REPORT DOCUME	Form Approved OMB No. 0704-0188								
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1. REPORT DATE (DD-MM-YYYY) 2. REI MAY 2013 1000000000000000000000000000000000000	PORT TYPE CONFERENCE	PAPER (Postpr	rint)	3. DATES COVERED (From - To) JAN 2012 – APR 2013					
4. TITLE AND SUBTITLE			5a. CONTRACT NUMBER IN-HOUSE						
RANK DEFICIENT DECODING OF LIN	EAR NETWORK	CODING	5b. GRANT NUMBER N/A						
	5c. PROGRAM ELEMENT NUMBER 62788F								
6. AUTHOR(S)	5d. PROJECT NUMBER T2AW								
Bruce Suter (AFRL)	5e. TASK NUMBER IN								
	5f. WOR	if. work unit number HO							
7. PERFORMING ORGANIZATION NAME(S) AN PRIME Air Force Research Laboratory/ Information Directorate Rome Research Site/RITB	B ighigh Universit 41 Southwood ston, PA 18045	y Dr	8. PERFORMING ORGANIZATION REPORT NUMBER N/A						
525 Brooks Road Rome NY 13441-4505									
9. SPONSORING/MONITORING AGENCY NAM Air Force Research Laboratory/Information Rome Research Site/RITB		10. SPONSOR/MONITOR'S ACRONYM(S) AFRL/RI							
525 Brooks Road Rome NY 13441-4505		11. SPONSORING/MONITORING AGENCY REPORT NUMBER AFRL-RI-RS-TP-2013-039							
12. DISTRIBUTION AVAILABILITY STATEMENT APPROVED FOR PUBLIC RELEASE; I DATE CLEARED: 26 NOV 2012	T DISTRIBUTION U	JNLIMITED. P	A Case N	lumber: 88ABW-2012-6128					
13. SUPPLEMENTARY NOTES © 2012 IEEE. Proceedings IEEE International Conference on Acoustics, Speech, and Signal Processing (ICASSP, Vancouver, Canada; 26-31, May 2013. One or more of the authors is a U.S. Government employee working within the scope of their Government job; therefore, the U.S. Government is joint owner of the work and has the right to copy, distribute, and use the work. All other rights are reserved by the copyright owner									
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15. SUBJECT TERMS Network Coding; Compressive Sensing; Rank Deficient Decoders									
16. SECURITY CLASSIFICATION OF:	17. LIMITATION OF ABSTRACT	18. NUMBER OF PAGES	19a. NAME (MICH	AME OF RESPONSIBLE PERSON 11CHAEL LITTLE					
a. REPORT b. ABSTRACT c. THIS PAGE U U U U	UU	6	19b. TELEPI N/A	ab. TELEPHONE NUMBER (<i>Include area code)</i> N∕A					

Standard Form 298 (Rev. 8-98) Prescribed by ANSI Std. Z39.18

Rank Deficient Decoding of Linear Network Coding

Zhiyuan Yan, Hongmei Xie, and Bruce W. Suter

Abstract-Network coding is a new paradigm of communication networks that promises advantages in throughput, robustness, and complexity. Since the fundamental premise of linear network coding is that transmitted data packets are subject to linear combinations, for all network coding schemes so far, a full rank of received packets is required to invert the linear mapping so as to recover the transmitted data packets. This requirement unfortunately results in a key drawback of network coding: either all the packets (or bits) in a session are recovered simultaneously or none can be recovered. Aiming to overcome this all-or-nothing property, which leads to long delays and low throughputs, in this work we propose a variety of rank deficient decoders of linear network coding. To this end, we first reformulate the decoding problem of linear network coding as a collection of underdetermined systems. This reformulation reveals the connection among the decoding problems of network coding and error control coding, and enables rank deficient decoding. We then propose two classes of rank deficient decoders. The first class of decoders take advantage of the sparsity inherent in data and produce the data vectors with the smallest Hamming weight, and hence they are called Hamming norm decoders. Since these decoders have high complexities, we propose a class of decoders based on linear programming, referred to as linear programming decoders. Considering linear programming relaxation of the Hamming norm decoders and solving them by using standard linear programming procedures, the linear programming decoders have polynomial complexities and are much more affordable. Both classes of decoders recover data from fewer received packets and hence achieve higher throughputs and shorter delays than the full rank decoder.

I. INTRODUCTION

Communication networks (CNs) are ubiquitous in our everyday life as well as our national infrastructure. Network coding [1] has the potential to fundamentally transform current and future CNs due to its promise of significant throughput gains. Furthermore, network coding has other advantages such as robustness and can be implemented in a distributed manner with random linear network coding (RLNC) [2]. Hence, network coding is already used or considered for a wide variety of wired and wireless networks.

Although network coding does not suffer from the couponcollector problem, one significant drawback of network coding is its all-or-nothing property in more than one sense. First, a full rank of received packets at the receiver nodes of a multicast (or a unicast) is needed before decoding can start, leading to long delays and low throughputs, especially when the number of packets of a session is large. This is particularly undesirable for military or civil applications with stringent delay requirements. Second, all the bits in any packet are equal in the sense that they are recovered simultaneously.

Aiming to solve this problem, we propose rank deficient decoding for linear network coding, which can start even when the rank of the received packets is smaller than the threshold. By reformulating the decoding problem of network coding in a different fashion, the decoding problem reduces to a collection of syndrome decoding problems, where the code is defined by the global kernel matrix and its minimum distance is upper-bounded by the rank of the received packets. Solving these syndrome decoding problems, rank deficient decoding leads to smaller delays and higher throughput, at the expense of possible decoding errors. Specifically, we propose two classes of rank deficient decoders. The first class of decoders take advantage of the sparsity inherent in data and produce the data vectors with the smallest Hamming weight, and hence they are called Hamming norm decoders. Since these decoders have high complexities for large size systems, we propose a class of decoders based on linear programming, referred to as linear programming decoders. Considering linear programming relaxation of the Hamming norm decoders and solving them by using standard linear programming procedures, the linear programming decoders have polynomial complexities and are much more affordable. Both classes of decoders recover data from fewer received packets and hence achieve higher throughputs and shorter delays than the full rank decoder. Since these decoders could produce erroneous outputs, within each class several different decoding strategy have been proposed for different tradeoffs between delays/throughput and data accuracy, and they include the traditional decoder of network coding as a special case.

In the literature, there are two different approaches to deal with the synergy of network coding and compressive sensing, and they also aim for different applications. One approach was proposed in [3], statistical property of data blocks are taken advantage of to alleviate the "all-or-nothing" drawback of network coding in distributed storage systems. In this approach, random linear network coding is carried out over some finite fields, and the data are represented by bits. The other approach [4], [5] aims to take advantage of the statistical correlation of data generated by distributed sensor networks. A salient feature of this approach is that in theory data are real values and linear combinations are now performed over the real (or complex) field. The rationale for this is that the real representation of data is a more natural one for sensor networks [4], [5]. In practice, data are represented in a finite precision system. It has been shown that information loss due to finite precision grows with the network size [6].

Our work is quite different from both existing approaches. Above all, our reformulation of the decoding problem in network coding is novel, and this reformulation was not considered in the open literature to the best of our knowledge. Furthermore, the approach in [3] focuses on the application of random linear network coding in distributed storage systems. In contrast, we consider linear network coding in general, and our work applies to a wide variety of applications. Also, network coding is carried out over the real (or complex) field in the approach in [4], [5], whereas in our work network coding remains over some finite fields. Thus, our scheme does not suffer the information loss due to finite precision as the approach in [4], [5].

II. RANK DEFICIENT DECODING

A. System Model

In this work, we make several assumptions about the underlying network coding. First, we treat all packets as N-dimensional row vectors over some finite field GF(q), where q is a prime power. For simplicity, as most network coding schemes in practice, we assume that GF(q) is a finite field of characteristic two, because information (in bits) can be easily mapped to finite field symbols. Second, we focus on linear network coding (LNC) [7] only, which was shown to be optimal in most cases. Thirdly, we assume that the network is error-free, and error control (see, for example, [8]–[11]) is not embedded in network coding.

Suppose a source node of a unicast or multicast injects a collection of n data packets (or vectors over GF(q)), X_0, X_1, \dots, X_{n-1} , into the network. At any sink node, m packets (or vectors over GF(q)), Y_0, Y_1, \dots, Y_{m-1} , are received, where $Y_i = \sum_{j=0}^{n-1} a_{i,j} X_j$ for $i = 0, 1, \dots, m-1$ and $a_{i,j} \in GF(q)$. In other words, each received packet is a linear combination of the injected packets. Since the sink node can locally generate more linear combinations of Y_0, Y_1, \dots, Y_{m-1} , it is assumed that Y_0, Y_1, \dots, Y_{m-1} are linearly independent, which implies that $m \leq n$. That is, the $m \times n$ matrix $A = [a_{i,j}]$, often called the global coding kernel matrix, has a rank of m.

B. Full Rank Decoding

Let us further denote the matrices $\begin{bmatrix} X_0^T X_1^T \cdots X_{n-1}^T \end{bmatrix}^T$ and $\begin{bmatrix} Y_0^T Y_1^T \cdots Y_{m-1}^T \end{bmatrix}^T$ as X and Y, respectively, and they are related by Y = AX. The sink node can recover the transmitted data packets by reversing the encoding of the data packets by the network. This is easily achievable when m = n, as the sink node can recover the data packets by computing $X = A^{-1}Y$. Thus, the decoding in network coding starts only after the sink node has received an enough number of linearly independent combinations of the transmitted data packets. That is, either all data packets are recovered simultaneously, or none is recovered. This is often referred to as the "all-ornothing" property by network coding. Note that this is different from the coupon collector problem suffered by communication networks without network coding. Nevertheless, the required number of linearly independent packets received by the sink node leads to longer delays and lower throughputs, which may be undesirable for some applications. Furthermore, in this setting, the "all-or-nothing" property also holds on the bit level. That is, all bits of all packets are equal in the sense that, either all of them are recovered simultaneous or none of them can be recovered.

C. Rank Deficient Decoding

We can formulate the data recovery problem at the sink node in a different way. Let us consider coordinate l of Y_i , and we have $Y_{i,l} = \sum_{j=0}^{n-1} a_{i,j}X_{j,l}$ for $i = 0, 1, \dots, m-1$ and $l = 0, 1, \dots, N-1$. Let us denote the column vectors $(Y_{0,l}Y_{1,l} \cdots Y_{m-1,l})^T$ and $(X_{0,l}X_{1,l} \cdots X_{n-1,l})^T$ as Z_l and W_l , respectively. Clearly, we have $Z_l = AW_l$ for $l = 0, 1, \dots, N-1$. The sink node can recover the data packets if it can obtain W_l from

$$Z_l = AW_l \text{ for } l = 0, 1, \cdots, N-1.$$
 (1)

Eq. (1) shows that the data recovery problem at the sink node can be viewed as N parallel decoding problems in Eq. (1), and each corresponds to one coordinate in the packet (or vector). When these N parallel decoding problems are solved at the same time, it is essentially equivalent to the traditional decoding problem of network coding.

This reformulated problem is related to two well known decoding problems. First, if we treat the $m \times n$ matrix A as a parity check matrix for a linear block code of length n and dimension n - m, the decoding problem in Eq. (1) is closely related to a syndrome decoding problem. That is, the sink node needs to recover W_l based on the syndrome Z_l . Second, if we treat W_l as a data vector and A a measurement matrix, this is analogous to the decoding problem in compressive sensing.

D. Decoding Strategy

Once a full rank of received packets are available, the fullrank decoder recovers all data packets correctly. In contrast, the proposed rank deficient decoders may produce wrong decisions. Analogous to classical error control coding, the preference between decoding failures and decoding errors varies from one application to another. For instance, for military applications with stringent delay constraints, partially correct data packets may be more desirable than decoding failures. For other applications such as cloud storage, data integrity may be a top priority than delays, especially packet retransmission is possible. Hence, it is necessary to consider a wide range of decoding strategy so as to offer different tradeoffs between delays/throughputs and accuracy.

Two extreme strategy are natural and straightforward. One extreme, called the error-free decoder, is similar to the full-rank decoder in the sense that it decodes only if decoding success is guaranteed. This can be implemented based on Lemma 1: decode only if W_l in Eq. (1) satisfies $w_H(W_l) < \frac{d_H(A)}{2}$ for all *l*'s. The other extreme, referred to as the best-effort decoder, always tries to decode with available received packets. The error-free and best-effort decoders represent the most conservative and the most aggressive strategy.

We also devise a family of decoding strategy that fill the gap between these two extremes. These decoding strategy are based on one observation about error control codes. For an (n,k) perfect code over GF(2), we have $\sum_{i=0}^{t} \binom{n}{i} = 2^{n-k}$, where $t = \lfloor \frac{d_H(A)-1}{2} \rfloor$. In other words, all the coset leaders are unique and have Hamming weight up to t. However, since

most codes are not perfect and some allowance needs to be made. Hence, we devise a greedy-l decoding strategy: decodes only if $\sum_{i=0}^{cw-l} \binom{n}{i} = 2^{n-k}$. The parameter l represents how aggressive the decoder is: for the same code defined by A, the greater l is, the more aggressive the decoder is. In fact, one can use different l values to approach the two extremes, the best-effort and error-free decoders.

E. Hamming Norm Decoders

Let us further consider the problem in Eq. (1). Since the data recovery problem at any sink node is equivalent to a collection of parallel problems in Eq. (1), we focus on one such problem. In other words, we try to solve Z = AW for W, where Zand W are m- and n-dimensional column vectors, respectively, and A remains an $m \times n$ matrix with full rank. Without loss of generality, we assume that m < n.

For a linear block code of length n and dimension n - m with a parity check matrix A, Z = AW can be viewed as a syndrome of the received vector W. It is well known that for a linear block code, the syndromes have a one-toone correspondence with its cosets, each of which is of size q^{n-m} . In other words, all vectors in a coset lead to the same syndrome. Thus, solving Z = AW for W is equivalent to finding a vector within a coset.

If no side information is available, we can make a decision within the coset by taking advantage of some inherent properties of the data vector. In this work, we proceed by relying on the sparsity of the data vector, which is well justified in many applications. That is, the proposed rank deficient decoders produce the vector with the smallest Hamming weight in the coset. Hence, we refer to them as Hamming norm decoders.

As is common in compressive sensing literature, we consider two possible scenarios for sparsity. First, when W is sparse, we use a vector with the smallest Hamming weight in the coset corresponding to Z as the estimate of W. Second, suppose that ΦW is sparse for a known nonsingular $n \times n$ matrix Φ . Since $Z = AW = A\Phi^{-1}\Phi W$, we can treat Z as a syndrome for the linear block code defined by $A\Phi^{-1}$. Thus, in this scenario, we first select a vector with the smallest Hamming weight in the coset corresponding to Z, and then produces an estimate of W by multiplying the selected vector with the smallest Hamming weight in the coset corresponding to the given syndrome. Thus, we assume W is sparse without loss of generality.

In coding theory terminology, a vector with the smallest Hamming weight among a coset is called a leader of the coset. Note that some coset leaders may not be unique, when more than one vector in the coset has the smallest Hamming weight. In this case, either the coset leader is selected among these vectors at random or a list of all potential leaders.

We remark that this problem is closely related to but different from the syndrome decoding problem in classic coding theory. In our decoding, a vector or a list of vectors with the smallest Hamming weight in the coset corresponding to the given syndrome is considered as the estimate of the data vector. In the syndrome decoding problem, a coset leader is often considered as an estimate of the error vector. However, the key step in both problems is to select a vector or a list of vectors with the smallest Hamming weight in the coset corresponding to the given syndrome. For this reason, we refer to our decoding problem the modified syndrome decoding problem.

Thus, we have the following sufficient condition for successful decoding:

Lemma 1. The minimum Hamming distance of the linear block code defined by A, denoted by $d_H(A)$, satisfies $d_H(A) \le m+1$. When the Hamming weight of W, denoted by $w_H(W)$, is less than half of the minimum Hamming distance of the linear block code defined by A, that is $w_H(W) < \frac{d_H(A)}{2}$, W can be recovered by syndrome decoding.

Proof: The first part is due to the Singleton bound on the minimum Hamming distance of linear block codes. The second part holds because it is well known that a coset leader with Hamming weight less than $\frac{d_H(A)}{2}$ is unique.

When W is not a unique coset leader, there are two possibilities. First, when the Hamming weight of W is minimal in its coset, either W has a probability to be selected when coset leaders are chosen at random or W is one of the possible vectors produced by the decoder, depending on whether the decoder needs to generate only one vector or a list of vectors. Second, when the Hamming weight of W is not minimal, a wrong vector will be produced by the modified syndrome decoder.

F. Linear Programming Decoders

Since both the computational complexity and the memory requirement of the Hamming norm decoders grow exponentially with the size of A, we also adopt a linear programming (LP) approach. Since A is not necessarily sparse, we formulate the problem based on that for binary linear block code with high-dense polytopes in [12].

An $m \times n$ parity-check matrix A can be represented by a Tanner graph G, a bipartite graph with a set of variable nodes $\mathcal{I} = \{1, 2, ..., n\}$ and a set of check nodes $\mathcal{J} = \{1, 2, ..., m\}$. A node $i \in \mathcal{I}$ is adjacent to a node $j \in \mathcal{J}$ if the element $A_{i,j}$ is nonzero. N(j) is the set of variable nodes that are adjacent to a check node j, and N(i) is the set of check nodes adjacent to a variable node i.

Let f_1, f_2, \ldots, f_n be the variables representing the code bits of **w**, and **s** = $(s_1, s_2, \ldots, s_m)^T$ be the syndrome received. For each check node $j \in \mathcal{J}$, let $T_j^E = \{0, 2, 4, \ldots, 2\lfloor |N(j)|/2 \rfloor\}$ for $s_j = 0$, and $T_j^O =$ $\{1, 3, 5, \ldots, 2\lfloor (|N(j)| - 1)/2 \rfloor + 1\}$ for $s_j = 1$. Then for each $j \in \mathcal{J}$ and $k \in T_j^E$ (T_j^O), define a variable $\alpha_{j,k}$. For all $j \in \mathcal{J}, k \in T_j^E$ (T_j^O) and $i \in N(j)$, define $z_{i,j,k}$. Then the linear programming formulation for the syndrome decoding is to minimize $\sum_{i=1}^n f_i$, subject to the following constraints:

$$\forall i \in \mathcal{I}, j \in N(i), \qquad f_i = \sum_{k \in T_j} z_{i,j,k}$$



Fig. 1. Standard array vs LNC decoding: packets level

$$\begin{split} \forall j \in \mathcal{J}, & \sum_{k \in T_j} \alpha_{j,k} = 1 \\ \forall j \in \mathcal{J}, k \in T_j, & \sum_{i \in N(j)} z_{i,j,k} = k \alpha_{j,k} \\ \forall i \in \mathcal{I}, & 0 \leq f_i \leq 1 \\ \forall j \in \mathcal{J}, k \in T_j, & 0 \leq \alpha_{j,k} \leq 1 \\ \forall i \in \mathcal{I}, j \in N(i), k \in T_j, & 0 \leq z_{i,j,k} \leq \alpha_{j,k} \end{split}$$

The above constraints are similar to those in [12], except that $T_j = T_j^E$ in the previous constraints if $s_j = 0$, and $T_j = T_j^O$ if $s_j = 1$. In addition, the following constraint is added to narrow down the optimal solutions:

$$\sum_{i=1}^{n} f_i \ge cu$$

Linear programming may produce non-integral results, in which case two approaches are considered. The first type is simply to round off the real numbers into integers, which are compared with the original data to count decoding error or success rate, and we mark this approach LP I. The other one is to declare declare decoding failure of the entire generation, as the decoding is performed column wisely, and each packet in the same generation will be affected. Both LP I and LP II are applicable to all greedy as well as the EF and BE strategies.

III. SIMULATION RESULTS

In our simulations, n = 8 transmitted packets of length N = 8 are generated such that the transmission matrix has a constant column weight of cw = 2. Note that such small parameters are chose so that the complexities of Hamming norm decoders are manageable. The matrix A is generated randomly, with each element being 0 or 1 with equal probability. The number of received packets m varies from 1 to 15, while the packets may not be linearly independent. Simulation results are obtained based on 100,000 generations of packets injected into the network.



Fig. 2. Standard array vs LNC decoding: bits level



Fig. 3. Linear programming vs LNC decoding: packets level

Fig. 1 and Fig. 2 show the packet level and bit level performance of different decoding algorithms, where the syndrome decoding adopts the standard array decoding algorithm. Both the PSR and BSR approach 1 following increased number of received packets for the syndrome decoding and the LNC decoding. But LNC performs no decoding when the number of received packets m is smaller than the number of transmitted packets n. Further, when $m \ge n$, the syndrome decoding algorithm achieves much better results than the traditional LNC for both the packet and bit levels performance.

Simulation results obtained from the linear programming decoding algorithm for the syndrome decoding are shown in Fig. 3 and Fig. 4. As expected, the linear programming approach performs slightly worse compared to the standard array decoding algorithm. However, the performance difference vanishes when the number of received packets is larger enough.

To measure the throughputs of these decoders, the average numbers of packets required to reach a packet success rate (PSR) of 1 or a bit success rate (BSR) of 0.95 are compared in Table I. The BE strategy requires approximately 2 less packets than the FR strategy to ensure all the packets are decoded correctly, for both the SA and the LP decoding algorithms.

TABLE	
AVERAGE NUMBER OF PACKETS FOR	R 100% PSR AND 95% BSR

Strategy F	FR	FR EF	greedy-(-1)		greedy-0		greedy-1			BE				
			SA	LP I	LP II	SA	LP I	LP II	SA	LP I	LP II	SA	LP I	LP II
100% PSR	9.60	8.84	8.12	8.12	8.12	7.57	7.78	7.77	7.44	7.73	7.72	7.44	7.73	7.72
95% BSR	9.60	8.84	8.05	8.05	8.05	7.40	7.50	7.63	7.17	7.37	7.54	7.17	7.37	7.54



Fig. 4. Linear programming vs LNC decoding: bits level

Note that the numbers are the same as the 100% PSR case for both the FR and the EF strategies. However, for the other four strategies, the number of packets required for a 95% BSR is smaller than that for a 100% PSR. For the last three strategies, the LP I algorithm requires about 0.2 to 0.3 more packets compared to the SA decoding algorithm in order to decode all the packets correctly. The corresponding increase for a 95% BSR is about 0.1 to 0.2. For the LP II algorithm, both the PSR and the BSR decrease as the failure rates are slightly higher. As a result, 0.1 to 0.2 more packets are required to to reach a 95% BSR for the last three strategies, while the average numbers for a a 100% PSR remain the same for both algorithms.

IV. CONCLUSIONS

We have proposed a variety of rank deficient decoders of linear network coding. Compared with the full rank decoder universally used in linear network coding, our proposed decoders require fewer received packets to decoder and hence achieve higher throughputs and shorter delays.

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