

Numerical Investigation of Relative Contributions of R_g Scattering and Incomplete Dissipation to L_g Excitation¹

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Abstract

Numerous mechanisms have been proposed over the years to explain how the regional L_g phase can be generated by nuclear explosions. Commonly quoted mechanisms include trapped pS phase, non-geometrical S^* , spall, multiple reflections of initial P rays, anisotropy, and various near-source, near-surface scattering processes. Recent observational studies (*e.g.*, Patton and Taylor, 1995) indicate that R_g plays an important role in L_g excitation for Yucca Flat explosions. Numerical experiments by Jih and McLaughlin (1995) readily demonstrate that rough topography and random heterogeneity can scatter significant R_g energy into body waves. In this study, an additional R_g -to- L_g conversion mechanism is presented and the relative effectiveness and importance of all three R_g -related mechanisms are examined.

It might be anticipated intuitively that the net effect of anelasticity in the surface layers is solely to reduce the amplitude of incident seismic waves. R_g wave is particularly susceptible to such a mechanism since it is confined in the uppermost crustal layers. If the anelastic attenuating layer is only thick enough to dissipate the retrograde rolling near the surface, then the free surface would behave asymptotically like a fixed point. Beyond certain distance, the fundamental mode can no longer be sustained by such a waveguide, and accordingly any undissipated R_g energy would have to propagate in other wave types or modes. Linear finite-difference calculations show that this process couples the undissipated R_g energy into pure shear waves or higher modes, depending on the complexity of the structure. In terms of R_g -to- S to R_g -to- P ratio, this process appears to be more efficient than other near-surface R_g scattering mechanisms. Furthermore, in this process, the R_g spectrum is naturally imprinted onto the converted S waves, which could help to explain some recently observed spectral characteristics of L_g waves.

For models embedded with shallow random heterogeneity, the RMS velocity fluctuation correlates very well with the R_g transmission coefficient. For 1 Hz R_g , a 2%–5% variation in the velocity leads to an equivalent spatial Q value of several hundreds or larger, regardless which of the three commonly used random media is embedded. Rough topography typically results in a Q value ranging from 10 to 100, which is approximately equivalent to a random medium with a 10% (or larger) velocity variation. Incomplete dissipation of R_g waves produces a very simple wave field, with almost all of the undissipated energy continues to propagate laterally towards the forward, and hence postcritical, directions. On the other hand, the scattering by shallow heterogeneity or rough topography would generate a rather complicated wave field, with a significant fraction of the scattered energy going downward steeply. Whichever of the three mechanisms is invoked, the S waves converted from R_g always dominate the whole scattered field. The uppermost crust is highly heterogeneous, and in many places very attenuative and hilly as well. All of the three R_g -related mechanisms should therefore contribute to L_g and coda excitation.

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Project Objective

The long-term objective of this project is to improve the fundamental understanding of seismic wave excitation and propagation. The full potential of linear finite-difference [LFD] method and other techniques shall be exploited in modeling various seismological problems directly related to a CTBT monitoring.

Research Accomplished

The first task of this project is to improve the capability of modeling L_g , R_g , P_n , P_g , and S_n in complex geological / geophysical environments, using LFD or hybrid modeling tools. Following the LFD implementation of a pure L_g wave packet (Jih, 1994), which is an ideal tool for investigating certain wave propagation phenomena (such as L_g blockage), our research effort under this project has been re-directed to several subtasks:

- [1] Use synthetic waveforms as an analysis aid to improve the phase-identification capability.²
- [2] Explore the physical basis of high-frequency shear wave excitation in the vicinity of explosions due to cracking or pre-existing cracks.³
- [3] Continue to investigate mechanisms responsible for explosion L_g excitation.

This paper summarizes our results obtained to date under subtask [3], with emphasis placed on topics related to R_g . A new R_g -to- L_g conversion mechanism is presented, and the relative effectiveness and importance of all three R_g -related mechanisms are reviewed.

Numerous mechanisms have been proposed over the years to explain how the regional L_g phase can be generated by nuclear explosions. Commonly quoted mechanisms include trapped pS phase, non-geometrical S^* , spall, multiple reflections of initial P rays, anisotropy, and various near-source, near-surface scattering processes. Recent observational studies (e.g., Patton and Taylor, 1995) indicate that R_g plays an important role in L_g excitation for Yucca Flat explosions. Numerical studies conducted at Teledyne Geotech and Phillips Laboratory (e.g., McLaughlin and Jih, 1986, 1987; Jih, 1993ac, 1994) readily demonstrate that rough topography and random heterogeneity can scatter significant R_g energy into body waves. However, in several cases only a fraction of the scattered energy would be favorably trapped in the crust as L_g or L_g coda, with more scattered energy lost to steeply going directions. In reality some additional R_g -to- S mechanisms may have contributed to the observed L_g signal as well.

It might be anticipated intuitively that the net effect of anelasticity in the surface layers is solely to reduce the amplitude of incident seismic waves. R_g wave is particularly susceptible to such a mechanism since it is confined in the uppermost crustal layers. If the anelastic attenuating layer is only thick enough to dissipate the retrograde rolling near the surface, then the free surface would behave asymptotically like a fixed point. Beyond certain distance, the fundamental mode can no longer be sustained by such a waveguide, and accordingly any undissipated R_g energy would have to propagate in other wave types or modes. Linear finite-difference calculations show that this process couples the undissipated R_g energy into pure shear waves or higher modes, depends on the complexity of the structure (Figure 1). In terms of R_g -to- S to R_g -to- P ratio, this process appears to be far more efficient than other near-surface R_g scattering mechanisms (Figure 5). Furthermore, in this process, the R_g spectrum is

² See Kadinsky, Jih, Dainty, and Cipar (1995) of this issue.

³ In progress with collaboration from A. Dainty and R. Blandford.

naturally imprinted onto the converted S waves, which could help to explain some recently observed spectral characteristics of L_g waves. Figure 2 compares the propagation of R_g waves incident upon an elastic and an attenuative basin models with identical velocity structures. Both the wave field snapshots (Figure 2) and the synthetic seismograms (Figure 3) clearly illustrate that R_g -to- L_g conversion can be enhanced if the sedimentary rocks are shallow and strongly attenuative.

For the R_g waves, rough topography could still be the strongest means of scattering (Jih, 1993abc). Scattering by random heterogeneity in the upper crust (*cf.* McLaughlin and Jih, 1987, and Jih, 1993b), is important in that random variations of velocity are virtually present in any type of crustal structure. McLaughlin and Jih (1987) made a comparison with Greenfield's (1971) P-coda observations (at teleseismic distance), and it was concluded that self-similar or Gaussian models with RMS velocity fluctuation between 7% and 15% in the uppermost 3 km of the crust can produce the observed P-coda/P power levels reported in Greenfield (1971). With the emphases of treaty-monitoring seismic research shifted to regional phases, R_g scattering by shallow random heterogeneity needs to be re-examined in order to evaluate its importance and efficiency, with respect to other mechanisms, in exciting L_g waves from explosions. In this study, a suite of forty five models embedded with shallow self-similar heterogeneous layer of varying randomness and thickness have been tested with LFD. Table 1 summarizes the propagation statistics we measured. Within 15% of velocity variation, the transmission, reflection, and the scattering loss all exhibit a linear relationship with the RMS velocity fluctuation. Models with thicker heterogeneities certainly associated with a stronger scattering and reflection, as well as a weaker transmission, as expected. However, the thickness appears to be less relevant than the RMS velocity variation (See Figure 4), primarily because R_g scattering in the top 1 km is more important. These observations are also valid for random media with Gaussian or exponential correlations (see Frankel and Clayton, 1986, for the definitions of various random models).

Conclusions and Recommendations

There are at least three R_g -to-SV(L_g) mechanisms: [A] scattering by shallow, random heterogeneity, [B] scattering by rough surface topography, and [C] incomplete dissipation by anelastic attenuation. Under this project, forward modeling is used to gain a better understanding of these three mechanisms. It is shown that, through extensive LFD modeling, each of these mechanisms can contribute to L_g and coda waves from explosions. In terms of $R_g \rightarrow S$ / $R_g \rightarrow P$ power ratio, [C] is the most efficient one, followed by [B] and then [A]. R_g -to-S conversion systematically dominates the scattered wave field. In terms of equivalent spatial Q 's, rough surface topography typically corresponds to a Q_0 in the range between 10 and 100 (Jih, 1993c), which is approximately equivalent to a self-similar random medium with 10% (or larger) RMS variation in the velocity. An RMS velocity fluctuation between 5% and 10% would correspond to a Q_0 value between 100 and 450 (Table 1). Stable shield regions have been reported to have an RMS velocity fluctuation less than 5%, which would yield a Q_0 larger than a few hundreds, regardless which type of random heterogeneity is considered. For all three types of random media that are commonly used in numerical studies with RMS velocity variation below 15%, all four measurable R_g propagation statistics correlate extremely well with the RMS velocity fluctuation. Incomplete dissipation of R_g waves produces a very simple wave field, with almost all of the undissipated energy continues to propagate laterally towards the forward, and hence postcritical, directions. On the other hand, the scattering by shallow heterogeneity or rough topography would generate a rather complicated wave field, with a significant fraction of the scattered energy going downward steeply.

An accurate prediction of the regional phases in areas of high proliferation concern requires a decent understanding of the attenuation/scattering mechanisms along the propagation paths. Synthetic seismograms are particularly useful for regions where earthquake or explosion data are not available. 2D numerical experiments, as described herein and in our previous studies, demonstrate that R_g can be a significant contributor to the formation of L_g and coda waves, in support of several observational studies. It would seem reasonable that, as 3D structure is taken into account, R_g 's possible role in L_g excitation would only become more important. On a long term, however, extending 2D modeling capability to 3D is definitely useful, as it would add an extra level of realism and complexity to the earth's structures that we need to model. In particular, in order to quantify 3D effects of surface topographic irregularities, the operational 2D formulations of Neumann boundary conditions (Jih *et al.*, 1988) need to be expanded to a 3D version.

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Table 1. Transmission/Reflection/Scattering Statistics of Self-Similar Models					
Model	T(1Hz)	R(1Hz)	1-T-R	Q(1Hz)	γ
1km, 2%	0.99	0.01	0.01	10172	0.000
2km, 2%	0.98	0.01	0.01	8018	0.000
5km, 2%	0.98	0.01	0.01	6710	0.000
10km, 2%	0.98	0.01	0.01	6179	0.000
1km, 3%	0.96	0.02	0.03	2000	0.001
2km, 3%	0.95	0.02	0.03	1788	0.001
5km, 3%	0.95	0.02	0.04	1646	0.001
1km, 4%	0.92	0.03	0.06	931	0.001
1km, 5%	0.86	0.04	0.10	548	0.002
2km, 5%	0.85	0.04	0.11	502	0.002
5km, 5%	0.84	0.04	0.12	473	0.002
10km, 5%	0.84	0.04	0.12	457	0.002
15km, 5%	0.83	0.04	0.12	451	0.002
1km, 6%	0.80	0.06	0.14	363	0.003
1km, 7%	0.73	0.07	0.20	258	0.004
1km, 8%	0.66	0.09	0.25	192	0.005
1km, 9%	0.58	0.10	0.31	147	0.007
1km, 10%	0.51	0.12	0.38	116	0.009
2km, 10%	0.47	0.11	0.42	105	0.009
5km, 10%	0.45	0.11	0.44	99	0.010
10km, 10%	0.45	0.11	0.44	99	0.010
15km, 10%	0.45	0.11	0.44	98	0.010
1km, 11%	0.43	0.13	0.44	92	0.011
1km, 12%	0.35	0.14	0.50	75	0.013
1km, 13%	0.28	0.16	0.56	61	0.016
1km, 14%	0.22	0.17	0.61	51	0.020
1km, 15%	0.16	0.18	0.66	42	0.024
2km, 15%	0.13	0.17	0.71	37	0.027
5km, 15%	0.12	0.17	0.72	36	0.028
10km, 15%	0.13	0.16	0.71	38	0.026
15km, 15%	0.13	0.16	0.71	38	0.026
1km, 16%	0.11	0.19	0.70	35	0.028
1km, 17%	0.08	0.20	0.72	30	0.034
1km, 18%	0.05	0.21	0.74	25	0.040
1km, 19%	0.03	0.22	0.76	21	0.048
1km, 20%	0.01	0.22	0.76	17	0.058
2km, 20%	0.01	0.23	0.76	15	0.066
5km, 20%	0.01	0.23	0.77	14	0.069
10km, 20%	0.01	0.23	0.76	15	0.066
15km, 20%	0.01	0.24	0.75	17	0.060
1km, 21%	0.01	0.23	0.77	14	0.070
1km, 22%	0.00	0.23	0.76	12	0.081
1km, 23%	0.00	0.24	0.76	11	0.088
1km, 24%	0.00	0.24	0.76	11	0.091
1km, 25%	0.00	0.24	0.76	10	0.097

T: transmitted power, R: reflected power, 1-T-R: scattering loss, γ : attenuation coefficient.

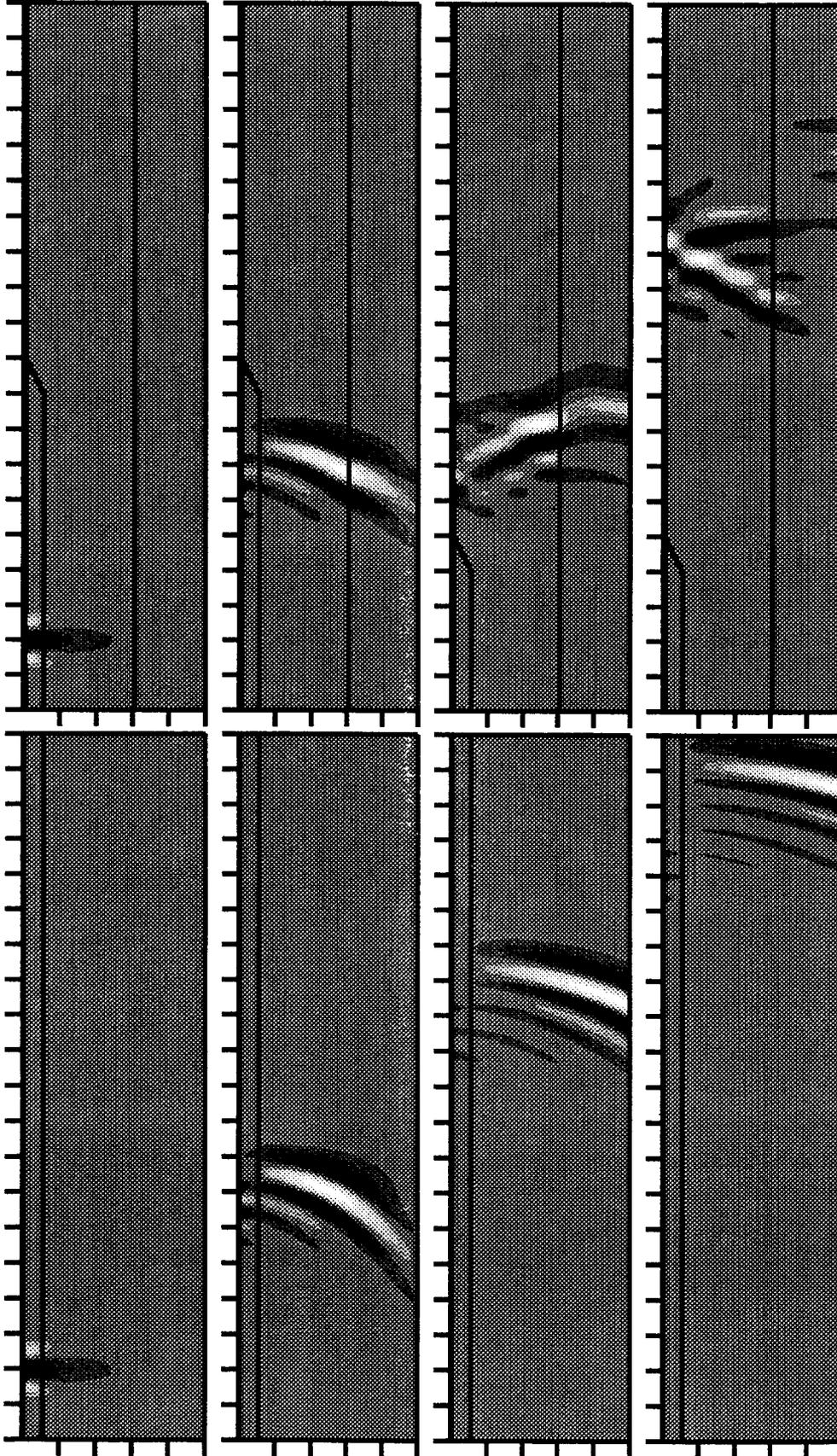


Figure 1. Snapshots of vertical wavefield of planar R_g incident upon simple attenuative structures. In the case of an elastic half space overlain by a strong, shallow attenuative layer (left), the retrograde rolling near the surface is dissipated after certain distance. With the free surface behaves asymptotically like a fixed point, this waveguide could no longer support the fundamental mode. As a result, most of the undissipated R_g energy is forced to propagate (in the forward direction) as shear waves. As the structure becomes more complex, the converted shear waves can easily couple into higher modes and contribute to L_g and L_g coda. Shown on the right is a model with a terminating attenuative layer on the top. Adding an extra layer (of higher velocity) to the model helps to trap the converted shear waves in the waveguide.

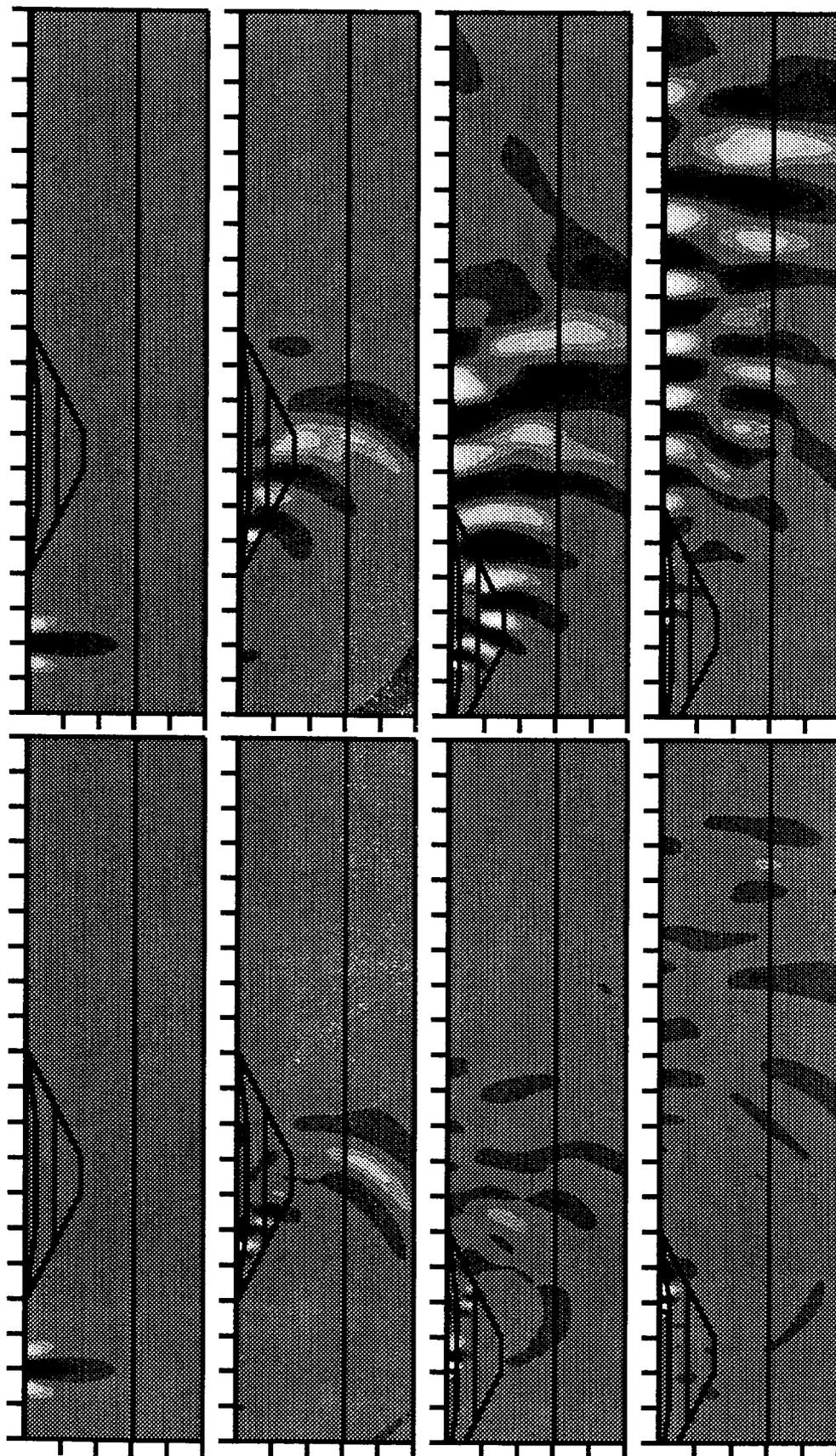


Figure 2. Snapshots of planar R_g incident upon contained basin structures. In the elastic basin model (left), the low-velocity basin slows down the fundamental mode. Although the scattering at the basin edges removes some energy from the R_g wave packet, the fundamental mode still retains the largest amplitude (See Figure 3). When the basin is replaced with depth-dependent low-Q materials (with the velocity unchanged), the fundamental mode is broken up, with the energy that tunneling through the deeper portion of the basin dominates the wavefield. This energy propagates as higher modes after passing through the basin.

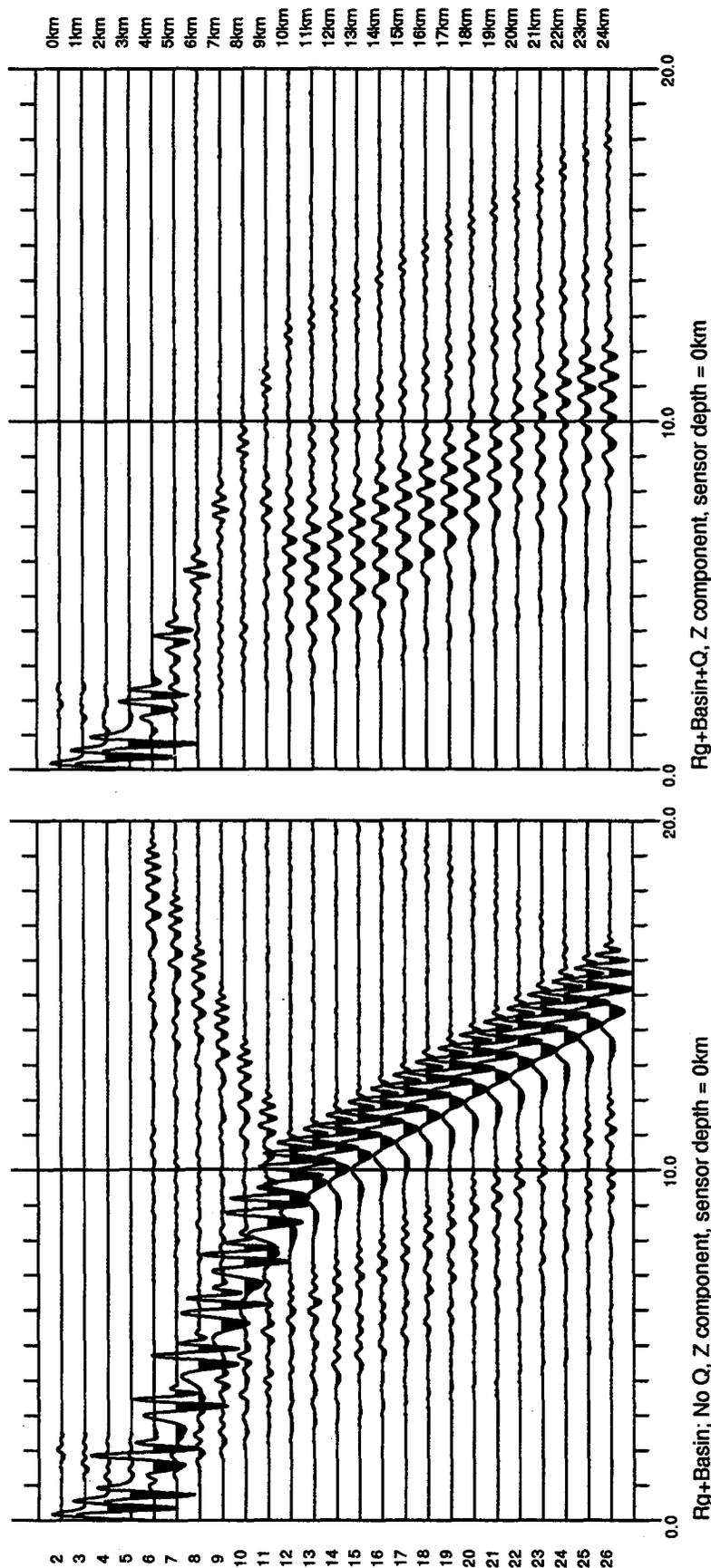


Figure 3. Synthetic seismograms, plotted in the same scale, for the two models shown in Figure 2. In the elastic basin model (left), the low-velocity sedimentary layers slow down the fundamental mode and cause significant backscattering at the basin edge. A fraction of the energy tunnels through (and under) the deeper layers of the basin and becomes higher modes, which travels ahead of the dominating fundamental mode. A little R_g -to-P conversion is also visible. When the basin is replaced with depth-dependent low-Q material (with the velocities unchanged), the R_g amplitude is reduced dramatically. The higher modes become the dominant phase in the transmitted wave train. Forward R_g -to-P conversion is enhanced as well. Note that the backscattering of R_g at basin edges becomes negligible (in this scale).

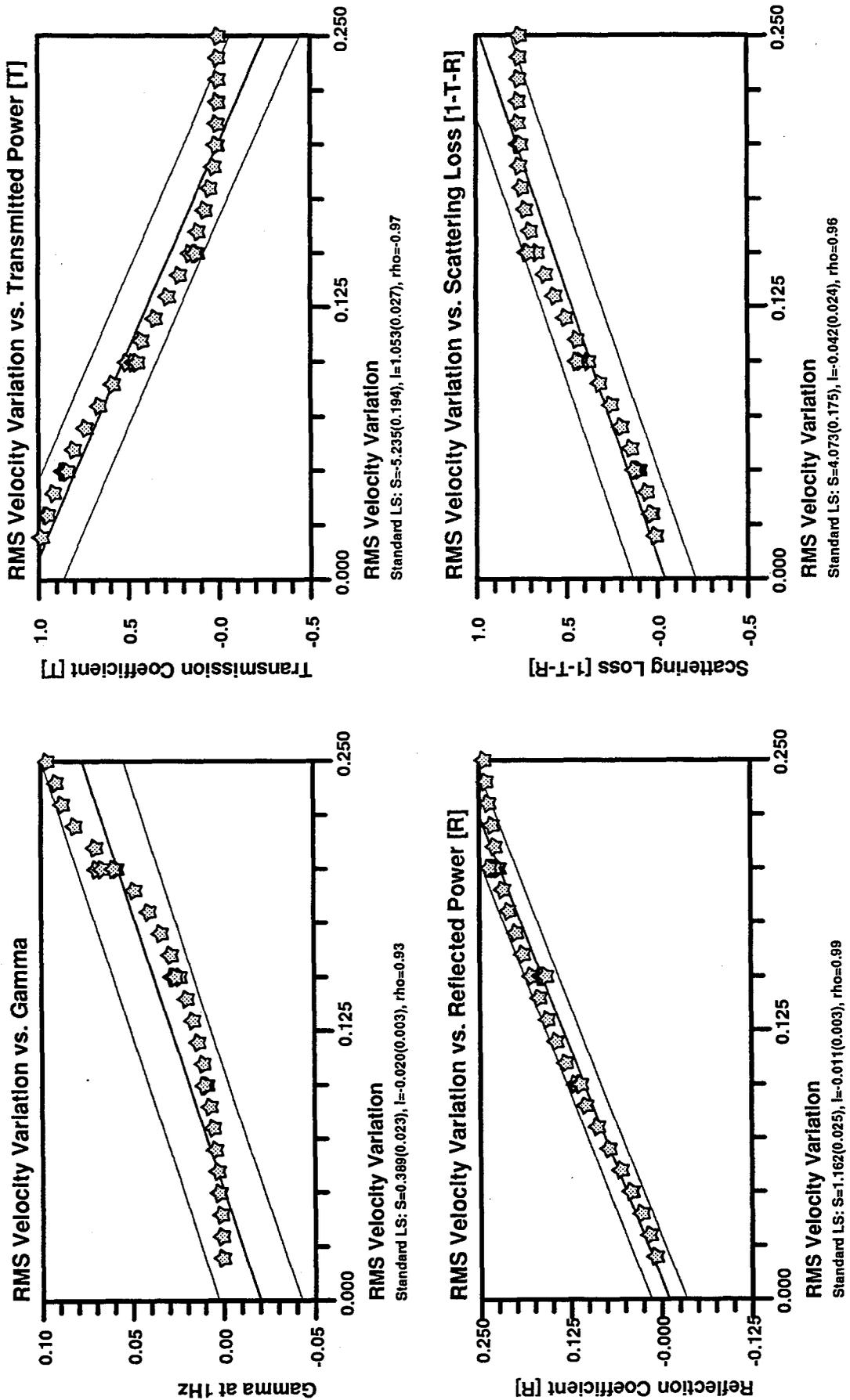


Figure 4. Regressing the attenuation coefficients [γ] (top left), transmitted power [T] (top right), reflected power [R] (bottom left), and scattering loss [1-T-R] (bottom right), respectively, on the RMS velocity fluctuation, σ , of 45 models with the thickness of the embedded self-similar shallow heterogeneous layer ranges from 1km to 5km. A 2%-5% variation in the velocity leads to an equivalent spatial Q value of 400 or larger for 1Hz F_g phase. Models with stronger heterogeneities have larger γ 's, stronger reflection, and smaller T's, as expected. The excellent linear fit (for up to 15%) suggests that general propagation statistics can be predicted with the RMS velocity variation alone.

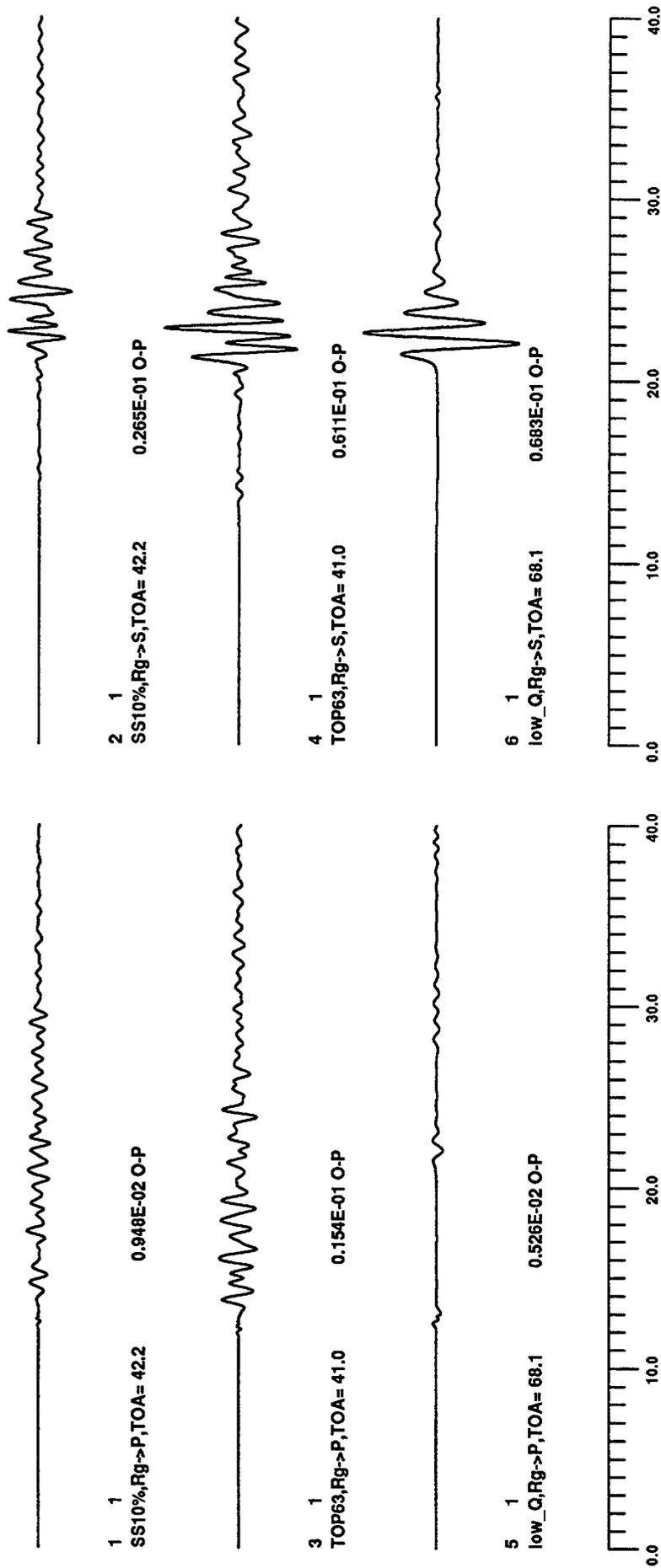


Figure 5. Comparison of LFD synthetic displacement seismograms of scattered body waves converted from R_g due to three different mechanisms. Shown on the left and right are the converted P and S waves, respectively, recorded at a depth of 5 km. The take-off angle and the peak amplitude of the scattered rays are shown under each trace. The three heterogeneous structures being compared are (from top) [1] a half-space model embedded with self-similar shallow heterogeneity with 10% velocity fluctuation, [2] a half-space model overlain by a rough topographic profile, and [3] a half-space model overlain by a strongly attenuative layer. A pure R_g wave packet was injected into the homogeneous portion of the grid to trigger the LFD calculations. In addition to the identical initial condition, other parameters (such as the grid size, the grid spacing, and the material properties of the bedrock) were also identical in these LFD simulations. Controlled numerical experiments using LFD are particularly convenient in isolating the effect of different mechanisms on R_g (or other phases). In terms of $R_g \rightarrow S / R_g \rightarrow P$ ratio or peak S-wave amplitude, incomplete dissipation of R_g waves appears to be more efficient than the two scattering processes. Scattering by topography or heterogeneity would generate a much longer coda, however. For each of the three $R_g \rightarrow S$ mechanisms investigated so far, $R_g \rightarrow S$ conversion is univocally stronger than that of $R_g \rightarrow P$.