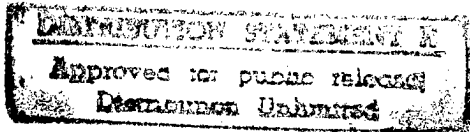


Serial No. 715,741  
Filing Date 19 September 1996  
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NOTICE

The above identified patent application is available for licensing. Requests for information should be addressed to:

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CODE OCCC3  
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DTC QUALITY INSPECTED 3

19970103 053

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SYSTEM AND METHOD FOR COMPENSATING FOR DOPPLER SHIFTS

4

IN SIGNALS BY DOWNSAMPLING

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STATEMENT OF GOVERNMENT INTEREST

7 The invention described herein may be manufactured and used  
8 by or for the Government of the United States of America for  
9 governmental purposes without the payment of any royalties  
10 thereon or therefor.

11

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BACKGROUND OF THE INVENTION

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(1) Field Of The Invention

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The present invention pertains to compensation of Doppler  
affected signals and in particular, to compensation of Doppler  
shift in signals by oversampling and downsampling using  
decimation.

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(2) Description of the Prior Art

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In data transmission between one or more moving vehicles,  
the Doppler effect causes a shift in a signal between the  
transmission from a signal source to the reception of the signal  
in a signal receiver. When either the signal source or the  
signal receiver are moving with respect to the other, Doppler  
shift will occur, affecting the frequency and duration of the  
signals. One particular type of communication in which Doppler  
shift is a concern is when acoustic signals are transmitted by an  
underwater moving vehicle. The Doppler effect on the signals,

1 such as acoustic signals, depends on the movement of the  
2 transmitter and/or receiver with respect to each other and the  
3 medium in which the signals are being transmitted, for example,  
4 water.

5 Systems designed to receive acoustic signals must either be  
6 insensitive to Doppler shift or be able to correct or compensate  
7 for the Doppler shifting. Typically, the systems that receive  
8 and analyze signals, such as underwater acoustic signals, are  
9 digital systems which sample the incoming data at a fixed  
10 sampling frequency or rate. The digitally sampled signals  
11 reflect the shift caused by the Doppler affect as a translation  
12 in frequency and therefore a compression or expansion in time or  
13 duration of the signal. Some existing systems and methods  
14 correct the Doppler shifted signal that has been sampled, for  
15 example, by mathematical manipulation of the data sampled at a  
16 fixed sampling rate or by adjusting the sampling frequency or  
17 rate to compensate for the Doppler affect.

18 Mathematical techniques for manipulating the sampled data  
19 have included time-domain interpolation of samples and discrete  
20 Fourier transform methods for non-integer decimation. Such  
21 methods have a high numeric complexity and are mathematically  
22 intensive. The computational burden of such mathematical methods  
23 can be prohibitively large for many real-time applications, for  
24 example, in communications systems. The mathematical methods can  
25 also create phase distortions or other unwanted and detrimental  
26 effects in the data. Such mathematically intensive and complex  
27 techniques are disclosed, for example, in U.S. Patent Nos.

1 5,130,952 and 5,388,080 to Feintuch, et al., U.S. Patent No.  
2 4,905,211 to MacKelburg, et al. and in U.S. Patent No. 4,099,249  
3 to Casasent.

4 Adjusting the sampling frequency to compensate for the  
5 Doppler shifting is limited by the resolution of the clock in a  
6 system's analog to digital (A/D) converter. Achieving a fine  
7 degree of Doppler compensation often requires a special external  
8 clock for control of the analog to digital converter. Although  
9 adjusting the sampling frequency to compensate for Doppler  
10 shifting may not introduce signal distortion, adding the external  
11 clock increases the cost and complexity of the systems' hardware  
12 and software.

#### 13 14 SUMMARY OF THE INVENTION

15 Accordingly, one object of the present invention is to  
16 provide a signal shift compensation system and method using  
17 downsampling by way of non-integer decimation involving less  
18 mathematical complexity than existing systems and methods.

19 Another object of the present invention is to provide a  
20 signal shift compensation system and method that is effective for  
21 many applications without requiring significant additions of  
22 hardware or software.

23 A further object of the present invention is to provide a  
24 signal shift compensation system and method that causes less  
25 signal distortion than existing interpolation-based Doppler  
26 correction techniques.

1           According to the present invention, a fixed sampling rate is  
2 used to oversample a shifted signal and the oversampled sequence  
3 is downsampled using non-integer decimation to remove the shift  
4 from the sampled sequence of the shifted signal. The present  
5 invention features a signal shift compensation system and method,  
6 for compensating at least one shifted signal transmitted in a  
7 medium from a signal source and received by a signal receiver.  
8 The signal shift compensation system includes a signal sampler,  
9 responsive to an oversampling factor value, for determining a  
10 fixed oversampling rate based upon the oversampling factor value.  
11 The signal sampler is also responsive to the shifted signal, for  
12 oversampling the shifted signal at the fixed oversampling rate  
13 and for providing an oversampled shifted signal digital value  
14 sequence including a number of digital shifted signal sample  
15 values.

16           The signal shift compensation system also includes a  
17 compensation downsampler, responsive to a signal shift estimate  
18 (e.g., Doppler estimate) value and to the oversampling factor  
19 value, for determining a downsampling factor value. The  
20 compensation downsampler is also responsive to the oversampled  
21 shifted signal digital value sequence and the determined  
22 downsampling factor value, for decimating the oversampled shifted  
23 signal digital value sequence by the determined downsampling  
24 factor value to provide a decimated, corrected (or unshifted)  
25 signal sequence. The decimated, corrected signal sequence  
26 includes a plurality of signal samples. Each signal sample in the  
27 decimated, corrected signal sequence is exactly equal to a

1 determined one of the signal sample values from the oversampled  
2 shifted signal digital value sequence.

3       The determined one of the oversampled shifted signal sample  
4 values is determined by multiplying a decimated sequence index  
5 value by the determined downsampling factor value to obtain an  
6 index value in the oversampled shifted signal digital value  
7 sequence. In the preferred embodiment, the determined one of the  
8 oversampled shifted sequence is the sample whose index value is  
9 closest to the value of the decimated sequence index multiplied  
10 by the downsampling factor.

11       In one preferred embodiment, the signal shift is a Doppler  
12 shifted signal. The fixed oversampling rate is the Nyquist  
13 sampling rate multiplied by the oversampling factor value. The  
14 decimation downsampling rate value is determined from the  
15 oversampling factor value divided by a Doppler multiplier based  
16 on the signal shift estimate value. According to one embodiment,  
17 the system also includes a device for determining the signal  
18 shift estimate value and the Doppler multiplier based upon a  
19 predetermined reference signal transmitted with the Doppler  
20 shifted signal.

21       The method of compensating at least one shifted signal  
22 according to the present invention comprises the steps of:  
23 oversampling the shifted signal at a fixed oversampling rate  
24 based on an oversampling factor value to establish an oversampled  
25 shifted signal digital value sequence having a number of digital  
26 shifted signal sample values; and decimating the oversampled  
27 shifted signal digital value sequence by a downsampling factor

1 value to establish a decimated, corrected (unshifted) digital  
2 value sequence including a number of decimated signal samples.  
3 The value of any one of the decimated signal samples is equal to  
4 a determined one of the digital shifted signal sample values of  
5 the oversampled shifted signal digital value sequence.

6 According the preferred method, the step of oversampling the  
7 shifted signal includes oversampling the shifted signal at a  
8 fixed oversampling rate that is equivalent to the Nyquist  
9 sampling rate multiplied by the oversampling factor value. The  
10 step of decimating the oversampled shifted signal digital value  
11 sequence includes determining the downsampling factor value  
12 according to the oversampling factor value and signal shift  
13 estimate value.

14 According to the preferred method, the step of decimating  
15 the oversampled shifted signal digital value sequence includes  
16 the steps of initializing a decimated sequence index of the  
17 number of decimated signal samples in the decimated, corrected  
18 digital value sequence; determining a corresponding sequence  
19 index of a corresponding digital shifted signal sample value in  
20 the oversampled shifted signal digital value sequence; and  
21 assigning to each decimated corrected signal sample, a value of  
22 each corresponding digital shifted signal sample. The  
23 corresponding sequence index of the corresponding digital shifted  
24 signal sample value is determined for each decimated signal  
25 sample by multiplying the decimated sequence index of the  
26 decimated signal sample by the downsampling factor value.







1 shifted analog signal 20 received by the signal receiver 14,  
2 according to the fixed oversampling rate. The fixed oversampling  
3 rate is preferably determined by multiplying a typical sampling  
4 rate by the oversampling/decimation factor ( $N$ ). In one example,  
5 the typical sampling rate is the Nyquist rate (e.g., 5 KHz for  
6 the examples shown in FIGS. 2 and 3) and the oversampling/  
7 decimation factor ( $N$ ) is 10. However, the present invention  
8 contemplates multiplying any sampling rate by any oversampling/  
9 decimation factor ( $N$ ) to determine the fixed oversampling rate.

10 The power and information in the shifted analog signal 20 is  
11 contained within a number of digitized samples in an oversampled  
12 sequence. The number of digitized samples in the oversampled  
13 sequence depends on the fixed oversampling rate. The signal  
14 shift compensation system 10 further includes a compensation  
15 downsampler 18, responsive to the signal sampler 16, to  
16 compensate for or remove the signal shift by downsampling the  
17 oversampled sequence using a downsampling factor based on the  
18 oversampling/decimation factor ( $N$ ) and a previously estimated  
19 signal shift, as will be described in greater detail below. The  
20 signal shift compensation system 10 can also include a signal  
21 shift estimator 19, for estimating and providing the estimated  
22 signal shift, such as an estimated Doppler shift, to the  
23 compensation downsampler 18.

24 The signal shift compensation system 10 and method according  
25 to the exemplary embodiment of the present invention is used to  
26 compensate for the Doppler shift in a signal, such as an acoustic  
27 signal, transmitted through a medium such as water. The Doppler

1 effect causes Doppler shifting to occur in a signal when either  
2 the signal source 12 or signal receiver 14, or both, are moving  
3 through the medium. A Doppler shifted signal undergoes both a  
4 change in signal spectrum and a compression or expansion in time,  
5 FIGs 2A - 2D. If  $f_o$  is the original frequency of a signal, the  
6 Doppler shifted frequency,  $f_d$  is given by

$$7 \quad f_d = f_o(1-v/c) \quad (1)$$

8 where  $v$  = radial component of the signal source's velocity away  
9 from the receiver, and  $c$  = speed of sound in the given medium.  
10 Correspondingly, if  $T_o$  is the original duration of the signal,  
11 the duration of the signal,  $T_d$  after Doppler compression or  
12 expansion is given by

$$13 \quad T_d = T_o / (1-v/c). \quad (2)$$

14 The term,  $(1-v/c)$ , will be referred to as the Doppler multiplier,  
15  $D$ , wherein  $v/c$  equals the previously estimated signal (or Doppler)  
16 shift.

17 For example, assume that a 1 second long signal with a  
18 2.5KHz wide spectrum undergoes a +0.1% Doppler shift, i.e.  
19 Doppler multiplier,  $D = 1.001$ , FIGs 2A and 2C. In this example,  
20 the resulting Doppler shifted signal will have a bandwidth of  
21 2502.5 Hz and a compressed signal duration of 0.999 seconds long,  
22 FIGs 2B and 2D. The signal shift compensation system and method  
23 10, according to the present invention, compensates for this  
24 translation in spectrum and the compression or expansion in time  
25 of a Doppler shifted signal.

1           If the original signal of 1 second duration was sampled at  
2 the Nyquist sampling rate of 5 KHz, the resulting sampled  
3 sequence would have 5,000 samples. That same original signal  
4 after a +0.1% Doppler shift ( $D = 1.001$ ) would have only 4,995  
5 samples when sampled at the Nyquist rate of 5 KHz. Thus, if the  
6 clock of the analog to digital (A/D) converter in the signal  
7 receiver 14 were adjusted such that the Doppler shifted signal  
8 were sampled at 5,005 Hz (as opposed to 5KHz), the sampled  
9 sequence of the Doppler shifted signal would also contain 5,000  
10 samples within the duration of the signal. One way of  
11 compensating for or removing the Doppler shift in a signal is by  
12 adjusting the clock and modifying the sampling rate according to  
13 the Doppler multiplier. According to the present invention, the  
14 fixed oversampling rate is used to oversample the Doppler shifted  
15 signal. The oversampled sequence is then downsampled using non-  
16 integer decimation to remove the Doppler shift from the sampled  
17 sequence of the Doppler shifted signal.

18           An exemplary Doppler shifted signal wave form 20a, FIG 3A,  
19 illustrates a Doppler compressed time duration  $T_d$  when compared  
20 to the duration  $T_o$  of the original signal wave form 20b. The  
21 original signal wave form 20b represents the original signal as  
22 it originated from the signal source whereas the Doppler shifted  
23 wave form 20a represents the Doppler shifted signal as it is  
24 received at the signal receiver. According to the signal shift  
25 compensation method of the present invention, the Doppler shift  
26 is removed from the Doppler shifted signal 20a by oversampling  
27 and downsampling the Doppler shifted signal 20a using the

1 downsampling factor based upon the oversampling factor ( $N$ ) and  
2 the estimated Doppler shift ( $v/c$ ).

3 The Doppler shifted signal is oversampled at the fixed  
4 sampling rate to form an oversampled shifted signal digital value  
5 sequence 24, FIG 3B. The oversampled shifted signal digital  
6 value sequence 24 includes a number of digital shifted signal  
7 sample values 25 representing the Doppler shifted signal 20a in  
8 digital form.

9 According to the example above, the 1 second original or  
10 unaffected signal would contain 50,000 samples if sampled at a  
11 fixed oversampling rate of 50 KHz (e.g., the Nyquist rate of 5  
12 KHz multiplied by an oversampling factor of 10). As a result of  
13 the +0.1% Doppler shift ( $D = 1.001$ ), the oversampled Doppler  
14 shifted signal contains 49,950 samples when sampled at the fixed  
15 sampling rate of 50 KHz. As a result of the Doppler shift, the  
16 number of digital shifted signal samples 25 in the oversampled  
17 shifted signal digital value sequence 24 of the Doppler shifted  
18 signal 20a is either greater or less than the number of samples  
19 that would be present in a sampled sequence of the original  
20 signal (i.e., unaffected by a signal shifting) at the same  
21 sampling rate.

22 By decimating the oversampled shifted signal digital value  
23 sequence 24 of the Doppler shifted signal by the downsampling  
24 factor,  $F$ , based on the Doppler multiplier,  $D$ , and the  
25 oversampling factor,  $N$ , (e.g., 10), a corrected decimated signal  
26 sequence 26, FIG 3C, having a desired number of decimated shifted  
27 signal samples 27 (e.g., 5,000 samples) is established. The

1 downsampling factor,  $F$ , is determining according to the following  
2 equation:

$$3 \quad F = N(1 - v/c). \quad (3)$$

4 For example, if the sampling rate is 50 KHz (or 10 times the  
5 Nyquist rate of 5 KHz) and the Doppler multiplier  $D$  is 1.001, the  
6 resulting downsampling factor  $F$  is 9.99, i.e.,  $F = 10/D$ . The  
7 number of decimated signal samples 27 in the corrected decimated  
8 signal sequence 26 is equal to the number of digital sample  
9 values 25 in the oversampled shifted signal digital value  
10 sequence 24 divided by the downsampling factor  $F$ , e.g., 9.99.

11 The fixed oversampling rate is preferably determined based  
12 upon the desired outcome of the decimated signal sequence. For  
13 example, to arrive at a corrected decimated signal sequence 26  
14 having the same number of samples as would the original,  
15 unaffected signal if the original signal were sampled at the  
16 Nyquist rate of 5 KHz, the oversampling is performed at a fixed  
17 oversampling rate that is equivalent the Nyquist rate multiplied  
18 by the oversampling factor  $N$ . By decimating using a downsampling  
19 factor ( $F$ ) equal to the oversampling factor ( $N$ ) divided by the  
20 Doppler multiplier ( $D$ ), the resulting decimated signal sequence  
21 has the same number of samples as would the original, unaffected  
22 signal if sampled at the Nyquist rate.

23 Each sample 27 in the corrected decimated signal sequence 26  
24 is assigned a value of a corresponding sample 25 in the  
25 oversampled shifted signal digital value sequence 24. The  
26 decimated signal sequence 26 compensates for the Doppler shifting

1 by using the most evenly spaced samples within the oversampled  
2 shifted signal digital value sequence 24, e.g., the most evenly  
3 spaced 5,000 samples within the 49,950 samples of the oversampled  
4 sequence according to the above example.

5 One way of determining the corresponding sample 25 in the  
6 oversampled sequence 24 for each decimated sample 27 having an  
7 index value (or sequence number) in the decimated sequence 26, is  
8 by multiplying the decimated sequence index value of the  
9 decimated sample 27 by the down sampling factor,  $F$ , to determine  
10 a corresponding fractional index in the oversampled sequence 24  
11 and using the value of the sample 25 in the oversampled sequence  
12 24 having an index nearest to the corresponding fractional index.  
13 For example, the fifth entry in the decimated sequence 26 (i.e.,  
14 index = 5) would correspond to the 50th sample in the oversampled  
15 shifted signal digital value sequence 24 (corresponding  
16 fractional index =  $5 \times 9.99 = 49.95$ ). Similarly, the 100th entry  
17 in the decimated sequence 26 would use sample 999 from the  
18 oversampled sequence 24, ( $100 \times 9.99$ ) and the 5,000th sample in  
19 the Doppler compensated sequence 26 would be given the value of  
20 sample 49,950 from the oversampled shifted signal sequence 24  
21 ( $5000 \times 9.99$ ).

22 The signal shift compensation method 100, FIG. 4, includes  
23 providing an estimated signal shift, such as an estimated Doppler  
24 shift ( $v/c$ ), step 104, for example, using a known reference  
25 signal and discrete Fourier analysis methods known to those  
26 skilled in the art. The oversampling/decimation factor ( $N$ ) is  
27 also provided, step 108, and preferably depends on the

1 capabilities of the system and the desired accuracy of the  
2 compensation. The fixed oversampling rate is then computed by  
3 multiplying the oversampling/decimation factor ( $N$ ) by a typical  
4 sampling rate, such as the Nyquist rate, step 112. The shifted  
5 signal is oversampled using the fixed oversampling rate, step  
6 116, and in step 120 an oversampled digital value sequence having  
7 a number of samples based upon the fixed oversampling rate and  
8 the duration of the signal is generated. The downsampling factor  
9  $F$  is determined, step 124, by dividing the oversampling/  
10 decimation factor ( $N$ ) by the Doppler multiplier ( $D$ ). The  
11 oversampled digital value sequence is then decimated using the  
12 downsampling factor ( $F$ ), step 130, to generate a decimated  
13 sequence having a number of samples corresponding to selected  
14 samples in the oversampled digital value sequence.

15 In one example, the decimation process 130, FIG. 5, begins  
16 by determining the number of samples ( $S$ ) that are in the  
17 oversampled digital value sequence, step 134. Next, the maximum  
18 number of samples ( $MaxS$ ) that would be in an unaffected signal  
19 oversampled sequence are determined, step 138, for example, the  
20 number of samples if the original signal not affected by the  
21 Doppler shift were sampled at the fixed oversampling rate (e.g.,  
22  $S(1-v/c)$ ). A decimated sequence index counter is initialized  
23 ( $DecI=1$ ), step 140, and the decimation of the oversampled digital  
24 value sequence is begun, step 150.

25 The decimation process steps through the oversampled  
26 sequence samples according to the oversampling factor ( $N$ ) and  
27 assigns values of corresponding samples in the oversampled



1 sequence to each sample in the decimated sequence. For each  
2 sample in the decimated sequence, the corresponding sample in the  
3 oversampled sequence is determined by dividing the oversampled  
4 sequence index by the Doppler multiplier  $D$  and rounding to find  
5 the nearest sample in the oversampled sequence, step 160. The  
6 value of the corresponding sample in the oversampled sequence is  
7 then assigned to the decimated sequence sample, step 170, and the  
8 decimated sequence index counter is incremented, step 180.

9       The decimation process continues to determine a  
10 corresponding sample in the oversampled sequence for each sample  
11 in the decimated sequence and assigning the value of that sample  
12 in the oversampled sequence to the sample in the decimated  
13 sequence until decimation of the oversampled sequence is  
14 completed, step 190, and the decimation process ends, step 200.

15       One way of implementing the signal shift compensation system  
16 and method according to the present invention is in the form of  
17 software. In one example, the psuedo code for the decimation  
18 process used to compensate for Doppler shift would appear as  
19 shown in Table 1.

1

TABLE 1

```

/* Let over_smpl_Dop be the oversample Doppler shifted signal and
/* let dec_sec be the resultant Doppler compensated decimated sequence
max_sample = 50000; /* max. number of samples in original, un-Doppler
                    /* shifted signal
decimate = 10;      /* desired oversampling factor
D = 1.001;         /* Doppler multiplier
dec_Dop_indx = 1; /* initialize index for decimated Doppler sequence
for orig_indx = 1: decimate: max_sample
    near_smpl = round (orig_indx/D); /* find index of nearest sample in the
                                    /* oversampled Doppler shifted signal
    dec_seq (dec_Dop_indx) = over_smpl_Dop(near_smpl); /* assign value of
                                                        /* nearest sample to
                                                        /* decimated sequence

    dec_Dop_indx = dec_Dop_indx + 1;
end;

```

2

3       The signal shift compensation system and method according to  
4 the present invention, preferably uses a fixed oversampling rate  
5 that is much greater than the sampling rate that would be used if  
6 sampling a non-Doppler affected signal. For example, if the  
7 Nyquist rate would typically be used to sample the signal, the  
8 decimated sequence should be equivalent to the original sequence  
9 sampled at the Nyquist rate and the oversampling should be at a  
10 fixed oversampling rate which is a multiple of the Nyquist rate.  
11 At greater fixed sampling rates, the adjacent samples in the  
12 oversampled sequence will be closer in value, and the  
13 corresponding values assigned to the samples in the decimated  
14 sequence will be a better approximation of the actual value at

1 the fractional index. The oversampling factor used in the  
2 examples described herein is a factor of 10 but the present  
3 invention contemplates other possible ratios depending on the  
4 required accuracy of the application.

5       Accordingly, the present invention provides a signal shift  
6 compensating system and method which is relatively low in  
7 mathematical complexity. The signal shift compensating system  
8 and method using non-integer decimation also results in signal  
9 shift compensation with less signal distortion than existing  
10 Doppler compensating techniques. The signal shift compensating  
11 system and method can also be easily implemented in many  
12 applications without requiring significant additional hardware  
13 and/or software.

14       Many modifications of the presently disclosed invention will  
15 become apparent to those of skill in the art

16

2

3 SYSTEM AND METHOD FOR COMPENSATING FOR DOPPLER SHIFTS

4 IN SIGNALS BY DOWNSAMPLING

5

6 ABSTRACT OF THE INVENTION

7 A signal shift compensation system and method compensates  
8 for a shift in a signal, such as a Doppler shift in an acoustic  
9 signal. The system includes a signal sampler for oversampling  
10 the shifted signal at a fixed oversampling rate to establish an  
11 oversampled shifted signal digital value sequence. The fixed  
12 sampling rate is greater than the typical sampling rate, such as  
13 the Nyquist rate, of the signals by an oversampling factor. The  
14 system further includes a compensation downsampler for decimating  
15 the oversampled Doppler shifted signal according to a  
16 downsampling factor to establish a decimated digital value  
17 sequence. The downsampling factor is determined according to the  
18 oversampling factor by which the signal is oversampled and an  
19 estimate of the (Doppler) shift value. In one example, the  
20 downsampling factor is equal to the oversampling factor divided  
21 by a Doppler multiplier reflecting the Doppler shift. Each  
22 sample in the decimated sequence is given the value of a  
23 corresponding sample in the oversampled sequence. Decimation  
24 according to the downsampling factor results in a decimated  
25 sequence that closely approximates the original unshifted signal.

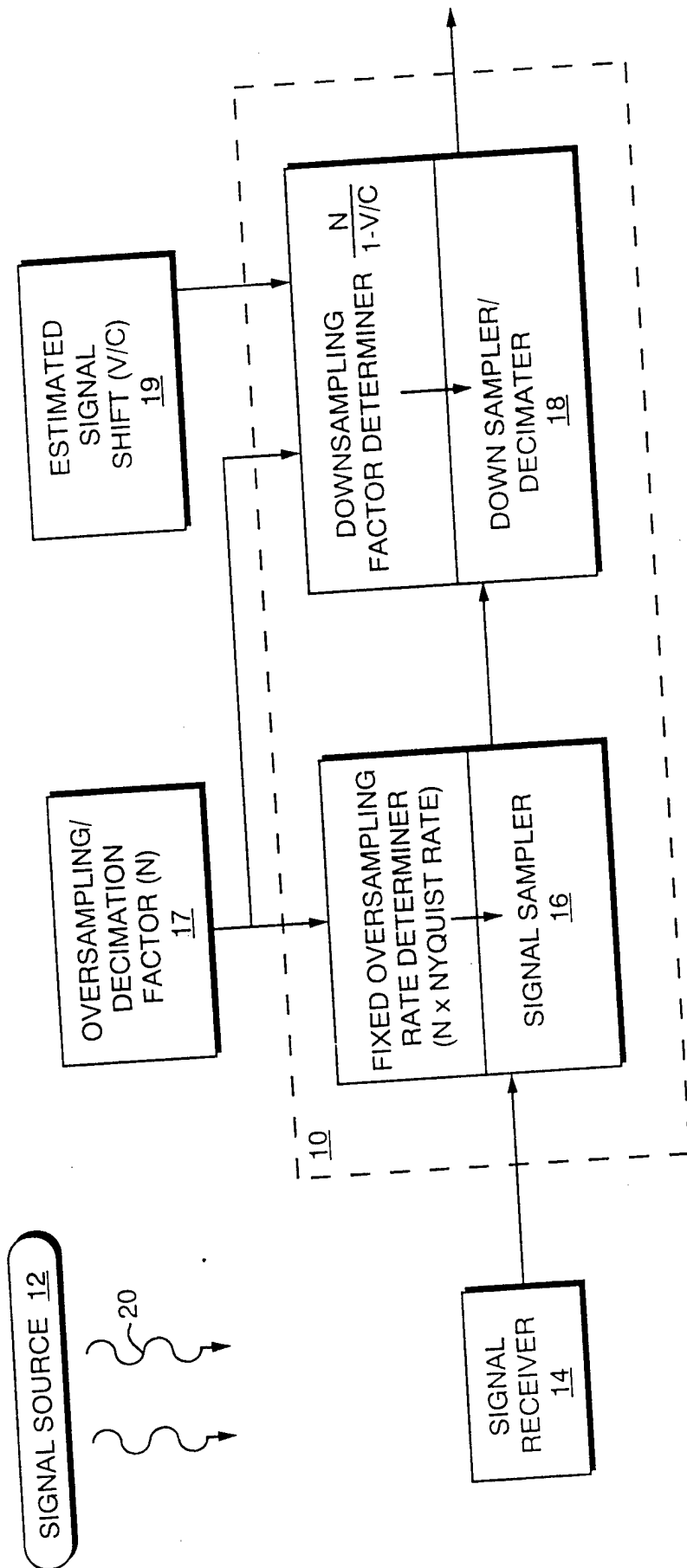


FIG. 1

ORIGINAL SIGNAL SPECTRUM

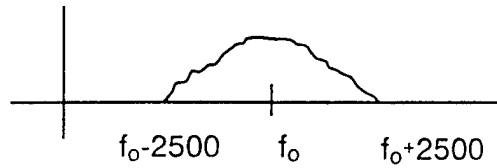


FIG. 2A

SPECTRUM—0.1% DOPPLER SHIFT

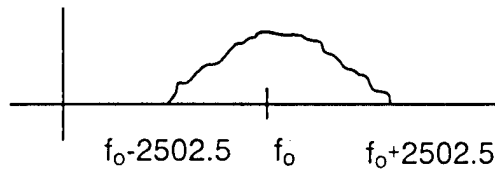


FIG. 2B

ORIGINAL TIME SERIES

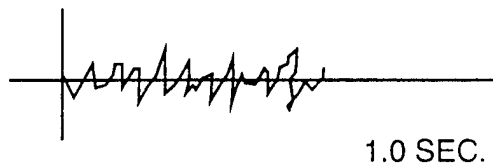


FIG. 2C

TIME SERIES—0.1% DOPPLER

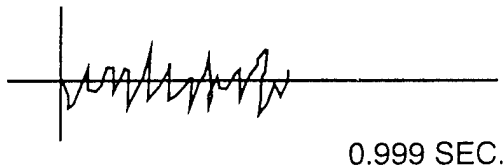


FIG. 2D

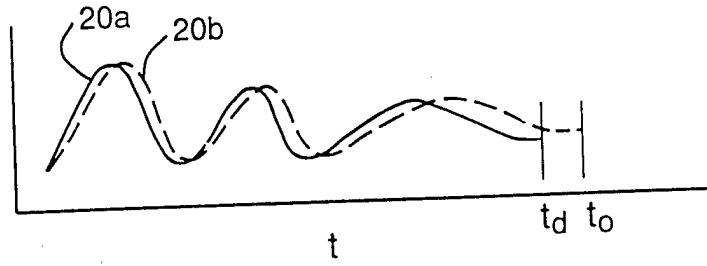


FIG. 3A

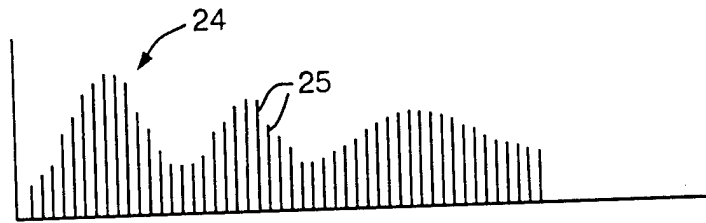


FIG. 3B

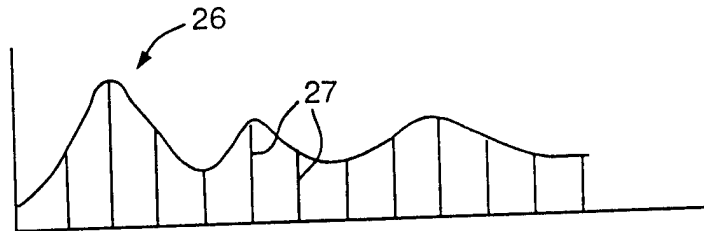


FIG. 3C

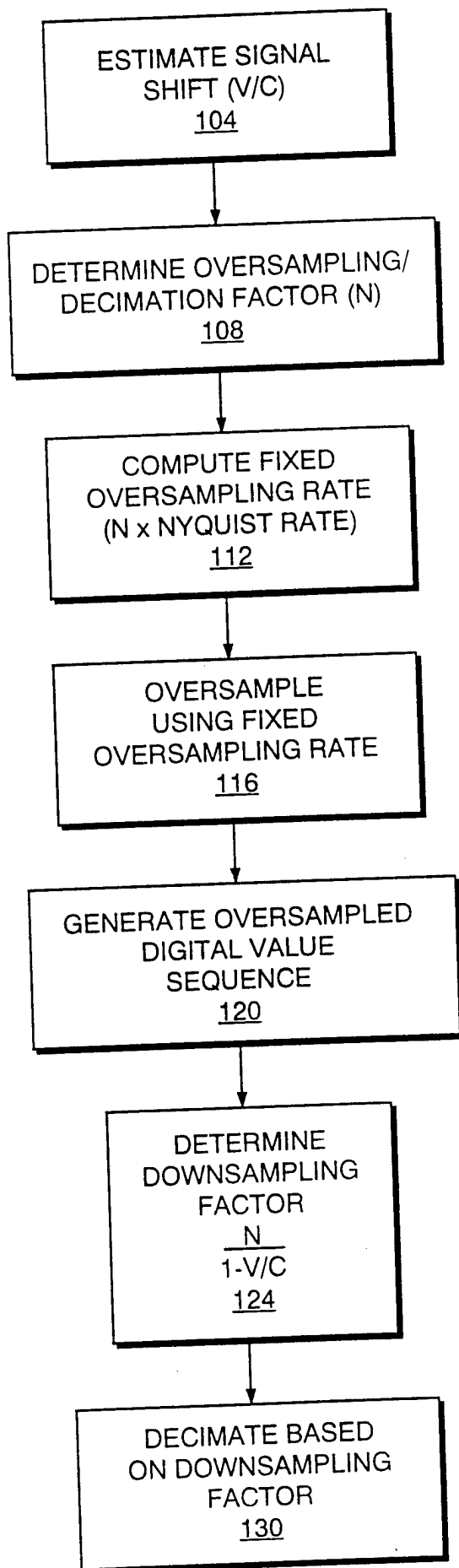


FIG. 4



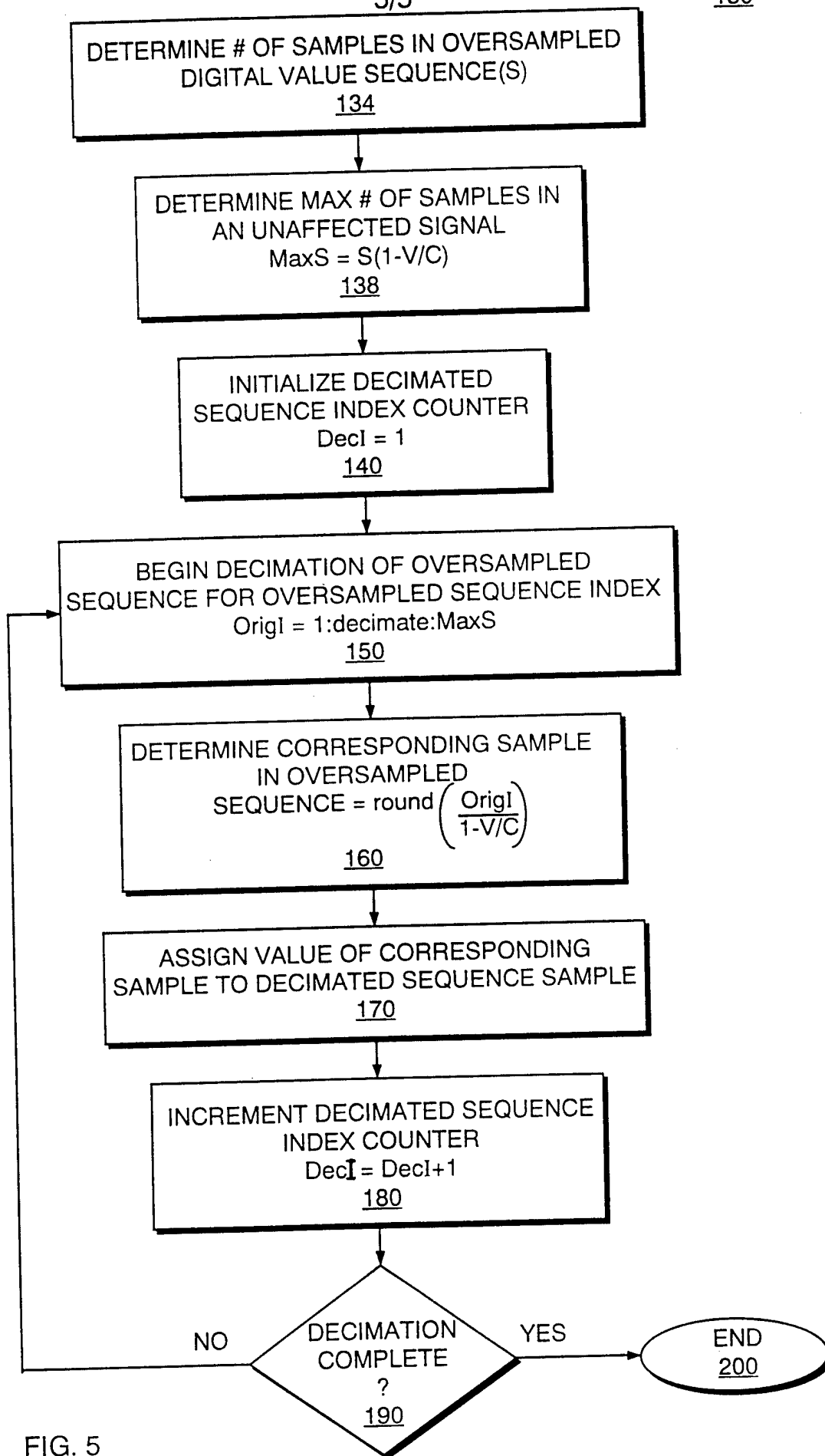


FIG. 5