A One-Dimensional Atmospheric Boundary Layer Model: Intermittent Wind Shears and Thermal Stability at Night

Arnold Tunick

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A One-Dimensional Atmospheric Boundary Layer Model: Intermittent Wind Shears and Thermal Stability at Night

Arnold Tunick
Computational and Information Sciences Directorate
Abstract

A one-dimensional, time-dependent computer model of the atmospheric boundary layer was developed to simulate intermittent turbulence and the near-ground microclimate under nighttime stable conditions. In this study, the model produced several turbulent events (oscillations) through the nighttime period that varied in number, frequency, and strength along the axes of initial geostrophic wind speed. These results were found to be in close agreement with results from several previous observational and theoretical studies of this type. It is suggested, therefore, that the one-dimensional computer model is a useful mathematical representation of the nighttime case that includes intermittency.
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1. Introduction

Field experimenters have frequently observed turbulent "bursts" in the lower boundary layer, suggesting that they are likely the result of gravity-wave activity and other wind-shear or thermal instabilities (e.g., Schubert, 1977; Lu et al, 1983; Coulter, 1990; Nappo, 1991; Weber and Kurzeja, 1991; and Blumen et al, 1999). Such turbulent events have even been linked to particular mesoscale events and synoptic situations, like outflow from nearby thunderstorms, as reported in Zhou Ming-yu et al (1980) and Neff (1980). In contrast, atmospheric computer modelers (e.g., Blackadar, 1979; McNider and Pielke, 1981; Lin, 1990; ReVelle, 1993; and McNider et al, 1995) describe time-dependent oscillations at night as resulting from nonlinear interactions between the ground surface and the airflow aloft. From the modeler's point of view, several external parameters, in the right combination, can increase the chances for a model to produce intermittent turbulence during the nighttime period. These parameters are typically surface roughness, initial soil moisture or heat capacity, and geostrophic (upper level) wind speed. Since intermittent "bursts" of turbulence in the lower boundary layer cause wind gusts and fluctuations in temperature, much attention has been directed toward nighttime cases that include intermittency in modeling atmospheric pollution (Nappo and Bach, 1997; Nappo and Johansson, 1998).

Model results for the nighttime case that includes intermittency have been shown in previous works, e.g., Lin (1990) and ReVelle (1993), along with descriptions of the parameter space within which time-dependent oscillations occur. From these earlier discussions, however, it is not clear to what extent variations initial geostrophic wind speed, surface roughness, and soil moisture affect the onset and cycling of wind shear and thermal instabilities at the surface and aloft. In this report, therefore, the author presents an expanded and improved view of the nighttime intermittently stable solution within the continuum of several varying model parameters. The author provides incremental time series of potential temperature and wind speed as well as time-height series of the derived momentum and heat flux for the layers \(2 \leq z \leq 150 \text{ m} \).
2. The Atmospheric Boundary-Layer Model

The one-dimensional, time-dependent model used in this study is based on the previous works of Pielke and Mahrer (1975), McNider and Pielke (1981), and Avissar and Mahrer (1988). It is a first-order, local-turbulence closure computer model formulated to calculate the transfer of momentum, heat, and moisture at the surface and aloft. The model uses an implicit finite difference scheme to integrate the boundary layer and soil-diffusion equations and contains many detailed formulations for the surface-energy budget. The model's surface-layer turbulence scaling is as described by Zilitinkevich (1970) and Businger et al (1971). A formulation suggested by Smeda (1979) is used for the time-dependent calculation of the depth of the nighttime stable layer. Table 1 summarizes the model parameters for this study of the lower nighttime boundary layer.

Table 1. Nighttime boundary-layer model parameters.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Number of vertical levels</td>
<td>19</td>
</tr>
<tr>
<td></td>
<td>(2, 5, 15, 30, 80, 150, 208, 445, 690, 943, 1203, 1470, 1743, 2023, 2311, 2609, 2916, 3250, 3500 m)</td>
</tr>
<tr>
<td>Latitude, longitude</td>
<td>45.0 N, 0.0 E</td>
</tr>
<tr>
<td>Surface roughness</td>
<td>0.28 m</td>
</tr>
<tr>
<td>Canopy height</td>
<td>2.0 m</td>
</tr>
<tr>
<td>Surface emissivity</td>
<td>0.95</td>
</tr>
<tr>
<td>Soil water content</td>
<td>0.1 m³/m³</td>
</tr>
<tr>
<td>Average soil density</td>
<td>1400 kg/m³</td>
</tr>
<tr>
<td>Soil texture</td>
<td>28.0, 70.0, 2.0</td>
</tr>
<tr>
<td>(% sand, % clay, % organic)</td>
<td></td>
</tr>
<tr>
<td>Geostrophic wind speed</td>
<td>$u_g = 6.5, 8.0, 9.5$ m/s ; $v_g = 0.0$ m/s</td>
</tr>
<tr>
<td>Day of the year</td>
<td>91</td>
</tr>
<tr>
<td>Initial time (sunset)</td>
<td>~18 local time</td>
</tr>
<tr>
<td>Initial potential temperature in the surface layer</td>
<td>~284.0 K</td>
</tr>
<tr>
<td>Time step</td>
<td>3 s</td>
</tr>
</tbody>
</table>
The model equations for the time-dependent calculation of the winds \((u\text{-} and v\text{-components})\), potential temperature \((\theta)\), and specific humidity \((q)\) over flat earth can be expressed as

\[
\frac{\partial u}{\partial t} = f(v - u) + \frac{\partial}{\partial z} \left( K_m \frac{\partial u}{\partial z} \right)
\]

\(1\)

\[
\frac{\partial v}{\partial t} = f(u - u_g) + \frac{\partial}{\partial z} \left( K_m \frac{\partial v}{\partial z} \right)
\]

\(2\)

\[
\frac{\partial \theta}{\partial t} = \frac{\partial}{\partial z} \left( K_h \frac{\partial \theta}{\partial z} \right), \text{ and}
\]

\(3\)

\[
\frac{\partial q}{\partial t} = \frac{\partial}{\partial z} \left( K_h \frac{\partial q}{\partial z} \right)
\]

\(4\)

where \(f\) denotes the Coriolis parameter, subscript \(g\) refers to the geostrophic wind, \(K_m\) denotes the turbulence transfer coefficient for momentum, and \(K_h = K_n\) denotes the transfer coefficients for heat and moisture. In the surface layer, \(K_m\) and \(K_h\) are calculated as \(K_m = \frac{k u_* z}{\phi_m}\) and \(K_h = \frac{k u_* z}{\phi_h}\), respectively, where \(k\) is Kármán's constant, \(z\) is height above ground level (agl) (in meters), \(u_*\) is the friction velocity (in units of m/s), and \(\phi_m\) and \(\phi_h\) are nondimensional lapse-rate functions that account for surface-layer stabilities other than neutral. A list of symbols is provided in the appendix.

During the nighttime, when the surface layer is generally stable, that is, \(\theta_* > 0\), where \(\theta_* = \frac{k z \partial \theta}{\phi_h \partial z}\) is the potential temperature scaling constant, the model derives the diffusion coefficients above the surface layer as suggested by Blackadar (1979)

\[
K_m(z) = K_h(z) = \begin{cases} 
sl^2 \left(1 - 18Ri\right)^{0.5}, & Ri < 0 \\
sl^2 \left( Ri_{crit} - Ri \right) / Ri_{crit}, & 0 < Ri \leq Ri_{crit} \\
0, & Ri > Ri_{crit}
\end{cases}
\]

\(5\)

where \(s\) is the local wind shear. The parameter, \(Ri\), called the Richardson number, is the ratio of thermal to mechanical (wind shear) production of turbulent energy, so that \(Ri = \frac{g \partial \theta}{\theta \partial z} \left/ \left( \left( \partial u/\partial z \right)^2 + \left( \partial v/\partial z \right)^2 \right) \right.\). \(Ri_{crit}\) is the limiting value of the Richardson number, where it is often assumed that \(Ri_{crit} = 0.25\). Alternatively, \(Ri_{crit} = 0.115 \Delta z^{0.175}\) (McNider and Pielke, 1981; Avisser and Mahler, 1988), where \(\Delta z\) is the model grid spacing in centimeters. This expression results in having values approaching 0.25 for finer
grid spacing and values closer to 0.65 where the grid is more coarse (i.e., 150 to 250 m). The length, $l$ (in meters), $l = k_z \left(1 + \frac{k_z}{0.0063 u_f}ight)^{-1}$ is generally thought of as the width of turbulence and is characterized by this formulation reported in Blackadar (1979), for $z$ above the surface layer. As mentioned earlier, the formulation suggested by Smeda (1979) for the depth of the nighttime planetary boundary layer, $z_u$, is calculated as

$$\frac{dz_u}{dt} = 0.06 \frac{u^2}{z_f} \left[1 - \left(\frac{3.3z_f}{u_f}\right)^3\right].$$

(6)

Some previous results obtained with the use of this expression for the depth of the nighttime planetary boundary layer were in good agreement in comparison to the observed data (Tunick, 2000).

The surface-energy budget as described by Pielke (1984) and Avissar and Mahrer (1988) can be written as

$$(1 - A)R_{s\downarrow} + R_{L\downarrow} - R_{L\uparrow} - \rho c_p u_\theta u_\theta - \rho L_v u_q + Q_s = F,$$

where $A$ is surface reflectivity (albedo); $R_{s\downarrow}$, $R_{L\downarrow}$, and $R_{L\uparrow}$ are the incoming solar, incoming long-wave, and outgoing long-wave radiative fluxes, respectively; $u_\theta$, $\theta$, and $q_\theta$ are the surface-layer turbulence scaling parameters for wind speed, temperature, and moisture, in that order; $\rho$ is the air density; $c_p$ is the specific heat of air at constant pressure; $L_v$ is the heat of transformation for water vapor; $Q_s$ is the soil heat flux; and $F$ is the function applied in solving iteratively for the surface temperature. The formulation for downward long-wave radiation is based on the earlier works reported by Paltridge and Platt (1976), which can be expressed as

$$R_{L\downarrow} = -170.9 + 1.195 \sigma T_r^4 + 0.3 cld \varepsilon_c \sigma T_c^4,$$

(8)

where $\sigma = 5.6697 \times 10^{-8} \text{ W m}^{-2} \text{ deg}^{-4}$, $T_r$ is the reference level (~2 m) temperature in kelvins, $cld$ is the cloud amount, $\varepsilon_c$ is the emissivity of the cloud base, and $T_c$ is the temperature of the cloud base in kelvins. This expression has worked quite well in two previous studies (i.e., Rachele and Tunick, 1994; Tunick et al., 1994).

Integration of the partial differential equations (1) to (4) is achieved with a generalized form of the Crank-Nicholson implicit finite difference scheme (Paegle et al., 1976; also see Pielke, 1984, sect. 10.1.2, and Ahlberg et al., 1967). Boundary conditions applied at the top of the model are such that the variables retain their initial values.
3. Model Results

As reported in Businger (1973), McNider et al (1995), and Mahrt (1998), the following events frequently characterize the nighttime stable boundary layer:

(a) Strong surface radiative cooling and the formation of a stably stratified layer near the ground.
(b) Suppressed turbulence as the ground cools and the development of a laminar layer.
(c) Heat and momentum transfer of from higher layers is blocked and the Richardson number exceeds its critical value at some height above the ground.
(d) Surface wind speeds decrease (calm). The nocturnal low-level jet intensifies.
(e) Above the laminar layer, momentum continues to be transferred downward.
(f) Above the laminar layer, little heat is exchanged since the thermal gradient at this level is close to neutral.
(g) If there is very strong thermal stability at the surface, the airflow aloft may, in effect, become disconnected or decoupled from it.
(h) Winds above the laminar layer will continue to accelerate in the absence of surface friction.
(i) Temperatures at the surface will continue to decrease.
(j) Wind shears above the laminar layer will build up in the absence of offsetting heat flux.
(k) The Richardson number begins to decrease below its critical value. The laminar surface layer will be eroded from above by wind shears.
(l) Downbursts of turbulence cause wind gusts and oscillations in temperature (and moisture). Vertical mixing depletes strong wind shears.
(m) The series of events (a) through (l) repeats itself through the nighttime period. This is the intermittently stable nighttime case.
(n) If, however, winds and wind shears are initially strong through the lower nighttime boundary layer, a more turbulently mixed, weakly stratified layer is maintained.
(o) Windier and warmer conditions at the surface will prevail. This is the coupled nighttime boundary-layer solution.
Figure 1 shows the coupled, decoupled, and intermittently stable nighttime results for (a) potential temperature and (b) modeled wind speed in the surface layer at 5 m agl. The dashed, circled, and solid lines are for levels of stability corresponding to three different initial values of geostrophic wind speed, i.e., 6.5, 8.0, and 9.5 m/s, respectively. Where turbulence is maintained by strong wind shears (dashed line), temperatures and wind speeds in the surface layer remain high and highly coupled to the air aloft. Where turbulence is suppressed by strong thermal stability (solid line), the model produces lower surface temperatures* and lower wind speeds. The intermittently stable solution (circled line) clearly oscillates between the coupled (windier, warmer) and decoupled (calmer, cooler) states. Figure 1 of the

*Certainly, the temperature results in figure 1 are unrealistically low. The so-called “runaway” cooling (as expressed by Mahrt, 1998) is apparently a common defect in numerical models that calculate meteorological gradients near the ground at night with the use of Obukhov similarity functions (Monin and Obukhov, 1954). In this situation, not enough heat is transferred from aloft to offset steady radiative and surface losses.
The present study looks very similar to ReVelle’s (1993) figures 3 and 4, where, over a period of 16 hours, four oscillations in temperature and wind speed were shown to occur at approximately 4.0, 7.5, 10.5, and 13.0 h past sunset. In this example, three oscillations occurred (over a period of 12 hours) at approximately 3.75, 6.5, and 10.0 h past sunset, which is in close agreement with ReVelle’s results. By this example, the model is also found to be in close agreement with several other observational and theoretical results (reported in the literature) on nighttime downburst events. Table 2 gives a comparative summary of the current and previous results.

Figure 2 contains data from several consecutive model runs (i.e., fig. 2 contains fig. 1). The incremental time series of potential temperature (a) and wind speed (b) in the surface layer at 5 m agl show that several oscillations are generated through the nighttime period that vary greatly in number, frequency, and strength along the axes of initial geostrophic wind speed. Figure 2 shows that the onset of such events, in hours past sunset, also varies along this dimension. The numbers of oscillations that occur are shown to increase from 1 to 8 or more in the direction of increasing of geostrophic winds. At the same time, as the total numbers of oscillations increase, their intensity or strength tends to decrease. Figure 2 also indicates where the decoupled nighttime solution occurs (i.e., an extreme depression in temperature and calmer winds, as explained above). In contrast, the coupled nighttime boundary-layer solution is indicated where temperatures decrease less severely. An unexpected result for this case is that the model produces oscillations in two cycles. This result is interesting because it suggests that a layer with sufficiently strong wind speeds and wind shears can become intermittently turbulent at even higher windspeeds under the right set of conditions.

Table 2. Summary of previous observational and theoretical results on nighttime “bursting” events.

<table>
<thead>
<tr>
<th>Source</th>
<th>Type (O/T)</th>
<th>Surface roughness (m)</th>
<th>Geostrophic wind speed (m/s)</th>
<th>Average number of events per night</th>
</tr>
</thead>
<tbody>
<tr>
<td>Thorpe and Guymer (1977)</td>
<td>O</td>
<td>not indicated</td>
<td>&lt; 10.0</td>
<td>3 h⁻¹ per event</td>
</tr>
<tr>
<td>Schubert (1977)</td>
<td>O</td>
<td>1.5</td>
<td>not indicated</td>
<td>1–2 within ~5 h</td>
</tr>
<tr>
<td>Blackadar (1979)</td>
<td>T</td>
<td>1.0</td>
<td>8.0</td>
<td>5–6</td>
</tr>
<tr>
<td>Coulter (1990)</td>
<td>O</td>
<td>0.1–1.0</td>
<td>not indicated</td>
<td>4–5</td>
</tr>
<tr>
<td>Lin (1991)</td>
<td>T</td>
<td>1.0</td>
<td>8.0</td>
<td>2–3</td>
</tr>
<tr>
<td>Nappo (1991)</td>
<td>O</td>
<td>0.1–1.0</td>
<td>not indicated</td>
<td>13–18</td>
</tr>
<tr>
<td>Reveille (1993)</td>
<td>T</td>
<td>0.1–1.0</td>
<td>1.0–3.0</td>
<td>3–8</td>
</tr>
<tr>
<td>Present study</td>
<td>T</td>
<td>0.28 (0.1–1.0)</td>
<td>8.0 (3.0–11.0)</td>
<td>3 (1–8)</td>
</tr>
</tbody>
</table>

*aAdapted from Reveille (1993), table 2, p. 1177.

*bO—observations; T—theory.

*cNumbers inside the parentheses are implied from the model results shown in figures 2, 5, and 6.
Figure 2. Surface plot of potential temperature (K) at 5 m agl in surface layer (a) and wind speed (m/s) at 5 m agl in surface layer (b) as a function of time past sunset and value of initial geostrophic wind speed.

Figures 3 and 4 show times series of potential temperature data and wind speed data, respectively, at 15, 30, 80, and 150 m agl. Away from the surface \((z > 30 \text{ m})\), temperatures and wind speeds are shown to change very little through the nighttime period when geostrophic wind speeds are low and heat transfer is limited. In contrast, when initial geostrophic wind speeds are higher and turbulent transfers of heat and momentum are maintained, potential temperatures are shown to decrease steadily through the nighttime period. Figures 3 and 4 also show that oscillations are affected through the entire layer \((z \leq 150 \text{ m})\), although additional evidence regarding the onset of the instabilities would be desirable.

Figure 5 is similar to figure 2 except that it shows the model results as they are affected by changes in surface roughness, that is, \(z_0 = 0.01 \text{ m}\) (fig. 5(a) and 5(c)) and \(z_0 = 1.0 \text{ m}\) (fig. 5(b) and 5(d)). (In calculating the data in figure 2, \(z_0 = 0.28 \text{ m}\).) These results show that the surface layer tends toward warmer temperatures (approximately 8 to 10 K) and calmer wind speeds (approximately 2 to 3 m/s) as surface roughness increases from 0.01 to 1.0 m. This is likely due to increased surface stress (Munn, 1966). The results also show...
Figure 3. Surface plot of potential temperature (K) at (a) 15, (b) 30, (c) 80, and (d) 150 m agl in lower boundary layer as a function of time past sunset and value of initial geostrophic wind speed.
Figure 4. Surface plot of wind speed (m/s) at (a) 15, (b) 30, (c) 80, and (d) 150 m agl in lower boundary layer as a function of time past sunset and value of initial geostrophic wind speed.
that turbulence is generated about 1.0 to 2.0 hours earlier and at 1.0 to 2.0 m/s lower geostrophic wind speeds as surface roughness increases. In other words, oscillations are more likely to occur over more rough (aerodynamically turbulent) surfaces with lower geostrophic wind speeds. The distribution and frequency of the oscillations also varies with changes in the roughness parameter. The numbers presented in parentheses in table 2 reflect these additional results.

Figure 6 is also similar to figure 2 except that it shows the model results as they are affected by changes in initial soil moisture, that is, $m_s = 0.05 \text{ m}^3/\text{m}^3$ (fig. 6(a) and (c)) and $m_s = 0.20 \text{ m}^3/\text{m}^3$ (fig. 6(b) and (d)). (In calculating the data in figure 2, $m_s = 0.10 \text{ m}^3/\text{m}^3$.) These model results show that the surface layer tends toward warmer temperatures (approximately 2 to 3 K) as soil moisture increases. This is likely due to decreasing radiative losses and other surface-energy budget considerations (Munn, 1966). The results also show that the intensity of the oscillations increases for higher initial values of soil moisture, which is also an effect related to the heat capacity of the soil and surface cooling (see Lin, 1990).
**Figure 6.** Surface plot of potential temperature (K) at 5 m agl in the surface layer (a) and (b) and wind speed (m/s) at 5 m agl in surface layer (c) and (d) as they are affected by changes in initial soil moisture (i.e., $m_s = 0.05$ m$^3$/m$^3$ (a) and (c) and $m_s = 0.20$ m$^3$/m$^3$ (b) and (d)).

**Figure 7(a), (b), and (c)** shows the calculated momentum flux, $-\overline{u'w'} = K_m \sqrt{\left(\frac{\partial u}{\partial z}\right)^2 + \left(\frac{\partial v}{\partial z}\right)^2}$ in units of m$^2$/s$^2$, and heat flux, $-\overline{w'\theta'} = K_h \left(\frac{\partial \theta}{\partial z}\right)$ in figure 7(d), (e), and (f) in units of m s$^{-1}$ K, in the lower boundary layer for levels of stability corresponding to three different initial values of geostrophic wind speed, that is, 6.5, 8.0, and 9.5 m/s. In the very stable layer case (fig. 7(a) and 7(d)), momentum increases through the lower boundary layer as the nocturnal low-level jet forms aloft. The model results show that the momentum flux continues downward through the lower boundary layer, even as the surface layer becomes increasingly more stable (and eventually laminar). This may explain why, in figure 1, the surface-layer wind speeds are around 2.5 m/s, rather than calm, through the nighttime period. In contrast, the heat flux through the laminar layer decreases as surface-layer temperatures (not shown) approach a kind of radiative equilibrium with the ground (Mahrt, 1998). Above the laminar layer ($z \geq 30$ m), the heat flux is nearly absent.
In the intermittently stable case (fig. 7(b) and 7(e)), a series of sporadic breakdowns are shown as fluctuations of momentum and heat flux in the layer, $2 \leq z \leq 150$ m. There appear to be about 5 or 6 such events through the nighttime period. For this example, the surface roughness and initial geostrophic wind speed were 0.28 m and 8.0 m/s, respectively (same as fig. 1). Further analysis of these results would be desirable to provide additional information regarding the onset wind shear and thermal instabilities aloft.

In the weakly stable case (fig. (c) and (f)), both the heat and momentum flux remain strong through the nighttime period. The increased wind speeds (and wind shears) in this example do not permit the formation of a separate, highly stratified layer at the surface. Instead, the model derives a steady and much less severe decrease in temperatures (not shown) through the entire layer, that is, $2 \leq z \leq 150$ m. This is the coupled nighttime boundary-layer result.
4. Conclusion

In this study a computer atmospheric model is developed to simulate the lower nighttime stable-boundary layer. An overview is given for the development of wind shear and thermal stability in the lower boundary layer under weakly stable, highly stable, and intermittently stable conditions. Several graphs show incremental time series of the model data. They provide an improved and expanded view of the nighttime wind and temperature oscillations and of the parameter space within which such time-dependent oscillations occur. The model used in this study is shown to be a useful representation of the nighttime case that includes intermittent turbulence.

Acknowledgment

I would like to thank Ronald Meyers and Keith Deacon of the U.S. Army Research Laboratory for their comments on this study. I would also like to thank David Rosen of the U.S. Army Research Laboratory for reading through my report and for offering many helpful comments.
References


### Appendix. Symbols

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>$A$</td>
<td>surface reflectivity (albedo)</td>
</tr>
<tr>
<td>cld</td>
<td>cloud amount (in tenths)</td>
</tr>
<tr>
<td>$c_p$</td>
<td>specific heat of air at constant pressure</td>
</tr>
<tr>
<td>$f$</td>
<td>Coriolis parameter</td>
</tr>
<tr>
<td>$F$</td>
<td>function applied in solving for the surface temperature through the surface-energy budget</td>
</tr>
<tr>
<td>$g$</td>
<td>acceleration due to gravity</td>
</tr>
<tr>
<td>$k$</td>
<td>Kármán’s constant (~0.4)</td>
</tr>
<tr>
<td>$K_h$</td>
<td>eddy transfer coefficient for heat</td>
</tr>
<tr>
<td>$K_m$</td>
<td>eddy transfer coefficient for momentum</td>
</tr>
<tr>
<td>$K_q$</td>
<td>eddy transfer coefficient for moisture</td>
</tr>
<tr>
<td>$l$</td>
<td>mixing length</td>
</tr>
<tr>
<td>$L_v$</td>
<td>heat of transformation for water vapor</td>
</tr>
<tr>
<td>$m_s$</td>
<td>soil moisture or soil water content</td>
</tr>
<tr>
<td>$q$</td>
<td>specific humidity</td>
</tr>
<tr>
<td>$q_c$</td>
<td>surface-layer turbulence scaling parameter for moisture</td>
</tr>
<tr>
<td>$Q_s$</td>
<td>soil heat flux</td>
</tr>
<tr>
<td>$R_i$</td>
<td>ratio of thermal to mechanical (wind shear) production turbulent energy called the Richardson number</td>
</tr>
<tr>
<td>$R_{i \text{crit}}$</td>
<td>limiting value of the Richardson number</td>
</tr>
<tr>
<td>$R_s$</td>
<td>incoming solar radiative flux</td>
</tr>
<tr>
<td>$R_{L \uparrow}$</td>
<td>incoming long-wave radiative flux</td>
</tr>
<tr>
<td>$R_{L \downarrow}$</td>
<td>outgoing long-wave radiative flux</td>
</tr>
<tr>
<td>$s$</td>
<td>local wind shear,</td>
</tr>
<tr>
<td>$t$</td>
<td>time in hours past sunset</td>
</tr>
<tr>
<td>$T_c$</td>
<td>temperature of the cloud base (in kelvins)</td>
</tr>
<tr>
<td>$T_r$</td>
<td>reference level (~2 m) temperature (in kelvins)</td>
</tr>
<tr>
<td>$u$</td>
<td>east-west component of horizontal wind speed</td>
</tr>
<tr>
<td>$u_g$</td>
<td>east-west component of geostrophic wind speed</td>
</tr>
<tr>
<td>$u_s$</td>
<td>surface friction velocity</td>
</tr>
<tr>
<td>$u'$</td>
<td>eddy fluctuating component of the horizontal wind speed</td>
</tr>
<tr>
<td>$v$</td>
<td>north-south component of horizontal wind speed</td>
</tr>
<tr>
<td>$v_g$</td>
<td>north-south component of geostrophic wind speed</td>
</tr>
<tr>
<td>$w'$</td>
<td>eddy fluctuating component of the vertical wind speed</td>
</tr>
<tr>
<td>$\varepsilon_c$</td>
<td>emissivity of the cloud base</td>
</tr>
<tr>
<td>$\phi_h$</td>
<td>nondimensional temperature lapse rate</td>
</tr>
<tr>
<td>$\phi_m$</td>
<td>nondimensional wind shear</td>
</tr>
<tr>
<td>$\theta$</td>
<td>potential temperature</td>
</tr>
<tr>
<td>$\psi$</td>
<td>potential temperature scaling constant</td>
</tr>
<tr>
<td>$\rho$</td>
<td>air density</td>
</tr>
<tr>
<td>$\sigma$</td>
<td>Stefan-Boltzmann constant</td>
</tr>
<tr>
<td>$\overline{\text{any}}$</td>
<td>overbar denotes the mean</td>
</tr>
</tbody>
</table>
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**Abstract**

A one-dimensional, time-dependent computer model of the atmospheric boundary layer was developed to simulate intermittent turbulence and the near-ground microclimate under nighttime stable conditions. In this study, the model produced several turbulent events (oscillations) through the nighttime period that varied in number, frequency, and strength along the axes of initial geostrophic wind speed. These results were found to be in close agreement with results from several previous observational and theoretical studies of this type. It is suggested, therefore, that the one-dimensional computer model is a useful mathematical representation of the nighttime case that includes intermittency.