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2
3 ROUTE PLANNER WITH AREA AVOIDANCE CAPABILITY
4

5 STATEMENT OF GOVERNMENT INTEREST

6 The invention described herein may be manufactured and used by or
7 for the Government of the United States of America for
8 governmental purposes without the payment of any royalties
9 thereon or therefor.
10

11 CROSS-REFERENCE TO RELATED PATENT APPLICATIONS

12 Not applicable.
13

14 BACKGROUND OF THE INVENTION

15 (1) Field of the Invention

16 This invention generally relates to navigational systems and
17 more specifically to the generation of a route with intermediate
18 way points that avoid predetermined areas.

19 (2) Description of the Prior Art

20 A number of navigation systems exist that have the
21 capability of plotting a course from an initial point to a
22 destination. Often times these courses involve individual paths
23 or legs to intermediate way points. Many of these systems take
24 into account various terrain features in plotting such a course
25 and locating particular way points.

26 For example, United States Letters Patent No. 4,812,990
27 (1989) to Adams et al. discloses a system and method for

1 determining the optimal path for an aircraft. A two-dimensional
2 reference grid is constructed so that a first position is in the
3 center of a first rank of the grid and a second position is
4 adjacent to the center cell of the last rank. Dynamic
5 programming techniques enable the determination of possible
6 flight paths between the first and second positions and the
7 selection of a path of minimum cost. Possible flight paths are
8 constructed by identifying possible connections between the last
9 rank and the second position and then between each pair of
10 adjacent ranks, working backward from the last rank to the first
11 position in the first rank. A possible connection is deemed to
12 exist when an aircraft can fly from one point to a target point,
13 as between specified cells and adjacent ranks, and arrive at the
14 target point within particular heading limits without exceeding a
15 predetermined maximum lateral exhilaration of the aircraft.
16 Corresponding heading limits are determined for each connected
17 cell on the grid so that all possible flight paths are examined
18 consistent with preselected heading limits at the second position
19 and the maximum lateral exhilaration allowed for the aircraft.
20 In essence therefore, this patent discloses a system that
21 establishes a flight path with intermediate way points that take
22 into account certain constraints on the aircraft.

23 United States Letters Patent No. 5,086,396 (1992) to
24 Waruazewski discloses an aircraft navigation system for use in
25 determining routes in unfamiliar terrain or in terrain having
26 hostile forces. The navigation system includes an inertial
27 navigation system, a map of the terrain with elevational

1 information stored in digitized format as a function of location,
2 a typical energy managed or narrow beam altimeter, a display
3 system and a central processing unit for processing data
4 according to preselected programs. The system operates to
5 maintain the true position of the aircraft with respect to the
6 digitized map. A display of the map and the aircraft provide
7 presentations useful to the navigation of the aircraft and enable
8 the aircraft to engage in terrain following procedures using only
9 the relatively difficult to detect altitude range finding
10 apparatus as a source of emitted electromagnetic radiation. The
11 navigation system, in conjunction with and information regarding
12 hostile anti-aircraft facilities, can provide a display
13 permitting an operator to determine a reduced risk flight path.
14 This patent therefore discloses a navigation system that provides
15 a means for enabling an aircraft operator to determine an
16 appropriate route to avoid particular areas.

17 United States Letters Patent No. 5,087,916 (1992) to
18 Metzдорff et al. discloses a method for navigating and updating
19 navigation information by means of range imaging processing and a
20 reference store that segmentizes range image data in order to
21 obtain a particular pattern of type features for purposes of
22 classifying particular types of objects across which the aircraft
23 flies. The system extracts particular signature features
24 including localized elevational jumps and determines the position
25 of the aircraft by correlating a plurality of features and their
26 spatial orientation to each other as extracted with corresponding
27 stored reference information. This provides a maximum fit that

1 is indicative of deviation of a flight from a flight path as
2 identified by reference information. Thus this patent discloses
3 a system that utilizes images and data base information
4 containing terrain features to determine flight deviation from a
5 predetermined path.

6 United States Letters Patent No. 5,187,667 (1993) to Short
7 discloses a tactical route planning method for determining
8 tactically sound paths or routes for vehicles from an initial
9 position to a goal position across a piece of terrain. The
10 system uses heuristic methods to select the most promising paths
11 by sorting a list using a minimum estimated total cost value. If
12 any of the list of paths reaches the goal it is selected.
13 Otherwise new paths are generated by moving from the position at
14 the end of the path to each of the adjacent terrain sections.
15 Thus this patent discloses a method of obtaining a final path
16 from a plurality of available paths.

17 United States Letters Patent No. 5,204,817 (1993) to Yoshida
18 discloses a car mounted navigation system that uses map data in
19 the form of polygons defined by roads of a predetermined rank or
20 more of significance to connect a starting polygon containing a
21 starting point to a destination polygon containing a destination
22 with a chain of polygons adjoining at common sides of each pair
23 of adjoining polygons and arranged between the starting and
24 destination polygons to compute a plurality of routes extending
25 from the starting point to the destination polygon. Each route
26 can include a combination of sides of the chained polygons, the
27 starting polygon and the destination polygon. A car operator

1 selects an appropriate route from the computed routes. Thus this
2 patent discloses a navigation system that divides an area into
3 polygonal structures for use in generating one of a possible
4 number of routes.

5 Generally, each of the foregoing applications discloses a
6 system that is capable of plotting a navigation route. However,
7 in each case the route can be plotted over an interval that is
8 not time dependent. That is, the initial and final points remain
9 fixed for a long period in comparison to the duration of an
10 event. Time dependence, however, becomes an issue when in a
11 dynamic situation such as determining a flight path for a missile
12 in a tactical situation where the launch site for the missile is
13 changing.

14 United States Letters Patent No. 3,990,657 (1976) to Schott
15 discloses a method and apparatus for reducing ballistic missile
16 range errors due to viscosity uncertainties. Predictions of
17 these errors provide a missile circular error probability in the
18 form of a ballistic position error ellipse. The ellipse can be
19 used to significantly improve performance by reducing error
20 probability. This patent therefore discloses the use of ellipses
21 in determining navigational information in a more dynamic
22 scenario.

23 United States Letters Patent No. 4,044,237 (1977) to Cowgill
24 et al. discloses a lifting body missile that is controlled by
25 pitch and roll commands. A yaw auto pilot is caused to change in
26 accordance with roll and estimated angle of attack input
27 information. Command logic determines the polarity of the

1 command signals to the auto pilot. This patent discloses onboard
2 real-time apparatus for improving the trajectory of a missile.

3 United States Letters Patent No. 4,529,151 (1985) to Skarman
4 discloses a method for steering an aerodynamic body in response
5 to a body control variable signal. Specifically, the system
6 responds to a signal value representing a line of sight angular
7 rate and a signal value representing a body attitude angular
8 rate. The two signal values are combined to form a signal value
9 of an error angle. A difference error angle signal value is
10 formed by an error angle measurement received from a homing
11 device. The approximate error angle signal is fed back to the
12 aerodynamic relationships in order to update the quantities of
13 the relationships. This patent therefore provides a guidance
14 system for moving a device from a launching point to a
15 destination point in response to a target device that is moving.

16 In summary, each of these references discloses various
17 approaches for guiding a vehicle from a starting point to a
18 destination point. However, none of these references discloses
19 any method or means for defining a route with intermediate way
20 points set to avoid particular areas. Further, none of these
21 references discloses any method or means for defining such a
22 route in situations where the location of a starting point or
23 distribution point may vary with time.

24 25 SUMMARY OF THE INVENTION

26 Therefore it is an object of this invention to provide a
27 method for establishing a route through a plurality of way points

1 positioned to avoid particular areas between a starting or launch
2 point and a destination point.

3 Another object of this invention is to provide a method for
4 establishing a route with intermediate way points between a
5 starting or launch point and a destination point that enables the
6 system to select the best possible route.

7 Still another object of this invention is to provide a
8 method for establishing a route with intermediate way points
9 between a starting or launch point and a destination point that
10 enables the system to select a best possible route on a real-time
11 basis.

12 Yet another object of this invention is to provide a method
13 for establishing a flight path for a missile with intermediate
14 way points between a starting or launch point and a destination
15 point that enables the system to select a best possible flight
16 path taking into account any constraints on the maneuverability
17 of the missile.

18 A method according to this invention establishes at least
19 one way point on a route for a steerable vehicle between a source
20 point and a destination point that avoids at least one
21 intermediate obstacle or area by defining first and second
22 bearing lines from the source point to first and second tangents
23 of each obstacle. Each of the bearing lines is extended an
24 incremental distance beyond its tangent point with the area to
25 define a potential way point. Thereafter each potential way
26 point is converted to a way point for a route.

1 According to another aspect of this invention, a route is
2 established for a missile between a launch point and a
3 destination point that avoids at least one intermediate landmass
4 or area. The method includes establishing a data base of
5 landmasses in which each landmass is circumscribed with a polygon
6 defined by a plurality of data points. After defining an initial
7 source point and final way point, the method iteratively
8 generates a plurality of routes between the initial source point
9 and final way point. The final way point is the destination
10 point unless destination is inside an obstacle (i.e., land mass
11 boundary). During each iteration first and second bearing lines
12 are generated from the source point to first and second tangents
13 of the polygons surrounding each intermediate landmass. A
14 potential way point relative to the tangent of each bearing line
15 to the polygon is defined. Thereafter each potential way point
16 is converted to an intermediate way point for the route and this
17 way point is substituted as the source point. This process
18 produces a number of routes. One of those routes is selected as
19 a final route for the missile between the launching and
20 destination points.

21

22 BRIEF DESCRIPTION OF THE DRAWINGS

23 The appended claims particularly point out and distinctly
24 claim the subject matter of this invention. The various objects,
25 advantages and novel features of this invention will be more
26 fully apparent from a reading of the following detailed

1 description in conjunction with the accompanying drawings in
2 which like reference numerals refer to like parts, and in which:

3 FIG. 1 is a map that depicts a launch point, destination
4 point and landmasses as a background against which this invention
5 can be utilized and that depicts a direct flight route from a
6 first launch point to a destination point;

7 FIG. 2 is a block diagram of apparatus embodying this
8 invention;

9 FIG. 3 is a basic flow diagram depicting general operations
10 and procedures according to this invention;

11 FIGS. 4 through 6 depict a procedure of FIG. 3 for defining
12 initial and final way points;

13 FIG. 7 depicts a procedure of FIG. 3 for performing
14 constraint tests;

15 FIG. 8 depicts a procedure of FIG. 3 for augmenting a flight
16 path;

17 FIG. 9 is an augmented map based upon the map of FIG. 1
18 useful in understanding the operation of this invention in
19 defining a route from a second launch point to the destination
20 point with intermediate way points;

21 FIG. 10 depicts a procedure of FIG. 3 for determining way
22 points and generating a flight path in accordance with this
23 invention;

24 FIGS. 11 through 14 depict other procedures useful in the
25 procedure of FIG. 10;

26 FIG. 15 is a augmented map based upon the map of FIG. 1
27 useful in understanding the operation of the invention in

1 defining a route from a third launch point to a destination point
2 with intermediate way points;

3 FIG. 16 depicts another scenario in which a destination
4 point is in close proximity to a land mass;

5 FIG. 17 depicts a procedure used in FIG. 10 for defining way
6 points for the scenario shown in FIG. 16;

7 FIG. 18 depicts a rough path from a launch point to a
8 destination point as achieved in accordance with aspects of this
9 invention; and

10 FIGS. 19A and 19B depict a procedure for reducing and
11 optimizing the rough path shown in FIG. 18 to obtain a selected
12 shortest optimized and reduced path.

13

14 DESCRIPTION OF THE PREFERRED EMBODIMENT

15 This invention enables the development of a flight plan for
16 a vehicle, such as a missile, from a launch point to a
17 destination point such that the missile flight path avoids
18 predetermined landmasses or other geographical areas. More
19 specifically, a flight plan generated in accordance with this
20 invention will include a route with one or more intermediate way
21 points that is the shortest possible path between the launch
22 point and destination point taking into consideration the
23 maneuvering capabilities of the vehicle, or missile. An
24 understanding of the operation and advantages of this invention
25 can be enhanced by describing the invention first in the context
26 of both direct and indirect flight paths between the launch and
27 destination points and thereafter in a context in which either or

1 both of the launch and destination points are proximate to or
2 even within such landmasses or geographical areas.

3 FIG. 1 depicts a map with three potential starting or launch
4 points 10, 11 and 12 designated LP1, LP2 and LP3, and a final
5 destination point (DP) 13. The map of FIG. 1 also contains
6 landmasses 14 through 19 that represent geographical areas to be
7 avoided during a flight as the vehicle travels from a launch
8 point to a destination point. As apparent from inspection, a
9 direct route exists between the LP1 launch point 10 and the
10 destination point 13. However, a direct route to the DP
11 destination point 13 from either the LP2 launch point 11 and the
12 LP3 launch point 12 crosses landmasses. Particularly, both the
13 paths from the LP2 launch point 11 and the LP3 launch point 12
14 cross the landmass 18. This invention enables a real time
15 generation of flight paths from the LP2 launch point 11 and the
16 LP3 launch point 12 to the destination point 13 that define at
17 least one intermediate way point thereby to establish a route
18 that avoids any landmasses.

19 A precursor to the generation of such a flight path is the
20 generation of certain data concerning landmasses of interest will
21 be stored in a data base. The data for each landmass will
22 contain a landmass identification, the parameters of a
23 circumscribing polygon and the parameters of a min/max rectangle.
24 There will also be a field for receiving data concerning the
25 position of a destination point relative to the landmass.

26 For example, in FIG. 1 a polygon 20 with data points 20-1
27 through 20-6 circumscribes the landmass 14. The exact position

1 and number of data points are arbitrary, but typically will
2 define a polygon that is located completely outside the landmass.
3 The polygon definition could be according to any number of
4 systems, as, for example, a latitude/longitude system. In such a
5 system, the sides of each polygon can be defined as vectors from
6 one data point to an adjacent data point in a particular
7 direction. In this example it is assumed that the direction is
8 clockwise so that a vector could be defined from the data point
9 20-1 to the data point 20-2 in terms of a bearing and range.
10 Procedures for generating a vector having bearing and range
11 information between two way points is well known in the art. In
12 the following discussion such a vector has the general
13 designation $V_n(i,j)$ where "n" is the polygon number and "i" and
14 "j" are successive data point numbers for the polygon. For
15 example, the vector from data point 20-1 to data point 20-2 is
16 $V_{20}(1,2)$ and the vector from the data point 20-6 to the data
17 point 20-1 is $V_{20}(6,1)$.

18 A landmass min/max rectangle is the smallest rectangle that
19 circumscribes a landmass or group of interconnected landmasses.
20 Typically a landmass min/max rectangle will have sides lying on
21 the north-south and east-west axes. One such landmass min/max
22 rectangle 21 circumscribes the landmass 14 and is determined by
23 the data points 20-1, 20-2, 20-4 and 20-5.

24 The data base contains similar data for defining the
25 remaining landmasses. A polygon 22 and a landmass min/max
26 rectangle 23 define the landmass 15; a polygon 24 and a landmass
27 min/max rectangle 25, the landmass 16. Polygons 26, 27 and 28

1 define the landmasses 17, 18 and 19 respectively. As apparent,
2 the polygon 27 has data points or segments lying within the
3 polygons 26 and 28. A landmass min/max rectangle 29 therefore
4 circumscribes the totality of the landmasses 17, 18 and 19
5 defined by the corresponding intersecting polygons 26 through 28.
6 In this particular example the extreme positions on the polygons
7 26 and 28 define the landmass min/max rectangle 29.

8 Referring now to FIG. 2 a system 30 for producing the
9 different paths from the LP1, LP2 and LP3 launch points 10, 11
10 and 12 respectively to the DP destination point 13 in FIG. 1 will
11 include an input console 31 and a landmass data base 32
12 containing the aforementioned information about landmasses of
13 interest. For any particular solution, the system references a
14 limited number of landmasses from the data base 32. A tangent
15 generator 33 produces information in conjunction with a
16 constraint generator 34. A route selector 35 and a route
17 optimizer 36 produce the best route from a given launch point to
18 the destination point. An interface 37 provides a means for
19 transferring the selected path to a vehicle guidance system 38.
20 Each of the foregoing elements can comprise a circuit module or a
21 software module in a general or special purpose digital computer.
22 Consequently, each element will be described functionally. The
23 particular form of implementation is well within the capabilities
24 of persons of ordinary skill in the relevant art.

25 Referring to FIG. 3, as an initial step an operator will use
26 step 40 in FIG. 3 to input a launch point and a destination point
27 through the input console 31 of FIG. 2. For example, the

1 operator could input the latitude and longitude for each. The
2 tangent generator 33 uses this information and the landmass
3 information to generate possible routes from the launch point to
4 the destination point. More specifically, a procedure 41 defines
5 an initial way point (IWP) and a final way point (FWP) as
6 described later. For purposes of understanding the operation of
7 the system in connection with a path from the LP1 launch point 10
8 to the destination point 13, the LP1 launch position 10 is the
9 initial way point and the destination point 13 is the final way
10 point in the procedure 41.

11 In analyzing this path the system of FIG. 2 or resulting
12 control program in a general purpose digital computer tests for a
13 direct path between the initial way point and the final way point
14 in step 42. If a direct route exists, as from the LP1 launch
15 point 10, step 43 transfers control to a procedure 44 that
16 performs various constraint tests on the route. As disclosed
17 later these typically relate to the length of flight paths
18 between maneuvers and minimum or maximum maneuver angles.
19 Assuming that the flight path from the LP1 launch point 10 to the
20 destination point 13 satisfies the constraints, step 45 diverts
21 control to procedure 46. In this particular example the launch
22 point and destination points are the initial way points and final
23 way points respectively, so no further action is necessary. Step
24 47 transfers the flight path information through the interface 37
25 to the vehicle guidance system 38 as shown in FIG. 2. Thus, for
26 the flight path between the LP1 launch point 10 and the

1 destination point 13, the system computes a direct flight path
2 because there are no intermediate landmasses to be avoided.

3 Procedure 41 and step 46 determine and utilize initial and
4 final way points. Generally, but not necessarily, the launch
5 point and destination point will lie outside the polygons around
6 the landmasses. In Fig. 1, the LP1 and LP2 launch points 10 and
7 11 and the DP destination point 13 all lie outside any polygons
8 and outside any landmass min/max rectangle. In such scenarios,
9 the launch point and initial way point are identical and the
10 destination point and final way point are identical. However,
11 either or both of the launch point or destination point can lie
12 within a polygon. The LP3 launch point 12 is an example of a
13 launch point lying within a polygon. In such an event it will be
14 necessary for a portion of the flight path to pass over a
15 landmass line segment. The path to or from a way point within a
16 land mass is to or from an initial or final point.

17 Procedure 41 in FIG. 3 takes these possibilities into
18 account. Referring to FIG. 4, a first step 50 in procedure 41
19 determines whether either the launch point or the destination
20 point is located within a landmass polygon. In the example of
21 FIG. 1, neither of the LP1 or LP2 launch points 10 and 11 are
22 within any landmass polygon. Consequently, and as previously
23 indicated, step 51 diverts to step 52 to set an initial way point
24 (IWP) to the launch point (LP). For a path from the LP3 launch
25 point 12 within the landmass polygon 22 in FIG. 1, step 51 in
26 FIG. 4 diverts to a procedure 53 for defining an auxiliary way
27 point (AWP) as described later. Once that auxiliary way point

1 has been established, it is set as the initial way point (IWP)
2 and the course from the launch point to the initial way point is
3 saved in step 54.

4 A similar set of steps provides the final way point (FWP).
5 In this particular example the destination point 13 lies outside
6 any landmass polygon so step 55 diverts to step 56 whereupon the
7 FWP is set to be the destination point (DP). If the destination
8 point were within a landmass polygon, the procedure 53 would
9 define an auxiliary way point for the destination point. Then in
10 step 57 the system would set the final way point (FWP) to the
11 auxiliary way point and save the course from the final way point
12 (FWP) to the destination point (DP).

13 The final test in FIG. 4 determines, in step 58, whether the
14 destination point (DP) lies within a landmass min/max rectangle
15 but outside the corresponding landmass polygon. If such a
16 condition exists, step 59 diverts to step 60 to mark the data
17 base for the corresponding landmass as containing a destination
18 point within the landmass min/max rectangle. By implication from
19 the path in FIG. 4, step 60 is only used if the destination point
20 meets the additional criteria of lying outside the corresponding
21 landmass polygon. If the destination point 13 were inside a
22 polygon, the path would be through step 57 so the landmass would
23 not be marked. Step 61 defines the converse state. As will be
24 seen, steps 60 and 61 provide a basis for making a decision
25 concerning alternatives used in the procedure 62 in FIG. 3 that
26 determines intermediate way points when a direct path does not
27 exist.

1 FIG. 5 depicts the procedure 53 in FIG. 4 for defining an
2 auxiliary way point (AWP). Whenever a launch point or
3 destination point (DP), such as the LP3 launch point 12, lies
4 within a landmass polygon, the procedure 53 initially tests the
5 launch point or destination point (designated "LP/DP") against
6 the data points that define the surrounding landmass polygon in
7 step 64 of FIG. 5. In the particular example of FIG. 1 none of
8 the data points directly match the LP3 launch point 12, so step
9 65 diverts to step 66 to determine whether the LP3 launch point
10 13 actually lies within the polygon 23. Step 66 determines the
11 latitude through the LP3 launch point 12. Step 67 identifies
12 polygon segments that cross the LP/DP latitude. In this
13 particular example two such segments corresponding to vectors
14 22(6,1) and 22(3,4) cross the latitude line represented by line
15 68 in FIG. 1. The closest landmass polygon segment is then
16 selected in step 66. By inspection in this case that is the
17 segment corresponding to vector 22(6,1). Assuming a clockwise
18 vector rotation, the segment corresponding to vector 22(6,1) has
19 a direction generally from north to south. Consequently from
20 this step 70 can determine that the LP3 launch point 12 lies
21 within the polygon 22.

22 If the launch point or destination point is outside a
23 polygon, step 71 diverts to step 72 thereby to set AWP to the
24 value of a launch point or destination point. This would occur
25 for each of the LP1 and LP2 launch points 10 and 11 and for the
26 destination point 13. If a launch point is being analyzed, step
27 54 of FIG. 4 sets the initial way point (IWP) to the launch

1 point. In situations exemplified by the positions of the LP3
2 launch point 12, step 71 diverts to procedure 73 that generates
3 an AWP outside the boundary defined by the polygon, such as
4 polygon 22. That AWP then becomes the IWP or FWP depending upon
5 whether the launch point or destination point is being analyzed.

6 The procedure 73 for generating the AWP outside a polygon is
7 depicted in FIG. 6. Step 74 determines the distance from the
8 LP/DP, that in this case the LP3 launch point 12, to each
9 landmass data point in the polygon 23. In step 75 the system
10 selects the closest data point. As shown in FIG. 1, that would
11 be the data point 22-1. Step 76 then tests to determine if a
12 perpendicular line exists from any of the segments that
13 additionally intersect the LP/DP. If an intersection does not
14 exist, as for example for the segment corresponding to vector
15 22(5,6), step 77 diverts to step 78 to determine if more segments
16 exist. If more exist, control reverts to step 76 to test another
17 segment.

18 In FIG. 1, the segments corresponding to vectors 22(6,1) and
19 22(1,2) have such perpendicular lines. Assuming that the
20 segments are processed sequentially in a clockwise fashion from
21 the data point 22-1, the first intersection will occur in the
22 analysis of the segment corresponding to vector 22(1,2) as stated
23 above. Step 79 in FIG. 6 will determine the distance along the
24 perpendicular to the intersection with the line segment. If the
25 distance is shorter than that distance in comparison with the
26 prior shortest distance, step 80 diverts to step 78 to test
27 another segment. In this particular example the distance from

1 the LP3 launch point along the perpendicular to the segment
2 corresponding to vector 22(1,2) is shorter than the previous
3 distance from the LP3 launch point 12 to the data point 22-1 so
4 that perpendicular is saved in step 81 as the shortest path.

5 The next five iterations of the loop comprising steps 76
6 through 81 produce no change in the shortest path as none of the
7 corresponding line segments have a perpendicular that intersects
8 the LP3 launch point 12. However, during the final iteration a
9 perpendicular will exist to the segment corresponding to vector
10 22(6,1). This will be the shortest distance so that it will be
11 saved in step 81.

12 When all the segments have been examined, step 78 diverts to
13 step 82 that extends the range of the shortest path by some
14 arbitrary distance along the perpendicular line in step 80 to
15 define an auxiliary way point (AWP). Control then returns from
16 the procedure 73 in FIGS. 5 and 6 to assign the AWP to the IWP in
17 step 54 or to the FWP in step 57 in FIG. 4, as appropriate.

18 Thus, when the procedure 41 in FIG. 3 as set forth in detail
19 in FIGS. 4, 5 and 6 has been completed, the initial way point
20 (IWP) and a final way point (FWP) will be defined. In the
21 example of FIG. 1, the IWP will be the LP1 or LP2 launch points
22 10 or 11 or an offset from the LP3 launch point 12. The final
23 way point will be the destination point 13 or an offset from that
24 destination point. If the IWP or FWP is offset from a
25 corresponding launch point or destination point, respectively,
26 the range and bearing from the launch point to the initial way

1 point or from the final way point to the destination point will
2 also have been saved.

3 Still referring to FIG. 3, the procedure 44 performs various
4 constraint tests. As will become evident later, these tests are
5 also performed in the procedure 62 and during route optimization
6 to assure that the missile or vehicle can maneuver to the next
7 possible course from a current source point (CSP). The current
8 source point initially is the initial way point (IWP), but will
9 also be constituted by intermediate way points. Thus, when the
10 procedure 44 is implemented after a determination that a direct
11 path exists from the IWP to the FWP, the current source point
12 will be the IWP.

13 Referring to FIG. 7, step 83 determines the distance from
14 the current way point (CSP) to a next possible way point. Step
15 84 determines the turn angle from a bearing to the CSP to the
16 bearing from the CSP to the next possible way point. The
17 distance is tested against any limit in step 85. For example,
18 there may be a requirement for a minimal distance between turning
19 maneuvers. If the distance does not meet the criteria, step 86
20 diverts to step 87 to move the way point to conform to the
21 constraint. This movement typically will constitute an extension
22 along the bearing line from the CSP to the next possible way
23 point. Next the system in step 88 will test any turn angle to
24 determine whether it exceeds any limits. Step 89 diverts to step
25 90 to change that turn angle to conform to the constraint if
26 needed and thus modify the way points as a next possible way
27 point.

1 Although not required in a direct path calculation, the
2 system can then also test the next possible way point as modified
3 above for elimination in step 91 and then, based upon the
4 characteristics (i.e., distance and angle) of that way point, use
5 step 92 either to accept the way point in step 93 or eliminate
6 the way point in step 94.

7 Referring again to FIG. 3, if a direct path exists and the
8 constraints are not met, step 45 can divert to a procedure 95
9 that alters the path accordingly. Such procedures could
10 constitute an error message or some other process, and therefore
11 not disclosed in any detail.

12 If both the launch point and the destination point are the
13 initial and final way points respectively, step 46 in FIG. 3
14 diverts to transfer the flight path to the vehicle in step 47.
15 Otherwise the procedure 48 augments the flight path as shown in
16 FIG. 8. As previously indicated, any course between a launch
17 point and the initial way point or a final way point and a
18 destination point is saved. In the procedure of FIG. 8, step 96
19 determines whether the launch point and the initial way point are
20 identical. If they are not, the saved path from launch point to
21 initial way point path is added to the beginning of the route in
22 step 97. Similarly step 98 determines whether the destination
23 point and the final way point are identical. If they are not,
24 step 99 adds the path from the final way point to the destination
25 point to the route.

26 With this information as background, it will now be possible
27 to discuss the process by which this invention produces a route

1 or flight path with intermediate way points. In FIG. 9, the LP2
2 launch point 11, as previously indicated, lies outside any
3 landmass min/max rectangle. However, a direct line from the LP2
4 launch point 11 to the destination point 13 intersects a
5 landmass, namely the landmass 18. Consequently step 43 in FIG. 3
6 diverts to the procedure 62 to generate a shortest flight path
7 with intermediate way points that avoids all the landmasses
8 before returning to step 46.

9 Referring to FIG. 10, the procedure 62 starts at step 111 by
10 obtaining data for the relevant landmasses and determining direct
11 and indirect landmass intersections in step 112. As shown in
12 FIG. 9, the landmasses 17, 18 and 19 are intersecting when viewed
13 from the LP2 launch point and are considered to be a single
14 landmass. Step 113 defines a current source point (CSP). On the
15 first pass this is the initial way point, or in the particular
16 example of FIG. 9 the LP2 launch point 12. Step 114 tests for a
17 direct path from the current source point to the final way point.
18 As this duplicates step 43 in FIG. 3, during the first pass
19 through this procedure and in the context of FIG. 9, no direct
20 path exists, so step 115 shifts control to procedure 116 that
21 obtains all possible way points for the next leg.

22 This procedure is detailed in FIG. 11 but for purposes of an
23 overview of this operation it is sufficient to understand that
24 the procedure 116 obtains, as possible way points, positions
25 defined by extending tangents to each landmass from the current
26 source point to all surrounding landmasses, provided certain
27 criteria are satisfied. In the example of FIG. 9 a pair of

1 tangent lines will be drawn to each of the landmasses 14, 15, and
2 16 and the combined intersecting landmasses 17 through 19.

3 The system then uses step 117 to sort the remaining possible
4 way points by a bearing relative to an azimuth from the current
5 source point to the final way point. Using this sorted order is
6 based upon an assumption that a way point with the smallest
7 bearing is likely to produce the shortest path.

8 A recursive call procedure 118 determines if there are more
9 way points to be processed. If there are, the recursive
10 procedure selects another way point and passes control back to
11 step 114 by moving the current source point to the next possible
12 way point that has passed the test. The details of this
13 recursive call procedure are described in more detail later. At
14 this point, it is sufficient to understand that the recursive
15 call procedure provides an orderly analysis to produce
16 alternative possible flight paths from the LP2 launch point 11 to
17 the destination point 13.

18 Once the recursive call procedure determines that all
19 possible paths have been defined, control passes to step 120 to
20 the shortest path. Step 121 reduces and optimizes that path for
21 transfer the missile or other vehicle.

22 FIG. 11 depicts the procedure 116 by which all next possible
23 way points from a current source point are obtained. Steps 130
24 and 131 determine whether the destination point lies outside a
25 landmass polygon but still within the landmass min/max rectangle.
26 If the data for a particular landmass is marked, as previously
27 indicated, control transfers to a procedure 132 described later.

1 Generally, and for other landmasses control passes to step 133
2 that is a normal procedure for defining tangents to a landmass.

3 Looking particularly at the LP2 launch point in FIG. 4, the
4 procedure 133 in FIG. 11 determines the tangent to each landmass
5 of interest in an iterative fashion. As shown in FIG. 9, the
6 tangent A procedure 133 produces tangents to the landmasses 14,
7 15 and 16 and to the combined landmasses 17, 18 and 19 that have
8 been combined as a single landmass in step 112 of FIG. 10. More
9 specifically, and as shown in FIG. 12, the tangent A procedure
10 uses step 134 to determine a bearing from the current source
11 point to each landmass data point. As shown in FIG. 9, bearing
12 lines have been taken from the LP2 launch point 11 to each of the
13 data points 20-1 through 20-6. In step 135 of FIG. 12 the system
14 establishes an orientation bearing. This typically will be one
15 of the ordinal bearings that does not lie within the general
16 range of the bearings to the landmass. For example, with respect
17 to the LP2 launch point 11 and the landmass 14, the orientation
18 bearing could be east, west or south. Any other bearing that is
19 not included in the bearings to the landmass data points can also
20 be used.

21 Step 136 then converts the bearings, B_n to bearings relative
22 to the orientation bearing and this step enables the bearings
23 having a minimum and maximum relative bearing values to be
24 defined in step 137 as bearings to the tangent points. That is,
25 the tangent points become the data points with the minimum and
26 maximum relative bearings so the tangent bearings 138A and 138B
27 define the tangents to the landmass 14. The procedure 133 in

1 FIG. 12 repeats for each of the remaining landmasses thereby to
2 define tangent lines 15A, 15B, 16A, 16B, the bearing lines 17A
3 and 19B constituting the tangent bearings for the combined
4 landmasses 17, 18 and 19.

5 When all the tangent lines from the current source point
6 (i.e., the LP2 launch point at this stage) have been defined a
7 next procedure 140 in FIG. 11 tests each tangent line to
8 determine whether the line intersects a landmass. That is, each
9 bearing line is tested to determine whether it lies between the
10 tangent bearing lines to any other landmass. More specifically,
11 step 141 in FIG. 13 selects a landmass for which tangent bearing
12 lines already exist from the current source point. Step 142
13 tests the tangent line to the next possible way point to
14 determine if it lies between these existing tangent bearing
15 lines. If the tangent bearing line under test lies between
16 tangent lines to another landmass, step 143 diverts operation to
17 step 144 whereupon the tangent line is tested against all the
18 data points for an intersection with the landmass. If an
19 intersection exists, step 145 exits through step 146 indicating
20 that a landmass intersection exists. If no intersection exists
21 step 145 exits through step 147 to indicate that fact.
22 Similarly, step 143 diverts and exits through step 147 if the
23 tangent line is not between existing tangent lines.

24 With the example shown in FIG. 9, the bearing lines 16A and
25 16B lie between the bearing lines 17A and 19B. Consequently they
26 must be checked with respect to those landmasses. However, they
27 need not be checked with respect to any of the other landmasses

1 because they do not lie between the tangent lines to those
2 landmasses. As will be apparent, the foregoing screening test
3 limits the test of steps 144 and 145 to the combined landmasses
4 17, 18 and 19. In the scenarios of FIG. 9 there is no need to
5 test any of the bearing lines to the landmasses 14 and 15.
6 Consequently this screening test minimizes the processing
7 required to determine intersecting bearing lines. When this test
8 is complete, control returns to step 148 in FIG. 11 that diverts
9 to step 149 and eliminates the bearing lines 16A and 16B because
10 they are intersecting.

11 Assuming a tangent bearing line does not intersect a
12 landmass, the system uses step 150 in FIG. 11 to determine the
13 range of the tangent point and extends the range in step 151.
14 This defines a possible next way point. That is, in the example
15 of FIG. 9, next possible way points would be generated by steps
16 150 and 151 for the tangent bearings to the landmasses 15 and 16
17 and the combined landmasses 17, 18 and 19.

18 The step of extending the way point is shown in FIG. 9 with
19 respect to the tangent bearings 17A and 19B that are extended by
20 a distance Δr to WP44 and WP45 next possible way points. The
21 extension of each bearing line is tested for intersection in a
22 procedure 152. If the extension Δr causes the resulting way
23 points to intersect a landmass step 153 shifts control to step
24 154 decrease Δr , typically by one half. Then control returns to
25 step 152. Once the extension has been determined, step 153
26 diverts to procedure 44 (FIG. 7) to determine whether the path

1 from the CSP to the next possible way point each way point passes
2 a constraint test. If it does, step 154 diverts to accept the
3 way point in step 155. Consequently when the process of FIG. 11
4 has been completed with respect to the LP2 launch point, way
5 points will have been produced along the tangent bearing lines to
6 landmasses 14 and 15 and the combined intersecting landmasses 17
7 through 19. No tangent bearing lines will be extended with
8 respect to the tangent bearing lines 16A and 16B.

9 Referring again to FIG. 10, after all next possible way
10 points from the current source point have been determined and
11 sorted, the recursive procedure 118 analyzes each of these next
12 possible way points in sorted order by bearing relative from an
13 azimuth from the current source point to the destination point.
14 At this particular stage the LP2 launch point 11 in FIG. 9 is the
15 current source point. Thus the order will be (1) way point 44,
16 (2) way point 45, (3) the way point through data point 23-6, (4)
17 the way point through data point 20-1, (5) the way point through
18 data point 20-2 and (6) the way point through data point 23-4.

19 Referring now to FIG. 14, one portion of the recursive
20 procedure determines whether each next possible way point meets
21 certain criteria for further consideration. Step 160 selects the
22 next possible way point (NPWP) with the closest relative bearing
23 to the bearing from the current source point (CSP) to the
24 destination point (DP) as previously described.

25 A first criteria establishes whether the next possible way
26 point is moving away from the destination point. Step 161
27 determines the distance from the original starting point (IWP)

1 through the current source point to the next possible way point
2 (NPWP) plus the distance from the next possible way point
3 directly to the destination point. If that distance is greater
4 than the shortest previously calculated complete path, step 162
5 eliminates this next possible way point from further
6 consideration in step 163 and returns to step 160 to obtain a
7 next one of the sorted next possible way points for analysis.

8 Otherwise step 162 diverts control to step 164 that
9 substitutes the selected next possible way point for the current
10 source point. Step 165 then determines the total number of way
11 points from the initial way point to the current source point.
12 In this case where the WP44 next possible way point is being
13 analyzed, the total number of way points to the WP44 way point is
14 one, and under a maximum. Step 166 therefore diverts control to
15 step 167. If the maximum value had been exceeded, step 166 would
16 divert to step 163 to eliminate that next possible way point from
17 further analyses as a current source point.

18 Step 167 determines if a complete path has previously been
19 generated to the final way point. If it has, step 170 diverts
20 control to step 171 that obtains the distance from the initial
21 way point to the current source point ($d_{IWP-CSP}$) plus the distance
22 from the current source point to the final way point ($d_{CSP-FWP}$).
23 If this distance exceeds the distance of a shortest complete
24 path, no additional consideration need be given to a route
25 through the current source point. Consequently step 172 diverts
26 to step 163. If the distance is shorter or if no prior complete
27 path has yet been determined, control will pass from either step

1 172 or step 170 to step 173 to enable the process to analyze a
2 next possible way point. If, for example, the CSP is the WP44
3 way point, step 173 would enable other portions of the recursive
4 control procedure 118 to return control to step 114 in FIG. 10.

5 In a next iteration of FIG. 10, this system replaces the
6 current set point with the way point WP44. As shown in FIG. 9 a
7 direct path will exist from way point 44 to the destination point
8 13 so the system calculates the total flight length in step 175
9 and transfers to the recursive call. As the direct flight path
10 is, a priori, the shortest path from the WP44 way point, there is
11 no need to analyze any other paths from the WP44 way point.
12 Consequently the recursive call 118 returns control to designate
13 the LP2 launch point 11 as the current source point and looks to
14 the way point having the next closest bearing to the azimuth from
15 the LP2 launch point 11 to the destination point 13. This is the
16 WP45 way point. In the same fashion as previously described, the
17 WP45 way point is analyzed and designated to be the current
18 source point. No direct path exists so the process, through the
19 recursive call procedure 118, determines tangent bearings from
20 the WP45 way point to all the other landmasses. Tangent bearings
21 16C and 16D depict two such bearing lines to the landmass 16.
22 Tangent data points would also be produced with respect to the
23 combined landmasses 17, 18, 19 and to each of the landmasses 15
24 and 16. However, only one of the tangent bearings of the
25 landmasses 15 and 16 would be retained after procedure 117
26 because both tangent bearings to the landmass 16 intersect the
27 combined landmasses 17, 18 and 19 as does the tangent bearing to

1 the northern portion of landmass 15. This tangent bearing is
2 shown as 15C.

3 Next the system extends the tangent points to next possible
4 way points WP46, WP47 and WP48. In this case the extensions do
5 not intersect any landmasses. The azimuth from the WP45 way
6 point to the destination point 13 is established and the next
7 possible way points are sorted according to steps 118 and 119.
8 This establishes the order WP47 - WP46 - WP48.

9 The system next substitutes the WP47 way point as the
10 current source point and determines whether any of the limits set
11 in recursive call procedure 118 as detailed in FIG. 14, have been
12 exceeded. In addition during this process step 161 tests the
13 distance from LP2 launch point through the way point WP45 as the
14 current set point to the way point WP47 as the next possible way
15 point and the line-of-sight distance the next possible way point
16 WP47 to the destination point. In this case that distance is
17 less than the minimum distance previously calculated so the way
18 point is retained in step 173. A similar step occurs with
19 respect to way point 46. However, way point 48 produces a
20 possible way point that produces a longer path so the way point
21 48 is eliminated.

22 Once all these paths have been exhausted, the recursive call
23 procedure 118 in FIG. 10 returns back through the way point WP45
24 to the LP2 launch point 11 and looks at a next possible way
25 point, namely a way point established by extending the tangent
26 bearing through data point 23-6. The analysis through this way
27 point and through the way points established by extending the

1 tangent bearings through data points 20-1, 20-3 and 20-4 will
2 essentially eliminate these way points from any further possible
3 consideration. Thus when the entire process is completed, three
4 potential paths exist. The first is from the LP2 launch point 11
5 through the way point 44 to the destination point 13; the second,
6 through the way point WP45 and WP46 way point; and the third,
7 from the WP45 way point through the WP47 way point to the
8 destination point 13.

9 Once these have been established, the system uses procedure
10 120 in FIG. 10 to reduce and optimize the various paths, called
11 "rough paths". This step generally will include the constraints
12 procedure 44 of FIG. 7.

13 FIG. 15 depicts a scenario wherein the LP3 launch point 12
14 lies within the polygon 23 so the previously described process of
15 establishing an initial way point (IWP) outside the landmass is
16 used. Two different tangents from the way point will be again
17 generated with respect to all of the landmasses. However, the
18 tangents generated to the landmass 16 will be eliminated because
19 they intersect the landmasses 17, 18 and 19. In addition
20 tangents passed the landmass 15 will eventually be eliminated by
21 virtue of length. The results are three possible routes. The
22 first including a leg 200 to a way point 201 and then directly to
23 the destination point 13. The second includes a leg 202 to a way
24 point 203. Parallel paths then exist with a first path 204
25 passing through a way point 205 and a successive path 206 moving
26 directly to the destination point 13. The alternate includes a
27 path 207 to a way point 208 and another path from the way point

1 208 directly to the destination point 13. Again as previously
2 indicated one of these will be selected as the shortest. In this
3 case the path including the path through the way points 203 and
4 208.

5 FIG. 16 depicts a landmass 210 with a circumscribing polygon
6 211 with data points 211-1 through 211-10 and a min/max rectangle
7 212. A destination point 13A lies outside the polygon 211 but
8 inside the landmass min/max rectangle 212. The use of the
9 tangent A procedure 133 in FIG. 11 may not produce a shortest
10 path from a current source point 213 to the destination point
11 13A. In FIG. 16 the tangent procedure would produce tangent
12 bearings to data points 211-8 and 211-1. The way point along the
13 later bearing would be intermediate the latitudes of data ports
14 211-1 and 211-10.

15 When this condition exists, as previously indicated, step
16 131 in FIG. 11 diverts to the tangent B procedure 132 shown in
17 detail in FIG. 17. In this procedure step 233 determines the
18 distance from the DP destination point 13A to each data point on
19 the landmass. Step 134 selects the closest data point; namely
20 data point 211-5 in this particular example, as an initial point.

21 A line is projected from this data point 211-5 to the CSP 213.
22 Procedure 235 determines that the line intersects the landmass,
23 so step 236 shifts control to step 237 to identify a next data
24 point 211-6. No intersection exists, so step 238 identifies a
25 tangent bearing to the data point 211-6 in FIG. 16.

26 Next step 239 returns to the initial point, in this case the
27 data point 211-5, and begins an analogous loop comprising steps

1 240 through 244 to select a next data point in a counter
2 clockwise direction. In FIG. 16 this is data point 211-4. A
3 line from the data point 211-4 to the CSP 213 intersects the
4 landmass as a result of an analysis by the procedure 235. So the
5 test in step 242 transfers control to step 243 to identify a next
6 data point, namely data point 211-3. Intersections continue to
7 be sensed until step 243 identifies data point 211-1. The second
8 tangent bearing is taken through the data point 211-1. Once
9 identified, the procedure set forth in FIG. 10 extends the range
10 (step 151) to identify, in this particular example, a way point
11 250 with a direct path to the destination point 13A. An
12 alternate way point 251 on the tangent through the data point
13 211-1 will be eliminated through the various tests previously
14 described.

15 FIG. 16 demonstrates the difference between the operations
16 of the procedures 132 and 133 in FIG. 11. Specifically, both
17 produce the way point 251. However, while the procedure 132
18 produces the way point 250, the procedure 133 produces a way
19 point 252 shown along a bearing line 253 (shown by a dashed line)
20 through the data point 211-8. In this particular example, the
21 test of step 161 in FIG. 14 precludes way point 252 from analysis
22 as a next possible way point. In turn, the CSP would be
23 precluded as an intermediate way point.

24 Once all the possible paths have been determined in
25 accordance with the procedure shown particularly in FIG. 10,
26 control transfers to the procedure 120 to further modify these
27 paths. As previously indicates each path obtained as a result of

1 the operation of FIG. 10 is a "rough path". FIG. 18 depicts a
2 scenario in which this procedure is particularly well adapted for
3 reducing and optimizing a particular rough path while FIGS. 19A
4 and 19B constitute a flow chart that defines the particular
5 procedure. Referring specifically to FIG. 18, the rough path
6 between a LP launch point 300 and a DP destination point 301
7 avoids landmasses 302, 303 and 304 by using way points 305, 306
8 and 307. The procedure of FIGS. 19A and 19B generally will
9 reduce the path length and, in some situations, may eliminate
10 one or more way points.

11 Referring to FIG. 19A, step 310 selects a particular rough
12 path from the rough path produced by the operation of FIG. 10.
13 Assuming that the path of FIG. 18 is obtained, step 311 in FIG.
14 19A selects the closest way point to the destination point. In
15 this particular case that is the way point 307.

16 Now the system enters a loop to backtrack along the rough
17 path. Referring to FIGS. 18 and 19A, step 312 in FIG. 19A moves
18 the selected way point 307, along the bearing line toward the
19 prior way point 306. This motion continues until a line from the
20 new location of way point 307 intersects a landmass. In FIG. 18
21 this occurs when the way point 307 moves to become way point 313.

22 Next the system performs a constraint test according to
23 procedure 44 previously described with respect to FIGS. 3 and 7.

24 These tests determine whether the vehicle is capable of
25 maneuvering from the bearing line between the way point 306 and
26 the way point 313 and the new bearing line from the way point 313
27 to the destination point 301 (i.e., a bearing line represented by

1 dashed line 314). If the maneuver is possible, the new way point
2 313 is accepted and the way point 307 deleted. Step 315 notes
3 this way point position.

4 Next the system uses step 316 to identify a prior way point
5 and test that way point in step 317 to determine if that prior
6 way point is the initial way point. If not, the prior way point
7 is selected in step 320. More specifically, after identifying
8 way point 313, the system will identify the way point 306. As
9 that way point 306 is not the initial way point, it is selected
10 in step 320 and the process repeats beginning with step 312 in
11 FIG. 19A. This will substitute way point 321 for way point 306.

12 Step 316 then identifies the way point 305 as a prior way point,
13 but this is not the initial way point. So the loop replaces way
14 point 305 with way point 322. As the next prior way point is the
15 launch point 300, step 317 in FIG. 19A diverts control to step
16 323 in FIG. 19B that begins a test to eliminate any unnecessary
17 way points.

18 Thus, when the process identified by steps 311 through 320
19 have been completed, the rough path has been modified so that the
20 new rough path extends from the launch point 300 and through the
21 way point 322, the way point 321, the way point 313 to the
22 destination point. As will be apparent in each of these new
23 route segments such as the route segment 314 constitutes one side
24 of a triangle including the old way point. By definition,
25 therefore, each of the new segments is shorter than the prior
26 path. Thus, this process reduces the selected rough path length.

1 Defining each of the new way points as reduced path way
2 points, the system next determines whether any way points can be
3 deleted. For example, assume that the system selects the way
4 point 313 as a first reduced path way point. Step 324 then
5 identifies subsequent and prior way points 301 and 321 along the
6 path. Step 325 defines a straight line between these way points,
7 (i.e., a straight line between the way point 321 and the
8 destination point 301). Step 326 determines whether this line
9 intersects the landmass. In this case a straight line from the
10 way point 321 to the destination point 301 does not intersect any
11 landmass. In that event, step 326 diverts to step 327 that
12 eliminates the selected reduced path way point 313 to change the
13 path starting from the launch point 300 through the way point 322
14 and the way point 321 to the destination point 301. Step 330 in
15 FIG. 19B determines whether additional way points need to be
16 reviewed. In this particular case the next way point to be
17 analyzed is the way point B' 321. Now the subsequently and prior
18 reduced path way points are the destination point 301 and way
19 point 322. A straight line defined in step 325 intersects the
20 landmass 303, so step 326 diverts to step 330 to determine if
21 additional way points are to be processed. Likewise testing the
22 way point 322 will produce a line between the launch point 300
23 and the way point 321 that intersects the landmass 304 so the way
24 point 322 remains in the route. Consequently when the path is
25 complete, a new route extends from the launch point 300 through
26 the way point 322 and the way point 321 to the destination point
27 301. The elimination of the way point 313 has two effects.

1 First, it further reduces the length of the path. Second, it
2 eliminates a way point. As the number of way points are
3 generally limited, the reduction of way points has an obvious
4 positive effect.

5 Once all the way points on a path have been analyzed, step
6 330 diverts control to step 331 that determines whether
7 additional remote paths need to be processed. Control returns
8 from step 331 to step 310 in FIG. 19A if more paths exist.
9 Otherwise control diverts to step 332 whereupon each of the
10 optimized and reduced paths is analyzed to identify the shortest
11 path and this path is then the path that will be transferred as
12 the route, subject to augmentation according to steps 46 and
13 procedure 48 in FIG. 3.

14 Therefore there has been described in accordance with this
15 invention a method for generating one or more rough paths that
16 avoid restricted areas by the use of different way points. Each
17 rough path is optimized and reduced, and the shortest of the
18 optimized and reduced paths is selected. The various procedures
19 set forth in this disclosure enable this entire process to occur
20 on an essentially real time basis. Moreover, the method takes
21 into account a number of practical variations such as the
22 potential location of a destination point in close proximity to a
23 landmass area that would otherwise be avoided. Further the
24 method takes into account any constraints on the operation of a
25 particular vehicle such as a missile that is being projected
26 along that path. Finally the system provides a simple process
27 for transferring the way point information including bearings and

1 ranges into the missile or other vehicle for use during flight or
2 other trajectory motion.

3 This application has been defined in terms of particular
4 steps and procedures with certain coordinate systems. It will be
5 apparent that other steps and procedures and coordinate systems
6 could be substituted while still attaining the same or most of
7 the results and advantages of this invention. Many other
8 modifications can also be made to the disclosed method without
9 departing from the invention. Therefore, it is the intent
10 to cover all such variations and modifications as
11 come within the true spirit and scope of this invention.

1 Attorney Docket No. 75738

2
3 ROUTE PLANNER WITH AREA AVOIDANCE CAPABILITY

4
5 ABSTRACT OF THE DISCLOSURE

6 A method for establishing a path from a launch point to a
7 destination point that can include multiple way points while
8 avoiding landmass areas. Launch points and destination points
9 can lie outside or inside the particular landmass areas. The
10 method includes steps for defining tangents path areas to be
11 avoided, extending those tangents to define way points and
12 testing the individual way points to assure conformance to
13 various conditions and constraints. A subset of paths are
14 optimized. The shortest of the optimized paths becomes a final
15 path.

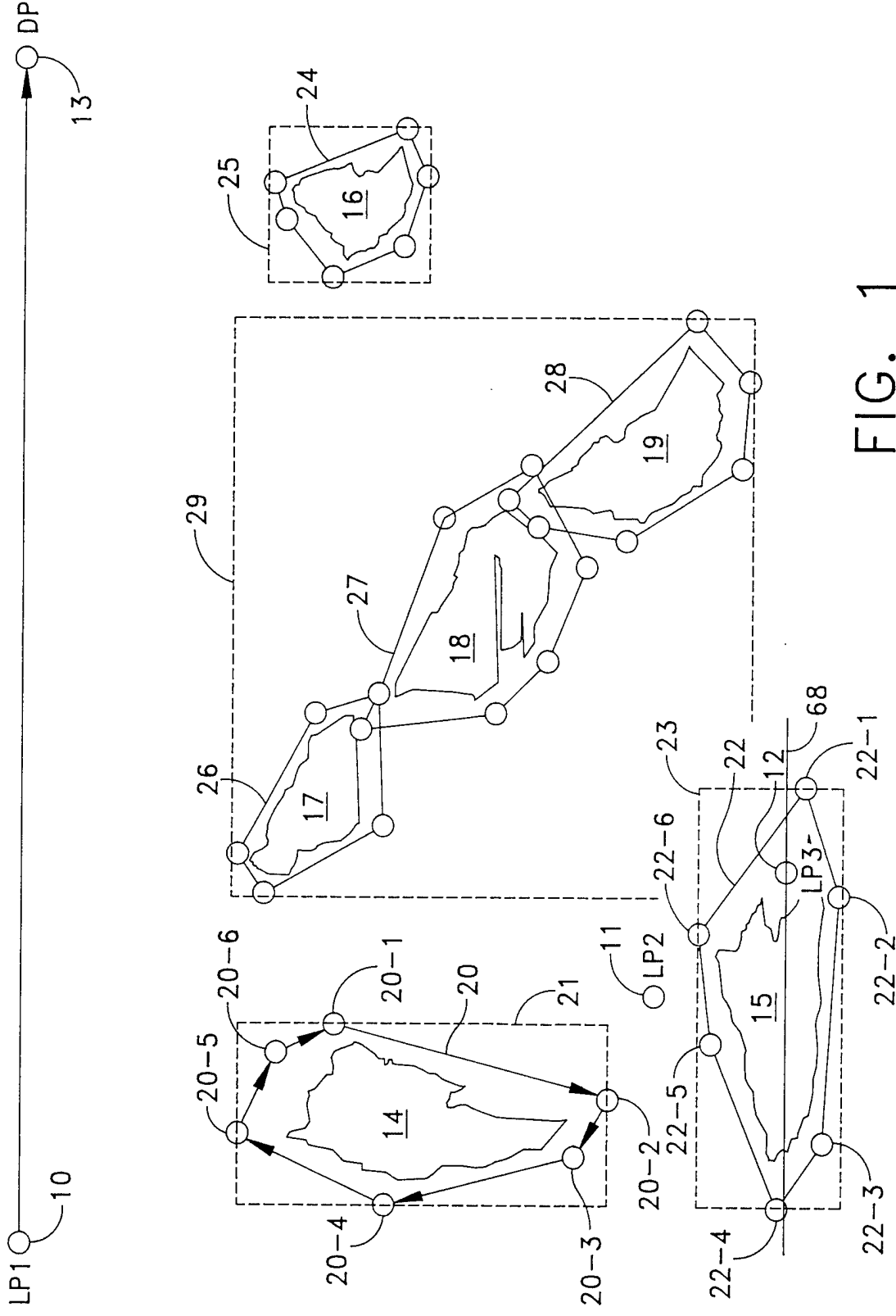


FIG. 1

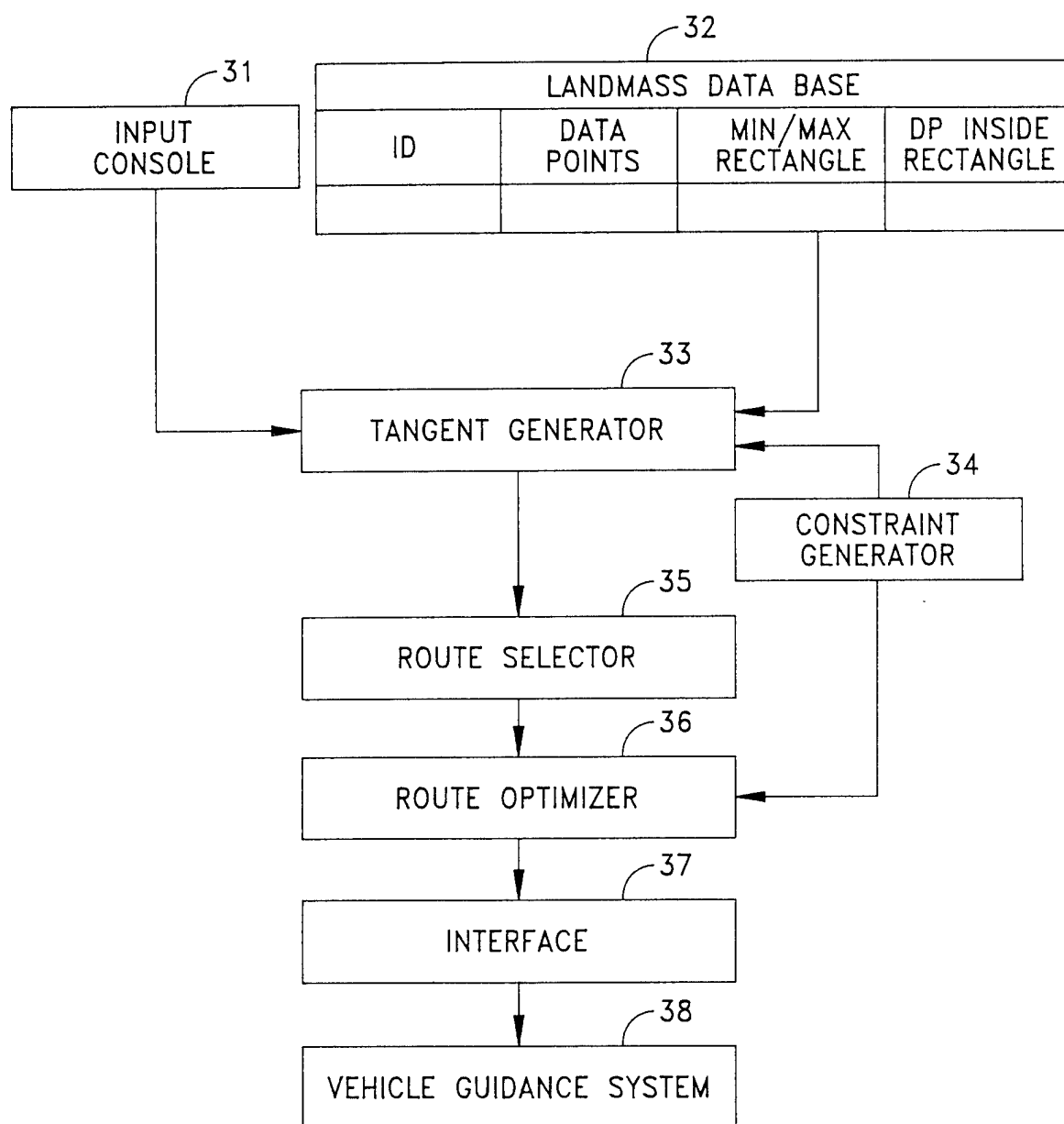


FIG. 2

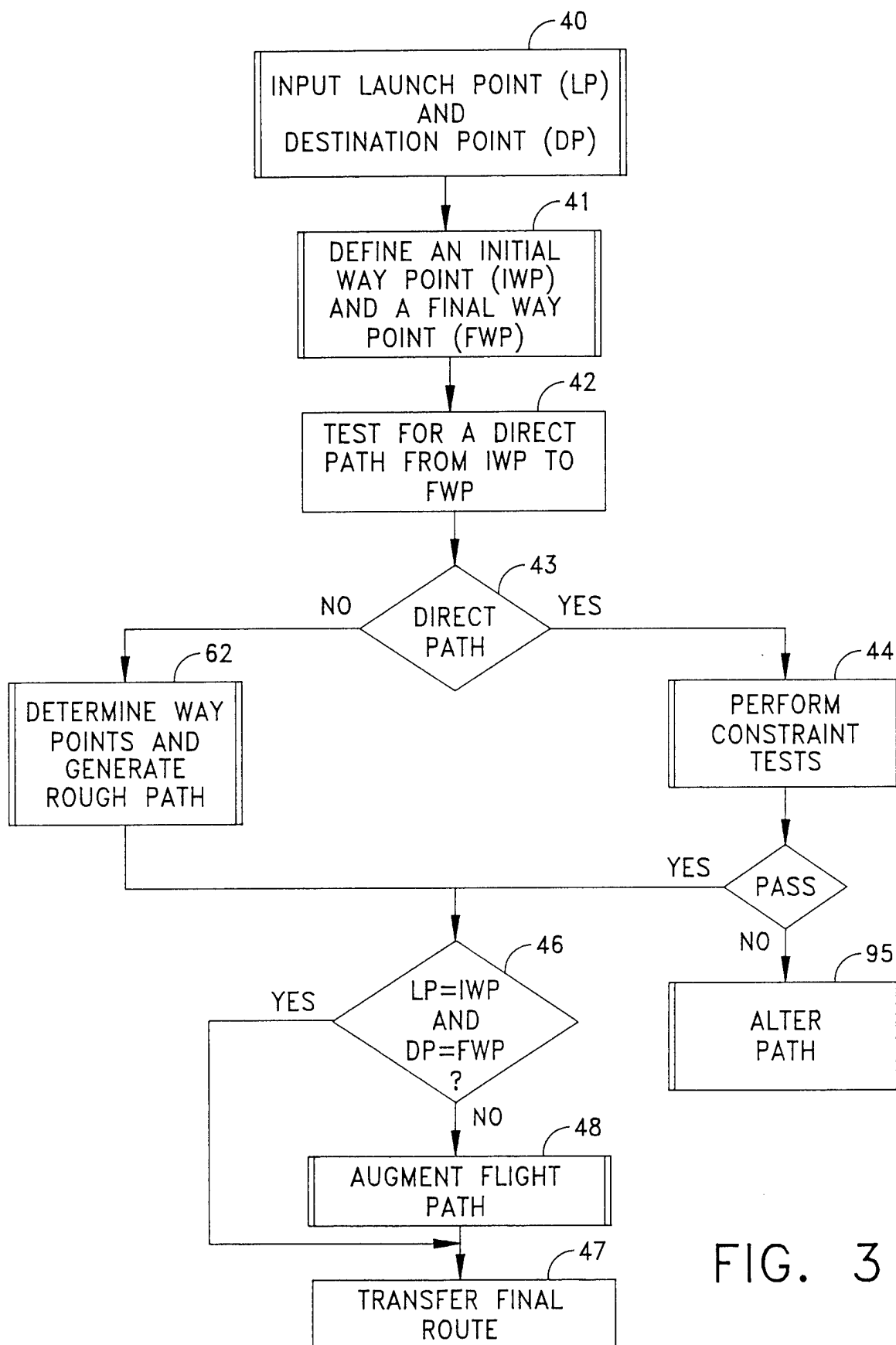


FIG. 3

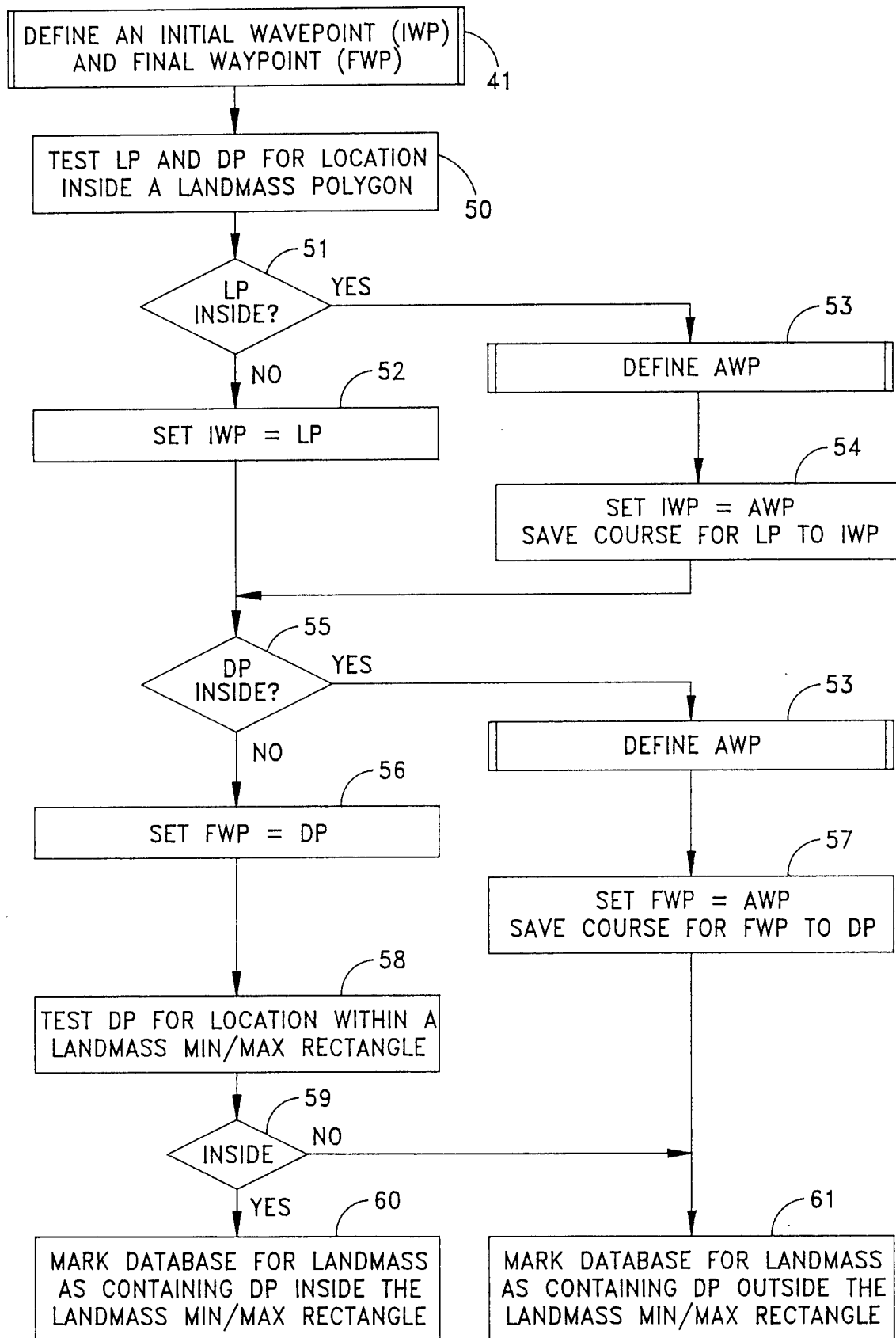


FIG. 4

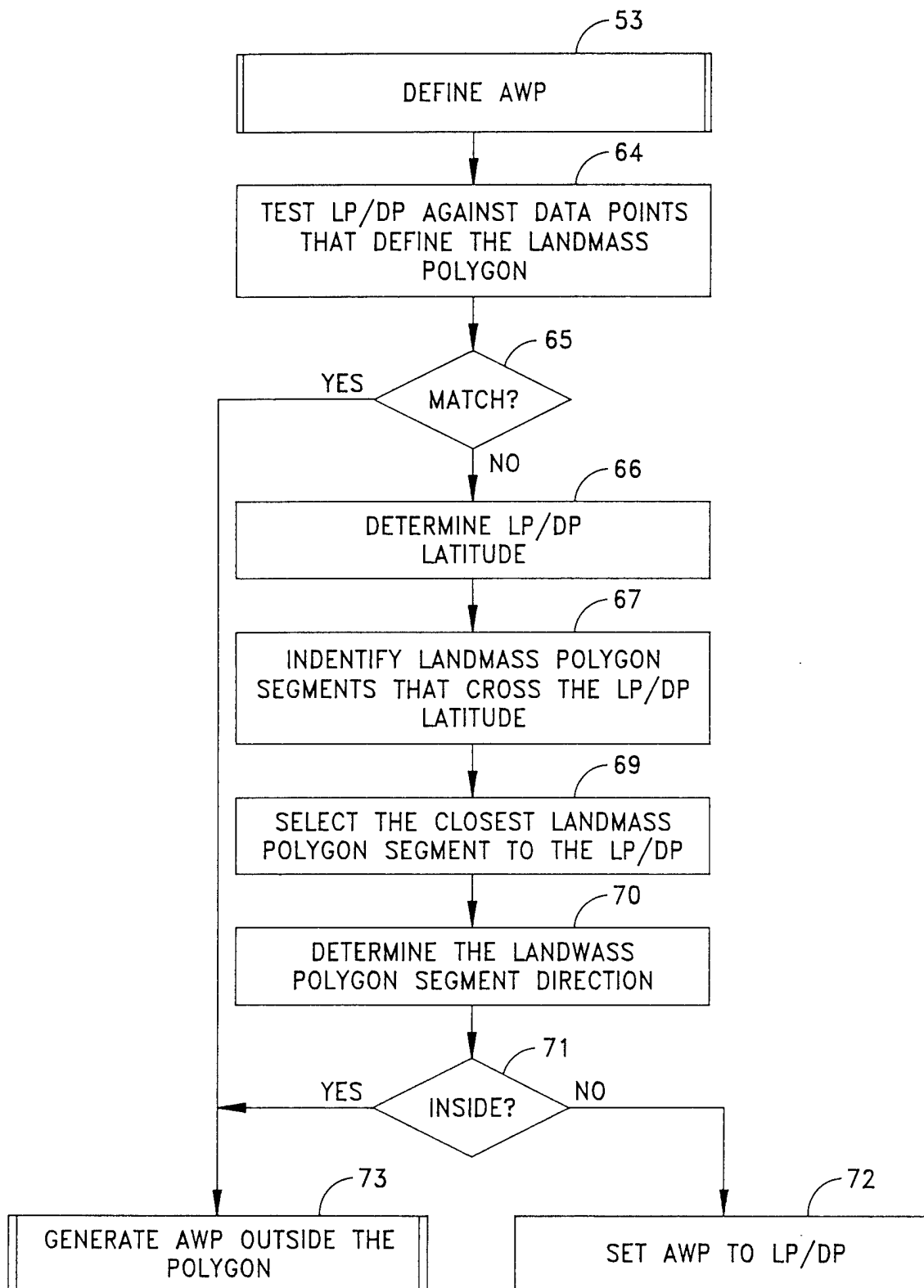


FIG. 5

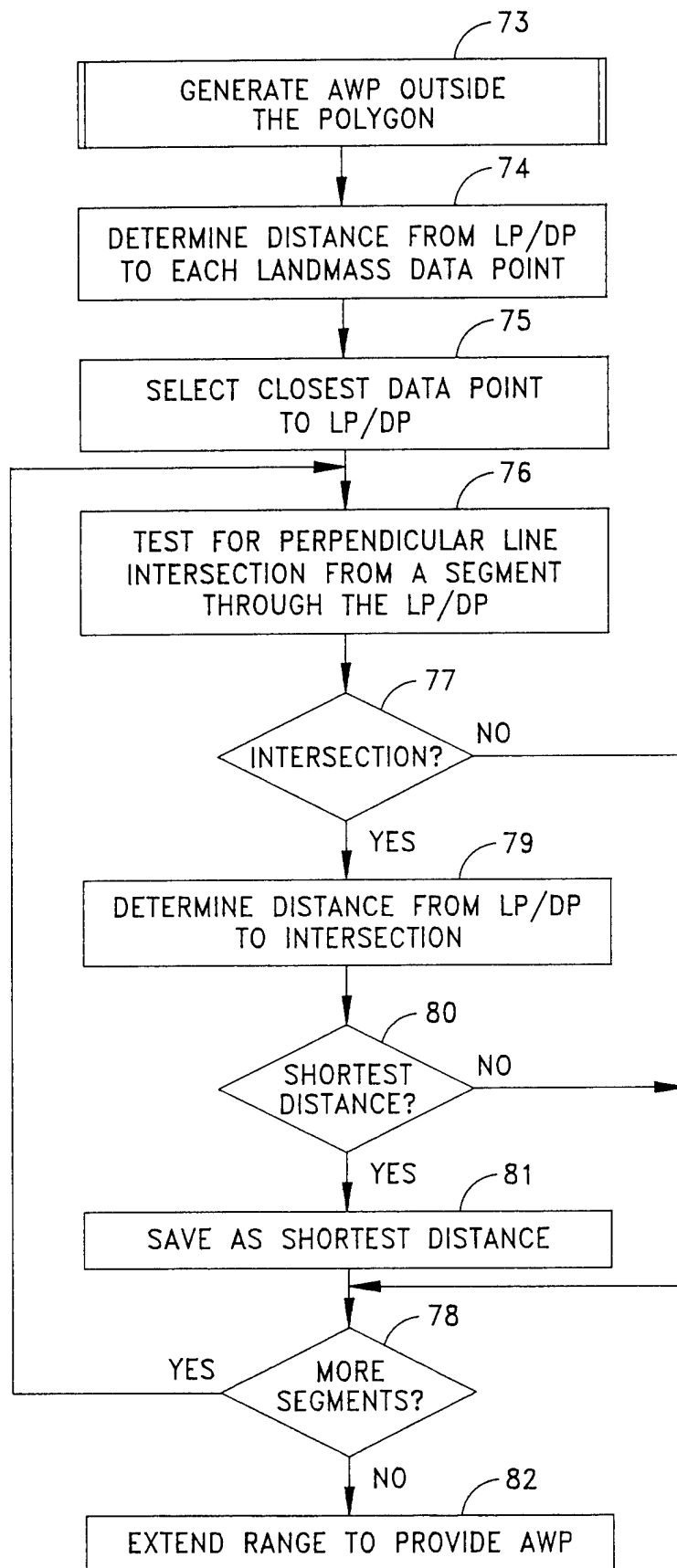


FIG. 6

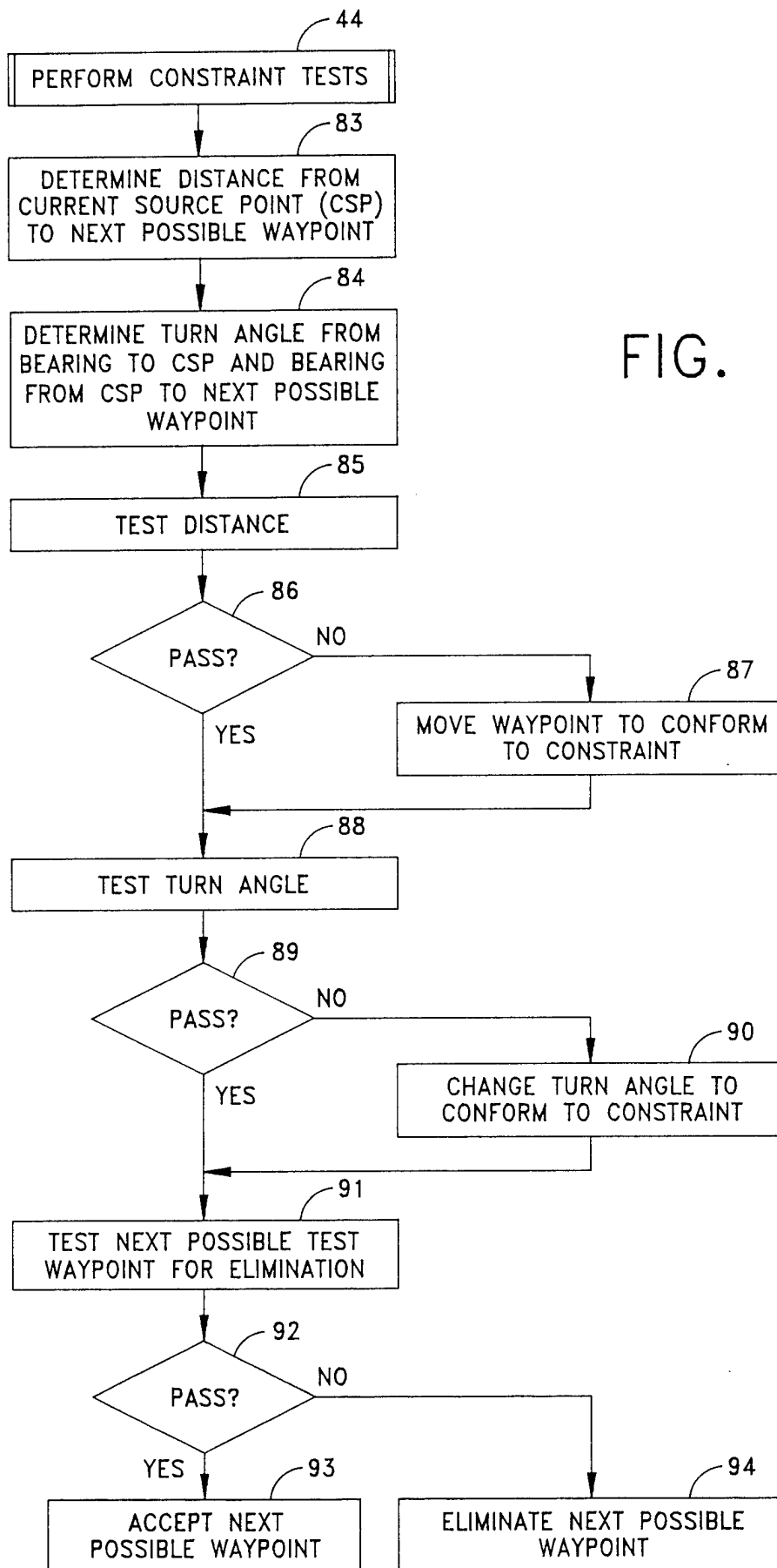


FIG. 7

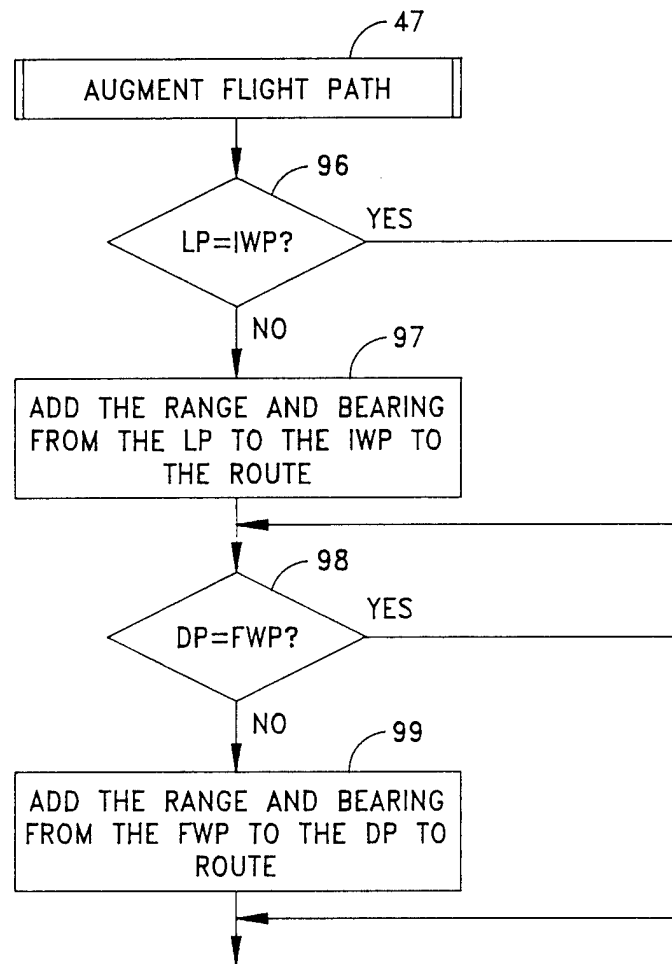


FIG. 8

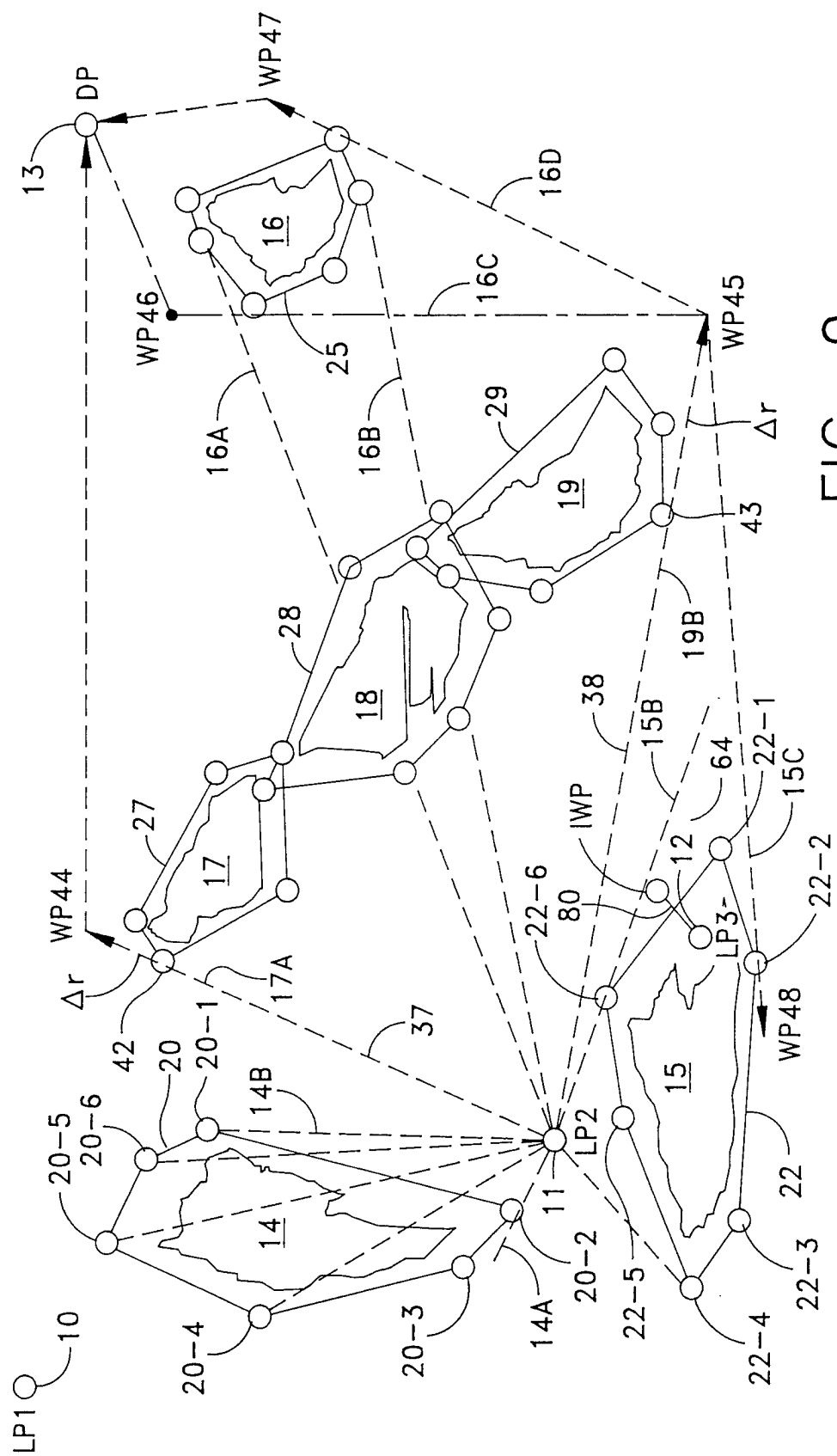


FIG. 9

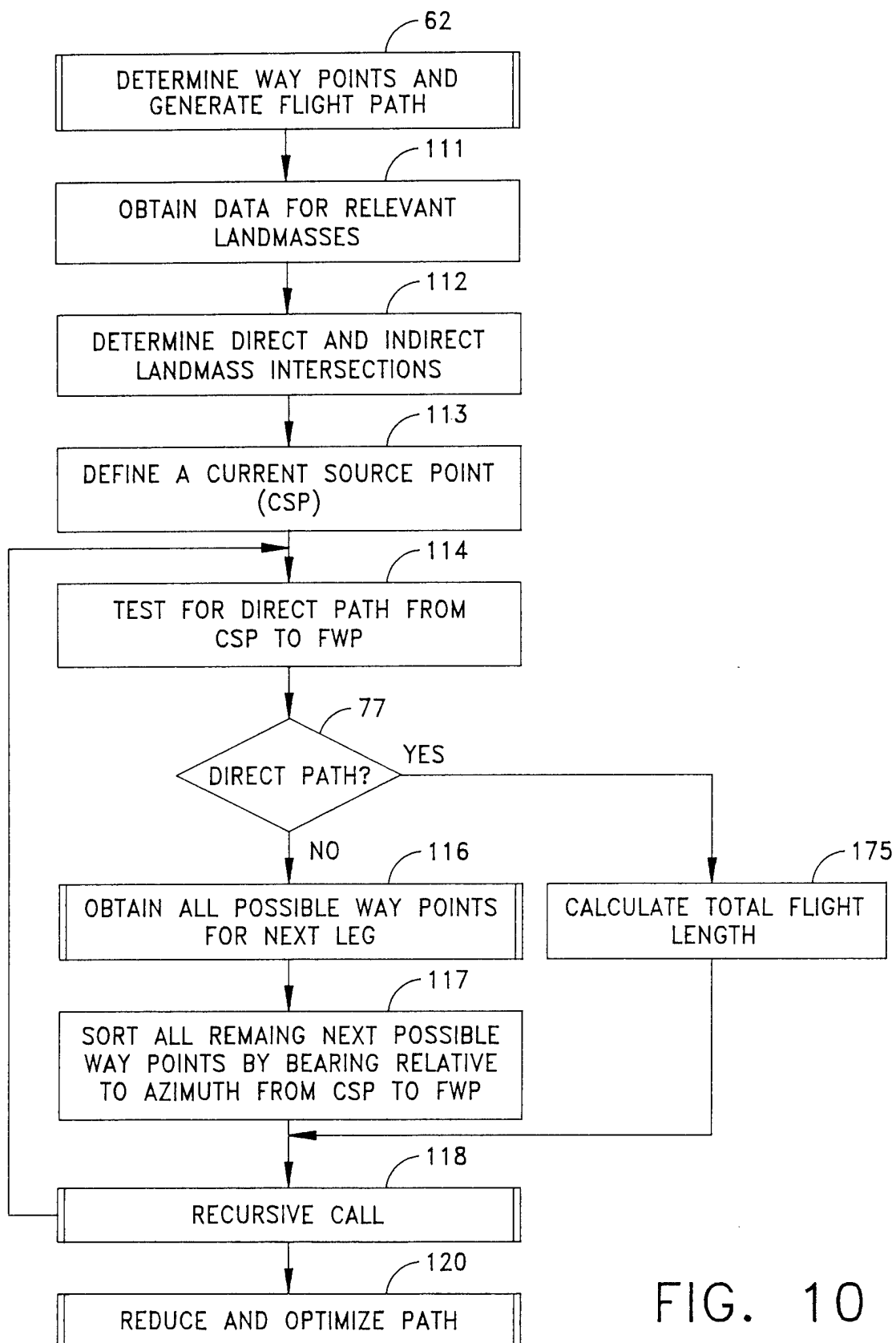
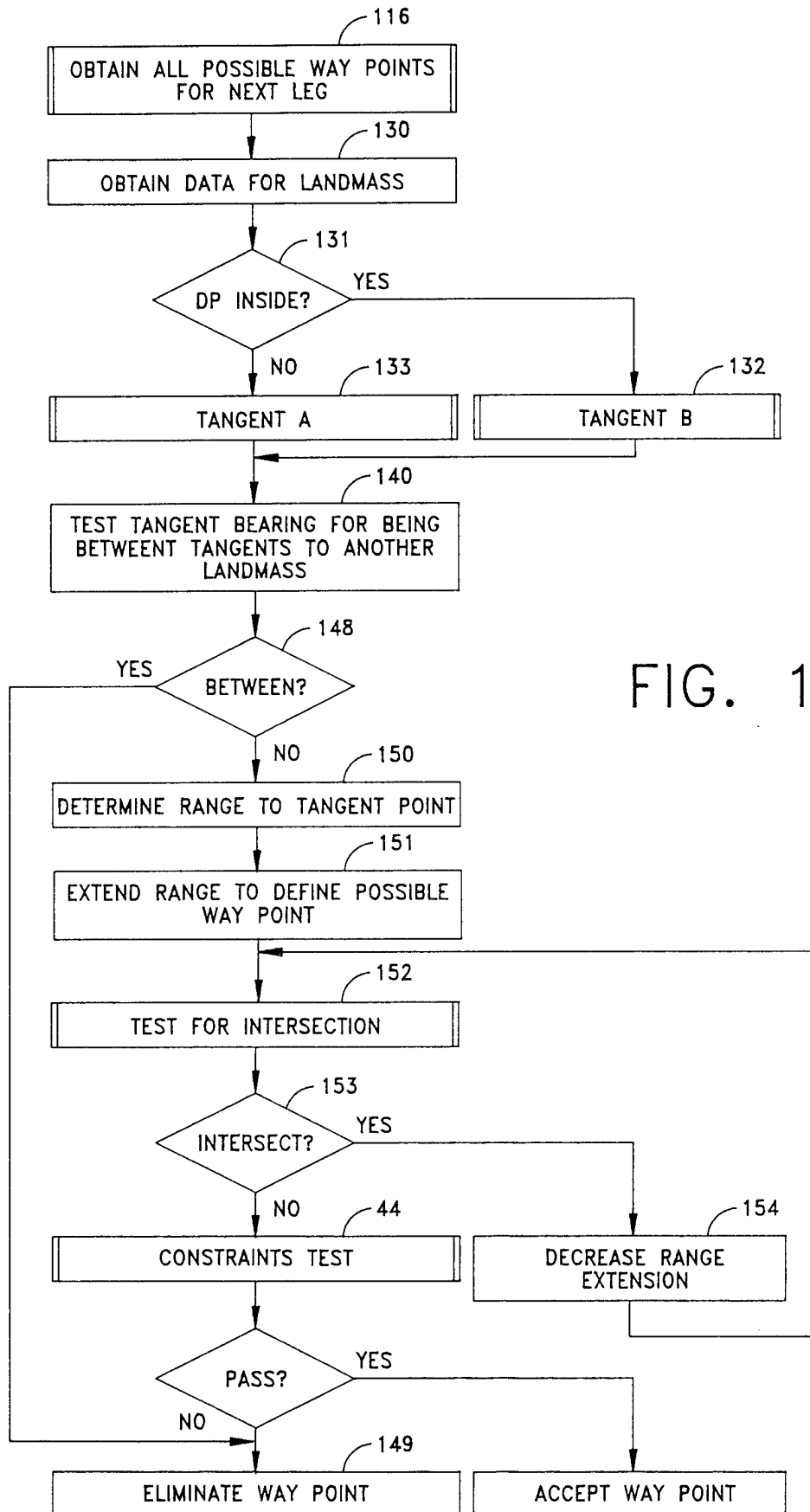


FIG. 10



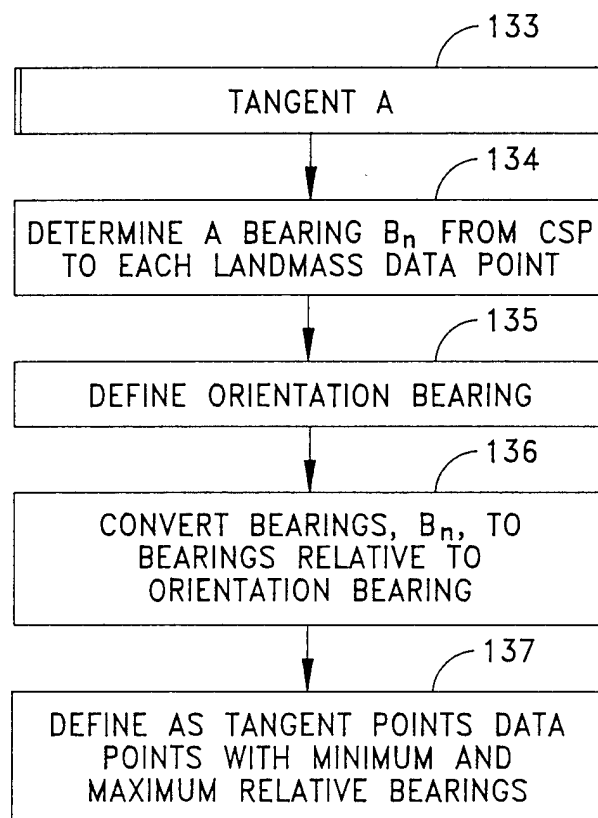


FIG. 12

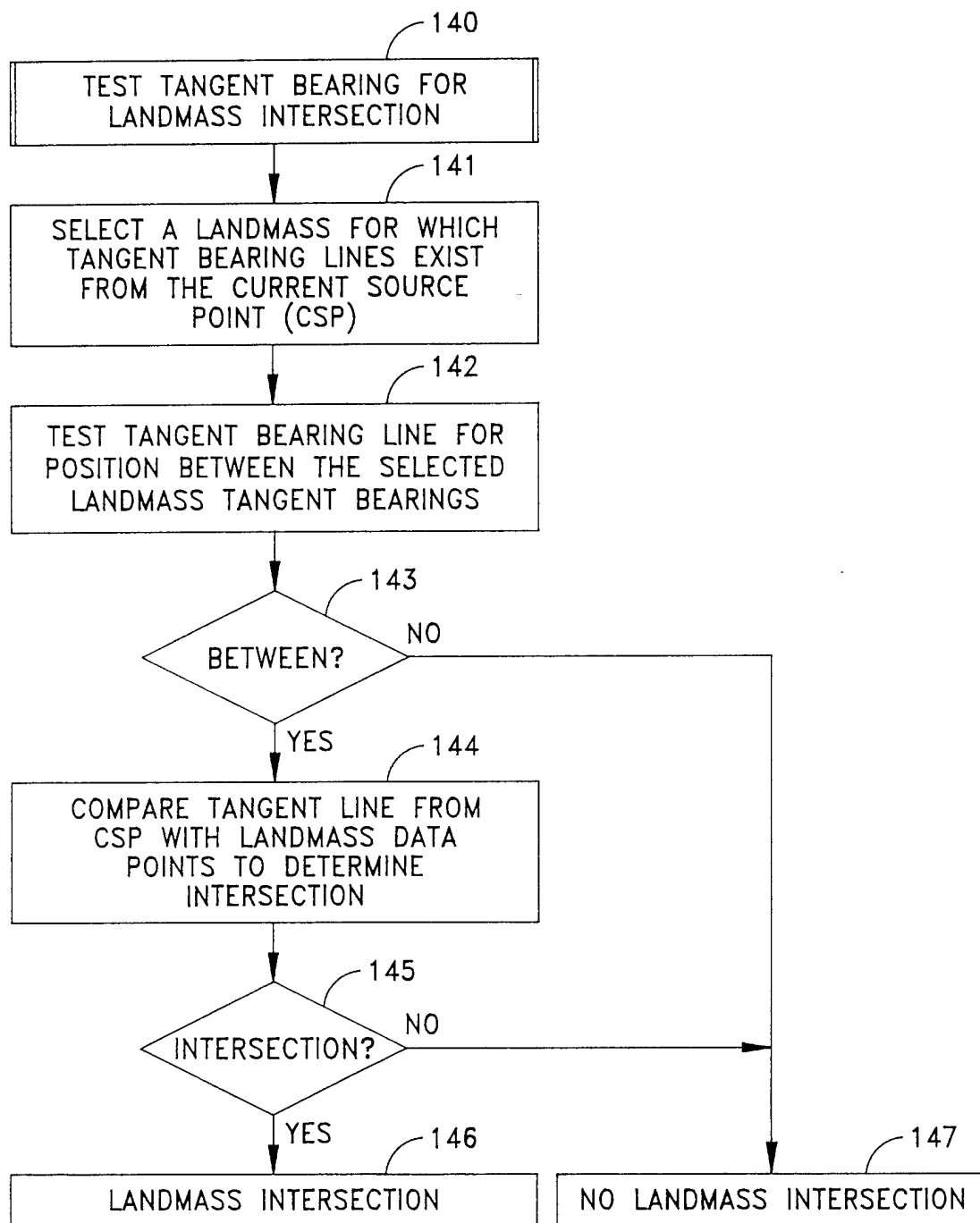


FIG. 13

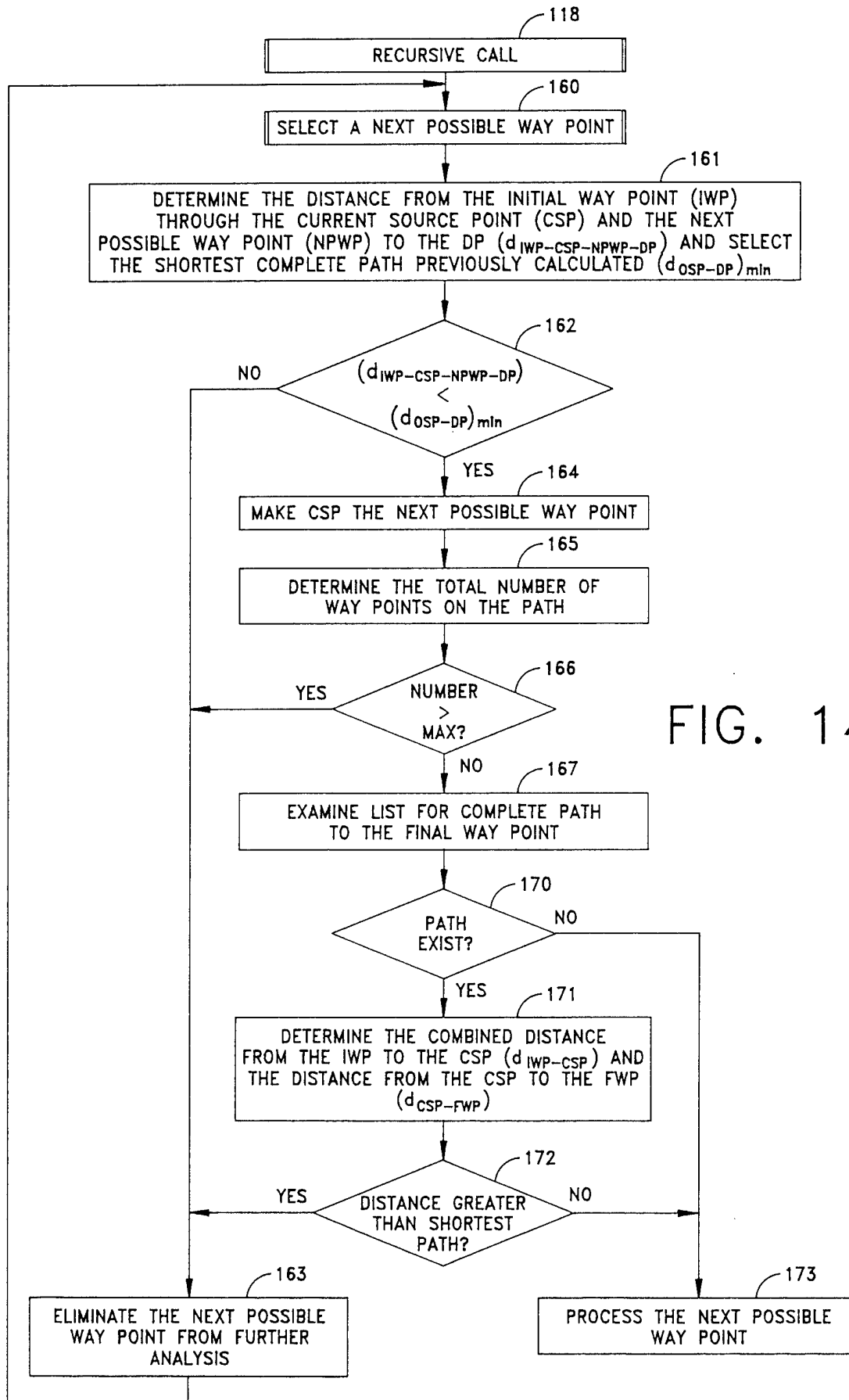


FIG. 14

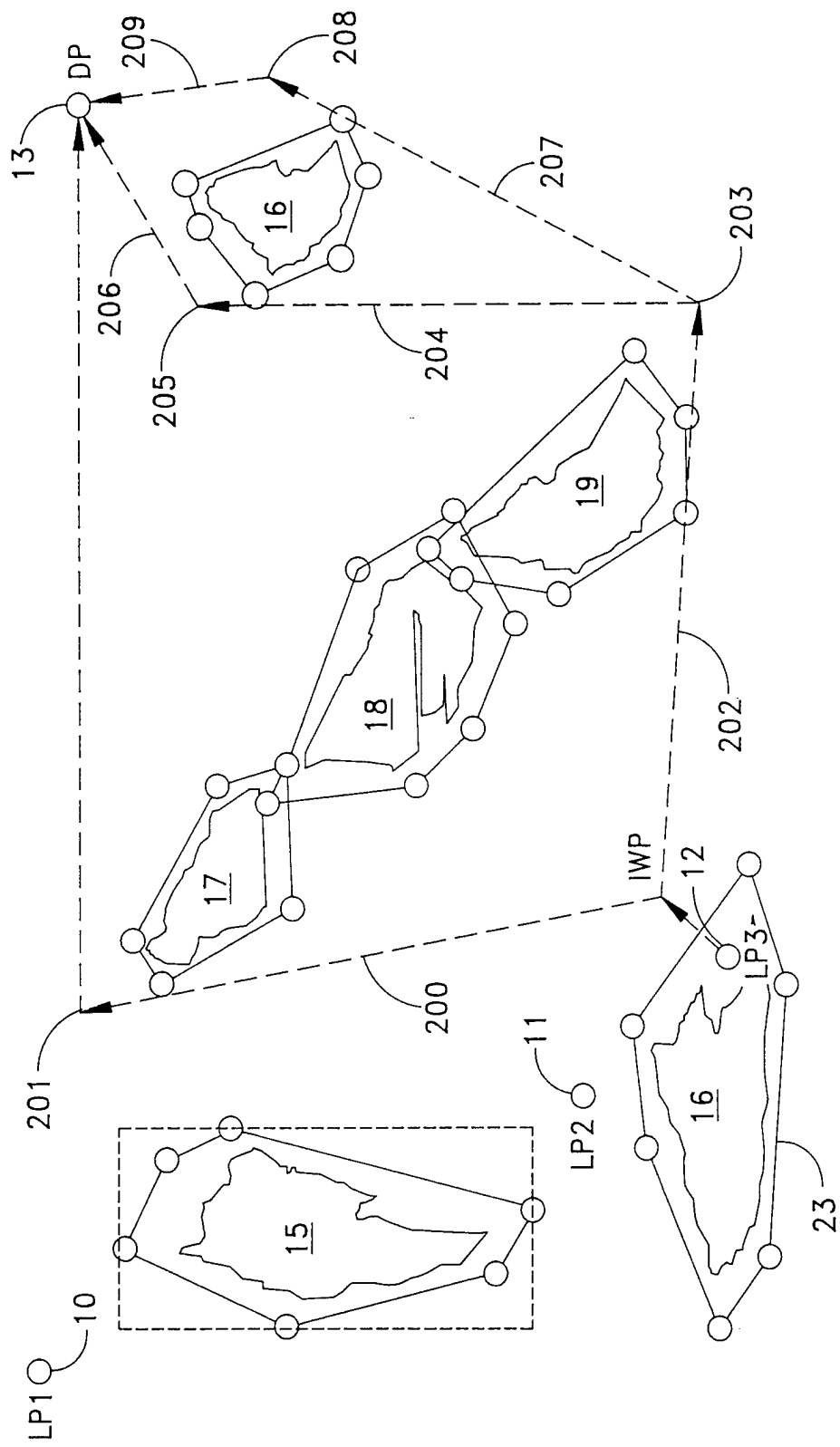


FIG. 15

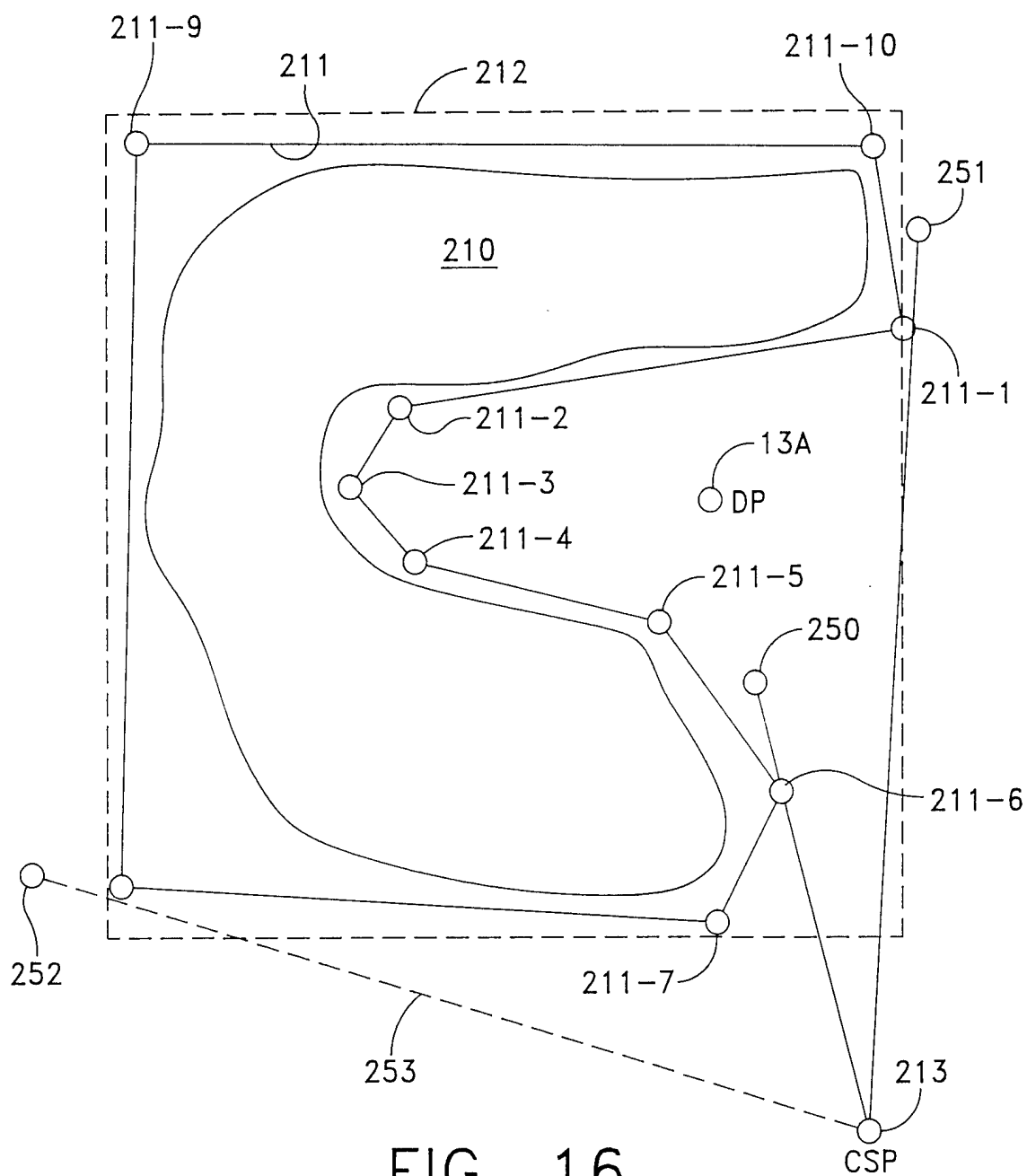


FIG. 16

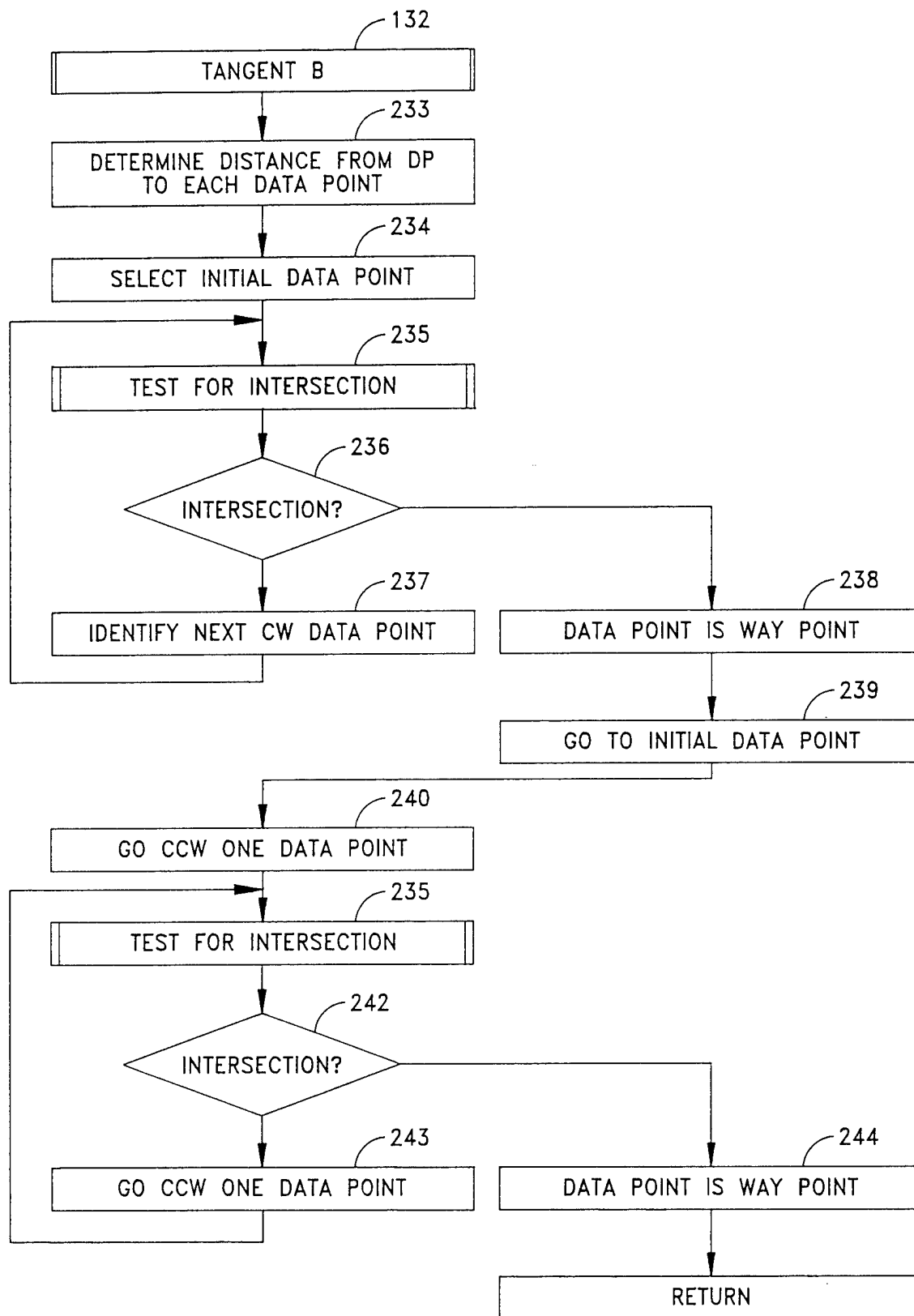


FIG. 17

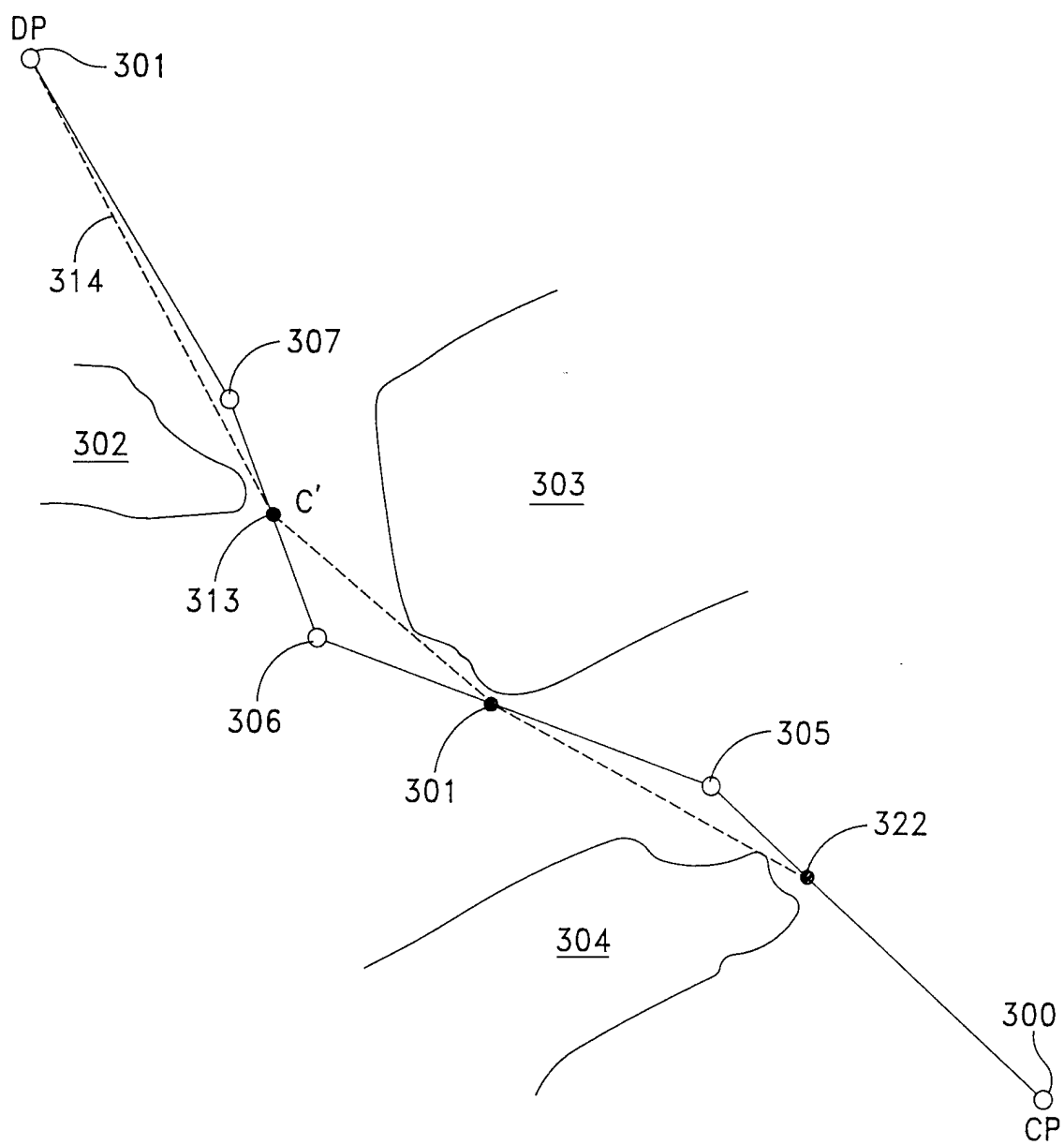


FIG. 18

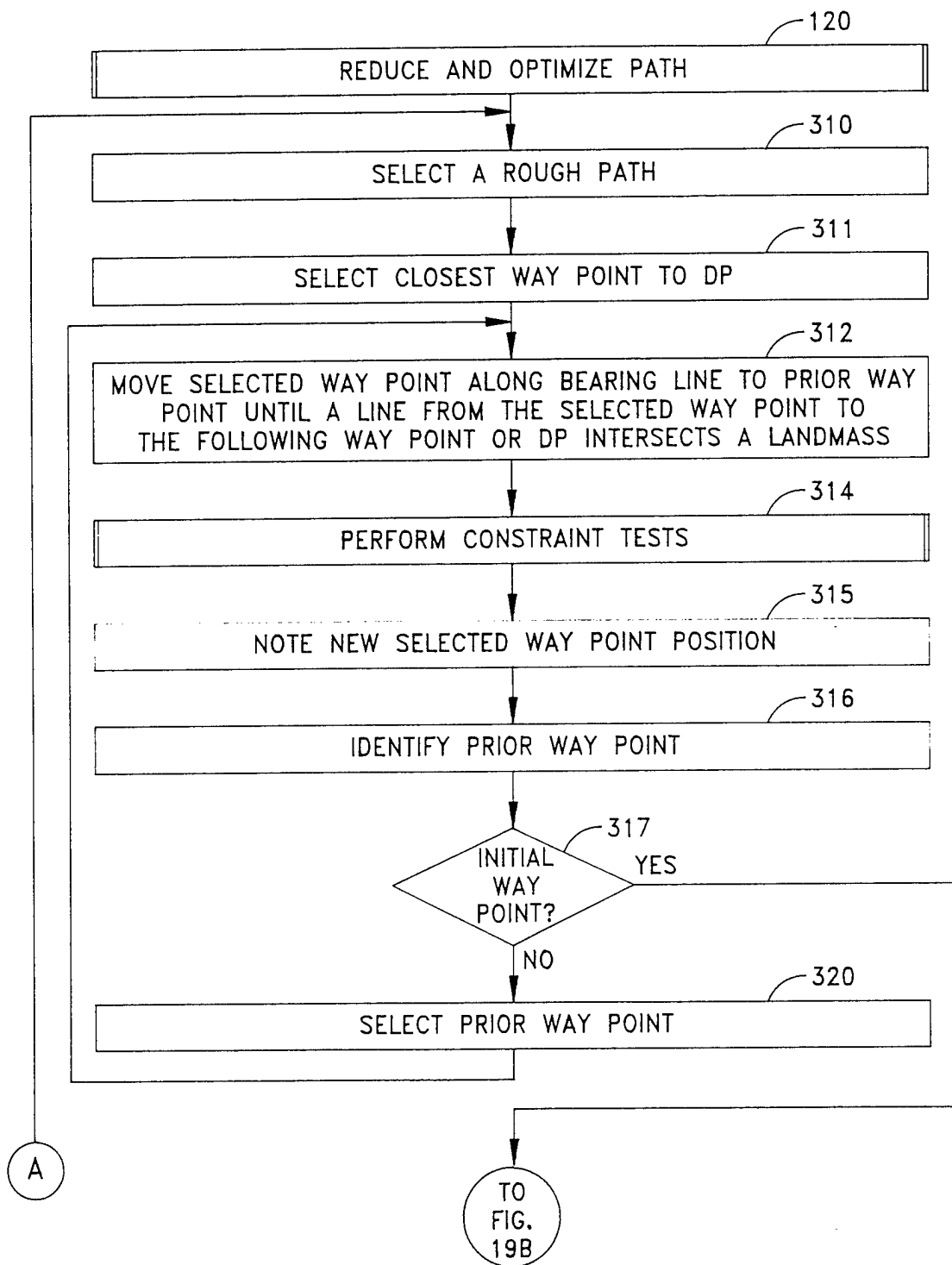


FIG. 19A

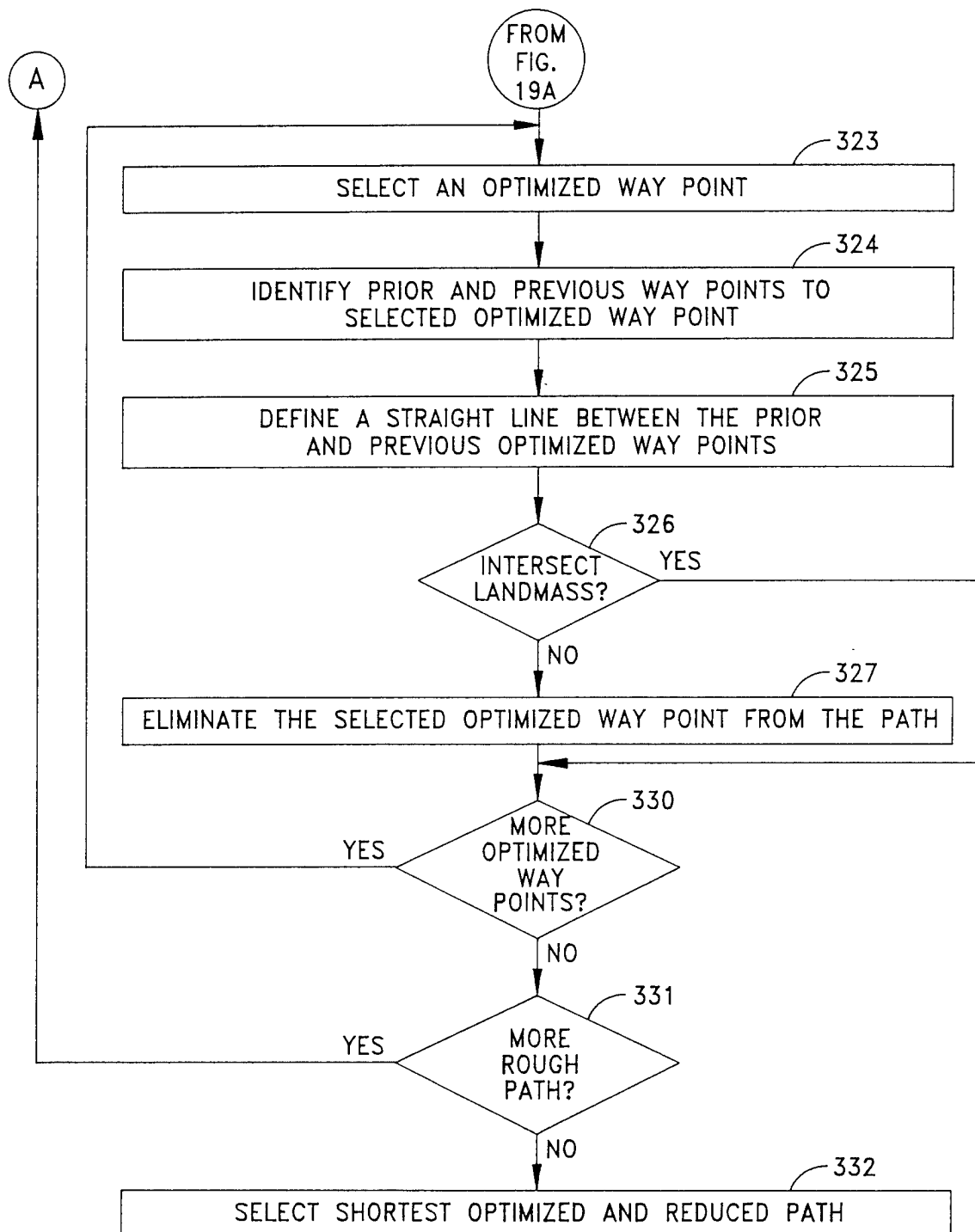


FIG. 19B