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	HILLER HELI PALO ALTO, CA	COPTERS
	ENGINEERIN	g report
	REPORT NO56-	-108
	MODEL NO. 103	31-A
TITLE	AERODYNAMICS OF D	DUCTED PROPELLERS
-	AS APPLIED TO THE	PLAIFORM PRINCIPLE
NO. OF PAG	Appendix I Appendix II Appendix III Appendix IV Appendix V	DATE <u>November 30</u> , By <u>A. Morse</u> CHECKED <u>R. Herda</u> APPROVED <u>R. M. Carle</u> R. Carlson APPROVED <u>R. Mungu</u> R. Wagner
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CON	FIDEN1	IAL		
		Symbol	<u>5</u>	
		2		
	A	Flow area $\sim ft^2$		
	AF	Activity factor		
	a	Lift curve slope $\sim dC_L/d$	a	
	Ъ	Number of blades		
	$C_{\mathbf{D}_{O}}$	Zero lift drag coefficie	nt	
	c_{LO}	Lift coefficient at a -	0	
	$C_{\mathbf{L}}$	Lift coefficient		
	Cm	Moment coefficient		
	D	Duct or propeller diamet	er \sim ft	
	F	Force \sim Pounds		
	f	Ratio of equivalent inte to flow area	rnal flat plate drag area	3
	HP	Horsepower		
	h	Clearance between blade	tip and duct	
	К	(l + f)		
	K '	Function of V_2/V_T		
	L	Lift \sim Pounds		
	Μ	Moment ~ foot pounds		
	m	Mass rate of flow \sim slu	gs/second	
	Р	Power $\sim \frac{\text{ftlbs.}}{\text{scc}}$		
	р	Pressure \sim lbs./ft. ²		
	q	Dynamic pressure \sim 1bs	•/ft. ² .	

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$\begin{array}{c} \underbrace{\text{SYREOLS}}_{(\text{Continued})} \\ \text{R} & \text{Duct or propeller radius } \sim \text{ ft} \\ \text{r} & \text{Propeller station radius } \sim \text{ ft} \\ \text{SHP} & \text{Shaft horsepower input} \\ \text{T} & \text{Thrust } \sim \text{ 1hs} \\ \text{V} & \text{Velocity } \sim \text{ ft/sec} \\ \text{Wg} & \text{Gross weight } \sim \text{ 1hs} \\ \text{W} & \text{Disk loading } \sim \text{ 1hs/ft}^2 \\ \text{a} & \text{Duct aerodynamic angle of attach } (\beta - \theta) \\ \beta & \text{Angle between the horizontal and duct centerline} \\ \eta_p & \text{Propeller efficiency} \\ \theta & \text{Angle between the horizontal and the free stream flow} \\ \rho & \text{Kass density} \\ \end{array}$	ONF	IDENTI	A L
$\frac{\text{SYNBOLS}}{(\text{Continued})}$ R Duct or propeller radius ~ ft r Propeller station radius ~ ft SMP Shaft horsepower input T Thrust ~ lbs V Velocity ~ ft/sec W _G Gross weight ~ lbs w Disk loading ~ lbs/ft ² a Duct aerodynamic angle of attach ($\beta = \theta$) β Angle between the horizontal and duct conterline η_p Propeller efficiency θ Angle between the horizontal and the free stream flow ρ Mass density V			
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r Propeller station radius ~ ft SiP Shaft horsepower input T Thrust ~ 1bs V Velocity ~ ft/sec W _G Gross weight ~ 1bs w Disk loading ~ 1bs/ft ² a Duct derodynamic angle of attack: $(\beta - \theta)$ β Angle between the horizontal and duct centerline η_p Propeller efficiency θ Angle between the horizontal and the free stream flow ρ Mass density		R	Duct or propeller radius \sim ft
SHP Shaft horsepower input T Thrust \sim 1bs V Velocity \sim ft/sec W _G Gross weight \sim 1bs W Disk loading \sim 1bs/ft ² a Duct aerodynamic angle of attach ($\beta = \theta$) β Angle between the horizontal and duct centerline η_p Propeller efficiency θ Angle between the horizontal and the free stream flow ρ Mass density		r	Propeller station radius \sim ft
T Thrust ~ lbs V Velocity ~ ft/sec W _G Gross weight ~ lbs w Disk loading ~ lbs/ft ² a Duct aerodynamic angle of attack ($\beta - \theta$) β Angle between the horizontal and duct centerline η_p Propeller efficiency θ Angle between the horizontal and the free stream flow ρ Mass density		S:P	Shaft horsepower input
$\begin{array}{llllllllllllllllllllllllllllllllllll$		Т	Thrust \sim 1hs
$\begin{array}{llllllllllllllllllllllllllllllllllll$		V	Velocity ~ ft/sec
$\begin{array}{llllllllllllllllllllllllllllllllllll$		WG	Gross weight 🗻 1bs
aDuct aerodynamic angle of attach $(\beta - \theta)$ β Angle between the horizontal and duct centerline η_p Propeller efficiency θ Angle between the horizontal and the free stream flow ρ Mass densityV		W	Disk loading $\sim lbs/ft^2$
$ \begin{array}{ccc} \mathbf{a} & & \mbox{Duct aerodynamic angle of attack: } \left(\beta - \theta \right) \\ \beta & & \mbox{Angle between the horizontal and duct centerline} \\ \eta_p & & \mbox{Propeller efficiency} \\ \theta & & \mbox{Angle between the horizontal and the free stream flow} \\ \rho & & \mbox{Mass density} \\ \end{array} $			
 β Angle between the horizontal and duct centerline η_p Propeller efficiency θ Angle between the horizontal and the free stream flow ρ Mass density 		۵	Duct aerodynamic angle of attack: (β - θ)
 η_p Propeller efficiency θ Angle between the horizontal and the free stream flow ρ Mass density V 		ß	Angle between the horizontal and duct centerline
 Angle between the horizontal and the free stream flow ρ Mass density V. 		$\eta_{ m P}$	Propeller efficiency
ρ Mass density V.		θ	Angle between the horizontal and the free stream flow
		ρ	Mass density
μ . Matio of induced velocity to blade potetional velocity $\mu = \frac{1}{12}$		μ	Actio of induced velocity to blade rotational velocity $\mu = \frac{v_{o}}{4\pi r}$
ø Inflow angle		ø	Inflow angle
¥ Flow coefficient		¥	Flow coefficient
2 Angular velocity rad./sec.		52	Angular velocity rad./sec.

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			(Continued)		
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			Subscripts		
	0	Free strea	996 619		
	1	Duct inlet			
	2	Propeller	inlet		
	3	Propeller			
	!	Duct exit			
	5	Wake, far	benind 4		
	D	Duct or dr	ng		
	Н	Hover			
	INT	Internal			
	N	Net			
	Р	Propeller			
	1	Resultant			
	S.L.	Sea Level			
	S	Shroud			

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I. SUMMARY

This report is intended to provide analytical means of prodicting the performance spectrum for ducted propeller aircraft that maintain an equilibrium of forces by adjusting the angle between the vertical and the exit stream tube. Equations are derived relating the tilt angle, free stream velocity, propeller characteristics, and available power, to the net force produced by the platform and to the direction of this force. Particular emphasis has been placed on the relation between the duct exit velocity and propeller tip speed for fixed pitch propellers, because this variation determines the relation.between the power available and the power required.

It is impossible to determine the accuracy of the individual relations without further test data, because they must be combined to determine the overall performance, and the overall performance - not individual performance contributions - was all that was obtained by test. The net force calculated for the condition indicating the greatest difference between theory and test (V = 45 knots, tilt angle = 31° , and 100% power) produced a net thrust of 515 pounds directed 8.05° aft of the vertical.

The test data of Reference 3 for the same conditions of tilt angle and velocity indicate a net thrust of 624 pounds directed aft 12° . The difference between the theoretical net thrust and test net thrust is 17.5%. This is rather poor correlation, but the error cannot be completely attributed to the theory, because the net thrust is dependent upon the square root of the available power cubed. The test was conducted at full power, and it is not apparent exactly how the power available varied with RPM or what effect tilting the engines had on power output. The expressions for the moment are empirical and involve non dimensional parameters which were determined from the truck test data of Reference 3; therefore the moment equation cannot be checked against the experimental data to determine their accuracy.

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INTRODUCTION

This analysis is complete for coaxial fixed pitch propellers, but not necessarily limited to exclude other types of propeller configurations. The procedure for calculating the performance will be outlined. Curves are presented which allow rapid estimation of tilt angles and power required for all disk loadings and power loadings. All information is based on the assumption that the flow does not separate from the duct lip. The flow will actually separate from the forward lip at a high duct angle of attack (a) (Figure 1) and large free stream velocity, but the lip shapes and disk loadings currently in use have shown no tendency toward separation.

The advantage of good internal aerodynamic design is obvious from Figure 2 and the definition of the quantity $[1 + (A_{\rm L}/A_2)^2 f]$. It can also be seen that high values of disk loading will require lower tilt angles for a given forward speed. Figure 2 indicates a minimum cruise power for platforms designed to cruise where $V_0(\rho/w_{\rm DH})^2 = .8$ to 1.0. If a platform is to be designed in this region, particular attention should be given to the moment, both from a standpoint of magnitude and the possibilities of the rate of change of the moment with velocity becoming negative.

A. Procedure for Performance Calculations

The conditions of altitude and temperature under which the platform must hover are used as a starting point. The required flow area and velocity are determined, and the propeller blade design is straight forward once the actual diameter and internal drag has been determined. The power required under these conditions is readily determined, since the flow velocity, areas, and tip speed are known. Figure 2 may be used to determine the relation between tilt angle and velocity. The external drag is very small compared to the lift; therefore the assumption that T/L sin β is zero (Equation 1.15) will be valid and will allow the determination of V_0/V_5 , consequently ψ , and an estimation of the pitching moment may be made. An indication of the hover ceiling and power required can be obtained from the curves by assuming that the propeller efficiency does not change.

If the performance obtained thus far is desirable, the relation between V_5/V_T and V_0/V_5 , given by Equation (4.01) or (4.02) should be determined. This information can then be used in Equation (2.07) of Section 2. Equation (2.07) should be plotted against V_0/V_5 ; this holds for all conditions and with Equation (1.04) relates the actual shaft power input to V_5 and V_0 . The power required along

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the flig thus np	ht equilibr: are known.	ium line can now be calculated as V _O /Vg	f and	
Sufficie formance	nt information for condition	ion is available for the calculation of ions other than flight equilibrium.	per-	
The cile	ct of tip cl	learance on power loading for the shrou	ided	

The effect of tip clearance on power loading for the shrouded propeller of Reference 4 is given in Figure 5. If the velocity over the lip increases or the lip is made sharper, the tendency toward flow separation is increased and the tip clearance must be held to closer tolerances.

The product of the number of blades and the activity factor is used in most propeller weight equations; of interest here is the design value of b(AF) which may be calculated using the velocity and tip speed under the same conditions used to design the propeller. The method outlined in Section 8 is straight forward. The assumption of constant taper is put into the equation, but an ideal taper blade will actually have a b(AF) slightly lower than the calculated value; therefore the assumption is conservative.

ANALYSIS

A. <u>Aerodynamics of Ducted Propellers with Particular Application</u> to Platforms

The general equations relating power and thrust will be calculated using the conservation of energy and the momentum equation.



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The equation for the net thrust is obtained immediately by the use of the momentum equation between stations (0) and (5)

 $T_N = mV_5 - mV_0 + p_5A_5 - p_0A_0 - p_0(A_5 - A_0)$

A pressure equilibrium exists between the jet stream and the surrounding air at station 5; therefore $p_3 = p_0$.

$$T_{\rm NC} = nV_{\rm C} \left(1 - V_{\rm O}/V_{\rm C}\right) \tag{1.01}$$

The change in kinetic energy is equal to the power put into the air stream.

$$P = KE(5) - KE(0) + \Delta KE(0) - (5)$$

$$P = \frac{m}{2} \left(V_5^2 - V_0^2 + \frac{2\Delta KE(0) - (5)}{m} \right)$$

The energy lost by the air in passing from station (0) to (5) is equal to the integral of the product of the drag and velocity from station (0) to station (5).

If the conservative assumption is made that the internal drag is acting at station (2) where the velocity is the greatest, the evaluation of $\triangle \text{KE}(0) = (5)$ is simplified.

$$\triangle \text{KE}(0) = (5) = \text{DV}_2$$

 and

 $D = C_D A_{REF}$, q_2

By definition

f

$$= \frac{C_{D} A_{REF}}{A_2}$$
(1.02)

$$D = \mathbf{f}_{2}A_{2} = \frac{\mathbf{m}}{2}\mathbf{f}_{2}$$
$$\Delta KE(0) - (5) = \frac{\mathbf{m}V_{5}^{2}}{2}\left(\frac{A_{1}}{A_{2}}\right)^{2}\mathbf{f}$$
$$\mathbf{P} = \frac{\mathbf{m}}{2}\left[V_{5}^{2} + V_{5}^{2}\left(\frac{A_{1}}{A_{2}}\right)^{2}\mathbf{f} - V_{0}^{2}\right]$$

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	P = but 1 +	$\frac{mV_5^2}{2} \begin{bmatrix} 1\\ 1\\ \left(\frac{A_{l_1}}{A_2}\right)^2 f \end{bmatrix}$	$ \left(\frac{\mathbf{A}_{11}}{\mathbf{A}_{2}}\right)^{2} \mathbf{f} - \frac{\mathbf{v}_{0}^{2}}{\mathbf{v}_{5}^{2}}] $ $= \mathbf{K} $		
	by definit P =	$\frac{mV_5^2}{2}$ K	$\left[1 - \left(\frac{V_0}{V_5}\right)^2 \frac{1}{K}\right]$	(1.03)
	The term of required; equivalent when the p as the dis Therefore; large dist included f included f is more ne	defined as the defini- t flat pla blatform is stance is , if there tance above in calcula- in the extension early that	"K" has a large influence on the total ition of f, Equation (1.02), shows that te drag area ($C_{D}A_{AEF}$) must be kept smill s hovering, the velocity diminishes ray traversed from station (1) to station (is an appreciable amount of drag area e the duct lip, this drag area should a ting the value of "K". Instead it show ernal drag, since the velocity in this of the free stream.	l power t the all. bidly (0). a not be ald be region	
	The power the air by	put into the para: <u>horsep</u>	the shaft is greater than the power in: site power and induced drag power. ower input to air	out to	

S.

8,

$$\eta_{p} = \frac{SHP - (HP_{0} + HP_{1})}{SHP}$$

$$\eta_{p} = 1 - \frac{HP_{0} + HP_{1}}{SHP}$$

$$SHP = \frac{mV_{5}^{2}}{1100 \eta_{p}} \left[K - \left(\frac{V_{0}}{V_{5}}\right)^{2} \right] \qquad (1.0h)$$

The power input to the air is equal to the product of the propeller thrust and the velocity of the air through the propeller disk.

$$T_{P_G} \frac{V_2}{550} = SHP \eta_P$$

but

 $V_2 = \frac{A_{l_1}}{A_2} V_5$

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$$T\mathbf{P}_{G} = SHP \eta_{F} \frac{550}{V_{5}} \frac{A_{2}}{A_{4}}$$
$$T\mathbf{P}_{G} = \frac{mV_{5}}{2} \frac{A_{2}}{A_{4}} \left[K - \left(\frac{V_{0}}{V_{5}}\right)^{2} \right]$$
(1.05)

This gross propeller thrust is actually the thrust that the propeller is producing; however part of this thrust is required to draw the air through the shroud, and the net propeller thrust is all that is actually lifting the platform.

$$T_{\mathbf{P}_{\mathbf{U}}} = \mathbf{D} + T_{\mathbf{P}_{\mathbf{N}}}$$
$$T_{\mathbf{P}_{\mathbf{N}}} = \frac{m \, \mathbf{V}_{5}}{2} \, \frac{\mathbf{A}_{2}}{\mathbf{A}_{L}} \left[1 - \left(\frac{\mathbf{V}_{0}}{\mathbf{V}_{5}} \right)^{2} \right]$$
(1.06)

When $V_0 = 0$

$$T_{N} = mV_{5} \text{ from (1.01)}$$

$$SHP = \frac{mV_{5}^{2} K}{1100 \eta_{p}}$$

$$SHP = \frac{T_{N}}{1100 \eta_{p}} \left(\frac{T_{N}}{\rho A_{l_{1}}}\right)^{\frac{2}{3}} K \qquad (1.07)$$

ShiP =
$$\frac{(T_N)^{3/2}}{(\rho/\rho_{S.L.} A_{\mu})^{\frac{1}{2}}} = 1.865(10)^{-2} \frac{K}{\eta_P}$$
 (1.05)

$$T_{\rm N} = 14.22 \, \left(\rho / \rho_{\rm S.L.} A_{l_1}\right)^{1/3} \, \left(\frac{\rm SHP}{\rm K} \eta_{\rm P}}{\rm K}\right)^{2/3} \tag{1.09}$$

when $V_0 \neq 0$

The equations for thrust involve both velocity and direction; therefore it will be necessary to express the equations in terms of their components in the directions of lift and thrust so that the equations for equilibrium flight can be shown explicitly. Defining the angles, as shown in Figure 1, and assuming that V_5 is parallel to the centerline of the duct, the equations for lift and thrust become:

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	ΣF	/ = L		
	L	- m (V ₅ s	inβ - V _O sin Θ)	
	۷ _O	sin G =	$V_{\varsigma} \sin \beta = \frac{L}{m}$	
		2 / V		
	sin		$\frac{1}{\alpha} \sin \beta = \frac{1}{\alpha V_0} $	
	7 8	- T		
	۲x	- 1		
	<u> </u>	- m (V5 c	$os\beta - V_0 \cos \Theta$)	
	COS	$r^2 = \left(\frac{v}{v}\right)$	$\frac{5}{\cos \beta} - \frac{T}{T}$	
			0 • mv 0 /	
	but sin	$^2 \Theta + \cos^2$	0 = 1.0	
	(Ve)	2 2	$(V_{5})^{2}$ 2 $(L)^{2}$ $(T)^{2}$ 2L	sin 6
	$\left(\overline{v_{0}} \right)$) sin β +	$\left(\frac{1}{V_{O}}\right) \cos^{2}\beta + \left(\frac{1}{mV_{O}}\right) + \left(\frac{1}{mV_{O}}\right) = \frac{1}{\rho}$	AL VOZ
			+ 2'	$\frac{\Gamma \cos \beta}{\sqrt{2}} + 1$
			þ.	°Ц V0
		$\frac{2}{2}$ ($\frac{2}{1}$) ²	$\int (\pi)^2 \mathbf{J}$ or π	
	$\left(\frac{v_{O}}{v_{O}}\right)$	$\left(\frac{L}{mV_{O}}\right) + \left(\frac{L}{mV_{O}}\right)$	$\left[1 + \left(\frac{1}{L}\right)\right] = \frac{2L}{\rho A_{1} V_{0}^{2}} (\sin \beta + \frac{1}{L} \cos \beta)$	psβ) + 1
			$\sim 10^{2}$	
	V54	$+\left(\frac{L}{\rho A_{1}}\right)^{2}$	$\left[1 + \left(\frac{T}{L}\right)^{2}\right] = \frac{2L \sqrt{5}}{\rho A_{5}} (\sin \beta + \frac{T}{L} \cos \beta) $	+ (V ₅ V ₀) ²
		4		
	v ₅ 4	$-V_5^2 \frac{2L}{2A}$	$\left(\sin\beta + \frac{T}{L}\cos\beta + \frac{\rho A_{l_1} V_0^2}{2L}\right) + \left(\frac{L}{\rho A_{l_2}}\right)^2$	$\left[1 + \left(\frac{T}{T}\right)^2\right] = 0$
)	> pr]		
				(1.12)

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	. 2	L (.	PALVO ²		
	¥ 5	$\overline{\rho A_{l_1}}$ (sin	$\mu + \frac{\Gamma}{\Gamma} \cos \beta + \frac{5\Gamma}{2\Gamma}$		1
		$\frac{1}{2} \left\{ \int_{\rho A_{l_{i}}}^{L} d\rho \right\}$	$\left(\sin\beta + \frac{T}{L}\cos\beta + \frac{\rho A_{L}V_{0}}{2L}\right)^{2} - \left(\frac{L}{\rho A_{L}}\right)^{\frac{1}{2}} \left[1\right]$	$-\left(\frac{T}{L}\right)^2$]}
				((1.13)
	Equation (actual cas simplified	1.13) is v e for equi •	ery cumbersome. If $\theta = 0^{\circ}$ which is th librium flight, the solution is greatl	e Y	
	₽ =	0 ⁰			
	V _O s	in 9 = V	$5 \sin\beta - \frac{L}{n}$		
	V ₅ s	in β = ρ	L A ₁ , V ₅		
	۷ ₅	$= \left(\begin{array}{c} L \\ \rho A \\ \mu \end{array} \right)$	sin ² p		(1.1!.)
	V _O c	os 🔒 📼 V	$\frac{T}{5}\cos\beta - \frac{T}{n}$		
	CO S	0 = 1.0			
	۷ _O	≡ V _{r,} cos	$p = \frac{T}{\rho A_{1}V_{5}}$		
	V _O V ₅	= cosβ -	$\frac{T}{\rho A_{li}V_5^2}$		
	but v_5^2	$= \frac{L}{\rho A_{\downarrow} si}$	nβ		
	V _O V ₅	= cos β	$-\frac{\mathrm{T}}{\mathrm{L}}\sin\beta$		(1.15)
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	but JHP	= <u>n V5</u> = 1100 ŋ	$\frac{2}{\mathbf{P}} = \left[\mathbf{X} - \left(\frac{\mathbf{V}_{0}}{\mathbf{V}_{0}} \right)^{2} \right] \text{Equation (1.7.)}$	
	J. :P	11/2 11/2 r	$\frac{1}{\mathbf{P}} \begin{bmatrix} \mathbf{X} - (\mathbf{b} \mathbf{x} + \frac{\mathbf{p}}{2} \sin \mathbf{p}) \end{bmatrix}$	
	SilP	= <u>ρΑ_ι</u> 1100 η	$\frac{\frac{3}{2}}{P} \left(\frac{L}{\rho A_{l_1}}\right)^{3/2} \beta \left[K - (\cos \beta - \frac{T}{L} \sin \beta)^2 - \frac{T}{L} \sin \beta \right]$	r: ¢) ²]
1	SHP	$\frac{L^{3/2}}{1100}$	$\frac{K}{\left[1 - \frac{(\cos\beta - T/L)}{K}\right]^{2} \sin^{3/2}\beta} \left[1 - \frac{(\cos\beta - T/L)}{K}\right]$	<u>sinβ</u>) ²] (1.16)

Equation (1.16) gives the lorsepower required to produce a given lift and thrust when $\Theta = 0^{\circ}$ and β is the angle defined. For $L = W_{G}$ Equation (1.07) becomes:

$$SHP_{H} = \frac{L^{3/2} K}{1100 \eta_{P_{H}} (\rho A_{L})^{\frac{5}{2}}}$$

and Equation (1.16) becomes:

$$\frac{SHP}{SHP_{\rm H}} = \frac{\eta_{\rm P_{\rm H}}}{\eta_{\rm P}} \frac{1}{\sin^{3/2}\beta} \left[1 - \frac{(\cos\beta - T/L\sin\beta)^2}{K}\right] \qquad (1.17)$$

$$\frac{\eta_{\mathbf{P}} \text{SHP}}{\eta_{\mathbf{P}_{H}} \text{SHP}_{H}} = \frac{1}{\sin^{3/2} \beta} \left[1 - \frac{(\cos \beta - T/L \sin \beta)^{2}}{K} \right] \quad (1.13)$$

Figure 2 is a graphical representation of Equation (1.1°) . Another equation is required to determine what free stream velocity is associated with the different tilt angles $(90 - \beta)$.

The equations obtained from summing the forces in the directions of L and T with the assumption of $\theta = 0$ will provide the necessary relation. This is equation 1.19 which is also shown on Figure 2.

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		L = mV5 sin	ja ja		
		2 (L			
		VS OA	sin ß		
	Land	4 4			
	and	T = n (V, c	os 6 - V.)		
		$V = \cos \theta = -$	T V		
		5 το ρ	ali ^v 5		
		17			
		$\frac{1}{V_{\mu}} = \cos \beta$			
		ь. У	Palit		
		vo	Th.		
		$\frac{\sigma}{V_5} = \cos \beta$	$-\frac{1}{L}\sin\beta$		
	but				
	240	$w_{D_{H}} = \frac{L}{A_{L}}$			
		4			
		$V_{0} \equiv \left(\frac{L}{L} \right)^{\frac{1}{12}}$	$-\frac{T}{L}\sin\beta$		
			sin'β		
		$V_{O}\left(\underline{\rho}\right)^{2} =$	$\frac{1}{1}$ (cos $\beta = \frac{T}{2}$ sin β)		(1.19)
		$\cup (w_{D_{Ii}})$	sin ⁵ β		
	From	Figure 1 the cr	kit velocity is directed & degrees from	the	

From Figure 1 the exit velocity is directed p degrees from the horizontal, and the assumption was made that the lation was tilted to an angle $(90^{\circ} - \beta)$. If it is assumed that the platform tilt angle remains zero $(\beta = 90^{\circ})$ and only the exit stream is turned through the angle $(90^{\circ} - \beta)$, the force diagram remains the same. Therefore, the tilt angle $(90^{\circ} - \beta)$, shown in Figure 2, can be interpreted as the angle through which the exit stream is turned. The moment produced by a platform propelled by turning the exit stream, rather than tilting the platform, will be effected to a large extent. This can be seen if the equations for the thrust

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	produced t	by the duct	are found. This can be accomplished	by	
	component;	s of the pr	opeller net thrust	LNC	
	TP _N	* <u>n V5</u>	$\frac{\lambda_2}{\lambda_1} \left[1 - \left(\frac{v_0}{V_1} \right) \right]$		
	* • 1	-			
	, .	n m (V a ci	n Verste a)		
		- IN (40 DI	m b = x0 prn a)		
	ŗ.	•	osid – Vo cosi⊖)		
				2	
	$^{\mathrm{T}}\mathrm{D}_{\mathrm{I}}$	= :: V5 (s	$\sin \beta = \frac{\gamma_0}{\gamma_2} \sin \beta = \frac{\pi \gamma_5}{2} \frac{\kappa_2}{\kappa_1} \sin \beta = \frac{1}{2}$	$\left(\frac{O}{V_{z}}\right)$	
	2			· 57	
	ጥ	జా చింది	$\frac{A_2}{V_0} \left[1 - \left(\frac{V_0}{V_0} \right)^2 \right] = \frac{V_0}{V_0} \sin \theta$		
	ι υĽ		$\sum_{i=1}^{n-1} \frac{1}{2A_{i}} \left[\frac{1}{1} - \left(\sqrt{c_{f}} \right) \right] = \sqrt{c_{f}} \frac{1}{\sin \beta}$	ſ	
			$\begin{bmatrix} A_2 & A_2 & (V_0)^2 & V_0 & J_1 & 0 \end{bmatrix}$		
	T_{D_L}	= n Vg si	$\ln \beta \left[1 - \frac{\alpha_2}{2A_h} + \frac{\alpha_2}{2A_h} \left(\frac{0}{V_c} \right) - \frac{\alpha_0}{V_c} \frac{\sin \theta}{\sin \rho} \right]$	(1	.20)
				n	
	TDm	= m V _C (c	$\cos \rho = \frac{V_0}{V} \cos \theta$) $= \frac{\omega V_5}{2} \frac{A_2}{A_2} \cos \rho = \frac{1}{2} \frac{1}{1} - \frac{1}{1} $	$\left(\frac{v_{c}}{v}\right)$	
) (v s z a _l	(*5/ J	
	_		$\begin{bmatrix} A_2 & A_2 & (V_0)^2 & V_0 & cos \end{bmatrix}$	7	
	TDm	= mVc co	$s_{\beta} < 1 - \frac{1}{24} + \frac{1}{24} (\frac{1}{24}) - \frac{1}{24} + \frac{1}{24}$) (1	.21)

Examination of Equations (1.20) and (1.21) indicate an increase in the total duct force when $\theta = 0^{\circ}$ and V_0/V_5 is increased. The point of application of the resultant duct lift moves forward as V_0/V_5 increases and the duct lift becomes larger; therefore the moment will increase rapidly with V_0/V_5 when the tilt angle $(90^{\circ} - \beta)$ is small.

The drag to lift ratio is difficult to determine, because the direction of the streamlines over the external surfaces are not easily determined. If Equation (1.15) is plotted (V_0/V_5 VS β) for T/L = 0, θ = 0 and the truck test data for the platform model 1031 is corrected so as to keep the lift equal to a constant (Figure 3)

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reasonably good agreement between test and theory is found. This indicates that the drag component in the direction of flight is very small and can be neglected. The method used to correct the test data and an example calculation is shown in Appendix A.

POWER REQUIRED

The term η_P has appeared frequently with no mention of how it is to be obtained. To do this, it will be necessary to determine where the total power put into the propeller shaft is consumed.

The total power required is the sum of the induced power, the blade profile power, the shroud profile power, and the induced drag power.

The induced drag power (PL) is the power necessary to overcome the torque caused by the component of lift in the plane of rotation.

The shroud profile power (P_{OS}) is the power necessary to overcome the resistance to flow caused by the shroud and internal objects in the flow field. Because the propeller thrust must overcome the shroud profile power, the product of propeller thrust and velocity through the propeller is equal to the sum of the shroud profile power and the induced power.

$$\mathbf{P}_{\underline{S}} + \mathbf{P}_{O_{\underline{S}}} = \mathbf{T}_{\mathbf{P}} \mathbf{V}_{2} = \mathbf{T}_{\mathbf{P}} \mathbf{V}_{\underline{S}} \frac{\mathbf{A}_{\underline{L}}}{\mathbf{A}_{2}}$$

but

$$T_{\mathbf{P}} = \frac{vV_{5}}{2} \left[K - \left(\frac{V_{0}}{V_{5}}\right)^{2} \right]$$

$$P_{1} + P_{v_{5}} = \frac{mV_{5}^{2}}{2} \frac{A_{L}}{A_{2}} \left[K - \left(\frac{V_{0}}{V_{5}}\right)^{2} \right]$$
(2.01)

A. Induced Drag Power

$$dQ = \frac{\rho}{2} V_{R}^{2} c r C_{L} \sin \phi dr$$

but $V_{\rm R} = \frac{V_2}{\sin \phi}$

$$dQ = \frac{\rho}{2} \frac{V_2^2 c C_L}{\sin \phi} r dr$$

and $\sin \phi = \tan \phi = \frac{V_2}{\Omega r}$

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	Q	$\frac{\rho}{2} V_2 c$	C _L gr rdr		
	ೆPL		$\int_{0}^{R} C_{L} c r^{2} dr$ for one blade		
	dPL	$=\frac{b\rho}{2}V_2$	$\int_{0}^{R} C_{L} c r^{2} dr$ for b blades		
	The induce and shroud CL and c w	d drag pow profile:p ill be ade	er is small compared to the induced popower; therefore the assumption of consequate.	stant	
	. • PL	<u>pbci</u> 6	CL V2VTR		
	PL	<u> </u>	$\frac{R}{2}$ C_{L} V_{T}^{2} $\frac{V_{2}}{V_{T}}$ R		(2.02)
	Expressing section cha uniform cha be related	the prope aracterist ord and 11 to the pr	eller thrust in terms of the propeller tics, and raking use of the assumption ift coefficient, the induced drag power ropeller thrust.	blade of can	
	Tp	$= \int_{0}^{\mathbf{R}} \frac{\mathbf{p}}{2} \left(\mathbf{y} \right)$	er) ² C _L b c dr		
	Ţ P	<u>pbcR</u>	<u>CL</u> V _T ²		
	PL ·	$= T_{\mathbf{P}} \frac{V_2}{V_T} F$			(^.03)
F	B. <u>Propeller 1</u> P _O =	Profile Po b c RPC 8	Dwer DOV ³ K' (Reference 1)		
	where	K • - V	$\frac{2}{T}$ by definition (Figure 8)		
	P ₀ =	<u>pbcF</u>	$\frac{c_{\rm L} v_{\rm T}^2}{6} \frac{3}{L} v_{\rm T} \kappa' \frac{c_{\rm DO}}{c_{\rm L}}$		
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		P ₀	= <u>3</u> Tp V ₁	r K · CDO		(2.04)
		P ₀	• P _L =	$T_{\mathbf{P}} \left[\frac{3}{L} V_{\mathrm{T}} K' \frac{C_{\mathrm{D}_{\mathrm{O}}}}{C_{\mathrm{L}}} + \frac{V_{2}}{V_{\mathrm{T}}} R \right]$		(2.05)
	but	TPG	$=\frac{m V_5}{2}$	$\frac{1}{V_{4}} \left[K - \left(\frac{V_{0}}{V_{5}} \right)^{2} \right] \text{from equation (1.05)}$	5)	
		T _{PG}	ρ <u>Αι</u> V	$\frac{2}{2} \frac{A_2}{A_{l_1}} \left[K - \left(\frac{V_0}{V_5} \right)^2 \right]$		
(C. <u>Summa</u>	tion	of Power i	lequired		
		Pr	= P <u>4</u> +	$P_{0_{S}} + P_{0} + P_{D}$		
		Pr	$\frac{\pi V_5^2}{2}$	$\left[\mathbf{K} - \left(\frac{\mathbf{V}_0}{\mathbf{V}_5} \right)^2 \right] + \frac{\mathbf{m} \cdot \mathbf{V}_5}{2} \frac{\mathbf{A}_2}{\mathbf{A}_4} \left[\mathbf{K} - \left(\frac{\mathbf{V}_0}{\mathbf{V}_5} \right)^2 \right]$]	
			$\begin{bmatrix} \frac{3}{L} v_T \end{bmatrix}$	$K' \frac{C_{DO}}{C_L} + \frac{V_2 R}{V_T}$		
		Pr	$\frac{m V 5^2}{2}$	$\left[\mathbf{K} - \left(\frac{\mathbf{V}_{0}}{\mathbf{V}_{5}} \right)^{2} \right] \left[1 + \frac{\mathbf{A}_{2}}{\mathbf{A}_{l_{4}}} \left[\frac{3}{l_{4}} \frac{\mathbf{V}_{T}}{\mathbf{V}_{5}} \mathbf{K}^{*} \frac{\mathbf{C}_{D_{G}}}{\mathbf{C}_{L}} + \frac{\mathbf{A}_{2}}{\mathbf{A}_{1}} \right] \right] \left[\mathbf{K} + \frac{\mathbf{A}_{2}}{\mathbf{A}_{1}} \right] \left[\frac{3}{l_{4}} \frac{\mathbf{V}_{T}}{\mathbf{V}_{5}} \mathbf{K}^{*} \frac{\mathbf{C}_{D_{G}}}{\mathbf{C}_{L}} + \frac{\mathbf{A}_{2}}{\mathbf{A}_{1}} \mathbf{K}^{*} \frac{\mathbf{V}_{T}}{\mathbf{V}_{5}} \mathbf{K}^{*} \frac{\mathbf{C}_{D_{G}}}{\mathbf{C}_{L}} \right] \left[\frac{3}{l_{4}} \frac{\mathbf{V}_{T}}{\mathbf{V}_{5}} \mathbf{K}^{*} \frac{\mathbf{C}_{T}}{\mathbf{C}_{L}} \mathbf{K}^{*} \frac{\mathbf{C}_{T}}{\mathbf{C}_{L}} \mathbf{K}^{*} \mathbf{K}^{*} \mathbf{K}^{*} \frac{\mathbf{C}_{T}}{\mathbf{C}_{L}} \mathbf{K}^{*} \mathbf$	$\left[\frac{R}{L_2} \frac{R}{V_T}\right]$	}
	when	VO	= 0			
		T ≃	m V5 =	$PA_{4}V_{5}^{2}$		
		vș	$=\left(\frac{T}{\rho A_{\downarrow}}\right)^{\frac{1}{2}}$	2		
		Pr	$= \frac{T^{3/2}}{2\sqrt{\rho A_1}}$	$\frac{K}{L} = \left[1 + \left[\frac{3}{L} \frac{A_2}{A_L} V_T \left(\frac{\rho A_L}{T} \right)^{\frac{1}{2}} \frac{K \cdot C_{D_0}}{C_L} + \frac{R}{V_T} \right] \right]$	[]]	

 $HP_{r} = \frac{T^{3/2} K}{1100 \sqrt{\rho A_{L}}} \left\{ 1 + \left[\frac{3}{L} \frac{A_{2}}{A_{L}'} V_{T} \left(\frac{\rho A_{L}}{T} \right)^{\frac{1}{2}} \frac{K \cdot C_{D_{0}}}{C_{L}} + \frac{R}{V_{T}} \right] \right\} (2.06)$

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but $\frac{A_{\downarrow}}{A_{2}}\frac{R}{V_{T}} < < 1.0$

Therefore, the approximation of $R/V_T = R/V_{TH}$ will be rood, particularly in view of the fact that V_T was found to vary very little when the five foot Hiller platform was truck tested. This data was not published.

$$\frac{1}{\eta_{\rm P}} = 1 + \left[\frac{3}{L}\frac{V_{\rm T}}{V_5}K'\frac{C_{\rm DO}}{C_{\rm L}}\frac{A_2}{A_{\rm L}} + \frac{R}{V_{\rm T_{\rm H}}}\right]$$
(2.07)

BLADE DESIGN

This analysis is concerned only with counter-rotating coaxial blades. The method of analysis given in Reference 2 has been shown to give good results, provided the substitution of $C_L = (a \alpha + C_{LO})$ is made rather than $C_L = a \alpha$. The above

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substitution was necessary to generalize the equations for use with other than symmetrical airfoil sections. This effects only Equation (10) and (11) of Reference 2.

If no substitution is used for CL but b is used as defined in this report and Equations (10) and (11) of Reference ? are solved for the chord, the resulting equations can be used to determine the variation of chord with radius.

$$c_1 = \frac{2 R K \pi (r/i) \mu \sin p_1}{C_1 b}$$

similarly for the lower propeller.

$$c_2 = \frac{2 R K \pi (r/d) \mu \sin \phi_2}{C_L b}$$

The optimum propeller design is one which has a maximum lift to drag ratio at all blade stations ($C_L = \text{constant}$).

If the required performance is known, V2 can be calculated from Section 1; a tip speed and number of blades can be chosen, thus giving all the information necessary to compute the variation of the chord with radius. Blade angles are then computed in accordance with Reference (2). When design requirements dictate a constant taper, proceed as above and approximate the optimum chord versus r/R curve with a straight line and use the constant taper variation of chord with radius to determine the blade angle setings as per Reference (2).

VARIATION OF TIP SPEED WITH DUCT EXIT VELOCITY

FOR FIXED PITCH PROPELLERS

The variation of propeller efficiency with forward velocity is dependent upon the variation of the outt exit velocity and propeller tip speed (Equation 2.07).

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	and [1 dT dT	$ \cdot \left(\frac{V_2}{2r}\right)^2 $ $ = \frac{\rho}{2} \frac{\rho}{2r^2} $ $ = \frac{\rho}{2} \frac{\rho}{2r^2} \left[\frac{\rho}{2r^2} + \frac{\rho}{2r^2} \right]^2 $	$\begin{bmatrix} \frac{1}{2} \\ \frac{1}{2} \end{bmatrix} = \begin{bmatrix} 1 + \frac{1}{2} \left(\frac{y_2}{2r} \right)^2 \end{bmatrix}$ $\begin{bmatrix} a \beta \\ - a \frac{y_2}{2r} + c_{L_0} \end{bmatrix} \begin{bmatrix} 1 + \frac{1}{2} \left(\frac{y_2}{2r} \right)^2 \end{bmatrix} i edi$ $\begin{bmatrix} a \beta \\ - a \frac{y_2}{2r} + c_{L_0} + \frac{a \beta}{2} \left(\frac{y_2}{2r} \right)^2 - \frac{a}{2} \left(\frac{y_2}{2r} \right)^2 \end{bmatrix}$ $= \begin{bmatrix} \frac{y_2}{2r} + c_{L_0} + \frac{a \beta}{2} \left(\frac{y_2}{2r} \right)^2 \end{bmatrix} i edi$	$\left(\frac{2}{r}\right)^3$

The last three terms in the bracket are small compared to the first three.

$$dT = \frac{\rho}{2} \frac{\rho}{2r} \frac{r^2}{2r} \left(\beta - \frac{V_2}{2r} + \frac{C_{LO}}{a}\right) \text{ bed}r$$

$$r = \lambda \frac{r}{\lambda}$$

$$dr = \lambda d \left(\frac{r}{\lambda}\right)$$

$$dT = \frac{a}{2} \rho V_T^2 \lambda \left(\beta - \frac{V_2}{V_T \left(\frac{r}{\lambda}\right)} + \frac{C_{LO}}{a}\right) \text{ be } \left(\frac{r}{\lambda}\right)^2 d \left(\frac{r}{\lambda}\right)$$

This element of force summed over r/R must equal the propellor thrust. It must to remembered that blockare and the necessary fairing of the blade near the root will alter the flow in that area. In practice, then, it will be necessary to account for this during summation. Pernaps the simplest method would be to assume ideal blade conditions down to some minimum radius, producing uniform inflow beyond and zero velocity inside this radius.

$$T_{\mathbf{P}} = \int_{\binom{\mathbf{r}}{R}_{\min}}^{1 \cdot 0} dT = \frac{\rho}{2} \mathbf{a} V_{\mathbf{T}}^{2} R \left(\frac{1 \cdot 0}{(\beta - \frac{V_{2}V}{V_{\mathbf{T}}(\frac{\mathbf{r}}{R})} + \frac{O_{LO}}{a}) \operatorname{bc} \left(\frac{\mathbf{r}}{R}\right)^{2} \operatorname{d} \left(\frac{\mathbf{r}}{R}\right)$$

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			As Applied to the Platform Principle	* CPORT HO: 56-30
CONF	<u>1 D E N T I A</u> 2 авр	$\frac{\mathbf{L}}{\mathbf{v}_{\mathrm{T}}^{2} \mathbf{R}} = \int_{0}^{\infty}$	1.0 $\beta c \left(\frac{r}{R}\right)^2 d \left(\frac{r}{R}\right) - \frac{V_2}{V_T} \int_{\left(\frac{r}{R}\right)_{rin}}^{1.0} c \left(\frac{r}{R}\right) d \left(\frac{r}{R}\right)$	r) <u>R</u>)
			$ + \frac{C_{L_0}}{a} \int_{\frac{r}{R}}^{1.0} c \left(\frac{r}{R}\right)^2 d\left(\frac{r}{R}\right) $	
	c _l	$= \int_{\left(\frac{r}{R}\right)}^{1.0}$	$p c \left(\frac{r}{R}\right)^2 d \left(\frac{r}{R}\right)$	
	C ₂	$= \int_{\left(\frac{r}{R}\right)_{\min}}^{1.0}$	$c \left(\frac{r}{R}\right) d \left(\frac{r}{R}\right)$	
	c ₃	$= \int_{\left(\frac{r}{R}\right)_{\min}}^{1.0}$	$\frac{C_{L_0}}{a} c \left(\frac{r}{R}\right)^2 d \left(\frac{r}{R}\right)$	
	2 abp	$\frac{T_{\mathbf{P}}}{V_{\mathrm{T}}^{2}R} =$	$c_1 - \frac{V_2}{V_T} c_2 + c_3$	
	abp 1	$r_{\mathbf{P}}$ + v_{T}^{2} R +	$\frac{v_2}{v_T} c_2 - (c_1 + c_3) = 0$	(4.01)
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	to calculate	the pitenin	drige an 195 d dribobent by	i artacz m s Simplifi	akes it impossi ed tho dimensio	nal			
	approach.								
	The only info	rmation ava	uilable on pr	Chine hore	ent is data obt	ained			
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	of pressure s	urvey data.	Using the	pressure s	urwey data to c	ieterm	ľ. e		
	the moment co	intributed b	y the fuct t	he followi:	n⊤ resal s w∈re	e ofita:	t, de la		
	At 1° ti	lt angle vi	thost dury	nnd 35 .mo	t forward speed	9 9			
	Cal	culated mon	ent 1.6.	(t]!s.					
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	values, parti	cularly in	view of the	fact that	the pressure su	n veð 1	n		
	cluded only f tions.	our static	is: front lip	, rear lip	h ⁵⁰ and 900 1	lip pos			
	The conclusio	m drawn "ro duct. This	om this deta s does not so	ns that th Ave the pr	e uctal noment oblem of determ	is pro nanc	1		
	the moment to	be expecte	ed from any a	ruitrary d	acted provelies	., but			
	it does shed some light on the problem.								
	The force pro	ducing the	noment is th	e interni	of the pressa	(e. a.c.			
	the velocity	increases (n flor dear	from the filed	stream va	lue to the dut	exit			
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	Έ,	= Ar Vr	$(Y_{\mathcal{C}} \cdots Y_{\mathcal{O}})$	From E	nuation 1.0				
	-1.		(1)						
	T	<u>v</u> <u>v</u> 5	$\left(\frac{V_5}{1} \right)$	= \k	5. () I				
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This non-dimensional parameter (ψ) has been taken as a representation of the flow field. The moment must increase directly with the diameter and with the square of the velocity over the lip, but at the same value of V₀/V₅ this is proportional to the square of the free stream velocity. For this reason the moment coefficient has been taken as:

$$C_{m} = \frac{W}{2q_{0} D A_{l_{1}}}$$
(5.02)

The five foot platform truck test data has been plotted in coefficient form (Figure h).

It has previously been mentioned that the only moment data available is from one configuration, but it is believed that the use of Figure 4 will at least give the order of magnitude and trend of the moment to be expected from an abitrary selected ducted propeller.

PLATFORM HOVER CEILING

Equation 1.08 indicates that the power required varies with the reciprocal of the density ratio. The power available is also a function of the density ratio; therefore to eliminate trial on error the equations have been combined.

The variation of power available with density ratio is given in deference l_i as:

$$SHP_{ALT} = SHP_{SL} (1.132 c / SL - .132)$$
 (6.01)

By combining Equation 1.09 and Equation 6.01 the variation of thrust with altitude becomes:

$$T_{ALT} = 14.22 (c/p_{JL} A_{l_1})^{1/3} \left[\frac{31P_{ALT} P_{ALT}}{K}\right]^{2/3}$$
 Equation 1.09

$$T_{SL} = 14.22 (A_{L}) \left[\frac{SHP_{SL} \eta_{P_{SL}}}{K} \right]^{2/3}$$
(6.02)

$$\cdot \cdot \frac{T_{ALT}}{T_{SL}} = \left(\frac{\eta_{P_{ALT}}}{\eta_{P_{SL}}}\right)^{2/3} \left(\frac{\rho_{ALT}}{\rho_{SL}}\right)^{1/3} (1.132 \,\rho/\rho_{SL} - .132)^{2/3} (6.03)$$

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$$\frac{T_{ALT}}{T_{SL}} \left(\frac{\eta_{P_{ALT}}}{\eta_{P_{SL}}}\right)^{2/3} \cdot \left(\frac{\rho}{\rho_{SL}}\right)^{1/3} (1.132 \ \rho/\rho_{SL} - .132)^{2/3}$$
(6.04)

For convenience Equation 6.04 is plotted in Figure 5. To determine the thrust at a given altitude, the thrust for a corresponding power setting is calculated at sea level. The product of the ratio of propeller efficiencies and the function of density ratios read from the curve gives the correction factor to be applied to the sea level thrust to obtain the thrust at altitude. To determine the maximum hover altitude the gross weight is divided by the maximum sea level thrust; the propeller efficiency ratio is assumed equal to 1.0 and an altitude is read from the curve. The actual propeller efficiency ratio is then calculated and the altitude is again determined. The propeller efficiency does not change rapidly with altitude and the second altitude is normally very accurate.

PROPELLER TIP CLEARANCE

The effect of tip clearance on trust and power does not lend itself to calculation; therefore test data must be used to determine the magnitude of the losses. The test data of deference 5 has been replotted so as to reflect the variation of shroud thrust to horsepower with tip clearance to diameter ratio (Figure 6).

ACTIVITY FACTOR FOR DUCTED PROPELLERS

The thrust required to hover and the lift that must be maintained at forward speeds are dependent upon the gross weight. The loads acting on the duct have been given in equation form, and the weight can be estimated. Equations for the propeller thrust have also been given, but most propeller weight equations involve terms containing b and AF; therefore the ducted propeller has been analyzed to facilitate calculation of the quantity b x AF.

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	٨F	<u>- 2•4.31</u> D	$\frac{(10)^2 \operatorname{n} \operatorname{V_2}^2 (1 \cdot f) \operatorname{D}}{2\operatorname{C}_L \operatorname{V_T}^2 \operatorname{b}} \left[\frac{2 \cdot 59}{\left[1 \cdot \left(\frac{\operatorname{V_2}}{\operatorname{V_T}}\right)^2\right]^{\frac{1}{2}}} \right]$. 09	$\frac{1}{\cdot \left(\frac{V_2}{\nabla_T}\right)^2}$
	Ţ	+ pA5 V5	$\frac{2}{D} = \frac{1}{Q} = \frac{1}$		
	p i	A ₅ ¥ ₅ = ρ1	$V_2 V_2 = V_2^2 - \left(\frac{\Lambda_5 V_5}{\Lambda_2}\right)^2 = \frac{1}{\rho} V_D \left(\frac{\Lambda_5}{\Lambda_2}\right)^2$)2	
	b(A:	F) <u>135</u>	$\frac{5 \cdot (1 \cdot f) w_{D}}{C_{L} v_{T}^{2} \rho} \left(\frac{A_{5}}{A_{2}}\right)^{2} \left[\frac{2 \cdot 59}{\left[1 \cdot \left(\frac{V_{2}}{V_{T}}\right)^{2}\right]^{2}}\right]$		
		+ [.05	$\frac{1}{\frac{v_2}{v_T}^2}$		(8.01)

A typical curve obtained from Equation (.01) is shown on Figure 7.

CONTROL MOMENT

When a ducted propeller is placed in a flow field with the propeller axis parallel to the flow, the propeller thrust is acting along the axis, and the duct forces form a cone, the apex of which is on the propeller axis some distance above the duct lip. When the axis of the ducted propeller is at some angle with respect to the free stream. the propeller thrust continues to act along the axis of rotation, but the apex of the cone formed by the duct forces moves upstream. The apex of this cone will continue to move upstream until the angle between the propeller axis and free stream reaches 90 degrees; as the angle is increased, the apex of the cone will move back until it again lies on the axis of rotation of the propeller at 1°0 degrees. The platform maintains an equilibrium of forces by tilting the axis of rotation of the propeller into the free stream velocity and the center of aerodynamic forces is continually changing as the free stream velocity is increased. The center of gravity of the entire mass can be moved, within limits, by the operator while in flight. However, when the mass

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of the pilot is small compared to the total mass, the distance through which the total center of gravity can be moved diminishes, and insufficient control results. The duct produces approximately one hal? of the total lift; therefore, if the total lift remains constant, but the diameter of the duct is increased, the moment arm and thus the moment will increase and again insufficient control results. The necessity of additional control forces is obvious. Several methods have been considered and are included in this report.

The method used to calculate the performance of a ducted propeller outlined in Appendix II of this report has been superseded by this report. However, the differences are small and the description of the forces and moments are not affected. As indicated, the use of duct exit guide vanes for creating nose down pitching moments are not advisable, unless exceptionally large distances between the exit vanes and C.G. location are possible. The maximum moment obtainable from a means of propeller tip clearance control (see Appendix II) such as boundary layer removal at the blade tip, can quickly be estimated.

If the test data shown in Figure 6 of this report can be extrapolated, a tip clearance to diameter ratio of .005 will decrease the duct thrust 16.5 percent. The model 1031-A has a duct thrust of approximately 250 lbs.; therefore the loss due to this tip clearance is h1.3lbs. If it is assumed that the clearance is reduced to zero over one half the duct, an additional force of 20.6 lbs. would be created, and the moment arm would be approximately .7R = 1.75'. The maximum moment would be 36 ft-lbs. The propeller tip clearance should be kept at a minimum value to minimize losses, but any attempt to cause a cyclic variation in tip clearance to produce a control moment will be nonrewarding.

The third means of producing a control moment, discussed in Appendix II, and also in Appendix IX of this report, has to do with the control of the duct lip forces through the boundary layer. The natural circulation due to a differential lift would probably not reduce the moment to a large degree. If a powered system were used to direct the flow field, the moment would be significantly reduced and at the same time additional lift would be produced. This appears to be a promising means of reducing the moment to the point where kinesthetic control would be adequate.

An analysis has been presented. Appendix III of this report, which indicates promising values of moment obtained from duct inlet lip vanes. This information is believed to be misleading in that the forces calculated would be cancelled by opposite forces originating due o the

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interference between the lip and vane. The calculated thrust, assuming 100 percent inlet diffuser efficiency, snows very good agreement with test data. Therefore, additional inlet guide vanes cannot improve the performance of the inlet diffuser to a large extent, and the moment calculated must be in error.

A cyclic pitch change can be effected by changing the inflow direction. This means of producing a pitching moment was investigated, Appendix V of this report, and found copable of producing approximately one tenth of the required moment with essentially no loss in performance. It would be necessary to increase the propeller strength, but this type of system should show good reliability due to simplicity of the mechanism.

CONCLUSION

The maximum nose down pitching moment developed by the control of the discussed are of the order of all percent of the total hose up momental For this reason, it would appear that attempts to decrease the momental by changes in lip confiduration mucht be more reparding than attempts to overpower the nose up moment. The powered boundary layer would appear to have the greatest possibility of controlling the moment in that it can be used either to therease or decrease the moment by u raing on the shall quantity of air within the boundary layer, which is turn alters the online flow field.

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	2. "[] po	Oucted Coaxial ort No. 120.3,	L Propeller Blade Angle Settings", Hill , March, 1954.	er Re-
	3. "T -	ruck Test Sta Phase II", Hi	and Tests of Hiller Airborne Personnel Iller Report No. 6º0.2, September, 1955	Platform •
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The power required may be written in the form:

$$\mathbf{P}_{\mathbf{R}} = \frac{\rho \mathbf{A} \cdot \mathbf{V}_{5}^{3}}{\mathbf{1100} \eta_{\mathbf{P}}} \begin{bmatrix} 1 + \mathbf{f} - \left(\frac{\mathbf{V}_{0}}{\mathbf{V}_{5}}\right)^{2} \end{bmatrix} = \frac{\rho \mathbf{A} \cdot \mathbf{V}_{5}^{3}}{\mathbf{1100} \eta_{\mathbf{P}}} c_{\mathbf{h}}$$

Values of C_1 and V_5 at hover (V_5 obtained from the nomentum equation) were substituted as a cross check, yielding a value equal to the available power. To determine the range of V_5 , V_7 , and available horsepower, the assumed RPM was increased from 3800 to 3810. When the corresponding values were substituted, it was found that the power required decreased with increasing V₅. In this range, the term K = (V_0/V_5)² controls in spite of the fact that V₅ is cubed. This means that not even this small increase in available power can be absorbed, and this, in turn, shows that the horsepower and RPM are constant regardless of the value of U_5 in the operating range. Experimental data definitely confirms this.

The qualitative interpretation of these data is that, as forward speed increases, more and more thrust is shifted from the probabler to the duct. Figure 1 shows the prodicted decrease in power required; this curve appeared as the D/L = 0, 1 + f = 1.2 curve of Figure 2, Hiller deport No.56-108. During the truck tests, nowever, the power was not allowed to decrease. As should be expected, the probabler produced a V5 greater than that required for lift. In Figure 7 of Hiller deport 680.2 the lift curve for drag-thrust equilibrium reflects the decrease in power required for equilibrium, having the peak lift just short of the bucket of the power curve and decreasing to lift equilibrium again just short of required power equal to hover power.

The test data contain lift, thrust, and thrust equilibrium curves for full power. A curve of V5/VT versus V_0/V_5 has already been calculated. Now it is possible to draw a curve of V5 versus V_0 , since V_T is a constant for full power operation. This is done in Figure 2.

The forces on the platform may be found by momentum theory.

 $L = \rho A V_5^2 \cos \alpha$ $T = \rho A V_5 (V_5 \sin \alpha - V_0)$

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These curves are plotted in Figures 3 and 4. Experimental curves may be found in Figures 7 and 8, Hiller deport No. 680.2.

A thrust equilibrium curve may be drawn in two ways. First, the thrust equation may be equated to zero, reducing the condition of equilibrium to:

This curve is plotted in Figure 5. As a check, a cross plot of the intersection of each thrust curve with the V_{\odot} axis may be used. These points deviated by a small amount confirming the calculations. leading to the lift and thrust curves.

The condition described above does not constitute a true equilibrium since the vertical forces are not balanced. In fact, no such equilibrium is possible at full power except at a single V_0 already excluded by other limitation and, of course, at hover. Equilibrium can occur only along the (BEP) $\gamma/(BEP)$ g curve of Figure 1. It is more easily and directly done by simply equating forces. This curve also appears in Figure 5.

In order to check the propeller operation, it is necessary to compare the design and test values for V_5 , V_T , T, and P_R .

	Design	Test	Error
۷ ₅	112.7 ft./sec.	110.5 ft./sec.	
v ₅ V _T	$\frac{112.7}{707} = .1594$	$\frac{110.5}{675} = .163?$	2 70 2 • 10
ľ	483 1b.	500 lb.	3.5%

No direct and definite information as to either power available or power actually expended is available. However, the design estimation of power required left but a small margin from the maximum output of the engines. Therefore, since the expected V5 and T were obtained at full power, the estimation was reasonably good.

It is safe to conclude that the propeller was properly designed, for a slightly larger than predicted amount of power was absorbed producing the predicted thrust.

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Page 1

I. DISCUSSION:

Before the merits or disadvantages of a control system can be determined, it is necessary to understand how the basic forces produce lift and thrust. Figure 1 shows these forces in hovering and forward flight, and the accompanying diagrams illustrate how Hiller Report 120.5 is used to calculate the net force (F_G) and its direction. If this method is applied correctly, very good agreement between theory and test results are obtained. The assumptions essential to apply this theory to ducts at forward speed and angle of attack are:

1. The net force is in a direction opposite to the flow through the duct.

 The direction of the flow through the duct is the vector sum of the free stream velocity and a vector (X) parallel to the duct axis.

3. The magnitude of the vector (X) is the vector sum of the free stream velocity (V_{0}) and the duct exit velocity (V_{5}) .

Returning now to Figure 1, first, we must define the terms used.

- FG Net Aerodynamic Force
- F_C Control Force
- L (Vertical) Component of F
- T Horizontal Component of F
- Wg Gross Weight
- V Induced Velocity
- V_O Free Stream Velocity
- Vg Duct Exit Velocity
- P A Point on the Q of the Duct
- Ma Aerodynamic Moment
- M_C Control Moment
- a Duct Angle of Attack (Figure 16)
- ϕ (Angle of) Inclination of the Net Thrust (F_G)

 β Angle Between the Vectors X and V_r

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 $V_5 \downarrow X$ $W_G = F_G$

HOVER (C)

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FIGURE 1

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 (\mathcal{A})

Х

GUST

MAR P

ŴG

D+T

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I. DISCUSSION (Continued)

It will be noted from Figure 1, (c) and (d), that a platform hovering in still air subjected to a gust will develop a drag force in the direction of the gust and simultaneously a variation in lift along the duct lip, creating a moment H which rotates the duct and tips the vector $F_{0,2}$ because there is only a small translation ($V_0 = 0$) $\neq a$ and a force T + D is produced in the direction of the gust. The translation velocity is increased, but the moment M_ will not vanish until the translation velocity reaches the velocity of the gust. At this point Ma = 0, but there is no restoring moment. However, if the translation velocity exceeds the gust velocity a restoring moment will develop which will stabilise the platform approximately at the speed of the gust if sufficient time is allowed.

Now that the direction of the aerodynamic forces can be found, it is possible to see how a platform may be controlled by a shift in the center of gravity.





AFG

WG



 $L = F_6$

MA

WG

(d)

<u>v</u>



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W_G

(a)

L= FG

Pd

FIGURE 2

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Page 3

I. DISCUSSION (Continued)

Figure 2(a) shows a hovering platform; all forces are in equilibrium, and no moment exists. In Figure 2(b) the c.g. has suddenly been displaced, and a moment appears due to the shift in weight with no corresponding shift in lift. If this c.g. position is maintained, the velocity is increased, and the lift on the leading duct lip becomes sufficiently larger than that on the trailing edge to produce an aerodynamic moment equal to the weight moment. At this point, the thrust vector (F_0) is inclined at the angle \neq and $F_0 \sin \neq =$ drag. The entire system is in equilibrium, Figure 2(c). If the c.g. is returned to its original position, Figure 2(d), the aerodynamic moment restores the platform to the horisontal position, and \neq decreases to zero; thus the thrust (F_0) is again equal to the weight and equilibrium is again attained as in Figure 2(a).

Now let's examine the platform with exit vane control.



In Figure 3(a), the situation is the same as in Figure 2(a). In Figure 3(b), the operator has initiated a force intended to roll the machine clockwise, but in so doing he has created an unbalanced control force F_{C} , which starts to move the platform backward. If a constant control setting is maintained, the entire machine will rotate so that ϕ increases, and a component of thrust overcomes the control force and forward motion is initiated. Eventually, an equilibrium point will be found, Figure 3(c), where the control moment and aerodynamic moment are of equal magnitude but opposite in direction, and at the same time the control force and drag are equal and opposite to the thrust (T) and F₀ is still sufficient to maintain a lift force equal to the weight.

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I. DISCUSSION (Continued)

when the controls are returned to neutral, there is an aerodynamic moment tending to return the platform to the upright position, but the balance of the horizontal forces has been destroyed, and the thrust is greater than the drag, Figure 3(d), and the platform will accelerate. If the controls are maintained, the machine will begin to decrease its angle of attack. ϕ and consequently T will reduce, and again it will return to a balanced position, Figure 3(a).

If we examine Figure 3(c) in light of the test results of the present platform, we find that the control moment is very large. Hiller Heport 545.91 indicates an equilibrium at approximately 25 degree tilt angle and 30 knots forward speed. The moment that must be overcome is 380 foot-pounds. If we assume that the exit fins are located 3.8 feet below the c.g., FC, Figure 3(c) has a magnitude of 100 pounds. Now $T = F_C + D$ for equilibrium. This additional 100 pounds must come from FG; therefore the tilt angle must increase considerably as well as the magnitude of FG. Therefore, the forward speed for any tilt angle will decrease, and consequently the maximum forward speed will be reduced by a considerable amount.

The larger the distance between the c.g. and the control fin, the smaller F_C required to overcome the moment. For instance, if the distance between the c.g. and control fin were 10 feet, F_G would be 38 pounds or about twice as large as the drag force D.

In practice when the control force is applied and the machine commences to respond in the opposite direction, more control is applied and by this time the angular acceleration has produced sufficient tilt angle so that the norizontal component of FG, that is T, has become predominant and forward motion is increasing. The reaction is to decrease the vane deflection which increases $T-(F_C + D)$ and the forward acceleration increases. In brief, though not unstable, it is a difficult means of control.

II. METHODS OF CONTROL:

If spoilers are used to control the platform, a control force will be associated with a decrease in thrust. If suction is applied to the duct lip, a stable machine results with the opposite effect on required power as the spoiler; however, the tendency to follow a gust is not alleviated.

How, then, can a platform be controlled satisfactorily?

A plenum chamber connected to the duct lip and vented through the lip will reduce its natural stability as will be shown. Figure $\mu(a)$ shows the hovering duct.



II. METHODS OF CONTROL (Continued)

There is no flow because all portions of the duct are lifting uniformly. When the duct is subjected to a gust or forward flight, as in Figure 4(b), the velocity over the duct lip increases on the up stream side and decreases on the opposite side. A relatively high pressure will develop on the side with the low velocity, while reduced pressure will prevail on the upwind side. Thus a flow will be developed in the plenum chamber from the high to the low pressure side. The boundary layer will be forced into the plenum chamber on the side where the velocity is $V - V_0$ and the low energy air will be forced into the boundary layer on the opposite side. This will tend to neutralize the lift and moment; however, there will always be a restoring moment, which is less than the non-vented platform.

This, then, is not a means of control but rather a means of reducing the stability. The control force need not be as large with the vented lip, but exit vanes below the c.g. will still produce undesirable forces. Therefore, a spoiler or other means must be employed to produce the control force or moment. If vanes are desirable, they must be placed in a stream of high energy air, both in hovering and forward flight. Vanes placed above the c.g. in the inlet stream would produce both a favorable force and moment but would probably be ineffective in hover due to the low velocity. If vanes are placed in the vicinity of the duct lip, the vane on the down wind side can be used to produce additional lift and a desirable moment at low forward speeds. At high forward speeds the velocity over the down stream lip is insufficient to produce the necessary lift; therefore, a vane on the leading duct lip must produce the same moment and force change as spoilers. We find ourselves reverting to c.g. change or boundary layer control for the control force, if we do not wish to accept a means of reducing lift, such as, spoilers. The change in c.g. location is good, and with a vented lip should give adequate control. Boundary layer control with the vented lip should be adequate, but the vented lip is in reality a boundary layer control, and at high forward flight speeds where VO approaches V, suction on the rearward lip would become ineffective.

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II. METHODS OF CONTROL (Continued)



FIGURE 5

Figure 5(a) shows what is happening at the propeller tip. The higher pressure air at the down stream side flows over the blade tip, causing separation ahead of the propeller. Figure 5(b) shows possibilities of local control, which would cause a cyclic lift. The first method may not be possible, due to the bending of the blade, but, if possible, should result in a smaller quantity of air to be removed. The duct lip is an extremely handy source of low pressure, which could be used to supply the suction. This could be accomplished with only a small overall loss in thrust, because the duct lip thrust is reduced but the propeller thrust is increased.

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			APPENDIX III			
			PLATFORM CONTROL			
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	A. Morte	11/30/50	HILLER HELICOPTERS	PADE A-III-]
			Acrodynamics of Ducted Propellers	HOPEL 1-31-1
APPROVED			As Applied to the Platform Principle	-EPONT NO. 17-138
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PLATFORK CONTROL

Hemorandum (C) E-56-159

A. Introduction

An inlet guide vane control has been successed as a means of platform control. The vane would be located in the vicinity of the duct lip, either on the forward side, the rearward side, or both. If both fore and aft vanes are used, they would act in opposite directions; that is, the forward vane would cause a dacrease in lift on the forward duct lip and a negative vane lift, and the aft vane would increase the lift of the aft portion of the duct and produce a lifting force on the vane.

This a lysis is not intended to give absolute values, But Tan indication of the forces and the feasibility of such a means of control, either for gust stability or forward flight.

H. Hover Analysis

Tests were conducted to determine the velocity profile in a vertical direction above the doct lip. The test was run in ground effect with the duct exit approximately one foot above the paved surface. The velocities of tained were converted to dynamic prescure (1) and plotted against the distance above the lip in inches (n), Figure 1.

The variation of dynamic pre-sure along the surface of the duct is shown in Figure 2. The values of dynamic pre-sure for a tilt antile of 0° and forward velocity of 0 knots are probably quite accurate; however the values for a forward speed of 3° knots and a tilt angle of 30° are somewhat in error, due to the assumption that the total pressure is equal to the static pressure. In reality, the total pressure is clightly higher than static; howyer the velocities are probably of the general order of magnitude.

The test results are duct lip pressure below ambient pressure. This was assumed to $\cdot \cdot$ the same as static to total pressure in detoraining the values of dynamic pressure. Actually the total pressure on the aft lip is above arbient as evidenced by the fact that a pressure of one incu of water above ambient was measured at H = 0on the aft duct lip for the conditions of 3^{p} 'mots forward speed and a tilt angle of 30° .

Because it is a vertical force, that is, desired from the inlet guide vane, it is been assumed that the maximum chord is of the order of six inches. This assumption enables one to evaluate the

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		As A lined to the Platform Principle		io1-9

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The maximum Wane shord has been assumed as . I feet.

- $\mathbf{A} = \frac{\mathbf{n} \mathbf{D}}{300} (\Psi_{1} \Psi_{1})$
- $E = \frac{\mathbf{D}^{\prime} \circ \mathbf{n}}{2(50)} \left(\mathbf{\Psi}_{2} \mathbf{\Psi}_{1} \right) \circ \cup \left(\frac{\mathbf{\Psi}_{2} \mathbf{\Psi}_{1}}{2} \right)$

because the number of the state of the stat

$$\mathbf{L}_{\mathrm{TF},\mathrm{av}} = \frac{\mathbf{D}^{\mathrm{c}} \cdot \mathbf{\pi}}{\mathrm{Tr}_{\mathrm{TF}}} \cdot \mathbf{\Psi}_{\mathrm{D}} \cos\left(\frac{\mathbf{\Psi}_{\mathrm{D}}}{\mathrm{c}}\right).$$

and

$$\frac{11}{2} = -2223 \psi_2 = 222 \left(\frac{\psi_2}{2}\right)$$

Values of h/γ of the intervalues symplem are plotted afainst $2|\psi|$ in Figure 3.

An average value of q can satisfied from Figure 1 and 2. The average $q_{\rm H}$ for x between -2 and +4 is most 10 from Figure 2. Starting at a coff 5 cm Figure 1 and role qup to 2 inches above the light the average quite correct value (1) and role with 120° of arc covered by the correct value, then from figure 3. N/q = 11.3. The maximum moment evaluable is 9(11.5) = 101.7 ft.-1bs.

If one value is that thed on the franc end a dome of a mal size on the rear lip, the noment would be coproxit toly subst it.-The. or buicd the value of a single value.

C. Forwarn Flight Analysis

The accompanying states is the same as the corresponding one for the noverner analysis; herever q not varius with ψ . Assure that the variation is of the form:

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	A. Horse	11/30/-0	HILLER HELICOPTERS	P466	A-III-5
			Narrayr nes of Dictor Propelates	MODEL	10.51 - 2
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$\frac{1}{NY} = \frac{1 \cdot 25(1+0)}{1 \cdot 25(1+0)} \left[\frac{1}{1 \cdot 25} \left(\frac{1}{2} - \frac{1}{2} + \frac{1}{2$					
$\mathcal{A}^{(1)}$ $(\mathbf{A}^{(1)} + \mathbf{A}^{(1)})$					
	but area x moment arm = $\frac{(\pi D)}{(\pi D)} (\Psi_{\beta} - \Psi_{2}) \cos\left(\frac{-2}{2} + \frac{1}{2}\right)$				
		2			
	M = 0. 1.2	Cos	$\begin{pmatrix} \Psi_2 - \Psi_1 \\ \end{pmatrix}$ [1.1.396 ($\Psi_2 - \Psi_3$) · (Ψ_1	- 110	*:]
	* · · · · ·	č.			.Г.]
	N 1 1	2	/*··*		7
	iu <u>1.</u>	cos	$\left(\frac{2}{2}\right)\left[-2\pi\omega\left(\psi_2-\psi_1\right)-(\sin\psi_2)\right]$	- S.E.	¥1'
	• •		•		
	Arain, ass	unity the	vrstē extends en both sides of ∰t = 0 a	f the	
	leading du	ict edge: '	ne above ski reasion bindomes:		

Forward vane, D = 51

 $\frac{M}{q_{\rm H}} = 15.61 \cos \frac{\Psi_2}{2} = .02350 \Psi_2 + \sin \Psi_2$

Trailing lip vane

$$\frac{1}{3H} = 15.61 \cos \frac{100 - \Psi_1}{2} = .02395 (130 - \Psi_1) - \sin \Psi_1$$

Figure 4 indicates the magnitude of the commut available at forward speed. To find the moment proceed as in the previous example. Assuming the same location of the case, we have an average q of 9. From Figure 4, 120° of arc covered by the vane on the forward lip yields $M/q_{\rm H}$ = 30 and the moment will be M = 30 x 2 = 270 ft.-lbs. If an additional vane covering 120° of the aft lip is used, it will have M/q = 7.5. This will produce an additional moment of 7.5 x 9 = 67.5 ft.-lbs., making the schement required at a trib angle of 30° and 35 mots forward speed to be here ft.-lbs. It would, therefore, be been say for the pilot to supply approximately 100 ft.-lbs. In this condition the net force due to the vane would be approximately 12° 13 s. down on the forward lip and T1 Los. additional lift on the aft lip.

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	A. Korse	11/30/56	HILLER HELICOPTERS	PA01	AIV-1
C=66460			Aerodynamics of Ducted Propellers		1031 - A
			As Applied to the Platform Principle		но. 56-108
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APPENDIX IV

STABILITY AND CONTROL

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	J. Nichola	0476 11/30 55	HILLER HELICOPTERS	PADE A-IV-2
6×68460			Merodynamics of Ducted Propellers	MODEL 1031-A
APPROVED			As Applica to the Platform Principle	REPORT NO. 56-108

STABILITY AND CONTROL

Hemorandum, E-56-504

A. Introduction

One of the methods proposed for reducing the large pitchup moment on the platform in forward flight is BLC - venting and interconnecting the duct lips to equalize the pressures.

It is the considered opinion of the writer that this method will not work. The following qualitative analysis is offered in support of this opinion.

B. Analysis

Consider a "two dimensional" duct (i.e., a longitudinal cross section). Furthermore, consider the lip edges carried around to the trailing edge to complete the airfoil.



Figure 1

- AL

second The Accodynamics of Ducted Propeller As Applied to the Platform Principle		A. Morse	11/30/56	HILLER HELICOPTERS	PAGE A-IV-3
As Applied to the Platform Principle eccentre. So <u>CONFIDENTIAL</u> In hovering flight the air enters symmetrically over both "airfoils". i = 1 i = 1				Aerodynamics of Ducted Propeller	
$\begin{array}{c} \underline{\texttt{CONFIDENTIAL}}\\ \hline \\ $	APPROVED			As Applied to the Platform Principle	
Firure 2 Firure 2 Lift, L ₁ , equals lift, L ₂ , and if we consider that the lift is generated by a circulation about the two airfoils, we can see that the fan is generating the velocity and the circulation about both airfoils, but the circulation is in the <u>opposite</u> sense on each air- foil.					
Figure 3		Lift, L ₁ , generated the fan i airfoils, foil.	, equals lif i by a circu s generatin , but the ci	Figure 2 Figure 2 Tt, L ₂ , and if we consider that the life lation about the two airfoils, we can ag the velocity and the circulation about reculation is in the <u>opposite</u> sense on	It is see that but both each air-
r 1 Ø11re 5		Ν		Figure 2	Ϋ́ν
				Figure 3	

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PREPARED	J. Nichola	DATE 11/30/56	HILLER HELICOPTERS	PAGE A	-IV-5
			Aerodynamium of Ducted Propallers	MODEL	1031-4
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The circulation over the aft airfoil is in the OPPOSITE DIRECTION as that set up by the fan in hovering flight, and the circulation is now in the same sense as for the forward airfoil.



Figure 6

Now we see that the fan "bucks" the "normal" circulation buildup, or conversely the forward velocity "bucks" the circulation set of by the fan.

Now if we want to maintain the sympetrical lift over the two alc-foils, we must maintain the same sympetrical flow pattern as occurs in hovering.

Our moment would be eleminated if the flow pattern looken like Figure 7 felow rather than like Figure $\hat{\mu}_{\bullet}$

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PREPARED	J. Nichols	11/30/56	HILLER HELICOPTERS	PAGE A-IV-Y
GH ES KED			Aerodynamics of Ducted Propellers	MODEL 1931-A
			As Applied to the Platform Principle	аероятно. 56-10
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	a) Mi	thout BLC		
			Suction	
	b) If	suction is	s applied, the pressure does <u>not</u> decrea	850
	b) If ne	suction in ar the suct	s applied, the pressure does <u>not</u> decreation hole, thus:	8.5 0



In order to do what we propose, we have to put in a large amount of <u>power</u> to change the flow field.

If we bleed from the front hip, we will destroy the lift in the front without materially increasing the lift on the rear, and we will have to but more power into the platform. So we see we are still left with the conclusion that we will have to may a nor er price for moment control, IF WE CONSIDER EQUALIZING THE AUTIMTS BY flow alteration around the duct.

If, on the other hand, we reduce the power put into the "forward" air to keep L_1 constant as forward speed is increased, then we can put that power into the "aft" air to keep L_2 high.

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G======		1	Nen unun 118 alt Bartes Priveiri in	
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This power can be transferred in the first of sub-to-the bread wir by employing cysics block on the transferring the non-er trais wi<u>powered</u> PLC system for the respond the platform.

The former approach leads to the location of modic purch mechanisms, the latter approach to the location much mechanisms.

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		As Applied to the Platform Principle		на 56-108

APPENDIX V

PRELIMINARY AERODYNAMIC ANALYSIS

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		NO111.9	
	MODEL N	IO1031A	
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		INDEX	
			Page No.
	INTROL		1
	SUMMAR	ar	2
	I.	MOMENT APPLIED TO THE PROPELLER BY CHANGING THE INFLOW DIRECTION	3
	п.	ADDITIONAL MOMENT DUE TO INCHEASED INFLOW VELOCITY OVER THE DUCT LIP	10
	III.	CHANCE IN PROPELLER BLADE LIFT COEFFICIENT	14
	IV.	DECREASE IN HOVER PERFORMANCE DUE TO INSTALLATION OF PROPELLER INLET GUIDE VANES	17
	♥.	INCREASE IN PARASITE POWER DUE TO DEFLECTION OF PROPELLER INLET GUIDE VANES	2)

This is a preliminary issue of t report to be submitted in satisf of Contract Nonr-1357(00). The present content of this repo analysis of the radial inlet vaning moment.	ERODYNAMIC ANALYSIS	001-1031-4 19097
PRELIMINARY A CONFIDENTIAL INTRODUCTION This is a preliminary issue of t report to be submitted in satisf of Contract Nonr-1357(00). The present content of this repo analysis of the radial inlet vaning moment.	he final aerodynamic action of Phase III rt covers only the e control of pitch-	************
CONFIDENTIAL <u>INTRODUCTION</u> This is a preliminary issue of t report to be submitted in satisf of Contract Nonr-1357(00). The present content of this repo analysis of the radial inlet van- ing moment.	he final aerodynamic action of Phase III rt covers only the e control of pitch-	
INTRODUCTION This is a preliminary issue of t report to be submitted in satisf of Contract Nonr-1357(00). The present content of this repo analysis of the radial inlet van ing moment.	he final aerodynamic action of Phase III rt covers only the e control of pitch-	
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SUMMARY

It has been suggested that propeller inlet guide vanes, or stator vanes, be used to direct the induced velocity into or opposite from the direction of rotation of the propeller blade, and thus change the angle of attack and lift coefficient of the propeller. This will again change the inflow velocity and, in turn, the lift of the duct lip.

According to the analysis, an optimum configuration is reached when the area covered by the inlet guide vanes is a circular segment of approximately 160° on the front and another equal segment on the rear portion of the duct. If it is assumed that the propeller inlet guide vanes are capable of turning the flow through an angle of 25° , the moment from the propeller will be 20.6 ft.lbs, and the additional moment will be 67.6 ft.lbs, or a total of 88.3 ft.lbs. The thrust divided by brake horsepower in the hovering condition will be reduced by .156.

If the machine develops 475 lbs. of thrust with the consumption of 77 BHP without propeller inlet guide vanes, the addition of guide vanes would require an increase in horsepower to 79 BHP for the same performance. When the vanes are deflected to achieve 25° of turning, the maximum blade lift coefficient (assumed to occur at r/R = .5) will be increased by approximately 0.5. This increase in lift coefficient is associated with an increase in drag coefficient. The increase in brake horsepower required was calculated and found to be negligible.



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$$\Delta M = \frac{11.87 \sin 2\omega}{(2 + \cos \theta)^2} \left[1 + 2.013(2 + \cos \theta)^2 \right] (1 - .2475\cos \theta) (\cos \theta + 0.01 \, \text{mV}) \left(1 - \frac{\cos \theta}{\sin \Psi} \right)$$

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B fr pd ti or We th	ecause of in rom the equat oint is about his point and r tip losses are interes e tip radius	let losses tion does n t 7" above l assume th due to the $\Delta c_{1} = \frac{5.1}{3}$ ted in the we are to	and boundary la ot agree with the the blade tip. at there will be increase or de $73V_1 = \begin{bmatrix} 1 - \cos t \end{bmatrix}$ change in infi-	ayer effects, test data. The It will be no be no change in perease in inle $\pm \frac{V_1 \sin 2\epsilon}{2\Omega r}$	the V ₁ of ecessary n boundar et veloci from of ma lift luct lip,	tained test to use y layer ty. determina ximum bla coefficie	tion de
Asa	ume V ₁ = 1	$\Delta c_{L} = \frac{5.73}{\Omega r}$	$\frac{\mathbf{v}_1}{\mathbf{\Omega}} \begin{bmatrix} 1 - \cos \varepsilon \pm \frac{1}{2} \end{bmatrix}$	$\frac{V_1 \sin 2\varepsilon}{2\Omega r}$ and $R = 2$.	5 ft.		
	Ĺ	V ₁ = [(1 -	683 11.56 cos ± .1025	sin2) - 1			
The	duct lift L) = 1 PA,	where $\angle P = F$	P _T - P			
and	P _T = P	+ q					
	P _T - P	≖q≖∠P		¥5			r h
A =	πD(²⁰ / ₃₆₀)(b)(1	$) = \frac{\pi(75\theta)}{36}$	-=.06550	R			S
Mome	nt arm = $\left[(R + C_{R})^{2} \right]$	$+\frac{b}{2}+(R+\frac{b}{2})$)cos0]		+		
t A	$0 = 8^{"} = .75^{"}$	R = ;	2.51			/	
L.	· = •00558 (6	in degrees	s)			1	
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JUNI		42 ∆q 0(1+	cos0) = .0942 (0 in	degrees)
		∆q = p/2	$2 \Delta v_1^2 = 1.189 \Delta v_1^2 (10^{-3})$ Sea	Level
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		OATE		
-4-4460	A. Morse	6-15-56		15
HEGGED				MODEL 1031A
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		da =	$\frac{V_1}{\sigma r} = \begin{bmatrix} 1 - \frac{\cos \ell}{V} \end{bmatrix}$	
			$\left[\left(1 \pm \frac{1}{2r} \sin \ell\right) \right]$	
		dC,		
		da	= 5.73 $d\alpha \left(\frac{L}{d\alpha}\right) = dC_L$	
			-	
		dC.	$\frac{5.73V_1}{1} \begin{bmatrix} 1 & \frac{\cos \varepsilon}{2} \end{bmatrix}$	
			$\frac{\sqrt{1}}{1 \pm \frac{1}{\sqrt{2}}} \sin \varepsilon$	
		v ₁		
b	out	ST 6	ine << 1.0	
			5.73V J	
		.'. dC _L	$\frac{1}{2\pi} \left 1 - \cos \varepsilon \left(1 + \frac{1}{2\pi} \sin \varepsilon \right) \right $	
		dC.	$\frac{5.73V_1}{1-\cos t} = \frac{V_1}{\sin 2t}$	
		-T	$\Delta \mathbf{r}$ $\begin{bmatrix} 2 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix}$	
T b	he maximum ch out	nange in C _l	L will be at the radius where $V_1/\Omega r$ i	s a maximum;

 $v_1 = \frac{\Omega r}{\left(\frac{1}{C_L^{\sigma}} - 1\right)^{\nu_L}}$

$$\therefore \frac{v_1}{sr} = \frac{1}{\left(\frac{1}{C_L \sigma} \cdot \cdot 1\right)^2}$$

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HILLER HELICOPTERS PAGE 6-15-50 A. Morse 1c-----CHERGED 103 n PRELIMINARY AERODYNAMIC ANALYSIS * CPORT NO 114.9 CONFIDENTIAL At r/R = .5, C_L reaches a maximum value of $C_{L,5} = .76$. $\therefore \frac{v_1}{cr} = \frac{1}{\left(\frac{6.78}{C_r} - 1\right)^2} = \frac{1}{\left(\frac{8.92 - 1}{2.815}\right)^2} = \frac{1}{2.815} = .365$ $dC_{L} = 5.73(.365) \left(1 - \cos \varepsilon \pm \frac{.365}{2} \sin 2\varepsilon\right)$ $C_L + dC_L = 1.2_{max}$ and $dC_{L} = 1.2 - .76 = .44_{max}$.44 = 5.73(.365) $(1 - \cos \varepsilon \pm .1825 \sin 2\varepsilon)$.2105 = $(1 - \cos \epsilon \pm .1825 \sin 2\epsilon)$ -.7895 = -cose ± .1825 sin2 &



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The total vane area required can be found from the force produced.

$$F = \frac{\rho V_1^2 D^2 \sin z}{2} \left(\frac{\rho V_1 2 \Omega^2 \sin z}{2} \right)$$

$$F = L = \frac{C_L \rho V_1^2 A_s}{2}$$

 $\therefore A_{s} = \frac{D^{2} \sin \varepsilon}{C_{T}} \left(\theta - \frac{\sin 2\theta}{2} \right)$

but

This is the vane area required when the maximum C_L and $sin \varepsilon$ are used. To this the supporting strut will have to be added, which has a length of $LRsin\Theta$. If a chord length for the supporting strut of L/12 foot is assumed:

$$A_{s} = \frac{D^{2} \sin \varepsilon}{C_{L}} \left(0 - \frac{\sin 2\theta}{2}\right) + 1.333 \text{ R sin}\theta$$

$$\Delta \mathbf{f} = \frac{C_{\mathrm{D}}^{\mathrm{A}}}{\pi \mathrm{D}^{2}/\mathrm{L}} = \frac{C_{\mathrm{D}}^{\mathrm{A}}}{\pi \mathrm{R}^{2}}$$

$$\Delta \mathbf{f} = \frac{4C_{\mathrm{D}} \sin \varepsilon}{C_{\mathrm{L}} \pi} \left(\theta - \frac{\sin 2\theta}{2} \right) + \frac{1.333 C_{\mathrm{D}} \sin \theta}{\pi R}$$

$$\Delta \mathbf{f} = \frac{\mathbf{h} \mathbf{C}_{\mathrm{D}}}{\pi} \left[\frac{\sin \varepsilon}{\mathbf{C}_{\mathrm{L}}} \left(\mathbf{\theta} - \frac{\sin 2\mathbf{\theta}}{2} \right) + \frac{.334 \sin \theta}{\mathbf{R}} \right]$$
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•			1.92 n 2	peed.	
		^t P – W	$I_{\rm p} (1+f)^{\prime}$		
		¥ _D = -	$\frac{18 P_{o} P_{p} W_{p}}{T_{o} (1+f)}$		
		∴ l	$p = \frac{26.6 \eta_{p}}{(1+1)} \left(\frac{P_{o}}{T_{o} w_{D}} \right)^{\frac{1}{2}}$		
a	nd	∆2 _p = 2	26.0 $\eta_p \left(\frac{P_0}{T_0 M_D}\right)^{\frac{N}{2}} \left[\frac{1}{(1+f_2)} - \frac{1}{(1+f_1)}\right]$		
ď	ut	1+f ₁	= 1.05 and $(1 + f_2) = (1 + f_1 + \Delta)$	ſ)	
		∴ f ₁	and $f_2 << 1.0$		
		;p = 2	6.6 $\eta_p \left(\frac{P_o}{T_o W_D} \right)^2 \left[(1 - f_1 - \Delta f) - (1 - f_1) \right]^2$	f 1)]	
		∆ (_p = 2	$6.6 \eta_{p} \left(\frac{P_{o}}{T_{o}W_{D}} \right) (- \Delta f)$		
	$\Delta l_p = -2$	6.6 np 70	$\frac{\frac{1}{2}}{D} \frac{\mu C_{\rm D}}{\pi} \left[\frac{\sin \varepsilon}{C_{\rm L}} \left(\theta - \frac{\sin 2\theta}{2} \right) + \frac{.33\mu}{R} \right]$	sin0	

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		rhp •	$\frac{\sigma A_{F} \rho c_{D_0} v_T^3}{1100} \bigg] \kappa = \frac{\sigma A_{F} \rho v_T^3 \kappa c_{I}}{1100}$	<u>)</u> 0		
T 1	here is a chaift coefficie	ange in drag ent.	coefficient associated with t	he chan	ge in	
		c _{Do} = δ _o + δ	$5_2 a_r^2$ and $da_r = \frac{dC_L}{a} = \frac{dC_L}{5.7}$	3		
		c _{Do} = δ _o + -	$\frac{5}{32.85}$			
		drhp = -	$\frac{\delta_{\rm F} \rho V_{\rm T}^{3} K}{4400} \left(\frac{\delta_2 dC_{\rm L}^{2}}{32.85}\right)$		δ ₂ = .3	
		o drhp = -	$\frac{V_{\rm F} \rho V_{\rm T}^{3} \kappa}{4400}$ (.9125 x 10 ⁻² dC ² _L)			
Fr	om the deter	mination of	the blade lift coefficient -			
		dC _L =	$\frac{5.73 V_1}{\Omega r} \left[1 - \cos \varepsilon \frac{t}{2\Omega r} \frac{V_1}{2\Omega r} \sin 2\varepsilon \right]$			
			$\frac{5.73}{\left(\frac{1}{C_{L}\sigma}-1\right)}\left[1-\cos\varepsilon \pm \frac{1}{2\left(\frac{1}{C_{L}\sigma}-1\right)}\right]$	sin2 {		

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$$\frac{1}{2} \frac{1}{2} \frac{1}$$

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