ATOM CHIPS ON DIRECT BONDED COPPER SUBSTRATES (POSTPRINT)

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Atom chips on direct bonded copper substrates

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We present the use of direct bonded copper (DBC) for the straightforward fabrication of high power atom chips. Atom chips using DBC have several benefits: excellent copper/substrate adhesion, high purity, thick (>100 μ m) copper layers, high substrate thermal conductivity, high aspect ratio wires, the potential for rapid (<8 h) fabrication, and three-dimensional atom chip structures. Two mask options for DBC atom chip fabrication are presented, as well as two methods for etching wire patterns into the copper layer. A test chip, able to support 100 A of current for 2 s without failing, is used to determine the thermal impedance of the DBC. An assembly using two DBC atom chips is used to magnetically trap laser cooled ⁸⁷Rb atoms. The wire aspect ratio that optimizes the magnetic field gradient as a function of power dissipation is determined to be 0.84:1 (height:width). © 2011 American Institute of Physics. [doi:10.1063/1.3529434]

Atom chips have been used in many cold atomic physics experiments, including magneto-optical traps,¹ magnetic traps,^{1,2} waveguides,^{3,4} transports,^{5,6} Bose–Einstein condensates,⁷ coherent and incoherent beam splitters,^{8–10} and have been integrated with optical elements.^{11–13} Using atom chips for cold neutral atom physics has two main advantages. First, by manipulating atoms 1–500 μ m from the chip wires, high magnetic field gradients can be generated at low power dissipation (<10 W). Second, by using well established lithographic fabrication techniques, atom chip wires can be precisely placed to generate well defined magnetic fields.

For many applications, e.g., atom interferometry using light pulses, working distances of several hundred microns are common. As shown in the Appendix, power dissipation of a magnetic trap is minimized when the working distance from the top surface of a rectangular wire is $z_0 = 0.7h$ and when the aspect ratio is $h/w = \alpha = 0.8$, where *h* is the thickness and *w* is the width of the wire. Realization of thick $h \gtrsim 100 \,\mu$ m high quality metallizations with standard lithographic techniques has proven to be technologically challenging, time consuming, and very expensive. For atom chip based magnetic traps that require working distances $z_0 \gtrsim 100 \,\mu$ m, we present the use of direct bonded copper (DBC) substrates for atom chip fabrication.

Direct bonded copper is the direct joining of a thin sheet of pure copper to a ceramic substrate¹⁴ and is commonly used in power electronics due to its high current handling and heat dissipation properties. Using DBC for atom chips addresses several atom chip fabrication requirements including power dissipation, ease of fabrication, thick metallizations, and excellent wire adhesion. The power dissipation of DBC atom chips is reduced for two reasons. First, thick, pure copper layers are readily available for DBC substrates with a resistivity equal to bulk copper. Second, the ability to easily produce thick atom chip wires that have a reduced net resistance. Another benefit of using DBC for atom chips is the potential for rapid in-house fabrication with minimal equipment. We have produced moderate quality atom chips in less than 8 h, and high quality wires in approximately 1 week with most of the time being taken by mask design and printing. By using DBC it is straightforward to fabricate various rectangular wire cross sections or aspect ratios because of the availability of a thick copper layer. Wires with aspect ratio $\alpha \gtrsim 2$ can be fabricated by wet etching, and it may be possible to realize high aspect ratio wires, $\alpha \sim 20$, using ablative laser micromachining.¹⁵

To date, most atom chips have been fabricated using a Damscene process, where the wire height and aspect ratio are determined by the photoresist thickness and the metal deposition (electroplating or evaporation) with typical wire heights on the order of $10 \,\mu$ m.^{16–22} Thick lithographic wires have been fabricated using thick photoresists³ or by depositing metal in channels formed in the substrate (e.g., deep reactive ion etching in silicon) but the difficulty of fabrication has made thick wires less common. The thickness of a DBC layer is variable but is commonly as thick as 200 μ m for high current applications.

Wire substrate adhesion is another key consideration when fabricating atom chips and this is especially true for thick wires because residual stress from metallization increases the probability of delamination. This problem is most often manifested after the atom chip has been fabricated and is being prepared for use. While this is a technological problem with a known solution (i.e., careful surface preparation), it is a frequent issue that is solved by using DBC. In our experience, it takes considerable effort to remove the copper from the substrate, which has made it possible to perform significant postprocessing of the atom chip. For example, we have mechanically removed selected areas of the ceramic substrate after the copper has been etched so that the chip can be folded to yield a three-dimensional (3D) "origami chip."

In this paper, we will discuss basic fabrication methods, the resulting wire quality, and power dissipation. We will show DBC atom chips that are postprocessed to make three-dimensional chip structures that simplify electrical connections to the atom chip.

I. FABRICATION OF ATOM CHIPS USING DIRECT BONDED COPPER

To make DBC substrates, a copper sheet and a ceramic are bonded using the oxygen-copper eutectic (1.5% oxygen at \sim 1065 °C) that is just below the melting point of pure copper (\sim 1085 °C). During bonding, a thin melt layer occurs at the oxide-copper interface that wets the ceramic surface and fills surface irregularities. The resulting bond is very strong because of the surface wetting between the copper and the oxide and has excellent thermal conductivity because the intermediate liquid stage fills voids between the copper and the substrate. During bonding, the melt layer solidifies as diffusion of copper and oxygen at the interface moves the stoichiometric composition of the melt away from the eutectic transition. To provide enough oxygen for the eutectic transition, a thin ceramic oxide layer is required on the surface of the copper and ceramic. The substrate can be an oxide [e.g., aluminum oxide (Al₂O₃) or beryllium oxide (BeO)] or the surface can be oxidized prior to bonding [e.g., Al₂O₃ formation on aluminum nitride (AlN) or copper oxide on copper], however, the surface oxidation step can reduce the bulk thermal conductivity due to the diffusion of oxygen along grain boundaries.²³

While any oxide can be used for DBC, most applications use electrically insulating substrates that are thermally conductive. Beryllium oxide has the highest thermal conductivity (260 W/m °C) of the ceramics, but is not commonly used because of beryllium toxicity. Most DBC substrates are Al₂O₃ or AlN. Aluminum oxide is commonly used despite a moderate thermal conductivity (~25 W/m °C) because of its low cost, high substrate quality, and high bond strength. Aluminum nitride is also used because of its high thermal conductivity (170 W/m °C) and a coefficient of thermal expansion (~4.7 μ m/m °C) that is closely matched to silicon.

Aluminum nitride has previously been used for atom chips with electroplated wires¹ where the wires are in direct and conformal contact with the substrate, however, electroplated metals typically have higher resistivities than the bulk metal and, as a result, the maximum current density is reduced.²⁴ Additionally, electroplated metals have a grained structure that results in variations of the magnetic field close to the wire.¹⁹ In DBC, the bonded copper maintains the electrical properties of the original copper sheet (i.e., high purity, high density, and low resistivity) for all thicknesses of DBC. The high purity of DBC permits high total currents relative to electroplated wires of the same thickness²³ or for the same current reduced power dissipation. Pure and high density atom chip wires have been deposited via evaporation with bulk resistivity and smooth wire edges.²⁰ The evaporation process is suitable for thin films ($<5 \mu m$) but is complicated (e.g., refilling the evaporation source) and inefficient because only a small fraction of the evaporated metal is deposited on the substrate while the remainder sticks to the walls of the vacuum system.

Excellent wire to substrate adhesion is a significant practical benefit of DBC atom chips. Atom chips that use electroplated or evaporated wires need an adhesion layer (e.g., Ti, TiW, and Cr) to avoid delamination of the atom chip wires. The quality of the adhesion can vary significantly and depends on substrate cleanliness, deposition parameters, and substrate compatibility. Wire adhesion is especially important for thicker wires that may have residual stress from the growth process. The adhesion of DBC is excellent; it takes significant force to remove bulk copper or thin wires from the substrate. Because of the excellent adhesion, atom chips can be modified after patterning (see Sec. II) while maintaining the integrity of the rest of the atom chip.

High current hermetic vias is another option made possible by DBC and is a standard option for DBC substrates²⁵ and have been used in a neutral atom trap.²⁶ Commercially available vias are incorporated into the substrate during the bonding process and require a custom manufacturing run. It may also be possible to form vias by drilling through the substrate and soldering or electroplating in the hole to form a via.

Although there are many potential methods for fabricating a DBC atom chip, the chips in this paper are fabricated by applying a mask to the surface of the DBC and then etching the copper away from the exposed areas leaving wire traces on the AlN substrate. For rapid prototyping (several hours), laser printer toner is used for the mask and the copper is etched with hydrochloric acid plus dilute hydrogen peroxide. For 125 μ m thick copper, this method can reproducibly produce $\sim 175 \,\mu m$ wide wires with \sim 500 μ m center to center spacing. The minimum feature size is determined by the resolution of the laser printer and the thickness of the copper. The second fabrication method uses photoresist and a commercially printed mask with submicron resolution. After the pattern transfer, using standard lithographic procedures, the wires are etched using either hydrochloric/peroxide or reverse electroplating.²⁷ For 125 μ m thick copper this method can reproducibly produce wires widths of $\sim 100 \,\mu$ m with $\sim 250 \,\mu$ m spacing. With care, wire widths of $\sim 50 \,\mu \text{m}$ with $\sim 200 \,\mu \text{m}$ spacing can be fabricated. Specific processing details of each method follow below.

To promote mask adhesion, the DBC surface is cleaned by scrubbing the surface with a mild abrasive and then rinsing with acetone and methanol. For rapid mask production, laser printer toner provides a chemically resistant thermo-plastic that adheres to a surface when it is melted. The toner may be remelted for multiple transfers between different substrates. A 600 dpi laser printer is used to print the chip design onto a commercially available PCB transfer film.²⁸ The transfer film will release the backing at the areas where the toner sticks to the DBC making it possible to remove the original printing media. The toner transfer procedure follows the manufacturer's instructions with special care given to the temperature cycling because overheating will result in a distorted toner mask. After etching, the mask is removed with acetone. The advantage of the toner transfer mask is rapid mask production with minimal equipment. The feature size using toner transfer is limited by the printer resolution, the spreading of the toner during transfer, and the DBC thickness.

Improved mask quality and smaller wires are achieved using photolithography. First, a silicon nitride layer is applied to the DBC to improve photoresist adhesion. A 20 μ m photoresist layer (AZ4620 or SU8) is spin coated and then lithographically patterned. Compared to the toner transfer method,



FIG. 1. A scanning electron micrograph of the top view of test chip A.

the photolithographically defined atom chip wires are significantly straighter and the achievable wire width is significantly narrower (\sim 50 μ m). The sidewall definition and minimum line size is a strong function of the total copper thickness. For the 125 μ m thick DBC used in this paper, the narrowest line feature that could be reproducibly etched was (\sim 50 μ m). Compared to a toner transfer produced atom chip, a lithographically produced atom chip requires more time (multiple days versus hours) and additional equipment but is able to produce finer features, more consistent lines, and accurate wire placement not possible using a toner mask.

Several test chips were etched using solutions of 37% hydrochloric acid (HCl), hydrogen peroxide, and water in a mixture of approximately 5:1:10 by volume. The wire quality depended on the peroxide concentration, etching time, and solution agitation. The hydrogen peroxide concentration was varied from 2 to 0.2 by volume, with lower concentrations yielding longer etching times (1-2 h) and the best wires. Solution agitation reduces the etch times by removing bubbles from the surface and provides fresh chemical to the etching areas. At the end of the etching procedure, a pipette was used to provide local agitation to reduce wire footing and assure electrical isolation of the atom chip wires. For low concentrations of hydrogen peroxide (≤ 0.4 by volume), no agitation is necessary because of reduced surface bubbles. The acid/hydrogen peroxide etching method is isotropic and causes undercutting of the mask, resulting in a trapezoidal wire shape and a wire width that is smaller than the original mask.

The quality of various masking and etching methods was investigated by evaluating the wire quality of various wire widths and spacings. The resulting quality of the etching processes and masking methods were quantified using a scanning electron microscope. Two test chips (A and B) are presented below and are representative of the photolithographically defined process. Figures 1 and 2 are top and cross sectional views of test chip A. This chip was fabricated using a photoresist mask (Hoechst AZ4620) that consisted of equally spaced $200 \,\mu$ m wide traces on 125 μ m thick DBC on AlN. The copper was etched using a concentration of hydrogen peroxide



FIG. 2. A scanning electron micrograph of the cross sectional view of test chip A.

of 1.2 parts by volume and the etching took about 15 min. As shown in Fig. 1, the traces produced by this method are straight, parallel, and the dimensions of each trace are nearly identical. The footing of the wire is less uniform than the top of the wire because of varying etch rates at the end of the etching process. Figure 2 is a cross sectional view of test chip A that shows a trapezoidal shape that is the result of the wet etching process. The width of the traces at the bottom is about 200 μ m and the width at the top of the trace is about 100 μ m. The wet etch process caused undercutting of approximately 50 μ m from each side of the mask. The aspect ratio of these wires is about $\alpha \approx 1.25$.

Figures 3 and 4 are electron micrographs of test chip B. This chip was made using the same substrate as test chip A, however, the hydrogen peroxide concentration was reduced to 0.6 parts by volume and the wire mask widths were $100 \,\mu$ m. The etching of this chip took about 30 min. Similar to the 200 μ m wide traces, Fig. 3 shows the $100 \,\mu$ m wide traces are



FIG. 3. A scanning electron micrograph of the top view of test chip B.



FIG. 4. A scanning electron micrograph of the cross sectional view of test chip B.

also straight, parallel, and reproducible. Figure 4 shows that for this chip, the traces have straighter sidewalls and less undercutting than observed in test chip A. This is attributed to the lower concentration of hydrogen peroxide. The width of the top of these wires was about 50 μ m yielding an aspect ratio of $\alpha \approx 2.5$.

Test chips were also fabricated using reverse electroplating. The DBC with applied photoresist mask was fixed parallel to a blank, similar sized piece of copper, and suspended in a copper sulfate solution with brighteners.²⁹ A positive voltage was applied to the atom chip which removed copper from the unmasked areas which was then deposited on the blank copper. Low current densities (0.5 A/m^2) produced the best results, but resulted in increased etching times. A magnetic stirrer was used to provide fresh solution to the surface of the DBC, however, for long etching times the photoresist mask debonded because of the constant agitation of the electroplating solution. Toward the end of the reverse electroplating, small ($\approx 10 \ \mu m$ diameter) copper islands remain because they were no longer electrically connected. The copper islands were removed by a rapid (<5 min) acid etch. While reverse electroplating has the potential to provide higher aspect ratio wires and close wire placement, the limits of the process are not determined at this time because of the mask integrity.

The maximum current handling and the thermal impedance of DBC atom chips was tested by fabricating a test chip (125 μ m thick copper, 125 μ m thick AlN) with three 1cm long wires with different widths: 170, 230, and 340 μ m. To approximate the reduced thermal dissipation in vacuum, the chip was tested in air *without* a heat sink. With a suitable heat sink the DBC atom chips should have equal or better performance in vacuum. Only the results of the thinnest wire are reported because the heating effects were less pronounced for the wider wires. The heating (measured using a thermocouple on the substrate ~5 mm from the wire) and the voltage drop across the wire were measured for currents of 10–100 A (~0.4–5 × 10⁹ A/m²). A 2 s current pulse of 100 A (110 W



FIG. 5. (Color online) Toner masks for etching the front (a) and back (c) chips and photographs of the etched DBC atom chips of front (b) and back (d) chips.

average power) resulted in a 2.7 times increase in the wire resistance and a <15 °C temperature rise. For short times (<10 ms) the thermal conductance of the wire/substrate junction was determined to be $11 \pm 2 \times 10^6$ W/K m², which is approximately 1.5–2 times the wire/substrate junction thermal conductance of silicon with a 20 nm oxide layer.²⁰

II. ASSEMBLY

We are currently developing a trapped atom interferometer gyroscope³⁰ that uses a cigar shaped harmonic trap, generated using a two layer DBC atom chip. The chips were fabricated using the same substrate material as the test chip with a toner transfer mask and a HCl/peroxide etch. The chip closest to the atoms (front chip) has four parallel wires that are 200 μ m wide and spaced 500 μ m center to center. Figure 5(a) shows the mask and Fig. 5(b) is a photograph of the final front chip. The chip farthest from the atoms (back chip) has four parallel wires that are 400 μ m wide and are separated by 1500 μ m. The mask and chip are shown in Figs. 5(c) and 5(d). Areas of the chip that would otherwise be open are filled to reduce the amount of etchant used and to maintain a level top surface. The chip wire leads are 2.5 mm wide to reduce power dissipation and provide strength when the substrate is removed in later processing.

After the atom chips were etched, the substrates were modified for making electrical connections by drilling holes³¹ at the end of the chip. To improve optical access and to accommodate the space requirements, the edges of the chip were folded back so that the electrical connections could be made behind the mounting structure. To avoid stressing and breaking the copper at the bend areas, the AlN substrate was removed with a diamond grinding bit that is 2-3 times wider than the substrate thickness. This is a straight forward and reliable process because the diamond bit removes hard material significantly faster than soft materials (i.e., the AlN can be removed without damaging the copper). The copper traces were deformed by the slight pressure of the diamond grinding bit but have no noticeable degradation in performance. This processing was made possible due to the excellent adhesion of the copper to the substrate and the copper thickness that is readily available using DBC. This can also be accomplished by bonding multiple substrates with appropriate gaps, however, this requires minimum lot runs and is not practical for one-off atom chip designs.

Perhaps the main advantage of foldable atom chips (dubbed "origami chips") is that they permit potentially bulky



FIG. 6. (Color online) Photograph of DBC atom chip assembly on copper mounting post.

electrical connections to be made away from the surface of the atom chip. This allows direct connections to be made to the chip while maintaining optical access over the full range of the chip. High power electrical connections are available to the chip without bond wires, soldering, or vias. The effect of the leads can be easily taken into account because the wires have a well defined path away from the chip.

Figure 6 is a photograph of a DBC atom chip assembly constructed using two atom chips, shown in Fig. 5, that were processed, folded, stacked, and epoxied to a copper heat sink (using Epotek 353 ND). Four of the atom chip wires were connected using vacuum compatible screws. The assembly was placed in an ultrahigh vacuum (UHV) chamber and baked at ~130°C for approximately 1 week. After bakeout, the UHV chamber was isolated from the turbo pump and was pumped solely by a 40 l/s ion pump to a final pressure of $< 2 \times 10^{-10}$ Torr. A ⁸⁷Rb MOT was loaded directly below the DBC atom chip assembly and was then compressed and cooled in a compressed MOT. The atoms were magnetically trapped and transported to the DBC atom chip where they were transferred to a chip quadrupole magnetic trap made by running current in the front chip wire (~5 A limited by the eletrical vacuum feedthrough) plus an appropriate bias field. The ability to quantify the quality of the first chip was limited by the optical quality of the glass vacuum chamber. A new vacuum chamber has been constructed to address the optical quality issues.

III. CONCLUSION

Direct bonded copper substrates are an excellent candidate for atom chip fabrication because of thick high purity copper that is intimately bonded to a high thermal conductivity substrate. Direct bonded copper atom chips can support very high currents (at minimum 100 A) for several seconds for high magnetic field gradient traps or for reduced power dissipation at lower currents. Wires with the appropriate cross section will further optimize the magnetic field gradient for a given power dissipation. The fabrication of DBC atom chips is straight forward and requires very little equipment. Direct bonded copper atom chips are very robust and can be bent to form 3D atom chip structures that simplifies the electrical connections away from the chips or for precision wire placement in multiple dimensions.

While this paper demonstrates the initial design and use of DBC for atom chips, there are multiple avenues for future improvements, such as other copper patterning techniques (laser etching or dry etching³²), which could produce higher density and/or higher aspect ratio wires. Additionally, high precision and high current coils can be made for precise generation of centimeter size magnetic fields. The DBC can also be patterned as a thermally conductive carrier for atom chips with finely patterned lithographic wires.⁶ The ability to form vias in the DBC also allows for greater flexibility in chip designs and for high power hermetic feedthroughs.

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APPENDIX: OPTIMAL WIRE ASPECT RATIO

Multiple methods for fabricating DBC atom chip are possible, each with resolution, time, and complexity trade-offs, therefore, the optimal aspect ratio and trapping height are determined to identify which fabrication methods are required for making DBC atom chips. The following analysis is for the power optimized case, similar results can be obtained for a fixed current density.

To determine the optimal aspect ratio that minimizes the power dissipated by a wire, consider the magnetic field produced by a rectangular wire with height *h* and width *w* that carries current in the *x*-direction. In addition to the field produced by the rectangular wire, there is a uniform bias field applied in the *y*-direction, such that there is a minimum in the field along the line y = 0, $z = z_0$. Near this point, the magnitude of the magnetic field is

$$|\mathbf{B}| \approx \sqrt{(B'y)^2 + (B'z)^2},\tag{A1}$$

and the magnetic field gradient is

$$B' = \frac{J \mu_0}{\pi} \left[\arctan\left(\frac{2(z_0 + h)}{w}\right) - \arctan\left(\frac{2z_0}{w}\right) \right], \quad (A2)$$

where J is the current density in the wire.

In a typical experiment, the magnetic field gradient B' is set at a particular value. For example, in evaporative cooling, the magnetic field must be large enough that the collision rate is high, but not so high that three body collisions limit the lifetime of the trapped atoms. Additionally, in atom chip experiments the distance from the magnetic trap to the chip z_0 is made as small as possible to achieve a high magnetic field gradient at a low current. The minimum distance is typically chosen to avoid fragmentation, the Casimir–Polder effect,²¹ thermal noise, or for optical access in atom interferometry experiments. The following analysis determines the height *h* and width *w* of a wire that minimizes the power dissipation for a given magnetic field gradient B' and working distance z_0 . The maximum B' and corresponding power dissipation is limited



FIG. 7. The optimal aspect ration α as a function of the ratio of trap height to wire thickness ζ .

by the power dissipation of the surrounding system and the maximum current density.³³

The power dissipated by the current carrying wire is

$$P = \rho lhw J^2, \tag{A3}$$

where ρ is the resistivity and *l* is the length of the wire. Combining Eqs. (A2) and (A3), the dimensionless magnetic field gradient as a function of power dissipation can be written as

$$\beta = \zeta \alpha^{1/2} \left[\arctan 2\alpha(\zeta + 1) - \arctan 2\alpha\zeta \right], \qquad (A4)$$

where $\alpha = h/w$ is the aspect ratio of the wire and $\zeta = z_0/h$ is the ratio of the trapping distance to the wire thickness. The conductor height *h* is chosen as the common scaling factor because *h* is typically fixed by the thickness of the DBC or the photolithographic process. The power dissipated by the wire is

$$P = \rho l \left(\frac{\pi z_0 B'}{\mu_0 \beta}\right)^2,\tag{A5}$$

and is minimized when β is maximized. The power of Eq. (A5) also scales as z_0^2 so the closest possible trapping distance will also reduce the total power.

Analysis of Eq. (A4) shows that for each value of ζ , there is a value of α that maximizes β . Figure 7 shows the optimal value of α as a function of ζ . For small values of ζ the optimal aspect ratio is greater than 1 (i.e., the wire is taller than it is wide). This narrowing of the top surface of the wire avoids the flattening of the magnetic field and gradient close to the surface of a broad wire.³³ For $\zeta > 0.56$ the aspect ratio is less than 1 because the magnetic trap is far enough away to avoid the flattening of the magnetic field and a wider wire has less total resistance for reduced power dissipation.

The optimal value of β for a given ζ is found by combining α_{opt} with Eq. (A4) (see Fig. 8). The dimensionless magnetic field gradient β is a maximum when $\zeta = 0.71$ and $\alpha = 0.84$ and shows there is an optimal configuration that minimizes the power dissipation for a given magnetic field gradient. For $\zeta < 0.71$ the dimensionless magnetic field gradient β decreases rapidly until $\beta = 0$ when $\zeta = 0$. Since the power dissipation is $P \propto 1/\beta^2$, the power dissipation increases rapidly as the trap is brought close to the wire. For $\zeta > 0.71$, the maximum value of β moderately decreases also



FIG. 8. The maximum value of the dimensionless magnetic field gradient β as a function of the ratio of trap height to wire thickness ζ .

resulting in increased power dissipation. However, the slowly varying nature of β_{max} for $\zeta > 0.71$ means magnetic traps can be made at distances other than $\zeta = 0.71$ while still being close to the optimal power condition.

As an example, consider the first BEC on a chip⁷ achieved using $\sim 10 \times 50 \,\mu\text{m}$ gold wires electroplated on an AlN substrate. The atoms were trapped $\sim 70 \,\mu\text{m}$ from the chip surface. Thus, $\alpha = 0.2$, $\zeta = 7$, and using Eq. (A4) $\beta = 0.13$. For an optimal wire with h = 100 and w = 120 with the same field gradient and trapping distance can be achieved while dissipating 0.3 times the power.

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