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Technical Report ARMET-TR-08019

# COMPUTER SIMULATION OF A 155-mm PROJECTILE IN A SCAT GUN ASSEMBLY

Kenneth P. Walsh, Ph.D.

September 2008



U.S. ARMY ARMAMENT RESEARCH, DEVELOPMENT AND ENGINEERING CENTER

Munitions Engineering Technology Center

Picatinny Arsenal, New Jersey

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14. ABSTRACT This report presents the results of a computer simulation of a 45.36 kg 155-mm projectile as it moves through a scat gun assembly using a FORTRAN program. The experimental data was taken from a test performed by the Analysis Engineering and Technical Division at the U.S. Army Armament Research, Development and Engineering Center, Picatinny Arsenal, New Jersey on 7 April 2007 (test CBR5). The data was filtered using an Abaqus Butterworth Filter with a cutoff frequency of 500 Hz because the data plot exhibited "noisy" displays due to the electronic circuitry. The simulation entails aerodynamic deceleration of the projectile and the acceleration/deceleration of the piston inside the assembly in a long tube attached to the gun barrel. The projectile had an entrance velocity of 516 m/s and the shock wave preceding it ruptures the diaphragm. The projectile decelerates as high pressure builds between it and the free piston due to shock- wave propagation. The piston disengages and travels forward scooping water. The waterlog that forms in front of the piston effectively increases the piston's mass and also induces a braking force because of the water friction with the tube wall. The simulation predicts the piston will be decelerated with the piston coming to a rest about 22 m from the back end of the assembly. The computer simulation is based on the closed form formulas, incorporating unsteady one-dimensional fluid dynamics. This report details effects of shockwave induced pressure on the projectile and piston and how accurate the simulations are compared to the actual data plot.						
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#### INTRODUCTION

Resent testing was conducted at the U.S. Army Armament Research, Development and Engineering Center (ARDEC), Picatinny Arsenal, New Jersey on a soft recovery system for a 155-mm projectile in an assembly as shown in figure 1 and with numerical details given in figure 2. Sense and destroy armor, such as the 155-mm projectile, have very sensitive components and packaging intrinsic to their design. Projectiles tested to evaluate performance and failure analysis using a soft recovery system is very expensive. As of date, recovery was employed to retrieve the projectile in such a way that the projectile does not exceed damage thresholds. The complexity of the projectile makes it vulnerable to damage during testing and may become too damaged for useful analysis. The use of soft recovery will enhance and enable the verification of launch functionality/performance of the projectile's components, by measuring these variables during the actual testing. This report details a non-numerical closed form model and its predictions for the flow dynamics in the proposed soft recovery work. Not only is there a need for a soft recovery system, but also for a computer program that could accurately predict the projectile's behavior as it is fired through a gun assembly, which could reduce testing costs and speed research and development in ballistics design and implementation.



Scat gun parameters

#### THEORY

The formulas used in the FORTRAN program (app A) that simulates the scat recovery system were taken from a standard text by Anderson (ref. 2). A shockwave is initially created as the projectile enters the gun tube with a velocity of 516 m/s. The shockwave travels back and forth along the tube where the length of the path in a given direction changes because of the projectile's forward motion. The Mach number of the shockwave changes from its initial value to when the shockwave reflects off the back of the diaphragm and the front of the piston. When the pressure due to the shockwave exceeds the threshold of the diaphragm, the diaphragm bursts and pressure is then exerted upon the back of the piston. Shockwaves are reflected off the back of the piston and the front of the projectile until the piston displacement creates pressure on the water plug until it bursts. The energy expended by the piston in bursting the water plug is equal work done in bursting the water plugs encasing the water section of the scat assembly and pushing the water mass forward. The yield strength of the water plug is used to calculate the energy expended and lost by the piston. The yield strength of the diaphragm and water plugs were both assumed to be equal to 3,447,378 P. The FORTRAN program used in the simulations has two loops: a G loop with and embedded N loop. Both loops have an initial value of one and are incremented by one for each loop. Different Gs represent changing conditions when a barrier is burst. Each N calculates changing variables (i.e., Mach number, shockwave velocity, projectile/piston displacements and velocities) during the simulation when the shockwave completes a circuit in both forward and backward directions as it reflects off of surfaces within the assembly.

#### Calculation of Initial Mach Number

The non-reflected Mach number can be calculated by knowing the particle velocity in front of the projectile. The particle velocity can be approximated as the initial speed of the projectile  $V_P$ . The initial Mach number is calculated as (fig. 3)

$$V_{P\gamma} = V_{S}(p_{2} / p_{1} - 1)\sqrt{2\gamma / (\gamma + 1) / (p_{2} / p_{1} + (\gamma - 1) / (\gamma + 1))}$$
(1)

where  $\gamma = c_p / c_v$ ,  $V_S$  is the shockwave velocity,  $p_2$  is the shockwave pressure in back of the shockwave and on the front of the projectile, and  $p_1$  is the pressure in front of the shockwave and on the back of the diaphragm.

The initial shockwave Mach number is given by

$$M_{INT} = \sqrt{((\gamma + 1)/2\gamma)(p_2/p_1 - 1) + 1}$$
(2)

Solving equation 1 for  $p_2 / p_1$ 

$$(p_2 / p_1)^2 - p_2 / p_1 \Big( 2 + (V_P / V_S)^2 \Big) (\gamma + 1) / \gamma \Big) - (\gamma - 1) / \gamma (V_P / V_S)^2 = 0$$
  
$$(p_2 / p_1)^2 - p_2 / p_1 \Big( 2 + (V_P / V_S)^2 (\gamma + 1) / \gamma \Big) - (\gamma - 1) / \gamma (V_P / V_S)^2 = 0$$
  
$$a = 1, b = -\Big( 2 + (V_P / V_S)^2 (\gamma + 1) / \gamma \Big), c = -(\gamma - 1) / \gamma (V_P / V_S)^2$$







Mathematically, the solution to this quadratic equation is

$$(p_2 / p_1) \pm = (1/2a) \left( -b \pm \sqrt{b^2 - 4ac} \right)$$
 (3)

Physically, the only possible solutions occur if

1. 
$$b < 0, \sqrt{b^2 - 4ac} < -b, p_2/p_1 = (1/2a) \left( -b - \sqrt{b^2 - 4ac} \right)$$
  
2.  $b > 0, -4ac > 0, \sqrt{b^2 - 4ac} > abs(-b), p_2 / p_1 = (1/2a) \left( -b + \sqrt{b^2 - 4ac} \right)$ 

Substitute equation 3 into equation 2 to find initial Mach number.

#### Calculation of Sound Speed in Region Ahead of Shockwave

Temperatures in regions in front of and in back of the shockwave are function of pressures in those respective regions, which is given generally as

$$T_{2N} = (T_N p_N / p_{2N})(1 + ((\gamma + 1)/(\gamma - 1))p_{2N} / p_N)/((\gamma + 1)/(\gamma + 1) + p_{2N} / p_N)$$
(4)

when shockwaves are reflected in the forward direction and

$$T_{2N+1} = (T_{2N}p_{2N}p_{2N+1})(1 + ((\gamma+1)/(\gamma-1))p_{2N+1}/p_{2N})/((\gamma+1)/(\gamma-1) + p_{2N+1}/p_{2N})$$
(5)

when shockwaves are reflected in the backward direction. Temperatures with the higher subscripts are in regions behind the shockwave.

Substitute the previous relation for  $p_2 / p_1$  from equation 3 to find  $T_1, T_2, T_3$ . The initial temperature  $T_1$  in the region where the shockwave is propagating is 300K. The initial sound speed in front of the shockwave can then be calculated from  $V_{Si} = \sqrt{\gamma R T_i}$ .

#### Calculation of the Time for Shockwave to Transverse Length of Tube in the Forward Direction

The time  $\Delta \tau_N$  upon hitting the back of a barrier the nth time is  $\Delta \tau_N = L/V_S$ , where *L* is the initial distance from the projectile to the barrier and  $V_S$  is the shockwave velocity.

# Calculation of How Far the Projectile Travels within Tube When Shockwave Reflects Off Front of Projectile

The projectile velocity and displacement at any time can be taken from standard formulas in physics. During the time a shockwave is traveling through a medium, the pressure on the front of the projectile is constant and is decelerating it. The nth distance traveled during time  $\Delta \tau_n$  in the forward direction

$$\Delta x_{N} = \int_{0}^{\Delta \tau_{n}} (v(x_{N}) - p_{2N}At / M_{P})dt = v(x_{N})(\Delta \tau_{N}) - p_{2N}A\Delta \tau_{N}^{2} / 2M_{P} =$$

$$- p_{2N}A(L/V_{S})^{2} / 2M_{P}$$
(6)

where *A* is the cross-section area of the projectile,  $v(x_N)$  is the initial velocity of the projectile when shockwave is either reflected or created at the surface of the projectile, *L* is the distance the shockwave has to travel before hitting a barrier,  $V_S$  is the shockwave velocity, and  $M_P$  is the projectile mass.

#### Calculation of Time for Reflected Shockwave to Hit Front of Projectile

As the shockwave reflects off the diaphragm, the projectile is still moving forward, but in a decelerating manner. The time the shockwave takes to reflect off the diaphragm and hit the front part of the projectile can easily be shown to be

$$\Delta \tau_{N+I} = (L - \Delta x_N - \Delta x_{N+I}) / M_{BNR} V_S \tag{7}$$

and how far the projectile is displaced during this time interval is

$$\Delta x_{N+I} = \int_{0}^{\Delta \tau_{N+I}} (v(x_{N+I}) - p_{2N}At / M_P)dt = v(x_{N+I})\Delta \tau_{N+I} - p_{2N}A(\Delta \tau_{N+I})^2 / 2M_P$$
$$\Delta x_{N+I} = v(x_{N+I})(L - \Delta x_N - \Delta x_{N+I}) / M_{BNR}V_S - p_{2N}A((L - \Delta x_N - \Delta x_{N+I}) / M_{BNR}V_S)^2 / 2M_P$$

where  $v(x_{N+1})$  is the projectile's velocity when the shockwave is reflected backwards and  $M_{BNR}$  is the Mach number calculated from equation 9. Solving  $\Delta x_{N+1}$  involves a quadratic equation.

$$\Delta x_{N}^{2} p_{2N} A_{P} / \left( 2M_{P} (M_{BNR} V_{S})^{2} \right) + \Delta x_{N+1} \left( l + v(x_{N+1}) / M_{BNR} V_{S} - p_{2N} A (L - \Delta x_{N}) / (M_{P} (M_{BNR} V_{S})^{2}) - v(x_{N+1}) (L - \Delta x_{N}) / M_{BNR} V_{S} + p_{2N} A_{P} / 2M_{P} ((L - \Delta x_{N}) / M_{BNR} V_{S})^{2} = 0$$

$$\mathbf{a} = p_{2N} A / \left( 2M_{P} (M_{BNR} V_{S})^{2} \right)$$

$$\mathbf{b} = \left( l + V(x_{N+1}) / M_{BNR} V_{S} - p_{2N} A (L - \Delta x_{N}) / (M_{P} (M_{BNR} V_{S})^{2}) \right)$$

$$\mathbf{c} = -v(x_{N+1}) (L - \Delta x_{N}) / M_{BNR} V_{S} + p_{2N} A / \left( 2M_{P} ((L - \Delta x_{N}) / M_{BNR} V_{S})^{2} \right)$$

$$\Delta x_{N+1} (\pm) = \left( -b \pm \sqrt{b^{2} - 4ac} \right) / (2a)$$
(8)

Physically, the only possible solutions occur if

1. 
$$b < 0, \sqrt{b^2 - 4ac} < -b, p_2 / p_1 = (1/2a) \left( -b - \sqrt{b^2 - 4ac} \right)$$
  
2.  $b < 0, -4ac > 0, \sqrt{b^2 - 4ac} > abs(-b), p_2 / p_1 = (1/2a) \left( -b + \sqrt{b^2 - 4ac} \right)$ 

Knowing  $\Delta x_N$  and  $\Delta x_{N-1}$ ,  $\Delta \tau_{N+1}$  can be determined from equation 8.

#### Calculation of the Reflective Mach Number M<sub>R</sub> after Shockwave Hits Surface of a Barrier

Upon forward reflection from a surface, the pressure in back of the shockwave becomes  $p_{2N+1}$  and in the front of the shockwave  $p_N$  as shown in figure 2. For backward reflection from a surface, the pressure in back of the shockwave becomes  $p_{2N+1}$  and in the front of the shockwave  $p_N$ .

One can now calculate the new reflected Mach number using

$$M_R^2 M_C - M_R - M_C = 0 (9)$$

where  $M_C = (M_I / (M_I^2 - I)) \sqrt{1 + 2(\gamma - I)(M_I^2 - I)(\gamma + I / M_I^2)/(\gamma + I)^2}$  and  $M_I$  is the old Mach number of the shockwave before reflection and  $M_R$  is the new reflected Mach number.

Generally speaking, knowing  $M_R$ , the new pressure on the surface of a barrier can be estimated. For backward reflection,  $P_{2N+1} = FACTOR * P_{2N}$ ; for forward reflection  $P_{2N} = FACTOR * P_{2N=1}$ , where factor is a constant obtainable from standard tables (ref. 3). In both cases, the pressure with the higher subscript is the shockwave pressure on the surface of a barrier nearest to the reflected shockwave.

#### Calculation Velocity of Piston as a Function of its Displacement

Computer simulation showed that the pressure P of the shockwave on the piston is always much greater than the gas pressure on the front of the piston and the friction forces F during the time the shockwave travels towards or away from the piston. Thus, the acceleration of the piston can be approximated as constant.

$$A_{PS} = \left[ \left( PA - F \right] / M_{PS} \right] \tag{10}$$

There are three forces acting on the piston: shock pressure, friction, and pressure from the ideal gas in the chamber between the piston and the water plug. The net force on the piston can be used to calculate the increase in its kinetic energy when the net force on the piston increases its kinetic energy as it is displaced a distance X.

$$M_{PS}V_{PS}^{2}/2 = \int_{0}^{X} ((P - vRT)/(L_{PW} - X))A - F)dx = \int_{0}^{X} (-vRT/(L_{PW} - X))Adx + \int_{0}^{X} (PA - F)dx$$

$$PM_{PS}V_{PS}^{2}/2 = vRTALN(1 - X/L_{PW}) + (PA - F)X$$

$$V_{PS} = \sqrt{(2vRTA_{P}LN(1 - X/L_{PW}) + 2(PA_{P} - F)X/M_{PS})}$$
(11)

For the constants used, X / LPW = .0736 so the above simplified to

$$V_{PS} = \sqrt{2(PA - F)X / M_{PS}} \text{ or } X = M_{PS}V_{PS}^2 / (2(PA - F))$$
 (12)

After diaphragm bursts, the piston is being accelerated by pressure of the shockwave from the projectile and decelerated by friction forces and gas pressure between the piston and the water plug. When the water seal bursts, energy will be expanded to break the seal which decelerated the piston to zero. To calculate when the water seal burst, one calculates how far the piston travels to the point when the gas pressure in the region in between the piston and the seal reached its yield strength  $Y_D$ . If the water plug bursts before the piston is displaced *x*, the critical displacement can be calculated using the Ideal Gas Law PV = vRT.

$$Y_D = vRT / (A(L_{PW} - x_{crit}))$$

$$(AL_{PW} - x_{crit})) = vRT / Y_D$$

$$x_{crit} = L_{PW} - vRT / (Y_D A)$$
(13)

where v equals the number of moles of air between the piston and water plug, T = temperature, A = the cross-section area of the front of piston,  $x_{crit}$  is the critical displacement of the piston when the water plug bursts, and  $L_{PW}$  = initial distance between piston and water plug.

#### Time/Displacement Offsetting of the Projectile and Piston

Time increments in the computer program are not calculated continuously; they are, in face only, calculated when the shockwave strikes a surface within the assembly; i.e., the surface of the projectile, diaphragm, piston, or water plug. When a barrier bursts, the computer program calculates, using a subroutine, when and where the projectile/piston is when the bursting occurs.

#### **RESULTS OF COMPUTER SIMULATIONS**

The computer simulations and data plots are shown in figure 4. There were few quantitative agreements with the results of the FORTRAN computer simulations and the experimental data. The results are, however, qualitatively similar to the point that there was a sharp spike in the pressure followed by a plateau outing.

The initial pressure on the projectile was calculated from the FORTRAN program (app A) to be 569,000 P, which was consistent with the value at point 2 on the data plot in figure 4. The initial pressure was determined to be instantaneous from the computer simulation; from the data plot from points 1 and 2, the plot shows a sharp pressure gradient 0.04 sec with noisy entries, which was the result of the projectile not entering the scat assembly before that time. In the computer simulation, the projectile pressure remains constant until the diaphragm bursts during which the shockwave pressure "spikes" upwards when the shockwave hits the back of the diaphragm. However, the data projectile pressure abruptly decreases after point 2 in figure 4 to one atmosphere, which was the projectile pressure before it entered the assembly. This could only have happened if the stiff coupler in figure 1 leaked out the pressure in the chamber in between the projectile and the stiff coupler. The diaphragm bursts at 0.2 sec in the data plot and 0.38 sec in the computer simulations. The difference was partially due to the effect of the stiff coupler in the scat assembly, which was not noted of the FORTRAN program. Differences of pressure maximum at points 3 and 4 in figure 4 were most likely due to the effects of turbulence, which the computer program didn't simulate. For both the data and computer simulation, the projectile pressure remained constant - indicating that the water plugs burst during the time after the shock reflected off the back of the piston and hit the projectile. The negative pressures are artifacts from the circuitry in the pressure sensor since negative pressures are not physically realistic. Most likely, they were offset incorrectly when the circuitry processed the data resulting in a negative pressure. Simulations predicted that the piston will decelerate to zero within the passably which was consistent with the experimental results.

The pressure in back of the shockwave is always greater than the pressure in front of the shockwave. In figure 4, the diaphragm bursts when the projectile pressure is just above the yield strength of the diaphragm in the simulation plot and about 36% below it in the case of the data plot. In both plots, the diaphragm could have only burst when the shockwave hit the back of the diaphragm. The large difference between the two plots in projectile pressure between the diaphragm burst may have been due the effect of turbulence in increasing pressure at surfaces during shockwave propagation. Different values of  $\gamma$  could explain the difference, but the same value of  $\gamma = 1.4$  was used.



Figure 4 Projectile pressure versus time

#### CONCLUSIONS

The computer simulations matched the experimental data only in a qualitative sense to the point that there was a sharp spike in the projectile pressure when the diaphragm bursts, which instantaneously dropped to the initial projectile pressure until the water plug burst. The disparity between the two plots exists because the simulation failed to take into account the effects of turbulence on the generation of pressures throughout the assembly so there was not an exact quantitative concurrence between the simulations and data plots in terms of projectile pressure and the time coordinate when the diaphragm bursts. The simulations accurately predict a zero exit velocity for the piston.

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# APPENDIX A FORTRAN COMPUTER PROGRAM

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A flowchart for the FORTRAN program used in this report is shown in figure A-1.



Figure A-1 Computer flowchart

#### **PROGRAM SCAT**

**!PROGRAMMER: KENNETH P. WALSH, PHD !DATE 08/10/2008 !PORGRM CALCULTES THE PRESSURE ON THE FRONT OF A !PROJECTILE IN A SCAT GUN ASEMBLY** 

INTEGER Z,N REAL PENETRATION,VO,VS,MASS,PENETRATION\_OLD,B REAL P(100),DT(100),DX(100),MC(100),MR(100) REAL GAMMA,R,T(100),DTTOTAL,FACTOR,L,A,C,DP\_OLD REAL VSOUND,TINIT,VINIT,DELTA\_V,NU,RATIO,VP\_OLD REAL YIELD,AREA,V(100),DTTOTAL\_OLD,A1,B1,C1 CHARACTER\*8 FILENAME

#### **INITIALIZE PHYSICAL PARAMETERS**

YIELD = 3447378 !YIELD STRENGTH OF DIAPHRAGM MU\_ST\_STEEL = .74 MU\_KN\_STEEL = .57 NU=.0411 MP = 5.01 MASS=45.6 !MASS OF PROJECTILE ATM=101325 !ATMOSPHERIC PRESSURE P(1)=ATM DIA\_THICKNESS = .002 !DIAPHRAGM THICKNESS LPW=24.4 !DISTANCE FROM PISTON TO WATER PLUG AREA= .0189 !CORSS SECTION AREA OF PISTON AND PROJECTILE R=289 T(1)=300 GAMMA=1.4

 $VP\_OLD = 0$  $DP\_OLD = 0$ 

55 FORMAT(E16.7,E16.6)

PRINT \*,'ENTER NUMBER OF SECTIONS' READ \*,GFINAL

# **!G CHANES WHEN DIAPHRAM BURST !N CHANGES AS SHOCKWAVE TRAVELS FROM ONE SURFACE TO ANOTHER**

DO 100 G=1,GFINAL,1 IF(G.EQ.1)THEN PRINT \*,'ENTER FILENAME' READ \*, FILENAME OPEN(UNIT=1,FILE=FILENAME,STATUS='NEW')

```
PRINT *,'ENTER INTIAL PROJECTILE VELOCITY'
READ *,VO
V(1) = VO
TINIT = 0
IF(P(1).GT.YIELD)THEN
```

```
GFINAL = GFINAL +1
```

**ENDIF** 

ENDIF

```
IF(G.EQ.2)THEN
```

#### **DELTA\_V = SQRT(2\*YIELD\*AREA\*DIA\_THICKNESS/MP)**

TINIT OLD = TINIT

**ENDIF** 

```
PRINT *,'ENTER LENGTH OF SECTION'
READ *,L
```

```
N=1
Z=1
!PENETRATION = HOW FAR PROJECTLE IS DISPLACED
PENETRATION_OLD =0
PENETRATION=0
DTTOTAL OLD=DTTOTAL
```

#### **!CALCULATE VELOCITY OF SOUN**

VSOUND=SQRT(GAMMA\*R\*T(1))

**DO WHILE(N.LT.100)** NOLD=N

#### **IF(N.EQ.1)THEN**

**!CALCULATE INITIAL MACH NUMBER** 

A1=1

B1=-2 - (GAMMA+1)\*V(N)\*V(N)\*GAMMA/(2\*VSOUND\*VSOUND) C1=1-(GAMMA-1)\*V(N)\*V(N)\*GAMMA/(2\*VSOUND\*VSOUND) RATIO = (1/(2\*A1))\*(-B1-SQRT(B1\*B1-4\*A1\*C1))MR(N) = SORT((GAMMA+1)\*(RATIO-1)/(2\*GAMMA)+1)TOTO1 = MR(N)/(MR(N)\*MR(N)-1)TOTO2=(1+2\*(GAMMA-1))\*(MR(N)\*MR(N)-1) TOTO3= (GAMMA+1/(MR(N)\*MR(N)))/((GAMMA+1)\*(GAMMA+1))

IF(-B1.GT.SQRT(B1\*B1-4\*A1\*C1))THEN

IF(MR(N).GT.1)THEN

MC(N)=(TOTO1)\*SQRT(TOTO2\*TOTO3) MR(N+1) = .5\*(1+SQRT(1+4\*MC(N)))

**ENDIF** 

IF(MR(N).LE.1)THEN

```
RATIO = (1/(2*A1))*(-B1+SORT(B1*B1-4*A1*C1))
MR(N) = SQRT((GAMMA+1)*(RATIO-1)/(2*GAMMA)+1)
TOTO1 = MR(N)/(MR(N)*MR(N)-1)
TOTO2=(1+2*(GAMMA-1))*(MR(N)*MR(N)-1)
TOTO3= (GAMMA+1/(MR(N)*MR(N)))/((GAMMA+1)*(GAMMA+1))
MC(N)=(TOTO1)*SQRT(TOTO2*TOTO3)
MR(N+1) = .5*(1+SORT(1+4*MC(N)))
```

**ENDIF** 

**ENDIF** 

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IF(-B1.LT.SQRT(B1\*B1-4\*A1\*C1))THEN

MC(N)=(TOTO1)\*SQRT(TOTO2\*TOTO3) MR(N+1) = .5\*(1+SORT(1+4\*MC(N)))

**ENDIF** 

VS=MR(N)\*VSOUND

RATIO=(GAMMA+1+2\*GAMMA\*SQRT(MR(N+1)\*MR(N+1)-1))/(GAMMA+1) R1=((GAMMA+1)/(GAMMA-1)+RATIO)/(1+(GAMMA+1)\*RATIO/(GAMMA-1))

**ENDIF** 

**ENDIF** 

**IF(N.GT.1)THEN** 

**READ \*, FACTOR** 

VS=VSOUND\*MR(Z)

**ELSEIF(N.GT.1)THEN** 

DT(Z)= (L-PENETRATION)/VS

**IF(N.EQ.1)THEN** 

**ENDIF** 

**P(2\*N)=P(2\*N-1)\*FACTOR** 

**IF(G.LT.2)THEN** 

ALPHA=RATIO\*R1

WRITE(1,55)TINIT,P(2\*N)

T(2\*N) = ALPHA\*T(2\*N-1)

**!CALCULATE REFLECTION MACH NUMBER** 

MC(Z-1)=(TOTO1)\*SQRT(TOTO2\*TOTO3)

CALL SOUNDSPEED1(MR,N,T,VSOUND)

TOTO2=(1+2\*(GAMMA-1))\*(MR(Z-1)\*MR(Z-1)-1)

TOTO1 = MR(Z-1)/(MR(Z-1)\*MR(Z-1)-1)

MR(Z) = .5\*(1+SQRT(1+4\*MC(Z-1)))**PRINT \*, 'MR(Z), MC(Z-1), MR(Z+1)'** PRINT \*,MR(Z-1),MC(Z-1),MR(Z)

P(2\*N)=P(Z)\*(GAMMA+1+2\*GAMMA\*(MR(Z)\*MR(Z)-1))/(GAMMA+1)

TOTO3= (GAMMA+1/(MR(Z-1)\*MR(Z-1)))/((GAMMA+1)\*(GAMMA+1))

PRINT \*, 'ENTER FACTOR TO CALCULATE NEWPRESSURE'

DT(Z)= (L-PENETRATION)/VS + TINIT OLD

17

ENDI DX1=V(Z)\*(L-PENETRATION)/VS DX2=-P(2\*N)\*AREA\*(L-PENETRATION)\*(L-PENETRATION)/(2\*MASS\*VS\*VS)

**!CALCULATE DISPLACEMENT OF PROJECTILE AS SHOCKWAVE MOVES LEFT TO RIGHT** 

 $\mathbf{DX}(\mathbf{Z}) = \mathbf{DX1} + \mathbf{DX2}$ 

**PENETRATION = PENETRATION\_OLD + DX(Z)** 

IF(G.EQ.2.AND.N.GE.2)THEN

PRINT \*, 'G.EQ.2.AND.N.GE.2'

**!CALCULATE POSITION OF PISTON WHEN WATER PLUG BURSTS** 

CALL PSHIFT2(DCRIT,P,N,VP,DP,VP\_OLD,DP\_OLD,DT,Z,TC,DP

#### **IF(DP.GE.DCRIT)THEN**

L = L + DCRIT

**PRINT \*,'WATER PLUID HAS BURST'** 

VINIT = V(Z) TINIT= DTTOTAL\_OLD + TC + TINIT\_OLD WRITE(1,55)TINIT,P(2\*N) CALL PISTON2(N,P,VP,LPW,XCRIT) GO TO 100

ELSEIF(DP.LT.DCRIT)THEN

**PENETRATION = PENETRATION - DPP** 

**ENDIF** 

ENDIF

PENETRATION\_OLD=PENETRATION 17 FORMAT(1X,'DX(',I2,')=',E10.4)

V(Z+1)=V(Z)-P(2\*N)\*AREA\*DT(Z)/MASS

51 FORMAT(1X,'V(',I2,')= ',E10.4)

IF(N.GE.2)THEN

**CALCULATE REFLECTIVE MACH NUMBER** 

TOTO1= MR(Z)/(MR(Z)\*MR(Z)-1) TOTO2=(1+2\*(GAMMA-1))\*(MR(Z)\*MR(Z)-1) TOTO3= (GAMMA+1/(MR(Z)\*MR(Z)))/((GAMMA+1)\*(GAMMA+1))

MC(Z)=(TOTO1)\*SQRT(TOTO2\*TOTO3) MR(Z+1)= .5\*(1+SQRT(1+ 4\*MC(Z)))

PRINT \*,'MR(Z),MC(Z),MR(Z+1)' PRINT \*,MR(Z),MC(Z),MR(Z+1) PRINT \*,'ENTER FACTOR TO CALCULATE NEWPRESSURE' READ \*, FACTOR P(2\*N+1)=P(2\*N)\*FACTOR

IF(P(2\*N+1).GT.YIELD.AND.G.EQ.1) THEN

**!CALCULATE POSITION OF PROJECTLE WHEN DIAPHRAGM BURSTS** 

CALL XTSHIFT1C(TFINAL,DT,DX,L,V,P,N,Z) PRINT \*,'THERE IS TOO NUCH PRESSURE!' PRINT 300,L-PENETRATION

VINIT=V(Z+1) TINIT=DTTOTAL\_OLD + TFINAL WRITE(1,55)TINIT,P(2\*N) GO TO 100

ENDIF

**!CALCULATE SPEED OF SOUND WHEN SHOCKWAVE TRAVELS RIGHT TO LEFT** 

CALL SOUNDSPEED2(MR,N,T,VSOUND)

VS=VSOUND\*MR(Z+1)

#### ENDIF

#### IF(N.EQ.1)THEN

**!CALCULATE PRESSURE IN BACK OF SHOCKWAVE** 

PRINT \*,'MR(Z),MC(Z),MR(Z+1)' PRINT \*,MR(Z),MC(Z),MR(Z+1) PRINT \*,'ENTER FACTOR TO CALCULATE NEWPRESSURE'

READ \*, FACTOR P(2\*N+1)=P(2\*N)\*FACTOR

IF(P(2\*N+1).GT.YIELD.AND.G.EQ.1) THEN

PRINT \*,'THERE IS TOO NUCH PRESSURE!' 300 FORMAT(1X,'ADD ',E19.4,1X,'TO THE NEXT SECTION') PRINT 300,L-PENETRATION

**!CALCULATE POSITION OF PROJECTILE WHEN DIAPHRAGM BURSTS** 

CALL XTSHIFT1C(TFINAL,DT,DX,L,V,P,N,Z) VINIT = V(Z+1) TINT=DTTOTAL\_OLD + TFINAL WRITE(1,55)TINIT,P(2\*N) PRINT \*,'DTTOTAL\_OLD,DT(Z)' PRINT \*,DTTOTAL\_OLD,DT(Z) GO TO 100

**ENDIF** 

CALL SOUNDSPEED2(MR,N,T,VSOUND)

VS=VSOUND\*MR(Z+1)

ENDIF

PRINT \*,'AREA,MASS.MR(Z+1),VS,VSOUND' PRINT \*,AREA,MASS,MR(Z+1),VS,VSOUN

## **!CALCULATEDISPLACEMENT OF PROJECTILE WHEN SHOCKWAVE MOVES RIGHT TO LEFT**

A=P(2\*N)\*AREA/(2\*MASS\*VS\*VS) B1=(MASS\*VS\*VS) B=1+V(Z)/VS -P(2\*N)\*AREA\*(L-PENETRATION)/B1 C=-V(Z)\*(L-PENETRATION)/VS +P(2\*N)\*AREA\*(L-PENETRATION &)\*(L-PENETRATION)/(2\*MASS\*VS\*VS) DX(Z+1) = (1/(2\*A))\*(-B+SQRT(B\*B-4\*A\*C))

PRINT \*,'A,B,C,DX(Z+1)' PRINT \*,A,B,C,DX(Z+1)

PENETRATION = PENETRATION\_OLD + DX(Z+1) VINIT=V(Z+1) DT(Z+1)= (L - PENETRATION)/VS

**IF(G.EQ.2)THEN** 

**!CALCUALTE POSITION OF PISTON WHEN WATER PLUG BURSTS** 

CALL PSHIFT(DCRIT,P,N,VP,DP,VP\_OLD,DP\_OLD,DT,Z,TC,DPP) PRINT \*,'PSHIFT'

**IF(DP.GE.DCRIT)THEN** 

L = L + DCRIT

**PRINT \*,'WATER PLUID HAS BURST'** 

VINIT = V(Z+1) TINIT= DTTOTAL\_OLD + TC + TINIT\_OLD PRINT \*,'DTTOTAL\_OLD,TINIT\_OLD,TC' PRINT \*,DTTOTAL\_OLD,TINIT\_OLD,TC WRITE(1,55)TINIT,P(2\*N) CALL PISTON1(N,P,VP,LPW,XCRIT) GO TO 100

ELSEIF(DP.LT.DCRIT)THEN

**PENETRATION = PENETRATION - DPP** 

**ENDIF** 

ENDIF DTTOTAL= DT(Z+1) + DT(Z) + DTTOTAL\_OLD DTTOTAL\_OLD = DTTOTAL WRITE(1,55)DTTOTAL,P(2\*N) PRINT \*,'DTTOTAL,P(2\*N)' PRINT \*,DTTOTAL,P(2\*N)

V(Z+2)=V(Z+1)- P(2\*N)\*AREA\*DT(Z+1)/MASS
FORMAT(1X,'TIME SHOCKWAVE #',I2,1X,'HITS PROJECTILE =',E10.2)
FORMAT(1X 'PRESSURE OF SHOCKWAVE #',I2 ', -1510.2)

**3** FORMAT(1X,'PRESSURE OF SHOCKWAVE # ',I2,'= ',E10.2)

PRINT \*, 'Z,DTTOTAL,PENETRATION,N,P(2\*N),V(Z+1)' PRINT \*, Z,DTTOTAL,PENETRATION,N,P(2\*N),V(Z+1)

PENETRATION\_OLD=PENETRATION

Z = Z + 2N = N + 1

PRINT \*,'SHOCKWAVE VELOCITY ='

PRINT \*,VS

ENDDO

**100 CONTINUE** 

END

SUBROUTINE SOUNDSPEED1(MR,N,T,VSOUND)

INTEGER N REAL RATIO,GAMMA,ALPHA,MR(100),T(100) REAL VSOUND,R1

R=289 GAMMA =1.4

RATIO=(GAMMA + 1 + 2\*GAMMA\*SQRT(MR(N+1)\*MR(N+1)-1))/(GAMMA+1) R1=((GAMMA+1)/(GAMMA-1)+RATIO)/(1+(GAMMA+1)\*RATIO/(GAMMA-1)) ALPHA=RATIO\*R1

T(2\*N) = ALPHA\*T(2\*N-1)

VSOUND = SQRT(GAMMA\*R\*T(2\*N-1)) RETURN END

SUBROUTINE SOUNDSPEED2(MR,N,T,VSOUND)

REAL RATIO, GAMMA, ALPHA, MR(100), T(100)

R=289 GAMMA =1.4

**RATIO** = (GAMMA + 1 + 2\*GAMMA\*SQRT(MR(N+1)\*MR(N+1)-1))/(GAMMA+1)

ALPHA=RATIO\*((GAMMA+1)/(GAMMA-1)+RATIO)/(1+(GAMMA+1)\*RATIO/(GAMM &A-1))

T(2\*N+1) = ALPHA\*T(2\*N)

VSOUND= SQRT(GAMMA\*R\*T(2\*N+1))

RETURN END

SUBROUTINE XTSHIFT1A(TFINAL,DT,PENETRATION\_OLD,L,V,P,N,Z)

INTEGER Z,N REAL Z1,Z2,Z3,PENETRATION\_OLD,TFINAL,MASS,AREA REAL V(100),P(100),DT(100),F, MU\_KN\_STEEL

MASS=45.26 AREA=.0189 MU\_KN\_STEEL = .57 F=9.8\*MASS\*MU\_KN\_STEEL

PRINT \*,'SHIFT IT 1A'

Z1=(P(2\*N)\*AREA+F)/MASS Z3=L - PENETRATION\_OLD Z2=-V(Z)

TFINAL=(-Z2+SQRT(Z2\*Z2-4\*Z1\*Z3))/(2\*Z1)

#### RETURN

END

SUBROUTINE XTSHIFT1B(TFINAL, DT, PENETRATION OLD, L, V, P, N, Z)

INTEGER Z REAL Z1,Z2,Z3,PENETRATION\_OLD,TFINAL,MASS,AREA,L REAL V(100),P(100),DT(100),MU\_KN\_STEEL

MASS=45.26 AREA=.0189 MU\_KN\_STEEL = .57 F=9.8\*MASS\*MU\_KN\_STEEL

**PRINT \*, 'SHIFT IT 1B'** 

Z1=(P(2\*N)\*AREA+F)/(2\*MASS) Z3=L - PENETRATION\_OLD Z2=-V(Z)

PRINT \*,'Z2\*Z2-4\*Z1\*Z3' PRINT \*, Z2\*Z2-4\*Z1\*Z3

TFINAL=(-Z2+SQRT(Z2\*Z2-4\*Z1\*Z3))/(2\*Z1) RETURN END

SUBROUTINE XTSHIFT2(TFINAL, PENETRATION OLD, L, V, P, N, Z)

INTEGER Z,N REAL Z1,Z2,Z3,PENETRATION\_OLD,L,MASS,AREA REAL V(100),P(100),TFINAL,MU\_KN\_STEEL

MASS=45.26 AREA=.0189 MU\_KN\_STEEL = .57 F=9.8\*MASS\*MU\_KN\_STEEL

Z1=(P(2\*N)\*AREA+F)/(2\*MASS) Z3=L - PENETRATION\_OLD Z2=-V(Z+1) PRINT \*,Z1,Z2,Z3 TFINAL=(-Z2+SQRT(Z2\*Z2-4\*Z1\*Z3))/(2\*Z1) RETURN

**END** 

SUBROUTINE XTSHIFT1C(TFINAL,DT,DX,L,V,P,N,Z)

INTEGER Z,N REAL Z1,Z2,Z3,TFINAL,MASS,AREA, MU\_KN\_STEEL REAL V(100),P(100),DT(100),DX(100)

MASS=45.26 AREA=.0189 MU\_KN\_STEEL = .57 F=9.8\*MASS\*MU\_KN\_STEEL PRINT \*,'SHIFT IT 1C'

Z1=(P(2\*N)\*AREA+F)/MASS Z3= DX(Z) Z2=-V(Z)

TFINAL=(-Z2+SQRT(Z2\*Z2-4\*Z1\*Z3))/(2\*Z1)

RETURN

END

### SUBROUTINE PISTON1(N,P,VP,LPW,XCRIT)

INTEGER N REAL P(100),YIELD, DELTA\_V,VFINAL REAL PISTONMASS,WATERMASS, L,MU\_KN\_STEEL,FWORK REAL VP,LPW,XCRIT

```
PISTONMASS = 5.01
WATERMASS = 100
AREA = .0189
L=.002
YIELD = 3447378
MU_KN_STEEL = .57
F=9.8*PISTONMASS*MU_KN_STEEL
FWORK= (P(2*N+1)*AREA -F)* (LPW-XCRIT + 24.4)
DELTA_V =SQRT(2*FWORK/PISTONMASS)
VFINAL = VP - DELTA V
```

**IF(VFINAL.GT.0)THEN** 

**PRINT \*,'FINAL PISTON VELOCITY IS'** 

**PRINT \*, VFINAL** 

ENDIF

**IF(VFINAL.LE.0)THEN** 

PRINT \*,'PISTON WILL STOP AT' PRINT \*, 24.4 + (LPW-XCRIT) -PISTONMASS\*VP\*VP/(2\*(P(2\* &N+1)\*AREA -F)) PRINT \*,'METERS FROM END OF SCAT'

-

ENDIF

RETURN

END

SUBROUTINE PSHIFT(DCRIT,P,N,VP,DP,VP\_OLD,DP\_OLD,DT,Z,TC,DPP)

```
INTEGER N,Z
REAL YIELD,MU_KN_STEEL,NU,MP,DCRIT,P(100)
REAL AREA,LPW,T,F,A,TC,A1,A2,A3,DP_OLD,VP_OLD
REAL DPP,VP,DP,DT(100)
```

```
MP = 5.01
LPW=24.4
AREA=.0189
YIELD = 3447378
MU_KN_STEEL = .57
NU=.0411
T=300
R=289
DCRIT = LPW - NU*R*T/(YIELD*AREA)
A=(P(2*N+1)*AREA - F)/MP
VP = VP_OLD + A*DT(Z+1)
DP= DP_OLD + VP_OLD*DT(Z) + A*DT(Z)*DT(Z)/2
DPP= VP_OLD*DT(Z) + A*DT(Z)/2
A1 = A/2
A2 = VP OLD
```

```
A3 = -DPP
TC = (-A2+SQRT(A2**2-4*A1*A3))/(2*A1)
PRINT *,'TC'
PRINT *,TC
DP_OLD = DP
VP_OLD = VP
```

RETURN

**END** 

SUBROUTINE PSHIFT2(DCRIT,P,N,VP,DP,VP\_OLD,DP\_OLD,DT,Z,TC,DPP)

```
INTEGER N,Z

REAL YIELD,MU_KN_STEEL,NU,MP,DCRIT,P(100)

REAL AREA,LPW,T,F,A,TC,A1,A2,A3,DP_OLD,VP_OLD

REAL DPP,VP,DP,DT(100)

MP = 5.01

LPW=24.4

AREA= .0189

YIELD = 3447378

MU_KN_STEEL = .57

NU=.0411

T=300

R=289

DCRIT = LPW - NU*R*T/(YIELD*AREA)
```

```
A=(P(2*(N-1)+1)*AREA - F)/MP
VP = VP_OLD + A*DT(Z+1)
DP= DP_OLD + VP_OLD*DT(Z+1) + A*DT(Z+1)*DT(Z+1)/2
DPP= VP_OLD*DT(Z+1) + A*DT(Z+1)*DT(Z+1)/2
A1 = A/2
A2 = VP_OLD
A3 = -DPP
```

TC = (-A2+SQRT(A2\*\*2-4\*A1\*A3))/(2\*A1) DP\_OLD = DP VP\_OLD = VP PRINT \*,'TC' PRINT \*,TC

RETURN END

#### **SUBROUTINE PISTON2(N,P,VP,LPW,XCRIT)**

INTEGER N REAL P(100),YIELD, DELTA\_V,VFINAL REAL PISTONMASS,WATERMASS, L,MU\_KN\_STEEL,FWORK REAL VP,LPW,XCRIT

PISTONMASS = 5.01 WATERMASS = 100 AREA = .0189 L=.002 YIELD = 3447378 MU\_KN\_STEEL = .57 F=9.8\*PISTONMASS\*MU\_KN\_STEEL

FWORK=(P(2\*(N-1)+1)\*AREA -F)\* (LPW-XCRIT + 24.4)

DELTA\_V =SQRT(2\*FWORK/PISTONMASS) VFINAL = VP - DELTA\_V PRINT \*,'VFINAL =' PRINT \*,VFINAL

**IF(VFINAL.GT.0)THEN** 

**PRINT \*, 'FINAL PISTON VELOCITY IS'** 

**PRINT \*, VFINAL** 

**ENDIF** 

**IF(VFINAL.LE.0)THEN** 

PRINT \*,'PISTON WILL STOP AT' PRINT \*,'PISTON WILL STOP AT' PRINT \*, 24.4 + (LPW-XCRIT) -PISTONMASS\*VP\*VP/(2\*(P(2\* &N+1)\*AREA -F)) PRINT \*,'METERS FROM END OF SCAT'

> ENDIF RETURN

END

# GLOSSARY

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$\Delta \tau_N$	Time shockwave takes for its nth transversal along the tube
L	Initial distance between projectile and diaphragm or piston
M <sub>NR</sub>	Mach number of shockwave after the nth reflection
V <sub>S</sub>	Velocity of sound in tube
$\Delta x_N$	Displacement of projectile during the nth transversal of the shockwave along the tube
$\Delta x_{crit}$	Displacement of piston where water plug bursts
M <sub>IC</sub>	Constant used to determine the Mach number after the nth reflection of shockwave
V <sub>P</sub>	Particle velocity
M <sub>INT</sub>	Mach number before shockwave is reflected off of a surface
<i>T</i> <sub>2</sub>	Temperature in back of shockwave before shockwave first hits back of diaphragm
$T_I$	Temperature in front of shockwave before shockwave first hits back of diaphragm
$V_{I}$	Sound speed at temperature $T_I$
и	Particle velocity
$M_P$	Mass of projectile
$L_{PW}$	Initial distance between piston and water plug
Р	Pressure exerted on back of piston by shockwave
F	Friction force
V <sub>P</sub>	Velocity of projectile
$V_{PS}$	Velocity of piston
Х	Displacement

$Y_D$	Yield pressure of diaphragm and water plugs
$v(x_N)$	Projectile velocity after nth reflection/creation of shockwave on the surface of the projectile
$v(x_N)$	Projectile velocity after nth reflection of shockwave on the surface of the piston/diaphragm
A <sub>PS</sub>	Piston acceleration
$M_{PS}$	Piston mass
A	Cross-section area of projectile and piston
t	Time
M <sub>BNR</sub>	nth backward reflected Mach number
V <sub>Si</sub>	Speed of sound in region with temperature
$T_i$	Projectile pressure in front of the shockwave

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