Serial No.736,551Filing Date24 October 1996InventorThomas L. Carroll

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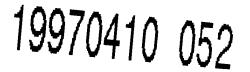
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#### AMPLITUDE INSENSITIVE SYNCHRONIZATION OF NONLINEAR SYSTEMS

#### BACKGROUND OF THE INVENTION

The present invention relates generally to the synchronization of nonlinear systems and
 more particularly to a system which allows the synchronization of one nonlinear dynamical or
 chaotic system to another nonlinear dynamical or chaotic system insensitive to attenuation in the
 driving signal.

5 A synchronized nonlinear system can be used as an information transfer system. The 6 transmitter, responsive to an information signal, produces a drive signal for transmission to the 7 receiver. An error detector compares the drive signal and the output signal produced by the 8 receiver to produce an error signal indicative of the information contained in the information 9 signal.

It is known to those skilled in the art that a nonlinear dynamical system can be driven (the response) with a signal from another nonlinear dynamical system (the drive). With such a configuration the response system actually consist of duplicates of subsystems of the drive system, which are cascaded and the drive signal, or signals, come from parts of the drive system that are included in the response system.

A system with extreme sensitivity to initial conditions is considered chaotic. The same chaotic system started at infinitesimally different initial conditions may reach significantly different states after a period of time. Lyapanov exponents (also known in the art as "characteristic exponents") measure this divergence. A system will have a complete set of

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Lyapunov exponents, each of which is the average rate of convergence (if negative) or divergence
 (if positive) of nearby orbits in phase space as expressed in terms of appropriate variables and
 components.

Sub or Conditional Lyapunov exponents are characteristic exponents which depend on the signal driving the system. It is also known to those skilled in the art that, if the sub-Lyapunov, or conditional Lyapunov, exponents for the driven response system are all negative, then all signals in the response system will converge over time or synchronize with the corresponding signals in the drive. When the response system is driven with the proper signal from the drive system, the output of the response system is identical to the input signal. When driven with any other signal, the output from the response is different from the input signal.

11 In brief, a dynamical system can be described by the ordinary differential equation

12 
$$\dot{\alpha}(t) = f(\alpha).$$
 (1)

- 13 The system is then divided into two subsystems.  $\alpha = (\beta, \chi)$ ;
- 14  $\dot{\beta} = g(\beta, \chi)$
- 15  $\dot{\chi} = h(\beta, \chi)$  (2)

16 where  $\beta = (\alpha_1, \dots, \alpha_n)$ ,  $g = (f_1(\alpha), \dots, f_n(\alpha))$ ,  $h = (f_{n+1}(\alpha), \dots, f_m(\alpha))$ ,  $\chi = (\alpha_{n+1}, \dots, \alpha_m)$ , 17 where  $\alpha$ ,  $\beta$  and  $\chi$  are measurable parameters of a system, for example vectors representing a 18 electromagnetic wave.

19 The division is arbitrary since the reordering of the  $\alpha_i$  variables before assigning them to 20  $\beta$ ,  $\chi$  g and h is allowed. A first response system is created by duplicating a new subsystem 21  $\chi$  identical to the  $\chi$  system, and substituting the set of variables  $\beta$  for the corresponding  $\beta$  in

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	Inventor: Inomas Carton	<b></b>
1	the function $h$ , and augmenting Eqs. (2) with this new system, giving	
2	$\hat{\beta} = g(\beta, \chi),$	
3	$\hat{\chi} = h(\beta, \chi) $ (3)	
4	$\chi' = h(\beta, \chi').$	
5	If all the sub-Lyapunov exponents of the $\chi$ ' system (ie. as it is driven	) are less than zero,
6.	then $[\chi' - \chi] \rightarrow 0$ as $t \rightarrow$ infinity. The variable $\beta$ is known as the driving signal	gnal. One may also
7	reproduce the $\beta$ subsystem and drive it with the $\chi$ ' variable, giving	
8	$\hat{\beta} = g(\beta, \chi),$	
9	$\dot{\chi} = h(\beta, \chi),$	
10	$\chi^{\bullet}$ , =h( $\beta$ , $\chi^{\bullet}$ ). (4)	
11	$\hat{\boldsymbol{\beta}}^{\prime\prime} = g(\boldsymbol{\beta}^{\prime\prime}, \boldsymbol{\chi}^{\prime}).$	
12	The functions $h$ and $g$ may contain some of the same variables. If a	ll the sub-Lypaunov
13	exponents of the $\chi'$ , $\beta''$ subsystem (ie. as it is driven) are less than 0, the	then $\beta'' \rightarrow \beta$ as $t \rightarrow \beta$
14	infinity. The example of the Equ. (4) is referred to as cascade	ed synchronization.
15	Synchronization is confirmed by comparing the driving signal $\beta$ with the	signal β".
16	Generally, since the response system is nonlinear, it will only sy	nchronize to a drive
17	signal with the proper amplitude. If the response system is as some remote	location with respect
18	to the drive system, the drive signal will probably be subjected to some u	inknown attenuation.
19	This attenuation can be problematic to system synchronization.	
20	The present invention is a system design featuring subsystems whi	ch are nonlinear and
21	possibly chaotic, but will still synchronize when the drive signal is attenuate	ed or amplified by an

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1	unknown amount. This invention builds on the design of two previous inventions, the
2	synchronizing of chaotic systems, US patent 5,245,660, and the cascading of synchronized chaotic
3	systems, US patent 5,379,346, both herein incorporated by reference. The present invention
4	extends those principles to situations where the drive signal has been attenuated by some
5	unknown amount. Applicants overcome this limitation by providing for a nonlinear response
6	system that is not amplitude dependent and a separate function that is part of the drive system
7	only that is amplitude dependent.
8	
9	SUMMARY OF THE INVENTION
10	Accordingly, it is an object of the present invention to provide a chaotic system which
11	will reproduce a signal that is a scaled version of one or more drive signals even when the drive
12	signal, or signals, are subject to attenuation, fading, and desynchronize this response signal by
13	varying a parameter in the drive or response system.
14	It is also an object of the present invention to provide a chaotic system which will detect
15	the variation of a parameter or parameters in the drive or response systems by detecting
16	desynchronization.
17	A further object of the present invention is to provide a system which will send
18	information on a chaotic carrier in a way that is not sensitive to noise or fading by comparing
19	the input and output of the response system while varying the drive system. These and additional
20	objects of this invention are accomplished by the structures and processes hereinafter described.
21	The present invention is an amplitude insensitive synchronized nonlinear system (AISN)

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which allows communication between nonlinear systems operating in the chaotic realm which is 1 largely insensitive to attenuation or signal noise affecting the amplitude of the drive signal, 2 3 thereby allowing communication between remote systems where the amplitude of the transmitted 4 signal has been varied by an unknown amount. AISN comprises a transmitter system (drive) employing linear or scale invariant nonlinear 5 subsystems, the output of the one driving the other, at least two which are amplitude insensitive 6 7 in operation. The signal produced by the second scale invariant nonlinear subsystem is then used to drive an amplitude dependent nonlinear function. The amplitude dependent nonlinear function 8 acts to bound the chaotic signal and prevent the signals from diverging uncontrollably, and is 9 10 designed to have characteristics that ensure a plot of its input vs. output can be related at the 11 same reference point. This is critical because this common reference point serves as a baseline 12 point for one to determine system synchronization. The chaotic transmitter signal produced by 13 the amplitude dependent function is then transmitted to a nonlinear cascaded receiver. 14 AISN employs a receiver (response) which comprises subsystems which are duplicates of 15

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transmitted signal.

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The synchronized nonlinear system can be used as an information transfer system. The

the transmitters scale invariant subsystems and are arranged to be responsive to the AISN

transmitter. Synchronization is confirmed by sampling the value of the transmitted signal. If the

input to the receiver and the output pass through known reference points at the same time, then

the transmitter and receiver are known to be synchronized. Information may be encoded by

making the output from the receiver go out of synchronization with the input by altering the

Serial No. (unassigned) **Patent Application** Inventor: Thomas Carroll Attorney Docket No. 77,203 transmitter, responsive to an information signal, produces a drive signal for transmission to the 1 2 receiver. An error detector compares the drive signal and the output signal produced by the 3 receiver to produce an error signal indicative of the information contained in the information signal. 4 5 6 BRIEF DESCRIPTION OF THE DRAWINGS 7 8 Figure 1. is a block diagram of a cascaded synchronized nonlinear system (prior art). Figure 2. is a block diagram of an amplitude insensitive synchronized nonlinear system. 9 Figure 3. is a schematic diagram of an example chaotic drive circuit constructed in accordance 10 11 with this invention. 12 Figure 4(a). is a graphical representation of input signal Y and the output signal from circuit 13 function  $g_i(x)$ 14 Figure 4(b). is a graphical representation of input signal X and the output signal from circuit 15 function  $g_{2}(x)$ . 16 Figure 4(c). is a graphical representation of input signal Y and the output signal from circuit 17 function  $g_{i}(y)$ . 18 Figure 5. is the chaotic attractor from the example drive circuit of figure 3. 19 Figure 6. is a schematic diagram of an example response circuit for figure 3 constructed in 20 accordance with this invention. 21 Figure 7. is a representation of the power spectrum of the transmitted chaotic signal  $u=\Gamma g_1(y)$ . 22 Figure 8(a). is a plot of the Y signal form the driving circuit vs. the Y' signal from the receiving 23 circuit with a scaling factor of  $\Gamma$ =1.0. 24 Figure 8(b). is a plot of the Y signal form the driving circuit vs. the Y' signal from the receiving 25 circuit with a scaling factor of  $\Gamma=0.2$ Figure 9. is the chaotic attractor for the response circuit with a scaling factor of  $\Gamma$ =0.5. 26 Figure 10. is a plot of the drive signal  $u_d$  vs. the output signal Y' from the response circuit. 27 Figure 11. is a schematic diagram of an example of the synchronization detection circuit. 28 29 Figure 12. is a plot of the low frequency power spectrum of  $u_{e}$ . 30 Figure 13. is a block diagram of an signal transmission system featuring amplitude insensitive 31 chaotic synchronization. 32 33 34 DETAILED DESCRIPTION 35 36 Referring now to the figures, wherein like reference characters indicate like elements

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scale-invariant set of differential equations:

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1	throughout the several views, figure 1 illustrates a block diagram of the basic architecture of a
2	cascaded synchronizing nonlinear system 100 divided into subsystems A 298, B 299, A' 390
3	and <b>B</b> ' 399, for producing synchronized communication signals $S_B$ 222 and $S_B$ ' 333. The
4	system is a tangible system that can be of any form. Examples of signals, such as signals $S_B$
5	222 and $S_B$ ' 333 can be associated with system 100 can be electrical, optical or other
6	electromagnetic signals, pressure, force temperature, chemical concentration, population or
7	others.
8	Since the response system 300 is nonlinear, it will only synchronize to a drive signal
9	222 from the drive system 200 having the proper amplitude. In other words, for some
10	nonlinear function $f(x)$ , rescaling x produces a different result: $f(\Gamma x) \neq \Gamma f(x)$ . There are

11 nonlinear functions for which the equality does not hold; for example, if f(x) is polynomial

12 nonlinear, exponentially nonlinear or piecewise linear the desired characteristics are present.

13 For example, if f(x) is piecewise nonlinear, (f(x) may be constructed from the line segments

14 with different slopes) and f(x) has its only break point at the origin, then  $f(Tx) = \Gamma f(X)$ , so that

15 f(x) is scale invariant. Any amplitude dependent nonlinear function in which the input and

16 output can be related at some point will is acceptable. If one has functions f(x, y, z), h(x, y, z)

17 z), and u(x, y, z) which contain only scale invariant nonlinearities, it is possible to construct a

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$$\frac{d(\Gamma x)}{dt} = \Gamma \frac{dx}{dt} = f(\Gamma x, \Gamma y, \Gamma z) = \Gamma f(x, y, z)$$

$$\frac{d(\Gamma y)}{dt} = \Gamma \frac{dy}{dt} = h(\Gamma x, \Gamma y, \Gamma z) = \Gamma h(x, y, z)$$

$$\frac{d(\Gamma z)}{dt} = \Gamma \frac{dz}{dt} = u(\Gamma x, \Gamma y, \Gamma z) = \Gamma u(x, y, z)$$

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The scale factor  $\Gamma$  will cancel, so that rescaling all of the variables does not affect the 3 dynamics of the system. This relation is also true for a linear set of equations. It is not 4 possible to get chaos out of a scale invariant set of equations such as equation (5). Some 5 6 instability is necessary for chaos to exist, so that nearby phase space trajectories diverge from 7 each other. The trajectories will diverge to infinity, however, unless some mechanism exists to fold them back when some variable becomes too large. This requires that some part of the 8 differential equations for a chaotic system depend on the amplitude of at least one of the 9 variables. It is useful to isolate the amplitude dependence in one function, g(x) for example. 10 When the chaotic system is constructed properly, then g(x) may also be used as a driving 11 signal to drive a cascaded response system. Figure 2 is a block diagram of such a system. 12 Referring now to figure 2, the signal from B to A in the full chaotic system passes through 13 the amplitude-dependent function g. The signal  $S_{g(x)}$  may then be used to drive A' in the 14 response system, which then drives B'. Rather than comparing  $S_B$ ' to  $S_B$  to confirm 15

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1	synchronization, as is Figure 1, synchronization is confirmed by comparing $S_B$ with $g(x)$ . In
2	order to make the detection of synchronization easier, it is useful to make $g(x_0) = \alpha_0$ , where
3	$\alpha_0$ is a known reference point for some $x_0$ so that the input and output of the response system
4	may be directly compared.
5	If A and B are linear or contain only scale-invariant nonlineaities, then if the driving
6	signal $S_{g(x)}$ is replaced by $\Gamma S_{g(x)}$ , the signals in <b>B</b> ' and <b>A</b> ' will be scaled by $\Gamma$ relative to the
7	signals in A and B. The use of a function of a variable rather than the variable itself as a
8	driving signal to synchronize the chaotic systems has been described before (L. Kocarev and
9	U. Parlitz, General Approach for Chaotic Synchronization with Applications to
10	Communication, Phys. Rev. Lett. 74, p. 5028, (June 1995)), but in the Kocarev and Parlitz
11	approach the entire chaotic drive system must be reproduced and the other subsystems contain
12	non scale-invariant nonlinearities. In the present invention, the driving function need not be
13	reproduced.
14	It should be noted that with the right choice of g, it is possible for A and B to be
15	linear. It is advantageous for communications to have A or B include some nonlinearity, as
16	this makes it harder to decode an encoded information signal and easier to separate noise from
17	the chaotic signal.
18	As a specific example, figure 3 shows a schematic diagram for a chaotic drive circuit
19	fulfilling the above conditions.
20	Drive circuit 400 comprises two interdependent subsystems A 498 and B 499 which
21	may or may not overlap in part but which together constitute the essential aspects of the

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1	amplitude independent system of the drive. Subsystems A 498 and B 499 are not overlapping
2	in the sense that neither subsystem A 498 nor subsystem B 499 is contained within the other
3	system. Drive circuit 400 also comprises an amplitude dependent function g(x), 500.
4	Drive circuit 400 comprises integrator circuits formed by differential amplifiers 411,
5	413, 415, 417, resistors 420, 421, 422, 423, 426, 427, 439, 440, 443, 444, and capacitors
6	451, 452, 453, and 454, amplitude independent nonlinear functions formed by differential
7	amplifiers 414, 416 resistors 437, 438 442 and diodes 480 and 481 and a summing circuit
8	formed by differential amplifier 412 and resistors 424 and 425. These circuits are coupled to
9	form subsystems A 498 and B 499 in the drive circuit as illustrated in figures 2 and 3. Drive
10	circuit 400, also comprises g(x), the nonlinear amplitude dependent nonlinear function 500
11	(piecewise in this example), formed by differential amplifiers 510, 511, resistors 518, 519 520
12	521, 522, 523, 524, 525 and diodes 580 and 581. Component values for the resistors and
13	capacitors which were used are set fourth in the following table:
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1	
2	$R420 = 1M\Omega$ $R421 = 68k$ R422 = 2M $R423 = 1M$
	R424 = 20k $R425 = 10k$
3	R426 = 100k R427 = 680k R438 = 5k R439 = 100k
4	R440 = 100k $R441 = 2.2k$
•	R442 = 10k $R443 = 10kR444 = 10k$ $R518 = 20k$
5	R519 = 10k $R520 = 10k$
	R521 = 10k $R522 = 10k$
6	R523 = 150k R524 = 150k R525 = 33k
7	
•	$\begin{array}{rcl} C451 &=& 0.001 \mu F & C452 &=& 0.001 \mu \\ C453 &=& 0.001 \mu & C454 &=& 0.001 \mu \end{array}$
8	$C_{1}S_{2} = 0.001\mu$ $C_{1}S_{1} = 0.001\mu$
-	P461 = 30k  set to  22.5k
9	P462 = 200k break/ g2 @ 0.0V P463 = 200k break/ g3 @ 0.0V
10	
11	
12	Resistance values are expressed in Ohms and capacitance values are expressed in Farads.
13	
1.5	
14	Drive circuit 400 can be subdivided into three subsystems A 498, B 499 and g(x) 500.
	(1)  (1)  (1)  (2)  (2)  (3)
15	Although the illustrative subsystems $g(x)$ 500, A 498 and B 499 shown in figure 2
16	correspond to the two circuits forming drive circuit 400 its is not necessary, and the division
17	of a given drive circuit 400 into subsystems in order to determine the proper configuration for
18	a synchronized response circuit 600 is made in accordance with the analysis described herein.
19	The nonlinear folding function is $g_1(y)$ , while the amplitude(scale)-invariant
20	nonlinearities are provided by functions $g_2(x)$ and $g_3(y)$ . The equations describing the circuit
	· · · · · · · · · · · ·
21	are:

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(6)

$$\frac{dx}{dt} = -\alpha (0.05x + 0.05g_1(y) + 1.47z + 0.1S_1)$$

$$\frac{dy}{dt} = -\alpha (-0.5x - 0.44g_1(y) + 0.147y)$$

 $\frac{dz}{dt} = -\alpha \left(-0.5g_2(x) + z - 0.5w\right)$ 

$$\frac{dw}{dt} = -\alpha (-10.0g_3(g_1(y)) + 10.0w)$$

 $g_{1}(y): \begin{bmatrix} y \le -1.6 & g_{1} = -2.5y - 7.2 \\ -1.6 \le y \le 1.6 & g_{1} = 2.0y \\ 1.6 \le y & g_{1} = -2.5y + 7.2 \end{bmatrix}$ 

$$g_{3}(y):\begin{bmatrix} y \le 0 & g_{3}=4.5y \\ y > 0 & g_{3}=0 \end{bmatrix}$$
$$g_{2}(x):\begin{bmatrix} x \le 0 & g_{2}=0 \\ x > 0 & g_{2}=4.5x \end{bmatrix}$$

2 where the time factor  $\alpha$  was 10<sup>4</sup>.

The plots of functions  $g_1(y)$ ,  $g_2(x)$  and  $g_3(y)$  as defined in figure 3 and equation (6), are illustrated in figures 4a, 4b, and 4c, respectively. These plots reflect the driving of the above nonlinear functions with a 10Hz sine wave. S<sub>1</sub> is a non-zero information signal,

6 injected into drive circuit 400 when the circuits are used for communications. The presence

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1	of chaos in drive circuit 400 is confirmed by calculating the largest Lyapunov exponent
2	numerically from eqs. (6). This exponent is 765 s <sup>-1</sup> . Conventional methods for calculating
3	Lyapunov exponents, as analytical measurement, numerical and otherwise can be used, such
4	as, for example those described by Eckmann et al., Rev. Mod. Phys., Vol. 57, p.617 et seq.
5	(1985); Lichtenberg et al., Regular and Stochastic Motion, Springer-Verlag, New York
6	(1983): Rashband, Chaotic Dynamics of Nonlinear Systems, John Wiley & Sons, New York
7	(1990); and Wolf et al., Physica. Vol. 16D, p. 285 et seq.(1985).
8	The chaotic attractor for example drive circuit 400, produced by plotting the y signal
9	vs. the x signal is shown in Figure 5.
10	Referring now to figure 6, which shows an example of a chaotic response circuit 600
11	built to synchronize with drive circuit 400 of figure 3, comprises duplicates of subsystems A
12	498 and B 499 of drive circuit 400, labeled as subsystems A' 698 and B' 699.
13	Response circuit 600 comprises integrator circuits formed by differential amplifiers
14	611, 613, 615, 617, resistors 620, 621, 622, 623, 626, 627, 639, 640, 643, 644, and
15	capacitors 651, 652, 653, and 654, amplitude independent nonlinear functions formed by
16	differential amplifiers 614, 616 resistors 637, 638, 642 and diodes 680 and 681 and a
17	summing circuit formed by differential amplifier 612 and resistors 624 and 625. These
18	circuits are coupled to form subsystems A' 698 and B' 699 in response circuit 600 as
19	illustrated in figures 2 and 6. The reader should note that $g(x)$ , the amplitude dependent
20	nonlinear circuit 500, is not reproduced in response circuit 600. Component values for the
21	resistors and capacitors which were used are set fourth in the following table:

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2	$R621 = 68k\Omega \qquad R622 = 2M$	
3	R623 = 1M $R624 = 20kR625 = 10k$ $R626 = 100k$	
•	R627 = 680k R638 = 5k R639 = 100k R640 = 100k	
4	R641 = 2.2k $R642 = 10k$	
5	R643 = 10k $R644 = 10k$	
	$C651 = 0.001 \mu F C652 = 0.001 \mu$	
6	$C653 = 0.001\mu$ $C654 = 0.001\mu$	
7	P661 = 30k  set to  22.5k	
,	P662 = 200k break/ g2 @ 0.0V P663 = 200k break/ g3 @ 0.0V	
8		
9		
10	Resistance values are expressed in Ohms and capacitance values are expressed in Farads.	
10	Resistance values are expressed in Oninis and capacitance values are expressed in Yalues.	
11		
12	Response circuit 600 can be subdivided into two subsystems A' 698 and B' 699.	
13	Although the illustrative subsystems A' 698 and B' 699 shown in figure 2 correspond to t	he
14	two circuits forming response circuit 600, its is not necessary, and the division of a given	
15	response circuit 600 into subsystems in order to determine the proper configuration for	
16	synchronization with a drive circuit 400 is made in accordance with the analysis described	
17	herein.	
18	The equations describing the circuit are:	
19	(7)	

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 $u_d = \Gamma g_1(y)$ 

$$\frac{dx'}{dt} = -\alpha (0.05x' + 0.05u + 1.47z')$$

$$\frac{dy'}{dt} = -\alpha (-0.5x' - 0.44u + 1.47y')$$

$$\frac{dz'}{dt} = -\alpha (-0.5g_2(x') + z - 0.5w')$$

$$\frac{dw'}{dt} = -\alpha (-10.0g_3(u) + 10.0w')$$

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The output function g<sub>1</sub>(y) has been rescaled by a factor Γ to produce the driving
variable u<sub>d</sub>. The largest Lyapunov for the response circuit is calculated numerically to be
-1470.0s<sup>-1</sup>, independent of the scaling factor Γ.

It is necessary for  $u_d = \Gamma g_1(y)$  to have a known relation to y' at some known value of 5 y in order to detect synchronization of the drive 400 and response 600 circuits. This 6 relationship must be independent of the scaling factor  $\Gamma$ . In the example circuit above this 7 8 relation is satisfied by  $\Gamma g_1(0) = 0$ . Referring now to figure 10, which is a graph of y' vs the transmitted signal  $u_d$  when the scaling factor is  $\Gamma=1$ , the reader should note that for all values 9 of  $\Gamma$ , the graph passes through the origin (0,0). This allows synchronization to be confirmed 10 by sampling the value of the transmitted signal  $\mu_d$  when y' crosses 0. When the circuits are in 11 synchronization, the sampled value is 0. 12

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1 Among the many embodiments of the present invention, AISN may be employed to transmit information on a chaotic carrier in the form of data encoded on a pure frequency 2 signal. The system allows the transmission of the data by a means which is insensitive to 3 fading distortion and not very sensitive to other types of noise. Referring to figures 2, 3, 6, 4 and 13 example chaotic drive circuit 400, forms a portion of a transmitter 800 and example 5 chaotic response circuit 600 forms part of a receiver 900. Drive circuit 400 is injected with 6 an information signal  $S_I$ . Assume, for purposes of example, the signal  $S_I$  is configured as 7 2.0sin(2 $\Pi$ f<sub>1</sub>t) where f<sub>1</sub> is less than 200Hz. The frequencies which contain much of the power 8 for the transmitted signal approach 2kHz, so the  $S_I$  frequency is small in comparison to 9 maximize the S/N ratio in receiver 900. Frequencies above 200Hz for  $S_i$  would tend to lower 10 the S/N ratio in this example. The effects of different types of signal encoding are system 11 dependent; for the circuit described in figure 3 and equation (6), the fact that different types 12 13 of signal encoding move the plot (see figure 10) of y' vs  $u_d$  in different directions may be used for sending multiple information signals on one chaotic signal. 14

15 Referring again to figure 3, the information signal  $S_1$  is injected into the integrator 16 whose output voltage is labeled as X. The drive signal  $u_d$  may be transmitted to response 17 circuit 600 by any desired conventional wired or wireless fashion, 11. The information signal 18 is decoded from the chaotic carrier  $u_d$  by comparing  $u_d$  to response 600 output y' as y' crosses 19 0. In order to detect the information in the chaotic carrier signal  $u_d$ , the negative-going 20 zero crossings of the signal y' from the response circuit is used to strobe  $u_d$ , generating a 21 detected signal  $\Delta$ . When drive 400 and response 600 circuits are synchronized,  $u_d$  is zero

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1	when y' is zero, therefore $\Delta$ is zero. When response 600 and drive 400 are not synchronized,
2	$u_d$ is nonzero when y' crosses zero, so $\Delta$ is non-zero. Generally, for a small signal S <sub>1</sub> injected
3	into the drive 400 system (or if any parameter is changed by a small amount), the average of
4	$\Delta$ is proportional to the injected signal (or the parameter difference between the drive and
5	response system). If $S_1$ has a much lower frequency than the average rate at which y' crossed
6	zero, $\Delta$ can also be used to detect S <sub>1</sub> , since the information signal S <sub>1</sub> , causes a lack of
7	synchronization. Passing $\Delta$ through a low pass filter (not shown) has the effect of averaging $\Delta$
8	to reveal the information signal S <sub>I</sub> .
9	Detector circuit 900, shown in figure 11, may be used to decode the information
10	signal. The signal y' is greatly amplified and applied to a comparator 960 so that a pulse is
11	generated when y' crosses 0 in the negative direction. This pulse is applied to a sample and
12	hold amplifier 950 which samples the difference between y' and $u_d$ when y' crosses 0. The
13	output of the sample and hold amplifier 900 is the detected signal. Figure 12 shows the low
14	frequency power spectrum of the transmitted signal $u_d$ when the informational signal $f_1$ is 30
15	Hz. The signal to noise ratio at $f_1$ was calculated by subtracting the average signal power (in
16	dB) within 2 Hz of $f_1$ (not including the power at $f_1$ ) from the power at $f_1$ . Figure 7 displays
17	a plot of the power spectrum of the transmitted signal $u_d$ , which shows the broad band nature
18	of chaos. Figure 8(a) shows a plot of the y' signal vs. y when $\Gamma=1$ , showing synchronization.
19	In figure 8(b) also shows a plot of the y' signal vs. y however in 8(b) $\Gamma$ =0.2. The signal y' is
20	now a scaled version of y. Figure 9 shows y' vs. x' in the response circuit when $\Gamma=0.5$ . The
21	plot of figure 9 is a scaled reproduction of the attractor in figure 5.

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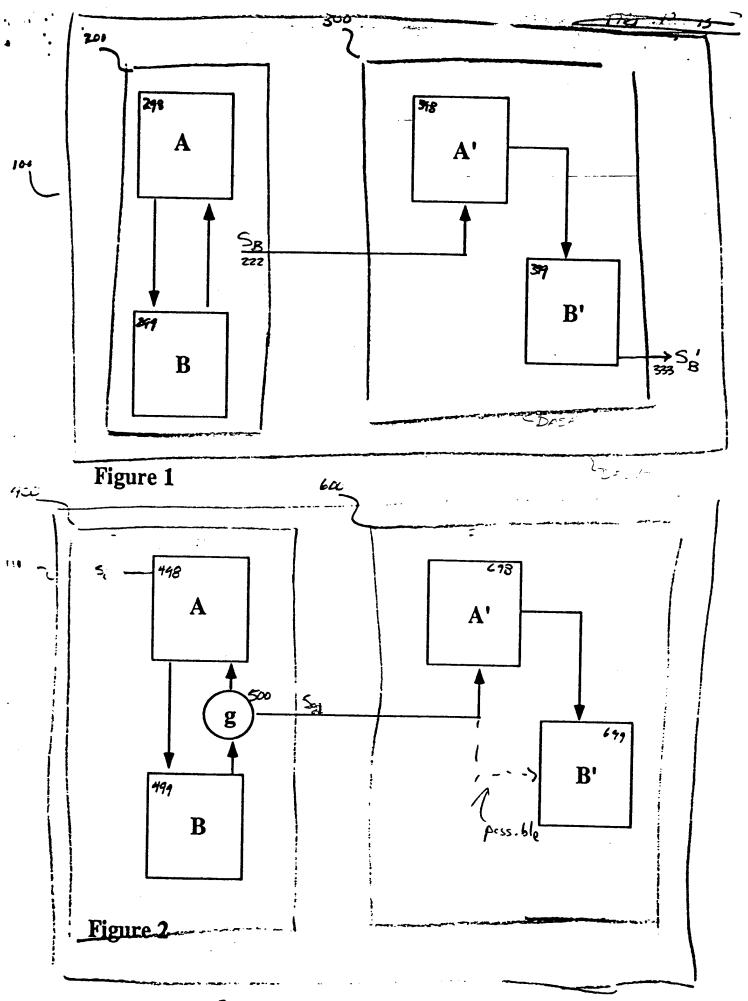
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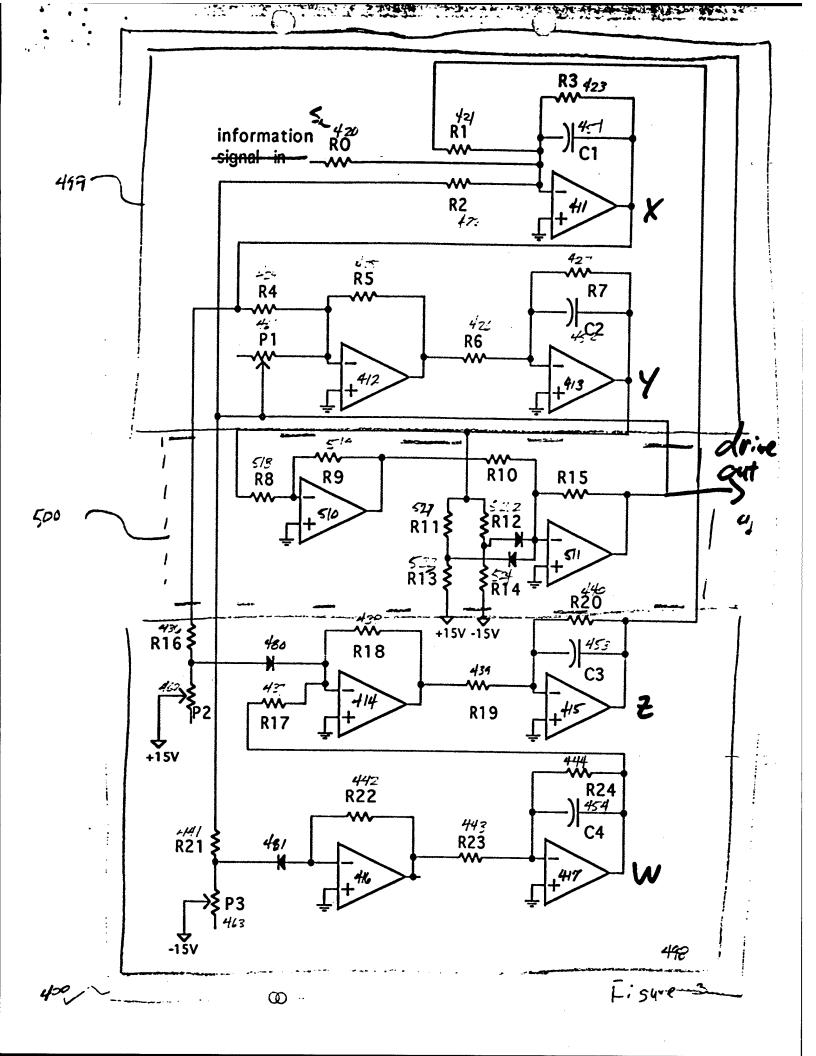
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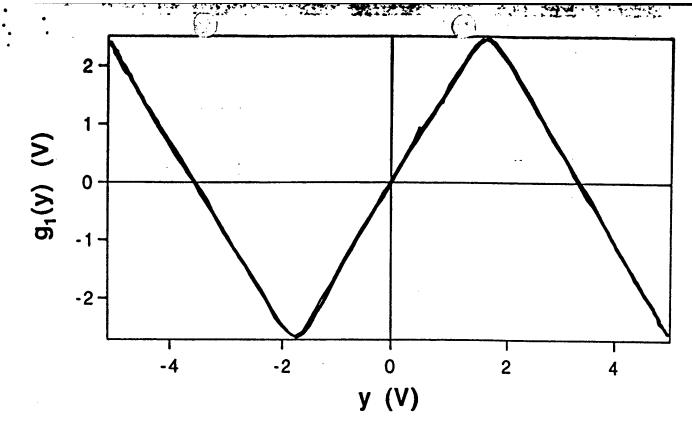
# Patent Application Attorney Docket No. 77,203

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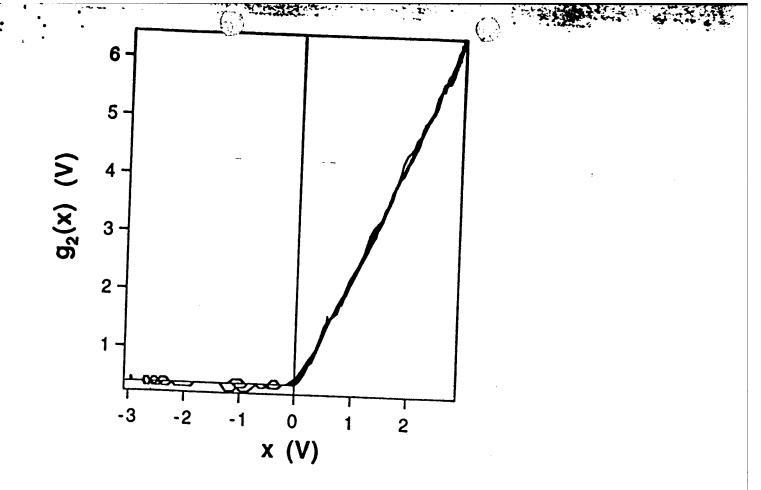
1	ABSTRACT
2	The present invention is an amplitude insensitive synchronized nonlinear system
3	(AISN) which allows communication between nonlinear systems operating in the chaotic
4	realm which is largely insensitive to attenuation or signal noise affecting the amplitude of the
5	drive signal, thereby allowing communication between remote systems where the amplitude of
6	the transmitted signal has been varied by an unknown amount.
7	AISN comprises a transmitter system (drive) grouped into linear or scale invariant
8	nonlinear subsystems, the output of the first driving the second, both amplitude insensitive in
9	operation. The signal produced by the second subsystem is then used to drive a amplitude
10	dependent nonlinear function. The amplitude dependent nonlinear function is designed to
11	have characteristics that ensure a plot of its input vs. output can be related at the same
12	reference point. The chaotic transmitter signal produced by the amplitude dependent function
13	is then transmitted to a nonlinear cascaded receiver.
14	AISN employs a receiver (response) which comprises subsystems which are duplicates
15	of the transmitters scale invariant nonlinear subsystems arranged to be responsive to the AISN
16	transmitter. Synchronization is confirmed by sampling the value of the transmitted signal.
17	When the input to the receiver and the output pass through known reference points at the
18	same time, then the transmitter and receiver are known to be synchronized. Information may
19	be encoded by making the output from the receiver go out of synchronization with the input
20	by altering the transmitted signal.
21	

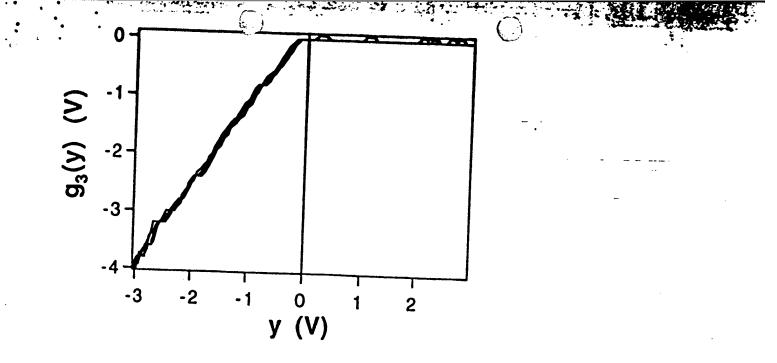




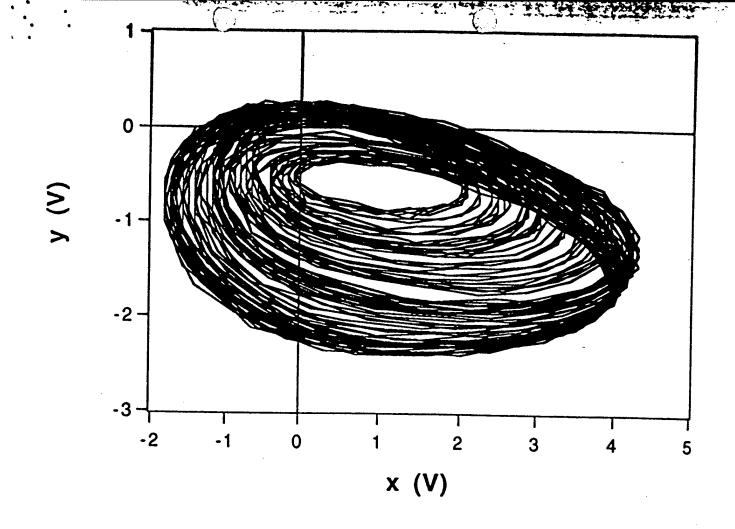


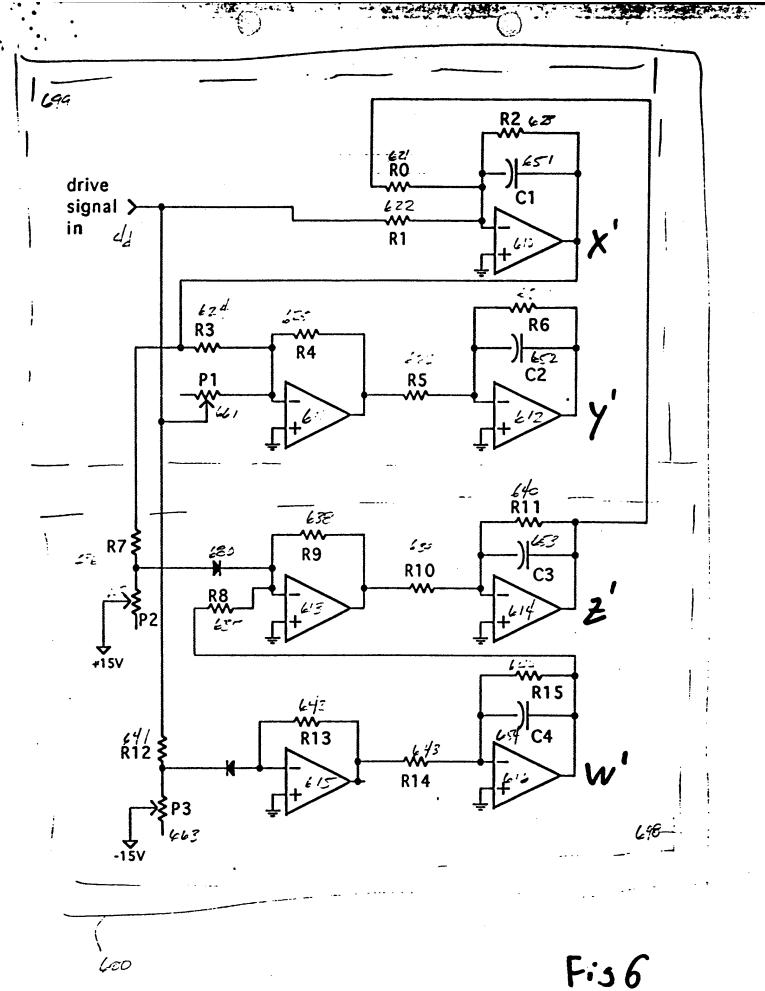
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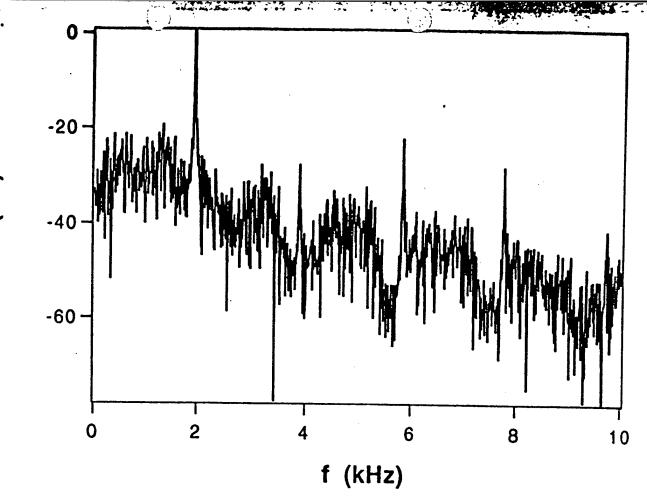


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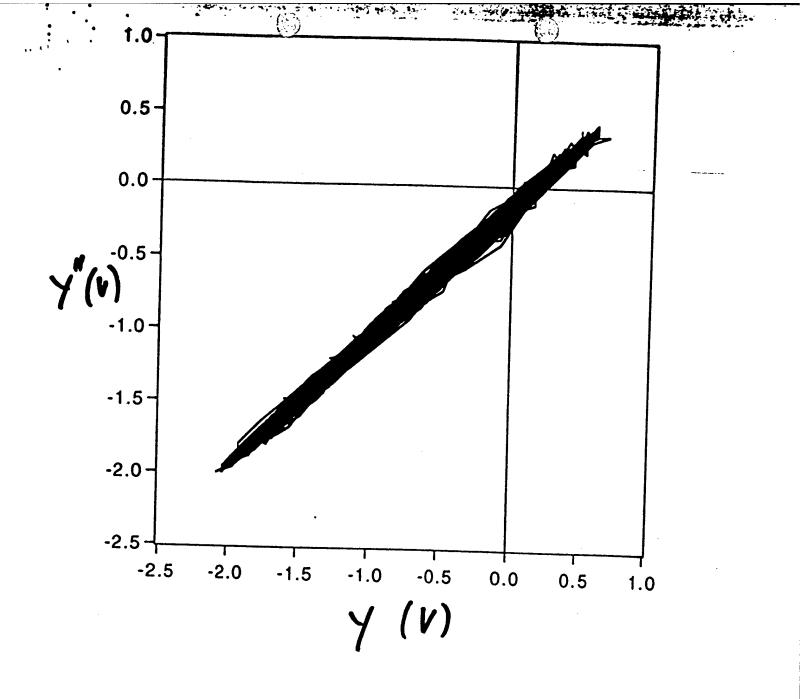
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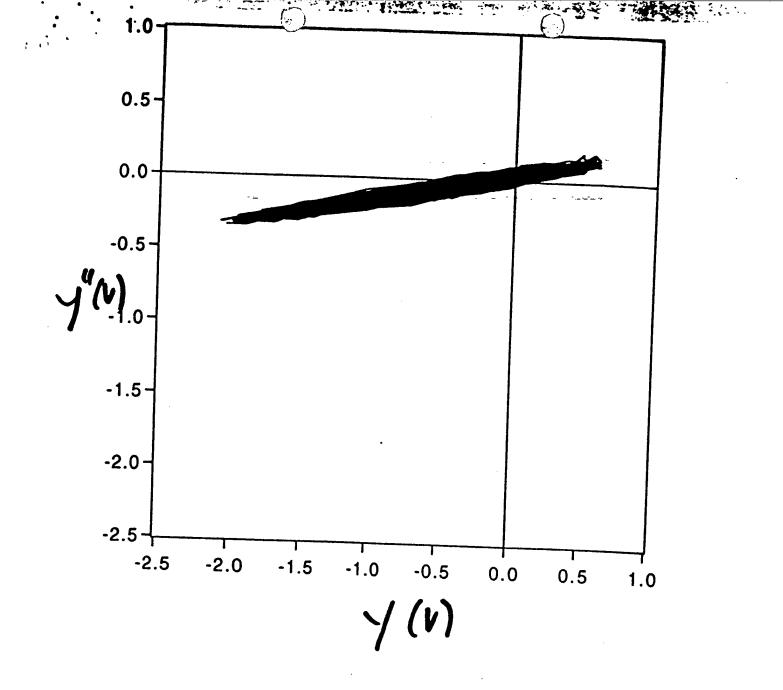
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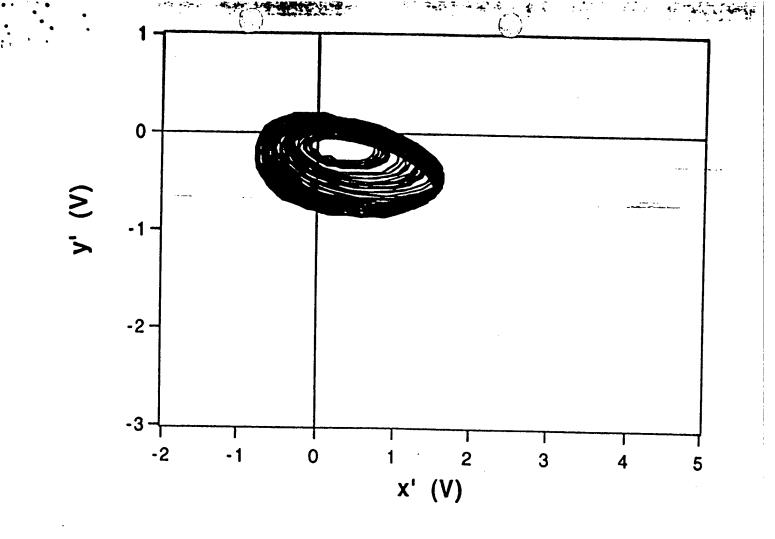
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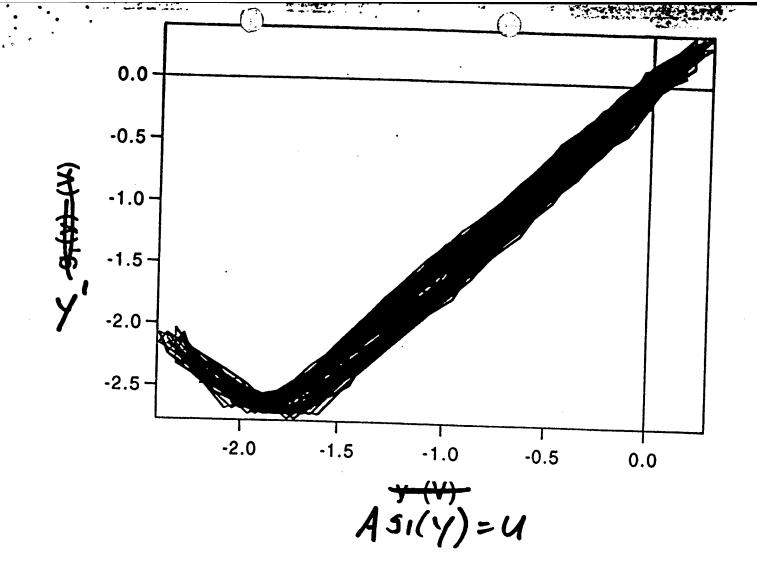


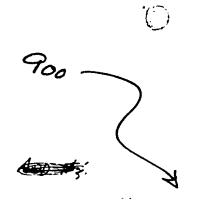
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Fis 9





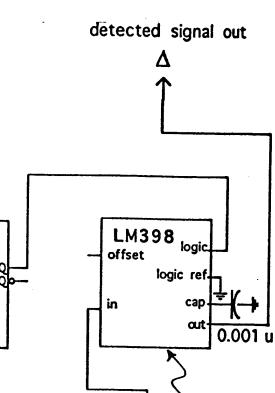
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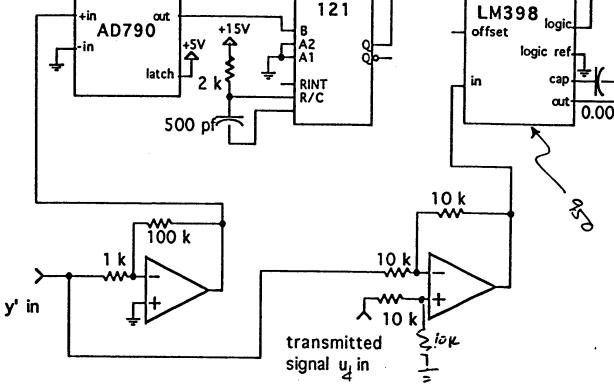
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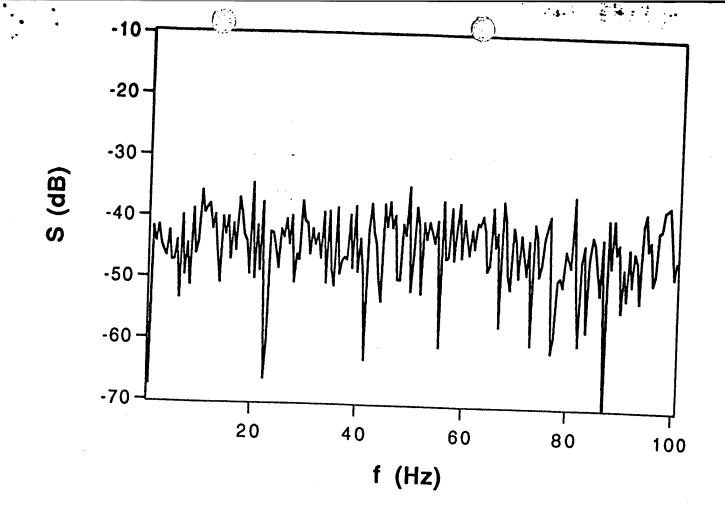
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Fis II



Fis 12