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THERMAL INTERACTIONS IN ROLLING BEARING DYNAMICS

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Table of Contents

	List of Figures List of Tables Foreword Preface	vi vii
1.	Introduction	1
1.		-
2.	Technical Approach to Thermal Modeling	4
2.1	Contact Heat Generation	
2.2	Θ	78
2.3 2.4		
2.4		-
2.6		10
2.7		
2.8	Numerical Implementation	16
2.9		
2.1	0 Overall Boundary Conditions and Model Implementation	21
		• •
3.1 3.2	Generalized Equilibrium Formulations	
3.2	Fatigue Life Model	21
4	Enhancements to Bearing Dynamics Code ADORE	36
4.1	Conversion to FORTRAN-90 Standard	36
4.2		
4.3		
4.4	Other Refinements	40
	Results	
5.1	Test Ball Bearing	
5.2		
5.3	U	
5.4		. 6/
5.5	Thermal Interactions Cylindrical Roller Bearing	08
6. (Conclusions	82
7. F	Recommendations for Future Development	. 83
8. F	References	84
		0.5
	Appendix A - Typical ADORE Data Module	86
	Appendix B - Typical ADORE Code Segment	90
	Appendix C - Ball Bearing Data	102
	Appendix D - Cymurical Koller Bearing Data	109

List of Figures

1.	Schematic of heat flow from rolling element/race contact to the	
-	external system	4
2.	Ball/Race contact schematic	5
3.	Typical slip velocity distribution along the major axis of a ball/race	
	contact	7
4.	Schematic of a cylindrical body	8
5.	Rolling element solid model for heat conduction	9
6.	Contact zone schematic	14
7.	Basic coordinates in the contact zone	15
8.	Grid point schematic for a linear function	17
9.	Comparison of temperature distribution resulting from elliptical and	
	unform heat fluxes	21
10.	Schematic of ball and race relative position	23
11.	Schematic outline of code elements of ADORE	37
12.	Schematic architecture of the thermal module in ADORE	38
13.	Integration of thermal interaction module ADRH with other modules	
	in the bearing dynamics computer code ADORE	39
14.	Ball/Race load distribution at the outer race contact with aligned and	• •
	misligned condition resulting from moment equilibrium	47
15.	Ball/Race load distribution at the inner race contact with aligned and	• •
101	misligned condition resulting from moment equilibrium	48
16.	Overall powerloss in the test ball bearing with no thermal interactions	50
17.	Time-averaged wear rates in the test ball bearing with no thermal	50
17.	interactions	51
18.	Computed bulk temperatures with no change in bearing geometry	52
10. 19.	Typical ball/race interaction with no change in internal geometry	53
20.	Ball bearing cage mass center velocities in absence of any thermal	55
20.	interactions	54
21.	Ball bearing cage/race contacts in absence of any thermal interactions	55
21.	Ball bearing cage mass center whirl orbits in absence of any thermal	55
<i>LL</i> .		56
23.	Typical ball/cage contacts in absence of any thermal interactions	57
23. 24.	Ball bearing poer loss with time-varying bearing geometry due to	57
<i>2</i> 4 .		59
25.	Time-averaged wear rates for the ball bearing with geometrical	39
23.		60
26	distortions due to thermal effects	60
26.	Computed bulk tempeeratues in the ball bearing with thermal effects	61
27.	Typical ball/race interactions with thermal effects	62
28.	Ball bearing cage mass center velocities with changing bearing	<i>c</i> 2
20	geometry as a result of thermal effects	63
29.	Ball bearing cage/race contacts with thermal effects	64
30.	Ball bearing cage mass center whirl orbits with thermal effects	65
31.	Typical ball/cage interactions with applied thermal effects	66
32.	Traction-Slip relation for the test roller bearing	68

List of Figures .. continued

Figure

33.	Roller bearing powerloss with no thermal effects	69
34.	Computed bulk temperatures in the roller bearing with no thermal effects	70
35.	Typical roller/race interactions with no thermal effects	71
36.	Roller bearing cage mass center velocities with no thermal effects	73
37.	Cage/race contacts in the roller bearing with no thaermal effects	74
38.	Roller bearing cage whirl orbits with no thermal effects	75
39.	Roller bearing powerloss with all thermal effects	76
40.	Computed roller bearing bulk temperatures with changing bearing	
	geometry as a rsult of thermal effects	77
41.	Typical roller/race contacts in the cylindrical roller bearing with	
	changing bearing geometry due to thermal effects	78
42.	Change in cage mass center velocities in the roller bearing with	
	changing bearing geometry as a result of thermal effects	79
43.	Increased cage/race forces in the roller bearing with thermal effects	80
44.	Cage mass center whirl in the roller bearing with thermal effects	81

List of Tables

Table		Page
1. 2. 3. 4. 5. 6.	Coefficients of Heat Transfer Coefficients for Cylinders in Air Physical Properties of Air Material Matrix Susceptibility Multiplier Steel Processing Multiplier Ball Bearing Geometry and Operating Conditions Cylindrical Roller Bearing Geometry and Operating Conditions	13 29 31 46
3. 4. 5.	Material Matrix Susceptibility Multiplier Steel Processing Multiplier Ball Bearing Geometry and Operating Conditions	

Foreword

The work reported herein was carried out under the Small Business Innovation Research (SBIR) Phase II program. In addition to SBIR, the project development was supported by the Air Force Propulsion Laboratory and NASA Marshall Space Flight Center. The related SBIR Phase I project was carried out under Air Force Contract F33615-95-C-2528. Principal project engineers were Dr. Jeff Brown of the Air Force Propulsion Laboratory and Mr. Howard Gibson of NASA Marshall Space Flight Center.

Preface

Procedures for modeling thermal interactions and implementation of the models in rolling bearing dynamics computer code constitute the principal objectives of the current program. The well established bearing dynamics computer code ADORE (Advanced Dynamics Of Rolling Elements) is taken as the baseline model. Numerical enhancements are carried out for improved computation of bearing heat generation and geometrical variations in the dimensions of bearing elements. With the computed internal heat generation thermal interaction models based on conduction through the bearing elements and convection through the circulating fluid or lubricants are developed. The output from these models is a detailed temperature field throughout the bearing. Certain averaging procedures are then implemented to compute bulk temperature of the various bearing elements. Well established procedures are then implemented to compute change in bearing geometry as a function of temperatures. All mechanical interactions in the bearing are then modified as a function of new geometry. All thermal interactions are free of any transients while the mechanical interactions are controlled by the classical differential equations of motion of the bearing elements. Thus the thermal interactions are implemented in a stepwise averaged manner; for a selected time domain the thermal interactions are averaged before computing the temperature fields and the associated geometrical distortions. Such a stepwise implementation of thermal interactions, although results in a step change in bearing performance parameters, the numerical integration is free of any truncation problems when an explicit algorithm is used, and the integration is inherently convergent. Parametric dynamic simulations based on such modeling procedures show numerically convergent temperature fields as the bearing performance simulations approach steady-state. Thus the model is numerically sound and convergent.

1. Introduction

Rolling element bearings, due to their high load support and stiffness characteristics, serve as the main support bearings in a wide range of practical applications. As the operating conditions become severe in terms of the applied loads and speeds the bearing behavior gets increasingly complex, not just due to the applied external conditions, but the internal interactions and heat generation between the interacting bearing element. It has been well established that frictional interactions and lubrication mechanics are the most critical factors which determine the performance of a rolling bearing. While the friction forces directly contribute to the bearing element motion, the frictional heat generated at the contacts leads to substantial temperature rise of the interacting surfaces, which may appreciably alter the lubricant behavior and therefore, the resulting friction or traction forces. Thus the frictional and thermal phenomena are very closely linked in producing dynamic instabilities in rolling bearings. In addition, the bulk temperature rise of the bearing elements results in a change in the geometrical parameters, such as bearing element size and internal clearance distributions, which again contribute to altered geometrical interaction between the bearing elements, and overall bearing motion. Modeling of thermal interactions in rolling bearings, therefore, has a substantial practical significance.

While the intricate relationship between temperature and traction behavior of liquid lubricants is quite well known, the requirement for higher operating temperatures has recently led to significant interest in the development of high temperature materials and solid lubricants. Since the friction forces are generally higher in a dry contact environment, when compared to liquid lubricated conditions, thermal interactions have increased practical significance for solid lubricated contacts. In fact, the high temperatures, in addition to changing the solid lubricant behavior, often affect bulk properties of the bearing materials. Thus modeling of thermal interaction becomes significant for both bearing behavior and materials development.

The recent development of ceramic bearings has shown that although these advanced materials render acceptable performance at high temperatures, improved modeling of the thermal problem and prediction of temperature distribution is extremely essential in resolving several practical bearing design problems. First, solution to mounting problems resulting from the difference in the thermal coefficient of expansion between ceramics and some of the mating steel parts, require accurate assessment of the temperature fields. Second, and more important, is the fact that the contact temperature, which may be significantly higher than the bulk temperature, greatly affects the chemical phenomena which controls traction behavior of the lubricant. In the case of liquid lubricants, the exponential viscosity-pressure-temperature relations and the shear stress and strain rate behavior have led to the development of acceptable traction models for practical design. In solid lubricants, however, the traction behavior demonstrates certain transitions as a function of temperature. In other words the traction behavior may be subjected to a drastic change as the operating temperature crosses a certain threshold. Such a behavior may trigger instabilities in motion of the bearing elements which may lead to a sudden and very often a catastrophic failure. Precise estimates of internal bearing temperatures and the overall thermal management of the bearing system, therefore, have increased importance in solid lubricated bearings.

While traction behavior of a lubricant depends on the operating temperature, the bearing heat generation is dependent on the traction coefficients, contact loads and operating speeds. Aside from the external applied loads, the internal load distribution in the bearing depends on the operating internal clearance, which in turn is a function of temperature. The variations in internal clearance with temperature are particularly significant in hybrid ceramic bearings due to a significant difference in the thermal coefficient of expansion of the interacting materials. Due to such closely connected frictional and geometrical effects, a realistic modeling of bearing performance requires a solution to the coupled mechanical and thermal interactions between the bearing elements.

In addition to the overall motion of bearing elements and the associated instabilities, the modeling of thermal interactions is very critical in bearings where a thin coating of a certain material is applied to the bearing surfaces to enhance the tribological behavior. Here the contact temperature not only determines the resulting friction or traction coefficients, but also the bond between coating and substrate, since the thermal coefficient of expansion for the two materials may be quite different. To further complicate the problem the contact stresses, which affect the traction forces and bearing heat generation, are also dependent of the coating thickness and the temperature distribution in the composite solid. The problem becomes even more complicated when more than one coating are applied on the interacting surfaces.

Based on the above discussion, practical significance of thermal interactions in rolling bearings may be established on three grounds: (1) mechanical behavior of the materials and structural integrity of fabricated parts, (2) the effect of temperature on traction or friction coefficients at the mating surfaces, and (3) changes in bearing internal geometry due to temperature rise. While the significance of structural integrity is quite obvious, the importance of frictional behavior and changes in bearing internal geometry can be understood in terms of bearing instabilities triggered by internal friction, and the associated thermal effects. A number of investigations [1-5] have shown a strong relationship between bearing failures and instabilities in bearing elements, particularly the cage, triggered by frictional interactions. From a practical standpoint, cage instabilities have several modes [4]: (1) the irregular whirl may cause an erratic variation in bearing torque, (2) the whirl velocities may go through irregular variations to produce bearing squeal, or (3) geometric interactions of the cage may progressively increase with time to produce excessive cage forces and wear. While the first two modes are of interest in precision gyro bearings, the third mode, which often leads to a catastrophic bearing failure, is most important in turbine engine bearings. With a comprehensive model for all thermal and mechanical interactions, parametric modeling studies may reveal an acceptable range of traction parameters, and therefore, a range of thermal environment, over which the motion is stable. Such a study, aside from practical design, provides significant guidance for materials development and selection for a given application.

The thermal effects have an intricate coupling with the geometrical interactions, which affect the applied loads, which in turn control the heat generation and thereby result in a feed back to the thermal problem. Due to such a connection between the thermal, geometrical and mechanical effects, realistic simulation of bearing performance requires a close integration of the thermal models with geometrical interaction and resulting applied loadings. Modeling of all thermal interactions in the bearings and an integration of the thermal models with the models for geometrical interactions is the primary objective of this development project. The existing bearing dynamics

computer code, ADORE [3], is used as a baseline, and the code is enhanced by incorporating the thermal interactions models developed as a part of the current effort.

In addition to incorporation of the thermal interactions, other enhancements to ADORE, include, renewed code structure conforming to the FORTRAN-90 standard, refinement of ball bearing equilibrium module to include moment equilibrium, and enhancements of the fatigue life computations to include the recently developed models for life corrections as a function of the advanced materials behavior and applied operating conditions. Presentation of technical accomplishments during this project are, therefore, divided into several sections. The next section outlines the thermal modeling effort while section 3 is devoted to the moment equilibrium and life enhancement models. ADORE enhancements are reported in section 4, which is followed by some parametric runs with the final version of ADORE.

2. Technical Approach To Thermal Modeling

The main source of heat generation in a rolling bearing is the rolling element to race contact, where for a given set of operating conditions and a prescribed lubricant, local sliding in the contact produces frictional heat. Transfer of this heat to the external environment through the bearing constitutes the basic foundation of the thermal modeling task. Schematically the heat generated in the contact may be partitioned such that part of it goes to the races and part of it goes to the rolling element. The heat going to the races travels via conduction to the external system, while the heat going to the rolling elements is transferred to the circulating lubricant or any other coolant. Thus the lubricant, in addition to providing favorable traction characteristics at the rolling element to race contacts, serves as a coolant. The interactions are shematically described in figure 1 below.



Figure 1. Schematic of heat flow from rolling element/race contact to the external system.

Formulation of thermal interactions, thus consists of the following parts:

- Contact heat generation
- Heat partition between rolling element and race
- Conduction through the races
- Conduction through the rolling element
- Convection to the coolant
- Local temperature rise in the contact

A discussion of the approach used to model each of the above is presented below.

2.1 Contact Heat Generation

Model of computing contact heat generation is quite straightforward. First from the relative position of rolling element and race the normal contact load and size of contact zone are computed. Then for each point in the contact zone the sliding velocity with prescribed rolling element and race velocities is computed. Then using a prescribed traction model, or a traction slip relation, the traction coefficient is computed, which when multiplied by the normal contact load, gives the traction force. Finally, an integration of the product of traction force and sliding velocity over the contact zone gives the total heat generated in the contact.

Figure 2 shows schematically an elliptical contact corresponding to ball/race interaction. Depending on the type of traction model, either variation in traction from point to point in the contact may be permitted, or the variation along the minor axis may be neglected and integration may be performed only along the major axis of the contact ellipse.



Figure 2. Ball/Race contact schematic.

The shear stress, τ , depends on both normal stress σ and the sliding velocity *u* for a given traction model. The expressions for one and two dimensional variation may be written as:

$$\tau(x) = \sigma(x)\kappa[u(x)] \tag{1}$$

$$\tau(x, y) = \sigma(x, y)\kappa[u(x, y)]$$
⁽²⁾

Here κ is the traction coefficient, which may be a function of both the sliding velocity and load. For elastohydrodynamic models, the relationship may be quite complex in the sense that variation of lubricant temperatures with pressure and temperature, and variation of lubricant film thickness with load and rolling speed also enter in the model.

In equation (1) corresponding to a one dimensional variation, the sliding velocity is computed only a the point on major axis, while the load is an integrated value over the incremental strip. Also, in this case, only the sliding velocity component along the rolling direction (y) enter in the calculation. In the two dimensional case the direction of slip may be determined by the actual sliding velocity vector which is defined by the cross product of the angular velocity and the position vector locating the contact point in the contact zone. Thus if **r** and **R** respectively locate the contact point relative to the rolling element and race centers, and ω and Ω are the angular velocity vectors of the rolling element and race, and $\dot{\phi}$ is the orbital velocity of the rolling element, then the sliding velocity *u* at any point in the contact zone is written as:

$$\mathbf{u} = \boldsymbol{\omega} \times \mathbf{r} - (\boldsymbol{\Omega} - \dot{\boldsymbol{\varphi}}) \times \mathbf{R} \tag{3}$$

Note that the race angular velocity vector normally has only one component as does the rolling element orbital velocity.

Using equation (3) a component of the slip velocity in plane of contact may be determined and then input the traction model to obtain a traction coefficient, which along with the slip velocity may depend on other performance parameters as well.

The total heat generation in the contact, \bar{q} , in the contact is now simply an integration of equation (1) or equation (2) depending on one or two dimensional variation.

$$\bar{q} = \int \langle \int \sigma(x, y) dy \rangle \kappa[u(x)] dx \tag{4}$$

or

$$\bar{q} = \iint \sigma(x, y) \kappa[u(x, y)](dx) dy$$
(5)

Implementation of the above equation in the bearing dynamics codes is done numerically since both the traction model and the slip distribution may be rather complicated functions of the position coordinates. Equation (5) is implemented by using numerical quadrature similar to the classical Chebyshev integration procedures [6], while the conventional Gaussian quadrature formulae [7] may be used in implementing equation (4). However, when the slip velocities are computed along the major axis of the contact ellipse, there may be discontinuities at the points of pure rolling, as shown in figure 3. Under such conditions, direct application of the Gaussian quadrature formula over the entire contact length may provide accurate results. Thus the computed in the range of contact limits. The roots define the pure rolling points, as shown in figure 3. The contact zone is now divided into subzones by using the pure rolling points as the terminal points for the zone; the slip distribution shown in figure 3 has three zones as shown. The Gaussian quadrature formula is now applied in each zone and the total integral value is obtained by summation. Such an implementation is found to provide fairly accurate results.



Figure 3. Typical slip velocity distribution along the major axis of a ball/race contact.

2.2 Heat Partition at Rolling Element to Race Contact

In concentrated rolling/sliding contacts, the rolling speed normally pumps the lubricant in the contact and a lubricating film is formed. When sliding is imposed, the film is sheared to produce a traction force and the frictional energy is dissipated as heat. A part of this heat may be carried, via convection, by the circulating lubricant, and the remainder may be transferred from the film to the mating surfaces via conduction. For most machine elements, Trachman and Cheng [8] have shown that the convective part is quite small and it can be reasonably neglected. Thus if the total heat flux at the contact is q and it is partitioned into two parts, q_1 and q_2 , which are transferred to the rolling element and race:

$$q_1 = \gamma q \tag{6}$$

and

$$q_2 = (1 - \gamma)q \tag{7}$$

If the two surfaces are separated by a film with thickness, h, and they are at temperatures T_1 and T_2 , then there should be an additional conduction term:

$$q_{1} = \frac{k_{f}}{h}(T_{2} - T_{1}) + \gamma q$$
(8)

and

$$q_2 = \frac{k_f}{h} (T_1 - T_2) + (1 - \gamma)q$$
(9)

Here k_f is the thermal conductivity of the film and γ is the heat partition fraction. The value of this heat partition fraction will depend on the thermal properties of the two interacting bodies. The actual value will be an outcome of the contact temperature computation discussed later in section 2.6.

2.3 Conduction Through the Races

Conduction through the races, housing and a hollow shaft, can be all be modeled by classical text book approach [9-11]. Consider a cylindrical element of length L, outer and inner radii of r_1 and r_2 at temperatures T_1 and T_2 respectively, as shown in figure 4.



Figure 4. Schematic of a cylindrical body.

The heat flow, q, through an elementary section, as shown in figure 4, is simply

$$q = -kA\frac{dT}{dr} \tag{10}$$

Where k is the thermal conductivity and the area of the incremental section, $A = 2\pi rL$, L being length of the cylindrical element.

The temperature distribution along the radius is obtained by simple integration of equation (10):

$$T = T_2 - \frac{q}{2\pi Lk} \ln \frac{r}{r_2} \tag{11}$$

The bulk temperature of the cylindrical element may be approximated by an average temperature, T_{av} , which is obtained by integrating equation (11) with respect to the radius r.

$$T_{av} = T_2 - \frac{q}{2\pi Lk} \left[\frac{r_1 \ln \frac{r_1}{r_2}}{r_1 - r_2} - 1 \right]$$
(12)

The above formulation may also be applied to an angular sector of the cylinder, with an arc length, θ , by simply replacing the term, 2π by the angle, θ . This becomes useful when conduction through the race is carried out at each rolling element location, where the race surface temperature may be different due to variation in contact load, slip velocity and traction characteristics.

2.4 Conduction Through the Rolling Element

Temperature distribution in the rolling element can be very complicated. With the prescribed heat input at the race contacts and certain boundary conditions, the two or three dimensional partial differential equation may certainly be solved with either finite difference or finite element techniques. However, implementation of such a procedure in the bearing dynamics code will be practically impossible due to constraints on the required computing effort for solving the differential equation of motion of the bearing elements. Thus for the present investigation the rolling is modeled by a cylindrical core with a length equal to the rolling element diameter, and cross sectional area determined such that the total volume of this core is equal to the rolling element. Schematic of the model is shown in figure 5. Thus the equivalent cross sectional will be the rolling element volume divided by its diameter:



Figure 5. Rolling element solid model for heat conduction.

$$A = \frac{1}{6}\pi D^2 \text{ for ball bearings}$$
(13)

and

$$A = \frac{1}{4}\pi DL \text{ for roller bearings.}$$
(14)

The conduction equations are simply

$$q_1 = k(T_1 - T_0)\frac{A}{D}$$
(15)

and

$$q_2 = k(T_2 - T_0)\frac{A}{D}$$
(16)

Here T_1 and T_2 are the contact temperatures and T_o is the mid point temperature. Normally the heat inputs at the outer and inner race contacts (q_1, q_2) are given. So with the temperature known at either the inner or outer race contact, the other temperature and the temperature at mid point can be computed by simultaneous solution of equations (15) and (16).

The average temperature is simply computed by the shaded area under the linear temperature distribution shown in figure 5.

$$T_{av} = \frac{T_o}{2} + \frac{T_1 + T_2}{4} \tag{17}$$

2.5 Conduction Through the Cage

Model for conduction through the cage is identical to that discusses above for the races. The cage is modeled as a cylindrical element and the heat is assumed to conduct radially away from the surface being guided on the race. Heat generated at the cage/race land and all pockets constitutes the total heat flux. Base temperature of the cage is set at the average ambient temperature in the vicinity of the rolling elements. More rigorous temperature distribution in the cage is excluded from the present model. Such an analysis may be best carried out by a finite element model where the heat generation values, as computed in ADORE, may be input to model detailed temperature distribution in the vicinity of all cage contacts.

2.6 Convection Through the Coolant

Convective heat transfer is generally expressed in terms of three dimensionless groups [10, pp 265-268], [11, pp 410-415], [12, pp 200-202]

Reynolds Number:
$$Re = \frac{V_{\infty}\rho_{\infty}D}{\mu_f}$$
 (18)

Nusselt Number:
$$Nu = \frac{hD}{k_f}$$
 (19)

Prandtl Number:
$$\frac{c_p \mu_f}{k_f}$$
 (20)

Here V_{∞} , ρ_{∞} , μ_f , k_f , c_p , D and h are respectively the characteristic fluid velocity, density, viscosity, thermal conductivity, specific heat, characteristic length of the solid and the heat transfer coefficient. Normally the relationship for heat transfer coefficients are expressed in terms of empirical algebraic equations containing the above three group.

Pertinent to rolling bearings the solids of interest are spheres and cylinders, and the fluids of interest are air and liquids. Air may be used for solid lubricated bearings while the formulae for liquids are used for oil lubricated bearings. The formulae used in the current model are presented below.

2.6.1 Spheres in Air

The common equations for spheres in air are:

$$Nu = 0.37 R e^{0.60}, \, 25 \le Re \le 100, \, 000 \tag{21}$$

and

$$Nu = RePr\left(\frac{2.2}{Re} + \frac{0.480}{Re^{0.50}}\right), \ 1 \le Re \le 25$$
(22)

2.6.2 Spheres in Liquids

For spheres in liquids the following relation may be used for all Reynolds numbers:

$$Nu = Pr^{0.30}[0.97 + 0.68Re^{0.50}]$$
⁽²³⁾

In the limiting case, with Re < 1, and Pr = 1, the Nusselt number approaches a value of 2.

2.6.3 Cylinders in Air

For cylinders in air, the polynomial relationship between the Nusselt and Reynold numbers has a larger variation as a function of the Reynolds number. The suggested expression is:

$$Nu = CRe^n \tag{24}$$

Where constants C and n are tabulated below, in Table 1, as a function of the Reynolds number.

Re	С	n
0.40 - 4	0.891	0.330
4 - 40	0.821	0.385
40 - 4,000	0.615	0.466
4,000 - 40,000	0.174	0.618
40,000 - 400,000	0.0239	0.805

Table 1: Coefficients of Heat Transfer Coefficients for Cylinders in Air

2.6.4 Cylinders in Liquids

Similar to spheres in liquids, one expression may be used for all Reynolds numbers for cylinders in liquids:

$$Nu = [0.35 + 0.56Re^{0.50}]Pr^{0.31}$$
⁽²⁵⁾

An equation similar to that described above for air has also been suggested for cylinders in liquids:

$$Nu = 1.1CRe^{n}Pr^{0.31}$$
(26)

Here the constants C and n are same as those listed in table 1 for air. However, in the present investigation equation (25) is used for cylinders in liquids.

2.6.5 Properties of Air

Required properties of air for applying the above models for convective heat transfer in air are documented below.

Density at atmospheric pressure is expressed as a function of temperature $T(^{o}K)$ as [13]:

$$\rho = \frac{353}{T} \text{ kg/m}^3 \tag{27}$$

Other required properties are extracted from ref [10, pp 483], converted to current SI units, and are tabulated below in Table 2:

	I		
Temperature	Specific Heat	Viscosity	Thermal Conductivity
(^{<i>o</i>} <i>K</i>)	$\left(\frac{Nm}{kg^{o}K}\right)$	$\left(\frac{Ns}{m^2}\right)$	$\left(\frac{N}{s^{o}K}\right)$
88.88	1.0019409E+03	6.3274590E-06	8.2733628E-03
144.44	1.0019409E+03	1.0008138E-05	1.3206225E-02
200	1.0019409E+03	1.3316613E-05	1.8000622E-02
227.77	1.0023596E+03	1.4888138E-05	2.0423783E-02
273.33	1.0031970E+03	1.7245428E-05	2.4231607E-02
311.11	1.0052905E+03	1.9023733E-05	2.7174014E-02
366.66	1.0098962E+03	2.1546445E-05	3.1328006E-02
422.22	1.0136644E+03	2.3903733E-05	3.5308913E-02
477.77	1.0241318E+03	2.6054243E-05	3.8943654E-02
533.33	1.0358553E+03	2.8080685E-05	4.2578392E-02
588.88	1.0484163E+03	3.0024413E-05	4.6040051E-02
644.44	1.0613959E+03	3.1844074E-05	4.9328627E-02
700	1.0743754E+03	3.3622379E-05	5.2444120E-02
755.55	1.0877737E+03	3.5317973E-05	5.5386531E-02
811.11	1.1011721E+03	3.6889498E-05	5.8328938E-02
922.22	1.1250377E+03	3.9991194E-05	6.3867588E-02

Table 2: Physical Properties of Air

2.7 Contact Temperature Modeling

A model for estimate of contact temperature rise for a given heat generation was developed in the first phase of this project [14]. The model is based on the classical flash temperature theory of moving heat sources, as documented by Jaeger [9]. The modeling procedure is reviewed here for completeness.

As shown in figure 6, let the generalized elliptical contact zone between the rolling element and race be divided into incremental strips. The temperature distribution, T(y), along the rolling direction (y), on the incremental strip is given by the equation

$$T(y) = T_{0} + \frac{1}{\sqrt{\pi\rho c k U}} \int_{-b}^{y} \frac{q(y)}{\sqrt{y - \xi}} d\xi$$
(28)

where T_o is a reference temperature and ρ , c, k, U are respectively the density, heat capacity, thermal conductivity, and rolling velocity. The heat flux q(y) for a given pressure distribution p(y), traction coefficient κ , and sliding velocity u_s , is simply written as

$$q(y) = \kappa u_s p(y) \tag{29}$$



Figure 6. Contact zone schematic.

In accordance to the basic equations, (8) and (9) presented earlier, if the two surfaces are separated by a lubricant film of thickness, h, and the heat generated in the contacts is partitioned into the two surfaces by fractions γ and $(1 - \gamma)$, then the heat fluxes going into surfaces 1 and 2 at any coordinate position, y, as shown schematically in figure 7 are given by

$$q_{1}(y) = \frac{k_{f}}{h}(T_{2} - T_{1}) + \gamma q(y)$$
(30)

$$q_2(y) = \frac{k_f}{h}(T_1 - T_2) + (1 - \gamma)q(y)$$
(31)

where k_f is the thermal conductivity of the fluid, or lubricant. The corresponding temperature distributions on the two surfaces, denoted by subscripts 1 and 2, may be written as

$$T_{1}(y) = T_{0} + \frac{1}{\sqrt{\pi\rho_{1}c_{1}k_{1}U_{1}}} \int_{-b}^{y} \frac{q_{1}(y)}{\sqrt{y-\xi}} d\xi$$
(32)

$$T_{2}(y) = T_{0} + \frac{1}{\sqrt{\pi\rho_{2}c_{2}k_{2}U_{2}}} \int_{-b}^{y} \frac{q_{2}(y)}{\sqrt{y-\xi}} d\xi$$
(33)



Figure 7. Basic coordinates in the contact zone.

When the two surfaces are assumed to be equal temperatures, the conduction term in equations (30) and (31) vanishes, and the heat partition fraction reduces to

$$\alpha = \frac{1}{\sqrt{\pi \rho_1 c_1 k_1 U_1} + \sqrt{\pi \rho_2 c_2 k_2 U_2}}$$
(34)

The expression for temperature rise, $\Delta T(y) = T(y) - T_o$, in the contact along the rolling direction thereby reduces to

$$\Delta T(y) = \frac{1}{\sqrt{\pi \rho_1 c_1 k_1 U_1} + \sqrt{\pi \rho_2 c_2 k_2 U_2}} \int_{-b}^{y} \frac{q(y)}{\sqrt{y - \xi}} d\xi$$
(35)

The above equation gives the local temperature rise over an incremental strip in the contact along the rolling direction. For computation of average temperature this equation may be integrated over the contact area

$$T_{ave} - T_o = \frac{1}{\pi ab} \int_{-a}^{a} \int_{-b}^{b} \Delta T(y) dy dx$$
(36)

where *a* is the contact half width in the direction normal to rolling.

2.8 Numerical Implementation

Although the implementation of the above equations, when the two surfaces are at equal temperatures, is rather straightforward, a generalized numerical procedure is presented below and the equal temperature case is discussed later as a special case. Thus a close examination of the general equations (28) to (31) reveals a recursive relationship for the computation of the required temperature distribution. For the purpose of developing such a relationship and the associated numerical procedure, it is convenient to introduce the following dimensionless variations

$$T' = \frac{T}{T_o}, \tau' = \frac{\tau}{\tau_o}, y' = \frac{y}{b}, \xi' = \frac{\xi}{b}, u' = \frac{u}{U} = \frac{|U_2 - U_1|}{U}, q' = \frac{q}{\tau_o U}, A = \frac{k_f}{h} \frac{\sqrt{b}}{\sqrt{\pi \rho c k U}},$$

and $B = \frac{\tau_o U \sqrt{b}}{T_o \sqrt{\pi \rho c k U}}$

In terms of the above variables, equations (28) to (31) may be combined to yield:

$$T_{1}(y) = 1 + A_{1} \int_{-1}^{y} \left\{ \{T_{2}(\xi) - T_{1}(\xi)\} \frac{d\xi}{\sqrt{y - \xi}} \right\} + B_{1} \int_{-1}^{y} \frac{\gamma q(\xi)}{\sqrt{y - \xi}} d\xi$$
(37)

and

$$T_{2}(y) = 1 + A_{2} \int_{-1}^{y} \left\{ \{T_{1}(\xi) - T_{2}(\xi)\} \frac{d\xi}{\sqrt{y - \xi}} \right\} + B_{2} \int_{-1}^{y} \frac{(1 - \gamma)q(\xi)}{\sqrt{y - \xi}} d\xi$$
(38)

where the subscripts $_1$ and $_2$ on the constants *A* and *B* represent the corresponding properties of the two surfaces. Also, the superscript, prime ('), has been dropped for brevity.

Note that although the required temperatures T1 and T2 appear on both side of the equations, the integrating limits are such that no values of temperatures for coordinates $\xi > y$ are required. Therefore, a recurrence type of relation can be developed by expressing these equations in discrete form. In order to develop the numerical form of such a relation, it will be convenient to develop certain quadrature, which can be readily used to evaluate the integral expressions. Consider a function $f(\xi)$ to be linear between the grid points *j*-1 and *j* corresponding to coordinates ξ_{j-1} and ξ_j , as shown shematically in figure 8. In other words:

$$f(\xi) = f_{j-1} + \frac{f_j - f_{j-1}}{\xi_j - \xi_{j-1}} (\xi - \xi_{j-1})$$
(39)



Figure 8. Grid point schematic for a linear function.

Using the above linearized form of a function, two quadrature, *I* and *J* may be expressed to define the integrals:

$$I_{j}^{i} = \int_{\xi_{j-1}}^{\xi_{j}} \frac{d\xi}{\sqrt{\xi_{i} - \xi}} = 2\left[\sqrt{\xi_{i} - \xi_{j-1}} - \sqrt{\xi_{i} - \xi_{j}}\right]$$
(40)

and

$$J_{j}^{i} = \int_{\xi_{j-1}}^{\xi_{j}} \frac{\xi d\xi}{\sqrt{\xi_{i} - \xi}} = \frac{2}{3} [(2\xi_{i} + \xi_{j-1})\sqrt{\xi_{i} - \xi_{j-1}} - (2\xi_{i} + \xi_{j})\sqrt{\xi_{i} - \xi_{j}}]$$
(41)

In addition, an integral of the function $f(\xi)$ between the two grid points may be defined by the quadrature:

$$S(f)_{ij} = \int_{\xi_{j-1}}^{\xi_j} \frac{f(\xi)d\xi}{\sqrt{\xi_i - \xi}} + \left(f_{j-1} + \frac{f_j - f_{j-1}}{\xi_j - \xi_{j-1}}\xi_{j-1}\right) I_j^i + \left(\frac{f_j - f_{j-1}}{\xi_j - \xi_{j-1}}\right) J_j^i$$
(42)

Using the above quadrature the integral terms in equations (37) and (38) may be represented in the following discrete form:

$$\int_{-1}^{\xi_{i}} \frac{f(\xi)d\xi}{\sqrt{\xi_{i}-\xi}} = \sum_{j=2}^{i-1} S(f)_{ij} + \left(f_{i-1} + \frac{f_{i}-f_{i-1}}{\xi_{i}-\xi_{i-1}}\xi_{i-1}\right) I_{i}^{i} + \left(\frac{f_{i}-f_{i-1}}{\xi_{i}-\xi_{i-1}}\right) J_{i}^{i}$$

$$= \sum_{j=2}^{i-1} S(f)_{ij} + f_{i-1} \left(\frac{I_{i}^{i}\xi_{i}-J_{i}^{i}}{\xi_{i}-\xi_{i-1}}\right) + f_{i} \left(\frac{J_{i}^{i}-I_{i}^{i}\xi_{i-1}}{\xi_{i}-\xi_{i-1}}\right)$$
(43)

Now substitution of the above in equations (27) and (38) gives the discrete expressions for temperatures at the various grid points:

$$T_{1i} = 1 + A_1 \sum_{j=2}^{i-1} [S(T_2)_{ij} - S(T_1)_{ij}] + B_1 \gamma \sum_{j=2}^{i} S(q)_{ij}$$

$$+ T_{2i-1} A_1 \left(\frac{I_i^i \xi_i - J_i^i}{\xi_i - \xi_{i-1}} \right) + T_{2i} A_1 \left(\frac{J_i^i - I_i^i \xi_{i-1}}{\xi_i - \xi_{i-1}} \right)$$

$$+ T_{1i-1} A_1 \left(\frac{I_i^i \xi_i - J_i^i}{\xi_i - \xi_{i-1}} \right) + T_{1i} A_1 \left(\frac{J_i^i - I_i^i \xi_{i-1}}{\xi_i - \xi_{i-1}} \right)$$
(44)

and

$$T_{2i} = 1 + A_2 \sum_{j=2}^{i-1} [S(T_1)_{ij} - S(T_2)_{ij}] + B_2(1-\gamma) \sum_{j=2}^{i} S(q)_{ij}$$

$$+ T_{1i-1} A_2 \left(\frac{I_i^i \xi_i - J_i^i}{\xi_i - \xi_{i-1}} \right) + T_{1i} A_2 \left(\frac{J_i^i - I_i^i \xi_{i-1}}{\xi_i - \xi_{i-1}} \right)$$

$$+ T_{2i-1} A_2 \left(\frac{I_i^i \xi_i - J_i^i}{\xi_i - \xi_{i-1}} \right) + T_{2i} A_2 \left(\frac{J_i^i - I_i^i \xi_{i-1}}{\xi_i - \xi_{i-1}} \right)$$
(45)

For the purpose of implementing the above equations in a computer subprogram, the above equations may be written in the following matrix form:

$$[C_{kl}]\{T_l\} = \{R_k\}$$
(46)

where the various components are written as

$$C_{11} = 1 + \left(\frac{J_i^i - I_i^i \xi_{i-1}}{\xi_i - \xi_{i-1}}\right) A_1 \qquad C_{12} = -\left(\frac{J_i^i - I_i^i \xi_{i-1}}{\xi_i - \xi_{i-1}}\right) A_1$$

$$C_{21} = -\left(\frac{J_i^i - I_i^i \xi_{i-1}}{\xi_i - \xi_{i-1}}\right) A_2 \qquad C_{22} = 1 + \left(\frac{J_i^i - I_i^i \xi_{i-1}}{\xi_i - \xi_{i-1}}\right) A_2$$

$$R_1 = 1 + A_1 \left(\sum_{j=2}^{i-1} [S(T_2)_{ij} - S(T_1)_{ij}]\right) + B_1 \gamma \sum_{j=2}^{i} S(q)_{ij}$$

$$+ \left(\frac{I_i^i \xi_i - J_i^i}{\xi_i - \xi_{i-1}}\right) (T_{2i-1} - T_{1i-1}) A_1$$

$$R_{2} = 1 + A_{2} \left(\sum_{j=2}^{i-1} [S(T_{2})_{ij} - S(T_{1})_{ij}] \right) + B_{2}(1-\gamma) \sum_{j=2}^{i} S(q)_{ij} + \left(\frac{I_{i}^{i} \xi_{i} - J_{i}^{i}}{\xi_{i} - \xi_{i-1}} \right) (T_{1i-1} - T_{2i-1}) A_{1}$$

Solution to the above equations for the temperatures T_1 and T_2 is now straightforward, when the shear is known over the contact, and it is independent of temperature. In the event the shear stress depends on the temperature, then a certain iterative procedure shall be necessary to determine compatible shear stress and temperatures. Alternatively, if no temperature dependence of shear stress is assumed between two consecutive nodes, *i*-1 and *i*, then q_i may simply be calculated at temperature T_{i-1} and the iterative procedure may be conveniently eliminated. As the grid size becomes smaller such a simplification may become increasingly reasonable.

A special case of the above formulation is when the temperatures of the two interacting surfaces are assumed to be equal. Such a case is certainly applicable to solid lubricant bearings. For liquid lubricated bearings, particularly when the lubricant film thickness is significant, such a simplification is indeed an assumption. In view of the fact, that for most of the experimental traction data and subsequent regression analysis, the contact temperatures are assumed to be the same, since no reliable experimental values are available, the assumption of equal surface temperatures may not be unreasonable for liquid lubricated bearings as well. Thus such an assumption in made in the current development. A result of such an assumption is elimination of the conduction terms in the above formulation, which is indeed a significant numerical simplification. The base equations for temperature distribution are now written as:

$$T_{1}(y) = B_{1}\gamma \int_{-1}^{y} \frac{q(\xi)}{\sqrt{y-\xi}} d\xi$$
(47)

and

$$T_{2}(y) = B_{2}(1-\gamma) \int_{-1}^{y} \frac{q(\xi)}{\sqrt{y-\xi}} d\xi$$
(48)

Since $T_1 = T_2$, the heat partition fraction is simply expressed in terms of the material properties

$$\gamma = \frac{B_2}{B_1 + B_2} \tag{49}$$

Thus the temperature equation may now be written as

$$T(y) = 1 + \frac{B_1 B_2}{B_1 + B_2} \int_{-1}^{y} \frac{q(\xi)}{\sqrt{y - \xi}} d\xi$$
(50)

and in discrete form

$$T_{i} = 1 + \frac{B_{1}B_{2}}{B_{1} + B_{2}} \sum_{j=2}^{i} S(q)_{ij}$$
(51)

Arguments with regard to temperature dependence of shear stress apply as discussed in the general case. When the shear stress does not depend on temperature, the integration is straighforward. Now if we define a dimensionless temperature rise at any point i, in the contact, as

$$\Delta \tilde{T}_i = \frac{(T_i - 1)(B_1 + B_2)}{B_1 B_2}$$
(52)

then equation (51) may be expressed in the form of temperature rise as:

$$\Delta \tilde{T}_i = \sum_{j=2}^i S(q)_{ij}$$
(53)

To elaborate on the results obtained with the above equations, consider an elliptical contact with a Hertzian pressure distribution. Also, assume a constant coefficient of friction and sliding velocity. Under such conditions, the heat flux will also be elliptical. The results obtained by implementing equation (53) under such conditions are plotted below in figure 9, along with the results obtained with a uniform heat flux.

2.9 Geometrical Distortions Due to Thermal Effects

As the heat travels through the bearing elements the overall temperatures of the various elements will change which will result in change in internal clearances, and, therefore, the applied load. Models used to compute such geometrical distortions are based on text book formulae for cylindrical and spherical elements as documented in the literature. These formulae are very well understood and they are, therefore, omitted here for brevity.

When changes in bearing geometry are applied, a change in bearing internal clearance will lead to a step change in performance parameters, such as contact load, when the races are held in a fixed position. If the applied loads are required to remain constant then it will be necessary to impose an equilibrium constraint and move the races accordingly. Note also, that there are no thermal transients in the current model. Thus changes in bearing geometry will be instantaneous when applied. Considering such limitations, the local heat generations are first averaged over a certain time domain before computing the temperature field. Then the geometrical changes are applied in a step wise fashion at selected time steps. Both the averaging times and the times for implementation of geometrical changes are inputs to the numerical procedure. Such a step wise procedure is justified in absence of any thermal transients. Also, when explicit procedures are used to integrate the equations of motion, such an implementation will be free of any truncation problems.



Figure 9. Comparison of temperature distribution resulting from elliptical and unform heat fluxes.

2.10 Overall Boundary Conditions and Model Implementation

Implementation of the above thermal formulation to ADORE will require certain boundary conditions. Basically, the models define a thermal resistance for computation of temperature rise for a given heat generation. Thus it is necessary that temperature at one reference point be prescribed. In the present investigation this temperature is assumed to be the housing temperature. Alternatively, the reference temperature can be shaft or the exit coolant temptress. The inlet temperature of the coolant is of course an input. Thus the steps in thermal model implementation consist of the following:

1. Compute heat generation from bearing interactions.

2. Continue the heat generation computations over a specified time domain and compute an average over the selected time domain.

3. Establish heat partition from prescribed material properties and compute heat transferred to the housing.

4. Compute temperature distribution in the housing and then the outer race.

5. Based on the established outer race contact temperature distribution, compute the temperature at contact with the rolling elements. Temperatures of both the race and rolling element are presently assumed to equal at contact.

6. Now implement the rolling element model to compute the base rolling element temperature and the contact temperature at the inner race.

7. Carry out heat transfer analysis through the inner race and shaft to compute appropriate temperature distribution and bulk temperatures.

8. From overall heat balance the heat transferred to the coolant may not be determined. Now given the flow rate and inlet temperature, the exit temperature may be computed.

9. All of the above is carried out at certain time intervals over which the heat generations are averaged. Clearly, all thermal transients are being neglected. In other words, there is no thermal inertia. However, when the averaging time is large enough such a stepwise implementation is reasonable.

10. Once the temperatures are computed determine the changes in bearing internal geometry if desired and update all geometrical parameters.

11. Apply any constraints, such as equilibrium to maintain constant applied load.

12. Continue numerical integration of equations of motion.

Note that when explicit procedures are used to integrate the equations of motion the above stepwise implementation will not introduce any local truncation. Thus stability or convergence of the integration procedure is unaffected.

3. Other Analytical Models

With the implementation of thermal models provides a dynamic coupling between applied conditions and overall bearing behavior. For the prescribed conditions a realistic model for bearing heat generation and transfer of heat through the bearing, a dynamically changing thermal field may be computed, which becomes a subsequent input to the operating materials parameters and bearing geometry. With such enhancements to bearing performance modeling any imposed constraints, in terms of applied loads and/or displacements, have added practical significance. In particular, equilibrium constraints may be very effectively applied to speed up the dynamic simulations in a rather complex operating environment. For this purpose, enhancements to the equilibrium models in ADORE are developed as a part of the current development. In addition, since the overall modeling approach provides significant improvement in the prediction of actual conditions at the rolling element to race contacts, the models for computing fatigue life are also refined.

3.1 Generalized Equilibrium Formulations

In all prior version of ADORE race equilibrium was restricted to radial and axial force equilibrium. Simulation of applied moments was only possible by prescribed relative misalignment between the races. Although such a formulation is adequate for the simulation of overall load distribution and other quasi-static parameters, it has a limited use for imposing time-varying dynamic constraints involved with moment equilibrium, particularly with angular contact ball bearings with combined thrust and radial loads. An extension of the equilibrium equations to include moment about the two transverse axes is, therefore, the objective of this enhancement.

As shown in figure 10, ball to race interaction is modeled by locating the ball center relative to the raceway.



Figure 10. Schematic of ball and race relative position.

Let \mathbf{r}_b and \mathbf{r}_r be the position of ball and race centers in an inertial coordinate frame. When a cylindrical frame is used to track ball position and a cartesian frame is used for prescribing the race position, then these vectors may be written in terms of there components, as

$$\mathbf{r}_{b} = \begin{bmatrix} x \\ -r\sin\varphi \\ r\cos\varphi \end{bmatrix} \text{ and } \mathbf{r}_{r} = \begin{bmatrix} X \\ Y \\ Z \end{bmatrix}$$
(54)

and the relative position in inertial frame is simply

$$\mathbf{r}_{br}^{i} = \begin{bmatrix} x \\ -r\sin\varphi \\ r\cos\varphi \end{bmatrix} - \begin{bmatrix} X \\ Y \\ Z \end{bmatrix}$$
(55)

For the purpose of computing geometric interaction the above may be transformed to a race coordinate frame

$$\mathbf{r}_{br}^{r} = \begin{bmatrix} T_{ir} \end{bmatrix} \begin{bmatrix} x - X \\ -r\sin(\varphi - Y) \\ r\cos(\varphi - Z) \end{bmatrix}$$
(56)

Here $[T_{ir}]$ is the transformation matrix from the inertial to race fixed coordinate frame as defined by the three transformation angles [3]. These angles are rotations, η , θ_2 and θ_3 about the X, Y and Z axes respectively. For the race rotation about X axis simply constitutes race rotation, and when the race is symmetric about the X axis, then this rotation has no effect on any interactions with the rolling elements; the other two rotations represent race misalignment about the two transverse axes. In terms of these three angles the transformation matrix is written as:

$$[T_{ir}] = \tag{57}$$

$$\begin{bmatrix} \cos\theta_2\cos\theta_3 & \cos\eta\sin\theta_3 + \sin\eta\sin\theta_2\cos\theta_3 & \sin\eta\sin\theta_3 - \cos\eta\sin\theta_2\cos\theta_3 \\ -\cos\theta_2\sin\theta_3 & \cos\eta\cos\theta_3 - \sin\eta\sin\theta_3\sin\theta_2 & \sin\eta\cos\theta_3 + \cos\eta\sin\theta_2\sin\theta_3 \\ \sin\theta_2 & -\sin\eta\cos\theta_2 & \cos\eta\cos\theta_2 \end{bmatrix}$$

From the above a race azimuth angle, ϕ' , and a corresponding transformation matrix from the race to race azimuth frame may be defined as follows:

$$T_{ra} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & \cos\varphi' & \sin\varphi' \\ 0 & -\sin\varphi' & \cos\varphi' \end{bmatrix}$$
(58)

where
$$\sin \phi' = \frac{-r_{br2}}{\sqrt{(r_{br2}^r)^2 + (r_{br3}^r)^2}}$$
 and $\cos \phi' = \frac{r_{br3}}{\sqrt{(r_{br2}^r)^2 + (r_{br3}^r)^2}}$

Using the above transformation, the relative position vector may now be transformed to the race azimuth frame and then referenced to a certain reference point for the purpose of computing the geometric interaction. In the case of ball bearings, this reference point is the center of race groove curvature located by axial and radial coordinate values equal to \overline{X} and \overline{R} respectively. The assumption here is that the race is ideally round and these two components are constant for all angular positions. Thus the ball center relative to the race curvature center at any azimuth position is written as:

$$\mathbf{r}_{brb}^{a} = \begin{bmatrix} T_{ia} \end{bmatrix} \begin{pmatrix} x - X \\ -r\sin\varphi - Y \\ r\cos\varphi - Z \end{bmatrix} - \begin{bmatrix} T_{ir} \end{bmatrix} \begin{bmatrix} \overline{X} \\ -\overline{R}\sin\varphi' \\ \overline{R}\cos\varphi' \end{bmatrix} = \begin{bmatrix} a_{1} \\ a_{2} \\ a_{3} \end{bmatrix}$$
(59)

Note that if the load vector and bearing axis (X) are in a plane then in the azimuth frame, the compound a_2 will be zero.

The geometric interaction, δ , is now for a prescribed ball diameter, *d*, and race curvature factor *f*,

$$\delta = \sqrt{a_1^2 + a_2^2 + a_3^2} + d(1 - f) \tag{60}$$

and the contact load is expressed as

$$Q = K\delta^n \tag{61}$$

Using equation (59), and ignoring the out of plane y-component, the contact angle, α , as shown schematically in figure 10, may be computed from the relations

$$\sin \alpha = \frac{a_1}{\sqrt{a_1^2 + a_3^2}}$$
(62)

and

$$\cos \alpha = \frac{a_2}{\sqrt{a_1^2 + a_3^2}}$$
(63)

The position vector locating the contact point relative to the ball center is simply determined by the unit vector, corresponding to equation (59) multiplied by the ball radius:

$$\mathbf{r}_{p} = \frac{d}{2}\sqrt{a_{1}^{2} + a_{2}^{2} + a_{3}^{2}} \begin{bmatrix} a_{1} \\ a_{2} \\ a_{3} \end{bmatrix}$$
(64)

The above formulation is applied to both outer and inner races. The equilibrium equations may then be written for both the balls and races. Using the subscript, j, for the races the ball equilibrium equations may be written as summation of the axial and radial component of forces on the outer and inner race contacts. Thus,

$$\sum_{j=1}^{2} Q_j \sin \alpha_j = 0 \tag{65}$$

and

$$\sum_{j=1}^{2} Q_{j} \cos \alpha_{j} + F_{c} = 0$$
(66)

where F_c is the centrifugal force acting on the ball.

The race equilibrium equations may be written in the cartesian inertial frame in terms of a summation of forces acting on all ball/race contacts. Generally, one of the races, normally the outer, is assumed to be fixed while relative position of the other race may be computed by solving the equilibrium equations. In addition to the force equilibrium equations along the X,Y,Z axes, we also have two moment equilibrium equations along the Y and Z axis. Moment equilibrium about the X axis is not applicable, since this is the axis of bearing rotation. Race moment is first computed in the azimuth frame, where the only applicable component is about the y axis. In terms of the various position and force vectors presented above, the moment on the race about the y axis in the azimuth frame may be written as:

$$M_{i} = \begin{bmatrix} a_{1i} + \overline{X} + \frac{d}{2}\sin\alpha_{i} \\ 0 \\ a_{3i} + \overline{R} + \frac{d}{2}\cos\alpha_{i} \end{bmatrix} \times \begin{bmatrix} Q_{i}\sin\alpha_{i} \\ 0 \\ Q_{i}\cos\alpha_{i} \end{bmatrix}$$
(67)

Clearly, the vector moment equation has only one component about the y-axis. The overall force and moment equilibrium equations on the race may now be written as summation over all rolling elements:

$$\sum_{i=1}^{n} Q_i \sin \alpha_i + F_x = 0 \tag{68}$$

$$\sum_{i=1}^{n} Q_i \cos \alpha_i \sin \varphi_i + F_y = 0$$
(69)

$$\sum_{i=1}^{n} Q_i \cos \alpha_i \cos \varphi_i + F_z = 0$$
(70)

$$\sum_{i=1}^{n} M_i \sin \varphi_i + M_y = 0 \tag{71}$$

$$\sum_{i=1}^{n} M_{i} \cos \varphi_{i} + M_{z} = 0$$
(72)

For the above five race equilibrium equations, (68) to (69), the five unknown are the three race center positions coordinates *X*, *Y*, *Z*, and the two relative misalignment angles, θ_2 and θ_3 . For the ball equilibrium equations, (65) and (66), the unknowns are the axial and radial position of ball center, *x* and *r*. Clearly, the equations are nonlinear, and an iterative procedure shall be required for a solution. In ADORE a Newton-Raphson procedure is used in two steps. First for a given race position, the ball equilibrium equations are solved. After obtaining the loads satisfying ball equilibrium, iterations for the race equations are performed in the second step. In both steps a Jacobian matrix is required for solution of the simultaneous algebraic equations. The various components of this matrix are obtained by straightforward differentiation of the equilibrium equations.

3.2 Fatigue Life Model

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A model for computation of improved fatigue life is based on the recent work done by Tallian [16-17]. Enhancement to life prediction is achieved by applying life mollification factors on the basic Lundburg-Palmgren life, N_{LP} , to obtain the corrected life, N_{10} , with a 10% failure probability. Formulae used in ADORE for the base N_{LP} life of a rolling contact, as used in ADORE, are documented in an earlier publication[21].
$$N_{LP} = \left(\frac{Q_e}{Q_c}\right)^{-p} \tag{73}$$

where Q_e is an equivalent contact load, Q_c is the contact load capacity, and p is a load exponent.

In the case of a ball bearing, the equivalent load is the actual contact load, and the load capacity is defined by an expression [22]:

$$Q_c = A \left(\frac{2f}{2f-1}\right)^{0.41} (1\pm\gamma)^{1.39} \left(\frac{D}{d_m}\right)^{0.39} D^{1.80} n^{-1/3}$$
(74)

where A is an ANSI fatigue contact $[N/m^{1.80}]$, d_m is the pitch diameter [m], *D* is the ball diameter [m], *f* is the race groove conformity ration (groove radius/ball diameter), *n* is the number of stress cycles per race revolution per rolling element, $\gamma = (D\cos\alpha)/d_m$, α being the contact angle. The positive and negative signs in the second term in parenthesis apply respectively to the outer and inner races. Also, the commonly used value for the fatigue constant A is $2.3615 \cdot 10^7$ N/m^{1.80}.

For roller bearings, there the contact load intensity may vary significantly along the roller length, the equivalent load is defined in terms of an equivalent load intensity

$$Q_{e} = 2a \left[\frac{1}{2a} \int_{-a}^{a} q^{pe} dx \right]^{1/(pe)}$$
(75)

where a is the contact half width, p is a load exponent and e is the Weibull dispersion slope for the contact under consideration.

Also, the load capacity for a line contact is written as:

$$Q_c = \mathbf{B}(1\pm\gamma)^{29/27} \left(\frac{D}{d_m}\right)^{2/9} D^{29/27} l^{7/9} n^{-1/4}$$
(76)

where B is the ANSI fatigue constant $[N/m^{50/27}]$ for line contact, *l* is the length of contact and all other variables are same as those defined above for ball bearing contacts. The commonly used value for the constant B is $1.98 \cdot 10^8 (N/m^{50/27})$

Life correction factors are now applied on the above computed base life, as formulated by Tallian [16-20].

$$N_{10} = 12AM^{-\frac{1}{\beta}} \left[N_{LP}^{-\frac{1}{\zeta}} \tilde{\Psi}^{\frac{1}{\beta\zeta}} - \tau_o \Phi_{0LP}^{\frac{1}{\beta\zeta}} \right]^{-\zeta}$$
(77)

where A is a dimensionless scaling multiplier (=0.23), M is a dimensionless matrix sensitivity multiplier, as tabulated below in table 3, β is a dimensionless life dispersion exponent (=1.60), ζ is a dimensionless stress/life exponent (=7.33), τ_o is the material fatigue limit stress (MPa) with a default (τ_o =0), and Φ_{0LP} is a baseline matrix susceptibility factor (=3 \cdot 10⁻⁴⁵).

Material (Steel Composition)	Matrix susceptibility multiplier M
52100	1.197
8620	1.773
M50	2.267

Table 3: Material Matrix Susceptibility Multiplier

The equivalent hazard factor ratio $\tilde{\Psi}$ in equation (77) over one duty cycle is defined as:

$$\tilde{\Psi} = \frac{\tilde{\Phi}_T}{\tilde{\Phi}_{TLP}} \tag{78}$$

An expression for equivalent hazard factor product $\tilde{\Phi}_T$ over one duty cycle is written as:

$$\tilde{\Phi}_{T} = \frac{\beta}{l} \tilde{N}^{-\beta} \sum_{j=1}^{q} \left\{ \sum_{k=1}^{m} \left[\Phi_{4,k,j} \sum_{i=a,b,f} \Phi_{1i} \Phi_{2i} \Phi_{3i} \right] \Delta l N_{k}^{\beta-1} \right\} \Delta N_{j}$$
(79)

Here ΔN_j in a load cycle increment in relative race revolutions,

$$\tilde{N} = \sum_{j=1}^{q} \Delta N_j \tag{80}$$

is the duty cycle in relative race revolutions divided in q increments per duty cycle, Δl is the track increment in radians, m is the number of equal track increments, with $l = m\Delta l$. The number of track increments, m, may be quite arbitrary. This track increment and the total number of track increments shall determine accuracy of the overall computation of the integrated value by using the above summation. In the bearing dynamics code, however, the load values, at any instant

of time, may be available only at the points where the rolling elements are located. Thus it is may be convenient to set *m* equal to the number of rolling elements. This may result in a slight inaccuracy when the number of rolling elements is quite small, but for most practical bearings, such an assumption may be quite acceptable.

The severity balancing factors for asperity and furrow defects are model constants

$$\Phi_{1a} = \Phi_{1f} = 1.50 \tag{81}$$

Also, the severity balancing factor for subsurface defects is a model constant,

$$\Phi_{1b} = 1.0 \tag{82}$$

The asperity defect severity factor Φ_{2a} is given by the relation:

$$\Phi_{2a} = D_s [1 - G(\Lambda - 0.40)], \text{ with } \Lambda > 0.40$$
(83)

while, G() is the standardized Gaussian cumulative distribution function, which may be approximated by the curve fitted relation:

$$\frac{1 - G(x)}{\varphi(x)} = 1.03 \{ e^{0.75x} + 0.22 \}$$
(84)

with the Gaussian frequency function,

$$\varphi(x) = \sqrt{2\pi}e^{-\frac{x^2}{2}}$$
(85)

The asperity count, D_s in equation (83) is defined as

$$D_s = 0.0306 \left(\frac{\sigma}{\theta}\right)^{-2} \alpha \tag{86}$$

with the roughness spectrum width parameter, $\alpha = 40$, σ and θ are respectively the composite roughness height (mm) and slope (radians) for the two interacting surfaces:

$$\sigma = \sqrt{\sigma_1^2 + \sigma_2^2} \text{ and } \theta = \sqrt{\theta_1^2 + \theta_2^2}$$
 (87)

In the event no data on roughness height and slope is available, the following empirical relation may be used:

$$\frac{\sigma}{\theta} = 0.02683 \sigma^{0.2607} \text{ mm/rad}$$
(88)

The defect severity factor, Φ_{2b} , in equation (79) is really the materials processing multiplier:

$$\Phi_{2b} = \Phi_{2bLP}I \tag{89}$$

where $\Phi_{2bLP} = 1$, is a model constant and it represents the Lundberg-Palmgren steel processing factor, and *I* is a materials processing multiplier, depending on the manufacturing process used. The default values are tabulated below in table 4.

Processing Method Designation	Method Description	Processing Multiplier, I
CVD	Carbon vacuum deoxidation through-hardening steel (groups pre-dating 1975)	2.58
CVD _{new}	Carbon vacuum deoxidation through-hardening steel (groups 1975 and later)	0.077
CVD _{carb}	Carbon vacuum deoxidation through-hardening steel (all dates)	4.85
VIMVAR	Vacuum induction melt, vacuum are remelt	0.0030

Table 4: Steel Processing Multiplier

The furrow defect severity factor Φ_{2f} allows for cleanliness of the manufacturing process.

$$\Phi_{2f} = \Phi_{2fclean} C_{cont} \tag{90}$$

Here the baseline factor, $\Phi_{2fclean}$ has a default value of 600, while C_{cont} is a cleanness factor, introduced primarily for future implementation. Presently, there is no significant experimental data to substantiate any value other than the present default of 1.0.

The subsurface stress field factor Φ_{3b} is expressed as:

$$\Phi_{3b} = t_b^{\beta\zeta} \tag{91}$$

with

$$t_b = 0.39 + 0.10s_{stat} \tag{92}$$

and

$$s_{stat} = \frac{(\sigma_{res} + 0.834\sigma_{hoop})}{p_{max}}$$
(93)

where σ_{res} , σ_{hoop} and p_{max} are respectively the residual stress, hoop stress and the maximum Hertzian pressure. All quantities are in stress units.

The stress field factor for furrows, Φ_{3f} is estimated from the relation

$$\Phi_{3f} = t_f^{\beta\zeta} \tag{94}$$

with

$$t_f = 1.25 z_{frac} + 1.22 \mu_a + 0.15 s_{stat}$$
(95)

in which $z_{frac} = 0.0270$, and $\mu_a = 0.10$ are the suggested default values for the depth factor and the asperity traction coefficient.

The stress field factor for asperity defects Φ_{3a} is:

$$\Phi_{3a} = t_a^{\beta\zeta} \tag{96}$$

where

$$t_a = 1.25z_{frac} + 1.22\mu_{TOT} + 0.15s_{stat}$$
(97)

in which the total traction coefficient, $\mu_{TOT} = \mu_{eff} + \mu_{EHD}$, is the sum of the EHD film traction coefficient, μ_{EHD} , and μ_{eff} is the effective asperity traction coefficient, which is give by:

$$\left(\frac{\mu_{eff}}{\mu_{a}} = 0.05 \frac{E'}{p_{max}} \theta(\alpha - 0.9)^{3/4} F_{32}\right) \le 1$$
(98)

where, $\frac{1}{E'} = \frac{1 - v_1^2}{E_1} + \frac{1 - v_2^2}{E_2}$, E_1 , v_1 , E_2 , v_2 being the elastic modulus (Mpa) and Pois-

son's ratio respectively for the two interacting materials, p_{max} is the maximum Hertz pressure (MPa), θ is the composite asperity slope defined earlier, α was defined earlier in equations (86-87), and the function F_{32} is given by the relation

$$F_{32} = \exp\left[-15.50 + 7.50(4.30 - \Lambda)^{\frac{1}{2}}\right]$$
(99)

where Λ is the ratio of lubricant film thickness to the composite asperity height. Note also that when equation (98) yields a value for $\frac{\mu_{eff}}{\mu_a}$ greater than 1.0, then value must be set equal to 1.0. In addition when there is no lubricant film, $\mu_{eff} = \mu_a$, and the EHD traction coefficient, μ_{EHD} is set to zero.

The load distribution factor, Φ_4 , in equation (79), is identical to its Lundberg-Palmgren value and it is given by:

$$\Phi_4 = \Phi_{4LP} = -0.39^{-\beta\zeta} \ln(0.90) \Phi_{0LP}^{-1} N_{LP}^{-\beta}$$
(100)

When the factors are substituted in equation (78), the constant part of the above equation will cancel out; thus for numerical implementation the only relevant part is $N_{LP}^{-\beta}$.

In addition, the Lundberg-Palmgren hazard factor product, $\Phi_{TLP}^{\tilde{}}$, in equation (78), is a special case of equation (79), with the asperity (subscript *a*) and furrow (subscript *f*) defect products set to zero, with equations (82), (89), $\Phi_{1bLP} = \Phi_{2bLP} = 1$, and with equations (91) and (92), $\Phi_{3bLP} = 0.39^{\beta\zeta} = 1.60 \cdot 10^{-5}$,

$$\tilde{\Phi}_{TLP} = 0.39 \frac{\beta}{l} \tilde{N}^{-\beta} \sum_{j=1}^{q} \left\{ \sum_{k=1}^{m} \Phi_{4LPkj} \Delta l N_{j}^{\beta-1} \right\} \Delta N_{k}$$

$$(101)$$

Now the equations for both $\tilde{\Phi}_T$ and $\tilde{\Phi}_{TLP}$ are computed for both races independently and they are applied in equations (78) and (79) to compute modified life of each race independently. These computed lives are then combined to obtain the composite bearing life using the expression:

$$N_{10}^{-e} = N_{100R}^{-e} + N_{10IR}^{-e}$$
(102)

Since the formulae for computing the life modifying factors involves both variation with load and time, all computations are first performed for one relative race rotation. Normally, in a practical bearing one of the races rotates with respect to the applied load, while the other is stationary. For the rotating race each contact will be subject to the same load condition while for the stationary race each contact will be subject to a different load condition, however, there will be no variation with time in this case. Now for the rotating race, and for a load cycle comprising of one revolution, we can make the following substitutions in equation (79):

$$l = 2\pi, N_k = \frac{2\pi}{m}k, \tilde{N} = 2\pi \text{ and } \sum_{j=1}^{q} \Delta N_j = \tilde{N} = 2\pi$$
 (103)

Thus the expression for $\tilde{\Phi}_T$, as stated in equation (78) becomes:

$$\tilde{\Phi}_{TR} = \frac{\beta}{m} (2\pi)^{1-\beta} \sum_{k=1}^{m} \Phi_{TRk} \left(\frac{2\pi}{m}k\right)^{\beta-1}$$
(104)

Note that since all contacts are subject to the same load condition the terms under the outer summation are constant. Therefore, the summation $\sum_{j=1}^{q} \Delta N_j$ may be written as a constant with a

value equal to 2π . Also, the subscript *R* is used for the rotating race, and the product of various life modification factor is denoted by Φ_T as:

$$\Phi_{Tk} = \Phi_{4k} \sum_{i = a, b, f} \Phi_{1i} \Phi_{2i} \Phi_{3i}$$
(105)

For the race which is stationary with respect to the load, each contact is subject to different load conditions but there is no variation in time. Thus in equation (79) the time and space integrals may be separated to yield:

$$\tilde{\Phi}_{TS} = \frac{\beta}{(\beta - 1)m} \sum_{k=1}^{m} \Phi_{TSk}$$
(106)

where the subscript S is used to denote stationary race.

Corresponding to equations (104) and (106) the corresponding Lundberg-Palmgren factors are written as:

$$\tilde{\Phi}_{TLPR} = \frac{\beta}{m} (2\pi)^{1-\beta} \sum_{k=1}^{m} \Phi_{TLPRk} \left(\frac{2\pi}{m}k\right)^{\beta-1}$$
(107)

$$\tilde{\Phi}_{TLPS} = \frac{\beta}{(\beta - 1)m} \sum_{k=1}^{m} \Phi_{TLPSk}$$
(108)

and

$$\Phi_{TLPk} = \Phi_{4LPk} \sum_{i=a,b,f} \Phi_{1LPi} \Phi_{2LPi} \Phi_{3LPi} = \Phi_{4LPk} \Phi_{2bLP} \Phi_{3bLP}$$
(109)

In a bearing if both races rotate relative to the applied load, then the expressions for rotating race are used for both races.

Implementation of the life model is now straightforward. After performing the load computation at each outer and inner race contact, carry out the following steps to compute the corrected life:

1. Use equations (73) to (76) to compute the base Lundberg-Palmgren life for each contact.

2. Compute the life modification products, Φ_{Tk} and Φ_{TLPk} at each contact using equations (105) and (108) respectively. This will of course implement all the other equations, (79) to (101) for computation of the various factors.

3. Use equations (104) and (107), if the race is rotating, or (106) and (108), when the race is stationary, to compute the integrated factors $\tilde{\Phi}_T$ and $\tilde{\Phi}_{TLP}$ for each of the races.

4. Use equation (78) to compute the overall factor life modification factor $\tilde{\Psi}$ for each of the races.

5. Perform appropriate summation to computer the base Lundberg-Palmgren life for each raceway, N_{LP} .

6. Implement equation (77) for each of the races to compute the modified life. Note the fact that τ_o is in units (MPa), while the numerical value of Φ_{0LP} is $3 \cdot 10^{-45}$. Depending on the precision of floating point numbers, direct implementation of these values may result in some numerical problems. It may, therefore, be more convenient to input stress in units (Pa) and prescribe the value of $\Phi_{0LP}^{1/(\beta\zeta)}$. This will reduce the second terms in equation (77) to $\tau_0 \cdot 1.5985 \cdot 10^{-10}$, which may be numerically more manageable.

7. Apply equation (102) to combine the base and modified lives of the races to obtain the base and modified life of the entire bearing.

4. Enhancement to Bearing Dynamics Code ADORE

All analytical models during this project are implemented in the bearing dynamics computer code, ADORE. In addition to the model enhancements, the code is basically rewritten to conform to the FORTRAN-90 standard. It is expected that this new code architecture will be better understood by the users and it will be more amiable to future enhancements and refinements.

4.1 Conversion to FORTRAN-90 Standard

ADORE when first published in 1984 [3] was written in FORTRAN-77, which at the time was the most common language used for the development of engineering applications. As the modeling technology advanced, ADORE was continually updated to incorporate new models and improvements in overall modeling technology. Both due to the complex nature of the models and limitations of FORTRAN-77, the code architecture became continually complicated until it reached a point where it became extremely difficult for a user to comprehend. This prompted conversion of the code to FORTRAN-90 standard which gained popularity in the 1990's.

With regard to ADORE and other complex engineering applications, FORTRAN-90 offers several programming enhancements:

- 1. Completely "top-down" design free of any statement labels and "go-to" statements.
- 2. Descriptive variable names.
- 3. Array operations for efficient array processing and vector operations.
- 4. Data modules for efficient data handling.
- 5. Internal procedures for better code encapsulation.
- 6. User defined precision for consistent computational accuracy.

The above are only some of the features used by ADORE. On the whole FORTRAN-90 comes very close to other more popular languages, such as C, C++ and Java, in terms of code architecture, although FORTRAN-90 is not a object oriented language. Perhaps, the next step in code enhancement will be in terms of implementation of Java tools and techniques. It is anticipated that the FORTRAN-90 conversion, undertaken in the current project, will greatly facilitate such future developments.

Although there are a number of application conversion software packages available to convert old FORTRAN codes to the new FORTRAN-90 standard, the output from these convertors do not provide any simplifications in code architecture and variable descriptions. The current effort was, therefore, directed toward essentially rewriting the code to make use of the new features available in the FORTRAN-90 standard. As shown schematically in figure 11, the newly converted FORTRAN-90 consists of data modules, and both internal and external procedures. In addition the input and output facilities provide efficient user interfaces for preparation of input data and review of program output.



Figure 11. Schematic outline of code elements of ADORE

The development process consisted of first encapsulating all data in data modules with new descriptive variable names and related documentation. A typical data module is listed in Appendix A. This module encapsulates all data pertaining to bearing geometry. Next, the code in each of the compute modules was rewritten in the form of external procedures or subroutines, with new variable names and significantly improved code architecture. All statement labels and "go-to" statements were eliminated to obtain a truly "top-down" design. This permits easy code readibility. The numerical processing procedures uniquely required by the external procedures were incorporated as internal procedures within the given external procedure. A typical code segment is documented in Appendix B. This procedure computes the rolling element to race interaction and contact load. First the rolling element is located relative to the race, then depending on the geometry of elements appropriate geometrical interaction is computed. While a single computation is adequate for a point contact problem, the line contact computations are divided in two parts, first computation of overall contact length and then computation of geometrical interaction for the various grid points within the contact zone. Then appropriate constitutive relation is called for computation of contact load and other contact parameters. In the case of a roller bearing, the roller end to guide flange contact is also contained in this subprogram. Clearly, the code can be easily read from top to bottom without any complicated nesting.

4.2 Procedures for Thermal Interactions

All analytical modules and numerical procedures outlined in section 3 of this report are implemented in ADORE. New subprograms for both external and internal procedures, along with appropriate data modules are developed in a new program group for thermal interactions. Consistent with the naming convention used in ADORE, a new program group ADRH is introduced. The main procedure ADRH1 takes the relevant material properties, prescribed boundary conditions, and computed heat generations as input, to perform the overall heat balance and compute the temperature field through the bearing. Computation of temperature rise, module ADRH2, in the contact is directly related to rolling element to race traction and heat generation. It is therefore, called directly by the rolling element to race traction models. Presently, the contact temperature rise does not feed back to the traction model due to model limitation in traction model limitations for thermal interactions. Such a complex interaction is presently deferred to future development. The program module ADRH3 carries out all the convection analysis to provide appropriate heat transfer coefficients, and this is interactively called by the main module ADRH1 as a function of computed temperatures. Thus the heat transfer coefficients may vary as a function of temperature. The overall compute module structure is illustrated in the simplified diagram shown below in figure 12.



Figure 12.Schematic architecture of the thermal module in ADORE.

The above thermal interaction modules are first debugged independently to ensure proper operation and then incorporated in ADORE as a new program group. In its current form, ADORE consists of modules A to G, as shown schematically in figure 13. All module names start with ADR, abbreviation for ADORE, following by a group letter A, B, C, etc., and then followed by a numerical digit indicating the sequence number of the procedure. Module ADRH, shown in the shaded box in figure 13, is the outcome of the current effort. This module is primarily called by the traction module ADRD, where all details of contact geometry and load conditions are available. The modules may also be called by the main program, any time when an estimate of current temperature fields is desired. Module inputs, e.g., material properties and computed heat generation, are provided by appropriate data interfaces. Similarly, the computed contact temperatures and other thermal parameters are output via pertinent data structures.



Figure 13. Integration of thermal interaction module ADRH with other modules in the bearing dynamics computer code ADORE.

4.3 Implementation of Time-varying Geometry

Although not shown, for simplicity, in figure 13, the computed thermal field interacts with the rolling element to race interaction module responsible for the computation rolling element to race geometrical interaction and normal load. The interaction is provided via the thermal distortions module, ADRC2. Here the computed temperatures by ADRH1 are taken as input to compute the change in element geometry and internal clearance in the bearing, which in turn is fed as input to the normal load computation. Thus the thermal interactions affect the normal load computation, which in turn will alter traction and, therefore, the heat generation, which is fed back to temperature computation. Thus the computation appears to be an iterative loop. However, in view of transient effects associated with the thermal problem, which are presently not considered, such an iterative interaction may not be fully justified. Thus implementation in ADORE is such that the temperatures computed at a given step are used to compute thermal interaction at the next step. Hopefully, if the step size is small enough and the integration is convergent, the final temperatures will stabilize to some steady state.

It should be noted that the above interaction between the thermal and mechanical effects introduces a fairly sophisticated level of complexity in modeling of bearing dynamics. Before extensive use of such a feature, adequate experimental validation of the models used in ADORE is necessary. In absence of such a validation, the results must be viewed with some caution. The input options stream in ADORE, is therefore, structured to permit computation of the temperature fields without feeding it back to change bearing element geometry. This option may be parametrically used to determine the significance of thermal interactions in overall bearing performance.

4.4 Other Refinements

Other refinements to ADORE, carried out as a part of the current effort, include generalization of equilibrium module for ball bearings and enhancements to the life module as outlined in section 3 of this report. In addition, there have been a number of other enhancements to ADORE, which were carried out as a part of an ongoing commercial effort in parallel with this effort. All of these enhancements are also part of the current version of ADORE. Some of the major improvements are listed below after describing the moment equilibrium and life modeling work carried out as a part of this effort:

4.4.1 Moment Equilibrium for Ball Bearings

Two new moment equilibrium equations for the race have been introduced to perform moment equilibrium about the two transverse axes. Thus a total of five degrees of freedom are now available for equilibrium solutions. This resulted in a complete rewrite of the race equilibrium module which consists of the equilibrium equations and associated Jacobian matrix for solving the equations by Newton-Raphson techniques. All of these enhancements are in the subprogram ADRA4. Since the number of algebraic equations now becomes five, a new subroutine ADRG0 for the solution of a set of algebraic equations is introduced. Earlier the solutions were obtained within the quasi-static subroutine ADRA4. Also, in order to track the very small rotations, resulting from race misalignment, the transformation matrices with small angles are now computed by using series expansions of the sine and cosine functions. In addition appropriate procedures to compute the derivative of these matrices for accurate computation of Jacobian matrices are also incorpo-

rated. Appropriate changes to input data module are also carried out to execute the newly introduced degrees of freedom in the equilibrium formulation. These enhancements is presently available for ball bearings only. The code has not yet been fully developed for roller bearings. Since roller bearings involve flange interactions when the roller are misaligned and/or skewed, convergence of moment equilibrium equations becomes more complicated; particularly due to discontinuities resulting from the rollers getting in and out of flange contact during the iterative process. Thus roller bearings should be run with prescribed misalignment rather than moment.

4.4.2 Fatigue Life Model Refinements

The fatigue life correction factors outlined in section 3.2 of this report are incorporated in the subprogram ADRF1. The old life mollification factors are replaced by the newly developed formulae documented in this report. Implementation of the various algebraic equations is quite straightforward. Appropriate options in the input data are also introduced to invoke the newly introduced materials factors.

Although computation of fatigue life does not interact in any way with the dynamics modeling, the output is useful for practical design. Since all the contact loads and related parameters are collected from the main computing stream of ADORE, the effects of thermal interactions on contact loads are automatically taken care of. Thus in addition to the newly developed life improvement factors, the current version of ADORE includes the effect of thermal interactions on life when appropriate thermal options are invoked.

4.4.3 Partition of Rolling Element to Inertial Frame Transformation

With particular emphasis on accurate modeling of roller misalignment and skew in tapered roller bearings, the roller to inertial frame transformation is broken up into two parts: a base transformation for nominal position, and second, a time dependent transformation as a function of roller misalignment and skew. Thus roller misalignment angle excludes the nominal tilt of the roller axis as applied to tapered roller bearings. Such a partition of the transformation matrices provides improvements in precision in modeling tapered bearings. The enhancement is insignificant for other bearings.

4.4.4 Cage Initial Conditions

For a large number of simulations obtained over the last many years, it has been found that the most stable motion of the cage is when the mass center whirl velocity is equal to its angular velocity. In addition to the published literature, numerous steady-state solutions obtained by ADORE have confirmed such a behavior. Based on these findings, such a whirl behavior is now prescribed as an initial condition. Thus if there are no cage interactions, the cage will whirl in a well defined circular orbit, with the prescribed radius. The orbit may deviate a bit, as a result of cage contacts, but it will basically retain the general shape in case of a stable motion. Under unstable situations, however, the orbit will disintegrate into an erratic motion as a function of time. Thus this enhancement provides a greatly improved diagnosis of cage stability. In earlier versions, only a tangential velocity corresponding to the above whirl was applied at zero time, the remainder of the whirl motion was left up to the cage interactions and overall dynamics. Although such an initial condition will also lead to stable, almost circular, whirl orbits, the time required to reach such a condition may be significantly longer. Note that under stable conditions the steady-state solution does not depend on the initial conditions. It is only the simulation time, required to reach steady-state, which is affected by the initial conditions.

4.4.5 Simulations of Large Number of Time Steps

For low speed bearings, the steady state solutions normally require simulations over a large number of time steps, where stability of integration becomes strongly dependent on control of numerical precision. With the use of "kind" parameter offered in FORTRAN-90, precision of numerical computation is tightly controlled in ADORE. As a result stable integration of the differential equations of motion is possible overall several hundreds of thousands of time steps. A number of runs recently made on slow speed ball bearings have confirmed such a conclusion. It is also anticipated that with such a control of numerical precision within the program, simulations over millions of steps may now be possible. Of course, such investigations will require the fastest possible processor speeds.

When making runs over a large number of time steps, control of output data is another issue. To effectively address this problem, the notion of substeps, within a step, is introduced. This features simply introduces several substeps within a nominal step, while maintaining the required local step size for integration with a prescribed precision. However, neither the output is processed nor saved over the sub steps. Thus a run over 20,000 time steps, with 10 substeps within a step will result in integration over 200,000 time steps. This feature, along with earlier options of data control, provides fairly efficient management of output over large a number of time steps.

4.4.6 Arbitrary Constraints of Degrees-of-freedom

A new option to constrain the degrees-of-freedom on both rolling elements and cage has been implemented. This permits fairly fast integration of bearing under simplified conditions. For example, in the case of a perfectly aligned cylindrical roller bearing with purely radial load, the degrees of freedom corresponding to axial mass center motion and transverse rotation of both the roller and cage may be suppressed, to produce a relatively fast integration. With the implementation of this option, the need for MODE=3, as used in an earlier version, is eliminated. Thus, in the current version of ADORE, the variable MODE may only have values in the range of -2 to 2.

4.4.7 Initial Ball Angular Velocities

In all earlier versions of ADORE initial ball angular velocity in angular contact ball bearings was set by using the "race control" hypothesis where relative ball spin is permitted on only one of the races. Again, by a number of simulations obtained over the years, it is found that this hypothesis does not really hold for well lubricated bearings, instead the ball angular velocity vector lines up to be essentially parallel with the shaft axis. Some recent investigations in this area have shown that the orientation of the ball angular velocity vector is better determined by minimizing the energy dissipated in the ball/race contacts. Thus in the current version of ADORE, a new option for computing the initial orientation of the ball angular vector by minimizing the energy dissipated in the contacts is introduced. The procedure consists of computing the energy dissipation in the outer and inner race contacts as a function of the orientation of ball angular velocity vector. The point of minimum energy is then determined by interpolation. Due to these additional computations, the startup computing time at step zero is somewhat larger than that required with the race control options used earlier. However, such an initial condition, once again provides faster convergence to steady-state in comparison to the use of race control hypothesis. An input option to use the race control theory, whenever necessary, is, however retained.

4.4.8 Geometrical Imperfections in Modeling Cage/Race Interactions

In all the earlier versions of ADORE, although extensive geometrical imperfections were permitted in the cage pockets, treatments at the guide lands has always been based on ideal geometry. In practice, when the cage, or the interacting race surface, is out-of-round, there are two new problems: (1) the cage can contact the race at more than one point and cause a "lock-up" situation, and (2) contact with the race, on which is cage is not guided, may also become possible. In order to address these situations, the current version implements the following enhancements:

(a) Cage/race interaction module is modified to compute the derivative of geometrical interaction with respect to the angular position, and then determine the number of points where the derivative is zero, or it changes sign. These points define the potential contact points. Therefore, more than one contact point may be easily modeled.

(b) The number of guide lands is now an arbitrary input; the value can be greater than 2. This permits modeling of geometric interaction at the non-guiding race.

(c) ADORE input includes three options for geometric imperfections at the guide lands: (1) elliptical geometry of cage, race or both, (2) sinusoidal variation of radius of cage or race surfaces, and (3) arbitrary geometrical profiles of both the cage and race guide surfaces.

Although all output generated under the above contact conditions is documented in the print output, the plot output is still restricted to the two guide lands which have dominant interactions. In case of multiple contacts, the contact with a larger force is selected for plotting. These restrictions will be lifted in the next revision of the plot program. In the meantime, the option for arbitrary monitoring of output data, in user subroutine ADRX9, may be used and the data can be plotted by using any data processing programs, such as Microsoft Excel.

4.4.9. Arbitrary Traction Data

Very often the user may have experimental traction/slip data obtained at the bearing operating conditions. In such a case it is now possible to compute the traction coefficient by interpolating this data, thus eliminating any uncertainties associated by first computing regression coefficients for a given family of traction curves. This is done in the new user subroutine ADRX7.

The cage geometrical imperfections, specified earlier in ADRX7, are now modeled in ADRX8 and the optional output monitoring is moved to ADRX9.

4.4.10 Moving Reference Frames

A new flag kRotFrames is introduced on input record 3.4 to simulate the effect of moving reference frames as encountered in bearing applications in planetary systems and crank shafts of reciprocating engines. This flag permits rotation of the base bearing frame with a constant veloc-

ity and a fixed radius; these inputs are supplied on new data record 9.4. Again the new inputs have been added to the input facility ADRIN.

4.4.11 Cylindrical Pockets for Roller Bearings

A new cage pocket code, kPocType=-1, has been introduced on record 7.0 to implement cylindrical pockets for roller bearings. This permits simulation of roller guided cages with cylindrical pockets. The output contact angles are included in the plot data files to precisely define position of contacts. Minor modifications to the plot program ADRPB have been made to plot these angles.

4.4.12 Step Size Control During Cage Contacts

When the size of time step is large, either under prescribed inputs or as a result of dynamic step size control, the cage pocket interactions may become quite large or sometimes they may even go out of bounds. To control such an occurrence and model the cage interaction more accurately two enhancements have been made in the current version:

1. The rolling element to cage contact stiffness is refined to make it equivalent to conventional Hertzian contact. This has resulted in a reduction in step size corresponding to an increase in contact stiffness. However, the simulation of rolling element to cage collision if significantly enhanced.

2. In the event of an abnormal contact, an internal error flag is introduced in the rolling element to cage interaction procedure. This flag is seen by the numerical integration procedure, which rejects the solution and starts the integration again with a reduced step.

A combination of the above refinements has added a significant precision to the simulation of rolling element to cage contacts. Such an enhancement is particularly significant when there are a large number of cage pocket interactions, either due to reduced clearances or in the event of an instability. However, these improvements have resulted in a reduction in permissible step size.

4.4.13 Enhancement of ADRX1 Interface

Output as a function of time may now be controlled in the user programmable subroutine ADRX1. The output may be written in any user created data file and later interfaced with other applications and graphics packages. This is particularly helpful when the transient response from ADORE has to be either compared with or implemented in other dynamic models.

In default mode ADORE makes use of symmetry of the bearing and applied loads to save computing effort. However, a generalized programming in ADRX1 may sometimes violate the symmetry rules and thereby produce errors in the solutions. To eliminate such a problem, a symmetry switch kSymetry may now be turned on and off within ADRX1. This switch is stored in the data module SubX, which is generally used in the user programmable subroutines.

4.4.14 Applied Loads and Moments Output

The applied loads and moments in the print output are now divided into two parts: the externally applied loads and moments, and the forces and moments generated internally by the rolling element to race contacts. This helps in better understanding of race accelerations in the dynamic mode. In equilibrium mode, all forces and moments, of course, sum up to zero.

5. Results

After incorporating the program enhancements, outlined in the preceding sections, several test runs were made to demonstrate the enhanced capabilities. Both ball and cylindrical roller bearings are used to perform these test runs. Bearing geometry and the imposed operating conditions are discussed below before presenting the respective results.

5.1 Test Ball Bearing

A typical gas turbine engine 100 mm bore angular contact ball bearing is used to carry out the ball bearing runs. Bearing geometry and operating conditions are presented below in table 5. Actual input data for ADORE and typical print output for the current bearing are documented in Appendix C.

Bearing Bore (m)	0.100	Lubricant Type	MIL-L-7808	
Bearing Outside Diameter (m)	0.180	Traction Model	EHD	
Ball Diameter (m)	0.01905	Cage Friction Coefficient	0.050	
Number of Balls	18	Applied Thrust Load (N)	4,500	
Pitch Diameter (m)	0.140	Applied Radial Load (N)	2,000	
Free Contact Angle (deg)	25.00	Shaft Speed (RPM)	20,000	
Outer Race Curvature Factor	0.52	Room Temperature (K)	323	
Inner Race Curvature Factor	0.54	Outer Race Fit (m)	0.000010	
Cage Outer Diameter (m)	0.146292	Inner Race Fit (m)	0.000050	
Cage Inner Diameter (m)	0.130073	Coolant Type	Lubricant	
Cage/Race Guidance Type	Inner	Coolant Inlet Temperature (K)	323	
Cage Width (m)	0.036241	Coolant Flow Rate (m**3/s)	0.000010	
Cage Guide Land Clearance (m)	0.0015			
Cage Guide Land Width (m)	0.0080			
Cage Pocket Clearance (m)	0.0012			

Table 5: Ball Bearing Geometry and Operating Conditions

5.2 Moment Equilibrium for Angular Contact Ball Bearings

When an angular contact ball bearing is subjected to a combined thrust and radial load, then the contact loads on the balls vary around the bearing. As a result a moment is exerted about the transverse axis. If one of the races is free to move, then the race will misalign to satisfy moment equilibrium. The added moment equilibrium equations in ADORE, permit computation of this misalignment and appropriate change in load distribution. The load distribution solutions obtained by performing such a moment equilibrium are shown in figure 14 and 15 for the outer and inner races respectively. Such a distribution is a result of race misalignment about the transverse axis and it will affect the overall ball motion in the bearing.



Figure 14. Ball/Race load distribution at the outer race contact with aligned and misligned condition resulting from moment equilibrium.

The figures compare the solutions obtained under a perfectly aligned condition to those obtained under a misalignment computed from the moment equilibrium condition.



Figure 15. Ball/Race load distribution at the inner race contact with aligned and misligned condition resulting from moment equilibrium.

5.3 Thermal Interactions in Ball Bearings

Thermal analysis is carried out in two parts. First the bearing simulations are obtained without any modifications to the bearing geometry resulting from the change in temperature of the various bearing elements. Since the thermal model in ADORE does not perform any thermal transients, the heat generation at the various interactions is averaged over a prescribed time and then a new temperature field is computed. Thus the temperatures are updated at selected times. In the present example the heat generations are averaged over every ten shaft revolutions. The overall results of the simulation obtained under the conditions outlined in table 5 are shown in figures 16 to 23.

Figure 16 shows the variation in total heat generation or powerloss in the bearing. After the initial transients the heat generation stabilizes to a fairly constant value. The overall mechanical

interaction between the bearing elements is indicated by the time-averaged wear rate plotted in figure 17. As the simulation reaches steady-state these rates stabilize to a well defined constant value. Overall bulk temperatures as computed by the thermal models are shown in figure 18, while details of a typical ball/race interaction are shown in figure 19, which shows the local contact heat generation, the temperature rise in the contact, and the estimated race contact temperatures. The race contact temperatures are output of the thermal model where the local heat generations are averaged over a shaft revolution. Note that the race contact temperatures, along with other bulk temperatures shown in figure 18, change in steps. This is a result of the thermal averaging procedure.

Cage motion is shown in figure 20 to 23. Figure 20 shows the variation in cage mass center velocity. Clearly, the cage whirls at a fairly constant velocity with practically no radial velocity. The resulting cage/race forces are shown in figure 21, which shows that after the initial transient there is little or no contact at the guide land. This is also confirmed by the orbit radius being less than the cage/race clearance as shown in figure 22. The dotted circle in figure 22 denotes the clearance circle. Typical interaction in cage pockets is shown in figure 23. The balls occasionally contact the cage pockets over very short times. This is typical of cage pocket contacts in most bearings.



Figure 16. Overall powerloss in the test ball bearing with no thermal interactions.



Figure 17. Time-averaged wear rates in the test ball bearing with no thermal interactions.



Figure 18. Computed bulk temperatures with no change in bearing geometry.



Figure 19. Typical ball/race interaction with no change in internal geometry.



Figure 20. Ball bearing cage mass center velocities in absence of any thermal interactions.



Figure 21. Ball bearing cage/race contacts in absence of any thermal interactions.



Figure 22. Ball bearing cage mass center whirl orbits in absence of any thermal interactions.



Figure 23. Typical ball/cage contacts in absence of any thermal interactions.

In the second set of results the internal bearing geometry is updated corresponding to the computed bulk temperatures. Also averaging of thermal parameters is now carried out at every shaft revolution. Sudden change in geometry can sometimes lead to a drastic change in bearing interactions. Therefore, considerable care is necessary to handle the mechanical transients when computing the thermal interactions and the resulting change in bearing geometry. Since initially there are fairly high mechanical transients, which are basically a result of the imposed initial conditions, it is quite appropriate to not apply any geometrical changes until some of these transients die out. This is particularly reasonable since the thermal analysis is free of any transients. In the present example, no change in bearing geometry is applied for the first ten shaft revolutions. However the thermal analysis and computation of temperature fields are carried out at each revolution. After the first ten revolutions change in bearing geometry is computed and applied at every shaft revolution. When geometrical changes are applied the bearing internal clearance will change and this may cause a change in applied loads if the races are held at a fixed position. In the example considered here, an equilibrium constraint is applied to move the races and maintain the thrust and radial loads equal to the initially applied values. Thus the applied loads are constant even with the changing bearing geometry.

The overall power loss after accounting for all geometrical changes is basically unchanged as shown in figure 24, and so are the overall mechanical interactions as shown by the time-averaged wear plots in figure 25. The bulk temperatures, after some cyclic variations, stabilize to fairly constant values as seen in figure 26. Local interactions in the ball/race contacts, shown in figure 27, are basically identical to those shown earlier in figure 19. This is primarily due to identical load conditions.

Changes in cage motion due to subtle geometrical changes, are also minimum when the applied loads remain constant. The overall whirl variation, cage/race contacts, whirl orbits and pocket interactions are shown respectively in figure 28, 29, 30 and 31, respectively.

The above results show that when the applied loads are maintained constant, the subtle changes in bearing geometry resulting from thermal interactions do not change the overall bearing behavior. If however, the races are held in a fixed position and the applied loads are permitted to change, there may be a significant change in bearing behavior. The simulations obtained by ADORE will certainly predict such changes in bearing behavior. However, significant experimental validations of such predictions are essential before such predictions may be used in practical design. Such simulations are therefore deferred until some experimental data becomes available.

Another limitation of the current modeling procedures related to the effect of traction as a function of temperature. Although the Newtonian elastohydrodynamic model computes a fairly rigorous temperature and shear stress distribution through the lubricant film, the input rheological constants are derived by regression analysis experimental traction data obtained over a rather limited range of temperature. Thus extrapolation of these model constants over a wider range of temperatures may introduce certain uncertainties. In view of such limitations in the model, the traction model constants are presently not subject to change as the bulk temperatures of the bearing elements vary. However, once reliable data for the traction model coefficients becomes available, elimination of these constraints is straightforward.



Figure 24. Ball bearing poer loss with time-varying bearing geometry due to thermal effects.



Figure 25. Time-averaged wear rates for the ball bearing with geometrical distortions due to thermal effects.



Figure 26. Computed bulk tempeeratues in the ball bearing with thermal effects.



Rolling Element / Race Interaction: Set #3

Figure 27. Typical ball/race interactions with thermal effects.



Figure 28. Ball bearing cage mass center velocities with changing bearing geometry as a result of thermal effects.


Figure 29. Ball bearing cage/race contacts with thermal effects.



Figure 30. Ball bearing cage mass center whirl orbits with thermal effects.



Figure 31. Typical ball/cage interactions with applied thermal effects.

5.4 Test Cylindrical Roller Bearing

A small 30 mm high speed cylindrical roller bearing with ceramic rollers is considered as the test roller bearing. The bearing geometry and operating conditions are described below in table 6.There is no coolant in the bearing, except ambient air.

Tuble 6. Cymarical Roher Dearing Geometry and Operating Conditions			
Bearing Bore (m)	0.030	Lubricant Type	Arbitrary
Bearing Outside Diameter (m)	0.055	Traction Model	Figure 5-19
Number of Rollers	8	Cage Friction Coefficient	0.050
Roller Diameter (m)	0.0080	Applied Radial Load (N)	1,000
Roller Length (m)	0.0080	Shaft Speed (RPM)	70,000
Central Land Width (m)	0.0020	Room Temperature (K)	294
Crown Radius (m)	0.250	Outer Race Fit (m)	0.
Corner Radius	0.000250	Inner Race Fit (m)	0.000020
Internal Diametral Clearance (m)	0.000040		
Pitch Diameter (m)	0.0430		
Cage Outer Diameter (m)	0.0450	Coolant Type	Ambient Air
Cage Inner Diameter (m)	0.040		
Cage/Race Guidance Type	Outer		
Cage Width (m)	0.010		
Cage Guide Land Clearance (m)	0.00010		
Cage Guide Land Width (m)	0.0010		
Cage Pocket Clearance (m)	0.00010		

 Table 6: Cylindrical Roller Bearing Geometry and Operating Conditions

An arbitrary traction model, simulating solid lubrication is assumed, with relatively high traction coefficients. ADORE option for an arbitrary traction slip relation is used to prescribe the traction model. The relationship prescribed in shown in figure 32. Detailed input data to ADORE and typical print output corresponding to the present bearing are summarized in Appendix D.



Figure 32. Traction-Slip relation for the test roller bearing.

5.5 Thermal Interactions Cylindrical Roller Bearing

Thermal modeling, once again, is carried out in two parts. First the heat generation is averaged over a shaft revolution and no change in bearing geometry is assumed. Typical results are shown in figures 33 to 38.

The overall heat generation in this bearing under the prescribed operating conditions is quite low as shown in figure 33. The peaks in the curve are a result of roller/cage contacts while the small humps are due to cage/race contacts. As may be expected, he temperature change under such conditions is small, as seen in figure 34. The small step change in bulk temperatures at every shaft revolution is a result of the thermal analysis. Note that there is no circulating coolant in this bearing except for ambient air. The fluid exit temperature, therefore represents the ambient air temperature near the rolling elements. Details of the local thermal interactions at the roller/race contacts are shown in figure 35. Again the temperature rise in the contact and the change in race temperatures at the contact are small due to low value of heat generation.



Figure 33. Roller bearing powerloss with no thermal effects.



Figure 34. Computed bulk temperatures in the roller bearing with no thermal effects.



Figure 35. Typical roller/race interactions with no thermal effects.

Cage interactions are also minimum. Mass center whirl is practically unchanged from the initially prescribed circular motion. Small variations in whirl velocity, the cage/race forces and the whirl orbits are shown in figures 36, 37 and 38 respectively.

In the next simulation, internal bearing geometry is updated corresponding to the computed temperature field. Again the heat generation is averaged over every shaft revolution and after computing the temperatures the bearing geometry is updated. Again at each instant of altered temperatures a quasi-static constraint is applied to maintain the applied radial load at the initially prescribed value. Primarily due to rather low value of overall heat generation, the roller/race contacts are practically unchanged. The overall power loss, computed bulk temperatures and typical roller/race interactions are shown respectively in figures 39, 40 and 41.

Cage motion resulting from the modified cage/race clearance with varying temperatures is perhaps more significant. The whirl velocity variation is slightly larger, as seen in figure 42. This is probably due to the increase cage/race interaction, as shown by the guide land force variation plotted in figure 43. Mass center whirl still remains circular, as seen in figure 44, although there is a small shift from the initial circular orbit.

Again it must be remembered that the predicted changes in bearing performance as a function of changing geometry due to thermal effects must be validated experimentally before attaching a significant design significance to them. In addition, the roller/race traction relation may also vary significantly with changing race and/or roller temperatures. Again, these models are inputs to ADORE and significant experimental development is necessary before the thermal modeling procedures, as implemented in ADORE, may be effectively used for practical bearing design.



Figure 36. Roller bearing cage mass center velocities with no thermal effects.



Figure 37. Cage/race contacts in the roller bearing with no thaermal effects.



Figure 38. Roller bearing cage whirl orbits with no thermal effects.



Figure 39. Roller bearing powerloss with all thermal effects.



Figure 40. Computed roller bearing bulk temperatures with changing bearing geometry as a rsult of thermal effects.



Figure 41. Typical roller/race contacts in the cylindrical roller bearing with changing bearing geometry due to thermal effects.



Figure 42. Change in cage mass center velocities in the roller bearing with changing bearing geometry as a result of thermal effects.



Figure 43. Increased cage/race forces in the roller bearing with thermal effects.



Figure 44. Cage mass center whirl in the roller bearing with thermal effects.

6. Conclusions

Based on the thermal modeling procedures developed in the current investigation and the preliminary parametric modeling of bearing performance it may be concluded that implementation of thermal interactions on overall bearing dynamics may be accomplished in three parts: first the computation of internal heat generation by precise and numerically accurate integration of mechanical interactions in the bearing; second computation of temperature field from transport of the internally generated heat to rest of the system; and finally an implementation of a change in bearing geometry and altered friction or traction conditions as a function of temperature. All of these steps, except changing traction with temperature, have been carried out in the present investigation. although implementation of time-varying traction models is straightforward, the required inputs require significant experimental development.

A step wise implementation of thermal effects seems to provide satisfactory results when the thermal model is free of any transients. The computed heat generation at each time step is averaged over a prescribed time interval before computing the thermal interactions and any changes in bearing geometry as a result of newly computed temperature field. In addition, any external constraint, such as equilibrium, may be imposed when the geometry is updated. Although such an implementation results in a step change in bearing performance parameters, no truncation errors in the integration of equations of motion are introduced when an explicit integration method is used. Thus the integrated solutions are numerically stable.

Parametric bearing performance simulations also show that when the traction characteristics are held constant the overall bearing performance as a function of changing internal geometry, due to thermal distortions, may not be significant if the bearing races are permitted to move and the applied loads are maintained at a constant value. Thus external systems constraints may be significant in thermal modeling of rolling bearing dynamics.

The computer models developed in the present investigation have been numerically tested for precision and convergent integration. The models are, therefore, very reliable for carrying out parametric or sensitivity studies to model overall effect of a given design parameter. However, significant experimental validation of the predicted results must be carried out before implementation of the computed results in practical designs.

7. Recommendations for Future Development

As a result of the modeling work carried out in the present investigation, several recommendations for further enhancements of the models may be made:

1. Experimental work leading to a more precise correlation of traction behavior with temperature is essential in overall rolling bearing dynamics. Once such data becomes available for potential lubricants, inputs to the current models can be significantly improved by varying traction as a function of computed temperatures.

2. Overall experimental validation of predicted results, such as bearing heat generation and computed temperatures fields is essential before the model can be reliably used for practical design and performance diagnosis. Since such investigations do not require measurement of any complicated motions within the bearings, they should be relatively easy to carry out.

3. Once thermally dependent traction is implemented and the model predictions have been experimentally validated, the model becomes an efficient tool for parametric studies leading classification of thermally induced phenomena, such as instabilities in bearing element motion. Such parametric studies may provide substantial guidance for practical bearing design and materials development.

4. The issue of thermal transients is another area where additional modeling work may be recommended. Since the time scales for thermal and mechanical interactions are greatly different, it may not be numerically efficient to integrate the generalized differential equations. However, once the models have some experimental validations, adequate number of parametric studies may be carried out to develop guidance for numerically averaging the thermal interactions, as arbitrarily carried out in the present investigation.

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Appendix A - Typical ADORE Data Module

module BrgGeom 1 - - -This module contains all geometrical data for the bearing use Parameters overall bearing implicit none run identification string (max 36 chars) character*36 :: runId ! bearing type, defined as ! 1 = ball bearing ! 2 = cylindrical roller bearing integer :: kBrg =0 ! 3 = spherical roller bearing
! 4 = tapered roller bearing ! 5 = spherical tapered roller bearing ! re/race contact type defined as follows --! 0 = point contact (ball,sph roller/grooved race) !-1 = point contact (flat race/crowned roller) integer, dimension(2, maxRe) :: kConType =0 !-2 = point contact (crowned race/flat roller) !-3 = point contact (crowned race/crowned roller) ! 1 = line contact number of rolling elements bearing bore (ID of inner race) integer :: nRe = 0real(r8) :: brgBore =0. real(r8) :: brgOD =0. ! bearing outer diameter :: hsngOD =0. shaft inner diameter (hollow shaft) real(r8) housing outer diameter real(r8) 1 real(r8) :: freeIntCls =0. unmounted bearing internal clearance 1 ! unmounted bearing contact angle (ball brgs only) ! unmounted end play (ball bearings only) ! bearing pitch diameter :: freeConAng =0. real(r8) real(r8) :: freeEndPlay real(r8) :: pitchDia =0. integer :: nTE =0 total number of bearing elements (re+cage+race) average of outer and inner race taper angles initial transformation from inertial azimuth to real(r8) :: reAx real(r8),dimension(3,3) :: reBaseTran 1 ! rolling element coordinate frame, corresponding to ! initial orientation of rolling elements rolling element data 1 real(r8) :: bReDia =0 ! nominal rolling element diameter diameter at large end for tapered roller brgs variation in rolling element diameter [1] real(r8),dimension(maxRe) :: reDia =0. real(r8),dimension(maxRe) :: reDiaVar =0. variation in diameter at large end for tapered bearings real(r8),dimension(maxRe) :: reRad =0. rolling element radius [1] (mean rad for tapered brg) nominal roller length real(r8) :: bReLen =0. :: reLen =0. :: reLenVar =0. roller length [1] variation in roller length [1] real(r8),dimension(maxRe) real(r8), dimension(maxRe) nominal roller crown radius real(r8) :: bReCrn =0. real(r8),dimension(maxRe) :: reCrn =0. :: reCrnVar =0. roller crown radius [1] variation in roller crown [1] real(r8), dimension(maxRe) real(r8),dimension(2,maxRe) :: reCurCen =0. rolling element cur center (axial & radial comp) relative to rolling element geometric center nominal central land length on roller :: bReCenLen =0. real(r8) real(r8), dimension(maxRe) central land half length on roller [1] :: reCenLen =0. :: reCenLenVar =0. :: reCenLenOffset =0. real(r8),dimension(maxRe)
real(r8),dimension(maxRe) variation in central land length on roller [1] axial offset of central land [1] real(r8),dimension(maxRe) crown drop on central land [1] :: reCenCrnDrop =0. limit on major contact halfwidth [2] axial coordinate limits corresponding to central land real(r8),dimension(2,maxRe)
real(r8),dimension(2,maxRe) :: reConLmt :: reCenLmt real(r8), dimension(2, maxRe) :: reCur =0 rolling element curvatures [2] rad of deformed pressure surface at outer and inner race contact :: rePrRad =0. real(r8), dimension(2, maxRe) nominal semi taper angle of rollers semi taper angle of rollers [1] variation in semi taper angle of rollers [1] :: bReTaper =0. real(r8) real(r8),dimension(maxRe)
real(r8),dimension(maxRe) :: reTaper =0. :: reTaperVar =0. real(r8),dimension(maxRe) :: reTanTaper =0. tangent of roller taper angle [1] real(r8),dimension(maxRe)
real(r8),dimension(2) :: reCosTaper =1._r8
:: bReCorRad =0. cosine of roller taper angle [1]
nominal corner radii on neg & pos roller axis real(r8), dimension(2, maxRe)
real(r8), dimension(2,2, maxRe)
real(r8), dimension(2,2, maxRe) :: reCorRad =0. roller corner radii [3] roller corner center position [32] variation in roller corner radii [3] :: reCorCen =0. :: reCorRadVar =0. real(r8),dimension(2) :: bReEndRad =0. nominal end radii on neg & pos roller axis real(r8),dimension(2,maxRe)
real(r8),dimension(2,maxRe) :: reEndRad =0. roller end radii [3] axial position of roller end center [33] :: reEndCen =0. variation in roller end radii [3] transformation angles for roller end face real(r8),dimension(2,maxRe) :: reEndRadVar =0. :: reEndFrame =0. real(r8), dimension(3,2, maxRe) orientation [4] trans from roller geo to end face coords [34] base mass (nominal rolling element mass) base roll element moment of inertia real(r8),dimension(3,3,2,maxRe) :: tre :: bReMass =0. real(r8) real(r8), dimension(3) :: bReMI =0. i real(r8), dimension(3) :: bReGeoCen =0. ! base roll element geom center rel to mass center

```
! base roll element principal frame orientation ! principal frame rel to geometric frame
           real(r8),dimension(3)
                                                                                                   :: bReFrame =0.
                                                                                                                                                    rolling element geom center rel to geometric frame
rolling element geom center rel to mass center[5]
rolling element moment of inertia [5]
orientation of rolling element principal axes [6]
re geometrical to principal frame transformations
           real(r8),dimension(3,maxRe)
real(r8),dimension(maxRe)
real(r8),dimension(3,maxRe)
                                                                                                   :: reGeoCen =0.
                                                                                                    :: reMass =0.
                                                                                                   :: reMI =0.
           real(r8),dimension(3,maxRe)
real(r8),dimension(3,3,maxRe)
                                                                                                   :: reFrame =0.
                                                                                                    :: reGeoToPrin
I race data
                                                                                                                                                  ! race curvature factors [7]
! race land semi taper angle [7]
! tangent of race semi taper angle [7]
           real(r8),dimension(2)
                                                                                                   :: raceCurFac =0.
           real(r8),dimension(2)
real(r8),dimension(2)
                                                                                                   :: raceTaper =0.
                                                                                                   :: raceTanTaper =0.
           real(r8),dimension(2)
                                                                                                   :: raceCosTaper =1._r8
                                                                                                                                                      cosine of race semi taper angle (7)
                                                                                                                                                      race cross groove curvature (1/radius) [7]
race cross groove rad of cur for ball, spherial
           real(r8),dimension(2)
real(r8),dimension(2)
                                                                                                   :: raceCur =0.
                                                                                                   :: raceCurRad =0.
                                                                                                                                                      race cross groove rad of cur for ball, spherial
and tapered spherical roller bearings
axial and radial pos of race curvature center [12]
race surface crown used for cyl and tapered roller brgs
half length of central land on races [7]
race crown drop on central land [7]
limiting length on race for roller interaction [7]
width of races [7]
           real(r8),dimension(2,2)
real(r8),dimension(2)
                                                                                                   :: raceCurCen =0.
                                                                                                   :: raceCrn
           real(r8),dimension(2)
real(r8),dimension(2)
real(r8),dimension(2)
real(r8),dimension(2)
                                                                                                   :: raceCenLen =0.
                                                                                                   :: raceCenCrnDrop =0.
                                                                                                    :: raceLandLmt =0.
           real(r8),dimension(2)
real(r8),dimension(2,2)
real(r8),dimension(3,2)
                                                                                                   :: raceWidth =0.
:: raceRad =0.
                                                                                                                                                      width of races [7]
radius of race surface at mid point [31]
race out-of-round variation [35]
                                                                                                   :: rlRadVar =0.
                                                                                                                                                     race curvature factor variaion [35]
race central land offset [35]
race land taper variaton [35]
           real(r8),dimension(3,2)
real(r8),dimension(3,2)
real(r8),dimension(3,2)
real(r8),dimension(3,2)
                                                                                                   :: cFacVar =0.
:: rlOffset =0.
                                                                                                   :: rlTaper =0.
:: raceGeoCen =0.
          real(r8),dimension(3,2)
real(r8),dimension(2)
real(r8),dimension(3,2)
real(r8),dimension(3,2)
                                                                                                                                                      race geometric center rel to it masscenter [9] equivalent race mass [7]
                                                                                                    :: raceMass =0.
                                                                                                                                                  : equivalent race mass [7]
! race principal moment of inertia [9]
! orientation of race principal axes relative
! to its geometric frame [10]
! race geometrical to principal frame transformation
! race indices, element numbers
                                                                                                   :: raceMI =0.
                                                                                                   :: raceFrame =0.
           real(r8),dimension(3,3,2)
integer,dimension(2)
                                                                                                   :: raceGeoToPrin
                                                                                                   :: mRace(2)
! guide flange data
1 -
                                                                                                                                                  ! guide flange origin rel to race geo center [11]
! race flange identifier [13]
! (0-no flange, 1=flange present)
! sum of flngInd for outer and inner races
! sum of all components of flngInd
! guide flange height [13]
! guide flange height [13]
! guide flange lay back angles [13]
! flange clearance (cyl brg only) [7]
! transformation from race azimuth to flange coordinates
           real(r8),dimension(2,2,2)
                                                                                                   :: flngOrigin =0.
           integer, dimension(2,2)
                                                                                                   :: kFlngInd =0
            integer, dimension(2)
                                                                                                   :: kFlngIndr =0
           integer
                                                                                                   :: kFlngInds =0
           real(r8), dimension(2,2)
                                                                                                   :: flngHt =0.
           real(r8), dimension(2,2)
real(r8), dimension(2)
real(r8), dimension(3,3,2,2)
                                                                                                   :: flngAng =0.
:: flngCls =0.
                                                                                                   :: traf
! cage data
! -
                                                                                                                                                  ! number of cage segments
! cage segment indices, element numbers
! cage pocket identifier
           integer
                                                                                                   :: nCseg =0
           integer,dimension(maxCseg)
                                                                                                   :: mCage
           integer
                                                                                                   :: kPocType =0
                                                                                                                                                      for ball bearaings:
 0=cylindrical,
                                                                                                                                                                                                           1=spherical
                                                                                                                                                        2=elongated cylindrical, 3=conical
                                                                                                                                                      4=rectangular
for roller bearings: 0=rectangular
                                                                                                                                                      for roller bearings: 0=rectangular
positive nonzero value, n, defines pairs of
pocket interaction surfaces located symetrically
relative to the pocket center, (maximum 5)
=-1 cylindrical pocket, roller guided cage
                                                                                                                                                      pocket contact type, assigned in Adra2
number of guide surfaces in cage pocket
cage outer and inner diameter
           integer
                                                                                                   :: kPocConType
:: nPocSur =1
           integer, dimension(maxRe, maxCseg)
           real(r8),dimension(2,maxCseg)
                                                                                                   :: cageDia =0.
                                                                                                                                                      outer and inner radius of cage
cage width
           real(r8),dimension(2,maxCseg)
real(r8),dimension(maxCseg)
                                                                                                   :: cageRad =0.
:: cageWidth =0.
                                                                                                                                                      angular width of cut for segmented cage
           real(r8)
                                                                                                   :: cageAngCut =0
           real(r8),dimension(maxCseg)
integer
                                                                                                   :: cageConeAng =0.
:: nGL
                                                                                                                                                      cage semi-cone angle for tapered roller bearings
number of cage/race guide lands, maximum value set
                                                                                                                                                      by parameter maxGL in the Parameters module
                                                                                                                                                      cage guidance type (1=outer, 2=inner) [14]
diameters at cage guide surface [14]
           integer, dimension(maxGL,maxCseg)
real(r8),dimension(maxGL,maxCseg)
                                                                                                   :: iCageGuide =0
:: cageGsDia =0.
                                                                                                                                                      radius at cage guide surface [14]
cage guide surface diametral clearances [14]
cage guide surface width [14]
           real(r8),dimension(maxGL,maxCseg)
                                                                                                   :: cageGsRad =0.
           real(r8),dimension(maxGL,maxCseg)
real(r8),dimension(maxGL,maxCseg)
                                                                                                   :: cageGsCls =0.
:: cageGsWidth =0.
                                                                                                                                                      axial pos of outer edge of guide surface from cage center
inverse of cls value used to scale mass center position
nominal diametral pocket clearances
           real(r8),dimension(maxGL,maxCseg)
                                                                                                    :: cageGsPos =0.
                                                                                                   :: cageGsClss =0.
:: bPocCls =0.
           real(r8),dimension(maxCseg)
real(r8),dimension(2,maxCseg)
           real(r8),dimension(maxGL,maxCseg)
real(r8),dimension(3,maxGL,maxCseg)
real(r8),dimension(3,maxGL,maxCseg)
                                                                                                   :: raceGsRad =0.
:: cageGsRadVar =0.
:: raceGsRadVar =0.
                                                                                                                                                      race guide surface radius
cage guide land radius variation (amp,freq & phase)
race guide land radius variation (amp,freq & phase)
           real(r8),dimension(2,maxRe,maxCseg)
real(r8),dimension(2,maxRe,maxCseg)
real(r8),dimension(2,maxCseg)
                                                                                                                                                      radial (diametral/2) pocket clearances [15]
variation in pocket diametral clearances [15]
cage outer and inner diametral clearances for churning
                                                                                                   :: pocCls =0.
                                                                                                   :: pocClsVar =0.
:: cageCls =0.
                                                                                                                                                        calculations
                                                                                                                                                      calculations
cage pocket radius [15]
or circumferential pocket width for rect pockets
axial pocket width for rect pockets [15]
nominal pocket guide surface orientation relative to
nominal pocket surface orientation [16]
                                                                                                    :: pocRad =0.
           real(r8), dimension(maxRe, maxCseq)
           real(r8),dimension(maxRe,maxCseg)
real(r8),dimension(3,maxPgs,maxCseg)
                                                                                                    :: pocWidth =0.
                                                                                                    :: bPocGsAng =0.
           real(r8), dimension(3, maxPgs, maxCseg)
                                                                                                   :: bPocGsCen =0.
                                                                                                                                                  ! nominal coordinates of pocket guide surface center
```

		! rel to nominal pocket center [17]
real(r8),dimension(2,maxPgs,maxCseg)	:: bPocGsLen =0.	! nominal pocket guide surface lengths[18]
real(r8), dimension(3, maxPqs, maxRe, maxCseq)	:: pocGsAng =0.	! pocket quide surface angles relative to nominal
,	Feeering	! pocket surface orientation [19]
real(r8),dimension(3,3,maxPgs,maxRe,maxCseg	() :: pocToGs = 0	! cage pocket to guide surface transformation
real(r8), dimension(3, maxPqs, maxRe, maxCseq)		! variations in pocket quide surface angles [19]
real(r8), dimension(3, maxPgs, maxRe, maxCseg)		! coordinates of guide surface center [20]
real(r8), dimension(3, maxPqs, maxRe, maxCseq)		! variation in coordinates of quide surface
1041(10) / 41. (Chip 101 (C) / Marine 50 / Marine 7 (Marine 50)	poodboomvar of	! center [20]
<pre>real(r8),dimension(2,maxPgs,maxRe,maxCseg)</pre>	:: pocGsLen =0	! width of pocket guide surfaces [21]
real(r8), dimension(2, maxPqs, maxRe, maxCseq)		! variation in with of pocket quide surfaces [21]
real(r8), dimension(2,4, maxPgs, maxRe, maxCseg		! pocket guide surface corner coordinates (x & z comp
	:: pocCen =0.	! pocket center relative to cage geometric
rear(ro), armenbron(o, maxic, maxebeg)	poccell =0.	! center [22]
real(r8),dimension(3,maxRe,maxCseq)	:: pocAng =0.	! pocket orientation [23]
real(r8), dimension(maxRe, maxCseg)	:: pocConeAng	! semi cage pocket cone angle for conical pockets
real(r8), dimension(maxRe, maxCseg)	:: sPocConeAng	! sine of semi cage pocket cone angle
real(r8), dimension(maxRe, maxCseg)	:: cPocConeAng	! cosine of semi cage pocket cone angle
real(r8), dimension(3,3, maxRe, maxCseg)	:: cageToPoc	! cage to pocket transformation
	:: pocThkns =0.	pocket thickness along the radial direction [24]
real(r8), dimension(maxRe, maxCseg)	:: pocThknsVar =0.	! variation in pocket thickness
real(r8), dimension(maxRe, maxCseg)	:: pocWidthVar =0.	! variation in pocket width in axial direction
real(r8), dimension(2, maxRe, maxCseg)	:: pocCenVar =0.	! variation in axial & circum coordinate of pocket ce
real(r8), dimension(2, maxRe, maxCseg) real(r8), dimension(3, maxRe, maxCseg)		! variation in pocket angular orientation (y & z rots
	:: pocAngVar =0.	
real(r8), dimension(2, maxRe, maxCseg)	:: pocLimT =0.	! angles theta defining pocket surface limits [25]
real(r8),dimension(2,maxRe,maxCseg)	:: pocLimP =0.	! angles phi defining pocket surface limits
real(r8), dimension(2, maxRe, maxCseg)	:: pocLimZ =0.	! z-coordinate limits defining pocket surface limits
real(r8),dimension(maxRe,maxCseg)	:: pocConLimB =0.	! limit on contact half width for roller brg pockets
	:: bCageMass =0.	! base cage segment mass
real(r8), dimension(maxCseg)	:: cageMass =0.	! mass of cage segment [26]
real(r8),dimension(3,maxCseg)	:: cageGeoCen =0.	! cage geometric center relative to its mass ! center [27]
real(r8),dimension(3,maxCseg)	:: cageFrame =0.	! orientation cage princial frame rel to its ! geometric frame [28]
real(r8),dimension(3,3,maxCseq)	:: cageGeoToPrin	! cage geometric to principal frame transformation
real(r8), dimension(3)	:: bCageMI =0.	! base cage moment of inertia
	:: cageMI =0.	! cage principal moment of intertia [29]
	:: iPocRe =0	! rolling element identifier for a pocket [30]
	:: nPoc =0	! number of pockets in cage segments
	:: cseqLen =0.	! cage segment length in degrees
	:: pocFrac	! extent of effective fractional pocket area for
10d1(10)/d1menb10n(manne/manobeg)	Pool 2 do	
		! for rolling element interaction 1.0=full pocket
TES		
		l ha a mata na sheka da na sana ha sabata i mbana
escription of dimensional indices in the abov otes are documented in the table below:	re arrays is indicated	by a note number is squares brackets. These

Note #	Dim Index #	Max Limit	Index Description
1	1	nRe	rolling element #
2	1	2	along and normal to rolling direction
	2	nRe	rolling element #
3	1	2	negative and positive roller axis
	2	nRe	rolling element #
4	1	3	x,y,z rotations
	2	2	negative and positive roller axis
	3	nRe	rolling element #
5	1	3	x,y,z components
	2	nRe	rolling element #
6	1	3	x,y,z rotations
	2	nRe	rolling element #
7	1	2	race # (1=outer, 2=inner)
7a	1	2	axial and radial position
	2	2	race # (1=outer, 2=inner)
8	1	2	along and normal to rolling directi
-	2	2	race # (1=outer, 2=inner)
9	ĩ	3	x,y,z components
-	2	2	race # (1=outer, 2=inner)
10	1	3	x,y,z rotations
10	2	2	race # (1=outer, 2=inner)
11	1	2	axial and radial components
	2	2	negative and positive x-axis
	3	2	race # (1=outer, 2=inner)
12	1	2	axial and radial components
	2	2	race # (1=outer, 2=inner)
13	ĩ	2	negative and positive x-axis
	2	2	race # (1=outer, 2=inner)
14	1	2	negative and positive x-axis
15	ī	nRe	pocket #
10	2	nCseq	cage segment #
16	1	3	x,y,z rotations
10	2	numPqs	pocket guide surface #
17	1	3	x,y,z components
	2	numPqs	pocket guide surface #
18	1	2	normal and along roller axis
10	2	numPqs	quide surface #
19	1	3	x,y,z rotations
17	2	numPqs	guide surface #
	3	nRe	pocket #

	4	nCseg	cage segment #
20	1	3	x,y,z components
	2	numPgs	guide surface #
	3	nRe	pocket #
	4	nCseg	cage segment #
21	1	2	normal and along roller axis
	2	numPgs	guide surface #
	3	nRe	pocket #
	4	nCseq	cage segment #
22	1	3	x,y,z components
	2	nRe	pocket #
	3	nCseq	cage segment #
23	1	3	x,y,z rotations
	2	nRe	pocket #
	3	nCseq	cage segment #
24	1	nRe	pocket #
	2	nCseq	cage segment #
25	1	2	two angles, rotaton about z and x-axes
20	2	nRe	pocket #
	3	nCseq	cage segment #
26	1	nCseq	cage segment #
27	1	3	x, y, z components
27	2	nCseq	cage segment #
28	ī	3	x, y, z rotations
20	2	nCseq	cage segment #
29	1	3	x,y,z components
20	2	nCseq	cage segment #
30	1	nRe	pocket #
50	2	nCseq	cage segment #
31	1	2	race radius at mid point of contact surface (1=outer, 2=inner)
21	2	2	race # (l=outer, 2=inner)
32	1	2	axial position of roller corner center rel to geo center (1=neg axis, 2=pos ax
52	2	2	radius of roller corner center locus (1=neg axis, 2=pos axis)
	3	maxRe	rolling element index
33	1	2	axial position of roller end center rel to geo center (1=neg axis, 2=pos axis)
33	2	maxRe	rolling element index
34	1,2	3	transformation matrix from roller geo to end face coordinate system
34	3	2	
	3	-	1=neg axis, 2=pos axis
35	4	maxRe 3	rolling element index
20			1=magnitude, 2=frequency of variation and 3=phase shift from principal frame
	2	2	1=outer race, 2=inner race.

Appendix B - Typical ADORE Code Segment

subroutine Adrc1

Adrc1 rolling element/race normal		
use Parameters use BrgGeom use Constants		
use VecMats use ReVecs use LoadDer use Solutions		
use OpCond use SubX use TmpArea		! used in LineContact
use FatigueCons use Errors use ErrorCodes use FlngData use SetUpB1 implicit none		! used in LineContact ! used in NewContLmts ! used in NewContLmts ! used in FlngContact ! store results for use in AdrB1
local variables:		
<pre>integer integer real(r8),dimension(3,3) real(r8),dimension(3,3) real(r8),dimension(3)</pre>	:: j :: k,l,ll :: tib :: tbra :: bgi :: rgi	! race index ! loop indices ! inertial to re frame transformation ! roll ele to race azimuth transformation ! re geo center in intertial frame
<pre>real(r8),dimension(3) real(r8),dimension(3) real(r8),dimension(3) real(r8),dimension(3) real(r8),dimension(3)</pre>	:: bgrgi	<pre>! race geo center in intertial frame ! re geo center rel to race geo center in intertial frame ! re geo center rel to race geo center in race azimuth fram ! race cur center rel to race geo center in race azimuth fra ! re cur center rel to re geo center in race frame ! re cur center rel to re geo center in race azimuth frame ! re cur center rel to re geo center in race azimuth frame ! re cur center rel race cur center in race azimuth frame</pre>
<pre>real(r8),dimension(3) real(r8),dimension(3) real(r8),dimension(3) real(r8)</pre>	:: sbs1,cbs1 :: si	! sine and cosine of inertial azimuth angle ! azimuth angle
real(r8) real(r8) real(r8) real(r8) real(r8)	:: Adrb3,Adrx6	! sine and cosine of azimuth angle ! race radius variation ! race curvature factor variation ! local variables ! define function types
these variables are computed in LCI and used in LineContact procedure		
<pre>real(r8),dimension(4)</pre>	:: delQbj	! derivative of load with roller displacements
<pre>real(r8),dimension(4)</pre>	:: delMbj	! x, r, ang2 and ang3 ! derivaatie of moment with roller displacements ! x, r, ang2 and ang3
<pre>real(r8),dimension(5)</pre>	:: delQrj	! derivative of load with race displacements ! X, Y, Z, ang2 and ang3
<pre>real(r8),dimension(5)</pre>	:: delMrj	! derivative of moment with race displacements ! X, Y, Z, ang2 and ang3
rolling element geo center and base		
tia=inertToIaz(:,:,ire) cbsi=tia(3,3) sbsi=tia(2,3)		! inertToIaz,inertToRe,reToIaz->VecMats
<pre>bgi=reGci(:,ire) tib=inertToRe(:,:,ire) tbia=reToIaz(:,:,ire) if (ider /= 0) then call Adrb22(sinBt(:,ire),cosBt) call Adrb23(sinBt(:,ire),cosBt) end if</pre>		<pre>! roll ele geo center in intertial frame ! inertial to rolling element frame transformation ! roll ele to azimuth frame transformationation, tbia->ReV ! ider->LoadDer ! sinBt,cosBt->ReVecs</pre>
start race loop		
idFlngSol=0 reEndWR(1,ire)=zero reEndWR(2,ire)=zero		! initialize flange solution indicator, idFlngSol->Solution ! initialize roller end wear, reEndWR->Solutions
reFlngFor=zero reFlngMom=zero raceFlngFor=zero raceFlngMom=zero		! flange force vector on roll elements, reFlngFor->ReVecs ! flange moment vector on roll elements, reFlngMom->ReVecs ! flange force vector on races, raceFlngFor->ReVecs ! flange moment vector on races, raceFlngMom->ReVecs

```
bFlngFor=zero
                                                                                  ! normal flange force vector on roller, bFlngFor->ReVecs
 bFlngMom=zero
                                                                                  ! normal flange moment vector on roller, bFlngMom->ReVecs
 rFlngFor=zero
                                                                                   normal race flange force vector, rFlngFor->ReVecs
normal race flange moment vector, rFlngMom->ReVecs
 rFlngMom=zero
                                                                                  ! roller flange force derivatives, dbFlngFor->LoadDer
! roller flange mment derivatives, dbFlngFor->LoadDer
! race flange force derivatives, drFlngFor->LoadDer
! race flange moment derivatives, drFlngFor->LoadDer
 dbFlngFor=zero
 dbFlngMom=zero
 drFlngFor=zero
 drFlngMom=zero
do j=1,2
irace=j
                                                                                  ! irace->ReVecs
    race centers and transformations
     rqi(:)=raceGc(:,irace)
                                                                                  ! raceGc->VecMats
     tir(:,:)=inertToRace(:,:,irace)
                                                                                    inertToRace->VecMats, tir->ReVecs
     tbr=matmul(tir,transpose(tib))
                                                                                    roll element to race coordinate frame transformation
                                                                                  1
                                                                                  ! tbr->ReVecs
     tria=raceToIaz(:,:,j,ire)
                                                                                    race to inertial azimuth frame transformation
                                                                                  ! raceToIaz->VecMats
     if (ider /= 0) then
                                                                                  ! ider->LoadDer
        tir2=inertToRace2(:,:,j)
                                                                                  ! inertToRace2, inertToRace3->LoadDer
        tir3=inertToRace3(:,:,j)
     end if
    rolling element relative to race
    bqrqi=bqi-rqi
                                                                                  ! roll element geo center relative to race geo center
     bgrgr=matmul(tir,bgrgi)
                                                                                  ! in race frame, bgrgr->ReVecs
     tra=zero
                                                                                  ! zero->Constants, tra->ReVecs
     si=Adrb3(bgrgr(2),bgrgr(3))
                                                                                  ! race azimuth
     sii=si
                                                                                  ! sii->ReVecs, store azimuth for use in Adrc3
     ssi=dsin(si)
     csi=dcos(si)
     tra(1,1)=one
    tra(2,2)=csi
tra(3,3)=csi
tra(2,3)=ssi
     tra(3,2)=-ssi
    tras(:,:,j)=tra
do k=1,3
                                                                                  ! tras, tra->ReVecs
        bgrgra(k)=zero
        do 1=1,3
           bgrgra(k)=bgrgra(k)+tra(k,l)*bgrgr(l)
                                                                                 ! re geo cen rel to race geo cen in race azimuth frame
        end do
    end do
    base point on race for roll ele interaction
     if (jcm(6) == 0) then
                                                                                  ! icm->SubX
                                                                                  ! zero->Constants, race radius variation
        rv=zero
        rcfv=zero
                                                                                  ! groove curvature factor variation
     else
        rv=Adrx6(irace,rcfv,si)
     end if
     rcrgra(1)=raceCurCen(1,j)
                                                                                  ! raceCurCen->BrgGeom
                                                                                  ! for flat race, raceCurCen is zero
     rcrgra(2)=zero
    ircrgra(3)=raceCurCen(2,j)
if (raceCurRad(j) > crnLmt) then
    if (irace == 1) then
                                                                                  ! set base point to race land mid point
                                                                                  ! for flat race surface
            rcrgra(3)=raceRad(2,irace)+rv
                                                                                  ! race rad is base for line contact
                                                                                  ! raceRad->BrgGeom
        else
           rcrgra(3)=raceRad(1,irace)+rv
    end if
else if (raceCenLen(j) > zero) then
                                                                                  ! set base point to race land mid point
        if (irace == 1) then
  rcrgra(3)=raceRad(2,irace)+rv
                                                                                  ! for partly crowned race surface
                                                                                  ! race rad is base for line contact
! raceRad->BrgGeom
        else
        rcrgra(3)=raceRad(1,irace)+rv
end if
    end if
     re cur center relative to re geo center
    if (kConType(j,ire) > 0) then
    bcbgra=zero
                                                                                  ! for line contact this vector is zero
     else
        tbra=matmul(tra,tbr)
si=datan(tbra(2,3)/tbra(2,2))
                                                                                  ! re to race azimuth transformation
                                                                                  ! compute angular position of contact on re
        if (reCurCen(1,ire) /= zero) then
al=tbra(2,1)*reCurCen(1,ire)/(reCurCen(2,ire)
    *dsqrt(tbra(2,2)**2+tbra(2,3)**2))
                                                                                 &
δ.
            a2=dsqrt(one-a1*a1)
            si=si+datan(a1/a2)
        end if
        bcbgb(1)=reCurCen(1,ire)
bcbgb(2)=-reCurCen(2,ire)*dsin(si)
bcbgb(3)=reCurCen(2,ire)*dcos(si)
        al=tbra(3,1)*bcbgb(1)+tbra(3,2)*bcbgb(2)+tbra(3,3)*bcbgb(3) ! z oomponent of cur cen location in azimuth frame
```

1

!

!!

!

!!!

```
if ((sig(j)*al) > zero) then
                  bcbgb(3) = -bcbgb(3)
                  bcbgb(2) = -bcbgb(2)
               end if
              bcbgra=matmul(tbra,bcbgb)
                                                                                           ! re cur center in race azimuth frame
           end if
           bcbgr=matmul(transpose(tra),bcbgra)
                                                                                           ! this vector is used later to define contact position
           re cur center rel to race base point
1
!
          bcrcra=bgrgra+bcbgra-rcrgra
!
           call appropriate load module
۱
i
           if (kConType(irace,ire) <= 0) then
                                                                                           ! kConType->BrgGeom
                                                                                           ! point contact solution
              call PointContact
           else
              call LineContact
                                                                                           ! line contact solution
           end if
           if (kFlngIndr(j) /= 0) then
                                                                                           ! kFlngIndr->BrgGeom
                                                                                           ! flange contact for roller bearings
! stored for later use in Adrb1
! stored for later use in Adrb1
              call FlngContact
raceFlngFors(:,j,ire)=raceFlngFor(:,j)
raceFlngMoms(:,j,ire)=raceFlngMom(:,j)
           end if
                                                                                           ! raceFlngFors,raceFlngMom2->SetUpB1
       end do
       if (kFlngInds /= 0) then
                                                                                           ! kFlngInds->BrgGeom
1
           store re flange results for future use
i
          reFlngFors(:,ire)=reFlngFor
reFlngMoms(:,ire)=reFlngMom
                                                                                           ! reFlngFors->SetUpB1, stored for Adrb1
! reFlngMoms->SetUpB1, stored for Adrb1
       end if
       return
       contains
           subroutine PointContact
          point contact solutions
                                                    _____
1
                                                                                           ! roll ele # and race #
                                                              :: i,j
           integer
                                                              :: k,1
                                                                                             loop indices
           integer
                                                                                           ! unit vector along load in contact frame
! unit load vector in race azimuth frame
! unit load vector in race frame
! unit load vector in intertial azimuth frame
           real(r8),dimension(3)
                                                              :: uvcon
           real(r8), dimension(3)
real(r8), dimension(3)
                                                              :: uvra
                                                              :: uvr
                                                              :: uvia
           real(r8), dimension(3)
           real(r8)
                                                              :: tol =1.0E-05_r8
                                                                                             tolerance for out-of-plane contact
                                                             :: pRad
:: cal
           real(r8)
                                                                                             race radius at contact point
                                                                                             cosine of contact angle
           real(r8)
           real(r8)
                                                              :: tal
                                                                                             tangent of contact angle
                                                                                             zero or pi, used in contact angle computation
sine and cosine of computed contact angles
           real(r8)
                                                             :: ang
:: sal,sa2,cal,ca2
           real(r8)
                                                                                           1
                                                                                             magnitude of vector bcrcra
           real(r8)
                                                              :: bcrca
                                                                                           ! race curvatures along and normal to rolling dir
! curvature sum and function for load computation
           real(r8)
                                                              :: rrx,rry
                                                              :: sum, fr
           real(r8)
                                                              :: aj,bj,dj,aa
                                                                                             local variables used for contact load computation
           real(r8)
                                                                                           !
                                                                                           ! local variables for line contact computation
! elastic constants for line contact computation
           real(r8)
                                                              :: efl,bl,dq,ql
           real(r8), dimension(2)
                                                              :: pqs
           real(r8), dimension(3)
                                                              :: bcrcc
                                                                                           ! re cur center rel race center in contact frame
           initialize solutions
1
ļ
           i=ire
                                                                                           / ire->ReVecs
                                                                                             irace->ReVecs
           j=irace
           dqt(j)=zero
                                                                                             dqt->LoadDer, zero->Constants
           dmt(j)=zero
dmx(j)=zero
                                                                                             dmt->LoadDer
                                                                                             dmx->LoadDer
           dmr(j)=zero
                                                                                             dmr->LoadDer
           dqx(j)=zero
dqr(j)=zero
                                                                                             dqx->LoadDer
                                                                                             dqr->LoadDer
           dqxx(j)=zero
                                                                                             dqxx->LoadDer
           dqyy(j)=zero
dqzz(j)=zero
                                                                                           ! dqyy->LoadDer
! dqzz->LoadDer
           geo interaction and unit load vector
1
ļ
           uvcon(1)=zero
                                                                                           ! unit vector along load in contact frame
           uvcon(2)=zero
                                                                                           ! zero->Constants
           uvcon(3)=one
           pRad=rcrgra(3)
if(dabs(raceCurRad(j)) > crnLmt) then
                                                                                           ! base radius for rec/race contact
                                                                                           ! raceCurRad->BrgGeom, crnLmt->Constants
              flat race
!
```

```
tac(:,:)=tacs(:,:,j,i)
                                                                                                                                         ! race azimuth to contact frame transformation
                                                                                                                                         ! tac->ReVecs, tacs->VecMats
                                                                                                                                         ! re cur cen rel to race land in contact frame
! geometric interaction, del->Solutions, reCrn->BrgGeom
! unit vector along load in race azimuth frame
      bcrcc=matmul(tac,bcrcra)
      conDef(j,i)=bcrcc(3)+reCrn(i)
      uvra=matmul(transpose(tac),uvcon)
                                                                                                                                           in race frame, tra->ReVecs
in inertial azimuth frame
      uvr=matmul(transpose(tra),uvra)
      uvia=matmul(tria,uvr)
      cal=tac(1,1)
                                                                                                                                         ! tac->ReVecs
else if(dabs(reCrn(i)) > crnLmt) then
                                                                                                                                         ! reCrn->BrgGeom, crnLmt->Constants
      flat re surface
      to be formulated later
      continue
else
      both surfaces are curved
      bcrca=dsqrt(bcrcra(1)**2+bcrcra(2)**2+bcrcra(3)**2)
conDef(j,i)=bcrca+reCrn(i)-raceCurRad(j)
                                                                                                                                         ! reCrn->BrgGeom, raceCurRad->BrgGeom
      uvra(1)=bcrcra(1)/bcrca
uvra(2)=bcrcra(2)/bcrca
      uvra(3)=bcrcra(3)/bcrca
      uvr=matmul(transpose(tra),uvra)
uvia=matmul(tria,uvr)
                                                                                                                                        ! in race frame, tra->ReVecs
! in inertial azimuth frame
      cal=uvra(3)
      contact angles
      ang=(j-1)*pi
tal=uvia(1)/uvia(3)
                                                                                                                                         ! pi->Constants
                                                                                                                                         1
                                                                                                                                            tangent of contact angle
      ! tolr->Constants
                                                                                                                                         ! conAng->Solutions
      else
            conAng(j,1,i)=ang+datan(tal)
                                                                                                                                        ! conAng->Solutions
      end if
      if(dabs(uvia(2)) <= tol) then
            conAng(j,2,i)=zero
                                                                                                                                        ! conAng->Solutions, zero->constants
      else
            conAng(j,2,i)=datan(-uvia(2)
/dsqrt(uvia(1)**2+uvia(3)**2))
                                                                                                                                        & ! conAng->Solutions
      end if
      sal=dsin(conAng(j,1,i))
                                                                                                                                         ! inertial azimuth to contact frame transformation
      sal=dsin(conAng(j,1,1))
sa2=dsin(conAng(j,2,i))
ca1=dcos(conAng(j,1,i))
                                                                                                                                         ! tac->ReVecs
      ca2=dcos(conAng(j,2,i))
      tac(1,1)=cal
      tac(2,1)=sa1*sa2
      tac(3,1)=sa1*ca2
tac(1,2)=zero
      tac(2,2)=ca2
tac(3,2)=-sa2
      tac(1,3)=-sa1
      tac(2,3)=ca1*sa2
tac(3,3)=ca1*ca2
end if
tacs(:,:,j,i)=tac
contact load and half widths
if(conDef(j,i) > tolr(1)) then
    if(dabs(raceCurRad(j)) < crnLmt) then
        rrx=-one/(pRad/cal+raceCurRad(j))
                                                                                                                                         ! tolr->Constants, conDef->Solutions
                                                                                                                                         ! raceCurRad->BrgGeom, crnLmt->Constants
            rry=-one/raceCurRad(j)
      else
            rrx=-cal/pRad
            rry=zero
      end if
                                                                                                                                        ! eq rad along x direc (rolling direc), radX->ReVecs
! radX is used in traction procs
! reCur->BrgGeom, i->ReVecs
      radX(j)=one/(rrx+reCur(1,i))
      sum=rrx+rry+reCur(1,i)+reCur(2,i)
      sum=rrx+rry+recur(1,1)+recur(2,1)
fr=(rrx+reCur(1,i)-rry-reCur(2,i))/sum
if(fr <= 0.9995_r8) then
    call Adrc4(fr,aj,bj,dj,0)
    if (ierInd /= 0) return
    conLoad(j,i)=(two*sum/three)*(two*conDef(j,i)
        /(dj*sum))**(one2*three)
    acconc2*three
    acconc2*three

                                                                                                                                       & ! conLoad,del->Solutions, two,three,one2->constants
            aa(one2*three*conLoad(j,i)/sum)**one3
conWidthA(j,i)=aj*aa
conWidthB(j,i)=bj*aa
                                                                                                                                         ! one3->Constants
                                                                                                                                         ! conWidthA->Solutions
! conWidthB->Solutions
            ! conLoad->Solutions, qmReRace->Constants
            dqn(j)=one2*three*conLoad(j,i)/conDef(j,i)
                                                                                                                                         ! dgn->LoadDer
      else
efl=two*reConLmt(j,i)
                                                                                                                                         ! line contact with predefined length when
            conWidthA(j,i)=one2*efl
                                                                                                                                         ! curvature function is close to 1.0, bl->BrgGeom
```

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```
pqs(1)=qReRace(1,j)
                                                                               ! conWidthA->Solutions
           pqs(2)=qReRace(2,j)
                                                                               ! qReRace->Constants
            call Adrc6(1,conDef(j,i),pqs,efl,sum,bl,dq,ql)
           conLoad(j,i)=ql
                                                                               1
                                                                                 conLoad->Solutions
            conWidthB(j,i)=bl
                                                                               ! conWidthB->Solutions
           & ! conPress->Solutions
8
                                                                               ! dqn->LoadDer
       dqn(j)=dqn(j)*raceCosTaper(j)*sig(j)
dqx(j)=dqr(j)*raceTanTaper(j)
dqxy(j)=dqx(j)
dqyy(j)=dqx(j)
dqyy(j)=dqr(j)*si

                                                                               ! dqr->LoadDer, raceCosTaper->BrgGeom, sig->Constants
                                                                                 dqx->LoadDer, raceTanTaper->BrgGeom
                                                                                 dgxx->LoadDer
                                                                                  dqyy->LoadDer, ssi from main part of Adrcl
        dqzz(j)=-dqr(j)*csi
qcl(j,i)=conLoad(j,i)
acl(j,i)=one3*four*conWidthA(j,i)
                                                                                 dqzz->LoadDer, csi from main part of Adrc1
                                                                                 qcl->Solutions
acl->Solutions, one3,four->Constants
                                                                               Ì.
    else
        conLoad(j,i)=zero
conWidthA(j,i)=zero
                                                                               ! conLoad, conWidthA, conWidthB, gcl, acl ->Solutions
                                                                               ! zero->Constants
        conWidthB(j,i)=zero
        qcl(j,i)=zero
acl(j,i)=zero
        conPress(j,i)=zero
    end if
    contact position
    ccbgr=uvr*reCrn(i)+bcbgr
                                                                               ! contact center relative to re geo center
    tbc=matmul(tac,tbia)
                                                                               ! roll ele to contact frame transformation, tbc->ReVecs
    trc=matmul(tbc,transpose(tbr))
                                                                               ! race to contact frame transformation, trc->ReVecs
    do k=1,3
        cbs(k,j,i)=zero
        crs(k,j,i)=zero
do l=1,3
                                                                               ! cbs,crs->VecMats, both vectors in contact frame
           \& ! contact position relative to re geo center
                                                                               ! add terms to locate cont pos rel to re mass center
& ! contact position relative race mass center
8
æ
        end do
    end do
    return
    end subroutine PointContact
    subroutine LineContact
    line contact solutions
                                                                               ! roller # and race #
    integer
                                                    :: i,j
                                                                               ! loop indices
! elastic constants for line contact computation
                                                    :: k,ĺ,ll,lj
    integer
    real(r8), dimension(2)
                                                    :: pqs
    integer
                                                    :: ksol
                                                                               ! flag for computing contact length
                                                                               ! 0 =previously computed coordinates are valid
! 1 compute new values
                                                                               ! flag for computing local interaction
! 0 =no load condition, do not compute local interactions
! normalized x-coordinate defining the contact zone
    integer
                                                    :: jsol
    real(r8),dimension(2)
                                                    :: xj
    real(r8)
real(r8)
                                                    :: aā
                                                                               ! contact length
! x-ccordinate of center of contact
                                                    :: xxo
    real(r8)
                                                    :: qbs,qcs,bls,ccs,cc ! integrated load,halfwith and geom interaction
    real(r8)
real(r8)
                                                    :: qc,bl
                                                    :: ccm
                                                                               ! max geom interaction
                                                    :: xx,wk
                                                                                 Gaussian abscissa and weight
    real(r8)
    real(r8)
real(r8),dimension(3,3)
                                                    :: ccj
:: tira
                                                                               ! local geom interaction
! transformation from inertial to race azimuth frame
                                                    :: xtx,ytx,drx,dqxj
                                                                               ! local variables for computing derivatives
    real(r8)
    real(r8)
real(r8)
                                                    :: dqtj,dqrj,dqnj
                                                    :: bmj,rmj
                                                                               ! moment on roller and race at grid j
    real(r8)
                                                    :: sum
                                                                               ! curvature sum
                                                    :: Adrc5
                                                                               ! geom interaction function
    real(r8)
    initialize solutions
    i=ire
                                                                               ! ire->reVecs
    i=irace
                                                                                 irace->reVecs
    bm=zero
                                                                               ! bm,rm->LoadDer
    rm=zero
    drx=-raceTanTaper(i)
    dqx(j)=zero
    dqr(j)=zero
                                                                               ! all derivatives in LoadDer
    dqt(j)=zero
dqp(j)=zero
    dmx(j)=zero
    dmr(j)=zero
dmt(j)=zero
    dqxx(j)=zero
    dqyy(j)=zero
dqzz(j)=zero
    dqt2(j)=zero
```

!

1

!

```
dqt3(j)=zero
            dmxx(j)=zero
            dmyy(j)=zero
dmzz(j)=zero
            dmt2(j)=zero
           dmt3(j)=zero
pqs(1)=qReRace(1,j)
                                                                                                  ! qReRace->Constants
            pqs(2)=qReRace(2,j)
                                                                                                  ! race azimuth to contact frame transformation ! tac->ReVecs, tacs->VecMats
            tac(:,:)=tacs(:,:,j,i)
            qcs=zero
                                                                                                  ! initialization for computation of averages
            qbs=zero
bls=zero
            ccs=zero
              _____
            check existing contact limits
!
            call OldContLmts(ksol,xj)
                                                                                                  ! check old contact limit coordinates
            if (ksol == 0) then
    xx=one2*(xj(1)+xj(2))
                                                                                                  ! check if contact exists
                ccj=Adrc5(xx)
                if (dabs(ccj) <= tolr(1)) then
                    cci=zero
                    ccm=ccj
                    jsol=0
                else if (ccj < zero) then
                    ccm=ccj
                    jsol=0
                else
               jsol=1
end if
            else
               call NewContLmts(jsol,xj)
                                                                                                  ! compute new values when ksol /= 0
                ccm=conDef(j,i)
                                                                                                  ! in case of no contact ccm = max cls
            end if
            conLmts(1,j,i)=xj(1)
                                                                                                  ! store results for future use
            conLmts(2,j,i)=xj(2)
if (jsol == 0) then
                                                                                                     conLmts->Solutions
                                                                                                  ! when jsol = 0, there is no contact
                qc=zero
               bl=zero
            else
                local interactions in contact frame
I
                aa=(xj(2)-xj(1))/reCosTaper(i)
                                                                                                  ! reCosTaper->BrgGeom
                acl(j,i)=aa
                                                                                                  ! acl->Solutions
               conWidthA(j,i)=one2*aa
aa=aa**expLen(j,iRaceRot(j))
                                                                                                  ! major contact halfwidth, conWidthA->Solutions
! contact lenth parameter for life calculation
! axial position of center of contact
                xxo=one2*(xj(1)+xj(2))
                ccm=-1.0e+10_r8
                                                                                                  ! nGrid,xgl,wgl->reVecs
                do k=1,nGrid
                                                                                                  ! start loop for local interaction
! grid is in accordance with Gaussian quadrature
                    xx=conWidthA(j,i)*xgl(k)+xxo
wk=conWidthA(j,i)*wgl(k)
                 xx=conWidthA(j,i)*Wg1(K,
ccj=Adrc5(xx)
asc(1,k,j)=tra(2,2)
asc(2,k,j)=tra(2,3)
do l=1,3
cbsl(1,k,j)=zero
do l1=1,3
cbsl(1,k,j)=cbsl(1,k,j)+trc(1,11)*ccbgr(11)
+tbc(1,11)*reGeoCen(11,i)
crsl(1,k,j)=crsl(1,k,j)+trc(1,11)*(ccrgr(11)
+raceGeoCen(11,j))
'' 11)=zero
'' 1i)*tir(1j,11
                                                                                                  ! store cosine of azimuth angle, asc->reVecs
                                                                                                  ! store sine of azimuth angle
                                                                                                  ! cbsl->reVecs
                                                                                                     crsl->reVecs
                                                                                                  ! ccbgr,ccrgr->reVecs defined in Adrc5
& ! contact center rel to roller center in contact frame
                                                                                                  ! add term to locate relative to mass center
      8
                                                                                                  & ! contact center rel to race center in contact frame ! add vector to locate rel to mass center
      &
                                                                                                  ! transformation from inertial to race azimuth frame
                            do lj=1,3
    tira(l,ll)=tira(l,ll)+tra(l,lj)*tir(lj,ll)
                            end do
                        end do
                    end do
I
                    elastic line contact solution
i
                    sum=(rRad-sig(j)*bRad)*raceCosTaper(j)/(bRad*rRad)
ccs=ccs+wgl(k)*ccj
                                                                                                  ! sig->constants.raceCosTaper->BrgGeom
                                                                                                  ! wgl->reVecs
                    if(ccj > ccm) ccm=ccj
call Adrc6(1,ccj,pqs,one,sum,bl,dqnj,qc)
xCoord(k,j,i)=cbsl(1,k,j)
                                                                                                  ! one->Constants
                                                                                                  ! store x-coordinate of grid point
                    conDefDis(k,j,i)=ccj
conLoadDis(k,j,i)=qc
conWidthDis(k,j,i)=bl
qcs=qcs+wk*qc**expLoadA(j,iRaceRot(j))
                                                                                                    geometric interaction at grid point
                                                                                                    conLoadDis->Solutions
                                                                                                  1
                                                                                                     conWidthDis->Solutions
                                                                                                  ! expLoadA, iRaceRot->fatigueCons
                    dqn(j)=dqnj
bls=bls+wgl(k)*bl
                    qbs=qbs+wk*qc
                    call LCDerivatives(qc,dqnj,bmj,rmj)
                    bm(j)=bm(j)+wk*bmj
                                                                                                  ! moment on roller, bm->LoadDer
                    rm(j)=rm(j)+wk*rmj
                                                                                                  ! moment on race, rm->LoadDer
```

```
if (ider /= 0) then
                                                                                   ! ider->LoadDer, set derivatives
                dqx(j)=dqx(j)+wk*delQbj(1)
                                                                                     dqx->LoadDer
               dqx(j)=dqx(j)+wk*delQbj(1)
dqr(j)=dqr(j)+wk*delQbj(2)
dqt(j)=dqr(j)+wk*delQbj(3)
dqp(j)=dqp(j)+wk*delQbj(4)
dmx(j)=dmx(j)+wk*delMbj(1)
dmr(j)=dmr(j)+wk*delMbj(2)
dm(j)=dmt(j)+wk*delMbj(4)
dqxx(j)=dqxx(j)+wk*delQrj(1)
dqxy(j)=dqx(j)+wk*delQrj(1)
                                                                                    dqr->LoadDer
dqt->LoadDer
                                                                                     dqp->LoadDer
                                                                                     dmx->LoadDer
                                                                                     dmr->LoadDer
                                                                                     dmt->LoadDer
                                                                                     dmp->LoadDer
                                                                                     dqxx->LoadDer
               dqxx(j)=dqxx(j)+wk*delQrj(1)
dqyy(j)=dqyz(j)+wk*delQrj(2)
dqzz(j)=dqzz(j)+wk*delQrj(3)
dqt2(j)=dqt2(j)+wk*delQrj(4)
dqt3(j)=dqt3(j)+wk*delQrj(5)
dmxx(j)=dmxx(j)+wk*delMrj(1)
dmyy(j)=dmyy(j)+wk*delMrj(2)
                                                                                     dqyy->LoadDer
                                                                                     dqzz->LoadDer
dqt2->LoadDer
                                                                                     dqt3->LoadDer
                                                                                     dmxx->LoadDer
                                                                                     dmyy->LoadDer
               dmzz(j)=dmzz(j)+wk*delMrj(3)
dmt2(j)=dmt2(j)+wk*delMrj(4)
dmt3(j)=dmt3(j)+wk*delMrj(5)
                                                                                    dmzz->LoadDer
dmt2->LoadDer
                                                                                     dmt3->LoadDer
            end if
        end do
        qc=aa*qcs**expLoadAI(j,iRaceRot(j))
        cc=one2*ccs
bls=one2*bls
        xx=one2*(xj(1)+xj(2))
        parameters at center of contact
        ccj=Adrc5(xx)
        asc(1,ngm,j)=tra(2,2)
        asc(2,ngm,j)=tra(2,3)
sum=(rRad-sig(j)*bRad)*raceCosTaper(j)/(bRad*rRad)
        radX(j)=one/sum
                                                                                   ! store equivalent radius for trac procs, radX->ReVecs
        call Adrc6(1,ccj,pqs,one,sum,bl,dqnj,qc)
        do 1=1,3
            cbsl(l,ngm,j)=zero
            crsl(l,ngm,j)=zero
            do 11=1,3
                                                                                   ! trc,tbc,ccbgr,ccrgr->ReVecs, set in Adrc5
                   & ! contact center rel to roller center in contact frame
! add term to locate relative to mass center
δ.
                                                                                  & ! contact center rel to race center in contact frame
æ
                                                                                   ! add vector to locate rel to mass center
            end do
        end do
        do 1=1.3
            cbs(l,j,i)=cbsl(l,ngm,j)
            crs(1,j,i)=crsl(1,ngm,j)
        end do
     end if
     conLoadDis(ngm,j,i)=qc
                                                                                   ! conLoadDis->Solutions
     conWidthDis(ngm,j,i)=bl
                                                                                   ! conWidthDis->Solutions
     conDef(j,i)=ccm
                                                                                     conDef->Solutions
    conLoad(j,i)=qbs
conWidthB(j,i)=bls
                                                                                   ! conLoad->Solutions
! conWidthB->Solutions
     qcl(j,i)=qc
                                                                                   ! qcl->Solutions
    ! conPress->Solutions
     end if
     return
     end subroutine LineContact
     subroutine OldContLmts(ksol,xj)
                                               _____
contact limit coordinates from existing solutions
                                                      :: i,j
                                                                                  ! re and race #
! 0 =computations based on existing solutions are ok
    integer
                                                      :: ksol
    integer
                                                                                   ! 1 =new solutions are requid
                                                      :: xj
:: xab,xa,xaa,x1,x2
                                                                                   ! computed contact limits
! local variables for contact length
     real(r8),dimension(2)
     real(r8)
     real(r8)
                                                      :: cci,ccj
                                                                                   ! local variables for geometric interaction
                                                                                   ! loop index
! error indicator
     integer
                                                      :: k
                                                      :: ier
     integer
     real(r8)
                                                      :: Adrc5
                                                                                   ! geometric interaction function
     external Adrc5
     i=ire
     j=irace
     xab=one2*dabs(conLmts(2, i, i)-conLmts(1, i, i))
                                                                                   ! contact length from earlier solutions
                                                                                   ! conLmts->Solutions
     ksol=0
     k=1
     do while (k \le 2)
        xa=conLmts(k,j,i)
        ccj=Adrc5(xa)
        if (dabs(ccj) < tolr(1)) then
                                                                                  ! stored solution is valid, tolr->Constants
            xj(k)=xa
        &
                                                                                   ! contact exists for entire length of roller
                                                                                   ! reConLmt->BrgGeom
            xj(k)=xa
        else
                                                                                   ! modify existing contact coordinate
            xaa=one10*dabs(reConLmt(k,i))
                                                                                     length increment for updating contact length
            if (xaa > xab) xaa=xab
                                                                                   ! reConLmt->BrgGeom
            x1=xa-xaa
```

!

x2=xa+xaa if(k == 1) then ! check coordinate against max permissible con length if(x1 < reConLmt(k,i)) x1=reConLmt(k,i)</pre> ! reConLmt->BrgGeom else if(x2 > reConLmt(k,i)) x2=reConLmt(k,i) ! reConLmt->BrgGeom end if call Adrg3(xa,x1,x2,Adrc5,ier) ! solve for new coordinate value with old if(ier == 0) then ! value as a first guess xj(k)=xa else ksol=1 ! set switch for more generalized computations when ! a solution near the old value cannot be found k=2 end if end if if(k == 1 . and. ksol == 0) then ! look for symetrical solutions cci=Adrc5(xa) xa=-xa cci=Adrc5(xa) if(dabs(cci-ccj) < tolr(1)) then xj(2)=xa k=2 else if(ccj > zero .and. dabs(xa-reConLmt(k,i)) <= tolr(1)) then & ! check for limiting coordinate 8 ! reConLmt->BrqGeom xj(2)=xa k -2 end if end if k=k+1 end do return end subroutine OldContLmts subroutine NewContLmts(jsol,xj) compute new coordinates for defining contact length 1 - - -_____ integer :: i,i ! roller and race # integer :: jsol ! contact solution flag ! 0 =no contact, 1 =contact exists ! computed contact limit coordinate values real(r8),dimension(2) :: xj ! array also used for lower bound for iterative soln ! number of grid points for coarse bounds on contact length integer :: nx =5 :: xxi = (/1.0_r8, 0.75_r8,0.50_r8,0.25_r8,0.0_r8/) real(r8), dimension(5) & ! grid points for coarse bounds æ ! local variables for geom interaction real(r8) :: cc,ccm,cci,ccj :: k,l loop index grid indices for contact limit values grid indices used for contact limits integer 1 integer, dimension(2) :: jí :: ll,lk Т integer ! array used for upper bound for iterative soln ! local coordinate along roller axis real(r8),dimension(2) :: xjk real(r8) :: xa :: ier error indicator integer 1 real(r8) :: Adrc5 ! geometric interaction function external Adrc5 i=ire j=irace 1 l maximum geom interaction and grid indices for contact limit 1 jl=0 ccm=-1.0e+10_r8 k=1 do while (k <= nx) do l=1,2
 if (jl(1) == 0) then xa=xxi(k)*reConLmt(l,i) ! reConLmt->BrgGeom cc=Adrc5(xa)
if (cc > ccm) ccm=cc ! maximum interaction if (cc > tolr(1)) then ! check for positive interaction, tolr->Constants jl(1)=k xj(1)=xa if (k > 1) xjk(1)=xxi(k-1)*reConLmt(1,i)end if ! if k=1, then xj is the desired coordinate value ! and no iterative computations will be requid ! reConLmt->BrgGeom end if end do if(jl(1) /= 0 .and. jl(2) /= 0) k=nx+1 k=k+1 ! terminate loop when both limits are found end do jsol=1
if (jl(1) == 0 .and. jl(2) == 0) then ! set initial value to indicate contact no contact condition i conWidthA(j,i)=zero ! conWidthA->Solutions, zero->Constants conWidthB(j,i)=zero
conDef(j,i)=ccm ! conWidthB->Solutions 1 conDef->Solutions conLoad(j,i)=zero conLmts(1,j,i)=reConLmt(1,i) conLmts(2,j,i)=reConLmt(2,i) conLoad->Soluitons L. conLmts->Solutions ! conLmts->Solutions xj(1)=reConLmt(1,i) xj(2) = reConLmt(2,i)jsol=0 ! contact flag for no contact return

```
else if (jl(1)*jl(2) == 0) then
    partial contact at either end of roller
    contact limit coordinate defines one
    end of the contact zone
    if (jl(1) > 0) then
                                                                                    ! index of contact limit point to be computed ! index of point defined by contact limit
        11=2
       1k=1
    else
                                                                                    ! index of contact limit point to be computed ! index of point defined by contact limit
       11 = 1
       1k=2
    end if
    k=4
                                                                                      determine point of positive interaction for the
   do while (k > 1)
    xa=xxi(k)*reConLmt(lk,i)
                                                                                      limiting point defined by index 11
scan backwards starting with grid point #4 (0.25)
                                                                                    1
                                                                                    i
        cc=Adrc5(xa)
        if (cc > tolr(1)) then
            jl(11)=k
           xj(ll)=xa
           xjk(ll)=xxi(k+1)*reConLmt(lk,i)
            k=0
        end if
       k=k-1
    end do
    if (k == 1) then
                                                                                    ! when contact in within the first grid point ! near edge of roller
        jl(11)=2
        xj(ll)=xxi(2)*reConLmt(lk,i)
       xjk(ll)=xxi(l)*reConLmt(lk,i)
    end if
end if
compute axial coordinates for contact length
k=1
do while (k <= 2)
    if(jl(k) /= 1) then
        if(xjk(k) < xj(k)) then</pre>
                                                                                   ! when this index corresponds to first grid point ! the value in xj already contains the desid soln
           xa=xjk(k)
           xjk(k)=xj(k)
                                                                                   ! xj and xjk are sorted in ascending order
       xj(k)=xa
end if
       xa=one2*(xjk(k)+xj(k))
                                                                                   ! initial guess is at mid point
! compute iterative solution
        call Adrg3(xa,xj(k),xjk(k),Adrc5,ier)
if(ier /= 0) then
            ierInd=kRootLC
                                                                                   ! kRootLC->ErrorCodes, ierInd->Errors
            jerInd=ier
                                                                                   ! jerInd->Errors
! iMess->Errors
            iMess(1)='Error in LineContact procedure in Adrc1'
                                                                                   ! numM->Errors
           numM=1
       return
end if
        xj(k)=xa
        if(k.eq.1) then
           cci=Adrc5(xa)
           xa=-xa
                                                                                  ! look for symetrical solution
            ccj=Adrc5(xa)
            if (dabs(cci-ccj) < tolr(1)) then
               xj(2)=xa
               k=2
           end if
       end if
    end if
   k=k+1
end do
return
end subroutine NewContLmts
subroutine LCDerivatives(qj,sj,bmj,rmj)
line contact load and moment derivaties at grid point j
all derivative terms are set in variables declared in Adrc1
real(r8)
                                                                                    ! input load at grid point
                                                     :: qj
                                                                                    ! stiffness at grid point
! moment on roller and race about y axis in
real(r8)
                                                     :: si
real(r8)
                                                     :: bmj,rmj
                                                                                      in contact frame
                                                                                    !
                                                                                      derivative of deflection with race position X derivative of deflection with race position Y
real(r8)
                                                     :: delXX
                                                                                    1
real(r8)
                                                     :: delYY
                                                                                    i
real(r8)
                                                     :: delZZ
                                                                                      derivative of deflection with race position Z
                                                                                    !
                                                                                      derivative of deflection with roller position X derivative of deflection with roller position R
real(r8)
                                                     :: delx
                                                                                    1
real(r8)
                                                     :: delr
                                                                                    Ì.
                                                                                      derivative of deflection with race trans ang 2
derivative of deflection with race trans ang 3
derivative of deflection with roller trans ang 2
real(r8)
                                                     :: delAng2r
                                                                                    1
                                                     :: delAng3r
real(r8)
                                                                                    1
real(r8)
                                                     :: delAng2b
                                                                                    1
                                                                                      derivative of deflection with roller trans ang 3 derivative of moment arm with race position X derivative of moment arm with race position Y
real(r8)
                                                     :: delAng3b
                                                                                    L.
real(r8)
                                                     :: armXX
                                                                                    1
real(r8)
                                                     :: armYY
                                                                                    1
real(r8)
                                                     :: arm77
                                                                                      derivative of moment arm with race position Z
                                                                                    1
                                                                                      derivative of moment arm with roller position X
derivative of moment arm with roller position R
                                                     :: armx
real(r8)
                                                                                    1
real(r8)
                                                     :: armr
                                                                                    1
real(r8)
                                                     :: armAng2r
                                                                                    ! derivative of moment arm with race trans ang 2
```

!

!

```
real(r8)
                                                                                                          ! derivative of moment arm with race trans ang 3
                                                                        :: armAng3r
                                                                                                            derivative of moment arm with roller trans ang 2
            real(r8)
                                                                        :: armAng2b
            real(r8)
                                                                        :: armAng3b
                                                                                                            derivative of moment arm with roller trans ang 3 inertial to race azimuth transformation
                                                                        :: tira
            real(r8), dimension(3,3)
            real(r8),dimension(3,3)
                                                                        :: t1,t2,t3,t4
                                                                                                             local transformation matrix
                                                                                                            local vectors moment arm on race and roller in contact frame
            real(r8), dimension(3)
                                                                        :: r1.r2
            real(r8)
                                                                        :: arm1,arm2
            tira=matmul(tra,tir)
                                                                                                            tra,tir->ReVecs, inertial to race azimuth
ccbgb->ReVecs, roller cont point -inertial frame
bgrgi->Adrcl, race cont point - iertial frame
            r2=matmul(transpose(tib),ccbgb)
            rl=r2+bgrgi
                                                                                                            inertial to contact transformation
moment arm for race
moment arm for roller
            t4=matmul(tac,tira)
            arml=t4(1,1)*r1(1)+t4(1,2)*r1(2)+t4(1,3)*r1(3)
arm2=t4(1,1)*r2(1)+t4(1,2)*r2(2)+t4(1,3)*r2(3)
            bmj=qj*arm2
                                                                                                            moment on roller
            rmj=-qj*arm1
if (ider == 0) return
                                                                                                            moment on race
                                                                                                             return if no derivatives are required
                                                                                                          ! ider->LoadDer
            derivatives of deflection and moment arm for race
                                                                                                          ! derivative of def with race dis X
! tac->ReVecs tac(1,1)=cos(alfa)
            delXX=-tira(3,1)*tac(1,1)
                                                                                                            derivative of def with race dis X
moment arm with race dis X
            delYY=-tira(3,2)*tac(1,1)
            delZZ=-tira(3,3)*tac(1,1)
armXX=-t4(1,1)
            armYY=-t4(1,2)
                                                                                                             moment arm with race dis Y
            armZZ=-t4(1,3)
t1=matmul(tra,tir2)
                                                                                                            moment arm with race dis Z
tra->ReVecs tir2->Adrc1
            t2=matmul(tra,tir3)
                                                                                                          ! tir3->Adrc1
            t3=matmul(tac,t1)
t4=matmul(tac,t2)
            delAng2r=zero
                                                                                                          ! derivative of del with race angle 2
                                                                                                            derivative of del with race angle 3 derivative of moment arm with race angle 2
            delAng3r=zero
            armAng2r=zero
            armAng3r=zero
                                                                                                          ! derivative of moment arm with race angle 3
            do k=1,3
                A+1,3
delAng2r=delAng2r+t1(3,k)*r1(k)*tac(1,1)
delAng3r=delAng3r+t2(3,k)*r1(k)*tac(1,1)
armAng2r=armAng2r+t3(1,k)*r1(k)
                 armAng3r=armAng3r+t4(1,k)*r1(k)
            end do
            derivatives of deflection and moment arm for roller
I.
                                                                                                          ! derivative of def with roller dis x
! derivative of def with roller dis r
            delx=tira(3,1)*tac(1,1)
            delr=(-tira(3,2)*sbsi+tira(3,3)*cbsi)*tac(1,1)
                                                                                                          ! sbsi,cbsi->Adrc1, defined in Adrc5
! tib2,tib3->Adrc1
            t1=matmul(tira,transpose(tib2))
            t2=matmul(tira,transpose(tib3))
t3=matmul(tac,t1)
            t4=matmul(tac,t2)
                                                                                                          ! derivative of del with roller angle 2
! derivative of del with roller angle 3
! derivative of moment arm with roller angle 2
            delAng2b=zero
            delAng3b=zero
            armAng2b=zero
            armAng3b=zero
                                                                                                            derivative of moment arm with roller angle 3
            do k=1.3
                delAng2b=delAng2b+t1(3,k)*ccbgb(k)*tac(1,1)
delAng3b=delAng3b+t2(3,k)*ccbgb(k)*tac(1,1)
armAng2b=armAng2b+t3(1,k)*ccbgb(k)
                                                                                                          ! ccbgb->ReVecs
                 armAng3b=armAng3b+t4(1,k)*ccbgb(k)
            end do
            assemble terms for load and moment derivaties for roller
            armx=zero
                                                                                                          ! derivative of moment arm with roller dis x
                                                                                                            derivative of moment arm with roller dis r
            armr=zero
            delQbj(1)=sj*delx
delQbj(2)=sj*delr
delQbj(3)=sj*delAng2b
delQbj(4)=sj*delAng3b
delMbj(1)=arm2*delQbj(1)+qj*armx
                                                                                                            roller load der with displacement x roller load der with displacement r
                                                                                                            roller load der with trans angle 2
                                                                                                            roller load der with trans angle 3
roller moment der with disp x
roller moment der with disp r
            delMbj(2)=arm2*delQbj(2)+qj*armr
delMbj(3)=arm2*delQbj(3)+qj*armAng2b
delMbj(4)=arm2*delQbj(4)+qj*armAng3b
                                                                                                          ! roller moment der with trans ang 2
! roller moment der with trans ang 3
            assemble terms for load and moment derivaties for race
                                                                                                          ! race load der with disp x
! race load der with disp y
! race load der with disp z
            delQrj(1)=sj*delXX
            delQrj(2)=sj*delYY
delQrj(3)=sj*delZZ
            delQrj(4)=sj*delAng2r
delQrj(5)=sj*delAng3r
delQrj(1)=-arml*delQrj(1)-qj*armXX
                                                                                                            race load der with trans ang 2
race load der with trans ang 3
                                                                                                            race moment der with disp x
            delMrj(2)=-arm1*delQrj(2)-qj*armYY
delMrj(3)=-arm1*delQrj(3)-qj*armZZ
delMrj(4)=-arm1*delQrj(4)-qj*armAng2r
                                                                                                            race moment der with disp y
                                                                                                            race moment der with disp z race moment der with trans ang 2
            delMrj(5)=-arm1*delQrj(5)-qj*armAng3r
                                                                                                          ! race moment der with trans ang 3
            return
            end subroutine LCDerivatives
            subroutine FlngContact
            flange contacts for roller bearings
```

```
99
```
:: i,j :: k,l,m,ll ! roller and race # integer integer loop indices integer :: 1tc ! flange contact code i=ire j=irace set up velocities ļ do k=1.3 ! roller velocity, vbr->FlngData, zero->Constants vbr(k)=zero roller ang velocity, ombr->FlngData race velocity, vrr->FlngData race angular velocity, omrr->FlngData ombr(k)=zero vrr(k)=zero omrr(k)=raceAngVel(k,irace) do l=1,3 vbr(k)=vbr(k)+tir(k,1)*reVel(1,ire) ! transform all velocities to race frame ombr(k)=ombr(k)+tbr(k,1)*reAngVel(1,ire) vrr(k)=vrr(k)+tir(k,l)*raceVel(l,irace) end do end do 1 start loop for flanges ļ do k=1,2 if (kFlngInd(k,irace) /= 0) then ! kFlngInd->BrgGeom setup data iArray(2)=k ! store flange indices in case of error iArray(3)=j
iArray(1)=i ! iArray->Errors raceFlngWRi(k,j,i)=zero ! initialize solutions flngSV(k,j,i)=zero xcc=reCorCen(1,k,i) raceFlngWRi,flngSV->Solutions xcc->FlngData rcc=reCorCen(2,k,i) ! rcc->FlngData do 1=1.3 do m=1,3 ! ter->FlngData ter(l,m)=zero do ll=1,3
 ter(1,m)=ter(1,m)+tbr(1,ll)*tre(m,ll,k,i) ! tre->BrgGeom end do end do end do rf(1)=flngOrigin(1,k,j) ! rf->flngData rf(2)=zero ! raceExp->OpCond ! trafjk->FlngData, traf->BrgGeom ! trf->FlngData, tra->ReVecs rf(3)=flngOrigin(2,k,j)+raceExp(j) trafjk=traf(:,:,k,j)
trf=matmul(trafjk,tra) tria->ReVecs eRad->FlngData tria=raceToIaz(:,:,k,i) eRad=reEndRad(k,i) corRad=reCorRad(k,i) corRad-> roller corner radius ecc=reEndCen(k,i)
fHt=flngHt(k,j)
conf(:)=flngCons(:,k,j) ! ecc->FlngData ! fHt->FlngData conf->FlngData, flngCons->Constants if (iStat(k,j,i) > 0) then
 th=ths(k,j,i) iStat->FlngData angular coordinate for cor int ! th, ths, reRotc, reRotp->FlngData else th=ths(k,j,i)-reRotc(i)+reRotp(i)
end if call Adrc3(iStat(k,j,i),ltc) ! flange interaction procedure if (ierInd /= 0) call Adra9 ! process error if any store results I. iStat(k, j, i) = 1! iStat->FlngData idFlngCon(k,j,i)=ltc flngForce(k,j,i)=qf fqdel(k,j)=qdel idFlngCon->Solutions flngForce->Solutions store contact stiffness, fqdel-LoadDer qdel->FlngData if (qf > zero) idFlngSol=idFlngSol+1
flngConWidthA(k,j,i)=af
flngConWidthB(k,j,i)=bf idFlngSol->ReVecs flngConWidthA->Solutions flngConWidthB->Solutions fingbef(k,j,i)=delf flngbef(k,j,i)=ceff(3) reEndWR(k,i)=reEndWR(k,i)+qvf raceFlngWRi(k,j,i)=qvf ths(k,j,i)=th fl=ceff(k,j,i)=ceff flngDef->Solutions ccff->flngData reEndWR->Solutions raceFlngWRi->solutions ths,th->FlngData flngSV(k,j,i)=svf flngSV->Solutions do 1=1,3 I=1,3
raceFlngFor(1,j)=raceFlngFor(1,j)+raceFlngForjk(1)
raceFlngMom(1,j)=raceFlngMom(1,j)+raceFlngMomjk(1)
reFlngFor(1)=reFlngFor(1)+reFlngForjk(1)
reFlngMom(1)=reFlngMom(1)+reFlngMomjk(1) raceFlngFor->ReVecs raceFlngMom->ReVecs reFlngFor->ReVecs reFlngMom->ReVecs rFlngFor(1,j)=rFlngFor(1,j)+rFlngForjk(1)
rFlngMom(1,j)=rFlngMom(1,j)+rFlngMomjk(1)
bFlngFor(1)=bFlngFor(1)+bFlngForjk(1) rFlngFor->ReVecs rFlngMom->ReVecs bFlngFor->ReVecs bFlngMom(1)=bFlngMom(1)+bFlngMomjk(1) ! transform der and unit vectors to azimuth frame ! derivative of roller flange force ! derivative of roller flange moment ! derivative of race flange force (comp 1-4) ! derivative of race flange moment (comp 1-4) do m=1,4 dbFlngFor(l,m)=dbFlngFor(l,m)+dbFlngForjk(l,m) dbFlngMom(1,m)=dbFlngMom(1,m)+dbFlngForjk(1,m) drFlngFor(1,m,j)=drFlngFor(1,m,j)+drFlngForjk(1,m) drFlngMom(1,m,j)=drFlngMom(1,m,j)+drFlngMomjk(1,m) end do

Appendix C - Ball Bearing Data

Adore input data for the ball bearing case with the associated print ouput is documented below. Only the output and initial and final time steps is included for brevity.

```
\begin{smallmatrix} 1 & 0 & 0 & 0 & 0 & 1 & 500 & 1 & 0 & 0 & 1 \\ 5.0000E-02 & 5.0000E-03 & 3.0000E-01 & 1.0000E+03 & 1.0000E-04 & 0.0000E+00 \\ 1 & 0 & 2 \\ 3.2300E+02 & 1.0000E-05 & 0.0000E+00 & 3.0000E-03 & 3.0000E-02 \\ \end{smallmatrix}
Rec 1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             2500
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   5
Rec 2.1
Rec 2.4
Rec 2.5
Rec 2.7
Rec 3.1
                                                                                          3.2300E+02 1.2300E+02 3.2300E+02 
Rec 3.2
Rec 3.3
Rec 3.4
                                                                                                 0 0 0 0 0 2 1 19 0 0 0 0

1.0000E-01 1.800E-01 2.000E-02 2.0500E-01 3.0000E-02 3.0000E-02

1.9050E-02 1.4000E-01 2.5000E+01 0.0000E+00 5.2000E-01 5.4000E-01

0 0 0 0 0 0 0 0 2 2 2

1.4629E-01 1.3007E-01 3.6241E-02 5.0000E-03 1.5000E-03 1.2000E-03 0.0000E+00 0.0000E+00 0.0000E+00

1.3007E-01 8.0000E-03 1.8120E-02 1.5000E-03

1.3007E-01 8.0000E-03 1.8120E-02 1.5000E-03

2.2000E-03 1.8120E-02 1.5000E-03

1.3007E-01 8.0000E-03 1.8120E-02 1.500E-03

1.3007E-01 8.0000E-03 1.8120E-02 1.500E-03

1.3007E-01 8.0000E-03 1.8120E-02 1.500E-03

1.3007E-01 8.000E-03

1.
Rec 4
Rec 5A
Rec 7.0
Rec 7.1
Rec 7.2.1
Rec 7.2.2
                                                                                                  3.2300E+02 1.0000E+05 5.0000E+05
4.5000E+03 0.0000E+00 2.0000E+03 0.0000E+00 0.0000E+00 0.0000E+00
0.0000E+00 0.0000E+00 0.0000E+00 0.0000E+00 0.0000E+00 0.0000E+00 2.0000E+04
Rec 9.0
Rec 9.1.1
Rec 9.1.2
                                                                                                  6.6360E-04 1.0000E+00 1.0000E+00 0.0000E+00 0.0000E+00-6.0000E-04 0.0000E+00 0.0000E+00 0.0000E+00
3 1 0 0 0
0.0000E+00 2.0000E-02 1.6000E-02 1.0000E+00
Rec 9.5.1
Rec 10.0
Rec 10.1C
                                                                                                  1.2500E-07 1.0000E+01
5.0000E-02 0.0000E+00 0.0000E+00 0.0000E+00 1.2500E-07
5.0000E-02 0.0000E+00 0.0000E+00 0.0000E+00 1.2500E-07
Rec 10.3
Rec 10.5.1B
Rec 10.5.2B
Rec 11
                                                                                                    0.0000E+00 0.0000E+00-9.8100E+00
```

Input from optional user subroutines

Listing of input data records

ADVANCED DYNAMICS OF ROLLING ELEMENTS A Real Time Simulation of Rolling Bearing Performance

[Version (ADORE 5.0)]

Copyright Pradeep K Gupta Inc											
* Bearing Type = BALL	Program	Mode = 1 Run Id = Ball Bear	ing Test Case kGeoMod=100 *								
BEARING GEOMETRY											
NO OF BALLS 18 BALL DIA (m) 1.90500E-02 PITCH DIA (m) 1.40000E-01 CON ANGLE (deg) 2.50000E+01	OUTER CUR FAC 5.20000E-01 INNER CUR FAC 5.40000E-01 DIA FLAY (m) 2.14180E-04 END FLAY (m) 9.66105E-04	OUTER FIT (m) 1.00000E-05 INNER FIT (m) 5.00000E-05 WIDTH I (m) 3.00000E-02 WIDTH II (m) 3.00000E-02	SHAFT OD (m) 1.00000E-01 SHAFT ID (m) 2.00000E-02 BEARING OD (m) 1.80000E-01 HOUSING OD (m) 2.05000E-01								
CAGE OD (m) 1.46292E-01 CAGE ID (m) 1.30073E-01 CAGE CONE (deg) 0.00000E+00	CAGE WIDTH (m) 3.62410E-02 SEG CUT (deg) 0.00000E+00 POCKET SHAPE 0	POC CLS I (m) 1.20000E-03 POC CLS II (m) 0.00000E+00 NO OF C/R LANDS 2	OUTER CLS (m) 5.00000E-03 INNER CLS (m) 1.50000E-03 NO OF CAGE SEGS 1								
GUIDE GUIDE GUIDE LAND LAND TYPE DIA 1 2 1.30073E-01 2 2 1.30073E-01	GUIDE LAND GUIDE LAND CLS WIDTH (m) (m) 1.50000E-03 8.00000E-03 1.50000E-03	GUIDE LAND POSITION (m) 1.81204E-02 1.81204E-02									

MATERIAL PROPERTIES

		ROLLING ELEMENT	OUTER RACE	INNER RACE	CAGE	SHAFT	HOUSING
DENSITY ELASTIC MODULUS POISSON-S RATIO COEFF OF THERMAL EXP THERMAL CONDUCTIVITY HEAT CAPACITY ELASTIC STRAIN LIMIT HARDNESS NEAD. COEFFEIGUENT	(kg/m**3) (Pa) (W/m/K) (J/kg/K) (RC)	7.75000E+03 2.00000E+11 2.50000E-01 1.17000E-05 4.30000E+01 4.7000E+02 2.00000E-03 6.10000E+01	7.75000E+03 2.00000E+11 2.50000E-01 1.17000E-05 4.30000E+01 4.70000E+02 2.00000E-03 6.10000E+01	7.75000E+03 2.00000E+11 2.50000E-01 1.17000E-05 4.30000E+01 4.70000E+02 2.00000E-03 6.10000E+01	7.75000E+03 2.00000E+11 2.50000E-01 1.80000E-05 4.30000E+01 4.70000E+02 2.00000E-03 2.00000E+01 5.00000E+01	7.75000E+03 2.00000E+11 2.50000E-01 1.17000E-05 4.30000E+01	7.75000E+03 2.00000E+11 2.50000E-01 1.17000E-05 4.30000E+01
WEAR COEFFICIENT		5.00000E-06	5.00000E-06	5.00000E-06	5.00000E-04		

INERTIAL PARAMETERS

	MASS	MO	MENT OF INERT	'IA	MAS	S TO GEO CENT	ER		
	(kg)	(kg*m**2)				(m)			
		X-COMP	Y-COMP	Z-COMP	X-COMP	Y-COMP	Z-COMP		
RE	2.80534E-02	1.01806E-06	1.01806E-06	1.01806E-06	0.00000E+00	0.00000E+00	0.00000E+00		
CAGE	6.24437E-01	2.99108E-03	1.56388E-03	1.56388E-03	0.00000E+00	0.00000E+00	0.00000E+00		
OUTER RACE	1.29291E+00	9.32831E-03	4.76112E-03	4.76112E-03	0.00000E+00	0.00000E+00	0.00000E+00		
INNER RACE	8.38958E-01	2.57921E-03	1.35252E-03	1.35252E-03	0.0000E+00	0.0000E+00	0.00000E+00		

	.PRINCIPAL	то	GEO	FRAME					
(deg)									

		(ueg)	
	X-COMP	Y-COMP	Z-COMP
R	E 0.00000E+00	0.00000E+00	0.00000E+00
CAG	E 0.00000E+00	0.00000E+00	0.00000E+00
OUTER RAC	E 0.00000E+00	0.00000E+00	0.00000E+00
INNER RAC	E 0.00000E+00	0.00000E+00	0.00000E+00

LUBRICATION PARAMETERS

HYPOTHETICA MODELS		TRAC COEFF AT ZERO SLIP	MAXIMUM TRAC COEFF	TRAC COEFF AT INF SLIP	SLIP AT MAX TRACTION (m/s)	COEFFICIENT A	COEFFICIENT B (s/m)	COEFFICIENT C (s/m)	COEFFICIENT D
RE/RACE1 RE/RACE2 RE/CAGE RACE/CAGE	1.25000E-07 1.25000E-07 1.25000E-07 1.25000E-07	0.00000E+00 0.00000E+00	2.00000E-02 2.00000E-02	1.60000E-02 1.60000E-02		-1.60000E-02 -1.60000E-02 5.00000E-02 5.00000E-02	3.82896E-02 3.82896E-02 0.00000E+00 0.00000E+00	1.71782E+00 1.71782E+00 0.00000E+00 0.00000E+00	1.60000E-02 1.60000E-02
PRESSURE C	F VISCOSITY	MIL-L-7808 8.61565E-03 1.07562E-08	(1/Pa)	DENSITY 9.4 0.0	3000E+02 (K) 5429E+02 (kg/ 0000E+00 (1/F	(m**3) HEA Pa) **2	T CAP 1.836 0.000	18E-01 (W/m/K 10E+03 (J/kg/ 00E+00 (1/Pa)	K) **3
	DEFFICIENTS:	2.96433E+03 0.00000E+00	(K/Pa)		00000E+00 (K)* 00000E+00 (K/F			00E+00 (K)**3 00E+00 (K/Pa)	**3
PRESSURE C TEMP COEFF	REF VISCOSITY COEFFICIENTS: CICIENTS: DEFFICIENTS:	8.15882E-02 5.22140E-09 4.25519E-02 0.00000E+00	(1/Pa) (1/K)	0.0	00000E+00 (1/F 00000E+00 (1/K 00000E+00 (1/F	()**2	0.000	00E+00 (1/Pa) 00E+00 (1/K)* 00E+00 (1/Pa/	*3

FATIGUE PARAMETERS

LINE CO FATIGUE CONS (N/m**(50/27))	LOAD EXP	POINT C FATIGUE CONS (N/m**1.80)	LOAD EXP	WEIBULL DISPERSION EXPONENT	BEARING WEIBULL SLOPE: LIFE MODIFICATION CODE:	
OUTER RACE 1.66550E+08 INNER RACE 1.66550E+08						

	ASPERITY INTERACTIONS			LIMIT SHEAR	RESIDUAL	MATERIALS	CONTAM-	PROCESSING
	COMPOSITE	COMPOSITE	TRACTION	STRESS	STRESS	FACTOR	INATION	FACTOR
	RMS HEIGHT	RMS SLOPE	COEFF				FACTOR	
	(m)	(rad)		(Pa)	(Pa)			
	1.00000E-07							
INNER RACE	1.00000E-07	4.11320E-02	1.00000E-01	0.00000E+00	0.00000E+00	1.19700E+00	1.00000E+00	7.70000E-02

INITIAL OPERATING CONDITIONS

Ball Bearing Test Case kGeoMod=100

					OUTER RACE	INNER RACE
ROOM TEMPERATURE HOUSING TEMPERATURE SHAFT TEMPERATURE ROLLING ELEMENT TEMPERATURE	(K) (K) (K) (K)	3.23000E+02 3.23000E+02 3.23000E+02 3.23000E+02	ANGULAR VELOCITY TEMPERATURE MISALIGNMENT-Y MISALIGNMENT-Z	(K) (rad)	0.00000E+00 3.23000E+02 0.00000E+00 0.00000E+00	3.23000E+02 0.00000E+00
CAGE TEMPERATURE	(K)	3.23000E+02				

QUASI-STATIC CONSTRAINTS CONSTRAINING LOAD FRACTION	0 1 0 1 1 0.00000E+00		TRANSLATIONAL CONSTRAINTS ROTATIONAL CONSTRAINTS	$\begin{array}{ccc} 1 & 1 \\ 1 & 1 \end{array}$	1 1	1 1	1 1
BEARING COOLANT TYPE: VARY GEOMETRY WITH TEMPERATURE: HEAT TRANS COEFF (W/m**2/K)	SOMETRY WITH TEMPERATURE: Yes			1.00000E 3.23000E			
	X-COMP	Y-COMP	Z-COMP				

APPLIED LOAD VECTOR (N) 4.5	0000E+03	0.00000E+00	2.00000E+03
RELATIVE DISPLACEMENT VECTOR ((m) 0.0	0000E+00	0.00000E+00	0.00000E+00
APPLIED MOMENT VECTOR (N.	.m)	(0.00000E+00	0.00000E+00
GRAVITY VECTOR (m/s**	2) 0.0	0000E+00	0.00000E+00	-9.81000E+00
CAGE GEOM CEN POSITION ((m) 0.0	0000E+00	0.00000E+00	-6.00000E-04
CAGE ANGULAR POSITION (de	eg) 0.0	0000E+00	0.00000E+00	0.00000E+00
CAGE WHIRL TO ANG VEL RATIO	1.0	0000E+00		
CAGE ANG VEL TO EPICYCLIC VEL RAT	TIO 1.0	0000E+00		

SCALE FACTORS AND OUTPUT CONTROLS

SCA	LE FA	CTORS	STEP SI	STEP SIZE INFO				
LENGTH	(m)	9.52500E-03	MINIMUM	5.00000E-03	DATA CONTROL	1	500	
LOAD	(N)	4.50000E+03	MAXIMUM	3.00000E-01	AUTO PLOTS	1	19	0
TIME	(S)	2.43679E-04	INITIAL	5.00000E-02		0	0	0
			ERROR LIMIT	1.00000E-04	INT METHOD	5		

step	tau	Time	Outer Race Rot	Inner Race Rot	(ADORE 5.0)
no		(s)	(rev)	(rev)	
0	0.000E+00	0.000E+00	0.000E+00	0.000E+00	Ball Bearing Test Case kGeoMod=100
====					

1. Rolling Element Parameters

no Re	Orbital Position		t Angle eq)	Contact	Load	Contact	Stress Pa)		lf Width	Minor Hal	
										Outer Race	
1	0.000E+00	8.472E+00		2.474E+03						3.149E-04	
2	2.000E+01	8.334E+00	2.753E+01	2.457E+03	7.704E+02	1.577E+09	1.386E+09	2.367E-03	1.249E-03	3.142E-04	2.123E-04
3	4.000E+01	7.936E+00	2.778E+01	2.411E+03	7.142E+02	1.568E+09	1.352E+09	2.352E-03	1.218E-03	3.122E-04	2.071E-04
4	6.000E+01	7.327E+00	2.816E+01	2.348E+03	6.345E+02	1.554E+09	1.299E+09	2.331E-03	1.171E-03	3.095E-04	1.991E-04
5	8.000E+01	6.591E+00			5.460E+02		1.235E+09	2.308E-03	1.114E-03		1.895E-04
6	1.000E+02	5.816E+00	2.911E+01	2.218E+03	4.621E+02	1.524E+09	1.168E+09	2.288E-03	1.054E-03		1.793E-04
7	1.200E+02	5.101E+00	2.956E+01	2.170E+03	3.912E+02	1.513E+09	1.105E+09	2.271E-03	9.966E-04	3.016E-04	1.696E-04
8	1.400E+02 1.600E+02	4.505E+00 4.139E+00	2.993E+01 3.016E+01	2.153E+03	3.389E+02 3.064E+02	1.509E+09 1.504E+09	1.053E+09 1.018E+09	2.265E-03	9.500E-04 9.186E-04		1.618E-04
9	1.800E+02		3.016E+01 3.024E+01			1.504E+09 1.503E+09	1.018E+09 1.006E+09	2.258E-03		2.999E-04 2.996E-04	1.565E-04 1.546E-04
10 11	2.000E+02	4.014E+00 4.139E+00	3.024E+01 3.016E+01	2.127E+03 2.133E+03	2.955E+02 3.064E+02	1.503E+09	1.018E+09	2.256E-03 2.258E-03	9.076E-04 9.186E-04		1.546E-04 1.565E-04
12	2.200E+02	4.505E+00	2.993E+01		3.389E+02	1.504E+09	1.053E+09	2.265E-03	9.500E-04		1.618E-04
13	2.400E+02	4.505E+00 5.101E+00	2.993E+01 2.956E+01		3.912E+02	1.513E+09	1.105E+09	2.205E-03 2.271E-03	9.966E-04		1.696E-04
14	2.600E+02	5.816E+00	2.950E+01 2.911E+01	2.218E+03	4.621E+02	1.524E+09	1.168E+09	2.288E-03	1.054E-03		1.793E-04
15	2.800E+02	6.591E+00	2.862E+01		5.460E+02			2.308E-03	1.114E-03		1.895E-04
16	3.000E+02	7.327E+00	2.816E+01	2.348E+03	6.345E+02	1.554E+09	1.299E+09	2.331E-03	1.171E-03		1.991E-04
17	3.200E+02	7.936E+00	2.778E+01		7.142E+02	1.568E+09	1.352E+09	2.352E-03	1.218E-03		2.071E-04
18	3.400E+02				7.704E+02				1.249E-03	3.142E-04	
10	5.1002.02	0.0012.00	21/002/01	211072.00		1.5772.05	1.0002.00	2.50/2 05	1.1.1.1.1. 0.5	5.1100 01	211202 01
RE	Orbital	Ano	qular Veloc	ity	RE Ang 1	Position	Spin	/Roll	Contact	Loss	Time Ave
	Velocity	Amplitude	Theta	Phi	Theta	Phi				(W)	Wear Rate
	(rpm)	(rpm)	(deg)	(deg)	(deg)	(deg)	Outer Race	Inner Race	Outer Race	Inner Race	(m**3/s)
1											1 (00= 10
1	8.999E+03		-8.452E+00	0.000E+00	0.000E+00		-1.958E-02	3.654E-01	1.848E+01	3.165E+01	1.683E-12
2	9.006E+03	7.529E+04	-8.313E+00	0.000E+00	0.000E+00	0.000E+00	-1.926E-02	3.695E-01	1.803E+01	3.030E+01	1.652E-12
		7.529E+04		0.000E+00 0.000E+00	0.000E+00 0.000E+00	0.000E+00 0.000E+00	-1.926E-02 -1.835E-02	3.695E-01		3.030E+01	
2 3 4	9.006E+03 9.028E+03 9.061E+03	7.529E+04 7.547E+04 7.576E+04	-8.313E+00 -7.916E+00 -7.309E+00	0.000E+00 0.000E+00 0.000E+00	0.000E+00 0.000E+00 0.000E+00	0.000E+00 0.000E+00 0.000E+00	-1.926E-02 -1.835E-02 -1.695E-02	3.695E-01 3.812E-01 3.994E-01	1.803E+01 1.686E+01 1.535E+01	3.030E+01 2.667E+01 2.178E+01	1.652E-12 1.566E-12 1.443E-12
2 3 4 5	9.006E+03 9.028E+03 9.061E+03 9.100E+03	7.529E+04 7.547E+04 7.576E+04 7.617E+04	-8.313E+00 -7.916E+00 -7.309E+00 -6.572E+00	0.000E+00 0.000E+00 0.000E+00 0.000E+00	0.000E+00 0.000E+00 0.000E+00 0.000E+00	0.000E+00 0.000E+00 0.000E+00 0.000E+00	-1.926E-02 -1.835E-02 -1.695E-02 -1.517E-02	3.695E-01 3.812E-01 3.994E-01 4.218E-01	1.803E+01 1.686E+01 1.535E+01 1.381E+01	3.030E+01 2.667E+01 2.178E+01 1.674E+01	1.652E-12 1.566E-12 1.443E-12 1.286E-12
2 3 4 5 6	9.006E+03 9.028E+03 9.061E+03 9.100E+03 9.147E+03	7.529E+04 7.547E+04 7.576E+04 7.617E+04 7.659E+04	-8.313E+00 -7.916E+00 -7.309E+00 -6.572E+00 -5.798E+00	0.000E+00 0.000E+00 0.000E+00 0.000E+00 0.000E+00 0.000E+00	0.000E+00 0.000E+00 0.000E+00 0.000E+00 0.000E+00	0.000E+00 0.000E+00 0.000E+00 0.000E+00 0.000E+00	-1.926E-02 -1.835E-02 -1.695E-02 -1.517E-02 -1.339E-02	3.695E-01 3.812E-01 3.994E-01 4.218E-01 4.458E-01	1.803E+01 1.686E+01 1.535E+01 1.381E+01 1.260E+01	3.030E+01 2.667E+01 2.178E+01 1.674E+01 1.238E+01	1.652E-12 1.566E-12 1.443E-12 1.286E-12 1.152E-12
2 3 4 5 6 7	9.006E+03 9.028E+03 9.061E+03 9.100E+03 9.147E+03 9.194E+03	7.529E+04 7.547E+04 7.576E+04 7.617E+04 7.659E+04 7.700E+04	-8.313E+00 -7.916E+00 -7.309E+00 -6.572E+00 -5.798E+00 -5.085E+00	0.000E+00 0.000E+00 0.000E+00 0.000E+00 0.000E+00 0.000E+00	0.000E+00 0.000E+00 0.000E+00 0.000E+00 0.000E+00 0.000E+00 0.000E+00	0.000E+00 0.000E+00 0.000E+00 0.000E+00 0.000E+00 0.000E+00 0.000E+00	-1.926E-02 -1.835E-02 -1.695E-02 -1.517E-02 -1.339E-02 -1.174E-02	3.695E-01 3.812E-01 3.994E-01 4.218E-01 4.458E-01 4.684E-01	1.803E+01 1.686E+01 1.535E+01 1.381E+01 1.260E+01 1.174E+01	3.030E+01 2.667E+01 2.178E+01 1.674E+01 1.238E+01 9.077E+00	1.652E-12 1.566E-12 1.443E-12 1.286E-12 1.152E-12 1.040E-12
2 3 4 5 6 7 8	9.006E+03 9.028E+03 9.061E+03 9.100E+03 9.147E+03 9.194E+03 9.272E+03	7.529E+04 7.547E+04 7.576E+04 7.617E+04 7.659E+04 7.700E+04 7.765E+04	-8.313E+00 -7.916E+00 -7.309E+00 -6.572E+00 -5.798E+00 -5.085E+00 -3.612E+00	0.000E+00 0.000E+00 0.000E+00 0.000E+00 0.000E+00 0.000E+00 0.000E+00	0.000E+00 0.000E+00 0.000E+00 0.000E+00 0.000E+00 0.000E+00 0.000E+00	0.000E+00 0.000E+00 0.000E+00 0.000E+00 0.000E+00 0.000E+00 0.000E+00	-1.926E-02 -1.835E-02 -1.695E-02 -1.517E-02 -1.339E-02 -1.174E-02 7.041E-03	3.695E-01 3.812E-01 3.994E-01 4.218E-01 4.458E-01 4.684E-01 5.042E-01	1.803E+01 1.686E+01 1.535E+01 1.381E+01 1.260E+01 1.174E+01 1.101E+01	3.030E+01 2.667E+01 2.178E+01 1.674E+01 1.238E+01 9.077E+00 7.225E+00	1.652E-12 1.566E-12 1.443E-12 1.286E-12 1.152E-12 1.040E-12 9.767E-13
2 3 4 5 6 7 8 9	9.006E+03 9.028E+03 9.061E+03 9.100E+03 9.147E+03 9.194E+03 9.272E+03 9.297E+03	7.529E+04 7.547E+04 7.576E+04 7.617E+04 7.659E+04 7.700E+04 7.705E+04 7.785E+04	-8.313E+00 -7.916E+00 -7.309E+00 -6.572E+00 -5.798E+00 -5.085E+00 -3.612E+00 -3.319E+00	0.000E+00 0.000E+00 0.000E+00 0.000E+00 0.000E+00 0.000E+00 0.000E+00 0.000E+00	0.000E+00 0.000E+00 0.000E+00 0.000E+00 0.000E+00 0.000E+00 0.000E+00 0.000E+00	0.000E+00 0.000E+00 0.000E+00 0.000E+00 0.000E+00 0.000E+00 0.000E+00 0.000E+00	-1.926E-02 -1.835E-02 -1.695E-02 -1.517E-02 -1.339E-02 -1.174E-02 7.041E-03 6.469E-03	3.695E-01 3.812E-01 3.994E-01 4.218E-01 4.458E-01 4.684E-01 5.042E-01 5.150E-01	1.803E+01 1.686E+01 1.535E+01 1.381E+01 1.260E+01 1.174E+01 1.101E+01 1.064E+01	3.030E+01 2.667E+01 2.178E+01 1.674E+01 1.238E+01 9.077E+00 7.225E+00 5.920E+00	1.652E-12 1.566E-12 1.443E-12 1.286E-12 1.52E-12 1.040E-12 9.767E-13 9.234E-13
2 3 4 5 6 7 8 9 10	9.006E+03 9.028E+03 9.061E+03 9.100E+03 9.147E+03 9.194E+03 9.272E+03 9.297E+03 9.306E+03	7.529E+04 7.547E+04 7.576E+04 7.617E+04 7.659E+04 7.700E+04 7.765E+04 7.785E+04 7.785E+04 7.792E+04	-8.313E+00 -7.916E+00 -7.309E+00 -6.572E+00 -5.798E+00 -5.085E+00 -3.612E+00 -3.319E+00 -3.218E+00	0.000E+00 0.000E+00 0.000E+00 0.000E+00 0.000E+00 0.000E+00 0.000E+00 0.000E+00 0.000E+00	0.000E+00 0.000E+00 0.000E+00 0.000E+00 0.000E+00 0.000E+00 0.000E+00 0.000E+00	0.000E+00 0.000E+00 0.000E+00 0.000E+00 0.000E+00 0.000E+00 0.000E+00 0.000E+00	$\begin{array}{c} -1.926 \pm -02 \\ -1.835 \pm -02 \\ -1.695 \pm -02 \\ -1.517 \pm -02 \\ -1.339 \pm -02 \\ -1.174 \pm -02 \\ 7.041 \pm -03 \\ 6.469 \pm -03 \\ 6.271 \pm -03 \end{array}$	3.695E-01 3.812E-01 4.218E-01 4.458E-01 4.684E-01 5.042E-01 5.150E-01 5.187E-01	1.803E+01 1.686E+01 1.535E+01 1.381E+01 1.260E+01 1.174E+01 1.01E+01 1.064E+01 1.052E+01	3.030E+01 2.667E+01 2.178E+01 1.674E+01 1.238E+01 9.077E+00 7.225E+00 5.920E+00 5.507E+00	1.652E-12 1.566E-12 1.443E-12 1.286E-12 1.152E-12 1.040E-12 9.767E-13 9.234E-13 9.056E-13
2 3 4 5 6 7 8 9 10 11	$\begin{array}{c} 9.006E+03\\ 9.028E+03\\ 9.061E+03\\ 9.100E+03\\ 9.147E+03\\ 9.272E+03\\ 9.272E+03\\ 9.297E+03\\ 9.297E+03\\ \end{array}$	7.529E+04 7.547E+04 7.576E+04 7.659E+04 7.700E+04 7.765E+04 7.785E+04 7.792E+04 7.785E+04	-8.313E+00 -7.916E+00 -7.309E+00 -6.572E+00 -5.798E+00 -3.612E+00 -3.319E+00 -3.319E+00 -3.319E+00	$\begin{array}{c} 0.000\pm+00\\ \end{array}$	$\begin{array}{c} 0.000\pm+00\\ \end{array}$	$\begin{array}{c} 0.000\pm +00\\ \end{array}$	$\begin{array}{c} -1.926\pm02\\ -1.835\pm02\\ -1.695\pm02\\ -1.517\pm02\\ -1.517\pm02\\ -1.339\pm02\\ -1.174\pm02\\ 7.041\pm03\\ 6.469\pm03\\ 6.271\pm03\\ 6.469\pm03 \end{array}$	$\begin{array}{c} 3.695 \pm -01\\ 3.812 \pm -01\\ 4.218 \pm -01\\ 4.458 \pm -01\\ 4.684 \pm -01\\ 5.042 \pm -01\\ 5.150 \pm -01\\ 5.187 \pm -01\\ 5.150 \pm -01\\ 5.150 \pm -01\\ \end{array}$	1.803E+01 1.686E+01 1.335E+01 1.260E+01 1.174E+01 1.101E+01 1.064E+01 1.052E+01 1.064E+01	3.030E+01 2.667E+01 2.178E+01 1.674E+01 1.238E+01 9.077E+00 7.225E+00 5.920E+00 5.920E+00	1.652E-12 1.566E-12 1.286E-12 1.286E-12 1.152E-12 1.040E-12 9.767E-13 9.056E-13 9.234E-13
2 3 4 5 6 7 8 9 10 11 12	$\begin{array}{c} 9.006\pm 03\\ 9.028\pm 03\\ 9.061\pm 03\\ 9.100\pm 03\\ 9.147\pm 03\\ 9.194\pm 03\\ 9.272\pm 03\\ 9.272\pm 03\\ 9.297\pm 03\\ 9.297\pm 03\\ 9.272\pm 03\\ 9.272\pm 03\\ \end{array}$	7.529E+04 7.547E+04 7.576E+04 7.6576E+04 7.659E+04 7.705E+04 7.765E+04 7.785E+04 7.785E+04 7.765E+04	-8.313E+00 -7.309E+00 -6.572E+00 -5.798E+00 -3.612E+00 -3.319E+00 -3.218E+00 -3.319E+00 -3.319E+00 -3.319E+00 -3.612E+00	$\begin{array}{c} 0.000\pm+00\\ \end{array}$	$\begin{array}{c} 0.000\pm+00\\ \end{array}$	$\begin{array}{c} 0.000\pm +00\\ \end{array}$	$\begin{array}{c} -1.926\pm02\\ -1.835\pm-02\\ -1.835\pm-02\\ -1.517\pm-02\\ -1.517\pm-02\\ -1.339\pm-02\\ 7.041\pm-03\\ 6.469\pm-03\\ 6.271\pm-03\\ 6.469\pm-03\\ 7.041\pm-03\\ 7.041\pm-03\end{array}$	3.695E-01 3.812E-01 3.994E-01 4.218E-01 4.458E-01 5.042E-01 5.150E-01 5.187E-01 5.150E-01 5.042E-01	$\begin{array}{c} 1.803\pm 01\\ 1.686\pm 01\\ 1.535\pm 01\\ 1.381\pm 01\\ 1.260\pm 01\\ 1.174\pm 01\\ 1.01\pm 01\\ 1.064\pm 01\\ 1.052\pm 01\\ 1.064\pm 01\\ 1.001\pm 01\\ \end{array}$	$\begin{array}{c} 3.030\pm01\\ 2.667\pm01\\ 2.178\pm01\\ 1.674\pm01\\ 1.238\pm01\\ 9.077\pm00\\ 7.225\pm00\\ 5.920\pm00\\ 5.507\pm00\\ 5.920\pm00\\ 7.225\pm00 \end{array}$	$\begin{array}{c} 1.652E-12\\ 1.566E-12\\ 1.443E-12\\ 1.286E-12\\ 1.152E-12\\ 1.040E-12\\ 9.767E-13\\ 9.234E-13\\ 9.234E-13\\ 9.234E-13\\ 9.767E-13\\ \end{array}$
2 3 4 5 6 7 8 9 10 11 12 13	$\begin{array}{c} 9.006\pm 03\\ 9.028\pm 03\\ 9.061\pm 03\\ 9.100\pm 03\\ 9.147\pm 03\\ 9.194\pm 03\\ 9.272\pm 03\\ 9.272\pm 03\\ 9.297\pm 03\\ 9.297\pm 03\\ 9.297\pm 03\\ 9.292\pm 03\\ 9.272\pm 03\\ 9.194\pm 03\\ \end{array}$	$\begin{array}{c} 7.529\pm 04\\ 7.547\pm 04\\ 7.576\pm 04\\ 7.576\pm 04\\ 7.617\pm 04\\ 7.659\pm 04\\ 7.705\pm 04\\ 7.765\pm 04\\ 7.785\pm 04\\ 7.785\pm 04\\ 7.785\pm 04\\ 7.765\pm 04\\ 7.765\pm 04\\ 7.705\pm 04\\ 7.700\pm 04\\ \end{array}$	-8.313E+00 -7.309E+00 -6.572E+00 -5.798E+00 -3.612E+00 -3.319E+00 -3.319E+00 -3.319E+00 -3.612E+00 -3.612E+00 -3.612E+00 -5.085E+00	$\begin{array}{c} 0.000\pm+00\\ \end{array}$	$\begin{array}{c} 0.000\pm+00\\ \end{array}$	$\begin{array}{c} 0.000\pm+00\\ \end{array}$	$\begin{array}{c} -1.926\pm02\\ -1.835\pm02\\ -1.695\pm02\\ -1.517\pm02\\ -1.339\pm02\\ -1.174\pm02\\ 7.041\pm03\\ 6.469\pm03\\ 6.271\pm03\\ 6.469\pm03\\0469\pm03\\041\pm03\\041\pm03\\ -1.174\pm02\end{array}$	$\begin{array}{c} 3.695E-01\\ 3.812E-01\\ 3.994E-01\\ 4.218E-01\\ 4.458E-01\\ 4.684E-01\\ 5.042E-01\\ 5.150E-01\\ 5.150E-01\\ 5.150E-01\\ 5.042E-01\\ 4.684E-01\\ \end{array}$	$\begin{array}{c} 1.803\pm\!01\\ 1.686\pm\!01\\ 1.535\pm\!01\\ 1.381\pm\!01\\ 1.260\pm\!01\\ 1.174\pm\!01\\ 1.012\pm\!01\\ 1.064\pm\!01\\ 1.052\pm\!01\\ 1.064\pm\!01\\ 1.064\pm\!01\\ 1.101\pm\!01\\ 1.174\pm\!01 \end{array}$	$\begin{array}{c} 3.030 \pm +01\\ 2.667 \pm +01\\ 2.178 \pm +01\\ 1.674 \pm +01\\ 1.238 \pm +01\\ 9.077 \pm +00\\ 7.225 \pm +00\\ 5.920 \pm +00\\ 5.920 \pm +00\\ 5.920 \pm +00\\ 7.225 \pm +00\\ 9.077 \pm +00\\ \end{array}$	$\begin{array}{c} 1.652E-12\\ 1.566E-12\\ 1.443E-12\\ 1.286E-12\\ 1.152E-12\\ 1.040E-12\\ 9.767E-13\\ 9.234E-13\\ 9.056E-13\\ 9.234E-13\\ 9.767E-13\\ 1.040E-12\\ \end{array}$
2 3 4 5 6 7 8 9 10 11 12 13 14	$\begin{array}{c} 9.006E+03\\ 9.028E+03\\ 9.061E+03\\ 9.100E+03\\ 9.147E+03\\ 9.194E+03\\ 9.272E+03\\ 9.297E+03\\ 9.297E+03\\ 9.297E+03\\ 9.272E+03\\ 9.194E+03\\ 9.147E+03\\ \end{array}$	$\begin{array}{c} 7.529\pm04\\ 7.576\pm04\\ 7.576\pm04\\ 7.670\pm04\\ 7.659\pm04\\ 7.705\pm04\\ 7.705\pm04\\ 7.705\pm04\\ 7.785\pm04\\ 7.785\pm04\\ 7.785\pm04\\ 7.785\pm04\\ 7.765\pm04\\ 7.765\pm04\\ 7.705\pm04\\ 7.705\pm04\\ 7.655\pm04\\ 7.659\pm04\\ 7.65\pm04\\ 7.65\pm04$ 7.65\pm04\\ 7.65\pm04 7.65\pm04\\ 7.65\pm04 7.65\pm00 7.65\pm	-8.313E+00 -7.309E+00 -6.572E+00 -5.798E+00 -3.612E+00 -3.319E+00 -3.319E+00 -3.319E+00 -3.612E+00 -5.798E+00	$\begin{array}{c} 0.000\pm 00\\ \end{array}$	$\begin{array}{c} 0.000\pm +00\\ \end{array}$	$\begin{array}{c} 0.000E+00\\ \end{array}$	$\begin{array}{c} -1.926E-02\\ -1.835E-02\\ -1.695E-02\\ -1.517E-02\\ -1.517E-02\\ -1.174E-02\\ 7.041E-03\\ 6.469E-03\\ 6.271E-03\\ 6.469E-03\\ 7.041E-03\\ -1.174E-02\\ -1.339E-02\end{array}$	$\begin{array}{c} 3.695E-01\\ 3.812E-01\\ 3.994E-01\\ 4.218E-01\\ 4.684E-01\\ 5.042E-01\\ 5.150E-01\\ 5.150E-01\\ 5.150E-01\\ 5.042E-01\\ 4.684E-01\\ 4.458E-01 \end{array}$	$\begin{array}{c} 1.803\pm 01\\ 1.686\pm 01\\ 1.535\pm 01\\ 1.381\pm 01\\ 1.260\pm 01\\ 1.174\pm 01\\ 1.01\pm 01\\ 1.064\pm 01\\ 1.064\pm 01\\ 1.064\pm 01\\ 1.01\pm 01\\ 1.174\pm 01\\ 1.260\pm 01\end{array}$	$\begin{array}{c} 3.030 \pm +01\\ 2.667 \pm +01\\ 1.674 \pm +01\\ 1.238 \pm +01\\ 9.077 \pm +00\\ 7.225 \pm +00\\ 5.920 \pm +00\\ 5.920 \pm +00\\ 7.225 \pm +00\\ 7.225 \pm +00\\ 7.225 \pm +00\\ 9.077 \pm +00\\ 1.238 \pm +01\\ \end{array}$	$\begin{array}{c} 1.652E-12\\ 1.566E-12\\ 1.443E-12\\ 1.286E-12\\ 1.152E-12\\ 1.040E-12\\ 9.767E-13\\ 9.234E-13\\ 9.056E-13\\ 9.234E-13\\ 9.767E-13\\ 1.040E-12\\ 1.152E-12\\ \end{array}$
2 3 4 5 6 7 8 9 10 11 12 13 14 15	$\begin{array}{c} 9.006E+03\\ 9.028E+03\\ 9.061E+03\\ 9.100E+03\\ 9.147E+03\\ 9.194E+03\\ 9.272E+03\\ 9.297E+03\\ 9.297E+03\\ 9.297E+03\\ 9.272E+03\\ 9.194E+03\\ 9.100E+03\\ \end{array}$	$\begin{array}{c} 7.529\pm04\\ 7.547\pm04\\ 7.576\pm04\\ 7.659\pm04\\ 7.659\pm04\\ 7.700\pm04\\ 7.765\pm04\\ 7.765\pm04\\ 7.785\pm04\\ 7.785\pm04\\ 7.785\pm04\\ 7.785\pm04\\ 7.765\pm04\\ 7.700\pm04\\ 7.659\pm04\\ 7.659\pm04\\ 7.659\pm04\\ 7.659\pm04\end{array}$	-8.313E+00 -7.309E+00 -6.572E+00 -5.798E+00 -3.612E+00 -3.319E+00 -3.319E+00 -3.319E+00 -3.319E+00 -3.319E+00 -3.319E+00 -5.78E+00 -5.79E+00	$\begin{array}{c} 0.000\pm 0\\ 0.000\pm 0\\$	$\begin{array}{c} 0.000\pm 0\\ 0.000\pm 0\\$	$\begin{array}{c} 0.000\pm +00\\ \end{array}$	$\begin{array}{c} -1.926E-02\\ -1.835E-02\\ -1.695E-02\\ -1.517E-02\\ -1.339E-02\\ -1.174E-02\\ 7.041E-03\\ 6.469E-03\\ 6.271E-03\\ 6.469E-03\\ 7.041E-03\\ -1.174E-02\\ -1.339E-02\\ -1.517E-02\end{array}$	$\begin{array}{c} 3.695E-01\\ 3.812E-01\\ 3.994E-01\\ 4.218E-01\\ 4.458E-01\\ 5.042E-01\\ 5.150E-01\\ 5.150E-01\\ 5.187E-01\\ 5.042E-01\\ 4.684E-01\\ 4.458E-01\\ 4.218E-01 \end{array}$	$\begin{array}{c} 1.803\pm 01\\ 1.686\pm 01\\ 1.535\pm 01\\ 1.381\pm 01\\ 1.260\pm 01\\ 1.174\pm 01\\ 1.01\pm 01\\ 1.064\pm 01\\ 1.064\pm 01\\ 1.064\pm 01\\ 1.01\pm 01\\ 1.174\pm 01\\ 1.260\pm 01\\ 1.381\pm 01 \end{array}$	$\begin{array}{c} 3.030 \pm +01\\ 2.667 \pm +01\\ 2.178 \pm +01\\ 1.674 \pm +01\\ 1.238 \pm +01\\ 9.077 \pm +00\\ 7.225 \pm +00\\ 5.920 \pm +00\\ 5.920 \pm +00\\ 7.225 \pm +00\\ 9.077 \pm +00\\ 1.238 \pm +01\\ 1.674 \pm +01 \end{array}$	$\begin{array}{c} 1.652E-12\\ 1.566E-12\\ 1.443E-12\\ 1.286E-12\\ 1.152E-12\\ 1.040E-12\\ 9.767E-13\\ 9.234E-13\\ 9.234E-13\\ 9.234E-13\\ 9.767E-13\\ 1.040E-12\\ 1.152E-12\\ 1.286E-12 \end{array}$
2 3 4 5 6 7 8 9 10 11 12 13 14 15 16	$\begin{array}{c} 9.006E+03\\ 9.028E+03\\ 9.061E+03\\ 9.100E+03\\ 9.147E+03\\ 9.194E+03\\ 9.272E+03\\ 9.297E+03\\ 9.297E+03\\ 9.297E+03\\ 9.297E+03\\ 9.194E+03\\ 9.147E+03\\ 9.100E+03\\ 9.061E+03\\ \end{array}$	7.529E+04 7.547E+04 7.576E+04 7.617E+04 7.659E+04 7.705E+04 7.785E+04 7.785E+04 7.785E+04 7.785E+04 7.765E+04 7.652E+04 7.659E+04 7.6576E+04	-8.313E+00 -7.309E+00 -6.572E+00 -5.798E+00 -3.612E+00 -3.319E+00 -3.218E+00 -3.319E+00 -3.612E+00 -3.612E+00 -5.085E+00 -6.572E+00 -7.309E+00	$\begin{array}{c} 0.000\pm+00\\ \end{array}$	$\begin{array}{c} 0.000\pm+00\\ \end{array}$	$\begin{array}{c} 0.000\pm +00\\ \end{array}$	$\begin{array}{c} -1.926\pm02\\ -1.835\pm-02\\ -1.695\pm02\\ -1.517\pm-02\\ -1.339\pm-02\\ -1.174\pm-02\\ -0.1174\pm-03\\ 6.469\pm-03\\ 6.271\pm-03\\ 6.469\pm-03\\ 7.041\pm-03\\ -1.174\pm-02\\ -1.339\pm-02\\ -1.517\pm-02\\ -1.695\pm-02\end{array}$	3.695E-01 3.812E-01 3.994E-01 4.218E-01 4.458E-01 4.684E-01 5.042E-01 5.150E-01 5.042E-01 4.684E-01 4.684E-01 4.218E-01 3.994E-01	$\begin{array}{c} 1.803\pm +01\\ 1.686\pm +01\\ 1.535\pm +01\\ 1.381\pm +01\\ 1.260\pm +01\\ 1.012\pm +01\\ 1.012\pm +01\\ 1.064\pm +01\\ 1.052\pm +01\\ 1.064\pm +01\\ 1.101\pm +01\\ 1.260\pm +01\\ 1.381\pm +01\\ 1.535\pm +01 \end{array}$	$\begin{array}{c} 3.030 \pm +01\\ 2.667 \pm +01\\ 2.178 \pm +01\\ 1.674 \pm +01\\ 1.238 \pm +01\\ 9.077 \pm +00\\ 5.920 \pm +00\\ 5.920 \pm +00\\ 5.920 \pm +00\\ 7.225 \pm +00\\ 9.077 \pm +00\\ 1.238 \pm +01\\ 1.674 \pm +01\\ 2.178 \pm +01\end{array}$	$\begin{array}{c} 1.652E-12\\ 1.566E-12\\ 1.443E-12\\ 1.286E-12\\ 1.152E-12\\ 1.040E-12\\ 9.767E-13\\ 9.234E-13\\ 9.234E-13\\ 9.234E-13\\ 9.767E-13\\ 1.040E-12\\ 1.152E-12\\ 1.286E-12\\ 1.443E-12\\ \end{array}$
2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17	$\begin{array}{c} 9.006E+03\\ 9.028E+03\\ 9.061E+03\\ 9.100E+03\\ 9.147E+03\\ 9.272E+03\\ 9.272E+03\\ 9.297E+03\\ 9.297E+03\\ 9.297E+03\\ 9.272E+03\\ 9.147E+03\\ 9.147E+03\\ 9.100E+03\\ 9.028E+03\\ \end{array}$	$\begin{array}{c} 7.529\pm04\\ 7.576\pm04\\ 7.576\pm04\\ 7.670\pm04\\ 7.659\pm04\\ 7.705\pm04\\ 7.705\pm04\\ 7.705\pm04\\ 7.785\pm04\\ 7.785\pm04\\ 7.785\pm04\\ 7.785\pm04\\ 7.765\pm04\\ 7.765\pm04\\ 7.659\pm04\\ 7.617\pm04\\ 7.617\pm04\\ 7.576\pm04\\ 7.547\pm04\\ \end{array}$	-8.313E+00 -7.916E+00 -6.572E+00 -5.798E+00 -3.612E+00 -3.319E+00 -3.319E+00 -3.319E+00 -3.612E+00 -5.085E+00 -5.798E+00 -6.572E+00 -7.309E+00 -7.916E+00	$\begin{array}{c} 0.000\pm 00\\ 0.000\pm 0.00\\ 0.000\pm 00\\ 0.000\pm 00\\ 0.000\pm 00\\ 0.000\pm 0.00\\ 0.0$	$\begin{array}{c} 0.000\pm +00\\ \end{array}$	$\begin{array}{c} 0.000E+00\\ 0.000E+0\\ 0.0$	$\begin{array}{c} -1.926E-02\\ -1.835E-02\\ -1.695E-02\\ -1.517E-02\\ -1.517E-02\\ -1.339E-02\\ -1.174E-02\\ 7.041E-03\\ 6.469E-03\\ 6.271E-03\\ 6.469E-03\\ -1.174E-02\\ -1.339E-02\\ -1.517E-02\\ -1.695E-02\\ -1.835E-02\end{array}$	$\begin{array}{c} 3.695E-01\\ 3.812E-01\\ 3.994E-01\\ 4.218E-01\\ 4.684E-01\\ 5.042E-01\\ 5.042E-01\\ 5.150E-01\\ 5.150E-01\\ 5.150E-01\\ 5.042E-01\\ 4.458E-01\\ 4.218E-01\\ 3.994E-01\\ 3.812E-01 \end{array}$	$\begin{array}{c} 1.803\pm 01\\ 1.686\pm 01\\ 1.535\pm 01\\ 1.381\pm 01\\ 1.260\pm 01\\ 1.174\pm 01\\ 1.01\pm 01\\ 1.064\pm 01\\ 1.064\pm 01\\ 1.064\pm 01\\ 1.101\pm 01\\ 1.174\pm 01\\ 1.260\pm 01\\ 1.381\pm 01\\ 1.535\pm 01\\ 1.686\pm 01 \end{array}$	$\begin{array}{c} 3.030 \pm 01\\ 2.667 \pm 01\\ 1.674 \pm 01\\ 1.674 \pm 01\\ 1.238 \pm 01\\ 9.077 \pm 00\\ 7.225 \pm 00\\ 5.920 \pm 00\\ 5.920 \pm 00\\ 7.225 \pm 00\\ 7.225 \pm 00\\ 7.225 \pm 00\\ 9.077 \pm 00\\ 1.238 \pm 01\\ 1.674 \pm 01\\ 2.178 \pm 01\\ 2.667 \pm 01\end{array}$	$\begin{array}{c} 1.652E-12\\ 1.566E-12\\ 1.443E-12\\ 1.286E-12\\ 1.152E-12\\ 1.040E-12\\ 9.767E-13\\ 9.234E-13\\ 9.056E-13\\ 9.234E-13\\ 9.234E-13\\ 1.040E-12\\ 1.152E-12\\ 1.286E-12\\ 1.566E-12\\ \end{array}$
2 3 4 5 6 7 8 9 10 11 12 13 14 15 16	$\begin{array}{c} 9.006E+03\\ 9.028E+03\\ 9.061E+03\\ 9.100E+03\\ 9.147E+03\\ 9.194E+03\\ 9.272E+03\\ 9.297E+03\\ 9.297E+03\\ 9.297E+03\\ 9.297E+03\\ 9.194E+03\\ 9.147E+03\\ 9.100E+03\\ 9.061E+03\\ \end{array}$	$\begin{array}{c} 7.529\pm04\\ 7.576\pm04\\ 7.576\pm04\\ 7.670\pm04\\ 7.659\pm04\\ 7.705\pm04\\ 7.705\pm04\\ 7.705\pm04\\ 7.785\pm04\\ 7.785\pm04\\ 7.785\pm04\\ 7.785\pm04\\ 7.765\pm04\\ 7.765\pm04\\ 7.659\pm04\\ 7.617\pm04\\ 7.617\pm04\\ 7.576\pm04\\ 7.547\pm04\\ \end{array}$	-8.313E+00 -7.309E+00 -6.572E+00 -5.798E+00 -3.612E+00 -3.319E+00 -3.218E+00 -3.319E+00 -3.612E+00 -3.612E+00 -5.085E+00 -6.572E+00 -7.309E+00	$\begin{array}{c} 0.000\pm+00\\ \end{array}$	$\begin{array}{c} 0.000\pm+00\\ \end{array}$	$\begin{array}{c} 0.000E+00\\ 0.000E+0\\ 0.0$	$\begin{array}{c} -1.926\pm02\\ -1.835\pm-02\\ -1.695\pm02\\ -1.517\pm-02\\ -1.339\pm-02\\ -1.174\pm-02\\ -0.1174\pm-03\\ 6.469\pm-03\\ 6.271\pm-03\\ 6.469\pm-03\\ 7.041\pm-03\\ -1.174\pm-02\\ -1.339\pm-02\\ -1.517\pm-02\\ -1.695\pm-02\end{array}$	$\begin{array}{c} 3.695E-01\\ 3.812E-01\\ 3.994E-01\\ 4.218E-01\\ 4.684E-01\\ 5.042E-01\\ 5.042E-01\\ 5.150E-01\\ 5.150E-01\\ 5.150E-01\\ 5.042E-01\\ 4.458E-01\\ 4.218E-01\\ 3.994E-01\\ 3.812E-01 \end{array}$	$\begin{array}{c} 1.803\pm +01\\ 1.686\pm +01\\ 1.535\pm +01\\ 1.381\pm +01\\ 1.260\pm +01\\ 1.012\pm +01\\ 1.012\pm +01\\ 1.064\pm +01\\ 1.052\pm +01\\ 1.064\pm +01\\ 1.101\pm +01\\ 1.260\pm +01\\ 1.381\pm +01\\ 1.535\pm +01 \end{array}$	$\begin{array}{c} 3.030 \pm +01\\ 2.667 \pm +01\\ 2.178 \pm +01\\ 1.674 \pm +01\\ 1.238 \pm +01\\ 9.077 \pm +00\\ 5.920 \pm +00\\ 5.920 \pm +00\\ 5.920 \pm +00\\ 7.225 \pm +00\\ 9.077 \pm +00\\ 1.238 \pm +01\\ 1.674 \pm +01\\ 2.178 \pm +01\end{array}$	$\begin{array}{c} 1.652E-12\\ 1.566E-12\\ 1.443E-12\\ 1.286E-12\\ 1.152E-12\\ 1.040E-12\\ 9.767E-13\\ 9.234E-13\\ 9.056E-13\\ 9.234E-13\\ 9.234E-13\\ 1.040E-12\\ 1.152E-12\\ 1.286E-12\\ 1.566E-12\\ \end{array}$
2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17	$\begin{array}{c} 9.006E+03\\ 9.028E+03\\ 9.061E+03\\ 9.100E+03\\ 9.147E+03\\ 9.272E+03\\ 9.272E+03\\ 9.297E+03\\ 9.297E+03\\ 9.297E+03\\ 9.272E+03\\ 9.147E+03\\ 9.147E+03\\ 9.100E+03\\ 9.028E+03\\ \end{array}$	$\begin{array}{c} 7.529\pm04\\ 7.576\pm04\\ 7.576\pm04\\ 7.670\pm04\\ 7.659\pm04\\ 7.705\pm04\\ 7.705\pm04\\ 7.705\pm04\\ 7.785\pm04\\ 7.785\pm04\\ 7.785\pm04\\ 7.785\pm04\\ 7.765\pm04\\ 7.765\pm04\\ 7.659\pm04\\ 7.617\pm04\\ 7.617\pm04\\ 7.576\pm04\\ 7.547\pm04\\ \end{array}$	-8.313E+00 -7.916E+00 -6.572E+00 -5.798E+00 -3.612E+00 -3.319E+00 -3.319E+00 -3.319E+00 -3.612E+00 -5.085E+00 -5.798E+00 -6.572E+00 -7.309E+00 -7.916E+00	$\begin{array}{c} 0.000\pm 00\\ 0.000\pm 0.00\\ 0.000\pm 00\\ 0.000\pm 00\\ 0.000\pm 00\\ 0.000\pm 0.00\\ 0.0$	$\begin{array}{c} 0.000\pm +00\\ \end{array}$	$\begin{array}{c} 0.000E+00\\ 0.000E+0\\ 0.0$	$\begin{array}{c} -1.926E-02\\ -1.835E-02\\ -1.695E-02\\ -1.517E-02\\ -1.517E-02\\ -1.339E-02\\ -1.174E-02\\ 7.041E-03\\ 6.469E-03\\ 6.271E-03\\ 6.469E-03\\ -1.174E-02\\ -1.339E-02\\ -1.517E-02\\ -1.695E-02\\ -1.835E-02\end{array}$	$\begin{array}{c} 3.695E-01\\ 3.812E-01\\ 3.994E-01\\ 4.218E-01\\ 4.684E-01\\ 5.042E-01\\ 5.042E-01\\ 5.150E-01\\ 5.150E-01\\ 5.150E-01\\ 5.042E-01\\ 4.458E-01\\ 4.218E-01\\ 3.994E-01\\ 3.812E-01 \end{array}$	$\begin{array}{c} 1.803\pm 01\\ 1.686\pm 01\\ 1.535\pm 01\\ 1.381\pm 01\\ 1.260\pm 01\\ 1.174\pm 01\\ 1.01\pm 01\\ 1.064\pm 01\\ 1.064\pm 01\\ 1.064\pm 01\\ 1.101\pm 01\\ 1.174\pm 01\\ 1.260\pm 01\\ 1.381\pm 01\\ 1.535\pm 01\\ 1.686\pm 01 \end{array}$	$\begin{array}{c} 3.030 \pm +01\\ 2.667 \pm +01\\ 1.674 \pm +01\\ 1.238 \pm +01\\ 9.077 \pm +00\\ 7.225 \pm +00\\ 5.920 \pm +00\\ 5.907 \pm +00\\ 5.920 \pm +00\\ 7.225 \pm +00\\ 9.077 \pm +00\\ 1.238 \pm +01\\ 1.674 \pm +01\\ 2.178 \pm +01\\ 2.667 \pm +01\\ \end{array}$	$\begin{array}{c} 1.652E-12\\ 1.566E-12\\ 1.443E-12\\ 1.286E-12\\ 1.152E-12\\ 1.040E-12\\ 9.767E-13\\ 9.234E-13\\ 9.056E-13\\ 9.234E-13\\ 9.234E-13\\ 1.040E-12\\ 1.152E-12\\ 1.286E-12\\ 1.566E-12\\ \end{array}$
2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18	$\begin{array}{c} 9.006E+03\\ 9.028E+03\\ 9.061E+03\\ 9.100E+03\\ 9.194E+03\\ 9.272E+03\\ 9.297E+03\\ 9.297E+03\\ 9.297E+03\\ 9.272E+03\\ 9.272E+03\\ 9.194E+03\\ 9.147E+03\\ 9.100E+03\\ 9.061E+03\\ 9.006E+03\\ \end{array}$	7.529E+04 7.547E+04 7.576E+04 7.676E+04 7.70EE+04 7.70EE+04 7.785E+04 7.785E+04 7.785E+04 7.765E+04 7.65E+04 7.659E+04 7.659E+04 7.547E+04 7.529E+04	-8.313E+00 -7.309E+00 -6.572E+00 -5.085E+00 -3.612E+00 -3.319E+00 -3.319E+00 -3.612E+00 -3.612E+00 -3.612E+00 -5.798E+00 -5.798E+00 -6.572E+00 -7.309E+00 -8.313E+00	$\begin{array}{c} 0.000\pm+00\\ 0.00$	$\begin{array}{c} 0.000\pm 00\\ 0.000\pm 0.0\\ 0.000\pm 00\\ 0.000\pm 0.000\pm 00\\ 0.000\pm 0.000\pm 0.000\pm 00\\ 0.000\pm 0$	$\begin{array}{c} 0.000\pm+00\\ 0.00$	$\begin{array}{c} -1.926E-02\\ -1.835E-02\\ -1.695E-02\\ -1.517E-02\\ -1.517E-02\\ -1.339E-02\\ -1.174E-02\\ 7.041E-03\\ 6.469E-03\\ 6.469E-03\\ 7.041E-03\\ -1.174E-02\\ -1.339E-02\\ -1.339E-02\\ -1.517E-02\\ -1.835E-02\\ -1.835E-02\\ -1.926E-02\\ \end{array}$	3.695E-01 3.812E-01 3.994E-01 4.218E-01 4.458E-01 5.042E-01 5.150E-01 5.042E-01 5.042E-01 4.458E-01 4.458E-01 4.218E-01 3.994E-01 3.695E-01	$\begin{array}{c} 1.803E+01\\ 1.686E+01\\ 1.535E+01\\ 1.260E+01\\ 1.174E+01\\ 1.01E+01\\ 1.064E+01\\ 1.064E+01\\ 1.064E+01\\ 1.101E+01\\ 1.260E+01\\ 1.381E+01\\ 1.686E+01\\ 1.803E+01\\ \end{array}$	$\begin{array}{c} 3.030 \pm +01\\ 2.667 \pm +01\\ 1.674 \pm +01\\ 1.238 \pm +01\\ 9.077 \pm +00\\ 7.225 \pm +00\\ 5.920 \pm +00\\ 5.907 \pm +00\\ 5.920 \pm +00\\ 7.225 \pm +00\\ 9.077 \pm +00\\ 1.238 \pm +01\\ 1.674 \pm +01\\ 2.178 \pm +01\\ 2.667 \pm +01\\ \end{array}$	$\begin{array}{c} 1.652E-12\\ 1.566E-12\\ 1.443E-12\\ 1.286E-12\\ 1.152E-12\\ 1.040E-12\\ 9.767E-13\\ 9.234E-13\\ 9.234E-13\\ 9.234E-13\\ 9.234E-13\\ 9.767E-13\\ 1.040E-12\\ 1.152E-12\\ 1.266E-12\\ 1.443E-12\\ 1.556E-12\\ 1.652E-12\\ \end{array}$

no (m/s) (N) (N.m) (W) Outer Race Inner Race Outer Race Inner Race Outer Race Inner Race Outer Race Inner Race (Drag+Chur)

1 2 3	1.978E+00 1.967E+00 1.937E+00	4.216E+00 4.212E+00 4.197E+00	7.673E-03 7.608E-03 7.433E-03	1.267E-02 1.253E-02 1.214E-02	1.293E-06 1.294E-06 1.298E-06	1.188E-06 1.190E-06 1.194E-06	3.559E-01 3.559E-01 3.559E-01	3.908E-01 3.919E-01 3.951E-01
4	1.895E+00	4.169E+00	7.191E-03	1.156E-02	1.304E-06	1.202E-06	3.557E-01	4.000E-01
5	1.785E+00	4.122E+00	6.412E-03	1.087E-02	1.311E-06	1.212E-06	3.543E-01	4.057E-01
6	1.730E+00	4.055E+00	6.096E-03	1.016E-02	1.318E-06	1.223E-06	3.535E-01	4.121E-01
7	1.683E+00	3.973E+00	5.834E-03	9.503E-03	1.325E-06	1.234E-06	3.524E-01	4.182E-01
8	1.637E+00	4.014E+00	5.672E-03	9.171E-03	1.333E-06	1.241E-06	3.502E-01	4.244E-01
9	1.626E+00	3.937E+00	5.611E-03	8.796E-03	1.336E-06	1.248E-06	3.497E-01	4.277E-01
10	1.622E+00	3.909E+00	5.591E-03	8.665E-03	1.337E-06	1.250E-06	3.495E-01	4.289E-01
11	1.626E+00	3.937E+00	5.611E-03	8.796E-03	1.336E-06	1.248E-06	3.497E-01	4.277E-01
12	1.637E+00	4.014E+00	5.672E-03	9.171E-03	1.333E-06	1.241E-06	3.502E-01	4.244E-01
13	1.683E+00	3.973E+00	5.834E-03	9.503E-03	1.325E-06	1.234E-06	3.524E-01	4.182E-01
14	1.730E+00	4.055E+00	6.096E-03	1.016E-02	1.318E-06	1.223E-06	3.535E-01	4.121E-01
15	1.785E+00	4.122E+00	6.412E-03	1.087E-02	1.311E-06	1.212E-06	3.543E-01	4.057E-01
16	1.895E+00	4.169E+00	7.191E-03	1.156E-02	1.304E-06	1.202E-06	3.557E-01	4.000E-01
17	1.937E+00	4.197E+00	7.433E-03	1.214E-02	1.298E-06	1.194E-06	3.559E-01	3.951E-01
18	1.967E+00	4.212E+00	7.608E-03	1.253E-02	1.294E-06	1.190E-06	3.559E-01	3.919E-01

RE	Rel Axial	.Contact De	flection.	Race Fl	exing	Contact '	Cemp Rise	Contac	t. Temp	Bulk Temp	Convec HTC
no	Pos	(n		(n		(1		(K		(K)	
	(m)							Outer Race	Inner Race	. ,	(W/m**2/K)
1	-7.498E-05	1.595E-05	8.916E-06	0.000E+00	0.000E+00	6.288E-01	2.437E+00	3.230E+02	3.230E+02	3.230E+02	0.000E+00
2	-7.594E-05	1.588E-05	8.762E-06	0.000E+00	0.000E+00	6.159E-01	2.365E+00	3.230E+02	3.230E+02	3.230E+02	0.000E+00
3	-7.870E-05	1.568E-05	8.330E-06	0.000E+00	0.000E+00	5.816E-01	2.167E+00	3.230E+02	3.230E+02	3.230E+02	0.000E+00
4	-8.291E-05	1.540E-05	7.698E-06	0.000E+00	0.000E+00	5.369E-01	1.883E+00	3.230E+02	3.230E+02	3.230E+02	0.000E+00
5	-8.800E-05	1.510E-05	6.964E-06	0.000E+00	0.000E+00	4.807E-01	1.567E+00	3.230E+02	3.230E+02	3.230E+02	0.000E+00
6	-9.336E-05	1.483E-05	6.230E-06	0.000E+00	0.000E+00	4.424E-01	1.266E+00	3.230E+02	3.230E+02	3.230E+02	0.000E+00
7	-9.829E-05	1.462E-05	5.575E-06	0.000E+00	0.000E+00	4.148E-01	1.014E+00	3.230E+02	3.230E+02	3.230E+02	0.000E+00
8	-1.024E-04	1.454E-05	5.067E-06	0.000E+00	0.000E+00	3.928E-01	8.725E-01	3.230E+02	3.230E+02	3.230E+02	0.000E+00
9	-1.049E-04	1.445E-05	4.737E-06	0.000E+00	0.000E+00	3.814E-01	7.542E-01	3.230E+02	3.230E+02	3.230E+02	0.000E+00
10	-1.058E-04	1.442E-05	4.624E-06	0.000E+00	0.000E+00	3.778E-01	7.152E-01	3.230E+02	3.230E+02	3.230E+02	0.000E+00
11	-1.049E-04	1.445E-05	4.737E-06	0.000E+00	0.000E+00	3.814E-01	7.542E-01	3.230E+02	3.230E+02	3.230E+02	0.000E+00
12	-1.024E-04	1.454E-05	5.067E-06	0.000E+00	0.000E+00	3.928E-01	8.725E-01	3.230E+02	3.230E+02	3.230E+02	0.000E+00
13	-9.829E-05	1.462E-05	5.575E-06	0.000E+00	0.000E+00	4.148E-01	1.014E+00	3.230E+02	3.230E+02	3.230E+02	0.000E+00
14	-9.336E-05	1.483E-05	6.230E-06	0.000E+00	0.000E+00	4.424E-01	1.266E+00	3.230E+02	3.230E+02	3.230E+02	0.000E+00
15	-8.800E-05	1.510E-05	6.964E-06	0.000E+00	0.000E+00	4.807E-01	1.567E+00	3.230E+02	3.230E+02	3.230E+02	0.000E+00
16	-8.291E-05	1.540E-05	7.698E-06	0.000E+00	0.000E+00	5.369E-01	1.883E+00	3.230E+02	3.230E+02	3.230E+02	0.000E+00
17	-7.870E-05	1.568E-05	8.330E-06	0.000E+00	0.000E+00	5.816E-01	2.167E+00	3.230E+02	3.230E+02	3.230E+02	0.000E+00
18	-7.594E-05	1.588E-05	8.762E-06	0.000E+00	0.000E+00	6.159E-01	2.365E+00	3.230E+02	3.230E+02	3.230E+02	0.000E+00

step	tau	Time	Outer Race Rot	Inner Race Rot	(ADORE 5.0)
no		(s)	(rev)	(rev)	
0	0.000E+00	0.000E+00	0.000E+00	0.000E+00	Ball Bearing Test Case kGeoMod=100
====	=========		=========	=========	

2. Race and Cage Parameters

	RE				RE/Cage Inte	eraction					
	NO C				Con Ang				Time Ave		
	C			THETA			Pos Z				
		(m)	(N)	(deg)	(deg)	(m)	(m)	(W)	(m**3/s)		
	1 0	5.844E-04	0.000E+00	2.700E+02	0.000E+00	9.541E-03	1.544E-03	0.000E+00	0.000E+00		
	2 0			3.558E+02			1.508E-03		0.000E+00		
	3 0	2.206E-04	0.000E+00	3.582E+02	0.000E+00	3.110E-04	1.406E-03	0.000E+00	0.000E+00		
	4 0	8.900E-05	0.000E+00	3.591E+02	0.000E+00	1.513E-04	1.249E-03	0.000E+00	0.000E+00		
	5 0	1.898E-05	0.000E+00	3.597E+02	0.000E+00	4.552E-05	1.057E-03	0.000E+00	0.000E+00		
	60	1.897E-05	0.000E+00	2.702E-01	0.000E+00	-4.766E-05			0.000E+00		
	7 0	8.900E-05	0.000E+00	8.609E-01	0.000E+00	-1.508E-04	6.600E-04	0.000E+00	0.000E+00		
	8 0		0.000E+00			-3.076E-04					
		3.977E-04					4.009E-04		0.000E+00		
	10 0			9.000E+01			3.654E-04		0.000E+00		
	11 0			1.759E+02			4.009E-04				
	12 0			1.782E+02		-3.076E-04			0.000E+00		
	13 0			1.791E+02			6.600E-04		0.000E+00		
	14 0			1.797E+02		-4.766E-05					
	15 0			1.803E+02			1.057E-03	0.000E+00			
	16 0			1.809E+02			1.249E-03				
	17 0			1.818E+02			1.406E-03		0.000E+00		
	18 0	3.977E-04	0.000E+00	1.842E+02	0.000E+00	7.055E-04	1.508E-03	0.000E+00	0.000E+00		
	LD C		Race/Cage I	nteraction.		Effective	Contact	Time Ave			
	NO C	Geo Int	Force	Con Angle	Att Angle	Dia Play	Loss	Wear Rate			
		(m)	(N)	(deg)	(deg)	(m)	(W)	(m**3/s)			
	1 0	1 2175-04	0 000 - 00	0 000 - 00	0.000E+00	1 4428-02	0 00000+00	0 000 - 00			
		1.217E-04			0.000E+00						
	20	1.21/5 04	0.000100	0.000100	0.0001100	1.445E 05	0.000100	0.000100			
					Angı						
	Axial	Radial			Amplitude		Phi		Phi		Wear Rate
	(m)	(m)	(deg)	(rpm)	(rpm)	(deg)	(deg)	(deg)	(deg)	(Pa)	(
Cage	4.285E-05	5.900E-04	1.800E+02	9.140E+03	9.140E+03	0.000E+00	0.000E+00	0.000E+00	0.000E+00	0.000E+00	0.000E+00
ORace	0.000E+00						0.000E+00			-6.402E+06	
IRace		1.002E-05			2.000E+04					1.184E+08	

step no	tau	Time (s)	Outer Race Rot (rev)	Inner Race Rot (rev)	(ADORE 5.0)
0	0.000E+00	0.000E+00	0.000E+00	0.000E+00	Ball Bearing Test Case kGeoMod=100
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3. Applied Parameters -----

							Basic Fat	ique Life	(hours)	5.334E+02	
	Forces i	n Inertial	Frame	Moments i	n Body-Fixe	d Frame		<u> </u>	(hours)	4.460E+03	
	x-qmoD	Comp-y		Comp-x	Comp-y	Comp-z	Outer Rac		(m)	1.000E-05	
	<u>-</u>		<u>-</u>			<u>-</u>			. ,	9.918E-07	
	(N)	(N)	(N)	(N.m)	(N.m)	(N.m)	Inner Rac		(m)		
							Internal	Clearance	(m)	1.525E-04	
Cage	0.000E+00	0.000E+00	0.000E+00	0.000E+00	0.000E+00	0.000E+00					
Int ORace	4.495E+03	-7.394E+01	1.453E+03	-3.472E-01	6.726E+01	4.428E-03	Total Pow	er Loss	(W)	5.464E+02	
Int IRace	-4.495E+03	-4 926E-01	-1 995E+03	-1.004E-01	-6.827E+01	-3 967E-02	Churning	Loss Fraction		0.000E+00	
Ext ORace	-4.495E+03		-1.440E+03		-6.726E+01	-4 428E-03		d Temperature		0.000E+00	
Ext IRace	4.495E+03	4.926E-01	2.003E+03	1.004E-01	6.827E+01	3.967E-02	DATC LIGI	a remperature	(10)	0.0001.00	
EXU INACE	4.4956+05	4.9206-01	2.003E+03	1.004E-01	0.02/6+01	3.90/E-02					
			-						()	2 2225 22	
	MC Acc i		Frame	Ang Acc 1	n Body-Fıxe	d Frame		Hsng/Bulk Ter	± , ,	3.230E+02	
		(m/s**2)			(rpm/s)		(K)	Hsng/Outer Te	emp (K)	3.230E+02	
	Comp-x	Comp-y	Comp-z	Comp-x	Comp-y	Comp-z		Hsng/Inner Te	emp (K)	3.230E+02	
	-		-	-		-		Shft/Bulk Ter	mp (K)	3.230E+02	
Cage	0.000E+00	0.000E+00	-9.810E+00	0.000E+00	0.000E+00	0.000E+00	3.230E+02				
	0.000E+00	0.000E+00	0.000E+00	0.000E+00	0.000E+00	0.000E+00	3.230E+02	abft (out on m	(77)	3.230E+02	
ORace								Shft/Outer Te			
IRace	0.000E+00	0.000E+00	0.000E+00	0.000E+00	0.000E+00	0.000E+00	3.230E+02	Shft/Inner Te	emp (K)	3.230E+02	

4. Time Step Summary

Step	Time	Outer Race	Inner Race	Fatigue	Power	RE Orbital	Cage Omega	Cage Whirl	Cage	Average RE		
no		Rotation	Rotation	Life	Loss	Vel Ratio	Ratio	Ratio	Wear Rate	Excursion		
	(s)	(rev)	(rev)	(hours)	(W)				(m**3/s)	(m)		
0	0.000E+00	0.000E+00	0.000E+00	4.460E+03	5.464E+02	4.570E-01	4.570E-01	4.570E-01	0.000E+00	1.174E-03		

step	tau	Time	Outer Race Rot	Inner Race Rot	(ADORE 5.0)
no		(s)	(rev)	(rev)	
2500	3.534E+02	8.612E-02	0.000E+00	2.871E+01	Ball Bearing Test Case kGeoMod=100
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1. Rolling Element Parameters

Re no	Orbital Position			Contact						Minor Hal	
										Outer Race	Inner Race
	(===),										
1	4.347E+03	7.675E+00	2.782E+01	2.416E+03	6.914E+02	1.568E+09	1.337E+09	2.354E-03	1.205E-03	3.125E-04	2.049E-04
2	4.367E+03	7.241E+00	2.809E+01	2.359E+03	6.316E+02	1.556E+09	1.297E+09	2.335E-03	1.169E-03	3.100E-04	1.988E-04
3	4.387E+03	6.708E+00	2.843E+01	2.293E+03	5.626E+02	1.541E+09	1.248E+09	2.313E-03	1.125E-03	3.071E-04	1.914E-04
4	4.407E+03	6.127E+00	2.881E+01	2.229E+03	4.937E+02	1.527E+09	1.194E+09	2.291E-03	1.077E-03	3.042E-04	1.833E-04
5	4.427E+03	5.592E+00	2.916E+01	2.172E+03	4.344E+02	1.513E+09	1.144E+09	2.271E-03	1.032E-03	3.016E-04	1.756E-04
б	4.447E+03	5.120E+00	2.947E+01	2.137E+03	3.876E+02	1.505E+09	1.101E+09	2.259E-03	9.936E-04	3.000E-04	1.691E-04
7	4.467E+03	4.830E+00	2.967E+01	2.113E+03	3.594E+02	1.499E+09	1.074E+09	2.251E-03	9.688E-04	2.989E-04	1.650E-04
8	4.487E+03	4.596E+00	2.982E+01	2.084E+03	3.358E+02	1.493E+09	1.050E+09	2.241E-03	9.471E-04	2.976E-04	1.613E-04
9	4.507E+03	4.854E+00	2.969E+01	2.108E+03	3.601E+02	1.498E+09	1.074E+09	2.249E-03	9.694E-04	2.987E-04	1.651E-04
10	4.527E+03	4.743E+00	2.973E+01	2.104E+03	3.508E+02	1.497E+09	1.065E+09	2.248E-03	9.610E-04	2.985E-04	1.636E-04
11	4.547E+03	5.091E+00	2.950E+01	2.139E+03	3.855E+02	1.506E+09	1.099E+09	2.260E-03	9.917E-04	3.002E-04	1.688E-04
12	4.567E+03	5.555E+00	2.920E+01	2.185E+03	4.336E+02	1.516E+09	1.143E+09	2.276E-03	1.031E-03	3.023E-04	1.755E-04
13	4.588E+03	6.114E+00	2.883E+01	2.245E+03	4.957E+02	1.530E+09	1.196E+09	2.297E-03	1.079E-03	3.050E-04	1.835E-04
14	4.608E+03	6.703E+00	2.845E+01	2.311E+03	5.661E+02	1.545E+09	1.250E+09	2.319E-03	1.127E-03	3.079E-04	1.918E-04
15	4.628E+03	7.264E+00	2.809E+01	2.360E+03	6.336E+02	1.556E+09	1.298E+09	2.335E-03	1.171E-03	3.100E-04	1.990E-04
16	4.648E+03	7.639E+00	2.785E+01	2.415E+03	6.871E+02	1.568E+09	1.334E+09	2.353E-03	1.203E-03	3.124E-04	2.045E-04
17	4.668E+03	7.914E+00	2.768E+01	2.454E+03	7.276E+02	1.577E+09	1.360E+09	2.366E-03	1.226E-03	3.141E-04	2.084E-04
18	4.688E+03	8.352E+00	2.744E+01	2.506E+03	7.900E+02	1.588E+09	1.398E+09	2.383E-03	1.260E-03	3.163E-04	2.141E-04
RE	Orbital	Ang	gular Veloc:	ity	RE Ang 1	Position	Spin	/Roll	Contact	Loss (W)	Time Ave
	Velocity	Amplitude	Theta								
	(rpm)	(rpm)	(deg)	(deg)	(deg)	(deg)	Outer Race	Inner Race	Outer Race	Inner Race	(m**3/s)
1	9.094E+03	7.611E+04	-6.154E+00	6.906E-05	1.012E+01	1.447E+02	1.201E-02	4.129E-01	1.632E+01	2.735E+01	2.149E-13
2	9 0968+03	$7 612 E \pm 04$	-6 0748+00	1 6668-05	$1 402 E \pm 01$	1 936 - 02	6 0208-03	4 1998-01	$1 457 E \pm 01$	2 271 8+01	2 0548-13

	(+ Piii)	(pin)	(acg)	(acg)	(acg)	(acg)	outer nace	TIMET Race	outer hace	TIMET Race	(
1	9.094E+03	7.611E+04	-6.154E+00	6.906E-05	1.012E+01	1.447E+02	1.201E-02	4.129E-01	1.632E+01	2.735E+01	2.149E-13
2	9.096E+03	7.612E+04	-6.074E+00	1.666E-05	1.402E+01	1.936E+02	6.020E-03	4.199E-01	1.457E+01	2.271E+01	2.054E-13
3	9.094E+03	7.611E+04	-6.141E+00	3.600E+02	1.374E+01	1.931E+02	-4.609E-03	4.257E-01	1.307E+01	1.822E+01	2.045E-13
4	9.096E+03	7.612E+04	-6.186E+00	3.600E+02	1.325E+01	1.929E+02	-1.563E-02	4.326E-01	1.255E+01	1.432E+01	2.037E-13
5	9.092E+03	7.610E+04	-6.335E+00	3.600E+02	1.249E+01	1.942E+02	-2.794E-02	4.372E-01	1.316E+01	1.145E+01	2.031E-13
6	9.115E+03	7.629E+04	-6.340E+00	3.600E+02	1.181E+01	1.928E+02	-3.627E-02	4.436E-01	1.413E+01	8.797E+00	2.038E-13
7	9.121E+03	7.635E+04	-6.346E+00	3.600E+02	1.116E+01	1.912E+02	-4.146E-02	4.477E-01	1.480E+01	7.595E+00	2.030E-13
8	9.104E+03	7.622E+04	-6.331E+00	3.600E+02	9.697E+00	1.884E+02	-4.526E-02	4.512E-01	1.505E+01	7.474E+00	2.031E-13
9	9.107E+03	7.624E+04	-6.329E+00	3.600E+02	9.558E+00	1.863E+02	-4.072E-02	4.485E-01	1.450E+01	8.171E+00	2.013E-13
10	9.118E+03	7.633E+04	-6.202E+00	3.600E+02	9.284E+00	1.866E+02	-4.012E-02	4.516E-01	1.431E+01	7.608E+00	2.014E-13
11	9.127E+03	7.639E+04	-6.095E+00	3.600E+02	9.338E+00	1.849E+02	-3.192E-02	4.487E-01	1.334E+01	8.763E+00	1.999E-13

13 14 15 16 17		7.642E+04 7.641E+04 7.610E+04 7.617E+04 7.619E+04	-6.010E+00 -5.998E+00 -5.972E+00 -5.953E+00 -6.113E+00	3.600E+02 3.600E+02 1.996E-03 3.600E+02 3.600E+02	1.092E+01 1.164E+01 1.234E+01 1.299E+01 1.379E+01	1.879E+02 1.881E+02 1.895E+02 1.930E+02 1.924E+02	-1.239E-02 -1.867E-03 8.449E-03 1.535E-02 1.700E-02	4.170E-01	1.264E+01 1.346E+01 1.477E+01 1.669E+01 1.791E+01	1.411E+01 1.880E+01 2.305E+01 2.725E+01 3.093E+01	1.993E-13 1.990E-13 2.009E-13 2.091E-13 2.042E-13
RE	Slip Ve	locity	Trac (Coeff	Iso Luk	o Film	Thermal	Red Fac	Drag	Chrn Mom	Net Loss
no	(m/	s)			(n	n)			(N)	(N.m)	(W)
	Outer Race	Inner Race	Outer Race	Inner Race	Outer Race	Inner Race	Outer Race	Inner Race		(Drag+Chur)
			6.869E-03								
			6.274E-03								
	1.662E+00		5.963E-03				3.546E-01				
	1.788E+00		6.451E-03				3.557E-01				
	1.936E+00		7.005E-03				3.569E-01				
	2.045E+00	4.166E+00					3.567E-01				
	2.108E+00		7.613E-03				3.570E-01				
	2.140E+00		7.684E-03				3.581E-01				
	2.088E+00		7.516E-03								
	2.079E+00		7.473E-03								
	1.981E+00		7.140E-03				3.561E-01				
12	1.887E+00	4.108E+00					3.552E-01				
13	1.757E+00	4.065E+00		1.042E-02			3.541E-01				
	1.639E+00	4.031E+00			1.313E-06		3.530E-01				
	1.742E+00	4.449E+00			1.307E-06						
	1.886E+00		7.095E-03								
			7.363E-03								
18	2.079E+00	4.393E+00	8.062E-03	1.280E-02	1.300E-06	1.183E-06	3.517E-01	3.892E-01			
RE	Rel Axial	.Contact De	eflection	Race Fl	lexing	Contact '	ſemp Rise	Contac	t Temp	Bulk Temp	Convec HTC

RE	Rei Axiai	.Contact De	erlection	Race F	Lexing	Contact 1	Cemp Rise	Contac	t Temp	BUIK Temp	Conved HTC
no	Pos	(n	n)	(r	n)	(F	ζ)	(K)	(K)	
	(m)	Outer Race	Inner Race	Outer Race			Inner Race	Outer Race	Inner Race		(W/m**2/K)
1	-8.067E-05	1.570E-05	8.152E-06	0.000E+00	0.000E+00	5.579E-01	2.265E+00	3.428E+02	3.433E+02	3.354E+02	2.620E+06
2	-8.367E-05	1.545E-05	7.674E-06	0.000E+00	0.000E+00	5.048E-01	1.972E+00	3.418E+02	3.471E+02	3.354E+02	2.620E+06
3	-8.737E-05	1.516E-05	7.105E-06	0.000E+00	0.000E+00	4.596E-01	1.678E+00	3.427E+02	3.535E+02	3.364E+02	2.618E+06
4	-9.139E-05	1.488E-05	6.512E-06	0.000E+00	0.000E+00	4.460E-01	1.409E+00	3.451E+02	3.606E+02	3.382E+02	2.617E+06
5	-9.511E-05	1.462E-05	5.978E-06	0.000E+00	0.000E+00	4.705E-01	1.199E+00	3.480E+02	3.663E+02	3.407E+02	2.614E+06
6	-9.838E-05	1.447E-05	5.541E-06	0.000E+00	0.000E+00	5.062E-01	9.800E-01	3.512E+02	3.707E+02	3.437E+02	2.612E+06
7	-1.004E-04	1.436E-05	5.268E-06	0.000E+00	0.000E+00	5.312E-01	8.794E-01	3.543E+02	3.735E+02	3.472E+02	2.610E+06
8	-1.020E-04	1.423E-05	5.036E-06	0.000E+00	0.000E+00	5.428E-01	8.876E-01	3.539E+02	3.680E+02	3.477E+02	2.611E+06
9	-1.003E-04	1.434E-05	5.275E-06	0.000E+00	0.000E+00	5.213E-01	9.399E-01	3.593E+02	3.691E+02	3.535E+02	2.611E+06
10	-1.010E-04	1.432E-05	5.184E-06	0.000E+00	0.000E+00	5.147E-01	8.889E-01	3.541E+02	3.582E+02	3.476E+02	2.613E+06
11	-9.861E-05	1.448E-05	5.521E-06	0.000E+00	0.000E+00	4.781E-01	9.801E-01	3.542E+02	3.530E+02	3.464E+02	2.614E+06
12	-9.540E-05	1.468E-05	5.971E-06	0.000E+00	0.000E+00	4.572E-01	1.139E+00	3.541E+02	3.483E+02	3.445E+02	2.615E+06
13	-9.152E-05	1.495E-05	6.529E-06	0.000E+00	0.000E+00	4.478E-01	1.390E+00	3.529E+02	3.438E+02	3.420E+02	2.616E+06
14	-8.744E-05	1.524E-05	7.134E-06	0.000E+00	0.000E+00	4.713E-01	1.726E+00	3.518E+02	3.407E+02	3.400E+02	2.617E+06
15	-8.356E-05	1.546E-05	7.691E-06	0.000E+00	0.000E+00	5.095E-01	1.998E+00	3.501E+02	3.386E+02	3.382E+02	2.618E+06
16	-8.094E-05	1.570E-05	8.118E-06	0.000E+00	0.000E+00	5.696E-01	2.264E+00	3.475E+02	3.373E+02	3.365E+02	2.619E+06
17	-7.904E-05	1.587E-05	8.434E-06	0.000E+00	0.000E+00	6.060E-01	2.490E+00	3.460E+02	3.404E+02	3.367E+02	2.618E+06
18	-7.613E-05	1.609E-05	8.910E-06	0.000E+00	0.000E+00	6.886E-01	2.745E+00	3.519E+02	3.489E+02	3.440E+02	2.616E+06

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2500	3.534E+02	8.612E-02	0.000E+00	2.871E+01	Ball Bearing Test Case kGeoMod=100
no		(s)	(rev)	(rev)	
step	tau	Time	Outer Race Rot	Inner Race Rot	(ADORE 5.0)

2. Race and Cage Parameters

RE			R	E/Cage Inte	eraction			
NO C	Geo Int	Con Ang	Con Ang	Con Ang	Contact	Contact	Contact	Time Ave
С		Force	THETA	PHI	Pos X	Pos Z	Loss	Wear Rate
	(m)	(N)	(deg)	(deg)	(m)	(m)	(W)	(m**3/s)
1 0	5.830E-04	0.000E+00	3.463E+02	0.000E+00		7.258E-04	0.000E+00	6.826E-12
2 0	3.686E-04	0.000E+00	1.785E+02		-2.535E-04	7.000E-04	0.000E+00	2.838E-12
3 0	3.859E-04	0.000E+00	1.720E+02		-1.360E-03	7.081E-04	0.000E+00	2.148E-12
4 0	4.971E-04	0.000E+00	1.423E+02		-5.887E-03	7.481E-04	0.000E+00	2.878E-12
5 0	4.770E-06	0.000E+00	1.009E+01		-1.774E-03	8.107E-04	0.000E+00	3.116E-12
60	8.030E-05	0.000E+00	1.640E+01		-2.838E-03	8.977E-04	0.000E+00	3.386E-12
70	1.728E-04	0.000E+00	2.573E+01		-4.323E-03	9.940E-04	0.000E+00	3.926E-12
8 0	5.334E-05	0.000E+00	2.337E+01		-3.997E-03	1.086E-03	0.000E+00	5.003E-12
90	3.130E-04	0.000E+00	5.465E+01	0.000E+00	-8.007E-03	1.167E-03	0.000E+00	5.094E-12
10 0	3.101E-04	0.000E+00	5.597E+01		-8.138E-03	1.224E-03	0.000E+00	5.149E-12
11 0	2.266E-04	0.000E+00	1.419E+02		-6.107E-03	1.250E-03	0.000E+00	3.916E-12
12 0	2.107E-04	0.000E+00	3.212E+01		-5.275E-03	1.242E-03	0.000E+00	2.846E-12
13 0	1.697E-04	0.000E+00	1.565E+02		-3.969E-03	1.201E-03	0.000E+00	1.696E-12
14 0	1.038E-04	0.000E+00	1.648E+02		-2.628E-03	1.132E-03	0.000E+00	3.033E-12
15 0	1.181E-05	0.000E+00	1.715E+02	0.000E+00	-1.495E-03	1.044E-03	0.000E+00	2.686E-12
16 0	5.913E-05	0.000E+00	1.749E+02	0.000E+00	-8.948E-04	9.488E-04	0.000E+00	5.201E-12
17 0	2.713E-04	0.000E+00	1.770E+02		-5.197E-04	8.581E-04	0.000E+00	4.808E-12
18 0	6.551E-05	0.000E+00	1.804E+02	0.000E+00	7.453E-05	7.765E-04	0.000E+00	5.625E-12
	R					Contact	Time Ave	
NO C	Geo Int	Force	Con Angle	Att Angle	Dia Play	Loss	Wear Rate	

(m)	(N)	(deg)	(deg)	(m)	(W)	(m**3/s)
				1.472E-03 1.472E-03		

	Mass Axial (m)	Center Pos Radial (m)	Orbital		Amplitude		ty Phi (deg)	Ang Pos Theta (deg)	Phi	Stress	Time Ave Wear Rate (m**3/s)
ORace	0.000E+00	0.000E+00	0.000E+00	0.000E+00	0.000E+00	0.000E+00	0.000E+00	9.271E-02 0.000E+00 0.000E+00	0.000E+00	-9.333E+06	1.792E-12

=====					
2500	3.534E+02	8.612E-02	0.000E+00	2.871E+01	Ball Bearing Test Case kGeoMod=100
no		(s)	(rev)	(rev)	
step	tau	Time	Outer Race Rot	Inner Race Rot	(ADORE 5.0)

3. Applied Parameters

							Basic Fat	ique Life	(hours)	5.515E+02	
	Forces i	n Inertial	Frame	Moments i	n Body-Fixe	d Frame	Modified	Fatique Life	(hours)	4.594E+03	
	Comp-x	Comp-y	Comp-z	Comp-x	Comp-y	Comp-z	Outer Rac	e Fit	(m)	1.458E-05	
	(N)	(N)	(N)	(N.m)	(N.m)	(N.m)	Inner Rac	e Fit	(m)	-2.484E-05	
	()	()	()	(,	(,	(,		Clearance	(m)	1.537E-04	
Cage	0.000E+00	0.000E+00	0.000E+00	0.000E+00	0.000E+00	0.000E+00			()		
Int ORace	4.457E+03	-6.830E+01	1 694E+03	-1.153E-01	5 525E+01	-1.273E+00	Total Pow	er Loss	(W)	5.677E+02	
Int IRace					1.426E+01			Loss Fraction		0.000E+00	
Ext ORace	-4.457E+03		-1.682E+03		-5.525E+01	1.273E+00		d Temperature		3.419E+02	
Ext IRace	4.457E+03		1.639E+03		-1.426E+01	5.424E+01	DATC ITUI	a remperature	(10)	5.1190.02	
BAC INACC	4.4571105	5.2046101	1.0398103	0.0505 01	1.4205.01	5.1216:01					
	MC Acc i	n Inertial	Frame	Ang Acc i	n Body-Five	d Frame	Bulk Temp	Hsng/Bulk Te	mp (K)	3.468E+02	
		(m/s**2)	110mc	ig nee i	(rpm/s)	a rranc	(K)	Hsng/Outer T	± ` '	3.457E+02	
	x-qmoD	Comp-y	Comp-z	Comp-x	Comp-y	Comp-z	(10)	Hsng/Inner T		3.480E+02	
	COMP X	comp y	COMP 2	COMP X	comp y	COMP 2		Shft/Bulk Te		3.293E+02	
0	0.000E+00	0.000E+00	-9.810E+00	0.000E+00	7.266E+00	8.652E-01	3.420E+02	SHIL/BUIK IE	mp (n)	3.2936+02	
Cage								abft (out on m	(TC)	2 4060.00	
ORace	0.000E+00	0.000E+00	0.000E+00	0.000E+00	0.000E+00	0.000E+00	3.490E+02	Shft/Outer T		3.496E+02	
IRace	0.000E+00	0.000E+00	0.000E+00	0.000E+00	0.000E+00	0.000E+00	3.514E+02	Shft/Inner T	emp (K)	3.174E+02	

4. Time Step Summary

						'ime Average	Parameters			
Step	Time		Inner Race	Fatigue		RE Orbital				
no				Life		Vel Ratio	Ratio	Ratio		
	(s)	(rev)	(rev)	(hours)	(W)				(m**3/s)	(m)
2500	8 6128-02	0 000 -	2.871E+01	6 9528+02	1 406 - 402	7 0248-02	7 0248-02	7 3068-02	2 4568-10	1 8415-04
2000	0.0125 02	0.000100	2.0/101	0.9521102	1.4000102	7.0246 02	7.0246 02	7.500E 02	2.4306 10	1.0410 04
	Normal te	rmination:	Last Step N	umber =	2500	Final Time	= 3.5340	E+02		
			<u>-</u>							

Statistics of this Run

Minimum Object Of		E 00000E 03
Minimum Step Size		5.00000E-03
Maximum Step Size	=	1.86684E-01
Last Step Size	=	1.64618E-01
Max Truncation	=	1.72086E-03
Total Derivative Calls	=	21160

Appendix D - Cylindrical Roller Bearing Data

Adore input data for the roller bearing case with the associated print ouput is documented below. Only the output and initial and final time steps is included for brevity.

```
1 0 0 0 1 500 2 0 0 1
5.0000E-02 1.0000E-04 5.0000E-01 1.0000E+03 1.0000E-04 5.0000E-02
0 0 0 1
                                                                                                                                                                                                                                                                                                                                                              4000
                                                                                                                                                                                                                                                                                                                                                                                                       0
                                                                                                                                                                                                                                                                                                                                                                                                                            5
Rec 1
Rec 2.1
Rec 2.4
                                                       0 U U L
0.0000E+00 0.0000E+00 0.0000E+00 8.5700E-04 8.5700E-04
2.9400E+02 2.9400E+02 2.9400E+02 2.9400E+02 2.9400E+02 2.9400E+02
Rec 2.5
Rec 2.7
                                                    Cyl Roller Bearing Geo Mod
Rec 3.1

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Rec 3.2
Rec 3.3
Rec 3.4
Rec 4
Rec 5B
Rec 5B.1
                                                       1.0000E-02 0.0000E+00 1.0000E-02 0.0000E+00
Rec 7.0
Rec 7.1
                                                        0 0 0 0 0 0 0 0 2 1 1
4.5000E-02 4.0000E-02 1.0000E-02 1.0000E-04 1.0000E-03 1.0000E-04 0.0000E+00 0.0000E+00 0.0000E+00
Rec 7.2.1
Rec 7.2.2
Rec 8.1
                                                       4.5000E-02 1.0000E-03 5.0000E-03 1.0000E-04
4.5000E-02 1.0000E-03 5.0000E-03 1.0000E-04
3.2000E+03 3.1000E+11 2.6000E-01 2.9000E-06 8.3700E+02 3.0500E+01 2.0000E-03 8.0000E+01 2.0000E-06
                                                       2.9400E+02 0.0000E+00 2.0000E-05
0.0000E+00 0.0000E+00 1.0000E+03 0.0000E+00 0.0000E+00 0.0000E+00
0.0000E+00 0.0000E+00 0.0000E+00 0.0000E+00 0.0000E+00 0.0000E+00 7.0000E+04
Rec 9.0
Rec 9.1.1
Rec 9.1.2
                                                        2.5000E-04 1.0000E+00 1.0000E+00 0.0000E+00 0.0000E+00 5.0000E-05 0.0000E+00 0.000E+00 0.000E+00 0.000E+00 0.000E+00 0.000E+000
Rec 9.5.1
Rec 10.0
Rec 10.1B
                                                       5.0000E-02 0.0000E+00 0.0000E+00 0.0000E+00 1.2500E-07
5.0000E-02 0.0000E+00 0.0000E+00 0.0000E+00 1.2500E-07
0.0000E+00 0.0000E+00-9.8100E+00
Rec 10.5.1B
Rec 10.5.2B
Rec 11
```

Input from optional user subroutines

Listing of input data records

ADVANCED DYNAMICS OF ROLLING ELEMENTS A Real Time Simulation of Rolling Bearing Performance [Version (ADORE 5.0)]

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**************************************		Mode = 1 Run Id = Cyl Rolle	
BEARING GEOMETRY			
NO OF ROLLERS 8 ROLLER DIA (m) 8.00000E-03 ROLLER LEN (m) 8.00000E-03 CEN LAND (m) 2.00000E-03 OUTER LEN1 (m) 1.00000E-02 OUTER LEN2 (m) 0.00000E+00	PITCH DIA (m) 4.30000E-02 CROWN RAD (m) 2.50000E-01 COR RAD I (m) 2.50000E-04 COR RAD II (m) 2.50000E-04 INNER LEN1 (m) 1.00000E-02 INNER LEN2 (m) 0.00000E+00	OUTER FIT (m) 0.00000E+00 INNER FIT (m) 2.00000E-05 DIA PLAY (m) 4.00000E-05 OUTER CRN (m) 1.00000E+10 INNER CRN (m) 1.00000E+10	SHAFT OD (m) 3.00000E-02 SHAFT ID (m) 1.00000E-02 BEARING OD (m) 5.50000E-02 HOUSING OD (m) 6.50000E-02 WIDTH I (m) 1.20000E-02 WIDTH II (m) 1.20000E-02
CAGE OD (m) 4.50000E-02 CAGE ID (m) 4.00000E-02 CAGE CONE (deg) 0.00000E+00	CAGE WIDTH (m) 1.00000E-02 SEG CUT (deg) 0.00000E+00 POCKET SHAPE 0		OUTER CLS (m) 1.00000E-04 INNER CLS (m) 1.00000E-03 NO OF CAGE SEGS 1
GUIDE GUIDE GUIDE LAND LAND TYPE DIA (m)	GUIDE LAND GUIDE LAND CLS WIDTH (m) (m)	GUIDE LAND POSITION (m)	

1	1	4.50000E-02	1.00000E-04	1.00000E-03	5.00000E-03
2	1	4.50000E-02	1.00000E-04	1.00000E-03	5.00000E-03

MATERIAL PROPERTIES ____

		CAGE	SHAFT	HOUSING
NT RACE	RACE			
03 7.75000E+03	7.75000E+03	7.75000E+03	7.75000E+03	7.75000E+03
11 2.00000E+11	2.00000E+11	2.00000E+11	2.00000E+11	2.00000E+11
01 2.50000E-01	2.50000E-01	2.50000E-01	2.50000E-01	2.50000E-01
06 1.17000E-05	1.17000E-05	1.80000E-05	1.17000E-05	1.17000E-05
01 4.30000E+01	4.30000E+01	4.30000E+01	4.30000E+01	4.30000E+01
02 4.70000E+02	4.70000E+02	4.70000E+02		
03 2.00000E-03	2.00000E-03	2.00000E-03		
01 6.10000E+01	6.10000E+01	2.00000E+01		
06 5.00000E-06	5.00000E-06	5.00000E-04		
	NT RACE 03 7.75000E+03 11 2.00000E+01 01 2.50000E-01 06 1.17000E-05 01 4.30000E+01 02 4.70000E+03 03 2.00000E-03 01 6.10000E+01	03 7.75000E+03 7.75000E+03 11 2.00000E+11 2.0000E+11 01 2.50000E-01 2.50000E-01 06 1.17000E-05 1.17000E-05 01 4.30000E+01 4.30000E+01 02 4.70000E+02 4.70000E+02 03 2.00000E-03 2.00000E-03 01 6.10000E+01 6.10000E+01	NT RACE RACE 03 7.75000E+03 7.75000E+03 7.75000E+11 11 2.00000E+11 2.00000E+11 2.00000E+11 10 2.50000E-01 2.50000E-01 2.50000E-01 06 1.17000E-05 1.17000E-05 1.80000E+01 01 4.3000E+01 4.30000E+01 4.30000E+01 02 4.70000E+02 4.70000E+02 3.0000E+02 03 2.00000E+03 2.00000E+03 2.00000E+03 01 6.10000E+01 6.10000E+01 2.00000E+01	NT RACE RACE 03 7.75000E+03 7.75000E+03 7.75000E+03 11 2.00000E+01 2.00000E+11 2.00000E+11 2.00000E+01 12 2.50000E-01 2.50000E-01 2.50000E-01 2.50000E-01 11 2.50000E-01 2.50000E-01 2.50000E-01 2.50000E-01 11 2.50000E+01 4.3000E+01 4.30000E+01 4.30000E+01 11 4.30000E+01 4.30000E+01 4.30000E+01 4.30000E+01 12 4.70000E+02 4.70000E+02 4.70000E+02 4.70000E+02 12 2.00000E-03 2.00000E-03 2.00000E-03 1.0000E+01 12 6.10000E+01 2.00000E+01 2.00000E+01 1.1000E+01

INERTIAL PARAMETERS

	MASS				MAS	S TO GEO CENT	'ER	
	(kg)		(kg*m**2)		(m)			
		X-COMP	Y-COMP	Z-COMP	X-COMP	Y-COMP	Z-COMP	
F	E 1.28108E-03	1.02486E-08	1.19567E-08	1.19567E-08	0.00000E+00	0.00000E+00	0.00000E+00	
CAG	E 1.58251E-02	7.17073E-06	3.71724E-06	3.71724E-06	0.00000E+00	0.00000E+00	0.00000E+00	
OUTER RAC	E 3.08208E-02	2.16826E-05	1.12111E-05	1.12111E-05	0.00000E+00	0.00000E+00	0.00000E+00	
INNER RAC	E 2.36364E-02	6.27429E-06	3.42078E-06	3.42078E-06	0.00000E+00	0.00000E+00	0.00000E+00	

.....PRINCIPAL TO GEO FRAME..... KINCEPAL TO GEO FRAME. (deg) X-COMP Y-COMP Z-COMP RE 0.00000E+00 0.00000E+00 0.00000E+00 CAGE 0.00000E+00 0.00000E+00 0.00000E+00 OUTER RACE 0.00000E+00 0.00000E+00 0.00000E+00 INNER RACE 0.00000E+00 0.00000E+00 0.00000E+00

LUBRICATION PARAMETERS _____

HYPOTHETICA MODELS		TRAC COEFF AT ZERO SLIP	MAXIMUM TRAC COEFF	TRAC COEFF AT INF SLIP	SLIP AT MAX TRACTION (m/s)	COEFFICIENT A	COEFFICIENT B (s/m)	COEFFICIENT C (s/m)	COEFFICIENT D
RE/RACE1 RE/RACE2 RE/CAGE RACE/CAGE	0.00000E+00 0.00000E+00 1.25000E-07 1.25000E-07	0.00000E+00 0.00000E+00				-8.00000E-02 -8.00000E-02 5.00000E-02 5.00000E-02	9.57239E-01 0.00000E+00	8.58912E+00 8.58912E+00 0.00000E+00 0.00000E+00	

FATIGUE PARAMETERS

INITIAL OPERATING CONDITIONS

LINE CO FATIGUE CONS (N/m**(50/27))	LOAD EXP	POINT C FATIGUE CONS (N/m**1.80)	CONTACT LOAD EXP	WEIBULL DISPERSION EXPONENT	BEARING WEIBULL SLOPE: LIFE MODIFICATION CODE:	
OUTER RACE 1.66550E+08 INNER RACE 1.66550E+08						

	ASPE	RITY INTERACT	'IONS	LIMIT SHEAR	RESIDUAL	MATERIALS	CONTAM-	PROCESSING
	COMPOSITE	COMPOSITE	TRACTION	STRESS	STRESS	FACTOR	INATION	FACTOR
	RMS HEIGHT	RMS SLOPE	COEFF				FACTOR	
	(m)	(rad)		(Pa)	(Pa)			
OUTER RACE	1.00000E-07	4.11320E-02	1.00000E-01	0.00000E+00	0.00000E+00	1.19700E+00	1.00000E+00	7.70000E-02
INNER RACE	1.00000E-07	4.11320E-02	1.00000E-01	0.00000E+00	0.00000E+00	1.19700E+00	1.00000E+00	7.70000E-02

Cyl Roller Bearing Geo Mod

					OUTE	ER RA	ACE	INNI	ER R <i>i</i>	ACE
ROOM TEMPERATURE	(K) 2	.94000E+02	ANGULAR VELOCITY	(rpm)	0.000	000E-	+00	7.000)00E-	+04
HOUSING TEMPERATURE		.94000E+02	TEMPERATURE	(K)	2.940			2.940		
SHAFT TEMPERATURE ROLLING ELEMENT TEMPERATURE		.94000E+02 .94000E+02	MISALIGNMENT-Y MISALIGNMENT-Z	(rad) (rad)	0.000			0.000		
CAGE TEMPERATURE	. ,	.94000E+02	MISALIGNMENI-Z	(Iau)	0.000	1005-	+00	0.000	1005-	FUU
QUASI-STATIC CONSTRAINTS		1011	TRANSLATIONAL CONSTR	AINTS	1	1	1	1	1	1
CONSTRAINING LOAD FRACTION	5	.00000E-02	ROTATIONAL CONSTRAIN	TS	1	1	1	1	1	1
BEARING COOLANT TYPE:	1	No Coolant								
NODE AT BASE TEMPERATURE:	Hous	sing/Outer								
VARY GEOMETRY WITH TEMPERATURE:		Yes								

	X-COMP	Y-COMP	Z-COMP
APPLIED LOAD VECTOR (N) RELATIVE DISPLACEMENT VECTOR (m)	0.00000E+00 0.00000E+00	0.00000E+00 0.00000E+00	1.00000E+03 0.00000E+00
APPLIED MOMENT VECTOR (N.m) GRAVITY VECTOR (m/s**2)	0.00000E+00	0.00000E+00	0.00000E+00
CAGE GEOM CEN POSITION (m) CAGE ANGULAR POSITION (deg)	0.00000E+00 0.00000E+00 0.00000E+00	0.00000E+00 0.00000E+00 0.00000E+00	5.00000E-05
CAGE ANGULAR POSITION (deg) CAGE WHIRL TO ANG VEL RATIO CAGE ANG VEL TO EPICYCLIC VEL RATIO	1.00000E+00 1.00000E+00	0.00000±+00	0.00000±+00

SCALE FACTORS AND OUTPUT CONTROLS

	LENGTH LOAD TIME	ALE F7 (m) (N) (S)	ACTORS 4.00000E-03 1.00000E+03 7.15843E-05	MINIMUM MAXIMUM INITTAI ERROR I	ZE INFO 1.00000E-04 5.00000E-01 5.00000E-02 1.00000E-04	DA AU	OF STEPS TA CONTROL TO PLOTS T METHOD	4000 1 1 0 5	500 9 0	0 0
step no	tau	+00	Time (s) 0.000F+00	Outer Race Rot (rev)	Race Rot (rev)	(ADORE 5.0)	ring Geo Mc	od		

 no
 (s)
 (rev)
 (rev)

 0
 0.000E+00
 0.000E+00
 0.000E+00
 Cyl Roller Bearing Geo Mod

1. Rolling Element Parameters

Re no	Position	(de	eg)	Contact	(N)	(1	Pa)	(n	n)	(r	n)
	(deg)	Outer Race	Inner Race								
1	0.000E+00	0.000E+00	0.000E+00	7.693E+02	5.240E+02	1.354E+09	1.414E+09	1.963E-03	1.777E-03	9.215E-05	6.641E-05
2	4.500E+01	0.000E+00	0.000E+00	5.819E+02	3.366E+02	1.219E+09	1.191E+09	1.824E-03	1.595E-03	8.329E-05	5.638E-05
3	9.000E+01	0.000E+00	0.000E+00	2.453E+02	0.000E+00	8.708E+08	0.000E+00	1.485E-03	0.000E+00	6.036E-05	0.000E+00
4	1.350E+02	0.000E+00	0.000E+00	2.453E+02	0.000E+00	8.708E+08	0.000E+00	1.485E-03	0.000E+00	6.036E-05	0.000E+00
5	1.800E+02	0.000E+00	0.000E+00	2.453E+02	0.000E+00	8.708E+08	0.000E+00	1.485E-03	0.000E+00	6.036E-05	0.000E+00
6	2.250E+02	0.000E+00	0.000E+00	2.453E+02	0.000E+00	8.708E+08	0.000E+00	1.485E-03	0.000E+00	6.036E-05	0.000E+00
7	2.700E+02	0.000E+00	0.000E+00	2.453E+02	0.000E+00	8.708E+08	0.000E+00	1.485E-03	0.000E+00	6.036E-05	0.000E+00
8	3.150E+02	0.000E+00	0.000E+00	5.819E+02	3.366E+02	1.219E+09	1.191E+09	1.824E-03	1.595E-03	8.329E-05	5.638E-05
RE	Orbital	Ano	ular Veloc	ity	RE Ang H	Position	Spin	/Roll	Contact	Loss	Time Ave

RE	Orbital	Ang	ular Veloci	ty	RE Ang P	osition	Spin	/Roll	Contact	Loss	Time Ave
	Velocity	Amplitude	Theta	Phi	Theta	Phi				(W)	Wear Rate
	(rpm)	(rpm)	(deg)	(deg)	(deg)	(deg)	Outer Race	Inner Race	Outer Race	Inner Race	(m**3/s)
1	2 849E+04	1.817E+05	1.800E+02	0.000E+00	0.000E+00	0 000 -	0 00000+00	0 00000+00	3.315E-01	2 3348-01	2 8568-15
-	2.849E+04		1.800E+02		0.000E+00				1.616E-01		
3	2.849E+04	1.817E+05	1.800E+02		0.000E+00				1.452E-02		
4	2.849E+04	1.817E+05	1.800E+02	0.000E+00	0.000E+00	0.000E+00	0.000E+00	-1.225E-16	1.452E-02	0.000E+00	1.300E-16
5	2.849E+04	1.817E+05	1.800E+02	0.000E+00	0.000E+00	0.000E+00	0.000E+00	-1.225E-16	1.452E-02	0.000E+00	1.300E-16
6	2.849E+04	1.817E+05	1.800E+02	0.000E+00	0.000E+00	0.000E+00	0.000E+00	-1.225E-16	1.452E-02	0.000E+00	1.300E-16
7	2.849E+04	1.817E+05	1.800E+02	0.000E+00	0.000E+00	0.000E+00	0.000E+00	-1.225E-16	1.452E-02	0.000E+00	1.300E-16
8	2.849E+04	1.817E+05	1.800E+02	0.000E+00	0.000E+00	0.000E+00	0.000E+00	0.000E+00	1.616E-01	6.976E-02	1.390E-15

RESlip Velocity	Trac Coeff	Iso Lub Film	Thermal Red Fac	Drag	Chrn MomNet Loss
no (m/s)		(m)		(N)	(N.m) (W)
Outer Race Inner Race		(Drag+Chur)			

1	8.312E-02	9.075E-02	7.979E-02	8.315E-02
2	6.742E-02	6.412E-02	7.133E-02	6.926E-02
3	3.388E-02	0.000E+00	4.444E-02	0.000E+00
4	3.388E-02	0.000E+00	4.444E-02	0.000E+00
5	3.388E-02	0.000E+00	4.444E-02	0.000E+00
6	3.388E-02	0.000E+00	4.444E-02	0.000E+00
7	3.388E-02	0.000E+00	4.444E-02	0.000E+00
8	6.742E-02	6.412E-02	7.133E-02	6.926E-02

RE	Rel Axial	.Contact De	eflection	Race Fl	lexing	Contact 1	Cemp Rise	Contac	t Temp	Bulk Temp	Convec HTC
no	Pos	(r	n)	(r	n)	(1	ζ)	(F	ζ)	(K)	
	(m)	Outer Race	Inner Race	Outer Race	Inner Race	Outer Race	Inner Race	Outer Race	Inner Race		(W/m**2/K)
1	0.000E+00	5.706E-06	4.313E-06	0.000E+00	0.000E+00	1.498E-02	1.253E-02	2.940E+02	2.940E+02	2.940E+02	0.000E+00
2	0.000E+00	4.656E-06	3.090E-06	0.000E+00	0.000E+00	7.766E-03	4.166E-03	2.940E+02	2.940E+02	2.940E+02	0.000E+00
3	0.000E+00	2.413E-06	-1.534E-07	0.000E+00	0.000E+00	8.495E-04	0.000E+00	2.940E+02	2.940E+02	2.940E+02	0.000E+00
4	0.000E+00	2.413E-06	-5.638E-06	0.000E+00	0.000E+00	8.495E-04	0.000E+00	2.940E+02	2.940E+02	2.940E+02	0.000E+00
5	0.000E+00	2.413E-06	-7.910E-06	0.000E+00	0.000E+00	8.495E-04	0.000E+00	2.940E+02	2.940E+02	2.940E+02	0.000E+00
6	0.000E+00	2.413E-06	-5.638E-06	0.000E+00	0.000E+00	8.495E-04	0.000E+00	2.940E+02	2.940E+02	2.940E+02	0.000E+00
7	0.000E+00	2.413E-06	-1.534E-07	0.000E+00	0.000E+00	8.495E-04	0.000E+00	2.940E+02	2.940E+02	2.940E+02	0.000E+00
8	0.000E+00	4.656E-06	3.090E-06	0.000E+00	0.000E+00	7.766E-03	4.166E-03	2.940E+02	2.940E+02	2.940E+02	0.000E+00

step	tau	Time	Outer Race Rot	Inner Race Rot	(ADORE 5.0)
no		(s)	(rev)	(rev)	
0	0.000E+00	0.000E+00	0.000E+00	0.000E+00	Cyl Roller Bearing Geo Mod
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1a. Load Distribution Along Roller no. 1

		Oute	r Race Cont	act			Inne	r Race Cont	act	
	Axial Pos	Geo Int	Half Width	Nor Load	Trac Load	Axial Pos	Geo Int	Half Width	Nor Load	Trac Load
	(m)	(m)	(m)	(N/m)	(N/m)	(m)	(m)	(m)	(N/m)	(N/m)
1	-1.895E-03	5.258E-07	2.891E-05	7.206E+01	5.749E+00	1.715E-03	4.307E-07	2.145E-05	1.443E+04	-1.200E+03
2	-1.639E-03	2.333E-06	6.619E-05	3.774E+02	2.350E+01	1.483E-03	1.912E-06	4.910E-05	7.560E+04	-4.822E+03
3	-1.305E-03	4.298E-06	9.296E-05	7.440E+02	2.375E+01	1.181E-03	3.521E-06	6.895E-05	1.490E+05	-4.005E+03
4	-1.050E-03	5.503E-06	1.067E-04	9.790E+02	5.134E+00	9.500E-04	4.313E-06	7.718E-05	1.867E+05	0.000E+00
5	-8.451E-04	5.706E-06	1.088E-04	1.019E+03	0.000E+00	7.650E-04	4.313E-06	7.718E-05	1.867E+05	0.000E+00
6	-3.337E-04	5.706E-06	1.088E-04	1.019E+03	0.000E+00	3.020E-04	4.313E-06	7.718E-05	1.867E+05	0.000E+00
7	3.337E-04	5.706E-06	1.088E-04	1.019E+03	0.000E+00	-3.020E-04	4.313E-06	7.718E-05	1.867E+05	0.000E+00
8	8.451E-04	5.706E-06	1.088E-04	1.019E+03	0.000E+00	-7.650E-04	4.313E-06	7.718E-05	1.867E+05	0.000E+00
9	1.050E-03	5.503E-06	1.067E-04	9.790E+02	5.134E+00	-9.500E-04	4.313E-06	7.718E-05	1.867E+05	0.000E+00
10	1.305E-03	4.298E-06	9.296E-05	7.440E+02	2.375E+01	-1.181E-03	3.521E-06	6.895E-05	1.490E+05	-4.005E+03
11	1.639E-03	2.333E-06	6.619E-05	3.774E+02	2.350E+01	-1.483E-03	1.912E-06	4.910E-05	7.560E+04	-4.822E+03
12	1.895E-03	5.258E-07	2.891E-05	7.206E+01	5.749E+00	-1.715E-03	4.307E-07	2.145E-05	1.443E+04	-1.200E+03

step	tau	Time	Outer Race Rot	Inner Race Rot	(ADORE 5.0)
no		(s)	(rev)	(rev)	
0	0.000E+00	0.000E+00	0.000E+00	0.000E+00	Cyl Roller Bearing Geo Mod
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2. Race and Cage Parameters

(m) .778E-05 .314E-05 .243E-05 .078E-04 .000E-35 .314E-05 .243B-05 .778E-05 .778E-05	(N) 0.000E+00 0.000E+00 0.000E+00 0.000E+00 1.516E+01 0.000E+00 0.000E+00 0.000E+00	0.000E+00 0.000E+00 0.000E+00 0.000E+00 0.000E+00 0.000E+00	(deg) 0.000E+00 0.000E+00 0.000E+00 0.000E+00 0.000E+00 0.000E+00 0.000E+00	Pos X (m) -6.405E-20 -3.973E-20 -1.031E-19 0.000E+00 -7.604E-21 -3.973E-20 2.682E-19	(m) 2.157E-04 -2.157E-04 2.293E-04 -2.293E-04 2.624E-04 -2.624E-04 2.978E-04	0.000E+00 0.000E+00 0.000E+00 0.000E+00 0.000E+00 6.673E+01 0.000E+00	0.000E+00 0.000E+00 0.000E+00 3.402E-10 0.000E+00
778E-05 .314E-05 .243E-05 .078E-04 .000E-35 .314E-05 .243E-05 .778E-05	0.000E+00 0.000E+00 0.000E+00 1.516E+01 0.000E+00 0.000E+00 0.000E+00	0.000E+00 0.000E+00 0.000E+00 0.000E+00 0.000E+00 0.000E+00 0.000E+00	0.000E+00 0.000E+00 0.000E+00 0.000E+00 0.000E+00 0.000E+00 0.000E+00	-6.405E-20 -3.973E-20 -1.031E-19 0.000E+00 -7.604E-21 -3.973E-20	-2.157E-04 2.293E-04 -2.293E-04 2.624E-04 -2.624E-04 2.978E-04	0.000E+00 0.000E+00 0.000E+00 0.000E+00 6.673E+01 0.000E+00	0.000E+00 0.000E+00 0.000E+00 0.000E+00 3.402E-10 0.000E+00
.314E-05 .243E-05 .078E-04 .000E-35 .314E-05 .243E-05 .778E-05	0.000E+00 0.000E+00 1.516E+01 0.000E+00 0.000E+00 0.000E+00 0.000E+00	0.000E+00 0.000E+00 0.000E+00 0.000E+00 0.000E+00 0.000E+00	0.000E+00 0.000E+00 0.000E+00 0.000E+00 0.000E+00 0.000E+00	-3.973E-20 -1.031E-19 0.000E+00 -7.604E-21 -3.973E-20	2.293E-04 -2.293E-04 2.624E-04 -2.624E-04 2.978E-04	0.000E+00 0.000E+00 0.000E+00 6.673E+01 0.000E+00	0.000E+00 0.000E+00 0.000E+00 3.402E-10 0.000E+00
2.243E-05 .078E-04 .000E-35 .314E-05 .243E-05 .778E-05	0.000E+00 0.000E+00 1.516E+01 0.000E+00 0.000E+00 0.000E+00	0.000E+00 0.000E+00 0.000E+00 0.000E+00 0.000E+00 0.000E+00	0.000E+00 0.000E+00 0.000E+00 0.000E+00 0.000E+00 0.000E+00	-1.031E-19 0.000E+00 -7.604E-21 -3.973E-20	-2.293E-04 2.624E-04 -2.624E-04 2.978E-04	0.000E+00 0.000E+00 6.673E+01 0.000E+00	0.000E+00 0.000E+00 3.402E-10 0.000E+00
.078E-04 .000E-35 .314E-05 .243E-05 .778E-05	0.000E+00 1.516E+01 0.000E+00 0.000E+00 0.000E+00	0.000E+00 0.000E+00 0.000E+00 0.000E+00	0.000E+00 0.000E+00 0.000E+00 0.000E+00	0.000E+00 -7.604E-21 -3.973E-20	2.624E-04 -2.624E-04 2.978E-04	0.000E+00 6.673E+01 0.000E+00	0.000E+00 3.402E-10 0.000E+00
000E-35 .314E-05 .243E-05 .778E-05	1.516E+01 0.000E+00 0.000E+00 0.000E+00	0.000E+00 0.000E+00 0.000E+00	0.000E+00 0.000E+00 0.000E+00	-7.604E-21 -3.973E-20	-2.624E-04 2.978E-04	6.673E+01 0.000E+00	3.402E-10 0.000E+00
.314E-05 .243E-05 .778E-05	0.000E+00 0.000E+00 0.000E+00	0.000E+00 0.000E+00	0.000E+00 0.000E+00	-3.973E-20	2.978E-04	0.000E+00	0.000E+00
.243E-05 .778E-05	0.000E+00 0.000E+00	0.000E+00	0.000E+00				
.778E-05	0.000E+00			2.682E-19	-2 9788-04	0 000 - 00	
		0 000E+00			2.2708 04	0.0005+00	0.000E+00
.778E-05	0 000 - 00		0.000E+00	-6.405E-20	3.124E-04	0.000E+00	0.000E+00
	0.000E+00	0.000E+00	0.000E+00	-6.405E-20	-3.124E-04	0.000E+00	0.000E+00
.243E-05	0.000E+00	0.000E+00	0.000E+00	2.682E-19	2.978E-04	0.000E+00	0.000E+00
.314E-05	0.000E+00	0.000E+00	0.000E+00	-3.973E-20	-2.978E-04	0.000E+00	0.000E+00
.781E-06	0.000E+00	0.000E+00	0.000E+00	-1.783E-19	2.624E-04	0.000E+00	0.000E+00
.078E-04	0.000E+00	0.000E+00	0.000E+00	0.000E+00	-2.624E-04	0.000E+00	0.000E+00
.243E-05	0.000E+00	0.000E+00	0.000E+00	2.682E-19	2.293E-04	0.000E+00	0.000E+00
.314E-05	0.000E+00	0.000E+00	0.000E+00	-3.973E-20	-2.293E-04	0.000E+00	0.000E+00
R	ace/Cage In	nteraction.		Effective	Contact	Time Ave	
Geo Int	Force	Con Angle	Att Angle	Dia Play	Loss	Wear Rate	
(m)	(N)	(deg)	(deg)	(m)	(W)	(m**3/s)	
000E+00	2.052E-01	0.000E+00				3.519E-12	
000E+00	2.052E-01	0.000E+00	0.000E+00	1.000E-04	6.903E-01	3.519E-12	
	.314E-05 .781E-06 .078E-04 .243E-05 .314E-05 R Geo Int (m) 000E+00	.314E-05 0.000E+00 .781E-06 0.000E+00 .078E-04 0.000E+00 .243E-05 0.000E+00 .314E-05 0.000E+00 Race/Cage II Geo Int Force (m) (N) 000E+00 2.052E-01	.314E-05 0.000E+00 0.000E+00 .781E-06 0.000E+00 0.000E+00 .078E-04 0.000E+00 0.000E+00 .243E-05 0.000E+00 0.000E+00 .314E-05 0.000E+00 0.000E+00 .314E-05 0.000E+00 0.000E+00 Race/Cage Interaction. Geo Int Force Con Angle (m) (N) (deg) 000E+00 2.052E-01 0.000E+00	.314E-05 0.000E+00 0.000E+00 0.000E+00 .781E-06 0.000E+00 0.000E+00 0.000E+00 .078E-04 0.000E+00 0.000E+00 0.000E+00 .243E-05 0.000E+00 0.000E+00 0.000E+00 .314E-05 0.000E+00 0.000E+00 0.000E+00 .314E-05 0.000E+00 0.000E+00 0.000E+00	.314E-05 0.000E+00 0.000E+00 0.000E+00 -3.973E-20 .781E-06 0.000E+00 0.000E+00 0.000E+00 -1.783E-19 .078E-04 0.000E+00 0.000E+00 0.000E+00 0.000E+00 .243E-05 0.000E+00 0.000E+00 0.000E+00 2.682E-19 .314E-05 0.000E+00 0.000E+00 0.000E+00 -3.973E-20 Race/Cage Interaction Effective Geo Int Force Con Angle Att Angle Dia Play (m) (N) (deg) (m) 0.000E+00 1.000E-04	.314E-05 0.000E+00 0.000E+00 0.000E+00 -3.973E-20 -2.978E-04 .781E-06 0.000E+00 0.000E+00 0.000E+00 -1.783E-19 2.624E-04 .078E-04 0.000E+00 0.000E+00 0.000E+00 0.000E+00 -2.624E-04 .243E-05 0.000E+00 0.000E+00 0.000E+00 2.682E-19 2.293E-04 .314E-05 0.000E+00 0.000E+00 0.000E+00 -3.973E-20 -2.293E-04	.314E-05 0.000E+00 0.000E+00 -3.973E-20 -2.978E-04 0.000E+00 .781E-06 0.000E+00 0.000E+00 -1.783E-19 2.624E-04 0.000E+00 .078E-04 0.000E+00 0.000E+00 0.000E+00 -2.624E-04 0.000E+00 .078E-05 0.000E+00 0.000E+00 0.000E+00 2.624E-04 0.000E+00 .243E-05 0.000E+00 0.000E+00 0.000E+00 2.682E-19 2.293E-04 0.000E+00 .314E-05 0.000E+00 0.000E+00 -3.973E-20 -2.293E-04 0.000E+00 .314E-05 0.000E+00 0.000E+00 -3.973E-20 -2.293E-04 0.000E+00 .314E-05 0.000E+00 0.000E+00 -3.973E-20 -2.293E-04 0.000E+00

	Mass	Center Pos	ition	Orbital	Ang	ular Veloci	ty	Ang Pos	ition	Ноор	Time Ave
	Axial	Radial	Orbital		Amplitude	Theta	Phi	Theta		Stress	
	(m)	(m)	(deg)	(rpm)	(rpm)	(deg)	(deg)	(deg)	(deg)	(Pa)	(m**3/s)
					2.849E+04						
					0.000E+00						
IRace	0.000E+00	7.758E-06	0.000E+00	0.000E+00	7.000E+04	0.000E+00	0.000E+00	0.000E+00	0.000E+00	1.532E+08	6.540E-15

step	tau	Time	Outer Race Rot	Inner Race Rot	(ADORE 5.0)
no		(s)	(rev)	(rev)	
0	0.000E+00	0.000E+00	0.000E+00	0.000E+00	Cyl Roller Bearing Geo Mod

3. Applied Parameters

							Basic Fatigue Life	(hours)	1.369E+02		
	Forces i	n Inertial	Frame	Moments i	n Body-Fixe	ed Frame	Modified Fatique Life	(hours)	1.369E+02		
	Comp-x	Comp-y	Comp-z	Comp-x	Comp-y	Comp-z	Outer Race Fit	(m)	0.000E+00		
	(N)	(N)	(N)	(N.m)	(N.m)	(N.m)	Inner Race Fit	(m)	5.743E-06		
							Internal Clearance	(m)	1.774E-05		
Cage	0.000E+00	-7.374E-01	-1.557E+01	3.226E-01	1.847E-03	9.234E-05					
Int ORace	0.000E+00	-1.376E+01	1.000E+03	5.640E-01	-1.847E-03	-9.234E-05	Total Power Loss	(W)	6.921E+01		
Int IRace	0.000E+00	8.763E+00	-1.000E+03	-1.742E-01	3.427E-17	1.745E-18	Churning Loss Fraction	1	0.000E+00		
Ext ORace	0.000E+00	1.376E+01	-1.000E+03	-5.640E-01	1.847E-03	9.234E-05	Exit Fluid Temperature	e (K)	0.000E+00		
Ext IRace	0.000E+00	-8.763E+00	1.000E+03	1.742E-01	-3.427E-17	-1.745E-18	-				

	MC Acc i	n Inertial (m/s**2)	Frame	Ang Acc i	n Body-Fixe (rpm/s)	d Frame	Bulk Temp (K)	Hsng/Bulk Temp Hsng/Outer Temp		2.940E+02 2.940E+02
	Comp-x	Comp-y	Comp-z	Comp-x	Comp-y	Comp-z		Hsng/Inner Temp Shft/Bulk Temp	(K)	2.940E+02 2.940E+02
Cage	0.000E+00	-4.660E+01	-9.936E+02	1.799E+02	1.987E+00	9.937E-02	2.940E+02	_		
ORace IRace	0.000E+00 0.000E+00	0.000E+00 0.000E+00						Shft/Outer Temp Shft/Inner Temp		2.940E+02 2.940E+02

4. Time Step Summary

						Time Average	Parameters	3		
Step	Time	Outer Race	Inner Race	Fatigue	Power	RE Orbital	Cage Omega	Cage Whirl	Cage	Average RE
no	(s)	Rotation (rev)	Rotation (rev)	Life (hours)		Vel Ratio	Ratio	Ratio	Wear Rate (m**3/s)	Excursion (m)
0	0.000E+00	0.000E+00	0.000E+00	1.369E+02	6.921E+01	4.070E-01	4.070E-01	4.070E-01	3.473E-10	1.269E-06

step	tau	Time	Outer Race Rot	Inner Race Rot	(ADORE 5.0)
no	E (10E 01	(s)	(rev)	(rev)	
4000	7.618E+01	5.453E-03	0.000E+00	6.362E+00	Cyl Roller Bearing Geo Mod
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1. Rolling Element Parameters

Re no				Contact							
	(deg)	Outer Race	Inner Race								
				2.453E+02							
2	6.172E+02			2.453E+02							
3	6.621E+02	0.000E+00	0.000E+00	4.815E+02	2.362E+02	1.134E+09	1.035E+09	1.740E-03	1.474E-03	7.771E-05	4.928E-05
4	7.071E+02	0.000E+00	0.000E+00	7.575E+02	5.122E+02	1.346E+09	1.401E+09	1.955E-03	1.767E-03	9.164E-05	6.586E-05
5	7.522E+02	0.000E+00	0.000E+00	6.714E+02	4.262E+02	1.287E+09	1.306E+09	1.893E-03	1.688E-03	8.774E-05	6.155E-05
6	7.972E+02	0.000E+00	0.000E+00	3.231E+02	7.778E+01	9.713E+08	6.469E+08	1.580E-03	1.215E-03	6.701E-05	3.150E-05
7	8.422E+02	0.000E+00	0.000E+00	2.453E+02	0.000E+00	8.708E+08	0.000E+00	1.485E-03	0.000E+00	6.037E-05	0.000E+00
8	8.872E+02	0.000E+00	0.000E+00	2.453E+02	0.000E+00	8.709E+08	0.000E+00	1.485E-03	0.000E+00	6.037E-05	0.000E+00

RE		Ang Amplitude (rpm)		Phi	RE Ang Theta (deg)		-			(W) Inner Race	Time Ave Wear Rate (m**3/s)
1	2.849E+04	1.817E+05	1.800E+02	0.000E+00	0.000E+00	0.000E+00	0.000E+00	0.000E+00	1.331E-02	0.000E+00	2.311E-17
2	2.849E+04	1.817E+05	1.800E+02	0.000E+00	0.000E+00	0.000E+00	0.000E+00	0.000E+00	1.331E-02	0.000E+00	2.009E-17
3	2.849E+04	1.817E+05	1.800E+02	0.000E+00	0.000E+00	0.000E+00	0.000E+00	0.000E+00	8.355E-02	2.412E-02	1.966E-17
4	2.849E+04	1.817E+05	1.800E+02	0.000E+00	0.000E+00	0.000E+00	0.000E+00	0.000E+00	2.700E-01	1.913E-01	2.206E-17
5	2.849E+04	1.817E+05	1.800E+02	0.000E+00	0.000E+00	0.000E+00	0.000E+00	0.000E+00	1.996E-01	1.173E-01	2.551E-17
6	2.849E+04	1.817E+05	1.800E+02	0.000E+00	0.000E+00	0.000E+00	0.000E+00	0.000E+00	2.793E-02	6.026E-04	2.592E-17
7	2.849E+04	1.817E+05	1.800E+02	0.000E+00	0.000E+00	0.000E+00	0.000E+00	0.000E+00	1.331E-02	0.000E+00	2.537E-17
8	2.849E+04	1.817E+05	1.800E+02	0.000E+00	0.000E+00	0.000E+00	0.000E+00	0.000E+00	1.331E-02	0.000E+00	2.560E-17

RESlip Velocity	Trac Coeff	Iso Lub Film	Thermal Red Fac	Drag	Chrn MomNet Loss
no (m/s)		(m)		(N)	(N.m) (W)
Outer Race Inner Race		(Drag+Chur)			

1	3.200E-02	0.000E+00	4.250E-02	0.000E+00
2	3.200E-02	0.000E+00	4.249E-02	0.000E+00
3	5.357E-02	4.537E-02	6.187E-02	5.523E-02
4	7.469E-02	8.217E-02	7.552E-02	7.934E-02
5	6.854E-02	7.149E-02	7.201E-02	7.374E-02
6	3.964E-02	1.708E-02	5.008E-02	2.504E-02
7	3.202E-02	0.000E+00	4.251E-02	0.000E+00
8	3.201E-02	0.000E+00	4.251E-02	0.000E+00

RE	Rel Axial	.Contact De			Race Flexing		Contact Temp Rise		Contact Temp		Convec HTC
no	Pos	(1	(m)		(m)		(K)		ζ)	(K)	
	(m)	Outer Race	Inner Race	Outer Race	Inner Race	Outer Race	Inner Race	Outer Race	Inner Race		(W/m**2/K)
1	0.000E+00	2.413E-06	-6.877E-06	0.000E+00	0.000E+00	7.676E-04	1.262E-07	2.940E+02	2.940E+02	2.940E+02	4.178E+05
2	0.000E+00	2.413E-06	-1.956E-06	0.000E+00	0.000E+00	7.674E-04	4.509E-07	2.940E+02	2.940E+02	2.940E+02	4.178E+05
3	0.000E+00	4.052E-06	2.345E-06	0.000E+00	0.000E+00	4.129E-03	1.535E-03	2.940E+02	2.940E+02	2.940E+02	4.178E+05
4	0.000E+00	5.642E-06	4.242E-06	0.000E+00	0.000E+00	1.204E-02	1.018E-02	2.940E+02	2.939E+02	2.939E+02	4.179E+05
5	0.000E+00	5.167E-06	3.699E-06	0.000E+00	0.000E+00	9.149E-03	6.529E-03	2.940E+02	2.938E+02	2.936E+02	4.184E+05
б	0.000E+00	2.994E-06	9.531E-07	0.000E+00	0.000E+00	1.521E-03	5.643E-05	2.940E+02	2.938E+02	2.936E+02	4.184E+05
7	0.000E+00	2.413E-06	-4.404E-06	0.000E+00	0.000E+00	7.678E-04	9.446E-08	2.940E+02	2.939E+02	2.939E+02	4.179E+05
8	0.000E+00	2.413E-06	-7.890E-06	0.000E+00	0.000E+00	7.677E-04	3.206E-07	2.940E+02	2.940E+02	2.940E+02	4.178E+05

step	tau	Time	Outer Race Rot	Inner Race Rot	(ADORE 5.0)
no		(s)	(rev)	(rev)	
4000	7.618E+01	5.453E-03	0.000E+00	6.362E+00	Cyl Roller Bearing Geo Mod
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1a. Load Distribution Along Roller no. 1

		Oute	r Race Cont	act		Inner Race Contact				
	Axial Pos	Geo Int	Half Width	Nor Load	Trac Load	Axial Pos	Geo Int	Half Width	Nor Load	Trac Load
	(m)	(m)	(m)	(N/m)	(N/m)	(m)	(m)	(m)	(N/m)	(N/m)
1	-1.434E-03	3.011E-07	2.122E-05	3.879E+01	1.648E+00	9.664E-04	4.703E-09	1.745E-06	9.541E+01	-1.898E-01
2	-1.240E-03	1.336E-06	4.858E-05	2.031E+02	4.635E+00	8.360E-04	4.703E-09	1.745E-06	9.541E+01	-1.898E-01
3	-9.878E-04	2.413E-06	6.747E-05	3.918E+02	-1.203E+00	6.658E-04	4.703E-09	1.745E-06	9.541E+01	-1.898E-01
4	-7.943E-04	2.413E-06	6.747E-05	3.918E+02	-1.203E+00	5.353E-04	4.703E-09	1.745E-06	9.541E+01	-1.898E-01
5	-6.396E-04	2.413E-06	6.747E-05	3.918E+02	-1.203E+00	4.311E-04	4.703E-09	1.745E-06	9.541E+01	-1.898E-01
6	-2.525E-04	2.413E-06	6.747E-05	3.918E+02	-1.203E+00	1.702E-04	4.703E-09	1.745E-06	9.541E+01	-1.898E-01
7	2.525E-04	2.413E-06	6.747E-05	3.918E+02	-1.203E+00	-1.702E-04	4.703E-09	1.745E-06	9.541E+01	-1.898E-01
8	6.396E-04	2.413E-06	6.747E-05	3.918E+02	-1.203E+00	-4.311E-04	4.703E-09	1.745E-06	9.541E+01	-1.898E-01
9	7.943E-04	2.413E-06	6.747E-05	3.918E+02	-1.203E+00	-5.353E-04	4.703E-09	1.745E-06	9.541E+01	-1.898E-01
10	9.878E-04	2.413E-06	6.747E-05	3.918E+02	-1.203E+00	-6.658E-04	4.703E-09	1.745E-06	9.541E+01	-1.898E-01
11	1.240E-03	1.336E-06	4.858E-05	2.031E+02	4.635E+00	-8.360E-04	4.703E-09	1.745E-06	9.541E+01	-1.898E-01
12	1.434E-03	3.011E-07	2.122E-05	3.879E+01	1.648E+00	-9.664E-04	4.703E-09	1.745E-06	9.541E+01	-1.898E-01

step	tau	Time	Outer Race Rot	Inner Race Rot	(ADORE 5.0)
no		(s)	(rev)	(rev)	
4000	7.618E+01	5.453E-03	0.000E+00	6.362E+00	Cyl Roller Bearing Geo Mod
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2. Race and Cage Parameters

IONOC Geo C	o Int Contact Force		Con Ang PHT	Contact Pos X	Contact Pos Z		Time Ave Wear Rate	
0	(m) (N)	THETA (deg)	(deg)	(m)	(m)	(W)	(m**3/s)	
	95E-05 0.000E+00	0.000E+00	0.000E+00	1.580E-05	2.317E-04	0.000E+00	0.000E+00	
1 2 0 7.6	51E-05 0.000E+00	0.000E+00	0.000E+00	-1.605E-05	-2.317E-04	0.000E+00	0.000E+00	
	79E-05 0.000E+00			-1.237E-05			0.000E+00	
2 2 0 4.1	77E-05 0.000E+00	0 0.000E+00	0.000E+00	1.840E-06	-2.171E-04	0.000E+00	0.000E+00	
	54E-05 0.000E+00	0.000E+00	0.000E+00	-2.018E-05	2.307E-04	0.000E+00	0.000E+00	
	02E-05 0.000E+00			4.973E-05			1.731E-15	
4 1 0 9.0	51E-05 0.000E+00	0.000E+00	0.000E+00	-1.731E-05	2.638E-04	0.000E+00	0.000E+00	
4 2 0 2.5	0.000E+00	0.000E+00	0.000E+00	5.965E-05	-2.638E-04	0.000E+00	2.485E-14	
	50E-05 0.000E+00			-3.366E-06				
5 2 0 1.6	97E-05 0.000E+00	0.000E+00	0.000E+00	5.161E-05	-2.959E-04	0.000E+00	0.000E+00	
	96E-05 0.000E+00	0.000E+00	0.000E+00	1.302E-05	3.083E-04	0.000E+00	0.000E+00	
6 2 0 4.8	51E-05 0.000E+00	0 0.000E+00	0.000E+00	-4.076E-07	-3.083E-04	0.000E+00	0.000E+00	
7 1 0 3.6	22E-05 0.000E+00	0.000E+00	0.000E+00	4.237E-05	2.958E-04	0.000E+00	7.018E-15	
7 2 0 7.93	34E-05 0.000E+00	0 0.000E+00	0.000E+00	-1.238E-05	-2.958E-04	0.000E+00	0.000E+00	
8 1 0 2.3	46E-05 0.000E+00	0.000E+00	0.000E+00	6.466E-05	2.643E-04	0.000E+00	0.000E+00	
8 2 0 9.2	LOE-05 0.000E+00	0 0.000E+00	0.000E+00	-1.738E-05	-2.643E-04	0.000E+00	0.000E+00	
LD C	Race/Cage 1	Interaction.		Effective	Contact	Time Ave		
NO C Geo	o Int Force	Con Angle	Att Angle	Dia Play	Loss	Wear Rate		
	(m) (N)	(deg)	(deg)	(m)	(W)	(m**3/s)		
	7E-06 0.000E+00							
0 0 0 00	7E-06 0.000E+00	4.798E+01	0.000E+00	9.359E-05	0.000E+00	1.165E-13		
2 0 2.82								
	er Position	Orbital	Ang	lar Veloci	- 17	Ang Pog	ition	Hoop Ti

(m)	(m)	(deg)	(rpm)	(rpm)	(deg)	(deg)	(deg)	(deg)	(Pa)	(m**3/s)
Cage -5.457E-08 ORace 0.000E+00 IRace 0.000E+00	-1.687E+04	4.224E-16								

step	tau	Time	Outer Race Rot	Inner Race Rot	(ADORE 5.0)
no		(s)	(rev)	(rev)	
4000	7.618E+01	5.453E-03	0.000E+00	6.362E+00	Cyl Roller Bearing Geo Mod
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3. Applied Parameters

							Basic Fatique Life	(hours)	1.347E+02			
	Forces i	n Inertial	Frame	Moments	in Body-Fixe	d Frame	Modified Fatigue Life	(hours)	1.347E+02			
	Comp-x	Comp-y	Comp-z	Comp-x	Comp-y	Comp-z	Outer Race Fit	(m)	6.272E-09			
	(N)	(N)	(N)	(N.m)	(N.m)	(N.m)	Inner Race Fit	(m)	5.732E-06			
							Internal Clearance	(m)	1.779E-05			
Cage	0.000E+00	0.000E+00	0.000E+00	0.000E+00	0.000E+00	0.000E+00						
Int ORace	0.000E+00	1.198E+01	1.003E+03	-3.887E-05	4.327E-18	2.143E-17	Total Power Loss	(W)	9.677E-01			
Int IRace	0.000E+00	-1.159E+01	-1.003E+03	-1.503E-04	-5.919E-18	-1.720E-17	Churning Loss Fraction	1	0.000E+00			
Ext ORace	0.000E+00	-1.198E+01	-1.003E+03	3.887E-05	-4.327E-18	-2.143E-17	Exit Fluid Temperature	e (K)	2.939E+02			
Ext IRace	0.000E+00	1.159E+01	1.003E+03	1.503E-04	5.919E-18	1.720E-17	- <u>1</u>					

	MC Acc i	n Inertial (m/s**2)	Frame	Ang Acc i	in Body-Fixed (rpm/s)	d Frame	Bulk Temp (K)	Hsng/Bulk Temp Hsng/Outer Temp	2.940E+02 2.940E+02
	Comp-x	Comp-y	Comp-z	Comp-x	Comp-y	Comp-z		Hsng/Inner Temp Shft/Bulk Temp	2.940E+02 2.939E+02
Cage	0.000E+00	0.000E+00	-9.810E+00	0.000E+00	-6.448E+00	1.225E+00	2.939E+02		
ORace IRace	0.000E+00 0.000E+00				0.000E+00 0.000E+00			Shft/Outer Temp Shft/Inner Temp	2.939E+02 2.939E+02

4. Time Step Summary

Step	Time		Inner Race	Fatigue				Cage Whirl		
no	(s)	Rotation (rev)	Rotation (rev)	Life (hours)	Loss (W)	Vel Ratio	Ratio	Ratio	Wear Rate (m**3/s)	
4000	5.453E-03	0.000E+00	6.362E+00	2.784E+00	7.198E-02	8.345E-03	8.345E-03	8.770E-03	2.666E-13	2.472E-06
	Normal te	ermination:	Last Step N	umber =	4000	Final Time	e = 7.6180	E+01		

Statistics of this Run

Minimum Step Size	=	4.06716E-03
Maximum Step Size	=	4.37787E-02
Last Step Size	=	2.65720E-02
Max Truncation	=	9.93185E-05
Total Derivative Calls	=	43010