UNCLASSIFIED

Defense Technical Information Center Compilation Part Notice

ADP011856

TITLE: Comparison of Two 1550 nm Ultra Narrow-Band Optical Infinite Impulse Response Filters for High-Speed Optical Signal Processing

DISTRIBUTION: Approved for public release, distribution unlimited

This paper is part of the following report:

TITLE: Optical Storage and Optical Information Held in Taipei, Taiwan on 26-27 July 2000

To order the complete compilation report, use: ADA399082

The component part is provided here to allow users access to individually authored sections of proceedings, annals, symposia, etc. However, the component should be considered within the context of the overall compilation report and not as a stand-alone technical report.

The following component part numbers comprise the compilation report: ADP011833 thru ADP011864

UNCLASSIFIED

Comparison of Two 1550 nm Ultra Narrow-Band Optical Infinite

Impulse Response Filters for High-Speed Optical Signal Processing

Shyh-Lin Tsao* and Te-Yu Chen Department of Electrical Engineering, Yuan Ze University Chung-Li,Taiwan, R.O.C.

ABSTRACT

Comparison of the frequency responses of two high-speed optical fiber processing elements is reported. The two filters we considered are a two-loops optical infinite impulse response (IIR) filter and a three-loops optical IIR filter. The theoretical models of these two kinds of optical IIR band pass filters are built up. Some suitable coupling coefficients are searched for simulating the narrow band-pass filters. The frequency responses under different conditions are analyzed. The theoretical models can provide parameter evaluation for experimental design. A higher design flexibility can be given by the three-loops optical IIR filter. These filters can be implemented with PIC (photonic IC) techniques and applied for optical data signal processing.

Keywords : Optical Data Storage, Optical Signal Processing, Optical IIR filter, Optical Fiber Communication

1.INTRODUCTION

In the next generation memory system, high capacity optical data storage will be the future trend. Many methods, such as hologram, CD-R, DVD, are studied for high capacity data storage above Giga-byte¹⁻³. In recent years, some fast data access and optical signal processing methods are extensively reported⁴⁻⁸. Especially reading optically storaged data by fiber, then using time-space-conversion optical signal processing attract a lot of attentions⁵.

Promising progress is shown in high speed optical communication systems developments recently ⁹⁻¹⁸. The fiber optic recirculating delay line is one of the basic optical signal elements generally being studied. We also reported some various designs and applications for high speed signal processing ¹⁹⁻²¹. Ultra fast signal processing over 100 Gbps is difficult to do by traditional electric signal processing circuit. This optical digital signal processor (OPSP) may be applied in high-speed DVD data storage systems as shown in Fig.1. In this paper, we design and analyze two ultra narrow-band optical infinite impulse response IIR filters for high-speed optical signal processing. Those two designed narrow-band optical IIR filters are operating at wavelength of 1550nm. The center of the narrowband filter is located at 100GHz. We use Z-transform to analyze the frequency responses of these two IIR filters: two-loops optical IIR filter. The two theoretical models for comparing their frequency responses are built up. Optimal coupling coefficients are sorted for simulating narrow bandwidth optical band pass filters.

Correspondence : Email : jimmy@saturn.yzu.edu.tw ; Telephone : 886-3-4638800-424 ; Fax : 886-3-4638355

2. THEORETICAL MODELS

We use Z-transform techniques to build up the theoretical model of a two-loops optical IIR filter and a three-loops optical IIR filter, respectively in this section. Assume these two kinds filters are linearly time-invariant systems and no temperature fluctuation effect, we derive the transfer functions as following.

2.1 Two-Loops Optical IIR Filter

The schematic diagram of two-loops optical IIR filter with two 3×3 optical couplers and four optical delay lines is shown in Fig.2. In Fig.3, we modeled the equivalent theoretical model by signal flow diagram. The signal can be represented as Eq. (1) to Eq. (6)

$$X_{1}(Z) = K_{3}[I_{1}(Z) + r_{X_{4}}Z^{-X_{4}}X_{4}(Z) + r_{X_{3}}Z^{-X_{3}}X_{3}(Z)]$$
(1)

$$X_{2}(Z) = K_{2}[I_{1}(Z) + r_{X_{4}}Z^{-X_{4}}X_{4}(Z) + r_{X_{3}}Z^{-X_{3}}X_{3}(Z)]$$
(2)

$$X_{3}(Z) = K_{6}[I_{2}(Z) + r_{X_{2}}Z^{-X_{2}}X_{2}(Z) + r_{X_{1}}Z^{-X_{1}}X_{1}(Z)]$$
(3)

$$X_{4}(Z) = K_{5}[I_{2}(Z) + r_{X_{2}}Z^{-X_{2}}X_{2}(Z) + r_{X_{1}}Z^{-X_{1}}X_{1}(Z)]$$
(4)

$$O_{1}(Z) = K_{1}[I_{1}(Z) + r_{X_{4}}Z^{-X_{4}}X_{4}(Z) + r_{X_{3}}Z^{-X_{3}}X_{3}(Z)]$$
(5)

$$O_{2}(Z) = K_{4}[I_{2}(Z) + r_{X_{2}}Z^{-X_{2}}X_{2}(Z) + r_{X_{1}}Z^{-X_{1}}X_{1}(Z)]$$
(6)

 $I_1(Z)$ and $I_2(Z)$ are the input signals at the input ports. $O_1(Z)$ and $O_2(Z)$ are the output signals at two ports. $X_1(Z)$, $X_2(Z)$, $X_3(Z)$, $X_4(Z)$ represent the input signals of delays Z^{-X_1} , Z^{-X_2} , Z^{-X_3} , Z^{-X_4} , respectively. The coupling coefficients and path transmittive coefficients for each optical output are represented as $K_{j(j=1-6)}$ and $r_{Xj(j=1-6)}=1$, respectively.

The relationship of the above six equations can be simplified as

$$X_{1}(Z) = K_{3}[I_{1}(Z) + \frac{K_{5}}{K_{6}}r_{X_{4}}Z^{-X_{4}}X_{3}(Z) + r_{X_{3}}Z^{-X_{3}}X_{3}(Z)]$$
(7)

$$X_{3}(Z) = K_{3}[I_{2}(Z) + \frac{K_{2}}{K_{3}}r_{X_{2}}Z^{-X_{2}}X_{1}(Z) + r_{X_{1}}Z^{-X_{1}}X_{1}(Z)]$$
(8)

Substitute Eq. (8) into Eq. (7), we find

$$X_{1}(Z) = \frac{K_{3}\left[I_{1}(Z) + \left(K_{5}r_{X_{4}}Z^{-X_{4}} + K_{6}r_{X_{3}}Z^{-X_{3}}\right)I_{2}(Z)\right]}{\Delta}$$
(9)

and

$$\Delta = 1 - K_3 K_6 r_{X_1} r_{X_3} Z^{-(X_1 + X_3)} - K_3 K_5 r_{X_1} r_{X_4} Z^{-(X_1 + X_4)} - K_2 K_6 r_{X_2} r_{X_3} Z^{-(X_2 + X_3)} - K_2 K_5 r_{X_2} r_{X_4} Z^{-(X_2 + X_4)}$$
(10)

Similarly, we can write $X_3(Z)$ as

$$X_{3}(Z) = \frac{K_{6}\left[I_{2}(Z) + \left(K_{3}r_{x_{1}}Z^{-X_{1}} + K_{2}r_{X_{2}}Z^{-X_{2}}\right)I_{1}(Z)\right]}{\Delta}$$
(11)

Then the output signals can be represented as

$$O_{1}(Z) = \frac{K_{1} \left[I_{1}(Z) + \left(K_{5} r_{X_{4}} Z^{-X_{4}} + K_{6} r_{X_{3}} Z^{-X_{3}} \right) I_{2}(Z) \right]}{\Delta}$$
(12)

$$O_{2}(Z) = \frac{K_{4}\left[I_{2}(Z) + \left(K_{3}r_{x_{1}}Z^{-X_{1}} + K_{2}r_{x_{2}}Z^{-X_{2}}\right)I_{1}(Z)\right]}{\Delta}$$
(13)

In this paper, we assume no input signal launched to port I_2 . Therefore, the above two transfer functions can be simplified as

$$H_{11}(Z) = \frac{O_1(Z)}{I_1(Z)} = \frac{K_1}{\Delta}$$
(14)

$$H_{12}(Z) = \frac{O_2(Z)}{I_1(Z)} = \frac{K_4 \left(K_3 r_{x_1} Z^{-X_1} + K_2 r_{x_2} Z^{-X_2} \right)}{\Delta}$$
(15)

2.2 Three-Loops Optical IIR Filter

The schematic diagram of a three-loops optical IIR filter is shown in Fig.4. This filter includes two 4×4 optical couplers and six optical delay lines. The schematic diagram of theoretical model of this filter is illustrated in Fig.5. Similarly, we consider the nodal signals $X_1(Z)$, $X_2(Z)$, $X_3(Z)$, $X_4(Z)$, $X_5(Z)$, and $X_6(Z)$, represent the input signals of the phase delays Z^{-X_1} , Z^{-X_2} , Z^{-X_3} , Z^{-X_4} , Z^{-X_5} , Z^{-X_6} , respectively. The transmittive coefficient of each delay path $r_{X_{j(j=1-8)}}$ is set to be 1. The coupling coefficient of each optical output is represented as $K_{j(j=1-8)}$ which is a positive real number. Because of energy conservation, the signal in each coupler should satisfy $K_1+K_2+K_3+K_4+K_5+K_6+K_7+K_8 = (1-L)$, and L means the intrinsic loss of optical couplers. In this paper, we assume the intrinsic loss is small enough that can be neglected. According to Fig.5, the transfer functions can be derived according to the following equations as

$$X_{1}(Z) = K_{4}[I_{1}(Z) + r_{X_{4}}Z^{-X_{4}}X_{4}(Z) + r_{X_{5}}Z^{-X_{5}}X_{5}(Z) + r_{X_{6}}Z^{-X_{6}}X_{6}(Z)]$$
(16)

$$X_{2}(Z) = K_{3}[I_{1}(Z) + r_{X_{4}}Z^{-X_{4}}X_{4}(Z) + r_{X_{5}}Z^{-X_{5}}X_{5}(Z) + r_{X_{6}}Z^{-X_{6}}X_{6}(Z)]$$
(17)

$$X_{3}(Z) = K_{2}[I_{1}(Z) + r_{X_{4}}Z^{-X_{4}}X_{4}(Z) + r_{X_{5}}Z^{-X_{5}}X_{5}(Z) + r_{X_{6}}Z^{-X_{6}}X_{6}(Z)]$$
(18)

$$X_{4}(Z) = K_{8}[I_{2}(Z) + r_{X_{1}}Z^{-X_{1}}X_{1}(Z) + r_{X_{2}}Z^{-X_{2}}X_{2}(Z) + r_{X_{3}}Z^{-X_{3}}X_{3}(Z)]$$
(19)

$$X_{5}(Z) = K_{7}[I_{2}(Z) + r_{X_{1}}Z^{-X_{1}}X_{1}(Z) + r_{X_{2}}Z^{-X_{2}}X_{2}(Z) + r_{X_{3}}Z^{-X_{3}}X_{3}(Z)]$$
(20)

$$X_{6}(Z) = K_{6}[I_{2}(Z) + r_{X_{1}}Z^{-X_{1}}X_{1}(Z) + r_{X_{2}}Z^{-X_{2}}X_{2}(Z) + r_{X_{3}}Z^{-X_{3}}X_{3}(Z)]$$
(21)

$$O_{1}(Z) = K_{1}[I_{1}(Z) + r_{X_{4}}Z^{-X_{4}}X_{4}(Z) + r_{X_{5}}Z^{-X_{5}}X_{5}(Z) + r_{X_{6}}Z^{-X_{6}}X_{6}(Z)]$$
(22)

$$O_{2}(Z) = K_{5}[I_{2}(Z) + r_{X_{1}}Z^{-X_{1}}X_{1}(Z) + r_{X_{2}}Z^{-X_{2}}X_{2}(Z) + r_{X_{3}}Z^{-X_{3}}X_{3}(Z)]$$
(23)

Similarity, we deduce the above equations and find that

$$X_{1}(Z) = K_{4}[I_{1}(Z) + r_{X4}Z^{X_{4}}X_{4}(Z) + r_{X5}\frac{K_{7}}{K_{8}}Z^{X_{4}}X_{5}(Z) + r_{X6}\frac{K_{6}}{K_{8}}Z^{X_{4}}X_{6}(Z)]$$
(24)

$$X_{4}(Z) = K_{8}[I_{2}(Z) + r_{X_{1}}Z^{-X_{1}}X_{1}(Z) + r_{X_{2}}\frac{K_{3}}{K_{4}}Z^{-X_{1}}X_{2}(Z) + r_{X_{3}}\frac{K_{2}}{K_{4}}Z^{-X_{1}}X_{3}(Z)]$$
(25)

From the above two equations, $X_1(Z)$ can be derived as

$$X_{1}(Z) = \frac{K_{4} \left[I_{1}(Z) + \left(K_{8} r_{X_{4}} Z^{-X_{4}} + K_{7} r_{X_{5}} Z^{-X_{5}} + K_{6} r_{X_{6}} Z^{-X_{6}} \right] I_{2}(Z) \right]}{\Delta'}$$
(26)

and

$$\Delta' = 1 - K_4 K_8 r_{X_1} r_{X_4} Z^{-(X_1 + X_4)} - K_4 K_7 r_{X_1} r_{X_5} Z^{-(X_1 + X_5)} - K_4 K_6 r_{X_1} r_{X_6} Z^{-(X_1 + X_6)} - K_3 K_8 r_{X_2} r_{X_4} Z^{-(X_2 + X_4)} - K_3 K_7 r_{X_2} r_{X_5} Z^{-(X_2 + X_5)} - K_3 K_6 r_{X_2} r_{X_6} Z^{-(X_2 + X_6)} - K_2 K_8 r_{X_3} r_{X_4} Z^{-(X_3 + X_4)} - K_2 K_7 r_{X_3} r_{X_5} Z^{-(X_3 + X_5)}$$

$$- K_2 K_6 r_{X_3} r_{X_6} Z^{-(X_3 + X_6)}$$
(27)

The $X_4(Z)$ can also be derived as

$$X_{4}(Z) = \frac{K_{8} \left[I_{2}(Z) + \left(K_{4} r_{X_{1}} Z^{-X_{1}} + K_{3} r_{X_{2}} Z^{-X_{2}} + K_{2} r_{X_{3}} Z^{-X_{3}} \right) I_{1}(Z) \right]}{\Delta'}$$
(28)

After a lot of reductions, we can find the transfer functions of the three-loops IIR optical filter as

$$H_{11}(Z) = \frac{O_1(Z)}{I_1(Z)} = \frac{K_1}{\Delta'}$$
(29)

$$H_{12}(Z) = \frac{O_2(Z)}{I_1(Z)} = \frac{K_5 \left(K_4 r_{X_1} Z^{-X_1} + K_3 r_{X_2} Z^{-X_2} + K_2 r_{X_3} Z^{-X_3} \right)}{\Delta'}$$
(30)

3. SIMULATION RESULTS AND COMPARISONS

Here we use the theoretical model derived in the above section, the frequency responses of these two optical IIR filters are simulated. The simulation results can be applied for practical realizing various filters. Taken narrow bandwidth optical band pass filters as example, the optimal parameters searching work is performed.

Table I shows three set of searched parameters corresponding to the simulated three examples of frequency responses of the two-loops optical IIR filter. According to the theoretical model we derived in subsection 2.1, three examples of frequency responses of two-loops IIR filters are shown in Fig.6. Example I is the best result we found. If the parameter K_4 increases, the sidelobe will arise as shown in the curveture of example II. The delay coefficients X_1 , X_2 , X_3 , X_4 can be adjusted for designing higher order filters. The simulation result example III shown in Fig.6 give a general scope of view of higher order filter.

The parameters we used for simulating three-loops IIR filters in Fig.7 are listed in Table 2. Similarly, the numerical results are shown as example I, II and III for comparing the results of Fig.6. The optimal result of narrowband filter is

shown in example I. When K_4 increases, the sidelobe will grow up as shown in example II like the two loops IIR filters. Increasing the order of this filter, the ripple of this filter will increased as shown in example III. We found the ripple is larger than the two loops IIR filters if the parameter is not well choosen.

Comparison of the optical two numerical results in Fig.6 and Fig.7, we zoom in the two cases of example I and show the spectra details in Fig.8. We can find that the three-loops IIR filter has a narrower optical frequency bandwidth than the two-loops IIR filter. The narrowest bandwidths of the two-loops IIR filter and the three-loops IIR filter we found are 0.00012 Hz and 0.00007 Hz, respectively. The narrow linewidth can provide pure filtering effect for extracting the phase lock loop carrier signal in DVD control systems.

4. CONCLUSIONS

The access data rate of optical storage systems increases rapidly in the last five years. Therefore, the signal processing will follow the trend, increasing the processing speed in the future. Accompany with the age of optical data storage above Tera byte, studying all-optical fiber high speed signal processing elements is important. The research results in this paper are very helpful for practical realizing various optical signal processing filters. The narrow band filter at 100GHz can be applied for clock recovery in high speed data-accessed DVD systems accompany some fiber pick up heads.

ACKNOWLEDGEMENT

This work was partially supported by the National Science Council of R.O.C. under contract NSC89-2215-E-155-003.

REFERENCE

- 1. L. Hesselink (Chairman), International Workshop on Holographic Data Storage, Nice, France, March, 1999.
- 2. K. Goto and K. Kurihara, "High speed VCSEL array head for Tera byte optical disk", *Proceeding of CLEO/Pacific Rim '99*, PP.1113-1114, 1999.
- 3. K. Goto, "High bit rate and Tera bytes optical memory in a disk system", SPIE, 3109, pp. 192-195, 1997.
- 4. J. Ma, J. Chang, S. Choi, J. Hong, "Digital holographic data storage with fast access" proceeding of CLEO/Pacific Rim '99, pp. 1241-1242, 1999.
- 5. T. Kurokawa, H. Takenouchi, H. Tsuda, "Time-Space-Conversion optical processing using arrayed-wavegnide grating", *Proceeding of CLEO/Pacific Rim '99*, pp. 809-810, 1999.
- 6. K.P.Jackson ,J.E. Bowers.S.A. Newton, and C.C.Cutler, "Microbend optical fiber tapped delay line for gigahertz signal processing". *Appl. Phys. Lett*, **41**, pp. 139-141,1982.
- 7. K.P., Jackson ,S.A. Newton, B.Moslehi, M. Tur, C.C.Cutler, J.W.Goodman, and H.J.Shaw, "Optical fiber delay-line signal processing", *IEEE Trans. on Microwave Theory and Techniques*, **33**, pp. 193-210,1985.
- 8. J, Capmany., "Time domain analysis of direct coupled fiber ring resonator", Opt. Comm. 192, pp. 283-290,1992.
- W.Pieper, "4-channel × 40 Gbps unrepeated TDM transmission over 100Km standard fiber", *IEEEE Photonic Technology Letter* 10, pp. 451-453,1998.

- 10. E.A. Varvarigos, "Control protocols for multigigabit-per-second networks", *IEICE Transactioons on Communications*, E81-B, 2, pp. 440-448, 1998.
- G.D.Bartoliini, D.K.Serkland, P.Kumar, "All-optical storage of a picosecond- pulse packet using parametric amplification: Demonstration of single-shot loading", *Technical Digest of Conference on Optical Fiber Communication*, pp. 201-202, 1998.
- J.-H.Han, S. K.Taejon, J.-W.Ko, J.-S. Lee, "0.1-nm slim bandwidth transmission of a 2.5-Gbit/s spectrum-sliced incoherent channel using an all-optical bandwidth expansion technique at the recceiver", *Technical Digest of* conference on Optical Fiber Communication, pp. 127-128, 1998.
- A.K.Dutta, H.Kosaka, K.Kurihara, Y.Sugimoto, K.Kasahara, "High-speed VCSEL of modulation bandwidth over 7.0 GHz and its application to 100m PCF datalink", *IEEE Journal of Lightwave Technology*, 16, pp. 870-875, 1998.
- J.Manchester, J.Anderson, B.Doshi, S.Dravida, "IP over SONET", *IEEE Communications Magazine*, 36, pp. 136-142, 1998.
- R.K. Butler, M.L. Jones, W.C. Szeto, "OC-48/STC-480 IP direct on wavelength application", Technical digest of Conference on Optical Filber Communication, pp. 153~155, 1999.
- H.Suzuki, N. Takachio, Y.Hamazumii, H.Masuda, S.Kawai, K.Arays, "Seamless 32×10G bit/s transmission over 320km of 1.55µm dispersion-shifted fiber using wavelengths ranging from 1546 nm to 1587 nm ",Technical dugest of *Conference on Optical Fiber Communication*, pp. 221-223,1999.
- 17. I.Morita, M.Suzuki, N.Edagawa, "20 Gbit/s single-channel soliton transmission over 9000km without inline filters", *First Optoelectronics and Communications Conference*, pp. 30-31,1996.
- T.Ido, S.Tonaka, M.Suzulci, M.Koizumi and H.Znoue, "Ultra-high speed multiple-quantum well electroabsorption modulators with integrated wawegnides", *First Optoelectronics and Communication Conference*, pp. 172-173, 1996.
- S.-L. Tsao, H.-W. Tsao And Y.-H. Lee, "Design of a self-routing frequency division multiple access (SR-FDMA) network using an optical ring filter with or without gain as a router", IEEE Journal of Lightwave Technology, 13, pp. 2168-2182, 1995.
- 20. S.-L. Tsao.Y.-T. Chen, H.-W. Tsao and J. Wu, "Active optical two-coupler fiber ring filter", *International Symposium on Communications*(ISCOM'93), **2**, pp. 15-22, 1995.
- 21. S.-L. Tsao, J. Wu. C.-F. Tsai, "Filter response of a third-order masterslave fiber-optic recirculating delay lines", *Chinese Journal of Radio Science, Proceedings of ICRS'95*, pp. 448-451, 1995.

	K ₁	K ₂	K ₃	K4	K ₅	K ₆	X ₁	X ₂	X ₃	X4			
Ι	0.0001	0.49995	0.49995	0.001	0.4995	0.4995	1	2	1	2			
П	2	4	4	2	4	4	1	2	1	2			
Ш	0.0001	0.49995	0.49995	0.9	0.05	0.05	3	4	5	6			

Table 1

Table 2														
	K ₁	K ₂	K ₃	K ₄	K5	K_6	K ₇	K ₈	X_1	X ₂	X ₃	X ₄	X_5	X ₆
I	0.0001	0.3333	0.3333	0.3333	0.001	0.25	0.499	0.25	1	2	3	1	2	3
П	2.5	2.5	2.5	2.5	2.5	2.5	2.5	2.5	1	2	3	1	2	3
Ш	0.0001	0.3333	0.3333	0.3333	0.91	0.03	0.03	0.03	4	7	1	7	4	1



Fig.1 The schematic diagram of application of high speed optical digital signal processing (ODSP) elements



Fig.2 The schematic diagram of a two-loops optical IIR band-pass filter



Fig.3 Two-loops optical IIR band-pass filter signal flow chart



Fig.4 The schematic diagram of a three-loops optical IIR band-pass filter



Fig.5 Three-loops optical IIR band-pass filter signal flow chart



Fig.6 Frequency response T_{12} of two- loops optical IIR band-pass filter



Fig.7 Frequency response T_{12} of three- loops optical IIR band-pass filter



Fig.8 Comparison of Two and Three-loops optical IIR narrow band-pass filter frequency responses