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**An Automated Fluid-Structural Interaction  
Analysis of a Large Segmented Solid Rocket  
Motor**

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Brigham City, UT**

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Huntsville, AL**

# **An Automated Fluid-Structural Interaction Analysis of a Large Segmented Solid Rocket Motor**

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The ETM-3 motor is basically an RSRM motor with an additional center segment added. The propellant burn rate was lowered to account for the additional surface area of the motor and the nozzle throat diameter was increased. The additional segment also increased mass flow and mach number in the motor. Because of this harsher flow environment, it was thought necessary to chamfer the leading edges of every segment and conduct a detailed fluid/structural interaction (FSI) analysis to ensure propellant grain stability against boot-strapping. The analyses showed that the addition of the 3 inch radial by 24 inch axial chamfer on the leading edges of the center/forward, center, center/aft, and aft segments was sufficient to give the ETM-3 motor stable grain displacements at much lower than expected propellant moduli. This report documents the FSI analysis work done for ETM-3.

The analyses conducted and documented in this report assumed linear elastic material behavior and quasi-steady state fluid behavior without time response in either the structural or fluid models. Thus, the analyses represented only an approximation at a single snapshot in time. This led to selecting the largest chamfer size analyzed herein to get the biggest safety factor against boot-strapping.

## **INTRODUCTION**

The ETM-3 motor is basically an RSRM motor with an additional center segment added to the original 4 segments. The propellant burn rate was lowered to account for the additional surface area of motor. The additional segment also increased mass flow and mach number in the motor, even with the lower burn rate. Because of this harsher flow environment, it was necessary to conduct a detailed fluid/structural interaction (FSI) analysis to ensure propellant grain stability against boot strapping.

Boot-strapping is the name given to the phenomenon where flow in the rocket motor imposes pressure on the propellant grain, which displaces in response, which then leads to flow changes, which produce even more grain displacement until flow is ultimately blocked or the grain fails.

## **TEST ARTICLE DESCRIPTION**

The ETM-3 motor was a 5 segment RSRM type motor. The RSRM has 4 segments. Thus, one segment was added to create the ETM-3 motor. The propellant used in the motor was TP-H1148, Type VII, which is basically RSRM propellant with different AP grind ratios and different burn rate catalyst. The ETM-3 motor was to be static tested in summer of 2003, at T-97, Promontory, Utah. The center and aft segments of ETM-3 had 3 inch radial and 24 inch axial chamfers on the forward bore surfaces.

## **METHOD OF ANALYSIS**

Boot strapping in a solid rocket motor is both an undesirable and complex phenomenon involving interaction between the flow/ballistics and grain structure of the motor itself. The analysis method used in this report used an automated, iterative procedure between a steady-state CFD flow solution and a linear elastic deformation

analysis. FLUENT® software was used for the flow solution, while ABAQUS® was used for the structures solver. The procedure was automated between the two solvers with FEM Builder®, an in-house, finite element, pre- and post-processor, and Python scripting language.

The procedure was as follows:

1. Fluid and solid models are prepared and linked with FEM Builder®/Python Script
2. FEM Builder®/Python script is started, which calls FLUENT®
3. FLUENT® calculates flow (pressures) on nominal geometry
4. Pressures from FLUENT® solution are applied to structural model (nominal geometry) automatically with FEM Builder®/Python script
5. ABAQUS® calculates deformations for the applied pressure
6. These deformations (or some percentage of them) are applied to

the fluid grid, which is then re-meshed and smoothed.

7. FLUENT® calculates flow (pressure) for the second time
8. Pressures from FLUENT® solution are applied to structural model (nominal geometry) automatically with FEM Builder®/Python script
9. Process continues until maximum number of iterations specified or until convergence of the solid model is reached (grain is no longer moving between each iteration)
10. Each Fluid-Structural Interaction (FSI) analysis is performed with a fixed propellant modulus
11. Critical modulus is determined to be the value at which the grain deformations are stable (i.e. not changing with iteration)

A schematic of the foregoing FSI analysis process description is shown in Figure 1.

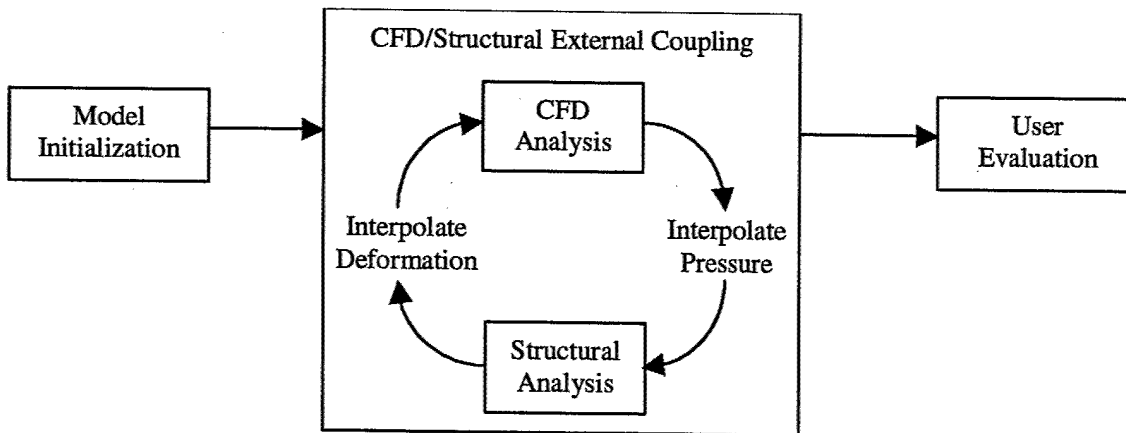
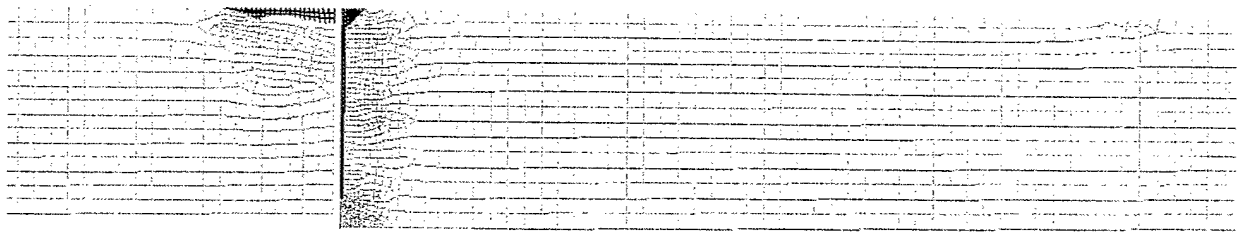


Figure 1. Schematic of FSI Analysis Process

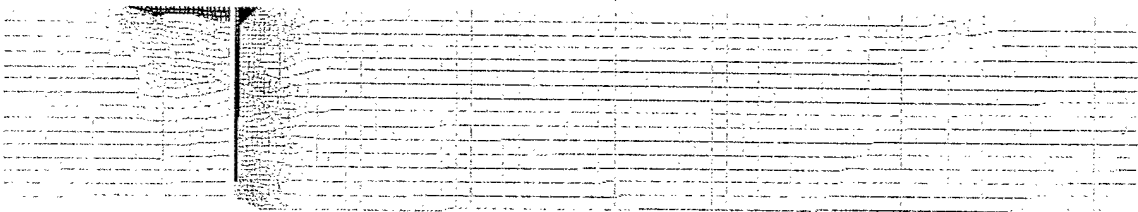
## STRUCTURAL MODELS

Portions of the structural models of ETM-3, with and without various sizes of chamfers are shown in Figures 2 through 5. All

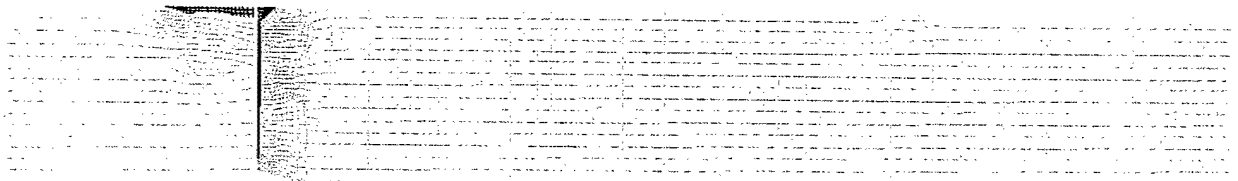
segments of ETM-3 were modeled, even though only a portion is shown in the figures. Figure 6 shows the outline of the entire motor, and the location of the critical slot for boot strapping.



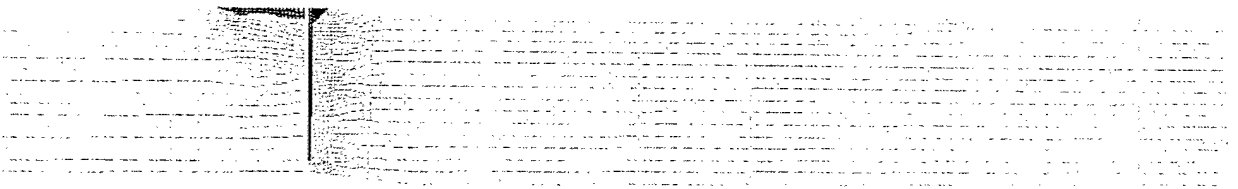
**Figure 2. Structural Model of ETM-3, Nominal Geometry, No Chamfers**



**Figure 3. Structural Model of ETM-3, Nominal Geometry, 3 x 6 inch Chamfers**



**Figure 4. Structural Model of ETM-3, Nominal Geometry, 3 x 12 inch Chamfers**



**Figure 5. Structural Model of ETM-3, Nominal Geometry, 3 x 24 inch Chamfers**



**Figure 6. Structural Model of ETM-3 showing critical slot for boot strapping**

## BOUNDARY CONDITIONS FOR STRUCTURAL/FLUID MODELS

A summary of the boundary conditions analyzed in this report is shown in Table 1. The fluid models used the burn rates shown to compute pressures that were applied to the structural models as boundary conditions. Additional boundary conditions used in the structural models are also shown. The head end pressures calculated for the given burn rates are shown in the table for reference. No horizontal slump loading was

included with any of the models because of the 2-D limitations of the models.

The last three analyses shown in Table 1 were performed to provide converged pressure boundary conditions for the PLI structural analyses. Furthermore, these analyses were performed at the expected propellant moduli based on Reference 1, namely 990 and 2150 psi for 90° and 40°F, respectively. The analysis at 55°F was performed at 1675 psi propellant modulus, which was determined by interpolation of the 50°F and 60°F data from TR-12874.

**Table 1. Summary of Boundary Conditions**

| Motor  | Configuration                    | 2-D Burn Rate for Pressure Boundary Conditions                  | Head End Pressure (for Ref.) | Temp Load                | Slump | Propellant Modulus                    |
|--|----------------------------------|---|------------------------------|--------------------------|-------|---------------------------------------|
| ETM-3  | no chamfer, nominal geometry     | MEOP<br>.343 in/sec propellant<br>1.629 in/sec fin propellant   | ~940 psi                     | SFT to 70°F              | no    | varying to determine critical modulus |
| ETM-3  | 3 x 6 chamfer, nominal geometry  | MEOP<br>.3698 in/sec propellant<br>1.7563 in/sec fin propellant | ~1023 psi                    | SFT to 70°F              | no    | varying to determine critical modulus |
| ETM-3  | 3 x 12 chamfer, nominal geometry | MEOP<br>.361 in/sec propellant<br>1.7147 in/sec fin propellant  | ~1010 psi                    | SFT to 70°F              | no    | varying to determine critical modulus |
| ETM-3  | 3 x 24 chamfer, nominal geometry | MEOP<br>.361 in/sec propellant<br>1.7147 in/sec fin propellant  | ~1010 psi                    | SFT to 70°, 80°, or 90°F | no    | varying to determine critical modulus |
| <b>Converged Analyses Used for PLI Structural Analysis Boundary Conditions</b> |                                  |   |                              |                          |       |                                       |
| ETM-3  | 3 x 24 chamfer, nominal geometry | MEOP<br>.3635 in/sec propellant<br>1.7261 in/sec fin propellant | 1011 psi                     | SFT to 90°F              | no    | 990 psi                               |
| ETM-3  | 3 x 24 chamfer, nominal geometry | MEOP<br>.3381 in/sec propellant<br>1.6057 in/sec fin propellant | 913 psi                      | SFT to 40°F              | no    | 2150 psi                              |
| ETM-3  | 3 x 24 chamfer, nominal geometry | MEOP<br>.3492 in/sec propellant<br>1.6581 in/sec fin propellant | 955 psi                      | SFT to 55°F              | no    | 1675 psi                              |

## FLUID MODELS

In the fluid-structural analysis shown in this report, FLUENT® version 5.6 is used as the flow solver. FLUENT® is a state-of-the-art CFD code written in the C programming language for modeling fluid flow and heat

transfer problems. FLUENT® has been used in a number of internal motor flow analyses. See Reference 2. The flow is assumed to be steady-state and 2D axisymmetric. The 3D fin regions near the headend of ETM-3 are taken into account by adjusting the burn rate coefficient such that the total propellant



surface area is modeled correctly. It was also assumed that the combustion gas is a single-phase, chemically frozen, calorically perfect gas. That is, the fluid is assumed to be a homogeneous mixture of gas and particles with an equivalent molecular weight while no combustion model is applied and no real gas effect is taken into account.

Both pressure-based and density-based solvers are available in FLUENT® although only the former is used in this work. While various turbulence models and near-wall treatments are implemented in FLUENT®, the two-equation RNG k-ε model with the standard wall function is applied. The constants in the RNG k-ε model used are  $C_{\mu}=0.06$ ,  $C_{\epsilon 1}=1.42$ , and  $C_{\epsilon 2}=1.68$  while the wall Prandtl number is 0.85. The turbulence viscosity ratio is limited to 10,000.

The propellant surface is modeled in FLUENT® by a mass inflow boundary condition with the mass flow rate being calculated as

$$\dot{m} = ap^n \rho_s A$$

where  $p$  is the static pressure,  $\rho_s$  is the density of the propellant and  $A$  is the surface area. The burn rate coefficient  $a$  and the exponential  $n$  depend on the formulation of the propellant. In this work, a burn rate exponential of 0.35 is used for RSRM whereas 0.32 is used for ETM-3. At the propellant boundaries, a turbulence intensity of 5% and a turbulent viscosity ratio of 100 are applied. A flame temperature of 3387 K is also specified. The inhibitor and nozzle walls are modeled by the adiabatic wall boundary condition while the nozzle exit plane is modeled as the pressure outlet boundary condition.

Figures 7 - 10 show the pressure and Mach number contours predicted from FLUENT® before coupling with ABAQUS® for both RSRM and ETM-3. The computational domain for the fluid is the whole motor including headend, slots and nozzle.

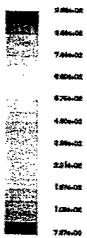
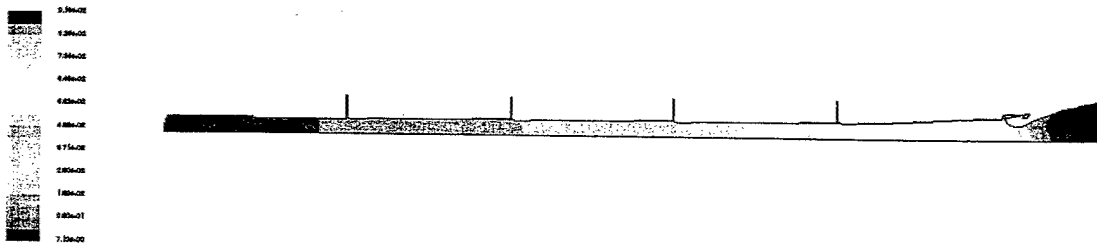


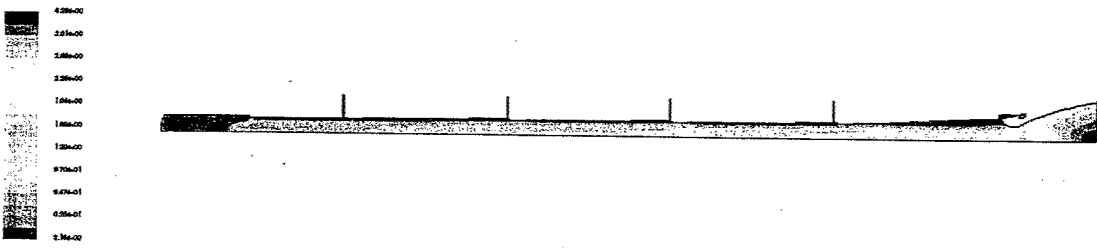
Figure 7: Pressure in RSRM.



Figure 8: Mach number for RSRM.



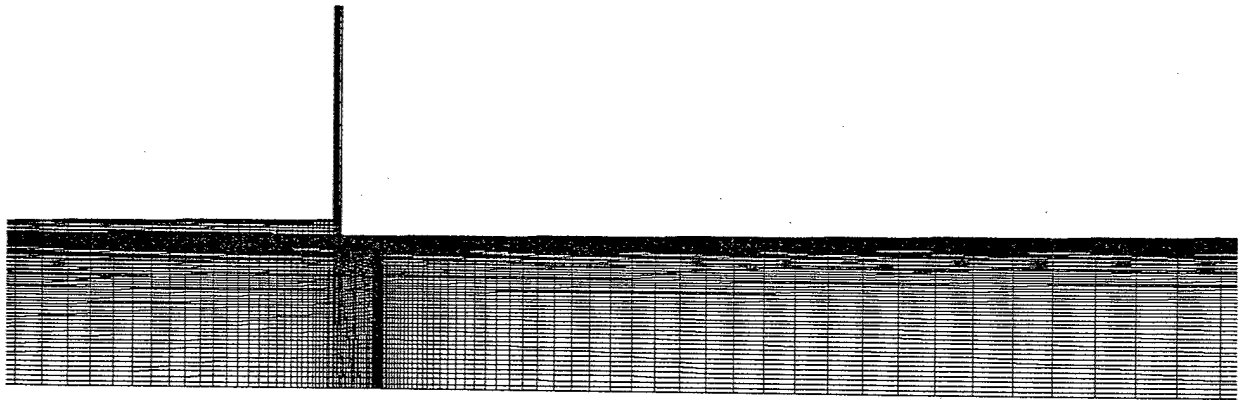
**Figure 9: Pressure for ETM-3.**



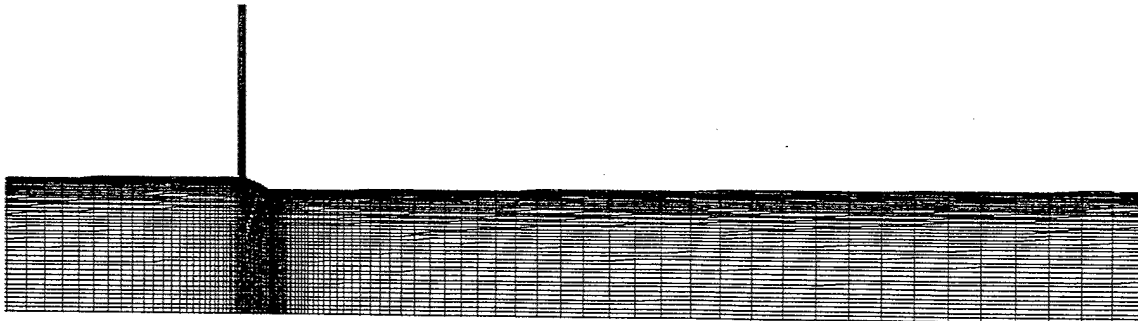
**Figure 10: Mach number for ETM-3.**

A close-up of the fluid models (portions) of ETM-3, with and without chamfers are shown in Figures 11 through 14. As

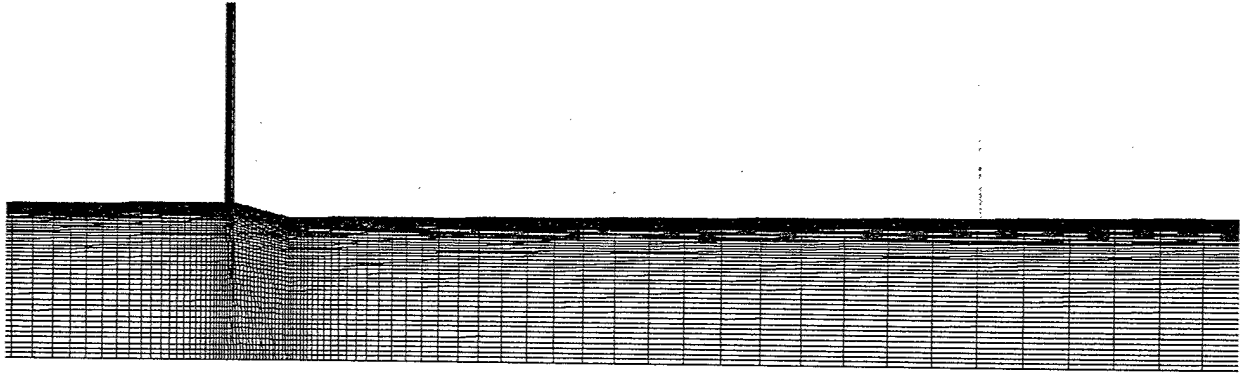
mentioned before, all segments of both motors were modeled, including the nozzles, even though only a portion is shown here.



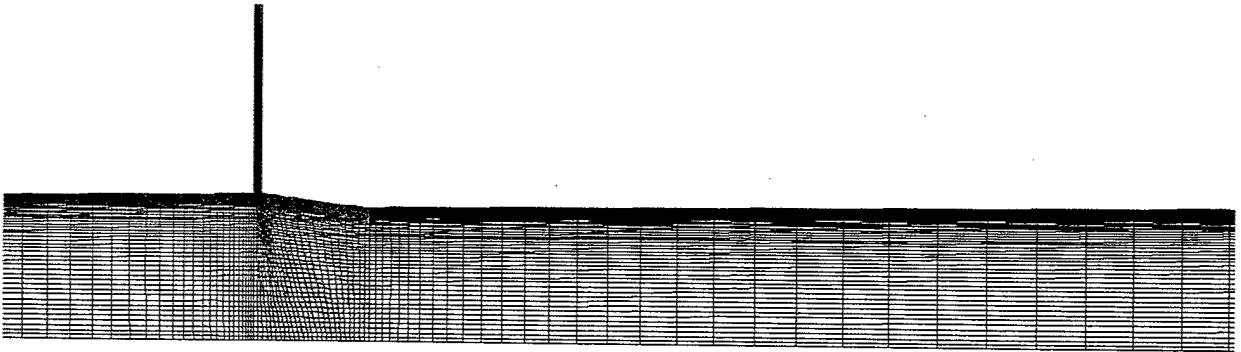
**Figure 11. Fluid Model of ETM-3, No Chamfers**



**Figure 12. Fluid Model of ETM-3, 3 x 6 Chamfers**



**Figure 13. Fluid Model of ETM-3, 3 x 12 Chamfers**



**Figure 14. Fluid Model of ETM-3, 3 x 24 Chamfers**

### **MECHANICAL PROPERTIES ASSESSMENT**

The FSI analyses of ETM-3 presented in the proceeding sections assumed that the propellant mechanical properties of TP-H1148 Type IV and TP-H1148 Type VII were identical. This assumption regarding the relaxation modulus was confirmed by the mechanical properties report for TP-H1148 Type VII, as documented in Reference 3.

Further study of the ignition modulus properties, shown in Table 2, of TP-H1148 Type IV were documented in Reference 1. This work was based on a number of studies, whose details were not covered here. Only the ignition modulus values from that report are presented in this document.

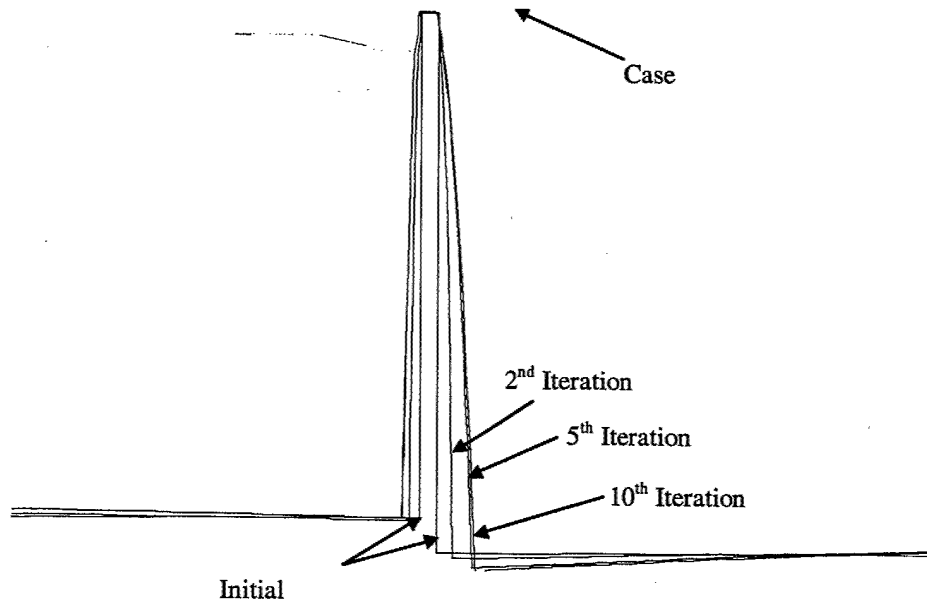
Additionally, high rate, bi-rate-and-hold testing on TP-H1148 was performed to verify the moduli and is documented in Reference 4. This testing confirmed that the ignition modulus values used were conservative.

**Table 2. Ignition Modulus Values from TR12874 (in psi)**

| T<br>°F | Modulus<br>.6 sec |
|---------|-------------------|
| 40      | 2150              |
| 50      | 1800              |
| 60      | 1550              |
| 70      | 1300              |
| 75      | 1200              |
| 80      | 1100              |
| 90      | 990               |

**RESULTS OF ANALYSES**

The resulting deformations of the propellant grain from each iteration between the fluid and structural models were scrutinized. From these observations, it was obvious that a particular slot (joint between segments) was of interest. (See Figure 6.) This is where the potential for boot-strapping existed. A few iterations at the critical slot for ETM-3 without chamfers are shown in Figure 15. These iterations showed that the slot widened and the leading edge corner of the grain moved radially inward.



**Figure 15. Sample Deformation Results at Critical Slot for ETM-3 Without Chamfers**

Numerous FSI analyses were conducted in the above manner while varying the propellant modulus of the structural model. Of course, the deformations at the critical slot (and all other locations) were effected by

the changing stiffness of the propellant. These many results were condensed into Figure 16 by only plotting the radial grain deformations at the critical slot of ETM-3, with and without chamfers, versus modulus.

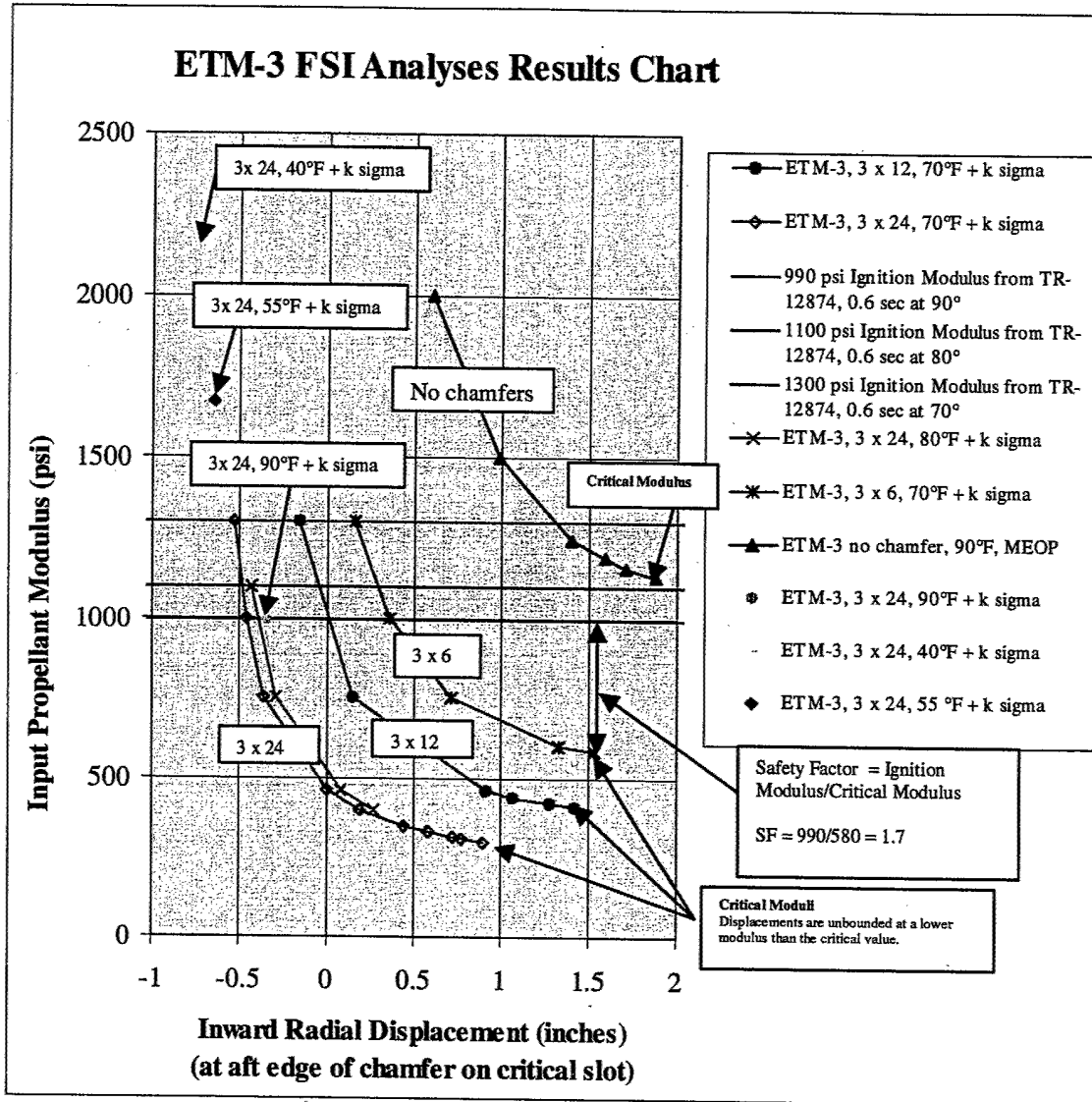
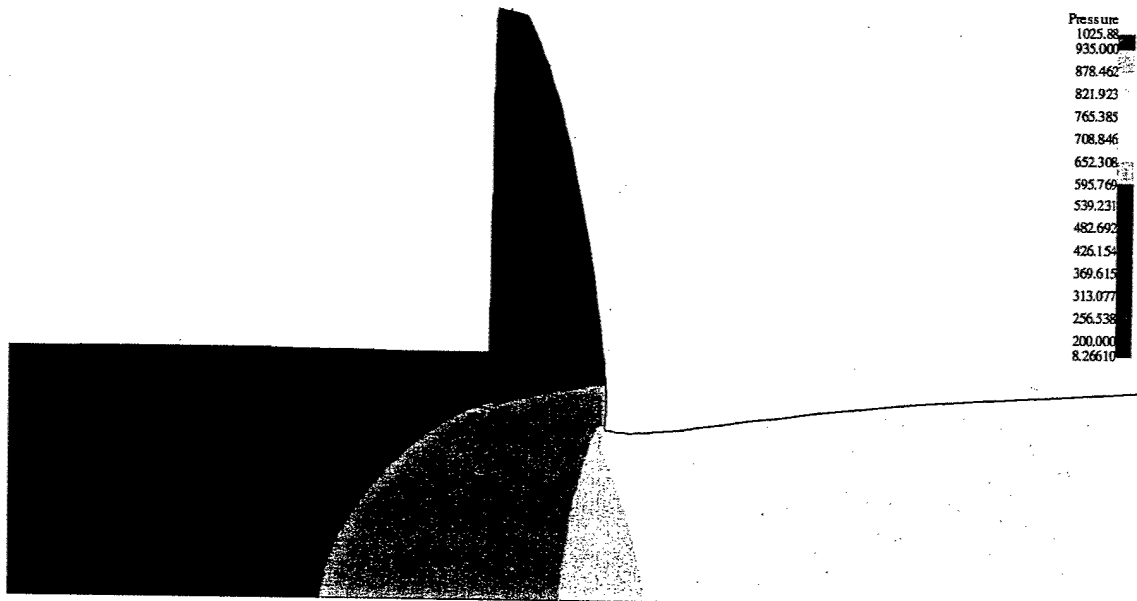


Figure 16. ETM-3 FSI Analyses Results

The critical modulus for each motor/burn rate condition was the propellant modulus at which the propellant grain at the critical slot would reach a stable position through multiple fluid/structural iterations at that modulus. Figure 16 shows that when a FSI analysis was run at a propellant modulus less

than the critical value, the grain displacements would be unbounded, meaning they would continue to increase and cause flow restriction and eventual bore choking in the motor. The effect on flow of this unbounded grain displacement is shown in Figure 17.

Pressure, Step=1, Inc=1  
Averaged



**Figure 17. Flow Restriction Due to Low Propellant Modulus**

The critical moduli were then used to calculate safety factors using the following formula.

$$SafetyFactor = \frac{IgnitionModulus}{CriticalModulus}$$

The safety factors for the 3 sizes of chamfers at 3 temperatures are summarized in Table 3.

**Table 3. Safety Factors Against Boot Strapping**

| Chamfer Size (inches)                        | Temperature (°F) | Ignition Modulus (TR-12874, psi) | Critical Modulus (psi) | Safety Factor (Ignition modulus/Critical modulus) |
|--|------------------|----------------------------------|------------------------|---|
| 3 x 6  | 70               | 1300                             | 570                    | 2.3   |
|  | 80               | 1100                             | 580                    | 1.9   |
|  | 90               | 990                              | 590                    | 1.7   |
| 3 x 12                                       | 70               | 1300                             | 410                    | 3.2   |
|  | 80               | 1100                             | 420                    | 2.6   |
|  | 90               | 990                              | 430                    | 2.3   |
| 3 x 24<br>(expected static test temperature) | 70               | 1300                             | 300                    | 4.3   |
|  | 80               | 1100                             | 310                    | 3.6   |
|  | 90               | 990                              | 320                    | 3.1   |

(Note: The critical moduli for some of the conditions were extrapolated based on the well behaved family of curves for the 3 x 24 chamfer at 70, 80, and 90°F.)

## DISCUSSION

The lowest safety factor against bore choking was 1.7 for a 3 x 6 chamfer at 90°F. The safety factor increased to 3.1 for a 3 x 24 chamfer at 90°F, which further increased to a 3.6 safety factor at 80°F. This represented the approximate expected static test temperature for ETM-3.

The family of curves for each chamfer size of varying modulus and radial displacement was well behaved and showed increasing safety factor with increasing chamfer size. This gave confidence that the analyses were providing consistent results, though not necessarily absolutely correct.

## CONCLUSIONS

It was concluded that 3 x 24 inch chamfers would be desirable because they gave the largest safety factors against boot-strapping. Also, without chamfers, ETM-3 would experience boot-strapping.

The critical propellant modulus for ETM-3, with 3 by 24 inch forward bore chamfers, at MEOP and 80°F was 310 psi. This compared with an expected propellant

ignition modulus of 990 psi, as documented in TR12874, ETM-3 Ignition Modulus for Fluid/Structural Interaction Analysis. Thus, no boot-strapping of the propellant grain will occur in ETM-3.

## REFERENCES

- <sup>1</sup> Wynn, R., "ETM-3 Ignition Modulus for Fluid/Structural Interaction Analysis," ATK Thiokol Propulsion, TR12874, Dec 2001.
- <sup>2</sup> Ahmad, R. A., R. A. Morstadt, and A. M. Eaton, "RSRM and ETM03 Internal Flow Simulations and Comparisons," AIAA-2003-5104, AIAA/ASME/SAE/ASEE 39<sup>th</sup> Joint Propulsion Conference, Huntsville, AL, July 20-23, 2003
- <sup>3</sup> Sorenson, K., "Final Test Report for ETP-1977, (ETM-3, TP-H1148 (Type VII) Propellant Standardization)," ATK Thiokol Propulsion, TWR-74361, April 2002
- <sup>4</sup> Larsen, D., "TP-H1148 Birate Relaxation Modulus," ATK Thiokol Propulsion, TR13196, to be published.