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ALGORITHMS FOR LEARNING AND DECISION MAKING

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MASSACHUSETTS INSTITUTE OF

12/09/2013

Final Report

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Final Report, GRANT NO FA9550-10-1-0412

ALGORITHMS FOR LEARNING AND DECISION MAKING

PI: Prof. Dimitri P. Bertsekas, Massachusetts Institute of Technology

We have investigated learning algorithms for inference and decision making, by using exact and approximate optimization methods. Most of our research has been in approximate dynamic programming/reinforcement learning methods, with a focus on Markovian Decision Problems with a very large number of states. Much of our work is related to a fundamental algorithm, Q-learning, and related new methods that relate to exact and approximate policy iteration. In particular, we have investigated, convergence issues, error bounds, policy oscillation, exploration-enhanced methods, and issues of decision making in a multi-agent environment.

Another research area is large-scale convex optimization methods, with a focus on problems whose cost function involves a sum of a large number of component functions. This includes a unifying framework for polyhedral approximation recently proposed by the principal investigator, incremental gradient and subgradient methods, which are currently at the forefront of algorithmic machine learning research, as well as a new incremental version of the proximal minimization algorithm. We have developed new polyhedral approximation algorithms, including a simplicial decomposition method that applies to large-scale conic programming problems.

Complete List of Publications Supported in Part by this Grant:

D. P. Bertsekas, "Approximate Policy Iteration: A Survey and Some New Methods," Lab. for Information and Decision Systems Report LIDS-P-2833, MIT, April 2010; Journal of Control Theory and Applications, Vol. 9, pp. 310-335.

D. P. Bertsekas, "Centralized and Distributed Newton Methods for Network Optimization and Extensions," Lab. for Information and Decision Systems Report LIDS-P-2866, MIT, April 2011.

D. P. Bertsekas and H. Yu, "Distributed Asynchronous Policy Iteration in Dynamic Programming," Proc. of 2010 Allerton Conference on Communication, Control, and Computing, Allerton Park, ILL, Sept. 2010.

D. P. Bertsekas and H. Yu, "Q-Learning and Enhanced Policy Iteration in Discounted Dynamic Programming," Lab. for Information and Decision Systems Report LIDS-P-2831, MIT, April, 2010; Math. of Operations Research, Vol. 37, 2012, pp. 66-94.

D. P. Bertsekas and H. Yu, "A Unifying Polyhedral Approximation Framework for Convex Optimization," SIAM J. on Optimization, Vol. 21, 2011, pp. 333-360.

D. P. Bertsekas, "Incremental Proximal Methods for Large Scale Convex Optimization," Lab. for Information and Decision Systems Report LIDS-P-2847, MIT, August 2010; Mathematical Programming, Vol. 129, 2011, pp.163-195.

H. Yu and D. P. Bertsekas, "On Boundedness of Q-Learning Iterates for Stochastic Shortest Path

Problems," Lab. for Information and Decision Systems Report LIDS-P-2859, MIT, March 2011; Mathematics of Operations Research 38(2), pp. 209-227, 2013.

H. Yu and D. P. Bertsekas, "A Mixed Value and Policy Iteration Method for Stochastic Control with Universally Measurable Policies," Lab. for Information and Decision Systems Report LIDS-P-2905, MIT, July 2013.

H. Yu and D. P. Bertsekas, "Weighted Bellman Equations and their Applications in Dynamic Programming," Lab. for Information and Decision Systems Report LIDS-P-2876, MIT, October 2012.

D. P. Bertsekas, "Weighted Sup-Norm Contractions in Dynamic Programming: A Review and Some New Applications", Lab. for Information and Decision Systems Report LIDS-P-2884, MIT, May 2012.

M. Wang and D. P. Bertsekas, "Stabilization of Stochastic Iterative Methods for Singular and Nearly Singular Linear Systems", Lab. for Information and Decision Systems Report LIDS-P-2878, MIT, December 2011 (revised March 2012); to appear in Mathematics of Operations Research.

M. Wang and D. P. Bertsekas, "Convergence of Iterative Simulation-Based Methods for Singular Linear Systems", Lab. for Information and Decision Systems Report LIDS-P-2879, MIT, December 2011 (revised April 2012); to appear in Stochastic Systems.

M. Wang and D. P. Bertsekas, "Incremental Constraint Projection-Proximal Methods for Nonsmooth Convex Optimization ", Lab. for Information and Decision Systems Report LIDS-P-2907, MIT, July 2013.

M. Wang and D. P. Bertsekas, "Incremental Constraint Projection Methods for Variational Inequalities", Lab. for Information and Decision Systems Report LIDS-P-2898, MIT, December 2012.

D. P. Bertsekas, "Lambda-Policy Iteration: A Review and a New Implementation", Lab. for Information and Decision Systems Report LIDS-P-2874, MIT, October 2011. To appear in "Reinforcement Learning and Approximate Dynamic Programming for Feedback Control," by F. Lewis and D. Liu (eds.), IEEE Press Computational Intelligence Series.

D. P. Bertsekas and H. Yu, "Stochastic Shortest Path Problems Under Weak Conditions," Lab. for Information and Decision Systems Report LIDS-P-2909, MIT, August 2013.

H. Yu and D. P. Bertsekas, "A Mixed Value and Policy Iteration Method for Stochastic Control with Universally Measurable Policies," Lab. for Information and Decision Systems Report LIDS-P-2905, MIT, July 2013.