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# PDF MODELLING OF TURBULENT COMBUSTION

### AROSR Grant F-49620-00-1-0171 Principal Investigator: Stephen B. Pope

Mechanical & Aerospace Engineering Cornell University Ithaca, NY 14853

#### SUMMARY

Significant progress was made in the application of PDF-based turbulent combustion models to the Sandia pilot-jet nonpremixed flames. These PDF calculations were described in two recent papers (Xu & Pope 2000 and Tang, Xu & Pope 2000) and they are summarized in this report. The first of these works showed that the PDF method is capable of describing, quantitatively, the phenomena of local extinction and reignition (as functions of jet velocity and axial distance) that are observed in these flames. The second paper extended the methodology to include radiative heat loss, and the calculation of  $NO_x$ .

#### PDF MODEL

The model is based on the transport equation for the joint probability density function of velocity, turbulence frequency and thermochemical composition. For the combustion of methane considered, the chemical kinetics are represented by the augmented reduced mechanism of Sung, Law & Chen (1998). Without  $NO_x$  chemistry (ARM1) there are 16 species; with  $NO_x$  there are 19. For computational tractability, the effects of reaction are implemented by the in situ adaptive tabulation (ISAT) algorithm (Pope 1997).

#### LOCAL EXTINCTION

The piloted jet nonpremixed flames measured by Barlow & Frank (1998) consist of a central jet of methane, a substantial annular pilot, and coflowing air. In the three flames considered, D, E and F, the jet velocities are  $U_J = 50$ , 74 and 99 m/s, respectively. The amount of local extinction increases with the jet velocity.

Figure 1 shows scatter plots of the  $CO_2$  mass fraction against mixture fraction for Flame F at 30 jet radii downstream. In the measurements (left-hand figure), each point represents a laser shot: in the calculations (right-hand figure), each point represents a particle from the particle/mesh method used to solve the PDF equation. The upper curve is the composition of a mildly strained laminar flame. The fact that the bulk of the points lie beneath this line is an indication of local extinction. The lower curve is the conditional mean from the data. Good agreement between the calculations and the measurements may be observed.

Xu & Pope (2000) define a "burning index" (BI) as a measure of (the lack of) local extinction. To explain the definition of the burning index we again refer to Fig. 1.

The vertical dashed line shows a mixture fraction range around strichiometric (defined by Barlow & Frank 1998). The lower solid circle is the mean of the data points that lie in this range; whereas the upper solid circle is the value from the laminar flame. The burning index is defined as the ratio of these two values. Consequently, a burning index of 1 corresponds (roughly) to complete combustion, and 0 corresponds to complete extinction.



Figure 1: Scatter plots of  $CO_2$  mass fraction against mixture fraction for flame F at an axial distance of 15 jet diameters. Left-hand plot, experimental data of Barlow & Frank (1998); right-hand plot, PDF calculations of Xu & Pope (2000).

Figure 2 compares the measured and calculated burning indexes of different species (and temperature) for all three flames as functions of axial distance. As may be seen, with few exceptions, the PDF calculations accurately describe the dependence of BI on both the jet velocity and on the axial distance. These results demonstrate a significant advance in our abilities to calculate substantial finite-rate chemistry-turbulence interactions.

#### MAJOR AND MINOR SPECIES

For flame D, Fig. 3 shows calculated radial profiles of the mean and r.m.s. of the NO mass fraction compared to the experimental data. Good agreement may be observed for both quantities, and the downstream evolution is well represented. It may be seen that radiative heat loss does not have a significant impact on NO (in this flame).

Figure 4 shows the conditional mean (conditioned on mixture fraction  $\xi$ ) of various quantities. These conditional means provide a good indication of the accuracy of the chemistry calculations. As may be seen, the agreement between the calculations and the experiments is uniformly satisfactory. The trends of *NO* with jet velocity and downstream distance are accurately represented; and the accuracy of the *CO* calculations shows that ARM remedies previously observed discrepancies.



Figure 2: Burning indexes for flames D, E and F. Filled symbol: experiments; lines with empty symbols, PDF calculations. Circle and solid line, flame F; down-triangle and dashed line, flame E; up-triangle and dashed-dotted line, flame D. (From Xu & Pope 2000.)



Figure 3: Radial profiles of the mean (upper plots) and r.m.s. (lower plots) of NO mass fraction in flame D. Symbols, experimental data (Barlow & Frank 1998); solid and dashed lines, PDF calculations without and with radiative heat loss. (From Tang, Xu & Pope 2000.)

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- 1. Barlow R.S. and Frank J.H. "Effects of turbulence on species mass fraction in methane/air jet flames," In *Twenty-seventh Symp. (Int'l) on Combust.*, page 1087, Pittsburgh, 1998. The Combustion Institute.
- Pope S.B. (1997) "Computationally Efficient Implementation of Combustion Chemistry using In Situ Adaptive Tabulation," Combustion Theory and Modelling, 1, 41-63.
- 3. Sung, C. J., Law C. K., and Chen J.-Y. (1998). "An augmented reduced mechanism for methane oxidation with comprehensive global parametric validation." In *Twentyseventh Symp. (Int'l) on Combust.*, Pittsburgh, pp. 295–304. The Combustion Institute.
- 4. Tang Q., Xu J. and Pope S.B. (2000) "PDF calculations of local extinction and *NO* production in piloted-jet turbulent methane/air flames", Twenty-Eighth Symp. (Int'l) on Combust. (to be published).
- 5. Xu J. and Pope S.B. (2000) "PDF calculations of turbulent nonpremixed flames with local extinction," Combust. Flame (to be published).

#### PERSONNEL SUPPORTED

Prof. S.B. Pope, PI S. Joseph, graduate student Q. Tang, graduate student

#### DEGREES GRANTED

S. Joseph, M.S.

#### PUBLICATIONS

The following papers were written during the reporting period.

- 1. Q. Tang, J. Xu and S.B. Pope (2000) "PDF calculations of local extinction and NO production in piloted-jet turbulent methane/air flames," Twenty-Eighth Symp. (Int'l) on Combust. (to be published).
- 2. J. Xu and S.B. Pope (2000) "PDF calculations of turbulent nonpremixed flames with local extinction," Combust. Flame (to be published).

#### PRESENTATIONS

June 5, 2000—University of California, Santa Barbara, Institute of Theoretical Physics.

June 13, 2000—AFOSR/ARO Contractors' Meeting, Workshop presentation, Santa Fe, NM.

July 27, 2000—Fifth International Workshop on Nonpremixed Turbulent Combustion, Delft, Netherlands.

July 31, 2000—International Combustion Symposium, presentation.

## OTHER INTERACTIONS

During the reporting period the PI has visited:

Rolls Royce Corporation, Indianapolis, IN Rocketdyne, Canoga Park, CA Los Alamos National Lab, NM



Figure 4: Conditional means in flames D and F. Lines and symbols as in Fig. 3.

# Principal Investigator Annual Data Collection (PIADC) Survey Form

NOTE: If there is insufficient space on this survey to meet your data submissions, please submit additional data in the same format as identified below.

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