Application of Markov Random Fields to Landmine Discrimination in Ground Penetrating Radar Data

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Alternative Phenomenologies

- Many other phenomenologies for landmine detection have been suggested
 - Electromagnetic induction (EMI)
 - Infrared techniques [Lopez, 2004]
 - Seismic & Acoustic-seismic coupling [Sabatier, 2001. Scott, 2001]
 - Ground penetrating radar (GPR)
 - Many others [MacDonald, 2003]
- Note:
 - Due to differences in:
 - Landmine types
 - Percent clearance requirements
 - Other operational requirements
 - No "silver bullet" landmine detection phenomenology
- Sensor fusion is an active area of research [Collins, 2002. Ho, 2004.]



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Motivation & Goal

- Significant diverse research on landmine detection in time-domain GPR data
 - Ground tracking and removal [Gu, 2002. Abrahams, 2001. Larsson, 2004. Guangyou, 2001]
 - Pre-screening [Carevic, 1999. Zoubir, 2002. Kempen, 2001. Karlsen 2001]
 - Feature extraction [Kleinman,1993. Carevic,1997. Frigui, 2004. Gader, 2004. Ho, 2004]
 - Image segmentation [Verdenskaya, 2006. Bhuiyan, 2006. Shihab, 2003]
 - Etc...
- Many proposed techniques are implicitly based on different underlying models of received time-domain data
 - Makes direct motivation and comparison of algorithms difficult without expert modifications
- Propose an underlying statistical model for GPR responses that incorporates spatial variations in response heights and response gains
 - Can formalize development of pre-screener algorithms based on underlying models
 - Under what conditions will adaptive algorithms perform well?
 - Are other algorithms also applicable?
 - Can provide forward generative model of large data sets
 - Given parameters, can simulate roads

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• Can not model responses from mines, etc.

Outline

- Consider various modeling techniques for GPR data
 - Computational concerns FDTD, transmission lines
 - Applicability under fielded (unknown soil property) scenarios
- Incorporating statistical parameterization of transmission line models
 - Markov Random Fields (MRF)
 - Gaussian Markov random fields (GMRF)
 - Application of MRFs to parameters of interest in transmission-line model
- Implications of proposed statistical model for pre-screener development
 - Adaptive maximum likelihood solution for GMRF parameters in GPR data time-slices
 - Adaptive discriminative algorithms for dual GMRF under both hypotheses
- Results & Conclusions / Future work

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Modeling of GPR Returns

- Finite difference timedomain (FDTD) models provide state of the art modeling of GPR responses
 - Highly generalizable
 - Computationally expensive
- Require:
 - Accurate knowledge of soil and anomaly properties
 - Locations of discontinuities
 - Etc
- Inversion / fielded application of FDTD models is difficult



Basic Transmission Line Model



- Significant simplification of GPR responses
 - Treats dielectric discontinuities in soils as impedance mismatches on a transmission line
 - Received signal is a sum of time-delayed pulses
 - Response depends on: time of arrival, gain on received pulses

Restrictions of Transmission Line-Based Modeling



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- Transmission line models assume:
 - Planar waves
 - Planar interfaces
 - Homogeneous transmission media
 - Etc.
- Obviously these assumptions are violated in fielded scenarios
- Question:
 - Can a statistical model over parameters (time of arrival, gain) mitigate these violated assumptions?

GMRF Modeling of TOA and Gain



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Modeling of Received Gain

• Model received gain as combination of deterministic part (spreading loss)

$$g_r = A + B\frac{1}{t_0}$$

• Stochastic part (soil roughness, dielectric properties, etc)

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$$g = g_r + g_{mrf}$$

• Image on right shows original measured gain, deterministic gain, MRF gain



Proposed Statistical Model



- Combination of simple A-scan transmission line modeling & spatial statistical modeling of underlying gain & time of arrival (TOA)
- By applying spatial statistical models over A-scan parameters → computationally tractable 3-D volume model for GPR data

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Sample Generative Model Application

- Images on right show original data (top images), synthetic data (bottom images)
 - Top figure shows \sim 500 scans
 - Bottom figure shows 50 scans
- Synthetic data only models initial ground bounce response
 - Both height and gain terms are modeled stochastically using Markov random fields
 - MRF parameters trained using data from UK testing site
- Generative model may be useful in its own right for simulating responses over soils with varying parameters, simulating large data sets, etc.

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 Modeling sub-surface structure is a little more complicated; requires parameter estimation techniques, statistics for appearance / disappearance of sub-surface responses



Implications of Transmission Line MRF Modeling of Soils For Pre-Screening



• Consider distribution of data in a time-slice

$$A_{i,j}(t_m) = g_{i,j}f(t_m - t_{0_{i,j}})$$

$$p(A_{i,j}(t_m)) = p(g_{i,j}f(t_m - t_{0_{i,j}}))$$
$$p(A_{i,j}(t_m)) = p(g_{t_{0_{i,j}}}f(t_m - t_{0_{i,j}}))$$
$$+ p(g_{mrf_{i,j}}f(t_m - t_{0_{i,j}}))$$

- → Data in time slice also MRF, although not closed form;
 - Assume GMRF

Target Detection Using GMRF For Data Under H₀

• Desire LRT:

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 $\lambda(x) = \frac{p(x|H_1)p(H_1)}{p(x|H_0)p(H_0)}$

 Assume data under H₁ is ~ improper uniform; data under H₀ is ~ GMRF

$$p(x(n)|\mathbf{x}_{N_n}) = \frac{1}{\sqrt{2\pi\sigma^2}} e^{-\frac{(x(n)-\sum_{n'\in N_n}\beta_{n'}x(n'))^2}{2\sigma^2}}$$

- Need parameters for GMRF!
- Consistent parameter estimation equations [Kashyap, 1983] $\beta_c = [\sum_{s \in \Omega} \mathbf{x}(N(s))\mathbf{x}^T(N(s))]^{-1} \sum_{s \in \Omega} \mathbf{x}(N(s))x(s)$

MPLE MRF Modeling → Weiner Hopf?

$$p(x|\mathbf{w}, \mathbf{x}_N) = \frac{1}{\sqrt{2\pi\sigma}} \exp^{\frac{(x-\mathbf{w}^T \mathbf{x}_N)^2}{2\sigma^2}}$$
$$p(\mathbf{x}|\mathbf{w}) \approx \prod_s p(x_s|\mathbf{w}, \mathbf{x}_{N_s})$$

 $\max_{\mathbf{w}} \mathbf{E}_{x,\mathbf{x}_N}(\log(p(x|\mathbf{w},\mathbf{x}_N)))$

$$\max_{\mathbf{w}} \mathbf{E}_{x,\mathbf{x}_N} \log \frac{1}{\sqrt{2\pi\sigma}} - \frac{1}{2\sigma^2} (x - \mathbf{w}^T \mathbf{x}_N)^2$$

$$\max_{\mathbf{w}} \log \frac{1}{\sqrt{2\pi}\sigma} - \frac{1}{2\sigma^2} \mathbf{E}(x^2) - \mathbf{w}^T \mathbf{R} \mathbf{w} - 2\mathbf{w}^T \rho$$

$$\frac{d}{d\mathbf{w}} = 0 = 2\mathbf{R}\mathbf{w} - 2\rho$$

$$ightarrow$$
 $\mathbf{w} = \mathbf{R}^{-1} \rho$

- Kashyap et al. result is very similar to Weiner-Hopf equations
- Turns out, can directly motivate Weiner-Hopf from maximum pseudolikelihood form of distributions

Motivating Adaptive Pre-Screening

- Last slides illustrated how pseudo-likelihood GMRF leads to Weiner-Hopf
- Similar arguments (removing expected values) show that ML estimates of nonstationary GMRF parameters yield LMS update equations
- This provides a model-based motivation of the application of AR based signal processing to pre-screening in GPR data

$$\frac{d}{d\beta} = -2x(n)d(n) + 2\mathbf{x}_N \mathbf{x}_N^T \hat{\beta}_n$$

$$\hat{\beta}_{n+1} = \hat{\beta}_n + \mu \mathbf{x}_N (x(n) - \mathbf{x}_N^T \hat{\beta}_n)$$



Discriminative Learning in GMRF Models

- Previously $H_1 \sim \text{improper uniform}$
- Alternatively, Consider if data under H₁ is also ~ GMRF
- Can directly solve for *discriminative* parameters

$$p(y_i|x_i, \theta) = \frac{p(x_i, y_i|\theta)}{\sum_k p(x_i, c_k|\theta)}$$

• Turns out, for many models the form of the discriminative logistic function is *linear* in the weights

$$p(H_1|\mathbf{X}) = \sigma(\mathbf{w}^T \mathbf{x})$$

• GMRF Models do not lead to linear logistic discriminative models



Solving For Adaptive Discriminative GMRF/GMRF Update Equations

$$p(x_i | \mathbf{x}_{N_i}, \theta_1, H_1) = \frac{1}{\sqrt{2\pi\sigma}} \exp^{-\frac{(\theta_1^T \mathbf{x}_{N_i} - x_i)^2}{2\sigma_1^2}}$$
$$a_{gmrf} = \log \frac{p(H_1)}{p(H_0)} + \log \frac{\sigma_0}{\sigma_1} - \frac{(\theta_1^T \mathbf{x}_{N_i} - x_i)^2}{2\sigma_1^2} + \frac{(\theta_0^T \mathbf{x}_{N_i} - x_i)^2}{2\sigma_0^2}$$
$$\frac{da_{gmrf}}{d\theta_1} = -\frac{(\theta_1^T \mathbf{x}_{N_i} - x_i)\mathbf{x}_{N_i}}{\sigma_1^2}$$

• Turns out

- Given: $\Theta_1, \Theta_2, \sigma_1, \sigma_2$

- Given:
$$\mathbf{x}_{i}, \mathbf{y}_{i}$$

$$\theta_{1} = \theta_{1} + -\frac{(\theta_{1}^{T} \mathbf{x}_{N_{i}} - x_{i}) \mathbf{x}_{N_{i}}}{\sigma_{1}^{2}} (y_{i} - \sigma(a)) * \mu$$

$$\theta_{2} = \theta_{2} + \frac{(\theta_{2}^{T} \mathbf{x}_{N_{i}} - x_{i}) \mathbf{x}_{N_{i}}}{\sigma_{2}^{2}} (y_{i} - \sigma(a)) * \mu$$

$$\sigma_{1} = \sigma_{1} + \left(\frac{-1}{\sigma_{1}} + \frac{(\theta_{1}^{T} * \mathbf{x}_{N_{i}} - x_{i})^{2}}{\sigma_{1}^{2}} (y_{i} - \sigma(a))\right) * \mu$$

$$\sigma_{2} = \sigma_{2} + \left(\frac{1}{\sigma_{2}} - \frac{(\theta_{2}^{T} * \mathbf{x}_{N_{i}} - x_{i})^{2}}{\sigma_{2}^{2}} (y_{i} - \sigma(a))\right) * \mu$$

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Advantages of Discriminative Classification

- Modeling data under H₁ as GMRF has several implicit advantages
 - Provides natural estimation of discriminative Akaike Information Criteria
 - Probabilistic outputs from each time-slice allow principled depth-bin fusion
 - Inclusion of prior information regarding target depths
- Can be computationally complex, however



Pre-Screener ROC Curves



- Results show sample ROC curves for energy (red-dotted), LMS (blue), discriminative (green-dashed)
 - Note, no pre-processing/postprocessing of outputs.
 - ROCs not indicative of system performance, provide algorithm comparison only
- Discriminative algorithm provides slight performance improvements
 - Underlying H₁ model (GMRF) may be overly simplistic

Other MRF Applications (Image Segmentation)

- Image segmentation for target localization
 - Improve extracted feature SNR, computational complexity
- Shown to improve performance for target identification against AP, AT, IED responses









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GMRF-HMM For Landmine Detection



- Similar to [Gader, 2001] consider locally stationary distributions of target responses
- Idea: *Directly model received data* as GMRF
 - No need for ad-hoc feature extraction
 - Requires neighborhood system
 N
 - Can we simultaneously learn parameters of GMRF (features) and underlying states?

$$p_{s_n}(x_n|x) = p_{s_n}(x_n|x_{N_n}) =$$
$$p_{s_n}(x_n|x_{N_n}) = \text{GMRF}(\theta_{s_n}, \sigma_{s_n})$$

Conclusions & Future Work

- Developing a generative model for GPR responses based on spatial stochastic parameterization of the transmission line model
 - Enables generation of data from sample data; eliminates need to estimate soil electromagnetic properties directly
- Proposed model
 - Provides direct motivation for application of AR approaches to pre-screening
 - Motivates application of discriminative approaches to prescreening when distribution under H_1 is known
 - Current GMRF distribution appears to be overly simplistic
- Future work:
 - Incorporate model implications to:
 - Ground tracking, image segmentation, feature extraction

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Adaptive Training Issues

- Haven't incorporated the p(H1), p(H0) terms in adaptive updates; these will need to be set
 Should not be learned adaptively?
- Issues in adaptively training discriminative models when we may only see data from H0 – the parameters under H1 will be driven to unrealistic values since model will do "well" when everything is considered H0
 - Solution: Consider library of mine signatures; stochastically select from these and for every H0 sample, train the model also with a random set of mine data



Image Depth-Bin Fused Decision Statistics

• Top image: Energy



Sum LMS OUT



Sum P(H1 | D, θ)

	14-11-11-11-11-11-11-11-11-11-11-11-11-1
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• Middle image: LMS Outputs

• Bottom image: p(H1 | D,M)



Global Model

- $p(\mathbf{Y}|\mathbf{X}, M) = \prod_{n=1}^{N} p(H_1|M, X_n)^{y_n} (1 p(H_1|M, X_n))^{1-y_n}$ $\log(p(\mathbf{Y}|\mathbf{X}, M)) = \sum_{n=1}^{N} y_n \log(p(H_1|M, X_n)) + (1-y_n) \log(1-p(H_1|M, X_n))$ $p(H_1|\mathbf{X}) = \sigma(a)$
 - Differentiating:

$$\frac{d}{d\theta_1} = \sum \frac{da_{gmrf}}{d\theta_1} (y_n - \sigma(a))$$
$$\frac{d}{d\theta_1} = \sum -\frac{(\theta_1^T \mathbf{x}_{N_i} - x_i) \mathbf{x}_{N_i}}{\sigma_1^2} (y_n - \sigma(a))$$

