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This technical report has been reviewed and is approved for publication.

MICHAEL P. DOUGHE

Project Engineer

per an

RICHARD L. VERGA Technical Area Manager/POD-1

FOR THE COMMANDER

PHILIP E. STOVER Chief, High Power Branch Aerospace Power Division

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The resonant current  $i_1$ : (a) for  $\psi_{\mathbf{rk}} \neq \psi_{\mathbf{rk}} \min$ ; (b)  $\psi_{\mathbf{rk}} \neq \pi$ ; 40 (c)  $\psi_{\mathbf{rk}} = \pi$  and  $\Delta \beta_{\mathbf{k}} > 2\pi$ .

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#### SECTION I

#### INTRODUCTION

The purpose of this work was to investigate and experimentally demonstrate the feasibility of a reliably operating light weight converter to process kilowatts of electric power, and with the promise to operate in the megawatt range.

The system was studied as a voltage transforming and stabilizing dc to dc converter. Yet, its internal structure and mechanisms were to be suited for direct three phase ac to dc conversion without the use of a heavy low pass input filter.

The reliability of operation was to be demonstrated by the continued converter operation in the presence of severe disturbances, such as short circuited output terminals. This reliability should be also indicated by operation of the switching elements at a low and, unconditionally, predictable stress and thus a low heat dissipation level at the required switching frequencies.

The light weight of the system is rooted in the high internal frequency of 10 kHz at full power, since the weight of magnetics and filters is, roughly, inversly proportional to the frequency of converter operation for a given power level.

- 1 -

A 10 kW converter system was constructed. Its test verified the proposed functional concepts and the expected performance. An efficiency of the inverter which drives the high voltage transformer of up to 97 percent could be derived from the test data. The inverter was successfully integrated with the light weight 10 kW transformer-rectifier-filter for a dc output voltage of 10 kV and with an internal frequency of 10 kHz.

The system aspects of an ac or dc to dc converter and the therewith associated external characteristics are treated in section II. Special attention is given to potential ripple suppression in the currents of an ac generator and in the load using methods of active, nondissipative, filtering; the available mechanisms for potential systems stabilization are indicated.

The important frequency limiting phenomena, especially in switches, are treated in section III. The method used to overcome the now classical limitations of static power converters to below 1 kHz and to attain 10 kHz with existing components, is presented. The potential for use of yet higher frequencies is indicated. The method can be applied to any type of available and future fast switching elements, such as thyristors, transistors and vacuum spark gap switches.

The used power circuit and its characteristic features are presented in section IV. Design of the 10 kW converter is treated in section V, followed by the presentation of test results of the experimental model in section VI.

- 2 -

An analysis of the experimentally obtained results is contained in the conclusions of section VII. The results are related to the characteristics of the components which perform the individual converter functions and are used to project estimates of their usefulness in the construction of larger converter systems, as intended.

The above referred to analysis is based on a differentiated approach to power and energy densities of the major converter components reflecting the actual stresses which are being, intrinsically, imposed on the respective devices.

The road to the construction and demonstration of larger power units, such as 200 kW and beyond seems to have been cleared by the successful completion of the 10 kW system. Newly available GATT type thyristors appear to allow construction of up to 0.15 MW modules with one set of switches in one single bridge.

#### SECTION II

#### SYSTEM ASPECTS

The converter links the load to its dedicated source of electric energy. The converter's purpose is to

- (a) transfer the electric energy to the load;
- (b) transform the pattern of the voltage waveform of the source of electric energy, the generator, to another pattern as required by the load, such as a three phase ac to dc transformation;
- (c) perform a voltage scaling function;
- (d) stabilize the average load voltage so that it remain within preset limits of tolerance during conditions of steady state operation;
- (e) limit the harmonic content that is "seen" by the generator and by the load, respectively, and which is caused by:
  - (el) possibly, an inherent conflict between the intrinsic characteristics of generator and load, respectively, and the
  - (e2) internal functional mechanism of converter operation;
- (f) facilitate over all system stability by reconciliation of conflicting dynamic characteristics of the source and the load;
- (g) provide specified generator terminal conditions between cycles of operation, such as possibly a path for continued current flow, as required by certain sources of electric dc energy

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The number of above enumerated functions which the converter has to perform will depend on the respective characteristics of the generator and on the load. This is discussed with reference to an example in which a three phase generator feeds a dc load.

1. AC to DC Conversion.

First, it is stated, that the polyphase generator technology produces a machine which is meant to generate sinusoidal ac voltage waveforms in its individual phases. These phases are meant to supply current of the same waveforms to the load, which if possible, should be in phase with the voltage, or at least, should not be lagging the voltage appreciably. The desired harmonic spectrum of the current  $i_s$  of the individual phases of the generator is shown in figure l(a). The dc load requires, ideally, a harmonic content of its load



Desired harmonic spectra of the current (a)  $i_s$  of each

phase of a polyphase generator and (b) i of the dc load.

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- 6 -

current i with no other spectral line than that at f = 0, as shown in figure 1(b). The converter should thus transform the composite action of the individual waves of the generator phases to a smooth dc in accordance with its functions stated in (b). This above described functions of waveform transformation is independent of the voltage scaling function, as stated under (c) above. The various aspects which are characteristic for the chosen example are now discussed with reference to figure 2. The three phase generator, shown in figure 2(a), emits the well known three phase voltage waveforms e. shown in figure 2(b) which is transformed to its rectified waveform e , filtered to the form e, and eventually scaled to the voltage ae. The letter "a" designates the scaling factor of a function which is performed within the inverterscaler; this is the function cited in (c) above. The current waveform in each phase, the composite current i srec of the rectified phases, its filtered form  $i_i$  and, eventually, its scaled form  $i_i/a = I_0$  which is the load current are shown in figure 2(c). The frequency spectra of the current waveforms shown in figure 2(c) are indicated in figure 2(d) by  $|F_{i_s}|, |F_{i_i}|$  and  $|F_{i_o}|$  as functions of the order number n=1,2,.... of the spectral frequencies nf, where f is the single phase frequency of the three phase generator.

The classical function of the low frequency filter indicated as part of figure 2(c) is to "remove" the harmonic content of the voltage waveform  $e_{s rec}$ , so as to smooth the voltage  $e_i$  and the thereto pertaining current  $i_i$ , before inversion for the purpose of voltage scaling takes place. The high frequency filter removes only the harmonic content that has been generated by the process of inversion and rectification.

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It means, that all of the reconciliatory functions between the desired spectra shown in figure I(a) and (b) should be performed by the full wave rectifier bridge in conjunction with the therewith associated low frequency filter.

No known rectifier-filter can perform that function, even if weight and size were of no concern. The currently accepted "ideal" is a low pass filter with an infinitely large inductor  $L_i$  in its conventional  $L_iC_i$  configuration as indicated in figure 3. The infinitely large inductor  $L_i$  would cause a





rectangular phase current i with a flat top and without the indentation shown in figure 2(c). The Fourier series for this current waveform is given by

$$i_{s}(t) = (2\sqrt{3} I_{so}/\pi) \{ \sin\omega_{s}t - \frac{1}{5} \sin 5\omega s_{t} + \frac{1}{7} \sin 7\omega_{s}t - .... \}$$
 (1)

- 8 -

where I is given by

 $I_{so} = P_o/\eta_s e_{sp}\sqrt{6}$ 

and

0	=	the intended output power of the system;
<sup>1</sup> s	=	the over all efficiency of the electric
		power system, except that of the generator;
sp	=	the rms voltage of the individual phases
		of the ac generator

The "infinitely large" inductor will guarantee a smooth current  $i_{s}$  rec and result in an equally smooth form of the load current  $i_{o}$ . Yet, it creates the harmonic content of the current in the individual phases of the generator which are quantified in equation (1).

(2)

If on the other hand there were a rectifier-low-frequency-low-pass-filter combination which would allow the phase currents  $i_s$  to remain sinusoidal then the generator would get its desired current waveform and a near infinite filter capacitor  $C_i$  could smooth the voltage  $e_i$ , as desired by the load.

It was the purpose of the preceding argument to show that no known rectifier filter combination could satisfy the requirements that were stated with reference

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to figure 1, even if infinitely large filter components could be afforded.

The low pass filters of the reality of technology consist of components of the minimum acceptable size. The inductors are, usually, sufficiently large to provide a continuous current  $i_{s rec}$  so that the current in one diode pair of the full wave bridge rectifier as shown in figure 3 would not be interrupted and reinitiated during a work cycle of that diode pair. The purpose of this restriction is to avoid current peaking in the diodes in the filter capacitor and, possibly, in the generator, all of which would contribute to undue instantanuous stresses on components and to their heating.

The needed kVA rating of the dedicated generator can be estimated from the relation

(3)

kVA required = 
$$\frac{P_o}{\eta_e (p.f.)}$$

where

í

 $p.f. = \frac{\int_{0}^{T} \int_{0}^{f} e_{s} dt}{\int_{0}^{e} e_{s} rms^{i} s rms}}$ , being the power factor, as defined in the time domain [1], and where

s rms = 
$$\left(\frac{1}{T}\int_{0}^{1}i_{s}^{2}(t)dt\right)^{\frac{1}{2}}$$

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so that  $i_s$  can be any function of time and need not be considered as being the composite of its Fourier components.

The power factor p.f. of a rectifier-filter with an "infinitely" large inductor is approximately .955. Yet, this power factor decreases rapidly with the decreasing size of L. Power factors of 0.7 and less are, therefore, i commonplace in these type of systems and are the cause for use of a commensurately larger generator.

The converter which operates from an input voltage  $e_i$  can be equipped with the property of a nondissipative type active filter which would remove the low frequency content of  $e_i$ . This converter can thus reduce the burden that is, otherwise, imposed on the low pass input filter. This can be restated in the following way: If

$$e_{i} \simeq e_{i} \qquad \{1 + m \sin 6 \omega_{i} t\} \qquad m < < 1 \tag{4}$$

then the maximum possible attenuations  $a_d$  of the normalized ripple amplitude m and caused by this active filters is approximated by

$$\mathbf{a}_{\mathbf{d}} \simeq (\mathbf{f}_{\mathbf{F}}/\mathbf{6}\mathbf{f}_{\mathbf{s}})/\pi \tag{5}$$

for the given conditions [2], where

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The total attenuation of the peak to peak ripple of, approximately, 11 percent of the rectified waveform  $e_{s rec}$  is given by

(6)

$$100 v_{orpp}/v_{o av} = 11/a_{pi}a_{d}$$

where

 $f_F = 2f_i$ 

vorpp = the peak to peak ripple of the output voltage vo av = the average value of the output voltage api = the attenuation of the passive input filter as shown in figure 3.

The two attenuation factors  $a_{pi}$  and  $a_d$  are considered to be independent of each other because it concerns the attenuation of a passive network followed by the effect of a pulse modulation process, by way of approximation.

The pulse modulation process which is incorporated in the converter operation [2] serves the dual purpose: (1) to stabilize the output voltage by performing pulse width (PW), pulse frequency (PF) or mixed PW-PF modulation (PW-PFM) to contribute to the attenuation of the low frequency ripple contained in

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e<sub>s rec</sub> and (3) to, possibly, contribute to the dynamic stability of the over all electric power system by performing the appropriate variations of this process of pulse modulation, as needed. The physical structure of the power circuit and its intrinsic mode of operation, preserve the functional integrity of the system as a whole independent of externally imposed adverse conditions. The above discussed example illustrates the functions (a) through (g) of the converter as stated as the outset of this section.

Means to attempt a reconciliation of the inherent conflict between an ac generator and a dc load are currently being investigated [3]. The discussion of these means is beyond the scope of this treatise.

#### 2.2 DC to DC Conversion.

In this case power is derived from a dc source, as shown in figure 4. All properties, required of a converter and listed in (a) through (g) at the outset of this section apply, except (b), which does not apply in this case, since dc is converted to dc, even though the voltage of the source of electric energy may vary and, possibly, oscillate in a damped or undamped manner.

The functions of the converter which include output voltage scaling and stabilization could be extended to include maximum power point tracking of the source and if required, dynamic stabilization of the system as a whole. There is no other function in the power system which lends itself as suitably for the purpose of system stabilization as the application of a control signal

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Figure 4. DC converter system in block diagram form.

to a very high impedance electronic mechanism which controls the rate and the rate of change of transfer of energy. It controls, namely, the pulse modulation process which in turns governs the power system behavior as a whole. The functional mechanism of any dc to dc converter, for brevity referred to as dc converter, is described with reference to figures 5(a) and (b). The current  $i_s$  of the dc source of electric energy with the voltage  $e_s$  passes through a high frequency (H.F.) input filter on its way to the inverter and pulse modulator. This inverter consists of a set of switches and other thereto pertaining nondissipative elements such as inductors and capacitors. The inverter generates a high frequency (kHz) carrier current  $i_1$  as shown in figure 5(b). This carrier

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Figure 5. DC converter: (a) functional block diagram, (b) current waveforms.

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current is being modulated in frequency and in amplitude, while it is being generated. The referred to modulation process serves the purpose of control of the transfer of charge per half cycle

$$A_{k} = \int |i_{1}| dt = T_{ok} |i_{1}|_{av} = T_{ok} i_{s}$$

$$t_{k}$$
(7)

where:

t k

A

= the instant of time at which the k-th half cycle of operation starts; i<sub>1</sub> is not, necessarily, zero at that instant; ۱

 $T_{ok} = t_{k+1} - t_k$ , the duration of one half cycle;

$$t_{k} = \sum_{i=1}^{k-1} T_{oi}; \quad T_{om} \neq T_{on};$$
$$t_{k+1}$$
$$|i_{1}|_{av} = (1/T_{ok}) \int |i_{1}| dt$$
$$t_{k}$$

The charge  $A_s$  which is tranferred from the source of energy through the inverter to the transformer during one second

$$s = \sum_{k=1}^{F} A_{k}$$
(8)

where

F = the number of half cycles with duration  $T_{ok}$  per second, even through  $T_{om} \neq T_{on}$ 

The magnitude of the average current  $i_{s av}$  during the second in which all  $A_k$  of equation (7) are being summered up,

$$\left|\mathbf{i}_{s,av}\right| = \left|\mathbf{A}_{s}\right| \tag{9}$$

The "absolute magnitude" signs in equation (9) are meant to emphasize that Amperes are being equated to Coulombs per second which is, dimensionally, correct.

The carrier current i<sub>1</sub> is processed by the high frequency transformer XF with a voltage step-up ratio 1:a which performs the function of a scaler. The secondary transformer circuit includes the rectifier which consists of a set of diodes in form of a diode bridge. This bridge converts the scaled current

$$i_2 = i_1/a$$

(10)

to its rectified form i2r. The high frequency (H.F.) output filter removes

the harmonic content at double the average inverter frequency and beyond. Thus

$$f_{F} = 2f_{i}$$
(11)

where

f; = the average inverter frequency;

 $f_F$  = the pulse repetition rate F as defined with reference to equation (8)

The input filter and the output filters of the converter perform an analogous function: they isolate the high frequency operation of the dc converter from the low frequency characteristic of the source and of the load. In that sense, they provide short circuit paths for the high frequency components which are being generated by the internal functional mechanism of the converter.

The listing of the converter's functions which were enumerated at the outset of this section is now repeated and identified in terms of the preceding discussion of figure 5:

- (a) the converter, clearly, transfers the electric energy from the source to the load;
- (b) not applicable for a dc to dc conversion;
- (c) voltage scaling is performed by the transformer XF;

(d) the average load voltage is stabilized by letting the electric charge per cycle;

$$A_k/T_{ok} = \text{constant};$$
 (12)

if a constant  $Z_L$  is assumed, even though  $e_s$  may vary during every pulse interval  $T_{ok}$ ;

- (e1) modify relation (12), if so desired, to shift part or all of the burden of the harmonic content which is generated by variations of e<sub>s</sub> to the source, or to the load according to a preset pattern; yet, let A<sub>s</sub> as defined in (8) be a constant;
- (e2) remove the harmonic content at the average frequency  $f_F$  and beyond by use of the input and the output filters;
- (f) contribute to the dynamic stability of the electric power system by introduction of appropriate effects of the current carrier modulation process;
- (g) not treated in this section.

The purpose of high internal frequencies is the reduction of the physical sizes of

- (1) the transformer XF;
- (2) the input and the output filters;
- (3) all reactive components which are needed for the inversion and for the pulse modulation processes.

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The physical weight of the above named power components is, roughly, proportional with the inverse of the frequency  $f_i$  of the inverter operation, everything else being equal. A figure of merit FM can be formulated in an attempt to quantify the significant aspects of this causal relationship between the physical weight  $W_p$  and some of the other conditions. The figure of merit

$$FM = \frac{\Pr_{o}f_{i}}{W_{p}(1-\eta_{s})f_{s}}$$
(13)

All symbols, used in equation (13) have been defined before. This figure of merit modifies the more commonly used power density  $P_0/W_p$ , expressed in kW/kg by introduction of the relative power loss  $(1-\eta_s)$  and by the frequency ratio  $f_i/f_s$ . It is observed that if for a change of the inverter frequency  $f_i$  from  $f_{i1}$  to  $f_{i2}$  and of the corresponding physical weight from  $W_{p1}$  to  $W_{p2}$ 

$$(W_{p1} - W_{p2})/W_{p1} \simeq (f_{12} - f_{11})/f_{11}$$
 (14)

then the figure of merit will not change substantially if

$$W_{p2} \simeq (f_{11}/f_{12}) W_{p1}$$
 (15)

Selation (15) is meant to express only a gross approximation.

The same figure of merit can be applied to any of the individual passive components of the converter system, especially to the transformer XF, the filter components, and other reactive components.

The quest for increasingly higher frequencies of operation is an obvious result of the desire to reduce the physical weight of power equipment, especially in the case of air or space born equipment.

A number of phenomena which can cause an increase of power losses and in doing so imperil the integrity of the functional mechanism of converters, tend to limit the upper limits of internal frequencies of converter operation. These are treated in the following section III.

#### SECTION III

#### FREQUENCY LIMITING PHENOMENA

Skin and proximity effects in conductive elements, parasitic effects associated with the individual components, and the physical limits of functional concepts supply most of the frequency limiting phenomena.

The presence of skin and proximity effects in magnetic components and capacitors requires the careful application of design techniques which are well known from the areas of radio and radar engineering. The significant frequency ranges which are being encountered are:

- (a) the low frequency region of conventional and advanced electrical power engineering, say, from zero to near 1 kHz;
- (b) the intermediate region of internal frequencies of advanced dc converter technology, from 10 to 50 kHz;
- (c) the high frequency region caused by the switching phenomena in power semiconductors within fractions of microseconds, which cause appreciable frequency components in the order of MHz.

Sizable energies are involved in all of these frequency ranges. The significance of the effects of abrupt switching in power circuits is discussed with reference to figure 6.

Opening of switch  $S_f$  in the circuit shown in figure 6(a) causes the forcible interruption of the current  $i_f$  flowing through inductor L The magnetic field which is maintained in the inductor L and is caused by the current  $i_f$  before its interruption cannot be sustained without this current. The magnetic energy  $\varepsilon_m$  which is associated with this field can, likewise, not vanish and tends to be reconverted to electric energy  $\varepsilon_a$ .

This energy reconversion process from  $\varepsilon_m$  to  $\varepsilon_e$  seeks to maintain current flow through the opening switch  $S_f$ . A mechanical switch will arc under



Figure 6. Power electronic switching circuits which incorporate intended and parasitic inductive elements in series with the switching elements for (a) forced interruption of the switched current, (b) the thereto pertaining current form i<sub>s</sub> in the switch S<sub>f</sub> and (c) switching at the instant of natural termination of the switch current i<sub>res</sub> in a resonant circuit, (d) the thereto pertaining current form i<sub>res</sub> in the switch <sup>s</sup>res.

CLOSED

(d)

CLOSED

(b)

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Oscilloscope trace of: (a) current voltage and power dissipation waveforms of a switching transistor operating under conditions of forced current interruption as discussed with reference to figures 6(a) and (b); (c) the power dissipation of a switching transistor which processes a resonant current as described with reference to figures 6(c) and (d).

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these conditions and thus demonstrate visibly the stresses that are imposed on it. The semiconductor switch undergoes similar stresses whose phenomena are limited to the concerned lattice structure of the device and not visible, but not less severe.

The extent of these stresses as translated into conversion of electric energy to heat is indicated by the photographs of curve traces shown in figure 7(a). The upper photograph of this figure shows current  $i_f$ and the voltage  $v_{ce}$  of a transistor which performs the function of switch  $S_f$ . The lower photograph in figure 7(a) shows the  $v_{ec}$   $i_f$  product as provided by a multiplying (Philips) oscilloscope.

It is seen that the  $v_{ce}i_{f}$  product has a moderate value for conditions of settled current flow. There is a narrow peak at the instant of closing of the switch  $S_{f}$  which is due to the finite time which is needed for the closing process. Falling of the voltage  $v_{ce}$  across the switch and rise of the current  $i_{f}$  is the cause for this narrow peak of the  $v_{ce}$  $i_{f}$  product at the initiation of the current pulse.

The area under the peak of the  $v_{ce}$  i product at the termination of the current pulse appears to exceed the area under the remainder of the  $v_{ce}$  i curve for this current pulse. It is obvious that most of the heat dissipations in the switch is not caused by the process of conduction, but by the processes of current termination. The power loss

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in the switch

$$P_d = v_{cess} i_{fss} (T_k/T_{ok}) + f_F (\varepsilon_s + \varepsilon_T)$$

where

vcess	= the voltage drop over the conducting transistor under
	conditions of settled current flow;
ifss	= the transistor current under the same conditions;
T <sub>k</sub>	= the pulse width;
ε <sub>s</sub>	= the energy dissipation caused by the turn on process;
ε <sub>T</sub>	= the energy dissipation during the opening phase of the
	switch.

Equation (16) demonstrates the frequency dependence of the switching losses. Each switching device is limited in its capability to dissipate heat. This limitation imposes one ceiling on the repetition rate  $f_F$  with which it can switch a current  $i_f$ .

Another, more subtle limitation on the tolerance of the  $v_{ce}$  if peak is imposed by the internal distribution of current density within the lattice of the semiconductor device. This internal distribution of current density can exceed the heat tolerance of the material on that spot and can

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(16)
thus cause damage to the device. This damage increases rather sooner than later and can cause a break down of the device, often referred to as "secondary" break down.

The above described phenomena are the primary cause for limitation of the internal frequency of operation of power converters. This limitation increases with the increasing magnitude of currents that are being processed by the switching elements [4].

The preceeding description of the difficulties of the opening of switches in inductive circuits does not reveal a new phenomenon, but reiterates a well known process. The argument is not limited to semiconductor switches but remains valid for any type of switches, whether they are mechanical in structure, gas filled or vacuum tubes with spark gap ignition.

The current  $i_{res}$  in the circuit shown in figure 6(c) assumes a sinusoidal form when switch  $S_{res}$  closes at the instant of time t=0 and if  $i_{res}(0)=0$ , as indicated in figure 6(d). It is assumed that the initial conditions on capacitors C and C<sub>o</sub> and on the inductor L are appropriate for that purpose. The current  $i_{res}$  rises with a limited di<sub>res</sub>/dt at the time where the switch S<sub>res</sub> is closed This di/dt is determined by

$$di_{res}/dt = (e_s - v_c - v_c)/L$$
 at t=0 (17)

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where

 $v_{co}$  = the voltage on capacitor C<sub>o</sub> at t=0;  $v_{c}$  = the voltage on capacitor C at t=0

Likewise is

$$di_{res}/dt(T_{o}) \simeq - di_{res}/dt(0)$$

(18)

if

$$T = \pi \sqrt{LC}$$

and if the bulk of the electric energy, present in the circuit is not removed during the time interval  $T_o$ . The switch closes at time t=0 and does not commutate a (diode) current of appreciable magnitude as could be the case in the circuit shown in figure 6(a). The  $v_{ce}^{i}res$  product in the switching element associated with the circuit of figure 6(c) near the time t=0 is, therefore, minute compared to the one described with reference to the circuit shown in figure 6(a).

Yet, the real problem could arise at the time t=T when the switch S res is opened. The resonant current

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$$i_{res}(T_0) = 0$$
 when  $t = T_0$  (19)

as indicated in figure 6(d).

The  $v_{ce}$   $i_{res}$  product is there, necessarily zero at that time. This fact is verified by the photograph of the  $v_{ce}$   $i_{res}$  curve trace, shown in figure 7(b). A larger amplification of the  $v_{ce}$   $i_{res}$  product was used this time because of the absence of the substantial spike which appears in figure 7(a). The effect of the sinusoidal current on the shape of the power dissipation curve in figure 7(b) is clearly discernible. The small spikes which resemble electric noise at the termination of the pulse are comparable to the maximum magnitude of the  $v_{ce}$   $i_{res}$  product. The area under these spikes can be termed minute compared to the area under the dissipation curve under conditions of settled current flow.

It appears that the opening of a switch in an inductive circuit at a time when the switch current is zero, has the advantage of minimum power dissipation during the opening process of the switch. The preceeding statement is nothing else, but the reiteration of a fact that has been well known from the early days of electric science. The disappearence of the substantial dissipation spike shown in figure 7(a), removes the frequency dependent part from equation (16) for all practical purposes. The power loss in the switching elements becomes thus, practically, independent of the internal converter frequency (4), (5). The above

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explained advantage of the use of series resonant circuits for purpose of converter operation was used for the technical approach for development of a converter technology which would tolerate relatively high internal frequencies.

### SECTION IV

#### THE DC CONVERTER WITH SERIES RESONANT CIRCUITS

A dc converter system was chosen which utilizes a modulated current carrier as discussed above for purpose of controlled power transfer and combines this function with the advantage of switch operation in resonant circuits.

# 1. The Power Circuit

The essential features of the power circuit of a dc converter which employs series resonant circuits are shown in figure 8. The shown simplified schematic illustrates the above referred to type of dc converter in its half bridge configuration. Two switch pairs consisting of one thyristor CRli and an anti-parallel diode Dli (i = 1,2) are used to close and open in alternating succession two series resonant circuits. Each of these two circuits connects to the junction of capacitors Cl1 and Cl2, and includes the inductor L<sub>1</sub>, the primary



Figure 8. Simplified schematic of a dc converter which employs a series resonant circuit.

winding  $W_1$  of the transformer XF, and one of the above identified switch pairs. The first switch pair CR11-D11 connects the described circuit to the possitive terminal of the source of electric energy with voltage  $e_s$ ; the second switch pair CR12-D12 connects the same circuit to the negative terminal of the same source.

The output voltage  $v_0$  of the converter is assumed to be of constant magnitude at this time. The secondary winding  $W_2$  of the transformer XF switches abruptly within the rectifier bridge consisting of diodes D2j (j = 1,2,3,4). This transformer reflects a voltage  $v_{xa}$  back into the primary circuit which always apposes the directions

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of flow of the resonant current  $i_1$ . The polarity of this voltage  $v_{xa}$  opposes, necessarily, the directions of flow of the current  $i_1$ , since  $v_{xa}$  is limited by the output voltage  $v_0$  as modified by the transformer winding ratio

(20)

$$a = N_2/N_1$$

where

 $N_i$  = the number of turns in winding  $W_i$  of transformer XF.

The above stated limitation that

$$\begin{vmatrix} v_{xa} \end{vmatrix} = \frac{v_o}{a}$$
(21)

is due to the fact that the voltage on the secondary winding  $W_2$  of transformer XF rises under the impact of the voltage that is impressed on the primary winding of the same transformer until it is, forcibly, limited by the secondary diode bridge to the voltage  $v_0$  of capacitor  $C_0$ . The size of this capacitor as reflected into the primary circuit, namely

$$a^{2}C_{0} = C_{2} >> C_{1} = C11 + C12$$
 (22)

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Capacitors  $C_1$  and  $C_0$  are so dimensioned that the voltage  $v_0$  over  $C_0$  will

$$v_{\text{orpp max}} < 2e_s \frac{C_1'a}{C_0}$$
 (23)

Inequality (23) follows from the application of the simple rule that

$$\Delta Q = (C_1/a^2) 2ae_s = C_o v_{orpp}$$
(24)

where

The inequality (22) renders the magnitude of  $v_{xa}$  almost invariant with the tacit understanding that a control system exerts an influence on  $i_2$  so that  $v_o$  remain within prescribed limits of tolerance from a nominal value  $V_o$ . The voltage  $v_x$  on the primary transformer winding WI







# Figure 9.

(a) Equivalent source voltage  $e_{sac}$ ; (b) equivalent load voltage  $v_{oac}$ ; (c) net excitation voltage  $e_{sac} - v_{oac}$  of resonant circuit; (d) resonant current  $i_1$ ; (e) capacitor voltage  $v_{c1}$ ; (f) double excited  $L_1C_1$  circuit; (g) equivalent circuit of series capacitor inverter-converter.

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presents itself then as a square wave with amplitude  $v_{xa}$  as given by equation (21) and a frequency which is dictated by the pattern of operation of the switches CR11-D11 and CR12-D12.

The operation and the philosophy of the power circuit shown in figure 8 is briefly explained with reference to figure 9.

The series resonant circuit consisting of inductor  $L_1$  and the (Thevenin) equivalent capacitors  $C_1 = C_{11}+C_{12}$  is indicated in figure 9(f). This resonant circuit is driven on one port by a square wave  $e_{s ac}$  with amplitude  $e_s/2$  and on the other port by a square wave  $v_{o ac}$  with amplitude  $v_o$ . These square waves are indicated in figures 9(a) and (b) respectively. The amplitude  $e_s/2$  stems from the fact that the resonant elements of the circuit in figure 8 "see" Thevenins equivalent of  $e_s$  when "looking" into the junction of capacitors  $C_{11}$  and  $C_{12}$  toward the source. This equivalent source has the voltage  $e_s/2$ if  $C_{11} = C_{12}$ . The square wave  $e_{s ac}$  is generated by connecting the resonant circuit with inclusion of the transformer XF in continuing succession and abruptly to the positive terminal of the source with voltage  $e_s$ , thus creating a potential  $e_s - e_s/2$ , or to the negative terminal of the same source and creating a potential  $0 - e_s/2$ . The negative voltage  $-\frac{1}{es}/2$  is defined with respect to the same terminals of the LC circuit as the possitive voltage  $+e_s/2$  was defined for the positive amplitude of  $e_{s ac}$ .

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The cause of the voltage  $v_{c\ ac}$  which appears on the terminals of the primary winding  $W_1$  of the transformers XF was explained above in the context of circuit operations with respect to figure 8. The winding ratio  $N_2/N_2$  is here assumed to be unity so that for the sake of simplicity  $v_{xa} = v_0$ , with the tacit assumption that all components are ideal.

Square waves  $e_{s \ ac}$  and  $v_{o \ ac}$  have the same frequency under conditions of cyclic stability, yet they differ by a "phase shift" which amounts to a "phase angle"  $\psi_{rk} = \omega_{o \ kr}^{T}$  as indicated in figures 9(a) through (e). Under the assumed conditions of cyclic stability is  $\psi_{rk} = \psi_{rk+1}$ .

The net driving voltage of the resonant circuit  $e_{s ac} - v_{o ac}$  is indicated in figure 9(c). The ensuing resonant current  $i_{l}$  is indicated in figure 9(d). Finally the capacitor voltage  $v_{cl}$  which was defined before is depicted in figure 9(e).

Slope and magnitude of the resonant current  $i_1$  can be derived immediatly from the net driving voltage  $e_{sac} - v_{oac}$ . Under conditions of cyclic stability the energy exchange  $\varepsilon_{sk}$  between the two equivalent sources and the resonant circuit must be zero over each closed cycle of operation, or half cycle of the resonant current. It means that

$$\varepsilon_{sk} = \int (e_{sac} - v_{oac})i_{1}dt = 0$$

(25)

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The transfer of energy from the source to the load is controlled by adjusting the "phase angle"  $\psi_{rk}$  which is predominantly governed by the natural half period of the resonant circuit T<sub>o</sub> and by the externally controlled instant of time t<sub>k</sub> at which the appropriate thyristor is being energized.

The current  $i_1$  is conducted by thyristor CR11 during the time interval  $T_{kf}$  as indicated in figure 9(d). The capacitor voltage  $v_{c1}$  reaches its crest when  $i_1 = 0$  at the end of the above referred to time interval  $T_{kf}$ . The net voltage  $e_{s ac} - v_{o ac}$  then apposes the flow of current through the diode D11 and energy is being returned from the resonant circuit to its driving "sources". This return of energy increases with increasing phase angle  $\psi_{rk}$  and this in turn requires that the energy which is accepted during the interval  $T_{kf}$  decrease for unchanged  $e_s/2$  and  $v_o$ . Decrease of the energy accepted by the resonant circuit in this time interval requires, thus a decrease of the amplitude of  $i_1$ . The "phase angle"  $\psi_{rk}$  thus controls the amplitude of  $i_1$  and by implication the average  $|i_1|_{av}$  of the absolute value of  $i_1$  which is being transferred to the load.

Another way to describe this control process of  $i_1$  is to state that the amplitude of  $i_1$  and the average of its absolute value

 $|i_1|_{av}$  increases for  $T_{ok} + T_{o}$ , or  $\psi_r \neq 0$  (26)

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$$i_1|_{av}$$
 decreases for  $T_{ok} \neq 2T_{o}$ , or  $\psi_{rk} \neq \pi$  (27)

It means that

$$i_1 |_{av} \to \infty$$
 (28)

if the inverter frequency of operation

$$f_{io} = 1/(T_{ok} + T_{ok+1}) \rightarrow f_{o} = 1/2T_{o} = 1/2\pi\sqrt{L_{1}C_{1}}$$
 (29)

is tuned to near the natural frequency of the resonant circuit, assuming ideal conditions for simplicity of explanation. Conversely,

$$i_1 |_{av} \rightarrow I_i$$
 (30)

if the inverter frequency of operation

$$f_i = 1/(T_{ok} + T_{ok+1}) = 1/2hT_o < f_o = 1/2T_o$$
 (31)

and

 $I_i$  = an average current which is a function of h h > l, an arbitrary constant.

The converter frequency is detuned from the natural frequency of the resonant circuit in the case which is characterized by relation (31). Detuning is achieved by appropriate choice of the instants of time  $t_k$  at which the thyristors are being energized. Detuning of  $f_i$  from  $f_o$  increases the apparent impedance of the resonant circuit and reduces the transfer of energy from the source to the load.

The "phase angle"  $\psi_{rk}$  which governs the ratio  $f_i/f_o$ , controls the magnitude of  $|i_1|_{av}$  and, in effect, the power flow toward the converter's load.

The "mechanism" by which  $\psi_{rk}$  controls the rate of flow of charge  $A_k = |i_1|_{av}$ T<sub>ok</sub> for the kth cycle toward the load is further explained with reference to figure 10. All time intervals are expressed in radians  $\beta$  by use of the formerly implied, transformation

$$t \rightarrow \beta/\omega_{o}$$
 (32)

The angle  $\psi_{rk}$  is in figure 10(a) near its minimum

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The resonant current  $i_1$ : (a) for  $\psi_{rk} \neq \psi_{rk \min}$ ; (b)  $\psi_{rk} \neq \pi$ ; (c)  $\psi_{rk} = \pi$  and  $\Delta \beta_k > 2\pi$ .

$$\psi_{rk} \min = T_{off} \omega_{o}$$

where

t<sub>off</sub> = the required turn-off time of thyristors CRli.

The amplitude Ikl of  $i_1$  is for these conditions near its maximum steady state value, as determined by design. Figure 10(b) indicates  $i_1$  when  $\psi_{rk} \approx 2/3\pi$ . The capacitor  $C_1$  loses the charge  $\Delta Q_k$  which corresponds to the ampere-seconds during the time interval  $\psi_{rk-1}$  prior to ignition of the thyristor CR1i at time  $\beta_k$ . The initial inductor voltage  $v_L$  ( $\beta_k$ ) is therefore smaller than in the case illustrated in figure 10(a). This mechanism can be also recognized by a study of figures 9(d) and (e) in this context. The amplitude  $I_{k1}$  depends, largely, on  $v_L(\beta_k)$ . It is seen that  $I_{k1}$ , as indicated in figure 10(b), has appreciably decreated with respect to its magnitude in figure 10(a). So has the average  $|i_1|_{av}$  of the absolute value of  $i_1$ . It also appears by visual comparison of figures 10(a) and (b) that a smaller amount of ampere-seconds of  $i_1$  in figure 10(b) stretchs over a larger time interval  $\Delta\beta_k = \beta_{k+1} - \beta_k$ .

The amplitude  $I_{k1}$  reaches for invariant  $e_s$  and  $v_o$ , its minimum where  $\psi_{rk} \ge \pi$ and  $\Delta\beta_k > 2\pi$ , as indicated in figure 10(c). The transfer of charge toward the load is for  $\psi_{rk} \ge \pi$  governed by a pulse frequency modulation process because the charge per cycle

(33)

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$$\beta_{k} + 2\pi$$

$$\int |i_{1}| d\beta = \Delta_{k \min} \quad \text{for } \psi_{rk} \ge \pi \quad (34)$$

$$\beta_{k}$$

is independent of the pulse repetition rato  $f_F$  and the average current

$$|\mathbf{i}_1|_{av} = \mathbf{f}_F \Delta_k \min$$
(35)

for conditions of cyclic stability for any  $e_s$  and any  $v_o$  within design limits, provided  $\psi_{rk} \ge \pi$ .

It is noted in passing that the waveforms of the current i, in figures 10(a) and (b) illustrate cases of the mixed pulse amplitude-pulse frequency modulation (PA-PFM).

A more detailed treatment of this tropic is found in the literature [6],[8].

The above described process of power transfer and control embodies the characteristics of a converter which were enumerated at the outset of section II, including the capacity to modify the harmonic content of the source voltage by means of active filtering. It embodies, furthermore, the advantageous process of terminating resonant currents through its controlled switching elements at the instants of time when  $i_1 = 0$  which was discusses in the preceeding section 3. These characteristics allows the construction of high power converters with

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capacities in the multikilowatt range with employ internal frequencies of 10 kHz with presently available materials. The ongoing improvement of materials, devices and circuits could raise this frequency of hardware type equipment within the following 5 to 10 years, to 50 kHz and beyond.

2. The Electronic Protection and Control System.

a. General Principles.

The power circuit of the dc converter shown in figure 8 is governed by an electronic system which performs two distinct and totally separated functions: (1) the protection of the power system against the possible effects of untimely firing of any of the thyristors CR1i and (2) the control of transfer of energy to the load.

The two above named parts of the electronic system are named in the shown order, because of their relative significance for the converter operation as a whole. The transfer of energy through the converter is controlled by the application of trigger signals to the appropriate thyristors at the appropriate instants of time  $t_k$ , as discussed throughout sections II and III. These instants of time  $t_k$ determine the frequency of operation  $f_i$  of the current carrier  $i_l$  for everyone of its succeeding half cycles with duration  $T_{ok}$  as discussed with reference to figures 9 and 10.

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The converters which use forced current commutation for the turn-off of their thyristors provide an ohmic closed circuit for the conduction of current from the positive terminal of the source of electric energy through the thyristor(s) and back to the negative terminal of the source. It means, that the integrity of the system relies on the presumed certainty that this thyristor will be turned off before the current in this circuit would reach a magnitude which could not be handled by the turn-off mechanism [9]. In other words: a once initiated state of conduction of a "load current" i<sub>th</sub> carrying thyristor has to be terminated by a mechanism of the converter which is limited to a maximum thyristor current value i<sub>th max</sub>. If for any reason that turn-off mechanism would not work, then it is hoped that the inverter fuse will.

In the case of the occurence of a short circuit condition as described above, it becomes irrelevant wheter firing of the complementary thyristor which would also provide a short circuit path for the source current would take place or would be avoided. The integrity of the conventional system which employs forced commutation of thyristor currents thus depends on satisfying both of the following two conditions:

- (a) that the thyristor current i<sub>th</sub> would not rise above a preset maximum value i<sub>th</sub> under any regular or irregulat conditions of operation;
- (b) that the complementary thyristor in series with the current carrying thyristor would not be fired as long as the current carrying thyristor has

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not completed its cycle and the thereupon following turn-off time has elapsed.

The converter which employs the series resonant circuit shown in figure 8 places the series capacitor  $C_1 = C_{11} + C_{12}$  in the path of "load current" i<sub>th</sub> flow through the conducting thyristor. No mechanism, other than the aposing voltage  $v_{c1}$  of the series capacitor is needed to turn-off  $i_{th} = |i_1|$ . And this voltage  $v_{c1}$  feeds on  $i_{th}$  so that the conducting thyristor will, unfailingly, terminate the current conductions under all conditions of operation.

The preceeding argument was made to show that it suffices to comply only with requirement described above in (b) in order to safequard the integrity of the series capacitor converter, indicated in figure 8. Requirement (a) is, unconditionally, satisfied by an inherent circuit property: the presence of the series capacitor C1. Avoidance of excessive voltage and current stresses is discussed in subsection 4.2.3.

b. The Electronic Protection System.

The electronic protection system prevents firing of thyristors CRIi as long as the companion thyristor has not terminated its cycle of conduction and has regained its forward blocking capability [10].



Figure 11. Block diagram of the protection and of the control systems.



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Figure 12. Critical signal waveforms of power control system.

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The implementation of this principle is indicated in the block diagram representation shown in figure 11. The critical waveforms which are associated with this process are indicated in figure 12. The function of the electronic protection system is discussed here with reference to these figures.

A back bias signal appears on thyristor CR11 after completion of conduction of the resonant current in the normalized time interval  $\omega_{o}T_{kf}$ , formerly defined with reference to figures 9 and 10. The cause for appearance of this signal is the state of conduction of the antiparallel diode D11 which now conducts the current  $i_{1}$  for the normalized time interval  $\psi_{rk} \ge \psi_{r \min}$ . The length of this time interval  $\psi_{rk}$  is not known yet at  $t = t_{k} + \omega_{o}T_{kf}$ . The Back Bias Sensor 1 established the fact of the existence of a back bias condition and conveys this information in the form of a 0-1 signal  $e_{BB1}$  to the Signal Delay and Continuity Check block; this block emits a signal  $e_{sD1}$  if, and only if the signal  $e_{BB1}$ has persisted without interruption for a time interval  $\psi_{r \min} = \omega_{o} t_{off}$ . Signal  $e_{sD1}$  energizes the Clear Signal Storage 1, which stored the received information "indefinitely" until such time when a reset signal is applied to it. The above referred to clear signal appears at the time  $\psi_{r \min}$  and energizes one input port of the following AND circuit. Thyristor CR12 is now free to be triggered at the option of the electronic control system.

A signal Z1 which emanates from the electronic control system appears at the second port of the above referred to AND gate when  $\beta = \psi_{rk}$ ; the origin of this signal Z1 will be explained at a later point of this description.

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Coinciduce of signals  $e_{sD1}$  and 21 at the AND port energizes the Firing Pulse Generator 2 which then fires CR12; this thyristor will conduct current  $i_1$ until i=0, at which time diode D12 continues conduction of this current. The ensuing back bias condition of thyristor CR12 is detected by the Back Bias Sensor 2. Analogous signal processing as explained concerning signal  $e_{BB1}$ ensues and thyristor CR11 is, eventually, fired.

It is stressed that the protection system acts completely independent from the control system, in its approval for access of the firing signals of the control system to the respective gates. Condition (b) stated in subsection a. is thus satisfied and the system can perform.

c. The Electronic Control System.

The series capacitor converter which was introduced with reference to figure 8 can be provided with the output characteristics of a voltage limited current source [6],[8].

The principle of control is based on the functional philosophy of the "Analog signal to discrete time, interval converter (ASDTIC)" [2],[12],[13]. This type of converter control is now in increasing use because it provides a high degree of static and dynamic stability to the therewith controlled pulse modulaters and is largely temperature insensitive due to an internal auto-compensating mechanism. It is often - incompletely - referred to as a "two loop" control

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system which does not characterize its inherent feature. A replica  $k_i i_l$  of the resonant current  $i_l$  is derived via a current transformer CT from the resonant circuit. This replica is rectified to the form  $k_i |i_l|$  and fed into an integrater, as indicated in figure 11.

The signal processing operation which follows is, abundantly, described in the literature [2],[8],[12],[13]. If the attenuated output voltage signal

$$k_{o}v_{o} < (k_{o}v_{o})_{nom}$$
(36)

is smaller than the nominal value  $\begin{pmatrix} k & v \\ o & o & nom \end{pmatrix}$  of this signal then the signals Zi(i=1,2) are generated at the instants of time when

$$\beta_{k+1}$$

$$k_{i} \int |i_{1}| d\beta = e_{ir} \Delta\beta_{k}$$

$$\beta_{k}$$
(37)

(38)

It follows that  

$$\beta_{k+1}$$

$$(1/\Delta\beta_{k}) \int |i_{1}|d\beta = |i_{1}|_{av} = e_{ir}/k_{i}$$

$$\beta_{k}$$

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The average of the absolute value of  $i_1$  is thus a constant, whatever the shape of  $i_1$  and whatever the length of the time interval  $\Delta\beta_k$ . It means that the output current  $i_0$  of the system indicated in figure 8 is, arbitrarily, determined by adjusting

$$e_{ir}^{/ak_{i}} = i_{o} = |i_{2}|_{av} = |i_{1}|_{av}^{/a}$$
 (39)

The peak to peak voltage of C1

$$v_{c1pp} = \int |i_1| dt$$

$$t_k^{-T} (k-1)r$$
(40)

(41)

where

$$t_{k}^{+T}kf$$

$$\int |i_{1}|d\beta \approx |i_{1}|_{av} T_{ok}$$

$$t_{k}^{-T}(k-1)r$$

for conditions of cyclic stability.

It follows from (40) and (41) that

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$$v_{clpp} = |i_1|_{av} T_{ok}/C_1 = e_{ir} T_{ok}/C_1 k_1$$
 (42)

where equation (38) is included into the consideration. Equation (42) states that  $v_{clpp}$  can vary as much as  $T_{ok}$  for the case of continuous current. This variation is limited to

$$T_{0} + t_{off} \stackrel{\sim}{\sim} T_{0k} \ge 2T_{0} \tag{43}$$

which is less than two to one [6]. In practice the ratio

$$T_{ok max}/T_{ok min} \approx 2/(5/4) = 1.6$$
 (44)

If  $k_{oo} v_{oo} > (k_{oo} v_{oo})_{nom}$ , then the maximum Threshold Sensor in figure 11 removes the blocking signal from the AND circuit which will then let the  $k_{oo} v_{oo}$  signal go out to the summer  $\Sigma$ . The effect is that the  $e_{ir}$  level is modified. The current  $|i_1|_{av}$  is then reduced to a value so that a preset value  $v_o$  is maintained. The current source characteristic of the converter is modified and assumes the characteristic of a voltage limited current source.

## SECTION V

## DESIGN OF THE 10 kW CONVERTER

1. General Requirements.

Certain specific requirements were formulated to demonstrate the feasibility of a reliable light weight dc converter. A number of critical functional characteristics had to be demonstrated that would justify the expectation that a converter with the capacity of handling megawatts of power could be constructed, based on the demonstrated principles.

The critical characteristics had to hold the promise that this converter

- (a) would operate with a high degree of reliability;
- (b) could be constructed with a high power density, expressed in kW/kg.

The requirement of reliability includes:

- (al) applications of a functional concept that holds a minimum of uncertainties; this includes a progressive overload and short circuit capability of the output terminals;
- (a2) minimization and enforcement of an absolute and predictable limit on all ratios

$$i_{\text{max}}/i_{\text{av}}$$
 and  $v_{\text{max}}/v_{\text{av}}$  (44)

for all converter and component functions;

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(a3) a well controlled limitation of heat development in all parts of the converter.

The high power density requires:

(b1) a relatively high internal frequency of operation, such as 10 kHz(b1) demonstration of successful converter operation at that frequency.

The following basic requirements were formulated:

Voltage, es

Input:

Current, i ~ 20 ADC

Output: Voltage, v<sub>ol</sub> 250 VDC, to be dissipated in a resistive load For Test Purpose Only: Current, i<sub>ol</sub> 40 A

For Integration Voltage, v<sub>02</sub> 250 VAC, square wave with a frequency with HV between 5 and 10 kHz; Transformer:

Current  $|i_{o2}|_{av}$  1 A, in phase with above square wave.

600 VDC, to be supplied from a battery bank;

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Voltage Ripple

vorms

1% of v o av

Duty Cycle

d

120 seconds "on" as a maximum,followed by 15 minutes "off".

2. The Power Circuit Design.

The lower limit for the composite efficiency of the converter and of the high voltage transformer was, as a precautionary measure, assumed to be

$$\eta_{\min \text{ comp}} \simeq 0.83$$
 (45)

The amplitude  $v_x$  of the square wave  $e_{s ac}$  which is imposed on the transformer was estimated to be [6]

$$v_{xa} \simeq \eta e_s/2 = (0.83)(300) = 250 V$$
 (46)

An average current

$$|i_1|_{av} = P_0/v_{av} = 10^4/250 = 40 A_{av}$$
 (47)

appeared necessary in order to transfer 10 kW to the load.

The peak to peak voltage of capacitor C

$$\mathbf{v}_{clpp} > |\mathbf{i}_{l}|_{av} \mathbf{T}_{ok} / C_{l}$$
(42)

The voltage

$$v_{clpp} > 2e_{s}$$
 (48)

in order that the system operate properly [6]. It follows from (42) and (48) that

$$C_1 > |i_1|_{av} T_{ok}/2e_s = 40.50.10^{-6}/1200 \simeq 2\mu F$$
 (49)

where

$$T_{ok min} = 1/2f_i = 50 \cdot 10^{-6}$$
 seconds

The series inductance

$$L_{1} = (T_{0}/\pi)^{2}/C_{1} = (40 \cdot 10^{-6}/\pi)^{2}/2 \cdot 10^{-6} = 80 \ \mu H$$
(50)

assuming that [6]

$$T_o/t_{off} \simeq 4$$

The size of the output capacitor  $C_o$  is governed by the output current  $i_o$ , the filter frequency  $f_F$  and the acceptable peak to peak output voltage ripple  $v_{orpp}$ . The node equation for the positive terminal of the output filter capacitor  $C_i$  can be written as:

$$i_2 = i_c + i_o = Cdv_{co}/dt + i_o$$
 (51)

where

i<sub>c</sub> the capaciter current leaving the above defined node di<sub>o</sub>/dt  $\approx$  0 for purpose of estimate of C<sub>o</sub> with the understanding that v<sub>orpp</sub> < < 1.

From equation (51) follows that for a normalized frequency  $f_n = 1/\pi$ 

• 
$$v_{co}(\beta) = v_{co}(0) + (I_2/C_{on})(1 - \cos\beta - 2\beta/\pi)$$
 (52)

$$i_2 = I_2 \sin\beta$$
  
 $C_{on} = f_n C_o / f_F$ 

The maximum of  $v_{co}$  occurs when  $\beta_{max} = \arcsin 2/\pi$ , as found from (51). The minimum of  $v_{co}$  occurs when  $\beta_{min} = \pi - \arcsin 2/\pi$ . Introduction of these values into (52) yields:

$$v = v - v$$
(53)

$$v_{\rm orpn} = (2I_2/C_{\rm ln}) \{\cos \ {\rm arc} \ \sin \ 2/\pi + (1/\pi) \ {\rm arc} \ \sin \ (2/\pi) - 1\}$$
(54)

$$v_{orpp} \simeq .421 I_2 / C_{on} = .421 \pi i_0 / 2C_{on}$$
 (55)

$$\frac{v_{orpp}}{v_{oav}} = .661 \text{ i}_{o} / v_{oav} \text{ C}_{on}$$
(56)

or

$$C_{\text{on}} = .661 \text{ i}_{\text{o}}/\text{v}_{\text{orpp}}$$
(57)

The percentage ripple pc of the rms value  $v_{or rms}$  of the output voltage ripple is related to the peak to peak voltage  $v_{orpp}$  by

$$v_{\rm or \ rms} = v_{\rm orpp}/2\sqrt{2}$$
 (58)

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if

Introduction of (58) into (59) yields:

$$C_{\text{on}} = \frac{.661 \text{ i}_{0} 10^{2}}{2\sqrt{2} \text{ pc } \mathbf{v}_{\text{oav}}} \simeq \frac{24 \text{ i}_{0}}{\text{ pc } \mathbf{v}_{0} \text{ av}}$$
(59)

where

$$pc = 100 v v v v o rms v o av$$

For  $i_0 = 1$  and pc = 1:

$$C_{op} = 24 \cdot 10^{-4}$$
 (60)

The value of the actual output capacitor is found by application of the frequency transformation

$$C_{o} = C_{on} f_{n} / f_{F}$$
(61)

where

 $f_n =$ the normalized frequency  $1/\pi$ ;

 $\rm f_{_{\rm F}}$  = the filter frequency of 20 kHz at full power.

The output characteristic was calculated with the use of equation (61) and

$$C_{o} \simeq 24 \cdot 10^{-4} / \pi \cdot 20 \cdot 10^{3} \simeq .04 \ \mu F$$
 (62)

A capacitor value of 0.1  $\mu$ F was chosen for that purpose for reasons of practically, to yield an rms ripple of, approximately, 0.4 percent at full power operation.

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The idelized model powered from a rectified sine wave with amplitude  $I_2$  was chosen in order to attain the above carried out approximation.

The input capacitor  $C_i$  is calculated in an analogous manner, even though the charge accepted by the converter is smaller than the charge  $A_k$  which is processed by the converter within the same time interval  $T_{ok}$ . The input capacitor

$$C_{i} \simeq (10^{4}/250)^{2} C_{o} \simeq 64 \ \mu F$$
 (63)

The design of the system as a whole was, basically, oriented toward a very generous interpretation of the 2 "on" 15 "off" minute duty cycle which was stated in the general requirements (1) above.

## 3. The Power Capacitors.

The series capacitor  $C_1 = C11+C12$  processes all of the resonant current  $i_1$ . The rms value  $i_1$  rms is given by [1],[6]

$$\mathbf{i}_{1 \text{ rms}} = \rho_{\mathbf{i}} |\mathbf{i}_{1}|_{\text{av}}.$$
 (64)

The current form factor  $\rho_{1}$   $\simeq$  1.25 for full power conditions of operation [6]. The value

$$i_{1, rms} \simeq (1.25)(40) = 50 A_{rms}$$
 (65)

This rms current is equally divided between capacitors Cll and Cl2, respectively. The current in capacitor Cll is then

$$i_{1c1 \text{ rms}} = \frac{1}{2} i_{1 \text{ rms}} = 25 \text{ A}_{\text{rms}}$$
 (66)

High quality capacitors, made of extended aluminium foil and polypropylene dielectric material (Components Research, Santa Monica, CA) were used for the indicated purpose. These oil impregnated, 1500 VDC capacitors are provided with heave screw type terminals to accomodate the above referred to currents. Test of these capacitors indicated a loss factor

$$\tan \delta \simeq 2 \cdot 10^{-4} \tag{67}$$

for test conditions of a current density  $d_{is} = 50 A_{rms}/\mu F$  and a frequency of 50 kHz. The power loss  $P_{dcs}$  in the two series capacitors is approximated by

$$P_{des} \simeq (50)(660/\sqrt{2}) \ 2 \cdot 10^{-4} \simeq 4.5 \text{ Watts.}$$
 (68)

The temperature rise of these capacitors which operate at one quarter of their rating was only a few degrees Celsius. The capacitors weigh approximately 200 g per unit. The power density d<sub>es</sub> of the series capacitor

$$d_{1s} = \frac{1}{2} (1.5 \cdot 10^3)^2 \ 10^{-6} / 0.2 \simeq 5.6 \ J/kg$$
(69)

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The output filter capacitor  $C_0$  for 10 kVDC consists of four series elements, each rated in excess of 3 kV. Oil impregnated metallized film on polypropylene was used for this purpose (Component Research). These elements of the .1  $\mu$ F, 10 kVDC capacitor weighed, approximately, 50 grams before their potting into one block. The energy density of this capacitor can be described by

$$d_{eo} = \epsilon_{co} / kg = \frac{1}{2} 0.1 \cdot 10^{-6} \cdot 10^8 / 0.05 = 100 J/kg$$
 (70)

The rms current

$$i_{\rm co} \ \rm rms \simeq 2\pi f_{\rm F} \ \rm C \ v_{\rm or} \ \rm rms \tag{71}$$

or

$$i_{\rm co} \, {\rm rms} \simeq 2\pi \cdot 20 \cdot 10^3 \cdot 10^{-7} \cdot 40 \simeq 0.5 \, {\rm A}_{\rm rms}$$
 (72)

The current density d per microfarad is given by

$$d_{10} = 0.5/0.1 = 5 \text{ Ampères per }\mu\text{F}$$
 (73)

An ordinary laboratory type capacitor is being used as input filter capacitor for purpose of isolating the resonant circuit from the high frequency impedance characteristic of the source of electric energy, the storage battery and the supply lines. The used capacitor has an electric value of 100  $\mu$ F.

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An rms current i ci rms of approximately

$$i_{ci} rms \approx 1/2 i_{1} rms \approx 25 A_{rms}$$
 (74)

is accomodated by this 100 µF capacitor with a current density

$$d_{11} = 25/100 = 0,25$$
 Ampères per  $\mu F$  (75)

The preceeding presentation distinguishes clearly between the energy densities and the current densities of the series capacitor  $C_1$ , the output capacitor  $C_0$ and the input capacitor  $C_1$  respectively. Each of these capacitors has a different function at a specific impedance level, a specific frequency of operation (10 or 20 kHz) and needs to be designed and dimensioned, accordingly. The constraints which are being imposed on the design of each of these capacitors are different and will, therefore, yield different energy densities.

4. The Series Inductor.

The value for the series inductor  $L_1$  was determined in subsection 5.2. to be 80 µH. The inductor was designed for continuous operation to allow the necessary time intervals for the investigation of the experimental high voltage transformer. This inductor is, therefore, considerably bulkier than it needed to be for the specified duty cycle and, furthermore, because of a disadvantagecus input voltage The inductor was fabricated with the use of two Arnold molybdenium permalloy iron powder cores, of toroidal shape with an outside diameter of 5 inches and a net cross-section of ~ 0.8 square inches. The relative permeability  $\mu_r$ =14. Two inductors were connected in series for simplicity, each with an inductance of, approximately 40 µH and a number of N<sub>L</sub> of turns

$$N_{L} \simeq L_{1} I_{kf} / A_{c} B_{max} = 40 \cdot 10^{-6} \cdot 65 / 5.34 \cdot 10^{-4} \cdot 0.13 \simeq 38$$
(76)

Length and cross-section of the wire for both inductor halves were adjusted such that

$$R_{T ac} \simeq \frac{1.4}{58} \frac{\text{length of wire in meters}}{\text{cross-section in mm}} \simeq 20 \text{ mohms}$$
 (77)

so that each inductor winding would dissipate, approximately

$$i_{1 \text{ rms}}^{2} R_{\text{Tac}} \simeq 2500 \cdot 20 \cdot 10^{-3} \simeq 50 \text{ Watts}$$
 (78)

The factor 1.4 in equation (77) accounts for an estimated rise of resistance by 30 percent, due to the rise of the average temperature of the winding by up to 75  $^{\circ}$ C and for the ohmic losses which are caused by skin and proximity effects at the operating frequency of 10 kHz. No detailed analysis of the trade-off aspects for the design of this inductor is presented here, since the primary objective of this effort was to demonstrate the feasibility of a concept, including its reliability of operation.

5. The Thyristors.

One pair of thyristors, each with a current carrying capacity of 150  $A_{av}$ , a forward and reverse blocking voltage of 1000 VDC and an rms current tolerance of 225  $A_{rms}$  was used. These thyristors have a wafer of one inch diamter; their conduction is initiated by a center ring gate. The turn-off time is guaranteed to be less than 12 µsec. for the appropriate back bias conditions for a junction temperature of 125  $^{\circ}$ C. The rate of rise of the anode to cathode voltage after turn-off has to be limited to 1000 V/µsec. for the first 350 Volt rise and then in succession to 500 and to 300 V/µsec.

These thyristor characteristics appeared unequaled at the time of their selection for this purpose (1975). Newer thyristors with considerably improved characteristics are currently available. The described thyristors handle, easily, the  $50 \text{ A}_{rms}$  and peak voltages up to 800 VDC. The thyristors were attached to undersized cool plates, jointly with their antiparallel diodes. Individual RLC networks are being used to limit the rate of rise of anode to cathode voltage to approximately 200 V/µsec.

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6. System Construction.

The frame of the power system consists of the aluminium cool plates for the semiconductor devices. These cool plates with vertical fins are interconnected by nonconductive materials. The assembly forms a rectangular box, shown in figure 13. Two 5" fans force air vertically up through this rectangle which is "crowned" by the two described inductor halves. The power assembly weighs 10.2 kg with exclusion of the fans. Again, no serious attempt was made to optimize the components or the associated structure.

The control electronics are mounted on two boards so that all components which are mounted on printed circuits are, readily, accessible. The electronics are energized by closely regulated power supplies at 20, 15, -10 and -15 Volts. The power for that purpose is derived from a 117 VAC single phase line. All signals which emanate from the power system are conveyed by shielded coaxial cables to the control electronics to avoid the intrusion of the dreaded common mode effects into the high impedance circuits of the control electronics. A carefully engineered system of sequentially interlocking functions avoids the penetration of faulty and spurious signals, which are even being anihilated after they would penetrate into the logic system. Analog logic is used for that purpose in preference to digital logic because of a high level of rejection of disturbances. A photograph of the control electronics is shown in figure 14. The assembled converter system is illustrated in figure 15.

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Figure 14. The control electronics of the 10 kW converter.



#### SECTION VI

## RESULTS

A lead-acid battery was used as source of electric dc energy for the test of the converter. This battery consists of assemblies with individual nominal voltages of 96 VDC.

The test was carried out in, essentially, six steps. One of the above referred to battery assemblies after another was added to provide the supply voltage es in successive steps from 100 to 600 VDC for purpose of system check-out.

The output terminals of the converter were, initially, short circuited for test of the converter with the average of the absolute value  $|i_1|_{av max}$  of the resonant current  $i_1$ ; the converter was then powered from a 100 VDC source. Proper operation of all critical converter functions was verified for the above described conditions.

A resistive load of 7.3 ohm was then connected to the "low voltage" output terminals of a floating full wave diode rectifier bridge which simulated the primary winding of transformer XF, indicated in figure 8. It means that the output rectifier bridge, the output filter  $C_0$  and the load were, physically, brought into the primary circuit at the appropriate impedance level, for purpose of systems check-out and test. The high voltage transformer with rectifier bridge and filter for an output of 10 kV was to be connected subsequent to successful check-out of the inverter part of the converter system. The results of the low output voltage test are summarized in Table I. All indicated values are given in their average form. They are, therefore, designated by capital letters and thus related to the same symbols with lower case letters in the preceeding text. Distinction is made between dc output power  $P_{odc}$  and

## Table |

Es	I <sub>s</sub>	V <sub>o2</sub>	I <sub>o2</sub>	RL	Ps	Podc	Poac	100 8 dc	100 8 ac	dv/dt
VDC	ASC	VDC	ADC	OHM	WATT	WATT	WATT	%	%	v/µsec.
100	2.7	41	5.61	7.3	270	231	248	85.5	91.8	15
200	5.9	90	12.33	7.3	1180	1110	1137	94.0	96.3	25
295	9.0	137	18.76	7.3	2655	2570	2626	96.8	98.9	40
475	15.3	233	30.55	7.3	7267	6812	6904	93.7	95.1	120
560	20.1	250	42.10	5.94	11256	10525	10651	93.5	94.6	180

## TEST RESULTS OF THE 10kW CONVERTER

the ac output power  $P_{o ac}$ . An estimate of the ac output power is calculated as follows:

$$P_{o ac} \simeq P_{odc} + 3 v_{D} I_{o2}$$
(79)

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v<sub>D</sub> = the voltage drop (~ IV) in each diode of the output rectifier bridge;

A factor three (3), rather than two (2) is used for the diode bridge pair, 3  $v_p \approx 3$  V, in (79) to accomodate the switching losses at 10 kHz.

It was necessary to lower the load resistance  $R_L$  from 7.3 to 5.94 ohms when it became apparent that the six battery assemblies in series could not sustain an input voltage of 600 VDC but reduced their output voltage to 560 VDC when a load current of 20.1 Amperes was drawn. An ac output power of 10.65 kW was attained at this point with an efficiency of 34.6 percent, as calculated from the test data.

The above given test data are compared to those obtained by tests performed by the contractor in a comprehensivly equipped laboratory. A pair of calibrated wide band wattmeters with a cut-off frequency of 100 kHz and with an accuracy of 2 percent of the full scale value were used for that purpose. Tracking of the two wattmeters of the same make (Marek, Hamburg) and the same type was observed on both sides of the systems for correction of possible errors. The residual error is estimated to be less than 0.2 percent.

where

Two sets of data are given in Table II. One set of data was taken with capacitor values of .02  $\mu$ F in the dv/dt limiting network for each of the two thyristors. The maximum rate of rise was then limited to

$$(dv/dt)_{max} \approx 500 \text{ V/}\mu\text{sec. for } e_s = 520 \text{ VDC}$$
 (80)

which is 50% of the concerned stress capability of the thyristor, as stated in subsection 5.5. The power loss  $P_{dv/dt}$  in both dv/dt networks can then be arproximated by

$$P_{du/dt} \simeq 2\frac{1}{2} (520)^2 (.02 \cdot 10^{-6}) 2 \cdot 10^4 \simeq 108 \text{ Watt}$$
 (81)

# Table 2

CONVERTER'S TEST DATA WITH SIMPLE AND WITH AUGMENTED dv/dt NETWORKS

с <sub>d</sub>	Es	Is	V <sub>o2</sub>	I <sub>o2</sub>	Ps	Podc	P <sub>o ac</sub>	100 8 <sub>dc</sub>	100 8 <sub>ac</sub>	dv/dt
μF	VDC	ADC	VDC	ADC	WATT	WATT	WATT	72	%	V/usec.
0.02	520	21.72	248	43.54	11294	10798	10928	95.6	96.8	500
0.06	520	21.70	243	43.53	11284	10578	10708	93.7	94.9	160

The first set of data in Table II gives the test results which were obtained with a "light" dv/dt-network that contained a capacitor  $C_d = .02 \ \mu F$ .

The dv/dt networks were then augmented for purpose of preemting any adverse effect on the thyristor operation that could be caused by a condition of resonance between the parasitic effects of the source, the battery, the supply line and the input filter capacitor. Such a condition of resonance could cause added voltage overshots to the input filter and with it, more severe voltage stresses on the thyristors.

These augmented dv/dt-networks include capacitors  $C_d = .06 \ \mu\text{F}$ , which have three times the "normally" needed values. The added power loss  $P_{dv/dt}$  which is caused by the increase of  $C_d$  from its design value .02  $\mu\text{F}$  for the full power operation reflects itself in the data of the second line in Table II:

$$P_{dv}/_{dt} + \simeq 2\frac{1}{2} (560)^2 .04 \cdot 10^{-6} \cdot 2 \cdot 10^4 \simeq 250 \text{ Watt}$$
 (83)

The concern about possible overshots for the above described reasons appeared unfounded.

The "heavy" dv/dt-networks proved to be the most noticeable hot spot of the which was constructed for the 2-15 minute duty cycle. Even though, the syste could be operated continuously for 30 minutes without damage to it.

The capability of the system to operate for lengths of time beyond the presc duty cycle proved welcome during the prolonged tests which were associated w the development work of the high voltage transformer. This high voltage tran former with its rectifier stack was integrated with the described converter with the high voltage filter. The therewith associated voltage divider was i tegrated with the control electronics and operation of the thus integrated s established. The short circuit capability of the system without damage to it and without even blowing a fuse proved invaluable for the integration work.

## SECTION VII

#### CONCLUSIONS

1. The Demonstrated Technology

The feasibility of a highly reliable and light weight multikilowatt dc converter was demonstrated. The characteristic operation of this type of converter allows internal operating frequencies in the order of 10 kHz. This internal frequency which is attained with available components exceeds the "state of the art" of converters with these power capacities by more than an order of magnitude.

The high power frequency reduces weight and size of apperatus by approximately an order of magnitude over the state of the art with the added features of (a) voltage control capability, (b) active filtering according to the needs of source and load, and (c) performing necessary functions of stabilization.

The high degree of efficiency (up to 97% for the inverter) which is, almost, inherent in the presented type of converter adds to its reliability and reduces the need for elaborate and heavy cooling mechanisms. The high degree of realibility is emphasized by the converters capability to endure repeatedly the suddenly occuring short circuit conditions at its output terminals.

The feature of resonant type internal circuits allows the use of any fast switching elements, such as conventional or GATT [14] thyristors, transistors, spark gap triggered vacuum tubes and related devices at considerably higher frequencies than otherwise attainable.

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There is no appearent indication of an upper limit for the power level of the presented system. One of the key elements is the current carrying capability of the switching elements. The converter technology is, usually, developed around the therewith imposed limitations.

2. Switching Elements: Available and in Development.

The introduction of a high power frequency concept into the high power (MW) converter design has had a major impact on high voltage transformer technology and led to a drastic improvement of transformer power density [15].

The continued improvement of fast switching thyristor technology seems to increase the expectations in that direction where a few years ago there were only speculations based on exploratory work in its early phases. A powerful fast switching thyristor of the GATT type [14] has, recently, become available. This thyristor has forward and reverse voltage blocking capabilities of ~ 1 kV, a current switching capability of ~ 1 kA<sub>rms</sub> and a turn off time of 10 µsec. without and of 5 µsec. with assistance in the gate turn off process. These four terminal devices have a "snow flake" type gate structure; they are mounted inside a "hockey puck" frame with relativly large double side cooling areas. Further development of those devices to higher blocking voltages such as ~ 3 kV appears more subject to the expectations of a lucrative market than being impeded by serious physical or technical limitations. The 2.6 kV thyristor for 900 A<sub>rms</sub> with the inner ring gate is, presently, used in installed equipment for high

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voltage dc (HVDC) transmission lines up to 1.4 GW. The above cited fast switching transistor can be viewed as derived from the inner ring gate thyristor by application of the "snow flake" structure. This development can be, also, viewed as a first step toward the fast switching multikilowatt thyristor in the context of multimegawatt ac to dc conversion and its converse, involving higher internal frequencies [3].

It is believed that it should be possible to construct a one MW converter with the employ of six sets of presently available thyristors in full bridge configurations [8]. The number of thyristor sets would not be affected by the input voltage or by the use of one half or full bridge configurations in the converter. Yet, the apparently ongoing development of these thyristors toward a 2.6 kV blocking voltage could cut the number of needed sets from six to two for a megawatt converter.

The triggered spark gap switch appears to hold the promise to perform the switching function within its limited life span for appreciable currents and blocking voltages [16].

3. Capacitors.

The brief analysis of capacitors requirements contained in subsection 5.3. reveals the necessity to differentiate between the functions of these capacitors and the therewith associated needed indivudual characteristics. The main three functions of these capacitors which are used as input filters, as series capacitor and as output filter differ in (a) impedance level and (b) rms current carrying capacity per microfarad. The above named two conditions (a) and (b) have profound effects on the applied technology in terms of thickness of the dielectric material, current capacity of the "plates" which are implemented in the form of metallized dielectric or solid foil and the type internal and external structure of the current carrying terminals. These effects translate themselves, necessarily, into different energy densities  $d_e$  for each of the above named three functions, depending upon the applied maximum voltage  $v_c \max$ , the current density per microfarad  $d_i$  and the concerned frequency of operation.

Zero order approximations can be obtained by extrapolation of the capacitor weight for larger converters, by use of a differentiated approach as referred to above; simplification of this process by referral to indiscriminate energy densities of capacitors would yield less than that.

The series capacitor which was used for construction of the presented system has an energy density  $d_{es}$  of 5.6 J/kg, as given by equation (69). Yet, the usable part of this energy density  $d_{es max}$  as limited by the current density  $d_{is}$  of the same capacitor is 50  $A_{rms}/\mu F$  as cited with reference to equation (67). The useful energy density is calculated from

$$d_{es max} = 1/2 (v_{ci max})^2 10^{-6} / 0.2$$
(84)

in analogy to (69). The peak voltage amplitude

$$v_{cl} = \sqrt{2} i_{cs} rms max/2\pi f_i c_s$$

where

 $C_s = 1 \ \mu F$ 

 $i_{cs rms max} = 50 A_{rms}$  at 10 kHz.

The useful maximum capacitor amplitude thus becomes

$$v_{c1 max} \simeq 70 \ 10^6 / 6.28 \cdot 10^4 \simeq 1100 V$$
 (86)

The useful energy density in (84) is then given by

$$d_{es max} = 1/2 (1100)^2 10^{-6}/0.2 \simeq 3 J/kg.$$
 (87)

This relativly low energy density emphasizes the need for a departure from oversimplifications of this matter. Yet, the impact on the converter technology is not as significant as may appears on the surface. The capability of this capacitor to transfer electric power  $P_{cs}$  in a 10 kHz system is given by

$$P_{cs} \simeq 1/2 v_{c1} \frac{2}{max} C_{s} 2f_{i} \simeq 12 kW$$
 (88)

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(85)

The power density  $d_{ps}$  of this type of capacitors is thus

$$d_{ps} = P_{cs} / kg = 12/0.2 = 60 \ kW/kg$$
(89)

It means that approximately 16 kg of the currently used type of capacitor is needed for each MW of a series capacitor power converter, or approximately .035 lbs./kW.

The size of the output capacitor depends on the permissible output voltage ripple. In the case of the presented converter it was shown that for an output voltage ripple  $v_{or rms} = 0.4 \cdot 10^{-2} V_o$  it was necessary to apply an energy storage ratio

$$\varepsilon_0 / \varepsilon_s = 5/0.3 \simeq 16$$
 (90)

where

 $\varepsilon_{0} = \frac{1}{2} 0.1 \cdot 10^{-6} \cdot 10^{8} = 5$  Joules, the energy stored in the output filter capacitor  $C_{0}$ ;  $\varepsilon_{s} = \frac{1}{2} 2 \cdot 10^{-6} (550)^{2} \simeq 0.3$  Joules, the peak energy stored in the series capacitor  $C_{s} = C_{1} = 2 \mu F$ 

 $550 \simeq 70/6.28 \cdot 10^4 \cdot 2 \cdot 10^{-6} = \sqrt{2} i_1 \text{ rms} / 2\pi f_i C_1$ 

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The ratio  $\varepsilon_0/\varepsilon_s$  in (90) can be changed as a function of

$$\varepsilon_0/\varepsilon_s = 64/0.1 \ k_s \tag{91}$$

where

 $k_{\varepsilon}$  = a constant which indicates how many times the output voltage ripple can exceed the value of a 0.1 percent rms ripple.

The relative weight ratio

$$W_{T_o}/W_{T_s} = (\varepsilon_o/d_{eo})(d_{es}/\varepsilon_s) = 16(.75/100) = 0.12$$
 (92)

where

 $W_{T_o}$  = the needed weight of the output filter capacitor  $C_o$ ;  $W_{T_s}$  = the needed weight of the series capacitor  $C_1$ ;

0.75=(1/4)3 = the maximum energy density of C<sub>1</sub> for an amplitude of 550 V, thus one quart of d<sub>es max</sub> in (87).

The relative weight ratio (92) depends in each case on the chosen value of  $k_{\varepsilon}$  in (91). The numbers used in (92) are based on the materials of the constructed model which, in turn did only partially use the power capacities of the used components. The output capacitor was designed and constructed for the specific purpose for which it was used. The series capacitor  $C_1$  was used only at one quarter of its energy density  $d_{es\max}$  given by (87) and employed only part of its peak energy storage capability  $d_{es} = 5.6$  J/kg given by (69). If all of the available energy storage capability of  $C_1$  had been used, then

$$(W_T / W_T) = (5/100)(5.6/1.2) \approx 0.32$$
 (93)

It means that the weight of the output filter capacitor could become comparable to that of the series capacitor, even though the energy density ratio  $d_{eo}/d_{es}$  of the two types of capacitors is approximately 100/5.6  $\simeq$  18. The necessary derating of  $C_1$  was left out of the consideration for purpose of simplicity at this time.

A similar situation arises for the input filter capacitor  $C_i$ . The ratio (93) is (a) increased because of the lower input voltage level  $e_s$  and (b) decreased because of the, probably, less stringent input current ripple requirements.

All functional requirements will have to be known before a meaningful prediction for the weight of a large converter can be made. It is the purpose of the above argument to highlight the diversity of considerations which concern the converter design and to develop the concerned technology. 4. Magnetics.

The high frequency converter with its present base line at 10 kHz made a drastic reduction of weight and size of the power transformer possible, thus opening the road to a reliable light weight converter for power transfer, control, active filtering and dynamic stabilization.

The series inductor L<sub>1</sub> and the dv/dt coils should be given continued attention for purpose of further increase of their power density, even though the system, as described here, is feasible with application of existing materials and techniques. The above referred to attention should be, primarily, directed toward the development of new concepts for magnetic energy storage with the use of existing materials. Superconductivity should be excluded from consideration of frequencies in excess of 10 kHz. The above referred to concepts are distinguished from other more conventional, attempts to attain higher energy densities by the application of cooling methods. A study on how to reduce intrinsically the dissipated heat per Joule of stored magnetic energy should preceede a "cooling" study, which should, indeed, be used to cool an intrinsically more efficient process.

5. General Recommendations.

It appears productive for the purpose of yet higher power densities to further increase the internal frequencies of dc converters. Present semiconductor technology may allow frequencies up to 20 kHz at the MW level with use of proven circuit concepts, as the one presented here.

More advanced circuit concepts may allow the application of even higher frequencies with existing components and materials [17].

The interface requirements of the converter with its intended source and load, respectively, can add considerably to strengthen the purposeful direction of the power converter development.

The US semiconductor industry should be **exhorted** and supported in a drive for fast switching thyristors with large power capacitors to secure the capability for construction of equipment for long life operation.

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