

A Space-Sweep Approach to True Multi-Image Matching *

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Abstract

The problem of determining feature correspondences across multiple views is considered. The term "true multi-image" matching is introduced to describe techniques that make full and efficient use of the geometric relationships between multiple images and the scene. A true multi-image technique must generalize to any number of images, be of linear algorithmic complexity in the number of images, and use all the images in an equal manner. A new space-sweep approach to true multi-image matching is presented that simultaneously determines 2D feature correspondences and the 3D positions of feature points in the scene. The method is illustrated on a seven-image matching example from the aerial image domain.

1 Introduction

This paper considers the problem of **multi-image stereo reconstruction**, namely the recovery of static 3D scene structure from multiple, overlapping images taken by perspective cameras with known extrinsic (pose) and intrinsic (lens) parameters. The dominant paradigm is to first determine corresponding 2D image features across the views, followed by triangulation to obtain a precise estimate of 3D feature location and shape. The first step, solving for matching features across multiple views, is by far the most difficult. Unlike motion sequences, which exhibit a rich set of constraints that lead to efficient matching techniques based on tracking, determining feature correspondences from a set of widely-spaced views is a challenging prob-

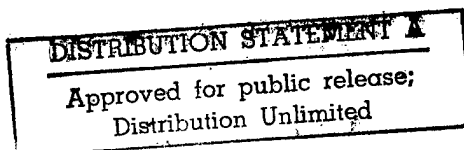
lem. However, even disparate views contain underlying geometric relationships that constrain which 2D image features might be the projections of the same 3D feature in the world. The purpose of this paper is to explore what it means to make full and efficient use of the geometric relationships between multiple images and the scene.

In Section 2, a set of conditions is presented that must hold for a matching algorithm to be called a "true multi-image" method. Briefly, we claim that a true multi-image matching technique should be applicable to any number of images $n \geq 2$, that the algorithmic complexity should be $O(n)$ in the number of images, and that the images should all be treated in an equal manner. Examples from the literature are presented to illustrate the meaning and motivation for each condition.

Section 3 presents a new approach to true multi-image matching that simultaneously determines 2D image feature correspondences together with the positions of observed 3D features in the scene. The method can be visualized as sweeping a plane through space, while noting positions on it where many backprojected feature rays intersect. Careful examination of the projective relationships between the images and the plane in space, and between different positions of the sweeping plane, shows that the feature mappings involved can be performed very efficiently. A statistical model is developed to help decide how likely it is that the results of the matching procedure are correct.

Section 4 shows an illustrative example of the space-sweep method applied to imagery from the RADIUS aerial image understanding project. The paper concludes with a brief summary and discussion of extensions. A more detailed version of this paper can be found in [2].

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2 True Multi-Image Matching

2.1 Definition

This section presents, for the first time, a set of conditions that a stereo matching technique should meet to be called a "true multi-image" method. By this we mean that the technique truly operates in a multi-image manner, and is not just a repeated application of two- or three-camera techniques.

Definition: A true multi-image matching technique satisfies the following conditions:

1. the method generalizes to any number of images greater than 2,
2. the algorithmic complexity is $O(n)$ in the number of images, and
3. all images are treated equally (i.e. no image is given preferential treatment).

Condition 1 is almost a tautology, stating that a multi-image method should work for any number of images, not just two or three. An algorithm for processing three images is not a "multi-image" method, but rather a trinocular one. Condition 2 speaks directly to the issue of efficiency. To enable processing large numbers of images, the method used should be linear in the number of images. This condition precludes approaches that process all pairs of images, then fuse the results. Such an approach is not a multi-image method, but rather a repeated application of a binocular technique.

Condition 3 is the most important – it states that the information content from each image must be treated equally. Note that this is **not** intended to mean that information from all images must be equally weighted; some may be from better viewing positions, of higher resolution, or more in focus. Instead, condition 3 is meant to preclude singling out one image, or a subset of images, to receive a different algorithmic treatment than all the others. A common example is the selection of one image as a "reference" image. Features in that image are extracted, and then the other images in the dataset are searched for correspondence matches, typically using epipolar constraints between the reference image and each other image in turn. Although a popular approach, there is an inherent flaw in this style of processing – if an important feature is missing in the reference image due to misdetection or occlusion, it will not be present in the 3D reconstruction even if it has been detected in all the other views, because the system won't know to look for it.

2.2 Examples

Although the conditions presented above are well-motivated and reasonable, it is hard to locate stereo matching algorithms in the literature that meet all three. This section presents a range of negative and positive examples, and examines the latter to extract characteristics they have in common.

Okutomi and Kanade describe a **multi-baseline stereo** method for producing a dense depth map from multiple images by performing two-image stereo matching on all pairs of images and combining the results [10]. Although they show convincingly that integrating information from multiple images is effective in reducing matching ambiguity, using all pairs of images makes this an $O(n^2)$ algorithm and violates condition 2 of the true multi-image definition. The basic multi-baseline system design was later transferred to hardware, and the control strategy changed to combining two-image stereo results between a "base" view and all other views [8]. This yields an $O(n)$ method rather than $O(n^2)$ (and the added efficiency is no doubt important for making a system that runs in real-time), however the implementation now violates condition 3, since one image is given special importance as a reference view. Any areas of the scene that are occluded in that image can not be reconstructed using this method.

Gruen and Baltsavias describe a **constrained multiphoto matching** system for determining correspondences across multiple views [5]. An intensity template extracted from a reference image is searched for in a set of remaining views. Affine template warping is introduced to compensate for differences in camera viewing angle, and the position of intensity templates in each image are constrained to move by fixed "step ratios" along their epipolar lines to guarantee that all template positions correspond to a single point in space. Once again, however, condition 3 has been violated by choosing templates from a special reference image.

Kumar et.al. describe a multi-image extension to the basic **plane+parallax matching** approach [9]. They compensate for the appearance of a known 3D surface between a reference view and each other view, then search for corresponding points along lines of residual parallax. Yet again, a special reference view has been chosen, and the approach is basically that of repeatedly applying a two-image method to pairs of images that contain the reference view.

The reason why so many approaches attempt to

solve the multi-image matching problem by splitting the set into pairs of images that are processed binocularly is because matching constraints based on the epipolar geometry of two views are so powerful and well-known. What is needed for simultaneous matching of features across multiple images is to generalize two-image epipolar relations to some **multilinear relation** between the views. For example, Shashua presents a "trilinear" constraint [12] where points in three images can be the projections of a single 3D scene point if and only if an algebraic function vanishes. Hartley devised a similar constraint for lines in three views [7]. A recent paper by Triggs [13] provides a framework in which all projective multilinear relationships can be enumerated: the binocular epipolar relationship, Shashua's trilinear relationship for points, Hartley's trilinear relationship for lines, and a quadrilinear relation for points in four views. The number of views is limited to four since the projective coordinates of 3D space have only four components. This violates condition 1 of the definition of a true multi-image method, and calls into question whether any approach that operates purely in image space can be a true multi-image method.

In contrast to the strictly image-level approaches above, photogrammetric applications favor an **object-space least-squares matching** approach where correspondences between multiple images are determined by backprojecting image features onto some surface in the world and performing correspondence matching in object space. Helava presents a typical example [6], where a grid of ground elements or "groundels" in the scene is estimated along with the precise correspondence of intensity patches appearing in multiple images. Although this least-squares approach potentially involves solving for a huge number of parameters (DTM grid sizes of 500×500 are not uncommon), it does meet all three conditions for a true multi-image method. It generalizes to any number of images, the algorithm is linear in the number of images (although the run-time will typically be dominated by the number of groundels that have to be estimated), and most importantly, information from all of the images is treated on an equal footing.

Fua and Leclerc describe an approach for object-centered reconstruction via **image energy minimization** where 3D surface mesh representations are directly reconstructed from multiple intensity images [3]. Loosely speaking, triangular surface elements are adjusted so that their projected appear-

ance in all the images is as similar as possible to the observed image intensities, while still maintaining a consistent shape in object-space. This work also fits the definition of a multi-image method.

One thing that the true multi-image matching/reconstruction methods above have in common is the explicit reconstruction of a surface or features in object space, simultaneous with the determination of image correspondences. In this way, object-space becomes the medium by which information from multiple images is combined in an even-handed manner. Unfortunately, the two object space approaches mentioned here involve setting up huge optimization problems with a large number of parameters, and initial estimates of scene structure are needed to reliably reach convergence. We present a much more efficient approach in the next section that is suitable for matching point- or edge-like features across multiple images.

3 An Efficient Space-Sweep Approach

This section presents a true multi-image matching algorithm that simultaneously determines the image correspondences and 3D scene locations of point-like features (e.g. corners, edgels) across multiple views. The method is based on the premise that areas of space where several image feature viewing rays (nearly) intersect are likely to be the 3D locations of observed scene features. A naive implementation of this idea would partition a volume of space into voxels, backproject each image point out as a ray through this volume, and record how many rays pass through each voxel. The main drawback of this implementation would be its intensive use of storage space, particularly when partitioning the area of interest very finely to achieve accurate localization of 3D features.

3.1 The Space-Sweep Method

We propose to organize the computation as a space-sweep algorithm. A single plane partitioned into cells is swept through the volume of space along a line perpendicular to the plane. Without loss of generality, assume the plane is swept along the Z-axis of the scene, so that the plane equation at any particular point along the sweep has the form $Z = z_i$ (see Figure 1). At each position of the plane along the sweeping path, the number of viewing rays that intersect each cell are tallied. This is done by backprojecting point features from each image onto the sweeping plane (in a manner described in Section 3.2), and incrementing cells whose centers

fall within some radius of the backprojected point position (as described in Section 3.3).

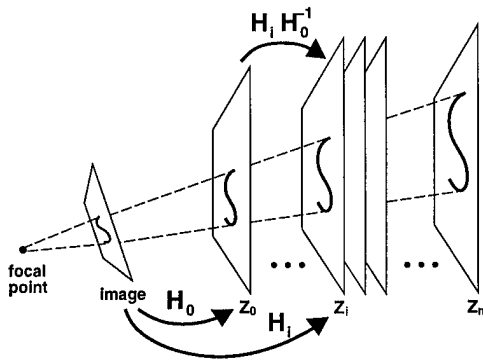


Figure 1: Illustration of the space-sweep method. Features from each image are backprojected onto successive positions $Z = z_i$ of a plane sweeping through space.

After accumulating counts from feature points in all of the images, cells containing counts that are “large enough” (Section 3.3) are hypothesized as the locations of 3D scene features. The plane then continues its sweep to the next Z location, all cell counts are reset to zero, and the procedure repeats. For any feature location (x, y, z_i) output by this procedure, the set of corresponding 2D point features across multiple images is trivially determined as consisting of those features that backproject to cell (x, y) within the plane $Z = z_i$.

Two implementation issues are addressed in the remainder of this section. Section 3.2 presents a fast method for determining where viewing rays intersect the sweeping plane, which is crucial to the efficiency of the proposed algorithm. In Section 3.3 a statistical model is developed to help decide whether a given number of ray intersections is statistically meaningful, or could instead have occurred by chance.

We note in passing a method developed by Seitz and Dyer that, while substantially different from the approach here, is based on the same basic premise of determining positions in space where several viewing rays intersect [11]. However, because feature evidence is combined by geometric intersection of rays, only the correspondences and 3D structure of features detected in EVERY image are found – a severe limitation.

3.2 Efficient Backprojection

Recall that features in each image are backprojected onto each position $Z = z_i$ of the sweeping plane. For a perspective camera model, the transforma-

tion that backprojects features from an image onto the plane $Z = z_i$ is a nonlinear planar homography represented by the 3×3 matrix:

$$H_i = A [r_1 \ r_2 \ z_i r_3 + t],$$

where A is the 3×3 matrix describing the camera lens parameters, and the camera pose is composed of a translation vector t and an orthonormal rotation matrix with column vectors r_i . This section shows that it is more efficient to compute feature locations in the plane $Z = z_i$ by modifying their locations in some other plane $Z = z_0$ to take into account a change in Z value, than it is to apply the homography H_i to the original image plane features.

Let matrix H_0 be the homography that maps image points onto the sweeping plane at some canonical position $Z = z_0$. Since homographies are invertible and closed under composition, it follows that the homography that maps features between the plane $Z = z_0$ and $Z = z_i$ directly, by first (forward) projecting them from the z_0 -plane onto the image, then backprojecting them to the z_i -plane, can be written as $H_i H_0^{-1}$ (refer to Figure 1).

It can be shown that the homography $H_i H_0^{-1}$ has a very simple structure [2]. In fact, if (x_0, y_0) and (x_i, y_i) are corresponding backprojected locations of a feature point onto the two positions of the sweeping plane, then

$$\begin{aligned} x_i &= \delta x_0 + (1 - \delta)C_x \\ y_i &= \delta y_0 + (1 - \delta)C_y \end{aligned} \quad (1)$$

where $\delta = (z_i - C_z)/(z_0 - C_z)$ and $(C_x, C_y, C_z) = (-r_1 \cdot t, -r_2 \cdot t, -r_3 \cdot t)$ is the location of the camera focal point in 3D scene coordinates. A transformation of this form is known as a *dilation*.¹ The trajectories of all points are straight lines passing through the fixed point (C_x, C_y) , which is the perpendicular projection of the camera focal point onto the sweeping plane (see Figure 2). The effect of the dilation is an isotropic scaling about point (C_x, C_y) . All orientations and angles are preserved.

Our strategy for efficient feature mapping onto different positions of the sweeping plane is to first perform a single projective transformation of feature points from each image $I_j, j = 1, \dots, n$ onto some canonical plane $Z = z_0$. These backprojected point positions are not discretized into cells, but instead

¹This is unrelated to the morphological dilation operator.

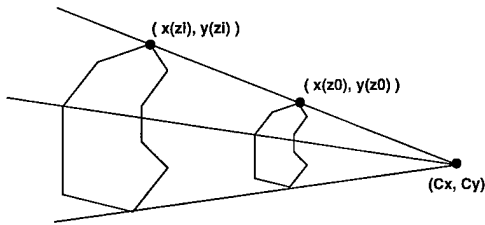


Figure 2: Transformation $H_i H_0^{-1}$ is a dilation that maps points along trajectories defined by straight lines passing through the fixed point (C_x, C_y) .

are represented as full precision (X, Y) point locations. For any sweeping plane position $Z = z_i$, each of these (X, Y) locations is mapped into the array of cells within that plane using formula (1), taking care to use the correct camera center $(C_x, C_y, C_z)_j$ for the features from image I_j .

3.3 A Statistical Model of Clutter

This section sketches an approximate statistical model of clutter that tells how likely it is for a set of viewing rays to coincide by chance (more details are given in [2]). The model will be used to choose a threshold on the number of votes (viewing rays) needed before an accumulator cell will be considered to reliably contain a 3D scene feature. The term “clutter” as used here refers not only to spurious features among the images, but also to sets of correctly extracted features that just don’t correspond to each other.

Determining the expected number of votes each cell in the sweeping plane receives is simplified considerably by assuming that extracted point features are roughly uniformly distributed in each image. This is manifestly untrue, of course, since image features exhibit a regularity that arises from the underlying scene structure. Nonetheless, they will be uniform enough for the purpose of this discussion as long as a $k \times k$ block of pixels in the image contains roughly the same number of features as any other $k \times k$ block. Under this assumption, let the density of point features in image i be $E_i \ll 1$ (computed empirically). The expected number of features that image i projects into the sweeping plane is then this expected number of features per pixel E_i times the number of pixels O_i that have viewing rays passing through some cell in the sweeping plane.

Recall that each point feature in image i is allowed to vote for a set of cells surrounding the intersection of its viewing ray with the sweeping plane. Votes are given to the set of cells roughly contained in the

region subtended by a pixel-shaped cone of viewing rays emanating from the point feature in image i . Pixels from images farther away from the sweeping plane thus contribute votes to more cells than pixels from images that are closer. This mechanism automatically accounts for the fact that scene feature locations are localized more finely by close-up images than by images taken from far away.

The number of cells in the sweeping plane that a pixel in image i votes for is specified by the Jacobian J_i of the projective transformation from image i onto the sweeping plane. We make a second simplifying assumption that this Jacobian is roughly constant, which is equivalent to assuming that the camera projection equations are approximately affine over the volume of interest in the scene. The total expected number of votes that image i contributes to the sweeping plane is thus estimated as the number of features mapped to the plane, times the number of cells that each feature votes for, that is $E_i * O_i * J_i$. Dividing this quantity by the number of accumulator cells in the sweeping plane yields the probability θ_i that any cell in the sweeping plane will get a vote from image i .

For each accumulator cell, the process of receiving a vote from image i is modeled as a Bernoulli random variable with probability of success (receiving a vote) equal to θ_i . The total number of votes V in any sweeping plane cell is simply the sum of the votes it receives from all n images. Thus V is a sum of n Bernoulli random variables with probabilities of success $\theta_1, \dots, \theta_n$. Its probability distribution function $D[V]$ tells, for any possible number of votes $V = 0, 1, \dots, n$, what the probability is that V votes could have arisen by chance. In other words, $D[V]$ specifies how likely is it that V backprojected feature rays could have passed through that cell due purely to clutter or accidental alignments.

Once the clutter distribution function $D[V]$ is known, a solid foundation exists for evaluating decision rules that determine which sweeping plane cells are likely to contain scene features based on the evidence provided by backprojected image feature rays. A simple decision rule compares the number of votes V in each cell against a global threshold T , and declares that cell location to contain a feature when $V \geq T$. For each potential threshold $T \in \{1, \dots, n\}$, the false positive rate $F[T]$ of this decision rule is easily computed as $F[T] = \sum_{i=j}^n D[i]$. A threshold T can then be chosen based on how certain one wants the matching results to be.

4 Experimental Example

This section presents an in-depth example of the space-sweep algorithm for multi-image matching using aerial imagery from the RADIUS project [4]. Seven images of Fort Hood, Texas were cropped to enclose two buildings and the terrain immediately surrounding them. The images exhibit a range of views and resolutions (see Figure 3). The point fea-

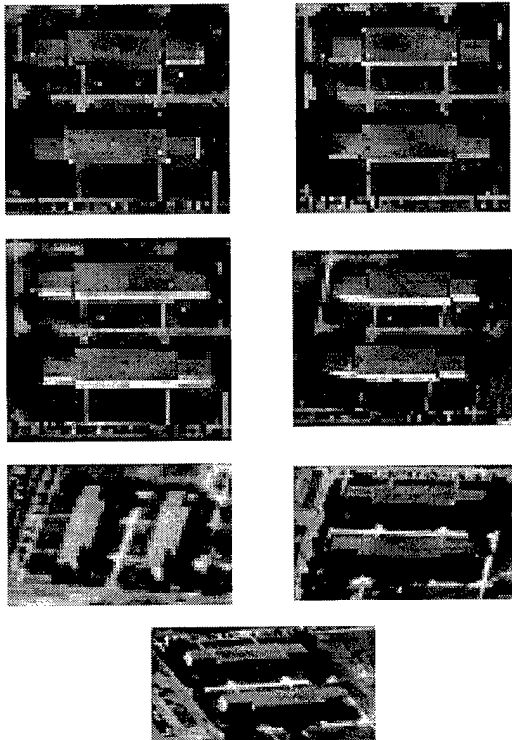


Figure 3: Seven aerial subimages of two buildings.

tures used are edgels detected by the Canny edge operator [1]. Figure 4 shows a binary edge image extracted from one of the views. Structural features of particular interest are the building rooftops and the network of walkways between the buildings. Note the significant amount of clutter due to trees in the scene, and a row of parked cars at the bottom.

Reconstruction was carried out in a volume of space with dimensions $136 \times 130 \times 30$ meters. A horizontal sweeping plane was swept through this volume along the Z-axis. Each accumulator cell on the plane was $1/3$ meter square, a size chosen to roughly match the resolution of the highest resolution image. Viewing ray intersections were sampled at 100 equally-spaced locations along the sweeping path, yielding approximately a $1/3$ -meter resolution in the vertical direction as well. Figure 5 shows three sample plane locations along the sweeping

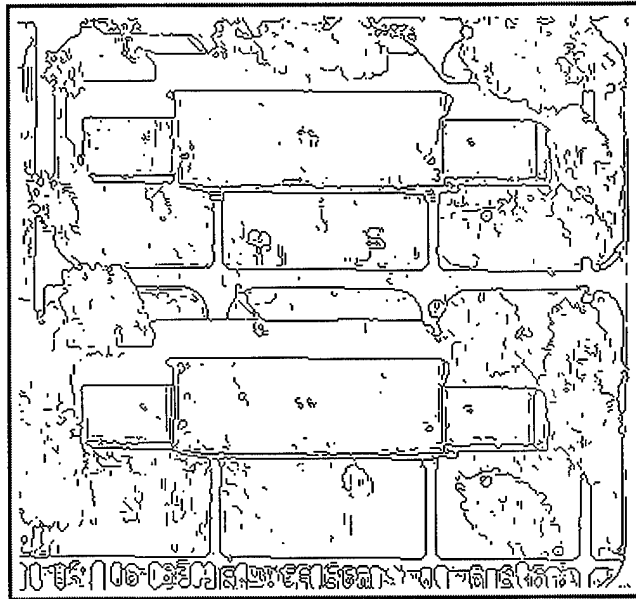


Figure 4: Canny edges extracted from one image.

path, chosen to illustrate the state of the sweeping plane when it is coincident with ground-level features (a), roof-level features (c) and when there is no significant scene structure (b). Also shown are the results of thresholding the sweeping plane at these levels, displaying only those cells with five or more viewing rays passing through them.

The approximate statistical model of clutter presented in Section 3.3 needs to be validated with respect to the data, since it is based on two simplifying assumptions, namely that edgels in the each image are distributed uniformly, and that the Jacobian of the projective transformation from each image to the sweeping plane is roughly constant. This was done by comparing the theoretical clutter probability distribution $D[V]$, $V = 0, 1, \dots, 7$ against the empirical distributions of feature votes collected in each of the 100 sweeping plane positions. Recall that the clutter distribution $D[V]$ tells how many ray intersections are likely to pass through each accumulator cell purely by chance. This theoretical distribution should match the empirical distribution well for sweeping plane positions where there is no significant 3D scene structure. The chi-square statistic was used to measure how similar these two discrete distributions are for each Z-position of the sweeping plane; the results are plotted in Figure 6. Lower values mean good agreement between the two distributions, higher values mean they are not very similar. Two prominent, sharp peaks can be seen, implying that the dominant 3D

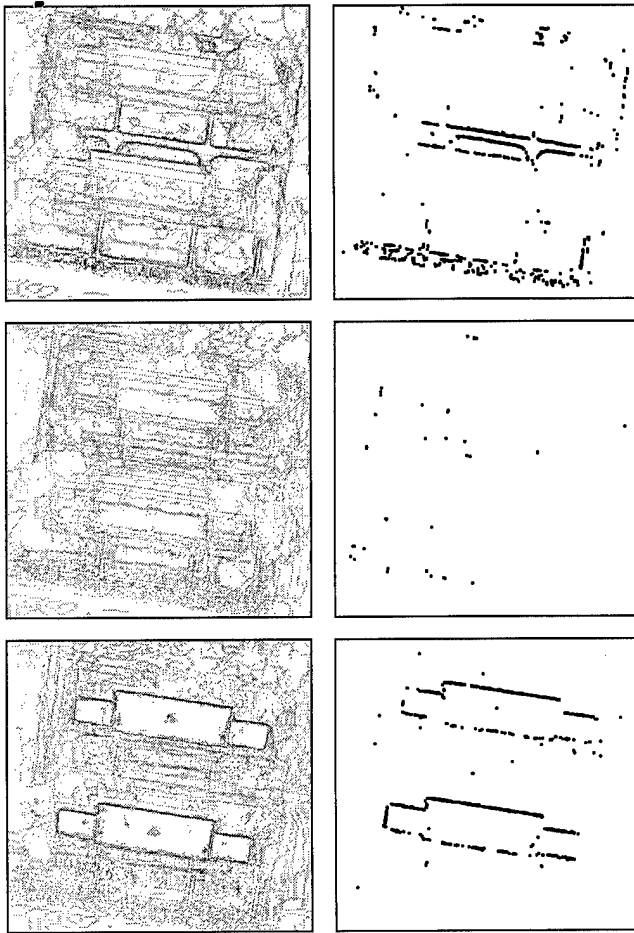


Figure 5: Three sample Z -positions of the sweeping plane coinciding with (top) ground-level features, (middle) no structure, and (bottom) roof features. Left shows votes in the sweeping plane, encoded by 0 = pure white and 7 = pure black. Right is the results of feature classification using a threshold value of 5.

structure of this scene lies in two well-defined horizontal planes, in this case ground-level features and building rooftops. More importantly, the plot is very flat for Z -levels that contain no significant scene structure, showing that the theoretical clutter model is actually a very good approximation to the actual clutter distribution. The ground-level peak in the plot is a bit more spread out than the peak for roof-level features, because the ground actually slopes gently in the scene.

Recall that once the clutter distribution $D[V]$ is computed for any Z -position of the sweeping plane, a vote threshold $T = 1, \dots, n$ for classifying which cells contain 3D scene features can be chosen taking into account the expected false positive rate $F[T]$. The false positive rates computed for this dataset are very consistent across all Z positions of

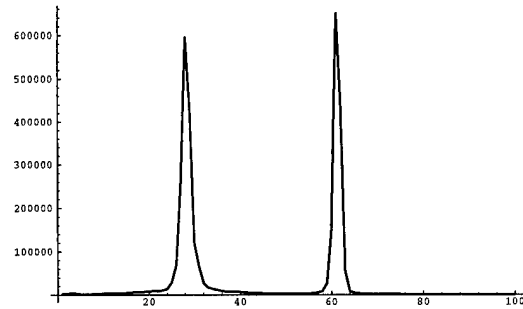


Figure 6: Validation of the statistical clutter model by plotting chi-square test values comparing theoretical and empirical clutter distributions at each sweeping plane position (see text).

the sweeping plane. A representative sample is:

T	1	2	3	4	5	6	7
$100 F[T]$	88.4	59.0	27.3	8.3	1.6	0.17	0.01

This table displays for any given choice of threshold T , what the percentage of false positives would be if cells with votes of T or higher are classified as the locations of 3D scene features.

A desired confidence level of 99% was chosen for recovered 3D scene features, implying that we are willing to tolerate only 1% false positives due to clutter. Based on this choice and the above table, the optimal threshold should be between 5 and 6, but closer to the former. Figure 7 graphically compares extracted 3D ground features and roof features using these two different threshold values. Each image displays the (x,y) locations of cells that are classified as scene features within a range of Z locations determined by the two peaks in Figure 6. It can be seen that feature locations extracted using a threshold of 5 trace out the major rooftop and walkway boundaries quite well, but there are a noticeable number of false positives scattered around the image. A threshold of 6 shows significantly less clutter, but far fewer structural features as well. Choosing an optimal threshold is a balancing act; ultimately, the proper tradeoff between structure and clutter needs to be determined by the application.

5 Summary and Extensions

This paper defines the term "true multi-image" matching to formalize what it means to make full and efficient use of the geometric relationships between multiple images and the scene. Three conditions are placed on a true multi-image method: it should generalize to any number of images, the algorithmic complexity should be linear in the num-

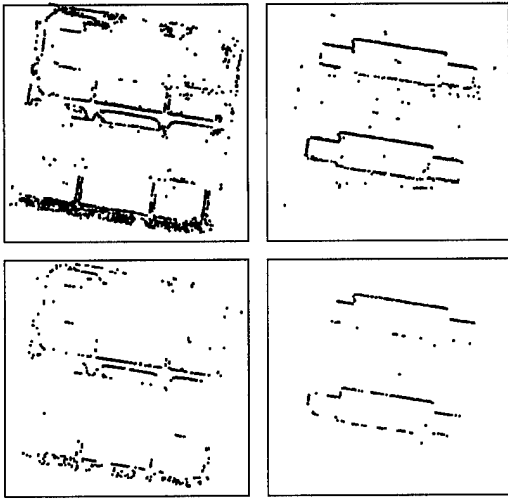


Figure 7: XY locations of detected scene features for a range of Z -values containing ground features (left) and roof features (right). Results from two different threshold values of 5 (top) and 6 (bottom) are compared.

ber of images, and every image should be treated on an equal footing, with no one image singled out for special treatment as a reference view. Several multi-image matching techniques that only operate in image-space were found not to pass this set of conditions. Two techniques that **can** be considered to be true multi-image methods reconstruct scene structure in object space while determining correspondences in image space. Object space seems to be the conduit through which successful multi-image methods combine information,

A new space-sweep approach to true multi-image matching is presented that simultaneously determines 2D feature correspondences between multiple images together with the 3D positions of feature points in the scene. It was shown that the intersections of viewing rays with a plane sweeping through space could be determined very efficiently. A statistical model of feature clutter was developed to tell how likely it is that a given number of viewing rays would pass through some area of the sweeping plane by chance, thus enabling a principled choice of threshold to be chosen for determining whether or not a 3D feature is present. This approach was illustrated using a seven-image matching example from the aerial image domain.

Several extensions to this basic approach are being considered. One is the development of a more sophisticated model of clutter that adapts to the spatial distribution of feature points in each image. The second extension is to consider the gradient

orientations of potentially corresponding edge features; when accumulating feature votes in a sweeping plane cell, only edgels with compatible orientations should be added together. With the introduction of orientation information, detected 3D edgels could begin to be linked together in the scene to form 3D chains, leading to the detection and fitting of symbolic 3D curves.

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