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**ULTRASHORT-PULSE FIBER LASER WITH A
DISPERSION-MANAGED CAVITY**

10

BACKGROUND OF THE INVENTION

15 **Field of the Invention**

This invention in general refers to dispersion management within a laser cavity and more particularly to a laser apparatus where dispersion management is used to enhance the performance of the laser by reducing the timing jitter of the pulses produced by the laser and by reducing the occurrence of pulse dropouts or multiple pulse production.

20

Description of the Related Art

25 Dispersion management within a laser cavity allows a fiber laser to produce optical pulses of lower amplitude and phase noise and with greater immunity to pulse dropouts than is otherwise possible. These features are of great importance to lasers used as sources in telecommunications applications, as research instruments, or in optical-to-digital conversion and analysis application.

30

Dispersion management is a concept usually encountered only in optical soliton fiber transmission applications. In that field, it has been found that the use of lengths of at least two

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5 types of fibers with different chromatic dispersions, usually of
differing signs, but with a (usually small) net anomalous
dispersion, yields a transmission medium with distinct advantages
over one with a uniform dispersion: i) the optical energy of the
solitons carrying information is greater than those in a uniform-
10 dispersion fiber with the net dispersion, yielding a greater
signal-to-noise (S/N) ratio of the signal; ii) the timing jitter
in the system is lower; iii) the pulses tend to have a Gaussian
temporal profile, reducing pulse-to-pulse interactions; iv)
nonlinear pulse interactions such as four-wave mixing are
15 strongly reduced because of the strong local dispersion. The
strength of dispersion management is usually expressed as a
unitless parameter

$$\gamma = 2 \sum_n |\beta''_n \ell_n| / \tau^2$$

20 where β''_n and ℓ_n are the dispersion and length respectively, of
fiber segment n, and τ is the pulse duration.

Dispersion-managed solitons have two salient properties for
the purposes herein: their energy is greater than that of an
equivalent uniform-dispersion soliton, and their pulse duration
25 changes much less with a change in pulse energy than does an
equivalent uniform-dispersion soliton.

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5 In an actively harmoncally mode-locked soliton laser four
regimes of operation are expected to be seen as the amount of
energy per pulse is varied: (i) At the lowest energies, the
laser cannot form solitons, and a very noisy output of long-
duration pulses is evident. (ii) At somewhat higher energies,
10 there is not enough power available for a full train of solitons,
so the laser can form either a train of long-duration pulses or
an occasional soliton. The laser loss is higher for long-
duration pulses, since they would be clipped by the finite
duration of the amplitude mode-locking time window. Therefore a
15 combination of solitons and dropouts is observed. (iii) At
higher frequencies, the laser can produce an uninterrupted stream
of solitons. In this regime, the pulse duration becomes briefer
as the pulse energy increases. (iv) At the highest energies,
pulses are prevented from becoming more brief by the fact that
20 energy is lost when they become so brief and their bandwidth
consequently becomes so large that the pulses are clipped
spectrally by the finite gain bandwidth (or the bandwidth of an
intracavity bandpass filter). Then multiple pulses begin to
appear in each time slot.

25 The desirable operating regime from a telecommunications
standpoint is (iii), in which an uninterrupted stream of pulses
is generated. The maximum and minimum pulse widths which define
the boundaries of this regime are determined by the details of

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5 the laser parameters.

10 In a laser of uniform dispersion, the pulse energy range over which the laser operates in the stable regime can be as small as 30%. One characteristic of a dispersion-managed laser is that the pulse duration decreases by comparatively little as the pulse energy increases; as a consequence, the laser can operate in the stable regime over a pulse energy range of as much as a factor of 100.

BRIEF SUMMARY OF THE INVENTION

15

The object of this invention is to provide a dispersion-managed soliton laser exhibiting a greater immunity to pulse dropouts than an equivalent uniform-dispersion soliton laser along with lower amplitude noise and timing jitter.

20

Another objective of this invention is to produce a soliton fiber laser that can produce pulses with adjustable temporal and spectral intensity profiles and durations to suit particular applications.

25

These and other objectives are attained by ultrashort fiber laser with a dispersion-managed cavity. The laser is an actively mode-locked sigma laser, typically locked at a repetition rate of 10 GHz, driven by an external frequency source and actively length stabilized, and nearly 10,000 pulses circulate within the

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5 laser cavity. A Mach-Zehnder modulator is placed in a loop of
polarization-maintaining (PM) fiber. The polarization state of
light injected into the non-PM branch evolves in a random manner
but is transformed into an orthogonal state by a Faraday mirror;
linearly polarized light injected into the branch by a polarizing
10 beamsplitter returns to the beamsplitter also linearly polarized
but rotated by 90° . The cavity of the laser is composed of
several fibers. The average dispersion D_{av} is anomalous and is
approximately equal to $2 \text{ ps}/(\text{nm}\cdot\text{km})$. The measured noise in the
output of the laser is very low, the rms amplitude noise is less
15 than 1.1% and the rms timing jitter is less than 160
femtoseconds.

BRIEF DESCRIPTION OF THE DRAWINGS

20 **Figure 1a** shows a basic schematic of a dispersion-managed,
actively mode-locked, all polarization-maintaining fiber laser.

Figure 1b shows a basic schematic of a dispersion-managed,
actively mode-locked, all polarization-maintaining fiber laser
containing an optical bandpass filter.

25 **Figure 1c** shows a basic schematic of a dispersion-managed,
actively mode-locked, all polarization-maintaining fiber laser
containing an optical isolator.

Figure 1d shows a basic schematic of a dispersion-managed,
actively mode-locked, all polarization-maintaining fiber laser

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5 containing a PZT cylinder-based length-stabilizing system.

Figure 1e shows a basic schematic of a dispersion-managed, actively mode-locked, all polarization-maintaining fiber laser containing a air gap-based length-stabilization system.

10 **Figure 2a** shows an ultrashort-pulse dispersion-managed soliton sigma fiber laser with the optical modulator in the polarization-maintaining branch.

Figure 2b shows an ultrashort-pulse dispersion-managed soliton sigma fiber laser with the optical modulator in the birefringence-compensating branch.

15 **Figure 2c** shows a regeneratively-locked laser without length-stabilization.

Figure 2c shows a regeneratively-locked laser with length-stabilization.

20 **Figure 3a** shows an infinite-persistence oscilloscope trace of the lowest optical powers of the detected optical pulses of a duration of ~5 ps on the left and an autocorrelation trace on the right the three regimes of operation as the amount of energy per pulse is varied.

25 **Figure 3b** shows an infinite-persistence oscilloscope trace of the lowest boundary of Regime II, showing the pulse dropouts whose number decreases from lower to higher powers, and pulse durations between 2.6 and 3.3 ps.

Figure 3c shows an infinite-persistence oscilloscope trace

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5 of the upper boundary of regime II, showing the pulse dropouts whose number decreases from lower to higher powers, and pulse durations between 2.6 and 3.3 ps.

10 **Figure 3d** shows an infinite-persistence oscilloscope trace of the lower boundary of regime III, showing filled pulse trains and pulse durations between 1.4 and 3.3 ps.

Figure 3e shows an infinite-persistence oscilloscope trace of the highest experimental power, showing filled pulse trains and pulse durations between 1.4 and 3.3 ps.

15 **Figure 4** shows a plot of the bit-error rate in a data transmission experiment using the dispersion-managed soliton sigma laser.

Figure 5a shows the temporal characteristics of the output pulses.

20 **Figure 5b** shows the spectral characteristics of the output pulses.

Figure 6a shows a basic dispersion-managed, actively mode-locked, partially polarization-maintaining fiber, partially non-polarization-maintaining fiber laser with a polarization controller.

25 **Figure 6b** shows a basic dispersion-managed, actively mode-locked, non-polarization-maintaining fiber laser with a polarization controller.

Figure 6c shows a basic dispersion-managed, actively mode-

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5 locked, partially polarization-maintaining, partially non-polarization-maintaining fiber laser containing an optical isolator, a birefringence-compensating branch, a polarizing beamsplitter, an optical bandpass filter, and a Faraday mirror.

10 **DETAILED DESCRIPTION OF THE INVENTION**

In a first preferred embodiment a basic mode-locked pulse dispersion-managed soliton sigma laser 10, as shown in **Figure 1a**, comprises a dispersion-managed cavity 11 having at normal dispersion medium 13 and an anomalous-dispersion medium 15. The
15 normal dispersion medium 13 and the anomalous-dispersion medium 15 has opposite signs of chromatic dispersion for stretching the pulse width and lower the peak power of the optical pulse. An optical signal within a loop 21 is modulated by applying a signal from a periodic drive 12 applied to a modulator by an optical
20 modulator 14, and amplified by an optical amplifier 17. An optical coupler 19 removes the optical signal from the loop and applies it to other processing elements (not shown). The periodic drive 12 may be an external frequency source such as a master clock (synthesizer). The loop 21 is, preferably, a
25 polarization-maintaining optical fiber.

In a second embodiment of a basic dispersion-managed, actively mode-locked, all polarization-maintaining fiber laser 20, as shown in **Figure 1b**, the same optical circuit is utilized,

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5 as that shown in **Figure 1a**, however an optical tunable or
variable bandpass filter **24** is inserted into the loop **21** prior to
the modulator **14** to pass a select band of optical frequencies.

In another embodiment of a basic dispersion-managed,
actively mode-locked, all polarization-maintaining fiber laser
10 **30**, as shown in **Figure 1c**, the same optical circuit is utilized,
as that shown in **Figure 1a**, however an optical isolator **46** is
inserted into the loop **21** prior to the modulator **14** to ensure
unidirectional flow of optical light.

In another embodiment of a basic dispersion-managed,
15 actively mode-locked, all polarization-maintaining fiber laser
40, as shown in **Figure 1d**, the same optical circuit is utilized,
as that shown in **Figure 1a**, however an optical fiber wound on a
PZT cylinder **27** with length-stabilizing electronics **28** controls
the length of the optical fiber

20 In another embodiment of a basic dispersion-managed,
actively mode-locked, all polarization-maintaining fiber laser
60, as shown in **Figure 1e**, the same optical circuit is utilized,
as that shown in **Figure 1a**, however an adjustable air gap **48** with
length-stabilizing electronics **28** controls the length of the
25 optical fiber

In a second preferred embodiment of the ultrashort-pulse
fiber laser, as shown in **Figure 2a**, the laser **70** is an actively
mode-locked sigma laser, driven by an external frequency source,

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5 or master clock (synthesizer) **12** and actively length-stabilized.
An optical modulator **14**, such as a Mach-Zehnder modulator, is
placed in a loop **21** of polarization-maintaining (PM) fiber
forming a polarization-maintaining loop. To ensure
unidirectional operation, an optical isolator **23** is contained
10 within the laser cavity. The polarization state of light injected
into the birefringence-compensating section or branch **18** evolves
in a random manner but is transformed into an orthogonal state by
a Faraday mirror **22**; linearly polarized light injected into the
birefringent-compensating branch **18** by the polarizing
15 beamsplitter **24** returns to the beamsplitter **24** also linearly
polarized but rotated by 90°. An optical circulator may be used
in place of a polarizing beamsplitter **24** if so desired. An
optical gain medium within the laser cavity amplifies the
intensity of light circulating in the cavity. The linearly
20 polarized light injected into the birefringence-compensating
branch **18** passes through a section of optical fiber wrapped
around a piezo electric cylinder **27** forming a laser cavity whose
length is controlled by the application of an electrical signal
from length-stabilization electronics **28**. The means for
25 controlling the length of the laser cavity may also be through
the use of an adjustable air gap.

In another preferred embodiment **80**, **Figure 2b**, the optical
modulator **14** may be placed elsewhere in the cavity, such as in

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5 the birefringent-compensating branch **18**, adjacent to the Faraday mirror **22**. The modulator **14** should be very close to the end of the birefringent-compensating branch **18** since it must be "open" both for incident and returning light.

10 The cavity of the laser **70** is composed of several fibers, which types, lengths, and locations are set forth in **Table 1**. The average dispersion D_{av} is anomalous and is approximately equal to 0.1 ps/(nm·km); the total cavity is typically ~ 195 m.

15 The lasers **70**, **80**, and **90** are mode-locked at a repetition rate of, preferably, 10 GHz, by driving the modulator **14** with an external periodic drive **12** at 10 GHz which is an integral of the fundamental cavity frequency. Within the laser cavity there are nearly 10,000 pulses circulating and it is usually difficult to attain a uniform stream of uninterrupted pulses in an actively mode-locked laser with such a high harmonic order.

20 In another preferred embodiment **90** as shown on **Figure 2c**, a regenerative mode-locked device is shown. An optional soliton propagation fiber **32** is placed in the optical circuit prior to the Faraday mirror **22**. The optical signal is modulated in a modulator **14** with an electrical signal that is the product of a
25 regenerative cycle. The regenerative cycle is comprised of removing an optical signal from the loop by the use of a pair of optical couplers **19** and **33**, converting the optical signal to an electrical signal in a photodetector **38**, removing any unwanted

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5 frequencies in a bandpass filter 36, adjusting the phase 37, amplifying the phase adjusted electrical signal, amplifying it and applying it to the optical signal in the loop in a modulator 14.

10 In another preferred embodiment 100, as shown on Figure 2d, a regenerative mode-locked device with length-stabilization is shown. The optical signal is modulated by a regenerative electrical signal similar to that shown in Figure 2c, however, a electrical signal from after a bandpass filter 36 is applied after phase adjustment 42 to the length stabilization electronic
15 circuit 28 to control an optically wound PZT cylinders 27 diameter, similar to that described for Figure 2a.

The lasers 70, 80, 90, and 100 exhibit a measured pulse dropout rates below 10^{-14} . The measured noise in the output 26 of the lasers 70, 80, 90, and 100 are also very low: the rms
20 amplitude noise is less than 1.1% and the rms timing jitter is less than 160 femtoseconds.

In the subject invention, three regimes are predicted, See Figures 3a through 3e, and show long-duration sampling oscilloscope pulse traces, on the left, paired with the pulse autocorrelation, on the right, for a series of average pulse
25 powers expressed as a fraction of the maximum pulse power P_{\max} . The Roman numerals signify the three observed regimes of operation of the laser. The highest energy regime cannot be

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5 obtained with the optical amplifier powers available, however, modeling shows that stable operation may be obtained over a range of pulse energies of at least a factor of three.

TABLE 1

10	Fiber Type	Location	Length(m)	Dispersion D (ps/[nm km]) *
15	Polarization-maintaining (PM)	PM Loop	15	~17
	SMF-28	Birefringence-compensating branch	10†	~17
20	Dispersion-shifted (DSF)	"	55†	~10
25	Dispersion-compensating (DCF)	"	15†	- 65
	Gain fiber (EFA)	"	10†	~8

30 It is evident in **Figures 3a** through **3e** that the amplitude noise of the laser output decreases as the pulse energy is increased; the same is true for the timing jitter. The decrease in noise levels as pulse energy is increased is also a consequence of dispersion-management: a dispersion-managed
35 soliton has a higher energy than an equivalent uniform-dispersion

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5 soliton, and the noise-inducing effects of amplified spontaneous emission in the fiber amplifier are therefore minimized.

Figure 4 is a plot of the bit-error rate in a data transmission experiment using the dispersion-management soliton sigma laser, demonstrating that its pulse dropout ratio is as low
10 as 10^{-14} . These back-to-back bit-error ratio measurements were made at 10Gb/s using the soliton sigma laser as a source.

Figures 5a and **5b** show the temporal and spectral characteristics of the output pulses; pulse duration is 1.1 picoseconds generated with the dispersion-managed soliton laser,
15 the autocorrelation, on the left, and optical spectrum, on the right. The pulse is approximately Gaussian in temporal shape.

A dispersion-managed soliton laser exhibits a greater immunity to pulse dropouts than an equivalent uniform-dispersion soliton laser and exhibits lower amplitude noise and timing
20 jitter. Also, a dispersion-managed soliton fiber laser can produce pulses with adjustable temporal and spectral intensity profiles and durations to suit particular applications.

The critical factor in the dispersion-managed soliton fiber laser is the existence of a dispersion map in the laser cavity;
25 other construction details of the laser may vary.

(i) A passively mode-locked dispersion-managed laser should exhibit superior characteristics to an equivalent uniform-managed soliton laser -- its amplitude noise and timing jitter should be

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5 lower.

(ii) An actively mode-locked laser can be either amplitude- or phase-modulated using any of a number of modulator types.

10 (iii) An actively mode-locked laser can be mode locked by an external frequency standard and length-stabilized by a number of means, such as electronic circuits; such stabilization techniques are well known to those skilled in the art,.

(iv) An actively mode-locked laser can be regeneratively mode-locked.

15 (v) A dispersion-managed laser can have more or all types of its fibers compose of PM fiber, so that fewer fibers need be placed in the birefringence-compensating branch; if all fiber types are polarization-maintaining, the birefringence-compensating branch is not needed.

20 (vi) Although it is preferred if the dispersion-managed laser cavity be partially polarization-maintaining and birefringent-compensating, as in **Figures 2a** and **2b**, it may also be partially polarization-maintaining and partially non-polarization-maintaining, as shown in **Figure 6a** and **6c**, non-polarization-maintaining, as shown in **Figure 6b**, or totally
25 polarization-maintaining, as shown in **Figure 1a**.

(vii) A dispersion-managed laser can have several of its component fibers serving more than one purpose. For instance, the optical gain fiber might be designed to have a large normal

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5 dispersion, eliminating the need for a separate dispersion-compensating fiber.

(viii) Normal-dispersion fiber might not be necessary in a dispersion-managed laser. Component fibers that possess anomalous dispersion but of differing magnitudes may be used and
10 some or all of the advantages of dispersion management may be retained.

(ix) Dispersion of either sign need not be provided by lengths of fiber. For instance, fiber Bragg gratings can add either type of dispersion to the laser cavity; so can fiber-
15 integrated diffraction gratings, prisms, photonic bandgap materials, or bulk dispersive material.

(x) For ensuring that the periodic drive is an integral multiple of the fundamental frequency a PZT cylinder is preferred, however, an air gap may be used, as shown in **Figure**
20 **1e**. Or, the frequency of the periodic drive may be varied to match the integral multiple fundamental cavity frequency by the use of a voltage control oscillator or regenerative locking, as in **Figures 2c** and **2d**.

(xi) The modulator may be an optical modulator, such as a
25 Mach-Zehnder modulator, wherein it is modulated with an electrical signal, or it may be of another type, such as a light-by-light modulator wherein the optical signal is modulated by another optical signal.

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5 (xii) A polarization controller **62** may be used, as in
Figures 6a and **6b** to control the phase of the optical signal.

 This above-described invention differ from what is taught in
the Statutory Invention Registration (SIR) by Carruthers et al.,
entitled PICOSECOND-TO-FEMTOSECOND ERBUIM FIBER LASER, Serial No.
10 08/825,942, filed on April 1, 1997; in that the dispersion map
has close to optimum strength so that the average dispersion is
much closer to zero than that taught in the SIR. The device
taught in the SIR does not have a dispersion map *per se*; the
purpose of the dispersion-compensating fiber in the SIR is merely
15 to reduce the average dispersion of the laser to a manageable
level.

 Although the invention has been described in relation to an
exemplary embodiment thereof, it will be understood by those
skilled in the art that still other variations and modifications
20 can be affected in the preferred embodiment without detracting
from the scope and spirit of the invention as described in the
claims, as can be seen in the various figures..

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ABSTRACT

The ultrashort fiber laser with a dispersion-managed cavity.

10 The laser is an actively mode-locked sigma laser, typically
locked at a repetition rate of 10 GHz, driven by an external
frequency source and actively length stabilized, and nearly
10,000 pulses circulate within the laser cavity. A Mach-Zehnder
modulator is placed in a loop of polarization-maintaining (PM)

15 fiber. The polarization state of light injected into the non-PM
branch evolves in a random manner but is transformed into an
orthogonal state by a Faraday mirror; linearly polarized light
injected into the branch by a polarizing beamsplitter returns to
the beamsplitter also linearly polarized but rotated by 90°. The

20 cavity of the laser is composed of several fibers. The average
dispersion D_{av} is anomalous and is approximately equal to
0.1 ps/(nm·km). The measured noise in the output of the laser is
very low; the rms amplitude noise is less than 0.1 percent over a
frequency range of 10 Hz - 1 MHz, and the rms timing filter is

25 less than 10 femtoseconds over a frequency range of 100 Hz - 1
MHz.

10

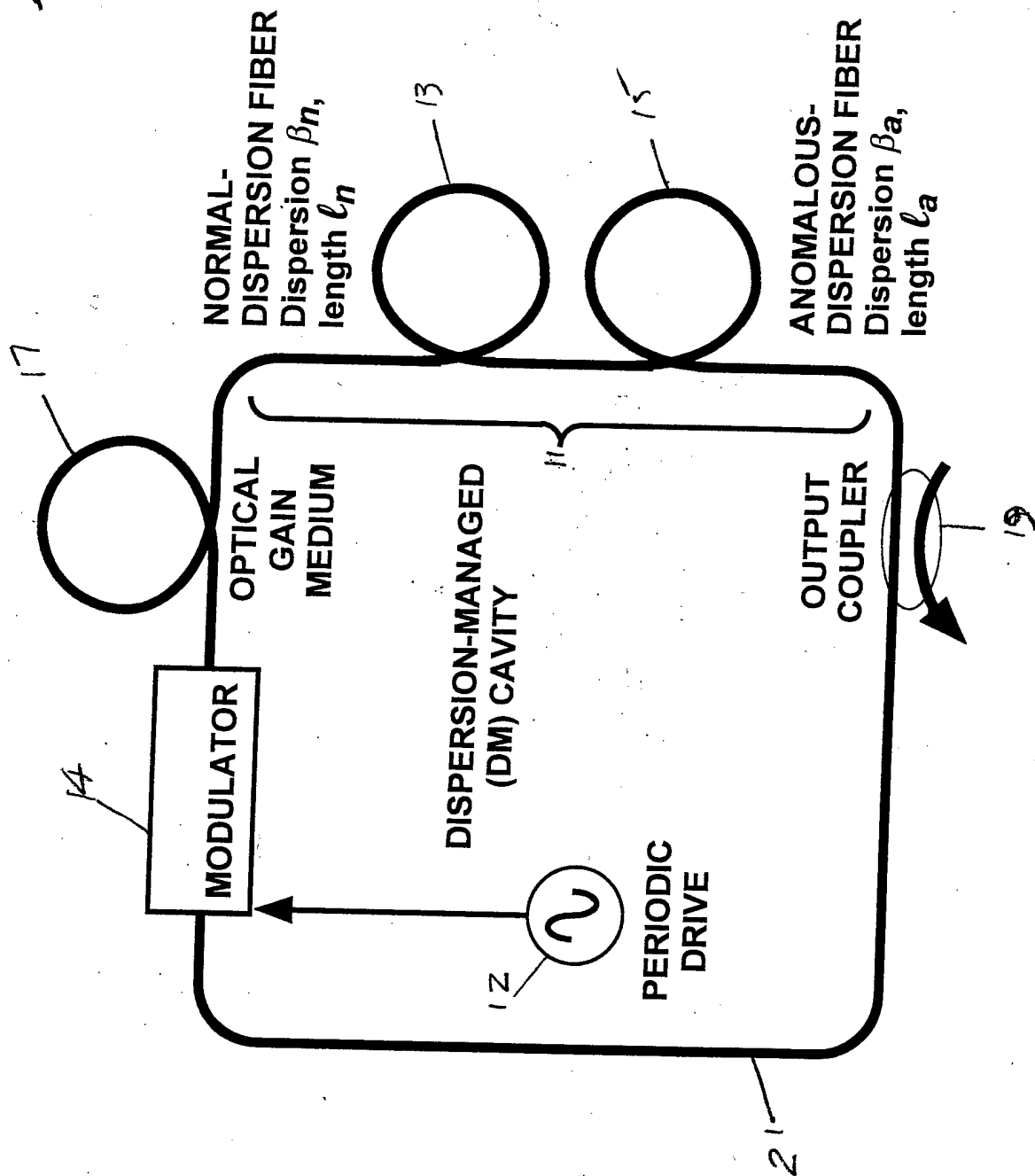


Figure 1a

20

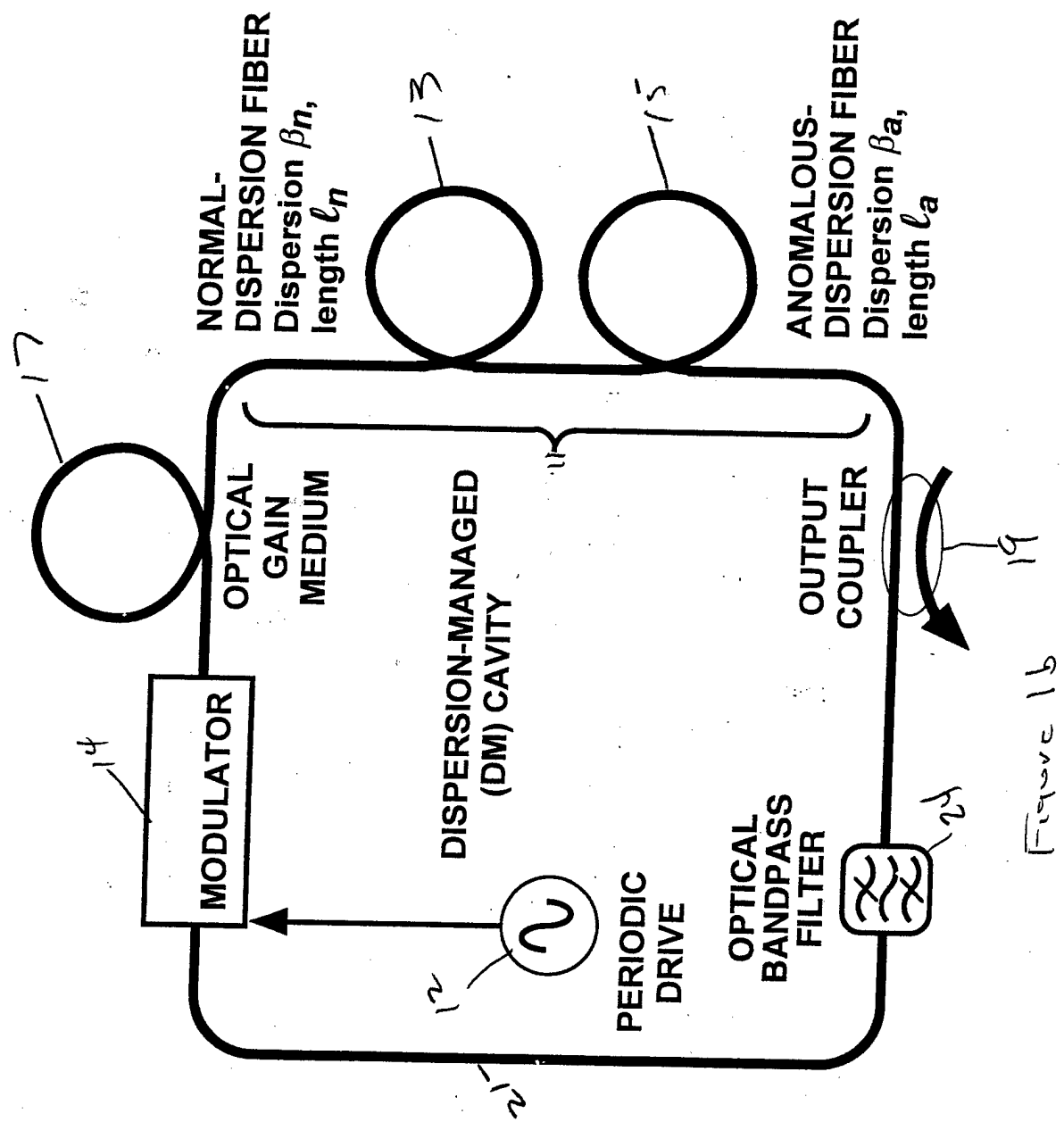


Figure 1b

30

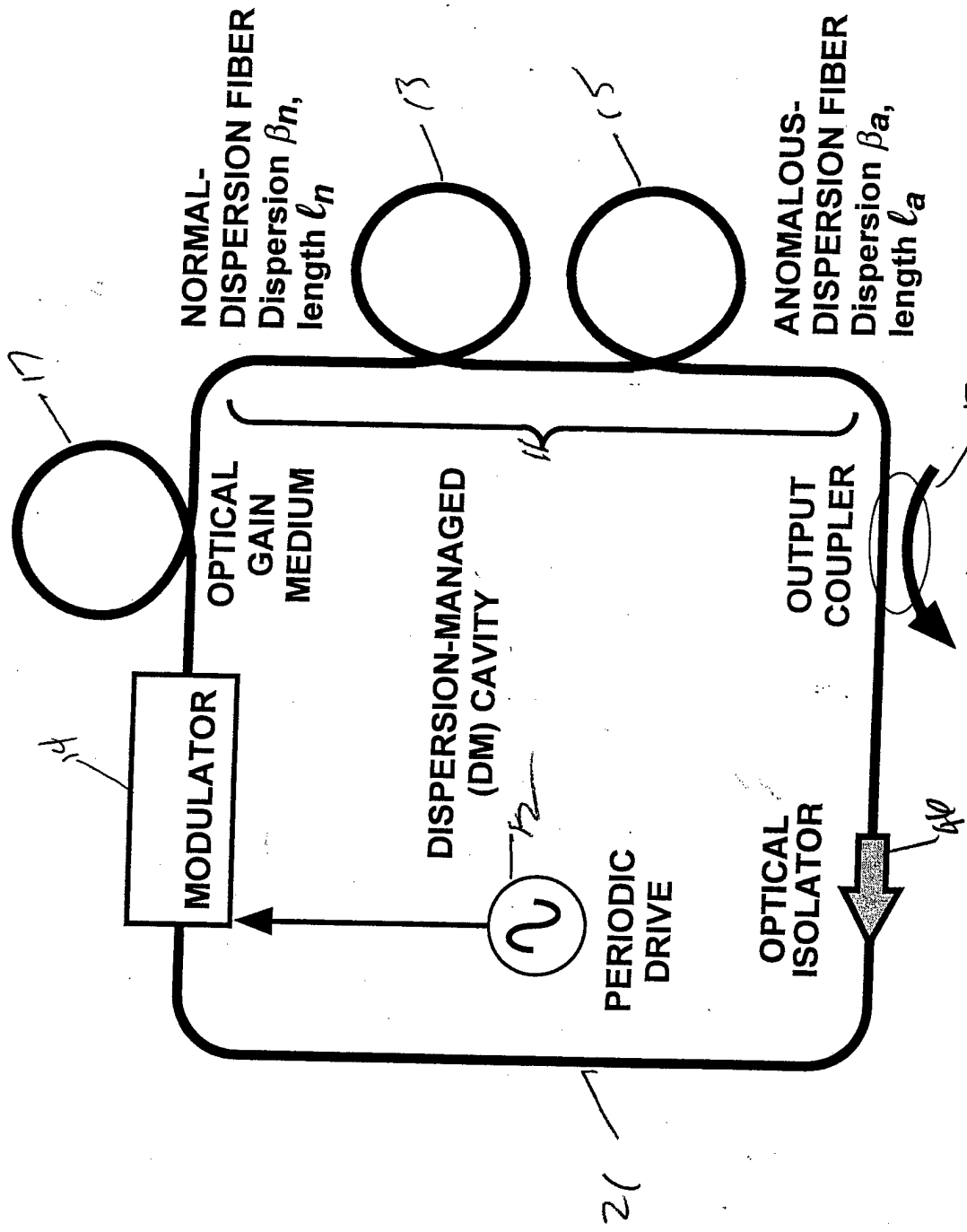


Figure 1c

40

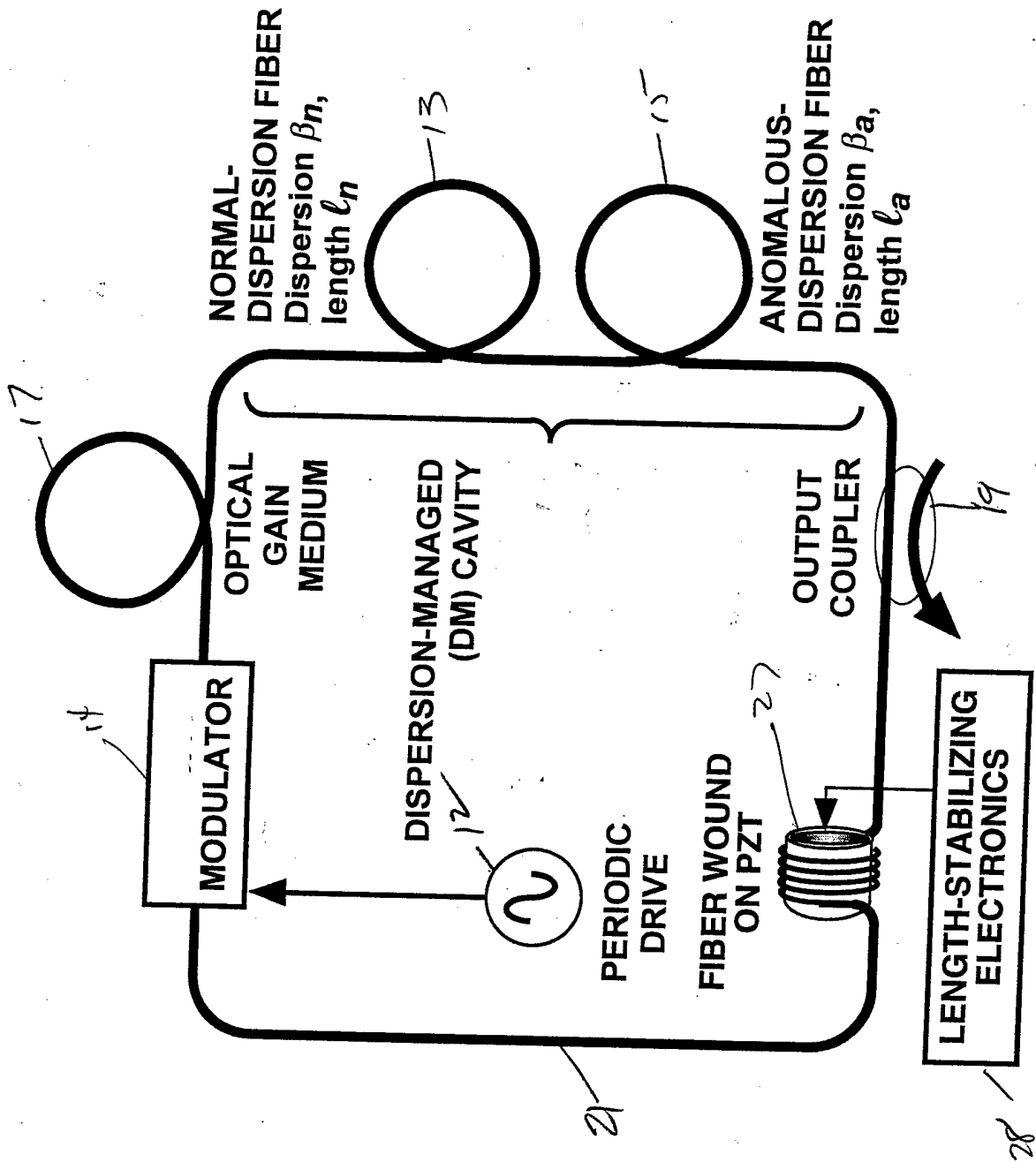


Figure 1d

60

17

14

NORMAL-
DISPERSION FIBER
Dispersion β_n ,
length ℓ_n

13

15

ANOMALOUS-
DISPERSION FIBER
Dispersion β_a ,
length ℓ_a

MODULATOR

OPTICAL
GAIN
MEDIUM

DISPERSION-MANAGED
(DM) CAVITY

PERIODIC
DRIVE

21

ADJUSTABLE
AIR GAP

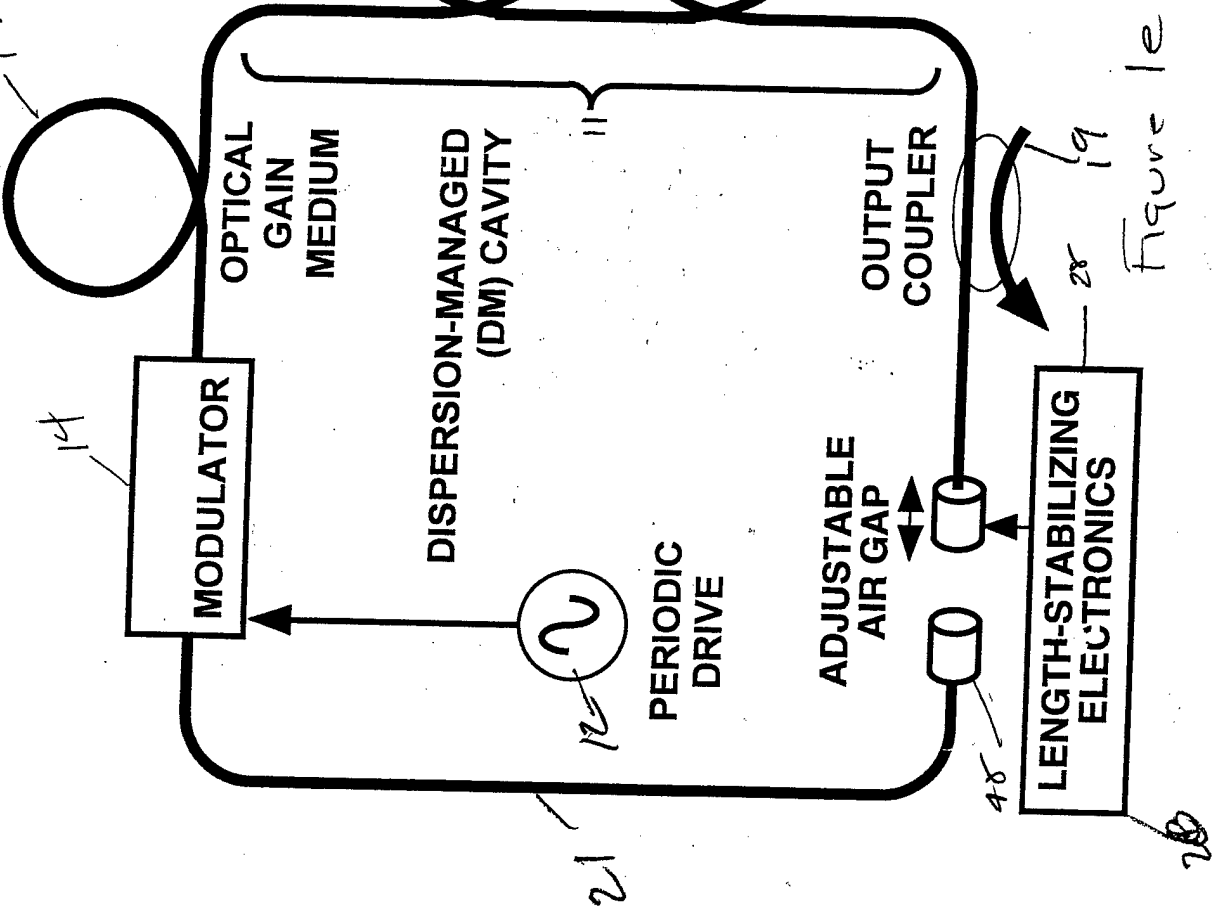
OUTPUT
COUPLER

LENGTH-STABILIZING
ELECTRONICS

19

Figure 1e

20



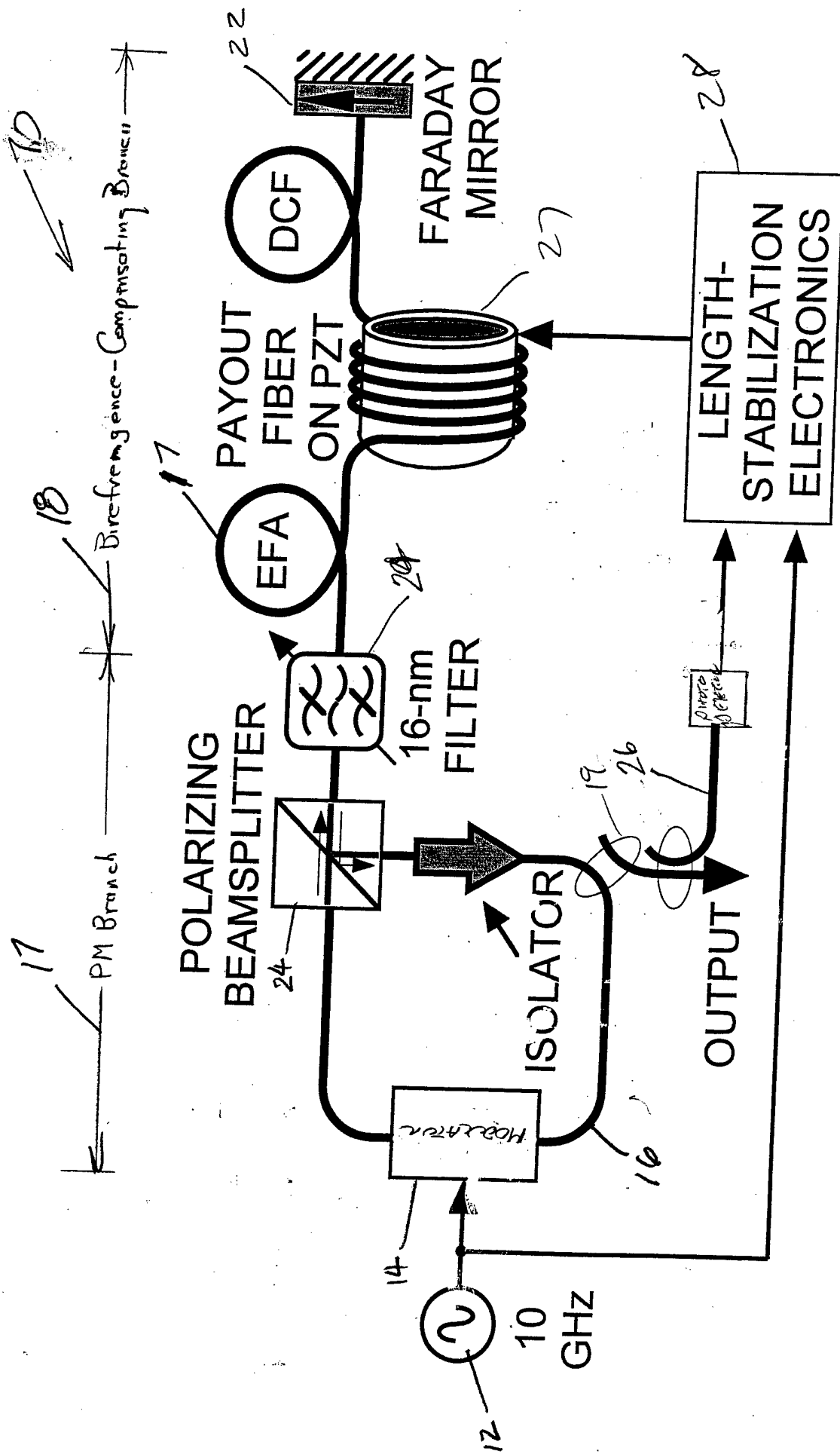


Figure 2a

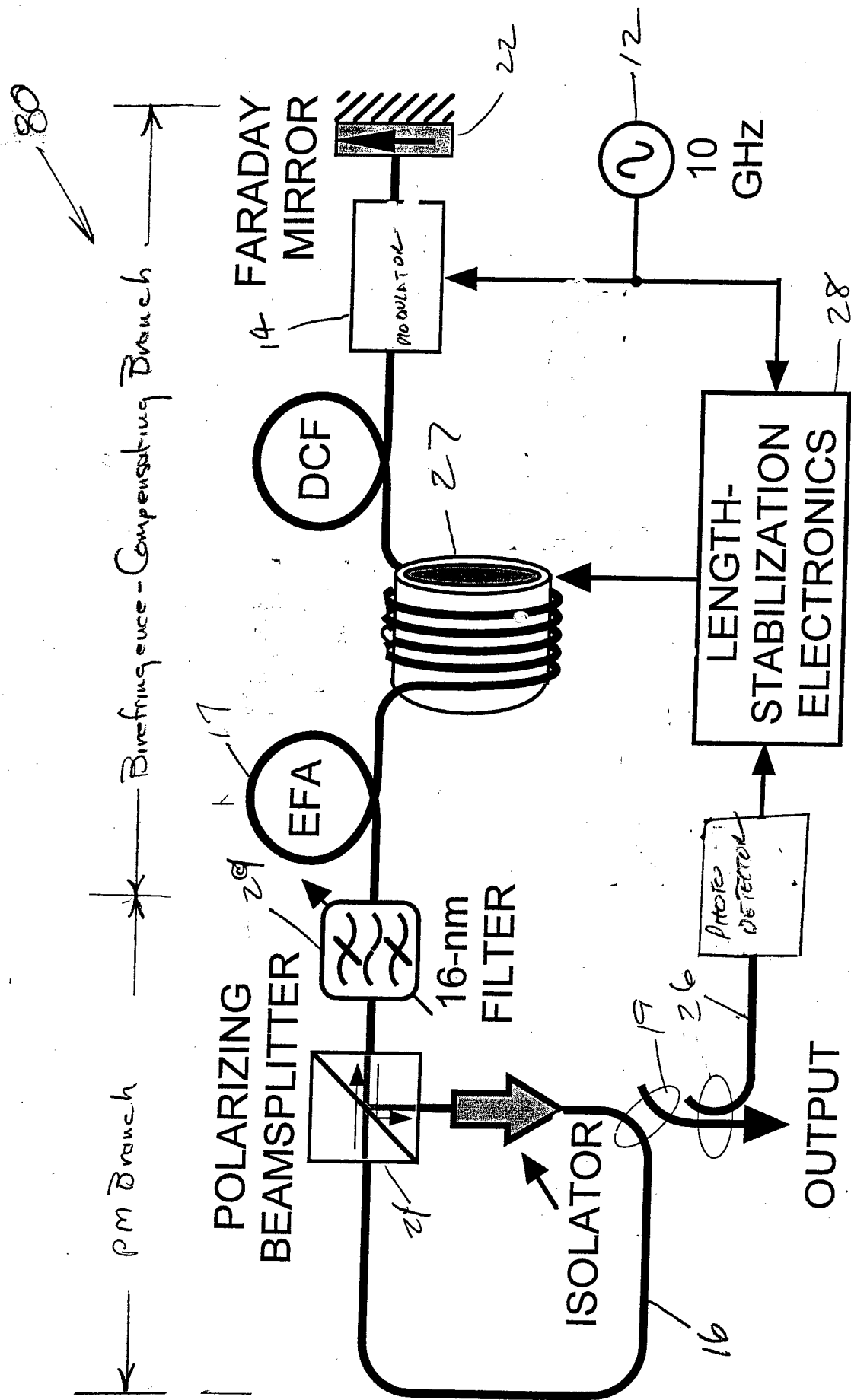


Figure 2b.

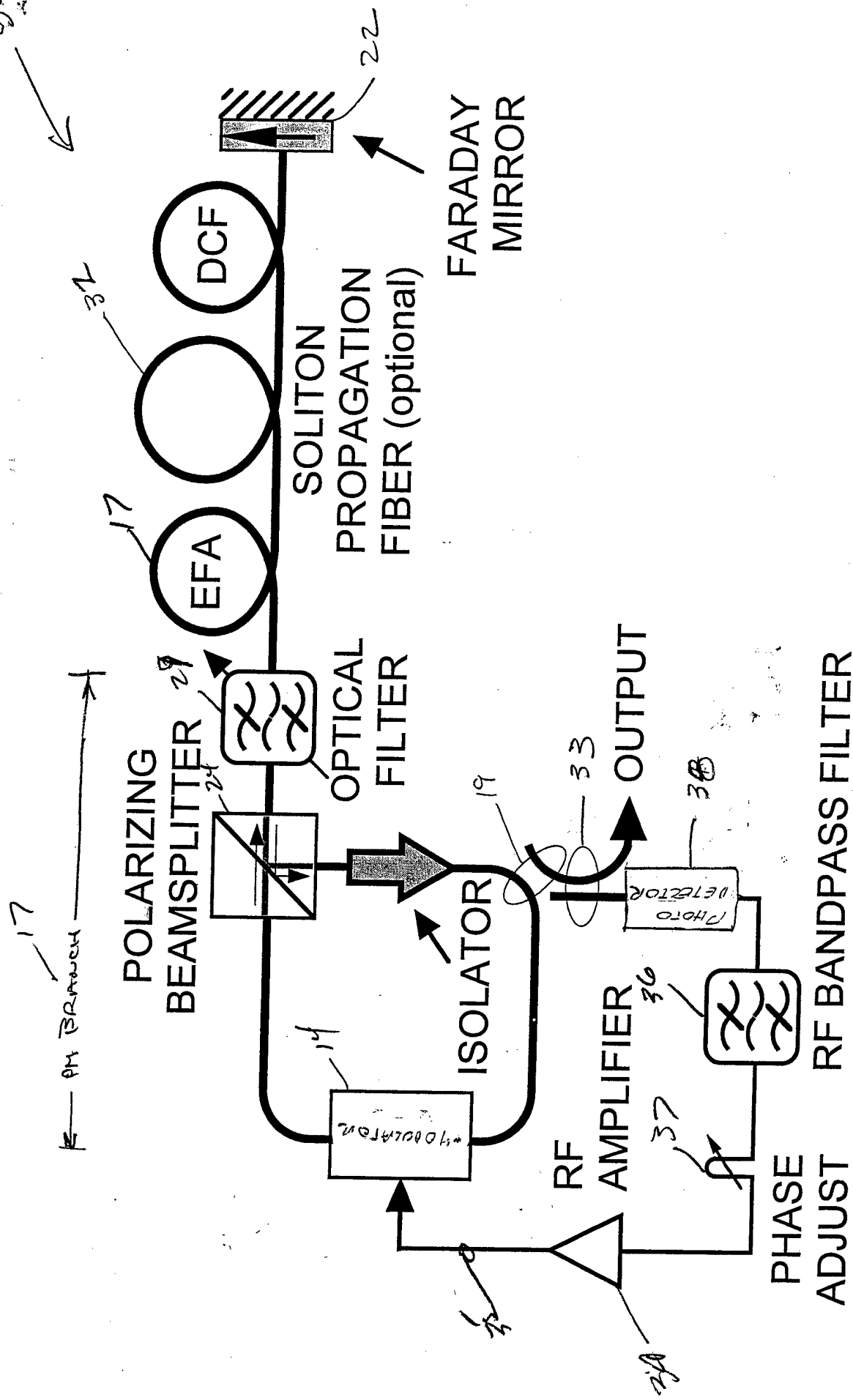
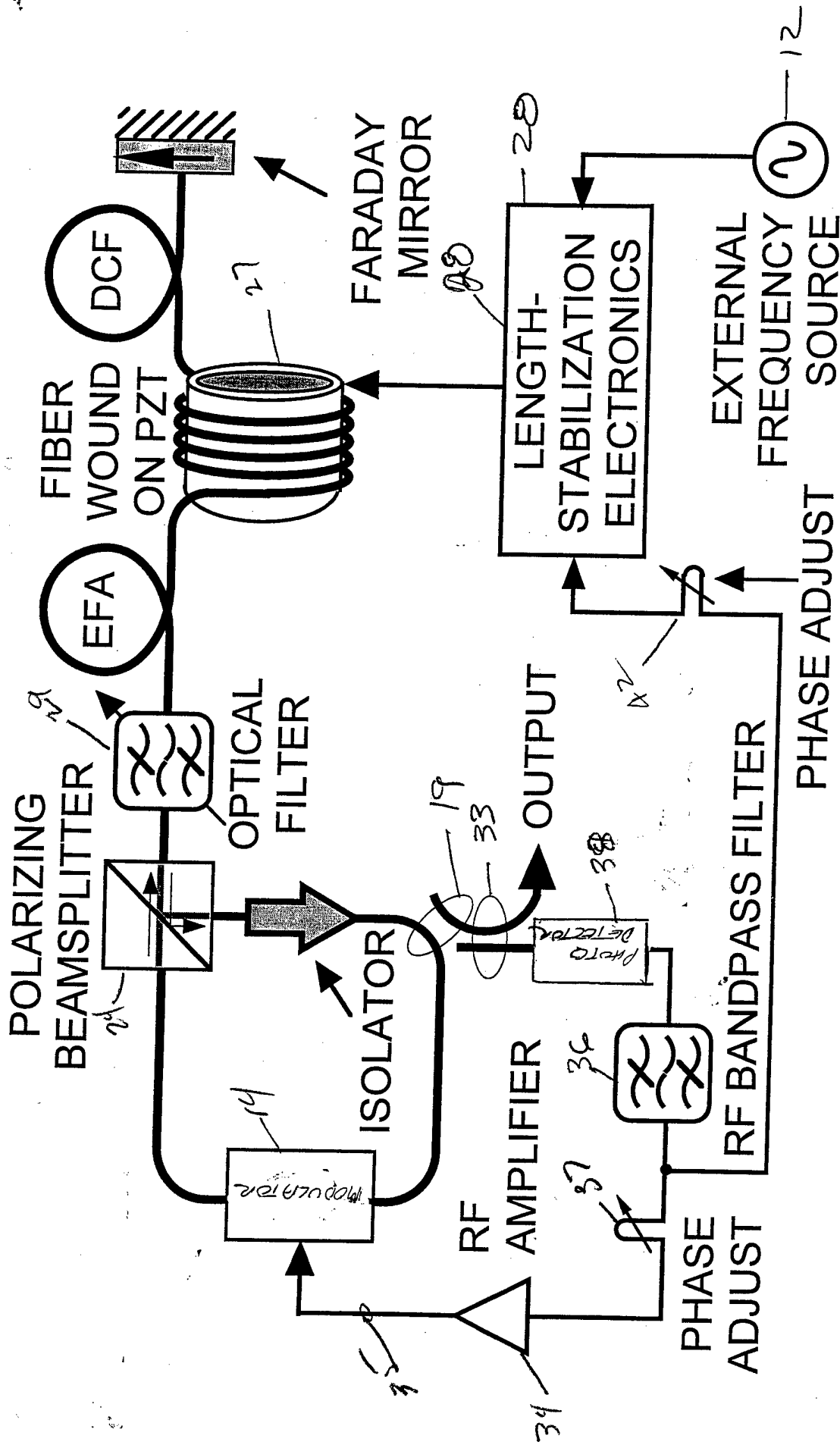


Figure 2c



Regeneratively mode-locked laser with length stabilization.

Figure 2d

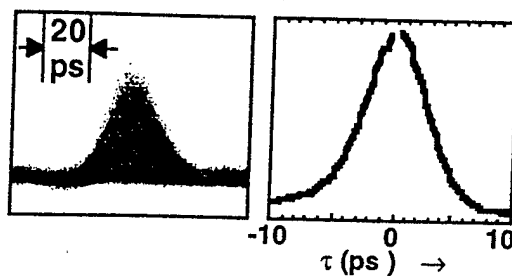


Fig. 3a

I. $P_{out}/P_{max} = 0.047$

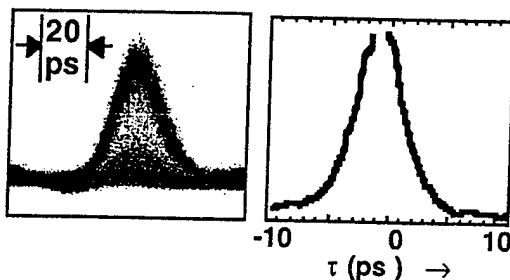


Fig. 3b

IIa. $P_{out}/P_{max} = 0.064$

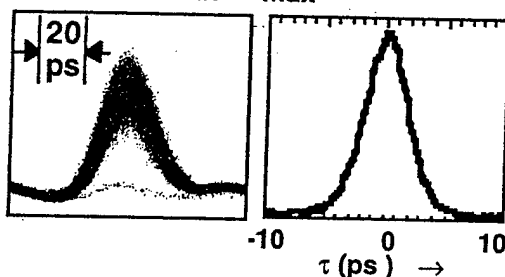


Fig. 3c

IIb. $P_{out}/P_{max} = 0.27$

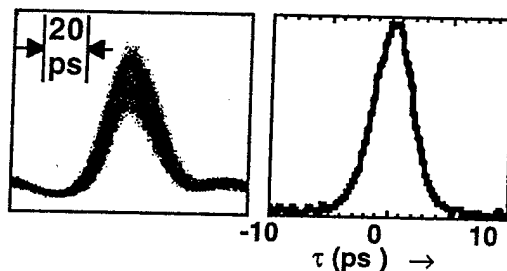


Fig. 3d

IIIa. $P_{out}/P_{max} = 0.34$

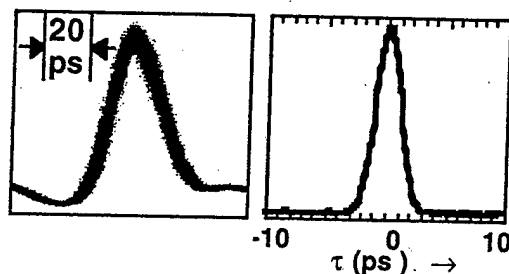


Fig. 3e

IIIb. $P_{out}/P_{max} = 1.00$

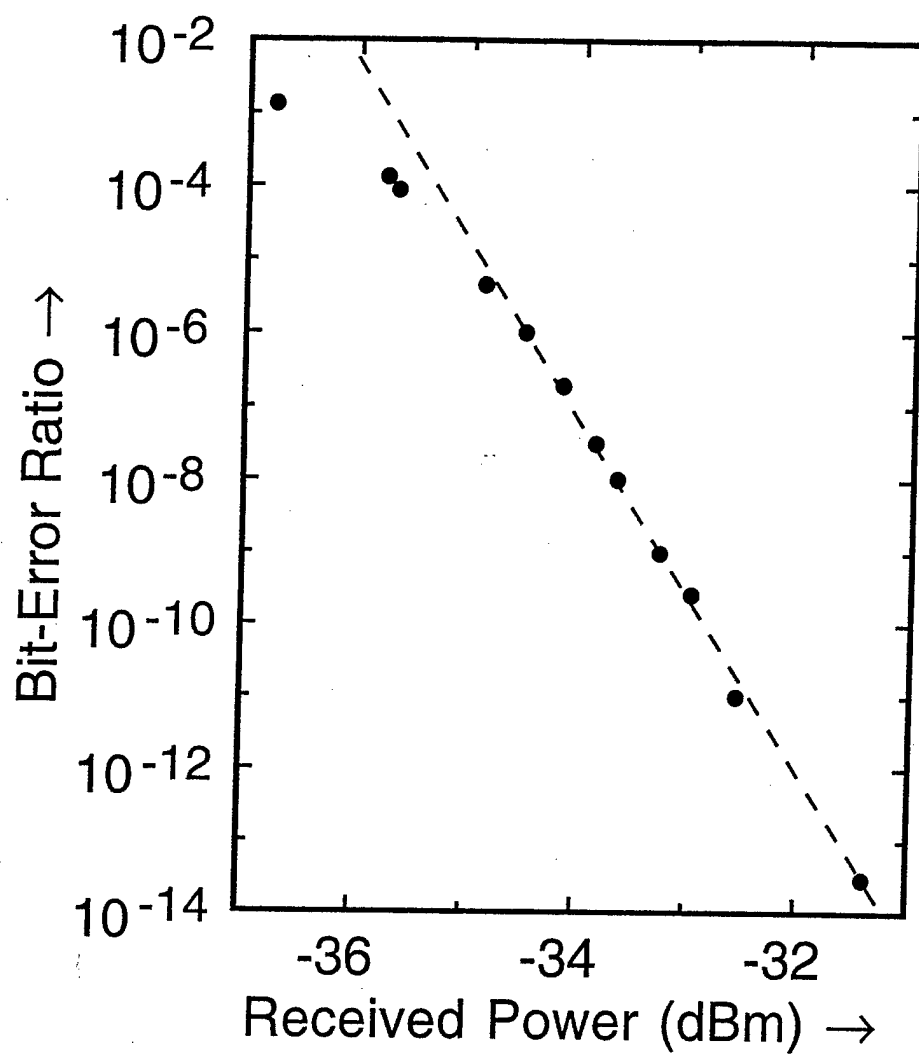


FIGURE 4

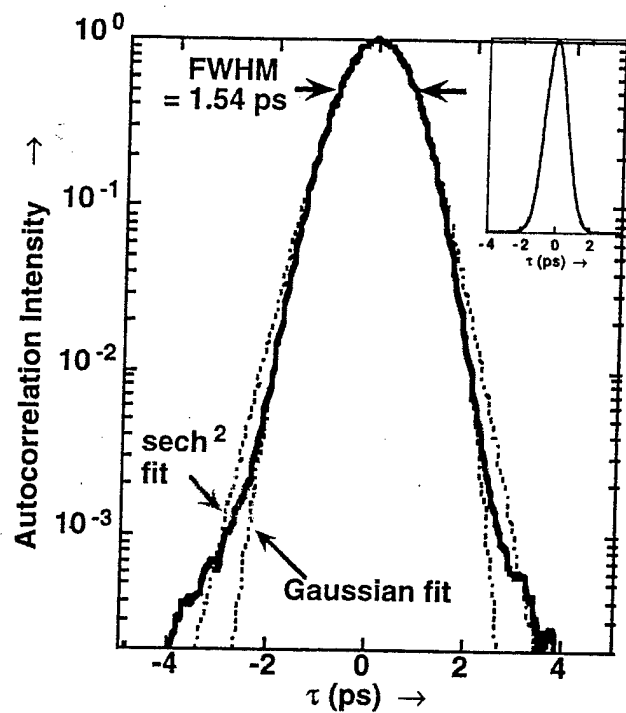


Figure 5a

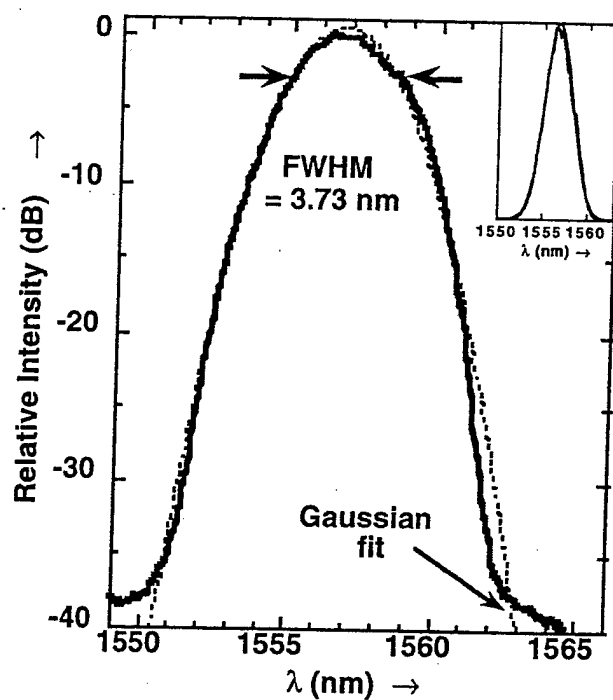
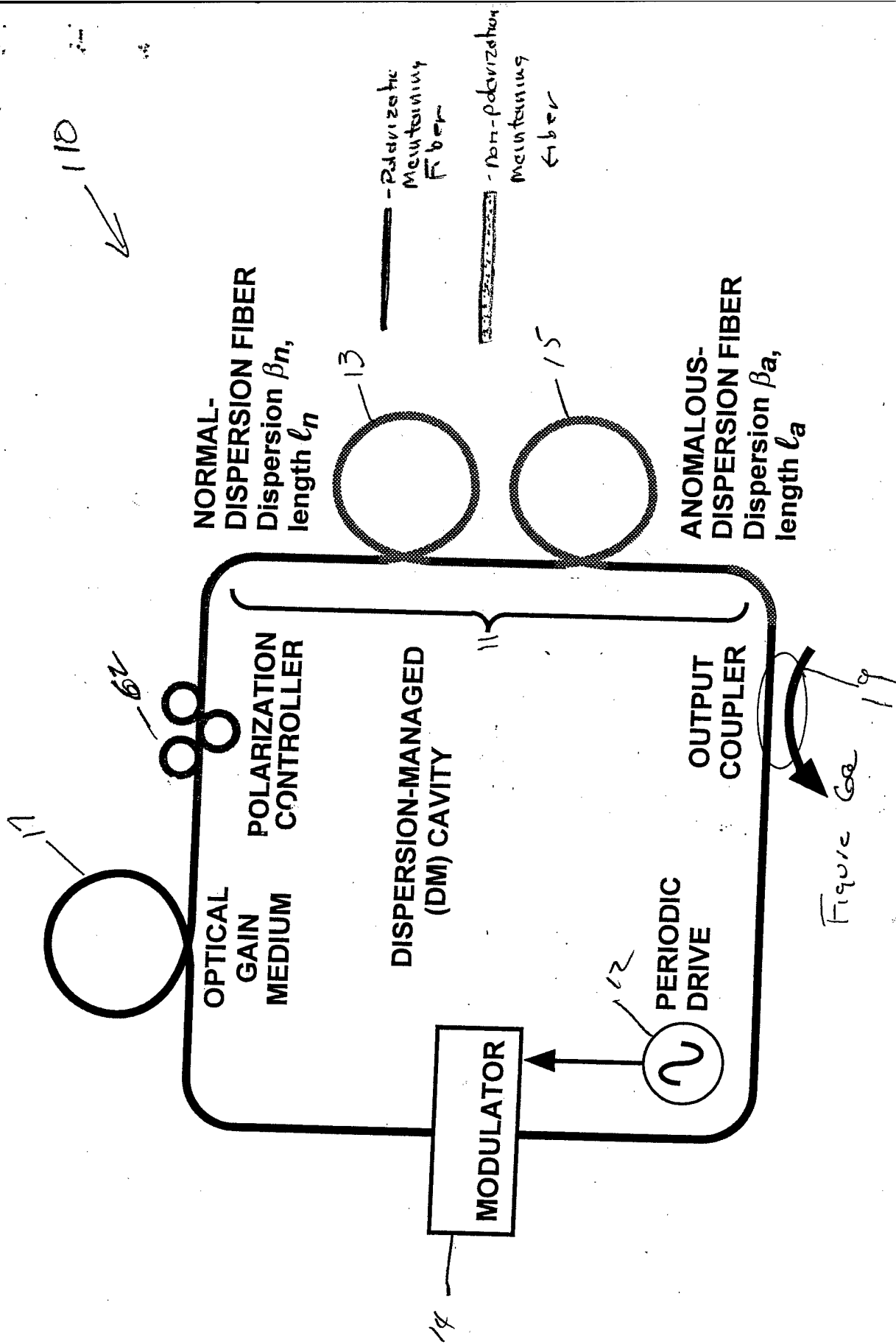


Figure 5b



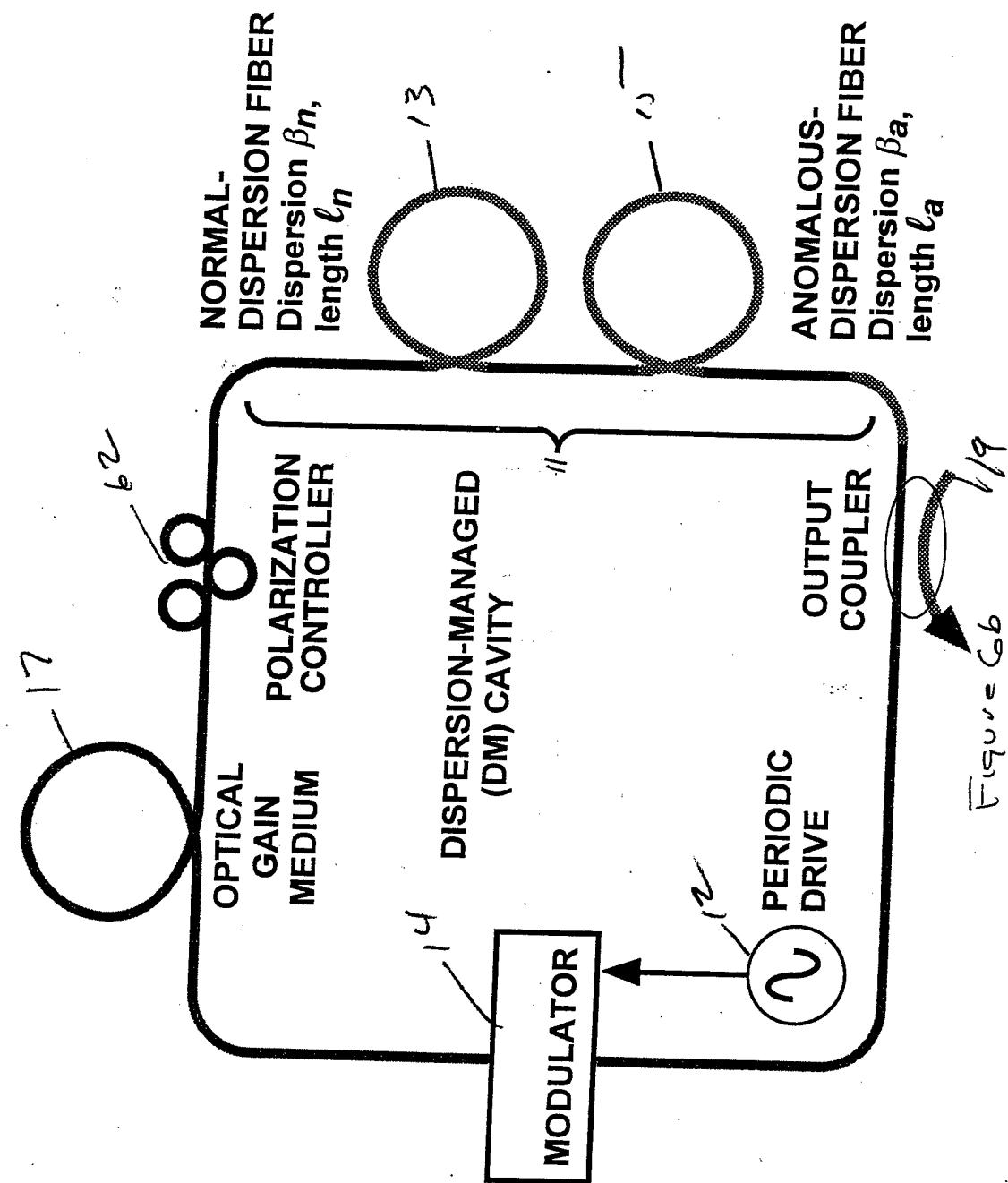
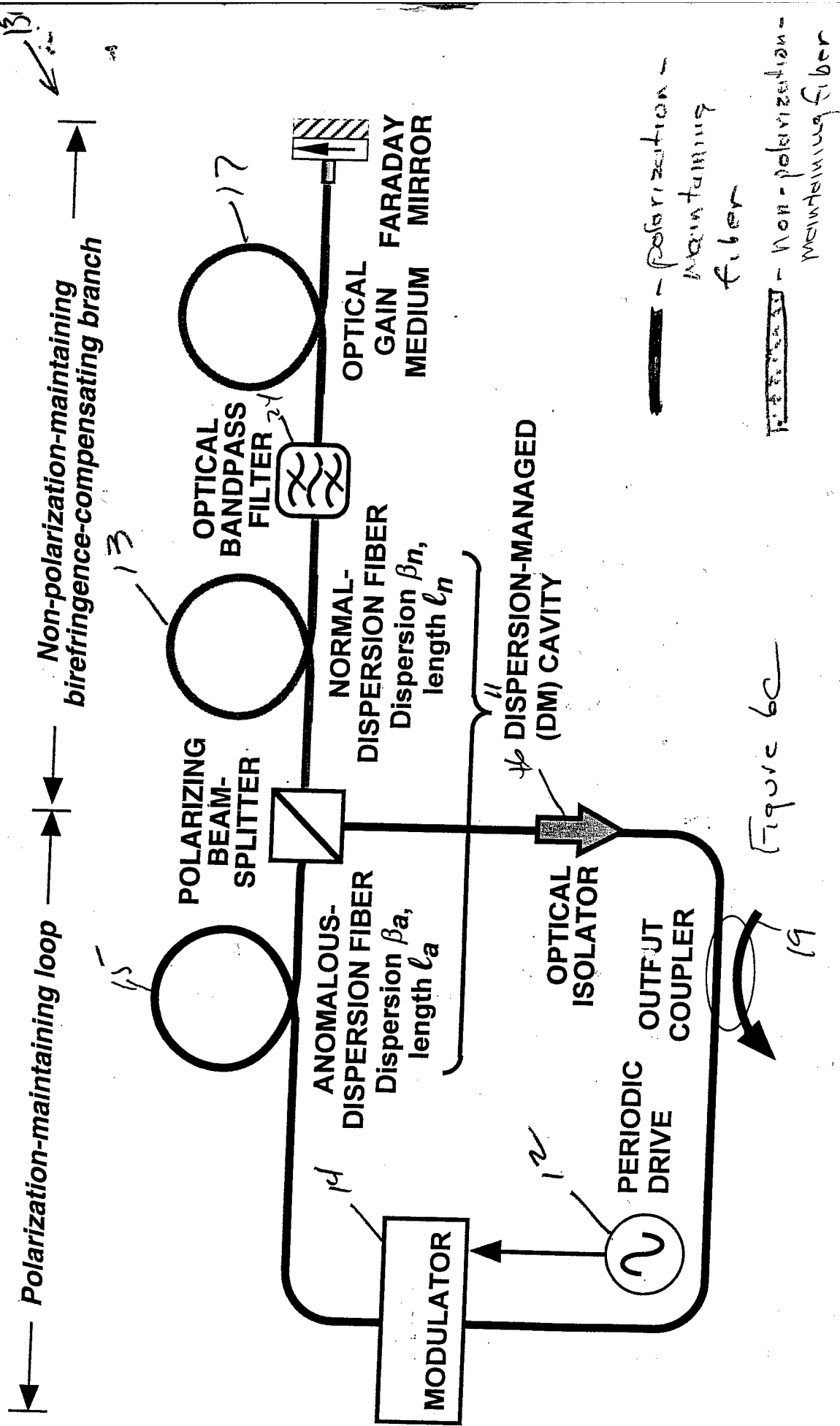


Figure 6b



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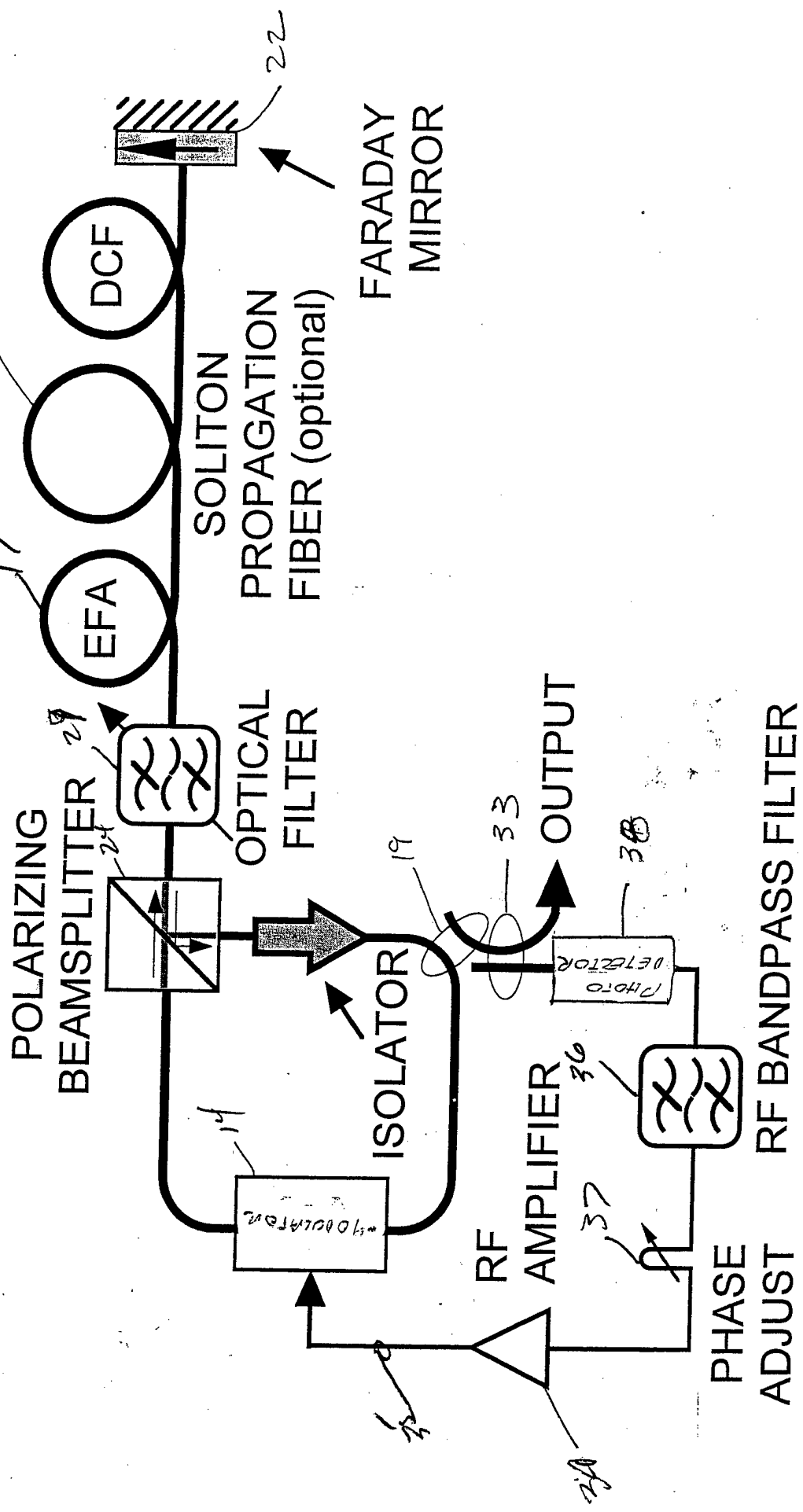
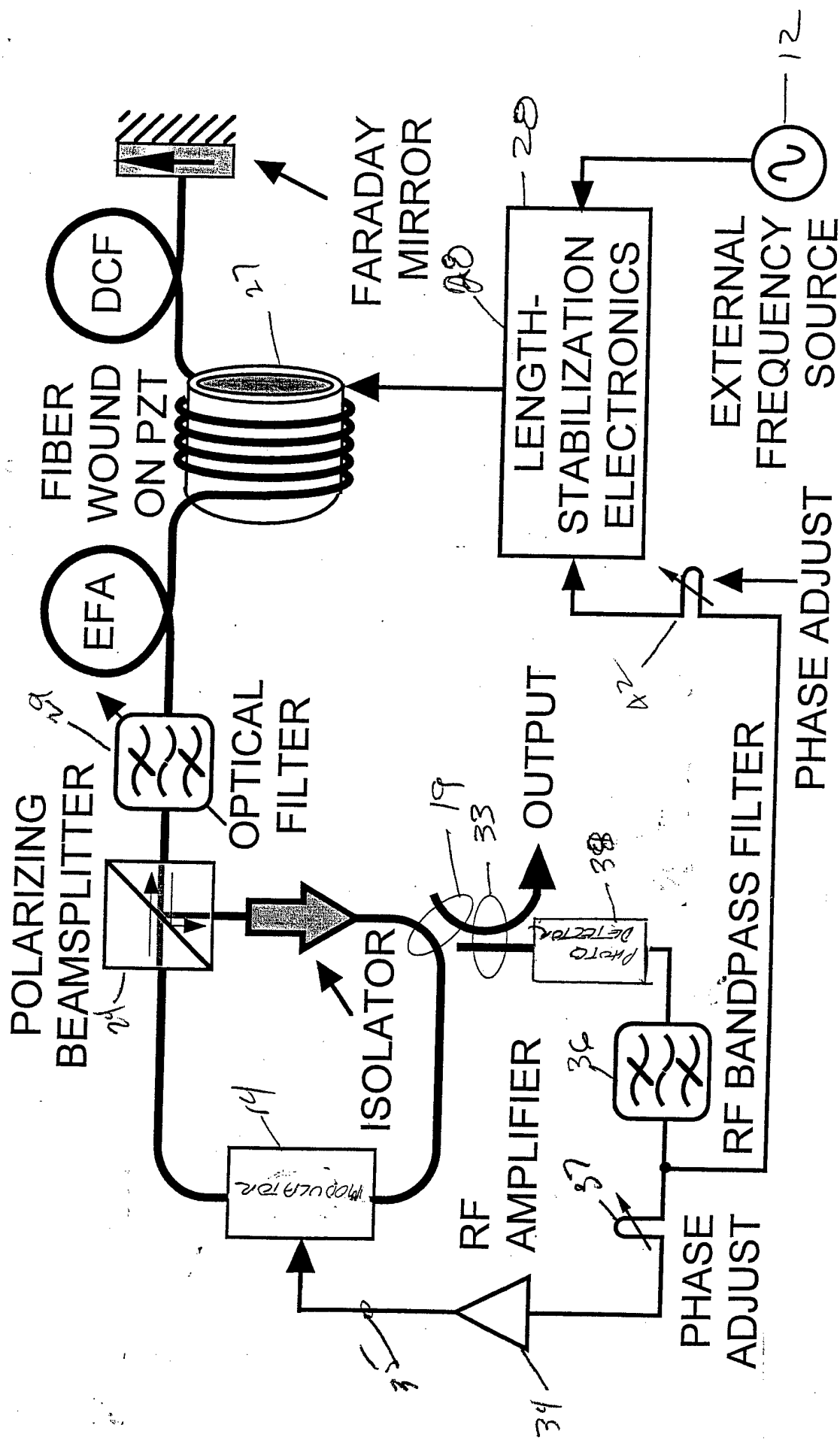


Figure 2c



Regeneratively mode-locked laser with length stabilization.

Figure 2d

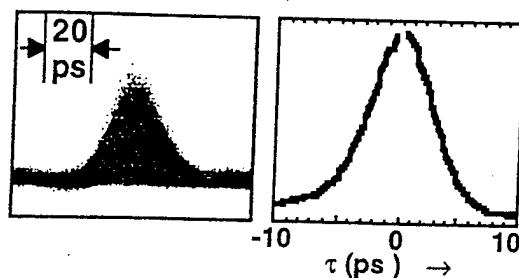


Fig. 3a

I. $P_{out}/P_{max} = 0.047$

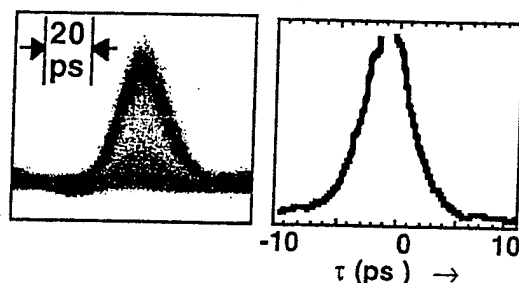


Fig. 3b

IIa. $P_{out}/P_{max} = 0.064$

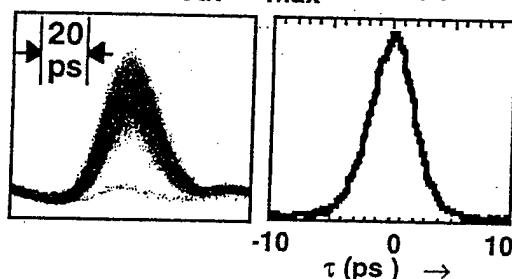


Fig. 3c

IIb. $P_{out}/P_{max} = 0.27$

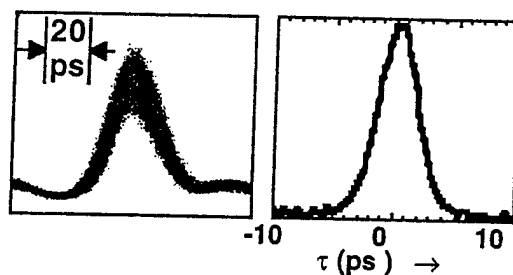


Fig. 3d

IIIa. $P_{out}/P_{max} = 0.34$

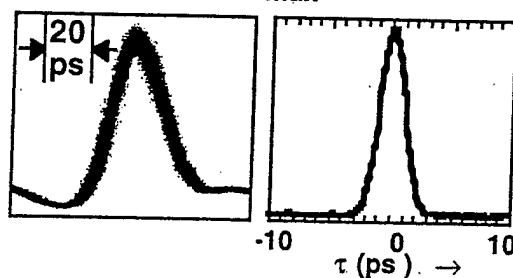


Fig. 3e

IIIb. $P_{out}/P_{max} = 1.00$

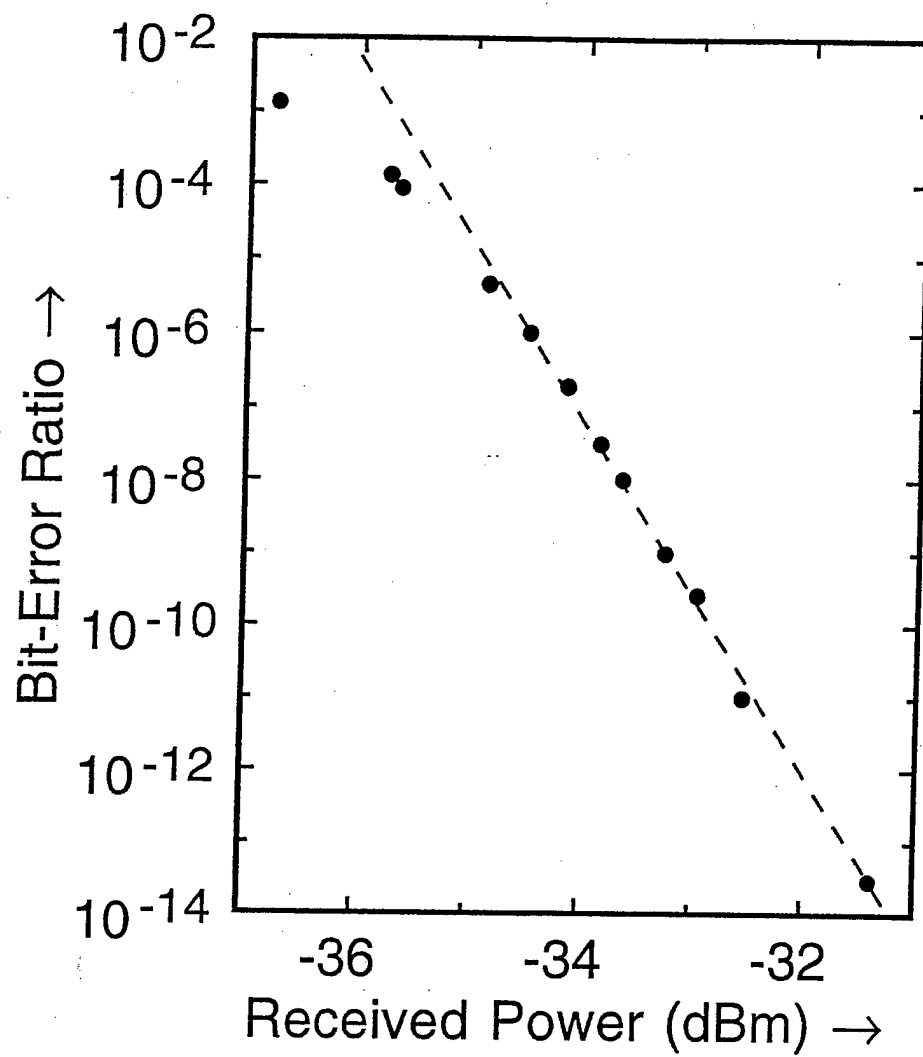


FIGURE 4

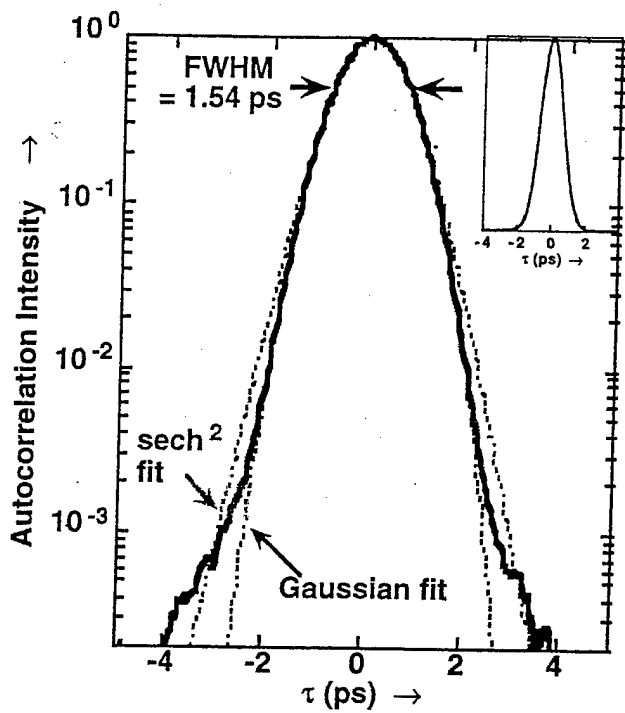


Figure 5a

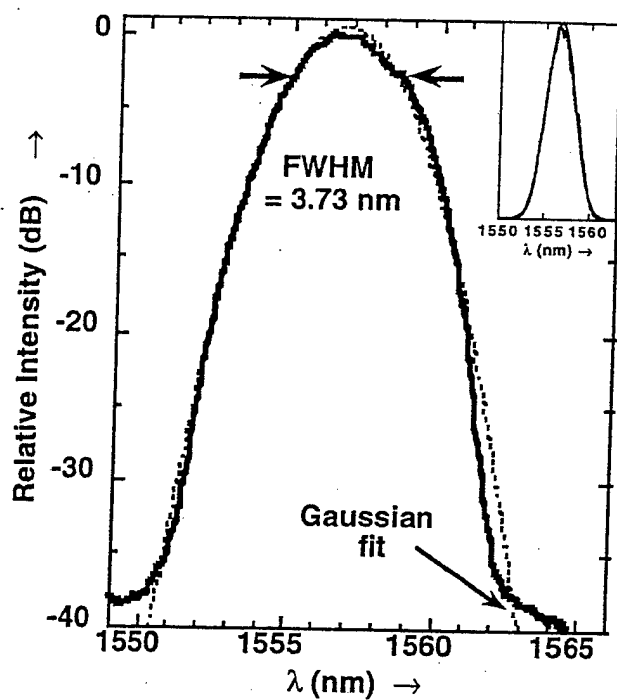


Figure 5b

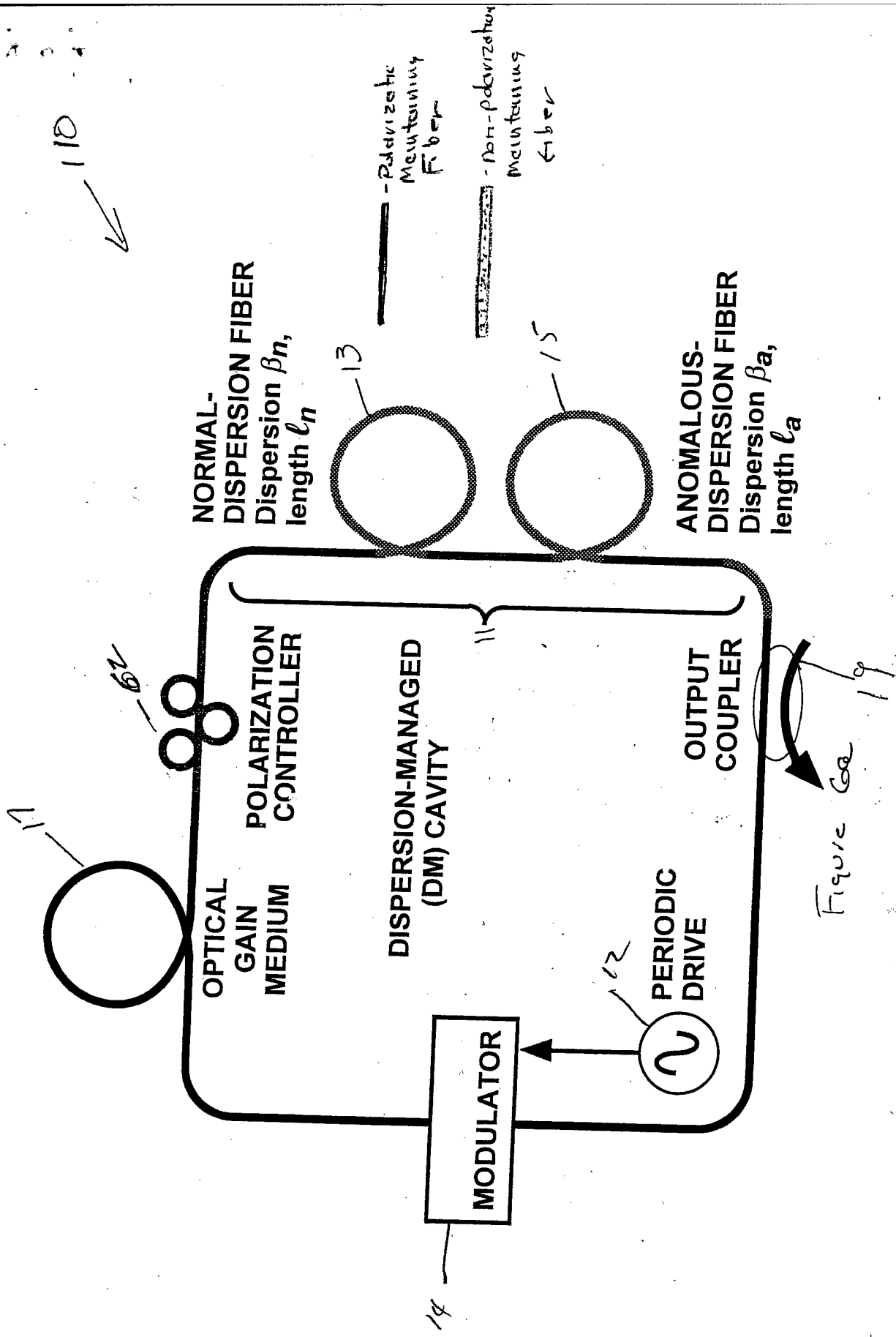


Figure 6a

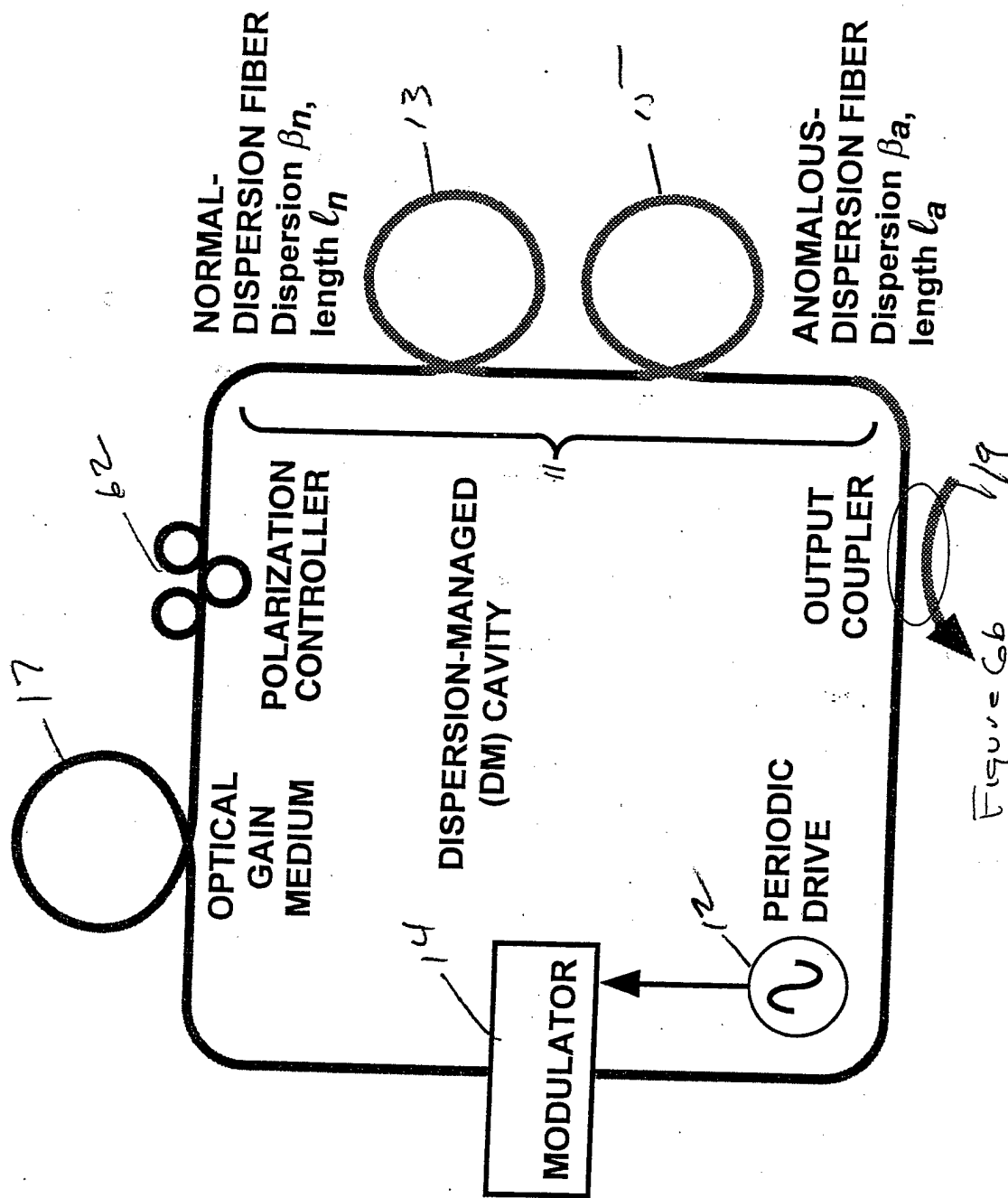


Figure 6b

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