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Tutorial Survey of Algorithms For Locating and Identifying Spatially Distributed Sources and Receivers

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We present a short tutorial survey of algorithms for locating and identifying spatially distributed sources and receivers. The emphasis is on methods that are either considered to be very basic or lend theaselves potentially to distributed computations, the main objective of this work.r.ge shall also very briefly outline our own approach to this set of problems.

1. introduction

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in many practical problems it is necessary to actermine the location of signal (noise) sources from measurements provided by one or more sensors. Typical applications include:

- Acoustic surveillance systems (e.g., sonar detection of low flying aircraft),
- Seismic arrays for seismic exploration, monitoring earthquakes and nuclear explosions, or actacting vehicle movements,
- Antenna arrays for radio astronomy or electronic surveillance (e.g., direction finding),
- Multiple radar systems for detection and tracking.

The diversity of applications involving the target location problem makes a general unified treatment of this subject quite difficult. To provide some focus for our discussion we will use the following sample problem:

Consider a small number of sensor sites (pernaps ten) distributed over a specified area. A number of targets are present in the area and their location is to be estimated based on the data collected by the sensors. The sensors measure signals which are either emitted by the target (the passive case) or reflected by it (the active case which requires target illumination). By processing the signals provided by the sensor, information about target bearing and/or range can be determined.

Sometimes a single sensor is not capable of measuring either range or bearing, as for example with omnidirectional passive sensors. Combining data from a group or array of sensors, however, makes it possible to find the desired information. A sensor array of this type may be located at a single site, in which case we consider it as one whit, or it may be distributed among many sites.

In other cases the sensor sites can provide different types of target related data, in particular:

- (i) Range only (ranging radar, active sonar)
- (ii) Bearing only (optical, infrared sensor, direction finder)
- (iii) bearing and range (search, tracking redar)
- (iv) Target velocity (Doppler radars, MTI)

Different data types lead to different location estimation tecnniques. For example, range only or bearing only measurements are related to target association techniques (section 2.2). Bearing and range data is usually associated with tracking algorithms for moving targets. Data from a single canidirectional passive sensor is treated by time-of-arrival methods (section 2.1) or beamforming and array processing techniques (section 2.4). The estimation method also depends on the type of signals provided by the sensor site: concrett/nonconcret, "raw" or filtered cata (linear processing), data after detection (nonlinear processing), etc.

Classical methods of processing sensor data have generally been of the centralized type, that is, all of the sensor data was collected at one site and then processed. An alternative is to process much of the data at the collection site and to send only the relevant data to either a central site or (more generally) to the appropriate user. In Section 3 we shall discuss the different types of distributed processing and their advantages.

In the last section we will describe our own approach to the development of distributed algorithms for the estimation of position, location and other characteristics of sensors and sources, (Morf et al.). We will give a short description of sample algorithms of a fully distributed nature that have desirable features. We shall also outline several of the honclassical approaches to solving these problems.

2.0 Techniques for estimating target location

Inis work was supported by ARPA under contract ADA This section provides a brief summary of the 903-73-C-0179. solution techniques associated with the target

location problem. Only the casic ideas are presented; the details can be found in the references.

# 2.1 fime-of-Arrival Estimation

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A signal emanating from a remote source and measured in the presence of noise at two spatially separated sensors can be modeled as

$$x_{1}(t)=s(t)+n_{1}(t)$$
 (1a)

$$x_{p}(t)=as(t+D)+n_{p}(t), \qquad (1b)$$

where s(t),  $n_1(t)$ ,  $n_2(t)$  are assumed to be stationary, independent, random processes. One common method of estimating the time delay,  $\vartheta$ , is to compute the cross correlation function

$$R_{x_1x_2} = E\{x_1(t)x_2(t-t)\}$$
 (2)

$$\bar{a} \mathbf{x}_{1 \leq 2}(\mathbf{T}) = \hat{a} d_{\mathbf{r}}(\mathbf{T} - \mathbf{0}) \tag{3}$$

where d<sub>3</sub>(') is the signal autocorrelation funcan important property of autocorrelation t10n. functions is that  $R_{ss}(\tau) \leq R_{ss}(0)$ . Thus, the peak of  $\hat{\pi}_{ss}(\tau-0)$  will occur at t=D. This provides us with a way for finding the delay by calculating the estimated cross-correlation function. If s(t) is a white noise source,  $R_{s}(\tau-D) \neq \delta(\tau-D)$ , and the peak will be sharply defined. In general,  $R_{s}(\cdot)$ will be "spread out" which tends to broaden the peak, making it more difficult to pinpoint the actual delay. Furthermore, when multiple targets (and multiple delays) are present, the "tails" of the autocorrelation functions for different targets will be overlayed and more difficult to separate. Thus, it is desirable to preprocess the sensor measurements x, x so that after crosscorrelation sharper peaks will result, as in Fig. 4. In the absence of measurement noise this can be done by passing  $x_*(t)$ ,  $x_2(t)$  through a "whitening" filter for s(t), hence the correlation of s is removed. When hoise is present, the filter has to take into account both signal and noise spectra.



# Fig. 1: A time-delay estimator.

Different cnoices for the pre-fitter are possible depending upon the performance criterion chosen by the designer: the likelinood function [hann and Tretter], the deflection function [Knapp and Carter], etc. it should be noted that several estimator structures besides the multipliercorrelator estimator have been developed. All of the information about the target location are encoded in the relative time-delays of the various sensors. To see this consider the following:



Fig. 2: Target-sensor geometry

$$D_{ij} \frac{r_{i} - r_{i}}{c}, \qquad (4)$$

where  $b_{i,j}$  is the relative delay between sensor i and sensor j, and c is the propagation velocity.

$$r_{i}^{2} = (x_{T} - x_{i})^{2} + (y_{T} - y_{i})^{2}, i = 1, 2, ... N.$$
 (5)

It can be shown [Schmidt] that for  $N \ge j$ , the set of equations (+),(5) can be rewritten as a <u>linear</u> set of equations for  $x_{i} y_{T}$ , where the coefficients are known quantities' (i.e. written in terms of  $D_{ij} x_i y_i$ ). This set of equations can now be solved'to determine the target location.

The discussion above indicates that one way of solving the target location problem is to first estimate the time-of-arrival delays and then to compute the location based on the geometry of the problem [Hann]. It is possible, of course, to combine these two steps and develop an estimator directly for the target coordinates  $(x_T, y_m)$  or, as jis more commonly done, for its bearing and range. This leads to alternative estimator structures, typically using the maximum likelihood approach [Bangs and Schultheiss], [MacDonald].

## 2.2 Target Association Techniques

A special type of problem arises when multiple sensors which measure range but not azimuth (or vice versa) are used to estimate target location. If only a single target is present, its location is found by multilateration. For example, if azimuth measurements from several sensors are available, one has only to compute the intersection of the various lines-of-sight. The situation becomes more complex when multiple targets are present. This is illustrated by fig. 3.





Fig 3: The target association problem

Each sensor is assumed to have detected the two targets  $\Gamma_{1}$   $\Gamma_{2}$ . However, these detections are not properly associated. It is not known which seasurement of each sensor corresponds to which target. Thus, it is necessary to associate targets with sensor measurements before estimating the target locations (in fact the association and location problems are addressed simultaneously). Note also that if there are more targets than sensors, ambiguities ("gnost" targets) may result. In fig. 3, if S, was not there, the measurements of S, and S<sub>2</sub> would be consistent with the assumption that the targets are at  $\xi_{1}$ ,  $\xi_{2}$  rather than at  $\Gamma_{1}$ ,  $\Gamma_{2}$ .

Several schemes have been proposed to solve the target association problem, and they are priefly described below.

#### List Forming

Plok a pair of sensors and compute all the intersections of their lines-of-sight to potential targets (i.e. directions in which they detected scmetning). Inese intersection points are potential target locations. Now pick a third sensor and cneck whether its lines-of-sight pass through any of the intersection points. if not, aelete these points from the list of potential targets. by proceeding this way with the other sensors, the list will finally include only those target locations which are consistent with all the observait should be emphasized that this is a tions. nighly simplified description of more realistic list forming algorithms.

## Back-projection or Space-Search

The space to be searched is divided into cells of a size corresponding to the system resolution. The number 1 is added to those cells of the space which lie along the line of sight of a given sensor detection. This process is repeated for all lines-of-sight of all sensors. As can be seen from Fig. 4 the target locations can be identified as those having the signest number (= the number



Fig. 4: Association by back-projection

# Image reconstruction techniques

It is possible to view the sensor measurements as line integrals through an image consisting of "points of light" at the target locations. The line integrals are over the infrared emissivity map (for IR sensors) or the radar reflectivity map (for ranging radars). The problem of reconstruct-ing images from their line-integral projections nas been extensively treated in literature [e.g., Brooks and Di Chiro, Horn]. Recently it was snown how these techniques can be applied to the target association problem (Friedlander et al., Denton et al.] oy reconstructing the "brightness map" of the area under surveillance and identifying targets as the "bright spots". It should be noted that the image reconstruction method requires that the sensors provide the actual energy seasured in maca direction (range) and not just target/no target information. The detection takes place after processing the information from all the sensors; in list forming and space-search, only the results of the detection performed at each individua. sensor are passed on.

# 2.5 Spectral estimation

Multiple-sensor measurements can be considered as samples of a time-space function  $y(t, \underline{2})$ where P represents a point in 3-D space. The notions of (temporal) correlation function and (temporal) spectral density can be extended to time-space functions of this type. We define a random field  $y(t, \underline{2})$  as stationary and nonogeneous if  $\Xi_1y(t, \underline{2})=0$  and

where

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Any nonogeneous random field nas a spectral representation

$$y(t, \underline{t}) = \int \int \int e^{j(\mathbf{z} \mathbf{z} + \mathbf{k}^{-2})} Z(\mathbf{c} \mathbf{z}, \mathbf{d} \mathbf{k}), \qquad (7)$$

where  $\underline{x}^{\pm}(x_1, x_2, x_3)$ ,  $\underline{P}^{\pm}(x, y, z)$  and  $\underline{z}(\underline{A}, \underline{A}, \underline{k})$  is a random function with certain properties. The correlation function can be represented by

X(4,\_)=

$$\int \int \int e^{j(\alpha E \cdot K \cdot E)} P(m \cdot K) \, \mathrm{d} \mathbf{k}$$
(3)

where P is the spatial-temporal spectral density. As in the temporal case, an inversion formula nois:

$$\frac{\partial (\mathbf{u}, \underline{x}) = \frac{1}{(2\pi)^{4}} \int_{-\infty}^{\infty} \int_{\mathbb{T}} e^{-j(\mathbf{u} \mathbf{x}^{*} \underline{k}^{*} \underline{r})} e^{-j(\mathbf{u} \mathbf{x}^{*} \underline{r})} e^{-j(\mathbf{u} \mathbf{x}^{*}$$

As an important example, consider a zonochromatic (single frequency) plane wave at tenporal frequency  $\mathbf{m}_{i}$  propagating in the direction given by a unit vector  $\hat{\mathbf{x}}$  at velocity c. Such a wave is represented by

$$y(t, \underline{P}) = \exp(j\omega_{1}t + \kappa_{0}T)$$
(10a)

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it is easy to verify that for this space-time function we have

and

which is a delta function located at temporal frequency  $\boldsymbol{w}_{j}$  and spatial frequency (or wave number)  $\boldsymbol{\kappa}_{j}$ . This example indicated now  $P(\boldsymbol{w},\boldsymbol{\kappa})$  provides information regarding the direction (and velocity) of propagation of waves.

The point of this discussion is that (spatial) spectral estimation is a way of estimating target bearing, since if we plot  $P(w,\underline{x})$  in the  $\underline{x}$ plane (for a fixed w), it will tend to be concentrated around the point  $\underline{x}$  which corresponds to the direction of the wave propagation and hence the bearing of the target (the source of these waves).

Thus, target bearing estimation reduces to the problem of estimating  $P(\boldsymbol{\omega}, \underline{k})$  from the measurements  $y(t_{\underline{i}}, \underline{r}_{\underline{j}})$ , where  $r_{\underline{j}}$  represents sensor locations and  $t_{\underline{i}}$  are the sampling times of the output of that sensor.

Many spectral estimation techniques have been used in this context; several are described in the references.

# 2.4 Beamforming and Array Processing

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Fernaps the most common operation in processing signals in a sensor array is that of beamforming. Antenna arrays (for radar, communication, etc.) and acoustic sensor arrays (sonar) are typical examples of beamforming. Beamforming consists of a summation of time-delayed (or phase-shifted) versions of the sensor outputs. i.e.

$$Z(t) = \sum_{i=1}^{n} y(t-t_i, \underline{p_i}),$$
 (12)

where  $t_i$  represents the time-delay for sensor i and  $P_i$  its location. Proper choice of the delays  $t_i$  enhances the signals received from a particular direction and attenuates signals from other directions. This operation is the spatial equivalent of a temporal narrow bandpass filter.

The output 2(t) of the ceanformer is a (scalar) time function, which is processed so as to obtain a measure of the signal energy in an optimal way. The most common processing schemes include

Matched filtering Wiener filtering or least-squares estimation Maximum likelihood estimation

This linear filtering is often followed by a nonlinear operation, e.g. squaring and integration. The order of linear filtering and transforming (also a linear operation) is often reversed, the exact structure depending on the application. The implementation of these processes is usually done in the fourier domain (with phase shifts replacing time delays) but time domain implementations are also used. A sample of the vast literature on beamforming and the associated signal processing (referred to as "array processing") is given in the bubliography.

A class of array processor of particular interest are the different types of adaptive arrays. The need for adaptive arrays arises for many reasons. Some examples:

- Null steering, to minimize interference from sources other than the target of inter-st.
- Adaptive filtering, to manule unknown noise and signal statistics.
- Adaptive beamforming. Seamforming requires precise knowledge of the sensor locations (within fractions of a wavelength) in order

that the steering delays be computed. Relatively small errors can lead to serious performance degradation. Thus, when sensor locations are imprecisely known or are constantly changing, a fixed processing scheme is infeasible.

# 5. The Need for Distributed Computation

There are many advantages in distributing computations for a large sensor network; some of the main arguments are the following:

## (1) Reduction of Computational Complexity

Distributed processing is often used as a means for solving problems related to large-scale systems. This approch leads to the decomposition of a nigh-dimensional problem into a sequence of smaller-dimensional ones. This often results in considerable computational savings; many fast algorithms, such as the Fast Fourier Transform, are of this type. Also, certain large-scale problems simply cannot be solved in a direct manner (e.g., inversion of very large matrices) and ways nave to be found to decompose the problem into smaller parts that can be nandled. This can, of course, be cone in a centralized manner, but the distributed approach often leads to natural decompositions and valuable insignts.

## (2) Reliability

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Distributed systems have good properties from a reliability standpoint due to their innerent parallelism. Failure of a computational module does not necessarily result in system failure since the computational load can be redistributed among the remaining modules. Thus, a distributed system may have the ability to reconfigure and continue operation. Depending on the type of the system and its structure, its operation after reconfiguration may be at a reduced performance level. (This would be the case if the remaining computational resources were insufficient to complete the solution of the problem, or if the loss of a computational module was associated with the loss of a sensor site.) The system graceful degradation of performance, displays which contrasts with the "catastrophic" failure mode of centralized systems.

#### (j) flexibility

The distributed nature of computations is often associated with distributed system structures; such a system structure sight be a collection of sensor/computer/communication modules interconnected in a network. This organization leads to a /ery flexible structure, possessing desirable properties which are not always present in a centralized system:

- Sasy system growth
- The capcity to nandle topological snanges in the system structure (e.g., adding or delet-

ing modes during maintainance without interrupting system operation).

- The possibility of incorporating many compinations of resources, with variable performance levels, as determined by the needs of each user.
- The combination, in a single network, of many types of information sensors.
  - 4. Our Approacnes

environment.

Distributed processing has by now become a term that is applied to many types of systems and is not very well defined. Since the distributed sensor net problem can be well described, see e.g. [ISL DSN Report], we shall use it as a basis for defining distributed processing. We consider three computational organizations which could be used in this context: centralized, independently distributed, and cooperatively distributed.

 Centralized -- all sensor data is passed to a central site, where computation is performed, and the pertinent results are then returned to the appropriate remote sites.
Independent -- all sensor information is communicated to every other site, and each site then makes its best estimate of the 3) Cooperative -- sites exchange processed information, and at most partial sensor data. It is the second and third organizations that are normally referred to as distributed organizations, and the third, in particular, that we consider to be of greatest interest.

The Search for Distributed Algorithms

Centralized algorithms are now quite well understood, as a perusal of the extensive literature indicates. nowever, very few attempts have been made to unify and integrate all tuese different approaches and results. A typical book on radar or sonar signal processing is a rather ad hoc collection of data, methods and theory (ruminiscent of a cook-ocok). To an outsider of this field it is extremely difficult to get a concreme picture and to make intelligent choices in applying these methods in the design of systems. systematic representation of this knowlege, by itself a tremendous task, is required in order to make effective use of the available alternatives. It is very tempting to suggest the asvelopment of an "expert support system" combining and extending recent approaches in A1, data-oase management and related fields.

Our approach to the development of (cooperatively) distributed algorithms can be summarized under the following headings:

Partitioning of optimal centralized algorithms, such as Maximum-Likelincol, Extended Kalman Filtering, and beam Forming. This approach is deful when the system under consideration can be

- Application and extension of methods developed in the context of decentralized control and estimation, e.g. team decision theory and differential games, hierarchical and multilevel systems, aggregation methods, singular perturbation and other perturbation techniques, periodic coordination and spatial dynamic programming (sdp).
- 5. Development of new optimal distributed algoritms for specific subsets of sensor lata. For example,
  - Time/Frequency Difference Of arrival (TDOA/FDOA) data, using ARMA modeling.
  - Range only or Angle only data, using image reconstruction techniques or distributed versions of the backprojection technique described in Section 2.2.
  - Range and Angle data, using Nonlinear Stimation techniques.
  - Mixed, possibly inconsistent/incomplete data, using a nierarchical approacn.
- 4. Advanced Concepts

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- The physical problem of locating and identifying sources has much mathematical structure; for example, it is heavily dependent upon the choice of coordinate systems. Non fuclidean Geometry and Non Classical Statistics (Non-Gaussian) will very probably de of great benefit.
- Signal processing of onedimensional signals is a very well developed field; spatial and other multi- dimensional problems, however, require more advanced mathematical tools.
- Our preliminary investigations indicate that most candidate algorithms for distributed processing require high communication bandwidths. As an alternative approach, we are investigating Probabilistic Algorithms; these algorithms potentially require lower bandwidths, are naturally suited to parallel and distributed organizations, and they can be very robust.
- From a systems-design perspective one should consider interactions between software and hardware architecture early in the develop-

# ment of algorithms. For this reason, we are considering the potential impact of VLS1/VHS1 designs.

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Using these approaches, examples of fully distributed processing and communication algorithms can be proposed. One such example is the combination of the TDOA approach [Schmidt], the distributed estimation algorithm in [ISL-DSN Asport] and a distributed protocol a la [Merlin and Segall]. These algorithms have the desired robustness and low communication bandwidths that characterize desirable distributed algorithms.

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