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EVANESCENT WAVEGUIDE APPARATUS AND METHOD FOR  
MEASUREMENT OF DIELECTRIC CONSTANT

TO WHOM IT MAY CONCERN:

BE IT KNOWN THAT DAVID A. TONN, employee of the United States Government, citizen of the United States of America, resident Charlestown, County of Washington, State of Rhode Island, has invented certain new and useful improvements entitled as set forth above of which the following is a specification:

JEAN-PAUL A. NASSER, ESQ.  
Reg. No. 53372

2  
3 EVANESCENT WAVEGUIDE APPARATUS AND METHOD FOR  
4 MEASUREMENT OF DIELECTRIC CONSTANT

5  
6 STATEMENT OF GOVERNMENT INTEREST

7 The invention described herein may be manufactured and used  
8 by or for the Government of the United States of America for  
9 governmental purposes without the payment of any royalties  
10 thereon or therefore.

11  
12 BACKGROUND OF THE INVENTION

13 (1) Field of the Invention

14 The present invention relates generally to measuring the  
15 dielectric constant of an unknown material and, more  
16 specifically, to a waveguide apparatus and method to thereby  
17 determine the dielectric constant.

18 (2) Description of the Prior Art

19 The dielectric constant of a material is an essential  
20 parameter that is important to know with confidence when doing  
21 electromagnetics work. This parameter, denoted  $\epsilon_r$ , may be  
22 utilized to determine the wave number of an electromagnetic wave  
23 in a material and as a result, the phase velocity, guided  
24 wavelength, and so forth, of the electromagnetic wave.

1 Current methods for measuring the static dielectric constant  
2 include plating two opposite surfaces of a sample with conductive  
3 material and measuring the static capacitance that results. This  
4 is useful when the material is to be used for a capacitor or for  
5 low-frequency applications. This method may not be sufficiently  
6 informative when the material is to be used for RF applications  
7 because for most materials, the static (f=0 Hz) dielectric  
8 constant is different from that seen by a RF signal.

9 For RF purposes, measurement of the dielectric constant is  
10 often accomplished by use of an open-ended coaxial probe that is  
11 placed in contact with the sample and the impedance that is seen  
12 can be used to calculate  $\epsilon_r$ . Measurement of the dielectric  
13 constant can also be performed by transmission of an RF signal  
14 through a plate of the unknown material in an anechoic  
15 environment, i.e., an environment that is free from echoes and  
16 reverberations. Another prior art method measures the frequency  
17 at which a block of the unknown material resonates at RF. In  
18 each of these prior art methods, a large sample of the material  
19 is required along with a suitable anechoic test environment.

20 The following patents discuss prior art attempts to solve  
21 problems related to the above:

22 U.S. Patent No. 4,891,573, issued January 2, 1990, to Gordon  
23 D. Kent, discloses a ceramic or other substrate, which is tested  
24 for dielectric constant K, and loss tangent by placing it on a

1 central transverse plane across a cylindrical waveguide. A swept-  
2 frequency signal is injected into the waveguide at an input  
3 coupling loop and is picked up at an output coupling loop.  
4 Maximum transmission through the dielectric substrate occurs at a  
5 frequency that depends on the waveguide radius, the substrate  
6 thickness, and the dielectric constant. The dielectric constant  
7 can be obtained from the resonant frequency of a predetermined  
8 transmission mode. The loss tangent can be calculated from the  
9 transmission bandwidth. The measurement of the dielectric  
10 constant is insensitive to the position of the substrate in the  
11 gap between waveguide sections, and thus intimate contact is not  
12 required.

13 U.S. Patent No. 4,996,489, issued February 26, 1991, to P.  
14 L. Sinclair, discloses a system for measuring the complex  
15 dielectric constant of a core sample. The system incorporates a  
16 circular waveguide having a central axial transmitter coil.  
17 Equally spaced axial receiver coils are placed on both sides of  
18 the transmitter coil. The opposite polarity receiver signals are  
19 connected to an adder circuit to provide an output signal  
20 representing only the difference in the two received signals. By  
21 placing a standard, such as air, between the transmitter coil and  
22 one receiver coil, and a core sample positioned between the  
23 transmitter coil and the other receiver coil, the system obtains  
24 an output indicative of complex dielectric constant. Optionally,

1 the system is operated in an oven to provide an elevated  
2 temperature, and can also be pressurized with a compressed fluid.

3 U.S. Patent No. 5,001,433, issued March 19, 1991, to S.  
4 Osaki, discloses apparatus and method for measuring electric  
5 characteristics of sheet-like materials using an instrument which  
6 includes a waveguide tube member having one end connected to  
7 transmitter for introducing a microwave into the tube member and  
8 the other end fully opened, a waveguide terminal member having an  
9 opened end facing the opened end of the tube member to form slit  
10 of the whole wave guide body constituted from the tube and  
11 terminal members and having the other end connected to first  
12 microwave detector, and an auxiliary waveguide branching from the  
13 wall portion of said tube member adjacent to the slit with the  
14 branch-extension end being associated with a second microwave  
15 detector.

16 U.S. Patent No. 5,103,181, issued April 7, 1992, to Gaisford  
17 et al., discloses radio frequency bridge techniques used to  
18 parameterize the complex dielectric properties of solids,  
19 liquids, gasses and mixtures thereof. This parameterization is  
20 performed in an electrically isolated, physically open structure,  
21 which allows continuous or batch monitoring of the materials and  
22 their mixtures. A method and apparatus are provided for measuring  
23 the composition of multi-component process streams flowing in  
24 pipes or ducts. The method uses the pipe in which the mixture

1 flows as a waveguide in which propagating radio frequency  
2 electromagnetic energy is induced through dielectric loaded  
3 apertures. The dielectric measurement is performed in an  
4 electrically isolated, flow through test section that induces  
5 constructive or destructive interference patterns at  
6 characteristics frequencies. The characteristic frequency  
7 determines the dielectric constant of the mixture. The dielectric  
8 properties are used in turn to determine mixture composition. A  
9 density measurement is also provided for three component streams  
10 such as oil, water, and gas. Temperature and pressure  
11 measurements are made to correct for temperature and pressure  
12 induced variations in calibrated component impedance and density  
13 values.

14       The above cited prior art does not provide an apparatus and  
15 method utilizing an air-filled metallic waveguide fitted with a  
16 metal (e.g. brass) septum or plate that divides the waveguide in  
17 half for a portion of its length whereby the material to be  
18 measured is fitted in the waveguide on either side of the metal  
19 sheet. The above-cited prior art does not show a tapered or  
20 restricted diameter waveguide that may be utilized with a single  
21 sample of the material without requiring a metal sheet. The  
22 above-cited prior art does not utilize a waveguide section  
23 operated in a cutoff or evanescent mode. Moreover, it would be  
24 desirable to be able to measure the dielectric constant of a

1 sample material without the need to accurately measure the length  
2 of the sample.

3 The solutions to the above-described problems are highly  
4 desirable but have never been obtained or available in the prior  
5 art. Consequently, those skilled in the art will appreciate the  
6 present invention that addresses the above and other problems.

7

8

#### SUMMARY OF THE INVENTION

9 An object of the present invention is to provide an improved  
10 apparatus and method to determine the dynamic dielectric constant  
11 of an unknown material.

12 An advantage of the present invention is that a very small  
13 sample may be utilized.

14 Another advantage of the present invention is that the  
15 method does not require a shielded or anechoic environment.

16 A feature of the present invention is a split waveguide  
17 having a reduced cross-sectional area in a middle portion  
18 thereof.

19 These and other objects, features, and advantages of the  
20 present invention will become apparent from the drawings, the  
21 descriptions given herein, and the appended claims. However, it  
22 will be understood that above listed objects and advantages of  
23 the invention are intended only as an aid in understanding  
24 aspects of the invention, are not intended to limit the invention



1 in any way, and do not form a comprehensive list of objects,  
2 features, and advantages.

3       Accordingly, the present invention provides an apparatus for  
4 measuring a dielectric constant of an unknown material that may  
5 comprise one or more elements such as, for example, a waveguide  
6 frame that defines a rectangular cross-section waveguide aperture  
7 there through. The waveguide frame comprises a first end on one  
8 side of the waveguide aperture and a second end on an opposite  
9 side of the waveguide aperture. The first end and the second end  
10 define the waveguide aperture with a width  $a$  and a height  $b$   
11 wherein the width  $a$  is greater than the height  $b$ . The waveguide  
12 frame is split along a length of the waveguide to permit the  
13 waveguide frame to be opened and closed. The waveguide frame has  
14 a middle section with at least one reduced waveguide aperture  
15 portion comprising a reduced width less than the width  $a$ . At  
16 least one sample of the unknown material is utilized and has a  
17 width equal to the reduced width  $a$  and height  $b$  to thereby mate  
18 with the reduced waveguide aperture portion. The at least one  
19 sample of unknown material is insertable into the middle section  
20 when the waveguide frame is opened and then mates to the reduced  
21 waveguide aperture portion when the waveguide frame is closed to  
22 permit measurement of the dielectric constant of the sample of  
23 unknown material.

1 In one embodiment, the apparatus may further comprise a  
2 metal septum insertable into the middle section of the waveguide  
3 frame for dividing the waveguide width  $a$  into one-half whereby  
4 the reduced waveguide aperture portion actually comprises two  
5 reduced waveguide aperture portions. For this embodiment, two  
6 samples of the unknown material are insertable on opposite sides  
7 of the metal septum. The metal septum may be comprised of brass.  
8 The metal septum has a septum length, and the two samples may  
9 preferably have a length equal to the septum length.

10 In a preferred embodiment, the reduced width for the  
11 waveguides discussed above has a width of  $a/2$  such that this  
12 section of the waveguide operates in a cutoff or evanescent mode.  
13 Preferably, the first end and the second end of the waveguide  
14 are conveniently filled with air.

15 A method is provided for determining a dielectric constant  
16 of an unknown material which may comprise one or more steps such  
17 as, for instance, providing a split waveguide frame with first  
18 and second ends defining a cross-sectional area for a waveguide  
19 when the split waveguide frame is closed together, and/or  
20 providing at least one restriction in a middle section of the  
21 split waveguide frame between the first and second ends to define  
22 at least one reduced cross-sectional area waveguide, and/or  
23 making at least one sample of the unknown material with a size  
24 and shape to mate with the at least one reduced cross-sectional

1 area waveguide in the middle section. Other steps may comprise  
2 opening the split waveguide frame, inserting the at least one  
3 sample into the middle section of the split waveguide frame,  
4 closing the split waveguide frame, and/or measuring a frequency  
5 response of the split waveguide frame with the at least one  
6 sample therein.

7 The method may further comprise determining a lowest order  
8 minimum from the frequency response of the split waveguide with  
9 the sample therein. Other steps may comprise determining the  
10 dielectric constant of the unknown material from the lowest order  
11 minimum of the frequency response of the split waveguide  
12 utilizing a graph for visual determination or equations discussed  
13 hereinafter for calculating the value.

14 The method may further comprise inserting a metal septum  
15 into the middle section of the split waveguide frame between to  
16 thereby define two reduced cross-sectional area waveguide  
17 apertures wherein the method further comprises inserting two  
18 samples into the two reduced cross-sectional area waveguide  
19 apertures. Alternatively, the method comprises providing  
20 internally tapering sections of the split waveguide frame on  
21 either side of the middle section.

1 BRIEF DESCRIPTION OF THE DRAWINGS

2 A more complete understanding of the invention and many of  
3 the attendant advantages thereto will be readily appreciated as  
4 the same becomes better understood by reference to the following  
5 detailed description when considered in conjunction with the  
6 accompanying drawings, wherein like reference numerals refer to  
7 like parts and wherein:

8 FIG. 1a is an exploded perspective view of a dielectric  
9 constant waveguide measuring apparatus in accord with one  
10 embodiment of the present invention;

11 FIG. 1b is a normal perspective view of a dielectric  
12 constant waveguide measuring apparatus in accord with one  
13 embodiment of the present invention;

14 FIG. 2 is a graph of the frequency response of the waveguide  
15 of FIG. 1 with a Teflon sample therein in accord with one  
16 embodiment of the invention;

17 FIG. 3 is a graph of resonant frequency versus dielectric  
18 constant that may be utilized to visually determine the  
19 dielectric constant from the frequency response in accord with  
20 one embodiment of the present invention; and

21 FIG. 4 is a graph of the frequency response the waveguide of  
22 FIG. 1 with an unknown material therein whereby the dielectric  
23 constant is determined from the graph of FIG. 3 after the lowest  
24 order minimum frequency response of the waveguide is determined

1 utilizing a network analyzer in accord with one embodiment of the  
2 present invention.

3 FIG. 5 is a perspective view of the dielectric constant  
4 waveguide measuring apparatus connected to a vector network  
5 analyzer via coaxial cables in accord with the present invention.

6

7

#### DESCRIPTION OF THE PREFERRED EMBODIMENT

8 The present invention provides a tool for measuring the  
9 dynamic (as opposed to static) dielectric constant of an unknown  
10 material in the microwave regime by using only a small sample  
11 placed in a cutoff section of a preferably rectangular waveguide.

12 Only a very small sample of the unknown material is required.  
13 Because the measurement can take place without the need to build  
14 a shielded or anechoic environment, the cost and effort involved  
15 in measuring the dielectric constant is reduced.

16 It is well known from microwave theory that rectangular  
17 waveguides have a lower cutoff frequency below which they cannot  
18 propagate a real energy flow. This lowest order cutoff is  
19 determined by the width of the waveguide so long as the width,  
20  $a$ , is at least twice the height,  $b$ :

$$21 \quad f_c = \frac{c}{2a\sqrt{\epsilon_r}} \quad (1)$$

22 where  $c$  is the velocity of light ( $3 \times 10^8$  m/s),  $a$  is the width  
23 of the waveguide in meters, and  $\epsilon_r$  is the dielectric constant of

1 the material filling the waveguide. Above this cutoff frequency,  
2 the waveguide has a real characteristic impedance and carries a  
3 real power flow. Below the cutoff frequency, the impedance is  
4 purely imaginary and the power flow is evanescent or imaginary.

5 Referring now to the figures and, more particularly, to FIG.  
6 1a and 1b, there is shown an exploded and normal view of a  
7 dielectric constant waveguide measuring apparatus 10 in accord  
8 with the present invention. Apparatus 10 comprises two identical  
9 outer fixtures 16a and 16b. Each outer fixture is a rectangular  
10 metal block with a rectangular groove running the length of one  
11 side of the fixture along the longitudinal axis of the fixture.  
12 When fixture 16a is mated with fixture 16b such that the sides  
13 with their respective grooves are in contact with each other the  
14 two fixtures define an air filled metallic rectangular waveguide  
15 20. Apparatus 10 comprises one preferred embodiment that may be  
16 utilized for measuring the dielectric constant of unknown samples  
17 12 which are the same length  $L$ . Samples 12 fill waveguide 20 on  
18 either side of septum 14 and are the same length as septum 14.  
19 Septum 14 is centered along the length of the fixtures 16a and  
20 16b, and connects the grooved surfaces of mating fixtures 16a and  
21 16b. Septum 14 divides the width  $a$  of waveguide 20. In a  
22 preferred embodiment, septum 14 is preferably comprised of metal  
23 such as brass. Guide pins 18 may be utilized to connect fixtures  
24 16a and 16b, which close around septum 14, and samples 12.

1 In the areas in front of and behind septum 14, waveguide 20  
2 is filled with air and its lower cutoff frequency  $f_c$  is  
3 determined from equation (1). The characteristic impedance of  
4 waveguide 20 in the air-filled region is real for  $f > f_c$  and is:

$$5 \quad Z_1 = \frac{k_0 \eta_0}{\sqrt{k_0^2 - k_{c0}^2}} \quad (2)$$

6 where:

$$7 \quad k_0 = \frac{2\pi f}{c}, \quad k_{c0} = \frac{\pi}{a}, \quad \eta_0 = 377\Omega \quad (3)$$

8 In the region of waveguide 20 at septum 14 and samples 12,  
9 the cutoff is defined by equation (1) where  $a$  is replaced by  
10  $a/2$ , because septum 14 cuts width  $a$  of waveguide 20 in half.  
11 Therefore, the impedance of waveguide 20 in this region is  
12 imaginary so long as

$$13 \quad f < \frac{c}{a\sqrt{\epsilon_r}} \quad (4)$$

14 and this impedance will be:

$$15 \quad Z_2 = j \frac{k\eta}{\sqrt{k_c^2 - k^2}} \quad (5)$$

16 with:

$$17 \quad k = \frac{2\pi f \sqrt{\epsilon_r}}{c}, \quad k_c = \frac{2\pi}{a}, \quad \eta = \frac{\eta_0}{\sqrt{\epsilon_r}} \quad (6)$$

18 From transmission line theory, the total reflection coefficient  
19 seen looking into the section of the waveguide 20 containing the  
20 samples 12 and the septum 14 is:

$$\Gamma = \Gamma_1 \frac{1 - e^{-j2L\sqrt{k^2 - k_c^2}}}{1 - \Gamma_1^2 e^{-j2L\sqrt{k^2 - k_c^2}}} \quad (7)$$

where  $L$  is the length of samples 12 in meters and:

$$\Gamma_1 = \frac{Z_2 - Z_1}{Z_2 + Z_1} \quad (8)$$

When  $\epsilon_r > 1$ , it can be shown there exists at least one frequency at which equation (7) is nearly zero, indicating that this is a place where the impedance match looking into the evanescent section around septum 14 of waveguide 20 is good.

An example is shown in FIG. 2 for 0.5 inch long Teflon-type samples ( $\epsilon_r = 2.5$ ) placed in a WR90 standard rectangular waveguide ( $a = 0.900$  inches,  $b = 0.400$  inches). In FIG. 2, the value of  $|S_{11}| = 20 \cdot \log_{10}(|\Gamma_1|)$  for apparatus 10 versus frequency is plotted. The location of minimum 26 can be easily and accurately measured using a network analyzer. The location of minimum 26 in FIG. 2 is a strong function of  $\epsilon_r$ , but is not a strong function of  $L$ , the length of samples 12. This means that it is possible to establish an accurate one-to-one correspondence between the location of minimum or spike 26 in the response and the value of  $\epsilon_r$ , without having to accurately measure the length  $L$  of samples 12. (Note: The length  $L$  of samples 12 determines the number of such spikes in the  $|S_{11}|$  response, but does not appear to play a major role in the location of the lowest order spike 26.) This



1 correspondence has been computed for a nominal sample length of  
2 0.500 inches in a WR90 standard rectangular waveguide and is  
3 shown in FIG. 3, which may be utilized for visually determine  $\epsilon_r$ ,  
4 from minimum 26. It is worth noting in FIG. 3, that it can be  
5 seen that a small change in  $\epsilon_r$  will give an appreciable change in  
6 the location of spike 26, making accurate characterization of the  
7 sample possible.

8 FIG. 4 shows the results of a test of the present invention  
9 wherein apparatus 10 is utilized to determine the  $\epsilon_r$  of samples  
10 of an unknown material placed therein. The minimum in  $|S_{11}|$  takes  
11 place at 8.83 GHz. Therefore, FIG. 3 visually indicates a  
12 dielectric constant of around 2.66. The material was in fact a  
13 fiberglass reinforced polystyrene plastic, and its dielectric  
14 constant is known to be in the vicinity of 2.62. The  
15 measurement, then, is in good agreement with the known properties  
16 (within 1.5%).

17 In summary of the operation of apparatus 10, one example of  
18 the method of use provides for preparing two samples 12 of  
19 material that may be 0.45 inches wide, 0.400 inches tall, and  
20 0.500 inches long. The two samples 12 are inserted into  
21 waveguide 20 on either side of septum 14 as indicated in FIG. 1  
22 whereupon outer fixtures 16a and 16b are closed together using  
23 guide pins 18 and preferably tightened with screws. FIG. 5 shows  
24 waveguide to coax adapters 40 and 41 are connected to each end of

1 waveguide 20. Using stand coax cables 42, waveguide 10 is then  
2 connected to a calibrated vector network analyzer 44. The vector  
3 network analyzer is an important tool for measuring the complex  
4 impedance of a circuit at a given frequency. In this case, an HP  
5 8720C network analyzer was utilized. The HP 8720C is a high  
6 performance microwave vector network analyzer used for  
7 measurements of reflection and transmission parameters of  
8 circuits or systems. This analyzer covers a frequency range of  
9 50 MHz to 20 GHz. The position of the lowest order spike in the  
10  $|S_{11}|$  response is located. Then the graph of FIG. 3 or the  
11 equations provided hereinbefore are utilized to compute  $\epsilon_r$ .

12 It will be understood that many additional changes in the  
13 details, materials, steps and arrangement of parts, which have  
14 been herein described and illustrated in order to explain the  
15 nature of the invention, may be made by those skilled in the art  
16 within the principle and scope of the invention as expressed in  
17 the appended claims.

2

3

EVANESCENT WAVEGUIDE APPARATUS AND METHOD FOR

4

MEASUREMENT OF DIELECTRIC CONSTANT

5

6

ABSTRACT OF THE DISCLOSURE

7

A dielectric constant waveguide measuring apparatus

8

preferably comprises a rectangular waveguide aperture on each end

9

with a width  $a$  and height  $b$ . The waveguide frame is preferably

10

split to permit the waveguide to be opened for insertion of the

11

unknown material into a middle reduced cross-sectional area

12

portion of the waveguide frame. In one embodiment, a metal

13

septum is inserted between two samples of the unknown material to

14

thereby reduce the cross-sectional area of the waveguide aperture

15

by splitting width  $a$  of the rectangular waveguide in half. The

16

waveguide frame is closed and a frequency response of the

17

waveguide is then measured. The dynamic dielectric constant of

18

the unknown material is determined from the frequency of the

19

lowest order minimum value of the frequency response of the

20

waveguide apparatus wherein the unknown material has been

21

inserted.

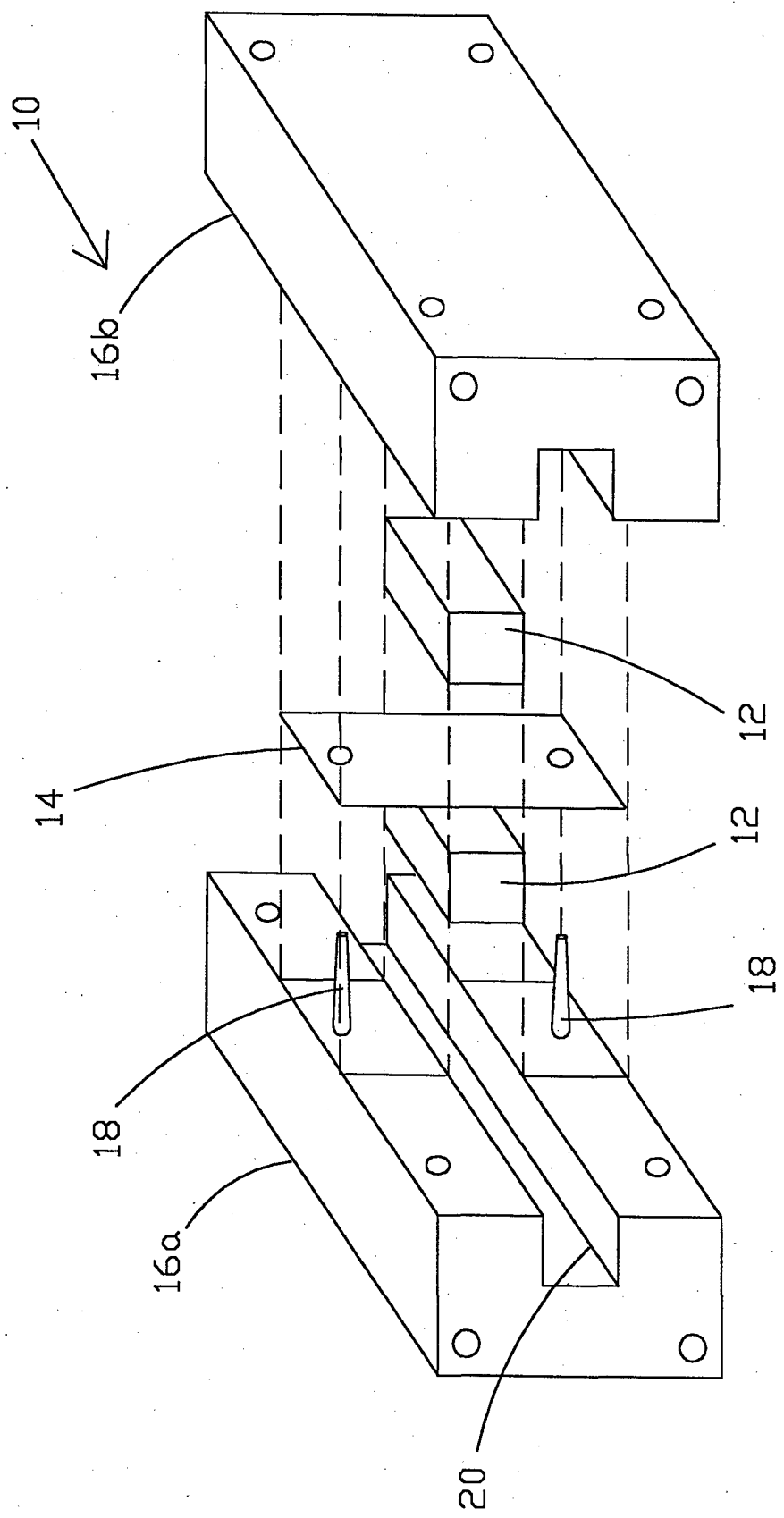


FIG. 1a

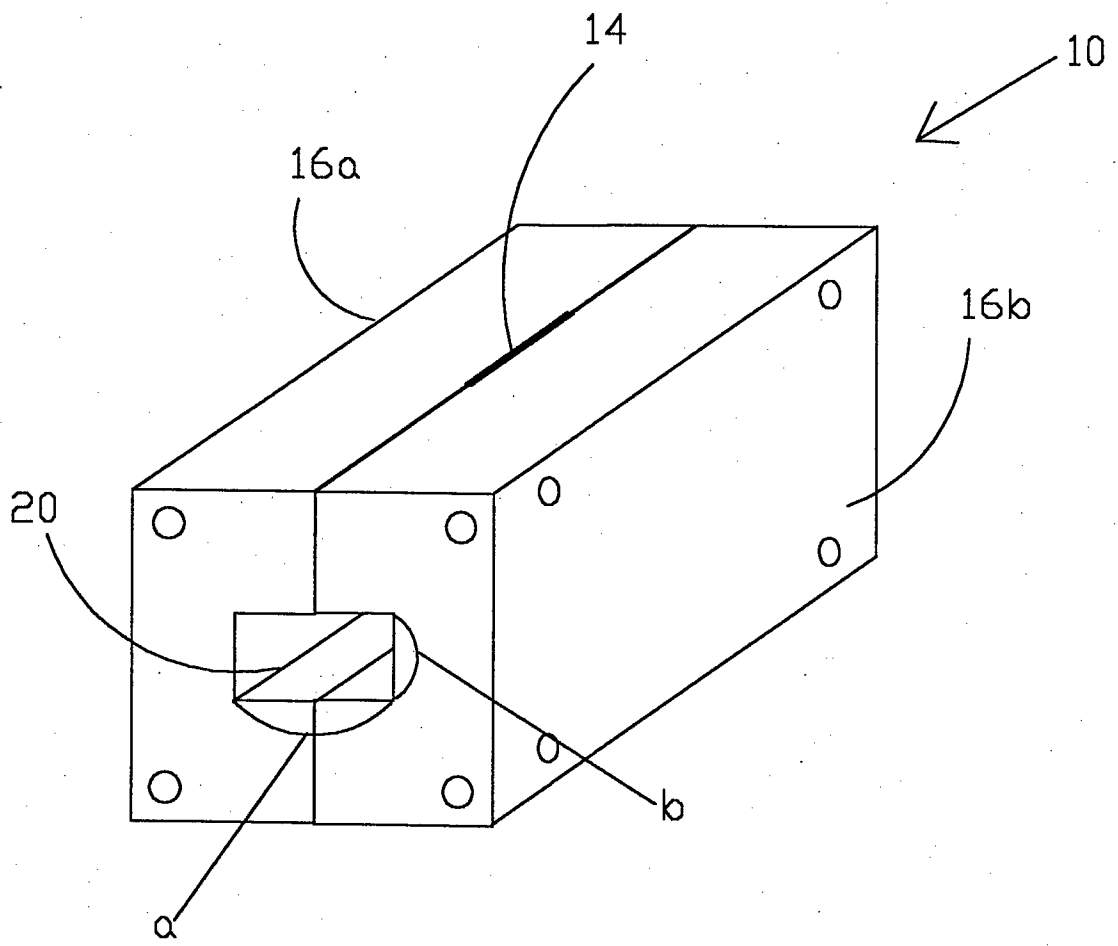


FIG. 1b

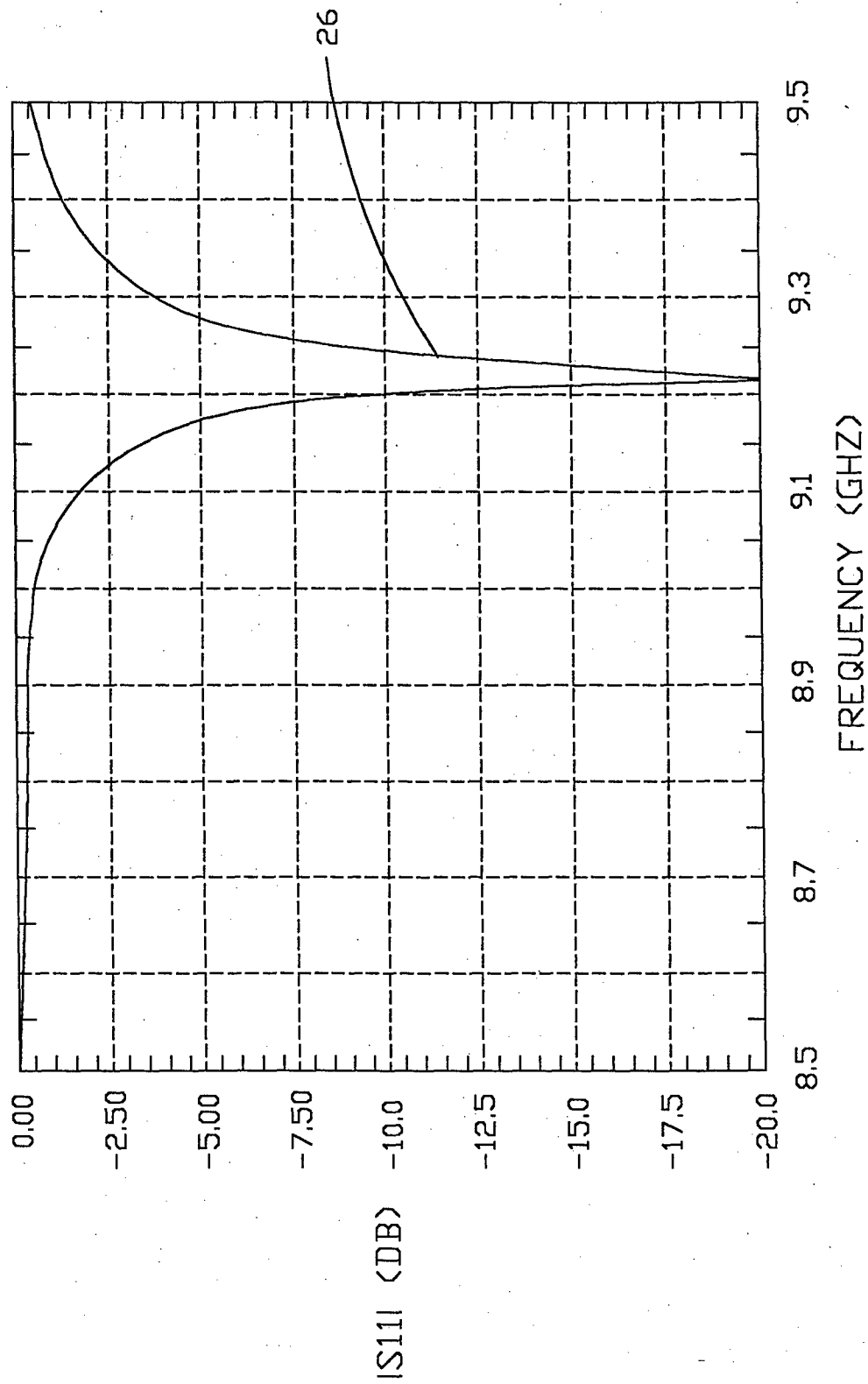
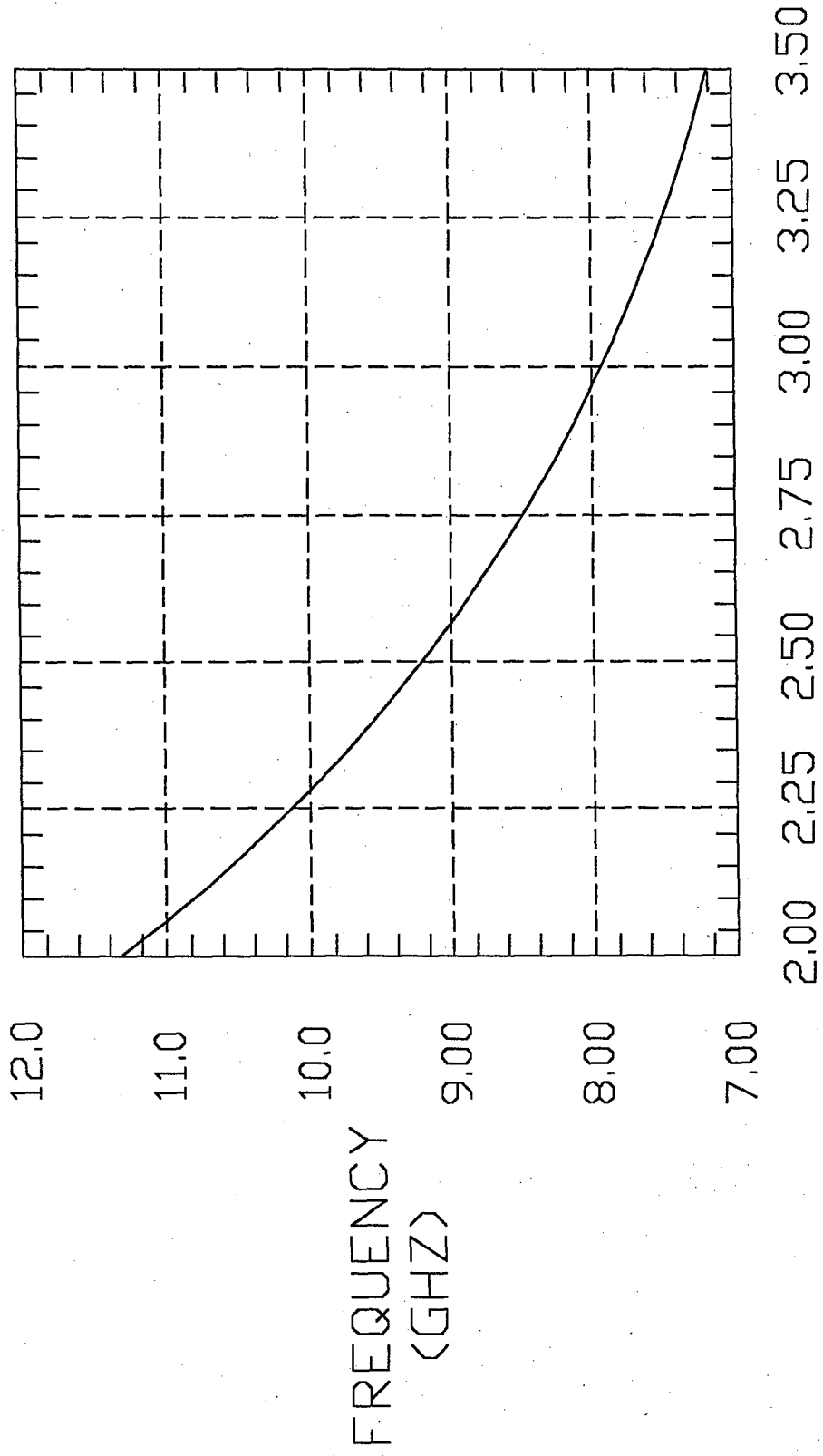


FIG. 2



$\epsilon_r$

FIG. 3

|S11| (DB)

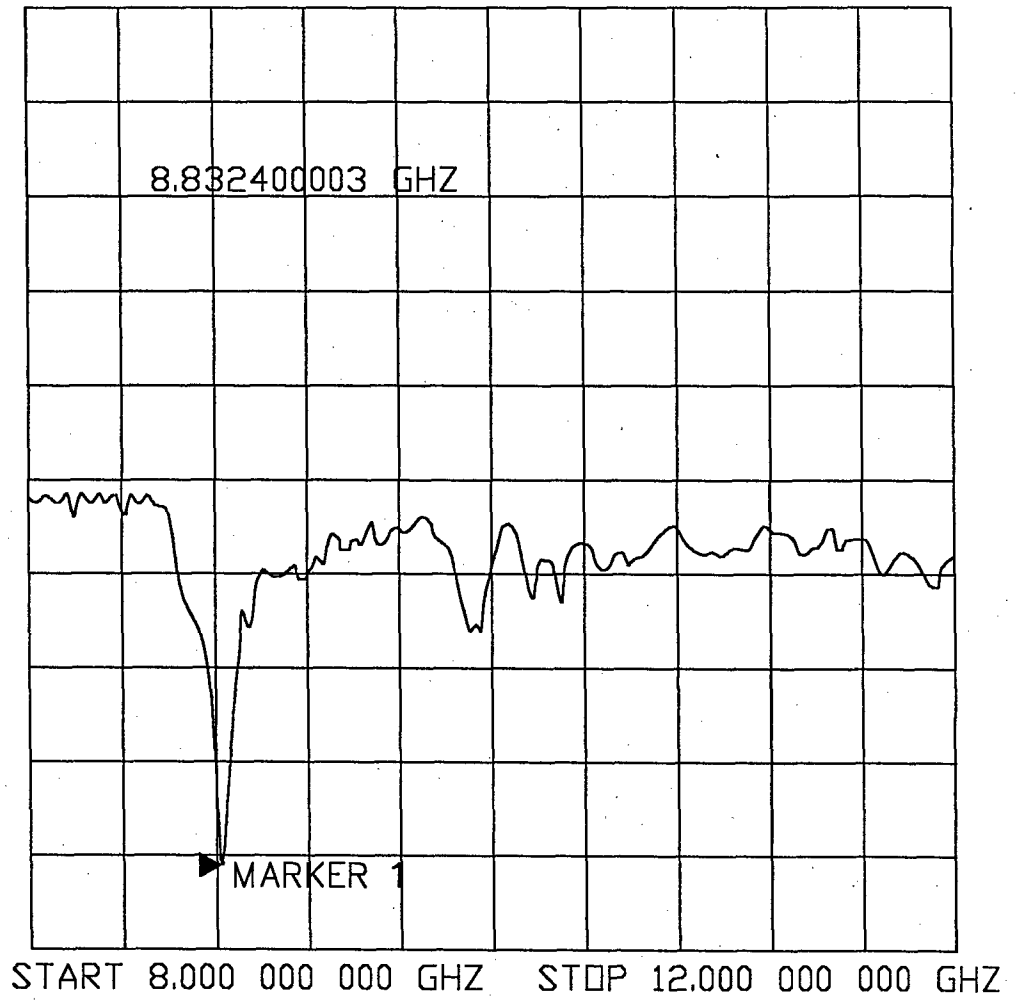


FIG. 4



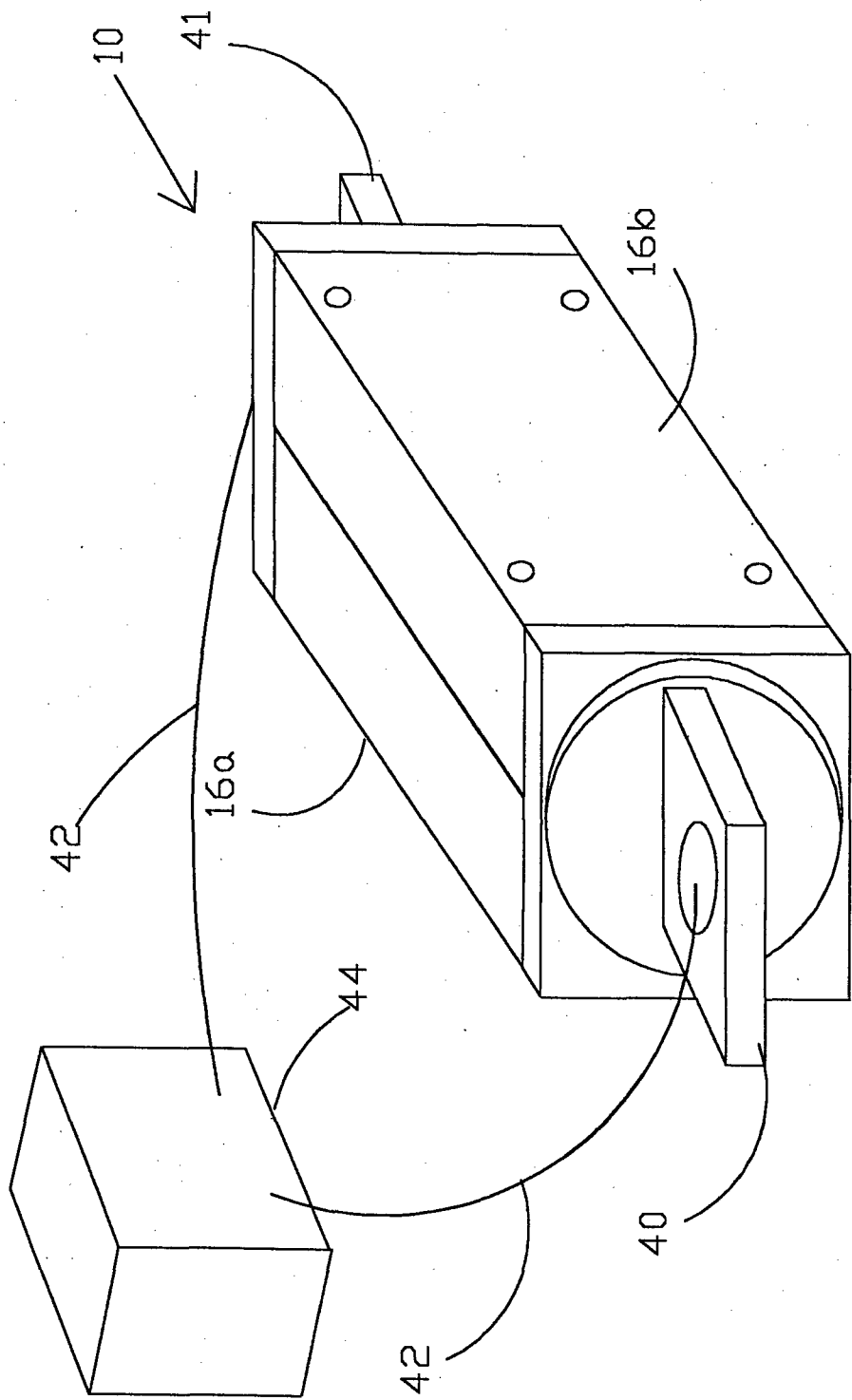


FIG. 5