of the test model.





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The sectional enclosed fairing is basically a DTMB Number 7 shape as de <sup>s</sup>cribed in Reference 11 and is similar to that presently in use on the SQA-lO VDS system . A typical section, shown in Figure 1, consists of a ha <sup>r</sup>d plastic trailing section, a stainless steel headpiece or leading section, alineme nt rods and associated hardware. Each of these sections is placed over the simulated cable to form a 7-foot test model. The completed model formed an enclosed fairing model with a scalloped leading edge. The scalloped leading edge is the result of the design of the fairing for winding on a storage drum . The simulated cable, 2.4 inches in diameter, consists of twenty-four 0.25-inchdiameter copper strands with a left-hand lay joined to a seamless tube.

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# Figure 1 - A Sectional-Type Fairing Section



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## DESCRIPTION OF DYNAM OMETER AND INSTRUME NTA TION

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The cable-fairing dynamometer is shown in Figure 2 with the faired-cable model attached. The normal force  $X$ , lateral force  $Y$ , and tangential force Z on the model are sensed by 4-inch-cube modular force gages of the type described in Reference 3. Interchangeable gages with capacities ranging from 50 pounds to 1000 pounds are available depending on the accuracy desired. The dynamometer design limits any of the three component forces to 500 pounds or less.

The tilt-table angle is adjustable so that the cable angle  $\varphi$  relative to the free stream may be varied from 90 degrees to 30 degrees in 5-degree increments. The vertical position of the model and tilt table is also adjustable by me ans of an electric hoist so that the model subme rgence may be varied from 0 to 7 feet. A weight-pan system provides a means of counterbalancing the model weight on the gage s at each subme rgence and cable angle .

Instrumentation for this test consisted of a 200-pound-capacity gage for • the X force, a 1000-pound-capacity gage for the Y force, and a 50-pound capacity gage for the Z force; two integrating digital voltmeters, a scanner and a printer for processing the X and Z gage signals; and a strip chart recorder for monitoring the Y force. Carriage speed was measured using a photo-cell and gear wheel with the signal fed to an electronic counter.

### TEST PROCEDURES

The model was towed in the high-speed basin of the David Taylor Model Basin from 90 degrees to 30 degrees in approximately 10-degree increments. The model submergence was varied from 31 inches to 73.5 inches in approximately 9-inch increments at towing speeds of  $2$ ,  $4$ , and  $6$  knots. In addition, for a cable angle of 90 degrees, the model was towed at various speeds from  $l$  to  $l0$  knots at all submergences. The  $X$ ,  $Y$ , and  $Z$  forces were recorded for each test condition. The Y force measurement was used primarily as a basis for alining the model with the flow to minimize the  $Y$ force and to provide a means of monitoring lateral oscillations at various speeds.



## HYDRODY NAMIC FORCES

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Since the measured forces were generated by a three-dimensional model which pierced the water surface, the data contain both end effects and surface effects . The desired two-dimensional hydrodynamic forces were obtained from these data by the following analysis. The X and Z forces were plotted as a function of model submergence for each angle and speed . As model subme rgence increases, a length is reached after which both X and Z forces become linear functions of submergence for a given speed, i.e., end and surface effects become essentially constant. Typical plots for the X and Z force as a function of submergence for an angle of 59.9 degrees are shown in Figures 3 and 4, respectively. Slopes of the linear portion of the force-subme rgence curves were determined for each angle and speed and have been tabulated in Table 2. These slopes represent the two-dime nsiona l hydrodynamic forces per unit length acting on the faired cable model.

#### TABLE 2



Two-Dimensional Hydrodynamic Force for an Enclosed Sectional Fairing





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80 04 O9  $50$ Submergence in inches ó C ♦  $\overline{\mathbf{6}}$ p Þ  $\overline{\mathbf{30}}$  $\overline{\mathbb{E}}$  $\frac{0.2 \text{ km/s}}{0.4 \text{ km/s}}$ 10  $\frac{1}{\sigma}$  $\overline{12}$  $\tilde{8}$  $\overline{\textbf{r}}$ Tangential Force in pounds



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## HYDRODYNAMIC LOADENG FUNCTIONS

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The hydrodynamic loading functions are defined as the ratio of the steady-state, two-dimensional, hydrodynamic forces acting on an element of cable at an angle  $\varphi$  to the free stream to the force when the element is normal to the free stream  $(\varphi = 90$  degrees). For a given faired-cable geometry and speed, these loading functions are dependent only on the cable angle .

The normal and tangential loading functions were determined using the slopes of Table 2. The slopes at each cable angle were divided by the slope of the normal-force curve for  $\varphi = 90$  degrees to obtain the loading values for each angle and speed and the resulting values are tabulated in Table 3.

#### TABLE 3

## Values of Normal and Tangential Lording Functions



A curve-fitting process was performed on each set of values in Table 3 to obtain mathematical expressions for the loading functions. The process consisted of generating a group of least-squares curves for each set of loading values using the BVPDE3 program and selected combinations of terms in the trigonometric series,

 $A_0 + A_1 \cos \varphi + B_1 \sin \varphi + A_2 \cos 2\varphi + B_3 \sin 2\varphi$ 

for which the loading boundary conditions are satisfied. Using the CMPFN2

program, curves in each group were compared with the data to determine the best form for each loading function. The resulting mathematical expressions for the loading functions, neglecting any effect of Reynolds number, are

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 $\Lambda$ (φ) = -1.5716 + 1.7367 cos  $\phi$  + 2.4065 sin  $\phi$  -0.1651 cos 2 $\phi$  -0.7808 sin 2 $\phi$  [1]

and

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 $\Gamma(\varphi) = -0.1158 + 0.4641 \cos \varphi + 0.1158 \sin \varphi$  [2]

where  $\Lambda$  and  $\Gamma$  are the normal  $(X/X_{90})$  and tangential  $(Z/X_{90})$  loading functions, respectively. The foregoing expressions and the attendant data from Table 3 are plotted in Figures 5 and 6. The prescribed boundary conditions are

 $\Lambda(0) = 0$ ,  $\Lambda(90) = 1$ , and  $\Gamma(90) = 0$  [3]

On the tangential loading function shown in Figure 6, there appears to be some effect due to Reynolds number. However, the effect with this sectional fairing is the reverse of that shown in Table 2 of Reference 8.

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Figure 5 - Normal Loading Function as a Function of Cable Angle

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90 80 70  $60$ Cable Angle  $\varphi$  in degrees  $50$ æ  $\Gamma(\phi) = -0.1158 + 0.4641 \cos \phi + 0.1158 \sin \phi$ 40 æ  $30$ Be  $\frac{6 - 2 \text{ knots}}{\sqrt[3]{2 + 6 \text{ knots}}}$ 20  $10$  $\frac{1}{2}$  $0.4$  $0.3$  $0.2$  $0.1$ 

Figure 6 - Tangential Loading Function as a Function of Cable Angle

Tangential Loading Functions, Z/X<sub>80</sub>

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## DRAG COEFFICIENT

The drag coefficient  ${\tt C_R}$  and corresponding Reynolds number  ${\tt R_d}$  were calculated for each speed using the following expressions:

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C_R = \frac{R}{\frac{1}{2} \rho dV^2}
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 [4]

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and

$$
R_d = \frac{Vd}{V}
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 [5]

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d is the fairing thickness,

- R Is the drag per unit length of cable When the cable is normal to stream and is equal to the slope  $\frac{\Delta X}{\Delta s}$  of the linear force versus submergence plot at  $\varphi = 90$  degrees  $(R = X_{90})$ ,
- s is the distance along the cable (submergence),
- V is the speed,
- p is the mass density of fresh water at 70 degrees F, and
- v is the kinematic viscosity of fresh water at 70 degrees F.

The results of these computations are shown in Figure 7 as fairing drag coefficient as a function of Reynolds number.

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