



Applied Physics Laboratory

University of Washington

1013 NE 40th Street
Box 355640
Seattle, WA 98105-6698

206-543-1300
FAX 206-543-6785
www.apl.washington.edu

25 February 2013

To: Robert H. Headrick, ONR 322
Office of Naval Research
875 North Randolph Street
Arlington, VA 22203-1995

From: Daniel Rouseff

Subj: ONR Grant N00014-10-1-0495, "Scintillation in a shallow water waveguide"

Encl: (1) Final Report for Scintillation in a Shallow Water Waveguide
(2) "Striation-based beamforming for estimating the waveguide invariant with passive sonar," by Daniel Rouseff, University of Washington, and Lisa M. Zurk, Portland State University
(3) SF298 for "Striation-based beamforming for estimating the waveguide invariant with passive sonar"

Please see the enclosures listed above, they constitute the final deliverables for the subject grant, "Scintillation in a shallow water waveguide." Enclosure (1) is the final report that closes the subject grant, referencing enclosure (2) which is the final publication from the grant, with an attached SF298 form for that publication as enclosure (3).

D. Rouseff SKH
Daniel Rouseff

cc: Grant & Contract Administrator, APL-UW
Office of Sponsored Programs, UW
Administrative Contracting Officer, ONRRO Seattle
Naval Research Laboratory
Defense Technical Information Center

Final Report

SCINTILLATION IN A SHALLOW WATER WAVEGUIDE

Daniel Rouseff

Applied Physics Laboratory

University of Washington

1013 NE 40th St.

Seattle, WA 98105

phone: (206) 543-1300 fax: (206) 543-6785 email: rouseff@apl.washington.edu

Grant Number: N00014-10-1-0495

<http://www.apl.washington.edu>

Background

Acoustic rays or modes propagating in the shallow water waveguide combine constructively and destructively to produce richly structured interference patterns. In the early 1980s, Russian scientists showed how the primary features of these interference patterns could be distilled into a single scalar parameter, the so-called waveguide invariant. In recent years, the waveguide invariant concept has become central to many signal processing schemes for both passive and active sonar. A difficulty in applying the concept is that one must know the waveguide invariant's numerical value. The canonical value in shallow water is 1.0, but several experiments have shown that a larger number is often appropriate when the sound speed profile has a sharp gradient. Deviations from the canonical value become more pronounced as the frequency is increased. These deviations are of more than academic interest: errors in the assumed numerical value for the waveguide invariant translate directly into errors in the estimated range to a target.

Work Completed

The waveguide invariant has traditionally been regarded as a low frequency technique. Under current support, the objective has been to address issues relevant to extending the method into the mid-frequency (1-10 kHz) regime. The first objective was to develop an algorithm for estimating the numerical value of the waveguide invariant directly from acoustic data without having a priori knowledge of a source's range or depth. The second objective was to study how signal fluctuations (scintillation) caused by random variability in the water column from such features as internal waves would affect the waveguide invariant concept. The work has made use of existing data sets collected under ONR support: the Shallow Water 2006 (SW06) experiment and the 2011 Gulf Experiment (GulfEx11)

As listed below, the completed work has been documented in 7 journal publications and 5 invited conference presentations.

Research Highlight

Existing algorithms allow one to estimate only the ratio between the invariant and range: to get the source's range, one must know the numerical value of the invariant. The primary result produced under current funding is a new algorithm for isolating range from the waveguide invariant thereby permitting one to calculate both quantities and not just the ratio. The algorithm works by twice beamforming the measured acoustic field. Beamforming conventionally, the

processor first focuses at the true bearing of the source. The field is then beamformed with each hydrophone in the array evaluated at a slightly different frequency. The frequency-shifted output will shift the processor's focus to a different bearing. The extent to which the focus shifts between the two calculations provides a direct measurement of the waveguide invariant that is independent of the source's range. With this independent knowledge of the waveguide invariant, one can then calculate the range unambiguously.

The method of twice-beamforming the field was first demonstrated successfully with numerical simulations. It was further shown that the method could provide a coarse estimate of source's depth as it could distinguish near-surface sources from sources that were located below the mixed layer. Analysis of data collected during GulfEx11 provided additional support for the proposed algorithm.

The complete paper is included as part of this report.

Professional Activities and Honors

Acoustical Society of America. Technical Committee service: Underwater Acoustics (three terms, 1998-2004 and 2009-2012), Acoustical Oceanography (four terms, 2002-2014). Technical Program Organizing Meeting (TPOM) representative for Underwater Acoustics and Acoustical Oceanography, Hong Kon. Organizer and Co-chair of Special Session "Underwater acoustic communications and networking," Joint Acoustical Society of America/Chinese Acoustical Society Meeting, Hong Kong May 14-18, 2012.

Excellent Reviewer Award, *IEEE Journal of Oceanic Engineering*, 2012.

Invited lecture series, Xiamen University, Xiamen, China, November 27-30, 2011.

Invited lecture series, Ocean University, Qingdao, China, November 22-26, 2011.

Invited lecture, Harbin Engineering University, Harbin, China, July 19, 2010.

Invited lecture series, Zhejiang University, Hangzhou, China, July 12-14, 2010.

Publications

Refereed Journal Articles (7 total)

M. Xia, D Rouseff, J. A. Ritcey, X. Zou, C. Polprasert, and W. Xu, "Underwater acoustic communication in a highly refractive environment using SC-FDE," submitted to *IEEE J. Oceanic. Eng.* (2012).

L. M. Zurk and D. Rouseff, "Striation-based beamforming for active sonar with a horizontal line array" *J. Acoust. Soc. Am.* **132**, EL264-EL270 (2012).

S. H. Abadi, D. Rouseff, and D. R. Dowling, "Blind deconvolution for robust signal estimation and approximate source localization," *J. Acoust. Soc. Am.* **131**, 2599-2610 (2012).

D. Rouseff and L. M. Zurk, "Striation-based beamforming for estimating the waveguide invariant with passive sonar," *J. Acoust. Soc. Am.* **130**, EL76-EL81 (2011).

D. Rouseff and D. Tang, "Internal waves as a proposed mechanism for increasing ambient noise in an increasingly acidic ocean," *J. Acoust. Soc. Am.* **127**, EL235-EL239 (2010).

J. Yang, D. Rouseff, D. Tang, and F. S. Henyey, "Effect of the internal tide on acoustic transmission loss at mid-frequencies," *IEEE J. Oceanic Eng.* **35**, 3 – 11 (2010).

A. Turgut, M. Orr, and D. Rouseff, "Broadband source localization using horizontal-beam acoustic intensity striations," *J. Acoust. Soc. Am.* **127**, 73-83 (2010).

Invited Conference Talks (five total)

D. Rouseff, M. Xia, J. A. Ritcey, X. Zou, C. Polprasert, and W. Xu, "Experimental demonstration of underwater communication using Single-Carrier Frequency-Domain Equalization," Invited talk in underwater acoustic communications session, *Euro. Conf. Underwater Acoustics*, Edinburgh, UK July 2-6, 2012.

D. Rouseff, "Underwater acoustic communications results from the joint China-US Cooperative Array Performance Experiment," Invited talk, *3rd Int. Conf. Underwater Acoustics*, Beijing, China May 21-25, 2012.

D. Rouseff, "Performance of underwater acoustic communications algorithms: Limitations imposed by the dynamic ocean environment." Invited keynote lecture, *9th Int. Symposium Modern Acoustics (ISMA9)*, Nanjing, China May 20-22, 2012.

D. Rouseff, F. S. Henyey, and D. Tang, "Effect of linear internal waves on mid-frequency acoustic fluctuations in shallow water," Invited talk, structured session on internal waves. *4th Int. Conf. Underwater Acoustic Measurements Technology*, Kos, Greece, June 20-24, 2011.

D. Rouseff, R. Light, Z. Wang, and S. Zhou, "Comparing vector- and pressure-sensor arrays: the Cooperative Array Performance Experiment (CAPEx09)," Special session on vector sensors, *162nd Mtg. of Acoustical Society of America*, San Diego, CA, Oct. 31-Nov. 4, 2011.

Striation-based beamforming for estimating the waveguide invariant with passive sonar

Daniel Rouseff

*Applied Physics Laboratory, University of Washington, 1013 NE 40th Street, Seattle, Washington 98105
rouseff@apl.washington.edu*

Lisa M. Zurk

*Department of Electrical and Computer Engineering, Portland State University, Portland, Oregon 97201
zurkl@pdx.edu*

Abstract: The waveguide invariant summarizes the pattern of constructive and destructive interference between acoustic modes propagating in the ocean waveguide. For many sonar signal-processing schemes, it is essential to know the correct numerical value for the waveguide invariant. While conventional beamforming can estimate the ratio between the waveguide invariant and the range to the source, it cannot unambiguously separate the two terms. In the present work, striation-based beamforming is developed. It is shown that the striation-based beamformer can be used to produce an estimate for the waveguide invariant that is independent of the range. Simulation results are presented.

© 2011 Acoustical Society of America

PACS numbers: 43.60.Fg, 43.30.Cq, 43.30.Wi [JFL]

Date Received: January 31, 2011 Date Accepted: June 3, 2011

1. Introduction

Consider an underwater passive sonar scenario where a horizontal array measures the acoustic field produced by a distant source. Mapped as a function of frequency ω and range r , the observed acoustic intensity I often exhibits striations. These striations, alternating bands of high and low intensity, result from constructive and destructive interference between the propagating acoustic modes supported by the ocean waveguide. Chuprov¹ developed a simple formula for the slope $d\omega/dr$ of the striations:

$$\frac{d\omega}{dr} = \frac{-\partial I / \partial r}{\partial I / \partial \omega} = \omega\beta/r, \quad (1)$$

where β is the so-called waveguide invariant. Typically, one would know the frequency and measure the slope allowing the β/r ratio to be calculated.

While the ratio between the waveguide invariant and the range may be readily determined, isolating the range from the numerical value for β is more problematic. In practice, one might simply assume that β is known and then calculate r from the β/r ratio. The canonical value in shallow water is $\beta=1$, but this choice may prove far too coarse. If both the source and array are below the thermocline, both simulations² and experiments^{3,4} have shown that $\beta=1.3$ or 1.4 is more appropriate. Erroneously assuming $\beta=1$ when it is actually $\beta=1.3$ translates directly into a 30% error in the estimated value for the range.

In the present work, a method is proposed for isolating the waveguide invariant and producing an estimate for its numerical value that is independent of the range. The method relies on twice beamforming the acoustic pressure measured on a horizontal array due to a distant source. The pressure field is first beamformed conventionally at a single frequency to achieve a focus at the correct bearing of the source. The field is then beamformed again but with each point on the array evaluated at a slightly

different frequency. The frequency offset is selected based on the observed slope of the intensity striations. It is shown that the focus will shift from what is observed with conventional beamforming and that the extent of the shift gives a measure of β that is independent of r . The method also gives an indirect coarse estimate of the source's depth.

To begin the development, assume a point source at $\mathbf{r}_0 = (r_0 \cos \phi_0, r_0 \sin \phi_0, z_0)$ in the ocean waveguide. The resulting field is measured on a horizontal line array of length L oriented along the y -axis, $-L/2 < y < L/2$, at depth z_a . Assuming a range-independent environment and an $\exp(-i\omega t)$ convention, the measured complex field is expanded in normal modes as

$$p(y, \omega) = \sum_m (\xi_m r)^{-1/2} \Psi_m(z_0) \Psi_m(z_a) \exp(i\xi_m r), \quad (2)$$

where each mode Ψ_m has corresponding horizontal wavenumber ξ_m and certain unimportant scaling factors are neglected. It is assumed that the source is coherent over the narrow frequency band of interest. The range r to a point on the array is

$$\begin{aligned} r &= [(r_0 \cos \phi_0)^2 + (y - r_0 \sin \phi_0)^2]^{1/2} \\ &\approx r_0 - y \sin \phi_0 + y^2/(2r_0) \end{aligned} \quad (3)$$

to the term second order in y that expresses wavefront curvature.

Since $I = |p|^2$, the slope of the observed intensity follows from Eqs. (1)–(3):

$$\frac{d\omega}{dy} = \frac{d\omega}{dr} \frac{dr}{dy} \approx -\omega(\beta/r_0) \sin \phi_0, \quad (4)$$

where the distant source is assumed not too near broadside, $\phi_0 = 0$, so the wavefront curvature term can be neglected. Solving the separable differential equation yields

$$\ln(\omega/\omega_0) = -(\beta/r_0) \sin(\phi_0)y, \quad (5)$$

that may be approximated for frequencies near the center frequency ω_0 as

$$\omega = \omega_0 - Sy, \quad \text{where } S = \omega_0(\beta/r_0) \sin \phi_0. \quad (6)$$

Equation (6) says that the level curves of constant intensity as observed along the array will map onto straight lines of slope S . Consequently, incoherent processing using only the intensity is sufficient to estimate S . The numerical value for S might be calculated by spectral methods, as originally suggested by Chuprov,¹ or perhaps by using Radon transforms.⁵ Regardless of the specific method used to do the calculation, the remainder of this report assumes that the value for S is known.

Having first processed the measured field incoherently to deduce S , it is now processed coherently by beamforming. Define the beamformer output in look direction ϕ as

$$B(\phi) \equiv |b(\phi)|^2 \quad \text{with } b(\phi) = L^{-1} \int_{-L/2}^{L/2} p(y, \omega) w^*(y, \omega; \phi) dy. \quad (7)$$

For a conventional Bartlett beamformer, the weights are

$$w^*(y, \omega; \phi) = \exp[i(\omega/c_0) \sin(\phi)y], \quad (8)$$

where c_0 is the reference sound speed. Substituting Eqs. (2) and (8) into (7) and rearranging terms yields

$$b(\phi) = \sum_m C_m D_m(\omega; \phi). \quad (9)$$

The terms slowly varying in y and ω are lumped into C_m . The rapidly varying phase terms are included in D_m :

$$D_m(\omega; \phi) = L^{-1} \int_{-L/2}^{L/2} \exp[i\xi_m(\omega)r + i(\omega/c_0) \sin(\phi)y] dy, \quad (10)$$

where the frequency dependence of the horizontal wavenumber ξ_m has been made explicit.

In conventional beamforming, the frequency is fixed at some constant value, say, $\omega = \omega_0$. In the present work, a striation-based beamformer is considered where different points along the array are evaluated at different frequencies. The frequency varies linearly across the array based on the observed slope S of the intensity striations. To maintain generality, let the frequency across the array be

$$\omega = \omega_0 - \alpha S y, \quad (11)$$

where α is an adjustable parameter. For conventional beamforming, $\alpha = 0$ and the frequency is constant across the array. For beamforming along the striations, $\alpha = 1$; see Eq. (6). The frequency-dependent modal wavenumber across the array can be approximated by a Taylor's series expansion. To first order,

$$\begin{aligned} \xi_m(\omega_0 - \alpha S y) &\approx \xi_m(\omega_0) + (\partial \xi_m / \partial \omega)(-\alpha S y) \\ &= \omega_0 / v_m - (\alpha S / u_m) y, \end{aligned} \quad (12)$$

where v_m and u_m are the phase and group velocities, respectively, for mode m at $\omega = \omega_0$. The expansion in Eq. (12) should retain the quadratic term to be strictly consistent with the expansion in Eq. (3). The quadratic term in expansions like Eq. (12) is usually neglected; see the discussion in Ref. 6 for the limitation associated with this approximation.

Combining the above equations yields for the striation-based beamformer

$$D_m(\omega_0 - \alpha S y; \phi) = L^{-1} \int_{-L/2}^{L/2} \exp[i(\theta_0 + \theta_1 y + \theta_2 y^2)] dy, \quad (13)$$

where terms have been grouped in like order of y with coefficients

$$\theta_0 = (\omega_0 / v_m) r_0, \quad (14)$$

$$\begin{aligned} \theta_1 &= (\omega_0 / c_0) \sin(\phi) - (\omega_0 / v_m) \sin(\phi_0) - \alpha S r_0 / u_m \\ &= (\omega_0 / c_0) \sin(\phi) - (\omega_0 / v_m) \sin(\phi_0) [1 + \alpha \beta (v_m / u_m)], \end{aligned} \quad (15)$$

$$\theta_2 = (\omega_0 / v_m) / (2r_0) + (\alpha S / u_m) [\sin(\phi_0) - (u_m / c_0) \sin(\phi)]. \quad (16)$$

It is instructive to consider the linear coefficient θ_1 in greater detail. In transitioning between the two forms of Eq. (15), the definition of the striation slope S , Eq. (6), has been applied. Since S is proportional to the ratio β / r_0 , the product $S r_0$ appearing in Eq. (15) is independent of r_0 . The key point is that θ_1 therefore depends on the waveguide invariant but is independent of range; β has been isolated from r_0 by striation-based beamforming.

Equation (13) can be evaluated exactly in terms of Fresnel integrals.⁷ To gain greater insight into the result, it is useful to assume that the source is in the far field of

the receiving array. In the far field, the quadratic term in Eq. (13) is neglected and the integral reduces to

$$D_m(\omega_0 - \alpha S y; \phi) = e^{i\theta_0} \text{sinc}(\theta_1 L/2), \quad (17)$$

where $\text{sinc}(x) \equiv \sin(x)/x$. The magnitude is a maximum when $\theta_1 = 0$ implying focusing when the beamformer look direction ϕ satisfies

$$\begin{aligned} \sin(\phi) &= (c_0/v_m) \sin(\phi_0) [1 + \alpha\beta(v_m/u_m)] \\ &\approx \sin(\phi_0)(1 + \alpha\beta), \end{aligned} \quad (18)$$

where the approximate form ignores the small differences between c_0 and the phase and group velocities to yield a result that is independent of the mode index.

Equations (6) and (18) suggest a three step processing strategy for estimating the waveguide invariant. First, process the field incoherently to estimate the slope S of the intensity striations. Second, beamform conventionally with $\alpha = 0$. The beamformer will focus at the true bearing of the source, $\phi = \phi_0$. Finally, perform striation-based beamforming with $\alpha \neq 0$. The focus will shift to some new $\phi \neq \phi_0$ but, since the true ϕ_0 has already been estimated, the location of the new focus can be used in Eq. (18) to solve for β . The value for the waveguide invariant is thereby estimated without knowing the range or depth of the source.

The numerical value for the adjustable parameter α should be selected with some care. The choice $\alpha = 1$ is attractive because it means a strong signal across the array without fades. This should improve performance in a noisy environment. When the source is at a bearing too far from array broadside, however, the choice $\alpha = 1$ will fail to produce a focus. For example, no beamformer look direction ϕ will satisfy Eq. (18) if $\alpha = \beta = 1.0$ and $|\phi_0| > 30^\circ$. If conventional beamforming ($\alpha = 0$) reveals a source far removed from broadside, the striation-based beamformer should use a value for α that ensures that Eq. (18) will have a solution. In addition, α must be selected so that the total frequency shift across the array, αSL , is within the coherence bandwidth of the source.

A specific numerical simulation serves to illustrate the striation-based beamforming concept. Consider an environment typical of the East China Sea as observed during a 2001 experiment.⁸ The 105 m deep water column has a 40 m deep surface mixed layer above a sharp thermocline. The sound speed contrast between the surface mixed layer and bottom of the water column is 12 m/s. Assume a 128 element horizontal receiving array with 0.5 m spacing ($L = 63.5$ m) positioned at depth $z_a = 60$ m. The source is positioned at range $r_0 = 5$ km and bearing relative to array broadside $\phi_0 = 20^\circ$. The initial source depth is $z_0 = 60$ m so that both the source and the receiving array are positioned below the part of the thermocline with a sharp gradient. With both the source and the receiving array below the main thermocline, the low-order acoustic modes that have an upper turning depth below the sea surface will contribute strongly to the acoustic field. In such a scenario, previous results²⁻⁴ show that $\beta > 1.0$ might be expected.

Figure 1 shows the simulated intensity as calculated along the array over a 50 Hz band. The calculation was made using a normal mode code and the plot has 20 dB dynamic range. Striations are plainly evident. A plausible estimate for the slope of the striations is $S = 0.089$ Hz/m implying a $SL = 5.7$ Hz frequency shift over the length of the array. Superimposed on the image are lines corresponding to $\alpha = 0$ and $\alpha = 1$ using reference frequency $\omega_0/2\pi = 1$ kHz in Eq. (11).

A discrete Bartlett beamformer was implemented and Fig. 2 shows the results. Beamforming conventionally ($\alpha = 0$), the figure shows a focus at look direction $\phi = \phi_0 = 20^\circ$ as expected. The plot is normalized so the conventional $B(\phi_0) = 1.0$. The field was then beamformed along the striation ($\alpha = 1$) with the same normalization applied and the result plotted. As expected, the output at the focus is higher for the

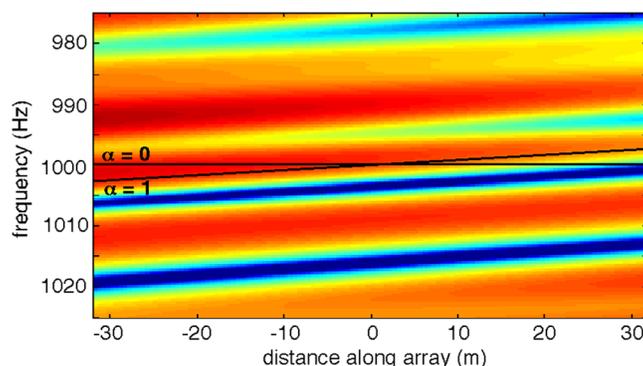


Fig. 1. (Color online) Acoustic intensity observed across horizontal array as function of frequency. Superimposed lines $\alpha = 0$ and $\alpha = 1$ denote trajectories for conventional and striation-based beamforming, respectively. Dynamic range is 20 dB. See text for simulation details.

striation-based beamformer. More importantly, the location of the focus has shifted to $\phi = 52^\circ$. Using $\phi = 52^\circ$ and $\phi_0 = 20^\circ$ in Eq. (18) yields a value for the waveguide invariant $\beta = 1.3$, a value consistent with experimental results^{3,4} when both source and receiver are below the main thermocline.

The simulation was repeated with all the same parameters except the source depth was changed to $z_0 = 10$ m. With the source in the surface mixed layer, the low-order modes that cause $\beta > 1.0$ are not excited. Striations are again evident, but with a shallower slope than is observed in Fig. 1; $S = 0.069$ Hz/m is a reasonable value. The conventional and striation-based beamformers focus at $\phi = \phi_0 = 20^\circ$ and $\phi = 43^\circ$, respectively. Using these angles in Eq. (18) yields $\beta = 1.0$ for the shallow source.

Because the striation-based beamformer is able to quantify β , it also provides a coarse estimate of the source depth, at least to the extent that it can distinguish between shallow and deep sources. A caveat is that the present analysis has assumed a range-independent environment. Range dependence from such environmental factors as internal waves will cause the acoustic modes to couple⁷ and make source depth estimation more problematic.

To summarize, while conventional beamforming can determine a source's bearing and the β/r_0 ratio, it is unable to separate the waveguide invariant β from the range r_0 . Striation-based beamforming breaks the β/r_0 ambiguity and provides an independent estimate for the waveguide invariant.

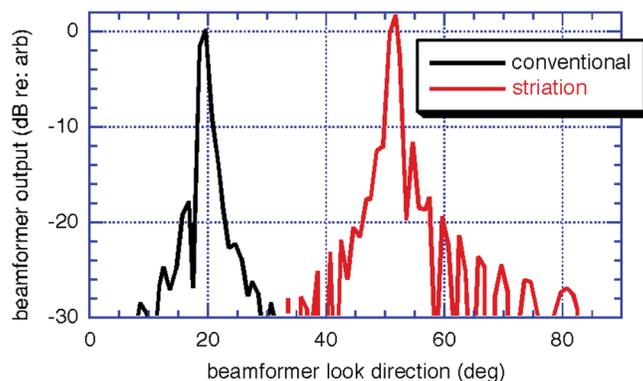


Fig. 2. (Color online) Beamforming results. True source at bearing $\phi_0 = 20^\circ$. Shift in location of focus from conventional ($\alpha = 0$) to striation-based ($\alpha = 1$) beamforming can be used to estimate the waveguide invariant using Eq. (18). See text for details.

Acknowledgments

This work was supported by the Office of Naval Research.

References and links

- ¹S. D. Chuprov, "Interference structure of a sound field in a layered ocean," in *Ocean Acoustics: Current State*, edited by L. M. Brekhovskikh and I. B. Andreevoi (Nauka, Moscow, 1982), pp. 71–91.
- ²D. Rouseff and R. C. Spindel, "Modeling the Waveguide Invariant as a Distribution," in *Ocean Acoustic Interference Phenomena and Signal Processing*, edited by W. A. Kuperman and G. L. D'Spain (AIP, New York, 2002), pp. 137–148.
- ³W. S. Hodgkiss, H. C. Song, W. A. Kuperman, T. Akal, C. Ferla and D. R. Jackson, "A long-range and variable focus phase-conjugation experiment in shallow water," *J. Acoust. Soc. Am.* **105**, 1597–1604 (1999).
- ⁴J. E. Quijano, L. M. Zurk, and D. Rouseff, "Demonstration of the invariance principle for monostatic active sonar," *J. Acoust. Soc. Am.* **123**, 1329–1337 (2008).
- ⁵M. Born and E. Wolf, *Principles of Optics*, 7th ed. (Cambridge University Press, Cambridge, 1999), pp. 219–227.
- ⁶J. A. Stratton, *Electromagnetic Theory* (McGraw-Hill, New York, 1941), pp. 330–340.
- ⁷*Handbook of Mathematical Functions*, edited by M. Abramowitz and I. A. Stegun (U. S. Govt. Printing Office, Washington, D.C., 1964), p. 304.
- ⁸D. Rouseff and D. Tang, "Internal wave effects on the ambient noise notch in the East China Sea: model/data comparison," *J. Acoust. Soc. Am.* **120**, 1284–1294 (2006).

REPORT DOCUMENTATION PAGE

Form Approved
OMB No. 0704-0188

The public reporting burden for this collection of information is estimated to average 1 hour per response, including the time for reviewing instructions, searching existing data sources, gathering and maintaining the data needed, and completing and reviewing the collection of information. Send comments regarding this burden estimate or any other aspect of this collection of information, including suggestions for reducing the burden, to the Department of Defense, Executive Service Directorate (0704-0188). Respondents should be aware that notwithstanding any other provision of law, no person shall be subject to any penalty for failing to comply with a collection of information if it does not display a currently valid OMB control number.

PLEASE DO NOT RETURN YOUR FORM TO THE ABOVE ORGANIZATION.

1. REPORT DATE (DD-MM-YYYY) 22-07-2012		2. REPORT TYPE Final Publication		3. DATES COVERED (From - To) 01 Feb 2010 - 31 Dec 2012	
4. TITLE AND SUBTITLE Striation-based beamforming for estimating the waveguide invariant with passive sonar				5a. CONTRACT NUMBER	
				5b. GRANT NUMBER N00014-10-1-0495	
				5c. PROGRAM ELEMENT NUMBER	
				5d. PROJECT NUMBER	
				5e. TASK NUMBER	
				5f. WORK UNIT NUMBER	
6. AUTHOR(S) Daniel Rouseff, University of Washington Lisa M. Zurk, Portland State University				8. PERFORMING ORGANIZATION REPORT NUMBER	
7. PERFORMING ORGANIZATION NAME(S) AND ADDRESS(ES) Applied Physics Laboratory University of Washington 1013 NE 40th St Seattle, WA 98105				10. SPONSOR/MONITOR'S ACRONYM(S) ONR	
9. SPONSORING/MONITORING AGENCY NAME(S) AND ADDRESS(ES) Office of Naval Research 875 North Randolph Street Arlington, VA 22203-1995				11. SPONSOR/MONITOR'S REPORT NUMBER(S)	
12. DISTRIBUTION/AVAILABILITY STATEMENT Distribution Statement A: Approved for public release; distribution is unlimited.					
13. SUPPLEMENTARY NOTES					
14. ABSTRACT The waveguide invariant summarizes the pattern of constructive and destructive interference between acoustic modes propagating in the ocean waveguide. For many sonar signal-processing schemes, it is essential to know the correct numerical value for the waveguide invariant. While conventional beamforming can estimate the ratio between the waveguide invariant and the range to the source, it cannot unambiguously separate the two terms. In the present work, striation-based beamforming is developed. It is shown that the striation-based beamformer can be used to produce an estimate for the waveguide invariant					
15. SUBJECT TERMS beamforming, passive sonar, sonar signal-processing, waveguide invariant					
16. SECURITY CLASSIFICATION OF:			17. LIMITATION OF ABSTRACT	18. NUMBER OF PAGES 6	19a. NAME OF RESPONSIBLE PERSON Daniel Rouseff
a. REPORT U	b. ABSTRACT U	c. THIS PAGE U			19b. TELEPHONE NUMBER (Include area code) 206-543-1300