

Engineering Experiment Station

University of Illinois

Technical Memorandum No. 5

CROSS-WIRE PROBE FOR HOT-WIRE ANENOMETER

by

J. E. Romano and H. F. Johnstone

Issued in Conjunction with the Final Report on the Program

"Mixing of Fluid Streams"

Contract No. N6-ori-071(11)

Office of Naval Research, Department of the Navy

Urbana, Illinois September 30, 1953

Distribution List

1. S 1523

Copies	Government Agencies	Cory No.
15	ONR, Washington, Attn: Fluid Mech. Br. (Sode 426)	1-15
ğ	Biological Dept., Camp Detrick, Attn: Dr. J. B. Bateman	16-23
1	ONR, Boston 10, Mass.	24
1	ONR, New York	25
2	ONR, Chicago	26-27
1 2 1 1	ONR, San Francisco	28
1	ONR, Pasadena	29
2	ONR, F.F.O. 100, New York	30-31
1	ONP, Washington, Attn: Mechanics Div. (Code 3800)	32
	BuAer, Washington, Attn: Capt. W.S. Diebl (AER-23)	33
1 3	BuOrd, Washington, Attn: Code Re9	34
3	Wright Air Dev. Sen., Dayton, Mr. L.S. Wasserman,	35-37
	Flight Res. Lab	
Ĵ	Air Res. and Dev. Command, Baltimore, Dr. T. Theodorsen	38
1	BuAer, Washington, Attn: Mr. J.S. Attizello	39
1	Director, David Taylor Mod. Basin, Washington, Attn:	40
	Dr. Brode	
1	Air Materiel Command, Dayton, Air Doc. Div. (MCIDXR)	μl
1	Ballistic Res. Lab., Aberdeen, Attn: Mr. R.H. Kent	42
1	Army Chemical Center, Attn: Dr. D. Machae	43
1	NACA, Washington	44
1	NACA, Langley Aero. Lab., Langley Air Force Base, Va.	45
1	NACA, Ames Aero. Lab., Moffett air Force Base, Salif.	46
ī	NACA, Lewis Flight Propulsion Lab., Cleveland	47
1 1	Dr. Francis H. Clauser, Johns Hopkins Univ., Baltimore	48
1	Dr. Arnold Kuethe, University of Michigan, Ann Arbor	49
1	Dr. Hans W. Lippmann, GAL. CIT, Pasadena	50
1	Dr. G.B. Schubauer, Nat'l Bur. of Stds., Washington	51
1	Dr. R. J. Seeger, NOL, Silver Spring, Md.	52

Universities and Research Organizations

1	Atlantic Res. Corp., Alexandria, Attn: Dr. A.C. Scurlock	53
1	Polytech. Inst. of Brooklyn, Prof. R.P. Harrington	54
1	GAL, CIT, Pasadene, Attn: Dr. C. B. Millikin	55
1	Jet Prop. Lab., Cal. Tech., Pasadena, Attn: Librarian	56
1	Univ. of Calif., Berkeley, Attn: Dr. R. G. Folsom	57
1	Cornell Aero. Lab., Buffalo, Attn: Dr. J. V. Foa	58
1	Cornell Univ., School of Aero. Eng., Ithaca, Dr. W.R. Sears	59
1	Cornell Univ., School of Aero. Eng., Dr. A. Kantrowitz	60
1	Univ. of Del., Chem. Eng. Dept., Newark, Attn: Dr. K. Wohl	61
1	Earvard Univ., Dept. App. Phys. Engr. Sci.,	62
	Attn: Prof. H. W. Emmons	
1	Univ. of Illinois, Attn: Dr. H. F. Johnstone	63
j .	Univ. of Illinois, Library	64
1	Univ. of Illinois, Eng. Library	65
1	Univ. of Iowa, Inst. Hydraulic Res., Attn: Dr. H. Rouse	66
1	Johns Hopkins Univ., Dept. Aero, Eng., Frof. S. Corrsin	67

· · · · ·

Distribution List (Cont'd)

Control of Lands

Mart

The state of the second second

Corte	8 Universities and Research Organizations	Copy No.
1	Applied Phys. Lab., Silver Apring, Attn:Supervisor, Tech. Repts.	68
1	Arthur D. Little Co., Attn: Dr. R. V. Kleinschmidt	69
1	MIT, Gas Turbine Lab., Attn: Prof. A. H. Shapiro	70
1	MIT, Guided Missiles Comm., Attn: Supervisor, Tech. Repts.	71
1	MIT, Aero. Eng. Dept., Attn: Dr. J. C. Hunsaker	72
1	MIT, Chem. Eng. Dept., Attn: Prof. G. C. Williams	73
1	MIT, Math. Dert., Attn: Dr. C. C. Lin	74
1	MIT, Mech. Eng. Dept., Attn: Prof. J. H. Keenan	75 76
1	Univ. of Mich., Dept. Aero. Eng., Attn: Prof. E.W. Conlon	76
1	Princeton Univ., Aero. Eng. Dept., Attn: Prof. L. Lees	77
l	Princeton Univ., Guge. Jet Prop. Lao., Attn: Prof. J.Y. Charyk	
1	Furdue Univ., Attn: Prof. M. J. Zucrow	79
1	Stanford Univ., Attn: Prof. P. A. Leighton	80
1	Univ. of Texas, Attn: Dr. M. J. Thompson	81
1	Univ. of Wichita, Aero. Eng. Dept., Attn: Mr. K. Razak	82
1	Appd. Phys. Lab., Silver Spring, Attr: Dr. F.N. Frenkiel	83
1	Purdue Univ., Dept. Chem., Met. Eng., Attn: Dr. E.W. Comings	84
1	Dr. T. Baron, Shell Devel. Co., Emeryville	85 86
1	Dr. A.E. Weller, Battelle Inst., Columbus	
1	Dr. H. C. Heu, Iowa Inst. of Hydraulic Res., Iowa City	87
1	Dr. S. I. Pai, Univ. of Maryland, College Fk.	88
1	Dr. Irvin Glassman, Guggenheim Lab., Princeton Univ.	89
1	Mr. Frank Ereith, Dept. Mech. Eng., Univ. of Cal., Berkeley	90
1	Nat. Res. Corp., Cambridge, Attn: Librarian	91
1	Mr. G. J. Maslach, Dept. Mech. Eng., Univ. Cal., Berkeley	92
1	Prof. R. W. McCloy, Univ. of Ill., Dept. Aero. Eng.	93
1	Prof. Paul Torda, Univ. of Ill., Dept. Aero. Eng.	94
1	Prof. Stillwell, Univ. of Ill., Dept. Aero. Eng.	95 96
1	Prof. H. H. Korst, Univ. of Ill., Dept. Mech. Eng.	96
1	Mr. S. F. Gilman, Univ. of Ill., Dept. Mech. Eng.	97
1	James Forrestal Res. Center, Princeton Univ., Attn: Librarian	98
1 1	Dr. Arnold Kivnick, Penn. Salt Mfg. Co., Philadelphia	99 100
T	Dr. L. G. Alexander, Sak Ridge, Tennessee	100

~

CROSS-WIRE PROBE FOR HOT-WIRL ANEMOMETER

J. E. Romano and H. F. Johnstone

An improved cross-wire probe for the study of turbulence in gas streams is described. It consists of two single-wire probes clamped together. The wires are oriented with the aid of a microscope and a haemocytometer in order to reduce the error due to the deviation of the wire angles. A method is presented for equalizing the time constants of the wires to reduce errors in compensation.

Introduction

Among the quantities which are of interest in studying the characteristics of turbulent flow are the intensities of the longitudinal and transverse components of the velocity fluctuations, the turbulent shear stress, and the uv correlation coefficient. Let u and v be the longitudinal and transverse components of the velocity fluctuations, respectively; ρ the density of the fluid; the primes refer to r. m. s. values and bars refer to time average values. Then the shear stress and the uv correlation coefficient are defined, respectively, by

$$T = -\rho \, \overline{uv} \tag{1}$$

and

$$K_{uv} = \frac{\overline{uv}}{u^{v}v^{t}} \qquad (2)$$

The three quantities u', v', and uv can be measured with the hot-wire snemometer using a cross-wire probe placed in the fluid stream. The relations between these quantities and the response of the cross-wire probe are given by Schubauer and Klebanoff¹. The fluctuating components of the voltages across the two ¹Schubauer, G. B., and Klebanoff, P. S., A. C. R. No. 5K27, N. A. C. A. (1927).

wires for a constant-current hot-wire anemometer are given by

$$- \mathbf{o}_1 = \mathbf{\delta}_1 \frac{\mathbf{u}}{\mathbf{v}} + \mathbf{\epsilon}_1 \frac{\mathbf{v}}{\mathbf{v}}$$
(3)

(4)

(6)

and

The sensitivities of the wires to velocity fluctuations are

 $E = 3 \cot \Phi$

 $- \theta_2 = S_2 \frac{u}{u} - \epsilon_2 \frac{u}{u}$

$$\delta = \frac{\left(\overline{R} - R_{a}\right)^{2}}{2IR_{a}} F\overline{U}^{\frac{1}{2}}$$
(5)

and

The subscripts 1 and 2 refer to wires 1 and 2, respectively; \overline{U} is the mean velocity, R the resistance of the wire at the wire temperature, R_g the resistance of the wire at the air temperature, I the current through the wire, and \bigoplus the angle between the wire and the axis of flow. F is the calibration coefficient in the equation

$$\frac{I^2 \overline{R}}{\overline{R} - R_a} = A + \overline{FU}^{\frac{1}{2}}$$
(7)

A is an empirically determined constant for the wire. Sources of Error

In developing the relations between the three turbulent quantities and the velocity fluctuations as given by Equations 3 and 4, Schubauer and Klebanoff¹ assumed that $S_1 = S_2$, $\varphi_1 = \varphi_2 = 45^\circ$, and that the attenuation in wire response due to the time constant of the wire, which is a measure of the lag of the wire to the fluctuating velocity signal, has been properly compensated. Kunstman² has shown that, elthough the sensitivies of the two wires ²Kunstman, R. W., Ph.D. Thesis in Chemical Engineering, University of Illinois (1952). are calculated from the following equations

$$\frac{u'}{\overline{u}} = \frac{(-e_1 - e_2)'}{S_1 + S_2} - \frac{(S_1 - S_2)}{(S_1 + S_2)} \frac{(-e_1 + e_2)'}{(S_1 + S_2)}$$
(8)
$$\frac{v'}{\overline{u}} = \frac{(-e_1 + e_2)'}{S_1 + S_2} - \frac{(S_1 - S_2)}{(S_1 + S_2)} \frac{(-e_1 - e_2)'}{(S_1 + S_2)}$$
(9)
$$\overline{u} = \frac{(-e_1 + e_2)'}{S_1 + S_2} - \frac{(-e_2 - S_2)}{(S_1 + S_2)} \frac{(-e_1 - e_2)'}{(S_1 + S_2)}$$
(9)

$$\frac{uv}{v^2} = \frac{1}{4} \left(\frac{-e_1}{\zeta_1} - \frac{1}{4} \left(\frac{-e_2}{\zeta_2} \right)^2 \right)$$
(10)

The error in \in caused by deviations of ϕ from 45°, however, may be considerable

Table I

Errors in Wire Sensitivity E caused by

Deviations of Φ from 45°

φ	Per Cent Error	¢	Per Cent Error
<u>40</u>	+ 16.1	46	- 3.6
41	+ 13.1	47	- 7.2
42	+ 10.1	48	-11,1
43	+ 6.8	49	-15.0
կկ	+ 3.4	50	-19.2

as shown in Table I.

Appreciable error will sloo result if the time constants of the wires are not equal. Dryden and Kuethe³ have shown that the actual value of the ³Dryden, H. T., and Kuethe, A. M., T. R. <u>320</u>, N. A. C. A. (1929). functuating voltage of an anemometer wire is lower in amplitude than predicted by Equations 3 and 4 because of the slow response of the wire resulting from its mass. The ratio of the actual r. m. s. voltage to that for a wire with zero mass is given by

.

$$\frac{\frac{e_{a}}{e_{t}}}{e_{t}} = \frac{1}{\sqrt{1 + 4\pi r^{2}M^{2}}}$$
(11)

Here, N is the time constant of the wire, and f is the frequency of the fluctuating velocity being measured. To compensate for this attenuation, a circuit may be introduced in the hot-wire anemometer with the inverse characteristics of the right hand side of Equation 11. Since the attenuation depends on the frequency, a signal sent to the wire containing many frequencies (e.g., a square wave signal) will be distorted. The compensator is adjusted until such a signal remains undistorted. If the response of the two wires must be measured simultaneously, i.e., when measuring the sums or differences of the instanteneous voltages of the two wires, the time constants of both wires must be the same since the compensator must compensate for the attenuation of both wires simultaneously.

- 4 -

Adjustment of Wire Angles

Deviations from the assumed condition $\phi_1 = \phi_2 = 45^\circ$ arise from two sources: (1) the deviation of the angle between the two wires from 90° when constructing the cross-wire probe, and (2) the error in alignment of the probe axis with the axis of flow. Because of the difficulty of accurately controlling the angle between the wire and the axis of the wire holder during the construction of a probe, a cross-wire probe with both wires fixed on one holder does not lend itself to accurate control of the wire angles. A system of two singlewire probes is more flexible.

The properties of the wire and supports for each single-wire probe were chosen from a consideration of a balance of their limiting characteristics as discussed by Zignen⁴. The probe wire used was 0,000139 inch diameter ¹¹Zignen, B. G. van der Hegge, Applied Sci. Res. A2, 351 (1951). tungsten, and the wire supports were No. 12 nickel plated Boye embroidery needles spaced 1/16 inch apart. The wire was soldered to the supports at approximately 45° to the probe axis by means of a jig, and cleaned with hot benzene to remove excess flux. If any forsign perticles were detected on the wire under a binocular microscope, which could not be removed with repeated washings with hot benzene or with blasts of air, the wire was removed and the construction was repeated with a new wire.

The two single-wire probes were put together to form a cross-wire probe and held firmly by means of clamps as shown in Figure I. The clamps were first fastened loosely and the top probe adjusted until the wires were at exactly 90° to each other with their midpoints in a line perpendicular to the horizontel. A binocular microscope and a heemocytometer were used to obtain the correct orientation as shown in Figure 2. The clamp screws were tightened and the distance between the wires observed with a second microscope. This distance could be adjusted with peper shims between the clamps. The error in orientation of a wire with another wire could thus be reduced to less than $\pm 0.5^{\circ}$. This was possible because the diameter of the wire and the thickness of the cross-hetches on the haemocytemeter were comparable in size, and because the length-to-diameter ratio of the wire was 635.

In order to reduce the error in alignment of the probe exis with the exis of flow, the binocular microscope and the haemocytometer were also used to orient the cross-wire probe in the gas stream. The grid lines on the haemocytometer were

- 5 -



TOP HALF OF CROSS-WIRE PROBE



BOTTOM HALF OF CROSS-WIRE PROBE

FIGURE I. CROSS-WIRE PROBE



FIGURE 2. ASSEMBLY OF CROSS-WIRE PROBE

first fixed at 45° to the axis of flow by bringing the face of the haemocytemeter in line with a jig (Figure 3), which had been adjusted to 45° with the axis of flow. The binocular microscope was then used to orient the wires to coincide with the grid lines on the haemocytometer.

Equalization of Wire Time Constants

Corrsin⁵ has shown that the time constant for a wire is given by ⁵Corrsin, S., T. N. <u>1864</u>, N. A. C. A. (1949).

$$M = \frac{4.2ms}{I^2} \frac{(\bar{R} - R_a)}{R_a R_o} = \frac{4.2ms}{R_a R_o} P$$
(12)

where R_0 is the resistance of the wire at $0^{\circ}C_{\circ}$, m the mass of the wire, s its specific heat, and the other variables are as defined previously. For a given wire, the only terms in Equation 12 that can be veried in order to adjust M to a predetermined value (i.e., to match the value of 3 for a second wire) are contained in the term P, viz., the current I and the heat transfer potential $(\overline{R} - R_p)$.

Figure 4 shows the observed variation of the parameter P with the wire temperature for one of the single-wire probes studied. The data indicate that a change of wire temperature of 120°C. produces approximately a thirty purcent change in the parameter, and, therefore, a thirty percent change in the wire time constant. Thus, by varying the current through one of the two wires, the time constant of this wire can be adjusted to match the time constant of the other wire.

The exact procedure for determining the correct compensator setting for









FIGURE 4. VARIATION OF TIME CONSTANT PARAMETER P WITH WIRE TEMPERATURE both wires is as follows. A square wave signal is first sent to one of the two wires. The temperature of this wire is then set equal to the temperature used in obtaining the calibration coefficients of this wire (see Equation 7). This is accomplished by adjusting a direct current through the wire until the wire attains a resistance, $\overline{R_1}$, corresponding to the calibration temperature. The compensator is then adjusted until the square wave signal is no longer distorted. Maintaining the compensator at this setting, the square wave signal is then sent to the second wire and the direct current through the second wire is adjusted until the signal is no longer distorted. The resistance of the second wire under these conditions, $\overline{R_2}$, is then measured. For the given flow conditions, if the first wire is operated at $\overline{R_1}$ and the second wire experted at $\overline{R_2}$, the two wires will have the same time constant and a single setting of the compensator will correctly compensate for the attenuation by each wire when measuring the response of the two wires simultaneously.

The temperature at which the first wire is operated for turbulence measurements is the temperature at which it was calibrated. Since the current through the second wire is adjusted until its time constant equals that of the first wire, this wire will be operated at a temperature different from that used for its calibration. This will affect the value of the calibration coefficient in Equation 7, and, consequently, the wire constituity as defined in Equation 5. A relationship between the calibration coefficient and the wire temperature is required. In order to find this relationship, several probes were calibrated separately at different wire temperatures as shown in Figure 5. The observed values of F_2/F_1 are given in Table II.

- 7 -



FIGURE 5. VARIATION OF CALIBRATION COEFFICIENT F WITH WIRE TEMPERATURE

Table II

Reference wire temperature = 150° C.				
Probe	tw °C.	(T ₁ /T ₂) ¹ /2	F ₂ /F ₁ Observed	
A	200	0.963	0.971	
	230	0.950	0.955	
	260	0.932	0.941	
B	200	0.963	0.964	
	230	0.950	0.944	
	260	0.932	0.923	
C	200	0.963	0.970	
	230	0.950	0.954	
	260	0.932	0.937	

Effect of Wire Temperature on Calibration Coefficient F

The simple equation

$$\frac{F_2}{F_1} = \left(\frac{T_1}{T_2}\right)^{\frac{1}{2}}$$
(13)

represents the effect of the temperature on F within one percent. Here, T denotes the arithmetic everage of the wire temperature and the air temperature in O K. The new value of the calibration coefficient F resulting from a change in its temperature can be determined with this equation. Thus, the time constant of two wires can be equalized by adjusting the current through one of the wires until a single setting on the compensator suffices.

This report has been submitted for publication in <u>Review of Scientific</u> Instruments.