

**THESIS** 

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### **THESIS**

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#### Abstract

A scramjet consists of four main components: an inlet, an isolator, a combustor, and a nozzle. The isolator of the scramjet decelerates the incoming high Mach number flow to a lower Mach number and stabilizes the flow to a suitable condition before it enters the combustor. Because the combustion is not necessarily a steady phenomenon and may yield inconsistent heat release depending on the completeness of the combustion, pressures within the combustion zone can vary significantly. Variations in pressures caused by combustion can propagate forward and affect the flow field in the isolator and even create a large enough pressure blockage to un-start the inlet. Other factors that can influence the airflow in the isolator include changes in free stream conditions, vehicle geometry, and the vehicle's orientation with respect to the free stream velocity. As a result of these factors, the incoming flow to the inlet can change dramatically: as the airflow enters the isolator, a shock-train may develop upstream of the combustor. In this research, the shock-train location as affected by the back-pressure is examined experimentally. The back-pressure is artificially created by symmetric, top and bottom, ramps that can close the flow cross-sectional area in a controlled manner. Raising or lowering these ramps results in higher or lower back-pressures, respectively. Higher back-pressure moves the shock-train forward, with too high a back-pressure causing un-start. This experiment is conducted for a variation in Reynolds number, ramp angle, and two incoming Mach numbers. As a result, for Mach 1.8 case, a shock is imminent at the back-pressure ratio (i.e. back-pressure to stagnation pressure) of ~0.25,

and un-start occurs at the back-pressure ratio of ~0.55. For the Mach 3 case, a shock is imminent at the back-pressure ratio of ~0.04, and un-start occurs at the back-pressure ratio of ~0.28. A higher Reynolds number affects these values by increasing them a little. This research also describes a hysteresis found in the shock-train characteristics. When restarting an un-started flow, the restart will occur at a lower back-pressure value than the one at un-start. In this research, the data is non-dimensionalized to collapse onto one graph. By using the Mach number ratio (i.e., Mach number at the test section when no shock is present to Mach number at various back-pressure), it is possible to find one ratio value when the shock-imminent and un-start occurs regardless of the different Mach number. The ratio for this particular test facility is found to be near 1.83.

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Richard I. Paek

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#### I. Introduction

#### General Issue

In a past development of a scramjet, proving the feasibility of the scramjet engine technology was the primary goal. Many past ground and flight experiments demonstrated the practicality of the scramjet. However, the technical maturity of the scramjet engine is still in progress and there is much room for improvement.

The Air Force Research Laboratory Propulsion Directorate (AFRL/RZ) at Wright Patterson Air Force Base has been looking at the engine un-start problem in a scramjet engine, especially the aerodynamics in the isolator of the scramjet engine. This problem can be caused by either pressure drop at the entrance of the isolator or pressure rise at the exit of the isolator. The pressure drop before the isolator can be caused by a high angle of attack of the vehicle that makes the flow-direction component of the airflow velocity towards the inlet decrease. The pressure rise behind the isolator can be caused by the irregular combustion pressure fluctuation at the combustor. To overcome this problem, the current scramjet engine isolator is designed long enough to contain the subsequent shock-train within the isolator's length and accommodate reasonable pressure variations in front of or behind the isolator. But, a long isolator brings another problem. The longer the isolator is, the more an air vehicle weighs and the more fuel it requires. Reducing the weight of an air vehicle ultimately improves the range of that vehicle for the same amount of fuel. Eventually, this improvement will be applied to long-range-rapid-attack

missiles or economic access-to-space programs. The AFRL/RZ requested the U.S. Air Force Institute of Technology to investigate this issue.

#### **Problem Statement**

Currently, scramjet engines do not have a feedback control system to stabilize the shock-train within the isolator. They have a lengthy isolator section designed with an extra margin of safety to contain the shock-train. As a result of pressure variations before and after the isolator, un-start can be imminent. This engine un-start problem leads to engine flame out and thrust loss. A lengthy isolator section also results in more weight on a hypersonic vehicle, thus, requiring more fuel, and consequently, reducing the air vehicle's flight range. Therefore, the problem to solve is how to make the shock-train reside within a shorter isolator. How does one control the shock-train position? Is it possible to build a feedback control system to do so? What further research is needed to design a feedback control system? Ultimately, answering these questions will enable technology to stabilize the supersonic aerodynamics inside the isolator and shorten the section's length. The particular problem for this research was to design a test facility to for this experiment and determine how the back-pressure affects the shock-train locations inside the isolator.

### **Research Objectives**

The primary objective of this research is to find the back-pressure effect on the shock-train location in the isolator of the scramjet engine. For this research, the primary objective can be divided into two categories. The first one is to design, build, and set up the test facility to simulate the isolator of the scramjet engine. The new facility requires a

capability of applying back-pressure in a controlled manner and allowing the addition of a feedback control system later. The second category is to execute experiments to examine the steady-state behavior of the shock-train as a function of back-pressure.

## **Investigative Questions**

What does it take to build a test facility to simulate the isolator of the scramjet isolator? Can this test facility produce a similar air flow condition as the real operating condition in the scramjet isolator? What is required to maintain the data integrity? How is the laboratory set up so that the research objectives are met? At what back-pressures are shocks and un-start imminent? What does the pressure distribution inside the isolator look like between those two points? How is the leading edge of the shock-train going to be determined from the collected data? Does shock-train location have a linear relationship with the back-pressure value? How does a change in Mach number or Reynolds number affect the shock-train location? If time allows, what does the dynamic behavior of the shock-train look like?

## Methodology

A 2.5"x2.5" supersonic wind tunnel was used for this research. A new test section was built to simulate the scramjet isolator. An adjustable ramp was installed in the floor and one in the ceiling of tunnel downstream of the test section to create a backpressure. Pressure transducers and amplifiers were installed along the top and bottom of the test section. Further a schlieren camera collected visual data through windows in the sides of the test section. A LabVIEW program operated the tunnel and provided position

commands the MTS actuator that controlled the two ramps. Refer to Chapter II Methodology for more detail.

## **Assumptions/Limitations**

Currently, there are two nozzles in this laboratory. One produces a Mach 1.8 flow to the test section and the other produces a Mach 3 flow.

One of the assumptions made was that the flow was isentropic throughout the wind tunnel when calculating the flow Mach and Reynolds numbers within the test section. The available information for this calculation is a stagnation chamber pressure and temperature as well as static pressure measurements from the test section top and bottom. Also, ideal gas behavior was assumed for the air in the test section.

#### **II. Literature Review**

## **Scramjet Engine**

A scramjet engine allows a vehicle to fly at hypersonic speeds while its combustion occurs at supersonic speeds. The turbojet engine has rotating parts, which limit its maximum speed because there is a limitation on how fast airflow can travel through compressor and turbine blades. Ideally, for maximum velocity, the airflow inside the engine would not slow down; therefore, the rotating blades must be rethought. An evolution toward this ideal, from the turbojet engine, is the ramjet engine, in which the rotating parts are removed. In a ramjet, the airflow inside the engine slows down to a subsonic flow for combustion. Still, a ramjet does not allow a vehicle to fly at high hypersonic speeds so the next evolution toward the ideal is to keep the airflow supersonic throughout the engine. When a vehicle flies in a hypersonic speed, airflow within the engine cannot be slowed down dramatically since drops in the airflow velocity convert the flow's kinetic energy to thermal energy. Then, the air itself would be excessively hot and result in ineffective combustion, resulting in thrust degradation. One way to avoid this problem is to have the combustion occur at supersonic speeds. The figure below shows the general schematic of a scramjet engine.

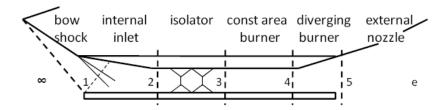


Figure 1. Schematic of dual-mode scramjet engine with stations 1-5 labeled(1)

At supersonic or hypersonic speeds, the nose of the air vehicle creates an oblique (or bow, if it is a blunt body) shock and the airflow speed drops across the oblique shock. When this airflow reaches the inlet of the ramjet/scramjet engine, the cowl lip creates another oblique shock and airflow is slowed down even more. The air finally reaches the combustor after crossing several oblique shocks in the inlet and isolator. The scramjet mixes hydrogen or hydrocarbon fuel with oxygen from the air to generate thrust through combustion.(2) Mixing the fuel and oxidizer in the combustor and burning them at a supersonic speed is still one of the challenges when designing a scramjet because the supersonic airflow does not allow enough time for that to happen.(2) This problem leads to a longer combustor section which ultimately results in more aircraft weight.(3) Currently, there are many ongoing research efforts on mixing fuel and oxygen in a scramjet combustor more effectively.

## History

Genesis of the scramjet engine goes back to one century ago. In 1913, René Lorin in France brought an idea of employing ram pressure in propulsion hardware. In 1928, Albert Fono in Hungary was first to patent a ramjet engine (granted in 1932). In 1935, René Leduc in France designed a ramjet powered aerial vehicle and attempted his first flight on 21 April 1949.(4)

NASA's interest in the hypersonic air-breathing propulsion area goes back 60 years. The interest started from the hydrocarbon-fueled conventional ramjet (CRJ) engine concept and later progressed to scramjets. World War II also stimulated the

technology needs for high-speed flight. The first supersonic flight was accomplished in 1947 with the Bell X-1.(5)

In the 1960's, the interest in scramjets grew as did the understanding of their technical challenges. In that time, a comparison study between CRJ and scramjet was done and proved that the scramjet was more effective in hypersonic speed. In 1964, the Hypersonic Research Engine (HRE) program was initiated by NASA and its goal was to flight-test the scramjet engine on the X-15 rocket-powered vehicle. In April 1965, the U.S. Air Force initiated the Scramjet Incremental Flight Test Vehicle (IFTV) program and its goal was to show the acceleration of the vehicle with 4 hydrogen fuel scramjets.(2) During this decade, the US and UK were the major players in the scramjet propulsion community.(5)

In 1986, the U.S. Air Force and NASA began a serious hypersonic flight research program called the National Aerospace Plane (NASP) program. The goal of this program was to build and flight-test an air-breathing single-stage-to-orbit (SSTO) reusable spacecraft, X-30. It made a great contribution towards developing a rectangular, airframe-integrated scramjet. This program was cancelled without conducting a flight test. The goal of this program was to build a full scale operational SSTO vehicle and it was too big a jump in technology development, and the cost overran.(2) Australia also started scramjet research led by Professor Ray Stalker in 1981. In 1987, the University of Queensland in Australia built the T4 ground test facility. The T4 facility is the world's first facility that can produce the full range of a scramjet operating environment and measure the distinctive parameters inside the scramjet engine.(4)

In 1996, the Hyper-X program was initiated by NASA and built the X-43 series of prototype vehicles. First flight test was attempted in June 2001, but was not successful due to a booster failure. The second flight was successfully conducted at Mach 7 in March 2004. The third flight was also successful at Mach 10 in November 2004 and set a Guinness world record for the fastest air-breathing engine.(2)

In September 2001, the Defense Advanced Research Projects Agency (DARPA) made the first successful ground test flight at the Arnold Engineering Development

Center in Tennessee. They tested a hypersonic scramjet projectile in a gun barrel tube.(4)

Currently, beside the U.S. military and NASA, other countries like UK, Australia, France, Russia, and India are making progress in the hypersonic propulsion area.(5) The implementation of this technology can be a hypersonic cruise missile, bomber, SSTO, or hypersonic transportation.

## **Shock system**

A shock-train is a system of series of oblique or normal shocks, which is a very complex flow structure. Through a shock-train, the pressure rises and Mach number decreases.(6) The majority of the pressure rise occurs at the first oblique or normal shock, and then the pressure rises gradually thru the subsequent shocks.(7) There is a boundary layer between the wall and the shock-train. The boundary layer is thick at the leading edge of the shock-train and becomes thinner towards the downstream direction. The information from downstream can only propagate forward through the boundary layer because flow in the boundary layer is subsonic.(8)

In one experiment, once the shock-train propagated forward out of isolator, the so-called 'un-start' condition, pressure inside the isolator started fluctuating vigorously and its fluctuation frequency was dominant at 124 Hz.(8) According to Rodi et al, this frequency was very close to the natural resonant frequency of their dual-mode configuration. His method to find the resonant frequency was to calculate the ratio of the speed of sound at the flow stagnation temperature to the out-and-back travel length from the inlet entrance to throttle throat, assuming that the exit of the isolator was open. The natural resonant frequency from his calculation came out to be 275 Hz, which was more than twice the observed dominant frequency.(9)

The shock-train length is dependent upon the following factors: incoming flow conditions, isolator geometry, and the pressure ratio at the exit and entrance of the isolator.(10)

There are three criteria for detecting the leading edge of shock-train examined in the study by Lee et al: first, a location where the normalized pressure magnitude upstream of combustion increases by 1.5 times, second, a location where the normalized pressure standard deviation level upstream of combustion increases by 1.5 times, and third, the normalized pressure standard deviation reaches its maximum value. The study shows that the second criteria occurs earlier than other two, and then, first and third in this sequence. The frequency content of the pressure signal with power spectra analysis is another method to detect the shock-train leading edge. When the frequency content of the pressure signal changes significantly, it indicates the vicinity of shock-train leading edge. So, a change in spectral content of measured pressure means that the shock-train leading edge reached the measuring location.(10)

According to Torrez et al., in an early scram mode, the separated boundary layer inside the isolator reduces the effective supersonic airflow area and combustion pressure is expected to be constant during this mode. As you can see in the second picture in Figure 2, the separated boundary layer is getting thinner in the downstream direction so the effective flow area is increasing which results in decrease in static pressure, but heat addition causes the static pressure to rise at the same time.(1)

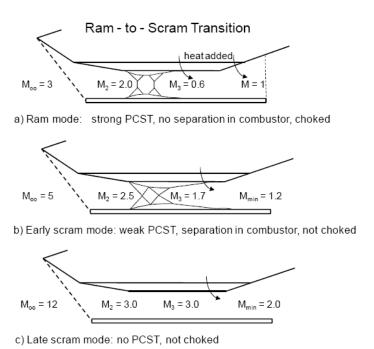


Figure 2. Schematic of Isolator Pre-Combustion Shock-train for Ram, Early Scram, and

Late Scram Modes(1)

There are three methods to calculate the shock-train strength: the empirical method of Billing et al., the constant impulse function method of Heiser and Pratt, and the full CFD solution of Baurle and Eklund.(1)

According to Wagner, a typical shock-train propagation speed is 26 m/s from the laboratory frame of reference.(8) On the other hand, its velocities have been measured to range between 10 to 27 m/s by Weiting(11) and from 55 to 70 m/s by Rodi et al.(9) One journal indicates that the speed is affected by the heat release rate.(12)

#### **Isolator**

The name, isolator, came from its function, which is to isolate the incoming airflow at the inlet from any perturbations in the combustor, which may cause an engine un-start.(10) Its job is also to slow down and stabilize the incoming flow for ideal combustion condition.

The isolator plays a very critical role in a dual-mode scramjet engine. In order to avoid the high pressure in the combustor causing a un-start, an isolator contains the shock-train. For a scramjet, airflow is still supersonic after the shock-train and, for a ramjet it is subsonic which reduces the sensitivity of the inlet against combustor pressure perturbations. The performance of the isolator very closely relies on static pressure rise, total pressure recovery, shock system stability and exit flow uniformity, which are affected by the incoming free stream. Uniform incoming flow structure to the isolator yields uniform flow to a combustor. Ideal flow structure in an isolator would be one where the entire shock-train from leading edge to last shock is contained in the isolator region. For maximum performance, the maximum pressure rise through the isolator should be less than or equal to the pressure rise thru one normal shock.(8)

Without a high pressure from a combustor, there is no shock-train.(13) Why does the shock-train look like crossing oblique shocks? According to Reinartz at el., 'The high

back-pressure leads to the separation of the upper and lower boundary layer and generates a shock wave pattern of two crossing oblique shock waves.'(7)

#### **Pressure measurements**

A few pressure measurement methods were found in other papers. One of them is to use the time resolved measurements of pressure in the isolator to examine the shock-train leading edge detection. The second one is to look at 150% of the normalized pressure standard deviation level upstream of combustion influences. This gives the earlier warning of approaching shock-train from the downstream in the isolator. The third method is to monitor the peak in the normalized pressure standard deviation and this method is proved to be the most conservative one.(10)

### **Control of the shock**

In the NASA Hyper-X program, X-43A was equipped with a Propulsion System Controller (PSC) to reduce the risk of inlet un-start. This device monitors isolator pressure signals as an indicator for shock train location to help predict un-start.(14)

Other research shows that scheduling of the engine pressure ratio to an empirically defined value was an effective way to control the shock-train location. The drawback of this method is that sensor noise and reference value uncertainties can degrade the controller performance. This method does not only require significant margin for error, but also relatively complex compensation to adapt to the changes in flight environment and vehicles orientation with respect to free stream. AuBuchon, et al argue that the control system should not just look at specific reference values or limits.(15)

According to Häberle et al., 'the existing boundary layer separation due to shock interaction in the inlet throat can lead to inlet un-start. Therefore, an optional pressure boundary layer bleed has been integrated at the throat. The passive bleed reduces the lip shock induced separation bubble in the throat significantly.'(16)

Reinartz et al. used a ramp method to create a back-pressure. In their inlet experiments, at Mach 3 condition, he observed a serious flow separation over the ramp and the boundary layer covered one third of duct height. This big separation was not acceptable. So their team attached a wire behind the ramp, so that air flow over the ramp may attach to the ramp more and reduce the flow separation.(7)

#### **Un-start**

There are several things that can cause a un-start: high combustion pressure, heat addition resulting in boundary layer separation, too large inlet contraction ratio, and ignition of entrained hydrogen in the combustor sidewall boundary layer and subsequent separation.(8) (9) (17)(18)(19) Un-start is characterized by high thermal and pressure loads, loss of air mass capture, and an increase in drag.(10)

When un-start occurs, hot combusted gas propagates forward and can damage aircraft components which may lead to the loss of aircraft.(8) A bigger contraction ratio inlet causes more dramatic combustor pressure losses and abrupt un-start. Conversely, a lower contraction inlet causes gradual un-start. Pressure fluctuations become large and irregular during un-start which is also influenced by the inlet geometry.(9)(19)(12) Usually pressure spikes and significant increases in pressure root-mean-square values and inflection points occur right before the un-start.(19)(12)

There also seems to be something like a pause during un-start. Wagner et al. stated "the throttle induced shock system seemed to stop its upstream propagation momentarily in the isolator while the upstream shock-induced separated flow became stronger. After this pause, upstream propagation ensued and the condition of un-start was complete."(8) His data indicates the shock-train transient behavior happened within 9 ms.

### Flight conditions

Usually, the hypersonic vehicle geometry is determined by the cruise flight condition; at that condition, the vehicle is designed to have a bow shock impinge upon the engine inlet lip. This leads to maximum mass flow into the engine. If the vehicle is cruising at a slower speed, there may be mass flow spillage as the shock is ahead of the inlet lip.(20)

One study shows the experiments were done with Reynolds number between 1.07E05 to 2.89E05. In the higher Reynolds number range, the oblique shock generated by the inlet lip propagates downstream uninterrupted beyond the exit plane and the airflow in the isolator just expands continuously. Because of its own favorable pressure gradient, the shear layer remained attached. But at the lower Reynolds number range, the induced shock became stronger and impinged on the internal surface to create another high pressure gradient due to the interaction between shock and boundary layer. As a result, the airflow separated and the pressure propagation expanded upstream. At a Reynolds number near or less than 1.07E05, the flow inside the isolator showed the shock-train transient behavior and led to a choking condition.(21)

Shang pointed out some Mach number and Reynolds number effect on the flow structure inside the isolator. He mentioned, "the lower the entrance Reynolds number, the greater is the induced pressure by the pressure interaction at the leading edge. In this case, the coalescing shock also has a steeper oblique angle to move the shock impingement upstream and leads to reflected shock wave downstream. The stronger adverse pressure gradient within the constant area duct unavoidably generates flow separation and consequently to a choking un-start."(21)

In Shang's experiment, he assumes that the flight region of the scramjet is at high altitude, so that the flow is laminar. Therefore, the turbulent effects were not a player in his investigation. In his experiment, he set his stagnation pressure at 580 Torr (7.47kPa, 11.2 psi) and temperature at 300K with an incoming Mach number of 5.15, which results in air number density of 1.57E17/cc and Reynolds number of 7.55E5/m. In his investigation, the real gas effect was not considered. At a lower Reynolds number, the oblique shock angle was steep, impinged on the sidewalls, and bounced off in the downstream direction. But at the higher Reynolds number, the oblique shock angle was shallow so it went to the exit of the isolator without bouncing off the wall.(21)

In Mirmirani et al.'s research, they had a flight condition of Mach number 10 at an altitude of 30 km, where the standard atmospheric temperature and pressure are T1=227K and P1=1172 Pa respectively. A corrected specific heat ratio was  $\gamma$ =1.36 for hypersonic flight condition. They used oblique shock relations for their calculations. Their combustion process was simply modeled by Rayleigh flow theory, one-dimensional compressible flow with head addition.(2)

It is important to recall how the air behaves at the molecular level at both supersonic and hypersonic speed. In supersonic speed, Mach 5 or less, the diatomic molecule, air, has five degrees of freedom. Those are three translational and two rotational modes. As the Mach number becomes greater than 5, the temperature across the normal shock increases and the inert degrees of freedom are energized. They are vibration, dissociation, and ionization, which significantly change the aerothermodynamics properties of air. Then the air no longer behaves as ideal gas; instead, it has real gas effects.(3)

In hypersonic flight, the temperature rises across the shock and thickens the boundary layer around the vehicle. This might damage the aircraft structure and alter the pressure distribution around the body. As the boundary layer become thicker, the flow sees the aircraft bigger than its actual size. This makes the shock at the leading edge become stronger, and the skin friction increases by induced pressure gradients. High Mach number increases the skin friction drag and this may increase the total drag by twice.(3)

## III. Methodology

## Entire experiment apparatus set-up

The laboratory is located in Bldg 640 Room 273 of the Air Force Institute of Technology (AFIT), Wright Patterson Air Force Base. A 2.5"x2.5" supersonic wind tunnel was used for this research. This wind tunnel and other peripherals occupy 17 ft x27 ft floor space. See the picture below.



Figure 3. Picture of the 2.5"x2.5" supersonic wind tunnel laboratory

The 2.5"x2.5" supersonic wind tunnel facility consists of the following components: a vacuum pump, a vacuum tank, two compressor pumps, an air dryer, a high pressure dry air tank, a main control computer with LabVIEW software, and National

Instruments data acquisition system. These are the main components driving this tunnel are not shown in the picture above, but are described later in this section. The components shown in the picture are schlieren set-up, a high speed camera, a computer that controls the camera with PFV software, a MTS hydraulic actuator, a hydraulic pump, a computer that controls the MTS hydraulic actuator with interface software, a hydraulic actuator stand, pressure transducers and amplifiers. The detailed list and their descriptions are written below. To better understand the laboratory system, a symbolic diagram is drawn and shown below.

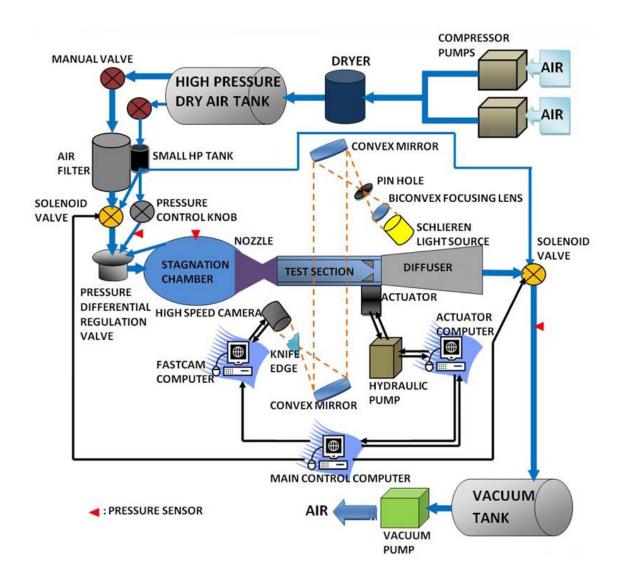


Figure 4. Entire laboratory diagram

## 2.5"x2.5" supersonic wind tunnel

At the very upstream of this supersonic wind tunnel, there are two compressor pumps, which bring air from the atmosphere and pressurize it into a tank outside the building. A picture of a compressor pump is shown in the Figure 5 below.



Figure 5. High air pressure compressor pump

This compressor is made by Ingersoll Rand Industrial Technologies Inc. and its model number is UP6-50PE-200. It can produce the maximum pressure of 200 psig. The next component that air goes thru is the desiccant compressed air dryer, which makes the air free of moisture and suitable for experimental use. This dryer is made by Donaldson and its model number is AHLD-350. The volumetric flow rate of gas for this dryer is rated at 350 standard cubic feet per minute (SCFM).



Figure 6. Desiccant compressed air dryer

Once the air goes thru this dryer, next it goes to the pressure tank outside the building. The volume of the tank is approximately 6,000 gallons. The pressure tank is shown in Figure 7 below.



Figure 7. Vacuum tank (left) and pressure tank (right)

The next component that air sees is the main manual shut off valve. This valve is regularly shut down at the end of the test day for safety purpose or when calibrating sensors.



Figure 8. Main manual shut off valve

Then air goes to a small high-pressure tank and, in parallel, to an air filter until the user begins a test run. A black knob on the top of the air filter controls the stagnation chamber pressure, which results in different Reynolds number of the air flow in the test section.(22)



Figure 9. A small high pressure tank (black), air filter (gray), and stagnation chamber pressure control knob on the top of the air filter

When the wind tunnel is started, the main control computer sends electronic signals to two solenoid valves. The downstream solenoid valve opens first, and then the upstream solenoid valve opens next. This sequence prevents the test section from being pressurized. Also, when the tunnel stops, the upstream solenoid valve closes first, and then the downstream solenoid valve closes next for the same reason. This logic sequence is built in the LabVIEW program in the main control computer. The picture below shows the upstream solenoid valve.



Figure 10. Upstream solenoid valve

After the air goes through the opened upstream solenoid valve, it goes to a regulation valve, and then stagnation chamber. The stagnation chamber is shown below. In the stagnation chamber, the velocity of the air is supposed to be zero, so the pressure measured at the stagnation chamber is the total pressure.

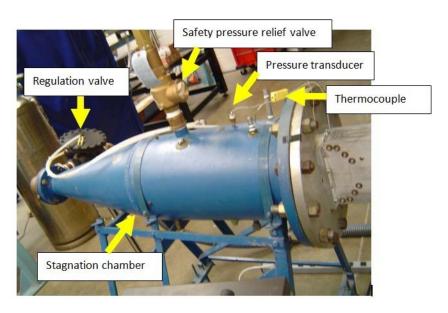


Figure 11. A regulation valve (black component on the left) and stagnation chamber (blue)

Then the air goes thru the diverging nozzle, which generate a desired Mach number of the incoming airflow to the test section. There are two diverging nozzles in the laboratory; one can produce Mach 1.8 and the other one can produce Mach 3 speed. Those nozzles are shown below.

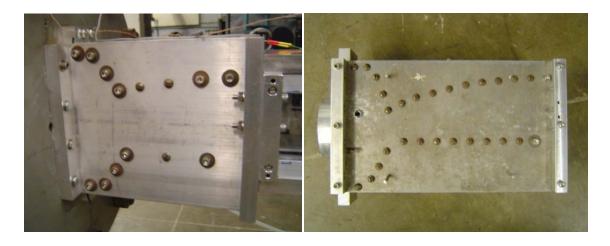


Figure 12. Mach 1.8 nozzle (left) and Mach 3 nozzle (right)

After going thru the nozzle, the air enters the test section. Figure 13 below shows the test section. This test section is specially designed for this research and is designed to simulate the scramjet isolator. The design process, fabrication process, and more detail about the test section are written later in this section.



Figure 13. A new test section

Once the air exits the test section, it goes to the diffuser, a downstream solenoid valve, and then the vacuum tank outside the building. See pictures below.

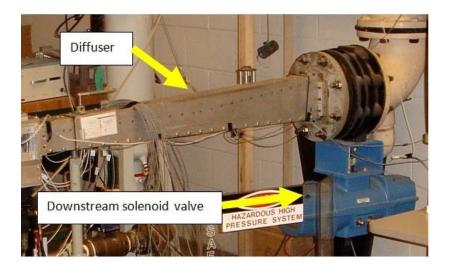


Figure 14. Diffuser and downstream solenoid valve

The volume of the vacuum tank is also approximately 6,000 gallon and the picture of the vacuum tank is in Figure 7. The air in the vacuum tank is forced out by the vacuum pump and it returns to the atmosphere. The vacuum pump is made by Stokes Vacuum Inc. It has two motors: one main motor with 10 H.P. and a turbo pump motor with 20 H.P. The vacuum pump is shown below.



Figure 15. Stokes vacuum pump

There is one unique characteristic about this wind tunnel. With Mach 1.8 nozzle, prior to test runs, the upstream regulator pressure valve (Figure 9) was set at approximately from 18 to 49 psia. After the wind tunnel started and air flow became stabilized, the total pressure measured at the stagnation chamber (Figure 11) was approximately from 14 to 18 psia. However, with Mach 3 nozzle, the upstream regulator pressure valve was set at from approximately 18 to 49 psia, and the pressure measured at the stagnation chamber was approximately from 14 to 44 psia. This phenomenon indicates that the throat area of the Mach 1.8 nozzle may be greater than the throat area of either the regulator valve (Figure 9) or the main shut-off valve (Figure 8), so the smaller throat area at either regulator valve or main shut-off valve does not supply enough air mass flow which results in low total pressure in the stagnation chamber. This phenomenon brings an importance of monitoring the stagnation chamber pressure during

the test runs to see whether the total pressure was steady or transient during the runs. The Figure 16 below shows the total pressure value at the stagnation chamber with respect to time. As you can see, the total pressure remain constant throughout the tests; therefore, there is no transient effects by total pressure in this wind tunnel. To note, the R.V.P in the figure's legend means the pressure setting at the regulator valve.

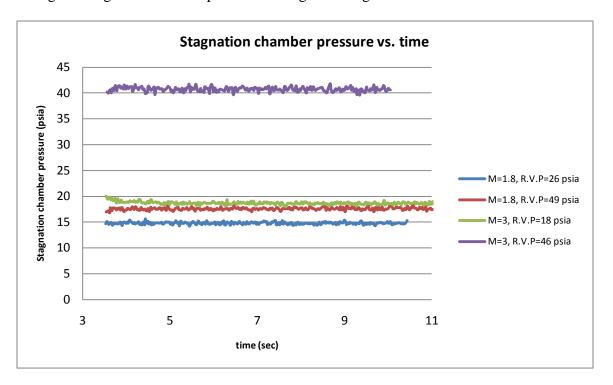


Figure 16. Stagnation pressure behavior during the test runs

#### The new test section

Probably the biggest challenge in this research was designing and fabricating the new test section. A lot of engineering studies were required during this process. First, a previous test section was carefully examined to see if it can be used for this research. To serve this research's purpose, the old test section did not only require a significant modification, but it also did not satisfy all this research's needs. For example, its length

in flow direction was too short, so it might not have covered the entire range of the shock train from the leading edge to a terminating shock. One idea came up was to put an additional section on the downstream side of the original section and install a mechanism to create a back-pressure. But, two different sections do not allow one smooth surface and any gaps or non-smoothness at the joint of two surfaces can create shock waves. Moreover, the old test section was not designed to hold any positive gauge pressure. In this research, the pressure in the test section might become high by raising the back-pressure. Moreover, the joint between the old section and the additional section can block the schlieren view. This first idea is shown below.

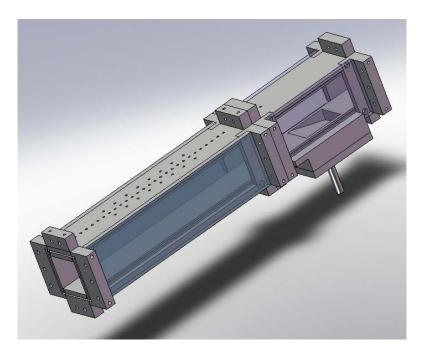


Figure 17. First concept: adding a new section behind the existing section

After in-depth examination and consideration, the decision was to take a risk of re-inventing the wheel. Then, so many questions followed. How long does the test section have to be? What kind of mechanism should be used to produce the back-

pressure? How strong does the test section have to be in order to hold the high pressure caused by the back-pressure inside the test section? Where should the sensors be mounted? How far should the sensors be spaced? What kind of material should be used for the test section? How about the window? How thick does the window have to be? And so on. The questions were countless. Some of the questions could be answered from other researchers' work. Some questions were answered because of the limitation of the current laboratory's configuration. For example, the maximum length of the test section cannot exceed 2 feet; otherwise, the walkway beside the wind tunnel is blocked and violates the safety code of the building.

Aluminum 6061-T6 was chosen for the test section material because aluminum is fairly light, strong, and used a lot for aerospace applications.(23) The material for the window was chosen to be cast acrylic because it is safer to handle and easier to fabricate than glass. Also, it provides outstanding optical clarity even at greater thicknesses, which is very important for schlieren video.

For a safety concern, the required minimum window thickness was calculated. The calculation is shown in Appendix A. The calculation shows that the window thickness has to be at least 0.729 inch. For optical use, i.e., schlieren imaging, it was also important to know the window deflection subject to the pressure because it affects the light refraction thru the window. Its calculation is shown in Appendix B. The results say that the maximum deflection of the window under 35.5 psig pressures would be 0.00211 inch. Both these calculations were based on the assumption that the maximum pressure at the test section is 35.5 psig. This case is only possible when the upstream pressure is set at 35.5 psig and the downstream of the tunnel is completely blocked. According to

the experiments on this tunnel in the past, the maximum gauge pressure inside the tunnel was -12 psig. Assuming the maximum pressure of 35.5 psig is conservative.

What to use to create a back-pressure brought some good discussion. At the very beginning, there was a debate over a pneumatic method versus a mechanical ramp method. The pneumatic method idea was turned down because it might not be able to produce constant steady pressure and also the valve mechanism's speed does not seem to keep up with the dynamic speed of the shock-train and the feedback control system.

Moreover, the air from the pneumatic system can have significant non-linearities. Hence, the mechanical ramp method was chosen.

The size of the ramp was the next problem to solve. After a discussion with the previous researcher who used this tunnel, he noted that when he placed a test object with a diameter of 1 inch in the test section, he observed the shock-train propagated forward. The cross section area of 1 inch diameter object is 0.785 square inch. There is also a mount for the test object and it blocks some flow area as well. The wind tunnel cross-section area is 6.25 square inches. It means that at least 12.57% of area blockage can create the shock-train. From that number and engineering educated estimate, the ramp width was chosen to be 1 inch.

The hydraulic actuator has an extension range of 1.5 inches, but its reading is accurate only within middle 1 inch region. This number helps determine the location of the ramp's pivot point, the length of the ramp, and the maximum ramp angle.

The idea of using two ramps, top and bottom, was brought up for creating a symmetric flow. Though this is good idea, it also brings a new challenge. In order to move two ramps simultaneously and synchronize them, the gears are necessary.

However, a drawback about the gear is that it creates backlash in motion. Therefore, two big high precision gears were chosen and cut in Japanese-fan-shapes, so that the required number of gears and space around them can be reduced. Small dimension around the test section only allows the small gears, and then four gears are required to connect them. The more gears there is, the bigger the backlash is. Cutting two big gears into Japanese fan shapes does not only reduce the number of gears, but also makes the big gears fit in a small area. Because high precision gears were chosen, almost no backlash was noticeable.

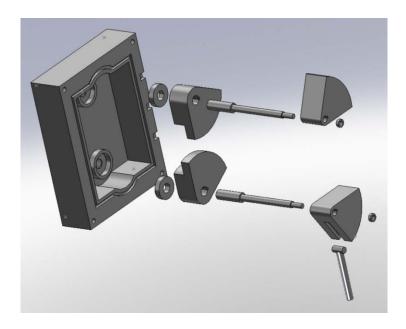


Figure 18. Gearing mechanism to synchronize two ramps

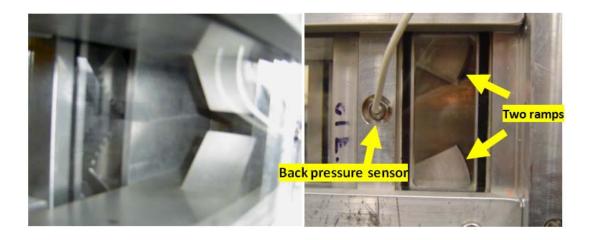


Figure 19. Two ramps inside the wind tunnel

There are some moving parts in this test facility, i.e., ramps, gears, an actuator, and shafts. Eventually, these parts will be moving at high frequency after the control system is installed. Wear-and-tear would be another problem to encounter. So, ball bearings are installed at almost every rubbing surface. High precision miniature-size ball bearings were chosen for this facility.

Sealing was another challenge. To keep the integrity of the airflow inside the test section, there must not be any air leaks in any joints in the test section. O-ring seals were used at almost every contacting surface. Sealing between the test section and the hydraulic actuator was another challenge. Making the joint parts precisely and using O-rings was a key to the success.

There was some design variables already determined due to the dimension of the other existing parts of the wind tunnel. The new test section had to mate with the upstream diverging nozzle and the downstream diffuser, and the inside cross section area had to be 2.5"x2.5." The hole locations for bolts, hole size, thread size, etc. on those

front and back end, were already determined. Other dimensions had to be worked around those fixed parameters.

Many ideas about how to link the actuator and the ramp together came up. Some of the ideas on the actuator end are shown below.



Figure 20. Clevis rod ends (left), wheel rod ends (center), T rod end (right)

The T-shape rod end was chosen because it reduces the complexity of the design, fits in a tighter space, and is easy to assemble and disassemble. When considering the future research, when the feedback control system will be used, there might be a time when the feedback control system goes unstable. Then, the actuator will move up and down out of control. In order to prevent the actuator from pulling, pushing, and breaking the ramp and other parts, the T-bar was chosen. T-bar disengages from the ramp when the actuator is all the way up or down. T-bar will slide out the back end of the ramp at those two situations. See Figure 115 in Appendix E for better understanding.

Figuring out the pressure sensor locations and their numbers was another difficult task because the goal of this research was to find where the shock-train would occur.

Also, the oscillation amplitude of the shock-train was unknown. The number of sensors and location of them were limited by the physical space around the test section. The goal was to try to put as many as possible as close as physically possible. The pictures below

show the number and the locations of pressure transducer locations on a top plate and a bottom plate. They are the holes in the rectangular box.

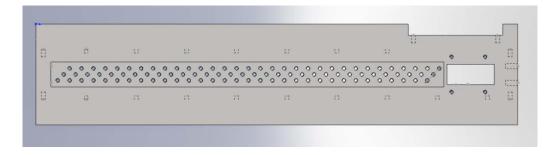


Figure 21. Top view of a top plate

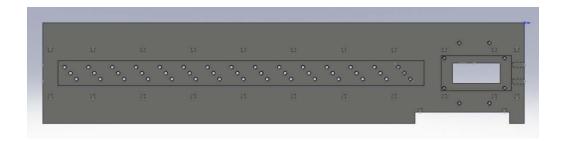


Figure 22. Bottom view of bottom plate

In order to communicate with the model makers at the machine shop, Solidworks software was used. Solidworks is an outstanding, sophisticated, professional, versatile, and visually beautiful program. But learning such a program by oneself was a challenge and requires significant time. Besides, the design for this project involves many complex geometries and moving parts. Drawing them in the Solidworks program was a very time-intensive effort. The final drawing of the test facility in Solidworks program is shown below. In addition, the engineering drawings are attached in the back of the report in Appendix C.

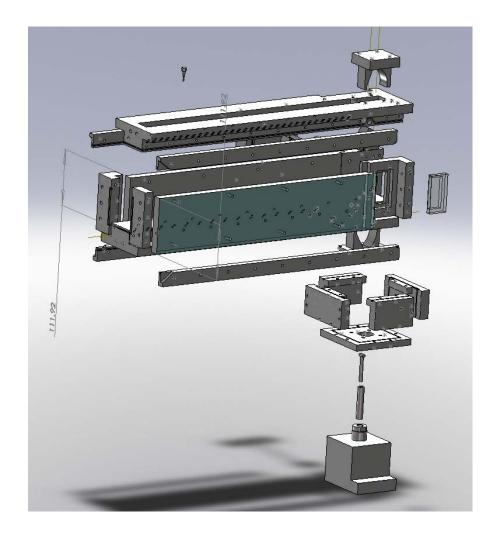


Figure 23. The new test section drawn in the Solidworks software

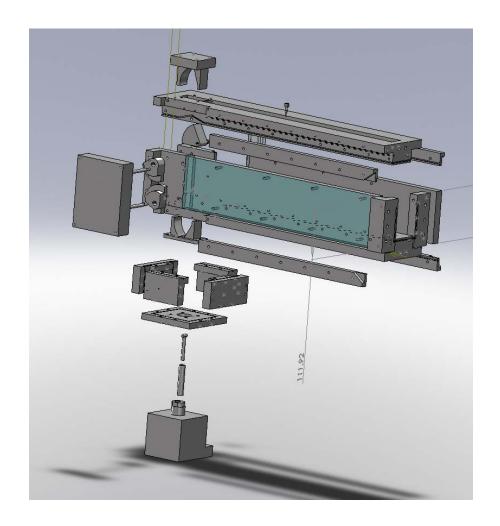


Figure 24. (Continued) the new section drawn in the Solidworks software Also, the finished test section is shown in the picture below.







Figure 25. The picture of the new test facility

# Main control computer

There was a main control computer already prepared for the 2.5"x2.5" supersonic wind tunnel in this laboratory. See the picture below.

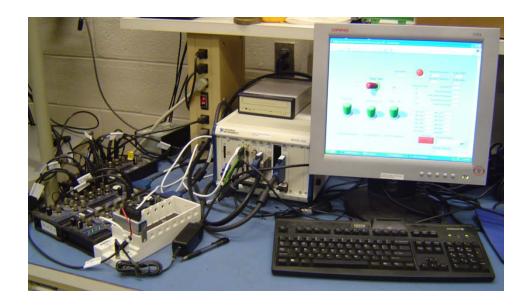


Figure 26. A main control computer for 2.5"x2.5" supersonic wind tunnel

This computer has the following components.

- A monitor, a keyboard, and a mouse
- NI PXI-1042 8-slot chassis
- NI PXI-8196 Embedded Controller
- NI PXI-6120 Simultaneous Sampling Multifunction I/O
- NI PXI-6259 M series Multifunction DAQ
- NI PXI-6070E Multifunction I/O
- NI PXI-1409 Image Acquisition
- External CD drive
- 68 pin cables (x3) and USB cables (x1)
- NI BNC-2120 boards (x3)
- NI cDAQ-9172 and NI 9263
- LabVIEW software

#### • NI Measurement & Automation software

A NI PXI-8196 Embedded Controller is the motherboard of this computer. It has 512 MB (2 x 256 MB DIMMs) dual-channel DDR2 RAM standard and 2GB maximum memory, 2.0 GHz Pentium M 760 processor, Windows OS and drivers, ExpressCard/34 slot and 4 USB 2.0 ports, Integrated hard drive, GPIB, serial, 10/100/1000 BaseTX (Gigabit) Ethernet, and other peripherals.(24)



Figure 27. NI PXI-8196 Embedded Controller

A NI PXI-6120 Simultaneous Sampling Multifunction I/O board was used for data acquisition of pressure and actuator position readings. It can take 4 simultaneously sampled analog inputs at 1MS/s per channel with warp mode enabled. It has onboard memory of 64 MS, extended input ranges up to +/-42V, and onboard anti-aliasing filters. It also has two 16-bit analog outputs that can send 4 MS/s per single channel or 2.5 MS/s per dual channel. It has 8 digital I/O lines, two 24-bit counters, analog and digital triggering.(24)



Figure 28. NI PXI-6120 Simultaneous Sampling Multifunction I/O

A NI PXI-6259 M series Multifunction DAQ is used for data acquisition of pressures. It has four 16-bit analog outputs (2.8 MS/s), 48 digital I/O, 32-bit counters, and NI-MCal calibration technology for increased measurement accuracy. It also has NIST-traceable calibration certificate, more than 70 signal conditioning options, correlated DIO (32 clocked lines, 10 MHz), analog and digital triggering.(24)



Figure 29. NI PXI-6259 M series Multifunction DAQ

A NI PXI-6070E Multifunction I/O was used for data acquisition of pressure and temperature, and analog output triggering to run the wind tunnel and start the camera. It

has 1.25 MS/s rate, 12-bit resolution, 16 analog inputs, 2 analog outputs, 8 digital I/O lines, two 24-bit counters, and analog triggering.(24)



Figure 30. NI PXI-6070E Multifunction I/O

A NI PXI-1409 Image Acquisition and an external CD drive were installed to this computer but were not used for this experiment.

The NI BNC-2120 board is a shielded connector block with signal-labeled BNC connectors. This device simplifies the connection of analog signals, some digital signals, and two user-defined connections to the DAQ device.(24) A picture of this unit is shown below.



Figure 31. NI BNC-2120 boards

The command output for a hydraulic actuator goes through a NI cDAQ-9172 and a NI 9263. The NI cDAQ-9172 is a compact DAQ chassis. It can run analog input modules at different rates. It has 8 slots for I/O modules. One NI 9263 module was installed in NI cDAQ-9172 chassis. The NI 9263 has 4 simultaneous channels, collects 100 kS/s with 16-bit resolution, and outputs +/- 10V analog signal.(24) Pictures of these units are shown below.



Figure 32. NI cDAQ-9172 and NI 9263

The information and specifications stated above were found at the NI official website.(24)

The LabVIEW software installed in this main computer was used to operate the wind tunnel, collect data, and trigger the camera. Figure 33 below shows the GUI panel of LabVIEW for the supersonic wind tunnel.

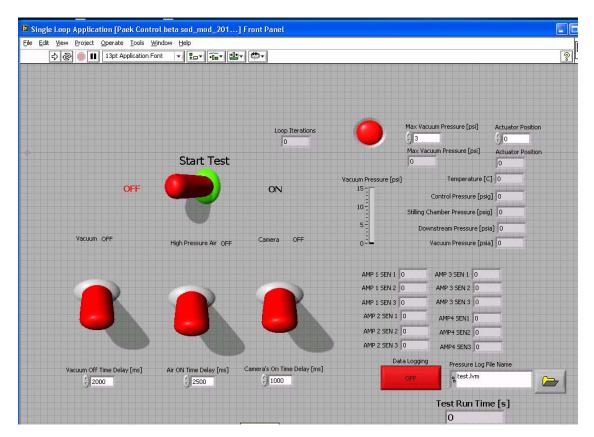


Figure 33. LabVIEW GUI panel for supersonic wind tunnel

Behind this front panel, there is a logic circuit panel and this is shown below.

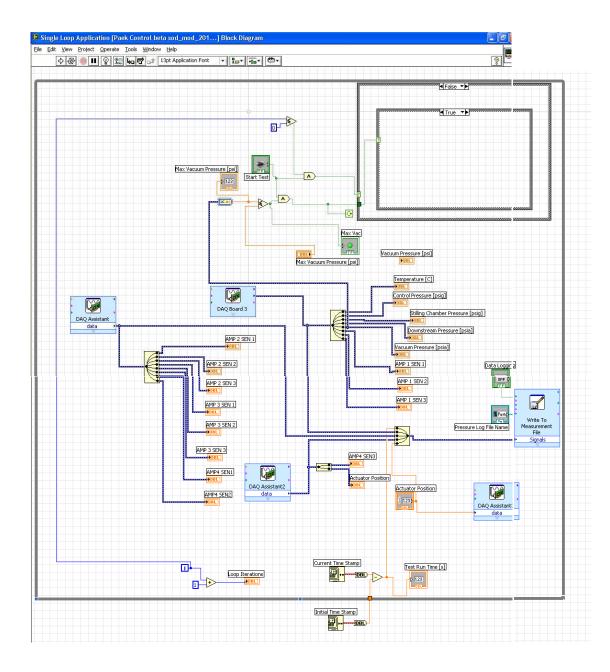


Figure 34. LabVIEW internal structure

Also, the NI Measurement & Automation Explorer software was used to install/uninstall, troubleshoot, and configure NI software or drivers. The screenshot of this program is shown below.

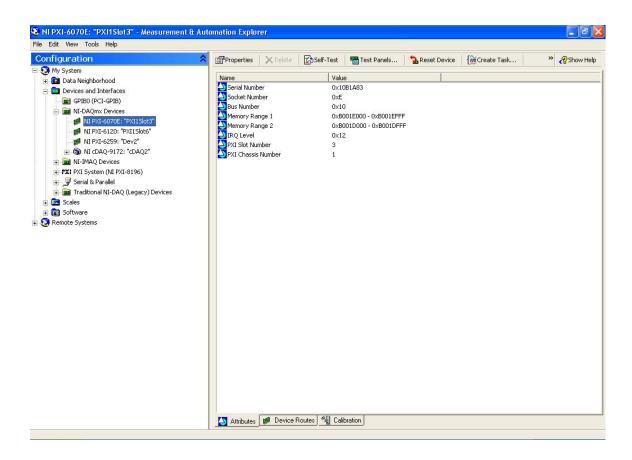


Figure 35. NI Measurement & Automation Explorer

#### **Endevco pressure transducers and amplifiers**

There were already four Endevco pressure transducers and four DC amplifiers installed in the wind tunnel for the operation purpose. Twelve additional Endevco 8530C-50 piezoresistive pressure transducers are purchased for the experimental purpose. They have a measurement range of 0 – 50 psi, 4.5 mV/psi sensitivity, 1ms of warm-up time, and diaphragm burst pressure of 250 psi min. It also has full scale output of 225mV typical at 10.0Vdc, active four-arm piezoresistive bridge electrical configuration, noise of 5 microvolts rms typical, DC to 50,000 Hz and 50 microvolts rms maximum, DC to 50,000 Hz. It weighs 2.3 gram and cable weighs 9 grams/meter.(25)



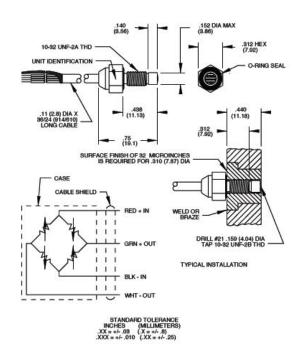


Figure 36. Endevco 8530C-50 piezoresistive pressure transducers

Four additional Endevco Model 136 DC Amplifiers were acquired for this experiment. Each one has three DC channels, 200 kHz bandwidth (-3dB corner), gain range from 0 to 1000 depending on the input voltage, built-in 4-pole Butterworth low-pass filter, linear output of 10V peak, current output of 10 mA minimum, output noise of 1mV rms maximum from 10 Hz to 50kHz with 1 kOhm load, accuracy of +/-0.5% of full scale maximum with DC to 1kHz and filters disabled, linearity of 0.1% of full scale with best fit straight line at 1kHz reference, power dissipation of 10 Watts, and weight of 4 lbs.(25) A picture of these amplifiers is shown in a Figure 37 below.

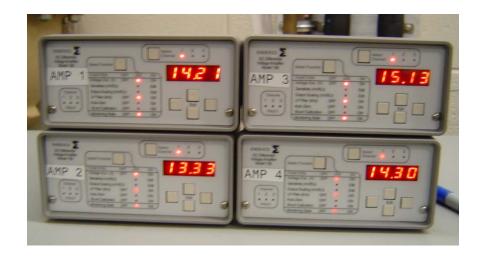


Figure 37. Endevco Model 136 DC Amplifier

The product information and specifications are available at the Endevco official website.(25)

Upon receiving Endevco products, a calibration was done on the sensors although the factory specification sheets were provided with the calibration results. After in-house calibration was complete, it was found that their results do not exactly match with the factory calibration data. Additionally, although the sensors themselves had linear behavior, the DC amplifiers were showing non-linear input-output relationships.

Moreover, the digital readout on the DC amplifier has +/- 10% error. So the engineers had to find the direct relationship between pressures acting on the sensor versus the voltage outputs from the amplifier and kept in mind not to trust the digital readout on the DC amplifier. The pressure sensor/amplifier calibration results are shown in Appendix D. Also, a daily calibration was done at the very beginning of a test day to adjust any offsets due to any day-to-day pressure and temperature fluctuations. For this calibration, the reference pressure digital barometer was used in the laboratory and it is shown in the picture below.



Figure 38. Reference pressure digital barometer for day-to-day calibration purpose

## Schlieren imaging setup

Schlieren imaging equipment was available in the laboratory, but engineers had to configure it. The schlieren setup consists of following components.

- Light source: OSRAM HBO Mercury Short Arc lamps, 130W/2
- Biconvex focusing lens
- Pinhole
- Two convex mirrors (focal point: 80 inches)
- Knife edge
- High speed camera

The schlieren setup is shown in the diagram below.

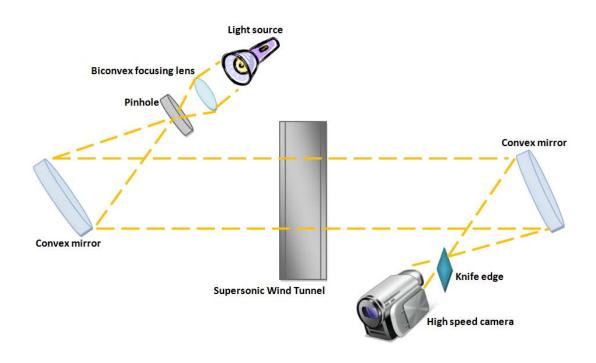


Figure 39. Schlieren imaging setup



Figure 40. Light source for schlieren imaging



Figure 41. Biconvex lens (left) and pinhole (right)



Figure 42. Convex mirror



Figure 43. A knife edge and high speed camera

The high speed camera is made by Photron and its model number is FASTCAM-X 1280PCI. It provides an 1,280x1,024 pixel image at frame rate to 500 frames per second, and at reduced resolution up to 16,000 fps. Electronic global shutter is as fast as 7.8 µs. The knife-edge was set vertical because research focuses on the horizontal movement of the shock-train.

There is a separate computer station connected to the FASTCAM, which receives and records the video from the camera. The PFV ver.2.4.3.8 is the interface software for the high-speed camera. They are shown in the picture below.



Figure 44. Schlieren imaging control and viewing computer

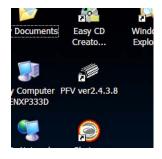


Figure 45. High speed camera interface software: PFV ver.2.4.3.8

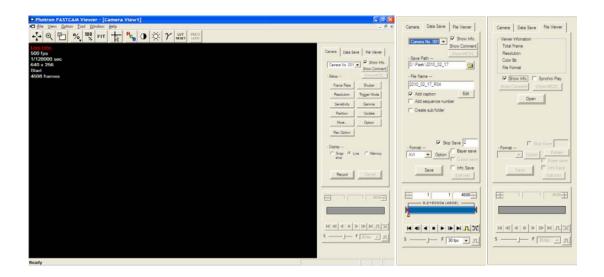


Figure 46. Screenshots of PFV.2.4.3.8 software

In the Figure 46 above, there are three menu taps on the right side of the screen, which allow a user to operate the camera, edit/save the video, and view the multiple videos. This software has a standby mode feature. When it is set at standby mode, it is waiting for a signal from the external source (main control computer for this experimental case). This feature allows a user to record the images automatically, remotely, and in a controlled timely manner with a single click of button.

### **Actuator system**

The actuator system is composed of four main components. They are a hydraulic actuator, hydraulic fluid pump, a control computer, and interface software. The hydraulic actuator, the pump and the interface software are made by MTS Systems Corporation.

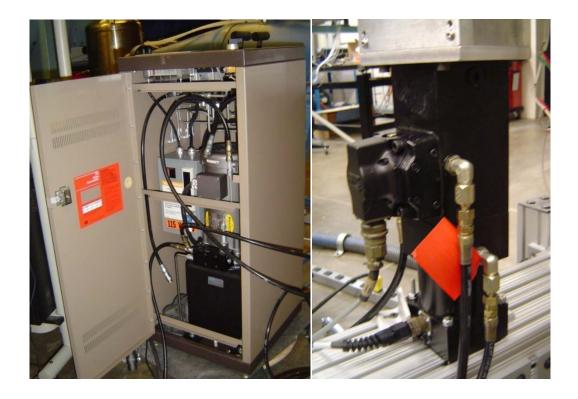


Figure 47. Hydraulic pump (left) and actuator (right)

The pictures above show the hydraulic pump and actuator used in these tests. The model number of the actuator is 242.01 and it can produce a force of 1 kip (= 5kN) over an effective area of 0.42 square inch. The model number of the pump is 685.03 and it is a 3,000 psi hydraulic grip supply.

The actuator control computer is linked to the main control computer, so the actuator position can be controlled and monitored by the main computer.

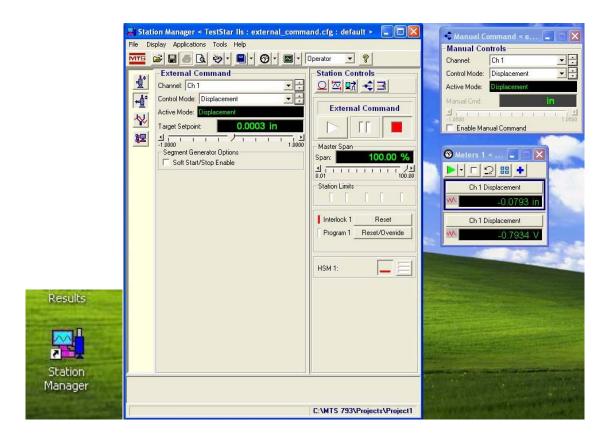


Figure 48. MTS software, desktop icon (left) and GUI (right)

The MTS software provides multiple capabilities. An actuator can be controlled by a real time manual command, a programmed command, or an external command. A Proportional-Integral-Derivative (PID) feedback controller is built in this software, so the position of the actuator can be accurately measured and controlled. Moreover, the PID gains in the software can be adjusted by a user, so the user can change the dynamics of the actuator. The MTS software also provides many types of preprogrammed inputs: step input, sinusoidal inputs, triangle inputs, ramp inputs, etc. The dynamics of the actuator can be customized in every aspect.

# Safety pressure relief valves

There are two safety pressure relief valves in this supersonic wind tunnel. One is located on the stagnation chamber and the other one is located at the end of the diffuser. They both are pop-off type valves.



Figure 49. Safety pressure relief valves

# Side project: making an actuator stand

In order to position the actuator at the right place and height, a stand was needed. First, small height adjustable carts or tables were looked at, but the space under the test section is very tight. So, the next option was to create new one. The 80/20 Inc. parts were suggested to use by lab technicians. First, the design schematic was done in the Solidworks program. By doing this way, it is easy to visualize the structure of the stand

and estimate the required material accurately. Once the design was done, the parts were acquired and assembled.

The stand should be height-adjustable, and able to handle hydraulic weight and its vibration. The actuator can be operated under very high frequency. In order to dampen out the vibration, rubber padding was inserted under an actuator. To raise and lower the heavy hydraulic actuator conveniently, a motorcycle jack was acquired. And there were 4 brakes installed on the stand to hold it at a fixed height. Pictures below show the Solidworks drawing and the final product.

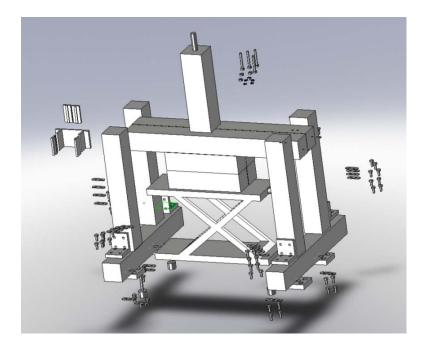


Figure 50. A stand for the hydraulic actuator, drawn in the Solidworks software



Figure 51. Final product: hydraulic actuator stand

### IV. Analysis and Results

#### Overview

In the very beginning of the test phase, the test section was delivered. When and where the shock-train occurs in terms of the actuator height and its back-pressure value were of initial interest. After many test runs at a few different Reynolds numbers and two different Mach numbers, a rough idea of when and where the shock-train occurs in terms of actuator heights was determined.

The first method tried was a static ramp test. In this test, the ramp height was preset before the running the wind tunnel, and the tunnel was run with a fixed ramp height. An advantage of this approach is that one eliminates any dynamic or timetransient effects by ramp. One drawback of this approach, however, is that the airflow condition near the simulated isolator un-start point is uncertain. The simulated isolator un-start here means that the back-pressure caused by raising the ramps, creates the shocktrain in the test section and causes it to propagate forward out of the test section. For example, compare two cases where the ramp was already raised before the wind tunnel started versus where the ramp was raised after the tunnel was already running. In the first case, the ramp was raised to a 35 degree angle, the tunnel started, and the shock-train appeared in the middle of test section. Next, the ramp was raised by a small increment, e.g., 36 degree angle, the tunnel was started, and one observed that the shock-train propagated all the way upstream. Let's compare this condition to the second case. The tunnel was started and running, the step input of 35 degree angle was introduced, and the shock-train appears in the middle of test section. Next, similarly, the tunnel was started

and running, and then the 36 degree step input was introduced. This time the shock-train stayed in the test section rather than propagated forward. The difference between two cases would be that the first case with the ramp angle of 36 degree choked the tunnel from the very beginning and the second case did not. Therefore, the second case seems to be a correct way to proceed because a stable test environment should be reached before any object is introduced. The second case also allows for airflow to stabilize before the object is introduced.

This issue was more apparent with the Mach 3 nozzle. With Mach 3 air flow, the shock-train was statically stable up to duct height 4 or 5 (10 to 12.5 inches) from the ramp at specific ramp heights. When trying to hold the shock-train beyond 4 or 5 duct heights, the simulated isolator un-started as the tunnel was starting. With Mach 1.8 nozzle, this issue was not a concern because shock-train had its own stable static positions throughout the test section with its corresponding ramp height. In other words, the stable shock-train could be held at any location in the test section, and there appeared no location where the shock-train goes to un-start with Mach 1.8 speed. A longer test section would possibly allow one to find the unstable point for the shock-train.

### Ramp input to an actuator: constant increase in height

The next approach was to give the ramp a continuing increase in height after the tunnel started. This method prevents the tunnel from a un-start from the beginning, but would not be a truly static test, rather a quasi-static test. Quasi-static effects will be discussed later in the Analysis and Results.

In order to mitigate the quasi-static effect, the ramp was raised as slow as possible. The slope of the ramp input was determined by the three factors: the height where the shock-train first appear, the height where the shock-train became unstable, and the wind tunnel run time, which is roughly 5 to 6 seconds. Because the heights where the shock-train imminent and un-start conditions occur are different for different Reynolds and Mach numbers, the ramp input (the starting height, slope, and end height) must be adjusted in accordance with each test condition. In this constant-increasing-height test, 9 different test conditions were executed and those conditions are shown in Table 1 below:

Table 1. Constant slope input test conditions

| Test No. | Mach   | Reynolds number | Actuator command input  |
|----------|--------|-----------------|---|
| Test No. | number | (1/m)           | (See a NOTE below for the unit)   |
| 1        | 1.8    | 1.280 E07       | Starting height: 0 inch / Slope: 0.11 in/sec / end height: 0.22 inch      |
| 2        | 1.8    | 1.436 E07       | Starting height: 0 inch / Slope: 0.11 in/sec / end height: 0.22 inch      |
| 3        | 1.8    | 1.659 E07       | Starting height: 0.04 inch / Slope: 0.072 in/sec / end height: 0.22 inch  |
| 4        | 1.8    | 1.712 E07       | Starting height: 0.05 inch / Slope: 0.072 in/sec / end height: 0.23 inch  |
| 5        | 1.8    | 1.719 E07       | Starting height: 0.04 inch / Slope: 0.072 in/sec / end height: 0.22 inch  |
| 6        | 3      | 7.8 E06         | Starting height: 0.36 inch / Slope: 0.012 in/sec / end height: 0.446 inch |
| 7        | 3      | 1.185 E07       | Starting height: 0.36 inch / Slope: 0.012 in/sec / end height: 0.5 inch   |
| 8        | 3      | 1.7 E07         | Starting height: 0.37 inch / Slope: 0.012 in/sec / end height: 0.467 inch |
| 9        | 3      | 2.3 E07         | Starting height: 0.35 inch / Slope: 0.019 in/sec / end height: 0.476 inch |

NOTE: The unit of the actuator height is in inches in MTS digital reading. Refer to Appendix E for conversion to other dimensions.

The calculation of Mach and Reynolds numbers are based upon the isentropic relationship and ideal gas law. The equations can be found in Chapter 8 of Anderson's 'Fundamentals of Aerodynamics' book. Total pressure and temperature in this experimental is those at the stagnation chamber. The static pressure is at the test section. The gamma of 1.4 and gas constant of 287 J/kg/K was used.

With the test conditions above, the test results are shown below. In each figure, the vertical axis is the ratio of static pressure over stagnation chamber pressure, and the horizontal axis is the distance from the leading edge of the ramp in inches. The legend in the figures above indicates the actuator height in the MTS reading (raw reading from the MTS software). The bold black \* indicates the location of the leading edge of the shock-train from the schlieren video. They are put on the same plot to confirm if a match at the pressure data and visual data.

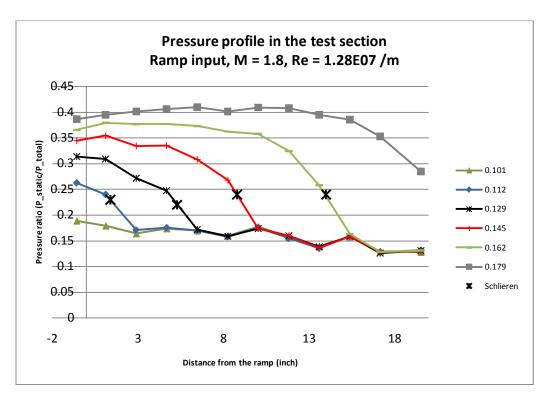


Figure 52. Pressure profile in the test section with ramp input, M=1.8, Re=1.28E07 /m

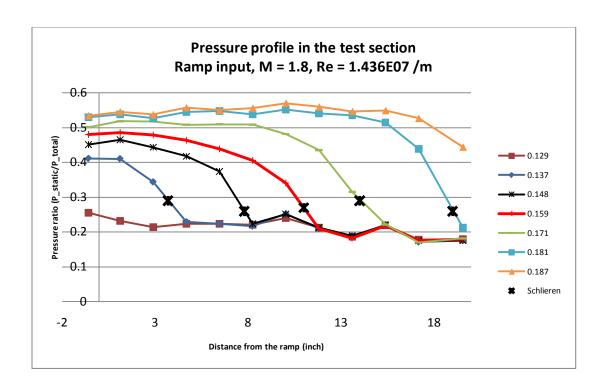


Figure 53. Pressure profile in the test section with ramp input, M=1.8, Re=1.436E07 /m

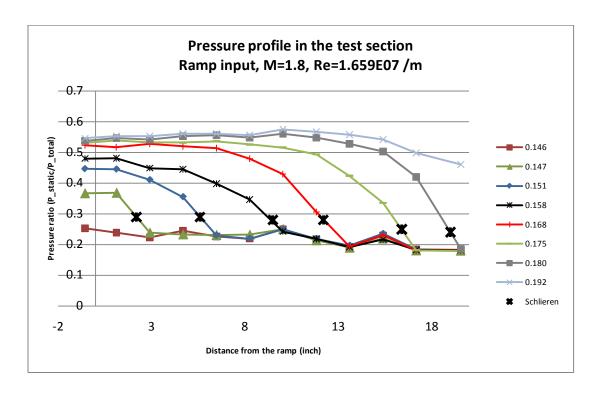


Figure 54. Pressure profile in the test section with ramp input, M=1.8, Re=1.659E07 /m

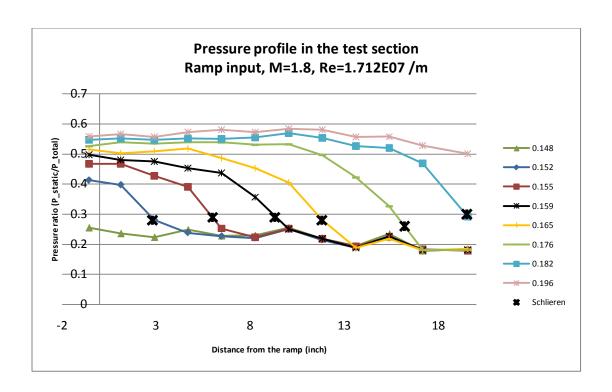


Figure 55. Pressure profile in the test section with ramp input, M=1.8, Re=1.712E07 /m

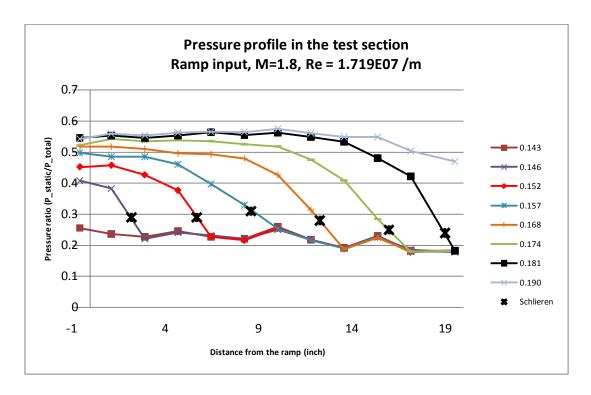


Figure 56. Pressure profile in the test section with ramp input, M=1.8, Re=1.719E07 /m

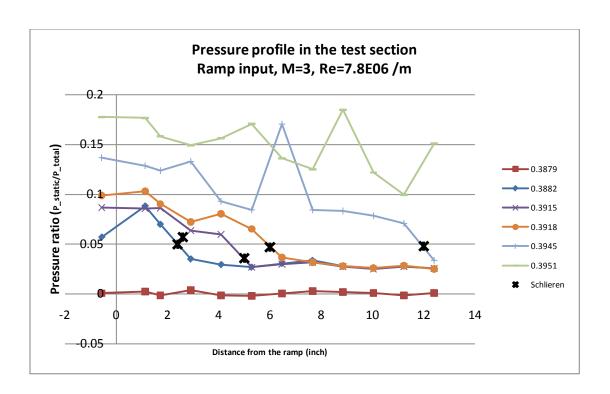


Figure 57. Pressure profile in the test section with ramp input, M=3, Re=7.8E06/m

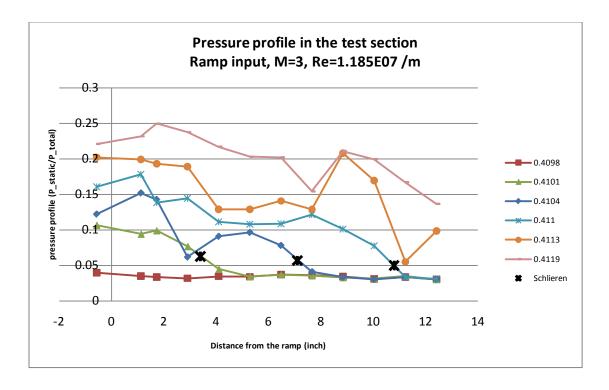


Figure 58. Pressure profile in the test section with ramp input, M=3, Re=1.185E07 /m

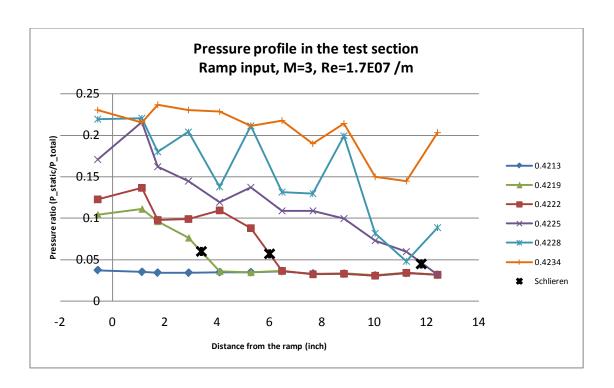


Figure 59. Pressure profile in the test section with ramp input, M=3, Re=1.7E07 /m

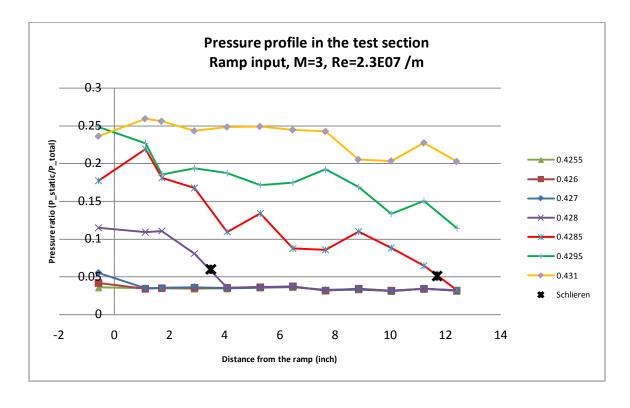


Figure 60. Pressure profile in the test section with ramp input, M=3, Re=2.3E07 /m

To note, actual data has more lines in the graphs, but a few of them are shown in Figure 52 through Figure 60 to help read the graph easier. Similar to the static test, one notices that the Mach 1.8 incoming flow case had stable shock-train locations with certain ramp heights throughout the test section as seen in the Figure 52 through Figure 56. In Figure 52 through Figure 56, the shock-train moves forward smoothly as the ramp height increases. On the other hand, with Mach 3 incoming flow, the shock-train had only a few stable locations and became unstable beyond a duct height 4 or 5. The shock-train's motion from one stable location to the next was very irregular, sudden, and jumpy. The higher Mach air flow seems to be very noisy or oscillatory and this behavior drives the flow unstable without much effort. From the schlieren video, the shock-train leading edge was oscillating in a flow direction within 0.1 - 0.2 duct heights for Mach 1.8 tests and within 0.2 - 0.4 duct heights for Mach 3 tests.

Schlieren photography in Figure 61 and Figure 62show the shape of shock-train for two different Mach numbers.

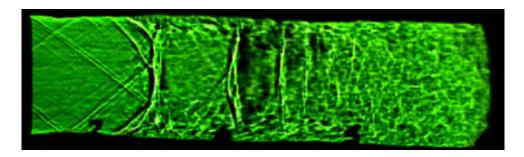


Figure 61. Schlieren photo of shock-train (M = 1.8, Re = 1.712 E07 / m, upstream is left)

At Mach 1.8, the shock-train in Figure 61 looks like a train of normal or bow shocks. In Figure 61, the numbers along the bottom of the picture indicate the distance from the ramp in terms of a duct height. From the pressure ratio data in Figure 52 thru

Figure 56, the Mach number after the shock-train is subsonic. Additionally, from static pressure, it can be noticed that the pressure ratio decreases towards downstream. This is indicative of frictional flow in a constant-area duct preceded by an isentropic nozzle (Fanno flow(26)). Subsonic flow in a constant-area duct preceded by an isentropic nozzle tends to speed up until it reaches sonic speed. The Mach number at the downstream end can be calculated using isentropic relationships with the stagnation pressure and temperature. In this test condition, the Mach number where the back-pressure sensor is located is calculated to be Mach 0.958.

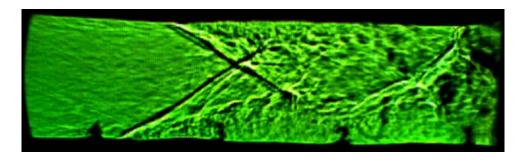


Figure 62. Schlieren photo of shock-train (M = 3, Re = 1.7 E07 / m, upstream is left)

Mach 3 flow in Figure 62 creates a shock-train with shallow angles, more like oblique shocks created by a wedge. Across each oblique shock, the Mach number drops and static pressure increases. The pressure ratio profiles in Figure 57 thru Figure 60 indicate that the air flow behind the shock-train is still supersonic and the pressure ratio increases towards the downstream. Again, this indicates Fanno flow behavior. The supersonic flow in a constant-area duct preceded by an isentropic nozzle tends to slow down until it reaches sonic speed.(26)

With Mach 1.8 incoming flow, the shock-train starts appearing at a smaller angle of the ramp; and with Mach 3 incoming flow, the shock-train starts appearing at a higher ramp angle. The detailed numerical values are tabulated below:

Table 2. Actuator height and % flow area at shock-train imminent and un-start

|      | MTS reading |           |             |          |       | Equivalent % flow area |          |      |
|------|-------------|-----------|-------------|----------|-------|------------------------|----------|------|
| Test | Mach        | Reynold's | Shock-train | un-start | Δh    | Shock-train            | un-start | Δ%Α  |
| No.  | #           | number    | imminent    |          |       | imminent               |          |      |
| 1    | 1.8         | 1.280 E07 | 0.104       | 0.181    | 0.077 | 95.99                  | 92.34    | 3.65 |
| 2    | 1.8         | 1.436 E07 | 0.131       | 0.187    | 0.056 | 94.78                  | 92.02    | 2.76 |
| 3    | 1.8         | 1.659 E07 | 0.147       | 0.190    | 0.043 | 94.03                  | 91.87    | 2.16 |
| 4    | 1.8         | 1.712 E07 | 0.149       | 0.192    | 0.043 | 93.93                  | 91.76    | 2.17 |
| 5    | 1.8         | 1.719 E07 | 0.146       | 0.187    | 0.041 | 94.08                  | 92.02    | 2.06 |
| 6    | 3           | 7.8 E06   | 0.387       | 0.395    | 0.008 | 78.98                  | 78.35    | 0.63 |
| 7    | 3           | 1.185 E07 | 0.410       | 0.412    | 0.002 | 77.17                  | 77.01    | 0.16 |
| 8    | 3           | 1.7 E07   | 0.422       | 0.424    | 0.002 | 76.21                  | 76.05    | 0.16 |
| 9    | 3           | 2.3 E07   | 0.427       | 0.429    | 0.002 | 75.81                  | 75.64    | 0.17 |

As shown in Table 2, at a lower Mach number, a shock-train starts at a smaller ramp angle and the height range from the shock-train imminent position to the un-start position is between 0.033 and 0.077 inches (in MTS reading). At a higher Mach number, the ramp has to be raised higher to start the shock-train and the range of the actuator height is only a few thousandths of an inch (in MTS reading). The shock-train is definitely more sensitive to the ramp angle (or back-pressure) in Mach 3 flow than in Mach 1.8 flow. In other words, small increases in the ramp angle can un-start the air flow at a higher Mach number.

Additionally, the Reynolds number plays a significant role here. At both high and low Mach flow, as the Reynolds number increases, the shock-train imminent position and the un-start position occurs at a higher ramp angle. Also, as the Reynolds number increases, the range of the actuator height from the shock-train imminent position to the un-start position decreases. The shock-train becomes more responsive to the ramp motion at the higher Reynolds number. See the Reynolds number effect section for more detail.

From Figure 52 to Figure 60, it might be interesting to look at the two farthest upstream sensors to find whether there is any precursor of a un-start. The graphs are drawn with the back-pressure ratio versus the pressure ratio from two farthest upstream pressure sensors and they are shown below.

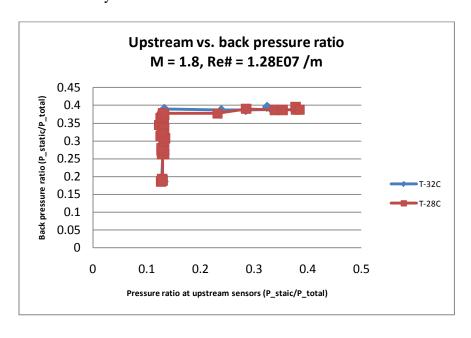


Figure 63. Upstream versus back-pressure ratio (M=1.8, Re# = 1.28E07 /m)

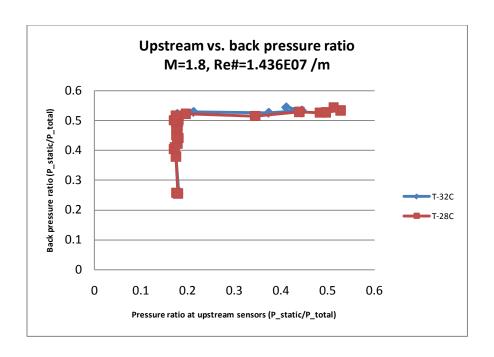


Figure 64. Upstream versus back-pressure ratio (M=1.8, Re# = 1.436E07 /m)

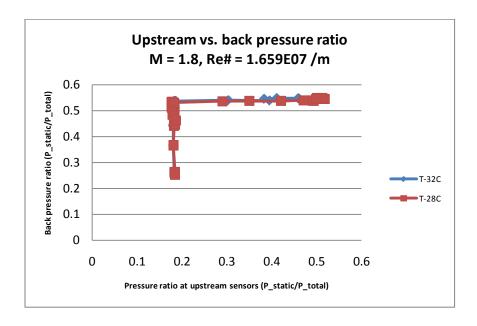


Figure 65. Upstream versus back-pressure ratio (M=1.8, Re# = 1.659E07 /m)

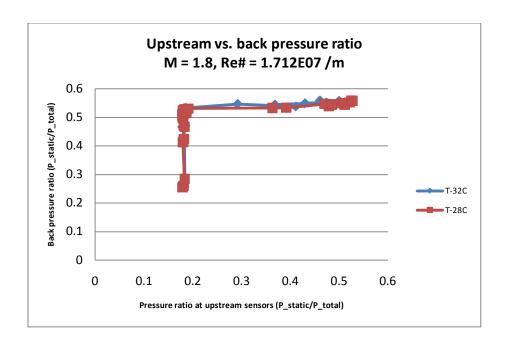


Figure 66. Upstream versus back-pressure ratio (M=1.8, Re# = 1.712E07 /m)

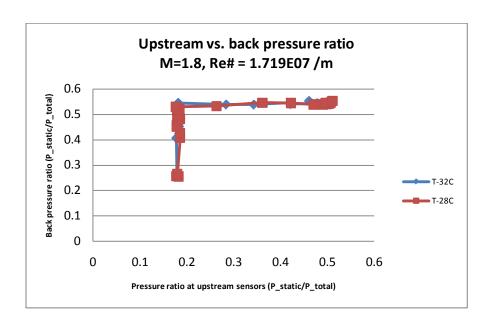


Figure 67. Upstream versus back-pressure ratio (M=1.8, Re# = 1.719E07 /m)

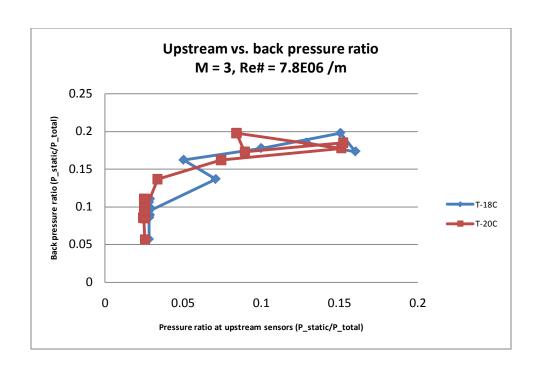


Figure 68. Upstream versus back-pressure ratio (M=3, Re# = 7.8E06 / m)

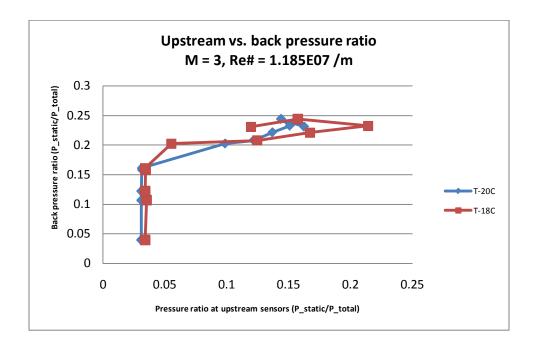


Figure 69. Upstream versus back-pressure ratio (M=3, Re# = 1.185E07 / m)

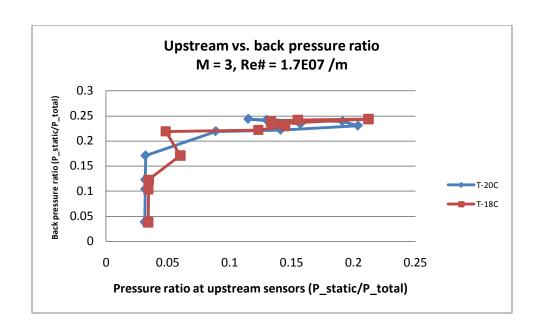


Figure 70. Upstream versus back-pressure ratio (M=3, Re# = 1.7E07 / m)

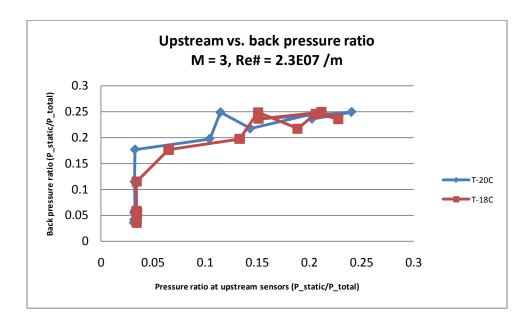


Figure 71. Upstream versus back-pressure ratio (M=3, Re# = 2.3E07 / m)

In a legend, for example, 'T-32C' means that the sensor is located on a top plate,  $32^{nd}$  sensor hole from the ramp along a center line. In Figure 63 through Figure 67, Mach 1.8 air flow shows that the two far upstream sensors show sudden pressure rise when un-

start occurs. These two relationships do not seem to be a good method to use as precursor of a un-start. From Figure 68 to Figure 71, Mach 3 air flow shows some oscillatory behavior at two far upstream sensors near the un-start point. The oscillation in pressure reading is due to the oscillation of the shock-train leading edge in a flow direction. The two far upstream sensors in Mach 3 flow seems ok to be used as early warning indicators, however, one thousandths movement of an actuator make the shock-train go from start to un-start in a very short time. Again, this method does not work in Mach 1.8 cases.

## **Hysteresis examination**

The next question was of hysteresis behavior. To determine hysteresis, a triangle voltage was input to the actuator, i.e., increasing ramp angle and followed by decreasing ramp angle. Because each test condition has different ramp heights where the un-start occurs and a different range of the actuator height from the shock imminent position to the un-start position, the triangle input was adjusted according to the test condition. The test conditions and the triangle inputs are shown below.

Table 3. Test conditions for hysteresis experiments

|      |      |          | Triangle input |              |           |          |  |  |
|------|------|----------|----------------|--------------|-----------|----------|--|--|
| Test | Mach | Reynolds | Freq           | Phase        | Amplitude | Offset   |  |  |
| No.  | #    | # (/m)   | (Hz)           | Offset (deg) | (MTS      | (MTS     |  |  |
|      |      |          |                |              | reading)  | reading) |  |  |
| 1    | 1.8  | 1.196E07 | 0.25           | 250          | 0.11      | 0.11     |  |  |
| 2    | 1.8  | 1.365E07 | 0.25           | 250          | 0.11      | 0.11     |  |  |
| 3    | 1.8  | 1.568E07 | 0.2            | 270          | 0.09      | 0.13     |  |  |
| 4    | 1.8  | 1.619E07 | 0.2            | 270          | 0.09      | 0.14     |  |  |
| 5    | 1.8  | 1.621E07 | 0.2            | 270          | 0.09      | 0.13     |  |  |
| 6    | 3    | 7.15E06  | 0.2            | 270          | 0.045     | 0.38     |  |  |
| 7    | 3    | 8.95E06  | 0.2            | 270          | 0.04      | 0.39     |  |  |
| 8    | 3    | 1.419E07 | 0.2            | 270          | 0.04      | 0.4      |  |  |
| 9    | 3    | 1.895E07 | 0.2            | 270          | 0.05      | 0.4      |  |  |
| 10   | 3    | 2.212E07 | 0.2            | 270          | 0.05      | 0.4      |  |  |

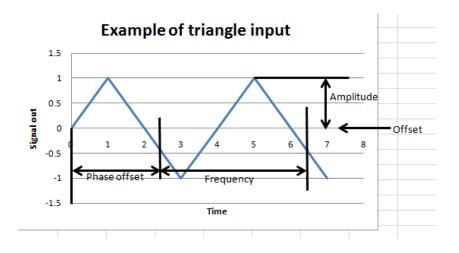


Figure 72. Triangle input explanation

In Table 3, the frequency means the 1/(period time), the phase offset is where the triangle input starts, the amplitude means the peak value, and the offset means the center of the triangle input as shown in Figure 72.

The results are shown below. The x-axis is the run time and the y-axis is the pressure ratio for three sensors (downstream, upstream, and back-pressure sensors). Also, the y-axis is shared with the actuator height in inches (MTS reading). As the ramp rises, the green graph (back-pressure) responds first, and then the downstream sensors see that the shock-train is imminent. As the ramp increases, the upstream sensor sees a shock-train propagating forward and pressure reading peaks. As the ramp lowers (purple graph), the upstream sensor sees the shock-train moving back. Then, the downstream and back-pressure sensors see that the shock-train is near the ramps and disappears.

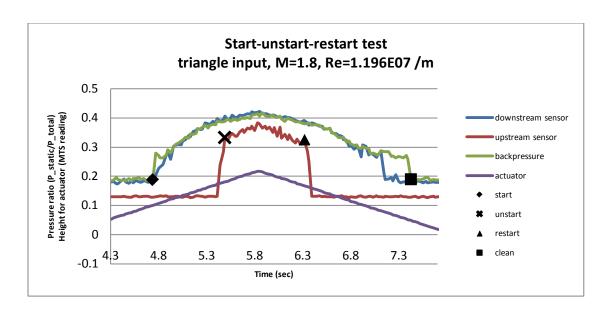


Figure 73. Shock-train start/un-start/restart/clean behavior in response to triangle input (M=1.8, Re=1.196E07 /m)

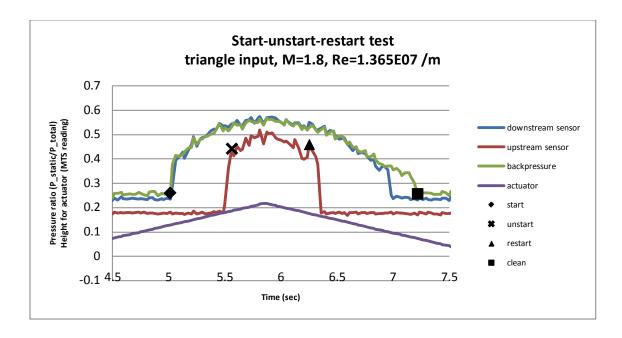


Figure 74. Shock-train start/un-start/restart/clean behavior in response to triangle input (M=1.8, Re=1.365E07 /m)

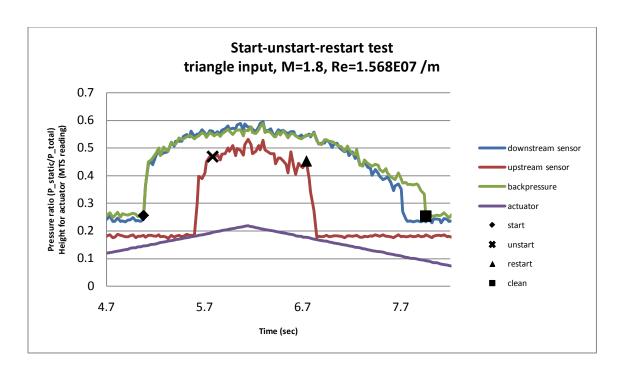


Figure 75. Shock-train start/un-start/restart/clean behavior in response to triangle input  $(M=1.8,\,Re=1.568E07\,/m)$ 

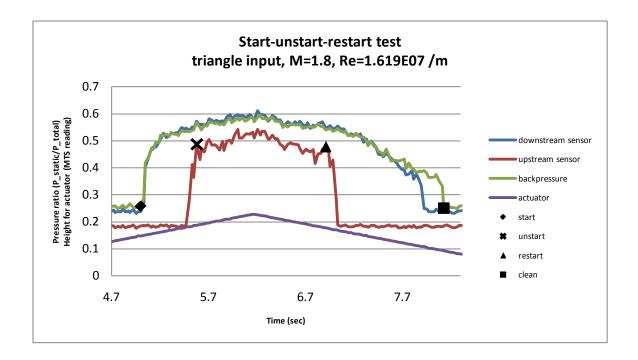


Figure 76. Shock-train start/un-start/restart/clean behavior in response to triangle input (M=1.8, Re=1.619E07 /m)

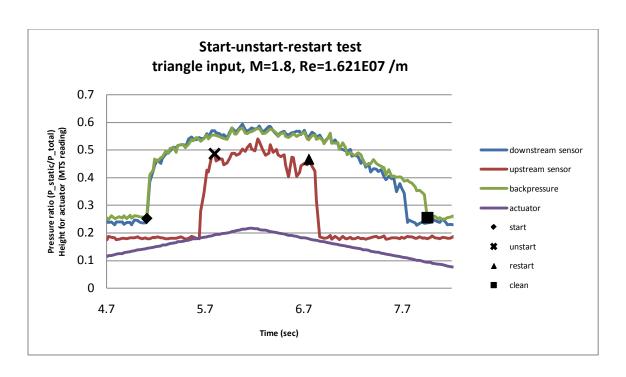


Figure 77. Shock-train start/un-start/restart/clean behavior in response to triangle input  $(M=1.8,\,Re=1.621E07\,/m)$ 

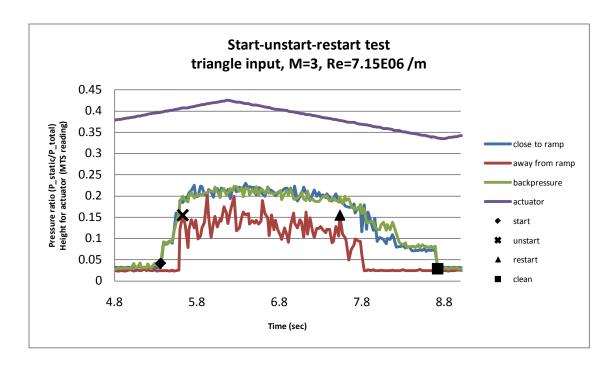


Figure 78. Shock-train start/un-start/restart/clean behavior in response to triangle input

$$(M=3, Re=7.15E06 / m)$$

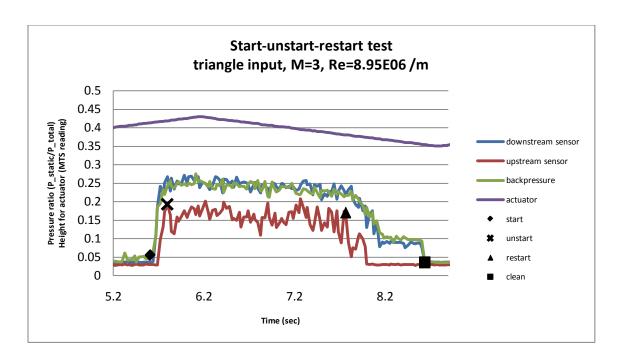
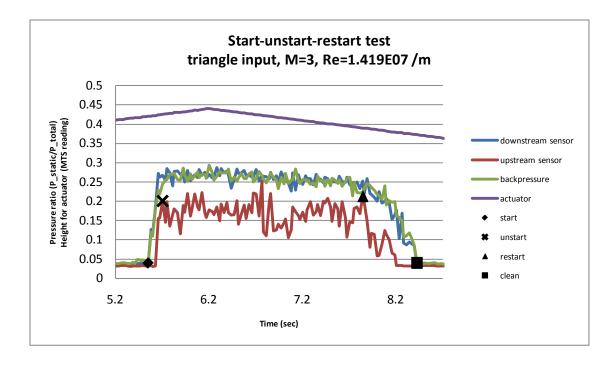


Figure 79. Shock-train start/un-start/restart/clean behavior in response to triangle input  $(M=3,\,Re=8.95E06\,/m)$ 



Figure~80.~Shock-train~start/un-start/restart/clean~behavior~in~response~to~triangle~input

$$(M=3, Re=1.419E07 / m)$$

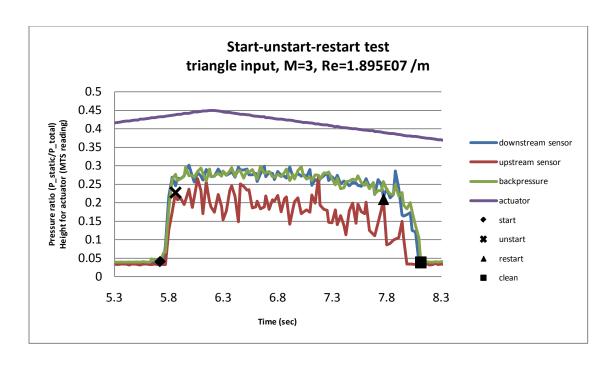


Figure 81. Shock-train start/un-start/restart/clean behavior in response to triangle input (M=3, Re=1.895E07 /m)

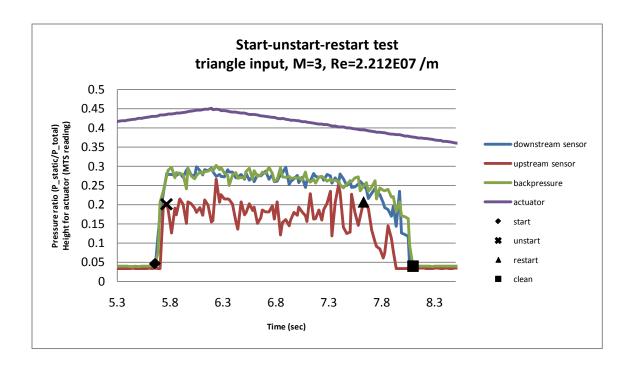


Figure 82. Shock-train start/un-start/restart/clean behavior in response to triangle input (M=3, Re=2.212E07 /m)

A speed of a triangle input signal to the actuator was slower for Mach 3 tests because it took only a few thousandths of inches of actuator height from a shock-train imminent to a un-start position. Going slowly from a shock-train imminent to a un-start was desired. This explains why the time difference from a un-start to restart position was longer in Mach 3 tests.

For the Mach 1.8 tests, the downstream sensor was placed at 1.1281 inches upstream of the leading edge of the ramp and the upstream sensor was placed at 19.5421 inches from the leading edge of the ramp, the furthest location where a sensor can be physically located.

For Mach 3 tests, the downstream sensor was placed at 1.1281 inches upstream of the leading edge of the ramp. The upstream sensor was placed at 12.4141 inches (approximately 5 duct heights) from the leading edge of the ramp since the un-start occurs when the shock-train reaches around 4 or 5 duct height for Mach 3 case. For both the Mach 1.8 and 3 cases, the back-pressure sensor is located on the side wall between the ramps (0.5636 inches downstream from the leading edge of the ramp).

From the Figure 78 thru Figure 82 above, the pressure data in Mach 3 flow was more noisy or oscillatory compared to the Mach 1.8 cases. This oscillatory behavior also can be observed in the schlieren video.

As can be seen in the Figure 73 and Figure 82, the un-start ramp heights are not the same as the restart ramp heights. The black X indicates where un-start occurred, and the black triangle indicates where restart occurred. At those points, the reading from the actuator (triangle shape graph) shows that the un-start height is slightly higher than the restart height. Similarly, the points where the shock-train starts (diamond mark) and

where it goes back to shock free (square mark) are not the same height, i.e., the shock-train starting point is higher than the clean (or shock free) point. This phenomenon can be observed in all the graphs above. So, there is a hysteresis in this shock-train behavior. The numerical values of the actuator height are shown in the Table 4 below.

Table 4. Start/un-start/restart/clean height summary

|             |           |                    | Actuator Height (MTS reading) |          |         | ΔH  (MTS reading) |                     |                       |                    |                  |
|-------------|-----------|--------------------|-------------------------------|----------|---------|-------------------|---------------------|-----------------------|--------------------|------------------|
| Test<br>No. | Mach<br># | Reynolds<br># (/m) | start                         | un-start | restart | clean             | start -<br>un-start | un-start -<br>restart | restart -<br>clean | clean -<br>start |
| 1           | 1.8       | 1.196E+07          | 0.101                         | 0.181    | 0.168   | 0.049             | 0.08                | 0.013                 | 0.119              | 0.052            |
| 2           | 1.8       | 1.365E+07          | 0.129                         | 0.187    | 0.175   | 0.073             | 0.058               | 0.012                 | 0.102              | 0.056            |
| 3           | 1.8       | 1.568E+07          | 0.146                         | 0.194    | 0.177   | 0.092             | 0.048               | 0.017                 | 0.085              | 0.054            |
| 4           | 1.8       | 1.619E+07          | 0.148                         | 0.187    | 0.178   | 0.093             | 0.039               | 0.009                 | 0.085              | 0.055            |
| 5           | 1.8       | 1.621E+07          | 0.145                         | 0.192    | 0.178   | 0.095             | 0.047               | 0.014                 | 0.083              | 0.05             |
| 6           | 3         | 7.150E+06          | 0.397                         | 0.407    | 0.378   | 0.337             | 0.01                | 0.029                 | 0.041              | 0.06             |
| 7           | 3         | 8.950E+06          | 0.413                         | 0.419    | 0.381   | 0.355             | 0.006               | 0.038                 | 0.026              | 0.058            |
| 8           | 3         | 1.419E+07          | 0.42                          | 0.425    | 0.39    | 0.373             | 0.005               | 0.035                 | 0.017              | 0.047            |
| 9           | 3         | 1.895E+07          | 0.433                         | 0.438    | 0.39    | 0.377             | 0.005               | 0.048                 | 0.013              | 0.056            |
| 10          | 3         | 2.212E+07          | 0.431                         | 0.435    | 0.395   | 0.377             | 0.004               | 0.04                  | 0.018              | 0.054            |

From the numerical results, a small height change will cause the flow to go from start to un-start. But when it goes back from restart to clean, a significant change in height of the actuator is required.

In Figure 78 and Figure 79, the back-pressure oscillates a little before the shock-train initiates. The common parameter among those two test conditions is the low Reynolds number, i.e., below 10<sup>7</sup>/m. Nonetheless, the upstream pressure readings do not show any un-start precursor. For example, let's look at only the upstream pressure readings from Figure 76 and Figure 82. The following graphs show the zoomed-in view of the upstream pressure reading prior to the un-start.

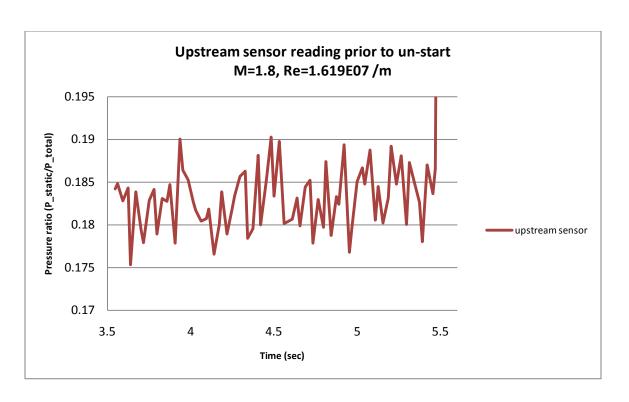


Figure 83. Upstream pressure reading prior to un-start (M = 1.8, Re# = 1.619E07 / m)

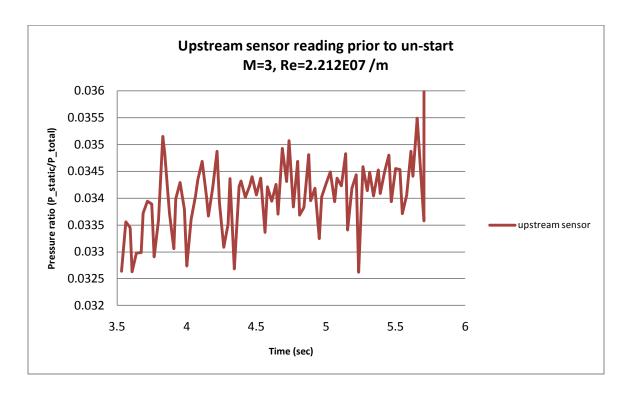


Figure 84. Upstream pressure reading prior to un-start (M = 3, Re# = 2.212E07 / m)

As shown in Figure 83 and Figure 84, the upstream pressure readings do not show any energy content changes prior to the un-start. As far as the frequency content changes are concerned, more jagged lines can be observed from Figure 84 prior to the un-start. But, the data sampling rate was limited to a low number, so it is hard to determine the precursor of un-start from this data.

Figure 85 shows the back-pressure ratio ( $P_{BP}/P_{TOTAL}$ ) versus the actuator height in MTS reading.

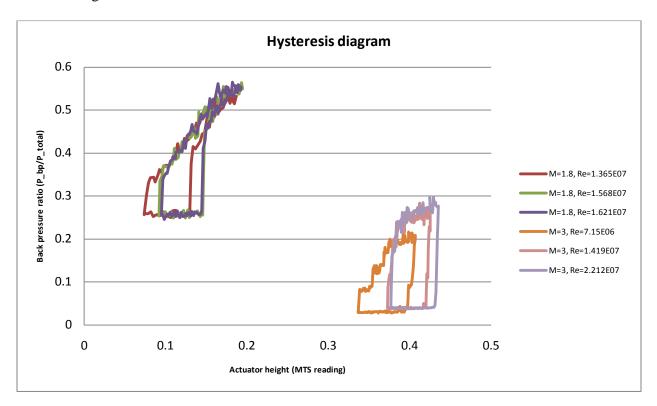


Figure 85. Comparison of hysteresis diagram of shock-train

As be seen in Figure 85, a trapezoidal shaped hysteresis graph formed from the data used to create Figure 73 through Figure 82 describes the shock-train behavior with respect to actuator height. The bottom right corner of the trapezoid is the shock-train imminent (start) position. The back-pressure rises towards the top right corner of the

trapezoid (un-start), then proceeds to top left (restart), and decreases to the bottom left corner for the shock free condition (clean).

In Figure 85, at Mach 1.8, the start and clean points occur at a back-pressure ratio of  $\sim$ 0.25, and un-start and restart occurs at a back-pressure ratio of  $\sim$ 0.55. At Mach 3, the hysteresis loop occurs at lower back-pressure ratio and higher actuator height. At Mach 3, start and clean occur at a back-pressure ratio of  $\sim$ 0.04, and un-start and restart occurs at the back-pressure ratio of  $\sim$ 0.28. One sees that the lines going from start to un-start and from restart to clean, i.e., the slant vertical lines in the hysteresis graph, vertical lines are steeper for Mach 3 than for Mach 1.8. In Mach 3 flow, the back-pressure increase per actuator height increase ( $\Delta P_{BP}/\Delta h_{act}$ ) is greater.

Once again, the Reynolds number effect can be seen here. As the Reynolds number increases, it tends to move the graph toward the top right corner, i.e., towards higher back-pressure ratio and higher actuator height. The Reynolds number effect is explained more in the Reynolds number effect section later on the report.

### Ramp speed effect

Because applying the constant increase in actuator height or the triangle wave input creates a non-static state (although it is a very slow increase called quasi-static here), one cannot ignore the dynamic effects of the ramp. For this investigation, the Mach number and the Reynolds number were fixed while the rate of increase in actuator height was varied. The test conditions are as follows.

Table 5. Test conditions for ramp slope effect experiments

| Test | Mach | Reynolds | Ramp slope        |
|------|------|----------|-------------------|
| No.  | #    | # (/m)   | (MTS reading/sec) |
| 1    | 1.0  | 1 200007 | 0.088             |
|      | 1.8  | 1.389E07 |                   |
| 2    |      |          | 0.22              |
| 3    |      |          | 0.088             |
|      | 1.8  | 1.628E07 |                   |
| 4    |      |          | 0.22              |

The test results are shown in the Figure 86 and Figure 87 below.

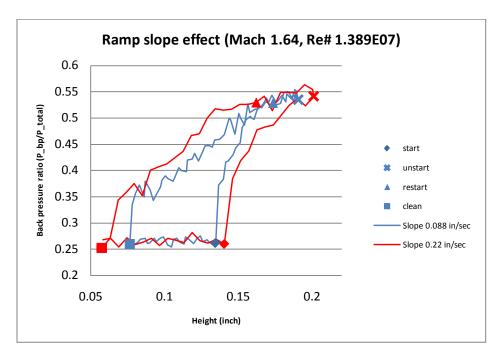


Figure 86. Ramp slope effect in hysteresis graph (M=1.8, Re=1.389E07 /m)

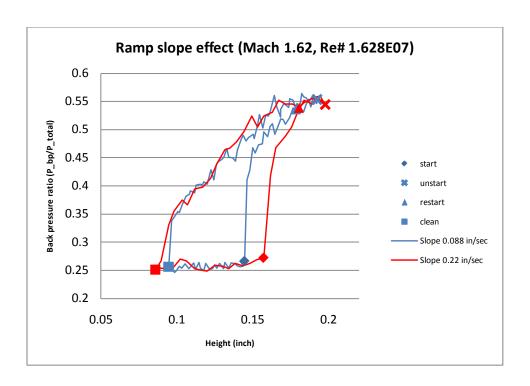


Figure 87. Ramp slope effect in hysteresis graph (M=1.8, Re=1.628E07 /m)

In Figure 86 and Figure 87, increasing ramp speed causes the hysteresis loop to be wider in the x-direction. That is, the clean and restart occurs at a lower height of the actuator and the start and un-start occurs at a higher actuator height. Thus, there is a lag or delay behavior in the shock-train's movement in relation to ramp angle changes.

# Reynolds number effect

The Reynolds number has an important effect on the behavior of the shock-train. Figure 73 through Figure 82 are re-drawn for the Reynolds number versus back-pressure ratio in Figure 88 and Figure 89 below.

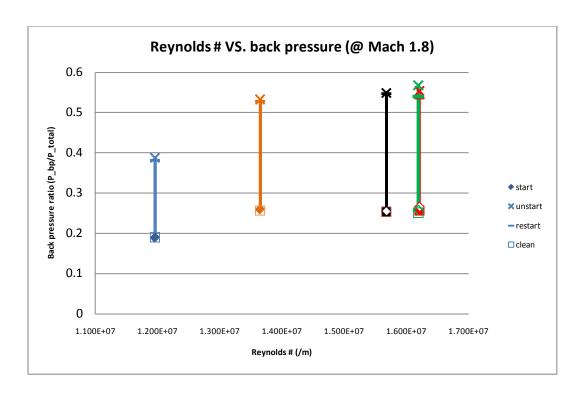


Figure 88. Reynolds number effect at M=1.8

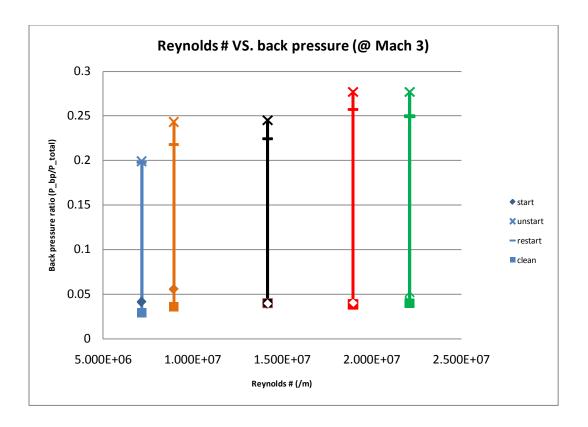


Figure 89. Reynolds number effect at M=3

The higher Reynolds numbers causes the un-start points to occur at a higher backpressure; on the other hand, the start point does not seem to be affected as much.

## Non-dimensionalization

In Figure 85, one can see two groups of graphs with respect to their Mach numbers. Mach 1.8 graphs are in the upper left region of the chart and the Mach 3 graphs are in the lower right region of the chart.

The ratio of Mach number in the test section at the shock free condition compared to the Mach number at the back-pressure location at any other condition eliminates the Mach number effect and groups the graphs together. The Mach number in the test section at shock free condition is constant, but the Mach number at the back-pressure

location for any condition throughout a run depends on ramp angle. The higher the ramp angle, the lower the Mach number, and vice versa. Two test conditions are selected: one for Mach 1.8 and a Reynolds number of 1.369E07 /m and the other for Mach 3 and a Reynolds number of 1.419E07 /m. The Mach numbers are different but their Reynolds numbers are similar.

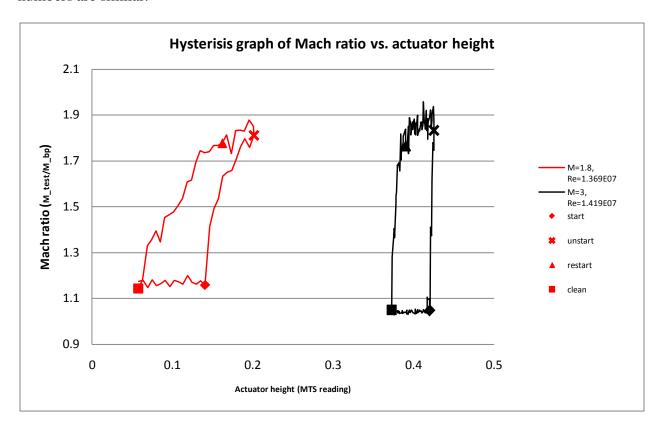


Figure 90. Hysteresis graph with Mach number ratio

Figure 90 shows that un-start occurs at a Mach number ratio of ~1.82 regardless of their Mach numbers, although start and clean points for the Mach 3 graph was a little lower than the Mach 1.8 graph. A next attempt was made to non-dimensionalize the x-axis. Rather than using the MTS reading, the difference in percent flow area is computed. Thus each value in x-direction (i.e., actuator height in the MTS reading) is

converted to the percent flow area using a conversion shown in Appendix E. The clean point (the square mark, lower left corner of the hysteresis graph) was set as a reference point. Any data point is expressed as the difference between the reference point and a given data point. Mathematically, it can be expressed as:

$$\Delta\% A_{flow,i} = \% A_{flow@clean} - \% A_{flow,i}$$
 Eqn. 1

After non-dimensionalizing the x-axis using the method above, Figure 78 shows results.

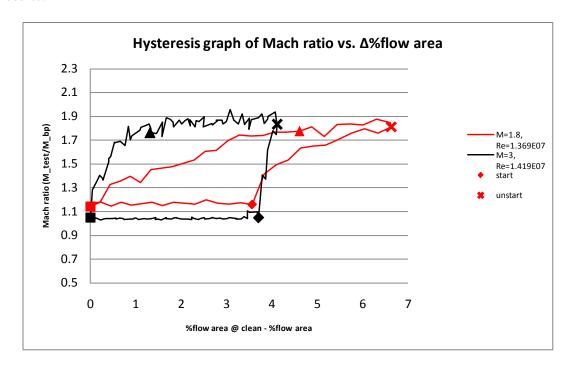


Figure 91. Hysteresis graph of Mach ratio vs. Δ% flow area

Figure 91 shows that un-start and restart occurs at near Mach number ratio of 1.83 and shock-train appears and disappears within the 7% of flow area change regardless of the Mach number for this specific test facility. The numerical value of Mach number ratio, however, would be affected by the physical length of the test section because of the Fanno flow phenomenon.(26) To compare all the test conditions for Reynolds number

effect, the hysteresis graphs of different test conditions were created and nondimensionalized by the method describe above. Figure 92 shows all the hysteresis graphs for the Mach 1.8 flow. Figure 93 shows all the hysteresis graphs for the Mach 3 flow. These are shown in Figure 94.

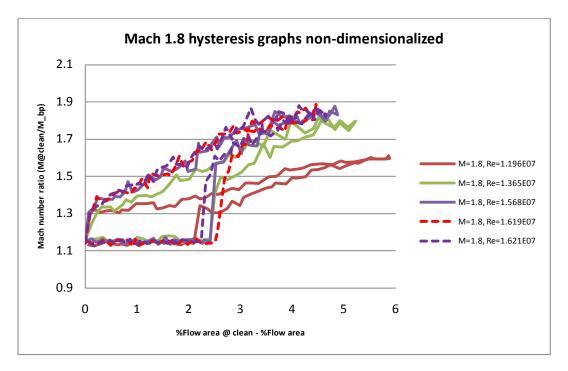


Figure 92. Mach 1.8 hysteresis graphs non-dimensionalized and combined

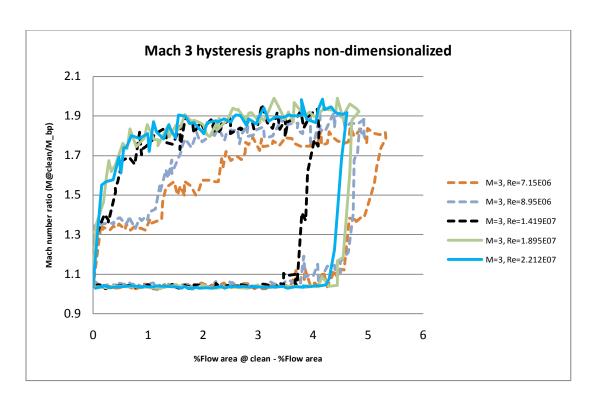


Figure 93. Mach 3 hysteresis graphs non-dimensionalized and combined

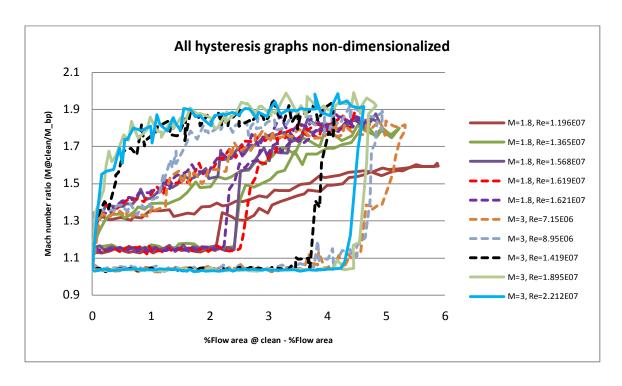


Figure 94. All hysteresis graphs are non-dimensionalized

In Figure 94, the Mach number ratio at the un-start points are between 1.8 and 1.95. The Mach number ratio at the start and clean points are approximately 1.03 for Mach 3 cases and 1.14 for Mach 1.8 cases. The bottom flat portions of the graphs for Mach 1.8 do not match with the one for Mach 3 because of two reasons.

First, the Mach number decreases as the flow travels in an adiabatic frictional constant-area duct due to the Fanno flow phenomenon. (26) It is interesting to calculate how much effect the Fanno line has here. The incoming Mach number toward the test section can be calculated using isentropic flow relationship with the total pressure and temperature at stagnation chamber and the static pressure at the test section. These values can be obtained by sensors. From this Mach number, the P<sub>1</sub>/P<sub>1</sub>\* can be found using the Table A4 in a 'Compressible Fluid Flow' book by Saad. (26) Here, subscript 1 indicates the upstream and 2 indicates the downstream. The L<sub>1</sub>\* can be calculated with the Equation 5.35 on page 201 in Saad's book. The  $L_2$ \* (L\* at downstream) is  $L_1$ \* subtracted by the physical distance between two sensors (one at  $L_1$ \* and the other at  $L_2$ \*). With the  $L_2^*$  value and a gamma of 1.4, the 4f  $L_2^*/D_H$  can be calculated, and then  $P_2/P_2^*$ can be found in the Table A4. Divide  $P_1/P_1^*$  by  $P_2/P_2^*$ , and then end up with  $P_1/P_2$ . Since the experimental data is the measured static pressure at both places, the experimental  $P_1/P_2$  is simply the static pressure ratio at those two locations. Next, compare the static pressure ratio of the Fanno line computation and the experimental data. For example, one of the Mach 3 tests shows that Fanno line computation yields  $P_1/P_2 =$ 0.87738, and the experimental data yields  $P_1/P_2 = 0.85467$ , in which case, their ratios are very close to each other. For a Mach 1.8 test, the Fanno line computation yields  $P_1/P_2$  = 0.86565, and the experimental data yields  $P_1/P_2 = 0.7625$ . The reason why the Mach 1.8

case showed a bigger difference is due to the dimension difference between the upstream nozzle and the test section, and this is explained in detail in the next a few paragraphs.

Second, the newly built test section front cross section area does not exactly match the back end of the nozzle cross section area. This small difference in interior cross section dimension trips the incoming supersonic flow and creates weak shocks off the little gap between them. The shocks travel down the test section. Even though those shock lines fade as they march downstream, the Mach lines affect and slow down the air flow. In Figure 95 and Figure 96, the schlieren pictures show the weak Mach lines diagonally across the test section area when the tunnel is clean. Mach 3 air flow has a shallower angle of oblique shock lines and Mach 1.8 air flow has a steep angle of oblique shock lines that form diamond shapes throughout the tunnel. These shock lines causes small errors and result in differences between experimental values and theoretical values.

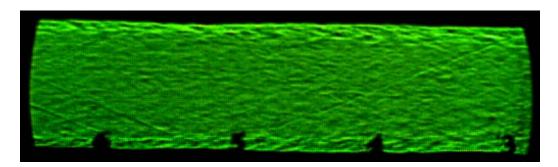


Figure 95. Clean run with Mach 3 nozzle

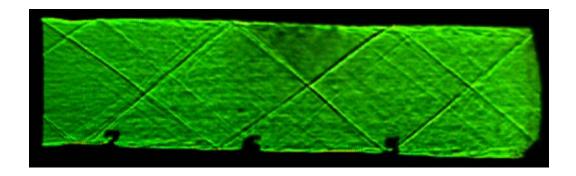


Figure 96. Clean run with Mach 1.8 nozzle

In Figure 94, the Reynolds number has a small effect. The higher Reynolds number tends to bring the hysteresis graphs a little higher, but not significantly.

In Figure 94, the graph with Mach 1.8 and Reynolds number 1.196E07 /m has its un-start point much lower than the other cases. The same data is also used to show the effect of the Reynolds number in Figure 88. The upstream control pressure was set at a very low pressure. When the tunnel was running, the upstream stagnation pressure dropped even more and the tunnel was slowing down. That is why the one low Reynolds number graph has lower pressure values than other graphs. The test condition was not ideal in that case.

In Figure 73 and Figure 82, the ramp speed was not set at the same rate. Table 3 shows the test condition. So the width of the hysteresis loop is irrelevant.

As a result, regardless of the Mach number of the incoming air flow, the un-start would happen when the Mach number ratio of the shock free to the back-pressure location is near 1.85 for this specific test section. The percent flow area change from shock free to un-start is less than 6%. The Mach number ratio of 1.85 would be different for other test facilities because the Mach number downstream depends on the length of the tube and the friction on the inside wall of the duct.

# Air flow symmetry test

This test investigates the integrity of the collected data, pressure sensor, and the test section, to help find any errors when analyzing the data. The eight test conditions are shown in Table 6.

Table 6. Test conditions for symmetry tests

| Test No. | Mach # | Test type                    | Reynolds # (/m) |
|----------|--------|------------------------------|-----------------|
| 1        | 1.8    | Top and bottom symmetry test | 1.427E07        |
| 2        |        |                              | 1.665E07        |
| 3        |        | Left and right symmetry test | 1.72E07         |
| 4        |        |                              | 1.773E07        |
| 5        | 3      | Top and bottom symmetry test | 1.692E07        |
| 6        |        |                              | 2.388E07        |
| 7        |        | Left and right symmetry test | 1.79E07         |
| 8        |        |                              | 3.025E07        |

Eight test conditions were executed. In all eight tests, the ramp was slowly raised to a height between the start and un-start positions to ensure shock-train was present during the symmetry runs. The results are shown in Figure 97 through Figure 104.

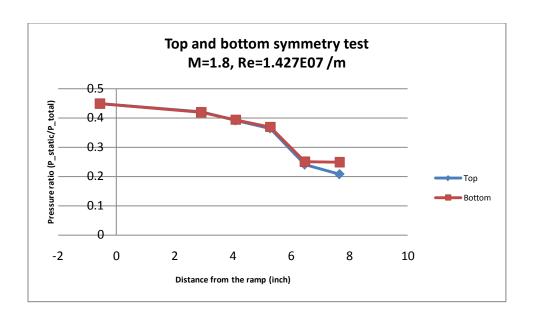


Figure 97. Top and bottom symmetry test (M=1.8, Re=1.427E07 /m)

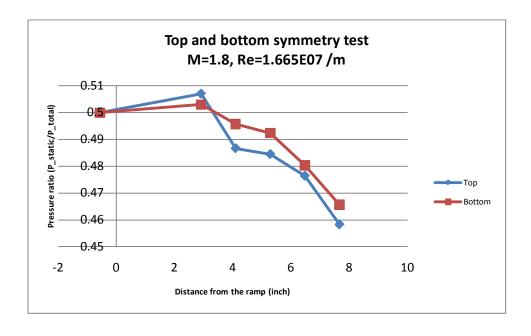


Figure 98. Top and bottom symmetry test (M=1.8, Re=1.665E07 / m)

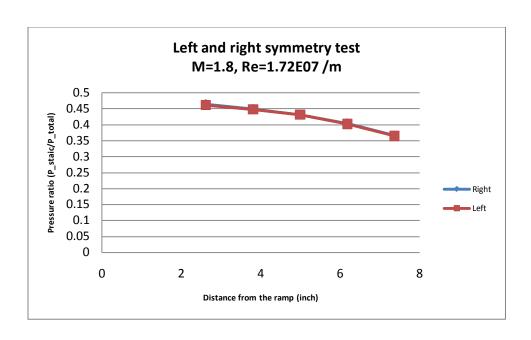


Figure 99. Left and right symmetry test (M=1.8, Re=1.72E07 /m)

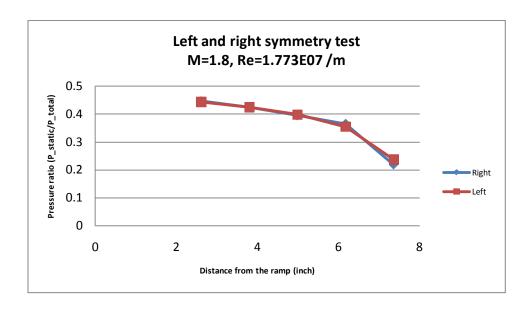


Figure 100. Left and right symmetry test (M=1.8, Re=1.773E07 /m)

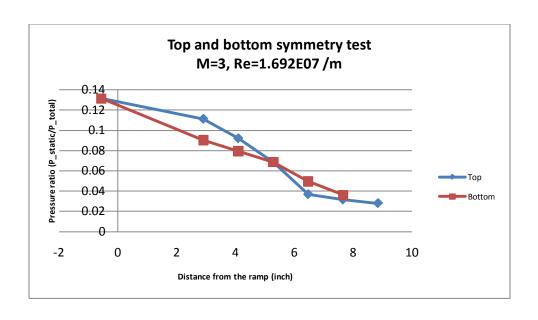


Figure 101. Top and bottom symmetry test (M=3, Re=1.692E07 /m)

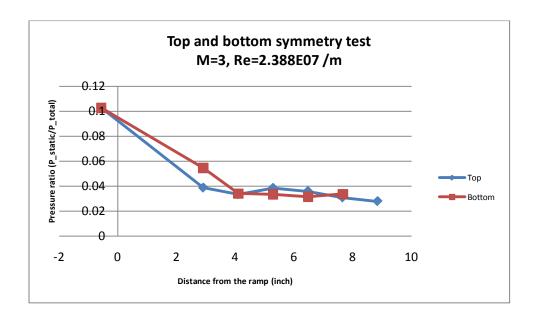


Figure 102. Top and bottom symmetry test (M=3, Re=2.388E07 /m)

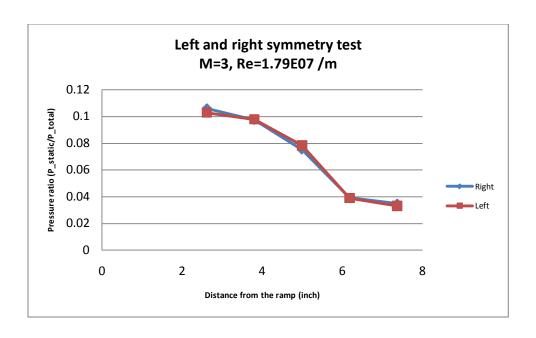


Figure 103. Left and right symmetry test (M=3, Re=1.79E07 /m)

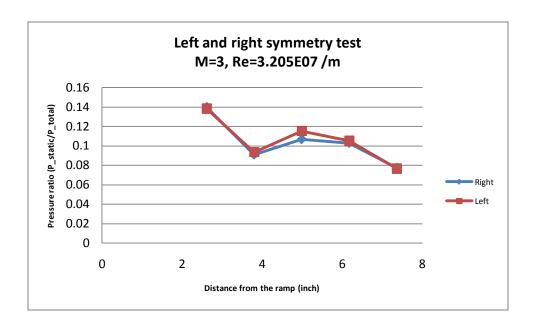


Figure 104. Left and right symmetry test (M=3, Re=3.205E07 /m)

In Figure 97 through Figure 104, the data are similar. The pressure ratio in the left and the right symmetry tests are nearly identical. From Figure 97 to Figure 104, a big

pressure rise or drop from one pressure sensor to the next one indicates that there is a shock between those two sensors. For example, in Figure 102, the big pressure difference between the second and third sensor from the left in the chart indicates that there is a shock-train leading edge presence. There are reasons for the minor differences in the top and bottom pressure readings. First, the upstream diffusing nozzle is not completely vertically symmetric. The Mach 3 nozzle is very asymmetric. It has a straight bottom and a diverging top. The Mach 1.8 nozzle is close to symmetric. To note, the exit flow uniformity from the inlet nozzle (i.e., incoming flow to the test section) was not investigated. The second reason is that the pressure data in Figure 97 through Figure 104 is time averaged. (PR = Pressure Ratio)

$$PR = \frac{Ave(\sum P_{static,i})}{Ave(\sum P_{total,i})}$$
 Eqn. 2

Because the shock-train always oscillates within 0.2 - 0.4 duct heights depending on the Mach number and Reynolds number, there were some fluctuations in the pressure data. Third, the sensor itself has some noise. In conclusion, the air flow inside the tunnel is reasonably symmetric and should not be a problem for data integrity.

#### Adding injection pressure upstream test

One question arose as to whether upstream injection would push the shock-train back in the downstream directions. Air was input by opening one of the upstream pressure sensor plugs to allow the room pressure to enter the test section area which is below room pressure when the tunnel is running.

The additional pressure raised the overall pressure throughout the test section, including the back-pressure, and caused the test section to un-start at a lower ramp height

than when the pressure was not added. According to the results in Figure 85, when the tunnel is shock free, the back-pressure ratio is 0.25 for Mach 1.8 and 0.05 for Mach 3 flow, and un-start occurs at back-pressure ratio of 0.55 for Mach 1.8 and 0.27 for Mach 3 flow. Adding pressure upstream raises the overall pressure inside the tunnel, so it does not take much for the ramp to raise the back-pressure to its un-start point. Therefore, the shock imminent and un-start points occur at lower actuator heights.

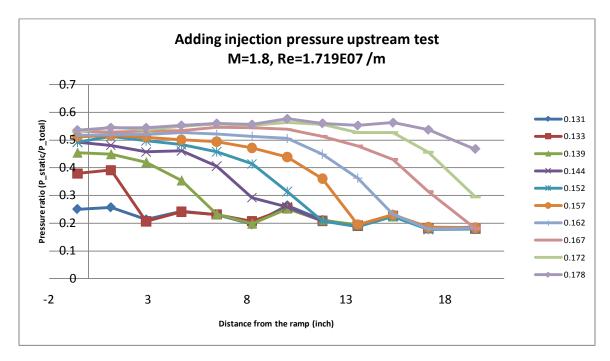


Figure 105. Results of adding pressure in upstream

As shown in Figure 105, adding pressure upstream causes the shock imminent point to occur at an actuator height of 0.131 and the un-start point to occur at an actuator height of 0.178 (in MTS reading). In Figure 56, without any additional pressure upstream, the shock imminent point occurred at a height of 0.149 and the un-start point occurred at a height of 0.191, which are higher values than the ones with injection.

In Figure 106, the injection pressure was added at approximately 6 ducts height away from the ramp on the top surface. As the atmospheric static air enters the test section, it encounters the supersonic flow and creates a shock wave. In Figure 106, two distinct oblique shocks from the open hole can be seen. The reason for two oblique shocks is that the actual shock wave is three dimensional. The wave upstream is the result of the leading edge of the curved shock and the second wave results from the outer edge of the curved shock. In Figure 106, the shock-train is at approximately 4.4 duct heights.

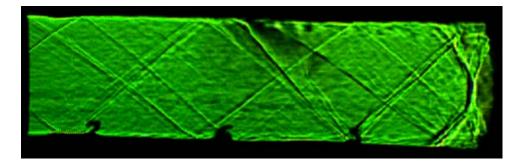


Figure 106. Schlieren image when the pressure added upstream

From work in the past, the shock-train can be made more stable by bleeding air out of the isolator because, by doing so the boundary layer will be thinned.

## **Comparison with other researches**

From a research paper, 'Characterization of Shock Train Structures inside Constant-Area Isolators of Model Scramjet Combustors,' by Lin et al., the x- and y-axis variables in their graphs are different from the ones in this report.(27) One of the graphs in their paper was the shock-train location in x-axis versus the static back-pressure divided by the static upstream-pressure in y-axis, which is a Figure 3(a) in their paper.

This graph was chosen for a comparison study because its flow speed is Mach 1.8, which is also tested in this experiment as well. Their Figure 3(a) is shown below.

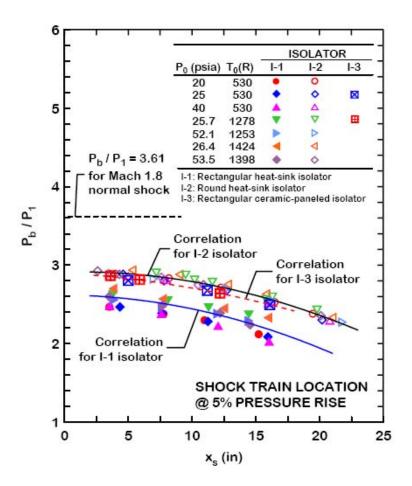


Figure 107. From Lin et al., shock-train locations for rectangular and round isolators at various back pressures in Mach 1.8 flow (27)

To compare with theirs, the result of the flow condition of Mach 1.8 and total pressure of 17 psia from this experiment was chosen. The graph is shown below in Figure 108.

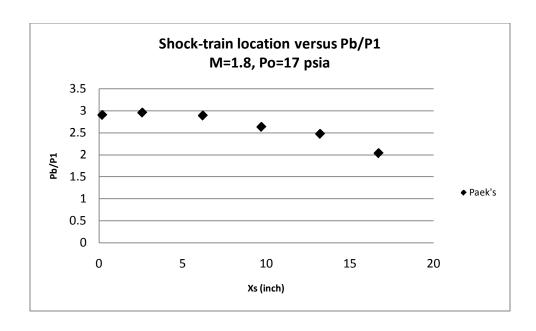


Figure 108. Shock-train location versus Pb/P1 in Mach 1.8 and Po=17psia

The next graph shows the Figure 107 and Figure 108 overlaid together for a better direct comparison. Black diamond symbols indicate Paek's data.

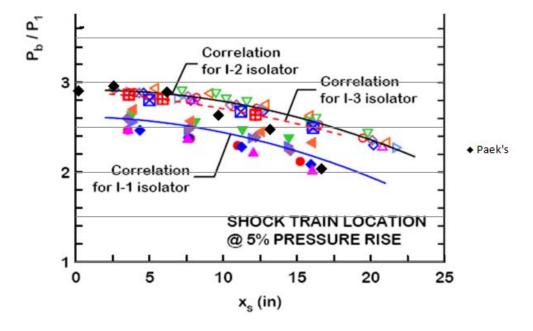


Figure 109. Comparison between Lin et al.'s and Paek

First of all, it is important to point out that the geometry of the cross section, an isolator length, and the surface roughness of Lin et al.'s isolators is different from Paek's. Nonetheless, those two data sets seem to agree with each other.

Since the Mach 3 flow was tested in this experiment, the same type of graph for Mach 3 flow was drawn and shown below. Since Lin et al. did not tested Mach 3 flow, no direct comparison can be made. Because the shock-train moved jumpy, sudden, and fast in Mach 3 flow case as the back pressure rose, there were a few stable shock-train locations recorded per one flow case. This explains a few data point in the Figure 110.

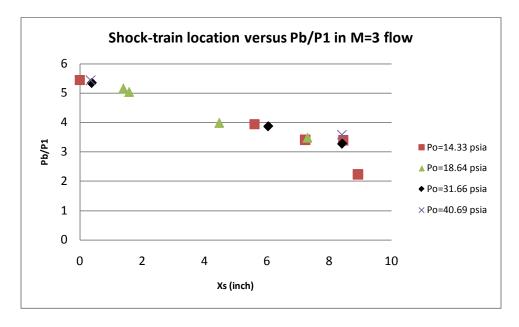


Figure 110. Shock-train location versus P<sub>b</sub>/P<sub>1</sub> in Mach 3 and P<sub>o</sub>=31.7psia

Additionally, one of Lin et al.'s graphs demonstrated the one common characteristic from all the data they gathered. The data uses a free-stream distance from shock leading edge  $(x' = x - x_s)$  in an x-axis and  $\left[\left(\frac{P_s}{P_o}\right) - \left(\frac{P_{s'}}{P_o}\right)\right] \frac{M_o^2}{(P_b/P_1)}$  in a y-axis. The nomenclatures are as follows.

 $M_o$  = nominal Mach number at the upstream nozzle exit

P = pressure

x = pressure transducer location

 $x_s$  = shock train leading edge location

x' = free-stream distance from shock leading edge,  $x'=x-x_s$ 

# Superscript

' = condition at shock leading edge

# Subscript

0 = total condition

1 = condition at the upstream nozzle exit

b = condition at extension piece exit

s = static condition

Their graph is shown in Figure 111 below.

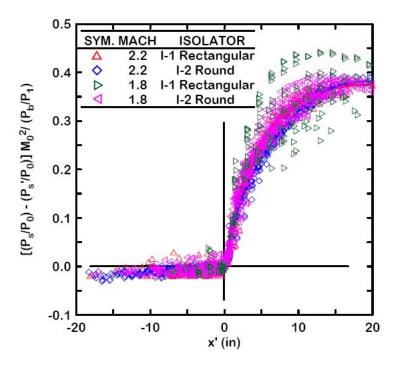


Figure 111. Lin et al.'s graph – shifted and normalized shock train pressure profiles for I
1 rectangular and I-2 round isolators in Mach 1.8 and 2.2 flow (27)

Using same x and y-axis as Lin et al., the data collected in this research was calculated and drawn on a chart. The graph is shown in Figure 112 and Figure 113 for Mach 1.8 and 3 cases respectively.

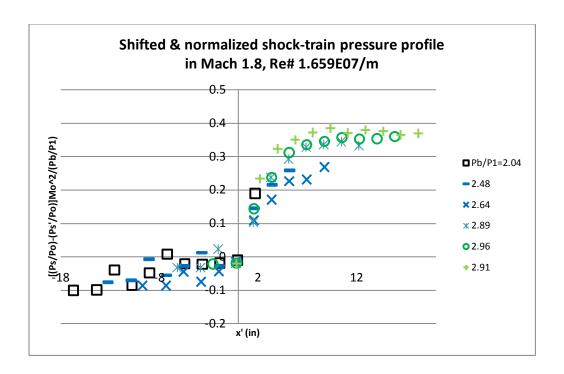


Figure 112. From this research – shifted and normalized shock train pressure profile for rectangular isolator in Mach 1.8

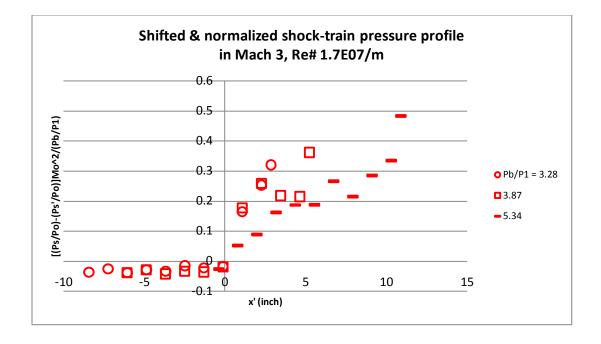


Figure 113. From this research – shifted and normalized shock train pressure profile for rectangular isolator in Mach 3

In Figure 113, one value (triangle symbol) peaks to  $P_b/P_1 \sim 0.5$  at  $\sim 12$  inch downstream from the shock-train leading edge. This is due to a great pressure fluctuation behind the shock-train at Mach 3 flow. As you can see in Figure 57 through Figure 60, the pressure profile behind the shock-train leading edge is very jagged. Lin et al. did not test at Mach 3 flow; therefore, this jagged pressure profile cannot be seen in their graphs.

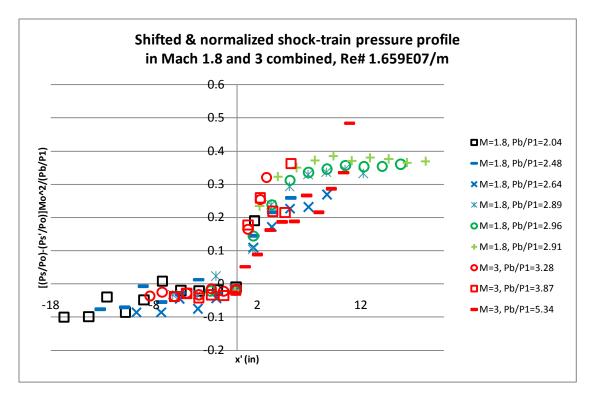


Figure 114. From this research – shifted and normalized shock train pressure profile for rectangular isolator in Mach 1.8 and 3 combined

One difference to notice in Figure 114 from Lin et al.'s graph is the amount of scatterings of the data in an upstream of the shock-train. In Lin et al.'s graph, the value in an upstream of the shock-train was between -0.03 and 0.03. The Paek's graph has a range of the values from -0.1 to 0.03. However, the values in a downstream of the shock-

train seem alike. Again, it is important to keep in mind that the geometry of the Lin et al.'s isolator is different from that of Paek's.

#### V. Conclusions and Recommendations

#### **Conclusions of Research**

From the conceptual idea to designing the experiment and its facility, to fabricating the test facility, and then to executing the experiments, there were a lot of findings. Designing a test section allowed abundant learning opportunities. Learning new software, Solidworks, and working with machine shop showed another side of engineering. During this process, continuous communication with machine shop experts accelerated the fabrication process and solved any type of design challenge.

While working on the design in the Solidworks, many engineering analyses were required. Material strength and stress/strain computation were required. As a result, the wind tunnel test section window thickness and its deflection with a respect to the pressure acting on it were calculated.

Once the test section was delivered and completely built, the experiment took place right away. The first phase of the experiment started with a fixed ramp position. This method can only yield useful data when test condition is away from the un-start condition. In other words, the results when the ramp was already raised were slightly different from when the ramp was introduced after the air flow was run and stabilized. It was important to stabilize air flow before introducing any objects into the test section.

In Mach 3 flow, the shock-train can be stable up to 4 or 5 duct heights from the ramp. Beyond this point, the shock-train was not stable at one location, rather it propagated forward. On the other hand, the Mach 1.8 flow was stable all the way up to the entrance of the test section, i.e., 7 or 8 duct heights. Also, in the higher Reynolds

number flows, the shock-train was more unstable and un-start would occur with a slight increase in the ramp height. The lower the Mach number, the more stable the shock-train. The lower the Reynolds number, the lower ramp height required to start the shock-train.

When changing a ramp input signal to the actuator during a run, data could be collected at one run, but this method introduced a quasi-static state. While the ramp was slowly raised, the shock imminent point, the un-start point, and the back-pressure values at those times were easily observable. At a lower Mach number, a smaller ramp angle started the shock-train and the range of actuator height from the shock imminent point to the un-start point was not as small. At a higher Mach number, a higher ramp angle was required to start the shock-train, and from there, a smaller angle increase caused the test section to un-start. A higher Mach number had a smaller ramp angle range when going from the shock imminent point to the un-start point compared to the lower Mach number. The flow Reynolds number also played a part. Similar to the Mach number effect, for a higher Reynolds number, the shock imminent point and the un-start point occurred at a higher ramp angle. Additionally, the range of the ramp angle from the shock imminent point to the un-start point decreased.

A triangle input signal to the actuator revealed important shock-train behavior. When the ramp was raised and lowered, the shock-train appeared, un-started, restarted, and disappeared. The most important discovery was that the ramp height at the un-start was not same as the height at restart. The height at the restart point was lower than that at the un-start point. In other words, there was a hysteresis in the aerodynamics of the shock-train movement. The back-pressure ratio versus actuator height showed a distinctive trapezoidal shape of the hysteresis. This hysteresis was also influenced by the

Mach number and Reynolds number. Where the back-pressure ratio is the y-axis and the actuator height is the x-axis, the higher Mach number moved the hysteresis graph to the bottom right corner, and the higher Reynolds number moved the hysteresis graph to the top right corner on the chart.

On dynamic runs, even though the ramp was very slowly moving up or up/down, the dynamic effect of the ramp cannot be ignored. Different ramp speeds were varied to observe the behavior of the shock-train. Surprisingly, faster ramp movement widened the hysteresis graph in x-direction, i.e., actuator height. This showed another non-linearity in the shock-train system: time delay between the ramp position and the shock train location changes. A further study of dynamic behavior of the shock-train is required to analyze on this delay behavior.

The coordinate system with a back-pressure ratio on the y-axis and the actuator height on the x-axis located the graph in several places depending on their Mach numbers. However, the Mach number ratio (Mach number at shock free condition to the Mach number at the back-pressure location) as a function of actuator height normalized the data. Also, the x-axis can be non-dimensionalized using the  $\Delta\%$  flow area. This non-dimensionalization put all the graphs together with a slight variation depending on the Reynolds number. For this test facility, the Mach number ratio at the un-start point, regardless of the incoming Mach number, was near 1.85. This value would be different for a different test facility due to the dimensions of the duct.

Air flow inside the test section was found to be reasonably symmetric according to the symmetry test. It is found that, when injecting pressure upstream of the shock-train,

the shock imminent point and the un-start point occurred at a lower ramp height and made the shock-train system more unstable.

### **Significance of Research**

The non-linearity of the aerodynamics of a shock train was discovered through quasi-static tests. When applying a triangle input to the actuator, it was observed that the un-start point was not the same as the restart point. The ramp height at the restart point was actually lower than that at the un-start point. Through this experiment, hysteresis graphs were created and hysteresis behavior was clearly noticeable.

Another non-linearity observed was the delay in the shock train system when the ramp speed was changed. This delay non-linearity widened the hysteresis graph in x-direction, i.e., actuator height. These two non-linear behaviors of the shock train emphasized the importance of further study of the dynamics of the shock train prior to building a feedback loop control system.

#### **Recommendations for Future Research**

When doing the experiment with the Mach 1.8 nozzle, the shock train was stable throughout the test section. One could not find a point where the shock train becomes unstable. A longer test section would be required to find the static unstable point.

Currently, in this laboratory, there are two different diverging nozzles. One nozzle produced approximately Mach 1.8 and the other produced approximately Mach 3 flow. Both nozzles were used throughout this research. It would be interesting to test with a Mach number somewhere between, e.g., Mach 2.4. Data collected with a Mach

2.4 nozzle would provide missing data between the two Mach numbers and present a better picture of Mach number effects.

The focus of this research was to investigate the static relationship of the backpressure versus the shock train location. During this research, it was apparent that
applying varying ramp inputs to the actuator while running tests created dynamic effects.

Even though only a small portion of the dynamic study was touched on here, some
important information about non-linearity was noted. It was strongly suggested that
further study into shock train dynamics should be done before designing a feedback
control system.

There were eleven pressure sensors available for test section measurement.

Because the number of sensors was less than the number of points of interest, it was necessary to move the sensors around for different types of experiments. Repeatedly uninstalling and installing sensors could damage the sensors and test facilities, and might affect the integrity of the data. Having more sensors and keeping them in a fixed location would save a lot of test time in the future and maintain the integrity of the test configuration.

Each test-run-duration was approximately 4 to 9 seconds depending on a Mach or Reynolds number. A higher Mach number and a lower Reynolds number allows a longer run time. Time between runs, however, was 20 to 30 minutes because it took time for the vacuum pump to pump out the pressure from the vacuum tank. The test run time versus wait time needs to be improved. A 4-9 second run to a 20-30 minute recovery time ratio did not seem efficient.

As mentioned before, the inlet nozzles are not symmetric. The flow uniformity at the exit of the inlet nozzle needs to be investigated in order to help provide more accurate boundary conditions to the CFD analysts for future CFD works.

# **Appendix A. Test section window thickness calculation**

The book, High-speed wind tunnel testing by Alan Pope(28), was used for wind tunnel test section calculation. The bottom of page 114 shows the window thickness calculation for a simply supported rectangular window. In this case, the four edges of a window would be fixed. The calculation for a window thickness for a simply supported window would yield thicker thickness than the one for fixed edge window. So this calculation would yield more thickness than what is required for the safety purpose.

t = long side of window (inch)

s =short side of window (inch)

$$t/s = 19.9228 / 4.4062 = 4.5215$$

From the Fig. 2:19 on page 115, the coefficient from ratio of long side to short side and Poisson's ratio (B) is 0.124. The maximum gauge pressure (p) would be 35.5 psig. Then, the maximum moment ( $M_{max}$ ) is

$$M_{\text{max}} = B \cdot p \cdot s^2$$
  
 $M_{\text{max}} = 0.1245 * 35.5 * 4.4062^2 = 90.4(in \cdot lb)$ 

 $S_{max} = maximum \ allowable \ stress, \ lb/inch^2 \ (S_{max} \ occurs \ at \ the \ center \ of \ the$  window)

 $S_{max}$  = modulus of rupture / safety factor

Modulus of rupture for the cast acrylic is 10200 psi.(29)(30)

Safety factor is 10

$$S_{max} = 10200/10 = 1020 \text{ psi}$$

$$S_{max} = (M_{max}*c)/I$$

,where  $c=\mbox{half}$  the glass thickness = t/2 and  $I=\mbox{moment}$  of inertia for 1 inch wide  $strip=t^3/12$ 

$$S_{max} = (6*M_{max})/t^2$$

Hence, 
$$t = \sqrt{\frac{6 \cdot M_{\text{max}}}{S_{\text{max}}}}$$

$$t = \sqrt{\frac{6 \cdot M_{\text{max}}}{S_{\text{max}}}} = \sqrt{\frac{6 * 90.4}{1020}} = 0.729 inch$$

In this calculation, 35.5 psig was chosen to be the maximum pressure acting on the window, but in this research, 35 psig would be never reached.

# Appendix B. Window deflection calculation

Because the static pressure of the air flow inside the tunnel is acting on wind tunnel window, it is interesting to know how much deflection of the window the pressure causes. The book, Roak's formulas for stress and strain written by Warren C. Yong and Richard G. Budynas, was used as a reference.(31)

I chose the example of a rectangular plate with all edges fixed.

$$y_{\text{max}} = \frac{\alpha q b^4}{E t^3}$$

 $y_{max} = maximum deflection (inch)$ 

 $\alpha$  = coefficient from length and width ratio = 0.0284 for this case

q = pressure (psi) = 35.5 psi

b =short side length (inch) = 4.4062 inch

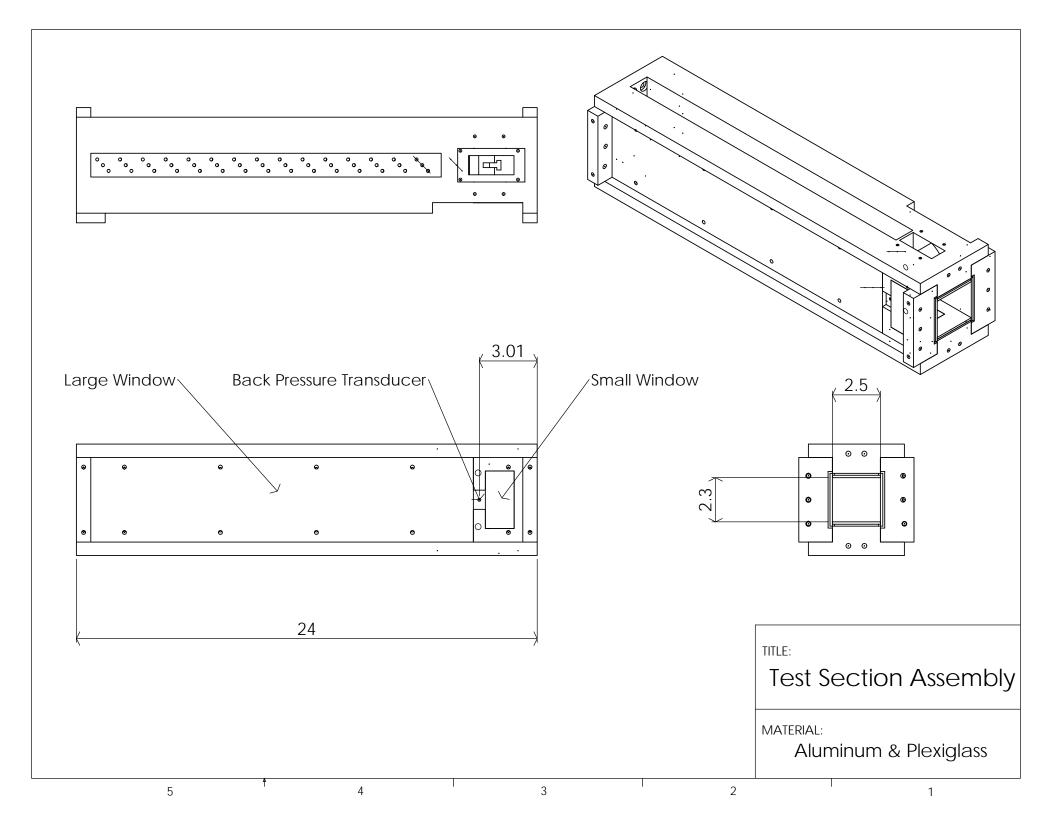
E = Young's modulus (psi) = 464000 psi

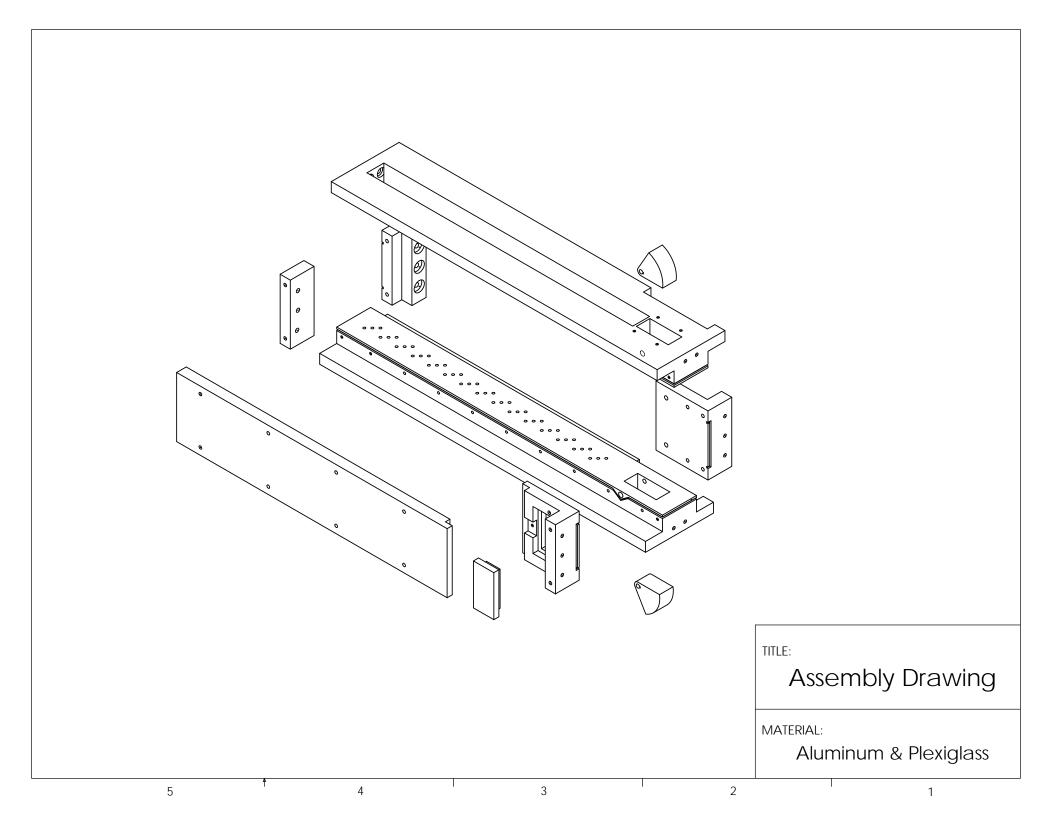
t = thickness (inch) = 0.729 inch

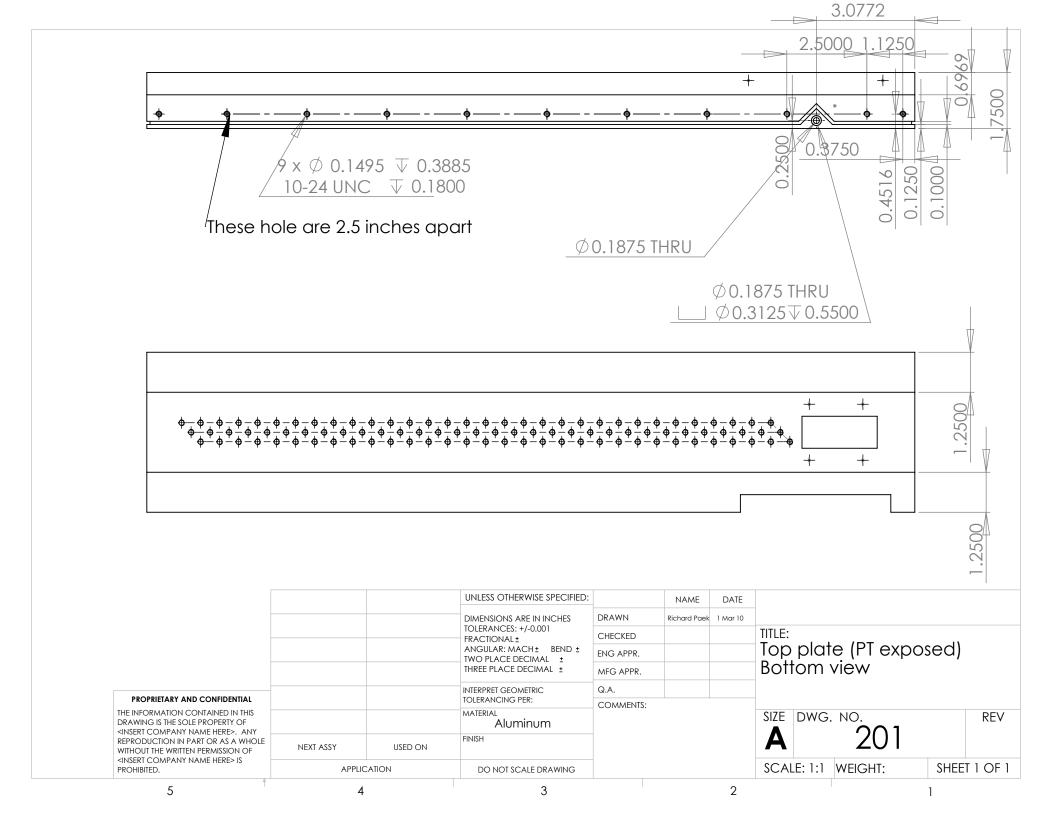
$$y_{max} = \frac{\alpha q b^4}{E t^3} = \frac{0.0284 \cdot 35.5 \cdot 4.4062^4}{464000 \cdot 0.729^3} = 0.00211 \text{ (inch)}$$

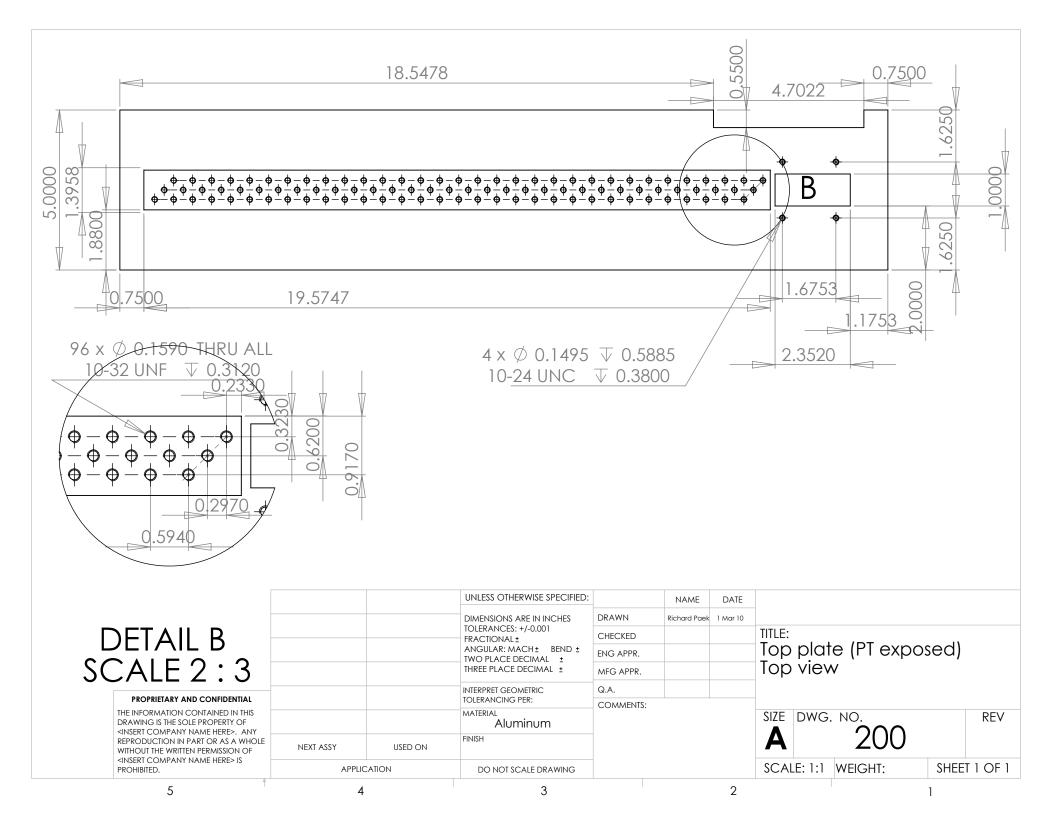
In this calculation, 35.5 psig was chosen to be the maximum pressure acting on the window, but in this experiment, 35.5 psig would be never reached.

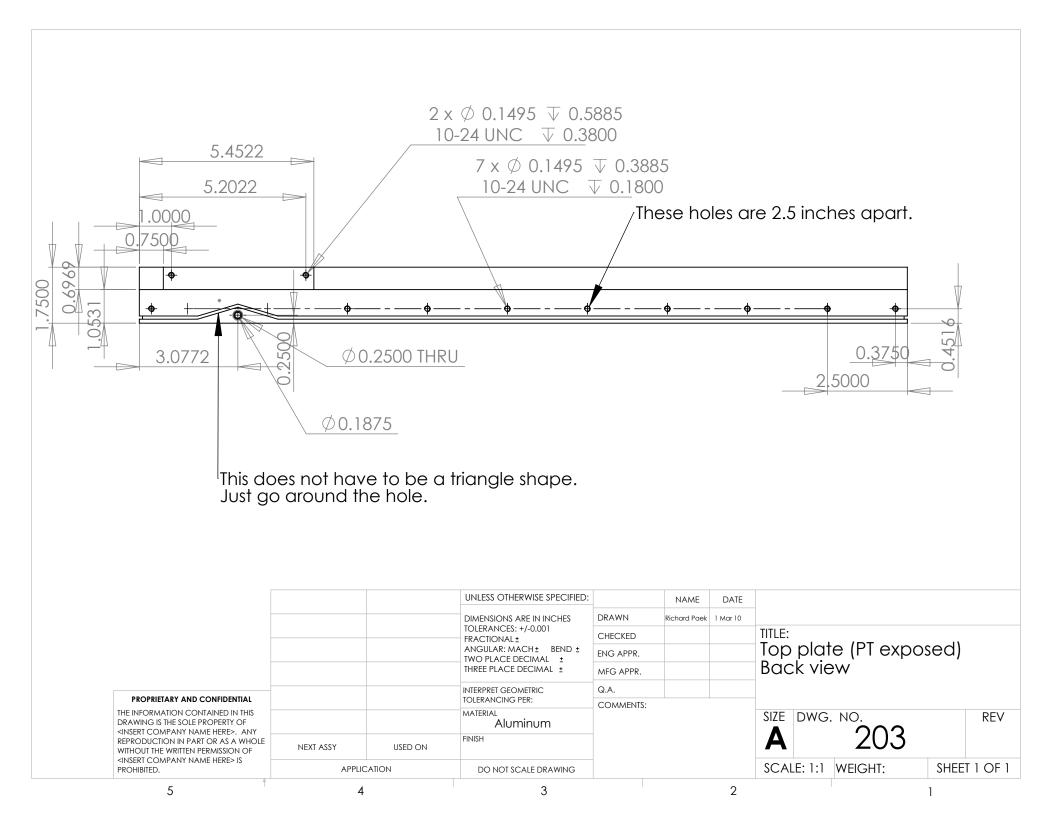
# Appendix C. Test facility engineering drawings

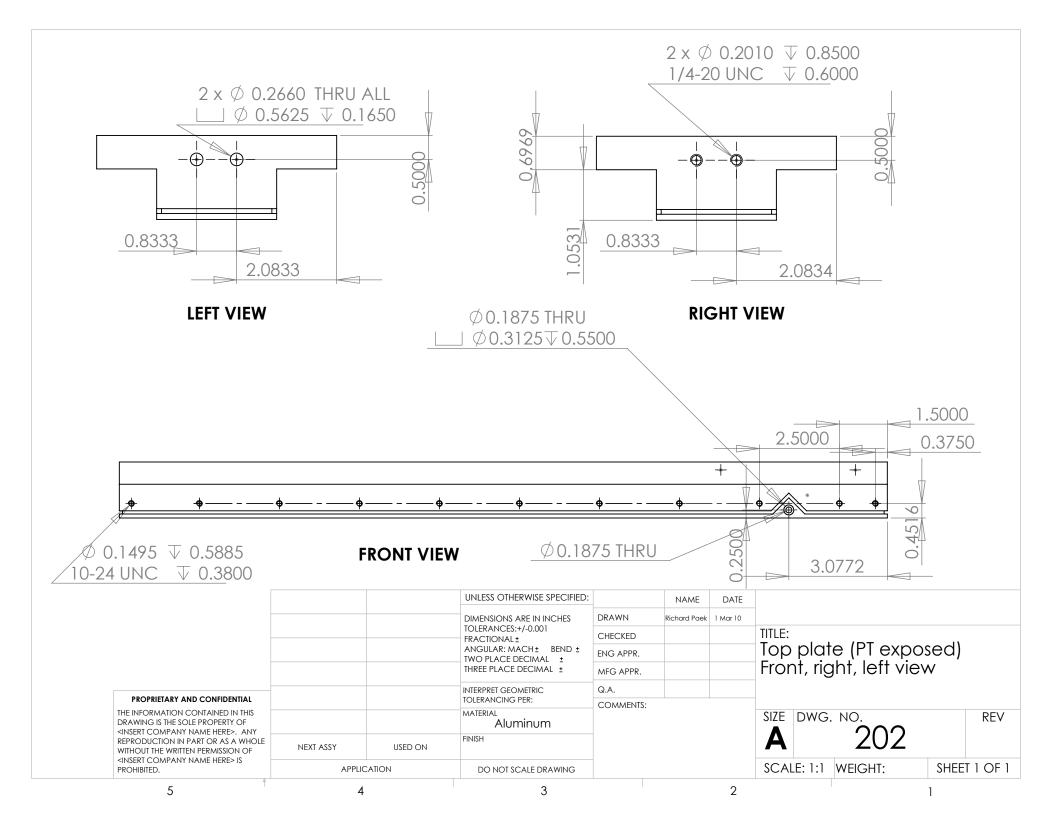


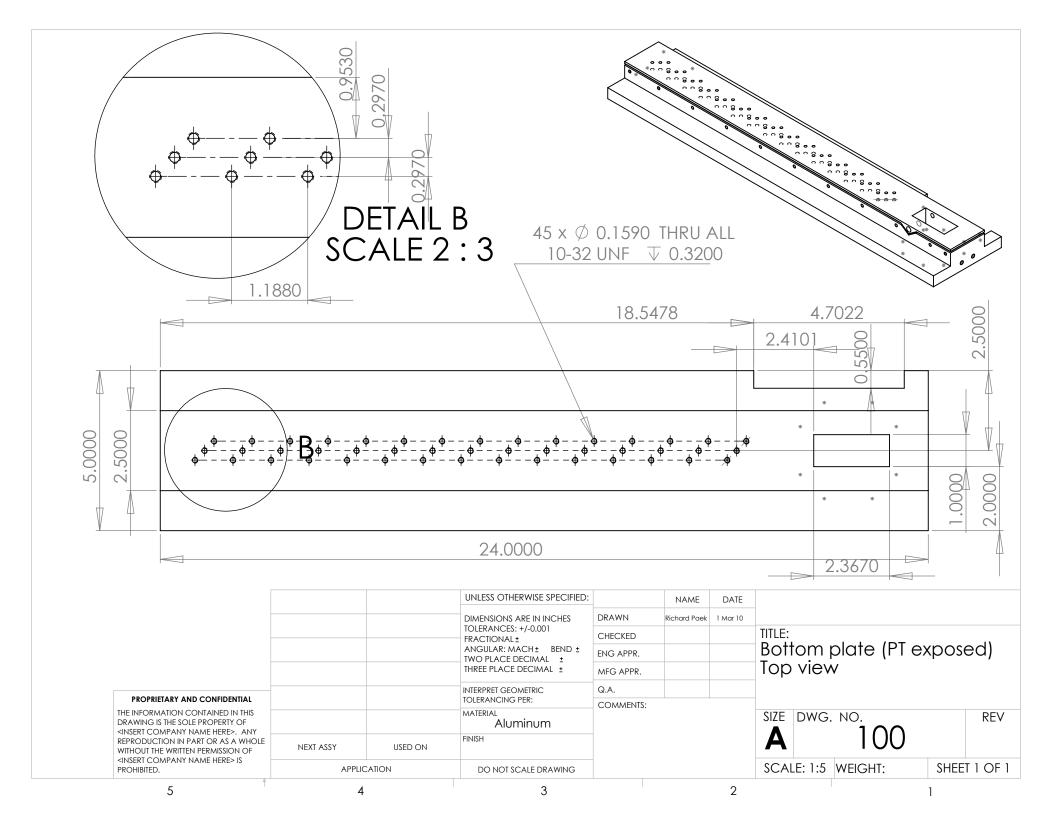


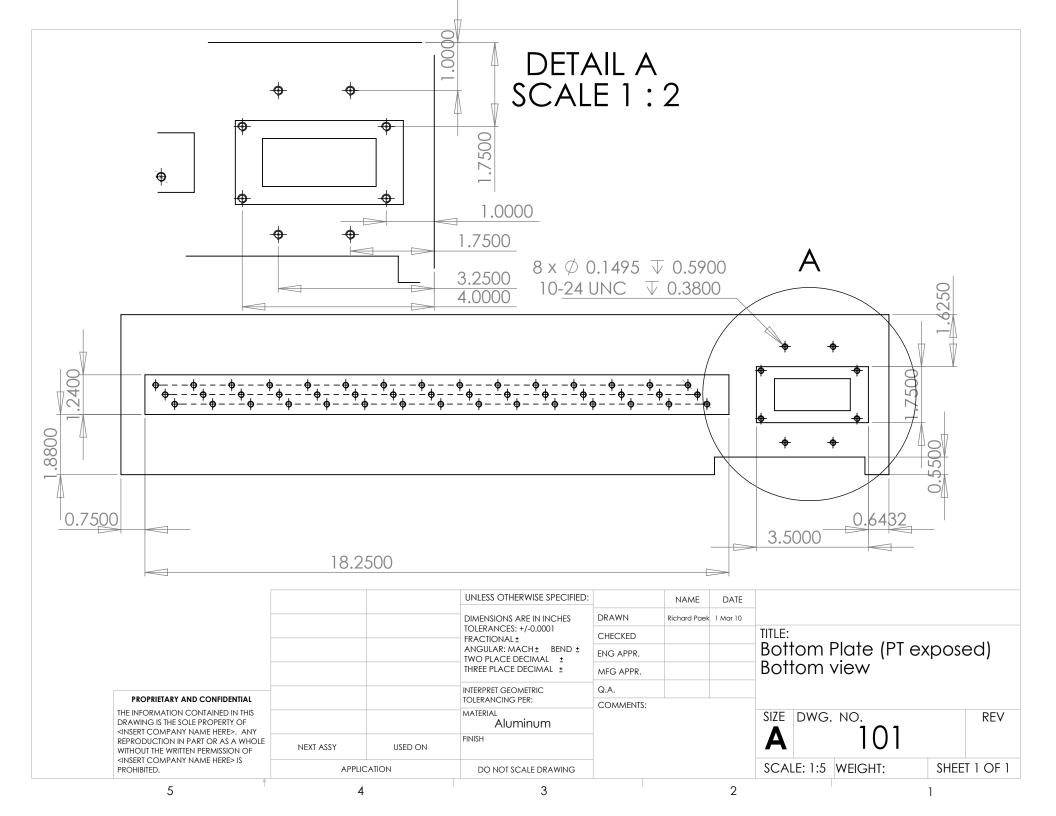


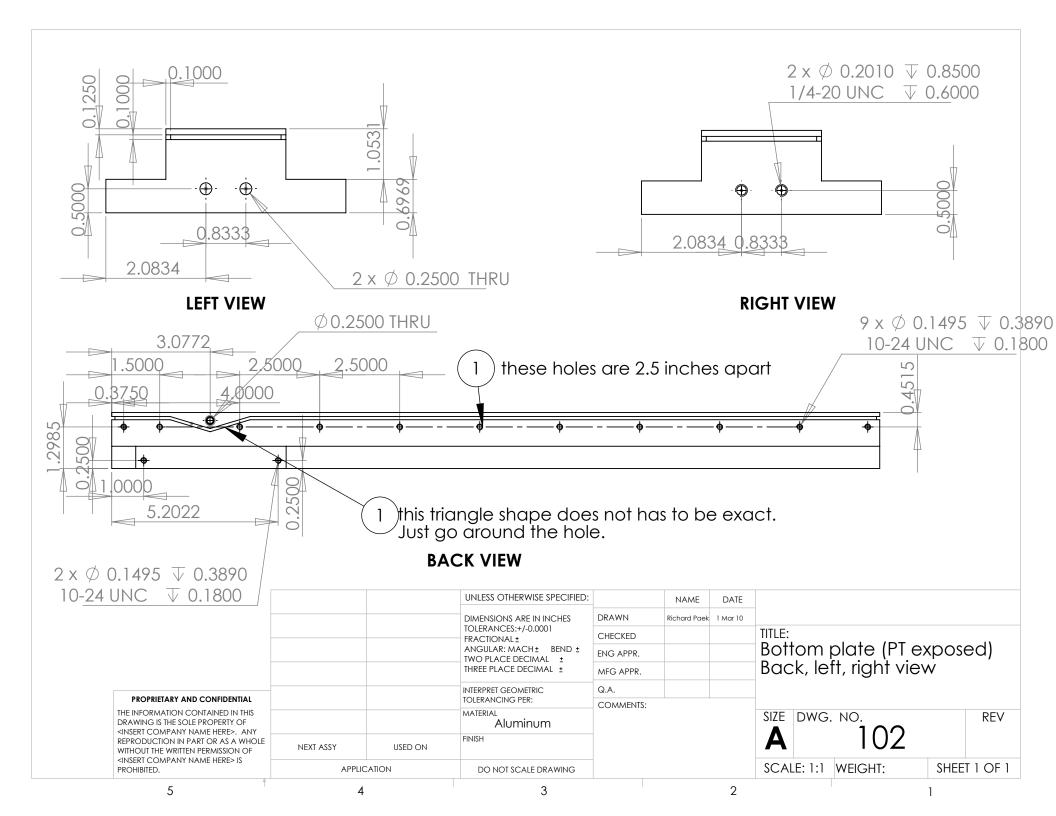


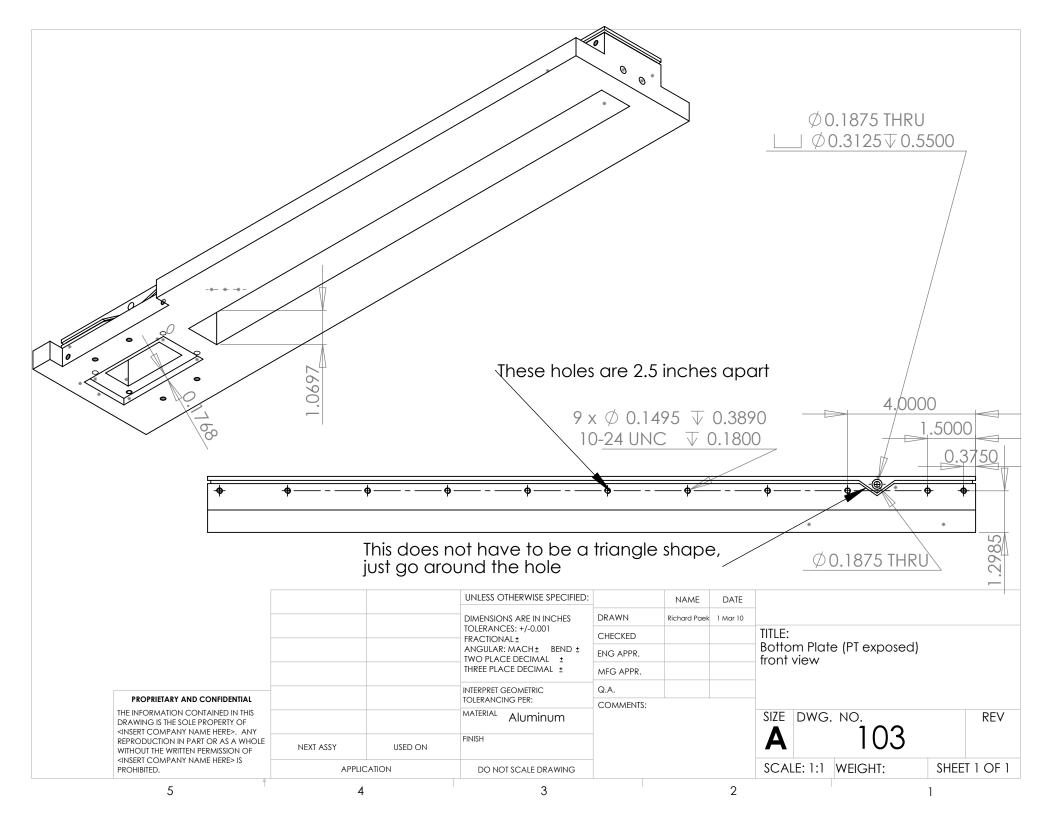


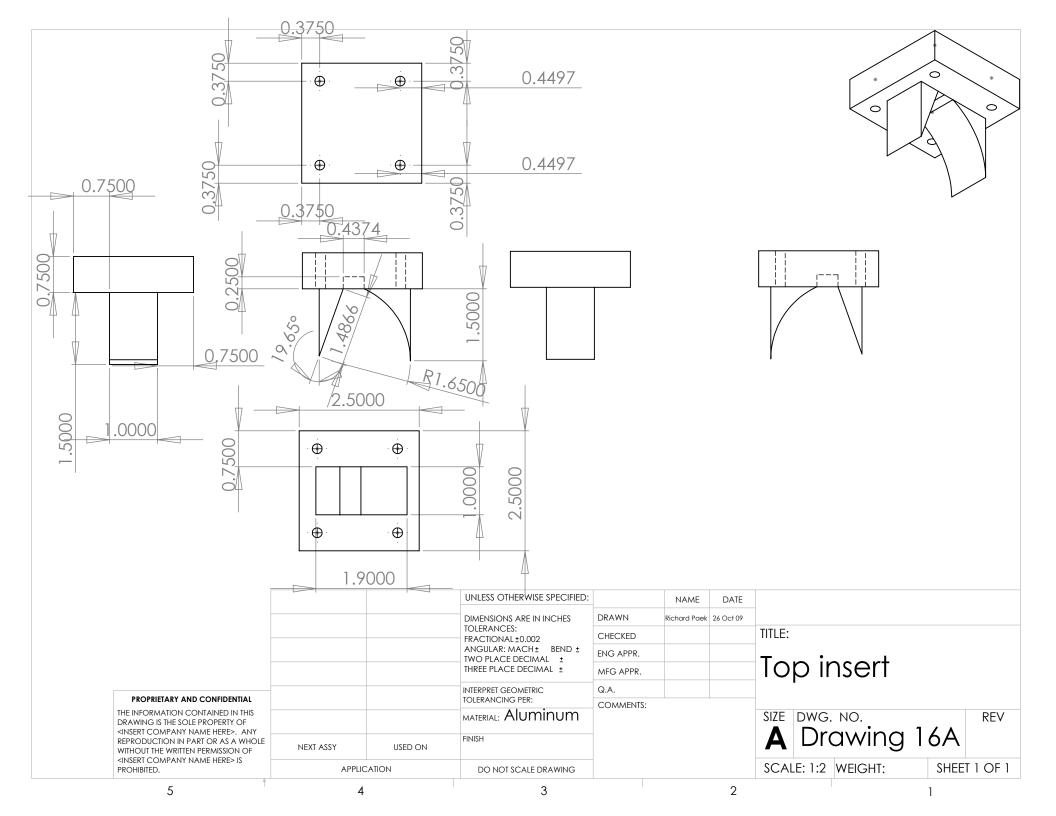


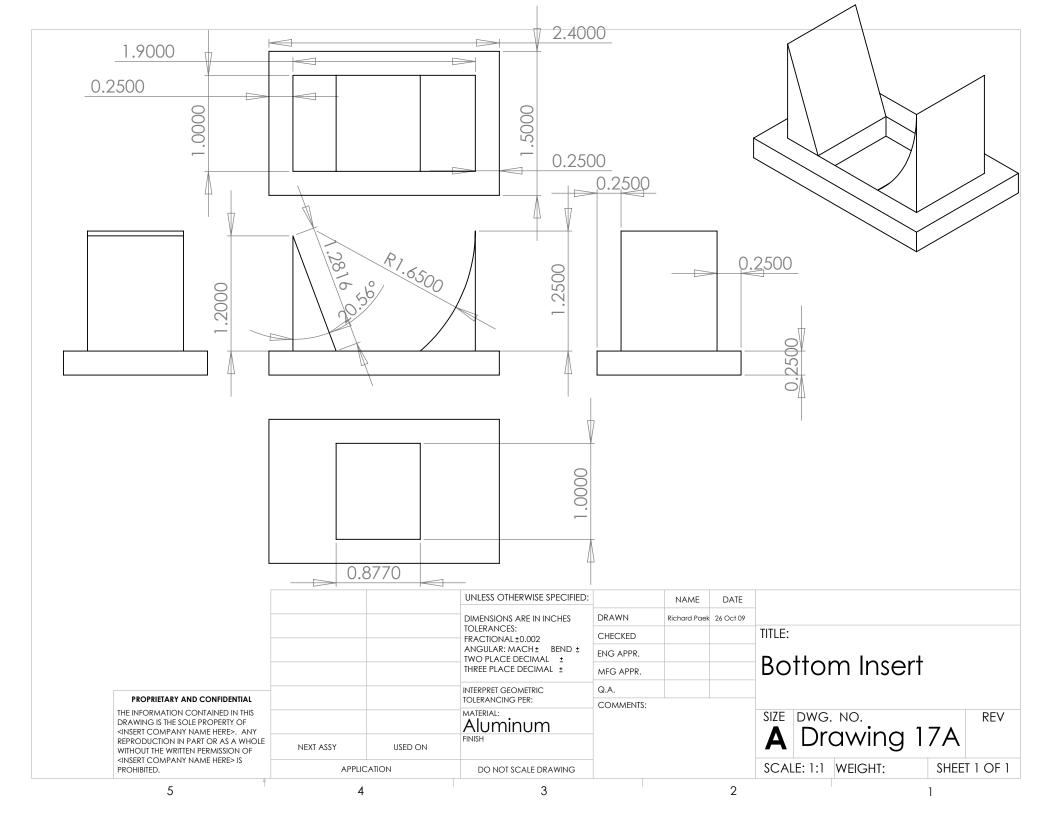


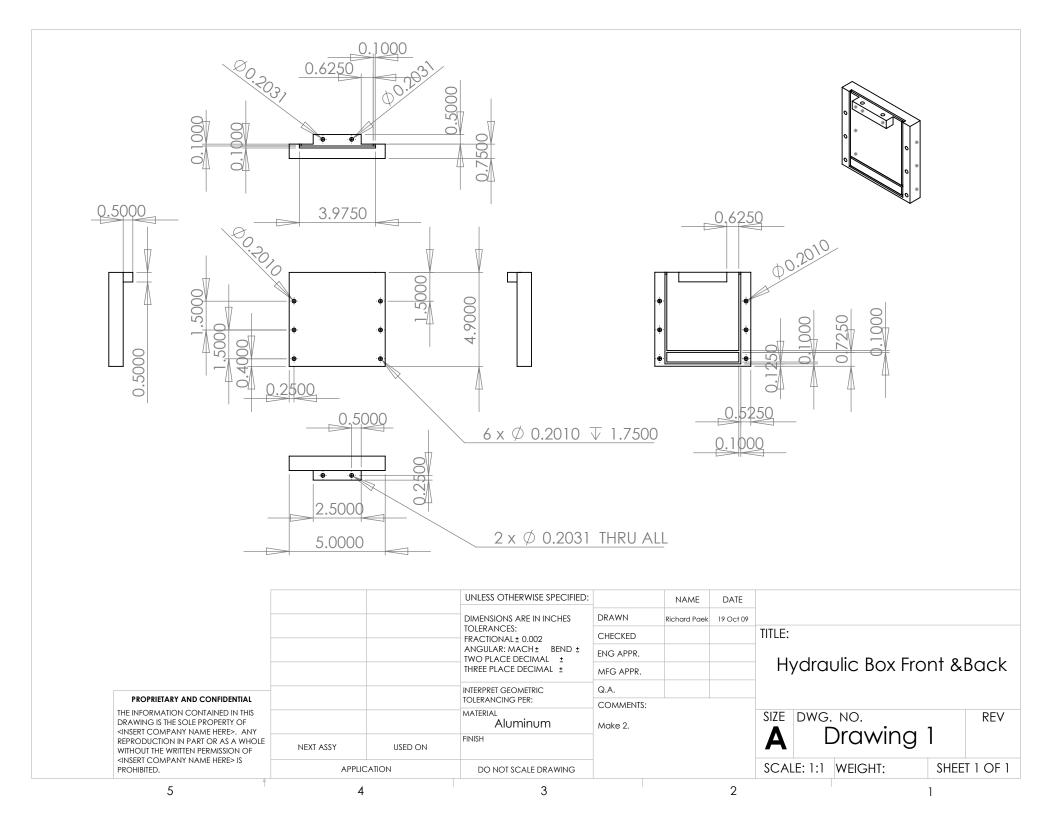


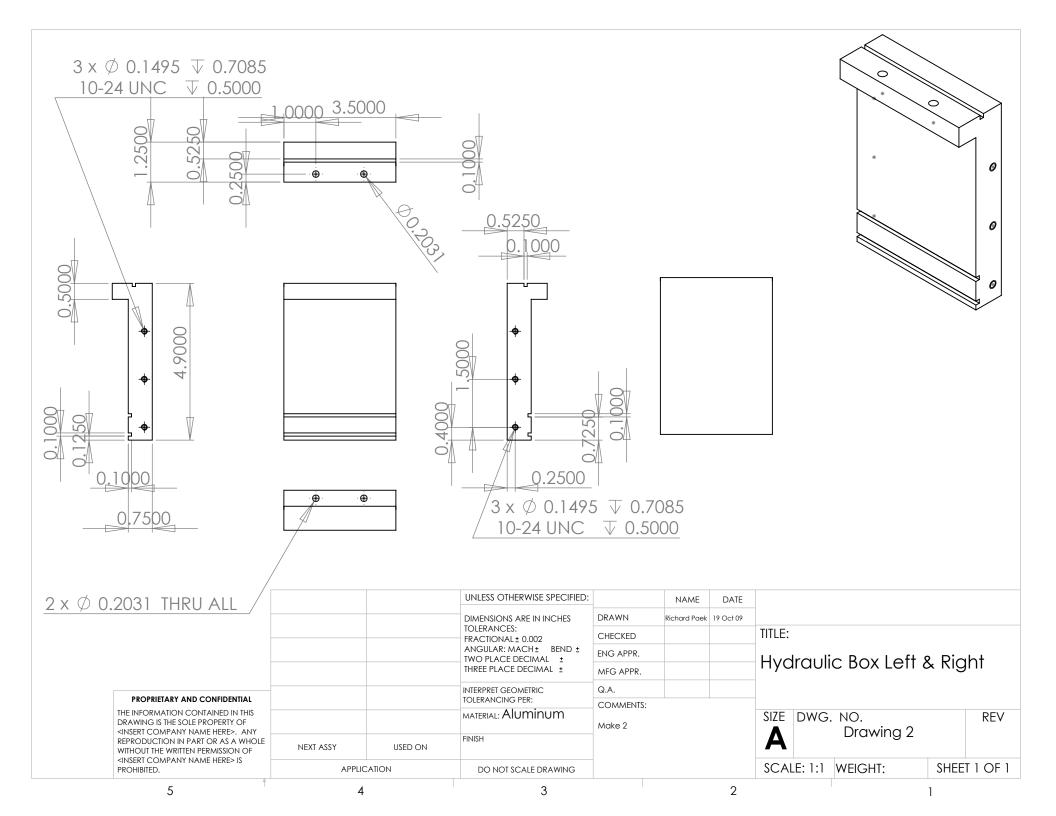


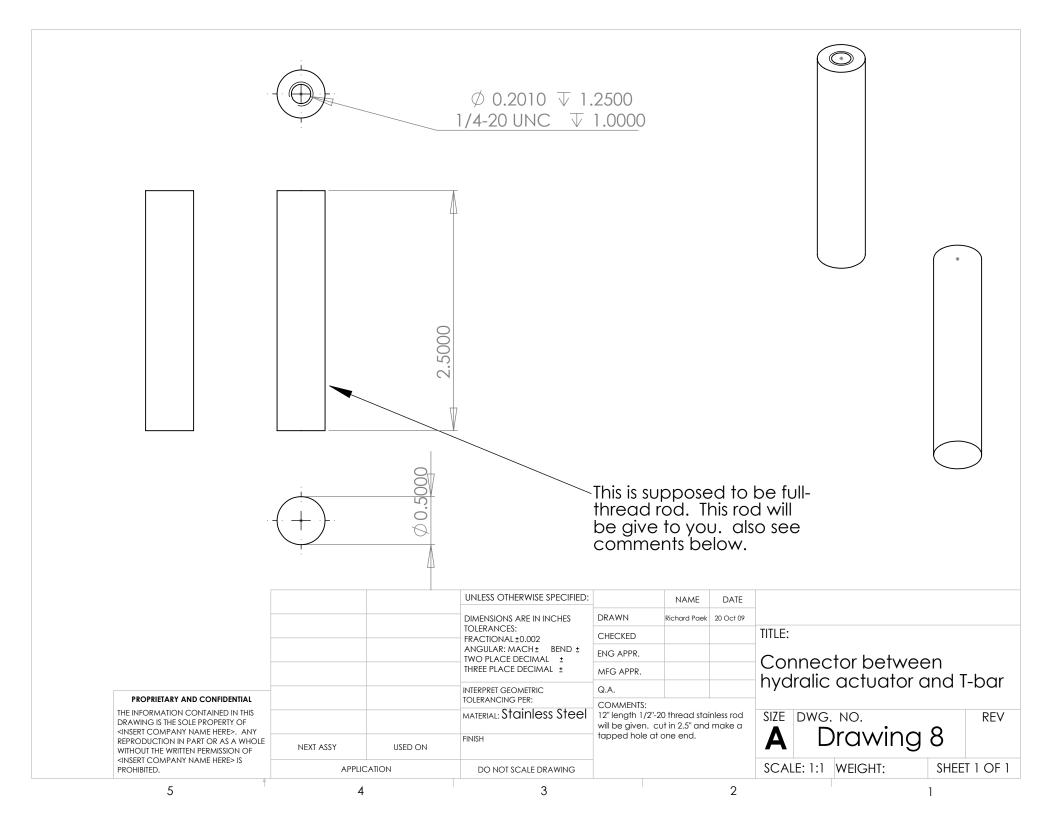


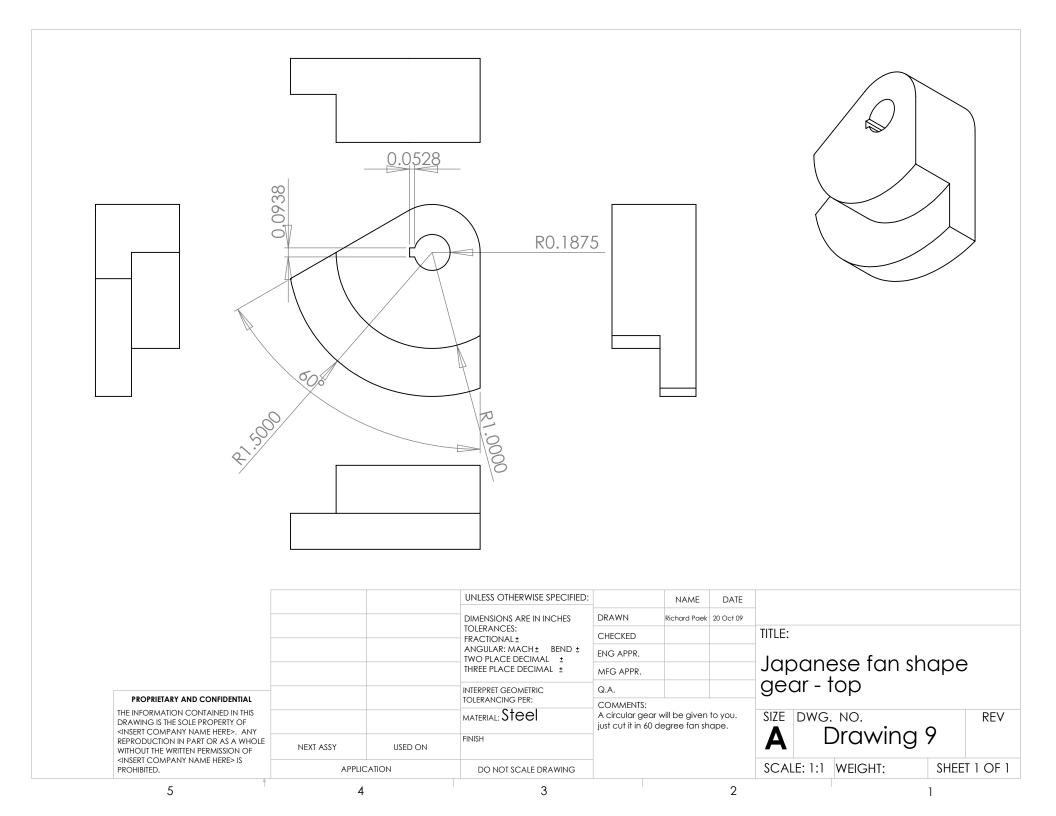


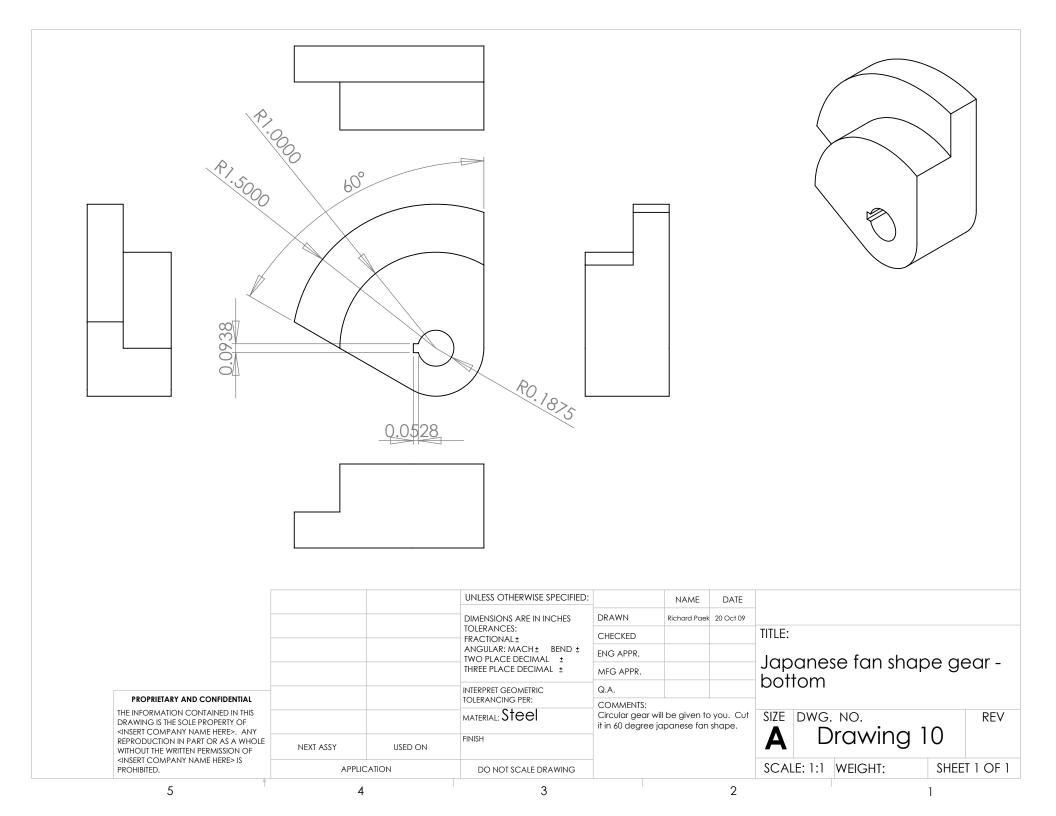


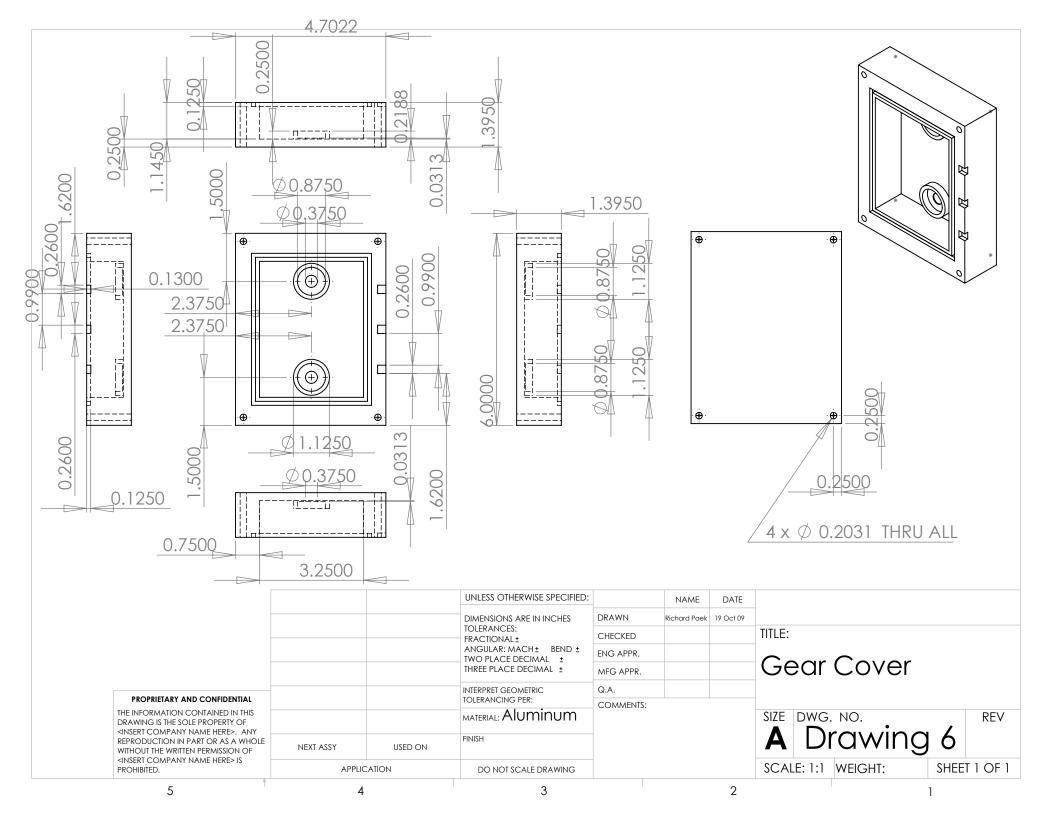


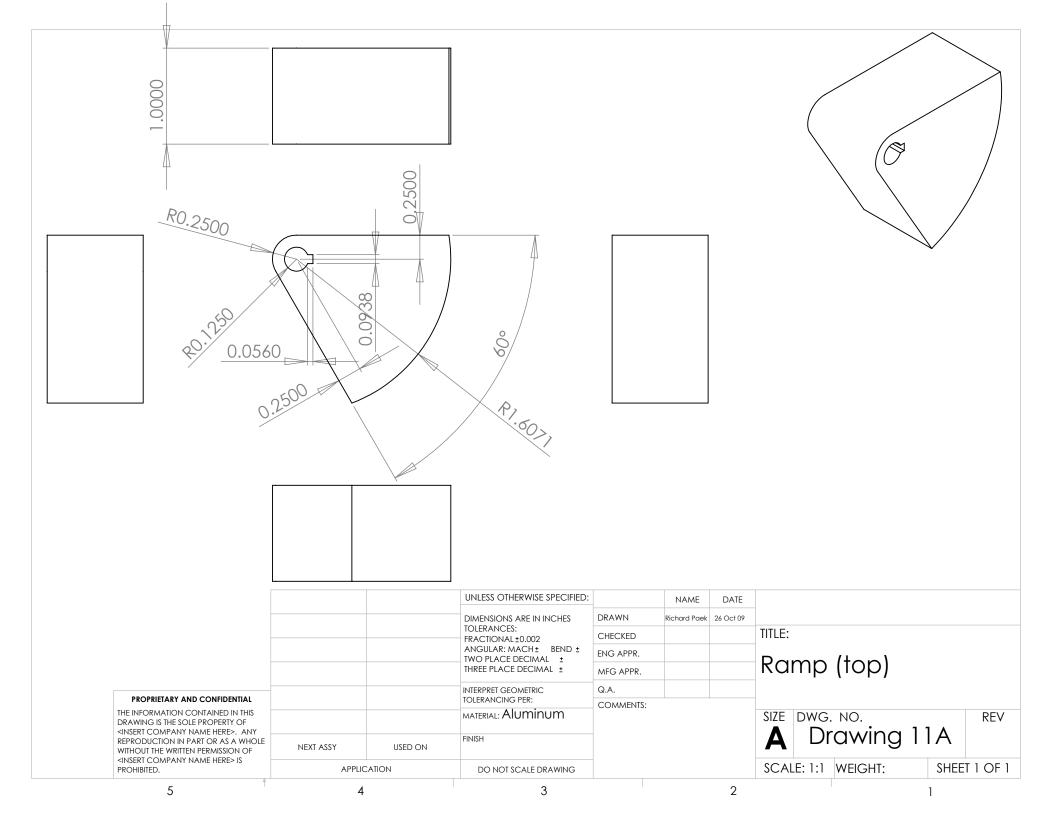


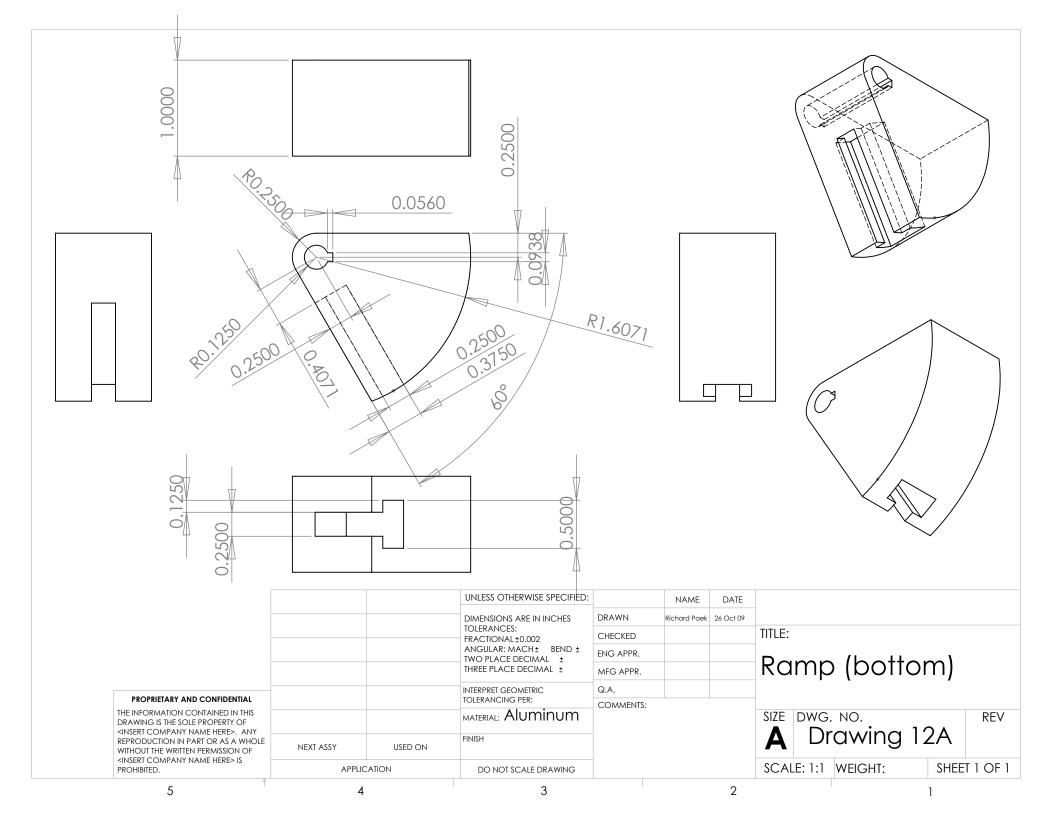


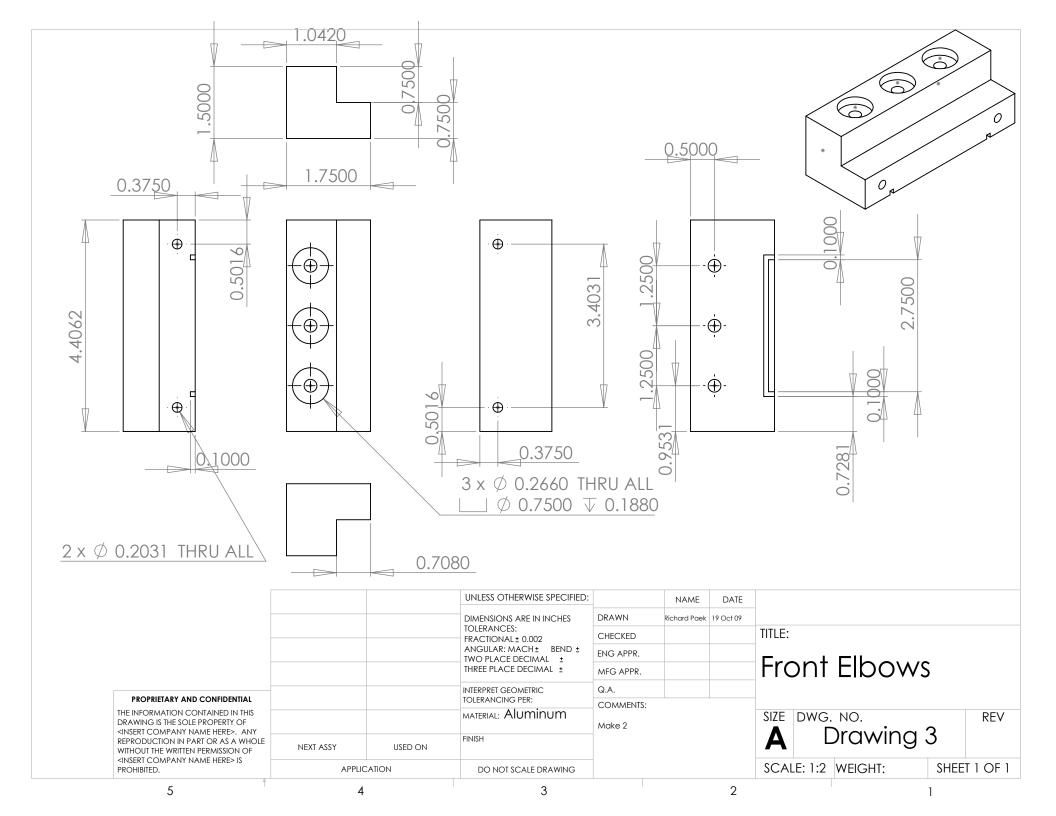


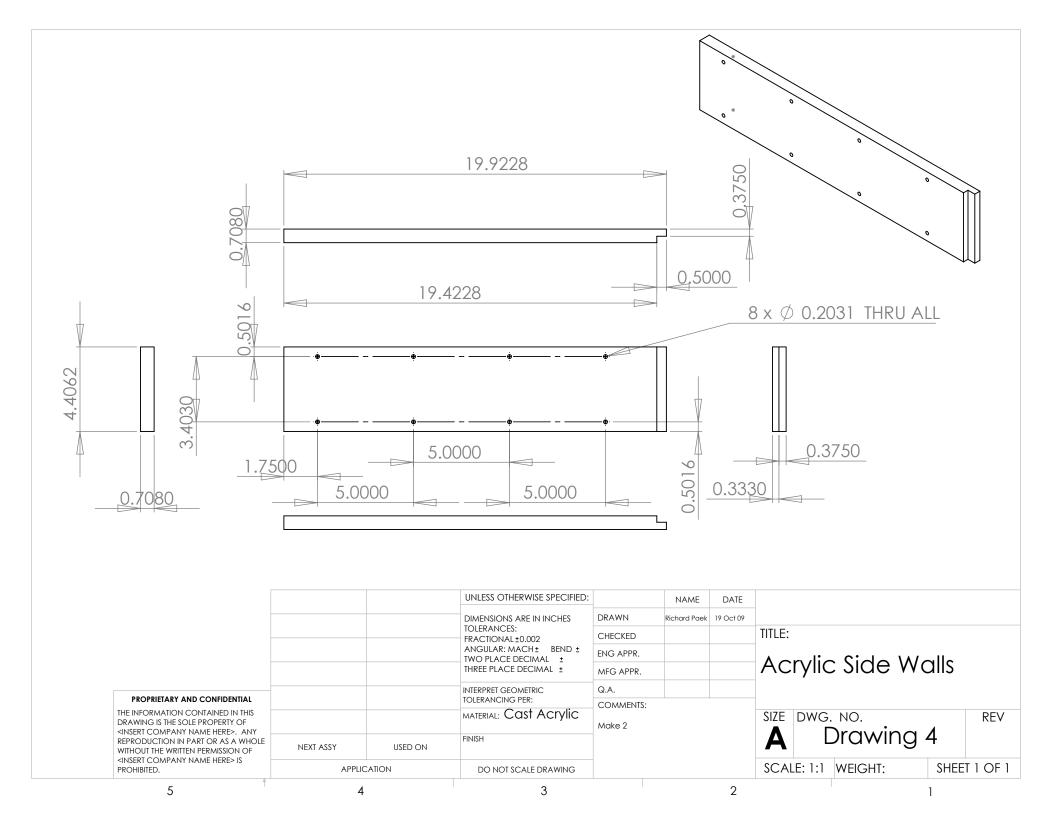


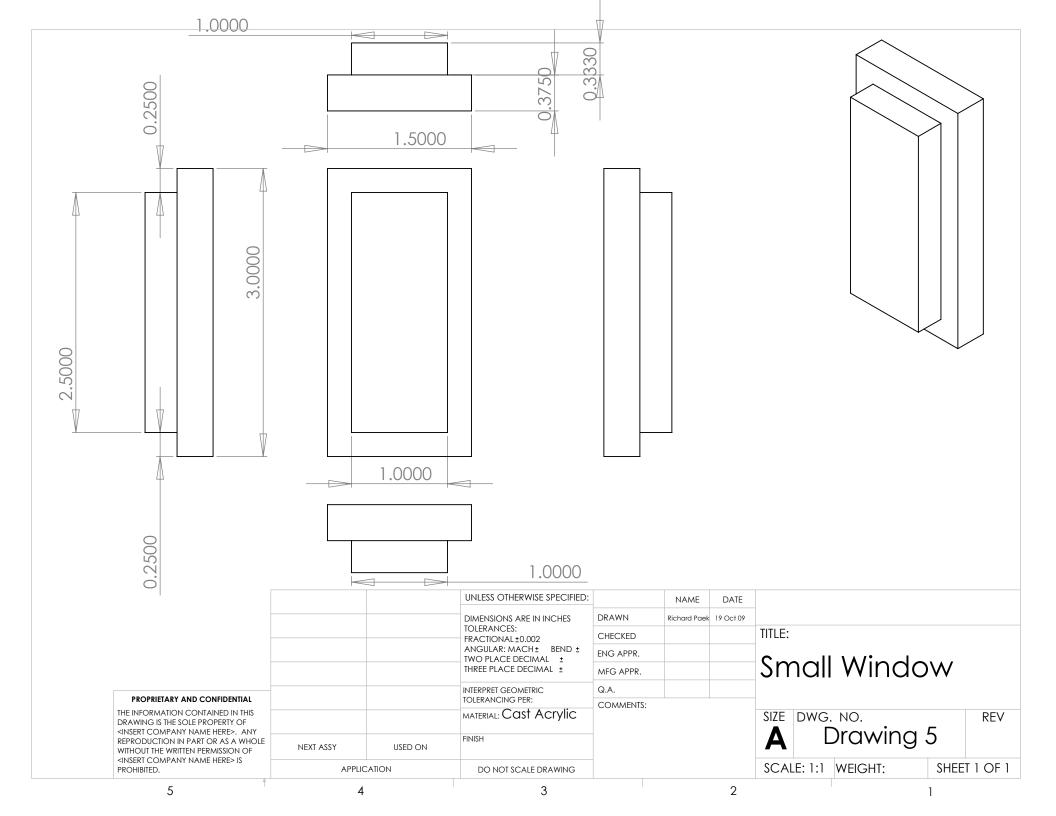


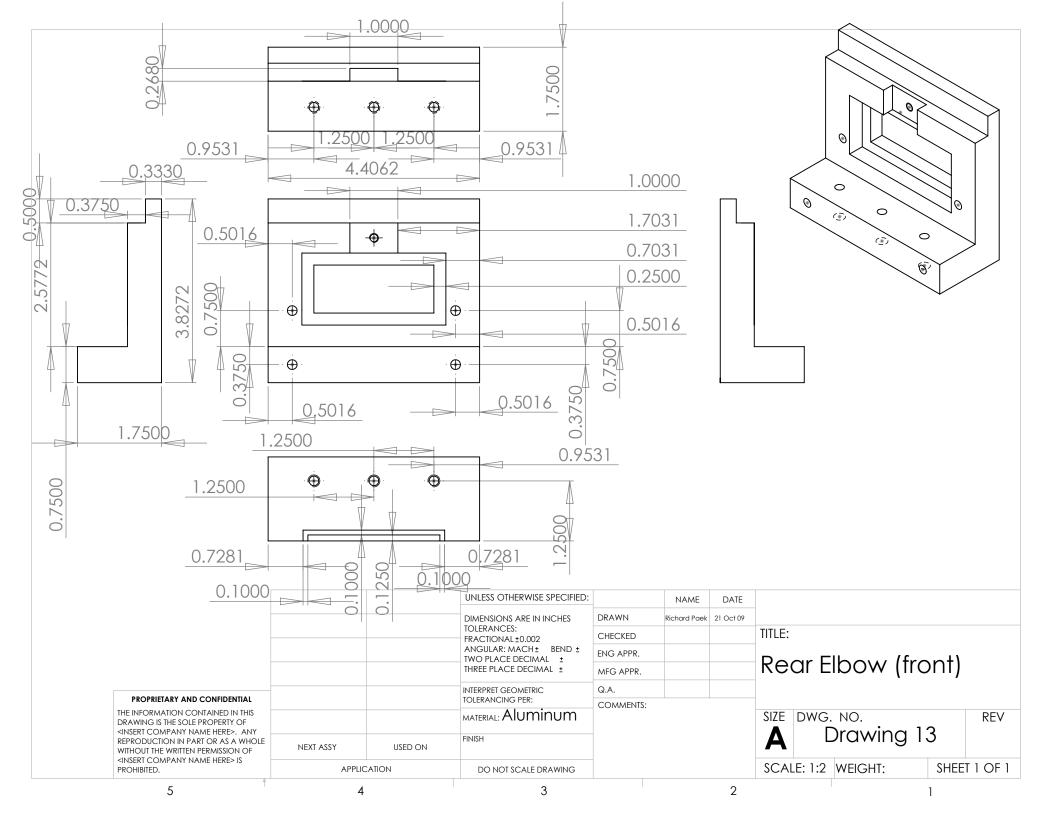


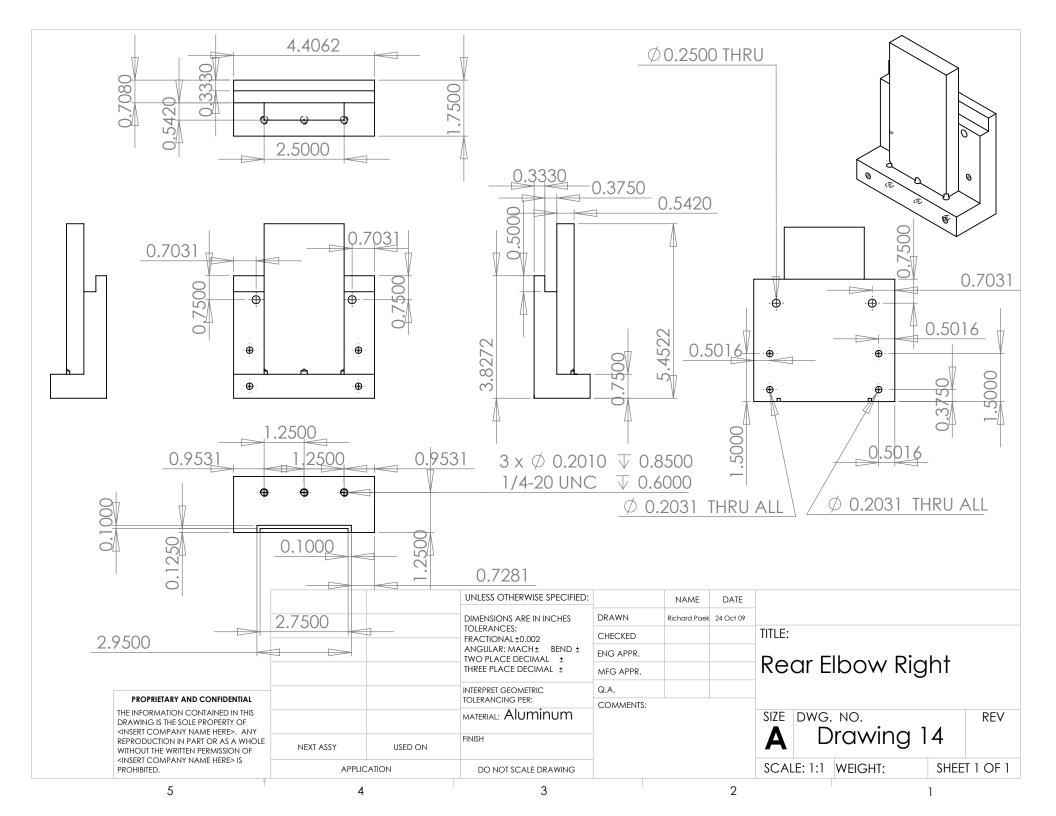


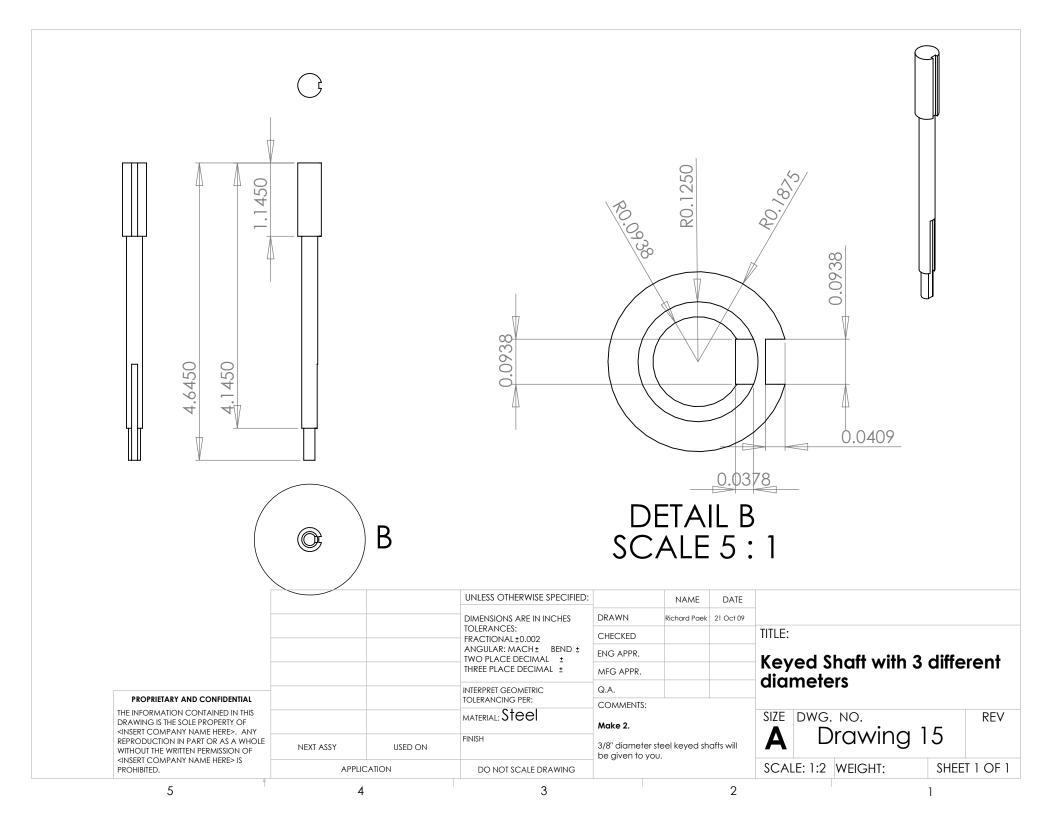


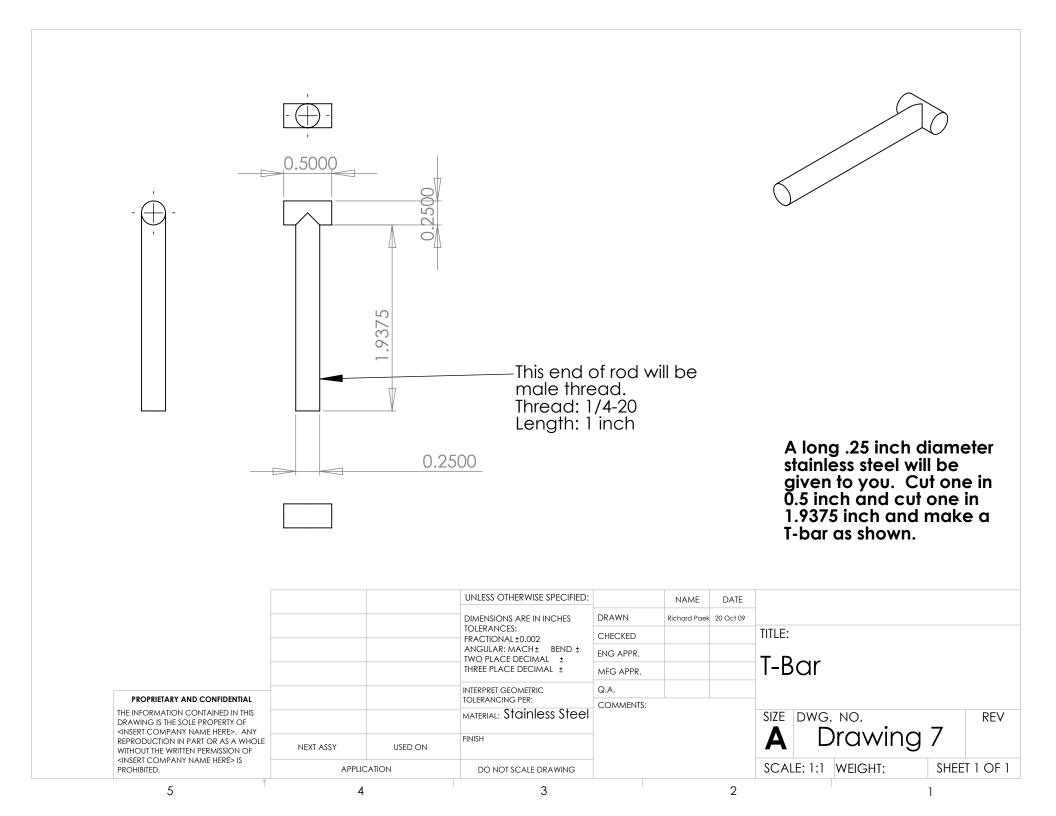












## Appendix D. Endevco pressure sensor/amplifier in-house calibration results

$$y = a*x + b$$
  
 $y =$ pressure applied on the sensors (psi)  
 $a =$ sensitivity (psi/V)  
 $x =$ voltage out from the amplifier (V)  
 $b =$ offset (psi)

Table 7. Endevco pressure sensor/amplifier in-house calibration results

| Amplifier # | Sensor<br># | Calibration results   |  |  |
|-------------|-------------|-----------------------|--|--|
|             | 1           | y = 0.198 x + 0.0014  |  |  |
| 1           | 2           | y = 0.2015 x + 0.23   |  |  |
|             | 3           | y = 0.2024 x - 0.4672 |  |  |
|             | 1           | y = 0.2019 x - 0.2252 |  |  |
| 2           | 2           | y = 0.201 x + 0.0566  |  |  |
|             | 3           | y = 0.2034 x + 0.1279 |  |  |
|             | 1           | y = 0.2 x + 0.1785    |  |  |
| 3           | 2           | y = 0.2019 x + 0.1441 |  |  |
|             | 3           | y = 0.2001 x - 0.11   |  |  |
|             | 1           | y = 0.2001 x + 0.0132 |  |  |
| 4           | 2           | y = 0.201 x + 0.076   |  |  |
|             | 3           | y = 0.2013 x - 0.66   |  |  |

## Appendix E. Unit conversion from MTS reading

- 1. The ratio of the MTS reading to the true length is 0.643:0.99974.
- 2. Converting from true actuator height to ramp angle.

converting \_ from \_ actuator \_ height \_ to \_ ramp \_ angle 
$$\theta = ramp \_ angle(\deg)$$

$$\Delta h_{act} = actuator \_ height(inch)$$

$$\theta = 60 - \tan^{-1} \left( \frac{0.99974 - \Delta h_{act}}{0.5772} \right)$$

3. Converting from ramp angle to ramp edge height.

converting \_ from \_ ramp \_ angle \_ to \_ ramp \_ edge \_ height 
$$\Delta h_{ramp} = ramp _ height(inch)$$
 
$$\Delta h_{ramp} = 1.5875 \cdot \sin \theta - 0.25 + 0.25 \cdot \cos \theta$$

4. Calculating area blocked from the ramp edge height.

5. Percentage of the area blocked to the total area

Percent \_ of \_ area \_ blocked \_ is : 
$$\% A = \frac{A}{6.25} \cdot 100$$

6. The air flow area is:

$$A_{flow} = A_{Total} - A_{blocked}$$

7. The percentage of the flow area to the total area is:

$$8 A_{flow} = \frac{A_{flow}}{A_{Total}}$$

See the following pages for the tabulated results.

Table 8. Unit conversion from MTS reading

| MTS     | true length   | ramp angle | Δh_ramp_edge | Area blocked | % area  | Flow area |            |
|---------|---------------|------------|--------------|--------------|---------|-----------|------------|
| reading | (Δh_actuator) | (deg)      | (inch)       | (inch^2)     | blocked | (inch^2)  | %Flow area |
| 0       | 0.0000        | 0.000      | 0.000        | 0.000        | 0.00%   | 6.250     | 100.00%    |
| 0.001   | 0.0016        | 0.039      | 0.001        | 0.002        | 0.03%   | 6.248     | 99.97%     |
| 0.002   | 0.0031        | 0.077      | 0.002        | 0.004        | 0.07%   | 6.246     | 99.93%     |
| 0.003   | 0.0047        | 0.116      | 0.003        | 0.006        | 0.10%   | 6.244     | 99.90%     |
| 0.004   | 0.0062        | 0.155      | 0.004        | 0.009        | 0.14%   | 6.241     | 99.86%     |
| 0.005   | 0.0078        | 0.194      | 0.005        | 0.011        | 0.17%   | 6.239     | 99.83%     |
| 0.006   | 0.0093        | 0.233      | 0.006        | 0.013        | 0.21%   | 6.237     | 99.79%     |
| 0.007   | 0.0109        | 0.272      | 0.008        | 0.015        | 0.24%   | 6.235     | 99.76%     |
| 0.008   | 0.0124        | 0.312      | 0.009        | 0.017        | 0.28%   | 6.233     | 99.72%     |
| 0.009   | 0.0140        | 0.351      | 0.010        | 0.019        | 0.31%   | 6.231     | 99.69%     |
| 0.01    | 0.0155        | 0.390      | 0.011        | 0.022        | 0.35%   | 6.228     | 99.65%     |
| 0.011   | 0.0171        | 0.430      | 0.012        | 0.024        | 0.38%   | 6.226     | 99.62%     |
| 0.012   | 0.0187        | 0.470      | 0.013        | 0.026        | 0.42%   | 6.224     | 99.58%     |
| 0.013   | 0.0202        | 0.509      | 0.014        | 0.028        | 0.45%   | 6.222     | 99.55%     |
| 0.014   | 0.0218        | 0.549      | 0.015        | 0.030        | 0.49%   | 6.220     | 99.51%     |
| 0.015   | 0.0233        | 0.589      | 0.016        | 0.033        | 0.52%   | 6.217     | 99.48%     |
| 0.016   | 0.0249        | 0.629      | 0.017        | 0.035        | 0.56%   | 6.215     | 99.44%     |
| 0.017   | 0.0264        | 0.669      | 0.019        | 0.037        | 0.59%   | 6.213     | 99.41%     |
| 0.018   | 0.0280        | 0.709      | 0.020        | 0.039        | 0.63%   | 6.211     | 99.37%     |
| 0.019   | 0.0295        | 0.750      | 0.021        | 0.041        | 0.66%   | 6.209     | 99.34%     |
| 0.02    | 0.0311        | 0.790      | 0.022        | 0.044        | 0.70%   | 6.206     | 99.30%     |
| 0.021   | 0.0327        | 0.831      | 0.023        | 0.046        | 0.74%   | 6.204     | 99.26%     |
| 0.022   | 0.0342        | 0.871      | 0.024        | 0.048        | 0.77%   | 6.202     | 99.23%     |
| 0.023   | 0.0358        | 0.912      | 0.025        | 0.050        | 0.81%   | 6.200     | 99.19%     |
| 0.024   | 0.0373        | 0.953      | 0.026        | 0.053        | 0.84%   | 6.197     | 99.16%     |
| 0.025   | 0.0389        | 0.993      | 0.027        | 0.055        | 0.88%   | 6.195     | 99.12%     |
| 0.026   | 0.0404        | 1.034      | 0.029        | 0.057        | 0.92%   | 6.193     | 99.08%     |
| 0.027   | 0.0420        | 1.076      | 0.030        | 0.060        | 0.95%   | 6.190     | 99.05%     |
| 0.028   | 0.0435        | 1.117      | 0.031        | 0.062        | 0.99%   | 6.188     | 99.01%     |
| 0.029   | 0.0451        | 1.158      | 0.032        | 0.064        | 1.02%   | 6.186     | 98.98%     |
| 0.03    | 0.0466        | 1.199      | 0.033        | 0.066        | 1.06%   | 6.184     | 98.94%     |
| 0.031   | 0.0482        | 1.241      | 0.034        | 0.069        | 1.10%   | 6.181     | 98.90%     |
| 0.032   | 0.0498        | 1.282      | 0.035        | 0.071        | 1.13%   | 6.179     | 98.87%     |
| 0.033   | 0.0513        | 1.324      | 0.037        | 0.073        | 1.17%   | 6.177     | 98.83%     |
| 0.034   | 0.0529        | 1.366      | 0.038        | 0.076        | 1.21%   | 6.174     | 98.79%     |
| 0.035   | 0.0544        | 1.408      | 0.039        | 0.078        | 1.25%   | 6.172     | 98.75%     |
| 0.036   | 0.0560        | 1.450      | 0.040        | 0.080        | 1.28%   | 6.170     | 98.72%     |
| 0.037   | 0.0575        | 1.492      | 0.041        | 0.082        | 1.32%   | 6.168     | 98.68%     |
| 0.038   | 0.0591        | 1.534      | 0.042        | 0.085        | 1.36%   | 6.165     | 98.64%     |
| 0.039   | 0.0606        | 1.576      | 0.044        | 0.087        | 1.39%   | 6.163     | 98.61%     |
| 0.04    | 0.0622        | 1.618      | 0.045        | 0.089        | 1.43%   | 6.161     | 98.57%     |
| 0.041   | 0.0637        | 1.661      | 0.046        | 0.092        | 1.47%   | 6.158     | 98.53%     |
| 0.042   | 0.0653        | 1.704      | 0.047        | 0.094        | 1.51%   | 6.156     | 98.49%     |

| MTS reading    | true length (Δh_actuator) | ramp angle<br>(deg) | Δh_ramp_edge (inch) | Area blocked (inch^2) | % area<br>blocked | Flow area (inch^2) | %Flow area       |
|----------------|---------------------------|---------------------|---------------------|-----------------------|-------------------|--------------------|------------------|
| 0.043          | 0.0669                    | 1.746               | 0.048               | 0.097                 | 1.54%             | 6.153              | 98.46%           |
| 0.044          | 0.0684                    | 1.789               | 0.049               | 0.099                 | 1.58%             | 6.151              | 98.42%           |
| 0.045          | 0.0700                    | 1.832               | 0.051               | 0.101                 | 1.62%             | 6.149              | 98.38%           |
| 0.046          | 0.0715                    | 1.875               | 0.052               | 0.104                 | 1.66%             | 6.146              | 98.34%           |
| 0.047          | 0.0731                    | 1.918               | 0.053               | 0.106                 | 1.70%             | 6.144              | 98.30%           |
| 0.048          | 0.0746                    | 1.961               | 0.054               | 0.108                 | 1.73%             | 6.142              | 98.27%           |
| 0.049          | 0.0762                    | 2.004               | 0.055               | 0.111                 | 1.77%             | 6.139              | 98.23%           |
| 0.05           | 0.0777                    | 2.048               | 0.057               | 0.113                 | 1.81%             | 6.137              | 98.19%           |
| 0.051          | 0.0793                    | 2.091               | 0.058               | 0.116                 | 1.85%             | 6.134              | 98.15%           |
| 0.052          | 0.0808                    | 2.135               | 0.059               | 0.118                 | 1.89%             | 6.132              | 98.11%           |
| 0.053<br>0.054 | 0.0824                    | 2.179<br>2.222      | 0.060<br>0.061      | 0.120                 | 1.93%             | 6.130              | 98.07%           |
| 0.054          | 0.0840<br>0.0855          | 2.222               | 0.061               | 0.123<br>0.125        | 1.96%<br>2.00%    | 6.127<br>6.125     | 98.04%<br>98.00% |
| 0.056          | 0.0853                    | 2.310               | 0.064               | 0.123                 | 2.04%             | 6.123              | 97.96%           |
| 0.057          | 0.0871                    | 2.355               | 0.065               | 0.120                 | 2.04%             | 6.120              | 97.92%           |
| 0.057          | 0.0902                    | 2.399               | 0.066               | 0.132                 | 2.12%             | 6.118              | 97.88%           |
| 0.059          | 0.0917                    | 2.443               | 0.067               | 0.135                 | 2.16%             | 6.115              | 97.84%           |
| 0.06           | 0.0933                    | 2.488               | 0.069               | 0.137                 | 2.20%             | 6.113              | 97.80%           |
| 0.061          | 0.0948                    | 2.532               | 0.070               | 0.140                 | 2.24%             | 6.110              | 97.76%           |
| 0.062          | 0.0964                    | 2.577               | 0.071               | 0.142                 | 2.28%             | 6.108              | 97.72%           |
| 0.063          | 0.0980                    | 2.622               | 0.072               | 0.145                 | 2.32%             | 6.105              | 97.68%           |
| 0.064          | 0.0995                    | 2.667               | 0.074               | 0.147                 | 2.35%             | 6.103              | 97.65%           |
| 0.065          | 0.1011                    | 2.712               | 0.075               | 0.150                 | 2.39%             | 6.100              | 97.61%           |
| 0.066          | 0.1026                    | 2.757               | 0.076               | 0.152                 | 2.43%             | 6.098              | 97.57%           |
| 0.067          | 0.1042                    | 2.802               | 0.077               | 0.155                 | 2.47%             | 6.095              | 97.53%           |
| 0.068          | 0.1057                    | 2.847               | 0.079               | 0.157                 | 2.51%             | 6.093              | 97.49%           |
| 0.069          | 0.1073                    | 2.893               | 0.080               | 0.160                 | 2.55%             | 6.090              | 97.45%           |
| 0.07           | 0.1088                    | 2.938               | 0.081               | 0.162                 | 2.59%             | 6.088              | 97.41%           |
| 0.071          | 0.1104                    | 2.984               | 0.082               | 0.165                 | 2.63%             | 6.085              | 97.37%           |
| 0.072          | 0.1119                    | 3.030               | 0.084               | 0.167                 | 2.67%             | 6.083              | 97.33%           |
| 0.073          | 0.1135                    | 3.076               | 0.085               | 0.170                 | 2.71%             | 6.080              | 97.29%           |
| 0.074          | 0.1151                    | 3.122               | 0.086               | 0.172                 | 2.75%             | 6.078              | 97.25%<br>97.20% |
| 0.075<br>0.076 | 0.1166<br>0.1182          | 3.168<br>3.214      | 0.087<br>0.089      | 0.175<br>0.177        | 2.80%<br>2.84%    | 6.075<br>6.073     | 97.20%           |
| 0.076          | 0.1182                    | 3.261               | 0.090               | 0.177                 | 2.88%             | 6.070              | 97.10%           |
| 0.077          | 0.1213                    | 3.307               | 0.091               | 0.182                 | 2.92%             | 6.068              | 97.08%           |
| 0.079          | 0.1228                    | 3.354               | 0.092               | 0.185                 | 2.96%             | 6.065              | 97.04%           |
| 0.08           | 0.1244                    | 3.400               | 0.094               | 0.187                 | 3.00%             | 6.063              | 97.00%           |
| 0.081          | 0.1259                    | 3.447               | 0.095               | 0.190                 | 3.04%             | 6.060              | 96.96%           |
| 0.082          | 0.1275                    | 3.494               | 0.096               | 0.193                 | 3.08%             | 6.057              | 96.92%           |
| 0.083          | 0.1290                    | 3.541               | 0.098               | 0.195                 | 3.12%             | 6.055              | 96.88%           |
| 0.084          | 0.1306                    | 3.588               | 0.099               | 0.198                 | 3.16%             | 6.052              | 96.84%           |
| 0.085          | 0.1322                    | 3.636               | 0.100               | 0.200                 | 3.21%             | 6.050              | 96.79%           |
| 0.086          | 0.1337                    | 3.683               | 0.101               | 0.203                 | 3.25%             | 6.047              | 96.75%           |
| 0.087          | 0.1353                    | 3.731               | 0.103               | 0.206                 | 3.29%             | 6.044              | 96.71%           |

| MTS reading | true length<br>(Δh_actuator) | ramp angle<br>(deg) | Δh_ramp_edge (inch) | Area blocked (inch^2) | % area<br>blocked | Flow area (inch^2) | %Flow area       |
|-------------|------------------------------|---------------------|---------------------|-----------------------|-------------------|--------------------|------------------|
| 0.088       | 0.1368                       | 3.778               | 0.104               | 0.208                 | 3.33%             | 6.042              | 96.67%           |
| 0.089       | 0.1384                       | 3.826               | 0.105               | 0.211                 | 3.37%             | 6.039              | 96.63%           |
| 0.09        | 0.1399                       | 3.874               | 0.107               | 0.213                 | 3.41%             | 6.037              | 96.59%           |
| 0.091       | 0.1415                       | 3.922               | 0.108               | 0.216                 | 3.46%             | 6.034              | 96.54%           |
| 0.092       | 0.1430                       | 3.970               | 0.109               | 0.219                 | 3.50%             | 6.031              | 96.50%           |
| 0.093       | 0.1446                       | 4.018               | 0.111               | 0.221                 | 3.54%             | 6.029              | 96.46%           |
| 0.094       | 0.1462                       | 4.067               | 0.112               | 0.224                 | 3.58%             | 6.026              | 96.42%           |
| 0.095       | 0.1477                       | 4.115               | 0.113               | 0.227                 | 3.62%             | 6.023              | 96.38%           |
| 0.096       | 0.1493                       | 4.164               | 0.115               | 0.229                 | 3.67%             | 6.021              | 96.33%           |
| 0.097       | 0.1508                       | 4.213               | 0.116               | 0.232                 | 3.71%             | 6.018              | 96.29%           |
| 0.098       | 0.1524                       | 4.261               | 0.117<br>0.119      | 0.235                 | 3.75%             | 6.015              | 96.25%           |
| 0.099       | 0.1539<br>0.1555             | 4.310<br>4.359      | 0.119               | 0.237<br>0.240        | 3.80%<br>3.84%    | 6.013<br>6.010     | 96.20%<br>96.16% |
| 0.101       | 0.1555                       | 4.409               | 0.120               | 0.240                 | 3.88%             | 6.007              | 96.10%           |
| 0.101       | 0.1576                       | 4.458               | 0.123               | 0.245                 | 3.92%             | 6.005              | 96.08%           |
| 0.102       | 0.1601                       | 4.508               | 0.124               | 0.248                 | 3.97%             | 6.002              | 96.03%           |
| 0.104       | 0.1617                       | 4.557               | 0.125               | 0.251                 | 4.01%             | 5.999              | 95.99%           |
| 0.105       | 0.1633                       | 4.607               | 0.127               | 0.253                 | 4.05%             | 5.997              | 95.95%           |
| 0.106       | 0.1648                       | 4.657               | 0.128               | 0.256                 | 4.10%             | 5.994              | 95.90%           |
| 0.107       | 0.1664                       | 4.707               | 0.129               | 0.259                 | 4.14%             | 5.991              | 95.86%           |
| 0.108       | 0.1679                       | 4.757               | 0.131               | 0.262                 | 4.19%             | 5.988              | 95.81%           |
| 0.109       | 0.1695                       | 4.807               | 0.132               | 0.264                 | 4.23%             | 5.986              | 95.77%           |
| 0.11        | 0.1710                       | 4.857               | 0.134               | 0.267                 | 4.27%             | 5.983              | 95.73%           |
| 0.111       | 0.1726                       | 4.908               | 0.135               | 0.270                 | 4.32%             | 5.980              | 95.68%           |
| 0.112       | 0.1741                       | 4.958               | 0.136               | 0.273                 | 4.36%             | 5.977              | 95.64%           |
| 0.113       | 0.1757                       | 5.009               | 0.138               | 0.275                 | 4.41%             | 5.975              | 95.59%           |
| 0.114       | 0.1772                       | 5.060               | 0.139               | 0.278                 | 4.45%             | 5.972              | 95.55%           |
| 0.115       | 0.1788                       | 5.111               | 0.140               | 0.281                 | 4.49%             | 5.969              | 95.51%           |
| 0.116       | 0.1804                       | 5.162               | 0.142               | 0.284                 | 4.54%             | 5.966              | 95.46%           |
| 0.117       | 0.1819                       | 5.213               | 0.143               | 0.286                 | 4.58%             | 5.964              | 95.42%           |
| 0.118       | 0.1835                       | 5.265               | 0.145               | 0.289                 | 4.63%             | 5.961              | 95.37%           |
| 0.119       | 0.1850<br>0.1866             | 5.316<br>5.368      | 0.146<br>0.147      | 0.292<br>0.295        | 4.67%<br>4.72%    | 5.958<br>5.955     | 95.33%<br>95.28% |
| 0.12        | 0.1881                       | 5.420               | 0.149               | 0.293                 | 4.72%             | 5.953              | 95.24%           |
| 0.121       | 0.1897                       | 5.472               | 0.150               | 0.300                 | 4.81%             | 5.950              | 95.19%           |
| 0.123       | 0.1912                       | 5.524               | 0.152               | 0.303                 | 4.85%             | 5.947              | 95.15%           |
| 0.124       | 0.1928                       | 5.576               | 0.153               | 0.306                 | 4.90%             | 5.944              | 95.10%           |
| 0.125       | 0.1944                       | 5.628               | 0.154               | 0.309                 | 4.94%             | 5.941              | 95.06%           |
| 0.126       | 0.1959                       | 5.681               | 0.156               | 0.312                 | 4.99%             | 5.938              | 95.01%           |
| 0.127       | 0.1975                       | 5.733               | 0.157               | 0.315                 | 5.03%             | 5.935              | 94.97%           |
| 0.128       | 0.1990                       | 5.786               | 0.159               | 0.318                 | 5.08%             | 5.932              | 94.92%           |
| 0.129       | 0.2006                       | 5.839               | 0.160               | 0.320                 | 5.13%             | 5.930              | 94.87%           |
| 0.13        | 0.2021                       | 5.892               | 0.162               | 0.323                 | 5.17%             | 5.927              | 94.83%           |
| 0.131       | 0.2037                       | 5.945               | 0.163               | 0.326                 | 5.22%             | 5.924              | 94.78%           |
| 0.132       | 0.2052                       | 5.998               | 0.165               | 0.329                 | 5.26%             | 5.921              | 94.74%           |

| MTS reading    | true length<br>(Δh_actuator) | ramp angle<br>(deg) | Δh_ramp_edge (inch) | Area blocked (inch^2) | % area<br>blocked | Flow area (inch^2) | %Flow area       |
|----------------|------------------------------|---------------------|---------------------|-----------------------|-------------------|--------------------|------------------|
| 0.133          | 0.2068                       | 6.051               | 0.166               | 0.332                 | 5.31%             | 5.918              | 94.69%           |
| 0.134          | 0.2083                       | 6.105               | 0.167               | 0.335                 | 5.36%             | 5.915              | 94.64%           |
| 0.135          | 0.2099                       | 6.159               | 0.169               | 0.338                 | 5.40%             | 5.912              | 94.60%           |
| 0.136          | 0.2115                       | 6.212               | 0.170               | 0.341                 | 5.45%             | 5.909              | 94.55%           |
| 0.137          | 0.2130                       | 6.266               | 0.172               | 0.344                 | 5.50%             | 5.906              | 94.50%           |
| 0.138          | 0.2146                       | 6.320               | 0.173               | 0.346                 | 5.54%             | 5.904              | 94.46%           |
| 0.139          | 0.2161                       | 6.375               | 0.175               | 0.349                 | 5.59%             | 5.901              | 94.41%           |
| 0.14           | 0.2177                       | 6.429               | 0.176               | 0.352                 | 5.64%             | 5.898              | 94.36%           |
| 0.141          | 0.2192                       | 6.483               | 0.178               | 0.355                 | 5.68%             | 5.895              | 94.32%           |
| 0.142          | 0.2208                       | 6.538               | 0.179               | 0.358                 | 5.73%             | 5.892              | 94.27%           |
| 0.143          | 0.2223                       | 6.593               | 0.181               | 0.361                 | 5.78%             | 5.889              | 94.22%           |
| 0.144          | 0.2239                       | 6.648               | 0.182               | 0.364                 | 5.83%             | 5.886              | 94.17%           |
| 0.145          | 0.2254                       | 6.703               | 0.184               | 0.367                 | 5.87%             | 5.883              | 94.13%           |
| 0.146<br>0.147 | 0.2270<br>0.2286             | 6.758<br>6.813      | 0.185<br>0.187      | 0.370<br>0.373        | 5.92%<br>5.97%    | 5.880<br>5.877     | 94.08%<br>94.03% |
| 0.147          | 0.2301                       | 6.869               | 0.188               | 0.376                 | 6.02%             | 5.874              | 93.98%           |
| 0.149          | 0.2317                       | 6.925               | 0.190               | 0.379                 | 6.07%             | 5.871              | 93.93%           |
| 0.15           | 0.2332                       | 6.980               | 0.191               | 0.382                 | 6.11%             | 5.868              | 93.89%           |
| 0.151          | 0.2348                       | 7.036               | 0.193               | 0.385                 | 6.16%             | 5.865              | 93.84%           |
| 0.152          | 0.2363                       | 7.092               | 0.194               | 0.388                 | 6.21%             | 5.862              | 93.79%           |
| 0.153          | 0.2379                       | 7.148               | 0.196               | 0.391                 | 6.26%             | 5.859              | 93.74%           |
| 0.154          | 0.2394                       | 7.205               | 0.197               | 0.394                 | 6.31%             | 5.856              | 93.69%           |
| 0.155          | 0.2410                       | 7.261               | 0.199               | 0.397                 | 6.36%             | 5.853              | 93.64%           |
| 0.156          | 0.2425                       | 7.318               | 0.200               | 0.400                 | 6.41%             | 5.850              | 93.59%           |
| 0.157          | 0.2441                       | 7.375               | 0.202               | 0.403                 | 6.45%             | 5.847              | 93.55%           |
| 0.158          | 0.2457                       | 7.432               | 0.203               | 0.406                 | 6.50%             | 5.844              | 93.50%           |
| 0.159          | 0.2472                       | 7.489               | 0.205               | 0.410                 | 6.55%             | 5.840              | 93.45%           |
| 0.16           | 0.2488                       | 7.546               | 0.206               | 0.413                 | 6.60%             | 5.837              | 93.40%           |
| 0.161          | 0.2503                       | 7.603               | 0.208               | 0.416                 | 6.65%             | 5.834              | 93.35%           |
| 0.162          | 0.2519                       | 7.661               | 0.209               | 0.419                 | 6.70%             | 5.831              | 93.30%           |
| 0.163          | 0.2534                       | 7.719               | 0.211               | 0.422                 | 6.75%             | 5.828              | 93.25%           |
| 0.164          | 0.2550                       | 7.777               | 0.213               | 0.425                 | 6.80%             | 5.825              | 93.20%           |
| 0.165          | 0.2565                       | 7.835               | 0.214               | 0.428                 | 6.85%             | 5.822              | 93.15%           |
| 0.166          | 0.2581                       | 7.893               | 0.216               | 0.431                 | 6.90%             | 5.819              | 93.10%           |
| 0.167<br>0.168 | 0.2597<br>0.2612             | 7.951<br>8.009      | 0.217<br>0.219      | 0.434<br>0.438        | 6.95%<br>7.00%    | 5.816<br>5.812     | 93.05%<br>93.00% |
|                | 0.2612                       |                     |                     |                       |                   |                    |                  |
| 0.169<br>0.17  | 0.2628                       | 8.068<br>8.127      | 0.220<br>0.222      | 0.441<br>0.444        | 7.05%<br>7.10%    | 5.809<br>5.806     | 92.95%<br>92.90% |
| 0.171          | 0.2659                       | 8.186               | 0.223               | 0.447                 | 7.10%             | 5.803              | 92.85%           |
| 0.171          | 0.2674                       | 8.245               | 0.225               | 0.450                 | 7.13%             | 5.800              | 92.80%           |
| 0.173          | 0.2690                       | 8.304               | 0.227               | 0.453                 | 7.25%             | 5.797              | 92.75%           |
| 0.174          | 0.2705                       | 8.363               | 0.228               | 0.456                 | 7.30%             | 5.794              | 92.70%           |
| 0.175          | 0.2721                       | 8.423               | 0.230               | 0.460                 | 7.35%             | 5.790              | 92.65%           |
| 0.176          | 0.2736                       | 8.483               | 0.231               | 0.463                 | 7.41%             | 5.787              | 92.59%           |
| 0.177          | 0.2752                       | 8.542               | 0.233               | 0.466                 | 7.46%             | 5.784              | 92.54%           |

| MTS reading | true length<br>(Δh_actuator) | ramp angle<br>(deg) | Δh_ramp_edge (inch) | Area blocked (inch^2) | % area         | Flow area (inch^2) | %Flow area       |
|-------------|------------------------------|---------------------|---------------------|-----------------------|----------------|--------------------|------------------|
| 0.178       | 0.2768                       | 8.602               | 0.235               | 0.469                 | 7.51%          | 5.781              | 92.49%           |
| 0.179       | 0.2783                       | 8.663               | 0.236               | 0.472                 | 7.56%          | 5.778              | 92.44%           |
| 0.18        | 0.2799                       | 8.723               | 0.238               | 0.476                 | 7.61%          | 5.774              | 92.39%           |
| 0.181       | 0.2814                       | 8.783               | 0.239               | 0.479                 | 7.66%          | 5.771              | 92.34%           |
| 0.182       | 0.2830                       | 8.844               | 0.241               | 0.482                 | 7.72%          | 5.768              | 92.28%           |
| 0.183       | 0.2845                       | 8.905               | 0.243               | 0.485                 | 7.77%          | 5.765              | 92.23%           |
| 0.184       | 0.2861                       | 8.966               | 0.244               | 0.489                 | 7.82%          | 5.761              | 92.18%           |
| 0.185       | 0.2876                       | 9.027               | 0.246               | 0.492                 | 7.87%          | 5.758              | 92.13%           |
| 0.186       | 0.2892                       | 9.088               | 0.248               | 0.495                 | 7.92%          | 5.755              | 92.08%           |
| 0.187       | 0.2907                       | 9.150               | 0.249               | 0.499                 | 7.98%          | 5.751              | 92.02%           |
| 0.188       | 0.2923                       | 9.211               | 0.251               | 0.502                 | 8.03%          | 5.748              | 91.97%           |
| 0.189       | 0.2939                       | 9.273               | 0.253               | 0.505                 | 8.08%          | 5.745              | 91.92%           |
| 0.19        | 0.2954                       | 9.335               | 0.254               | 0.508                 | 8.13%          | 5.742              | 91.87%           |
| 0.191       | 0.2970                       | 9.397               | 0.256               | 0.512                 | 8.19%          | 5.738              | 91.81%           |
| 0.192       | 0.2985                       | 9.459               | 0.257               | 0.515                 | 8.24%          | 5.735              | 91.76%           |
| 0.193       | 0.3001                       | 9.522               | 0.259               | 0.518                 | 8.29%          | 5.732              | 91.71%           |
| 0.194       | 0.3016                       | 9.584               | 0.261               | 0.522                 | 8.35%          | 5.728              | 91.65%           |
| 0.195       | 0.3032                       | 9.647               | 0.262               | 0.525                 | 8.40%          | 5.725              | 91.60%           |
| 0.196       | 0.3047                       | 9.710               | 0.264               | 0.528                 | 8.45%          | 5.722              | 91.55%           |
| 0.197       | 0.3063                       | 9.773               | 0.266               | 0.532                 | 8.51%          | 5.718              | 91.49%           |
| 0.198       | 0.3079                       | 9.836               | 0.268               | 0.535                 | 8.56%          | 5.715              | 91.44%           |
| 0.199       | 0.3094                       | 9.900               | 0.269               | 0.538                 | 8.61%          | 5.712              | 91.39%           |
| 0.2         | 0.3110                       | 9.963               | 0.271               | 0.542                 | 8.67%          | 5.708              | 91.33%           |
| 0.201       | 0.3125                       | 10.027              | 0.273               | 0.545                 | 8.72%          | 5.705              | 91.28%           |
| 0.202       | 0.3141                       | 10.091              | 0.274               | 0.549                 | 8.78%          | 5.701              | 91.22%           |
| 0.203       | 0.3156                       | 10.155              | 0.276               | 0.552                 | 8.83%          | 5.698              | 91.17%           |
| 0.204       | 0.3172                       | 10.219              | 0.278               | 0.555                 | 8.89%          | 5.695              | 91.11%           |
| 0.205       | 0.3187                       | 10.284              | 0.279               | 0.559                 | 8.94%          | 5.691              | 91.06%           |
| 0.206       | 0.3203                       | 10.348              | 0.281               | 0.562                 | 9.00%          | 5.688              | 91.00%           |
| 0.207       | 0.3218                       | 10.413              | 0.283               | 0.566                 | 9.05%          | 5.684              | 90.95%           |
| 0.208       | 0.3234                       | 10.478              | 0.285               | 0.569                 | 9.10%          | 5.681<br>5.677     | 90.90%           |
| 0.209       | 0.3250                       | 10.543              | 0.286               | 0.573                 | 9.16%          |                    | 90.84%           |
| 0.21        | 0.3265<br>0.3281             | 10.608<br>10.674    | 0.288<br>0.290      | 0.576<br>0.579        | 9.22%<br>9.27% | 5.674              | 90.78%<br>90.73% |
| 0.211       | 0.3281                       | 10.740              | 0.291               | 0.583                 | 9.33%          | 5.671<br>5.667     | 90.73%           |
| 0.212       | 0.3312                       | 10.740              | 0.293               | 0.586                 | 9.38%          | 5.664              | 90.62%           |
| 0.213       | 0.3312                       | 10.803              | 0.295               | 0.590                 | 9.44%          | 5.660              | 90.56%           |
| 0.214       | 0.3343                       | 10.938              | 0.297               | 0.593                 | 9.49%          | 5.657              | 90.51%           |
| 0.216       | 0.3358                       | 11.004              | 0.298               | 0.597                 | 9.55%          | 5.653              | 90.45%           |
| 0.217       | 0.3374                       | 11.070              | 0.300               | 0.600                 | 9.61%          | 5.650              | 90.39%           |
| 0.217       | 0.3389                       | 11.137              | 0.302               | 0.604                 | 9.66%          | 5.646              | 90.34%           |
| 0.219       | 0.3405                       | 11.204              | 0.304               | 0.607                 | 9.72%          | 5.643              | 90.28%           |
| 0.22        | 0.3421                       | 11.271              | 0.305               | 0.611                 | 9.77%          | 5.639              | 90.23%           |
| 0.221       | 0.3436                       | 11.338              | 0.307               | 0.614                 | 9.83%          | 5.636              | 90.17%           |
| 0.222       | 0.3452                       | 11.406              | 0.309               | 0.618                 | 9.89%          | 5.632              | 90.11%           |

| MTS reading    | true length<br>(Δh_actuator) | ramp angle<br>(deg) | Δh_ramp_edge (inch) | Area blocked (inch^2) | % area<br>blocked | Flow area (inch^2) | %Flow area       |
|----------------|------------------------------|---------------------|---------------------|-----------------------|-------------------|--------------------|------------------|
| 0.223          | 0.3467                       | 11.473              | 0.311               | 0.622                 | 9.94%             | 5.628              | 90.06%           |
| 0.224          | 0.3483                       | 11.541              | 0.313               | 0.625                 | 10.00%            | 5.625              | 90.00%           |
| 0.225          | 0.3498                       | 11.609              | 0.314               | 0.629                 | 10.06%            | 5.621              | 89.94%           |
| 0.226          | 0.3514                       | 11.677              | 0.316               | 0.632                 | 10.12%            | 5.618              | 89.88%           |
| 0.227          | 0.3529                       | 11.746              | 0.318               | 0.636                 | 10.17%            | 5.614              | 89.83%           |
| 0.228          | 0.3545                       | 11.814              | 0.320               | 0.639                 | 10.23%            | 5.611              | 89.77%           |
| 0.229          | 0.3561                       | 11.883              | 0.322               | 0.643                 | 10.29%            | 5.607              | 89.71%           |
| 0.23           | 0.3576                       | 11.952              | 0.323               | 0.647                 | 10.35%            | 5.603              | 89.65%           |
| 0.231          | 0.3592                       | 12.021              | 0.325               | 0.650                 | 10.40%            | 5.600              | 89.60%           |
| 0.232          | 0.3607                       | 12.090              | 0.327               | 0.654                 | 10.46%            | 5.596              | 89.54%           |
| 0.233          | 0.3623                       | 12.159<br>12.229    | 0.329<br>0.331      | 0.658                 | 10.52%            | 5.592<br>5.589     | 89.48%           |
| 0.235          | 0.3638<br>0.3654             | 12.229              | 0.332               | 0.661<br>0.665        | 10.58%<br>10.64%  | 5.585              | 89.42%<br>89.36% |
| 0.236          | 0.3669                       | 12.299              | 0.334               | 0.668                 | 10.70%            | 5.582              | 89.30%           |
| 0.237          | 0.3685                       | 12.439              | 0.336               | 0.672                 | 10.75%            | 5.578              | 89.25%           |
| 0.238          | 0.3700                       | 12.509              | 0.338               | 0.676                 | 10.81%            | 5.574              | 89.19%           |
| 0.239          | 0.3716                       | 12.580              | 0.340               | 0.680                 | 10.87%            | 5.570              | 89.13%           |
| 0.24           | 0.3732                       | 12.651              | 0.342               | 0.683                 | 10.93%            | 5.567              | 89.07%           |
| 0.241          | 0.3747                       | 12.722              | 0.343               | 0.687                 | 10.99%            | 5.563              | 89.01%           |
| 0.242          | 0.3763                       | 12.793              | 0.345               | 0.691                 | 11.05%            | 5.559              | 88.95%           |
| 0.243          | 0.3778                       | 12.864              | 0.347               | 0.694                 | 11.11%            | 5.556              | 88.89%           |
| 0.244          | 0.3794                       | 12.936              | 0.349               | 0.698                 | 11.17%            | 5.552              | 88.83%           |
| 0.245          | 0.3809                       | 13.007              | 0.351               | 0.702                 | 11.23%            | 5.548              | 88.77%           |
| 0.246          | 0.3825                       | 13.079              | 0.353               | 0.706                 | 11.29%            | 5.544              | 88.71%           |
| 0.247          | 0.3840                       | 13.151              | 0.355               | 0.709                 | 11.35%            | 5.541              | 88.65%           |
| 0.248          | 0.3856                       | 13.224              | 0.357               | 0.713                 | 11.41%            | 5.537              | 88.59%           |
| 0.249          | 0.3871                       | 13.296              | 0.358               | 0.717                 | 11.47%            | 5.533              | 88.53%           |
| 0.25           | 0.3887                       | 13.369              | 0.360               | 0.721                 | 11.53%            | 5.529              | 88.47%           |
| 0.251          | 0.3903                       | 13.442              | 0.362               | 0.724                 | 11.59%            | 5.526              | 88.41%           |
| 0.252          | 0.3918                       | 13.515              | 0.364               | 0.728                 | 11.65%            | 5.522              | 88.35%           |
| 0.253          | 0.3934                       | 13.588              | 0.366               | 0.732                 | 11.71%            | 5.518              | 88.29%           |
| 0.254          | 0.3949                       | 13.661              | 0.368               | 0.736                 | 11.77%            | 5.514              | 88.23%           |
| 0.255<br>0.256 | 0.3965<br>0.3980             | 13.735<br>13.809    | 0.370<br>0.372      | 0.740<br>0.743        | 11.83%<br>11.89%  | 5.510<br>5.507     | 88.17%<br>88.11% |
| 0.257          | 0.3980                       | 13.883              | 0.374               | 0.743                 | 11.96%            | 5.507              | 88.04%           |
| 0.258          | 0.4011                       | 13.957              | 0.376               | 0.747                 | 12.02%            | 5.499              | 87.98%           |
| 0.259          | 0.4027                       | 14.032              | 0.377               | 0.755                 | 12.08%            | 5.495              | 87.92%           |
| 0.26           | 0.4042                       | 14.106              | 0.379               | 0.759                 | 12.14%            | 5.491              | 87.86%           |
| 0.261          | 0.4058                       | 14.181              | 0.381               | 0.763                 | 12.20%            | 5.487              | 87.80%           |
| 0.262          | 0.4074                       | 14.256              | 0.383               | 0.766                 | 12.26%            | 5.484              | 87.74%           |
| 0.263          | 0.4089                       | 14.332              | 0.385               | 0.770                 | 12.33%            | 5.480              | 87.67%           |
| 0.264          | 0.4105                       | 14.407              | 0.387               | 0.774                 | 12.39%            | 5.476              | 87.61%           |
| 0.265          | 0.4120                       | 14.483              | 0.389               | 0.778                 | 12.45%            | 5.472              | 87.55%           |
| 0.266          | 0.4136                       | 14.559              | 0.391               | 0.782                 | 12.51%            | 5.468              | 87.49%           |
| 0.267          | 0.4151                       | 14.635              | 0.393               | 0.786                 | 12.58%            | 5.464              | 87.42%           |

| MTS reading    | true length<br>(Δh_actuator) | ramp angle<br>(deg) | Δh_ramp_edge (inch) | Area blocked (inch^2) | % area<br>blocked | Flow area (inch^2) | %Flow area       |
|----------------|------------------------------|---------------------|---------------------|-----------------------|-------------------|--------------------|------------------|
| 0.268          | 0.4167                       | 14.711              | 0.395               | 0.790                 | 12.64%            | 5.460              | 87.36%           |
| 0.269          | 0.4182                       | 14.788              | 0.397               | 0.794                 | 12.70%            | 5.456              | 87.30%           |
| 0.27           | 0.4198                       | 14.864              | 0.399               | 0.798                 | 12.76%            | 5.452              | 87.24%           |
| 0.271          | 0.4214                       | 14.941              | 0.401               | 0.802                 | 12.83%            | 5.448              | 87.17%           |
| 0.272          | 0.4229                       | 15.018              | 0.403               | 0.806                 | 12.89%            | 5.444              | 87.11%           |
| 0.273          | 0.4245                       | 15.096              | 0.405               | 0.810                 | 12.95%            | 5.440              | 87.05%           |
| 0.274          | 0.4260                       | 15.173              | 0.407               | 0.814                 | 13.02%            | 5.436              | 86.98%           |
| 0.275          | 0.4276                       | 15.251              | 0.409               | 0.818                 | 13.08%            | 5.432              | 86.92%           |
| 0.276          | 0.4291                       | 15.329              | 0.411               | 0.822                 | 13.14%            | 5.428              | 86.86%           |
| 0.277          | 0.4307                       | 15.407              | 0.413               | 0.826                 | 13.21%            | 5.424              | 86.79%           |
| 0.278<br>0.279 | 0.4322<br>0.4338             | 15.485              | 0.415               | 0.830                 | 13.27%            | 5.420              | 86.73%           |
| 0.279          | 0.4353                       | 15.564<br>15.643    | 0.417<br>0.419      | 0.834<br>0.838        | 13.34%<br>13.40%  | 5.416<br>5.412     | 86.66%<br>86.60% |
| 0.281          | 0.4369                       | 15.722              | 0.421               | 0.842                 | 13.47%            | 5.408              | 86.53%           |
| 0.282          | 0.4385                       | 15.801              | 0.423               | 0.846                 | 13.53%            | 5.404              | 86.47%           |
| 0.283          | 0.4400                       | 15.880              | 0.425               | 0.850                 | 13.60%            | 5.400              | 86.40%           |
| 0.284          | 0.4416                       | 15.960              | 0.427               | 0.854                 | 13.66%            | 5.396              | 86.34%           |
| 0.285          | 0.4431                       | 16.040              | 0.429               | 0.858                 | 13.72%            | 5.392              | 86.28%           |
| 0.286          | 0.4447                       | 16.120              | 0.431               | 0.862                 | 13.79%            | 5.388              | 86.21%           |
| 0.287          | 0.4462                       | 16.200              | 0.433               | 0.866                 | 13.86%            | 5.384              | 86.14%           |
| 0.288          | 0.4478                       | 16.281              | 0.435               | 0.870                 | 13.92%            | 5.380              | 86.08%           |
| 0.289          | 0.4493                       | 16.361              | 0.437               | 0.874                 | 13.99%            | 5.376              | 86.01%           |
| 0.29           | 0.4509                       | 16.442              | 0.439               | 0.878                 | 14.05%            | 5.372              | 85.95%           |
| 0.291          | 0.4524                       | 16.524              | 0.441               | 0.882                 | 14.12%            | 5.368              | 85.88%           |
| 0.292          | 0.4540                       | 16.605              | 0.443               | 0.886                 | 14.18%            | 5.364              | 85.82%           |
| 0.293          | 0.4556                       | 16.687              | 0.445               | 0.891                 | 14.25%            | 5.359              | 85.75%           |
| 0.294          | 0.4571                       | 16.768              | 0.447               | 0.895                 | 14.32%            | 5.355              | 85.68%           |
| 0.295          | 0.4587                       | 16.850              | 0.449               | 0.899                 | 14.38%            | 5.351              | 85.62%           |
| 0.296          | 0.4602                       | 16.933              | 0.452               | 0.903                 | 14.45%            | 5.347              | 85.55%           |
| 0.297          | 0.4618                       | 17.015              | 0.454               | 0.907                 | 14.52%            | 5.343              | 85.48%           |
| 0.298          | 0.4633                       | 17.098              | 0.456               | 0.911                 | 14.58%            | 5.339              | 85.42%           |
| 0.299          | 0.4649                       | 17.181              | 0.458               | 0.916                 | 14.65%            | 5.334              | 85.35%           |
| 0.301          | 0.4664<br>0.4680             | 17.264<br>17.347    | 0.460<br>0.462      | 0.920<br>0.924        | 14.72%<br>14.78%  | 5.330<br>5.326     | 85.28%<br>85.22% |
| 0.301          | 0.4696                       | 17.431              | 0.464               | 0.924                 | 14.76%            | 5.322              | 85.15%           |
| 0.302          | 0.4711                       | 17.515              | 0.466               | 0.932                 | 14.92%            | 5.318              | 85.08%           |
| 0.304          | 0.4727                       | 17.519              | 0.468               | 0.937                 | 14.98%            | 5.313              | 85.02%           |
| 0.305          | 0.4742                       | 17.683              | 0.470               | 0.941                 | 15.05%            | 5.309              | 84.95%           |
| 0.306          | 0.4758                       | 17.768              | 0.473               | 0.945                 | 15.12%            | 5.305              | 84.88%           |
| 0.307          | 0.4773                       | 17.852              | 0.475               | 0.949                 | 15.19%            | 5.301              | 84.81%           |
| 0.308          | 0.4789                       | 17.937              | 0.477               | 0.954                 | 15.26%            | 5.296              | 84.74%           |
| 0.309          | 0.4804                       | 18.022              | 0.479               | 0.958                 | 15.32%            | 5.292              | 84.68%           |
| 0.31           | 0.4820                       | 18.108              | 0.481               | 0.962                 | 15.39%            | 5.288              | 84.61%           |
| 0.311          | 0.4835                       | 18.193              | 0.483               | 0.966                 | 15.46%            | 5.284              | 84.54%           |
| 0.312          | 0.4851                       | 18.279              | 0.485               | 0.971                 | 15.53%            | 5.279              | 84.47%           |

| MTS reading    | true length<br>(Δh_actuator) | ramp angle<br>(deg) | Δh_ramp_edge (inch) | Area blocked (inch^2) | % area<br>blocked | Flow area (inch^2) | %Flow area       |
|----------------|------------------------------|---------------------|---------------------|-----------------------|-------------------|--------------------|------------------|
| 0.313          | 0.4867                       | 18.365              | 0.487               | 0.975                 | 15.60%            | 5.275              | 84.40%           |
| 0.314          | 0.4882                       | 18.452              | 0.490               | 0.979                 | 15.67%            | 5.271              | 84.33%           |
| 0.315          | 0.4898                       | 18.538              | 0.492               | 0.984                 | 15.74%            | 5.266              | 84.26%           |
| 0.316          | 0.4913                       | 18.625              | 0.494               | 0.988                 | 15.81%            | 5.262              | 84.19%           |
| 0.317          | 0.4929                       | 18.712              | 0.496               | 0.992                 | 15.87%            | 5.258              | 84.13%           |
| 0.318          | 0.4944                       | 18.799              | 0.498               | 0.996                 | 15.94%            | 5.254              | 84.06%           |
| 0.319          | 0.4960                       | 18.887              | 0.500               | 1.001                 | 16.01%            | 5.249              | 83.99%           |
| 0.32           | 0.4975                       | 18.975              | 0.503               | 1.005                 | 16.08%            | 5.245              | 83.92%           |
| 0.321          | 0.4991                       | 19.063              | 0.505               | 1.010                 | 16.15%            | 5.240              | 83.85%           |
| 0.322          | 0.5006                       | 19.151              | 0.507               | 1.014                 | 16.22%            | 5.236              | 83.78%           |
| 0.323          | 0.5022                       | 19.239              | 0.509               | 1.018                 | 16.29%            | 5.232              | 83.71%           |
| 0.324<br>0.325 | 0.5038<br>0.5053             | 19.328<br>19.417    | 0.511<br>0.514      | 1.023<br>1.027        | 16.36%<br>16.43%  | 5.227<br>5.223     | 83.64%           |
| 0.326          | 0.5069                       | 19.417              | 0.516               | 1.027                 | 16.50%            | 5.223              | 83.57%<br>83.50% |
| 0.327          | 0.5084                       | 19.595              | 0.518               | 1.036                 | 16.57%            | 5.214              | 83.43%           |
| 0.328          | 0.5100                       | 19.685              | 0.520               | 1.040                 | 16.64%            | 5.210              | 83.36%           |
| 0.329          | 0.5115                       | 19.775              | 0.522               | 1.045                 | 16.72%            | 5.205              | 83.28%           |
| 0.33           | 0.5131                       | 19.865              | 0.525               | 1.049                 | 16.79%            | 5.201              | 83.21%           |
| 0.331          | 0.5146                       | 19.955              | 0.527               | 1.054                 | 16.86%            | 5.196              | 83.14%           |
| 0.332          | 0.5162                       | 20.046              | 0.529               | 1.058                 | 16.93%            | 5.192              | 83.07%           |
| 0.333          | 0.5178                       | 20.136              | 0.531               | 1.062                 | 17.00%            | 5.188              | 83.00%           |
| 0.334          | 0.5193                       | 20.228              | 0.533               | 1.067                 | 17.07%            | 5.183              | 82.93%           |
| 0.335          | 0.5209                       | 20.319              | 0.536               | 1.071                 | 17.14%            | 5.179              | 82.86%           |
| 0.336          | 0.5224                       | 20.410              | 0.538               | 1.076                 | 17.21%            | 5.174              | 82.79%           |
| 0.337          | 0.5240                       | 20.502              | 0.540               | 1.080                 | 17.29%            | 5.170              | 82.71%           |
| 0.338          | 0.5255                       | 20.594              | 0.542               | 1.085                 | 17.36%            | 5.165              | 82.64%           |
| 0.339          | 0.5271                       | 20.686              | 0.545               | 1.089                 | 17.43%            | 5.161              | 82.57%           |
| 0.34           | 0.5286                       | 20.779              | 0.547               | 1.094                 | 17.50%            | 5.156              | 82.50%           |
| 0.341          | 0.5302                       | 20.872              | 0.549               | 1.098                 | 17.57%            | 5.152              | 82.43%           |
| 0.342          | 0.5317                       | 20.965              | 0.551               | 1.103                 | 17.65%            | 5.147              | 82.35%           |
| 0.343          | 0.5333                       | 21.058              | 0.554               | 1.107                 | 17.72%            | 5.143              | 82.28%           |
| 0.344          | 0.5349                       | 21.151              | 0.556               | 1.112                 | 17.79%            | 5.138              | 82.21%           |
| 0.345<br>0.346 | 0.5364<br>0.5380             | 21.245<br>21.339    | 0.558<br>0.561      | 1.117<br>1.121        | 17.86%<br>17.94%  | 5.133<br>5.129     | 82.14%<br>82.06% |
| 0.347          | 0.5395                       | 21.433              | 0.563               | 1.126                 | 18.01%            | 5.129              | 81.99%           |
| 0.348          | 0.5411                       | 21.528              | 0.565               | 1.130                 | 18.08%            | 5.124              | 81.92%           |
| 0.349          | 0.5426                       | 21.623              | 0.567               | 1.135                 | 18.16%            | 5.115              | 81.84%           |
| 0.35           | 0.5442                       | 21.718              | 0.570               | 1.139                 | 18.23%            | 5.111              | 81.77%           |
| 0.351          | 0.5457                       | 21.813              | 0.572               | 1.144                 | 18.30%            | 5.106              | 81.70%           |
| 0.352          | 0.5473                       | 21.908              | 0.574               | 1.149                 | 18.38%            | 5.101              | 81.62%           |
| 0.353          | 0.5488                       | 22.004              | 0.577               | 1.153                 | 18.45%            | 5.097              | 81.55%           |
| 0.354          | 0.5504                       | 22.100              | 0.579               | 1.158                 | 18.52%            | 5.092              | 81.48%           |
| 0.355          | 0.5520                       | 22.196              | 0.581               | 1.162                 | 18.60%            | 5.088              | 81.40%           |
| 0.356          | 0.5535                       | 22.293              | 0.584               | 1.167                 | 18.67%            | 5.083              | 81.33%           |
| 0.357          | 0.5551                       | 22.389              | 0.586               | 1.172                 | 18.75%            | 5.078              | 81.25%           |

| MTS reading    | true length<br>(Δh_actuator) | ramp angle<br>(deg) | Δh_ramp_edge (inch) | Area blocked (inch^2) | % area<br>blocked | Flow area (inch^2) | %Flow area       |
|----------------|------------------------------|---------------------|---------------------|-----------------------|-------------------|--------------------|------------------|
| 0.358          | 0.5566                       | 22.486              | 0.588               | 1.176                 | 18.82%            | 5.074              | 81.18%           |
| 0.359          | 0.5582                       | 22.584              | 0.590               | 1.181                 | 18.90%            | 5.069              | 81.10%           |
| 0.36           | 0.5597                       | 22.681              | 0.593               | 1.186                 | 18.97%            | 5.064              | 81.03%           |
| 0.361          | 0.5613                       | 22.779              | 0.595               | 1.190                 | 19.04%            | 5.060              | 80.96%           |
| 0.362          | 0.5628                       | 22.877              | 0.597               | 1.195                 | 19.12%            | 5.055              | 80.88%           |
| 0.363          | 0.5644                       | 22.975              | 0.600               | 1.200                 | 19.19%            | 5.050              | 80.81%           |
| 0.364          | 0.5659                       | 23.074              | 0.602               | 1.204                 | 19.27%            | 5.046              | 80.73%           |
| 0.365          | 0.5675                       | 23.172              | 0.605               | 1.209                 | 19.34%            | 5.041              | 80.66%           |
| 0.366          | 0.5691                       | 23.271              | 0.607               | 1.214                 | 19.42%            | 5.036              | 80.58%           |
| 0.367          | 0.5706                       | 23.371              | 0.609               | 1.218                 | 19.49%            | 5.032              | 80.51%           |
| 0.368          | 0.5722                       | 23.470              | 0.612               | 1.223                 | 19.57%            | 5.027              | 80.43%           |
| 0.369          | 0.5737                       | 23.570              | 0.614               | 1.228                 | 19.65%            | 5.022              | 80.35%           |
| 0.37           | 0.5753                       | 23.670              | 0.616               | 1.233                 | 19.72%            | 5.017              | 80.28%           |
| 0.371          | 0.5768                       | 23.770              | 0.619               | 1.237                 | 19.80%            | 5.013              | 80.20%           |
| 0.372          | 0.5784                       | 23.871              | 0.621               | 1.242                 | 19.87%            | 5.008              | 80.13%           |
| 0.373          | 0.5799                       | 23.972              | 0.623               | 1.247                 | 19.95%            | 5.003              | 80.05%           |
| 0.374          | 0.5815                       | 24.073              | 0.626               | 1.252                 | 20.03%            | 4.998              | 79.97%           |
| 0.375<br>0.376 | 0.5831<br>0.5846             | 24.174<br>24.276    | 0.628<br>0.631      | 1.256<br>1.261        | 20.10%<br>20.18%  | 4.994<br>4.989     | 79.90%<br>79.82% |
| 0.377          | 0.5862                       | 24.270              | 0.633               | 1.266                 | 20.16%            | 4.984              | 79.75%           |
| 0.377          | 0.5877                       | 24.480              | 0.635               | 1.271                 | 20.23%            | 4.979              | 79.67%           |
| 0.379          | 0.5893                       | 24.582              | 0.638               | 1.275                 | 20.41%            | 4.975              | 79.59%           |
| 0.38           | 0.5908                       | 24.685              | 0.640               | 1.280                 | 20.48%            | 4.970              | 79.52%           |
| 0.381          | 0.5924                       | 24.787              | 0.643               | 1.285                 | 20.56%            | 4.965              | 79.44%           |
| 0.382          | 0.5939                       | 24.891              | 0.645               | 1.290                 | 20.64%            | 4.960              | 79.36%           |
| 0.383          | 0.5955                       | 24.994              | 0.647               | 1.295                 | 20.72%            | 4.955              | 79.28%           |
| 0.384          | 0.5970                       | 25.098              | 0.650               | 1.300                 | 20.79%            | 4.950              | 79.21%           |
| 0.385          | 0.5986                       | 25.202              | 0.652               | 1.304                 | 20.87%            | 4.946              | 79.13%           |
| 0.386          | 0.6002                       | 25.306              | 0.655               | 1.309                 | 20.95%            | 4.941              | 79.05%           |
| 0.387          | 0.6017                       | 25.410              | 0.657               | 1.314                 | 21.02%            | 4.936              | 78.98%           |
| 0.388          | 0.6033                       | 25.515              | 0.659               | 1.319                 | 21.10%            | 4.931              | 78.90%           |
| 0.389          | 0.6048                       | 25.620              | 0.662               | 1.324                 | 21.18%            | 4.926              | 78.82%           |
| 0.39           | 0.6064                       | 25.725              | 0.664               | 1.329                 | 21.26%            | 4.921              | 78.74%           |
| 0.391          | 0.6079                       | 25.831              | 0.667               | 1.333                 | 21.34%            | 4.917              | 78.66%           |
| 0.392          | 0.6095                       | 25.937              | 0.669               | 1.338                 | 21.41%            | 4.912              | 78.59%           |
| 0.393          | 0.6110                       | 26.043              | 0.672               | 1.343                 | 21.49%            | 4.907              | 78.51%           |
| 0.394          | 0.6126                       | 26.149              | 0.674               | 1.348                 | 21.57%            | 4.902              | 78.43%           |
| 0.395          | 0.6141                       | 26.256              | 0.676               | 1.353                 | 21.65%            | 4.897              | 78.35%           |
| 0.396          | 0.6157                       | 26.362              | 0.679               | 1.358                 | 21.73%            | 4.892              | 78.27%           |
| 0.397          | 0.6173                       | 26.470              | 0.681               | 1.363                 | 21.80%            | 4.887              | 78.20%           |
| 0.398          | 0.6188                       | 26.577              | 0.684               | 1.368                 | 21.88%            | 4.882              | 78.12%           |
| 0.399          | 0.6204                       | 26.685              | 0.686               | 1.373                 | 21.96%            | 4.877              | 78.04%           |
| 0.4            | 0.6219                       | 26.792              | 0.689               | 1.377                 | 22.04%            | 4.873              | 77.96%           |
| 0.401          | 0.6235                       | 26.901              | 0.691               | 1.382                 | 22.12%            | 4.868              | 77.88%           |
| 0.402          | 0.6250                       | 27.009              | 0.694               | 1.387                 | 22.20%            | 4.863              | 77.80%           |

| MTS reading    | true length<br>(Δh_actuator) | ramp angle<br>(deg) | Δh_ramp_edge (inch) | Area blocked (inch^2) | % area<br>blocked | Flow area (inch^2) | %Flow area       |
|----------------|------------------------------|---------------------|---------------------|-----------------------|-------------------|--------------------|------------------|
| 0.403          | 0.6266                       | 27.118              | 0.696               | 1.392                 | 22.28%            | 4.858              | 77.72%           |
| 0.404          | 0.6281                       | 27.227              | 0.699               | 1.397                 | 22.36%            | 4.853              | 77.64%           |
| 0.405          | 0.6297                       | 27.336              | 0.701               | 1.402                 | 22.43%            | 4.848              | 77.57%           |
| 0.406          | 0.6313                       | 27.446              | 0.704               | 1.407                 | 22.51%            | 4.843              | 77.49%           |
| 0.407          | 0.6328                       | 27.555              | 0.706               | 1.412                 | 22.59%            | 4.838              | 77.41%           |
| 0.408          | 0.6344                       | 27.665              | 0.709               | 1.417                 | 22.67%            | 4.833              | 77.33%           |
| 0.409          | 0.6359                       | 27.776              | 0.711               | 1.422                 | 22.75%            | 4.828              | 77.25%           |
| 0.41           | 0.6375                       | 27.886              | 0.713               | 1.427                 | 22.83%            | 4.823              | 77.17%           |
| 0.411          | 0.6390                       | 27.997              | 0.716               | 1.432                 | 22.91%            | 4.818              | 77.09%           |
| 0.412          | 0.6406                       | 28.108              | 0.718               | 1.437                 | 22.99%            | 4.813              | 77.01%           |
| 0.413          | 0.6421                       | 28.220              | 0.721               | 1.442                 | 23.07%            | 4.808              | 76.93%           |
| 0.414          | 0.6437                       | 28.331              | 0.723               | 1.447                 | 23.15%            | 4.803              | 76.85%           |
| 0.415          | 0.6452                       | 28.443              | 0.726               | 1.452                 | 23.23%            | 4.798              | 76.77%           |
| 0.416          | 0.6468                       | 28.555              | 0.728               | 1.457                 | 23.31%            | 4.793              | 76.69%           |
| 0.417          | 0.6484                       | 28.668              | 0.731               | 1.462                 | 23.39%            | 4.788              | 76.61%           |
| 0.418          | 0.6499                       | 28.781              | 0.733               | 1.467                 | 23.47%            | 4.783              | 76.53%           |
| 0.419          | 0.6515                       | 28.894              | 0.736               | 1.472                 | 23.55%            | 4.778              | 76.45%           |
| 0.42           | 0.6530                       | 29.007              | 0.738               | 1.477                 | 23.63%            | 4.773              | 76.37%           |
| 0.421          | 0.6546                       | 29.120              | 0.741               | 1.482                 | 23.71%            | 4.768              | 76.29%           |
| 0.422          | 0.6561                       | 29.234              | 0.743               | 1.487                 | 23.79%            | 4.763              | 76.21%           |
| 0.423          | 0.6577                       | 29.348              | 0.746               | 1.492                 | 23.87%            | 4.758              | 76.13%           |
| 0.424          | 0.6592                       | 29.463              | 0.748               | 1.497                 | 23.95%            | 4.753              | 76.05%           |
| 0.425          | 0.6608                       | 29.577              | 0.751               | 1.502                 | 24.03%            | 4.748              | 75.97%           |
| 0.426          | 0.6623                       | 29.692              | 0.754               | 1.507                 | 24.11%            | 4.743              | 75.89%           |
| 0.427<br>0.428 | 0.6639<br>0.6655             | 29.807<br>29.923    | 0.756<br>0.759      | 1.512<br>1.517        | 24.19%<br>24.27%  | 4.738<br>4.733     | 75.81%<br>75.73% |
| 0.428          | 0.6670                       | 30.039              | 0.761               | 1.522                 | 24.27 %           | 4.733              | 75.64%           |
| 0.429          | 0.6686                       | 30.039              | 0.764               | 1.527                 | 24.44%            | 4.723              | 75.56%           |
| 0.431          | 0.6701                       | 30.133              | 0.766               | 1.532                 | 24.52%            | 4.723              | 75.48%           |
| 0.432          | 0.6717                       | 30.387              | 0.769               | 1.537                 | 24.60%            | 4.713              | 75.40%           |
| 0.433          | 0.6732                       | 30.504              | 0.771               | 1.542                 | 24.68%            | 4.708              | 75.32%           |
| 0.434          | 0.6748                       | 30.621              | 0.774               | 1.547                 | 24.76%            | 4.703              | 75.24%           |
| 0.435          | 0.6763                       | 30.739              | 0.776               | 1.553                 | 24.84%            | 4.697              | 75.16%           |
| 0.436          | 0.6779                       | 30.856              | 0.779               | 1.558                 | 24.92%            | 4.692              | 75.08%           |
| 0.437          | 0.6795                       | 30.974              | 0.781               | 1.563                 | 25.00%            | 4.687              | 75.00%           |
| 0.438          | 0.6810                       | 31.092              | 0.784               | 1.568                 | 25.08%            | 4.682              | 74.92%           |
| 0.439          | 0.6826                       | 31.211              | 0.786               | 1.573                 | 25.17%            | 4.677              | 74.83%           |
| 0.44           | 0.6841                       | 31.329              | 0.789               | 1.578                 | 25.25%            | 4.672              | 74.75%           |
| 0.441          | 0.6857                       | 31.448              | 0.792               | 1.583                 | 25.33%            | 4.667              | 74.67%           |
| 0.442          | 0.6872                       | 31.567              | 0.794               | 1.588                 | 25.41%            | 4.662              | 74.59%           |
| 0.443          | 0.6888                       | 31.687              | 0.797               | 1.593                 | 25.49%            | 4.657              | 74.51%           |
| 0.444          | 0.6903                       | 31.807              | 0.799               | 1.598                 | 25.57%            | 4.652              | 74.43%           |
| 0.445          | 0.6919                       | 31.927              | 0.802               | 1.603                 | 25.65%            | 4.647              | 74.35%           |
| 0.446          | 0.6934                       | 32.047              | 0.804               | 1.609                 | 25.74%            | 4.641              | 74.26%           |
| 0.447          | 0.6950                       | 32.167              | 0.807               | 1.614                 | 25.82%            | 4.636              | 74.18%           |

| MTS reading    | true length<br>(Δh_actuator) | ramp angle<br>(deg) | Δh_ramp_edge (inch) | Area blocked (inch^2) | % area<br>blocked | Flow area (inch^2) | %Flow area       |
|----------------|------------------------------|---------------------|---------------------|-----------------------|-------------------|--------------------|------------------|
| 0.448          | 0.6966                       | 32.288              | 0.809               | 1.619                 | 25.90%            | 4.631              | 74.10%           |
| 0.449          | 0.6981                       | 32.409              | 0.812               | 1.624                 | 25.98%            | 4.626              | 74.02%           |
| 0.45           | 0.6997                       | 32.531              | 0.814               | 1.629                 | 26.06%            | 4.621              | 73.94%           |
| 0.451          | 0.7012                       | 32.652              | 0.817               | 1.634                 | 26.14%            | 4.616              | 73.86%           |
| 0.452          | 0.7028                       | 32.774              | 0.820               | 1.639                 | 26.23%            | 4.611              | 73.77%           |
| 0.453          | 0.7043                       | 32.896              | 0.822               | 1.644                 | 26.31%            | 4.606              | 73.69%           |
| 0.454          | 0.7059                       | 33.019              | 0.825               | 1.649                 | 26.39%            | 4.601              | 73.61%           |
| 0.455          | 0.7074                       | 33.142              | 0.827               | 1.654                 | 26.47%            | 4.596              | 73.53%           |
| 0.456          | 0.7090                       | 33.265              | 0.830               | 1.660                 | 26.55%            | 4.590              | 73.45%           |
| 0.457          | 0.7105                       | 33.388              | 0.832               | 1.665                 | 26.64%            | 4.585              | 73.36%           |
| 0.458          | 0.7121                       | 33.511              | 0.835               | 1.670                 | 26.72%            | 4.580              | 73.28%           |
| 0.459          | 0.7137                       | 33.635              | 0.837               | 1.675                 | 26.80%            | 4.575              | 73.20%           |
| 0.46           | 0.7152                       | 33.759              | 0.840               | 1.680                 | 26.88%            | 4.570              | 73.12%           |
| 0.461<br>0.462 | 0.7168                       | 33.883              | 0.843               | 1.685                 | 26.96%            | 4.565              | 73.04%           |
| 0.462          | 0.7183<br>0.7199             | 34.008<br>34.133    | 0.845<br>0.848      | 1.690<br>1.695        | 27.04%            | 4.560<br>4.555     | 72.96%           |
| 0.463          | 0.7199                       | 34.133              | 0.850               | 1.701                 | 27.13%<br>27.21%  | 4.555              | 72.87%<br>72.79% |
| 0.465          | 0.7214                       | 34.238              | 0.853               | 1.701                 | 27.21%            | 4.549              | 72.79%           |
| 0.466          | 0.7245                       | 34.509              | 0.855               | 1.711                 | 27.37%            | 4.539              | 72.71%           |
| 0.467          | 0.7261                       | 34.635              | 0.858               | 1.716                 | 27.45%            | 4.534              | 72.55%           |
| 0.468          | 0.7276                       | 34.761              | 0.861               | 1.721                 | 27.54%            | 4.529              | 72.46%           |
| 0.469          | 0.7292                       | 34.887              | 0.863               | 1.726                 | 27.62%            | 4.524              | 72.38%           |
| 0.47           | 0.7308                       | 35.014              | 0.866               | 1.731                 | 27.70%            | 4.519              | 72.30%           |
| 0.471          | 0.7323                       | 35.141              | 0.868               | 1.736                 | 27.78%            | 4.514              | 72.22%           |
| 0.472          | 0.7339                       | 35.268              | 0.871               | 1.741                 | 27.86%            | 4.509              | 72.14%           |
| 0.473          | 0.7354                       | 35.396              | 0.873               | 1.747                 | 27.95%            | 4.503              | 72.05%           |
| 0.474          | 0.7370                       | 35.523              | 0.876               | 1.752                 | 28.03%            | 4.498              | 71.97%           |
| 0.475          | 0.7385                       | 35.651              | 0.878               | 1.757                 | 28.11%            | 4.493              | 71.89%           |
| 0.476          | 0.7401                       | 35.779              | 0.881               | 1.762                 | 28.19%            | 4.488              | 71.81%           |
| 0.477          | 0.7416                       | 35.908              | 0.884               | 1.767                 | 28.27%            | 4.483              | 71.73%           |
| 0.478          | 0.7432                       | 36.037              | 0.886               | 1.772                 | 28.35%            | 4.478              | 71.65%           |
| 0.479          | 0.7448                       | 36.166              | 0.889               | 1.777                 | 28.44%            | 4.473              | 71.56%           |
| 0.48           | 0.7463                       | 36.295              | 0.891               | 1.782                 | 28.52%            | 4.468              | 71.48%           |
| 0.481          | 0.7479                       | 36.425              | 0.894               | 1.788                 | 28.60%            | 4.462              | 71.40%           |
| 0.482          | 0.7494                       | 36.554              | 0.896               | 1.793                 | 28.68%            | 4.457              | 71.32%           |
| 0.483          | 0.7510                       | 36.684              | 0.899               | 1.798                 | 28.76%            | 4.452              | 71.24%           |
| 0.484          | 0.7525                       | 36.815              | 0.901               | 1.803                 | 28.85%            | 4.447              | 71.15%           |
| 0.485          | 0.7541                       | 36.945              | 0.904               | 1.808                 | 28.93%            | 4.442              | 71.07%           |
| 0.486          | 0.7556                       | 37.076              | 0.907               | 1.813                 | 29.01%            | 4.437              | 70.99%           |
| 0.487          | 0.7572                       | 37.207              | 0.909               | 1.818                 | 29.09%            | 4.432              | 70.91%           |
| 0.488          | 0.7587                       | 37.338              | 0.912               | 1.823                 | 29.17%            | 4.427              | 70.83%           |
| 0.489          | 0.7603                       | 37.470              | 0.914               | 1.828                 | 29.25%            | 4.422              | 70.75%           |
| 0.49           | 0.7619                       | 37.602              | 0.917               | 1.833                 | 29.33%            | 4.417              | 70.67%           |
| 0.491          | 0.7634                       | 37.734              | 0.919               | 1.839                 | 29.42%            | 4.411              | 70.58%           |
| 0.492          | 0.7650                       | 37.866              | 0.922               | 1.844                 | 29.50%            | 4.406              | 70.50%           |

| MTS reading   | true length<br>(Δh actuator) | ramp angle (deg) | Δh_ramp_edge (inch) | Area blocked (inch^2) | % area           | Flow area (inch^2) | %Flow area       |
|---------------|------------------------------|------------------|---------------------|-----------------------|------------------|--------------------|------------------|
| 0.493         | 0.7665                       | 37.999           | 0.924               | 1.849                 | 29.58%           | 4.401              | 70.42%           |
| 0.494         | 0.7681                       | 38.131           | 0.927               | 1.854                 | 29.66%           | 4.396              | 70.34%           |
| 0.495         | 0.7696                       | 38.264           | 0.929               | 1.859                 | 29.74%           | 4.391              | 70.26%           |
| 0.496         | 0.7712                       | 38.398           | 0.932               | 1.864                 | 29.82%           | 4.386              | 70.18%           |
| 0.497         | 0.7727                       | 38.531           | 0.934               | 1.869                 | 29.90%           | 4.381              | 70.10%           |
| 0.498         | 0.7743                       | 38.665           | 0.937               | 1.874                 | 29.98%           | 4.376              | 70.02%           |
| 0.499         | 0.7758                       | 38.799           | 0.940               | 1.879                 | 30.07%           | 4.371              | 69.93%           |
| 0.5           | 0.7774                       | 38.933           | 0.942               | 1.884                 | 30.15%           | 4.366              | 69.85%           |
| 0.501         | 0.7790                       | 39.068           | 0.945               | 1.889                 | 30.23%           | 4.361              | 69.77%           |
| 0.502         | 0.7805                       | 39.203           | 0.947               | 1.894                 | 30.31%           | 4.356              | 69.69%           |
| 0.503         | 0.7821                       | 39.338           | 0.950               | 1.899                 | 30.39%           | 4.351              | 69.61%           |
| 0.504         | 0.7836                       | 39.473           | 0.952               | 1.904                 | 30.47%           | 4.346              | 69.53%           |
| 0.505         | 0.7852                       | 39.608           | 0.955               | 1.909                 | 30.55%           | 4.341              | 69.45%           |
| 0.506         | 0.7867                       | 39.744           | 0.957               | 1.914                 | 30.63%           | 4.336              | 69.37%           |
| 0.507         | 0.7883                       | 39.880           | 0.960               | 1.919                 | 30.71%           | 4.331              | 69.29%           |
| 0.508         | 0.7898<br>0.7914             | 40.016           | 0.962               | 1.924<br>1.929        | 30.79%           | 4.326              | 69.21%<br>69.13% |
| 0.509<br>0.51 | 0.7914                       | 40.153<br>40.289 | 0.965<br>0.967      | 1.929                 | 30.87%<br>30.95% | 4.321<br>4.316     | 69.05%           |
| 0.511         | 0.7930                       | 40.269           | 0.970               | 1.940                 | 31.03%           | 4.310              | 68.97%           |
| 0.511         | 0.7961                       | 40.420           | 0.972               | 1.945                 | 31.11%           | 4.305              | 68.89%           |
| 0.512         | 0.7976                       | 40.701           | 0.975               | 1.950                 | 31.11%           | 4.300              | 68.81%           |
| 0.514         | 0.7992                       | 40.838           | 0.977               | 1.954                 | 31.27%           | 4.296              | 68.73%           |
| 0.515         | 0.8007                       | 40.976           | 0.980               | 1.959                 | 31.35%           | 4.291              | 68.65%           |
| 0.516         | 0.8023                       | 41.114           | 0.982               | 1.964                 | 31.43%           | 4.286              | 68.57%           |
| 0.517         | 0.8038                       | 41.252           | 0.985               | 1.969                 | 31.51%           | 4.281              | 68.49%           |
| 0.518         | 0.8054                       | 41.391           | 0.987               | 1.974                 | 31.59%           | 4.276              | 68.41%           |
| 0.519         | 0.8069                       | 41.530           | 0.990               | 1.979                 | 31.67%           | 4.271              | 68.33%           |
| 0.52          | 0.8085                       | 41.669           | 0.992               | 1.984                 | 31.75%           | 4.266              | 68.25%           |
| 0.521         | 0.8101                       | 41.808           | 0.995               | 1.989                 | 31.83%           | 4.261              | 68.17%           |
| 0.522         | 0.8116                       | 41.947           | 0.997               | 1.994                 | 31.91%           | 4.256              | 68.09%           |
| 0.523         | 0.8132                       | 42.087           | 1.000               | 1.999                 | 31.99%           | 4.251              | 68.01%           |
| 0.524         | 0.8147                       | 42.227           | 1.002               | 2.004                 | 32.06%           | 4.246              | 67.94%           |
| 0.525         | 0.8163                       | 42.367           | 1.004               | 2.009                 | 32.14%           | 4.241              | 67.86%           |
| 0.526         | 0.8178                       | 42.507           | 1.007               | 2.014                 | 32.22%           | 4.236              | 67.78%           |
| 0.527         | 0.8194                       | 42.648           | 1.009               | 2.019                 | 32.30%           | 4.231              | 67.70%           |
| 0.528         | 0.8209                       | 42.788           | 1.012               | 2.024                 | 32.38%           | 4.226              | 67.62%           |
| 0.529         | 0.8225                       | 42.929           | 1.014               | 2.029                 | 32.46%           | 4.221              | 67.54%           |
| 0.53          | 0.8240                       | 43.070           | 1.017               | 2.033                 | 32.54%           | 4.217              | 67.46%           |
| 0.531         | 0.8256                       | 43.212           | 1.019               | 2.038                 | 32.61%           | 4.212              | 67.39%           |
| 0.532         | 0.8272                       | 43.353           | 1.022               | 2.043                 | 32.69%           | 4.207              | 67.31%           |
| 0.533         | 0.8287                       | 43.495           | 1.024               | 2.048                 | 32.77%           | 4.202              | 67.23%           |
| 0.534         | 0.8303                       | 43.637           | 1.026               | 2.053                 | 32.85%           | 4.197              | 67.15%           |
| 0.535         | 0.8318                       | 43.779           | 1.029               | 2.058                 | 32.92%           | 4.192              | 67.08%           |
| 0.536         | 0.8334                       | 43.922           | 1.031               | 2.063                 | 33.00%           | 4.187              | 67.00%           |
| 0.537         | 0.8349                       | 44.064           | 1.034               | 2.067                 | 33.08%           | 4.183              | 66.92%           |

| MTS reading    | true length<br>(Δh_actuator) | ramp angle<br>(deg) | Δh_ramp_edge (inch) | Area blocked (inch^2) | % area<br>blocked | Flow area (inch^2) | %Flow area       |
|----------------|------------------------------|---------------------|---------------------|-----------------------|-------------------|--------------------|------------------|
| 0.538          | 0.8365                       | 44.207              | 1.036               | 2.072                 | 33.16%            | 4.178              | 66.84%           |
| 0.539          | 0.8380                       | 44.350              | 1.038               | 2.077                 | 33.23%            | 4.173              | 66.77%           |
| 0.54           | 0.8396                       | 44.493              | 1.041               | 2.082                 | 33.31%            | 4.168              | 66.69%           |
| 0.541          | 0.8411                       | 44.637              | 1.043               | 2.087                 | 33.39%            | 4.163              | 66.61%           |
| 0.542          | 0.8427                       | 44.780              | 1.046               | 2.091                 | 33.46%            | 4.159              | 66.54%           |
| 0.543          | 0.8443                       | 44.924              | 1.048               | 2.096                 | 33.54%            | 4.154              | 66.46%           |
| 0.544          | 0.8458                       | 45.068              | 1.050               | 2.101                 | 33.61%            | 4.149              | 66.39%           |
| 0.545          | 0.8474                       | 45.212              | 1.053               | 2.106                 | 33.69%            | 4.144              | 66.31%           |
| 0.546          | 0.8489                       | 45.357              | 1.055               | 2.110                 | 33.77%            | 4.140              | 66.23%           |
| 0.547          | 0.8505                       | 45.501              | 1.058               | 2.115                 | 33.84%            | 4.135              | 66.16%           |
| 0.548          | 0.8520                       | 45.646              | 1.060               | 2.120                 | 33.92%            | 4.130              | 66.08%           |
| 0.549          | 0.8536                       | 45.791              | 1.062               | 2.124                 | 33.99%            | 4.126              | 66.01%           |
| 0.55           | 0.8551                       | 45.936              | 1.065               | 2.129                 | 34.07%            | 4.121              | 65.93%           |
| 0.551<br>0.552 | 0.8567<br>0.8583             | 46.081<br>46.227    | 1.067<br>1.069      | 2.134<br>2.139        | 34.14%<br>34.22%  | 4.116<br>4.111     | 65.86%<br>65.78% |
| 0.553          | 0.8598                       | 46.227              | 1.072               | 2.139                 | 34.22%            | 4.117              | 65.71%           |
| 0.554          | 0.8614                       | 46.518              | 1.074               | 2.148                 | 34.37%            | 4.102              | 65.63%           |
| 0.555          | 0.8629                       | 46.664              | 1.076               | 2.152                 | 34.44%            | 4.098              | 65.56%           |
| 0.556          | 0.8645                       | 46.811              | 1.079               | 2.157                 | 34.51%            | 4.093              | 65.49%           |
| 0.557          | 0.8660                       | 46.957              | 1.081               | 2.162                 | 34.59%            | 4.088              | 65.41%           |
| 0.558          | 0.8676                       | 47.104              | 1.083               | 2.166                 | 34.66%            | 4.084              | 65.34%           |
| 0.559          | 0.8691                       | 47.250              | 1.085               | 2.171                 | 34.73%            | 4.079              | 65.27%           |
| 0.56           | 0.8707                       | 47.397              | 1.088               | 2.175                 | 34.81%            | 4.075              | 65.19%           |
| 0.561          | 0.8722                       | 47.544              | 1.090               | 2.180                 | 34.88%            | 4.070              | 65.12%           |
| 0.562          | 0.8738                       | 47.692              | 1.092               | 2.185                 | 34.95%            | 4.065              | 65.05%           |
| 0.563          | 0.8754                       | 47.839              | 1.095               | 2.189                 | 35.03%            | 4.061              | 64.97%           |
| 0.564          | 0.8769                       | 47.987              | 1.097               | 2.194                 | 35.10%            | 4.056              | 64.90%           |
| 0.565          | 0.8785                       | 48.134              | 1.099               | 2.198                 | 35.17%            | 4.052              | 64.83%           |
| 0.566          | 0.8800                       | 48.282              | 1.101               | 2.203                 | 35.24%            | 4.047              | 64.76%           |
| 0.567          | 0.8816                       | 48.430              | 1.104               | 2.207                 | 35.31%            | 4.043              | 64.69%           |
| 0.568          | 0.8831                       | 48.578              | 1.106               | 2.212                 | 35.39%            | 4.038              | 64.61%           |
| 0.569          | 0.8847                       | 48.727              | 1.108               | 2.216                 | 35.46%            | 4.034              | 64.54%           |
| 0.57           | 0.8862                       | 48.875              | 1.110               | 2.221                 | 35.53%            | 4.029              | 64.47%           |
| 0.571          | 0.8878                       | 49.024              | 1.112               | 2.225                 | 35.60%            | 4.025              | 64.40%           |
| 0.572<br>0.573 | 0.8893<br>0.8909             | 49.173<br>49.322    | 1.115<br>1.117      | 2.229<br>2.234        | 35.67%<br>35.74%  | 4.021<br>4.016     | 64.33%<br>64.26% |
| 0.574          | 0.8925                       | 49.322              | 1.117               | 2.234                 | 35.81%            | 4.010              | 64.19%           |
| 0.575          | 0.8940                       | 49.471              | 1.119               | 2.243                 | 35.88%            | 4.012              | 64.12%           |
| 0.576          | 0.8956                       | 49.769              | 1.123               | 2.247                 | 35.95%            | 4.007              | 64.05%           |
| 0.577          | 0.8971                       | 49.919              | 1.126               | 2.251                 | 36.02%            | 3.999              | 63.98%           |
| 0.578          | 0.8987                       | 50.069              | 1.128               | 2.256                 | 36.09%            | 3.994              | 63.91%           |
| 0.579          | 0.9002                       | 50.219              | 1.130               | 2.260                 | 36.16%            | 3.990              | 63.84%           |
| 0.58           | 0.9018                       | 50.368              | 1.132               | 2.264                 | 36.23%            | 3.986              | 63.77%           |
| 0.581          | 0.9033                       | 50.519              | 1.134               | 2.268                 | 36.30%            | 3.982              | 63.70%           |
| 0.582          | 0.9049                       | 50.669              | 1.136               | 2.273                 | 36.36%            | 3.977              | 63.64%           |

| MTS reading    | true length<br>(Δh_actuator) | ramp angle<br>(deg) | Δh_ramp_edge (inch) | Area blocked (inch^2) | % area<br>blocked | Flow area (inch^2) | %Flow area       |
|----------------|------------------------------|---------------------|---------------------|-----------------------|-------------------|--------------------|------------------|
| 0.583          | 0.9065                       | 50.819              | 1.139               | 2.277                 | 36.43%            | 3.973              | 63.57%           |
| 0.584          | 0.9080                       | 50.970              | 1.141               | 2.281                 | 36.50%            | 3.969              | 63.50%           |
| 0.585          | 0.9096                       | 51.120              | 1.143               | 2.285                 | 36.57%            | 3.965              | 63.43%           |
| 0.586          | 0.9111                       | 51.271              | 1.145               | 2.290                 | 36.63%            | 3.960              | 63.37%           |
| 0.587          | 0.9127                       | 51.422              | 1.147               | 2.294                 | 36.70%            | 3.956              | 63.30%           |
| 0.588          | 0.9142                       | 51.573              | 1.149               | 2.298                 | 36.77%            | 3.952              | 63.23%           |
| 0.589          | 0.9158                       | 51.724              | 1.151               | 2.302                 | 36.84%            | 3.948              | 63.16%           |
| 0.59           | 0.9173                       | 51.875              | 1.153               | 2.306                 | 36.90%            | 3.944              | 63.10%           |
| 0.591          | 0.9189                       | 52.026              | 1.155               | 2.310                 | 36.97%            | 3.940              | 63.03%           |
| 0.592          | 0.9204                       | 52.178              | 1.157               | 2.315                 | 37.03%            | 3.935              | 62.97%           |
| 0.593          | 0.9220                       | 52.329              | 1.159               | 2.319                 | 37.10%            | 3.931              | 62.90%           |
| 0.594<br>0.595 | 0.9236<br>0.9251             | 52.481<br>52.633    | 1.161<br>1.163      | 2.323<br>2.327        | 37.16%            | 3.927              | 62.84%           |
| 0.596          | 0.9251                       | 52.785              | 1.165               | 2.321                 | 37.23%<br>37.29%  | 3.923<br>3.919     | 62.77%<br>62.71% |
| 0.597          | 0.9287                       | 52.785              | 1.167               | 2.335                 | 37.36%            | 3.915              | 62.64%           |
| 0.598          | 0.9298                       | 53.089              | 1.169               | 2.339                 | 37.42%            | 3.911              | 62.58%           |
| 0.599          | 0.9313                       | 53.241              | 1.171               | 2.343                 | 37.49%            | 3.907              | 62.51%           |
| 0.6            | 0.9329                       | 53.393              | 1.173               | 2.347                 | 37.55%            | 3.903              | 62.45%           |
| 0.601          | 0.9344                       | 53.545              | 1.175               | 2.351                 | 37.61%            | 3.899              | 62.39%           |
| 0.602          | 0.9360                       | 53.698              | 1.177               | 2.355                 | 37.68%            | 3.895              | 62.32%           |
| 0.603          | 0.9375                       | 53.850              | 1.179               | 2.359                 | 37.74%            | 3.891              | 62.26%           |
| 0.604          | 0.9391                       | 54.003              | 1.181               | 2.363                 | 37.80%            | 3.887              | 62.20%           |
| 0.605          | 0.9407                       | 54.156              | 1.183               | 2.366                 | 37.86%            | 3.884              | 62.14%           |
| 0.606          | 0.9422                       | 54.308              | 1.185               | 2.370                 | 37.93%            | 3.880              | 62.07%           |
| 0.607          | 0.9438                       | 54.461              | 1.187               | 2.374                 | 37.99%            | 3.876              | 62.01%           |
| 0.608          | 0.9453                       | 54.614              | 1.189               | 2.378                 | 38.05%            | 3.872              | 61.95%           |
| 0.609          | 0.9469                       | 54.767              | 1.191               | 2.382                 | 38.11%            | 3.868              | 61.89%           |
| 0.61           | 0.9484                       | 54.920              | 1.193               | 2.386                 | 38.17%            | 3.864              | 61.83%           |
| 0.611          | 0.9500                       | 55.073              | 1.195               | 2.389                 | 38.23%            | 3.861              | 61.77%           |
| 0.612          | 0.9515                       | 55.227              | 1.197               | 2.393                 | 38.29%            | 3.857              | 61.71%           |
| 0.613          | 0.9531                       | 55.380              | 1.198               | 2.397                 | 38.35%            | 3.853              | 61.65%           |
| 0.614          | 0.9547                       | 55.533              | 1.200               | 2.401                 | 38.41%            | 3.849              | 61.59%           |
| 0.615<br>0.616 | 0.9562<br>0.9578             | 55.687<br>55.840    | 1.202<br>1.204      | 2.404<br>2.408        | 38.47%<br>38.53%  | 3.846<br>3.842     | 61.53%<br>61.47% |
| 0.617          | 0.9578                       | 55.994              | 1.206               | 2.412                 | 38.59%            | 3.838              | 61.41%           |
| 0.618          | 0.9609                       | 56.147              | 1.208               | 2.415                 | 38.64%            | 3.835              | 61.36%           |
| 0.619          | 0.9624                       | 56.301              | 1.209               | 2.419                 | 38.70%            | 3.831              | 61.30%           |
| 0.62           | 0.9640                       | 56.455              | 1.211               | 2.423                 | 38.76%            | 3.827              | 61.24%           |
| 0.621          | 0.9655                       | 56.609              | 1.213               | 2.426                 | 38.82%            | 3.824              | 61.18%           |
| 0.622          | 0.9671                       | 56.762              | 1.215               | 2.430                 | 38.87%            | 3.820              | 61.13%           |
| 0.623          | 0.9686                       | 56.916              | 1.217               | 2.433                 | 38.93%            | 3.817              | 61.07%           |
| 0.624          | 0.9702                       | 57.070              | 1.218               | 2.437                 | 38.99%            | 3.813              | 61.01%           |
| 0.625          | 0.9718                       | 57.224              | 1.220               | 2.440                 | 39.04%            | 3.810              | 60.96%           |
| 0.626          | 0.9733                       | 57.378              | 1.222               | 2.444                 | 39.10%            | 3.806              | 60.90%           |
| 0.627          | 0.9749                       | 57.532              | 1.224               | 2.447                 | 39.15%            | 3.803              | 60.85%           |

| MTS reading | true length<br>(Δh_actuator) | ramp angle<br>(deg) | Δh_ramp_edge (inch) | Area blocked (inch^2) | % area<br>blocked | Flow area (inch^2) | %Flow area |
|-------------|------------------------------|---------------------|---------------------|-----------------------|-------------------|--------------------|------------|
| 0.628       | 0.9764                       | 57.686              | 1.225               | 2.451                 | 39.21%            | 3.799              | 60.79%     |
| 0.629       | 0.9780                       | 57.840              | 1.227               | 2.454                 | 39.26%            | 3.796              | 60.74%     |
| 0.63        | 0.9795                       | 57.994              | 1.229               | 2.457                 | 39.32%            | 3.793              | 60.68%     |
| 0.631       | 0.9811                       | 58.149              | 1.230               | 2.461                 | 39.37%            | 3.789              | 60.63%     |
| 0.632       | 0.9826                       | 58.303              | 1.232               | 2.464                 | 39.43%            | 3.786              | 60.57%     |
| 0.633       | 0.9842                       | 58.457              | 1.234               | 2.467                 | 39.48%            | 3.783              | 60.52%     |
| 0.634       | 0.9857                       | 58.611              | 1.235               | 2.471                 | 39.53%            | 3.779              | 60.47%     |
| 0.635       | 0.9873                       | 58.765              | 1.237               | 2.474                 | 39.58%            | 3.776              | 60.42%     |
| 0.636       | 0.9889                       | 58.920              | 1.239               | 2.477                 | 39.64%            | 3.773              | 60.36%     |
| 0.637       | 0.9904                       | 59.074              | 1.240               | 2.481                 | 39.69%            | 3.769              | 60.31%     |
| 0.638       | 0.9920                       | 59.228              | 1.242               | 2.484                 | 39.74%            | 3.766              | 60.26%     |
| 0.639       | 0.9935                       | 59.383              | 1.244               | 2.487                 | 39.79%            | 3.763              | 60.21%     |
| 0.64        | 0.9951                       | 59.537              | 1.245               | 2.490                 | 39.84%            | 3.760              | 60.16%     |
| 0.641       | 0.9966                       | 59.691              | 1.247               | 2.493                 | 39.89%            | 3.757              | 60.11%     |
| 0.642       | 0.9982                       | 59.846              | 1.248               | 2.497                 | 39.94%            | 3.753              | 60.06%     |
| 0.643       | 0.9997                       | 60.000              | 1.250               | 2.500                 | 39.99%            | 3.750              | 60.01%     |

The actuator shaft pushes the ramp vertically under the ramp. As it rises, the T-bar pushes the ramp up and the head of T-bar slides within the T-slot. See the Figure 115 on the following page.

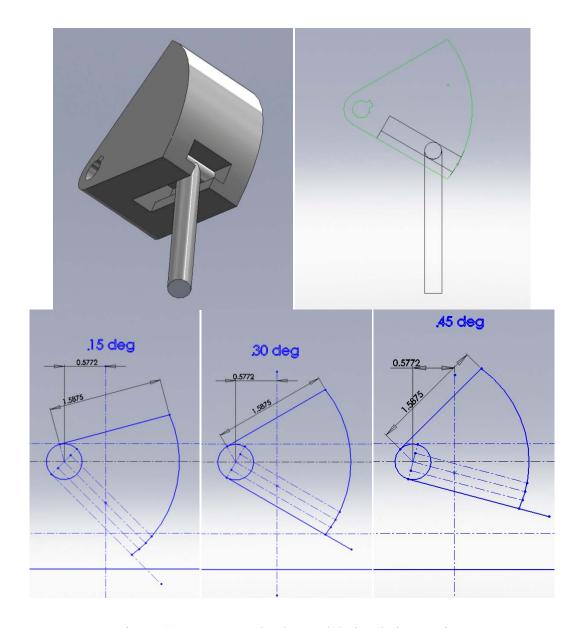


Figure 115. Ramp and T-bar and their relative motion

Because the T-slot does not coincide with the centerline of the pivot of the ramp, the linear increase in the actuator height does not mean the linear increase in the ramp angle, the area blocked, nor the flow area. Their non-linear relationships are shown in three figures on the following pages.

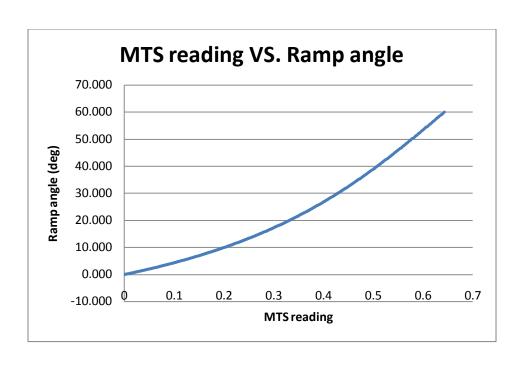


Figure 116. MTS reading increase VS. Ramp angle increase

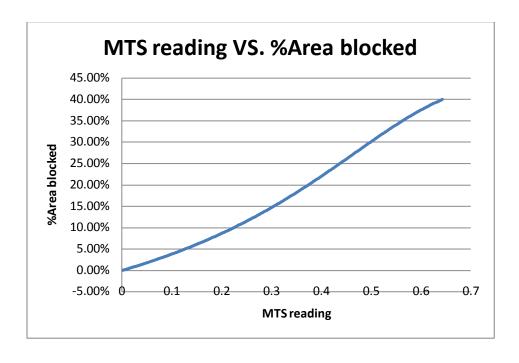


Figure 117. MTS reading increase VS. % Area blocked increase

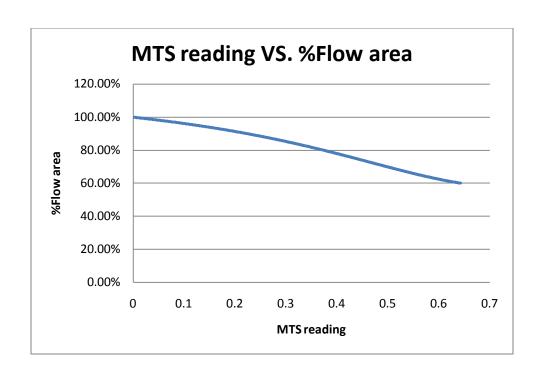


Figure 118. MTS reading increase VS. %Flow area decrease

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## Vita

Captain Richard I. Paek graduated from Joel E. Ferris High School in Spokane, WA in 2000 as a valedictorian. He completed his Bachelor of Science degree in Astronautical Engineering at University of Washington, Seattle, WA in 2004. After graduation, he was admitted to U.S. Air Force Officer Training School and received his commission in November 2004.

His first assignment was a flight test operational engineer at 419th Bomber Flight Test Squadron in Edwards Air Force Base, California. In 2007, he was assigned to the Hypersonic Flight Combined Test Force at the same base where he served as an X-51 lead project engineer. In September 2008, he received an admission to the department of Aeronautics and Astronautics at AFIT in 2008. Upon completion of his degree, he will follow-on to the Air Force Research Laboratory, Propulsion Directorate, Technology Branch (AFRL/RZAT).

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#### 13. SUPPLEMENTARY NOTES

### 14. ABSTRACT

The isolator of the scramjet decelerates the incoming high Mach flow to a lower Mach number and stabilizes the flow before it enters the combustor. Because of the unsteady combustion phenomenon and inconsistent completeness of the combustion, pressures within the combustor can vary drastically. These pressure variations can propagate forward and affect the flow field in the isolator - worst case unstarting the inlet. In this research, the shock train location VS. the back-pressure is examined experimentally. The back-pressure is artificially created by symmetric (top & bottom) ramps that can close the flow area. Raising/lowering ramps result in higher/lower back-pressure. Higher back-pressure moves the shock train forward, with too high a back-pressure causing un-start. This experiment is conducted for a variation in Reynolds number, ramp angle, and two incoming Mach #s, and will result in a relationship between back-pressure and shock train location for various airflow conditions.

# 15. SUBJECT TERMS

Scramjet, isolator, shock-train, back-pressure, un-start

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