

# Bayesian Inversion of Radar Clutter

Peter Gerstoft

Marine Physical Laboratory, Scripps Institution of Oceanography  
La Jolla, CA 92093-0238

phone: (858) 534-7768 fax: (858) 534-7641 email: [gerstoft@ucsd.edu](mailto:gerstoft@ucsd.edu)

William S Hodgkiss

Marine Physical Laboratory, Scripps Institution of Oceanography  
La Jolla, CA 92093-0238I

phone: (858) 534-1798 fax: (858) 534-7641 email: [wsh@mpl.ucsd.edu](mailto:wsh@mpl.ucsd.edu)

William A Kuperman

Marine Physical Laboratory, Scripps Institution of Oceanography  
La Jolla, CA 92093-0238

phone: (858) 534-7990 fax: (858) 534-7641 email: [wak@mpl.ucsd.edu](mailto:wak@mpl.ucsd.edu)

Award Number: N00014-03-1-0393

<http://www-mpl.ucsd.edu/people/gerstoft>

## LONG-TERM GOALS

The long-term goal of this project is to develop inversion approaches that enable the estimation of refractivity profiles and the associated uncertainty. Further to develop methods for mapping the refractivity parameters and their associated uncertainty into propagation.

## OBJECTIVES

The development of new parametric approaches for the inversion of radar clutter data to estimate atmospheric refractivity including an assessment of the quality of the parameter estimates.

## APPROACH

Our inversion approach has mainly been based on SAGA [Gerstoft 97] and focused on estimation of the parameters corresponding to the field that gives the best fit to the data. We have concentrated on demonstrating the feasibility of RFC using an efficient 11-parameter description of the environment. The quality of the inversion was addressed by comparing the field using the estimated parameters to a measured field [Gerstoft 03a, Gerstoft 03b, Gerstoft 03c]. Little has been done to indicate the quality of the solution for each parameter, either with the variance of parameter-estimate or preferably the complete *a posteriori* distribution. We have already done much work on this in an ocean acoustic context [Gerstoft 98], but this has not been explored in our RFC processing to date. This will entail developing likelihood formulations and importance sampling algorithms. This inversion approach will show the information content in the data, the importance of each parameter, and the quality of the inversions.

## WORK COMPLETED

# Report Documentation Page

Form Approved  
OMB No. 0704-0188

Public reporting burden for the collection of information is estimated to average 1 hour per response, including the time for reviewing instructions, searching existing data sources, gathering and maintaining the data needed, and completing and reviewing the collection of information. Send comments regarding this burden estimate or any other aspect of this collection of information, including suggestions for reducing this burden, to Washington Headquarters Services, Directorate for Information Operations and Reports, 1215 Jefferson Davis Highway, Suite 1204, Arlington VA 22202-4302. Respondents should be aware that notwithstanding any other provision of law, no person shall be subject to a penalty for failing to comply with a collection of information if it does not display a currently valid OMB control number.

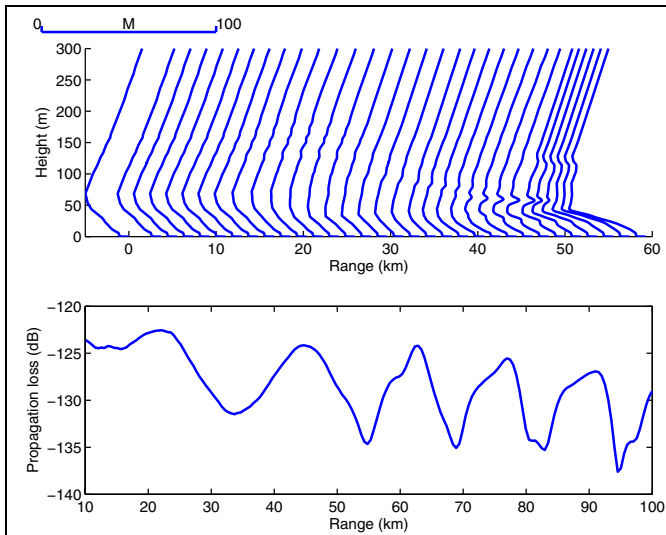
1. REPORT DATE <b>30 SEP 2003</b>		2. REPORT TYPE		3. DATES COVERED <b>00-00-2003 to 00-00-2003</b>	
4. TITLE AND SUBTITLE <b>Bayesian Inversion of Radar Clutter</b>				5a. CONTRACT NUMBER	
				5b. GRANT NUMBER	
				5c. PROGRAM ELEMENT NUMBER	
6. AUTHOR(S)				5d. PROJECT NUMBER	
				5e. TASK NUMBER	
				5f. WORK UNIT NUMBER	
7. PERFORMING ORGANIZATION NAME(S) AND ADDRESS(ES) <b>Marine Physical Laboratory, Scripps Institution of Oceanography,,La Jolla,,CA,92093</b>				8. PERFORMING ORGANIZATION REPORT NUMBER	
9. SPONSORING/MONITORING AGENCY NAME(S) AND ADDRESS(ES)				10. SPONSOR/MONITOR'S ACRONYM(S)	
				11. SPONSOR/MONITOR'S REPORT NUMBER(S)	
12. DISTRIBUTION/AVAILABILITY STATEMENT <b>Approved for public release; distribution unlimited</b>					
13. SUPPLEMENTARY NOTES					
14. ABSTRACT					
15. SUBJECT TERMS					
16. SECURITY CLASSIFICATION OF:			17. LIMITATION OF ABSTRACT	18. NUMBER OF PAGES	19a. NAME OF RESPONSIBLE PERSON
a. REPORT <b>unclassified</b>	b. ABSTRACT <b>unclassified</b>	c. THIS PAGE <b>unclassified</b>			

An algorithm for estimation of propagation loss and its statistical properties based on radar sea clutter has been developed [Gerstoft 03d].

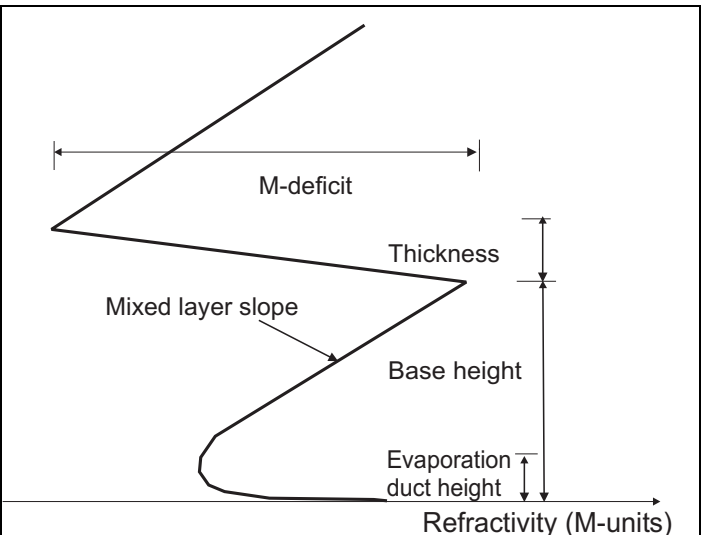
## RESULTS

The simulated data are generated based on the helicopter measured range-dependent refractivity profiles (Run 7) for the Wallops 98 experiment [Gerstoft03a], see Fig 1. A range interval from 10-100 km is used. A simple trilinear model (Fig 2) is used for the inversion of the refractivity profile as outlined in the Appendix of [Gerstoft03a]. We then search for tri-linear refractivity parameters at 0 and 100 km range. To obtain refractivity profiles at other ranges the parameters are interpolated linearly. The first 3 parameters were given a uniform distribution but the slope was given a non-uniform distribution as indicated in Fig 3 (left bottom). This is because a negative mixed layer slope is only likely for shallow ducts (low base height).

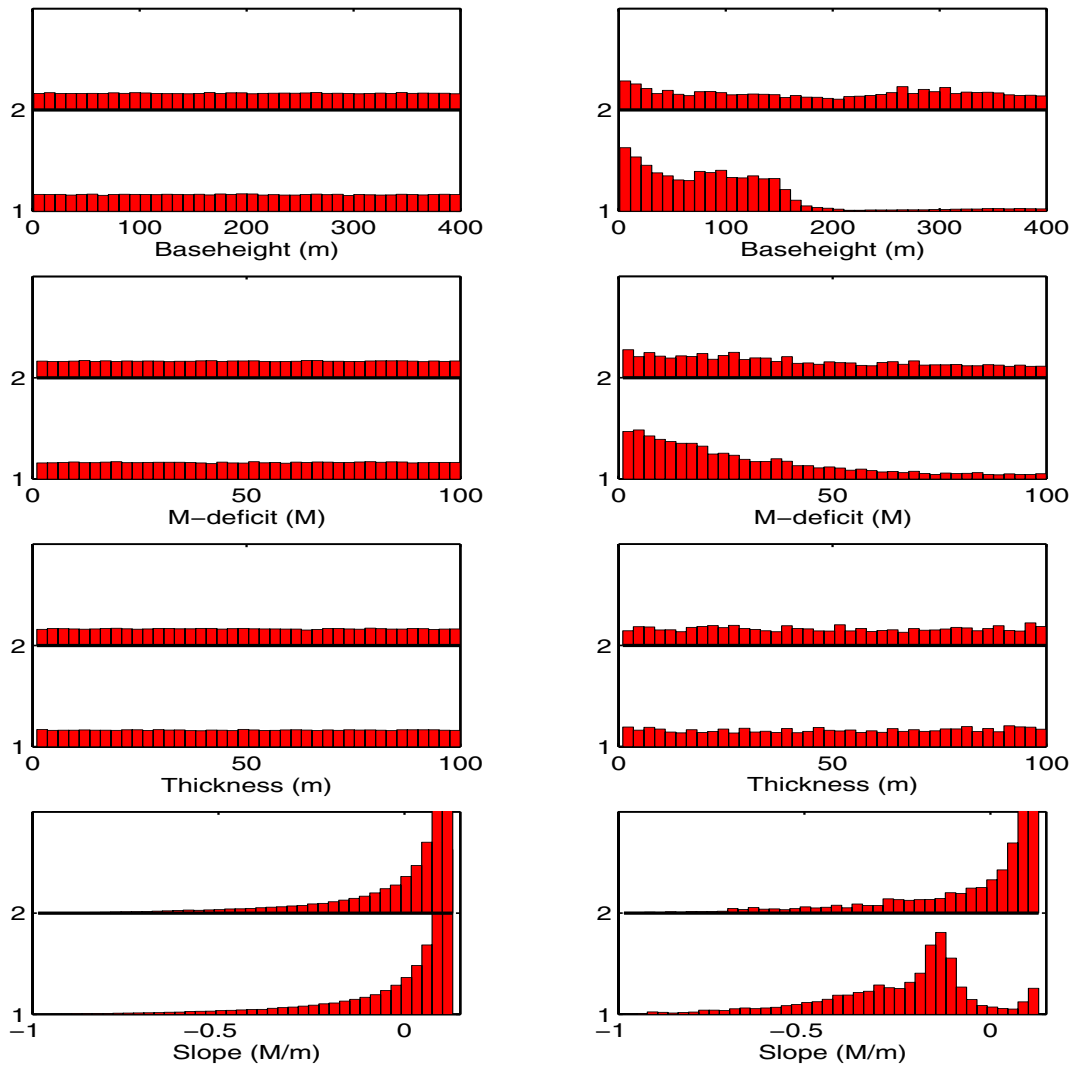
First, 90,000 environmental models are selected from the prior distributions, Fig 3 left. Using these environmental models, 90,000 vectors of propagation loss versus range are precomputed. The posteriori distribution (right column Fig. 3) is computed as a product of the prior distributions with the likelihood distribution. The likelihood distribution shows how well the environmental models describe the data. We note that the overall behavior of the posteriori distributions seems reasonable.



**Figure 1 (a) The observed refractivity profile and (b) the simulated propagation loss data.**



**Figure 2 Trilinear model. We invert for the base height, thickness, M-deficit and the mixed layer slope.**

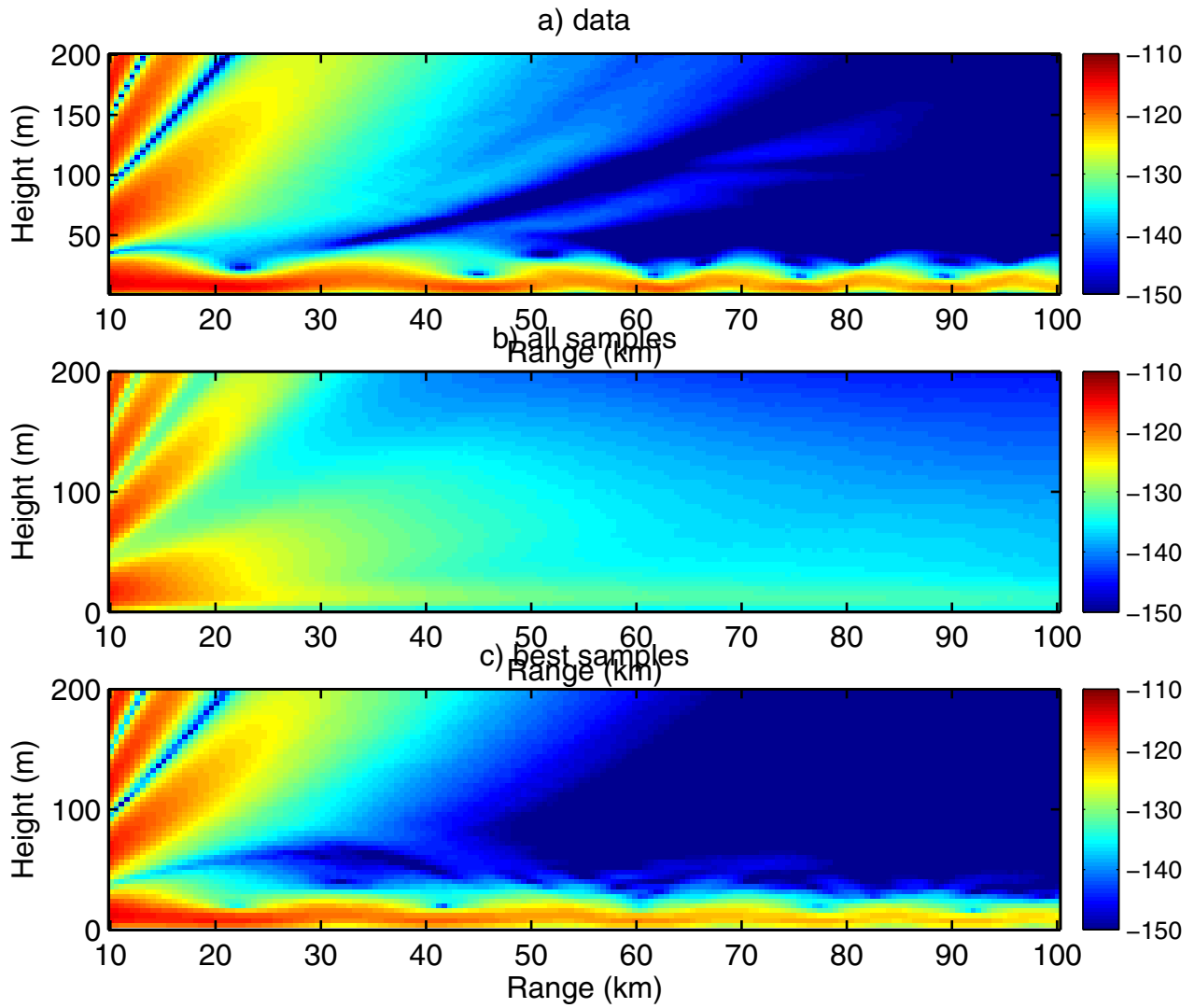


**Figure 3** Prior (left) and posteriori (right) distributions of the parameter estimates. The abscissa “1” and “2” refers to the values at emitter and receiver, respectively.

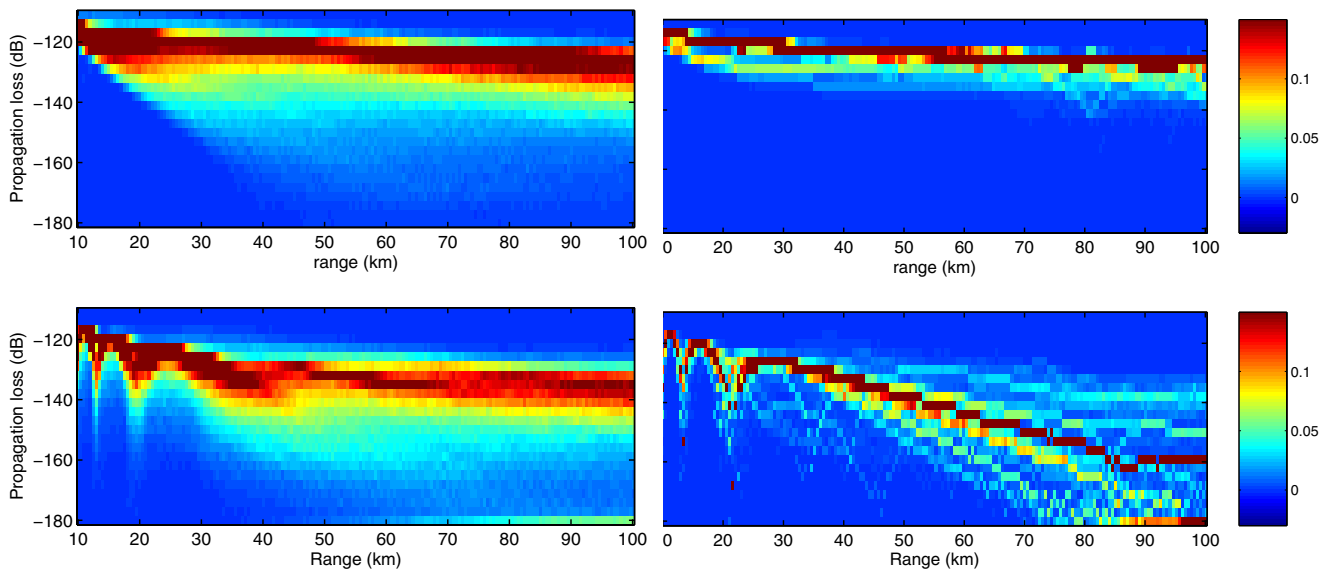
The overall objective is being able to estimate posteriori statistics of propagation loss. An example of this is shown in Fig 4. We compute the average priori propagation loss based on an even weighting of the propagation loss from each generated refractivity model. The posteriori probability distribution of the propagation loss is based on weighting the propagation loss from each refractivity model with the posteriori probability.

The average prior and posteriori propagation losses are shown in Fig. 4b and c. It is seen that the average posteriori propagation loss identifies a ducting environment as observed in the data, Fig. 4a, but the prior does not.

The probability distribution of the propagation loss then is computed at all ranges and depths. Both prior (Fig. 5 left) and posteriori (Fig. 5 right) propagation loss are shown at 10 and 100 m height as a function of range. Clearly, the posteriori plot shows how the data has improved our estimation of propagation loss.



**Figure 4:** The propagation-loss field from the true environment (from Fig. 1a) and the average propagation-loss field based on (b) prior information, and (c) posteriori information (bottom).



**Figure 5** Prior (left) and posteriori (right) propagation loss probability distributions at 10 m (top) and 100 m (bottom).

## IMPACT/APPLICATIONS

Knowledge of refractivity profiles is important for radar performance prediction. A very promising approach is to determine refractivity based on the radar clutter return.

## RELATED PROJECTS

*Refractivity Data Fusion and Assimilation (Ted Rogers, SPAWAR)*: This project is concerned with near real-time techniques for inferring refractivity parameters from radar sea clutter.

## REFERENCES

- [Gerstoft 97] Gerstoft, P., "SAGA user guide 2.0, an inversion software package," SACLANTCEN SM-333. SACLANT Undersea Research Centre, La Spezia, Italy, (1997)
- [Gerstoft 98] Gerstoft, P. and C.F. Mecklenbräuker, "Ocean acoustic inversion with estimation of a posteriori probability distributions," *J. Acoust. Soc. Am.* 104:808-819. (1998)
- [Gerstoft 03a] Gerstoft, P., L. Ted Rogers, W.S. Hodgkiss and J. Krolik "Inversion for refractivity parameters from radar sea clutter," *Radio Science*, 38:1-22, (March 2003)
- [Gerstoft 03b] Gerstoft, P., L. T. Rodgers, W.S. Hodgkiss and L.J. Wagner, "Refractivity estimation using multiple elevation angles," *IEEE Oceanic Eng.* (July 2003)
- [Gerstoft 03c] Gerstoft, P., L.T. Rogers, W.S. Hodgkiss, "Refractivity Estimation using Multiple Elevation Angles," *URSI, IEEE Antennas and Propagation Meeting, Columbus, June 2003*

## **PUBLICATIONS**

[Gerstoft 03d] Gerstoft, P., L.T. Rogers, and W.S. Hodgkiss, "Posteriori estimation of low altitude propagation loss from radar sea clutter data," IEEE Oceans Conference, San Diego (2003)