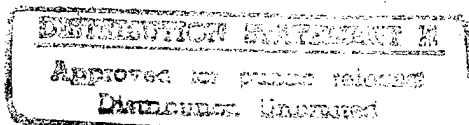


Serial Number 865,150
Filing Date 29 May 1997
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19971119 011

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2
3 FIELD CALIBRATION OF THE NORMAL PRESSURE TRANSFER FUNCTION
4 OF A COMPLIANT FLUID-FILLED CYLINDER

5
6 STATEMENT OF GOVERNMENT INTEREST

7 The invention described herein may be manufactured and used
8 by or for the Government of the United States of America for
9 Governmental purposes without the payment of any royalties
10 thereon or therefor.

11
12 BACKGROUND OF THE INVENTION

13 (1) Field of the Invention

14 The present invention relates generally to determining the
15 transfer function of a fluid-filled compliant cylinder, and more
16 particularly to a field method by which the calibration of the
17 transfer function of a fluid-filled compliant cylinder is
18 measured as a function of temporal frequency and spatial
19 frequency (or wavenumber).

20 (2) Description of the Prior Art

21 Towed acoustic arrays are used in a variety of commercial
22 and military applications. For example, towed arrays are used in
23 seismic survey applications as well as in antisubmarine warfare
24 applications. In general, a towed array is used to measure a
25 pressure field propagating in a fluid environment.

1 A towed array typically consists of a compliant (e.g.,
2 rubber or plastic) fluid-filled hose or cylinder containing an
3 array of hydrophones or other sensors for making measurements of
4 the pressure field incident upon its outer surface. The pressure
5 field of interest will be referred to hereinafter as the signal.
6 When there is relative movement between the fluid environment and
7 the cylinder (e.g., the cylinder is towed or the cylinder is
8 stationary and the fluid environment is moving), a turbulent
9 pressure field develops which also impinges on the outer surface
10 of the cylinder. This pressure field will be referred to
11 hereinafter as the noise pressure field.

12 The major elements of the noise pressure field are separated
13 in spatial frequency or wavenumber from the signal and can be
14 filtered by a spatial filter. The cylinder acts as the first and
15 primary spatial filter to the noise pressure field arising from
16 the turbulent boundary layer. As such, it is desirable to be
17 able to calibrate or measure the attenuation provided by the
18 cylinder transfer function $T_H(k, \omega)$ as a function of the spatial
19 frequency or wavenumber k and the frequency ω . The cylinder
20 transfer function $T_H(k, \omega)$ is defined as the ratio of inner
21 pressure to outer pressure according to equation (1)

$$T_H(k, \omega) = P_i(k, \omega) / P_o(k, \omega) \quad (1)$$

22 where $P_i(k, \omega)$ is the pressure field measured in the fluid in the
23 cylinder at a radius r and $P_o(k, \omega)$ is the pressure field
24 impressed on the outer surface of the cylinder. At present, no

1 impressed on the outer surface of the cylinder. At present, no
2 methods exist to field calibrate the cylinder transfer function
3 $T_H(k, \omega)$ in which pressure fields $P_i(k, \omega)$ and $P_o(k, \omega)$ are measured.

4 5 SUMMARY OF THE INVENTION

6 Accordingly, it is an object of the present invention to
7 provide a measurement method of calibrating the transfer function
8 of a fluid-filled compliant cylinder.

9 Another object of the present invention is to provide a
10 measurement method of calibrating the transfer function to normal
11 pressure for a fluid-filled compliant cylinder as a function of
12 wavenumber and frequency.

13 Other objects and advantages of the present invention will
14 become more obvious hereinafter in the specification and
15 drawings.

16 In accordance with the present invention, a method is
17 presented to calibrate the transfer function for a fluid-filled
18 compliant cylinder as a function of wavenumber and frequency. A
19 first compliant cylinder is filled with air and has a first
20 linear array of force sensors (e.g., pressure or strain sensors)
21 coupled to the cylinder's exterior surface. The first compliant
22 cylinder is made from an elastomeric material that has enough
23 stiffness to prevent cylinder collapse under hydrostatic
24 operational pressures. The force sensors are spaced along the
25 length of the cylinder. The first compliant cylinder with its
26 first linear array coupled thereto are immersed in a fluid

1 environment. A first turbulent flow field is generated in the
2 fluid environment such that it is experienced by the first linear
3 array. A first output generated by the first linear array in the
4 first turbulent flow field is measured and is indicative of
5 pressure incident upon the first linear array. A second
6 compliant cylinder having an identical outside diameter
7 measurement as the first compliant cylinder houses a second
8 linear array of force sensors spaced along a central longitudinal
9 axis thereof. The second compliant cylinder is made from a more
10 flexible elastomeric material than that used for the first
11 compliant cylinder. The second compliant cylinder is further
12 filled with a fluid that surrounds the second linear array. The
13 second compliant cylinder with its second linear array contained
14 therein is immersed in the fluid environment. A second turbulent
15 flow field (substantially equivalent to the first turbulent flow
16 field) is then generated in the fluid environment about the
17 second complaint cylinder. A second output generated by the
18 second linear array is then measured and is indicative of
19 pressure incident upon the second linear array. A ratio of the
20 first output to the second output is indicative of the transfer
21 function of the fluid-filled compliant cylinder. Each output can
22 be further adjusted by a calibrated sensitivity of the
23 corresponding first and second linear arrays. Elastic scattered
24 pressure field effects are removed from the pressure measurements
25 via dynamic elasticity models of each cylinder. The wavenumber-
26 frequency dependence of the first compliant cylinder's

1 sensitivity to pressure is also removed by application of the
2 dynamic elasticity models.

3 4 BRIEF DESCRIPTION OF THE DRAWINGS

5 Other objects, features and advantages of the present
6 invention will become apparent upon reference to the following
7 description of the preferred embodiments and to the drawings,
8 wherein corresponding reference characters indicate corresponding
9 parts throughout the several views of the drawings and wherein:

10 FIG. 1 is a schematic of a pressure-field sensing array
11 being towed through the water by a ship;

12 FIG. 2 is a graph of wavenumber k versus frequency ω for the
13 fluid in the array's cylinder indicating the propagating and non-
14 propagating regions of the wavenumber-frequency plane;

15 FIG. 3 is a side view of a composite hydrophone array
16 assembly used in the method of the present invention;

17 FIG. 4 is a schematic of an acoustic calibration set-up used
18 to measure the acoustic sensitivity of the composite hydrophone
19 array assembly; and

20 FIG. 5 is a schematic of a fluid-filled compliant cylinder
21 housing an array of hydrophones therein for measuring the inner
22 pressure field generated in the cylinder due to a pressure field
23 impinging on the outside of the cylinder.

1 DESCRIPTION OF THE PREFERRED EMBODIMENT(S)

2 Referring now to the drawings, and more particularly to FIG.
3 1, a pressure-field sensing array is shown and is referenced
4 generally by the numeral 10. A sealed elastic or compliant hose
5 or cylinder 12 is filled with a fluid 14. Sealing of cylinder 12
6 at either end thereof can be accomplished with end caps or
7 bulkheads 16 and 18 as is known in the art. The length of
8 cylinder 12 is not limited. Typically, cylinder 12 is made from
9 a fairly flexible elastomer such as a rubber or urethane
10 material, e.g., ESTANE 58881 or ESTANE 58886 available
11 commercially from BF Goodrich. Other suitable materials include
12 melt-process rubbers such as ALCRYN 1160, 1180 or 3155
13 commercially available from DuPont.

14 Maintained within cylinder 12 are a plurality of hydrophones
15 20 spaced apart from one another along the length of cylinder 12.
16 Electronics (not shown) associated with each hydrophone 20 can be
17 included within cylinder 12 or can be maintained on a host
18 platform, e.g., on a ship 30, to which array 10 is tethered.
19 Typically, hydrophones 20 are coupled to one another via
20 communication lines 22, and are further coupled to ship 30 over a
21 tether/communication line 24. In a typical scenario, array 10 is
22 immersed in a fluid environment 50, e.g, seawater, and is towed
23 therethrough by ship 30. The movement of fluid environment 50
24 over cylinder 12 generates noise pressure fields over a broad
25 frequency spectrum. The method of the present invention
26 calibrates the transfer function of the system presented by

1 cylinder 12/fluid 14 as a function of temporal frequency and
2 spatial frequency (or wavenumber).

3 The mathematical space for discussing the present invention
4 is known as the wavenumber-frequency space or plane defined by
5 the relationship $k = 2\pi/\lambda$, where k is the wavenumber in
6 radians/meter and λ is the spatial wavelength of vibration of
7 cylinder 12. Within the wavenumber-frequency plane, the pressure
8 field in either fluid 14 or outer fluid environment 50 is
9 characterized by two distinct regions, the propagating and non-
10 propagating regions. The propagating region for inner fluid 14
11 is contained between the lines $k = \pm\omega/c_i$ and is hatched as shown
12 at 26 in FIG. 2. In propagating region 26, the radial variation
13 of the pressure field follows the Bessel function of the first
14 kind, and does not undergo decay with respect to radial position
15 within cylinder 12. The remainder of the wavenumber-frequency
16 plane comprises the non-propagating regions 28 where $|k| >$
17 $|\omega/c_i|$. Pressure fields in non-propagating regions 28 impinging
18 on the outer surface of the cylinder undergo an exponential
19 decay. The decay follows a modified Bessel function where decay
20 varies with respect to radial position within cylinder 12.

21 Also shown in FIG. 2 are lines 29A and 29B representing the
22 convective ridge for two different tow speeds v_1 and v_2 ,
23 respectively. The convective ridge is the region of the
24 wavenumber-frequency plane in which the calibration is occurring.
25 This ridge is the region where most of the energy exists in the
26 turbulent boundary layer. The convective ridge is influenced by

1 the relative motion between the surface of the cylinder and the
2 outer fluid. Pressure levels in the convective ridge are at
3 least an order of magnitude (ten times) greater than the noise
4 pressure level that exists across the propagating region.

5 The magnitude of the inner fluid pressure field P_i ,
6 normalized by the outer fluid pressure field magnitude P_o , is
7 expressed in decibels (dB) according to the following equation

$$10 \log \left(\frac{P_i(r_1)}{P_o} \right)^2 \quad (2)$$

8 where r_1 is the radial distance from the central longitudinal
9 axis of cylinder 12 at which the inner pressure field is
10 evaluated. The mathematical derivation of the dynamic response
11 is contained in "A Closed-Form Dynamic Elasticity Solution to the
12 Fluid/Structure Interaction Problem of a Two-Layer Infinite
13 Viscoelastic Cylinder With Inner and Outer Fluid Loading Subject
14 to Forced Harmonic Excitation," by M.S. Peloquin, NUWC-NPT
15 Technical Report 11,067, Naval Undersea Warfare Center, Newport,
16 Rhode Island, June 1996, the contents of which are hereby
17 incorporated by reference.

18 In order to measure the outer pressure field P_o for
19 calibration of the transfer function T_H , the present invention
20 utilizes a multi-channel composite hydrophone array assembly such
21 as that disclosed by this applicant in U.S. Patent No. 5,550,791.
22 As shown schematically in FIG. 3, applicant's patented composite
23 hydrophone array assembly 100 is made from a compliant hollow

1 cylinder 102 and wraps 20-1, ..., 20-n of piezoelectric film
2 adhered to cylinder 102 at a plurality of locations thereon. The
3 material used for cylinder 102 must be somewhat stiffer than the
4 compliant material used for cylinder 12 because cylinder 102 is
5 air-backed and must withstand hydrostatic pressure. A design
6 goal for cylinder 102 is for it to have the flattest response
7 possible in the wavenumber-frequency plane so that wavenumber-
8 frequency pressure variations are minimized. Suitable materials
9 for cylinder 102 include polycarbonate or other materials similar
10 thereto.

11 Each location wrapped with piezoelectric film defines a
12 composite force sensor or hydrophone channel 30-1, ..., 30-n.
13 The respective centers 31, ..., 3n of adjacent hydrophone
14 channels are separated along the length of cylinder 102. In its
15 simplest form, each wrap is a single wrap of piezoelectric film
16 glued over its entire area of contact with the circumference of
17 cylinder 102. The edges of a wrap, e.g., edges 201 and 202 of
18 wrap 20-1, can butt up against one another as shown, overlap
19 slightly, or continue around the circumference of cylinder 102
20 multiple times. Edges 201 and 202 preferably have tabs 204 and
21 205, respectively, extending therefrom for purpose of providing
22 pads for connection to electrical leads (not shown). Array
23 assembly 100 is constructed so that each channel 30-1, ..., 30-n
24 is of uniform sensitivity as a function of its length in the
25 longitudinal or axial direction of array assembly 100.

1 Before utilizing array assembly 100 in the measurement of
2 the outer pressure field P_o , it is necessary to determine its
3 acoustic sensitivity. Such an acoustic sensitivity calibration
4 is performed as follows. As shown in FIG. 4, array assembly 100
5 is placed a distance D from an acoustic source 300. A reference
6 hydrophone 302 is also placed a distance D from source 300.
7 Since it is desired for array assembly 100 and reference
8 hydrophone 302 to experience the same pressure field, array
9 assembly 100 and reference hydrophone 302 are only spaced apart
10 from one another by some small distance (e.g., one meter). Each
11 is also oriented to have pressure waves 304 from
12 source 300 impinge thereon from a broadside direction where
13 wavenumber k is equal to 0.

14 Array assembly 100 produces a total pressure response
15 P_{T-100} at the outer surface of cylinder 102 that is the sum of the
16 incident field P_{o-100} and the elastic scattered field P_{s-100} or

$$P_{T-100} = P_{o-100} + P_{s-100} \quad (3)$$

17 A similar relationship exists at reference hydrophone 302, except
18 that it is safe to assume that the elastic scattered field from
19 reference hydrophone 302 is sufficiently small so that it can be
20 ignored (as is generally the practice for reference hydrophones).
21 Therefore, the total pressure response P_{T-302} at reference
22 hydrophone 302 is given by

$$P_{T-302} = P_{O-302} \quad (4)$$

Since array assembly 100 is constructed on an air-backed cylinder 102, it is necessary to explore the elastic scattered field produced by the radial vibration of cylinder 102 in response to pressure waves from source 300. By using the dynamic elasticity model disclosed in applicant's afore-referenced publication, it can be shown that P_{s-100} is sufficiently small so that it too can be neglected. More specifically, for typical cylinder constructions used in towed acoustic arrays, applicant's dynamic elasticity model indicated that ignoring P_{s-100} introduced less than 1% error at frequencies below 500 Hz and only 1% error at frequencies above 500 Hz. Thus, the total pressure response P_{T-100} at array assembly 100 and P_{T-302} at reference hydrophone 302 can be considered similar enough to produce a good calibration of acoustic sensitivity for array assembly 100.

Calibration of array assembly 100 is performed using only sound arriving directly from acoustic source 300, i.e., all reflected paths are eliminated by time gating the output of array assembly 100 as is known in the art. Such restrictions on calibration make the relationship

$$P_{O-100} = P_{O-302} \quad (5)$$

true. Thus, the measured acoustic sensitivity S_{a-100} of array assembly 100 is calculated from the voltage V_{channel} measured from any channel of array assembly 100 and the measured incident pressure P_{o-302} as follows

$$S_{a-100} = \frac{V_{channel}}{P_{o-302}} \quad (6)$$

1 With the acoustic sensitivity S_{a-100} of array assembly 100
 2 known, the incident pressure field $P_{o-100}(k, \omega)$ at array assembly
 3 100 can be measured as a function of wavenumber k and frequency
 4 ω . As described in applicant's U.S. Patent No. 5,550,791, array
 5 assembly 100 defines a multiplicity of channels spaced along the
 6 length thereof. Each channel's sensor responds to
 7 circumferential strain in cylinder 102 induced by pressure field
 8 $P_{s-100}(k, \omega)$. In order to generate $P_{o-100}(k, \omega)$ having a broad
 9 wavenumber content, it is necessary to place array assembly in a
 10 turbulent flow field. One way of accomplishing this is to tow
 11 array assembly 100 through a fluid environment, e.g., water.
 12 Alternatively, array assembly 100 could be maintained stationary
 13 in a moving fluid environment.

14 The energy in a turbulent flow field is concentrated at
 15 convective wavenumbers k_c according to the relationship
 16 $k_c = \omega/c_c$, where c_c is the convection velocity. Thus, the
 17 calibration will be performed along the convective ridge or the
 18 slope in the wavenumber-frequency plane that corresponds to the
 19 convective wavenumbers k_c . The convective velocity c_c is
 20 proportional to the free stream velocity of the flow. Therefore,
 21 by towing array assembly at a variety of tow speeds, it is
 22 possible to vary the free stream velocity of the flow and obtain
 23 the calibration over a broad range of wavenumbers and

1 frequencies. However, for simplicity, the remainder of the
2 description will address only one tow speed.

3 The response of array assembly 100 is not totally accounted
4 for by the acoustic sensitivity S_{a-100} since an acoustic
5 calibration is confined to wavenumbers within the range $\pm\omega/c_d$
6 where c_d is the dilatation wave velocity of plane wave
7 propagation in water, i.e., the acoustic calibration was confined
8 to the case $k=0$. Accordingly, it is necessary to augment the
9 measured sensitivity S_{a-100} in order to obtain an acoustic
10 sensitivity for a broad range of wavenumbers and frequency. To
11 do this, a mathematical response model disclosed by applicant in
12 the aforereferenced publication is used to develop a broad-range
13 wavenumber and frequency composite sensitivity S_{c-100} for array
14 assembly 100.

15 The sensitivity of array assembly 100 can also be written

$$S_v \times S'_\epsilon \quad (7)$$

16 where the voltage-to-circumferential strain ratio S_v is equal to

$$\frac{V_{channel}}{\epsilon_{102}} \quad (8)$$

17 where ϵ_{102} is the circumferential strain at the outer surface of
18 cylinder 102. The general circumferential strain-to-pressure
19 sensitivity S'_ϵ is equal to

$$\frac{\epsilon_{102}}{P_{0-100}} \quad (9)$$

The general circumferential strain-to-pressure sensitivity S'_ϵ can be expanded into a low wavenumber, low-frequency constant term and a normalized field sensitivity by the following relationship

$$S'_\epsilon = (S_\epsilon|_{k=0, \omega=\min}) \frac{S_\epsilon(k, \omega)}{S_\epsilon|_{k=0, \omega=\min}} \quad (10)$$

where the expression " $\omega=\min$ " means a frequency in the range of 3-5 Hz.

The acoustic calibration conditions used in the present invention confine the measured acoustic sensitivity S_{a-100} to be a product of S_v and the low wavenumber, low-frequency term of equation (10). Written mathematically,

$$S_{a-100} = S_v(S_\epsilon|_{k=0, \omega=\min}) \quad (11)$$

Substitution of equation (10) into equation (7) while making use of equation (11) results in a composite sensitivity S_{c-100}

$$S_{c-100} = S_{a-100} S_n = S_{a-100} \left(\frac{S_\epsilon(k, \omega)}{S_\epsilon|_{k=0, \omega=\min}} \right) \quad (12)$$

Thus, composite sensitivity S_{c-100} becomes the product of acoustic sensitivity S_{a-100} and a term that represents the normalized wavenumber-frequency field sensitivity referred to hereinafter as S_n . As discussed in detail in applicant's aforereferenced publication, the S_n term can be written as a function of

1 strain/pressure relations

$$S_n = \frac{\left[\frac{\epsilon_{102}}{P_{o-100}} (k, \omega) \right]}{\left[\frac{\epsilon_{102}}{P_{o-100}} \Big|_{k=0, \omega=\min} \right]} \quad (13)$$

2 Substituting equation (13) into equation (12),

$$S_{c-100} = S_{a-100} \frac{\left[\frac{\epsilon_{102}}{P_{o-100}} (k, \omega) \right]}{\left[\frac{\epsilon_{102}}{P_{o-100}} \Big|_{k=0, \omega=\min} \right]} \quad (14)$$

3 For a given data collection cycle consisting of towing array
4 assembly 100 at a given tow velocity, the output voltage of the
5 array is designated $V_{100}(k, \omega)$ and the composite sensitivity is $S_{c-100}(k, \omega)$. Output voltage $V_{100}(k, \omega)$ is divided by the composite
6 sensitivity $S_{c-100}(k, \omega)$ to obtain a measurement of the pressure P_{o-100}
7 incident upon the outer surface of array assembly 100 or
8

$$P_{o-100}(k, \omega) = \frac{V_{100}(k, \omega)}{S_{c-100}(k, \omega)} \quad (15)$$

9 Note that equation (15) is predicated upon the earlier
10 assumption that P_{T-100} can be considered equal to P_{o-100} , i.e., P_{S-100}
11 is nearly zero. However, the voltage generated by array assembly
12 100 during towing (or $V_{100}(k, \omega)$) is in truth proportional to the
13 total pressure acting on the outer surface of a coating (not
14 shown) that would typically coat the hydrophone elements bonded
15 to the surface of cylinder 102. Within the range of the
16 unaliased wavenumber space of array assembly 100, the elastic

1 scattered to incident pressure ratio or

$$\left[\frac{P_{s-100}}{P_{o-100}}(k, \omega) \right] \quad (16)$$

2 is typically on the order of -30dB. Maintaining the assumption
3 that $P_{T-100} = P_{o-100}$ introduces a maximum error of approximately 3%
4 into the value obtained for $P_{o-100}(k, \omega)$. If this error is
5 unacceptable, or if array assembly 100 had a larger unaliased
6 wavenumber range (which would increase the ratio in equation
7 (16)), a correction for the elastic scattered field would be
8 necessary.

9 The total pressure P_{T-100} for the field can be written

$$P_{T-100}(k, \omega) = P_{o-100}(k, \omega) \left(1 + \left[\frac{P_{s-100}}{P_{o-100}}(k, \omega) \right] \right) \quad (17)$$

10 The correction for the elastic scattered field is obtained by
11 substituting equation (15) into equation (17) and solving for the
12 incident pressure field $P_{o-100}(k, \omega)$ where, in its expanded form
13 using equation (14),

$$P_{o-100}(k, \omega) = \frac{V_{100}(k, \omega)}{\left(S_{a-100} \frac{\left[\frac{\epsilon_{102}}{P_{o-100}}(k, \omega) \right]}{\left[\frac{\epsilon_{102}}{P_{o-100}} \right]_{k=0, \omega=\min}} \right) \left(1 + \left[\frac{P_{s-100}}{P_{o-100}}(k, \omega) \right] \right)} \quad (18)$$

14 For best accuracy, equation (18) will be used in the remainder of
15 the description to define the incident pressure field
16 $P_{o-100}(k, \omega)$.

1 One last effect that will add an unwanted wavenumber filter
2 function to the measurement of either $P_{o-100}(k, \omega)$ or
3 $P_{T-100}(k, \omega)$ is the filtering, i.e., attenuation, that occurs due to
4 the axial dimension of the sensors used in array assembly 100.
5 Attenuation increases as wavenumber increases. Such attenuation
6 can be accounted for in the calculation of pressure at the
7 surface of array assembly 100 by dividing equation (18) (or
8 equation (15) if the elastic scattered field of array assembly
9 100 is assumed to be zero) by the well known sensor aperture
10 function $A_{100}(k, \omega)$ which varies only with respect to wavenumber k .
11 This function is disclosed in Burdic, William S., Underwater
12 Acoustic Systems Analysis, Prentice-Hall, Inc., 1984.

13 The next step in the present invention involves the
14 measurement of the inner pressure field $P_i(k, \omega)$. To do this, a
15 compliant hollow cylinder 402 is configured as shown in FIG. 5.
16 Cylinder 402 (identical in outer diameter to cylinder 12 and
17 cylinder 102) houses a linear array of force sensors 404-1, ...,
18 404-n forming array assembly 400. The number of force sensors
19 used for each of array assembly 100 and array assembly 400 is
20 approximately the same. The spacing between force sensors in
21 array assembly 400 should be approximately equivalent to the
22 spacing used for array assembly 100 such that there is an area of
23 overlap between array assembly 100 and array assembly 400 in the
24 wavenumber-frequency plane. Each of force sensors 404-1, ...,
25 404-n can be conventional air-backed, nodal-mounted ceramic
26 cylinder hydrophone. Such hydrophones are available commercially

1 from Benthos Inc., North Falmouth, MA. Cylinder 402 is further
2 filled with a fluid 406 (identical to fluid 14) that surrounds
3 array assembly 400.

4 An acoustic calibration is similarly performed on array
5 assembly 400. The calibration of array assembly is performed
6 with a $k=0$ excitation which is sufficient for use throughout the
7 wavenumber-frequency plane since force sensors 404-1, ..., 404-n
8 typically have a flat response with respect to wavenumber.

9 In the present invention, cylinder 402 housing array
10 assembly 400 is towed through the same type of fluid environment,
11 e.g., water, and at the same speed(s) as array assembly 100.
12 Array assembly 400 measures the pressure field in fluid 406 as a
13 voltage designated herein by $V_{400}(k, \omega)$. However, the measured
14 pressure field voltage $V_{400}(k, \omega)$ is a measure of the total
15 pressure field at the surface of cylinder 402 (designated $P_{T-402}(k, \omega)$)
16 filtered by the transfer function of cylinder 402/fluid
17 406. Accordingly, it is necessary to convert the measured
18 pressure field voltage $V_{400}(k, \omega)$ to the filtered amount due only
19 to $P_{O-402}(k, \omega)$.

20 Applying logic similar to that used to develop equation
21 (17), $P_{T-402}(k, \omega)$ can be written

$$P_{T-402}(k, \omega) = P_{O-402}(k, \omega) \left(1 + \left[\frac{P_{S-402}(k, \omega)}{P_{O-402}(k, \omega)} \right] \right) \quad (19)$$

22 where the quantity

1

$$\left[\frac{P_{s-402}}{P_{o-402}}(k, \omega) \right] \quad (20)$$

2 is a mathematical simulation obtained as explained in detail in
3 applicant's aforereferenced publication.

4 Solving for $P_{o-402}(k, \omega)$ and replacing $P_{T-402}(k, \omega)$ with
5 $V_{400}(k, \omega)/S_{a-400}$, yields

$$P_{o-402}(k, \omega) = \frac{V_{400}(k, \omega)}{S_{a-400} \left(1 + \left[\frac{P_{s-402}}{P_{o-402}}(k, \omega) \right] \right)} \quad (21)$$

6 Similar to the calculations performed for array assembly 100,
7 the inner pressure field $P_{i-402}(k, \omega)$ is obtained by dividing
8 equation (21) by acoustic sensitivity S_{a-400} of array assembly 400
9 and an aperture function $A_{400}(k, \omega)$ so that

$$P_{i-400}(k, \omega) = \frac{V_{400}(k, \omega)}{\left(S_{a-400} \left(1 + \left[\frac{P_{s-402}}{P_{o-402}}(k, \omega) \right] \right) \right) A_{400}(k, \omega)} \quad (22)$$

10 In generating the turbulent flow field for both the outer
11 and inner pressure field measurements (i.e., measurements of
12 $V_{100}(k, \omega)$ and $V_{400}(k, \omega)$, each array assembly 100 and 400 should be
13 maintained at the same set back distance relative to the forward
14 end of the array structure. Further, each structure being towed
15 should have the same outer diameter. By doing so, each generated
16 turbulent flow field can be considered the same such that the
17 relationship

$$P_{o-100}(k, \omega) = P_{o-402}(k, \omega) \quad (23)$$

is true. Having established the condition set forth in equation (23) and insuring that the amount of $P_{i-400}(k, \omega)$ used is only due to $P_{o-402}(k, \omega)$, the transfer function for cylinder 402/fluid 406 (i.e., cylinder 12/fluid 14) is

$$T_H(k, \omega) = \frac{P_{i-400}(k, \omega)}{P_{o-100}(k, \omega)} \quad (24)$$

where $P_{i-400}(k, \omega)$ is given by equation (22) and $P_{o-402}(k, \omega)$ is given by equation (18) further divided by the acoustic aperture function $A_{100}(k, \omega)$.

It is possible to simplify the number of terms to be evaluated in the expanded form of equation (24). For example, if the lengths of the force sensors used in both array assembly 100 and array assembly 400 are the same or approximately so, their spatial Fourier transforms will be nearly identical. This essentially causes the cancellation of the sensor aperture correction terms $A_{100}(k, \omega)$ and $A_{400}(k, \omega)$. Another simplification is that at low frequencies of approximately 100 Hz or less, the term

$$\left[\frac{P_{s-402}}{P_{o-402}}(k, \omega) \right] \quad (25)$$

is negligible and can be ignored.

The advantages of the present invention are numerous. The field measurement calibration technique described herein will provide an accurate transfer function for a fluid-filled

compliant cylinder of the type used in towed acoustic arrays. As a result, acoustic measurements of such towed arrays can be interpreted with an increased certainty.

Although the present invention has been described relative to a particular embodiment, it is not so limited. For example, the force sensors used in array assemblies 100 and 400 can be pressure sensors (as described) or strain sensors. Thus, it will be understood that many additional changes in the details, materials, steps and arrangement of parts, which have been herein described and illustrated in order to explain the nature of the invention, may be made by those skilled in the art within the principle and scope of the invention.

2
3 FIELD CALIBRATION OF THE NORMAL PRESSURE TRANSFER FUNCTION
4 OF A COMPLIANT FLUID-FILLED CYLINDER

5
6 ABSTRACT OF THE DISCLOSURE

7 A method is presented to calibrate the transfer function for
8 a fluid-filled compliant cylinder as a function of wavenumber and
9 frequency. An air-filled compliant cylinder has a first linear
10 array of force sensors coupled to the cylinder's exterior
11 surface. A turbulent flow field is generated in a fluid
12 environment about the first linear array which generates an
13 output indicative of pressure incident thereupon. A fluid-filled
14 compliant cylinder identical in diameter to the air-filled
15 compliant cylinder houses a second linear array of force sensors.
16 A similar turbulent flow field is generated in the fluid
17 environment about the fluid-filled complaint cylinder to generate
18 an output indicative of pressure incident upon the second linear
19 array. The ratio of outputs is indicative of the transfer
20 function of the fluid-filled compliant cylinder. Each output can
21 be further adjusted by a calibrated sensitivity of the
22 corresponding first and second linear arrays. The method
23 compensates for elastic scattered pressure fields and the
24 wavenumber-frequency dependence of the air-filled compliant
25 cylinder's sensitivity to pressure.

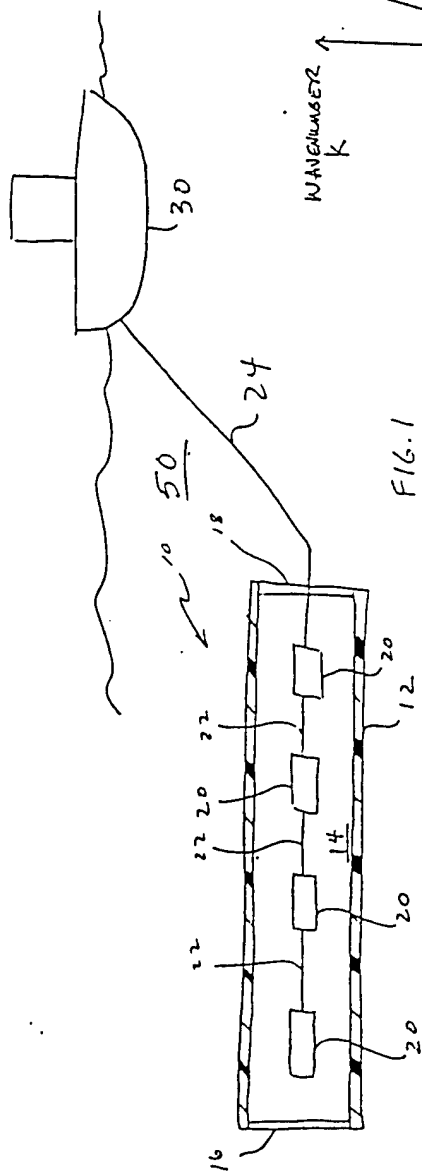


FIG. 1

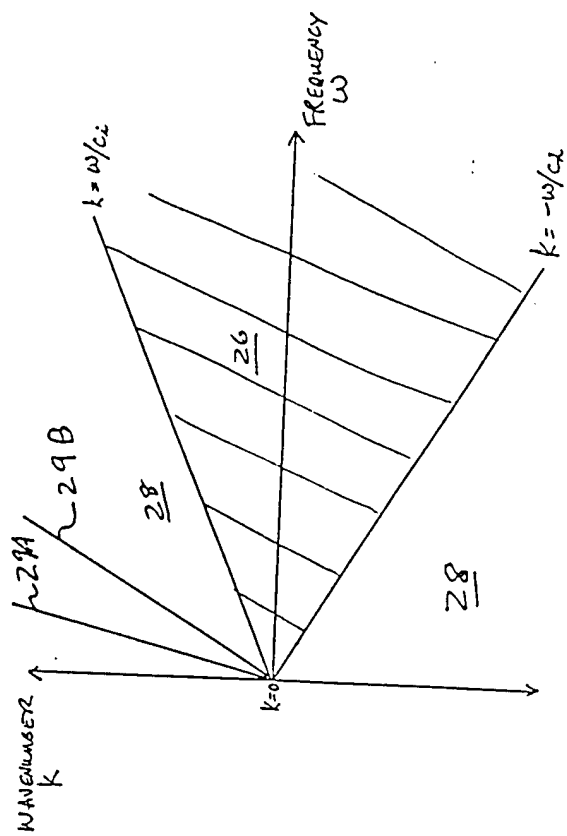


FIG. 2

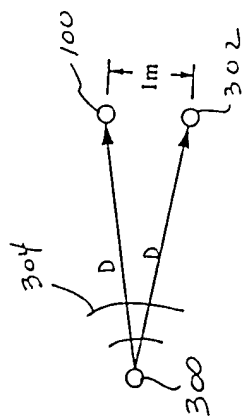


FIG. 4

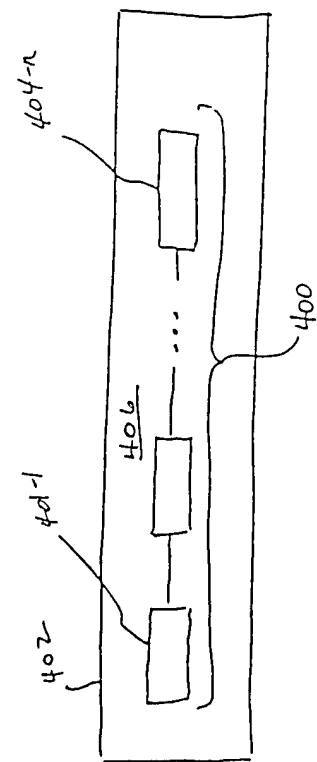


FIG. 5

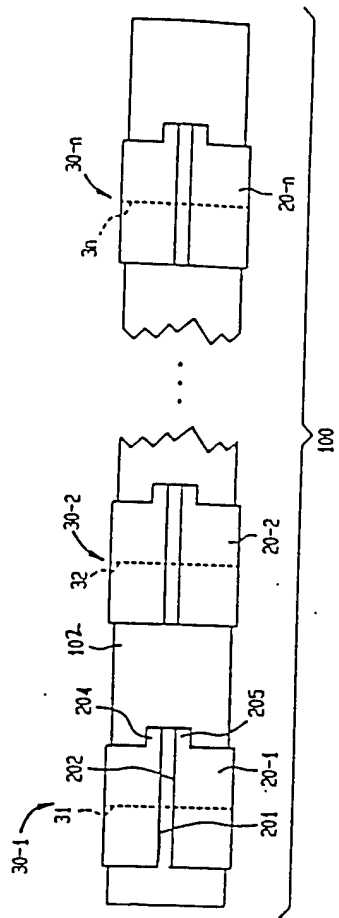


FIG. 3