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Attorney Docket No. 80067

METHOD AND APPARATUS FOR ACTIVE

SONAR DETECTION ENHANCEMENT

TO ALL WHOM IT MAY CONCERN:

BE IT KNOWN THAT (1) RICHARD A. KATZ and (2) ALBERT H. NUTTALL, employees of the United States Government, citizens of the United States of America, and residents of (1) East Lyme, County of New London, State of Connecticut, and (2) Old Lyme, County of New London, State of Connecticut, have invented certain new and useful improvements entitled as set forth above of which the following is a specification.

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Attorney Docket No. 80067 1 2 METHOD AND APPARATUS FOR ACTIVE 3 4 SONAR DETECTION ENHANCEMENT 5 STATEMENT OF THE GOVERNMENT INTEREST 6 The invention described herein may be manufactured and used 7 by or for the Government of the United States of America for 8 Governmental purposes without the payment of any royalties 9 10 thereon or therefore. 11 12 BACKGROUND OF THE INVENTION (1) Field of the Invention 13 The present invention relates generally to systems and 14 methods for active sonar systems and, more particularly, to a 15 sonar system and method for improved active sonar detection by 16 accurate estimation of the channel/target nonlinear response 17 function. 18 (2) Description of the Prior Art 19 Active sonar signal propagation and reflection has 20 intrinsic properties that are noticeably affected by the channel 21 and/or target characteristics. Often, one knows, through 22 measurements, the signal transmitted into the propagation 23 channel and the waveform at the receiver output. The difficulty 24

is to accurately measure and estimate what happens between the
 excitation input and output.

Signal distortion in an active sonar system may arise for 3 many reasons such as, for example, shallow basins with nonlinear 4 boundary conditions, irregular sea bottoms and surface 5 interactions, bubble formations and nonlinear scattering within 6 7 the propagation channel, reverberation, nonhomogeneities in sound speed propagation, inelastic target response, target 8 scattering profiles, multipath reflections, additive noise 9 10 generated by waves, transmission losses, changing distances from the target, and the like. 11

Active sonar as used herein refers to sonar systems that 12 utilize radiating acoustic sources to probe an area to be 13 searched so as to acoustically illuminate the submerged object. 14 One example of this type of sonar system is a conventional sonar 15 device, wherein a highly directional beam of sonic energy 16 periodically radiates from a scanning transducer, which in turn 17 operates as a receiver to detect echoes reflected from any 18 object(s) within the propagation channel. Modern active sonar 19 systems commonly provide multibeam capabilities as well. Active 20 sonar signals can have relatively high transmission losses which 21 increase as a function of the frequency of the propagated 22 23 energy.

1 A large number of active sonar data processing techniques rely on linearity in an acoustic signature (e.g., temporal 2 fluctuations, power spectra) for extracting and identifying 3 4 information about a particular target illuminated by the active transmission. However, if linear techniques are applied to a 5 target-of-interest in which the target and/or channel response 6 is actually nonlinear, then subsequent purely linear processing 7 of these data leads to results that are incorrect and can be 8 9 misleading.

10 Various inventors have attempted to solve the above and 11 related problems as evidenced by the following patents.

U.S. Patent No. 6,285,972 B1, issued September 4, 2001, to A. J. Barber, discloses a method for generating an improved nonlinear system model that includes generating a linear system model and using a response therefrom to generate the nonlinear system model. A method and system for generating drive signals for a test system uses the improved nonlinear system model or a conventional nonlinear system model.

U.S. Patent No. 6,327,315 B1, issued December 4, 2001, to
O. Purainen, discloses a method for estimating an impulse
response and a receiver in a radio system where the signal to be
sent comprises a known training sequence, which receiver
comprises means for sampling the received signal, and means for

1 calculating a first estimate for the impulse response by means of the known training sequence. To enable an accurate 2 determination of the impulse response, the receiver comprises 3 4 means for making preliminary decisions on the received samples by means of the first impulse response estimate, means for 5 calculating an error value of the estimated samples and the 6 received samples calculated by means of the preliminary 7 decisions, means for calculating a second estimate of the 8 impulse response by minimizing said error value, and means for 9 calculating a new estimate for the impulse response, by 10 combining the first and second estimates with each other. 11 U.S. Patent No. 6,275,523 B1, issued August 14, 2001, to 12 Chen et al., discloses a system for in-service nonlinearity 13 measurements that measures such nonlinearities by way of 14 comparing received linear error-corrected unfiltered signal 15 samples with re-generated reference signal samples to calculate 16 magnitude and phase nonlinear error values. Linear distortion is 17 removed from the received signal samples in order to truly 18 characterize nonlinear behavior of the transmitter. The linear 19 error-corrected received signal samples are generated without 20 applying the receiver shaping filtering. Reference signal 21 samples are re-generated from estimated transmitted symbols from 22 the unfiltered linear error-corrected received signal samples. 23 24 The transmitted symbols are estimated using a multi-region

1 slicer which dynamically estimates constellation decision levels
2 from the unfiltered signal samples. A weighted, least-square
3 based polynomial regression is performed on magnitude and phase
4 nonlinear error values in order to estimate magnitude and phase
5 nonlinear error functions while suppressing the impact of other
6 non-systematic distortions.

7 The above cited prior art does not provide a means for 🖉 accurately measuring and estimating what occurs between the 8 9 excitation input produced by the acoustic transmitter and output or received response. Consequently, there remains a long felt 10 11 but unsolved need for an improved means for improved techniques to determine the channel/target response function, including 12 nonlinear effects therein. Those skilled in the art will 13 appreciate the present invention that addresses the above and 14 other problems. 15

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SUMMARY OF THE INVENTION

Accordingly, it is an object of the present invention to provide an improved active sonar detection apparatus and method. Another object of the present invention is to provide a method and apparatus to determine a channel/target nonlinear response function and/or the significance of the effect of nonlinearities in the channel/target response function.

These and other objects, features, and advantages of the 1 present invention will become apparent from the drawings, the 2 descriptions given herein, and the appended claims. However, it 3 will be understood that the above listed objects and advantages 4 5 of the invention are intended only as an aid in understanding aspects of the invention, and are not intended to limit the 6 invention in any way, and do not form a comprehensive list of 7 8 objects, features, and advantages.

In accordance with the present invention, a method for 9 enhancing active sonar is provided by determining optimum 10 detector. This includes providing a controlled excitation 11 signal for in-water transmission of an acoustic signal and 12 receiving a response signal produced in response to said in-13 water transmission of said acoustic signal. The method then 14 calculates a Wiener/Volterra kernel from the excitation signal 15 and response signal. Any Wiener/Volterra kernels related to 16 random noise contributions are omitted. The optimum detector is 17 determined by using the remaining Wiener/Volterra kernels to 18 give an optimal correlation between the excitation signal and 19 20 the response signal. Additional details are provided for determining different orders of Wiener/Volterra kernels. 21

The method may further comprise comparing a power of the response signal to the residual power to determine the contribution of nonlinearity to the total response signal. In a

preferred embodiment, the Volterra/Wiener expansion is limited
 to third order using the above described remaining
 Wiener/Volterra kernels which are represented by the following
 equation:

$$y(t) = h_0 + \int d\tau_1 h_1(\tau_1) x(t-\tau_1) + \int \int d\tau_1 d\tau_2 h_2(\tau_1,\tau_2) x(t-\tau_1) x(t-\tau_2) + \int \int \int d\tau_1 d\tau_2 d\tau_3 h_3(\tau_1,\tau_2,\tau_3) x(t-\tau_1) x(t-\tau_2) x(t-\tau_3)$$

The invention may also comprise a system or apparatus for 6 active sonar detection which may comprise one or more features 7 such as, for instance, an in-water transmitter operable to 8 produce an excitation signal for transmission of an acoustic 9 signal, a receiver to receive a response signal, a model for 10 operating on the excitation signal and the response signal, and 11 a nonlinear processor operable for computing h_0 , h_1 , h_2 , and h_3 12 13 from the above described equation.

The nonlinear processor is preferably operable for 14 measuring the response signal when the excitation signal is 15 zero, for purposes of determining h_0 . The nonlinear processor is 16 preferably operable for measuring the response signal while 17 controlling the excitation signal to be real white Gaussian 18 noise at different power factor levels to thereby compute h_1 . 19 Furthermore, the nonlinear processor is operable for utilizing a 20 correlation between the excitation signal and the response 21 signal for determining h_2 . The nonlinear processor can also 22 utilize a second correlation between the excitation signal and 23

1 the response signal for determining h_3 . The nonlinear processor 2 can utilize h_0 , h_1 , h_2 , and h_3 , for determining a residual power. 3 The nonlinear processor can also compare a power of the response 4 signal to the residual power to determine the total contribution 5 of nonlinear components to the response signal.

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BRIEF DESCRIPTION OF THE DRAWINGS

A more complete understanding of the invention and many of the attendant advantages thereto will be readily appreciated as the same becomes better understood by reference to the following detailed description when considered in conjunction with the accompanying drawings wherein corresponding reference characters indicate corresponding parts throughout several views of the drawings and wherein:

FIG. 1 is a block diagram view which shows a sonar detection enhancement system in accord with the present invention; and

FIG. 2 is a schematic diagram view which shows a model for nonlinear sonar signal propagation in accord with the present invention.

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22 BRIEF DESCRIPTION OF THE PREFERRED EMBODIMENTS 23 The proposed system and method of signal detection 24 enhancement incorporates a Wiener/Volterra model for

characterizing the channel/target response function from an
 acoustic time series measurement of the output response of a
 receiving hydrophone element or array, given a known white
 Gaussian pseudo-random noise excitation input.

5 Referring now to the drawings, and more specifically to 6 FIG. 1, there is provided a block diagram for the sonar 7 detection enhancement method and apparatus 10 in accord with the 8 present invention.

In a presently preferred embodiment, a Wiener/Volterra 9 series expansion is provided for a given excitation x(t) which 10 is indicated as input x(t) 12 in FIG. 1, and response y(t) as 11 indicated as response y(t) 14 in FIG. 1. The details of a 12 presently preferred embodiment of the invention are discussed in 13 detail below. However, as an aid to understanding, a brief 14 summary of operation is given at this time. Input 12 and 15 response 14 are applied to model 16, which is shown in more 16 detail in FIG. 2. The output of model 16 is applied to 17 nonlinear processor 18. Nonlinear processor 18 is utilized to 18 determine kernels $h_0,\ h_1,\ h_2,\ \text{and}\ h_3$ as indicated at 20, 22, 24, 19 and 26. Computed residual 28 may be determined from the above 20 information. The computed residual may be utilized to determine 21 the importance of nonlinear components that arise due to the 22 environment of operation as well. If desired, an estimate can 23

also be provided for the signal and noise interference for a
 particular environment.

3	Accordingly, a very general model is initially used for
4	determining channel/target response from acoustic time series
5	measurements. Starting with the most general case, time
6	variation of the channel is incorporated and a variety of
7	additive and multiplicative noise types are considered. For
8	practical considerations, both of these conditions are relaxed
9	hereinafter as discussed subsequently.
10	$y(t) = h_0(t) + \sum_{K} \int \dots^{(K)} \int d\tau_1 \dots d\tau_K h_K(t;\tau_1,\dots,\tau_K) x(t-\tau_1) \dots x(t-\tau_K) $ (1)
11	From equation (1), one deduces a variety of noise types:
12	$h_0(t) = h_{0D} + h_{0R}(t)$ (2)
13	where: h_{0D} is a constant additive deterministic component,
14	and
15	$h_{0R}(t)$ is a stationary random process of zero mean
16	(without loss of generality).
17	Note that $h_{0R}(t)$ takes the place of additive noise, $n(t)$. Next
18	consider:
19	$h_1(t; \tau_1) = h_{1D}(\tau_1) + h_{1R}(t; \tau_1)$ (3)
20	where: $h_{1D}(\tau_1)$ is a nonrandom first-order deterministic
21	filter, and
22	$h_{1R}(\texttt{t}; \ \tau_1)$ is a stationary random process of zero mean
23	(without loss of generality).

1 The output corresponding to $h_{1R}(t; \tau_1)$ is given by the following 2 expression:

3
$$y_{1R}(t) = \int d\tau_1 h_1(t;\tau_1) x(t-\tau_1)$$
 (4)
4 where the integrand of equation (4) represents
5 multiplicative noise of first-order.
6 Similarly, we can have multiplicative noise of second-order
7 by breaking $h_2(t; \tau_1, \tau_2)$ into a deterministic and a random
8 component. For the higher-order kernels, one obtains:
9 $h_R(t; \tau_1,..., \tau_R) = h_{RD}(\tau_1,..., \tau_R) + h_{RR}(t; \tau_1,..., \tau_R)$ (5)
10 where: $h_{RD}(\tau_1,..., \tau_R)$ is a K-th order deterministic filter,
11 and
12 $h_{RR}(t; \tau_1,..., \tau_R)$ is a random filter of zero mean
13 (without loss of generality).
14 Note that the latter term on the right-hand side of equation (5)
15 yields multiplicative noise of order K.
16 For problems of practical interest in sonar applications, a
17 time-invariant environment is assumed. Therefore, to simplify
18 the analysis, all random noise contributions, $h_{RR}(t; \tau_1,..., \tau_R)$ are
19 disregarded. These omissions are accepted as the natural
20 contributions to measurement and estimation errors induced by
21 the model. This leads to the following expression:
22 $y(t) = h_0 + \sum_R \int ...^{(K)} \int d\tau_1...d\tau_R h_R(\tau_1,...,\tau_R) x(t-\tau_1)...x(t-\tau_R)$ (6)

The kernels, $\{h_{K}(\tau_{1},...,\tau_{K})\}$, are represented in this sonar 1 context by the channel response, target response, or interaction 2 of the two together. The aim is to evaluate contributions up to 3 and including third order which would yield complete information 4 on h_1 , h_2 , and h_3 . If the actual sonar system is greater than 5 third order, the kernel estimates will be biased. It is 6 presently believed that third-order estimates will be sufficient 7 for most practical applications. For this case, it is also 8 assumed that the random processes x(t) and y(t) are stationary. 9 10 Another point of note is that the kernels in the above expression can be taken to be symmetric, without loss of 11 generality. That is to say, the order of the arguments is 12 immaterial. 13

14 The main goal, in this presently preferred embodiment, is 15 to obtain a solution for the kernels $\{h_K(\tau_1,...,\tau_K)\}$, K \leq 3, while 16 considering a time-invariant system of order 3. For example, if 17 we restrict the general equation (6) to a third-order system, we 18 obtain explicitly (for no additive noise) a presently preferred 19 model as indicated at 16 in FIG. 1, shown in more detail in FIG. 20 2, and described by the following equation:

21
$$y(t) = h_0 + \int d\tau_1 h_1(\tau_1) x(t - \tau_1) + \iint d\tau_1 d\tau_2 h_2(\tau_1, \tau_2) x(t - \tau_1) x(t - \tau_2) + \iint d\tau_1 d\tau_2 d\tau_3 h_3(\tau_1, \tau_2, \tau_3) x(t - \tau_1) x(t - \tau_2) x(t - \tau_3)$$
(7)

22 where the subscript "D" has been suppressed for convenience.

1 This equation provides the basis of model 16, as shown in FIG. 2 2, which is limited, in this presently preferred embodiment, to 3 a third-order system of the general equation (6). Thus, linear 4 elements 30, quadratic elements 32, cubic elements 34, and Kth 5 order elements 38 may be added within summation unit 36 to 6 produce a model output that is applied to nonlinear processor 7 18.

8 With the presently preferred model 16 in mind, the9 following cases are now considered.

10 Case I:

11 If x(t) = 0 for all t then:

12

22

This allows for explicit determination of h₀ as indicated at 14 20 in FIG. 1 within nonlinear processor 18. 15 Case II:

 $y(t) = h_0$.

(8)

Let excitation x(t) be real white Gaussian noise of spectral level, ρ watts/Hz, and y(t) is the observed response. Consider cross-correlation, $C(\tau_a) \equiv \overline{(y(t)x(t-\tau_a))}$. The overbar is an ensemble average over many realizations. In actual use, an acceptable practice is to take the sample mean in place of the ensemble mean.

$$\overline{y(t)x(t-\tau_{a})} = \rho h_{1}(\tau_{a}) + \rho^{2} \iiint d\tau_{1} d\tau_{2} d\tau_{3}(\tau_{1},\tau_{2},\tau_{3}) [\delta(\tau_{1}-\tau_{2})\delta(\tau_{a}-\tau_{3}) + \delta(\tau_{1}-\tau_{3})\delta(\tau_{a}-\tau_{2}) + \delta(\tau_{a}-\tau_{1})\delta(\tau_{2}-\tau_{3})] = \rho h_{1}(\tau_{a}) + 3\rho^{2} \int d\tau_{1} h_{3}(\tau_{1},\tau_{2},\tau_{a}).$$
(9)

- 1 If the system is only second-order, the last term on the 2 right-hand side of equation (9) is zero and the equation is 3 reduced accordingly.
- 4 Case III:

7

5 The higher order correlation where $\tau_a \neq \tau_b$ is obtained as 6 follows:

$$\overline{y(t)x(t-\tau_{a})x(t-\tau_{b})} = h_{0}\rho\delta(\tau_{a}-\tau_{b}) + \rho^{2} \iint d\tau_{1}d\tau_{2}h_{2}(\tau_{1},\tau_{2})[\delta(\tau_{1}-\tau_{2})\delta(\tau_{a}-\tau_{b}) + \delta(\tau_{1}-\tau_{a})\delta(\tau_{2}-\tau_{b}) + \delta(\tau_{1}-\tau_{b})\delta(\tau_{2}-\tau_{a})]$$

$$= h_{0}\rho\delta(\tau_{a}-\tau_{b}) + \rho^{2}[\delta(\tau_{a}-\tau_{b})\int d\tau_{1}h_{2}(\tau_{1},\tau_{1}) + 2h_{2}(\tau_{a},\tau_{b})]$$

$$= [h_{0} + \rho \int d\tau_{1}h_{2}(\tau_{1},\tau_{1})]\rho\delta(\tau_{a}-\tau_{b}) + 2\rho^{2}h_{2}(\tau_{a},\tau_{b})$$

$$= \overline{y(t)}\rho\delta(\tau_{a}-\tau_{b}) + 2\rho^{2}h_{2}(\tau_{a},\tau_{b}).$$
(10)

8 This allows for determination of $h_2(\tau_a, \tau_b)$ at any τ_a, τ_b pair of 9 interest. Thus, h_2 can be determined as indicated at 24 in 10 nonlinear processor 18 of FIG. 1

11 Case IV:

12 Consider the higher order correlation, $\overline{y(t)x(t-\tau_a)x(t-\tau_b)x(t-\tau_c)}$, 13 where $\tau_{a} \neq \tau_{b} \neq \tau_{c}$:

$$\overline{y(t)x(t-\tau_{a})x(t-\tau_{b})x(t-\tau_{c})} = \rho^{2}[h_{1}(\tau_{a})\delta(\tau_{b}-\tau_{c})+h_{1}(\tau_{b})\delta(\tau_{a}-\tau_{c})+h_{1}(\tau_{c})\delta(\tau_{a}-\tau_{b})]
+3\rho^{3}\int d\tau_{1}h_{3}(\tau_{1},\tau_{1},\tau_{a})\delta(\tau_{b}-\tau_{c})+3\rho^{3}\int d\tau_{1}h_{3}(\tau_{1},\tau_{1},\tau_{b})\delta(\tau_{a}-\tau_{c})
+3\rho^{3}\int d\tau_{1}h_{3}(\tau_{1},\tau_{1},\tau_{c})\delta(\tau_{a}-\tau_{b})+6\rho^{3}h_{3}(\tau_{a},\tau_{b},\tau_{c})$$

$$(11)$$

$$= \rho[C(\tau_{a})\delta(\tau_{b}-\tau_{c})+C(\tau_{b})\delta(\tau_{a}-\tau_{c})+C(\tau_{c})\delta(\tau_{a}-\tau_{b})]
+6\rho^{3}h_{3}(\tau_{a},\tau_{b},\tau_{c}).$$

15 This allows for determination of $h_3(au_a, au_b, au_c)$ at any arguments of

1 interest, so that h_3 can be determined as indicated at 26 in 2 nonlinear processor 18 of FIG. 1.

3	To summarize the model, mean value, $y(t)$, provides
4	information on $\int d au_1 h_2(au_1, au_1)$, while $\overline{y(t)x(t- au_a)}$ provides information on
5	$\int d au_1 h_3(au_1, au_1, au_1, au_a)$. Note that because these expressions are integrals,
6	only partial information on the kernels themselves is yielded.
7	Moreover, higher-order correlations are used to determine $h_2(au_a, au_b)$
8	and $h_1(\tau_a, \tau_b, \tau_c)$ for any arguments $\tau_a \neq \tau_b \neq \tau_c$.

By measuring $\overline{y(t)x(t-\tau_a)}$, one can extract information about $h_1(\tau_a)$, and as already stated, h_0 is determined by setting x(t) =10. The sum of all the nonlinear components, which will be 12 referred to as the nonlinear residual (as indicated at 28 in 13 FIG. 1), r(t), is defined according to the following equation:

 $r(t) \equiv y(t) - h_0 - \int d\tau_1 h_1(\tau_1) x(t - \tau_1).$ (12)

If it turns out that the power in the residual, r(t), is 15 significantly lower than the power in the measured total system 16 output y(t), then one could conclude that the total contribution 17 of the nonlinear components in y(t) is inconsequential. On the 18 other hand, if the totality of nonlinear components in y(t) are 19 substantial, then the system nonlinearity is of paramount 20 importance. It is most likely that the relative degree of 21 nonlinearity for a particular sonar problem of interest will be 22

highly situationally dependent. That is to say, it will depend on environmental conditions, source and receiver measurement geometry, oceanography, target characteristics, the acoustic waveform(s) under consideration as well as their absolute levels, and combinations of all these variables.

Given a solution for kernels, $\{h_k(\tau_{\dots})\}$, the detection 6 enhancement feature of the method of the present invention falls 7 out immediately, because the channel/target response can be used 8 as an optimum predictor to estimate the signal and noise 9 interference for determining the likelihood ratio (LR) processor 10 for a particular environment. In other words, the kernels can 11 be used to remove the effects the transmission channel has on 12 the input and give the sonar operator a clearer view of the 13 target. 14

Thus, the proposed method has an advantage over 15 conventional methods in that the kernels, $\{h_k(\tau...)\}$, are 16 determined empirically from the Wiener/Volterra model using 17 measured values of the excitation input and receiver output. By 18 knowing the channel/target response (i.e., the kernels, $\{h_k(\tau_{--})\}$, 19 one can determine the probability density distributions with 20 which to calculate the optimum LR processor for a prescribed 21 22 signal environment.

1 The active sonar detection enhancement method and apparatus 2 is applicable to any situation which utilizes the transmission, 3 propagation, and reception of active underwater acoustic 4 signals. It is particularly useful in environments in which 5 nonlinearity may be the dominant factor, such as shallow basins 6 with nonlinear boundary conditions.

7 Therefore, it will be understood that many additional 8 changes in the details, materials, steps and arrangement of 9 parts, which have been herein described and illustrated in order 10 to explain the nature of the invention, may be made by those 11 skilled in the art within the principle and scope of the 12 invention as expressed in the appended claims.

1 Attorney Docket No. 80067

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METHOD AND APPARATUS FOR ACTIVE SONAR 3 DETECTION ENHANCEMENT 4 5 ABSTRACT OF THE DISCLOSURE 6 7 The present invention provides a method and apparatus for enhancing active sonar signal detection by estimating the 8 channel/target response utilizing measured values of the 9 excitation signals and received signals. A Wiener/Volterra 10 series expansion for the excitation and received signals is used 11 as a model, wherein a time invariant environment is assumed, 12 thereby disregarding all random noise contributions. The 13 Wiener/Volterra kernels are then determined in a nonlinear 14 processor using a method of correlations which is designed to 15 produce the kernels utilizing only measured white Gaussian 16 excitation signals and received signals. The kernels can be 17 used to give an optimum correlation between the excitation 18 signals and the received signals. 19



FIG. 1

