



Spray Combustion Modeling Including Detailed Chemistry

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Report Documentation Page

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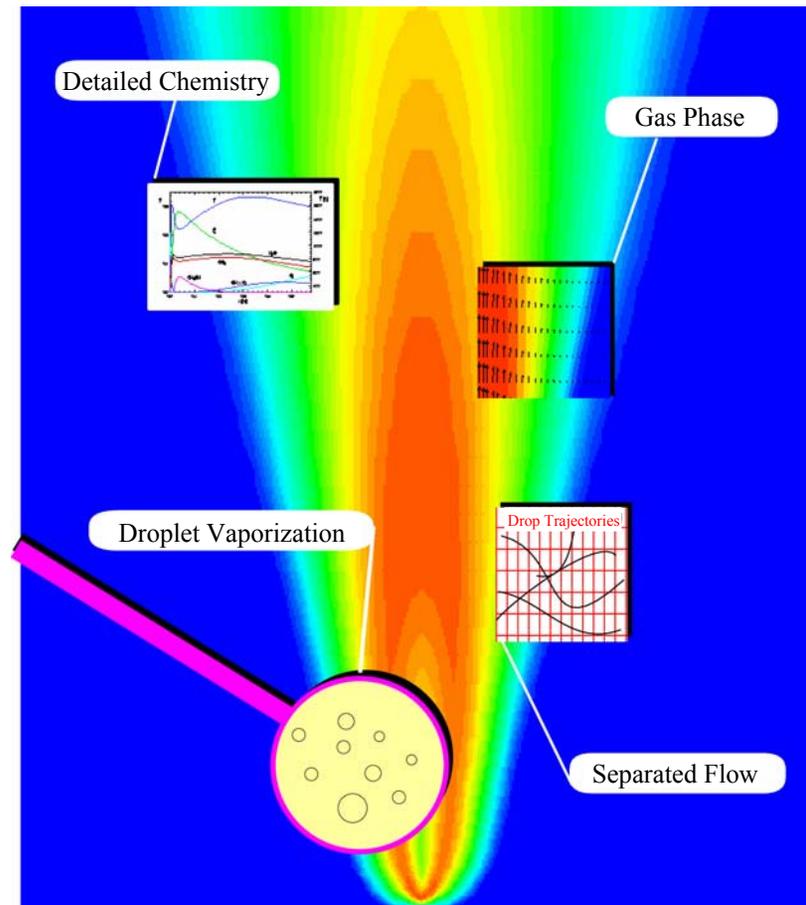
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- I. Why Detailed Chemistry?
- II. Structures of Spray Flames in the Counterflow Configuration
- III. Turbulent Spray-Flame Modeling
- IV. Summary and Conclusions

Modeling of Technical Spray Flames





Why Detailed Chemistry?

Detailed Chemical Reaction Mechanisms are Available for a Considerate Number of Relevant Combustion Systems (Alkanes, Alcohols, Hydrogen/Air, Hydrogen/Oxygen, ...)

- Combustion of liquid fuel sprays in air (e.g. internal engine combustion, industrial furnaces, gas turbine combustors)
- Liquid oxygen in (gaseous) hydrogen (liquid rocket propulsion)
- Liquid oxygen in gaseous hydrocarbons or alcohols (green propellants)



Advantages of Using Detailed Chemistry:

- Mechanism is independent of the experimental configuration, it depends only on pressure (not for hydrogen/air or hydrogen/oxygen)
- Mechanism is the base for development of reduced mechanisms (both manually or automatically developed systems)
- Prediction of pollutants and precursors of soot formation

Disadvantages of Using Detailed Chemistry:

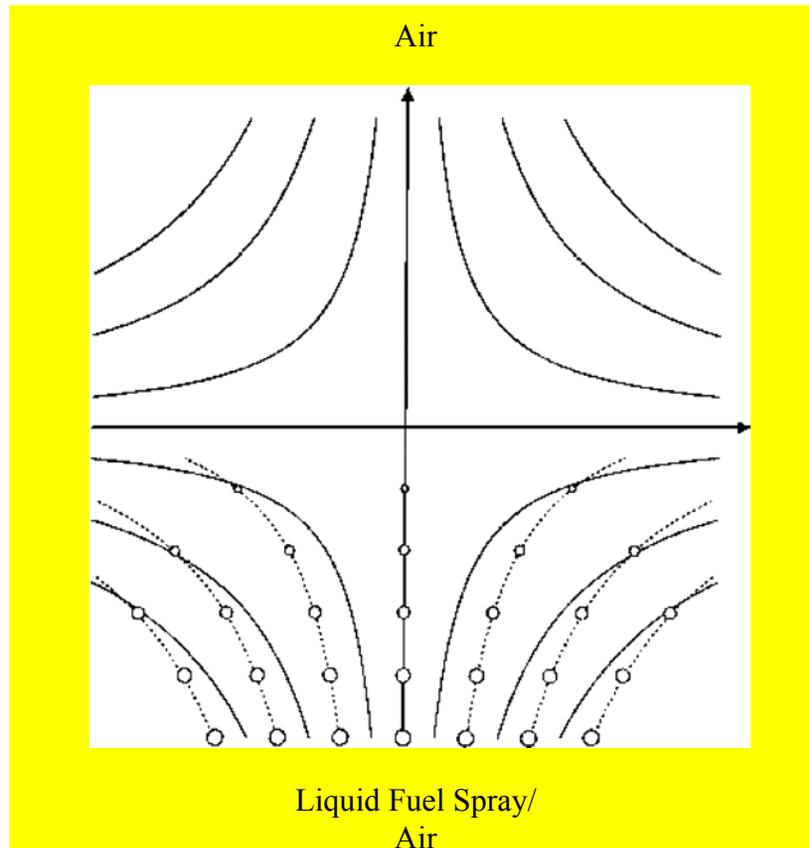
- Stiffness of the conservation equations
- Consume a considerable amount of computer time

Applications:

Laminar Flames: Detailed mechanisms can be implemented directly for hydrogen and small hydrocarbons and alcohols

Turbulent Flames: Detailed chemistry may be implemented through use of the flamelet model

Modeling of Laminar Spray Flames in the Counterflow Configuration



Motivation:

Investigation of laminar spray flame structures using detailed models for instance for chemical reactions

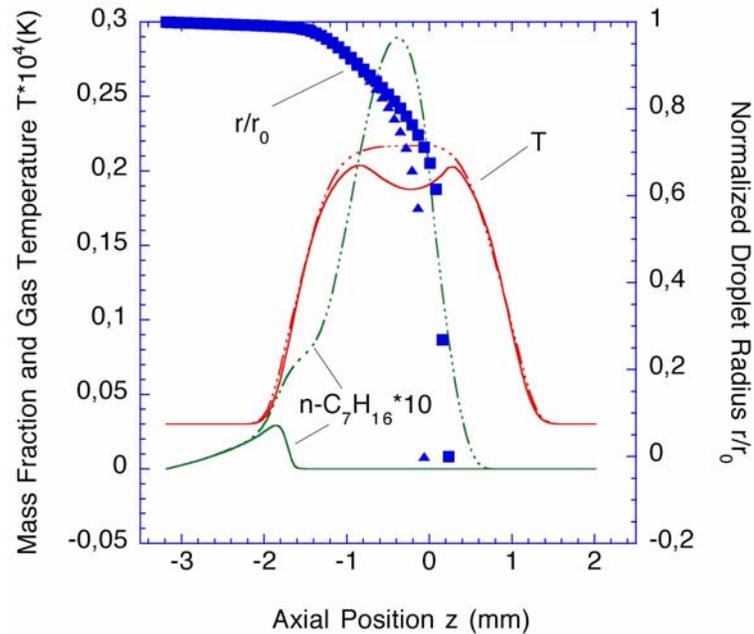
Flamelet modeling of turbulent spray diffusion flames

Properties:

- Planar or axisymmetric
- Two-dimensional
- Strained

Detailed Versus One-Step Chemistry

n-Heptane/Air Spray Flame at Atmospheric Pressure



$$a = 500/s$$

Detailed Chemistry:

Solid Lines, Square

One-Step Chemistry:

Dashed Lines, Triangles

⇒ **One-Step Chemistry is not Suitable to Correctly Predict Even the Outer Flame Structure**

Gutheil, E., Sirignano, W. A.: *Counterflow Spray Combustion Modeling Including Detailed Transport and Detailed Chemistry*, Combustion and Flame: 113(2), 92-105 (1998).



Mathematical Model

Gas-phase with dilute spray

- Boundary layer approximation, low Mach number
- Dimensionless, steady equations
- Similarity transformation \Rightarrow 2D \rightarrow 1D equations
- Ideal gas law
- Detailed chemical reaction mechanisms.
 - **H₂/O₂** (8 species and 38 elementary reactions)
 - **methanol/air** (23 species and 170 elementary reactions)
- Detailed transport: molecular diffusion and thermo diffusion
- Gas-phase properties between 300 and 5000 K from NASA polynomials
- Physical properties of H₂ and O₂ in the range of 80 to 300 K and 1 to 200 bar from *JSME* tables

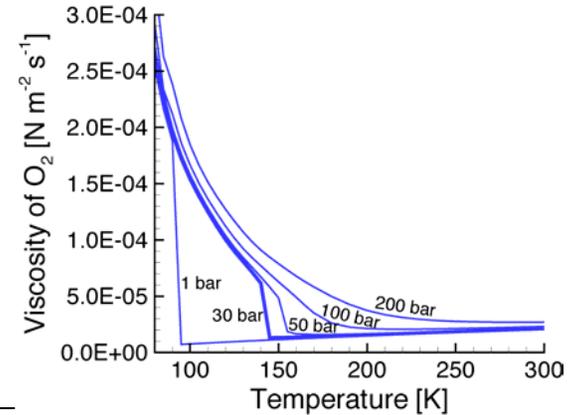
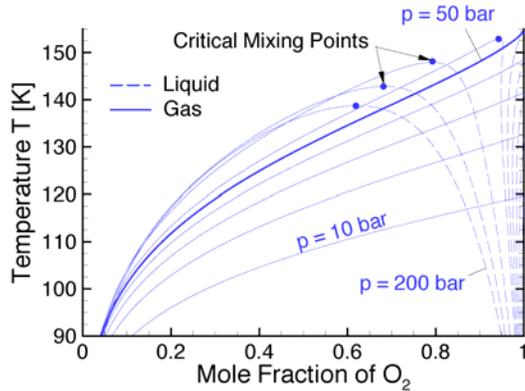
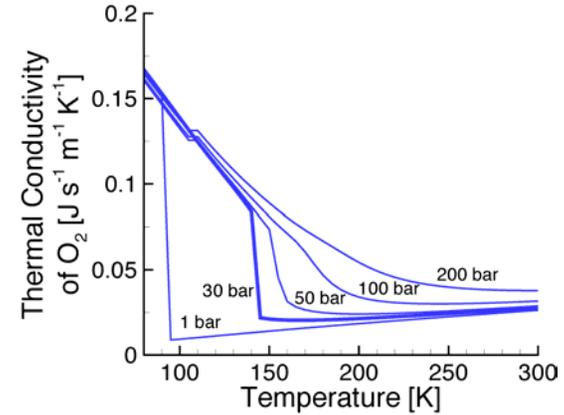
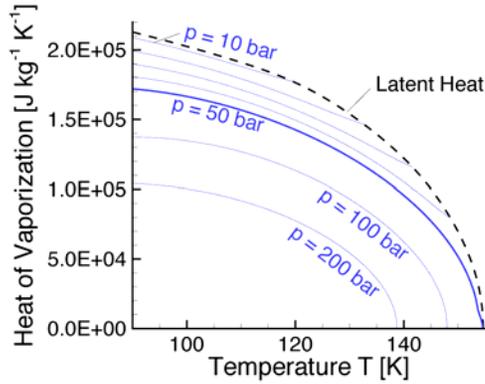


Mathematical Model

Liquid phase

- Mono-, bi- and polydisperse sprays, single-component sprays
- Discrete droplet model
- Spherically symmetric droplets
- Convective droplet model for heating and vaporization (Abramzon-Sirignano model)
- Pressure and temperature dependent heat of vaporization
- Assumption of thermodynamic equilibrium:
 - Ambrose's equation for the evaluation of the vapor pressure for methanol/air
 - Calculation of binary H_2/O_2 mixtures to obtain the gas mixture composition at the interface (replacement of Raoult's law)
- Droplet motion (drag)

Physical Properties of Oxygen (Cryogenic, High Pressure)



Yang, V., Lin, N.N., Shuen, J.S., *Combust. Sci. and Tech.*, 97: pp. 247-270, 1994

JSME Data Book, Thermophysical Properties of Fluids, 1983.

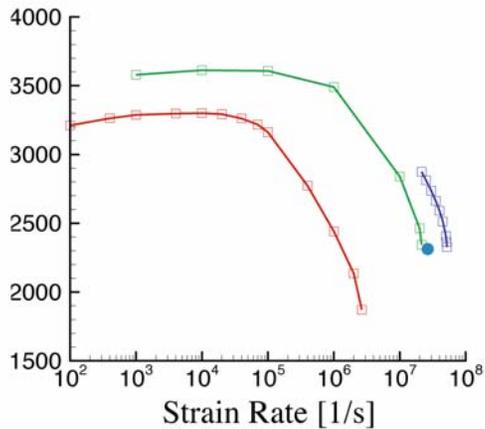
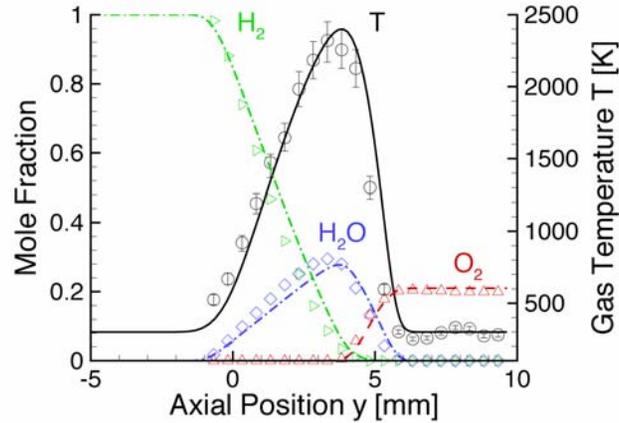
Prausnitz, J.M., Lichtenthaler, R.N., de Avezedo, E.G., *Molecular Thermo-dynamics of Fluid-Phase Equilibria*, Prentice-Hall, New Jersey, 1986.

Litchford, R.R., Jeng, S.M., *AIAA Paper 90-2191*, 1990.

H₂/Air Spray Flame at Atmospheric Pressure

$p = 1 \text{ bar}$, $T_+ = T_- = 300 \text{ K}$, $a = 100/\text{s}$

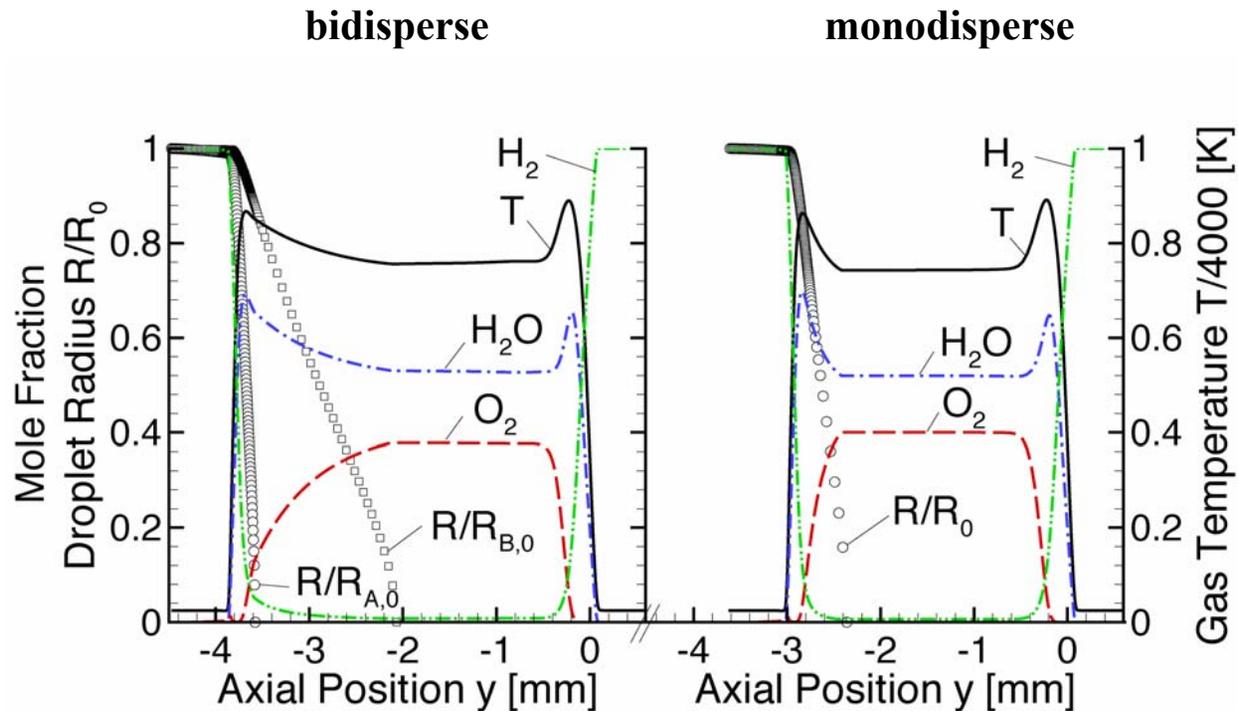
Symbols: Experiment: T. M. Brown *et. al.*,
Combust. Sci. and Tech., Vol. 129, pp. 71-88,
 1997.



Pressure	Inlet Temperature	
	H ₂	O ₂
5 bar	100 K	110 K
30 bar	100 K	142 K
30 bar	500 K	160 K
30 bar	500 K	160 K

- Experiment: Sohn, C. H., Chung, S. H., Lee, S. R., Kim, J. S.,
Combustion and Flame, 115 (3): 299-312, 1998.

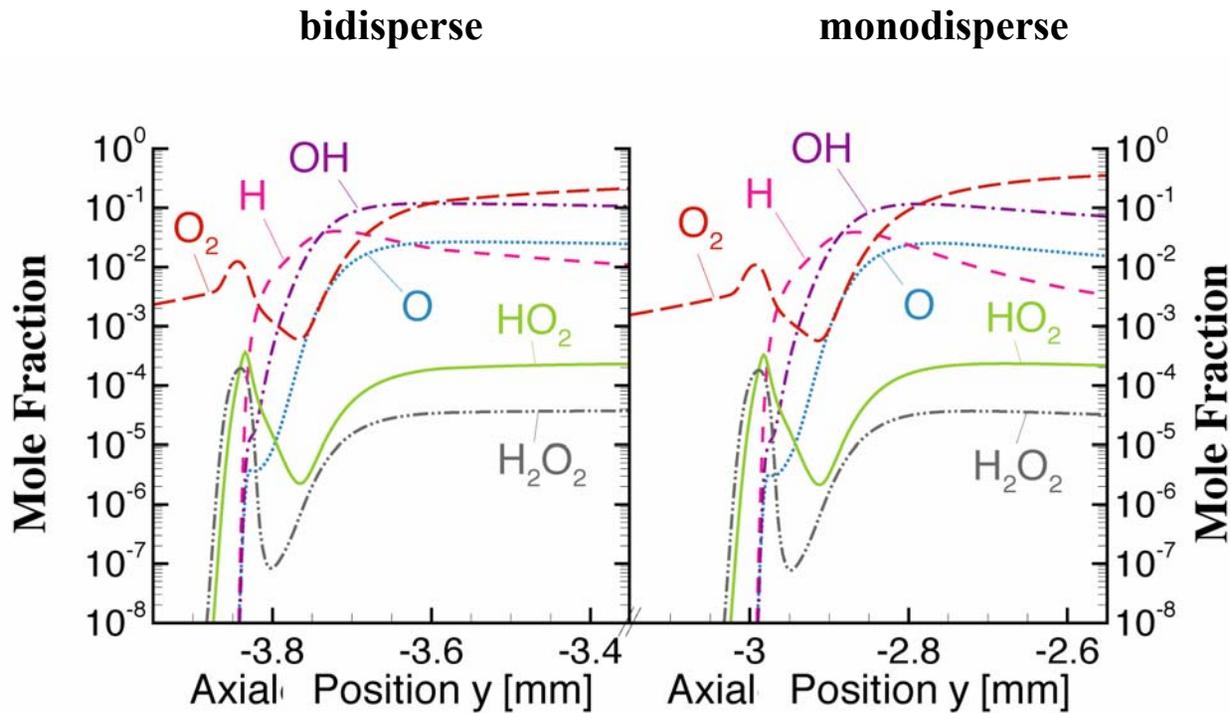
LOX/H₂ Spray Flame



$p = 30 \text{ bar}$, $\Phi = 6$, $a = 3,000/\text{s}$ (spray side), $R_{A,0} = 10 \text{ }\mu\text{m}$, $R_{B,0} = 25 \text{ }\mu\text{m}$, $\text{SMR}_0 = 14.3 \text{ }\mu\text{m}$

Schlottz, D., Gutheil, E.: *Modeling of Laminar Mono- and Bidisperse Liquid Oxygen/Hydrogen Spray Flames in the Counterflow Configuration*, Combustion Science and Technology, 158, 195-210 (2000).

LOX/H₂ Spray Flame

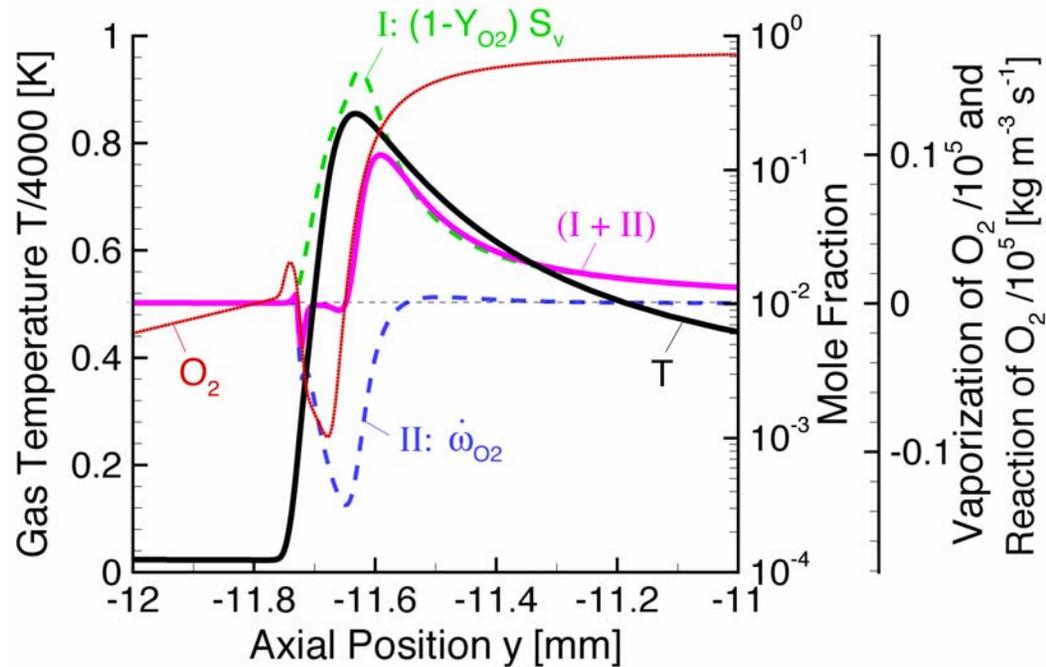


$p = 30$ bar, $\Phi = 6$, $a = 3,000/s$ (spray side), $R_{A,0} = 10 \mu m$, $R_{B,0} = 25 \mu m$, $SMR_0 = 14.3 \mu m$

Schlotz, D., Gutheil, E.: *Modeling of Laminar Mono- and Bidisperse Liquid Oxygen/Hydrogen Spray Flames in the Counterflow Configuration*, Combustion Science and Technology, 158, 195-210 (2000).

LOX/H₂ Spray Flame

Chemical Reaction Rate and Vaporization Rate



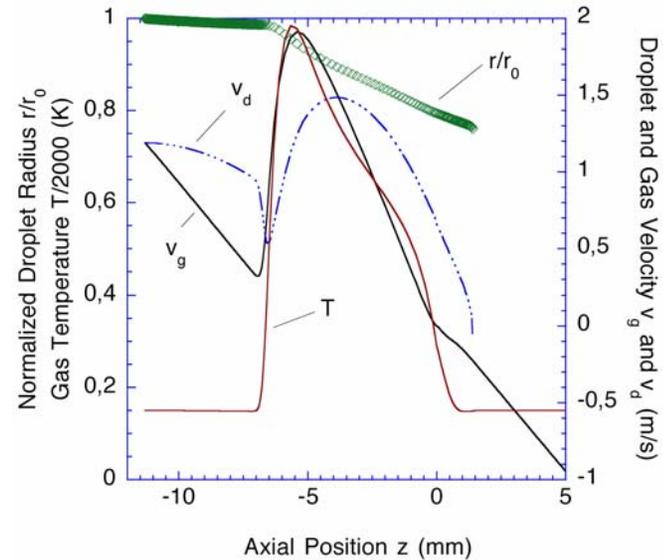
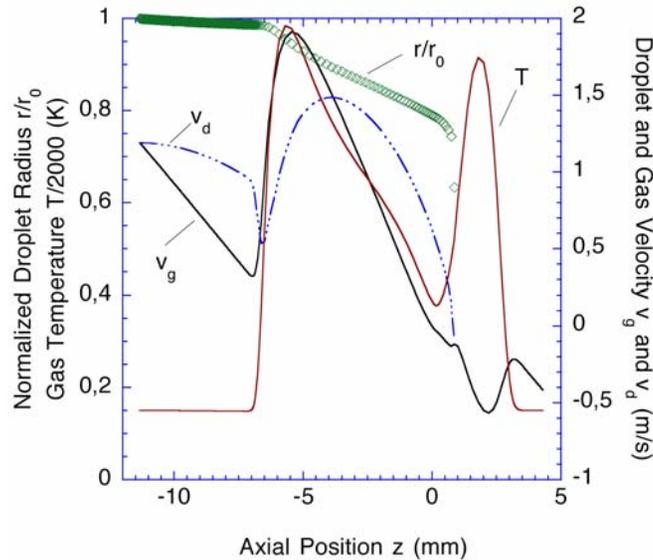
$p = 30$ bar, $\Phi = 6$, $a = 3,000/s$ (spray side), $R_{A,0} = 10$ μm , $R_{B,0} = 25$ μm , $SMR_0 = 14.3$ μm

Schlotz, D., Gutheil, E.: *Modeling of Laminar Mono- and Bidisperse Liquid Oxygen/Hydrogen Spray Flames in the Counterflow Configuration*, Combustion Science and Technology, 158, 195-210 (2000).

Multiple Structures of Spray Flames

Methanol/Air Spray Flame at Atmospheric Pressure

$$a = 100/s$$

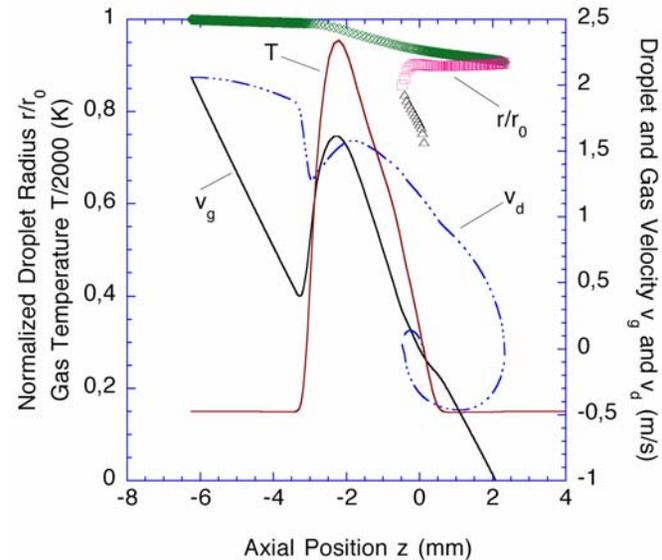
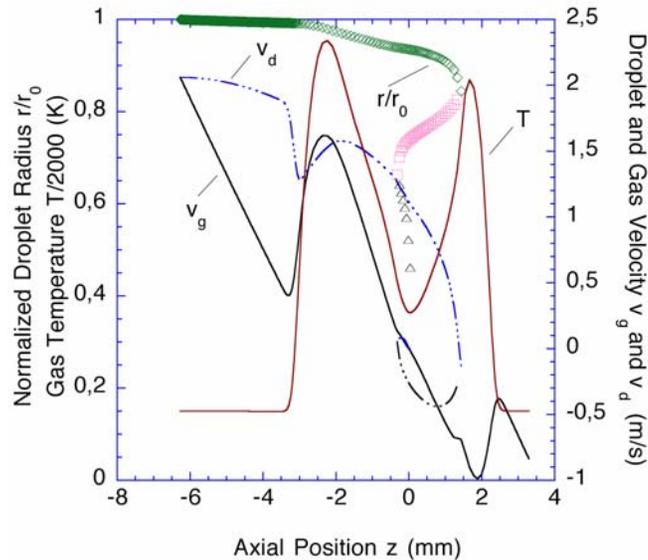


Gutheil, E.: *Multiple Solutions for Structures of Laminar Counterflow Spray Flames*, Progress in Computational Fluid Dynamics, 2004, to appear.

Multiple Structures of Spray Flames

Methanol/Air Spray Flame at Atmospheric Pressure

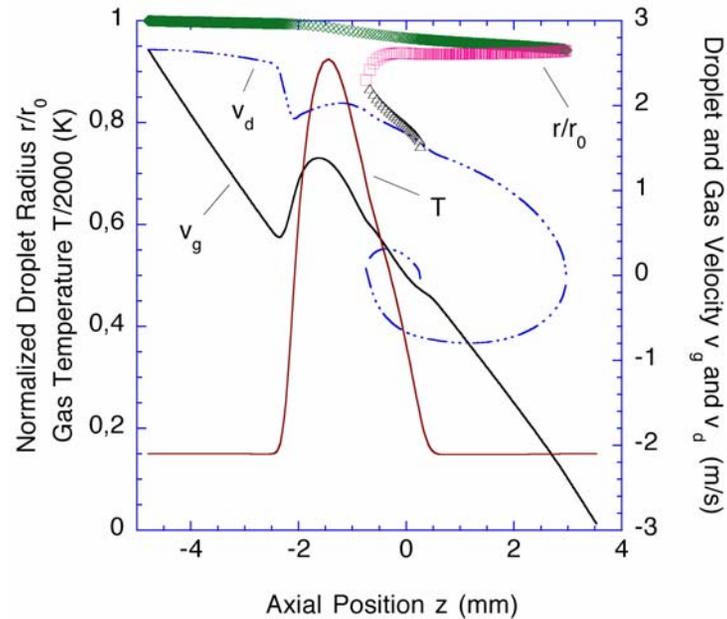
$$a = 300/s$$



Gutheil, E.: *Multiple Solutions for Structures of Laminar Counterflow Spray Flames*, Progress in Computational Fluid Dynamics, 2004, to appear.

Methanol/Air Spray Flame at Atmospheric Pressure

$a = 500/s$

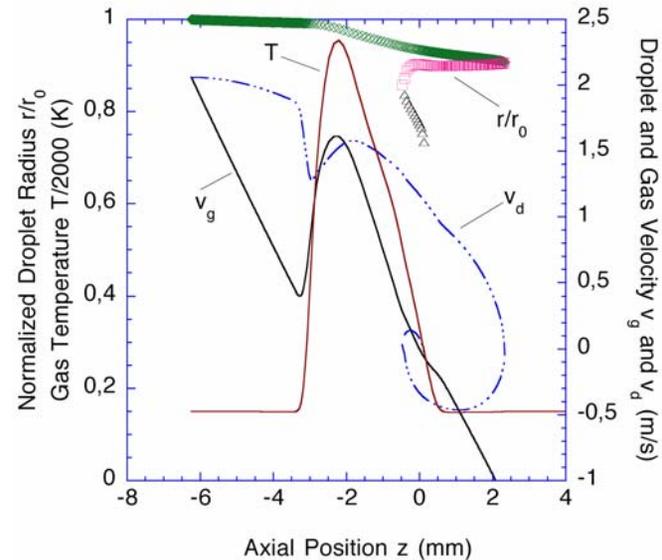
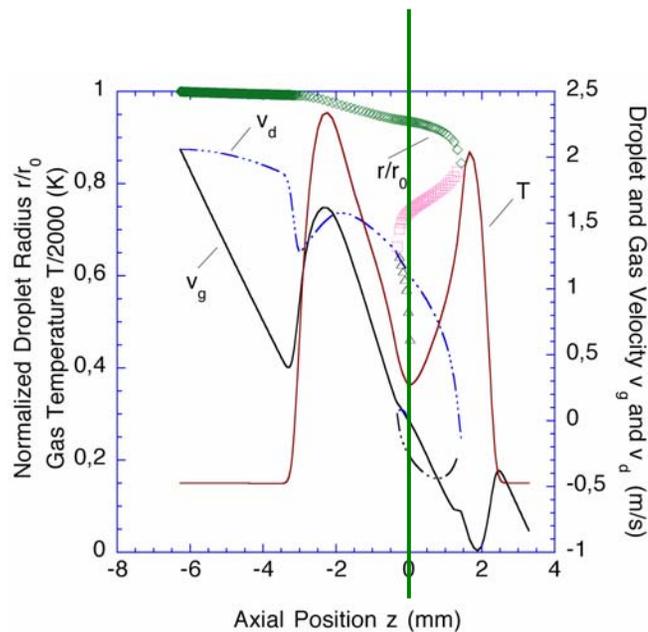


Gutheil, E.: *Multiple Solutions for Structures of Laminar Counterflow Spray Flames*, Progress in Computational Fluid Dynamics, 2004, to appear.

Multiple Structures of Spray Flames

Methanol/Air Spray Flame at Atmospheric Pressure

$$a = 300/s$$



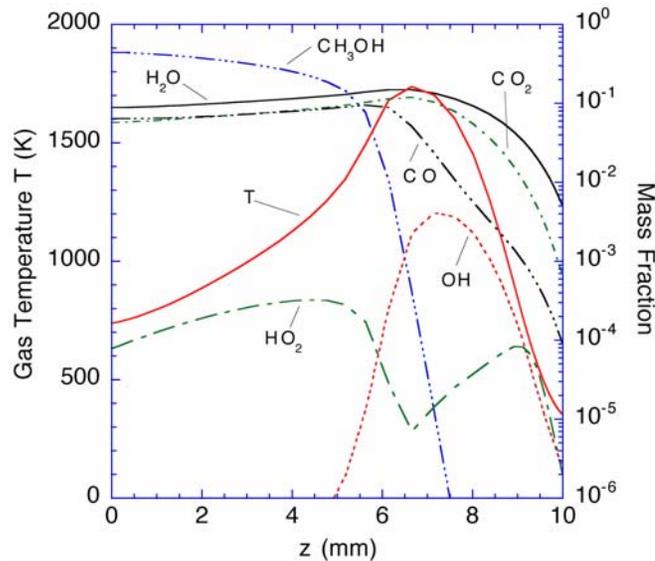
Gutheil, E.: *Multiple Solutions for Structures of Laminar Counterflow Spray Flames*, Progress in Computational Fluid Dynamics, 2004, to appear.

Comparison: Gas-Sided Flame and Pure Gas Flames

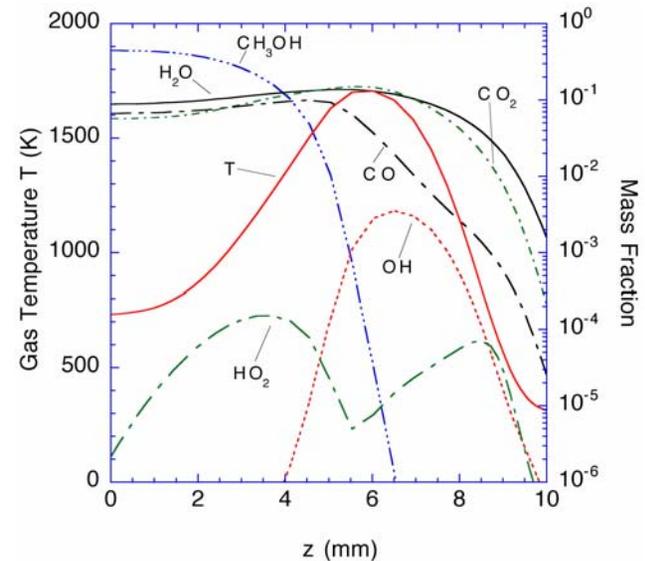
Methanol/Air Spray Flame at Atmospheric Pressure

$$a = 300/s$$

Gas Side (Spray Flame)



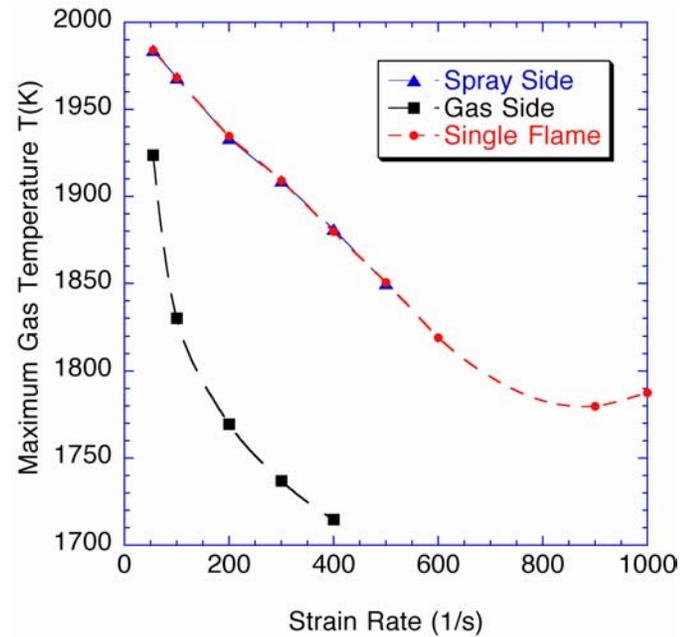
Gas Flame



Gutheil, E.: *Multiple Solutions for Structures of Laminar Counterflow Spray Flames*, Progress in Computational Fluid Dynamics, 2004, to appear.

Methanol/Air Spray Flame at Atmospheric Pressure

Comparison of Spray and Gas Flame



Gutheil, E.: *Multiple Solutions for Structures of Laminar Counterflow Spray Flames*, Progress in Computational Fluid Dynamics, 2004, to appear.



Structures of Laminar Spray Flames in the Counterflow Configuration

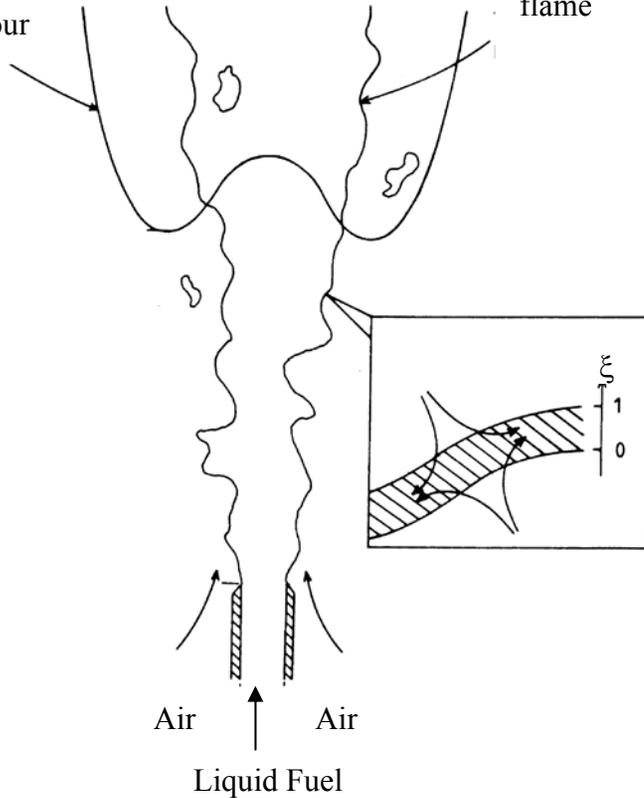
- The LOX/H₂ Spray Flames are very stable and persist to strain rates of 25,000/s. The non-monotonicity of the gaseous oxygen profile on the spray side stems from the competition of vaporization and combustion.
- Multiple structures of methanol/air spray flames have been found for strain rates up to 400/s. The inner structure of the gas-sided flame is the same as a pure gas flamelet with appropriate initial conditions.
- At high strain, the gas-sided flame is extinguished and the spray-sided flame moves towards the gas-side of the counterflow configuration.

Question: How does the finding affect models such as the flamelet model for turbulent spray diffusion flames?

Flamelet-Model for Turbulent Diffusion Flames

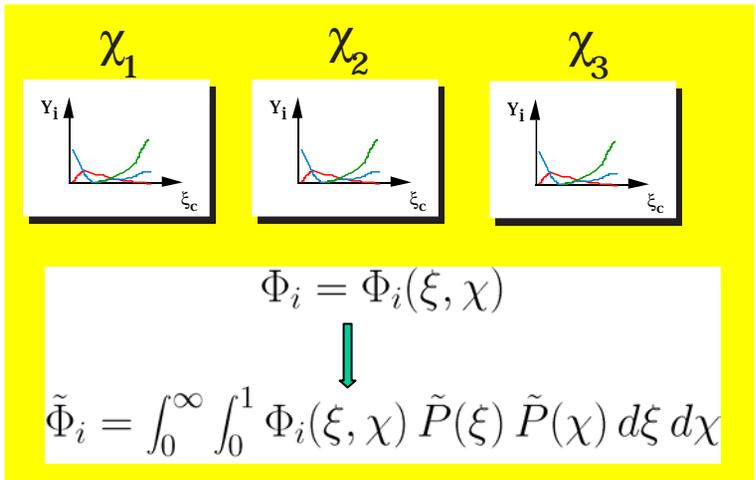
Turbulent Flame

Mean luminous
flame contour



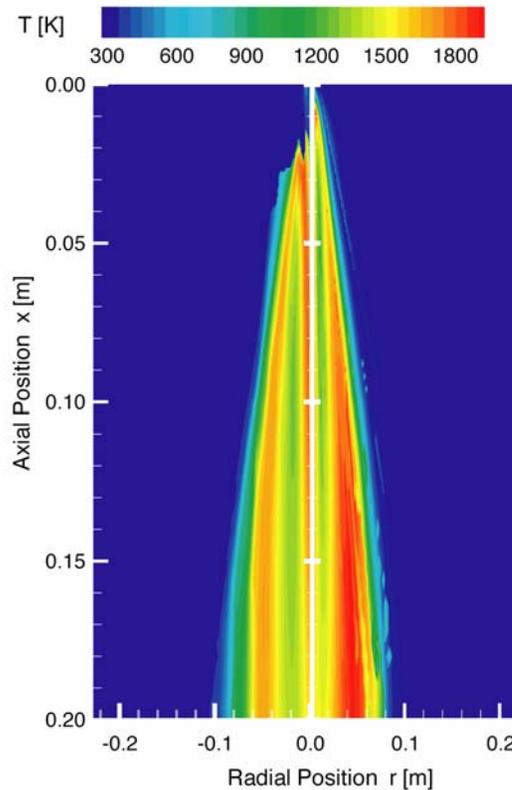
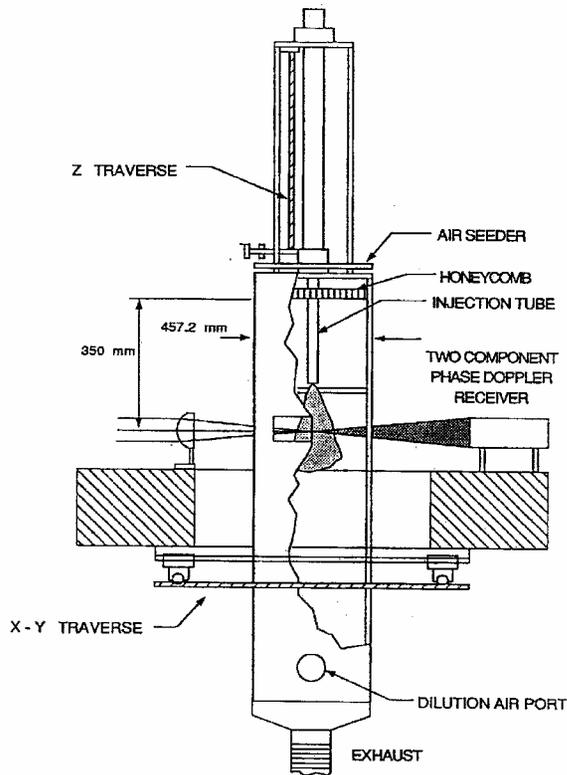
Thin diffusion
flame

Library of laminar flame structures
in the counterflow configuration



- Gas flames
 - Strain rate
- Spray flames
 - Strain rate
 - Droplet size
 - Droplet velocity
 - Equivalence ratio

Laminar Spray Flame Structures for Use in Flamelet Models for Turbulent Spray Diffusion Flames (Methanol/Air)

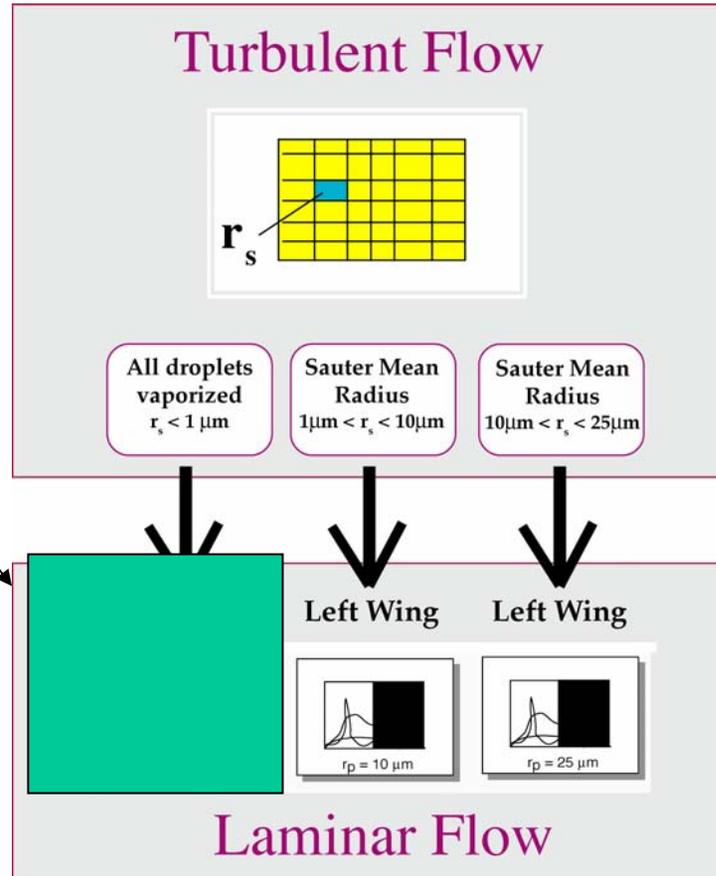


LHS: Gas Flamelets
RHS: Spray Flamelets

Experiment: McDonnell V.G., Samuelsen, G.S., *UCI-Laboratory Report UCI-ARTR-90-17A-C* (1990)

Simulation: Hollmann, C., Gutheil, E., *Combust. Sci. and Tech.* **135** 1-6, 175 (1998).

Modeling of Turbulent Spray Flames



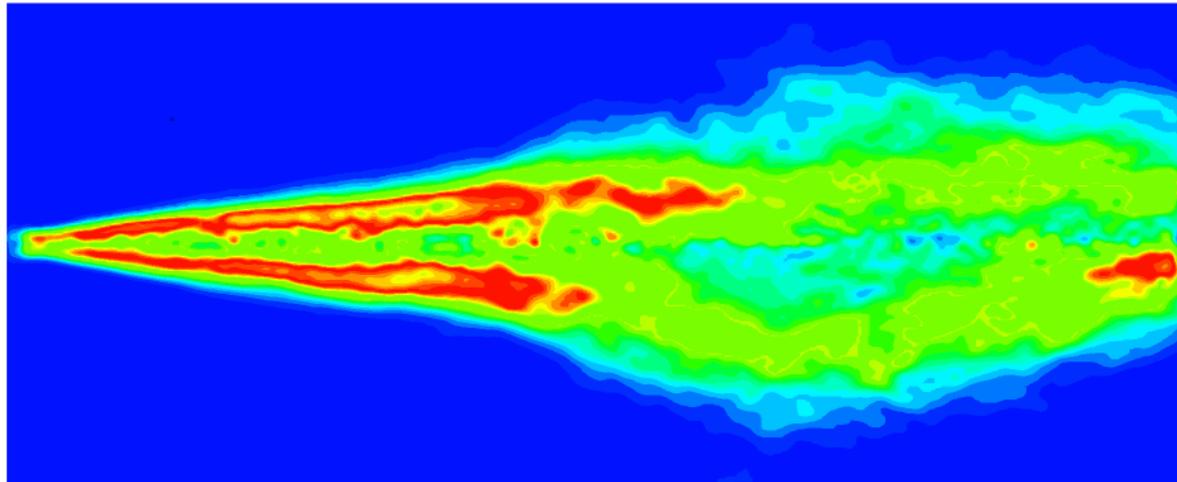
Replace by Pure
Gas Flamelet

Leads to Simplification
of Implementing
Laminar Spray Flamelets

Modeling of Turbulent LOX/H₂ Spray Flames

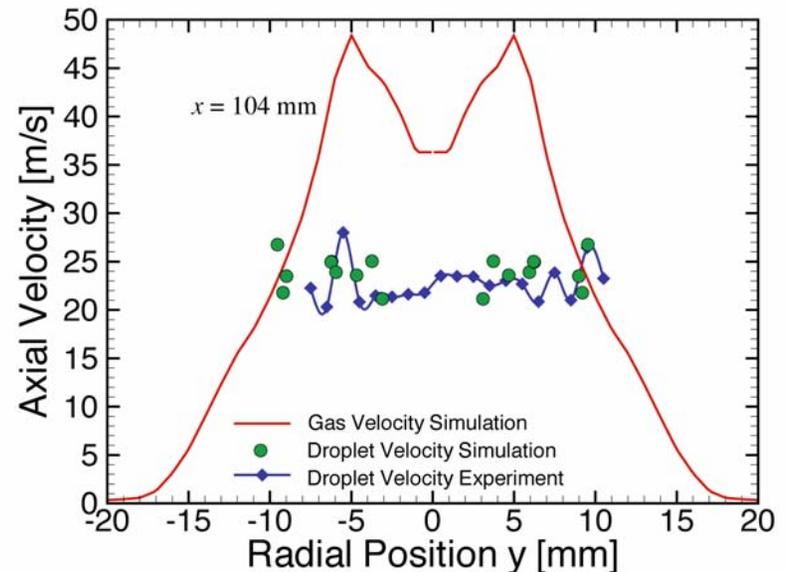
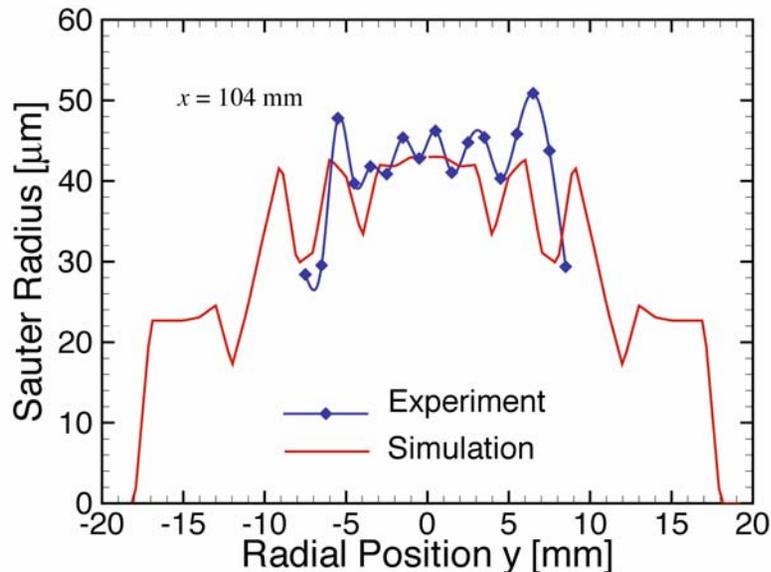
Micro Combustion Chamber M3 (DLR Lampoldshausen)

OH-Emission, $p = 5$ bar, $T_0 = 100$ K



← 140 mm →

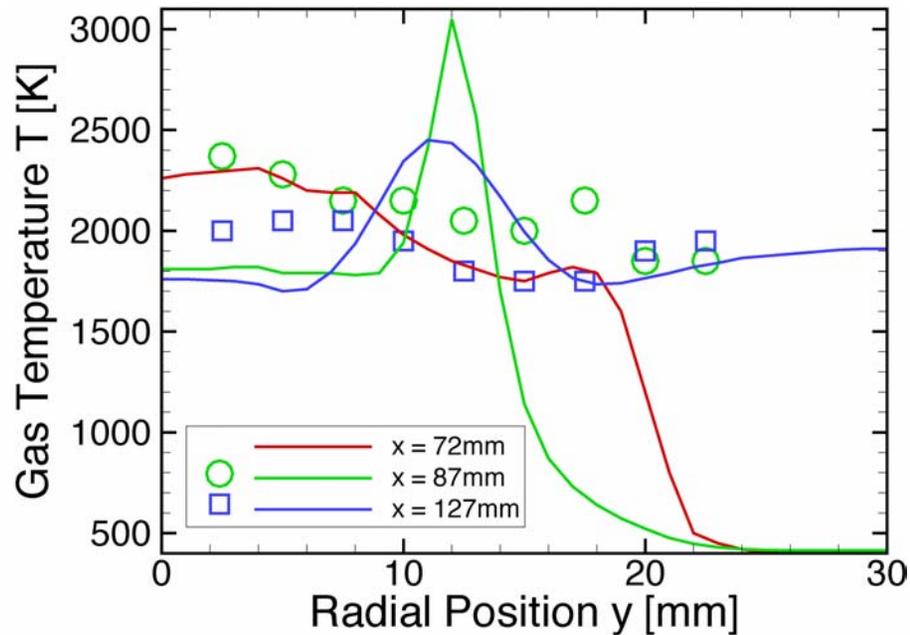
Modeling of Turbulent Spray Flames



Experiment: Sender, J., *et al.*, *Proceedings of the 13th Annual Conference on Liquid Atomization on Spray Systems*, Florence, Italy, 145-154 (1997).

Simulation: Schlotz, D., Brunner, M., Gutheil, E.: *Modeling of Turbulent LOX/H₂ Combustion under Cryogenic and Elevated Pressure Conditions*, ILASS Europe Conference, Zürich, September 2-6 (2001).

Modeling of Turbulent Spray Flames



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Mixing in Turbulent Sprays

- The β -function that is typically used to describe the mixing in turbulent diffusion flames does not perform well in regions where vaporization is present¹.
- **Here:** Modification of the description of the β -function through use of a transport equation for the probability density function of the mixture fraction, \tilde{f} , in turbulent sprays²:

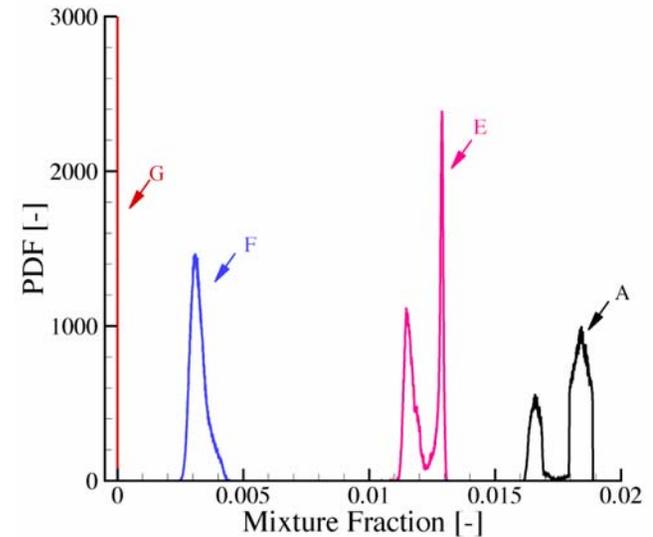
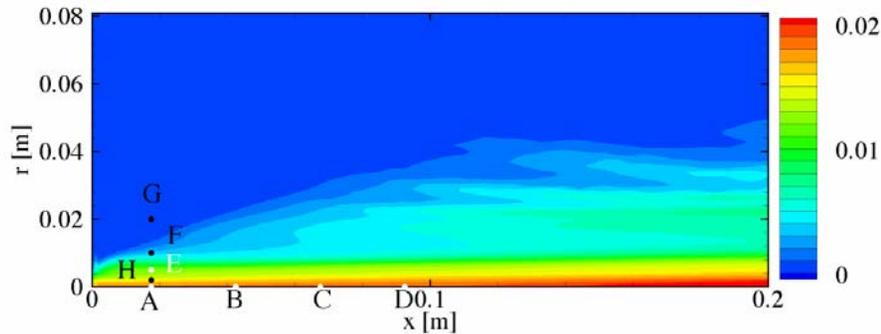
$$\bar{\rho}_g \frac{\partial \tilde{f}}{\partial t} + \bar{\rho}_g U_j \frac{\partial \tilde{f}}{\partial x_j} + \frac{\partial (\bar{\rho}_g \bar{S}_s \tilde{f})}{\partial \zeta_c} = - \frac{\partial}{\partial \zeta_c} \left[\bar{\rho}_g \left\langle \frac{\partial}{\partial x_j} \left(D_M \frac{\partial \xi_c}{\partial x_j} \right) \middle| \zeta_c \right\rangle \tilde{f} \right].$$

¹Miller R.S. Bellan, J. On the Validity of the Assumed Probability Density Function Method for Modeling Binary Mixing/ Reaction of Evaporated Vapor in Gas/Liquid-Droplet Turbulent Shear Flow, *Proc. Combust. Inst.* **27**: 1065-1072, 1998.

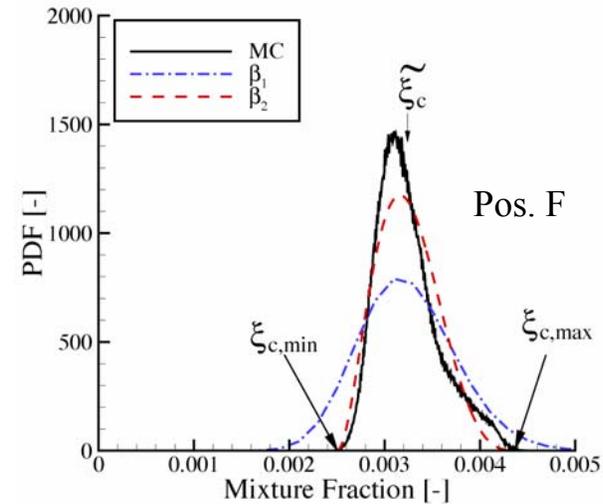
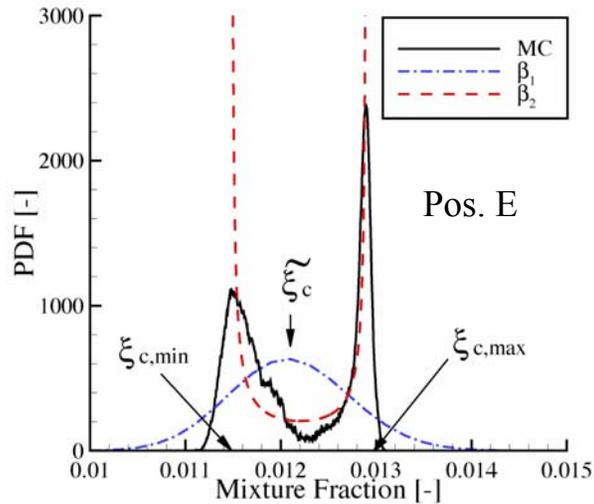
²Ge, H.-W., Gutheil, E.: PDF Simulation of Turbulent Spray Flows, *Atomiz. Sprays*, 2004, submitted.

Mixing in Turbulent Methanol/Air Sprays

Methanol Vapor Fraction and PDF of the Mixture Fraction



Probability Density Functions at Various Positions

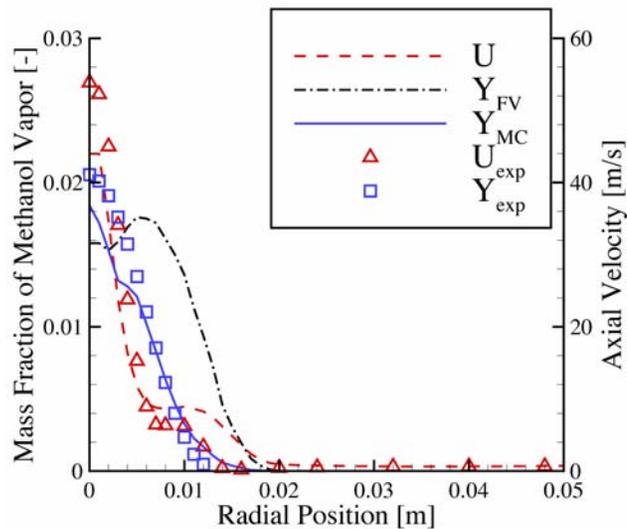


$$P(\xi_c) = \frac{\Gamma(\alpha + \beta)}{\Gamma(\alpha)\Gamma(\beta)} \xi_c^{\alpha-1} (1 - \xi_c)^{\beta-1}$$

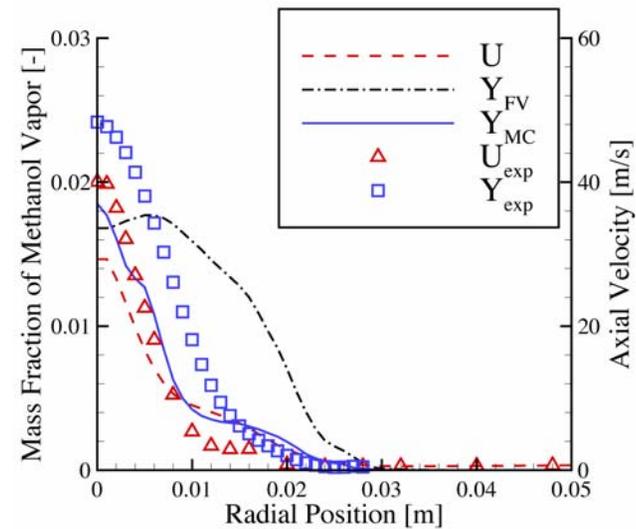
$$P(\xi_c) = \frac{\Gamma(\alpha + \beta)}{\Gamma(\alpha)\Gamma(\beta)} (\xi_{c,max} - \xi_{c,min})^{1-\alpha-\beta} (\xi_c - \xi_{c,min})^{\alpha-1} (\xi_{c,max} - \xi_c)^{\beta-1}$$

Comparison of Results with Presumed and Monte-Carlo PDF, and with Experiment

$x = 25 \text{ mm}$



$x = 50 \text{ mm}$



Experiment: McDonnell, V. G. and Samuelsen, G.S., An Experimental Data Base for Computational Fluid Dynamics of Reacting and Nonreacting Methanol Sprays, *J. Fluids Engin.* **117**: 145-153, 1995.

Simulation: Ge, H.-W., Gutheil, E.: PDF Simulation of Turbulent Spray Flows, *Atomiz. Sprays*, 2004, submitted.



Summary and Conclusions

- LOX/H₂ spray flames in the counter-flow configuration have been studied, and the gaseous oxygen profile shows a non-monotonic behavior because of the high reactivity of the system. The flames persist to strain rates up to 25,000/s, and extinction has not yet been found.
- Multiple structures of laminar methanol/air counter-flowing spray flames have been identified at low strain rates up to 400/s on the spray side of the configuration for the present conditions. The gas-sided spray flame shows the same inner structure as a pure gas flamelet with appropriate boundary conditions, and this simplifies the implementation of the flamelet model for turbulent spray diffusion flames.
- The assumed β -function for the turbulent mixing in spray flames is poor in regions where vaporization exists, and it has been replaced by a PDF transport equation for the mixture fraction. A modified β -function is suitable to predict the shape of the PDF of the mixture fraction.



Future Research

- Extension of the model to unsteady flamelets
- Application of the PDF method to turbulent spray flame simulations
- Extension to other liquids