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A STUDY OF THE ELASTIC PROPERTIES OF ORIENTED FIBERGLASS BY THE IMPULSE ACOUSTICAL METHOD

by

Ye. N. Kvasnikov, and A. I. Fotapov



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FOLLOWING ARE THE CORRESPONDING RUSSIAN AND ENGLISH
 DESIGNATIONS OF THE TRIGONOMETRIC FUNCTIONS

Russian	English
sin	sin
cos	cos
tg	tan
ctg	cot
sec	sec
csc	csc
sh	sinh
ch	cosh
th	tanh
cth	coth
sch	sech
csch	csch
arc sin	sin ⁻¹
arc cos	cos ⁻¹
arc tg	tan ⁻¹
arc ctg	cot ⁻¹
arc sec	sec ⁻¹
arc csc	csc ⁻¹
arc sh	sinh ⁻¹
arc ch	cosh ⁻¹
arc th	tanh ⁻¹
arc cth	coth ⁻¹
arc sch	sech ⁻¹
arc csch	csch ⁻¹
rot	curl
lg	log

U. S. BOARD ON GEOGRAPHIC NAMES TRANSLITERATION SYSTEM

Block	Italic	Transliteration	Block	Italic	Transliteration
A	A	A, a	P	P	R, r
B	B	B, b	C	C	S, s
V	V	V, v	T	T	T, t
G	G	G, g	Y	Y	U, u
D	D	D, d	X	X	F, f
E	E	Ye, ye; E, e*	K	K	Kh, kh
Ж	Ж	Zh, zh	T	T	Ts, ts
З	З	Z, z	Ч	Ч	Ch, ch
И	И	I, i	Ш	Ш	Sh, sh
Н	Н	N, n	Щ	Щ	Shch, shch
К	К	K, k	Ъ	Ъ	Y, y
Л	Л	L, l	Ы	Ы	Y, y
М	М	M, m	Ь	Ь	E, e
Н	Н	N, n	Ю	Ю	Yu, yu
О	О	O, o	Я	Я	Ya, ya
П	П	P, p			

* Ye initially, after vowels, and after ъ, Ъ, elsewhere.
 When written as ъ in Russian, transliterate as yѐ or ѐ.
 The use of diacritical marks is preferred, but such marks
 may be omitted when expediency dictates.

A STUDY OF THE ELASTIC PROPERTIES OF ORIENTED FIBERGLASS BY THE IMPULSE ACOUSTICAL METHOD

Ye. N. Kvasnikov, and A. I. Potapov

Some of the essential mechanical characteristics of fiberglass are the elastic modulus and Poisson's ratio. For determining the elastic characteristics of oriented fiberglass, we used the impulse acoustical method, since it permits revealing the influence of different technological factors and the mode of hardening for mechanical properties of the material.

Elastic properties of oriented fiberglass. Oriented fiberglass belongs to the group of orthogonally-anisotropic materials. Elastic deformations of fiberglass can be described with the aid of Hooke's generalized law. In general, the equations of Hooke's generalized law contain 21 elastic constants. However, inasmuch as constructions made of fiberglass such as pipes, plates, the hulls of ships, constructions used in wall and roof panels and others are subject to plane stress and have an orthotropic structure, then the equations of Hooke's generalized law will have four independent elastic constants in all.

With the aid of the impulse acoustical method, the physical constants of Hooke's generalized law are directly determined [1]:

$$\begin{aligned} \epsilon_{11} &= \nu_1^2 \rho, & (1) \\ \epsilon_{22} &= \nu_2^2 \rho, & (2) \\ \epsilon_{33} &= \nu_3^2 \rho = \nu_1^2 \nu_2^2 \rho. & (3) \end{aligned}$$

where ρ - density; ν_x and ν_y - speed of propagation of longitudinal waves in a plate along the axes of elastic symmetry x and y ; ν_{yx} and ν_{xy} - corresponding propagation speeds of shear waves.

By using formulas (1-3) and the expression of technical elastic constants through the physical [2, 3], the values of Young's modulus E and shear modulus can be obtained:

$$E_x = \rho (\nu_x^2 / \nu_y^2 - \nu_{yx}^2), \quad (4)$$

$$E_y = \rho (\nu_y^2 / \nu_x^2 - \nu_{xy}^2), \quad (5)$$

$$G_{xy} = \nu_{xy}^2 \rho. \quad (6)$$

where ν_{12} and ν_{21} - Poisson's ratio, subscripts x and y , as before, pertain to the direction of the axes of elastic symmetry, while C_{11} , C_{22} , C_{66} - physical elastic constants.

For determining the elastic characteristics in rods it is possible to use this expression:

$$\nu = \sqrt{\frac{E}{\rho}}. \quad (7)$$

where ν_ϕ - speed of elastic waves in the rod; E_ϕ - Young's modulus, and subscript ϕ indicates direction. This formula is accurate for directions, which coincide with the axes of elastic symmetry. In the first approximation dependence (7) can also be accepted for other directions.

By equating the values of elastic modulus obtained by the speed of propagation of waves in a plate (4) and (5), to the corresponding values calculated by the speed of propagation of waves in a rod (7), one can determine ν_{12} and ν_{21} :

$$v_{11} = \sqrt{\frac{E_1}{\rho_1}} \quad (8)$$

$$v_{22} = \sqrt{\frac{E_2}{\rho_2}} \quad (9)$$

where v_0 and v_{90} - speeds of longitudinal waves in a rod along axes x and y .

For determination of E_0 there is no need to cut rods in directions which differ from the basic, and it is possible to use the known formulas of the theory of elasticity of an anisotropic body [2, 3]. By applying the previously deduced expressions (7) and (8), we will obtain:

$$E_0 = \frac{\rho_0^2 (v_0^2/v_1^2 - v_2^2/v_0^2)}{\cos^2 \theta + \sin^2 \theta \frac{v_0^2}{v_1^2} + \frac{1}{2} \frac{v_0^2}{v_2^2}} \quad (10)$$

$$\lambda = \frac{E_0}{2(1+\mu)}, \quad \mu = \frac{v_0^2 (v_0^2/v_1^2 - v_2^2/v_0^2)}{2} - \frac{1+\mu}{2},$$

where

here v_{45} - speed of longitudinal waves in a rod, cut at an angle of 45° to the direction of the fibers.

Below, on the basis of experimental data, it will be shown that for determining the speed at any angle to the direction of fibers both in a plate and in a rod this formula is applicable:

$$v_0 = \frac{v_{45}^2}{\cos^2 \theta + \sin^2 \theta \frac{v_{45}^2}{v_1^2} + \frac{1}{2} \frac{v_{45}^2}{v_2^2}} \quad (11)$$

$$\lambda = \mu_0 \mu_{45}, \quad \mu_0 = \mu_{45} - (\mu + \mu_{45})$$

where

here v_0 , v_{45} , v_{90} - speed of propagation of elastic waves either in a rod or in a plate at angles of 0° , 45° and 90° to the direction of the fibers.

Formula (11) is empirical and was taken by analogy with the theoretical equation.

Experimental investigations. As the object of investigation the anisotropic fiberglass material SVAM was selected, the physical and mechanical properties of which have been sufficiently completely and widely discussed in literature [4]. For investigating the elastic characteristics by the impulse acoustical method [5, 6] SVAM material made by the Leningrad laminated plastics plant was used. The characteristics of these materials are given in Table 1.

Table 1. Characteristics of sheet fiberglass SVAM adhesive - epoxy-phenol resin.

Sheet number	Dimensions, mm	Density, g/cm ³	Content of fibers, %		
			fiberglass	resin	impregnating fibers
3-1	500x200x4.5	2.08	78	14	14
3-10	500x200x4.5	2.04	72	14	14
3-3	500x200x4.5	2.07	77	14	14

All fiberglass of the sheets were marked and sonicated in accordance with the layout shown in Fig. 1. As an emitter of ultrasonic waves the Polish ultrasonic instrument Betonoskop was used, as well as elastic wave converters on a frequency of 40 kHz. As a result of sonification the speed of propagation of elastic waves in a plate of fiberglass in the directions shown in Fig. 1 was determined; after that, from each sheet at angles of 0° , 15° , 30° , 45° , 60° , 75° and 90° to the direction of fibers from 4 to 5 samples each were cut. The length of the samples was from 200 to 400 mm, the width was 20 mm, and the thickness corresponded to the thickness of sheets shown in Table 1. All of the samples were sonified to determine the speed of elastic waves in the rods by the layout shown in Fig. 2. The values of speeds in the plate and in the rods were compared with the values of speeds calculated by formula (11).

Along with measurements of elastic properties, mechanical tests were conducted of material by the acoustical method for determining the value of elastic constants in accordance with All-Union State

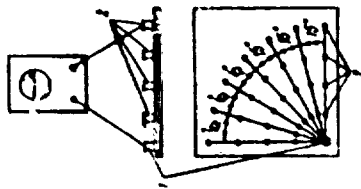


Fig. 1. Location diagram of the emitter (1) and the receivers (2) during surface sonification of a plate made of fiberglass.

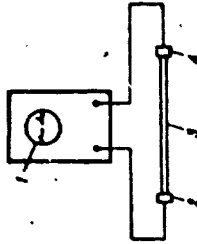


Fig. 2. Diagram of through sonification of fiberglass samples. 1 - ultrasonic instrument. 2 - emitter. 3 - sample. 4 - receiver.

Standard 9550-60. The very same samples were subjected to the mechanical tests on which the dynamic elastic characteristics were determined by the acoustical method.

As a result of the tests Young's moduli were determined in directions of 0°, 15°, 30°, 45°, 60°, 75° and 90° to the direction of fibers in the fiberglass. All measured and calculated data are given in Table 2.

These data show that the dynamic elastic characteristics noticeably differ from the static, where this difference is increased with a change of angle between the direction of sonification and the axis of elastic symmetry, reaching a maximum value for the direction with minimum elastic modulus. The dependence of the elastic modulus on the

Let us note that for the first two sheets, the axes of symmetry coincided with the directions 0°, 90° and 45°, and for the last one only with two - 0° and 90°.

Table 2. Results of determining the elastic characteristics of SVAM oriented fiberglass by the impulse acoustical method.

Direction of fibers	Type of sonification				Dynamic elastic modulus, kg/cm^2	Static elastic modulus, kg/cm^2	Conversion factor, μ
	(I) - in a plate	(II) - in a rod	(III) - in a rod	(IV) - in a rod			
0	4130	4130	4130	4130	3030	3120	0.79
15	4130	4130	4130	4130	3030	3120	0.79
30	4130	4130	4130	4130	3030	3120	0.79
45	4130	4130	4130	4130	3030	3120	0.79
60	4130	4130	4130	4130	3030	3120	0.79
75	4130	4130	4130	4130	3030	3120	0.79
90	4130	4130	4130	4130	3030	3120	0.79
0	4130	4130	4130	4130	3030	3120	0.79
15	4130	4130	4130	4130	3030	3120	0.79
30	4130	4130	4130	4130	3030	3120	0.79
45	4130	4130	4130	4130	3030	3120	0.79
60	4130	4130	4130	4130	3030	3120	0.79
75	4130	4130	4130	4130	3030	3120	0.79
90	4130	4130	4130	4130	3030	3120	0.79

Note. Values of constants were calculated by formulas (4), (5), (7), (8), (10) and (12) in this article.

rate of application contradicts its physical sense. This dependence is explained by the fact that in fiberglass, along with elastic deformations, highly elastic deformations are also developed. When testing by the impulse method, samples of fiberglass experience minute stresses at extraordinarily high rates of load application; therefore, the fiberglass does not "succeed" in manifesting nonelastic properties.

For converting from the elastic characteristics determined by the acoustical method to the characteristics obtained in the standard tests, it is possible to use conversion factors. Determination of these factors was made by comparing the dynamic elastic characteristics with the elastic characteristics defined by the All-Union State Standard. The results of this comparison are given in Table 2, where the conversion factors were obtained in the following way:

$$K_{\text{trans}} = \frac{E_{\text{trans}}/E_{\text{std}}}{K_{\text{std}}} = \frac{K_1}{\sqrt{1 + \frac{1}{2} \frac{K_2}{K_1} + \frac{1}{4} \frac{K_3}{K_1}}}, \quad (12)$$

$$\text{where } \lambda_1 = \frac{K_1}{K_2}, \quad \bar{\mu} = K_2/K_3 \sim (\lambda_1 + 1)/4.$$

In conclusion, it is possible to note that the impulse acoustical method permits reliably determining the elastic characteristics of fiberglass.

The investigations conducted showed that acoustical parameters and dynamic elastic constants of orthotropic fiberglass are described with sufficient accuracy by tensor formulas of the theory of elasticity of an anisotropic body. For converting from dynamic elastic characteristics to standard, conversion factors were obtained which consider the pressure of nonelastic deformations in a polymeric adhesive.

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