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FINAL SCIENTIFIC REPORT

RESEARCH ON ELEMENTARY PARTICLES

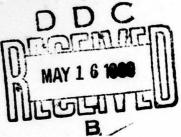
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Professor Abdus Salam and Professor P.T. Matthews.

Department of Physics,

Imperial College of Science & Technology,

LONDON - ENGLAND.



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ABSTRACT

The research described in this report extends over a broad range of topics in the theory of elementary particles and related fields, especially concerned with space-time and internal symmetries, current algebras and Regge-pole theory.

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- 1. Introduction.
- 2. Space-Time Symmetries.
- 3. Internal Symmetries and Current Algebras.
- 4. Regge-pole Theory and Finite-Energy Sum Rules.
- 5. Weak Interactions.
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- 7. Quantum Optics.
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1. JNTRODUCTION.

Our group has devoted its attention to a large number of research projects covering a wide variety of subjects within the general field of elementary particle theory. Among the most important of these have been studies of group-theoretical aspects of space-time and internal symmetries of elementary particles. Particularly significant results have been obtained in the theory of symmetries of scattering amplitudes at small momentum transfer, and in Regge-pole theory. Studies of various processes have been undertaken using the techniques of current algebras and finite-energy sum rules. Other fields in which significant advances have been made are quantum optics, astrophysics and axiomatic quantum field theory. These researches are summarized below and described in detail in the publications listed at the end of the report.

2. SPACE-TIME SYMMETRIES.

Scattering amplitudes can be decompsed in various ways, appropriate to different ranges of energy and momentum transfer. These decompositions include the partial-wave expansion, useful at low energies, and the expansion in terms of Regge poles, which is convenient at high energies and small momentum transfers. In the special case of zero momentum transfer, there is an extended symmetry which imposes constraints on the expansion parameters, and a corresponding special decomposition, related to limiting forms of the more general expansions. A comprehensive group-theoretic discussion of these decompositions has been given which is fully relativistically covariant and which clearly exhibits the relationships between the various special cases. This treatment also yields very convenient techniques for handling the practical problems involved in studies of many processes.

The relationships between helicity amplitudes and invariant amplitudes have also been studied extensively. A general discussion of this problem has been given, which in particular yields very simply the set of invariant amplitudes free of kinematic singularities for any given process. This method is well adapted to the determination of the constraints imposed by the symmetry at zero momentum transfer. It has been extended to cover not only massive particles but also particles of zero mass, such as the photon for which special problems associated with gauge invariance arise.

3. INTERNAL SYMMETRIES AND CURRENT ALGEBRAS.

A variety of mathematical problems involved in the study of internal symmetry groups, especially of the groups U(6,6) and SL(6,C) have been investigated. In particular, important results have been obtained in the representation theory of these groups, and of SO(n), SU(n) and $SU(n) \times SU(n)$.

The precise physical significance of the assumptions involved in internal symmetry theories, and the correct formulation of such theories has been another subject of several investigations. One of the most promising techniques is that of current algebras, in which the basic content of the theory is expressed in the assumption that the vector and axial vector currents of the theory form a representation of an appropriate algebra. The possibility of saturating the sum rules derived from current algebras by a small number of resonant states has been considered, and the results compared with experiment.

An alternative model which can also incorporate the internal symmetry in a rather different way is the absorption model. Here the basic assumption is that in peripheral scattering processes the coupling constants

which describe the coupling of the exchanged particle have the symmetry described by, for example, the group U(6,6). The insertion of these constraints into the absorption model yields powerful predictions which have been successfully compared with experiment for a variety of scattering processes.

4. REGGE-POLE THEORY AND FINITE-ENERGY SUM RULES.

The theory of Regge poles, already discussed above, has also been investigated in an approximation scheme based on the ladder approximation. This technique yields the possibility of computing the parameters of a Regge trajectory - the trajectory function and residue functions - in a self-consistent manner analogous to a bootstrap theory. The results obtained so far are extremely promising, and full computer calculations are now under way.

Regge-pole theory is also involved in another subject, the study of finite-energy sum rules. The use of the asymptotic behaviour derived from Regge-pole theory permits the derivation of sum rules which extend only to a finite upper limit of energy rather than to infinity, and which are therefore more amenable to direct comparison with experiment. The incorporation of internal symmetry into this scheme leads to interesting predictions which have been compared with experiment.

For certain amplitudes, Regge asymptotic behaviour requires so-called superconvergent sum rules, which are in effect restrictions imposed on scattering amplitudes by the assumptions of Regge theory. Here too the incorporation of U(6,6) symmetry has led to remarkable predictions. An extensive study of these relations has been made, especially for the nonet of 2⁺ mesons. The results are generally in good agreement with experiment, in those cases where the

experimental data are adequate to make a meaningful comparison.

5. WEAK INTERACTIONS.

Applications of current algebra to weak interactions have been studied, and calculations made of various processes, for comparison with experiment. A study has also been made of the $\Delta I = \frac{1}{2}$ rule in non-leptonic weak interactions. The experimental status of the rule has been examined and a theory proposed which fits the available data. A possible explanation of the violation of CP symmetry has also been proposed.

6. AXIOMATIC FIELD THEORY.

Several nonrelativistic model field theories which are soluble, or can be shown to have well-behaved solutions, have been studied. In particular a large class of model theories which exhibit spontaneous symmetry breaking have been investigated, using the rigorous mathematical techniques of axiomatic quantum field theory. Certain possible generalizations of the Heisenberg theory of the ferromagnet have been investigated, and it has been demonstrated that a ferromagnetic continuum is impossible.

Axiomatic studies of representations of current algebras have also been made, with very interesting results. One result of importance is a 'no-go theorem' which demonstrates the impossibility of constructing representations with certain properties which had commonly been assumed in the literature.

7. QUANTUM OPTICS.

Interactions with matter of intense electromagnetic fields such as those produced by a laser, have been studied. In particular, a quantum-mechanical calculation has been made of stimulated Raman scattering, a phenomenon of considerable recent experimental interest. An investigation

has also been made of certain molecular features which appear in the spectra of atoms trapped in inert gas matrices.

A related topic which has been the subject of lengthy studies is that of the infrared divergences of quantum electrodynamics. A formalism which uses generalized coherent states to describe the emitted infrared photons has been developed, which is capable of reproducing in a more physically satisfactory way the conventional results, and moreover which can be used in circumstances where the conventional theory is inadequate.

8. ASTROPHYSICS.

An interesting proposal has been made that in certain circumstances the velocity of sound in ultradense matter may exceed the velocity of light. This proposal would remove certain difficulties in the way of one of the theories of quasars. Some simple models which exhibit this behaviour have been developed, and its various implications investigated.

A study has also been made of the role of certain elementaryparticle interactions, beyond the scope those hitherto generally considered,
in astrophysical problems. Another important topic considered was crystalization
and torsional oscillations of superdense stars.

9. CONCLUSIONS.

In addition to the topics mentioned in the preceding sections, several other subjects have been investigated. Notable among these were a study of the Lovelace equation, using partial-wave analysis, a consideration of certain aspects of parastatistics, and several phenomenological studies of various reaction processes.

Our group has continued to make a very significant contribution to the advancement of our understanding of the basic laws of physics. Very considerable progress has been made, particularly by using the techniques of current algebra and Regge-pole theory. The symmetry properties of the elementary particles are beginning to take on a more established and secure appearance. Although we still lack a comprehensive theory, certain portions of the theory which must eventually emerge have become much clearer. Much work however remains for this and other groups.

The following papers have been published.

TCTP 66-26	Oct. 10th.	B.H. Kellett.	Nuovo Cim.
2017 00 20	occ. Idem	"A Limitation on the Use of Current Algebra Techniques for Meson Decays".	L1, 768, *67.
27	Oct. 13th.	R. Delbourgo, Abdus Salam, & J. Strathdee. "Stress Tensor & the 2 ⁺ Mesons"	ILA, 593,'67
ICTP 66- 1	Oct. 21st.	Helen S. Freedhoff. "Quantum Theory of Stimulated Raman Scattering".	Jour. Chem. Phys. 47, 2554, 167.
2	Dec. 5th.	G. Fraser & R. Roberts. "A Model for High Energy Single Pion Production"	Nucvo Cim. 47, 339, 167.
4	Dec. 13th.	H.F. Jones. "Threshold Conditions for Helicity Amplitudes".	Nuovo. Cim. L4, 814, '67.
5	Dec. 20th.	H.F. Jones & M.D. Scadron. "U(6,6) & Superconvergent Sum Rules for $\pi N \rightarrow \pi N$ Scattering".	Nuovo Cim. 68A, 546 '67.
6	Dec. 29th	G. Feldman, T. Fulton & P.T. Matthews. "The $ I\Delta = \frac{1}{2}$ Rule without Neutral Currents".	Nuovo Cim. 50, 349, '67.
ICTP 67- 7	Feb. 2nd.	J.H.R. Migneron & H.D.D. Watson. "The Absorption Model & U(6,6) for the Reactions pr	Phys. Rev. 1.66, 1654 *68.
8	Feb. 9th.	K. Barnes, E. Kazes, & J. Paton. "Properties of the Colinear-ised Algebra of Vector Densities in the Infinite Momentum Representation".	Nuovo Gim. 1.4, 935, 167.
9	Feb. 13th.	R.F. Streater & D.A. Dubin. "Nonexistence of the Ferro- magnetic Continuum".	Nuovo Cim. 50, 154, '67.
10	Mar. 2nd.	K. Moriarty & R. Migneron "Nucleon-Antinucleon Charge Exchange Scattering using U(6,6) & the Absorption Model".	Phys. Pev. Letts. 978, Vol.18,No.22, '67.

Mar. 14th.	R.J. Rivers. "The Meson Spectrum & Superconvergence Sum Rules for the J = 2++"	Phys. Rev. 161, 1687, '67.
Mar. 21st.	K.J. Barnes & E. Kazes. "Approximate Saturation of the Colinearized Algebra of Vector Densities in the Group Theoretic Limit".	Nuovo Cim. 51, 128, '67.
Apr. 4th.	Ruth M. Williams. "The Stability of Current Algebra Predictions of the Normalized Axial Coupling Constant".	Nuovo Cim. 52, 107, 67.
Apr. 10th	T.W.B. Kibble. "Coherent Soft Photon States & Infra-red Divergences. I. Classical Currents.	Jour.Math.Phys. 9, 315, '68.
Apr. 13th.	K.J. Birnes & E. Kazes. "An Inverse Mass Approximation to the Saturation of the Algebra of Vector Densities".	Nuovo Cim. 52, 903, '67.
Apr. 14th.	H.F. Jones & M.D. Scadron. "U(6,6) & Superconvergent Sum Rules for Meson-Baryon Scattering".	Nuovo Cim. 52, 107, '67.
Apr. 4th.	R.J. Rivers. "Superconvergence Relations for Axial-Vector Pseudo- scalar Meson Scattering.	Nuovo Cim. 51, 728, 67.
May 12th.	R.F. Streater. "Current Commutation Relations & Continuous Tensor Products".	Nuovo Cim. 53, 487, '68.
May 22nd.	R. Delbourgo, K. Koller & P. Mahanta. "On Transformations between Basic Vectors of Unitary SL(2,c) Representations.	Nuovo Cim. 52, 1254, ¹ 67.
May 30th.	M.D. Scadron. "Covariant Propagators & Vertex Functions for any Spin".	Phys. Rev. 165, 1640, '68.
June 5th.	R. Delbourgo, Abdus Salam & J. Strathdee. "Harmonic Analysis in Terms of the Homogeneous Lorentz Group".	Physics Letts. 25B, 230, '67.
	Mar. 21st. Apr. 4th. Apr. 10th Apr. 13th. Apr. 4th. May 12th. May 22nd.	"The Meson Spectrum & Superconvergence, Sum Rules for the J°C = 2+"" Mar. 21st. K.J. Barnes & E. Kazes. "Approximate Saturation of the Colinearized Algebra of Vector Densities in the Group Theoretic Limit". Apr. 4th. Ruth M. Williams. "The Stability of Current Algebra Predictions of the Normalized Axial Coupling Constant". Apr. 10th T.W.B. Kibble. "Coherent Soft Photon States & Infra-red Divergences. I. Classical Currents. Apr. 13th. K.J. Birnes & E. Kazes. "An Inverse Mass Approximation to the Saturation of the Algebra of Vector Densities". Apr. 14th. H.F. Jones & M.D. Scadron. "U(6,6) & Superconvergent Sum Rules for Meson-Baryon Scattering". Apr. 4th. R.J. Rivers. "Superconvergence Relations for Axial-Vector Pseudoscalar Meson Scattering. May 12th. R.F. Streater. "Current Commutation Relations & Continuous Tensor Products". May 22nd. R. Delbourgo, K. Koller & P. Mahanta. "On Transformations between Basic Vectors of Unitary SL(2,c) Representations. May 30th. M.D. Scadron. "Covariant Propagators & Vertex Functions for any Spin". June 5th. R. Delbourgo, Abdus Salam & J. Strathdee. "Harmonic Analysis in Terms of the Homogeneous Lorentz

ICTP 67-25	June 13th.	K. Koller. "Feynman Diagrams for Unitary Representations."	Nuovo Cim. 79, 95, '68.
28	July 6th.	H.F. Jones & M.D. Scadron. "Reggeization of Invariant Amplitudes".	Nuc. Physics. B4, 267, '68.
29	July 12th.	K.J. Barnes & Ruth M. Williams. "The TNN Coupling from Current Algebra."	Nuc. Phys. B4, 424, '67.
30	July 18th.	B.H. Kellett. "The General Scattering Process PV VV & Super- convergence".	Nuovo Cim. 53. 625, '68.
31	July 20th.	R.J. Rivers. "Non-forward Na Super- convergent Relations".	Phys. Rev. 166, 1841 '68.
34	Sept. 9th.	P.T. Matthews. "Group Theoretic Approach to Quantum Fields".	Boulder Lectures in Theor. Phys. (1967).
36	Oct. 10th.	D.A. Dubin. "Fock Space Formulation of the Heisenberg Ferromagnet".	Nuovo Cim. 53, 182, 68.
ICTP 67- 1	Nov. 6th.	R. Delbourgo, M.A. Rashid, Abdus Salam & J. Strathdee. "Reggeization of U(6) x U(6)".	Phys. Rev. 170, 1477, '68.
2	Nov. 17th.	G. Feldman & P.T. Matthews. "Covariant Angular Momentum Analysis & Analytic Continuation".	Phys. Rev. 168, 1587 '68.
3	Nov. 22nd.	T.J. Weare. "Hadron Decay Widths".	Nuov. Cim LVIA, 64, '68.
4	Dec. 8th.	R. Delbourgo. "Representation Functions for the Degenerate Baryon Series in U(6) x U(6)".	Jour.Math.Phys. 9, 1936, '68.
5	Dec. 20th.	M.A. Ruderman & S.A. Bludman. "Possibility of Sound Speed Exceeding Light Speed in Ultradense Matter".	Phys. Rev. 170, 1176, '68.
6	Jan. 1st.	R.J. Rivers. "Analyticity Constraints & Superconvergence Relations".	Phys. Rev. 170, 1473, '68.

ICTP 67- 7	Jan. lst.	H.F. Jones & M.D. Scadron. "Natural Zeros of Regge Residues".	Phys. Rev. 171, 1809, '68.
8	Jan. 11th.	I.T. Grodsky & R.F. Streater. "A No-Go Theorem".	Phys. Rev. Letts. 20, 131, 695, 68.
9	Jan. 11th.	J.R. Fox. "Finite Energy Sum Rules in Nucleon Compton Scattering".	Nuc. Phys. B5, 331, '68.
10.	Feb. 15.h.	H.F. Jones. "On Threshold Cusps in Regge Trajectories".	Nuov. Cim. Lv, 354, '68.
11	Feb. 16th.	M. Martinis. "Low Energy Theorem for Pions".	Nuov. Cim. 56A, 935, '68.
12	Mar. 1st.	I.G. Halliday & P.V. Landshoff. "Grand-Daughter Trajectory in the Ladder Approximation."	Nuov. Cim. 56A, 983, '68.
13	Mar. 4th.	M.D. Scadron & H.F. Jones. "Covariant M-functions for Any Spin".	Phys. Rev. 173, 1734, '68.
15	Mar. 19th.	M. Ruderman. "Causes of Sound Faster than Light in Classical Models of Ultradense Matter".	Phys. Rev. 172, 1286, '68.
16	Mar. 21st.	B.H. Kellett. "General Fermion-Fermion Scattering in the Covariant Formalism."	Nuov. Cim. 56A, 1003, '68.
19	Apr. 24th.	I.V. Prokhorov. "On the Connection between the T-Matrix at Zero Momenta & the Classical Lagrangian".	Nuov. Cim. 57A, 245, '68.
20	May 1st.	R.J. Rivers & L.M. Saunders. "Regge Cuts & Charge Exchange Polarisation".	Nuov. Cim. 58A, 385, '68.
22	May 21st.	M.A. Ruderman. "Crystalization & Torsional Oscillations of Superdense Stars".	Nature. 218, 1129, '68.
24	May 22nd.	R.J. Rivers. "Effective Trajectories in the Presence of Regge Cuts".	Nuov. Cim. 58A, 100, '68.

ICTP	67-27	June 25th.	J.L. Schonfelder. "Absorption Corrections for the Double Peripheral Model."	Nuov. Cim. 58A, 221, '68.
	28	June 28th.	D.G. Fincham, J.H.R. Migneron, K. Moriarty. "A Model for High Energy Inelastic Processes".	Nuov. Cim. 57A, 588, '68.
	29	July 8th.	K.J. Barnes. "Current Algebra & Form Factors".	Nuov. Cim. 58A, 595, '68.
	30	July 8th.	H.F. Jones. "Covariant O(4) Propagators & Toller Poles".	Nuov. Cim. 59A, 81, '68.

The following papers have been submitted for publication.

ICTP 67-18	Apr. 1st.	P. Mahanta "Nesons in the Higher-	Nuov.	Cim.
		Symmetry Reggeisation".	0.	
23	May 22nd.	R. Delbourgo, K. Koller, & Ruth M. Williams. "Degenerate Representation Functions for SO(v), SU(v) & SU(v) & their Analytical Reductions".	Jour.	Math.Phys.
25	June 5th.	C.J. Isham. "A Group Theoretic Approach to Chiral Transformations"	Nuov.	Cim.
31	July 15th.	H.D.D. Watson, R. Migneron, K. Moriarty & D. Fincham. "The U(6,6) Peripheral Absorption Model for Reduction Processes".	Nuov.	Cim.
32	July 15th.	R.J. Rivers. "A Regge Model for Double Charge Exchange Processes".	Nuov.	Cim.
34	Aug. 7th.	I.G. Halliday & L.M. Saunders. "The Unitarity Equation at High Energy".	Nuov.	Cim.
35	Aug. 30th.	M. Martinis. "Multiparticle Terms in the 2-Body Scattering Amplitude".	Nuov.	Cim.
36	Sept. 24th.	I.G. Halliday. "Self-Consistent Regge Singularities".	Nuov.	Cim.
ICTP 68- 1	Sept. 25th.	C.J. Isham & A.A. Patani. "Meson-Meson Scattering	Nuov.	Cim.
		Lengths from Chiral SU3 x SU3"		
2	Oct. 1st.	I.G. Halliday & L.M. Saunders. "Self-Consistent Regge	Nuov.	Cim.
	7	Singularities - II".		
3	Oct. 10th.	Louis A.P. Balazs. "An I=1 nn Dynamical Calculation using Finite-	Phys.	Letters.
		Energy Sum Rules & Unitarity".		

ICTP 6	8- 5	Nov.	6th.	C.J. Isham. "Matrix Structures & Chiral Symmetries".	, Nuov.	Cim.
	6	Nov.	18th.	R. Delbourgo, A. Salam & J. Strathdee "A Yang-Mills Gauge Theory of Supermultiplets".		ubov Present Volume.
	7	Nov.	21st.	J.D. Jenkins. "Daughters & Weinberg Field Theory".	Nuov.	Cim.
	8	Nov.	26th	R. Delbourgo & Abdus Salam. "Analysis of Charge Exchange Meson-Baryon Reactions from Reggeized Supermultiplet Theory".	Phys.	Letters

The research described in this report extends over a broad range of the theory of elementary particles and related fields, especially elementary elementary particles and related fields, especially elementary elementary

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