

# Similar Pathogen Targets in *Arabidopsis thaliana* and *Homo sapiens* Protein Networks

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## Abstract

We study the behavior of pathogens on host protein networks for humans and *Arabidopsis* - noting striking similarities. Specifically, we perform  $k$ -shell decomposition analysis on these networks - which groups the proteins into various “shells” based on network structure. We observe that shells with a higher average degree are more highly targeted (with a power-law relationship) and that highly targeted nodes lie in shells closer to the inner-core of the network. Additionally, we also note that the inner core of the network is significantly under-targeted. We show that these core proteins may have a role in intra-cellular communication and hypothesize that they are less attacked to ensure survival of the host. This may explain why certain high-degree proteins are not significantly attacked.

**Citation:** Shakarian P, Wickiser JK (2012) Similar Pathogen Targets in *Arabidopsis thaliana* and *Homo sapiens* Protein Networks. PLoS ONE 7(9): e45154. doi:10.1371/journal.pone.0045154

**Editor:** Ying Xu, University of Georgia, United States of America

**Received:** April 23, 2012; **Accepted:** August 16, 2012; **Published:** September 21, 2012

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**Funding:** P.S. and J.K.W. are supported by ARO grant 611102B74F, the opinions in this paper are those of the authors and do not necessarily reflect the opinions of the funders, the U.S. Military Academy, or the U.S. Army. <http://www.arl.army.mil/www/default.cfm?page=29> The funders had no role in study design, data collection and analysis, decision to publish, or preparation of the manuscript.

**Competing Interests:** The authors have declared that no competing interests exist.

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## Introduction

Recently, the work of Mukhtar et al. [1,2] mapped protein interactions from the reference plant *Arabidopsis thaliana* (hereafter, *Arabidopsis*) and two pathogenic effectors. Additionally, the recent work of Navratil et al. [3] studied a human protein interaction network and its interactions with 416 viral proteins. In this paper, we perform  $k$ -shell decomposition analysis [4–6] and other techniques on these networks. In doing so, we are able to identify several interesting aspects of the behavior of the pathogens with respect to both species. First, we observe a strong power-law correlation between the average degree of certain parts of the network called shells and the average number of pathogen interactions for each node. This provides us some insight on which parts of the network are more attacked by the pathogens. We also show that the proteins most often attacked tend to lie in the higher numbered shells (i.e. more toward the “core” of the network). Next, we find that the nature of the attack of the pathogens is somewhat limited in that an important structural component - the core - of both networks is significantly under-attacked. Finally, we also present some species-specific results for the two protein networks.

## Results

### Shells of Higher Average-Degree are Targeted by Pathogens

Here we discuss that certain portions of the protein networks known as “shells” are more heavily targeted by the pathogens. The shells are determined using  $k$ -shell decomposition analysis. This procedure systematically divides the networks into sub-

networks called shells (details on this procedure are in the Materials and Methods section). We show in Figure 1 a strong power-law correlation between the average degree ( $k_{av}$ ) and average number of pathogen effectors per protein ( $\pi_{av}$ ) in each shell for both networks - despite being associated with species from different kingdoms (for humans, power-law regression produces  $\pi_{av} = 0.033 \cdot k_{av}^{0.744}$ ,  $r^2 = 0.788$ ,  $p = 3.039 \cdot 10^{-10}$ , MIC = 0.820; for *Arabidopsis*,  $\pi_{av} = 0.012 \cdot k_{av}^{1.223}$ ,  $r^2 = 0.905$ ,  $p = 9.727 \cdot 10^{-4}$ , MIC = 1.0). For cross-validation, we also measure correlation with the Maximal Information Coefficient [7] (MIC), which does not assume a linear relationship (for details see the Materials and Methods section). Our finding suggests that pathogens seem to target proteins located in the more dense shells of the networks (shells with a higher average degree). Previous attempts to relate network measures with the behavior of the pathogens have provided only weak correlation (e.g. regression analysis correlating degree to number of pathogen interactions in the human protein networks gives  $r^2 = 0.095$  as reported by Navratil et al. - we provide a complete summary of these correlations later in the paper). With the *Arabidopsis*, Mukhtar et al. [1] shows that proteins of degree 50 or greater were often interacted more with the pathogens, but do not show a correlation - most likely because many high degree proteins in that network were not significantly affected by pathogens. This study differs from these previous attempts in that we focus on layers of the networks as opposed to individual nodes. We also note that if, based on certain observable irregularities, we dis-regard a small handful of shells in the human protein network, that the correlation significantly increases. In the human protein network, the average degree monotonically increases with the first 23 shells then becomes irregular. Further, the average number of pathogen interactions in each shell follows

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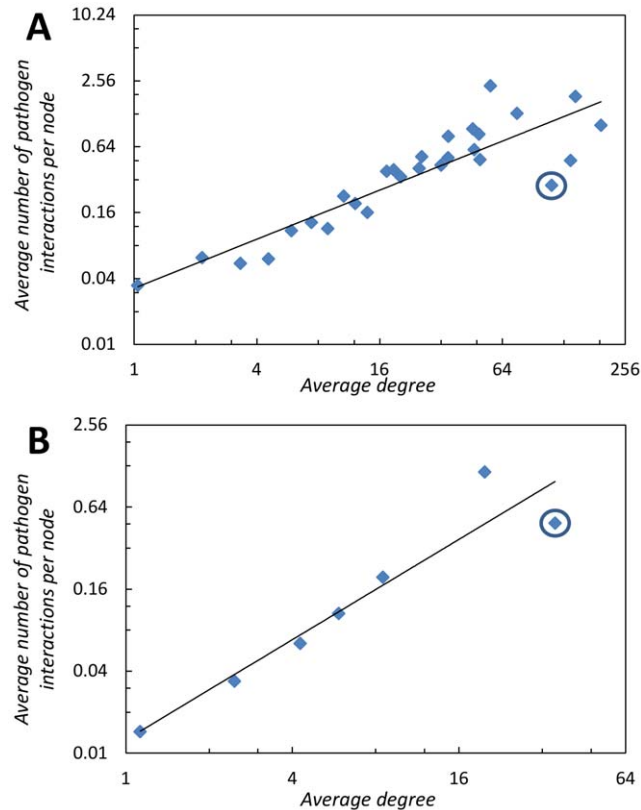
1. REPORT DATE <b>12 SEP 2012</b>	2. REPORT TYPE	3. DATES COVERED <b>00-00-2012 to 00-00-2012</b>	
4. TITLE AND SUBTITLE <b>Similar Pathogen Targets in Arabidopsis thaliana and Homo sapiens Protein Networks</b>		5a. CONTRACT NUMBER	
		5b. GRANT NUMBER	
		5c. PROGRAM ELEMENT NUMBER	
6. AUTHOR(S)		5d. PROJECT NUMBER	
		5e. TASK NUMBER	
		5f. WORK UNIT NUMBER	
7. PERFORMING ORGANIZATION NAME(S) AND ADDRESS(ES) <b>United States Military Academy, J. Kenneth Wickiser Department of Life Science, West Point, NJ, 10996</b>		8. PERFORMING ORGANIZATION REPORT NUMBER	
9. SPONSORING/MONITORING AGENCY NAME(S) AND ADDRESS(ES)		10. SPONSOR/MONITOR'S ACRONYM(S)	
		11. SPONSOR/MONITOR'S REPORT NUMBER(S)	
12. DISTRIBUTION/AVAILABILITY STATEMENT <b>Approved for public release; distribution unlimited</b>			
13. SUPPLEMENTARY NOTES <b>PLoS ONE 7(9): e45154. Published September 21, 2012</b>			
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			18. NUMBER OF PAGES <b>8</b>
			19a. NAME OF RESPONSIBLE PERSON

a very similar pattern - generally increasing during the first 22 shells before becoming irregular (see Figure 2). Although we are unsure why this occurs, we do note that if power-law analysis is performed on the data for the first 23 shells, the correlation significantly increases ( $r^2=0.927$ ,  $p=2.078 \cdot 10^{-13}$ ,  $MIC=0.999$ , the  $r^2$  value when all shells are considered is  $0.788$ ,  $p=3.039 \cdot 10^{-10}$ ,  $MIC=0.820$ ).

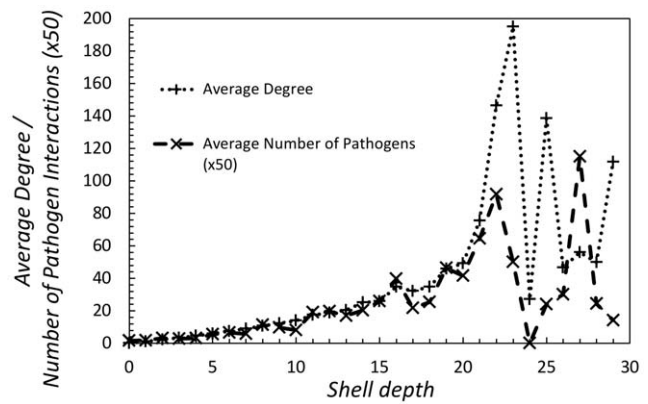
Can we extend the above analysis to identify highly-targeted proteins? Unfortunately, as with degree and betweenness (betweenness is defined in the Materials and Methods section), it appears that the shell number for each node is not correlated with number of pathogen effectors. However, can we extract a rule from the data of the form “if node  $X$  is targeted by at least  $Y$  pathogen interactions then it must have a shell number of at least  $Z$ ”? We looked at the minimum shell number targeted by a certain number of pathogen effectors (or greater) and found that such rules appear to be true for both datasets we examined. Figure 3 illustrates this relationship. We normalized the minimum shell-number, degree and betweenness associated with nodes being targeted by at least a certain number of pathogen interactions. It is noteworthy that the results for the human protein-interaction network, though striking, may actually be understated as the shell number (85) of the core is significantly higher than the next shell (which has a shell number of 34).

**Core Network Proteins Under-Targeted**

The core nodes of the network (the nodes in the inner-most shell) are consistently less attacked by the pathogens than



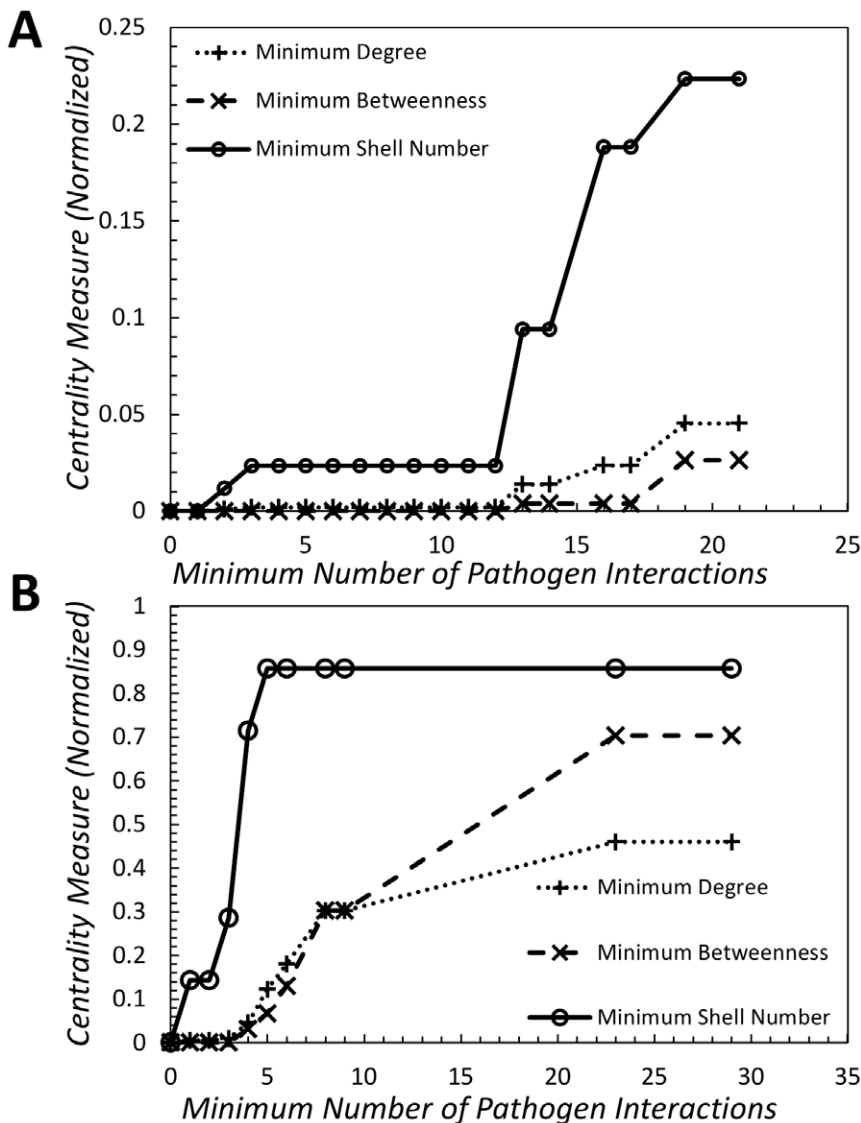
**Figure 1. Average degree ( $k_{av}$ ) vs. average number pathogen interactions ( $\pi_{qv}$ ) per node in a shell (log-log scale) with power-law fits.** The core of each network is circled. (A) Human protein interaction network (B) *Arabidopsis* protein interaction network. doi:10.1371/journal.pone.0045154.g001



**Figure 2. The average degree of each shell in the human protein interaction network increases for the first 23 shells before becoming irregular.** The average number of pathogen interactions for each shell follows a similar pattern. doi:10.1371/journal.pone.0045154.g002

expected. The core nodes (a.k.a. network nucleus), are a relatively small set of densely-connected nodes (a node in the core has many connections to other nodes in the core) that in other networks were shown to be associated with a key function of the network [5] and/or are amplifying the spread of a phenomenon [6]. An example of such a function could be the spread of information. Hence, targeting the core nodes does not seem to be part of the pathogen attack strategy in both humans and *Arabidopsis*. In the *Arabidopsis* network, core nodes are targeted by pathogens about half as expected based on the power-law correlation. For the human, these nodes are targeted only about a quarter as expected (the core nodes are circled in Figure 1). Further, it appears that highly targeted nodes are not found in the core. Of the top 25 (1%) of targeted nodes in the *Arabidopsis* network, only one of them is in the core. Of the top 100 (1%) of targeted nodes in the human network, only two are in the core. In Mukhtar et al. [1] the authors examine nodes with a degree of 50 or greater - a set of 15 nodes referred to as *hub*<sub>50</sub> in the *Arabidopsis* network. Five of these are what those authors consider “highly targeted” and none of them are in the core. Of the remaining 10 nodes in *hub*<sub>50</sub>, six of them are in the core. Membership in the core appears to correlate with high-degree nodes not being targeted.

There exists an optimal virulence - the degree of pathogenicity an infecting microbe has upon its host - that depends upon the fitness of both the host and the infecting entity [8]. The pathogen relies upon the host cellular machinery for replication so it impacts the genetic network involved in the immune response, pathogen infection process, and gene expression architecture to produce pathogen offspring. On the route to achieving optimal virulence, a pathogen may evolve to target the genetic circuits to allow maximum fitness of both itself and the host [9]. While some highly connected nodes of a genetic network prove to be lethal when either knocked down experimentally or perturbed by a pathogen in nature, the data analyzed herein demonstrates a plethora of viruses, bacteria, and eukaryotic pathogens target well-connected, but non-core nodes in both plant and human interactome datasets. It may be that the step-wise evolution of a pathogen involves the sampling of different host protein circuits in an effort to ensure optimum host viability and maximum pathogen replication [10,11]. The targeting of high density, but non-core proteins may reflect an evolved strategic solution pathogens have employed to achieve optimal virulence [12]. The high density of the targeted nodes may accelerate a pathogen’s ability to adapt to selective



**Figure 3. Normalized minimum centrality measure (the centrality measures depicted here are degree, betweenness, and shell number) of nodes targeted by at least a certain number of pathogen interactions.** (A) Human protein interaction network. (B) *Arabidopsis* protein interaction network. Betweenness is defined in the Materials and Methods. doi:10.1371/journal.pone.0045154.g003

pressure by switching to a closely related target or it may simply reflect the highly connected nature of the targeted suite of proteins involved with the control of gene expression and cellular metabolism.

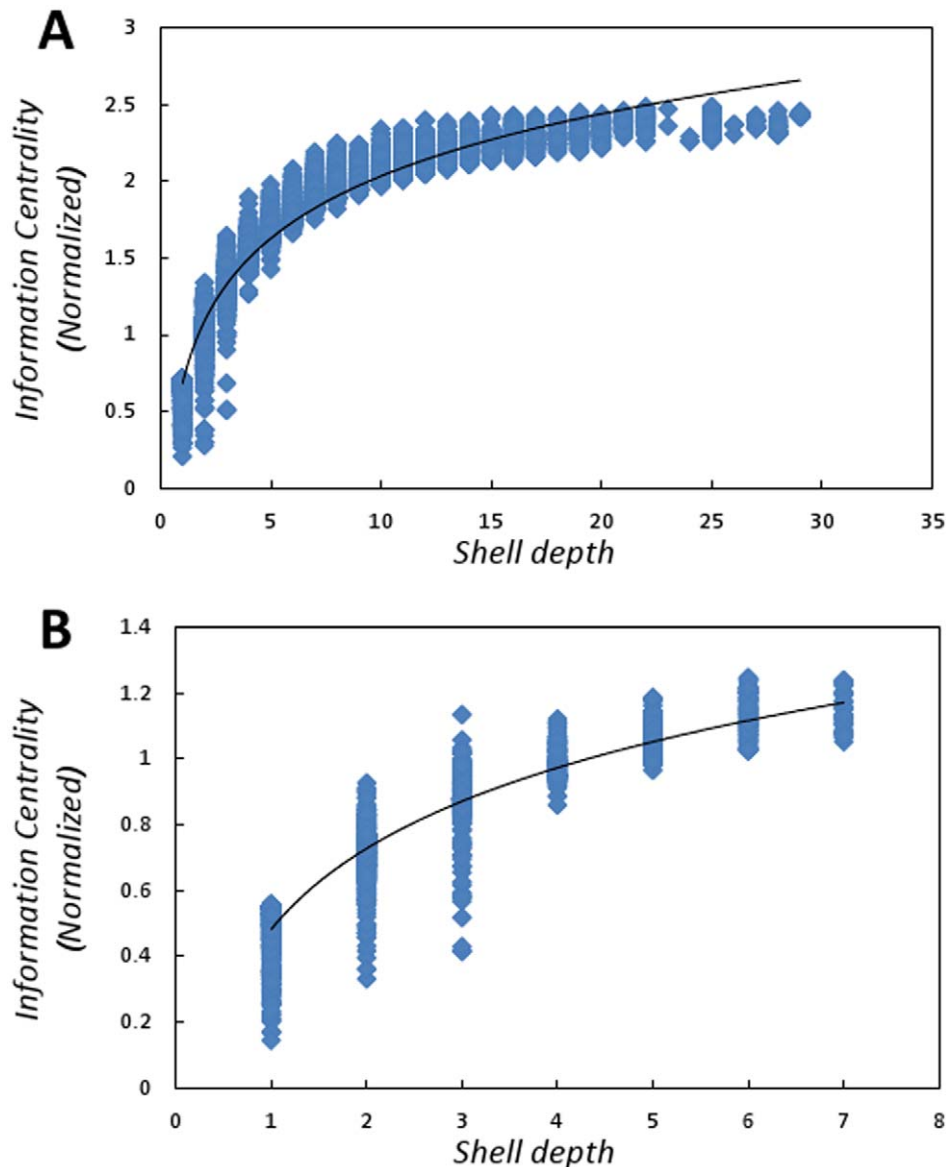
The intra-cellular communication circuits include signals transduction components between organelle such as the nucleus and mitochondria as the cell strives to maintain homeostasis. Many of these communication circuits are involved with host metabolism and are the same proteins co-opted to construct pathogen progeny. We now illustrate how nodes in and near the core can be viewed as superior spreaders of information by examining the information centrality [13–15] ( $C_I$ ) of the proteins in the various shells. Hence, nodes with high information centrality are thought to be excellent spreaders of information. Information centrality is more formally defined in the Materials and Methods section.

In both protein networks explored in this paper, the nodes in and near the core are superior spreaders of information given the

information centrality of the proteins in various shells. We found a strong logarithmic correlation between shell depth ( $\delta$ ) and information centrality in both the human and *Arabidopsis* protein networks (for humans, the relationship is  $\delta = 0.586 \cdot \ln(C_I) + 0.683$ ,  $r^2 = 0.972$ ,  $p = 0.0$ , MIC = 0.999; for *Arabidopsis*, the relationship is  $\delta = 0.354 \cdot \ln(C_I) + 0.482$ ,  $r^2 = 0.897$ ,  $p = 0.0$ , MIC = 0.985, see Figure 4). In general, nodes toward the more inner shells have greater information centrality.

**Identifying Highly-Targeted Proteins in the *Arabidopsis* Network**

Within a given shell of the *Arabidopsis* protein interaction network, the correlation coefficient (based on Pearson’s  $r$ , linear) for betweenness ( $C_B$ ) and number of pathogen interactions per node ( $\pi$ ) monotonically increased with the average degree of a given shell (power law regression fit yields  $r^2 = 0.847$ ,  $p = 0.00327$ , MIC = 1.0.). This proves to be useful information in identifying

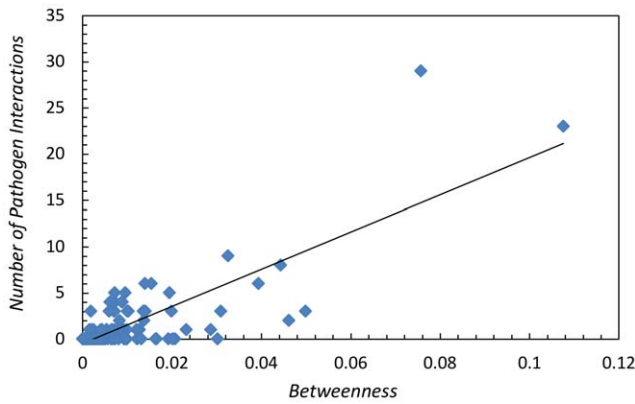


**Figure 4. Shell depth vs. information centrality:** (A) human protein interaction network, (B) *Arabidopsis* protein interaction network. Information centrality is defined in the Materials and Methods. doi:10.1371/journal.pone.0045154.g004

high-targeted nodes as the shell with the highest average degree (shell 6, the last shell before the core, containing 155 nodes) appeared to have a correlation for betweenness-number of pathogen interactions (linear regression fit gives  $\pi = 201.299 \cdot C_B - 0.485$ ,  $r^2 = 0.645$ ,  $p = 2.958 \cdot 10^{-36}$ , MIC = 0.493). This is significantly greater than the linear-fit for the relationship among betweenness-number of pathogen interactions for the entire dataset ( $r^2 = 0.435$ ,  $p = 0.0$ , MIC = 0.144). The relationship for this shell is shown graphically in the Figure 5. As an anecdote, the top 5 attacked proteins in the entire network were all contained within the top 7 high-betweenness proteins of shell 6. We note that similar results described in this paragraph can be derived based on degree-number of pathogen correlations. However, this is most likely a side-effect of the high correlation among degree and betweenness within shell 6 of the *Arabidopsis* protein interaction network (linear regression  $r^2 = 0.849$ ,  $p = 1.024 \cdot 10^{-64}$ , MIC = 0.901).

### Characterizing Attacks on Essential Proteins in the Human Network

For the human network, we also further examined the relationship between essential host factors (EHF's) and the pathogen interactions. We used a list of 1501 EHF's from Navratil et al. [3]. In that work, the authors noted that over 40% of the EHF's were within the local neighborhood (within 1 edge or less distance) from a targeted protein. While this indicated that pathogens target areas of the protein network near EHF's, it may be that the pathogens limit their attack to ensure the survival of the host (i.e. as with the lower-than-expected attacks of the core proteins we noted earlier). To examine this issue, we studied the average and maximum number of EHF proteins that are neighbors of node attacked by a certain number of pathogen effectors. We found that the average percentage of EHF neighbors remained at 0.2 while the maximum decreased as the minimum number of pathogen interactions increased - see Figure 6.



**Figure 5. Betweenness centrality ( $C_B$ ) vs. number of pathogen interactions ( $\pi$ ) for the nodes in shell 6 of the *Arabidopsis* protein interaction network.**  
doi:10.1371/journal.pone.0045154.g005

**Notes on Essential Host Factors in the Human PIN**

We also found some results concerning the relationship between EHF proteins and network structure. In Figure 7, we show that there is a linear relationship between the size of a shell and the number of EHF proteins in that shell (where  $n_j$  ( $n_j^{EHF}$ ) is the number of nodes (EHF nodes) in shell  $j$  the relationship is  $n_j^{EHF} = 0.06843 \cdot n_j + 9.556$ ,  $r^2 = 0.932$ ,  $p = 7.649 \cdot 10^{-18}$ , MIC = 0.792). We also noticed (in Figure 8) that there is a linear relationship between the average degree of proteins in a shell and the average degree of EHF proteins in a shell (the relationship is  $k_{av}^{EHF} = 0.0861 \cdot k_{av}$ ,  $r^2 = 0.956$ ,  $p = 3.322 \cdot 10^{-19}$ , MIC = 0.999).

**Correlation Studies On Node Centrality vs. Number of Pathogen Interactions Per Node (Negative Result)**

We found a negative result on the correlation between node centrality measures and number of pathogen interactions per node. In general, there was little correlation found using linear regression. Similar results were obtained using power-law regression. On the human protein network, the  $r^2$  value associated with

linear regression on degree-pathogen correlation is 0.058 ( $p = 1.298 \cdot 10^{-132}$ , note that Navratil et al. report a slightly higher value - their analysis is most likely based on a power-law correlation) while MIC = 0.0830, for betweenness-pathogen correlation is 0.037 ( $p = 9.412 \cdot 10^{-85}$ ) while MIC = 0.109, and for shell number-pathogen correlation is 0.030 ( $p = 5.970 \cdot 10^{-69}$ ) while MIC = 0.067. On the *Arabidopsis* protein network, the  $r^2$  value associated with linear regression on degree-pathogen correlation is 0.314 ( $p = 8.274 \cdot 10^{-220}$ ) while MIC = 0.098, for betweenness-pathogen correlation is 0.435 ( $p = 0.0$ ) while MIC = 0.144, and for shell number-pathogen correlation is 0.050 ( $p = 2.889 \cdot 10^{-31}$ ) while MIC = 0.050.

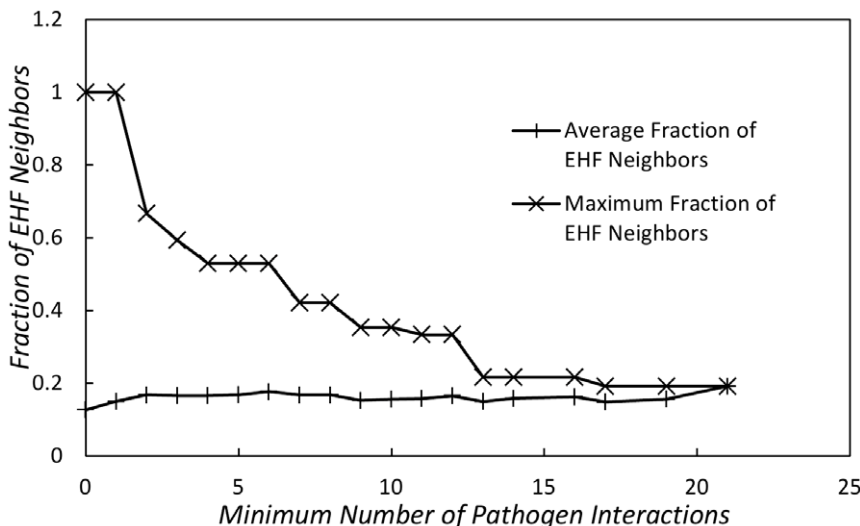
**Discussion**

We believe these results are exciting as they show that pathogen effectors seem to attack protein networks of entirely different organisms in very similar ways. Further, through  $k$ -shell decomposition and regression analysis, we are able to identify high-risk shells for attack. We are currently looking to extend this work by creating software tools to extract highly-relevant patterns of pathogens attacks. Other future work of interest would be to explore pathogen relationships with host protein networks for other organisms.

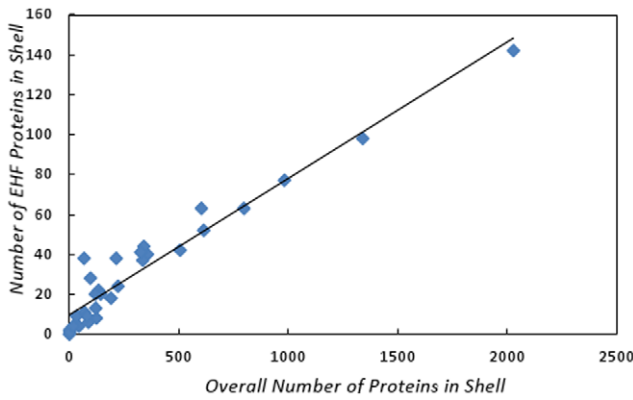
**Materials and Methods**

The degree of a host protein node in the networks considered is the number of other host proteins interacting with it. The number of interacting pathogens for a given protein node (denoted by  $\pi$  in this paper) is the total number of proteins in all pathogen protein networks (considered for that host species) which interact with that protein node.

The  $k$ -shell decomposition method can be described as follows. At the first iteration, all unconnected nodes are removed and are considered to be in shell 0 (note that we did not consider this shell in our analysis – as it has been observed that unconnected proteins were largely unaffected by pathogens [1,3]). Then all nodes connected to the graph by one edge are removed, they are in shell 1. Upon their removal, there may be other nodes connected to the



**Figure 6. Minimum number of pathogen interactions for a given node vs. fraction of EHF neighbors for that node.**  
doi:10.1371/journal.pone.0045154.g006

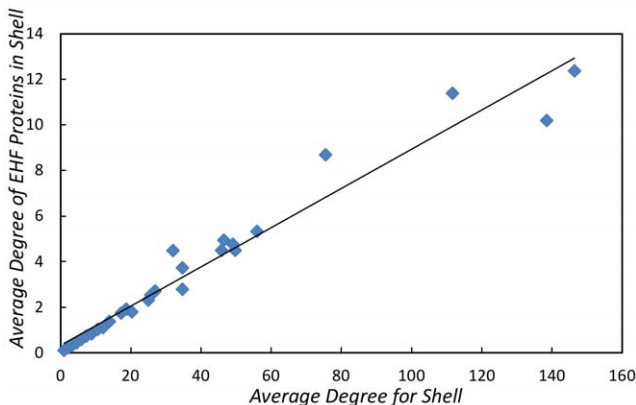


**Figure 7. Total number of proteins vs. number of EHF proteins in a shell.**  
doi:10.1371/journal.pone.0045154.g007

graph by one edge or less - they too are removed and are also considered in shell number 1 (we then continue removing nodes from the graph for shell 1 until there are no more nodes connected by just one edge or less). The process repeats for nodes connected to the graph with only two edges (they are in shell 2) and so on until nodes are removed. The nodes in the highest *k*-shell are known as the core. We define the term “shell depth” as the number representing the order in which the shell is determined - for example if shell number 1 is followed by shell number 3, then the depth of shell 3 would be 2. We define “shell size” simply as the number of nodes in a particular shell.

Betweenness centrality, [16], often simply called “betweenness,” is defined as follows. Let  $\sigma_{st}$  be the number of shortest paths between nodes *s* and *t* and  $\sigma_{st}(v)$  be the number of shortest paths between *s* and *t* containing node *v*. Betweenness centrality for node *v* is then  $\sum_{s \neq v \neq t} \frac{\sigma_{st}(v)}{\sigma_{st}}$ . Intuitively, nodes of high-betweenness can be thought of as “bottlenecks” as their removal often results in an increase in shortest path length between node pairs in the network. The NetworkX package used in our analysis implements the algorithm of [17] to compute this measure.

Information centrality [13], studies all different paths between two nodes in a network. In [13], the information value between two nodes is related to the inverse length of the different paths



**Figure 8. Average node degree vs. average EHF node degree in a shell.**  
doi:10.1371/journal.pone.0045154.g008

between them. For node pair (*i,j*), they define a square matrix  $D^{(ij)}$  where the number of rows in the matrix is equal to the total number of paths between *i* and *j*. The *r,s* component of the matrix,  $D_{rs}^{(ij)}$ , is equal to the number of shared links between the path specified at row *r* and row *s*. Hence, for undirected networks (as the protein networks used in this paper) the matrix is symmetric. To define the information between *i* and *j*, denoted  $I_{ij}$ , the authors sum the components of the inverse of  $D^{(ij)}$ . Based on this calculation, for a network of *n* nodes, the information centrality of a given node *i* (denoted  $C_I(i)$ ) is defined as follows.

$$C_I(i) = \frac{n}{\sum_j 1/I_{ij}} \tag{1}$$

Hence, the information centrality of node *i* is the harmonic mean of the information associated with the paths from *i* to all other nodes in the network.

The *Arabidopsis* protein network of Mukhtar et al. [1] consisted of 5664 interactions among 2661 proteins and 306 interactions with pathogens. The maximum degree was 222 and excluding unconnected nodes the network was decomposed into 7 shells. The human protein interaction network of Navratil et al. [3] consisted of 65,533 interactions among 10,057 proteins. There were 1911 interactions with pathogens. The maximum degree was 1012. Decomposed, the human network had 29 shells.

All network analysis was performed using NetworkX (<http://networkx.lanl.gov/>) and all statistics were performed using SciPy (<http://www.scipy.org/>).

In the power-law regression analysis of the human network, shell 25 (consisting of three nodes with degrees 25, 26, and 30) was omitted from the power-law analysis as it was not affected by any virus. For the high-quality human network, shell 21 (consisting of one node with a degree of 45) was omitted for the same reason. No shells were omitted in analysis done with the Maximum Information Coefficient.

For all linear regression analysis, the *p*-value (2-tailed unless specified otherwise) refers to the probability that the slope is zero (roughly the probability that an uncorrelated system produces datasets that have an *r* value greater than or equal to one reported). For power regression, this refers to the probability that the scaling exponent is zero.

In addition to the normal regression analysis, we also computed the Maximal Information Coefficient (MIC) [7] that measures the correlation of two variables without assuming a linear relationship. This coefficient is a number in the interval [0,1] that monotonically increases with correlation. We used the the MINE software available from <http://exploredata.net> to compute this quantity. Note that if we compared two variables, the MIC was computed on the two original variables (i.e. not the logarithm).

For the results on information centrality, all of our results are on the greatest connected components of either graph. This is because information centrality [13–15] is only defined for strongly connected graphs.

For our EHF results, the set of “EHF neighbors” includes all the neighbor of a given node and itself. Hence, we assume a self-loop. For instance, an EHF protein not adjacent to any other EHF protein has one “neighbor” – itself.

**Acknowledgments**

P.S. would like to thank Paul Maxwell and Patrick Roos for their help on an earlier version.

## Author Contributions

Conceived and designed the experiments: PS JKW. Performed the experiments: PS. Analyzed the data: PS JKW. Contributed reagents/materials/analysis tools: PS JKW. Wrote the paper: PS JKW.

## References

- Mukhtar MS, Carvunis AR, Dreze M, Epple P, Steinbrenner J, et al. (2011) Independently Evolved Virulence Effectors Converge onto Hubs in a Plant Immune System Network. *Science* 333: 596–601.
- Consortium AIM (2011) Evidence for Network Evolution in an Arabidopsis Interactome Map. *Science* 333: 601–607.
- Navratil V, de Chasse B, Combe CRR, Lotteau V (2011) When the human viral infectome and disease networks collide: towards a systems biology platform for the aetiology of human diseases. *BMC systems biology* 5: 13+.
- Seidman S (1983) Network structure and minimum degree. *Social Networks* 5: 269–287.
- Carmi S, Havlin S, Kirkpatrick S, Shavitt Y, Shir E (2007) From the Cover: A model of Internet topology using k-shell decomposition. *PNAS* 104: 11150–11154.
- Kitsak M, Gallos LK, Havlin S, Liljeros F, Muchnik L, et al. (2010) Identification of influential spreaders in complex networks. *Nat Phys* 6: 888–893.
- Reshef D, Reshef Y, Finucane H, Grossman S, McVean G, et al. (2011) Detecting novel associations in large data sets. *Science* 334.
- Jensen K, Little TJ, Skorpning A, Ebert D (2006) Empirical support for optimal virulence in a castrating parasite. *PLoS Biology* 4.
- Berenos C, Schmid-Hempel P, Wegner K (2011) Experimental coevolution leads to a decrease in parasite-induced host mortality. *Journal of Evolutionary Biology* 24.
- Smith J (2007) A gene's-eye view of symbiont transmission. *American Naturalist* 170: 542–550.
- Kover P, Clay K (1998) Trade-off between virulence and vertical transmission and the maintenance of a virulent plant pathogen. *American Naturalist* 152: 165.
- Best A, White A, Boots M (2009) The implications of coevolutionary dynamics to host-parasite interactions. *American Naturalist* 173: 779.
- Stephenson K, Zelen M (1989) Rethinking centrality: Methods and examples. *Social Networks* 11: 1–37.
- Noh JD, Rieger H (2004) Random walks on complex networks. *Physical Review Letters* 92: 118701.
- Brandes U, Fleischer D (2005) Centrality measures based on current flow. In: *STACS*. pp. 533–544.
- Freeman LC (1977) A set of measures of centrality based on betweenness. *Sociometry* 40: pp. 35–41.
- Brandes U (2001) A faster algorithm for betweenness centrality. *Journal of Mathematical Sociology* 25.