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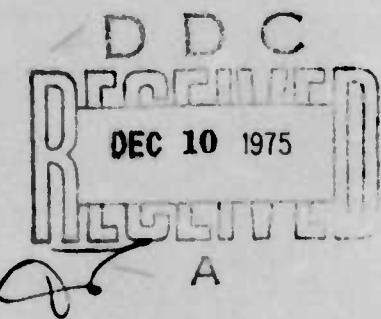
AFFDL-TR-75-103

**COMPUTER PROGRAMS FOR CALCULATING
SMALL DISTURBANCE TRANSONIC FLOWS
ABOUT OSCILLATING PLANAR WINGS**

SCIENCE APPLICATIONS, INCORPORATED

AUGUST 1975

TECHNICAL REPORT AFFDL-TR-75-103
REPORT FOR PERIOD JULY 1974 - AUGUST 1975



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problems for the components. The governing equation for the steady perturbation potential is the usual nonlinear transonic potential equation and it is solved in computer program TDSTRN using the mixed differencing relaxation procedure of Murman and Cole. The governing equation for the unsteady perturbation potential is linear and, for the harmonic boundary disturbance considered, of mixed elliptic hyperbolic type depending on the local nature of the steady potential. Using a steady solution previously generated by TDSTRN computer program TDUTRN solves the unsteady potential equation by the same relaxation procedure. The solution procedures are found to be quite efficient, permitting the calculation of unsteady aerodynamic forces to engineering accuracy in a few minutes on a CDC 6600 computer.

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FOREWORD

This computer program User's Manual was prepared by the Los Angeles Division of Science Applications, Incorporated, for the Vehicle Dynamics Division of the Air Force Flight Dynamics Laboratory, Wright-Patterson Air Force Base, Ohio. The computer programs were developed under Project 1370, "Dynamic Problems in Flight Vehicles", Task 137004, "Design Analysis", Contract F33615-74-C-3094. James J. Olsen and later Lt. William L. Holman (AFFDL/FYS) were the Air Force Task Engineers.

R. M. Traci was the principal investigator for the study and J. L. Farr, Jr., developed the computer programs described in this report. Consultant E. D. Albano contributed to the development and implementation of the numerical method.

The authors submitted this report in July 1975 for publication as an AFFDL technical report.

Other reports prepared and submitted under the aforementioned contract are: AFFDL-TR-74-37, "Small Disturbance Transonic Flows about Oscillating Airfoils," AFFDL-TR-74-135, "Computer Programs for Calculating Small Disturbance Transonic Flows about Oscillating Airfoils," AFFDL-TR-75-100, "Small Disturbance Transonic Flows about Oscillating Airfoils and Planar Wings."

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1.0 INTRODUCTION

Computer programs TDSTRN and TDUTRN implement a small disturbance potential flow theory for three-dimensional unsteady transonic flow about thin planar wings undergoing harmonic oscillation. The theory is based on the fact that a linear system can be obtained by considering the unsteady flow as a small perturbation to the non-uniform mean flow. The perturbation expansion approach has recently been developed with different emphasis in independent studies by the present authors^{1,2,3} and Ehlers⁴. Detailed descriptions of the theory and numerical solution method used in the three-dimensional version of the programs, documented in the users manual, are presented in References 1-3. The method is a generalization of that described for two-dimensional airfoils in Reference 1 and of the 2-D computer programs documented in Reference 2. The final report of the present phase of research¹ describes the generalization and presents some illustrative results.

In the perturbation expansion approach used, the perturbation potential function is expanded in a series of increasing powers of a small parameter which is a measure of the amplitude of an unsteady disturbance to the boundary. The resulting expansion of the unsteady potential equation results in a sequence of partial differential equations for the perturbation potentials. The zeroth order equation is the usual nonlinear steady transonic potential equation of mixed elliptic/hyperbolic type and is solved in TDSTRN using the mixed differencing, relaxation procedure of Murman and Cole⁵. The first order unsteady potential equation is linear and for harmonic boundary disturbances is also of the mixed elliptic/hyperbolic type, depending upon the steady solution. It is solved in TDUTRN using the same numerical technique as used in TDSTRN.

The theory and practice of the computer program operation are discussed in the following sections. The small perturbation theory and numerical solution procedure are summarized in Sections 2.0 and 3.0, respectively. A description of the program's logical operation and a brief subroutine description are given in Section 4.0. Section 5.0 presents a complete description of the program input, with suggested values for various control variables, and the program output. Section 6.0 describes the program usage and includes suggestions for making effective use of the programs. Sample cases which exercise all program options are presented in Section 7.0 with a complete specification of all input and sample output. Finally, complete FORTRAN listings of TDSTRN and TDUTRN are presented in the appendices.

2.0

SMALL PERTURBATION THEORY FOR UNSTEADY TRANSONIC FLOW

Small disturbance theory is the principal analytical tool for all speed ranges and has become increasingly important in the transonic speed range in recent years. The general theory including the unsteady small perturbation approach used in this work is summarized in this section. The required numerical solution methods for the steady and unsteady systems are described in Section 3.0. It is noted that, following usual programming practice, the FORTRAN variables used in TDSTRN and TDUTRN are descriptive of the physical variables.

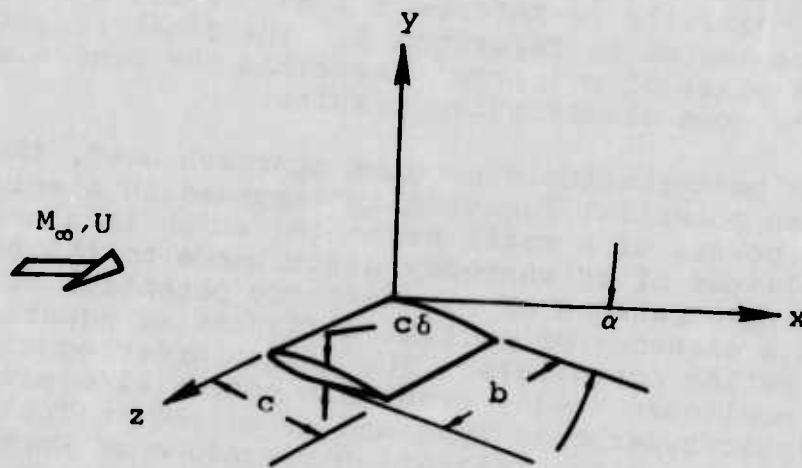


FIGURE 1. SCHEMATIC OF THREE-DIMENSIONAL PLANAR WING

The problem of interest is the flow about an airfoil (two-dimensional) or planar wing (three-dimensional) oscillating with various flexible or rigid body degrees of freedom in the transonic speed range. The airfoil geometry, flow-field schematic and coordinate definition are given in Figure 1 above. Rectangular coordinates (x, y, z) are fixed to the airfoil leading edge with origin at the wing root and U, M_∞ , a are the freestream velocity, Mach number and sound speed respectively. The airfoil has a thickness ratio δ , which is the airfoil maximum thickness divided by its chord c , and angle of attack α and a semi-span b (ZSPAN). The assumption is made that $\delta \ll 1$ and α is of the same order of magnitude as δ .

Also, the oscillatory motion of the airfoil is assumed to be described by a small non-dimensional displacement $\epsilon \ll \delta$ and a reduced frequency $k = \omega c/U$ based on airfoil chord where ω is the frequency of oscillation.

Assuming inviscid, isentropic flow, the problem can be reduced to the solution of a single equation for a velocity potential plus the tangency boundary condition on the airfoil surface. As is well known, the derivation of a small disturbance theory for transonic flows requires a singular perturbation approach. The following scaling is thereby introduced:

$$\begin{aligned}\tilde{x} &= \frac{x}{c}, \quad \tilde{y} = [(1+\gamma)\delta M_\infty^2]^{1/3} \frac{y}{c} \quad \tilde{z} = [(1+\gamma)\delta M_\infty^2]^{1/3} \frac{z}{c} \\ \tilde{t} &= \frac{[(1+\gamma)\delta M_\infty^2]^{2/3}}{M_\infty^2} \frac{U}{c} t\end{aligned}\quad (1)$$

and the total potential is expanded about the uniform flow:

$$\psi = U c \tilde{x} + \frac{\delta^{2/3} U c}{[(1+\gamma)M_\infty^2]^{1/3}} \tilde{\phi}(\tilde{x}, \tilde{y}, \tilde{z}, \tilde{t}) + \dots \quad (2)$$

Retaining all terms of leading order in to total potential equation and boundary conditions results in the following form for the unsteady small disturbance system.

$$(K - \tilde{\phi}_{xx}^2) \tilde{\phi}_{xx}'' + \tilde{\phi}_{yy}'' + \tilde{\phi}_{zz}'' = 2 \tilde{\phi}_{xt}'' + \frac{k}{\Omega} \tilde{\phi}_{tt}'' \quad (3)$$

where the transonic similarity parameters are:

$$K = \frac{(1-M_\infty^2)}{[(1+\gamma)\delta M_\infty^2]^{2/3}} \quad \Omega = \frac{M_\infty^2}{[(1+\gamma)\delta M_\infty^2]^{2/3}} k$$

with boundary conditions:

$$\tilde{\phi}_y = \left(\frac{\partial}{\partial \tilde{x}} + \underline{\frac{k}{\Omega} \frac{\partial}{\partial \tilde{t}}} \right) f_{u,l}(\tilde{x}, \tilde{z}, \tilde{t}) \quad (4)$$

on $y = \pm 0$ $\begin{cases} 0 \leq \tilde{x} \leq 1 \\ 0 \leq \tilde{z} \leq b \end{cases}$

$$\left[\tilde{\phi}_x + \underline{\frac{k}{\Omega} \tilde{\phi}_t} \right] = 0, \text{ on } \tilde{y}=0 \quad \begin{cases} \tilde{x} > 1 \\ 0 \leq \tilde{z} \leq b \end{cases} \quad (5)$$

$$\tilde{\phi}_x^2 + \tilde{\phi}_y^2 + \tilde{\phi}_z^2 \rightarrow 0 \text{ as } \tilde{x}^2 + \tilde{y}^2 + \tilde{z}^2 \rightarrow \infty \quad (6)$$

where $f_{u,l}$ is the unsteady airfoil shape function (Equation 7 below) on the upper and lower surfaces respectively, and where $[]$ denotes a jump in the enclosed quantity between $y=0^-$ and 0^+ . It is noted that the airfoil tangency boundary condition (Equation 4) and the Kutta condition (Equation 5) are applied in the small disturbance manner on $y=0$.

The system of Equations 3-6 provides a formulation of the unsteady airfoil problem in the non-linear domain, which includes flowfields with shocks. Certain terms in the above system are underlined as they may be omitted for a low frequency [$k^0(\delta^{2/3})$] approximation. The present version of TDUTRN includes the low frequency approximation ($IOPT=0$) or general frequency formulation ($IOPT=1$) and either can be used at the discretion of the user.

The approach presented herein for solving the non-linear system given above (Equations 3-6) is to expand the perturbation potential function in terms of the unsteady boundary disturbance $\epsilon \ll 1$. From this point on all tildas (\sim) will be

dropped with the understanding that all variables are scaled variables. Harmonic boundary disturbances are explicitly treated:

$$f(x, z, t) = f_0(x, z) + \epsilon f_\epsilon(x, z) e^{i\Omega t} \quad (7)$$

and the perturbation potential is expanded as follows:

$$\phi(x, y, z, t) = \phi^0(x, y, z) + \epsilon \phi^1(x, y, z) e^{i\Omega t} + \dots \quad (8)$$

Substituting this into the perturbation potential equation plus boundary conditions and combining terms results in the following pair of boundary value problems for ϕ^0 and ϕ^1 respectively. (In the following text, the superscript has been dropped from ϕ^1 .)

$$\begin{aligned} & (\kappa - \phi_x^0) \phi_{xx}^0 + \phi_{yy}^0 + \phi_{zz}^0 = 0 \\ & \phi_y^0 = f'_0(x, z), \quad \text{on } y = \pm 0 \quad \left\{ \begin{array}{l} 0 \leq x \leq 1 \\ 0 \leq z \leq b \end{array} \right. \\ & [\phi_x^0] = 0, \quad \text{on } y = 0 \quad \left\{ \begin{array}{l} x > 1 \\ 0 < z < b \end{array} \right. \\ & (\phi_x^0)^2 + (\phi_y^0)^2 + (\phi_z^0)^2 \rightarrow 0 \quad \text{as } x^2 + y^2 + z^2 \rightarrow \infty \end{aligned} \quad \left. \right\} \quad (9)$$

and

$$\begin{aligned} & (\kappa - \phi_x^0) \phi_{xx}^0 + \phi_{yy}^0 + \phi_{zz}^0 - (\phi_{xx}^0 + 2i\Omega) \phi_x^0 + \underline{k\Omega\phi} = 0 \\ & \phi_y^0 = f'_\epsilon + ikf_\epsilon, \quad \text{on } y = \pm 0 \quad \left\{ \begin{array}{l} 0 \leq x \leq 1 \\ 0 \leq z \leq b \end{array} \right. \\ & [\phi_x^0 + \underline{ik\phi}] = 0, \quad \text{on } y = 0 \quad \left\{ \begin{array}{l} x > 1 \\ 0 \leq z \leq b \end{array} \right. \\ & (\phi_x^0)^2 + (\phi_y^0)^2 + (\phi_z^0)^2 \rightarrow 0, \quad \text{as } x^2 + y^2 + z^2 \rightarrow \infty \end{aligned} \quad \left. \right\} \quad (10)$$

System 9 is recognized as the usual formulation for steady transonic flow and system 10 is the formulation for the unsteady perturbation thereof. It is noted that the governing equation for ϕ is linear but of the same mixed elliptic/hyperbolic type as the steady solution. It is also noted that ϕ is in general complex thereby permitting phase shifts between field quantities and the boundary disturbance. As before, underlined terms in system 10 are neglected for a consistent low frequency approximation. Also for two dimensional airfoil sections, the z dependence on all quantities and the ϕ_{zz} terms in the equations are neglected.

The main physical quantities of interest are the pressure coefficient and airfoil force coefficients. The pressure coefficient, defined in the usual manner, is given by:

$$c_p = \frac{\delta^{2/3}}{[(1+\gamma)M_\infty^2]^{1/3}} (\bar{C}_p^0 + \epsilon \bar{C}_p e^{i\Omega t}) \quad (11)$$

where the steady and unsteady scaled pressure coefficients are given to leading order in the small disturbance approximation by:

$$\bar{C}_p^0 = -2\phi_x^0, \quad \bar{C}_p = -2(\phi_x + ik\phi) \quad (12)$$

The formulations of the boundary value problems are essentially complete with the exception of the practical matter of setting the boundary conditions away from the airfoil, which depends on the particular problem; subsonic or supersonic free field, wind tunnel wall etc. Asymptotic far field solutions to Equations 10 have been developed for two-dimensional subsonic or supersonic free air or wind tunnel flows and for three-dimensional subsonic flow. These solutions are described in the present three-dimensional subsonic free air version of the computer programs.

3.0 NUMERICAL SOLUTION METHOD

The numerical solution procedure for the boundary value problems for the steady and unsteady perturbation potential, is based on the mixed differencing, line relaxation procedure developed by Murman, Cole and Krupp^{5,6}. They pointed out the essential ingredient for the success of relaxation procedures for the steady transonic potential equation. The key to the approach is to account for the local nature of the flow (elliptic in subsonic regions, hyperbolic in supersonic regions) in the finite difference approximation to the governing equations. The solution method used in the present work for the steady perturbation potential, ϕ^0 , is patterned after the method for general lifting airfoils developed by Krupp⁶.

The application of the theory and solution method to two-dimensional airfoil sections presented in previous work are interesting and illustrative but for practical application to dynamics or flutter problems three-dimensional effects must be considered. As with most other effects, 3-D effects are more important at transonic speeds than in the other speed ranges. The efficiency of the present scheme is such that realistic three-dimensional computations are practical on modern computers and it is the purpose of this section to describe the generalization of the numerical solution procedure to permit 3-D calculations (Section 3.1).

The initial development of the method is restricted to rectangular planforms undergoing oscillations symmetric with respect to the wing root ($z = 0$). The small disturbance analysis and the unsteady perturbation theory valid for three-dimensional flows were described in Section 2. As indicated there, the generalization to three dimensions requires but the addition of the ϕ^{zz} term to the governing equations for the steady and unsteady perturbation potentials. Asymptotic solutions to the governing equations have been derived for lifting wings in subsonic free-stream flow by Klunker⁷, for the steady flow, and by the present authors for the unsteady perturbation. These solutions are summarized in Section 3.2 and used in the numerical solution method to fix farfield boundary conditions. Three dimensional solutions for steady transonic flow have been presented by Bailey and Steger⁸ and Newman and Klunker⁹; the latter work being most closely related to the method for steady flows used in this work. Extensions of the solution method for the unsteady perturbation parallel the steady method and these are now described.

3.1 Finite Difference Solution Method

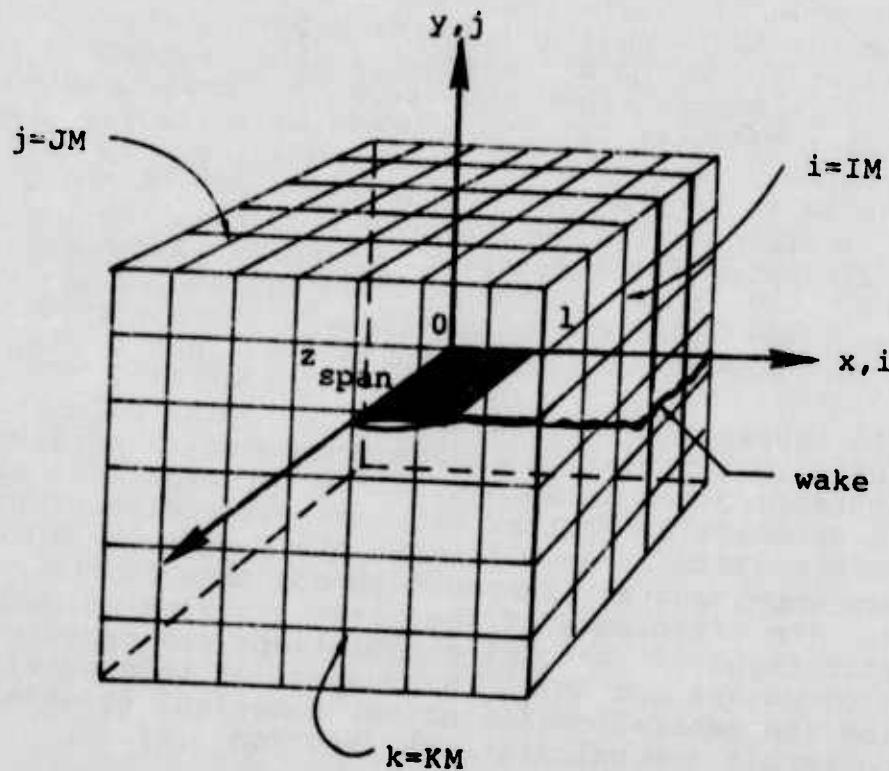


FIGURE 2. SCHEMATIC OF NUMERICAL SOLUTION DOMAIN

The three-dimensional numerical scheme constitutes the most straightforward extension of the two-dimensional method previously described in detail in Reference 1. As shown schematically in Figure 2, a cubic rectangular mesh of finite extent with uneven grid line spacing is overlayed on the 3-D solution space. The grid is concentrated near the airfoil and expanded out to the far boundaries of the grid. The finite difference equations are identical to the corresponding two-dimensional versions^{1,2} with the addition of a centered difference form for ϕ_{zz} given by:

$$\phi_{zz}^{ij,k} = \frac{2}{(\Delta z_k + \Delta z_{k-1})} \left\{ \frac{1}{\Delta z_k} (\phi_{i,j,k+1} - \phi_{i,j,k}) - \frac{1}{\Delta z_{k-1}} (\phi_{i,j,k} - \phi_{i,j,k-1}) \right\} \quad (13)$$

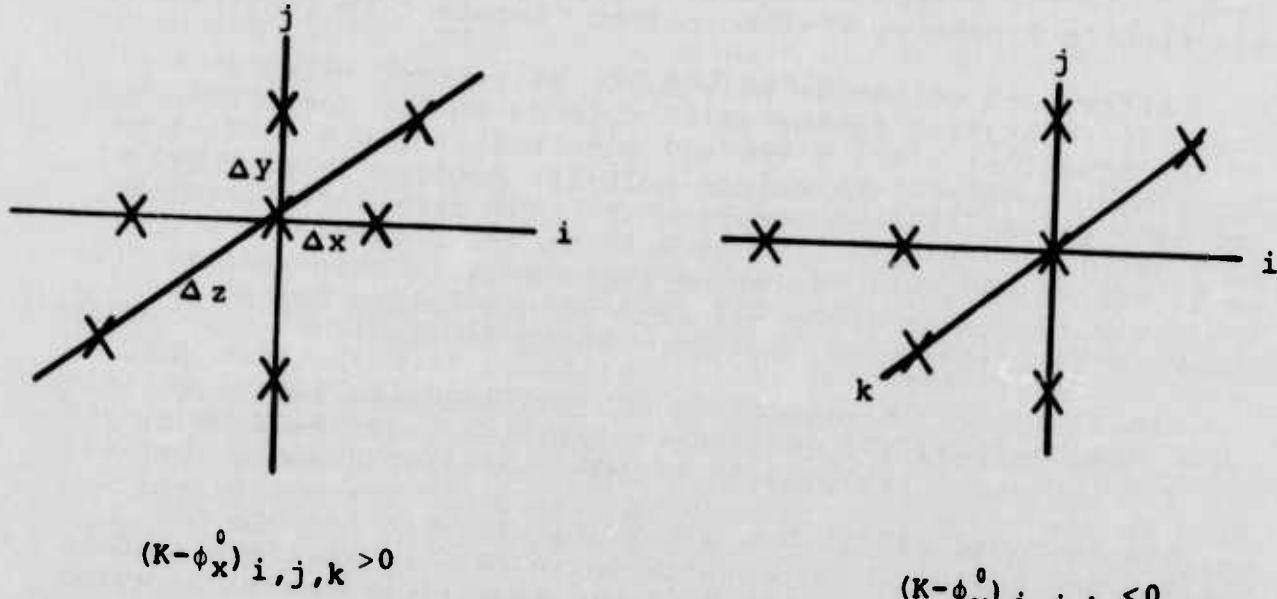


FIGURE 3. SCHEMATIC OF DIFFERENCE SCHEME

The computational star for the three-dimensional scheme is shown schematically in Figure 3 above. The tests for the elliptic or hyperbolic nature of the equation are made on the centered difference form of $(K - \phi^0)$, and depending on the value of this coefficient the x derivatives of ϕ are centered or backward differenced as in the 2-D case. A parabolic point operator is used in both the steady and unsteady schemes and a shock point operator is used in the finite difference scheme for the steady potential.

As before, the finite difference equations are set up for each column ($x, z = \text{constants}$) in turn, taking account of the airfoil, wake and farfield boundary conditions. In the steady solution this results in a set of quadratic equations for the column of ϕ 's which are solved by linearizing and

iterating. The linearization is accomplished by using the previous iterate for the coefficient $V = K - \phi^0$. The resulting linear system is tridiagonal and is solved by optimum Gaussian elimination. The column iteration process is terminated when the difference between successive iterates is less than an arbitrary small amount (usually 10^{-5}). As in the 2-D case, convergence is usually achieved in three or four iterations. In the unsteady solution it is recalled that the equation is linear so that no column iteration is required.

After each column is solved, it is relaxed using a variable relaxation factor which depends on the local nature of the equation; $\omega \sim 1.7$ for elliptic points and $\omega \sim .75$ for hyperbolic points. The column solution process is performed for each column in turn sweeping the grid from left to right in x and from the wing root ($k = 1$) to the farfield ($k = KM$) in z . The entire grid is swept repeatedly in this manner until the change in ϕ for all grid points during one grid sweep is less than some arbitrary small amount.

The numerical treatment of airfoil and wake boundary conditions in both steady and unsteady cases is the same as the 2-D case with the exception that the airfoil shape function is now a function of z as well as x and the airfoil circulation is a function of z along the airfoil. In the subsonic freestream case considered to date, asymptotic solutions for the steady and unsteady systems described in Section 3.2 are used to fix a Dirichlet boundary condition on five sides of the grid. On the grid boundary containing the wing root, a symmetry boundary condition is used whereby $\phi_z = 0$ on $z = 0$. The farfield solution depends on the spanwise distribution of circulation and as the solution for circulation is refined the farfield is updated periodically during the solution process.

The solution process summarized above has worked well in the few cases calculated to date. Convergence, for instance, seems to be comparable to the two-dimensional method as will be discussed in Section 6.0. It is reiterated that the details of the finite difference equations and wing, wake and farfield boundary conditions as well as details of the iteration procedures are identical in TDSTRN and TDUTRN as described previously for STRANS and UTRANS in Reference 2.

3.2 Steady and Unsteady Farfield Prescriptions

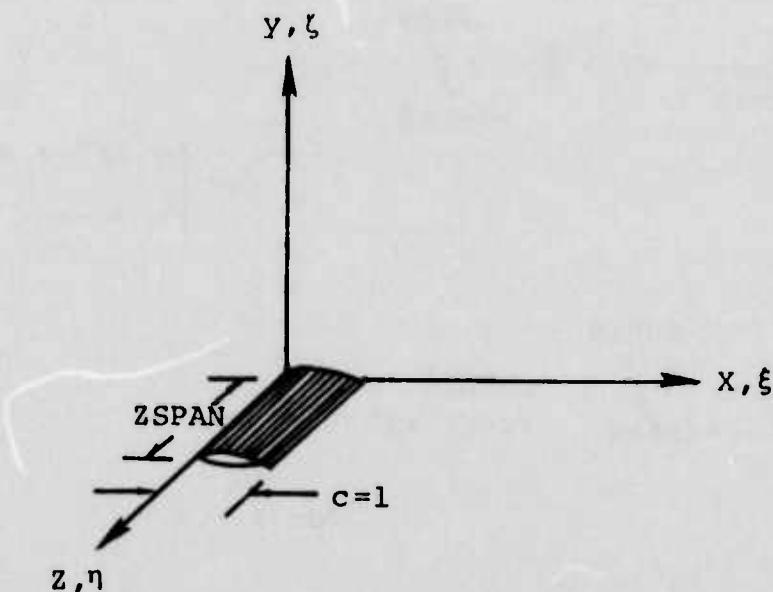


FIGURE 4. COORDINATE DEFINITION

The development of three-dimensional subsonic farfield approximations for the steady and unsteady perturbation potentials proceeds in the same manner as described in previous work for the two-dimensional flow. As before the method involves the approximation of various integrals over the wing and wake which result from the application of Green's theorem to the appropriate partial differential equation. Klunker⁷ has used the method to develop asymptotic solutions for the three-dimensional steady flow and his result in the following form is used:

$$\phi_{ff}^0(x, y, z) = -\frac{x}{2\pi R} \left\{ \int_{-ZSPAN}^{ZSPAN} \int_0^1 t(\xi, \eta) d\xi d\eta \right\}$$

$$+ \left\{ \begin{array}{l} \frac{y}{4\pi(y^2+z^2)} \left(1 + \frac{x}{R}\right) \int_{-ZSPAN}^{ZSPAN} \gamma(\eta) d\eta \\ \text{for } \begin{cases} y^2+z^2 \rightarrow \infty \\ x \rightarrow -\infty \end{cases} \\ \frac{y}{2\pi} \int_{-ZSPAN}^{ZSPAN} \frac{\gamma(\eta)}{(z-\eta)^2+y^2} d\eta \\ \text{for } x \rightarrow +\infty \end{array} \right. \quad (14)$$

where $R = [(x^2 + K(y^2 + z^2))]^{1/2}$, $t(\xi, \eta)$ is the wing thickness distribution and $\gamma(\eta)$ is the spanwise distribution of circulation.

The development of an asymptotic solution for the unsteady perturbation potential follows the method of Klunker and is now described in some detail. The field equation for the unsteady perturbation potential (Equation 10) is written as:

$$\begin{aligned} L[\phi] &\equiv K\phi_{xx} + \phi_{yy} + \phi_{zz} - 2i\Omega\phi_x + k\Omega\phi \\ &= (\phi_x^0 \phi_x)_x \end{aligned} \quad (15)$$

The application of Green's theorem to the linear operator L and the use of wing and wake boundary conditions and weak shock conditions results in the following integral equation for ϕ :

$$\phi(x, y, z) = \iint_{\text{wing}} \Delta\phi(\xi, \eta) \psi_\zeta d\xi d\eta + \int_{\text{SPAN}} \gamma(\eta) \int_1^\infty \psi_\zeta e^{-ik(\xi-1)} d\xi d\eta$$

wake integral

$$+ \iiint_{-\infty}^{\infty} (\phi_\xi^0 \phi_\xi^0) \psi_\zeta d\xi d\eta d\zeta$$

where ψ is the source solution to $L[\phi] = 0$:

$$\psi(x, y, z; \xi, \zeta, \eta) = \frac{1}{4\pi R} e^{i \left(\frac{\Omega}{K} (x - \xi) - \frac{\mu}{\sqrt{K}} R \right)} \quad (17)$$

where

$$\mu = \sqrt{\Omega \left(\frac{\Omega}{K} + k \right)}$$

$$R = \sqrt{(x - \xi)^2 + K [(y - \zeta)^2 + (z - \eta)^2]}$$

The use of the source function ψ in Equation 16, neglecting the volume integral as a higher order term, and after considerable manipulation and approximation (as $x^2 + y^2 + z^2 \rightarrow \infty$) of the various integrals results in the following farfield solution:

$$\phi_{ff}(x, y, z) = \frac{ky}{4} \frac{(1+i\sqrt{k} R)}{R^3} e^{i\left(\frac{\Omega}{k}x - \frac{\mu}{\sqrt{k}}R\right)} \int_{-ZSPAN}^{ZSPAN} \int_0^1 \Delta\phi(\xi, \eta) e^{-i\frac{\Omega}{k}\xi} d\xi d\eta$$

$$+ \frac{y}{4\pi} e^{-ik(x-1)} \cdot \begin{cases} \left[G_1(x, y, z; \eta) + G_2(x, y, z; \eta) \right] \int_{\eta=0}^{ZSPAN} \gamma(\eta) d\eta \\ -ZSPAN \end{cases} \\ \text{for } \begin{cases} y^2 + z^2 \rightarrow \infty \\ x \rightarrow -\infty \end{cases} \quad 13) \\ \left\{ \begin{array}{l} \int_{-ZSPAN}^{ZSPAN} \left[G_1(x, y, z; \eta) + G_2(x, y, z; \eta) \right] \gamma(\eta) d\eta \\ \text{for } x \rightarrow +\infty \end{array} \right.$$

where

$$G_1 = \frac{KM_\infty e^{-ikt_1}}{R(R-M_\infty(x-1))}$$

$$G_2 = \frac{I_1}{r^2}$$

and where

$$r = \sqrt{k[y^2 + (z-\eta)^2]}$$

$$R = \sqrt{(x-1)^2 + k[y^2 + (z-\eta)^2]}$$

$$t_1 = \frac{M_\infty R - (x-1)}{1 - M_\infty^2}$$

I_1 , in the equation, is an integral that can be evaluated using a rational approximation to its integrand and is presented at the end of the section.

It is noted that both the steady and unsteady farfield solutions involve integrals over the wing and span which depend on the solution $(\Delta\phi, \gamma)$. These integrals are evaluated numerically as the numerical solution proceeds and the respective equations are used to update the values of the steady or unsteady potential on the farfield boundaries.

The use of a rational approximation to evaluate the portion of the wake integral given as I_1 , above, results in the following function:

$$I_1 = \frac{-|u_1|}{\sqrt{1+u_1^2}} e^{-ik\hat{r}|u_1|} + ik\hat{r} \sum_{v=0}^{11} \frac{b_v}{cv+ik\hat{r}} e^{-(cv+ik\hat{r})|u_1|}$$

$$+ \left(1 - \frac{u_1}{|u_1|}\right) \cdot \text{Re} \left\{ \frac{u}{\sqrt{1+u^2}} e^{-ik\hat{r}u} \Big|_0^{|u_1|} \right\} \quad (19)$$

$$- ik\hat{r} \sum_{v=0}^{11} \frac{b_v}{cv+ik\hat{r}} e^{-(cv+ik\hat{r})u} \Big|_0^{|u_1|} \left\} \right.$$

where

$$\hat{r} = \frac{r}{[(1+\gamma)\delta M_\infty^2]^{1/3}}$$

$$u_1 = \frac{t}{\hat{r}}$$

and $c = 0.372$ with b_v defined in the table.

v	b_v	
0	1.0	
1	-0.2418	6198
2	2.7918	027
3	-24.9910	79
4	111.5919	6
5	-271.4354	9
6	305.7528	8
7	41.1836	30
8	-545.9853	7
9	-644.7815	5
10	-328.7275	5
11	64.2795	11

4.0 PROGRAM DESCRIPTIONS

Computer programs TDSTRN and TDUTRN, used in conjunction, implement the theory and numerical solution procedure for unsteady transonic flow described in the previous two sections. As described above, the boundary value problems for the steady perturbation potential (Equation 9) and the unsteady perturbation potential (Equation 10) are solved in TDSTRN and TDUTRN respectively using a finite difference relaxation procedure. The use and manipulation of magnetic tapes forms an integral part of the operation of each program as well as serving as the necessary "data link" between the two programs. As a result the user is assumed to have some familiarity with the use of tapes and their manipulation with control cards. The reading and writing of data files on magnetic tape is described in the next section and motivated in Section 6.0. In this section, the logical flow of the TDSTRN and TDUTRN programs is described and a brief summary of each subroutine is presented. Both programs are quite similar in logical approach and operation, so that they are described together. Differences between the programs are highlighted with appropriate comments as needed.

The logical flow of the TDSTRN and TDUTRN programs are almost identical with minor exceptions noted in the description below. The calculation is begun by reading card input and, if a restart is being performed, a tape dump. In TDUTRN the tape dump of the steady solution being perturbed is also read. All finite difference coefficients and airfoil boundary conditions are initialized in a call to INITAL and subsonic farfield quantities are initialized in a call to FARFLD. If a restart is not being performed, initial values for ϕ at all grid points are determined by the linearized subsonic or supersonic solution. The computational cycle is executed by setting up the tridiagonal equations for a column of grid points using the mixed differencing finite difference equations. The equations are solved iteratively in TDSTRN and in one pass in TDUTRN, by Gaussian elimination in a call to TRI. Each column is solved and relaxed in turn proceeding through the grid from left to right. The grid is swept iteratively in this manner until the change in ϕ for all grid points is less than EPSGRD(1). A call to PRINT prints out the airfoil pressure coefficients every NPRINT iterations, and the farfield is updated every NGFF iterations, in FARFLD.

When the converged solution is obtained, a tape dump of all relevant input and calculated quantities is performed and a call to FPRINT calculates and prints out the airfoil pressure and force coefficients. Various diagnostic prints are also performed in TDSTRN and TDUTRN after every grid iteration, when the farfield is updated, when the grid is refined and when a tape dump is performed. The iterative procedure may also be terminated when the maximum number of iterations (NGRID) has been exceeded. In either case, a final tape dump and final print are executed.

A summary of each subroutine is now presented.

TDSTRN/TDUTRN

These are the driver routines for the respective programs. The logical flow of the mixed differencing relaxation procedure as just described is controlled by these routines and all operations including input, initialization, finite difference solution and output are performed either internally or by calls to the various subroutines described below.

DØUBLE

(Not in present version).

FARFLD

The subsonic farfield is calculated and updated in this routine using the asymptotic solutions for the steady or unsteady perturbation potentials.

FLP (in TDSTRN only)

This is a function statement which contains the airfoil lower surface slope distribution used in the linearized tangency boundary condition. This function is called from subroutine INITIAL and its value at each grid point on the lower surface of the airfoil is stored in the FPL array.

FPRINT

This routine produces the final print and is called when the solution has converged to the desired accuracy or when the problem is terminated for reaching the maximum number of grid iterations allowed (NGRID). The unscaled pressure coefficients above and below the airfoil at various specified spanwise stations and the airfoil force coefficients are also calculated and printed out in this routine.

FPU (in TDSTRN only)

This is a function statement which contains the airfoil upper surface slope distribution used in the linearized tangency boundary condition. This function is called from subroutine INITIAL and its value at each grid point on the upper surface of the airfoil is stored in the FPU array. The doublet strength due to airfoil thickness ($D\emptyset_{UB}$) must also be given in this subroutine. This quantity is defined by an integral of the airfoil thickness distribution function (normalized to airfoil thickness):

$$D\emptyset_{UB} = \int_{-ZSPAN}^{+ZSPAN} \int_0^1 t(\xi, \eta) d\xi d\eta$$

GAMFUN

This routine performs the relaxation to update farfield circulation (GAMFF).

INITAL

The finite difference coefficients AX1, AX2, BX1, BX2, CX, AY1, AY2, AZ1, AZ2, $\Delta X(DX)$, $\Delta Y(DY)$ and $\Delta Z(DZ)$ are computed in this subroutine. The airfoil boundary conditions FPU and FPL are also set here, using functions FUP and FLP respectively.

PRINT

This routine computes and prints the scaled pressure coefficients above and below the airfoil every NPRINT grid iterations.

TRI

This routine solves a system of tridiagonal equations using Gaussian elimination.

WAKE

This routine solves an integral used in the unsteady farfield solution based on a rational approximation for the integrand.

5.0 INPUT AND OUTPUT

A description of the input required to run TDSTRN and TDUTRN, and the resulting output of each program is presented in this section. All card input is entered using the standard CDC NAMELIST package with the exception of a title card.

5.1 TDSTRN Input

The input for TDSTRN is now considered in three sets. Recommended and/or typical values for some of the input variables which control the numerical scheme, appear in parentheses. Also presented at the end of this section is a description of the restart capability which requires input from a magnetic tape dump of a previous calculation.

First Set

BCD title card containing any information in columns 1 through 80 (Format 8A10). This can be used to define the case being run and is printed out on the last page of output which presents the final converged results.

Second Set

The second set of data is read in under NAMELIST name \$C0NTRL. The single variable read defines the use of the restart option. Some comments concerning the mechanics of the use of this option are given at the end of the section.

<u>NAME</u>	<u>DESCRIPTION</u>
ITAPE	This is a flag for using a restart tape. ITAPE = 0 means the problem is being started from scratch (iteration 0) using an initial guess defined in TDSTRN. ITAPE = 1 means the problem is being restarted from a previous run which is to be read from a dump tape.

Third Set

The third set of data is read in under NAMELIST name \$IN, and includes all of the variables required to define a problem, and control the numerical iteration procedure.

NAME	DESCRIPTION
X	An Array containing the streamwise grid coordinates; IM of them
Y	An array containing the normal grid coordinates; JM of them
Z	An array containing the spanwise grid coordinates; KM of them
IM	Number of grid points in the streamwise direction (maximum of 40)
JM	Number of grid points in the normal direction (maximum of 40)
KM	Number of grid points in the spanwise direction; (maximum of 20)
ILE	I location of airfoil leading edge (X(ILE))
ITE	I location of airfoil trailing edge (X(ITE))
JW	J location of airfoil (Y(JW))
KSPAN	K location of wing tip
ZSPAN	Wing semi-span; Z location of wing tip
M8	Freestream Mach number
GAM	γ , ratio of specific heats
DEL	Airfoil thickness ratio in percent
ALPHA	Airfoil angle of attack in radians
GAMFF	Initial guess for the spanwise distribution of airfoil circulation; to be used in the initialization of the farfield; KSPAN values.
NGFF	Every NGFF grid iterations the farfield is updated (~10).

NAME	DESCRIPTION
ØMEGAH	Relaxation parameter for hyperbolic grid points (~.75)
ØMEGAE	Relaxation parameter for elliptic grid points (~1.7)
ØMEGAP	Relaxation parameter for parabolic grid points (~.75)
EPSCØL	Convergence criteria for column solution. The change in ϕ^0 during a column iteration at every point in the column must be less than EPSCØL for convergence to occur ($\sim 5 \times 10^{-5}$)
NCØL	Maximum number of column iterations allowed. Note that if NCØL iterations is reached without convergence, a printout of the degree of convergence is given and the calculations proceed as if convergence had occurred (~10)
EPSGRD	An array containing criteria to control grid convergence. The change in ϕ^0 at every grid point during one grid sweep must be less than EPSGRD(1) for convergence to occur.
KEPS	Set equal to 1. (Not used in current version)
NGRID	Maximum number of grid iterations allowed. When the number of grid iterations equals NGRID the calculation is terminated and a final print given.
NDUMP	Binary tape dump frequency. Every NDUMP grid iterations current values of all variables will be dumped on tape. Note that a tape dump occurs automatically whenever the grid converges or the number of grid iterations equals NGRID (set equal to large number if a dump of only the final iteration is desired).
NPRINT	Every NPRINT grid iterations the scaled pressure coefficient above and below the airfoil is printed.

<u>NAME</u>	<u>DESCRIPTION</u>
IK	Setting IK = 1, flags the use of a previous solution as an initial guess for the current problem where the Mach number, airfoil thickness or shape and/or angle of attack may be different.
NKPRT	Number of spanwise sections for which pressure coefficient data is printed in final print.
KPRT	K location of spanwise sections for which pressure coefficient data is printed in final print (maximum of 20).
ZE	Spanwise locations for numerical integration along span used in farfield calculations (maximum of 25). This permits the specification of more spanwise points than available in grid (KSPAN) to increase accuracy of the numerical evaluation of wing integrals.
NZE	Number of spanwise locations for wing integration.

The input data listed above are necessary to initiate a calculation for which no previous calculation is available. Most calculations, however, are performed as restarts using data which has been stored as binary files on the restart tape according to the format described in Section 5.2. This use of the restart capability is an inherent aspect of the recommended computational procedure. Some brief comments describing the initiation of a calculation using the restart capability are pertinent at this juncture.

It is noted that the restart or dump tape (TAPE7) may be manipulated in any way desired using the appropriate control cards. In general the tape will contain data from many runs, stored as individual binary files. For restarting the TDSTRN program, the desired file from the restart tape (TAPE7) is copied to a disc file (TAPE8). The user is reminded to rewind TAPE8. TAPE7 is then positioned at the end of the last file on the tape so that new dumps can be written by the program without losing any of the old data. The first two sets of data are then input with ITAPE=1. In the third set of data the following control variables are needed as input:

ØMEGAH, ØMEGAE, ØMEGAP, EPSCØL, EPSGRD, NDUMP,
NCØL, NGRID, NGFF, PGFF, KEPS, NPRINT, NKPRT,
KPRT, ZE, and NZE.

The remaining input variables are stored on the restart tape and need not be input unless the restart option is being used to run a new case. If a new case is being run, IK must be set to 1 which allows the Mach number, airfoil thickness or airfoil angle of attack (M8, DEL, ALPHA) to be changed. If the airfoil angle of attack and/or the flap angle are changed a new guess for the farfield circulation (GAMFF) can and should be made.

5.2 TDSTRN Output

The output from TDSTRN consists of three parts: (i) a continuous commentary which describes the progress of the iterative solution procedure, (ii) a final print summarizing results of interest from the final converged solution, and (iii) a binary tape dump of all pertinent input and calculated parameters.

The continuous commentary consists of various print statements executed in the main program TDSTRN or the subroutine PRINT which describe the current state of the solution as well as the occurrence of various "milestones" in the iteration process. The only print that occurs every iteration is the value of the maximum change in ϕ^0 throughout the grid during one grid iteration. When a column iteration fails to converge, a print occurs which defines the degree of column convergence and the j and k locations of the most poorly converged point. Every NGFF iterations, the subsonic farfield is updated and the new values of farfield circulation (GAMFF) and airfoil circulation (GAMTE) are printed. The user can examine the effect of degree of convergence on the solution by specifying a print of the scaled pressure coefficients on the upper and lower airfoil surfaces every NPRINT iterations. Finally, a descriptive print occurs at certain milestone points such as the occurrence of a binary tape dump and solution convergence.

The final print is executed in subroutine FPRINT when the solution has converged to the desired accuracy or when the number of grid iterations equals NGRID. The print is self-explanatory and includes the input parameters which define the problem and various calculated quantities of interest. The calculated quantities are of course based on the final converged solution. The section lift coefficients are printed out as well as the upper and lower surface pressure coefficients for various spanwise coordinates.

The most important form of TDSTRN output is the binary tape dump of all input parameters defining the problem and of the most recent values of ϕ^0 at all grid points. A tape dump occurs automatically if the solution has converged to the desired accuracy or if the number of grid iterations equals NGRID. The user may also specify that such a dump occur every NDUMP grid iterations. The tape so generated, not only forms a permanent record of the results of a calculation for possible future editing and examination but also forms a necessary part of the computational procedure. Most important is its use as required input for a TDUTRN calculation. However, it may also be used to restart the calculation to refine accuracy or convergence or be used as the initial guess for ϕ^0 throughout the grid for a similar calculation, as described in Section 5.1.

The format used for writing and reading the binary tape is given in the following FORTRAN statements:

```
WRITE (7)      NITERG,IM,IM1,JM,JM1,KM,KM1,JW,  
                JWP1,JWM1,ITE,ILE,KSPAN,KCAP,DEL,  
                ALPHA,NDB,M8,GAM,DYBUL,DYBU2,DYBL1,  
                DYBL2,DØUB,ZSPAN  
  
WRITE (7)      (X(I),DX(I),AX1(I),AX2(I),BX1(I),  
                BX2(I),CX(I),I=1,IM)  
  
WRITE (7)      (Y(I),DY(I),AY1(I),AY2(I),I=1,JM)  
  
WRITE (7)      (Z(I),DZ(I),AZ1(I),AZ2(I),I=1,KM)  
  
L=ITE*KM  
  
WRITE (7)      (FPU(I),FPL(I),PHIUB(I),I=1,L)  
  
WRITE (7)      (GAMTE(I),GAMFF(I),I=1,KSPAN)  
  
L=IM*JM*KM  
  
WRITE (7)      (PHI(I),I=1,L)  
  
END FILE 7
```

Any information may be retrieved from the tape by using the appropriate READ statements as is done in the restart option described above.

5.3 TDUTRN Input

The input for TDUTRN consists of normal card input plus input from a binary file which contains the steady solution generated by an TDSTRN run. TDUTRN also has a restart capability which is implemented in exactly the same manner as previously described in Section 5.1 for TDUTRN and elaborated upon at the end of this section. The required input is now described and some comments are presented at the end of this section pertaining to the tape read of the steady solution. As before, the card input is described in three sets.

First Set

BCD title card containing any information in columns 1 through 80 (Format 8A10).

Second Set

The second set of data is read in under NAMELIST name \$C0NTRL.

<u>NAME</u>	<u>DESCRIPTION</u>
ITAPE	This is a flag for using a restart tape. ITAPE=0 means the problem is being started from scratch (iteration 0), ITAPE=1 means the problem is being restarted from a previous run using the restart tape. Note that a tape is also used for the input of steady results independent of the value of ITAPE.

Third Set

The third set of data is read in under NAMELIST name \$IN.

<u>NAME</u>	<u>DESCRIPTION</u>
X	An array containing the streamwise grid coordinates; IM of them.
Y	An array containing the normal grid coordinates; JM of them.
Z	An array containing the spanwise grid coordinate KM of them

<u>NAME</u>	<u>DESCRIPTION</u>
IM	Number of grid points in the streamwise direction (maximum of 40).
JM	Number of grid points in the normal direction (maximum of 40).
KM	Number of grid points in the spanwise direction (maximum of 20).
ILE	I location of airfoil leading edge ($X(ILE)$).
ITE	I location of airfoil trailing edge ($X(ITE)$).
JW	J location of airfoil ($Y(JW)$).
SMALLK	Reduced frequency based on chord = wc/U .
KSPAN	K location of wing tip
GAMFF	Initial guess for the airfoil circulation used in the initialization of the farfield. Note that GAMFF is a complex number.
NGFF	Every NGFF grid iterations the airfoil circulation in the farfield is updated. This also causes the farfield to be updated (~10).
PGFF	Relaxation parameter used in the iteration for the airfoil circulation in the farfield (~1.5).
ØMEGAH	Relaxation parameter for hyperbolic grid points (~.75).
ØMEGAE	Relaxation parameter for elliptic grid points (~1.7).
ØMEGAP	Relaxation parameter for parabolic grid points (~.75).
EPSGRD	An array containing criteria to control grid convergence. The change in ϕ^1 at every grid point during one grid sweep must be less than EPSGRD(1) for convergence to occur.
KEPS	Set equal to 1. (Not used in current version)

<u>NAME</u>	<u>DESCRIPTION</u>
NGRID	Maximum number of grid iterations allowed. When the number of grid iterations equals NGRID the calculation is terminated.
NDUMP	Binary tape dump frequency. Every NDUMP grid iterations current values of all variables will be dumped on tape. Note that a tape dump occurs automatically whenever the grid converges or the number of grid iterations equals NGRID. (Set equal to large number if a dump of only the final iteration is desired.)
NPRINT	Every NPRINT grid iterations the scaled upper and lower surface pressure coefficient per unit angle of oscillation is printed.
IK	Setting IK=1 allows the user to use a previous solution as an initial guess for the current problem where the reduced frequency and/or mode of oscillation is different.
XP	Streamwise location of pitch point for pitching oscillation.
ITYPE	Unsteady mode of rigid body oscillation ITYPE=1 → Pitch about XP ITYPE=3 → Uniform plunge
IØPT	Unsteady formulation option; IØPT=0 for low frequency approximation, IØPT=1 for general frequency theory.
NKPRT	Number of spanwise sections for which pressure coefficient data is printed in final print.
KPRT	K location of spanwise sections for which pressure coefficient data is printed in final print (maximum of 20).
ZE	Spanwise locations for numerical integration along span used in farfield calculation (maximum of 20). This permits the specification of more spanwise points than available in grid (KSPAN) to increase accuracy of the numerical integration of wing integrals.
NZE	Number of spanwise locations for wing integration.

It is recalled, that the solution for the unsteady perturbation potential, implemented in TDUTRN, requires the solution of the steady potential, generated by TDSTRN. This is accomplished by reading the appropriate file on a dump tape generated by TDSTRN, in much the same way as is done in the restart option. It is instructive to briefly describe the TDUTRN restart including the tape read of the steady solution.

Restarting the TDUTRN program is only slightly more complicated than TDSTRN. In this case, two tape dumps or files are required. First the file containing the desired steady tape dump is copied from TAPE7 to a disc file, TAPE8. Next the file containing the desired unsteady tape dump is copied from TAPE7 to a disc file, TAPE9, and TAPE8 and TAPE9 are rewound for reading by the program. TAPE7 is then positioned at the end of the last file on the tape in preparation for accepting a new tape dump. The first two sets of data are input as before (be sure to set ITAPE=1). In the third set of data the following variables are necessary:

\emptyset MEGAH, \emptyset MEGAE, \emptyset MEGAP, EPSGRD, NDUMP, NGRID,
NGFF, PFGG, KEPS, NPRINT, NKPRT, KPRT, ITYPE,
IQPT, ZE, and NZE.

Again there is an option (IK=1) which allows the user to change the reduced frequency and/or the mode of oscillation (SMALLK and ITYPE). In either case a new guess for the farfield circulation (GAMFF) should be made.

5.4 TDUTRN Output

The output from TDUTRN is very similar to that of TDSTRN and includes a continuous commentary, final print and binary tape dump.

The printed output is of the form described above for TDSTRN. The only difference is that the field variables in TDUTRN are complex so that the real and imaginary parts are printed out in that order. The descriptive prints are all the same with the deletion of the unneeded comment on column convergence. The final print is executed in subroutine FPRINT when the solution has converged or has reached the maximum number of iterations desired by the user (NGRID). The print includes all important input variables which define both the steady solution being perturbed and the unsteady solution being generated. Also, various calculated quantities, based on the final con-

verged solution, are printed. These include the real and imaginary parts of the unsteady contribution (per unit angle of oscillation) to the aerodynamic force coefficients. Also unsteady contributions to the upper and lower surface pressure coefficients (per unit angle of oscillation) are printed for every computational point on the airfoil. It is again noted that these are complex so that the real and imaginary parts are printed out in order.

The other form of TDUTRN output is the binary tape dump of all input parameters and the most recent values of ($Re\phi^1$, $Im\phi^1$) at all grid points. As before the tape dump occurs automatically at normal program termination or at the users discretion every NDUMP iterations. The format used for writing and reading the binary tape is given in the following FORTRAN statements:

```
WRITE (7)      NITERG,IM,IM1,JM,JM1,KM,KM1,JWPI,  
                JWML,ILE,ITE,KSPAN,ØMEG,SMALLK,  
                DYBUL,DYBU2,DYBL1,DYBL2,NDØUB,XP  
  
WRITE (7)      (X(I),DX(I),AX1(I),AX2(I),BX1(I),  
                BX2(I),CX(I),I=1,IM)  
  
WRITE (7)      (Y(I),DY(I),AY1(I),AY2(I),I=1,JM)  
  
WRITE (7)      (Z(I),DZ(I),AZ1(I),AZ2(I),I=1,KM)  
  
L=ITE*KM  
  
WRITE (7)      (FPU(I),FPL(I),PHIUB(I),I=1,L)  
  
WRITE (7)      (GAMTE(I),GAMFF(I),I=1,KSPAN)  
  
L=IM*JM*KM  
  
WRITE (7)      (PHI(I),I=1,L)  
  
END FILE 7
```

6.0 PROGRAM USAGE

The general structure and usage of the three-dimensional programs TDSTRN and TDUTRN are very similar to that for the original two-dimensional versions STRANS and UTRANS. This being the case, it is recommended for economy sake that the first time user initially become acquainted with those programs. The programs are documented in detail in Reference 2 so that the comments concerning program usage in this manual are kept necessarily brief.

In their present configuration, both TDSTRN and TDUTRN allow a maximum of 11,500 computational grid points and the number of grid lines in the streamwise, normal and spanwise directions must each be less than 40, 40, 20 respectively. In this configuration, TDSTRN requires 70.5_sK words to load and 57.0_sK words to execute and TDUTRN requires 161.7_sK words to load and 150.0_sK words to execute. This configuration was chosen so that each program could fit into small core storage of a CDC 7600 computer. If greater storage is available and used, (Ex. CDC 6600) it is a relatively simple matter to increase the array sizes of the primary variables PHI, X, Y, Z, FPU, FPL, etc.

Detailed comments and suggestions are given in Reference 2 concerning grid design, farfield location and update, choice of relaxation factors and accuracy and convergence. These same comments apply to the present three-dimensional programs and will not be repeated here. The sample cases presented in the next section should provide some guidance with respect to such items.

7.0 SAMPLE CASES

Detailed input and sample output for sequences of TDSTRN and TDUTRN runs are presented in this section.

7.1 TDSTRN Test Case

A sequence of computer runs are described in this section, which calculate the steady transonic flow over a 6 percent thick, symmetric circular arc, rectangular planform wing with aspect ratio 8, at $M_{\infty} = .86$, $\alpha = 0$. The individual runs required to complete the calculation are described in the run log given in Table 1. The table lists the restart tape read by each run, total grid iterations, convergence achieved and the tape dump generated. The grid used consisted of approximately 11000 points with IM=30 over $-3.2 < x < 3.4$, JM=19 over $-5.4 < y < 5.4$ and KM=19 over $0 < z < 6.0$. In the x direction, 16 grid lines were distributed along the airfoil chord with $\Delta x \sim .06$ and in the z direction 10 grid lines were distributed over the span with $\Delta z \sim .2$. The runs shown in the log implement a "bootstrapping" technique by which the calculation is initiated at a low sub-critical Mach number and the Mach number raised in later runs to the final desired value. The final run was taken to a convergence of $\Delta \phi_{max} = 3.7 \times 10^{-5}$. All runs were completed in a total time of 65 seconds on a CDC 7600 which indicates a computer time requirement of $3. \times 10^{-5}$ CPU sec/grid point/iteration. The final convergence achieved is believed to be more than sufficient for engineering accuracy.

Run	M_{∞}	Restart Tape Used	Grid Iterations	Convergence Achieved	Tape Dump Generated
1S	.7	--	38	10^{-3}	1S
2S	.8	1S	19	10^{-3}	2S
3S	.86	2S	50	1.9×10^{-4}	3S
4S	.86	3S	50	3.7×10^{-5}	4S

TABLE 1. SEQUENCE OF RUNS FOR TDSTRN SAMPLE CASE

7.1.1 Input for TDSTRN Sample Cases

The card input for each of the TDSTRN runs described above is given in this section.

- Run 1S: no tape read, generate file 1S

3D CIRCULAR ARC

```
$CØNTRL
ITAPE=0,
$END
$IN
X(1)=-3.2,-2.2,-1.5,-1.02,-.67,-.42,-.24,-.1,0.,.07,
.14,.21,.28,.35,.42,.5,.55,.6,.65,.7,.76,.82,
.9,1.,1.14,1.34,1.62,2.02,2.58,3.38,
Y(1)=-5.4,-3.41,-2.91,-1.91,-1.21,-.74,-.43,-.22,-.08,
0.,.08,.22,.43,.74,1.21,1.91,2.91,3.41,4.3,
Z(1)=0.,.25,.5,.75,1.,1.25,1.5,1.75,1.9,2.,2.1,2.25,
2.45,2.75,3.2,3.85,4.75,6.,6.8,
IM=30,
JM=19,
KM=19,
ILE=9,
ITE=24,
JW=10,
KSPAN=10,
ZSPAN=2.,
M8=.7,
GAM=1.4,
DEL=.06,
ALPHA=0.0,
GAMFF(1)=10*0.,
ØMEGAH=.75,
ØMEGAE=1.7,
ØMEGAP=.75,
EPSCØL=5.E-5,
EPSGRD(1)=1.E-3,
NDUMP=2000,
NCØL=10,
NGRID=50,
NGFF=2000,
PGFF=1.5,
KEPS=1,
IK=0,
NPRINT=5,
NKPR=10,
KPRT(1)=1,2,3,4,5,6,7,8,9,10,
ZE(1)=0.,2.,
NZE=2,
$END
```

- Run 2S: read file 1S, generate file 2S

3D CIRCULAR ARC

```
$CØNTRL  
ITAPE=1,  
$END  
$IN  
ØMEGAH=.75,  
ØMEGAE=1.7,  
ØMEGAP=.75,  
EPSCØL=5.E-5,  
EPSGRD=1.E-3,  
NDUMP=2000,  
NCØL=10,  
NGRID=50,  
NGFF=2000,  
PGFF=1.5,  
KEPS=1,  
NPRINT=5,  
NKPRT=10,  
KPRT(1)=1,2,3,4,5,6,7,8,9,10,  
ZE(1)=0.0,2.0,  
NZE=2,  
IK=1,  
M8=0.8,  
$END
```

- Run 3S: read file 2S, generate file 3S

3D CIRCULAR ARC

```
$CØNTRL  
ITAPE=1,  
$END  
$IN  
ØMEGAH=.75,  
ØMEGAE=1.7,  
ØMEGAP=.75,  
EPSCØL=5.E-5,  
EPSGRD=1.E-4,  
NDUMP=2000,  
NCØL=10,  
NGRID=50,  
NGFF=2000,  
PGFF=1.5  
KEPS=1,  
NPRINT=5,  
NKPRT=10,
```

```
KPRT(1)=1,2,3,4,5,6,7,8,9,10,  
ZE(1)=0.0,2.0,  
NZE=2,  
IK=1,  
M8=.86,  
$END
```

- Run 4S: read file 3S; generate file 4S

*** 3D CIRCULAR ARC***

```
$CØNTRL  
ITAPE=1,  
$END  
$IN  
ØMEGAH=.75,  
ØMEGAE=1.7,  
ØMEGAP=.75,  
EPSCØL=5.E-5,  
EPSGRD=1.E-3,  
NDUMP=2000,  
NCØL=10,  
NGRID=50,  
NGFF=2000,  
PGFF=1.5,  
KEPS=1,  
NPRINT=5,  
NKPRT=10,  
KPRT(1)=1,2,3,4,5,6,7,8,9,10,  
ZE=0.0,2.0,  
NZE(1)=2,  
IK=0,  
$END
```

7.1.2 Sample Output for TDSTRN Test Case

The following pages contain a sample of the continuous commentary output for the first 4 cycles of Run 1S in addition to the final printed page of all runs. Also included is the complete final output for the final converged result (Run 4S).

• SAMPLE OUTPUT FROM RUN 1S

```

SIMILARITY PARAMETER (E) = .20467E+00
SCALING FACTOR (C/CSTAR) = .10526E+00

AT ITERATION 1 COLUMN 11 FAILED TO CONVERGE ENE = -.579021E-01 J = 0 K = 1
AT ITERATION 1 COLUMN 15 FAILED TO CONVERGE LNR = -.12937E-03 J = 0 K = 1
AT ITERATION 1 COLUMN 22 FAILED TO CONVERGE FAN = -.15179E-05 J = 0 K = 1
AT ITERATION 1 COLUMN 25 FAILED TO CONVERGE LPR = -.73166E-01 J = 0 K = 1
AT ITERATION 1 COLUMN 4 FAILED TO CONVERGE ECR = .72860E-01 J = 0 K = 2
AT ITERATION 1 THE MAXIMUM ERROR = .23879E+01 AND OCCURRED AT NODE 150
AT ITERATION 2 COLUMN 4 FAILED TO CONVERGE ENE = -.466027E-04 J = 0 K = 1
AT ITERATION 2 COLUMN 12 FAILED TO CONVERGE LPR = .83004F-06 J = 7 K = 1
AT ITERATION 2 COLUMN 15 FAILED TO CONVERGE ENE = -.59371E-01 J = 7 K = 1
AT ITERATION 2 THE MAXIMUM ERROR = .22038E+01 AND OCCURRED AT NODE 270
AT ITERATION 3 COLUMN 10 FAILED TO CONVERGE LPR = .25477E-02 J = 9 K = 1
AT ITERATION 3 COLUMN 20 FAILED TO CONVERGE LNR = -.27270E-01 J = 9 K = 1
AT ITERATION 3 COLUMN 22 FAILED TO CONVERGE LPR = -.74007E-01 J = 9 K = 1
AT ITERATION 3 COLUMN 25 FAILED TO CONVERGE ENE = -.18813E-01 J = 9 K = 1
AT ITERATION 3 THE MAXIMUM ERROR = .30798E+01 AND OCCURRED AT NODE 410
AT ITERATION 4 COLUMN 14 FAILED TO CONVERGE FAN = -.68272E-01 J = 6 K = 1
AT ITERATION 4 COLUMN 25 FAILED TO CONVERGE LPR = -.72451E-01 J = 6 K = 1
AT ITERATION 4 COLUMN 26 FAILED TO CONVERGE FAN = -.24119E-01 J = 6 K = 2
AT ITERATION 4 COLUMN 25 FAILED TO CONVERGE ENE = -.31298E-01 J = 6 K = 2
AT ITERATION 4 THE MAXIMUM ERROR = .584832E+01 AND OCCURRED AT NODE 1030
AT ITERATION 5 AND ON 1 SCALE PRESSURE CONVERGENCE FILE TO ITET = .10868E+02 .75477E+01 -.016105E+01 -.003093E+01
.16925E+01 .169316E+01 .9605E+01 .32554E+01 .15594E+01 .12317E+01 -.016145E+01 -.003091E+01
.20590E+02 .20590E+02 .65156E+02 .56551E+02 -.016145E+01 .14921E+01 .12317E+02 -.016145E+01 -.003091E+01
AT ITERATION 6 AND ON 1 STRESS CONVERGENCE FILE TO ITET = .50488E+02 .75677E+01 -.016105E+01 -.003093E+00
.16925E+01 .169316E+01 .9605E+01 .32554E+01 .15594E+01 .12317E+01 -.016145E+01 -.003091E+00
.20590E+02 .20590E+02 .65156E+02 .56551E+02 -.016145E+01 .14921E+01 .12317E+02 -.016145E+01 -.003091E+00
AT ITERATION 6 AND ON 1 SCALD DIVERGENCE CRITICAL, INFER FILE TO ITET = .422532E+00 -.66498E+00 -.004969E+00 -.004969E+00
.16925E+01 .169316E+01 .9605E+01 .32554E+01 .15594E+01 .12317E+01 -.016145E+01 -.003091E+00
.20590E+02 .20590E+02 .65156E+02 .56551E+02 -.016145E+01 .14921E+01 .12317E+02 -.016145E+01 -.003091E+00
AT ITERATION 6 AND ON 1 SCALD DIVERGENCE CRITICAL, LINTEN FILE TO ITET = .28929E+00
.16925E+01 .169316E+01 .9605E+01 .32554E+01 .15594E+01 .12317E+01 -.016145E+01 -.003091E+00
.20590E+02 .20590E+02 .65156E+02 .56551E+02 -.016145E+01 .14921E+01 .12317E+02 -.016145E+01 -.003091E+00
AT ITERATION 6 AND ON 1 SCALD DIVERGENCE CRITICAL, LINTEN FILE TO ITET = .56171E+00 -.51378E+00 -.024532E+00 -.024532E+00
.16925E+01 .169316E+01 .9605E+01 .32554E+01 .15594E+01 .12317E+01 -.016145E+01 -.003091E+00
.20590E+02 .20590E+02 .65156E+02 .56551E+02 -.016145E+01 .14921E+01 .12317E+02 -.016145E+01 -.003091E+00

```

RUN 1S

3-D CINEMATOGRAPHY

AUGUST 1979

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四庫全書

• 314 •

אלה ימיה כהנום מילון עליון יוניברסיטאי

3-0 CIRCULAR AAC

earth resistance = 0.04 ohms/km
equivalent parallel earth (eq) = 115900 ohms
transient earth resistance = 115900 ohms
angle of attack (standang) = 0.
wing aspect ratio = 2.000000
core scaling factors (scalars) = 12500000
geometric scaling factors (scalars) = -22500000

SIMPLY EASY LEARN CIVICS 119

• 31-312662 • 11-312662 • 9 (681) 11-312662 •

SECTION LINE COEFFICIENT = .127216-12

ALTERNATE STRATEGIES CONSIDERED
B. ALTERNATIVE OUTCOMES CONSIDERING INPUTS
ALTERNATIVE OUTCOMES CONSIDERING INPUTS
ALTERNATIVE OUTCOMES CONSIDERING INPUTS

*** 1-D CIRCULAR ANC ***

WALL VISCOSITY = 0.00000000E+00
SIMILARITY PROFILE TYPE = 11,000
TURBULENCE LEVEL = 0.000000E+00
ALBEDO AND IR ATTACH (WATLAW) = 0.
WING ASPECT RATIO = 2.0000E+01
CA SCALING FACTOR (CFS) = 1.2656E+00
CRITICAL PERTURB COEFFICIENT (CFC) = -0.29340E+00

AIRFOIL STATE=1SE Coordinate = 0.
0. 76000E-01 1.60000E-00 .21000E+00 .20000E+00 .35000E+00 .42000E+00 .50000E+00 .59000E+00 .68000E+00 .76000E+00 .85000E+00

AIRFOIL SPANWISE COORDINATE = 0.

AIRFOIL SPANWISE COORDINATE, UP/DOWN = 0.
0.1297E-01 -0.8561E-01 -0.1719E-00 -0.2731E+00 -0.3669E+00 -0.4662E+00 -0.5610E+00 -0.6542E+00 -0.7472E+00 -0.8401E+00 -0.9330E+00

AIRFOIL SPANWISE COEFFICIENTS, L/D/R = 0.
0.1297E-01 -0.8561E-01 -0.1719E-00 -0.2731E+00 -0.3669E+00 -0.4662E+00 -0.5610E+00 -0.6542E+00 -0.7472E+00 -0.8401E+00 -0.9330E+00

AIRFOIL SPANWISE COORDINATE = 0.25000E+00 SECTION LIFT COEFFICIENT = 0.12772E-12

AIRFOIL SPANWISE COEFFICIENTS, UP/DOWN = 0.
0.1472E+00 -0.1319E-01 -0.4561E-01 -0.1719E-00 -0.2472E+00 -0.3093E+00 -0.3664E+00 -0.4234E+00 -0.4804E+00 -0.5245E+00

AIRFOIL SPANWISE COEFFICIENTS, L/D/R = 0.
0.1472E+00 -0.1319E-01 -0.4561E-01 -0.1719E-00 -0.2472E+00 -0.3093E+00 -0.3664E+00 -0.4234E+00 -0.4804E+00 -0.5245E+00

AIRFOIL SPANWISE COORDINATE = 0.50000E+00 SECTION LIFT COEFFICIENT = 0.12547E-12

AIRFOIL SPANWISE COEFFICIENTS, UP/DOWN = 0.
0.1472E+00 -0.1319E-01 -0.4561E-01 -0.1719E-00 -0.2472E+00 -0.3093E+00 -0.3664E+00 -0.4234E+00 -0.4804E+00 -0.5245E+00

AIRFOIL SPANWISE COEFFICIENTS, L/D/R = 0.
0.1472E+00 -0.1319E-01 -0.4561E-01 -0.1719E-00 -0.2472E+00 -0.3093E+00 -0.3664E+00 -0.4234E+00 -0.4804E+00 -0.5245E+00

AIRFOIL SPANWISE COORDINATE = 0.75000E+00 SECTION LIFT COEFFICIENT = 0.11942E-12

AIRFOIL SPANWISE COEFFICIENTS, UP/DOWN = 0.

• FINAL OUTPUT OF RUN 4S (CONT'D)

airfoil pressure coefficient, upper a	.115747e-01	.115747e-01	.117129e+00	.246475e+00	.196791e+00	.182938e+00	.661962e+00	.490724e+00	.523872e+00
airfoil pressure coefficient, lower a	.045534e+00	.045534e+00	.042118e+01	.211848e+01	.132495e+00				
airfoil pressure coefficient, LCFW a	.107400e+00	.107400e+00	.171246e+00	.246497e+00	.196516e+00	.193946e+00	.663626e+00	.490724e+00	.523872e+00
airfoil pressure coefficient, LCFW b	.107400e+00	.107400e+00	.042118e+01	.211848e+01	.132495e+00				
airfoil spanwise coordinate a	.100092e+01	.100092e+01	.1250nt+01	.SECTION LIFT COEFFICIENT a	.110162e+12				
airfoil pressure coefficient, upper a	.115747e-01	.115747e-01	.117074e+00	.246516e+00	.196751e+00	.182956e+00	.661962e+00	.490724e+00	.523872e+00
airfoil pressure coefficient, lower a	.045534e+00	.045534e+00	.042118e+01	.211848e+01	.132495e+00				
airfoil pressure coefficient, LCFW a	.107400e+00	.107400e+00	.042118e+01	.211848e+01	.132495e+00				
airfoil pressure coefficient, LCFW b	.107400e+00	.107400e+00	.171246e+00	.246497e+00	.196516e+00	.193946e+00	.663626e+00	.490724e+00	.523872e+00
airfoil spanwise coordinate a	.100092e+01	.100092e+01	.1250nt+01	.SECTION LIFT COEFFICIENT a	.9999af-13				
airfoil pressure coefficient, upper a	.115747e-01	.115747e-01	.117088e+00	.246536e+00	.196751e+00	.182956e+00	.661962e+00	.490724e+00	.523872e+00
airfoil pressure coefficient, lower a	.045534e+00	.045534e+00	.042118e+01	.211848e+01	.132495e+00				
airfoil pressure coefficient, LCFW a	.107400e+00	.107400e+00	.042118e+01	.211848e+01	.132495e+00				
airfoil pressure coefficient, LCFW b	.107400e+00	.107400e+00	.171246e+00	.246497e+00	.196516e+00	.193946e+00	.663626e+00	.490724e+00	.523872e+00
airfoil spanwise coordinate a	.150000e+01	.150000e+01	.175000e+01	.SECTION LIFT COEFFICIENT a	.9999af-13				
airfoil pressure coefficient, upper a	.115747e-01	.115747e-01	.118029e+00	.246576e+00	.196807e+00	.183032e+00	.662752e+00	.492752e+00	.549915e+00
airfoil pressure coefficient, lower a	.045534e+00	.045534e+00	.042118e+01	.211848e+01	.132528e+00				
airfoil pressure coefficient, LCFW a	.107400e+00	.107400e+00	.042118e+01	.211848e+01	.132528e+00				
airfoil pressure coefficient, LCFW b	.107400e+00	.107400e+00	.171246e+00	.246576e+00	.196807e+00	.193946e+00	.663626e+00	.492752e+00	.549915e+00
airfoil spanwise coordinate a	.150000e+01	.150000e+01	.175000e+01	.SECTION LIFT COEFFICIENT a	.9999af-13				
airfoil pressure coefficient, upper a	.115747e-01	.115747e-01	.118029e+00	.246576e+00	.196807e+00	.183032e+00	.662752e+00	.492752e+00	.549915e+00
airfoil pressure coefficient, lower a	.045534e+00	.045534e+00	.042118e+01	.211848e+01	.132528e+00				
airfoil pressure coefficient, LCFW a	.107400e+00	.107400e+00	.042118e+01	.211848e+01	.132528e+00				
airfoil pressure coefficient, LCFW b	.107400e+00	.107400e+00	.171246e+00	.246576e+00	.196807e+00	.193946e+00	.663626e+00	.492752e+00	.549915e+00
airfoil spanwise coordinate a	.150000e+01	.150000e+01	.175000e+01	.SECTION LIFT COEFFICIENT a	.9999af-13				
airfoil pressure coefficient, upper a	.115747e-01	.115747e-01	.118029e+00	.246576e+00	.196807e+00	.183032e+00	.662752e+00	.492752e+00	.549915e+00
airfoil pressure coefficient, lower a	.045534e+00	.045534e+00	.042118e+01	.211848e+01	.132528e+00				
airfoil pressure coefficient, LCFW a	.107400e+00	.107400e+00	.042118e+01	.211848e+01	.132528e+00				
airfoil pressure coefficient, LCFW b	.107400e+00	.107400e+00	.171246e+00	.246576e+00	.196807e+00	.193946e+00	.663626e+00	.492752e+00	.549915e+00
airfoil spanwise coordinate a	.150000e+01	.150000e+01	.175000e+01	.SECTION LIFT COEFFICIENT a	.9999af-13				
airfoil pressure coefficient, upper a	.115747e-01	.115747e-01	.118029e+00	.246576e+00	.196807e+00	.183032e+00	.662752e+00	.492752e+00	.549915e+00
airfoil pressure coefficient, lower a	.045534e+00	.045534e+00	.042118e+01	.211848e+01	.132528e+00				
airfoil pressure coefficient, LCFW a	.107400e+00	.107400e+00	.042118e+01	.211848e+01	.132528e+00				
airfoil pressure coefficient, LCFW b	.107400e+00	.107400e+00	.171246e+00	.246576e+00	.196807e+00	.193946e+00	.663626e+00	.492752e+00	.549915e+00

● FINAL OUTPUT OF RUN 4S (CONT'D)

AIRPORT STATIONS CONDUCTANCE = .2000000 SECTION LEFT COEFFICIENT = .128282E-13
AIRPORT POSITION CROSSFIRE, LUFTHAUS = .128748E+00 -.173141E+01 -.20704E+00 -.24551E+00 -.25174E+00
.11612E+00 -.14942E+02 -.16111E+00 -.47777E+01 .40731E-01
.21245E+00 .15652E+00 .15652E+00 .15652E+00 .15652E+00
AIRPORT POSITION CROSSFIRE, LUFT = .128748E+00 -.173141E+01 -.20704E+00 -.24551E+00 -.25174E+00
.10341E+00 .34962E+01 .70785E+01 .15451E+00 .15451E+00 .15451E+00

RUN 4S

114

Wach Kunde in
Sternwarte Bonn für 100
Sternwarte-Erdaten a. d. Stern- u. Planeten-
warte Bonn und für andere Beobachtungs-
stätten auf der Erde ist ein
spezielles Abrechnungs-
scheme eingeführt. Es besteht aus
einem allgemeinen Teil, der die Kosten
für die Verarbeitung der Beobachtungen
und für die Berechnung der Resultate
enthält, und einem speziellen Teil, der
die Kosten für die Beobachtungen
der einzelnen Sterne und Planeten
enthält.

1979-06-11 00:00:00 00000000000000000000000000000000

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CERTIFICATION LIFER COEFFICIENTS • 012345678910

7.2 TDUTRN Test Cases

A sequence of TDUTRN runs are described in this section which calculate the unsteady flow perturbation for the previously described circular arc rectangular wing oscillating in pitch about the leading edge at:

$$M_{\infty} = .86 \quad \left| \begin{array}{l} k = 0.0 \\ k = 0.1 \end{array} \right.$$

The individual runs required to calculate these cases are described in the run log in Table 2. All runs used the steady solution given on tape dump 4S. The table presents the reduced frequency, restart tape read, grid iterations, convergence achieved and tape dump generated. The runs were calculated using the same grid as the steady runs. They were performed in the order shown to implement the "bootstrapping" technique for getting from one reduced frequency to another. The input required for each run and sample output are presented in the following section.

Run	k	Restart Tape Used	Grid Iteration	Convergence Achieved	Tape Dump Generated
1U	0.0	--	50	2.2×10^{-3}	1U
2U	0.0	1U	100	1.9×10^{-4}	2U
3U	0.0	2U	50	6.8×10^{-5}	3U
4U*	0.0	3U	86	1.0×10^{-5}	4U
5U	0.05	4U	50	1.3×10^{-3}	5U
6U*	0.1	5U	200	6.0×10^{-5}	6U

TABLE 2. SEQUENCE OF RUNS FOR TDUTRN SAMPLE CASES
(*DENOTES CONVERGED SOLUTION)

7.2.1 Input for TDUTRN Test Cases

The card input for each of the TDUTRN runs described above is given in this section.

- Run 1U: read file 4S, no restart tape read; generate file 1U.

3D CIRCULAR ARC

```
$CØNTRL
ITAPE=0,
$END
$IN
X(1)=-3.2,-2.2,-1.5,-1.02,-.67,-.42,-.24,-.1,0.,.07,
.14,.21,.28,.35,.42,.5,.55,.6,.65,.7,.76,.82,
.9,1.,1.14,1.34,1.62,2.02,2.58,3.38,
Y(1)=-5.4,-3.41,-2.91,-1.91,-1.21,-.74,-.43,-.22,-.08,
0.,.08,.22,.43,.74,1.21,1.91,2.91,3.41,4.3,
Z(1)=0.,.25,.5,.75,1.,1.25,1.5,1.75,1.9,2.,2.1,2.25,
2.45,2.75,3.2,3.85,4.75,6.,6.8,
IM=30,
JM=19,
KM=19,
ILE=9,
ITE=24,
JW=10,
KSPAN=10,
GAMFF(1)=10*(1.,0.),
ØMEGAH=.75,
ØMEGAE=1.7,
ØMEGAP=.75,
EPSGRD(1)=1.E-4,
NDUMP=2000,
NGRID=50,
NGFF=10,
PGFF=1.5,
KEPS=1,
NPRINT=5,
NNPRT=10,
KPRT(1)=1,2,3,4,5,6,7,8,9,10,
SMALLK=0.0,
IK=0,
XP=0.0,
ITYPE=1,
IØPT=0,
ZE(1)=0.,.125,.25,.375,.5,.625,.75,.875,1.,1.125,1.25,
1.375,1.5,1.625,1.75,1.825,1.9,1.95,2.,
NZE=19,
$END
```

- Run 2U: read file 4S, restart file 1U; generate file 2U

3D CIRCULAR ARC

```
$CØNTRL
ITAPE=1,
$END
$IN
ØMEGAH=.75,
ØMEGAE=1.7,
ØMEGAP=.75,
EPSGRD=1.E-4,
NDUMP=2000,
NGRID=100,
NGFF=10,
PGFF=1.5,
KEPS=1,
NPRINT=5,
NKPRRT=10,
KPRT=1,2,3,4,5,6,7,8,9,10,
ITYPE=1,
IØPT=0,
ZE(1)=0.,.125,.25,.375,.5,.625,.75,.875,1.,1.125,1.25,
1.375,1.5,1.625,1.75,1.825,1.9,1.95,2.,
NZE=19,
IK=0,
$END
```

- Run 3U: read file 4S, restart file 2U; generate file 3U

3D CIRCULAR ARC

```
$CØNTRL
ITAPE=1,
$END
$IN
ØMEGAH=.75,
ØMEGAE=1.7,
ØMEGAP=.75,
EPSGRD=1.E-4,
NDUMP=2000,
NGRID=50,
NGFF=10,
PGFF=1.5,
KEPS=1,
NPRINT=5,
NKPRRT=10,
KPRT=1,2,3,4,5,6,7,8,9,10,
```

```
ITYPE=1,  
IØPT=0,  
ZE(1)=0.,.25,.25,.375,.5,.625,.75,.875,1.,1.125,1.25,  
1.375,1.5,1.625,1.75,1.825,1.9,1.95,2.,
```

```
NZE=19,
```

```
IK= 0,
```

```
$END
```

- Run 4U: read file 4S, restart file 3U; generate file 4U

3D CIRCULAR ARC

```
$CØNTRL
```

```
ITAPE=1,
```

```
$END
```

```
$IN
```

```
ØMEGAH=.75,
```

```
ØMEGAE=1.7,
```

```
ØMEGAP=.75,
```

```
EPSGRD=1.E-5,
```

```
NDUMP=2000,
```

```
NGRID=100,
```

```
NGFF=10,
```

```
PGFF=1.5,
```

```
KEPS=1,
```

```
NPRINT=5,
```

```
NKPRT=10,
```

```
KPRT=1,2,3,4,5,6,7,8,9,10,
```

```
ITYPE=1,
```

```
IØPT=0,
```

```
ZE(1)=0.,.125,.25,.375,.5,.625,.75,.875,1.,1.125,1.25,  
1.375,1.5,1.625,1.75,1.825,1.9,1.95,2.,
```

```
NZE=19,
```

```
IK=0,
```

```
$END
```

- Run 5U: read file 4S, restart file 4U; generate file 5U

3D CIRCULAR ARC

```
$CØNTRL
```

```
ITAPE=1,
```

```
$END
```

```
$IN
```

```
ØMEGAH=.75,
```

```
ØMEGAE=1.7,
```

```
ØMEGAP=.75,
```

```
EPSGRD=1.E-5,
```

```
NDUMP=2000,
```

```
NGRID=50,  
NGFF=10,  
PGFF=1.5,  
KEPS=1,  
NPRINT=10,  
NKPR=10,  
KPRT=1,2,3,4,5,6,7,8,9,10,  
ITYPE=1,  
IOP=0,  
ZE(1)=0.,.125,.25,.375,.5,.625,.75,.875,1.,1.125,1.25,  
1.375,1.5,1.625,1.75,1.825,1.9,1.95,2.,  
NZE=19,  
IK=1,  
SMALLK=.05,  
$END
```

- Run 6U: read file 4S, restart file 5U; generate file 6U

3D CIRCULAR ARC

```
$CØNTRL,  
ITAPE=1,  
$END  
$IN  
ØMEGAH=.75,  
ØMEGAE=1.7,  
ØMEGAP=.75,  
EPSGRD=1.E-5,  
NDUMP=2000,  
NGRID=200,  
NGFF=10,  
PGFF=1.5,  
KEPS=1,  
NPRINT=10,  
NKPR=10,  
KPRT=1,2,3,4,5,6,7,8,9,10,  
ITYPE=1,  
IOP=0,  
ZE(1)=0.,.125,.25,.375,.5,.625,.75,.875,1.,1.125,1.25,  
1.375,1.5,1.625,1.75,1.825,1.9,1.95,2.,  
NZE=19,  
IK=1,  
SMALLK=.1,  
$END
```

7.2.2 Sample Output for TDUTRN Test Cases

The following pages contain a sample of the continuous commentary output for the first 9 cycles of Run 1U in addition to the final printed page for all runs. Also included in the complete final output for the final run.

• SAMPLE OUTPUT FOR RUN 1U

```

STABILITY PARAMETERS (u) = 11500.01
SCALING FACTOR (CP/CDMA2) = 0.12500E000

AT ITERATION 1 THE MAXIMUM TENSION = -0.74324E+000 -0.
AND OCCURRED AT NODE 144
AT ITERATION 2 THE MAXIMUM TENSION = -0.44110E+000 0.
AND OCCURRED AT NODE 970
AT ITERATION 3 THE MAXIMUM TENSION = -0.36657E+000 -0.
AND OCCURRED AT NODE 591
AT ITERATION 4 THE MAXIMUM TENSION = -0.29070E+000 0.
AND OCCURRED AT NODE 1222

AT ITERATION 4 AND AS 1 SCALED PRESSURE COEFFICIENT. UPDATE (FILE TO ITET) =
-0.41573E+01 -0. 0.25934E+01 -0. -11152E+01 -0. -35641E+00 -0.
-0.30574E+01 -0. 0.22239E+01 -0. -60141E+00 -0. -72367E+00 -0.
-0.57412E+01 -0. 0.11654E+02 -0. -62117E+01 -0. -86903E+00 -0.
-0.87053E+01 -0. 0. 0. 0. 0. 0. 0. 0.

AT ITERATION 5 AND AS 1 SCALED PRESSURE COEFFICIENT. UPDATE (FILE TO ITET) =
-0.41573E+01 -0. 0.25934E+01 -0. -11152E+01 -0. -35641E+00 -0.
-0.30574E+01 -0. 0.22239E+01 -0. -60141E+00 -0. -72367E+00 -0.
-0.57412E+01 -0. 0.11654E+02 -0. -62117E+01 -0. -86903E+00 -0.

AT ITERATION 5 AND AS 10 SCALED PRESSURE COEFFICIENT. UPDATE (FILE TO ITET) =
-0.12637E+01 -0. 0.16516E+00 -0. -63191E+01 -0. -17459E+00 -0.
-0.35019E+00 -0. 0.29768E+02 -0. -22660E+01 -0. -39926E+00 -0.
-0.35061E+01 -0. 0.28661E+01 -0. -12500E+01 -0. -12094E+01 -0.
-0.10739E+00 -0. 0. 0. 0. 0. 0. 0.

AT ITERATION 6 AND AS 10 SCALED PRESSURE COEFFICIENT. LD-EW (FILE TO ITET) =
-0.12637E+01 -0. 0.16516E+00 -0. -63191E+01 -0. -17459E+00 -0.
-0.35019E+00 -0. 0.29768E+02 -0. -22660E+01 -0. -39926E+00 -0.
-0.35061E+01 -0. 0.28661E+01 -0. -12500E+01 -0. -11674E+01 -0.

AT ITERATION 6 THE MAXIMUM TENSION = -0.31044E+000 -0.
AND OCCURRED AT NODE 924
AT ITERATION 6 THE MAXIMUM ERROR = -0.31616E+00 0.
AND OCCURRED AT NODE 924
AT ITERATION 7 THE MAXIMUM TENSION = -0.18791E+000 0.
AND OCCURRED AT NODE 889
AT ITERATION 9 THE MAXIMUM TENSION = -0.11366E+000 0.
AND OCCURRED AT NODE 662
AT ITERATION 9 THE MAXIMUM ERROR = -0.13339E+001 0.
AND OCCURRED AT NODE 643

AT ITERATION 9 AND AS 1 SCALED PRESSURE COEFFICIENT. UPDATE (FILE TO ITET) =
-0.31215E+01 -0. 0.20494E+01 -0. -61670E+01 -0. -21160E+01 -0.
-0.14974E+01 -0. 0.15951E+01 -0. -60350E+00 -0. -10684E+01 -0.
-0.14931E+01 -0. 0.15951E+01 -0. -61728E+00 -0. -22614E+00 -0.
-0.30424E+00 -0. 0. 0. 0. 0. 0. 0.

AT ITERATION 9 AND AS 1 SCALED PRESSURE COEFFICIENT. UPDATE (FILE TO ITET) =
-0.15211E+01 -0. 0.20494E+01 -0. -61670E+01 -0. -21160E+01 -0.
-0.14974E+01 -0. 0.15951E+01 -0. -60350E+00 -0. -10684E+01 -0.
-0.14931E+01 -0. 0.15951E+01 -0. -61728E+00 -0. -22614E+00 -0.
-0.30424E+00 -0. 0. 0. 0. 0. 0. 0.
```


... 30 CIRCUMFERENTIAL PITCH ANGLE IN RADIAN

UNSTEADY SOURCE COEFFICIENTS (PER UNIT PITCH ANGLE IN RADIAN)

POLARIZING COEFFICIENTS (PER UNIT PITCH ANGLE IN RADIAN)

AERONAUTICAL SOURCE COEFFICIENTS (PER UNIT PITCH ANGLE IN RADIAN)

STRUCTURAL SOURCE COEFFICIENTS (PER UNIT PITCH ANGLE IN RADIAN)

STRUCTURAL SOURCE COEFFICIENTS (PER UNIT PITCH ANGLE IN RADIAN)

STRUCTURAL SOURCE COEFFICIENTS (PER UNIT PITCH ANGLE IN RADIAN)

UNSTEADY SOURCE COEFFICIENTS (PER UNIT PITCH ANGLE IN RADIAN)

LIFT = 1.0000000000000000E+00.

AERONAUTICAL SOURCE COEFFICIENT = 0.

STRUCTURAL SOURCE COEFFICIENTS (PER UNIT PITCH ANGLE IN RADIAN)

Atmospheric pressure coefficient	-0.293476×10^0	-0.032252×10^1	-0.07652×10^1	-0.45760×10^1
Atmospheric density coefficient	-0.700000×10^0	-0.350000×10^1	-0.150000×10^1	-0.050000×10^1
Atmospheric temperature coefficient	-0.420000×10^0	-0.180000×10^1	-0.070000×10^1	-0.030000×10^1
Atmospheric humidity coefficient	-0.240000×10^0	-0.090000×10^1	-0.030000×10^1	-0.010000×10^1
Atmospheric wind coefficient	-0.120000×10^0	-0.040000×10^1	-0.010000×10^1	-0.003000×10^1
Atmospheric angle of attack coefficient	-0.060000×10^0	-0.020000×10^1	-0.005000×10^1	-0.001000×10^1
Atmospheric angle of sideslip coefficient	-0.030000×10^0	-0.010000×10^1	-0.002000×10^1	-0.000500×10^1
Atmospheric angle of roll coefficient	-0.015000×10^0	-0.005000×10^1	-0.001000×10^1	-0.000200×10^1
Atmospheric angle of yaw coefficient	-0.007500×10^0	-0.002000×10^1	-0.000400×10^1	-0.000100×10^1
Atmospheric angle of pitch coefficient	-0.003750×10^0	-0.001000×10^1	-0.000200×10^1	-0.000050×10^1
Atmospheric angle of roll rate coefficient	-0.001875×10^0	-0.000500×10^1	-0.000100×10^1	-0.000020×10^1
Atmospheric angle of yaw rate coefficient	-0.0009375×10^0	-0.000200×10^1	-0.000040×10^1	-0.000010×10^1
Atmospheric angle of pitch rate coefficient	-0.00046875×10^0	-0.000100×10^1	-0.000010×10^1	-0.000002×10^1
Atmospheric angle of sideslip rate coefficient	-0.000234375×10^0	-0.000050×10^1	-0.000005×10^1	-0.000001×10^1
Atmospheric angle of roll rate squared coefficient	$-0.0001171875 \times 10^0$	-0.000020×10^1	-0.000002×10^1	-0.0000005×10^1
Atmospheric angle of yaw rate squared coefficient	$-0.00005859375 \times 10^0$	-0.000010×10^1	-0.000001×10^1	-0.0000002×10^1
Atmospheric angle of pitch rate squared coefficient	$-0.000029296875 \times 10^0$	-0.000005×10^1	-0.0000005×10^1	-0.0000001×10^1
Atmospheric angle of sideslip rate squared coefficient	$-0.00001464765625 \times 10^0$	-0.000002×10^1	-0.0000002×10^1	-0.00000005×10^1

*** 3-D CIRCULAR A/C ***

WALL NUMBER = 0.00000000
 SURFACE WINDING NUMBER = 0.00000000
 YAW-ELEVATION = 0.00000000
 ALBEDO AND SURFACE ATTENUATION COEFFICIENT = 0.
 SURFACE REFLECTIVITY COEFFICIENT ON C=001 = 0.
 SURFACE REFLECTIVITY (0=001) = 0.
 PITCH AXIS LENGTH = 0.
 WING ASPECT RATIO = 20000E+01
 CP SCALING FACTOR (CP/CHM) = 12050E+00

UNSTEADY FLUX COEFFICIENTS (FOR UNIT PITCH ANGLE IN RADIAN)

LIFT = 1.0000E+02 0.
 WEIGHT AFFECT COEF = .55774E+01 0.

AERONAUTIC COORDINATE = 0.

SPECIFIC LIFT COEFFICIENT = .10293E+02 0.

PRESSURE COEFFICIENTS ON THE AEROFIL (PFW UNIT PITCH ANGLE IN RADIANS)

AERONAUTIC COORDINATE = 0.

.35000E+00
 .42000E+00
 .45000E+00
 .48000E+00

AERONAUTIC COEFFICIENTS (INPUT)

-70000E+01
 -50000E+01
 -30000E+01
 -10000E+01
 -20000E+01

.18000E+00
 .19000E+00
 .17000E+00
 .16000E+00

AERONAUTIC COEFFICIENTS (INPUT 2)

-50517E+01
 -32016E+01
 -69505E+01
 -115201E+01

.45911E+01
 .31169E+01
 .63306E+00
 .90301E+00

AERONAUTIC COEFFICIENTS (INPUT 3)

-47422E+01
 -35665E+01
 -12291E+01

.45913E+01
 .31136E+01
 .61049E+00
 .91109E+00

*** 1-0 CIRCULAR ARC ***

MACH NUMBER = .64000E+00
 STICKSLIP PARAMETER = .11500E+01
 THICKNESS RATIO = .0000E+01
 AIRFOIL ANGLE OF ATTACK (RADIAN) = .0.
 REDUCED FREQUENCY (BASED ON CHORD) = .0.
 SCALED FREQUENCY (OMEGA) = .0.
 PITCH RATIO (X1) = .0.
 WING ASPECT RATIO = .20000E+01
 CP SCALING FACTOR (CP/CSPAN) = .12050E+00

UNSTEADY FORCE COEFFICIENTS (PER UNIT PITCH ANGLE IN RADIANS)
 LIFT = .11416E+02 0.
 MOMENT ABOUT (XSPAN) = .59005E+01 0.

AIRFOIL SPANWISE COORDINATE = 0.

SECTION LIFT COEFFICIENT = .10300E+02 0.

PRESSURE COEFFICIENTS ON THE AIRFOIL (PER UNIT PITCH ANGLE IN RADIANS)

AIRFOIL SPANWISE COORDINATE	0.	.16000E+00	.32000E+00	.55000E+00	.82000E+00	.20000E+00	.00000E+00
0.	.70000E+01	.50000E+00	.42000E+00	.32000E+00	.22000E+00	.13200E+01	.00000E+00
.15000E+00							
.45000E+00							
.10000E+01							

AIRFOIL PRESSURE COEFFICIENTS, UPPER	0.	.50000E+01	.47407E+01	.45975E+01	.45975E+01	.31262E+01	.01050E+00
0.	.50741E+01						
.42039E+01	-0.	-0.	-0.	-0.	-0.	-0.	-0.
.50712E+01	-0.	-0.	-0.	-0.	-0.	-0.	-0.
.20932E+00	-0.	-0.	-0.	-0.	-0.	-0.	-0.

AIRFOIL PRESSURE COEFFICIENTS, LOWER	0.	.50000E+01	.47407E+01	.45975E+01	.45975E+01	.31262E+01	.01050E+00
0.	.50741E+01						
.42039E+01	-0.	-0.	-0.	-0.	-0.	-0.	-0.
.50712E+01	-0.	-0.	-0.	-0.	-0.	-0.	-0.
.20932E+00	-0.	-0.	-0.	-0.	-0.	-0.	-0.

*** 3-D CIRCULAR ***

WALL NUMBER = 0000000000
 CIRCULAR PARAMETERS = 115002.01
 THICKNESS RATIO = 1.0000000000000000
 AEROTL ANGLE OF ATTACK (RADIAN) = 0.
 REFLECTED FREQUENCY (BASED ON COMB) = .200000E+01
 SCALING FREQUENCY (COMB) = 1.000000E+00
 SCALING FREQUENCY (CFL) = 1.000000E+00
 PITCH ASPECT RATIO = 0.
 AIRFOIL ASPECT RATIO = 200000E+01
 CP SCALING FACTOR (CP/CP0000) = .123500E+00

UNREFINED PRESSURE COEFFICIENT (PER UNIT WITCH ANGLE IN RADIANS)

L167 = .110592E+02 - .100000E+01
 M167 = .000000E+00 - .000000E+01 - .002266E+00

AEROTL SPANWISE COORDINATE = 0.

PRESSURE COEFFICIENTS ON THE AIRFOIL (PER UNIT PITCH ANGLE IN RADIANS):

AIRFOIL SPANWISE COORDINATE	UPPER	LOWER
0.000000E+00	.0469102E+01	.760505E+00
.020000E+00	.0431002E+01	.760505E+00
.035000E+00	.0427002E+01	.760505E+00
.050000E+00	.0427002E+01	.760505E+00
.065000E+00	.0427002E+01	.760505E+00
.080000E+00	.0427002E+01	.760505E+00
.095000E+00	.0427002E+01	.760505E+00
.110000E+00	.0427002E+01	.760505E+00
.113020E+00	.0427002E+01	.760505E+00
.117300E+00	.0427002E+01	.760505E+00
.121700E+00	.0427002E+01	.760505E+00
.126100E+00	.0427002E+01	.760505E+00
.130500E+00	.0427002E+01	.760505E+00
.134900E+00	.0427002E+01	.760505E+00
.139300E+00	.0427002E+01	.760505E+00
.143700E+00	.0427002E+01	.760505E+00
.148100E+00	.0427002E+01	.760505E+00
.152500E+00	.0427002E+01	.760505E+00
.156900E+00	.0427002E+01	.760505E+00
.161300E+00	.0427002E+01	.760505E+00
.165700E+00	.0427002E+01	.760505E+00
.170100E+00	.0427002E+01	.760505E+00
.174500E+00	.0427002E+01	.760505E+00
.178900E+00	.0427002E+01	.760505E+00
.183300E+00	.0427002E+01	.760505E+00
.187700E+00	.0427002E+01	.760505E+00
.192100E+00	.0427002E+01	.760505E+00
.196500E+00	.0427002E+01	.760505E+00
.200900E+00	.0427002E+01	.760505E+00
.205300E+00	.0427002E+01	.760505E+00
.209700E+00	.0427002E+01	.760505E+00
.214100E+00	.0427002E+01	.760505E+00
.218500E+00	.0427002E+01	.760505E+00
.222900E+00	.0427002E+01	.760505E+00
.227300E+00	.0427002E+01	.760505E+00
.231700E+00	.0427002E+01	.760505E+00
.236100E+00	.0427002E+01	.760505E+00
.240500E+00	.0427002E+01	.760505E+00
.244900E+00	.0427002E+01	.760505E+00
.249300E+00	.0427002E+01	.760505E+00
.253700E+00	.0427002E+01	.760505E+00
.258100E+00	.0427002E+01	.760505E+00
.262500E+00	.0427002E+01	.760505E+00
.266900E+00	.0427002E+01	.760505E+00
.271300E+00	.0427002E+01	.760505E+00
.275700E+00	.0427002E+01	.760505E+00
.280100E+00	.0427002E+01	.760505E+00
.284500E+00	.0427002E+01	.760505E+00
.288900E+00	.0427002E+01	.760505E+00
.293300E+00	.0427002E+01	.760505E+00
.297700E+00	.0427002E+01	.760505E+00
.302100E+00	.0427002E+01	.760505E+00
.306500E+00	.0427002E+01	.760505E+00
.310900E+00	.0427002E+01	.760505E+00
.315300E+00	.0427002E+01	.760505E+00
.319700E+00	.0427002E+01	.760505E+00
.324100E+00	.0427002E+01	.760505E+00
.328500E+00	.0427002E+01	.760505E+00
.332900E+00	.0427002E+01	.760505E+00
.337300E+00	.0427002E+01	.760505E+00
.341700E+00	.0427002E+01	.760505E+00
.346100E+00	.0427002E+01	.760505E+00
.350500E+00	.0427002E+01	.760505E+00
.354900E+00	.0427002E+01	.760505E+00
.359300E+00	.0427002E+01	.760505E+00
.363700E+00	.0427002E+01	.760505E+00
.368100E+00	.0427002E+01	.760505E+00
.372500E+00	.0427002E+01	.760505E+00
.376900E+00	.0427002E+01	.760505E+00
.381300E+00	.0427002E+01	.760505E+00
.385700E+00	.0427002E+01	.760505E+00
.390100E+00	.0427002E+01	.760505E+00
.394500E+00	.0427002E+01	.760505E+00
.398900E+00	.0427002E+01	.760505E+00
.403300E+00	.0427002E+01	.760505E+00
.407700E+00	.0427002E+01	.760505E+00
.412100E+00	.0427002E+01	.760505E+00
.416500E+00	.0427002E+01	.760505E+00
.420900E+00	.0427002E+01	.760505E+00
.425300E+00	.0427002E+01	.760505E+00
.429700E+00	.0427002E+01	.760505E+00
.434100E+00	.0427002E+01	.760505E+00
.438500E+00	.0427002E+01	.760505E+00
.442900E+00	.0427002E+01	.760505E+00
.447300E+00	.0427002E+01	.760505E+00
.451700E+00	.0427002E+01	.760505E+00
.456100E+00	.0427002E+01	.760505E+00
.460500E+00	.0427002E+01	.760505E+00
.464900E+00	.0427002E+01	.760505E+00
.469300E+00	.0427002E+01	.760505E+00
.473700E+00	.0427002E+01	.760505E+00
.478100E+00	.0427002E+01	.760505E+00
.482500E+00	.0427002E+01	.760505E+00
.486900E+00	.0427002E+01	.760505E+00
.491300E+00	.0427002E+01	.760505E+00
.495700E+00	.0427002E+01	.760505E+00
.500100E+00	.0427002E+01	.760505E+00
.504500E+00	.0427002E+01	.760505E+00
.508900E+00	.0427002E+01	.760505E+00
.513300E+00	.0427002E+01	.760505E+00
.517700E+00	.0427002E+01	.760505E+00
.522100E+00	.0427002E+01	.760505E+00
.526500E+00	.0427002E+01	.760505E+00
.530900E+00	.0427002E+01	.760505E+00
.535300E+00	.0427002E+01	.760505E+00
.539700E+00	.0427002E+01	.760505E+00
.544100E+00	.0427002E+01	.760505E+00
.548500E+00	.0427002E+01	.760505E+00
.552900E+00	.0427002E+01	.760505E+00
.557300E+00	.0427002E+01	.760505E+00
.561700E+00	.0427002E+01	.760505E+00
.566100E+00	.0427002E+01	.760505E+00
.570500E+00	.0427002E+01	.760505E+00
.574900E+00	.0427002E+01	.760505E+00
.579300E+00	.0427002E+01	.760505E+00
.583700E+00	.0427002E+01	.760505E+00
.588100E+00	.0427002E+01	.760505E+00
.592500E+00	.0427002E+01	.760505E+00
.596900E+00	.0427002E+01	.760505E+00
.601300E+00	.0427002E+01	.760505E+00
.605700E+00	.0427002E+01	.760505E+00
.610100E+00	.0427002E+01	.760505E+00
.614500E+00	.0427002E+01	.760505E+00
.618900E+00	.0427002E+01	.760505E+00
.623300E+00	.0427002E+01	.760505E+00
.627700E+00	.0427002E+01	.760505E+00
.632100E+00	.0427002E+01	.760505E+00
.636500E+00	.0427002E+01	.760505E+00
.640900E+00	.0427002E+01	.760505E+00
.645300E+00	.0427002E+01	.760505E+00
.649700E+00	.0427002E+01	.760505E+00
.654100E+00	.0427002E+01	.760505E+00
.658500E+00	.0427002E+01	.760505E+00
.662900E+00	.0427002E+01	.760505E+00
.667300E+00	.0427002E+01	.760505E+00
.671700E+00	.0427002E+01	.760505E+00
.676100E+00	.0427002E+01	.760505E+00
.680500E+00	.0427002E+01	.760505E+00
.684900E+00	.0427002E+01	.760505E+00
.689300E+00	.0427002E+01	.760505E+00
.693700E+00	.0427002E+01	.760505E+00
.698100E+00	.0427002E+01	.760505E+00
.702500E+00	.0427002E+01	.760505E+00
.706900E+00	.0427002E+01	.760505E+00
.711300E+00	.0427002E+01	.760505E+00
.715700E+00	.0427002E+01	.760505E+00
.720100E+00	.0427002E+01	.760505E+00
.724500E+00	.0427002E+01	.760505E+00
.728900E+00	.0427002E+01	.760505E+00
.733300E+00	.0427002E+01	.760505E+00
.737700E+00	.0427002E+01	.760505E+00
.742100E+00	.0427002E+01	.760505E+00
.746500E+00	.0427002E+01	.760505E+00
.750900E+00	.0427002E+01	.760505E+00
.755300E+00	.0427002E+01	.760505E+00
.759700E+00	.0427002E+01	.760505E+00
.764100E+00	.0427002E+01	.760505E+00
.768500E+00	.0427002E+01	.760505E+00
.772900E+00	.0427002E+01	.760505E+00
.777300E+00	.0427002E+01	.760505E+00
.781700E+00	.0427002E+01	.760505E+00
.786100E+00	.0427002E+01	.760505E+00
.790500E+00	.0427002E+01	.760505E+00
.794900E+00	.0427002E+01	.760505E+00
.799300E+00	.0427002E+01	.760505E+00
.803700E+00	.0427002E+01	.760505E+00
.808100E+00	.0427002E+01	.760505E+00
.812500E+00	.0427002E+01	.760505E+00
.816900E+00	.0427002E+01	.760505E+00
.821300E+00	.0427002E+01	.760505E+00
.825700E+00	.0427002E+01	.760505E+00
.830100E+00	.0427002E+01	.760505E+00
.834500E+00	.0427002E+01	.760505E+00
.838900E+00	.0427002E+01	.760505E+00
.843300E+00	.0427002E+01	.760505E+00
.847700E+00	.0427002E+01	.760505E+00
.852100E+00	.0427002E+01	.760505E+00
.856500E+00	.0427002E+01	.760505E+00
.860900E+00	.0427002E+01	.760505E+00
.865300E+00	.0427002E+01	.760505E+00
.869700E+00	.0427002E+01	.760505E+00
.874100E+00	.0427002E+01	.760505E+00
.878500E+00	.0427002E+01	.760505E+00
.882900E+00	.0427002E+01	.760505E+00
.887300E+00	.0427002E+01	.760505E+00
.891700E+00	.0427002E+01	.760505E+00
.896100E+00	.0427002E+01	.760505E+00
.900500E+00	.0427002E+01	.760505E+00
.904900E+00	.0427002E+01	.760505E+00
.909300E+00	.0427002E+01	.760505E+00
.913700E+00	.0427002E+01	.760505E+00
.918100E+00	.0427002E+01	.760505E+00
.922500E+00	.0427002E+01	.760505E+00
.926900E+00	.0427002E+01	.760505E+00
.931300E+00	.0427002E+01	.760505E+00
.935700E+00	.0427002E+01	.760505E+00
.939100E+00	.0427002E+01	.76050

• FINAL OUTPUT FOR RUN 6U (CONT'D)

卷之三

0-11517-00
000-2015511
0-11517-00

REPORT	PRESSURE	Coefficient	Upper	Lower		
1	0.25170E+00	1.00000E+00	-0.07095E+00	1.21336E+00	-3.00000E+00	1.00207E+0
2	0.30070E+00	1.00000E+00	-0.20503E+00	0.74600E+00	-3.00000E+00	1.35500E+00
3	0.35070E+00	1.00000E+00	-0.26501E+00	0.67132E+00	-3.00000E+00	1.55500E+00
4	0.39570E+00	1.00000E+00	-0.30508E+00	0.61972E+00	-2.36528E+00	2.17460E+00
5	0.43070E+00	1.00000E+00	-0.33511E+00	0.58000E+00	-2.17460E+00	2.79776E+00
6	0.46570E+00	1.00000E+00	-0.36514E+00	0.54000E+00	-2.00000E+00	3.00000E+00
7	0.50070E+00	1.00000E+00	-0.39517E+00	0.50000E+00	-1.80000E+00	3.20000E+00
8	0.53570E+00	1.00000E+00	-0.42520E+00	0.46000E+00	-1.60000E+00	3.40000E+00
9	0.57070E+00	1.00000E+00	-0.45523E+00	0.42000E+00	-1.40000E+00	3.60000E+00
10	0.60570E+00	1.00000E+00	-0.48526E+00	0.38000E+00	-1.20000E+00	3.80000E+00
11	0.64070E+00	1.00000E+00	-0.51529E+00	0.34000E+00	-1.00000E+00	4.00000E+00
12	0.67570E+00	1.00000E+00	-0.54532E+00	0.30000E+00	-8.00000E+00	4.20000E+00
13	0.71070E+00	1.00000E+00	-0.57535E+00	0.26000E+00	-6.00000E+00	4.40000E+00
14	0.74570E+00	1.00000E+00	-0.60538E+00	0.22000E+00	-4.00000E+00	4.60000E+00
15	0.78070E+00	1.00000E+00	-0.63541E+00	0.18000E+00	-2.00000E+00	4.80000E+00
16	0.81570E+00	1.00000E+00	-0.66544E+00	0.14000E+00	-1.00000E+00	5.00000E+00
17	0.85070E+00	1.00000E+00	-0.69547E+00	0.10000E+00	-1.00000E+00	5.20000E+00
18	0.88570E+00	1.00000E+00	-0.72550E+00	0.60000E+00	-1.00000E+00	5.40000E+00
19	0.92070E+00	1.00000E+00	-0.75553E+00	0.20000E+00	-1.00000E+00	5.60000E+00
20	0.95570E+00	1.00000E+00	-0.78556E+00	-0.20000E+00	-1.00000E+00	5.80000E+00

SCHNEIDER, SCHAFFNER, AND WILHELM

• FINAL OUTPUT FOR RUN 6U (CONT'D)

418P01 PRESSURE COEFFICIENTS, UPFRONT ■
 05.94613E+00 1.67500E+00 -4.16132E+00 1.15000E+00 -5.82015E+00 1.04610E+00
 03.0525E+00 8.1548E+01 -2.15013E+00 0.92943E+01 0.66795E+01 0.61550E+01
 06.20742E+00 2.02267E+01 -3.57604E+00 -7.74027E+01 -1.76666E+01 1.02361E+00
 08.12135E+02 -3.66355E+02

418P01 PRESSURE COEFFICIENTS, LD-FR ■
 9.93132E+00 -1.67500E+00 4.16132E+00 -1.15000E+00 3.82015E+00 -1.04610E+00
 3.0525E+00 -8.1548E+01 2.15013E+00 0.92943E+01 0.66795E+01 0.61550E+01
 0.26474E+00 -2.22267E+01 3.57604E+00 7.74027E+01 1.76666E+01 1.02361E+00
 04.12013E+02 3.66355E+02

418P01 SPANWISE COORDINATE ■ 1.75000E+00 SECTION LIFT COEFFICIENT ■ 5.54041E+00 -1.16639E+00

418P01 PRESSURE COEFFICIENTS, UPFR ■
 5.27170E+00 1.15411E+00 -3.0337E+00 9.16891E+01 -1.27116E+00 8.28421E+01
 -2.49794E+00 6.24229E+01 -2.24630E+00 5.75508E+01 -2.30002E+00 6.38302E+01
 -7.47747E+01 -3.25197E+01 7.77006E+01 -2.03729E+01 -3.61599E+01 -1.19266E+01
 7.15221E+02 -3.46027E+02

418P01 SPANWISE COORDINATE ■ 1.90000E+00 SECTION LIFT COEFFICIENT ■ 9.15309E+00 -8.89770E+01
 418P01 PRESSURE COEFFICIENTS, LD-FR ■
 5.27170E+00 -1.15411E+00 3.0337E+00 -9.16891E+01 1.27116E+00 -8.28421E+01
 2.49794E+00 -6.24229E+01 2.24630E+00 5.75508E+01 2.30002E+00 6.38302E+01
 7.47747E+01 -3.25197E+01 7.77006E+01 2.03729E+01 3.61599E+01 1.19266E+01
 -7.15221E+02 3.46027E+02

418P01 SPANWISE COORDINATE ■ 1.90000E+00 SECTION LIFT COEFFICIENT ■ 9.15309E+00 -8.89770E+01

418P01 PRESSURE COEFFICIENTS, UPFR ■
 0.37446E+00 1.64709E+00 -2.04162E+00 6.87704E+01 -2.53730E+00 6.05800E+01
 1.84642E+00 -8.01460E+01 1.78759E+00 4.32648E+01 -2.04331E+00 4.16037E+01
 0.81649E+00 7.20195E+02 5.82674E+01 0.56535E+02 -5.82674E+01 0.20701E+02
 -0.30101E+01 0.35057E+02

418P01 SPANWISE COEFFICIENTS, LD-FR ■
 0.37446E+00 -1.64709E+00 2.04162E+00 -6.87704E+01 2.53730E+00 -6.05800E+01
 1.84642E+00 8.01460E+01 -1.78759E+00 4.32648E+01 2.04331E+00 4.16037E+01
 0.81649E+00 2.17456E+01 -1.17844E+00 2.01400E+01 -1.22649E+00 2.22522E+01
 -0.30044E+01 -7.08415E+02 0.21707E+01 -3.41502E+02 -2.36300E+02 -8.07566E+02
 1.30071E+01 0.35057E+02

418P01 SPANWISE COEFFICIENTS, LD-FR ■ 2.00000E+00 SECTION LIFT COEFFICIENT ■ 2.74197E+00 -5.56909E+01

418P01 PRESSURE COEFFICIENTS, UPFR ■
 0.140244E+00 7.23678E+01 -2.02605E+00 4.56110E+01 -1.66691E+00 -5.91742E+01 1.65161E+00 -3.16916E+00
 1.84642E+00 -8.01460E+01 1.78759E+00 4.32648E+01 2.04331E+00 4.16037E+01 -2.35730E+00 1.79125E+00
 0.81649E+00 2.17456E+01 -1.17844E+00 2.01400E+01 -1.22649E+00 2.22522E+01 -1.25235E+00 1.15015E+02
 -0.30044E+01 -7.08415E+02 0.21707E+01 -3.41502E+02 -2.36300E+02 -8.07566E+02 1.04662E+01

418P01 SPANWISE COEFFICIENTS, LD-FR ■
 0.140244E+00 -7.23678E+01 2.02605E+00 -4.56110E+01 1.66691E+00 -5.91742E+01 1.65161E+00 -3.16916E+00
 1.84642E+00 8.01460E+01 -1.78759E+01 4.32648E+01 -2.04331E+00 4.16037E+01 2.35730E+00 -1.79125E+00
 0.81649E+00 2.17456E+01 -1.17844E+01 2.01400E+01 -1.22649E+00 2.22522E+01 -1.25235E+00 -1.15015E+02
 -0.30044E+01 -7.08415E+03 0.21707E+01 3.41502E+02 2.36300E+02 8.07566E+02 -1.04662E+01

*** 1-D CIRCULAR ANC ***

MACH NUMBER = 0.00000E+01
 STOCHASTIC PREDICTOR = 1.15900E+00
 TURBULENCE SEED = 0.00000E+02
 AEROFIL ANGLE OF ATTACK (deg) = 0.
 SCALED PRESSURE (BASED ON CHW00) = 1.00000E+01
 SCALED PRESSURE (PDEGA) = 3.20173E-01
 PITCH AXIS ROLL = 0.
 DILS ASPECT RATIO = 2.00000E+00
 CP CALCULUS FACTOR (CP/CP000) = 1.26590E-01

UNSTRUCTURED PLATE COORDINATES (PDE UNIT PITCH ANGLE IN RADIAN)

LIFT = 1.27049E+01 -3.08726E+00
 WIND = 4.6507 (LIFT) = 5.18001E+00 -9.97192E+01

AEROFIL SPANWISE COORDINATE = 0.

SECTION LIFT COEFFICIENT = 0.10540E+00 -2.56641E+00

* * * * * COORDINATE ON THE AEROFIL (PDE UNIT PITCH ANGLE IN RADIANS)

AEROFIL STREAMWISE COORDINATE	0	7.00000E-01	1.00000E-01	2.10000E-01	2.00000E-01
	7.00000E-01	5.00000E-01	5.50000E-01	6.00000E-01	6.50000E-01
	4.20000E-01				
	0.30000E-01				
	1.00000E-00				

AEROFIL POSITION COORDINATE	0	7.00000E-02	1.00000E-01	2.10000E-01	2.00000E-01
	7.00000E-02	5.00000E-01	5.50000E-01	6.00000E-01	6.50000E-01
	4.20000E-01				
	0.30000E-01				
	1.00000E-00				

AEROFIL POSITION COORDINATE, UPPTS

-6.35024E-01 2.25310E+00 0.71147E+01 1.57457E+00 -6.37673E+00 1.67132E+00 -6.11074E+00 1.39520E+00 -3.09723E+00 1.36220E+00
 -1.73631E+00 1.20210E+00 0.2.06701E+00 0.37414E+01 -2.04529E+00 0.60026E+01 -5.35076E+00 1.13507E+00 -2.63546E+00 1.05751E+00
 -0.11604E+00 1.94240E+00 -0.70150E+00 1.00010E+00 0.2.27059E+00 3.00013E+01 -1.33110E+00 -9.72575E+02 -6.00050E+01 -7.00077E+00
 -0.02404E+01 -3.82700E+02

AEROFIL POSITION COORDINATE, L0FF

6.03000E+00 -2.25170E+00 4.71147E+00 -1.37457E+00 1.17671E+00 -1.07132E+00 0.115745E+00 -1.39510E+00 1.39702E+00 -1.36220E+00
 1.73431E+00 1.20210E+00 0.2.06701E+00 0.37414E+01 -2.04529E+00 0.60026E+01 -5.35076E+00 1.13507E+00 -2.63546E+00 1.05751E+00
 5.10640E+00 -1.94240E+00 0.70150E+00 1.00010E+00 0.2.27059E+00 3.00013E+01 -1.33110E+00 -9.72575E+02 -6.00050E+01 -7.00077E+00
 2.02010E+01 3.82700E+02

8.0 REFERENCES

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5. Murman, E.M., and Cole, J.D., "Calculation of Plane Steady Transonic Flows," AIAA Paper 70-188, June 1970.
6. Krupp, J.A., "The Numerical Calculation of Plane Steady Transonic Flows Past Thin Lifting Airfoils," Boeing Scientific Research Laboratories, D180-12958-1, June 1971.
7. Klunker, E.B., "Contribution to Methods for Calculating the Flow about Thin Lifting Wings at Transonic Speeds," NASA TN D-6530, November 1971.
8. Bailey, F.R., and Steger, J.L., "Relaxation Techniques for Three-Dimensional Transonic Flows About Wings," AIAA Paper 72-189, San Diego, California, 1972.
9. Newman, P.A., and Klunker, E.B., "Computation of Transonic Flow About Finite Lifting Wings," AIAA Journal Vol. 10, No. 7, p. 971, 1972.

APPENDIX A

FORTRAN LISTING OF TDSTRN

A FORTRAN listing of the source deck for the TDSTRN program is presented in the following pages. The program, as configured here, requires 70.5_sK words to load and 57.0_sK words to execute. In this configuration the programs fit into small core of the CDC 7600.

```

PROGRAM TDSTRN (INPUT,OUTPUT,TAPE5=INPUT,TAPE6=OUTPUT,TAPE7,
1 TAPE8)
REAL KCAP,M8,IWTNG
COMMON /DELTA/ DX(40),DY(40),DZ(20),AX1(40),AX2(40),BX1(40),
1 BX2(40),CX(40),AY1(40),AY2(40),AZ1(20),AZ2(20),X(40),Y(40),
2 Z(20),FPU(800),FPL(800),PHIUB(800),IM,IM1,JM,JM1,KM,KM1,JW,
3 JWP1,JWM1,ITE,ILE,KSPAN,DYBU1,DYBU2,DYBL1,DYBL2,ALPHA,DEL,M8,
4 GAM,KCAP,NDB,TITLE(8),DOUB,IWING,ZSPAN,NKPRT,KPRT(20)
COMMON /COEFF/ A(40),B(40),C(40),D(40),PHI(11500)
COMMON /GAMMA/ GAMTE1(20),GAMTE(20),PGFF,GAMFF(20)
COMMON /INTERP/ ZE(25),NZE
DIMENSION PHI0C(40),PHI0G(40),OMEGA(40),V(40),EPSGRD(3)
NAMELIST /IN/ X,Y,Z,IM,JM,KM,ILE,ITE,JW,KSPAN,ZSPAN,M8,GAM,DEL,
1 ALPHA,GAMFF,OMEGAH,OMEGAE,OMEGAP,EPSCOL,EPSGRD,NDUMP,NCOL,
2 NGRID,NGFF,PGFF,KFPS,IK,NPRINT,NKPRT,KPRT,ZF,NZE
NAMELIST /CTRL/ ITAPE
DATA AL,BET /,.5,.5/
C
C TO RESTART PROGRAM, COPY THE DATA FOR RESTART FROM TAPE7 TO A DISC
C FILE TAPE8, POSITION TAPE7 AT THE END OF THE LAST FILE ON THE TAPE
C SO NEW DATA MAY BE WRITTEN ON THE TAPE WITHOUT LOSING ANY OF THE
C OLD DATA
C
READ (5,912) (TITLE(I),I=1,8)
READ (5,CTRL)
IF (ITAPE,EQ,0) GO TO 10
C READ DATA FROM RESTART TAPE
READ (8) NITERG,IM,IM1,JM,JM1,KM,KM1,JW,JWP1,JWM1,ITE,ILE,
1 KSPAN,KCAP,DEL,ALPHA,NDB,M8,GAM,DYBU1,DYBU2,DYBL1,DYBL2,
2 DOUB,ZSPAN
READ (8) (X(I),DX(I),AX1(I),AX2(I),BX1(I),BX2(I),CX(I),I=1,IM)
READ (8) (Y(I),DY(I),AY1(I),AY2(I),I=1,JM)
READ (8) (Z(I),DZ(I),AZ1(I),AZ2(I),I=1,KM)
L=ITE+KM
READ (8) (FPU(I),FPL(I),PHIUB(I),I=1,L)
READ (8) (GAMTE(I),GAMFF(I),I=1,KSPAN)
L=IM+JM+KM
READ (8) (PHI(I),I=1,L)
IK=0
READ (5,IN)
C THE IK OPTION IS USED TO BOOT STRAP TO DIFFERENT MACH NUMBERS,
C AIRFOIL THICKNESSES AND/OR ANGLES OF ATTACK MAKE SURE YOU HAVE INPUT
C THE NEW M8, DEL AND/OR ALPHA
IF (IK,EQ,0) GO TO 1
KCAP=(1.-M8**2)/((1.+GAM)*DEL+M8**2)**.6666666667
CALL INITAL
CALL FARFLD
1 CONTINUE
SK=SQRT(KCAP)
DO 2 I=1,KSPAN
GAMTE1(I)=GAMTE(I)
2 CONTINUE
WRITE (6,900)
WRITE (6,901) NITERG
NITERG=0

```

```

GO TO 15
C START PROBLEM FROM SCRATCH
10 CONTINUE
READ (5,IN)
KCAP=((1.+MB**2)/((1.+GAM)*DEL*MA**2))**,6666666667
R=SQRT(KCAP)
DO 3 I=1,KSPAN
GAMTE(I)=GAMFF(I)
GAMTE1(I)=GAMFF(I)
3 CONTINUE
NITERG=0
NDB=0
IM1=IM-1
JM1=JM-1
KM1=KM-1
JWP1=JW+1
JWM1=JW+1
C INITIALIZE FINITE DIFFERENCE COEFFICIENTS AND FARFIELD
CALL INITAL
CALL FARFLD
C INITIAL GUESS FOR SUBSONIC CASE (INTERIOR ONLY)
DO 20 K=1,KM1
MP=IM*JM*(K-1)
Z2=Z(K)**2
DO 30 I=2,IM1
M=MP+(I-1)*JM
X2=X(I)**2
CON=X(I)*DOUB/(6.2831853)
DO 40 J=2,JM1
L=M+J
R=SQRT(X2+KCAP*(Y(J)**2+Z2))
IF (R.EQ.0.) GO TO 41
PHI(L)=CON/R**3
IF (ABR(PHI(L)),GT,1.) PHI(L)=SIGN(1.,X(I))
GO TO 40
41 CONTINUE
PHI(L)=PHI(L-JM)
40 CONTINUE
30 CONTINUE
20 CONTINUE
L=ITE*KM
DO 5 I=1,L
PHIUB(I)=0.
5 CONTINUE
M=(ILE-2)*JM+JW
KK=(ILE-1)*KM
DO 47 K=1,KSPAN
L=M+IM*JM*(K-1)
PHIUB(KK+K)=PHI(L)
47 CONTINUE
15 CONTINUE
WRITE (6,IN)
WRITE (6,900)
CPCPB=DEL**,6666666667/((1.+GAM)*MB**2)**,3333333333
WRITE (6,913) KCAP,CPCPB

```

```

      KGRD=1
C RE-CYCLE POINT FOR GRID ITERATION
75 CONTINUE
  ERROR=0.
  NIT=NITERG
  NITERG=NITERG+1
  IF (MOD(NITERG,NPRINT),EQ,0) CALL PRINT(NIT)
  IF (MOD(NITERG,NGFF),NE,0) GO TO 76
  CALL GAMFJN
  CALL FARFLD
  WRITE (6,910) NITERG,IWING,GAMTE(1),GAMFF(1),GAMTE(KSPAN),
  1 GAMFF(KSPAN)
76 CONTINUE
C BEGIN LOOP ON THE PLANES (Z DIRECTION)
  IMJM=IMJM
  DO 100 K=1,KM1
  MP=IMJM*(K-1)
C CHECK FOR AIRFOIL (CORRECT PLANE)
  IFOIL=0
  IF (K,LE,KSPAN) IFOIL=1
C BEGIN LOOP ON A GIVEN PLANE (X DIRECTION)
  DO 200 I=2,IM1
  MBMP+(I-1)*JM
C CHECK FOR AIRFOIL (CORRECT COLUMN)
  IFLAG=0
  IF (IFOIL,EQ,1,AND,ILE,LE,I,AND,I,LE,ITE) IFLAG=1
  IF (IFLAG,EQ,1) NS=(I-1)*KM+K
C SAVE THIS COLUMN OF PHI
  DO 201 J=2,JM1
  L=JM+J
  PHI0G(J)=PHI(L)
201 CONTINUE
  NITERC=0
C LOOP BACK POINT FOR COLUMN ITERATION
250 CONTINUE
  NITERC=NITERC+1
  IF (NITERC,GT,NCOL) GO TO 394
C SAVE PREVIOUS PHI FOR COLUMN ITERATION
  DO 202 J=2,JM1
  L=JM+J
  PHI0C(J)=PHI(L)
202 CONTINUE
C BEGIN LOOP ON COLUMN (Y DIRECTION)
  DO 300 J=2,JM1
C CALCULATE CELL INDICES
  L=JM+J
  LR=LM+JM
  LL=LM-JM
  LLL=LL-JM
  IF (I,EQ,2) LLL=LL
  LABL+1
  LBBL=1
  LPBL=IMJM
  LBKL=L-IMJM
  IF (K,EQ,1) LBKL=LF

```

```

      PHI=PHI(LR)
      PHI=PHI(LL)
      PHI=PHI(LLL)
      PHI=BK*PHI(LBK)
      IF (IFOIL,FQ,0,OR,J,NE,JW) GO TO 301
      IF (I,EQ,ILE-1) PHI(LR)=.5*(PHIUR((ILE-1)*KM+K)+PHI(LR))
      IF (I,EQ,ITE+1) PHI(LL)=.5*(PHIUR((ITE-1)*KM+K)+PHI(LL))
      IF (I,EQ,ITE+1) PHI(LLL)=.5*(PHIUR((ITE-2)*KM+K)+PHI(LLL))
      IF (I,EQ,ITE+2) PHI(LLL)=.5*(PHIUR((ITE-1)*KM+K)+PHI(LLL))

301 CONTINUE
      IF (ILE,LE,I,AND,I,LE,ITE,AND,J,EQ,JW,AND,K,EG,KSPAN+1)
      1 PHI(LBK)=.5*(PHIUR((I-1)*KM+KSPAN)+PHI(LBK))
      V(J)=KCAP=AX1(I-1)*(PHI(L)-PHI(LL))-AX2(I-1)*(PHI(LL)-PHI(LLL))
C SET UP TRIDIAGONAL MATRIX TO SOLVE FOR PHI(I,J,K)
C A + PHI(I,J+1,K) + R * PHI(I,J,K) + C * PHI(I,J-1,K) = D
      IF (IFLAG,EQ,1,AND,J,EQ,JWP1) GO TO 350
      IF (IFLAG,EQ,1,AND,J,EQ,JW) GO TO 360
      IF (IFLAG,EQ,1,AND,J,EQ,JWM1) GO TO 370
      PART=0.
      IF (I,LE,ITE,OR,IFOIL,FQ,0) GO TO 302
C KUTTA CONDITION
      SIGI=(X(I)-1.)*(GAMFF(K)-GAMTE(K))/(X(IM1)-1.)*GAMTE(K)
      IF (J,EQ,JWM1) PART=.5*AY1(J)*SIGI
      IF (J,EQ,JW) PART=.5*(AY1(J)-AY2(J))*SIGI
      IF (J,EQ,JWP1) PART=-.5*AY2(J)*SIGI
      302 CONTINUE
      VV=BKCAP=AX1(I)*(PHI(LR)-PHI(L))-AX2(I)*(PHI(L)-PHI(LLL))
      IF (VV,LT,0.) GO TO 320
      IF (V(J),LT,0.) GO TO 380
C *****
C *
C ***** ELLIPTIC DIFFERENCING *****
C *****
      OMEGA(J)=OMEGAFA
      A(J)=AY1(J)
      B(J)=-(VV+(BX1(I)+BX2(I))+AY1(J)+AY2(J))-AZ1(K)-AZ2(K)
      C(J)=AY2(J)
      D(J)=-VV*(BX1(I)+PHI(LR)+BX2(I)*PHI(LL))+PART-(AZ1(K)*PHI(LF)+I
      AZ2(K)*PHI(LBK))
      IF (J,EQ,2) GO TO 303
      IF (J,EQ,IM1) GO TO 304
      GO TO 390
C BOTTOM BOUNDARY
303 CONTINUE
      D(J)=D(J)-AY2(J)*PHI(LB)
      GO TO 390
C TOP BOUNDARY
304 CONTINUE
      D(J)=D(J)-AY1(J)*PHI(LA)
      GO TO 390
320 CONTINUE
      IF (V(J),GT,0.) GO TO 340
C *****
C *
C ***** HYPERBOLIC DIFFERENCING *****
C *****
      OMEGA(J)=OMEGAH

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VVVKCAP=CX(I-1)*(PHI(L)-PHI(LL))-CX(I+2)*(PHI(LL)-PHI(LLL))
A(J)=AY1(J)
B(J)=VV*BX1(I-1)-AY1(J)-AY2(J)-AZ1(K)-AZ2(K)
C(J)=AY2(J)
D(J)=VV*(BX1(I-1)+PHI(LL)+BX2(I-1)*(PHI(LL)-PHI(LLL)))+PART-
1 (AZ1(K)*PHI(LF)+AZ2(K)*PHI(LBK))
IF (J.EQ.2) GO TO 322
IF (J.EQ.JM1) GO TO 323
GO TO 390
C BOTTOM BOUNDARY
322 CONTINUE
D(J)=D(J)-AY2(J)*PHI(LB)
GO TO 390
C TOP BOUNDARY
323 CONTINUE
D(J)=D(J)-AY1(J)*PHI(LA)
GO TO 390
C *****
C *****
C ***** PARABOLIC DIFFERENCING *****
340 CONTINUE
OMEGA(J)=OMEGAP
A(J)=AY1(J)
B(J)=VV*BX1(I-1)-AY1(J)-AY2(J)-AZ1(K)-AZ2(K)
C(J)=AY2(J)
D(J)=VV*(BX1(I-1)+BX2(I-1))*PHI(LL)-VV*BX2(I-1)*PHI(LLL)+PART-
1 (AZ1(K)*PHI(LF)+AZ2(K)*PHI(LBK))
IF (J.EQ.2) GO TO 342
IF (J.EQ.JM1) GO TO 343
GO TO 390
C BOTTOM BOUNDARY
342 CONTINUE
D(J)=D(J)-AY2(J)*PHI(LB)
GO TO 390
C TOP BOUNDARY
343 CONTINUE
D(J)=D(J)-AY1(J)*PHI(LA)
GO TO 390
C *****
C *****
C ***** SHOCK POINT DIFFERENCING *****
380 CONTINUE
OMEGA(J)=OMEGAE
A(J)=AY1(J)
B(J)=AL*VV*(BX1(I)+BX2(I))+BET*V(J)*BX1(I-1)-AY1(J)-AY2(J)-
1 AZ1(K)-AZ2(K)
C(J)=AY2(J)
D(J)=AL*VV*(BX1(I)*PHI(LR)+BX2(I)*PHI(LL))+BET*V(J)*(BX1(I-1)*
1 PHI(LL)+BX2(I-1)*(PHI(LL)-PHI(LLL)))-(AZ1(K)*PHI(LF)+AZ2(K)*
2 PHI(LBK))
GO TO 390
C *****
C *****
C ***** AIRFOIL UPPER SURFACE BOUNDARY CONDITION *****
390 CONTINUE

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VV=KCAP=AX1(I)*(PHI(LR)=PHI(L))-AX2(I)*(PHI(L)=PHI(LL))
IF (VV,LT,0.) GO TO 351
IF (V(J),LT,0.) GO TO 353
C ELLIPTIC
  OMEGA(J)=OMEGA_E
  A(J)=DYBU1
  B(J)=-(DYBU1+VV*(BX1(I)+BX2(I)))-AZ1(K)-AZ2(K)
  C(J)=0.
  D(J)=DYBU2+FPU(N)=VV*(BX1(I)*PHI(LR)+BX2(I)*PHI(LL))-(AZ1(K)*
  1 PHI(LF)+AZ2(K)*PHI(LBK))
  GO TO 390
351 CONTINUE
IF (V(J),GT,0.) GO TO 352
C HYPERBOLIC
  OMEGA(J)=OMEGA_H
  VV=KCAP=CX(I-1)*(PHI(L)=PHI(LL))-CX(I-2)*(PHI(LL)=PHI(LLL))
  A(J)=DYBU1
  B(J)=VV*BX1(I-1)=DYBU1-AZ1(K)-AZ2(K)
  C(J)=0.
  D(J)=DYBU2+FPU(N)+VV*(BX1(I-1)*PHI(LL)+BX2(I-1)*PHI(LL)=
  1 PHI(LLL)))-(AZ1(K)*PHI(LF)+AZ2(K)*PHI(LBK))
  GO TO 390
C PARABOLIC
352 CONTINUE
  OMEGA(J)=OMEGA_P
  A(J)=DYBU1
  B(J)=VV*BX1(I-1)=DYBU1-AZ1(K)-AZ2(K)
  C(J)=0.
  D(J)=DYBU2+FPU(N)+VV*(BX1(I-1)*PHI(LL)+BX2(I-1)*PHI(LL)=
  1 PHI(LLL)))-(AZ1(K)*PHI(LF)+AZ2(K)*PHI(LBK))
  GO TO 390
C SHOCK POINT
353 CONTINUE
  OMEGA(J)=OMEGA_E
  A(J)=DYBU1
  B(J)=DYBU1=AL*VV*(BX1(I)+BX2(I))+BET*V(J)*BX1(I-1)-AZ1(K)-AZ2(K)
  C(J)=0.
  D(J)=DYBUP+FPU(N)=AL*VV*(BX1(I)*PHI(LR)+BX2(I)*PHI(LL))+BET*V(J)*
  1 (BX1(I-1)*PHI(LL)+BX2(I-1)*PHI(LL))-AZ1(K)*PHI(LF)+
  2 AZ2(K)*PHI(LBK))
  GO TO 390
C *****
C *          AIRFOIL LOWER SURFACE BOUNDARY CONDITION
C *****
370 CONTINUE
VV=KCAP=AX1(I)*(PHI(LR)=PHI(L))-AX2(I)*(PHI(L)=PHI(LL))
IF (VV,LT,0.) GO TO 371
IF (V(J),LT,0.) GO TO 373
C ELLIPTIC
  OMEGA(J)=OMEGA_E
  A(J)=0.
  B(J)=-(DYBL1+VV*(BX1(I)+BX2(I)))-AZ1(K)-AZ2(K)
  C(J)=DYBL1
  D(J)=DYBL2+FPL(N)=VV*(BX1(I)*PHI(LR)+BX2(I)*PHI(LL))-(AZ1(K)*
  1 PHI(LF)+AZ2(K)*PHI(LBK))

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      GO TO 390
371 CONTINUE
  IF (V(J).GT.0.) GO TO 372
C HYPERBOLIC
  OMEGA(J)=OMEGAH
  VV=KCAP=CX(I-1)*(PHI(L)-PHI(LL))-CX(I-2)*(PHI(LL)-PHI(LLL))
  A(J)=0.
  B(J)=VV+BX1(I-1)-DYBL1-AZ1(K)-AZ2(K)
  C(J)=DYBL1
  D(J)=DYBL2+FPL(N)+VV*(BX1(I-1)*PHI(LL)+BX2(I-1)*PHI(LL)-
  1 PHI(LLL))-(AZ1(K)*PHI(LF)+AZ2(K)*PHI(LBK))
  GO TO 390
C PARABOLIC
372 CONTINUE
  OMEGA(J)=OMEGAP
  A(J)=0.
  B(J)=VV+BX1(I-1)-DYBL1-AZ1(K)-AZ2(K)
  C(J)=DYBL1
  D(J)=DYBL2+FPL(N)+VV*(BX1(I-1)*PHI(LL)+BX2(I-1)*PHI(LL)-
  1 PHI(LLL))-(AZ1(K)*PHI(LF)+AZ2(K)*PHI(LBK))
  GO TO 390
C SHOCK POINT
373 CONTINUE
  OMEGA(J)=OMEGAE
  A(J)=0.
  B(J)=DYBL1-AL+VV*(BX1(I)+BX2(I))+BET*V(J)*BX1(I-1)-AZ1(K)-AZ2(K)
  C(J)=DYBL1
  D(J)=DYBL2+FPL(N)-AL+VV*(BX1(I)*PHI(LR)+BX2(I)*PHI(LL))+BET*
  1 V(J)*(BX1(I-1)*PHI(LL)+BX2(I-1)*PHI(LL))-AZ1(K)*
  2 PHI(LF)+AZ2(K)*PHI(LBK))
  GO TO 390
360 CONTINUE
C BODY BOUNDARY J=JW
  A(J)=0.
  B(J)=1.
  C(J)=0.
  D(J)=PHI(L)
390 CONTINUE
  PHI(LR)=TPHILR
  PHI(LL)=TPHILL
  PHI(LLL)=TPPHILL
  PHI(LBK)=TPPHIBK
300 CONTINUE
C TRIDIAGONAL MATRIX IS SET NOW SOLVE FOR COLUMN OF PHI
  CALL TRI(I,K)
C CHECK FOR COLUMN CONVERGENCE OF PHI
  DO 395 J=2,JM1
    L=M+J
    JERROR=J
    ERRRC=PHIOC(J)-PHI(L)
    IF (ABS(ERRRC).GT.EPSCOL) GO TO 250
395 CONTINUE
394 CONTINUE
  IF (NITERC.GT.NCOL) WRITE (6,904) NITERG,I,ERRRC,JERROR,K
C CONVERGED, RELAX PHI, FIND ERROR AND MOVE TO NEXT COLUMN

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DO 396 J=2,JM1
L=M+J
ERR=OMEGA(J)*(PHI(L)-PHIUG(J))
PHI(L)=PHIUG(J)+ERR
IF (ABS(ERR).LT.ABS(ERROR)) GO TO 396
ERROR=ERR
LERR=REL
396 CONTINUE
IF (IFLAG.NE.1) GO TO 200
L=M+JW
PHI(L)=PHI(L-1)+DY(JWM1)*(PHI(L-1)-PHI(L-2))/DY(JW-2)
PHIUB(N)=PHI(L+1)-DY(JW)*(PHI(L+2)-PHI(L+1))/DY(JWP1)
IF (I.EQ.ITE) GAMTE(K)=PHIUB(N)-PHI(L)
200 CONTINUE
100 CONTINUE
C PRINT OUT ERROR AFTER GRID SWEEP
WRITE (6,905) NITERG,ERROR,LERROR
IF (ABS(ERROR).LT.10.) GO TO 101
WRITE (6,915)
STOP
101 CONTINUE
IDOUB=0
IF (ABS(ERROR).LE.EPSGRD(KGRD)) GO TO 400
IF (NITERG.EQ.NGRID) GO TO 410
IF (MOD(NITERG,NDUMP).EQ.0) GO TO 410
GO TO 75
400 CONTINUE
KGRD=KGRD+1
IDOUB=1
GO TO 410
#01 CONTINUE
CALL GAMFUN
WRITE (6,910) NITERG,IWING,GAMTE(1),GAMFF(1),GAMTE(KSPAN),
 1 GAMFF(KSPAN)
CALL FPRINT
WRITE (6,900)
WRITE (6,906) NITERG
CALL DOUBLE
WRITE (6,914) IM,JM,JW,KM,ILE,ITE,KSPAN
WRITE (6,902)
WRITE (6,903) (X(I),I=1,IM)
WRITE (6,911)
WRITE (6,903) (Y(I),I=1,JM)
WRITE (6,916)
WRITE (6,903) (Z(I),I=1,KM)
GO TO 75
410 CONTINUE
C TAPE DUMP
WRITE (7) NITERG,IM,IM1,JM,JM1,KM,KM1,JW,JWP1,JWM1,ITE,ILE,
 1 KSPAN,KCAP,DEL,ALPHA,NDB,MB,GAM,DYBUI,DYBU2,DYBL1,DYBL2,
 2 DOUB,ZSPAN
WRITE (7) (X(I),DX(I),AX1(I),AX2(I),BX1(I),BX2(I),CX(I),I=1,IM)
WRITE (7) (Y(I),DY(I),AY1(I),AY2(I),I=1,JM)
WRITE (7) (Z(I),DZ(I),AZ1(I),AZ2(I),I=1,KM)
L=ITE*KM

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      WRITE (7) (FPU(I),FPL(I),PHIUB(I),I=1,L)
      WRITE (7) (GAMTE(I),GAMFF(I),I=1,KSPAN)
      L=IM*JM*KM
      WRITE (7) (PHI(I),I=1,L)
      FND FILE 7
      WRITE (6,907) NITERG
      CALL PRINT(NITERG)
      IF (KGRD.GT.KEPS) GO TO 420
      IF (NITERG.EQ.NGRID) GO TO 430
      IF (IDOUR.EQ.1) GO TO 401
      GO TO 75
 420 CONTINUE
      WRITE (6,908) NITERG
      GO TO 450
 430 CONTINUE
      WRITE (6,909) NITERG
 900 FORMAT (1H$)
 901 FORMAT (1H //,* CASE IS BEING RESTARTED AT ITERATION*IS*)
 902 FORMAT (1H //,* X(I),I=1,IM*)
 903 FORMAT (10E13.5)
 904 FORMAT (1H //,* AT ITERATION*IS* COLUMN*I4* FAILED TO CONVERGE*)
 905 FORMAT (1H //,* AT ITERATION*IS* THE MAXIMUM ERROR ==E13.5* AND OC
    ICURRED AT NODE*IS*)
 906 FORMAT (1H //,* THE NUMBER OF NODES IS BEING DOUBLED AT ITERATION*
    1 IS)
 907 FORMAT (1H //,* TAPE HAS BEEN DUMPED AT ITERATION*IS*)
 908 FORMAT (1H //,* SOLUTION HAS CONVERGED TO DESIRED ACCURACY AT ITER
    ATION*IS*)
 909 FORMAT (1H //,* MAXIMUM NUMBER OF ITERATIONS HAS BEEN REACHED, CAS
    IE IS BEING TERMINATED AT ITERATION*IS*)
 910 FORMAT (1H //,* UPDATE GAMFF AND FARFIELD AT ITERATION*IS*,/
    1 * IWING ==E13.5* GAMTE(I) ==E13.5* GAMFF(I) ==E13.5* GAMTE(KSPAN
    2) ==E13.5* GAMFF(KSPAN) ==E13.5)
 911 FORMAT (1H //,* Y(J),J=1,JM*)
 912 FORMAT (8A10)
 913 FORMAT (1H //,* SIMILARITY PARAMETER (K) ==E13.5,/* SCALING FACTO
    SR (CP/CPBAR) ==E13.5)
 914 FORMAT (1H //,* IM ==I4* JM ==I4* JW ==I4* KM ==I4* ILE ==I4
    1 * ITE ==I4* KSPAN ==I4)
 915 FORMAT (1H //,* SOLUTION IS DIVERGING, THE PROBLEM IS BEING TERMIN
    IATED*)
 916 FORMAT (1H //,* Z(K),K=1,KM*)
 450 CONTINUE
      CALL FPRINT
      END
      SUBROUTINE DOUBLE
      REAL KCAP,M8,IWING
      COMMON /DELTA/ DX(40),DY(40),DZ(20),AX1(40),AX2(40),BX1(40),
      1 BX2(40),CX(40),AY1(40),AY2(40),AZ1(20),AZ2(20),X(40),Y(40),
      2 Z(20),FPU(800),FPL(800),PHIUB(800),IM,IM1,JM,JM1,KM,KM1,JW,
      3 JW1,JWM1,ITE,ILE,KSPAN,DYBU1,DYBU2,DYBL1,DYBL2,ALPHA,DEL,M8,
      4 GAM,KCAP,NDB,TITLE(8),DOUB,IWING,ZSPAN,NKPRT,KPRT(20)
      COMMON /COEFF/ A(40),B(40),C(40),D(40),PHI(1500)
      COMMON /GAMMA/ GAMTE1(20),GAMTE(20),PGFF,GAMFF(20)

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      RETURN
      END
      SUBROUTINE FARFLD
      REAL KCAP,M8,IWING
      COMMON /DELTA/ DX(40),DY(40),DZ(20),AX1(40),AX2(40),BX1(40),
1     BX2(40),CX(40),AY1(40),AY2(40),AZ1(20),AZ2(20),X(40),Y(40),
2     Z(20),FPIJ(800),FPL(800),PHIUB(800),IM,IM1,JM,JM1,KH,KM1,JW,
3     JWP1,JWH1,ITE,ILE,KSPAN,DYBU1,DYBU2,DYBL1,DYBL2,ALPHA,DEL,M8,
4     GAM,KCAP,NDB,TITLE(8),DOUB,IWING,ZSPAN,NKPRT,KPRT(20)
      COMMON /COEFF/ A(40),B(40),C(40),D(40),PHI(11500)
      COMMON /GAMMA/ GAMTE1(20),GAMTE(20),PGFF,GAMFF(20)
      COMMON /INTERP/ ZE(25),NZE
C   SUBSONIC FARFIELD
C   CALCULATE WING INTEGRAL
      CON1=DOUB/6.2831853
      IWING=0.
      DO 10 I=2,KSPAN
      IWING=IWING+.5*(GAMTE(I)+GAMTE(I-1))*DZ(I-1)
10    CONTINUE
      IWING=2.*((IWING+.5*GAMTE(KSPAN))*(ZSPAN-Z(KSPAN)))
      CON2=IWING/12.5663706
C   Z=Z(KM)
      MP=IM*JM*KM1
      Z2=Z(KM)**2
      DO 20 I=1,IM1
      M=MP+(I-1)*JM
      X2=X(I)**2
      CON3=X(I)*CON1
      DO 25 J=1,JM
      L=MP+J
      Y2=Y(J)**2
      R=SQRT(X2+KCAP*(Y2+Z2))
      PHIT=CON3/R**3
      PHI(L)=PHIT+CON2*Y(J)*(1.+X(I)/R)/(Y2+Z2)
25    CONTINUE
20    CONTINUE
C   X=X(1)
      X2=X(1)**2
      CON3=X(1)*CON1
      DO 30 K=1,KM1
      M=IM*JM*(K-1)
      Z2=Z(K)**2
      DO 35 J=1,JM
      L=MP+J
      Y2=Y(J)**2
      R=SQRT(X2+KCAP*(Y2+Z2))
      PHIT=CON3/R**3
      IF (Y2,EQ.0.,AND,Z2,EQ.0.) GO TO 36
      PHI(L)=PHIT+CON2*Y(J)*(1.+X(1)/R)/(Y2+Z2)
      GO TO 35
36    CONTINUE
      PHI(L)=PHIT
35    CONTINUE
30    CONTINUE
C   Y=Y(1) AND Y=Y(JM)

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DO 40 ID=1,2
IF (ID.EQ.2) GO TO 4.
J=1
Y2=Y(1)**2
GO TO 42
41 CONTINUE
J=JM
Y2=Y(JM)**2
42 CONTINUE
DO 45 K=1,KM
MP=IM+JM*(K-1)
Z2=Z(K)**2
CON3=CON2*Y(J)/(Y2+Z2)
DO 46 I=2,IM
L=MP+(I-1)*JM+J
R=SQRT(X(I)**2+KCAP*(Y2+Z2))
PHIT=X(I)*CON1/R**3
PHI(L)=PHIT+CON3*(1.+X(I)/R)
46 CONTINUE
45 CONTINUE
40 CONTINUE
C X=X(IM)
X2=X(IM)**2
DO 50 K=1,KM
MP=IM+JM*(K-1)
M=MP+IM1*JM
Z2=Z(K)**2
DO 70 I=1,NZE
A(I)=Z(I)
70 CONTINUE
NEND=NZE
IFLIP=0
IZ=0
IF (Z(K).LE.ZSPAN) IZ=1
DO 60 J=1,JM
IF (ABS(Y(J)).LE..5.OR.IFLIP.EQ.1) GO TO 71
A(I)=Z(I)
72 CONTINUE
NEND=KSPAN
IFLIP=1
71 CONTINUE
L=MP+J
Y2=Y(J)**2
CON3=Y(J)/3.14159265
AINT=0,
IF (IZ.EQ.1.AND.J.EQ.JW) GO TO 65
IZE=2
DO 61 KK=1,NEND
62 CONTINUE
IF (A(KK).LE.Z(IZE)) GO TO 63
IZE=IZE+1
GO TO 62
63 CONTINUE
ANEW=(GAMTE(IZE=1)+(A(KK)-Z(IZE=1))/DZ(IZE=1)*(GAMTE(IZE)=

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1 GAMTE(IZE=1)))/((Z(K)-A(KK))*2+Y2)
IF (KK.EQ.1) GO TO 64
AINTE=AINT+.5*(ANEW+OLD)*(A(KK)-AF(KK-1))
64 CONTINUE
OLD=ANEW
61 CONTINUE
AINTE=AINT+.5*ANEW*(ZSPAN-Z(KSPAN))
65 CONTINUE
R=SQRT(X2+KCAP*(Y2+Z2))
PHIT=Y(IM)*CON1/R**3
PHI(L)=PHIT*CON3*AINT
60 CONTINUE
50 CONTINUE
RETURN
END
FUNCTION FLP(XY,ZZ)
REAL KCAP,M8,IWING
COMMON /DELTA/ DX(40),DY(40),DZ(20),AX1(40),AX2(40),BX1(40),
1 BX2(40),CX(40),AY1(40),AY2(40),AZ1(20),AZ2(20),X(40),Y(40),
2 Z(20),FPU(800),FPL(800),PHIUB(800),IM,IM1,JM,JM1,KM,KM1,JW,
3 JWP1,JWM1,ITE,ILE,KSPAN,DYB1,DYB2,DYBL1,DYBL2,ALPHA,DEL,M8,
4 GAM,KCAP,NDB,TITLE(8),DOUB,IWING,ZSPAN,NKPRT,KPRT(20)
C AIRFOIL LOWER SURFACE SLOPE DISTRIBUTION
FLP=0.*XX-.5
RETURN
END
SUBROUTINE FPRINT
REAL KCAP,M8,IWING
COMMON /DELTA/ DX(40),DY(40),DZ(20),AX1(40),AX2(40),BX1(40),
1 BX2(40),CX(40),AY1(40),AY2(40),AZ1(20),AZ2(20),X(40),Y(40),
2 Z(20),FPU(800),FPL(800),PHIUB(800),IM,IM1,JM,JM1,KM,KM1,JW,
3 JWP1,JWM1,ITE,ILE,KSPAN,DYB1,DYB2,DYBL1,DYBL2,ALPHA,DEL,M8,
4 GAM,KCAP,NDB,TITLE(8),DOUB,IWING,ZSPAN,NKPRT,KPRT(20)
COMMON /CNEFF/ A(40),B(40),C(40),D(40),PHI(11500)
COMMON /GAMMA/ GAMTE1(20),GAMTE(20),PGFF,GAMFF(20)
CPCPB=DEL**,6666666667/((1.+GAM)*M8**)**,3333333333
CPCRIT=2.*CPCPB*KCAP
WRITE (6,900)
WRITE (6,901) (TITLF(I),I=1,8)
WRITE (6,902) M8
WRITE (6,903) KCAP
WRITE (6,904) DEL
WRITE (6,905) ALPHA
WRITE (6,907) ZSPAN
WRITE (6,906) CPCPB
WRITE (6,916) CPCRIT
WRITE (6,912)
WRITE (6,915) (Y(I),I=ILE,ITE)
CLIFT=0.
CMOMBO.
DO 10 K81,KSPAN
PART=.5*((X(ITE+1)-1.)*(GAMFF(K)-GAMTE(K))/(X(IM1)-1.)*GAMTE(K))
MP=IM*JM*(K-1)
IJK=MP+ITE*JM+JW
PHI(IJK)=PHI(IJK)+PART

```

```

L=MP+(ILE-2)*JM+JW
LP=(ILE-2)*KM+K
PHIUB(LP)=PHI(L)
LP=ITE*KM+K
PHIUB(LP)=PHI(IJK)+2,*PART
DO 20 I=ILE,ITE
M=MP+(I-1)*JM
L=M+JW
LP=(I-1)*KM+K
A(I)=-2.*(AX1(I)*(PHI(L+JM)-PHI(L))+AX2(I)*(PHI(L)-PHI(L-JM)))*
1 CPCPB
B(I)=-2.*(AX1(I)*(PHIUB(LP+KM)-PHIUB(LP))+AX2(I)*(PHIUB(LP)-
1 PHIUB(LP-KM)))*CPCPB
IF (K.GT.1) GO TO 21
C(I)=A(I)
D(I)=B(I)
21 CONTINUE
C1=A(I)-B(I)
C2=C1*X(I)
IF (I.GT.ILE) GO TO 22
CL=C1*X(ILE)
CM=.5*C2*X(ILE)
GO TO 23
22 CONTINUE
CL=CL+.5*(C1+C10)*DX(J-1)
CM=CM+.5*(C2+C20)*DX(I-1)
23 CONTINUE
C10=C1
C20=C2
20 CONTINUE
PHI(IJK)=PHI(IJK)+PART
IF (K.EQ.1) GO TO 11
CLIFT=CLIFT+.5*(CL+CLO)*DZ(K-1)
CMOM=CMOM+.5*(CM+CMO)*DZ(K-1)
11 CONTINUE
CLO=CL
CMO=CM
DO 12 N=1,NKPRT
IF (KPRT(N).NE.K) GO TO 12
GAMPRT=2.*GAMTE(K)*CPCPB
WRITE (6,908) Z(K),GAMPRT
WRITE (6,913)
WRITE (6,915) (B(I),I=ILE,ITE)
WRITE (6,914)
WRITE (6,915) (A(I),I=ILE,ITE)
GO TO 10
12 CONTINUE
10 CONTINUE
WRITE (6,900)
WRITE (6,901) (TITLE(I),I=1,8)
WRITE (6,902) M8
WRITE (6,903) KCAP
WRITE (6,904) DEL
WRITE (6,905) ALPHA
WRITE (6,907) ZSPAN

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```

      WRITE (6,906) CPCPB
      WRITE (6,916) CPCRIT
      WRITE (6,909)
      WRITE (6,910) CLIFT,CMOM
      GAMPR=2.*GAMTE(1)*CPCPB
      WRITE (6,908) Z(1),GAMPR
      WRITE (6,912)
      WRITE (6,915) (X(I),I=ILE,ITE)
      WRITE (6,913)
      WRITE (6,915) (D(I),I=ILE,ITE)
      WRITE (6,914)
      WRITE (6,915) (C(I),I=ILE,ITE)
900  FORMAT (1H1)
901  FORMAT (30X,BA10)
902  FORMAT (1H ,/,1H ,/,1H ,/,* MACH NUMBER *E13.5)
903  FORMAT (* SIMILARITY PARAMETER (K) *E13.5)
904  FORMAT (* THICKNESS RATIO *E13.5)
905  FORMAT (* AIRFOIL ANGLE OF ATTACK (RADIAN) *E13.5)
906  FORMAT (* CP SCALING FACTOR (CP/CPBAR) *E13.5)
907  FORMAT (* WING ASPECT RATIO *E13.5)
908  FORMAT (1H ,/,1H ,/,21X*AIRFOIL SPANWISE COORDINATE *E13.5
   1 * SECTION LIFT COEFFICIENT *E13.5)
909  FORMAT (1H ,/,1H ,/,* AIRFOIL FORCE COEFFICIENTS*)
910  FORMAT (1H ,/,3X*LIFT *E13.5,/,3X*MOMENT ABOUT (X=0) *E13.5)
912  FORMAT (1H ,/,1H ,/,3X*AIRFOIL STREAMWISE COORDINATE*)
913  FORMAT (1H ,/,1H ,/,3X*AIRFOIL PRESSURE COEFFICIENTS, UPPER *)
914  FORMAT (1H ,/,3X*AIRFOIL PRESSURE COEFFICIENTS, LOWER *)
915  FORMAT (3X10E13.5)
916  FORMAT (* CRITICAL PRESSURE COEFFICIENT (SONIC) *E13.5)
      RETURN
      END
      FUNCTION FUP(XX,ZZ)
      REAL KCAP,M8,IWING
      COMMON /DELTA/ DX(40),DY(40),DZ(20),AX1(40),AX2(40),BX1(40),
   1 BX2(40),CX(40),AY1(40),AY2(40),AZ1(20),AZ2(20),X(40),Y(40),
   2 Z(20),FPU(800),FPL(800),PHIUB(800),IM,IM1,JM,JM1,KM,KM1,JW,
   3 JWP1,JWM1,ITE,TLE,KSPAN,DYBU1,DYBU2,DYBL1,DYBL2,ALPHA,DEL,M8,
   4 GAM,KCAP,NDB,TITLE(8),DOUR,IWING,ZSPAN,NKPRT,KPRT(20)
C AIRFOIL UPPER SURFACE SLOPE DISTRIBUTION
      FUP=4.*((XX-,5)
C DOUB IS THE DOUBLET STRENGTH DUE TO THICKNESS
      DOUB=1.33333333*ZSPAN
      RETURN
      END
      SUBROUTINE GAMFLN
      REAL KCAP,M8,IWING
      COMMON /DELTA/ DX(40),DY(40),DZ(20),AX1(40),AX2(40),BX1(40),
   1 BX2(40),CX(40),AY1(40),AY2(40),AZ1(20),AZ2(20),X(40),Y(40),
   2 Z(20),FPU(800),FPL(800),PHIUB(800),IM,IM1,JM,JM1,KM,KM1,JW,
   3 JWP1,JWM1,ITE,ILE,KSPAN,DYBU1,DYBU2,DYBL1,DYBL2,ALPHA,DEL,M8,
   4 GAM,KCAP,NDB,TITLE(8),DOUR,IWING,ZSPAN,NKPRT,KPRT(20)
      COMMON /GAMMA/ GAMTE1(20),GAMTE(20),PGFF,GAMFF(20)
      DO 10 I=1,KSPAN
      GAMFF(I)=GAMTE1(I)+PGFF*(GAMTE(I)-GAMTE1(I))
      GAMTE1(I)=GAMTE(I)

```

```

10 CONTINUE
RETURN
END
SUBROUTINE INITIAL
REAL KCAP,M8,IWING
COMMON /DELTA/ DX(40),DY(40),DZ(20),AX1(40),AX2(40),BX1(40),
1 BX2(40),CX(40),AY1(40),AY2(40),AZ1(20),AZ2(20),X(40),Y(40),
2 Z(20),FPU(800),FPL(800),PHIUB(800),IM,IM1,JM,JM1,KM,KM1,JW,
3 JWP1,JWM1,ITE,ILE,KSPAN,DYBU1,DYBU2,DYBL1,DYBL2,ALPHA,DEL,M8,
4 GAM,KCAP,NDB,TITLE(8),DOUB,IWING,ZSPAN,NKPRT,KPRT(20)
C CALCULATE DX,DY AND DZ
DO 10 I=1,IM1
DX(I)=X(I+1)-X(I)
10 CONTINUE
DO 20 I=1,JM1
DY(I)=Y(I+1)-Y(I)
20 CONTINUE
DO 30 I=1,KM1
DZ(I)=Z(I+1)-Z(I)
30 CONTINUE
C FINITE DIFFERENCE COEFFICIENTS
DO 40 I=2,IM1
AX1(I)=DX(I-1)/(DX(I)*(DX(I-1)+DX(I)))
AX2(I)=DX(I)/(DX(I-1)*(DX(I-1)+DX(I)))
BX1(I)=2.*AX1(I)/DX(I-1)
BX2(I)=2.*AX2(I)/DX(I)
CX(I)=.5/DX(I)
40 CONTINUE
CX(1)=.5/DX(1)
DO 50 I=2,JM1
AY1(I)=2./((DY(I)*(DY(I)+DY(I-1))))
AY2(I)=2./((DY(I-1)*(DY(I)+DY(I-1))))
50 CONTINUE
DO 60 I=2,KM1
AZ1(I)=2./((DZ(I)*(DZ(I)+DZ(I-1))))
AZ2(I)=2./((DZ(I-1)*(DZ(I)+DZ(I-1))))
60 CONTINUE
AZ1(1)=2./DZ(1)**2
AZ2(1)=0.
DYBU1=2./((DY(JWP1)+2.*DY(JW))*DY(JWP1))
DYBU2=DY(JWP1)*DYBU1
DYBL1=2./((DY(JW-2)+2.*DY(JWM1))*DY(JW-2))
DYBL2=DY(JW-2)*DYBL1
C SET AIRFOIL BOUNDARY CONDITION
DO 70 K=1,KSPAN
DO 80 I=ILE,ITE
L=(I-1)*KM+K
FPU(L)=FUP(X(I),Z(K))
FPL(L)=FLP(X(I),Z(K))
80 CONTINUE
70 CONTINUE
RETURN
END
SUBROUTINE PRINT (NITERG)
REAL KCAP,M8,IWING

```

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COMMON /DELTA/ DX(40),DY(40),DZ(20),AX1(40),AX2(40),BX1(40),
1 BX2(40),CX(40),AY1(40),AY2(40),AZ1(20),AZ2(20),X(40),Y(40),
2 Z(20),FPU(800),FPL(800),PHIUB(800),IM,IM1,JM,JM1,KM,KM1,JW,
3 JWP1,JWM1,ITE,ILE,KSPAN,DYBU1,DYBU2,DYBL1,DYBL2,ALPHA,DEL,M8,
4 GAM,KCAP,NDB,TITLE(8),DOUB,IWING,ZSPAN,NKPRT,KPRT(20)
COMMON /COEFF/ A(40),B(40),C(40),D(40),PHI(11500)
COMMON /GAMMA/ GAMTE1(20),GAMTE(20),PGFF,GAMFF(20)
KSPAN1=KSPAN-1
DO 10 K=1,KSPAN,KSPAN1
PART=.5*((X(ITE+1)-1.)*(GAMFF(K)-GAMTE(K))/(X(IM1)-1.)+GAMTE(K))
MP=IM*JM*(K-1)
IJK=MP+ITE*JM+JW
PHI(IJK)=PHI(IJK)+PART
L=MP+(ILE-2)*JM+JW
LP=(ILE-2)*KM+K
PHIUB(LP)=PHI(L)
LP=ITE*KM+K
PHIUB(LP)=PHI(IJK)+2.*PART
C COMPUTE CP LOWER (A) AND CP UPPER (B)
DO 20 I=ILE,ITE
L=MP+(I-1)*JM+JW
LP=(I-1)*KM+K
A(I)=-2.*((AX1(I)*(PHI(L+JM)-PHI(L))+AX2(I)*(PHI(L)-PHI(L+JM)))
B(I)=-2.*((AX1(I)*(PHIUB(LP+KM)-PHIUB(LP))+AX2(I)*(PHIUB(LP)-
1 PHIUB(LP+KM))))
20 CONTINUE
PHI(IJK)=PHI(IJK)+PART
WRITE (6,901) NITERG,K
WRITE (6,902) (B(I),I=ILE,ITE)
WRITE (6,903) NITERG,K
WRITE (6,902) (A(I),I=ILE,ITE)
10 CONTINUE
901 FORMAT (1H ,/, * AT ITERATION=I5* AND K =I3* SCALED PRESSURE COEFF
1ICIENT, UPPER (ILE TO ITE) **)
902 FORMAT (10E13.5)
903 FORMAT (1H ,/, * AT ITERATION=I5* AND K =I3* SCALED PRESSURE COEFF
1ICIENT, LOWER (ILE TO ITE) **)
RETURN
END
SUBROUTINE TRI (I,K)
REAL KCAP,M8,IWING
COMMON /DELTA/ DX(40),DY(40),DZ(20),AX1(40),AX2(40),BX1(40),
1 BX2(40),CX(40),AY1(40),AY2(40),AZ1(20),AZ2(20),X(40),Y(40),
2 Z(20),FPU(800),FPL(800),PHIUB(800),IM,IM1,JM,JM1,KM,KM1,JW,
3 JWP1,JWM1,ITE,ILE,KSPAN,DYBU1,DYBU2,DYBL1,DYBL2,ALPHA,DEL,M8,
4 GAM,KCAP,NDB,TITLE(8),DOUB,IWING,ZSPAN,NKPRT,KPRT(20)
COMMON /COEFF/ A(40),B(40),C(40),D(40),PHI(11500)
MP=IM*JM*(K-1)
DO 10 KK=3,JM1
J=JM1-KK+3
P=A(J-1)/B(J)
B(J-1)=B(J-1)-P*C(J)
D(J-1)=D(J-1)-P*D(J)
10 CONTINUE
M=MP+(I-1)*JM

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```
PHI(M+2)=D(2)/B(2)
DO 20 J=3,JM1
L=M+J
PHI(L)=(D(J)-PHI(L-1)*C(J))/B(J),
20 CONTINUE
RETURN
END
```

APPENDIX B

FORTRAN LISTING OF TDUTRN

A FORTRAN listing of the source deck for the TDUTRN program is presented in the following pages. The program, as configured here, requires 161.7,K words to load and 150.0,K words to execute. In this configuration the programs fit into small core of the CDC 7600.

```

PROGRAM TDUTRN (INPUT,OUTPUT,TAPES=INPUT,TAPE6=OUTPUT,TAPET,
1 TAPE8,TAPE9)
COMPLEX B,D,PHIUB,PHI,PHI0G,GAMTE1,GAMTE,GAMFF,ERR,ERROR,
1 OMEG2I,SIGI,PART,FPU,FPL,TPHIR,TPHIL,TPHILL,TPHIBK,CON
REAL KCAP,M8
COMMON /DELTA/ DX(40),DY(40),DZ(40),AX1(40),AX2(40),BX1(40),
1 BX2(40),CX(40),AY1(40),AY2(40),AZ1(20),AZ2(20),X(40),Y(40),
2 Z(20),FPU(800),FPL(800),PHIUB(800),IM,IM1,JM,JM1,KM,KM1,JW,
3 JWP1,JWM1,ITE,ILE,KSPAN,DYB1,DYB12,DYBL1,DYBL2,SMALLK,OMEG,
4 NDOUR,CPCPB,TITLE(8),M8,DEL,ALPHA,ITYPE,IUPT,XP,NKPRT,KPRT(20),
5 ZSPAN,KCAP,RPAR
COMMON /COEFF/ A(40),B(40),C(40),D(40),PHI(11500)
COMMON /GAMMA/ GAMTE1(20),GAMTE(20),PGFF,GAMFF(20)
COMMON /STEADY/ PHI8(11500),AX18(40),AX28(40),BX18(40),BX28(40),
1 CX8(40),PHIUB8(800)
COMMON /INTERP/ ZE(25),NZE
DIMENSION PHI0G(40),OMEGA(40),V(40),EPSGRD(3)
NAMELIST /IN/ X,Y,Z,IM,JM,KM,ILE,ITE,JW,KSPAN,GAMFF,OMEGAH,
1 OMEGAE,OMEGAP,EPSGRD,NUMP,NGRID,NGFF,PGFF,KEPS,NPRINT,NKPRT,
2 KPRT,SMALLK,IK,XP,ITYPE,IUPT,ZE,NZE
NAMELIST /CTRL/ ITAPE

C TO START PROGRAM, STEADY (PHI8) DATA IS TO BE READ FROM A DISC FILE
C TAPES, UNSTEADY DATA WILL NOW BE WRITTEN ON TAPE7.
C TO RESTART PROGRAM, AGAIN STORE STEADY DATA AS ABOVE AND STORE
C THE UNSTEADY DATA ON A DISC FILE TAPE9. NEW UNSTEADY DATA WILL
C NOW BE WRITTEN ON TAPE7.
C READ STEADY SOLUTION
READ (8) DUM,IMS,IM1S,JMS,JM1S,KMS,KM1S,JWS,DUM,DUM,ITES,ILES,
1 KSPANS,KCAP,DEL,ALPHA,NDB,M8,GAM,DUM,DUM,DUM,DUM,DUM,ZSPAN
READ (8) (DUM,DUM,AX1S(I),AX2S(I),BX1S(I),BX2S(I),CX8(I),I=1,IMS)
READ (8) DUM
READ (8) DUM
L=ITES*KMS
READ (8) (DUM,DUM,PHIUB8(I),I=1,L)
READ (8) DUM
L=IMS*KMS
READ (8) (PHI8(I),I=1,L)

C MODIFY LEADING AND TRAILING EDGE PHI
M=IMS*KMS
MC1=(ILES-1)*JMS+JWS
MC2=(ITES-1)*JMS+JWS
MC3=(ITES-2)*JMS+JWS
LP1=(ILES-1)*KMS
LP2=(ITES-1)*KMS
LP3=(ITES-2)*KMS
DO 1 K=1,KSPANS
MP=M+(K-1)
L=MP+MC1
LP=LP1+K
PHI8(L)=.5*(PHI8(L)+PHIUB8(LP))
L=MP+MC2
LP=LP2+K

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```

PHIS(L)=.5*(PHIS(L)+PHIUBS(LP))
L=MP+MC3
LP=LP3+K
PHIS(L)=.5*(PHIS(L)+PHIUBS(LP))
1 CONTINUE
SK=SQRT(KCAP)
CPCPB=DEL**.6666666667/((1.+GAM)*M8**2)**.3333333333
RPAR=1./((1.+GAM)*M8**2*DEL)**.3333333333
READ (5,911) (TITLE(I),I=1,8)
READ (5,CONTRL)
IF (ITAPE.EQ.0) GO TO 10
C READ DATA FROM RESTART TAPE
READ (9) NITERG,IM,IM1,JM,JM1,KM,KM1,JW,JWP1,JWM1,ITE,ILE,
1 KSPAN,OMEG,SMALLK,DYRU1,DYBU2,DYBL1,DYBL2,ND0UB,XP
READ (9) (X(I),DX(I),AX1(I),AX2(I),BX1(I),BX2(I),CX(I),I=1,IM)
READ (9) (Y(I),DY(I),AY1(I),AY2(I),I=1,JM)
READ (9) (Z(I),DZ(I),AZ1(I),AZ2(I),I=1,KM)
L=ITE*KM
READ (9) (FPU(I),FPL(I),PHIUB(I),I=1,L)
READ (9) (GAMTE(I),GAMFF(I),I=1,KSPAN)
L=IM*JM*KM
READ (9) (PHI(I),I=1,L)
DO 2 I=1,KSPAN
GAMTE1(I)=GAMTE(I)
2 CONTINUE
IK=0
READ (5,IN)
WRITE (6,900)
WRITE (6,901) NITERG
NITERG=0
WRITE (6,913) KCAP,CPCPB
C THE IK OPTION IS USED TO BOOTSTRAP TO DIFFERENT REDUCED FREQUENCIES
C AND/OR MODES OF OSCILLATION
IF (IK.EQ.0) GO TO 15
OMEG=SMALLK*M8**2/((1.+GAM)*DEL*M8**2)**.6666666667
CALL INITAL
CALL FARFLD
GO TO 15
C START PROBLEM FROM SCRATCH
10 CONTINUE
READ (5,IN)
NITERG=0
ND0UB=0
OMEG=SMALLK*M8**2/((1.+GAM)*DEL*M8**2)**.6666666667
DO 3 I=1,KSPAN
GAMTE1(I)=GAMFF(I)
GAMTE(I)=GAMFF(I)
3 CONTINUE
IM1=IM-1
JM1=JM-1
KM1=KM-1
JWP1=JW+1
JWM1=JW-1
C INITIALIZE FINITE DIFFERENCE COEFFICIENTS AND FARFIELD
CALL INITAL

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      CALL FARFLD
C  INITIALIZE GUESS FOR SUBSONIC CASE (INTERIOR ONLY)
C  ASSUMED SYMMETRY IN Y
      JW2=2*jw
      CON=GAMFF(1)/6.2831853
      DO 20 K=1,KM1
      MP=IM*JM*(K-1)
      ZP=Z(K)+ZSPAN
      ZM=Z(K)-ZSPAN
      Z2=Z(K)**2
      DO 30 I=2,IM1
      M=MP+(I-1)*JM
      PHI(M+JW)=CMPLX(0.,0.)
      X2=X(I)**2
      DO 40 J=JWP1,JM1
      L=M+J
      LL=M+JW2-J
      Y2=Y(J)**2
      IF (X(I).LT.1.) GO TO 41
      PHI(L)=CON*(ATAN(ZP/Y(J))-ATAN(ZM/Y(J)))
      GO TO 42
41  CONTINUE
      R=SQRT(X2+KCAP*(Y2+Z2))
      PHI(L)=CON*ZSPAN*(Y(J)/(Y2+Z2))*(1.+X(I)/R)
42  CONTINUE
      CPHI=CABS(PHI(L))
      IF (CPHI.GT.1.) PHI(L)=PHI(L)/CPHI
      PHI(LL)=-PHI(L)
40  CONTINUE
30  CONTINUE
20  CONTINUE
      L=ITE*KM
      ERR=CMPLX(0.,0.)
      DO 4 I=1,L
      PHIUB(I)=ERR
4   CONTINUE
      M=(ILE-2)*JM+jw
      KK=(ILE-1)*KM
      DO 45 K=1,KSPAN
      L=M+IM*JM*(K-1)
      PHIUB(KK+K)=PHI(L)
45  CONTINUE
15  CONTINUE
      OMEG2I=CMPLX(0.,2.*OMEG)
      WRITE (6,IN)
      WRITE (6,900)
      IF (ITAPE.EQ.0) WRITE (6,913) KCAP,CPCPB
      KGRD=1
C  RE-CYCLE POINT FOR GRID ITERATION
50  CONTINUE
      ERROR=CMPLX(0.,0.)
      NIT=NITERG
      NITERG=NITERG+1
      IF (MOD(NITERG,NPRINT),EQ,0) CALL PRINT(NIT)
      IF (MOD(NITERG,NGFP),NE,0) GO TO 51

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```

CALL GAMFUN
CALL FAHFLD
WRITE (6,910) NITERG,GAMTE(1),GAMFF(1),GAMTE(KSPAN),GAMFF(KSPAN)
51 CONTINUE
INCR=2** (NDB=NDoub)
K8=1+INCR
IMJMB=IMB*JM
IM8JMB=IMB*JMS
C BEGIN LOOP ON THE PLANES (Z DIRECTION)
DO 100 K=1,KM1
K8=K8+INCR
DO 102 I=2,JM1
V(I)=KCAP
102 CONTINUE
MP=IMJMA*(K-1)
MPS=IM8JMB*(K8-1)
C CHECK FOR AIRFOIL
IFOIL=0
IF (K,LE,KSPAN) IFOIL=1
IS=2+INCR
C BEGIN LOOP ON A GIVEN PLANE (X DIRECTION)
DO 200 I=2,IM1
IS=IS+INCR
C CHECK FOR AIRFOIL
IFLAG=0
IF (IFOIL,EQ,1,AND,ILE,LE,I,AND,I,LF,ITE) IFLAG=1
IF (IFLAG,EQ,1) NB=(I-1)*KM+K
NB=NB+(I-1)*JM
NB=MPS+(IS-1)*JMS
C SAVE THIS COLUMN OF PHI
DO 201 J=2,JM1
L=M+J
PHIOG(J)=PHI(L)
201 CONTINUE
JS=2+INCR
C BEGIN LOOP ON COLUMN (Y DIRECTION)
DO 300 J=2,JM1
JS=JS+INCR
C CALCULATE CELL INDICES FOR PHIO
LS=MS+JS
LSR=LS+JMS
LSL=LS-JMS
LSLL=LSL-JMS
IF (IS,EQ,2) LSL=L
C CALCULATE CELL INDICES FOR PHI
L=M+J
LR=LS+JM
LL=LS-JM
LLL=LL-JM
IF (I,EQ,2) LLL=LL
LB=LS-1
LA=LS+1
LF=LS+IMJM
LK=L-IMJM
IF (K,EQ,1) LK=L

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C *****
C *          CALCULATE V AND PHIXX FROM STEADY SOLUTION
C *****
C      VVKCAP=AX1S(IS)*(PHIS(LSR)-PHIS(LS))-AX2S(IS)*(PHIS(LS)-
1  PHIS(LSL))
      VVS=VV
      IF (VVS.LT.0.) GO TO 301
C ELLIPTIC
      OMEGA(J)=OMEGAEE
      PHIXX=BX1S(IS)*(PHIS(LSR)-PHIS(LS))-BX2S(IS)*(PHIS(LS)-PHIS(LSL))
      GO TO 302
301 CONTINUE
      OMEGA(J)=OMEGAP
      IF (V(J).GT.0.) GO TO 303
C HYPERBOLIC
      OMEGA(J)=OMEGAH
      VVKCAP=CX8(IS-1)*(PHIS(LS)-PHIS(LSL))-CX8(IS-2)*(PHIS(LSL)-
1  PHIS(LSLL))
303 CONTINUE
C PARABOLIC
      PHIXX=BX1S(IS-1)*(PHIS(LS)-PHIS(LSL))-BX2S(IS-1)*(PHIS(LSL)-
1  PHIS(LSLL))
302 CONTINUE
      V(J)=VVS
      TPHIR=PHI(LR)
      TPHIL=PHI(LL)
      TPHILL=PHI(LLL)
      TPHIBK=PHI(LBK)
      IF (IFOIL.EQ.0.OR.J.NE.JW) GO TO 304
      IF (I.EQ.ILE-1) PHI(LR)=.5*(PHIUB((ILE-1)*KM+K)+PHI(LR))
      IF (I.EQ.ITE+1) PHI(LL)=.5*(PHIUB((ITE-1)*KM+K)+PHI(LL))
      IF (I.EQ.ITE+1) PHI(LLL)=.5*(PHIUB((ITE-2)*KM+K)+PHI(LLL))
      IF (I.EQ.ITE+2) PHI(LLL)=.5*(PHIUB((ITE-1)*KM+K)+PHI(LLL))
304 CONTINUE
      IF (ILE.LE.I.AND.I.LE.ITE.AND.J.EQ.JW.AND.K.EQ.KSPAN+1)
1  PHI(LBK)=.5*(PHIUB((I-1)*KM+KSPAN)+PHI(LBK))
C SET UP TRIDIAGONAL MATRIX TO SOLVE FOR PHI(I,J,K)
C A = PHI(I,J+1,K) + B = PHI(I,J,K) + C = PHI(I,J-1,K) = D
      IF (IFLAG.EQ.1.AND.J.EQ.JWP1) GO TO 330
      IF (IFLAG.EQ.1.AND.J.EQ.JW) GO TO 340
      IF (IFLAG.EQ.1.AND.J.EQ.JWM1) GO TO 350
      PART=CMPLX(0.,0.)
      IF (I.LE.ITE.OR.IFOIL.EQ.0) GO TO 305
C KUTTA CONDITION
      SIGI=(X(I)-1.)*(GAMFF(K)-GAMTE(K))/(X(IM1)-1.)*GAMTE(K)
      IF (IOPT.EQ.1) SIGI=SIGI+CEXP(CMPLX(0.,-SMALLK*(X(I)-1.)))
      IF (J.EQ.JWM1) PART=.5*AY1(J)*SIGI
      IF (J.EQ.JW) PART=.5*(AY1(J)-AY2(J))*SIGI
      IF (J.EQ.JWP1) PART=-.5*AY2(J)*SIGI
305 CONTINUE
      IF (VVS.LT.0.) GO TO 320
C *****
C *          ELLIPTIC DIFFERENCING
C *****
      A(J)=AY1(J)

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B(J)=-{VV*(BX1(I)+BX2(I))+AY1(J)+AY2(J)+(OMEG2I+PHIXX)*(AX2(I)-
1 AX1(I))}-AZ1(K)-AZ2(K)
C(J)=AY2(J)
D(J)=-VV*(BX1(I)*PHI(LR)+BX2(I)*PHI(LL))+(OMEG2I+PHIXX)*(AX1(I)*
1 PHI(LR)-AX2(I)*PHI(LL))+PART-(AZ1(K)*PHI(LF)+AZ2(K)*PHI(LBK))
IF (J.EQ.2) GO TO 311
IF (J.EQ.JM1) GO TO 312
GO TO 390
C BOTTOM BOUNDARY
311 CONTINUE
D(J)=D(J)-AY2(J)*PHI(LB)
GO TO 390
C TOP BOUNDARY
312 CONTINUE
D(J)=D(J)-AY1(J)*PHI(LA)
GO TO 390
C **** HYPERBOLIC AND PARABOLIC DIFFERENCING ****
C ****
320 CONTINUE
A(J)=AY1(J)
B(J)=VV*BX1(I=1)-AY1(J)-AY2(J)-(OMEG2I+PHIXX)*CX(I=1)-AZ1(K)-
1 AZ2(K)
C(J)=AY2(J)
D(J)=VV*(BX1(I=1)*PHI(LL)+BX2(I=1)*(PHI(LL)-PHI(LLL)))-(OMEG2I+
1 PHIXX)*(CX(I=1)*PHI(LL)-CX(I=2)*(PHI(LL)-PHI(LLL)))+PART-
2 (AZ1(K)*PHI(LF)+AZ2(K)*PHI(LBK))
IF (J.EQ.2) GO TO 321
IF (J.EQ.JM1) GO TO 322
GO TO 390
C BOTTOM BOUNDARY
321 CONTINUE
D(J)=D(J)-AY2(J)*PHI(LH)
GO TO 390
C TOP BOUNDARY
322 CONTINUE
D(J)=D(J)-AY1(J)*PHI(LA)
GO TO 390
C **** AIRFOIL UPPER SURFACE BOUNDARY CONDITION ****
C ****
330 CONTINUE
IF (VVS.LT.0.) GO TO 331
C ELLIPTIC
A(J)=DYBU1
B(J)=-(VV*(BX1(I)+BX2(I))+DYBU1+(OMEG2I+PHIXX)*(AX2(I)-AX1(I)))-
1 AZ1(K)-AZ2(K)
C(J)=0.
D(J)=DYBU2*FPU(N)-VV*(BX1(I)*PHI(LR)+BX2(I)*PHI(LL))+(OMEG2I+
1 PHIXX)*(AX1(I)*PHI(LR)-AX2(I)*PHI(LL))-(AZ1(K)*PHI(LF)+
2 AZ2(K)*PHI(LBK))
GO TO 390
C HYPERBOLIC AND PARABOLIC
331 CONTINUE
A(J)=DYBU1

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B(J)=VV*BX1(I=1)=DYBU1=(OMEG2I+PHIXX)*CX(I=1)=AZ1(K)=AZ2(K)
C(J)=0,
D(J)=DYBU2=FPU(N)+VV*(BX1(I=1)*PHI(LL)+BX2(I=1)*PHI(LL)-
1 PHI(LLL))=(OMEG2I+PHIXX)*(CX(I=1)*PHI(LL)+CX(I=2)*PHI(LL)-
2 PHI(LLL))=(AZ1(K)*PHI(LF)+AZ2(K)*PHI(LBK))
GO TO 390
C ***** AIRFOIL LOWER SURFACE BOUNDARY CONDITION *****
C * ***** 350 CONTINUE
C * ***** IF (VVS.LT.0.) GO TO 351
C ELLIPTIC
A(J)=0,
B(J)=-(DYBL1+VV*(BX1(I)+BX2(I))+OMEG2I+PHIXX)*(AX2(I)-AX1(I))-
1 AZ1(K)-AZ2(K)
C(J)=DYBL1
D(J)=DYBL2+FPL(N)=VV*(BX1(I)*PHI(LR)+BX2(I)*PHI(LL))+OMEG2I+
1 PHIXX)*(AX1(I)*PHI(LR)-AX2(I)*PHI(LL))=(AZ1(K)*PHI(LF)+
2 AZ2(K)*PHI(LBK))
GO TO 390
C HYPERBOLIC AND PARABOLIC
351 CONTINUE
A(J)=0,
B(J)=VV*BX1(I=1)=DYBL1=(OMEG2I+PHIXX)*CX(I=1)=AZ1(K)=AZ2(K)
C(J)=DYBL1
D(J)=DYBL2+FPL(N)+VV*(BX1(I=1)*PHI(LL)+BX2(I=1)*PHI(LL)-
1 PHI(LLL))=(OMEG2I+PHIXX)*(CX(I=1)*PHI(LL)-CX(I=2)*PHI(LL)-
2 PHI(LLL))=(AZ1(K)*PHI(LF)+AZ2(K)*PHI(LBK))
GO TO 390
C BODY BOUNDARY J=JW
340 CONTINUE
A(J)=0,
B(J)=CMPLX(1.,0.)
C(J)=0,
D(J)=PHI(L)
390 CONTINUE
PHI(LR)=TPHILR
PHI(LL)=TPHIL
PHI(LLL)=TPHILL
PHI(LBK)=TPHIBK
IF (IOPT,EQ,0) GO TO 300
IF (IFLAG,EQ,1,AND,J,EQ,JW) GO TO 300
B(J)=B(J)+SMALLK*OMEG
300 CONTINUE
C TRIDIAGONAL MATRIX IS SET NOW SOLVE FOR COLUMN OF PHI
CALL TRI(I,K)
C RELAX PHI, FIND ERROR AND MOVE TO NEXT COLUMN
DO 395 J=2,JM1
L=M+J
ERR=OMEGA(J)*(PHI(L)-PHI0G(J))
PHI(L)=PHI0G(J)+ERR
IF (CABS(ERR),LT,CABS(ERROR)) GO TO 395
ERROR=ERR
L=ERR+L
395 CONTINUE

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IF (IFLAG,NE,1) GO TO 200
L=JM+JW
PHI(L)=PHI(L-1)+DY(JWM1)*(PHI(L-1)-PHI(L-2))/DY(JW-2)
PHIUB(N)=PHI(L+1)-DY(JW)*(PHI(L+2)-PHI(L+1))/DY(JWP1)
IF (I,EQ,ITE) GAMTE(K)=PHIUB(N)=PHI(L)
200 CONTINUE
100 CONTINUE
C PRINT OUT ERROR AFTER EACH GRID SWEEP
WRITE (6,905) NITERG,ERROR,LERROR
IF (CABS(ERROR),LT,10.) GO TO 101
WRITE (6,912)
STOP
101 CONTINUE
IDOUB=0
IF (CABS(ERROR),LE,EPSPRD(KGRD)) GO TO 400
IF (NITERG,EQ,NGRID) GO TO 410
IF (MOD(NITERG,NDUMP),EQ,0) GO TO 410
GO TO 50
400 CONTINUE
KGRD=KGRD+1
IDOUB=1
GO TO 410
401 CONTINUE
CALL GAMFUN
WRITE (6,910) NITERG,GAMTE(1),GAMFF(1),GAMTE(KSPAN),GAMFF(KSPAN)
CALL FPRINT
WRITE (6,900)
WRITE (6,906) NITERG
CALL DOUBLE
WRITE (6,914) IM,JM,JW,KM,ILE,ITE,KSPAN
WRITE (6,902)
WRITE (6,903) (X(I),I=1,IM)
WRITE (6,904)
WRITE (6,903) (Y(I),I=1,JM)
WRITE (6,915)
WRITE (6,903) (Z(I),I=1,KM)
GO TO 50
410 CONTINUE
WRITE (7) NITERG,IM,IM1,JM,JM1,KM,KM1,JW,JWP1,JWM1,ITE,ILE,
1 KSPAN,OMEG,SMALLK,DYBU1,DYBU2,DYBL1,DYBL2,NDUUB,XP
WRITE (7) (X(I),DX(I),AX1(I),AX2(I),BX1(I),BX2(I),CX(I),I=1,IM)
WRITE (7) (Y(I),DY(I),AY1(I),AY2(I),I=1,JM)
WRITE (7) (Z(I),DZ(I),AZ1(I),AZ2(I),I=1,KM)
L=ITE*KM
WRITE (7) (FPU(I),FPL(I),PHIUB(I),I=1,L)
WRITE (7) (GAMTE(I),GAMFF(I),I=1,KSPAN)
L=IM*JM*KM
WRITE (7) (PHI(I),I=1,L)
END FILE 7
WRITE (6,907) NITERG
CALL PRINT(NITERG)
IF (KGRD,GT,KEPS) GO TO 420
IF (NITERG,EQ,NGRID) GO TO 430
IF (IDOUB,EQ,1) GO TO 401
GO TO 50

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420 CONTINUE
  WRITE (6,908) NITERG
  GO TO 450
430 CONTINUE
  WRITE (6,909) NITERG
900 FORMAT (1H)
901 FORMAT (1H ,/* CASE IS BEING RESTARTED AT ITERATION=I5)
902 FORMAT (1H ,/* X(I),I=1,IM*)
903 FORMAT (10E13.5)
904 FORMAT (1H ,/* Y(I),I=1,JM*)
905 FORMAT (1H ,/* AT ITERATION=I5* THE MAXIMUM ERROR =2E13.5* AND 0
           OCCURRED AT NODE=I5)
906 FORMAT (1H ,/* .THE NUMBER OF NODES IS BEING DOUBLED AT ITERATION*
           I  I5)
907 FORMAT (1H ,/* TAPE HAS BEEN DUMPED AT ITERATION=I5)
908 FORMAT (1H ,/* SOLUTION HAS CONVERGED TO DESIRED ACCURACY AT ITER
           ATION=I5)
909 FORMAT (1H ,/* MAXIMUM NUMBER OF ITERATIONS HAS BEEN REACHED, CAS
           IE IS BEING TERMINATED AT ITERATION=I5)
910 FORMAT (1H ,/* UPDATE GAMFF AND FARFIELD AT ITERATION=I5,4X* GAMT
           1E(1) =2E13.5,4X* GAMFF(1) =2E13.5,/,4X* GAMTE(KSPAN) =2E13.5*
           2GAMFF(KSPAN) =2E13.5)
911 FORMAT (8A10)
912 FORMAT (1H ,/* SOLUTION IS DIVERGING, THE PROBLEM IS BEING TERMIN
           IATED*)
913 FORMAT (1H ,/* SIMILARITY PARAMETER (K) =E13.5,/,/* SCALING FACTO
           R (CP/CPBAR) =E13.5)
914 FORMAT (1H ,/* IM =I4* JM =I4* JW =I4* KM =I4* ILE =I4
           I * ITE =I4* KSPAN =I4)
915 FORMAT (1H ,/* Z(I),I=1,KM*)
450 CONTINUE
  CALL FPRINT
END
SUBROUTINE DOUBLE
  COMPLEX B,D,PHIUB,PHI,GAMTE1,GAMTE,GAMFF,FPU,FPL
  REAL KCAP,MB
  COMMON /DELTA/ DX(40),DY(40),DZ(40),AX1(40),AX2(40),BX1(40),
1   BX2(40),CX(40),AY1(40),AY2(40),AZ1(20),AZ2(20),X(40),Y(40),
2   Z(20),FPU(800),FPL(800),PHIUB(800),IM,IM1,JM,JM1,KM,KM1,JW,
3   JWP1,JWH1,ITE,ILE,KSPAN,DYBU1,DYBU2,DYBL1,DYBL2,BMALLK,DMEG,
4   NDOUB,CPCPB,TITLE(8),MB,DEL,ALPHA,ITYPE,IOPT,XP,NKPRT,KPRT(20),
5   ZSPAN,KCAP,RPAR
  COMMON /CNEFF/ A(40),B(40),C(40),D(40),PHI(11500)
  COMMON /GAMMA/ GAMTE1(20),GAMTE(20),PGFF,GAMFF(20)
  RETURN
END
SUBROUTINE FARFLD
  COMPLEX B,D,PHI,PHIUB,FPU,FPL,GAMTE1,GAMTE,GAMFF,P1,P10,PART1,
1  PART10,OMK,WING,AMUK,WAKEIN,G1,G2,GAMTE1,CON4,CONS
  REAL KCAP,MB
  COMMON /DELTA/ DX(40),DY(40),DZ(40),AX1(40),AX2(40),BX1(40),
1   BX2(40),CX(40),AY1(40),AY2(40),AZ1(20),AZ2(20),X(40),Y(40),
2   Z(20),FPU(800),FPL(800),PHIUB(800),IM,IM1,JM,JM1,KM,KM1,JW,
3   JWP1,JWH1,ITE,ILE,KSPAN,DYBU1,DYBU2,DYBL1,DYBL2,BMALLK,DMEG,
4   NDOUB,CPCPB,TITLE(8),MB,DEL,ALPHA,ITYPE,IOPT,XP,NKPRT,KPRT(20),

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5 ZSPAN,KCAP,RPAR
COMMON /COEFF/ A(40),B(40),C(40),D(40),PHI(11500)
COMMON /GAMMA/ GAMTE1(20),GAMTE(20),PGFF,GAMFF(20)
COMMON /INTERP/ ZE(25),NZE
C SUBSONIC FARFIELD (ASSUMED SYMMETRY IN Y)
SK=SQRT(KCAP)
CON1=1./6.2831853
CON2=KCAP*CON1
CON3=OMEG/KCAP
AMU=SQRT(OMEG*(CON3+SMALLK))
AMUK=CMPLX(0.,AMU/SK)
BETA2=1.-M5**2
OMK=CMPLX(0.,-CON3)
JW2=2*JW
IMJM=IM*JM
C CALCULATE PART OF WING INTEGRAL
DO 10 I=ILE,ITE
ML=(I-1)*JM+JW
MU=(I-1)*KM
CON4=CEXP(OMK*X(I))
PART1=CMPLX(0.,0.)
DO 20 K=1,KSPAN
L=IMJM+(K-1)+ML
LP=MU+K
P1=PHIUB(LP)-PHI(L)
IF (K.EQ.1) GO TO 21
PART1=PART1+.5*(P1+P10)*DZ(K-1)
21 CONTINUE
P10=P1
20 CONTINUE
PART1=CON4*(PART1+.5*P1*(ZSPAN-Z(KSPAN)))
IF (I.EQ.ILE) GO TO 11
WING=WING+.5*(PART1+PART10)*DX(I-1)
11 CONTINUE
IF (I.EQ.ILE) WING=.5*PART1*X(ILE)
PART10=PART1
10 CONTINUE
C INTEGRATE GAMTE
GAMTEI=CMPLX(0.,0.)
DO 15 K=2,KSPAN
GAMTEI=GAMTEI+.5*(GAMTE(K)+GAMTE(K-1))*DZ(K-1)
15 CONTINUE
GAMTEI=GAMTEI+.5*GAMTE(KSPAN)*(ZSPAN-Z(KSPAN))
C Z=Z(KM)
MP=IMJM*KM1
Z2=Z(KM)**2
DO 30 I=1,IM1
M=MP+(I-1)*JM
X2=X(I)**2
X0=X(I)=1,
X02=X0**2
PHI(M+JW)=CMPLX(0.,0.)
CON4=CON1*CEXP(CMPLX(0.,-SMALLK*X0))*GAMTEI
CON5=CON2*WING*CEXP(CMPLX(0.,CON3*X(I)))
DO 31 J=JWP1,JM

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L=M+J
LL=M+JW2=J
Y2=Y(J)**2
R=KCAP*(Y2+Z2)
BR=SQRT(X02+R)
SR=SQRT(R)
T1=(MB*BR-X0)/BETA2
RH=SR*RPAR
U=T1/RH
CALL WAKE (U,SMALLK,RH,WAKEIN)
G1=KCAP*MB*CEXP(CMPLX(0.,-SMALLK*T1))/(BR*(BR-MB*X0))
G2=WAKEIN/R
BR=SQRT(X2+KCAP*(Y2+Z2))
PHI(L)=CON4*Y(J)*(G1+G2)+CON5*Y(J)*(1.+AMUK*BR)*CEXP(-AMUK*BR)/
1 BR**3
PHI(LL)=PHI(L)
31 CONTINUE
30 CONTINUE
C X=X(1)
X2=X(1)**2
X0=X(1)=1.
X02=X0**2
CON4=CON1*CEXP(CMPLX(0.,-SMALLK*X0))*GAMTEI
CON5=CON2*WING*CEXP(CMPLX(0.,CON3*X(1)))
DO 60 K=1,KM1
M=IMJM*(K-1)
Z2=Z(K)**2
PHI(M+JW)=CMPLX(0.,0.)
DO 61 J=JWP1,JM
L=M+J
LL=M+JW2=J
Y2=Y(J)**2
R=KCAP*(Y2+Z2)
BR=SQRT(X02+R)
SR=SQRT(R)
T1=(MB*BR-X0)/BETA2
RH=SR*RPAR
U=T1/RH
CALL WAKE (U,SMALLK,RH,WAKEIN)
G1=KCAP*MB*CEXP(CMPLX(0.,-SMALLK*T1))/(BR*(BR-MB*X0))
G2=WAKEIN/R
BR=SQRT(X2+KCAP*(Y2+Z2))
PHI(L)=CON4*Y(J)*(G1+G2)+CON5*Y(J)*(1.+AMUK*BR)*CEXP(-AMUK*BR)/
1 BR**3
PHI(LL)=PHI(L)
61 CONTINUE
60 CONTINUE
C X=X(IM)
IJ=IM1*JM
X2=X(IM)**2
X0=X(IM)=1.
X02=X0**2
CON4=CON1*CEXP(CMPLX(0.,-SMALLK*X0))
CON5=CON2*WING*CEXP(CMPLX(0.,CON3*X(IM)))
DO 43 K=1,KM

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M=IMJM*(K-1)+IJ
PHI(M+JW)=CMPLX(0.,0.)
Z2=Z(K)**2
DO 70 I=1,NZE
A(I)=ZE(I)
70 CONTINUE
NEND=NZE
IFLIP=0
DO 44 J=JWP1,JM
IF(Y(J).LE.,5.0R,IFLIP.EQ.1) GO TO 71
DO 72 I=1,KSPAN
A(I)=Z(I)
72 CONTINUE
NEND=KSPAN
IFLIP=1
71 CONTINUE
L=M+J
LL=M+JW2-J
Y2=Y(J)**2
PART1=CMPLX(0.,0.)
IZE=2
DO 45 KK=1,NEND
47 CONTINUE
IF (A(KK).LE.Z(IZE)) GO TO 48
IZE=IZE+1
GO TO 47
48 CONTINUE
R=KCAP*(Y2+(Z(K)-A(KK))**2)
BR=SQRT(X02+R)
SR=SQRT(R)
T1=(MB*BR-X0)/BETA2
RH=SR*RPAR
U=T1/RH
CALL WAKE (U,SMALLK,RH,WAKEIN)
G1=KCAP*MA*CEXP(CMPLX(0.,-SMALLK*T1))/(BR*(BR-MB*X0))
G2=WAKEIN/R
P1=GAMTE(IZE-1)+(A(KK)-Z(IZE-1))/DZ(IZE-1)*(GAMTE(IZE)-
1 GAMTE(IZE-1)))*(G1+G2)
IF (KK.EQ.1) GO TO 46
PART1=PART1+.5*(P1+P10)*(A(KK)-A(KK-1))
46 CONTINUE
P10=P1
45 CONTINUE
PART1=CON4*Y(J)*(PART1+.5*P1*(ZSPAN-Z(KSPAN)))
BR=SQRT(X2+KCAP*(Y2+Z2))
PHI(L)=PART1+CON5*Y(J)*(1.+AMUK*BR)*CEXP(-AMUK*BR)/BR**3
PHI(LL)=PHI(L)
44 CONTINUE
43 CONTINUE
C Y=Y(1) AND Y=Y(JM)
J=JM
Y2=Y(J)**2
DO 53 K=1,KM1
MP=IMJM*(K-1)
Z2=Z(K)**2

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DO 54 I=2,IM1
M=MPI+(I-1)*JM
L=M+J
LL=M+JW2-J
X2=X(I)**2
X0=X(I)-1.
X02=X0**2
CON4=CON1*CEXP(CMPLX(0.,-SMALLK*X0))*GAMTE1
CON5=CON2*WING*CEXP(CMPLX(0.,CON3*X(I)))
R=KCAP*(Y2+Z2)
BR=SQRT(X02+R)
SR=SQRT(R)
T1=(MB*BR-X0)/BETA2
RH=SR*RPAR
U=T1/RH
CALL WAKE(U,SMALLK,RH,WAKEIN)
G1=KCAP+MB*CEXP(CMPLX(0.,-SMALLK*T1))/(BR*(BR-MB*X0))
G2=WAKEIN/R
BR=SQRT(X2+KCAP*(Y2+Z2))
PHI(L)=CON4*Y(J)*(G1+G2)+CON5*Y(J)*(1.+AMUK*BR)*CEXP(-AMUK*BR)/
1 BR**3
PHI(LL)=-PHI(L)
54 CONTINUE
55 CONTINUE
RETURN
END
SUBROUTINE FPRINT
COMPLEX B,D,PHIUB,PHI,GAMTE1,GAMTE,GAMFF,FPU,FPL,PART,C1,C2,
1 C10,C20,CL,CM,CL0,CM0,CLIFT,CMOM,GAMPRT,B1,D1
REAL KCAP,MB
COMMON /DELT/ DX(40),DY(40),DZ(40),AX1(40),AX2(40),BX1(40),
1 BX2(40),CX(40),AY1(40),AY2(40),AZ1(20),AZ2(20),X(40),Y(40),
2 Z(20),FPU(800),FPL(800),PHIUB(800),IM,IM1,JM,JM1,KM,KM1,JW,
3 JWP1,JWM1,ITE,ILE,KSPAN,DYBU1,DYBU2,DYBL1,DYBL2,SMALLK,OMEG,
4 NDOUM,CPCPB,TITLE(8),MB,DEL,ALPHA,ITYPE,IOPT,XP,NKPRT,KPRT(20),
5 ZSPAN,KCAP,RPAR
COMMON /COEFF/ A(40),B(40),C(40),D(40),PHI(11500)
COMMON /GAMMA/ GAMTE1(20),GAMTE(20),PGFF,GAMFF(20)
DIMENSION B1(40),D1(40)
CPDEL=CPCPB/DEL
WRITE (6,900)
WRITE (6,901) (TITLE(I),I=1,8)
WRITE (6,902) MB
WRITE (6,903) KCAP
WRITE (6,904) DEL
WRITE (6,905) ALPHA
WRITE (6,906) SMALLK
WRITE (6,907) OMEG
WRITE (6,908) XP
WRITE (6,909) ZSPAN
WRITE (6,910) CPCPB
WRITE (6,911)
WRITE (6,912) (X(I),I=ILE,ITE)
CLIFT=CMPLX(0.,0.)
CMOM=CMPLX(0.,0.)

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DO 10 K=1,KSPAN
PART=.5*((X(ITE+1)=1.)*(GAMFF(K)-GAMTE(K))/(X(IM1)=1.)*GAMTE(K))
IF (IOPR.EQ.1) PART=PART*CEXP(CMPLX(0.,-SMALLK*(X(ITE+1)=1.)))
MP=IM+JM*(K-1)
IJK=MP+ITE*JM+JW
PHI(IJK)=PHI(IJK)-PART
L=MP+(ILE-2)*JM+JW
LP=(ILE-2)*KM+K
PHIUB(LP)=PHI(L)
LP=ITE*KM+K
PHIUB(LP)=PHI(IJK)+2.*PART
DO 20 I=ILE,ITE
M=MP+(I-1)*JM
L=M+JW
LP=(I-1)*KM+K
B(I)=-2.*AX1(I)*(PHI(L+JM)-PHI(L))+AX2(I)*(PHI(L)-PHI(L+JM))*
! CPDEL
D(I)=-2.*AX1(I)*(PHIUB(LP+KM)-PHIUB(LP))+AX2(I)*(PHIUB(LP)-
! PHIUB(LP-KM)))*CPDEL
IF (IOPR.EQ.0) GO TO 24
C1=CMPLX(0.,2.*SMALLK)*CPDEL
B(I)=B(I)-C1*PHI(L)
D(I)=D(I)-C1*PHIUB(LP)
24 CONTINUE
IF (K.GT.1) GO TO 21
B1(I)=B(I)
D1(I)=D(I)
21 CONTINUE
C1=B(I)-D(I)
C2=C1*(X(I)-XP)
IF (I.GT.ILE) GO TO 22
CL=C1*X(ILE)
CM=.5*C2*X(ILE)
GO TO 23
22 CONTINUE
CL=CL+.5*(C1+C10)*DX(I-1)
CM=CM+.5*(C2+C20)*DX(I-1)
23 CONTINUE
C10=C1
C20=C2
20 CONTINUE
PHI(IJK)=PHI(IJK)+PART
IF (K.EQ.1) GO TO 11
CLIFT=CLIFT+.5*(CL+C10)*DZ(K-1)
CMOM=CMOM+.5*(CM+C20)*DZ(K-1)
11 CONTINUE
CLO=CL
CMO=CM
DO 12 N=1,NKPRT
IF (KPRT(N).NE.K) GO TO 12
GAMPRT=2.*GAMTE(K)*CPDEL
WRITE (6,913) Z(K),GAMPRT
WRITE (6,914)
WRITE (6,915) (D(I),I=ILE,ITE)
WRITE (6,916)

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        WRITE (6,915) (B(I),I=ILE,ITE)
        GO TO 10
12 CONTINUE
10 CONTINUE
        WRITE (6,900)
        WRITE (6,901) (TITLE(I),I=1,8)
        WRITE (6,902) M8
        WRITE (6,903) KCAP
        WRITE (6,904) DEL
        WRITE (6,905) ALPHA
        WRITE (6,906) SMALLK
        WRITE (6,907) OMEG
        WRITE (6,908) XP
        WRITE (6,909) ZSPAN
        WRITE (6,910) CPCPB
        GAMPRTE2,*GAMTE(1)*CPDEL
        GO TO (30,35,40),ITYPE
30 CONTINUE
        WRITE (6,917)
        WRITE (6,918) CLIFT,CMOM
        WRITE (6,913) Z(1),GAMPRT
        WRITE (6,919)
        GO TO 45
35 CONTINUE
        WRITE (6,920)
        WRITE (6,918) CLIFT,CMOM
        WRITE (6,913) Z(1),GAMPRT
        WRITE (6,921)
        GO TO 45
40 CONTINUE
        WRITE (6,922)
        WRITE (6,918) CLIFT,CMOM
        WRITE (6,913) Z(1),GAMPRT
        WRITE (6,923)
45 CONTINUE
        WRITE (6,911)
        WRITE (6,912) (X(I),I=ILE,ITE)
        WRITE (6,914)
        WRITE (6,915) (D1(I),I=ILE,ITE)
        WRITE (6,916)
        WRITE (6,915) (B1(I),I=ILE,ITE)
900 FORMAT (1H1)
901 FORMAT (30X,8A10)
902 FORMAT (1H ,/,1H ,/, * MACH NUMBER **E13.5)
903 FORMAT (* SIMILARITY PARAMETER **E13.5)
904 FORMAT (* THICKNESS RATIO **E13.5)
905 FORMAT (* AIRFOIL ANGLE OF ATTACK (RADIAN) **E13.5)
906 FORMAT (* REDUCED FREQUENCY (BASED ON CHORD) **E13.5)
907 FORMAT (* SCALED FREQUENCY (OMEGA) **E13.5)
908 FORMAT (* PITCH AXIS (XP) **E13.5)
909 FORMAT (* WING ASPECT RATIO **E13.5)
910 FORMAT (* CP SCALING FACTOR (CP/CPBAR) **E13.5)
911 FORMAT (1H ,/,1H ,/,3X*AIRFOIL STREAMWISE COORDINATE*)
912 FORMAT (3XE13.5,13XE13.5,13XE13.5,13XF13.5,13XE13.5)
913 FORMAT (1H ,/,1H ,/,15X*AIRFOIL SPANWISE COORDINATE **E13.5

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1 * SECTION LIFT COEFFICIENT **2E13.5)
914 FORMAT (1H ,/,1H ,/,3X*AIRFOIL PRESSURE COEFFICIENTS, UPPER **)
915 FORMAT (3X10E13.5)
916 FORMAT (1H ,/,1H ,/,3X*AIRFOIL PRESSURE COEFFICIENTS, LOWER **)
917 FORMAT (1H ,/,1H ,/,* UNSTEADY FORCE COEFFICIENTS (PER UNIT PITCH
    ANGLE IN RADIANS)*)
918 FORMAT (1H ,/,3X*LIFT **2E13.5,/,3X*MOMENT ABOUT (X=XP) **2E13.5)
919 FORMAT (1H ,/,1H ,/,* PRESSURE COEFFICIENTS ON THE AIRFOIL (PER UN
    IT PITCH ANGLE IN RADIANS)*)
920 FORMAT (1H ,/,1H ,/,* UNSTEADY FORCE COEFFICIENTS*)
921 FORMAT (1H ,/,1H ,/,* PRESSURE COEFFICIENTS ON THE AIRFOIL*)
922 FORMAT (1H ,/,1H ,/,* UNSTEADY FORCE COEFFICIENTS (PER UNIT PLUNGE
    1 DISPLACEMENT NORMALIZED TO CHORD)*)
923 FORMAT (1H ,/,1H ,/,* PRESSURE COEFFICIENTS ON THE AIRFOIL (PER UN
    IT PLUNGE DISPLACEMENT NORMALIZED TO CHORD)*)
      RETURN
      END
      SUBROUTINE GAMFUN
      COMPLEX PHIUB,GAMTE1,GAMTE,GAMFF,FPU,FPL
      REAL KCAP,MB
      COMMON /DELTA/ DX(40),DY(40),DZ(40),AX1(40),AX2(40),BX1(40),
1     BX2(40),CX(40),AY1(40),AY2(40),AZ1(20),AZ2(20),X(40),Y(40),
2     Z(20),FPU(800),FPL(800),PHIUB(800),IM,IM1,JM,JM1,KM,KM1,JW,
3     JWP1,JWM1,ITE,ILE,KSPAN,DYBU1,DYBU2,DYBL1,DYBL2,SMALLK,OMEG,
4     NDOUB,CPCPB,TITLE(8),MB,DEL,ALPHA,ITYPE,IOPT,XP,NKPRT,KPRT(20),
5     ZSPAN,KCAP,RPAR
      COMMON /GAMMA/ GAMTE1(20),GAMTE(20),PGFF,GAMFF(20)
      DO 10 I=1,KSPAN
      GAMFF(I)=GAMTE1(I)+PGFF*(GAMTE(I)-GAMTE1(I))
      GAMTE1(I)=GAMTE(I)
10   CONTINUE
      RETURN
      END
      SUBROUTINE INITIAL
      COMPLEX PHIUB,FPU,FPL
      REAL KCAP,MB
      COMMON /DELTA/ DX(40),DY(40),DZ(40),AX1(40),AX2(40),BX1(40),
1     BX2(40),CX(40),AY1(40),AY2(40),AZ1(20),AZ2(20),X(40),Y(40),
2     Z(20),FPU(800),FPL(800),PHIUB(800),IM,IM1,JM,JM1,KM,KM1,JW,
3     JWP1,JWM1,ITE,ILE,KSPAN,DYBU1,DYBU2,DYBL1,DYBL2,SMALLK,OMEG,
4     NDOUB,CPCPB,TITLE(8),MB,DEL,ALPHA,ITYPE,IOPT,XP,NKPRT,KPRT(20),
5     ZSPAN,KCAP,RPAR
C   CALCULATE DX,DY AND DZ
      DO 10 I=1,IM1
      DX(I)=X(I+1)-X(I)
10   CONTINUE
      DO 20 I=1,JM1
      DY(I)=Y(I+1)-Y(I)
20   CONTINUE
      DO 30 I=1,KM1
      DZ(I)=Z(I+1)-Z(I)
30   CONTINUE
C   FINITE DIFFERENCE COEFFICIENTS
      DO 40 I=2,IM1
      AX1(I)=DX(I-1)/(DX(I)+(DX(I-1)+DX(I)))

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AX2(I)=DX(I)/(DX(I-1)+(DX(I-1)+DX(I)))
BX1(I)=2.*AX1(I)/DX(I-1)
BX2(I)=2.*AX2(I)/DX(I)
CX(I)=.5/DX(I)
40 CONTINUE
CX(I)=.5/DX(I)
DO 50 I=2,JM1
AY1(I)=2./(DY(I)*(DY(I)+DY(I-1)))
AY2(I)=2./(DY(I-1)*(DY(I)+DY(I-1)))
50 CONTINUE
DO 60 I=2,KM1
AZ1(I)=2./(DZ(I)*(DZ(I)+DZ(I-1)))
AZ2(I)=2./(DZ(I-1)*(DZ(I)+DZ(I-1)))
60 CONTINUE
AZ1(1)=2./DZ(1)*2
AZ2(1)=0.
DYBU1=2./(DY(JWP1)+2.*DY(JW))*DY(JWP1)
DYBU2=DY(JWP1)*DYBU1
DYBL1=2./(DY(JW-2)+2.*DY(JWM1))*DY(JW-2)
DYBL2=DY(JW-2)*DYBL1
C SET AIRFOIL BOUNDARY CONDITION
FLOPT=FLOAT(IOPT)
DO 70 K=1,KSPAN
DO 80 I=ILE,ITE
L=(I-1)*KM+K
IF (ITYPE.EQ.1) FPU(L)=CMPLX(-1.,-FLOPT*SMALLK*(X(I)-XP))
C *** A NEW FUNCTIONAL DEPENDENCE CAN BE INSERTED HERE FOR ITYPE=2
IF (ITYPE.EQ.3) FPU(L)=CMPLX(0.,-FLOPT*SMALLK)
FPL(L)=FPU(L)
80 CONTINUE
70 CONTINUE
RETURN
END
SUBROUTINE PRINT (NITERG)
COMPLEX B,D,PHIUB,PHI,GAMTE1,GAMTE,GAMFF,FPU,FPL,PART
REAL KCAP,M8
COMMON /DELTA/ DX(40),DY(40),DZ(40),AX1(40),AX2(40),BX1(40),
1 BX2(40),CX(40),AY1(40),AY2(40),AZ1(20),AZ2(20),X(40),Y(40),
2 Z(20),FPU(800),FPL(800),PHIUB(800),IM,IM1,JM,JM1,KM,KM1,JW,
3 JWP1,JWM1,ITE,ILE,KSPAN,DYBU1,DYBU2,DYBL1,DYBL2,SMALLK,OMEG,
4 NDQUB,CPCPB,TITLE(R),M8,DEL,ALPHA,ITYPE,IOPT,XP,NKPRT,KPRT(20),
5 ZSPAN,KCAP,RPAR
COMMON /COEFF/ A(40),B(40),C(40),D(40),PHI(11500)
COMMON /GAMMA/ GAMTE1(20),GAMTE(20),PGFF,GAMFF(20)
KSPAN1=KSPAN-1
DO 10 K=1,KSPAN,KSPAN1
PART=.5*((X(ITE+1)-1.)*(GAMFF(K)-GAMTE(K))/(X(IM1)-1.)*GAMTE(K))
MP=IM*JM*(K-1)
IJK=MP+ITE*JM+JW
PHI(IJK)=PHI(IJK)-PART
L=MP+(ILE-2)*JM+JW
LP=(ILE-2)*KM+K
PHIUB(LP)=PHI(L)
LP=ITE*KM+K

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      PHIUB(LP)=PHI(IJK)+2.*PART
C COMPUTE CP LOWER (B) AND CP UPPER (D)
      DO 20 I=ILE,ITE
      L=MPI+(I-1)*JM+JW
      LP=(I-1)*KM+K
      B(I)=2.*AX1(I)*(PHI(L+JM)-PHI(L))+AX2(I)*(PHI(L)-PHI(L-JM))
      D(I)=2.*AX1(I)*(PHIUB(LP+KM)-PHIUB(LP))+AX2(I)*(PHIUB(LP)-
      1 PHIUB(LP-KM)))
20 CONTINUE
      PHI(IJK)=PHI(IJK),PART
      WRITE (6,901) NITERG,K
      WRITE (6,902) (D(I),I=ILE,ITE)
      WRITE (6,903) NITERG,K
      WRITE (6,902) (B(I),I=ILE,ITE)
10 CONTINUE
901 FORMAT (1H ,/, * AT ITERATION*IS* AND K =*I3* SCALED PRESSURE COEFF
1ICIENT, UPPER (ILE TO ITE) **)
903 FORMAT (1H ,/, * AT ITERATION*IS* AND K =*I3* SCALED PRESSURE COEFF
1ICIENT, LOWER (ILE TO ITE) **)
902 FORMAT (10E13.5)
      RETURN
      END
      SUBROUTINE TRI (I,K)
      COMPLEX B,D,PHIUB,PHI,FPU,FPL,P
      REAL KCAP,M8
      COMMON /DELTA/ DX(40),DY(40),DZ(40),AX1(40),AX2(40),BX1(40),
1 BX2(40),CX(40),AY1(40),AY2(40),AZ1(20),AZ2(20),X(40),Y(40),
2 Z(20),FPU(800),FPL(800),PHIUB(800),IM,IM1,JM,JM1,KM,KM1,JW,
3 JWP1,JWM1,ITE,ILE,KSPAN,DYBU1,DYBU2,DYBL1,DYBL2,SMALLK,OMEG,
4 NDOUB,CPCPA,TITLE(8),M8,DEL,ALPHA,ITYPE,IOPT,XP,NKPRT,KPRT(20),
5 ZSPAN,KCAP,RPAR
      COMMON /COEFF/ A(40),B(40),C(40),D(40),PHI(11500)
      MPI=IM*KM*(K-1)
      DO 10 KK=3,JM1
      J=JM1-KK+3
      P=A(J-1)/B(J)
      B(J-1)=B(J-1)-P*C(J)
      D(J-1)=D(J-1)-P*D(J)
10 CONTINUE
      MPI=(I-1)*JM
      PHI(M+2)=D(2)/B(2)
      DO 20 J=3,JM1
      L=M+J
      PHI(L)=(D(J)-PHI(L-1)*C(J))/B(J)
20 CONTINUE
      RETURN
      END
      SUBROUTINE WAKE (U,SMALLK,RH,WAKEIN)
      COMPLEX PART1,PART2,PART3,PART4,EKRAU,CKRH,WAKEIN
      REAL KRM
      DIMENSION B(12)
      DATA C / .372 /
      DATA (B(I),I=1,12) / 1., -24186198, 2.7918027, -24.991079, 111.59196,
1 -271.43549, 305.75288, 41.18363, -545.98537, 644.78155, -328.72755,
2 64.279511 /

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C CALCULATE I1 FOR WAKE INTEGRAL
IF (SMALLK,EQ.,0.) GO TO 15
PART2=CMPLX(0.,0.)
PART3=PART2
PART4=PART2
AU=ABS(U)
SU=SQRT(1.+U**2)
KRH=SMALLK*RH
CKRH=CMPLX(0.,KRH)
EKRAU=CEXP(CMPLX(0.,-KRH*AU))
PART1=-AU*EKRAU/SU
DO 10 I=1,12
AM=FLOAT(I=1)
PART2=PART2+B(I)*EKRAU*EXP(-C*AM*AU)/(C*AM+CKRH)
10 CONTINUE
IF (U.GT.0.) GO TO 30
PART3=PART1
PART4=PART2
DO 20 I=1,12
AM=FLOAT(I=1)
PART4=PART4-B(I)/(C*AM+CKRH)
20 CONTINUE
30 CONTINUE
PART2=PART2*CKRH
PART4=PART4*CKRH
WAKEIN=PART1+PART2+2.*REAL(PART3+PART4)
RETURN
15 CONTINUE
WAKEIN=CMPLX(1.,-U/SQRT(1.+U**2),0.)
RETURN
END

```