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HELIX-PLASMA' COUPLING' COLIN M. JONES

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HELIX - PLASMA COUPLING

Colin M. Jones

HELIX - PLASMA COUPLING

by

Colin M. Jones Lieutenant, United States Navy

Submitted in partial fulfillment of the requirements for the degree of

MASTER OF SCIENCE IN ENGINEERING ELECTRONICS

United States Naval Postgraduate School Monterey, California

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MASTER OF SCIENCE

IN

ENGINEERING ELECTRONICS

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United States Naval Postgraduate School

ABSTRACT

As efforts continue to effectively utilize the microwave frequencies a need is apparent for a traveling wave type device capable of handling greater power at higher frequencies. One possible solution is the plasma microwave amplifier tube.

This paper discusses an analysis of the plasma - helix coupling problem which may hopefully lead to development of such a device whereby the R. F. energy is coupled directly to the plasma with a helix, rather than coupling to an electron beam as has been the case heretofore. A theoretical analysis is presented, and the computer solution to the analytical equations evolved and the resulting $\omega - \beta$ plots are included.

This writer wishes to express his appreciation for the assistance and inspiration provided by Dr. Glen A. Gray of the U. S. Naval Postgraduate School in carrying out this investigation.

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1. Background.

The purpose of this investigation was to study the problem of coupling electromagnetic energy between a slow wave structure and a plasma column.

The underlying reason for interest in this problem is the design of a plasma microwave amplifier tube. A plasma microwave amplifier tube, where the plasma column acts as the slow wave structure, interacting with the electron beam, may well provide some advantages over present day types of traveling wave tubes. At the present time, conventional traveling wave tubes are limited in the power they can handle at high microwave frequencies. As frequency increases, it becomes difficult to construct a satisfactory slow wave structure which will dissipate any appreciable heat. Even at the lower microwave frequencies, heat dissipation in the slow wave structure may be a problem for high power applications. The plasma as a slow wave structure offers definite possibilities in that heat dissipation in the structure should no longer be a problem. There should be no inherent limitation insofar as mechanical dimensions are concerned, as the frequency is increased. Further, the plasma microwave amplifier device appears to offer promise of high gain and high power in a relatively small package.

The device proposed (Fig. (1)) is in many respects similar to a conventional traveling wave tube. The tube consists of a conventional



electron gun assembly, a d.c. heated filament consisting of a .001" tungsten ribbon approximately 1/2" X 3/4" at either end of the interaction region, and two helix slow wave structures in the interaction region.

The concept is to generate a plasma by heating the two filaments to 2300° C in a cesium gas environment at a very low pressure, on the order of 10^{-6} to 10^{-7} mm. Hg. These hot filaments will then cause contact ionization of the cesium gas thereby generating a plasma. R. F. energy is then coupled from the helix slow wave structure to the plasma, exciting the plasma. In turn, the electron beam on passing thru the plasma interacts with the wave excited on the plasma, giving a traveling wave type interaction.

A helix slow wave structure was chosen for several reasons. First, it is rather easily fabricated. Second, it has been used extensively in tube work, and experience is available regarding its characteristics. Finally, a theoretical analysis of the helix is available, Beck (1), and Hutter (2).

The cesium plasma was chosen for several reasons. First, the plasma frequency may be easily varied by control of the envelope temperature, and thereby the gas pressure. Second, it provides a relatively homogenous plasma, and may be quite highly ionized. Third, it provides a quiet plasma, that is, it is relatively free from spurious oscillations and noise. Finally, it may be readily ionized by contact

ionization. Since the ionization voltage of the cesium is below the work function of the heated tungsten filament, the filament will emit electrons and at the same time ionize the cesium gas, generating a plasma which is relatively homogenous. Knechtli and Wada (7) have done considerable work on this type of plasma generation. Kino (8) has also used a similar scheme. In his tube, Fig. (3), a spiral heater was used, and due to the fields set up across the spiral, it was necessary to make all measurements during the time when power was not applied to the heater. By use of a flat ribbon, it is hoped to be able to reduce the field of the heater sufficiently so that measurements may be taken continously while applying a d.c. voltage to the heater.

Work on plasma microwave amplifier tubes has been carried on by several authors, (8), (9), (12), (13), (14), and (15). The major difference between the operation of the tube proposed here and the work of some previous authors is in the manner of coupling the energy into the device. Boyd, Field, and Gould, (9) studied plasma oscillations and growing plasma waves using a mercury arc discharge for a plasma, coupling the input R. F. signal to the electron beam, and thence to the plasma. Fig. (2) is a sketch of the device they used. Allen and Kino (8) studied the interaction of an electron beam with a fully ionized plasma using a cesium plasma and coupling the input R. F. signal to the electron beam, and thence to the plasma. Fig. (3) is a sketch of the device they



F1g. (2)



F1g. (3)

used. Paik (12) used a coupled mode approach to study the coupling of modes between a slow wave mode and a helix. The experimental work he reported on was done with a device as shown in Fig. (4) which used a mercury plasma. He excited only one mode by careful coupling, using a selective mode coupler. This device did not include an electron beam, and his theoretical and experimental work was limited to the case of no magnetic field.

B.M. Bulgakov, et al. (13) studied slow waves in a helix - plasma column with an arbitrary magnetic field. This did not include any experimental work, and the final dispersion plots they developed showed discontinuities in the curves, which one would not expect to see. This has caused some workers in the field to question their results.

E. V. Bogdanov, et al. (14) studied very nearly the same problem as Boyd, Field, and Gould (9). The device they used for experimental work, although physically different, used an arc discharge type of plasma generator and coupled the input R. F. energy to an electron beam, and the output R. F. energy from the electron beam. The significant thing about this work is they were able to obtain gain from 25 cm. up to 3 cm. This was possible because they used an arc discharge to generate the plasma, and by increasing the arc current could generate a dense plasma, which was then contained by a magnetic field.

Work on an experimental X band tube has been carried out by



F18° (4)

Microwave Associates, Burlington, Massachusetts.¹ This is a mercury device, again coupling the signal via an electron beam. Elcon Laboratory, Cambridge, Massachusetts is working on a device using the fast wave, designed to utilize the negative conductance of the plasma. All other devices proposed to date have used the slow wave mechanism. General Electric Ltd., Wembly England, has reported¹ a plasma X band unit which develops 60 db of gain in a six cm. tube. Philips Research Laboratories, Eindhoven, Netherlands has reported¹ a helix coupled tube giving 19 db gain at four Gc.

In all of the preceding devices coupling of the input signal to the device was accomplished by coupling as in a conventional traveling wave tube, to an electron beam with a helix, and then using the wave propagated on the beam to couple to the plasma. As a result of this, in the experimental work performed to date it has not been possible to couple directly to a backward wave plasma mode. It is anticipated that with the experimental device proposed, Fig. (1), it will be possible to investigate backward wave modes by direct coupling, as shown in Fig. (5).

¹M. Meisels, Plasma Amplifiers Move Closer to Hardware Stage, Microwaves, pp 4-6, Jan. 1963



If energy is coupled into and out of the plasma in this fashion, then <u>if</u> interaction with the electron beam is observed, it must necessarily be interaction with a backward wave. Of course, care must be exercised to ascertain whether this interaction occurs in the helix or in the drift region.

In considering the specific problem of coupling electromagnetic energy to a plasma column, it is perhaps worthwhile to review the work done in studying propagation on an electron beam. Hahn (10) and Ramo (11) considered a drifting, ion-neutralized cylindrical electron beam in an infinite axial magnetic field and found that in general there are two space charge waves, the propagation equation being.

$$\omega_{\rm p}^{2} - (\omega - \beta u_{\rm o})^{2} = 0 \tag{1.1}$$

for the one dimensional case, where

$$\omega_{\rm p}^{\ 2} = -\eta \frac{\rho_{\rm o}}{\epsilon_{\rm o}} \tag{1.2}$$

$$\eta = \frac{e}{m}$$

and all quantities are assumed to have $e^{j(\omega t - \beta z)}$ dependence. Thus, the solutions are;

$$\beta = \frac{\omega \pm \omega_{\rm p}}{u_{\rm o}} \tag{1.3}$$

If u_0 is zero, this one dimensional ion-neutralized electron beam does not propagate space charge disturbances. Trivelpiece (6) has shown however, that a finite u_0 is not essential to the propagation of space charge disturbances when the beam has a finite transverse geometry.

Rigrod and Lewis (3) considered the problem of an electron beam under Brillouin flow conditions and found two types of space charge wave propagation, one involving a perturbation of the average charge density, and the other surface rippling. Brewer (4) considered the more general case of an arbitrary magnetic field.

2. Statement of the problem.

In order to study the coupling of R.F. energy between a helix slow wave structure and a plasma column, it is desirable to determine the $\omega - \beta$ plot or Brillouin diagram for the proposed circuit. This provides all the information required to forecast the performance in interaction with electron beams, except knowledge of the actual field amplitudes involved, ref. Beck (1).

The term plasma as used here denotes a partially ionized gas which is electrically neutral in any macroscopic volume in the absence of disturbances. Further, for this discussion it has been assumed the ions are stationary, and the electrons have no random velocities and suffer no collisions. The neutral gas molecules are assumed to play no part in the process studied. It is felt this is a reasonable model for the plasma. Fig. (6) shows the basic configuration of the problem. The helix slow wave structure has been appproximated by the sheath helix model.

3. Analytical Solution.

Trivelpiece (6), has solved the problem of a plasma filled cylindrical waveguide in an infinite axial magnetic field, starting with the basic Maxwell equations. He further considers the finite magnetic field case where he neglects the a.c. magnetic fields, (quasi-static approximation). He presents, for the finite magnetic field case, the development of a complex dielectric tensor, to take into account the effects of the plasma in a finite magnetic field. This is:



$$\underline{\boldsymbol{\epsilon}} = \boldsymbol{\epsilon}_{0} \begin{vmatrix} \boldsymbol{\epsilon}_{\mathrm{rr}} & j\boldsymbol{\epsilon}_{\mathrm{r}\theta} & \boldsymbol{0} \\ -j\boldsymbol{\epsilon}_{\theta\mathrm{r}} & \boldsymbol{\epsilon}_{\theta\theta} & \boldsymbol{0} \\ \boldsymbol{0} & \boldsymbol{0} & \boldsymbol{\epsilon}_{\mathrm{ZZ}} \end{vmatrix}$$
(3.1)

$$\epsilon_{\rm rr} = \epsilon_{\theta\theta} = 1 - \frac{\omega_{\rm p}^2}{\omega^2 - \omega_{\rm c}^2}$$
 (3.2)

$$\epsilon_{r\theta} = \epsilon_{\theta r} = \frac{(\omega_c) \omega_p^2}{(\omega) (\omega_c^2 - \omega^2)}$$
(3.3)

$$\epsilon_{ZZ} = 1 - \frac{\omega_{\rm p}^2}{\omega^2} \tag{3.4}$$

Making the quasi-static approximation, i.e. setting the a.c. magnetic fields to zero, we may solve the problem of matching between the helix and plasma column as follows:

$$\nabla \mathbf{x} \, \overline{\mathbf{E}} = -\mathbf{j} \, \boldsymbol{\omega} \overline{\mathbf{B}} = \mathbf{0} \tag{3.5}$$
$$\therefore \, \overline{\mathbf{E}} = -\nabla \, \boldsymbol{\phi}$$

This approximation is presumed good for $V^2 \mbox{ phase } < < c^2$

Now, for the equivalent dielectric,

$$\nabla \cdot \mathbf{\bar{D}} = \nabla \cdot (\underline{\boldsymbol{\epsilon}} \cdot \mathbf{\bar{E}}) = 0 \tag{3.6}$$

which suggests the differential equation

$$\nabla \cdot \underline{\epsilon} \circ \nabla \phi = 0 \tag{3.7}$$

The solution to which in cylindrical coordinates is:

$$\frac{1}{r} \frac{\partial}{\partial r} \left[r \epsilon_{rr} \frac{\partial \phi}{\partial r} + j \epsilon_{r\theta} \frac{1}{r} \frac{\partial \phi}{\partial \theta} \right]$$

$$+ \frac{1}{r} \frac{\partial}{\partial \theta} \left[-j \epsilon_{\theta r} \frac{\partial \phi}{\partial r} + \epsilon_{\theta \theta} \frac{1}{r} \frac{\partial \phi}{\partial \theta} \right]$$

$$+ \frac{\partial}{\partial_{z}} \left[\epsilon_{zz} \frac{\partial \phi}{\partial_{z}} \right] = 0$$

$$(3.8)$$

In general one may assume a solution of the form

$$\phi = R(r) e^{-jn\theta} e^{-j\beta z}$$
(3.9)

However, we shall restrict ourselves to the case of no variation in θ (i.e. n = 0). This is not essential, but will simplify the analysis. Also this is the case of greatest practical importance. This then leads to the partial differential equation

$$\frac{1}{r} \frac{\partial}{\partial r} \left(r \frac{\partial \phi}{\partial r} \right) + \frac{\epsilon_{ZZ}}{\epsilon_{rr}} \frac{\partial^2 \phi}{\partial_z^2} = 0 \qquad (3.10)$$

and solve

$$\frac{1}{r} \frac{d}{dr} \left(r \frac{dR}{dr} \right) - \beta^2 \frac{\epsilon_{ZZ}}{\epsilon_{rr}} R = 0$$
(3.11)

and now let

$$\Gamma = -\beta^{2} \frac{\epsilon_{ZZ}}{\epsilon_{rr}} = -\beta^{2} \frac{1 - (\omega_{p}^{2}/\omega^{2})}{1 - [\omega_{p}^{2}/(\omega^{2} - \omega_{c}^{2})]}$$
(3.12)

The solution to this equation, then is: 0 < r < b

$$\mathbf{E}_{z} = \mathbf{A}\mathbf{J}_{o}\left(\mathbf{\Gamma}\mathbf{r}\right)\mathbf{e}^{\mathbf{j}\left(\omega \,\epsilon \,-\,\beta_{z}\right)} \tag{3.13}$$

$$E_{r} = -A \frac{j\Gamma}{\beta} J_{1} (\Gamma r) e^{j(\omega t - \beta_{z})}$$

$$H\phi = -A \frac{j\Gamma\omega\epsilon}{\beta^{z}} J_{1} (\Gamma r) e^{j(\omega t - \beta_{z})}$$
(3.13)

and for $b \le r \le a$

$$E_{z} = \left[BI_{0}(\beta r) + CK_{0}(\beta r)\right] e^{j(\omega t - \beta} z)$$

$$Er = j \left[BI_{1}(\beta r) - CK_{1}(\beta r)\right] e^{j(\omega t - \beta} z)$$

$$H\phi = \frac{j \omega \epsilon}{\beta} \left[BI_{1}(\beta r) - CK_{1}(\beta r)\right] e^{j(\omega t - \beta} z)$$
(3.14)

and with suitable matching at the boundaries, we may reduce the above to:

$$\frac{\epsilon_{\rm rr}}{\beta \rm a} \frac{J_1(\Gamma \rm a)}{J_0(\Gamma \rm a)} = (3.15)$$

$$\frac{I_{1}(\beta a) [K_{0}(\beta b) + FK_{1}(\beta b)] + K_{1}(\beta a) [I_{0}(\beta b) - FI_{1}(\beta b)]}{-I_{0}(\beta a) [K_{0}(\beta b) + FK_{1}(\beta b)] + K_{0}(\beta a) [I_{0}(\beta b) - FI_{1}(\beta b)]}$$

where F is a function of the admittance Y_s of the sheath helix, defined as:

$$F = -\frac{j\omega\epsilon_0}{\beta Y_s}$$
(3.16)

 Y_s is the admittance of the helix. The expression for Y_s is given by Hutter (2) as:

$$Y_{s} = \frac{-j \omega \epsilon_{o}}{\beta} \frac{I_{o}(\beta a)}{I_{1}(\beta a)} + \frac{K_{o}(\beta a)}{K_{1}(\beta a)} - \frac{K_{1}(\beta a)}{K_{o}(\beta a)} (\frac{ka}{\beta a})^{2} \cot^{2} \psi$$

$$(\frac{ka}{\beta a})^{2} \cot^{2} \psi$$
(3.17)

using the sheath helix approximation. It should be noted that inherent in use of this expression for the admittance of the sheath helix is the further assumption of a free space TE mode within the helix. The use of a TE mode in addition to the TM mode is required to match the boundary conditions at the helix.

Paik, (12) has developed an analysis using the coupled mode approach for a helix-plasma column in the zero magnetic field case. The above general expression, equation (3.15) may be shown to reduce to that of Paik in the zero magnetic field case, (let ω_c go to zero).

Fig. 14 shows an $\omega - \beta$ plot for the zero and infinite magnetic field case, with the parameters defined as follows:

$$C_{1} = k_{p} \cot \psi$$

$$C_{2} = b/a$$

$$C_{3} = k_{c} a \cot \psi$$

$$x = pa$$

$$y = ka \cot \psi$$
where $k = \omega/C$

$$C = the velocity of light$$

The data was obtained by use of a digital computer. The general program and necessary function subroutines are given in appendix I.

Fig. (7) and Fig. (9) thru Fig. (17) show $\omega - \beta$ plots for various parameters in the general magnetic field case. Fig. (7) shows the principle modes, as well as a few of the higher order modes. These higher order modes result mathematically from the multiple roots of the Bessel functions, and represent higher order modes of operation. Since there are an infinite number of roots to the Bessel functions, there are an infinite set of these higher order modes in the regions where the propagation constant is real. A sample plot of this situation is shown in Fig. (8) for a typical case. The symbols used follow those of the computer program. Z is the right hand side of Eq. (3.15) and BB is the left hand side of this equation. This plot is for a fixed value of x. In the region where the propagation constant is imaginary, Z reduces to a function of two modified Bessel functions, usually represented as $I_n(x)$ which do not exhibit this multiplicity of roots, and therefore do not indicate higher order modes of operation in these regions.

4. Discussion.

The $\omega - \beta$ curves for the finite magnetic field case show several promising facets. The backward wave mode is an interesting phenomenon, and indicates the possibility of a backward wave oscillator.

Fig. (7) shows a detailed set of $\omega - \beta$ relationships for the case of $k_p^a \cot \psi = 3.0$, b/a = 0.8, and $k_c^a \cot \psi = 5.0$. Fig. (8) shows plots of the left hand and right hand sides of Eq. (3.15) vs ka $\cot \psi$ for pa = 4.0. The perturbations of the helix wave as shown in Fig. (7) indicate that considerable coupling exists between the helix and plasma for this finite magnetic field case. This is encouraging, and indicates that one might reasonably expect to couple the input and output energy directly to and from the plasma rather than coupling to the electron beam and thence to the plasma as has been done by previous workers, and this direct coupling to the plasma would thereby allow excitation of the backward waves as previously discussed.

The various modes of operation depicted in Fig. (7) are plasma modes, that is, they are not space harmonic modes of the helix, inasmuch as the sheath helix approximation does not include the space harmonics which exist with the actual helix. Therefore, in a solution which utilized a more exact representation for the helix one might expect to see in addition a coupling between the plasma and higher order helix modes. In the limiting case as the sheath helix goes over to a

conducting cylinder, these modes shown would be the various radial modes found by Trivelpiece, (6) and denoted as the p_{ov} modes where p_{ov} is the vth zero of the zero order Bessel Function of the first kind. From Fig. (8), we see that the solution at point a represents the perturbed helix wave, the solutions to the right of point a, the modes in the backward wave region, and those solutions to the left of a the modes in the forward wave region. For example the solution at point b represents the first plasma wave, and this point corresponds to the point b on Fig. (7). The solution at point e represents the first order solution of the backward wave region and corresponds to the point e on Fig. (7). The other points correspond as they are lettered. Thus we may see the mathematical generation of these higher order modes, and may visualize them as representing higher order radial modes. There are of course an infinite set of these modes, only a few of which have been shown.

The slight backward wave region of the perturbed helix mode indicates this device might have some promise as a backward wave oscillator. It is noted, however, that the bandwidth of any such device would be relatively narrow. The forward wave characteristics indicate that a forward wave amplifier might be designed to be quite broadband, however.

It should be noted that the higher order radial modes are probably

not particularly useful for interaction inasmuch as it would be difficult if not impossible to couple to them due to the reversal of field potential in the radial cross section which such a mode would represent.

Fig. (9) thru Fig. (16) show the effect of variations in $\omega_{\rm p}$ and $\omega_{\rm c}$ as well as the ratio of b/a. These curves are included to provide some insight into the effects of a variation of these parameters. First it is to be noted that for $\omega_{\rm p} < \omega_{\rm c}$ the lowest order plasma wave cuts off at $\omega_{\rm p}$, and for $\omega_{\rm c} < \omega_{\rm p}$ the plasma wave appears to cut off somewhere between $\omega_{\rm p}$ and $\omega_{\rm c}$. The backward waves and helix wave approach as a limit $\omega_{\rm c}$ when $\omega_{\rm c} > \omega_{\rm p}$, and approach as a limit $\omega_{\rm p}$ when $\omega_{\rm p} > \omega_{\rm c}$. Further, the backward waves cut off at the $\sqrt{\omega_{\rm p}^2 + \omega_{\rm c}^2}$. The above observations are similar to those found by Trivelpiece (6) in the plasma - cylinder problem. The larger b/a, the more completely the plasma fills the helix. It is seen that this leads to more bandwidth in the backward wave region. Also, the knee of the curve is less sharp as the helix wave goes over into a backward wave mode. This one might expect since a larger b/a would lead one to expect tighter coupling between the helix and the plasma.

Fig. (17) shows a plot of the helix and plasma waves for the zero and infinite magnetic field case. The infinite magnetic field case shows a continuation of the effects noted previously. There appears to be a smooth transition to the zero magnetic field case as well. As ω_{c}

is decreased, the backward wave region, essentially between ω_p and $\sqrt{\omega_p^2 + \omega_c^2}$ becomes smaller and smaller, until in the limiting case there is no such region. The helix wave becomes more and more nearly like the uncoupled helix wave as ω_c is decreased, and finally for $\omega_c^{=0}$ we see that the helix wave shows no backward wave region, and is only slightly perturbed by the plasma as may be seen by comparison with the free helix wave also plotted on the same figure. The plasma wave, which at values of $\omega_c > \omega_p$ appears to cut off at ω_p , cuts off at lower and lower frequencies as ω_c is decreased below ω_p and finally approaches the limit as shown for the zero magnetic field or $\omega_c = 0$ case.























5. Conclusions.

In conclusion it appears from the results of the analysis presented here that a plasma microwave amplifier device in which the R. F. Energy is coupled to the plasma directly offers some real possibilities of success. It appears that such a device would have several advantages over conventional type traveling wave devices. Principally these are that one might reasonable expect high power operation in a small device, and that one might be able to alleviate the serious mechanical and cooling problems inherent in higher frequency microwave devices of the type presently in use.

However, it should be emphasized that the analysis presented contains three basic approximations which limit the validity of the theory. First, the quasi - static approximation is made, which should be good for the low values of beam voltage used in typical tubes. Second, the sheath helix model is used, which is believed to be a reasonable model within the limitations previously mentioned. Finally, the assumption of a free space TE mode within the helix is made. This assumption would appear to be justified since the solution obtained in the case of zero magnetic field agrees with Paik's analysis (12) which does not make this assumption.

The dispersion relationships of Fig. (9) thru Fig. (16) do not show any anomalous discontinuities as were found by B. M Bulgakov et al.

(13).

The data contained in this paper is not sufficient in itself to draw firm conclusions regarding the operation of a plasma microwave amplifier device, however. The ω - β diagram does not provide any information regarding the magnitudes of fields involved, and thus no insight into the interaction impedances involved. A theoretical study of interaction impedance should be an interesting and worthwhile project and is suggested as the subject for some future investigation.

6. Proposed Experimental Work.

After completing all connections for the experimental tube, it is proposed that the following experimental work be accomplished:

Make cold tests of impedance match to the helix, and determine the losses incurred in the helix couplers over a frequency range of at least 1.0 to 2.5 Gc.

2. Determine the ω - β relationships as indicated from the theoretical work.

4. Carry out electron beam interaction experiments.

5. Investigate the backward wave regions shown theoretically, this being of special interest. These experiments should be designed to determine the range and magnitude of self oscillation available as well as bandwidth optimization by variation of field strength and

plasma density.

In the experiments involving measurements of the R. F. interaction, measurements should also be made to determine the impedance levels, gain, or loss in the helix regions, and gain or loss in the drift region. Further, these experiments should be carried on over a wide range of magnetic fields, tube temperatures, and frequencies.

Care should be exercised to assure the cooling provided by the water jacket is adequate to maintain an effective temperature along the region so cooled. Fig. (18) shows a photograph of the laboratory equipment designed to work with the proposed tube. The magnet, tube, and heat sinks for the filament rectifiers are water cooled. Fig. (19) shows a block diagram of the proposed measurement setup.

The magnet is designed to provide an adjustable uniform field from 0 to 2000 gauss. The plasma generation filament supplies are designed to provide from two to six volts, and up to a maximum of 120 amps each. The rectifiers are rated at 250 amps., the transformer being the limiting element.





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JONES GRAPH ON PROGRAM JONES3 • • JOB 8 7 PRINT 1 FORMAT (12H TUBE DESIGN) FORMAT (18H IMAGINARY GAMMA FORMAT (2X,6(2X,E15.8)) FORMAT (2X,6(2X,E15.8)) FORMAT (18H X,Y,HZ,HZY,F,HBB FORMAT (5X,3(5X,E15.8)) PRINT 17 DIMENSION X1(200) X1(200) 111 16557)) DIMENSION X1(900),Y1(903) DIMENSION T(1000) Y= KACO+ PSI CCCCCC X= PA CON1 =KPACOT(PS1) CON1 =KPACUT(PST) CON2=B/A F= -J(OMEGA) (EPSOION ZERO)/P(YS) CON3=5.0 CON2=0.8 CON1=3.0 PRINT 7,CON1,CON2,CON3 II=50 LL=200 CONTINUE DO 40 M=LL,1500C,II 43 L=M KA=-1 DO 50 K=5,375,1 X=FLOATF(K)/25.0 353 N=L N=L AA=CON2*X AO=BESI(0.0,X) A1=BESI(1.0,X) CALL PESS(0,X,2,B0,T) CALL BESS(1,X,2,B1,T) CO=BESI(0.0,AA) C1=BESI(1.0,AA) CALL PESS(0,AA,2,D0,T) CALL PESS(1,AA,2,D1,T) D0 60 J=N, 15000, 1 Y=FL0ATF(J)/2000.0 L=J 4 L=J L=J A=.0000001 IF(SENSE SWITCH 2) 102,103 Y=2.*Y1(KK-1)-Y1(KK-2)-4 AB=Y/X Q=(CON1/Y) RA=Y**2.0 RB=CON3**2.0 PC=PA-PB 102 RC=RA-RB RC=RA-RB RD=(CON1)**2.0/RC-1.0 RR=1.0-(CON1)**2.0/RC GAP'= ABSF((((Q)**2.0)-1.0)/RD)**0.5 GAB = CON2*X* GAP XNUM1 = (AB)** 2.0 XNUM1 = (AB)** 2.0 51 GAB = CON2*X* GAP XNUM1 = (AB)** 2.0 DEN1=AO/A1 +BO/B1 - (B1/BO)*XNUM1 F = XNUM1/DEN1 IF (SENSE SWITCH 1) 101,120 IF(Q-1.0) 12,13,13 IF(RD) 10,11,11 IF (RD) 10,11,11 IF (RD) 11,99,10 PRINT 2 FORMAT (16H GAMMA INFINITE) CALL BES(1:GAB:0:BES.11.1) 120 12 13 99 2 11 FORMAT (16H GAMMA INFINITE CALL BES(1,GAB,O,BESJ1,T) CALL BES(0,GAB,O,BESJ0,T) E1=BESJ1 E0=BESJ0 BB=RR*GAP*E1/E0 CC=C1*(B0+F*(B1)) DD= D1* (A0- F*(A1)) 91

EE = -CO*(BO+F*(B1)) FF = DO*(AO-F*(A1)) XNUM2 = CC+DD DEN2 = EE +FF Z = XNUM2 / DEN2 ZY = Z / BB ALFA = AB SF(ZY = 1.) EPS = 0.1 I = (ALEA - EPS) = 20.2IF (ALFA-EPS) 20,20,59PRINT 5, X, Y, Z, ZY, F, BB G0 TO 95 HAP = -GAP 20 10 HAP = -GAP F0 = RESI(0.C,GAB) F1= BESI(1.C,GAB) HCC=C1*(RO+F*(B1)) HDD= D1*(AO-F*(A1)) UEE = -CO*(RO+F*(B1)) 93 HEE = -CO*(BO+F*(B1))HFF= DO*(AO-F*(A1))HEB=RR*HAP*F1/FC DHN=HEE+HFF HNM=HCC+HDD HZ=HNM/DHN HZ=HNM/DHN HZY=HZ/HBB HLFA= ABSF (HZY-1.0) EPS=0.1 IF(HLFA-EPS)21,21,59 IF(SENSE SWITCH 2) 105,60 IF(SENSE SWITCH 3)106,107 A=A+.000005 GO TO 102 A=A-.000005 59 105 106 A=A-.000005 GO TO 102 107 CONTINUE PRINT 15,X,Y,HZ,HZY,F,HBB PRINT 16 210 95 KK = K - 4X1(KK)=X Y1(KK)=Y NUMPTS=KK CONTINUE 50 PRINT 5, X, Y, Z, ZY, F, BB PRINT 5, HZ, HZY, F, HBE, Q, RD CALL GRAPH (NUMPTS, X1, Y1, 8) IF(SENSE SWITCH 3) 128,41 101 II = 100128 II=100 LL=M+II GO TO 43 CONTINUE CONTINUE STOP END SUBROUTINE BESS (NO, X, KODE, RESULT, T) DIMENSION T(1000) PI=3.1415926536 IF (KODE) 41,1,2 CALL BES (NO, X, 0, RESULT, T) RETURN 41 4Ô 1 RETURN 23 IF (KODE-1) 41,3,4 CALL BES (NO,X,1,RESULT,T) RETURN IF (KODE-2) 41,5,6 IF(NO-1) 11,11,12 PRINT 13 452 FORMAT (34H1ORDER ERROR FOR K AND Y FUNCTIONS) 14 STOP 14 IF(X-1.) 15,15,16 T(1)=1./X DO 240 I=2,12 T(I)=T(I-1)*T(1) ii 16 240

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IF(N0) 21,2C,21

XGO=1.2533141375-.1566641816*T(1)+.6881112782*T(2)-.0913909546*

IT(3)+.1344596229*T(4)-.2299850328*T(5)+.3792409730*T(6)

2-.5247277331*T(7)+.557566367*T(8)-.4262632912*T(9)

3+.2184518096*T(10)-.0669097672*T(11)+.0091893330*T(12)

RESULT = EXPF(-1.*X)/SQ3TF(X)*XG0

RETURN

IF(NC-1) 12,22,12

XG1= 1.2533141373 +.4699927013*T(1)-.1468582957*T(2)

1+.1280426636*T(3)-.1736431637*T(4)+.2847618149*T(5)

2-.4594342117*T(6)+.62833806811*T(7)-.66820954*T(8)

3+.5050238576*T(9)-.2581303765*T(10)+.0788000118*T(11)

4-.0108241775*T(12)

RESULT = EXPF(-1.*X)/SQ3TF(X)*XG1

RETURN

CALL PES (1,X,1,XI1,T)

X10=T(1)

T(2)=X*X/4.

D0 310 I=4,12,2

J(1)=T(1-2)*T(2)

SUM = -.57721566 +.42278420*T(2) +.23069756*T(4)

1 +.03488590*T(6)+.00262698*T(8) +.00010750*T(10)

2 +.0000740*T(12)

ANSK0 = SUM - LCGF(X/2.) * X10

IF(N0) 31,30,31

RESULT = ANSK0

RETURN

IF(NC-1) 12,32,12

RESULT = ANSK0

RETURN

IF(NC-1) 12,32,12

XESULT = ANSK0

RETURN

IF(NC-1) 12,32,12

XESULT = COMPACE

XESULT = COMPACE

XESULT = ANSK0

RETURN

IF(NC-1) 12,32,12

XESULT = ANSK0

RETURN

IF(NC-1) 12,32,12

XESULT = COMPACE

XESULT = ANSK0

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IF(NC-1) 12,32,12

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XESULT = ANSK0

XESULT = COMPACE

XESULT = ANSK0

XESULT = COMPACE

XESULT = ANSK0

XESULT = ANS
        20
        21
         15
310
         30
                                  IF(NC-1) 12,32,12
RESULT = (1./X -ANSKO*XI1)/XIO
         31
32
                                IF (KODE-3) 41,40,41
PRINT 42
FORMAT (11H1KODE E
STOP 43
                                  RETURN
IF (KO
                  6
         4230
                                                                                                                           (11H1KODE ERROR)
                               STOP 43
IF (NO-1) 50,50,12
T(1)=X/3.
DD 400 I=2,12
T(I)=T(I-1)*T(1)
IF (3.-X) 52,51,51
SUMY = .36746691 + .60559366 * T(2) - .74350384 * T(4)
+.253C0117*T(6)- .04261214 * T(8) + .00427916 * T(10)
-.00024846*T(12)
CALL RES(1,X,0,XJ1,T)
XJ0=T(1)
Y0=2./PI*LOGF(X/2.)*XJ0+SUMY
IF (NO) 53,54,53
RESULT =Y0,
RETURN
IF(NO -1) 12,55,12
         50
 400
     51
1
2
         54
                          RETURN

IF(NO -1) 12,55,12

RESULT=(XJ1*YC-2./(PI*X))/XJO

RETURN

IF(4.-X) 59,60,60

T(1)=X/3.

DO 402 I=2,12

T(1)=T(I-1)*T(1)

SUMF0 =.79788456 -.00000077 *3./X

1 -.00009512/T(3)+.00137237 /T(4)

2 +.00014476/T(6)

SUMS =.78539816 +.04166397 *3./X

1 -.00262573/T(3)+.00054125 /T(4)

2 -.00013558/T(6)

YO = SUMF0/ SQRTF(X) * SINF(X-SUMS)

IF(ND) 71,70,71

RESULT =Y0
         53
55
         52
         60
 402
                                                                                                                                                                                                                                                                                                                                                                                              -.00552740/T(2)
-.00072805/ T(5)
                                                                                                                                                                                                                                                                                                                                                                                              +.00003954/ T(2)
+.00029333/ T(5)
         TO RESULT =YO
RETURN
                                  IF (NO-1) 12,555,12
CALL_BES(1,X,0,XJ1,T)
555
                                 XJO=T(1)
GO TO 55
T(1)=4./X
         59
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44
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401 73	DO 401 I=2,12 T(I)=T(I-1)*T(1) IF (NO) 12,73,72 PO = .39894227930017530620 *T(2) +.0001734300 *T(4) 0000487613*T(6)+.2000173565 *T(8)0000037043 *T(10)
1	Q0 =0124669441 +.0004564324*T(2)0000869791 * T(4) +.0000342468*T(6)0000142078*T(8) +.0000032312 * T(10) Y0 = 2./SQRTF(X)*(P0*SINF(X-PI/4.)+4./X*Q0*COSF(X-PI/4.)) RESULT=Y0 RETURN
74	$ \begin{array}{rcl} \text{IF} & (\text{NU-1}) & 12,74,12 \\ \text{P1} & & & & & & & & & & & & & & & & & & &$
	RESULT=Y1 RETURN END SUBROUTINE_BES(NO,X,KODE,RESULT,T) DIMENSION_T(100)
1009	KLAM=1 KO=NO+1 IF(X) 81,101,82 ERR=.CO1 IF (X+ERR)108,101,101
32 101 102	IF(X-ERR)101,101,108 IF(ND)103,102,105 T(KD)=1.0 RESULT = 1.0 RETURN
103 104 105	RESULT=9.999999999200 RETURN RESULT=0.0 RETURN
06 07 1071 08 081	PRINT 107 FORMAT(55HINEGATIVE ORDER NOT ACCEPTED IN BESSEL FUNCTION ROUTINE) STOP 1071 IF(ND)106,1081,1081 IF(KDDE)11,12,11
12	KLAM=KLAM+1 JO=2*XABSF(XFIXF(X)) MO=NO TIF(MO-JO)2,21,21 MO=JO
21	MO=MO+11 T(MO)=0. LUB=MC-1 T(LUB)=1.0E-300 GO_TO (23,51),KLAM
231	F=2*LUB ENA(-3)RAD(MO) LIL2(MO),ENA(T). INA(1)SAU(233P) INA(1)SAU(233A)
232 233A 233B	INA(I) SAL(233A) LDA(F) FSB(2.) STA(F) FDV(X) FMU2(N) FSB2(N) STA2(N) I JP2(232)
39 +	SUM=1(1) GD TD (39,69),KLAM M3=M0+3 DD 4 J=3,M3,2 SUM=SUM+2.*T(J)
5	P=1./SUM DO 5 J=1.KO T(J)=T(J)*F RESULT=T(KO)

51	RETURN KON=7777777776777778	
69.	GO TO 23 LAC(KON), RAD(233A)	
7	M3=M0+3 D0 7 J=2, M3 SUM=SUM+2 =T(1)	
	F=1./SUM*EXPF(X) DO 8 J=1.KO	
8	T(J)=T(J)*F RESULT=T(KO) END	
	SUBROUTINE RGAM (X,Z) DIMENSION B(13)	
	B(1) =422784335092 B(2) =233093736365 B(3) = .191091101162	
	B(4) =02455249087 B(5) =017645242118	
	B(7) =000804541335 B(8) =000360951491	
	B(9) = .000145624324 B(10) =000017527917	
	$B(12) =000001328554 \\B(13) =000000181220$	
301	Z = B(13) I = 12 Z = Z*X + B(I)	х.
501	I = I - 1 IF (I+1) 302,302,301	
302	Z = (Z+1.) * X * (X+1.) END	
202	SUBROUTINE RCPGAMR((X, Z) IF ($X-1$.) 208,202,203	
202	ŘETURN Y = 1.	
205	X = X - 1. Y = Y * X IE(X - 1) = 206 = 204 = 205	
204	Z = 1./Y RETURN	
206	Z = Z/Y RETURN	
208	INT = X Q = INT	
209	Z = 0.0 RETURN	
211 213	IF (X+1.) 212,209,213 CALL RGAM(X,Z)	
212 216	Y = X $X = X + 1.$	
214	IF $(X+1.)$ 214,209,215 Y = Y*X GD TD 216	
215	ČÁLL RGAM(X,Z) Z = Y*Z	
	FUNCTION BESI(FN,Z) IF(Z) 4,5,5	
4	PRINT 6 FORMAT(42H BESI NOT PROGRAMMED FOR NEGATIVE PRINT 7	ARGUMENT

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FORMAT(45H BESI COMPUTED FOR ABSOLUTE VALUE OF ARGUMENT Z=ABSF(Z) IF(MCDF(FN,1.)) 8,9,8 FN=ABSF(FN) 7 5 **9** 8 FN=ABSF(FN) FK=1. FN1=FN+1. FN2=FN+2. CALL RCPGAMR(FN1,ZA) CALL RCPGAMR(FN1,ZA) AI=(Z/2.)**2*ZB A=ZA+AI FK=ZA+AI FK=FK+1. AI=AI*(Z/2.)**2/((FK+FN)*FK) FN2=FN2+1. 3 A = A + A IIF(ABSF(AI)-ABSF(A)*10.**(-14)) 2,3,3 BESI=(Z/2.)**FN*A END 2 FUNCTION BESK(FN,Z) FN=ABSF(FN) IF(MODF(FN,1.)) 13,12,13 FA=-FN BESK=1.570796327*(BESI(FA,Z)-BESI(FN;Z))/(SINF(3.141592654*FN)) 13 RETURN 12. N = FNA=(-1.)**(N+1)*BESI(FN,Z)*LDGF(1.781072418*Z/2.) HZ=Z/2. BIBA=1. BIA=0.B1B=0. . IF(N) 100,100,101 B=0. GO TO 105 KK 100 Ğ0 D0 102 KK=1,N 101 FKK=KK BIBA=BIBA/FKK 102 BIB=BIB+1./FKK BI = BIBAB=BIBA*BIB FK=1. FNK=FN+FK BIA=BIA+1./FK BIB=BIB+1./FNK BI=BI*HZ**2/(FK*FNK) 103 FK=FK+1. TEST=BI*(BIA+BIB) B=B+TEST IF(ABSF(TEST)-ABSF(B)*10.**(-14)) 104,103,103 B=(-HZ)**N*B IF(N-1) 200,201,202 C-0 104 C=0. GO TO 300 C=1. GO TO 204 200 201 NA=N-1202 NN = 1DO 203 J=1,NA 203 NN=NN*J C = NNČB=C KD=1 205 FKD=KD CB=(-1.)**KD*CB*HZ**2/((FN-FKD)*FKD) KD=KD+1 C=C+CB IF(KD-N) 205,204,205 C=C*HZ**(-N) BESK=A+(B+C)/2. 204 END END

0202	OMEGA COLIN	BETA PLOT, C1=3., C2=0.5 C3=2.0 M. JONES	10	9	2
00000	OMEGA Colin	BETA PLOT, C1#3., C2=0.5 C3=2.0 M. JONES	10	9	2
0202	OMEGA COLIN	BETA PLOT, C1=3., C2=0.5 C3=2.0 M. JONES	10	9	2
02002	OMEGA COLIN	BETA PLOT, C1=3., C2=0.5 C3=2.0 M. JONES	10	9	2
0202	OMEGA Colin	BETA PLOT, C1=3., C2=0.5 C3=2.0 M. JONES	10	9	2
022	OMEGA COLIN	BETA PLOT, C1=3., C2=0.5 C3=2.0 M. JONES	10	9	2
002002	OMEGA COLIN	BETA PLOT, C1=3., C2=0.5 C3=2.0 M. JONES	10	9	2
02002	OMEGA COLIN	BETA PLOT, C1=3., C2=0.5 C3=2.0 M. JONES	10	9	2
0202	OMEGA COLIN	BETA PLOT, C1=3., C2=0.5 C3=2.0 M. JONES	10	9	2
0202	OMEGA COLIN	BETA PLOT, C1=3., C2=0.5 C3=2.0 M. JONES	10	9	2
002002	OMEGA Colin	BETA PLOT, C1=3., C2=0.5 C3=2.0 M. JONES	10	9	2
00202	OMEGA COLIN	BETA PLOT, C1=3., C2=0.5 C3=2.0 M. JONES	10	9	2
00202	OMEGA COLIN	BETA PLOT, C1=3., C2=0.5 C3=2.0 M. JONES	10	9	2
00202	OMEGA COLIN	BETA PLOT, C1=3., C2=0.5 C3=2.0 M. JONES	10	9	2
00202	OMEGA COLIN	BETA PLOT, C1=3., C2=0.5 C3=2.0 M. JONES	10	9	2
0202	OMEGA COLIN	BETA PLOT, C1=3., C2=0.5 C3=2.0 M. JONES	,10	9	2
0202	OMEGA COLIN	BETA PLOT, C1=3., C2=0.5 C3=2.0 M. JONES	10	9	2
0			10	9_	2

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