

AFRL-RX-WP-TM-2010-4263

JOINT AOARD/AFRL/LLNL WORKSHOP ON THE NUCLEATION OF PHASE TRANSFORMATIONS IN METALLIC SOLIDS

University of North Texas

MAY 2010 Final Report

Approved for public release; distribution unlimited.

See additional restrictions described on inside pages

STINFO COPY

AIR FORCE RESEARCH LABORATORY MATERIALS AND MANUFACTURING DIRECTORATE WRIGHT-PATTERSON AIR FORCE BASE, OH 45433-7750 AIR FORCE MATERIEL COMMAND UNITED STATES AIR FORCE

NOTICE AND SIGNATURE PAGE

Using Government drawings, specifications, or other data included in this document for any purpose other than Government procurement does not in any way obligate the U.S. Government. The fact that the Government formulated or supplied the drawings, specifications, or other data does not license the holder or any other person or corporation; or convey any rights or permission to manufacture, use, or sell any patented invention that may relate to them.

This report was cleared for public release by the USAF 88th Air Base Wing (88 ABW) Public Affairs Office (PAO) and is available to the general public, including foreign nationals. Copies may be obtained from the Defense Technical Information Center (DTIC) (http://www.dtic.mil).

AFRL-RX-WP-TM-2010-4263 HAS BEEN REVIEWED AND IS APPROVED FOR PUBLICATION IN ACCORDANCE WITH THE ASSIGNED DISTRIBUTION STATEMENT.

*//Signature//

JAIMIE TILEY, Project Engineer Metals Branch Metals, Ceramics & NDE Division //Signature//

PAUL RET, Chief Metals Branch Metals, Ceramics & NDE Division

//Signature//

ROBERT MARSHALL, Deputy Chief Metals, Ceramics & NDE Division Materials & Manufacturing Directorate

This report is published in the interest of scientific and technical information exchange, and its publication does not constitute the Government's approval or disapproval of its ideas or findings.

*Disseminated copies will show "//Signature//" stamped or typed above the signature blocks.

REPORT DOCUMENTATION PAGE					Form Approved OMB No. 0704-0188		
The public reporting burden for this collection of information is estimated to average 1 hour per response, including the time for reviewing instructions, searching existing data sources, gathering and maintaining the data needed, and completing and reviewing the collection of information. Send comments regarding this burden estimate or any other aspect of this collection of information, including suggestions for reducing this burden, to Department of Defense, Washington Headquarters Services, Directorate for Information Operations and Reports (0704-0188), 1215 Jefferson Davis Highway, Suite 1204, Arlington, VA 22202-4302. Respondents should be aware that notwithstanding any other provision of law, no person shall be subject to any penalty for failing to comply with a collection of information if it does not display a currently valid OMB control number. PLEASE DO NOT RETURN YOUR FORM TO THE ABOVE ADDRESS .							
1. REPORT DATE (DD-MM-YY)		2. REPORT TYPE		3. DATI	ES COVERED (From - To)		
May 2010		Technical Men	10	18 3	eptember 2008 – 30 April 2010		
4. TITLE AND SUBTITLE JOINT AOARD/AFRL/LLNL WORKSHOP ON THE NUCLEATION OF PHASE TRANSFORMATIONS IN METALLIC SOLIDS					5a. CONTRACT NUMBER FA8650-08-C-5226		
					5b. GRANT NUMBER		
					5c. PROGRAM ELEMENT NUMBER 62102F		
6. AUTHOR(S)					5d. PROJECT NUMBER 4349		
					5e. TASK NUMBER		
					20		
					5f. WORK UNIT NUMBER		
					LM114100		
7. PERFORMING ORGANIZATION NAME(S) AND ADDRESS(ES)					8. PERFORMING ORGANIZATION		
University of North Texas					REPORT NUMBER		
1147 Union Circle							
Denton, TX 76203							
9. SPONSORING/MONITORING	GAGENCY NAM	E(S) AND ADDRESS(E	ES)		10. SPONSORING/MONITORING		
Air Force Research La	boratory				AGENCY ACRONYM(S)		
Materials and Manufac	cturing Direct	orate			AFRL/RXLM		
Wright-Patterson Air Force Base, OH 45433-7750					11. SPONSORING/MONITORING		
Air Force Materiel Command					AGENCY REPORT NUMBER(S)		
United States Air Force							
12. DISTRIBUTION/AVAILABILITY STATEMENT Approved for public release; distribution unlimited.							
13. SUPPLEMENTARY NOTES							
Document contains color. This is the best quality available of the presentations assembled from the conference (pagination							
is not continuous across the document).							
PAO Case Number: 88ABW 2010-3948; Clearance Date: 22 July 2010.							
14. ABSTRACT A workshop on the Nucleation of Phase Transformations in Metallic Solids was held in Maui, Hawaii on May 2-7. 2010.							
The meeting was spon	sored by the A	Asian Office of Ae	rospace Researc	ch and Develog	pment (AOARD), the Air Force		
Research Laboratory (AFRL), the Air Force Office of Scientific Research (AFOSR), and the Lawrence Livermore							
National Laboratory (LLNL). Representatives attended from the United States, Australia, Singapore, India, and France.							
I ne focus of the workshop was to develop research tasks aimed at improving current capabilities in the areas of avantimentation, modeling and characterization as they apply to the pucleation of solid phase transformations. The							
experimentation, modering and characterization as they apply to the nucleation of solid phase transformations. The overall objectives of the workshop were to bring together a diverse group of researchers to establish the state of the art in							
experimenting, characterizing and modeling. Specifics items addressed included (1) what advances are needed in the							
atomistic/computational modeling area to significantly impact the science? (2) what tools and techniques are required to							
characterize the formation of nucleants and the local chemical and energy environment? and (3) what opportunities exist							
for combining advance characterization techniques with experimental validation of nucleation models. The results are							
provided within this document, including the presentation materials from participants.							
15. SUBJECT TERMS advanced characterization, nucleation							
16. SECURITY CLASSIFICATIO	N OF:	17. LIMITATION	18. NUMBER	19a. NAME OF	RESPONSIBLE PERSON (Monitor)		
a. REPORT b. ABSTRACT	c. THIS PAGE	E OF ABSTRACT: OF PAGES Jaimie Tiley		Гiley			
Unclassified Unclassified	Unclassified	SAK	1108	19b. TELEPHO	NE NUMBER (Include Area Code)		
				IN/A			

Table of Contents

Summary	1	
Findings	1	
Presented Experimental and Theory Topics	2	
Presented Modeling Topics		
Presented Characterization Topics	3	
Participants	4	
Acknowledgments	4	
Appendix A: List of Participants	5	
Appendix B: Presentation Materials	6	

Joint AOARD/AFRL/LLNL Workshop on the Nucleation of Phase Transformations in Metallic Solids

Summary

A workshop on the Nucleation of Phase Transformations in Metallic Solids was held in Maui, Hawaii on May 2-7, 2010. The meeting was sponsored by the Asian Office of Aerospace Research and Development (AOARD), the Air Force Research Laboratory (AFRL), the Air Force Office of Scientific Research (AFOSR), and the Lawrence Livermore National Laboratory (LLNL). Representatives attended from the United States, Australia, Singapore, India, and France. The focus of the workshop was to develop research tasks aimed at improving current capabilities in the areas of experimentation, modeling and characterization as they apply to the nucleation of solid phase transformations. The overall objectives of the workshop were to bring together a diverse group of researchers to establish the state of the art in experimenting, characterizing and modeling. Specifics items addressed included (1) what advances are needed in the atomistic/computational modeling area to significantly impact the science? (2) what tools and techniques are required to characterize the formation of nucleants and the local chemical and energy environment? and (3) what opportunities exist for combining advance characterization techniques with experimental validation of nucleation models?

Findings

The following points were made by the participants during discussions:

1. *Experimentation and Theory.* Classical theory has provided tremendous insight into the nucleation process although it has been difficult to experimentally verify specific elemental composition changes, vacancies, and energies associated with nucleant and embryo formation. The use of composition wave functions, understanding of shear, consideration of dynamic nucleation events from atom clustering, knowledge of electronic structures, and spinoidal decomposition events may provide added insight into nucleation. There is a need for improved thermodynamic data, diffusivities, and interfacial energies as well as requirements for statistical analysis of rare events.

2. *Modeling.* The modeling discussions centered on the use of phase field approaches that utilize nudged elastic band methods, Langevin noise terms and/or use of monte carlo simulations. There is a need for accurate energy surface representations in addition to better thermodynamic and surface energy terms. The use of these techniques provides nucleation parameters that are very difficult to measure directly. Researchers also identified the need for new techniques for atomistic descriptions of multi-component systems, identifying the transition states, and the need for understanding the interactions between defects and nucleation events.

3. *Advanced Characterization Techniques.* Advances with atom probe tomography provides atomic level compositions, critical for evaluation of embryos and nucleants. However efficiency problems with the techniques still present serious issues and should be resolved. Dynamic and hi-resolution transmission electron microscopy techniques have also advanced to the art of

providing structural and chemical information at the atomic level. Although there are issues related to surface and thin film considerations, in situ experiments utilizing these techniques may provide vital information on embryo and nucleant precursors that are critical for model verification.

Presented Experimental and Theory Topics

Experts in the field of experimentation and theory of nucleation presented 4 topics, including 3 plenary speeches. In addition, four sessions were designed to address specific nucleation theory and experimental concerns. The sessions were titled (1) Heterogenieties, (2) Nucleation as a Rare Event, and (3) Experimental Advances.

Dr. Jim Belak (Lawrence Livermore National Laboratory) presented the first Plenary Speech, providing an overview of the field from the first work by Kolmogorov, Johnson. Mehl and Avrami to the work by Cahn, Russel, up to the recent work of today. He was followed by Professor John Perepezko (University of Wisconsin) who gave a plenary presentation on the analysis and modeling of nucleation controlled reactions. Secretary Srikumar Banerjee, PhD, (Government of India) gave a plenary presentation on the structural evolution during nucleation processes. The final plenary presentation was provided by Dr. Alan Ardell (National Science Foundation) on the nucleation and coarsening in normal and inverse Ni-Al alloys. In the Heterogenieties session chaired by Dr. Belak, Dr. Brian Reed (Lawrence Livermore National Laboratory) presented material on grain boundary engineered materials as correlated networks, and the implications of large-scale twin nucleation. Professor Gary Shiflet (University of Virginia) gave a presentation on the control of embryo formation and critical nucleus properties. He discussed the possibilities of developing and applying knowledge of electronic structures and atomic interactions into the modeling of the nucleation process. Professor Julia Hammer (University of Hawaii) combined classical theory and advanced characterization in her presentation on the nucleation of crystals in magma. She discussed the use of high temperature, high pressure furnaces to experimentally validate nucleation models of glass that forms deep beneath the surface in volcanoes.

Presented Modeling Topics

Leaders in the field of modeling presented current problems and successes that have been achieved at the different length scales. There were three classes of modeling: (1) atomistic studies, (2) research at the meso scale, and (3) continuum scale modeling.

Professor Wolfgang Windl (The Ohio State University) presented a briefing on lessons learned from the world of semiconductors. His presentation was followed by Professor Jeff Rickman (Lehigh University) who discussed the kinetics and microstructure associated with heterogenous nucleation and growth. Dr. Alphonse Finel (ONERA, France) provided a briefing on the coarse grain derivation of the phase field equations. Dr. Blas Uberuaga (Los Alamos National Laboratory) discussed the use of accelerated dynamics methods. Professor Srini Srivillipurtha (University of North Texas) followed with a presentation on first principles simulation of beta to omega transformations in titanium alloys. His talk was supported in part by experimental work conducted by Professors Hamish Fraser (The Ohio State University) and Rajarshi Banerjee (University of North Texas), also in attendance. During the discussion period, Professor Srivillipurtha discussed the need for new approaches to address atomistic modeling of multicomponent systems. Professor Yunzhi Wang (The Ohio State University) provided a discussion on the effect of local stress on nucleation and variant selection during solid state transformation with symmetry reductions. His use of the phase field approach was heavily discussed during several of the presentations. Professor Qiang Du (Penn State University) also presented a discussion on the use of phase field, focusing on the prediction of critical nucleus morphologies in solids. His work was followed by a briefing by Dr. Chen Shen (General Electric, USA) on the use of phase field techniques. Professor Greg Olson (Northwestern University) and Dr. Fan Zhang (Computherm Inc.) gave presentations on their meso-scale models. Professor Olson discussed the use of multiscale integration in the study of nucleation engineering. He presented numerous examples where multi-scale modeling had effectively captured the nucleation and growth of phase transformations. Dr. Zhang discussed the use of thermodynamic modeling of multi-component systems and the integration of the modeling into kinetic simulations. She discussed the current challenges facing the use of thermodynamic models in simulations of nucleation events, especially in commercial alloys where specific data on three and four component energy interactions are limited. Dr. S. Ranganathan (National Metallurgical Laboratory, India) spoke about the thermodynamic modeling of the early stages of solid state precipitation in alloy systems. Dr. Dan Miracle (AFRL) presented on the nucleation mechanisms for aluminum crystals in amorphous aluminum alloys.

Presented Characterization Topics

Leaders in the field of advanced characterization presented 11 topics. The major discussions concerned the use of transmission electron microscopes and/or atom probe tomography.

Dr. Thomas LaGrange (Lawrence Livermore National Laboratory) gave a presentation on the quantification of crystallization kinetics using nanosecond time resolved electron microscopy. His talk was followed by Dr. Daniel Orlikowski (Lawrence Livermore National Laboratory) who presented a briefing on high pressure considerations and the use of the dynamic anvil cell. Dr. Barry Muddle (Monash University, Australia) presented material on the heterogenous nucleation of plate shaped transformation products. His characterization techniques employed the high resolution transmission electron microscope. Professor Rajarshi Banerjee (University of North Texas) also used advanced TEM techniques in his presentation on the early stages of nucleation and growth of omega precipitates within the beta matrix of titanium alloys. His work provided the experimental validation for the modeling work presented by Professor Srivillipurtha. Dr. Mike Miller (Oak Ridge National Laboratory) followed with a presentation on the advances in atom probe tomography for nucleation studies. His discussion included an overview of the limitations associated with the techniques. Dr. Babu Viswanathan (UES, AFRL) presented a briefing on the gamma/gamma prime phase transformation in nickel alloys, including the issues with characterizing fine scale precipitates. Professor Dipankar Banerjee (IISC, India) provided a presentation on the alpha and beta transformations in titanium alloys, including the nucleation of alpha during thermal processing. Professor Jian Feng Nie (Monash University, Australia) presented on shape strain and its accommodation during the precipitation of precipitate plates. He relied heavily on the use of hi-resolution TEM techniques as well. Professor Raju

Ramanujan (Nanyang Technological University, Singapore) presented material on the nucleation of soft magnetic nanomaterials. He highlighted the impact of different elements on the nucleation rate and growth rate of particles. He also suggested the use of a hot stage TEM to further study the concepts. The final presentation was provided by Professor Hamish Fraser (The Ohio State University) on the use of new characterization techniques. His talk emphasized the need to apply different characterization techniques to validate techniques and offset limitations associated with different approaches. One example was the use of image corrected high resolution TEM systems along with atom probe tomography techniques to determine structural information.

Participants

The workshop was attended by 37 people, including speakers from academia, government laboratories, and industry. The audience was predominantly from the US, although six attendees traveled under the Window on Science program sponsored by AOARD.

Academic Institution Representation. The audience included representatives from 10 academic institutions: Monash University, Nanyang Technological University, India Institute of Science, University of Virginia, Northwestern University, The Ohio State University, University of North Texas, Penn State University, University of Hawaii, and Lehigh University.

Government Laboratory Representation. Seven government laboratories or agencies were represented: Air Force Research Laboratory, Air Force Office of Scientific Research, Asian Office of Aerospace Research and Development, Los Alamos National Laboratory, Lawrence Livermore National Laboratory, Oak Ridge National Laboratory, and the National Science Foundation. In addition the Secretary of Nuclear Energy for India attended (Atomic Energy Commission), and the Deputy Director of the National Metallurgical Laboratory, India, attended.

Industrial Representation. Representatives of 3 private sector entities were also represented: Questek, Computherm, and General Electric Global Research.

International Representation. Five nations were represented in the audience: Singapore, India, France, Australia, and the United States.

Acknowledgments

Funding for this workshop was provided by Air Force Research Laboratory and the Asian Office of Aerospace Research and Development. The workshop was also supported by the Lawrence Livermore National Laboratory. Administrative and logistic support was provided by the Maui Economic Development Company under a contract with the Air Force Research Laboratory.

Appendix A

List of Participants

Jim Belak* John Perepezko Srikumar Banerjee Alan Ardell Barry Muddle * Wolfgang Windl Jeff Rickman Alphonse Finel Blas Uberuaga Jeff Simmons* Jay Tiley* Greg Olson **Dipankar Banerjee** Fan Zhang Dan Miracle Long-Qing Chen* Chen Shen Jian-Feng Nie S. Ranganathan Julia Hammer Hamish Fraser* Rajarshi Banerjee* Ken Gorretta Yunzhi Wang* Laura Cooney Thomas LaGrange Daniel Orlikowski Brian Reed Srini Srivillipurtha Mike Miller Babu Viswanathan* Raju Ramanujan Gary Shiflet Qiang Du Traci Haerr Sandy Ryan Leilani Bulosan

Lawrence Livermore National Laboratory University of Wisconsin Atomic Energy Comission, India National Science Foundation Monash University, Australia **Ohio State University** Lehigh University **ONERA.** France Los Alamos National Laboratory Air Force Research Laboratory Air Force Research Laboratory Northwestern University India Institute of Science, India Computherm Inc. Air Force Research Laboratory Penn State University General Electric Global Research Monash University, Australia National Metallurgical Laboratory, India University of Hawaii Ohio State University University of North Texas Asian Office of Aerospace Research and Development **Ohio State University** Air Force Office of Scientific Research Lawrence Livermore National Laboratory Lawrence Livermore National Laboratory Lawrence Livermore National Laboratory University of North Texas Oak Ridge National Laboratory Air Force Research Laboratory Nanyang Technological University, Singapore University of Virginia Penn State University Air Force Research Laboratory Maui Economic Development Board Inc. Maui Economic Development Board Inc.

* workshop organizer

Appendix B

Presentation Materials

Nucleation and Coarsening in Normal and Inverse Ni-Al Alloys

Alan J. Ardell

Program Director Metals and Metallic Nanostructures Program Division of Materials Research National Science Foundation Arlington, VA 22201



Outline

- Brief review of the classical theory of homogeneous nucleation
- The nucleation of γ' (Ni₃AI) precipitates in normal Ni-AI alloys and γ (Ni-AI solid-solution) precipitates in "inverse" Ni-AI alloys offer the best prospects ever of investigating homogeneous nucleation during precipitation from solid solution---Why and How!!!
 - The Ni-rich region of the Ni-Al phase diagram;
 - How data on coarsening of precipitates in normal and inverse Ni-Al alloys can be used to provide values of parameters that are important in the process of nucleation;
 - Observations that suggest the efficacy of studying nucleation in inverse alloys, and experimental advantages that can be used to inform nucleation studies;
 - Observations that highlight the obstacles to studying nucleation in normal alloys and what can be done to overcome them;
- Presentation of data that might be useful in studies of nucleation in Ni-Al alloys...elastic constants, lattice mismatch
- Musings about diffuse γ/γ' interfaces---might these muddy the waters?



Classical Theory of Nucleation---Energetics



Total change in free energy on formation of a nucleus of radius r is

$$\Delta G = \frac{4\pi r^3}{3} \Delta G_v + 4\pi r^2 \sigma$$

 ΔG_v is the difference in the Gibbs free energy/vol of the α and β phases ($\Delta G_v < 0$);

Elastic energy/vol (>0) for coherent precipitates can contribute, but it is usually very small compared to ΔG_v

 σ is the energy/area of the α - β interface (σ > 0)



 ΔG has a maximum value of ΔG^* at a critical value of r^{*}, as shown in the diagram below:



Interfacial energy opposes the formation of the nucleus, giving rise to an energy barrier, ΔG^* , that must be overcome before the nucleus can be considered stable. Nuclei with radii r > r* are always able to grow with a reduction in energy of the system.



It is sometimes more useful to express the change in free energy in terms of n, the number of B atoms in the nucleus:



The variation of ΔG in the vicinity of n* (or r*) is relatively small over the range of energy $\Delta G^* - kT$. Nuclei with sizes n* $\pm \delta/2$ are considered to "random walk" over the energy barrier until they reach a size n* $\pm \delta/2$, beyond which the probability that they become subcritical is essentially zero.



It is possible to derive partial differential equation that describes the concentration of nuclei of size n, C_n , at any time t. This equation does not have a formal solution. The Classical Theory assumes a solution of the form

 $J^* = J_s exp(-t / \tau)$

 \boldsymbol{J}_{s} is the STEADY STATE NUCLEATION RATE

 $J_{s} = \beta^{*} C_{n^{*}}^{o} Z$

 β^* is the rate at which B atoms attach themselves to a nucleus of critical size

$$\beta^* = \frac{4\pi (r^*)^2 X_o}{a^4} D_B$$

 X_{o} is the initial concentration of B in α

 D_B is diffusion coefficient of B in α

a is the jump distance



 $C^o_{n^\star}$ is the concentration of nuclei containing n^\star B atoms

$$C_{n^*}^{o} = X_o N_o exp(-\Delta G_{n^*} / kT)$$

No is number of atomic sites/vol

Z is the Zeldovich non-equilibrium factor. It takes into account the fact that there is a finite probability that a nucleus can become subcritical until it contains more than $n^* + \delta/2$ B atoms and depends on the curvature of the ΔG vs. n curve at n = n*

$$Z = \left[\frac{-1}{2\pi kT} \left(\frac{\partial^2 \Delta G_n}{\partial n^2}\right)_{n^*}\right]^{\frac{1}{2}}$$



The incubation time, $\boldsymbol{\tau}\text{,}$ is

$$\tau = \frac{\delta^2}{2\beta^*} = \frac{2}{\pi Z^2 \beta^*}$$

$$\delta = \begin{cases} \frac{-8kT}{\left(\frac{\partial^2 \Delta G_n}{\partial n^2}\right)_{n=n^*}} \end{cases}^{\frac{1}{2}} = \frac{2}{Z\sqrt{\pi}}$$



Any attempt to validate the classical theory of nucleation necessarily involves measurements of J_s and τ , preferably as functions of T and X_o , both of which govern the supersaturation of the solid solution.

This in turn involves measurements of the number of precipitates/vol, Nv, vs aging time t, with the expectation that only stable precipitates with $n > n^*$ will be detectable.



The expected behavior is shown below:



To compare experiment and theory there is a lot we need to know, with many necessary precautions.

The CRUCIAL parameters are ${\scriptstyle {\mathbb G}},\; \Delta G_{_V} \; and \; D_{_B}$

In Ni-Al alloys ${}_{\odot}$ and D_B can be estimated with reasonable accuracy from data on coarsening, but ΔG_v is tricky.



Free Energy Diagram for Nucleation of an A-B alloy, initial composition X_o



 $G_v = G_m / V_m$; V_m is the partial molar volume of B

The distance -DC = ΔG_m = free energy/mol β for nucleation of a β -phase nucleus of equilibrium composition, X_{Be} .

The distance -D'C' = $\Delta G_{m,max}$ is the maximum value of the driving force for nucleation. But it is for a β -phase nucleus of composition $X_{\beta} > X_{\beta e}$.

For any β -phase composition > $X_{\beta,min}$ there exists a positive driving force for nucleation (i.e. $\Delta G_m < 0$). This region is represented in green for nucleus compositions up to $X_{\beta e}$.



Estimating ΔG_v requires knowledge of the Gibbs free energy of mixing of the α and β phases, and is sensitive to the curvatures of the free energy functions

If both phases are ideal solutions

$$\Delta \mathbf{G}_{\mathbf{v}} = -\frac{\mathbf{kT}}{\mathbf{V}_{\mathbf{m}}} \left\{ \mathbf{X}_{\beta \mathbf{e}} \ln \frac{\mathbf{X}_{\mathbf{o}}}{\mathbf{X}_{\alpha \mathbf{e}}} + \left(1 - \mathbf{X}_{\beta \mathbf{e}}\right) \ln \left(\frac{1 - \mathbf{X}_{\mathbf{o}}}{1 - \mathbf{X}_{\alpha \mathbf{e}}}\right) \right\}$$

This equation is a very good approximation when α and β are both terminal solid solutions with limited solubility



So...What's the big deal? Why is classical nucleation theory so difficult to verify, and why are we talking about it amost 75 years after Becker and Doring published their paper in 1935[†]:

[†]R. Becker and W. Doring, ANNALEN DER PHYSIK, 24 (1935) 719-752.

The reason is that, at least for precipitation from solid solution, accurate measurements of steady-state nucleation rates and incubation times are DIFFICULT

One important factor is that diffusion is strongly affected by Quenched-in Vacancies, even when every effort is made to minimize their influence!

Some results that illustrate this follow



Alloys quenched directly from solution treatment temperature, 870 °C, to the aging temperature.

fcc Co precipitates are fully coherent, lattice mismatch = -1.7%



Cu-1% Co

The equilibrium volume fraction is ~0.01 The maximum value of $N_{\rm v}$ is ~10^{21}/m^3

F.K. LeGoues and H.I. Aaronson, Acta Metall. 32 (1984) 1855



Steady-state Nucleation Rates



There is reasonably good agreement with theory assuming diffusion of Co at the solution-treatment temperature

F.K. LeGoues and H.I. Aaronson, Acta Metall. 32 (1984) 1855



Incubation Times



Here there is reasonably good agreement with theory assuming diffusion of Co at the aging temperature

F.K. LeGoues and H.I. Aaronson, Acta Metall. 32 (1984) 1855



Strain energy was included in the previous comparisons with theory. Here it is ignored.



F.K. LeGoues and H.I. Aaronson, Acta Metall. 32 (1984) 1855



Crucial role of excess vacancies on nucleation in AI -5.9% Zn-2.9% Mg alloys



Ternary alloy solution-treated and quenched into boiling water, below the GP zone solvus and held for (a) 0.1 min; (b) 1 min; (c) 15 min; (d) 60 min

The alloy is then aged for 3 hr at 180 °C, ABOVE the GP zone solvus, but where η^{*} is stable, producing these microstructures

GP zones coarsen at 100 °C, aided by quenched-in vacancies, and serve as nuclei for ¶' at 180 °C. Depletion of excess vacancies at the GB is responsible for the width of the PFZ

G.W. Lorimer and R.B. Nicholson, Acta Metall. 14 (1966) 1009



Despite a heroic effort by LeGoues and Aaronson to test the classical theory, uncertainty remains. Depending on how you look at the results, the disagreement is as much as several orders of magnitude. The role of excess vacancies in the evolution of precipitate microstructures in Al alloys is crucial.

Can we possibly do better in testing the nucleation of precipitates in Ni-Al alloys, avoiding the problems that plague these studies in other alloys?

I think so!





Nearly all the data in the world on the Ni-Ni₃Al phase diagram



How do the kinetics of precipitation of γ in γ' compare with those of γ' in γ ?



Precipitation observed in a dendritic region of an alloy containing 22.25 at.% Al. The specimen was aged for 48 h at 700 °C. The kinetics are much faster in normal alloys. One contributing factor is much slower diffusion in the ordered Ni_3Al matrix in the inverse alloy. Other factors could also be important (the free energy functions for example).

Jaykumar Joshi, 2000



INVERSE ALLOYS

 $\mathrm{Ni}_{3}\mathrm{AI}$ is the matrix phase, Ni-AI is the precipitate phase







Results on coarsening of $\boldsymbol{\gamma}$ precipitates in "inverse" Ni-Al alloys



Y. Ma and A.J. Ardell, Zeit. für Metallkunde 94 (2003) 972.







fe

Y. Ma and A.J. Ardell, Acta Mater 55 (2007) 4419





Data on the kinetics of coarsening at 650 °C. The slopes of the curves provide values of $k(f_e)$, which clearly increases with increasing f_e .

Y. Ma and A.J. Ardell, Scripta Mater. 52 (2005) 1335




The data on k(f_e) for the 5 inverse alloys aged at 650 °C were fit to the MLSW theory, yielding k(0) = $1.7065 \pm 0.0917 \times 10^{-31} \text{ m}^{-3}$ /s. As can be seen, the agreement between the MLSW theory and experiment is quite good.

Y. Ma and A.J. Ardell, Scripta Mater. 52 (2005) 1335



To calculate \tilde{D} we need to know G_m'' . For this we used the thermodynamic model of T. Ikeda et al.

$$G_{m\gamma}^{"} = \frac{4RT}{X_{AI}(1 - X_{AI})} \Phi$$

$$\Phi = X_{AI}X_{NI} \left\{ 24 \frac{E}{RT} + \frac{X_{AI}X_{NI} \cdot \frac{3S^{2}}{16} \cdot \frac{S}{2} \left(X_{NI} \cdot X_{AI} \cdot \frac{S}{2}\right) \left(\frac{3}{8} \frac{\partial S}{\partial X_{AI}} \cdot 1\right)}{\left(X_{NI} \cdot \frac{3S}{4}\right) \left(X_{AI} \cdot \frac{S}{4}\right) \left(X_{NI} + \frac{S}{4}\right) \left(X_{AI} + \frac{3S}{4}\right)} \right\}$$

$$\frac{\left(X_{NI} - \frac{3S}{4}\right) \left(X_{AI} - \frac{S}{4}\right)}{\left(X_{NI} + \frac{S}{4}\right) \left(X_{AI} + \frac{3S}{4}\right)} = \exp\left(-8\frac{ES}{RT}\right)$$

$$\frac{\partial S}{\partial X_{AI}} = \frac{S\left(X_{NI} - X_{AI} - \frac{S}{2}\right)}{X_{AI}X_{NI} - \frac{3S^{2}}{16} - 8\frac{E}{RT} \left(X_{NI} - \frac{3S}{4}\right) \left(X_{AI} - \frac{S}{4}\right) \left(X_{AI} - \frac{S}{4}\right) \left(X_{NI} + \frac{S}{4}\right) \left(X_{AI} + \frac{3S}{4}\right)}$$

S is the long-range-order parameter and E is the ordering energy

T. Ikeda, H. Numakura and M. Koiwa, Acta Mater 46 (1998) pp. 6605



Chemical Diffusion Coefficients calculated from data on coarsening of γ in inverse Ni-Al alloys using $\odot = 8.3 \text{ mJ/m}^2 +$ thermodynamic model of Ikeda et al. (filled symbols) & extrapolation (Y. Ma, Ph.D. thesis) of high-temperature thermodynamic data on activities of Hilpert et al. (open symbols)



Lines---extrapolation of high-temperature data on diffusion, 23 and 24 % Al

Y. Ma and A.J. Ardell, Mater. Sci. Engr. A516 (2009) 259



PSDs in inverse Ni-Al alloys



Particles with radii < 0.4 r are not observed, even though they should be visible

Estimate of minimum visible particle size, r_{min}, from Structure-Factor contrast:

$$r_{\min} = \frac{\left|\Delta I / I\right|}{4\pi \left|\xi_{gp}^{-1} - \xi_{gm}^{-1}\right|}$$

 $\Delta I/I = contrast = 0.1;$

 ξ_{gm} extinction distance for a {100} superlattice reflection in Ni₃Al at 100 kV = 385 nm; ξ_{ap} extinction distance for a {100} reflection in Ni-Al at 100 kV = ∞ nm;

r_{min} **≈** 3.1 nm

Conclusion: the missing particles in the PSDs are not missing because they are too small to be seen

Y. Ma and A.J. Ardell, Scripta Mater. 52 (2005) 1335



Reasons why experiment on nucleation in inverse alloys are likely to succeed





Ni-22.25 at.% Al alloy solution treated at 1000 °C, quenched and aged at 700 °C for (a) 8 h and (b) 24 h.



Even though the undercooling is large ($\Delta T > 100$ °C), nucleation is slow!



700 °C for 120 h. Only dislocations are visible in the image.



1000 900 **()** 800 700 600 0.22 0.23 0.21 X_{AI}

650 °C for 96 h + 730 °C for 1.5 h. Many γ precipitates visible at a small undercooling (~25 to 30 °C)

These results suggest that the incubation time for an alloy containing 22.6 % AI aged exceeds 120 h at 700 °C, but is less than 96 h at 650 °C.



These observations suggest that an investigation of nucleation kinetics in inverse Ni-Al alloys have a very good chance of being successful: f_e is small, incubation times are long, significant concentrations of excess vacancies are avoidable and except for the thermodynamics the physical parameters are reasonably well known.

Assuming that the γ' phase is an ideal solution, I obtain r^{*} = 4.83 and 17.40 nm for the 22.25 and 22.60 % Al alloys aged at 700 °C. These are undoubtedly inaccurate, but suggest that stable nuclei should be readily visible in the TEM by either structure-factor or stain-field contrast



Is there any chance of investigating nucleation in normal Ni-Al alloys?

This was attempted years ago by Kirkwood and co-workers, Wagner & Kampmann and Xiao & Haasen without quantitative success, because nucleation of γ' is typically extremely rapid, occuring during quenching from the solution treatment temperature

It is advantageous to keep f_e small in the hope that N_v will be roughly equal to the values in the experiments of LeGoues and Aaronson (10²¹/m³). This helps minimize the issue of overlapping diffusion fields during nucleation.

Seidman and co-workers have measured N_v vs. t during the early stages of decomposition of ternary Ni-Cr-Al alloys using APT, f_e ranging from 0.10 to 0.16, N_v as large as 10^{24} /m³. Measured nucleation rates are 2 to almost 3 orders of magnitude slower than predicted by theory, but the physical parameters are not well constrained as they are in the binary alloy system.



An Illustration of the effect of small compositional non-uniformity on a γ' dispersion at small undercoolings

Ni-11.78 % AI aged at 630 °C for 273.5 h





The γ' precipitates are much larger in the part of the specimen with the smaller volume fraction as a consequence of the anomalous dependence of coarsening kinetics on f: Region A is slightly depleted in Al while Region B is slightly enriched



A. Maheshwari and A.J. Ardell, *Scripta Metall. Mater.* **27** (1992) 943

Can we devise a heat treatment that eliminates compositional inhomogeneities in the starting alloy, suitable for investigations of nucleation of γ precipitates?





Yes...We can first age a concentrated alloy (~16% AI) at a high temperature (~800 °C), producing a homogeneous matrix of γ with a concentration of 13.16% AI

then re-age this same alloy at a lower temperature (~600 °C) to produce a relatively large volume fraction of γ (~0.17)

This aging sequence produces a bimodal distribution of γ , not unlike the bimodal and trimodal distributions found in commercial superalloys



Ni-15.91 %Al aged first for 16.67 h at 800 °C, followed by aging at 600 °C for the times indicated



D.J. Chellman and A.J. Ardell, in *Materials Architecture*, Proc. 10th Risø International Symposium on Metallurgy and Materials Science, Roskilde, Denmark, 1989, p. 295.



The small Class II precipitates coarsen as if the large Class I precipitates were not there, until only very few of them remain. The Class I precipitates grow by consuming the Class II precipitates, not by coarsening in the conventional sense



D.J. Chellman and A.J. Ardell, in *Materials Architecture*, Proc. 10th Risø International Symposium on Metallurgy and Materials Science, Roskilde, Denmark, 1989, p. 295.



We can also use the same idea to produce very small volume fractions of γ , comparable to the volume fractions in the dispersions of Co precipitates in Cu-Co alloys





The alloy containing 11.78 % Al is now first aged at 648 \pm 2 °C for 120 h.

It is then re-aged at 630 °C for various times.

The microstructure (f_e = 0.0332) after aging for 120 h is





Results of experiments on coarsening at small f_e

Specimens containing 11.66, 11.70 and 11.78 % AI were PRE-AGED a few degrees below the best estimate of the solvus temperature for each alloy for 120 to 160 h, then aged for various times at 630 °C



The rate constant DECREASES as $\rm f_e$ increases. It is exactly the opposite of the behavior in inverse alloys. In this sense the coarsening behavior is ANOMALOUS

A. Maheshwari and A.J. Ardell, Acta Metall. Mater. 40 (1992) 2661



Coarsening in pre-aged alloys is anomalous, but the success of the aging sequence in removing compositional fluctuations bodes well for possible investigations of homogeneous nucleation of γ' precipitates in Ni-Al alloys, which has proved heretofore impossible. The possibility of a successful investigation of nucleation is at least feasible.



Inverse alloys are not immune from compositional nonuniformity, as shown below, but they can also be heat-treated to minimize this problem



Different regions of 22.4 % Al alloy aged at 650 °C for 240 h plus 800 °C for 6 h



Summary

- The nucleation of γ' (Ni₃Al) precipitates in normal Ni-Al alloys and γ (Ni-Al solid-solution) precipitates in "inverse" Ni-Al alloys offer the best prospects ever of investigating homogeneous nucleation during precipitation from solid solution
 - Pre-aging treatments can be used to eliminate compositional variations in the parent matrix phase;
 - Pre-aged normal and inverse alloys can aged at small undercoolings to produce small volume fractions of precipitates, thereby minimizing the influence of excess vacancies on diffusion;
 - The important parameters needed to compare steady-state nucleation rates and incubation times, namely interfacial free energy and chemical diffusion coefficients, are known within reasonable limits for both normal and inverse alloys;
 - The Gibbs free energies of mixing of both phases is perhaps not known with the same certainty, but this is always an issue;
 - Just In case data on elastic constants and lattice mismatch might be useful in studies of nucleation in Ni-Al alloys...



There are now well-constrained estimates of the following quantities as well, just in case they are needed:



The "Equilibrium" Elastic Constants for Binary Ni-Al Alloys from 800 to 1200 K



Ni-Al Data: S.V. Prikhodko, J.D. Carnes, D.G. Isaak and A.J. Ardell, *Scripta Mater*. <u>38</u> (1997) 67; S.V. Prikhodko, J. D. Carnes, D. G. Isaak, H. Yang and A. J. Ardell, *Metall. Mater. Trans.* A <u>30A</u> (1999) 2403



Temperature dependence of the equilibrium lattice mismatch in 4 binary Ni-X alloys





Ferromagnetic Curie temperature as a function of AI concentration in Ni-AI solid solutions



In principle, this offers the prospect of measuring the AI content of γ nuclei

A.J. Ardell, Acta Metall. 16 (1968) 511



• Musings about diffuse γ/γ' interfaces---might these muddy the waters?



Results of Monte Carlo computer simulation experiments on planar γ/γ' interfaces



Y. Mishin, Acta Mater. 52 (2004) 1451



A.J. Ardell and V. Ozolins, Nature Mater. 4 (2005) 309



Composition profiles across $\gamma\!/\!\gamma'$ interfaces in a ternary Ni-Cr-Al alloy measured using APT







Long-range-order profile across a γ/γ interfaces in René 88 measured using HRTEM



R. Srinivasan, R. Banerjee, J.Y. Hwang, G.B. Viswanathan, J. Tiley, D.M. Dimiduk and H.L. Fraser, PRL 102 (2009) 086101



 γ/γ' interfaces must become sharper the smaller the particle, e.g. as the critical radius is approached. γ' particles a few unit cells in size should have sharp interfaces to be regarded as particles of a new phase

Thanks for putting up with me!



ALPHA/BETA TITANIUM ALLOYS REVISITED

Adam Pilchak, *Air Force Research Laboratory, Materials and Manufacturing Directorate, Wright Patterson Air Force Base, OH 45433, USA adam.pilchak@wpafb.af.mil

Dipankar Banerjee, Department of Materials Engineering, Indian Institute of Science, Bangalore 5601012, India. <u>dbanerjee@materials.iisc.ernet.in</u>

Jim Williams, Department of Materials Science and Engineering, The Ohio State University, Columbus, OH-43210, USA williams.1726@osu.edu

Joint AFRL/AOARD/LLNL Workshop on Nucleation during Solid-Solid Phase Transformations in Metallic Systems: Current Understanding and Future Directions Maui, Hawaii May 2 - 7, 2010

PHASE DIAGRAM



- A simple phase diagram underlies all useable titanium alloy structure
- inclusion free, two phase structures at different length scales ranging from the nanometric to the micrometer scale

 $\boldsymbol{\beta}$ - Stabilizer Concentration

STRUCTURE





- The starting cast/beta cooled structure is dominated by alpha morphologies determined by interface and strain energies between the two phases –the burgers relationship
- Grain boundary and alpha and related sideplates emanating from it can dominate the structure under some conditions

THE BURGERS RELATIONSHIP[0001]//[1-10][1-210]//[111][10-10]//[112]12 variants of alpha from the beta to alpha transition











Bands of microtexture are often evident in thermomechanically processed titanium alloys

Texture of the entire cross-section of a fatigue specimen would reveal weak texture, less than 2x random.

MICROTEXTURE
DWELL FATIGUE CRACK ORIGINS

Courtesy: Amit Bhattacharjee, OSU and DMRL

OIM on layer 3 after removing 59 μm from layer 1







DWELL FATIGUE LIFE DEBIT IN TI-6242

At room temperature! Courtesy: Amit Bhattacharjee, OSU and DMRL

Material	Load Ratio	σ_{max}/σ_{YS}	Dwell Time (minutes)	Plastic Strain –to- Failure (ϵ^{pl}_{f})	Nf (Cycles to failure)	Dwell Life Debit
Ladish P1 (Low microT)	0	0.954	2 0	3.0 % 0.6 %	8803 51235	6
Ladish P1 (Low microT)	0	0.954	2 0	2.8 % 1.5 %	11946 47906	4
Ladish P2 (High microT)	0	0.955	2 0	3.8 % 2.0 %	1303 22991	18
Ladish P2 (High microT)	0	0.915	2 0	2.3 % 1.0 %	3074 45843	15
Ladish P3 (β forged)	0	0.957	2 0	3.2 % 0.5%	10846 30020	3
Ladish P3 (β forged)	0	0.957	2 0	B767 com	pressor dis	c failure
Retired Impeller $(\alpha/\beta \text{ forged})$	0	0.933	2 0	1		
Retired Impeller $(\alpha/\beta \text{ forged})$	0	0.933	2 0		THU	

STRUCTURE





- The starting cast/beta cooled structure is dominated by alpha morphologies determined by interface and strain energies between the two phases –the burgers relationship
- Grain boundary and alpha and related sideplates emanating from it can dominate the structure under some conditions

GRAIN BOUNDARY NUCLEATION: A BRIEF HISTORY

Winterbottom, Acta Met, 1967 The equilibrium nucleus shape at a grain boundary

Lee and Aaronson , Acta Met 1975



Luo and Weatherly, Acta Met 1989

fcc-bcc in the Ni-Cr system

Preferred nucleation at boundaries where habit plane in one grain is close to boundary plane

Growth into neighboring irrationally oriented grain



FIG. 9. Variation of $\Delta G^*/\Delta G_s^*$ with ϕ , where ΔG_s^* is the the critical free energy of formation for an unfaceted grain boundary allotriomorph ($\sigma_{aa}/\sigma_{a\beta} = 1.05$).

GRAIN BOUNDARY ALPHA: A BRIEF HISTORY





Fig. 14—Schematic illustration showing the rule of variant selection in grain boundary α precipitation.

Furuhara, Tagaki, Watanabe and Maki, Met Trans 1996

Variant selection rules:

Burgers OR with one of the two grains

Close packed directions in gb plane Low misorientation from Burgers OR in neighbouring grain

Bhattacharya, Viswanathan, Denkenberger, Furrer, and Fraser, Acta Materiala, 2003

R. Banerjee *, D. Bhattacharyya, P.C. Collins, G.B. Viswanathan, H.L. Fraser Acta Materialia 52 (2004) 377–385

Stanford and Bate, Acta Materiala, 2004

Bhattacharya, Viswanathan and Fraser, Acta Materiala, 2007



If adjacent beta grains share a common (110) pole, then those (2)variants with (0001) parallel to this (110) are selected

GRAIN BOUNDARY ALPHA and INTRAGRANULAR ALPHA

Greater detail in the variant selection process to understand specific choices among the 24 variants

EBSD for better statistics, 3d information including grain boundary normal

The variant selection process when the habit plane/close packed direction parallel to gb plane condition is not on offer ?

What happens at triple points ?

Why do colony structures (of parallely oriented variants) form ?



THE IDEAL GRAIN BOUNDARY ALPHA

THE IDEAL GRAIN BOUNDARY ALPHA Terrace (10-10)//(112), or macroscopic habit plane parallel to boundary plane?

ΤΡ1 β1									
<111>		<110>		<112>		<335>		BF	
111	85.40	1-10	88.00	11-2	5.70	335	80.20	10.3	
1-1-1	65.60	101	76.20	-1-21	28.70	3-5-3	79.50		
-1-1-1	85.40	01-1	28.40	2-1-1	62.10	533	78.80		
111	85.40	10-1	32.40	-12-1	58.10	353	77.90		
1-11	61.90	011	78.20	-2-11	31.00	-53-3	76.00		
-111	65.60	01-1	28.40	-2-1-1	76.60	5-3-3	63.00		
1-11	61.90	10-1	32.40	121	75.40	-35-3	58.76		
-111	65.60	110	50.20	-11-2	49.80	3-3-5	55.80		
1-11	61.90	110	50.20	-112	52.80	-33-5	52.70		
-1-11	15.20	011	78.20	-21-1	80.90	-5-33	26.40		
-1-11	15.20	101	76.20	-121	84.40	-3-53	24.40		
-1-11	15.20	1-10	88.00	112	75.20	-3-35	3.30		
			TP	1β2					
<111>		<110>		<112>		<335>		BF	
-1-11	73.90	1-10	87.90	112	16.50	-3-35	88.30	3.7	
-111	70.70	01-1	86.10	-2-1-1	19.90	5-3-3	85.10		
1-11	67.10	10-1	88.20	121	23.10	-35-3	81.50		
-1-11	73.90	101	31.90	-121	63.40	-3-53	67.60		
-1-11	73.90	011	35.70	-21-1	59.30	-5-33	66.70		
1-1-1	70.70	101	31.90	-1-21	65.70	3-5-3	65.00		
-111	70.70	110	38.70	-11-2	58.00	3-3-5	63.20		
1-11	67.10	011	35.70	-2-11	64.40	-53-3	61.00		
1-11	67.10	110	38.70	-112	60.80	-33-5	60.10		
111	4.70	10-1	88.20	-12-1	86.60	353	18.10		
-1-1-1	4.70	01-1	86.10	2-1-1	89.90	533	15.00		





THE IDEAL GRAIN BOUNDARY ALPHA

The observed variant has the lattice invariant line and macroscopic habit plane in the gb plane

Normal to ledge ten

1000114/111018

1105-orellu 1218

1112010/111118

133518

Macroscopic Broad face

Latice invariant line

SPECIAL BOUNDARIES

TP2/BETA1										
111		110		112		335		BROAD FACE		
-1-11	31 5	101	61	-121	89.8	-3-53	34.5	77.5		
1-1-1	73 3	101	61	-1-21	36.7	3-5-3	85.5	31.9		
111	47 3	10-1	45.7	-12-1	83.2	353	46.6	86.9		
1-11	83 5	10-1	45.7	121	47.2	-35-3	86.6	46.7		
1-11	83 5	110	20.4	-112	74.6	-33-5	87.5	73.4		
-111	73 3	110	20.4	-11-2	88.9	3-3-5	74.1	84.8		
-1-11	31 5	1-10	75.8	112	65.3	-3-35	43.8	51.9		
111	47 3	1-10	75.8	11-2	48.4	335	60.6	35.7		
1-11	83 5	011	76.2	-2-11	19.2	-53-3	69.8	27.6		
-1-11	31 5	011	76.2	-21-1	65	-5-33	21.45	78.7		
-1-1-1	47 3	01-1	63.1	2-1-1	57	533	37.6	69		
-111	73 3	01-1	63.1	-2-1-1	34.8	5-3-3	61.1	43.6		

					TP2/BETA3						
	BROAD FACE		335		112		110		111		
	62.8	66 2	-3-53	57.1	-121	39.8	101	73 9	-1-11		
	71.1	58 9	3-5-3	63.8	-1-21	39.8	101	65.1	1-1-1		
	78.8	16 9	353	87.2	-12-1	84.9	10-1	12.7	111		
Near ideal	12.6	87 9	-35-3	20.6	121	84.9	10-1	73 8	1-11		
	62.8	66.1	-33-5	57	-112	39.9	110	73 8	1-11		
actual	71	58 8	3-3-5	63.6	-11-2	39.9	110	65.1	-111		
	12.5	88	-3-35	20.5	112	85	1-10	73 9	-1-11		
	78.8	16 8	335	87	11-2	85	1-10	12.7	111		
	71.9	68 5	-53-3	66.9	-2-11	31.3	011	73 8	1-11		
	71.8	68.6	-5-33	66.9	-21-1	31.3	011	73 9	-1-11		
	70.1	23.1	533	84.2	2-1-1	89.9	01-1	12.7	-1-1-1		
	15.7	79 2	5-3-3	27.6	-2-1-1	89.9	01-1	65.1	-111		



SPECIAL BOUNDARIES: the chosen variant is Burgers oriented to both grains, in preference to a near ideal variant

THE RANDOM BOUNDARY

	TP1 beta1										
<111>		<110>		<112>		<335>		BF			
1-1-1	53.8	101	63.5	-1-21	47.7	3-5-3	66.20	28.76			
111	61	10-1	29.5	-12-1	85	353	63.40	36.03			
-111	53.8	01-1	68.9	-2-1-1	43.7	5-3-3	41.30	36.98			
1-11	75.9	10-1	29.5	121	64.7	-35-3	82.60	49.34			
-1-1-1	61	01-1	68.9	2-1-1	37.1	533	48.10	54.30			
1-11	75.9	110	36.3	-112	57.3	-33-5	84.20	56.44			
-1-11	33.8	011	86.3	-21-1	56.5	-5-33	19.50	58.09			
-1-11	33.8	101	63.5	-121	70.6	-3-53	43.70	61.64			
1-11	75.9	011	86.3	-2-11	14.6	-53-3	61.50	65.16			
111	119	1-10	59.3	11-2	44.7	335	73.00	70.88			
-1-11	33.8	1-10	59.3	112	77.3	-3-35	41.40	78.18			
-111	53.8	110	36.3	-11-2	92.8	3-3-5	56.00	78.76			



TP1 beta3										
<111>		<110>		<112>		<335>		BF		
-1-11	62.1	101	48.00	-121	54.8	-3-53	72.00	40.6		
-111	64.5	110	33.50	-11-2	69.9	3-3-5	70.70	43.59		
1-11	64.5	110	83.20	-112	26.5	-33-5	50.20	47.52		
1-11	48.5	011	56.60	-2-11	59.5	-53-3	59.00	48.92		
111	48.5	1-10	80.50	11-2	43.1	335	34.60	50.18		
111	45.6	10-1	56.60	-12-1	62.9	353	55.60	52.03		
-1-1-1	62.1	01-1	33.50	2-1-1	73.1	533	67.60	57.14		
-111	64.5	01-1	44.30	-2-1-1	56.6	5-3-3	73.70	59.49		
-1-11	45.6	1-10	48.00	112	75.6	-3-35	52.00	63.86		
1-1-1	62.1	101	80.50	-1-21	29.8	3-5-3	48.00	65.45		
-1-11	48.5	011	44.30	-21-1	77.1	-5-33	54.10	66.51		
1-11	45.6	10-1	83.20	121	45.2	-35-3	31.40	67.64		

The chosen variant neither has the nearest habit plane to the boundary, nor the growth direction in the boundary The chosen variant is oriented to thebeta1 grain but has no relationship to beta2 No relationship to the variants at the other grain boundaries



WIDMANSTATTEN ALPHA SIDEPLATES AND DISCONTINUOUS PRECIPITATION

GRAIN BOUNDARY ALPHA AND SIDEPLATE GROWTH AT SPECIAL BOUNDARIES



INTRAGRANULAR STRUCTURE



S.C. Wang M. Aindow M.J. Starink Acta Materialia (2003)

- self -accommodation structures?
- 144 combinations of two variants220 combinations of three variants495 combinations of 4 variants
 - the colony structure dominates at low undercooling and high growth rate conditions

COLONY STRUCTURES



Does the colony structure originate from elastic interactions?

C. Shen, J.P. Simmons, and Y. Wang ,2006

Focus: grain boundary nucleation

Is the grain boundary alpha structure(observed variants) nucleation dominated or growth dominated

we can devise critical experiments to test this then determine the variant selection process under different conditions identify the configuration at earliest stages of gb alpha formation

Can you predict variant selection at grain boundaries?

Do we have a statistical data base? What is the structure of the nucleus: coherent or semicoherent? Do elastic stresses play a role? Can we understand stress relaxation at grain boundaries? How accurately do we need to know relevant surface energies, especially grain boundary energy as a function of grain boundary orientation?

What is the origin of the colony structure at low undercooling and high growth rate conditions?

elastic stresses alone?

coupling of stresses and diffusion fields?

RECRYSTALLISATION AND STRUCTURE

thermomechanical processing controls distribution and morphology of the two phases



Strategies to eliminate microtexture:

Control colony size prior to processing (section thickness effects)
Large superplastic deformation (extensive grain rotation)
Friction stir processing of surfaces (extensive shear and rotation)



PROCESSING AND STRUCTURE the initiation of 'recrystallisation'





Weiss and co., 1986

subgrain formation in alpha, beta percolation

BETA RECRYSTALLISATION

The {110} poles of the beta grains are often clustered together and the relative rotation about these poles is about 60°



The nucleation of recrystallisation in multiphase materials?

Early Stages of Nucleation and Growth of ω Precipitates within the β Matrix of Titanium Alloys

Rajarshi Banerjee

Center for Advanced Research and Technology Department of Materials Science and Engineering University of North Texas Denton, Texas, U.S.A.



Acknowledgements

S. Nag, A. Devaraj, and S. Srivilliputhur University of North Texas Denton, Texas, U.S.A.

S. Rajagopalan* and H. L. Fraser Ohio State University Columbus, Ohio, U.S.A. *Now at Exxon Mobil





Financial support for this work has been provided by the National Science Foundation and the Air Force Research Laboratory



Nucleation and Growth of ω and α in β matrix

Two types of sites for nucleation of α:

- \succ Inter-granular at β grain boundaries
- Intra-granular sites

Intra-granular heterogeneous nucleation sites within β grains:

- Instabilities within the β matrix *compositional and structural*
- Uniformly distributed ω precipitates
- Phase separation leading to $\beta + \beta'$ compositional partitioning

Alloy systems:

Commercial system TIMETAL 5553: Ti-5Al-5Mo-5V-3Cr-0.5Fe (all wt%, Ti-5553) or Ti-9Al-2.5Mo-5V-3Cr-0.5Fe (at%) - nominal alloy composition

```
≻Ti-18wt%Mo (or Ti-9at%Mo)
```

Ti-5553 Quenching from Above T_{β}

$\beta \rightarrow \beta + \omega$ (Precipitation of the ω phase)



SAD [011] $\beta + \omega$ reflections at 1/3{112} positions



Dark Field TEM micrograph Athermal ω phase in as-quenched condition

Ti-5553 Nucleation site for $\alpha - \omega$ precipitates



SAD [113] $\beta + \omega$ reflections at 1/3{112} positions + α reflections at 1/2{112} positions

Nag, Banerjee, Srinivasan, Harper, and, Fraser, *Acta Mater.* (2009)

Dark-field TEM image from $\omega + \alpha$ reflections



 α lath nucleating on ω precipitate



Annealing at 400° C for 2 hours - TEM





Dissolution of ω precipitates Coarsening of α precipitates



Nag, Banerjee, Srinivasan, Harper, and, Fraser, Acta Mater. (2009)



Nucleation and Growth of ω in β matrix

- Early stages of formation of athermal ω precipitates when quenched from above β - transus temperatures
 - Formation of ω nuclei structural collapse of {111} β planes
 - Compositional partitioning
- Isothermal growth of ω precipitates during aging post quenching
 - 3D morphology of ω precipitates
 - $\succ Compositional partitioning between \beta and \omega during isothermal growth$

Alloy system studied:

Model alloy Ti-18Mo (wt%) or Ti-9Mo (at%) - binary alloy

Goal: Better understanding of $\beta-\omega$ transformation by coupling advanced microscopy techniques: *Aberration-corrected high-resolution HAADF-STEM – TITAN 3D atom probe - LEAP (nanoscale compositional analyses)*

ω (hexagonal) Precipitation in β (bcc) Phase of Titanium





{111} planes of bcc β
Stacked as abcabca...
0th and 3rd planes are
undisplaced
1st and 2nd planes
collapse into one plane



J. C. Williams, D. de Fontaine, and, N. E. Paton, Metall. Trans. A, 4, 2701 (1973) D. de Fontaine, N. E. Paton, and, J. C. Williams, Acta Metall., 19, 1153 (1971)

Ti-9Mo (β solutionized + water quenched)



- Nanometer scale homogeneously distributed athermal ω preciptates
- Diffraction patterns *Intensity maxima developing at 1/3 and 2/3* {112}βlocations – early stages of formation of ω preciptates

HRTEM of Ti-18Mo (β-soln. + water-quenched)



- HRTEM images early stages of formation of ω precipitates
- Change in structure between β matrix and ω precipitates is clearly visible

HAADF-HRSTEM of Ti-9Mo (water-quenched)



- Aberration-corrected HAADF-HRSTEM images early stages of formation of ω nuclei
- Darker contrast in HAADF image corresponding to ω nuclei Diffusional partitioning of Mo? independent analysis using 3D atom probe required
- Displacement of atomic columns visible


Quantifying the Displacement of {111} β Planes



Partial collapse of $\{111\} \beta$ planes within ω nuclei – *still not complete collapse*

Complete collapse corresponds to displacement of the {111} planes by 0.5d₂₂₂ *Maximum displacement observed = 0.2d*₂₂₂



3D atom probe: Ti-9Mo (β solutionized + water quenched)

Overall Composition: Ti = 91.22at%, Mo = 8.78at%

01 9 0 9-01- /

20

\$

8

8 N

8

20

4

80

Ti = 92% isosurface (blue) Mo = 8% isosurface (red)

Some compositional partitioning of Ti and Mo based on iso-concentration surfaces

Statistical relevance needs to be determined



3D atom probe: Composition fluctuations in Ti-9Mo

Overall Composition: Ti = 91.22at%, Mo = 8.78at%

Compositional fluctuations in Mo content



Interconnected network of marginally Ti-rich regions *Phase separation in* β *matrix prior to* ω *nucleation?* Statistical relevance – *Frequency distribution plot for 100 atom bins of Ti*





Ti-9Mo β solutionized + WQ - RDF function



Ti- Ti bonds favored over **Ti-Mo** bonds -> Clustering tendency Average alloy composition: Ti-8.8at%Mo **Phase separation into ~Ti-6at%Mo and ~Ti-9at%Mo regions**

Ti-9Mo (β soln. + WQ + 475° C/30



Growth and coarsening of ω precipitates as compared with as-quenched
 Sharper intensity maxima at 1/3 and 2/3 {112}β – structurally well developed ω precipitates



 \succ Ledges present at ω/β interfaces

 \triangleright Displacive component involved in the isothermal $\beta \rightarrow \omega$ transformation

HRTEM of Ti-9Mo (β soln. + WQ + 475° C/30 mins)



Fraction of d₂₂₂

0.27

0.31

0.35

0.35

0.

Full collapse of β planes within ω – *fully developed \omega structure*



A. Devaraj et.al., Scripta Materialia,61, 701-704 (2009).

- **>** Mechanism of $\beta \rightarrow \omega$ transformation not completely understood
- β solutionized and quenched Ti-18Mo exhibits fine scale ω embryos
 - Different stages of the collapse of {111} β planes *aberration corrected HAADF-STEM*
 - Clear evidence of Ti-Ti clustering from 3D atom probe 3D atom probe
 - \blacktriangleright Phase separation in β matrix prior to ω formation?
- Subsequent annealing at 475° C/30mins
 - well-developed ω precipitates complete collapse of {111} β
 planes
 - \succ Substantial partitioning of Mo between β and ω



> Mo-depleted pockets with compositions $< T_0$ undergo displacive collapse to form ω nuclei

> Is the displacive collapse complete within ω nuclei?

Schematic G – η plots for Ti-Mo $\mathsf{X}_{\mathsf{Mo}} < \mathsf{X}(\mathsf{T}_0) \approx 6 \; \mathsf{at}\%$ $X_{Mo} > X(T_0) \approx 6 \text{ at}\%$ ß ω G G ω β η η > Mo-depleted pockets with $X_{Mo} \approx 0$ E compositions $< T_0$ undergo displacive collapse to form ω nuclei G **Extent of displacive collapse can** be incomplete within ω nuclei – composition dependent amplitude ω of phonon wave?

η

Questions

- Is phase separation in β matrix mandatory for ω formation in Ti-18Mo (or Ti-9at%Mo)?
- Though ω forms via a displacive collapse of {111} β planes, why is the collapse arrested (partial collapse) in quenched ω embryos
 - Is the extent of collapse dependent on the composition of the ω pocket? Why?
- Is there a mixed-mode displacive-diffusional transformation involved in the formation of isothermal ω precipitates?
- We use first-principles calculations using the Vienna Ab Initio Simulation Package (VASP) coupled with the Nudged Elastic Band (NEB) transition path technique to investigate the β to ω transformation in Ti-Mo system



 \succ Nucleation of α precipitates appears to be assisted by ω precipitates

- > Nucleation of α precipitates at composition far-from equilibrium minimal partitioning of alloying additions between α and β phases
- Structurally well-defined α platelets exhibiting *hcp* crystal structure formed in the early stages *ledges at the* α/β *interface*

Nag, Banerjee, Srinivasan, Harper, and, Fraser, Acta Mater. (2009)



Structural Evolution in the Process of Nucleation

Srikumar Banerjee Department of Atomic Energy, India

Pacific Rim Workshop on Nucleation

May 2-7, 2010

What is Nucleation

 Creation of an assembly of atoms which 'represent' the product phase

All symmetry elements of the product appear \implies At least one unit cell

"Structural Evolution in the Nucleation Process"

means

Probing the embryonic structures appearing during the evolutionary process ahead of nucleation

Outline

- How fluctuations in the earlier stage lead to the formation of nuclei ?
 - Chemical Ordering
 - Magnetic Ordering
 - Displacement Ordering
 - Mixed mode-displacement + chemical ordering

Nucleation mediated by defects

Ordering – Chemical, ferromagnetic, ferroelectric



Ordering & Clustering Processes



Ordering & Clustering tendencies are dictated by sign & magnitude of pair & multisite interaction potentials (J's) Disordered

Evolution of Ordering: Discrete Mode (Nucleation & Growth)

















Continuous vis-à-vis Discrete Transformations

Fluctuations – large in extent – small in degree

classical example – continuous decomposition of a solid solution through

- SPINODAL DECOMPOSITION
- Fluctuations small in extent large in degree
- NUCLEATION & GROWTH

GIBB'S Criterion

Originally proposed for unmixing of fluids

If $\partial^2 G/\partial^2 c < 0$: No thermodynamic barrier for continuous phase separation

First & second order transitions: Landau Plots



First & second order transitions: Landau Plots



First & second order transitions: Landau Plots



Special-Point Ordering

A wide range of phenomena related to order–disorder and magnetic transitions can be explained using the symmetry properties of the pair potentials (Vij).

Landau Theory of Continuous Phase Transitions

- The symmetry, H, of the ordered phase should be a subset of symmetry, G, of the disordered phase $(\textbf{H} \subset G)$
- The ordering wave vector must be located at the **special points** of the Brillouin zone of the disordered phase, where symmetry elements intersect at a point.
- It must not be possible to find combinations of three members of the star* of the ordering wave vector satisfying rule II which will sum (vectorially) to a reciprocal lattice vector (No 3rd order invariant)

Special points are the points in the Brillouin zone where $\nabla V(k) = 0$ For simple structures: two symmetry elements intersect at these points

*The star associated with a vector \mathbf{k} is a set of vectors obtained by applying all the Rotation or rotation-inversions on \mathbf{k} .

Special Points, Stars and Ground State Structures

\mathbf{k} -vector Star	Members	Brillouin Zone Points	Ordering Structure
(000)	[000]	Г	
(100)	[100]	Н	B2
$\left< \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \right>$	$\begin{bmatrix} \frac{1}{2} \\ \frac{1}{2} \\ \frac{1}{2} \end{bmatrix} \begin{bmatrix} \overline{\frac{1}{2} \\ \frac{1}{2} \\ \frac{1}{2} \\ \frac{1}{2} \end{bmatrix}}$	Р	<i>B</i> 32
$\left< \frac{1}{2} \frac{1}{2} 0 \right>$	$\begin{bmatrix} \frac{1}{2} \frac{1}{2} 0 \end{bmatrix} \begin{bmatrix} \frac{1}{2} 0 \frac{1}{2} \end{bmatrix} \begin{bmatrix} 0 \frac{1}{2} \frac{1}{2} \end{bmatrix}$		
	$\left[\frac{1}{2}\frac{1}{2}0\right] \left[\frac{1}{2}0\frac{1}{2}\right] \left[0\frac{1}{2}\frac{1}{2}\right]$	Ν	AB

k-vector Star	Members	Brillouin Zone Points	Ordering Structure
(000)	[000]	Г	
(100)	[100] [010] [001]	x	$L1_2, L1_0$
$\left<1\frac{1}{2}0\right>$	$\left[1\frac{1}{2}0\right] \left[\frac{1}{2}01\right] \left[01\frac{1}{2}\right]$	w	A_2B_2
$\left< \frac{1}{2} \frac{1}{2} \frac{1}{2} \right>$	$\begin{bmatrix} \overline{1} \ \overline{1} \ 0 \end{bmatrix} \begin{bmatrix} \overline{1} \ \overline{2} \ 0 \overline{1} \end{bmatrix} \begin{bmatrix} 0 \overline{1} \ \overline{2} \ 0 \end{bmatrix}$ $\begin{bmatrix} \overline{1} \ \overline{2} \ \overline{2} \end{bmatrix} \begin{bmatrix} \overline{1} \ \overline{2} \ \overline{2} \end{bmatrix} \begin{bmatrix} \overline{1} \ \overline{2} \ \overline{2} \end{bmatrix}$ $\begin{bmatrix} \overline{1} \ \overline{2} \ \overline{2} \end{bmatrix} \begin{bmatrix} \overline{1} \ \overline{2} \ \overline{2} \end{bmatrix}$	L	$L1_1$

For fcc structure

For bcc structure

Free Energy of Ordering

The configurational free energy, in the simple mean-field theory, can be expanded in a Taylor series about the homogeneous state:

$$\Delta F = F_M - F_o = \frac{N}{2} \sum_h F''(h) |X(h)|^2 + \frac{N}{3!} f_o''' \sum_{h,h',h''} X(h) X(h') X(h'') \delta(h+h'+h'';g) + \frac{N}{4!} f_o'''' \sum_{h,h',h'',h'''} X(h) X(h') X(h'') X(h''') \times \delta(h+h'+h''+h''';g)$$

X(h): Fourier transform of concentration deviation from the mean value, C_o. V(h): Fourier transform of pair interaction function, V(r). **g** :reciprocal lattice translational vector,.

$$F''(h) = 2V(h) + \tau / q_o$$

As amplification rate $\alpha(h)$ of a Fourier Component *h* is proportional to F"(*h*), is expected to mimic the V(*h*) function at relatively lower temperatures

Amplification Rates for Clustering and Ordering Instabilities

Amplification rate $\alpha(h)$ vs. a/λ for a system inside the spinodal.

The λ_c is the critical wavelength and λ_m is the one receiving the maximum amplification

Amplification rate $\alpha(h)$ vs. a/λ for a Ordering system below the critical temperature



HE Cook, D de Fontaine and JE Hilliard, Acta metal. Vol. 17, 765 (1969).

Lattice Wave Descriptions of Homogeneous Transformations

Nature of Wave	Long Wavelength	Short Wavelength
Replacive	Spinodal Clustering	Spinodal Ordering
Displacive	Martensitic	Omega
Electric	Ferroelectric	Antiferroelectric
Magnetic	Ferromagnetic	Antiferromagnetic








Structural Description of <1 1/2 0> Ordering

- Microdomain model
 Isostructural microdomains
 Multiple microdomains
- Subunit cell structure
- Concentration wave
- Concentration wave packets



<1 ½ **0**>

1/5 <420>



Concentration wave packets Microdomains

Evolution of Order in Ni₄Mo under Electron Irradiation



<1 ¹/₂ 0> & 1/5 <420> diffraction spots remain linked During evolutionary stages

S Banerjee, K Urban, M. Wilkens Acta Met., 32 (1984) 299

Evolution of Order in Ni₃Mo under Electron Irradiation

495K





^{480s} <

240s

to

695K to



30s



Diffuse intensity links superlattice reflections associated with $<1 \frac{1}{2} 0 > (N_2M_2),$ $1/5 <420 > (N_4M) \&$ $1/3 <420 > (N_2M)$ ordering

Damage rate: 10⁻³ dpa/s

S. Banerjee, U.D. Kulkarni, K. Urban, Acta Met., 37 (1989) 35

Superimposition of <1 ½ 0> Concentration Waves



(B)

U.D. Kulkarni, S. Banerjee, Acta Met, 36 (1988) 413

DPs Showing Evolutionary Stages of Ordering in Ni₃Mo



Experimental

Simulated

Simulated pattern	# of clusters	Ratio
d	N ₂ M ₂ (16), Pt ₂ Mo (16), Pt ₂ Mo (4)	1:1:4
е	N ₂ M ₂ (16), D1a (16), D1a (4)	1:1:4
f	D1a (16), Pt ₂ Mo (16), D1a (4), Pt ₂ Mo (4)	1:2:2:4

S. Banerjee, U.D. Kulkarni, K. Urban, Acta Met., 37 (1989) 35

Coexistence of N₄M and N₂M tiles in Ni₁₀Mo₄Cr



A Arya, G.K. Dey V. Vasudevan S. Banerjee Acta Mater., 50 (2002) 3301

Coexistence of Competing Superlattices in Ternary Ni₁₀Mo₄Cr



Ni₄(Mo,Cr) & Ni₂(Mo,Cr) domains



DO₂₂ Plates Forming at T≈873 K

A Arya, G.K. Dey, V. Vasudevan, S. Banerjee, Acta Mater., 50 (2002) 3301

Coherent Arrangement of Superlattice Tiles



U.D. Kulkarni, S. Banerjee & S.D. Kulkarni, Acta Met., 41 (1993) 1283



Formation Energies of fcc-based Superstructures of Ni-Mo System Under NN & NNN Approximation Using DFT-LDA based TB-LMTO Method



Mo Concentration (at%)

Landau Plots: <1 1/2 0> vs. 1/5 <420> ordering



A Arya, S. Banerjee, G.P. Das, I. Dasgupta, T. Saha-Dasgupta & A. Mookerjee, Acta Mater. 49, 3575 (2001).



Mater. 49, 3575 (2001).







Monte Carlo Simulation: V(k) Maps for v_i , i = 1, 10

3D ensemble size of 128x128x32 points

Random selection of atom pair & calculation of energy change for a possible exchange based on pair interaction energies, v_i , i = 1, 10

Computed diffraction patterns (CDPs) are a FFT spectrum of atom positions in the ensemble for compariosn with experimentally obtained SAEDPs



Monte Carlo Simulation of Ordering in Ni₄Mo Alloy

Ni₈₀Mo₂₀Alloy

MALLA LAZINA A A

U D Kulkarni, Acta Mater. Vol. 52, 2721 (2004).

V(k) Maps & Early Stage CDPs



Interference of Concentration Waves Leading to the Formation of Nuclei

- Very early stage of the transformation is dictated by the second derivatives of free energy w.r.t. order parameter.
- Formation of localized clusters can be a consequence of superimposition of concentration waves. The resulting embryo can be viewed as the transformation nucleus. Superimposition of waves leads to a positive third order coefficients in LL, the condition necessary for ordering of the first kind.
- Phase locking causes localization of the nucleation event
- The final structure is determined by the deepest well in the free energy space.

Analogy with Magnetic Ordering

Analogy with Magnetic Ordering

Naturally Occurring Layered Compounds: Ca_{2.5-x}La_xSr_{0.5}GaMn₂O₈

"Locking" of 2D & 3D short-range Antiferromagnetic Ordering over extended temperature range





Naturally Occurring Layered Compounds: Ca_{2.5-x}La_xSr_{0.5}GaMn₂O₈





$Ca_{2.45}La_{0.05}Sr_{0.5}GaMn_{2}O_{8}$







Coupling of Chemical phase separation and magnetic ordering

Coupling between the magnetic and chemical ordering lead to the formation of different degree of two dimensional and three dimensional ordering.

Free energy vs composition plot for a temperature below the bicritical point.

The paramagnetic A2_p phase separates into two phase: one rich in magnetic component (A2) and the other lean (B2).

The former orders into Antiferromagnetic and the later remains paramagnetic Paramagnetic phase



Displacive Ordering

Displacive Ordering: $\beta \rightarrow \omega$ Phase Transformation



Omega Transformation



Longitudinal Displacement Waves



Landau plots explaining Dual phase β + ω structure

HREM Image of Aged Zr-20Nb Alloy



G.K. Dey, R. Tewari, S. Banerjee, G. Jyoti, S.C. Gupta, K.D. Joshi, S.K. Sikka, Acta Materialia, 52, (2004),

Diffuse ω Patterns


Diffuse ω Patterns



Embryonic ω



Embryonic ω





HREM of Diffuse ω



G.K. Dey, et al., Acta Materialia, 52, (2004),



Irradiation Induced ω Formation

300 K



t = 0 s450 K







t = 0 s

120 s

240 s

Zr-20Nb, 1 MeV

2Mev

15 Seconds60 Seconds120 Seconds480 Seconds473K

30 Seconds120 Seconds480 Seconds600 Seconds573K



Time of exposure (sec.)

Deviation Parameter Estimation

Comparison of Deviation Parameter in Irradiation and Thermal $\boldsymbol{\omega}$



Both streak length and scatter in it are more pronounced in irradiation

Deviation is more pronounced in case of irradiation indicating more fraction of higher $\boldsymbol{\omega}$ structural units

Stacking of $\boldsymbol{\omega}$



Sinkler and Luzzi Acta Mater.







Coupling Between Displacive and Concentration Ordering: Ordered ω Phases

Ordered ∞ Structures - B8₂ and D8₈



Spinodally Decomposed Microstructure in Zr₃Al-Nb Alloys

<100 > Concentration modulation

-Solute lean regions transform into $\boldsymbol{\alpha}$

-Solute rich regions transform to B8₂ (ordered ω)





40nm











Ordered Omega Phases in Zr – Al – Nb



Tewari et al. Acta Mat.(1999)

Atomic Correspondence of the β and D8₈ Phases



Tewari et al. Acta Mat. (1999)

Symmetry Tree



Tewari et al. Acta Mat(1999)

Nucleation mediated by defects

Nucleation in a Complex Metallic Alloy- AIPdFe

C₂ phase (FCC) of AI-Pd-Fe has large lattice parameter of 15.52Å and number of atoms per unit cell is 250.

Exhibits plasticity through dislocation motion

Energy of such dislocations will be very high as $E \propto |b|^2$



Source: Michael Feuerbacher

Source: CMA website

Dislocations are stabilized by nucleation of a defect phase

Novel Defects in AI-Pd-Fe Complex Alloy



Dislocation showed the presence of nano sized defect phase in the matrix on compressive stress field of dislocation Self energy of the dislocation is substantially reduced by the nucleation of the defect phase

Possible Mechanism of fcc to bcc Transformation



It can be seen that minor flip flop of structural motifs converts the fcc to bcc with a net drop of 1% lattice parameter.

Micro-mechanical Model of the bcc Defect as Infinite Elliptical Cylinder Running Along the Core of the Dislocation



 σ_{ii}^{o} stress due to dislocation at any given point

- \mathcal{E}_{ij}^{p} constrained stress at the point due to defect,
- σ_{ij} eigen strain of the defect
- $\hat{\mathcal{E}}_{ij}$ equivalent eigen strain

Driving Force for bcc defect formation, elastic interaction energy, given by

$$W_{1} = -\frac{1}{2} \int_{\Omega} \sigma_{i}^{o} \mathcal{E}_{i}^{*} dD - \frac{1}{2} \int_{\Omega} \sigma_{i} \mathcal{E}_{i}^{p} dD - \int_{\Omega} \sigma_{i}^{o} \mathcal{E}_{i}^{p} dD$$

Simulation of Defect Induced Strain



nucleation could indeed reduce over energy of dislocation substantially

The predicted size and strain of the defect phase are close to experimental values

Summary

Homogeneous fluctuations in concentration, displacement and spin correlation mark the early stage of several transformations.

Interference of waves of different types results in localization of a transformation process

Cluster/motif mimicking partial symmetry elements of product are created.

Spatial correlations of such clusters allow establishment of all symmetry elements of the product: Nucleation sets in

Incommensurate Structures & Lock-in Transitions

- If critical star does not correspond to a special point or critical wave vectors are not commensurate with vectors of the reciprocal lattice – LL rules fail
- If any incommensurate wave vector, k', is not very different from commensurate wave vector, k_c, one may obtain third & higher order terms in Landau functional with the possibility that sum of several vectors of the relevant star is equal to a vector of reciprocal lattice.
- > This yields additional terms in Landau Functional called 'Umklapp' terms.
- It may so happen that quadratic term favors the incommensurate state; while the quartic term favors the commensurate state. Below Tc, the latter terms dominate & one may expect an incommensurate-commensurate transition; where phase φ in the functional gets locked-in at that point.
- > This is a **lock-in transition** driven by Umklapp terms in Landau functional.
- These may be treated by Soliton Theory



Coupling of Atomistic and Meso-scale Phase-field Modeling of Rapid Solidification

James Belak, Patrice Turchi, Milo Dorr, David Richards, Jean-luc Fattebert, Daniel Orlikowski, Michael Wickett, and Fred Streitz Lawrence Livermore National Laboratory

AFRL/AOARD/LLNL Workshop on Nucleation

May 2-7, 2010, Maui, HI, USA

"Art (simulation) is the lie that helps us see the truth." -Picasso

Lawrence Livermore National Laboratory, P. O. Box 808, Livermore, CA 94551 This work performed under the auspices of the U.S. Department of Energy by Lawrence Livermore National Laboratory under Contract DE-AC52-07NA27344

All roads lead to Tamman



G. Tammann, Z. Andrg. Chemie 214 (1933) 407, "The States of Aggregation," by Gustav Tammann, Translated by Robert Mehl (Van Nostrand 1925), KJMA: Kolmogorov (1937), Johnson-Mehl (1939), Avrami (1941)

Lawrence Livermore National Laboratory



Quotes

"... in general it seems to me that it is through particular problems which can be subjected to experimental verification or compared with natural phenomena that most advances are made." - G.I. Taylor

"Nothing can be learned as to the physical world save by observation and experiment, or by mathematical deductions from data so obtained." - P.G. Tait

"Crystals are like people---it's the defects in them that make them interesting." - F.C. Frank

"Art (simulation) is the lie that helps us see the truth." - Picasso



Focus: Pressure-driven Solidification of Metals

Explicitly model the details of the solidification process

- Extend highly successful molecular dynamics (MD) results to longer times and larger lengths
- Determine structure and stability of metals under dynamic loading conditions
- Identify relevant time scales (from ps to μs) for solidification
- Locate non-equilibrium phase boundaries
- Describe rate and path dependence of approach to final structure



Pressure

- Corroborate details with experiments where possible
- Condense results into phenomenological models which can be incorporated into hydrocodes



Molecular Dynamics (MD) are now large enough to model the initiation of realistic microstructure



Simulations suggest novel in situ x-ray scattering experiments using emerging sources such as LCLS

Streitz et al. Phys. Rev. Lett. 2006

Lawrence Livermore National Laboratory



Quantification of local order from the atom positions

- Utilize locally averaged combinations of spherical harmonics
- For L = 6, local structure described by a 13 component vector q_l.
- Dot product defined to measure correlation between atomic sites. Q₆ defined by summing these over neighbors.
- Truly a local quantity assigned atom by atom

21+1 components of $v\vec{q}_{l}(t)$ or

given by:

$$q_{lm}(i) = \left\langle Y_{lm}(\hat{r}_{ij}) \right\rangle_{N_i}$$

Define dot product:

$$\vec{q}_l(i) \cdot \overset{\mathsf{r}}{q}_l(j) \equiv \sum_{m=-l}^l q_{lm}(i) \ q^*_{lm}(j)$$

Then

$$Q_{l}(i) = \frac{\left\langle q_{l}(i) \cdot q_{l}(j) \right\rangle_{N_{i}}}{\frac{r}{q_{l}(i) \cdot q_{l}(i)}}$$

Steinhardt *et al.* PRB **28**, 784, 1983 ten Wolde *et al.* PRL **75**, 2714,1995

Distribution of Local Order Parameter: Q₆



- L=6 allows excellent discrimination between the liquid and solid.
- Identifies mixed phase region
- Does not discriminate between crystal phases
- Define liquid for Q < 0.67
- Define solid for Q > 0.87
- Define interface for 0.67 < Q < 0.87

The time-scale for nucleation is fast



Molecular dynamics simulations provide initial structure for continuum phase evolution model



MD will not get us to the hydrodynamic time of interest



Phase Field Modeling (PFM) will get us to the hydrodynamic time of interest

What is Phase Field modeling? - PFM



- Each color represents a different value of the phase field ϕ (solid orientation)
- Free energy describes how colors interact and evolve
- Accuracy depends on fidelity of physics in the equations

Thermodynamic representation of phase (or "color") everywhere

Evolution Equations

$$F(P,T) = \int dx \left\{ \left| \nabla \vec{\phi} \right|^2 + f(\vec{\phi}, P, T) + \dots \right]$$

$$\frac{\partial \vec{\phi}}{\partial t} = -\Gamma \frac{\delta F}{\delta \vec{\phi}} + noise$$

We propagate the phase order parameter using the molecular dynamics

100 nm Atoms Coarse Graining Phase time

Validate micro-physics within Phase Field Model with MD simulations that overlap in time and space

Lawrence Livermore National Laboratory
What is Phase Field modeling? Basic Equations

Phase Field modeling is time-dependent Ginzburg-Landau theory



Total Free Energy of multi-phase material



Local Free Energy Density $f(\phi) \approx \phi(1-\phi)(1+\phi)$



Kinetic Equation with Thermal Noise

Lawrence Livermore National Laboratory

Order Parameter

 $\phi(r,t)$

What does a crystallographic-aware phase-field model of polycrystal solidification look like?

Pusztai et al., have proposed a 3D quaternion-based phase-field model

- Represents crystal orientation with quaternion order parameter
- Quaternions are widely used to analyze crystallography of polycrystal interfaces
- Quaternion algebra is fast, efficient, avoids singularities, ...

Free Energy	$F = \int \left[\frac{\varepsilon_{\phi}^{2}}{2} \nabla \phi ^{2} + f(\phi, c, T) + HT[1 - p(\phi)] \left(\sum_{i} (\nabla q_{i})^{2} \right)^{1/2} \right] d^{3}r$
Evolution	$\frac{\partial q_i}{\partial t} = -M_q \frac{\delta F}{\delta q_i} + \zeta_i = M_q \left[\nabla \cdot \left(D \frac{\nabla q_i}{ \nabla q_i } \right) - 2\lambda q_i \right] + \zeta_i$

Where q_i is the quaternion order parameter, M_q is the associated mobility and ζ is the fluctuation in q.

We have implemented the Pusztai model in our 3D AMR code

- · Enhance energy functional to represent energetics of grain boundaries
- Crystal symmetry aware quaternion mathematics
- Extend energy functional to include elasticity and alloy concentration

Refs: T. Pusztai, G. Bortel, and L. Granasy, "Phase field theory of polycrystalline solidification in three dimensions," Europhys. Lett, 71 (2005) 131-137; R. Kobayoshi and J.A Warren, "Modeling the formation and dynamics of polycrystals in 3D," Physica A 356 (2005) 127-132.

Quaternions are used extensively to represent rotations, e.g. in computer graphics (games)

Complex numbers have the form, a + ib, and multiplying by $e^{i\theta}$ produces rotation by an angle θ in the complex plane



Quaternions have the form, a + ib + jc + kd, where $i^2=j^2=k^2=ijk=-1$. A rotation about the unit vector \hat{n} by an angle θ can be computed using the unit quaternion:



$$(s,v) = (\cos(\frac{\theta}{2}), \hat{n}\sin(\frac{\theta}{2}))$$

We assign to each atom a quaternion that best represents the local value of the Q6 order parameter with the smallest rotation from a reference unit cell.

The associated quaternion enables quick calculation of the rotation between two misoriented grains (c.f. Reed et.al Acta Cryst. (2004) A60, 263-277)

Model Problem: Single Spherical Grain (2D with scalar orderparameter)





We obtain strong scalability to thousands of processors by leveraging LLNL's investment in parallel computing (e.g. SAMRAI)



Representation of MD Data onto the AMR Grid Hierarchy - 2D example





MD nucleated microstructure onto the micro-second hydro time-scale with the crystallographic quaternion model



Phase Order Parameter



While significant grain coarsening has occurred on the microsecond scale, the microstructure is far from log-normal



Focus: Pressure-driven Solidification of Metals

Explicitly model the details of the solidification process

- Extend highly successful molecular dynamics (MD) results to longer times and larger lengths
- Determine structure and stability of metals under dynamic loading conditions
- Identify relevant time scales (from ps to μs) for solidification
- Locate non-equilibrium phase boundaries
- Describe rate and path dependence of approach to final structure



Pressure

- Corroborate details with experiments where possible
- Condense results into phenomenological models which can be incorporated into hydrocodes

Becker-Doring-Volmer (Gibbs-Thomson)

$$\Delta G = \gamma 4 \pi R^2 - \Delta G_v \frac{4}{3} \pi R^3$$
$$\frac{\partial \Delta G}{\partial R} = \gamma 8 \pi R - \Delta G_v 4 \pi R^2 = 0$$
$$R_c = \frac{2\gamma}{\Delta G_v} = \frac{2\gamma}{\Delta S_f (T_m - T)}$$



Fig. 5.2 The variation of ΔG with r for a homogeneous nucleus. There is an activation energy barrier ΔG^* .



Molecular Dynamics simulation of nucleant evolution



Lawrence Livermore National Laboratory

20

Growth Kinetics obeys a "C" curve









How do we know MD with an empirical potential gets the "kinetics" anywhere right?



In Situ Kinetics

- Material "State"
- Kinetics = Change of "State"
 - Phase (Strain): Observable = Diffraction
 - Strength (Defects/Dislocations): Observable = Diffuse Scattering
 - Damage (Voids/Porosity): Observable = Imaging/Tomography + Small-Angle Scattering



Molecular dynamics (MD) simulations are used to model *Nucleation (homogeneous and beyond)*



Simulations suggest novel in situ x-ray scattering experiments using emerging sources

Lawrence Livermore National Laboratory

Streitz et al. Phys. Rev. Lett. 2006



What is spallation fracture?



Spallation fracture is an internal rupture process when strong shock waves interact in solids. The dynamic fracture of ductile metals occurs through the nucleation, growth and linking of microscopic voids.

NDE: Synchrotron-based 3D X-ray Tomography



The region surrounding the voids shows increased hardness (strength)



The enhanced hardness (strength) in the metal surrounding the voids suggests a plastic zone with higher dislocation content.

The microbeam-Laue diffraction in single x-tal AI with voids reveals several distinct zones located at different depth



Lawrence Livermore National Laboratory



Small angle x-ray scattering (SAXS) directly measures sub-micron void distribution



Analysis of SAXS/SANS data yields information on particle size, spacing and morphology



Conclusions: Questions

- What is a nucleant?
- How does it become a nucleus? (lag time)
- How do we NDE characterize the initial nucleant, their potencies, their transition into a nucleus, and the kinetics in situ and non-destructively?
- How does the picture change (if at all) when thermodynamics are changed? (stress/pressure)
- Can we "calculate" the nucleation curve "ab initio"?





Coarse Graining for Time

Timescales **Deterministic** part timestep Δt

> **Stochastic part** timestep dt





Strategy

Deterministic part

integrate as usual with timestep Δt

Stochastic part

replace with stochastic term with timestep Δt integrate as usual with timestep Δt











Fisher-Tippett Theorem (1928)

Space of initial distributions of $\boldsymbol{\xi}$



Frechet

$$\lim_{t \to \infty} (1 - F(t \xi)) / (1 - F(t)) = e^{-\gamma}$$

$$Pr(\xi_{max} < \beta) = e^{-e^{-1/b_n} (\beta^{-\gamma})}$$

Gumbel

$$\lim_{t \to \infty} \frac{(1 - F(t + \xi r(t)))}{(1 - F(t))} = e^{-\xi}$$

$$Pr(\xi_{max} < \beta) = e^{-e^{-1/b_n}(\beta - a_n)}$$

Weibull

•••

$$\lim_{t \to \infty} (1 - F(t \xi)) / (1 - F(t)) = e^{-\gamma}$$

x has a maximum possible value

$$Pr(\xi_{max} < \beta) = e^{-e^{-1/b_n}((-\beta)^{\gamma})}$$

determined by tails of ξ distribution invertable: random numbers can be generated directly use this as Langevin noise

UnstableRegion Time dependent distribution

Phase Field Simulation of Critical Nuclei Morphology in Solid State Transformations

Qiang Du

Department of Mathematics, Penn State University With Lei Zhang, Long-Qing Chen

Joint ARL/AOARD/LLNL Workshop on Nucleation During Solid-Solid Phase transformations, Maui, 2010

Nucleation

Nucleation: a process where clusters of atoms form via fluctuations in a meta-stable phase with those beyond certain critical threshold grow.

Significance: predicting nucleation rate and its dependence on composition and temperature is an interesting and challenging problem in materials sciences, given the complex energy landscape in high dimension and the unstable nature of saddle/transition points. Phase field/diffuse interface critical nuclei morphology

Outline

- 1. Problem/Objective
- 2. Approach/Algorithms
- 3. Examples
 - Single nonconserved order parameter
 - Single conserved order parameter
 - Two order parameters
- 4. Observation/Conclusion



I. Problem/Objective

The importance of the problem and the challenging computational nature motivated our recent studies:

- to build rigorous mathematical foundation to the models of nucleation;
- to develop algorithms needed in the computational study of nucleation in solid state transformations;
- to develop methods and codes for the computation of the critical nucleus shape/size and nucleation rate.

II. Approach: Critical nuclei morphology via the large deviation principle

- Large Deviation Principle: for a Langevin system, the most probable transition path between local energy wells, in the zero fluctuation limit and without any time limitation, is the minimum energy path (MEP) connecting the equilibria.
- The lowest energy barrier is given by the largest energy difference reached on the MEP



• Points on the MEP with the highest energy: saddle points (unstable critical point) with a minimax property



II. Approach: diffuse interface/phase field

- We work with the diffuse interface/phase field framework.
- We develop/implement suitable algorithms (minimax method/constrained string method) to gather information on the saddle point and minimum energy path (transition pathway) which helps to determine the nucleation rate and the critical nuclei profiles
- We incorporate the gathered information into phase field simulations of the nucleation and growth processes



II. Approach: Phase Field and Nucleation

In existing phase field simulations, nucleation mostly are treated either via Monte Carlo or classical theory

Classical theory: nucleus shares the same thermodynamic properties as the equilibrium with assumed shape *a priori*.

Non-classical: Cahn-Hilliard, diffuse interface

ergy

Free energy

$$\int_{\Omega} \left(\frac{\epsilon}{2} |\nabla \phi|^2 + \frac{1}{4\epsilon} (\phi^2 - 1)^2 + \lambda (3\phi - \phi^3) \right) dx$$

 λ : driving force ϵ : interfacial width





II. Approach: Cahn-Hilliard theory

Nonclassical theory of Cahn-Hilliard considers bulk and interfacial energy contributions but not the contribution due to the anisotropic elasticity energy







Profile of critical nuclei,

consistent with classical theory in the thin interface limit **II. Approach: Energy and Nucleation**

Solid state phase transformations:

Energy contribution: bulk + interfacial + elastic

$$\int_{\Omega} \left(\frac{\epsilon}{2} |\nabla \phi|^2 + \frac{1}{4\epsilon} (\phi^2 - 1)^2 + \lambda (3\phi - \phi^3) \right) dx + E_e$$

Misfit Elastic Energy: via Khachaturyan's micro-elasticity theory

$$\frac{\beta}{2} \int_{\widehat{\Omega}} \frac{dk}{(2\pi)^d} B(n_k) |\widehat{\eta}(k) - \widehat{\eta}_0(k)|^2$$



III. Examples: first, a proof of concept

- A single order parameter: isotropic/anisotropic elastic energy
- Elastic energy

$$\frac{\beta}{2} \int_{\widehat{\Omega}} \frac{dk}{(2\pi)^d} B(n_k) |\widehat{\eta}(k) - \widehat{\eta}_0(k)|^2$$

$$\begin{split} B(n) &= 3(c_{11} + 2c_{12})\epsilon_0^2 - (c_{11} + 2c_{12})^2\epsilon_0^2.\\ &\frac{1 + 2\zeta s(n) + 3\zeta^2 n_1^2 n_2^2 n_3^2}{c_{11} + \zeta(c_{11} + c_{12})s(n) + \zeta^2(c_{11} + 2c_{12} + c_{44})n_1^2 n_2^2 n_3^2}\\ \zeta &= (c_{11} - c_{12} - 2c_{44})/c_{44} \quad \text{elastic anisotropic factor}\\ s(n) &= n_1^2 n_2^2 + n_1^2 n_3^2 + n_2^2 n_3^2 \end{split}$$

 $\epsilon_0 \text{ lattice mismatch, } \Omega \text{ periodic cell } \widehat{\Omega} \text{ reciprocal domain} \end{split}$

Georgia
II. Approach: energy functionals for diffuse/sharp interface

$$E_{\epsilon}(\eta) = \int_{\Omega} \left[\frac{\epsilon}{2} |\nabla \eta|^2 + \frac{1}{4\epsilon} (\eta^2 - 1)^2 + \frac{\lambda}{2} (3\eta - \eta^3)\right] dx$$
$$+ \frac{\beta}{2} \int_{\widehat{\Omega}} \frac{dk}{(2\pi)^d} B(n_k) |\widehat{\eta}(k) - \widehat{\eta}_0(k)|^2$$

Sharp interface limit: $\varepsilon \rightarrow 0$

$$\begin{split} E_0(v) &= \int_{\Omega} (\frac{\sqrt{2}}{3} |\nabla v| + \lambda v) + \frac{\beta}{2} \int_{\widehat{\Omega}} B(n) |\widehat{v}(k) - \widehat{\eta}_0(k)|^2 \\ \text{if } v \in BV(\Omega, \{\pm 1\}), \text{ and } E_0(v) = \infty \text{ otherwise.} \end{split}$$

Center for Computational Materials Design (CCMD) www.cond.psu.cfu Zhang-Chen-D. 2007

II. Approach: saddle point of diffuse interface energy

$$E_{\epsilon}(\eta) = \int_{\Omega} \left[\frac{\epsilon}{2} |\nabla \eta|^2 + \frac{1}{4\epsilon} (\eta^2 - 1)^2 + \frac{\lambda}{2} (3\eta - \eta^3)\right] dx$$
$$+ \frac{\beta}{2} \int_{\widehat{\Omega}} \frac{dk}{(2\pi)^d} B(n_k) |\widehat{\eta}(k) - \widehat{\eta}_0(k)|^2$$

With periodic boundary condition:

a) the energy satisfies the Palais-Smale condition;b) for small ε, there is a nontrivial saddle point connecting two trivial local minima

Zhang-Chen-Du 2008 J. Sci. Comp., Barrett lecture special issue



II. Approach: numerical method

Most of our algorithms for computing MEP/Saddle point are based on:

Minimax method : classical calculus of variation. *Rabinowitz 1986; Choi, 1993; Lin, 1997; Zhou, 2001*

String method: more recently developed W. E, W. Ren and E. Vanden-Eijnden, 2002

With suitable modifications (for conserved variables) and high order, adaptive implementation



III. Example: first, a proof of concept

• A single order parameter describing structural difference with an anisotropic elastic energy



Critical nuclei with increasing elastic energy contributions (Zhang, Chen, Du, PRL, 2007, Acta Mater., 2008)



III. Example: effect of anisotropic elasticity – 2d

Zhang-Chen-Du PRL 2007



Elastic energy contribution (changing β)



III. Example: simulations of 3D critical nuclei



Saddle point branches with varying elastic energy contribution



III. Example: most probable 3D nuclei morphology





III. Exampleat riticato in the conserved field

- Composition profile: **c**(**x**)
- Total free energy increase:

$$E_{total}(c) = \int_{\Omega} [f^{c}(c) + \frac{\alpha}{2} |\nabla c(x)|^{2}] dx + \beta \cdot E^{elastic}$$

where
$$f^{c}(c) = f(c) - f(c_0) - \frac{\partial f(c)}{\partial c}|_{c=c_0}$$

and
$$f(c) = \frac{1}{4}(c^2 - 1)^2$$



• The volume constraint is

 $\int [c(x) - c_0] dx = 0$

MEP gets modified when one or more constraints are imposed



III. Example: an illustration of constrained MEP

- **3-D potential energy** $E(x, y, z) = (1 x^2)^2 + y^2 + 2z^2$ with the constraint $x^2 + y^2 + z^2 - 1 = 0$
- Containing the two energy wells of E: $(\pm 1,0,0)$



MEP without constraint and constrained MEP

 We developed a constrained string method via augmented Lagrange multipliers to compute MEP

III. Example: nucleation with a single conserved field

• Critical nucleus, equilibrium solution, and MEP



Zhang, Chen, Du, Comm. Comp. Phys., 2010



III.Examples effect of elastic energy

• MEP with increasing elastic energy in conserved field



Critical nuclei morphology can be very different from that of the equilibrium!

• Compare with critical nuclei in the non-conserved field



	Center for Computational Materials Design (CCMD)	
-	www.comd.pou.edu	

III. Example: nucleation involving multiple order parameters

- Extensions to more complicated systems, in particular, those with multiple order parameter fields
 - A case of two non-conserved phase field order parameters representing different orientation variants
 - A case of a conserved field (composition) with a nonconserved field (order parameter):
 - θ ' precipitates in Al-Cu alloys
 - γ' precipitates in Ni-Al alloys



III.Example: two non-conserved order parameters Type 1: Critical nucleus

Type I: Equilibrium state

Equilibrium state





III.Example: two non-conserved order parameters



First type of critical nuclei

Third type of critical nuclei







Second type of critical nuclei

Center for Computational Materials Design (CCMD)
www.comd.psu.edu

III.Example: One conserved + one nonconserved

Applications are now considered for Ni-Al and Al-Cu alloys involving both conserved and nonconserved fields

Example (in progress): θ' precipitates in Al-Cu alloy, with data from L.Q. Chen/T.W. Heo

Parent (Al-Cu s	phase solid solution (α ph	nase))
	Coherent θ' precipitate	Semi- coherent

Parent phase (Al solid solution) → η = 0 c = c_{eq.matrix} III.Example: integrating dynamic phase field simulations with diffuse-interface nuclei computation

Solving dynamic Allen Cahn equations, using a classical nulceation event sampling (Simmons 2000), but with nucleation via diffuse interface nuclei computation



Heo, Zhang, Du, Chen, 2010 Scripta Mat.



III.Example: integrating dynamic phase field simulations with diffuse-interface nuclei computation

The growth of a single nucleus via Allen-Cahn



62400 time steps 78000 time steps





III.Example: phase field simulations with diffuse-interface nuclei and classical nucleation theory

Comparison with the phase transformation kinetics using the classical nucleation and normal growth theory and the Kolmogorov-Johnson-Mehl-Avrami equation



IV. Observation/Conclusion: phase field/diffuse interface

• Phase field type methods are insensitive to topological changes (advantage/deficiency?



- How about the detection/control of topology of the implicitly defined surfaces? (or for collecting statistics)
- Formulae were developed to detect /control topology change in shape transformation via Euler number
- Providing interesting statistics of large scale simulations and connecting geometry with topology: the key is to effectively estimate curvatures in the diffuse interface framework Du -Liu-Wang SIAM Appl Math 2005



IV. Observation: Euler-Poincare index in Phase Field

• In 3d:
$$\chi = \frac{1}{4\pi(b-a)} \int_{\Omega_a^b} |\nabla \phi|^{-1} \Lambda(M) d\Omega$$

$$M = c(\nabla^2 \phi - (\nabla |\nabla \phi|^2 \cdot \nabla \phi) |\nabla \phi|^{-4} \nabla_i \phi \nabla_j \phi$$





• In 2d:

$$\chi = rac{1}{2\pi(b-a)} \int_{\Omega^b_a} F d\Omega$$

$$F = c(
abla^2 \phi + (
abla |
abla \phi|^2 \cdot
abla) |
abla \phi|^{-2}/2$$

Phase-field Based Euler number!

Georgia Tech Simplified versions possible Du–Liu-Ryham-Wang 2007 CMS

IV Conclusion

Goals: rigorous mathematical description and robust algorithms and codes for nucleation in solid-state transformation.

Progress: methods to compute diffuse-interface critical nuclei; some stand-alone codes for single order parameter already available; demonstration of integration with phase field dynamic simulations.

Collaborators: L. Zhang, L.-Q. Chen, T.W. Heo **Thanks:** support from NSF-ITR (2002-2007), NSF-IUCRC CCMD



A coarse grained derivation of the Phase Field equations

A. Finel

Q. Bronchart , Y. Le Bouar,

Laboratoire d'Etudes des Microstructures ONERA-CNRS, Chatillon

Why Phase Field modeling (1)?

→ Mesoscopic modeling:

- large scale simulation (µm³)
- easy to incorporate elastic effects
- extended to dislocation dynamics (plasticity), fracture, voids ...
- polycrystals, grain boundaries...

Microstructures in γ/γ'





Sequiera et al, Scripta Met. Mat., 30(1994)

Formation and ageing of bimodale microstructures in γ/γ^{\prime}



Boussinot et al., Acta Mat (2009)

from Chellman et al. (1989)

Directional coarsening under external stress (rafting): phase field + viscoplasticity

 $10 \ \mu m$



Phase Field + viscoplasticity Gaubert et al., Phil. Mag. (2010)

Caron et al. (2002)

Why Phase Field modeling (2)?

→ Mesoscopic modeling:

- large scale simulation (µm³)
- easy to incorporate elastic effects
- extended to dislocation dynamics (plasticity), fracture, voids ...
- polycrystals, grain boundaries...

Ex : Shape memory alloys: the martensitic transition



- \rightarrow Phase Field simulation in Ti-Ni:
 - heterogeneous precipitation of R phase along a screw dislocation
 - elastic accomodation
 - thermoelastic equilibrium

Questions \rightarrow Transitions driven by fluctuations : nucleation - how well can the Phase Field method reproduce nucleation ? - how to intruduce fluctuations in a consistent way? - what is the meaning of a local free energy density ? - which fluctuations are already incorporated into this free energy density ?

Q. Bronchart, Y. Le Bouar, and A. Finel, Phys. Rev. Lett., vol.100 (2008) 015702

Introduction (1)

\rightarrow basics of the Phase Field method:

- consider a simple miscibility gap:
- "good" order parameter: concentration field: c(r,t)







Phase Field method: how to get the basic equation (1)

 \rightarrow Starting point: Microscopic master equation

- atomic configuration:

$$\mathcal{C} = (\dots p_i \dots p_j \dots) \qquad p_i = 0 \text{ or } 1 \text{ if } A \text{ or } B \text{ on site } i$$

- kinetic model: direct exchange between A and B on 1st neighbor sites

$$\frac{\partial P(\mathcal{C})}{\partial t} = -\sum_{i,j}^{*} W(\mathcal{C} \to \mathcal{C}^{ij}) P(\mathcal{C}) + \sum_{i,j}^{*} W(\mathcal{C}^{ij} \to) P(\mathcal{C}^{ij})$$

- transition probability:

local mechanism:

direct exchange through saddle point (G. Martin, Phys. Rev. B, 1990)

$$W(\mathcal{C} \to \mathcal{C}^{ij}) = \theta \exp{-\beta(2E_{saddle} - h_i^A(\mathcal{C}) - h_j^B(\mathcal{C}))} \,\delta(p_i)\delta(p_j - 1)$$

 $h^A_i(\mathcal{C})$: interaction energy between site i and the other sites if i is occupied by atom A

if pair interactions only:
$$h_i^A(\mathcal{C}) = \sum_i V_{ij}^{AA} p_j + V_{ij}^{AB} (1 - p_j)$$







Phase Field method: how to get the basic equation (4)

 \rightarrow Master equation becomes:

$$\frac{\partial P(\tilde{C})}{\partial t} = -N_d \frac{a}{d} \theta e^{-2\beta E_{col}} \sum_{n,m}^* e^{\frac{\beta}{2}(g_n^A(\tilde{C}) + g_n^B(\tilde{C}) + g_m^A(\tilde{C}) + g_m^B(\tilde{C}))} e^{\frac{\beta}{2} \frac{a}{d}(\mu_m(\tilde{C}) - \mu_n(\tilde{C}))} P(\tilde{C}) + (gain term)$$
mobilities
$$\frac{g_n^A(\tilde{C}) = \frac{1}{N_d} \sum_{i \in n} kT \ln < \delta(p_i(C)) \exp \beta h_i^A(C) >_{C/\tilde{C}} g_n^B(\tilde{C}) = \frac{1}{N_d} \sum_{i \in n} kT \ln < \delta(p_j(C) - 1) \exp \beta h_j^B(C) >_{C/\tilde{C}} g_n^B(\tilde{C}) = \frac{1}{N_d} \sum_{i \in n} kT \ln < \delta(p_j(C) - 1) \exp \beta h_j^B(C) >_{C/\tilde{C}}$$
"alloy chemical potential":
$$\mu_n(\tilde{C}) = g_n^B(\tilde{C}) - g_n^A(\tilde{C})$$

$$\rightarrow \text{ look for the equivalent dynamical equation on C (evolution of a single system)}$$

- Kramers-Moyal expansion to 2nd order in a/d to get a Fokker-Planck equation
- Itô calculus to get the equivalent Langevin equation





How to compute the chemical potentials ? (1) (*i.e. Ginzburg-Landau free energy*)

 \rightarrow Chemical potentials $g_n^A(\widetilde{C})$ and $g_n^B(\widetilde{C})$ are function of all the cell concentrations c_n :

$$g_n^A(\tilde{\mathcal{C}}) = g_{homo}^A(c_n) + \ H^A(c_n) ||\hat{\nabla}c_n||^2 + K^A(c_n)\hat{\nabla}^2 c_n \ + \dots$$

 $\rightarrow g_n^A(\widetilde{\mathcal{C}})$ and $g_n^B(\widetilde{\mathcal{C}})$ enter into the mobilities and in the alloy chemical potential :

$$l_{mn}(\widetilde{\mathcal{C}}) = \exp(-2\beta E_{saddle}) \exp\frac{\beta}{2} (g_n^A(\widetilde{\mathcal{C}}) + g_n^B(\widetilde{\mathcal{C}}) + g_m^A(\widetilde{\mathcal{C}}) + g_m^B(\widetilde{\mathcal{C}}))$$
$$\mu_n(\widetilde{\mathcal{C}}) = g_n^B(\widetilde{\mathcal{C}}) - g_n^A(\widetilde{\mathcal{C}})$$

 \rightarrow If cells large enough : inhomo. components can be neglected in mobilities, but are crucial in the alloy chem. potential

- for the mobilities:

$$g_n^A(\widetilde{\mathcal{C}}) \simeq g_{homo}^A(c_n)$$

- for the alloys chemical potential:

$$\mu_n(\widetilde{\mathcal{C}}) \simeq g^B_{homo}(c_n) - g^A_{homo}(c_n) + H(c_n) ||\hat{\nabla}c_n||^2 + K(c_n)\hat{\nabla}^2 c_n + H(c_n)\hat{\nabla}^2 c_n + H(c_n)\hat{\nabla}^2$$








How to compute the stiffness coefficient ? ex: simple cubic lattice

 \rightarrow Next: stiffness coefficient $\lambda^d(c_n)$

$$\mu_n^d(\widetilde{\mathcal{C}}) = \mu_{homo}^d(c_n) - \lambda^d(c_n)\hat{\nabla}^2 c_n + \frac{1}{2}\frac{\partial\lambda^d(c_n)}{\partial c_n}||\hat{\nabla}c_n||^2$$

 $\rightarrow \lambda^{d}(c_{n})$ governs (in part) fluctuations between cells

 \rightarrow Monte Carlo analysis of gaussian fluctuations between cells:



$$\lambda^d(\bar{c}) = A + B \ \bar{c}(1 - \bar{c})$$



• \rightarrow precipitation for c = 0.17 ($c_0 < c < c_s$): nucleation and growth mechanism....









On the influence of the coarse-graining size



Comparison with classical nucleation theory





Conclusion

\rightarrow "exact" procedure:

- the Phase Field as a coarse-graining procedure
- a stochastic equation with a "simple" noise term (fluctuation theorem)
- Mobility M(c) and noise correlations depend on coarse-graining size and on local concentration
- "stiffness" constant $\lambda^d(c)$ depend on coarse-graining size and on local concentration
- no arbitrary parameters !!!
- reproduces equilibrium fluctuations as well as precipitation
- no need for an extra nucleation flux

\rightarrow needed if:

- nucleation and growth mechanism (activated processes)
- if complete time scale needed

Cool New Stuff with Experiments

A. Genç^{*}, S. Rajagopalan, [#]G. Thompson, [@]R. Banerjee, ^{**}J. Ringnalda, ^{\$\$}D. McComb, ^{##}C. Dwyer and Hamish L Fraser

Center for the Accelerated Maturation of Materials Department of Materials Science and Engineering The Ohio State University Columbus, OH *Now at Intel Inc., Hillsboro, OR *Now at University of Alabama (Tuscaloosa) @Now at University of North Texas **Now at FEI Company \$\$Imperial College, London ##Monash University, Clayton, Vic, Australia

> Jay's Fun Workshop 2010 *Ka'anapali, Maui*



Thanks to Jay and other organizers and research sponsors Integrated Computational Materials Science & Engineering

Integrated Computational Materials Science and Engineering

- The art and practice of predicting materials' behavior and properties
- A discipline changing activity
 - e.g., 2009 Gordon Research Conference on Physical Metallurgy (topic: ICSME)
 - From 65 attendees at the last Phys. Met. Conference (GRC threatened to terminate conference) to an attendance maximized (160) for the current one
 - 60 graduate students
 - 2nd highest funding of all GRCs (only medical GRC higher!!)



Demonstrates tremendous level of interest and points the way forward





= CAMM Center for the Accelerated Maturation of Materials

<u>Aim</u>: To develop research tools for the accelerated insertion of new materials and optimization of existing ones.

<u>Method</u>: This is done by developing and integrating computational modeling and simulation with advanced materials characterization

Integration between modelers and materials characterization folks

Multiscale modeling – integration over length and time scales

Integration from ab-initio to industrial practice







T H L OH SI STATE

Linear lengthening and parabolic thickening kinetics, and tip radius and tip velocity from simulations all match analytical solutions.

α/β -Ti alloys – Side-plates vs. Basketweave Structure



Needed in both cases: details of nucleation mechanisms, variant selection, etc.





Cool New Stuff with Experiments

- •Topics:
- •Integration modeling with experiments
- •Useful recent characterization techniques
- •Limitations with experimental techniques
 - •sample preparation
 - •compositional analysis
- •What are we (OSU/CAMM) doing?





3D information

- Why do we need 3D information ?
 - Superposition
 - Projection



Drawing by John O'Brien, The New Yorker Magazine (1991)

-=CAMM



3D Characterization Tools

Solute distributions β phase separation β -ribs $-\alpha$ -laths - $_$ secondary $\alpha _$ Equiaxed α $\boldsymbol{\omega}$ Reconstruction Depth (z) 200 µm RoboMet 50 µm FIB kV & Z BSE 150 SE 125 nm z resolution (nm) 100 50 (S)TEM Tomography 100 150 200 500 µm 50 50 µm 3 um Resolution of x,y plane (nm) Atom Probe x,y Area of reconstruction Т · Н · Е UNIVERSITY

Robo.Met-3D™



DualBeam (FIB/SEM)TM



*Raw Robo.Met-3D*TM*Data Set*



120 μm x 90 μm x 120 μm



Ti – 6246 Grain Boundary α Interrogation



300, ~50 nm slices taken through a 40 μ m x 20 μ mx 15 μ m volume







Promise of Aberration-Corrected Electron Microscopy



Spatial Resolution Improvements using Aberration-Corrected Electron Microscopy



PHYSICAL REVIEW B 79, 081405(R) (2009)

Oxygen octahedron reconstruction in the SrTiO₃/LaAlO₃ heterointerfaces investigated using aberration-corrected ultrahigh-resolution transmission electron microscopy

C. L. Jia,^{1,*} S. B. Mi,¹ M. Faley,¹ U. Poppe,¹ J. Schubert,² and K. Urban¹ ¹Institute of Solid State Research and Ernst Ruska Centre for Microscopy and Spectroscopy with Electrons, Forschungszentrum Jülich, D-52425 Jülich, Germany ²Institute of Bio- and Nanosystems and Centre of Nanoelectronic Systems for Information Technology, Forschungszentrum Jülich, D-52425 Jülich, Germany

- Measurement of atom (column) location to within a few picometers precision
- To image in this manner (NCSI) requires thin foils of thickness ≈ 4nm
- What is the effect of foil thickness on relaxations?
- Need for computational assistance to interpret correct result

Ti-L near-edge : monochromated STEM-EELS





But, not possible to perform spatially resolved monochromated EELS in our system: - need more signal – the high brightness gun

Comparison of monochromated vs. non-monochromated EELS





• Need for computational assistance to interpret correct result, i.e., electronic structure

Cool New Stuff with Experiments

- •Topics:
- •Integration modeling with experiments
- •Useful recent characterization techniques
- •Limitations with experimental techniques
 - •sample preparation
 - •compositional analysis
- •What are we (OSU/CAMM) doing?





Low Energy Ar Milling



UNIVERSITY



500V Ar Ion Image of FIB lamella at $15^{\rm o}$ beam incidence angle

CAA

Focused Ar beam source : $10-12\mu m$ beam size

Low energy : 2000-50V

Low angle: 0° to +30°/-10°

Conventional ion mill damage in Ni-based superalloy (Renè 88DT)



5kV Ar milling

+15%/-10%



500V Low energy Ar ion milling





Phenomenological Correlation between depth of amorphous damage and atomic displacements



Phenomenological Correlations – our results for Ge



Tells us about removing the amorphous damage but the secondary defects may still be present



Cool New Stuff with Experiments

- •Topics:
- •Integration modeling with experiments
- •Useful recent characterization techniques
- •Limitations with experimental techniques
 - •sample preparation
 - •compositional analysis
- •What are we (OSU/CAMM) doing?





XEDS – Spatial Resolution and Quantification EPMA From Chris Kiely AEM or SEM **0.1** μm 10 nm 1 nm 1 Å? 100 nm 10 nm Volume excited Volume excited Volume excited ~ 10-8 µm³ ~ 10-₅ μm³ ~ 1 µm³ FEG Thermionic source source Spatial resolution Analytical sensitivity Improving STEM-XEDS Maps Increase dwell time of probe (more X-rays collected) Increase current (more X-rays generated) Multivariate statistical analysis (MSA) of spectrum images UNIVERSITY



T H E OHIO STATE

95at.%Au-5at.%Pd : 1% total metal loading
"Bulk Samples": Phase stability/ Ti/Nb multilayers



Layer thickness : 2nm Ti / 3.2nm Nb

Question: How compositionally sharp are the interfaces? Answer: Need compositional analysis at the nanometer scale



Analysis of nanoscale multilayers





Use of Tomographical Atom Probe to determine intermixing in Ti/Nb Multilayers

Nb has significantly intermixed into Ti

Atom Probe composition profile



Layer thickness : 2nm Ti / 3nm Nb

T H E OHIO STATE bcc/bcc

Probe Corrected Titan: STEM/EELS Ananlysis of Ti/Nb Multilayers



Layer thickness : 1.6nm Ti / 2.1nm Nb

bcc/bcc

Atom Probe composition profile



Layer thickness : 2.2nm Ti / 3.3nm Nb bcc/bcc



Beam Broadening

Beam broadening

EELS

 $b \sim \beta t$

(EELS collection angle, $\beta = 20$ mrad and specimen thickness, t = nm)

XEDS $b \sim \text{Monte Carlo simulation}$ (MC) $b = 7.21x10^5 \frac{Z}{E_o} \left(\frac{\rho}{A}\right)^{1/2} t^{3/2}$

Single scattering (SS) approach



Fig. 4. The plot of beam broadening, b (nm) vs. TEM specimen thickness, t (nm) in Nb and Ti (SS = single scattering, MC = Monte Carlo).



Limits to High Spatial Resolution of EDS and EELS in an Aberration-Corrected (S)TEM

- Topics:
- Sample preparation
- Composition from EELS & EDS (not spatially resolved)
- Spatially resolved EELS not monochromated
- Spatially resolved EELS monochromated





Spectrum Image







EELS profile on Sr-Ti/O-Sr





Accelerating Voltage: 300kV

EELS profile on Ti/O-O-Ti/O





Possible Causes and Remedies

Possible causes:

• Electron tails

C2:50µm C3: 2000 µm



C2:150µm C3: 30µm



25% electron beam intensity in skirt Probe corrected up to 18mrad





Possible Causes and Remedies

C. Dwyer and J. Etheridge,

Possible causes:

- Electron tails
- Beam broadening

 Column jumping • Christian Dwyer

> transverse momentum for • highly convergent probe



Probe on column A1







Possible Causes and Remedies

Possible causes:

- Electron tails
- •Beam broadening

•Column jumping Christian Dwyer transverse momentum for highly convergent probe

Sample is changing

Radiation damage

Possible remedies:

Use thinner foils



Use lower accelerating voltages





5.43 Å -

1.92 /



Using thin foils of STO to improve spatial resolution



Point 1: 0.03λ Point 2: 0.21λ Point 3: 0.14λ Point 4: 0.20λ Point 5: 0.24λ Point 6: 0.22λ Point 7: 0.26λ



Near Point 1 (thinnest region)

Before



After





0.00E+00 5.00E-10 1.00E-09 1.50E-09 2.00E-09 2.50E-09



Accelerating Voltage: 300kV



Near Point 4

Before



After







Accelerating Voltage: 300kV

Possible Causes and Remedies – Radiation Damage

Displacement damage:

Direction	Threshold Displacement Energy (eV)		
	Oxygen	Strontium	Titanium
<001>	30	35	115
<110>	60	70	90

Thomas, Marks and Begg, Nucl. Instr. & Methods in Physics Research B, 254, 2007, 211

Maximum Energy Transferred (Windl):

Element	Accelerating Voltage		
	80kV	300kV	
Ο	12eV	53eV	
Ti	4eV	18eV	
Sr	2eV	10eV	



Obvious experiment: repeat measurements at 80kV

STO – lattice image at 80 kV



Acquisition conditions (imaging and analysis):

Camera length: 7.2 mm GIF aperture: 2.5 mm Conv. semi-angle: 23.9 mrad Collection semi-angle: ~ 125 mrad Spot size: 9 C2 Aperture: 70 mm

Mode: non-monochromated Probe current: 40 pA

Acquisition time: 300 ms/pixel (line profiles) 30 ms/pixel (maps)





Ti/O-O-Ti/O columns



 $\equiv CAMM$



Accelerating Voltage: 80kV

Cool New Stuff with Experiments

- •Topics:
- •Integration modeling with experiments
- •Useful recent characterization techniques
- •Limitations with experimental techniques
 - •sample preparation
 - •compositional analysis
- •What are we (OSU/CAMM) doing?





Our Efforts aimed at Improving (ST)EM Imaging & Analysis

<u>Features</u>:

- Chromatic-aberration corrected STEM
- Lower voltage to reduce damage
- Make foil and observe in STEM in same microscope

The FEI Magellan SEM, which is the basis of the Helios NG, the proposed acquisition.



A thin section of pig skin prepared at room temperature by use of a dual-beam FIB imaged (as-FIB'd) in an FEI Magellan, with an accelerating voltage of 350V.



- Accelerated and automated analysis
- Foil thickness measurement supplied to modeling backup

STEM images of an FIB extracted crosssection of a LiFePO cathode from a commercial Li ion battery showing the ability of technique to prepare thin-foils of this delicate, highly porous, multi-scale structure of these cathode materials.



Our Efforts at Novel Approaches to Improving Laser-assisted Atom Probe Analysis



Dramatic improvement in mass spectrum (mass to charge ratio versus number) of W with a decrease in λ , and by use of an improved PSD).



· H ·

UNIVERSITY

Similar improvement in mass spectrum of ZnO with a decrease in λ



Correlation of laser wavelengths used for different materials and corresponding band gap energies with their electrical resistivities

Question: Have we reached the maximum mass resolution with UV lasers or not?

Cool New Stuff with Experiments

Importance of Coupling of Efforts between Computational folks (unimaginative) and Experimentalists (creative):

• Provision of accurate and physically relevant mechanistic data

•Computational assistance in interpreting experimental data

Validation of predictions - at scale!!







Analysis of nanoscale multilayers / Ti/Nb multilayers



EELS profile on Sr-O-Sr







Accelerating Voltage: 200kV

EELS profile on Ti/O-O-Ti/O





Accelerating Voltage: 200kV

OSU Studies: Spectrum Image





Quantitative Analysis

Calculation

The relation between the concentration and characteristic X-ray intensity is given by;

$$C = \left\{ \frac{1}{K\left(\frac{\sigma \omega a\varepsilon}{A}\right)} \right\} \left(\frac{I}{t}\right)$$

Thin film criterion;

$$\frac{C_A}{C_B} = \frac{A_A(\sigma \omega a \varepsilon)_B}{A_B(\sigma \omega a \varepsilon)_A} \left(\frac{I_A}{I_B}\right)$$
$$\frac{C_A}{C_B} = k_{AB} \left(\frac{I_A}{I_B}\right)$$

Cliff-Lorimer factor;

$$k_{AB} = \frac{\left(\sigma \omega a \varepsilon / A\right)_{B}}{\left(\sigma \omega a \varepsilon / A\right)_{A}}$$



The concentration is given by;

$$C = \frac{n}{V}$$

Atom ratio;

$$R = \frac{n_A / V_A}{n_B / V_B}$$

Atom ratio, R_s assuming specimen thickness is constant and where h is layer width;

$$R_{S} = \left(\frac{h_{A}}{h_{B}}\right) \frac{n_{A}/V_{A}}{n_{B}/V_{B}}$$

Experimental Cliff-Lorimer factor;

$$k_{AB} = \left\{ \frac{I_A^{Total} / I_B^{Total}}{R_s} \right\}$$

Quantitative analysis XEDS

$$\frac{C_A}{C_B} = k_{AB} \left(\frac{I_A}{I_B} \right)$$

EELS

$$\frac{N_{A}}{N_{B}} = \frac{I_{A}(\beta\Delta)\sigma_{B}(\beta\Delta)}{I_{B}(\beta\Delta)\sigma_{A}(\beta\Delta)}$$

Partial cross-sections for EELS were measured using an experimental spectrum in Gatan DM software





Knowledge of Sample?

Sr deficient: phase separation – oxygen vacancies Layer: Sr_{0.8}TiO₃ Substrate: SrTiO₃

Т · Н ·

Do the STO layers adjust composition because of the constraints of the interface with BTO?





Experimental study of crystal nucleation in magma

Julia E Hammer

Dept. Geology and Geophysics School of Ocean and Earth Science and Technology University of Hawaii http://www.soest.hawaii.edu/GG/FACULTY/JHAMMER/

Carrie Brugger, University of Hawaii Tom Sharp, Arizona State University Malcolm Rutherford, Brown University



NSF EAR-Geochemistry and Petrology CAREER program NASA- Mars Fundamental Research Program

Joint AFRL/AOARD/LLNL Workshop on Nucleation During Solid-Solid Phase Transformations in Metallic Systems: Current Understanding and Future Directions

Maui, Hawaii May 2 - 7, 2010








clinopyroxene formina in syntl



3D aspect ratio (Underwood 1968) interface area per unit phase volume= 2N/o



divergence of cpx surface area per unit volume among populations

textural geospeedometer applied to Martian meteorite MIL03346



Hammer (2006) Earth Planet Sci Let

Hammer (2009) Meteoritics Planet Sci



Driving forces for crystallization



MELTS output, Ghiorso et al. 1995

 plagioclase: tricilinc framework silicate clinopyroxene: monoclinic chain silicate orthopyroxene: orthorhombic chain silicate hornblende: monoclinic chain silicate titanomagnetite: cubic Fe-Ti oxide quartz: trigonal framework silicate

Hammer et al. (2002) Contributions to Mineralogy and Petrology

 $\begin{array}{l} {\rm CaAl_2Si_2O_8-NaAlSi_3O_8} \\ {\rm (Ca,Na)(Mg,Fe^{2+},Al,Fe^{3+},Ti)[(Si,Al)_2O_6]} \\ {\rm MgSiO_3-FeSiO_3} \\ [\][{\rm Ca_2}][{\rm Fe_4^{2+}Al}][(OH)_2[{\rm AlSi_7O_{22}}]-[\][{\rm Ca_2}][{\rm Mg_4Al}][(OH)_2[{\rm AlSi_7O_{22}}] \\ {\rm Fe_3O_4-Fe_2TiO_4} \\ {\rm SiO_2} \end{array}$

Apparatus





Objectives

- Transitions in eruptive style
- Lava flow dynamics
- Magma ascent rate
- Magma degassing



Predictive power of microtexture

- Nucleation rate as a function of undercooling
- Nucleation response to continuous change in temperature or pressure
- Heterogeneous nucleation of major rock-forming minerals
 - Effects of shear flow
 - Metastable nucleating phases



Experiment types



Experiment type determines application





Hammer and Rutherford (2002) J Geophysical Research





Fit data with CNT

$$I = A \exp\left[\frac{-(\Delta G^* + \Delta G_D)}{k_B T}\right]; \Delta G^* = \frac{16\pi\sigma^3}{3\Delta G_V^2}S(\theta)$$
$$S(\theta) = \frac{(2 + \cos\theta)(1 - \cos\theta)^2}{4}$$

assumptions:

homogeneous Stokes-Einstein

$$\Delta G_{\rm D} = -\mathbf{k}_{\rm B} T \ln \left(\frac{h}{\lambda^3 3 \pi \eta}\right)$$
$$I = \frac{A_{\rm c}}{\eta} T \exp \left(\frac{-\Delta G^*}{\mathbf{k}_{\rm B} T}\right); A_{\rm c} = \frac{n_{\rm v} \mathbf{k}_{\rm B}}{3 \pi \lambda^3}$$

Turnbull

$$\Delta G = \frac{\Delta H \Delta T}{T_L}$$

 $\Delta T_{_{eff}}$ for ΔT

$$\begin{split} &V_{M} = 1.003 \text{ x } 10^{-4} \text{ m}^{3} \text{ mol} \\ &n_{v} = N_{A}/V_{M} \\ &\lambda = 3 \text{ x } 10^{-10} \text{ m} \\ &\Delta H_{f} = 74300 \text{ J mol}^{-1} \end{split}$$



Hammer (2004) American Mineralogist



Hammer (2004) American Mineralogist



Hammer (2004) American Mineralogist

Spaepen (1994) Solid State Physics

Diffuse Interface Theory











fast decompression: far from equilibrium, NA progressively increases slow decompression: equally far from equilibrium, coarsening

Brugger and Hammer, submitted, J. Petrology

Conspicuous Contiguity



Merapi 1995 andesite dome lava

Etna 122 BC basaltic plinian

Etna 122 BC basaltic plinian



Hammer et al. (2010) Geology





Aniakchak rhyodacite decompression experiment

Hammer et al. (2010) Geology



Concluding Thoughts

CNT formalism fruitful?

Independent knowledge of σ and it's dependence on melt H_2O Theoretical framework suitable for dynamic experimental results? Imaging incipient crystallization in magmas Heterogeneities, metastable phases, shear effects





Quantifying Rapid Solid-state Crystallization Kinetics; Application of the KJMA Equation to High Time Resolution Electron Microscopy Data

Joint AFRL/AFOSR/LLNL Pacific Rim Workshop on Nucleation, May 2nd-7th, 2010

Thomas LaGrange

DTEM TEAM: Geoffrey H. Campbell, Nigel D. Browning, Bryan W. Reed, Melissa Santala, Joseph Mckeown, Katie Jungjohann, Marta Bonds, William J. Dehope, Glenn Huete and Richard Shuttlesworth

Lawrence Livermore National Laboratory, PO Box 808, Livermore, CA 94551

This work performed under the auspices of the U.S. Department of Energy by Lawrence Livermore National Laboratory supported by Office of Science, Office of Basic Energy Sciences, Division of Materials Sciences and Engineering of the U.S. Department of Energy under Contract DE-AC52-07NA27344.

At the nanoscale, structural evolution in materials happens quickly because distances are short.



In regimes that have never before been explored, we will observe new and noteworthy features of materials dynamics.

DTEM affords the opportunity to directly study complex transient phenomena in materials

DTEM experiments are on the same length and time scales as large scale atomistic simulation



H. Van Swengenhoven, PSI

Lawrence Livermore National Laboratory



G. Gilmer, LLNL



V.Bulatov, LLNL

Overview: The LLNL DTEM is a nanosecond-scale *in situ* TEM with single-shot capability

DTEM adds two lasers to a conventional TEM to enable:

- Driving sample events with extreme spatiotemporal temperature gradients
- Real-space imaging and diffraction with ~15 ns exposures
- Enough signal in one exposure to form an image (up to $2x10^9$ electrons)



We have achieved performance in DTEM adequate for most materials science investigations we could envision







Dynamical contrast formation allows DTEM to image those defect structures that control properties of materials.

Lawrence Livermore National Laboratory

Laser heating can be used to tailor microstructure and properties in NiTi thin films for shape memory applications.

- Laser annealing can be used to crystallize amorphous NiTi film and modify grain size
- DTEM laser pulse produces large spatiotemporal temperature gradients
- Kinetics *do not* extrapolate from low temperature studies



Lawrence Livermore National Laboratory

CW laser annealing, Wang et al., Acta Mater. 2005



Pulsed laser annealing in DTEM (~1500 K)



Conventional annealing and *in situ* TEM studies were used to determine the kinetic parameters for crystallization.

- We studied crystallization processes in 250 nm thick amorphous, equiatomic NiTi films.
- Films were annealed at 768K using *in situ* TEM heating holder.
- Crystallization processes were recording using a video camera.
- Comparable crystallization kinetics to CW laser annealing experiments.



Conventional *in situ* hot stage microscopy used to determine crystallized fraction as a function time for JMAK analysis



- Crystallization data were fit with the Johnson-Mehl-Avrami-Kolmogorov model to determine the kinetic parameters.
- Consistent with previous reports for NiTi in the literature.
- Kinetic data was extrapolated and compared with DTEM data measured at high temperatures (850-1550K).

Crystallization of amorphous NiTi films occurs on the μ s timescale, much faster than expected from known kinetics.



Lawrence Livermore National Laboratory

Crystallization kinetics depend strongly on laser fluence, film thickness and heat transport.



- Temperature rise was calibrated using ex-situ reflectivity measurements and observations of liquefaction.
- Radial temperature and cooling rate calculation assume Gaussian laser energy distribution and heat loss by lateral conduction in an infinite medium.

Time-resolved brightfield imaging used to study rapid nucleation rate under pulsed laser annealing.

- Nucleation rate can be determined by the change in the number of new sites as a function of time normalized to the untransformed volume.
- Requires multiple single-shot experiments.

$$J(t_i) = \frac{1}{1 - X(t_i)} \frac{dN}{dt}$$
$$= \frac{1}{1 - X(t_i)} \frac{(N_i - N_{i-1})}{(t_i - t_{i-1})}$$



Extraordinarily high nucleation rate occur under pulsed laser heating.



- Nucleation rate is 8 orders of magnitude higher under pulsed irradiation.
- Extrapolation of data acquired at 768K using JMAK kinetics still leads to a predicted nucleation rate that is orders of magnitude different. J_o≈370 μm⁻² s⁻¹

Crystallization data were fit with the Johnson-Mehl-Avrami-Kolmogorov model to determine the kinetic parameters.

- Assuming that k_o is the Debye frequency ~10¹³ s⁻¹, $k = k_o \exp(-Q/\kappa T)$ $Q_{DTEM} = 1.7 \pm 0.3 \text{ eV}$ $Q_{slow anneal} = 2.3 \pm 0.17 \text{ eV}$
- Assuming that n=3 and crystallization occurs under steady state nucleation and growth, the growth rate can be calculated, $V_o = 6.7 \times 10^5 \,\mu\text{m s}^{-1}$ $k = \sqrt[3]{(\pi/3) J_o V_o^2}$
- The associated grain size can also be predicted,

$$\overline{d} = 1.2 \sqrt[3]{V_o/J_o} = 1.05 \,\mu m$$

Lawrence Livermore National Laboratory

Crystallized volume fraction as a function of time at an estimated temperature of 1200K



Crystallization rate varies strongly with laser intensity showing a C-curve like behavior which has not been previously observed.



- Final microstructure varies strongly with initial pulsed laser annealing temperature.
- Crystallization rates appear to be highest at temperatures around 1200K.
- The threshold temperature for pulsed laser crystallization is ~850K



C-curve like behavior cannot be predicted from data obtained in the slow-heating experiments.

- Large discrepancy between pulsed laser heating and slow annealing.
- Extrapolation of DSC data using the JMAK equation show that mechanism occurring under pulsed laser appealing are not captured

nal thermal

havior___

m

1600 Pulsed laser Crystallization Data tional TEM Data nnon ner Extrapolation of Kinetic Data 1400 Limited Femperature, K 1200 **Kinetically Limited** 1000 DSC and Conventional TEM Data 800 Pulsed laser heating **DTEM Data** 600 + 10^{-1} 10^{0} 10^{1} 10^{2} 10^{3} 10^{4} 10^{5} 10^{6} 10^{7} 10^{8} 10^{9} Time, µs

Bulk Melting Tempeature, ~1650K

results from increased entropy (lower driving force) at high temperatures.

Future experiments will strive to measure precise growth rates and approximate interfacial energies.


Conclusions

- Using the DTEM, one can quantitatively measure the nucleation and growth rates associated with phase transformations with <u>ns time resolution.</u>
- We can gain insight into the subtle details of materials processes in previously unexplored regimes (kinetically driven and high temperature states).
- The discrepancy between pulsed laser and slow annealed induced devitrification kinetics is captured by the JMAK analysis and is not understood!



Lawrence Livermore National Laboratory



To follow the microstructural and defect evolution, multiple images must be acquired from drive event.

- Measurement of the growth rates requires multiple images of a moving interface to reveal its velocity.
- A time sequence of multiple images (a movie) allows the position of a given moving interface to be measured and its speed determined.



Movie Mode will let us capture a series of images from a single sample drive event.



DTEM needs bright sources, but ultimately higher time resolution limits spatial resolution!



Resolution is governed by the fixed normalized brightness of the gun! Lens aberrations and electron-electron interactions can reduce your effective average brightness in your system.

A high quality image needs N ~ 10^8 electrons. Suppose r = 1 μ m, α = 10 mrad, Δt = 1 ns. Brightness = 1.6×10^9 A cm⁻² steradian⁻¹, with 16 mA at the camera. This is the brightness of a typical field emitter, but with vastly more current. DTEM currently has brightness of ~1x10⁸ A cm⁻² steradian⁻¹

With high electron currents, electron-electron interactions limit brightness and spatial resolution.



History: DTEM grew out of developments in time-resolved TEM that date back to the 1960's

- "Stroboscopic" TEM uses many synchronized pulses to capture a cyclic process
 - Magnetic domain wall motion (Spivak et al., *Bull Acad. Sci. USSR* 30, 822 (1966))
- Groups in Europe and Japan developed pulsed TEM and SEM through the 1980's and 1990's
 - Multi-frame movies with 30 μs exposure, ms interframe time (Takaoka & Ura, *J. Elect. Mic.* 32, 299 (1983))
 - Nanosecond-scale single-shot TEM with 3-frame movies (Domer & Bostanjoglo, *Rev. Sci. Inst.* 74, 4369 (2003))
- Advances in lasers, TEM's, and ultrafast techniques have re-ignited the field in the last few years



A femtosecond stroboscopic approach was developed by the Zewail group at Caltech

- 120 keV G12 Twin Tecnai
- Gatan Ultrascan 1000 UHS 2048 x 2048
- Results reported were acquired with 1 electron per pulse
- More recently developed a second-generation machine

Four-dimensional ultrafast electron microscopy

Vladimir A. Lobastov, Ramesh Srinivasan, and Ahmed H. Zevvail*

Laboratory for Minkes Are Sciences, written were shown Laboratory of Chemical Physics, California Institute of Technology, Pasadama, CA 91125

Contributed by Anived III Zawal, March 50, 2005

Electron microscopy is arguably the most powerful tool for spatial imaging of structures. As such, 20 and 3D microscopies provide static structures with submanometer and increasingly with angstrom-scale spatial resolution, here we report the development of 4D uthrafast electron microscopy, whose capability impacts another dimension to imaging in general and to dynamics in particular. We demonstrate its versatility by reconfing images and diffraction patterns of crystalline and amorphous materials and images of

but for biological and nanoscopic materials with characteristic length scales ranging from nanometers to micrometers, electron microscopy enjoys unique advantages.

It is the purpose of this paper to report the development of 4D ultrafast electron microscopy (UEM), which provides the ability to rondestructively image complex structures with the spatial seclution of TEM, but as mapshots captured with ultrafast electron packets derived from a train of femtusecond pulses.

PNAS 2005;102[20]:7069-73



Lawrence Livermore National Laboratory

Time-resolved electron probes divide roughly into three categories

	Stroboscopic	Intermediate	Single Shot
Example	UFTEM	UED	DTEM
Electrons/Pulse	~1-10 ³	~10 ³ -10 ⁶	~10 ⁷ -10 ⁹
Pulses/Image	10 ⁵ +	Few-100	1
Time Resolution	Sub-ps	sub-ps to few ps	15 ns
Spatial Resolution	Å	Many µm	~10 nm
Energy Spread	~1 eV	~100 eV	~10 eV
Spectroscopy	Yes	Not demonstrated	Not demonstrated
Main Strength	Spatiotemporal resolution	Great for diffraction; systems are simple	Capture unique, irreversible events in real space
Main Weakness	Extremely repeatable processes only	Imaging is difficult	Resolution

Trajectory displacement will limit resolution to at best 5 nm at 1 ns, 200 keV



PSF 0.75 amplitude_{0.5} 0.25 -100 -50 Displacement (nm) 50 Juo⁻¹⁰⁰

Analytical formulas were applied to optical model of post-sample lens system. Result: 5-50 nm resolution limit, depending on current and lens settings Numerical multi-particle simulation of electron point spread function after sample interaction Result: 5-50 nm resolution limit, depending on current and spot size

Simulation has suggested the feasibility of ultrafast (< 10 ps) electron imaging



For picosecond resolution imaging, relativistic energies may be the only way to obtain high spatial resolution.

Lawrence Livermore National Laboratory

Relativistic pulses significantly mitigate stochastic blur.



Relativistic electrons have a shorter (proper) propagation time, diverge more strongly, and have smaller current density.

A future DTEM might look more like a particle accelerator



NUCLEATION IN AMORPHOUS AI ALLOYS Influence of Solute Distribution Joint AFRL/AOARD/LLNL Workshop on Nucleation During Solid-Solid Phase Transformations in Metallic Systems 5 May 2010

E.Spowart^a, D.B. Miracle^a and H.M. Mullens^b

a. AF Research Laboratory Materials and Manufacturing Directorate Dayton, OH USA b. Southwestern Ohio Council for Higher Education (SOCHE) Materials and Manufacturing Directorate Dayton, OH USA



FORCE RESEARCH LABORATOR

"metallurgists ^ are apt to be practical down-toearth people who stand no nonsense, but the theoriticians lurgists ^ are probably more lyrical and imaginative"











INTRODUCTION Properties and Applications of Metallic Glasses NUCLEATION IN AMORPHOUS AI MODELING OF NUCLEATION SITES CONCLUSIONS



MULTIFUNCTIONAL METALS OF DISTINCTION



Unique balance of properties distinguish metallic glasses as a distinct class of metals

– Mechanical

- Very high hardness
- Strength twice that of conventional metals
- Fracture toughness can be very high
- High resilience and low mechanical damping

– Magnetic

- High magnetic permeability & low hysteresis losses
- Highly tailorable magnetic properties

- Corrosion

Lack of crystal defects (grain boundaries) and unique formulations give exceptional corrosion behavior

- Processing

- High viscosity and low strain rate sensitivity of the supercooled liquid enables thermo-plastic forming that was previously impossible
- Low solidification shrinkage and lack of grain structure gives high precision and finish in castings









AMORPHOUS METALS *Current Applications*



Low loss magnetic material

power and current transformers
video recording heads
electronic surveillance tags

Corrosion resistance

corrosion resistant coatings for safety razors
nuclear containment coatings being validated

Structural applications

micro-mirror hinges for digital projection systems
golf club heads, tennis racquets, baseball bats
electronics cases for cell phones, laptops, PDAs
brazing alloy













Nucleation 5



MAGNETIC APPLICATIONS OF METALLIC GLASSES



Power transformer cores for electricity distribution

- Significant reduction in hysteresis losses, especially in systems with higher harmonics introduced by non-linear loads in modern electronics
 - Non-linear power supplies, variable speed motors, lighting controls, electronic power sources in personal computers and telecommunications...

Electronic power supplies and power conditioners

Magnetic read/write heads

– Also takes advantage of high hardness and excellent wear resistance

Magnetic shielding

Industries impacted by metallic glass applications

- Electrical power distribution
- Electronics
- Communications
- Computers
- Electronic article surveillance





TAILORABLE *B-H* CHARACTERISTICS











....leation 8





FRACTURE TOUGHNESS v. STIFFNESS









Conventional metals cannot be practically supercooled for processing Crystal nucleation occurs quickly at low undercooling, followed by rapid growth

The liquid is stabilized far below T_m in metallic glasses

Chemical and topological contributions stabilize the metallic glass structure

Enables injection molding to produce net shape metallic components

- process time increases dramatically after cooling below the 'nose'
- thick sections (>1 cm) can be formed in bulk metallic glasses

Metal injection molding provides important processing capability

- enables unitized construction of complex shapes where part volume is important
- ✤ metals compete successfully with plastics for both cost and performance



BLOW-MOLDING: <u>No</u> contact area Courtesy J. Schroers





Zr44Ti11Cu10Ni10Be25 (LM1b)

T=460°C, t =40 sec 10⁵ Pa, 400% strain

J. Schroers, T. Nguyen, A. Peker, N. Paton, R. V. Curtis, Scripta Materialia, 57, 341 (2007)

Unachievable shapes for metals? Courtesy J. Schroers





Hollow, thin, seamless, complex parts







J. Schroers, Processing of bulk metallic glass. Advanced Materials, 21, 2009

TPF OF BMG-How small can you go? Courtesy J. Schroers



500 nm

PtNiCuP into porous Al2O3

ZrTiNiCuBe on C (a) AIN (b)



G. Kumar, H. Tang, and J. Schroers, Nature 457, 868 (2009)



Metallic glasses properties motivate important applications

AMORPHOUS METALS

Potential Aerospace Applications

- Sensor/actuator applications
 - exceptional soft and hard magnetic properties
 - magneto-strictive and GMR behavior
 - remote sensing of temperature, stress, strain
- Power transformers
 - exceptional soft magnetic properties
- Structural applications
 - enabling specific strength
 - good fracture toughness
 - > penetrators
- Environmental applications
 - exceptional corrosion resistance
 - > unusual friction, wear resistance
- Information storage and reproduction
 - ability to reproduce very fine surface details









NUCLEATION IN AMORPHOUS METALS



- No fundamental differences from crystal nucleation in undercooled liduids and supersaturated solids
- Systems are characterized as far from equilibrium
- A significant number of systems show nucleation of icosahedral and quasicrystalline phases
- Some alloys show an exceptionally high number density of nuclei (~10²¹ to 10²³ m⁻³)







INTRODUCTION NUCLEATION IN AMORPHOUS AI Characteristics Influence on Properties

MODELING OF NUCLEATION SITES

CONCLUSIONS



In Situ NANOCRYSTALS IN AMORPHOUS METALS



Nanocrystal dispersions can be formed *in situ* in amorphous Al

- ✤ Al nanocrystals are 5-30 nm in diameter
- Al nanocrystals are at an exceptionally high number density (10²¹ to 10²³ /m³)

Improves strength and ductility

mechanisms unknown

Nucleation mechanism unknown

 conventional homogeneous and heterogeneous nucleation do not fit experimental observations

Control of nanocrystalline precipitation gives an approach to control properties of a-Al









Melt spinning produces amorphous product and crystallization initiates above T_x

- Al crystallites are very small (~10-30 nm), and occur at an exceptionally high volume density (~ $3x10^{21}m^{-3}$)
 - typical volume density for standard metals is ~10¹⁶ m⁻³
 - Heterogenous nucleation unlikely
 - Low apparent activation energy for nucleation
 - nucleation at "quenched-in features" may be related to Al-like MRO in a-Al (Perepezko and Imhoff, 2009)
 - features responsible for nucleation have not been identified



Figure 1: a) Bright-field TEM image and corresponding SAED pattern of as-span $Al_{87}Sm_{8}$ ribbon. The analyses do not show any signs of crystallinity. b) Continuous DSC trace of as-span $Al_{82}Sm_{8}$ at 20°C.min⁻³ [18]. The crystallization occurs in two steps. The primary crystallization peak with an onset at 172°C corresponds to the development of a high number density of Al-nanocrystals in the amorphous matrix. The second peak is attributed to the crystallization of the remaining amorphous phase.



Figure 5 : TEM images of $Al_{80}Y_7Fe_3$ a) and b) Bright-field and corresponding SAED images of as-spun samples that have been annealed at 245°C for 10 and 60 min, respectively, c) Dark-field and corresponding SAED images of an as-spun sample that has been cold-rolled to a true strain of $\epsilon = -10$. Both, thermal treatments and plastic deformation induce the development of Al-nanocrystals. The Dark-field TEM images in the inset show the shape evolution of nanocrystals from a spherical to a deudritic morphology with increasing annealing time.

Boucharat and Wilde, 2009.

"Gentleman, we have run models out of money." Now we

must think."

Winston Churchill







Provide a structural description of the sites responsible for the high nucleation density in partially devitrified amorphous Al







INTRODUCTION NUCLEATION IN AMORPHOUS AI MODELING OF NUCLEATION SITES CONCLUSIONS



STRUCTURAL MODEL FOR AMORPHOUS METALS



The structure of amorphous AI can be described as an organized arrangement of Y-centered clusters

- Y surrounded by ~14 AI and ~3Ni atoms
- Ni and Y solutes appear to be correlated
- Supported by measurement of partial coordination numbers

Intercluster regions are Al-rich and have a relatively high free volume

- high free volume produces local high internal energy, and also enables more rapid mass transport
- both of these favor nucleation of crystalline phases



Miracle, *Nature Materials*, **3**, 697 (2004). Miracle, Acta mater., **54**, 4317 (2006). Miracle, Louzguine, Louzguina, Inoue, *International Materials Review*, In press.

From our readers



A.R. Yavari, Nature Materials, 4, 2 (2005)

SOLVING THE PUZZLE OF EUTECTIC COMPOSITIONS WITH 'MIRACLE GLASSES'

To the editor - The structural model for metallic glasses published in the October issue of Nature Materiald may account for the observed compositions of binary A,B, eutectics, which occur most frequently at integer values of x and y. In 1935, D. Stockdale¹ suggested that, in binary alloy phase diagrams, the compositions of eutectic points should correspond with simple whole-number ratios of the two kinds of atoms A (solvent > 50 at.%) and B (solute < 50 at.%). There was insufficient data to confirm this prediction at the time, but in 1980, W. Hume-Rothery and E. Anderson' re-examined the Stockdale suggestion by plotting the frequency of occurrence of binary extectic compositions versus alloy compositions from the handbook of

found clear maxima corresponded to A/B-/1, 2/1 and 3/2.

Hume-Rothery and Anderson tried to explain this finding on the basis of the local short-range order (SRO) of the atomic structures in binary liquids by postulating that eutectic compositions are likely to form when interatomic interactions are used that B_B massest mainblumes are

INEFFICIENT ATOMIC PACKING AROUND AI ATOMS



	Coordination Number	Bond Distance (nm)	Local Atomic Concentration	Packing Efficiency
Al ₈₇ Y ₈ Ni ₅ (7)				
Y-A1	14.3 ± 1.9	0.320	77%	88%
Y–Ni	2.7 ± 0.7	0.297	15%	14%
Y-Y	0.4 ± 0.4	0.356	8%	3%
Al-Al*	7.2 ± 0.8	0.286	84%	57%
Al-Ni*	$0.4 \pm 0.1^{\#}$	0.268	4%	3%
Al-Y*	1.2 ± 0.2	0.320	12%	12%
Ni–Al*	$6.5 \pm 0.2^{\#}$	0.268	59%&	60%
Ni–Ni&	0&		9%&	~0%&
Ni–Y*	3.5 ± 2.6	0.303	32%&	40%
Al ₉₀ Y ₁₀ (⁷)				
Y–Y	1.1 ± 0.4	0.362	13%	9%
Y–Al	14.1 ± 1.5	0.320	87%	87%
Al-Y*	1.6 ± 0.2	0.320	12%	16%
Al–Al*	10.7 ± 0.8	0.288	88%	85%
Al ₉₀ Ce ₅ Fe ₅ (^{8,9})				
Ce-Al	14.0 ± 1.6	0.325		85%
Fe–Al	4.9 ± 2.4	0.249		45%
Al ₉₀ Ce ₃ Fe ₇ (^{8,9})				
Ce-Al	11.0 ± 2.3	0.325		67%
Fe-A1	64 ± 21	0 249		59%

* Data from total radial distribution functions.

Values corrected from original citation.

& Estimated value.

Miracle, J. Non-Cryst. Sol., 2004.

Local packing efficiency is only 72% around Al atoms


FREE VOLUME





Free volume is locally highest in the regions between Y–centered clusters. These regions are enriched in AI, and depleted in Y and Ni.

SOLUTE ATOMS DESTABILIZE CRYSTALLINE AI



Local lattice strains associated with solutes destabilize crystal (Egami, Waseda, JNCS, 1984.)

- Magnitude of lattice strains decrease with increasing distance from solute
- Rare earth metal (RE) solutes are non-interacting, and may be *randomly* distributed in the structure
- <u>Average</u> intersolute spacing is ~3 atom spacings
- Spacing between RE atoms will be larger than the average in some cases, producing lower lattice strains and large Al-rich regions
- These regions may be favored for nucleation of crystalline phases









Critical Al nuclei form in Al-rich areas where Y–Y spacing is sufficiently large to allow formation of a critical cluster critical nucleus size is generally held to be ~100 atoms atomic cube ~5 atoms on a side, or atomic sphere ~6 atoms in diameter



Spowart, Miracle, Mullens, J. Non-Cryst. Sol., 336, 202 (2004).



AI NUCLEI IN A RANDOM ARRAY OF Y ATOMS









Assume a <u>random</u> spatial distribution of discrete Y atoms in a continuous matrix of AI atoms

Search for Y-free regions that are large enough to contain a critical AI nucleus

- Suggest that AI atoms in these regions are non-crystalline, but will arrange into a crystal with only a small activation energy needed to rearrange atoms
- Solute diffusion is not required for nucleation, but will be required for growth

Determine the volume density of such sites as a function of the size of these regions and solute concentration

- Model solute concentrations from 0.04 to 0.10

Compare with experimental value of nucleus volume density



MODELING THE ALLOY



Amorphous alloy model:

- hard spheres
- hard edges
- -10^3 to 10^7 atoms



Random (non-overlapping) spatial distribution of 7 At% Y in Al



NUMBER OF NUCLEI vs CRITICAL NUCLEUS SIZE







NUMBER OF NUCLEI vs SOLUTE CONCENTRATION



Nucleation 32



COMPARISON WITH MEASUREMENTS



Table 1 Showing tabulated data from Fig. 4

Alloy system	$ ho_{ m V}~({ m m}^{-3})$	$n_{\rm a}$ (estimated)	Ref.
Al ₉₀ Nd ₄ Ni ₆	${\sim}10^{23}$	100	[7]
Al ₉₀ Gd ₅ Fe ₅	3.6×10^{23}	70	[2]
Al ₈₈ Y ₇ Fe ₅	$3-4 \times 10^{21}$	60	[5]
Al ₉₂ Sm ₈	$4 \times 10^{21} - 3.5 \times 10^{22}$	40–50	[12,25]
$Al_{85}\mathbf{Y}_{10}\mathbf{N}i_5$	${\sim}10^{21}{-}10^{22}$	30-40	[7]

Values of ρ_V are from experimental measurements, estimates of n_a are obtained by interpolating the modeled relationships between nucleus number density and RE solute concentration.







INTRODUCTION NUCLEATION IN AMORPHOUS AI MODELING OF NUCLEATION SITES CONCLUSIONS





A simple physical model of the atomic structure responsible for the high volume density of Al nanocrystals in a-Al has been analyzed

- Focuses on random solute distribution
- Thermal defects not addressed but may give similar results
- Does not address nucleation or growth of super-critical nuclei
- Observed nucleant volume densities are consistent with critical nuclei containing 40-100 atoms, matching estimated values
- Low activation energy conceived thru the local rearrangement of AI atoms
- Consistent with subsequent observations of Al-like MRO in a-Al alloys
- Need to understand chemical effects that influence solute distribution, especially next-nearest neighbors



THANK YOU!







RULE 1 CONSEQUENCES *Efficient Packing of Primary Clusters*



Four topologically distinct atomic species and sites

- Solvent atoms (Ω)
- Primary (α) solutes produce the structureforming unit clusters
- Cluster-octahedral interstices (β)
- Cluster-tetrahedral interstices (γ)
- $-r_{\alpha} > r_{\beta} > r_{\gamma}$

Solute atoms occupy ~ordered sites

- Provides basis for observed medium range atomic ordering (MRO)
- Variable cluster-cluster separation degrade cluster ordering beyond a few cluster diameters

Preferred atom positions introduces the possibility of structural defects

- Vacancy and anti-site point defects
- Constitutional and thermal





"Ninety-nine percent loyalty is 100% disloyalty."

Napoleon Bonaparte

"He's not dead. I said he's *mostly* dead. BIG difference."

Miracle Max, from "The Princess Bride"

"The Pirate's Code is more what you'd call 'guidelines' than actual rules."

Captain Barbossa, from "The Pirates of the Caribbean"



THERMAL DEFECT PAIR









Count the number of cubic volumes of side Q within the model system which contain no Y atoms

Considerations :

- fixed lattice
- cubic volume, (Q³) not spherical volume (4/ $3\pi r_{cluster}^{3}$)

Bounded Problem:







 $Q = 5 d_{AI}$

Q = 2.89 d_{AI}

 $Q = 3.52 d_{AI}$







Direct Counting:

- limited by size of domain
- computationally intensive
- fixed lattice







Measure the distribution of local V_f at length scale Q:



Random (non-overlapping) spatial distribution of 11 At% Y in Al sampled at length scale $Q = 2.29 d_p$ (4096 volume elements)





Model the distribution of local V_f :







Calculate the probability of finding $V_f = 0$, over a length scale Q:

$$\mathsf{Pr} \{ f : f + \Delta f \} = \int \phi(f) \, \mathrm{d}f$$

$$f$$



Assumptions :

$$- f = 0$$

$$- \Delta f = 0.005$$







Probabilistic Method:

- limited by statistical model
- fixed lattice



number of clusters per unit volume (m⁻³)



COMBINED RESULTS





Future Work:

- close the gap!
- new compositions
- multiscale effects: clustered clusters



CLUSTER MODELS *Cluster Linking*



Configurations producing a Y–Y separation of 2AI atoms

- Link adjacent clusters by nestling an AI atom from one cluster in a low-energy position of a 2nd cluster, then rotating to a final low-energy configuration
 - . . . into a trigonal array yields a tetrahedron
 - trigonal arrays exist in all clusters, so this may be a common linking configuration
 - \blacktriangleright . . . into a four-fold array yields an octahedron
 - these are intrinsic to the $\rm AI_{15}Y$ cluster, and can occur in terminations of all other clusters discussed
 - . . . into a five-fold array forms a portion of a low-energy icosahedron
- Another possibility is to link two trigonal arrays to form an AI_6 octahedron

Configurations producing a Y–Y separation of 1AI atom

- Adjacent Y atoms share a common trigonal array of Al atoms

Configurations producing adjacent Y-Y atoms

- Substitute an AI or Ni atom in a Y-centered cluster with Y
- "Linear molecules" obtained by stacking a given cluster upon itself
 - can be accomplished with each of the four clusters discussed

Significant structural diversity is enabled via linking

Inter-Solute Spacing



- Consider a regular distribution of solute atoms of concentration, c_i , which occupy the corners of a cube of edge length, x_i atoms. Then:

$$c_i = 1/x_i^3$$

- If we know C_i , then we can determine the mean inter-solute spacing, x_i :

$$x_i = 1/c_i^{1/3} = c_i^{-1/3}$$

- for $C_j = 0.09$, $L_j = 2.2$ atoms; for $C_j = 0.13$, $L_j = 2.0$ atoms
 - \succ on the average, every Y atom is separated by 1 1.2 other atom diameters



Each Y and its nearest neighbors may be treated as a RVE





Heterogeneous Nucleation of Plate-shaped Transformation Products

Barry C Muddle ARC Centre of Excellence for Design in Light Metals Monash University 3800 Victoria AUSTRALIA

Acknowledgements:

Y Kryvasheyeu, J Rosalie, GB Winkelman, L Bourgeois, JF Nie

Joint AFRL/AOARD/LLNL Workshop

'Nucleation During Solid-Solid Phase Transformations in Metallic Systems'

2-7 May, Maui, Hawaii





- AI-4Cu Alloy, and (a)
- (b) Al-4Cu-0.05Sn Alloy 18h at 190°C
 - **B** ~ <100>_α

Alloy

5h at 200°C

B ~ <111>_α









0.23 nm — T_1

T₁ Phase (Al₂CuLi) in Al-Cu-Li Alloys

Mg

ARC Centre of Excellence Design in Light Metals







Formation of γ' Phase (Ag₂Al) in Al-Ag Alloys







Fig. 3—Schematic representation of the lattice correspondence between parent and product lattices for the fcc to hcp transformation.

Muddle, Nie, Hugo, Metall. Mater. Trans. 25A p. 1841 (1994)



ARC Centre of Excellence Design in Light Metals





Muddle, Nie, Hugo, Metall. Mater. Trans. 25A p. 1841 (1994)

 $\mathbf{b}_{\mathbf{T}} = hm\mathbf{d} = h\tau\mathbf{t} + h\xi\mathbf{n}$

$$\mathbf{b}_{\mathbf{T}} = \frac{a}{6} \left\langle 112 \right\rangle + \frac{2\xi a}{3} \left\langle 111 \right\rangle$$



Howe, Dahmen, Gronsky, Philos. Mag. 56A p. 31 (1987)







Consider a platelet of the product phase to take the form of a thin oblate spheroid, with radius a and semi-thickness c, and an aspect ratio, A = c/a, such that $a \gg c$.

$$\Delta F^{0} = \frac{4}{3} \pi a^{3} A (\Delta F_{v} + E_{el}) + 2\pi a^{2} [1 + f(A)] \gamma_{s}$$
$$f(A) = \frac{A^{2}}{\sqrt{1 - A^{2}}} \tanh^{-1} \sqrt{1 - A^{2}}$$

Unconstrained transformation strain is an invariant plane strain, comprising a uniaxial expansion ξ normal to the invariant plane and a simple shear τ in the habit plane

J.K. Lee, H.I. Aaronson and D.M. Barnett, *Metall. Trans.* 8A(6), pp. 963-70, 1977





For small A, the shape-independent energy due to the uniaxial expansion alone may be expressed in the form:

$$E_{\xi} = \frac{\pi}{4(1-\nu)} A \mu \xi^2 \qquad \qquad \mu - \text{shear modulus} \\ \nu - \text{Poisson's ratio}$$

The strain energy per unit volume for the constrained shear au is given by:

ARC Centre of Excellence Design in Light Metals

$$E_{\tau} = \frac{\pi (2 - \nu)}{8(1 - \nu)} A \mu \tau^2 \qquad \qquad E_{\tau} >> E_{\xi}$$

The **total elastic strain energy** $E_{el} = E_{\xi} + E_{\tau}$ tends to a minimum of zero as the aspect ratio A goes to zero. However, surface energy of a thin plate-like form:

$$E_{\gamma} = 2\pi a^2 (1+A) \gamma_s$$

increases with square of plate radius. Equilibrium shape at nucleation will be that which achieves an appropriate balance in the competing needs to minimize both elastic strain energy and surface energy.

J.W. Christian, Acta Metall. 6 pp. 377-9 (1958)







$$\Delta F^{0} = \frac{4}{3}\pi a^{3} A (\Delta F_{v} + E_{el}) + 2\pi a^{2} [1 + f(A)] \gamma_{s}$$

Under the combined influence of interfacial energy and elastic strain energy, the energy barrier to nucleation ΔF^* may be considered a function of the critical values a^* and A^* which simultaneously satisfy the conditions

 $[\partial (\Delta F^o)/\partial a]_A = 0$ and $[\partial (\Delta F^o)/\partial A]_a = 0$

$$a^* = \frac{-2\gamma_s}{(\Delta F_v + E_{el})} \frac{1 + f(A)}{A}$$

In the limit of $A \to 1$ $a^* = -2\gamma_s/(\Delta F_v + E_{el})$

The corresponding $(a = a^*)$ value of ΔF_o is:

$$\Delta F^* = \frac{2}{3} \frac{\pi \gamma_s^3}{(\Delta F_v + E_{el})^2} \frac{[1 + f(A)]^3}{A^2}$$

J.K. Lee, H.I. Aaronson and D.M. Barnett, Metall. Trans. 8A(6), pp. 963-70, 1977





	ARC	Cen	tre	ofE	xcel	ence
Ti	De	sign	in I	Ligh	t Me	tals

Ma

Interface	γ	Method/Reference	
	mJ/m		
	30	Nearest neighbour, regular solution model [2]	
	156	MEAM (MD, empirical potentials calculations) [5]	
α/θ' , habit plane	190	Ab initio, DFT [4]	
	235	Ab initio, DFT [3]	
	510	Experiment, isothermal calorimetry [1]	
	360	Nearest neighbour, regular solution model [7]	
α/θ' , semicoherent	615	Ab initio, DFT [3]	
edges	694	MEAM [5]	
	21500	Experiment, isothermal calorimetry [1]	
alle habit alara	115	Nearest neighbour, regular solution model [2]	
ωγ, nabit plane	150	[6]	
α/γ' , habit plane	4-7	Discrete-lattice plane, regular solution model [6]	
	60	Nearest neighbour, regular solution model [2]	
	117	[6]	

1. JD Boyd and RB Nicholson, Acta Metall., 1971. 19(10): p. 1101-9.

2. HI Aaronson, JB Clark, and C Laird, Metal Sci. J., 1968. 2: p. 155-158.

3. V Vaithyanathan, C Wolverton and LQ Chen, Phys. Rev. Lett., 2002. 88(12): p. 125503-1.

4. V Vaithyanathan, C Wolverton and LQ Chen, *Mater. Sci. Forum*, 2004. 449-452: p. 19-24.

5. SY Hu, MI Baskes, M Stan, and LQ Chen, Acta Mater., 2006. 54(18): p. 4699-707.

6. RV Ramanujan, JK Lee and HI Aaronson, Acta Metall. et Mater., 1992. 40(12): p. 3421-32.

7. HI Aaronson and C Laird, Ford Motor Co. Scientific Laboratory Report, 1967.





ARC Centre of Excellence Design in Light Metals

Mg

AE	$\xi=0,\tau=0$			$\xi = 0.025, \tau = 0.0$			$\xi = 0.05, \tau = 0$			
ΔF_V I/m^3	<i>a</i> *	A *	ΔF^*	<i>a</i> *	A *	∆F*	<i>a</i> *	A **	ΔF^*	
J/111	nm	A^*	k_BT	nm	A^*	$k_B T$	nm	A^*	k_BT	
	$\gamma_h=0.03 \text{ J/m}^2$, $\gamma_e=3\gamma_h$									
1.0 10 ⁸	3.6	0.33	85.1	4.0	0.28	96.3	5.2	0.20	131.2	
2.0 10 ⁸	1.8	0.33	21.3	1.9	0.30	22.7	2.2	0.25	26.9	
3.0 10 ⁸	1.2	0.33	9.5	1.3	0.31	9.9	1.4	0.27	11.1	
$4.0 \ 10^8$	0.9	0.33	5.3	0.9	0.32	5.5	1.0	0.28	6.0	
5.0 10 ⁸	0.7	0.33	3.4	0.7	0.32	3.5	0.8	0.29	3.8	
	$\gamma_h=0.05 \text{ J/m}^2$, $\gamma_e=3\gamma_h$									
1.0 10 ⁸	6.0	0.33	394.0	6.7	0.28	445.8	8.7	0.20	607.4	
$2.0\ 10^8$	3.0	0.33	98.5	3.2	0.30	105.0	3.7	0.25	124.6	
3.0 10 ⁸	2.0	0.33	43.8	2.1	0.31	45.7	2.3	0.27	51.5	
4.0 10 ⁸	1.5	0.33	24.6	1.5	0.32	25.4	1.7	0.28	27.9	
5.0 10 ⁸	1.2	0.33	15.8	1.2	0.32	16.2	1.3	0.29	17.4	
$\gamma_h=0.1 \text{ J/m}^2$, $\gamma_e=3\gamma_h$										
1.0 10 ⁸	12.0	0.33	3152.1	13.5	0.28	3566.9	17.4	0.20	4859.6	
2.0 10 ⁸	6.0	0.33	788.0	6.4	0.30	839.5	7.4	0.25	996.7	
3.0 10 ⁸	4.0	0.33	350.2	4.2	0.31	365.5	4.7	0.27	411.7	
4.0 10 ⁸	3.0	0.33	197.0	3.1	0.32	203.5	3.4	0.28	222.9	
5.0 10 ⁸	2.4	0.33	126.1	2.5	0.32	129.4	2.6	0.29	139.3	









Activation barrier (expressed in $k_{\rm B}T$) for the nucleation of circular disc

ξ = 0.045, τ = 0

Transformation temperature = 520 K (250°C)







٨F	· · ·	$\xi = 0, \tau =$	0	$\xi = 0.05, \tau = 0.3$		
J/m^3	<i>a</i> *	A *	ΔF^*	<i>a</i> *	A *	$\varDelta F^*$
	nm	A ⁺	$k_B T$	nm	A	k_BT
1.0 10 ⁸	6.0	0.33	394.0	72.1	0.02	21148.0
2.0 10 ⁸	3.0	0.33	98.5	19.9	0.04	1754.5
3.0 10 ⁸	2.0	0.33	43.8	9.7	0.05	442.3
4.0 10 ⁸	1.5	0.33	24.6	5.9	0.06	173.6
5.0 10 ⁸	1.2	0.33	15.8	4.1	0.07	86.2






Nucleation Barrier

Nucleation Barrier

A

















Equilibrium shape an implicit function of the effective driving force (ΔF_v reduced by total elastic strain energy E_{el}) and is evaluated numerically as a function of ΔF_v and E_{el} .

$$\xi = -0.045, \ \tau = 0.33, \ \gamma_s = 0.1 - 0.3 \ \text{J.m}^{-2}, \ \mu = 26 \ \text{GPa}$$















Accommodation of shear strain energy may occur through:

self accommodation



or heterogenous nucleation:

- coherent nucleation in association with pre-existing defects providing an appropriate strain field
- sympathetic nucleation
- autocatalytic nucleation
- cluster-assisted nucleation







Self Accommodation



Christian, *The Theory of Transformations in Metals and Alloys* Pergamon (2002)



Howe, Dahmen, Gronsky, Philos. Mag. 56A p. 31 (1987)







Heterogeneous Nucleation

Nucleation at non-random, preferred sites providing assistance in surmounting activation barrier

1. Nucleation at Pre-existing Static Sites

1-, 2-, 3-D Structural Defects (in excess of equilibrium concentration)

- incoherent nucleation releasing strain energy of the defect
- coherent or partially coherent nucleation utilizing the strain field of the defect
- nucleation on stacking faults

Sequential Precipitation

- e.g. GP zone/ θ "/ θ '/ θ in Al-Cu
- nucleation on interphase boundaries
- sympathetic nucleation















Heterogeneous Nucleation

- 2. Nucleation at Preferred Sites defined Dynamically
 - Self-accommodation/Sympathetic Nucleation
 - Autocatalytic Nucleation

- formation of preferred heterogeneous arrays as a result of nucleation in the elastic strain fields of existing precipitates

Cluster-assisted Nucleation

- pre-nucleation solute clustering persists through the incubation period required for establishment of a finite nucleation rate





3DAP elemental mapping of an Al-4Cu-0.3Mg-0.4Ag (wt%) alloy aged 5 sec. at 180°C (Murayama and Hono, Scripta Mater. 1998)



3DAP elemental mapping of a {111}_a platelet in an AI-4Cu-0.3Mg-0.4Ag (wt%) alloy aged at 180°C *Reich, Murayama and Hono, Acta Mater.*, 1998









Figure 2. Elect for 0.083 h at 2 inside (in (a)) t line strain cor a dissociated F is shown in the

Rosalie, J.M., L.N. Bourgeois and B.C. Muddle, "Precipitate assemblies formed on dislocation loops in aluminium-silver alloys", *Philos. Mag*, Vol. 89, pp. 1267-78, 2009.









Figure 3. Micr Al_{98.3}Ag_{1.7} allo central (C) and showed that the









Figure 6. The disso in (a) where the loop loop lies. The faulted of this dislocation in The $(11\overline{1})$ glide plan the partial dislocation the passage of the Sh for each {110} facet which are located alt











Figure 2. The as-quenched defect structure of the $Al_{98,2}Ag_{0,9}Cu_{0,9}$ alloy, viewed close to the $[011]_{\alpha}$ zone in a two-beam condition with $g = 11\overline{1}$. The microstructure contains a population of approximately circular dislocation loops and some linear dislocations.

0.2h at 200°C

Rosalie, J.M., L.N. Bourgeois and B.C. Muddle, "Precipitate assemblies formed on dislocation loops in aluminium-silver-copper alloys", *Philos. Mag.*, Vol. 89, pp. 2195-2211, 2009.











2h at 200°C











































Al-Cu-Mg Alloys: Nucleation of S Phase on Dislocation Loops



Al-1.1Cu-0.5Mg

Al-0.2Cu-1.7Mg



Winkelman, G.B., R. Krishnamurthy and B.C. Muddle, "Orientation Relationships and Lattice Matching for the S Phase in Al-Cu-Mg Alloys", *Acta Mater.*, Vol. 55, pp. 3213-28, 2007.





Al-Cu-Mg Alloys: Nucleation of S Phase on Dislocation Loops

$\{111\}_{\alpha}$ -type Loop





















Autocatalytic Nucleation



Autocatalytic nucleation of θ^{\prime} in Al-Cu alloys

LM Brown, RH Cook, RK Ham and GR Purdy, *Scripta Met.*, **7** 815-20, 1973 V Perovic, GR Purdy and LM Brown, *Acta Metall.*, **27** 1075-84, 1979 V Perovic and GR Purdy, *Acta Metall.*, **29** 889-902, 1981 V Perovic, GR Purdy and LM Brown, *Scripta Metall.*, **15** 217-21, 1981













-1.5

Courtesy: Y Kryvasheyeu













-0.0002

-0.0003





















































Electron diffraction patterns using focused TEM probe **1nm** diameter.

Orientation relationship between β -Sn and matrix not found in the binary alloy Al-0.01Sn:

(100)β // (110)α, [010]β // [001]α























Christian, Progress in Materials Science 42 p. 101 (1997)







Summary

- those transformations giving rise to plate- or lath-shaped transformation products, and classically regarded as *diffusional*, are likely *diffusional-displacive* with a significant shear component
- at nucleation, the accommodation of shear strain energy may be at least as important as interfacial energy and may play a critical role in determining equilibrium nucleus shape – nucleation likely involves formation of 'loop' of transformation dislocation of critical form
- accommodation of shear strain energy may occur through:
 - (i) self-accommodation
 - (ii) coherent nucleation in association with pre-existing defects providing an appropriate strain field
 - (iii) autocatalytic nucleation
 - (iv) cluster-assisted nucleation







Shape Strain and Its Accommodation during Precipitation of Precipitate Plates

Jian-Feng Nie

Department of Materials Engineering Monash University, Australia

Joint AFRL/AOARD/LLNL Nucleation Workshop, Maui Hawaii, 2-7 May, 2010

www.monash.edu

Acknowledgements

Zhou Xu Matthew Weyland Hong Liu Yuman Zhu Allan Morton Yunzhi Wang **Barry Muddle** Australian Research Council ARC Centre of Excellence for Design in Light Metals





Questions

- Is there a shape strain in the formation of precipitate plates, and if so, how to quantify it
- What is the role of shape strain in nucleation and thickening of precipitate plates & what are the implications for alloy design




Plate-shaped precipitates are often key strengthening or toughening constituents in engineering







Mo₅Si₃ Precipitates in MoSi₂ S.Q. Xiao, S.A. Maloy, A.H. Heuer and U. Dahmen, Phil. Mag. A, 1995



Lattice Plane Deformation and Matching



planar interface is parallel to moire plane

J.F. Nie Acta Mater. 2004



J.F. Nie Acta Mater. 2004



(c)



J.W. Cahn, J.E. Taylor Acta Mater. 2004



Lattice Deformation Strain



Acta Mater. 2004



MARTENSITE*

F. C. FRANK †

*Received August 5, 1952. †The H. H. Wills Physical Laboratory, University of Bristol, England.

ACTA METALLURGICA, VOL. 1, JAN. 1953



Input Data: g_{mx} , g_{my} , g_{px} , g_{py} , θ_m , θ_p **Output:** α (or β), ϕ , lattice deformation strains, shape strain

J.F. Nie, Acta Mater. 2008

s, > 0	η _ν < 1	η _y = 1	η _y > 1
	a • • • • •	b 0• 0• 0•	с о•о•о•
η _x < 1	€ 	• • •	• • •
	• • • •	•0 •0 •0	0 0 Q
	d 0• 0• 0•	e g _{mx} ○• ○• ○•	f 0• 0• 0•
$\eta_x = 1$	• • •		• • •
	• 0 • 0 •0	•0 •0 •0	• • • • • •
	g •••••••	h 0.0.0.	i 0. 0. 0
η _x >1	• • •	• • •	G ()
	• 0 • 0 •0	•0 •0 •0	● ●○ ●○



J.F. Nie, Acta Mater. 2008



Mg₁₇Al₁₂ precipitate in Mg-9Al-1Zn





Lath Martensite in Fe-20.2Ni-5.4Mn T. Moritani, N. Miyajima, T. Furuhara and T. Maki, Scripta Mater. 2002



Input

ratio of $g_{(002)m}/g_{(002)t}$ $g_{(200)m}/g_{(200)t}$, θ_{m} , θ_{p}

Output

 $\varphi = 0^{\circ} (200)_{m} // (200)_{t}, [0\overline{10}]_{m} // [001]_{t}$ $\beta = 16.15^{\circ}$ $\epsilon_{d} = 0.0448; \epsilon_{s} = 0.1548$ J.F. Nie, B.C. Muddle, *Mater. Sci. Eng.*, 2006



Cr Precipitate in Cu - K.S.

T. Fujii, H. Nakazawa, M. Kato and U. Dahmen, Acta Mater., 2000





Cr Precipitate in Cu - N.W. T. Fujii, H. Nakazawa, M. Kato and U. Dahmen, *Acta Mater.*, 2000



LDS

$$\mathsf{T} = \begin{pmatrix} 1.092 & 0.365 \\ 0 & 1.030 \end{pmatrix}$$

OR and HP

$$\begin{array}{ll} \phi &= -0.44^{\circ} & (111)_{f} \, \mbox{//} \, (011)_{b} \\ \beta &= 14.50^{\circ} & [011]_{f} \, \mbox{//} \, [100]_{b} \\ \epsilon_{d} &= 0.1246; \, \epsilon_{s} = 0.3477 \end{array}$$





Output: $\phi = 0^{\circ}, \beta = 0^{\circ}$ $\varepsilon_d = 0.086; \varepsilon_s = 0.227$

J.F. Nie and B.C. Muddle *Acta Mater*. 2000



















Nucleation Engineering: Multiscale Integration

G.B. Olson

Northwestern University & QuesTek Innovations LLC Evanston, IL







Fig. 1 Dynamic Hierarchy of Martensitic Microstructure [5].

Structure Level



Principal parameters defining a "theory space" for martensitic nucleation

Reference: Olson, G.B., and Roitburd, A.L., 'Martensitic Nucleation', Ch. 9 in *Martensite*, ed. Olson, G.B. and Owen, W.S., ASM International (1992), p. 154

Hierarchy of Design Models








Fig. 11—Critical driving force for homogeneous, coherent nucleation in Fe-Co as a function of temperature. Circles are data from the article of Lin *et al.*^[15] The lower dotted line is the prediction of the nonclassical nucleation model with the material parameters taken directly from Lin *et al.* The solid line is a fit of the nonclassical model to the data



produce a/18 [121] partial dislocations of Figure 4, (c) simultaneous generation of lattice dislocations of Figure 4.



Grain-size dependence of acoustic-emission M_s^{AE} (open symbols) and electrical-resistivity M_b (closed symbols) measured in Fe-32.3Ni. Circles represent acoustic emission experiments conducted at 70 dB gain; triangles denote more sensitive measurements at 90 dB gain.

Reference: Olson, G.B., and Roitburd, A.L., 'Martensitic Nucleation', Ch. 9 in *Martensite*, ed. Olson, G.B. and Owen, W.S., ASM International (1992), p. 169

Distributed Heterogeneous Nucleation: CryoMART Simulator



Areal Fraction Martensite

Basic *PrecipiCalc* Equations: Particle Growth

Growth:
$$\frac{dR}{dt} = \frac{\left(1 + R\sqrt{4\pi N_v \langle R \rangle}\right)}{\left(R\Gamma + s(R) / \left(M_0 \exp \frac{-Q}{RT}\right)\right)} \left\{\Delta G_m - \frac{2\sigma(R)\overline{V}_m^\beta}{R}\right\}$$
where $\Delta G_m = \left[\Delta \overline{C_i}\right]^T \left[\frac{\partial^2 \overline{G}^\alpha}{\partial C_i \partial C_j}\right] \left[\Delta C_j^\infty\right] + \left[\overline{C}_m^\beta\right] \bullet \left(\left[\overline{\mu}_m^\alpha\right] - \left[\overline{\mu}_m^\beta\right]\right)$

$$\Gamma = \left[\Delta \overline{C_i}\right]^T \left[\frac{\partial^2 \overline{G}^\alpha}{\partial C_i \partial C_j}\right] \left[\overline{D}_{jk}\right]^{-1} \left[\Delta C_k^e\right]$$

$$\frac{\mathsf{I} hermodynamics}{\mathsf{Interfacial Property}} \qquad \mathsf{subcritical} \qquad \mathsf{subcritical} \qquad \mathsf{supercritical}$$

Basic PrecipiCalc Equations: Classical Homogeneous Nucleation

Steady State Nucleation Rate
$$J_{SS} = Z\beta^* \frac{N_a}{V_m^a} e^{\frac{-W_a^*}{k_B^T}} = \int_0^\infty \overline{J}_{SS}(R) dR$$

where Zeldovitch factor $Z = \left[\frac{V_m^{\beta^2}\sigma}{4\pi^2 N_a^2 k_B T R_c^4}\right]^{1/2}$
work to form a critical nucleus $W_R^* = \frac{16\pi\sigma^3}{3\left(\Delta G_m/V_m^{\beta}\right)^2}$
rate of atomic impingement $\beta^* = 4\pi R_c \frac{N_a}{V_m^{\beta}} \frac{\Delta G_m}{\Gamma}$
 N_a is Avogadro's number, k_B is Boltzmann's constant
 R_c is critical radius where $dR/dt = 0, T$ is temperature
Incubation Time τ calculated from $\begin{cases} \int_0^\tau \beta^*(t') dt' = \frac{1}{\theta Z(t)^2}, & \text{if } \tau < t \\ \int_0^\tau \beta^*(t') dt' + \beta^*(t)(\tau - t) = \frac{1}{\theta Z(t)^2}, & \text{if } \tau > t \end{cases}$, where $2 < \theta < 4\pi$

►R

-1/3

which gives $\tau = \frac{1}{\theta \beta^* Z^2}$, at isothermal conditions. Note t = 0 at the start of incubation.

NASA Microstructure Modeling: 3rd Generation Disk Alloys





Ni-6.5 Al-9.5Cr at. % alloy aged at 873K

Reference: Booth-Morrison, C., Zhou, Y., Noebe, R.D., and Seidman, D.N., (2009) 'On the nanometer scale phase separation of a low-supersaturation Ni-Al-Cr alloy', *Philosophical Magazine*, 99999:1.



The compositional trajectories of the γ -matrix and γ '-precipitate phases of Ni-6.5 Al-9.5 Cr at. %, displayed on a partial Ni-Al-Cr ternary phase diagram at 873K.

Reference: Booth-Morrison, C., Zhou, Y., Noebe, R.D., and Seidman, D.N., (2009) 'On the nanometer scale phase separation of a low-supersaturation Ni-Al-Cr alloy', Philosophical Magazine, 99999:1.





Reference: Staron, P. and Kampmann, R., (2000) 'Early-stage decomposition kinetics in Ni-Al alloys—I. Small and wide-angle neutron scattering investigation on Ni-13 at.% Al and clusterdynamic modelling', *Acta Materialia*, 48:701-712.

$$\frac{dC_{n_{\rm X}}}{dt} = J_{n_{\rm X}-1\to n_{\rm X}} - J_{n_{\rm X}\to n_{\rm X}+1} \quad \forall \ n_{\rm X} \ge 2,$$

$$J_{n_{\rm X}\to n_{\rm X}+1} = \beta_{n_{\rm X}}C_{n_{\rm X}} - \alpha_{n_{\rm X}+1}C_{n_{\rm X}+1},$$

$$\frac{dC_1}{dt} = -2J_{1\to 2} - \sum_{n_{\rm X}\ge 2} J_{n_{\rm X}\to n_{\rm X}+1},$$
Condensation Rate (long range diffusion control)
$$\beta_{n_{\rm X}} = 4\pi r_{n_{\rm X}}\frac{D_{\rm X}}{\Omega}C_1,$$
Dissolution Rate (equilibrium cluster size distribution)
$$\alpha_{n_{\rm X}+1} = 4\pi r_{n_{\rm X}}\frac{D_{\rm X}}{\Omega}\exp\left[(36\pi)^{1/3}a^2\left((n_{\rm X}+1)^{2/3}\sigma_{n_{\rm X}+1}\right) - n_{\rm X}^{2/3}\sigma_{n_{\rm X}} - \sigma_1\right)/kT\right].$$



Heterogeneous Nucleation at Grain Boundaries

Nucleation Rate $J = \exp\left(-\frac{\tau}{t}\right) Z\beta^* N(1-f_s)e^{\frac{-W}{k_B T}}$, k_B is Boltsman constant and T is temperature Energy Barrier $W^* = W_h^* f$, where f is a volumetric correction factor: $= \begin{cases} (2 - 3\cos\theta + \cos^3\theta)/4, (a) \\ (2 - 3\cos\theta + \cos^3\theta)/2, (b) \\ \frac{6}{4\pi} \left[\pi - 2\sin^{-1}\left(\frac{1}{2}\csc\theta\right) + \frac{1}{3}\cos^2\theta\sqrt{4\sin^2\theta - 1} - \cos^{-1}\left(\frac{\cot\theta}{\sqrt{3}}\right)\cos\theta\left(3 - \cos^2\theta\right) \right], (c) \end{cases}$ $f = \langle$ Available Nucleation Sites $N = \begin{cases} 2N_0 (\delta / \overline{D}), (a), \delta \approx 0.1 \text{nm}, \overline{D} \text{ is grain diameter} \\ N_0 (\delta / \overline{D}), (b) \\ N_0 (\delta / \overline{D})^2, (c) \end{cases}$ Nucleation Site Consumption Ratio $f_s = \begin{cases} \left(\frac{\pi N_v \overline{R} \sin^2 \theta}{\overline{D}}\right)_{,3}^{,3}, (a), \overline{D} \text{ is grain diameter, } \overline{R} \text{ is mean size} \\ \left(\frac{\pi N_v \overline{R} \sin^2 \theta}{\overline{D}}\right)_{,6}^{,6}, (b) \\ N_v \overline{R}^2 \left(1 - 4\cos^2 \theta / 3\right)^{1/2} \\ \frac{3\alpha_e}{\overline{D}^2}, \text{ where } \alpha_e \approx 30 \text{ (c)} \end{cases}$

Zeldovitch factor $Z = Z_h f^{1/2}$

Incubation Time $\tau = \frac{1}{\Theta \beta^* Z^2} = \frac{1}{\Theta \beta^* Z_h^2 f}$, where $\Theta \in (2, 4\pi)$

Impingement Rate $\beta^* = gR_c^2 \frac{N_a}{V_m^{\beta}} \begin{cases} dR/dt, \text{ for mass tranport controlled nucleation, } R_c \text{ critical size} \\ D/_{6a}, \text{ for interfacial controlled nucleation, } V_m^{\beta} \text{ molar volume} \end{cases}$

Surface correction factor
$$g = \begin{cases} 2\pi(1-\cos\theta), (a) \\ 4\pi(1-\cos\theta), (b) \\ 6\pi-12\sin^{-1}\left(\frac{1}{2}\csc\theta\right) - 12\cos\theta\cos^{-1}\left(\frac{\cot\theta}{\sqrt{3}}\right), (c) \end{cases}$$

mass balance $V^{\beta} = \frac{4\pi}{3} f R^3$

(a) coherent particle on flat impurity

(b) incoherent particle on grain boundary

(c) trijunction edge line

Heterogeneous Nucleation on Dislocations

Nucleation Rate = $Z\beta^* Ne^{\frac{-fW_R^*}{k_BT}}e^{-\tau/t}$, with a defect interaction factor f

Available Nucleation Site Density, $N = \frac{N_a}{V_m^{\alpha}} \left(\pi (1.5b)^2 \right) \left(\rho - 2N^{\text{tot}} \overline{R} \right)$

Incubation Time,
$$\tau = \frac{1}{\theta \beta^* Z^2 f}$$

Energy Barrier for Nuclation, $W_R^* = \frac{16\pi\sigma^3}{3(\Delta G_m / V_m^\beta)^2}$

Atomic Impingement Rate, $\beta^* = 4\pi R_c \frac{N_a}{V_m^{\beta}} \frac{\Delta G_m}{\Gamma}$

Heterogeneous M₂C Nucleation on Dislocations



Reference: King, K.C., Olson, G.B., and Mura, T., 'Elastic Energy of Coherent Precipitation at Dislocations in an Anisotropic Matrix', Ch. 7 in *Modern Theory of Anisotropic Elasticity and Applications*, ed. Wu, J.J., Ting, T.C.T., Barnett, D.M., Society for Industrial and Applied Mathematics (1991), pp.103-121.

AF1410 Precipitation Simulation

Isothermal M₂C precipitation simulation of AF1410 steel at 510°C, along with the experimental results from G.B. Olson, T.J. Kinkus and J.M. Montgomery, *Surface Science* 246 (1992) 238. Parameters used in the simulation include: surface energy σ_{coh} =0.25J/m², σ_{incoh} =1.0J/m², ρ =2.5x10¹⁴ (1/m²), f=0.55, ΔR_{tran} =5, D_{pipe}/D_{vof} =100.



Heterogeneous nucleation of solidification in atomized liquid metal droplets M. Libera, G.B. Olson and J. B. Vander Sande

Department of Materials Science and Engineering, Massachusetts Institute of Technology, Cambridge, MA 02139 (U.S.A)



Fatigue Nucleation

- Fatigue in gear steels:
 - Sliding-Rolling Contact
 - Single Tooth Bending
- Minimum bending fatigue strength controlled by subsurface inclusions:
 - Not all inclusions are equally potent
 - Al₂O₃ vs La₂O₂S inclusion clusters in GearMet C61 and C67



La₂O₂S inclusion cluster









Inclusion Clusters: 3D Tomography

Damaged TiN Pair in Mod4330

(J. Sebastian, H.-J. Jou, QuesTek; M. Uchic, AFRL)





La₂O₂S Cluster in C61-La Gear Steel (S. Chan, NU; G. Spanos, NRL)



Design Research Tools Consortium Contract No. N00014-05-C-0241



3D Microstructure-Sensitive Fatigue Simulator



Modeling fatigue in Ni base superalloys



S. Kajiwara et al.





(a) Change in angle between $(11\overline{1})_f$ and $(1\overline{1}\overline{1})_f$ when crossing the interface in the $[12\overline{1}]_f$ direction on the $(1\overline{1}\overline{1})_f$ plane from the austenite region to the martensite region. The abscissa represents distance along the $(1\overline{1}\overline{1})_f$ plane in the $[12\overline{1}]_f$ direction in units of $a_f\sqrt{6}/4(=0.2192 \text{ nm})$. (b) Change in angle between $(11\overline{1})_f$ and $(1\overline{1}\overline{1})_f$ when crossing the interface in the $[\overline{1}21]_f$ direction on the $(11\overline{1})_f$ plane. The abscissa represents distance along the $(11\overline{1})_f$ plane in the $[\overline{1}21]_f$ direction in the same units as in (a).



Fig. 8 Nucleation strain path. Schematic illustrations of nucleus structure in three regimes of behavior, with associated theoretical approximations

Heterogeneous Martensitic Nucleation

Discrete Dislocation



Ginzberg-Landau Continuum





Fig. 15 Role of heterogeneity of nucleation. Schematic curves of energy (ΔW) versus size (r) depict behavior for homogeneous, weak-defect heterogeneous, and strong-defect heterogeneous nucleation at four levels of driving force (Δg).

M_s Temperature Validation





Reference: Staron, P. and Kampmann, R., (2000) 'Early-stage decomposition kinetics in Ni-Al alloys—II. Cluster dynamic modelling of former experimental results', *Acta Materialia*, 48:713-720.



High Pressure: a new Realm

Daniel Orlikowski

Condensed Matter and Materials Division Physical and Life Sciences Directorate Lawrence Livermore National Laboratory, Livermore, CA

Maui, Hawai`i



UCRL-PRES-xxxx

This work performed under the auspices of the U.S. Department of Energy by Lawrence Livermore National

Laboratory under Contract DE-AC52-07NA27344.

Melt-line Kinetics Team: spanning time scales



Nucleation & Growth:	
Molecular Dynamics:	D. Richards, J. Glosili
DTEM:	T. Lagrange, B. Reed
dDAC:	W. Evans + Post Doc.
Any universal scaling of rates, heterogeneity, phase fraction	
Coalescence:	
Phase Field Simulations:	J. Belak, M. Tang
DTEM + dDAC	
Compression experiments + X-ray: J. Hawreliak, D. Swift	
Growth and micro-structure:	M. Kumar
Continuum strength:	
crystal continuum modeling:	N. Barton
Compression experiments	
"physics" code: thermo-mechanical, poly-crystal	
Model:	R. Minich, D. Orlikowski
self-consistent, homogenization, final continuum model	





Materials on Demand :: Pressure induce phase transitions



Amorphous Sulfur via Pressure

Vereshagin, et al. 1993





Icy planets: Water phases make the difference



Figure 9: Examples of central pit craters on Ganymede: Isis crater, 73 km in diameter (A); Sebek crater, 64 km in diameter (B); and Bes crater, 62 km in diameter (C). (Voyager images FDS 20640.33, 16405.48, and 20637.41.)

The character of these craters are determined by the ice phases of Water.

(Senft & Stewart 2009)

Kinetics model was not implemented.





Path Contributions to a Final State: sketch







Recent observations: water



Intensity measurements of Ice nucleation/growth at an interface

Dendritic or fractal growth

Interface particle velocities that indicate over-driven and relaxation processes occur.

Imaging Ice Formation



Dyna-DAC: G.W. Lee et al. (2006)



0.1mHz-20kHz => 0.1-10^4 1/s





Pressure loading dependence:



Time



FIG. 5 (color online). $\Delta P/kT$ as a function of strain rate across equilibrium Bi I-II equilibrium phase boundary.




Melt-line kinetics project flow:





From atomistics to the continuum...



J. Belak, et al.



Development toward a more physical model (Minich)

<u>CNT:</u>

Free Energy accounting for surface energy

$$\Delta G(N, P, T) = \underbrace{a \, \sigma \, N^{\frac{2}{3}}}_{\text{Surface}} - \underbrace{N \Delta \mu}_{\text{Volume}}$$

Critical Energies and lengths

$$\Delta G_c(N_c, P, T) \approx \frac{\sigma^{lpha}}{\Delta \mu^{eta}}$$

Distribution of size and shapes

$$J_n = \int j_n(R,t) dR$$

Phase fraction (iterative)

$$\dot{\phi} \propto \Delta G J(N, P, T) [1 - \phi] \Delta \mu(N, P, T)$$

Kolmogorov type phase fraction

$$f_2 = 1 - exp\left[-\frac{A}{4}J_d v_{int}(t-t_0)^4\right]$$







Phase fraction rate:

N

E

F

р

$$\dot{\Phi} = \Lambda \Delta G^{\Gamma} Exp \begin{bmatrix} -\frac{B}{\Delta G} \end{bmatrix} (1 - \Phi) \begin{bmatrix} a \Delta G^{\gamma} \Phi - b \Phi^{\alpha} \end{bmatrix}$$
Self-consistent hydro-code time step:
 $\delta t \frac{dP_r}{d\Phi} \dot{\Phi} + P_{rm} = P_r$
Melt-line: Pc and Tc
exponents are left open b/c of possible fractal
rystallites, not smooth nor round
four open parameters:
nucleation rate, over-pressurization,
hase fraction dependence, percolation
$$det = \frac{B}{\Delta G} \begin{bmatrix} (1 - \Phi) & [a \Delta G^{\gamma} \Phi - b \Phi^{\alpha}] \end{bmatrix}$$

Over-driven transition with relaxation similar to exp. Parameterization is meant to be bottom-up Lambda rate ~ 10⁵ Critical pressure is considered the meltline: P~ 2 GPa

Rate of change of Order parameter







Water phase diagram







Prototypical observations to be modeled: compressed water



PMMA

Sapphire

Exp. Input wave are not known well Impurities have been minimized





Hydro phase transformation: compression rate dep.





Evolution of compression as function of distance



With the model, Interpretations are difficult

Non-linear effects between Compression wave PT model Reflections



Pressure Wave Snapshots without phase transition











Increasing the duration of the phase transition





We plan to bring together the necessary components for a Melt-line phase transition model:

- Spans nanosec to microsec time scales.
- Atomistic, phase-field, crystallographic and continuum modeling will be used.
- · Understand missing physics.
- · Verify with experiments.
- . Understand sensitivities at the continuum level.

A comprehensive, physics-based model would incorporate

- I) Probabilistic Nucleation size/shape distribution
- II) Kinetics of the surface
- **III)** Percolation
- IV) Over-pressurization and relaxation
- V) Amorphous formation or freezing
- VI) Strength





Time: why is the delay time different---Exp. And Simulations Rare events?

Ion-interaction descriptions: what needs to be included ---viscosity, transition path ways ➡ DFT and metadynamics

Sensitivities: errors, "real" system variations,





To develop a robust continuum phase transition model that incorporates modern theory and simulates recent observations of pressure-induced phase transitions.... **Probabilistic variations** 1) Nucleation size/shape distribution II) Kinetics of the surface amorphous solid **III)** Percolation Pressure Nucleation IV) Over-pressurization and relaxation Nucleation + Growth V) Amorphous formation or freezing Pm liquid VI) Strength Time





Recent insight into past large-scale MD simulations(Belak)



D. Orlikowski, Lawrence Livermore National Laboratory, orlikowski1@IInl.gov, May 2010-24

Development toward a more physical hydro model (Minich)

<u>CNT:</u>

Free Energy accounting for
surface energy
$$\Delta G(N, P, T) = a \sigma N^{\frac{2}{3}} - N$$

 $\Delta G_c(N_c, P, T) \approx \frac{\sigma^{\alpha}}{\Delta u^{\beta}}$

Critical Energies and lengths

Distribution of size and shapes $J_n = \int j_n(R,t) dR$

Phase fraction (iterative) $\dot{\phi} \propto \Delta G J(N, P, T) [1 - \phi] \Delta \mu(N, P, T)$

Kolmogorov type phase fraction

$$f_2 = 1 - exp\left[-\frac{A}{4}J_d v_{int} (t - t_0)^4\right]$$

 Δu







Phase fraction rate:

$$\dot{\Phi} = \Lambda (P_r - P_c)^{\Gamma} Exp[-\frac{B}{(P_r - P_c)^y}] (1 - \Phi) [a(P_r - P_c)^{\lambda} \Phi - b\Phi^{\alpha}]$$

Self-consistent hydro-code time step:

$$\delta t \; \frac{dP_r}{d\Phi} \; \dot{\Phi} + P_{rm} = P_r$$

Melt-line: Pc and Tc

Four exponents are left open b/c of possible fractal crystallites, not smooth nor round Four open parameters:

nucleation rate, over-pressurization, phase fraction dependence, percolation







Each time scale needs to be benchmarked against experiment.



Materials on Demand ::



understanding the pressure dependent kinetic barriers

Ammonia borane stores 8-12 wt% hydrogen at 6 Gpa $NH_3BH_3 + H_2$

Hydrogen storage at pressure

Not stable at ambient pressure



Lin Y et al. PNAS 2009;106:8113-8116





Experiments: capturing the solidification front

Physics Quantity	Diagnostic	Facility	Platform
Nucleation Distribution Function(R,t)	SAXS Imaging	APS, LCLS LLNL	dDAC DTEM
Atomic Solidification Front	Coherent Diffractive X-ray Imaging	LCLS	dDAC LPXP
Nucleation, Growth, Coalescence	Imaging X-ray	APS, LCLS	dDAC LPXP
Solid Phase Fraction(t)	<i>in situ</i> X-ray Diffraction + Streak	JLF, LLE, SNL	Janus, OMEGA, Z-pinch
Indirect Material Response(t)	Velocimetry	JLF, LLE, SNL	Janus, OMEGA, Z-pinch

Prototypical observations to be modeled: compressed water



For Liquid-Solid transition,

there is limited experimental evidence, in general.

The over pressurization may be a strain-rate dependent.

Continuum models do not capture this relaxation



Atomistics: nucleation rates (Richards)









Atomistics: (Richards)





AI: 32m atoms



Issues: Ion potentials Rates Scale



MD will not get us to the hydrodynamic time of interest: Belak



Phase Field Modeling (PFM) will get us to the hydrodynamic time of interest



D. Orlikowski, Lawrence Livermore National Laboratory, orlikowski1@llnl.gov, May 2010-33

MD nucleated microstructure onto phase field model: linking time scales (Belak)





While significant grain coarsening has occurred on the microsecond scale, the microstructure is far from log-normal



Quasi-static polycrystal compression of Fe: transformation progresses from grain boundaries (Barton)





Interaction energy influences response and microstructure (Barton)





Phase Field modeling is time-dependent Ginzburg-Landau theory



$$F(\phi) = \int dx \left[\frac{1}{2} \left| \nabla \phi \right|^2 + f(\phi, P, T) + f_{GB}(\nabla \theta) + f_{el} \right]$$

Total Free Energy of multi-phase material



Local Free Energy Density $f(\phi) \approx \phi(1-\phi)(1+\phi)$

$$\frac{\partial \phi}{\partial t} = -\Gamma(-\nabla^2)^a \frac{\delta F}{\delta \phi} + noise$$

Kinetic Equation with Thermal Noise



Pusztai et al., have proposed a 3D quaternion-based phase-field model

- · Represents crystal orientation with quaternion order parameter
- · Quaternions are widely used to analyze crystallography of polycrystal interfaces
- · Quaternion algebra is fast, efficient, avoids singularities, ...

Free
Energy
$$F = \int \left[\frac{\varepsilon_{\phi}^{2}}{2} |\nabla \phi|^{2} + f(\phi, c, T) + HT[1 - p(\phi)] \left(\sum_{i} (\nabla q_{i})^{2} \right)^{1/2} \right] d^{3}r$$

Evolution
$$\frac{\partial q_{i}}{\partial t} = -M_{q} \frac{\delta F}{\delta q_{i}} + \zeta_{i} = M_{q} \left[\nabla \cdot \left(D \frac{\nabla q_{i}}{|\nabla q_{i}|} \right) - 2\lambda q_{i} \right] + \zeta_{i}$$

Where q_i is the quaternion order parameter, M_q is the associated mobility and ζ is the fluctuation in q.

We have implemented the Pusztai model in our 3D AMR code

- · Enhance energy functional to represent energetics of grain boundaries
- · Crystal symmetry aware quaternion mathematics
- · Extend energy functional to include elasticity and alloy concentration

Refs: T. Pusztai, G. Bortel, and L. Granasy, "Phase field theory of polycrystalline solidification in three dimensions," Europhys. Lett, 71 (2005) 131-137; R. Kobayoshi and J.A Warren, "Modeling the formation and dynamics of polycrystals in 3D," Physica A 356 (2005) 127-132.





A shift in dimension during the phase transition

Nucleation vs. growth velocity







D. Orlikowski, Lawrence Livermore National Laboratory, orlikowski1@Ilnl.gov, May 2010-40

1D dynamic simulations using ALE3D explore interactions between plasticity and phase transformation (Barton)

Bain transformation mechanism, with full reverse transformation modes



case	$\dot{\gamma}_{\sf ro}\left(\mu{\sf S}^{-1} ight)$	CS
а	10^{-3}	1
b	10 ⁰	1
С	10 ³	1
d	10 ⁶	1
е	10 ³	0.5
f	10 ³	0.25

For example:

Armstrong *et al.*, *JAP*, 2009 Barton *et al.*, *MSMSE*, 2009

- . Initially cube-oriented alpha single crystal
- Pressure BC on loading face: peak pressure of 20 GPa, 4 ns pulse duration
- Periodic lateral BCs
- 100 microns in depth









Varying the compression wave




There are several contributions that effect the final density rho(P,T) or rho(P,E):

- The cold and the electron (Pe) and/or ion (Pi) thermal contributions (blue solid)
- The material strength also contributes to the entropy or heat (blue dashed)
- The kinetics associated with every traversed phase line (red solid line) Delays in transition, developing shocks, not fully transformed material

We think we know (reasonably):

The cold contribution P(V,T=0), comparison to DAC

And to some extent the thermal contributions, comparison to Hugoniots and to *known* phase lines

(instice will contribute a min, of 100 ps in wave propagat

Kinetics will contribute a min. of 100 ns in wave propagation arrival time,

Comparison to experiment(J. Nguyen)

Unknown aspects:

The phase diagram in general is not well determined

---liquid-liquid transition, high temperature phases (suggested),

high pressure melt line

The strength is not well defined b/c of the unknown phases and

still is under development theoretically

Kinetics are completely unknown

---general theory is still developing, experiments are minimal to zero



Continuing LLNL's tradition as a forerunner...

Pressure component of phase transitions has not been significantly studied:

- ⇒ gives new insights into Classical Nucleation Theory(CNT) via pressure
- → asserts LLNL as an authority in phase transitions at pressure
- → begins to understand pressure-dependent kinetic barriers

Improved understanding and modeling enables:

- new materials on demand to be obtained/understood from high pressure
 significant computational resources for *quantitative results*
 - and analysis to overlap with experiments, in length and time.
- ➡ models that are high impact for Stockpile Stewardship Science and Boost







Analysis and Modeling of Nucleation Controlled Reactions

Professor John H. Perepezko University of Wisconsin--Madison Dept of Materials Science and Engineering 1509 University Avenue Madison, WI 53706 AFOSR Nucleation Workshop Maui, Hawaii, May 2-6, 2010



•INTRODUCTION •Classical Theory – Highlights •Applications and Limitations •Nucleation Theorem •Grain Refinement •Dynamics •Phenomenological •Experimental Approaches •Indirect •Direct •Nucleation Density •Size Distribution •Transient time •Nucleation Statistics •Experience •Primary Nanocrystallization

•Nucleant Refining

•Open Issues-Future Directions



(a) large Ni- base single-crystal droplet after 20°C/min cooling from a very pure melt; (b)/(c) laser processed Al-26%Si, laser velocity 100 mm/s (b) and 500 mm/s (c), showing fine equiaxed silicon crystals surrounded by a-Al cells and distributed in a fibrous eutectic matrix (plane view); (d)/(e) AlY₇Fe₅ droplets, cooled in the DTA with two intermetallic particles surrounded by a eutectic matrix (d) or water quenched with numerous intermetallic particles (e); (f) AlY₇Fe₅ melt spun ribbon after an isothermal annealing treatment for 10 min at 275°C, density of nanocrystals is greater than 10^{22} m⁻³.

Classical Nucleation Theory

Kinetic Model

- Clusters of particles originate when two atoms come together.
- These clusters are in equilibrium with the surroundings and can grow or shrink by the addition or removal of single particles.
- Most clusters will break up into single particles, but there will be some (small) probability that a cluster will grow large enough (i.e. to the critical size) that the number of particles that leave the cluster will just equal those that come to it.
- If the cluster grows larger that this critical size, it will not shrink, but will grow to a macroscopic size particle.

Nucleation Kinetics

In nucleation cluster size is a configurational coordinate. A flux is the net number of clusters/cm³-sec. growing from size n to (n+1).Let C(n,t) represent the number of clusters of size n that exist in the system at time t. Then,

$$\frac{\partial C}{\partial t} = \beta A'(n-1)C(n-1,t) + \alpha A'(n)C(n+1,t) - \beta A'(n)C(n,t) - \alpha A'(n-1)C(n,t)$$

Where β is the impingement frequency of a monomer (for nucleation in vapors) α is the evaporation frequency and A'(n) is the area of space around the cluster which will hold an impingement monomer. This procedure is called <u>Detailed Balancing</u>. By definition, at equilibrium $\partial c/\partial t=0$ and C=Co. Thus, at equilibrium:

$$\beta A'(n-1)Co(n-1,t) + \alpha A'(n)Co(n+1,t) = \beta A'(n)Co(n,t) + \alpha A'(n-1)Co(n,t)$$

If there is no steady state growth of clusters through the size classes (i.e. for steady state conditions), the preceding equation can be made more restrictive,

$$\beta A'(n-1)Co(n-1,t) = \alpha A'(n-1)Co(n,t)$$
or
$$Co(n-1,t)$$

$$\alpha = \beta \frac{CO(n-1,t)}{Co(n,t)}$$

It should be noted that by using an equilibrium condition, α has been determined by invoking the <u>principle of time reversibility</u>. This principle requires that at equilibrium every microscopic process takes place at the same rate as its reverse. Substituting for a in the rate equation

$$\frac{\partial C}{\partial t} = \beta A'(n) Co(n,t) \left[\frac{C(n+1,t)}{Co(n+1,t)} - \frac{C(n,t)}{Co(n,t)} \right]$$

$$=\beta A'(n-1)Co(n-1,t)\left[\frac{C(n,t)}{Co(n,t)}-\frac{C(n-1,t)}{Co(n-1,t)}\right]$$

The preceding is the difference-differential equation for nucleation. This equation can be greatly simplified if we assume that C/Co and Dco vary slowly with n and if we disregard terms of higher than second order. To proceed, we define

$$D(n) = \beta A/(n) = \beta A(n)$$

where A(n) is the surface area for size n, A'(n) is the area around a cluster of size n that can accept a monomer, and D(n) is the diffusion coefficient of cluster in cluster size space. Now, we expand in a Taylor series about n the following functions

$$\frac{C(n+1)}{Co(n+1)} \qquad \frac{C(n-1)}{Co(n-1)} \qquad D(n-1)Co(n-1)$$

Substituting these into the difference differential equation yields:

$$\frac{\partial C}{\partial t} = \frac{\partial}{\partial n} \left[D(n)Co(n) \frac{\partial \left(\frac{C(n)}{Co(n)}\right)}{\partial n} \right]$$

The above is the isothermal nucleation equation and has the form of Fick's 2nd law of diffusion in a force field. This observation is consistent with the view that nucleation is a random-walk process through cluster size space. We can rewrite the nucleation equation as an equation of continuity as follows:

$$\frac{\partial C}{\partial t} + \frac{\partial J(n)}{\partial n} = 0 \qquad and \qquad J(n) = -DCo \frac{\partial}{\partial n} \left(\frac{C}{Co} \right)$$

where J(n) is the net number of clusters growing from size n to (n+1). Equation (4) can also be written as:

$$J(n) = -D\frac{\partial C}{\partial n} + UC \qquad and \qquad U = D\frac{1}{Co}\frac{\partial Co}{\partial n} = D\frac{\partial}{\partial n}(\ln Co)$$

random walk term drift velocity, U, term

The Steady State

We now consider the possibility that a steady state current of clusters exists without any change in C (i.e. In order to produce such a situation, we must continuously supply monomers to keep C(1) constant and remove all the clusters equal to or larger than a certain size, n, so that size will not go to infinity). This scheme was first proposed by Becker and Döring, Ann. Physik, <u>24</u>, 719 (1935). Using the equation for the nucleation rate we have.

$$J_{s} = -DCo\frac{\partial}{\partial n}(Cs/Co)$$

where the subscript s indicates steady state. Also, from the steady state model we can write

$$(C_{S} / Co)_{n=1} = 1$$
 and $(C_{S} / Co)_{n=\hat{n}} = 0$

Integrating the equation for J_s yields

$$\int_{n=1}^{n=\hat{n}} -\frac{J_{s}}{DC_{o}} dn = \int_{1}^{\hat{n}} d(Cs/Co) = -1 \quad or \quad J_{s} = \frac{1}{\int_{1}^{\hat{n}} dn/DCo}$$

In general

$$Co(n) = C(1) \exp\left[\frac{-\Delta G(n)}{kT}\right]$$

Where C(1) is the number of monomers and $\Delta G(n)$ is the free energy to form a cluster of size n. C_o has a sharp minimum when ΔG is maximized, or when n=n_c. Thus, we can set D=D_c and approximate C_o by expanding $\Delta G(n)$ about n_c to the second order to get

$$J_{S} = D_{C}C_{O}(n_{C}) \left[\frac{\partial^{2} \Delta G(n_{C})}{\frac{\partial n^{2}}{2\pi kT}} \right]^{1/2} = DC_{O}Z$$

where

$$Z = \left[\frac{\partial^2 \Delta G(n_c)}{\frac{\partial n^2}{2\pi kT}}\right]^{1/2} = \left[\frac{-1}{2\pi}\left(\frac{\partial^2 \ln C_o(n_c)}{\partial n^2}\right)\right]^{1/2}$$

Z is generally called the <u>Zeldovich Factor</u>.

Nucleation Product Phase Size Distribution



Of ten, observations on nucleation processes yield a product phase size distribution. However, the usual analysis of nucleation does not seem to treat this result in a clear manner. We expect that the size distribution is Gaussian in nature. To develop an analytical expression we can examine a spherical nucleus geometry as an illustration. The work to form a cluster of radius, r is given by at the critical size, $d\Delta G(r)/dr = 0$ and

$$\Delta G(r) = 4\pi r^2 \sigma + \frac{4}{3}\pi r^3 \Delta G_{v}$$

which yields

$$r^* = -2\sigma / \Delta G_v$$

$$\Delta G^* = \frac{16\pi\sigma^3}{3\Delta G_v^2}$$

Now, ΔG^* can be expressed in terms of r^{*} by substituting $\Delta G_v = -2\sigma/r^*$ so that

$$\Delta G^* = \frac{4\pi\sigma r^{*2}}{3}$$

Thus, the nucleation barrier is 1/3 of the surface energy of the cluster. Also, the concentration of clusters is given by

$$c(r^*) = c(1) \exp\left(\frac{-\Delta G^*}{kT}\right)$$

where c(1) is the concentration of monomers. If we examine cluster sizes near r^* (i.e. (r^*-r)) and expand $\Delta G(r)$ we obtain

$$G(r) = \Delta G(r^* - \Delta r) = \Delta G(r)_{r^*} + \left[\frac{d\Delta G(r)}{dr}\right]_{r^*} \Delta r + \left[\frac{d^2 \Delta G(r)}{dr^2}\right]_{r^*} \frac{\Delta r^2}{2}$$

Since $\left[\frac{d\Delta G(r)}{dr}\right]_{r^*} = 0$
$$\Delta G(r) = \frac{4\pi\sigma r^2}{3} + \left[\frac{d^2 \Delta G(r)}{dr^2}\right]_{r^*} \frac{\Delta r^2}{2}$$

We can also note that

$$\left[\frac{d^{2}\Delta G(r)}{dr^{2}}\right]_{r^{*}} = 8\pi\sigma + 8\pi r^{*}\Delta G_{v} = 8\pi\sigma + 8\pi r^{*} \left(-2\sigma/\Delta G_{v}\right) \Delta G_{v} = -8\pi\sigma$$

then,
$$\Delta G(r) = \frac{4\pi\sigma r^2}{3} - 8\pi\sigma \frac{\Delta r^2}{2}$$

so that
$$c(r) = c(r^*) \exp\left(\frac{4\pi\sigma\Delta r^2}{kT}\right)$$

The normal distribution is

$$P(x) = \frac{1}{s(2\pi)^{\frac{1}{2}}} \exp\left(-\frac{\left(x-\bar{x}\right)^2}{2s^2}\right)$$

which indicates that

$$s = \left(\frac{kT}{4\pi\sigma}\right)^{\frac{1}{2}}$$
 and that $\bar{x} = r^*$

Thus, the measured distribution parameters can be used to determine r^* and σ which in turn will give ΔG^* and J.

Nucleation Theorems

Most of the existing methods of analyzing nucleation behavior are linked to specific models. Nucleation theorems developed by Kashchiev offer a general model independent analysis to determine properties of the critical nucleus. Since the initial introduction, several variants have been developed

1st Nucleation Theorem



 Δn^* is the excess number of atoms of type i in the nucleus over that present in the same volume of the original phase

1st Nucleation Theorem (cont'd)



Application

 $J = A \exp(-W^* / kT)$ $W^* = -kT\ln J + kT\ln A$

$$-\Delta n^* = \frac{\partial W^*}{\partial \mu_{oi}} \Big|_{\mathrm{T}} = -\frac{\partial (k \mathrm{T} \ln J)}{\partial \mu_{oi}} + \frac{\partial (k \mathrm{T} \ln A)}{\partial \mu_{oi}}$$

Binary Systems

• Measure "critical supersaturation" (or constant J)

$$k \operatorname{T} d \ln J = \operatorname{O} = k \operatorname{T} d \ln A - dW^* \cong -dW^*$$
$$W^* = f(a_1, a_2)$$
$$\operatorname{O} = -dW^* = -\left(\frac{\partial W^*}{\partial \ln a_1}\right)_{\mathrm{T}} d \ln a_1 - \left(\frac{\partial W^*}{\partial \ln a_2}\right)_{\mathrm{T}} d \ln a_2$$

Binary Systems (cont'd)

 $k \operatorname{T} d \ln a_1 = d \mu_{o,1}$ and $k \operatorname{T} d \ln a_2 = d \mu_{o,2}$ $O = \Delta n_1^* d \ln a_1 + \Delta n_2^* d \ln a_2$

or

$$\left(\frac{\partial \ln a_2}{\partial \ln a_1}\right)_{\mathrm{T},J} = -\frac{\Delta n_1^*}{\Delta n_2^*}$$

2nd Nucleation Theorem

$$\left(\frac{\partial (W^*/T)}{\partial T}\right)_p = -\frac{1}{T^2} (\Delta E^* - h_0 \Delta n^*)$$

 ΔE^* is the energy change through creation of the critical cluster and h_0 is the enthalpy per atom in the parent phase.

$$\left(\frac{\partial \ln J}{\partial T}\right)_{P_0} = \left(\frac{\partial \ln A}{\partial T}\right)_{P_0} + \frac{1}{kT^2}\left(\Delta E^* - n^*L_f\right)$$

Delay Time and Steady State Nucleation

$$J = Z\beta C(n^{*}) \qquad \tau = (\theta\beta Z^{2})^{-1}$$
$$J\tau = C(n^{*})/\theta Z$$
$$Z = [\Delta G(n^{*})/(3\pi kT)n^{*2}]^{1/2}$$
$$Z = (1/8\pi v_{b})(\sigma/kT)^{-3/2}(\ln S)^{2}$$
$$\ln(J\tau) = \ln(N_{0}/\theta Z) - (16\pi\sigma^{3}v_{b}^{3}/3k^{3})/[T^{3}(\ln S^{2})]$$





Single Run, Multiple Droplets	Single Droplet, Multiple Runs
average behavior of large number of	direct observation of individual
independent nucleation events	nucleation event
convolute nucleation statistics /	convolute nucleation statistics / site
multiple sites	development
identical thermal history for all	identical droplet for all nucleation
droplets	events
traces average behavior	traces the most potent site in a
	particular droplet





$$\lambda_i$$
 = nucleation probability/unit time
 h_i = interval width
 d_i = # events/ h_i
 s_i = # unfrozen
 $J = \lambda/v$ (nucleation rate)









• Homogeneous Nucleation

Nucleation rate

$$\mathbf{J}_{v} = \mathbf{n}_{v} \operatorname{vexp}\left[\frac{-\Delta \mathbf{G}_{A}}{\mathbf{k}T}\right] \exp\left[\frac{-a\sigma_{sl}^{3}}{\Delta \mathbf{G}_{v}^{2}\mathbf{k}T}\right]$$

• Heterogeneous Nucleation

$$n_{v} \Longrightarrow n_{s}$$
$$a \Longrightarrow a f(\theta)$$

 $N_v = n_{v0} exp(\beta \Delta T)$









Undercooled behavior of Al-Si alloys. The triangle point represents the quenched eutectic signal.



Microstructure developed in eutectic Al-Si powders (A) cooled in the DTA, 20K/min [primary Si-dark faceted particle] and (B) quenched, 500 K/sec [primary Al dendrites].



Variety of Possible Scenarios

$$\begin{split} V_{s} &= 0.01 \text{ m/s}; \\ \tau &\cong n^{*2} / \beta \\ \tau &\cong 10^{-8} - 10^{-6} \text{ s (liquid)} \\ \tau &\cong 0.1 - 10 \text{ s (glass)} \end{split} \qquad \qquad V_{N} &= f(h, \lambda, , , ...) \\ \beta &\cong 10^{10} / \text{s (liquid)}; \beta \cong 10^{4} / \text{s (glass)} \\ n^{*}: 10 - 100 \\ r^{*} &= 0.1 - 100 \\ f(\theta) &= \frac{\Delta G_{het}^{*}}{\Delta G_{hom}^{*}} = \frac{V_{het}^{*}}{V_{hom}^{*}} = \frac{(l_{1} - \tau v_{s})l_{0}^{2}}{l_{0}^{3}} \end{split}$$



A. L. Greer, "Metallic Glasses", Science, 267 (1995) pp. 1947



Isotherm at 245°C 10 min






General Features of Nanocrystals

- NC's are pure Al
 - Al_{fcc} is NOT favored thermodynamically
 - Competing against the intermetallic phase
- Growth velocity limited by RE diffusion





A. Inoue, Progress in Mat. Sci., 43, (1998)





C. A. Angell, Science, 267, (1995) pp. 1924







Heterogeneous Catalysis

Precursor Liquid Phase Separation Site Density Thermodynamics Clustering By Linked Fluxes Site Density Homophase/Heterophase Catalysis Local Structure Solute Centered Solvent MRO **Impurity Cores**





Sheng, et al, Acta Mat. 56, 6264 (2008)



Spatially heterogeneous dynamics Simulation by Glotzer group (U. of Michigan)





MRO Character



Measured V(k) for melt-spun as spun and simulated V(k) for a 30 Å Al sphere and a Sm-centered icosahedra. The Al sphere reproduces the peak positions and relative heights. The simulations have been multiplicatively scaled to match the data.

Crystallization behavior of Al-Y-Fe-Cu

- Primary (Al_{fcc}) crystallization onset shift due to substitution of Cu for:
 - Fe: $\Delta T_{\rm X} = -50$ (1 at%)
 - Y: $\Delta T_{\rm X} = -45$ (1 at%)
 - Al: $\Delta T_X = +10$ (1 at%)
- Changes also occur in the intermetallic crystallization
 - While not as significant, show the strong composition dependence.



Nucleation product density

N_v=6.9×10²⁰ m⁻³

N_v=3×10²¹ m⁻³

N_v=1.1×10²² m⁻³



MRO Changes with composition

- Number Density $-N_{m,no} = 1.2 \times 10^{27} \text{ m}^{-3} {}^{2} \text{$
- Average Size = .755 nm
- Volume Fraction
 - $-\Phi_{m,no} = 25\%$ $-\Phi_{m,Cu} = 41\%$

FEM data for $Al_{88}Y_7Fe_5$ and $Al_{88}Y_7Fe_4Cu_1$ at 1.6 nm spatial resolution. The peak positions occur at the Aluminum 200 and 220 reflections. The lower peaks in $Al_{88}Y_7Fe_4Cu_1$ indicate a more spatially homogeneous structure at a length scale of 1.6 nm.



Post-anneal Microstructure

- High density of nanocrystals
 N_{no} = 2.94*10²¹ #/m³ (9min)
 - $N_{Cu} = 1.09*10^{22} \#/m^3 (2min)$
 - $d_{no} = 31nm$ $d_{Cu} = 21nm$
 - Roughly equal final Al_{nc,fcc} volume fraction
 - $\Phi_{m,no} = 4.6 \%$ $\Phi_{m,Cu} = 5.2 \%$
 - To put these numbers in perspective, for each crystal that grows, 2 to 4*10⁵ MRO are annihilated.



Cluster Concentration

iv

• In an undercooled liquid the equilibrium cluster size concentration is

 $C(n)=C_1exp(-\Delta G_n/kT)$

 It is highly improbable that the MRO concentrations would be retained C(n) from the quench. Monomer concentration

MRO concentration

MRO Interpretation

- Within an undercooled liquid there are energetically preferred configurations of Al MRO regions.
- The MRO regions persist and evolve by a classical thermal fluctuation mechanism.
- The MRO is disordered/defective Al that acts as a seed for NC



Energetic Treatment of MRO



Seeded Nucleation Cont.

$$\Delta G(r) = 4\pi \sigma_{x/g} (r^2 - r_0^2) + \frac{4\pi}{3} (r^3 - r_0^3) \Delta G_v$$
$$r^* = \frac{-2\sigma_{x/g}}{\Delta G_v} = \frac{-2(0.0104 + 8 \times 10^{-5} T)}{-1.087 \times 10^9 + 1.29 \times 10^6 T}$$
$$r^* = \frac{0.296}{3.736 \times 10^8} = 0.79 \text{ nm at } 553 \text{ K}$$

For $d_0 = 0.74$ nm and $r_0 = 0.37$ nm

$$\Delta G^{*} = 4\pi \sigma_{x/g} (0.487) + \frac{4\pi}{3} (0.49 - 0.05)$$
$$\Delta G^{*} = 0.217 * 10^{-18} \text{ J}$$
$$k_{B}T = 1.38 * 10^{-23} * 553 = 7.63 * 10^{-21}$$
$$\frac{\Delta G^{*}}{(k_{B}T)} = 28.4 \text{ (reasonable)}$$

Steady State Model

Volume Dependent Heterogeneous Nucleation

$$J_{SS} = \rho\beta Z \exp\left(-\frac{\Delta G^*}{k_B T}\right)$$

$$\rho = \text{MRO number densty}$$

$$\beta = 4\pi r^{*2} DC_0 a^{-4} = \text{Attachment Frequency}$$

$$Z = \frac{\Delta G_V^2 v_a}{8\pi \sqrt{k_B T \sigma^3}} = \text{Zeldovich factor}$$

$$J_{SS} = \frac{\rho 4\pi r^{*2} DC_0 \Delta G_v^2 v_a}{8a^4 \pi \sqrt{k_B T \sigma^3}} \exp\left(-\frac{\Delta G^*}{k_B T}\right)$$

Temperature (K)

Transient Nucleation

- Changes in MRO number density do not account for nucleation enhancement
- The base model can now be used to analyze number densities observed at different temperatures

$$J_t = J_{SS} \exp\left(-\frac{\tau}{t}\right)$$

Solving for
$$\tau$$
,
 $\tau = \frac{1}{\beta Z^2} = \frac{8k_B T \sigma a^4}{D\Delta G_v^2 C_0 v_a^2}$



Time (s)

Transient Nucleation

Transient time constant evaluated for AlYFe.

$$J_T = J_{SS} \exp(-\frac{\tau}{t})$$





Growth Modeling

- Rapid size increase due to interfacial growth mechanism
- Diffusion controlled growth of larger particles
- Growth inhibited by diffusion field impingement.
- Interfacial instability leads to dendritic type growth



Current status of combined model

- Crystallization start temperatures can be reproduced over a range of compositions and heating rates.
- Poor fitting during the later stages of the reaction is attributed to the complicated growth.
- Improved growth/transport analysis will also aid the interpretation of nucleation

0.0 -

Nucleation Product Density Calculation

Extended Volume Fraction: $X_e = \int_0^t J_s \frac{4\pi}{3} [v(t-\tau)]^3 dt = \frac{4\pi J v^3}{3} \int_0^t t^3 dt$

$$X_e = \frac{\pi}{3} J v^3 t^4$$

Now, X, the real volume fraction transformed is: $X=1-\exp(-X_{o})$

For X = 0.99; $X_e \sim 5$

The number density, ρ , of nanocrystals is given by

$$\rho = \int_{0}^{t} J(1 - X(t)) dt = J \int_{0}^{t} \exp(-X_{e}) dt$$

to find the maimum in ρ we let $t \rightarrow \infty$

$$\rho_m = J \int_0^\infty \exp\left(\frac{-\pi}{3} J v^3 t^4\right) dt = J \int_0^\infty \exp\left(-k t^4\right) dt$$
$$k = \frac{\pi}{3} J v^3$$

Product Density Continued

Where: $\int \exp(-y) y^{-3/4} dy$ is the Γ function $\Gamma(n) = \int_{0}^{\infty} e^{-y} y^{n-1} dy \qquad \text{So},$ n-1=-3/4 ; n=1/4 $\Gamma(1/4) = \Gamma \frac{(1.25)}{0.25} = \frac{0.9064}{0.25} = 3.63$ $\rho = \frac{3.63 J}{4 k^{1/4}} = 0.897 \left(\frac{J}{v}\right)^{3/4}$ For $\rho = 2.9 * 10^{21}$ $\frac{J}{2} = 4.7 \times 10^{28}$ For $J = 10^{18}$ and $v_a = 10^{-10}$ (m/s) Now, for 1 hr, d = 21 nm $\frac{r}{t} = \frac{10 \text{ nm}}{3600 \text{ s}} = 2.7 \times 10^{-3} \text{ nm/s} = 2.7 \times 10^{-12} \text{ m/s}$ For $v = 2.7 * 10^{-12}$ m/s $J \rightarrow 1.2 * 10^{17} \text{ m}^{-3}$

Transport Question

- The magnitude of change in the transient behavior is very large (>10²⁾ for a single atomic percent substitution. This is puzzling if it is dependent upon the simple change in diffusion.
- How do we consider cluster development by atomic addition in this partially ordered environment with different time constants?





Intermediate Phase Nucleation During Interdiffusion

- •Initial Phase Establishes Phase Sequence
- •Role of C Precursor Stage i.e. r^{*} $\propto \Delta C / C$
- $\bullet Influence of \Delta D$
- $\bullet \Delta J \propto \Delta D {\small \textcircled{b}} C$
- •Growth Kinetic Competition
- Multicomponent Pathways



Position







Composition

(a)

Т

Compositio n



(b)

Composition



Table-I: Summary of the nature of the first phase formed

<c></c>	Al ₈₂ Ni ₁₈	Al ₇₅ Ni ₂₅	Al ₅₀ Ni ₅₀
Λ			
Short	Al ₃ Ni	Al ₃ Ni	AlNi
(10-14.4 nm)			
Intermediate	Al ₉ Ni ₂	Al ₉ Ni ₂	Al ₉ Ni ₂
(22.2-100 nm)			
Large			Al ₉ Ni ₂
(400 nm)			

XTEM of Al/Ni multilayer at point (a) of DSC trace without phase formation.

•Initial phase formation requires minimum volume with phase compositional range

•Interdiffusion is required to develop dc/dx for the critical volume

•Gradient can be modified by layer thickness which in turn can control phase selection and sequencing





(b) Open system processing
Effective Temperature



Amorphization Mechanism (Al₆₀Dy₂₀Ni₂₀)





Al-Sm Metallic Glass formed by Different Processes Cold-rolled sample: After annealed at 150°C, 60min:





Summary

Nanostructure Synthesis During Devitrification and Deformation of Al Glass Strong Composition Dependence

Strong Composition Dependence

- - T_x , T_g Relatively Stable: Tx> 250°C [Al-RE-TM]
- Phase Selection
- Solute Substitution Effects

Structural Heterogeneity----

-MRO (Processing and Solute Sensitivity)

Kinetics -Heterogeneous; Transient Nucleation

In AlYFe low level substitution of Cu for Fe results in:

- Increase in the MRO number density
- Transient nucleation time constant decrease
- Low level substitution of Cu for Al may promote BMG

Open Issues: Nucleation and Atomic Transport in Spatially Heterogeneous

Glass

Deformation Induced reactions

Deformation driven mixing provides a distinct kinetic pathway unavailable through thermal treatment. Alloying develops in stages through layer refinement and interface roughening with enhanced atomic exchange.

New Pathways for Nanostructure /BMG Synthesis

We Have Met the Enemy and He Is PowerPoint



A PowerPoint diagram meant to portray the complexity of American strategy in Afghanistan certainly succeeded in that aim. (NY Times, April 26, 2010)

Al88Y7Fe5 Annealed at 235C/508K



Al88Y7Fe4.5Cu0.5 Annealed at 205C/478K



Nucleation and Growth Model

- Measured

 nanocrystal and
 MRO densities and
 sizes act as the direct
 input to develop the
 model
- Analysis results are tested to reproduce the measured data





Volume per transformation zone: $10^{-28}m^3$ Heat per t. zone: $10^{-20}J$ With 10^{26} transformation zones per m³Heat released: $10^{6}J/m^3$

MRO and FEM mode

- •Medium range order in $AI_{88}Y_7Fe_5$ and with Cu substitution refers to Al crystal-like structure (0.6 to 2 nm in *d*)
- In nanodiffraction FEM mode, we can control the resolution by controlling the probe size
 Advantages in nanodiffraction mode:
- 1. Enhanced coherence
- 2. Resolution can vary continuously
- 3. High k range



Nucleation in Magnetic Nanomaterials

R.V. Ramanujan School of Materials Science and Engineering Nanyang Technological University Singapore Team: H.F. Li, S.W. Du, Y. Zhang

Soft Magnetic Nanomaterials

- Applications
 - Energy devices
 - Generators
 - Transformers
 - Motors
 - Electromagnetic shielding
 - Data Storage
 - Biomedical devices
 - Surveillance tags
- ↑ energy efficiency by making softer magnetic materials
- Solution: Go Nano!

What do we want?

- Many amorphous magnetic materials are very soft
- High density of soft magnetic nanocrystals in a soft magnetic amorphous matrix → magnetically softer!
- High nucleation rate of crystals + low growth rate
- Herzer Model: Nano ppts: H_c ~ (crystal size)⁶
- Crystallize amorphous magnetic material by heat treatment



Challenge

- Can a microstructure of high density of soft magnetic precipitates in a soft magnetic amorphous matrix be magnetically softer than the famous
 - Permalloy (Fe-Ni)
 - Fe-Co for high temp. aircraft applications
 - Fe-Si-B (transformer steel)

YES!

- Which elements will increase nucleation rate and reduce growth rate of precipitates?
- Commercial nanocrystalline magnetic alloys
 - Fe_{73.5}Si_{13.5}Nb₃B₉Cu₁ (FINEMET)
 - Fe₈₈Zr₇B₄Cu₁ (NANOPERM)
 - Fe₄₄Co₄₄Zr₇B₄Cu₁ (HITPERM)

Application of nucleation and growth concepts to produce soft magnetic nanostructures

- Fe-Ni-B-Mo
- Fe-Co-B-Zr
- Fe-Si-B-Nb-Cu

Nucleation in Permaloy based Fe-Ni-B-Mo magnetic nanomaterials

Objective

• Fe-Ni-B-Mo

 To understand role of Mo and B in producing high nucleation rate and low growth rate

J. Alloys Compounds, 425, 251-260 (2006) J. Non-Crystalline Solids, 351, 3105-3113 (2005)

Initially amorphous Fe₄₀Ni₃₈B₁₈Mo₄ crystallized by heat treatment



HEAT TREATED AT 400°C FOR 1 H.

Formation of Fe-Ni nano precipitates

Size distribution of crystals



Size distribution of alloy heat treated 350 °C Precipitate size almost constant with heat treatment time

Johnson-Mehl-Avrami Plot

- Johnson-Mehl-Avrami
- y=1-exp(-Ktⁿ)
 Avrami exponent
 - *n*=0.39
 - Usual value 1-4
- Counterpart alloys
 - Fe₄₀Ni₄₀B₂₀: 3
 - Fe₄₀Ni₄₀P₁₄B₆: 4



LOW VALUE OF AVRAMI EXPONENT N

Effect of boron on nucleation



Crystal Amorphous Crystal

SCHEMATIC PROFILE OF B AND MO CONCENTRATION IN THE AMORPHOUS MATRIX

FREE ENERGY FOR THE AMORPHOUS PHASE AND THE CRYSTALLINE PHASE

BORON DECREASES THE NUCLEATION RATE

Model of effect of Mo on growth

- Hillert's theory on normal grain growth $\frac{dR}{dt} = \frac{A}{R} \Longrightarrow R^{2}(t) - R^{2}(0) = 2At$
- Michels' Model

$$\frac{dR}{dt} = \frac{A}{R} - f(R)$$

• Boundary condition

$$\frac{dR}{dt} = 0, R \to R_{\max}$$

Concentration of Molybdenum



MOLYBDENUM PILE UP AT THE CRYSTAL:AMORPHOUS INTERFACE

$$R(t) = \{R_{\max}^2 - (R_{\max}^2 - R^2(0)) \exp[-2At / R_{\max}^2]\}^{1/2}$$

Crystal size and effect of Mo



GOOD AGREEMENT OF THE EXPERIMENTAL RESULT AND

Magnetic Properties



IMPROVED MAGNETIC PROPERTIES WAS ACHIEVED AT

Application of nucleation and growth concepts to produce soft magnetic nanostructures

- Fe-Ni-B-Mo
- Fe-Co-B-Zr
- Fe-Si-B-Nb-Cu

Nanocrystallization of HiTperm Co_{44.5}Fe_{44.5}Zr₇B₄

IEEE Trans. Nanotechnology, 6, 177-185 (2007)

IEEE Trans. Nanotechnology, 5, 295-300 (2006)

Nanocrystallization of initially amorphous HiTperm Co_{44.5}Fe_{44.5}Zr₇B₄



High nucleation rate, low growth rate

Application of nucleation and growth concepts to produce soft magnetic nanostructures

- Fe-Ni-B-Mo
- Fe-Co-B-Zr
- Fe-Si-B-Nb-Cu

Finemet type alloys

• Fe-Si-B-Cu-Nb alloys (transformer steel based)

 Excellent magnetic properties with combined Cu & Nb alloying additions in Fe-Si-B alloy due to nanostructure formation

- Conventional (incorrect) view:
 - Role of Cu is to \uparrow nucleation
 - role of Nb is to \downarrow growth.

Objective

 What is the role of Cu and Nb alloying additions in nanostructure formation in Fe-Si-B-Cu-Nb alloys?

Methodology

 Effects of alloying additions: 1 at% Cu and 3 at% Nb in amorphous Fe-Si-B-Cu-Nb alloy.

Morphology after primary crystallization

Fe-Si-B







Fe-Si-B-Cu



Fe-Si-B-Cu-Nb

 $(1)Fe_{77.5}Si_{13.5}B_{9}$

Fe-

Nb

Si-B-

Large microstructure difference due to alloying addition

Fe-Si-B alloy

Equiaxed to dendrite morphological transition in Fe-Si-B $_{\mbox{Appl. Phys. Lett., 88, 182506, 2006}}$



0s

6s

<u> 12</u>s




 Dendrites of closely spaced Fe-Si crystals, spacing ~ nanometers.

 In-situ hot stage TEM: equiaxed → dendritic morphological transition at critical size of ~ 45 nm.
 Explained by morphological stability theories.

Effect of Cu addition

In-situ hot stage TEM of Fe-Si-B-Cu



• 450°C for 600s

Unstable interface of spheroidal crystal when crystal size > than 100nm.

Effect of Cu alloying addition



Free energy G-curve for amorphous matrix and crystallization product

Fe-Si-B-Cu

- Cu addition influenced **both** nucleation and growth
 - spheroidal crystals ~ 100 nm, rough interfaces .

- Crystal density \uparrow , crystal size \downarrow . However, crystal density << than in Fe-Si-B-Nb-Cu.
- Driving force for nucleation ↑.

Effect of Nb addition

Eutectic crystallization of Fe-Si-B-Nb alloy



TEM micrographs of the alloy with Nb, after heat treatment at 550 °C for (1)0.5 h and (2)24 h

Equiaxed

Effect of Nb addition



Free energy G-curve for amorphous matrix and crystallization product

<u>Fe-Si-B-Nb</u>

- Eutectic crystallization:Fe-Si, Fe₃B and Fe₂₃B₆
- Greater \uparrow in crystal density, \downarrow of crystal size compared to Cu addition.
- But, cannot obtain high crystal density and small crystal size of Fe-Si-B-Nb-Cu.
- Hence, synergetic effects of combined Cu and Nb additions key to nanostructure formation

Effect of both Cu and Nb additions

Cu and Nb EELS map at initial stage of crystallization



(a) (b) (c)

(a) BF TEM micrograph of Fe-Si-B-Nb-Cu alloy after heat treatment at 500 °C for 10 min (b) EELS map of Cu (c) EELS map of Nb

Cu AND Nb rich regions

Quantitative analysis of crystallization



Maximum crystal size as function of annealing time: (1)Fe-Si-B (2)Fe-Si-B-Cu (3)Fe-Si-B-Nb (4)Fe-Si-B-Nb-Cu alloy at 500 °C



The number of crystal per unit volume as function of annealing time: (1) Fe-Si-B -Nb-Cu (2) Fe-Si-B-Nb (3) Fe-Si-B-Cu (4) Fe-Si-B alloy at 500 °C

Johnson-Mehl-Avrami-Kolmogorov Plot



Conclusions

 Alloying with Cu, Nb had dramatic effects on nanostructure formation in iron-based soft magnetic materials

• Studied by DSC, XRD, EDX, EELS, conventional & in-situ hot stage TEM.

Fe-Si-B-Nb-Cu

Novel mechanism of nanostructure formation (synergetic effects of combined Cu and Nb)

- Contrary to most models, we find that **both** Nb and Cu influence nucleation and growth processes.
- Combined additions → small crystal size and high crystal density.
- High nucleation rate → both Cu and Nb rich regions → high number of heterogeneous nucleation sites.
- Low growth rate due to strong interaction of Cu, Si, Nb and B atoms, consistent with Hunziker model.

Summary

- A high density of soft magnetic nanoprecipitates in an amorphous matrix yield superior soft magnetic properties
- Nucleation and growth concepts have been used to produce novel soft magnetic nanostructures in iron and Co based soft magnetic materials

Related Publications-1

- H.F. Li and R.V. Ramanujan, Coarsening of the nanolamellar structure in a soft magnetic alloy, *IEEE Trans. Nanotechnology*, 6, 177-185 (2007).
- R.V. Ramanujan and Y. Zhang, Quantitative transmission electron microscopy analysis of the nanocrystallization kinetics of soft magnetic alloys, *Phys. Rev. B.*, 74, 224408-1 to 224408-7 (2006). *This paper was selected by American Inst. of Physics and American Phys. Soc. for J. of Nanoscale Sci. Tech., Dec. 26, 2006*.
- R.V. Ramanujan and S.W. Du, Nanocrystalline structures obtained by the crystallization of an amorphous Fe40Ni38B18Mo4 soft magnetic alloy, *J. Alloys Compounds*, 425, 251-260 (2006).
- H.F. Li and R.V. Ramanujan, Nanolamellar structure obtained by simple crystallization of an amorphous cobalt based magnetic alloy, *IEEE Trans. Nanotechnology*, 5, 295-300 (2006). *XRD data from this paper has been incorporated in the Powder Diffraction file of the International Centre for Diffraction Data (USA).*
- Y. Zhang and R.V. Ramanujan, The effect of copper alloying additions on the crystallization of an amorphous Fe-Si-B alloy, *J. Mater. Sci.*, 41, 5292-5301 (2006).
- H.F. Li and R.V. Ramanujan, In situ hot stage transmission electron microscopy observations of nanocrystal formation in a Co65Si15B14Fe4Ni2 amorphous magnetic alloy, *Thin Solid Films*, 514, 316-322 (2006).
- R.V. Ramanujan and Y. Zhang, Solid state dendrite formation in an amorphous magnetic Fe77.5Si13.5B9 alloy observed by in-situ hot stage transmission electron microscopy, *Appl. Phys. Lett.*, 88, 182506 (2006).
- H.F. Li, D.E. Laughlin and R.V. Ramanujan, Nanocrystallization of an Fe44.5Co44.5Zr7B4 amorphous magnetic alloy, *Phil. Mag.*, 86, 1355-1372 (2006).
- H.F. Li and R.V. Ramanujan, <u>Crystallization behavior of the cobalt based metallic glass Co65Si15B14Fe4Ni2</u>, *Mater. Sci. Engg. A*, 375-377, 1087-1091 (2004).

Related Publications-2

- Y. Zhang and R.V. Ramanujan, Microstructural observation of the crystallization of amorphous Fe-Si-B based magnetic alloys, *Thin Solid Films*, 505, 97-102 (2006).
- Y. R. Zhang and R.V. Ramanujan, Characterization of the effect of alloying additions on the crystallization of an amorphous magnetic Fe73.5Si13.5 B9Nb3Cu1 alloy, *Intermetallics*, 14, 710-714 (2006).
- Y. Zhang and R.V. Ramanujan, A study of the crystallization behavior of an amorphous Fe77.5Si13.5B9 alloy, *Mater. Sci. Engg.*, A416, 161-168 (2006).
- S.W. Du and R.V. Ramanujan, Crystallization and Magnetic Properties of Fe40Ni38B18Mo4 Amorphous Alloy, *J. Non-Crystalline Solids*, 351, 3105-3113 (2005).
- Y. Zhang and R.V. Ramanujan, The effect of niobium alloying additions on the crystallization of a Fe-Si-B-Nb alloy, *J. Alloys Compounds*, 403, 197-205 (2005).
- H.F. Li and R.V. Ramanujan, In-situ TEM observations of the coarsening of a nanolamellar structure in a cobalt based magnetic alloy, *J. Mater. Sci.*, 40, 1901-1907 (2005).
- S.W. Du and R.V. Ramanujan, <u>Mechanical alloying of Fe-Ni based nanostructured magnetic materials</u>, *J. Magn. Magn. Mater.*, 292, 286-298 (2005).
- H.F. Li and R.V. Ramanujan, Mechanical alloying of FeCo nanocrystalline magnetic powders, *J. Electronic Mater.*, 33, 1289-1297 (2004). *Special Issue*.
- H. F. Li and R.V. Ramanujan, <u>Microstructural evolution during crystallization of a Co65Si15B14Fe4Ni2</u> <u>magnetic material</u>, *Intermetallics*, 12, 803-807 (2004).
- S.W. Du and R.V. Ramanujan, <u>Characterization of Fe40Ni38B18Mo4 nanomagnetic alloy</u>, *Mater. Sci. Engg.* A., 375-377, 1040-1043 (2004).

Thank You !

Thermodynamic Modeling of the Early Stages of Solid State Precipitation in Alloy Sysems

S.Rangnathan National Metallurgical Laboratory Jamshedpur 831 007, INIA

AFRL-AOARD-LLNL WORKSHOP ON NUCLEATION, May 2010

Nucleation

Not always an equilibrium process Nucleus – different from equbm. Phase can transform to non-equbm. phase true of composition interface composition – crucial Modelling the non-equilibrium process

Non-Equilibrium Process

any phase transformations do not reach equilibrium checked by kinetics mass transfer heat transfer chemical reaction Non-equilibrium state compositional (eq. Super-saturated solutions) (eq. Amorphous solids) structural morphological

Modelling - Equilibrium Phenomenon

Equilibrium State Unique Well-defined Easy to target and predict

Equilibrium State



Non-Equilibrium Transformation

Consider a system A-B Phases α , β

Equilibrium Processes Free Energy-Composition Diagram



Free Energy–Composition Diagram Invariant Composition Phases



Criterion for Non-Equilibrium Process

Consider system Possible phases Chemical potentials For transformation A-B (constituents) α,β $\mu_{A}{}^{a}, \mu_{A}{}^{\beta}, \mu_{A}{}^{a}, \mu_{A}{}^{\beta}$

$$\alpha \rightarrow \beta$$

$$\Delta G^{\alpha\beta} = X_A^{\alpha} \Delta \mu_A + X_B^{\alpha} \Delta \mu_B$$

$$\Delta \mu_i = \mu_i^{\alpha} - \mu_i^{\beta}$$

 $\Delta G^{\alpha\beta} < 0$ for process to occur Non-equilibrium process α,β can be solution phases or compounds Relevant for material synthesis





Free Energy Change = (G_B-G_A) Non - equilibrium process - nucleation $\Delta G < 0$ States A and B can be aqueous solution and compound Calphad, 2002



Transformation Diagram



The Bi-directional Transformation Diagram

 $\begin{array}{ll} \alpha & \rightarrow \beta & \text{possible at } X^{\beta}_{X} \\ X^{\alpha}_{X} \rightarrow X^{\beta}_{X} \\ \text{Will } \beta \text{ at } X^{\beta}_{B} \text{ transform to } \alpha \text{ ?} \\ \text{In other words, will } \beta \\ & \text{go back into solution?} \end{array}$



Will the nucleus Redissolve?





Loci for $\alpha \rightarrow \beta$ and $\beta \rightarrow \alpha$ transformation

Example : Transformation - closer in composition Possible at short time intervals May not be the equilibrium state



XL

Interfacial Composition

Solid solution-nucleus interface composition different from bulk plays a crucial role growth rate controlled by thermodynamics surface area mass transfer kinetics Predict – use transformation diagrams


Wt.% C

Usually explained

On the basis of phase diagram

Meta-stable extension of $(\gamma + L)$ field

Again, an equilibrium assumed (meta-stable) However, this approach does not explain why this route is preferred

Transformation Diagram Solidification of Steel



Region B: smaller fluctuations in composition required for $L \rightarrow \gamma$; $L > \delta$ not feasible in this region Larger fluctuations required for $L > \delta$ equilibrim Hence $L \rightarrow \gamma$ transformations occurs

Transformation Diagram Invariant-Composition Phase Invariant composition phase any chemical compound Fixed composition no solution phase Fe_3C , Cr_7C_3 Composition axes cannot be used Axis transformed chemical potential







Ti-Cr

Transformation at 873 K (α/β)





Ti-Cr

Transformation at 873 K (α/β)



0

Ti-Cr

Transformation at 873 K (α/β)





Summary

Nucleant – free energy criterion Can transform to alternative phases Trace the non-equilibrium – Transformation Diagrams



Thank You

Lawrence Livermore National Laboratory

Grain Boundary Engineered Materials as Correlated Networks: Large-Scale Implications of Twin Nucleation May 3, 2010



B. W. Reed, M. Tang, J. F. Belak, J. V. Bernier, V. V. Bulatov, T. LaGrange, and M. Kumar

Lawrence Livermore National Laboratory, P. O. Box 808, Livermore, CA 94551

This work performed under the auspices of the U.S. Department of Energy by Lawrence Livermore National Laboratory under Contract DE-AC52-07NA27344 and supported by the Office of Science, Office of Basic Energy Sciences, Division of Materials Sciences and Engineering, of the U.S. Department of Energy by SISGR Grant

This is a multi-institutional collaboration

(Institutions listed at the time of most active collaboration)

MSU: Phil Duxbury, Erin McGarrity **University of Michigan: Gary Was** GE Global Research Center: Peter Andresen, Martin Morra University of California–Berkeley: Robert Ritchie University of California–Davis: N. Sukumar, A. Tabarraei Washington State University: David Field Lehigh University: David Williams University of Minnesota: Barry Carter LANL: Mark Cola, Vivek Davé **MIT: Chris Schuh, Megan Frary** RWTH (Germany): Myrjam Winning **CMU: Tony Rollett** LLNL: Kerri Blobaum, Wayne King, Roger Minich, Robert Rudd, Adam Schwartz, Eira Seppälä, James Stölken, Ken King, Bob Etien

What is grain boundary engineering?

- Simple processing can enhance resistance to intergranular failure/degradation by 3X-5X or more
- Based on using "special" grain boundaries (e.g. coherent twin) to break up the network of weaker "random" grain boundaries
- Works on many different failure modes
 - Stress corrosion cracking
 - Impurity embrittlement
 - Microstructural coarsening
 - Magnetic flux penetration in superconductors

Key concept: Context matters! The grain boundary *network* is essential.

Consider two grain boundary networks.

Suppose red boundaries are strong, blue boundaries are weak.





Focus of this talk: What does nucleation and growth of twins do on the scale of the grain boundary network?

Given the characteristics of the nucleation and growth, ...

- Crystallography
- Anisotropy and texturing
- Combinatorics governed by crystallographic constraints
- Dominant morphologies

... what does this do to the network properties?

- Special/random percolation thresholds
- Correlation lengths and supra-grain structure
- Large-scale resistance to intergranular degradation



For many metals, the dominant special boundary is the Σ 3 {111} twin

- Low stacking fault energy fcc materials (e.g. Cu, Ni)
- Two mirror-image grains sharing a {111} plane
- Twins form as deformed material anneals
- Twin boundaries tend to be large, flat, smooth, and stable
- When Σ 3's meet, they can generate Σ 9's, Σ 27's, etc.
- Σ3ⁿ "twin-related" grain boundaries dominate the statistics



Non-Σ3ⁿ CSL

Σ3

Σ9

Σ27





LLNL-PRES-430016

Definition: CSL = Coincident Site Lattice

Σ1

70

60

50

40

30

20

10

0

Number Frequency (%)

6

All

Special

Cyclic thermomechanical processing enhances the populations of twin-related boundaries



LLNL-PRES-430016

There are two often-cited mechanisms for nucleating annealing twins in fcc materials

Growth accidents

- One layer of hcp within fcc (ABCBA stacking)
- Possible mechanism: Shockley partials forming on moving, faceted boundaries
- Often makes simple morphologies ("back-and-forth" twinning)

Recrystallization

- Driven by plastically stored energy
- Nucleation frequently at existing boundaries or triple junctions
- More isotropic; which variant you gets depends on unknown local factors





Recrystallization produces twins that have far more interesting effects on the boundary network

- Nucleate at boundaries (or junctions)
- Nucleation can be far more isotropic than for growth accidents
 - This facilitates cross-twinning, including creation of Σ 9, Σ 27, etc.
- Fueled by dislocation energy, leaving behind well-annealed crystal
- Σ3 boundaries include both coherent and incoherent segments
 - Complex morphology facilitates more complex network
 - Mobile incoherent segments can move into neighboring grains



TEM image of annealing twins in steel, from A. R. Jones, J. Mat Sci 16, 1374 (1981)

Lawrence Livermore National Laboratory



The grains develop into clusters that we call Twin-Related Domains (TRD)



An initial grain grows and forms multiple twins, making an extended complex structure with hundreds of grains

Lawrence Livermore National Laboratory

LLNL-PRES-430016



When the domains are well developed, we pass through a percolation threshold.



Lawrence Livermore National Laboratory

LLNL-PRES-430016

The surfaces created by intergranular cracking look completely different in normal and engineered materials



Normal Material

 Anisotropic ridges parallel to crack propagation over wide range of length scales

Engineered Material

Isotropic, uniform, more randomly rough (like a random walk)



Conventional representations of grain orientations don't handle multiple twinning well.

- There are specific mechanisms that produce, for a given grain, one of four variant twin orientations
- These are high-angle grain boundaries (60° <111>) that aren't going to be found in a local fluctuation
- The new misorientation is very nearly perfect, usually within 1°

You want to have a representation that explicitly includes these exact, discrete possibilities; nucleating "by chance" in quaternion space will waste a lot of CPU cycles.

Real microstructures can have twin chains 10 or 11 units long! This needs *a lot* of orientations to be in the ensemble.

Importance of misorientation relationships: To stop a random boundary path in two dimensions, you need a "J₂" triple junction



14

The Σ combination rule governs Coincident Site Lattice combinations allowed at a triple junction



Lawrence Livermore National Laboratory	Miyazawa et al (1996). <i>Acta Cryst.</i> A52, 787.		
	Cortomon V/V (2001) Acts Cruct AET 260		
LLNL-PRES-430016	Gensman, v. f. (2001). Acta Cryst. Asr, 309.		



The Σ combination rule alone significantly alters the statistical properties of the network.

(From Minich, Schuh, and Kumar, Phys. Rev. B 66, 052101 (2002) and Schuh, Minich, and Kumar, Phil. Mag. 83, 711 (2003).)



LLNL-PRES-430016

The Σ combination rule can be generalized by working out the structure of the entire group.

Vertex = grain orientation

Link = one of the four Σ 3 twinning operations (a,b,c,d)

Each vertex has exactly 4 neighbors

There are no loops

Tree is infinite and highly symmetric

Reed, Minich, Rudd, Kumar, Acta Crystallographica A (2004)

Lawrence Livermore National Laboratory



There is potentially an infinite number of constraints on the network.





It's possible to efficiently account for the constraints in a model developed for highly-twinned materials.

- Treat everything as a perfect Σ3ⁿ orientation
- Use string representation with 4-letter alphabet
- Define energy metric:

Σ	Comment	Typical Energy
1	No boundary at all	-1 (grain growth) or ∞ (static topology)
3	Perfect twin	-0.9 (Cu) to -0.3 (Al)
9	Twin variant	-0.5 to -0.2
27	2nd twin variant	-0.3 to -0.1
81+	Random	0

- Pick a topology (2-D or 3-D, random or ordered)
- Assign initial orientation strings to each grain
- Pick a temperature 1/β and run a Metropolis Monte Carlo calculation

The Potts-like Monte Carlo simulations yield statistically realistic microstructures with very few free parameters

Potts-like model including grain growth and twinning, efficiently calculated using $\Sigma 3^n$ strings, and guaranteed to satisfy all constraints



- Designed to mimic topology of a specific engineered Cu sample
- 5 free parameters
- <10 CPU-seconds to generate

	Experimental		Model (Average of	
	(EBSD)		10 runs)	
	Number	Length	Number	Length
	Fraction	Fraction	Fraction	Fraction
Σ3	27.3	44.1	27.1	43.7
Σ9	10.7	6.9	10.0	7.3
$\Sigma 27$	3.9	2.9	3.5	2.6
Other Σ	6.2	4.9	6.5	5.0
Random	51.8	41.2	52.9	41.3
J_0	14.4		13.6	
J_1	51.1		51.6	
J_2	14.3		14.4	
J_3	20.2		20.4	

- Designed to match detailed statistics of a specific engineered Cu sample
- ~10 CPU-hours to optimize over 5parameter space
- All metrics match within uncertainty



Work in progress: Combine the twin nucleation algebra with phase field modeling

- Monte Carlo run rapidly produces statistically realistic initial structure and a useable ensemble of grain orientations
- Phase field evolves this using a grain boundary energy and mobility metric
 - Multi-variable phase-field model for grain growth distinguishes among random boundaries, special boundaries and vicinal boundaries.
 - Assign GB energies and mobilities that depend on misorientation and will include grain boundary plane dependence in near future
 - Track evolution of grain size, GB character distribution, and network connectivity in phase-field simulations
- Progress towards efficient simulation of crystallographically realistic multiple-twinning model including nucleation of new twin grains



Adjusting the energy is not enough—low special boundary mobility is important for realistic stabilization of the network



Grain boundary plane anisotropy is necessary to get the model to nucleate while remaining stable



Lawrence Livermore National Laboratory

LLNL-PRES-430016

Multiply-twinned nanoparticles offer clues for making a finite orientation ensemble for the phase field model

- Many fcc nanoparticles (< 10 nm) form icosahedral multi-twinned structures
- 20 grains, 10 grain orientations, 30 twin boundaries, 12 twin pentajunctions
- Each grain exposes low-energy {111} faces to the outside world and to its neighbors
- Each link in the graph is a 72° <110> rotation, a good approximation to the 70.5° <110> Σ3
- Downsides:
 - Each grain is rhombohedrally distorted
 - Each orientation only has 3 neighbors in the network instead of 4
 - Pentajunctions are far too easy to form

X. Yang et. al, J. Phys. Chem. A. 111 (2007) 5048
C. Y. Yang, J. Crystal Growth 47, 274 (1979)
D. Reinhard et al., Phys. Rev. B 55, 7868 (1997)
K. J. Koski et al., Phys. Rev. B 78, 165410 (2008)

Lawrence Livermore National Laboratory

LLNL-PRES-430016





Summary and Future Directions

- Grain boundary engineered materials have complex network properties that depend heavily on mathematical constraints on twin nucleation, growth, and interaction
- These properties produce supra-grain correlations that are important for large-scale material properties
- We are developing simulation approaches that efficiently handle the mathematics of multiple twinning
 - Capturing the essence of the network constraints is demonstrated
 - Group theoretical formalism handles twin nucleation efficiently in Monte Carlo simulations
 - More predictive phase field simulations are under development
- Realistic network properties are easy to get. Realistic evolution needs a great deal more physics to be in the model.


Neighboring TRD's are usually separated by random boundaries



- The grain orientations in neighboring TRD's are unrelated.
- They still form special boundaries occasionally, breaking up the random boundary clusters.



Grain boundary networks in conventional and engineered materials are qualitatively different



- Mostly flat Σ3's, twinning back-andforth on the same {111} planes
- Simple intra-TRD networks
- Few distinct orientations in each TRD



300 μ m Engineered Material, *f* = 0.60

- Highly complex intra-TRD networks
- More frequent inter-TRD special boundaries
- Many distinct orientations in each TRD

Lawrence Livermore National Laboratory

Definition: *f* = fraction of CSL boundaries

Weak boundary paths exist on length scales that match measurements of fracture surface roughness

- Red boundaries are strong (special)
- Black boundaries are weak (random)
- Background colors are twin-related domains



Size Scales

Grain diameter 35-70 μm

TRD diameter 70-160 μm

Isolated Random Boundary 10-20 μm

Shows up in the roughness scaling of both materials

Large Random Boundary Cluster 140-160 μm

Shows up in the roughness scaling of the normal material

Example results from Reed et al., Acta Mat. 56, 3278 (2008)



LLNL-PRES-430016

The group structure can be efficiently represented by strings on a four-letter alphabet

- There are four "generators." Call them a, b, c, and d.
- Each represents a twin on a specific {111} plane.
- Each is its own inverse. $aa = bb = cc = dd = \phi$
- Any orientation in the group can be reached by a finite string of these 4 letters.
- Any orientation at all can be approximated by a string of length <16.
- After doing maximal pair cancellation, the string is unique, and the "type" of the rotation is $\Sigma 3^{\text{string length}}$
 - Example: abccbd = abbd = ad is a $\Sigma 3^2 = \Sigma 9$
- The inverse of a string is the same string in reverse order
- The misorientation between two strings is String₁-1String₂
 - Example: Misorientation between abd and abcd is $(abd)^{-1}abcd = dbaabcd = dbbcd = dcd$, which is a $\Sigma 27$.

These are <u>all</u> of the rules. Following these lets you efficiently handle all twinrelated orientations while guaranteeing crystallographic consistency. Computer Simulations of Evolving Microstructures: Nucleation, Growth, & Coarsening

J. M. Rickman Dept. of Mat. Sci. & Eng. and Dept. of Physics Lehigh University



<u>Collaborations</u>

K. Barmak W. S. Tong S.-B. Lee A. D. Rollett J. D. Gunton



Petroleum Research Fund



Outline

- Nucleation and Growth: Simulation and Analysis

Simulation Methodology

Correlation Functions

Microstructural Descriptors

Homogeneous vs. Heterogeneous Nucleation

Non-Isothermal Transformation

Non-Euclidean Geometry

- Applications

Deducing Nucleation Conditions From a Microstructure

Tailoring Microstructures in Transforming Films



Input to Coarsening Models

Stochastic Geometry

- kinetics of nucleation & growth to coalescence

- microstructural features

Distribution of nuclei \rightarrow Generator of point process

Tools

- computer simulation (Monte Carlo)
- nonequilibrium correlation functions
 - neighbor distributions

- Can one deduce nucleation conditions from kinetic data?

- Can one deduce nucleation conditions from a coalesced microstructure?

Simulating Nucleation and Growth

Partitioning of Space - burst of nuclei



burst of nuclei (Poisson process)
constant growth rate
growth stops at impingement

$10^{50} \frac{10^{50} 0^{0} 5^{-10}}{10^{10} 0^{10} 0^{10}}$

Partitioning of Space - time-dependent nucleation rate

- Constant nucleation rate \rightarrow Poisson process in space and time
- kinetic Monte Carlo (N-fold way) used to model time-variable rate of non-isothermal case

Simulating Nucleation and Growth



1.0 1.0

Burst of nuclei on sphere Constant angular growth rate

Burst of nuclei in plane Constant growth rate Non-isothermal conditions Temperature ramp







Sekimoto n-point correlation function

$$C_{n}(\vec{r}_{1},\vec{r}_{2},...,\vec{r}_{n},t) = \exp\left[-\int d^{2}r' \int d\tau I(\vec{r}',\tau) \left(1 - \prod_{i=1}^{n} D(\vec{r}_{i},t;\vec{r}',\tau)\right)\right]$$



Poisson Statistics

Prob. untransformed $\propto \exp[-n\pi r^2]$

- Fraction transformed determined from stochastic geometry (Poisson process).
- Correlated nuclei other point processes.
- Non-Euclidean spaces other metrics.



 $C_2(\vec{r}_1, \vec{r}_2, t) = \exp[-n \int d^2 r' (1 - D(\vec{r}_1; t; \vec{r}'; 0) D(\vec{r}_2; t; \vec{r}'; 0))]$

 $C_2(\delta, t) = [C_1]^2 \exp(n\pi G^2 t^2 \gamma(s)),$

$$\gamma(s) = \frac{2}{\pi} \left[\sin^{-1} \sqrt{1 - s^2} - s \sqrt{1 - s^2} \right] \Theta(1 - s).$$



Two-Point Function - Special Cases

Non-Isothermal System

$$\chi(\vec{r_1}, \vec{r_2}, t) = \frac{C_2(\vec{r_1}, \vec{r_2}, t) - C_1(\vec{r_1}, t)C_1(\vec{r_2}, t)}{C_1(\vec{r_1}, t)C_1(\vec{r_2}, t)}$$

$$\chi(|\vec{r}_1 - \vec{r}_2|, t) = \exp\left[\frac{2G_0^2 I_0 t^3}{3} \left(\arccos(y) - 2y\sqrt{1 - y^2} + y^3 \ln\left(\frac{1 + \sqrt{1 - y^2}}{y}\right)\right)\Theta(1 - y)\right] - 1,$$

Spherical Surface

$$\chi(\Phi, t) = \frac{\left[1 - A_{\cup}(\Phi, t) / 4\pi\right]^{N}}{\left[1 - f(t)\right]^{2N}},$$



Heterogeneous Nucleation - Kinetics



Nucleation on Grain Boundaries



Transformation Fraction









Microstructural Analysis



Final microstructure (burst of nuclei in plane)





Grain area distribution comparison with gamma dist. (Kiang)

$$P^{\gamma}(A') = \frac{1}{\beta^{\alpha} \Gamma(\alpha)} (A')^{\alpha - 1} \exp(A')$$

Correction due to spherical geometry

Heterogeneous Nucleation - Microstructures



random distribution of nuclei



GB catalyzed



grain corner catalyzed

Pair Correlation Function - Corner Sites

Shows nonrandomness of sites.



Distinguishing Among Nucleation Scenarios

r = internucl. sep. (boundary)/grain size



Other Microstructural Descriptors - Stochastic Geometry

Neighbor distributions - useful if locations of nuclei are known

 $\langle r_k \rangle = \frac{1}{\sqrt{\pi} (\lambda_d)^{1/d}} \left[\Gamma \left(1 + \frac{d}{2} \right) \right]^{1/d} \frac{\Gamma (k+1/d)}{\Gamma(k)}$ first moment of k-th neighbor distribution



Locating Nuclei from Coalesced Microstructure



microstructure after successive iterations

Reverse Monte Carlo Procedure

- choose trial positions for nuclei
- generate associated microstructure
- calculate objective function for markers
 - reject/accept criterion

Microstructure - Non-Isothermal Conditions



constant nucleation rate (isothermal)

constant heating rate



$$\begin{split} \langle N(B)\rangle &= I_0 \int_0^\infty dt \, \exp\!\left(\frac{-\epsilon_{\rm I}}{k_B T(t)}\right) (1-\phi(t)) \\ &\approx \langle N(B=0)\rangle \! \left[1 + \frac{5B}{6T_0} \! \left(\frac{3}{\pi I_0 G_0^2}\right)^{1/3} \frac{\Gamma\!\left(\frac{2}{3}\right)}{\Gamma\!\left(\frac{1}{3}\right)} \overline{\epsilon} \right], \end{split}$$

Applications

- tailoring microstructure in a transforming thin film
 - starting microstructure for models of coarsening



reverse MC



microstructural evolution by coarsening

Biased Nucleation - Thin Film



transforming film



misfit dislocation -> biasing stress



biased nucleation and growth



Connection with Nucleation & Growth Models

Initial (Precoarsened) States

- site-saturation kinetics \longrightarrow narrow distribution
- constant nucleation rate \longrightarrow wide distribution

Input For Coarsening Models



1.) Start with a coalesced microstructure from a nucleation and growth simulation

2.) Map onto a spin model

$$E = \frac{1}{2} \sum_{i}^{N} \sum_{j}^{26} e(s_i, s_j).$$

Q-state Potts Hamiltonian

Voxels: s = 1,2,...,Q

Srolovitz et al. (1983) Anderson et al. (1984) Rollett et al. (1989)

3.) Evolve in time to minimize energy.

Example: Liquid-Phase Sintering



Temporal Evolution

- 128x128x128
- -Initial solid fraction: 0.7
- -Liquid matrix omitted for visualization.
- -Only a portion of the particles present in (a)-(e).

- kT = 1.6



Conclusions

- Concepts from stochastic geometry are useful for describing phase transformation kinetics and associated microstructure.

- In some cases it is possible to deduce nucleation and growth conditions from kinetic data and coalesced microstructures.

-Computer simulation can be used to generate configurations needed for averaging and visualizing microstructures.

- Insights from stochastic geometry can help to tailor transformation microstructures in thin films.



Early Work

- Ostwald Ripening MC Potts Model: Tikare and Cawley (1998)
 - two-dimensional model
 - fully-wetting condition (interface energy relations)
- MC Potts Model of Solid-State Sintering of Ceramics: Xiangge et al. (2005)

- coarsening in eutectic microstructures

- Geometrical MC Method: Aldazabal et al. (2004)
 - simulation of liquid-phase sintering
 - no distinction among orientations

Potts Model



- Voxel spin value reflects phase and, for solids, orientation

Liquid voxels: s = -1 Solid voxels: s = 1,2,...,Q

- Interface Energies

e_{ij}=0, s_i=s_j

e_{ij}=0.8, s_is_j<0 (solid/liquid interface)

e_{ij}=2.0, s_is_j>0, s_i=s_j (solid/solid interface)

- Significance of Transitions

dissolution diffusion precipitation







Coarsening Curves



 $\langle V(t) \rangle - \langle V_0 \rangle = Kt$

 $K = 0.0034 - 0.0037 MCS^{-1}$

$$\chi(\Phi, t) = \frac{[1 - A_{\cup}(\Phi, t)/4\pi]^{N}}{[1 - f(t)]^{2N}},$$

Another Example: Liquid-Phase Sintering



Tailoring Transforming Microstructures in Thin Films


Finding critical configurations in phase transformations and plastic deformation

Chen Shen^a, Ju Li^b, Yunzhi Wang^c

^a GE Global Research
^b University of Pennsylvania
^c Ohio State University

Joint AFRL/AOARD/LLNL workshop on nucleation during solid-solid phase transformations in metallic systems, Maui, 2-7 May 2010



Outline

- Energy of nucleus
- Free-end NEB
- Critical nucleus and nucleus along "minimum energy path"
- Dislocation shearing gamma prime
- Summary





Free Energy of a Nonuniform System. III. Nucleation in a Two-Component Incompressible Fluid

JOHN W. CAHN AND JOHN E. HILLIARD

General Electric Research Laboratory, Schenectady, New York



$$W = \int_{V} \left[\Delta f' + \kappa (\nabla c)^{2} \right] dV, \qquad C = C(\mathbf{r})$$

 $\Delta f' = f'(c) - f'(c_0) - (c - c_0) \left(\frac{\partial f'}{\partial c}\right)_{c = c_0}.$





Nudged elastic band (NEB) method



(Mills & Jónsson, 1994; Jónsson et al, 1998; Henkelman & Jónsson, 2000)





"free-end" NEB

(Zhu, Li, Samanta, Kim, and Suresh: Proc. Nat. Acad. Sci. USA, 2007, vol. 104, pp. 3031–36)

Example: diffusional transformation (precipitation)



$$\frac{\delta}{\delta c} \left(F - \int d\mathbf{x} (c(\mathbf{x}) - c_0) \mu_0 \right) = \frac{\partial f}{\partial c} - \kappa \nabla^2 c - \mu_0 = 0$$
$$T = \alpha T_0$$
$$f(c) = \frac{\alpha}{2} \Omega [c \ln c + (1 - c) \ln(1 - c)] + \Omega c (1 - c)$$



Example: displacive (cubic \rightarrow tetragonal) transformation









Nucleus along the minimum energy path





Critical configurations





(Shen, Li, Wang, Met Trans, 2008)



What else can we do?



С



Shearing of gamma prime



(Shen, Li, Mills, Wang, 2007)



12 / GE /

Dislocation core structures





SISF formation at low temperature & high stress



Fig. 1. TEM micrograph showing a {111} section through TMS-82+ superalloy deformed in tension to 1.4% strain at 750°C and 750MPa. Evidence of primary creep is visible: γ channels are populated with $\frac{a}{2} \langle 110 \rangle$ dislocations, an $a \langle 112 \rangle$ ribbon has nucleated in the matrix and sheared several γ' precipitates leaving intrinsic and extrinsic faults.

(Rae & Reed, 2006)





(Vorontsov, Shen, Wang, Dye, Rae, Acta mater 2010)





(Vorontsov, Shen, Wang, Dye, Rae, Acta mater 2010)



$6C\delta$ core structures under applied stress





-30°; **τ1=0 < τ2 < τ3**







18/ GE/

200

Summary

Non-classical nucleation theory + NEB is a quite open platform to study nucleation in some details

- greater flexibilities to handle nucleus structure details
- leverage new techniques from phase-field community
- combine new data from other computational methods (ab initio, CALPHAD) or from experiment (e.g., 3DAP)
- at thermodynamic level. Perhaps the only way in the near future to handle chemically complex (multi-component) alloys

Commonality with other 'non-nucleation' problems



Can we control embryo properties?

GJ Shiflet

SJ Poon, EA Starke, A. Zhu, M. Widom (CMU) M.Gao, A. Csontos, B. Gable, A Cheung UVa; Charlottesville, VA

AFRL/AOARD/LLNL Workshop, Maui

....it is assumed that solids are so complex that it is better to make approximations first, and then try to show they are consistent with the basic rules of quantum mechanics, and that they yield properties consistent with measured values.

John Gilman "Electronic Basis of the Strength of Materials"

Effect of Trace Additions Cd, In and Sn on the Interfacial Structure and Kinetics of Growth of q' Plates in Al-Cu Alloy; R Sankaran and C Laird, Materials Science and Eng. 1974.

- Nucleation of θ' takes place by the coalescence of mobile impurity –Cu– vacancy clusters and growth of the precipitates by the movement of these clusters [Hardy 1950; Nobel 1968]
- 2- Trace elements modfy the α:θ' interface giving an easier match with the matrix lattice, so that the critical size and energy barrier height for nucleation are reduced [Silcock et al; 1955 and Hardy 1956]
- 3- In the presence of impurity elements, vacancies in the quenched Al-Cu alloy condense to form finer distribution of dislocation loops. An increased density of of θ' precipitate can result from their nucleation on the loops.[Nuyten 1967]

Effect of lattice disregistry variation on the late stage phase transformation behavior of precipitates in nickel-aluminum-molybdenum alloys. Conley, J. G.; Fine, M. E.; Weertman, J. R. Acta Metallurgica (1989), 37(4), 1251-63.

Use controlled lattice disregistry (tune AI+Mo) to affect precipitate morphology (cubes vs spheres) and coarsening kinetics



mostly affected Ni matrix



A variety of exptl. techniques were applied to examine how compositional variations in lattice disregistry (d) affect the coarsening kinetics and particle morphol. evolution of g'-particles in several Ni-Al-Mo alloys. Mo segregates to and increases the lattice parameter of the g-matrix in 2 phase Ni-base Al alloys. Controlled ternary addns. of Mo to dil. binary Ni-Al alloys permit variation of the lattice parameter disregistry between the Ni-base solid soln. and the Ni3Al ordered ppts. Compns. were selected to maintain an approx. .apprx.10 vol.% of the 2nd phase. The coarsening rate of the g'-phase decreases with decreasing lattice disregistry and decreasing Al/Mo ratio. The implications of this observation are discussed with ref. to differences in solid soly., diffusivity, and interfacial energy. The g'-particle shape in low coherency strain alloys is spherical and independent of particle size. In an alloy exhibiting appreciable d and coherency strain, the g'-particles evolve from randomly distributed spheres to sharply aligned cubes and rods as particle size increases. d Increases with aging time. Compression creep of [100] single crystals at 750° did not affect the shape of particles in the low coherency strain alloys while in a higher disregistry alloy, a highly oriented array of plates grew with long edges perpendicular to the applied stress direction. These findings are discussed with regard to stress and thermodn. considerations.

The precipitate Ω*-phase in aluminum-copper-magnesium-silver alloys. Muddle, B. C.; Polmear, I. J.* Acta Metallurgica (1989), 37(3), 777-89.

The combined addn. of small concess, of Ag and Mg to Al-Cu alloys promotes pptn, of a phase, Ω - $\pi\eta\alpha\sigma\epsilon$, that forms as thin, hexagonal-shaped plates on matrix (111ña planes. The structure, morphol., and compn. of this phase were examd. in 2 quaternary alloys using TEM, electron microdiffraction and energy dispersive x-ray spectroscopy. Electron microdiffraction patterns from the ppt. phase are indexed in accordance with an orthorhombic structure (a = 0.496 nm, b =0.859 nm, c = 0.848 nm) and the orientation relationship between ppt. and matrix lattices is such that (001)W||(111)a and [010] Ω ||[10.hivin.1]a. The morphol. of the ppt. phase is consistent with the intersection point group (2/m) defined by symmetry elements common to the 2 lattices in the obsd. orientation relationship. The plate shape parallel to (111)a is detd. by a pinacoid parallel to the common 2-fold axis, [010]W. The hexagonal form in this plane is defined by 4 equiv prism facets with a common direction perpendicular to [010]W and the truncation of this prism section by a second pinacoid normal to this 2-fold axis. The 6 facets thus defined are equiv. geometrically and are assocd. with the hexagonal lattice on which the orthorhombic structure of the ppt. phase is based. Energy dispersive x-ray microanal, indicates that the Ag in quaternary alloys partitions to the W phase during aging and there is evidence that segregates at the interface with the matrix. On the other hand, Ag does not partition to the phase q' when it coexists with W in these alloys or is present alone in the ternary alloy Al-Cu-Ag. There is also evidence to suggest that Mg assocs. itself with the Ω phase.

On the origin of the high coarsening resistance of Ω plates in Al-Cu-Mg-Ag Alloys. Hutchinson, C. R.; Fan, X.; Pennycook, S. J.; Shiflet, G. J.. Department of Materials Science and Engineering, University of Virginia, Charlottesville, VA, USA. Acta Materialia (2001), 49(14), 2827-2841.

The thickening kinetics of W plates in an Al-4Cu-0.3Mg-0.2Ag (wt.%) alloy were measured at 200, 250 and 300°C using conventional transmission electron microscopy techniques. At all temps. examd. the thickening showed a linear dependence on time. At 200°C the plates remained less than 6 nm in thickness after 1000 h exposure. At temps. above 200°C the thickening kinetics are greatly increased. At. resoln. Z-contrast microscopy has been used to examine the structure and chem. of the (001)W.dblvert.(111)a interphase boundary in samples treated at each temp. In all cases, two at. layers of Ag and Mg segregation were found at the broad face of the plate. The risers of the thickening ledges and the ends of the plates were free of Ag segregation. The necessary redistribution of Ag and Mg accompanying a migrating thickening ledge occurs at all temps. and is not considered to play a decisive role in the excellent coarsening resistance exhibited by the W plates at temps. up to 200°C. Plates transformed at 200°C rarely contained ledges and usually exhibited a strong vacancy misfit normal to the plate. A large increase in ledge d. was obsd. on plates transformed at 300°C, concomitant with accelerated plate thickening kinetics. The high resistance to plate coarsening exhibited by W plates at temps. up to 200°C, is due to a prohibitively high barrier to ledge nucleation in the strong vacancy field normal to the broad face of the plate. Results also suggest that accommodation of the large misfit that exists normal to the broad face of the plate is unlikely to provide the driving force for Ag and Mg segregation.





3D-AP: Al-Cu-Mg-Ag

Hono et al: Al-1.9Cu-0.3Mg-0.2Ag (at%), aged at 180 degC



Heterogeneous nucleation of δ ' on dislocations in a dilute aluminum-lithium alloy. Wang, Z. M. & Shiflet, G. J.. Metall and Materials Trans A: (1996), 27A(6), 1599-1609.



δ ' nucleation and growth on low-angle dislocation boundaries in Al-Li. Wang, Z. M.; Shiflet, G. J.. Physica Status Solidi A: (1995), 149(1), 105-22.



the reacted dislocation has a large edge component and at the site of the network plane where the dilatation stress is compressive. This is confirmed by calch. of the dilatation stress field of the dislocation nodes which also further clarifies and is consistent with the exptl. observations.

The effect of plastic deformation on aluminum-copper-lithium Al₂CuLi (T1) precipitation. Cassada, W. A.; Shiflet, G. J.; Starke, E. A., Jr.; Metallurgical Transactions A: Physical Metallurgy and Materials Science (1991), 22A(2), 299-306.

The enhancement of T1 pptn. in Al-Li-Cu alloys by plastic deformation prior to aging (i.e., cold work) and the subsequent increase in alloy strength is investigated. The increased understanding of the role of matrix dislocations in the nucleation and growth of T1 plates, discussed in a previous paper, permits a detailed study of the phenomenon. The effect of different levels of plastic strain on the T1 particle distributions as a function of aging time at 190° is quantified, and the subsequent influence on tensile properties is thereby described. Plastic deformation decreased the T1 plate length and thickness, increased the no. d. by .apprx.2 orders of magnitude, increased the yield strength by 100 MPa, while simultaneously reaching peak strength in 20% of the time required without plastic deformation.

Structural Evolution in Al₈₅Ni₇Gd₈ - Non-isothermal DSC Heating



1st stage finished

2nd stage

before

the 1st

stage

3rd stage

4th stage

Crystalline Phase Formation Sequences at $\leq 250^{\circ}$ C







On the Roles of Clusters during Intragranular Nucleation in the Absence of Static Defects

Nie, Muddle, Aaronson, Ringer and Hirth Metall. Mater. Trans, 2002.

- Clusters form and disappear on timescale shorter than embryos
- clusters another form of nucleation site and so are involved in 'cluster-aided intragranular nucleation' heterogeneous nucleation
- reduction of shear strain energy attending precipitate nucleation through segregation of trace solutes and vacancies bound to them to regions of the precipitate interfaces under compressive or tensile strains

Based on all we learned about bonding from amorphous metals – can we transfer ideas to nucleation in conventional alloys?

Balance between calculations and experiments*

- Focused calculations are necessary
 - Phase diagrams (partial phase diagrams)
 - Element associations (electronic)
 - Cluster formation f(T)
 - Elastic properties of clusters
 - If working with a modeler –<u>they must work on the</u> problem!
- Experiments are essential
 - Validation of calculations by small adjustments
 - Proof of concept predictive NOT postdictive

*for Shiflet

Information we are interested in from EELS


Aluminum nanocrystals form at high densities – 10¹⁸ cm⁻³ Fe and Gd rejected into the matrix forming shells



Zero Loss and Plasmon



No difference is observed for plasmon peak among as-spun $Fe_{71\text{-}X}Mo_{5\text{+}X}P_{12}C_{10}B_2$ ribbons

JOURNAL OF APPLIED PHYSICS 101, 054308 2007 VP Oleshko and JM Howe

Plasmons and Material Properties



• Collective oscillation of the valence electron density that occurs at a resonance angular frequency ω_p with a plasmon energy E_p given by:

 $E_{\rho} \cong h\omega_{\rho}$,

where $\omega_p = [ne^2/(\varepsilon_0 m)]^{1/2}$, *n* is the valence electron density, *e* is the electron charge, ε_0 is the permittivity of vacuum, *h* is Planck's constant, and *m* is the electron mass.

• The relation between E_p and n allows one to determine material properties that are governed by the valence electron density.

Scaling of experimental and calculated single-crystal B_m with E_n



Least-squares-fitted linear regressions for scaling relationships of the power law type $B_m = AE_p^B$ derived using experimental data for single-crystal bulk moduli and LDF quantum mechanical calculations

Properties of Metastable TiH_x precipitates in Ti-H alloy



 $B_m^{Ti} = 85.2 \text{ GPa}; B_m^{TiHx} = 112.5 \text{ GPa}$ $Y_m^{Ti} = 104.7 \text{ GPa}; Y_m^{TiHx} = 143.9 \text{ GPa}$ $G_m^{Ti} = 31.3 \text{ GPa}; G_m^{TiHx} = 42.4 \text{ GPa}$

Intensity profile shows B_m versus position with a spatial resolution ~1 nm and modulus resolution of a few GPA; the B_m map is also a H map because B_m scales linearly with H in solid solution in α -Ti alloys





→ Obtain fundamental scientific understanding concerning



Fracture Behavior in adjusted Amorphous Steel



Strain rate ~10⁻⁴ s⁻¹ Tensile fracture ≈ Compressive fracture

(Gu, Poon, Shiflet, J. Mater. Res. (2007))

Reason to be able to make alloys in-house

 $Fe_{65-X}Mo_{14}C_{15}B_6Er_X$



Goal is to develop a strategy for selecting compositions based on microscopic models involving <u>atomic bonding</u> & <u>local structure</u>

Er

Gu, McDermott, Poon, Shiflet, Appl. Phys. Lett. (2006)

Electronic Structure-Carbon



EELS Result-C-K edge



EELS Result-C-K edge



EELS Result-Fe-L_{2,3} edge



ab initio band calculation shows increase of Fe 3*d*-white intensity for both Er and Cr additions. (M. Widom) Er is a strong electron donor Confirmed by XPS



As-spun $Fe_{71-X}Mo_{5+X}P_{12}C_{10}B_2$ amorphous ribbons





Two humps corresponding to $P-L_{2,3}$ edge are observed for Fe_3P crystalline alloy. $Fe_{71}Mo_5P_{12}C_{10}B_2$ ribbon shows similar but less clear humps of $L_{2,3}$ edge as Fe_3P , indicating the Fe-P bond is the major bond of the bonding surrounding P atom. As Mo content increases, these two humps are smeared off. This might be due to the formation of stronger Mo-P bonds and thus reduce Fe-P interactions in amorphous structure. (Verified by the increasing 3*d* white line intensities of Fe with increasing Mo content).



Fe 3*d* white line intensities calculations show a slight increase of Fe 3*d* white line intensities and a decrease of L_3/L_2 ratio with increasing Mo content for as-spun Fe_{71-X}Mo_{5+X}P₁₂C₁₀B₂ ribbons. 3*d* electrons number decreases with increasing Mo content, indicating less Fe-P interactions, supporting the P- $L_{2,3}$ edge results.

can be tuned for G

Uniaxial compressive true stress-strain curves for four Fe-Cr-Mo-P-C-B BMGs (a) Fe63<u>Cr3Mo12</u>**P10**C7B5, (b) Fe64Cr3Mo10**P10**C10B3,

(c) Fe63<u>Cr3Mo10</u>P12C10B2, and

(d) Fe71Mo5**P12**C10B2.



adding electrons to a more than half filled shell weakens the bond (Pettifor tight-binding model)

Ab-Initial Calculation and Neutron Scattering Measurement

(Michael Widom and Despina Louca)

Partial contributions to total PDF Charge densities Bonding enthalpies Elastic moduli

. Ab-initio MD was performed using the density functional theory. Supercooled liquid of FeMoBC was first simulated; the resulting structures were then quenched using conjugate gradient relaxation to obtain the amorphous structure.

. <u>Density of states</u> and <u>charge transfer</u> were obtained from VASP using projector augmented wave potentials

. <u>Crystal Orbital Hamilton Population COHP</u> (Dronwkowski & Blöchl 1993) was computed to obtain the <u>bonding enthapy</u>. Orbital-projected data was obtained from TB-LMTO calculations.

$$\psi(r) = \sum_{\substack{\text{atomi}\\\text{orbital}\alpha}} c_i^{\alpha} \chi_{\alpha}(r - R_i)$$

$$E = \sum_{\substack{i\\\alpha}} E_i^{\alpha} + \sum_{\substack{i\neq j\\\alpha,\beta}} c_i^{\alpha*} c_j^{\beta} H_{\alpha\beta}^{ij}$$
COHP





Gu, Poon, Shiflet, **Widom**, Acta Materialia

Composing ductile Fe-SAM:

Bonding charge densities of Fe₃C (oP16) and Fe₃P (tl32). Color bar indicates the bonding charge density of electrons in units of Å⁻³ (note that negative (blue) means a *decrease* in electron density). *Isosurfaces enclose regions of bonding charge density greater than 0.06 Å⁻³.*





Covalent-like Fe-C bond in Fe₃C More metallic Fe-P bond in Fe₃P

Charge transfer from (Fe, Mo) to C Charge transfer from P to (Fe, Mo)

Coexistence of metallic & covalent bonds

Cut plane view of bonding charge densities. Color bar indicates the bonding charge density of electrons in units of Å⁻³ (negative (e.g blue) means a *decrease* in electron density).



Trace Elements & Nucleation

Clustering of Solute Atoms => Heterogeneous Nucleation Sites

Two questions as to which elements to add or remove:

- 1) Can they form clusters or co-clusters in the solid solutions?
- 2) Are the clusters "precursors" or "nonprecursors" for desired phases?

Cluster Formation Analysis

Objective: to predict clustering tendency of solute atoms

One Possible Approach:



Quasi-Chemical Model of Higher Order Systems

$$G = \sum_{i} N_{ii} E_{ii} + \sum_{i \neq j} N_{ij} E_{ij} - kT \cdot \ln \left\{ \frac{(zN/2)!}{\prod_{i} N_{ii}! \cdot (\prod_{i \neq j} (N_{ij}/2)!)^{2}} \cdot \frac{\prod_{i} [(z-1)NX_{i})!}{[(z-1)N]!} \right\}$$

$$\frac{Y_{ij}^{2}}{(x_{i} - \sum_{p=i,q} Y_{pq}) \cdot (x_{j} - \sum_{p,q=j} Y_{pq})} = \exp\left(-\frac{2\Omega_{ij}}{kT}\right)$$

Warren-Cowley SRO parameter

Pairs: $y_{ij} = 1 - Y_{i,j} / x_i x_j$

Triples / Tetrohedrans: $u_{ijk...} = 1 - U_{ijkl} / x_i x_j x_k...$

- positive: clustering
- zero: random
- negative: SRO or co-clustering

SRO Parameters: AI-0.0175Cu-xMg



SRO Parameters: Si, Ag Effects

AI-0.0175Cu-xMg-0.005Si x(Mg) AI-0.0175Cu-xMg-0.01Ag



3D-AP: Al-Cu-Mg-Ag

Hono et al: Al-1.9Cu-0.3Mg-0.2Ag (at%), aged at 180 \[]C

111

-5 nm



~8 nm

b) 300 s

-4 nm



Depth [nm]

Precursors or Non-Precursors?

- Precursor: enhance nucleation of desired phases, like Cu for θ & Ag for Ω
- Non-precursors: enhance nucleation of undesired phases and/or consume the solute content needed for desired phases, like Si for Omega

Hornstra-Bartels Model

$$E(\xi) = \frac{1}{2}C_{ijkl}(\varepsilon_{mis}\delta_{ij} + b_i\xi_j)(\varepsilon_{mis}\delta_{mn} + b_m\xi_n)$$

Cu-FCC in Al

Mg-FCC in Al



TEM: Si Effect

- Specimens were aged at 250°C for 30min and 2h
- Both aging conditions revealed similar microstructures, with the only difference being the size of precipitates.

Al-4.0Cu-xMg-(0.3Ag)-xSi	Mg	Mg / Si ratio	Ω Precipitation		
$[^{wt}/_{o}]$	[^{wt} / _o]	$[^{wt}/_{o}] \sim [^{at}/_{o}]$	no	very few	yes
	0.1	1	Х		
Constant Si content	0.2	2	Х		
~0.1 [^{wt} / _o]	0.3	3		Х	
	0.4	4			Х
Constant Si content	0.4	2	Х		
~0.2 [^{wt} / _o]	0.6	3		X	
	0.8	4		X	

• These results indicate that a Mg/Si ratio of ~2.0 must be overcome in order to nucleate Ω precipitation.

SRO Parameters: Si, Ag Effects

AI-0.0175Cu-xMg-0.005Si x(Mg) AI-0.0175Cu-xMg-0.01Ag



conclusions

• Why not build new precipitates by taking control of:

clusters \rightarrow embryos \rightarrow nuclei \rightarrow precipitates? High risk and possible high returns–

Keep close ties on elastic coefficients (electrons)
Use chemical and statistical thermodynamics
Good experimentalist controls the modelers –if
possible! Model what is needed.

First Principles Simulations Of Beta To Omega Transformation In Titanium Alloys

Srinivasan G. Srivilliputhur

Department of Materials Science and Engineering University of North Texas Denton, Texas, U.S.A.



Acknowledgements

<u>A. Devaraj, N. Gupta</u>, S. Nag, Rajarshi Banerjee University of North Texas Denton, Texas, U.S.A.

> S. Rajagopalan*, H. L. Fraser Ohio State University Columbus, Ohio, U.S.A. *Now at Exxon Mobil





Financial support for this work has been provided by the National Science Foundation and the Air Force Research Laboratory

Summary of Experimental Work

- \blacktriangleright Mechanism of $\beta \rightarrow \omega$ transformation not completely understood
- \blacktriangleright β solutionized and quenched Ti-9at%Mo exhibits fine scale ω embryos
 - Different stages of {111} β plane collapse *aberration corrected* HAADF-STEM
 - Clear evidence of Ti-Ti clustering *3D atom probe*
 - Phase separation in β matrix prior to ω formation?
- Subsequent annealing at 475°C/30mins
 - well-developed ω precipitates complete collapse of {111} β planes
 - Substantial partitioning of Mo between β and ω
What do we learn from experiments? – Schematic G – X plot for quenched Ti-Mo



 \blacktriangleright Phase separation in β matrix required for ω formation in Ti – 9 at% Mo

> Mo-depleted pockets with compositions < T_0 form ω nuclei by displacive collapse

 \succ Is the displacive collapse complete within ω nuclei?

Summary of Experimental Work: Schematic $G - \eta$ plots for Ti-Mo



- Mo-depleted pockets with compositions < T₀ form ω nuclei by displacive collapse
- Extent of displacive collapse can be incomplete within ω nuclei – composition dependent amplitude of phonon wave?





Questions

- > Is phase separation in β matrix mandatory for ω formation in Ti-9at%Mo?
- Though ω forms via a displacive collapse of {111} β planes, why is the collapse arrested (partial collapse) in quenched ω embryos
 - Does the extent of collapse depend on ω pocket composition? Why?
- Is there a mixed-mode displacive-diffusional transformation involved in the formation of isothermal ω precipitates?

Simulations Approach Used

- We use first-principles calculations using the Vienna Ab Initio Simulation Package (VASP) (Kresse and Hafnet, PRB 1993)
- β to ω transition path transformation in Ti-Mo system was determined using the Nudged Elastic Band (NEB) (Jónsson, Mills, Jacobsen, 1996)
- We use Projector Augmented Wave (PAW) potentials (Kresse and Joubert, PRB 1999)
- Generalized Gradient Approximation PBE (GGA-PBE) was used (Perdew, Burke, Ernzerhof, PRL 1996)
- Performed convergence tests to determine optimal parameters such as energy of plane wave cutoffs (400eV used) and K-mesh for integration

Our energy converged to 1 meV /atom

Hexagonal (ω) Phase Precipitation in BCC (β) Titanium

NOTE: Figures Not Drawn to Scale



(a) Completed collapsed {222} planes exhibit a 6-fold symmetry and an partial collapse leads to a 3-fold symmetry along <111> axis

(b) The displacement of {222} planes are visualized as a sinusoidal wave with upward and downward motions shown as positive and negative displacements respectively

UNIVERSITY OF NORTH TEXAS Discover the power of ideas. Banerjee and Mukhopadhyay, Phase Transformations (2007) de Fontaine, Paton, Williams, Acta Metall. **19**, 1153(1971)

Nudged Elastic Band (NEB) Method

- The nudged elastic band (NEB) is a method for finding saddle points and minimum energy paths (MEP) between <u>known</u> reactants and products
- NEB works by first constructing a "chain of images" of the system
- Each image connects to the previous and next image by 'springs' along the path
- Springs prevent images from sliding down to the nearest minima and forces them to find the lowest energy possible while maintaining equal spacing to their neighbors
- Minimization of the entire system, but with the end structures fixed, provides a MEP



Our Past Success with NEB: Minimum energy path for cross slip of a screw dislocation in Cu



(a) Initial configuration with parallel Shockley partials in the primary glide plane

Our Past Success with NEB: Understanding α to ω transformation in Pure Titanium



- In each stacking plane, 3 out of every 6 atoms shuffle by 0.74 Å along [11-20]_α while the other 3 shuffle along [-1-120]_α
- This shuffle is accompanied by a strain $\varepsilon_{xx} = 0.05 \text{ along } [1-100]_{\alpha}$ and $\varepsilon_{yy} = -0.05 \text{ along } [11-20]$ to produce a hexagonal ω cell with the correct c/a ratio.

Our Past Success with NEB: Understanding α to ω transformation in Pure Titanium



• The TAO-1 path gives the smallest barrier by a factor of 4 at 0 GPa.

Silcock pathway have larger barriers at from 0 GPa to 40 GPa

Our Past Success with NEB: Understanding α to ω transformation in Pure Titanium

Usikov and Zilbershtein $\alpha \rightarrow \omega$ transition path (Usikov & Zilbershtein, Phys. Status Solidi A 1973)

- > Mechanism: $\alpha \rightarrow \beta \rightarrow \omega$ transition via an unstable intermediary β -phase
- > $\alpha \rightarrow \beta$ transition occurs via an *inverse Burgers mechanism*, and is followed by $\beta \rightarrow \omega$ transition via collapse of 2 out of 3 (111)_{β} planes
- > This produces 2 unique pathways called variant-I and variant-2, depending on the direction of $\{111\}_{\beta}$ planes collapse.
- Allowing variants-1 and 2 to <u>relax away</u> from the β-phase yields our TAO-1 and TAO-2 direct transformation pathways

Our Past Success with NEB: Understanding how impurities block α to ω transformation in Titanium



- \succ C, N, O impurities suppresses the $\langle \Box |$ transformation by:
 - increasing both the energy relative to (and the energy barrier
- Despite different chemistry, C, N, O increase the energy barrier and the relative energy by nearly the same amount
- > This indicates that their primary effect is <u>steric</u>

Hennig et al, Nature Materials (2005)

Our Past Success with NEB: Understanding how impurities block α to ω transformation in Titanium



Interstitials in α and ω Ti

- Octahedral (o), tetrahedral (t), and hexahedral (h) sites for interstitial impurities
- A and B are substitutional impurity sites



Hennig et al, Nature Materials (2005)

Pure Ti Lattice Parameter and Energy

parameter	Ti beta super cell	Ti omega supercell	% change
а	4.5995	4.5773	0.5349 %
b	4.5995	4.5773	0.5349 %
С	5.6335	5.6595	-0.369 %
Supercell Energy (ev)	-46.693196	-47.380604	688 meV

Beta to omega transformation involves:

- Contraction of 0.53% along a and b axis
- Expansion of 0.37% along c axis of supercell.
- For pure Ti beta is 688 meV higher than omega

Mo substitution in Ti super cells

- Beta to omega transformation in pure Ti involves:
 - Contraction of 0.53% along a and b axis
 - Expansion of 0.37% along c axis of supercell.
- For pure Ti beta is 688 meV higher than omega



Beta to omega transformation in Pure Ti



No activation barrier observed in the nudge elastic band method for pure Ti beta to omega transformation

Ti – 16 at% Mo System (1 Mo + 5 Ti atoms in supercell)

- Energy of beta is lower than omega
- Systems with Mo substituted in the collapsing plane positions show same energy
- The omega structure with Mo in noncollapsing planes has a higher energy than omega with Mo in collapsing planes



A local minima at 21% partially collapsed structure observed near beta

Ti – 8.33 at% Mo System (1 Mo + 11 Ti atoms in supercell)

- Beta has a higher energy than omega
- A 30 meV activation barrier must be overcome by beta to transform to omega
- There is a local minima close to omega (41 meV) that must be overcome by system to transform fully to omega



Ti – 5.6 at% Mo System (1 Mo + 17 Ti atoms in supercell) CALCULATIONS NOT CONVERGED



NEB work summary

- In pure Ti beta omega transformation is thermodynamically favorable
- Trends observed in Ti-Mo alloys are
 - 4.16% Mo: Similar to pure Ti, Roll down with some minima close to omega
 - 5.55%Mo: in progress
 - 8.33%Mo: Similar to pure Ti, Roll down with some minima close to omega
 - 16.66%Mo: Opposite to pure Ti, minima close to beta

Points to Ponder

- Our preliminary calculations point to the ability of VASP + NEB calculations to determine activation barriers and order parameters for the beta to omega transformations rigorously
- As seen, our current systems are too small to allow variation of composition through out the supercell
- We are currently increasing our systems sizes to a couple of hundred atoms
- Such large systems may not be sufficient
- We may have to use semi-empirical atomisitic models such as MEAM, tight binding, MGPT or bond-order potentials to handle larger systems
- Need to couple these atomistic methods with combinatorial approaches to investigate effect of local compositional environment on saddle points in model binary systems

Thank you for your Attention Questions?



Accelerated Molecular Dynamics: Methods and Examples

Blas Pedro Uberuaga

Los Alamos National Laboratory



UNCLASSIFIED



Atomistic Dynamical Simulations 101

- Goal: simulate time evolution of a system of atoms
- Foundations:
 - Interatomic potential
 - Parameters fit to experiment, high quality calculations
 - Newton's Second Law
 - Tells how system evolves under forces
 - Can directly integrate to get time evolution
- But!
 - Can only perform ~2000 force evaluations/second (on Opteron)
 - Typical vibrational period of an atom is 10-100 fs
 - Need ~10 force evaluations per vibrational period for accurate integration
 - Each force evaluation advances system time by 1-5 fs
 - 10¹¹ years to simulate 1 second!



UNCLASSIFIED



MD may never get to relevant time scales





Brief Introduction to Accelerated Dynamics

- Many processes occur on much longer timescales than accessible via MD (ps-ns-μs)
 - e.g. surface growth
 - radiation damage annealing
 - nucleation
 - Etc.
- Need method to reach experimentally relevant timescales
- Three accelerated dynamics methods developed at LANL (Art Voter's team)
 - Parallel-Replica Dynamics
 - Hyperdynamics
 - Temperature Accelerated Dynamics (TAD)



UNCLASSIFIED



Infrequent Event System



- The system vibrates in 3N-dimensional basin
- Occasionally it escapes, crossing through a dividing surface to a new basin
- This behavior characterizes solid-state diffusion, as well as many other processes

Hyperdynamics



Increase rate by reducing effective barriers

AFV, J. Chem. Phys., 1997



UNCLASSIFIED



Hyperdynamics

Parallel Replica

Dynamics



Increase rate by reducing effective barriers

AFV, J. Chem. Phys., 1997

Explore basin with many processors M

AFV, Phys. Rev. B, 1998



UNCLASSIFIED



Hyperdynamics

Parallel Replica

Dynamics



Increase rate by reducing effective barriers

AFV, J. Chem. Phys., 1997

Explore basin with many processors M

AFV, Phys. Rev. B, 1998

Temperature Accelerated Dynamics



UNCLASSIFIED

Increase rate by raising temperature

M.R. Sorensen and AFV, J. Chem. Phys., 2000



Increase rate by reducing effective AFV, J. Chem. **Hyperdynamics** barriers Phys., 1997 Explore basin with **Parallel Replica** AFV, Phys. many processors M Rev. B, 1998 **Dynamics** M.R. Temperature Increase rate by Sorensen and Accelerated AFV, J. Chem. raising temperature **Dynamics** Phys., 2000

Common Themes: - reduce waiting time for a transition to order of picoseconds; - let trajectory find transitions "naturally"

Operated by Los Alamos National Security, LLC for the U.S. Department of Energy's NNSA

Introduction to Hyperdynamics

- Builds on umbrella-sampling techniques (e.g., Valleau 1970's); takes it into the time domain
- **Assumptions:**
 - infrequent events
 - transition state theory (no recrossings)
- **Procedure:**
 - design bias potential ΔV
 - zero at dividing surfaces
 - causes no recrossings
 - run thermostatted trajectory on the biased surface (V+ Δ V) ٠
 - accumulate hypertime as

 $t_{hyper} = \Sigma \Delta t_{MD} exp[\Delta V(R(t))/k_BT]$

UNCLASSIFIED

Result:

- state-to-state sequence correct (because relative rates are preserved)
- time converges on correct value in long-time limit (vanishing relative error)







Voter, JCP 106, 4665 (1997)

Hyperdynamics - characteristics

- Key challenge is designing a bias potential that:
 - meets the requirements of the derivation
 - is computationally efficient.

Bias potential can be a function of

- the shape of the energy surface (AFV, 1997)
- the energy (Steiner, Genilloud and Wilkins, 1998)
- the geometry (e.g., bond lengths, Miron and Fichthorn, 2003, 2005)
- Must be careful that bias is zero on all dividing surfaces or dynamics will be wrong.
- When barriers are high relative to T, boost can be many orders of magnitude.



UNCLASSIFIED



- Offers parallel speed-up in simulation time
 - Not as "glamorous" as other methods which offer exponential speed-up on a single processor
- However, parallel-replica can be applied to systems not suited to the other methods
 - Rough potentials
 - Floppy systems with fast transitions
 - Driven systems

Assumptions:

- infrequent events
- transitions can be detected
- correlation time known
- distribution of first-escape times is exponential





UNCLASSIFIED



Parallel-Replica Algorithm





UNCLASSIFIED



Parallel-Replica Algorithm



Replicate



UNCLASSIFIED



Parallel-Replica Algorithm



Dephase



UNCLASSIFIED




Parallel MD



UNCLASSIFIED





Parallel MD



UNCLASSIFIED





Correlation



UNCLASSIFIED





Replicate



UNCLASSIFIED









UNCLASSIFIED







Operated by Los Alamos National Security, LLC for the U.S. Department of Energy's NNSA

NATIONAL LABORATORY









Good parallel efficiency if t_{rxn} / M >> $\tau_{dephase}$ + τ_{corr}

Comparison of Parallel Algorithms

Standard MD



M simulations of size N for time t



UNCLASSIFIED



Comparison of Parallel Algorithms

Standard MD

Spatial Parallelization





Comparison of Parallel Algorithms





Detecting a Transition

- Best method depends on the system
- Simple method for EAM metal systems:
 - periodically perform minimization
 - see if geometry at basin minimum has changed



• Other Methods:

- change in bond connectivity/length (covalent systems) (Kum, Uberuaga)
- change in energy fluctuations (Pande)



UNCLASSIFIED



Examples of Parallel Replica Simulations

Vacancy void annealing in Cu

- Motivation
 - Examine void kinetics to understand void swelling under irradiation

Stretching of Ag nanowire

- Motivation
 - Understand tensile behavior of nano-sized wires



UNCLASSIFIED



Voids in Cu: Long time annealing of 20 vacancy

- EAM Cu
- Parallel-replica simulation of 20vacancy void annealing at 400 K
 - 20 vacancies is one too many for "perfect" void
- Total simulation is 7.82 μs
- At 1.69 μs, void transforms to SFT
- Run on 39 processors for 15 days
- Efficiency = 79%
- Equivalent single processor time: 1.3 years





Uberuaga, et. al., *PRL* **99**, 135501 (2007)

UNCLASSIFIED



Voids in Cu:

Transformation pathway for 20 vacancy void

- Full path for transformation to SFT calculated with NEB
- Initial barrier is > 2 eV
 - Should have taken >105 years at 400K to occur (assuming standard prefactor)
- Vineyard prefactor for first step is 2x10³⁶ s⁻¹
 - Vineyard rate is faster than one time step at 500K!





Uberuaga, et. al., *PRL* **99**, 135501 (2007)

UNCLASSIFIED



regionsRegion I: Cu

View material containing void as partitioned into two

Origin of Prefactor for Transformation

• Region II: void

Voids in Cu:

- Before transition, volume of Cu is Region I volume
- After, volume of Cu is Region I + Region II
- Entropy change ΔS due to volume change ΔV : $\Delta S = \alpha B \Delta V$
 - α =coefficient of thermal expansion, B=bulk modulus
- Assuming ∆V=10 atomic volumes ⇒ ∆S=67.5/kB ⇒ prefactor enhanced by factor of 10²⁹
- Consistent with observed/calculated prefactor of ~10⁴⁰

UNCLASSIFIED



Uberuaga, et. al., PRL 99, 135501 (2007)





Ag nanowire: ParRep of stretching nanowire

- Run on LANL Roadrunner (1 PFLOPS if using all 12,240 cell processors)
- Boost good at first; drops as events become more frequent.
- Outer edge atoms clamped, advanced 0.01A at regular intervals
- Preliminary results...

Ag[110] nanowire, 1.d5 A/s, 1 us per frame



Ag nanowire: Pulling slower changes behavior

At stretching speeds below ~10⁶ Å/s, the system can thin down to four layers, coming back to perfect fcc. At higher speeds, it disorders or necks, never recovering perfect fcc again.



Summary - Parallel-Replica Dynamics

Most exact of the accelerated dynamics methods

- no harmonic approximation
- goes beyond TST to include correlated dynamical events
- no assumption that barrier is energetic can be entropic

Easy to implement – requirements:

- transition detection
- good estimate of correlation time

Very general applicability

- any system with exponentially distributed events
- Good match to increasing availability of parallel processing power, distributed computing, etc.



UNCLASSIFIED



Limitations - Parallel-Replica Dynamics

Only get parallel boost

- If statistics are necessary such that number of samples is equal to or greater than number of processors, better to do MD
- Boost drops off when events are frequent (or become frequent because so many processors)
 - Requires "tuning" number of processors to temperature of interest
- Boost especially limited if correlation time is long
- For complex systems (e.g., proteins) even transition detection can be tricky



UNCLASSIFIED



Operated by Los Alamos National Security, LLC for the U.S. Department of Energy's NNSA

UNCLASSIFIED

Introduction to

Temperature Accelerated Dynamics (TAD)

Concept:

- System characterized by deep energy wells
- Run basin constrained MD at high temperature
- Extrapolate behavior to low temperature

Approximations:

- Harmonic Transition State Theory $(k = v e^{-\Delta E / k_B T})$
- Assumed minimum prefactor in system v_{min} •
- Uncertainty level δ of missing the correct event
- Very powerful when barriers are high relative to temperature



Sørensen and Voter. JCP 112, 9599 (2000)

Basin Constrained MD (BCMD)



- Run dynamics at T_{high}
- When event occurs, reflect trajectory back into basin
- Continue high-T dynamics
- Reflect trajectory after any other events
- Requires:
 - Detecting transition
 - Finding energy barrier



TAD algorithm



operated by Los mathematics mathematics, Let for the U.S. Department of Energy's NNSA



Examples of TAD Simulations

Interstitial clustering in MgO

- Motivation
 - Use MgO as model ceramic to understand radiation damage evolution

Interstitial emission at grain boundaries in Cu

- Motivation
 - Determine role of GBs in radiation tolerance of nanocrystalline materials



UNCLASSIFIED



MgO: Defect aggregation

- Using standard Buckingham potential with long range Coulomb interaction
- Begin with I_2 and I_4
 - Defects found at end of collision cascade
- I₂ attracted to I₄, binds forming I₆
- Metastable I₆ diffuses very quickly
 - ns timescale at 300 K
 - diffusion is 1D along <110>
 - decay to ground state takes years
- Boosts on the order of 10⁹
- Red=oxygen, Blue=magnesium
- Dark=interstitial, Light=vacancy



TAD simulation, Uberuaga et al, 2003



UNCLASSIFIED

Uberuaga, et. al., *PRL* **92**, 115505 (2004); *PRB* **72**, (2005); *NIMB* **28**, 260 (2005)



MgO: Interstitial cluster kinetics

- TAD simulations of interstitial clusters in MgO
- Diffusion barrier of ground state structures follow no clear pattern
- For clusters of size
 5 and greater, there
 are metastable
 structures that
 diffuse faster than
 the ground state





UNCLASSIFIED

Uberuaga, et. al., *PRL* **92**, 115505 (2004); *PRB* **72**, (2005); *NIMB* **28**, 260 (2005)



MgO: Effects of cluster mobility on observables

- 1-D reaction rate theory
 - Mobilities from TAD
 - Steady-state conditions
- Size of loops increases by more than 3 times when large clusters are mobile
 - "large" clusters contain more than 1 interstitial
- Enhanced defect mobility results in fewer, larger loops







UNCLASSIFIED



Grain boundaries in Cu: Damage production

- Snapshots of a 4 keV cascade initiated 25 Å below Σ11 symmetric tilt GB in Cu at 300 K
- Atoms colored by energy
- After cascade, a number of vacancies remain below the GB, all interstitials absorbed by GB





Bai, et. al., Science 327, 1631 (2010)

UNCLASSIFIED



Grain boundaries in Cu: **Damage production**

- Snapshots of a 4 keV cascade initiated 25 Å below Σ11 symmetric tilt GB in Cu at 300 K
- Atoms colored by energy
- After cascade, a number of vacancies remain below the GB, all interstitials absorbed by GB
- More vacancies than if GB not there!



UNCLASSIFIE

PKA

20

-20 0 X (A)

А

50

ž.

-50



Grain boundaries in Cu: Snapshots of TAD simulation

- Interstitial emission leads to annihilation of 5 bulk vacancies
- Interstitial emission barriers (0.1-0.2 eV) relatively small compared to bulk vacancy barrier (0.67 eV)
- Interstitial emission extends ~5 atomic spacings into bulk
- Vacancies can diffuse to boundary on longer time scale







Summary - Temperature Accelerated Dynamics

Potentially most powerful AMD method

- Extremely large boosts when temperature is small compared to barriers
- Basic algorithm is easy to implement requirements:
 - transition detection
 - Basin constrained MD
 - Saddle finding method



UNCLASSIFIED



Limitations - Temperature Accelerated Dynamics

- Least exact of the accelerated MD methods
 - Assumes *harmonic* transition state theory
- For full optimization, requires many bells and whistles
 - Detect revisited states
 - Ensure events do not involve double jumps, etc
- Requires the potential to be relatively smooth for efficient saddle point calculations



UNCLASSIFIED



AMD characteristics/challenges

- All three methods can give very large boost factors when events are very infrequent.
- Basically, the MD time to next event (+overhead) is collapsed to ~ps time scale.



- Low barriers mean low boost.
- Systems with persistent low barriers are our biggest ongoing challenge
 - e.g., soft-matter systems
- In principle, electronic structure forces can be used, but they are still pretty expensive
 - If we cannot reach ~10 ps, we cannot see any events
- Larger systems are also harder, although we are making progress
 - ParTAD (Shim, et. al. 2007)
 - TAD-KMC (Chatterjee and Voter, 2010),
 - Local hyperdynamics (Kim, Perez, AFV, 2010).



AMD characteristics/challenges

- All three methods can give very large boost factors when events are very infrequent.
- Basically, the MD time to next event (+overhead) is collapsed to ~ps time scale.



- Low barriers mean low boost.
- Systems with persistent low barriers are our biggest ongoing challenge
 - e.g., soft-matter systems
- In principle, electronic structure forces can be used, but they are still pretty expensive
 - If we cannot reach ~10 ps, we cannot see any events
- Larger systems are also harder, although we are making progress
 - ParTAD (Shim, et. al. 2007)
 - TAD-KMC (Chatterjee and Voter, 2010),
 - Local hyperdynamics (Kim, Perez, AFV, 2010).



Comparing AMD Methods: Accuracy

Parallel-Replica is most accurate

- Only assumes first order kinetics
 - Doesn't even assume TST
- Accounts for correlated events

Temperature Accelerated Dynamics least accurate

- Assumes harmonic approximation to TST
- Has known upper bound to error quantified by δ and ν_{min}

Hyperdynamics is intermediate

- Assumes TST
 - no harmonic approximation...
 - ...but no correlated events
- Error may creep in via definition of bias potential



UNCLASSIFIED





Comparing AMD Methods: Efficiency

- Temperature Accelerated Dynamics possibly most efficient
 - Large boost when barriers are high relative to T_{low}
- Efficiency of hyperdynamics really depends on bias potential
 - With Art's bias potential, computational cost is very high
 - Bond-boost bias overcomes costs

Currently, parallel-replica least efficient

- Only linear boost with number of processors
- Right now, typically don't have enough processors to compete with TAD or hyperdynamics
- In future, this limitation should be reduced
- Harder to tune accelerating parameter
 - TAD: high temperature
 - Hyperdynamics: bias potential strength
 - Parallel-replica: number of processors

All limited by smallest barrier/fastest event in system



UNCLASSIFIED


Summary

- Accelerated molecular dynamics concept:
 - Let the trajectory find an appropriate way out of state, but coax it into doing so more quickly
- Significant speedup over standard MD when barriers are high relative to temperature

Often encounter unexpected behavior

- Many mechanisms that would be left out of e.g. KMC if intuition alone is used
 - High mobility of interstitial clusters in MgO
 - Transformation of void to stacking fault tetrahedron in Cu
 - Interstitial emission near GBs in Cu
 - Thinning of Ag nanowires

Ongoing challenges

- low barriers and pesky local minima
- cuspy potentials
- scaling with system size

Review: Voter, Montalenti, and Germann, *Ann. Rev. Mater. Res.* **32**, 321 (2002)



UNCLASSIFIED

Operated by Los Alamos National Security, LLC for the U.S. Department of Energy's NNSA



Acknowledgements

• Art Voter (LANL)

Radiation damage evolution in ceramics:

- Kurt Sickafus (LANL)
- Robin Grimes, Antony Cleave, and Jon Ball (Imperial)
- Roger Smith and Pravesh Bacorisen (Loughborough)
- Francesco Montalenti (now at University of Milano)
- Graeme Henkelman (now at University of Texas, Austin)

• Void evolution in metals:

- Steve Valone, Richard Hoagland (LANL)
- Interstitial Emission at GBs:
 - Xian-Ming Bai, Richard Hoagland, Mike Nastasi (LANL)
- Stretching Ag nanowire:
 - Danny Perez, Chun-Wei Pao, Sriram Swaminarayan (LANL)
- Funding: BES, Enhanced Surveillance, Motorola, LANL LDRD



UNCLASSIFIED

Operated by Los Alamos National Security, LLC for the U.S. Department of Energy's NNSA



Fine Scale Characterization and Some New Insights into the Precipitation of the Ordered γ' Phase in Nickel base Superalloys

Gopal Babu Viswanathan

Air Force Research Laboratory Dayton, Ohio, U.S.A.



Partners in the Crime also called '*Collaborators*'

A. Singh, J.Y. Hwang, S. Nag, R. Banerjee Center for Advanced Research and Technology Department of Materials Science and Engineering University of North Texas Denton, Texas, U.S.A.



S. Rajagopalan and H. L. Fraser Center for the Accelerated Maturation of Materials Department of Materials Science and Engineering Ohio State University Columbus, Ohio, U.S.A.



CAMM

J. Tiley and D. Dimiduk Air Force Research Laboratory Dayton, Ohio, U.S.A. Financial support for this work has been provided by the Air Force Office of Scientific Research and the Air Force Research Laboratory





Variations in grain size, γ ' size, distribution and volume fraction

Organization

- γ' precipitation during continuous cooling from single γ phase field
 - Rapid cooling (Water Quenched)
 - Slow cooling
- Evolution of the γ/γ' interface
 - Compositional gradient (or width) across the interface
 - Order-disorder transition width
- Application to real multi-component engineering alloys => study on Rene88 alloy (turbine disk alloy)
 - 56.53Ni-16.24Cr-13.27Co-3.92Ti-2.09Al-4.08Mo-3.92W-0.76Nb (wt%)
 - Primary alloying elements are Cr, Co, Ti, Al, Mo

Organization

- γ' precipitation during continuous cooling from single γ phase field
 - Water-quenched (rapid cooling)
 - Slow cooling
- Evolution of the γ/γ ' interface
 - Compositional gradient (or width) across the interface
 - Order-disorder transition width
- Application to real multi-component engineering alloys => study on Rene88 alloy (turbine disk alloy)
 - 56.53Ni-16.24Cr-13.27Co-3.92Ti-2.09Al-4.08Mo-3.92W-0.76Nb (wt%)
 - Primary alloying elements are Cr, Co, Ti, Al, Mo

Continuous Cooling Experiments + Aging



Post continuous cooling, samples aged at 760°C for various time periods from 0 - 200 hrs

Typical γ+γ' Microstructures in Rene 88

Water-Quenched

As-cooled



Slow-Cooled



Cr-M edge Energy-filtered TEM (EFTEM) images Cr-depleted darker contrast regions – γ' precipitates

760°C Aged / 200 hours



Monomodal size distribution of γ' precipitates

Bimodal size distribution of γ' precipitates Tiley, Viswanathan, Srinivasan, Banerjee, Dimiduk and, Fraser, *Acta Mater.* (2009)





- Near-spherical primary γ' precipitates are formed on quenching (verified in 3D)
 - Monomodal microstructure
- Al, Ti partition to γ'
- •Cr, Co, Mo partition to γ

Hwang, Banerjee, Tiley, Srinivasan, Viswanathan, and, Fraser, Metall. Mater. Trans. A (2009)

γ and γ' composition in Water-quenched Rene 88

	<u>WQ0</u>				← → >5 nm size → ← ~3 nm size →								
	Bulk		γ	γ' (avg)		γ'1		γ'2		γ'3		γ'4	
	Atomic%	Error%	Atomic%	Atomic%		Atomic%	Error%	Atomic%	Error%	Atomic%	Error%	Atomic%	Error%
Ni	48.96	0.05	46.10	58.07	Ni	59.62	0.65	59.34	0.72	57.10	1.67	51.00	1.92
Co	12.89	0.02	14.30	8.83	Co	7.69	0.19	7.45	0.21	10.90	1.05	13.80	1.33
Ti	4.69	0.01	2.50	10.67	Ti	10.85	0.23	10.90	0.26	10.14	1.02	13.10	1.30
Cr	18.92	0.03	23.50	4.68	Cr	4.21	0.14	4.06	0.15	5.50	0.77	6.20	0.93
ΑΙ	6.13	0.02	4.20	10.49	AI	10.55	0.23	11.06	0.26	8.30	0.93	9.70	1.14
Nb	2.32	0.01	2.30	2.97	Nb	2.72	0.11	2.86	0.13	2.10	0.48	7.00	0.98
Мо	4.24	0.01	4.80	3.29	Мо	2.86	0.11	2.88	0.13	3.60	0.63	4.10	0.76
С	0.09	0.00	0.10	0.07	С	0.04	0.01	0.07	0.02	0.20	0.15	0.00	0.00
W	1.61	0.01	2.00	1.26	W	1.32	0.08	1.25	0.08	1.90	0.46	1.40	0.45
В	0.15	0.00	0.20	0.14	В	0.13	0.02	0.12	0.03	0.00	0.00	0.00	0.00

- Compositional partitioning between γ matrix and γ' precipitates
 - -γ matrix richer in Co, Cr, Mo
 - -γ' precipitates richer in Al, Ti
- Size dependent compositional variation in γ' precipitates
 - smaller precipitates are further from equilibrium contain excess of Co but depleted in Al content



Different Generations of \gamma' (**Primary**)

SEM secondary electron images (etched sample)







- Coarse non-spherical primary γ' precipitates
- 2D measurement of areas from SEM images converted to equivalent diameter
- Size distribution plot of primary γ' precipitates

Different Generations of y' (Secondary)





- Near-spherical secondary γ' precipitates
- 2D measurement of areas from EFTEM images converted to equivalent diameter
- Size distribution plot of secondary γ' precipitates

Different Generations of γ **' (Tertiary)**





- Nanometer scale tertiary γ ' precipitates
- 3D measurement of volumes from atom probe tomography equivalent diameter
- Size distribution plot of secondary γ' precipitates

Three Different Generations of y'



• Unique coupling of characterization techniques to identify three different generations of gamma prime precipitates and their relative size distributions

• Forming from 3 distinct nucleation bursts

Cr-M edge EFTEM images





3D atom probe tomography: Cr=14at% isosurface



- Presence of depletion zones between the primary and secondary γ' precipitates
 - Primary γ': Coarser, non-spherical
 - Secondary γ': much finer, near-spherical

	Primary γ'(avg)	Secondary (1)γ'	Secondary (2)γ'		
	Atomic %	Atomic %	Atomic %		
Со	6.70	8.70	10.99		
Ti	9.17	7.14	6.43		
Cr	1.77	8.23	11.53		
Мо	2.84	5.12	4.02		

- Compositional differences between primary and secondary γ' precipitates
 - secondary γ' precipitates
 - richer in Co, Cr, Mo
 - depleted in Ti

51

- further from equilibrium
- primary γ' precipitates
 - closer to equilibrium composition





SC0	γ near primary γ'	γ far from primary γ	γ near secondary γ'
	Atomic %	Atomic %	Atomic %
Со	18.63	13.71	15.38
Ti	0.68	1.21	2.68
Al	1.97	1.67	3.76

• Compositional differences between γ matrix near primary γ' precipitates vs. near secondary γ' preciptates

- γ away from the primary γ ' precipitates, near secondary γ ' precipitates:
 - depleted in Co
 - enriched in in Al, Ti
 - further from equilibrium driving force for secondary γ ' nucleation





Slow-Cooled + 760°C/50hrs aged sample

51

Cr-M edge EFTEM images

9



Secondary y'

50 nm

	Primary γ'(avg) Secondary (1)γ' Secondary (2)γ'					
	Atomic %	Atomic %	Atomic %			
Со	6.52	7.20	6.13			
Ti	9.22	8.31	9.73			
Cr	1.71	3.32	1.95			
Мо	2.96	1.94	2.10			

Lesser compositional variation between the primary and secondary γ' precipitates – composition of both types of precipitates approaching equilibrium

Slow-Cooled + 760°C/50hrs aged sample





Reduced pile-up of Co and Cr in the γ matrix near the primary γ' precipitates - Long range composition equilibration in γ matrix due to aging

Organization

- γ' precipitation during continuous cooling from single γ phase field
 - Water-quenched (rapid cooling)
 - Slow cooling
- Evolution of the γ/γ' interface
 - Compositional gradient (or width) across the interface
 - Order-disorder transition width
- Application to real multi-component engineering alloys => study on Rene88 alloy (turbine disk alloy)
 - 56.53Ni-16.24Cr-13.27Co-3.92Ti-2.09Al-4.08Mo-3.92W-0.76Nb (wt%)
 - Primary alloying elements are Cr, Co, Ti, Al, Mo



Structural Transition Across γ/γ' Interface

HAADF-HRSTEM image of interface recorded in a C_s corrected TITAN



- Interface does not appear to be abrupt, shows transition width
- γ' region exhibits darker contrast as compared with the γ region γ contains heavier alloying elements (e.g. Cr, Co) *higher intensity Z contrast in HAADF-STEM*



Two distinct interface widths

Avg. width of order-disorder transition (d1): 6-8 (002) planes ($\sim 1.2 \text{ nm}$) Avg. width of compositional gradient (d1+d2): 12-14 (002) planes ($\sim 2.2 \text{ nm}$)

Need to validate with independent measurements (3D atom probe)

Srinivasan, Viswanathan, Banerjee, et. al., Phys Rev. Lett. (2009)

3DAP Investigations of Compositional Transition Across Interface Со **2.0 nm** Ti 30 3 Cr Al 25 Mo 8 Composition (at%) 20 \$ 15 2 -2 3 -1 -3 **Distance** (nm)

- Compositional profiles across γ/γ' interface Proximity Histogram (proxigram) analysis used
- Compositional transition across interface occurs over $\sim 2~nm$
 - Non-abrupt compositional interface
- 3DAP results in good agreement with HRSTEM results

Srinivasan, Banerjee, Viswanathan, Tiley and Fraser ., Phys Rev. Lett. (2009)

Atomistic Simulations of γ/γ' Interface Structure



Y.Mishin, *Acta Materialia*, 52 (2004), 1451 *Order-disorder transition* ~ 6-8 *planes* Monte Carlo simulations of γ/γ ' interface structure in binary Ni-Al system



A.J. Ardell, V. Ozolins, *Nature Materials*, 4 (2005) 309 *Order-disorder transition* ~ 10 planes

- Atomistic simulations predict "ragged", non-abrupt interface structure
- Observed experimental results in very good agreement with atomistic simulations partially ordered γ/γ' interface of finite width - slows down diffusivity?

Organization

- γ' precipitation during continuous cooling from single γ phase field
 - Water-quenched (rapid cooling)
 - Slow cooling
- Evolution of the γ/γ ' interface
 - Compositional gradient (or width) across the interface
 - Order-disorder transition width
- Application to real multi-component engineering alloys => study on Rene88 alloy (turbine disk alloy)
 - 56.53Ni-16.24Cr-13.27Co-3.92Ti-2.09Al-4.08Mo-3.92W-0.76Nb (wt%)
 - Primary alloying elements are Cr, Co, Ti, Al, Mo



Experimental coarsening behavior



Aging time (Hours)

- Coarsening kinetics investigated as f (cooling rate)
- Aging treatment: 760°C for 25,50,100 and 200 hours
- Distinction made between growth and pure coarsening (>25 h aging)

Coarsening kinetics - LSW Model

Classical LSW Model (r³-r_o³=kt)



Experimental rate constants $k_{WQ} = 0.0157 \text{ nm}^3 \text{s}^{-1}$ $k_{FC} = 0.0049 \text{ nm}^3 \text{s}^{-1}$ $k_{SC} = 0.0057 \text{ nm}^3 \text{s}^{-1}$

Key Assumptions

- Pure coarsening regime
- · Constant volume fraction of γ'
- Equilibrium matrix composition

Modeling of Coarsening Kinetics - LSW Model

Coarsening rate constant, $k = \frac{A D C_e Y_i V_m}{RT} .10^{27}$ D is the diffusion coefficient of solute in the matrix (m²s⁻¹) C_e is the atomic fraction of solute in equilibrium with the precipitate γ_i is the precipitate/matrix interface energy, V_m is the molar volume of the precipitate (m³ mol⁻¹), R is the universal gas constant (J mole⁻¹-K⁻¹) T is the absolute temperature (K).

Substituting experimental values for D, C_e and γ_i the analytically derived coarsening rate constants for primary γ' in WQ sample

k = 0.002 nm³s⁻¹ (using D_{AI}) Good Experiment k = 0.005 nm³s⁻¹ (using D_{Cr}) Agreement k = 0.0157 nm³s⁻¹

Coarsening Kinetics - TIDC Model

Trans-Interface Diffusion Controlled $(r^2 - r_0^2 = \mathbf{k}t) - (Ardell and Ozolins, 2005)$



Experimental rate constants

k	WQ	=	0.0006	nm ² s ⁻¹
k	FC	=	0.0003	nm^2s^{-1}
k	SC	=	0.0003	nm ² s ⁻¹

Key Assumptions

- Independent of volume fraction
- Diffusion across interface is rate limiting
- Existence of a non-abrupt, ragged interface

Modeling of Coarsening Kinetics - TIDC Model

Coarsening rate constant
$$k^{i} = \frac{32D_{i} l_{\gamma}}{81\Delta X_{e}\delta} 10^{18}$$

 D_i is the trans interface diffusion coefficient (m²s⁻¹)

- I_{γ} is capillary length ΔX_e is the difference in the equilibrium solute concentration between γ and γ'
- δ is width of the interface

Obtained via 3DAP studies

Substituting experimental values for k^i , ΔX_e and δ the analytically calculated "effective" interface diffusivity in WQ sample is

 $D_i \sim 4.33 \times 10^{-19} \text{ m}^2 \text{s}^{-1}$

(between the diffusivity values for Al in Ni and Ni_3Al)
Summary

- Nucleation during continuous cooling from above the solutionizing temperature:
 - Long range equilibration of γ composition fields away from growing γ' precipitates plays a significant role
 - > Fast cooling rate results in monomodal distribution of γ ' precipitates
 - > Slower cooling rates result in bimodal or multi-modal γ ' precipitates
- Multiple nucleation bursts are different undercoolings clearly identified by coupling SEM, EFTEM, and 3DAP
- HRSTEM and 3DAP investigations clearly reveal two distinct transition widths associated with the γ/γ ' interface

> order-disorder transition width

> compositional gradient width

Effect of Coherency and Local Stress on Nucleation

R. Shi, N. Zhou, C. Shen* and Yunzhi Wang

Department of Materials Science and Engineering The Ohio State University *GE Global Research Center

Acknowledgement

ONR and NSF

Joint AFRL/AOARD/LLNL Workshop on Nucleation during Solid-Solid Phase Transformations Maui, Hawaii, May 2-7, 2010



Department of Materials Science and Engineering









Courtesy of J.F. Nie)

Department of Materials Science and Engineering

Nucleation in solids is the toughest nut to crack! K.C. Russell

Challenges:

- Coherency state and defect structure at interfaces/Interfacial energy anisotropy
- Orientation relationship and lattice correspondence
- Concentration non-uniformity in an embryo

Usefulness and limitations of the phase field approaches:

Langevin dynamics is qualitative in nature



VladKolarov.com

- Interaction energy calculation is at most semi-quantitative
- Phase field total energy functional + Nudged Elastic Band (NEB) quantitative but energetic only, feeding to explicit algorithm based on classical nucleation theory for kinetics

What we could do using phase field method to study nucleation

- I. Quantitative calculation of activation energy and critical nucleus configuration
- II. Qualitative understanding of autocatalytic effect and collective nucleation
- III. Semi-quantitative study of effects of local stress and pre-existing microstructure on nucleation



Phase Field Modeling of Nucleation



Reprinted from THE JOURNAL OF CHEMICAL PHYSICS, Vol. 28, No. 2, 258-267, February, 1958 Printed in U. S. A.

Free Energy of a Nonuniform System. I. Interfacial Free Energy

JOHN W. CAHN AND JOHN E. HILLIARD General Electric Research Laboratory, Schenectady, New York (Received July 29, 1957)

Reprinted from the JOURNAL OF CHEMICAL PHYSICS, Vol. 31, No. 3, 688-699, September, 1959 Printed in U. S. A.

Free Energy of a Nonuniform System. III. Nucleation in a Two-Component Incompressible Fluid

JOHN W. CAHN AND JOHN E. HILLIARD General Electric Research Laboratory, Schenectady, New York (Received February 16, 1959)

Comment by Mullins: The fundamental properties associated with an interface and a critical nucleus are expressed in terms of the parameters in the free energy model and there is no need to introduce the artificial dividing surface of Gibbs, nor to define a separate interfacial energy, nor to model the nucleus as homogeneous



Phase field description of defects

Order parameter $\phi(\mathbf{r})$

Chemical non-uniformity: $c(\mathbf{r}), \rho(\mathbf{r}), V_m(\mathbf{r}), ...$ Structural non-uniformity: $\eta(\mathbf{r}), \mathbf{u}(\mathbf{r}), \boldsymbol{\varepsilon}(\mathbf{r}), \mathbf{M}(\mathbf{r}),$

Total energy

Chemical or inelastic energy:

$$F^{ch} = \int [f(\phi(\mathbf{r})) + \kappa |\nabla \phi(\mathbf{r})|^2] d\mathbf{r}$$

Elastic energy: $\varepsilon_{ij}^{T}(\mathbf{r}) = \sum \varepsilon_{ij}^{T}(\phi_{p}(\mathbf{r}))$

$$E^{el} = \frac{1}{2} \sum_{pq} \int \frac{d^{3}k}{\left(2\pi\right)^{3}} \begin{bmatrix} C_{ijkl} \varepsilon_{ij}^{00}\left(p\right) \varepsilon_{kl}^{00}\left(q\right) \\ -n_{i} \sigma_{ij}^{00}\left(p\right) \Omega_{jk}\left(\mathbf{n}\right) \sigma_{kl}^{00}\left(q\right) n_{l} \end{bmatrix} \left\{ \phi_{p}^{m}\left(\mathbf{r}\right) \right\}_{k} \left\{ \phi_{q}^{m}\left(\mathbf{r}\right) \right\}_{k} \left\{ \phi_{q}^$$

Kinetics

Phase field approach is a superset of the Cahn-Hilliard description of chemical inhomogeneities and the Peierls description of displacive inhomogeneities.

Wang an Li, Acta Mater, Overview 150, 2010

Examples:

Martensitic transformation or

dislocation, order parameter

= inelastic displacement (or

strain) $\mathbf{u}(\mathbf{r})$ or $\boldsymbol{\varepsilon}(\mathbf{r})$

Defect cores are diffuse at their natural length scales



60 EAM simulation



Layer sumber

Monte Carlo simulation

A.J. Ardell, V. Ozolins, *Nature Materials*, 4 (2005) 309 *Order-disorder transition* ~ 10 planes

Department of Materials Science and Engineering

Interface width - atom probe data Results indicate a wider γ/γ' interface for the tertiary γ ' than for the larger secondary γ ' P. Sarosi (OSU) 80 80 cNi cCr cTi 70 70 δ 60 60 ο 50 50 Concentration (at.%) Concentration (at.%) ο 0 40 40 30 30 <u>_____</u>_________________ 20 20 10 10 ۵ nn 0 \u03cm \u0 0

Compositional profile of tertiary γ' (from 30 precipitates)

0

5

-5

Distance [nm]

-10

-15



Compositional profile across a secondary γ ' and matrix interface

Example I. Quantitative Calculations

- Works at natural length scales of extended defects (~nm)
- Using DFT calculations of GSF/MGSF and Landau free energy as direct inputs and predict defect structure, chemistry and energy
- Probe the total energy landscape using NEB for saddle point configuration and activation energy of defect nucleation
- When combined with experimental characterization, it could serve as a powerful tool to explore **deformation/transformation mechanisms** and provide critical inputs to coarse-grained phase field simulations



Energy landscape calculation by *ab initio*



GSF energy for dislocation core structure/energy, peierls stress, nucleation barrier **MGSF** energy for twin nucleation and growth



Landau free energy for martensitic transformation -"MGSF" energy for martensite nucleation and growth

Incorporation of activation energy into explicit nucleation algorithm in phase field



JP.Simmons et. al, *Scripta mater*. 2000; YH. W Acta Mater. 2006 Example II. Langevin dynamics Autocatalytic effect and collective nucleation • Cubic to tetragonal transformation in 2D: - autocatalytic effect

- Cubic to tetragonal transformation in 3D:
 collective nucleation
 - autocatalytic effect



В

malli

Quantitative Calculation





Critical nucleus from Nudged Elastic Band (NEB) calculation



Near critical nucleus from Langevin dynamics



Super critical nucleus from Langevin dynamics



Grownup configuration from Langevin dynamics



Formation of intersecting plates in Ti-64 Autocatalytic effect









Contribution from elastic interaction



t=2.5s (right before the two plates touch each other)

Typical chemical driving force for nucleation: 4.32×10⁷J/m³, which is comparable to elastic interaction energy



$$\begin{split} \Delta \Omega &= -V_0 \Delta f^{\text{ch}} + A_0 \gamma + \Delta E^{\text{el}} \\ \Delta E^{\text{el}} &= E^{\text{el},2} - E^{\text{el},1} \\ \Delta E^{\text{el}} &= \Delta E^{\text{el}}_{\text{int}} + \Delta E^{\text{el}}_{\text{self}} \\ \Delta E^{\text{el}}_{\text{int}} &= \sum_{p=1}^{N} \sum_{q=1}^{M} \int \frac{\mathrm{d}\mathbf{g}}{(2\pi)^3} B'_{pq}(\mathbf{n}) \tilde{\phi}_p(\mathbf{g}) \Delta \tilde{\phi}_q^*(\mathbf{g}) \\ \Delta E^{\text{el}}_{\text{self}} &= \frac{1}{2} \sum_{p=1}^{M} \sum_{q=1}^{M} \int \frac{\mathrm{d}\mathbf{g}}{(2\pi)^3} B'_{pq}(\mathbf{n}) \Delta \tilde{\phi}_p(\mathbf{g}) \Delta \tilde{\phi}_q^*(\mathbf{g}) \end{split}$$

Shen, Simmons and Wang, Acta Mater (2006), ibid, (2007).

Example III. Semi-quantitative calculations a) Variant Selection: motivation



Fatigue crack growth in OIM image α/β forged Ti-6242 alloy in compressor rotor JC. Williams and S. Ghosh (OSU)







- Interaction of local stress with elastically anisotropic polycrystalline microstructure
- Interaction of local stress with precipitation of coherent/semi-coherent α-phase particles

Interaction of local stress with evolving microstructures



{111}<110> y-fiber Texture







Applied stress: 98 MPa tensile along ND



Max (Red) 28.0 MPa Min (Blue) -35.4 MPa



Max (Red) 28.3 MPa Min (Blue) -35.1 MPa

Stress distribution in the polycrystalline sample under 98 MPa tension along ND.





Max (Red) 132.0 MPa Min (Blue) 62.6 MPa



Max (Red) 29.0 MPa Min (Blue) -34.8 MPa







Max (Red) 38.4 MPa Min (Blue) -29.6 MPa

Department of Materials Science and Engineering

BCC \rightarrow HCP Transformation Mechanism



Interface Dislocation Structure



SFTS Calculation of Semi-coherent & Lath

1. dislocation-free (coherent)



2. Displacement due to c-dislocations

$$F^{c} = \frac{-1}{30} \begin{pmatrix} 0 & & \\ & 0 & \\ & & 1 \end{pmatrix} + I = \begin{pmatrix} 1 & & \\ & 1 & \\ & & 0.9655 \end{pmatrix}$$

3. Shear accommodation due to a-dislocations

$$F^{a} = R \begin{pmatrix} 1 & -0.119 \\ 1 & \\ & 1 \end{pmatrix} R^{T} = \begin{pmatrix} 1.078 & -0.055 \\ 0.11 & 0.922 \\ & & 1 \end{pmatrix}$$

4. Contribution due to [100] dislocation

F



5. Effective (semi-coherent) SFTS

$$F_{T} = F^{100}F^{a}F^{c}F^{0} \qquad \varepsilon = \frac{1}{2}(F_{t}F_{t}^{T} - I) = \begin{pmatrix} -0.049 & 0.023 \\ 0.023 & 0.035 \\ 0.023 & 0.035 \end{pmatrix}$$

Department of Materials Science and Engineering



8

19

23

9

Grain ID						27
Variants	27	8	23	19	9	6
1	2.71259	0.89903	2.02104	2.08184	1.48684	1.01869
2	1.87571	0.88838	0.68961	1.37163	0.86486	0.37968
3	-0.64215	-0.06734	0.48023	-0.40484	0.17415	-0.02657
4	2.90566	3.41058	4.01198	2.98381	3.2216	3.3507
5	-4.49931	-4.37091	-4.31057	-4.33573	-4.6636	-4.19092
6	-1.11021	-1.08432	-0.90188	-1.10179	-1.75509	-0.9656
7	-0.66386	-2.39349	-1.35711	-1.14161	-1.41214	-2.19502
8	-1.03616	-2.62202	-1.56813	-1.46694	-1.68414	-2.40823
9	-0.98321	-0.28969	0.30907	-0.70342	-0.07474	-0.21775
10	2.10003	3.40611	2.72041	2.30036	2.62273	2.73372
11	-1.9285	-1.08286	-2.22398	-1.79573	-2.3635	-1.5942
12	-4.8277	-4.5992	-4.4512	-4.62381	-4.90296	-4.3705

Variant 5 and 12 are strongly favored by the applied stress Variant 4 and 10 are strongly un-favored by the applied stress

Department of Materials Science and Engineering



Ti-6Al-4V system: temperature=1073K, system size= $6.4 \mu m^3$, interfacial energy anisotropy = 3:2:1 (edge:side:broad) with interfacial energy of edge face = $500 mJ/m^2$, total simulation time = 2.5s, volume fraction of α -phase = 0.4 and the equilibrium volume fraction is 0.86.



Variant Distribution



(a) Time evolution of different orientation variants during $\beta \rightarrow \alpha$ transformation in Grain #8 (indicated in (b)). (c) Volume fraction of different variants at t = 2s.



Example III. Semi-quantitative calculations b) nucleation at GB: motivation





Fig. 1. An OIM Inverse pole figure map Department of Materials Science and Bigineering grains with grain boundary a and a gidanlatag

Heterogeneous nucleation at grain boundary





Phase field approach could be applied at several levels to develop fundamental understanding of nucleation behavior during solid state processes:

- At a **qualitative** level the Langevin dynamics could be applied to study effect of arbitrary chemical and structural non-uniformity in existing microstructure on nucleation. The examples given showed stress-induced collective and correlated nucleation, as well as autocatalytic effect. In particular, spatial distribution of different variants of the α phase was shown to correlate strongly with stress distribution in a polycrystalline sample. Under certain conditions, certain α variants may percolate through the entire sample.
- At a **semi-quantitative level**, the interaction energy calculation allows for systematic investigation of effect of stress fields associated with arbitrary existing microstructure on nucleation
- At a quantitative level the microscopic phase field model (in combination with NEB technique) could be applied to characterize activation energy and critical nucleus configuration. But this is energetic only. Need to put the activation energy into the framework of classical nucleation theory to predict nucleation (see next page for details)



Early Nucleation – Lessons Learned from the World of Semiconductors



50 nm

Si

Wolfgang Windl The Ohio State University Columbus, OH, USA



Computational Materials Science and Engineering

Semiconductor Devices – MOSFET

Metal Oxide Semiconductor Field Effect Transistor





Doping: N: e⁻, e.g. As P: holes, e.g. B (Donor) (Acceptor)





- Analog: Amplification
- Digital: Logic gates



Computational Materials Science and Engineering



Displacement Damage: Ion Implantation and Annealing



- Dopants inserted by ion implantation \Rightarrow damage
- Damage healed by annealing
- During annealing, dopants diffuse fast (assisted by defects)
 - \Rightarrow important to optimize anneal



* K. Beardmore, S. Srinivasan Computational Materials Science and Engineering





OHIO STATE

Computational Materials Science and Engineering
Example: Boron TED & Deactivation in Si

What you expect: Intrinsic diffusion $\frac{dC_B}{dt} = \nabla (D_B \nabla C_B)$

What you get:

•fast diffusion (TED)*

•immobile peak

•segregation & interface pileup

*W. Windl et al., PRL (99).





Bridging the Length Scales: Ab-Initio to Continuum

Point Defect Diffusion:

$$\frac{dC_I}{dt} = \nabla \left(D_I \nabla C_I \right)$$
$$D_I = D_I^0 \exp \left(-\frac{E_a}{k} \right)$$

Need to know: • Diffusion prefactors

- - [Uberuaga et al., PSS (02),

Stoddard et al., PRL (05)]

Migration barriers

[Windl et al., PRL (99)]



Computational Materials Science and Engineering



Bridging the Length Scales: Ab-Initio to Continuum

Impurity Diffusion:



$$\frac{dC_{\rm B}}{dt} = \nabla \left(D_{\rm B}^{\rm eff} \nabla C_{\rm B} \right)$$
$$D_{\rm B}^{\rm eff} \sim D_{\rm B}^{0} \exp \left(-\frac{E_{\rm form}^{I} - E_{\rm bind}^{BI} + E_{\rm mig}^{BI}}{k_{B}T} \right)$$

Need to know: • Effective macro-D [Daw, Windl, PRB (01)]
 • Binding free energies [previous papers]

• Previous quantities

W. Windl et al, PRL (99). Computational Materials Science and Engineering





Bridging the Length Scales: Ab-Initio to Continuum



Need to know: • Binding energies

• Capture radii

[Liu *et al*., APL (00)]

[Beardmore et al., Proc. ICCN (02)]



Computational Materials Science and Engineering



- classically exact rate if no recrossings or correlated events
- no dynamics required

Laidler, JPC (89).

- excellent approximation for materials diffusion
- can also exploit TST formalism to develop methods that do not require knowing in advance where the dividing surface is

ational Materials Science and Engineering

THE E



How To Find Saddle Points

"Drag method": Guess final state & diffusion path (reaction coord.)



Reliable search for diffusion path: "Nudged elastic band method (Jónsson *et al*.).



Final state unknown \Rightarrow Dimer method, (accelerated) MD







Prefactor

• **Necessary:** vibrational frequencies at minimum & saddle point (harmonic TST, Vineyard (1957))

$$D = \frac{p \cdot d^2}{12} \upsilon \exp\left(-\frac{\Delta S}{k_B}\right) \exp\left(-\frac{\Delta E}{k_B T}\right)$$

$$U = \frac{\prod_{j=1}^{N} \upsilon_j^A}{\prod_{j=1}^{N-1} \upsilon_j^S}$$

$$S = k_B \sum_{i=1}^{3N} \left\{\frac{\hbar \upsilon_i}{2k_B T} \coth\left(\frac{\hbar \upsilon_i}{2k_B T}\right) - \ln\left[2\sinh\left(\frac{\hbar \upsilon_i}{2k_B T}\right)\right]\right\}$$

Uberuaga et al. PSS (02), Stoddard et al, PRL (05).

Materials Science and Engineering



Si Self Diffusion - Experiment



Computational Materials Science and Engineering



Vacancy Interstitial
upper limit
(tracer)

$$D_T = 437 \exp\left(-\frac{3.9 \text{ eV}}{k_BT}\right) \frac{\text{cm}^2}{\text{s}}$$
 $D_T = 52 \exp\left(-\frac{4.0 \text{ eV}}{k_BT}\right) \frac{\text{cm}^2}{\text{s}}$

Theor: Uberuaga et al., Phys. Stat. Sol. B **233**, 24 (2002).

Materials Science and Engineering



Nitrogen Pair Diffusion: Comparison



W. Windl, ECS Trans. 13 (2008). Computational Materials Science and Engineering





Computational Materials Science and Engineering





Sub-Microscopic Boron Clusters

Experimental situation:

- Structures too small to be seen in EM
 - \Rightarrow only "few" atoms
 - New phase wants to nucleate, but decays quickly
- Clustering dependent on B concentration and interstitial concentration
 - \Rightarrow formation of B_mI_n clusters postulated; experimental estimate: $m / n \sim 1.5^*$

\Rightarrow Approach:

- Calculate clustering energies from first principles up to "max." m, n
- Build kinetic Monte Carlo / continuum model from it





X.-Y. Liu, W. Windl, and M. P. Masquelier, APL **77**, 2018 (2000).**Computational Materials Science and Engineering**





Activation and Clusters - GGA





Activation and Clusters - "



Expt: Mokhberi, Plummer Computational Materials Science and Engineering





Which Path Is Right?



B3I⁻ negatively charged, should insert hole concentration

Confirmed by Hall measurements





Summary

Semiconductors:

- Kinetic parameters from ab initio calculations today standard, including
 - charge effects
 - temperature effects (non-Arrhenius)
- Clustering/nucleation kinetics doable and helpful, demonstrated for
 - Pre-nucleation
 - Growth

Metals???



Computational Materials Science and Engineering



What Does It Take to Do Same Calculations for Metals?

- Start from different initial structure (e.g., fcc instead of diamond)
- Do not use pseudopotential file for silicon, but for metal
- Do same





Computational Materials Science and Engineering

Example: Superdiffusers



Explanation for superfast diffusion of Au in Pb: Interstitial mechanism





Ab-Initio Lessons from Semiconductors!?





Example: Ab-Initio Diffusion Coefficients – Semiconductors ~2000...

phys. st









Example: Ab-Initio Diffusion Coefficients – Metals ~2008...



Available online at www.sciencedirect.com



www.elsevier.com/locate/actamat

First principles impurity diffusion coefficients

M. Mantina^{a,*}, Y. Wang^a, L.Q. Chen^a, Z.K. Liu^a, C. Wolverton^b



Computational Materials Science and Engineering



Dose Loss from Arsenic Pile-Up – Can We See The Clusters?



Pei, Duscher, Steen, Pichler, Ryssel, Napolitani, De Salvador, Severac, Cristiano, Ravichandran, Gupta and Windl. **Steen**, Martinez-Limia, Pichler, Ryssel, Paul, Lerch, Pei, Duscher, Severac, Cristiano, and Windl. Both JAP 08.



SiAs: "Ugly" Precipitates – How Do They Fit and Grow?

- Monoclinic phase with incompatible lattice constants
- How does growth happen?



1414



*Fabio Iacona et. al, Physical Review B, Vol 58, 10990 (1998)

SiAs precipitate at Si/SiO₂ interface *



Final Summary

- Semicondutor research good guidance (e.g. irradiation to enhance supersaturation of solutes ("pre-amorphization implants")
- Diffusion and rate constants from DFT doable
- Reliance on "knowledge" of processes (reaction paths) dangerous – need good initial data and sensible modeling tasks
- Complimentary experiments necessary
- Modeling essential for full interpretation of experiments



Thermodynamic Modeling of Multi-component Systems and Its Integration with Kinetic Simulation

Fan Zhang, W. Cao, K. Wu, S. Chen, Y. Yang, and Y. A. Chang CompuTherm, LLC

> Present at Nucleation Workshop at Maui, Hawaii May 5, 2010

Outline

- Introduction to the CALPHAD Approach
- Integration of Thermodynamic Calculation with Kinetic Models for the Simulation of Nucleation, Growth and Coarsening
- Are Those Gibbs Energies Developed by the CALPHAD Approach Trustworthy?

Why CALPHAD Approach?



CALPHAD Approach



Three Binaries To Form A Ternary



$$G(x_A, x_B, x_C) = \frac{x_A \cdot x_B}{x_A^{AB} \cdot x_B^{AB}} G^{AB}(x_A^{AB}, x_B^{AB}) + \frac{x_B \cdot x_C}{x_B^{BC} \cdot x_C^{BC}} G^{BC}(x_B^{BC}, x_C^{BC}) + \frac{x_A \cdot x_C}{x_A^{AC} \cdot x_C^{AC}} G^{AC}(x_A^{AC}, x_C^{AC})$$

How to Construct A Multicomponent Database



Thermodynamic Databases of Multicomponent Systems



6

Outline

- Introduction to the CALPHAD Approach
- Integration of Thermodynamic Calculation with Kinetic Models for the Simulation of Nucleation, Growth and Coarsening
- Are Those Gibbs Energies Developed by the CALPHAD Approach Trustworthy?

Integration of Thermodynamic Calculation with Kinetic Simulation



Microstructure Modeling: Fast-acting Model

The Fast-acting Model:

- Concurrent nucleation, growth and coarsening
- Ø Evolution of average quantities:
 volume fraction, number density,
 particle size
- Average particle size change with time



Microstructure Modeling: the KWN Model

The KWN (Kampmann-Wagner Numerical) Model:

- Concurrent nucleation, growth and coarsening
- Ø Evolution of average quantities:
 volume fraction, number density,
 particle size
- Ø Evolution of PSD: Particle Size Distribution
- Ø Many size classes


Nucleation Rate

Classical nucleation theory:

$$J = N_{v} Z \beta^{*} e^{-\frac{\Delta G^{*}}{kT}} e^{\frac{-\tau}{t}}$$

- *Nv* : Number of nucleation sites per unit volume
- **Z** : Zeldovich factor accounting for decay of supercritical particles
- β * : Rate of solute atoms joining the critical nucleus
- au : Incubation time

 ΔG^* : Activation energy for nucleation

Growth Rate

Growth rate of multi-component alloys (small super-saturation)*

$$v = \frac{dR}{dt} = \frac{K}{R} \left(\frac{1}{R^*} - \frac{1}{R} \right)$$

 $\Delta Gm > 0, R < R^* \rightarrow Dissolution$ $\Delta Gm > 0, R > R^* \rightarrow Growth$

R: particle radius R*: critical nucleus radius

$$K = \frac{2\sigma V_m}{\left(\Delta C^{\alpha\beta}\right] \left[\mathbf{M}\right]^{-1} \left[\Delta C^{\alpha\beta}\right]}$$

kinetic parameter

 $(\Delta C^{\alpha \beta}]$: row vector of the solute concentration difference between α and β [$\Delta C^{\alpha \beta}$): column vector of the solute concentration difference between α and β [M] : chemical mobility matrix

* Morral, J.E. and Purdy, G.R., Scripta Metallurgica et Materialia, 1994. 30(7): p. 905-908

Coarsening Rate

Coarsening Rate of Multi-Component System

$$\overline{R}^3 - \overline{R}_0^3 = \frac{4}{9}Kt$$
 or $\frac{dR}{dt} = \frac{4}{27}\frac{Kt}{R^2}$

- R : average particle radius at time t
- $R_{\scriptscriptstyle
 m O}$: average particle radius at the onset of coarsening
- K : kinetic parameter



Microstructure evolution in Ni - 14 at.% Al alloy at 550 $^\circ\,$ C





Microstructure evolution in Ni - 14 at.% Al alloy at 550° C KWN - predictions & experiment



PanPrecipitation – Ni-5.2Al-14.2Cr at%



PanPrecipitation – Ni-5.2Al-14.2Cr at%



PanPrecipitation – Ni-5.2Al-14.2Cr at%



PanPrecipitation – Rene88DT

Predicted evolution of average size at different temperatures



Integration of Thermodynamic Calculation with Microstructural Evolution Models



Integration of Thermodynamic Calculation, Kinetic Simulation with Mechanical Property Models



Aging Hardening of AL Alloys



Age Hardening of an AA6005 Alloy

Comparison between measured and predicted response of an AA6005 Aluminum Alloy to artificial ageing at 185°C



Reheating of an AA6005 Alloy

Comparison between measured and predicted response of an AA6005 Aluminum Alloy to reheating at 350°C



AA6061: Response to Ageing and Reheating



Experiment:

Anderson, W.A., *Precipitation from Solid Solution*. 1959, Metals Park, OH: American Society for Metals.

Outline

- Introduction to the CALPHAD Approach
- Integration of Thermodynamic Calculation with Kinetic Models for the Simulation of Nucleation, Growth and Coarsening
- Are Those Gibbs Energies Developed by the CALPHAD Approach Trustworthy?

How to Construct A Multicomponent Database



A Complete Puzzle Picture



A Corner of a Puzzle Picture



Gibbs Energy-Outside the Stable Composition range



Ti-Al Phase Diagram

Gibbs Energy Curves at 1500K

Gibbs Energy-Outside the Stable Composition range

F. Zhang, S.-L. Chen, Y. A. Chang, W. A. Oates, *Intermetallics*, 9 (2001), 1079-1083.

Intrinsic Model Problems



W. A. Oates, F. Zhang, S-L. Chen, and Y. A. Chang, *Physical Review B*, 59(17) (1999), 11221-11225.
F. Zhang, Y. A. Chang, Y. Du, S.-L. Chen, and W. A. Oates *Acta. Materialia*, 51(1) (2003), 207-216.

Conclusions

- The CALPHAD approach has been applied to multi-component systems with some success
- Thermodynamic modeling can be integrated with kinetic models, microstructure models, mechanical property models for the simulation of materials properties
- Are there problems and concerns with the current CALPHAD approach? Yes
- Are there other better approaches for describing multicomponent systems at this moment? No
- What can we do? **Continue to improve this approach**

Acknowledgement

This work was financially supported by the USAF through SBIR, STTR and MAI projects

Thank You for Your Attention

