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FINAL TECHNICAL REPORT MATHEMATICS OF GEODETIC SECOR DATA PROCESSING FTR/71-2 25 September 1964

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Corps of Engineers

Placed by

U. S. Army Engineer Geodesy, Intelligence and Mapping Research and Development Agency Fort Belvoir, Virginia

> CUBIC CORPORATION 9233 Balboa Avenue San Diego, California 92123

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FOREWORD

Cubic Corporation developed the mathematics and methods for processing Geodetic SECOR USA-2 satellite tracking data obtained during the equipment test-service test (ET/ST). The ET/ST commenced with the USA-2 satellite launch in January 1964, and continued through May 1964. This report contains the mathematics, and a general discussion of the methods employed and results obtained in processing Geodetic SECOR USA-2 satellite tracking data. The report is prepared in compliance with the requirements of Department of the Army Contract DA-49-018-ENG-2390, Modification 24, Addition II to Exhibit A, paragraph 1d.

Cubic Corporation was the prime contractor, responsible for the implementation of all contract provisions. All work was administered under the supervision of the U. S. Army Engineer Geodesy, Intelligence and Mapping Research and Development Agency (GIMRADA), Fort Belvoir, Virginia.

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SECTION I SUMMARY

1.1 Introduction. This report contains a discussion of the data processing techniques employed by Cubic Corporation in the reduction and analysis of Geodetic SECOR tracking data. The data processed was taken during the period from 15 January 1964 to 24 April 1964 using the transponder aboard the USA-2 satellite. Several ground station configurations and tracking modes were used during this period, and many of the possible types of solution were performed with the data.

In the main text, the data processing techniques themselves are discussed, together with a summary of some of the results obtained. Recommendations for further processing techniques, and for modifications to the existing techniques are included. Details concerning the design or operation of the Geodetic SECOR system are not part of this document. Refer to Cubic engineering reports for the design characteristics of SECOR equipment.

To permit familiarization of the reader with the over-all processing techniques without becoming overburdened with mathematical detail, the mathematical discussions and operational procedures have been incorporated as appendices. Supplementing the report are two copies of the program listings given in Appendix T and one copy of the computer programs on punched cards. The programs, which include many general purpose subroutines developed in conjunction with this and other projects, have been extensively tested and refined to provide both accuracy and speed. Appendix A gives the constants, units, rotations, and translations used in the text.

For additional information concerning the results of the Geodetic SECOR data processing and analysis, refer to the following Cubic Corporation reports:

Geodetic SECOR Simulation Study, Satellite USA-2, Cubic Document ES/71-2, June 1964

Geodetic SECOR Data Processing Summary, USA-2 Satellite Orbits 463-1448, Cubic Document SR/71-1

Geodetic SECOR Range Accuracy Study

Geodetic SECOR Maximum Ranging Capability Study

1.2 Purpose of the Processing. Data processing of the Geodetic SECOR data (satellite USA-2) by Cubic Corporation was designed (1) to provide a rapid check of the system operation, (2) to provide an indication of the quality of the range data, and (3) to evaluate the data processing techniques employed with data from the various modes of system operation.

1.3 <u>Modes of Operation</u>. The Geodetic SECOR system operates in either the simultaneous mode or the orbital mode. For either mode, the data obtained can be used in one or more types of solution as described in the following paragraphs.

1.3.1 <u>Simultaneous Mode</u>. In the simultaneous mode, all four trackers take simultaneous range data over the same portion of one or more satellite passes. Thus, only the portions of the satellite orbit which are line-of-sight with all four trackers can be used in simultaneous mode operation.

1.3.1.1 <u>3-3 CORDEX Solution with Simultaneous</u> <u>Mode Data.</u> In the simultaneous mode 3-3 CORDEX (COoRDinates X, the unknown station) solution, the range measurements made over two or three satellite passes by three known sites and the CORDEX site are used to determine the position of the CORDEX site. (See figure 1-1.)

1.3.1.2 <u>3-2 CORDEX Solution</u>. The 3-2 CORDEX solution is similar to the 3-3 CORDEX solution, except that the height of the CORDEX station is assumed to be known and is constrained in the solution. In this solution, the (ORDEX site may be located using only one orbital pass as shown in figure 1-2. This solution is advantageous where good geometry may not be obtained for a 3-3 CORDEX solution, or where the height of the CORDEX site has been well-established by other means.

1.3.1.3 Line Crossing Computation. The line crossing computation is used to determine the distance along a reference spheroid (i.e., the geode_ic) between the CORDEX site and one or more of the known sites. (See figure 1-3.) These line length measurements may be used in a network adjustment program to provide a check on the other CORDEX solutions, or even to furnish a solution for the CORDEX site relative to some assumed spheroid. In the line crossing solution, the three known sites are used to establish the satellite's height while the simultaneous ranges taken from the ends of the baseline provide the primary control of the line length.

1.3.2 Orbital Mode. The orbital mode differs from the simultaneous mode in that the CORDEX site measures ranges to the satellite either before or after the satellite is line-of-sight with the three known sites. The positions of the satellite corresponding to the CORDEX site range measurements are determined by orbital prediction using orbital elements determined from the simultaneous range data taken by the three known stations.

By using the orbital mode, CORDEX sites much farther from the established survey grid can be located since the requirement for simultaneous line-of-sight conditions is eliminated. The results obtained using the orbital data indicate the presence of one or more sources of error which may include base site survey, range calibration, ionospheric refraction correction bias,



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and orbital prediction techniques. It is recommended that further investigation be undertaken to identify the sources of bias, and to eliminate them through extended solutions which solve for the residual biases. Also, orbital prediction techniques utilizing longer fitting spans (or even multiple orbit fitting) should be attempted to improve the long range prediction accuracy.

Only the 3-3 CORDEX solution as described in the following paragraph was performed with the orbital mode data.

1.3.2.1 <u>3-3 CORDEX Solution with Orbital Mode</u> Data. This solution is similar to that performed with the simultaneous mode data, except that satellite positions are determined from orbital prediction instead of from direct measurement.

1.4 Data Processing Facilities. Data processing was accomplished at the computer center of the University of California at San Diego (UCSD) on a Control Data 1604 computer system. The CDC 1604 computer has a core memory of 32,000 48-bit words, and an average cycle time of 4 μ sec. The peripheral equipment includes a 160A satellite computer, twenty magnetic tape units, a card reader and punch, and a 1000-line-per-minute printer. In addition, off-line key punches, a card lister, duplicator, and interpreter are available for those using the computer.

The data processing programs were written in FORTRAN 63 and in CODAP assembly language. Operational descriptions of these programs are included as Appendix T, and sample listings constitute Appendix S of this report.

SECTION II COMPUTATIONAL PROCEDURE

2.1 Introduction. Most of the data processing programs were written prior to the launching of satellite USA-2. Since the data in this report were obtained in the first truly operational test of the system, the various processing steps were set up to run on separate computer passes to allow inspection of the intermediate results before further processing steps were attempted. The results obtained during each computer pass were listed and recorded on magnetic tape for use in the subsequent processing steps. Figure 2-1 is the over-all data processing flow diagram. Each box in the diagram indicates a computer pass, and the arrows (unless otherwise indicated) designate the magnetic tape reels used. The tape reels, except for the original raw tapes, were identified with a letter, orbit number, and station number for processing purposes. For example, R 132.1 is the raw tape from orbit 132, station 1. The letter designations of the various tapes are in parentheses next to the arrows.

In the following paragraphs, the processing steps accomplished during each computer pass (as shown in figure 2-1) are discussed.

2.2 <u>Copy Raw Tapes</u>. The magnetic tapes recorded at each tracking site were forwarded to Cubic Corporation through the GIMRADA representative. The tapes were copied and the originals were returned to the GIMRADA representative for shipment to Army Map Service (AMS). Because the endof-record gap on the original raw tapes was not sufficiently long for use by the CDC 1604 c. nputer, copying the tapes could not be accomplished directly on the computer. The original tapes had an end-of-record gap of only 5/8inch, whereas the 1604 computer system tape units stop at the end of each physical record and require a 3/4-inch end-of-record gap. Therefore, the 'apes were copied on the CDC 160A satellite computer with a CDC 163-2 tape unit which reads continuously and requires a shorter inter-record gap. The tapes output by this program (R tapes) were compatible with the 1604 tape units, and were used for the subsequent processing steps.

Some delay in processing time was experienced as a result of this procedure because the 150A computer is not generally available for us 2 except as an integral part of the 1604 computer system. The time which would be saved in processing would probably justify an investigation into a tape format change to make the magnetic tapes compatible with standard tape units.

2.3 <u>Raw Data Listing</u>. Each raw tape was listed as a preliminary check of data quality and as a means of locating regions of usable data. The listing (program EXAMI) involved unpacking the raw tape data format (subroutine FORMAT), and converting it into a more convenient format; resolving the ranges (subroutine RESOLVE); and listing this information. Copies of the raw data listing were forwarded to the GIMRADA representative.



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Figure 2-1. Data Processing Flow Diagram

The method used to resolve the ranges is discussed in Appendix B, and the sample raw data listings (as previously noted) appear in Appendix S.

The raw data listings were made available within 24 hours of the receipt of the original raw tapes by Cubic Corporation. This turn-around time was continued throughout most of the data processing, and provided valuable assistance both to the GIMRADA representatives and to the Cubic field engineers.

2.4 Data Editing and Smoothing. During the data editing and smoothing pass (program PASS2), the raw tape from each tracking site was read, and the following operations performed:

(1) calibration constants were applied to the raw range and to the measured ionospheric correction (IC),

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(2) the raw ranges (plus calibration) were edited for ambiguities and spurious bad samples,

(3) the edited ranges were smoothed using a least squares moving span filter,

(4) the range rate and range acceleration were determined as a byproduct of the range-smoothing process,

(5) the smoothing residuals (differences between the smoothed and edited ranges) were calculated and used to determine a standard deviation (rms error) for each block of 132 samples.

The information from step (5) was used in the subsequent data evaluation. The editing and smoothing data were generally available within two days of the receipt of the original raw tapes.

2.4.1 <u>Calibration Constants</u>. The calibration constants to be applied to the data were calculated for each orbit in the field and forwarded to Cubic Corporation through the GIMRADA representative. These calibration constants included one for the very fine (VF) channel and one for the very fine ionospheric correction (VFIC) channel. These constants were input on cards during the data editing and smoothing pass (program PASS2).

The final calibration constants represented an estimate of the phase shift within the station-satellite loop other than that phase shift attributable to the range. In practice, these phase shifts were measured in four steps:

(1) Each station measured the range to a test transponder (TT) over a known distance (cable phase shifts included) and noted the offset $(\varphi_{\text{STA}} + \varphi_{\text{TT}})$.

(2) The test transponder of the station was compared with the transponder calibration unit (TCU) and the difference was noted ($c_{TT} + \phi_{TCU}$).

(3) The transponder calibration unit was compared with the satellite transponder ($\varphi_{TCU} + \varphi_{SAT}$).

(4) The phase delay from the satellite antenna to the satellite transponder was measured ($\omega_{SAT ANT}$).

The final calibration constant was found from:

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 $c_{CALIB} = (c_{STA} + c_{TT}) - (c_{TT} + c_{TCU}) + (c_{TCU} + \phi_{SAT}) + \phi_{SAT}$ ANT

2.4.2 Data Editing. The data editing process removed ambiguous and spurious bad samples from the raw range data. The editing was accomplished by comparing each first difference with a first difference predicted from previously edited ranges. Where the agreement was within the noise tolerance (25 meters), the corresponding range was passed unchanged. If the agreement was within the noise tolerance of an integral number of 256meter ambiguities, the total ambiguity was removed from the output range. Where neither of these conditions existed, the sample was considered to be a spurious bad sample, and it was replaced by an extrapolated range value. Since extrapolation depends on the use of 'good' samples, only five successive bad samples were allowed before a search for a new starting span was initiated.

The process of editing based on first differences requires that the editing process begin in a region of nonambiguous data. In order to find such a region, the average second difference of a span of five samples (the starting span) was computed and compared with a predetermined maximum value (10 meters/ $(0.1 \text{ sec})^2$). If the maximum value were not exceeded, editing commenced; if the maximum value were exceeded, the next five samples were examined. A detailed description of this data editing technique, together with a flow diagram of the process, is included as Appendix C.

The edited Geodetic SECOR range data exhibited two types of ambiguity, sporadic and consistent. The sporadic ambiguous samples occurring in 3 to 5 per cent of the ranges posed no problem, and they were completely eliminated from the data. The consistent ambiguities caused a constant offset of the data for an extended interval. These ambiguities sometimes resulted in an offset of the entire span of edited range data if the editing procedure started in an ambiguous span of data. These ambiguities were generally in the extended range (524, 288 meters) and resulted in an offset which was readily recognized from an approximate knowledge of the orbit, or by examining the permuted satellite positions. When such an offset occurred, it was removed during the satellite position calculation by applying the offset as a calibration constant. An example of the edited range data is shown in figure 2-2. In this data sample, the editing process was started in a region of consistently ambiguous data, resulting in an offset of +524, 288 meters in the edited ranges. The presence of the offset is obvious from the predicted range data supplied by the NASA Goddard Space Flight Center, and it was removed as a calibration offset in subsequent processing steps. The figure also illustrates one spurious ambiguity in the fifth sample; this was removed during the editing process.

2.4.3 <u>Data Smoothing</u>. The edited range data were smoothed to reduce the random noise content of the data. As a byproduct of the smoothing process, the range rate and the range acceleration were also determined. The smoothing filter used was a twenty-five, second degree, midpoint filter. This filter effectively fits a second degree polynomial to a span of twenty-five ranges, and from this polynomial a smoothed thirteenth range is calculated. By successively shifting the range data and repeating the process, a series of smoothed ranges were determined. The range rate and the range acceleration were then determined using the time derivative of the polynomial. This type of filter is discussed in more detail in Appendix D where plots indicate the theoretical noise reduction and frequency response.

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The differences between the edited and smoothed ranges (the smoothing residua s) were calculated and output as an indication of the data quality. A plot of a typical set of residuals is shown in figure 2-3. The horizontal dashed line in this figure indicates the probable error of a single observation based on these smoothing residuals (0.26 meter).

A more comprehensive understanding of the noise removed by the smoothing process may be gained by examining the frequency distribution of the smoothing residuals. A typical spectral density plot of the residuals is shown in figure 2-4. This plot is normalized in such a way that the area under the curve is equal to the sample variance of the residuals. The tapering off of the curve at low frequencies must be attributed to a combination of the spectral characteristics of the noise and the filter response.

2.5 <u>Satellite Position</u>. The satellite position program (program PASS3) time-synched either three or four ES tapes (edited and smoothed data tapes), and produced an output tape consisting of the station data plus the computed satellite position. During this computer pass the ranges were corrected for constant offsets, tropospheric refraction, ionospheric refraction, and transit time. These corrected ranges along with the range rates were then used to compute the final position of the satellite. In addition, when simultaneous mode data were used, an internal range consistency check was computed.

2.5.1 <u>Calculation of Satellite Position and Velocity</u>. The calculation of satellite position and velocity was performed twice. The first solution was performed with the smoothed ranges from the ES tapes plus the correction for constant offsets. This initial solution was used to calculate





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Figure 2-3. Range Smoothing Residuals

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the range, elevation angle, and the range rate of the satellite as observed at each tracking site. These parameters were then used (as described in the next paragraph) to compute the various range corrections. From the corrected ranges, the final satellite position was computed.

The mathematics for the calculation of satellite position using the simultaneous ranges measured at the three known stations is derived in Appendix E. This solution may be geometrically interpreted as the intersection of the three spheres, with the radii defined by the three ranges and centered at the three tracking sites.

The satellite velocity was determined using the simultaneous ranges and range rates from the three known sites and the set of linear equations derived in Appendix F.

2.5.2 Range Corrections.

2.5.2.1 Correction for Constant Range Offset. Since the data editing, at times, produced ranges which were offset by a constant ambiguity, provision was made to apply a calibration constant to each range during the satellite position calculation. The set of range corrections (if any) was input on cards by the PASS3 program and applied to the input ranges before any computations were made.

2.5.2.2 <u>Tropospheric Refraction Correction</u>. The tropospheric refraction range correction was made using the analytic model (subroutine REF) discussed in Appendix G. The correction was computed using the range and elevation angle at each site determined from the initial satellite position computation as the model parameters.

2.5.2.3 <u>Ionospheric Refraction Correction</u>. The ionospheric correction was made using the analytic model for the ionospheric correction (subroutine IONCR) described in Appendix H except for one orbit (1365) where the measured IC was directly applied to the data. (Refer to Appendix I.) The use of the analytic model was adopted because of the relatively high noise content of the measured IC compared to the measured very fine channel, and the consistent loss of IC lock at the Austin site.

In addition to the range and elevation angle, the analytic model for the ionospheric correction used the maximum electron density of the F2 layer and a slope constant, K2. These parameters were determined by a least squares adjustment to the measured IC values from all sites (program IONITR). Figure 2-5 shows the distribution of the maximum electron density plotted as a function of local time. These results indicate a probable residual error of about 20 per cent of the total ionospheric correction, which normally represents about five meters range error.

2.5.2.4 <u>Transit Time Correction</u>. The transit time correction (Appendix J) was applied to the ranges (program PASS3) to

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establish a consistent time base for the observations. This correction was applied to all range data used for satellite position determination, although it is only required when orbital prediction is to be employed.

2.5.3 Internal Consistency. When simultaneous mode data was used in the satellite position program, an internal consistency check was made by performing four different satellite position calculations with the four sets of three ranges. Comparing these four solutions with the average solution provided a measure of the consistency of the range measurements. The results of this internal comparison showed agreement in satellite position within a few meters in regions of good geometry.

2.6 Determination of Orbital Elements. The various solutions using orbital mode data required the determination of the position of the satellite corresponding to the time at which the range measurements were taken at the CORDEX site. This determination of satellite position depended on orbital prediction techniques based upon simultaneous range measurements made by the three known stations. From range data taken by the known stations, a set of orbital elements were derived for the orbital prediction program.

2.6.1 <u>Punch Cards</u>. For convenience, the equatorial satellite coordinates of position and velocity determined from measured data were punched onto cards (program SPUNCH) from the satellite position (SP) tape. The cards were then used in the orbital fit program discussed in the following paragraph.

2.6.2 Orbital Elements by Least Squares Trajectory Fit. The orbital prediction techniques employ the particular set of orbital elements known as injection vectors. These are the equatorial position and velocity of the satellite at a certain time (injection time). The choice of injection time usually corresponded to the first time for which satellite position was calculated. Thus, the measured satellite position and velocity at the injection time yielded a first estimate for the injection vectors. The orbit fitting technique is discussed in Appendix K, and a general discussion of the least squares adjustment techniques is included (for information) in Appendix L.

Orbit fitting (program PCMPTJ) consisted of adjusting the components of the injection vectors so that the differences between the measured and predicted equatorial position and velocity were minimum (in the least squares sense). The method of obtaining the predicted coordinates is discussed in a later paragraph. The results of a typical orbital fit are illustrated in figure 2-6 where the equatorial position residuals (differences between measured and predicted values) are plotted for the samples used in the fitting span.

Similar orbital fitting techniques were attempted, fitting only to the satellite position, and directly to the difference between predicted and measured ranges. (See figure 2-7.) However, all of these techniques produced similar results.



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5 180 **ORBIT 532** Ż 160 5 140 Figure 2-7. Urbit Fitting Residuals, Range Fit TIME FROM INJECTION (SECONDS) ٤ 120 100 چ ک 80 Ş 90 40 20 205 10 0 -10 -20 -200 20 -10 -20 20 10 o 10 -10 0 RESIDUALS (FEET)

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2.7 <u>Satellite Position by Orbital Prediction</u>. During the orbital prediction pass (program GSORB) the injection vectors determined from the trajectory fitting were used to predict the satellite position for each data sample read from the CORDEX site ES tape. These data were then packed on a predicted satellite position (PSP) output tape which was similar in format to the SP tapes, and was compatible with the various CORDEX solution programs.

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The actual prediction of satellite position was performed by numerically integrating the total force field, or by numerically integrating only the perturbation accelerations and adjusting a two-body reference orbit. (Refer to Appendix M.) Both these techniques are described in detail in Appendix N, and the two-body prediction techniques are described in Appendix O. The perturbations mentioned refer to forces other than the two-body central force field, and include the second through the ninth zonal harmonics of the earth's gravity, atmospheric drag, and lift. The last two perturbations are discussed in Appendix P, although, as expected, the effect was found to be negligible for the prediction intervals and vehicle altitudes involved.

The primary perturbation arises from the higher order terms of the gravitational force field. The gravitational perturbation was calculated using the first nine zonal harmonics as described in Appendix Q (subroutine GRAVITY).

The satellite position and velocity predicted were used to form a predicted range and range rate which could then be compared with the measured values. Figure 2-8 shows the comparisons over about three minutes of track for orbit 504.

2.8 <u>CORDEX Solutions</u>. The solution for the position of the CORDEX site is the primary function of the Geodetic SECOR system. In processing the data two types of solution (3-3 and 3-2 CORDEX solutions) were performed. Although each of these solutions may be performed with either simultaneous mode or orbital mode data, only the 3-3 CORDEX solution was actually attempted with orbital mode data.

The initial computation is the same for either solution. That is, the position of the satellite must be found at points along the orbit at which ranges to the CORDEX site are available. For the simultaneous mode data, all this information was available on the SP tapes. In the orbital mode, the satellite positions were found by orbital prediction, and were recorded along with the corresponding CORDEX site ranges on the PSP tapes.

In processing both the CORDEX solutions, discrete solutions were computed by choosing three (or two) spans of data and performing the solution with successive triads (or pairs) of data points. The resulting solutions were compared with the mean solution, and with the surveyed position of the CORDEX site in order to estimate the quality and consistency of the solutions.



TIME (MINUTES)

ORBIT 504 - GRAND FORKS

INJECTION TIME FIRST COMPARISON 00:44:32



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2.8.1 <u>3-3 CORDEX Solution</u>. In the 3-3 CORDEX solution (program PASS4) the position of the CORDEX site was determined by trilaterating to the CORDEX site from three satellite positions using the corresponding ranges to the CORDEX site. The mathematics of this solution is identical with that used to solve for the satellite position except that the three satellite positions form the reference sites and the CORDEX site position is solved for. (Refer to Appendix F.)

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Figure 1-1 shows the geometrical arrangement for the simultaneous mode 3-3 CORDEX solution where two orbital passes are used. An example of the results of the 3-3 CORDEX solution is illustrated in figure 2-9. In this figure, the difference between the CORDEX site latitude and longitude determined from range measurements and the survey values are plotted on the left. Each point of this plot represents a solution determined using a different triad of satellite locations. The approximate geometry for the solutions is illustrated at the right. The geometry for this set of solutions was good; hence, the distribution of solutions is quite symmetrical. Less favorable geometry tends to distribute the random errors within an elliptical region.

2.8.2 <u>3-2 CORDEX Solution</u>. The 3-2 CORDEX solution (program PASS432) is similar to the 3-3 CORDEX solution except that the height of the CORDEX site is assumed to be known; thus, the height replaces one range measurement. The trilateration to the CORDEX site requires two satellite positions plus the height of the CORDEX site. The mathematics of the two-range-and-altitude solution is derived in Appendix F, and the geometrical configuration using one satellite pass is shown in figure 1-2.

2.9 Line Crossing Solution. The line crossing mode illustrated in figure 1-3 consists of determining an estimate of the geodesic (shortest distance along the spheroid) between two of the tracking sites. In operation, four sites tracked the satellite simultaneously as it crossed the baseline. From the range data taken by three of the sites, the satellite's distance from the center of the earth was determined. One of these three sites and the fourth site formed the ends of the baseline. The mathematical details of the line crossing technique are contained in Appendix R.



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Figure 2-9. 3-3 CORDEX Solution Error (Larson AFB)

SECTION III SUMMARY OF RESULT.

3.1 Introduction. The method of computing the unknown site solutions for the Geodetic SECOR USA-2 satellite data processing did not weigh solutions or discriminate between them on the basis of optimum geometries. Because geometry bears a dramatic relation to accuracy, theoretical error propagations were processed which corresponded to the actual geometries used in the data reduction. A comparison of the theoretical accuracies and the observed results, therefore, provides a means of normalizing solutions. In many solutions, disagreement can be anticipated if poor results are predicted in the error propagation.

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It is important to remember that the theoretical error propagation is based on a statistical model, implying a large sample space. Actual solutions, on the other hand, are discrete cases or represent an average over a relatively small number of discrete cases. Observed solutions should approach the theoretical predictions in characteristics and in magnitude over many solutions, provided the theoretical error model is valid. The theoretical error propagation does not take into account that the standard (in this experiment, the assumed position of the unknown site) might be incorrect. The difference between the computed and surveyed site coordinates, therefore, includes some constant error because of the uncertainty in the assumed standard.

The assumed error models used in the theoretical error analysis are listed in table 3-1.

Model Number	σ System (feet)	g Tropo (per cent)	σ Scale (ppm)	σ Survey (ppm)	g Iono (per cent)	σ Site Height (feet)
CORDEX 1	9	5.	1	4	5	0
CORDEX 2	J 5	5	_ 1	4	5	0
CORDEX 3	15	5	1	10	5	0
Line Crossing	9	5	1	15	5	15

TABLE 3-1 ASSUMED ERROR MODELS

3.2 <u>Small Quad 3-3 CORDEX Solutions</u>. The base stations used in the small quad were Stillwater, Oklahoma; Las Cruces, New Mexico; Austin, Texas; and Fort Carson, Colorado (the unknown site). Table 3-2 includes the major portion of the CORDEX solutions processed on the early USA-2

TABLE 3-2

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GEODETIC SECOR USA-2 SATELLITE 3-3 CORDEX SOLUTIONS

		E	DRT CA	RSON S.	LTE SOLI	ITIONS	(3-:	2. SIMU	TANEOUS	(HODE)	Ś	ALL QUAD		
, •0] •1n[Orbits Used	10 VID	, ,	SECOR-	SURVEY		STA	NDARD D	EVIATIC	SNC			COMPARISONS	
N 05¦	for Solution *	oli			HOTAH	252 E	EATI E	LONG	HEIGHT	RSS B		TUTAL RS3 m	THEORETICAL	THEORETICAL
TT	132.173.173	46	1.1	-2.6	3.2	4.3	6.7	15.1	4.2	15.3		15.9	2 22	
5A	242.1.175.2.270.2	86	3.3	9.7	14.6	17.8;	2.2	3.5	1.8	4.5.		18.4	13.5	0.00 18 0
- 6A	270.1,132,173.2	27	-8.9	8.8	6.3	14.0	4.4	1.8	2.6	5.4		15.0	11.5	15.1
TA	152,270.1,173.1	74	-7.8	11.4	6.0	15.1	3.3	1.8	2.6	4.6		15.8	11.7	15.5
8A	152,173.1,187.2	72	4.1	-11.4	0.3	12.1	4.4	5.3	1.5	7.0		14.Ó	14.6	19.5
- 9A	234,173.2,270.2	87	3.3	9.7	14.8	18.0	4.4	3.5	2.6	6.2		19.0	21.1	28.3
TOA	187.1,173.2,270.2	3	12.3	8.8	18.4	23.8	1.1	3.5	1.5	3.9		24.1	15.1	20.7
TIA	132,270.1,242.2	56	-7.8	14.0	5.0	16.8	3.3	1.8	.2.1	4.3		17.3	1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1	15 5
13A	132,201,242.2	56	-5.6	11.4	4.4	13.4	2.2	1.8	2.4	5.7		13.9	. 2.11	15.7
144	201.132.173.2	74	-6.7	7.0	5.7	11.2	5.3	3.5	2.8	5 . ĉ		12.5	11.6	15.3
154	132.201.175.1	74	-6.7	8.8	5.6	12.4	5.3	1.8	2.9	4.7		· 15.3	12.0	15.7
16A	187.5.220.201	102	1.1	24.5	0.7	24.5	5.6	4.4	3.8	8.1		25.8	17.8	23.9
17	132,187,2,173.2	74	4.4	-4.4	1.3	6.4	4.4	4.4	1.7	.6 . 5		9.1	12.6	16. B
18	220.152.187.1	74	4.4	21.0	3.5	21.7	2.2	4.4	2.9	5:7		22.4	12.8	16.7
19	187.1.463.2.173.1	93	-1.1	-9.7	-3.9	10.5	1.1	.3.5	1.4	3.9		11.2	17.8	23.7
		Τ					•		•	ŕ				
	HEAN		70	7.1	5.7	14. 8	53 51	3.9	2.4	6.0		16.5	14.5	19.4
3 2	STANDARD DEVLATIONS		6.0	10.1	4.8			}				•	•	

satellite orbits. SECOR - SURVEY differences are the result of taking an average of a sequence of actual Geodetic SECOR solutions and subtracting the U. S. Coast and Geodetic Survey geodetic site coordinates from this average solution. The standard deviations shown per solution are computed from the residuals, where the residuals are the differences between each SECOR -SURV "Y offset, and the average of the offsets for one particular solution. RSS refers to root sum square, and indicates the composite bias and noise error. The RSS is computed by squaring the mean offsets and the standard deviations, adding, and taking the square root.

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where $\sigma^2 = \frac{\sum_{i=1}^{n} (\Delta - \overline{\Delta})_i^2}{\sum_{i=1}^{n-1} = \text{sample variance}}$

 $\Delta = SECOR - SURVEY = residual$

 $\overline{\Delta}$ = average residual

 $RSS = (\Sigma\Delta^2 + \Sigma\sigma^2)^{1/2}$

n = number of individual solutions

SEP =
$$\sqrt{\frac{\sigma_c^2 + \sigma_\lambda^2 + \sigma_h^2 + \Delta_{\varphi}^2 + \Delta_{\chi}^2 + \Delta_h^2}{3}}$$

with Δ_{c} , Δ_{λ} , Δ_{h} , σ_{c} , σ_{λ} , σ_{h} expressed in meters.

Note that in table 3-2 the over-all observed results fall between the theoretical error propagations given by error models 1 and 2. The controlling terms in these models were the system and survey errors. In both cases, a base site survey with an accuracy of 4 ppm was assumed. A ranging accuracy of approximately 3 and 5 meters was used in models 1 and 2, respectively. This indicates (nonconclusively) that over-all accuracy (ranging, correcting, processing, etc.) was approximately ±4 maters, and site survey was approximately 4 ppm for this quad.

Several solutions which were processed for the small quad are not included in this summary. Deleted solutions were adjudged nonrepresentative either because of geometry, or because of peculiarities in the data. Refer to the tabulations and listings for detailed information concerning the solutions.

Large Quad 3-3 CORDEX Solutions. In the large quad 3-3 3.3 simultaneous mode CORDEX solutions, the base stations were located at San Diego, Austin, Grand Forks, and in some cases, Fort Carson. Larson

Air Force Base in the state of Washington was the unknown station. Results tabulated are in the same format as those presented and explained for the small quad operation.

From table 3-3 it is apparent that solutions are not quite as accurate for the large quad operation. The error propagation, however, predicts reduced accuracy for the geometries used. It had been anticipated and proven by the error propagations that the large quad would give the opportunity for improved geometries and, consequently, improve solutions over those encountered in the small quad. In the actual operation, intervals of simultaneous track and the selection of orbits limited the geometries that could be used to obtain comparison data.

Considering the large quad results with respect to the theoretical error propagation, improved results were obtained over those experienced on the small quad. As a test criterion, if the total RSS observed is divided by the theoretical RSS means (using error model one), then from tables 3-2 and 3-3,

Small Quad Ratio = $\frac{\text{Observed}}{\text{Theoretical}} = \frac{16.5}{14.5} = 1.14$

Large Quad Ratio = $\frac{\text{Observed}}{\text{Theoretical}} = \frac{34.0}{75.7} = 0.45$

3.4 Orbital Mode 3-3 CORDEX Solutions. Table 3-4 includes the results of the orbital mode 3-3 CORDEX solutions. Sites in the small quad were used to determine the satellite position and velocity to which injection vectors were computed by an iterative least squares technique. Satellite positions were then predicted forward to times synchronous with ranging observation times at the Grand Forks station. With the predicted satellite positions and the measured ranges, the position of Grand Forks was computed. Error propagations of the Grand Forks CORDEX solution in the orbital mode were not processed. Solution results, therefore, have to be qualified subjectively.

It appears that the reduced accuracy in the orbital mode has three primary sources:

- (1) relatively small orbit fitting spans,
- (2) system and base site survey bias errors,
- (3) internal timing.

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Small fitting spans allow any error in the data to upset the vector fitting and give less accuracy in the injection vector determination. The forward prediction will then deteriorate rapidly. Timing error arises from the use of independent local time sources. A time offset will mean that the predicted

CEODETIC SECOR USA-2 SATELLITE 7-5 CORDEX SOLUTIONS (S'MULTANEOUS MODE)

DE) LARGE QUAD	
(3-3 SIMULTANEOUS NOI	STANDARD DEVIATIONS
N AFB SITE SOLUTIONS	SECOR-SURVEY
LARSO	•ndr •AŢĮ JO

•¢ •‡r	Orbits Used	•nc •^1 Jo		SECOR-	SURVEY		STANI	ARD DE	VIATION	ŝ		U	OMPARI SONS	
NN .	for Solution	ino.) Ind Vo	LATI m	LONG	HEIGHT	RSS	LATT	LONG	HEIGHT	RSS	<i>е</i> ж ——)TAL 33 m	THEORETICAL (1) RSS m	THEORETICAL (2) RSS m
,	1305,1519,1167	33	-15.6	-19.1	-36.4	44.0	2.2	3.8	5.0	6.7	4	5.1	1.19	101.5
ଝ	1305,1333,1167	55	11.1	14.5	14.9	23.6	2.2	2.3	2.8	4.2	57	0	61.0	68.3
3	1305,1305L,1319L	86	-15.6	8.1	0.5	18.1	3.3	2.3	3.5	5.2	16	3.8	83.6	94.5
#	1305,1319L,1291L	81	-14.5	3.8	-2.2	15.2	3.3	3.0	2.4	5.1	1(3.0	64.8	73.5
S	1167L,1291L,1319L	8	-20.0	5.3	-5.7	21.5	4.4	2.3	4.0	6.4	22	. 4.	64.3	1.57
9	12911,1167, 1319	ß	-5.6	-9.1	-16.4	19.6	3.3	2.3	6.1	-7.3.	ي ج	6.	95.0	1.801
t	1269,1269M,1291L	81	3.3	14.5	40.0	42.7	4.4	3.0	3.8	6.5	43	.2	84.7	96.4
80	1269W,1269,1305L	16	1.11	38.1	45.2	60.1	2.2	3.8	4.8	6.5	60	1.5	84.0	93.8
: თ	1269,1291L,1167L	81	-22.2	22.9	28.1	42.5	4.4	1.5	3.9	6.1	45	6.0	59.0	67.0
10	1269.1291L.1305L	81	31.1	25.9	23.7	46.9	3.3	2.3	3.4	5.3	45	2	69.0	79.5
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	•		-										•	
	•		14.4	10.6	9.2	33.4	3.3	2.7	4.0	6.0	. 34	0	75.7	85.6
	STANDARD DEV LATION		8.9	15.7	24.3	•								

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			(EU0,	~											:		•										•
•			•	•		•	TOTA	RSS	74.2	1.99.1	118.5	70.4	117.3	46.9	29.0	48.4	74.1	98.2	35.6	74.7	23.4	36.7	98.7	144.1	182.6	80.7	
•			• • • •			·	· SN	RSS	4.3	6.2	6.3	4.9	20.6	16.7	16.0	10.2	28.7	32.4	15.4	9.5	11.9	6.2	38.0	81.8	40.9	20.6	
			hui u n				EVIATIO	HEIGHT	1.7	1.0	1.1	0.5	7.3	2.0	3.7	2.0	5.2	5,5	2.1	3.8	5.2	2.3	17.9	38. 8	22.2	7.1	
		म्		•.	•	ODE)	DARD DI	TIONG	2.2	5.2	5.2	2.2	12.7	16.4	14.9	4.5	18.7	29.8	14.2	6.7.	6.0	3.7	26.9	50.7	34.3	15.0	·
	i	TABI				BITAL M	STAN	LATI	3.3	3.3	3.5	4.4	14.5	2.2	4.4	8°9	21.1	12.2	5.6	5.6	8.9	4.4	20.0	51.2	2,2	io.3	
	·			•	- , , - , ,	3-3 OR		r RSS	74.1	98.9	p18.3	70.2	p15. 5	43.8	24.2	47.3	68.3	92.7	52.1	74.1	20.1	36.2	91.1	118.6	178.0	76.7	
			•				URVEY	HEICH	-3.8	-60.4	-15.0	-18.3	-15.8	9.2	0. 6	-38.9	-24.4	-21.0	-10.9	3,8	. 0.3	-12.0	-17.1	-30.5	-67.4	-17.1	.17.5
							SECOR-S	I LORG	-9-1	7 36.6	-11.2	29.1	-111-	20.2	-20.9	8.2	-36.6	-89.5	-21.6	73.9	-12.7	-29.1	5°. 50	79.8	152.9	7.2	61.4
•			T. CRO				inc	TAT TAT	-73.	-86	'917-	-61	-42-	37.	12.	-25.	-52	-12.	21.]	÷	15.6	17.8	-62.3	-82.3	-61.2	-32.5	44.1
					•	SNOL	-A1 J0	.oV bal	3	ž	3	54	142	22	185	139	139	132	132	167	195	132	167	167	142	•	
	¢	ĸ	•			ND FORKS SITE SOLUT	Orbits Used	For Solution	465,465,477	477,477,532	377,477,463	532,532,477	463.1,463.2,477.2	620.1,463.1,463.2	725,463.1,465.2	725,477.1,477.2	532.2,477.1,477.2	552.1,532.2,477.2	532.1,532.2,477.1	620.2,727,463.2	504,463.1,463.2	504,532.1,552.2	504, 620. 2, 463. 2	504,620.2,532.2	620. 2, 727 , 477 . 2	HEAN	STANDARD DEVIATION
						GRA	.tu1	os N	1-0	9-2 %	3-0	4-0	5-0.	9-C	2-0	8-0	0-6	10-0	0-11	12-0	13-0	14-0	15-0	16-0	17-0		3-3

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satellite positions and the measured ranges are not synchronous. Time synchronization is not encountered while the Geodetic SECOR equipment is used in the simultaneous mode. System and survey bias will give a slight misorientation of the injection vectors and therefore will affect the forward predictions.

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The experience and extensive testing undertaken in the data reduction and computer program development has indicated that the orbit fitting and prediction techniques are extremely accurate. Over the intervals of prediction and fitting used in this reduction, it was demonstrated that the analytic methods did not contribute significant error in the solutions. It is thought that the two error sources of fitting span, and system and site survey bias error effects can both be overcome if multiple orbits are used in the fitting procedures. The lever arm inherent in the long predictions will allow recognition or compensation for any initial misalignment of the injection conditions. Of course, care will have to be exercised to assure that the analytic model and techniques of prediction and fitting do not then become major error sources.

3.5 Satellite Line Crossings. Table 3-5 is a summary of the line crossing solutions and comparisons computed from the USA-2 satellite data. The results of the line crossing mode are commensurate with the theoretical results with two exceptions. All lines measured to the Herndon, Virginia site are long. The correlation of these results over all lines indicates that the Herndon site is, in all likelihood, mislocated. The rms errors shown in table 3-5 are misleading because they are computed from the differences between an analytic curve fit to the geodetic distance sums and the observation computed sums. A parabolic form is assumed in the curve fit. The geodetic distance sum however is not parabolic due to the earth's rotation. Even though the rms error is quite high in some lines, the fit is representative at the crossing. A direct comparison between the computed minimum crossing from the analytic fit and the measured data shows that the solution is accurate (to within one meter in all cases processed).

The strength of the line crossing solution in this experiment is the result of accurate ranging and the accurate determination of the satellite's distance from the earth's center. Use of a ground station to track the satellite during the crossing allows this high accuracy. The line crossings processed here represent the longest lines ever processed and clearly demonstrate the strength of the technique.

3.6 Large Quad 3-2 CORDEX Solution. In the large quad 3-2 simultaneous mode CORDEX solution, the base stations were located at San Diego, Austin, and Grand Forks. The Herndon site was chosen as the CORDEX site with its survey height assumed correct. The 3-2 CORDEX solution was then run using different orbits and geometries to see if any survey bias could be detected. The possibility of such a bias was suggested by the line crossing results. The results of the five solutions attempted are given in table 3-6. Because of the relatively short baseline obtained, the polutions show inconclusive results in latitude. That is, the standard deviation of the various latitude determinations from the mean exceeds the average latitude offset. The longitude, however, shows a rather consistent bias.

3-7

TABLE ----GEODETIC SECOR USA-2 SATELLITE LINE CROSSING SOLUTIONS

	LINE CROSSING RESULTS *								
ORBIT	STATIONS	SECOR	SURVEY	SECOR-SURVEY	RMS NOISE m	OBSERVED RSS m	THEORETICAL (1) RSS m		
463	Austin Ft. Carson	1,137,573.2	1,137,559.8	13.4	5.6	14.5	2 5. 8		
532	Austin Ft. Carson	1,137,573.0	1,137,559.8	13.2	65.0	66.3	25.8		
648	Austin San Diego	1,860,074.3	1,860,051.9	22,4	9.0	24.1	15.0		
648	Stillwater San Diego	1,862,470.1	1,862,456.7	13.4	3.2	13.8	15.0		
670	Stillwater San Diego	1,862,473.4	1,762,456.7	16.7	15.4	22.7	15.0		
808	Stillwater San Diego	1,862,449.4	1,862,456.7	-7.3	12.3	14.3	15.0		
1131	Stillwater San Diego	1,862,457.0	1,862,456.7	0.3	2.0	2.0	15.0		
8 96 '	San Diego Herndon	3,628,320.3	3,628,265.0	55 . 3	0.5	55.3	9.6		
1401	San Diego Herndon	3,6%8,315.4	3,628,265.0	50.5	3.5	50.6	9.6		
1241	-San Diego Herndon	3,628,300.5	3,028,265.0	35.5	13.1	37.8	9.6		
1365	San Diego Herndon	3,628,296.3	3,628,265.0	31.3	5.0	31.7	9.6		
1365	Larson Herndon	3,494,039.5	3,493,993.6	45.9	3.5	46.0	10.3		
1365	Ft. Carson Herndon	2,374,063.3	2,374,034.5	28.8	7.7	29.8	13.8		
1305	Austin Larson	2,641,159.4	2,641,164.4	-6.0	2.7	6.6	11.4		
1305	G. Forks Larson	1,675,760.3	1,675,745.8	14.5	26.3	30.0	18.6		
1305	San Diego G. Forks	2,387,105.5	2,387,098.2	7.3	1.7	7.5	12.0		
1269	San Diego G. Forks	2,387,105.0	2,387,098.2	6.8	7.3	10.0	12.0		
MEAN				20.1	10.8	. 27.2	14.3		
STAN	NDARD DEVIAT	18.0							

* Line Crossing Results based on International Spheroid

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TABLE 3-6 CEODETIC SECOR USA-2 SATELLITE LARGE QUAD 3-2 CORDEX SOLUTIONS

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	TIONS	RSS M	4	19	18	9	18		
pr	DARD DEVIA	Long M	I	6	3	e	6	4.4	
de) Large Qué	STAN	Lat M	4	18	18	IJ	16	12.2	
ltaneous Mo	CY.	RSS M	177	138	103	145	134		
ons (3-2 Simu	COR - SURVE	Long M	138	109	91	142	114	118.8	19.0
on Site Soluti	SE(Lat M	-111	. 85	6¥	-30	-71	-15.6	73. 0
Hernd	10 .V	ibnl ImoD	108	137	53	140	06		
	Orbits Used	For Solution	896	1401	1401L - 896M	1365 - 1401	1365	Mean	Standard Deviation
	uoi.	tulo2 oN		2	m	-54	5		

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SECTION IV RECOMMENDATIONS

4.1 Introduction. Techniques of data processing developed in the reduction of Geodetic SECOR USA-2 satellite data form the bases of a second generation set of solutions and operational procedures which may significantly influence future uses of the Geodetic SECOR equipment. Noted below is a tentative list of solutions and procedures that should be attempted before the present processing effort is terminated. Observational information from USA-2 Geodetic SECOR satellite tracking is thought to represent the most accurate, consistent, and extensive accumulation of satellite positional data ever taken. If further processing and extended solutions are not undertaken in the near future, present interest and experience will probably dissipate.

4.2 Extended Solutions.

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4.2.1 <u>3-N Solutions</u>. The 3-N solution is an extension of the solutions discussed above in that all available data is included in a least squares solution for the CORDEX site position. This type of solution allows data from multiple satellite passes to be included and eliminates the necessity of using discrete solutions over limited spans of data.

The 3-N solution may be further enhanced by including weighting based upon geometry and an assumed error model plus observational noise estimates. This technique emphasizes data of low noise content in regions of good geometry. Preliminary solutions obtained with the 3-N solution indicate that stable solutions may be obtained where either all three coordinates of the CORDEX site are adjusted, or only the latitude and longitude are adjusted.

4.2.2 <u>Analytic Calibration</u>. An attempt should be made to utilize the overdeterminancy of the observations to adjust not only the coordinates of the CORDEX site, but also to adjust the calibration of the range data. This technique would help reduce the effect of calibration drifts (if any) in the satellite transponder. This type of adjustment is an extension of the technique used during the aircraft flight tests to establish range calibration.

4.2.3 <u>Range Rate Solutions</u>. Further solutions are possible using the computed range rate. The range rates could be used alone or in conjunction with the measured ranges. These solutions should be investigated to determine their relative merits.

4.3 Line Crossing Evaluation. An investigation should be made to determine the causes of the line length offsets which are evident in the data where Herndon was used as the CORDEX site. This investigation should include a network adjustment based upon the measured line lengths to determine if the errors might be attributed to survey offsets at one or more of the tracking sites.

4-1

4.4 <u>Ionospheric Correction Evaluation</u>. The ionospheric data obtained by using the dual frequency phase measurements should be further investigated. Of primary interest should be a comparison with data taken by other means (e.g., NBS ionosonde records) to determine the accuracy and consistency of the measurements. A secondary investigation should be made into better modeling of the ionosphere in order to account for predictable horizontal variations due to the solar zenith, magnetic latitude, etc. Such a model would allow a better ionospheric refraction correction to be made, and would enhance the accuracy of the solutions, particularly at lower elevation angles.

4.5 <u>Orbital Accuracy</u>. Further investigation should be made into the orbital prediction techniques. In particular, investigations of orbital prediction over larger portions of an orbit and also over multiple orbits should be made. These techniques are vital to the extension of the orbital mode operation and more automated techniques of data reduction.

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4.6 Operational Orbital Data. The large quantities of data which can be taken by the operational Geodetic SECOR system require more sophisticated data processing techniques. Use of predicted orbital information could provide a valuable basis for such techniques. For example, data editing based upon orbital prediction could reduce the chances of the occurrence of offset edited data. Furthermore, in regions where only two trackers were locked or within line-of-sight, all range data available could be used in an adjustment program for the orbital elements. į

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APPENDIX A

CONSTANTS, UNITS, HOTATIONS, AND TRANSLATIONS

<u>CONSTANTS</u>.... Conversions of measurements and definitions of basic shapes and sizes are pertinent in data reduction procedures. The constants used in all processing and in earth shape and spin rate computations are given in table A-1.

TABLE A-1

	< 14 H		
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Contraction of the local data and the local data an			

QUANTITY	DIMENSION
ONE METER	3.28083333333 FEET
GNE - DEGREE	0.01745329252 RADIANS
CNE NAUTICAL MILE	6076.10333333 FEET
ONE STATUTE MILE	5280.0000000 FERT
VACO VELOCITY OF LIGHT	983569220.000 FEET/SEC
π	<b>3.1415926</b> 536
ONE SIDEREAL DAY	86164 MEAN SCLAR SECONDS
CNE MEAN SOLAR DAY	86400 MEAN SCLAR SECONDS
EARTH'S ANGULAR RATE $(\omega_e)$	$\omega_{e} = \frac{2\pi}{1 \text{ SIDEREVL DAY}} = \frac{2\pi}{86164} \frac{\text{RADIANS}}{\text{MSS}}$
	$\omega_{e} = 0.0000729212351 \text{ RAD/SEC}$
KOZAL MODEL OF EARTH	
PRINCIPAL GRAVITY	$G = 32.14643177 \text{ FEET/SEC}^2$
SEMIMAJOR AXIS	a = 6378165 METERS
	a = 20925696.335 FEET
SEMIMINOR AXIS	b = 6356783.287 METERS
	b = 208555546.499 FLET
- FLATTENING	i = 1/298.3

*Kozai, Yoshihide, "Numerical Results from Orbits," Smithsonian Institute Astrophysical Observatory Special Report No. 101.

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### TABLE A-1 (Cont'd)

BASIC CONSTANTS

QUANTITY	DIMENSION
INTERNATIONAL EARTH MODEL	
PRINCIPAL GRAVITY	$G = 32.199 \text{ FEET/SEC}^2$
SEMIMAJOR AXIS	a = 6378388.0 METERS
	a = 20926427.961 FEET
SEMIMINCK	b = 6356911.946 METERS
	b = 20855968.607 FEFT
FLATTENING	: = 1/297
1866 CLARK EARTH MODEL	
SEMIMAJCR AXIS	a = 6378206.4 METERS
	a = 20925832.162 FEET
SEMIMINOR AXIS	b = 6356583.8 METERS
	b = 20854392.015 FEET
FLATTERING	£ = 1/294.978698

A sidereal day is the time for one rotation of the earth A mean solar day is an average of true solar days, where a true solar day is the time elapsed for successive intersection of an earth meridian with a sun reference. The mean solar day is defined as 24 hours and, correspondingly, 86400 seconds.

In trajectory predictions, the earth's sidereal period defines the earth's angular rate. Most local and universal time is expressed in mean solar time.

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UNITS . . . The formulae for development of two-body trajectory predictions and partial derivatives are conveniently represented when units of length and time are expressed in what is defined as canonical units. The values of canonical units for near earth two-body equations are given by:

1UL = one unit of length : = a
1UV = one unit of velocity = VUA
1UT = one unit of time = 1UL/1UV

where

- G = 32.14648177 feet/sec², the principal gravity term in the Kozai earth model.
- a = 20925696.335 reet, the earth's equatorial radius in the Kozai earth model.

ECTATIONS . . . Assume a right-handed convention (i.e., the X axis perpendicular to Y where a  $90^{\circ}$  counterclockwise rotation of X rotates X into Y and the Z exis is normal to the XY plane) for all coordinate systems; then the following set of simple rotations will reduce the complexity of representation in each reference frame used in trajectory prediction and vehicle position and velocity computations. In all rotations, the angle of rotation is measured counterclockwise from the new axis to the former axis.

In figure A-1, a rotation about the Z axis that would rotate a vector in the primed into the unprimed system takes the standard matrix form

$$M = \begin{bmatrix} \cos \alpha - \sin \alpha & 0 \\ \sin \alpha & \cos \alpha & 0 \\ 0 & 0 & 1 \end{bmatrix}$$
(1)

X-3

### CUEIC CURPURATION



Figure A-1 Convention for Kotation Angles

Hence,

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and because M will always be an orthogonal matrix (i.e.,  $M^{T}M = 1$ ).

 $\overline{\mathbb{Z}}^{T} \neq \mathbb{W}^{T}\overline{\mathbb{F}}$ 

 $\overline{E} \in M[\overline{z}]$ 

(3)

where the T superscript means transpose.

Adhering to the counterclockwise definition of angles and the righthanded convention stated abave, then the following matrices can be formed to rotate vectors from some local earth surface system of coordinates into equatorial coordinates; hence,

> $M_{1} = \begin{bmatrix} 1 & 0 \\ 0 & \cos \beta & -\sin \beta \end{bmatrix}$  about X to local vertical  $\begin{bmatrix} 0 & \sin \beta & \cos \beta \end{bmatrix}$

:end

cos A -sin A O .M_⊃ ≓ sin A about 2 to local east-north cos A O (5) 0 0 0 И. = sin þ -cos_D about local east to equatorial n vertical (6) $\sin \psi$ cos 🎲  $-\sin\lambda$   $-\cos\lambda$ ^{:м}4  $\cos \lambda - \sin \lambda$  0 about equatorial vertical to colinear equatorial (7)0 3  $M_{f} = M_{0}M_{p} \equiv 10$  cal to east-north-up (ENU) (8) $\dot{M}_{G} = M_{\chi}M_{3} = east-north-up to equatorial$ .(9)  $M_{LOF} = M_0 M_L = M_2 M_3 M_1 = local to equatorial$ (10)where Equatorial = axis in the equatorial plane through the center of mass of the earth and the Greenwich meridian, Y axis in the equatorial plane and 90° counterclockwise from X, and the Z axis along the axis of rotation of the earth. = the plurb line or normal to the local lines Vertical of equipotential gravity (CEOID) X = geodetic or geocentric longitude measured counterclockwise from the Greenwich meridian. b = geodetic (geographic) latitude measured from the equatorial plane

- A = azimuth angle offset between local and ENU coordinates
- is = vertical misalignment between local and ENU coordinates.

CULIC OCREORATION

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when the  $M_{LG}$  matrix above has been computed, a vector  $\overline{R}_{L}$  measured in a local reference system is rotated to equatorial by the single rotation

$$\overline{H}_{HQ} = M_{LU} \overline{F}_{L}$$

and  $\tilde{M}_{LG}^{T}$  will rotate from equatorial to local coordinates.

Rotation from equatorial to inertial is given by

		· 2	- 444
	$\cos \omega_{e} (t - t_{o})$	$-\sin \omega_e (t - t_o)$	0
M _{EI} =	$\sin \omega_e (t - t_o)$	$\cos \omega_{e} (t - t_{o})$	0
	C	0	1

where

inertial = space fixed system which is colinear with equatorial at to:

equatorial to inertial

(12)

to = time of epoch or injection to time in trajectory

<u>TRANSLETIGES</u>... All trajectory computations are performed in an inertial reference system. Measured and computed data may be recorded or desired in some arbitrary local system, with the above matrices, the rotations and translations of position and velocity vectors from a local system to inertial are given by

$$\vec{F}_{EQ} = (M_{L3} \vec{\Gamma}_{L} + \vec{F}_{e} + \vec{T}_{R}^{\dagger} + EJT + \vec{I}_{F}^{\dagger}]$$

$$\vec{F}_{IR} = M_{EI} \vec{F}_{EQ}$$

$$\vec{V}_{IQ} = M_{L3} \vec{V}_{L}$$

$$\vec{V}_{IQ} = M_{L3} \vec{V}_{L}$$

$$\vec{V}_{IR} = M_{E1} \vec{V}_{ele} + \vec{V}_{E}$$

$$(13)$$

CUBIC CURFORATION

where .

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$$\vec{1}_{e} = \begin{cases} \cos \lambda & \cos \psi' \\ \sin \lambda & \cos \psi' \\ \sin \psi' \\ \sin \psi' \\ \sin \psi' \\ \sin \lambda & \cos \psi \\ \sin \psi \\ \sin \psi \\ \sin \psi \\ \sin \psi \\ \cos \psi \\ \sin \psi \\ \sin \psi \\ \cos \psi \\ \sin \psi \\ \sin \psi \\ \cos \psi \\ \sin \psi$$

ctor in geocentric tes

ctor in geodetic tes

fliGT = height of the local coordinate system above mean sea level.

<u>ě</u>f = velocity components due to the earth's rotation

$$V_{E} = v_{e} \begin{bmatrix} -Y_{EQ} \\ X_{EQ} \\ \vdots \\ 0 \end{bmatrix},$$

P' = geocentrio latitude

= position and velocity vectors in inertial coordinates, respectively. RIN, VIN

Position and velocity vectors in inertial coordinates are trans-Formed to local coordinates by the following sequence of rotations and translations;

$$\overline{R}_{L} = M_{L}^{T} [\overline{R}_{PQ} - \overline{R}_{e} + \overline{\Gamma}_{R}]$$
(20)
$$\overline{R}_{L} = M_{L}^{T} [\overline{R}_{PQ} - \overline{R}_{e} + \overline{\Gamma}_{R}]$$
(21)

$$\overline{\overline{V}}_{EQ} = M_{\overline{E}\overline{I}}^{T} \ \overline{\overline{V}}_{\overline{I}\overline{I}} - \overline{\overline{V}}_{e}$$
(22)
$$\overline{\overline{V}}_{L} = M_{E}^{T} \ \overline{\overline{V}}_{EQ}$$
(23)

(18)

(19)

(17)

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when it is necessary to translate position vectors from arbitrary local origins to some known reference point, such as a bench mark, before transforming into equatorial, inertial, etc., the following convention will eliminate sign and sequence errors.

(24)

$$\overline{R}_{N} = \overline{R}_{0} + \overline{R}_{00} - \overline{R}_{NG}$$

where

 $\overline{R}_{N}$  = vector expressed in new (N) system  $\overline{R}_{O}$  = vector expressed in old (O) system  $\overline{R}_{OO}$  = origin of old system  $\overline{R}_{NO}$  = origin of new system

In summary--add the old and subtract the new.

## RANGE RÉSOLUTION

APPENDIX

Cubic Corporation is DME equipments measure slant range by observing the phase shift of a CW signal. The maximum non-ambiguous range obtained from such a measurement is determined by the wavelength of the signal while the precision is determined by the precision of the phase measuring device. In order to have long range tracking capability and a high degree of precision, the phase shifts of signals at two or more different wavelengths are measured.

The data output by most DME systems corresponds to two or more digital range words. The scaling of these words is chosen (i.e., choice of frequencies) so that the bit weightings form a continuous but overlapping binary word. The overlap is chosen to provide redundant information for use in removing intra-channel bias and noise. The basic assumption is that the combination of intra-channel bias and noise will not exceed the overlap bits.

In order to illustrate a method of range resolution, a two-channel (i.e., two frequency) system is illustrated in Figure B-1. The range resolution algorithm will be shown for this arrangement for simplicity but the generalization to a multi-channel system or one with different length words should be povious.

Bit deichting	2 ¹⁰ 2 29	2 ⁸ 2 ⁷ 2 ⁶	25 24 23		ын с. Р. Табра с. — С. С. Царана С. — С. — С. — С. С. — С. — С.
(meters)	C8 C7	6 C5 C4	C3. C2 C1	· -	COARS
Bit weighting		* *	F8 F7 F6 F5	F ₂ F ₃ F ₂ F ₁	Fine
			25 2 ⁴ 2 ³ 2 ²	2 ¹ 2 ⁰ 2 ⁻¹ 2 ⁻²	

Figure B-1. Two-Channel Range Resolution

B-1

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### Range Resolution Algorithm

1. Subtract the overlap bits adding a one as shown to force a positive difference.

1	F8 F7 F6	FINE OVERLAP
- 0	$c_3 c_2 c_1$	CGARSE OVERLAP
Ь	X ₃ X ₂ X ₁	DIFFERENCE

 Add the difference to the coarse to form the corrected coarse word discarding the carry bit, K. Note that the bit X₃ is repeated to the left.

	$c_{3} c_{7} c_{6} c_{5} c_{4} c_{3} c_{2} c_{1}$	COARSE
+	$x_3 x_3 x_3 x_3 x_3 x_3 x_3 x_2 x_1$	DIFFERENCE
K	$c_8^1 c_7^1 c_6^1 c_5^1 c_4^1 c_3^1 c_2^1 c_1^1$	CORRECTED COARSE

3. Combine the corrected coarse with the least significant bits of the fine word to obtain the resolved range:

4. For another channel, say a VERY COARSE, the corrected COARSE now plays the part of the FINE and the VERY COARSE the role of the COARSE in steps one through three.

EXAMPLE 1

10001000		COARSE
21000101		Fine
1110 .		FINE OVERLAP
• <u> </u>		COARSE OVERLAP
1 1 1 0	×	DIFFERENCE

B-2

CUPIC COELCRAI	LTCN
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ų.

(Note  $\dot{x}_3 = 1$ ) 10001000 + <u>1111110</u> 1/1000014000101 <u>EXAMPLE 2</u> 10001000 00100101

> 1001- <u>000</u> 1001

CCARSE <u>LIPPLENENCE</u> COFRECTED COARSE RESOLVED RANGE

CCALSE

FILLE

FIRE OVERLAS

CCARSE CVERLai

DIFFERENCE

(llote  $X_3 = 0$ 

10001000	oc-are.e
+ <u>0000001</u>	DIFFERENCE
1/10001001	CORRECTED COARSE

1000100100101

FEECLVED RANGE

8-3

# AFFEIDIX C

### DATA EDITING

In DME and AME Divital Processing Units, overlapping Prequency or baseline channels with successively higher resolution are processed into a single word. When these overlapping words are combined, high hoise levels, intrachannel bias, or spurious bits will occasionally give a disagreement in the channel overlap. Incorrect overlap can cause an amtiguity in the resolved word with a value dependent upon the bit weightlings of the overlap. Ambiguities may simultaneously occur in more than one overlap position to give some combination of integral number of least significant antiguities.

editing data is the process of recognizing and, if possible, removing ambiguities or spurious sampler. The three types of events which occur in the data and are cause for a decision during sliting are:

- 1. Arbiguities
- 2. Noise
- 3. Ead data

Antiguities car generally be recoved from data if sufficient non-ambiguous date is available. Noise implies randomness and may be removed to some extent by smorthing. Bad data are meaningless data which cannot be recovered by removal of ambiguities. A limited number of bad data points may be removed by replacement based on a prediction with dynamics established show previous Jota.

The pr cess of editing late must begin with some criteria for finding "good information" on which to start a testing procedure. The such criteria is to examine spans of data for an average second difference which is within

.C-1,

the limits of the dynamics of the vehicle. This minimizes the possibility that the span contains ambiguous or bad samples. A second criterion is to begin with an estimated data point and first difference. Other criteria may be dictated by the particular system being employed.

Once the criteria for "good information" are satisfied the basic editing procedure begins. In order to reduce the ellects of the target's dynamics, the editing is done on the first differences. Thus only acceleration and higher order rates affect the data.

The fundamental decision whether a sample may be edited or not is made by comparing the measured first difference against a predicted first difference. The predicted first difference is computed from a span of previously edited date using a linear extremolation.

The discrepancy between the measured and computed first differences is:

$$\mathbf{z}_{\mathbf{j}} = \left\{ (\mathbf{M}_{\mathbf{j}})_{\mathbf{p}} - [\mathbf{M}_{\mathbf{j}} - (\mathbf{M}_{\mathbf{j-1}})_{\mathbf{E}}] \right\}$$

P = predicted

E = edited

.Since all measurements are subject to random errors (8), ambiguities  $(n\underline{A}_{1})$ , and bias ( $\Delta$ ), then

$$(\Delta U_{1})_{P} = (\Delta U_{1})_{T} + \overline{\delta}_{1}, \quad T = true$$

$$U_{1} = (U_{1})_{T} + \overline{\delta}_{1} + nA_{L} + \Delta$$

$$(U_{1})_{E} = (U_{1})_{T} + \overline{\delta}_{1} + nA_{L} + \Delta$$

$$\varepsilon_{1} = [(\Delta U_{1})_{T} + \overline{\delta}_{1} = (U_{1})_{T} - \overline{\delta}_{1} = nA_{L} - \Delta + (U_{1-1})_{T} + \overline{\delta}_{1-1} + \Delta]$$

$$\varepsilon_{1} = [-nA_{L} + (\overline{\delta}_{1} + \overline{\delta}_{1-1} - \overline{\delta}_{1})]$$
where  

$$u = 0_{0} \pm 1, \pm 2, \dots$$
and  

$$\overline{\delta}_{1}, \overline{\delta}_{1} \text{ are random variables.}$$

C-2

It is plear that if the random noise is known to be small compared to A. a noise tolerance gate may be used to determine the acceptability of the data sample. That is, whether  $|\epsilon_1 + n\kappa_L| < \kappa_{\text{NCISE}}$ . Kncise is chosen from some knowledge of the noise content of the data (e.g., the 30 or 40 value or random noise). Any sample not meeting this requirement would be assumed to be bad.

The details of finding  $\left| \varepsilon_{i} + nA_{L} \right|$  depend upon the characteristics of the computer used. In any case,  $n = \begin{pmatrix} \frac{-1}{A_L} \\ A_L \end{pmatrix}$  Nearest Integer.

Once the basic decision is made as to the editability of the sample, a good sample is adjusted by  $\pm nA_L$  and a bad sample is either replaced by a predicted value, or if too many successive samples have been found to be bad, a new search for "good information" is initiated.

A flow diagram for an editing procedure, figure (C-1, i lustrates the general approach and sequence c. testing. A starting criteria is used which tests for continuity on the second differences. Symbols used in the flow diagram are defined below.

### NOTATION

	<b>、</b>	
NOTATION		DEFINITION POP
$(U_1, U_2,, U_N)$		Data Span
$(\Delta U_1, \Delta U_2, \ldots, \Delta U_{N-1}) =$		CIBIE
$(u_2 - u_3, u_3 - u_2, \dots,$	. u ₁₁ - u ₁₁₋₁ )	first differencés
N	م موثير مريم بي م م . -	Nurber of samples in data span
M		Number o.' samples in starting span
$\varepsilon_{i} = \lfloor (\Delta U_{i})_{F} - \Delta U_{i} \rfloor$	~ ~ ~ ~ ~ ~ ~	Residual
		Least significant embiguity
$n = \left(\frac{\varepsilon}{A_L}\right)$ INTEGER		Number of ambiguities added (or removed) from data
K _{NCISE}		lloise gate
^A START	, ,	Maximum average second difference



### HOTAPICN

### <u>DEFINITION</u>

N _{BAD}		Number of successive bad samples
K _{bAD}	************	Maximum allowable number of successive bad, samples
$\overline{\underline{A}}_{\ell}^{m} = \frac{1}{\mu - \ell - 1} \sum_{i=\ell}^{m-1}$	$\left  \Delta^{\mathcal{I}}_{i+1} - \Delta^{\mathcal{L}}_{i} \right  = $	Average second difference

The predicted ΔU's are determined by extrapolating the previous M edited first différences using a least squares polynomial fit.

Because of the finite memory available in computers, long tracks must be sectioned into blocks. In order to use the previous history of the data, the blocks are overlapped so that the starting precedure begins on previously edited data.

A sample of data editing is given in Figure C-2. Jnë set of data has a span d affiguous samples which are completely removed while the other set has a span of bad samples which are replaced by predicted values until the failure counter excess the limit (five in this case).



KER NOXIOT ACCH 359-14

### APPENDIX

### LEAST SQUARES MOVING SPAN COEFFICIENTS, SMOOTHING, AND DERIVATIVE COMPUTATION

If it is assumed that a set of data can be approximated by an arbitrary degree polynomial, then a set of least squares weighting coefficients can be precomputed and used to perform the curve fitting. The general form of the solution for position-to-position, position-to-velocity, etc., least squares smoothing is given by

$$\mathbf{U}_{(\boldsymbol{\beta})}^{\mathbf{L}} = \frac{1}{\Delta T^{\mathbf{L}}} \left[ \mathbf{W}_{1} \mathbf{U}_{1} + \mathbf{W}_{2} \mathbf{U}_{2} + \dots + \mathbf{W}_{i} (\mathbf{K}, \mathbf{L}, \mathbf{n}, \boldsymbol{\beta}) \mathbf{U}_{i} \right]$$
(1)

where

U₁ - the input data

 $1 = 1, 2, ..., n_{z}$  - number of equally spaced data points in linput span (i is odd)

 $W_i$  - least squares weighting coefficients which yield  $U_{(\beta)}^{\perp}$ 

∆T = time interval between data sampl⊕s -

L order of derivative (e.g., L = 1 for position to velocity)

K = degree of polynomial approximation

 $\beta$  = lead of output point or position of output point in input spañ with 21-point, -mid-point, first degree  $\beta$ , zero order coefficients; therefore,  $\beta = 11$ , n = 24,  $\mu = 0$ , and K = 1.

D-1

 $U_{(\beta)}^{L}$  = least squares fit at  $\beta$  point in input span.

Weighting coefficients* are given by

*"Manual for Moving Polynomial Arc Smoothing, " by J. K. Sterrett, Ballistics Research Laboratories, Nov. 1952.

$$W_{\hat{\mathbf{x}}}(\mathbf{K}, \mathbf{L}, \mathbf{n}, \boldsymbol{\beta}) = \sum_{\mathbf{V}=\mathbf{L}}^{\hat{\mathbf{K}}} \frac{P_{\mathbf{V}, \mathbf{n}}(\mathbf{i}) P_{\mathbf{V}, \hat{\mathbf{A}}}^{\mathbf{L}}(\boldsymbol{\beta})}{S_{\mathbf{V}, \mathbf{n}}}$$
(2).

where

 $P_{v_a, \eta}(i) = \alpha r the genal polynomials of any kind (3)$ 

$$S_{v,n} = \sum_{i=1}^{n} \left[ P_{v,n}(i) \right]^2$$
 the sum of the squares of the (4) orthogonal polynomials

$$\mathbf{P}_{\mathbf{v}_{i},\mathbf{n}}^{\mathbf{L}}(\boldsymbol{\beta}) = \frac{\mathbf{d}^{\mathbf{L}}}{\mathbf{d}_{i}\mathbf{L}} \cdot \mathbf{P}_{\mathbf{v}_{i},\mathbf{n}}(\mathbf{i}) \left[ \mathbf{i} = \boldsymbol{\beta} \right]$$
(5)

A sat  $a_{xy}q$  -thogonal polynomials for  $x = 0, 1, 2, 3^{y}$  and L = 0, 1, 2 are:

$$P_{0, \dot{n}}^{0} = 1$$
 (6)

$$\mathbb{P}_{1,n}^{0}(i) = (i - \frac{n+1}{2})$$
 (7)

$$P_{2,n}^{o}(i) = (i) - \frac{n+1}{2}i^{2} - \frac{n^{2}-1}{12}$$
(8)

$$P_{3,n}^{0}(i) = \frac{5}{6} \left[ \left(1 - \frac{n+1}{2}\right)^{3} - \left(i - \frac{n+1}{2}\right) \left(\frac{3n^{2} + 7}{20}\right) \right]$$
(9)

$$P_{o,n}^{1} = 0 \tag{10}$$

$$P_{1,n}^{1} = 1$$
 (11)

$$P_{2,n}^{1}(i) = 2\left(i - \frac{n+1}{2}\right)$$
 (12)

$$P_{3,n}^{1}(i) = \frac{5}{6} \left[ 3 \left( i - \frac{n+1}{2} \right)^2 - \frac{3n^2 - 7}{20} \right]$$
 (13)

$$P_{o,n}^2 = 0$$
 (14)

$$P_{1,n_{c}}^{2} = 0$$
 (15)

$$P_{2,n}^2 = 2$$
 (16)

D-2

$$P_{3,n}^{2}(i) = 5(i - \frac{n+1}{2})$$

(17)

p-3

Some typical, previously computed least squares weighting coefficients: are tabulated in table 1-1.

When equation (1) is used to fit sequential data samples having a variance  $\sigma_u^2$ , the variance of the mean or output sample is given by

$$\sigma_{u}^{2} L_{(5)} = \sum_{i=1}^{n} \frac{\left[ W_{i}(K, L, n, \beta) \right]^{2}}{(\Delta T^{L})^{2}} \sigma_{u}^{2}$$
(18)

$$c = \left(\sum_{i=1}^{n} \left[W_{i}(K, L, n, \beta)\right]^{2}\right)^{\frac{1}{2}}$$
(19)

is defined as the mean reduction factor, C. This factor is the root sum square of n smoothing coefficients, and serves as an index of noise reduction of the output point due to polynomial smoothing. By using the mean reduction factor one can intelligently select the appropriate data span, degree of fit, and output point position to obtain optimum refinement of noise reduction. Tabulations of mean reduction factor for various input spans, three different degrees, and three output point positions are shown in tables D-2 and D-3 for position-to-position and position-to-velocity, respectively. In addition, figures D-1 and D-2 plot the variations in mean reduction factor values with variations in lead point (8) for a 25-point span and third degree fit for position-to-position and position-to-velocity, respectively. In the case of position-to-position smoothing, optimum output point position for first and third degree polynomial least squares fit is the mid-point indicated by absolute minimum value of C. For second degree smoothing, either the one-quarter or three-quarter lead point position is ideal due to the filter symmetry. Further representations of this type of analytic filter are shown in figures D-3 through D-11 which illustrate the filter characteristic response curves to a unity-amplitude sin wave for the 25-n 51-n and 101point span for the three degrees.

1-4

TABLE 'D-L

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l

•		16060	81816	.04545	••08395	-58042	•04545	-,08392	12067.	- 05820
		.09091	.27273	•03636	.02098	.37762	.03636	96020 -	.33566	.05711
¢		16060	.22727	.02727	.10256	.20979	.02727	. 10256	.05594	AE601.
,		16060.	.13182	.01818	.16084	. 07692	algio.	.16084	- 08392	<i>TLL6</i> 0.
NA'S STAN	ICLENTS	16060*	.13636	~ <del>60600</del> •	.19580	02098	60600.	.19580	- 11888	.05750
I T POI	ING COEFF	16060*	16060	0	.20146	08392	0	-20746	80392	0
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SMOCTHIN		16060.	04545	02727	.10256	06294	02727	.10256	16060.	4.10334
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			POSITION-TO-	POSITION N. FACTORS"	
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SPAN N	ORLER L	LEAD β	FIRST DEGREE	: SECOND DEGREE	THIRD DEGREE
11	· 0	´ <b>6</b> ,	. 30151	• 45548	.45548
11	0	, <b>9</b>	.415609	.41700	•53545
11	0	<u> </u>	. 56407	.76185	s.88894
_ 21	0	11 Î	.21822	. 32795	.32795
21	, O	» <b>1</b> 6	.28300	<b>.</b> 29351	. 39109
21	0 [.]	.21	.42130	.59691	<b>.</b> 73759
31	<b>0</b>	16	<b>.</b> 17961	.26965	.26965
31	0	<b>24</b> :	.24096	,24429	. 31901
31 8	× 0	31	. 35069	. 50534	.63959
41	. Q	21	.15617	.2:1437	.23437
41	0	31 (	.20447	. 21/1050	.27877
- 41	0	41	. 30672	.44655	.57165
, <b>51</b>	° 0	1 (	.27599	.40413	.52133
51	0	26	.14004	.21012	.21012
51	Q	44	.22120	.23441	.24362
:51	0	<b>5</b> ]	.27600	. 40413	.52133
, 75		[°] 38 [°]	.11546	.17323	.17323
75	Ç	57	.15362	.15646	.20530
75	< 0	75	.22865	.33737	.43972
101	Ŭ Ŭ	51	•0 <del>9</del> 950	.,14926	.14926
101	0	76	.13107	.13435	.17729
101	0	101	. 197,53	.29269	. 38368
151	0 ·	76 .	.08136	.12207	. 12207
151	0.	,114 š	•10798	.11015	.14476
151	0	151	,16196	.24094	.31760

TABLE D-2

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11	1	° 6	•09535	.09535	.24572
11	<b>1</b>	9	.0953 <b>5</b>	.22594	.25446
. 11	1	11	.09535	.35446	.80949
21	.1	11	.03604	.03604	,09082
21	1	16	.03604	.07587	.07676
21	<u></u> 1	21	.03604	.13831	.32737
ĨŽI	ľ	16	.02008	.02008	.05039
31	, <b>1</b>	24	JÓ2008	-04496	•04755 [.]
31	1	31	.02008	.07805	.18770
41	1	21	.01320	.01320	<i>.</i> :03307
41	" <b>1</b>	31	01320	.02824	<b>.</b> Ø2883
41	1	41	<b>₊0132</b> Ó	.05165	.12531
51	ì	ີ່	.00951 *	.03738	.09120
51	[:] 1	<b>26</b> \	.00951	.00951	.02381
51	ļ	.44	.00951	· 02771	.04279
51	1	Š1	.00951	.03738	.09120
75	1	38 `	.00533	00533	.01334
.75	. 1	57 -	.00533	.01175	.01225
75	1.	7,5	00533.	.02108	.05181
101	į,	51	.'00341	.00341	.00854
101	1	76 [°]	.00341	.00738	<b>: 00759</b>
101	<u>,</u> 1	101	.00341	.01353	• .03339 ,
151	1	76	.00187	.00187	.00467
151	Ĩ	114	.00187	.00409	.00425
151	į	151	.00187	.00742	.01840

TABLE D-5

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## API ENDIX E

#### LANTH-LEF. RENCAL COOPDINATE SYSTEMS

Equatorial Coordinate Syster  $(X_{\rm F}, Y_{\rm H}, Z_{\rm E})$ 

The equatorial coordinate system is a right-handed Carlesian system with origin at the earth's center of mass. The posttive  $Z_{\rm E}$  axis is oriented along the earth's rotational axis toward the north pole. The  $X_{\rm E}$  axis lies in the equatorial plane and passes through the prime meridian and the earth's center of mass. The positive  $Y_{\rm E}$  axis lies in the equatorial plane and is 90° ocunterclockwist from  $X_{\rm E}$ . (See figure 5-1.)

## Geodetic Goordinate System (p. A. h)

Geodetic coordinates are expressed in terms of spheroidal angles and the height above the spheroid. Longitude ( $\lambda$ ; is the angle in the equatorial plane between the X_E axis and the projection of the radius vector. Longitude is measured positive in a counterclockwise direction from the positive X_E axis. Geodetic latitude is the angle subtended with the equatorial plane by the normal to the spheroid which passes through the point. The height is the distance of the point above (or below) the spheroid measured along the local normal. (See figures 5-1 and 5-2.)

#### Conversion between Geodetic and Equatorial Coordinates

Conversions between the geodetic and equatorial coordinate systems depend upon the spheroid constants used to represent the earth. As a matter of common definition, the earth is assumed to be an ellipsoid of revolution about the polar axis. This figure may be defined by specifying the semi-major and semi-minor axes, a and b respectively. The general equation for an ellipsoid is:



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$$\frac{X_{E}^{*} + Y_{T}^{2}}{b^{*}} + \frac{Z_{T}^{*}}{b^{2}} = 1$$

Further parefecters of the ellipsoid are defined as:

$$\frac{2}{a} = \frac{b^2 - b^2}{a}$$
(2)

(1)

$$=\frac{a_{n}+b_{n}}{a}$$

where  $\epsilon = \epsilon$  centricity

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It is eiten necessary to convert the (XYZ, equatorial coordinates of a point into geodetic latitude, longitude, and height. The following equations give the conversion between geodetic and equatorial coordinates.¹

It can be shown that

$$II = \frac{b}{\sqrt{1 - e^2 \sin^2 p}}$$
(4)

$$K_{E} = (N + h) \cos \eta \cos \lambda$$
 (5)

 $Y = (1 + h) \cos p \sin \lambda$  (6)

$$\omega_{\rm L} = \left[ N(1 - e^{\lambda}) + h \right] \sin \gamma \tag{7}$$

Determination of geodetic longitude from the equatorial coordinates is given by

$$\lambda = \tan^{-1} \left( \frac{1}{\frac{1}{\lambda_{L}}} \right)$$
(8)

with the appropriate quadrant selected from the signs of  $X_{\mu}$  and  $Y_{\mu}$ .

¹ Schreiter, J. B., <u>The Weed for Space Fectangular Coordinates in Modern Geodetic Operations</u>, ine Chie State University Fesearch Foundation, Project No. 378, Astia #AT1-90538.

## -12BIC CORPORATION

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Computation of geodetic latitude is not possible in closed form. An iterative solution for latitude is accomplished as follows:²

(1) estimate h and w Brom:

$$h = +\sqrt{x_{\rm E}^2 + Y_{\rm E}^2 + Z_{\rm L}^2} - b$$
(9)
$$y = \sin^{-1} \left[ \frac{2}{\sqrt{x_{\rm E}^2 + Y_{\rm E}^2 + Z_{\rm L}^2}} \right]$$
(10)

(2) calculate t:

$$= \frac{(1 + k)Z_{1} - k(h \sin 2)}{r}$$
(11)  

$$k = \frac{a^{2} - b^{2}}{b^{2}}$$
(12)  

$$r = + \sqrt{\chi_{E}^{2} + Y_{E}^{2}}$$
(13)

(3) calculatera:

$$p = \tan^{-1} \left[ \frac{(1 + k + t^2)Z_E + kt(t^2) + k + t^2 - r)}{(1 + t^2)r} \right]$$
(14)

(15)

: (4) calculate h:

$$h = \frac{r}{\cos \varphi} - N$$

Steps (2) through (4) are iterated to yield the desired result. Test cases run for heights up to 1000 n. miles indicate a convergence of  $\tan_{p}$  to  $10^{-8}$  in two iterations.

² Schreiter, Ibid.

#### APPENDIX T

# CARTESIAN POSITION, VELOCITY, ACCELERATION FROM RANGE AND HANGE RATE OBSERVATIONS

#### Three Range to Fosition (XYZ)

Let  $(XYZ)_1$ ,  $(XYZ)_2$ , and  $(XYZ)_3$  be the locations of three distance measuring equipment (i.e., DME) sites relative to some local coordinate system. Let (XYZ) be the unknown cartesian coordinates of the vehicle relative to this same coordinate system and  $K_1$ ,  $R_2$ ,  $R_3$  are measured slant ranges to the vehicle.

The basic equations relating thomeasured quantities to the vehicle position are:

$$F_{1}^{2} = (x - X_{1})^{2} + (y - Y_{1})^{2} + (z - Z_{1})^{2}$$

$$F_{2}^{2} = (x - X_{2})^{2} + (y - Y_{2})^{2} + (z - Z_{2})^{2}$$
(1)
$$F_{3}^{2} = (x - X_{3})^{2} + (y - Y_{3})^{2} + (z - Z_{3})^{2}$$

The solution of this set of equations may be obtained by eliminating unknowns by successive substitutions; however, the resulting solution is rather complex and has sign embiguities due to the quadratic nature of the equations. A simpler solution is possible if a temporary coordinate system is used. This temporary system has its origin at one of the three trackerssay site one so that  $X_1' = Y_1' = Z_1' = 0$ . Axes of this system are oriented so that the X' - Y' plane contains the other two trackers (i.e.,  $Z_2' = Z_3' = 0$ ). The orientation of the X' and Y' axes is arbitrary since the results will be transformed back to the original system. The transformation from the

**F-1**:

unprimed to the primed system will be

$$\overline{\mathbf{R}}' = \widehat{\mathbf{T}} \cdot (\overline{\mathbf{R}} - \overline{\mathbf{R}}_1) \tag{2}$$

where:

$$\overline{R} = \begin{bmatrix} \mathbf{x} \\ \mathbf{y} \\ \mathbf{z}^2 \end{bmatrix}, \quad \overline{T} = \begin{bmatrix} \mathbf{x}^1 \\ \mathbf{y}^1 \\ \mathbf{z}^2 \end{bmatrix}, \quad \overline{R}_1 = \begin{bmatrix} \mathbf{x}_1 \\ \mathbf{y}_1 \\ \mathbf{z}^2 \end{bmatrix}$$
(3)

and T is the rotation matrix.

The T rotation matrix may be found from the composition of rotations about the x and y axes and requiring that  $Z_2^{(1)} = Z_3^{(1)} = 0$ , hence,

$$T = T_{\alpha} T_{\beta} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & \cos \alpha & \sin \alpha \\ 0 & -\sin \alpha & \cos \alpha \end{bmatrix} \begin{bmatrix} \cos \beta & 0 & \sin \beta \\ 0 & 1 & 0 \\ -\sin \beta & 0 & \cos \beta \end{bmatrix}$$

$$T = \begin{bmatrix} \cos \beta & 0 & \sin \beta \\ -\sin \alpha & \sin \beta & \cos \alpha & \sin \alpha & \cos \beta \\ -\sin \beta & \cos \alpha & -\sin \alpha & \cos \beta \end{bmatrix}$$
(4)

Now,

$$Z_{2}' = -X_{2} \sin \beta \cos \alpha - Y_{2} \sin \alpha + Z_{2} \cos \alpha \cos \beta = 0$$
(5)  
$$Z_{3}' = -X_{3} \sin \beta \cos \alpha - Y_{3} \sin \alpha + Z_{3} \cos \alpha \cos \beta = 0$$
(6)

and upon dividing equations (5) and (6) by  $(-\cos \propto \cos \beta)$ ,

$$X_2 \tan \beta + Y_2 \frac{\tan \alpha}{\cos \beta} - Z_2 = 0$$
 (7)

$$X_3 \tan \beta + Y_5 \frac{\tan \alpha}{\cos \beta} - Z_3 = 0$$
 (8):

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Solving for tan 3 and tan  $\propto$  gives

$$\tan \beta = \begin{bmatrix} \frac{Z_2 Y_3 - Z_3 Y_2}{X_2 Y_3 - X_3 Y_2} \end{bmatrix}$$
(9)  
$$\tan \alpha = \begin{bmatrix} \frac{X_2 Z_3 - X_3 Z_2}{X_2 Y_3 - X_3 Y_2} \end{bmatrix}$$
cos 3. (10)

with tan 3 and tan 4 known, the T rotation matrix can be computed.

when the primed coordinate system is used, the basic range equations become:

$$F_1^2 = x^{1/2} + y^{1/2} + z^{1/2}$$
(11)

$$E_2^2 = (x^1 - X_2^{-1})^2 + (y^1 - Y_2^{-1}) + z^{12}$$
(12)

$$F_{3}^{2} = (\mathbf{x}' - X_{3}')^{2} + (y' - Y_{3}')^{2} + z^{2}$$
(13)

Subtracting equation (41) from equations (12) and (13) yields

$$-\frac{1}{2} (R_2^2 - R_1^2 - r_{2'}^2 = X_2' \mathbf{x}' + Y_2' \mathbf{y}')$$

$$-\frac{1}{2} (R_3^2 - R_1^2 - r_{3'}^2) = X_3' \mathbf{x}' + Y_3' \mathbf{y}'$$
(14)
where:  $r_1^2 = X_1'^2 + Y_1'^2$ 

Sclving the linear system in x' and y' by Gramer's rule,

$$x' = \frac{1}{2\Delta} \begin{bmatrix} x_1^2 - x_2^2 + r_2^2 & Y_2' \\ (r_1^2 - y_3^2 + r_3^2) & Y_3' \\ (r_1^2 - y_3^2 + r_3^2) & Y_3' \end{bmatrix}$$
(15)  
$$y' = \frac{1}{2\Delta} \begin{bmatrix} x_2' & (r_1^2 - r_2^2 + r_3^2) \\ x_3' & (r_1^2 - r_3^2 + r_3^2) \end{bmatrix}$$
(16)

¢

 $\Delta = \begin{bmatrix} x_{2}' & y_{2}' \\ x_{3}' & y_{3}' \end{bmatrix}$ 

Expanding and grouping the constant terms gives

$$\mathbf{x}^{1} = K_{1} R_{1}^{2} + R_{2} R_{2}^{2} + K_{3} R_{3}^{2} + K_{4}$$
(18)

$$y' = \kappa_5 \bar{\kappa}_1^2 + \kappa_6 \bar{\kappa}_2^2 + \kappa_7 \bar{\kappa}_3^2 + \kappa_8$$
(19)

- $K_{1} = \frac{1}{2\Delta} (Y_{3}^{i} Y_{2}^{i}) \qquad K_{5} = \frac{1}{2\Delta} (X_{2}^{i} X_{3}^{i})$   $K_{2} = -\frac{1}{2\Delta} (Y_{3}^{i}) \qquad K_{6} = \frac{1}{2\Delta} (X_{3}^{i})$
- $K_{2} = \frac{1}{2\Delta} (X_{2}^{*}) \qquad \qquad K_{\gamma} = -\frac{1}{2\Delta} (X_{2}^{*})$   $K_{4} = \frac{1}{2\Delta} (X_{3}^{*}r_{2}^{2} X_{2}^{*}r_{3}^{2}) \qquad \qquad K_{5} = \frac{1}{2\Delta} (X_{2}^{*}r_{3}^{2} X_{3}^{*}r_{2}^{2})$

and with  $x^{!}y^{i}$  know.,  $z^{i}$  may be found by

$$x' = -\sqrt{x_1^2 - x_1^2 - y_1^2}$$
(21)

In most applications the sign of 2' is easily determined. For example, with ground based trackers and an airborne vehicle, z' would be positive. The solution in the primed coordinate system can be transformed into

the unprimed system as collows:

$$= T^{T} \cdot \vec{p}^{T} + \vec{1} \cdot \vec{p}$$
 (22)

where

$$\mathbf{T}^{\mathbf{T}} = \mathbf{T}_{\boldsymbol{\beta}}^{\mathbf{T}} \cdot \mathbf{T}_{\boldsymbol{\alpha}}^{\mathbf{F}}$$

(23)

(17) -

(20)

# CUBIC CONFORATION

# Kange Rate and Acceleration to (XYZ) and (XYZ)

Suppose that  $R_1$ ,  $R_1$ , and  $R_1$  are determined from each of three known sites and it is desired to compute the velocity and acceleration in cartesian coordinates. The basic relationships at each site are given by

$$E_{i}^{2} = ((x_{i} - \dot{x}_{j})^{2} + (y - \dot{x}_{j})^{2} + (z - \ddot{z}_{j})^{2}$$
(24)

$$L_{i} = [(x - X_{i})x + (y - Y_{i})y + (z - Z_{i})z]$$
 (25)

$$R_{i}R_{j} + R_{i}^{2} = [(x - X_{j})x + (y - Y_{i})y + (z - Z_{i})z] + x^{2} + y^{2} + z^{2}$$
 (26)

where: X₁, Y₁, Z₁ are known site locations assumed to be fixed.

The quadratic set of equations (24) may be solved for x, y, z as described in the accompanying section. The set of equations resulting from (25) and (26) reduce to the linear forms:

$$\vec{v} = [c]^{-1} [\dot{R}]$$
 (27)

and -

$$\overline{A} = [C]^{-1} \{ [R] + [r] \}$$
(28)

where:

 $\vec{v} = \begin{bmatrix} \cdot \\ x \\ \cdot \\ y \\ \cdot \\ z \end{bmatrix}, \quad \vec{A} = \begin{bmatrix} \cdot \\ x \\ \cdot \\ y \\ \cdot \\ z \end{bmatrix}$ (29)

$$[C] = \begin{bmatrix} (x - X_1)/R_1 & (y - Y_1)/R_1 & (z - Z_1)/R_1 \\ (x - X_2)/R_2 & (y - Y_2)/R_2 & (z - Z_2)/R_2 \\ (x - X_3)/R_3 & (y - Y_3)/R_3 & (z - Z_3)/R_3 \end{bmatrix}$$
(30)

F-5

$$\begin{bmatrix} \mathbf{R} \end{bmatrix} = \begin{bmatrix} \mathbf{R} \\ \mathbf$$

# Two Ranges and Altitude to Losition (XYZ)

Let  $(XYZ)_1$  and  $(XYZ)_2$  be the locations of two distance measuring equipment (i.e., DME) sites relative to some local coordinate system. Let (xyz) be the unknown cartesian coordinates of the vehicle relative to this same coordinate system. Furthermore, let  $R_1$ ,  $R_2$  be the measured slant ranges to the vehicle and let h denote the altitude of the vehicle. The basic equations relating the measured quantities to the vehicle

position are:

$$R_{1}^{2} = (x - X_{1})^{2} + (y - Y_{1})^{2} + (z - Z_{1})^{2}$$

$$R_{2}^{2} = (x - X_{2})^{2} + (y - Y_{2})^{2} + (z - Z_{2})^{2}$$

$$R_{1}^{2} = (\rho_{1} + h_{1})^{2} + (\rho + h)^{2} - 2(\rho_{1} + h_{1})(\rho + h) \cos \psi$$
where:  $\cos \psi = \frac{\rho_{1} + h_{1} + z}{(\rho + h)^{2}}$ 

It is assumed that the altitude of the vehicle (h) is sufficiently small so that the local deflection of the normal does not introduce a significant error. (See figure E-1.)

F-6

(31)-

(32)



Figure F-1. Geometry for Two-Range and Altitude Solution

The above system of equations may be simplified by transforming to a temporary cartesian coordinate system. This system is denoted as the primed system and is defined as follows: (1) center at one of the tracking sites (site 1); (2)  $z^{i}$  exis along the radius vector from the center of the earth; (3) the y' axis is normal to the  $z^{i}$  axis and oriented such that  $X_{2}^{i} = 0$ ; (4) the  $x^{i}$  exis completes the right-handed cartesian coordinate system.

The transformation to the primed system is given by:

$$\overline{\mathbf{r}'} = T \cdot (\overline{\mathbf{r}} - \overline{\mathbf{R}}_1)$$
where: 
$$\overline{\mathbf{r}'} = \begin{bmatrix} \mathbf{x}' \\ \mathbf{y}' \\ \mathbf{z}' \end{bmatrix}, \quad \overline{\mathbf{r}} = \begin{bmatrix} \mathbf{x} \\ \mathbf{y} \\ \mathbf{z} \end{bmatrix}, \quad \overline{\mathbf{R}}_1 = \begin{bmatrix} \mathbf{x}_1 \\ \mathbf{y}_1 \\ \mathbf{z}_1 \end{bmatrix}$$

$$T = \begin{bmatrix} \cos \alpha & \sin \alpha & 0 \\ -\sin \alpha & \cos \alpha & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$A = \tan^{-1} \left( -\frac{\mathbf{x}_2}{\mathbf{z}_2} \right)$$

Y-7 -

The above set of equations in the primed system is:

$$R_{1}^{2} = x^{12} + y^{12} + z^{12}$$

$$R_{2}^{2} = x^{12} + (y^{1} - Y_{2}^{1})^{2} + (z^{1} - Z_{2}^{1})^{2}$$

$$R_{1}^{2} = (\rho_{1} + h_{1}^{2})^{2} + (\rho + h)^{2} - 2(\rho_{1} + h_{1})(\rho_{1} + h_{1} + z^{1})$$

This set of equations is not soluble in closed form since the radius of the earth ( $\rho$ ) at the latitude of the vehicle is not known. An iterative solution is used where initially it is assumed that  $\rho = \rho_1$ . The resulting solution may be expressed in latitude, longitude, and height relative to some spheroid. Using this latitude, a new approximation of  $\rho$  may be computed and compared with the previous value. The solution is iterated until  $/\rho^{(i+1)} - \rho^{(i)}/ < \text{LIMIT}$ , where LIMIT is some specified convergence limit. The solution of the above equations for a given  $\rho$  proceeds as follows:

1) The third equation is solved for z':  

$$z' = \frac{(\rho + h)^2 - (\rho_1 + h_1)^2 - R_1^2}{2(\rho_1 + h_1)}$$

(2) Subtracting the first two equations:

$$R_2^2 - R_1^2 = -2Y_2^1 y^1 - 2Z_2^1 z^1 + Y_2^1^2 + Z_2^{12}$$

(3) Solving for y':

$$\frac{R_1^2 - R_2^2 + Y_2^2 + Z_2^{12} - Z_2^{12} z^{11}}{2Y_2^{12}}$$

(4) Solving the first equation for x':

$$x^{1} = \frac{1}{2} \sqrt{E_{1}^{2} - y^{1}^{2} - z^{1}^{2}}$$

7-8

The solution in the primed system for a given  $\rho$  is complete except for the sign of x¹. This sign ambiguity results from the quadratic nature of the basic set of equations and must be resolved by a knowledge of on which side of the baseline the vehicle lies.

The solution in the primed system  $(\mathbf{r}^*)$  may now be transformed back into the original coordinate system by:

$$\overline{\mathbf{r}} = \mathbf{T}^{\mathrm{T}} \cdot \overline{\mathbf{r}}' + \overline{\mathbf{R}}_{1}$$

The latitude of the vehicle must now be determined from r by using the relationship between the unprimed coordinate system and the equatorial system.

The relationship between the radius (p) and the latitude  $(\phi)$  is given by:

$$\rho = \begin{pmatrix} b^2 + \frac{a^2 e^2 \cos m}{1 - e^2 \sin^2 p} \end{pmatrix}$$

where a, b, e are the semi-major and semi-minor axes and eccentricity of the reference spheroid.

#### FOF/UC //kkb

#### APPENDIX

## ALLYTIC TROPOSPHERIC REFRACTICE. CORRECTICS.

Empirical formulae for refraction correction may be computed quickly and require a minimum amount of meteorological data for their use. Eccauses of these features, empirical formulae are useful when high accuracy is not the primary requirement. Given here are empirical refraction correction formulae that require only the index of refraction at the surface, maximum range adjustment at zenith and zero elevation angle. The tropospheric refraction correction is accurate to about 10 per cent of the correction.

The retardation in range due to propagation in the lower atmosphere is given -

$$\Delta R = \frac{K_1 (1 - e^{-ZK})}{\sin E_0 + K_2 \cos E}$$

G-1

(1)

# CULIC CURPORATION

Angular bending in the vertical plane is given by

$$\Delta S = \left[1 - \frac{1}{2R} (1 - e^{-ZR})\right] - 2\gamma(n_0 - 1)(1 + 1^2 + 1^5)$$
 (2)

where  $\gamma = 3.0..., \pm \text{ control constant}$  $t = (1 + \gamma^2 t \sin^2 z_0)^{1/2} - \gamma t \sin z_0^{-1}$ 

 $n_{c} \approx$  1.000360....the surface index of refraction

Corrected runge and elevation angles are given by

Figures 1 and 2 illustrate typical values of  $\Delta R$  and  $\Delta C$  as a function of elevation angle when the vehicle is above 75 km altitude. For comparison, values for AR and AD using the CHFL Exponential Reference Atmosphere *

plot ed (circled points) in figures G-1 and G-2.

Bean, B.R. and Thuyer, G.D., <u>CRPL EXPONENTIAL ATMOSPHERE</u>, National Bureau of Standaris Monograph 4, October 29, 1959.

(4)

Figure **1-1** PROPOSEMENTE PLAN 10.00 1.1-1 144 DETON 9.00 Febra 1 EF FE ï ANALYTIC HODEL **a** 1 1.1 s.00 1 FIF 4-2141 <u>1. F</u> × ŢŢ <u>i FI</u> 1.74 177724-11 12 <u>,00</u> Ei+ ľ 15 ORNECTION 1- 1 -----F Ŧ sje. t: : : F. <u>i</u>del 1 1-1 » <u>600</u> + F! [-] ELEVATION A 1-7 GLEC; 1 ..... 1 ; Į. **!** + FLE • 4F + + Ŧ Īt ÷1 ٠+ <u>5 00</u> ÷. 4 1-1-1-H ļ ł 1 Ĵ. 1 1 <u>t 1</u> ; I. ł : 1.00 ii liit <u>i i i</u> TITE F 75 Km 14 1173 1 AVOVO 1 • -. ÷ 11 ÷ EH EEF 1 E Ŧ E 11 1 ļ Ż 3.00 ÷Ē + Ŧ 日 1 F -1 1 1.1 +-! 1-1-1 200 -------1. -1; ł 1. + | ī ł į. 11-F 1 -i-i -Ĩ, 17 1.1 ٠ŕ ∆r . 1-4-. . 1. 4-• • 14 . . 1 ļ. .... Ţ . 1 ÷ : 1 + ļ 1 (Meters 4-4-4 ì 十 , -----<u>ه_</u> 4 ÷. 1-1 T T -- **]**--٠ Ŧ ---l 1. -+-++ t ż i t-1-1 Ť Ŧ 100 1 ET 91.17 1-1-1 E4 1 -----1.1 -1 TEL. T ÷ 1 δΩ 11.1 =Ť E deleter -11 ; Ţ ÷ FEE EI T 33 8.0 H FFF <u>Et l</u> 1 Ŧ ΞĘ. 1 ī - - -- - <del>-</del> - <del>-</del> -1-1-1-1-1-1 ٠, ī <u>, 0</u> ÷È F E **+** | + सम्म Ŧ Ŧ 7 \$ <u>6 Q</u> <u>1:1-1</u> ÷ E 13-1 日 1-1-1 i Ŧŀ <u>, 0</u> t: 4 1-1-1-1 17 1:1-1-1-1-1 ţ 111 i tetet + ------1 10 TTT Ţţ 133 -•• . ..... T -: FL 1 TFD . ŗ 1. . . 1 30 11 11 .... Į. *** <u><u></u></u> Þ 1 1E T-1-1 i ř. Ŧ 1.I 6-17 ŧ - i - : F Ħ Ŧ 1.1 F + 1 •--<u>.</u>:+ - - h - h -] ..... 1 į - -----: 1-1-1 t ..... 1-1 i Ť ŦŦı ++++++ 計註 白 1 t 4 20 10 359-71 H H. HI!! 1 ور في ال هم ب T ţ. Ì f____ 11. 1 ٩ 1 * * * Ţ •-+ i 1 1-1 Ħ F TT 11 1.1 + ކ; 1 Ł + -1-1 ┥┥┥ ÷ H Semi-Logarithmic Kelpte - a ester co Sector 70 d ĭ T 4.1 ... A 44 4 Ī þ, -- +---++ 1-1-1 11 10 UB 1 7497 1-1-1-1-1935 1.15 FE. F T1 9___ : i EE ٦. 1 1.1.1 TT. 1-1-1-+ ÷ -33 ۲., ITT H 15 17-1-1 ŢĴ FT TH 1 EFF -1 7_ FT. T I I **1** 1711 N: FFIE 手) モ -----6_ Ŵ 11 :L 1. <u>i-</u> Ę * - - + -1 1-<u>*</u> 19 1. ÷.† ŀ İ İŦ -1-+ E-F-E 1=1=1 5. 11 <u>ter</u> T T 4-1-1-1 Ŧ.; 1 j-l 1 4-· # -----Ŧ 1 FH 4. 177 ŢŦ. Ŧŗ 1.1.1 1 11 --ŗ Ŧ H 173 1 1 +; ÷ Ē ectio ALL N IT Ē [===] -Ī. ----1.1.7 ĩ 1 ĩ • 1.15 ŧ Ľ Ŧ Э. -0-1 Ŀ 5 i ŧ. ÷ 1 Ŧ. Ŧ He te H opnent 11.1 E <u>++</u>: ٠ Ŧ dri Í. ETAN Ħ 2. -----: +++ ₽**¥** 1-1-1--t • ÷ sph ere --i **F.U.** ţŦ 4 17 11 T 1111 11 - 1 Ħ +-+ 1 4. ---------# * ŗ 1 ł . r. Ŧ H +11+ ++1 ł ŧ., ÷ 1++ 1 11 ŕ tt; 71 ľ Ť 70 20 50 60 10 40 0

## ELEVATION ANGLE (DEGREES)

G-5



#### APPENDIX H

#### ANALYTIC IONOSPHERIC CORRECTION

The correction for the range retardation due to ionospheric effects is given by:

$$\Delta R = \frac{40.3 \text{ H} \text{ H}_{0}}{4\Omega^{2}(\sin E + K \cos E)} \left\{ \tan^{-1} A - \tan^{-1} \left[ A \left( \frac{H_{0} - H}{H_{0}} \right) \right] \right\} \left( 1 - e^{-HT} \right)$$

 $N_0 \times 10^{12}$  = maximum electron density of the  $F_2$  layer in (electrons/meter³)

- f = carrier frequency in Mc/Sec.
- H = height of vehicle in meters
- H = height of N in meters
  - E = elevation angle

K = an empirical constant

 $\int_{d}^{\infty} = \left( \frac{\frac{2H_{o}}{H_{U}} - H_{L}}{H_{U}} \right) = \text{control constant}$ 

 $H_{U}$ ,  $H_{L}$  = upper and lower heights in meters of the half values of the electron density profile

T = 1/(50,000 mêters)

The corrected range is given by:

$$R_{C} = R_{M} - \Delta R$$

The general form of this correction may be deduced by assuming:

1. the refractive index for the ionosphere is given by:

$$n(f) \approx 1 = \frac{40.3 \text{ N(H)}}{2}$$

"Processing and Analysis of Azusa MK II Data" General Dynamics Astronautics Technical Report No. AE 60-0017, by A. Saastad and F. C. Forbes, 10 June 1960.

H-1

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2. the altitude dependence of the electron density is given by:

$$H(H) = \frac{N_{o}}{1 + \sqrt{2} \left(\frac{H - H_{o}}{H_{o}}\right)^{2}}$$

3. the flat earth approximation, and horizontally stratified ionosphere. The form of N(H) model is shown in figure H-1 and a comparison with ameasured profile is shown in figure H-2.

The range error due to ionospheric effects may be written:

$$\Delta R = + \frac{C}{\omega} (\Delta r)_{\dot{H}} = - \frac{A O_{\star 3}}{f^2} \int_{0}^{T} W(H) dr$$

Substituting for ::(H):

$$\Delta H = -\frac{40.3 \text{ H}_{0}}{f^{2} \sin E} \int_{0}^{H} \frac{dL}{1 + \sqrt{2}} \frac{dL}{(\frac{H - H_{0}}{H_{0}})^{2}}$$

Integration yields:

$$\Delta R = \frac{40.3 \text{ N}_{0} \text{ H}}{\text{wf}^{2} \sin E} \left\{ \tan^{-1} (w) - \tan^{-1} \left[ \left( \frac{\text{H}_{0} - \text{H}}{\text{H}_{0}} \right) w \right] \right\}$$

This expression is the same form as the final range correction formula. The additional term in the denominator and the exponential term are added to agree more closely to experimental results at low altitudes and low elevation angles.

TAIRE 12 ì - 4 -.-i + j ť, DENST Ť -1 +++ ĔŔ 105 mari HEIGHT T. --].]. ]...., Ì ļ TL Ţ. .K) . +-1 ----4 *** Í. -1 •---į. Ť Å 1 1.1 ••• • -• • -• í :. *_k.i ĵ . ŧ 1 ł 4 1-1 ł . ± • i - 1. ł ٠ łł ------1 七 ł 1 -----1 . . . . . . ; 7 i. I <u>+-</u>j ş ţ I 7 ŧ 2 Ĵ. ÷ 1111 11 ŧ, 1 11 1 × 1 т • 7 1 1 L -1 t ł 4 11 t N trop **Jane** ŧ £ L L -----11 ļ ÷ ł Î 1 İ · + 1 Į 11 -4 11 ĩ ļ. 1-1i ł * Li. 12 --* * +--· ł_ + Ŧ 1 1 ſ : ; ; 1 -----11 • • • 1 1 1 Ē 1 . .... -----•--: F - Inves 1 ı, ì 11ri LLI ŧ * . H. U Į., + 4-13 4-13 ł 1 1 .1 i r 1-1 -[-]-] ţ -1 r_____ 1 ļ ŕ Ì. . . • 1 1 1 -1 - . . 1 4 -+ 1 11 FI - i 1-1-* L t Į Нo 4  $\hat{\mathbf{v}}$ 1 1 i r 1 • • • • • • Ī. + • : -----17 \$ . . , Ĵ ÷ I ļ · · Ĭ i î ÷1 . ju ~ ţ .... : -1ŧ ł ŧ 359-500 °,14 . ł. : + HL **i**., -***** ----; ; ; : 1..... 1 1 . 1 * 1. • • • • • • • .... : KE KEUFFLA CASTERS. . Ļ × 1 14 . . 1 -+ Fil ł •• ļ ŧ *** į 1 4 +----1 ----4 -4 4 -4 7 1 ŕ . 1 ł -2 . . Ĩ , , ī, i ŧ .1. ŀ Ţ **†**-4 + ł t ſ ŧ 1.1. 11 -1 1_ Ĺ Fit 1 十 1 * ٠ 11 1 + : .: • 助 ۶. đ 1 T í ı *** 11 . t -15 Ť ; 1.1 ~ * * * ; ŧ 11 ÷ 7 į ş. . . Jul. * * * * * * * * . ... 1 1 + ŕ Į. 4-4 * 1 ÷ • • • . ļ 4 1. Ţ T ---------• \$. \$ *: ¥ • 1 Ì 1 4 ţ ļ • • 11 : ; -† 117 +1 0.00 0.2 0. 0,6 0.8 1.0Ξ

N/N_o

H-3



# BUBIC CORFORATION

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The parameters of the model generally vary as a function of the local time, sunspot activity, latitude, and various other factors. In order to fit the assumed model for N(H) to existing conditions, two parameters are adjusted using the measured range corrections from dual frequency range measurements. The two parameters adjusted are N_o and K plus a calibration constant.

The normal equation associated with the ith observation is:

 $(1x1) \quad (1x3)(3x1)$  $\varepsilon_{i} = \lfloor Q_{i} \rfloor \lfloor D \rfloor = 1$ 

where: 
$$[\varepsilon_{i}] = (\Delta R_{M} - \Delta R_{c} + K_{cal})i$$
  
 $[\Box_{i}] = \begin{bmatrix} \underline{\partial \Delta R} & \underline{\partial \Delta R} \\ \overline{\partial K_{cal}} & \underline{\partial \Delta R} \\ \overline{\partial N}_{0} & \overline{\partial K} \end{bmatrix} i$   
 $[D] = \begin{bmatrix} \Delta K_{cal} \\ \Delta N_{0} \\ \overline{\Delta K} \end{bmatrix} i$ 

The partial derivatives of  $[Q_i]$  are:

$$\frac{\partial \Delta R}{\partial K_{cul}} = -1$$

$$\frac{\partial \Delta R}{\partial N_{o}} = \frac{\Delta F_{c}}{N_{o}}$$

$$\frac{\partial \Delta F}{\partial K} = \frac{\Delta R_{c}}{\sin E + K \cos i}$$

 $\angle E_c = range correction calculated from model.$  $<math>\angle R_M = range correction from dual frequency range measurements.$  $K_{cal} = calibration constant for \angle R_M$ .

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The least squares solution for [D] with n observations is given by:

 $\begin{bmatrix} \mathbf{D} \end{bmatrix} = \left\{ \begin{bmatrix} \mathbf{n} \\ \boldsymbol{\Sigma} \\ \mathbf{i} = \mathbf{1} \end{bmatrix}^{\mathrm{T}} \begin{bmatrix} \mathbf{Q}_{\mathbf{i}} \end{bmatrix}^{\mathrm{T}} \begin{bmatrix} \mathbf{Q}_{\mathbf{i}} \end{bmatrix}^{\mathrm{T}} \begin{bmatrix} \mathbf{Q}_{\mathbf{i}} \end{bmatrix}^{\mathrm{T}} \begin{bmatrix} \mathbf{Q}_{\mathbf{i}} \end{bmatrix}^{\mathrm{T}} \begin{bmatrix} \mathbf{e}_{\mathbf{i}} \end{bmatrix} \right\}$ 2

The adjustments to  $k_{cal}$ ,  $N_o$ , K are added and the process iterated until the adjustments become small.

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## -CULIC CURPORATION

#### APPENDIX I

## DUAL FREQUENCY IONOSPHERIC CORRECTION

The Geodetic SECOR system has a built-in method for determining the phase shift of the signal due to interaction with the ionosphere. In the simplified derivation of the correction technique given below, the following assumptions are made:

1. The carrier frequencies are much greater than the gyromagnetic frequency and the effective electron collision frequency.

2. The modulation frequencies are sufficiently close to the carrier frequency so that the differential phase shifts may be ignored.

A similar derivation may be performed without using these assumptions, but the mathematical complexity is much greater and the results are not significantly changed for frequencies used by the system.

The Geodetic SECOR ground stations transmit a single carrier frequency to the satellite transponder. The transponder generates two return signals which are initially phase coherent with the signal received at the satellite. The carrier frequencies used in the Geodetic SECOR system are:

> $f_1 = f = 420.0 \text{ mc/sec}$   $f_2 = f + \Delta f = 449.0 \text{ mc/sec}$  $f_3 = \pi f = 224.5 \text{ mc/sec}$

The corresponding frequencies expressed in radian/sec are related to the above by:

 $\omega = 2\pi \mathbf{i} \times 10^6.$ 

1-1

(1):

(2)

# CUPIC CORFORATION

Under assumptions (1) and (2), the effective index of refraction for the ionosphere may be written:

$$n(\omega) = 1 - \frac{\eta k(r)}{\omega^2}, \quad \eta = \frac{2\pi\epsilon^2}{m}$$

e = electron charge = 4.8 x  $10^{-10}$  esu m = electron mass = 9.1 x  $10^{-28}$  gm N(r) = electron density (electrons/cc)

The total phase shifts referenced to  $\omega$  along each one-way path may be written as:

$$\Delta \varphi_1 = \frac{\omega}{c} \int_0^r n(\omega) dr$$
$$\Delta \varphi_2 = \frac{\omega}{c} \int_0^r n(v + \Delta u) dr$$
$$\Delta \varphi_3 = \frac{\omega}{c} \int_0^r n(v + \Delta u) dr$$

"hen the total two-way phase shifts are given by:

$$\Delta p_{12} = \omega p_1 + \Delta p_2 = \frac{\omega}{c} \int_0^r (n(\omega) + n(\omega + \Delta \omega)) dr$$
  
$$\Delta z_{13} = \Delta p_1 + \omega p_3 = \frac{\omega}{c} \int_0^r (n(\omega) + n(\omega)) dr$$

Substituting the functional form of n:

Š.

$$\Delta v_{12} = 2 \frac{\omega}{c} \int_{0}^{r} dr - \frac{\omega}{c} \int_{0}^{r} \left( \frac{\eta!!(r)}{\omega^{2}} + \frac{\eta!(r)}{(\omega + \Lambda \omega)^{2}} \right) dr$$
(6)  
$$\Delta v_{13} = 2 \frac{\omega}{c} \int_{0}^{r} dr - \frac{\omega}{c} \int_{0}^{r} \left( \frac{\eta!!(r)}{\omega^{2}} + \frac{\eta!(r)}{\omega^{2}} \right) dr$$

(4)

-(5)

I-2

(3)

In equations (6) the first term is the phase shift which would be observed in the absence of the ionosphere. Then the phase shifts along each path due to ionospheric effects are given by:

$$(\Delta p_{12})_{i} = -\frac{\pi}{\alpha \omega} \left[ 1 + \frac{1}{(1 + \frac{\Delta \omega}{\omega})^2} \right] \int_{0}^{r} \mathbb{I}(\mathbf{r}) d\mathbf{r}$$
(7)

$$(\Delta p_{13})_{i} = -\frac{n}{\omega} \left[1 + \frac{1}{\sqrt{2}}\right] \int_{0}^{r} N(r) dr$$

Now let:

$$B = (1 + \frac{\Delta \omega}{\omega})$$

 $I = \int_0^1 l(r) dr = integrated electron density$ 

-Then:

$$(\Delta v_{12})_{i} = -\frac{n}{\omega} \left(1 + \frac{1}{2}\right)_{i}$$
$$(\Delta v_{12})_{i} = -\frac{n}{\omega} \left(1 + \frac{1}{2}\right)_{i}$$

Now the relative phase shift  $(\Delta p_{13} - \Delta p_{12})$  scaled to a one-way range difference (K) is determined:

$$K = \frac{c}{2\omega} (\Delta r_{13} - \Delta r_{12}) = \frac{c}{2\omega} [(\Delta r_{13})_{12} - (\Delta r_{12})_{1}]$$
(10)  
$$= -\frac{n}{2\omega^{2}} [1 + \frac{1}{\omega^{2}} - 1 - \frac{1}{\omega^{2}}] I$$

Solving for I:

1

$$= \frac{\frac{2n}{\kappa}}{(\frac{1}{c^2}, \frac{1}{c^2})}$$

(11)

(8)

(9)

Having determined I; the range error due to ionospheric effects is given by:

$$(\Delta R_{12})_{1} = \frac{c}{b} (\Delta \varphi_{12})_{1} = \frac{(1 + \frac{1}{3^{2}})}{(\frac{1}{3^{2}} + \frac{1}{3^{2}})^{2}}$$
(12)

(13)

,(14),

<u>I-4</u>

For the Geodetic SECOR system:

× = 0.534

3 ≈ 1.067

K = V = VFIC

 $R_{c} = R_{m} - (\Delta R_{12})_{i}$ 

so that  $(\Delta H_{12})_1 = 0.715$  K and the corrected range is:



U

#### ARPENDIX J

# TRANSIT TIME CORRECTION

The purpose of the transit time correction is to associate with a set of simultaneous range data a meaningful time. That is, a time which represents the "measured time."



At time  $t_0$  (figure J-1 ) the read pulse is sent from the satellite transponder. Due to the finite velocity of propagation C, the two stations will record the range at times  $t_1$  and  $t_2$ , respectively. Assuming C is constant over the two paths;

It is clear that the times and/or the ranges must be adjusted if the time reference is to correspond to the vehicle position. (1)

 $t_1 = t_0 + \frac{t_0}{C}, \quad t_2 = t_0 + \frac{R_2}{C}$ 

Une approach would be to use the measured ranges and adjust the times. In the simplified figure above,  $\Delta t_1 = -R_1/c$  and  $\Delta t_2 = -R_2/c$ . The resulting times  $t_1 + \Delta t_1$  and  $t_1 + \Delta t_2$  would be equal and correspond to  $t_0$ . The resulting time scale, however, would be non-linear and vary with geometry (i.e., with changes in the ranges).

A second approach is to adjust the measured ranges to correspond to one of the recorded times. Suppose the time at station 1 is to be used as the reference. The measured ranges, however, correspond to time  $t_0$ . Using the Taylor's expansion about  $t_0$ ;

$$R_{1}(t_{1}) = F_{1}(t_{0}) + R_{1}(t_{0})(t_{1} - t_{0}) + \frac{1}{2}F_{1}(t_{0})(t_{1} - t_{0})^{2} + \dots$$
 (2)

bsing the relation between  $t_1$  and  $t_0$  above;

$$F_{1}(t_{1}) = F_{1}(t_{0}) + F_{1}(t_{0}) \frac{F_{1}(t_{0})}{CC} + \frac{1}{2} \dot{F}_{1}(t_{0}) \frac{F_{1}^{2}(t_{0})}{C^{2}} + \dots$$
(3)

(4)

(5)

(6)

J-2

For the second range;

$$R_{2}(t_{1}) = P_{2}(t_{0}) + R_{2}(t_{0})(t_{1}-t_{0}) + \frac{1}{2}R_{2}(t_{0})(t_{1}-t_{0})^{2} + \dots$$

$$R_{2}(t_{1}) = R_{2}(t_{0}) + \frac{1}{R_{2}}(t_{0}) \frac{R_{1}(t_{0})}{C} + \frac{1}{2}R_{2}(t_{0}) \frac{R_{1}^{2}(t_{0})}{C^{2}} + \dots$$

The range adjustments are:

$$\Delta R_{1} = \frac{R_{1}R_{1}}{C} + \frac{R_{1}R_{1}^{2}}{2C^{2}} + \cdots$$
$$\Delta R_{2} = \frac{R_{2}R_{1}}{C} + \frac{R_{2}R_{1}^{2}}{2C^{2}} + \cdots$$

In general.

$$\Delta R = \frac{R_1 R_1}{C} + \frac{R_1 R_1^2}{2C^2} + \dots$$

1

The acceleration term will always be less than 0.002 meters (in magnitude): since  $\Delta R_{MAX}^{(2)} = \begin{cases} \frac{R_{MAX}}{R_{MAX}} & \frac{R_{MAX}^2}{2C^2} \end{cases}$ - 10C N.M. sutellite:  $R_{MAX} \cong 2.5 \times 10^6$  meters R_{MAX} ≅ 50 m/sec² G ≅ 3 x 10⁸ m/sec

 $\Delta R_{MAX}^{(2)} \cong 0.002$  meters

which may be neglected with respect to  $\Delta R^{(1)}$ . Thus the final range

.(?)

(8)

(9)

3-3

adjustments are:

So,

 $\Delta E_{1} = \frac{R_{1}R_{1}}{C}$   $\Delta E_{1} = \frac{R_{1}R_{1}}{C}$   $\Delta E_{1} = \frac{R_{1}R_{1}}{C}$ 

#### APPENDIX K

## TRAJECTORY FITTING TO POSITION AND/OR VELOCITY DATA

Injection vectors  $(\overline{R}_0, \overline{V}_0)$  are initial conditions at some time  $(t_0)$  of a vehicle in freefall. When  $\overline{R}_0$ ,  $\overline{V}_0$  are known as a function of position and velocity and all accelerations affecting the vehicle's motion are sufficiently well behaved as to be representable as functions of position and velocity also, then the position, velocity, and these accelerations can be predicted as functions of time (t.). Trajectory fitting consists of establishing adjustments to  $\overline{R}_0, \overline{V}_0$  such that the trajectory computed from these injection vectors will satisfy some fitting criterion. A least-squares fit would be satisfied when the sum of the squares of the difference between computed and measured data (i.e., residuals) at each point along the trajectory was minimum.

To formulate a least-squares trajectory-fitting procedure, assume that the cartesian position and velocity vectors  $(\overline{R}_0, \overline{V}_0)$  of the vehicle are known at points along the trajectory. A set of condition equations can then be formed to give

<u>x6</u> 000	∆x°	+	<u>X6</u> 0 26	_{ΆΫ} ο	· <b>†</b>	<u>ðx</u> ðz	∆z _o	+	<u>. X0</u> X0	∆x°	<b>+</b>	<u>3x</u> ^{XY} o	ΔŸο	+ <u>3x</u> 3z	- <u>\</u>	<b>u</b> ľ	(X _m -	- X _c )	[,] ,,,,,,,,,,,,,,,,,,,,,,,,,,,	ر ان ان ان ان ان ان ان ان ان ان ان ان ان
<u>3X</u> 0X	۵x°	+	0 ²⁶	∆y _o	+	•		•	•		-	•	-	•		•	Ϋ́,Ϋ́,	- Y )	) = √	¢,
<u>82</u> 82	∿x°	+	1-		•				•									ţ	ł	(าะ)
<u>X6</u> X5	ΔX°	*	t													-	-	1	<b>ا</b> بر رو	
<u>ý:</u> X6	۲ ^۲ ο	ŧ.	ı	-								-				-	-	1	ı	،
<u>87</u> 000	∑.∆X _o	+	• \			•			ו				¢	87 87	∆Z ¢	- (	2,-	ż_;)	° 2	
where  $(X_m - X_c)$ , etc. are discrepancy vectors  $\xi$  and  $x_X$ ,  $v_X$ , etc. are the residuals to be minimized,

or in matrix form

 $M_{\Delta} = \zeta = v$ 

Q_{1²}

Q3.

Q1 92 M Q3 Q4

two-body partial derivatives of vehicle's
p sition and velocity with respect to the
injection vectors, R and V
o

$$\begin{bmatrix} \frac{\partial X}{\partial X_{0}} & \frac{\partial X}{\partial Y_{0}} & \frac{\partial X}{\partial Z_{0}} \\ \frac{\partial Y}{\partial X_{0}} & \frac{\partial Y}{\partial Y_{0}} & \frac{\partial Y}{\partial Z_{0}} \\ \frac{\partial Y}{\partial X_{0}} & \frac{\partial Y}{\partial Y_{0}} & \frac{\partial Y}{\partial Z_{0}} \\ \frac{\partial Z}{\partial X_{0}} & \frac{\partial Z}{\partial Y_{0}} & \frac{\partial Z}{\partial Z_{0}} \\ \frac{\partial Z}{\partial X_{0}} & \frac{\partial Z}{\partial Y_{0}} & \frac{\partial Z}{\partial Z_{0}} \\ \frac{\partial Z}{\partial X_{0}} & \frac{\partial X}{\partial Y_{0}} & \frac{\partial X}{\partial Z_{0}} \\ \frac{\partial Z}{\partial X_{0}} & \frac{\partial X}{\partial Y_{0}} & \frac{\partial X}{\partial Z_{0}} \\ \frac{\partial X}{\partial X_{0}} & \frac{\partial X}{\partial Y_{0}} & \frac{\partial X}{\partial Z_{0}} \\ \frac{\partial X}{\partial X_{0}} & \frac{\partial X}{\partial Y_{0}} & \frac{\partial X}{\partial Z_{0}} \\ \frac{\partial X}{\partial X_{0}} & \frac{\partial X}{\partial Y_{0}} & \frac{\partial X}{\partial Z_{0}} \\ \frac{\partial X}{\partial X_{0}} & \frac{\partial X}{\partial Y_{0}} & \frac{\partial X}{\partial Z_{0}} \\ \frac{\partial X}{\partial X_{0}} & \frac{\partial X}{\partial Y_{0}} & \frac{\partial X}{\partial Z_{0}} \\ \frac{\partial X}{\partial X_{0}} & \frac{\partial X}{\partial Y_{0}} & \frac{\partial X}{\partial Z_{0}} \\ \frac{\partial X}{\partial X_{0}} & \frac{\partial X}{\partial Y_{0}} & \frac{\partial X}{\partial Z_{0}} \\ \frac{\partial Z}{\partial X_{0}} & \frac{\partial X}{\partial Y_{0}} & \frac{\partial X}{\partial Z_{0}} \\ \frac{\partial Z}{\partial X_{0}} & \frac{\partial Z}{\partial Y_{0}} & \frac{\partial Z}{\partial Z_{0}} \\ \frac{\partial Z}{\partial X_{0}} & \frac{\partial Z}{\partial Z_{0}} \\ \frac{\partial Z}{\partial Z_{0}} & \frac{\partial Z}{\partial$$

٥x

<u>ک</u>۲ م

ΔZ

Δx

ΔY

adjustments to injection vectors

(5)

(4)

(2)

(3)

K-2

6

$$\chi = \begin{bmatrix} \overline{R}_{m} - \overline{R}_{c} \\ \overline{V}_{m} - \overline{V}_{c} \end{bmatrix} = \begin{bmatrix} \overline{R}_{m} - \overline{R}_{c} \\ \overline{V}_{m} - \overline{V}_{c} \\ \overline{V}_{m} - \overline{V}_{c} \end{bmatrix} = \frac{1}{2m - -c} = \text{discrepancy vectors of position} \quad (6 \text{ and velocity})$$

$$\chi_{n} - \chi_{c} \\ \chi_{n} - \chi_{c} \\ \chi_{n} - \chi_{c} \\ \overline{V}_{n} - \overline{V}_{c} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_{n} \\ \overline{V}_$$

 $\overline{R}_{n}$ ,  $\overline{V}_{m}$  = measured position and velocity vectors of the vehicle, respectively, at time t

 $\overline{R}_{c}$ ,  $\overline{V}_{c}$  = predicted position and velocity vectors of the vehicle, respectively, at time t.

### FITTING TO POSITION AND VELOCITY VECTORS

Consider the least squares solution for the injection vector adjustments where unity weighting is assumed, then the solution based on (n) vehicle positions and velocities has the form

$$(1x6) \frac{(6x6)}{\Delta} = (\frac{6x1}{2}) \frac{(6x1)}{[1+1]} \frac{n}{2} (M^{T} \zeta)_{1}$$
(7)

A weighted least, squares solution will be given by

$$\Delta = \left[ \sum_{i=1}^{n} (\mathbf{M}^{\mathrm{T}} \sigma^{-1} \mathbf{M})_{i} \right]^{-1} \sum_{i=1}^{n} (\mathbf{M}^{\mathrm{T}} \sigma^{-1} \boldsymbol{\xi})$$

where

_____

$$\sigma = \lfloor \frac{1}{2} \left( e^{T} \sigma_{0}^{-1} b \right)_{j} \right]$$

* Refer to appendix L. "Least Squares Adjustment."

X-3

(8)

covariance matrix (9); of vehicle position and velocity vectors

(10)

(11)

 $\sigma_{oj}^{-1}$  = inverse_variance of jth-observation used in computing the R V vectors at time t

σχχ

σχΥ

σ_{XZ}

σ_{YZ}

2

 $\boldsymbol{\sigma}_{Z}$ 

σXZ

σχγ

σ_{ŹY}

σŶ

σ_{ZX}

σ_{ΥΧ} σ_Υ

 $B^{T}$  = matrix of partial derivatives of the observations with respect to the  $R_{m}^{T}$  V vectors at time t.

As an example, when ranging is an observation used in computing  $\overline{R}_m^{}, \overline{V}_m^{},$  then

and  $\sigma_{c}^{-1} = \frac{1}{\sigma_{c}^{2}} \frac{\partial R}{\partial Y} \frac{\partial R}{\partial Z} \frac{\partial R}{\partial X} \frac{\partial R}{\partial Y} \frac{\partial R}{\partial Z}$ 

CUBIC CORPORATION

#### FITTING TO POSITION OR VELOCITY VECTORS

If the trajectory is to be adjusted only to measured positions or only velocity components, then for a position fit, the M matrix of equations (7) and (8) has the form

(3x6) $M = [G_1 - G_2]$  (12)

and for a velocity fit -

- (3x6) M ≈ 1€3 €4]

K-4:

(13)

**(** >

Constraining the adjustment of injection vectors to only the  $\overline{R}_{o}$  elements or  $\overline{V}_{o}$  will reduce the M matrix to

$$M = Q_1$$

for R position adjustent and

 $(3x3) M = Q_{\Delta}$ 

for an adjustment to only  $\overline{V}_{o}$ .

when the observational data or the adjustment is constrained, the weighting matrix and the discrepancy vectors must correspondingly be modified.

#### FITTING TO OBSERVATIONAL DATA

It is not essential that the cartesian coordinates of the vehicle be used in a fitting procedure. A fitting directly to observational data can be formulated by the condition equations of (1) in the form

$$\frac{\partial OBS_{1}}{\partial X_{0}} \Delta X_{0} + \frac{\partial OBS_{2}}{\partial Y_{0}} \Delta Y_{0} + \dots + \frac{\partial OBS_{1}}{\partial Z_{0}} \Delta Z_{0} - (OBS_{1} - OBS_{0}) = V_{1}$$

$$\frac{\partial OBS_{2}}{\partial X_{0}} \Delta X_{0} + \dots + \frac{\partial OBS_{1}}{\partial Z_{0}} \Delta Z_{0} - (OBS_{1} - OBS_{0}) = V_{1}$$

$$\frac{\partial OBS_{2}}{\partial X_{0}} \Delta X_{0} + \dots + \frac{\partial OBS_{1}}{\partial Z_{0}} \Delta Z_{0} - (OBS_{1} - OBS_{0}) = V_{1}$$

K-5

(16)

(14)

(15)

#### where 058 = arbitrary observation.

For example, a condition equation for a slant range observation which is to be used in adjusting  $\overline{R}_{0}$  and  $\overline{V}_{0}$  will be

 $\frac{\partial R_{1}}{\partial X} \Delta X_{0} + \frac{\partial R_{1}}{\partial Y} \Delta Y_{0} + \frac{\partial R_{1}}{\partial Z} \Delta Z_{0} + \frac{\partial R_{1}}{\partial X} \Delta X_{0} + \frac{\partial R_{1}}{\partial Y} \Delta Y_{0} + \frac{\partial R_{1}}{\partial Z} \Delta Z_{0} - (R_{1} - R_{1}) = V_{R_{1}}$ 

(17)

A system of equations similar to (17) can be formed with each range or other independent observation taken to a vehicle. Weighting the solution or constraining the adjustments follows the schemes shown above for vector fitting.

# COMMENTS REGARDING TRAJECTORY FITTING

The assumption of Mnessity implicit in the condition equations (1) is not sufficiently correct to avoid using an Aterative solution in the least aquares fitting procedure. This condition usually means that all measured data used in a fitting procedure be stored or retained for the successive iterations of the adjustment. In most problems, the amount of data used in a solution is less significant than the relative independence of the observations (i.e., the effective geometric variability of sampling).

The above methods of trajectory fitting have proven very accurate using two-body partial derivatives (for near earth trajectories) to form the condition equations of (1). Precision methods of trajectory prediction, which take into account all significant perturbative accelerations, are used to compute the discrepancy vectors (i.e., the computed  $\overline{R}_c$   $\overline{V}_c$ ). Twobody partials are representative enough to establish convergence of position

and velocity vectors to within a hundredth of a foot and a thousandth of a foot per second in three iterations for most trajectory fitting spans of up to 400 seconds of data. This does not imply that the trajectory is known to this accuracy, which is of course determined by the measured data quality and accuracy.

When the adjustments of injection vectors are in any way constrained, then it is accepted that any unsolved for adjustment will be distributed in the solution in such a way as to satisfy the imposed least-squares criterion. However, in any practical problem, not all observational biases, parameter offsets, etc., can be either anticipated or modeled adequately to allow for their solution. A natural constraining is therefore implicit in any adjustment. The problem is to define the compromise between constraining and adjusting. Over-constraining will cause an unnatural distribution of error. Over adjustment will reduce the strength of a solution by adding unknowns, which will in turn increase the amount of correlation between lements in the adjustment and result in a useless sympathetic adjustment. An evaluation of residuals over a large sampling space, combined with careful analysis of the adjustment based on experience, is the most practical way of verifying an adjustment scheme.

# APPENDIX L

#### LEAST SQUARES ADJUSTMENTS

Observations refer to quantities measured directly by some equipment. Paramèters are computed from observations. An example of independent observations would be three ranges measured to some vehicle when the ranging equipment are located at different sites. The cartesian XYZ coordinates of the vehicle would be parameters which could be computed from the independent observations.

Any observation will consist of the true value and some aggregation of error terms. Error terms will include noise, cyclic, and bias. Errors are grouped into categories customarily based on their frequency. As a matter of definition, cyclic errors are perturbations in the data with a time occurrence period greater than 10 and less than 100 seconds. Noise will be considered as spurious data with period less than 10 seconds. Biases are essentially constant or can be represented by some analytic form composed of constant terms. A measured observation could be expressed mathematically by

(1)

 $U_{0} = U_{T} + \Delta U_{0} + v$ 

where

- U = measured observation
- $v_{\rm T}$  = true value
- $\Delta U_{o}$  = aggregation of blases
  - = residual (noise and cyclic error)

Similarly, a calculated approximation to the observation is formed by

$$\mathbf{U}_{\mathbf{C}} \cdot \mathbf{U}_{\mathbf{T}} \cdot \Delta \mathbf{U}_{\mathbf{C}}$$

where

 $U_C$  = approximation to  $U_T$ 

 $\Delta U_{\hat{C}}$  - unknown adjustment to  $U_{\hat{C}}$  due to approximations

Equations (1) and (2) can be differenced to form the condition equation

(3)

-(4)

$$\Delta U_{0,\frac{n}{2}} \Delta U_{C} + v = (U_{0,-} - U_{C}) + \varepsilon$$

where E discrepancy vector

Equation (3) may not be amonable to solution if terms higher than the first degree are carried. The equation, however, can be linearized by expanding it 'n a Taylor's series and deleting all second and higher power terms. Expanding equation (3) by taking partials with respect to each free var. able gives

$$\Sigma \xrightarrow{U_0}_{U_0} \Delta b + \Sigma \xrightarrow{U_0}_{AP} \Delta P + \dots + \xi$$

where

b part and envery express of the observations with respect to observational biases

P = partial derivatives of the observations with respect to each free parameter adjustment

I hat is,  $\mathbb{L} \mathfrak{V}_{\mathbb{C}}$  and  $\mathbb{A} \mathfrak{V}_{\mathbb{C}}$  are assumed to have the form:



Δb 🛫 observational bias adjustments:

ΔP = parameter adjustments

As a matter of convenience, equation (4) can be written in matrix  $\frac{1}{2}$ 

notation, fthus, 🕤



(5)

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In order to simplify the general representation of the solution for adjustments, equation (5) is further reduced to yield

 $M_{\Delta} = 5$ where 3x(n+m)  $M_{\Delta} = 5$   $(n+m)x^{2}$   $\Delta = \frac{(n+m)x^{2}}{\Delta b}$ 

A line trized condution equation similar to (4) can be formed for each observation which is to anter into a solution. When more independent observations exist than unknowns in the solution, the assemblage of condition equations must be solved to satisfy some statistical or vonvergence criterion. Assaiming in overdetermined set of condition equations exist, then the composite set are expressed as



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It is assumed initially that the system of equations (7) will remain linear over the sampling space. The condition equations are also approximations in that second and higher order derivative terms are deleted from the expansion in equation (4). When the first order approximations of derivatives are not sufficiently representative, it becomes necessary to iterate the solution to equation (7). In the iterative procedure, computed adjustivents are sequenced, added to the initial estimates of the parameters and the observations.

To obtain a solution for the system of equations given by (7), some criterion must be established. A general least squares solution can be derived from equation (7) and the multivariate normal distribution function for a set of statistically independent observations. The multivariate probability density for statistically independent observations is given by

$$r(r_1, r_2, \dots, r_5) = \frac{5}{1 + 1} \frac{1}{\sqrt{2\pi}(\sigma_{y_1})} \exp^{-\frac{1}{2}} \left(\frac{r - \tilde{r}}{\sigma_{r_1}}\right)^2$$
 (9)

(8)

:(7)



where

. sample variance

From equation (10) it is seen that the solution which maximizes the density function (9) is the solution which makes the weighted sum of the squares of the residuals a minimum, where the weighting is the inverse variance of the observations.

with the matrix of observational variance given by equation (12), then from the two equations in two unknowns, V and  $\Delta$ , namely

and

 $y^{\mathrm{T}} \sigma^{-1} v = G$ 

V + ≦∆ - 12 = C

a solution for  $\Delta$  is given by

 $\Delta = \left[ \zeta^{T} \sigma^{-1} \zeta \right]^{-1} \zeta^{T} \sigma^{-1} \varepsilon$ 

Equation (14) is a general form ... the weighted least squares adjustment. A common form of the solution is that where unity weighting is assumed. Under the conditions of unity weighting, the solution reduces to

ε = ξ₂ ι ι τ₅

where

$$\mathbf{M}_{1}^{\mathrm{T}} = \left[\mathbf{M}_{1}^{\mathrm{T}}, \mathbf{M}_{2}^{\mathrm{T}}, \ldots, \mathbf{M}_{3}^{\mathrm{T}}\right]$$

(16)

(15)

(14)

(17)

* See pages 112-112 "FCS Eats Fechnical Report No. 39," by D. C. Brown, 20 August 1957.

It can also be shown that when the minimization condition specified by equation (10) is matisfied, then the accuracy of the final adjustments to the observations and parameters will be given by the matrix of covariance given by

(18)

For the case where the parameters being adjusted are the cartesian coordinates of some vehicle, then  $N^{\pm 1}$  has the form

 $N^{-1} = [Q^T : \sigma^{-1} Q]^{-1}$ 

 	σ ² χ	σ XY-	σxz	
N ^{−1} =	σΊΧ	2 2 7	JAN STREET	matrix of variance and covariance of the adjustment
-	σΖΧ	σΖΥ	$\sigma_{\rm Z}^2$	19) - 55-57 + 21-1 5- 5-3

The square roots of the diagonal elements of the inverse normal equations given by (18) are the projections of the error volume on the axis of the respective coordinate axis being considered and are customarily considered the standard deviations of the solution components. The covariance matrix (18) therefore defines the solution distribution when an overdetermined set of observations have been used in the solution adjustment.

 then i stable solution may not be possible. The adjustment may even satisfy the residual minimization criterion over some limited sampling space. The end condition is that the minimum criterion be satisfied over the entire sample space, which should in turn be adequate to insure validity of results.

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# APPENDIX M

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NUMERICAL INTEGRATION . . . In the most elementary two-body trajectory predictions, it is possible to develop and use a closed analytic form of the prediction equations. When precise trajectories are to be computed, all accelerations, including perturbation terms such as aerodynamic drag and lift, earth's asymmetric gravity field, etc., must be integrated. Closed form analytic expressions which describe a body's motion in a complex perturbation environment do not exist. The nature of perturbations usually dictates that they be represented in a series form which in turn will not have explicit integrals. Successive numerical approximations of numerical integrations therefore are conventionally used to evaluate at least some portion of the dynamic equation, used in precise trajectory computations.

There are no absolutely preferred methods of performing numerical integration. The method used is usually specified by the characteristics of the functions being evaluated and the associated available information which may aid the solution. A popular numerical integration procedure used in trajectory prediction computations is that termed Runge -Kurta - Gill Linear Lifferential Solver. This method has been used and tested, but is not described herein.

in practical applications where the high-order derivative is assumed linear, it was demonstrated that equivalent results could be achieved by a

I "Mathematical Methods for Digital Computers," A. Ralston, H. Will, published by John Writy and Sons, Inc. New York, 1960, pages 110-126

M - 1

less involved procedure based on expanding the dynamic function in a Taylor's series about an initial point. Successively incrementing and re-establishing initial conditions of the expansion yields the desired integration. Hence, the dynamic equations are written in the power series;

$$S_{1} = S_{0} + V_{0} t_{1} + \frac{a_{0} t_{1}^{2}}{2} + \frac{a_{0} t_{1}^{3}}{6} + \dots$$
(1)

$$V_1 = V_0 + a_0 t_1 + \frac{a_0 v_1}{2} + \dots$$
 (2)

where 
$$S_{0}$$
,  $V_{0}$ ,  $a_{0}$ ,  $a_{0}$  = the initial position, velocity,  
acceleration, and accelerosity at  
time t = 0.

The position and velocity at some later time to will be given by

$$\begin{aligned} \mathbf{x}_{2} &= \mathbf{y}_{1} + \mathbf{y}_{1} \mathbf{t}_{2} + \frac{\mathbf{a}_{1} \mathbf{t}_{2}^{2}}{2} + \frac{\mathbf{a}_{1} \mathbf{t}_{2}^{3}}{6} + \dots \end{aligned} \tag{3}$$

and so on,.

then the above method is used to perform numerical integration of the dynamic equations of a vehicle, it is assumed that the acceleration and at least the accelerosity term (i.e., rate of change of acceleration) can be evaluated at each initial position. Fositions and velocities are carried forward in the sequential computation. In simulations where thrusts are applied to the vehicle which are not predictable from the environment (predictable accelerations are gravity, drag, etc.), then these terms must be incremented and carried forward in the computation of position and velocity.

<u>RECTIFICATION AND PREDICTION INTERVALS</u>... The rectification interval is the time cyer which a prediction is made before initial conditions are re-established. Prediction interval is the total time, over which a prediction is to be carried.





# From figure M-1 the rectification and prediction intervals are, respectively

$$H = (t_{i+1} - t_i)$$
 (5)

$$PI = (t_n - t_n)_{i=1}$$
(6)

$$RI PI/n$$
(7)

where n - the number of time segments used to form the prediction interval

M-3

The equation of motion given as equations (1) and (2) showe describe the physical environment over only a limited region, thus, there is a requirement to rectify the prediction equations frequently. Accuracy tolerances and the manner in which the equations of motion are used will regulate the selection

of a rectification interval. For example, when the Encke's method of prediction is used (i.e., numerical integration of perturbation terms only and analytic closed for a computation of reference trajectory), the acceleration and higher order terms are small and the rectification interval can be increased with little degradation in accuracy.

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#### APPENDIX N

#### ENCKE'S AND COWELL'S METHODS OF TRAJECTORY PREDICTION

Consider the total accelerations acting on a vehicle which is not under powered flight to be composed of a primary term with a summation of generally lesser perturbation term; hence,

$$\overline{A} = \overline{5} + \sum \overline{5}_p$$

where  $\underline{}$  A = components of total acceleration

 $\tilde{G}$  = principal components of acceleration which are due to the earth's symmetric mass  $\sum_{\bar{J}_p}$  = perturbative accelerations due to earth's asymmetric mass distribution, atmospheric drag, aerodynamic lift, etc.

To preserve continuity, the components of acceleration are taken to be projected along the XYZ axes of an inertial coordinate system which is coincident with the equatorial earth-fixed coordinates at epoch (i.e., the  $X_{EQ}$  axis in the equatorial plane through the earth's center of mass and the Greenwich meridian,  $X_{EQ}$  axis in the equatorial plane and  $90^{\circ}$ counterclockwise from  $X_{EQ}$ , and  $Z_{EQ}$  axis along the polar rotational axis).

It the accelerations given by equation (1' can be predicted as a function of time and position, and the position and velocity vectors of the vehicle are known at an initial time t, then the trajectory can be computed as a function of time. It should be remembered that initial considerations and the dynamics are assumed known.

(1)

CLEIC CORPCHATICL

ENCKE'S METHUE . . . The method of predicting a reference trajectory based on two-body motion and then adding adjustments computed by numerically integrating perturbation terms is referred to as Encke's.

A technique similar to Encke's has been developed and tested. The peculiarities of the technique are described in the following. (See figure N-1.)



Encke's Reference Orbitswith Perturbations

If  $\overline{R}_{OO}$  are the position and velocity vectors expressed in inertial coordinates at epoch time to and the value of U of equation (1) (with the associate semination axis of the earth) is used to define the canonical units of length and time, then two-body position and velocity, predictions at time to are given by

(2)

(3)

$$\overline{V}_{T} = \overline{V}_{0}^{T} + \overline{V}_{0} g_{0}$$
$$\overline{V}_{T} = \overline{R}_{0}^{T} + \overline{V}_{0} g$$

where 1, 8, 1, g = two-body integration constants

Refer to appendix 0. Two-Body Trajectory Prediction.

The actual position and velocity vectors at  $\boldsymbol{t}_1$  will now be

$$\overline{\overline{L}}_{\overline{y}} = \overline{\overline{R}}_{T} + \Delta \overline{\overline{R}}$$

$$(4)$$

$$\overline{\overline{V}}_{x} = \overline{\overline{V}}_{T} + \Delta \overline{\overline{V}}$$

$$(5)$$

where  $\Delta \overline{k}$ ,  $\Delta \overline{V}$  = adjustments due to perturbations.

en the  $\overline{R}$ ,  $\overline{V}$ , are initial or rectified points along the trajectory, then

$$\Delta \bar{R} = \frac{\left[\frac{2}{p_{c}}\right]_{3}t^{2} + \left[\frac{2}{p_{o}}\right]_{3}t^{3} + \dots + \frac{1}{6}$$
(6)

$$\Delta \overline{\mathbf{v}} = \left( \Sigma_{\overline{\mathbf{u}}}_{\mathbf{p}_{0}} \right) \Delta t + \left( \frac{\Sigma_{\mathbf{u}}_{\mathbf{p}_{0}}}{2} \right) \Delta t^{2} + \dots$$
(7)

Free 
$$\Sigma_{\overline{G}} = \text{perturbative accelerations at } \overline{R}_{0}$$
  
 $\Sigma_{\overline{G}}^{2^{O}} \simeq \frac{\Sigma_{\overline{G}}}{P_{1}} - \frac{\Sigma_{\overline{G}}}{\Delta t}$   
 $\Sigma_{\overline{G}}^{2}_{P_{1}} = \text{perturbative accelerations at } \overline{R}_{1}$ 
(8)

 $\Delta t = the rectification interval$  $\Delta t = t_1 - t_2$ 

because all perturbation accelerations are a function of position and velocity, the  $\overline{E_0V}_0$  are used to compute  $\overline{-G_0}_0$  and correspondingly  $\overline{P}$   $\overline{V}_0$ are used to compute  $\overline{\Sigma G_0}_0$ . The assumption of linearity in  $\overline{\Sigma G_0}_0$  and that higher order terms in the series of (6) and (7, are negligible will cause error build up. How much error occurs is related to the rectification interval. Results of  $\overline{\Phi}$  simulation which demonstrates the influence of rectification interval are shown on figure. N-3 and N-4. It can be seen

N-8

that for a  $\Delta t$  of 20 sec which is larger than that used in the SECOR orbital mode, the total expected divergence should be less than one meter.

<u>COWELTES METHOD</u>... Numerical integration of the total accelerations and velocities is identified as Cowell's method of trajectory prediction. One variation of Cowell's method which has been developed and tested is presented here. Starting with initial composite accelerations given by equation (1) and the initial position and velocity vectors,  $\overline{R_0V_0}$ , we have

$$\vec{R}_{1} = \vec{R}_{0} + \vec{v}_{0} \Delta t + \left(\frac{\vec{u}_{0} + \vec{\Sigma} \vec{c}_{p}}{2}\right) \Delta t^{2} + \left(\frac{\vec{u}_{0} + \vec{\Sigma} \vec{c}_{p}}{6}\right) \Delta t^{3} + \dots \quad (9)$$

$$\vec{v}_{1} = \vec{v}_{0} + \left(\vec{u}_{0} + \vec{\Sigma} \vec{c}_{p}\right) \Delta t + \left(\frac{\vec{v}_{0} + \vec{\Sigma} \vec{c}_{p}}{2}\right) \Delta t^{2} + \dots \quad (10)$$
where  $\vec{J}_{0} = \frac{\vec{u}_{1} - \vec{u}_{0}}{\Delta t^{2}}$ 

The rate of change of  $(\overline{u}_{0} + \sum \overline{u}_{p_{0}})$  in equations (9, and (10) is computed in the same fashion as shown in equation (8) above. In the technique discussed here, the first estimates of  $\overline{v}_{1}\overline{v}_{1}$  used to compute  $(\overline{u}_{1} + \sum \overline{u}_{p_{1}})$ are obtained from a two-body prediction. An iteration of the total numerical integration would suffice. When  $\overline{u}_{1}\overline{v}_{1}$  have been computed as described above,  $\overline{u}_{1}\overline{v}_{1}$  become initial conditions for the next sequential prediction and so on. Derivative terms above  $\overline{v}_{0}$  have been deleted from the above power series.

<u>COMPARISON OF ENCKE'S. COWELL'S. AND TWC-BODY METHOD OF TRAJECTORY</u> <u>rikEDICTIONS</u>.... The advantage of one prediction method over another is of interest only in that limits of applicability of each are defined by comparison. It is obvious from the above formulation that Cowell's

method is subject to numerical approximation error to a greater extent than is Encke's. This require to the large magnitude of the terms carried in the numerical integration and the lack of physical

representation of terms over large time intervals. However, when a wehicle is in powored flight, the reference trajectory computed by Encke's method will be of little use and numerical integration of total accelerations, including thrusts, is preferable.

T' D-BODY METHOD, . . . In some applications, simple two-body predictions may be more representative than those given by either Cowell's or Encke's methods, both of which require numerical integration. If sufficient care is not taken to perform numerical integration accurately and to use reasonable rectification intervals, then the build up of error will exceed the total effect of perturbations and uscless computation results. Because accuracy, computing time, and rectification interval are

directly related in trajectory computations, simulations, were performed to give quantitative comparison of the three methods mentioned above. Actual measured data from two distinctly different type trajectories was

used to compute trajectories for the comparison. A nearly vertical trajectory with apogec of approximately 400 miles (obtained from Thor launchings at Johnston Island nuclear tests of 1962) and a nearly circular orbit with apogee of approximately 460 miles (USA -2 Geodetic SECOR satellite of 1964) were used in the simulation. Figure N-2 is a plot of the range and elevation angles versus time for the two vehicles.

The satellite orbit closely, follows lines of equal gravity while the Thor trejectory experiences a dramatic variation in gravity.



Atmospheric drag is also minimized for the satellite and conversely will become a predominant deceleration for the Thor during reentry. Figures N-3 through 6 illustrate the build up of error due entirely to analytic approximations using the Encke and Cowell methods of prediction. The amount of error is controlled by the rectification interval, or the interval over which the prediction is carried without re-establishing initial conditions. To avoid masking the prediction errors with other sources of error such as tracking equipment, gravity model, atmospheric drag, etc., the measured data was used in a least square fitting procedure to establish injection vectors. A test trajectory was then computed using a rectification interval of one second. The predicted and measured trajectories had agreement of about ±20 feet in each position component, over the 800 second span used in the simulation.

After the "standard" had been computed, a set of predictions were made varying only the rectification interval. The separation of the predicted trajectory from the "standard" was attributed to analytic approximations which are inherent in the numerical integration schemes. hectification intervals were reduced to 2.1 seconds and no separation from the "standard" was encountered. It was necessary to develop a veryaccurate solution of Kepler's equation of mean metion before the errors could be reduced to the values shown for Encke's method and the two-body predictions.

A review of Figures N-3 through N-8 demonstrates that Encke's method produced significantly better accuracies than the Gowell's. Computing time for the two procedures is about equal due to the use of two-body in both schemes. Computing time per rectification could be reduced in the

N-7

#### CUBIC CORPGEATION

Cowell's method; however, this method would require many more rectifications to achieve equivalent results. Comparison of Encke's and Cowell's results with the two-body predictions indicates that large rectification intervals can reduce accuracy more than the total effect of perturbations. For example, if a 100-second rectification interval is used, the arithmetic error after 800 seconds will be 58' and 7400' for Encke's and Cowell's, respectively, and 9600' of total perturbation offset for the USA-2 satellite orbit. With the Thor trajectory after only 500 seconds of prediction with a 100-second rectification interval. Encke's and Cowell's had errors of 38' and 9000', respectively, and 4700' of perturbation offset.

The problem of analytic approximation error quickly becomes the dominant consideration in predictions. When orbits are to be computed over several day periods, care must be exercised if results are to bear any resemblance to actual conditions.

Time/scales on all figures are in seconds with respect to an arbitrary epoch time, which is taken for convenience at some time in freefall. The "effect of perturbations" shown on Figures N-7 and N-8 is simply the offset difference between the two-body trajectory and the precise trajectory computed by Encke's method carrying all significant perturbations.' Perturbations included the first nine zonal harmonics of the earth's gravity and atmospheric drag and lift. The effect of drag and lift was undetectable over 800 seconds of the USA-2 satellite orbit.

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# RECTIFICATION



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#### APFENDIX

# TWO-BODY TRAJECTORY PREDICTION. FARTIAL DERIVATIVES. SOLUTION OF

# KETLERS LOUATION, AND INFETTAL TO LOUATORIAL ROTATIONS

TRAJECTORY PREDICTION . . . If the position and velocity vectors are known at one time for a body in freehall, a "closed expression" can be developed to predict the two-body motion of the body versus time. When all quantities are expressed in canonical units and the position and velocity vectors are expressed in inertial coordinates (i.e., with origin at the dynamic center, which is the center of mass of the earth for near earth trajectories and orbits), predicted positions and velocities for some time, t, following epoch (time t_) are given by

$$\overline{R} = \overline{\Gamma} \overline{R}_{0} + g \overline{V}_{0}$$
(1)  
$$\overline{V} = \overline{\Gamma} \overline{R}_{0} + g \overline{V}$$
(2)

where

 $\overline{N_0}$ ,  $\overline{V_0}$  = the position and velocity vectors at injection, respectively

$$f = a(\cos \Delta t - \beta_{c})/T_{c}$$
(3)

$$g = a^{3/2} (\sin \Delta 5 + \delta_{2}, (4))$$

$$i = -u^{3/2} (\sin \Delta k) / (1.F)$$
 (5)

$$r = a(\cos \Delta F - p)/E$$
(6)

"Position, Velocit?: a, Sphemerides, Referred to the Dynamical Center," Astrodynamical Report No. 7, by Samual Herrick, Dept. of Astronomy, University of California of Los Angeles and Aeronutronics, July, 1960. EFliptic motion assumed in this set of equations

$$F_{n} = (\bar{h}_{0} + \bar{h}_{0})^{\frac{1}{2}}$$
(7)  

$$V_{0}^{-2} = (\bar{V}_{0} + \bar{V}_{0})$$
(8)  

$$1/u = 2/F_{0} - V_{0}^{-2}$$
(9)  

$$\delta_{c} = (\bar{h}_{0} + \bar{V}_{0})/a^{\frac{1}{2}} = e \sin t_{0}$$
(10)  

$$\beta_{0} = 1 - F_{0}/u = e \cos E_{0}$$
(11)  

$$E_{0} = \tan^{-1} (h_{0}/F_{0}) \text{ with quadrant test}$$
(12)  

$$E_{0} = eccentric anomaly at time t_{0}$$
(12)  

$$E_{0} = eccentric anomaly at time t_{0}$$
(13)  

$$1/a^{3/2} = n = mean motion$$
(14)  

$$\overline{h}_{0} = \begin{bmatrix} X_{0} \\ Y_{0} \\ Z_{0} \end{bmatrix}$$

$$\overline{V}_{0} = \begin{bmatrix} X_{0} \\ Y_{0} \\ Z_{0} \end{bmatrix}$$
(15)  

$$\Delta t = E - E_{0}$$
(16)  

$$\mu = eccentric anomaly at time t$$

$$F = a(1 - p)$$
(17)

$$p^{i} = e \cos E$$
 (18)

$$\delta = e \sin \tilde{E}$$
 (19)

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Unce K and V are computed by equations (1) and (2) they can be transrormed into any desired coordinate system. The above equations are valid in an inertial reference frame. (1) • ligure (-1.)



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# CUBIC ECRECHATION

SOLUTION OF KEPLER'S FOUATION FOR AL . . . when  $(t - t_0)$  is given, ' an extremely efficient iteration (less than six iterations for accuracies of ±0.1 µ radian) can be set up to solve the transcendental function called Kepler's equation of two-body motion; namely,

$$n(t - t_{c}) = M - M_{c} = (E - E_{c}) - e \sin E + e \sin E_{c}$$
 (20)

(21)

(23)

$$\Delta M = \Delta E = e \sin (E_{a} + \Delta E) +$$

where M is the mean anomaly.

A common form of the solution for AE given in the literature is to Iterate equation 21 where the first approximation of AE is given by

$$\Delta E_1 = \Delta M + S_0 + e \sin (E_0 + \Delta M)$$
(22)

and succeeding iterations take the form

$$\Delta E_{i+1} = \Delta M + \delta_0 + e \sin_1(E_0 + \Delta \Sigma_i)$$

Convergence of the iteration is established when

$$\Delta E_{i+1} - \Delta E_i \gg F \approx 0$$
 (24)

where K = a precomputed accuracy limit.

The results of the such classic iteration are shown on figure 0-2. Differences of the  $\Delta E_i$  and the final  $\Delta \Xi$  are plotted versus the number of iterations. The solution oscillates systematically and converges slowly to a fixed value. In the example shown on figure 0-2, more than 170 iterations were required for  $h = 1.10^{-7}$ .
CUBIC CORPORATION 1.5 1 Ï. + E ...... 4 ŀ., NOT REPRODUCIBLE 20 Iterelive Solution Kepler e Bouation 1 1 J. ....................... j 359-14G Ŵ. N J To the source to the 0.24 A State of the

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It was observed that the successive iterations of equation (23) were opposite in sign and therefore susceptible to dampening. In order to make the solution given by equation (23) useful, an alternate form of the solution was tried; mamely,

$$\Delta E_{i+1} = \Delta M - \delta_0 + e \sin (E_0 + (\Delta E_{i-1} + \Delta E_1)/2)$$
(25)

For the same conditions used to test equation (23), equation (25) sadisfied the iteration convergence driterion in 5 iterations. The dampened iteration proved to be highly efficient and accurate and represents the most useful solution to Kepler's equation attempted, which has included several partial derivative techniques.

If the above set of equations are to be used in formulations where high accuracy and precision are essential (such as computing the reference orbit or trajectory in the Encké's method of predicting), then using a fixed constant for K in equation (24) can limit accuracy and make computations susceptible to truncation error in computers. The variability of  $\Delta E$  can be compensated by making K also variable in such a way as to retain proportionate accuracy of  $\Delta E$ . In order to achieve more uniform and higher accuracies from the iteration, a K-for the convergence test of equation (24) was computed as

 $K = K \Delta M$  where K = 0.000001.

The convergence test given by equation (24) now becomes

CONTINUE =  $K'' < \left| \Delta E_{i+1} - \Delta E_i \right| < K' = EXIT$ 

0~6

<u>TWO-BODY PARTIAL DERIVATIVES</u> . . . . Partial differential operators  $\nabla_i \nabla'$ , and D are defined with the following convention:

$$\nabla = \begin{bmatrix} \overline{\partial X}_{0} \\ \overline{\partial Y}_{0} \\ \overline{\partial Z}_{0} \end{bmatrix}, \quad \begin{bmatrix} \overline{\partial} \\ \overline{\partial X}_{0} \\ \overline{\partial} \\ \overline{\partial Z}_{0} \end{bmatrix}, \quad L = \begin{bmatrix} \overline{\gamma} \\ \overline{\gamma} \\ \overline{\gamma} \\ \overline{\partial} \\ \overline{\partial Z}_{0} \end{bmatrix}, \quad L = \begin{bmatrix} \overline{\gamma} \\ \overline{\gamma} \\ \overline{\gamma} \\ \overline{\gamma} \end{bmatrix}$$
(26)

Given the equations

P

 $\overline{R} = \frac{i}{\overline{R}_{o}} + \overline{V}_{o} g$  $\overline{V} = \overline{R}_{o} + \overline{V}_{o} g$ 

then the two-body partial derivatives of positon and velocity at time t with respect to injection vectors  $\overline{R}_0$   $\overline{V}_0$  at time t become

.(27)

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$$(3 \times 3)$$

$$Q_{1} = \overline{K}_{0} \sqrt{r^{T}} + rT + \overline{V}_{0} \sqrt{g^{T}}$$

$$Q_{2} = \overline{K}_{0} \sqrt{r^{T}} + rT + \overline{V}_{0} \sqrt{g^{T}}$$

$$Q_{3} = \overline{E}_{0} \sqrt{r^{T}} + rT + \overline{V}_{0} \sqrt{g^{T}}$$

$$Q_{3} = \overline{E}_{0} \sqrt{r^{T}} + rT + \overline{V}_{0} \sqrt{g^{T}}$$

$$Q_{4} = \overline{R}_{0} \sqrt{r^{T}} + rT + \overline{V}_{0} \sqrt{r} r^{T}$$

$$Q_{4} = \overline{R}_{0} \sqrt{r^{T}} + rT + rV + \overline{V}_{0} \sqrt{r} r^{T}$$

$$(28)$$

$$I = \begin{bmatrix} 3 \times 3 \\ -1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$I = \begin{bmatrix} 3 \times 6 & (3x2) & (2x6) & 3 \times 6 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$\frac{3 \times 6 & (3x2) & (2x6) & 3 \times 6 \\ r\overline{R} = tQ_{1}Q_{2}] = t\overline{K}_{0} \overline{V}_{0} r tDr D_{E} r^{T} + (rT r) r^{T}$$

$$F_{\overline{V}} = tQ_{2}Q_{4} = t\overline{R}_{c} \overline{V}_{0} r tDr D_{E} r^{T} + tr r r r r^{T}$$

$$(29)$$

where  $P_{\overline{R}}$  and  $P_{\overline{V}}$  are the two-body partials of position  $\overline{R}$  and velocity  $\overline{V}$ , with respect to both  $\overline{F}_{0}$  and  $\overline{V}_{0}$ , respectively.

Taking partials of f, g, f, and g will give

$$Df = \frac{1}{(1 - \beta_0)} \left[ D\beta_0 (f - 1) - \sin \Delta E D \Delta E \right]$$
(30)

$$Dg = (\frac{3}{2\pi}g) Da + \frac{1}{n}(\cos \beta E D\beta E - D\beta + D\delta_0)$$
 (31)

$$Df = f\left(\frac{a}{R_{0}}D_{P_{0}} + \frac{a}{R}D_{P} - \frac{3}{2}aDa + \frac{cos \Delta E}{sin \Delta E}D_{\Delta}E\right)$$
(32)

$$D_{g} = \frac{1}{(1-\beta)} \left[ D_{\beta}(g-1) - \sin \Delta E D \Delta L \right]$$
(33)

$$D_{\beta} = D_{c} + \beta D \Delta E \qquad (34)^{\circ}$$

$$D\Delta E = \frac{a}{R} \left[ Dc - Db_{0} - \frac{2}{2} \frac{n}{a} (t - t_{0}) Da \right]$$
(35)

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$$\hat{D}_{c} = \sin \Delta E b_{\beta_{0}} + \cos \Delta E \bar{D}_{\beta_{0}}$$
 (36)

$$D\beta = DD - 5 D\Delta n \qquad (37).$$

$$DD = \cos \Delta E D\beta_{o} - \sin \Delta E D\delta_{o}$$
(38)

$$D_{\beta_{0}} = \begin{bmatrix} \overline{\mu}_{\beta_{0}} \\ \overline{\mu}_{\beta_{0}} \end{bmatrix}^{2}$$

$$(39)$$

$$\overline{\sqrt{\beta_{0}}} = \frac{\sqrt{\frac{2}{R_{0}}}}{R_{0}} \qquad (40)$$

$$\overline{\gamma}'\beta_{0} = 2R_{0}\overline{V}_{0}$$
(21)

$$Db_{0} = \begin{bmatrix} \frac{1}{2} & \delta_{0} \\ 0 & \delta_{0} \end{bmatrix}$$
(42)

$$\overline{B}_{c} = \frac{\overline{\nabla}_{0}}{\mu^{2}} - \frac{\overline{B}_{0}\overline{\Gamma}_{0}}{\overline{B}_{0}^{3}}$$
(43)

$$\overline{\nabla}^{\dagger} \delta_{0} = \frac{\overline{E}_{0}}{a^{2}} - a \delta_{0} \overline{V}_{0}$$
(44)

$$D\mathbf{a} = \begin{bmatrix} \nabla^2 \mathbf{a} \\ \nabla^{-1} \mathbf{a} \end{bmatrix}$$
(45)  
$$\nabla \mathbf{a} = \frac{2\mathbf{a}^2}{R_0^3} \overline{R}_0$$
(46)

$$\overline{V}^{\prime}a = 2a^2 \,\overline{V}_{\rm c} \tag{47}$$

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INERTIAL TO EQUATORIAL ROFATIONS . . . All those equations are computed in a space fixed or inertial coordinates can be assumed to be coinorbits and trajectories, inertial coordinates can be assumed to be coincident with the equatorial coordinates at epoch time  $t_0$ . A rotation from the stationary inertial coordinates to the earth fixed equatorial coordinates is given by

$$M_{IE} = \begin{cases} cos \ \omega_e \ \Delta t & sin \ \omega_e \ \Delta t & 0 \\ \neq sin \ \omega_e \ \Delta t & cos \ \omega_e \ \Delta t & 0 \\ 0 & 0 & 1 \end{cases} = inertial to equationial (48) • rotation matrix$$

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where  $t_0 = time of epoch or injection$ t = time in trajectory

 $\Delta t = t - t_o$ 

With matrix  $M_{TE}$ , the inertial position, velocity, and partials will be rotated to equatorial by

$$\overline{\mathcal{R}}_{\mathbf{L}_{\mathbf{Q}}} = \mathbf{M}_{\mathbf{IE}} \,\overline{\mathbf{R}} \tag{49}$$

$$\overline{\overline{V}}_{EQ} = M_{IE} \overline{V} - \overline{V}_{E}$$
(50)

$$\dot{\mathbf{v}}_{\mathbf{E}} = \omega_{\mathbf{e}} \begin{bmatrix} \mathbf{v}_{\mathbf{E}\mathbf{Q}} \\ \mathbf{X}_{\mathbf{E}\mathbf{Q}} \\ \mathbf{Q} \end{bmatrix}$$
(51)

$$P_{\text{EQ}} = \begin{bmatrix} M_{\text{IE}} & M_{\text{IE}}^{\text{T}} & M_{\text{IE}} & M_{\text{IE}} & M_{\text{IE}} \\ \hline M_{\text{IE}} & Q_3 & M_{\text{IE}}^{\text{T}} & M_{\text{IE}} & M_{\text{IE}} \\ \end{bmatrix}$$
(52)

where  $\omega_{\rm c}$  = earth's angular rate

T = refers to matrix transpose.

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All equations given here for trajectory prediction are predicated on a spherical gravity field and the absence of all perturbations such as atmospheric drag, aerodynamic lift, thrusts, etc. The equations are very useful in evaluation considerations where simplicity and versatility are needed before solutions and problems can be economically simulated. Perturbations can be added to the above equations to strengthen their applicability to real problems. Frincipal attributes of these equations are their versatility, simplicity, and speed of computation on computers. The two-body partials can be used in orbit and trajectory fitting to observational data.

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#### APPENDIX P

#### NON-GRAVITATIONAL PERTURBATIONS

Let the accelerations acting on a vehicle in freefall be expressed by

 $\overline{A} = \overline{G} + \underline{Z} \ \overline{G}_{p} + \underline{Z} \ \overline{P}$ (1)

where,  $\overline{A} = \begin{bmatrix} a_x \\ a_y \\ \underline{a}_z \end{bmatrix}$  = total acceleration components  $\overline{G} = \begin{bmatrix} \overline{g}_x \\ g_y \\ g_z \end{bmatrix}$  = principal component of earth's gravity

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$$2\overline{G}_{p} = \begin{bmatrix} \mathbf{q}_{x} \\ \mathbf{q}_{y} \\ \mathbf{q}_{z} \end{bmatrix} = \text{perturbations of earth's gravity due to zonal} \\ \text{harmonics} \\ 2\overline{P} = \begin{bmatrix} \mathbf{p}_{x} \\ \mathbf{p}_{y} \\ \mathbf{p}_{z} \end{bmatrix} = \text{acceleration component due to non-gravitational} \\ \text{perturbations} \end{cases}$$

Examples of non-gravitational perturbations would be accelerations due to lift, drag, and solar radiation. As a matter of convention, the directional components are defined as being directed along the X; Y, Z axes of a right-handed orthogonal coordinate system. The reference frame used hereis an earth-centered; space-fixed inertial coordinate system.

when the vehicle is in close proximity of the earth's atmosphere and extremely long prediction intervals are not considered, then atmospheric

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lift and drag become the significant perturbative sources. Drag and lift accelerations,  $a_d$  and  $a_l$  respectively, are given by

 $a_{d} = 1/2 \rho V_{\ell}^{2} C_{d} S/m$  $a_{\ell} = 1/2 \rho V_{\ell}^{2} C_{\ell} S/m$ 

where

) m = mass of the vohicle

 $\rho = air density$ 

Vp = vehicle earth-related velocity

C_d = vehicle drag coefficient

C, = vehicle lift coefficient

S = vehicle effective cross-sectional area

A vehicle's drag coefficient is not constant, but rather a function of the vehicle's Mach speed and shape. Also, the value of the drag coefficient for different Mach speeds does not lend itself to analytical expression. Thus, a table of actual measured values of the vehicle drag coefficient versus Mach speed is required to compute acceleration due to drag. Such a table for an instrumentation pod is given in table 1-1. Once a table is provided, it is only necessary to compute the vehicle's Mach speed in order to determine the value of the drag coefficient. Vehicle Mach speed is defined by

 $M = V_{L}/C$ 

where

Ĉ = acoustic velocitý

 $C = a_0 + a_1 y + a_2 y^2 + a_3 y^3 + a_2 y^4 + a_5 y^5 + a_6 y^6$ 

y = vehicle altitude above the earth's surface in thousands of feet.

Puckett, Allen E., "Guided Missile Engineering," McGray-Hill, New York, 1959.

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(2)

(3)

## TABLE P-1

## DRAG COEFFICIENTS

	•	<u>`</u>
MACH NUMBER	COEFFICIENT	
•0	1.12	
. 63	1.27	
.90	1.38	
1.02	· 1.82	
1.05	1.95	
1.15	2.07	ļ
1.25	2.10	
1.37	2,06	
1.52	1,99	
2.40	1.64	
3.00	1.48	
3.30	1.41	
3.97	1.38	
5.00	1.35	î î
6.00	1.34	
10.00	1.31	
40.00	1.31	

The values of the coefficients,  $a_{i}$ , for different values of y are given in table ". A comparison of values of "constical velocity, computed using polynomials with the coefficients  $a_{i}$ , with data from the ARDC model atmosphere of 1959 is shown in table P-3.

The 1 ft coefficient,  $C_g$ , may be approximated by 24, where 4 is the angle of attack in radians, if the vehicle body is assumed to be basically blunt in shape. Air density is a function of altitude above the earth's surface and may be approximated by

$$= 10^{1} e^{3}$$
 (4)

where

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 $s = b_0 + b_1 y + b_2 y^3$ r = scaling exponent

Values of r and  $b_i$  for different values of y are given in table P-4. comparison of air density, computed from equation 4, with data from the ARDC model atmosphere of 1959 is given in table P-5. The coefficients  $b_i$ and  $a_i$  are primarily a result of fitting third degree polynomials to data from the ARDC model atmosphere of 1959.

The accelerations due to non-gravitational perturbations may now be expressed by

$$2\overline{P} = -a_{d}\overline{D} + a_{\ell}\overline{L}$$

where

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- D = unit vector directed along the longitudinal axis of the vehicle.
- L = unit vector normal to the longitudinal plane of the vehicle.

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	, ę	346.5	ę	- <b>0-</b>	-0-	: 0- -	, 0- - -	ę
<u>κ-1</u> )	Ś.	1.581094244 × 10 ³	-3.233401688 x 10 ⁰	5.65363161 x 10 ⁻³	-1.523623994 × 10 ⁻⁵	- <b>O</b> -	-0-	-0-
SOUND (FT. S	4	1105.7	9	, <b>-</b> 0-	-0-	-0-	-0-	, ,
COMPUTING SPRED OF S	* <b>~</b> ~	2.21401073 × 10 ⁴	-1.2858749 x 10 ⁵	3.9502867 × 10 ⁵	2.6069038 × 10 ⁵	-3.5596453 × 10 ⁶	6.6814040 × 10 ⁶	-4.0833579 × 10 ⁶
FIOLEUS	5	968.08	-0,	-0-	َ ب ا	- Ç	, <b>-0-</b>	د - ب د
	1	1.116243333 × 10 ³	-3.778722222 × 10 ⁰	-1.0177778 × 10 ⁻²	+3.77777326 x 10 ⁻⁵			-0-
	-1	з , 80,	5-1	B Ž		8, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2,	ڈ <b>ھ</b> ج	<b>a</b> 9

a₁ = 0 for i 2 4

-2000 S H S 38000	38000 < 11 🔬 80000	80,000 < H 🗴 155,000	J55,000 < H ≤ 175,000	175,000 < ∺ ≤ 260,000	260,000 < H ≤ 300,000°	300,000 < H	
Ţ	<u>بر،</u>	m	4	Ś	<u>ور</u>	-	,
			ध भ				
where							

H = altitude above mean sea level in vect

* In this case y = 'H/300,000. Coefficients are from Gianopulos, G. N., "Generalized Powered Flight Trajectory Program for IBM 704 Computer," JPL Technical Report No. 32-38, Sept., 1960.

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### TABLE P-3

## COMPARISON OF COMPUTED VS. ACTUAL SPEED OF SOUND

ALTITUDE (FT)	ACCUSTICAL VELOCITY (FT SEC ⁻¹ )	ACTUAL
5.0 x 10 ³	1097.1	1097.1
1.0 x 10 ⁴	1077.4	1077,4
$1.5 \times 10^4$	1057.4	1057.4
2.0 x 10 ⁴	1036.9	1036.9
2.5 x $10^4$	1016.0	1016.1
$3.0 \times 10^4$	999.7	994.8
3.5 x 10 ⁴	973.1	973.1
$4.0 \times 10^4$	968.0	968.0
5.0 x 104	968.0	968,0
6.0 x 10 ⁴	968.0	968.0
7.0 x 104	968.0	968.0
$8.0 \times 10^4$	968.0	968.0
8.5 x 10 ⁴	975.4	973:4
9.0 x 10 ⁴	983.9	983.4
$9.5 \times 10^4$	993.3	993.3
1.0 x 10 ⁵	1003.0	1003.2
$1.5 \times 10^5$	1095.3	1096.3
2.0 x 10 ⁵	1038.6	1038.7
$2.5 \times 10^5$	. 888.Ó ·	888.2
$3.0 \times 10^5$	846.5	846.5
3.5 x 10 ⁵	1100.0	14100.0
4.0 x 10 ⁵	1100.0	1100.0
4.5 $\times 10^5$	1100.0	1,100.0

* By "actual" is meant values given by "Handbook of Geophysics," ARDC, 1960.

TABLE F	·
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COEFFICIENTS IN COMPUTING AIR DENSITY (CB . FT-3)

Í.	, ^b l	^b 2	b ₃	bo
1	$-2.140228194 \times 10^{-2}$	-4.112711777 x 10 ⁻⁴	1.948636863 x 10 ⁻⁶	4.33696389 x 10°
2	-1.385607963 x 10 ⁻¹	+5.754215325 x 10 ⁻⁴	$-1.060362481 \times 10^{-6}$	1.385541893 x 10
3	+6.194417751 × 10 ⁻¹	-2.284935788 x 10 ⁻³	$2.543977892 \times 10^{-6}$	-4.859279372 x 10
4	$-5.301440339 \times 10^{-1}$	$+1.052418458 \times 10^{-3}$	-7.164439446 x 10 ⁻⁷	9.154608305 x 10
5	-1.423384892 x 10 ⁻²	+6.97170,417 x $10^{-6}$	-1.733376425 x 10 ⁻⁹	9,995812402 × 10°
6.	-8.730600381 x 10 ⁻³	+1.995115962 x 10 ⁻⁶	$-2.192314^{\circ}63 \times 10^{-10}$	1.254637591 x 10'

and.

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	1	2	3	4	5	6
(, r	-4	-6	-8	-11	-13	-1.5

where

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	(1	$0 \leq H \leq 100,000$
	2	100,000 < H < 250,000
i = {	3	250,000 < H ≤ 350,000
	4	350,000 < H ≤ 525,000
	5	525,000 < H ≤ 1,200,000
1	6	1,200,000 < H

H = altitude abově mean sea level in feet

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## TABLE P-5

## COMPARISON OF COMPUTED VS. ACTUAL AIR DENSITY

ALTITUDE (FT)	COMPUTED AIR DENSITY (CB·FT ⁻³ )	ACTUAL
2.5 x 10 ⁴	$3.570 \times 10^{-2}$	$3.430 \times 10^{-2}$
5.0 x 10 ⁴	$1.196 \times 10^{-2}$	$1.470 \times 10^{-2}$
7.5 x 10 ⁴	$3.457 \times 10^{-3}$	$3.546 \times 10^{-3}$
1.0 x 10 ⁵	$1.033 \times 10^{-3}$	$1.033 \times 10^{-3}$
1.25 x 10 ⁴	$-3.166 \times 10^{-4}$	$3.274 \times 10^{-4}$
1.50 x 10 ⁵	1.146 × 10 ⁴	1.146 x 10 ⁻⁴
1,75 x 10 ⁵	$4.695 \times 10^{-5}$	4.544 x 10 ⁻⁵
$2.00 \times 10^{5}$	$1.968 \times 10^{-5}$	$1.968 \times 10^{-5}$
2.25 $\times 10^5$	$7.647 \times 10^{-6}$	
2.5 x 10 ⁵	2.493 x 10 ⁻⁶	$2.493 \times 10^{-6}$
$3.0 \times 10^5$	1.327 x 10 ⁻⁷	$1.327 \times 10^{-7}$
$3.5 \times 10^5$	$7.282 \times 10^{-9}$	7.282 x 10 ⁻⁹
$4.0 \times 10^5$	7.561 x 10 ⁻¹⁰	7.561 x $10^{-10}$
$4.5 \times 10^5$	2.248 x 10 ⁻¹⁰	2.248 x 10 ⁻¹⁰
$5.0 \times 10^5$	$1.023 \times 10^{-10}$	9.789 x 10 ⁻¹¹
$7.0 \times 10^5$	1.735 × 10 ⁻¹¹	$1.689 \times 10^{-11}$
9.0 x 10 ⁵	$4.800 \times 10^{-12}$	4.809 $\ddot{x}$ 10 ⁻¹²
$1.1 \times 10^6$	$1.595 \times 10^{-12}$	$1.592 \times 10^{-12}$
1.3 x 10 ⁶	$5.954 \times 10^{-13}$	5.946 x 10 ⁻¹³
$1.5 \times 10^6$	$2.452 \times 10^{-13}$	$2.450 \times 10^{-13}$
$1.7 \times 10^6$	$1.094 \times 10^{-13}$	1.095 x 10 ⁻¹³
$1.9 \times 10^6$	5.243 × 10 ⁻¹⁴	5.243 x 10 ⁻¹⁴
$2.1 \times 10^6$	$2.665 \times 10^{-14}$	$2.662 \times 10^{-1.4}$

By "actual" is meant values given by "Handbook of Geophysics," ARDC, 1960.

Here, for simplicity,  $\overline{D}$  was taken to be directed coincidentally with the vehicle's earth-related velocity vector,  $\overline{V}_2$ . Thus,

$$\overline{D} = \overline{V}^{\dagger} = \frac{V_{2}}{V_{2}} = \frac{V_{1}^{\dagger}}{V_{2}^{\dagger}}$$

where

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$$\overline{\mathbf{v}}_{\boldsymbol{\ell}} = \begin{vmatrix} \mathbf{v}_{\mathbf{x}} \\ \mathbf{v}_{\mathbf{y}} \\ \mathbf{v}_{\mathbf{y}} \end{vmatrix}$$
$$\mathbf{v}_{\boldsymbol{\ell}} = |\overline{\mathbf{v}}_{\boldsymbol{\ell}}|$$

Normally L is taken to be normal to some reference plane containing the longitudinal axis of the vehicle. For example, in the case of an aircraft, this plane is determined by the position of the wings. However, no assumptions of wings, nor their positioning, has been made. Therefore, this plane was taken to be the plane defined as being perpendicular to the equatorial plane and containing  $\overline{V}'$ . The flow of air  $\overline{F}$ , was taken to be perpendicular to the position vector,  $\overline{R}$ , of the vehicle and directed to oppose  $\overline{V}'$ .



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Once the direction of F is leterminel, L becomes

$$\overline{\mathbf{L}} = \begin{vmatrix} \mathbf{n}_{1} \\ \mathbf{n}_{2} \\ \mathbf{n}_{3} \end{vmatrix} = [\overline{\mathbf{V}} + \cos \alpha + \overline{\mathbf{F}}] (1/\sin \alpha)$$

(7)

where

 $\leq \cos^{-1} \{ -\overline{V}^{\dagger} \cdot \overline{F} \}$ 

#### APPENDIX 🤤

#### EARTH'S CRAVITY FIELD

The earth's gravitational field may be derived from a scaler potential which obeys Poisson's equation; namely,

$$\nabla^{2} \psi (\mathbf{r}_{\mathbf{v}}, \lambda) = -\rho (\mathbf{r}, \mathbf{p}, \lambda)$$
(1)  
where  $\psi = \text{scal: } \mathbf{r} \text{ potential}$   
 $\rho = \text{mass density}$ 

when the region of interest is above the earth's surface,  $\rho = 0$  and equation (1) becomes

$$\nabla^2 \psi(\mathbf{r}, \mathbf{p}, \lambda) = 0 \tag{2}$$

A solution of equation (2) which is consistent with the physical earth is

$$\psi(r, \vartheta, \lambda) = \frac{\kappa}{e^2} \sum_{m=0}^{\infty} \sum_{m=0}^{\infty} \frac{a^{n+2}}{n+1} P_n^m (\sin \vartheta) [C_{n,m} \cos m\lambda + S_{n,m} \sin m\lambda] [2]$$

where

y = geocentric latitude

λ = east longitude Mon Greenwich meridian

r = radial distance from earth's mass center

a = earth's équatorial radius (seminajor axis).

 $F_{n}^{\mu}(\sin \psi) = associated Legendre polynomials of the first kind$ 

K = product of universal gravity constant and earth's mass

n, S = empirical coellicients

The potential equation (3) is commonly referred to as an expansion in fesseral harmonics. The coefficients  $C_{n,k}$  and  $S_{n,k}$  have been evaluated

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#### CULIC CORFORATION

based of observations of satellite orbits and the corresponding changes in the associated basic orbital elements. Current values of the longitude dependent coefficients are not sufficiently well defined or significant to be used in general prediction representation. If it is assumed that the earth is longitudinally symmetric, then equation (3) becomes (after separation of the principal term)

$$\Psi(\mathbf{r}, \Phi) = \frac{K}{a^2} \left[ \frac{1}{r} - \sum_{n=1}^{\infty} J_n \frac{a^{n+2}}{r^{n+1}} P_n (\sin \Phi) \right]$$
(5)

where

 $J_{n} =$  the zonal harmonics of the earth's gravity.

The principal term of equation (5),  $\frac{1}{r}$ , defines the potential of a spherical body with concentric distribution of mass. Perturbations due to the meridianal asymmetry of the earth are represented by the one to infinity summation iterms.

Gravitational acceleration of the earth as a function of radial distance and geocentric latitude is given by the gradients of the potential function. See figure Q-1.) Thus

$\overline{g} = \overline{\nabla} \psi,$		(6)
where $= \frac{\partial \Psi}{\partial r} 1_r$	$+ \frac{1}{r} \frac{\partial \psi}{\partial \varphi} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2$	(7)

 $\frac{\partial \psi}{\partial r} = g_r = radial component of gravity$ 

(8)

(9)

 $\frac{1}{r} \frac{\partial \Psi}{\partial p} = g_{0} \neq azimuthal component of gravity$ 

 $1_r, 1_{\phi}$  = unit vectors of the radial and azimuthal gradients expressed in an earth centered, inertially "ixed coordinate system.

CUEIC COMPONATION

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 $g_{r} = -\frac{\kappa}{a^{2}} \left[ \frac{1}{r^{2}} - \sum_{n=1}^{22} (\hat{n} + 1) J_{n} \left( \frac{a}{r} \right)^{n+2} J_{n} \left( \frac{a}{r} \right)^{n+2} \right]_{n}$  (sin b) (10)  $g_{p} = \frac{\kappa}{a^{2}} \left[ \sum_{n=1}^{\infty} J_{n} \left( \frac{a}{r} \right)^{n+2} F_{n}' (ain \phi) \right]$ (11)where  $P_n^{t}(\sin \phi) = \frac{\partial}{\partial \phi} \left[ P_n^{t}(\sin \phi) \right]$ 

and the components of gravity will therefore be

 $\overline{\mathbf{g}} = \mathbf{g}_{\mathbf{r}} \, \overline{\mathbf{1}}_{\mathbf{r}} + \mathbf{g}_{\mathbf{r}} \, \overline{\mathbf{1}}_{\mathbf{p}}$ 

Taking gradients of equation (5) yields



Figure Q-1

Components of Gravity

(12)

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Legendre polynomials  $P_n$  (sin p) and  $P_n^{-1}$  (sin  $\phi$ ) can be computed from the recurrsion relationship in the following manner:

$$P_{0}(\sin \phi) = 1$$

$$P_{1}(\sin \phi) = \sin \phi$$

$$P_{2}(\sin \phi) = (3 \sin^{2} \phi - 1)/2$$

$$P_{n+1}(\sin \phi) = \left[ \frac{2n+1}{n+1} \sin \phi P_{n}(\sin \phi) - \frac{n}{n+1} P_{n-1}(\sin \phi) \right]$$

$$P_{0}^{+}(\sin \phi) = 0$$

$$P_{1}^{+}(\sin \phi) = \cos \phi$$

$$F_{2}^{+}(\sin \phi) = 3 \sin \phi \cos \phi$$

$$F_{n+1}^{+}(\sin \phi) = \left[ P_{n-1}^{+}(\sin \phi) + (2n+1) F_{n}(\sin \phi) \cos \phi \right]$$

$$(13)$$

It the total gravity is to be expressed in an orthogonal cartesian coordinate system such as the earth centered inertial system, then the unit vectors of equation (7) become

(14)

(15)

$$\mathbf{\tilde{l}}_{r} = \begin{bmatrix} \mathbf{\tilde{X}} \\ \mathbf{\tilde{R}} \\ \mathbf{\tilde{Z}} \\ \mathbf{\tilde{R}} \\ \mathbf{\tilde{Z}} \\ \mathbf{\tilde{R}} \\ \mathbf{\tilde{S}} $

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The first nine zonal harmonics have been determined by Y. Kozai¹ from satellite orbital data. Kozai⁺s values for the zonal harmonics are accepted as the most representative now available and are listed here for reference.

$$J_{1} = 0$$

$$J_{2} = + 1082.48 \pm 0.04 \times 10^{-6}$$

$$J_{3} = -2.502 \pm 0.007 \times 10^{-6}$$

$$J_{4} = -1.84 \pm 0.09 \times 10^{-6}$$

$$J_{5} = -0.064 \pm 0.007 \times 10^{-6}$$

$$J_{6} = +0.39 \pm 0.009 \times 10^{-6}$$

$$J_{7} = -0.470 \pm 0.010 \times 10^{-6}$$

$$J_{8} = -0.02 \pm 0.07 \times 10^{-6}$$

$$J_{9} = +0.117 \pm 0.011 \times 10^{-6}$$

Also given by Kozai are the constants K and a, which are:

(16)

(17)

$$K = 3.986032 \times 10^{20} \text{ cm}^3/\text{sec}^2$$

a = 6378165 neters

$$\frac{K}{32} = 32.14648177$$
 :1/sec²

1 Kozai, Yoshihide. "Humerical Results From Grbits." Smithsonian Institute Astrophysical Observatory Special Report No. 101.

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## APPENDIX

#### GEGDETIC SECOR LINE CRGSSING

#### Introduction

1.0

The purpose of a line crossing operation is to estimate the distance between two points on the earth's surface. This distance is reduced to the shortest distance (i.e., the geodesi.) along some reference spheroid (e.g., Clark 1866 or International).

The classical line crossing technique is illustrated by the SHIRAN and HIRAN systems. In these systems an aircraft flies across the baseline at a nearly constant height and nearly perpendicular to the baseline. During the flight ranges from the two base stations are simultaneously measured. (See figure R-1.) if the puirs of measured ranges are added to form a series of range sume (Rs), a curve similar to that shown in figure R-2 will result. The minimum of this curve corresponds to the time at which the aircraft was directly over the line. Using the two ranges and the altitude corresponding to the range sum minimum, an estimate of the geodesic may be found.

The use of the Geodetic SECCR system to perform line crossings is operationally similar but differs from the classical techniques in several ways. First, the height of the satellite will not be constant but will vary with time. Second, the satellite cannot be expected to cross the baseline near the midpoint nor cross perpendicular to the baseline. These two conditions, as will be shown later, cause the range sum minimum to occur at some time before or after the baseline is crossed. This prevents the use of the classical technique for the solution of the problem.





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Time (Seconds)

R-3

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The distance  $R_p$  is computed at each point from the satellite's equatorial coordinates  $(X_E | Y_E | Z_E)$  by  $E_E = [X_E^2 + Y_F^2 + Z_E^2]^{\frac{1}{2}}$ . The sate lite position in equatorial coordinates may be determined using Geodetic SECCR date from base site number one and two additional sites whose coordinates are known or from some other tracking or ephemeris data.

Since the range sum minimum cannot be used to determine the time of

the line crossing, some other parameter must be found which will be minimum

as the baseline is crossed. The parameter used is the central angle sum

 $\Theta_s = \Theta_1 + \Theta_2$  ( figure R-3.) which takes on a minimum value when the vector

The latitude and longitude of the second site  $(\emptyset)_2$  are assumed to be approximately known. A schematic representation of these quantities is shown in figure R-3.

 $(\vec{p}_{Al})_{1}$  = latitude, longitude, height of base site number one. = height of base site number two. ho  $R_1, R_2 = simultaneous range observations from sites one and two to$ 

## Method For Geodetic SECCE Line Crossing Computation In the method for computing the line crossing from Geodetic SECOR

R -4

= distance from the center of the earth to the satellite.

satellite data the following are assumed to be known precisely:



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## Minimum Sum Determination

the deterministion of a minimum central angle sum assumes that in a limited region about the minimum; the sum, S(t), may be approximated by a second degree polynomial:  $n(t) = a_0 + a_1 t + a_2 t^2$  if the dynamics of the vehicle are not too extreme. Having determined F(t), the minimum may be obtained as follows:

$$\frac{d}{dt} P(t_{m}) = 0, P_{M} = P(t_{M})$$
 (4)

where tM is the time at which P(t) is an extremum.

$$\frac{d}{dt} P(t_{M}) = x_{1} + 2x_{2}t_{M}$$

So,

$$\frac{1}{242}$$

Then:

For a minimum:

$$\frac{d^2}{dt^2} : (t_{\chi}) > 0$$
$$\cdot \frac{d^2}{dt^2} : (t) = 2\epsilon_2 > 0$$

So  $a_2 > 0$  for a minimum.

The polynomial f(t) may be determined from the measured data (i.e., ventral angle sums;  $[1, 1_2, ..., U]$  by use of a least squares criterion. That is,  $y = \sum_{i=1}^{N} - F(t_i)]^2 = \sum_{i=1}^{N} (t_i - a_0 - a_1 t_i - a_2 t_i^2)^2$  is a minimur.

Ř - 6

(5)

(6)

(8)

(9)

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$$\frac{\partial a}{\partial a_0} = 0, \quad \frac{\partial a}{\partial a_1} = 0, \quad \frac{\partial a}{\partial a_2} = 0$$

$$\frac{\partial a}{\partial a_0} = -2 \quad \frac{\partial}{\partial a_1} = 0, \quad \frac{\partial a}{\partial a_2} = 0$$

$$\frac{\partial a}{\partial a_0} = -2 \quad \frac{\partial}{\partial a_1} = 0 \quad \frac{\partial a}{\partial a_1} = -2 \quad \frac{\partial}{\partial a_1} = 0 \quad \frac{\partial a}{\partial a_1} = -2 \quad \frac{\partial}{\partial a_1} = 0 \quad \frac{\partial}{\partial a_1} = -2 \quad \frac{\partial}{\partial a_1} = 0 \quad \frac{\partial}{\partial a_2} = -2 \quad \frac{\partial}{\partial a_1} = 0 \quad \frac{\partial}{\partial a_2} = -2 \quad \frac{\partial}{\partial a_1} = 0 \quad \frac{\partial}{\partial a_2} = -2 \quad \frac{\partial}{\partial a_1} = 0 \quad \frac{\partial}{\partial a_2} = -2 \quad \frac{\partial}{\partial a_1} = 0 \quad \frac{\partial}{\partial a_2} = -2 \quad \frac{\partial}{\partial a_1} = 0 \quad \frac{\partial}{\partial a_2} = -2 \quad \frac{\partial}{\partial a_1} = 0 \quad \frac{\partial}{\partial a_2} = -2 \quad \frac{\partial}{\partial a_1} = 0 \quad \frac{\partial}{\partial a_2} = -2 \quad \frac{\partial}{\partial a_1} = 0 \quad \frac{\partial}{\partial a_2} = -2 \quad \frac{\partial}{\partial a_1} = 0 \quad \frac{\partial}{\partial a_2} = -2 \quad \frac{\partial}{\partial a_1} = 0 \quad \frac{\partial}{\partial a_2} = -2 \quad \frac{\partial}{\partial a_1} = 0 \quad \frac{\partial}{\partial a_2} = -2 \quad \frac{\partial}{\partial a_1} = 0 \quad \frac{\partial}{\partial a_2} = -2 \quad \frac{\partial}{\partial a_1} = -2 \quad \frac{\partial}{\partial a_1} = -2 \quad \frac{\partial}{\partial a_1} = -2 \quad \frac{\partial}{\partial a_1} = -2 \quad \frac{\partial}{\partial a_1} = -2 \quad \frac{\partial}{\partial a_1} = -2 \quad \frac{\partial}{\partial a_1} = -2 \quad \frac{\partial}{\partial a_1} = -2 \quad \frac{\partial}{\partial a_1} = -2 \quad \frac{\partial}{\partial a_1} = -2 \quad \frac{\partial}{\partial a_1} = -2 \quad \frac{\partial}{\partial a_1} = -2 \quad \frac{\partial}{\partial a_1} = -2 \quad \frac{\partial}{\partial a_1} = -2 \quad \frac{\partial}{\partial a_1} = -2 \quad \frac{\partial}{\partial a_1} = -2 \quad \frac{\partial}{\partial a_1} = -2 \quad \frac{\partial}{\partial a_1} = -2 \quad \frac{\partial}{\partial a_1} = -2 \quad \frac{\partial}{\partial a_1} = -2 \quad \frac{\partial}{\partial a_1} = -2 \quad \frac{\partial}{\partial a_1} = -2 \quad \frac{\partial}{\partial a_1} = -2 \quad \frac{\partial}{\partial a_1} = -2 \quad \frac{\partial}{\partial a_1} = -2 \quad \frac{\partial}{\partial a_1} = -2 \quad \frac{\partial}{\partial a_1} = -2 \quad \frac{\partial}{\partial a_1} = -2 \quad \frac{\partial}{\partial a_1} = -2 \quad \frac{\partial}{\partial a_1} = -2 \quad \frac{\partial}{\partial a_1} = -2 \quad \frac{\partial}{\partial a_1} = -2 \quad \frac{\partial}{\partial a_1} = -2 \quad \frac{\partial}{\partial a_1} = -2 \quad \frac{\partial}{\partial a_1} = -2 \quad \frac{\partial}{\partial a_1} = -2 \quad \frac{\partial}{\partial a_1} = -2 \quad \frac{\partial}{\partial a_1} = -2 \quad \frac{\partial}{\partial a_1} = -2 \quad \frac{\partial}{\partial a_1} = -2 \quad \frac{\partial}{\partial a_1} = -2 \quad \frac{\partial}{\partial a_1} = -2 \quad \frac{\partial}{\partial a_1} = -2 \quad \frac{\partial}{\partial a_1} = -2 \quad \frac{\partial}{\partial a_1} = -2 \quad \frac{\partial}{\partial a_1} = -2 \quad \frac{\partial}{\partial a_1} = -2 \quad \frac{\partial}{\partial a_1} = -2 \quad \frac{\partial}{\partial a_1} = -2 \quad \frac{\partial}{\partial a_1} = -2 \quad \frac{\partial}{\partial a_1} = -2 \quad \frac{\partial}{\partial a_1} = -2 \quad \frac{\partial}{\partial a_1} = -2 \quad \frac{\partial}{\partial a_1} = -2 \quad \frac{\partial}{\partial a_1} = -2 \quad \frac{\partial}{\partial a_1} = -2 \quad \frac{\partial}{\partial a_1} = -2 \quad \frac{\partial}{\partial a_1} = -2 \quad \frac{\partial}{\partial a_1} = -2 \quad \frac{\partial}{\partial a_1} = -2 \quad \frac{\partial}{\partial a_1} = -2 \quad \frac{\partial}{\partial a_1} = -2 \quad \frac{\partial}{\partial a_1} = -2 \quad \frac{\partial}{\partial a_1} = -2 \quad \frac{\partial}{\partial a_1} = -2 \quad \frac{\partial}{\partial a_1} = -2 \quad \frac{\partial}{\partial a_1} = -2 \quad \frac{\partial}{\partial a_1} = -2 \quad \frac{\partial}{\partial a_1} =$$

Rewriting in matrix form

Solving for [A]:

Figure shows a sample curve fit to a central angle sum scaled by a neur earth's radius for a long-line satellite crossing. The residuals plotted represent  $[L_1 - F(t_1)]$  versus time.

#### Estimation of the Geodesic.

The mightinum distance between the two base stations: (geodesic) is not a plane curve and thus may not be determined in closed form from the central angle minimum. An estimate may be made by assuming that the geodesic may be expressed in the form:

 $S_{1D} \xrightarrow{\longrightarrow}$  geodesic  $\rho \xrightarrow{\longrightarrow}$  exact scaling radius  $\Theta_{1D} \xrightarrow{\longrightarrow}$  contral angle.

Now the estimate of  $\Theta_{12}$  is found directly from the minimum central angle sum (i.e.,  $\widetilde{\Theta}_{12} = (\widetilde{\Theta}_{3})$  minimum). An estimate of the scaling radius ( $\beta$ ) is made using the survey data for base station 1 and the approximate survey duta for base station 2 to compute a geodesic ( $\widetilde{\Theta}_{12}$ ) and central angle ( $\widetilde{\Theta}_{12}$ ). the central angle is found from:

$$c \cdot s \cdot \frac{1}{2} = \frac{1}{c} \frac{s_1 \cdot c_{s_2}}{s_1 \cdot c_{s_2}}$$

and  $S_{12}$  is found using codeno's method for the inverse computation.

R-8

(26)



The estimate for the scaling radius,  $(\beta)$ , is found from:

$$b = S_{GD}^{A} \Theta_{12}^{A}$$
(21)

The final estimate for the geodesic is given by:

$$\widehat{\mathbf{S}}_{\mathrm{JL}} = \widehat{\boldsymbol{\rho}} \, \widehat{\mathbf{\theta}}_{12} \tag{22}$$

Ine relative error is approximated by

$$\frac{\mathcal{L}\,\widetilde{S}_{0D}}{S_{0D}} \stackrel{*}{=} \frac{\mathcal{L}\,\widetilde{\phi}}{\phi} + \frac{\mathcal{L}\,\widetilde{\phi}_{12}}{\widetilde{\phi}_{12}}$$
(23)

The first term of this expression reflects the uncertainty in the survey position of the second base site while the second term reflects <u>primarily</u> the errors arising from the determination of  $R_{\rm H}$  and the ranging errors.

In order to determine more accurately the line length, a network of lines must be measured and a network adjustment procedure applied to improve the first estimates.

### Effect of Vehicle Dynamics on the Range Sum and Central Angle Sums

As indicated above, the minimum range sum does not necessarily occur as the vehicle crosses the baseline. The relations derived below show, for the case of a circular orbit, the magnitude of the offset.

Figure E-5 shows the geometry of a line crossing configuration for a circular orbit. The coordinate system is chosen so that the orbit is centered at the origin of the coordinate system and lies in the y-z plane. The radius (c) is constant and the angular velocity ( $\beta$ ) is constant.

R - 10





R-11

CUEIC CORPCREMICK

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Using the geometry of Figure R-5 the coordinates of the satellite (xyz) and of the two tracking sites  $(XYZ)_1$  and  $(XYZ)_2$  may be written:

 $x = 0 X_1 = d_1 \cos \alpha X_2 = -d_2 \cos \alpha (24)$   $y = \rho \sin \beta Y_1 = -d_1 \sin \alpha Y_2 = d_2 \sin \alpha (24)$   $z = \rho \cos \beta X_1 = Z_1 Z_2 = Z_2$ 

The ranges and range rates from each tracking site are:

$$R_{1} = \left[\rho^{2} + d_{1}^{2} + 2\rho(d_{1} \sin x \sin \beta - 2\cos \beta)\right]$$
(25)

$$k_2 = \left[\rho^2 + d_2^2 + Z_2^2 - 2\rho(d_2 \sin (\sin \beta + Z_2 \cos \beta))\right]$$
 (26)

$$R_{\underline{j}} = \frac{\rho_{12}}{R_{\underline{j}}} \left( d_{\underline{j}} \sin \alpha \cos \beta + Z_{\underline{j}} \sin \beta \right)$$
(27)

$$\dot{P}_2 = \frac{\rho_1^2}{R_2^2} \left( -\dot{c}_2 \sin \alpha \cos \beta + Z_2 \sin \beta \right)$$
 (29)

Now the range sum  $(r_s)$  is given by  $R_s = \Gamma_1 + R_2$ , and the range sum rate  $R_s$  by:

$$\dot{F}_{s} = \dot{R}_{1} + \dot{F}_{2} = \rho_{1}^{2} \left\{ \left[ \frac{d_{1}}{R_{1}} - \frac{d_{2}}{R_{2}} \right] \quad \sin \ll \cos \beta + \left[ \frac{Z_{1}}{R_{1}} + \frac{Z_{2}}{R_{2}} \right] \quad \sin \beta \right\} \quad (29)$$

(30)

h-12

In order that  $\lambda_{\beta}$  may be used, the range sum minimum must occur as the vehicle crosses the baseline. In the above situation this corresponds to  $\beta = 0$  or

$$\left(\hat{F}_{s',s=0} = \rho_{1}, \frac{d_{1}}{d_{1}} - \frac{d_{2}}{d_{2}}\right) \sin \alpha = 0$$

The conditions under which  $\frac{3}{3} = 0$  when  $\beta = 0$  are:

(1)  $\rho_{\rm P} = 0$  which is not of practical interest.

CULIC CORP. RATION

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# NOT REPRODUCIBLE

(2) 
$$x = 0$$
 which corresponds to perpendicular crossing of the baseline.

(3)  $\frac{d_1}{R_1} \neq \frac{d_2}{R_2}$  which corresponds to bisecting the baseline.

In general, then, use of the range sum will introduce an error in the baseling length determination.

The central angle sum rate  $(\dot{\theta}_s = \dot{\theta}_1 + \theta_2)$  may be obtained using the law of cosines to determine  $\theta_1$  and  $\theta_2$  as follows:

$$P_{s} = \left[ \cos^{-1} \left( \frac{\rho^{2} + \rho_{01}^{2} - R_{1}^{2}}{2\rho \rho_{01}^{2}} \right) + \cos^{-1} \left( \frac{\rho^{2} + \rho_{02}^{2} - R_{2}^{2}}{2\rho \rho_{02}^{2}} \right) \right]$$
(31)

$$\hat{\Theta}_{s} = \beta \left[ \frac{1}{\rho_{o1} \sin^{2} \Theta_{1}} \left( d_{1} \sin \times \cos \beta + Z_{1} \sin \beta \right) \right]$$

$$+ \frac{1}{\rho_{o2} \sin^{2} \Theta_{2}} \left[ -d_{2} \sin \propto \cos \beta + Z_{2} \sin \beta \right]$$
(32)

In order that  $\hat{\Theta}_{s}$  be a minimum as the satellite crosses the baseline, then  $\hat{\Theta}_{s} \neq 0^{\circ}$  at  $\beta = 0$ .

$$(\dot{\theta}_{s})_{j=0} = \beta \sin \left( \frac{d_{1}}{\rho_{c1} \sin \theta_{1}} - \frac{d_{2}}{\rho_{o2} \sin \theta_{2}} \right)$$
33)

but at k = 0,

$$\frac{d_1}{\rho_{o1}} = \sin \theta_1 \text{ and } \frac{d_2}{\rho_{o2}} = \sin \theta_2$$
(34)

R-13

so that  $\theta_s = 0$  at  $\beta = 0$  and  $\theta_s$  is a minimum. Thus for a circular orbit the central angle sum  $(\theta_s)$  may be used in the line crossing computation while the range sum  $(R_s)$  may not.

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## APPENDIX S

## SAMPLE LISTINGS

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This appendix provides a sample of each of the types of listing (printout) obtained during the data processing. A brief description of each heading is included unless the heading is self-explanatory.

.S-1
S.1 <u>Raw Listing</u>. The raw listing was made directly from the copied raw tape (program EXAM1) after unpacking the tape format (subroutine FORMAT) and resolving the range (subroutine RESOLVE). In general, every fourth or fifth sample was listed.

The following quantities were output (sample listing 1):

T	Time mark which was recorded (indicated by a 1)
-	every second. In the sample listing, these particular
	samples were missed
<u>Q</u> .	Quality mark which was recorded as a 1 if one or
	more of the tracking servos were not locked
S	Station number
R	Run number
MO, DA	Month and day of track
HR, M, S, MS	Time (GMT) recorded at the tracking site in hours,
	minutes, seconds, milliseconds
RANGE	Resolved range in meters
DIF	First differences of the ranges
VF	Very fine channel in meters $(1/2 \text{ and } 1/4 \text{ meter bits})$
	not indicated)
FN	Fine channel in meters
CS	Coarse channel in meters
VC	Very coarse channel in meters
ER	Extended range in meters
D1 - IC	Difference between the VF and VFIC channels (used
	to compute the ionospheric correction)

S-2

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VF	-	F	Difference between the overlap bits of	the very fine and
			and fine channels	

F - C Différence between the overlap bits of the fine and coarse channels

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C - VC Difference between the overlap bits of the coarse and warry coarse channels

In earlier listings, the last three columns included the following quantities:

R - D2, R - D3,	Reference phase minus the phase three of the D
R - D4	channels. The numbers were scaled so that the
	least significant bit indicated one unit. The $V{f F}$
	column is actually R - D1.

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GEODETIC SECOR USA-2 LARSON

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ORBIT 1

TQSRMD	DA HR M S MS	RANGE	DIF	VF	FN	CS	v
00314	21 22 19 12 12	951267.00	-25.75	227	976	34560	421
00314	21 22 19 12 262	951244.00	-23.00	204	944	34816	421
00314	21 22 19 12 512	951223.25	-20-75	183	912	34048	421
003142	21 22 19 12 762	951206.50	-16.75	166	912	34560	421
003142	21 22 19 13 12	951192.25	-14.25	152	880	34048	421
003142	22 19 13 262	951181.50	-10.75	141	896	34560	421
003142	22 19 13 512	951173.75	-7.75	133	880	34304	421
003142	22 19 13 762	951169.25	-4.50	129	864	34304	419
0 0 3 1 4 2	22 19 14 12	951167.25	-2.00	127	864	34304	419
003142	22 19 14 262	951167.75	•50	127	880	34560	421
003142	22 19 14 512	951171.75	4.0Ò	131	880	34560	419
003142	1 22 19 14 762	951178.75	7.00	138-	Å96	34560	421
003142	1 22 19 15 12	951188.50	9.75	148	896	34816	419
003142	1 22 19 15 262	951200.50	12.00	160	912	34304	421
003142	1 22 19 15 512	951215.75	15.25	175	912	34304	421
	1 22 19 15 762	951234.75	19.00	194	928	34304	419
003142	1 22 19 16 12	951256.25	21.50	216	944	34304	419
	1 22 19 16 262	951281.25	25.00	241	1008	34560	425
	1 22 19 16 512	951309.25	2800	13	1008	34304	419
	1 22 19 16 762	951339.00	29.75	43	1024	34304	4191
	1 22 19 17 12	951372.75	33,75	76	1088	34560	4239
	1 22 19 17 262	951409.75	37.00	113	1136	34816	4214
	1 22 19 17 512	951449.25	39.50	153	1152	34816	4198
	1 22 19 17 762	951490.25	41.00	194	1168	34304	41.98
		951536-50	46.25	240	1248	35072	4218
		951584.75	48.25	32	1,296	34816	4218
		951635.50	50 <b>•75</b>	83	1344	34816	4239
003142		951690.75	55.25	138	1424	35328	4259
003142		951747-25	56.50	195	1440	34816	4198
0 0 3 1 4 2		951807.50	60.25	255	1520	35072	4218
003142	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	991870-25	62.75	62	1568	34816	42.1-8
003142		951930. (5	66.50	128	1648	35328	4239
003142	1 22 19 20 12	952005.50	68.75	197	1696	35328	4198
003142		922077.50	72.00	13	1792	35328	4239
0 0 3 1 4 2	1 22 19 20 742	952152#25 953330 75	74.15	88	1872	35072	4259
003142	1  22  19  20  102	75225U-15	18.50	168	1952	35840	4239
003142	1   27   19   21   262	772311400	00.25	247	2032	35584	4259
003142	1 22 19 21 512	952481.75	05°+15 97 00	14	2080	35584	4218
003142	1 22 19 21 762	952571.25		101	2142	35840	4218
003142	1 22 19 22 12	952663.50	07.50	201	2230	35584	4218
003142	1 22 19 22 262	952759.50	76963	87	2306	35840	4239
003142	1 22 19 22 512	952857.75	90.00	103	2480	36095	4239
003142	1 22 19 22 762	952959.50	101 75	127	2300	36096	4218
0 0 3 1 4 2	1 22 19 23 12	953063-50	104 00	121	2070	20322	4218
0 0 3 1 4 2	1 22 19 23 262	953171,25	107.75	221	218%	30352	4259
003142	1 22 19 23 512	953281-25	110 00		2804	36352	4218
003142	22 19 23 762	953394.75	113.50	193	2992	30008	4259
0 0 3 1 4 2	1 22 19 24 12	953511.25	116.50	20	2120	30008	4239
003142	22 19 24 262	953630.00	118.76	201	2226	24944	4239
0 0 3 1 4 2	22 19 24 512	953752.50	122.50	152	JJ74 2664	ンロロロ4 スプコット	4639
003142	L 22 19 24 762	953877.50	125_00	21	2414	21210 37275	4234
0 0 3 1 4 2	L 22 19 25 12	954005.00	127.50	140	3707	27274	4230
0 0 3 1 4 2	l · 22 19 25 262	954135.75	130.75	<u>רדא</u> ביכ	2040 2040	21210	4239
0 0 3 1 4 2	22 19 25 512	<b>954270.25</b>	134.50	158	2020	27020	- 7627 6920
0 0 3 1 4 2	22 19 25 762	954406.75	136.50	38	7077 84	37632	4634

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DIF	VF	FN	CS	VC	ER	DI-IC	VF-Ř	F-C.	C-VC
25.75	227	976	34560	421888	1015808	<b>Í</b> 6	1	-3	2
23.00	204	944	34816	421888	1015808	1.7	1	-4	2
-20.75	183	912	34048	421888	1015808	18	2	~1	2
-16-75	166	912	34560	421888	1015808	18	1	-3	2
14.25	152	880	34048	421888	1015808	18	Ĵ	-1	2
10.75	141	-900	34540	421888	1015808	18	Ō		2
-7 76	12-2	880	34304	421000	1015808	17	1	-2	2
	120	064	34304	421000	1015808	17	2	- 2	2
	127	004 04.4	34304	419040	1012000	17	2	- 2	2
-2.00	127	004	34304	419840	1012900	17	1	-2	, ,
•50	151	800	34360	421888	1015808	17	0		2
4.00	131	088	34560	419840	1015808	17	1		5
1.00	130	840	34560	421888	1015808	17	U V		2.
9.75	148	896	34816	419840	1048576	1/	1	44 A.	3
12.00	160	912	34304	421888	1048576	18	ľ	2	2
15.25	175	912	34304	421888	1015808	18	1	-2	2
19.00	194	928	34304	419840	10485.76	1,7	2	-2	3
21.50	216	944	34304	419840	1048576	47	2	~ 2	3
25.00	241	1008	34560	425984	1048576	2.7	-0	- 3	C
28.00	13	1008	34304	419840	1048576	1.7	÷:2:4	~· <u>}</u>	3
29.75	43	1024	34304	419840	1048576	-17	2	-1	3
33.75	76	1088	34560	423936	1048576	17	0	-2	1
37.00	113	1136	34316	421888	1048576	16	0	-3	2
39.50	153	1152	34816	419840	1048576	17	1	~ 3	3
41.00	194	1:168	34364	419840	1048576	18	3	-1	3
46.25	240	1248	35072	421888	1048576	16	1	-4	2
48.25	32	1296	34816	421888	1048576	1:7	1	-2	2
50.75	92	1244	34816	423036	1048576	17	î	-2	1
55 75	130	1474	36324	425084	1048576	1.7	~0		ò
EL EO	105	1440	2/014	410940	1040570	17	2		2
20.20	192	1440	24010	419040	1048378	1. I 1. 7	2	-2	2
60.427	(22	1520	35072	421000	1048576	17	0	- 1	2
02.10	02	1568	34810	421888	1048576	17	1	-1	2
66.50	128	1648	35328	423936	1048576	17	1	د	I.
68.75	197	1696	35328	419840	1081344	17	2	-3	.5
72.00	13	1.792	35328	423936	1048576	16	0	-2	1
74.75	88	1872	35072	425984	1048576	16	0	- l·	0
78.50	166	1952	35840	423936	1081344	17	Q	-4	1
80.25	247	2032	35584	425984	1048576	16	0	-3	0
83.75	74	2080	35584	421888	1048576	17	2	-2	3
87.00	161	2192	35840	421888	1081344	18	1	- 3	3
89.50	251	2256	35584	421888	1048576	17	2	-2	3
92.25	87	2368	35840	423936	1048576	17	1	-2	2
96.00	183	2480	36096	423936	1048576	17	0	-3	2.
98.25	25	2560	36096	421888	1048576	17	1	-2	3
101.75	127	2656	36352	421888	1048576	16	1	- 3	3
04-00	231	2784	36352	425984	1081344	17	ō	-3	1
07.75	83	2864	36352	421888	1048576	16	2	-2	3
	103	2007	36608	425084	1048576	17	1	- 3	ĩ
	142	2.776	36608	423026	1081366	14		-2	2
114 EA	20	2222	271 20	ティンプンリームクスロスム	1061344	10	0	- <b>C</b> 1 1	· «
110.7C	101	2626	21220	763730 10004	1040570	11	0	12	د د
110+12	50	3344	20004	463730	10403/0	1.1	, ,	11	~ ~
122.50	152	5456	51510	423930	1040576	11	1		<b>C</b>
125.00	21	2010	51516	428032	1048576	16	-0	12	U Q
127.50	149	3696	37376	423936	1048576	17	2	12	2
130.75	23	3856	37376	425984	1048576	17	0	13	1
134.50	158	3984	37888	423936	1048576	17	0	11	2
136.50	38	48	37632	428032	1048576	17	~0	-2	1

**S-4** 

S.2 Edited and Smoothed Data Listing. The edited and smoothed data listing was obtained during the editing and smoothing pass (program PASS2) on each raw tape. The following quantities were listed:

HR, M, S, MS

Time recorded on the raw tape in hours, minutes, seconds, and milliseconds

RAWRANGE

Raw range obtained from the range resolution (subroutine RESOLVE) prior to application of any calibration

ED. RANGE

Edited range obtained from the data editing portion of PASS2 (subroutine EDITSR) with calibration constants applied

SM. RANGE

Smoothed range obtained from the edited ranges by using least squares smoothing coefficients (subroutine SCR)

RESIDUAL EDIT CORR Difference between the edited and smoothed ranges Edit correction applied to the raw range to obtain the edited range (minus calibration). With one exception, the edit correction is an integral multiple of the least significant ambiguity (256 meters). If a data sample is bad (cannot be reduced within the noise tolerance by using an integral number of ambiguities), the edit correction is indicated by a 9.0. In this case, the edited range is either an extrapolated range or the raw range, depending on the number of successive bad samples which have occurred.

5.5

	-
ED. DIFF.	First differences of the edited ranges
SM. DIFF.	First differences of the smoothed ranges
R:D -	Range rate derived from the least squares smoothing
	coefficient (subroutine SCR) in units of meters per-
	second
RDD	Range acceleration derived from the least squares
-	smoothing coefficients (subroutine SCR) in units of
	meters per second per second
١Ç	Measu ded ionospheric correction derived from DI -
	IC and including the calibration constants
С	Program data quality indicator
	- = no correction necessary
	A = ambiguity correction
	B = bad sample

-

At the end of each data block, the number of bad samples (NUM BAD), the number of least significant ambiguities applied (NUM AMB), and the RMS of the smoothing residuals (RMS ERROR) are indicated.

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				C	HODETIC SI	ECOR	USA 2	SAN DIEGO		ORBIT
HR	M	S	MS	RAN RANGE	En P	ANGE		PESTDUAL		50
8	25	19	628	1777600 00	479757	7 00	*777577 +3	LEAIDONE	CDII GUKKI	<b>C</b> D •
ñ	25	10	72A	4777400 25	↓ 777A7	100 1 25	4777474 17	= <u>* T</u> O	0	
n	25	10	628	4777700 25		しょとう	1777774 .7	* • 1 4	0	1
0	25	- 0	020	1777000 K.	1//////		1/////0.00	, 62	0	1
U	25	17	720	1///09.9.5[	1///0/0	2.20	1///8/0,00	, 44	0	1
U A	75		₹13	1///999.70	1/7/970	<b>,</b> 20	1777976,43	•07	Û	1
Ð	67 94	<b>4</b> 0	128	17/8100.25	177907	,25	1778077.15	.10	0	1
0	67	20	228	1778201.00	1778170	3.00	1778178,24	<b>-</b> ,24	0	1
C	<b>4</b> 7	20	328	1778558.50	1778279	120	1778279,65	+,15	-256,00	1
0	22	20	428	1778405.00	1778382	2.00	1778381,42	.58	0	1
0	25	20	528	1778762,50	177848	5.5n	1778483,50	00	=256.00	1
Û	25	21	628	1794993.00	1778586	5.00	1778585.97	.03	-16384.00	1
0	25	20	728	1778711.75	1778688	3.75	1778688.80	n.05	n	- 1
Ō	25	20	828	1778815.00	1778792	2.00	1778791.95	.05	0	4
Û	25	26	928	1778918.25	177889	5.25	1778895.50	- 25	0	<u>له</u>
n	25	21	28	1779022.00	1778999		1778000 34	- 34	0	4
ñ	25	29	128	1779126 50	4779103	5.50	17704 .3 57	- 07	U	7
ň	25	21	228	4770234 25	4770268	2 25		<b>■</b> • U /	0	1
6	25	24	328	4770336 75	1//76()0	) 76	1//9602.11	•14	0	1
0	55	24	420	177044	1//9014		1779313.00	• .25	0	1
0	25	21	500	1//9471.00	1//9510	• • • •	1/79418,24	• ,24	0	1
0	25	41	220	1//959/.22	1//9524	1.22	1779523.83	,42	0	1
U	25	<b>41</b>	028	1//9022./2	1//9029	1.15	1779829.77	02	0	1
0	20	21	/28	1780012.75	1779738	5,75	1779736,13	.62	-254.00	1
Q	23	21	828	1780122.00	1779843	5•Ú0	1779842,75	,25	-256.00	1
0	25	21	928	1779972,75	1778949	1,75	1779949.71	• 0 4	0	ī
0	25	22	28	1780080.00	1780057	.00	1780057.01	•.01	ti -	1
0	25	22	128	1780187.00	178n164	.00	1780164.65	. 65	0	1
0	25	22	228	1780295.25	1780272	25	1780272.63	. 38	0	1
0	25	22	328	1781403 75	1780380	15	1780380.94	. 19	U a	4
0	25	22	428	1780513.00	1786496		1780489.61	30	-0 -0	4
0	25	22	528	1780622.00	1781599	1.00	1780508.61	30	U O	4
n	25	22	628	1780731 25	1790708	25	1784747 08		U	1
ñ	25	22	728	1786444 75	1700700	· · · ·	1780947 40	, S ()	Ű	1
ñ	25	22	828	1780050 50	170001/		1704017.00	, 1 7 , 1 7	Q	1
ň	25	22	020	4794 440 50	1/0092/	• 11	1/0092/.00	• 13	0	1
ñ	25	27	760	4724474 95	1/8103/	120	1/8103/,99	<b>•</b> • 49	Û	1
U A	シュ	21	4 2 0	1/011/1./2	1/51148		1781148,75	<b>~</b> •00	0	1
0	25	2.17	160	1/01283.00	1781,260	.00	1781259.91	.09	0	1
U	22	23	228	1781394,50	1781371	.20	1781371.40	.10	0	1
0	27	20	328	1781506,25	1781483	.25	1781483,22	<b>.</b> 03	0	1
n	27	2.5	428	1781618,25	1781595	25	1781545,38	•,13	0	1
可	25	23	528	1781730,75	1781707	.75	1781707.90	15	0	1
0	25	23	628	1781843.50	1781820	• Ż()	1781820.79	<b>.</b> 29	ຄັ	1
()	25	23	728	1781957.00	2781934	. 10	1781934.05	. 05	0	4
0	25	23	828	1782070.25	1782047	25	1782047.63	- 38	0	4
0	25	23	928	1782184.50	1782161	20	1782161.54	- 04	0	4
ĵ,	25	24	28	4782299.25	782276	. 27	+762275.64		U	
Û	25	24	128	1782413.75	1782390	75	179230	36	U	1
Ó	25	24	228	1782529	4782546		1780525 4-	• 0 0 7 -	0	1
ň	25	24	328	1782643 50	479969~	100 50	178263- 41	• • • 0	0	1
ň	25	24	408	4783750 05	1702020	4-U 26	1702026.01	-,11	0	1
بر م	25	シー	520	1702/27.22	3/02/00	イモン	1/02/00,29	<b>~ + 0 </b> ⁴	0	1
11 12	5	€ " 2 4	- <u>2</u> 0	1/025/2,/2	1/82852	12	1782852,32	, 43	0	1
U	57 95	<b>6</b> 4	920	1/02991,00	1782968	*20	1782968,68	18	0	1
0	イブ	24	128	1703108.00	1783085	.00	1783085,37	<b>∞</b> ,37	0	1
n	67	24	82B	1783724.75	1783201	,75	1783202,41	-,66	Ū	1

NUM. BAD NUH, AMB. -5n RMS ERROR ,3232 0

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the second life	SAN DIEGO	)	ORBIT 1269					
GE	RESIDUAL	EDIT CORR.	ED, DIFF.	SH. DIFF.	RD	RDD	I.C.	C
10	-13	0	99,25	99.25	991	36	22.00	
53	* • I 4 22	0	100.00	99,66	994	36	21.33	
66	, 22	0	100,29	100.02	998	. 36	21.33	÷
43	7	0	100.00	100.37	1002	36	21.33	
15	.10	0	100.75	100,72	1005	35	21.33	ω
54	24	U O	100 J 72	101.09	1009	35	21.33	•
65	- 15	-256 00	102 50	101,72	1012	35	21.05	
42	.58	n	101.50	102 00	1010	37	22.00	Ą
5.0	00	-256.00	102.50		1019	37	21,00	•
97	.03	6384.00	102.75	102.83	1020	33	22.00	<b>.</b>
ÊÖ	•.05	0	103.25	103,16	1020	35	24.00	•
95	.05	Ŭ.	103.25	103.55	1033	35	22 00	
₿0	-,25	Ō	103.75	103.86	1037	35	22.00	-
56	-,36	Û	104.50	104.21	1040	35	22 00	-
27	= , 0 7	Ó	104.75	104.54	1044	35	24.33	-
11	.14	0	104.50	104.88	1 n 4-7	35	29.33	-
<u>0</u> 0	-,25	0	105.25	105.25	1051	35	22.00	
24	-,24	0	106.25	105,59	1054	35	21.33	
5	.42	0	105,50	105.95	1058	35	21.33	
	02	0	107.00	106.35	1061	35	22.00	
LO Fr	.02	-254.00	106.25	106,02	1064	34	21.33	A
	. 27	-520.00	106.75	106.96	1068	34	22.00	Å
	• 0 *	0	107,25	107.30	1071	34	22.00	•
	••01	0	107.00	107.65	1075	34	22.00	-
	••07 10	0	108.25	107,98	1078	34	22,67	
	· 10	0	108,50	108,31	1082	34	22,67	-
	*•17 30	0	109,25	108.67	1085	34	22.00	
5	30	Ű	109.00	109.00	1088	34	21.33	
	30	U	109.47	109.34	1092	34	22,67	•
60	.15	U	109+20	109,00	1095	35	22.00	٠
53	13	U O	110.00	110 37	1099	59	22.00	•
9		0 (1	111.25		1102	37	22.67	۰
.5	00	0	111.25	111 16	1100	37	22.0/	•
1	.09	Ő	111.50	111.40	4443	35	22.0/	-
0	.10	Ō	111.75	111.82	1110	36	22.50	
2	.03	Ū	112.00	112.16	1120	35	22 00	-
8	<b>•</b> .13	0	112,50	112,52	1123	35	22,00	_
0	-,15	0	112,75	112.88	1127	35	22.67	
<u> 69</u>	• .29	0	113.50	113.26	1130	35	22.67	
2	05	0	113,25	113,58	1134	35	22.00	-
3	• • 38	0	114,25	113.91	1137	34	22.00	
	• • 0 4	0	114.75	114,27	1141	34	22.00	-
	-8 <b>4 4</b> -8 <b>7</b> 2	0	114,50	114,25	1144	34	21.33	•
	, 30	0	115,25	114.91	1148	35	22.00	•
<u>,0</u> -	• 10	0	114,20	115,31	1151	35	22.00	•
EV FV	•,11	0	110,/5	119,68	1155	35	22,00	~
5	*•U7 43	0	110,20	116.03	1158	35	22.00	•
	• ۲۰ _ ۱۵	-0	117./2	110,36	1162	34	22.00	•
5	- 37	Ű	110,20	110,09	1165	34	22.00	•
5	- 64	U	110,/0	11/+04	1168	34	22.00	-
		U	110,4/2	11/,04	1172	34	22.00	•

S.3 <u>Satellite Position Data Listing</u>. The satellite position data listing was produced during the simultaneous mode satellite position calculation (program PASS3). In order to provide an easily read printout format, four sheets were used.

Sheet 1:

H, M, S, MS

TRACKERS

Time recorded by station 1 which was used as the time reference in hours, minutes, seconds, and milliséconds The four numbers indicate which of the four tapes were time-synched (e.g. 1234 if all four tapes were synched; 1230 if tapes 1, 2, and 3 were synched)

RANGE 1, AZ 1, EL 1 Range, azimuth, and elevation as determined from the input survey data and the satellite position using the ranges from stations 1, 2, and 3. This information is included for each of the four stations.

Sheet 2:

H; M, S, MS

LATITUDE.

LONGITUDE,

HEIGHT

as on sheet 1

Time in hours, minutes, seconds, and milliseconds

Latitude, west longitude, and height of the satellite as determined using stations 1, 2, and 3 in units of degrees and meters

EQ VELOCITY

Equatorial velocity determined from the ranges and range rates of stations 1, 2, and 3 in units of meters

S-8

per second

Sheet 3:

The corrections determined for each of the four stations are listed on this

TROPO REFR

The tropospheric correction computed using the analytic model (subroutine REF). The correction is printed in meters and must be subtracted from the smoothed range.

MEASURED IC

COMPUTED IC

lonospheric correction from the edited and smoothed data tapes. This correction is printed in meters and must be subtracted from the smoothed range (if used). lonospheric correction computed using the analytic model (subroutine IONCR). This correction is in meters, and must be subtracted from the smoothed ranges.

TRANSIT TIME

Transititime correction which makes the ranges correspond to the indicated time (computed in program PASS3). The correction is in meters and must be added to the smoothed ranges.

Sheet 4:

LSSQ OF PER -Average latitude, west longitude, and height of theMUTED SOLU -satellite determined from the four permuted solu-TIONStions.

VARIATION OF Difference of the latitude, longitude, and height of PERMUTED each permuted solution and the LSSQ or average SOLUTIONS FROM solution.

LSSQ

COMBINATION

The stations used in the four permuted solutions are:

123, 124, 134, 234.

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## GEODETIC SECUR USA 2 SATELLITE POSITION ORBIT I GRAND FORLS I SAN D

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					ROSIIN	i.	GORND	rvngð	1	
	н	M	S MS	TRACKERS	RANGE 1 AZ 1	EL 1	RANGE 2	AZ 2	FL 2	RANGE 3
1	14	92	8 348	1 2 8 4	2162010 307.3	16.8	2057921	241.7	18.7	1217863
Ż	14	9 2	8 548	1234	2162112 307.4	16.8	2056852	241.7	18.7	1218540
3	14	9 2	8 748	1234	2162200 307.4	16.8	2055743	241.7	18.8	1219417
4	14	92	8 949	1234	2162302 307.4	16.8	2054714	241.8	18.8	1220295
5	14	9 2	9 440	1234	2162390 367.5	16.8	2053646	241.8	18.8	1221174
t	54	0 0	9 348	1234	2102492 307.5	16.8	2052578	241.8	18.8	1222094
7	14	0 2	Q SAA	1234	2162593 307.6	16.8	2051510	241.8	18.8	1222934
8	14	9 2	9 748	1234	2162691 307.6	16.8	2050442	241.8	18.9	1223816
9	14	0 2	0 010	1234	2162791 307.6	16.8	2049375	241.8	18.9	1224698
4.0	14	ģ 3	0 440	1234	2162891 307.7	16.8	2048308	241.9	18.9	1225581
41	14	93	0 348	1234	2162992 307.7	16.8	2047242	241.9	18.9	1226465
12		03	0 548	1 2 3 4	2163094 307.8	16.8	2046175	241.9	19.0	1227350
3	14	93	n 748	1234	2163196 307.8	16.8	2045110	241.9	19.0	1228235
14	14	93	n 049	1234	2163300 307.8	16.8	2044044	241.9	19.0	1229122
15	14	93	1 140	1 2 3 4	2163403 307.9	16.8	2042979	242.0	19.0	1230009
46	14	93	1 348	1 2 3 4	2163568 367.9	16.8	2041914	242.0	19.0	1230897
17	14	93	1 548	1 2 3 4	2163614 308.0	16.8	2040849	242.n	19.1	1231786
48	14	93	1 748	1 2 3 4	2163720 308-0	16.8	2039784	242.0	19.1	1232675
19	14	93	1 049	1234	2163827 308.0	16.8	2138720	242.0	19.1	1233565
20	14	93	2 149	1234	2163935 3n8.1	16.8	2837657	242.1	19.1	1234457
21	14	93	2 348	1234	2164044 308.1	16.8	2036593	242.1	19.9	1235349
22	14	9 3	2 548	1234	2164153 308.2	10.8	2035530	242.1	19.2	1236242
23	14	93	2 748	1234	2164264 308.2	16.8	2034467	242.1	19.2	1237136
24	1.4	93	2 949	1234	2104375 308.2	16.8	2033404	242.1	19.2	1238031
25	14	93	3 149	1234	2164480 308.3	16.8	2032341	242.2	19.2	1238926
26	14	93	3 348	1234	2164598 308.3	16.5	2031200	242.2	19.2	1239822
27	14	93	3 548	1234	2164712 308.4	16.8	2030218	242.2	19.3	1240719
28	14	93	3 748	1234	2104820 308.4	16.8	2029156	242,2	19.3	1241617
29	14	93	3 949	1234	2104941 308,4	16,8	2028095	242.2	19.3	1242516
36	14	93	4 149	1234	2165057 308,5	16,8	2027034	242,3	19.3	1243415
31	14	93	4 348	1234	2165174 308,5	16,8	2025974	242,3	19.3	1244315
32	14	9 3	4 548	1234	2165291 308.6	16,8	2024913	242,3	19.4	1245217
33	14	93	4 748	1 2 3 4	2165410 308,6	16,8	2023853	242,3	19.4	1246119
34	14	.9 3	4 949	1234	21,65529 308.6	10.8	2022793	242,3	19.4	1247022
35	14	93	5 149	1234	2165645 308.7	16.8	2021734	242,3	19.4	1247925
30	14	93	5 348	1234	2165768 308.7	16.8	2020674	242.4	19.4	1248830
37	14	93	5 548	1234	2165889 308.8	16.8	2019615	242,4	19.5	1249735
38	14	93	5 748	1234	2166011 308,8	16.8	2018557	242.4	19.5	1250641
39	14	93	5 949	1234	2166133 308.8	16.8	2017498	242.4	19.5	1221548
40	14	93	6 149	1234	216627/ 308.9	16.8	2016440	242.4	19.3	1272475
41	14	.9 3	6 348	1234	2100301 308.9	10.0	2012383	242,9	19.0	1223303
42	14	93	6 548	1234	2100000 309.0	10.8	2014326	242,5	19.6	12242/2
4.5	14	93	56 748	1234	2100002 309.0	10.8	2813209	242.5	19.0	1222192
44	14	93	56 949	1204	2100/79 309.0	10,0	2012212	242,5	19.0	1220092
42	14	93	5/ 149	1234	2100000 309,1	10,/	2011120	242.7	17.5	1257003
40	14	93	348	1234	210/017 309.1	10./	2010100	242.0	19./	122/910
¶/ / u	14	93	7 770	1204	210/170 309.2	10./	2007074	672.0	17./	1220029
90	14	93	5/ /70	1234	210/2/2 309.2	10./	200/908	272.0	17./	1229/93
<b>₩</b>	14	93	o/ 949 10 .≜≏	1204	210/704 304.2	10,/	200723	240 4	17./	120007/
70	19	- Y (	199	1204	210/207 307.3		2002010	240 7	] 7 4 /	12012/3
21 50	- 14	Y .	00 370 10 870	1204	210/000 307.3	10.7	200-023	240 7	14.0	1002977
フィー・	14	9 7 6 7	טעב סו ישב או	1234	210//77 309.3	10,/	2000/08	242 7	12.0	1200900
20 # 4	19	У. У.	סק∕ סי סבי מי	1 2 9 4	210/700 007.4	10,/	£U02/19	676.1 949 7	12.0	1207329
24	17	- <del>У</del> 3	NO 949	1294	51000u/ 307.4	19./	2001000	646.1	] 7 • 0	8202545

SATELLITE POSITION ORBIT 1319

						PAGE	4	
GRAND	FORLS	I	SAN D	IEGO	I	l	ARSON	AFB
_						-		
RANGE 2	YZ 5	FL 2	RANGE 3	AZ 3	FL 3	RANGE 4	AZ 4	FL 4
2057921	241.7	18.7	1217663	17.0	46.0	1388796	4 55 . 4	37.3
2056852	241.7	j8.7	1218540	17.0	46.0	1388691	155.0	37.3
2055733	241.7	18.8	1219417	17.0	45.0	4387386	455 .	17 1
2054714	241.8	18.8	1220295	17.0	45.9	4384682	454 0	17 4
2053646	241.8	18.8	1221174	47.4	45. B	1385070	464 0	37 4 T
2152578	241.8	48.8	1222054	47.4	45 8	100/7/7		77 4
2051510	241.6	18.8	4 2 2 2 0 3 4	17.1	45 7	1002277	177.0	3/+9 77 E
2050442	244.8	48 0	4 7 2 3 8 4 6	1/01		13043/3	124.0	
2149375	24 8	48 0	1450010	1/+1		13030/9	129./	-3/+2
2548358	241 0		1627070	1/+1		13831/0	129.7	3/.9
2447242	244 0	10.7	1222201	1/+1		1382477	174.0	37.5
2046176	244 0	10.7	1/20403	1/11	42.2	1381/80	124.0	37.6
2045314	244 0	17.0	122/020	1/ • 1	42.9	1381083	124.5	37.6
2044044	244 0	19.0	1220235	1/-1	72.5	1380388	154.5	37,6
2.42070	271,9	19.0	1229122	17.1	42.3	1379693	154.4	37.7
20729/9	272.0	19.0	120009	17.1	45.3	1379000	154.3	37,7
2071917	242.0	19.0	1230897	17.1	45.2	1378308	154.3	37,7
2040049	242.0	19+1	1231786	17.1	45.2	1377616	154.2	37,8
2039754	242.0	17.1	1232675	17.2	45.1	1376925	154.2	37,8
2038/20	242.0	19.1	1233565	17.2	45.1	1376236	154.1	37,8
2037057	242.1	19.1	1234457	17,2	45.0	1375547	154.1	37.8
2036293	242.1	19.1	1235349	17,2	45.0	<u>;</u> 37486n	154.0	37.9
2035530	242.1	19.2	1539545	17.2	44,9	1374173	154.1	37.9
2034467	242.1	19,2	1237136	17,2	44.9	1373487	153.9	37.9
2033404	242.1	19.2	1238031	17.2	44,8	1372803	153.9	38.0
2032341	242,2	19.2	1539959	17.2	44.7	1372119	153.8	38.0
2031280	242.2	19.2	1239822	17.2	44.7	1371437	153.7	38.0
2030218	242,2	19.3	1240719	17,2	44.6	1370755	153.7	38.1
2029156	242,2	19.3	1241617	17,2	44.ŏ	1370074	153.6	38.1
2028095	242.2	19.3	1242516	17,2	44,5	1369394	153.6	38.1
2027034	242,3	19.3	1243415	17.2	44.5	1368716	153.5	38.2
2025974	242,3	19.3	1244315	17.3	44.4	1368038	153.5	38.2
2024913	242.3	19.4	1245217	17.3	44.4	1367360	153.4	38.2
2023853	242.3	19.4	1246119	17.3	44.3	1366684	153.4	38.2
2022793	242,3	19.4	1247022	17.3	44.3	1366019	153.3	38.3
2021734	242,3	19.4	1247925	17.3	44.2	1365336	153.2	38.3
2020674	242.4	19.4	1248830	17.3	44.2	1364663	153.2	38.3
2019615	242.4	19.5	1249735	17.3	44.1	1363992	153.4	38.4
2018557	242.4	19.5	1250641	17.3	44.1	1363321	153.4	38.4
2017498	242.4	19.5	1251548	17.3	44.0	1362652	153 0	38.4
2016440	242.4	19.5	1252455	17.3	44.0	1361983	153.0	38.5
2015333	242.5	19.6	1253363	17.3	43.9	1361315	152.0	38.5
2014526	242.5	19.6	1254272	17.3	43.9	1360648	152 A	38.5
2013269	242.5	19.6	1255192	17.3	43.8	1350082	152 8	18.5
2012212	242.5	19.6	1256092	17.3	43.8	1359318	152 7	38.6
2011156	242.5	19.6	1257003	17.4	43.7	1358654	452 7	<b>18 6</b>
2010100	242.6	19.7	1257916	17.4	43.7	1357000	499 4	19.0
2309144	242.6	19.7	1258829	17.4	43.6	1357334	152 K	18 7
2007988	242.6	19.7	1259743	17.4	43.6	1354440	エイルック しょうり 見	
2.100933	242.6	19.7	1260657	17.4	43.5	1356	1-6,7	10+1
2415878	242.6	19.7	1201573	17.4	43.5	4355384	1 · · · · · · · · · · · · · · · · · · ·	10)/ 18 0
2014823	242.7	19.8	1262449	47.A	43.4	4354608	ג≁€•7 ∗50 %	30,0 J0,0
2003708	242.7	10.6	1263406	47.4	47 4	1754-34	116.0	-70.0 72.0
2002714	242.7	19.A	1264324	47.4	43.7	1024890	176.0	-70,0 70,0
2004664	242 7	1740 40 0	1209067	1/19	70,0 A 7 7	1000000	172.2	00+00
トリリスタック	5 7 <b>6 1</b> 7	3740	1641676	1/+7	70.0	えいコン/2つ	172.2	30,8

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				1	ENDETIC SI	ECOR	USA 2	SATELLITE	POSITION	ORHIT 13
	н	H S	MS	LATITUDE	LONGITUDE	HEIGHT		Xe	YĘ	
1	14	9 28	348	39,1712	114,6279	925569	-236245	8,55 -	5153421.48	45917
2	14	9 28	548	39,1817	114.6221	y25574	-236159	1.78 -	5152901.79	45927
3	14	9 28	748	39,1921	114,6164	¥25579	<b>-236</b> 072	4,59 -	5152381.43	45938
4	14	9 28	949	30.2025	114.6106	925583	-235985	7.29 -	5151860.62	45941
5	14	9 29	149	39.2129	114.6048	42 <b>538</b> 8	-235899	0.14 -	5151339.90	45958
6	14	9 29	348	39.2234	114.5990	¥25592	-235812	2.65 •	515,818,50	45961
7	14	9 29	548	39.2338	114.5932	925597	-235725	5.07 -	5150296.99	45975
8	14	9 29	748	39.2442	114.5875	925601	-235638	7 45 .	5149775.42	45981
y	14	9 29	949	39,2546	114.5817	925000	-235551	9 79 -	5149253.82	46001
10	14	9 3 ก	149	39.2651	1 4 5759	¥25610	-235465	2.22 -	5148731.72	46011
11	14	9 3 ň	348	39.2755	414,57n1	925615	-235378	4,45 +	514H2n9.62	46021
12	14	9 30	548	39.2859	114.5643	925620	-235291	6.50 -	5147687.15	46031
13	14	9 30	748	39,2963	114,5585	925624	-235204	8.46 -	5147164,85	4504
14	14	9 30	949	39.3068	444.5527	925629	-235118	n.26 ·	5146542.35	46051
15	14	9 31	149	39.3172	114.5469	¥25633	-235631	1.88 -	5146119.92	46061
16	14	9 31	349	39.3276	144.5411	925638	-234944	3.51 -	5145597.12	4607
17	14	9 34	544	39.3380	444.5353	925642	-234857	5.07 -	5145073.66	4608;
18	14	9 31	748	39.3484	414,5295	925647	-234770	6.40 -	5144550.37	4609
19	14	9 34	949	39.3589	414.5237	925651	-234683	7.85 -	5144026.95	461 02
20	14	9 32	149	39.3693	114.5179	925650	-234596	לח.9	5143503.54	4611
21	14	9 32	348	39.3797	444.5121	92566n	+23451 a	n.14 =	5142979.68	4612;
22	14	9 32	548	39.3911	444.5063	925665	-234425	1.16 -	5142455.51	4613
23	14	9 32	74R	39.4005	114.5005	92567 n	-234336	1.93 0	5141931.20	46141
24	14	9 32	949	39,4110	114.4946	¥25674	+234249	2.45 -	5141406.89	46150
25	14	9 83	149	39.4214	414.4888	925679	-234162	2.98 -	5141882.54	46164
26	14	9 33	348	39.4318	444.4830	¥25683	-234075	3.47 -	5140358.10	46170
27	14	9 33	548	39,4422	444.4772	725688	-233988	3.88	5139833.18	4618!
28	14	9 33	748	39,4526	444.4713	925692	-233903	4.17	5139307.72	4619
29	14	9 33	949	39,4630	444,4655	925697	-233814	4 45 -	5138782.54	4620
3.	14	9 34	149	39,4735	4 4 4 4 5 9 7	Y25702	-233727	4.66	5138257 16	4621
31	14	9 34	348	39.4839	444 4539	9257n6	-233640	4 74 -	5137734 04	4522
32	14	9 34	548	39,4943	114.4480	425710	-233553	4 51 -	5137204.52	4623
33	14	9 34	748	39.5.47	1 4 4 4422	425715	-233466	4 3 4	5136678 30	4624
34	14	9 34	040	39,5151	444 4364	925721	-233374	3 89	5135154 84	4625
35	14	9 39	440	30 5256	444.4305	2-5724	-233292	3 66	5135625 59	4626
30	14	0 34	349	39.5360	444 4247	925729	-233205	4 98 -	5134099 20	4627
37	14	9 m.#	548	39 5464	444 4488	Y25734	-233118	- 88 -	5134572 87	4628
38	14	9 75	748	30 5568	444 4130	925738	-233030	0,00 0,65	5134046 21	4629
39	14	9 35	949	39.5672	114.4071	925743	-232943	H 39 -	5133510.16	4630
4 n	14	9 34	149	39.5776	144.4013	9-5748	-232856	7 20	5132992.11	4631
41	44	9 34	348	39.5880	444 3954	925752	-232769	A. 1.4	5.30464 47	46.52
42	14	9 34	548	39.5984	444.3896	925757	+232682	5.3	5.3.936.43	4633
4.5	14	9 34	748	39.6689	114,3837	925761	-232595	3 84	5131408 13	4634
44	14	9 14	949	39.6493	444.3779	425766	=2325nd	12.5n -	543.886.18	4635
45	14	9 17	49	39.0297	444.3720	925771	-232421	0.90	5+3-359.37	4636
40	14	Q 37	348	39.54.1	444.3662	925775	-232333	59.n7 •	5420824.05	4637
47	14	<b>y x</b>	7 55.	39.65.5	414.3563	72578n	-232246	5.84	5199905 49	4638
48	14	9 17	775.	39.66.9	444.3544	925784	-232450	4.36 -	549876A 7A	464.
4.0	47	0 11	/ 0∡0	30.6743	11400-44K	9257RJ	-208127		5.04010 +10	4040
5.	4 4	0 11 0 11		30.64.7	1341.1407	9,5704	-20EU/C		-149630+1/ 5+977x8 A8	4645
- U 5	4 4	0 1	· 177	30.6004	11-10-E/	425704	-21207	・ テ・エル 1人 万ち -	-16//J0500 5457478 47	4422
52	14	9 11	- 501 1 58-	30.7.06	114.3340	425802	- E J 1''7' • 2 % e % e .	393 -	5. 26844 AT	4643
53	44	0.30	1 76-	30.7470	144.3054	925847	-01-701	j⊌ą≠++ {ą_34 _	5496446 40	4645
54	11	- Q 71		39.7534	11-100-1	925844	-23-635	71.07 A 70	5425588 -0	4848
-	Τ.	,		· · · · · · · · · · · · · · · · · · ·	TTAINTER	- 4 <del>-</del> 4 <del>-</del> 7 - 1			-12/2/0+07	1010

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בריבולא בהיצע ההוציינובולישילומילוביניביביילוביניביילייביויבילייביויבילייביי

SATELLITE PO	DSITION
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			PA	GE 4	t
Xe	YE	ZE		EO. VE	FLOCITY
2428.22	-5153421.48	45 <u>91</u> 765.12	4335	2000	5155
1591.78	-5152901.79	4592795.91	4335	2501	5154
0724.59	-5352381,43	4593826,59	4336	2603	5153
29857.29	-515186 <u>0</u> ,62	4594857.14	4336	25 .4	5152
8940.14	-5151339.90	4595887,54	4337	26,5	5152
8122.65	-515n818,50	4596917.93	4337	2607	5151
7255.07	•5150296.99	4597948 n4	4338	2607	5150
6387 48	-5149775 42	4598977 <b>Š</b> 6	4338	2608	3149
5519,79	-5149253 82	460007.62	4339	26.9	548
4652.22	-5148731 72	4601037.19	4339	2010	5147
3784.45	-51442n9.62	4002066 59	4340	2514	5.46
2916,50	-5147687.15	4613095.68	4340	2012	5445
2048.46	-5147164 85	4614124.53	4341	2512	5.43
1180.26	-5146642.36	4605153.07	4341	2613	5442
0311.88	-5146119.92	4606181.26	4342	2014	5441
9443 51	-5145597.12	4607209.31	4342	2645	5440
8575 07	-5145073.66	4608237.33	4343	2646	5120
7706.40	-5144550.37	4609265.11	4343	2617	8438
68.57.85	-5144026.95	461 0292 57	4344	264.8	5100
5969 05	+5143503.54	4611320.03	4344	2649	5,37
5100.14	-5142979.68	4612347.44	4345	2620	5136
4231.16	-5142455.51	4613374.71	4346	2620	5135
0361.93	·5141931.2n	4614404.71	4346	2624	5+34
2492.45	-5141406.81	4615428.32	4347	2622	5.33
1022,98	-5141882.54	4616454.68	4347	2623	5432
0753.47	-5140358.16	461748n.75	4348	2624	5131
9883.88	-5139833.18	4618205.94	4348	2625	5130
9014.17	-51393n7.72	4619533.07	4349	2626	5130
81.44 . 45	-5138782 54	462n558.82	4349	2628	5129
7274.60	-5138257,16	4621584 47	4350	2629	5128
6404.74	-5137731.04	4622611,15	4351	2630	5127
5534 51	-5137204,52	4623635 84	4351	203n	5127
4664 34	-5136678,3 ₀	4624661.17	4352	2631	5126
3793.89	-5134151.84	4625686.30	4353	2632	5125
2923.06	-5135625,59	4626711.05	4354	2632	5123
2021.98	-5135099.20	4627735 56	4355	2633	5122
1180.88	-5134572.87	4528759.84	4355	2633	5121
0318.65	-5134046.21	4629784 03	4356	2635	5120
9438 39	-5133519,16	4631808,05	4356	2636	5119
8507.20	-5132992.11	4631831.73	4356	2637	5119
7.696.14	-5132464.47	4632855,23	4356	2639	5117
6825.13	~ ⁵ 131936,43	4633878,53	4357	2639	5116
5953.84	-5131408,13	4634901.64	4358	2440	5115
2042.20	-513n840.18	4635924.49	4358	2641	5114
1210.90	-513n352.37	4636947 <b>.</b> 20	4359	2641	5114
3339.0/	-5127824.05	4637969,84	4360	2643	5113
400,04	->129295,49	4638992.38	4361	2644	5112
124.30	-5128766.70	4640014.77	4362	2545	5112
0/21./2	-2123238,17	4641037.09	4362	2646	5111
7849.12	->1277 ₀ 8.63	4642059.34	4363	2647	5110
RY/0,22	-5127178.87	4643081.35	4363	2549	5102
0115.95	-2126648,43	4644103,22	4363	2550	5108
1231.34	-212/116,19	4645124.70	4363	2451	3107
0378,10	-2120548.09	4040145,99	4363	2652	5106

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SATELLITE POSITION

ORBIT TROPO, REFR. CURR. 4.7 7.9 3.1 MEASURED IC COMPUTED I 7.9 14.3 25.2 3.1 25.5 16.0 1 36.2 64.6 37,7 15, 23.4 14.3 4,7 15.3 2 26.2 35,5 3.1 37.7 15, 64 5 23.4 4.7 7,9 3 14.3 113.8 75,5 35.5 3.1 15.3 64,4 37,7 15, 23.4 4 14.3 4.7 7.9 3.1 25.2 10.0 36,8 15. 64,3 37.6 23.4 5 14,3 4.7 7,9 30.2 15.3 3.1 23.8 36,8 64,2 37.6 15. 23.4 6 14.2 4.7 7,9 14.0 3,1 26.2 23.2 35.5 37.0 15. 64,2 23.4 7 14.0 4.7 14.2 7,8 3.1 99,0 25.2 36.2 64.1 23.4 37.0 15. ð 14.2 14.7 4.7 7,3 3.1 36,8 30.2 24.5 64.0 37,5 15. 23.4 9 14.2 4.7 7,8 25.2 3.1 27.5 35.5 14.7 23.4 63.9 37.5 15. 10 14.2 4.7 7.8 3.1 125.5 23.8 37.5 14.7 63.8 37.5 23.3 15. 14+1 4.7 7.8 11 3.1 86.2 24.5 35.5 15,3 23.3 15. 63.8 37,5 12 7.8 14.1 4.7 3.1 64.5 24.5 35.2 13.3 23.3 63,7 37.4 15. 13 14.1 7,8 4.7 39,5 3.1 36.2 14.7 23.8 63.6 23.3 37.4 15. 14 7,8 14.1 4,7 34.9 24,5 3.1 36,8 14.7 63,5 37.4 15, 23.3 15 14.1 4.7 27.0 3.1 23.8 15.3 36.2 63.4 23.3 37.3 15. 16 14.0 4.7 7.8 22.2 3.1 24.5 36.2 10.7 37.3 63,4 23.3 15.! 17 14.0 7,8 4.7 3.1 20.8 23.8 36.2 10.0 37.3 15.! 63.3 23.3 14.0 18 7.8 4.7 8.2 3.1 24.5 35.5 16.0 37.3 63,2 15,! 23.3 19 14.0 4.7 7.8 .22.2 3.1 23.8 35,5 16.7 63,1 37,2 15.! 2**3.3** 14.0 20 4,7 7.8 3.1 51.5 25.2 36.8 10.7 63.U 23.3 37,2 15,! 13,9 7.8 21 4.7 76,8 23.8 3,1 36.2 10.0 63.0 37.2 15.! 23.2 13.9 22 7,8 7,7 10.1 4,7 25 2 23 A 97,5 36.2 3,1 62,9 27.2 15,! 23.2 23 13.9 4,7 36,2 3,1 34.2 15.3 62.8 37.1 23.2 15,! 24 13.9 4.7 7.7 25.2 12.8 3.1 31.5 15.3 37.1 62.7 15.! 23.2 25 13.9 4.7 7.7 23.8 52.8 14.0 3.1 36.2 37.1 62.7 23.2 15.1 26 13.8 7,7 4,7 94,8 25,2 3.1 36.2 16.0 62,6 23.2 15.1 37.1 27 13.8 24.5 4.7 7,7 3.1 36,2 10.0 36,8 37.0 62,5 15.1 23.2 25.2 28 13.8 4.7 7.7 18.2 3.1 16.7 35.5 62.4 37.0 15.1 23.2 29 13.8 4.7 25.2 7.7 66,8 3.1 16.0 34.8 62.3 23.2 37.0 19,1 4.7 30 13.8 7.7 3,1 109.7 24.5 35.5 12.3 62.3 15,0 23,2 36.9 31 13,7 4.7 7,7 25.2 35,5 3,1 1⁴.0 130.0 62,2 36.9 23.2 15.0 4.7 32 13.7 7.7 24.5 14.0 3.1 18,8 35,5 62.1 36,9 23.2 15.6 33 13.7 4.7 7,7 23.8 3.1 28,8 15.3 36.5 62.0 23.1 36,9 15.4 34 13.7 4.7 68.2 7,7 3.1 23.8 35.5 15,3 62.0 23.1 15.6 36.8 35 13.7 4.7 7.7 3.1 95.5 23.8 35.5 14.7 61.9 15.6 23.1 36.8 13.6 4.7 30 7,7 24,5 3.1 122.ª 34,8 15.3 61.8 23.1 36,8 15.4 37 13.6 4.7 7.7 3,1 21.5 23.8 36.2 16.9 61.7 23.1 36,8 15.0 33 13.6 4.7 7.7 6.5 24.5 3,1 36.2 10.0 61.7 23.1 36.7 15.6 39 13.6 4.7 7.6 23.8 14.2 34,8 3.1 16.7 23.1 61.6 36.7 15.6 7.6 4 ႐ 13.6 4.7 12.2 3.1 23.8 36,8 15.5 61.5 36,7 23.1 15.6 41 13.5 4.7 7.6 3.1 18,8 24.5 36,2 16.0 23.1 61,4 36.7 15.6 7.6 42 13.5 4.7 3.1 18.5 24.5 36.2 15.7 61.4 23.1 36.6 15,6 43 13.5 4,7 7.6 22.2 3.1 23.8 3%.5 15,3 61.3 23.1 36,6 15.6 44 4.7 13.5 7.6 3.1 12,5 24.5 36.2 15.3 23.1 61.2 45 36,6 15.6 13.5 4.7 7,6 13,5 24.5 3.1 36,2 16.7 23.0 61.1 36,5 15.6 7,5 46 13.4 7,6 4.6 24,5 3.1 36.8 15,3 36.5 61.1 23.0 15.0 47 13,4 7.6 4.0 24 5 3,1 21.7 35.5 15,3 15.0 61.0 23.0 36,5 13.4 48 7.6 4.6 3.1 41.5 24.5 36.8 17.3 23.0 36,5 60.9 15.6 7.0 49 13.4 4,6 3,1 24.5 19.0 122,2 36.8 23.0 60.8 36.4 15.6 50 13.4 7,6 4,6 3.1 23.8 112.3 35.5 16.0 60.8 36,4 23.0 15.0 51 7,6 13.4 4.6 3.1 99,5 23.9 36.2 16.7 80.7 23.0 36,4 15.6 52 13.3 7,6 4.6 3.1 24 5 23 8 70, " 36.2 15.0 23.0 69.6 36,4 15.6 53 13.5 7,6 4.6 3,1 32.2 35,5 23.0 10.7 60.5 15.7 36.3 13.3 54 7,6 4.6 16.2 3.1 23.2 35.2 15.3 60.5 23.0 36,3 15.7

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SATELLITE POSITION ORBIT 1255 PAGE ÍSURED IC COMPUTED IC TRANSIT TIME CORR. 64,6 16.0 23.4 37,7 15,5 -55.7 -21.2 -39,9 15.3 15.3 64.5 37.7 23.4 15.5 -55,7 -21,2 -39,9 64.4 37,7 23.4 15.5 -55,6 -21.1 -39,9 10.0 64.3 23.4 37,6 15,3 -55,6 -21,1 -39,8 15.3 64.2 23.4 37.6 15.5 -55,6 -21.0 -39,8 14.0 7.9 64.2 23.4 37.0 15.5 -55,5 -21,0 -39,7 8.0 14.0 64.1 23.4 37.0 15.5 -55.5 -20.4 -39.7 3.0 14.7 64.0 23.4 37.5 15.5 -55.5 -20.9 -39.7 8.1 14.7 63.9 23.4 37.5 15.5 -55.4 -20.8 -39.6 8.2 14.7 53.8 37.5 23.3 15.5 -55.4 -20.7 -39.6 8.3 15.3 53,8 23.3 37,5 15.5 -55.4 -20.7 -39.5 8.3 13.3 63,7 23.3 37.4 15.5 -55.4 -20.6 -39.5 8.4 14.7 63,6 23.3 37.4 15.5 -55.3 -20.6 -39.5 A. 3 14.7 63,5 23.3 37,4 15,5 -55.3 -20.5 -39.4 A . 5 15.3 63.4 23.3 37.3 15.5 -55.3 -20.5 -39.4 8.6 10.7 63.4 23.3 37.3 15.5 -55,2 -23,4 -39,4 9.7 16.0 63,3 -55.2 -20.3 -39.3 23.3 37,3 15.5 8.7 16.0 63.2 23.3 37.3 15.5 -57.2 -20.3 -39.3 A.8 16.7 63,1 53.3 37,2 15.5 -55.2 -20.2 -39.2 8.9 10,7 63.0 23.3 37.2 15,5 -55,1 -20,2 -39,2 8.9 10.0 63.0 23.2 37.2 15.5 -55.1 -20.1 -39,2 9.0 10.0 62.9 23.2 -55.1 -20.1 -39.1 37.2 15,5 9.1 62.8 23.2 37,1 -55.0 -20.0 -39.1 15,5 9.1 17,3 62.7 37,1 23.2 -55.0 -20.0 -39.0 15.5 14.0 9.2 62.7 37.1 23.2 -50.0 -19.9 -39.0 15.6 9.3 16.0 37.1 62.6 23.2 15.6 -55.0 -19.8 -39.0 9.3 10.0 62.5 37.0 23.2 15.6 -54.9 -19.8 -38,9 9.4 16.7 62.4 23.2 37,0 -54,9 -19,7 -38,9 15.6 9.5 16.0 62.3 23.2 37.0 15.0 -54,9 -19,7 -38,9 9,5 15.3 62.3 23,2 36,9 15,6 -54,8 -19,6 -38,8 9.6 14.0 62.2 36.9 23:2 15.6 -54.8 -19.6 -38.8 14.0 9.7 62.1 23.2 -54.8 -19,5 -38.8 36.9 15,6 9.7 15.3 62.0 23.1 36,9 -54,8 -19,5 -38,7 15.6 9 . A 15.3 62.0 23.1 36.8 -54.7 -19.4 -38.7 15.6 9.9 14.7 23.1 61.9 36.8 -54.7 -19.3 -38.6 15.6 4.9 15.3 61.8 23.1 36,8 15.6 -34.7 -19.3 -38.6 19.9 16.0 61.7 36,8 23.1 12.0 -54.6 -19.2 -38.5 23.1 10.1 10.0 36.7 61.7 -54.6 -19.2 -38.5 15.6 10.1 16.7 61.6 23.1 36,7 15.6 -54.6 -19,1 a38.5 11.2 15.5 23.1 61.5 36,7 15.6 -54.6 -19.1 -38.4 10.3 10.0 23.1 61.4 36.7 15.6 -54.6 -19.0 -38.4 10.3 10.7 61.4 23.1 15,6 36.6 -54,5 -18,9 -38,4 10.4 23.1 15.3 61,3 35,6 15.6 -54.5 -18.9 -38.3 10.5 23.1 15.3 61.2 36,6 15.6 -54,5 -18,8 -38,5 10.5 16.7 23.0 61.1 36,5 15.6 -54.4 -18.8 -38.3. 10.6 15.3 23.0 61.1 36.5 15.6 -54,4 -19,7 -38,2 10.5 15.3 23.0 61.0 30.5 15.6 -54,4 -18,7 -38,2 10.7 15.3 23.0 60,9 36.5 15.6 -54,4 -18,6 -38,1 10,8 10.0 23.0 15.6 00.8 36.4 -54.3 -18.6 -38.1 16.0 10.8 53.0 60,8 36.4 -54.3 -18,4 -38,1 19.9 16.7 23.0 60.7 36.4 -54.3 -18.4 -38.0 - 11.0 15.6 2 15.0 15.6 23.0 60.6 36.4 -54.2 -18.4 -38.0 -54.2 -18.3 -38.0 5 **11.** n 23.0 60.5 36,3 15.7 11,1 2 15.3 60.5 23.0 36.3 15.7 -54.2 -18.3 -37.9 11.2

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	LSSO OF PERMUTED SU	LUTIONS	VARIATIO	N OF	PER	MUTED S	SOLUTIONS	FROM	LSSO	CONI
1	39.1712 114.6279	925570	.8000 .000	n	-1	• 0 0 0 0	*** 0 0 0 0	1		
2	39.1817 114.6221	925575	.000. 000.	Ď	-0	.0000	0000	õ	0000	•1
ۍ	39.1921 114.6164	925579	.0000 .000	0	- 0	.0000	0000	ů.	0000	
4	39,2025 114,6106	925584	.0000 .000	• n	- 0	.0000	0000	ň		
5	\$9.2129 114.6048	925588	.0000 .000	ñ	- 0	.0000		ñ		
6	39,2234 114,5990	925593	.6000 .000	n n	-1	.0000	~.0000 ···	٠ •		
7	39,2338 114 5932	925597	.0000 .0000	n	-1	. 0.000		4	ñ n n n	
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Ŷ	39, 2546 114, 5817	925006	.0000 .000	n	= 0		~.0000	4		
10	39.2651 114.5759	925644	.0000 .000	0 N	-1	.0000	0000	1	~_0000	
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17	39 3380 114 5353	925643	000. 6000.	0	~1	. 0000	- 0000 -	1	0000	
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21	39, 3797 114 5121	025661	.0000 .000	0	- U	. 3000		U O	0000	
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24	39.411n 114.4946	025074		n N	-0	.0000		0	0000	•
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29	39.463n 114.4655	925097	0000000	0 7)	ň	0000	40000	- 6	.0000	- 9 - 9
34	39,4735 114,4597	925701	.0000 = .000	n n	0	~.0000	.0000	- U	. 0000	
31	39,4839 114,4939	9257 65		n	U D	0000	.0000	-U 	. 0000	
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34	39,5151 114,4364	92572n	.0000 .000	0 A	-1	. 0 0 0 0	0 0 0 0	4		•
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36	39,536n 114,4247	929720	.0000 .000	0 N	ט חר	.0000	0000	, ,	+ U U U U	•
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S-13

S. 4 <u>3-3 CORDEX Solution</u>. The 3-3 CORDEX solution (program PASS4) lists a summary of results followed by a listing of each discrete solution.

TM1, FM2, TM3 These three rows indicate for each time span used:

- 1. the first time in hears, minutes, seconds, and milliseconds
- 2. the last time in hours, minutes, seconds, and milliseconds
- the time between samples in hours, minutes,
   seconds, and milliseconds
- 4. the logical tape unit on which the satellite position tape was mounted.

FST INPUT

Latitude, west longitude, and height of the CORDEX station input (survey values) in units of degrees and meters

Latitude, west longitude, and height of the CORDEX

FST AVER

station determined by averaging all the discrete

solutions in units of degrees and meters.

EST BIAS

Difference between the survey and the average coordinates of latitude, west longitude, and height in units of degrees and meters

RMS ERROR

average solution. Units are degrees and meters.

The rms of the deviations of each solution from the

The following quantities are listed for each discrete solution.

SAMP

Sample number-

S-14

LATITUDE Latitude, west longitude, and height of the CORDEX LONGITUDE, station in degrees and meters HEIGHT DEVIATION FROM Deviation of each solution from the input survey posi-INPUT POSITION tion in latitude, west longitude and beicht

INPUT POSITIONtion in latitude, west longitude, and heightDEV ATION FROMDeviation of each solution from the average solution-AVERAGE POSI-in latitude, west longitude, and heightTION

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	GFODETIC SEC	DR LNKNOWN	STATION LOCATION	LARGE QUAD
TM1 13 52 21 895	1.3 52 38	92 0 0	0 200 1	FST LNPUT
TM2 36 3 52 86	16 4 5	86 0 0	0 200 2	FST AVER
TH3 14 8 55 948.	14 9 5	848 () ()	n 200 - 3	FST BIAS
NUMBER OF SAMPLES=	50	•		RMS FRROR
	•			-
SAMP LATITURE	LONGITUDE	HEIGHT	DEVIATION FROM IN	PUT POSITION
1 47.18498	1.14,33635	336.7	000156	10n13 =33.7
2 47.18500	119.33636	340.7	600146	10012 -29.7
3 47,18502	119.33637	344.6	00/12(	0010 -25.8
4 47.18505	119.33638	350.1	000096	10009 +20.3
5 47.18569	114.33639	355.0	000056	10nng -14.8
6 47.1A51.3	119.33639	361.8	000016	10n0A -8,7
7 47.18516	119,33639	365.1	.000020	10009 -5.3
C 47.18515	119.33639	364.7	•00001 *•0	)0NN9 -6.3
9 J7.18515	114,33639	364.2	.000n1n	-6.2.
10 47.18514	114,33639	363.6	.000010	10009 <b>-6.</b> 8.
11 47.18513	114.33638	362.1	00000 <u>.</u>	)∩n09 ~8.4
12 47.18513	119.33638	360.6	000016	0010 -9.8
13 47.18512	114.33638	359.3	-*************************************	10010 -11.1 ⁻
14 47.18510	119.33638	356.3	-,00084n	innin -14.2
15 47.18508	119.33638	354.4	u0006ú	10111 -16.0
16 47.18508	119.33638	352.8	(IOUUA)	
17 47,18507	114.33638	351.0	u0007n	10010 -19.4
18 47.18507	110.33637	350.0	000170	10n1n -20.4
19 47,18507	110.33637	350.3	00007 <b>0</b>	)AA1A -20.1
20 47.18507	119.33639	352.3	000060	00009 -18.1
21 47.18508	114.33639	353.5	≓.(⊭()ປິກ <u>ຮົ</u> ⊸.ກ	10109 -16.9
22 47.18509	114.33634	355.4	000050	10.09 -14.8
	119.33640	37641	∩(U)04ŋ	10,08 -12.4
24 4/+1/8510	119,3564U 440 77470	ひつメー/	100003 10	10./ 10./
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28 47.19510	116 77673	352 A		10030 714.0 NA4E -17.6
29 47.19510	110 37632	351 6		
30 47.18510	116 33631	351.4		
31 47.18510	110 33632	352.5		
32 47.18509	114.33632	352.1	- 00005 - 0	101110 -17.9
33 47.18509	119, 33633	353.0	- 60005 - 0	-174
34 47.1.5118	119.33635	353.7	6UU06 - 6	
35 47.18508	114,33636	354.2	00006 0	
36 47.18508	114,33636	354.1	000060	
37 47.18508	110,33635	352.2	~.00006 ~.0	
38 47.18508	114.33633	350.4	000066	
39 47.18508	119.33632	348.6	000060	10016 -21.9
40 47.18507	119.33631	346.1	000070	10016 <b>-24.3</b>
41 47.18506	119.33631	345.4	000080	nn16 +25.0
42 47.18507	114.33632	346.0	000070	0016 -24.4
43 47.18507	119.33632	346.3	00007	10016 -24.1
44 47.18505	119.33633	349.1	000060	10014 -21.3
45 47-18509	119.33635	352.u	00005	0013 -18.4
46 47.1851.1	114.33637	356.7	00u03n	10011 -13.7
47 47.18514	114.33639	362-1	• (EAU) () · · · · · · · · · · · · · · · · · ·	0009 -8.3
48 47.18513	114.33639	361.3	000010	0000 -9.1
49. 47.1.R512	114.33634	359.3	000020	10njn -11.1
50 47.18511	119.33638	358.3	r0003n	innin -12.1

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S-16

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S. 5 <u>3-2 CORDEX Solution</u>. The 3-2 CORDEX solution (program PASS432) listing is identical with the 3-3 CORDEX solution listing (paragraph S. 4) except:

1. only two spans of data are used, and

2. the height of the CORDEX station is input, and not calculated, so that no error is indicated in the height.

REU. ETIC SECOR UNKNOWN STATION ふニジ วัสคา Π. <u>4 986</u> 1 200 1 51 12 151 21 1 F 71 .4 ų F5 531 ٢, Ú. 5 ていえ 5 5 137 200 F 12 7 53 NUMPER (F SYMPLES= :2 541 5-1 4717616 1 ON-1THE HEIGHT AEVIATION EROM INPI 281. A7447 287. A7441 121.0 38.06177 -. NUU41 • • • - . NUUAS 20.0.17 121.1 . 10 74.00170 26, 67447 282, 67446 <u>-.</u>00045 .01 121... 121.4 -. 06.1142 .06 28: 67446 28 47446 20. 241 41 1.21 ... -.06038 5 • 0 (+ -.00035 19.94182 1.21.1 6 • 0 0 20- 67446 121. <u>. nn037</u> 7 P. 9C1 5; 7 • 10 78,40161 1.21 . .: -.nu05n • 0 0 282.4744A 284.47447 121... 38.00171 -. 00044 • 0 () a 70.90176 121... 1 1 • • 0 0 0 4 0 • 0 0 282.47447 -.00042 38,90176 121.6 11 • 0 0 1 24: 67446 12 19.90174 121.0 -.00039 • 00 282.47445 282.47445 121.0 -.00044 13 38.90174 • 🕅 🛛 14 121.0 30.90170 . 10045 .00 284 . A7445 267 . A7444 15 38,39170 121.0 -.00045 • 0 0/ 121.0 36 308.94178 -. n004n • 11 (1 282 47445 • 7 34.901.01 121.1 -.00037 •:0'0' न्त 121." 252.67445 -.0003A 78.96181 • 0 0 19 282 47446 282 67446 79.90171 121.1 -.non4n • 🛯 🖓 26 39.00177 121." -.00041 . 1) (1 21 20- 67446 26 67447 **∝,**∩ny4n 38.9C170 • • • 121.4 77 39,90175 121.1 -.00043 . 90 23 281,47447 38.96175 121.4 - . NG 644 ំ ភ្នំ ៤ 24 282, 47445 38.96174 121.0 -.06144 . 10 -,00034 25 281, 67444 121.0 . 10 38.90182 26 39.44174 261.67445 121.11 -.00044 . 9.6 267. 47445 267. 47444 <u>. /////46</u> 121.1 ン7 38.96171 • 10 24 38.96171 121.0 - .:nn42 .18 284,67444 284,67444 29 - . 11 (1 0 45 7.0.00172 121." • 0.0. 30 28.90173 121.0 **-**.00045 • 211 26- . 47445 -<u>.naa44</u> <u>31</u> 78,0017( 121.4 <u>. ) n</u> 28. . 47444 38- 90172 121.0 • • 00045 32 . 00 26: 47444 -<u>. 11 (+ 1)</u> 4 H 33 38.96176 121.4 • 0 0 34 78.90161 121.0 -.06051 • 0 () 74,06171 35 28 . 47442 **-.**00145 121.0 • 9 6 36 38.90575 28 . 67442 121.0 -.06043 •"价化 37 38.94174 26- 47.442 - <u>. nc-144</u> 121.0 • • • • • 26, 67443 38 38.94171 121.6 -. () () 1/42 • 0.0 28- 47443 50 34.90172 -. 1101145 121.0 • 10 ĩŋ 79,96176 121.0 · . 00039 • 0.0 281.47443 38,96171 121... , npa42 41 • 70 42 79.00175 24. 17442 121.0 -. 00139 + 9 0 281, 67443 251, 67443 43 34.90174 -. 00:)44 121.1 .00 28,00171 14 -.nnj42 121.0 • 20 28: . 57444 45 1<u>21.0</u> 121.6 - . N /i (i 4 R <u>19,90171</u> <u>• 90</u> 28- . 47443 16 38.94171 -.00041 • 0.0 121." <u>- , 00045</u> 47 285, 67443 74,9617: <u>• 10</u> 26. 67442 122.0 -,01:045 68 34.91172 . 10 285 67441 4 Q 7A, 46171 121.0 -<u>, NU(141</u> • 10 121.1 •• n (i () 4 0 50 39.90169 + 0.0

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A 200         1         FT 1 VPUT         30.99718         282.67742         121.0           0 200         FST AVEN         30.99775         282.57444         121.0           FST PTAS        00132        0132        0           FSS FRADR         .00004         .0132        0           FSS FRADR         .00004         .0132        0          0044         .00135         0         .00002         .0          0044         .0135         0        00002         .0          0045         .01135         0        00002         .00002         .0          0045         .01134         0         .00007         .00002         .0          0045         .01134         0         .00007         .00002         .0          0043         .01134         0         .00007         .00002         .0          0044         .01134         0         .00007         .00002         .0          0044         .00134         0         .00007         .00002         .0          0044         .00134         0         .00007         .00002         .0          00404         .00007 </th <th>STATIUN S.</th> <th>2 )6911</th> <th>1 1 2 4 5 1</th> <th>396</th> <th>HERNDON</th> <th>,</th> <th> /</th> <th></th>	STATIUN S.	2 )6911	1 1 2 4 5 1	396	HERNDON	,	/	
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S.6 Line Crossing Listing. The span of data used in the determination of the minimum angle sum is listed with the following quantities included:

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TIME	Time in hours, minutes, seconds, and milliseconds
RANGE F, RANGE	Ranges in meters from the two stations defining the
2	baseline
HEIGHT	Satellite height in meters
GEOD SUM	Geodetic sum determined by multiplying the central
	angle sum by the scaling radius
RANCE SUM	Sum of RANGE 1 and RANGE 2
ANGLE SUM	Sum of the central angle in radians
E1, E2	Elevation angles in degrees observed at the ends of
	the baseline
RESIDUAL	Difference between the geodetic distance sum rid the
	polynomial fit in meters
LAT, LONG	Latitude and west longitude of the satellite in-degrees
Following the above	listing, the results of the line computation are printed
follows:	
MEÀS MIN SUM	Measured minimum geodetic distance sum determined
	from the polynomial fit (meters)
COMPGEODESIC	Geodetic distance (geodesic) determined from the input
	survey data

RMS The rms of the polynomial fit residuals

CENTRAL ANGLE Central angle determined from the input survey data

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SCALING RADIUS	Scaling radius determined from the computed geodesic
	and the central angle (meters)
MIN CENTRAL	Minimum central angle determined from the polynomial
ANGLE	fit in radvans

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S.7 Orbital Mode Satellite Position. The orbital mode satellite position data listing (two sheets) was obtained during the orbital prediction pass (program GSORB). The following quantities were listed:

Sheet 1:	· ·
SAMPL	Cumulative count of samples
H, M, S, MS	Time in hours, minutes, seconds, and milliseconds
LATITUDE	Predicted latitude of the satellite
LONGITUDE	Predicted west longitude of the satellite
HEIGHT	Predicted height of the satellite above the spheroid
RC	Range from the predicted satellite point to the unknown
- <u>-</u>	station
AZ	Azimuth of the predicted satellite point with respect
-	to the unknown station
EL	Elevation of the predicted satellite point with respect
	to the unknown station
ŔDC	Predicted range rate at the unknown station
Sheet 2:	
SAMPI.	Cumulative count of samples
H, M, S, MS	Same as sheet 1
RM	Measured range from the unknown station in meters
	corrected for ionospheric effects, tropospheric re-
	fraction, transit time, and calibration
RM - RC	Difference between the measured and predicted ranges
RDM	Measured range rate at the unknown station in meters
-	per second

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RDM - RDC	Difference between the measured and the predicted
	range rates
CORŢ	Transit time correction
iC	Measured ionospheric correction (correction is
 -	subtracted from the range).
CORI	lonospheric correction from the analytic model in
	meters (correction is subtracted from the range)
COR	Tropospheric refraction correction (correction is
	subtracted from the range)

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917529.39	1453908.14	14/,40	34.14	-3244,23
917334.18	1452295,06	147.19	34,20	*3237.17
917342.76	1450688,08	147.85	34.32	-3207.87
917556 58	447489 33	140,71	34,28 34 44	-3 <u>1</u> 95,67
917363.3E	1445900,60	146.64	34.51	-3171.12
917376.98	1444318,11	146.50	34 57	-315A. 30
917383.80	1441174,82	140.22	34.63	-3146.46
91/391+61 9-7397.47	1439614.93	146.09	34,75	-3121.63
917404.26	4365,4.89	145.95	34.81 34.87	-3109+14
917411.99	2434959.73	145,66	34.93	*309540 <u>1</u> *3n84•n4
917494.70	1433420,86	145.52	34.99	-3071-342
917431.61	1430302.10	45.24	37.02 35.44	*3054.77
917438.40	1428842.25	145.10	35.17	-3,33.33
9.17452+16	192/320./0	144.95	35.53	-3020.55
917459,02	1424321+05	144.66	37.27	
$9_1/465,38$ $9_1/465,75$	1422426,84	144,52	35.41	-2981,97
917479.62	1921332+09 4419857-8z	144.37	35.47	-2969,02
917486.50	1418383,07	144.08	37.53 35,59	*2756+13 *2943-04
9475	1416014.83	143.93	35.45	-2929,94
917507.15	1413098	143,/0	35.71 35.77	-2915.83
91.7514.04	1412549.47	143.49	35,82	*2703+07 *289~ 48
¥1/320.93	1411107,54	143.34	35 A8	-2877.25

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S-24

UNKNOW	N S	578	T 1 0 i	N = a	GRAND FORKS I	GKAND	FORKS
SAMPL	н	м	S	мS	RN RH+RC	RDM	RDM-RDC
1	Ō	44	32	9	1497920.13 2.50	-3536.04	-3.12
2	0	44	32	510	1496194,50 4,15	-3524.40	-2.57
3	0	44	33	10	1494395.42 3.16	-3512.03	-1.30
4	Û	44	33	510	1492642.91 3.23	•3500.01	- 49
5	0	44	٦4	11	1490896.20 7.01	-3485.73	34
6	0	44	-34	511	1489154,53 6,73	-3478.18	=1 · n1
7	G	44	35	11	14874 <u>18</u> .01 5.98	-3466.7 <u>1</u>	⊒, A 0
<u> </u>	0	44	-35	511	1485687.51 5.62	<b>~3454.</b> 80	19
9	0	44	30	. 11	1483963.45 6.33	=3442. ⁸⁹	.37
10	0	44	30	511	1452245.20 6.63	-343 ₁ ,55	.34
11	0	44	-37	10	1480532.1 3.21	-3420.43	• 6 5
12	0	44	37	511	478824.57 6.39	-34 ₀ 8,56	. 44
13	0	44	78	11	1477123,43 6,88	-3396.21	1.29
14	0	44	70	510	1475428,87 4,79	-3384,47	1.50
15	0	44	.39	10	1473739.87 5.89	-3373.45	.94
15	0	44	39	510	1472055.78 6.09	-3363. ₀ 4	~.28
17	0	44	40	10	147 ₀ 376,66 5,43	-3352.37	-1.28
17	0	44	40	510	14687 ₀ 3,40 4,79	-3340.94	-1.56
19	0	44	41	10	1467035,76 3.91	=3329,43	=1,79
20	0	44	41	510	1465374.03 3.06	-3317,40	-1.55
21	0	44	42	_10	1463718.53 2.53	-33,5.52	-1.50
22	Ũ	44	15	511	1462048,79 5.12	-3293,58	-1.45
23	Û	44	43	_11	1400422.21 4.62	-328 <u>1</u> ,53	-1.31
24	0	44	43	511	1458787,20 3.80	-3269,48	*1.22
27	0	44	44	_11	1457155.79 3.40	-3256.67	- e <b>4</b> 0
20	0	44	44	511	1475530.75 3.55	-3244,23	01
27	Ó	44	45	_11	1453912.02 3.91	-3231.98	+17
28	Û	44	42	211	1472299.20	-3220,38	- 35
29	0		40	_11	1470691,99 3,87	-3503.50	-1.32
30	0	44	40	211		•3197,53	-1, 80
31	0		4/	12	144/494,21 4,98	-3185.22	-1.81
32	0		4/	212	1445404.05 4.05	-3171.54	41
い し し し	0		40	_12		-3197,99	1.27
04 TR	0	44	40	211		-3144,00	2.40
3. 44	0	44	• •	11		-3136.98	3.9/
75	0		47	P10		-3118.9/	2.60
37	0	44	20	10		-3100.94	5.50
3 C 7 A	0	44	70	210		-3097,31	1.30
3) 4 -	Õ		21	10		-3003.00	
<b>₹</b> 0	U		71	210		-30/1.01	- 34
40	0	44	50	10		-3060.00	-2.11
43	0	4.4	ς α τ	210		-304/ ./ 4	*1./2
40	- 51	44	50	10		-3034-1/	•.*3
47	0	44	50	-10		•301 • • • 5	• • • • •
46	U	44	54	10		-3000.00	1.00
<b>4</b> 7	Ŭ	44	85	-10	14208T4 AB 5 -4	-2-24+37	.40 _ ∡
<u>4</u> 8	0	44	55	10 54 n		-2-07413	
49	U A	44	56	~10	14:9862.44 4.64	-29KA - 1	- , , 0
50	0	44	56	34 A	1418387.87 4.80	- <u>-</u>	-•10
51	0	44	57	- 10	1416990.27 S.AA		• <del>•</del> • •
85	U 0	44	57	540	1445488.8n 5.47		A
53	V A	44	58	-10	1414003.34 5.23		
54	U A	4.8	58	540	1410545.77 4 30	-2892.44	
55	0	44	59	40		-2578.10	~1+02 A
• •	U			ιυ	***************************************		-1+00

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GRAND	FORKE	ORBIT 504	B		
			PAGE	1	
Вом	PakePac	008T	••	-	
-3536.04	#3.42	-17.67	10	COHI	COR
-3524.40	·2 57	-17.59	12.33	6.35	4.04 4 AT
-3515.03	-1.30	-17,51	12.33	8.33	4.62
-3-00-01	-,41	-17.43	11.00	5.32	4.62
-3485,/3	34	-17+35	11.67	8.31	4,61
-3444.7.	-1.72	17.88	11.90	A.30	4.60
+3454.8	<b>_</b> •9		11.07	n.29	4.59
-3442.89		• 17 • 12	11.07	8 . 4	4,57
-3431,55	.34	-16.97	10:00	8.45	4,90
-342ŋ.43	, n ⁵	-16.89	10.33	8.24	4 57
-3408,56	.44	-16.8 <u>1</u>	*9 ·00	8.23	4.56
-3396.21	1.28	-16.73	10.33	8,22	4,55
-3004,47	1.70	~10,00	10.33	A + 20	4 54
-33/3+42		10,50	11+20	^R •1 ⁹	4.54
•3352.37	28		10.33	² ,•1₫	4,53
-334n.94	-1.56	-10,44	11.00	<b>*</b> •1	4.52
-3329,43	-1 79	-16.29	10.33	7,10 8,45	4,52
-3317,40	<b>1</b> 55	-16.22	10.33	8.44	4 5
-3305,52	-1.50	-16.14	11.67	A.12	4.50
-3293,58	-1.45	-16,06	10.33	A . 11	4 49
-1269 -23	-1.31	*15,99	11.00	8.10	4 48
-3256.67	*1.22	•17.V1	10.33	n - 0 9	4,47
-3244.23	D 	-15 75	10.33	· · · · · · · · · · · · · · · · · · ·	4.47
-3231.98		*15.68	9.67		4 40
-3220,38	- 35	-15.60	11.00	?+80 8.45	4 45
-3500.50	-1.32	-17, 53	8.33	8.04	4 44
-3197,53	-1.86	~15.46	9.00	A.02	4 43
-3474 54	-1.41	-17,38	11.00	A.01	4,43
-3+57.55	4.41	-17,30	9.07	B•00	4.42
-3144.06	1.75			7.99	4.42
-3130.98	3.7	+15.05	10.00 10.33	/ , 70 7 07	7.41
-311 ⁸ ,97	2.66	-14,98	11.67	7.96	
-3106.94	2.20	-14,90	10.33	7,95	4 39
-3095,31	1.30	<del>-1</del> 4,83	11.00	7 94	4 38
-3003.00	. 75	-14,76	9,67	7.93	4 38
-3060.88	· 3·	•14,09	11.07	7.92	4,37
-3047.79		-14,52	11+00	7.91	4,36
-3034.17	- 83	-14.46	10+35	/ 3 ¥ 0 7 # 8	4,30
-3019.95	.60	-14.38	11.00	7.58	4,52
-3004.08	1.56	-14.30	~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~	7.87	4.34
-2794.39	. 48	-14.23	10.33	7.86	4.33
-2-07+13	- 10	-14+15	10.33	7.85	4.33
-2956 . 13		~1~+0 ⁰	12.33	7.84	4.32
-2942.58	•10	-13.92	10.33 9. <b>47</b>	7.80	4.32
-2929.65	. 29	13.85	9.67	7.84	4.71
-2917.20	-,38	-13.77	9.67	7.6	7 A U U
-2404.84	-1.17	-13.70	10.33	7,79	4,29
*20 42+10	-1.62	-13,63	9.67	7.78	4 29
-20/8.31	<b>*1</b> •0 ⁰	*13,55	11.00	7.77	4, 28

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<u>S-25</u>

## APPENDIX T

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## GEODETIC SECOR

(

## DATA PROCESSING COMPUTER PROGRAMS
NOT REPRODUCIBLE PFOJEGTY NG. HGC-Geodetic SNCCR 11 CL3: Geodatic SFCON Data List GATEGORY: Spensel IEONTIFICATION: Program EXAMI COF: Bortra. II CPC - 1604'POGFANNEF: G.M. Futnerford DATE: Fet., 1903 "UEPOSA: "To list remarked Geodetic SPCOR data including resolved renges and rates. UNAGE: Chairs Sequeror: Program LIST 1.0 2., Annuartal None 3. Thouts: (A'. Control cerd with 2 three dipit integers; the first specifies the number of samples to skip between printonte, and the second is the number of data triper leits used. 7 "nrough 99 data tapes is SFCOR format (See figure TelA.) 4. Untputs: lists-1 mark 1st difference Very fine channel mality rark Station contor Fine charnel Fur Jumper Coarse channel Nosth Very coarse channel 363 Extended Range cuannel Hour (24 .r. elcek) M-IC Minutes : - D2 F - D3 Sécords Pilliseconds. H = D4Frage (meters) 5. Routines Called: ESCLUE, FORM/T 6. Linkage: Nore ME PEOD: The range lata are corrected and complied into unambiguous range

words by the FORMET and PESCINE subroutines. Only every ith sample is considered where ! is the first integer or the control card (i.e., 1-1 samples are skipped). When as and of file is encountered, the program will begin a new tape or terringte, depending on whether or not the second control interer has loer satisfied.

CEMARKO:

For continuous lists of more than one tape, the tapes must le mounted on successive whits always beginning with unit 1. An alternate conjut format replaces R-Dg, F-13 and R-14 by the difference between the overlap bits.

P

T.

B COMMON IRNT(27) OUTPUT FORMAT

TAPE INPUT RECORD

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Ņ Ó Ő Ģ 0 0 0 ò 0 0 0 0 <del>آ</del>۔ --------1 اسم ----4 ÷-1 ----2 2 ŝ 2 2 0 2 2 0 2  $\sim$ ŝ ŝ ہنہ ຕ່ m ŝ ŝ ŝ  $\hat{}$ -ř: **51 ئ**ہ **"**1" ÷ ~**†** -f: -# 5 ŝ ŝ ŝ ហ ic.  $\sim$ 9 9 -\$ ~ ۱٢ ~ ∞ Q, 6 تر) MINUTES SECONDS STATION HINOW F LANK (47) (47) RANGE HOUR MSEC RUN DAY н > α žŪ <del>.</del> Д Ľ ~ ហំ 9 5 φ 30 ~ -1 D1_1' D.1.2 D14 D10,  $D^{i} V_{5}$ lle D Is D-16 D13 D 17 ×2 S1 ( D41 | D31 ( ER1 ( X3. R_2 / ER0 R_1 RO Υl Υ К К Å3 ж 4 R 5 R6 R 7 D22 D.2'5. D30 D20 D2₃,  $D_{24}$ D2: (D27  $D2_{1}$ X₀ × N 1C_2 Ç, Î, IC F CIC3 | D40 1C 6 i-C ¹⁰ i C I C MS43 IC2 MS₆ IC₄ MS₂° MS₇ MS 5 MS9. MS₁ MS₀ **VI53** MS3 S₀ ቧ . 2, ቢ ۵, Q, ۵, j, Ū, Ц Q, ይ. ኒ Ø υ υ <u>U</u> Ü ΰ υ υ υ 0 Ū, ΓO.

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		ו ואט 1	ו וגט ונ	"   IRU 22	2	- L	2 L	2	ې کې ۲	ີ ເດີ	· · · ·	2	». • • •	ົ້	2 ,	thut F
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2 2 2	· · · · ·		<u></u>	-		·	, , , , , , , , , , , , , , , , , , ,		<u> </u>		<u> </u>	-		<u> </u>	1	ut Re
	Z		υ	. 24	<u>0</u> - 0	- D2	- D3	- 104	- 14 14	I	2	ŝ	- <del>4</del>	<del>.</del> 73		વેઘ નિ હ્ય
12, <	13 F	U T	l5_ ∨	ર્ણ 9 	17 IČ	18 . R	19 R	20 R	21 R	22 D	23 D	24 D	25 D	26 10	- 12	Da Da
				<u> </u>		5.5. 				• • • • •	<u> </u>	<u></u>		<u>ra</u>	<u> </u>	្លប្ដី រ ដំ
X3	X4	÷ ×	N. S		×	ំ លំ ះ	N N	,i	Ø	, d	ΡQ	:		3	,	- 1
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D31	D32	D33	D34	⁶ D35	D36	D37	MOZ¢	ST 1	RUI	DA3	D'A7	· ··· ·	,	· · · ·		-
D41	D42	D43	D4 <u>4</u>	D45	D46	$D4_{7}$	MO3	ST2	หันว	DA4	DA8	; ; ;	e -			
ſs	s2	ش	5 45	S 2	Mo	MI	M2	X X	M4	NIS	HRO	HRI	HR 2	HR3.	HR	]
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1. A. A. A. A. A. A. A. A. A. A. A. A. A.	~ · .								Ē		•		-			, ¢.*

#### NU. \$130

#### PROJECT: Geodetic SECOR.

TITLE: Geodetic STGNR Range Resolution CATEGORY: Specia. IDENTIFICATION: Subroutine RESOLVE CCDF: CODAP CDC - 1004 PEOGFAMMEF: G.N. Rutherford DATE: Fet., 1965 FURFOSE: To compile the unempiguous range word from recorded STDOR data. USAGE:

1: Calling Sequence: CAEL RESOLVE

2. Arguments: None

3. Inputs: Bate stored in IRNT in the formet output by the Geodetre STOOR Format program, Figure T-18 with sectors 10 through 16 are blank.

4. Outputs: See figure T-1B

5. Routines Called: None

6. Linkage: COMMON A, B, C, IN(7), IRNE (27), IMP(9) METHOD:

> Compilation of the final range word is effected by combining the corrected chancel data recorded on the SECOR magnetic tape. The method used is us follows:

1.  $P_1$  is subtracted from the reference  $(R=D_1=VF_1)$  to obtain the very fine data.

2. D is subtracted from  $D_2$  ( $N_2$ - $D_1$ )=FN) to obtain the fine uncorrected data.

3. The 4 least significant bits (LSB) of the fine uncorrected data are subtracted from the 4 most significant bits (MSD) of the very fine data, the MSB of the difference is repeated for 4 more bits to make an 8-bit word which is called the fine difference (END) 4. The five difference is then added to the fine uncorrected to form the fine corrected data.

5. D. is suitracted from D, to obtain the coarse uncorrected data. 6. The coarse uncorrected data is corrected using the fine corrected data in the same manner as described in steps 5 and 4. 7. D, is suitracted from D, to obtain the very coarse uncorrected

data. 8. The very noarse uncorrected date is corrected using the coarse corrected data in the same manner as in steps 3 and 4 except that there are 5 bits cverlap.

9. The extended range data is corrected by using the very coarse corrected data in the same manner as ir steps 3 and 4. (Note that the extended range word meeds no runslation.)

The correction process can correct for a difference in the overtapping bits of plus  $\lfloor p^n \rfloor$  bits, and sinus  $\lfloor p^n \rfloor \rfloor$  bits where

n is the number of overlapping bits. The most significant bit of the difference between words to be connected is repeated to form an 8-bit word for the following reason:

When a 1 appears as the most significant bit of the difference, it indicates that the subtrahend is larger than the minuend, and therefore, should be subtracted from the subtrahend (which is the word being corrected). By repeating this 1 to complete an S-bit word, we have the complement of the number which should be subtracted from the subtrahend to give the corrected word. Hewever

No. G130 - RESOLVE, pg. 2

by adding the complement to the subtrahend, we have performed an effective subtraction.

After all the corrections have been made on the data words, the composite 25-bit range word is made up of the following: the

4 most significant bits of ER 3 most significant bits of VC 4 most significant bits of CS

4 most significant bits of FN

10 bits of the VE.

(NOTÉ: Refer to appendix B of this report for additional information on range resolution.) NO. G120

# PROJECT: Geodetic SECOR

TITLE: Geodetic SECOR Format Conversion CATEGORY: Special IDENTIFICATION: Subroutine FORMAT CODE: CODAP CDC - 1604

PROGRAMMER: G., W. Rutherford DATE: Feb., 1963

- PURPOSE: To rearrange input SECOR data into a meaningful format.
  - for processing.

USAGE.

1. Calling Sequence: CALL FORMAT

2. Arguments: None

- 3. Inputs: One Geodetic SECOR data record stored in COMMON IN(7) See figure T-1A for input tape format.
- 4. Outputs: Formatted data record stored in COMMON IRNT(27) as shown in figure T-1 except that locations 10 through 16 are left blank to be completed by the range resolution program.
- 5. Routines Called: None

6. Linkage: COMMONA, B. C. N(7), FRNT(27), TMP(9) METHOD:

> This program is simply a series of mask and shift operations, to group the data bits recorded on each information channel into a binary word occupying a unique memory cell. These words are stored in successive locations except for seven blank locations which allow for the insertion of a resolved range word and its components.

#### REMARKS

This program is usually used in conjunction with the RESOLVE program which resolves and inserts the range word into the list.

1.0° G200 PROJECT: Geodetic SECOR TITLE: Geodetic SECOR Editing and Smoothing CAPECORY: Data Processing IDENTIFICATION: Program PASS 2 CODE: Fortran 63 CDC 1604 PROGRAMMER: Dennis Wilson PURPOSE: To input a raw SECOR tape from one station and produce an output tape with the raw data plus edited and smoothed data. USAGE: 1. Gard, Input. Title Card - 80 columns 1048 (1) 1615 (2) Indicator Card: 1. Logical unit for input tape 2. Logical unit for output tape 3. Block length 4. IC Switch: 1 = apply IC, 2 = don't apply IC Edit and Smooth switch: 1 = yes, 2 = no 5. Edit span length, starting span length 6. 7. Noise gate 8. Maximum average second difference 9. Maximum number of successive bad samples Smoothing output point 10° 11. Overlap, smoothing span Degree polynomial for filter 12. 13. List 1 option: 1 = yes, 2 = no14. Not used 15. Not used 16. Nog used 12Ï5 (3) Time Card First time (H, M, S, MS), Last time (H; M, S, MS), Delta time (H, M, S, MS). 2(E17.10,3X) (4) Calibration Card Range calibration IC. calibration Multiple time spans may be processed by repeating cards (1) through (4). 2. Magnetic Tape Assignment The logical units are assigned (according to indicator 1 and) indicator 2. Generally 1 is the input unit and 2 the output unit. Printout ۵. Input Data The input data is listed once for reference. ь. List 1 This is a listing of the unprocessed data which may be deleted (and generally is) by use of indicator 13. The furmat is identical to that of EXAML. c. <u>List 2</u> This is a listing of the processed data. The Following is a brief description of the various columns:

- (1) <u>Time</u> the time recorded at the station is listed in hours, minutes, seconds, and milliseconds.
- (2) Raw Range the raw range from the input tape.
- (3) <u>Edited Range</u> the range output by the editing process plus the input range calibration.
- (4) <u>Smoothed Range</u> the range output from the smoothing filter.
- (5) <u>Residual</u> the difference between the edited range (input to smoothing filter) and the smoothed range
- (6) Edit Correction the correction applied to raw range to obtain edited range (minus calibration). With one exception; the edit correction will be an integral multiple of the least significant ambiguity (i.e., 256 meters). If a data sample is "bad" (i.e., cannot be reduced within the noise tolerance by using an integral number of ambiguities) then the edit correction is indicated with a "9.0." In this case the edited range will be either a predicted value or the measured value depending upon the number of successive bad samples which have occurred.
- (7) <u>Edited First Difference</u> the difference between the edited ranges  $(\Delta R_E)_{i} \approx (R_E)_{i+1} (R_E)_i$
- (8) <u>Smoothed First Difference</u> the difference between the smoothed ranges  $(\Delta R_S)_i = (R_S)_{i=1} (R_S)_i$
- (9) <u>Range Rate</u> the time derivation of the smooth range data. The units are meters/sec.
- (10) <u>Range Acceleration</u> the second time derivative of the smooth range data. The units are meters/sec².
- (11) <u>Measured Ionospheric Correction</u> the ionospheric correction derived from VFIC and VF including the IC calibration.
- (12) <u>Guality Indicator</u> -- = No correction
  - A = Ambiguous sample
    - $\ddot{B} \neq Bad sample$
- d. Tabulation at End of Block

At the end of each block three values are printed; (a) the number of bad samples, (b) the algebraic sum of the integral number of ambiguities used to correct the data of the block, (c) the RMS error for the block.

## Notes Regarding Listing

- (i) Because of the overlapping of data in the editing and smoothing process, the overlap portion will be processed twice. Because of this, the first samples of each block will only indicate the results of the second processing.
- (2) The values indicated in d. are not for the previous block but start beyond the overlap and continue into the overlap of the next block.

#### 4. Magnetic Tape Output Format

1 Quality mark

- 2 Station number
- 3 Run number

.4 Month

- 5. Day
- 6 Hour
- 7 Minute
- 8 Second
- 9 Millisecond
- 10: Raw Range
- 11 Raw first difference

12 VF

13 - FN

14 CS

15 VC

- 16 ER
- 17 D1-IC

18 R-D2

- 19 Ř.-D3
- 20 R-D4
- 21 Reference
- .22 D1

23 D2

- 24 D3
- 25 D4

26 IC

- 27 Edited range
- 28 Edited range plus calibration and IC
- 29 Raw first difference from edit routine
- 30 Edited First difference
- 31 Edit correction
- 32 Smoothed range
- 33 Smooth first difference
- 34 Residual
- 35 Range rate
- 36 Range acceleration
- 37 IC correction (including calibration)
- t

38

T-10

The output tape is in 1604 FORTRAN 63 format with all words expressed in floating point format.

REMARKS:

C ;

1. In processing multiple time spares, a time span of (overlap)  $\times \Delta t$  should be let't between spans.

DCw/kkb

NO: G205 PROJECT: Geodetic SECOR TITLE: Block Input for PASS 2 CATECORY: Special IDENTIFICATION: Subroutine BKINP CODE: Fortran 63 CDC 1604 PROGRAMMER: Dennis Wilson PURPOSE: To input a block of data for processing by PASS 2. USAGE:

1.

Calling Sequence CALL BKINP (TF, TL, DTM, NIN, NUM, KSTART, NUMIN, DATA, TML)

2. Parameters.

ΤF first time (seconds)

TL . last time (seconds)

DT**M** time increment

NIN logical input unit

NUM number of samples in block

KSTÄRT starting sample number

NUMIN number of samples input

DATA storage array (50)

ŤML actual last time input

Common Linkage 3.

COMMON A, B, C, IN(7), IRNT(27), TMP(9)

REMARKS

DCWikkb

No. G210 PROJECT: Geodetic SECOR TITLE: Compute IC Correction for PASS 2 CATEGOR.": Special Purpose CODE: Fortran 63 CDC 1604 PROGRAMESR: Dannis Wilson PURPOSE: To use the R-D1 channel, the IC calibration to compute the measured IC correction.

USAGE: 1. Calling Sequence

Call CURIC (DATA, CAL)

DATA A 50xl array containing the FASS 2 data. CAL The IC calibration

T-12

2. Common Linkage

COMMON A, E, C, IN(7), IRNT(27), THP(9)

REMARKS:

DCW/wj

No. G215 PROJECT: Geodetic SECOR DITES: First Listing for PAJS 2 CATEGORY: Special Furpose CODA: Fortran 63 CDC 1604 PROGRAMMER: Dennis Wilson PURFOSE: To provide the option 1 disting for PAJS 2 (i.e. edit & smooth data)

#### USACE: 1. Calling Secuence

Call LISTI(NFR, KSTART, DATA, TITLE)

AlPR - No. samples to print

KaTART - Starting sample in DATA block

DATA - A 50x array containing data to be listed.

TITLE - A lox1 erray containing the page title.

No. G220 PROJECT: Geodelic SECOR TITLE: Second Listing for PA35 2 CATEGORY: Special Furpose CODE: Fortran 63 GDC 1604 PROGRAMMER: Dennis Wilson FURPOSE: To provide the option 2 listing for PASS 2 (i.e. raw data list).

## USAGE: 1. Calling Sequence

Call LIST2(NFR, KSTART, DATA, TITLE)

NFR - No. samples to print.
KSTARI - Starting sample in DATA block
DATA - A 50x array containing data to be listed
TITL: - A loxi array containing the page title.

#### REMARKS:

DCW/wj

(

NOT REPRODUCIBLE

· NO. G225 PROJECT: Geodetic SECOR, SHIRAN TITLE: Data Editing Subroutine CATEGORY: Data Reduction IDENTIFICATION: Subroutine EDITSR CODE: Fortran II CDC - 1604 PROGRAMMER: Dennis Wilson DATO: July 17, 1963 PURPOSE: To edit a block of data stored in memory, USAGE: Calling Sequence: CALL EDITSR (ARRAY, LEDIT, LOUT, NSAMP, NSPAN, AMB, SNOISE, DELZMX, BADMAX, NBAD, NAMB, LAKE; 2. - A two dimensional array, the first subscript Arguments: APEAY specifying the word within a sample and the second subscript being the sample number, Maximum array size (48,100) LEDIT - An integer specifying the location within a sample of the data to be edited. LOUT - An integer specifying the first location within a sample where the results of the editing process will be stored. NSAMP - An integer giving the number of samples in APRAY to be edited. - An integer giving the number of samples to be used: (1)to determine a "good" starting NSFAM point; (2) to predict a new first difference. AMP - A floating point number giving the value of the least significant ambiguity (sg. 256.0 meters in the case of Geodetic SECR). SNUISE - The noise pate; that is, the maximum noise value to be tolerated by the program. DEL2MX - The maximum average second difference within SPAN for which editing will begin. BADMAX - The maximum number of successive bad samples which will be tolerated. NBAD - The number of "bad" (samples encountered NAMB - An algebraic sum of the humber of ambiguities edited BAKE - The number of the first sample ARRAY, LEDIT, LOUT, NSAMP, NSPAN, AMB, SNOISE, DEL2MA, 3. Inputs: BADMAX, LAKE 4. Outputs: ARFAY, NEAD, NAMB 5. Boutines Called: EDIT. CONSMP

METHOD:

14. The first NSAMP data samples are used to determine an average second difference. This average second difference is compared with DEL2MX. If it exceeds it, the span is then snifted one sample. The process is continued until NSAMP "pood" samples are found. 2. The NSAMP pood data samples are used to predict the first difference for the succeeding sample (an end point prediction is made using a least squares first degree polynomial). The prodicted and measured first differences and the noise gate are used to detect ambiguities. One of three cases will result: (a) the sample is good as it stinds; (b) there are an integral number of

**T - 1**'5 🗍

unifyuities to remove; (6) the sample is extraheous. 3. An extraheous sample will result in the predicted first difference wing used subject to the condition that no more than BADMAX successive extrahecus samples will be tolerated. If PADMAX is exceeded, the program will begin again as in Step 1. 4. The corrected data sample will be returned where the raw sample was found. Feginning at 100T the following information is stored tack into AFFAY:

LOUT - Corrected data sample

LOUT+1 - Paw first difference

LOUT+2 - Corrected first difference.

IOPT+3 - Correction.

"the code where a sample is ".ad," the number 9.0 will the recorded as the correction.

5. Two countered and the second is the number of "bad" samples encountered and the second is the number of least significant untipulties corrected. This second counter is alreoraic, i.e., an annihulty added is counted positively and an ambiguity subtracted is counted terminely.

PEMARKSE

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If more than one block of continuous data is to be edited, prior information may be inserted by overlapping the blocks of data such that the first NEFAN samples of a block have previously been edited.

#### PROJECT: SHIRAN

NO: GL30 PR THTLE: Edit-One Sample Subroutine

# CATEGORY: Data Reduction IDENTIFICATION: Subroutine EDIT

CODE: Fortran 62 CDC - 1604

PROGRAMMER: Dennis Wilson DATE: July 17, 1963

PURPOSE: To use parameters of the CALL statement to:

- (1). Remove integral multiple of the least significant ambiguity from the data,
- (2). To reject spurious data.

USAGE:

#### 1. Calling Sequence: CALL EDIT (XM, XPR, DELXP, COUNTB,

		SNO	DISI	E, AMEI, DELXM, DELXC, XC, CORR)
2.	Arguments.	XM	Ĩ.	Measured data sample
	-	XPR	-	Previous edited sample
		DELXP	-	Predicted first difference
		COUNTB	-	Number of successive "bad" samples
	-	SNOISE	-	Noise gate

AMB1 - Least significant ambiguity

- DELXM Measured first difference
- DELXC Corrected first difference
  - Corrected data sample
- CORR Correction

3. Inpats: XM, XPR, DELXP, COUNTE, SNOISE, AMEL

4. Outputs: COUNTB, DELXM, DELXC, XC. CORR

5. Routines Called: None

XČ

b. Linkage: None

#### METHOD:

The input values are used to edu the data. One of three to ugs will happen:

- 1. The data will be good and require no correction;
- 2. The data contains an integral number of ambiguities;
- 3. The data is extraneous and cannot be edited, in which case COUNTB is incremented, CORR = 9.0; DELXC = DELXP.

## REMARKS:

Primarily used with the EDITSR.

110. 55 PROJECT: Fishbowl TITLE: Smoothing CATEGORY: Utility IDENTIFICATION: Subroutine CONSMR CCDE: Fortran - 62 CDC - 1604 PROGRAMMER: Terry Yuen DATE: -6-27-63 PURPOSE: To compute smoothing coefficients and smooth input data; USAGE: Galling Sequence: CALL CONSMR (N, L, K, DELT, XM, COEF, SMX)-.1. 2. Arguments: N - Total number of equally spaced data samples within an input span (N = 101):
The order of the derivative (L = 2).
The degree of the polynomials (A = 3)
The degree of the polynomials (A = 3) L K Μ - The desired output position of the interval (M = 1), if the left most point of the interval is desired) DELT - The time between each successive data point COEÈ - Smoothing coefficients AMX. - Cutput point Inputsi 3. Outputs: 4. Routines Called: Hone 5. Linkage: DIMENSION XM(101), CCEF(101) 6.

METHOD:

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REMARKS :

This subrouting is primarily used for smoothing data; if the use requires only smoothing coefficients, subroutine SCR should be used.

T - 18

NO. UT002 PROJECT: Utility TITLE: Least Squares Moving Filter Coefficients Computation CATEGORY Filtering IDENTIFICATION: Subroutine SCR CODE: Fortran 62 CDC - 1604-DATE: June 1964 PROGRAMMER: Terry Yuen PURPOSE: To determine coefficients to be used in a least squares smoothing routine.

USAGE:

1. Calling Sequence: CALL SCR (N, L, K, M, COEF)

2. Arguments:

Ń

L

K

Μ

Total number of equally spaced data samples within an input span The order of the derivative (Lmax=2) The dègree of the polynomial (Kmax=3) The desired output point of the interval (M=F if it is in the left-most point of the interval). Coefficients computed by this subroutine COEF -

T-19

used to reduce the varians and to obtain

the desired output quantity.

3. Input: N, L, K.

Output: M, COEF 4.

5. Routines Galled:

METHOD: This subroutine computes a set of coefficients which are used for fitting a given function. The number of coefficients depends on the total number of an input span of samples. The number of coefficients is nominally limited to 501 points.

REMARKS: Revision of original routine to accommodate additional coefficients. (LBP)

No. 3290PRCJECT: Geodetic SECORTITLE: List E3 TapeIDENTIFICATION: Program EXAM2CATECONY: Special PurposeIDENTIFICATION: Program EXAM2CODE: Fortran 63 CDC 1604PROGRAMMER: Dennis WilsonPURPC3A: To provide a listing of a Geodetic SECOR 25 Tape

# USASE: 1. Gard input

- (7) Title 80 columns 10A8
- (2) Number of tapes, number to skip 215
- 2. Magnetic Tape Assignment

Une 23 tape on logical unit 1

3. Printout

(See FA332 - no raw list)

REMARKS:

1. No provision for multiple taxes.

#### NQ. G300

## PROJECT: Geodetic SECOR

TIT LF: Simultaneous Mode Satellite Positioning

CATEGORY: Data Processing IDENTIFICATION: Program PASS 3 CODE: FORZRAN 63 CDC 1604

PROGRAMMER: Dennis Wilson

PURPOSE: To input three or four ES-tapes, time synchronize them and generate a satellite position (SP) tape. USAGE:

1. Card Input

(2)

(4) Title card

Indicator card

10A8

~16**I**5`

4(E17.10.3X)

1. Input code

2. Number of tapes to synch

3. IC correction code

4. Number of samples to skip:

15. Slope for IC mode!

16. - Electron density for IC model

- (3) Time interval
  - First time (H, M, S, MS) 1215 Last time "

Delta time

(4-7) Base station locations

(latitude, longitude, height, name) 3(E17. 10, 3X)

(S) Range Calibration. 4 (E 17. 10, 3X)

IC calibration

2.

3.

Three or four input ES tapes are mounted on logical units 1 through 3 or 4. The output SP tape is mounted on logical unit 5.

Printout

:(9)

e. Listing of input cards

Magnetic Tape Assignment

- b. Page 1 station data
  - (1) Sample number (1-54)
    - (2) Time

The time from tape 1 is listed unless a time drift on 1 has occurred in which case it is the time from tape 2.

(3) Trackers

The four numbers indicate which of the four

tapes were time synched at this point (e.g. 1234, 1230, or 1240, etc.)

## (4) <u>Range 1</u>

The range to the satellite from station 1 (name appears in heading) as determined from the input survey and the solution using stations 123.

(5) <u>AZ1</u>

The azimuth of the satellite from station 1. (6) EL1

The elevation of the satellite from station 4. (7-15) The information of (4-6) is repeated for the

other three stations.

c.

d,

Page 2 - satellite position

(1) Sample number (corresponds to that of page 1)

(2) Time (same as page 1)

- (3-5) LATITUDE, LONGITUDE, HEIGHT
  - The latitude, west longitude, and height

above the spheroid as determined from the solution using stations 123.

(6-8) XE, YE, ZE

The equatorial coordinates as determined

from solution 123.

#### (9-1el)EQ. VELOCITY

The sätellite velocity in equatorial coordinates as determined from range and range rate data from stations 123.

Page 3 - corrections

(1) Sample, number (corresponds to that of page 1)

(2-5) TROPO: REFR. CORR.

The tropospheric refraction range correction determined from the model for stations. (Subtracted from ranges.)

(6-9) MEASURED IC

The measured IC for the four stations (subtracted

from ranges.)

#### (10-13) COMPUTED IC

The IC correction computed from the IC model using input slope and electron density for the four stations (subtracted from ranges).

(14-17) TRANSIT TIME CORR.

The transit time correction for the four stations

(added to ranges).

Page 4 - permuted satellite position

(Only applies and is printed if four tapes are synced)

(1) Sample number (corresponds to that of page 1)

(2-4) LSSQ OF PERMUTED SOLUTIONS

The average latitude, west longitude, and height using the four combinations of three tracking sites.

## (5-16) <u>VARIATION OF PERMUTED SOLUTIONS FROM</u> LSSQ COMBINATION

The difference between the average solution

above and each of the four individual solutions is taken and the difference in latitude. longitude, and height is printed.

Ort	put Tana Normat	
1.	Time (decimal seconds).	
∕⊊ ).	Run	
- 	Monto	
ۍ. ا.	Dag	
7 5	Number of trackors	
с. С.	Aumoer of an genera	
7		
ŝ		
9 °		
10		
11	Station Number	
12	Bange	
13	Range Rate	
<u>14</u>	Range Acceleration	
15:	Smoothing Residual	STATION 1
16	Meâsured IC	
17	FRange + Tropo + IC + TT	
18		
19		
20-		
21		-
2;2		
23	-	
24		
25	(same format as 1)	- STATION 2
26	· ,	-
27	-	
28	-	
29		
30 [.]	•	
31	· _	
32		
<u> </u>		
34	-	
35		
36	_(same format as 1)	STATION 3
37		
38	-	·
39		•
40		

ミグ

4

Т-23

41 42 43 44 45 (same format as 1) STATION 4 46 47 48 49 50 51 X_E 52Υ_E Z E 53 Х УЕ УЕ 54 'EQUATORIAL COORDINATES USING THREE TRACKERS 55 ż_e  $\mathbf{56}$ х_е 57 Y E 58Ξ_E 59 70 Latitude 71 Longitude STATIONS 123 72Ìleight 73 Latitude 7**4** Longítude STATIONS 124 75 ileight 76 Latitude 77 Longitude STATIONS 134 78 Height 79 Latitude  $\mathbf{S0}$ Longitude STATIONS 234 **8 l**: Íleight 5 82 Latitude Longitude \$3 AVERAGE SOLUTION \$4 fleight

т. 400-

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T - 24

REMARKS:

1. The input codes are

1 - 1, 2, 3

2 - 1, 2, 4

3 - 1, 3.4

4 - 2, 3, 4

5 - 1.2.3,4

2. The units are degrees and meters

3. The unknown station (if any) is number four.

4. Failure of the times on the four (or three) tapes to agree within 20 ms results in a diagnostic (time duift on unit  $\rightarrow$ ) to be printed

T - 25

No. G3O5	PROJECT: Geodet	ic SECOR
TITLE: Tape Time Sync and Search CATEGORY: Special Purpose CODE: Fortran 63 JC 1604	IDENTIFICATION:	Subroutine SYNC or Subroutine SEARCH
PROGRAMÆR: Dennis Wilson		-
PURPOSE: SYNC: To synch three or	four ES tapes to	the first time.
SEARCH: To search the t	hree or four ES t	ages for the next time.

USAGE: 1. Calling Sequence

1

CELL SYNC (NTP, N3KP, TIME, DATAIN, TFOUND, IK, NSYN, TES) OR Call SEARCH (NTP, N3KP, TIME, DATAIN, TFOUND, IK, NSYN, TES)

NTP	A code	indicating	which	tapes	are	to	be called
	1 =	123	4 =	234			
	2 =	124	5 ≈	1234			÷
	3 =	134					

NSAP No samples to skip

TIME A 3xl array giving the first, last and delta time. For 3EARCH TIME (1) is the desired time.

DATAIN A 50x4 array of input data in SP tape format.

TFOUND The time found on tape 1.

IK A 4xl array giving the tape units being called.

NSYN Number of tape units signed.

TES A 4xl array giving the relative time bias of the four (or three) tapes.

REMARK 3:

1. Buffering is overlapped.

No. 6310 TITL2: Permuted Solutions CATEGORY: General Purpose CODE: Fortran 63 CDC 1604 PROGRAMMER: Dennis Wilson

### PRCJECT: Geodetic 3ECOR

IDENTIFICATION: Subroutine PERMUT

FURPCSE: To compute from the ranges of four trackers the four possible three-range solutions.

#### USAGE: 1. Calling Sequence

Call PERMUT (STA, R, RV, RVAV, RES)

- STA A 3x1 array consisting of the latitude, longitude and height of the four trackers.
- R A 4x1 array consisting of the four ranges.
- RV A 3x4 array consisting of the four solutions in latitude, longitude, height.
- RVAV A 3xl array giving the average solution in latitude, longitude and height.
- RES A 3x4 array giving the difference in latitude, longitude and height of each solution from the average solution.

#### REMARKS:

1. Units - meters, degrees

2. Longitude is west longitude.

3. The order of the solutions is:

1,	2,	3
1,	2,	4
1,	3,	4
2,	3,	4

DCW/wj

No. 1515 PROJECT: Geodetic SECOR
 TITLA: Computation of Velocity and Acceleration from R₁, R₁, R₁
 CATEGORY: General Purpose IDENTIFICATION: SubFoutIne TSTVA
 CODA: Fortran 63 CEO 1604
 FRCGRAMMER: Dennis Wilson
 FURPOSE: To use range rate and acceleration from each of three tracking sites to determine velocity and acceleration.

USAGE: 1. Calling Sequence

Ĩ

Cell TSTVA (STA, RV., R, RD, RDD, V, A)

514. A 3x5 array consisting of tracker coordinates relative to some cartes an coordinate system.

i,ð.		x ₁	X ₂	X ₃
	•	Y	۲ _ź	Y ₃
		Z	z ₂	² 3

,RV

A 3x1 array consisting of the x,y,z coordinates of the vehicle in the same cartesian coordinate system

R, HD, 100 The range, range rate and range acceleration observed at the tracker.

V, A Two 3xl arrays giving the velocity and acceleration in the cartesian coordinate system.

REMARK 3:

1. The coordinate system and the units are arbitrary.

DCW/wj

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NOT REPRODUCIBLE NO. 0326 PROJECT: TITLE: Rotation to Tracker Place System IDENTIFICATION: Subroutine POTATE CATEGORY: Utility CODE: Fortran 62 CDC - 1604 PEOGRAMMEP: Den: is Wilson " DATE: May 18, 1963 PURPOSE: To rotate a Cartasian coordinate system centered at base station one into a new system such that the X.Y plane passes through two other base stations and the rotation is about the X and Y axes only. USAGE: 1. Calling Sequence: GALL ROTATE (ARRAN, ARPAY2) 2. Arguments: - APRAY1 - A 3x3 array of the station locations (r1 station one will be (0,0,0)). The first subscript refers to XYZ and the second to the station number. APPAI2 - A 3x3 array of the rotation matrix to rotate from the old to the new system. AFFAY1 Input: 3. 4. Output: AFRAY2 5. Poutimes Called: None METHOD :/ The rotation matrix, T1, is evaluated as follows: sin B Ĵ 0 -Э ces B T = Û coso sind Ĵ 1 0 -sir B cos 13 0 Û -sir 🖌 cos 🛠  $\frac{\sum_{2} \sum_{3} - \sum_{3} \sum_{2}}{\sum_{2} \sum_{3} - \sum_{3} \sum_{2}}$ i.anB= where: and: - ×3<u>~2</u> ter.cn = ros B FENTERS

NO. CO110 PROJECT: General TITLE: Compute Ionospheric Refraction IDENTIFICATION: Subroutine IONCR. CATEGORY: Utility CODE: Fortran 62 CDC-1604 PROGRAMMER: Fred C. Forbes, Jr. DATE: March, 1964 PURPOSE: To compute the ionospheric refraction correction to ranging using an empirical model of the ionosphere. USÁGË: Calling Sequence: CALL IONCR(R,SIN, DRINO) 1. Arguments: 2. R. - Slant range in feet SIN - Sine of elevation angle DRINO - Range correction in feet. з. Inputs: R.SIN 4. Outputs: DRINO 5. Routines Called: None.

METHOD:

6.

Linkage: None

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REMARKS:

T -30

#### PROJECT: SHIRAN

TITLE: C VIEGORY : CTC - 1604 COLS: Fort · 11 PROGRAMMERT art Ebert PURPOSE:

LEENTLFICATION: Subroutine RAYGEO

LATE: 3-16-63

USINE:

NG. 84

Calling Sequence: Jall RAYGED (S, U, J, F, UL, K, F) 1. 2. Arguments: S 4 Netual distince from the station to the device H - Noight of the device above the sphere surface - heithf of the station above the sphere surface 5 R - Radius of the schore GP - Wre langth in the sphere between radii extending to the station and the device from the sphere center X - Angle in rabians between the same two radii Ţ - Arror return with a value of one if S is less than the differonce between H and G, or if S is greater than R 3. Inputs: 5,H,J,R 4. Outouts: 5D,X,I 5. Routines Called: N..no 5. Linkagút Tone

METT F:

the Cos x term is replaced by its series expansion, the 1 term removed and K set equal to Cos x. " is solved for and the error is used to correct X. This procedure is repeated until the error is less than  $1 \ge 10^{-9}$  radians. Four terms in the series are used so that the accuracy decreases for A gruator than .25 radiuns.

ASMARKS :

S)

Functional Relationshirs:

8² = x² / B - - Nows X A FR FE 5 # 5 # 3 JD = R + X

NO. G200

## PROJECT: Geodetic SECOR.

TITLE: Orbital Mode Satellite Position

CATF GORY Data Processing CODE: FORTRAN 05 CDC 1604 IDENTIFICATION- Program GSORB

PROGRAMMER: Dennis Wilson

PURPOSE To use input injection vectors to predict the satellite position.

at times found on the remote site ES tape. An output tape in the formal of the simultaneous mode SP tape is produced. USACF+

> 1 rd Input

•	- Carr											
	iii	Orbital Perturbation data										
		CO .	4(E17, 10, 3X)									
		FMD	4(E17, 10), 3X)									
		NO. FMASS, EA	I20.2(E17.10.3X)									
		(This set of cards is input only	y once and is generally									
		left attached to the deck)										
	(1)	Title card	(10A8)									
	(2)	Times (for ES tape)	· ·									
		First time (II, M, S, MS)	-									
		Last "	(1275)									
-		Deita "	· _									
	(3)	Indicator card	(1615).									
		ions-(usually-4).										
		2. Number of samples to s	kip									
	3. It Stantha of geografic intermetion and											
		4. Dr j intervals										
		15. Slope										
		16. Electron density	model									
	(4)	Station Location Card	3(E17.10,3X)-4A5									
	(5)	Injection time (II, M.S. MS)	415									
	(6)	Injection position vector (EQ c	200rd.)= 3(E17.10,3X)-									
	(7)	Injection velocity vector (EQ a	coord.) 3(E17.10.3X)									
	(8)	Calibration constants	3(E17.10.3X)									
		Range, IC, time (Second	ls)									
-	(Fə:	r more than one time interval re	peat cards 1~8)									
2.	Mag	Magnetic Tape Assignment										
	One	ES tape for the unknown station	on logical unit 1.									
	One	output tape (PES) on logical uni	t 2.									
3	Pri	ntout	• •									
	d	Listing of the Input Cards										
		· · ·	-									

Page 1

b.

(1) SAMPL

A cumulative count of samples

(2) <u>Time</u>

(3) <u>Latitude</u> Predicted latitude of the satellite

(4) Longitude

Predicted west longitude of the satellite

(5) HEIGT

Predicted height of satellite above spheroid. RC

(6)  $\underline{RC}$ 

The range from the predicted satellite point

to the unknown station.

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X_)

(7) <u>NS.</u>

The azumuth of the predicted satellite point with respect to the unknown station,

(8) EL

The elevation of the predicted satellite point with respect to the unknown station.

(9) <u>RDC</u>

The predicted range rate at the unknown station.

- Page 2 (1) SAMPL
- (2)  $Time^{2}$
- (3) <u>RM</u>

Measured range from the unknown station in meters corrected for ionospheric effects. tropospheric refraction, transit time, and calibration.

(4) <u>RM-RC</u>

The difference between the measured and

predicted ranges.

(5) <u>RDM</u> The measured range rate at the unknown station

(6)

(7)

in meters (sec

RDM-RDC

The difference between the measured and the

predicted range rates.

CORT

The transit time correction

The measured ionospheric correction (correction

is subtracted from the range.)

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## (9) CORI-

The ionospheric correction from the analytic model in meters (correction is subtracted from the range).

(10) <u>COR</u>

The tropospheric refraction correction.

(Correction is subtracted from the range.)

4. Output Tape Format

See PASS 3 description. Sufficient data is packed in this format to allow use by PASS 4.

REMARKS:

F

1. Units are degrees, meters, and meters sec.

2 The first time for the ES tape must exceed the injection time.

PROJECT: Geodetic SECOR NO: G510 TITLE: Inverse Geodetic Problem IDENTIFICATION: Subroutine GDSIC CATEGORY: Utility CODE: Fortran 63 CDC 1604 PROGRAMMER: Dennis Wilson PURFOSE: To use the latitude and longitude for two points on the earth's surface given with respect to some reference spheroid to compute the geodesic,  $A_{12}$ ,  $A_{21}$  where  $A_{11}$  is the azimuth from i to J. USAGE: Calling Sequence CALL GDSIC (XLAT1, XLONG1, XLAT2, XLONG2, A12, A21, SGD) 1. Parameter List 2. XLAT1, XLONG1 latitude and longitude of point 1 (east longitude, degrees) XLAT2, XLONG2 latitude and longitude of point 2 (east longitude, degrees) A12, A21 azimuths (degrees CW from north ) Geodesic (meters)

#### REMARKS:

SGD

J

1. The method as outlined in the following reference was used:

Sodano, E. M., General Non-Iterative Solution of the Inverse and Direct Geodetic Problems Feseerch and Analysis Division, U.S. Army Engineer (GIMRADA); Et Belvoir, Virginia; April, 1963.

DCW:kb

Nu: ' 6511		PROJECT: Geodetic SECOR							
TITLE: 1 CATEGORY CODE: Fo PROGRAMM	Direct Geodetic Prob Utility Prtran 63 CDC 1604 R: Dennis Wilson	IDENTIFICATION: Subroutine DIRECT							
PURPOSE	To compute the let surface with respe and longitude of t azimuth.	Stude and longitude of a point on the earth a of to some reference spheroid from the latitude he other end point, the geodesic, and the							
USAGE:	Calling Sequence								
	CALL DIRECT (XLATI, XLONGI, A12, S, XLAT2, XLONG2, A21)								
2.	Parameter List								
	XLATI, XLONGI	latitude and longitude of point 1 (east longitude, degrees)							
	A12	Azimuth (OW from north) from point 1 to point 2							
	S	Geodesic (meters)							
	XLAT2, XLONG2	latitude and longitude of point 2 (east longitude, degrees)							
	A21	Azimuth (GW from north) from point 2 to point 1							
DEMANYO.		-							

REMARKS:

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NUMBER OF TAXABLE PARTY

1. The method as outlined in the following reference was used:

Sodano, E. M., <u>General Non-Iterative Solution of the Inverse and</u> <u>Direct Geodetic Problems</u>; Research and Analysis Division, U.S. Army Engineer (GIMRADA); Ft. Belvoir, Virginia; April, 3963.
No. G500 PROJECT: Geodetic SECOR TITLE: Geodetic SECOR fine Crossing CATEGORY: Data Processing CODE: Fortran 63 CDC 1604 PROGRAMMER: Dennis Wilson PURPOSE: To determine the geodetic distance between two points using a satellite line crossing.

USAGE: 1. Card Input

(1)	Title - 80 columns	10A8
(2)	Indicator Card	1615

IND1 - Span length IND2 - Station #1. IND3 - Station #2 IND4 - Print intermediate results 1=yes, 2-no IND5 - no. samples to skip IND6 - Satellité solution 1 = 1/2,3 2 = 1,2,4 3 = 1,3,44 = 2,3,4

(3,4) Station Locations
(5) First time (H,M,S,MS), Last time (H,M,S,MS), Delta time (H,M,S,MS)

3(E17.10,3%) 1215

# 2. Magnetic Tape Assignment

One SP tape on logical unit HDL (Density = 200)

3. Frintout

The input cards are listed. The span of data about the binimum geodetic sum is listed. The computed geodesic and measured minimum sum distance are listed.

REMARKS

1. The satellite solution should be chosen to avoid using both stations in the satellite solution.

20. If no crossing occurs, the output will be meaningless.

DCWywj

# No. G515 PROPECT: Geodetic SECOR TITLE: Determine Line Distances CATEGORY: General IDENTIFICATION: Program LINE CCDE: Fortran 63 CDC 1604 PROGRAMMSR: Dennis Wilson FURPCSE: To provide a listing of the geodesics between points on earth's surface using the GDSIC subroutine.

U3AG2: Card Input

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Pairs of station location cards. Latitude, longitude, height, station name

3(EL7.10,5X), 4A5

## Printout

Input cards, geodesic, azimuths

### REMARKS:

1. Alther Clark or international spheroids may be used by changing the subroutine GDSIC.

DCW/wj

NO. 410 PROJECT: SHIRAN TITLE: Latitude, Longitude, Radians to Meters and Azimuth CATEGORY: General IDENTIFICATION: Subroutine INVERS CODE: Fortran 63 BROCRAMMER: Robert Ebert DATE: March 19, 1964 PURPOSE: To compute azimuths and base line given the latitudes and longitudes of base stations. USAGE ; 1. Calling Sequence: CALL INVERS(FE1, FE2, F1, F2, A12, A21, 5) 2. Arguments: FE1 - Latitude at site 1 (Eastern) FE2 - Latitude at site 2 (Western) Fl - Longitude at site 1 (Eastern) F2 - Longitude at site 2 (Western) Al2 - Azimuth from site 1 to site 2 (South to East) A21 - Azimuth from site 2 to site 1 (South to West) - Distance between sites Ş 3. Inputs: FE1,FE2,F1,F2 4. Outputs: Al2, A21, S 5. Routines Called: None

METHOD:

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REMARKS: Units are radians and meters.

NO. G600	PROJECT: Geodetic SECOR	
TITLE: Punch Equatorial Coordinate	s on Cards	
CATEGORY: Data Processing	IDENTIFICATION: Program SPU	JNCH
CODE: Fortran 63 CDC 1604		
PRUGRAMMER: Dennis Wilson		
FURPOSE: To read a satellite posit	ion tage and punch onto cards	and list
satellite position in Equ	avorial coordinates.	r
USAGE:		
1. Card Input		
(1) Number of samples to a	kip	(15)
(2) First time (H, M, S, M	S), last time (H, M, S, MS),	
delta time (H, M, S, M	S)	(1215)
2. Gard Output		
(1) Injection vectors	time, Xr. Yr, Zr	4(E17.10, 3X)
(2) Injection vectors		3(E17.10,3X)
(3) Satellite position	time, X _r , Y _r , Z _r	4(E17.10,3X)
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3.

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Printout Format (Same as 2) The number of input samples is output at end.

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110: 0605 PROJECT: Geodetic SECOR TITLE: Funch Equatorial Coordinates and Velocity Onto Cards CATEGORY: Data Processing IDENTIFICATION: Program VUNCH CODE: Fortran 63, CDC 1604 PROGRAMMER: Dennis Wilson PURPOSE: To read a satellite position tape and punch onto cards and list satellite position and velocity in equatorial coordinates. USAGE: 1. Card. Input (1) Number of samples to skip. (15)(2) First time (H, M, S, MS), last time (H, M, S, MS), delta time (H, M, S, MS) (1215)2. Card Output, (1) Injection vectors -- time,  $X_E$ ,  $Y_E$ ,  $Z_E$ (2) Injection vectors --  $X_E$ ,  $Y_E$ ,  $Z_E$ (3) Satellite position -- time,  $X_E$ ,  $Y_E$ ,  $Z_E$ (4) Satellite Velocity --  $X_E$ ,  $Y_E$ ,  $Z_E$ , time [(3) and (4) repeated to last time] 4(E17.10,3X) 3(E17, 10, 3X)4(E17.10,3X)4(E17.10,3X)

3. Printout Format

(same as 2)

The number of input samples is output at end.

REMARKS:

No. 0610 PROJECT: Geodetic SECOR TITLI: Compute Gravitational Acceleration CATEGORY: General Purpose IDENTIFICATION: Subroutine GRAVITY CODE: Fortran 63, CDC 1604 PROGRAMMER: Dennis Milson FURPOSE: To compute the gravitational acceleration at a point above the south of the gravitational acceleration at a point above the

earth's surface using zonal harmonics. Constants of Y. Kozai are used for the computation.

USAGE: 1. Calling Sequence

:

CALL GRAVITY (EP, R, AC)

 $\begin{array}{l} \mathrm{kP} - \mathbf{A} \ 3\mathrm{xl} \ \mathrm{array} \ \mathrm{consisting} \ \mathrm{ol}' \ \mathrm{the} \ \mathrm{unit} \ \mathrm{vector} \ \mathrm{from} \ \mathrm{the} \\ \mathrm{earth's \ center} \ \mathrm{to} \ \mathrm{the} \ \mathrm{point}; \\ \mathrm{i.e.,} \quad \left\{ \begin{array}{l} \mathrm{FP}(1) = \cos p \ \cos \lambda \\ \mathrm{FP}(2) = \cos p \ \sin \lambda \\ \mathrm{FP}(3) = \sin p \end{array} \right. \end{array} \right.$ 

R - The range from the center of the earth to the point.

AC - A 3xl array consisting of the equatorial components of the acceleration.

REMARKS: 1. Units are feet.

2. Two versions of the subroutine:

(1) the total acceleration is computed

(2) the first harmonic (i.e.,  $1/r^2$ ) term is deleted so that only the perturbations to a two-body field are retained.

3. The inputs are referenced to the international spheroid.

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A New

No. 3406 TITLE: Unknown Station Solution - 3, 3 CATEGORY: Data Processing CODE: Fortran 63, CDC 1604 PROCHAMMER: Dennis Wilson PURPOSE: To compute the position of an unknown fourth station from two spans of satellite position and range data.

USAGE: 1. Card Input.

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- (1) Title Card &C columns 10A8
  (2,3) Time Cards: first time (H,M,S,M3) 1215, 15%, 15
  Inst time (H,M,S,MS), dolta time (b,M,S,MS), Logical tape number
  - (1,2,3)
- (4) Unknown station location (latitude, 3(S17.10, 3X) longitude, height)
- 2. Magnetic Tape Assignment

One or two- 3F tapes assigned to HD1, and/or HD2 corresponding to time cards.

3. Printout

The unknown static, position is computed with each succeeding set of two satellite position. The results of each computation are listed with the deviation from the input position and the overage solution. This is proceeded by a summary including input data, average deviation from the survey position and RMS error.

#### REMARK J:

- 1. The shortest of the three spans controls the number of solutions attempted.
- Two span, may be taken of one SP tape as long as the earliest span timewise is in the deck first.

DCW/wj

PROJECT: LRSS NO. G321 TITLE: Two Range and Height Solution IDENTIFICATION: Subroutine TWBASEC CATEGORY: Utility CODE: Fortran 62 CDC - 1604 PROGRAMMER: Dennis Wilson DATE: July 22, 1963 PURPOSE: To compute the location of a target, given the ranges from two known trackers and the height of the target. USAGE: 1. Calling Sequence: CALL TWBASEC(ECB, RAN1, RAN2, H, SIGN, POST) 2. Arguments: ECB - A 3x2 array consisting of the two trackers' geodetic latitude, longitude(west), and height RAN1, RAN2 - The ranges from the two trackers to the target SIGN - The sign associated with the solution POST - A 3x1 array consisting of the target's geodetic latitude longitude (west), and height 3. Inputs: POSB, RAN1, RAN2, H, SIGN Outputs: POST 4. Routines Called: MTXP, MTXT, QUTS, ECGD 5. Linkage: None 6. METHOD: See LRSS "Program Description Document FADAC," by Autonetics,

T-44

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REMARKS: All units are meters or degrees.

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415 PROJECT: Geodetic SECOR NO. TITLE: Compute Two-body Prediction in Inertial Coordinates CATEGORY; Trajectory IDENTIFICATION: Subroutine TAEVIN CODE: FORTRAN 63 GDC 1604, 3600 PROGRAMMER: F. C. Forbes, Jr. DATE: 3-31-64 PURPOSE: With the injection vectors  $R_{\rm E} V_{\rm E}$  and a time interval given, predict the position and velocity vectors based on Keplerian two-body motion at a time increment DT forward of  $\mathbb{R}_{\mu}$  V_µ. USAGE: Calling Sequence: Call TWBVIN (RE, VE, DT, RI, VI) Inputs: RE(3), VE(3) = position and velocity vectors of a vehicle in freefall expressed in earth centered, equatorial coordinates and in units of feet and feet/second. DT = time interval in seconds over which the two-body prediction is to be performed. Outputs: EI(3), VI(3) = predicted position and velocity vectors of a vehicle expressed in a non-rotating, space fixed (i.e., inertial) earth centered coordinate system and in units of feet and feet/second.

Routines Called: None

Linkage: Explicit transfer

- METHOD: Kepler's equation of mean motion is iterated to give the change in eccentric anomaly, which in turn is used to compute integration constants and then the desired forward predicted vectors.
- REMARKS: The iteration of Kepler's equation is based on a convergence test given by

$$\Delta E_{i+1} - \Delta E_i - K \Rightarrow 0$$

where  $K = 2.000001 \times \Delta E_{1}$ 

 $\Delta E$  = change in occentric anomaly.

A variable K allows control of truncation and maintenance of prediction accuracy. This routine is very accurate and is used primarily in conjunction with ENCKE's method of trajectory prediction.

T-45

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NO: TPCO6
                                          PROJECT: Bluerock
TITLE: Net Perturbations
CATEGORY: Impact Prediction
                                          IDENTIFICATION: Subroutine NETPT
CODE: Fortran 62
                    CDC - 1604
PROGRAMMER: L.Bruce Palmer DATE: June 1964
PURPOSE: To compute acceleration components of vehicle in free-fall, given
          position and velocity.
USAGE:
         Calling Sequence: CALL NETPT (RO, VO, AC, KP)
     1.
     2.
         Arguments:
                      RO(3) - Position vector in equatorial coordinates
                      VO(3) - Velocity vector in equatorial coordinates
                      AC(3) = Acceleration vector in equatorial coordinates
                                       KP = 1 Add drag and lift effects
                      KP
                            - Code:
                                       KP = 2 Do not add drag and lift effects
                            - Table of drag coefficients vs. mach. speed
                      FMD
                            - Number of values in FMD array
                      NO
                      CO
                            - Fit coefficients used in determining acoustical
                              velocity
                      FMASS - Mass of vehicle (1bs)
                            - Eff stive cross-sectional area of vehicle (FT^2)
                      ΕA
     3. Inputs: RO, VO, KP
     4. Outputs: AC
         RourinesCalled: GRAVITY, EQGD, ADEN; ACVEL, DRAG
     5.
         Linkage: COMMON/PERT/FMD(20,2), NO, FMASS, EA, CO(4,5)
     6.
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METHOD: .

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REMARKS: Units are in feet and seconds.

NO. TP 005 · PROJECT: Bluerock TITLE: Predict Free-fall Position and Velocity with Perturbations CATEGORY: Trajectory Prediction IDENTIFICATION: Subroutine TBWPT CODE: Fortran 62 CDC-1604 PROGRAMMER: Fred C. Forbes, Jr. DATE: January, 1964 PURPOSE: Given injection vectors predict the position and velocity vectors of a vehicle in free-fall at a future time. USAGE: Calling Sequence: MALL TBWPT(RQ,VQ,CT,DT,RN,VN,KP) 1., 2. Arguments: RQ(3), VQ(3) - Vehicle injection vectors in equatorial coordinates CT - Time interval between restifications of acceleration DT - Time to be predicted ahead RN(3), VN(3)- Vehicle position and velocity vectors at time DT ahead of injection in equatorial coordinates КP - Code: KP=1 Lift and drag effects added to acceleration KP=2 Lift and drag effects not added З. Inputs: RQ,VQ,CT,DT Outputs: RN,VN 4. 5. Routines Called: TWBVIN, NETPT 6. Linkage:

METHOD:

REMARKS: Units are feet and seconds,

T -47

PLOTECT P-49 No. 2 TTTLE - LAPTRI PAU 13 CAT TAPY: ULS .... IDENTIFICATION: SUPPORTING RADIUS CODE: Fortran CP PL:-1.14 PREPARMAR: DATES LASHA DATE: 8Nov 1963 PURPOSE: Pinis the earth's radius and normal from a geodetic or peopertrie infinde. PSAGE: CALL PADTUL (X'AT, GDP/D, CCBAD, GDNORM, GCNORM) 1. Calling Sequence: 2. Areumenta: XLAT -Latitude in radiana GDRAD -Sarth' radius in meters if latitude ir peodette CCR4D -Serth's red us in meters if latitude is pencentric GENOPM -Earth's norme, in meters if latitude is recording GUNDER -Farth's normal in meters if latitude 1s geocentric 3 Jucuta: XLAT 4. Outpats: CDHAD, CCEAD, GENORM, GENORM 5. Pout ines naeri: None MED HOUL

4

norma.  $\frac{a}{(1-e^2SIN^2 \frac{1}{4})^{\frac{1}{2}}}$  radius  $\frac{b^2+L^2e^2cps^2 \frac{1}{4}}{b^2}$  $\Phi_0 = \operatorname{ARCTAN}((2/b)^2 \operatorname{TAN}(\Phi_c))$ 

Pamarka: Isrumob the constants of Clarke's Scherold of 1866,

No. 6400 TITLE: Unknown Station Solution - 5, 3 GATEGORY: Data Processing GODE: Fortran 63, CDC 1604 PROGRAMMER: Dennis wilson PURPOSE: To compute the position of an unknown fourth station from

three spans of satellita position and range data.

USAGE: 1. Card Input

- (1) Title Card 80 columns
- (2,3,4) Time Cards: first time (H,M,S,MS) 1215, 15%, 15 last time (H,M,S,MS), dolta time (H,M,S,MS), Logical tape number

10A8

- (1, 2, 3)
- (5) Unknown station location (latitude, 3(17.10, 3X) longitude, height)

### 2. Megnetic Tope Assignment

Two or three JF tares assigned to HD1, HD2, and/or HD3 corresponding to time cards.

### 3. Printout

The unknown station position is computed with each succeeding set of three satellite position. The results of each computation are listed with the deviation from the input position and the average solution. This is preceded by a summary including input data, average deviation from the survey position and RMS error.

### REMARKS:

<u>1</u> ]

1. The shortest of the three spans controls the number of solutions attempted.

2. Two spans may be taken off one SP tape as long as the earliest span timewise is in the deck first.

NC. 3805 PRUJECT: Geodetic SECOR TITLL: List Packed Geodetic SECOR Tape CATEGORY: Data Processing IDENTIFICATION: Frogram EXAMPCK CODE: Fortran 63, CDC 1604 PECGRAMMER: Dennis Wil on FURPOSE: To produce a listing of one or more sets of station data from · a packed tape.

USAGE: 1. Card Input

(1) Title - 80 columns. 1048

(2)Indicators

> IND1-IND8 Desired data l=yes, 2=no

IND9- No. samples to skip

2. <u>Magnetic Tape Assignment</u>

One input tape on logical unit one.

3. Printout

The listing is by station with the station name (from the tape) at the top of the page and 55 simples. One such page is output for each station indicated.

1615

EIMASKS: 1. Program begins listing with the first sample on the tape and terminates when the end of lile is encountered.

NO. G800	5		PROJECT:	Geodetic 4	SECOR .	•	
TITLE: 1 CATECORY: CODE: Fo PROGRAMME FURPOSE:	fime Dortr R: .To on ti	Synch and Pack ata Processing an 63, CDC 1604 Dennis Wilson input two to eig e or more packed- me synchronized a	ES Tapes IDENTIFICA ght Geodetic SECC output tapes. I as it is packed.	VTION: Pro DR ES tapès Data from	ogram PACK s and produ the station	ES uce ns is	
USAGE: 1	L.	Card Input	*	-		`	
		(1) Title - 80 d	columns	1048			
		(2) Indicators		1615			
		IND1-IND8 = IND9-No. sar IND10-No. or	input tapes used 2=no, 1=yes ples to skip atput tapes	1.;-			_
		(3) Time Card		1215			
		First time ( Bast time () Delta time ()	(H,M,S,MS) H,M,S, <u>M</u> S) (H,M,Š,MS)				-
		(4) - (11) State	ion Calibration (	lards	3(E17.10,	3X), 12	X, A8
			Range Calibration IC Calibration Time Calibration Station Name	on 1 (sec)			,
2	2. <	Magnetic Tape As:	signment				
	-	Any logical unit indicator card. logical unit 9,	1-8 may be used The output tapes	for input 3 are moun	as indica ted ștarti	ted on ng on	-
с м	5.	Frintout			-		

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ч**су** Хл Input cards are listed along with self-explanatory indications of tape synch.

TAPE FORMAT: The generated output tape record consists of eight blocks of data. Each block is "ormated identically and consists of data from different input tapes.



15. NOT USED

LEMARK3:

A.

1. Data blocks not containing data are zeroed except for the first word which contains a floating point 2.

2. The output tapes are terminated with an end of file.

3. If the first sample is bad, the range calibration will be an error by -9.0.

4. If the IC is not locked, an erroneous IC calibration may result.

5. The maximum number of samples which may be recorded low density ~ 5000 or ~8 mm of data & 10 samples/sec.

T - 52

2

(1' 1913) FOF NO, PROJECT.: Fif .: DOWL: Tank Iteratively Fit Lonospheric Refraction CAT GORY: Genoral IDENTIFICATION: - Program IONITR CODE: Fortran 62, F63 CDC-1604 PROGRAMMER: Fred C. Forbes, Jr. DATEL PURPOSE: To iteratively solve for FMAX, BIAS, and CONTROL CONSTANT USAGE 1. ng Sequence: Program IONITR 2 ints: CARDS ъ DESCRIPTION FORMAT <u>71)</u>-Title 1048 (2)Indicator Cardi (311,17X,3(E17.10,3X)) NSOL(1) = Code: HSOL(1)=1 if calibrated - NSOL(1)=0 if not calibrated NSOL(2)=1 if FMAX is calibrated NSOL(2)=0 if FNAX is not calibrated NSOL(3) *1 if slope constant NSOL(3)=0 if Nosslope calibration (3) R,H,DRM, ICONT (3(E17.10,3X),15X,15) R = Range, in meters H = Height in meters DRM = Ionospheric correction ICONT#=Code: ICONT#1 end of data ICON1=0 continue data input Routines Called: IONO, MTXP, MTXA, MTXI

METHOD: Least squares adjustment of IC with calibration, FMAX, and/or slope.

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REMARKS

NO. 0412

CATEGORY :

1

PROJECT: General TITLE: Compute Predise Trajectories and Orbits from fit to Equatorial IDENTIFICATION: Program PCMPTJ

T-54

### DATEN 2-1-64

CODD: Fortrans D2 -CDC+1504 PROGRAMMER: Fred C. Forben, Jr.

Trajectory

Coordinates

PURPOSE: Compute precise trajectories and orbits with compensation for 2nd, 3rd and 4th zonal harmonics of the earth, atmospheric drag, and lift. Optional initial conditions of time, position and velocity vectors or two positions and apogee height are provided as well as provision for iterative least squares fit (with or without weighting) to the vehicle position coordinates. Equatorial coordinates are listed and topocentric coordinates are computed and listed with respect to cny. number of sites on the earth's surface. The final orbital parameters are adjusted to input equatorial coordinates.

USAGE: CÂR	DS Tradition	DESCRIPTION	FORMAT	
inputs: (4 (2	) ALTRE ) IOPTN IOPTN	NO., ITER, KP, KWT, IDTI, IUNITS initial conditions optio OQ1 - time with two posi and apogee height OQ2 - time with equatori	$ \begin{array}{c} \mathbf{A}  \mathbf{BU}  \mathbf{R} \mathbf{D} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} \mathbf{I} \mathbf{G} I$	
-	NC	<pre>position and veroc = number of input position fo be fit by iterative 1 sources NO 200</pre>	vectors east	
	ITER	= number of iterations of	the fit	
·	KP	= perturbation option indi 001 - drag and lift 202 - no drag and lift	cațor	-
	ĸwţ	<ul> <li>Teast squares weighting</li> <li>301 = input weighting</li> <li>302 = no unighting</li> </ul>	option.	3
-	IDŤĮ	<pre>&gt;&gt;&gt;&gt;&gt;&gt;&gt;&gt;&gt;&gt;&gt;&gt;&gt;&gt;&gt;&gt;&gt;&gt;&gt;&gt;&gt;&gt;&gt;&gt;&gt;&gt;&gt;&gt;&gt;&gt;&gt;&gt;&gt;&gt;&gt;</pre>	computation	
(Intion ) (3	) TT -=-	time of epoch	E17:192	
Option 1 (4		latitude: longitude, heigh	t of epoch 3(E17,10,3X)	
Option 1 (5	) CI =	latitude. longitude, heigh	t of second	
- <b>F</b>	÷ ÷	point on trajectory	3(E17,10,3X)	
Option 1 (6	5) AL =	apogee waight (AL is locat between CO and CL)	ed E17.10	
Option 2 03	) TI,RE	time and pomition vector a epoch where RE is the equa	it itoriàl	
		coordinates	4E20.10	-

*IUNITS = units code of input injection vectors (see (3) for code ID).

NU. 0412 Cont. Option  $2 \langle 4 \rangle = VE =$ equatorial velocity components 3 E20.10 at epoch KP=001 ( 7)-(16) FHD = table of mach speed versus drag coefficients. 4(E17.10.3x) KP=001 (17)-(23) table of curve fitting coefficients 4(17.10.3x)KP=001 (24.) INDT, FMASS, EA. 120,2(E17.10,3x NOT = number of coefficients in table FMASS = vehicle mass in pounds vehicle cross sectional area in ft² EA E (25.) TM, TRJP = trajectory points for fitting 4 E20,10 TM = fime in seconds TRJP =  $X_{E}, Y_{F}, Z_{E}$  of which (26) Same as 25 until NO (see item 2) are inpût COSITE E latitude, longitude, height of -KWT=001 -(27): local origin for error propagation 3(E17.10,3x) NWT=001 (28) IEQU, SITE 13,X17, 3(E17.10,3x) IEQU = equipment selection code. ∘001 ÷ "range 002 = height 003 = Ladirection cosine 004 = Madirection cosine 005 = azimuth 006 = elevation SITE = latitude, longitude, and height of equipment site KWT=001 (29) EM, ICONT = error model 5 E17.3,15 EM(1) = equipment error EM(2) = tropospheric refraction EM(3) = scale factorEM(H) = site survey EM(5) = ionospheric refraction for range and height equipment EM(S) = baseline length for L and M ICONT = continuation code ICONT(0) = continue input of EM TCONT(1)= indicates Test site input (30), (31) Same as (28) and (29) for all tracking KWT=ÖO1 equipment TO, DT, TF = times for forward (32.) 3(E17.10,3x) predictions TO = first time DT = time interval TF = final time of prediction ((TF-TO) /DT <1000) per run) (33) IPUNCH, IUNITS 213 IPUNCH = punch output code 000 = no punch output 001 = punch output IUNITS = output units code 001 = feát 002 = meters 003 = statute miles (-5280*)-004 = nautical miles (6076.10333') 005 = yards

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NO. 0412 Cont.

36) TITLE =	aite name	card
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(37) CS = latitude, longitude, height of points on earth to which trajectory points will be referred; A80 Hollersth

3(E17,10,3x)

(38); (39.) Same as (36); and (37.) for all

desired sites.

Output: From Fitting:

All input data are dumped for reference. On successive iterations, the adjusted injection vectors, as well as the difference between each predicted point and the corresponding input data are listed. The difference between the two-body prediction of position and velocity and the total field prediction values are listed. The error propagation (inverse weighting) in the XYZ coordinates are also listed when weighting is called out.

In Equatorial Coordinates:

Point number, hours, minutes, seconds, total seconds, XYZ, XYZ, latitude, longitude, height, and associated titles.

In Topocentric Coordinates:

Point number, hours, minutes, seconds, XYZ, XYZ, in local east-north-up coordinates, slant range, surface range, range rate, azimuth, elevation angle, and height ANSL with titles.

Method:

Trajectory prédictions are computéd by a method based on computing a reférence trajectory with closed form twobody equations and then adding numérically integrated perturbation terms.

In the least squares fitting, unity weighting or weighting based on the propagation of major sources of observational. error into pusition variance and covariance, are optional. See program GENEPQ No. 617 FCF, for method of error propagation.

Remarks:

All input is expressed in feet, seconds, degrees, and ratios. In the error propagation refraction is input as the ratio of the residual error to the total (mean atmosphere) correction (1.e., 5% residual would be input as 0.05). Scale factor, baseline length, and site survey are ratios. An error in site survey of 1 PNM would be input as 0.00001.

If punch output is desired, the source deck should be modified to give the desired output.

Reference should be made to the program listings for all necessary subroutines and memory usage.

PROJECT: FISHBOWL NO. 402 TITLE: Predict Two-Rody Position, Velocity, Partial Derivatives CATECORY: Trajectory IDENTIFICATION: Subroutine TBFVU CODE: Fortran 62, 63 CDC 1604; 3600 DATE: 1-10-62 PROGRAMMER: F. C. Forbes, Jr. PURPOSE Fredict two-body position and velocity vectors and optionally

the (3x6) matrix of two-body partial asrivatives with respect to position expressed in units of feet, feet/second, and in an coordinate system. inertial

UŜAĜE:

Calling Jequences CALL TERVS (TO, TM; VEC, PTL, NOTE) 1. Arguments: 2.

> INPUTS: TO = time of apoch or injection in seconds TM = time of forward predicted data in seconds'

CUTPUTE: VEC(E) = array of position and velocity components in inertial coordinates and in feet and feet/second.

-	<u>ax</u> ax	0Y0	•	•:	•	δx dż _c	
PTL 18/=	<u>26</u> 26	0 <u>57</u> 0	•	•	•	·	partial derivatives of predicted position vector
	3 <u>3</u> 0%	•	•	•	1 <b>•</b>	<u>25</u>	with respect to injection vectors. R V. o o.

NOTE = option indicator 1 = compute VEC only2 = compute VEC and FTL

3. Routines Called: MTXP, MTXT

Jubroutine TRJX or TRJKX 4. Linkage: COMMON/TRJCNTS/CU(3), PO(6), RO, AI, AIS, AAIS, GAMO, BATO, ECC, EO, DBC(6), DAI(6), WE, DCO(6), PTLI(3,6), VECI(6), IMINV(3,3)

Iterate Kepler's equation based on the time of prediction to compute the change in the eccentric anomaly. Integration constants are then computed and used to form the predicted quantities.

REMARKS:

METHOD :

This routine is used in conjunction with subroutine TRJK or TRJKX, which computes all necessary ponstants used in TBPVS. TBPVS 13 used in trajectory fitting, error propagation, and simulation programs.

NO. CO 413 FCF PROJECT: Gaodetic SECOR Adjust Range and Velocity to Input Trajectory Points using Precise TITLE IDENTIFICATION: Subroutine PTRJFT Trajectory Predictions CATEGORY: Trajactory Prediction CODE: Fortran 62 DATE: PROGRAMMER: Fred C. Forbes, Jr. PURPOSE: To predict a trajectory path using initial injection vectors. USAGE: Calling Sequence: CALL PTRJFT(TO,RO,VO,NO,TM,TRJP,ITER,KP,KWT,DTI) 1, 2. Arguments: NO - No. input position vectors to be fit by iterative least squares NO< 200 ITER - No. iterations of the fit KP - Perturbation option number: 001 = drag and lift 002 = no drag and lift KWT - Least squares weighting option:001 = input weighting 902 = no weighting TRJP - Latitude, longitude and height above mean sea level of vehicle TO - First time for prediction DTI - Time interval TM - Time of forward predicted data in seconds RO - Adjusted range injection vector VO - Adjusted velocity injection vector 3, Inputs: NO, ITER, KP, KWT, TRJP, TO, DTI, TM 4. Outputs: 20, VO Routines Called: EQCOOR, TBWPT, TBPVS, MTXT, MTXP, GEP, MTXA, INSS 5, METHOD: Trajectory predictions are computed with closed form two-body equations add ing numbrically integrated perturbation terms.

REMARKS: Input is expressed in feat, seconds and degrees.

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PROJECT: Geol'etic SECOR NO. CO412A TITLE: Call in Drag Coefficients CATEGORY: Trajectory CODE: F62, 63 PRCGRAMMER: P. C. Forbes, Jr. IDENTIFICATION: Subroutine DRGCOF DATE: PURPOSE: To read in drag coefficients USAGE: 1. Calling Sequence: CALL DRGCOF(KP) 2. Arguments: KP = option indicator1 = read in coefficients  $2 \propto used$  as a dummy routine 3. Inputs: 4. Outputs: 5. Routines Called: none 6. Linkage: COMMON/PERT/FMD(20, 2), NO, FMASS, EA, CO(4, 6) METHOD:

REMARKS:

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FCF/kkb

PC. 6320

.II h: Three Fa. 's Columpi. JARDAUTY: U-JIH-(User Sectors of the - Bat PFOJECT

IDENTSFICATION: Subreutine SOLID

DATE: May 12, 1962 PROTECT: De l'Estado -PPPONT: To empute a rerget's position relative to she gerierien "rate, given the losselor of three trackers in this reference litze, the three ranges from the truckers to the tright, and the sim tarks as retained with the z coordinate of the target The superious conten. The zearls of the seyster is hereal to a plane pesiding through the three trackersdand directed "up." 504012

1. CALLERS Superne: CALL SOLUT (CTA. P. SIGH, X; "Y. C) (A

2. Arguments: ETI - A 5x3 urray of the base station poel tions in the artistrary \$.Y.S eveter. Tim thret subceript 1.2.3 refere to X.X.Z and the Suddid subscript indicatos the kupe station number (1.2.8). - A 5x1 array of the ranges from base distions to fir target. The suborript reference the buse shation number.

SPT - Sther +1.0 c -1.0 to analgh the alth of t in the s system, .

1, 5, 34 The coordinates of the surport in the system in which the trace station locations were Baterid

3. Tuput: SIX, P. ETGN

4, Conference X, f

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Four le be Culler: TAPGET, FOTATE a.

METRON :

The shares the sense the TARGET and POTATE subroutines to deter mile the terret public. The coordinates are translated to ass station one and retained into the s system using the WTAT a subroutie. We zention is then made by the TARGET subroutine and the results transformed back to the optimizal systemic

REM/FRE:

PROJECT Geodette SECOR 332.5 NO. TITLE Three Pange Solution--Flane Jysten Subrouting TAPOET 15 CATEDORY . UELDETS CODE Fortran 62 CDC 1604 Pay. 17, 1963 DATE BROGRAMMER . Nennle Wilson PURROSE I To compute the position of some target using ranges Srow three base stations. The moults are relative to a plune woordinate system whose x-y plune passes through the three base stations and whose conter is not base station one. USACE CAPL TARGET(STA, RI, B2, RS, SIGNZ, X, Y, 2) 1. Calling Sequence Arguments. STA A 3x3 matrix of the xyz positions of the three base stations in the plane coordinate SYSTEM. NOTE: STALL, 1)-STA(2, 1)=STA(3, 1)= STA(3,2)- 3TA(3,3)=0 FT,82,83 The three granees STANZ The sign of the x coordinate The farget's position in the plane system k, Y. 3 STA, RI, PR. P3, SIGN7 Thout X, Y, Z Output RETHON x=K1 R12+ K1 R12+ K1 R12+ Ky y = K5. R1 + K6 R2 + K1 R3 + K4 = 3 = + [Ri - x2 - 32]

BEMARKS

Program SOLUT nass this bubbouling and converts between the local system and plane system

No. 0390 PROJECT: Geodetic SECOR TITLE: List Satellite Position Tape IDENTIFICATION: Program EXAMSP CARLORY: Special Furpose 1 CODE: Fortran 63, CDC 1604 PROGRAMMER: Dennis Wilson PURPOSE: To list all or part of the data on a Geodetic SECOR SP tapes Cará Inpat USAGE: 1. (1)Title - 80 columns 10A8 (2) indicator Card 315 ILL = no. samples to skip IND2 = print option 1 = 1 = yes1:03 - print option 2 2 = no > 1215 (3) Times - first time (H, M, S, ML), 10st time (H, M, 3, MS), delta time (H, M, J, MS) 2. Magnetle Lave Assignment Gue SF tape on Legical unit HD1 E. Printout (1)Input data -(2) lime, satellite position, ... Option 1: range data from each station Option 2: permuted solutions (3) (4)

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The two print options may be included or not independently.

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NO. US. PRCJ.CT: TITL: Quad Test for the Azimuth from North to East CATEGORY: Utility IDENTIFIC ATON: Subroutine QUTS CODÉ: Fortran HI CDC - 1604 PROORAMMER: Fred Forbes 04...: 6-28-63 PURPOS : US das 1. Calling Sequence: CALL QUTS (X, Y, A) 2. Arguments: X - X-component Y - Y-component - Radians A 3. Inputs: X, Ŷ Output: A 4. Routines Called: None 5. ML THOD:

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T-63°

# NC. U 2 PRCJECT: TITLE: Form Unit Vector CATERRY: Utility COTE: Fortran II CTC - 1604: ROGARMAR: Fred Forbes PURPOSE: USINA: 1. Calling Sequence: CALL UTYT (A, B, I) 2. Arguments: $A = V_{obtor}$ $B = \frac{Ax}{|A|/x|}$ I = Total elements

3. Input: A, I 4. Cutput: B 5. Routines Called: None 6. Linkage: DIMENSION A(1), B(1) Mathol:

T-64

, -. . NO.: U 3 PROJECT: TITLS: Form the Sum of the Squares CATEJORY: Utility CODE: Fortran II CPC - 1604 PROGRAMMER: Fred Forbes PURPOSL: USAJE: 1. Calling Sequence: CALL SMSQ (A, B, I) 2. Arguments: A = Vector  $B = \sum (A_{C})^{2}$ I = Total elements 3. Input: A_S I 4. Output: B 5. Routines Called: None 6. Linkage: CIMENSICE A(1) METHOD:

NG. 444 TITLE: Form Scaler Matrix Product C.T.JORY: Utility ODE: Fortran II CDC - 1604 PROGRAMMLR: Fred Forbes PUREOS. ; US AFE: 1. Cailing Sequence: CALL SCET (A, B, C, I) 2. Arguments: A - Scaler B - Matrix C - A+B I = Total elements £. 3. Input: A, B, I 4. Output: C 5. Routines Called: None Linkage: DIMENSION B(1), C(1)

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PROJECT:

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IDEN-TIFICATION : Subroutine CMT DATE: 2-12-63

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PROJECTI
NO. 11.5
TILE: Compact an Array into a Parger Array.
CATEGORY: Utility
                                         IDENTIFICATION: Subroutine TXC
CODE: Fortran II
                     CDC - 1604
PROGRAMMER: Fred Forbes
                                        DATE: 5-28-63.
PURPOSE:
USAGE:
     1.
        Calling Sequence: CALL MTXC (A, B, TA, IB, IC, IE, IE)
Arguments: A - Composite array
     2.
                          - Segment of array
                      В
                      IA - Rows in A
                     IB - Columns to skip in A
                      IC - A column elements to skip to first B element
                     ID - Rows in B
                      IE - Columns in B
        Input:
     8.
    4. Quiput:
5. Routines Called, None
     6. Linkage: DIMENSICN: A(1), B(1)
METHOD:
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T-67_

REM IRKS :

NO. U.6 PREJECT: TITLE: Magaltude of a Vector CATLGORY: Utility IDENTIFICATIN: Subroutine MGVT CCD5: Fortran I, CfC - 1604 FROJR/MMLR: Fred Forbos DATE: 6-28-63. PURPOSI.: USA.5: 1. Culting Sequence: CALL NO (A, B, I) 2. Arguments: A - Vector B - /A/II - Total elements: 3. Input: A, I 4. Output: B 5. Routines Culled: None 6. Linkage: DIMENSION A(1) METHOD:

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# NC. U 7 TITLE: Matrix Addition CATCORY: Utility CODE: Fortran II CDC - 1604 PROGRAMMER: Fred Forbes PURPOSE: USADE: 1. Calling Sequence: CALL MIXA (A, B, C, I) 2. Arguments A = Matrix B = Batrix $C = A \neq B$ i = iI. - Total elements 3. Input: A, B, I 4. Cutput: C 5. Routines Called: None c. Linkage: DIMENSIEN A(1), B(1), C(1)

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NO. U 8 PROJECT: ATTLE: Matrix Subtraction CATEGORY: Utility IDENTIFICATI #: Subroutine MTXS CCDA: Fortran II CPC PROIR WMER: Fred Forbes 010 - 1604 DATE: -6-28-63-FOR (SA: USALE 1. Calling Sequence: CALL MTXS (A, B, C, I) 2. Arguments: A --Matrix B - Matrix  $C = A_1 = B_1$ I - lotal elements 3. Input: A, B, I 4. Output: C 5. Routines Called: Mone 6. Linkage: DIMINSION A(1), B(1), C(1) -HS.BT:

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NO. U 9 · PROJECT: TITLE: Matrix Transpose CATEGORY: Utility IDENTIFICATION: Subroutine MTXT CODE: Fortrans 62 CDC - 1604 PROGRAMMER: Fred Forbes DATE: 28 June ]963 PURPOSE: To transpose a NxM matrix to a MxN matrix. USAGE : ]. Calling Sequence: CALL MTXT (A, B, N, M) 2. Arguments: A - Matrix (NXM) B - Matrix (MxN) N - Rows of matrix A, columns of matrix B M - Columns of matrix A, rows of matrix B 3. Input: A(NxM) 4. O ctput: B(MxN) Routines Called: Nong 5, 6, Linkage: DIMENSION A(1), B(1)

METHOD:

REMARKS:

T-71

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NO. U 10 PROJECT TITLE: Matrix Product IDENTIFICATION: Subroutine MTXP CATEGORY: Utility CODE: Fortran 62 CBC - 1604 PROGRAMMER: G; Rutherford PURPOSE: To multiply Matrix A by B and store results in C. USAGE : 1. Calling Sequence: CALL MTXP (A, B, C, N, M, K)
2. Arguments: A - Matrix (NxM) B - Matrix (MxK)-C - Matrix (NxN): C = A * B N = Rows in Matrix A, rows in Matrix C M - Columns in Matrix A, rows in Matrix B R. - Columns in Matrix B, columns in Matrix C Input: A(NxM), B(MxK) Output: C(NxK) 3. 4. 5. Routines Called: 6. Linkage: DIMENSION A(1), B(1), C(1)

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### REMARKS :

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## PROJECT: OLV.R

NO. U II TITLE: Vector Multiplication CATEGORY: Utility CODE: Fortran 62 CDC - 1604 PROGRAMMER: Dennis Wilson

METHOD:  $\vec{R} = \vec{R}_1 \times \vec{R}_2$ 

IDENTIFICATION: Subroutine VECMPY

DATE: November 20, 1963.

PURPOSE: To form the vector product of two vectors (cross product).

USAGE

3

Calling Sequence: CALL VECMPY (RI,R2,R3)
 Arguments: RL,R2,R3 - 3xl arrays for the three vectors
 Input: R1,R2
 Output: R3
 Routines Called: None

REMARKS :

NO. U 12 TITLE: Matrix Inversion and Einear Solution CATEGORY: Matrix Operations CODE: Fortran 62 CDC - 1604 PROGRAMMER: (From the UCSD Library) DATE: 22 June 1963

PURPOSE: To invert a matrix up to 20x20 and solve the matrix equation if desired.

USAGE:

1. Calling Sequence: CALL MATINV (À,N,B,M,W) 2. Arguments: A - Equals À inverted out

> N - The size of the matrix
>  B - Equals B times A out
>  M - Control; 0 if B is not to be computed, 1 if it is to be computed
>  W - The characteristic determinant

> > T-74

3. Input:

4. Output:

5. Routines Called:

METHOD: A more complete description is available in the University of California at San Diego write-up. A copy of this is available in the Master File of this series.

RENARKS: The A space should be reserved as 920, N), B(20), and W(1).

NO. UL3 PROJECT': ODVAR TITLE: Rotation Matrix CATEGORY: Utility IDENFICATION: Subroutine ROTMX CODE: Fortran II CDC - 1604 PROGRAMMER: Dennis Wilson DATE: August 13, 1963 -PURPOSE: To forma notation matrix given the angle and the axis about which to rotate. Ľ, USAGE: 1. Calling Sequence: CALL ROTNX(11,12,13, ANGRAD, ROT) 2. Arguments: 11,12,13 - Indicators: # 0 axis about which rotation is made the other two axes 51 ANGRAD - The angle in radians ROT - A 3x3 rotation matrix 3. Inputs: 4. Outputs: 5. Routines Called: None .6. Linkage: METHOD: Example: To rotate by an angle Alpha about the Y-axis to form matrix A; CALL ROTHX (1,0,1, ALPHA, A) cos o sine <u>.0</u> 1 0 sin~0 cos~ REMARKS:

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FROJECT: ODVAR NO. U 14 TITLE: Quadrant Test - Polar Angle-CATEGORY; Utility IDENTIFICATION: Subroutine QUAD CDC - 1504 CODE: Fortran II PROGRAMMER: Dennis Wilson DATE: August 8, 1963 PURPOSE: To compute the polar angle (CCW from X-axis) from the X and Y components.

USAGE:

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Calling Sequence: CALL QUAD (X,Y,ANGDEG,ANGRAD) 1. X,Y - X and Y components in any system of units 2. Arguments: ANGDEG - Angle in degrees CCW from X-axis ANGRAD - Angle in radians. CCW from X-axis

з. Inputs:

4. Outputs:

Routines Called: None 5:

Linkäge: None δ,

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METHOD: Arctangent function and quadrant test.

REMARKS:

X and/or Y may be zerò.

Т-76

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NÓ:Ú 15PROJECT:GeneralTITLE:Compute Equatorial Coordinates and Rotation MatrixCATEGORY:GéometricCODE:Fortran 62,63CDC = 1604PROGRAMMER:F.C. Forbes, Jr.DATE: 2-6-64

PURPOSE: Compute equatorial coordinates and topocentric to equatorial rotation imatrix from the geodetic Patitude, longitude, and height above mean sea level.

USAGE

1. Calling Sequence: CALL EQCOOR (COOR, XYZ, GD, MTFT) 2. Arguments:

COOR =3 element array -- geodetic latitude, east longitude in degrees, and height AMSD in feet.

XYZ - 3 element array -- equatorial coordinates in mèters or feet GD -9 element array -- local east-north-up to equatorial rotation matrix

T - 77

MTFT - units option on XYZ output

- 1 = meters
- 2 = feet

3. Inputs: COOR, MTFT

4. Outputs: XYZ, GD

METHOD: See coding.

REMARKS: The Clark spheroid of 1866 is assumed for all computations. Degrees and feet are input and feet or meters are optionally output.

ODE: FOR	ortran 62 CDC = 1604 ER: Dennis Wilson DATE: May 16, 1963
URPOSE:	To use geocentric coordinates of a point to determine the geodetic latitude, longitude and height.
SAGE:	· · ·
1.2.	Calling Sequence: CALL ECGD (X,Y,Z;SLAT,SLONG,HT.) Arguments: X;Y,Z = Location of a point in geocentric coordinates. X=axis is in the equitorial plane and is through the prime meridian; the Z-axis is along the minor axis of the geode and passes through the north pole Y is chosen to form a right-handed system.
	SLAT,
	HT - The geodetic coordinates of the point. SLAT is the latitude (positive north of equator) in degrees, SLONG is the longitude (west longitude) in degrees, HT is the height above the geode along the local
	normal in metors.
3.	normal in metors, Inpūt: X,Y,Z
3. 4.	normal in metors. Inpût: X,Y,Z Output: SLAT, SLONG, HT
3. 4. 5.	normal in metórs. Inpüt: X,Y,Z Output: SLAT, SLONG, HT Routines Called: None
3. 4. 5. Ethod:	normal in metors. Input: X,Y,Z Output: SLAT, SLONG, HT Routines Called: None The calculation uses the method described on pp.15-16 of ASTIA document #90538. This is an iterative solution for determining latitude and height. Constants for the Clark Spheroid of 1866 were used.
3. 4. 5. Ethod:	normal in metors. Input: X,Y,Z Output: SLAT, SLONG, HT Routines Called: None The calculation uses the method described on pp.15-16 of ASTIA document #90538. This is an iterative solution for determining latitude and height. Constants for the Clark Spheroid of 1866 were used.
3. 4. 5. Ethod:	normal in metors. Input: X,Y,Z Output: SLAT, SLONG, HT Routines Called: None The calculation uses the method described on pp.15-16 of ASTIA document #90538. This is an iterative solution for determining latitude and height. Constants for the Clark Spheroid of 1866 were used.
3. 4. 5. Ethod:	normal in metors. Input: X,Y,Z Output: SLAT, SLONG, HT Routines Called: None The calculation uses the method described on pp.15-16 of ASTIA document #90538. This is an iterative solution for determining latitude and height. Constants for the Clark Spheroid of 1866 were used.
3. 4. 5. Ethod:	normal in metors. Input: X,Y,Z Output: SLAT, SLONG, HT Routings Called: None The calculation uses the method described on pp.15-16 of ASTIA document #90538. This is an iterative solution for determining latitude and height. Constants for the Clark Spheroid of 1866 were used.
3. 4. 5. Ethod: Emarks:	Normal in metors. Input: X,Y,Z Output: SLAT, SLONG, HT Routines Called: None The calculation uses the method described on pp.15-16 of ASTIA document #90538. This is an iterative solution for determining latitude and height. Constants for the Clark Spheroid of 1866 were used.
3. 4. 5. 1ethod:	Normal in metors. Inpüt: X.Y.Z Output: SLAT, SLONG, HT Routines Called: None The calculation uses the method described on pp.15-16 of ASTIA document #90538. This is an iterative solution for determining latitude and height. Constants for the Clark Spheroid of 1865 were used. Versions using both Clark and International Spheroids are zvailable.

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NO: C0205

TITLE: Invert 3x3 Matrix

CATEGORY: Utility:

CODE: Fortran 62, Fortran 63, CDC-1604, 3600

PROGRAMMER: F.C. Forbes Jr.

PURPOSE: To invert a 3x3 matrix.

PURPOSE: To invert a 3x3 matrix.
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USAGE:

1. Calling Sequence: CALL MTXI(A,B,DETERM)

2. Arguments:

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A(9) = 3x3 matrix

B(9) = 1nverse matrix of A

DETERM- Determinant of A
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3. Inputs: A 4. Outputs: B.DETERM 5. Routines Called: None

6. Linkage: None

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REMARKS :

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NO. CO 114 FCF PROJECT: Fishbowl TITLE: Compute Empirical Ionospheric Refraction CATEGORY: General IDENTIFICATION: Subroutine IONO CODE: Fortran 62, F63 CDC-1604 PROGRAMMER: Fred C. Forbes, Jr. DATE: PURPOSL: USÁGĽ: 1. Calling Sequence: CALL IONO(RM,SIN,DRINO,FMAX,CK,FREQ) 2. Arguments: - Slant Range in meters ·KW - Sine of Elevation Angle SINC DRINO - Range correction in meters FMAX - Maximum electron density in the F2 Tayer CK - Control constant FREQ - Carrier frequency in mc/sec Inputs: RM,SIN,FMAX,CK,FREQ 3. Outputs: DRINO 4., <u>_</u>

Routines Called: None 5.

METHOD:

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REMARKS: 3/0 in units of meters with frequency in mc/sec, FMAXx10-12

PROJECT: General NO. CO 203 FCF TITLE: Compute Vector Dot Product CATEGORY: Utility IDENTIFICATION: Subroutine CCXPD CODE: Fortran 62, F63 CDC-1604 DATE : PROGRAMMER: Fred C. Forbes, Jr. PURPOSE: ÌISAGE': ľ, Calling Sequence: CALL CCXPD (RO,R1,COSV,VR,ROM,RIM) 2. Anguments: RO - 3x1 input array R1 - 3x1 input array ROM - Magnitude of vector RO RIM - Magnitude of vector RI COSV- Conine tof the angle between RQ and R1 VR - Angle between RO and R1 (cos⁻¹ (COSM)) 3. Inputs: RO, RL 4. Outputs: COSV, VR, ROM, RIM 5: Routines Called: None

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METHOD:

REMARKS:

T-81

PROJECT: Fishbowl NO, CO 307 FCF TITLE: Compute Rotation Matrix IDENTIFICATION: Subroutine VECROT CATEGORY: General CODE. Fortran 62, F63 CDC-1604 DATE: PROGRAMMER: Fred C. Forbes, Jr. PURPOSE: Given vectors, compute rotation matrix by vector cross product.

US'AGE :

1. Calling Sequence: CALL VECROT(RO,R1,VO,V1,GVR) 2: Arguments:

RO - 3xl input array R1 - 3x1 input array VO - 3x1 input array VI - 3x1 input array SVR - 3x3 rotation matrix Inputs: RO, RI, VO, VI

3. Outputs: GVR 4.

Routines Called: MTXI, MTXP 5.

METHOD:

REMARKS:

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NO. C0501 TITLE: Convert Seconds to Hours, Minutes, and Seconds to Midnight CATEGORY: General CODE: F-62, 63 PROGRAMMER: F. C. Forbes, JI. DATE: PURPOSE: To convert seconds to hours, minutes and seconds USAGE: 1. Calling Sequence: CALL TIMEC(TSEC, HR, TMIN, SEC). 2. Arguments: TSEC = input time in seconds HR = hours TMIN = minutes SEC = seconds

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3. Inputs: TSEC

4. Outputs: HR, T_{MIN}, SEC

5. Routines Called: none

6. Linkage: none

METHOD

1.1

# REMARKS

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# NO.LIAPROJECT:FISHBOALTITLE:Predict Two-Body Position, Velocity, Partial DerivativesCATEGORY:TrajectoryCOLE:Fortran 62, 63CDC 1604, 3600PROGRAMMER:F. C. Forbes, Jr.DATE: 1-10-62PUNPOSE:Predict two-body position and velocity vectors and optionally

the (3x6) matrix of two-body partial derivatives with respect to position expressed in units of feet, feet/second, and in an equatorial coordinate system.

USAGE:

1. Calling Sequence: CALL TBPVS (TO, TM, VEC, PTL, NOTE).

2. Arguments:

INPUTS: TO = time of epoch or injection in seconds

TM = time of forward predicted data in seconds

OUTPUTS: VEC(6) = array of position and velocity components in equatorial coordinates and in fact and feet/second.

x	ax ax	$\frac{\partial X}{\partial Y_{o}}$	•	•	٠	δx δż.	
PTL(13)=	<u>26</u> <u>9</u> X	<u>76</u> 0	' <b>†</b> '	•	•	•	= partial derivatives of predicted position vector
	<u>26</u> 0X	•		•	•	<u>87.</u>	vectors R V o o

NOTE = option indicator 1 = compute VEC only 2 = compute VEC and PTL

3. Routines Called: MTXE, MTXT

4. Tinkage: Jubrouting TRJK or TRJKX Common/TRJKS/CU(3), PI, WE, RO, PO(6), AI, AIS, AAIS, GAMC, BATO, ECC, EC, DEC(6), DAI(6), DGC(6)

METHOD: Iterate Kepler's equation based on the time of prediction to compute the change in the eccentric anomaly. Integration constants are then computed and useful form the predicted quantities.

REMARKS: This routine is used in conjunction with subroutine TRJK or TRJKX, which computes all necessary constants used in TBPVS. TBPVS is used in trajectory fitting, error propagation, and simulation programs. NO. CO 406 FCF NO. CO 406 FCF TITLE: Compute Two-Body Partials and Vectors IDENTIFICATION: Subroutine TBPV CATEGORY: Trajectory CODE: Fortran 62, F63 CDC-1604 PROGRAMMEN: Fred C. Forbes, Jr. DATE: PURPOSE: USAGE: 1. Calling Sequence. CALL TBPV(TO,TM,VEC,P,NOTE). 2. Arguments: TO - Time of epoch or injection in seconds TM - Time of forward predicted data in seconds

TM - Time of forward predicted data in seconds VEC - Array of position and velocity components NOTE - Option indicator: 1 = Compute VEC only 2 = Compute VEC and P

P(18)- a 3x3 array:



3. Inputs: TO, TM, NOTE:

Outputs: VEST P

5 Routines Called: MTXT, MTXP

6. Linkage: CONMON/TRJKS/CU\$3), PI, WE, RO, PO(6), AI, AIS, AAIS, GAMO, BATO, ECC, EO, DBO(6), DAI(6), DGO(6)

METHOD:

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REMARKS:

PROJECT: Geodetic SECOR NO. CO405 TITLE: Computation of Trajectory Constants CATEGORY: Utility IDENTIFICATION: Subroutine THJK CODE: Fortran 62 CDC-1604 DATE: June, 1964 PROGRAMMER: Fred C. Forbes PURPOSE: To compute trajectory constants and/or two body partials given position and velocity vectors in equatorial coordinates. USAGE: Calling Sequence: CALL TRJK (RE, VE) I. 2. Arguments: RE(3), VE(3) - Position and velocity of a vehicle in free-fall expressed in equatorial coordinates CU(3) - Canonical units for length, velocity, and time PIE - P1 ₩Ē - Earth's rotational velocity (redians/sec) RO(3), VO(3) - RE, VE represented in inertial coordinates and in cenonical units EC. - Eccentricity of ellipse = e - Eccentric anomaly st initial time = E ΕO AAIS  $\frac{-1/a}{-1/a}$  1/2 AI AIS 🛫 e šin E GAMO BATO - • cos E 'n. DBO(6), BAI(6), DGO(6) - Two body partials Inputs: RE, VE 3. GU(3), PIE, WE, RO(3), VO(3), AI, AIS, AAIS, GAMO, BATO, EC, EO, DBO(6), DAI(6), DOO(6) Outputs: 4. Routines Called: QUTS 5. COMMON/TRJKS/CU(3), PIE, WE, ROM, RO(3), VO(3), AI, AIS, 6. Linkagei AAIS, GAMO, BATO, EC, EO, DBO(6), DAI(6), DGO(6)

### METHOD:

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REMARKS: Units are in feet and seconds.

T-86

NO. CC206 PROJECT: General TITLE: Invert Ortho 6x6 Matrix by Partitioning GATEGORY: Utility CODE: Fortran CDC-1604 PROGRAMMER: F.C. Forbes, Jr. PATE: January, 1964 PURPOSE: To invert an orthogonal 6x6 matrix.

USAGE:

1. Calling Sequence: CALL INSS (A,B)

2. Arguments:

A(6) - 6x6: input matrix B(6) - Inverse matrix-of A

3. Inputs: A

4. Outputs: B

5. Routines Called: MTXT, MTXI, MTXP; MTXS

6. Linkage:

METHOD:

### REMARKS:

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NQ. CÓ 417 FCF PROJECT: Geodetic SECOR TITLE: Adjust RO and VO to Position and Velocity CATEGORY: Trajectory IDENTIFICATION: Subroutine PVTRJF CODE: Fortran 52, F63 PROGRAMMER: Fred C. Forbes, Jr. DATE: PURPUSE:

USAGE:

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Calling Sequence: CALL PVTRJF(TO,RO,VO,NO,TM,TRJP,ITER,KP,LTI)
 Arguments:

TO - Time of epoch or injection in seconds

RO - Adjusted range injection vector

VO - Adjusted velocity injection vector

NO - Number of input position vectors to be fit by iterative least squares NO<200

ITER - Number of iterations

DTE - Time interval (seconds)

TRJP - Latitude, longitude and height above mean sea level of vehicle.

TM - Timë of forward predicted data in seconds

3. Inputs: TO: NO, ITER, DTI, TRJP, TH

4. Outputs: RO,VO

5. Routines Calaed: TRJK, TBWPT, TBPV, MTXT, MTXP, MTXA, INSS

METHOD:

### REMARKS :

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PROJECT: Bluerock
NO. TPOOL
TITLÈ: Compute Air Density at Attitude (FT)
                                             IDENTIFICATION: Subroutine ADEN
CATEGORY: Impact Prediction
CODE: Fortran 63
                   CDC-1604
PROGRAMMER: LoBrucePalmer
                                             DATE: June 1964
FURPOSE: To compute the air density at a given altitude.
USAGE:
     1. Calling Sequence: CALL ADEN(H,X)
2. Arguments:
                     H. = Height above sea level (FT)
                     X = Air density (1b/ft^3)
                   <u>،</u> ۱
                     CO = Table of four coefficients for six third degree
                          polynomials
         Inputs: H.CO
     3.
     4,
         Outputs: X
         Routines Called: None
     5.
         Linkage: COMMON/PERT/FMD(20,2),NO,FMASS,EA,CO(4,6)
     6.
```

METHOD: Evaluation of one of six predatermined third degree polynomial. curve fit todata, depending upon height.

T-89

**REMARKS:** 

4

NO. TP003PROJECT: BluerockTITLE: Sound Velocity at Altitude (FT)CATEGORY: Impact PredictionCODE: Fortran 62CDC = 1604PROGRAMMER: L. Bruce PalmerPURPOSE: To compute the velocity of sound at a given altitude.

USAGE:

1. Calling Sequence: CALL ACVEL (H,X)

2. Arguments:

H = Height above sea level (FT)

X = Acoustical velocity (Et/Sec)

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- 3. Inputs: H
- 4. Outputs: X
- 5. Routines Called: None
- S. Linkage: None

METHOD: Evaluation of predetermined curve fit to values.

REMARKS:

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PROJECT: Bluerock
    TP002
NŐ.
TITLE: Interpolate for Drag Coefficient
CATEGORY: Impact Prediction
                                           IDENTIFICATION: Subroutine DRAG.
CODE: Fortran 62
                   CDC-1604
                                           DATE: June 1964
PROGRAMMER: L.Bruce Palmer
PURPOSE: To determine the drag coefficient for a given mach speed.
USAGE:
         Calling Sequence: CALL DRAG(DCOEF ,FMACH)
     1.
     2.
        Arguments:
                     DCOEF - Drag coefficient
                     FMACH - Nach speed
                     FMD
                           - Table of drag coefficients vs. Mach speed
                     NO
                           - Number of coefficients in TMD
         Inputs: FMACH, FMD, NO
     3.
     4.
        Outputs: DCOEF
     5. Routines Called: None
         Linkage: COMMON/PERT/FMD(20,2),NO,FMASS,EA,CO(4,6)
     Ğ.
METHOD:
          Table look-up.
```

REMARKS:

3-91

NO. 416

# PROJECT: General

TITLE:Compute Precise Trajectories and Orbits from fit to Equatorial<br/>Coordinates and VelocityIDENTIFICATION: Program PVCMPTCATEGORY:TrajectoryCODE::Fortran \$2.7 CDC+1604PBOGRANNER:Fred C. Forbes, Jr.

PURPOSE: Compute precise trajectories and orbits with compensation for 2nd, 3rd and 4th zonal harmonics of the earth, stmospheric drag, and lift. Optional initial conditions of time, position and velocity vectors or two positions and apoge height are provided as well as provision for iterative least squares fit (with or without weighting) to the vehicle position coordinates. Equatorial coordinates are listed and topocentric coordinates are computed and listed with respect to any number of sites on the earth's surface. The final orbital parameters are adjusted to input equatorial coordinates and velocity.

USAGE: ( Inputs:	CARDS (1 ² ) (2)	DESCRIPTIONFORMATTitleA 80 HollerIOPTN,NO,ITER,KP,KWT,IDTI,IUNITS*513,15,13IOPTN = initial conditions option 001 - time with two positions					
		NO	and apoges height 002 - time with equatorial position and velocity ve = number of input position vector	ictors D <b>rs</b>			
			to be fit by iterative least squares NO 200	-			
		ITER	= number of iterations of the fi	it '			
- ,		ЌР	<pre>= perturbation option indicator     001 - drag and lift     002 - no drag and lift</pre>				
		KWT .	<pre>= least squares weighting option</pre>				
		IĎTľ	<pre>maximum interval between recti- fication in perturbation computation times 10</pre>				
Option 1	(3)	ŤI =	time of enoch	EL7. 10.			
Option 1	(4)	CO ,=	latitude, longitude, height of a	epoch 3(E17.10.3X)			
Option 1	(5)	CI =	latitude, longitude, height of s	second 3(E17,10,3X)			
Option 1	(6)	AL =	apogee height (AL is lochted between CO and CL).	E17.10			
Option 2	(3)	.T <b>I</b> , ŖΕ=	time and position vector at epoch where RE is the equatorial coordinates	1 :4E20+10			

*IUNITS = units code of input injection vectors(sec(33) for code ID).

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Option 2	(- 4)	VE =	equatorial velocity components	
KD-001 (		TWD -	at epoch	3 E20.10
Kr=001 j	//~(10)	tub -	drag coefficients	4(E17.10.3x)
KP=001 (	17)~(23	)	table of curve fitting	
	•		coefficients	4(17,10 <b>,3x</b> )
KP=001	(24)	NOT, FM	ASS, EA I20	,2(E17.10,3x
•		N <b>O</b> I =	number of coefficients	
		ÈMASS =	In table	
		EA #	vehicle cross séctional	
			area in ft ²	
	(25)	TM, TRJI	P = trajectory points for fitting	4 E20.10
-		TM =	fine in seconds	
+		IKJP =	XE, YE, ZE OF Which XE, YEO ZE	of vehicle
	(26)	Same as	25 until NO (see item 2) are	
		input		
KWT=CO1	(27.)	COSITE	= latitude, longitude, height of	4
			local origin for error propagatio	n 3(E17.10,3x)
KWT≑001	(28)	IEQU, S	ITE I3,X17	, 3(E17.10,3X)
	•	TEÓN E	equipment selection code	-
-	-		002 = height	
			003 = L direction cosine	
			004 = M direction cosine	
			005 = azimuth	
			-006 = elevation	
		;SI1L =	Latitude, longitude, and neight	
ີລະຫາະກວາ	(29,)	EM. ICO	NT = error model	5 E17.8.15
· · · · · · · · · · · · · · · · · · ·		EM(1)	=sequipment error	
	•	ĚM(2)	= tropospheric refraction	
-	•	EM(3)	= scale factor	
,		EM(4)	= site survey	
		្ចំភេ(១)	= longspheric rerrection for	
		EM(5)	r= baseline length for L and M	
		ICONT =	continuation code	
	-	ICONT	(0)= continue input of EM	
		ICONT	(1)= indicates last site input	-
KWT=001	(30)/,	(31) (Same	e as (28)) and (29.) for all trackin	g
	(32.)	TO DT	equipment TE = times for forward	3(E17.10.3x)
	· //	101 011	predictions	- (
		<b>T</b> O =	first time	
		DT =	time interval	
-	-	TF =	final time of prediction	-
	(33)	TRUNOU	((TF-TO) /DT <1000) per run)	~ <b>*</b> •
	(00)	TPUNCH	= pubch ontont soge	213
		1.00001 /	2000 # no punch output	
			001 = punch output	
		IUNITS	= output units code	
			001 = feet	
	-		UUZ = meters	
-			- UVU: * BLALULE MILES (5200') - AOH & BANHIARI MILES (5200')	<b>\</b>
			OOA - HERCYCET (HITES (DALOTTAS).	1
			ODD & ABLAD	_ T÷

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- (36) TITLE = mite name card
- (37) CS = latitude, longitude, height of points on earth to which trajectory points will be referred.
- A80 Hollerith

3(E17,10,3x)

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(38), (39) Same as (36) and (37) for all desired sites.

Output: From Fitting:

All input data are dumped for reference. On successive iterations, the adjusted injection vectors, as well as the difference between each predicted point and the corresponding input data are listed. The difference between the two-body prediction of position and valocity and the total field prediction values are listed. The error propagation (inverse weighting) in the XYZ coordinates are also disted when weighting is called out.

In Equatorial Coordinates:

Point number, hours, minutes, seconds, total seconds, XYZ, XYZ, latitude, longitude, height, and associated titles.

In Topocentric Coordinates:

Point number, hours, minutes, seconds, XYZ, XYZ, in local east-north-up coordinates, slant range, surface range, range rate, azimuth, elevation angle, and height AMSL with titles.

Method:

Trajectory predictions are computed (by a method based on computing a reference trajectory with closed form twobody equations and then adding numerically integrated perturbation terms.

In the least squares fitting, unity weighting or weighting based on the propagation of major sources of observational error into position variance and covariance, are optional. See program GENEPQ No. 617 FCE, for method of error propagation. * and velocity

Remarks:

All input is expressed in feet, seconds, degrees, and ratios. In the error propagation refraction is input as the ratio of the residual error to the total (mean atmosphere) correction: (i.e., 5% residual would be input as 0.05). Scale factor, baseline length, and site survey are ratios. An error in site survey of 1 PNM would be input as 0.000001.

If punch output is desired, the source-deck should be modified to give the desired output.

Reference should be made to the program listings for all necessary subroutines and memory usage.