

ARMY RESEARCH LABORATORY



Modeling and Calibrating a 4-wheel Skid-Steer Research Robot

by Gary Haas

ARL-TN-0370

September 2009

NOTICES

Disclaimers

The findings in this report are not to be construed as an official Department of the Army position unless so designated by other authorized documents.

Citation of manufacturer's or trade names does not constitute an official endorsement or approval of the use thereof.

Destroy this report when it is no longer needed. Do not return it to the originator.

Army Research Laboratory

Aberdeen Proving Ground, MD 21005-5066

ARL-TN-0370

September 2009

Modeling and Calibrating a 4-wheel Skid-Steer Research Robot

Gary Haas

Vehicle Technology Directorate, ARL

Approved for public release; distribution unlimited.

REPORT DOCUMENTATION PAGE			Form Approved OMB No. 0704-0188		
Public reporting burden for this collection of information is estimated to average 1 hour per response, including the time for reviewing instructions, searching existing data sources, gathering and maintaining the data needed, and completing and reviewing the collection information. Send comments regarding this burden estimate or any other aspect of this collection of information, including suggestions for reducing the burden, to Department of Defense, Washington Headquarters Services, Directorate for Information Operations and Reports (0704-0188), 1215 Jefferson Davis Highway, Suite 1204, Arlington, VA 22202-4302. Respondents should be aware that notwithstanding any other provision of law, no person shall be subject to any penalty for failing to comply with a collection of information if it does not display a currently valid OMB control number. PLEASE DO NOT RETURN YOUR FORM TO THE ABOVE ADDRESS.					
1. REPORT DATE (DD-MM-YYYY) September 2009		2. REPORT TYPE Final		3. DATES COVERED (From - To) 2009	
4. TITLE AND SUBTITLE Modeling and Calibrating a 4-wheel Skid-Steer Research Robot			5a. CONTRACT NUMBER		
			5b. GRANT NUMBER		
			5c. PROGRAM ELEMENT NUMBER		
6. AUTHOR(S) Gary Haas			5d. PROJECT NUMBER 1L162618AH80		
			5e. TASK NUMBER		
			5f. WORK UNIT NUMBER		
7. PERFORMING ORGANIZATION NAME(S) AND ADDRESS(ES) U.S. Army Research Laboratory ATTN: RDRL-VTU Aberdeen Proving Ground MD 21005-5066			8. PERFORMING ORGANIZATION REPORT NUMBER ARL-TN-0370		
9. SPONSORING/MONITORING AGENCY NAME(S) AND ADDRESS(ES)			10. SPONSOR/MONITOR'S ACRONYM(S)		
			11. SPONSOR/MONITOR'S REPORT NUMBER(S)		
12. DISTRIBUTION/AVAILABILITY STATEMENT Approved for public release; distribution unlimited.					
13. SUPPLEMENTARY NOTES					
14. ABSTRACT This report describes the calibration of a commercial Roboteq motor controller which was installed in an iRobot ATRV Jr research robot as part of a system upgrade. The objective of the calibration was to determine the transfer function between a command issued to the robot control system and the path followed by the robot and all relevant parameters. Implicit in the calibration is validation of the model on which the transfer function is based, which is a kinematic model of a 4-wheel skid-steer vehicle.					
15. SUBJECT TERMS Robot, skid-steer, calibrate					
16. SECURITY CLASSIFICATION OF:			17. LIMITATION OF ABSTRACT UU	18. NUMBER OF PAGES 17	19a. NAME OF RESPONSIBLE PERSON Gary Haas
a. REPORT Unclassified	b. ABSTRACT Unclassified	c. THIS PAGE Unclassified			19b. TELEPHONE NUMBER (Include area code) (410) 278-8867

Contents

List of Figures	iv
List of Tables	iv
1. Background	1
2. Determining Motor Controller Constants	1
2.1 Odometer	2
2.2 Speed Setting	3
2.3 Turning Radius	4
3. Modeling and Calibrating	5
4. Results	7
5. Conclusions and Further Work	8
References	9
Distribution List	10

List of Figures

Figure 1. In 2-dimensional plan view, wheel centers (“tire-points”) describe a circular path about the center C, at left. At right, a single wheel is depicted in plan view, with vector components of its velocity.	6
---	---

List of Tables

Table 1. Measurements used in calculating conversion factor from wheel rotational velocity in revolutions per minute to Roboteq arbitrary speed units.	3
Table 2. Examples of Roboteq controller response to combinations of channel 1 and channel 2 (linear and rotational velocity) setpoints. In the fourth example, the speed setting for the right wheel exceeds the maximum, so both settings are adjusted to maintain rotational velocity at the maximum possible translational velocity.	4

1. Background

The programmatic background and design of the research robot of this report is documented in (1). All work was performed at the Unmanned Vehicles Technology (UVT) Division of the U.S. Army Research Laboratory. The effort described herein followed as part of the tuning process, selecting parameters for the motor controller so that the robot performance can be specified in engineering units and executed faithfully by the robot. The objective is a transfer function between an instantaneous element of the desired path, specified as a pair of linear velocity and rotational velocity, and the corresponding command to the motor controller. The major components of this process are the specification of the kinematic model according to which the robot responds to inputs, and the selection of parameters peculiar to the motor controller board.

The kinematics of a 4-Skid-Steer vehicle have been addressed in any number of academic papers and theses (2–4). The various descriptions of the model in the literature omit a couple of elements essential to the UVT implementation, so these elements are derived herein. These elements and the general approach to validating the model may be of general interest to others attempting similar projects. The section addressing calibration of the motor controller is specific to that controller and serves to document the specific steps and specific values determined for the UVT robot. In this section, only the general approach is likely to be of use to others, except for those integrating the same controller.

2. Determining Motor Controller Constants

The Roboteq controller (5) is configured as a closed-loop servo system using pulse-width modulation to control two direct current (DC) motors equipped with digital encoders. Each motor drives two wheels mechanically coupled together, one motor for the left wheels and one for the right wheels. The controller receives commands from the (external) control computer over a serial data port. During calibration the external computer was a laptop computer running the Roborun utility provided with the controller. In the intended use, the external computer will be an embedded computer on the ATRV (1).

The UVT robot is configured in the Roboteq “A & B speed mixed” mode (5), which specifies translational velocity and rotational velocity separately, in arbitrary units. A complete command to the Roboteq controller is of the form {channel 1, channel 2}, where “channel 1” is the value of the commanded translational velocity and “channel 2” is the value of the commanded rotational velocity. Details of this coordinated control will be discussed later. The conversion from engineering units (meters/second and radians/second) to the arbitrary units of the controller takes

place in an external computer programmed by UVT personnel. Parameters of the Roboteq controller affect this conversion and must be determined first.

The parameters in question are the “timebase” used by the controller in measuring and controlling motor speed and a “divider” applied to the accumulated encoder count (effectively an odometry measure). The controller manual does not explicitly describe how these parameters are used, so the following discussion is based on a certain amount of reverse engineering.

It appears that the timebase value sets a timer which defines a window within which encoder counts are accumulated. The faster the motor turns, the larger is the value of the count, to the maximum of the counter’s capability. At the end of the window, the number of counts is compared to the speed setpoint and the pulse-width fed to the motors is adjusted to zero the error between setpoint and count. This is a conventional design for this type of controller, and the Roboteq controller is assumed to conform to this design.

The value selected for the timebase determines the range of speeds to which the controller can be set, in this case, $\{-127:128\}$. Empirically it was determined that when the timebase is set to a value of 6, the range of setpoints substantially spans the range of speeds which can be attained by the motor. At a timebase value of 5, the motor does not reach its maximum speed at the maximum setpoint, while at a timebase value of 7 the maximum motor speed is reached at a value less than the maximum setpoint.

The “divider” value serves as a gain to the value reported by the odometry counter. This value was set to 128, the largest value accepted by the Roborun software, resulting in the lowest possible resolution of odometry. This resolution was later determined to be more than sufficient, and the value selected does not appear to be critical to this application.

2.1 Odometer

The next step in the calibration is the calculation of conversion factors between engineering units and the arbitrary units of the controller. Empirically it was determined that the counters (one each left and right, corresponding to the rotational displacement of the respective wheel sets) changed by approximately 44000 units during a single rotation of a wheel. The measurement of a rotation was determined by marking a line on the tire corresponding to an alignment with a pointer, zeroing the counter, then rotating the tire 360° using the Roborun utility and noting the counter value at the end. Several measurements were made for each wheel set. Alignment was not precise due to the crude measurement of alignment, but measures were within 0.5% of the mean. From this we conclude that a counter reading of 44000 corresponds to one revolution of the tire. Given a tire of nominal diameter 12” (= .304 m), one encoder count corresponds to 0.000857” of linear travel. The calibration was validated by commanding a straight-ahead translation and measuring the realized translation with a tape measure. Though the actual data has been lost, results were very close.

2.2 Speed Setting

With a means of measuring rotational displacement known, wheel rotational velocity could be calculated. Using a stopwatch to measure time and the Roborun counter display to measure displacement of both left and right wheels, the following findings were made. Elements of this calibration are shown in table 1.

Table 1. Measurements used in calculating conversion factor from wheel rotational velocity in revolutions per minute to Roboteq arbitrary speed units.

Speed Setting	Displacement Left (counts)	Displacement Right (Counts)	Duration (s)	V (Wheel RPM)
5	141631	141052	50.44	3.83
127	2138332	2172213	30.43	96.58

Speed setting is for Roboteq channel 1 (translational velocity setpoint), while Roboteq channel 2 (rotational velocity setpoint) remains at 0. In the “A & B speed mixed” mode, this provides the same internal speed setpoint for each wheel set.

Measured wheel speed in revolutions per minute is calculated from the raw measurements of figure 1 as:

$$V = \frac{\text{Displacement} * \frac{\text{rev}}{44000 \text{ count}}}{\text{Duration} * \frac{\text{min}}{60 \text{ sec}}}$$

The Roboteq speed setpoint, in arbitrary units, is calculated from the desired robot linear speed V as follows:

$$\text{Setpoint} = \frac{V}{\pi * \text{tire_diameter}} * k \quad (1)$$

The constant k is calculated from the data of figure 1:

$$k = 5 / 3.83 \approx 127 / 96.58 \approx 1.3$$

An alternate formulation using input speed V in meters/second, which requires tire diameter in meters, is given as:

$$\begin{aligned} \text{Setpoint} &= \frac{V}{\pi * \text{tire_diameter}} * k * 60 \\ &= \frac{V}{\text{tire_diameter}} * k2 = \frac{V}{\text{tire_diameter}} * 24.8 \end{aligned}$$

(2)

$$k2 = 24.8$$

2.3 Turning Radius

Turning radius for a skid-steered robot of track ‘T’ (distance between left and right tires across the direction of travel) is governed by the difference in velocity of each side of the robot, divided by the track. The Roboteq controller in “A & B speed mixed” mode decreases the internal speed setpoint of one wheel set by the setting of channel 2, while increasing the speed of the other by the same amount. If, for instance, channel 1 is set to 0 and channel 2 is set to 20, the setpoint to the right wheel set is forward at speed 20 and the left wheel set turns in reverse at setpoint 20, resulting in a pirouette about the center of the robot. If channel 1 is set to 20 and channel 2 is set to 20, the left wheels are stationary and the right wheels turn at setpoint 40.

This leads to the possibility of the controller issuing a motor speed setpoint greater than the maximum (127 or -126), which cannot be. Empirically it was determined that if the maximum is exceeded for either left or right wheel set, the controller reduces the translational speed so that rotational velocity is preserved while altering the translational velocity as little as possible (e.g., the side-to-side difference in rotational speed is preserved with one wheel set at its maximum speed, the other wheel set adjusted to maintain the maximum possible translational speed.).

Table 2. Examples of Roboteq controller response to combinations of channel 1 and channel 2 (linear and rotational velocity) setpoints. In the fourth example, the speed setting for the right wheel exceeds the maximum, so both settings are adjusted to maintain rotational velocity at the maximum possible translational velocity.

Channel 1	Channel 2	Left Speed	Right Speed	Left Speed (adj)	Right Speed (adj)
0	20	-20	20		
20	20	0	40		
40	20	20	60		
96	50	46	146 !!!	27	127

Note that the channel 2 setting is related to linear wheel speed in engineering units by the same constant as calculated earlier for ground speed, e.g., [1] or [2].

3. Modeling and Calibrating

The kinematics of a four-wheel skid-steer vehicle have been addressed in any number of academic papers and theses. It is not uncommon to begin with a model based on a wheelchair-like differential drive robot (7). The model defines an instantaneous center of rotation (ICR) which lies on the extended line of the axle at a distance defined by the difference in velocity between the two wheels. This model is easy to understand because it obeys the assumptions usual for wheels, that is, that instantaneous motion can occur only perpendicular to the axle.

A four-wheel skid-steer vehicle, however, must violate this assumption whenever it turns. Because the wheels do not steer, they must slip or skid whenever the wheels on opposite sides turn at different rates. The tire-ground interface is difficult to model, it varies with the surface, and it plays a major role in the amount of slip and thus the rate of the turn. Several papers describing dynamic models are cited (2–4), along with calibration methods (6) and results for selected vehicles and surfaces. For the intended purpose of the UVT research vehicle, an elaborate model is not necessary. The vehicle of this report, when finished, will use Simultaneous Localization and Mapping (SLAM) to correct in closed-loop fashion for inaccuracies in the model. A simplified model relating commanded rotation and translation to realized rotation and translation within constrained conditions will suffice. To this end, analysis will proceed in the local coordinate system embedded in the robot, oblivious to any world coordinate system.

The constraint imposed is, slip at each wheel is equal so the center of rotation is at the geometric center C of the robot, at the intersection of the diagonals between the contact point of tires on opposite corners of the robot. Under these constraints, it is easy to separate the analysis of translation and rotation. Analysis of translation is trivial, so the discussion will focus on rotation of the robot about its geometric center. See figure 1.

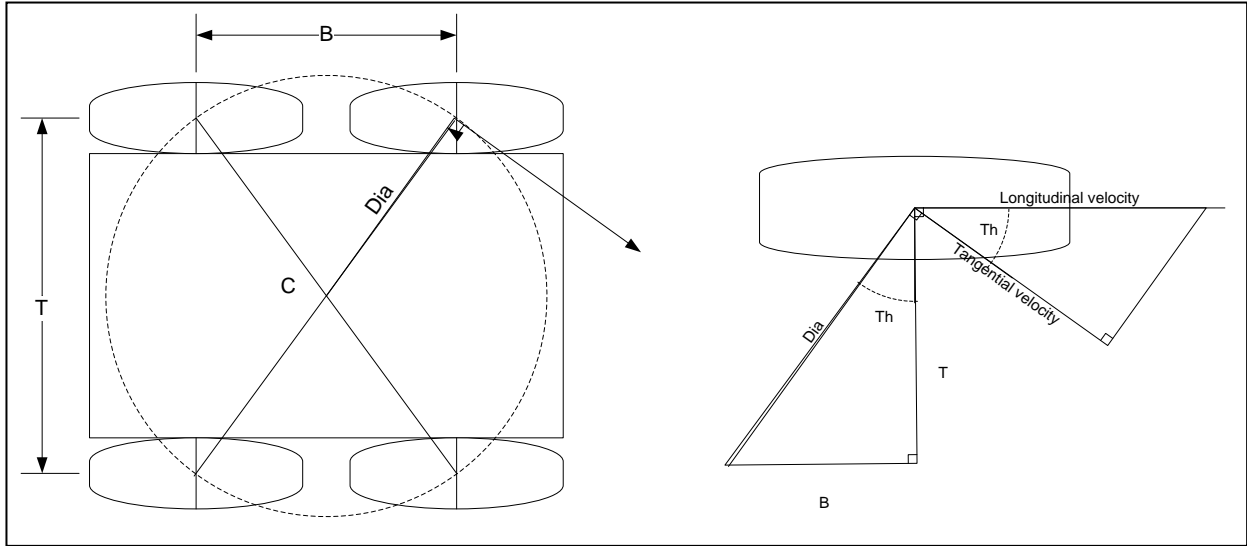


Figure 1. In 2-dimensional plan view, wheel centers (“tire-points”) describe a circular path about the center C, at left. At right, a single wheel is depicted in plan view, with vector components of its velocity.

At this point, it is convenient to represent the vehicle in 2-dimensional plan view. Each tire is represented by a point at the center of its contact patch, a tire-point. The diameter of rotation, labeled Dia in figure 1, is the resultant of the wheelbase B and the track T. The tangential velocity (VT) of each tire-point about the center C is the component of tire longitudinal velocity (VL) which is tangent to its path about the center. This can be formulated as:

$$VT = VL * \cos(Th) = VL * T / Dia$$

And the length of the diameter $Dia = \sqrt{T^2 + B^2}$

The angle Th between the longitudinal velocity and tangential velocity is useful in visualizing the similar triangles, but the direct representation of the inverse cosine, e.g., T / Dia , is more useful and will be used hence.

Rotation velocity of the tire-point about C in radians, denoted (VTr), is:

$$VTr = \frac{VT}{Dia/2} = 2 * VL * \frac{T}{T^2 + B^2}$$

At this point, the 3-dimensional tire is re-introduced.

From (2),

$$VTr = 2 * \left(\text{Setpoint2} * \frac{\text{tire_diameter}}{k2} \right) * \frac{T}{T^2 + B^2}$$

So the channel 2 setpoint for a desired rotational velocity VTr is:

$$\text{Setpoint2} = V_{\text{Tr}} * \frac{k2 * (T^2 + B^2)}{2 * T * \text{tire_diameter}}$$

For the UVT robot, track and tire diameter in meters, and input rotational velocity V_{Tr} in radian/second, the computing formula is

$$\text{Setpoint2} = V_{\text{Tr}} * 32.5$$

4. Results

Verification

Software was written to convert translational and rotational velocities in engineering units to arbitrary units according to the formulation described above, and to feed them to the Roboteq motor controller. A 5 m² test grid was laid out on the smooth concrete floor with masking tape at 1 meter intervals. Test trajectories of constant radius were defined as triples consisting of {time, velocity, rotational velocity} so that the robot would describe a circle, half-circle, or quarter-circle, beginning from a grid intersection and ending on a grid intersection, within the confines of the test grid. The expected radius of the circle and endpoint were computed from the following trajectories:

$$\text{Radius} = \text{velocity} / \text{rotational_velocity} = \{ 1, 2 \text{ m} \}$$

$$\text{Endpoint} = (\text{rotational_velocity} * \text{time}) = \{ \pi/2, \pi, 2 * \pi \}$$

These trajectories were implemented using combinations of the following parameters:

$$\text{Translational velocity} = \{ 0.1, 0.15, 0.2, 0.3 \text{ m/s} \}$$

$$\text{Rotational velocity} = \{ 0.1, 0.15, 0.2, 0.3 \text{ rad/s} \}, \text{ both clockwise and counter-clockwise}$$

$$\text{Duration} = \{ 15, 31, 63 \text{ s} \}$$

Deviation from the expected trajectory was measured as variation from the expected grid-crossing values at multiples of $\pi/2$. The measures were by means of measuring tape. Although crude, they were repeatable to the (admittedly low) standards of the test. They were sufficient to ascertain that, once the model was correct, the error was on the order of 2% of distance traveled along the path and less across the path. Angular error proved difficult to measure, but consistent success in approximating the starting point on full-circle trajectories indicates a tolerable error.

5. Conclusions and Further Work

Calibration of the UVT robot low-level controller was intended to assure coarse but sufficient accuracy in following a simple path. The path itself is to be prescribed by a path planner at a higher-level, enhanced by SLAM-based, closed-loop control. The successful execution of semi-circular and circular paths demonstrate that a simple model and correct calibration can provide control as intended, within a limited range of surfaces and velocities. With assurance of adequate accuracy from the lower-level control elements, research can progress in implementing higher-level control and autonomous behaviors built on a foundation of correct mobility.

References

1. Haas, Gary; Owens, Jason; Spangler, Jim. *A Platform for Developing Autonomy Technologies for Small Military Robots*; ARL-MR-709; U.S. Army Research Laboratory: Aberdeen Proving Ground, MD, December 2008. (UNCLASSIFIED)
2. Kozłowski, Krzysztof; Pazderski, Dariusz. Modeling and Control of a 4-Wheel Skid-steering Mobile Robot, *Int. J. Appl. Comput. Sci.* 2004; 14 (4) pp 477–496.
3. Anousaki, Georgia; Kyriakopoulos, K. J. A Dead-Reckoning Scheme for Skid-Steered vehicles in Outdoor Environments, Published by IEEE, Los Alamitos, CA. *Proceedings of the 2004 IEEE International Conference on Robotics and Automation*, New Orleans, LA, April 2004.
4. Mandow, Anthony; Martinez, Jorge L.; Morales, Jesus; Blanco, Jose; Garcia-Cerezo, Alfonso; Gonzalez, Javier. Experimental kinematics for wheeled skid-steer mobile robots, *Intelligent Robots and Systems, 2007. IROS 2007. IEEE/RSJ International Conference*, San Diego, CA, October 29 2007–November 2 2007.
5. Roboteq AX3500 Dual Channel High Power Digital Motor Controller User's Manual, v 1.9b, Roboteq, Inc.: Scottsdale, AZ, 1 June 2007.
http://roboteq.com/files_n_images/files/manuals/ax3500man19b-060107.pdf (accessed 18 September 2007)
6. Borenstein, Johann; Feng, Liqiang. UMBmark: A Benchmark Test for Measuring Odometry Errors in Mobile Robots, *SPIE Conference on Mobile Robots*, Philadelphia, PA, October 22–26, 1995.
7. Dudek, Gregory; Jenkin, Michael. *Computational Principles of Mobile Robotics*, Cambridge University Press, Cambridge, UK: 2000; pp. 18-22.

ADMNSTR
DEFNS TECHL INFO CTR
ATTN DTIC OCP (ELECTRONIC COPY)
8725 JOHN J KINGMAN RD STE 0944
FT BELVOIR VA 22060-6218

DARPA
ATTN IXO S WELBY
3701 N FAIRFAX DR
ARLINGTON VA 22203-1714

OFC OF THE SECY OF DEFNS
ATTN ODDRE (R&AT) (1 CD)
THE PENTAGON
WASHINGTON DC 20301-3080

US ARMY INFO SYS ENGRG CMND
ATTN AMSEL IE TD A RIVERA
FT HUACHUCA AZ 85613-5300

COMMANDER
US ARMY RDECOM
ATTN AMSRD AMR W C MCCORKLE
5400 FOWLER RD
REDSTONE ARSENAL AL 35898-5000

US ARMY RSRCH LAB
ATTN RDRL CIM G T LANDFRIED
BLDG 4600
ABERDEEN PROVING GROUND MD 21005-5066

US ARMY RSRCH LAB
ATTN RDRL VTU F G HAAS (1 CD, 6 HCs)
ABERDEEN PROVING GROUND MD 21005-5067

US ARMY RSRCH LAB
ATTN IMNE ALC HRR MAIL & RECORDS MGMT
ATTN RDRL CIM L TECHL LIB
ATTN RDRL CIM P TECHL PUB
ADELPHI MD 20783-1197

