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<u>NOTICE</u>

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3 METHOD FOR GENERATING 2 AND 3-DIMENSIONAL FLUID MESHES FOR STRUCTURAL/ACOUSTIC 4 5 FINITE ELEMENT ANALYSIS IN INFINITE MEDIUM 6 7 STATEMENT OF GOVERNMENT INTEREST 8 The invention described herein may be manufactured and used 9 by or for the Government of the United States of America for 10 governmental purposes without the payment of any royalties 11 thereon or therefor. 12 13 BACKGROUND OF THE INVENTION 14 (1) Field of the Invention 15 The present invention is a method for creating frequency 16 dependent structural/acoustic meshes for three dimensional 17 finite element problems in infinite or semi-infinite mediums. 18 The method maps a three dimensional object to a rectilinear 19 accustic field that can easily be modified for changes in 20 frequency.

1 (2) Description of the Prior Art

2 Finite element analysis of structures submerged in an 3 infinite medium are used to determine the stresses acting on 4 prototype undersea hardware. Simple two dimensional axisymetric 5 models are often employed because three dimensional models are 6 too large and cumbersome to create. The most difficult problems 7 in creating meshes for conventional finite element solvers are: 8 (1) the generation of a three dimensional mesh that can 9 accommodate a range of frequency responses without overstepping 10 the memory requirements of the computer; and (2) the creation of 11 a mesh that can capture small details of a structure and also be 12 transmitted to a larger size mesh suitable for low frequency 13 evaluation.

14 Not all finite element software packages are capable of 15 solving structural acoustic problems. Often preprocessors are 16 used to create elements that can be imported into nonlinear 17 solvers. The preprocessors become slow and inefficient when 18 processing the large number of nodes to be used in a coupled fluid/structure infinite medium analysis. Also the input files 19 20 they generate require editing before they can be imported into 21 the solver. When the files get too large, they exceed the 22 memory allotment of the editor on the computer. It is more

efficient in these cases to generate meshes using the solver
 program mesh generator.

Finite element software requires that a structure in a free 3 field be surrounded by one wavelength of acoustic medium on all 4 5 sides. An absorption fluid impedance condition is then placed at the boundaries to prevent reflections in the medium that 6 7 could affect the structure's response. Another requirement is 8 that the acoustic element length be a minimum of one-sixth of a 9 wavelength for a solution. Good finite element mesh construction dictates that mesh nodes of linear elements have 10 11 maximum dimensional ratios of 3:1:1. It also dictates that the 12 included angles on quadrilateral and brick elements be greater than 5 degrees and less than 135 degrees. Often a model is 13 desired to be evaluated for a frequency range over 500 Hz for 14 15 steady state operation. Using the above criteria, a mesh with 16 one-eighth symmetry that could be used at a frequency of 500 $\ensuremath{\text{Hz}}$ 17 would have a maximum element length of 29.5 inches. If this 18 mesh were also to be used at 10 Hz, the mesh would have to 19 extend 5905 inches in three directions. This would result in a 20 model with 7,919,529 elements. Solving a problem of this size 21 at each frequency of interest becomes an expensive task.

SUMMARY OF THE INVENTION 1 Accordingly, it is an object of the present invention to 2 provide a method for generating variable frequency rectilinear 3 4 meshes in two and three dimensions. 5 It is a further object of the present invention to provide a method as above which can be implemented with any preprocessor 6 7 software or solver software. 8 It is yet another object of the present invention to 9 provide a method as above for generating the meshes more 10 efficiently. 11 The method of the present invention attains the foregoing 12 objects. 13 In accordance with the present invention, a method for efficiently generating meshes in two and three dimensions is 14 15 provided. The method involves generating several meshes, each covering a range of frequencies. The method of the present 16 invention broadly comprises the steps of: enclosing a structure 17 to be analyzed in a block of fluid having each of its sides 18 formed by a plurality of equally sized elements; determining a 19 20 bias factor and coordinates for the mesh; and generating a two

4

dimensional mesh using said coordinates and said bias factor to

1 transition from said equally sized elements to frequency 2 dependent sized elements. After the two dimensional mesh has been created, the method of the present invention goes on to 3 continue the transition by generating a three dimensional mesh 4 5 using said coordinates. 6 Other details of the method of the present invention, as 7 well as other objects and advantages attendant thereto, are set forth in the following description and the accompanying drawings 8 9 wherein like reference numerals depict like elements. 10 11 BRIEF DESCRIPTION OF THE DRAWINGS 12 FIG. 1 shows a model of a fluid block surrounding a 13 submerged structure; 14 FIG. 2 and 3 show flow charts for performing the method of 15 the present invention; 16 FIG. 4 shows a mapped 2-dimensional mesh generated using 17 the method of the present invention; and 18 FIG. 5 shows a mapped 3-dimensional mesh generated using 19 the method of the present invention.

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DESCRIPTION OF THE PREFERRED EMBODIMENT(S)

2 As previously discussed, the present invention is a 3 frequency dependent mesh-generating method for use with finite element solvers having structural acoustic analysis capability. 4 5 The method may be implemented using any suitable computer known 6 in the art that has been programmed in any suitable language. 7 Referring now to FIGS. 1 and 2, the first step 100 of the 8 method of the present invention is to enclose a three 9 dimensional body (not shown) to be analyzed in a block of fluid, 10 such as water, of equally sized elements. FIG. 1 illustrates a 11 one-eighth symmetry model of a cube shaped block 10 as an 12 example. The element size e should be the same on all sides and 13 is chosen in a manner consistent with well known finite element analysis techniques. The number of elements, n, on each side 14 can be the same or different. The height, width and length of 15 16 the block 10, as shown in FIG. 1, are ne (n*e).

As previously mentioned, the frequency range, such as 10Hz to 500Hz, for the entire analysis is preferably split into several sub-ranges. The dimensions of a grid or two dimensional mesh are then mapped. As shown in FIG. 4, the two-dimensional mesh includes low frequency boundaries 12 and 14 and a high

1	frequency maximum element length 16, which preferably equals
2	$\lambda/6$, where λ is the highest frequency acoustic wavelength. The
3	mesh of FIG. 4 is shown broken to illustrate that the low
4	frequency boundaries 12 and 14 are very distant from the origin
5	(0,0,0). As will be discussed in more detail hereinafter, the
6	mesh elements have varying dimensions, which are expressed in
7	terms of the coordinates A, B, and L and a bias factor c.
8	The method efficiently maps the nodes necessary to create
9	the frequency dependent mesh, both in two dimensions and in
10	three dimensions, using the following equations:
11	(1) $d_1 = \lambda/6\cos\theta\Sigma c^2$, where the index is summed from
12	0 to i
13	(2) $c = (18/\lambda * e * cos \theta)^{-1}$
13 14	(2) $c = (18/\lambda * e * cos \theta)^{-1}$ (3) $\theta = (sin^{-1}(n\lambda/6 - ne))/(\lambda/6\Sigma c^{-1}), i = 0, i$
14	(3) $\theta = (\sin^{-1}(n\lambda/6 - ne))/(\lambda/6\Sigma c^{2}), i = 0, i$
14 15	(3) $\theta = (\sin^{-1}(n\lambda/6 - ne))/(\lambda/6\Sigmac^{1})$, $i = 0$, i In the second step 101 of the method of the present
14 15 16	(3) $\theta = (\sin^{-1}(n\lambda/6 - ne))/(\lambda/6\Sigmac^2)$, $i = 0$, i In the second step 101 of the method of the present invention, the coordinates A, B and L, which are used to form
14 15 16 17	(3) $\theta = (\sin^{-1}(n\lambda/6 - ne))/(\lambda/6\Sigmac^2)$, $i = 0$, i In the second step 101 of the method of the present invention, the coordinates A, B and L, which are used to form the two-dimensional mesh of FIG. 4 and the three dimensional
14 15 16 17 18	(3) $\theta = (\sin^{-1}(n\lambda/6 - ne))/(\lambda/6\Sigma c^{1})$, $i = 0$, i In the second step 101 of the method of the present invention, the coordinates A, B and L, which are used to form the two-dimensional mesh of FIG. 4 and the three dimensional mesh of FIG. 5, are calculated. As shown in more detail in FIG.
14 15 16 17 18 19	(3) $\theta = (\sin^{-1}(n\lambda/6 - ne))/(\lambda/6\Sigma c^{-})$, $i = 0$, i In the second step 101 of the method of the present invention, the coordinates A, B and L, which are used to form the two-dimensional mesh of FIG. 4 and the three dimensional mesh of FIG. 5, are calculated. As shown in more detail in FIG. 3, this involves, in step 102, defining the high and low

1 discussed, it has been found that a desirable element length is 2 $\lambda/6$.

3 In step 106, the minimum mesh boundary distance from the 4 lowest frequency wavelength is determined. The minimum boundary distance for low frequency is $\lambda_{\rm L},$ where $\lambda_{\rm c}$ 5 6 is the acoustic wavelength at the low frequency limit. In step 107, a first value is chosen for i. The value is 7 8 chosen to be less than the optimal number of transition 9 elements. A value of i = 1 can be used as a starting point if a 10 more suitable starting value cannot be intuitively determined. 11 θ_1 , as used herein, defines the increment in element 12 thickness. See FIG. 4. In step 108, it is assumed that θ is 13 15° . In step 110, the bias factor c is calculated using equation 14 (2). 15 In step 112, a new θ_1 is calculated using equation (3). If the new θ_i is greater than 0° and less than $18^\circ,$ the method 16 17 proceeds from step 114 to step 116. If the new θ_1 is outside of 18 this range, then the method proceeds to step 118 where i is

20 The value of i is preferably iterated until a minimum value is 21 found that results in realistic (nonnegative values) and θ_1 22 having a value of less than 18°. If θ_1 is greater than 18

19

increased.

8

Thereafter steps 108, 110, 112 and 114 are repeated.

degrees, included angle problems may appear later in the method.
Note that if the value of i chosen in step 107 is too large,
then the number of transition elements will not be a minimum.
In step 116, coordinates A, B, and L are calculated using
equations (4) - (6)

(4)

 $6 \qquad A = ne + dl$

 $7 \qquad B = n\lambda/18 \tag{5}$

8 $L = \lambda_{L}$ (6)

9 Having determined the coordinates A, B, and L and the bias 10 factor c, the two and three dimensional meshes, respectively shown in FIGS. 4 and 5, may be generated or constructed using 11 12 commercial preprocessors in step 120. Acceptable preprocessors 13 include ABAQUS, HYPERMESH and IDEAS. To construct the two 14 dimensional mesh shown in FIG. 4, one first computes the length $d_{\scriptscriptstyle 2}$ which is A - B. Then i equally spaced element nodes are 15 16 mapped along this edge to create element length e_2 , which is equal to d_2/i . For the two- and three-dimensional meshes of 17 18 FIGS. 4 and 5, i is shown as 5. Therefore, $e_2 = d_2/5$ and five nodes are mapped between coordinates (A, B, 0) and (A, A, 0) and 19 between coordinates (B,A,O) and (A,A,O). The ratio of ε_{λ} to $\lambda/6$ 20

is checked to verify the elements in the remaining area, i.e., 1 2 the area defined by coordinates (n_{p}, n_{p}) , (A, B), (A, A) and (B, A)of FIG. 4, have a ratio of 3:1. The length of e₂ preferably is 3 in the range of $\lambda/18 \le e_1 \le \lambda/6$. The maximum included angles of 4 the elements in the mesh are θ_2 and θ_3 , where $\theta_2 = 90 - 2*\theta_1$ and θ_3 5 = 90 + θ_1 . The mesh of FIG. 4 is checked for appropriate 6 7 included angles, i.e. $\theta_2 > 45^\circ$ and $\theta_3 < 135^\circ$. 8 It can be seen from FIG. 4 that n nodes are mapped between coordinates (A,O,O) and (A,B,O). For the mesh of FIG. 4, the 9 10 block 10 was taken as a cube, therefore, n nodes are also mapped 11 between coordinates (0,A,O) and (B,A,O). The spacing of nodes 12 along the length d, varies with c^{i} , from a value of $c^{i}(\lambda/6)$ 13 adjacent block 10 to $c^{1}(\lambda/6)$, or $\lambda/6$, as shown. It is noted that 14 to maintain the 3:1 ratio, $c^{1}(\lambda/6)$ should be less than or equal 15 to 3e. To complete the mesh from a distance A to low frequency 16 boundaries 12 and 14, additional nodes are spaced at $\lambda/6$.

17 If the ratio of e_2 to $\lambda/6$ is less than 0.3333, or included 18 angles are not acceptable, then the method is retried with a 19 higher frequency range or a larger value of i. Lower 20 frequencies can be accommodated by copying additional elements 21 in all directions. The element length can be extended in

increments of λ/6 in the x and y directions. After a suitable
 2-dimensional mesh is formed, a three dimensional mesh is
 generated in step 120 by mapping the two dimensional space of
 FIG. 4 to three dimensions as shown in FIG. 5.

5 The mapping of fluid meshes to rectilinear coordinates with 6 variable frequency ranges for use with commercial software is 7 novel and unique. The optimization of the transition from a 8 structural length on the order of "e" to a much greater length 9 " $\lambda/6$ " also distinguishes the method of the present invention 10 from other methods.

If desired, the method of the present invention may be performed with alterations in the recommended angles for the start of the iteration process and in the number of elements per wavelength. The outer boundary could be further or closer to the structure depending on the desired accuracy of the solution. The method of the present invention has particular utility in the generation of ABAQUS input meshes.

It is apparent that there has been described in accordance with the present invention a method for generating 2 and 3dimensional fluid meshes for structural/acoustic finite element analysis in an infinite medium which meets the objects, advantages, and means set forth hereinbefore. While the method

of the present invention has been described in the context of specific embodiments thereof, other alternatives, modifications and variations will become apparent to those skilled in the art having read the foregoing description. Therefore, it is intended to embrace all such alternatives, modifications and variations.

1 Attorney Docket No. 79284

3	METHOD FOR GENERATING 2 AND 3-DIMENSIONAL
4	FLUID MESHES FOR STRUCTURAL/ACOUSTIC
5	FINITE ELEMENT ANALYSIS IN INFINITE MEDIUM
6	
7	ABSTRACT OF THE DISCLOSURE
8	The present invention relates to a method for generating 2
9	and 3-dimensional fluid meshes for structural/acoustic finite
10	element analysis in an infinite medium. The method broadly
11	comprises the steps of: enclosing a structure to be analyzed in
12	a block of fluid; determining a bias factor and coordinates for
13	the mesh; and generating at least one of a two dimensional and a
14	three dimensional mesh using the coordinates and the bias
15	factor.



FIG. 1



FIG. 2



FIG. 3



FIG. 4

