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Exact chiral spin liquid with stable spin Fermi surface on the kagome lattice

ABSTRACT

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Exact chiral spin liquid with stable spin Fermi surface on the kagome lattice

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We study an exactly solvable quantum spin model of Kitaev type on the kagome lattice. We find a rich phase diagram which includes a topological (gapped) chiral spin liquid with gapless chiral edge states, and a gapless chiral spin liquid phase with a spin Fermi surface. The ground state of the current model contains an odd number of electrons per unit cell, which qualitatively distinguishes it from previously studied exactly solvable models with a spin Fermi surface. Moreover, we show that the spin Fermi surface is *stable* against weak perturbations.

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Introduction. The search for exotic ground states of quantum many-body systems has been at the fore in experimental and theoretical research for a number of decades, yet nature continues to tantalize us with ever more interesting behaviors. In recent years, systems with some type of topological order beyond Landau's broken symmetry principle,^{1,2} such as the fractional quantum Hall effect³ and quantum spin liquids,⁴ have garnered a great deal of attention. A quantum spin liquid (QSL) is an insulating state that does not exhibit any conventional magnetic order at zero temperature, typically due to a delicate balance of competing and/or "frustrating" effects (for a review, see Refs. 5 and 6).

Various flavors of QSLs with different types of quasiparticle excitations and braiding statistics have been proposed.^{7–9} However, the reliability of the approximations typically invoked in their solution are often imperfectly understood. Thus, it is useful to find exactly solvable (even though often contrived) models with spin liquid ground states so as to establish their stability as phases of matter and to understand their essential physical properties. The existence of such states is compellingly established¹⁰ for quantum dimer models¹¹ on the triangular lattice.

More recently, the discovery by Kitaev¹² of an exactly solvable, interacting two-dimensional (2D) spin-1/2 model on the honeycomb lattice with a spin liquid phase came as a great boon to the study of exotic ground states in magnetic systems. Since then, variants¹³ of Kitaev's model on trivalent lattices have appeared which realize chiral spin liquids with non-Abelian anyons¹⁴ and spin liquids with a spin Fermi surface.^{15–17} They have also been used to study quantum critical points,^{18,19} entanglement entropy and entanglement spectrum,²⁰ and edge solitons²¹ among others.^{22,23} If the coordination number of the lattice is larger than 3, a generalization of the Kitaev model, the so-called Γ -matrix model, ^{15,24–28} with extra degrees of freedom on each site is needed to ensure exact solvability. These additional degrees of freedom can be either interpreted as an "orbital" degree of freedom,^{26,29} or one may consider each site as having a larger spin, but no orbital degrees of freedom.^{15,30}

Partly motivated by the recent interest in finding a spin liquid with a spinon Fermi surface in Herbertsmithite—a Mott insulator on the kagome lattice³¹—we study an exactly solvable spin-3/2 model on the kagome lattice (see Fig. 1).

Our main finding is that our model possesses a gapless spin liquid phase with a finite spin Fermi surface. We show that the spin Fermi surface is *stable* against any weak perturbations. The stability follows from the lack of inversion symmetry, π rotation, and time-reversal symmetry (TRS) (that is spontaneously broken) in the ground state. Both the *odd* number of electrons per unit cell in the ground state and the stability of the spin Fermi surface qualitatively distinguishes our model from other known exactly solvable models with a finite spin Fermi surface.^{15–17} We also find a gapped Abelian chiral spin liquid phase,¹⁴ which possesses two gapless chiral Majorana edge states for a lattice geometry with boundary.

Model. The Γ -matrix model describing S = 3/2 spins¹⁵ we study respects the translational and threefold rotational symmetry of the kagome lattice and is given by

$$\mathcal{H} = J_{\Delta} \sum_{\langle ij \rangle \in \Delta} \Gamma_i^1 \Gamma_j^2 + J_{\nabla} \sum_{\langle ij \rangle \in \nabla} \Gamma_i^3 \Gamma_j^4 + J_5 \sum_i \Gamma_i^5 + J_{\Delta}' \sum_{\langle ij \rangle \in \Delta} \Gamma_i^{15} \Gamma_j^{25} + J_{\nabla}' \sum_{\langle ij \rangle \in \nabla} \Gamma_i^{35} \Gamma_j^{45},$$
(1)

where we have distinguished the nearest-neighbor couplings J_{ij} as J_{Δ} , J_{∇} and J'_{ij} as J'_{Δ} and J'_{∇} based on whether the link $\langle ij \rangle$ belongs to an up (Δ) triangle or down (∇) triangle, and $\langle ij \rangle$ is taken in the counterclockwise sense for each triangle. Locally, the five Γ matrices satisfy a Clifford algebra { Γ_i^a, Γ_i^b } = $2\delta^{ab}$, where a, b = 1, ..., 5, and $\Gamma^{ab} \equiv [\Gamma^a, \Gamma^b]/(2i)$. In terms of the components of the spin S = 3/2 operators, ^{15,30}

$$\Gamma^{1} = \frac{1}{\sqrt{3}} \{S^{y}, S^{z}\}, \quad \Gamma^{2} = \frac{1}{\sqrt{3}} \{S^{z}, S^{x}\}, \quad \Gamma^{3} = \frac{1}{\sqrt{3}} \{S^{x}, S^{y}\},$$

$$\Gamma^{4} = \frac{1}{\sqrt{3}} [(S^{x})^{2} - (S^{y})^{2}], \quad \Gamma^{5} = (S^{z})^{2} - \frac{5}{4}.$$
(2)

With the identification (2), it is clear the model (1) has a global Ising spin symmetry under 180° rotations about the *z* axis, and possesses TRS, although TRS will be spontaneously broken in the ground state as we describe below, in addition to the translational and threefold rotational lattice symmetry mentioned above.

Method of solution. The key to the exact solvability¹² of the model (1) is an infinite number of conserved operators \hat{W}_p that satisfy $[\hat{W}_p, \mathcal{H}] = 0$ and $[\hat{W}_p, \hat{W}_{p'}] = 0$ for all elementary



FIG. 1. (a) is a schematic representation of the kagome lattice which is a network of corner sharing triangles in two dimensions with three sites per unit cell. (b)–(e) are four energetically distinct flux configurations preserving the translational symmetry of the lattice. A doubled (magnetic) unit cell is required for (d) and (e), where the total flux through a unit cell is $\pm \pi$.

plaquettes labeled by p and p'. As shown in Fig. 1, the kagome lattice contains elementary up and down triangular plaquettes, and hexagonal ones. Specifically, $\hat{W}_{\triangle} = \Gamma_i^{12} \Gamma_j^{12} \Gamma_k^{12}$, $\hat{W}_{\nabla} = \Gamma_i^{34} \Gamma_j^{34} \Gamma_k^{34}$, and $\hat{W}_{\bigcirc} = \Gamma_i^{23} \Gamma_j^{14} \Gamma_k^{23} \Gamma_l^{14} \Gamma_m^{23} \Gamma_n^{14}$, where the sites are taken in a counterclockwise fashion and for \hat{W}_{\bigcirc} the first link (ij) is assumed to lie on a \triangle .

In order to solve the Hamiltonian (1) we introduce a Majorana representation of the Γ matrices,¹⁴

$$\Gamma_i^a = i\xi_i^a c_i, \quad \Gamma_i^5 = ic_i d_i, \quad \Gamma_i^{a5} = i\xi_i^a d_i, \tag{3}$$

with a = 1,2,3,4. There are thus six Majorana species on each site *i*: $\{\xi_i^1, \xi_i^2, \xi_i^3, \xi_i^4, c_i, d_i\}$. The Majorana representation enlarges the spin-3/2 Hilbert space, so that one must enforce the constraint $D_i = -\Gamma_i^1 \Gamma_i^2 \Gamma_i^3 \Gamma_i^4 \Gamma_i^5 = -i\xi_i^1 \xi_i^2 \xi_i^3 \xi_i^4 c_i d_i = 1$, namely, for any physical state $|\Psi\rangle_{\text{phys}} D_i |\Psi\rangle_{\text{phys}} = |\Psi\rangle_{\text{phys}}$ for any *i*. From the enlarged Hilbert space, physical states are obtained by applying the projection operator $P = \prod_i [\frac{1+D_i}{2}]$, where the product is over all sites in the lattice.

Using relations (3), the Hamiltonian (1) becomes

$$\tilde{\mathcal{H}} = \sum_{\langle ij\rangle} [J_{ij}iu_{ij}c_ic_j + J'_{ij}iu_{ij}d_id_j] + J_5 \sum_i ic_id_i, \quad (4)$$

where $u_{ij} = -u_{ji}$, with $u_{ij} = -i\xi_i^1\xi_j^2$ if $ij \in \Delta$ and $u_{ij} = -i\xi_i^3\xi_j^4$ if $ij \in \nabla$. The original Hamiltonian is obtained through $\mathcal{H} = P\tilde{\mathcal{H}}P$. Since $[u_{ij},\tilde{\mathcal{H}}] = [u_{ij}, u_{i'j'} = 0$, the original spin Hamiltonian has been reduced to a model of free Majorana fermions moving in a *static* background of \mathbb{Z}_2 gauge fields:¹² In (4) the u_{ij} can be replaced by their eigenvalues ± 1 . It remains to determine the pattern of the u_{ij} (up to gauge transformations) that yields the lowest-energy state. We will limit our discussion to positive *J* couplings only.

In terms of static Z_2 gauge fields, we define a flux ϕ_p via $\exp(i\phi_p) \equiv \prod_{jk \in p} i u_{jk}$, where *jk* is taken counterclockwise, on each elementary plaquette *p*. It is clear that $\phi_p = \pm \pi/2$ in the triangular plaquettes, and $\phi_p = 0, \pi$ in the hexagonal plaquettes. Since $W_p = \prod_{\langle ij \rangle \in p} u_{ij}$, where *ij* is also taken counterclockwise, $\exp(i\phi_p) = -W_p$ ($-iW_p$) when *p* is hexagon (triangular) plaquettes. Under TRS, $W_p \to \pm W_p$, where +(-) is for hexagon (triangle) plaquettes; it follows that $\phi_p \to -\phi_p$ for triangle plaquettes while ϕ_p remains

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unchanged for hexagon plaquettes. Consequently, a ground state with a certain flux pattern $\{\phi_p\}$ (regardless of any particular choice of u_{ij}) spontaneously breaks TRS and its energy must be degenerate with the ground state with a flux pattern obtained from $\{\phi_p\}$ by changing $\phi_p \rightarrow -\phi_p$ on all triangular plaquettes.¹⁴

In general, the nature of a ground state and its excitations crucially depends on the flux pattern $\{\phi_p\}$ in the ground state. As we will see below, the richness of this model is due in part to the freedom to add additional terms to (1) that preserve the exact solvability, but can be used to select different (gauge-inequivalent) configurations of u_{ij} as the ground state.

Chiral spin liquid. A chiral spin liquid (CSL) breaks TRS spontaneously and has no conventional magnetic order.^{8,14,32} As we have discussed, the current model (1) indeed breaks TRS spontaneously. It remains to be shown that a ground state exists without breaking spin-rotational or translational symmetry. To determine the ground-state flux configuration, we compute the ground-state energy E_G of the Hamiltonian (4) as a function of the u_{ij} .

For a bipartite lattice, the ground-state flux pattern is determined by the Lieb theorem³³ and the flux is always uniform. However, the kagome lattice is not bipartite, so we must determine it numerically and analytically in some special limits.¹⁴ By diagonalizing systems of up to ~10⁴ sites and computing E_G , we indeed find that for various possible parameters in Hamiltonian (1), the ground state has a uniform flux pattern. There are four possible time-reversal-inequivalent uniform flux configuration labeled by $\{\phi_{\Delta}, \phi_{\nabla}, \phi_{\bigcirc}\} = \{\frac{\pi}{2}, \frac{\pi}{2}, \pi\}, \{-\frac{\pi}{2}, \frac{\pi}{2}, \pi\}, \{\frac{\pi}{2}, \frac{\pi}{2}, 0\}, \{-\frac{\pi}{2}, \frac{\pi}{2}, 0\}$ as shown in Figs. 1(b)–1(e). The ground-state flux pattern depends on the relative size of all the coupling constants in Eq. (1), as seen in Fig. 2. For instance, when $J_5 \ll \{J_{\Delta}, J_{\nabla}, J_{\Delta}', J_{\nabla}'\}$, a uniform flux state of $\{\frac{\pi}{2}, \frac{\pi}{2}, 0\}$ or $\{-\frac{\pi}{2}, -\frac{\pi}{2}, 0\}$ is favored.

For small J_5 , the ground state has the uniform flux configuration $\{\frac{\pi}{2}, \frac{\pi}{2}, 0\}$ shown in Fig. 1(d) and all its excitations are fully gapped for a system with periodic boundary conditions. The total flux per lattice unit cell is π ; it follows that the magnetic unit cell must be doubled by a gauge choice. Note that even though a specific gauge choice u_{ij} with this flux configuration would "seemingly" double the unit cell



FIG. 2. (Color online) (a) Ground-state energy per site of (1) as a function of J_5/J with $J_{\triangle} = J'_{\triangle} = J_{\nabla} = J'_{\nabla} = J$ for the uniform flux configurations shown in Figs. 1(b)–1(e). (b) Ground-state flux configuration among Figs. 1(b)–1(e) as a function of $J_{\triangle}, J_{\nabla}, J_5$ for $J_{\triangle}^2 + J_{\nabla}^2 + J_5^2 = 1$ with $J_{\nabla} = J'_{\nabla}$ and $J_{\triangle} = J'_{\triangle}$. The coloring scheme follows that of the legend in Fig. 2(a).



FIG. 3. (a) Band structure on a cylindrical geometry for $J_{\triangle} = J'_{\triangle} = 1.0$, $J_{\nabla} = J'_{\nabla} = 0.8$, $J_5 = 0$. There are two gapless chiral Majorana edge states (dotted lines) which overlap on each other. (b) For $J_{\triangle} = 1.0$, $J'_{\triangle} = 0.6$, $J_{\nabla} = 0.9$, $J'_{\nabla} = 0.5$, and $J_5 = 0.1$, the two gapless edges states separate. These ground states are thus CSLs with a spectrum Chern number (±2) and the vortices obey Abelian statistics.

and break the threefold rotational symmetry of the lattice, the physical ground state obtained after the projection is translationally and threefold rotationally invariant because the gauge choice obeys the corresponding projective symmetry group transformations that combines a physical symmetry (here, translation or threefold rotation) and an appropriate gauge transformation.³⁴ Consequently, no symmetries other than the time reversal are broken in the physical ground state.

For the system with cylindrical symmetry, Figs. 3(a) and 3(b) illustrate the existence of chiral edge modes, indicating a finite spectral Chern number of ± 2 . For $J_{\triangle} = J'_{\triangle}$, $J_{\nabla} = J'_{\nabla}$, and $J_5 = 0$, the *c* and *d* Majorana fermions decouple and have identical spectrum. It follows that the two gapless chiral Majorana edge states overlap as shown in Fig. 3(a). Generically, the two chiral edge modes are separated, as shown in Fig. 3(b). Moreover, the arguments in Refs. 15, 25 and 35 for spin correlation apply here as well-the spin correlations vanish beyond nearest neighbors, establishing a CSL phase with a finite spectral Chern number and gapless chiral edge states on the boundary as a ground state of (1). Because of the even spectral Chern number (± 2) , we expect the vortex excitations are Abelian. Nonetheless, if the parameters in the Hamiltonian doubles the unit cell, a gapped non-Abelian chiral spin liquid can also be obtained.³⁶

Gapless spin liquid with stable spin Fermi surface. For arbitrary values of $J_{\triangle}, J_{\nabla}, J'_{\Delta}, J'_{\nabla}$ in (1), we found that the system is always gapped as long as we kept $J_5 = 0$, where $W_p = -1$ for all p.³⁶ By increasing J_5 , we found that the system closes its gap at some critical values of J_5 and the ground-state flux configuration changes when a critical point is crossed [see Fig. 2(a)]. Note that the energy differences between different flux states are surprising small, as shown in Fig. 2(a). For a generic J_5 not at those critical points, the system stays gapped, which seems to make the search for a spin Fermi surface difficult for the Hamiltonian (1). Fortunately, while changing J_5 , a particular flux configuration can be always favored by adding a pure flux term that does not destroy the



FIG. 4. The Fermi surface (solid line) for the flux configuration $\{\frac{\pi}{2}, \frac{\pi}{2}, \pi\}$ and $\{J_{\Delta}, J_{\nabla}, J'_{\Delta}, J'_{\nabla}, J_5\} = \{1.0, 0.3, 0.8, 0.5, 1.4\}$. The dashed hexagon is the Brillouin zone boundary. Note that there is only one Fermi pocket for this set of parameters and the three pockets shown are related by a reciprocal lattice vector and are thus equivalent.

exact solvability of the model. Specifically, to stabilize a flux configuration, we add the following term to Eq. (1),

$$\mathcal{H}_{\rm FS} = -\alpha \sum_{\bigcirc} \hat{W}_{\bigcirc} - \beta \sum_{\langle \triangle, \nabla \rangle} \hat{W}_{\triangle} \hat{W}_{\nabla}.$$
 (5)

The required value of α and β to stabilize a desired flux pattern depends on J_5 , but is typically rather small^{16,17} as the energy differences between different flux states are small—see Fig. 2(a).

For appropriate positive α and β , the ground state with the flux configuration $\{\frac{\pi}{2}, \frac{\pi}{2}, \pi\}$ (or $\{-\frac{\pi}{2}, -\frac{\pi}{2}, \pi\}$) is favored. For this flux configuration, we obtain a finite Fermi surface as shown in Fig. 4(a) for $J_{\Delta} = 1.0$, $J_{\nabla} = 0.3$, $J'_{\Delta} = 0.8$, $J'_{\nabla} = 0.5$, and $J_5 = 1.4$. The dashed line of the hexagon is the Brillouin zone boundary. Note that there is only one Fermi pocket around one inequivalent corner for this set of parameters. The Fermi surface has a C_3 rotational symmetry around the zone corner that is expected from the C_3 symmetry of the model. Varying the parameters in Eq. (1) by a small amount will only change the shape and size of the Fermi surface but the Fermi surface itself is robust.

An important question to ask about a Fermi surface is whether it is stable against any weak perturbations. In 2D, a generic Fermi surface cannot be fully gapped by a weak "density wave" due to the lack of perfect nesting. However, a generic Fermi surface can still be fully gapped by a "pairing" term with momentum Q if the spectrum at k and -k + Qare degenerate for any \vec{k} and some fixed \vec{Q} . In general, time reversal, π rotation, or lattice inversion symmetry enforces degeneracy at \vec{k} and $-\vec{k} + \vec{Q}$ and allows a putative Fermi surface to be gapped by an infinitesimal "pairing" term with momentum \vec{Q} . Note that a nonzero \vec{Q} is encountered in the physical state but no gauge choice possesses one of those symmetries. If the ground state has no time reversal, π rotation, or inversion symmetry, a putative Fermi surface will be *stable* against any weak perturbations. In the current model, the π rotation and inversion symmetries are explicitly broken by $J_{\triangle} \neq J_{\nabla}$ or $J'_{\triangle} \neq J'_{\nabla}$; the TRS is always spontaneously broken. It follows that the spin Fermi surface found in our model is stable against any weak perturbations. This is in contrast with the spin Fermi surface found in Refs. 15-17 that can be gapped by some sort of weak "nesting" or "pairing" terms. Lastly, this state has recently been shown to exhibit bond

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energy correlations that have a $1/|\mathbf{r}|^3$ power-law behavior³⁷ despite having ultrashort spin correlations.

Concluding remarks. We studied an exactly solvable model of spins on the kagome lattice with an odd number of electrons per unit cell (making it a "true" Mott insulator) that realizes a gapped chiral spin liquid with two gapless chiral Majorana edge modes and a gapless phase with a finite spin Fermi surface that is stable against any weak perturbations. While in terms of the spin variables the model may seem highly anisotropic and therefore somewhat artificial,

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Kitaev-type models have been derived as effective low-energy theories from more "realistic" Hamiltonians with strong spinorbit coupling³⁸ and can be readily engineered in optical lattices.^{39,40}

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