



**AFRL-RW-EG-TP-2012-009**

# **Mesoscale Simulations of Particle Reinforced Epoxy-Based Composites**

**Bradley W. White<sup>4</sup>**  
**H. Keo Springer<sup>2</sup>**  
**Jennifer L. Jordan<sup>1</sup>**  
**Jonathan E. Spowart<sup>3</sup>**  
**Naresh N. Thadhani<sup>4</sup>**

<sup>1</sup>Air Force Research Laboratory, AFRL/RW, Eglin AFB, FL 32542

<sup>2</sup>Lawrence Livermore National Laboratory, 7000 East Avenue, Livermore, CA 94550

<sup>3</sup>Air Force Research Laboratory, AFRL/RXBC, Wright-Patterson AFB, OH 45433

<sup>4</sup>School of Materials Science and Engineering, Georgia Tech, 771 Ferst Drive NW, Atlanta, GA 30332

**25 July 2012**

**Interim Report**

This paper was presented at the AIP Conference, July 2011. One or more of the authors is a U.S. Government employee working within the scope of their position; therefore, the U.S. Government is joint owner of the work and has the right to copy, distribute, and use the work. Any other form of use is subject to copyright restrictions.

This work has been submitted for publication in the interest of the scientific and technical exchange. Publication of this report does not constitute approval or disapproval of the ideas or findings.

**Distribution A: Approved for public release; distribution unlimited.  
Approval Confirmation 96 ABW/PA # 96ABW-2011-0363, dated  
August 2, 2011**

**AIR FORCE RESEARCH LABORATORY, MUNITIONS DIRECTORATE**

**Air Force Materiel Command ■ United States Air Force ■ Eglin Air Force Base**



## NOTICE AND SIGNATURE PAGE

Using Government drawings, specifications, or other data included in this document for any purpose other than Government procurement does not in any way obligate the U.S. Government. The fact that the Government formulated or supplied the drawings, specifications, or other data does not license the holder or any other person or corporation; or convey any rights or permission to manufacture, use, or sell any patented invention that may relate to them.

Qualified requestors may obtain copies of this report from the Defense Technical Information Center (DTIC) (<http://www.dtic.mil>).

AFRL-RW-EG-TP-2012-007 HAS BEEN REVIEWED AND IS APPROVED FOR PUBLICATION IN ACCORDANCE WITH ASSIGNED DISTRIBUTION STATEMENT.

FOR THE DIRECTOR:

//ORIGINAL SIGNED//

HOWARD G. WHITE, PhD  
Technical Advisor  
Ordnance Division

//ORIGINAL SIGNED//

CHRISTOPHER L. VARNER  
Branch Chief  
Energetic Materials Branch

//ORIGINAL SIGNED//

JENNIFER L. JORDAN, PhD  
Project Manager  
Energetic Materials Branch

This report is published in the interest of scientific and technical information exchange, and its publication does not constitute the Government's approval or disapproval of its ideas or findings.

This page intentionally left blank

# REPORT DOCUMENTATION PAGE

*Form Approved*  
OMB No. 0704-0188

Public reporting burden for this collection of information is estimated to average 1 hour per response, including the time for reviewing instructions, searching existing data sources, gathering and maintaining the data needed, and completing and reviewing this collection of information. Send comments regarding this burden estimate or any other aspect of this collection of information, including suggestions for reducing this burden to Department of Defense, Washington Headquarters Services, Directorate for Information Operations and Reports (0704-0188), 1215 Jefferson Davis Highway, Suite 1204, Arlington, VA 22202-4302. Respondents should be aware that notwithstanding any other provision of law, no person shall be subject to any penalty for failing to comply with a collection of information if it does not display a currently valid OMB control number. **PLEASE DO NOT RETURN YOUR FORM TO THE ABOVE ADDRESS.**

<b>1. REPORT DATE (DD-MM-YYYY)</b> 25 July 2012		<b>2. REPORT TYPE</b> Interim		<b>3. DATES COVERED (From - To)</b> July 2009 – July 2011	
<b>4. TITLE AND SUBTITLE</b>  Mesoscale Simulations of Particle Reinforced Epoxy-Based Composites				<b>5a. CONTRACT NUMBER</b>	
				<b>5b. GRANT NUMBER</b>	
				<b>5c. PROGRAM ELEMENT NUMBER</b> 62102F	
<b>6. AUTHOR(S)</b>  Bradley W. White <sup>4</sup> , H. Keo Springer <sup>2</sup> , Jennifer L. Jordan <sup>1</sup> , Jonathan E. Spowart <sup>3</sup> , Naresh N. Thadhani <sup>4</sup>				<b>5d. PROJECT NUMBER</b> 4347	
				<b>5e. TASK NUMBER</b> 95	
				<b>5f. WORK UNIT NUMBER</b> 05	
<b>7. PERFORMING ORGANIZATION NAME(S) AND ADDRESS(ES)</b> <sup>1</sup> Air Force Research Laboratory, AFRL/RW, Eglin AFB, FL 32542 <sup>2</sup> Lawrence Livermore National Lab, 7000 East Avenue, Livermore, CA 94550 <sup>3</sup> Air Force Research Laboratory, AFRL/RXBC, Wright-Patterson AFB, OH 45433 <sup>4</sup> School of Materials Science and Engineering, Georgia Tech, 771 Ferst Drive NW, Atlanta, GA 30332				<b>8. PERFORMING ORGANIZATION REPORT NUMBER</b>  AFRL-RW-EG-TP-2012-009	
<b>9. SPONSORING / MONITORING AGENCY NAME(S) AND ADDRESS(ES)</b>  Air Force Research Laboratory, Munitions Directorate Ordnance Division Energetic Materials Branch (AFRL/RWME) Eglin AFB FL 32542-5910 Technical Advisor: Dr. Jennifer L. Jordan				<b>10. SPONSOR/MONITOR'S ACRONYM(S)</b> AFRL-RW-EG	
<b>12. DISTRIBUTION / AVAILABILITY STATEMENT</b>  Distribution A: Approved for public release; distribution unlimited. Approval Confirmation 96 ABW/PA # 96ABW-2011-0363, Dated, August 2, 2011				<b>11. SPONSOR/MONITOR'S REPORT NUMBER(S)</b> AFRL-RW-EG-TP-2012-009	
<b>13. SUPPLEMENTARY NOTES</b>  DISTRIBUTION STATEMENT INDICATING AUTHORIZED ACCESS IS ON THE COVER PAGE AND BLOCK 12 OF THIS FORM.					
<b>14. ABSTRACT</b>  Polymer matrix composites reinforced with metal powders have complex microstructures that vary greatly from differences in particle size, morphology, loading fractions, etc. The effects of the underlying microstructure on the mechanical and wave propagation behavior of these composites during dynamic loading conditions are not well understood. To better understand these effects, epoxy (Epon826/DEA) reinforced with different particle sizes of Al and loading fractions of Al and Ni were prepared by casting. Microstructures from the composites were then used in 2D plane strain mesoscale simulations. The effect of varying velocity loading conditions on the wave velocity was then examined to determine the Us-Up and particle deformation response as a function of composite configuration.					
<b>15. SUBJECT TERMS</b> Split Hopkinson pressure bar, pressure dependence, high strain rate, poly(vinyl chloride)					
<b>16. SECURITY CLASSIFICATION OF:</b>			<b>17. LIMITATION OF ABSTRACT</b>  UL	<b>18. NUMBER OF PAGES</b>  11	<b>19a. NAME OF RESPONSIBLE PERSON</b> Jennifer L. Jordan
<b>a. REPORT</b>  UNCLASSIFIED	<b>b. ABSTRACT</b>  UNCLASSIFIED	<b>c. THIS PAGE</b>  UNCLASSIFIED			<b>19b. TELEPHONE NUMBER (include area code)</b> 850-882-8992

This page intentionally left blank

# MESOSCALE SIMULATIONS OF PARTICLE REINFORCED EPOXY-BASED COMPOSITES

Bradley W. White\*, H. Keo Springer<sup>†</sup>, Jennifer L. Jordan\*\*, Jonathan E. Spowart<sup>‡</sup> and Naresh N. Thadhani\*

\*School of Materials Science and Engineering, Georgia Tech, 771 Ferst Drive NW, Atlanta, GA 30332

<sup>†</sup>Lawrence Livermore National Laboratory, 7000 East Ave, Livermore, CA 94550

\*\*AFRL/RWME, 2306 Perimeter Road, Eglin AFB, FL 32542

<sup>‡</sup>AFRL/RXBC, Wright-Patterson AFB, OH 45433

**Abstract.** Polymer matrix composites reinforced with metal powders have complex microstructures that vary greatly from differences in particle size, morphology, loading fractions, etc. The effects of the underlying microstructure on the mechanical and wave propagation behavior of these composites during dynamic loading conditions are not well understood. To better understand these effects, epoxy (Epon826/DEA) reinforced with different particle sizes of Al and loading fractions of Al and Ni were prepared by casting. Microstructures from the composites were then used in 2D plane strain mesoscale simulations. The effect of varying velocity loading conditions on the wave velocity was then examined to determine the Us-Up and particle deformation response as a function of composite configuration.

**Keywords:** Particulate Composites, Shock, Mesoscale Simulations

**PACS:** 62.50.Ef, 81.05.Qk, 81.70.Bt

## INTRODUCTION

Particle reinforced polymer composites such as Al/Fe<sub>2</sub>O<sub>3</sub>/Epoxy [1] and Al/W/PTFE [2] are increasingly being studied for use as structural energetic materials designed to combine mechanical strength with reactive property characteristics from multiple materials into a single system designed to be inert under static loads and react and release energy under dynamic impact conditions [2, 3].

Factors such as particle size, morphology, and volume fraction are known to affect the mechanical behavior of particle reinforced composites. In a study conducted on nano-Al particle reinforced polymer composites [4], reactions were observed to occur at impact velocities < 150 m/s and were dependent on the volume fraction of the nano-Al. In computational studies on Ni/Al particulate composites [5] the effects of particle morphology on reaction mechanisms were investigated. They found mixtures containing

Ni-flake particles vs. spherical had significant flattening of the Al particles and opened up more surface area to come into contact with the Ni. One major difference between these granular composites and more homogeneous polymer matrix composites is that voids are largely not present. As such the mechanisms of mechanical mixing that lead to reactions under shock wave propagation for polymer-based composites are potentially different and need to be investigated.

In this work the interaction effects of particle size and loading fractions of Ni and Al on the dynamic mechanical behavior of epoxy cast particulate composites under shock loading conditions are examined. Computational efforts are specifically used to examine the shock wave propagation at the mesoscale to better understand the deformation of the composite constituents.

**TABLE 1.** Composite configurations used to obtain and import 2D microstructures in ALE3D.

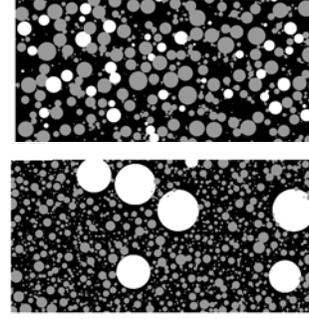
Material	Al Particle Size ( $\mu\text{m}$ )	Al Vol. Frac. (%)	Ni Vol. Frac. (%)
EAN-1	52	40	10
EAN-2	5	40	10
EAN-3	5	20	10
EA-1	52	40	0
EA-2	52	20	0

## MICROSTRUCTURE GENERATION

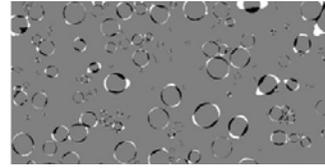
Due to their well known properties, Ni and Al were chosen as reinforcing particles in an epoxy matrix. The average Al particle size was varied between 5 and 52  $\mu\text{m}$ , the volume fraction of Al between 0.20 and 0.40, and the volume fraction of Ni (47  $\mu\text{m}$ ) from 0.00 to 0.10 (see Tab. 1). Representative microstructure images from samples were converted into shape files used in 2D plane-strain simulations in ALE3D. While simulations implementing the 'real' microstructures would be ideal, in order to have a greater control over the mesh resolution a MATLAB script converted the real microstructure into an idealized one with each particle defined as a sphere. This retained the volume fraction to within 1% of the original microstructure and kept the same spatial distribution of the particles. Two idealized microstructures are shown in Fig. 1 for materials EAN-1 and EAN-2 and an overlay of an idealized microstructure on top the original microstructure in Fig. 2 for composite EA-2. A mesh resolution study determined an element size of 2.0 and 0.5  $\mu\text{m}$  in each direction was sufficient to capture an accurate response for composites containing the large and small Al particles respectively.

## SIMULATION SETUP

The microstructure simulation domain was chosen to contain at least the homogeneous length scale of the microstructure in each direction and have an aspect ratio of 2:1 (w:h). This amounted to 1000 and 250  $\mu\text{m}$  in the horizontal direction for composites containing larger and smaller Al particles respectively. Along the top and bottom sides of the domain a symmetry plane was placed and along the right-hand side a



**FIGURE 1.** Idealized microstructures for EAN-1 (top) and EAN-2 (bot). Ni shown as white particles, and Al gray.



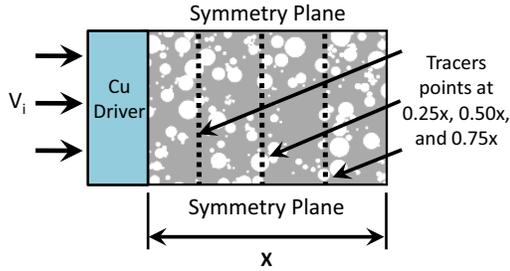
**FIGURE 2.** Overlay of an idealized microstructure on top of the original microstructure. The black and white regions highlight differences in particle shapes.

free surface boundary condition. To create a shock wave, a Cu driver impacted the domain at velocities between 400 and 1200 m/s to produce different shock ( $U_s$ ) and particle ( $U_p$ ) speeds. Tracer points were placed along the vertical direction at horizontal distances of .25, .50, and .75 times the domain width to track pressure and stress. See Fig. 3 for a schematic of the boundary conditions.

For Al and Ni the equation of state and strength models implemented were the Mie-Gruneisen and Steinberg-Guinan models respectively with material default parameters set for both Al and Ni. For epoxy a Mie-Gruneisen EOS was used with  $\gamma_0 = .763$ ,  $C_0 = 2367$  m/s, and  $S = 1.55$ . The constitutive behavior of epoxy was defined using a tabular rate hardening model where the flow stress is a function of the equivalent plastic strain  $\bar{\epsilon}_p$  and a power law strain rate dependence through the following equation:

$$Y(\bar{\epsilon}_p, \dot{\bar{\epsilon}}_p) = Y(\bar{\epsilon}_p) [a + b\dot{\bar{\epsilon}}_p]^m \quad (1)$$

Here,  $\dot{\bar{\epsilon}}_p$  is the equivalent plastic strain rate,  $a$  and  $b$  hardening model material constants and  $m$  the power law strain rate parameter. Using data from [6]

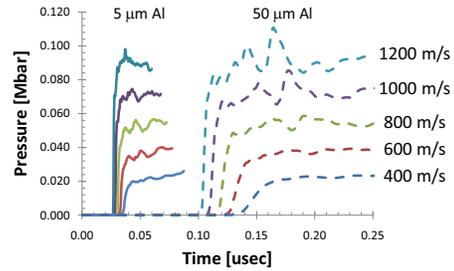


**FIGURE 3.** Schematic of the boundary and loading conditions used for the 2D plane strain simulations.

this model was applied to the stress-strain curves from strain rates of 134 to  $1.4 \times 10^4 \text{ s}^{-1}$ . By using a strain rate of  $3.9 \times 10^3 \text{ s}^{-1}$  as a reference curve a set of values for the parameters were found by minimizing the difference in the peak stress between the experiments and model curves. The values for  $a$ ,  $b$ , and  $m$  were determined to be 0.085, 249.0, and 0.14 respectively.

### EQUILIBRATION OF PRESSURE

From tracer data the pressure was monitored for the entire duration of the shock wave propagation. In comparing the average shock pressures between EAN-1 with EAN-2 there was little difference in the pressures achieved for each impact velocity (see Fig. 4). However, the variations in pressure were greater for composite EAN-1. This is contrary to what was expected since the Ni and Al particles are closer in size for this material and the pressures are averaged over a much larger vertical distance,  $500 \mu\text{m}$  as opposed to  $125 \mu\text{m}$  for composite EAN-2. This may be due to more homogeneous distribution of the Al particles when smaller particles are used while holding the volume fraction constant. When comparing the pressure differences between EA-1 and EA-2 there was a decrease in the pressure as the volume fraction of Al decreased. The pressure was 18% larger for the composite EA-1. This was expected since pressure is related to density and there was a marked drop in density as the volume fraction of Al decreased.



**FIGURE 4.** Pressure traces for EAN-2 (left) and EAN-1 (right) at the positions 125 and  $500 \mu\text{m}$  respectively.

**TABLE 2.** Us-Up Hugoniot parameters.

Material	S	$C_0$ [m/s]	Exp. $C_0$ [m/s]
EAN-1	1.590	2749	2374
EAN-2	1.385	2916	2357
EAN-3	1.708	2990	2079
EA-1	1.478	2968	2475
EA-2	1.417	2822	2280

### US-UP RELATIONSHIPS

By determining the time at which the pressure was  $0.20 \times$  the steady state pressure an average shock velocity was calculated from the distances between tracers. The results of the shock speed calculations were plotted for each composite and velocity with a linear line fit to the data. From these fits, values for  $S$  and  $C_0$  were determined using Eqn. 2 that relates  $U_S$  with  $U_P$ , and the bulk sound speed  $C_0$ .

$$U_S = S U_P + C_0 \quad (2)$$

The values for  $S$  and  $C_0$  are tabulated in Tab. 2 along with  $C_0$  experimentally determined from ultrasonic sound speed measurements. Despite shifts towards higher shock velocities as the volume fraction of particles increased the composite shock velocities, other than EAN-3, had shock velocities that fell within a 200m/s range with only slight differences in the slopes and no clear influence of particle size or the presence of Ni on the  $U_S$ - $U_P$  relationships. This may indicate the contiguous epoxy matrix phase has a dominant role on the shock propagation.

$C_0$  determined from ultrasonic methods are noticeably lower. This is attributed to the assumption of perfect bonding between the constituents since no in-

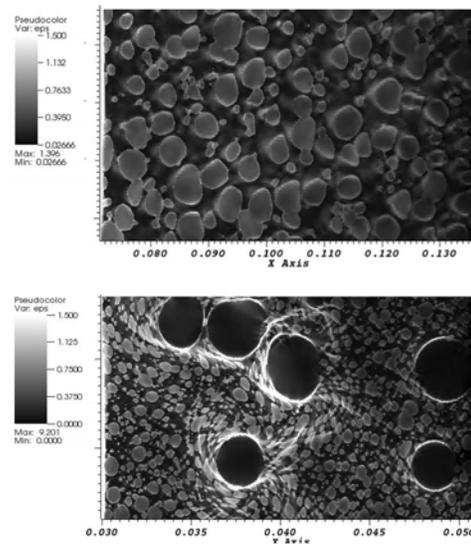
interfaces or bond strengths were defined in the simulations. The simulations also have no defects such as microcracks or pores present that would affect the bulk sound speed of the composite.

## PARTICLE DEFORMATION

To better understand the mechanisms involved with the mixing of constituents that can lead to a reaction the stresses and strains were monitored as the shock wave propagated through the microstructure domains. For composite EA-1 the stresses of the epoxy and Al particles were found to equilibrate quickly within each phase behind the shock front with no large variations. In all cases the epoxy carried more load than Al and in cases where the composites contained Ni most of the load was carried by Ni. This was an indication that the epoxy can be used to impart more strain into softer phases such as Al.

In the following plots the strains are shown for EA-1 and EAN-2 (see Fig. 5) at the completion of the simulations in which the shock front reaches the free surface for an impact velocity of 800 m/s. For the materials without Ni, the regions with the most plastic strains were located at the Al/epoxy interfaces. The Al appeared to have slight elongation perpendicular to the shock wave propagation direction (towards the right).

For composites containing Ni particles the deformation behavior of Al was drastically different. In regions surrounding Ni extreme strain values ( $> 400\%$ ) were observed at the Ni/Epoxy or Ni/Al interfaces. Al deformed to much larger extents than in composites without Ni and deformed to match the contours of the Ni particles which strained very little. Ni in these types of composites act as rigid anvils that enable much larger strains to be produced in the other less stiff phases. Additionally enhanced 'fluid-like' flow of epoxy and Al was observed to occur between and around the Ni particles. This behavior may act as a primary source of mixing that leads to reactions in epoxy-based composites. More enhanced flow and deformation of Al also occurred in composites with smaller Al particles. This may be due a finite strain field radius produced by the Ni particles. In Fig. 5 the large strains in Al are within approximately one Ni particle diameters. In composites with the larger Al the strain fields are on average only extend up to



**FIGURE 5.** Plastic strain plots for EA-1 (top) and EAN-2 (bottom) for an impact velocity of 800 m/s.

a radius equivalent to one Al particle diameter.

## ACKNOWLEDGMENTS

Funding was provided by the U.S. Air Force Research Labs, Eglin AFB under contract F08630-03-C-0001.

## REFERENCES

1. Ferranti, L., Jordan, J., Dick, R., and Thadhani, N., *Shock Compression of Condensed Matter*, pp. 123–126 (2007).
2. Cai, J., Walley, S., Hunt, R., Proud, W., Nesterenko, V., and Meyers, M., *Materials Science and Engineering A*, **472**, 308–315 (2008).
3. Ames, R. G., *Materials Research Society Symposium Proceedings*, **896**, 123–132 (2006).
4. Crouse, C. A., and Spowart, J. E., *Manuscript in Preparation, Wright-Patterson AFB*.
5. Eakins, D. E., *Role of Heterogeneity in the Chemical and Mechanical Shock-Response of Nickel and Aluminum Powder Mixtures*, Ph.D. thesis, Georgia Institute of Technology (2007).
6. Jordan, J. L., Foley, J. R., and Siviour, C. R., *Mech Time-Depend Mater*, **12**, 249–272 (2008).

DISTRIBUTION LIST  
AFRL-RW-EG-TP-2012-009

\*Defense Technical Info Center  
8725 John J. Kingman Rd Ste 0944  
Fort Belvoir VA 22060-6218

AFRL/RWME (6)  
AFRL/RWOC-1 (STINFO Office)