

AN EVALUATION OF MICROBURST PREDICTION INDICES FOR THE KENNEDY SPACE CENTER AND CAPE CANAVERAL AIR STATION (KSC/CCAS)

THESIS

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Abstract

A wet-microburst event on 16 August 1994 at the Kennedy Space Center's Shuttle Landing Facility alerted forecasters from the 45th Weather Squadron (45WS), the provider of weather support to the Kennedy Space Center (KSC) and Cape Canaveral Air Station (CCAS), to the challenges of wet-microburst prediction. Although there was no operational impact, this event caused the 45WS to revise their severe thunderstorm forecasting procedures to specifically address microbursts, resulting in the locally developed Microburst-Day Potential Index (MDPI). MDPI provides a several-hour outlook of microburst potential based on the results of the Microburst and Severe Thunderstorm (MIST) project. The 45WS also conducted a preliminary evaluation of the Wind INDEX (WINDEX) for the KSC/CCAS microburst forecast problem. WINDEX provides an estimate of the maximum observed gust speed that can be expected should a microburst occur. This thesis presents an evaluation of MDPI and WINDEX based on microbursts identified by Sanger (1999) in his KSC/CCAS microburst climatology. A new index for assessing microburst potential is also introduced, incorporating both the MDPI and WINDEX parameters. Overall neither the MDPI nor the WINDEX performed particularly well in this application. The MDPI showed very little improvement over random guessing, and the WINDEX showed very little correlation to observed maximum microburst gust speed. The new microburst potential index outperformed MDPI in almost all categories. Further refinement of the new index is needed to make it a more useful forecasting tool.

AN EVALUATION OF MICROBURST PREDICTION INDICES FOR THE KENNEDY SPACE CENTER AND CAPE CANAVERAL AIR STATION (KSC/CCAS)

1. Introduction

1.1 Background

High winds are a significant hazard to space-launch operations, including movement of the space vehicle to the launch pad, the launch, Space Shuttle landing, and takeoff and landing of the Space Shuttle ferry aircraft. An unforecasted high wind event during any of these phases can be catastrophic, causing numerous casualties and severe damage to the space vehicle and launch pad. Less visible than the launch are the many support operations that can be adversely impacted by unforecasted strong wind events. Examples of such operations include fueling/defueling of the space vehicle, launch tower repair, erecting vehicles and payloads, space vehicle transportation, and flying operations.

One of the most difficult high wind events to predict is the downburst. A downburst is a strong thunderstorm downdraft that produces a "starburst" outflow of damaging wind at or near the surface. Downbursts have been sub-classified into two types: the macroburst and the microburst. A macroburst is a large downburst with damaging outburst winds extending horizontally more than 4 km (2.5 miles). Damaging winds from a macroburst can last from 5 to 30 minutes, with winds as high as 60 ms⁻¹ (116 knots). Microbursts, on the other hand, are small downbursts with damaging

outburst winds not exceeding 4 km (2.5 miles) in horizontal extent. Microbursts generally last less than 10 minutes, with intense microbursts producing winds as high as 75 ms⁻¹ (146 knots). Microbursts are further classified into "wet-microburst" and "dry-microburst" depending on the amount of precipitation associated with the downdraft (Fujita 1985). The small temporal and spatial scales of the microburst make them difficult to predict and pose a significant threat to space launch and support operations.

On 16 August 1994, the Kennedy Space Center (KSC) and Cape Canaveral Air Station (CCAS) experienced several "downrush" wind events. The strongest wind gust, which was in excess of 33.5 ms⁻¹ (65 knots), was recorded at the Shuttle Landing Facility and was later attributed to a wet-microburst event (Wheeler and Roeder 1996).

Forecasters assigned to the 45th Weather Squadron (45WS), the provider of weather support to Patrick Air Force Base (PAFB), the Kennedy Space Center, Cape Canaveral Air Station and the Eastern Range, forecasted airmass-type thunderstorm activity for that afternoon and expected high wind gusts but not near the magnitude that was experienced.

Although there was no operational impact, this event sparked the 45WS to launch a full investigation into how such a severe wind event could elude forecasters. As a result of the investigation, the 45WS created a conceptual forecast model, the "Microburst Funnel," to guide forecasters in microburst prediction (Figure 1).

The Microburst Funnel begins with a review of thunderstorm and microburst climatology for the KSC and surrounding area. If forecasters predict thunderstorm activity in the next 6 to 10 hours microburst outlook techniques, such as the Microburst-Day Potential Index (MDPI), and the Wind Index (WINDEX), are used to determine if the environment is favorable for microburst development, and to determine the maximum

wind gust that can be expected should a microburst occur. Intermediate techniques, such as satellite imagery interpretation, are used to identify areas where thunderstorm development is imminent. Finally, nowcasting techniques, such as radar and visual identification are used just prior to issuance or non-issuance of a high wind warning.

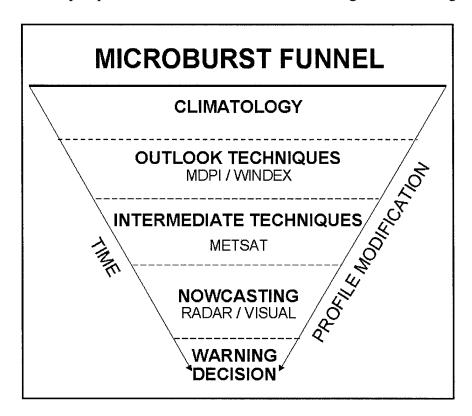


Figure 1. Microburst Funnel (Adapted from Roeder 1999)

This thesis focuses only on the two outlook techniques mentioned above, the MDPI and WINDEX indices, since most pre-launch operations, such as shuttle roll-out, can last up to eight hours. Early detection of a microburst producing environment in tandem with accurate microburst gust speed predictors can help mission planners postpone lengthy pre-launch operations when out-of-threshold winds are predicted, saving precious time and money.

Both MDPI and WINDEX are computed using upper-air sounding data. MDPI uses the difference between the minimum equivalent potential temperature (θ_e) found between 650 mb and 500 mb, and the maximum θ_e near the surface to assess the potential for microburst activity (Wheeler and Roeder 1996). WINDEX is an empirical index that gives an estimate of the maximum potential wind gust, at the surface, in knots (McCann 1994). Both indices are useful since they give significant lead time (6-10 hours) and are easily computed using data that is readily available.

Throughout this thesis, the terms "downburst" and "microburst" will be used interchangeably. This is common when the horizontal scale of the event is unknown (Caracena et al. 1990). All microbursts occurring at the KSC, CCAS, and Eastern Range will be assumed to be wet-microbursts since the thermodynamic requirements for dry-microbursts (an extensive, dry, sub-cloud layer) rarely exist on the Central Florida Atlantic Coast.

1.2 Problem Statement

Neither MDPI nor WINDEX have been evaluated by the 45WS for greater than a six month period. Additionally, neither index has been evaluated using the microburst cases identified by Sanger (1999) in his KSC/CCAS microburst climatology. Preliminary evaluation of MDPI indicated that $\Delta\theta_e$ values of greater than 30K suggest a high likelihood of a microburst, assuming thunderstorm or rainshower development. Evaluation of MDPI using a larger period of record is required.

Preliminary evaluation of the WINDEX caused the 45WS to question its usefulness at its locale. Expansion of the period of record is required before WINDEX

can be ruled out as a gust speed predictor for microbursts along the Central Florida Atlantic Coast. The 45WS is also interested in synergy between these two indices.

1.3 Objective

This thesis seeks to evaluate the MDPI by extending the evaluated data set from 6 months to 25 months (May-September 1994-1998).

A Weibull distribution is fit to 282 microburst gust speeds identified by Sanger (1999) in his KSC microburst climatology (see Chapter 2, section 2.6). The Weibull distribution is integrated for each of the 45WS warning thresholds, providing a "first guess" probability of needing to issue a convective wind warning should a microburst occur.

The WINDEX is also evaluated for its usefulness as a predictor of microburst gust speed for the Central Florida Atlantic Coast. Finally, a new index for assessing microburst potential is introduced. This new index incorporates both the MDPI and WINDEX variables.

1.4 Importance of Research

The 45WS provides weather support to launch and support activities conducted by the National Aeronautics and Space Administration (NASA), the Department of Defense (DOD), and other users of the CCAS, KSC, and Eastern Range launch facilities. Part of this support is issuance of convective wind warnings for the criteria listed in Table 1. The desired lead-times listed in Table 1 are needed to ensure PAFB, KSC, CCAS, and Eastern Range personnel have adequate time to protect valuable resources from adverse

weather. Failure to meet these lead-times may result in property loss and possible loss of human life. Accurate wind gust prediction indices play a vital role in helping to meet these stringent requirements.

| Location | Criterion | Lead-time |
|------------------|------------|------------|
| | ≥ 35 knots | 30 minutes |
| KSC (Sfc-300ft) | ≥ 50 knots | 60 minutes |
| | ≥ 60 knots | 60 minutes |
| CCAS (Sfc-200ft) | ≥ 35 knots | 30 minutes |
| | ≥ 50 knots | 60 minutes |
| PAFB (Sfc) | ≥ 35 knots | 60 minutes |
| | ≥ 50 knots | 60 minutes |

Table 1. Convective Wind Warning Criteria (Roeder 1999)

1.5 Overall Approach

Six steps were required to complete this research. First a Weibull distribution was fit to 282 microburst gust speeds identified by Sanger (1999) in his KSC microburst climatology. This distribution was integrated for each of the 45WS convective wind warning thresholds, providing a "first guess" of the probability of breaking a threshold should a microburst occur. Second was the identification of microburst-days and the identification of thunderstorm-days without microbursts. This was accomplished by identifying all thunderstorm-days for the KSC and CCAS between May - September 1994-98 by analyzing surface observations from the KSC and CCAS. A day was considered a "thunderstorm-day" if the KSC or CCAS surface observation reported thunderstorms, rainshowers, cumulonimbus, or lightning in either the significant weather section or the remarks section. These days were cross-referenced with the KSC/CCAS microburst-days identified by Sanger (1999) in his KSC microburst climatology. Since Sanger did not identify microburst events for 1994 a computer program was written to identify microbursts occurring in May-September 1994.

Step three consisted of computing the MDPI and WINDEX parameters. CCAS sounding data furnished by the Air Force Combat Climatology Center was used to compute MDPI and WINDEX values.

Step four consisted of a performance evaluation of both the MDPI and WINDEX equations. Statistical tools such as hit-rate, false-alarm rate, probability of detection, Heidke skill score, and the Pearson correlation coefficient (r) were used to measure the performance of each index.

Step five was development of a new microburst potential index using the MDPI and WINDEX parameters by way of discriminant analysis. Lastly, a performance comparison between the original MDPI and the new microburst potential index was completed using the same performance measurements listed in step three.

1.6 Organizational Overview

Chapter 2 presents an overview of literature regarding convective downbursts, including a brief history of terminology and the development of the MDPI and WINDEX indices. Chapter 3 describes the data set used in this thesis and the computation of the MDPI and WINDEX parameters. Chapter 4 discusses the research methodology. The statistical techniques used for data analysis and development of a new microburst index are also covered. Chapter 5 summarizes the results and conclusions, and discusses opportunities for future research.

2. Literature Review

2.1 A Brief History of Microburst Terminology

How have meteorologists gone from downdraft to "microburst?" The best way to answer this question is to look at the events, or discoveries, that led to this term. The existence of downdrafts, associated with thunderstorms, has been known to meteorologists since the late 19th century (Fujita and Caracena 1977). The most notable study of horizontal and vertical air currents in and around thunderstorms, the Thunderstorm Project, was conducted by Byers and Braham (1949) in the late 1940's. Based on this project, Byers and Braham (1949) established the three stages of thunderstorm cells that are commonly taught at universities around the world: a) the cumulus stage characterized by updrafts throughout the cell, b) the mature stage with both updrafts and downdrafts, and c) the dissipating stage dominated by strong downdrafts. Downbursts are a special type of downdraft first categorized in the mid-1970's.

While investigating the Eastern Airlines Flight 66 crash that occurred at John F. Kennedy Airport, New York City on 24 June 1975, Dr. T. Theodore Fujita hypothesized that the accident was a result of a unique wind phenomenon that he called a "downburst" (Fujita and Caracena 1977). Fujita defined a downburst as a downdraft with speeds "comparable to or greater than the approximate rate of descent or climb of a jet aircraft on the final approach or takeoff at 91 m (300 ft) above the surface." He chose what he considered a conservative threshold value of 3.6 m s⁻¹ (12 ft s⁻¹) as the dividing line between an ordinary downdraft and a downburst.

In 1978, the first field research project on downbursts, the Northern Illinois Meteorological Research On Downburst (NIMROD), was conducted by the University of Chicago, and was headed by Fujita and Srivastava (Fujita 1985). Using three Doppler radars and 27 portable automated mesonet stations, the research team collected data on a large number of downbursts over a period of 42 days. Because of the overwhelming number of wind observations recorded during the 42 day period (approx. 1,632,960 observations), Fujita (1985) developed a computer algorithm for identifying potential downbursts that occurred within the network (Table 2). Condition 1 sets a minimum gust speed of 10 ms⁻¹ (19.4 knots) to be considered a downburst. Conditions 2 and 3 state that the peak wind must be at least 5 ms⁻¹ (10 knots) faster than the five-minute mean wind speed prior to and after the peak wind. Conditions 4 and 5 ensure that the peak wind is not a gust "superimposed" on sustained high winds. Condition 6 excludes the gust front "which is characterized by an exponential decay of the gusty winds behind a front" (Fujita 1985).

| Condition 1 | Peak wind must be greater than 10 ms ⁻¹ (19.4 knots) |
|-------------|---|
| Condition 2 | Peak wind must be at least 5 ms ⁻¹ (10 knots) faster than five-minute mean |
| | prior to peak |
| Condition 3 | Peak wind must be at least 5 ms ⁻¹ (10 knots) faster than five-minute mean |
| | after the peak |
| Condition 4 | Peak wind must be 1.25 times the five-minute mean prior to the peak |
| Condition 5 | Peak wind must be 1.25 times the five-minute mean after the peak |
| Condition 6 | Five-minute mean prior to peak must be no more than 1.5 times the five- |
| | minute mean after the peak |

Table 2. Six Condition Algorithm for Identifying Potential Downbursts (Fujita 1985)

To obtain further evidence of a downburst, Fujita (1985) simultaneously plotted wind vectors for all towers at the time of the suspected downburst in order to analyze the field for a distinctive divergent flow pattern. A potential downburst was catagorized as a true downburst only if a divergent flow pattern was recognized. Fifty downbursts were identified during this project.

Noticing significant differences in the horizontal scale of these downbursts, Fujita (1985) subclassified them into "macroburst" and "microburst." A macroburst is a large downburst with damaging outburst winds extending horizontally more than 4 km (2.5 miles). Damaging winds from a macroburst can last from 5 to 30 minutes, with winds as high as 60 ms⁻¹ (116 knots). Microbursts, on the other hand, are small downbursts with damaging outburst winds not exceeding 4 km (2.5 miles) in horizontal extent. Microbursts generally last less than 10 minutes, with intense microbursts producing winds as high as 75 ms⁻¹ (146 knots) (Fujita 1985).

Of the 50 microbursts detected during the NIMROD field project, 64% were accompanied by 0.25 mm (0.01 inches) of rain or more. The remaining 36% had no measurable rain. Because of this, microbursts were further classified into "dry microburst" and "wet-microburst" depending on the accompaniment of measurable rain (Fujita 1985). Since then, research by Brown et al. (1982), Caracena et al. (1983), Wakimoto (1985), and many others, has helped to increase understanding of the dry microburst environment. Wet-microbursts have not been studied nearly as much; however, it is clear that the wet-microburst environment is quite different from the dry-microburst environment (Caracena et al. 1990).

2.2 Wet-Microburst Storm Structure

In 1975, a meteorological mesonetwork was established in south central Florida for the Florida Area Cumulus Experiment (FACE). The FACE project was not a microburst study; however, on 1 July 1975, a wet-microburst made nearly a direct hit on the experiment's Field Observing Site (FOS). Weather observers at the FOS originally believed that a tornado had touched down nearby. An investigation shortly after the storm determined that the damage pattern was indicative of outflow at the base of a downdraft versus flow into a tornado vortex (Caracena and Maier 1987). Because of the fine data resolution of the collected data, and the central location of the microburst within the mesonetwork, this microburst, known as the FACE microburst, has significantly enhanced current understanding of wet-microburst structure (Caracena and Maier 1987).

Generally, thunderstorms producing wet-microbursts are characterized by low cloud bases, storm tops reaching as high as 15 km (49,000 ft) and strong precipitation cores that are composed almost entirely of ice in the upper-levels (Atkins and Wakimoto 1991). They normally occur in environments that are nearly moist adiabatic and statically unstable from the surface to about 500 mb, with a deep layer of high relative humidity near the surface (Doswell 1994). This rather moist layer is capped by a cool, dry layer (low equivalent potential temperature) which is the most probable source of microburst energy once convection and precipitation begin to occur (Caracena and Maier 1987). As downdrafts from precipitation loading begin, the cool, dry layer ejects pockets of dry air into the saturated downdraft region (Caracena et al. 1990). Latent heat of evaporation into the dry air contributes significantly to the negative buoyancy of the parcel (Caracena and Maier 1987). The key to developing a wet-microburst is this

evaporation of condensed water during descent, thus maintaining saturation. Without this evaporation, the parcel would begin to warm at the dry adiabatic lapse rate, become warmer than its surrounding environment, and quickly lose its negative buoyancy (Doswell 1994). Figure 1 shows a schematic of a thunderstorm producing a wetmicroburst. In addition to the evaporative effects, the presence of high relative humidity in the low levels increases the virtual temperature difference between the downdraft and the environment, also contributing to an increase in negative buoyancy (Atkins and Wakimoto 1991).

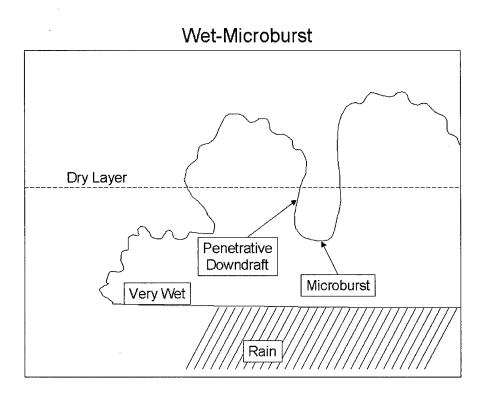


Figure 2. Conceptual model of a wet-microburst characterized by a dry source layer that ejects dry pockets of air into an underlying saturated layer, producing the evaporation that can cause a microburst (After Caracena et al. 1990).

2.3 The Wet-Microburst Environment

Using data collected during the Microburst and Severe Thunderstorm (MIST) project that operated in northern Alabama in 1986, Atkins and Wakimoto (1991) documented the general environmental conditions (thermodynamic characteristics) that favor wet-microburst development. The MIST project used a network of 41 Portable Automated Mesonet (PAM-II) stations and 30 FAA-Lincoln Laboratory Operational Weather Studies (FLOWS) stations, spaced approximately 2 km (1.25 miles) apart, to collect meteorological data every minute. Atmospheric soundings were also taken twice daily, one at 0700 CDT, and one at 1300 CDT. From this set of data, 33 microbursts were identified using a computer algorithm first suggested by Fujita (1985). Analyzing the synoptic charts, sounding data, and mesonetwork data from the MIST network area, Atkins and Wakimoto (1991) determined the thermodynamic characteristics for microburst-producing days and compared them to the characteristics for the days with thunderstorms that did not produce microbursts.

Atkins and Wakimoto described a wet-microburst environment as one that begins with a shallow morning radiation inversion that inhibits convection in the lowest 75 mb of the atmosphere. As the surface begins to heat, the inversion is replaced by a dry-adiabatic sub-cloud layer that extends from the surface to about 850 mb. The layer between 850 mb and 500 mb is relatively moist. This is capped by a cool, dry layer above 500 mb (Atkins and Wakimoto 1991). Figure 2 shows morning and afternoon sounding models for a wet-microburst-producing day.

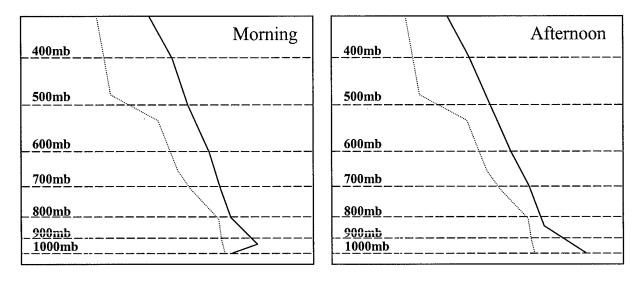


Figure 3. Model Thermodynamic Charts Conducive for Wet-Microburst Occurrence. Dashed line is the dew point curve; solid line is the temperature curve (After Atkins and Wakimoto, 1991).

By plotting the equivalent potential temperature (θ_e) profiles for the microburst producing days, Atkins and Wakimoto found a minimum of θ_e was typically found between 650 mb and 500 mb, or just below the capping cool, dry layer. The afternoon θ_e profile showed a $\Delta\theta_e$, from the surface to the mid-level minimum, greater than or equal to 20 K. The non-microburst producing storms had a $\Delta\theta_e$ less than or equal to 13 K. Equivalent potential temperature plots for other well-documented wet-microburst cases confirmed these results. Atkins and Wakimoto then suggested that by forecasting an afternoon sounding based on the morning sounding, the $\Delta\theta_e$ values of 20 K and 13 K can be used as "threshold" values for the development of wet-microbursts. They envisaged these thresholds being used to issue a general "area-wide alert" for potential wet-microburst activity. Figure 4 shows model morning and afternoon θ_e profiles for a wet-microburst environment.

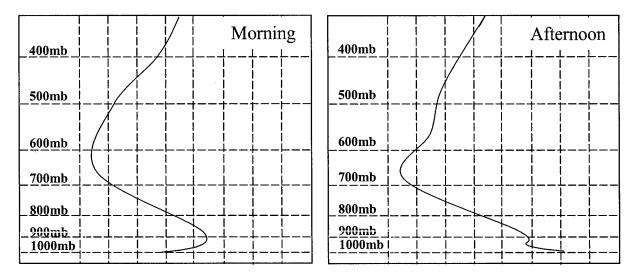


Figure 4. Model θ_e profile (solid curve) for an environment conducive to wet-microburst development. Vertical dashed lines are θ_e values increasing from left to right at a 5 K interval (After Atkins and Wakimoto 1991).

2.4 The Microburst-Day Potential Index (MDPI)

A wet-microburst event that occurred at the Kennedy Space Center's (KSC) Shuttle Landing Facility on 16 August 1994 led the 45WS to revise their severe thunderstorm forecasting procedures to specifically address microbursts. This resulted in the development of the Microburst-Day Potential Index (MDPI). MDPI provides a several-hour outlook of microburst potential based on θ_e profiles first introduced by Atkins and Wakimoto (1991). The MDPI equation is:

$$MDPI = \frac{Maximum\,\theta_e - Minimum\,\theta_e}{CT} \tag{1}$$

where

Maximum θ_e is the maximum θ_e in the lowest 150 mb of the sounding (Kelvin)

Minimum θ_e is the minimum θ_e in the layer between 650 and 500 mb (Kelvin), and

CT is the critical threshold (or normalization factor) currently defined as 30 K.

Given thunderstorm development, MDPI values of 1 or greater indicate a strong probability of a wet-microburst, and MDPI values of less than 1 indicate a low probability of a wet-microburst. Preliminary analysis of MDPI indicated that it shows good skill in alerting forecasters to the potential for wet-microbursts (POD = 96.4%) without an unreasonable false alarm rate (FAR = 32.5%) (Wheeler and Roeder 1996).

2.5 The Wind INDEX (WINDEX)

McCann (1994) introduced an index for identifying airmasses favorable for the development of microbursts. The "Wind INDEX," or WINDEX, is based on studies of observed and modeled microbursts. It is a highly empirical index based on the vertical momentum and continuity equations developed by Wolfson (1990). Wolfson showed that microburst vertical velocity is proportional to some "forcing" times the depth of the downdraft (Δz). "This forcing is proportional to the square of the environmental lapse rate, Γ , through which a downdraft descends (McCann 1994)." Since a major source of microburst negative buoyancy is from the absorption of latent heat due to melting and evaporation, McCann considers the downdraft depth to be the height of the melting level above the surface. The WINDEX equation is:

$$WI = 5[H_M R_Q (\Gamma^2 - 30 + Q_L - 2Q_M)]^{0.5}$$
 (2)

where

 H_M is the height of the melting level above the ground (km)

 Γ is the lapse rate from the surface to the melting level (°C km⁻¹)

 Q_L is the mixing ratio of the lowest 1 km above the surface (g kg⁻¹)

 Q_M is the mixing ratio at the melting level (g kg⁻¹)

N is the moisture adjustment 12 g kg⁻¹, and $R_Q = Q_L/N$ but not exceeding 1.

Before using WINDEX, it is important to consider the following: 1) When the lapse rate is low, the radicand may become negative. When this happens, WI is zero and the probability of a microburst is nil. 2) The term R_Q attempts to account for an overestimation of WINDEX values in a dry environment. This term implies that when the low-level mixing ratio is less than 12 g kg⁻¹, the atmosphere is too dry to produce a high precipitation storm. 3) WINDEX is very sensitive to environmental lapse rate error. 4) Multiplication of the radicand by five, on the right side of the WINDEX equation, gives an estimate of the maximum potential surface gust in knots (McCann 1994).

WINDEX is computed using observed sounding data or data from numerical prediction models. The actual WINDEX value is the maximum potential surface gust, in knots, that can be expected from a microburst (McCann 1994). Based on McCann's verification data, WINDEX correlates well with the observed gust speeds of known microburst events. Table 3 shows WINDEX values and observed gust speeds for well documented microbursts.

| LOCATION | DATE | WINDEX | OBSERVED | SOURCE |
|-----------------|-----------|--------|----------|----------------------------|
| Southern FL | 1 Jul 75 | 53 | 60 | Caracena and Maier (1987) |
| Northern AL | 20 Jul 86 | 59 | 60 | Wakimoto and Bringi (1988) |
| Northern AL | 13 Jul 86 | 56 | 56 | Wakimoto and Bringi (1988) |
| San Antonio, TX | 2 Sep 87 | 63 | 59 | Ladd (1989) |
| San Antonio, TX | 2 Sep 82 | 68 | 53 | Ladd (1989) |
| Norman, OK | 26 Aug 87 | 54 | 55 | Stewart (1991) |
| Tampa, FL | 19 Jul 88 | 56 | 52 | Stewart (1991) |
| Vero Beach, FL | 4 Jun 90 | 61 | 50 | Stewart (1991) |
| Amarillo, TX | 21 May 86 | 44 | 47 | Sohl (1987) |
| near Denver, CO | 19 May 82 | 47 | 48 | Wakimoto (1985) |

Table 3. WINDEX Calculations for Known Microburst Events (McCann 1994).

Preliminary analysis of WINDEX by the 45WS showed that it tends to underestimate gust speeds for the Central Florida Atlantic Coast (Roeder 1999). Further analysis is required to determine the usefulness of WINDEX at the KSC and CCAS.

2.5.1 Forcasting Dry Microbursts Using WINDEX

Murdoch (1997) evaluated WINDEX as a gust predictor for dry-microbursts in the Southwest United States. Dry-microbursts were identified using Storm Data (1983-1993) and other dry-microburst studies. Nineteen upper-air soundings taken at 12 UTC between the months of March - October, from Midland, Amarillo, and El Paso, Texas and Albuquerque, New Mexico were loaded into the Skew-T/Hodograph Analysis and Research Program (SHARP) workstation for analysis. The 19 soundings were provided by the National Climatic Data Center (NCDC) and from the National Weather Service Office (NWSO) Midland's upper-air data archives. Once loaded into SHARP, the soundings were modified to reflect the conditions at the time of the microburst. These "modified" soundings were used to calculate WINDEX.

Murdoch (1997) concluded that WINDEX "agreed well with the observed and estimated wind gusts, yeilding a mean error of -5.8 [knots]." Murdoch (1997) offered two explanations for this underestimation in cases where the cloud bases were high: 1) Loss of momentum as the absorption of latent heat ends and adiabatic heating continues, and 2) Low average 1 km mixing ratios compared to a typical dry microburst sounding.

2.5.2 WINDEX Computation from Weather Satellite Derived Soundings

The National Environmental Satellite Data and Information Service (NESDIS) Forecast Products Development Team (FPDT) evaluated two experimental microburst prediction products derived from Geostationary Operational Environmental Satellite (GOES) sounder retrievals (vertical temperature and moisture profiles) (Ellrod and Nelson 1998). One of the experimental products plots WINDEX as a color-coded graphic superimposed on a visible, infrared, or water vapor image. This product was evaluated for a two-month period. WINDEX values were compared to reports of wind damage or wind gusts greater than 50 knots reported in the National Weather Service (NWS) Storm Prediction Center's (SPC) preliminary storm data. More than 300 wind damage reports were compared to adjacent WINDEX values derived from sounder retrievals. In 92 percent of the cases WINDEX values were greater than 40 knots, while 60 percent exceeded 50 knots. Overall, Ellrod and Nelson (1998) found that the absolute value of the mean GOES WINDEX differed from the mean observed wind gusts by less than 3 knots. They found that the GOES WINDEX product was "generally most reliable over the eastern and central United States during daylight hours" (Ellrod and Nelson 1998).

2.6 Microburst Identification at the Kennedy Space Center (KSC)

A four-year, summertime microburst climatology was produced for the KSC, CCAS, and Eastern Range by Sanger (1999). This is the first microburst climatology ever produced in the United States. The period of record was May through September 1995-98. A total of 282 microbursts were identified over 114 microburst days during this

four-year period. Sanger showed that the most prominent months with microbursts, within the KSC WINDS network, are June, July, and August with the highest frequency in July. "The most favorable time for microbursts is between 1600 UTC (12 P.M. EDT) and 2200 UTC (6 P.M. EDT) with the peak occurring between 2000 UTC (4 P.M. EDT) and 2200 UTC (6 P.M. EDT)" (Sanger 1999). Appendix A lists the microburst events identified by Sanger.

2.6.1 The KSC/CCAS Weather Information Network Display System (WINDS)

The KSC operates one of the densest mesonetworks in continuous operation in the United States. This network collects, disseminates, and archives wind direction and speed, as well as other meteorological parameters, over an area of approximately 1200 km² which encompasses the KSC, CCAS, Eastern Range, and surrounding remote locations. On average there is one tower every 27 km². The most densely instrumented region is along the East Coast within the KSC, CCAS, and Eastern Range complexes (Figure 5). The instrumented towers that make-up this network take meteorological measurements every minute, but archive data at five-minute intervals. Therefore, the data used for Sanger's (1999) research consisted of the peak and mean wind speeds every five-minutes verses the one-minute interval used in the NIMROD and MIST studies (Sanger 1999).

Sanger (1999) mentions several limitations of the WINDS network that make microburst identification difficult. First is the overall placement of the towers. Sanger mentions that many of the towers have "poor meteorological exposure" resulting in erroneous data. Second is the overall tower spacing. Towers to the south and southwest of CCAS are sparsely populated potentially inhibiting detection of a microburst between

towers. Third is the varying number of sensors on each tower. Some towers may only have sensors at 6 and 30 feet (Tower 512) while others may have as many as 8 sensors at 6, 12, 54, 162, 204, 295, 394, and 492 feet (Tower 3131). Lastly, Sanger believes that the data interval of five-minutes may be too long for identifying short-lived microburst events (Sanger 1999).

2.6.2 Microburst Identification Technique

Sanger (1999) used a computer program, written in the Interactive Data Language (IDL), to analyze WINDS tower data from May through September 1995-98 to identify possible microbursts. Six conditions (Table 4) needed to be met simultaneously before a wind reading could be considered a possible microburst event. These conditions are a modified version of Fujita's (1985) six condition algorithm for identifying potential downbursts. Since the WINDS archive data interval is 5 minutes, the pre-peak mean wind speed and post-peak mean wind speed used by Fujita were replaced by the peak wind 5 minutes before and 5 minutes after the potential microburst.

| Condition 1 | Potential microburst must be greater than 10 ms ⁻¹ (19.4 knots) | | |
|-------------|---|--|--|
| Condition 2 | Potential microburst must be at least 5 ms ⁻¹ (10 knots) faster than the five- | | |
| | minute peak prior to the potential microburst | | |
| Condition 3 | Potential microburst must be at least 5 ms ⁻¹ (10 knots) faster than the five- | | |
| _ | minute peak after the potential microburst | | |
| Condition 4 | Potential microburst must be 1.25 times the five-minute peak prior to the | | |
| | potential microburst | | |
| Condition 5 | 5 Potential microburst must be 1.25 times the five-minute peak after the | | |
| | potential microburst | | |
| Condition 6 | Five-minute peak prior to potential microburst must be no more than 1.5 | | |
| | times the five-minute peak mean after the potential microburst | | |

Table 4. Sanger's Six Condition Algorithm for Identifying Potential Microburst (Sanger 1999)

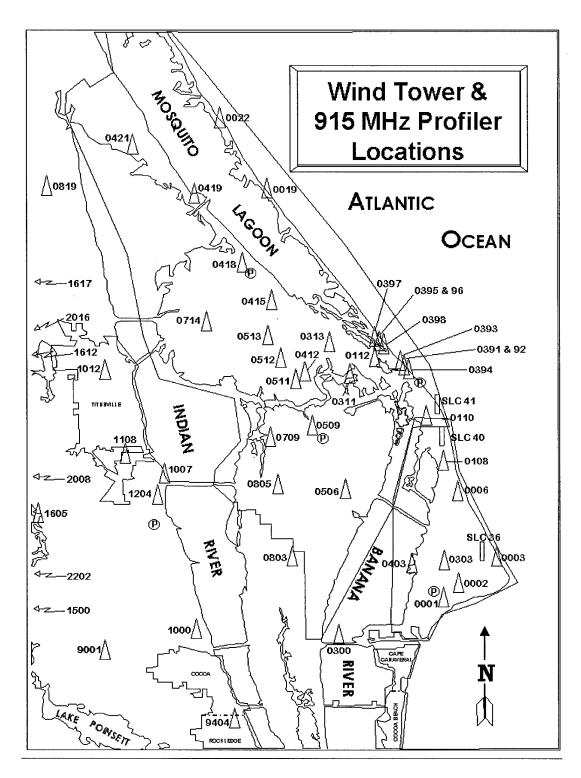


Figure 5. Map of KSC WINDS Tower Network. Triangles indicate tower location.

Like Fujita, Sanger simultaneously plotted wind vectors for all towers at the time of the suspected microburst in order to analyze the field for a distinctive divergent flow pattern. Sanger, however, did not throw-out a suspected microburst if a divergent flow pattern could not be identified, noting that the wide spacing of towers could miss the divergent flow pattern. This is consistent with the technique used in the 1986 MIST project (Atkins and Wakimoto 1991).

3. Data and Computation of MDPI and WINDEX Parameters

3.1 Introduction

Three data-sets were used to accomplish this research: a) Weather Information Network Display System (WINDS) tower data from May - September 1994, b) Upperair sounding data from May - September 1994-98, and c) KSC and CCAS surface observations from May - September 1994-98. The following gives a brief description of these data-sets and an overview of how they were used in the context of this research.

3.2 Weather Information Network Display System (WINDS) Tower Data

The Weather Information Network Display System (WINDS), operated by the KSC, collects, disseminates, and archives data from 201 meteorological sensors on 44 instrumented towers at the CCAS and KSC, and at remote surrounding sites. This network is one of the most dense mesonetworks in continuous operation in the United States, covering approximately 1200 km² for an average of one tower every 27 km². These towers are organized into three groups based on their primary application (Raytheon 1996):

a. Launch Critical Towers - These towers are at the launch complexes, the Shuttle Landing Facility (SLF) and in some remote locations. They use the most sensitive sensors in the network and are used to ensure that launch constraints are satisfied during countdown and major pad operations. These sensors are also used to assess possible blast damage effects due to detonation of the solid rocket motors.

- b. Safety Critical Towers These towers are located near areas where propellants and other toxic chemicals are stored or handled. They are used by Range Safety models to predict the diffusion of potential airborne contaminants released from chemical spills.
- c. Forecast Critical Towers These towers generally surround the KSC and CCAS, and are used primarily for weather forecasting and early detection of hazardous weather conditions.

It is important to mention that, although each tower is assigned to one of the above groups, the data from these towers is displayed and archived as one integrated network, allowing any tower to contribute to any application. The distinction between tower groups is, therefore, insignificant operationally (Raytheon 1996).

Of primary concern for this research are the wind speeds and gust speeds recorded by this network. WINDS data for May - September 1994 was provided by the 45WS in the format shown in Appendix B. The following parameters were provided: Julian Day, time (UTC), tower number, sensor height (ft), mean wind direction (degrees), 5-minute average wind speed (knots), instantaneous peak speed recorded in a 5-minute interval (knots), standard-deviation of wind direction (degrees), temperature (°C), dew-point temperature (°C), and relative humidity (%). Not all sensors report all of the above parameters. This data was used to identify potential microbursts that occurred in 1994, using Sanger's six condition algorithm for identifying potential microbursts (Sanger 1999).

3.3 KSC Upper-Air Sounding Data

Upper-Air Sounding Data from the KSC (station 74794) for the period May - September 1994-98 was provided by the Air Force Combat Climatology Center.

Soundings are taken routinely during the summer months at the KSC, at 10 UTC, 15 UTC, and 22 UTC. Additional soundings are taken on launch days, and on days with highly weather sensitive operations. The MDPI and WINDEX parameters were computed using the 15 UTC soundings since most microbursts, at KSC, occur between 16 UTC and 22 UTC (Sanger 1999). The 10 UTC sounding is too early and would have little predictive ability for microbursts that occur after 16 UTC. Use of the 22 UTC sounding would have virtually no predictive ability since most microbursts occur before this time. The sounding data provided includes the following: date, time, geopotential height, pressure level, temperature, dew-point temperature, wind direction, and wind speed. Missing data is indicated by a "999" entry. Appendix C is a sample upper-air sounding in decoded format. Column 1 is the time (UTC); column 2 is the day; column 3 is the month; column 4 is the year; column 5 is the pressure (mb); column 6 is the height (meters); column 7 is the temperature (°C); column 8 is the dew-point temperature (°C); column 9 is the wind direction (degrees); column 10 is the wind speed (knots).

3.3.1 Handling Missing Data Within a Sounding

Many of the WINDEX and MDPI parameters require temperature and/or dewpoint temperatures for levels that were reported as missing (reported as "999"). A computer program, written in IDL, was used to interpolate this data (Appendix D). Interpolation was done by assuming a constant lapse rate from the last known temperature (or dew-point) to the next known temperature (or dew-point) in the sounding. Figure 6 illustrates this interpolation process.

Step 1 takes the difference between the last known and next known temperatures in the sounding. Step 2 computes the difference between the height of the last known

temperature value and the next known temperature value in the sounding. Step 3 builds a weighting ratio by taking the ratio of the difference between the height of the missing temperature value and the value computed in Step 2. This weighting ratio ensures that the temperature used in place of the missing value is proportional to the change in height from the last known temperature. Step 4 multiplies the weighting ratio by the value computed in Step 1 and subtracts that value from the last known temperature, yielding the interpolated temperature value. This same process is used to interpolate missing dew point temperatures as well.

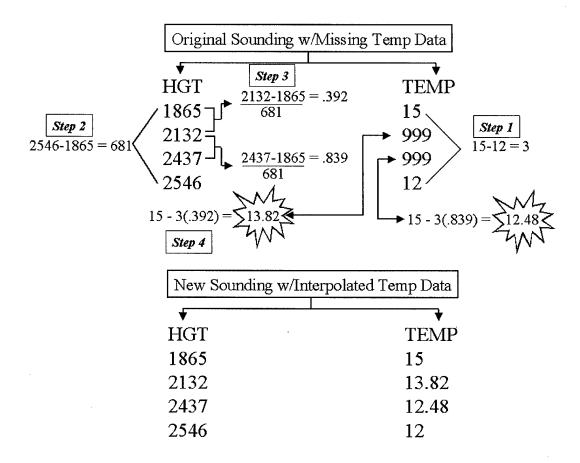


Figure 6. Interpolation of Missing Temperature Data. A weighting ratio was computed and then multiplied by the change in temperature between the two known levels. This value was then subtracted from the last known temperature reading. This ensured that the temperature was reduced by an amount that was proportional to the change in height from the last known temperature to the height of the missing value.

3.3.2 Computation of the MDPI parameters

The Microburst-Day Potential Index uses the difference in equivalent potential temperature between the surface (lowest 150 mb) and mid-levels (between 650 mb and 500 mb) to determine the potential for microburst activity within the next 6-10 hours. Equivalent potential temperature (θ_e) is the temperature a parcel of air would be if it was expanded pseudo-adiabatically until all the water vapor has condensed, released its latent heat, and fallen out, and was then compressed dry-adiabatically to 1000 mb (Wallace and Hobbs 1977). The following equations, from *AWS/TR-83/001 Equations and Algorithms for Meteorological Applications in Air Weather Service* (Duffield and Nastrom 1983), were used to compute equivalent potential temperature:

$$\mathcal{H} = T \left[\left(\frac{P_o}{P} \right)^{k(1 - 0.28w)} \right] \exp \left[\left(\left(\frac{A}{T_{LCL}} \right) - 2.54 \right) w (1 + 0.81w) \right]$$
(3)

where

$$T_{LCL} = T_d - (B + 0.001571T_d - 0.000436T_o)(T_o - T_d) + C$$
(4)

and

 θ_e is the equivalent potential temperature (Kelvin)

T is the temperature at pressure level P (Kelvin)

 P_o is the reference pressure level 1000 mb

P is pressure (mb)

A is the empirically derived value 3376 K

 T_{LCL} is the temperature at the lifted condensation level (LCL) (Kelvin)

k is 0.2854

w is the mixing ratio (kg kg⁻¹)

B is the empirically derived value 0.212 °C

C is the value 273.16 K which converts Celsius to Kelvin

 T_d is the surface dew point temperature (°C), and

 T_o is the surface temperature (°C)

A computer program written in the Interactive Data Language (IDL) was used to compute θ_e at each level of the atmospheric sounding (Appendix D). The following equations were used to compute the mixing ratio (w) needed in equation (3):

$$w = 0.622 \cdot \frac{e}{p - e} \tag{5}$$

where

$$e(T_d) = D \cdot \exp\left[\frac{17.67 \cdot T_d}{T_d + E}\right]$$
 (6)

and

w is the mixing ratio (kg kg⁻¹)

p is the pressure at the level where T is measured (mb)

e is the vapor pressure at the level where T_d is measured (mb)

D is the empirically derived value 6.112 mb

E is the empirically derived value 243.5 °C

 T_d is the dew-point temperature at the level where T is measured (°C)

Equation (6) approximates the vapor pressure, and is valid within 0.1% over the temperature range -30°C $\leq T_d \leq$ 35°C (Rogers and Yau 1996).

3.3.3 Computation of the WINDEX Parameters

WINDEX uses five parameters that are computed from an atmospheric sounding, to estimate the maximum gust speed at the surface that can be expected from a microburst. These parameters are the height of the melting level (H_m) (km), the mean environmental lapse rate from the surface to the height of the melting level (Γ) (°C km⁻¹), the mixing ratio in the lowest 1 km of the atmosphere (Q_l) (g kg⁻¹), the mixing ratio at the melting level (Q_m) (g kg⁻¹), and a moisture adjustment factor (R_q) which is equal to $Q_l/12$ but not greater than 1. A computer program written in IDL was used to compute WINDEX (Appendix D). The following is a brief overview of how each parameter was computed:

- a. Height of the Melting Level (H_m) The height where the temperature sounding first becomes less than zero (McCann 1999). This height was converted to kilometers by dividing by 1000.
- b. Mean Environmental Lapse Rate (Γ) from the Surface to H_m This was computed by dividing the surface temperature by the height of the melting level (H_m) (McCann 1999).
- c. Mixing Ratio in the Lowest 1 km (Q_l) Computed by using equations (5) and (6), above, to compute the mixing ratio at the surface and at 1 km. The arithmetic mean was then computed and used as Q_l .
- d. Mixing Ratio at the Melting Level (Q_m) Computed by using equations (5) and (6), above, at the level where the temperature sounding first becomes less than zero.

e. Moisture Adjustment Factor (R_q) - This is equal to $Q_l/12$ but not greater than 1. 3.4 KSC and CCAS Surface Observations

Surface observations from the KSC (KCOF) and the CCAS (KTTS), for the period May - September 1994-98, were used to identify thunderstorm days. A day was considered a "thunderstorm-day" if the KSC or CCAS surface observation reported thunderstorms, rainshowers, cumulonimbus, or lightning in either the significant weather section or the remarks section between 15 UTC and 22 UTC. These days were cross-referenced with the KSC/CCAS microburst-days identified by Sanger (1999), in his KSC microburst climatology, to determine which days had thunderstorms that produced microbursts and which days had thunderstorms that did not produce microbursts.

4. Methodology

4.1 Introduction

This thesis seeks to accomplish four objectives for the 45WS. 1) Fit a Weibull distribution to the 282 microburst gust speeds identified in Sangers's (1999) KSC microburst climatology and integrate for the 45WS convective wind warning criteria. 2) Evaluate MDPI using an expanded period of record. 3) Evaluate WINDEX as a predictor of microburst gust speed for the KSC/CCAS microburst forecast problem. 4) Develop a new microburst index using the MDPI and WINDEX parameters. The methodology presented in this chapter was designed to meet these objectives accurately and efficiently.

4.2 Summary of Methodology

- 1) Fit a Weibull Distribution to the KSC/CCAS observed microburst gusts identified by Sanger (1999) and integrate for convective wind warning criteria.
 - 2) Identify 1994 microburst cases and add to Sanger's climatology.
- 3) Distinguish microburst producing thunderstorm days from non-microburst producing thunderstorm days.
 - 4) Compute MDPI and WINDEX parameters.
- 5) Evaluate MDPI using standard forecast verification techniques (i.e., probability of detection, false alarm rate, hit rate, threat score, Heidke skill score).
- 6) Compare WINDEX versus observed microburst gust speed to determine predictive value.

- 7) Use WINDEX and MDPI parameters to develop a new microburst potential index by way of discriminant analysis.
 - 8) Compare new index to MDPI using standard forecast verification techniques.

4.3 Fitting a Weibull Distribution to the KSC Microburst Climatology

In 1939, the Swedish physicist Waloddi Weibull introduced a family of distributions now known as Weibull distributions. In some instances there are theoretical justifications for the use of a Weibull distribution, but in many applications they simply provide the best fit of observed data. The probability density function (pdf) for a Weibull distribution is

$$f(x; \gamma, \alpha, \beta) = \begin{cases} \frac{\alpha}{\beta^{\alpha}} (x - \gamma)^{\alpha - 1} e^{-\left(\frac{x - \gamma}{\beta}\right)^{\alpha}} & x \ge 0\\ 0 & x < 0 \end{cases}$$
 (7)

where

x is the range of the observed data

 γ is the offset (equal to 0 if distribution begins at the origin)

 α is the shape parameter

 β is the scale parameter

Weibull distributions are fit to a data set by adjusting the offset, shape and scale parameters to fit the distribution of the observed data (Devore 1995). Crystal Ball[©] was used to obtain the shape and scale parameters that fit the gust speed distribution of the 282 microbursts identified by Sanger (1999). Mathcad[©] was then used to integrate

equation (7) for the 45WS convective wind warning criteria yielding the probability of having microburst gusts greater than 35 knots, 50 knots, and 60 knots. Figure 7 is a sample Weibull distribution with $\gamma = 15$, $\alpha = 2$, and $\beta = 30$.

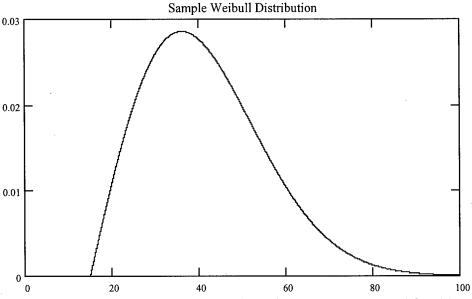


Figure 7. Sample Weibull Distribution with $\gamma = 15$, $\alpha = 2$, and $\beta = 30$.

4.4 Identifying 1994 Microbursts Using WINDS Tower Data

WINDS tower data was provided by the KSC for May - September 1994. A program written in IDL was used to identify microbursts based on Sanger's (1999) six-condition algorithm since these microbursts would be added to his climatology. Three hundred seventy-two potential microbursts were identified using this approach. Further analysis of the data indicated that an overwhelming majority of these "microbursts" were a result of an apparent archival problem with the 1994 data. Thirty-four of the potential microbursts had peak gusts greater than 90 knots even though Sanger identified only 2 microbursts with winds greater-than or equal-to 90 knots in his 4-year climatology. Most

of the extremely high peaks (70 knots or greater) had 5-minute mean winds, for the same period, of less than 10 knots. Additionally, many towers that have multiple sensors indicated a high peak wind at one level that was not reflected at levels above or below. Table 5 is a sample erroneous "microburst" from the 1994 WINDS data. Notice the peak wind of 117 knots at 54 feet with a mean during the same period of only 3 knots. Such a high peak wind should have a more significant influence on the mean for the same period. Additionally, the peak wind reading at 12 feet (just 42 feet below the "microburst"), for the same tower and period, is only 14 knots.

| Julian Date | Time | Tower | Height | Direction | Mean | Peak |
|-------------|------|-------|--------|-----------|------|------|
| 94142 | 1215 | 112 | 12 | 330 | 3 | 14 |
| 94142 | 1215 | 112 | 54 | 333 | 3 | 117 |

Table 5. Sample Erroneous Microburst. The 117-knot peak wind at 54 feet should have greater influence on the 5-minute mean for that height and the peak wind at 12 feet for the same period.

"Microbursts" like the one described in Table 6 plagued the 1994 WINDS data, making it impossible to distinguish real microbursts from erroneous data. It is believed that these anomalies are an archival problem since the errors are not isolated to just a few towers and heights. As a result, the 1994 tower data was discarded and not added to Sanger's (1999) climatology.

4.5 Distinguishing Microburst/Non-Microburst Thunderstorm Days

Surface observations from the KSC (KCOF) and the CCAS (KTTS), for the period May - September 1994-98, were used to identify thunderstorm days. A day was considered a "thunderstorm-day" if the KSC or CCAS surface observation reported

thunderstorms, rainshowers, cumulonimbus, or lightning in either the significant weather section or the remarks section between 15 UTC and 22 UTC. These days were cross-referenced with the microburst-days identified by Sanger (1999), in his KSC microburst climatology, to determine which days had thunderstorms that produced microbursts and which days had thunderstorms that did not produce microbursts.

4.6 Computing MDPI and WINDEX Parameters

The MDPI and WINDEX parameters were computed for microburst and non-microburst days that had 15 UTC soundings available. All parameters were computed using the equations and procedures described in Chapter 3. Of the 114 microburst-days identified by Sanger (1999), 92 had microbursts between 15 UTC and 22 UTC; of those, 73 had 15 UTC soundings available. One hundred sixty-seven non-microburst producing thunderstorm days had thundertorms between 15 UTC and 22 UTC, and 15 UTC soundings available. Appendix E lists the MDPI and WINDEX parameters for the 240 microburst and non-microburst producing thunderstorm days used in this study.

4.7 Evaluating MDPI

The MDPI was evaluated using the following forecast verification methods: probability of detection (POD), false alarm rate (FAR), hit rate (HR), threat score (TS), and Heidke skill score (HSS). These are the same methods used in previous MDPI studies conducted by the 45WS. A chi-squared (χ^2) test for goodness of fit was also computed for completeness. Additionally, a scatterplot of $\Delta\theta_e$ versus microburst occurrence was used to evaluate the MDPI critical threshold (CT).

Table 6 is a generic 2 X 2 contingency table used for forecast verification. Each position on the table displays the absolute frequencies, or counts, of each possible combination of forecast and observed pairs. Dividing these counts by the sample size (total number of forecast/observed pairs) transforms the counts into relative frequencies (Wilks 1995). The equations for computing the following accuracy and skill measures refer to Table 6.

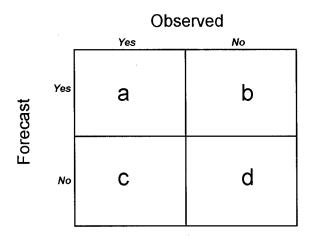


Table 6. 2 X 2 Contingency Table for Forecast Verification (After Wilks 1995)

4.7.1 Probability of Detection (POD)

The probability of detection (POD), also known as prefigurance, is the fraction of occasions in which the forecast event occurred when it was forecast. For this study it is the likelihood that a microburst would be forecast, given that it occurred. The best possible POD is 1, indicating all microbursts that occurred were forecast. The worst POD is 0, indicating all microbursts that occurred were not forecast (Wilks 1995). In terms of Table 6

$$POD = \frac{a}{a+c} \tag{8}$$

4.7.2 False Alarm Rate (FAR)

The false alarm rate (FAR) is the proportion of forecasts for which the forecasted phenomenon fails to materialize. For this thesis, it is the likelihood that a microburst is forecast but not observed. The best possible FAR is 0, indicating that all forecast microbursts were observed. The worst possible FAR is 1, indicating none of the forecast microbursts were observed (Wilks 1995). In terms of Table 6

$$FAR = \frac{b}{a+b} \tag{9}$$

4.7.3 Hit Rate (HR)

The hit rate (HR), sometimes known as the proportion correct, is the fraction of the total forecasts that are correct. The worst hit rate is zero and the best hit rate is 1.

The HR is sometimes multiplied by 100% and called the percent correct (Wilks 1995). In terms of Table 6

$$HR = \frac{a+d}{n} \tag{10}$$

where n is the total number of forecast/observation pairs (a+b+c+d).

4.7.4 Threat Score (TS)

Sometimes it is not always desirable to use HR as a measure of forecast accuracy since it credits "yes" and "no" forecasts equally. The threat score (TS), or critical success index (CSI), is often used when the event to be forecast, in this case microburst occurrence, occurs substantially less frequently than the non-occurrence. Essentially, the TS "is the number of correct "yes" forecasts divided by the total number of occasions on which that event was forecast and/or observed" (Wilks 1995). This is basically the same

as removing the correct "no" forecasts from the hit rate. The lowest attainable threat score is 0 and the best is 1 (Wilks 1995). In terms of Table 6

$$TS = CSI = \frac{a}{a+b+c} \tag{11}$$

4.7.5 Heidke Skill Score (HSS)

Equations (8), (9), (10), and (11) measure the average correspondence between a forecast and the event the forecast is trying to predict. They are measurements of accuracy but not skill. Forecast skill is a measure of the relative accuracy of a set of forecasts, based on a set of control or reference forecasts. To have skill, the forecasts must perform better than the reference forecasts. The Heidke skill score (HSS) is a measure of forecast skill using the hit rate that would be achieved by random chance as the reference. It is the most commonly used skill score for summarizing 2 X 2 contingency tables. Perfect forecasts receive a HSS of 1, forecasts that are as good as the reference receive a HSS of 0, and forecasts that perform worse than the reference receive a negative HSS (Wilks 1995). HSS is computed in terms of Table 6 by

$$HSS = \frac{2(ad - bc)}{(a+c)(c+d) + (a+b)(b+d)}$$
(12)

4.7.6 Chi-Squared Test for Goodness of Fit

To assess the validity of a forecast technique it is important to determine how the observed "hits" and "misses" in a 2 X 2 contingency table compare to the "hits" and "misses" that would be generated by a completely random selection process. The method for assessing the validity of the forecast technique is a chi-squared (χ^2) test for goodness of fit. The null hypothesis for the χ^2 test is that the forecasts do not perform better than a

random selection process; the researcher's hypothesis is that the forecasts do perform better than a random selection process (Kachigan 1986). The equation for computing χ^2 is

$$\chi^2 = \sum_{\text{all cells}} \frac{(\text{observed - expected})^2}{\text{expected}}$$
 (13)

where the expected value is computed by multiplying the marginal totals for the row and column, corresponding to the particular cell, and then dividing by the sum of all cells (n). In terms of Table 6 the expected value of cell a is

expected value of cell
$$a = \frac{(a+b)(a+c)}{a+b+c+d}$$
 (14)

If the χ^2 value is greater than a critical value determined by an a priori significance level (α) then the null hypothesis is rejected and the forecast technique is said to be valid. If the χ^2 value is less than the critical value the forecast technique is said to be without merit (Kachigan 1986).

P-values were also computed based on the χ^2 value. The p-value is the area under the χ^2 distribution to the right of the χ^2 value. It is the smallest level of significance (α) at which the null hypothesis would be rejected. The p-value can also be thought of as the probability of getting a χ^2 value greater than or equal to the one obtained by the sample data, given the null hypothesis is true. For example, if a χ^2 value of 8.15 is computed based on a 2 X 2 contingency table, the associated p-value of 0.0043 would indicate that there is a 0.43% probability of obtaining that value given the null is true (Devore 1995).

4.7.7 Evaluating MDPI Critical Threshold (CT)

The MDPI critical threshold was evaluated using a scatterplot of $\Delta\theta_e$ versus microburst occurrence. The $\Delta\theta_e$ was plotted on the ordinate and microburst occurrence was plotted on the abscissa. Microburst occurrence was plotted as a 1 and non-occurrence was plotted as a 0. Figure 8 is an idealized scatterplot of $\Delta\theta_e$ versus microburst occurrence. Note that ideally there is very little overlap between the $\Delta\theta_e$ values corresponding to microburst occurrence and the $\Delta\theta_e$ values corresponding to non-microburst occurrence, with the overlap centered roughly on the MDPI critical threshold (30K - horizontal line).

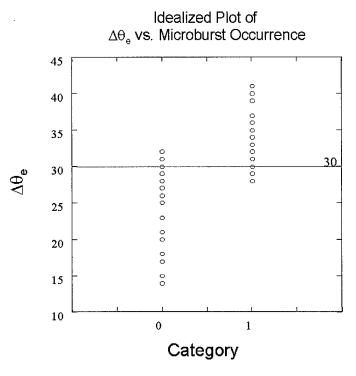


Figure 8. Idealized Plot of $\Delta\theta_e$ vs. Microburst Occurrence. Microburst occurrence is plotted as a 1 and non-microburst occurrence is plotted as a 0. Horizontal line marks the MDPI critical value (30K).

4.8 Evaluating WINDEX

The Pearson correlation coefficient (r) was used to evaluate the degree of association between the maximum gust speeds predicted by WINDEX and the observed microburst gust speeds identified by Sanger (1999). Commonly referred to as the correlation coefficient, r is used to determine if there is a linear relationship between two variables. The value of r is bound by 1 and -1, with 1 indicating a perfect positive correlation, 0 indicating no correlation, and -1 indicating a perfect negative correlation (Wilks 1995). The equation for computing the Pearson correlation coefficient for n pairs $(x_1, y_1), \ldots, (x_n, y_n)$ is

$$r = \frac{s_{xy}}{\sqrt{\sum (x_i - \overline{x})^2} \sqrt{\sum (y_i - \overline{y})^2}}$$
 (15)

where

$$s_{xy} = \sum_{i=1}^{n} (x_i - \overline{x})(y_i - \overline{y})$$
 (16)

For the purpose of this thesis, 73 (n=73) WINDEX/observed gust speed pairs $\{(x_i,y_i),...,(x_{73},y_{73})\}$ were evaluated. The WINDEX was computed using the 15 UTC soundings for microburst days identified by Sanger (1999). These WINDEX values were paired with the maximum microburst gust speed observed between 15 UTC and 22 UTC for the given microburst day.

A scatterplot of observed maximum microburst gust speed versus WINDEX was used to visually determine the degree of linear correlation and to see if a non-linear relationship exists. Figure 9 shows an idealized scatterplot of observed maximum microburst gust speed versus WINDEX. The correlation coefficient for the idealized plot

is 1. Notice that the plot increases from left to right at a 45 degree angle showing a perfect linear relationship.

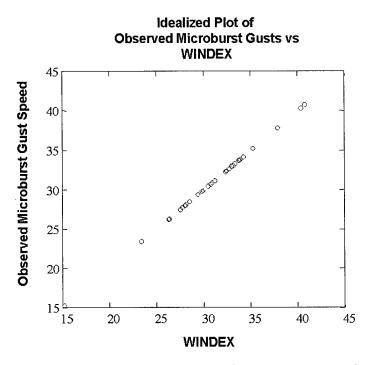


Figure 9. Idealized plot of observed maximum microburst gust speed versus WINDEX. The plot increases from left to right at a 45-degree angle indicating a perfect positive correlation (r = 1).

4.9 New Index Development

A statistical technique known as discriminant analysis was used to develop a new index for assessing wet-microburst potential for the Central Florida Atlantic Coast.

Discriminant analysis is a method of classifying individuals or objects into mutually exclusive and exhaustive groups based on a set of independent predictor variables. It involves deriving linear combinations of the predictor variables that will discriminate between two or more previously defined groups such that misclassification error is minimized (Dillon and Goldstein 1984). This is done by assigning discriminant weights to the predictor variables. A discriminant score for each measured object is calculated by

multiplying the discriminant weight, associated with each predictor variable, by the object's value on the predictor variable and then summing over the set of predictor variables. The equation for computing the discriminant scores is known as the discriminant function. For n number of objects to be classified and p predictor variables the discriminant function has the form

$$Y=b'X$$
 (17)

where

Y is a $1 \times n$ vector of discriminant scores

b' is a $1 \times p$ vector of discriminant weights, and

X is a $p \times n$ matrix containing the values for each of the n objects on the p predictor variables.

Objects are then grouped based on their discriminant scores and a discriminant cutoff score. Discriminant scores above the cutoff are placed into one group; discriminant scores below the cutoff are placed into the other. Figure 10 shows a graphical illustration of a two-group discriminant analysis with two predictor variables. The top part of the graph depicts a scatterplot of the two predictor variables (X_1 and X_2) for each object in the two groups. The lower part of the graph depicts the Y distributions (distributions of discriminant scores) for the two groups. The dotted line separating the two groups and two distributions is the cutoff score. Note that the greater the overlap of the two Y distributions (or scatterplots) the more errors in classification (Dillon and Goldstein 1984).

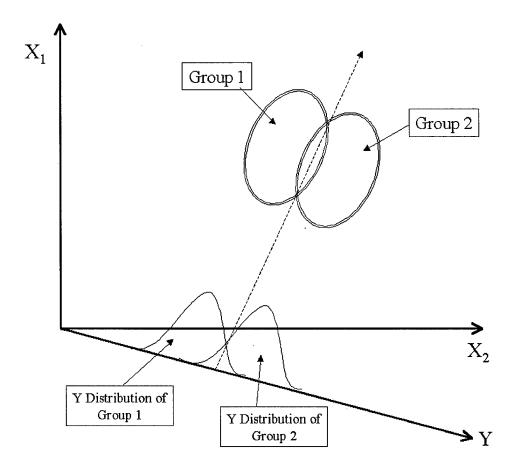


Figure 10. Graphical Illustration of Two-Group Discriminant Analysis. The upper part of the figure depicts a scatterplot (enclosed by ovals) of the two predictor variables $(X_1 \text{ and } X_2)$. The lower portion of the figure depicts the distributions of discriminant scores (Y) for each group (After Dillon and Goldstein 1984).

There were six steps to developing a new index using discriminant analysis. They were 1) choose predictor variables from the pool of MDPI and WINDEX parameters and other atmospheric measurements related to computing MDPI and WINDEX, 2) build a discriminant analysis input table (matrix) to train the discriminant model, 3) determine the discriminant weights, 4) compute discriminant scores for each group and determine the best cutoff score, 5) develop and evaluate the confusion matrix, and 6) compare the performance of the discriminant function (new index) to MDPI.

4.9.1 Choosing Predictor Variables

For the purpose of this thesis, the two groups being discriminated were microburst producing thunderstorm days and non-microburst producing thunderstorm days. The predictor variables were drawn from the pool of MDPI and WINDEX parameters and other MDPI and WINDEX related variables. The nine MDPI and WINDEX parameters are described in Chapter 3. Other atmospheric parameters used as potential predictor variables were

- a. The pressure corresponding to the maximum θ_e in the lowest 150 mb of the atmosphere (mb) $(P_{max}\theta_e)$
- b. The pressure corresponding to the minimum θ_e between 650 mb and 500 mb (mb) ($P_{min} \theta_e$). This is an indicator of the height of the cool, dry layer based on MDPI.
- c. The minimum θ_e regardless of the pressure level (K) ($Min \theta_{e-actual}$). This is the value used to compute $\Delta \theta_e$ in the MIST project (Atkins and Wakimoto 1991).
- d. The pressure corresponding to $Min \theta_{e-actual}$ (mb) ($P_{min \theta_{e-actual}}$). This is an indicator of the height of the cool, dry layer based on the MIST project.
- e. The change in θ_e between the maximum θ_e in the lowest 150mb and $Min \theta_{e-actual}$ (K) ($\Delta \theta_{e-actual}$). This is the method used to compute $\Delta \theta_e$ in the MIST project (Atkins and Wakimoto 1991).

Parameters for a stratified random sample of 50 microburst producing thunderstorm days and 50 non-microburst producing thunderstorm days were used to build (or train) the index. Equal samples of microburst and non-microburst producing thunderstorm days were used since the statistical software package used in this thesis (S-

Plus 2000) performs best using equal samples from each group. The remaining 23 microburst producing thunderstorm days and a random sample of 39 non-microburst producing thunderstorm days were used to verify the new index. Since using 13 parameters is cumbersome for an index, a method was developed to determine which parameters were most important for microburst development.

A Pearson correlation coefficient (r) table (Appendix F), showing the r-values for each parameter as they relate to microburst occurrence and as they relate to each other, was developed using Statistix[©] for Windows[©]. The parameters that had the highest correlation to microburst occurrence and the least inter-correlation were used to build the index. They were $\Delta\theta_{e-actual}$, $P_{min\thetae-actual}$, and Γ . A discriminant analysis input table (matrix) was build using these parameters.

4.9.2 Building the Discriminant Analysis Input Table

A discriminant analysis input table is a tool for organizing the parameters that will be used to develop the discriminant function (Kachigan 1991). Table 7 is a generic discriminant analysis input table. Column 1 contains the objects that will be discriminated; for this thesis, it contains the days for which the predictor variables were measured. Column 2 indicates the group in which the object belongs. A 1 indicates a microburst producing thunderstorm day and a 0 indicates a non-microburst producing thunderstorm day. Columns 3, 4, and 5 are the predictor variables; they are equivalent to the transpose of matrix **X** in equation (17).

| Object | Group | Predictor 1 | Predictor 2 | Predictor 3 |
|--------|-------|-----------------|-----------------|-----------------|
| Day 1 | 1 | x ₁₁ | X ₁₂ | x ₁₃ |
| Day 2 | 1 | x ₂₁ | X ₂₂ | X ₂₃ |
| Day 3 | 1 | X31 | X ₃₂ | X33 |
| Day 4 | 1 | X41 | X42 | X43 |
| Day 5 | 0 | X ₅₁ | X ₅₂ | X ₅₃ |
| Day 6 | 0 | x ₆₁ | X ₆₂ | X ₆₃ |
| Day 7 | 0 | X71 | X ₇₂ | X ₇₃ |
| Day 8 | 0 | X ₈₁ | X ₈₂ | X ₈₃ |
| Day 9 | 0 | X91 | X92 | X93 |

Table 7. Generic Discriminant Analysis Input Table (After Kachigan 1991).

Appendix G is the discriminant analysis input table for the 100 thunderstorm days used to train the discriminant function. Appendix H is the discriminant analysis input table for the 62 thunderstorm days used to verify the index.

4.9.3 Determining the Discriminant Weights

In 1936, Fisher developed a method for determining the discriminant weights based on the assumption that the variance-covariance matrices for each of the two groups have a common value (Dillon and Goldstein 1984). This common value is approximated by using the sample pooled variance-covariance matrix defined by the equation

$$\mathbf{S}_{\text{pooled}} = \frac{(n_1 - 1)[\mathbf{S}_1] + (n_2 - 1)[\mathbf{S}_2]}{(n_1 + n_2 - 1)} \tag{18}$$

where

 $\boldsymbol{S_{pooled}}$ is the sample pooled variance-covariance matrix

 $\mathbf{S_1}$ is the variance-covariance matrix for the predictor variables associated with group 1 $\mathbf{S_2}$ is the variance-covariance matrix for the predictor variables associated with group 2

 n_1 is the number of objects measured in group 1, and n_2 is the number of objects measured in group 2

The following equation is used to objectively determine the discriminant weights based on samples from each of the two groups.

$$\mathbf{b} = \mathbf{S}_{\mathsf{pooled}}^{-1}(\overline{\mathbf{x}}_{1} - \overline{\mathbf{x}}_{2}) \tag{19}$$

where

b is a vector of discriminant weights

 S_{pooled}^{-1} is the inverse of the sample pooled variance-covariance matrix

 $\overline{\mathbf{x}}_1$ is a vector of means of each predictor variable in group 1

 $\overline{\mathbf{x}}_2$ is a vector of means of each predictor variable in group 2

S-Plus[®] 2000 was used to compute the sample pooled variance-covariance matrix and the group mean vectors for the stratified random sample of 100 thunderstorm days in Appendix G. A Mathcad template (Appendix I) was used to compute the discriminant weights based on the S-Plus[®] 2000 output.

4.9.4 Computing Discriminant Scores and Determining the Cutoff

A Mathcad template (Appendix I) was used to compute the discriminant scores for each group in the training sample in Appendix G using equation (17). The cutoff score was computed by the equation

$$Y_{cutoff} = \mathbf{b}' \frac{\overline{\mathbf{x}}_1 + \overline{\mathbf{x}}_2}{2} \tag{20}$$

where \mathbf{b}' , $\overline{\mathbf{x}}_1$, and $\overline{\mathbf{x}}_2$ are defined above. Equation (18) is valid only when the sample sizes of group 1 and group 2 are the same (Dillon and Goldstein 1984). Future observations of Y can be grouped based on Y_{cutoff} according to the rule

Y belongs to group 1 if it is greater than or equal to Y_{cutoff}

Y belongs to group 2 if it is less than Y_{cutoff}

4.9.5 Developing and Evaluating Confusion Matrix

A confusion matrix is a type of contingency table used to evaluate a discriminant function's ability to properly categorize objects or events. Table 8 is a generic confusion matrix for thunderstorm classification (microburst producing or non-microburst producing). Cells a and d indicate the number of correctly categorized thunderstorms. Cells b and c indicate the number of incorrectly categorized thunderstorms. Confusion matrices can be produced for the training data or for verification data (Dillon and Goldstein 1984). If the discriminant function is used to forecast events, the confusion matrix is the same as a contingency table for forecast verification.

Actual Category

| | _ | Microburst | Non-Microburst |
|-----------------------|----------------|------------|----------------|
| Discriminant Category | Microburst | а | b |
| Discrimine | Non-Microburst | С | d |

Table 8. Generic Confusion Matrix for Thunderstorm Category (Microburst Producing and Non-Microburst Producing).

4.9.6 Comparing Performance of the Discriminant Function (New Index) to MDPI

Once the discriminant weights and the cutoff score have been computed equation (17) takes the form of a new index similar to MDPI. Future measures of the predictor variables can be used to compute a discriminant score (Y) that is categorized as either a microburst producing thunderstorm day or a non-microburst producing thunderstorm day based on the cutoff score (Y_{cutoff}). Discriminant scores and MDPI values were computed using a stratified random sample of 62 thunderstorm days (23 that produced microbursts and 39 that did not) to compare the performance of the two indices. None of the validation thunderstorm days were used to train the discriminant function. Two contingency tables were produced: one containing the absolute frequencies, or counts, of forecast and observed microbursts based on the discriminant cutoff (Y_{cutoff}) ; the other containing the absolute frequencies based on MDPI. The indices were compared using POD, FAR, HR, TS, HSS and χ^2 . Skill scores for POD, FAR, HR, and TS with MDPI as the reference forecast were also computed. Skill scores (SS) are interpreted as a percentage improvement over a reference forecast. They are computed with the following equation:

$$SS_{ref} = \frac{A - A_{ref}}{A_{perf} - A_{ref}} \times 100\%$$
 (21)

where

 SS_{ref} is the skill score of a forecast technique with respect to some reference forecast technique

A is the accuracy score for the set of forecasts associated with the forecast technique being evaluated A_{ref} is the accuracy score for a set of reference forecasts, and

 A_{perf} is the accuracy score that would be achieved by a set of perfect forecasts.

5. Results and Conclusions

5.1 Introduction

This chapter summarizes the results and conclusions of this thesis using the methods described in Chapter 4. The last section lists opportunities for future research.

5.2 Fitting a Weibull Distribution to the KSC Microburst Climatology

The program Crystal Ball[©] was used to determine the Weibull shape and scale parameters that best fit the gust speed distribution of the 282 microbursts identified by Sanger (1999) in his KSC microburst climatology. The shape parameter (α) was 1.6263 and the scale parameter (β) was 16.88. Figure 11 shows a histogram of microburst gust speed with a rough distribution curve overlay. Figure 12 shows the fitted Weibull distribution based on the shape and scale parameters computed by Crystal Ball. Both figures were computed using Mathcad[©]. The curve in Figure 12 was integrated for each of the 45WS convective wind warning critical thresholds yielding the probability of having winds greater than 35 knots, 50 knots, and 60 knots should a microburst occur. All computations were done using Mathcad[©]. The resulting probabilities are

- a. The probability of winds greater than 35 knots given microburst occurrence is .44
- b. The probability of winds greater than 50 knots given microburst occurrence is .08
- c. The probability of winds greater than 60 knots given microburst occurrence is .02

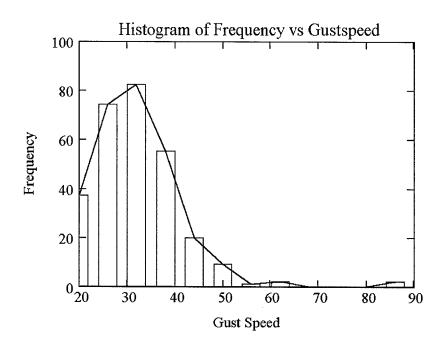


Figure 11. Histogram of Microburst Gust Speeds Identified by Sanger (1999) With Rough Distribution Curve Overlay.

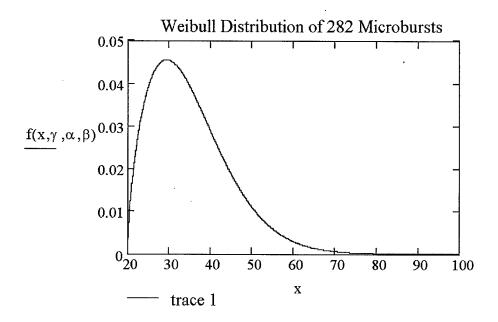


Figure 12. Weibull Distribution of 282 Microbursts Identified by Sanger.

5.3 Evaluation of MDPI

MDPI was computed for 73 microburst producing thunderstorm days and 167 non-microburst producing thunderstorm days using the procedure described in Chapter 3. Table 9 shows the 2 X 2 forecast verification contingency table for this data. The following accuracy and skill scores were computed using procedures described in Chapter 4.

Probability of Detection (POD) = 65%

Heidke Skill Score (HSS) = 8%

False Alarm Rate (FAR) = 65%

Chi-Square $(\chi^2) = 2.12$

Hit Rate (HR) = 51%

P-value = .145

Threat Score (TS) = 29%

Forecast

No

Observed Yes No Yes 93

MDPI Evaluation

Table 9. 2 X 2 Forecast Verification Contingency Table For MDPI

74

25

Overall MDPI did not perform particularly well. A χ^2 test was used to assess the validity of the index. The null hypothesis was that the "hits" and "misses" produced by

MDPI are no better than those that would be assigned by a random selection process; the researcher's hypothesis was that the "hits" and "misses" produced by MDPI are better than those that would be generated by a random selection process. A χ^2 value of 2.706 or greater is required to reject the null for a significance level (α) of 0.1. The χ^2 of 2.12 indicates that the cell values produced by MDPI are not significantly better than those produced by random chance (the null is not rejected). Although the contingency table failed the χ^2 test, the POD, FAR, HR, TS and HSS were computed since these are the measures used to evaluate MDPI in previous studies. The POD indicates that 65% of the microbursts would have been identified using MDPI, however, the high FAR indicates that 65% of the forecast "microbursts" would fail to materialize. This high FAR is unacceptable. The HR of 51% shows that using MDPI to determine if a microburst will occur is only slightly better than flipping a coin. The HSS, which compares MDPI to random guessing, indicates that MDPI only beats random guessing by 8%.

The MDPI critical threshold (CT) was evaluated using a scatterplot of $\Delta\theta_e$ versus microburst occurrence (Figure 13). The large overlap of the two $\Delta\theta_e$ "populations" indicates that the current CT of 30K is as good as any other value depending on the level of acceptable error determined by the user.

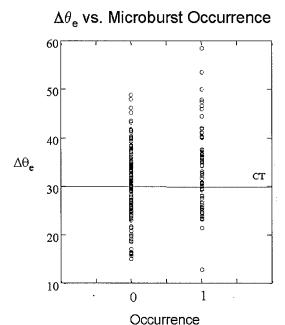


Figure 13. Scatterplot of $\Delta\theta_e$ vs Microburst Occurrence. A 0 indicates a non-microburst producing thunderstorm day and a 1 indicates a microburst producing thunderstorm day. The line marked CT is the MDPI critical threshold.

5.4 Evaluation of WINDEX

The Pearson correlation coefficient (r) was used to evaluate the degree of linear association between the maximum gust speeds predicted by WINDEX and the observed microburst gust speeds identified by Sanger (1999). Statistics for Windows was used to compute r. The r-value was 0.24 (p-value 0.29) indicating very little correlation between WINDEX and the observed gust speeds. This result is consistent with r values computed in previous WINDEX studies (Roeder 1999).

A scatterplot of observed maximum gust speed versus WINDEX (Figure 14) was used to visually determine the degree of linear correlation and to see if a non-linear relationship exists. It is clear from the plot that no discernable linear or non-linear relationship exists between WINDEX and the observed microburst gust speed.

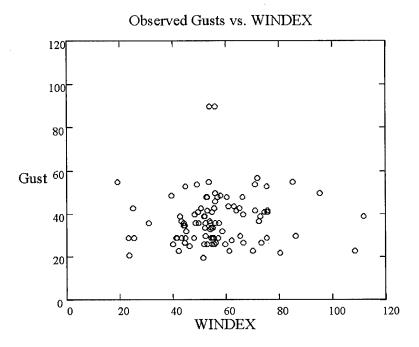


Figure 14. Scatterplot of Observed Microburst Gust Speed vs. WINDEX. It is clear from this plot that no discernable linear or non-linear relationship exists between WINDEX and the observed microburst gust speed.

5.5 New Index for Assessing Wet-Microburst Potential

A stratified sample of 50 microburst producing thunderstorm days and 50 non-microburst producing thunderstorm days was used to develop a new microburst potential index by way of discriminant analysis. The new index is

New Microburst Index =
$$\frac{b_1(Maximum\,\theta_e - Minimum\,\theta_e) + b_2(P_{\min}\,e_e) + b_3(\Gamma)}{Y_{cutoff}}$$
 (21)

where

 b_1 , b_2 , and b_3 are the discriminant weights 0.055 K⁻¹, -0.007876 mb⁻¹, and 0.966 km °C⁻¹ respectively

 Y_{cutoff} is the discriminant cutoff 3.231

Maximum θ_e is the maximum value of θ_e in the lowest 150 mb of the sounding (K)

Minimum θ_e is the minimum value of θ_e in the entire sounding (K) $P_{min\theta_e}$ is the pressure level corresponding to Minimum θ_e (mb), and Γ is the environmental lapse rate from the surface to the height of the melting level (°C km⁻¹).

New index values of 1 or greater indicate a strong potential for microburst development should a thunderstorm occur. New index values of less than 1 indicate a low potential for microburst development should a thunderstorm occur. This follows the same convention as MDPI.

Table 10 shows the confusion matrix for the 100 thunderstorm days used to train the index. Overall, the discriminant function classified 69% of the thunderstorm days correctly. The classification error rate was 31%. A χ^2 test was performed on the confusion matrix to determine if the classification procedure, defined by the discriminant function and cutoff, is statistically significant based on the training data set. The χ^2 of 14.49 and resulting p-value of 0.0001 imply that the procedure is statistically significant.

New Index Confusion Matrix

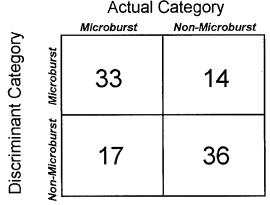


Table 10. New Index Confusion Matrix

A stratified random sample of 62 thunderstorm days (23 microburst producing and 39 non-microburst producing) was used to compare the performance of the new index to MDPI. None of the 62 verification thunderstorm days were used to build the new index. Table 11 shows the 2 X 2 forecast verification contingency table for MDPI based on the 62 thunderstorm day sample.

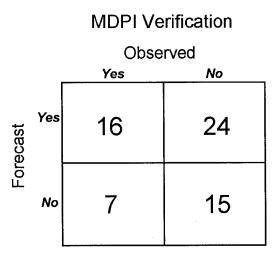


Table 11. 2 X 2 Forecast Verification Contingency Table for MDPI. This table is based on a stratified random sample of 62 thunderstorm days.

The following accuracy and skill scores were computed from Table 11.

POD = 69% HSS = 7%
$$\chi^{2} = .41$$
HR = 50% P-value = .522 TS = 34%

Overall MDPI performed about the same as the evaluation presented in section 5.3. Again a χ^2 test was used to assess the validity of the index. The null hypothesis was that the "hits" and "misses" produced by MDPI are no better than those that would be

generated by a random selection process; the researcher's hypothesis was that the "hits" and "misses" produced by MDPI are better than those that would be generated by a random selection process. Once again, the contingency table did not pass a χ^2 test for a significance level of 0.1 suggesting that the MDPI shows little merit. The *p*-value of .522 suggests that the χ^2 value of 0.14 would be attained 52.2% of the time as a result of a random selection process. Although the MDPI did not pass the χ^2 test, POD, FAR, HR, TS, and HSS were computed for comparative purposes. The 2 X 2 forecast verification contingency table for the new index is presented in Table 12.

New Index Verification

Observed Yes No 15 16 No 8 23

Table 12. 2 X 2 Forecast Verification Contingency Table for the New Index. This table is based on a random sample of 62 thunderstorm days.

The following accuracy and skill scores were computed from Table 12.

POD = 65% HSS = 23%
$$\chi^{2} = 3.39$$
 HR = 61% P-value = .066 TS = 38%

The new index outperformed MDPI in almost all accuracy and skill scores. A χ^2 test was used to assess the validity of the new index. The null hypothesis was that the "hits" and "misses" produced by new index are no better than those that would be generated by a random selection process; the researcher's hypothesis was that the "hits" and "misses" produced by the new index are better than those that would be generated by a random selection process. The new index passed the χ^2 test for a significance level of 0.1 (the null was rejected). The p-value of 0.066 suggests that the χ^2 value of 3.39 would be attained only 6.6% of the time as a result of a random selection process. This implies a significant improvement over the MDPI which reported a p-value of 0.522 for the same sample.

As per equation 21, skill scores for the new index were computed using the POD, FAR, HR, and TS for MDPI as reference accuracy tests. The new index performed 13% worse than MDPI with respect to POD, 15% better than MDPI with respect to FAR, 22% better than MDPI with respect to HR, and 6% better than MDPI with respect to TS. The HSS shows that the new index beat random guessing by 23%. This is a marked improvement over MDPI which only beat random guessing by 7%. Table 13 compares the new index performance to that of MDPI.

| , | MDPI | New Index | Skill Score |
|----------------|------|-----------|-------------|
| POD | 69% | 65% | -13% |
| FAR | 60% | 51% | 15% |
| HR | 50% | 61% | 22% |
| TS | 34% | 38% | 6% |
| HSS | 7% | 23% | N/A |
| χ ² | .41 | 3.39 | N/A |
| P-Value | .522 | .066 | N/A |

Table 13. MDPI and New Index Performance Comparison. Skill scores were computed using MDPI as the reference forecast.

5.6 Conclusion

Overall neither the MDPI nor the WINDEX performed particularly well. Neither index should be used operationally at the KSC/CCAS. The MDPI showed very little improvement over random guessing (HSS = 7%) and did not pass a χ^2 test for goodness of fit in either evaluation. The WINDEX showed very little correlation to observed maximum microburst gust speed (r = .24). Additionally, there was no discernable linear or non-linear relationship between WINDEX and observed maximum microburst gust speed. The Weibull distribution developed in this thesis is a good climatological starting point for assessing potential microburst gust speed.

A new index for predicting microburst potential was developed by way of discriminant analysis. Although the new index outperformed MDPI, its performance was, by no means, stellar. The new index did pass a χ^2 test for goodness of fit but showed only marginal improvement over random guessing (HSS = 23% and p-value

.066). Further refinement of the new index is needed to make it a more useful operational forecasting tool.

5.7 Opportunities for Future Research

There are five recommendations for future reasearch. They are

- 1) Add 1999 and 2000 microbursts to Sanger's (1999) KSC microburst climatology and evaluate the new index using an expanded data set
- 2) Redefine Γ as the environmental lapse rate from the surface to the height of the minimum θ_e aloft and re-evaluate the new index
- 3) Evaluate T1, T2, and Snyder methods for forecasting microburst gust speed at KSC/CCAS (found in AFWA TN-98/002 *Meteorological Techniques*)
- 4) Evaluate RAOB microburst prediction techniques used by the National Weather Service Office, Jackson, Mississippi for applicability at the KSC/CCAS. They include using Convective Available Potential Energy (CAPE), Vertical Totals (VT), and Wet Bulb Zero Height (WBZ) to assess microburst gust speed.
- 5) Evaluate the possibility of downward advection of momentum as a possible cause for microbursts at the KSC.

Appendix A: Microbursts Identified by Sanger (1999)

| Year | Day | Time | Tower | Height | Direction | Speed | Gust |
|------|--------|------|-------|--------|-----------|-------|------|
| 1995 | 11-May | 2045 | 819 | 54 | 300 | 15 | 36 |
| 1995 | 11-May | 2120 | 415 | 54 | 303 | 13 | 29 |
| 1995 | 11-May | 2130 | 3131 | 162 | 344 | 28 | 40 |
| 1995 | 11-May | 2215 | 300 | 54 | 325 | 21 | 41 |
| 1995 | 20-May | 0500 | 9001 | 54 | 284 | 14 | 30 |
| 1995 | 20-May | 0950 | 513 | 30 | 273 | 15 | 27 |
| 1995 | 20-May | 0955 | 1007 | 54 | 278 | 18 | 29 |
| 1995 | 20-May | 1000 | 394 | 60 | 262 | 21 | 36 |
| 1995 | 23-May | 2020 | 2008 | 54 | 79 | 16 | 32 |
| 1995 | 5-Jun | 1700 | 300 | 54 | 240 | 22 | 41 |
| 1995 | 10-Jun | 2005 | 2202 | 54 | 326 | 25 | 44 |
| 1995 | 12-Jun | 1645 | 1 | 54 | 261 | 21 | 39 |
| 1995 | 12-Jun | 1700 | 393 | 60 | 257 | 16 | 30 |
| 1995 | 12-Jun | 1700 | 398 | 60 | 257 | 16 | 35 |
| 1995 | 12-Jun | 1850 | 2016 | 54 | 295 | 13 | 23 |
| 1995 | 12-Jun | 1920 | 421 | 54 | 272 | 39 | 50 |
| 1995 | 12-Jun | 2010 | 509 | 12 | 263 | 8 | 22 |
| 1995 | 12-Jun | 2340 | 303 | 54 | 252 | 11 | 20 |
| 1995 | 12-Jun | 2345 | 36 | 90 | 249 | 15 | 32 |
| 1995 | 18-Jun | 1825 | 1000 | 54 | 39 | 13 | 26 |
| 1995 | 25-Jun | 1950 | 511 | 30 | 196 | 15 | 41 |
| 1995 | 25-Jun | 2005 | 412 | 54 | 172 | 11 | 21 |
| 1995 | 25-Jun | 2015 | 1000 | 54 | 230 | 19 | 32 |
| 1995 | 26-Jun | 2025 | 819 | 54 | 290 | 15 | 32 |
| 1995 | 26-Jun | 2040 | 9001 | 54 | 259 | 14 | 34 |
| 1995 | 26-Jun | 2050 | 403 | 54 | 262 | 12 | 37 |
| 1995 | 10-Jul | 1840 | 412 | 54 | 299 | 13 | 27 |
| 1995 | 10-Jul | 1850 | 394 | 60 | 318 | 19 | 36 |
| 1995 | 10-Jul | 1850 | 398 | 60 | 303 | 25 | 46 |
| 1995 | 10-Jul | 1925 | 506 | 54 | 171 | 14 | 36 |
| 1995 | 10-Jul | 1930 | 1 | 54 | 231 | 13 | 30 |
| 1995 | 10-Jul | 1935 | 3 | 54 | 256 | 15 | 30 |
| 1995 | 10-Jul | 1935 | 61 | 162 | 319 | 13 | 28 |
| 1995 | 10-Jul | 1935 | 108 | 12 | 147 | 2 | 21 |
| 1995 | 10-Jul | 2125 | 2008 | 54 | 234 | 7 | 25 |
| 1995 | 10-Jul | 2140 | 3131 | 54 | 302 | 13 | 27 |
| 1995 | 10-Jul | 2210 | 509 | 12 | 328 | 15 | 34 |
| 1995 | 10-Jul | 2230 | 1007 | 54 | 199 | 39 | 63 |
| 1995 | 13-Jul | 1745 | 1612 | 54 | 250 | 15 | 28 |
| 1995 | 17-Jul | 1750 | 398 | 60 | 239 | 3 | 21 |
| 1995 | 20-Jul | 1820 | 805 | 54 | 105 | 15 | 32 |
| 1995 | 20-Jul | 1855 | 3 | 54 | 263 | 19 | 32 |
| 1995 | 21-Jul | 2000 | 1007 | 54 | 274 | 15 | 27 |
| 1995 | 21-Jul | 2035 | 1 | 54 | 295 | 14 | 36 |

| Year | Day | Time | Tower | Height | Direction | Speed | Gust |
|--------------|------------------|--------------|----------|----------|-----------|----------|----------|
| 1995 | 21-Jul | 2100 | 1101 | 162 | 206 | 21 | 39 |
| 1995 | 24-Jul | 2035 | 513 | 30 | 234 | 13 | 27 |
| 1995 | 27-Jul | 1555 | 403 | 12 | 168 | 12 | 23 |
| 1995 | 28-Jul | 2145 | 397 | 60 | 109 | 16 | 37 |
| 1995 | 28-Jul | 2145 | 398 | 60 | 109 | 18 | 40 |
| 1995 | 29-Jul | 0930 | 311 | 54 | 162 | 15 | 29 |
| 1995 | 29-Jul | 0935 | 412 | 54 | 134 | 13 | 29 |
| 1995 | 30-Jul | 2050 | 397 | 60 | 66 | 18 | 29 |
| 1995 | 1-Aug | 1520 | 819 | 54 | 72 | တ | 25 |
| 1995 | 23-Aug | 1615 | 61 | 54 | 101 | 16 | 30 |
| 1995 | 23-Aug | 2235 | 61 | 54 | 109 | 22 | 39 |
| 1995 | 24-Aug | 0600 | 1101 | 54 | 145 | 23 | 43 |
| 1995 | 24-Aug | 0735 | 803 | 54 | 129 | 15 | 37 |
| 1995 | 24-Aug | 0750 | 506 | 54 | 149 | 22 | 40 |
| 1995 | 24-Aug | 0755 | 3131 | 54 | 150 | 23 | 49 |
| 1995 | 24-Aug | 0830 | 108 | 12 | 162 | 7 | 27 |
| 1995 | 24-Aug | 0840 | 511 | 30 | 140 | 18 | 36 |
| 1995 | 24-Aug | 1100 | 1101 | 162 | 149 | 34 | 50 |
| 1995 | 24-Aug | 1420 | 19 | 54 | 146 | 36 | 55 |
| 1995 | 24-Aug | 1450 | 412 | 54 | 145 | 20 | 39 |
| 1995 | 26-Aug | 2145 | 108 | 54 | 231 | 16 | 26 |
| 1995 | 27-Aug | 1840 | 303 | 54 | 257 | 8 | 22 |
| 1995 | 27-Aug | 2030 | 397 | 60 | 250 | 20 | 34 |
| 1995 | 31-Aug | 0755 | 513 | 30 | 111 | 11 | 23 |
| 1995 | 12-Sep | 1540 | 393 | - 60 | 194 | 6 | 22 |
| 1995 | 13-Sep | 1425 | 511 | 30 | 126 | 12 | 26 |
| 1995 | 25-Sep | 0305 | 403 | 12 | 222 | 9 | 30 |
| 1995 | 26-Sep | 0435 | 3131 | 162 | 182 | 13 | 32 34 |
| 1995 | 28-Sep | 0025 | 513 1 | 30 54 | 169 60 | 16 25 | 42 |
| 1995 1996 | 28-Sep 28-May | 0200 1950 | 40 | 54 | 153 | 4 | 43 |
| 1996 | 28-May | 1950 | 61 | 204 | 289 | 13 | 37 |
| 1996 | 28-May | 1950 | 311 | 54 | 15 | 16 | 39 |
| 1996 | 28-May | 1950 | 3131 | 12 | 341 | 12 | 27 |
| 1996 | 28-May | 1955 | 394 | 60 | 19 | 15 | 32 |
| 1996 | 28-May | 2010 | 108 | 12 | 1 | 8 | 27 |
| 1996 | 31-May | 0130 | 1 | 54 | 220 | 18 | 42 |
| 1996 | 31-May | 0130 | 61 | 204 | 246 | 34 | 53 |
| 1996 | 31-May | 0135 | 3 | 54 | 233 | 34 | 48 |
| 1996 | 9-Jun | 1925 | 714 | 54 | 216 | 11 | 25 |
| 1996 | 9-Jun | 2230 | 509 | 54 | 212 | 20 | 37 |
| 1996 | 19-Jun | 2115 | 36 | 90 | 291 | 20 | 41 |
| 1996 | 20-Jun | 1905 | 512 | 30 | 202 | 15 | 26 |
| 1996 | 20-Jun | 1910 | 509 | 54 | 261 | 22 | 48 |
| 1996 | 26-Jun | 1910 | 513 | 30 | 206 | 14 | 48 |
| 1996 | 27-Jun | 2235 | 393 | 60 | 349 | 9 | 29 |

| Year | Day | Time | Tower | Height | Direction | Speed | Gust |
|--------------|----------------|--------------|------------|----------|------------|----------|----------|
| 1996 | 4-Jul | 1825 | 415 | 54 | 238 | 15 | 36 |
| 1996 | 4-Jul | 1830 | 61 | 12 | 235 | 11 | 29 |
| 1996 | 4-Jul | 1830 | 112 | 54 | 248 | 25 | 40 |
| 1996 | 4-Jul | 1830 | 397 | 60 | 234 | 26 | 44 |
| 1996 | 5-Jul | 2025 | 1101 | 162 | 156 | 14 | 25 |
| 1996 | 5-Jul | 2035 | 311 | 54 | 161 | 8 | 20 |
| 1996 | 5-Jul | 2115 | 1101 | 204 | 139 | 20 | 36 |
| 1996 | 5-Jul | 2135 | 803 | 54 | 172 | 21 | 40 |
| 1996 | 6-Jul | 1940 | 803 | 12 | 223 | 6 | 20 |
| 1996 | 6-Jul | 1945 | 506 | 54 | 206 | 14 | 30 |
| 1996 | 6-Jul | 2140 | 512 | 30 | 200 | 15 | 26 |
| 1996 | 6-Jul | 2145 | 394 | 60 | 258 | 16 | 33 |
| 1996 | 6-Jul | 2145 | 397 | 60 | 209 | 16 | 32 |
| 1996 | 6-Jul | 2200 | 512 | 30 | 329 | 12 | 32 |
| 1996 | 11-Jul | 2000 | 805 | 54 | 325 | 15 | 27 |
| 1996 | 11-Jul | 2115 | 61 | 204 | 315 | 15 | 27 |
| 1996 | 23-Jul | 2135 | 9001 | 54 | 269 | 9 | 29 |
| 1996 | 24-Jul | 1930 | 393 | 60 | 265 | 20 | 44 |
| 1996 | 24-Jul | 2055 | 1 | 54 | 258 | 13 | 30 |
| 1996 | 24-Jul | 2055 | 403 | 54 | 253 | 13 | 23 |
| 1996 | 24-Jul | 2100 | 805 | 54 | 194 | 11 | 32 22 |
| 1996 | 1-Aug | 1745 | 1612 | 54 54 | 174 | 13 19 | 34 |
| 1996 | 1-Aug | 1825 | 311 412 | 12 | 264 175 | 12 | 29 |
| 1996 1996 | 1-Aug 3-Aug | 1825 1935 | 3131 | 204 | 248 | 16 | 33 |
| 1996 | 11-Aug | 1730 | 512 | 30 | 224 | 16 | 90 |
| 1996 | 11-Aug | 1735 | 3131 | 12 | 259 | 9 | 23 |
| 1996 | 13-Aug | 1830 | 513 | 30 | 357 | 13 | 27 |
| 1996 | 15-Aug | 2015 | 714 | 54 | 250 | 15 | 43 |
| 1996 | 15-Aug | 2015 | 1204 | 54 | 323 | 15 | 39 |
| 1996 | 15-Aug | 2025 | 61 | 204 | 295 | 22 | 34 |
| 1996 | 15-Aug | 2025 | 1204 | 54 | 69 | 14 | 36 |
| 1996 | 15-Aug | 2030 | 513 | 30 | 164 | 12 | 90 |
| 1996 | 15-Aug | 2035 | 61 | 162 | 265 | 22 | 43 |
| 1996 | 19-Aug | 2250 | 311 | 54 | 106 | 15 | 27 |
| 1996 | 19-Aug | 2300 | 394 | 60 | 66 | 21 | 29 |
| 1996 | 20-Aug | 0915 | 61 | 54 | 85 | 13 | 25 |
| 1996 | 20-Aug | 1630 | 1605 | 54 | 84 | 15 | 35 |
| 1996 | 20-Aug | 2100 | 421 | 54 | 68 | 15 | 29 |
| 1996 | 2-Sep | 1715 | 1204 | 54 | 260 | 9 | 22 |
| 1996 | 2-Sep | 1745 | 311 | 54 | 197 | 11 | 25 |
| 1996 | 2-Sep | 1750 | 418 | 54 | 118 | 12 | 25 |
| 1996 | 2-Sep | 1755 | 397 | 60 | 182 | 16 | 48 |
| 1996 | 2-Sep | 1755 | 398 | 60 | 211 | 18 | 49 |
| 1996 | 6-Sep | 0025 | 394 | 60 | 181 | 20 | 30 |
| 1996 | 7-Sep | 0020 | 3131 | 54 | 263 | 8 | 29 |

| Year | Days | Time | Tower | Height | Direction | Speed | Gust |
|------|--------|------|-------|--------|-----------|-------|------|
| 1996 | 10-Sep | 0710 | 41 | 54 | 321 | 3 | 20 |
| 1996 | 10-Sep | 1245 | 1204 | 54 | 102 | 13 | 43 |
| 1996 | 10-Sep | 1325 | 1204 | 54 | 92 | 11 | 39 |
| 1996 | 11-Sep | 1635 | 394 | 60 | 276 | 14 | 29 |
| 1996 | 11-Sep | 2005 | 1204 | 54 | 236 | 8 | 35 |
| 1996 | 17-Sep | 1725 | 506 | 54 | 248 | 13 | 29 |
| 1996 | 17-Sep | 1840 | 394 | 60 | 221 | 13 | 23 |
| 1996 | 17-Sep | 2340 | 511 | 30 | 279 | 18 | 35 |
| 1996 | 18-Sep | 2050 | 300 | 54 | 310 | 15 | 29 |
| 1997 | 3-May | 1815 | 805 | 54 | 201 | 9 | 26 |
| 1997 | 3-May | 1955 | 61 | 204 | 196 | 21 | 40 |
| 1997 | 3-May | 2010 | 61 | 204 | 200 | 15 | 35 |
| 1997 | 3-May | 2015 | 397 | 60 | 198 | 19 | 36 |
| 1997 | 3-May | 2015 | 3131 | 295 | 194 | 27 | 37 |
| 1997 | 3-May | 2020 | 41 | 54 | 206 | 14 | 35 |
| 1997 | 3-May | 2020 | 1101 | 162 | 230 | 18 | 36 |
| 1997 | 3-May | 2025 | 421 | 54 | 225 | 39 | 64 |
| 1997 | 3-May | 2030 | 22 | 54 | 219 | 25 | 42 |
| 1997 | 28-May | 0105 | 803 | 54 | 19 | 8 | 36 |
| 1997 | 28-May | 0115 | 803 | 54 | 20 | 3 | 30 |
| 1997 | 28-May | 1525 | 3 | 54 | 56 | 22 | 36 |
| 1997 | 31-May | 1900 | 1012 | 54 | 182 | 8 | 25 |
| 1997 | 31-May | 2205 | 3 | 12 | 259 | 11 | 22 |
| 1997 | 31-May | 2205 | 112 | 54 | 223 | 18 | 39 |
| 1997 | 1-Jun | 1750 | 509 | 54 | 215 | 22 | 55 |
| 1997 | 1-Jun | 1755 | 415 | 54 | 268 | 12 | 25 |
| 1997 | 1-Jun | 1805 | 512 | 30 | 233 | 19 | 41 |
| 1997 | 1-Jun | 1825 | 403 | 54 | 264 | 28 | 42 |
| 1997 | 2-Jun | 1520 | 3131 | 12 | 293 | 7 | 20 |
| 1997 | 2-Jun | 2115 | 36 | 90 | 298 | 15 | 29 |
| 1997 | 12-Jun | 1910 | 511 | 30 | 109 | 15 | 29 |
| 1997 | 12-Jun | 2020 | 403 | 12 | 156 | 11 | 22 |
| 1997 | 12-Jun | 2025 | 1 | 54 | 141 | 18 | 34 |
| 1997 | 12-Jun | 2105 | 805 | 54 | 339 | 9 | 27 |
| 1997 | 14-Jun | 1710 | 61 | 54 | 201 | 15 | 36 |
| 1997 | 14-Jun | 1710 | 108 | 12 | 199 | 6 | 25 |
| 1997 | 14-Jun | 1730 | 61 | 204 | 230 | 21 | 39 |
| 1997 | 14-Jun | 1745 | 513 | 30 | 221 | 20 | 42 |
| 1997 | 17-Jun | 1745 | 61 | 162 | 294 | 28 | 48 |
| 1997 | 19-Jun | 2015 | 512 | 30 | 34 | 15 | 27 |
| 1997 | 19-Jun | 2025 | 394 | 60 | 7 | 21 | 43 |
| 1997 | 19-Jun | 2045 | 412 | 54 | 130 | 15 | 39 |
| 1997 | 19-Jun | 2100 | 1000 | 54 | 33 | 18 | 28 |
| 1997 | 19-Jun | 2110 | 3 | 54 | 332 | 22 | 48 |
| 1997 | 24-Jun | 1730 | 2016 | 54 | 43 | 11 | 22 |
| 1997 | 27-Jun | 1715 | 393 | 60 | 258 | 11 | 23 |

| Year | Day | Time | Tower | Height | Direction | Speed | Gust |
|--------------|------------------|--------------|--------------|----------|------------|----------|----------|
| 1997 | 29-Jun | 2030 | 421 | 54 | 227 | 14 | 27 |
| 1997 | 1-Jul | 0035 | 108 | 54 | 268 | 12 | 36 |
| 1997 | 1-Jul | 2130 | 412 | 54 | 213 | 11 | 33 |
| 1997 | 1-Jul | 2130 | 511 | 30 | 110 | 11 | 32 |
| 1997 | 5-Jul | 1925 | 714 | 54 | 135 | 15 | 28 |
| 1997 | 5-Jul | 1935 | 1012 | 54 | 195 | 12 | 30 |
| 1997 | 9-Jul | 2110 | 805 | 54 | 328 | 15 | 39 |
| 1997 | 19-Jul | 2045 | 300 | 54 | 288 | 20 | 36 |
| 1997 | 26-Jul | 1835 | 1612 | 54 | 283 | 9 | 34 |
| 1997 | 26-Jul | 1900 | 1012 | 54 | 274 | 16 | 49 |
| 1997 | 26-Jul | 1925 | 714 | 54 | 322 | 11 | 46 |
| 1997 | 27-Jul | 2020 | 393 | 60 | 317 | 23 | 37 |
| 1997 | 29-Jul | 2130 | 421 | 54 | 154 | 22 | 43 |
| 1997 | 3-Aug | 2105 | 41 | 54 | 239 | 19 | 36 |
| 1997 | 4-Aug | 1905 | 393 | 60 | 281 | 22 | 48 |
| 1997 | 6-Aug | 2225 | 819 | 54 | 309 | 8 | 20 |
| 1997 | 10-Aug | 2005 | 19 | 54 | 298 | 34 | 50 |
| 1997 | 10-Aug | 2005 | 805 | 12 | 315 | 5 | 28 |
| 1997 | 10-Aug | 2025 | 509 | 54 | 188 | 18 | 33 |
| 1997 | 10-Aug | 2125 | 61 | 162 | 273 | 15 | 34 |
| 1997 | 19-Aug | 1805 | 1101 | 162 | 115 | 22 | 43 |
| 1997 | 19-Aug | 1810 | 112 | 12 | 53 | 4 | 20 |
| 1997 | 19-Aug | 1825 | 1500 | 54 | 247 | 8 | 25 |
| 1997 | 19-Aug | 1835 | 311 | 12 | 209 | 7 | 20 |
| 1997 | 20-Aug | 2150 | 513 | 30 | 326 | 23 | 43 |
| 1997 | 20-Aug | 2155 | 3131 | 295 | 299 | 23 | 42 |
| 1997 | 23-Aug | 2040 | 803 | 54 | 45 | 6 | 29 |
| 1997 | 1-Sep | 1040 | 3 | 54 | 68 | 18 | 28 |
| 1997 | 1-Sep | 1105 | 393 | 60 | 121 | 22 | 34 |
| 1997 | 1-Sep | 1320 | 3 | 54 | 75 | 23 | 32 |
| 1997 | 1-Sep | 1530 | 803 | 54 | 71 | 6 | 26 |
| 1997 | 3-Sep | 2005 | 3131 | 162 | 289 | 13 | 29 |
| 1997 | 23-Sep | 0750 | 506 | 54 | 212 | 15 | 36 |
| 1997 | 25-Sep | 2025 | 1000 | 54 | 244 | 16 | 34 |
| 1997 | 26-Sep | 1755 | 1612 | 54 | 205 | 12 | 27 |
| 1997 | 26-Sep | 1820 | 803 | 54 | 220 | 16 | 29 |
| 1997 | 26-Sep | 1835 | 61 | 204 | 194 | 18 | 36 |
| 1997 | 26-Sep | 1840 | 3131 | 12 | 173 | 9 | 28 |
| 1997 | 26-Sep | 1845 | 397 | 60 | 215 | 18 | 34 |
| 1998 | 4-May | 1900 | 112 | 54 | 293 | 14 | 32 41 |
| 1998 1998 | 4-May | 1950 1745 | 1000 1007 | 54 54 | 283 213 | 19 16 | 53 |
| 1998 | 5-May | 1925 | 9001 | 54 | 336 | 18 | 47 |
| 1998 | 7-Jun 21-Jun | 0105 | 418 | 54 | 227 | 22 | 43 |
| 1998 | 21-Jun 21-Jun | 2130 | 300 | 54 | 309 | 19 | 35 |
| 1998 | 21-Jun 21-Jun | 2140 | 300 | 54 | 337 | 11 | 39 |
| 1990 | Z I-Juli | 2140 | 1 300 | 1 34 | 331 | 11 | 1 38 |

| Year | Day | Time | Tower | Height | Direction | Speed | Gust |
|--------------|------------------|--------------|-------------|-----------|-----------|----------|----------|
| 1998 | 26-Jun | 1830 | 1101 | 54 | 238 | 22 | 39 |
| 1998 | 26-Jun | 1845 | 41 | 54 | 201 | 13 | 34 |
| 1998 | 6-Jul | 1925 | 1612 | 54 | 75 | 32 | 55 |
| 1998 | 6-Jul | 2005 | 1612 | 54 | 248 | 11 | 30 |
| 1998 | 7-Jul | 1640 | 1007 | 54 | 231 | 16 | 29 |
| 1998 | 11-Jul | 1825 | 300 | 54 | 292 | 14 | 26 |
| 1998 | 18-Jul | 2215 | 511 | 30 | 248 | 18 | 33 |
| 1998 | 18-Jul | 2215 | 512 | 30 | 224 | 28 | 44 |
| 1998 | 18-Jul | 2215 | 513 | 30 | 192 | 25 | 43 |
| 1998 | 18-Jul | 2250 | 819 | 54 | 225 | 13 | 36 |
| 1998 | 26-Jul | 1930 | 819 | 54 | 221 | 12 | 29 |
| 1998 | 28-Jul | 0220 | 1000 | 54 | 203 | 3 | 26 |
| 1998 | 28-Jul | 0230 | 303 | 54 | 208 | 13 | 35 |
| 1998 | 28-Jul | 0300 | 108 | 54 | 311 | 18 | 43 |
| 1998 | 28-Jul | 0300 | 112 | 12 | 177 | 13 | 27 |
| 1998 | 28-Jul | 0300 | 1101 | 162 | 188 | 36 | 57 |
| 1998 | 28-Jul | 2105 | 421 | 54 | 8 | 16 | 29 |
| 1998 | 28-Jul | 2120 | 421 | 54 | 340 | 18 | 34 |
| 1998 | 28-Jul | 2135 | 418 | 54 | 308 | 18 | 39 |
| 1998 | 28-Jul | 2145 | 714 | 12 | 21 | 11 | 32 |
| 1998 | 28-Jul | 2150 | 112 | 54 | 353 | 11 | 33 35 |
| 1998 | 28-Jul | 2150 | 398 | 60 204 | 336 14 | 20 16 | 36 |
| 1998 1998 | 28-Jul 28-Jul | 2150 2200 | 1101 397 | 60 | 316 | 26 | 51 |
| 1998 | 28-Jul | 2200 | 398 | 60 | 307 | 15 | 41 |
| 1998 | 28-Jul | 2200 | 513 | 30 | 189 | 5 | 36 |
| 1998 | 28-Jul | 2200 | 3131 | 295 | 354 | 29 | 44 |
| 1998 | 28-Jul | 2225 | 1007 | 54 | 274 | 13 | 47 |
| 1998 | 29-Jul | 1745 | 311 | 54 | 32 | 9 | 26 |
| 1998 | 5-Aug | 1855 | 1000 | 54 | 7 | 21 | 42 |
| 1998 | 6-Aug | 1750 | 805 | 54 | 135 | 15 | 32 |
| 1998 | 10-Aug | 1935 | 714 | 54 | 259 | 8 | 28 |
| 1998 | 13-Aug | 1955 | 421 | 54 | 7 | 22 | 41 |
| 1998 | 13-Aug | 2015 | 714 | 54 | 13 | 21 | 40 |
| 1998 | 13-Aug | 2045 | 3131 | 204 | 351 | 30 | 43 |
| 1998 | 14-Aug | 1900 | 819 | 54 | 137 | 18 | 43 |
| 1998 | 14-Aug | 1955 | 61 | 204 | 288 | 25 | 36 |
| 1998 | 14-Aug | 2020 | 1000 | 54 | 73 | 16 | 32 |
| 1998 | 17-Aug | 1645 | 311 | 54 | 114 | 12 | 26 |
| 1998 | 21-Aug | 0615 | 3131 | 204 | 129 | 22 | 36 |
| 1998 | 22-Aug | 0220 | 311 | 54 | 137 | 14 | 34 |
| 1998 | 22-Aug | 0220 | 397 | 60 | 144 | 22 | 37 |
| 1998 | 22-Aug | 0220 | 398 | 60 | 139 | 26 | 40 |
| 1998 | 31-Aug | 1805 | 1007 | 54 | 13 | 21 | 39 |
| 1998 | 31-Aug | 1815 | 714 | 54 | 251 | 18 | 35 |
| 1998 | 3-Sep | 0030 | 300 | 54 | 135 | 15 | 30 |

| Year | Day | Time | Tower | Height | Direction | Speed | Gust |
|------|--------|------|-------|--------|-----------|-------|------|
| 1998 | 3-Sep | 1815 | 9001 | 54 | 238 | 14 | 39 |
| 1998 | 3-Sep | 1825 | 803 | 12 | 234 | 9 | 28 |
| 1998 | 3-Sep | 1830 | 403 | 54 | 244 | 18 | 40 |
| 1998 | 3-Sep | 1835 | 108 | 54 | 245 | 27 | 43 |
| 1998 | 3-Sep | 1900 | 421 | 54 | 214 | 27 | 46 |
| 1998 | 7-Sep | 2145 | 513 | 30 | 169 | 19 | 33 |
| 1998 | 24-Sep | 1230 | 311 | 54 | 67 | 18 | 29 |
| 1998 | 25-Sep | 2055 | 3 | 54 | 162 | 25 | 34 |

Appendix B: Sample WINDS Data

| DAY | TIME | IDN | Z | DIR | SPD | GUS | DDEV | ${f T}$ | TD | RH |
|-------|------|-----|-----------|------|--------|-----|------|----------|----|-----|
| 94121 | | 1 | - 6 | | | | | 76 | | |
| 94121 | 0 | 1 | | 113 | 6 | 9 | 16 | | | |
| 94121 | 0 | 1 | 54 | 123 | 12 | 13 | 7 | 76 | | |
| 94121 | | 3 | 6 | 123 | | | , | 78 | | |
| 94121 | | 3 | 12 | 99 | 11 | 13 | 6 | , 0 | | |
| 94121 | | | 54 | 108 | 13 | 13 | 7 | 77 | | |
| 94121 | | | 6 | 100 | 13 | 13 | , | , , | | |
| 94121 | | 6 | 12 | | | | | | | |
| | | | 54 | | | | | | | |
| 94121 | | | | | | | | | | |
| 94121 | | | 162 | | | | | | | |
| 94121 | | | 204 6 | | | | | 75 | | |
| 94121 | | | | 100 | 2 | - | ٦٣ | 75 | | |
| 94121 | | | 12 | 100 | 3 | 7 | 25 | 72 | | |
| 94121 | | | 54 | 111 | 8 | 11 | 11 | 73 | 70 | 70 |
| 94121 | | | 6 | 105 | _ | 7 | 7.7 | 76 | 70 | 79 |
| 94121 | | | 12 | 105 | 5 | 7 | 11 | 7.6 | 60 | 70 |
| 94121 | | | | 111 | 8 | 9 | 9 | 76 | 69 | 79 |
| 94121 | | | | 101 | 10 | 11 | 6 | П.С | 60 | 7.0 |
| 94121 | | | | 103 | 11 | 12 | 5 | 76 | 69 | 78 |
| 94121 | | | 6 | 7.04 | | | 1.5 | 77 | | |
| 94121 | | | | 104 | 4 | 8 | 15 | | | |
| 94121 | | | 54 | 102 | 8 | 10 | 9 | 77 | | |
| 94121 | | | 6 | | | | | 76 | | |
| 94121 | | | | 108 | 3 | 4 | 20 | prq pr- | | |
| 94121 | | | | 113 | 6 | 9 | 13 | 75 | | |
| 94121 | | | 6 | | _ | _ | | 76 | | |
| 94121 | | | | 119 | 5 | 8 | 16 | | | |
| 94121 | | | | 105 | 8 | 10 | 11 | 74 | | |
| 94121 | | | 6 | | | _ | | 76 | 64 | 68 |
| 94121 | | | 12 | 127 | 5 | 8 | 11 | | | |
| 94121 | | | 54 | 108 | 7 | 10 | 10 | 77 | 66 | 71 |
| 94121 | | | 162 | 115 | 11 | 13 | 6 | | | =- |
| 94121 | | | | 115 | 12 | 13 | 7 | 76 | 66 | 73 |
| 94121 | | | 295 | 120 | 13 | 14 | 7 | | | |
| 94121 | | | 394 | 112 | 13 | 14 | 7 | -7 F | | 7.0 |
| 94121 | | | 492 6 | 109 | 14 | 14 | 6 | 75 | 66 | 73 |
| 94121 | | | | 124 | _ | 7 | 12 | 76 | | |
| 94121 | | | | 134 | 5 | | 13 | 77.6 | | |
| 94121 | | | 54 6 | 123 | 6 | 10 | 11 | 76 | | |
| 94121 | | | | 300 | _ | 7 | 7.4 | 76 | | |
| 94121 | | | 12 | 106 | 5 | 7 | 14 | 7- | | |
| 94121 | | | 54 | 98 | 8 | 11 | 10 | 75 74 | | |
| 94121 | | | 6 | 104 | 2 | _ | 10 | 74 | | |
| 94121 | | | 12 | 124 | 3 6 | 5 | 17 | 75 | | |
| 94121 | | | 54 | 99 | ь | 8 | 10 | 75 76 | | |
| 94121 | | | 6 | 100 | A | _ | 3.4 | 76 | | |
| 94121 | | | | 106 | 4 | 6 | 14 | | | |
| 94121 | | | 54 | 107 | 8 | 10 | 11 | 76 | | |
| 94121 | | | 6 | 102 | 3 | | 10 | 74 | | |
| 94121 | | | | 103 | 3 | 4 | 18 | | | |
| 94121 | 0 | 509 | 54 | 105 | 5 | 6 | 9 | 74 | | |

Appendix C: Sample Upper-Air Sounding in Decoded Format

```
15 4 5 1998 1013 5 25.8 16.8 210 8
15 4 5 1998 1011 22 24.6 17.6 999 999
15 4 5 1998 1000 123 24.2 18.2 215 13
15 4 5 1998 992 193 23.8 18.8 999 999
15 4 5 1998 979.4 304 999 999 210 16
15 4 5 1998 969 396 22 18.1 999 999
15 4 5 1998 948 584 20.4 16.8 999 999
15 4 5 1998 945.2 609 999 999 210 18
15 4 5 1998 933 721 20.8 10.8 999 999
15 4 5 1998 926 786 21.4 3.4 999 999
15 4 5 1998 925 796 999 999 999 999
15 4 5 1998 913 907 20.6 8.6 999 999
15 4 5 1998 912.3 914 999 999 205 22
15 4 5 1998 880.7 1219 999 999 205 22
15 4 5 1998 850.2 1524 999 999 205 22
15 4 5 1998 850 1526 14.8 4.8 210 22
15 4 5 1998 837 1655 13.8 3.8 999 999
15 4 5 1998 819.8 1828 999 999 210 20
15 4 5 1998 790.3 2133 999 999 210 18
15 4 5 1998 785 2189 10.6 -4.4 999 999
15 4 5 1998 770 2349 9.8 -3.2 999 999
15 4 5 1998 761.7 2438 999 999 215 18
15 4 5 1998 733.8 2743 999 999 220 21
15 4 5 1998 710 3013 4.6 -5.4 999 999
15 4 5 1998 700 3138 3.8 -6.2 225 22
15 4 5 1998 655.9 3657 999 999 240 22
15 4 5 1998 632 3954 -3.5 -6.8 999 999
15 4 5 1998 612 4207 -4.5 -6.7 999 999
15 4 5 1998 607.3 4267 999 999 260 24
15 4 5 1998 603 4323 -4.9 -8.7 999 999
15 4 5 1998 590 4493 -6.3 -10.3 999 999
15 4 5 1998 561.5 4876 999 999 260 26
15 4 5 1998 550 5036 -10.7 -15.7 999 999
15 4 5 1998 524 5405 -14.1 -16.5 999 999
15 4 5 1998 518.6 5486 999 999 255 28
15 4 5 1998 500 5770 -16.1 -17.5 250 28
15 4 5 1998 490 5921 -17.5 -18.3 999 999
15 4 5 1998 478.6 6096 999 999 245 29
15 4 5 1998 463 6342 -19.9 -21.3 999 999
15 4 5 1998 453 6503 -21.1 -23 999 999
15 4 5 1998 442 6684 -22.1 -27.1 999 999
15 4 5 1998 430 6885 -23.7 -31.7 999 999
15 4 5 1998 419 7073 -25.3 -36.3 999 999
15 4 5 1998 400 7410 -28.1 -38.1 265 34
```

Appendix D: IDL Program for Data Interpolation, and Computing MDPI and WINDEX

pro parameters10m, fn

```
; This program will interpolate missing temp and dp data from upper-air soundings and
 ; compute MDPI, WINDEX and associated parameters. Data is read-in in the format:
 ;Time,Day,Month, Year,Press,Height,Temp,Dewpoint,Direction,Speed. All parameters
 ; are saved to an output file.
 ; Written By: Steven Dickerson
 ; Last updated: 2 Dec 1999
 ; Count the number of lines in the sounding
n = 0
s = ''
close, 5
openr, 5, fn
while not (eof(5)) do begin
readf, 5, s
if (strlen(s) GT 5) then n = n+1
endwhile
point lun, 5, 0
  ; Now read in the sounding data
data = fltarr(10,n)
readf, 5, data
close, 5
  ;*******This identifies the variable associated with each column of the array******
time = data[0,*]
day = data[1,*]
month = data[2,*]
year = data[3,*]
pres = data[4,*]
hgt = data[5,*]
temp = data[6,*]
dp = data[7,*]
dir = data[8,*]
spd = data[9,*]
;rh = data[10,*]
```

; This identifies where the missing values of temp are

```
blanks = Where(strpos(temp, '999.0') GE 0, bc)
nonblank = Where(strpos(temp, '999.0') LT 0, nbc)
for i = 0L, bc-1 do begin
 ; find obs before 999.0 with number
before = max(where(nonblank LT blanks(i)))
after = min(where(nonblank GT blanks(i)))
temp(blanks(i)) = temp(nonblank(before)) + ((temp(nonblank(after))-
temp(nonblank(before))) * ( (hgt[blanks(i)] -
hgt[nonblank(before)])/(hgt[nonblank(after)]-hgt[nonblank(before)])))
;weight=( (hgt[blanks(i)] - hgt[nonblank(before)])/(hgt[nonblank(after)]-
hgt[nonblank(before)]) )
;print,weight
endfor
; This identifies where the missing values of DP are
blank = Where(strpos(dp, '999.0') GE 0, bc)
nonblanks = Where(strpos(dp, '999.0') LT 0, nbc)
for i = 0L, bc-1 do begin
  ; find obs before 999.0 with number
before = max(where(nonblanks LT blank(i)))
after = min(where(nonblanks GT blank(i)))
dp(blank(i)) = dp(nonblanks(before)) + ((dp(nonblanks(after))-dp(nonblanks(before))) *
((hgt[blank(i)] - hgt[nonblanks(before)])/(hgt[nonblanks(after)]-hgt[nonblanks(before)])
))
endfor
; ******* This section builds a Theta-E profile of the Atms ************
for i = 0, n-1 do begin
       ; compute the temperature at the Lifted Condensation Level
```

```
TLCL = dp(0) - (0.212 + .001571 * dp(0) - .000436 * temp(0)) * (temp(0) - dp(0)) + 273.16
                 ; compute the mixing ratio
e = 6.112*exp((17.67*dp)/(dp+243.5))
r = .622*((e)/(pres-e))
    ; Now compute thetaE
k = .2854
thetaE = (temp+273.16)*((1000.0/pres)^(k*(1.0-(.28*r))))*exp(((3376/TLCL)-(.28*r))))*exp(((.3376/TLCL)-(.28*r))))*exp(((.3376/TLCL)-(.28*r))))*exp(((.3376/TLCL)-(.28*r))))*exp(((.3376/TLCL)-(.28*r))))*exp(((.3376/TLCL)-(.28*r))))*exp(((.3376/TLCL)-(.28*r))))*exp(((.3376/TLCL)-(.28*r))))*exp(((.3376/TLCL)-(.28*r))))*exp(((.3376/TLCL)-(.28*r))))*exp(((.3376/TLCL)-(.28*r))))*exp(((.3376/TLCL)-(.28*r))))*exp(((.3376/TLCL)-(.28*r))))*exp(((.3376/TLCL)-(.28*r))))*exp(((.3376/TLCL)-(.28*r))))*exp(((.3376/TLCL)-(.28*r))))*exp(((.3376/TLCL)-(.28*r))))*exp(((.3376/TLCL)-(.28*r))))*exp(((.3376/TLCL)-(.28*r))))*exp(((.3376/TLCL)-(.28*r))))*exp(((.3376/TLCL)-(.28*r))))*exp(((.3376/TLCL)-(.28*r))))*exp(((.3376/TLCL)-(.28*r))))*exp(((.3376/TLCL)-(.28*r))))*exp(((.3376/TLCL)-(.28*r))))*exp(((.3376/TLCL)-(.28*r)))*exp(((.3376/TLCL)-(.28*r))))*exp(((.3376/TLCL)-(.28*r))))*exp(((.3376/TLCL)-(.28*r))))*exp(((.3376/TLCL)-(.28*r))))*exp(((.3376/TLCL)-(.28*r))))*exp(((.3376/TLCL)-(.28*r))))*exp(((.3376/TLCL)-(.28*r))))*exp(((.3376/TLCL)-(.28*r))))*exp(((.3376/TLCL)-(.28*r))))*exp(((.3376/TLCL)-(.28*r))))*exp(((.3376/TLCL)-(.28*r))))*exp(((.3376/TLCL)-(.28*r))))*exp(((.3376/TLCL)-(.28*r))))*exp(((.3376/TLCL)-(.28*r))))*exp(((.3376/TLCL)-(.28*r))))*exp(((.3376/TLCL)-(.28*r))))*exp((.3376/TLCL)-(.28*r)))*exp((.3376/TLCL)-(.28*r)))*exp((.3376/TLCL)-(.28*r)))*exp((.3376/TLCL)-(.28*r)))*exp((.3376/TLCL)-(.28*r)))*exp((.3376/TLCL)-(.28*r)))*exp((.3376/TLCL)-(.28*r)))*exp((.3376/TLCL)-(.28*r)))*exp((.3376/TLCL)-(.28*r)))*exp((.3376/TLCL)-(.28*r)))*exp((.3376/TLCL)-(.28*r))*exp((.3376/TLCL)-(.28*r)))*exp((.3376/TLCL)-(.28*r)))*exp((.3376/TLCL)-(.28*r))*exp((.3376/TLCL)-(.28*r))*exp((.3376/TLCL)-(.28*r))*exp((.3376/TLCL)-(.28*r))*exp((.3376/TLCL)-(.28*r))*exp((.3376/TLCL)-(.28*r))*exp((.3376/TLCL)-(.28*r))*exp((.3376/TLCL)-(.28*r))*exp((.3376/TLCL)-(.28*r))*exp((.3376/TLCL)-(.28*r))*exp((.3376/TLCL)-(.28*r))*exp((.28*r))*exp((.28*r))*exp((.28*r))*exp((.28*r))*exp((.28*r))*exp((.28*r))*exp((.28*r))*exp((.28*r))*exp((.28*r))*exp((.28*r))*exp((
2.54)*r*(1+(.81*r)))
endfor
; ******* This section computes the delta-ThetaE needed for MDPI *******
position lowest 150mb = where(pres GE (max(pres)-150))
lowPres = pres(position lowest 150mb)
maxThetaE = max(thetaE(position lowest 150mb))
maxPres = lowPres(where(max(thetaE(position lowest 150mb))))
;deltaThetaE=maxThetaE-min(thetaE)
 ;position minPres = where(thetaE EQ min(thetaE))
 ;minPres = pres(position minPres)
position minPres = where(pres GE 500 and pres LE 650)
midlevel Pres = pres(position_minPres)
midlevel thetaE = thetaE(position minPres)
                                                                                                                                             ;*Compute using min at mid*
minThetaE = min(midlevel thetaE)
minPres = pres(where(thetaE EQ min(midlevel thetaE)))
deltaThetaE = maxThetaE - minThetaE
min P Total = pres(where(thetaE EQ min(thetaE)))
min TH Total = min(thetaE)
 delta Total = maxThetaE - min TH Total
 Pres850=where(pres EQ 850)
 Pres500=where(pres EQ 500)
```

```
if ((min(Pres850)) AND (min(Pres500)) GT 0) then begin; min statements needed to
change from array to scalar
VT = temp(where(pres EQ 850)) - temp(where(pres EQ 500))
endif else begin
VT = 9999; if 850 or 500 mb level is missing 9999 is reported at VT
endelse
: ****** This section computes the WINDEX parameters **********
********* Find the Height of the Melting Level (Hm) in kilometers *******
position below zero = where(temp LE 0)
hgt below zero = hgt(position below zero)
Hm = hgt below zero(0)/1000
;******* Find the Mixing Ratio at the Melting Level (Qm) in g/kg ********
pres below zero = pres(position below zero)
pres ML = pres below zero(0)
dp below zero = dp(position below zero)
dp ML = dp below zero(0)
vaporpress = 6.112*exp((17.67*dp ML)/(dp ML+243.5))
Qm = (.622*((vaporpress)/(pres ML-vaporpress)))*1000
;*** Find the Mean Mixing Ratio in the lowest 1km of the Atmosphere (QL) in g/kg ***
position lowest 1km = where(hgt LE 1000)
dp lowest 1km = dp(position lowest <math>1km)
pres lowest 1km = pres(position lowest 1km)
for i=0, n-1 do begin
vaporpress = 6.112*exp((17.67*dp lowest 1km)/(dp lowest 1km+243.5))
mixingratio = (.622*((vaporpress)/(pres_lowest_1km-vaporpress)))*1000.0
number = n elements(mixing ratio)
```

```
QL = (mixingratio(0) + mixingratio(number-1))/2
endfor
Rq = QL/12
if (Rq GT 1) then Rq=1.0
:**** Now find the Mean Environmental Lapse Rate (gamma) in degrees C per 1km
*****
temp LT zero=temp(position below zero)
gamma = ((temp(0)-temp_LT_zero(0))/Hm)
WI = 5*(Hm*Rq*(gamma^2 - 30 + QL - 2*Qm))^.5
new_array = [time, day, month, year, pres, thetaE, hgt, temp, dp]
output = [maxPres, maxThetaE, minPres, minThetaE, min P Total, min TH Total,
deltaThetaE, delta_Total, VT, Hm, Qm, QL, Rq, gamma, WI]
print, output
openu, outfile, "parameters-micro-new.txt", /get lun, /append
printf, outfile, fn
close, outfile
free lun, outfile
openu, outfile, "parameters-micro-new.txt", /get lun, /append, width = 300
printf, outfile, output
close, outfile
free lun, outfile
end
```

Appendix E: MDPI and WINDEX Parameters

Legend

YR -- Year

MO -- Month

DY -- Day

<u>OCR</u> -- Occurrence or non-occurrence of microburst. A 1 indicates that this day is a microburst producing thunderstorm day; a 0 indicates that this is a non-microburst producing thunderstorm day

<u>MaxPr</u> -- The pressure level (mb) corresponding to the maximum θ_e recorded in the lowest 150 mb of the sounding

<u>MaxThetE</u> -- The maximum θ_e (K) recorded in the lowest 150 mb of the sounding

 $\underline{\text{MinPr}}$ -- The pressure level (mb) corresponding to the minimum θ_e found between 650 and 500 mb

MinThetaE -- The minimum θ_e (K) found between 650 and 500 mb

<u>MinPActu</u> -- The pressure level (mb) corresponding to the minimum θ_e found at any level in the sounding

MinTActu -- The minimum θ_e (K) found at any level in the sounding

MDPI -- MaxThetE - MinThetaE

DeltaActua -- MaxThetE - MinTActu

Hm -- The height of the melting level (km)

Qm -- The mixing ratio at the height of the melting level (g kg⁻¹)

Ql -- The mixing ratio in the lowest 1 km of the atmosphere (g kg⁻¹)

gamma -- The environmental lapse (°C km⁻¹) rate from the surface to the height of the melting level

WI -- The computed WINDEX value

| | | | - 1 | - | - | | | | | | - 1 | | _ | _ | | | | , | | | | | | | | - 1 | - | | | | 1 | 1 | _ |
|------------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|-----|
| WI | 57.006 | 49.799 | 61.831 | 50.436 | 41.699 | 53.66 | 52.956 | 39.872 | 27.356 | 35.555 | 45.052 | 44.274 | 50.771 | 51.276 | 37.152 | 55.022 | 55.954 | 57.211 | 52.544 | 44.54 | 62.085 | 53.349 | 45.779 | 46.087 | 21.799 | 53.844 | 41.56 | 35.524 | 53.045 | 56.48 | 54.596 | 54.596 | |
| gamma | 6.3386 | 6.3348 | 6.6765 | 6.5756 | 5.6657 | 6.7948 | 7.1029 | 6.1868 | 5.3575 | 6.1672 | 6.5488 | 6.5641 | 6.4382 | 6.8584 | 5.6729 | 6.7974 | 7.5815 | 6.7463 | 6.5894 | 6.3668 | 6.6225 | 7.032 | 5.8162 | 6.3919 | 5.4496 | 6.8435 | 6.246 | 5.9499 | 6.2606 | 6.6779 | 6.2059 | 6.2059 | |
| Ö | 16.126 | 13.803 | 18.101 | 15.19 | 14.997 | 14.119 | 14.219 | 14.674 | 16.132 | 14.505 | 16.955 | 16.515 | 19.176 | 15.849 | 17.544 | 15.408 | 15.403 | 16.468 | 15.979 | 13.704 | 14.004 | 16.003 | 16.583 | 14.4 | 16.492 | 18.464 | 18.029 | 15.748 | 17.615 | 17.392 | 18.088 | 18.088 | 1 : |
| Qm | 1.0349 | 1.7927 | 0.6539 | 2.2909 | 1.5119 | 1.6508 | 4.1909 | 4.953 | 4.347 | 5.4944 | 6.0593 | 5.9272 | 4.6067 | 4.8095 | 4.4631 | 2.5625 | 5.6164 | 2.5623 | 2.1529 | 3.9716 | 0.8405 | 3.9233 | 1.6079 | 3.2654 | 5.9372 | 5.2481 | 6.0802 | 5.3967 | 3.8831 | 2.0381 | 0.5431 | 0.5431 | |
| F | 5.364 | 4.875 | 4.875 | 4.267 | 4.942 | 4.268 | 4.267 | 4.875 | 4.875 | 4.378 | 4.581 | 4.418 | 4.815 | 4.52 | 5.112 | 4.572 | 3.957 | 4.875 | 4.401 | 4.869 | 5.889 | 4.124 | 4.875 | 4.537 | 4.404 | 4.676 | 4.643 | 4.874 | 5.91 | 4.572 | 4.673 | 4.673 | |
| DeltaActua | 36.8599 | 26.5071 | 44.8315 | 31.9383 | 31.4046 | 27.6133 | 29.8398 | 19.9941 | 23.637 | 26.2678 | 42.0995 | 32.9438 | 43.6061 | 38.441 | 27.2448 | 30.6852 | 44.6765 | 35.6141 | 35.8369 | 30.383 | 31.5515 | 29.7585 | 29.3167 | 29.476 | 25.5138 | 34.9978 | 30.4794 | 20.8067 | 34.4821 | 40.1619 | 40.3701 | 40.3701 | |
| MDPI | 35.255 | 26.507 | 38.081 | 30.776 | 25.235 | 24.612 | 28.161 | 16.236 | 20.809 | 26.268 | 42.1 | 32.697 | 43.606 | 36.901 | 25.53 | 30.685 | 37.242 | 35.614 | 35.837 | 24.085 | 31.552 | 29.394 | 29.236 | 29.476 | 23.787 | 34.998 | 30.479 | 19.033 | 29.394 | 40.162 | 40.37 | 40.37 | |
| MinTActu | 317.631 | 322.318 | 314.459 | 319.631 | 316.765 | 315.823 | 318.583 | 329.035 | 328.681 | 321.205 | 323.317 | 321.191 | 325.287 | 322.886 | 330.213 | 324.559 | 312.272 | 323.84 | 321.714 | 320.721 | 317.651 | 323.036 | 323.078 | 323.501 | 326.232 | 328.508 | 329.088 | 332.729 | 330.509 | 320.829 | 319.847 | 319.847 | |
| MinPActu | 723 | 614 | 706 | 700 | 804 | 676 | 269 | 466 | 999 | 545 | 561 | 705 | 900 | 741 | 703 | 614 | 721 | 627 | 603 | 852 | 649 | 899 | 491 | 517 | 477 | 628 | 530 | 700 | 700 | 615 | 585 | 585 | |
| MinThetaE | 319.236 | 322.318 | 321.21 | 320.793 | 322.935 | 318.824 | 320.262 | 332.793 | 331.509 | 321.205 | 323.317 | 321.439 | 325.287 | 324.426 | 331.928 | 324.559 | 319.706 | 323.84 | 321.714 | 327.019 | 317.651 | 323.4 | 323.158 | 323.501 | 327.958 | 328.508 | 329.088 | 334,503 | 335.598 | 320.829 | 319.847 | 319.847 | |
| MinPr | 641 | 614 | 567 | 611 | 615 | 613 | 650 | 610 | 615 | 545 | 561 | 522 | 500 | 635 | 909 | 614 | 586 | 627 | 603 | 500 | 649 | 637 | 588 | 517 | 546 | 628 | 530 | 649 | 500 | 615 | 585 | 585 | |
| MaxThetE | 354.491 | 348.825 | 359.291 | 351.57 | 348.17 | 343.436 | 348.423 | 349.029 | 352.317 | 347.473 | 365.417 | 354.135 | 368.893 | 361.327 | 357.457 | 355.244 | 356.948 | 359.455 | 357.551 | 351.104 | 349.203 | 352.794 | 352.395 | 352.977 | 351.745 | 363.506 | 359.568 | 353.536 | 364.991 | 360.991 | 360.217 | 360.217 | |
| MaxPr | 1014 | 1012 | 1013 | 1017 | 1019 | 1020 | 1017 | 1013 | 1016 | 1014 | 1013 | 1016 | 1017 | 1015 | 1009 | 1017 | 1016 | 1012 | 1015 | 1020 | 1016 | 1017 | 1015 | 1018 | 1014 | 1017 | 1018 | 1018 | 1016 | 1017 | 1018 | 1018 | |
| OCR | - | 0 | 0 | 1 | 0 | 0 | Ļ | 0 | 0 | 0 | - | - | 0 | 0 | - | - | 0 | - | 0 | 0 | 0 | 0 | 0 | 0 | - | - | 0 | 0 | _ | - | - | 0 | |
| δ | = | 12 | 19 | 23 | 28 | 17 | 8 | 21 | 73 | 24 | 25 | 78 | 78 | R | 2 | 2 | 7 | 12 | - | ٥ | | Ξ | 12 | 7 | 1, | 24 | 25 | 26 | 27 | 78 | 8 | 8 | 1 |
| Ø | 2 | 2 | 2 | 2 | 2 | ဖ | ဖ | ဖ | ۵ | ٥ | 9 | ٥ | ဖ | 9 | 9 | ۵ | 9 | ဖ | ~ | ~ | ~ | <u></u> | r~ | r~ | <u></u> | <u></u> | | r~ | ~ | r~ | ۲- | ~ | |
| ΥR | 95 | 95 | 95 | 95 | 95 | 95 | 95 | 95 | 95 | 98 | 95 | 98 | 95 | 98 | 95 | 95 | 95 | 95 | 95 | 95 | 98 | 95 | 95 | 98 | 98 | 95 | 95 | 95 | 95 | 95 | 95 | 95 | |

| | | | | | | | 1 | | _ | | | | | | | | | | | | | | | | | | | 1 | - | | 1 | | |
|-------------|---------|---------|---------|---------|---------|----------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|
| IW | 31.3 | 36.695 | 43.273 | 44.411 | 45.707 | 51.428 | 40.907 | 54.12 | 53.542 | 51.546 | 45.557 | 43.969 | 45.089 | 51.072 | 51.207 | 48.863 | 45.479 | 46.502 | 55.061 | 48.56 | 49.699 | 42.4 | 47.946 | 43.159 | 57.267 | 53.876 | 50.803 | 54.815 | 41.407 | 48.544 | 38.616 | 53.969 | 45.999 |
| gamma | 5.5844 | 5.9548 | 5.7874 | 5.6854 | 6.135 | 5.9093 | 6.1233 | 5.9161 | 6.3762 | 6.4848 | 6.2161 | 6.4772 | 6.4164 | 7.0226 | 6.3826 | 6.5303 | 6.3244 | 6.5522 | 6.3063 | 6.1621 | 6.3231 | 6.0922 | 5.9325 | 6.3277 | 6.4803 | 6.4839 | 6.2744 | 6.6881 | 6.0528 | 7.1307 | 5.9934 | 6.7127 | 6.2621 |
| ō | 17.653 | 17.231 | 14.828 | 20.104 | 16.282 | 16.307 | 16.526 | 19.619 | 14.812 | 15.393 | 15.535 | 14.958 | 17.181 | 15.574 | 18.497 | 16.418 | 14.419 | 16.086 | 20.124 | 17.865 | 15.968 | 17.745 | 18.284 | 18.357 | 18.383 | 16.815 | 16.149 | 15.661 | 15.014 | 14.577 | 15.579 | 16.677 | 17.646 |
| ω | 5.6465 | 5.8155 | 1.9308 | 3.599 | 2.8055 | 0.5302 | 4.9439 | 1.4792 | 0.5478 | 1.8401 | 3.5729 | 5.3776 | 5.2824 | 5.2196 | 3.8597 | 4.1368 | 3.7232 | 4.737 | 4.0218 | 3.8368 | 2.8416 | 5.0547 | 2.3079 | 6.0697 | 0.5322 | 1.8811 | 1.5899 | 2.2309 | 3.6681 | 6.123 | 4.1298 | 3.6489 | 4.7829 |
| E | 5.193 | 4.87 | 5.18 | 5.18 | 4.564 | 5.246 | 4.736 | 5.409 | 4.705 | 4.472 | 4.875 | 4.786 | 4.572 | 4.267 | 4.875 | 4.594 | 4.875 | 4.426 | 5.55 | 5.193 | 4.875 | 4.875 | 4.875 | 4.583 | 4,475 | 4.627 | 4.622 | 4.635 | 4.791 | 4.067 | 4.505 | 4.767 | 4.894 |
| DeltaActua | 24.4132 | 28.8326 | 27.5195 | 39.4521 | 30.5078 | 41.2154 | 37.1876 | 48.1011 | 35.7476 | 30.2353 | 23.5493 | 20.9608 | 26.5092 | 30.9844 | 34.2638 | 27.3894 | 30.9163 | 27.9205 | 36.8882 | 35.2491 | 33.9017 | 39.1073 | 33.76 | 33.4924 | 41.7661 | 34.1484 | 37.194 | 30.7538 | 25.2333 | 24.6991 | 29.1636 | 28.3034 | 33.1985 |
| MDPI | 24.413 | 25.553 | 27.52 | 39.452 | 30.508 | 37.831 | 37.188 | 48.101 | 31.966 | 30.235 | 23.549 | 18.844 | 26.509 | 30.984 | 34.264 | 27.389 | 30.469 | 27.921 | 36.888 | 32.704 | 30.194 | 27.075 | 33.76 | 33.492 | 41.766 | 34.055 | 36.214 | 30.754 | 25.233 | 24.699 | 27.996 | 28.303 | 33.199 |
| MinTActu | 337.683 | 332.586 | 325.745 | 327.931 | 322.918 | 316.182 | 320.877 | 320.942 | 316.617 | 321.459 | 326.315 | 330.734 | 330.621 | 325.98 | 330,208 | 327.002 | 326.275 | 324.718 | 334.388 | 327.336 | 320.208 | 321.129 | 325.218 | 329.037 | 317.968 | 323.573 | 319.286 | 321.598 | 323.139 | 325.886 | 327.726 | 327.275 | 329.189 |
| MinPActu | 545 | 463 | 603 | 200 | 535 | 693 | 587 | 630 | 069 | 567 | 601 | 752 | 634 | 576 | 571 | 538 | 728 | 574 | 500 | 689 | 718 | 739 | 537 | 534 | 597 | 486 | 678 | 582 | 509 | 519 | 999 | 999 | 649 |
| MinThetaE | 337.683 | 335.866 | 325.745 | 327.931 | 322.918 | 319.566 | 320.877 | 320.942 | 320.399 | 321.459 | 326.315 | 332.851 | 330.621 | 325.98 | 330.208 | 327.002 | 326.722 | 324.718 | 334.388 | 329.882 | 323.915 | 333.162 | 325.218 | 329.037 | 317.968 | 323.667 | 320.266 | 321.598 | 323.139 | 325.886 | 328.894 | 327.275 | 329.189 |
| MinPr | 545 | 543 | 603 | 500 | 535 | 649 | 587 | 630 | 612 | 295 | 601 | 610 | 634 | 576 | 571 | 538 | 538 | 574 | 500 | 638 | 522 | 633 | 537 | 534 | 597 | 585 | 616 | 582 | 509 | 519 | 999 | 560 | 649 |
| MaxThetE | 362.096 | 361.419 | 353.264 | 367.383 | 353.426 | 357.397 | 358.065 | 369.043 | 352,365 | 351.695 | 349.864 | 351.695 | 357.13 | 356.964 | 364.471 | 354.391 | 357.191 | 352.638 | 371.276 | 362.585 | 354.109 | 360.236 | 358.978 | 362.529 | 359.734 | 357.722 | 356.48 | 352.352 | 348.372 | 350.585 | 356.89 | 355.579 | 362.387 |
| MaxPr | 1011 | 1013 | 1014 | 1011 | 1014 | 1017 | 1012 | 1009 | 1015 | 1017 | 1014 | 1012 | 1011 | 1013 | 1019 | 1020 | 1020 | 1018 | 1011 | 1015 | 1015 | 1014 | 1014 | 1011 | 1017 | 1015 | 1015 | 1012 | 1017 | 1015 | 1015 | 1015 | 1015 |
| OCR | - | - | - | 0 | - | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | - | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | - | 0 | 0 | - | - | 0 | 0 |
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| ≻ R | 92 | 92 | 95 | 95 | 92 | 98 | 95 | 95 | 92 | 95 | 98 | 92 | 95 | 95 | 95 | 95 | 95 | 95 | 95 | 95 | 95 | 95 | 95 | 85 | 98 | 98 | 96 | 98 | 98 | 96 | 96 | 96 | 96 |

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|----------|---------------|-----------|----------|---------|--|--------------------|-------------------------------|--|---|--|--|--|--|---|---|---|---|---|---|---|--|--|--|--|---|---|--|---|--|---|--|--|
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| 6 48.934 | ł | - | 8 25.138 | l | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | 320.546 | 323.643 | 333,348 | | 321.058 | 321.058 322.743 | 321.058 322.743 324.208 | 321.058 322.743 324.208 318.584 | 321.058 322.743 324.208 318.584 323.873 | 324.058 322.743 324.208 318.584 323.873 320.378 | 321.058 322.743 324.208 318.584 323.873 320.378 | 321.058 322.743 324.208 318.584 323.873 320.378 320.378 320.378 | 321.058 322.743 324.208 318.584 323.873 322.0378 322.031 332.2031 | 321.058 322.743 324.208 318.584 323.873 320.378 326.829 332.221 332.221 | 321.058 322.743 324.208 318.584 323.873 320.378 322.031 326.829 332.221 321.64 | 321.058 322.743 324.208 318.584 323.873 320.378 320.378 320.378 320.378 320.378 320.378 320.378 320.378 320.378 320.378 | 321.058 322.743 324.208 318.584 323.873 322.031 326.829 332.221 321.64 326.459 326.459 | 321.058 324.208 324.208 318.584 323.873 320.378 320.378 320.378 321.64 326.459 326.459 326.459 326.459 326.459 | 321.058 324.208 324.208 318.584 320.378 320.378 320.378 322.031 326.829 322.22 322.22 322.22 323.23 323.22 323.22 323.22 323.22 323.22 323.22 323.22 323.22 323.22 | 321.058 324.208 324.208 318.584 323.873 320.378 322.031 322.031 326.459 320.657 320.657 320.657 | 321.058 324.208 324.208 318.584 323.873 320.378 320.378 320.378 320.378 320.829 320.657 320.657 320.3533 | 321,058 322,743 324,208 318,584 323,873 320,378 320,378 320,378 320,873 320,657 320,657 320,657 320,953 316,331 321,134 | 321.058 322.743 324.208 318.584 323.873 320.378 320.378 320.378 320.879 320.657 320.657 320.657 320.92 320.92 316.331 318.993 | 321.058 322.743 324.208 318.584 323.873 320.378 320.378 320.378 320.829 320.657 320.657 320.657 320.353 320.353 320.353 320.353 316.331 | 321.058 322.743 324.208 318.584 323.873 320.378 320.378 320.459 320.459 320.657 320.353 320.353 320.32 316.331 316.331 321.134 320.353 | 321.058 322.743 322.743 323.873 320.378 320.378 320.378 320.829 320.657 320.657 320.657 320.657 320.657 320.657 320.82 320.82 320.82 320.82 320.82 320.82 320.82 | 321.058 322.743 323.873 323.873 320.378 320.378 320.378 320.378 320.829 320.657 320.92 320.92 320.93 320.93 320.93 320.93 320.93 320.93 320.93 320.93 320.93 320.93 320.93 320.93 320.93 | 321.058 322.743 322.743 323.873 320.378 320.378 320.378 320.378 320.829 320.657 320.657 320.95 320.353 | 321.058 322.743 322.743 323.873 320.378 320.378 320.378 320.378 320.657 320.353 | 321.058 322.743 324.208 318.584 320.378 320.378 320.378 320.829 320.657 320.657 320.92 320.363 320.378 320.459 320.363 320.363 320.373 320.32 320.363 | 321.058 322.743 322.743 323.873 320.378 320.378 320.378 320.378 320.353 | 321.058 322.743 322.743 323.873 320.378 320.378 320.378 320.378 320.829 320.657 320.657 320.353 |
| | 589 | 621 | 661 | 733 | 22. | 541 | 541 | 541 567 653 | 541 567 653 565 | 541 567 653 565 727 | 541 567 653 565 565 727 696 | 541 567 653 565 727 727 700 | 541 567 653 565 727 700 700 | 541 567 653 565 727 727 696 696 640 | 541 567 653 565 565 727 700 700 640 683 | 541 567 653 565 727 700 700 640 683 683 | 541 567 653 565 727 700 640 683 683 602 454 | 541 567 653 565 727 700 640 683 602 683 665 | 541 567 663 565 565 727 700 640 683 683 602 454 454 752 | 541 567 663 565 565 727 700 640 683 602 454 454 752 665 740 | 541 567 565 565 565 727 700 640 683 602 602 454 752 762 762 763 763 | 541 567 653 565 565 727 700 640 683 683 683 683 683 683 683 685 752 865 865 | 541 567 663 565 565 727 700 640 683 683 683 683 685 740 740 740 681 681 | 541 567 663 565 565 727 700 640 683 602 454 454 454 454 454 667 661 661 661 661 | 541 567 663 565 565 565 727 700 640 683 602 454 454 752 665 665 661 661 661 | 541 567 565 565 565 727 700 640 683 683 683 662 454 740 661 661 617 610 | 541 565 565 565 565 565 700 640 683 683 683 683 685 752 661 661 617 610 610 | 541 567 653 565 565 727 696 602 602 603 665 661 661 617 610 614 614 | 541 567 663 565 565 727 700 640 683 683 602 454 454 454 454 454 454 454 661 661 661 661 661 661 661 661 661 66 | 541 567 663 696 696 696 602 602 602 603 604 604 604 604 605 605 607 610 610 610 610 610 610 610 611 610 | 541 567 663 696 770 640 698 602 602 661 661 661 661 610 610 614 610 610 610 610 610 610 610 610 610 610 | 541 567 653 565 565 727 696 602 602 602 661 661 617 610 610 610 610 610 610 610 610 610 610 |
| | 320.546 | 323.643 | 333.673 | 322.035 | | 322.743 | 322.743 324.208 | 322.743 324.208 321.426 | 322.743 324.208 321.426 323.873 | 322.743 324.208 321.426 323.873 327.166 | 322.743 324.208 321.426 323.873 327.166 327.582 | 322.743 324.208 321.426 323.873 327.166 327.582 327.582 | 322.743 324.208 321.426 323.873 327.166 327.582 328.615 | 322.743 324.208 321.426 323.873 327.166 327.582 327.582 328.615 332.221 | 322.743 324.208 321.426 323.873 327.166 327.582 328.615 332.221 323.204 | 322.743 324.208 321.426 323.873 327.166 327.582 328.615 323.221 323.224 326.459 | 322.743 324.208 321.426 323.873 327.166 327.582 328.615 332.221 323.204 328.459 329.925 | 322.743 324.208 321.426 327.166 327.166 327.582 328.615 323.221 323.224 326.459 333.001 321.589 | 322.743 324.208 321.426 327.166 327.166 327.221 328.615 328.221 328.224 328.224 328.925 328.925 328.925 328.925 | 322.743 324.208 321.426 327.166 327.166 327.221 328.615 328.615 328.204 328.925 329.925 333.001 333.001 335.852 326.852 | 322.743 324.208 321.426 323.873 327.166 327.582 328.615 328.615 328.459 326.459 321.589 321.589 321.589 321.589 | 322.743 324.208 321.426 327.166 327.582 328.615 328.615 328.221 328.925 328.925 328.925 328.925 328.925 328.925 328.925 328.925 328.925 328.925 328.925 328.925 | 322.743 324.208 321.426 327.166 327.166 327.582 328.615 328.221 328.925 328.925 328.925 328.925 328.925 328.925 328.925 328.925 328.925 328.925 328.93 | 322.743 324.208 321.426 327.166 327.166 327.582 328.615 328.624 328.925 | 322.743 324.208 321.426 327.166 327.166 327.221 328.615 328.615 328.625 328.625 328.626 328.62 | 322.743 324.208 321.426 327.166 327.166 327.221 328.615 328.615 328.622 328.62 | 322.743 324.208 321.426 327.166 327.582 328.615 328.615 328.224 328.925 | 322.743 324.208 321.426 327.166 327.166 327.582 328.615 323.204 328.925 328.925 320.92 320.92 320.92 320.93 321.134 321.134 321.134 321.134 321.134 321.134 321.134 321.134 321.134 | 322.743 324.208 321.426 327.166 327.166 327.582 328.615 322.221 328.925 328.925 328.925 320.92 320.92 320.92 320.92 320.92 320.92 320.92 320.92 320.92 320.93 320.9 | 322.743 324.208 324.208 327.166 327.166 327.221 328.221 328.925 328.925 320.92 320.92 320.92 320.92 320.92 320.92 320.92 320.92 320.92 320.92 320.92 320.92 320.92 320.93 | 322.743 324.208 324.208 327.166 327.166 327.166 328.615 328.615 328.629 | 322.743 324.208 324.208 321.426 327.582 327.582 328.615 328.615 328.623 328.925 |
| 000 | 200 | 621 | 572 | 539 | 541 | | 295 | 567 613 | 567 613 565 | 567 613 565 598 | 567 613 565 598 609 | 567 613 565 598 609 618 | 567 613 565 598 609 618 640 | 567 565 598 609 618 640 650 | 567 565 598 609 618 640 650 | 567 613 565 598 609 640 640 650 650 636 | 567 613 565 598 609 640 640 650 650 650 650 653 653 653 | 567 613 565 598 609 640 650 650 650 650 650 650 660 670 670 670 670 670 670 670 670 67 | 567 613 598 598 640 640 650 602 536 536 540 536 | 567 613 598 598 640 640 650 536 536 536 536 536 536 536 536 540 | 567 613 598 598 640 640 650 650 640 640 640 640 640 | 567 613 565 598 609 640 640 650 650 650 650 650 650 650 650 650 65 | 567 613 565 598 609 640 640 650 650 650 650 650 650 650 650 650 65 | 567 613 565 598 609 640 650 640 640 640 640 640 640 640 640 640 64 | 567 613 598 598 640 640 640 640 640 640 640 640 640 640 | 567 613 598 598 609 640 640 640 640 646 640 646 640 646 640 646 640 646 640 640 | 567 613 598 598 609 640 640 640 640 646 646 646 646 646 646 | 567 613 598 598 609 640 640 640 640 646 646 617 617 610 614 610 614 | 567 508 508 508 609 640 640 650 650 650 650 678 678 610 610 611 611 611 611 611 611 611 611 | 567 613 508 509 618 640 640 640 640 640 640 640 640 640 640 | 567 613 613 640 640 640 640 640 640 640 640 640 640 | 567 613 613 609 609 640 640 640 640 640 640 640 640 640 640 |
| 301.138 | 369.48 | 358.638 | 358.811 | 359.901 | 354.488 | | 355.951 | 355.951 351.414 | 355.951 351.414 350 | 355.951 351.414 350 363.637 | 355.951 351.414 350 363.637 363.093 | 355.951 351.414 350 363.637 363.093 354.596 | 355.951 351.414 350 363.637 363.093 354.596 355.472 | 355.951 351.414 350 363.637 363.093 354.596 354.72 | 355.951 351.414 350 363.637 363.093 354.596 355.472 361.495 | 355.951 351.414 350 363.637 363.093 354.596 355.472 351.495 359.619 | 355.951 351.414 350 363.637 364.596 355.472 361.495 359.619 345.758 | 355.951 351.414 350 363.637 363.093 354.596 355.472 361.495 359.619 345.758 345.758 345.758 | 355.951 351.414 351.414 363.033 354.596 355.472 361.495 359.619 359.293 359.235 | 355.951 351.414 351.414 363.033 354.596 355.472 361.495 359.819 358.299 358.299 359.235 349.331 | 355.951 351.414 351.414 363.093 354.596 354.472 354.495 359.819 359.299 359.293 359.235 349.331 349.331 | 355.951 351.414 351.414 363.093 354.596 354.472 361.495 359.619 359.299 359.299 359.235 349.331 349.331 | 355.951 351.414 351.414 363.637 363.093 354.596 355.472 361.495 359.619 359.295 359.235 349.331 346.513 349.331 349.482 | 355.951 351.414 351.414 363.637 363.093 354.596 355.472 361.495 359.295 359.235 349.331 349.331 349.827 338.827 | 355.951 351.414 351.414 363.637 363.093 354.596 355.472 361.495 359.619 359.235 349.331 349.482 349.482 349.482 349.482 351.936 351.936 | 355.951 351.414 351.414 363.093 354.596 354.596 356.472 356.193 359.235 349.331 349.482 349.331 349.482 359.235 359.235 359.235 359.235 359.235 | 355.951 351.414 351.414 363.093 354.596 354.495 356.193 359.235 349.331 349.331 349.331 349.331 350.916 350.916 350.916 | 355.951 351.414 351.414 363.637 363.093 354.596 355.472 361.495 359.299 359.235 349.331 349.331 349.331 359.235 359.235 359.236 359.235 359.236 359.236 359.236 359.236 359.236 359.236 | 355.951 351.414 351.414 363.637 363.637 364.596 355.472 361.495 358.299 361.413 358.299 346.513 346.513 346.513 350.216 350.214 350.214 350.214 | 355.951 351.414 351.414 363.637 363.093 354.596 356.472 361.495 356.299 345.758 346.513 346.513 349.331 349.331 350.916 350.916 350.916 350.371 350.374 353.357 | 355.951 351.414 351.414 363.093 354.596 355.472 361.495 359.299 345.758 345.758 346.413 359.235 349.331 349.482 359.214 350.916 350.916 350.714 360.714 360.714 362.744 362.744 | 355.951 351.414 351.414 363.637 363.093 354.596 354.596 356.299 359.235 349.331 349.331 350.916 350.916 350.916 350.371 360.371 360.371 360.371 360.373 360.374 360.373 |
| 1016 | 1016 | 1017 | 1015 | 1016 | 1016 | | 1017 | 1017 | 1017 1018 1016 | 1017 1018 1016 1011 | 1017 1018 1016 1011 | 1017 1018 1016 1011 1012 | 1017 1018 1011 1012 1019 | 1017 1018 1011 1012 1020 1020 | 1017 1018 1011 1012 1020 1014 | 1017 1018 1011 1012 1020 1020 1014 1011 | 1017 1018 1011 1012 1019 1014 1014 1017 | 1017 1018 1011 1011 1019 1014 1011 1015 | 1017 1018 1011 1012 1020 1014 1015 1015 1022 | 1017 1018 1011 1011 1010 1014 1015 1015 1020 1020 | 1017 1018 1019 1020 1014 1017 1017 1020 1020 | 1017 1018 1019 1010 1014 1017 1017 1018 1018 | 1017 1018 1019 1019 1017 1017 1019 1018 1019 | 1017 1018 1011 1011 1019 1017 1018 1018 1018 1018 | 1017 1018 1011 1011 1010 1015 1017 1018 1018 1018 1018 | 1017 1018 1011 1011 1010 1017 1017 1018 1018 | 1017 1018 1011 1011 1012 1017 1018 1018 1018 1019 1018 1019 1019 1019 | 1017 1018 1019 1019 1019 1019 1018 1019 1019 | 1017 1018 1011 1019 1010 1017 1019 1018 1018 1018 1018 1018 1019 1018 1019 1019 | 1017 1018 1019 1019 1019 1017 1018 1019 1019 1019 1019 1019 1019 1019 | 1017 1018 1019 1011 1019 1017 1019 1018 1018 1018 1018 1019 1019 1019 | 1017 1018 1019 1010 1010 1014 1017 1019 1019 1019 1019 1019 1019 1019 |
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| 3 23 | 3 25 | 3 26 | 3 28 | 8 | c | | <u> </u> | | | | | | | | | | | | | | | | | | | +++++++++++++++++++++++++++++++++++++++ | +++++++++++++++++++++++++++++++++++++++ | +++++++++++++++++++++++++++++++++++++++ | | | | |
| 96 | 9 96 | 96 | 9 96 | L | 96 | _ | | | | | | | | | | | | | | | | | | | | | | | | | | |

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|------------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|
| IAA | 59.682 | 55.027 | 47.988 | 47.378 | 39.396 | 53.394 | 45.183 | 41.92 | 48.134 | 50.523 | 43.072 | 34.023 | 51.514 | 42.251 | 43.92 | 46.142 | 32.216 | 45.364 | 61.036 | 56.877 | 37.144 | 45.012 | 44.579 | 45.369 | 50.754 | 48.394 | 51.022 | 52.529 | 45.893 | 49.421 | 48.13 | 50.036 | 56.071 |
| gamma | 6.987 | 7.1514 | 6.5674 | 6.5947 | 6.403 | 6.9117 | 6.0142 | 6.2472 | 5.9964 | 6.7661 | 6.2206 | 5.9601 | 6.4855 | 289.9 | 9600'9 | 6.6284 | 5.4388 | 5.9845 | 6.8829 | 7.3906 | 6.1889 | 6.1423 | 6.4946 | 6.0635 | 6.3502 | 6.5779 | 6.7216 | 6.4642 | 6.3345 | 6.8286 | 6.3303 | 6.5753 | 6.4089 |
| lo | 15.439 | 16.912 | 15.996 | 15.899 | 15.033 | 17.972 | 15.312 | 18.005 | 18.48 | 16.096 | 15.638 | 16.577 | 16.413 | 15.086 | 15.873 | 15.078 | 14.747 | 13.117 | 16.216 | 15.615 | 13.386 | 13.353 | 14.26 | 12.565 | 18.127 | 15.34 | 13.877 | 15.314 | 14.039 | 16.349 | 14.507 | 15.464 | 18.044 |
| Qm | 1.5737 | 4.591 | 4.4808 | 4.8259 | 5.9173 | 5.1593 | 2.274 | 6.1974 | 2.9565 | 4.0272 | 4.2083 | 6.1223 | 3.1341 | 5.5419 | 2.5553 | 4.5266 | 2.666 | 0.5413 | 0.4982 | 4.7423 | 4.2509 | 1.8073 | 3.9051 | 1.2611 | 3.6598 | 4.0439 | 2.9401 | 2.2968 | 2.8164 | 5.6946 | 2.1147 | 3.3925 | 1.1257 |
| НШ | 4.58 | 4.195 | 4.568 | 4.549 | 4.373 | 4.485 | 4.822 | 4.802 | 5.003 | 4.286 | 4.662 | 4.698 | 4.78 | 4.267 | 4.572 | 4.267 | 4.615. | 4.612 | 4.572 | 4.208 | 4.185 | 4.64 | 4.267 | 4.898 | 4.876 | 4.565 | 4.493 | 4.904 | 4.546 | 4.525 | 4.553 | 4.57 | 4.681 |
| DeltaActua | 38.4923 | 40.1196 | 41.9129 | 29.3979 | 18.1376 | 44.5963 | 29.2005 | 36.4901 | 37.0474 | 37.6819 | 27.7044 | 26.3604 | 30.6551 | 21.406 | 27.3818 | 30.0806 | 21.8422 | 25.2296 | 40.0195 | 30.493 | 18.0734 | 25.1748 | 25.4576 | 26.0056 | 47.9576 | 32.6949 | 28.1281 | 32.5981 | 27.0315 | 27.2876 | 31.1446 | 32.5481 | 46.949 |
| MDPI | 38.492 | 40.12 | 32.315 | 29.398 | 17.025 | 37.596 | 26.604 | 36.49 | 37.047 | 31.988 | 27.704 | 25.29 | 30.655 | 21.406 | 27.382 | 25.937 | 21.842 | 23.52 | .40.02 | 30.493 | 16.116 | 20.152 | 25.458 | 21.583 | 47.958 | 32.695 | 28.128 | 32.598 | 27.032 | 24.936 | 31.145 | 32.548 | 46.727 |
| MinTActu | 319.983 | 324.352 | 320.783 | 326.78 | 330.588 | 322.195 | 320.584 | 328.501 | 328.34 | 315.583 | 323.38 | 328.201 | 324.152 | 328.594 | 322.405 | 319.351 | 320.6 | 315.771 | 317.224 | 320.459 | 321.191 | 316.18 | 323.905 | 314.672 | 314.68 | 322.467 | 322.976 | 324.774 | 322.876 | 327.72 | 321.694 | 323.44 | 317.419 |
| MinPActu | 576 | 572 | 889 | 563 | 999 | 705 | 658 | 521 | 555 | 069 | 597 | 700 | 528 | 604 | 209 | 657 | 585 | 657 | 614 | 583 | 691 | 770 | 596 | 786 | 500 | 632 | 579.8 | 555 | 523 | 468 | 638 | 621 | 652.3 |
| MinThetaE | 319.983 | 324.352 | 330,381 | 326.78 | 331.701 | 329.195 | 323.18 | 328.501 | 328.34 | 321.277 | 323.38 | 329.271 | 324.152 | 328.594 | 322.405 | 323.495 | 320.6 | 317.481 | 317.224 | 320.459 | 323.149 | 321.203 | 323.905 | 319.094 | 314.68 | 322.467 | 322.976 | 324.774 | 322.876 | 330.071 | 321.694 | 323.44 | 317.641 |
| MinPr | 576 | 572 | 603 | 563 | 576 | 529 | 641 | 521 | 555 | 565 | 597 | 649 | 528 | 604 | 503 | 575 | 595 | 616 | 614 | 583 | 530 | 625 | 969 | 643 | 500 | 632 | 579.8 | 555 | 523 | 500 | 638 | 621 | 099 |
| MaxThetE | 358.475 | 364.471 | 362.696 | 356.178 | 348.726 | 366.791 | 349.785 | 364.991 | 365.388 | 353.264 | 351.084 | 354.561 | 354.807 | 350 | 349.787 | 349.432 | 342.443 | 341.001 | 357.243 | 350.952 | 339.264 | 341.354 | 349.363 | 340.677 | 362.638 | 355.162 | 351.104 | 357.372 | 349.907 | 355.007 | 352.839 | 355.988 | 364,368 |
| MaxPr | 1018 | 1019 | 1014 | 1014 | 1015 | 1013 | 1016 | 1016 | 1015 | 1014 | 1013 | 1020 | 1012 | 1018 | 1017 | 1016 | 1020 | 1018 | 1014 | 1014 | 1019 | 1018 | 1014 | 1014 | 1015 | 1019 | 1020 | 1019 | 1019 | 1019 | 1020 | 1020 | 1020 |
| OCR | 0 | + | - | 0 | 0 | - | 0 | - | - | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | - | 0 | - | 0 | - | 0 | 0 | 0 | 0 | 0 | - |
| λO | 14 | 15 | 2 | ω | 6 | ÷ | 16 | 17 | 18 | 21 | 22 | 30 | - | 19 | 20 | 21 | 23 | 25 | 26 | 27 | 29 | 30 | 3 | 16 | 17 | 18 | 19 | 20 | 22 | 23 | 25 | 26 | 27 |
| MO | ∞ | ω | 6 | 6 | 6 | 6 | 6 | 60 | 6 | 6 | 6 | 6 | 65 | 5 | 5 | 2 | 5 | 5 | 5 | 2 | 5 | 5 | 2 | ဖ | ဖ | ယ | ဖ | ۵ | ဖ | g | ဖ | 9 | ဖ |
| ΥR | 96 | 96 | 96 | 96 | 96 | 96 | 96 | 96 | 96 | 96 | 96 | 96 | 96 | 97 | 97 | 97 | 97 | 97 | 97 | 97 | 97 | 97 | 97 | 97 | 97 | 97 | 94 | 97 | 97 | 97 | 97 | 97 | 97 |

| | - | | | | | | - | | | | | | | | | | | | | | | | 1 | | | _ | | | | - | | | |
|------------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|
| IM. | 46.827 | 48.256 | 43.419 | 46.656 | 46.697 | 40.987 | 42.87 | 32.104 | 22.414 | 32.23 | 48.927 | 63.742 | 56.411 | 61.472 | 39.658 | 53.171 | 49.507 | 52.797 | 50.258 | 52.713 | 51.639 | 52.791 | 49.487 | 54.666 | 48.698 | 50.878 | 46.72 | 35.283 | 43.965 | 50.663 | 54.314 | 51.933 | 49 893 |
| gamma | 6.4518 | 6.5961 | 5.8898 | 6.0858 | 6.3977 | 6.5651 | 6.5566 | 6.0431 | 5.3931 | 5.5483 | 6.2513 | 7.5735 | 7.0145 | 6.922 | 6.1517 | 6.7628 | 6.5704 | 6.7673 | 6.5329 | 6.9671 | 7.2466 | 6.5029 | 6.3927 | 6.8242 | 5.9314 | 6.1794 | 6.9432 | 6.206 | 6.1398 | 6.3554 | 6.5638 | 6.9408 | 6.6129 |
| ۵I | 15.66 | 14.901 | 14.25 | 13.246 | 12.924 | 12.639 | 13.857 | 8.2637 | 15.975 | 16.155 | 16.33 | 17.299 | 16.297 | 17.198 | 15.359 | 14.264 | 16.56 | 14.877 | 14.905 | 15.31 | 14.908 | 15.988 | 16.155 | 14.913 | 16.636 | 16.59 | 14.177 | 14.323 | 17.062 | 20.699 | 17.042 | 16.448 | 15.396 |
| Qm | 3.9899 | 3.7204 | 1.4529 | 0.5422 | 2.0757 | 4.9961 | 4.5037 | 0.624 | 5.5773 | 3.84 | 2.4198 | 3.0365 | 2.8349 | 0.5156 | 5.1503 | 3.0127 | 4.1298 | 3.1847 | 2.7912 | 4.8259 | 6.2436 | 2.446 | 2.3283 | 2.1458 | 1.5309 | 1.3561 | 6.189 | 6.0906 | 4.7227 | 6.2233 | 2.9225 | 5.5749 | 4 27 49 |
| Hm | 4.543 | 4.442 | 4.703 | 4.535 | 4.427 | 4.267 | 4.121 | 4.423 | 5.146 | 4.488 | 4.655 | 4.212 | 4.267 | 4.435 | 4.876 | 4.717 | 4.566. | 4.588 | 4.592 | 4.593 | 4.278 | 4.767 | 4.38 | 4.396 | 5.058 | 4.693 | 4.364 | 4.673 | 5.049 | 5.507 | 4.86 | 4.596 | 4.839 |
| DeltaActua | 42.8651 | 37.2857 | 36.2374 | 39.0573 | 37.7988 | 37.7194 | 29.5479 | 22.8983 | 18.4207 | 28.4528 | 36.6702 | 46.2672 | 32.7751 | 41.2751 | 42.9333 | 27.692 | 33.6015 | 37.9271 | 36.7366 | 29.6205 | 31.9425 | 37.571 | 37.8591 | 39.3266 | 41.9255 | 37.1261 | 41.9799 | 17.972 | 32.3209 | 43.1975 | 31.6261 | 44.5634 | 27.0753 |
| MOPI | 30.939 | 37.286 | 32.691 | 33.936 | 36.17 | 37.719 | 29.548 | 16.456 | 16.04 | 28.453 | 29.98 | 45.222 | 32.775 | 41.275 | 23.928 | 25.204 | 31.711 | 35.331 | 34.439 | 29.324 | 31.943 | 31.741 | 31.718 | 36.092 | 41.926 | 35.027 | 41.98 | 15.026 | 32.321 | 43.198 | 30.33 | 44.563 | 26.471 |
| MinTActu | 313.413 | 313.487 | 316.165 | 312.292 | 314.744 | 308.892 | 317.179 | 309.209 | 330.928 | 318.528 | 318.605 | 318.967 | 321.35 | 316.672 | 314.295 | 324.015 | 326.889 | 320.09 | 320.015 | 325.539 | 327.441 | 315.931 | 313.506 | 318.114 | 324.687 | 320.025 | 313.8 | 332.524 | 330.284 | 334.918 | 324.708 | 312.665 | 324.826 |
| MinPActu | 714 | 900 | 715 | 785 | 747 | 900 | 593 | 729 | 446 | 581 | 622.9 | 725 | 629.8 | 609 | 400 | 685 | 700 | 828 | 729 | 485 | 540 | 675 | 746 | 679 | 558 | 654 | 500 | 819 | 650 | 642 | 702 | 500 | 786 |
| MinThetaE | 325.338 | 313.487 | 319.711 | 317.413 | 316.374 | 308.892 | 317.179 | 315.652 | 333.309 | 318.528 | 318.605 | 320.012 | 321.35 | 316.672 | 333.3 | 326.503 | 328.779 | 322.686 | 322.312 | 325.835 | 327.441 | 321.761 | 319.647 | 321.349 | 324.687 | 322.124 | 313.8 | 335.471 | 330.284 | 334.918 | 326.004 | 312.665 | 325.43 |
| MinPr | 647 | 500 | 643 | 643 | 643 | 500 | 593 | 643 | 643 | 581 | 622.9 | 575 | 629.8 | 609 | 500 | 614.5 | 594 | 643 | 581 | 500 | 540 | 209 | 643 | 594 | 558 | 578 | 500 | 643 | 650 | 642 | 610 | 200 | 545 |
| MaxThetE | 356.278 | 350.773 | 352.403 | 351.35 | 352.543 | 346.611 | 346.727 | 332.108 | 349.349 | 346.981 | 355.275 | 365.234 | 354.125 | 357.947 | 357.228 | 351.707 | 360.49 | 358.017 | 356.751 | 355.159 | 359.384 | 353.502 | 351.365 | 357.441 | 366.612 | 357.151 | 355.78 | 350.496 | 362.605 | 378.115 | 356.334 | 357.229 | 351,902 |
| MaxPr | 1018 | 1018 | 1007 | 1007 | 1006 | 1011 | 1009 | 1009 | 1014 | 1015 | 1012 | 1013 | 1015 | 1013 | 1015 | 1016 | 1020 | 1022 | 1021 | 1017 | 1019 | 1016 | 1017 | 1018 | 1018 | 1009 | 1017 | 1020 | 1019 | 1019 | 1016 | 1016 | 1018 |
| OCR | 0 | - | 0 | 0 | 0 | - | - | 0 | 0 | 0 | - | 0 | - | 0 | - | - | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | - | 0 | 0 | 0 | - | - | 0 |
| à | 28 | 29 | 귝 | S. | മ | - | 2 | m | 2 | 1 | 12 | 13 | 14 | 15 | - | 'n | 9 | ~ | | = | = | 13 | 4 | 15 | 17 | 200 | 13 | 21 | 22 | 23 | 26 | 27 | 28 |
| Ø ₩ | ဖ | 9 | 9 | ی | 9 | 9 | 9 | 9 | 9 | 9 | 9 | ی | ဖ | 9 | ۲~ | ~ | ~ | ~ | r- | ۴ | ~ | ۴ | ~ | - | ~ | ~ | ~ | ~ | r | ~ | ۲~. | r~ | ^ |
| ΥR | 46 | 6 | 26 | 97 | 26 | 97 | 97 | 97 | 97 | 97 | 97 | 97 | 97 | 97 | 97 | 97 | 97 | 97 | 97 | 97 | 97 | 97 | 97 | 97 | 97 | 97 | 97 | 97 | 97 | 6 | 97 | 97 | 97 |

| MaxPr | 1 1 | ш | MinPr | ш | MinPActu | MinTActu | \vdash | DeltaActua | ΗΉ | Qm | ō | gamma | IW |
|--------------|----------|-------|-------|---------|----------|----------|----------|------------|--------|--------|--------|--------|--------|
| 363.898 | 33.898 | ~, | 542 | 329.298 | 689 | 328.662 | 34.599 | 35.2354 | 4.713 | 4.8842 | 16.797 | 6.5774 | 48.896 |
| 356.154 | 56.154 | Ľ | 579 | 325.051 | 725 | 323.502 | 31.104 | 32.6526 | 5.231 | 1.5411 | 16.678 | 6.4319 | 57.138 |
| 356.967 | 56.967 | ٦ | 618 | 324.611 | 618 | 324.611 | 32.355 | 32.3553 | 5.041 | 2.9512 | 16.036 | 6.1495 | 47.562 |
| 358.513 | 58.513 | ۱*′ | 580 | 324.525 | 488 | 322.35 | 33.988 | 36.1621 | 4.78 | 1.8974 | 17.136 | 5.8579 | 45.933 |
| 356.912 | 56.912 | ۱~′ | 594 | 328.565 | 594 | 328.565 | 28.347 | 28.3468 | 5.23 | 2.3238 | 17.371 | 6.1049 | 51.129 |
| 350.536 | 50.536 | Ø | 619.5 | 324.696 | 619.5 | 324.696 | 25.84 | 25.84 | 4.76 | 4.862 | 15,531 | 6.3235 | 43.353 |
| 362.585 | 32.585 | ۳ | 625 | 322.681 | 625 | 322.681 | 39.904 | 39.9044 | 4.737 | 3.9164 | 16.951 | 6.5444 | 50.981 |
| 350.944 | 50.944 | l~′ | 531 | 332.324 | 451 | 331.076 | 18.62 | 19.8682 | 4.725 | 4.5746 | 14.996 | 5.9259 | 35.987 |
| 346.24 | 46.24 | ı~′ | 500 | 315.377 | 200 | 315.377 | 30.864 | 30.8637 | 4.876 | 3.5589 | 15.268 | 5.9362 | 40.398 |
| 353.7 | 353.7 | , | 643 | 316.402 | 699 | 315.763 | 37.298 | 37.9366 | 4.391 | 1.4187 | 16.014 | 6.149 | 47.998 |
| 353.901 | 53.901 | ۳, | 650 | 316.724 | 693 | 313,487 | 37.177 | 40.4143 | 4.73 | 2.2425 | 1.5 | 6.3427 | 51.86 |
| 349.785 | 19.785 | | 642 | 318.654 | 642 | 318.654 | 31.131 | 31.1309 | 4.514 | 1.4497 | 14.433 | 6.5962 | 53.162 |
| 353.31 | | . ~ / | 572 | 321.951 | 713 | 318.311 | 31.359 | 34.9985 | 4.467 | 3.7785 | 16.785 | 5.8203 | 38.254 |
| 362.514 | | | 500 | 315.071 | 500 | 315.071 | 47.443 | 47.4426 | 4.757 | 5.2513 | 16.389 | 8.5798 | 47.759 |
| 361.948 5 | _ | | 542.7 | 325.799 | 400 | 314.839 | 36.149 | 47.1086 | 4.81 | 4.4851 | 15.716 | 6.4241 | 46.544 |
| | | 110 | 543 | 326.301 | 543 | 326.301 | 34.226 | 34.2255 | 4.803 | 4.5906 | 15.373 | 6.4543 | 46.296 |
| 354,467 5 | | LO. | 564 | 327.673 | 564 | 327.673 | 26.794 | 26.7939 | 4.735. | 3.9232 | 16.506 | 5.9133 | 40.164 |
| | | 100 | 587.8 | 327.476 | 587.8 | 327.476 | 34.446 | 34.4464 | 4.876 | 3.327 | 15.465 | 6.0578 | 43.479 |
| 357.138 5 | 00 | LO. | 540 | 323.359 | 830 | 323.102 | 33.779 | 34.0359 | 4.74 | 2.8541 | 16.915 | 5.9072 | 43.682 |
| 357.129 | _ | | 648 | 322.053 | 648 | 322.053 | 35.076 | 35.0757 | 4.831 | 5.7848 | 16.727 | 6.0028 | 36.764 |
| 355.162 | _ | | 515 | 330.35 | 465 | 330.298 | 24.812 | 24.8645 | 5.203 | 3.2136 | 15.695 | 5.98 | 44.213 |
| 359.325 | 10 | 1.0 | 522.1 | 332.827 | 400 | 314.243 | 26.498 | 45.0815 | 4.876 | 5.4197 | 17.046 | 6.2334 | 42.849 |
| 362.148 | 32.148 | , ~ | 611 | 322.772 | 671 | 319.898 | 39.376 | 42.2501 | 4.739 | 2.6248 | 14.482 | 6.1194 | 44.453 |
| 360.923 | 30.923 | l ~ / | 594 | 323.773 | 651 | 323.366 | 37.15 | 37.5575 | 5.163 | 2.5527 | 16.011 | 6.0043 | 46.783 |
| 367.193 | 37.193 | ~ / | 292 | 327.053 | 567 | 327.053 | 40.14 | 40.14 | 4.943 | 2.4849 | 18.78 | 6.6762 | 59.222 |
| 359.71 | 59.71 | 1— | 650 | 336.376 | 400 | 315.801 | 23.334 | 43.9083 | 5.169 | 5.0338 | 16.091 | 6.0747 | 40.869 |
| 346.543 | 16.543 | 12 | 643 | 321.23 | 705 | 317.321 | 25.313 | 29.2216 | 5.081 | 1.415 | 14.663 | 6.298 | 52.256 |
| 359.88 | 59.88 | 140 | 500 | 336.449 | 400 | 317.761 | 23.43 | 42.1182 | 5.141 | 5.0721 | 17.381 | 5.7187 | 35.745 |
| 353.526 | 33.52e | 1-27 | 595 | 337.391 | 595 | 337.391 | 16.135 | 16.1347 | 5.126 | 5.1886 | 16.245 | 5.0721 | 14.29 |
| 348.288 | <u> </u> | فا | 631.9 | 335.463 | 631.9 | 335.463 | 12.824 | 12.8243 | 4.876 | 5.6553 | 16.503 | 5.1745 | 15.486 |
| 338.668 | 38.668 | ۱~′ | 550 | 317.19 | 785 | 314.052 | 21.477 | 24.616 | 3.657 | 3.5681 | 9.8256 | 7.2855 | 43.92 |
| 340.525 | 10.525 | l~′ | 583 | 311.117 | 583 | 311.117 | 29.408 | 29.4083 | 3.509 | 3.3188 | 13.214 | 7.666 | 55.682 |
| 1018 337.696 | 17 FIGE | , ~ | 639 | 318.798 | 633 | 318.798 | 18.898 | 18.898 | 4.513 | 1.3149 | 10.435 | 5.8788 | 34.83 |

| | | | | | | | | | | | | | | | | | | | | | ٠. | | | | | | | | | | | | |
|------------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|
| IAA | 52.563 | 29.299 | 49.567 | 63.024 | 52.884 | 50.65 | 51.699 | 22'8'99 | 41.751 | 42.497 | 48.3 | 53.652 | 47.48 | 37.492 | 47.614 | 56.062 | 56.462 | 48.182 | 49.441 | 78,427 | 54.842 | 30.884 | 55.062 | 43.002 | 54.689 | 56.224 | 40.04 | 42.675 | 50.825 | 65.38 | 43.6 | 47.637 | 46.325 |
| gamma | 6.1439 | 5.8229 | 6.2615 | 7.4997 | 6.3338 | 6.6812 | 6.6923 | 6.893 | 6.1383 | 6.2564 | 6.199 | 6.2087 | 6.4796 | 5.7875 | 6.3045 | 6.5322 | 6.9729 | 6.7567 | 6.3236 | 5.4823 | 6.7281 | 5.6681 | 6.7242 | 6.3644 | 6.7486 | 6.9159 | 6.1532 | 5.8633 | 6.1043 | 6.8318 | 5.9622 | 6.465 | 5.4564 |
| QI | 14.42 | 13.948 | 13.936 | 13.151 | 15.136 | 16.689 | 16.239 | 17.601 | 16.923 | 16.585 | 16.705 | 19.875 | 16.515 | 14.43 | 14.959 | 16.745 | 16.854 | 15.008 | 17.036 | 17.143 | 18.626 | 16.485 | 17.028 | 14.378 | 18.217 | 18.824 | 17.107 | 17.777 | 19.676 | 17.65 | 18.071 | 19.658 | 17.873 |
| Qm | 0.3371 | 5.5947 | 1.6463 | 2.3196 | 0.5353 | 0.4867 | 4.6723 | 4.7527 | 5.151 | 5.3306 | 3.5281 | 3.3472 | 4.5116 | 3.5637 | 3.069 | 1.816 | 3.7926 | 5.1758 | 3.4856 | 4.8013 | 4.6309 | 5.4448 | 3.6524 | 5.0861 | 4.6474 | 4.1762 | 5.2716 | 3.7138 | 2.8737 | 0.4748 | 3.9927 | 6.419 | 0.5611 |
| НШ | 5.142 | 5.152 | 4.951 | 4.571 | 4.626 | 4.595 | 4.931 | 4.876 | 4.876 | 4.795 | 5.162 | 5.299 | 4.63 | 5.207 | 4.884 | 4.876 | 4.572. | 4.572 | 4.876 | 4.56 | 4.884 | 4.94 | 4.863 | 5.028 | 4.89 | 4.468 | 4.453 | 4.946 | 4.876 | 5.123 | 4.864 | 4.876 | 5.195 |
| DeltaActua | 35.0082 | 33.9265 | 27.3869 | 33.5588 | 46.087 | 41.1958 | 40.0896 | 38.2603 | 39.2917 | 27.4828 | 24.9022 | 50.0744 | 31.1764 | 18.5088 | 28.2448 | 43.6378 | 41.8852 | 30.2016 | 35.8315 | 24.5946 | 36.0624 | 23.0522 | 26.8637 | 28.1228 | 37.4726 | 40.3238 | 32.2684 | 30.4287 | 58.4116 | 46.2595 | 31.231 | 53.5401 | 38.3011 |
| MDPI | 31.177 | 23.447 | 25.783 | 33.559 | 46.087 | 41.196 | 40.09 | 36.985 | 24.568 | 26.6 | 23.934 | 50.074 | 31.176 | 16.333 | 28.245 | 41.028 | 35.903 | 30.202 | 35.832 | 24.595 | 35.262 | 23.052 | 26.864 | 25.025 | 37.473 | 40.324 | 30.131 | 29.566 | 58.412 | 46.26 | 31.231 | 53.54 | 38.301 |
| MinTActu | 311.251 | 324.551 | 321.317 | 322.318 | 310.951 | 315.859 | 329.081 | 330.734 | 317.974 | 332.007 | 330.899 | 316.717 | 330.613 | 330.973 | 328.172 | 319.274 | 316.604 | 327.747 | 327.564 | 328.582 | 327.712 | 330.186 | 328.282 | 321.242 | 328.794 | 324.182 | 325.328 | 329.139 | 312.985 | 322.208 | 328.25 | 316.176 | 322.031 |
| MinPActu | 865 | 850 | 700 | 572 | 200 | 625 | 637 | 483 | 400 | 700 | 899 | 200 | 649 | 716 | 624 | 711 | 400 | 607 | 621 | 567 | 496 | 650 | 629 | 716 | 554 | 999 | 484 | 959 | 500 | 594 | 642 | 500. | 614 |
| MinThetaE | 315.082 | 335.031 | 322.921 | 322.318 | 310.951 | 315.859 | 329.081 | 332.009 | 332.698 | 332.889 | 331.867 | 316.717 | 330.613 | 333.149 | 328.172 | 321.884 | 322.586 | 327.747 | 327.564 | 328.582 | 328.513 | 330.186 | 328.282 | 324.34 | 328.794 | 324.182 | 327.465 | 330.002 | 312.985 | 322.208 | 328.25 | 316.176 | 322.031 |
| MinPr | 643 | 603 | 643 | 213 | 009 | 625 | 637 | 521 | 641 | 643 | 550 | 200 | 648 | 594 | 624 | 648 | 829 | 209 | 621 | 299 | 200 | 059 | 629 | 643 | 554 | 999 | 537 | 643 | 200 | 594 | 642 | 200 | 614 |
| MaxThetE | 346.26 | 358.478 | 348.704 | 355.876 | 357.038 | 357.055 | 369.171 | 368.995 | 357.266 | 359.489 | 355.801 | 366.791 | 361.79 | 349.482 | 356.417 | 362.912 | 358.49 | 357.948 | 363.395 | 353.177 | 363.775 | 353.238 | 355.145 | 349.365 | 366.267 | 364.506 | 357.596 | 359.568 | 371.397 | 368.468 | 359.481 | 369.716 | 360.332 |
| MaxPr | 1017 | 1017 | 1018 | 1017 | 1017 | 1016 | 1014 | 1015 | 1016 | 1018 | 1015 | 1013 | 1011 | 1018 | 1018 | 1019 | 1019 | 1017 | 1020 | 1018 | 1016 | 1017 | 1014 | 1018 | 1016 | 1018 | 1018 | 1018 | 1017 | 1018 | 1011 | 1008 | 1015 |
| OCR | 0 | 0 | 0 | 0 | - | 1 | 0 | _ | 1 | 0 | 0 | ļ. | 0 | 0 | 0 | 1 | 1 | 1 | 1 | 0 | 0 | 0 | _ | 0 | 0 | _ | _ | 0 | - | 0 | 0 | _ | 0 |
| λa | 19 | 78 | 18 | 13 | 21 | 26 | r. | 9 | 7 | œ | 10 | ÷ | 12 | 16 | 13 | 26 | 28 | 29 | 17 | -8 | 19 | 20 | 33 | - | С | 'n | 9 | ~ | 10 | 12 | 2 | က | 귝 |
| O.E | 2 | 5 | 9 | 9 | ဖ | 9 | ~ | 7 | ۲. | ۲~ | ۲. | ۲. | r~ | 7 | 7 | 7 | 7 | ۲- | 8 | œ | ω | ω | ω | 00 | ω. | | ω | 8 | ∞ | 8 | 60 | 65 | 6 |
| Դ | 88 | 88 | 88 | 88 | 88 | 88 | 86 | 86 | 88 | 98 | 86 | 86 | 86 | 98 | 98 | 98 | 98 | 98 | 86 | 88 | 98 | 98 | 98 | 86 | 98 | 88 | 98 | 98 | 86 | 98 | 86 | 98 | 88 |

| 52.093 | 41.879 | 26.852 | 38.408 | 28.24 | 24.942 | 33.831 | 44.171 | 54.343 |
|---------|--|---|--|---|--|---|--|--|
| 6.5347 | 6.0552 | 5.4765 | 6.0829 | 5.526 | 5.526 | 5.6337 | | 7.1144 |
| 16.813 | 18.191 | 18.496 | 17.316 | 16.042 | 16.28 | 17.859 | 20.89 | 15.234 |
| 3.6746 | 4.8424 | 6.3193 | 6.0624 | 5.1415 | 5.9525 | 5.389 | 6.1223 | 4.7932 |
| 4.897 | 4.624 | 4.93 | 4.84 | 5.067 | 5.067 | 5.191 | 4.709 | 4.498 |
| 28.9487 | 36.3401 | 25.5666 | 24.3942 | 20.0883 | 24.4497 | 24.8502 | 38.4479 | 326 679 41,566 41,5662 4,498 4,7932 15,234 |
| 28.949 | 34.743 | 25.496 | 23.244 | 19.901 | 24.24 | 24.047 | 38.448 | 41.566 |
| 329.936 | 321.806 | 335.944 | 336.178 | 335.867 | 337.462 | 336.938 | 333.474 | 326,679 |
| 571 | 700 | 654 | 929 | 423 | 710 | 439 | 645 | 591 |
| 329.936 | 323.403 | 336.015 | 337.329 | 336.055 | 337.672 | 337.741 | 333.474 | 326 679 |
| 57.1 | 643 | 603 | 565 | 645 | 640 | 601 | 645 | 594 |
| 358.884 | 358.146 | 361.511 | 360.573 | 355.956 | 361.912 | 361.789 | 371.922 | 368 246 |
| 1018 | 1019 | 1014 | 1012 | 1012 | 1015 | 1013 | 1017 | 1012 |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | _ |
| 5 | 9 | 1- | 9 | 19 | 21 | 22 | 26 | - |
| 60 | တ | 6 | 6 | 0 | 6 | 6 | 6 | o |
| 88 | 86 | 86 | 86 | 86 | 86 | 88 | 88 | ő |
| | 5 0 1018 358.884 571 329.936 571 329.936 28.949 28.9487 4.897 3.6746 16.813 6.5347 | 9 5 0 1018 358.884 571 329.936 571 329.936 28.949 28.9487 4.897 3.6746 16.813 6.5347 9 6 0 1019 358.146 643 323.403 700 321.806 34.743 36.3401 4.624 4.8424 18.191 6.0552 | 9 5 0 1018 358.884 571 329.936 571 329.936 28.949 28.9487 4.897 3.6746 16.813 6.5347 9 6 0 1019 358.146 643 323.403 700 321.806 34.743 36.3401 4.624 4.8424 18.191 6.0552 9 17 0 1014 361.511 603 336.015 654 335.944 25.496 25.5666 4.93 6.3193 18.496 5.4765 | 9 6 0 1018 358.884 571 329.936 571 329.936 571 329.936 28.949 28.9487 4.897 3.6746 16.813 6.5347 9 6 0 1019 358.146 643 323.403 700 321.806 34.743 36.3401 4.624 4.8424 18.191 6.0552 9 17 0 1014 361.511 603 336.015 654 335.944 25.496 25.5666 4.93 6.3193 18.496 5.4765 9 18 0 1012 360.573 565 337.329 676 336.178 23.244 24.3942 4.84 6.0624 17.316 6.0829 | 9 5 0 1018 358.884 571 329.936 571 329.936 571 329.936 571 329.936 571 329.936 28.949 28.9487 4.897 3.6746 16.813 6.5347 9 6 0 1019 358.146 643 323.403 700 321.806 34.743 36.3401 4.624 4.8424 18.191 6.0552 9 17 0 1014 361.511 603 336.015 654 335.178 25.496 25.5666 4.93 6.3193 18.496 5.4765 9 18 0 1012 360.573 565 337.329 676 335.178 23.244 24.3942 4.84 6.0624 17.316 6.0829 9 19 0 1012 356.956 645 336.056 423 335.867 19.901 20.0883 5.067 5.1415 16.042 5.526 | 9 5 0 1018 358.884 571 329.936 571 329.936 28.949 28.9487 4.897 3.6746 16.813 6.5347 9 6 0 1019 358.146 643 323.403 700 321.806 34.743 36.3401 4.624 4.8424 18.191 6.0552 9 17 0 1014 361.511 603 336.015 654 335.944 25.496 25.5666 4.93 6.3193 18.496 5.4765 9 18 0 1012 360.573 565 337.329 676 336.178 23.244 24.3942 4.84 6.0624 17.316 6.0829 9 19 0 1012 356.956 645 336.055 423 335.867 19.901 20.0883 5.067 5.1415 16.042 5.526 9 21 0 1015 361.912 640 337.672 710 337.462 24.24 24.24 <td>9 5 0 1018 358.884 571 329.936 571 329.936 28.949 28.9487 4.897 3.6746 16.813 6.5347 9 6 0 1019 358.146 643 323.403 700 321.806 34.743 36.3401 4.624 4.8424 18.191 6.0552 9 17 0 1014 361.511 603 336.015 654 335.944 25.496 25.5666 4.93 6.3193 18.496 5.4765 9 18 0 1012 360.573 565 337.329 676 336.178 23.244 24.3942 4.84 6.0624 17.316 6.0829 9 19 0 1012 356.956 645 336.055 423 335.867 19.901 20.0883 5.067 5.1415 16.28 5.526 9 21 0 1015 361.789 601 337.741 439 336.938 24.24 24.4497<!--</td--><td>9 5 0 1018 358.884 571 329.936 571 329.936 28.949 28.9487 4.897 3.6746 16.813 6.5347 9 6 0 1019 358.146 643 323.403 700 321.806 34.743 36.3401 4.624 4.8424 18.191 6.0552 9 17 0 1014 361.511 603 336.015 654 335.944 25.496 25.5666 4.93 6.3193 18.496 5.4765 9 18 0 1012 360.573 565 337.329 676 335.867 19.901 20.0883 5.067 5.1415 16.042 5.526 9 19 0 1015 361.912 640 337.672 710 337.462 24.24 24.4497 5.067 5.9525 16.28 5.526 9 22 0 1013 361.789 601 337.741 439 338.474 24.8502 5.191</td></td> | 9 5 0 1018 358.884 571 329.936 571 329.936 28.949 28.9487 4.897 3.6746 16.813 6.5347 9 6 0 1019 358.146 643 323.403 700 321.806 34.743 36.3401 4.624 4.8424 18.191 6.0552 9 17 0 1014 361.511 603 336.015 654 335.944 25.496 25.5666 4.93 6.3193 18.496 5.4765 9 18 0 1012 360.573 565 337.329 676 336.178 23.244 24.3942 4.84 6.0624 17.316 6.0829 9 19 0 1012 356.956 645 336.055 423 335.867 19.901 20.0883 5.067 5.1415 16.28 5.526 9 21 0 1015 361.789 601 337.741 439 336.938 24.24 24.4497 </td <td>9 5 0 1018 358.884 571 329.936 571 329.936 28.949 28.9487 4.897 3.6746 16.813 6.5347 9 6 0 1019 358.146 643 323.403 700 321.806 34.743 36.3401 4.624 4.8424 18.191 6.0552 9 17 0 1014 361.511 603 336.015 654 335.944 25.496 25.5666 4.93 6.3193 18.496 5.4765 9 18 0 1012 360.573 565 337.329 676 335.867 19.901 20.0883 5.067 5.1415 16.042 5.526 9 19 0 1015 361.912 640 337.672 710 337.462 24.24 24.4497 5.067 5.9525 16.28 5.526 9 22 0 1013 361.789 601 337.741 439 338.474 24.8502 5.191</td> | 9 5 0 1018 358.884 571 329.936 571 329.936 28.949 28.9487 4.897 3.6746 16.813 6.5347 9 6 0 1019 358.146 643 323.403 700 321.806 34.743 36.3401 4.624 4.8424 18.191 6.0552 9 17 0 1014 361.511 603 336.015 654 335.944 25.496 25.5666 4.93 6.3193 18.496 5.4765 9 18 0 1012 360.573 565 337.329 676 335.867 19.901 20.0883 5.067 5.1415 16.042 5.526 9 19 0 1015 361.912 640 337.672 710 337.462 24.24 24.4497 5.067 5.9525 16.28 5.526 9 22 0 1013 361.789 601 337.741 439 338.474 24.8502 5.191 |

Appendix F: Pearson Correlation Coefficient (r) Table

STUDENT EDITION OF STATISTIX

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CORRELATIONS (PEARSON)

| | OCCUR | HM | MDPI | DELTAACT | ru gamma | MINPACTU | JA MINPRES |
|------------|----------|---------|---------|----------|-------------|----------|------------|
| HM | -0.0583 | | | | | | |
| MDPI | 0.2385 | 0.0415 | | | | | |
| DELTAACTU | 0.2636 | 0.1336 | 0.8505 | | | | |
| GAMMA | 0.2010 | -0.5052 | 0.3540 | 0.3001 | | | |
| MINPACTUA | -0.3196 | -0.0833 | -0.0701 | -0.0996 | 0.0824 | | |
| MINPRES | -0.3418 | -0.0942 | -0.2237 | -0.2134 | -0.0234 | 0.6399 | |
| QL | 0.0548 | 0.4661 | 0.4072 | 0.3803 | -0.2189 | -0.1603 | -0.2120 |
| QM | 0.1321 | -0.0511 | -0.2159 | -0.1572 | -0.0662 | -0.3535 | -0.3106 |
| WI | 0.0899 | -0.0698 | 0.5863 | 0.5264 | 0.7753 | 0.2067 | 0.0418 |
| MAXTHETAE | 0.1846 | 0.5080 | 0.6224 | 0.6272 | 0.0075 | -0.1971 | -0.2233 |
| MINTHACTU | -0.1263 | 0.3781 | -0.3786 | -0.5568 | -0.3598 | -0.0882 | 0.0234 |
| MINTHETAE | -0.0944 | 0.4888 | -0.5563 | -0.3693 | -0.4229 | -0.1239 | 0.0352 |
| | QL | QM | WI | MAXTHETA | AE MINTHACT | ľU | |
| QM | 0.2745 | | | | | | |
| WI | 0.0330 | -0.5209 | | | | | |
| MAXTHETAE | 0.8017 | 0.2058 | 0.2488 | | | | |
| MINTHACTU | 0.3889 | 0.4122 | -0.3799 | 0.2977 | | | |
| MINTHETAE | 0.3555 | 0.4813 | -0.4495 | 0.3041 | 0.7770 | | |
| CASES INCL | UDED 100 | MISSING | CASES 0 | | • | | |

Appendix G: Discriminant Analysis Input Table for Training Data

| Number | Occur | DeltaActua | MinPActua | Gamma |
|--------|-------|------------|-----------|---------|
| 1 | 1 | 30.5078 | 535 | 6.13497 |
| 2 | 1 | 30.6852 | 614 | 6.79737 |
| 4 | 1 | 35.6141 | 627 | 6.74633 |
| 6 | 1 | 25.5138 | 477 | 5.44959 |
| 8 | 1 | 24.4132 | 545 | 5.58444 |
| 10 | 1 | 34.9978 | 628 | 6.84346 |
| 11 | 1 | 42.0995 | 561 | 6.54879 |
| 12 | 1 | 28.8326 | 463 | 5.95483 |
| 13 | 1 | 32.9438 | 705 | 6.56406 |
| 14 | 1 | 27.5195 | 603 | 5.78737 |
| 15 | 1 | 34.4821 | 700 | 6.26058 |
| 18 | . 1 | 27.2448 | 703 | 5.67293 |
| 19 | 1 | 37.194 | 678 | 6.27436 |
| 20 | 1 | 31.7443 | 541 | 6.61184 |
| 22 | 1 | 29.1636 | 666 | 5.99342 |
| 25 | 1 | 27.7669 | 700 | 6.63658 |
| 27 | 1 | 33.1595 | 602 | 6.05701 |
| 31 | 1 | 41.9129 | 688 | 6.56737 |
| 32 | 1 | 44.5963 | 705 | 6.91173 |
| 33 | 1 | 36.4901 | 521 | 6.24724 |
| 34 | 1 | 37.0474 | 555 | 5.99642 |
| 35 | 1 | 29.5479 | 593 | 6.55659 |
| 36 | 1 | 42.9333 | 400 | 6.15171 |
| 37 | 1 | 37.7194 | 500 | 6.56514 |
| 38 | 1 | 12.8243 | 631.9 | 5.17449 |
| 39 | 1 | 45.0815 | 400 | 6.23343 |
| 40 | 1 | 36.6702 | 622.9 | 6.25134 |
| 41 | 1 | 32.7751 | 629.8 | 7.01451 |
| 42 | 1 | 47.9576 | 500 | 6.35015 |
| 43 | 1 | 41.9799 | 500 | 6.94317 |
| 44 | 1 | 28.1281 | 579.8 | 6.72157 |
| 48 | 1 | 42.1182 | 400 | 5.71873 |
| 49 | 1 | 44.5634 | 500 | 6.94082 |
| 50 | 1 | 46.949 | 652.3 | 6.40889 |
| 51 | 1 | 37.2857 | 500 | 6.59613 |
| 52 | 1 | 47.4426 | 500 | 6.57978 |
| 53 | 1 | 43.9083 | 400 | 6.07468 |
| 54 | 1 | 25.4576 | 596 | 6.49458 |
| 56 | 1 | 27.692 | 685 | 6.76277 |
| 57 | 1 | 34.4464 | 587.8 | 6.05782 |
| 58 | 1 | 58.4116 | 500 | 6.10432 |
| 59 | 1 | 50.0744 | 500 | 6.20872 |
| 60 | 1 | 35.8315 | 621 | 6.32357 |

| Number | Occur | DeltaActua | MinPActua | Gamma |
|--------|-------|------------|------------|--------------------|
| 61 | 1 | 46.087 | 500 | 6.33377 |
| 62 | 1 | 43.6378 | 711 | 6.53218 |
| 63 | 1 | 41.1958 | 625 | 6.68118 |
| 69 | 1 | 40.3238 | 566 | 6.91585 |
| 70 | 1 | 29.4083 | 583 | 7.666 |
| 71 | 1 | 32.2684 | 484 | 6.15315 |
| 72 | 1 | 38.2603 | 483 | 6.89302 |
| 1 | 0 | 39.1073 | 739 | 6.09223 |
| 9 | 0 | 27.9205 | 574 | 6.55219 |
| 11 | 0 | 36.8882 | 500 | 6.30631 |
| 15 | 0 | 32.5415 | 615 | 5.98687 |
| 19 | 0 | 26.2678 | 545 | 6.1672 |
| 23 | 0 | 43.6061 | 500 | 6.43821 |
| 24 | 0 | 31.4046 | 804 | 5.66572 |
| 25 | 0 | 33.76 | 537 | 5.93245 |
| 27 | 0 | 39.4521 | 500 | 5.68543 |
| 28 | 0 | 38.441 | 741 | 6.85841 |
| 29 | 0 | 35.7476 | 690 | 6.3762 |
| 32 | 0 | 23.5493 | 601 | 6.21611 |
| 43 | 0 | 16.6397 | 454 | 5.89278 |
| 47 | 0 | 26.1268 | 565 | 7.0373 |
| 50 | 0 | 29.2005 | 658 | 6.01418 |
| 58 | 0 | 38.8821 | 740 | 6.50185 |
| 62 | 0 | 28.3476 | 617 | 6.90954 |
| 70 | 0 | 26.3604 | 700 | 5.96013 |
| 72 | 0 | 43.2587 | 727 | 6.12171 |
| 75 | 0 | 39.8554 | 683 | 6.60046 |
| 76 | 0 | 18.1376 | 665 | 6.40298 |
| 77 | 0 | 38.5907 | 601 | 5.87224 |
| 80 | 0 | 27.3818 | 607 | 6.0095 |
| 82 | 0 | 28.4528 | 581 | 5.54828 |
| 85 | 0 | 26.0056 | 786 | 6.06353 |
| 87 | 0 | 32.5981 | 555 | 6.46421 |
| 88 | 0 | 30.0806 | 657 | 6.62836 |
| 90 | 0 | 27.2876 | 468 | 6.82864 |
| 95 | 0 | 40.0195 | 614 | 6.88285 |
| 97 | 0 | 42.8651 | 714 | 6.45184 |
| 98 | 0 | 25.1748 | 770 | 6.14228 |
| 100 | 0 | 36.2374 | 715 | 5.88978 |
| 101 | 0 | 39.0573 | 785 | 6.08584 |
| 107 | 0 | 26.7939 | 564 | 5.91333 |
| 113 | 0 | 37.8591 | 746 | 6.39273 6.82418 |
| 115 | 0 | 39.3266 | 679 618 | 6.14947 |
| 116 | 0 | 32.3553 | | 5.93137 |
| 118 | 0 | 41.9255 | 558 | <u></u> |
| 121 | 0 | 29.2216 | 705 | 6.29795 |

| | | ., | | |
|--------|-------|------------|-----------|---------|
| Number | Occur | DeltaActua | MinPActua | Gamma |
| 124 | 0 | 19.8682 | 451 | 5.92591 |
| 125 | 0 | 32.3209 | 650 | 6.13981 |
| 131 | 0 | 32.6526 | 725 | 6.43193 |
| 138 | 0 | 37.9366 | 669 | 6.14901 |
| 142 | 0 | 31.1764 | 649 | 6.4796 |
| 144 | 0 | 25.5666 | 654 | 5.47652 |
| 145 | 0 | 24.5946 | 567 | 5.48232 |
| 152 | 0 | 20.0883 | 423 | 5.52596 |
| 159 | 0 | 31.231 | 642 | 5.96217 |
| 161 | 0 | 40.0896 | 637 | 6.69228 |
| 163 | 0 | 36.3401 | 700 | 6.0552 |

Appendix H: Discriminant Analysis Input Table for Verification

| Number | Occur | DeltaActu | MinPActu | Gamma |
|--------|-------|-----------|----------|---------|
| 3 | 1 | 36.8599 | 723 | 6.33855 |
| 5 | 1 | 34.2638 | 571 | 6.38257 |
| 7 | 1 | 29.8398 | 697 | 7.10294 |
| 9 | 1 | 31.9383 | 700 | 6.57558 |
| 16 | 1 | 40.1619 | 615 | 6.67788 |
| 17 | 1 | 40.3701 | 585 | 6.20586 |
| 21 | 1 | 24.6991 | 519 | 7.13066 |
| 23 | 1 | 34.9947 | 621 | 7.02293 |
| 24 | 1 | 41.0621 | 696 | 6.77486 |
| 26 | 1 | 23.2509 | 640 | 5.58692 |
| 28 | 1 | 36.7213 | 559 | 6.64398 |
| 29 | 1 | 50.5713 | 746 | 7.06269 |
| 30 | 1 | 40.1196 | 572 | 7.15143 |
| 45 | 1 | 25.84 | 619.5 | 6.32353 |
| 46 | 1 | 30.8637 | 500 | 5.93617 |
| 47 | 1 | 31.6261 | 702 | 6.56379 |
| 55 | 1 | 47.1086 | 400 | 6.42412 |
| 64 | 1 | 41.8852 | 400 | 6.97294 |
| 65 | · 1 | 30.2016 | 607 | 6.75672 |
| 66 | 1 | 53.5401 | 500 | 6.46495 |
| 67 | 1 | 26.8637 | 629 | 6.72424 |
| 68 | 1 | 24.616 | 785 | 7.28548 |
| 73 | 1 | 39.2917 | 400 | 6.13829 |
| 26 | 0 | 48.1011 | 630 | 5.91607 |
| . 34 | 0 | 41.2154 | 693 | 5.90926 |
| 39 | 0 | 29.3167 | 491 | 5.81623 |
| 44 | 0 | 32.8301 | 653 | 6.29317 |
| 46 | 0 | 38.4923 | 576 | 6.98701 |
| 49 | 0 | 25.2333 | 509 | 6.05282 |
| 53 | 0 | 28.3034 | 560 | 6.71272 |
| 54 | 0 | 37.6819 | 690 | 6.76606 |
| 55 | 0 | 33.1985 | 649 | 6.26208 |
| 57 | 0 | 38.1181 | 598 | 6.08861 |
| 69 | 0 | 30.7538 | 582 | 6.68811 |
| 71 | 0 | 30.0738 | 590 | 6.30429 |
| 74 | 0 | 38.8438 | 733 | 7.0528 |
| 78 | 0 | 42.43 | 743 | 6.56977 |
| 79 | 0 | 18.0734 | 691 | 6.18891 |
| 86 | 0 | 32.6949 | 632 | 6.57792 |
| 102 | 0 | 37.7988 | 747 | 6.39768 |
| 106 | 0 | 34.0359 | 830 | 5.90724 |
| 112 | 0 | 37.571 | 675 | 6.50294 |
| 117 | 0 | 36.1621 | 488 | 5.8579 |

| Number | Occur | DeltaActu | MinPActu | Gamma |
|--------|-------|-----------|----------|---------|
| 119 | 0 | 28.3468 | 594 | 6.10491 |
| 122 | 0 | 39.9044 | 625 | 6.54437 |
| 126 | 0 | 43.1975 | 642 | 6.3554 |
| 127 | 0 | 31.1309 | 642 | 6.59615 |
| 128 | 0 | 16.1347 | 565 | 5.07206 |
| 130 | 0 | 35.2354 | 689 | 6.57738 |
| 136 | 0 | 36.7366 | 729 | 6.53293 |
| 137 | 0 | 24.8645 | 465 | 5.97998 |
| 139 | 0 | 37.4726 | 554 | 6.7486 |
| 140 | 0 | 24.9022 | 668 | 6.19904 |
| 141 | 0 | 46.2595 | 594 | 6.83183 |
| 143 | 0 | 18.5088 | 716 | 5.78753 |
| 146 | 0 | 18.898 | 639 | 5.87884 |
| 154 | 0 | 41.5662 | 591 | 7.11438 |
| 160 | 0 | 38.3011 | 614 | 5.4564 |
| 162 | 0 | 28.9487 | 571 | 6.53472 |
| 164 | 0 | 30.4287 | 656 | 5.86334 |
| 165 | 0 | 27.4828 | 700 | 6.25637 |
| 166 | 0 | 24.8502 | 439 | 5.63372 |

Appendix I: Discriminant Analysis Mathcad Template

ORIGIN ≡1

This is a template that uses output from S-Plus 2000 to determine the cut-off between microburst occurrence and non-microburst occurrence.

$$xbar_1 := \begin{bmatrix} 36.29817 \\ 571.37 \\ 6.380975 \end{bmatrix} \qquad xbar_2 := \begin{bmatrix} 32.17186 \\ 632.90 \\ 6.2083707 \end{bmatrix}$$

These are the group means.

S_{pooled} :=
$$\begin{bmatrix} 58.16686 & -11.764 & .847691 \\ -11.764 & 8488.621 & 6.187427 \\ .847691 & 6.187427 & .180611 \end{bmatrix}$$

Pooled Sample Variance Covariance Matrix

 $b_{hat} := S_{pooled}^{-1} \cdot (xbar_1 - xbar_2)$ This computes the discriminant vector (weights).

$$b_{hat} = \begin{bmatrix} 0.055 \\ -7.876 \cdot 10^{-3} \\ 0.966 \end{bmatrix}$$
 s the discriminant vector (sample approximations of discriminant weights)

Cutoff :=
$$b \frac{T}{hat} \cdot \frac{\left(xbar_1 + xbar_2\right)}{2}$$
 This computes the cuttoff Cutoff = (3.231)

x :=

A:\verify62.txt

DeltaActual :=
$$x^{9}$$
 MinPActual := x^{6} $\Gamma := x^{13}$

| | | 1 |
|---|---|-------|
| | 1 | 2.466 |
| | 2 | 3.563 |
| | 3 | 3.022 |
| | 4 | 2.604 |
| | 5 | 3.827 |
| | 6 | 3.619 |
| | 7 | 4.166 |
| = | 8 | 3.828 |
| | 9 | 3.333 |

1.642 4.045 3.743 4.621 2.658 3.503 2.56

Y

Cutoff = (3.231)

The first 23 are microburst days the second 39 are non-microburst days

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<u>Vita</u>

Captain Steven N. Dickerson was born in Pt. Pleasant, New Jersey on 11 August 1971. He graduated from Brick Township High School in 1989 and enrolled at Rutgers University in New Brunswick, New Jersey. He graduated with a Bachelor of Science degree in Meteorology in May 1993, receiving a commission through the Air Force Reserve Officers Training Corps (ROTC).

In September 1993, Captain Dickerson was assigned to the 12th Air Support

Operations Squadron, Fort Bliss, Texas where he served as the Regimental Staff Weather

Officer to the 3rd Armored Cavalry Regiment. In November 1994, he was assigned to the

18th Weather Squadron, Fort Bragg, North Carolina where he served as the Special

Operations Forces Weather Flight Commander providing weather support to the U.S.

Army's 3rd and 7th Special Forces Groups (Airborne). Captain Dickerson was later

assigned to Detachment 5, 10th Combat Weather Squadron also on Fort Bragg. He

entered the School of Engineering and Management, Air Force Institute of Technology in

August 1998. His follow-on assignment is to the United States Air Forces Europe

(USAFE) Operational Weather Squadron, Sembach, Germany.

Captain Dickerson is married to the former Diane Guedes of Manahawkin, New Jersey. They have two children, Kevin and Amanda.

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| 13. ABSTRACT (Maximum 200 words) | | | |
| A microburst event on 16 Augus | t 1994 at the Kennedy Space | Center's (KSC) Shuttle Landin | g Facility alerted forecasters |
| from the 45th Weather Squadron (45 | 5WS), the provider of weath | er support to the KSC and Cape | Canaveral Air Station |
| (CCAS), to the challenges of microburst prediction. Although there was no operational impact, this event caused the 45WS t | | | |
| revise their thunderstorm forecasting procedures to specifically address microbursts, resulting in the locally developed | | | |
| Microburst-Day Potential Index (MDPI). MDPI provides a several-hour outlook of microburst potential based on the results | | | |
| of the Microburst and Severe Thunderstorm (MIST) project. The 45WS also conducted a preliminary evaluation of the Wind | | | |
| INDEX (WINDEX) for the KSC/CCAS microburst forecast problem. WINDEX estimates the maximum observed gust speed | | | |
| that can be expected should a micro | | | |
| This thesis presents an evaluation of MDPI and WINDEX. A new microburst potential index is also introduced, | | | |
| incorporating both the MDPI and WINDEX parameters. Overall neither the MDPI nor the WINDEX performed particularly | | | |
| well. MDPI showed very little improvement over random guessing, and WINDEX showed very little correlation to observed | | | |
| microburst gust speeds. The new microburst potential index generally outperformed MDPI. Further refinement of the new | | | |
| index is needed to make it more use | ful operationally. | | |
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