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Space-time adaptive FIR filtering with staggered PRI

Space-Time Adaptive FIR filtering with staggered PRI

Richard Klemm

FGAN

Wachtberg, Germany

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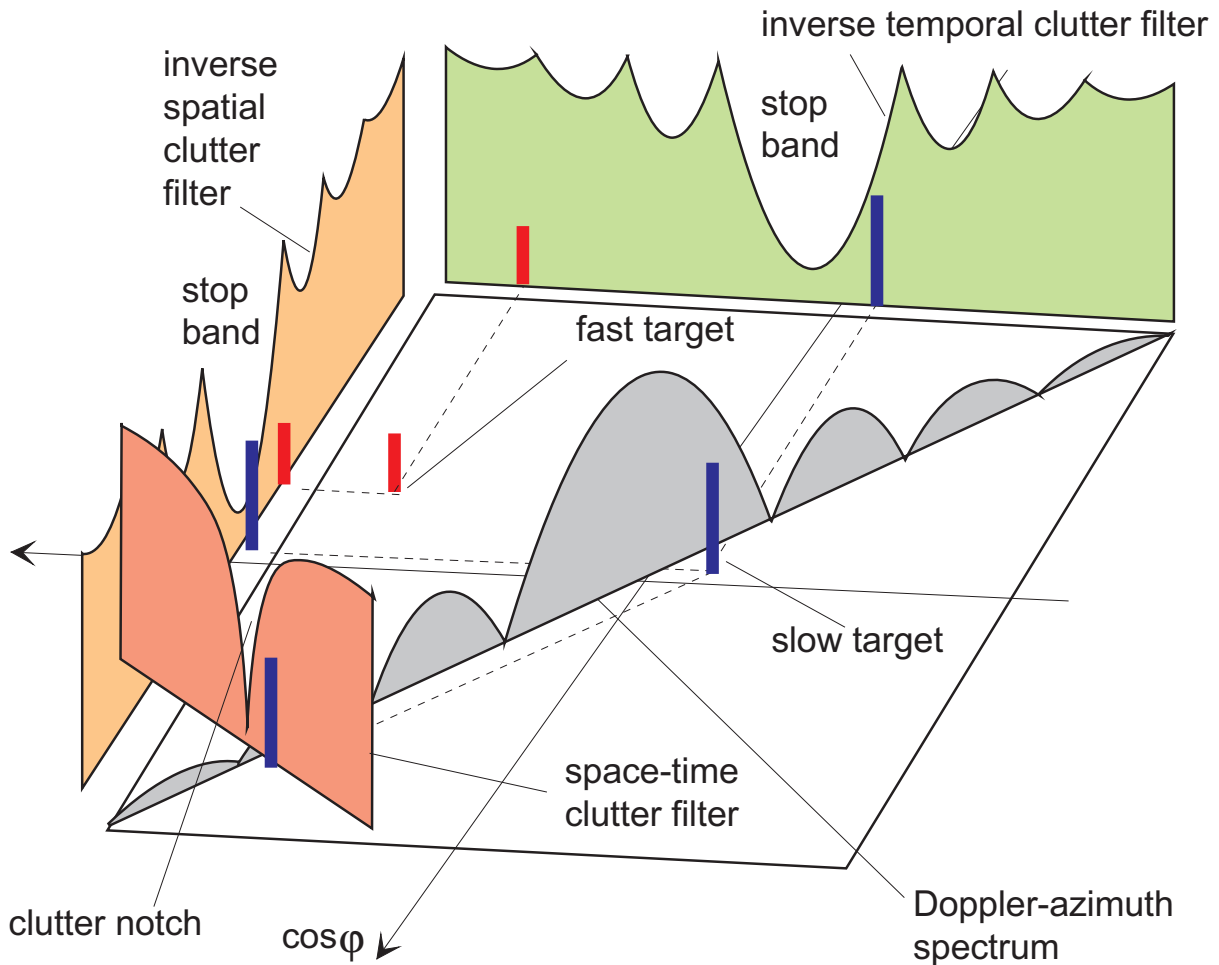
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Space-time adaptive FIR filtering with staggered PRI

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- Principle of STAP FIR filters
- FIR filters with staggered PRI
- Numerical example
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Principle of STAP

- clutter spectrum
- temporal filter
- spatial filter
- STAP

Principle of STAP

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Space-time adaptive FIR filtering with staggered PRI

The optimum processor

$$\mathbf{w} = \mathbf{a}\mathbf{Q}^{-1}\mathbf{s}(\mathbf{j}, \nu)$$

Q space-time clutter+noise covariance matrix

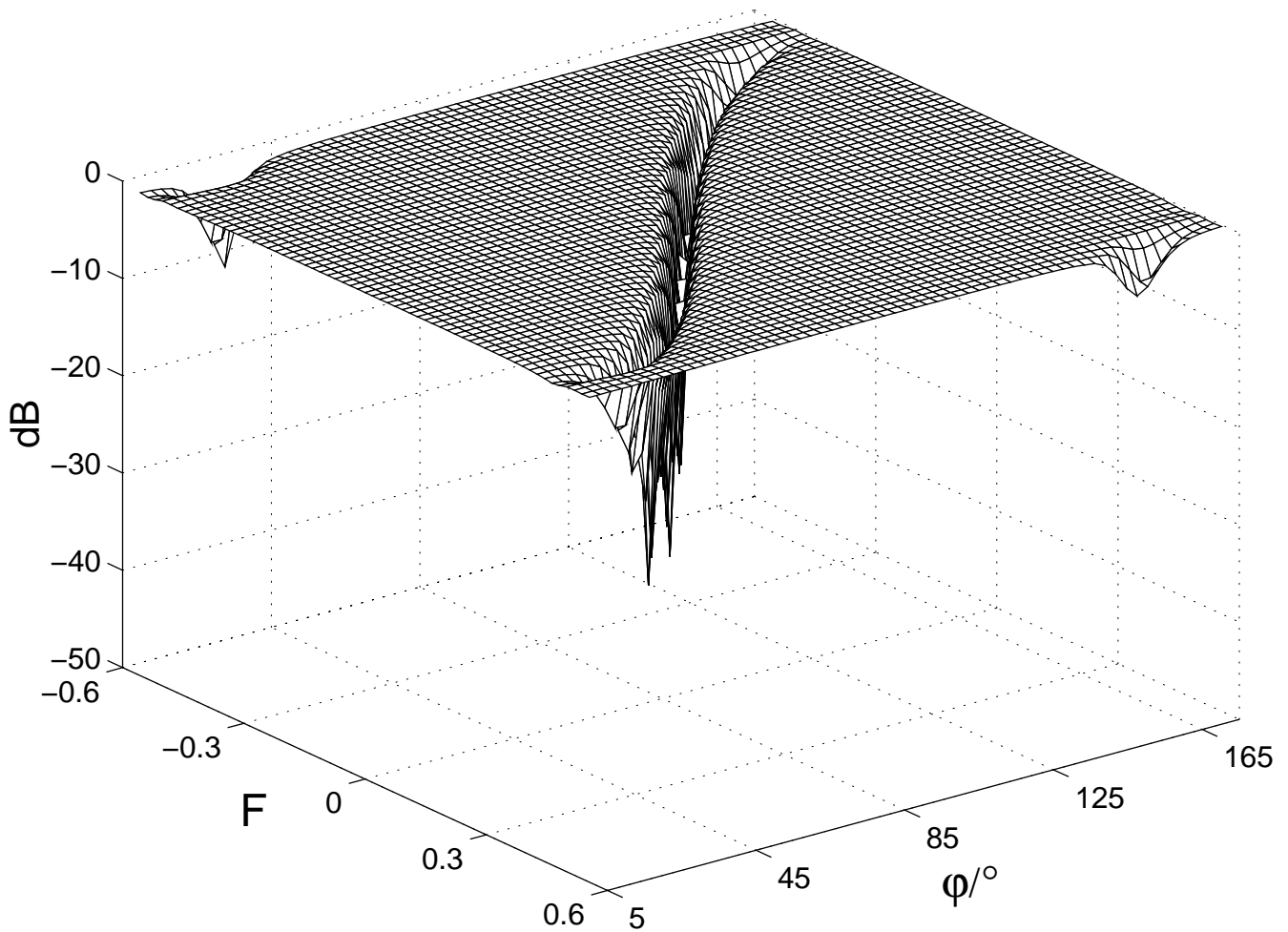
s space-time steering vector

For large dimensions N, M not realizable by various reasons
(amount of computations, lack of training data, accuracy)

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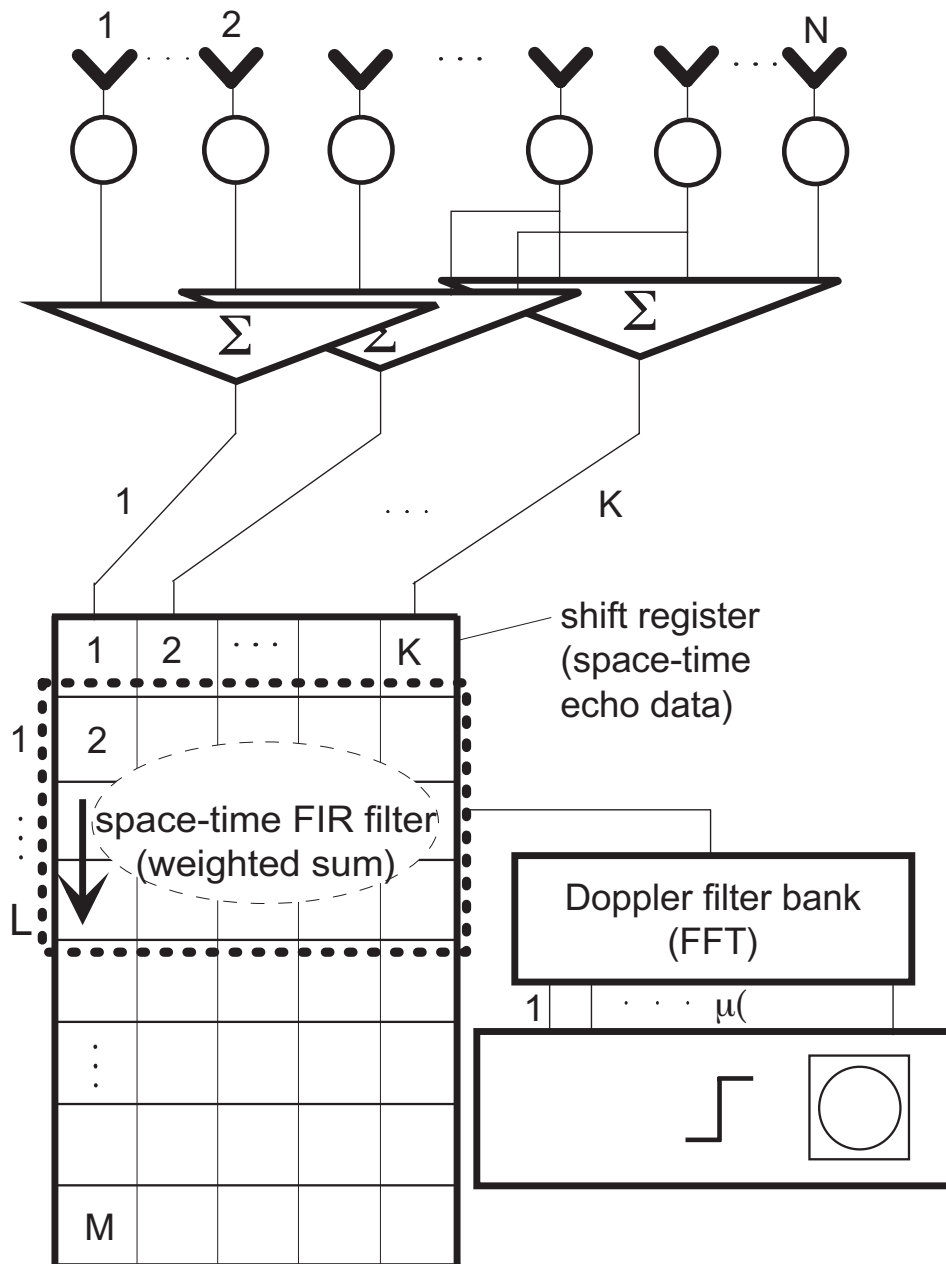
Azimuth-Doppler Characteristics of a STAP Filter for Sidelooking Array

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Subspace STAP techniques

- Space-time transforms (e.g. GSC concepts)
- Spatial transforms (reduction in the spatial dimension)
- **FIR filters** (reduction in the temporal dimension, => very efficient solution)
- Multi-stage filters
- Frequency dependent spatial processing (for large CPI only)
- Angle-Doppler subgroups (e.g. JDL-GLRT)
- others

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Overlapping subarray processor with space-time FIR filter

Space-time adaptive FIR filtering with staggered PRI

$$\mathbf{Q} = \begin{pmatrix} \mathbf{Q}_{11} & \mathbf{Q}_{12} & \cdots & \mathbf{Q}_{1M} \\ \mathbf{Q}_{21} & \mathbf{Q}_{22} & \cdots & \mathbf{Q}_{2M} \\ \vdots & \vdots & \ddots & \vdots \\ \mathbf{Q}_{M1} & \mathbf{Q}_{M2} & \cdots & \mathbf{Q}_{MM} \end{pmatrix}$$

The space-time clutter+noise covariance matrix

$$\mathbf{K} = \mathbf{Q}^{-1} = \begin{pmatrix} \mathbf{K}_{11} & \mathbf{K}_{12} & \cdots & \mathbf{K}_{1M} \\ \mathbf{K}_{21} & \mathbf{K}_{22} & \cdots & \mathbf{K}_{2M} \\ \vdots & \vdots & \ddots & \vdots \\ \mathbf{K}_{M1} & \mathbf{K}_{M2} & \cdots & \mathbf{K}_{MM} \end{pmatrix}$$

and its inverse

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$$\mathbf{K} = \mathbf{Q}^{-1} = \begin{pmatrix} \mathbf{K}_{11} & \mathbf{K}_{12} & \cdots & \mathbf{K}_{1L} \\ \mathbf{K}_{21} & \mathbf{K}_{22} & \cdots & \mathbf{K}_{2L} \\ \vdots & \vdots & \ddots & \vdots \\ \mathbf{K}_{L1} & \mathbf{K}_{L2} & \cdots & \mathbf{K}_{LL} \end{pmatrix}$$

The north-west $NL \times NL$ submatrix

(N number of antenna elements, L temporal filter length)

$$\tilde{\mathbf{K}} = \begin{pmatrix} \mathbf{K}_{11} \\ \mathbf{K}_{21} \\ \vdots \\ \mathbf{K}_{L1} \end{pmatrix}$$

The LS FIR filter matrix (1. Block column of inverse)

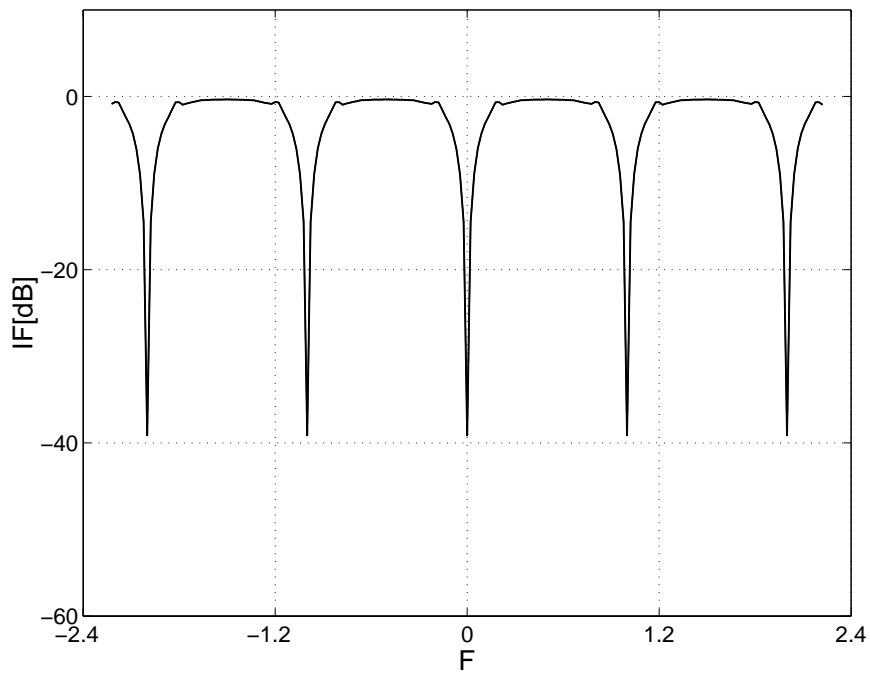
$$\mathbf{h} = \tilde{\mathbf{K}}\mathbf{b}$$

Further reduction: beamforming

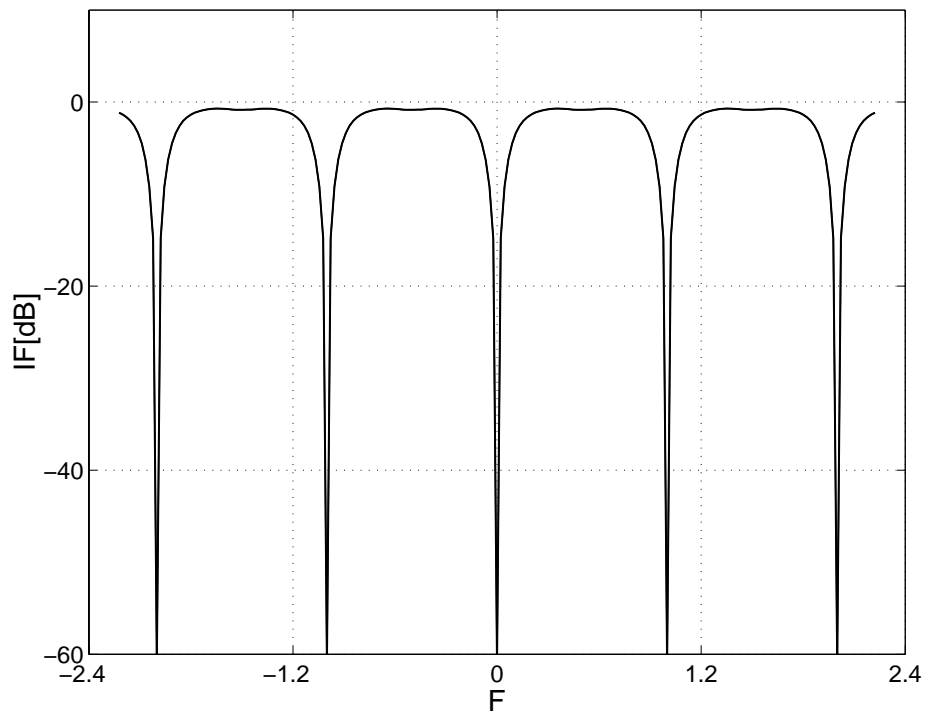
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Fully adaptive processing, constant PRI



FIR filter, 5 taps, constant PRI

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Space-time adaptive FIR filtering with staggered PRI

a. $\epsilon=0$



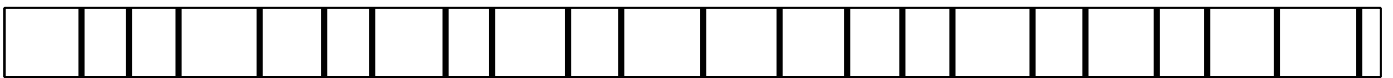
b. $\epsilon=0.03$



c. $\epsilon=0.1$



d. $\epsilon=0.3$



Pseudorandom PRI staggering

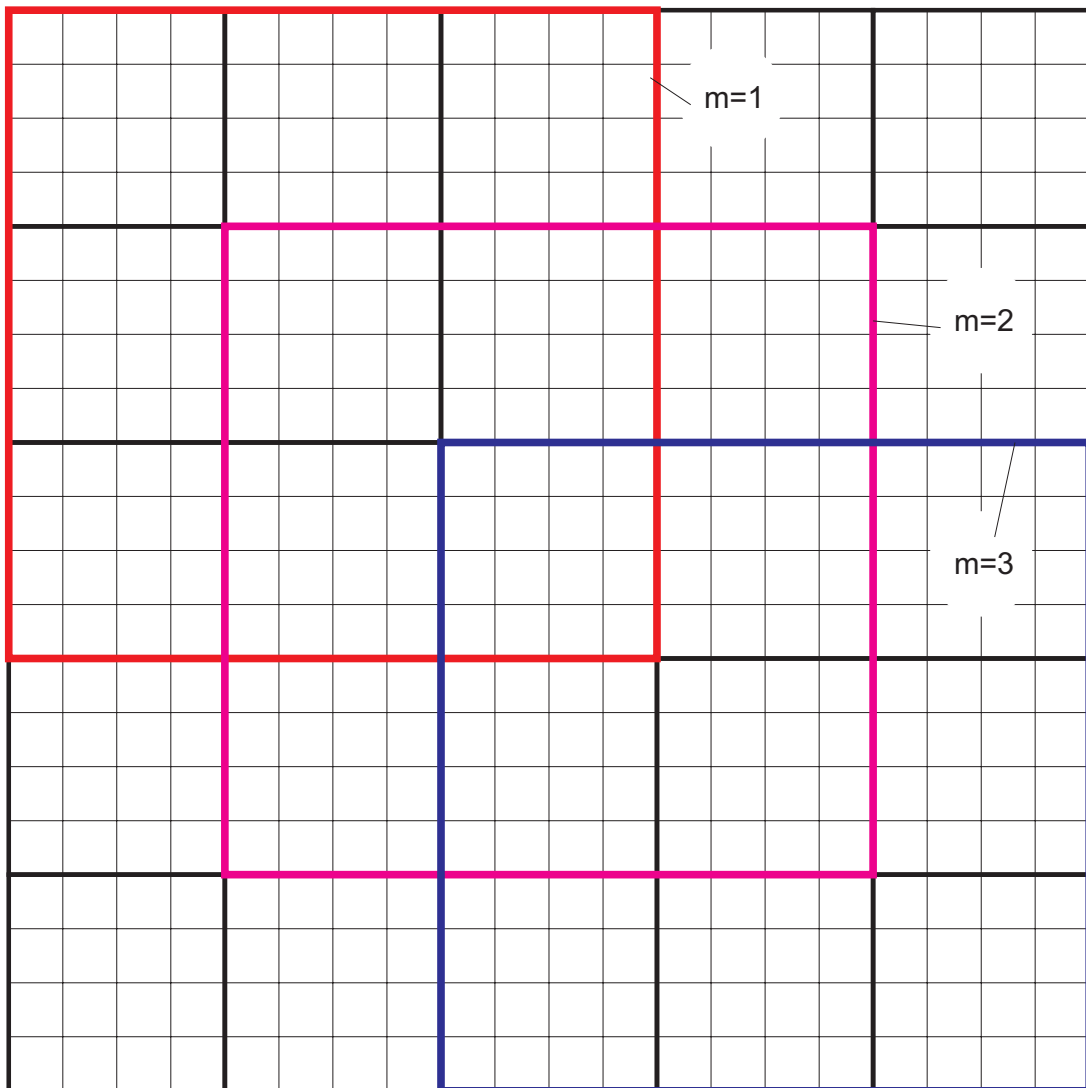
Properties of staggered PRI

- Avoidance of multiple clutter notches (blind velocities)
- Unambiguous target Doppler estimates
- Resistance against spot jammers
- However: no FFT for Doppler filter bank

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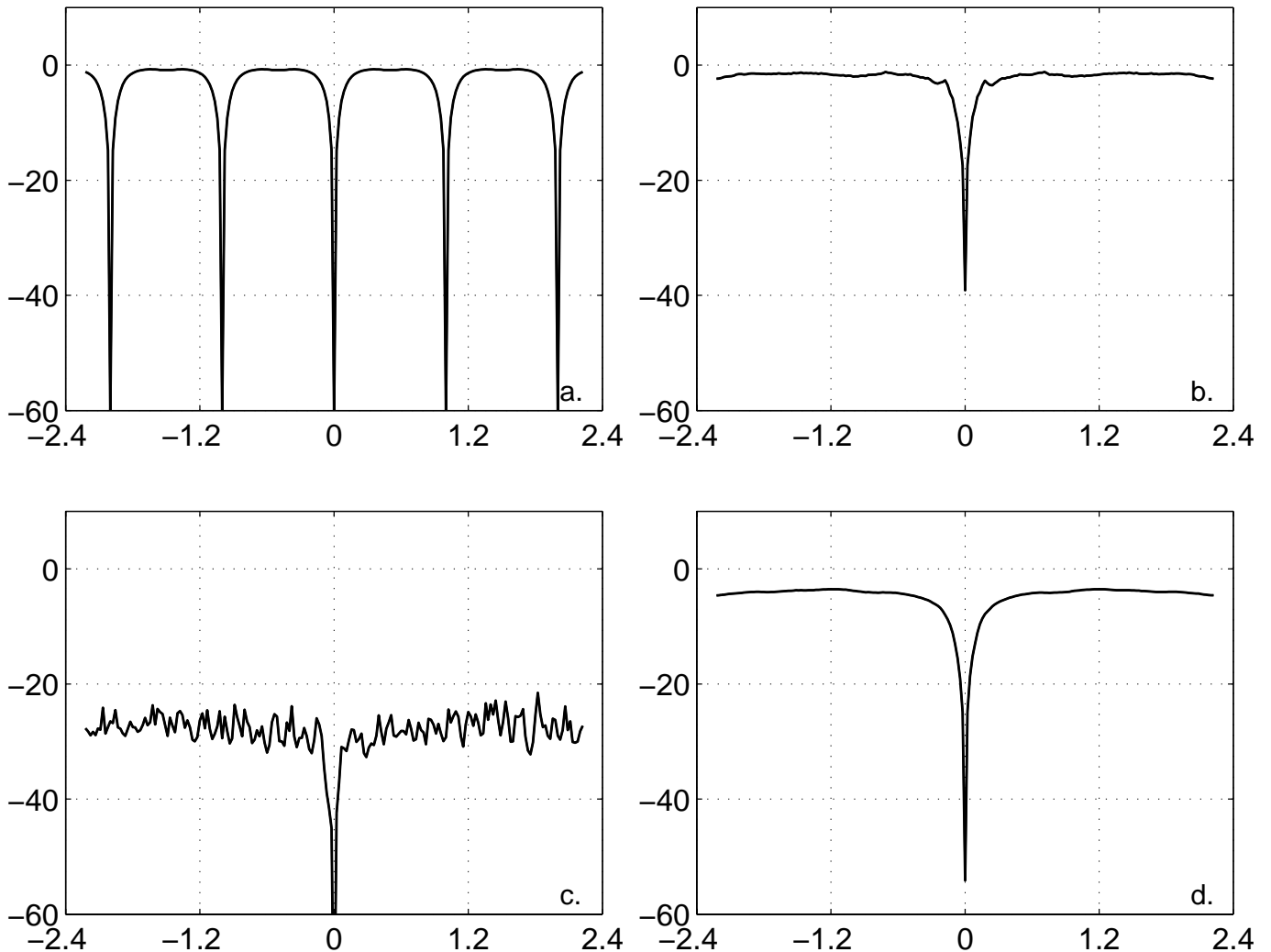
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- elements of spatial submatrices
- $K \times K$ spatial submatrices
- shifted diagonal space-time submatrices ($K=4$, $L=3$)

Matrix scheme for space-time FIR filtering
($K=4$, $M=5$, $L=3$)

Space-time adaptive FIR filtering with staggered PRI



Space-time FIR filter with staggered PRI

- a. optimum processing, **no staggering**, Nyquist sampling in space & time
- b. optimum processor, **staggered** PRI
- c. **fixed** ST FIR filter, **staggered** PRI
- d. **STAP** FIR filter with **variable** coefficients

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Space-time adaptive FIR filtering with staggered PRI

Summary

- **Staggered PRI:** avoiding blind velocities (ambiguous) clutter notches, unambiguous estimation of target Doppler, resistance against spot jammers
- The **optimum (LR) STAP processor** can cope with staggered PRI
- The STAP **FIR filter** is a most efficient tool for real-time clutter rejection
- **FIR** filters with **constant coefficients** are mismatched to staggered echo sequences
- FIR filters with **varying coefficients** (readaption at every PRI)
- **Loss** compared with constant FIR filter and constant PRI: a few dB